

D3Q27 NSE,

a supplementary material for

Lattice Boltzmann Method Analysis Tool (LBMAT)

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1 Global definitions

In \mathbb{R}^3 , the position and velocity vectors are given by $\mathbf{x} = (x_1, x_2, x_3)^T$ and $\mathbf{v} = (v_1, v_2, v_3)^T$, respectively.

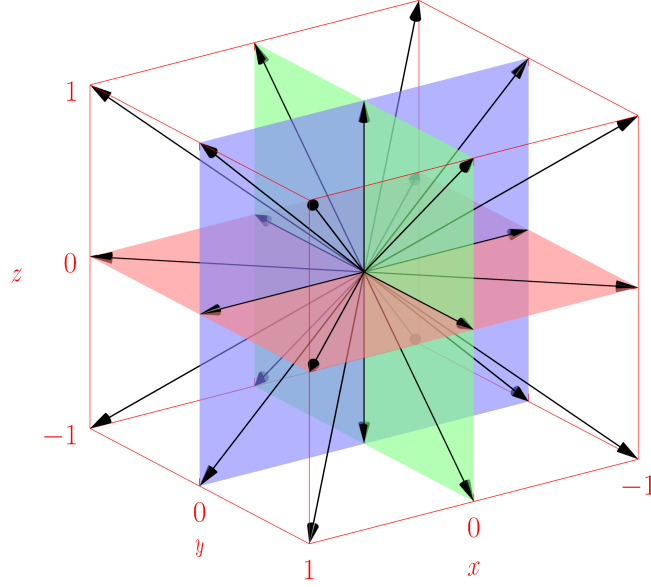
1.1 Discrete velocity vectors

Discrete velocity vectors and the lattice speed of sound are defined by

$$\{\mathbf{c}_i\}_{i=1}^{27} = \left(\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} -1 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ -1 \\ -1 \end{pmatrix} \right),$$

$$c_s = \frac{1}{\sqrt{3}},$$

respectively [1].



1.2 Raw and central moments

The raw and central moments are defined by

$$m_{\alpha} := \sum_{i=1}^{27} f_i \mathbf{c}_i^{\alpha},$$

and

$$k_{\alpha} := \sum_{i=1}^{27} f_i (\mathbf{c}_i - \mathbf{v})^{\alpha},$$

respectively, where $\alpha = (\alpha_1, \alpha_2, \alpha_3) \in \mathbb{Z}^3$ denotes a multi-index (as a row vector) and $\mathbf{c}_i^{\alpha} := \prod_{j=1}^3 [\mathbf{c}_i]_j^{\alpha_j}$.

1.3 Transformation matrix \mathbf{M}

Matrix \mathbf{M} , that defines macroscopic quantities (moments) $\boldsymbol{\mu}$ by

$$\boldsymbol{\mu} = \mathbf{M} \mathbf{f},$$

with $\mathbf{f} = (f_1, f_2, \dots, f_{27})^T$, is selected such that

$$\boldsymbol{\mu} = \begin{pmatrix} m_{(0,0,0)}, m_{(1,0,0)}, m_{(0,1,0)}, m_{(0,0,1)}, m_{(1,1,0)}, m_{(1,0,1)}, m_{(0,1,1)}, m_{(1,1,1)}, m_{(2,0,0)}, \\ m_{(0,2,0)}, m_{(0,0,2)}, m_{(2,1,0)}, m_{(2,0,1)}, m_{(2,1,1)}, m_{(1,2,0)}, m_{(0,2,1)}, m_{(1,2,1)}, m_{(1,0,2)}, \\ m_{(0,1,2)}, m_{(1,1,2)}, m_{(2,2,0)}, m_{(2,0,2)}, m_{(0,2,2)}, m_{(2,2,1)}, m_{(2,1,2)}, m_{(1,2,2)}, m_{(2,2,2)} \end{pmatrix}^T,$$

i.e., \mathbf{M} is given by

[illegible]

1.4 Equilibrium

The corresponding equilibrium raw moments are defined using the continuous Maxwell–Boltzmann distribution function [1]

$$f^{(eq)}(\boldsymbol{\xi}) = \frac{\rho}{(2\pi c_s^2)^{\frac{3}{2}}} \exp\left(-\frac{\|\boldsymbol{\xi} - \mathbf{v}\|^2}{2c_s^2}\right)$$

as

$$m_{\alpha}^{(eq)} = \int_{\mathbb{R}^3} \xi^{\alpha} f^{(eq)}(\xi) d\xi,$$

where $\alpha_i \in \{0, 1, 2\}$, $i = 1, 2, 3$. Hence, the equilibrium moments $\boldsymbol{\mu}^{(eq)}$ satisfy

$$\boldsymbol{\mu}^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho v_1 v_2 \\ \rho v_1 v_3 \\ \rho v_2 v_3 \\ \rho v_1 v_2 v_3 \\ \rho (v_1^2 + c_s^2) \\ \rho (v_2^2 + c_s^2) \\ \rho (v_3^2 + c_s^2) \\ \rho (v_1^2 v_2 + v_2 c_s^2) \\ \rho (v_1^2 v_3 + v_3 c_s^2) \\ \rho (v_1^2 v_2 v_3 + v_2 v_3 c_s^2) \\ \rho (v_1 v_2^2 + v_1 c_s^2) \\ \rho (v_2^2 v_3 + v_3 c_s^2) \\ \rho (v_1 v_2^2 v_3 + v_1 v_3 c_s^2) \\ \rho (v_1 v_3^2 + v_1 c_s^2) \\ \rho (v_2 v_3^2 + v_2 c_s^2) \\ \rho (v_1 v_2 v_3^2 + v_1 v_2 c_s^2) \\ \rho (v_1^2 v_2^2 + v_2^2 c_s^2 + v_1^2 c_s^2 + c_s^4) \\ \rho (v_1^2 v_3^2 + v_3^2 c_s^2 + v_1^2 c_s^2 + c_s^4) \\ \rho (v_2^2 v_3^2 + v_3^2 c_s^2 + v_2^2 c_s^2 + c_s^4) \\ \rho (v_1^2 v_2^2 v_3 + v_2^2 v_3 c_s^2 + v_1^2 v_3 c_s^2 + v_3 c_s^4) \\ \rho (v_1^2 v_2 v_3^2 + v_2 v_3^2 c_s^2 + v_1^2 v_2 c_s^2 + v_2 c_s^4) \\ \rho (v_1 v_2^2 v_3^2 + v_1 v_3^2 c_s^2 + v_1 v_2^2 c_s^2 + v_1 c_s^4) \\ \rho (v_1^2 v_2^2 v_3^2 + v_2^2 v_3^2 c_s^2 + v_1^2 v_3^2 c_s^2 + v_1^2 c_s^4 + v_2^2 c_s^4 + v_1 c_s^6) \end{pmatrix}.$$

2 Spatial EPDEs

2.1 SRT

2.1.1 Definitions

Collision operator \mathcal{C} :

$$\mathcal{C}(\mathbf{f}) = \omega \left(\mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)} - \mathbf{f} \right),$$

$\omega \in (0, 2)$.

2.1.2 Conservation of mass: ρ

$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{\delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + v_1^2 + 3c_s^2) \frac{\delta_l^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & (-1 + 3v_1^2 + c_s^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\delta_l^3 \rho c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\delta_l^3 \rho c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{\delta_l^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\ & \frac{\delta_l^3 \rho c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\delta_l^3 \rho c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\delta_l^3 \rho c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\delta_l^3 \rho c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_l^3 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\ & + (-6v_1^2 - 12\omega v_1^2 c_s^2 - 2c_s^2 + 3\omega v_1^2 + \omega c_s^2 - 3\omega v_1^4 - \omega c_s^4 + 6v_1^4 + 24v_1^2 c_s^2 + 2c_s^4) \frac{\delta_l^4}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 + 10v_1^2 + 6c_s^2 + 2\omega - 5\omega v_1^2 - 3\omega c_s^2) \frac{\delta_l^4 \rho v_1}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (2 - 2v_1^2 - 6c_s^2 - \omega + \omega v_1^2 + 3\omega c_s^2) \frac{\delta_l^4 \rho v_1}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \end{aligned}$$

$$\begin{aligned}
& (-2 + \omega) \frac{\delta_l^4 c_s^4}{6\omega\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_2^2 - 2v_2^2) \frac{\delta_l^4 \rho v_2}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-2c_s^2 + 6v_2^4 + 24v_2^2 c_s^2 + \omega c_s^2 - 3\omega v_2^4 + 3\omega v_2^2 - \omega c_s^4 - 12\omega v_2^2 c_s^2 - 6v_2^2 + 2c_s^4) \frac{\delta_l^4}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 2\omega - 3\omega c_s^2 - 5\omega v_2^2 + 10v_2^2) \frac{\delta_l^4 \rho v_2}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (2 - 2v_1^2 - 6c_s^2 - \omega + \omega v_1^2 + 3\omega c_s^2) \frac{\delta_l^4 \rho v_1}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_2^2 - 2v_2^2) \frac{\delta_l^4 \rho v_2}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 + \omega) \frac{\delta_l^4 c_s^4}{6\omega\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-2 + \omega) \frac{\delta_l^4 c_s^4}{6\omega\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_3^2 - 2v_3^2) \frac{\delta_l^4 \rho v_3}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_3^2 - 2v_3^2) \frac{\delta_l^4 \rho v_3}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (6v_3^4 - 2c_s^2 - 3\omega v_3^4 + \omega c_s^2 + 24v_3^2 c_s^2 + 3\omega v_3^2 - 12\omega v_3^2 c_s^2 - \omega c_s^4 - 6v_3^2 + 2c_s^4) \frac{\delta_l^4}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 6c_s^2 + 2\omega - 3\omega c_s^2 - 5\omega v_3^2 + 10v_3^2) \frac{\delta_l^4 \rho v_3}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.1.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\delta_l \rho v_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho v_2}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\delta_l \rho v_1}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho v_3}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\delta_l \rho v_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + 6v_1^2 + 4c_s^2 + \omega - 3\omega v_1^2 - 2\omega c_s^2) \frac{\delta_l^2}{\omega\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega) \frac{3\delta_l^2 \rho v_1}{\omega\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + \\
& (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + 2v_1^2 + 6c_s^2 + \omega - \omega v_1^2 - 3\omega c_s^2) \frac{\delta_l^2 v_1}{2\omega\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + 6v_1^2 + 2c_s^2 + \omega - 3\omega v_1^2 - \omega c_s^2) \frac{\delta_l^2 \rho}{2\omega\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega) \frac{\delta_l^2 \rho c_s^2}{2\omega\delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega) \frac{\delta_l^2 \rho c_s^2}{2\omega\delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega) \frac{\delta_l^2 \rho c_s^2}{2\omega\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega) \frac{\delta_l^2 \rho c_s^2}{2\omega\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 + 60v_1^2 + 36c_s^2 + 24\omega - 60\omega v_1^2 - 36\omega c_s^2 + 5\omega^2 c_s^2 + 11\omega^2 v_1^2 - 4\omega^2) \frac{\delta_l^3 \rho v_1}{6\omega^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (12 - 12v_1^2 - 36c_s^2 - 12\omega + 12\omega v_1^2 + 36\omega c_s^2 - 11\omega^2 c_s^2 - 3\omega^2 v_1^2 + 3\omega^2) \frac{\delta_l^3 \rho v_1}{12\omega^2\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 + 12\omega - \omega^2) \frac{\delta_l^3 c_s^4}{6\omega^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{\delta_l^3 \rho v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{\delta_l^3 v_1 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + \\
& (6 - 18c_s^2 - 6\omega - \omega^2 v_2^2 + 18\omega c_s^2 - 3\omega^2 c_s^2 + 6\omega v_2^2 + \omega^2 - 6v_2^2) \frac{\delta_l^3 \rho v_2}{6\omega^2\delta_t} \frac{\partial^3 v_1}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\delta_l^3 \rho v_1}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12v_1^2 - 36c_s^2 - 12\omega + 12\omega v_1^2 + 36\omega c_s^2 - 11\omega^2 c_s^2 - 3\omega^2 v_1^2 + 3\omega^2) \frac{\delta_l^3 \rho v_1}{12\omega^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\delta_l^3 \rho v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-12 + 12\omega - \omega^2) \frac{\delta_l^3 c_s^4}{6\omega^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \frac{\delta_l^3 \rho v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\delta_l^3 \rho v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_l^3 v_1 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (6 - 18c_s^2 - 6\omega + 18\omega c_s^2 - \omega^2 v_3^2 + 6\omega v_3^2 - 3\omega^2 c_s^2 + \omega^2 - 6v_3^2) \frac{\delta_l^3 \rho v_3}{6\omega^2\delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\delta_l^3 \rho v_1}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_2 \frac{\delta_l^4 v_1}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_3 \frac{\delta_l^4 \rho}{12\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_4 \frac{\delta_l^4 \rho}{12\omega^3\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_5 \frac{\delta_l^4 v_1 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (-24 + 72v_1^2 + 12c_s^2 + 36\omega - 108\omega v_1^2 - 18\omega c_s^2 + 8\omega^2 c_s^2 + 36\omega^2 v_1^2 - 12\omega^2 - \omega^3 c_s^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_6 \frac{\delta_l^4 v_2 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& + (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_2^2 - 2v_2^2) \frac{\delta_l^4 \rho v_1 v_2}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-12 + 18\omega + 18\omega^2 v_2^2 + 2\omega^2 c_s^2 - 54\omega v_2^2 - 6\omega^2 - \omega^3 c_s^2 + 36v_2^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\
& (-2c_s^2 + 6v_2^4 + 24v_2^2 c_s^2 + \omega c_s^2 - 3\omega v_2^4 + 3\omega v_2^2 - \omega c_s^4 - 12\omega v_2^2 c_s^2 - 6v_2^2 + 2c_s^4) \frac{\delta_l^4 v_1}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_7 \frac{\delta_l^4 \rho}{24\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 2\omega - 3\omega c_s^2 - 5\omega v_2^2 + 10v_2^2) \frac{\delta_l^4 \rho v_1 v_2}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_8 \frac{\delta_l^4 \rho}{12\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-36 + 54\omega - \omega^3 - 16\omega^2) \frac{\delta_l^4 \rho c_s^4}{12\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_2^2 - 2v_2^2) \frac{\delta_l^4 \rho v_1 v_2}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_9 \frac{\delta_l^4 v_1 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& (-24 + 72v_1^2 + 12c_s^2 + 36\omega - 108\omega v_1^2 - 18\omega c_s^2 + 8\omega^2 c_s^2 + 36\omega^2 v_1^2 - 12\omega^2 - \omega^3 c_s^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{10} \frac{\delta_l^4}{2\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& + C_{11} \frac{\delta_l^4 \rho}{2\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{12} \frac{\delta_l^4 \rho}{12\omega^3\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{13} \frac{\delta_l^4 \rho v_3}{\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{14} \frac{\delta_l^4}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{15} \frac{\delta_l^4 \rho}{4\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + \\
& C_{16} \frac{\delta_l^4 \rho v_2}{2\omega^3\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{17} \frac{\delta_l^4 \rho}{4\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{18} \frac{\delta_l^4 v_3 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_3^2 - 2v_3^2) \frac{\delta_l^4 \rho v_1 v_3}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (-12 + 18\omega + 18\omega^2 v_3^2 - 54\omega v_3^2 + 2\omega^2 c_s^2 - 6\omega^2 + 36v_3^2 - \omega^3 c_s^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_3^2 - 2v_3^2) \frac{\delta_l^4 \rho v_1 v_3}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} +
\end{aligned}$$

$$(6v_3^4 - 2c_s^2 - 3\omega v_3^4 + \omega c_s^2 + 24v_3^2 c_s^2 + 3\omega v_3^2 - 12\omega v_3^2 c_s^2 - \omega c_s^4 - 6v_3^2 + 2c_s^4) \frac{\delta_l^4 v_1}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{19} \frac{\delta_l^4 \rho}{24\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + (-4 + 6c_s^2 + 2\omega - 3\omega c_s^2 - 5\omega v_3^2 + 10v_3^2) \frac{\delta_l^4 \rho v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,$$

where:

$$\begin{aligned} C_1 &= -36v_1^2 - 144\omega v_1^2 c_s^2 - 12c_s^2 + 36\omega v_1^2 + \omega^2 c_s^4 + 12\omega c_s^2 + 7\omega^2 v_1^4 - \omega^2 c_s^2 - 36\omega v_1^4 - 7\omega^2 v_1^2 - 12\omega c_s^4 + 24\omega^2 v_1^2 c_s^2 + 36v_1^4 + 144v_1^2 c_s^2 + 12c_s^4 \\ C_2 &= 12 - 156v_1^2 - 5\omega^3 c_s^4 - 1008\omega v_1^2 c_s^2 - 132c_s^2 - 18\omega - 9\omega^3 v_1^4 + 234\omega v_1^2 + 82\omega^2 c_s^4 + 198\omega c_s^2 - 34\omega^3 v_1^2 c_s^2 + 90\omega^2 v_1^4 - 78\omega^2 c_s^2 - \omega^3 - 216\omega v_1^4 - 98\omega^2 v_1^2 - 216\omega c_s^4 + 8\omega^2 + 404\omega^2 v_1^2 c_s^2 + 144v_1^4 + 6\omega^3 c_s^2 + 672v_1^2 c_s^2 + 144c_s^4 + 10\omega^3 v_1^2 \\ C_3 &= 12 - 252v_1^2 - \omega^3 c_s^4 - 648\omega v_1^2 c_s^2 - 36c_s^2 - 18\omega - 29\omega^3 v_1^4 + 378\omega v_1^2 + 14\omega^2 c_s^4 + 54\omega c_s^2 - 18\omega^3 v_1^2 c_s^2 + 310\omega^2 v_1^4 - 22\omega^2 c_s^2 - \omega^3 - 756\omega v_1^4 - 154\omega^2 v_1^2 - 36\omega c_s^4 + 8\omega^2 + 252\omega^2 v_1^2 c_s^2 + 504v_1^4 + 2\omega^3 c_s^2 + 432v_1^2 c_s^2 + 24c_s^4 + 14\omega^3 v_1^2 \\ C_4 &= 36v_1^2 - \omega^3 c_s^4 + 54\omega v_1^2 c_s^2 - 24c_s^2 + 4\omega^3 v_1^4 - 54\omega v_1^2 + 20\omega^2 c_s^4 + 36\omega c_s^2 + 12\omega^3 v_1^2 c_s^2 - 26\omega^2 v_1^4 - 12\omega^2 c_s^2 + 54\omega v_1^4 + 26\omega^2 v_1^2 - 54\omega c_s^4 - 42\omega^2 v_1^2 c_s^2 - 36v_1^4 - 36v_1^2 c_s^2 + 36c_s^4 - 4\omega^3 v_1^2 \\ C_5 &= 24 - 24v_1^2 - 72c_s^2 - 36\omega + 36\omega v_1^2 + 108\omega c_s^2 - 46\omega^2 c_s^2 - \omega^3 - 14\omega^2 v_1^2 + 14\omega^2 + 5\omega^3 c_s^2 + \omega^3 v_1^2 \\ C_6 &= 24 + \omega^3 v_2^2 - 72c_s^2 - 36\omega - 14\omega^2 v_2^2 + 108\omega c_s^2 - 42\omega^2 c_s^2 - \omega^3 + 36\omega v_2^2 + 14\omega^2 + 3\omega^3 c_s^2 - 24v_2^2 \\ C_7 &= -3\omega^3 c_s^4 - 84\omega^2 v_2^2 c_s^2 - 3\omega^3 v_2^2 - 24c_s^2 - 72v_2^4 - 144v_2^2 c_s^2 + 42\omega^2 v_2^2 + 30\omega^2 c_s^4 + 36\omega c_s^2 + 108\omega v_2^4 - 14\omega^2 c_s^2 - 42\omega^2 v_2^4 - 108\omega v_2^2 - 72\omega c_s^4 + 6\omega^3 v_2^2 c_s^2 + 216\omega v_2^2 c_s^2 + 3\omega^3 v_2^4 + \omega^3 c_s^2 + 72v_2^2 + 48c_s^4 \\ C_8 &= 36v_1^2 - \omega^3 c_s^4 + 54\omega v_1^2 c_s^2 - 24c_s^2 + 4\omega^3 v_1^4 - 54\omega v_1^2 + 20\omega^2 c_s^4 + 36\omega c_s^2 + 12\omega^3 v_1^2 c_s^2 - 26\omega^2 v_1^4 - 12\omega^2 c_s^2 + 54\omega v_1^4 + 26\omega^2 v_1^2 - 54\omega c_s^4 - 42\omega^2 v_1^2 c_s^2 - 36v_1^4 - 36v_1^2 c_s^2 + 36c_s^4 - 4\omega^3 v_1^2 \\ C_9 &= 24 - 24v_1^2 - 72c_s^2 - 36\omega + 36\omega v_1^2 + 108\omega c_s^2 - 46\omega^2 c_s^2 - \omega^3 - 14\omega^2 v_1^2 + 14\omega^2 + 5\omega^3 c_s^2 + \omega^3 v_1^2 \\ C_{10} &= -36\omega v_2^2 v_3^2 c_s^2 + \omega^3 v_1 v_2^2 c_s^2 - 24v_1 v_2^2 c_s^2 + 36\omega v_1 v_2^2 v_3^2 + 24v_1^2 v_2 c_s^2 - 14\omega^2 v_1 v_2^2 c_s^2 - \omega^3 v_1^2 v_2 c_s^2 - 36\omega v_1^2 v_2 v_3^2 + 14\omega^2 v_1^2 v_2 c_s^2 - 24v_1 v_2^2 c_s^2 + \omega^3 v_1 v_2^2 c_s^2 - 14\omega^2 v_1 v_2^2 c_s^2 + 14\omega^2 v_2 v_3^2 c_s^2 + 14\omega^2 v_1^2 v_2 v_3^2 + 36\omega v_1 v_2^2 c_s^2 + 24v_1^2 v_2 v_3^2 - \omega^3 v_1^2 v_2 v_3^2 - 36\omega v_1^2 v_2 v_3^2 + \omega^3 v_1 v_2^2 v_3^2 - 24v_1 v_2^2 v_3^2 - \omega^3 v_2 v_2^2 c_s^2 + 36\omega v_1 v_2^2 c_s^2 + 24v_2 v_3^2 c_s^2 \\ C_{11} &= -2\omega^3 v_1 v_2 v_3^2 + 48v_1 v_2 v_3^2 - 14\omega^2 v_2^2 c_s^2 - 72\omega v_1 v_2 c_s^2 + 36\omega v_2^2 v_3^2 - 24v_2^2 c_s^2 - 14\omega^2 v_2^2 c_s^2 + \omega^3 v_2^2 v_3^2 + 28\omega^2 v_1 v_2 v_3^2 - 24v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 + 28\omega^2 v_1 v_2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 24v_2^2 v_3^2 - 2\omega^3 v_1 v_2 c_s^2 + 48v_1 v_2 c_s^2 - 14\omega^2 v_2^2 v_3^2 + \omega^3 v_2^2 v_3^2 - 72\omega v_1 v_2 v_3^2 \\ C_{12} &= 12\omega^3 v_1 v_2 v_3^2 + 144v_1^2 v_3^2 - \omega^3 c_s^4 - 288v_1 v_2 v_3^2 + 432\omega v_1 v_2 c_s^2 - 216\omega v_1^2 c_s^2 + 84\omega^2 v_1^2 v_3^2 + 84\omega^2 v_2^2 c_s^2 - 16\omega^2 c_s^4 - 6\omega^3 v_1^2 c_s^2 - 168\omega^2 v_1 v_2 v_3^2 + 144v_2^2 c_s^2 - 6\omega^3 v_1^2 v_3^2 - 216\omega v_2^2 c_s^2 - 168\omega^2 v_1 v_2 c_s^2 + 54\omega c_s^4 + 84\omega^2 v_1^2 c_s^2 + 12\omega^3 v_1 v_2 c_s^2 + 144v_1^2 c_s^2 - 288v_1 v_2 c_s^2 - 6\omega^3 v_2^2 c_s^2 - 36c_s^4 + 432\omega v_1 v_2 v_3^2 - 216\omega v_1^2 v_3^2 \\ C_{13} &= -24v_1 c_s^2 - 36\omega v_2 c_s^2 - 14\omega^2 v_1 c_s^2 + 36\omega v_1 v_2^2 + \omega^3 v_1 v_2^2 + 24v_1^2 v_2 - \omega^3 v_2 c_s^2 + 14\omega^2 v_1^2 v_2 + \omega^3 v_1 c_s^2 - 36\omega v_1^2 v_2 - 24v_1 v_2^2 - \omega^3 v_1^2 v_2 + 24v_2 c_s^2 + 14\omega^2 v_2 c_s^2 - 14\omega^2 v_1 v_2^2 + 36\omega v_1 c_s^2 \\ C_{14} &= -3\omega^3 v_1 v_2^2 c_s^2 - 42\omega^2 v_2^2 v_3 c_s^2 + 72v_1 v_2^2 c_s^2 - 108\omega v_1 v_2^2 v_3^2 + 42\omega^2 v_1 v_2^2 c_s^2 + 108\omega v_2^2 v_3 c_s^2 - 42\omega^2 v_1^2 v_2^2 v_3 + 72v_1 v_2^2 c_s^2 - 3\omega^3 v_1 v_2^2 c_s^2 + 2\omega^3 v_1 c_s^4 - 72v_1^2 v_2^2 v_3 + 3\omega^3 v_2^2 v_2^2 v_3 + 3\omega^3 v_1^2 v_2^2 v_3 - 72v_1^2 v_2^2 v_3 + 42\omega^2 v_1 v_2^2 c_s^2 + 42\omega^2 v_1 v_2^2 v_3 + 108\omega v_1^2 v_2^2 v_3 + 108\omega v_1^2 v_2^2 v_3 - 42\omega^2 v_2^2 v_2^2 v_3 - 108\omega v_1 v_2^2 c_s^2 - 72v_2^2 v_2^2 c_s^2 + 3\omega^3 v_2^2 v_2^2 c_s^2 - 3\omega^3 v_1 v_2^2 v_2^2 - 4\omega^2 v_1 c_s^4 + 72v_1 v_2^2 v_2^2 - 108\omega v_1 v_2^2 c_s^2 \\ C_{15} &= 14\omega^2 v_2^2 c_s^2 - 36\omega v_2^2 v_3^2 + 24v_2^2 c_s^2 + 14\omega^2 v_2^2 c_s^2 - 4\omega^2 c_s^4 - \omega^3 v_2^2 v_3^2 + 72\omega v_1 v_2 c_s^2 + 72\omega v_1 v_2^2 v_3 + 24v_2^2 c_s^2 - 36\omega v_2^2 c_s^2 + 2\omega^3 v_1 v_2^2 v_3 - 48v_1 v_2^2 v_3 - 48v_1 v_2 c_s^2 + 2\omega^3 v_1 v_2 c_s^2 + 12\omega c_s^4 - \omega^3 v_2^2 c_s^2 - 36\omega v_2^2 c_s^2 - 28\omega^2 v_1 v_2 c_s^2 + 24v_2^2 v_3 + 14\omega^2 v_2^2 v_3 - \omega^3 v_2^2 c_s^2 - 8c_s^4 - 28\omega^2 v_1 v_2 v_3 \\ C_{16} &= 24v_1 c_s^2 + \omega^3 v_2 c_s^2 - 36\omega v_1 v_2^2 + 14\omega^2 v_1 c_s^2 - 14\omega^2 v_1^2 v_3 - \omega^3 v_1 v_2^2 + 36\omega v_2 c_s^2 - 24v_1^2 v_3 - \omega^3 v_1 c_s^2 + 36\omega v_1^2 v_3 - 24v_2 c_s^2 - 14\omega^2 v_2 c_s^2 + 14\omega^2 v_1 v_2^2 + \omega^3 v_1^2 v_2 - 36\omega v_1 c_s^2 \\ C_{17} &= -14\omega^2 v_2^2 c_s^2 - 14\omega^2 v_1^2 v_2^2 + 36\omega v_1^2 c_s^2 - 24v_1^2 v_2^2 - 24v_2^2 c_s^2 - 72\omega v_1 v_2 c_s^2 - 72\omega v_1 v_2^2 v_3 + \omega^3 v_1^2 c_s^2 - 2\omega^3 v_1 v_2^2 v_3 + 48v_1 v_2^2 v_3 + \omega^3 v_1^2 v_2^2 + 48v_1 v_2 c_s^2 - 2\omega^3 v_1 v_2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 + 28\omega^2 v_1 v_2 c_s^2 - 14\omega^2 v_1^2 c_s^2 + 36\omega v_1^2 v_2^2 - 24v_1^2 c_s^2 + 28\omega^2 v_1 v_2^2 v_3 \\ C_{18} &= 24 - 72c_s^2 - 36\omega + \omega^3 v_3^2 + 108\omega c_s^2 - 14\omega^2 v_3^2 + 36\omega v_3^2 - 42\omega^2 c_s^2 - \omega^3 + 14\omega^2 - 24v_3^2 + 3\omega^3 c_s^2 \\ C_{19} &= -3\omega^3 c_s^4 - 72v_3^4 - 24c_s^2 - 3\omega^3 v_3^2 - 84\omega^2 v_3^2 c_s^2 + 108\omega v_3^4 + 30\omega^2 c_s^4 + 36\omega c_s^2 + 42\omega^2 v_3^2 - 144v_3^2 c_s^2 - 108\omega v_3^2 - 14\omega^2 c_s^2 + 216\omega v_3^2 c_s^2 - 72\omega c_s^4 - 42\omega^2 v_3^4 + 72v_3^2 + \omega^3 c_s^2 + 3\omega^3 v_3^4 + 6\omega^3 v_3^2 c_s^2 + 48c_s^4 \end{aligned}$$

2.1.4 Conservation of momentum: ρv_2

$$v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{\delta_l v_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho v_2}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l \rho v_1}{\delta_t} \frac{\partial v_2}{\partial x_1} + (c_s^2 + v_2^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2\delta_l \rho v_2}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_2 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho v_3}{\delta_t} \frac{\partial v_2}{\partial x_3} + \frac{\delta_l \rho v_2}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-2 + 4c_s^2 + \omega - 2\omega c_s^2 - 3\omega v_2^2 + 6v_2^2) \frac{\delta_l^2}{\omega \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} +$$

$$\begin{aligned}
& (2 - \omega) \frac{3\delta_t^3 \rho v_2}{\omega \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega) \frac{\delta_t^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega) \frac{\delta_t^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega) \frac{\delta_t^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + \\
& (-2 + \omega) \frac{\delta_t^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (-2 + 6c_s^2 + \omega - 3\omega c_s^2 - \omega v_2^2 + 2v_2^2) \frac{\delta_t^2 v_2}{2\omega \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + 2c_s^2 + \omega - \omega c_s^2 - 3\omega v_2^2 + 6v_2^2) \frac{\delta_t^2 \rho}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} \\
& + (-2 + \omega) \frac{\delta_t^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega) \frac{\delta_t^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-1 + v_1^2 + 3c_s^2) \frac{\delta_t^3 v_1 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{\delta_t^3 \rho v_2}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (6 - 6v_1^2 - 18c_s^2 - 6\omega + 6\omega v_1^2 + 18\omega c_s^2 - 3\omega^2 c_s^2 - \omega^2 v_1^2 + \omega^2) \frac{\delta_t^3 \rho v_1}{6\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 + 12\omega - \omega^2) \frac{\delta_t^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \\
& \frac{\delta_t^3 \rho v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + (12 - 36c_s^2 - 12\omega - 3\omega^2 v_2^2 + 36\omega c_s^2 - 11\omega^2 c_s^2 + 12\omega v_2^2 + 3\omega^2 - 12v_2^2) \frac{\delta_t^3 \rho v_2}{12\omega^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2} + \\
& C_1 \frac{\delta_t^3}{12\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-24 + 36c_s^2 + 24\omega + 11\omega^2 v_2^2 - 36\omega c_s^2 + 5\omega^2 c_s^2 - 60\omega v_2^2 - 4\omega^2 + 60v_2^2) \frac{\delta_t^3 \rho v_2}{6\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \frac{\delta_t^3 \rho v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3} \\
& + (12 - 36c_s^2 - 12\omega - 3\omega^2 v_2^2 + 36\omega c_s^2 - 11\omega^2 c_s^2 + 12\omega v_2^2 + 3\omega^2 - 12v_2^2) \frac{\delta_t^3 \rho v_2}{12\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\delta_t^3 \rho v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3} + \\
& (-12 + 12\omega - \omega^2) \frac{\delta_t^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3} - \frac{\delta_t^3 \rho v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_t^3 v_2 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (6 - 18c_s^2 - 6\omega + 18\omega c_s^2 - \omega^2 v_3^2 + 6\omega v_3^2 - 3\omega^2 c_s^2 + \omega^2 - 6v_3^2) \frac{\delta_t^3 \rho v_3}{6\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\delta_t^3 \rho v_2}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-6v_1^2 - 12\omega v_1^2 c_s^2 - 2c_s^2 + 3\omega v_1^2 + \omega c_s^2 - 3\omega v_1^4 - \omega c_s^4 + 6v_1^4 + 24v_1^2 c_s^2 + 2c_s^4) \frac{\delta_t^4 v_2}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 10v_1^2 + 6c_s^2 + 2\omega - 5\omega v_1^2 - 3\omega c_s^2) \frac{\delta_t^4 \rho v_1 v_2}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_2 \frac{\delta_t^4 \rho}{24\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_3 \frac{\delta_t^4 v_1 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& (-12 + 36v_1^2 + 18\omega - 54\omega v_1^2 + 2\omega^2 c_s^2 + 18\omega^2 v_1^2 - 6\omega^2 - \omega^3 c_s^2) \frac{\delta_t^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& (2 - 2v_1^2 - 6c_s^2 - \omega + \omega v_1^2 + 3\omega c_s^2) \frac{\delta_t^4 \rho v_1 v_2}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_4 \frac{\delta_t^4 v_2 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (-24 + 12c_s^2 + 36\omega + 36\omega^2 v_2^2 - 18\omega c_s^2 + 8\omega^2 c_s^2 - 108\omega v_2^2 - 12\omega^2 - \omega^3 c_s^2 + 72v_2^2) \frac{\delta_t^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_5 \frac{\delta_t^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} \\
& + C_6 \frac{\delta_t^4 v_2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_7 \frac{\delta_t^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (2 - 2v_1^2 - 6c_s^2 - \omega + \omega v_1^2 + 3\omega c_s^2) \frac{\delta_t^4 \rho v_1 v_2}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-36 + 54\omega - \omega^3 - 16\omega^2) \frac{\delta_t^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_8 \frac{\delta_t^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + C_9 \frac{\delta_t^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{10} \frac{\delta_t^4 \rho}{4\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& C_{11} \frac{\delta_t^4 \rho}{4\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + C_{12} \frac{\delta_t^4 \rho v_3}{2\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{13} \frac{\delta_t^4 \rho}{2\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{14} \frac{\delta_t^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{15} \frac{\delta_t^4 \rho v_2}{\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{16} \frac{\delta_t^4 \rho}{2\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{17} \frac{\delta_t^4 v_2 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (-24 + 12c_s^2 + 36\omega + 36\omega^2 v_2^2 - 18\omega c_s^2 + 8\omega^2 c_s^2 - 108\omega v_2^2 - 12\omega^2 - \omega^3 c_s^2 + 72v_2^2) \frac{\delta_t^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_3^2 - 2v_3^2) \frac{\delta_t^4 \rho v_2 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{18} \frac{\delta_t^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_3^2 - 2v_3^2) \frac{\delta_t^4 \rho v_2 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-12 + 18\omega + 18\omega^2 v_3^2 - 54\omega v_3^2 + 2\omega^2 c_s^2 - 6\omega^2 + 36v_3^2 - \omega^3 c_s^2) \frac{\delta_t^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& (6v_3^4 - 2c_s^2 - 3\omega v_3^4 + \omega c_s^2 + 24v_3^2 c_s^2 + 3\omega v_3^2 - 12\omega v_3^2 c_s^2 - \omega c_s^4 - 6v_3^2 + 2c_s^4) \frac{\delta_t^4 v_2}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{19} \frac{\delta_t^4 \rho}{24\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_3^4} + \\
& (-4 + 6c_s^2 + 2\omega - 3\omega c_s^2 - 5\omega v_3^2 + 10v_3^2) \frac{\delta_t^4 \rho v_2 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 24\omega^2 v_2^2 c_s^2 - 12c_s^2 + 36v_2^4 + 144v_2^2 c_s^2 - 7\omega^2 v_2^2 + \omega^2 c_s^4 + 12\omega c_s^2 - 36\omega v_2^2 - \omega^2 c_s^2 + 7\omega^2 v_2^2 + 36\omega v_2^2 - 12\omega c_s^4 - 144\omega v_2^2 c_s^2 - 36v_2^2 + 12c_s^4 \\
C_2 &= 72v_1^2 - 3\omega^3 c_s^4 + 216\omega v_1^2 c_s^2 - 24c_s^2 + 3\omega^3 v_1^4 - 108\omega v_1^2 + 30\omega^2 c_s^4 + 36\omega c_s^2 + 6\omega^3 v_1^2 c_s^2 - 42\omega^2 v_1^4 - 14\omega^2 c_s^2 + 108\omega v_1^4 + 42\omega^2 v_1^2 - 72\omega c_s^4 - \\
& 84\omega^2 v_1^2 c_s^2 - 72v_1^4 + \omega^3 c_s^2 - 144\omega v_1^2 c_s^2 + 48c_s^4 - 3\omega^3 v_1^2 \\
C_3 &= 24 - 24v_1^2 - 72c_s^2 - 36\omega + 36\omega v_1^2 + 108\omega c_s^2 - 42\omega^2 c_s^2 - \omega^3 - 14\omega^2 v_1^2 + 14\omega^2 + 3\omega^3 c_s^2 + \omega^3 v_1^2 \\
C_4 &= 24 + \omega^3 v_2^2 - 72c_s^2 - 36\omega - 14\omega^2 v_2^2 + 108\omega c_s^2 - 46\omega^2 c_s^2 - \omega^3 + 36\omega v_2^2 + 14\omega^2 + 5\omega^3 c_s^2 - 24v_2^2 \\
C_5 &= -\omega^3 c_s^4 - 42\omega^2 v_2^2 c_s^2 - 4\omega^3 v_2^2 - 24c_s^2 - 36v_2^4 - 36v_2^2 c_s^2 + 26\omega^2 v_2^2 + 20\omega^2 c_s^4 + 36\omega c_s^2 + 54\omega v_2^4 - 12\omega^2 c_s^2 - 26\omega^2 v_2^4 - 54\omega v_2^2 - 54\omega c_s^4 + \\
& 12\omega^3 v_2^2 c_s^2 + 54\omega v_2^2 c_s^2 + 4\omega^3 v_2^4 + 36v_2^2 + 36c_s^4 \\
C_6 &= 12 - 5\omega^3 c_s^4 + 404\omega^2 v_2^2 c_s^2 + 10\omega^3 v_2^2 - 132c_s^2 - 18\omega + 144v_2^4 + 672v_2^2 c_s^2 - 98\omega^2 v_2^2 + 82\omega^2 c_s^4 + 198\omega c_s^2 - 216\omega v_2^4 - 78\omega^2 c_s^2 + 90\omega^2 v_2^4 - \\
& \omega^3 + 234\omega v_2^2 - 216\omega c_s^4 - 34\omega^3 v_2^2 c_s^2 + 8\omega^2 - 1008\omega v_2^2 c_s^2 - 9\omega^3 v_2^4 + 6\omega^3 c_s^2 - 156v_2^2 + 144c_s^4
\end{aligned}$$

$$\begin{aligned}
C_7 &= 12 - \omega^3 c_s^4 + 252\omega^2 v_2^2 c_s^2 + 14\omega^3 v_2^2 - 36c_s^2 - 18\omega + 504v_2^4 + 432v_2^2 c_s^2 - 154\omega^2 v_2^2 + 14\omega^2 c_s^4 + 54\omega c_s^2 - 756\omega v_2^4 - 22\omega^2 c_s^2 + 310\omega^2 v_2^4 - \omega^3 + \\
& 378\omega v_2^2 - 36\omega c_s^4 - 18\omega^3 v_2^2 c_s^2 + 8\omega^2 - 648\omega v_2^2 c_s^2 - 29\omega^3 v_2^4 + 2\omega^3 c_s^2 - 252v_2^2 + 24c_s^4 \\
C_8 &= -\omega^3 c_s^4 - 42\omega^2 v_2^2 c_s^2 - 4\omega^3 v_2^2 - 24c_s^2 - 36v_2^4 - 36v_2^2 c_s^2 + 26\omega^2 v_2^2 + 20\omega^2 c_s^4 + 36\omega c_s^2 + 54\omega v_2^4 - 12\omega^2 c_s^2 - 26\omega^2 v_2^4 - 54\omega v_2^2 - 54\omega c_s^4 + \\
& 12\omega^3 v_2^2 c_s^2 + 54\omega v_2^2 c_s^2 + 4\omega^3 v_2^4 + 36v_2^2 + 36c_s^4 \\
C_9 &= -108\omega v_2 v_3^2 c_s^2 + 3\omega^3 v_1 v_3^2 c_s^2 - 72v_1 v_2^2 c_s^2 + 108\omega v_1 v_2^2 v_3^2 + 72v_1^2 v_2 c_s^2 - 42\omega^2 v_1 v_3^2 c_s^2 - 3\omega^3 v_1^2 v_2 c_s^2 - 4\omega^2 v_2 c_s^4 - 108\omega v_1^2 v_2 v_3^2 + \\
& 42\omega^2 v_1^2 v_2 c_s^2 - 72v_1 v_3^2 c_s^2 + 3\omega^3 v_1 v_3^2 c_s^2 - 42\omega^2 v_1 v_2^2 c_s^2 - 42\omega^2 v_1 v_2^2 v_3^2 + 2\omega^3 v_2 c_s^4 + 42\omega^2 v_2 v_3^2 c_s^2 + 42\omega^2 v_1^2 v_2 v_3^2 + 108\omega v_1 v_3^2 c_s^2 + 72v_1^2 v_2 v_3^2 - \\
& 3\omega^3 v_1^2 v_2 v_3^2 - 108\omega v_1^2 v_2 c_s^2 + 3\omega^3 v_1 v_2^2 v_3^2 - 72v_1 v_2^2 v_3^2 - 3\omega^3 v_2 v_3^2 c_s^2 + 108\omega v_1 v_2^2 c_s^2 + 72v_2 v_3^2 c_s^2 \\
C_{10} &= -2\omega^3 v_1 v_2 v_3^2 + 48v_1 v_2 v_3^2 - 14\omega^2 v_2^2 c_s^2 - 72\omega v_1 v_2 c_s^2 + 36\omega v_2^2 v_3^2 - 24v_2^2 c_s^2 - 14\omega^2 v_3^2 c_s^2 + \omega^3 v_2^2 v_3^2 + 28\omega^2 v_1 v_2 v_3^2 - 24v_3^2 c_s^2 + 36\omega v_3^2 c_s^2 + \\
& 28\omega^2 v_1 v_2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 24v_2^2 v_3^2 - 2\omega^3 v_1 v_2 c_s^2 + 48v_1 v_2 c_s^2 - 14\omega^2 v_2^2 v_3^2 + \omega^3 v_3^2 c_s^2 - 72\omega v_1 v_2 v_3^2 \\
C_{11} &= 2\omega^3 v_1 v_2 v_3^2 + 24v_1^2 v_3^2 - 48v_1 v_2 v_3^2 + 72\omega v_1 v_2 c_s^2 - 36\omega v_1^2 c_s^2 + 14\omega^2 v_1^2 v_3^2 + 14\omega^2 v_3^2 c_s^2 - 4\omega^2 c_s^4 - \omega^3 v_1^2 c_s^2 - 28\omega^2 v_1 v_2 v_3^2 + 24v_3^2 c_s^2 - \\
& \omega^3 v_1^2 v_3^2 - 36\omega v_3^2 c_s^2 - 28\omega^2 v_1 v_2 c_s^2 + 12\omega c_s^4 + 14\omega^2 v_1^2 c_s^2 + 2\omega^3 v_1 v_2 c_s^2 + 24v_1^2 c_s^2 - 48v_1 v_2 c_s^2 - \omega^3 v_3^2 c_s^2 - 8c_s^4 + 72\omega v_1 v_2 v_3^2 - 36\omega v_1^2 v_3^2 \\
C_{12} &= -24v_1 c_s^2 - 36\omega v_2 c_s^2 - 14\omega^2 v_1 c_s^2 + 36\omega v_1 v_2^2 + \omega^3 v_1 v_2^2 + 24v_1^2 v_2 - \omega^3 v_2 c_s^2 + 14\omega^2 v_1^2 v_2 + \omega^3 v_1 c_s^2 - 36\omega v_1^2 v_2 - 24v_1 v_2^2 - \omega^3 v_1^2 v_2 + \\
& 24v_2 c_s^2 + 14\omega^2 v_2 c_s^2 - 14\omega^2 v_1 v_2^2 + 36\omega v_1 c_s^2 \\
C_{13} &= -\omega^3 v_1 v_2^2 c_s^2 - 14\omega^2 v_1 v_3 c_s^2 + 24v_1 v_2^2 c_s^2 - 36\omega v_1 v_2^2 v_3^2 + 14\omega^2 v_1 v_3^2 c_s^2 + 36\omega v_2^2 v_3 c_s^2 - 14\omega^2 v_2^2 v_3^2 + 24v_1 v_3^2 c_s^2 - \omega^3 v_1 v_3^2 c_s^2 - 24v_1^2 v_2^2 v_3 + \\
& \omega^3 v_1^2 v_2^2 v_3 + \omega^3 v_1^2 v_3 c_s^2 - 24v_1^2 v_3 c_s^2 + 14\omega^2 v_1 v_3^2 c_s^2 + 14\omega^2 v_1 v_2^2 v_3^2 + 36\omega v_1^2 v_3 c_s^2 + 36\omega v_1^2 v_2^2 v_3 - 14\omega^2 v_2^2 v_3 c_s^2 - 36\omega v_1 v_3^2 c_s^2 - 24v_2^2 v_3 c_s^2 + \\
& \omega^3 v_2^2 v_3 c_s^2 - \omega^3 v_1 v_2^2 v_3^2 + 24v_1 v_2^2 v_3^2 - 36\omega v_1 v_2^2 c_s^2 \\
C_{14} &= -\omega^3 c_s^4 + 84\omega^2 v_2^2 c_s^2 - 216\omega v_2^2 v_3^2 + 144v_2^2 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 - 6\omega^3 v_2^2 v_3^2 + 432\omega v_1 v_3 c_s^2 + 432\omega v_1 v_2^2 v_3 + 144v_3^2 c_s^2 - 216\omega v_3^2 c_s^2 + 12\omega^3 v_1 v_2^2 v_3 - \\
& 288v_1 v_2^2 v_3 - 288v_1 v_3 c_s^2 + 12\omega^3 v_1 v_3 c_s^2 + 54\omega c_s^4 - 6\omega^3 v_2^2 c_s^2 - 216\omega v_2^2 c_s^2 - 168\omega^2 v_1 v_3 c_s^2 + 144v_2^2 v_3^2 + 84\omega^2 v_2^2 v_3^2 - 6\omega^3 v_3^2 c_s^2 - 36c_s^4 - 168\omega^2 v_1 v_2^2 v_3 \\
C_{15} &= 24v_1 c_s^2 + \omega^3 v_3 c_s^2 - 36\omega v_1 v_3^2 + 14\omega^2 v_1 c_s^2 - 14\omega^2 v_1^2 v_3 - \omega^3 v_1 v_3^2 + 36\omega v_3 c_s^2 - 24v_1^2 v_3 - \omega^3 v_1 c_s^2 + 36\omega v_1^2 v_3 - 24v_3 c_s^2 - 14\omega^2 v_3 c_s^2 + \\
& 14\omega^2 v_1 v_3^2 + 24v_1 v_3^2 + \omega^3 v_1^2 v_3 - 36\omega v_1 c_s^2 \\
C_{16} &= -14\omega^2 v_2^2 c_s^2 - 14\omega^2 v_1^2 v_2^2 + 36\omega v_1^2 c_s^2 - 24v_1^2 v_2^2 - 24v_2^2 c_s^2 - 72\omega v_1 v_3 c_s^2 - 72\omega v_1 v_2^2 v_3 + \omega^3 v_1^2 c_s^2 - 2\omega^3 v_1 v_2^2 v_3 + 48v_1 v_2^2 v_3 + \omega^3 v_1^2 v_2^2 + \\
& 48v_1 v_3 c_s^2 - 2\omega^3 v_1 v_3 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 + 28\omega^2 v_1 v_3 c_s^2 - 14\omega^2 v_1^2 c_s^2 + 36\omega v_1^2 v_2^2 - 24v_1^2 c_s^2 + 28\omega^2 v_1 v_2^2 v_3 \\
C_{17} &= 24 + \omega^3 v_2^2 - 72c_s^2 - 36\omega - 14\omega^2 v_2^2 + 108\omega c_s^2 - 46\omega^2 c_s^2 - \omega^3 + 36\omega v_2^2 + 14\omega^2 + 5\omega^3 c_s^2 - 24v_2^2 \\
C_{18} &= 24 - 72c_s^2 - 36\omega + \omega^3 v_3^2 + 108\omega c_s^2 - 14\omega^2 v_3^2 + 36\omega v_3^2 - 42\omega^2 c_s^2 - \omega^3 + 14\omega^2 - 24v_3^2 + 3\omega^3 c_s^2 \\
C_{19} &= -3\omega^3 c_s^4 - 72v_2^4 - 24c_s^2 - 3\omega^3 v_3^2 - 84\omega^2 v_3^2 c_s^2 + 108\omega v_3^4 + 30\omega^2 c_s^4 + 36\omega c_s^2 + 42\omega^2 v_3^2 - 144v_3^2 c_s^2 - 108\omega v_3^2 - 14\omega^2 c_s^2 + 216\omega v_3^2 c_s^2 - \\
& 72\omega c_s^4 - 42\omega^2 v_3^4 + 72v_3^2 + \omega^2 c_s^2 + 3\omega^3 v_3^4 + 6\omega^3 v_3^2 c_s^2 + 48c_s^4
\end{aligned}$$

2.1.5 Conservation of momentum: ρv_3

$$\begin{aligned}
& v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{\delta_1 v_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 \rho v_3}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_1 \rho v_1}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{\delta_1 v_2 v_3}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_1 \rho v_3}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_1 \rho v_2}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\
& \frac{2\delta_1 \rho v_3}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_2} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (-2 + 4c_s^2 + \omega - 2\omega c_s^2 - 3\omega v_3^2 + 6v_3^2) \frac{\delta_1^2}{\omega \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega) \frac{3\delta_1^2 \rho v_3}{\omega \delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega) \frac{\delta_1^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\
& (-2 + \omega) \frac{\delta_1^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega) \frac{\delta_1^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega) \frac{\delta_1^2 \rho c_s^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (-2 + 6c_s^2 + \omega - 3\omega c_s^2 - \omega v_3^2 + 2v_3^2) \frac{\delta_1^2 v_3}{2\omega \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} \\
& + (-2 + 2c_s^2 + \omega - \omega c_s^2 - 3\omega v_3^2 + 6v_3^2) \frac{\delta_1^2 \rho}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + (-1 + v_1^2 + 3c_s^2) \frac{\delta_1^3 v_1 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{\delta_1^3 \rho v_3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (6 - 6v_1^2 - 18c_s^2 - 6\omega + 6\omega v_1^2 + 18\omega c_s^2 - 3\omega^2 c_s^2 - \omega^2 v_1^2 + \omega^2) \frac{\delta_1^3 \rho v_1}{6\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{\delta_1^3 \rho v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\delta_1^3 \rho v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-1 + 3c_s^2 + v_2^2) \frac{\delta_1^3 v_2 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\delta_1^3 \rho v_3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (6 - 18c_s^2 - 6\omega - \omega^2 v_2^2 + 18\omega c_s^2 - 3\omega^2 c_s^2 + 6\omega v_2^2 + \omega^2 - 6v_2^2) \frac{\delta_1^3 \rho v_2}{6\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega - \omega^2) \frac{\delta_1^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\
& \frac{\delta_1^3 \rho v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 + 12\omega - \omega^2) \frac{\delta_1^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{\delta_1^3 \rho v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (12 - 36c_s^2 - 12\omega + 36\omega c_s^2 - 3\omega^2 v_3^2 + 12\omega v_3^2 - 11\omega^2 c_s^2 + 3\omega^2 - 12v_3^2) \frac{\delta_1^3 \rho v_3}{12\omega^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
& (12 - 36c_s^2 - 12\omega + 36\omega c_s^2 - 3\omega^2 v_3^2 + 12\omega v_3^2 - 11\omega^2 c_s^2 + 3\omega^2 - 12v_3^2) \frac{\delta_1^3 \rho v_3}{12\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_1 \frac{\delta_1^3}{12\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-24 + 36c_s^2 + 24\omega - 36\omega c_s^2 + 11\omega^2 v_3^2 - 60\omega v_3^2 + 5\omega^2 c_s^2 - 4\omega^2 + 60v_3^2) \frac{\delta_1^3 \rho v_3}{6\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} +
\end{aligned}$$

$$\begin{aligned}
& (-6v_1^2 - 12\omega v_1^2 c_s^2 - 2c_s^2 + 3\omega v_1^2 + \omega c_s^2 - 3\omega v_1^4 - \omega c_s^4 + 6v_1^4 + 24v_1^2 c_s^2 + 2c_s^4) \frac{\delta_l^4 v_3}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 10v_1^2 + 6c_s^2 + 2\omega - 5\omega v_1^2 - 3\omega c_s^2) \frac{\delta_l^4 \rho v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_2 \frac{\delta_l^4 \rho}{24\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + \\
& (2 - 2v_1^2 - 6c_s^2 - \omega + \omega v_1^2 + 3\omega c_s^2) \frac{\delta_l^4 \rho v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega) \frac{\delta_l^4 v_3 c_s^4}{6\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + (-2 + 3\omega - \omega^2) \frac{\delta_l^4 \rho c_s^4}{\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_2^2 - 2v_2^2) \frac{\delta_l^4 \rho v_2 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-2c_s^2 + 6v_2^4 + 24v_2^2 c_s^2 + \omega c_s^2 - 3\omega v_2^2 + 3\omega v_2^4 - \omega c_s^4 - 12\omega v_2^2 c_s^2 - 6v_2^2 + 2c_s^4) \frac{\delta_l^4 v_3}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 2\omega - 3\omega c_s^2 - 5\omega v_2^2 + 10v_2^2) \frac{\delta_l^4 \rho v_2 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_3 \frac{\delta_l^4 \rho}{24\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^4} + C_4 \frac{\delta_l^4 v_1 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& (-12 + 36v_1^2 + 18\omega - 54\omega v_1^2 + 2\omega^2 c_s^2 + 18\omega^2 v_1^2 - 6\omega^2 - \omega^3 c_s^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& (2 - 2v_1^2 - 6c_s^2 - \omega + \omega v_1^2 + 3\omega c_s^2) \frac{\delta_l^4 \rho v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_5 \frac{\delta_l^4 \rho}{2\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_6 \frac{\delta_l^4 \rho}{2\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_7 \frac{\delta_l^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_8 \frac{\delta_l^4 \rho v_3}{\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_9 \frac{\delta_l^4 \rho}{2\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{10} \frac{\delta_l^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{11} \frac{\delta_l^4 \rho v_2}{\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{12} \frac{\delta_l^4 \rho}{2\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{13} \frac{\delta_l^4 v_2 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + (-12 + 18\omega + 18\omega^2 v_2^2 + 2\omega^2 c_s^2 - 54\omega v_2^2 - 6\omega^2 - \omega^3 c_s^2 + 36v_2^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_3} + \\
& (2 - 6c_s^2 - \omega + 3\omega c_s^2 + \omega v_2^2 - 2v_2^2) \frac{\delta_l^4 \rho v_2 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{14} \frac{\delta_l^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& (-24 + 12c_s^2 + 36\omega - 18\omega c_s^2 + 36\omega^2 v_3^2 - 108\omega v_3^2 + 8\omega^2 c_s^2 - 12\omega^2 + 72v_3^2 - \omega^3 c_s^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{15} \frac{\delta_l^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& (-24 + 12c_s^2 + 36\omega - 18\omega c_s^2 + 36\omega^2 v_3^2 - 108\omega v_3^2 + 8\omega^2 c_s^2 - 12\omega^2 + 72v_3^2 - \omega^3 c_s^2) \frac{\delta_l^4 \rho c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{16} \frac{\delta_l^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{17} \frac{\delta_l^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^3} + C_{18} \frac{\delta_l^4 v_3}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3} + C_{19} \frac{\delta_l^4 \rho}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 36v_3^4 - 12c_s^2 + 24\omega^2 v_3^2 c_s^2 - 36\omega v_3^4 + \omega^2 c_s^4 + 12\omega c_s^2 - 7\omega^2 v_3^2 + 144v_3^2 c_s^2 + 36\omega v_3^2 - \omega^2 c_s^2 - 144\omega v_3^2 c_s^2 - 12\omega c_s^4 + 7\omega^2 v_3^4 - 36v_3^2 + 12c_s^4 \\
C_2 &= 72v_1^2 - 3\omega^3 c_s^4 + 216\omega v_1^2 c_s^2 - 24c_s^2 + 3\omega^3 v_1^4 - 108\omega v_1^2 + 30\omega^2 c_s^4 + 36\omega c_s^2 + 6\omega^3 v_1^2 c_s^2 - 42\omega^2 v_1^4 - 14\omega^2 c_s^2 + 108\omega v_1^4 + 42\omega^2 v_1^2 - 72\omega c_s^4 - 84\omega^2 v_1^2 c_s^2 - 72v_1^4 + \omega^3 c_s^2 - 144v_1^2 c_s^2 + 48c_s^4 - 3\omega^3 v_1^2 \\
C_3 &= -3\omega^3 c_s^4 - 84\omega^2 v_2^2 c_s^2 - 3\omega^3 v_2^2 - 24c_s^2 - 72v_2^4 - 144\omega v_2^2 c_s^2 + 42\omega^2 v_2^2 + 30\omega^2 c_s^4 + 36\omega c_s^2 + 108\omega v_2^4 - 14\omega^2 c_s^2 - 42\omega^2 v_2^4 - 108\omega v_2^2 - 72\omega c_s^4 + 6\omega^3 v_2^2 c_s^2 + 216\omega v_2^2 c_s^2 + 3\omega^3 v_2^4 + \omega^3 c_s^2 + 72v_2^2 + 48c_s^4 \\
C_4 &= 24 - 24v_1^2 - 72c_s^2 - 36\omega + 36\omega v_1^2 + 108\omega c_s^2 - 42\omega^2 c_s^2 - \omega^3 - 14\omega^2 v_1^2 + 14\omega^2 + 3\omega^3 c_s^2 + \omega^3 v_1^2 \\
C_5 &= -36\omega v_2^2 v_3^2 c_s^2 + \omega^3 v_1 v_2^2 c_s^2 - 24v_1 v_2^2 c_s^2 + 36\omega v_1 v_2^2 v_3^2 + 24v_1^2 v_2^2 c_s^2 - 14\omega^2 v_1 v_2^2 c_s^2 - \omega^3 v_1^2 v_2^2 c_s^2 - 36\omega v_1^2 v_2^2 v_3^2 + 14\omega^2 v_1^2 v_2^2 c_s^2 - 24v_1 v_2^2 c_s^2 + \omega^3 v_1 v_2^2 c_s^2 - 14\omega^2 v_1 v_2^2 c_s^2 - 14\omega^2 v_1 v_2^2 v_3^2 + 14\omega^2 v_2^2 v_3^2 c_s^2 + 14\omega^2 v_1^2 v_2^2 v_3^2 + 36\omega v_1 v_2^2 c_s^2 + 24v_1^2 v_2^2 v_3^2 - \omega^3 v_1^2 v_2^2 v_3^2 - 36\omega v_1^2 v_2^2 c_s^2 + \omega^3 v_1 v_2^2 v_3^2 - 24v_1 v_2^2 v_3^2 - \omega^3 v_2^2 v_3^2 c_s^2 + 36\omega v_1 v_2^2 c_s^2 + 24v_2^2 v_3^2 c_s^2 \\
C_6 &= -2\omega^3 v_1 v_2 v_3^2 + 48v_1 v_2 v_3^2 - 14\omega^2 v_2^2 c_s^2 - 72\omega v_1 v_2 c_s^2 + 36\omega v_2^2 v_3^2 - 24v_2^2 c_s^2 - 14\omega^2 v_3^2 c_s^2 + \omega^3 v_2^2 v_3^2 + 28\omega^2 v_1 v_2 v_3^2 - 24v_3^2 c_s^2 + 36\omega v_3^2 c_s^2 + 28\omega^2 v_1 v_2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 24v_2^2 v_3^2 - 2\omega^3 v_1 v_2 c_s^2 + 48v_1 v_2 c_s^2 - 14\omega^2 v_2^2 v_3^2 + \omega^3 v_3^2 c_s^2 - 72\omega v_1 v_2 v_3^2 \\
C_7 &= 12\omega^3 v_1 v_2 v_3^2 + 144v_1^2 v_3^2 - \omega^3 c_s^4 - 288v_1 v_2 v_3^2 + 432\omega v_1 v_2 c_s^2 - 216\omega v_1^2 c_s^2 + 84\omega^2 v_1^2 v_3^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 - 6\omega^3 v_1^2 c_s^2 - 168\omega^2 v_1 v_2 v_3^2 + 144v_3^2 c_s^2 - 6\omega^3 v_1^2 v_3^2 - 216\omega v_3^2 c_s^2 - 168\omega^2 v_1 v_2 c_s^2 + 54\omega c_s^4 + 84\omega^2 v_1^2 c_s^2 + 12\omega^3 v_1 v_2 c_s^2 + 144v_1^2 c_s^2 - 288v_1 v_2 c_s^2 - 6\omega^3 v_3^2 c_s^2 - 36c_s^4 + 432\omega v_1 v_2 v_3^2 - 216\omega v_1^2 v_3^2 \\
C_8 &= -24v_1 c_s^2 - 36\omega v_2 c_s^2 - 14\omega^2 v_1 c_s^2 + 36\omega v_1 v_2^2 + \omega^3 v_1 v_2^2 + 24v_1^2 v_2 - \omega^3 v_2 c_s^2 + 14\omega^2 v_1^2 v_2 + \omega^3 v_1 c_s^2 - 36\omega v_1^2 v_2 - 24v_1 v_2^2 - \omega^3 v_1^2 v_2 + 24v_2 c_s^2 + 14\omega^2 v_2 c_s^2 - 14\omega^2 v_1 v_2^2 + 36\omega v_1 c_s^2 \\
C_9 &= -\omega^3 v_1 v_2^2 c_s^2 - 14\omega^2 v_1^2 v_3 c_s^2 + 24v_1 v_2^2 c_s^2 - 36\omega v_1 v_2^2 v_3^2 + 14\omega^2 v_1 v_2^2 c_s^2 + 36\omega v_2^2 v_3 c_s^2 - 14\omega^2 v_1^2 v_2^2 v_3 + 24v_1 v_2^2 c_s^2 - \omega^3 v_1 v_2^2 c_s^2 - 24v_1^2 v_2^2 v_3 + \omega^3 v_1^2 v_2^2 v_3 + \omega^3 v_1^2 v_3 c_s^2 - 24v_1^2 v_3 c_s^2 + 14\omega^2 v_1 v_2^2 c_s^2 + 14\omega^2 v_1 v_2^2 v_3^2 + 36\omega v_1^2 v_3 c_s^2 + 36\omega v_1^2 v_2^2 v_3 - 14\omega^2 v_2^2 v_3 c_s^2 - 36\omega v_1 v_2^2 c_s^2 - 24v_2^2 v_3 c_s^2 + \omega^3 v_2^2 v_3 c_s^2 - \omega^3 v_1 v_2^2 v_3^2 + 24v_1 v_2^2 v_3^2 - 36\omega v_1 v_2^2 c_s^2 \\
C_{10} &= -\omega^3 c_s^4 + 84\omega^2 v_2^2 c_s^2 - 216\omega v_2^2 v_3^2 + 144v_2^2 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 - 6\omega^3 v_2^2 v_3^2 + 432\omega v_1 v_3 c_s^2 + 432\omega v_1 v_2^2 v_3 + 144v_3^2 c_s^2 - 216\omega v_3^2 c_s^2 + 12\omega^3 v_1 v_2^2 v_3 - 288v_1 v_2^2 v_3 - 288v_1 v_3 c_s^2 + 12\omega^3 v_1 v_3 c_s^2 + 54\omega c_s^4 - 6\omega^3 v_2^2 c_s^2 - 216\omega v_2^2 c_s^2 - 168\omega^2 v_1 v_3 c_s^2 + 144v_2^2 v_3^2 + 84\omega^2 v_2^2 v_3^2 - 6\omega^3 v_3^2 c_s^2 - 36c_s^4 - 168\omega^2 v_1 v_2^2 v_3 \\
C_{11} &= 24v_1 c_s^2 + \omega^3 v_3 c_s^2 - 36\omega v_1 v_3^2 + 14\omega^2 v_1 c_s^2 - 14\omega^2 v_1^2 v_3 - \omega^3 v_1 v_3^2 + 36\omega v_3 c_s^2 - 24v_1^2 v_3 - \omega^3 v_1 c_s^2 + 36\omega v_1^2 v_3 - 24v_3 c_s^2 - 14\omega^2 v_3 c_s^2 + 14\omega^2 v_1 v_3^2 + 24v_1 v_3^2 + \omega^3 v_1^2 v_3 - 36\omega v_1 c_s^2 \\
C_{12} &= -14\omega^2 v_2^2 c_s^2 - 14\omega^2 v_1^2 v_2^2 + 36\omega v_1^2 c_s^2 - 24v_1^2 v_2^2 - 24v_2^2 c_s^2 - 72\omega v_1 v_3 c_s^2 - 72\omega v_1 v_2^2 v_3 + \omega^3 v_1^2 c_s^2 - 2\omega^3 v_1 v_2^2 v_3 + 48v_1 v_2^2 v_3 + \omega^3 v_1^2 v_2^2 + 48v_1 v_3 c_s^2 - 2\omega^3 v_1 v_3 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 + 28\omega^2 v_1 v_3 c_s^2 - 14\omega^2 v_1^2 c_s^2 + 36\omega v_1^2 v_2^2 - 24v_1^2 c_s^2 + 28\omega^2 v_1 v_2^2 v_3
\end{aligned}$$

$$\begin{aligned}
C_{13} &= 24 + \omega^3 v_2^2 - 72c_s^2 - 36\omega - 14\omega^2 v_2^2 + 108\omega c_s^2 - 42\omega^2 c_s^2 - \omega^3 + 36\omega v_2^2 + 14\omega^2 + 3\omega^3 c_s^2 - 24v_2^2 \\
C_{14} &= 24 - 72c_s^2 - 36\omega + \omega^3 v_3^2 + 108\omega c_s^2 - 14\omega^2 v_3^2 + 36\omega v_3^2 - 46\omega^2 c_s^2 - \omega^3 + 14\omega^2 - 24v_3^2 + 5\omega^3 c_s^2 \\
C_{15} &= 24 - 72c_s^2 - 36\omega + \omega^3 v_3^2 + 108\omega c_s^2 - 14\omega^2 v_3^2 + 36\omega v_3^2 - 46\omega^2 c_s^2 - \omega^3 + 14\omega^2 - 24v_3^2 + 5\omega^3 c_s^2 \\
C_{16} &= -\omega^3 c_s^4 - 36v_3^4 - 24c_s^2 - 4\omega^3 v_3^2 - 42\omega^2 v_3^2 c_s^2 + 54\omega v_3^4 + 20\omega^2 c_s^4 + 36\omega c_s^2 + 26\omega^2 v_3^2 - 36v_3^2 c_s^2 - 54\omega v_3^2 - 12\omega^2 c_s^2 + 54\omega v_3^2 c_s^2 - 54\omega c_s^4 - \\
&\quad 26\omega^2 v_3^4 + 36v_3^2 + 4\omega^3 v_3^4 + 12\omega^3 v_3^2 c_s^2 + 36c_s^4 \\
C_{17} &= -\omega^3 c_s^4 - 36v_3^4 - 24c_s^2 - 4\omega^3 v_3^2 - 42\omega^2 v_3^2 c_s^2 + 54\omega v_3^4 + 20\omega^2 c_s^4 + 36\omega c_s^2 + 26\omega^2 v_3^2 - 36v_3^2 c_s^2 - 54\omega v_3^2 - 12\omega^2 c_s^2 + 54\omega v_3^2 c_s^2 - 54\omega c_s^4 - \\
&\quad 26\omega^2 v_3^4 + 36v_3^2 + 4\omega^3 v_3^4 + 12\omega^3 v_3^2 c_s^2 + 36c_s^4 \\
C_{18} &= 12 - 5\omega^3 c_s^4 + 144v_3^4 - 132c_s^2 - 18\omega + 10\omega^3 v_3^2 + 404\omega^2 v_3^2 c_s^2 - 216\omega v_3^4 + 82\omega^2 c_s^4 + 198\omega c_s^2 - 98\omega^2 v_3^2 + 672v_3^2 c_s^2 + 234\omega v_3^2 - 78\omega^2 c_s^2 - \\
&\quad 1008\omega v_3^2 c_s^2 - \omega^3 - 216\omega c_s^4 + 90\omega^2 v_3^4 + 8\omega^2 - 156v_3^2 + 6\omega^3 c_s^2 - 9\omega^3 v_3^4 - 34\omega^3 v_3^2 c_s^2 + 144c_s^4 \\
C_{19} &= 12 - \omega^3 c_s^4 + 504v_3^4 - 36c_s^2 - 18\omega + 14\omega^3 v_3^2 + 252\omega^2 v_3^2 c_s^2 - 756\omega v_3^4 + 14\omega^2 c_s^4 + 54\omega c_s^2 - 154\omega^2 v_3^2 + 432v_3^2 c_s^2 + 378\omega v_3^2 - 22\omega^2 c_s^2 - \\
&\quad 648\omega v_3^2 c_s^2 - \omega^3 - 36\omega c_s^4 + 310\omega^2 v_3^4 + 8\omega^2 - 252v_3^2 + 2\omega^3 c_s^2 - 29\omega^3 v_3^4 - 18\omega^3 v_3^2 c_s^2 + 24c_s^4
\end{aligned}$$

2.2 MRT

2.2.1 Definitions

Collision operator \mathbf{C} :

$$\mathbf{C}(\mathbf{f}) = \mathbf{M}^{-1} \mathbf{S} \left(\mu^{(eq)} - \mathbf{M} \mathbf{f} \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \dots, \omega_{27}),$$

$$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2).$$

2.2.2 Conservation of mass: ρ

$$\begin{aligned}
&\frac{\partial \rho}{\partial t} + \frac{\delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{\delta_l^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
&(-1 + c_s^2 + 3v_1^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{\delta_l^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\
&\frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\
&+ (-12c_s^2 \omega_9 v_1^2 - 2c_s^2 + c_s^2 \omega_9 + 3\omega_9 v_1^2 + 6v_1^4 - 3\omega_9 v_1^4 + 24c_s^2 v_1^2 - 6v_1^2 - c_s^4 \omega_9 + 2c_s^4) \frac{\delta_l^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
&(-4 + 6c_s^2 - 3c_s^2 \omega_9 - 5\omega_9 v_1^2 + 10v_1^2 + 2\omega_9) \frac{\delta_l^4 \rho v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
&(-3c_s^2 \omega_9 - \omega_9 v_1^2 + \omega_{12} v_1^2 + 3c_s^2 \omega_{12} + \omega_9 - \omega_{12}) \frac{\delta_l^4 v_2 v_1}{4\omega_9 \omega_{12} \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
&(-c_s^2 \omega_9 - 3\omega_9 v_1^2 + 3\omega_{12} v_1^2 + c_s^2 \omega_{12} + \omega_9 - \omega_{12}) \frac{\delta_l^4 \rho v_2}{4\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + (3c_s^2 \omega_5 \omega_{12} - 6c_s^2 \omega_9 \omega_{12} + 3c_s^2 \omega_5 \omega_9 \omega_{12} - \omega_5 \omega_{12} + \\
&\omega_5 \omega_{12} v_1^2 + 3\omega_5 \omega_9 - 3\omega_5 \omega_9 v_1^2 - \omega_5 \omega_9 \omega_{12} + \omega_5 \omega_9 \omega_{12} v_1^2 - 3c_s^2 \omega_5 \omega_9) \frac{\delta_l^4 \rho v_1}{12\omega_5 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_5) \frac{c_s^4 \delta_l^4}{6\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
&(\omega_5 - \omega_{12}) \frac{c_s^2 \delta_l^4 \rho v_1}{2\omega_5 \omega_{12} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + (\omega_5 - \omega_{15}) \frac{c_s^2 \delta_l^4 \rho v_2}{2\omega_5 \omega_{15} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\
&(-3\omega_{10} c_s^2 + \omega_{10} + \omega_{15} v_2^2 + 3c_s^2 \omega_{15} - \omega_{15} - \omega_{10} v_2^2) \frac{\delta_l^4 v_2 v_1}{4\omega_{10} \omega_{15} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + (-3\omega_{10} \omega_5 v_2^2 - 6\omega_{10} c_s^2 \omega_{15} - \omega_{10} \omega_5 \omega_{15} - \\
&\omega_5 \omega_{15} + 3c_s^2 \omega_5 \omega_{15} - 3\omega_{10} c_s^2 \omega_5 + 3\omega_{10} c_s^2 \omega_5 \omega_{15} + 3\omega_{10} \omega_5 + \omega_{10} \omega_5 \omega_{15} v_2^2 + \omega_5 \omega_{15} v_2^2) \frac{\delta_l^4 \rho v_2}{12\omega_{10} \omega_5 \omega_{15} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
&(-\omega_{10} c_s^2 + \omega_{10} + 3\omega_{15} v_2^2 + c_s^2 \omega_{15} - \omega_{15} - 3\omega_{10} v_2^2) \frac{\delta_l^4 \rho v_1}{4\omega_{10} \omega_{15} \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + \\
&(\omega_{10} c_s^2 - 2c_s^2 + 6v_2^4 - 3\omega_{10} v_2^4 - 12\omega_{10} c_s^2 v_2^2 - 6v_2^2 + 24c_s^2 v_2^2 + 3\omega_{10} v_2^2 - \omega_{10} c_s^4 + 2c_s^4) \frac{\delta_l^4}{24\omega_{10} \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
&(-4 - 3\omega_{10} c_s^2 + 2\omega_{10} + 6c_s^2 + 10v_2^2 - 5\omega_{10} v_2^2) \frac{\delta_l^4 \rho v_2}{12\omega_{10} \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
&(-\omega_{13} - 3c_s^2 \omega_9 - \omega_9 v_1^2 + 3\omega_{13} c_s^2 + \omega_9 + \omega_{13} v_1^2) \frac{v_3 \delta_l^4 v_1}{4\omega_{13} \omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-\omega_{13} - c_s^2 \omega_9 - 3\omega_9 v_1^2 + \omega_{13} c_s^2 + \omega_9 + 3\omega_{13} v_1^2) \frac{v_3 \delta_l^4 \rho}{4\omega_{13} \omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + (3\omega_{13} c_s^2 \omega_6 + \omega_{13} \omega_6 v_1^2 - 3c_s^2 \omega_9 \omega_6 - 3\omega_9 \omega_6 v_1^2 + \\
& 3\omega_{13} c_s^2 \omega_9 \omega_6 + \omega_{13} \omega_9 \omega_6 v_1^2 + 3\omega_9 \omega_6 - \omega_{13} \omega_6 - \omega_{13} \omega_9 \omega_6 - 6\omega_{13} c_s^2 \omega_9) \frac{\delta_l^4 \rho v_1}{12\omega_{13} \omega_9 \omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-\omega_8 + \omega_5) \frac{v_3 c_s^2 \delta_l^4 \rho}{2\omega_8 \omega_5 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + (-\omega_8 + \omega_6) \frac{c_s^2 \delta_l^4 \rho v_2}{2\omega_8 \omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + (-\omega_8 + \omega_5) \frac{v_3 c_s^2 \delta_l^4 \rho}{2\omega_8 \omega_5 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (\omega_7 - \omega_8) \frac{c_s^2 \delta_l^4 \rho v_1}{2\omega_7 \omega_8 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (-3\omega_{10} c_s^2 + \omega_{10} - \omega_{10} v_2^2 + v_2^2 \omega_{16} + 3c_s^2 \omega_{16} - \omega_{16}) \frac{v_3 \delta_l^4 v_2}{4\omega_{10} \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + \\
& (-\omega_{10} c_s^2 + \omega_{10} - 3\omega_{10} v_2^2 + 3v_2^2 \omega_{16} + c_s^2 \omega_{16} - \omega_{16}) \frac{v_3 \delta_l^4 \rho}{4\omega_{10} \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + (3\omega_{10} \omega_7 + 3\omega_7 c_s^2 \omega_{16} + 3\omega_{10} \omega_7 c_s^2 \omega_{16} + \\
& \omega_7 v_2^2 \omega_{16} + \omega_{10} \omega_7 v_2^2 \omega_{16} - 3\omega_{10} \omega_7 c_s^2 - \omega_7 \omega_{16} - \omega_{10} \omega_7 \omega_{16} - 3\omega_{10} \omega_7 v_2^2 - 6\omega_{10} c_s^2 \omega_{16}) \frac{\delta_l^4 \rho v_2}{12\omega_{10} \omega_7 \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{c_s^4 \delta_l^4}{6\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-\omega_{13} + \omega_6) \frac{c_s^2 \delta_l^4 \rho v_1}{2\omega_{13} \omega_6 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + (-\omega_{18} + \omega_6) \frac{v_3 c_s^2 \delta_l^4 \rho}{2\omega_{18} \omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& (-\omega_8 + \omega_6) \frac{c_s^2 \delta_l^4 \rho v_2}{2\omega_8 \omega_6 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + (\omega_7 - \omega_8) \frac{c_s^2 \delta_l^4 \rho v_1}{2\omega_7 \omega_8 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + (-2 + \omega_7) \frac{c_s^4 \delta_l^4}{6\omega_7 \delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3^2} + (\omega_7 - \omega_{16}) \frac{c_s^2 \delta_l^4 \rho v_2}{2\omega_7 \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} \\
& + (\omega_7 - \omega_{19}) \frac{v_3 c_s^2 \delta_l^4 \rho}{2\omega_7 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + (3c_s^2 \omega_{18} - v_3^2 \omega_{11} + \omega_{11} - 3c_s^2 \omega_{11} - \omega_{18} + v_3^2 \omega_{18}) \frac{v_3 \delta_l^4 v_1}{4\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + \\
& (v_3^2 \omega_{11} \omega_{18} \omega_6 - 6c_s^2 \omega_{11} \omega_{18} - \omega_{11} \omega_{18} \omega_6 + 3c_s^2 \omega_{18} \omega_6 + 3c_s^2 \omega_{11} \omega_{18} \omega_6 - 3c_s^2 \omega_{11} \omega_6 + 3\omega_{11} \omega_6 + v_3^2 \omega_{18} \omega_6 - \omega_{18} \omega_6 - \\
& 3v_3^2 \omega_{11} \omega_6) \frac{v_3 \delta_l^4 \rho}{12\omega_{11} \omega_{18} \omega_6 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + (c_s^2 \omega_{18} - 3v_3^2 \omega_{11} + \omega_{11} - c_s^2 \omega_{11} - \omega_{18} + 3v_3^2 \omega_{18}) \frac{\delta_l^4 \rho v_1}{4\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (-v_3^2 \omega_{11} + \omega_{11} + v_3^2 \omega_{19} - 3c_s^2 \omega_{11} - \omega_{19} + 3c_s^2 \omega_{19}) \frac{v_3 \delta_l^4 v_2}{4\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + (3\omega_7 c_s^2 \omega_{19} + 3\omega_7 c_s^2 \omega_{11} \omega_{19} + \omega_7 v_3^2 \omega_{11} \omega_{19} - \\
& \omega_7 \omega_{11} \omega_{19} - 3\omega_7 c_s^2 \omega_{11} + \omega_7 v_3^2 \omega_{19} - \omega_7 \omega_{19} + 3\omega_7 \omega_{11} - 3\omega_7 v_3^2 \omega_{11} - 6c_s^2 \omega_{11} \omega_{19}) \frac{v_3 \delta_l^4 \rho}{12\omega_7 \omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-3v_3^2 \omega_{11} + \omega_{11} + 3v_3^2 \omega_{19} - c_s^2 \omega_{11} - \omega_{19} + c_s^2 \omega_{19}) \frac{\delta_l^4 \rho v_2}{4\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& (-c_s^4 \omega_{11} + 3v_3^2 \omega_{11} - 2c_s^2 - 6v_3^2 + c_s^2 \omega_{11} - 3v_3^4 \omega_{11} + 24v_3^2 c_s^2 + 6v_3^4 - 12v_3^2 c_s^2 \omega_{11} + 2c_s^4) \frac{\delta_l^4}{24\omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 - 5v_3^2 \omega_{11} + 6c_s^2 + 2\omega_{11} + 10v_3^2 - 3c_s^2 \omega_{11}) \frac{v_3 \delta_l^4 \rho}{12\omega_{11} \delta_t} \frac{\partial^4 v_3}{\partial x_3^3} = 0.
\end{aligned}$$

2.2.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\delta_l \rho v_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2 v_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho v_2}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\delta_l \rho v_1}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\delta_l \rho v_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + 4c_s^2 - 2c_s^2 \omega_9 - 3\omega_9 v_1^2 + 6v_1^2 + \omega_9) \frac{\delta_l^2}{\omega_9 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\delta_l^2 \rho v_1}{\omega_9 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{c_s^2 \delta_l^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{c_s^2 \delta_l^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + 6c_s^2 - 3c_s^2 \omega_9 - \omega_9 v_1^2 + 2v_1^2 + \omega_9) \frac{\delta_l^2 v_1}{2\omega_9 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + 2c_s^2 - c_s^2 \omega_9 - 3\omega_9 v_1^2 + 6v_1^2 + \omega_9) \frac{\delta_l^2 \rho}{2\omega_9 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{c_s^2 \delta_l^2 \rho}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{c_s^2 \delta_l^2 \rho}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega_9^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 - 4\omega_9^2 + 5c_s^2 \omega_9^2 + 36c_s^2 - 36c_s^2 \omega_9 - 60\omega_9 v_1^2 + 11\omega_9^2 v_1^2 + 60v_1^2 + 24\omega_9) \frac{\delta_l^3 \rho v_1}{6\omega_9^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{\delta_l^3 v_2 v_1}{\omega_5 \omega_9^2 \omega_{12} \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& C_3 \frac{\delta_l^3 \rho v_2}{\omega_5 \omega_9^2 \omega_{12} \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + C_4 \frac{\delta_l^3 \rho v_1}{12\omega_5^2 \omega_9^2 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + (-12 + 12\omega_5 - \omega_5^2) \frac{c_s^4 \delta_l^3}{6\omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (-12\omega_9 \omega_{12} - 12\omega_5 \omega_{12} - 12\omega_5^2 \omega_9 - \omega_5^2 \omega_9 \omega_{12} + 12\omega_5 \omega_9 + 12\omega_5^2 + 12\omega_5 \omega_9 \omega_{12}) \frac{c_s^2 \delta_l^3 \rho v_1}{6\omega_5^2 \omega_9 \omega_{12} \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (2\omega_5 - \omega_5^2 - 2\omega_{15} + \omega_5 \omega_{15}) \frac{c_s^2 \delta_l^3 \rho v_2}{\omega_5^2 \omega_{15} \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{\delta_l^3 v_2 v_1}{12\omega_{10} \omega_5 \omega_{15} \delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + C_6 \frac{\delta_l^3 \rho v_2}{6\omega_5^2 \omega_{15} \delta_t} \frac{\partial^3 v_1}{\partial x_2^2} + C_7 \frac{\delta_l^3 \rho v_1}{12\omega_{10} \omega_5 \omega_{15} \delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + \\
& C_8 \frac{v_3 \delta_l^3 v_1}{\omega_{13} \omega_9^2 \omega_6 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + C_9 \frac{v_3 \delta_l^3 \rho}{\omega_{13} \omega_9^2 \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + C_{10} \frac{\delta_l^3 \rho v_1}{12\omega_{13} \omega_9^2 \omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (-\omega_8 \omega_6 - \omega_8 \omega_5 + \omega_8 \omega_5 \omega_6 + \omega_5 \omega_6 - \omega_5^2 \omega_6 + \omega_5^2) \frac{v_3 c_s^2 \delta_l^3 \rho}{\omega_8 \omega_5^2 \omega_6 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-\omega_8 \omega_6 - \omega_5 \omega_6^2 - \omega_8 \omega_5 + \omega_8 \omega_5 \omega_6 + \omega_5 \omega_6 + \omega_6^2) \frac{c_s^2 \delta_l^3 \rho v_2}{\omega_8 \omega_5 \omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-\omega_8 \omega_6 - \omega_8 \omega_5 + \omega_8 \omega_5 \omega_6 + \omega_5 \omega_6 - \omega_5^2 \omega_6 + \omega_5^2) \frac{v_3 c_s^2 \delta_l^3 \rho}{\omega_8 \omega_5^2 \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_8 \omega_6 - 6\omega_8 \omega_5 + 6\omega_8 \omega_5 \omega_6 - 6\omega_7 \omega_5 \omega_6 - \omega_7 \omega_8 \omega_5 \omega_6 + 6\omega_7 \omega_5 + 6\omega_7 \omega_6) \frac{c_s^2 \delta_l^3 \rho v_1}{6\omega_7 \omega_8 \omega_5 \omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4 \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} +
\end{aligned}$$

$$\begin{aligned}
& (-12\omega_{13}\omega_9 - 12\omega_9\omega_6^2 + 12\omega_9\omega_6 - \omega_{13}\omega_9\omega_6^2 + 12\omega_6^2 - 12\omega_{13}\omega_6 + 12\omega_{13}\omega_9\omega_6) \frac{c_s^2 \delta_l^3 \rho v_1}{6\omega_{13}\omega_9\omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
& (-2\omega_{18} + 2\omega_6 - \omega_6^2 + \omega_{18}\omega_6) \frac{v_3 c_s^2 \delta_l^3 \rho}{\omega_{18}\omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + (-\omega_8\omega_6 - \omega_5\omega_6^2 - \omega_8\omega_5 + \omega_8\omega_5\omega_6 + \omega_5\omega_6 + \omega_6^2) \frac{c_s^2 \delta_l^3 \rho v_2}{\omega_8\omega_5\omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_2 \partial x_3^2} + \\
& (-6\omega_8\omega_6 - 6\omega_8\omega_5 + 6\omega_8\omega_5\omega_6 - 6\omega_7\omega_5\omega_6 - \omega_7\omega_8\omega_5\omega_6 + 6\omega_7\omega_5 + 6\omega_7\omega_6) \frac{c_s^2 \delta_l^3 \rho v_1}{6\omega_7\omega_8\omega_5\omega_6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& C_{11} \frac{v_3 \delta_l^3 v_1}{12\omega_{11}\omega_{18}\omega_6 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{v_3 \delta_l^3 \rho}{6\omega_{18}\omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + C_{13} \frac{\delta_l^3 \rho v_1}{12\omega_{11}\omega_{18}\omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{\delta_l^4 v_1}{12\omega_9^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\delta_l^4 \rho}{12\omega_9^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& C_{16} \frac{\delta_l^4 v_2}{4\omega_2^2 \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{17} \frac{\delta_l^4 \rho v_2 v_1}{4\omega_5^2 \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{18} \frac{\delta_l^4 \rho}{12\omega_5^3 \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{19} \frac{\delta_l^4 v_1}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2^2} + \\
& C_{20} \frac{\delta_l^4 \rho}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2^2} + C_{21} \frac{\delta_l^4 \rho v_2 v_1}{2\omega_{10} \omega_5^3 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2^2} + C_{22} \frac{\delta_l^4 v_2}{12\omega_{10}^2 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& C_{23} \frac{\delta_l^4 \rho v_2 v_1}{12\omega_{10}^2 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{24} \frac{\delta_l^4 \rho}{12\omega_{10}^2 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{25} \frac{\delta_l^4 v_1}{24\omega_{10}^2 \omega_5^3 \omega_{15}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{26} \frac{\delta_l^4 \rho}{24\omega_5^3 \omega_{15}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& C_{27} \frac{\delta_l^4 \rho v_2 v_1}{12\omega_{10}^2 \omega_5^3 \omega_{15}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_{28} \frac{v_3 \delta_l^4}{4\omega_{13} \omega_9^3 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{29} \frac{v_3 \delta_l^4 \rho v_1}{4\omega_{13} \omega_9^3 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{30} \frac{\delta_l^4 \rho}{12\omega_{13}^2 \omega_9^3 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_3^3} + \\
& C_{31} \frac{v_3 \delta_l^4 v_2 v_1}{\omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9^3 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_2 \partial x_3} + C_{32} \frac{v_3 \delta_l^4 \rho v_2}{\omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9^3 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_2 \partial x_3} + C_{33} \frac{v_3 \delta_l^4 \rho v_1}{2\omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^3 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{\delta_l^4 \rho v_2 v_1}{2\omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^3 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_2 \partial x_3} + C_{35} \frac{2v_3 c_s^2 \delta_l^4}{\omega_5^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{36} \frac{v_3 c_s^2 \delta_l^4 \rho v_1}{2\omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^3 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{37} \frac{v_3 c_s^2 \delta_l^4 \rho v_2}{\omega_{17} \omega_8^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{38} \frac{\delta_l^4 \rho}{12\omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 \omega_5^2 \omega_9^3 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{39} \frac{v_3 \delta_l^4 v_2 v_1}{4\omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 \omega_6^2 \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + \\
& + C_{40} \frac{v_3 \delta_l^4 \rho v_2}{2\omega_{17} \omega_8^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3} + C_{41} \frac{v_3 \delta_l^4 \rho v_1}{4\omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 \omega_6^2 \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{42} \frac{\delta_l^4 \rho v_2 v_1}{12\omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_{15}^2 \omega_6^2 \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{43} \frac{\delta_l^4 v_1}{12\omega_{13}^2 \omega_{18} \omega_3^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{44} \frac{\delta_l^4 \rho}{12\omega_{13}^2 \omega_{18} \omega_3^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{45} \frac{v_3 \delta_l^4 \rho v_1}{2\omega_{13}^2 \omega_{11} \omega_{18} \omega_3^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{46} \frac{\delta_l^4 \rho}{2\omega_{13} \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{47} \frac{\delta_l^4 \rho}{2\omega_{13}^2 \omega_7 \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{48} \frac{\delta_l^4 \rho}{12\omega_{13} \omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{49} \frac{v_3 \delta_l^4 \rho}{\omega_{13} \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{\delta_l^4 \rho}{12\omega_7^2 \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{51} \frac{\delta_l^4 \rho}{4\omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + \\
& C_{52} \frac{\delta_l^4 \rho v_2}{2\omega_{10} \omega_7^2 \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{\delta_l^4 \rho}{4\omega_7^2 \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{54} \frac{v_3 \delta_l^4}{12\omega_{13} \omega_{11}^2 \omega_{18}^2 \omega_9^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{v_3 \delta_l^4 \rho v_1}{12\omega_{13}^2 \omega_{11}^2 \omega_{18}^2 \omega_9^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{56} \frac{\delta_l^4 \rho}{12\omega_{13} \omega_{11}^2 \omega_{18}^2 \omega_9^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{57} \frac{v_3 \delta_l^4 v_2 v_1}{4\omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{58} \frac{v_3 \delta_l^4 \rho v_2}{2\omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} + C_{59} \frac{v_3 \delta_l^4 \rho v_1}{12\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2 \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{60} \frac{\delta_l^4 \rho v_2 v_1}{4\omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{\delta_l^4 v_1}{24\omega_{11}^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{62} \frac{\delta_l^4 \rho}{24\omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + C_{63} \frac{v_3 \delta_l^4 \rho v_1}{12\omega_{11}^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -c_s^2 \omega_9^2 - 144c_s^2 \omega_9 v_1^2 - 12c_s^2 + 12c_s^2 \omega_9 + 36\omega_9 v_1^2 + 36v_1^4 + 7\omega_9^2 v_1^4 + c_s^4 \omega_9^2 - 36\omega_9 v_1^4 - 7\omega_9^2 v_1^2 + 144c_s^2 v_1^2 - 36v_1^2 + 24c_s^2 \omega_9^2 v_1^2 - 12c_s^4 \omega_9 + 12c_s^4 \\
C_2 &= 3c_s^2 \omega_5 \omega_{12} + \omega_9 \omega_{12} v_1^2 + 3c_s^2 \omega_9 \omega_{12} + \omega_9^2 - 3c_s^2 \omega_9^2 + \omega_5 \omega_9^2 v_1^2 - \omega_9 \omega_{12} - 3c_s^2 \omega_5 \omega_9 \omega_{12} - \omega_5 \omega_{12} + \omega_5 \omega_{12} v_1^2 + \omega_5 \omega_9 + 3c_s^2 \omega_5 \omega_9^2 - \omega_5 \omega_9 v_1^2 - \\
&\omega_9^2 v_1^2 + \omega_5 \omega_9 \omega_{12} - \omega_5 \omega_9 \omega_{12} v_1^2 - \omega_5 \omega_9^2 - 3c_s^2 \omega_5 \omega_9 \\
C_3 &= c_s^2 \omega_5 \omega_{12} + 3\omega_9 \omega_{12} v_1^2 + c_s^2 \omega_9 \omega_{12} + \omega_9^2 - c_s^2 \omega_9^2 + 3\omega_5 \omega_9^2 v_1^2 - \omega_9 \omega_{12} - c_s^2 \omega_5 \omega_9 \omega_{12} - \omega_5 \omega_{12} + 3\omega_5 \omega_{12} v_1^2 + \omega_5 \omega_9 + c_s^2 \omega_5 \omega_9^2 - 3\omega_5 \omega_9 v_1^2 - \\
&3\omega_9^2 v_1^2 + \omega_5 \omega_9 \omega_{12} - 3\omega_5 \omega_9 \omega_{12} v_1^2 - \omega_5 \omega_9^2 - c_s^2 \omega_5 \omega_9 \\
C_4 &= 6\omega_5 \omega_9^2 \omega_{12} v_1^2 - 12\omega_5^2 \omega_9^2 - 12c_s^2 \omega_5^2 \omega_9 - 12\omega_5 \omega_9^2 v_1^2 - 6\omega_5^2 \omega_9 \omega_{12} v_1^2 - 24c_s^2 \omega_5 \omega_9 \omega_{12} - 6\omega_5 \omega_9^2 \omega_{12} - 12\omega_5^2 \omega_9 v_1^2 + 12\omega_5^2 \omega_9 + 12c_s^2 \omega_5^2 \omega_9^2 - \\
&11c_s^2 \omega_5^2 \omega_9^2 \omega_{12} + 6\omega_5^2 \omega_9 \omega_{12} - 12\omega_5^2 \omega_{12} - 12c_s^2 \omega_5 \omega_9^2 + 12\omega_5^2 \omega_9^2 v_1^2 - 18c_s^2 \omega_5^2 \omega_9 \omega_{12} + 3\omega_5^2 \omega_9^2 \omega_{12} - 3\omega_5^2 \omega_9^2 \omega_{12} v_1^2 + 12\omega_5^2 \omega_{12} v_1^2 + 42c_s^2 \omega_5 \omega_9^2 \omega_{12} - \\
&24c_s^2 \omega_9^2 \omega_{12} + 36c_s^2 \omega_5^2 \omega_{12} + 12\omega_5 \omega_9^2 \\
C_5 &= -36\omega_{10} c_s^2 + 12\omega_{10} + 12\omega_{15} v_2^2 + 6\omega_{10} \omega_5 v_2^2 + 36c_s^2 \omega_{15} - 12\omega_{15} - 12\omega_{10} v_2^2 - \omega_{10} \omega_5 \omega_{15} + 6\omega_5 \omega_{15} - 18c_s^2 \omega_5 \omega_{15} + 18\omega_{10} c_s^2 \omega_5 + \\
&3\omega_{10} c_s^2 \omega_5 \omega_{15} - 6\omega_{10} \omega_5 + \omega_{10} \omega_5 \omega_{15} v_2^2 - 6\omega_5 \omega_{15} v_2^2 \\
C_6 &= -3c_s^2 \omega_5^2 \omega_{15} - \omega_5^2 \omega_{15} v_2^2 - 6\omega_5 v_2^2 + \omega_5^2 \omega_{15} - 12c_s^2 \omega_{15} + 6\omega_5 + 3\omega_5^2 v_2^2 - 3\omega_5^2 + 3c_s^2 \omega_5^2 - 3\omega_5 \omega_{15} + 15c_s^2 \omega_5 \omega_{15} - 6c_s^2 \omega_5 + 3\omega_5 \omega_{15} v_2^2 \\
C_7 &= -12\omega_{10} c_s^2 + 12\omega_{10} + 36\omega_{15} v_2^2 + 18\omega_{10} \omega_5 v_2^2 + 12c_s^2 \omega_{15} - 12\omega_{15} - 36\omega_{10} v_2^2 - \omega_{10} \omega_5 \omega_{15} + 6\omega_5 \omega_{15} - 6c_s^2 \omega_5 \omega_{15} + 6\omega_{10} c_s^2 \omega_5 + \\
&\omega_{10} c_s^2 \omega_5 \omega_{15} - 6\omega_{10} \omega_5 + 3\omega_{10} \omega_5 \omega_{15} v_2^2 - 18\omega_5 \omega_{15} v_2^2 \\
C_8 &= 3\omega_{13} c_s^2 \omega_6 + \omega_{13} \omega_6 v_1^2 - \omega_{13} \omega_9 - 3c_s^2 \omega_9 \omega_6 - \omega_9 \omega_6 v_1^2 + \omega_9^2 - 3c_s^2 \omega_9^2 - 3\omega_{13} c_s^2 \omega_9 \omega_6 - \omega_{13} \omega_9 \omega_6 v_1^2 + \omega_9 \omega_6 - \omega_9^2 \omega_6 - \omega_9^2 v_1^2 + 3c_s^2 \omega_9^2 \omega_6 - \\
&\omega_{13} \omega_6 + \omega_{13} \omega_9 v_1^2 + \omega_{13} \omega_9 \omega_6 + \omega_9^2 \omega_6 v_1^2 + 3\omega_{13} c_s^2 \omega_9
\end{aligned}$$

$$\begin{aligned}
C_{44} = & -132w_{13}c_s^2w_{18}w_6^2w_{22}v_1^2 - 12w_{13}c_s^2w_{18}w_6^2w_{22} + 84w_{13}c_s^2w_{18}w_6^2w_{22}v_1^2 + 36w_{13}v_3^2w_6^2w_{22}^2 - 36w_{13}c_s^2w_{18}w_6^2w_{22}v_1 + \\
& 6w_{13}c_s^4w_{18}w_6^2w_{22} - 36w_{13}v_3^2w_{18}w_6^2w_{22}v_1 + 18w_{13}v_3^2w_6^2w_{22}^2 - 18w_{13}c_s^4w_{18}w_6^2w_{22}v_1 + 72w_{13}v_3^2w_{18}w_6^2w_{22}v_1 - \\
& 24w_{13}v_3^2c_s^2w_{18}w_6^2w_{22} - 12w_{13}c_s^2w_6^2w_{22}^2 - 36w_{13}v_3^2w_{18}w_6^2w_{22}v_1 + 12w_{13}c_s^4w_{18}w_6^2w_{22} + 12w_{13}c_s^2w_6^2w_{22}^2 - 18w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - \\
& 12w_{13}c_s^4w_{18}w_6^2w_{22} + 24w_{13}v_3^2c_s^4w_{18}w_6^2w_{22} - 6w_{13}c_s^4w_{18}w_6^2w_{22} + 18w_{13}^3v_3^2w_{18}w_6^2w_{22} + 12v_3^2c_s^2w_{18}w_6^2w_{22} + 6w_{13}c_s^2w_{18}w_6^2w_{22} - \\
& 4w_{13}^3c_s^4w_{18}w_6^2w_{22} - 36v_3^2w_{18}w_6^2w_{22}^2 + 18w_{13}^3c_s^2w_6^2w_{22}^2 - 36w_{13}^3v_3^2w_{18}w_6^2w_{22} - 36w_{13}c_s^2w_{18}w_6^2w_{22}v_1 - 36w_{13}v_3^2w_{18}w_6^2w_{22}v_1 + \\
& 6w_{13}c_s^2w_6^2w_{22}^2 + 12w_{13}v_3^2w_{18}w_6^2w_{22} - 24c_s^2w_{18}w_6^2w_{22}^2 - 108w_{13}c_s^2w_{18}w_6^2w_{22}v_1 + 12w_{13}c_s^4w_{18}w_6^2w_{22} + 72w_{13}c_s^2w_{18}w_6^2w_{22}v_1 + \\
& 12w_{13}v_3^2c_s^2w_{18}w_6^2w_{22} - 6w_{13}^3c_s^2w_6^2w_{22}^2 + 36w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 - 12w_{13}v_3^2c_s^2w_{18}w_6^2w_{22} + 12w_{13}^3c_s^2w_{18}w_6^2w_{22} + 36v_3^2w_{18}w_6^2w_{22}^2 + \\
& 12w_{13}^3v_3^2w_{18}w_6^2w_{22} - 24w_{13}c_s^4w_{18}w_6^2w_{22} + 12v_3^2w_{18}w_6^2w_{22}^2 + 24c_s^2w_{18}w_6^2w_{22}v_1 + 36w_{13}v_3^2w_{18}w_6^2w_{22}v_1 - 24w_{13}^3v_3^2w_{18}w_6^2w_{22} + \\
& 12w_{13}^3c_s^4w_6^2w_{22}^2 + 18w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 - 12w_{13}^3c_s^4w_{18}w_6^2w_{22} + 12w_{13}^3v_3^2c_s^2w_6^2w_{22}^2 - 12w_{13}^3v_3^2w_6^2w_{22}^2 + 24w_{13}c_s^2w_{18}w_6^2w_{22} - 18w_{13}^3v_3^2w_6^2w_{22}^2 + \\
& 12w_{13}^3c_s^2w_{18}w_6^2w_{22} + 36w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 - 36w_{13}^3v_3^2w_{18}w_6^2w_{22} + 24w_{13}v_3^2c_s^2w_{18}w_6^2w_{22} + 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - 84w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 + \\
& 18w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 - 12w_{13}c_s^2w_{18}w_6^2w_{22} + 60w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 + 36w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22}v_1 + 18w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 + 12w_{13}^3c_s^2w_{18}w_6^2w_{22} - \\
& w_{13}c_s^4w_{18}w_6^2w_{22} - 6w_{13}^3c_s^2w_{18}w_6^2w_{22} + 6w_{13}^3v_3^2w_6^2w_{22}^2 - 12w_{13}^3v_3^2w_{18}w_6^2w_{22} - 12v_3^2c_s^2w_{18}w_6^2w_{22} - 12w_{13}^3v_3^2w_{18}w_6^2w_{22} - 12w_{13}^3c_s^4w_{18}w_6^2w_{22} - \\
& 6w_{13}^3v_3^2c_s^2w_6^2w_{22}^2 + 108w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 - 6w_{13}^3c_s^4w_6^2w_{22}^2 + 36w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 + 24w_{13}^3v_3^2w_{18}w_6^2w_{22} - 36w_{13}^3c_s^2w_6^2w_{22}^2v_1 - 12w_{13}^3v_3^2w_{18}w_6^2w_{22} + \\
& 12w_{13}^3v_3^2w_6^2w_{22}^2 - 24w_{13}^3c_s^2w_{18}w_6^2w_{22} + 18w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 - 24w_{13}^3v_3^2w_{18}w_6^2w_{22} + 24c_s^2w_{18}w_6^2w_{22}v_1 - 24w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} + \\
& 12w_{13}^3c_s^4w_{18}w_6^2w_{22} - 12w_{13}^3c_s^2w_6^2w_{22}^2 - 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - 12v_3^2c_s^2w_{18}w_6^2w_{22} - 48w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 + 36w_{13}^3c_s^2w_6^2w_{22}^2v_1 - \\
& 12w_{13}^3c_s^4w_{18}w_6^2w_{22} - 12w_{13}^3v_3^2c_s^2w_6^2w_{22}^2 + 24w_{13}^3c_s^4w_{18}w_6^2w_{22} + 72w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 - 12w_{13}^3c_s^4w_{18}w_6^2w_{22} + 12v_3^2w_{18}w_6^2w_{22} - \\
& 6w_{13}^3c_s^2w_{18}w_6^2w_{22} + 180w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 - 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} + 12w_{13}^3c_s^4w_{18}w_6^2w_{22} - 6w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} + 24w_{13}^3v_3^2w_{18}w_6^2w_{22} + \\
& 78w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 + 6w_{13}^3v_3^2w_{18}w_6^2w_{22} - 72w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 + 12w_{13}^3c_s^2w_{18}w_6^2w_{22} + 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - 36w_{13}^3v_3^2w_6^2w_{22}^2v_1 - \\
& 12w_{13}^3c_s^2w_{18}w_6^2w_{22} + 36w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 + 6w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} + 12w_{13}^3v_3^2w_{18}w_6^2w_{22} - 18w_{13}^3c_s^2w_6^2w_{22}^2v_1 - 6w_{13}^3c_s^4w_{18}w_6^2w_{22} + 6w_{13}^3v_3^2c_s^4w_{18}w_6^2w_{22} - \\
& 12w_{13}^3c_s^4w_{18}w_6^2w_{22} - 42w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 + 60w_{13}^3c_s^4w_{18}w_6^2w_{22}v_1 - 36w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 + 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} + 18w_{13}^3c_s^4w_{18}w_6^2w_{22} + \\
& 12w_{13}^3v_3^2w_{18}w_6^2w_{22} + 6w_{13}^3c_s^2w_{18}w_6^2w_{22} - 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - 12w_{13}^3c_s^4w_{18}w_6^2w_{22} + 6w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - 18w_{13}^3v_3^2w_{18}w_6^2w_{22}v_1 - \\
& 144w_{13}^3c_s^2w_{18}w_6^2w_{22}v_1 - 12w_{13}^3v_3^2c_s^2w_{18}w_6^2w_{22} - 72w_{13}^$$

[illegible]

[illegible]

[illegible]

$$C_{49} = 2\omega_{13}c_w^2\omega_{20}\omega_{14}\omega_8^2\omega_9^2\omega_{12}\omega_6^2\omega_{22}v_2 + 2\omega_{13}\omega_{20}\omega_8^2\omega_5^2\omega_{18}\omega_9\omega_{12}\omega_6^2\omega_{22}v_2^2v_1 + \omega_{13}\omega_{14}\omega_4^2\omega_5^2\omega_{18}\omega_9\omega_{12}\omega_6^2\omega_{22}v_2^2v_1 + 2\omega_{13}c_w^2\omega_{20}\omega_8^2\omega_5^2\omega_{18}\omega_9\omega_{12}\omega_6^3\omega_{22}v_2 - \omega_{13}\omega_{20}\omega_{14}\omega_8^2\omega_5^2\omega_{18}\omega_9\omega_{12}\omega_6^3\omega_{22}v_2^2v_1 - 2\omega_{13}c_w^2\omega_{20}\omega_8^2\omega_5^2\omega_{18}\omega_6^3\omega_{22}v_2v_1 -$$

$$\begin{aligned}
& 8v_3w_{20}w_8^2w_5^2w_{18}w_{15}w_6^3v_2^2v_1 + 4c_s^2w_{20}w_{17}w_8w_5^2w_{18}w_{15}w_6^3v_2^2 - 4c_s^4w_{20}w_{17}w_8w_5^3w_{18}w_{15}w_6^3 + 4c_s^4w_{20}w_{17}w_8w_5^2w_{18}w_{15}w_6 - \\
& 4v_3w_{17}w_8^2w_5^2w_{18}w_{15}w_6^3v_2^2v_1 - 4v_3^2w_{20}w_{17}w_8w_5^2w_{18}w_{15}w_6^3v_2^2 + 4v_3c_s^2w_{17}w_8^2w_5^3w_{15}w_6^3v_1 - v_3^2w_{20}w_{17}w_8^2w_5^2w_{18}w_{15}w_6^3v_2^2 + \\
& 4v_3^2c_s^2w_{20}w_{17}w_5^3w_{18}w_{15}w_6^3 - 4v_3^2c_s^2w_{20}w_{17}w_8^2w_5^2w_{18}w_{15}w_6^3 - 2v_3c_s^2w_{20}w_{17}w_8^2w_5^3w_{15}w_6^3v_1 + 4c_s^2w_{20}w_{17}w_8w_5^2w_{18}w_{15}w_6^3v_2^2 + \\
& 2c_s^2w_{20}w_{17}w_8^2w_5^3w_{18}w_{15}w_6^3v_2^2 - 2c_s^2w_{20}w_{17}w_8^2w_5^2w_{15}w_6^3v_2^2 - 4v_3w_{20}w_{17}w_8^2w_5^2w_{18}w_{15}w_6^3v_2v_1 - 4v_3w_{20}w_{17}w_8^2w_5^3w_{18}w_{15}w_6^3v_2^2v_1 + \\
& 8c_3v_3^2w_{20}w_{17}w_8w_5^2w_{18}w_{15}w_6^3v_1 + 4v_3c_s^2w_{17}w_8^2w_5^2w_{18}w_{15}w_6^3v_1 + 4c_s^2w_{20}w_{17}w_8^2w_5^3w_{18}w_{15}w_6^3v_2^2 - 4v_3c_s^2w_{20}w_8^2w_5^3w_{18}w_{15}w_6^3v_1 + \\
& 4c_s^4w_{20}w_{17}w_8w_5^2w_{18}w_{15}w_6^3 + 4v_3w_{20}w_{17}w_8^2w_5^3w_{15}w_6^3v_2^2v_1 + 4v_3^2w_{20}w_8w_5^2w_{18}w_{15}w_6^3v_2^2 - 4v_3^2w_{17}w_8w_5^2w_{18}w_{15}w_6^3v_2^2 + v_3^2w_{20}w_{17}w_8^2w_5^3w_{18}w_6^3v_2^2
\end{aligned}$$

$$\begin{aligned}
C_{53} = & -2\omega_7^2 w_{17w11} \omega_5^2 w_{5w18} w_{15w6} \omega_6^2 w_{19v2} v_1^2 - 16\omega_7^2 v_3 c_2^2 w_{20w17w11} w_8 w_5 w_{18w15} \omega_5^2 w_{19v1} - 8\omega_7^2 v_3 c_2^2 w_{20w17w11} w_8 \omega_5^2 w_{18w15w6} w_{19v1} + \\
& 8\omega_7^2 v_3 c_2^2 w_{20w17w11} w_8 w_5^2 w_{18w15w6} w_{19v1} - 4\omega_7^2 v_3 w_{20w17w11} \omega_5^2 \omega_6^2 w_{15w6w19} v_1^2 v_1 - 4\omega_7^2 v_3 c_2^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{15w6w19} v_1 - \\
& 4\omega_7^2 c_s^2 w_{20w11} w_8 w_5 w_{18w15} \omega_6^2 w_{19v2}^2 + 6\omega_7^2 v_3 c_2^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} v_1^2 - 4\omega_7^2 w_{17w11} w_8 w_5^2 w_{18w15w6w19} v_1^2 + \\
& 8\omega_7^2 v_3 c_2^2 w_{20w17w11} \omega_5^2 w_5 w_{18w15} \omega_6^2 w_{19v1} - 4\omega_7^2 v_3 w_{20w17w11} \omega_5^2 \omega_6^2 w_{15w6w19} v_2^2 v_1 + 4\omega_7^2 c_s^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6w19} v_2^2 + \\
& 4\omega_7^2 c_s^2 w_{17w11} w_8 w_5^2 w_{18w15w6} w_{19v2}^2 - 2\omega_7^2 c_2^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 + 8\omega_7^2 v_3 w_{20w11} w_8 w_5 w_{18w15w6} w_{19v2}^2 v_1 - \\
& \omega_7^2 c_2^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 + 2\omega_7^2 c_s^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 + 2\omega_7^2 c_s^2 w_{17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 + \\
& 4\omega_7^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 - 4\omega_7^2 w_{17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 - 4\omega_7^2 w_{20w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 - \\
& 8\omega_7^2 v_3 w_{17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 + 2\omega_7^2 c_s^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 + 2\omega_7^2 c_s^2 w_{17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 - \\
& \omega_7^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 + 8\omega_7^2 v_3 c_2^2 w_{20w11} w_8 w_5^2 w_{18w15w6} w_{19v1} - 2\omega_7^2 c_s^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v1}^2 + \\
& 4\omega_7^2 c_s^2 w_{17w11} w_8 w_5^2 w_{18w15w6} w_{19v1}^2 + 2\omega_7^2 v_3 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v1}^2 v_1 - \omega_7^2 c_s^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v1}^2 - \\
& 8\omega_7^2 v_3 w_{17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v1}^2 v_1 - 4\omega_7^2 w_{20w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v1}^2 v_1 + 4\omega_7^2 c_s^2 w_{17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v1}^2 - \\
& 4\omega_7^2 c_s^2 w_{20w11} w_8 w_5 w_{18w15w6} w_{19v1}^2 + 8\omega_7^2 v_3 w_{20w17w11} w_8 w_5^2 w_{18w15w6} w_{19v2}^2 v_1 + 4\omega_7^2 v_3 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 - \\
& 4\omega_7^2 v_3 c_2^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 + 4\omega_7^2 w_{20w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 + \omega_7^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1^2 + \\
& 8\omega_7^2 v_3 w_{20w11} w_8 w_5^2 w_{18w15w6} w_{19v2}^2 v_1 - 8\omega_7^2 v_3 c_2^2 w_{20w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 + 4\omega_7^2 c_s^2 w_{20w17w11} w_8 w_5^2 w_{18w15w6} w_{19v2}^2 v_1 + \\
& 4\omega_7^2 v_3 w_{20w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 + 2\omega_7^2 w_{20w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 v_1 - \omega_7^2 c_s^2 w_{20w17w11} \omega_5^2 \omega_6^2 w_{18w15w6} w_{19v2}^2 -
\end{aligned}$$

$$\begin{aligned}
& 4\omega_7 c_s^2 \omega_{11}^2 \omega_{18}^2 \omega_{19}^2 - 6\omega_7 v_3^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6^2 \omega_{19}^2 + 2\omega_7 \omega_{11}^2 \omega_8 \omega_{18}^2 \omega_6^2 \omega_{19}^2 - 3\omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6^2 \omega_{19}^2 - 2\omega_7 c_s^2 \omega_{20} \omega_8 \omega_5 \omega_{18} \omega_6^2 \omega_{19}^2 + \\
& 8\omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} - 6\omega_7 v_3^2 \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6^2 \omega_{19} + 2\omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18} \omega_6^2 \omega_{19} - 4\omega_{20} \omega_{11} \omega_8 \omega_{18}^2 \omega_6^2 \omega_{19} + 4\omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6 - \\
& 4\omega_7 \omega_{20} \omega_{11} \omega_8 \omega_{18} \omega_6 \omega_{19} - 3\omega_7 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} - 6\omega_7 v_3^2 \omega_{20} \omega_{11} \omega_8 \omega_{18} \omega_6^2 \omega_{19} + 2\omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_6^2 \omega_{19} - 12\omega_7 v_3^2 \omega_{20} \omega_{11} \omega_{18}^2 \omega_6^2 \omega_{19} - \\
& 4\omega_7 \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} + 4\omega_7 c_s^2 \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} - 12\omega_7 v_3^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18} \omega_6 \omega_{19} - 2\omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_6^2 \omega_{19} - 4\omega_7 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18}^2 \omega_6 - \\
& 12\omega_7 v_3^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_6 \omega_{19} + 4\omega_7 c_s^2 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} - 2\omega_7 \omega_{20} \omega_{11} \omega_8 \omega_{18} \omega_6^2 \omega_{19} - 12v_3^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}^2 \omega_6^2 - 2\omega_7 \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} - \\
& 12\omega_7 v_3^2 \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6 \omega_{19} + 4\omega_7 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18} \omega_6 - 4\omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} + 4\omega_7 c_s^2 \omega_{20} \omega_{11} \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} - 4\omega_7 c_s^2 \omega_{11}^2 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} + \\
& 3\omega_7 c_s^2 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} - 12v_3^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6 - 2\omega_7 \omega_{20} \omega_{11} \omega_8 \omega_{18} \omega_6^2 - 4\omega_7 \omega_{20} \omega_{11} \omega_5 \omega_{18}^2 \omega_6 \omega_{19} - 4\omega_7 c_s^2 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18} \omega_6 - \\
& 24\omega_7 v_3^2 \omega_{20} \omega_{11} \omega_8 \omega_5 \omega_{18}^2 \omega_6 \omega_{19} - 12\omega_7 v_3^2 \omega_{20} \omega_{11} \omega_5 \omega_{18}^2 \omega_6 \omega_{19} + 2\omega_7 c_s^2 \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6^2 \omega_{19} + 4c_s^2 \omega_{20} \omega_{11} \omega_8 \omega_{18} \omega_6^2 \omega_{19}
\end{aligned}$$

$$\begin{aligned}
C_{61} = & 72v_3^2 c_s^2 \omega_{11} \omega_{18} \omega_6^2 + 36v_3^4 \omega_{11} \omega_{18}^2 \omega_6^2 + 24v_3^2 \omega_{11}^2 \omega_6 - 14c_s^2 \omega_{11} \omega_{18}^2 \omega_6^2 + 216v_3^2 c_s^2 \omega_{11} \omega_{18}^2 + 12c_s^2 \omega_{18}^2 \omega_6^2 + 48v_3^2 \omega_{11} \omega_{18} \omega_6 - 24c_s^4 \omega_{11}^2 \omega_6 - \\
& 36v_3^4 \omega_{18}^2 \omega_6^2 + 288v_3^2 c_s^2 \omega_{18}^2 \omega_6 + 24c_s^4 \omega_{18}^2 \omega_6 - 48v_3^2 \omega_{11} \omega_{18}^2 + 12v_3^4 \omega_{11}^2 \omega_6^2 - 144v_3^2 c_s^2 \omega_{11}^2 \omega_6 + 24c_s^4 \omega_{11} \omega_{18}^2 - 72v_3^2 \omega_{18}^2 \omega_6 - 12c_s^2 \omega_{11}^2 \omega_6^2 - 30v_3^4 \omega_{11}^2 \omega_{18} \omega_6^2 - \\
& 12v_3^2 c_s^2 \omega_{11}^2 \omega_{18} \omega_6^2 + 12c_s^2 \omega_{11}^2 \omega_{18} \omega_6^2 + 3v_3^2 \omega_{11}^2 \omega_{18}^2 \omega_6^2 - 48c_s^2 \omega_{11}^2 \omega_{18} \omega_6^2 - 12c_s^4 \omega_{18}^2 \omega_6^2 + 72v_3^2 c_s^2 \omega_{11}^2 \omega_6^2 - 24v_3^4 \omega_{11}^2 \omega_6 - c_s^4 \omega_{11}^2 \omega_{18}^2 \omega_6^2 + 36v_3^2 \omega_{18}^2 \omega_6^2 + \\
& 96v_3^4 \omega_{11}^2 \omega_{18} \omega_6 + 24c_s^2 \omega_{11}^2 \omega_6 + 48c_s^2 \omega_{11} \omega_{18} \omega_6 - 12v_3^2 \omega_{11}^2 \omega_6^2 + 48v_3^4 \omega_{11} \omega_{18}^2 - 24c_s^2 \omega_{18} \omega_6^2 - 24v_3^2 \omega_{11} \omega_{18} \omega_6^2 + 12c_s^4 \omega_{11}^2 \omega_6^2 - 144v_3^2 c_s^2 \omega_{18}^2 \omega_6^2 + \\
& 72v_3^4 \omega_{18} \omega_6 - 24c_s^2 \omega_{11} \omega_{18}^2 - 144v_3^2 c_s^2 \omega_{11} \omega_{18} \omega_6 - 96v_3^4 \omega_{11} \omega_{18} \omega_6 - 216v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 36v_3^2 \omega_{11} \omega_{18}^2 \omega_6 - 48v_3^4 \omega_{11} \omega_{18} \omega_6 - 432v_3^2 c_s^2 \omega_{11} \omega_{18} \omega_6 + \\
& 14c_s^4 \omega_{11} \omega_{18} \omega_6^2 + 30v_3^2 \omega_{11} \omega_{18} \omega_6^2 - 12c_s^4 \omega_{11}^2 \omega_{18} \omega_6^2 + 48v_3^2 \omega_{11} \omega_{18} + 432v_3^2 c_s^2 \omega_{11}^2 \omega_{18} \omega_6 - 24c_s^4 \omega_{11}^2 \omega_{18} + 48c_s^4 \omega_{11}^2 \omega_{18} \omega_6 - 126v_3^2 c_s^2 \omega_{11}^2 \omega_{18} \omega_6^2 - \\
& 3v_3^4 \omega_{11}^2 \omega_{18} \omega_6^2 - 96v_3^2 \omega_{11} \omega_{18} \omega_6 + c_s^2 \omega_{11}^2 \omega_{18}^2 \omega_6^2 + 24v_3^4 \omega_{11} \omega_{18} \omega_6^2 + 150v_3^2 c_s^2 \omega_{11} \omega_{18}^2 \omega_6^2 - 48c_s^4 \omega_{11} \omega_{18} \omega_6^2 - 48v_3^4 \omega_{11}^2 \omega_{18} + 24c_s^2 \omega_{11}^2 \omega_{18} + 96v_3^2 \omega_{11} \omega_{18} \omega_6
\end{aligned}$$

$$\begin{aligned}
C_{62} = & -8c_s^2 \omega_{18}^2 \omega_6^2 - 24v_3^4 \omega_{18}^2 \omega_6^2 + 156v_3^2 c_s^2 \omega_{18}^2 \omega_6 - 48c_s^4 \omega_{18}^2 \omega_6 - 24v_3^2 \omega_{18}^2 \omega_6 + 3v_3^4 \omega_{18}^2 \omega_6^3 + c_s^2 \omega_{18}^2 \omega_6^3 - 12v_3^2 \omega_6^3 + 6v_3^2 c_s^2 \omega_{18}^2 \omega_6^3 - 96v_3^2 c_s^2 \omega_{18}^2 + \\
& 24c_s^4 \omega_{18}^2 \omega_6^2 + 24v_3^2 \omega_{18}^2 \omega_6^2 + 12c_s^2 \omega_{18}^2 \omega_6 + 24v_3^2 \omega_6^2 - 72v_3^2 c_s^2 \omega_{18}^2 \omega_6^2 + 24v_3^4 \omega_{18}^2 \omega_6 - 3v_3^2 \omega_{18}^2 \omega_6^3 - 3c_s^4 \omega_{18}^2 \omega_6^3 - 24c_s^2 \omega_{18} \omega_6 + 48v_3^2 c_s^2 \omega_{18} \omega_6^2 - \\
& 48v_3^4 \omega_{18} \omega_6 + 18v_3^2 \omega_{18} \omega_6^2 + 6c_s^4 \omega_{18} \omega_6^2 - 12v_3^2 c_s^2 \omega_{18} \omega_6^2 - 24c_s^4 \omega_{18} \omega_6^2 - 72v_3^2 \omega_{18} \omega_6^2 + 24c_s^4 \omega_{18} \omega_6 - 24v_3^2 \omega_6^2 + 48v_3^2 \omega_{18} \omega_6 + 24c_s^4 \omega_{18} - \\
& 18v_3^4 \omega_{18} \omega_6^3 + 12v_3^2 c_s^2 \omega_6^3 - 6c_s^2 \omega_{18} \omega_6^3 + 12v_3^4 \omega_6^3 + 24c_s^2 \omega_{18} \omega_6^2 - 24v_3^2 c_s^2 \omega_6^2 + 72v_3^4 \omega_{18} \omega_6^2 - 24v_3^2 c_s^2 \omega_{18} \omega_6
\end{aligned}$$

$$\begin{aligned}
C_{63} = & -48v_3^2 \omega_{11}^2 \omega_6 - 12\omega_{11} \omega_{18} \omega_6^2 + 39c_s^2 \omega_{11} \omega_{18}^2 \omega_6^2 - 48c_s^2 \omega_{18} \omega_6 - 36c_s^2 \omega_{18} \omega_6^2 - 72v_3^2 \omega_{11} \omega_{18} \omega_6 - 36\omega_{11} \omega_{18}^2 + 84v_3^2 \omega_{11} \omega_{18}^2 + 120v_3^2 \omega_{18}^2 \omega_6 + 24\omega_{11}^2 \omega_6 + \\
& 24c_s^2 \omega_{11}^2 \omega_6 + 2\omega_{11}^2 \omega_{18} \omega_6^2 - 33c_s^2 \omega_{11}^2 \omega_{18} \omega_6^2 - 5v_3^2 \omega_{11}^2 \omega_{18} \omega_6^2 + 120c_s^2 \omega_{11} \omega_{18} \omega_6 - 60v_3^2 \omega_{18}^2 \omega_6^2 - 12\omega_{11}^2 \omega_6^2 - 48c_s^2 \omega_{11}^2 \omega_6 - 120c_s^2 \omega_{11} \omega_{18}^2 \omega_6 + 24v_3^2 \omega_{11}^2 \omega_6^2 + \\
& 24\omega_{11} \omega_{18} \omega_6 + 24\omega_{18}^2 \omega_6^2 + 72c_s^2 \omega_{18}^2 \omega_6 + 36v_3^2 \omega_{11} \omega_{18} \omega_6^2 + 60c_s^2 \omega_{11} \omega_{18}^2 - 24c_s^2 \omega_{11} \omega_{18} \omega_6 + 72\omega_{11} \omega_{18}^2 \omega_6 + 36\omega_{11}^2 \omega_{18} + 61v_3^2 \omega_{11} \omega_{18} \omega_6^2 - 51v_3^2 \omega_{11}^2 \omega_{18} \omega_6^2 - \\
& 72\omega_{11}^2 \omega_{18} \omega_6 - 84v_3^2 \omega_{11}^2 \omega_{18} + 168v_3^2 \omega_{11}^2 \omega_{18} \omega_6 + 21\omega_{11}^2 \omega_{18} \omega_6^2 - 3c_s^2 \omega_{11}^2 \omega_{18} \omega_6^2 - 25\omega_{11} \omega_{18}^2 \omega_6 + 12c_s^2 \omega_{11} \omega_{18} \omega_6^2 - 60c_s^2 \omega_{11}^2 \omega_{18} - 168v_3^2 \omega_{11}^2 \omega_{18} \omega_6
\end{aligned}$$

2.2.4 Conservation of momentum: ρv_2

$$\begin{aligned}
& v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{\delta_1 v_2 v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 \rho v_2}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_1 \rho v_1}{\delta_t} \frac{\partial v_2}{\partial x_1} + (c_s^2 + v_2^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2\delta_1 \rho v_2}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_1 \rho}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\
& \frac{\delta_1 \rho v_2}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_5) \frac{c_s^2 \delta_1^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{c_s^2 \delta_1^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\
& (-2 - 2\omega_{10} c_s^2 + \omega_{10} + 4c_s^2 + 6v_2^2 - 3\omega_{10} v_2^2) \frac{\delta_1^2}{\omega_{10} \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_{10}) \frac{3\delta_1^2 \rho v_2}{\omega_{10} \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_7) \frac{c_s^2 \delta_1^2}{2\omega_7 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\
& (-2 + \omega_7) \frac{c_s^2 \delta_1^2}{2\omega_7 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{c_s^2 \delta_1^2 \rho}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_5) \frac{c_s^2 \delta_1^2 \rho}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (-2 - 3\omega_{10} c_s^2 + \omega_{10} + 6c_s^2 + 2v_2^2 - \omega_{10} v_2^2) \frac{\delta_1^2 v_2}{2\omega_{10} \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 - \omega_{10} c_s^2 + \omega_{10} + 2c_s^2 + 6v_2^2 - 3\omega_{10} v_2^2) \frac{\delta_1^2 \rho}{2\omega_{10} \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_7) \frac{c_s^2 \delta_1^2 \rho}{2\omega_7 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_7) \frac{c_s^2 \delta_1^2 \rho}{2\omega_7 \delta_t} \frac{\partial^2 v_2}{\partial x_3^2} + C_1 \frac{\delta_1^3 v_2 v_1}{12\omega_5 \omega_9 \omega_{12} \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_1^3 \rho v_2}{12\omega_5 \omega_9 \omega_{12} \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{\delta_1^3 \rho v_1}{6\omega_5^2 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + \\
& (-12 + 12\omega_5 - \omega_5^2) \frac{c_s^4 \delta_1^3}{6\omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (\omega_5 \omega_{12} + 2\omega_5 - \omega_5^2 - 2\omega_{12}) \frac{c_s^2 \delta_1^3 \rho v_1}{\omega_5^2 \omega_{12} \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (-12\omega_{10} \omega_{15} - \omega_{10} \omega_5^2 \omega_{15} - 12\omega_{10} \omega_5^2 + 12\omega_5^2 + 12\omega_{10} \omega_5 \omega_{15} - 12\omega_5 \omega_{15} + 12\omega_{10} \omega_5) \frac{c_s^2 \delta_1^3 \rho v_2}{6\omega_{10} \omega_5^2 \omega_{15} \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& C_4 \frac{\delta_1^3 v_2 v_1}{\omega_{10}^2 \omega_5 \omega_{15} \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + C_5 \frac{\delta_1^3 \rho v_2}{12\omega_{10}^2 \omega_5^2 \omega_{15} \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_6 \frac{\delta_1^3 \rho v_1}{\omega_{10}^2 \omega_5 \omega_{15} \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_7 \frac{\delta_1^3 \rho}{12\omega_{10}^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + \\
& (-24 - 36\omega_{10} c_s^2 + 24\omega_{10} + 36c_s^2 - 4\omega_{10}^2 + 11\omega_{10}^2 v_2^2 + 60v_2^2 - 60\omega_{10} v_2^2 + 5\omega_{10}^2 c_s^2) \frac{\delta_1^3 \rho v_2}{6\omega_{10}^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + \\
& (-\omega_8 \omega_5 + \omega_7 \omega_8 \omega_5 + \omega_7 \omega_5 - \omega_7 \omega_8 + \omega_5^2 - \omega_7 \omega_5^2) \frac{v_3 c_s^2 \delta_1^3 \rho}{\omega_7 \omega_8 \omega_5^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} + \\
& (-6\omega_8 \omega_5 + 6\omega_5 \omega_6 - 6\omega_7 \omega_5 \omega_6 - \omega_7 \omega_8 \omega_5 \omega_6 + 6\omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_7 \omega_6) \frac{c_s^2 \delta_1^3 \rho v_2}{6\omega_7 \omega_8 \omega_5 \omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (-\omega_8 \omega_5 + \omega_7 \omega_8 \omega_5 + \omega_7 \omega_5 - \omega_7 \omega_8 + \omega_5^2 - \omega_7 \omega_5^2) \frac{v_3 c_s^2 \delta_1^3 \rho}{\omega_7 \omega_8 \omega_5^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-\omega_8 \omega_5 + \omega_7^2 - \omega_7^2 \omega_5 + \omega_7 \omega_8 \omega_5 + \omega_7 \omega_5 - \omega_7 \omega_8) \frac{c_s^2 \delta_1^3 \rho v_1}{\omega_7^2 \omega_8 \omega_5 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3 \delta_1^3 v_2}{\omega_{10}^2 \omega_7 \delta_t \omega_{16}} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_9 \frac{v_3 \delta_1^3 \rho}{\omega_{10}^2 \omega_7 \delta_t \omega_{16}} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& + C_{10} \frac{\delta_1^3 \rho v_2}{12\omega_{10}^2 \omega_7^2 \delta_t \omega_{16}} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_8 \omega_5 + 6\omega_5 \omega_6 - 6\omega_7 \omega_5 \omega_6 - \omega_7 \omega_8 \omega_5 \omega_6 + 6\omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_7 \omega_6) \frac{c_s^2 \delta_1^3 \rho v_2}{6\omega_7 \omega_8 \omega_5 \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-\omega_8 \omega_5 + \omega_7^2 - \omega_7^2 \omega_5 + \omega_7 \omega_8 \omega_5 + \omega_7 \omega_5 - \omega_7 \omega_8) \frac{c_s^2 \delta_1^3 \rho v_1}{\omega_7^2 \omega_8 \omega_5 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + (-12 + 12\omega_7 - \omega_7^2) \frac{c_s^4 \delta_1^3}{6\omega_7^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_2^2} + \\
& (12\omega_{10} \omega_7 - 12\omega_{10} \omega_7^2 + 12\omega_7^2 - \omega_{10} \omega_7^2 \omega_{16} - 12\omega_7 \omega_{16} + 12\omega_{10} \omega_7 \omega_{16} - 12\omega_{10} \omega_{16}) \frac{c_s^2 \delta_1^3 \rho v_2}{6\omega_{10} \omega_7^2 \delta_t \omega_{16}} \frac{\partial^3 v_2}{\partial x_2 \partial x_2^2} +
\end{aligned}$$

$$\begin{aligned}
& (2\omega_7 - \omega_7^2 + \omega_7\omega_{19} - 2\omega_{19}) \frac{v_3 c_s^2 \delta_l^3 \rho}{\omega_7^2 \omega_{19} \delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3 \delta_l^3 v_2}{12\omega_7 \omega_{11} \omega_{19} \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{v_3 \delta_l^3 \rho}{6\omega_7^2 \omega_{19} \delta_t} \frac{\partial^3 v_2}{\partial x_3^3} + C_{13} \frac{\delta_l^3 \rho v_2}{12\omega_7 \omega_{11} \omega_{19} \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_{14} \frac{\delta_l^4 v_2}{24\omega_5^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\delta_l^4 \rho v_2 v_1}{12\omega_5^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{\delta_l^4 \rho}{24\omega_5^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_{17} \frac{\delta_l^4 v_1}{12\omega_{10} \omega_5^3 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_{18} \frac{\delta_l^4 \rho}{12\omega_{10} \omega_5^3 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{\delta_l^4 \rho v_2 v_1}{12\omega_{10}^3 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{20} \frac{\delta_l^4 v_2}{12\omega_{10}^3 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2^2} + \\
& C_{21} \frac{\delta_l^4 \rho v_2 v_1}{2\omega_{10}^3 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{\delta_l^4 \rho}{12\omega_{10}^3 \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{\delta_l^4 v_1}{4\omega_{10}^3 \omega_5^2 \omega_{15}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + \\
& C_{24} \frac{\delta_l^4 \rho}{12\omega_{10}^3 \omega_5^3 \omega_{15}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{25} \frac{\delta_l^4 \rho v_2 v_1}{4\omega_{10}^3 \omega_5^2 \omega_{15}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{26} \frac{\delta_l^4 v_2}{12\omega_{10}^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2} + C_{27} \frac{\delta_l^4 \rho}{12\omega_{10}^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& C_{28} \frac{v_3 \delta_l^4 v_2 v_1}{4\omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + C_{29} \frac{v_3 \delta_l^4 \rho v_2}{4\omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6 \delta_t} \frac{\partial^4 v_1}{\partial x_3^3 \partial x_3} + C_{30} \frac{v_3 \delta_l^4 \rho v_1}{2\omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_3^3 \partial x_3} + \\
& C_{31} \frac{\delta_l^4 \rho v_2 v_1}{12\omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_3^3 \partial x_3} + C_{32} \frac{2v_3 c_s^4 \delta_l^4}{\omega_7^2 \omega_5^2 \omega_9^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{33} \frac{v_3 c_s^4 \delta_l^4 \rho v_1}{\omega_7 \omega_{14} \omega_8^2 \omega_5^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{v_3 c_s^2 \delta_l^4 \rho v_2}{2\omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 \omega_6 \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{35} \frac{c_s^2 \delta_l^4 \rho}{12\omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8^2 \omega_5^3 \omega_{15} \omega_{12} \omega_6^2 \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{36} \frac{v_3 \delta_l^4 v_2 v_1}{\omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 \omega_6 \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{37} \frac{v_3 \delta_l^4 \rho v_2}{2\omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 \omega_6 \delta_t \omega_{16}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{38} \frac{v_3 \delta_l^4 \rho v_1}{\omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 \omega_6 \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& + C_{39} \frac{\delta_l^4 \rho v_2 v_1}{2\omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 \omega_6 \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{40} \frac{v_3 \delta_l^4}{4\omega_{10}^3 \omega_7^2 \delta_t \omega_{16}^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{41} \frac{v_3 \delta_l^4 \rho v_2}{4\omega_{10}^3 \omega_7^2 \delta_t \omega_{16}^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& C_{42} \frac{\delta_l^4 \rho}{12\omega_{10}^3 \omega_7^2 \delta_t \omega_{16}^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{43} \frac{\delta_l^4}{12\omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{12} \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{44} \frac{\delta_l^4 \rho}{4\omega_{13} \omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12} \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& C_{45} \frac{\delta_l^4 \rho}{4\omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^3 \omega_{12} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + C_{46} \frac{v_3 \delta_l^4 \rho}{2\omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18} \omega_{12} \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{47} \frac{\delta_l^4 \rho}{2\omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{48} \frac{\delta_l^4 \rho}{12\omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{49} \frac{\delta_l^4 \rho v_2}{2\omega_{10}^2 \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{50} \frac{\delta_l^4 \rho}{2\omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{51} \frac{\delta_l^4 v_2}{12\omega_{10}^3 \omega_7^2 \omega_{23} \omega_{19} \delta_t \omega_{16}^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{52} \frac{\delta_l^4 \rho}{12\omega_{10}^3 \omega_7^2 \omega_{23} \omega_{19} \delta_t \omega_{16}^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{v_3 \delta_l^4 \rho v_2}{2\omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11} \omega_{19}^2 \delta_t \omega_{16}^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{54} \frac{v_3 \delta_l^4 v_2 v_1}{4\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{v_3 \delta_l^4 \rho v_2}{12\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{56} \frac{v_3 \delta_l^4 \rho v_1}{2\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^3} + \\
& C_{57} \frac{\delta_l^4 \rho v_2 v_1}{4\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18} \omega_6 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{58} \frac{v_3 \delta_l^4}{12\omega_{10} \omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{59} \frac{v_3 \delta_l^4 \rho v_2}{12\omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19} \delta_t \omega_{16}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{60} \frac{\delta_l^4 \rho}{12\omega_{10} \omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{\delta_l^4 v_2}{24\omega_7^2 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{62} \frac{\delta_l^4 \rho}{24\omega_7^2 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_3^4} + C_{63} \frac{v_3 \delta_l^4 \rho v_2}{12\omega_7^2 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -18c_s^2 \omega_5 \omega_{12} - 36c_s^2 \omega_9 - 12\omega_9 v_1^2 + 3c_s^2 \omega_5 \omega_9 \omega_{12} + 6\omega_5 \omega_{12} - 6\omega_5 \omega_{12} v_1^2 - 6\omega_5 \omega_9 + 12\omega_{12} v_1^2 + 6\omega_5 \omega_9 v_1^2 + 36c_s^2 \omega_{12} + 12\omega_9 - \omega_5 \omega_9 \omega_{12} - \\
& 12\omega_{12} + \omega_5 \omega_9 \omega_{12} v_1^2 + 18c_s^2 \omega_5 \omega_9 \\
C_2 &= -6c_s^2 \omega_5 \omega_{12} - 12c_s^2 \omega_9 - 36\omega_9 v_1^2 + c_s^2 \omega_5 \omega_9 \omega_{12} + 6\omega_5 \omega_{12} - 18\omega_5 \omega_{12} v_1^2 - 6\omega_5 \omega_9 + 36\omega_{12} v_1^2 + 18\omega_5 \omega_9 v_1^2 + 12c_s^2 \omega_{12} + 12\omega_9 - \omega_5 \omega_9 \omega_{12} - \\
& 12\omega_{12} + 3\omega_5 \omega_9 \omega_{12} v_1^2 + 6c_s^2 \omega_5 \omega_9 \\
C_3 &= 15c_s^2 \omega_5 \omega_{12} - 3\omega_5 \omega_{12} + 6\omega_5 + 3\omega_5 \omega_{12} v_1^2 - 6\omega_5 v_1^2 + \omega_5^2 \omega_{12} + 3\omega_5^2 v_1^2 - 12c_s^2 \omega_{12} - 3\omega_5^2 + 3c_s^2 \omega_5^2 - \omega_5^2 \omega_{12} v_1^2 - 6c_s^2 \omega_5 - 3c_s^2 \omega_5^2 \omega_{12} \\
C_4 &= -\omega_{10}^2 \omega_5 + \omega_{10} \omega_{15} v_2^2 + 3\omega_{10}^2 c_s^2 \omega_5 - \omega_{10} \omega_{15} - \omega_{10} \omega_5 v_2^2 + \omega_{10}^2 - \omega_{10}^2 v_2^2 + 3\omega_{10} c_s^2 \omega_{15} + \omega_{10}^2 \omega_5 v_2^2 + \omega_{10} \omega_5 \omega_{15} - \omega_5 \omega_{15} + 3c_s^2 \omega_5 \omega_{15} - \\
& 3\omega_{10} c_s^2 \omega_5 - 3\omega_{10} c_s^2 \omega_5 \omega_{15} - 3\omega_{10}^2 c_s^2 + \omega_{10} \omega_5 - \omega_{10} \omega_5 \omega_{15} v_2^2 + \omega_5 \omega_{15} v_2^2 \\
C_5 &= 12\omega_{10}^2 \omega_5 - 12\omega_{10}^2 c_s^2 \omega_5 - 6\omega_{10} \omega_5^2 \omega_{15} v_2^2 + 36c_s^2 \omega_5^2 \omega_{15} + 12\omega_5^2 \omega_{15} v_2^2 - 18\omega_{10} c_s^2 \omega_5^2 \omega_{15} + 42\omega_{10}^2 c_s^2 \omega_5 \omega_{15} + 6\omega_{10} \omega_5^2 \omega_{15} - 12\omega_5^2 \omega_{15} + \\
& 12\omega_{10}^2 \omega_5^2 v_2^2 + 12\omega_{10}^2 c_s^2 \omega_5^2 - 12\omega_{10}^2 \omega_5^2 + 6\omega_{10}^2 \omega_5 \omega_{15} v_2^2 - 6\omega_{10}^2 \omega_5 \omega_{15} - 12\omega_{10}^2 \omega_5 v_2^2 + 12\omega_{10} \omega_5^2 + 3\omega_{10}^2 \omega_5^2 \omega_{15} - 11\omega_{10}^2 c_s^2 \omega_5^2 \omega_{15} - 12\omega_{10} c_s^2 \omega_5^2 - \\
& 12\omega_{10} \omega_5^2 v_2^2 - 24\omega_{10}^2 c_s^2 \omega_{15} - 3\omega_{10}^2 \omega_5^2 \omega_{15} v_2^2 - 24\omega_{10} c_s^2 \omega_5 \omega_{15} \\
C_6 &= -\omega_{10}^2 \omega_5 + 3\omega_{10} \omega_{15} v_2^2 + \omega_{10}^2 c_s^2 \omega_5 - \omega_{10} \omega_{15} - 3\omega_{10} \omega_5 v_2^2 + \omega_{10}^2 - 3\omega_{10}^2 v_2^2 + \omega_{10} c_s^2 \omega_{15} + 3\omega_{10}^2 \omega_5 v_2^2 + \omega_{10} \omega_5 \omega_{15} - \omega_5 \omega_{15} + c_s^2 \omega_5 \omega_{15} - \\
& \omega_{10} c_s^2 \omega_5 - \omega_{10} c_s^2 \omega_5 \omega_{15} - \omega_{10}^2 c_s^2 + \omega_{10} \omega_5 - 3\omega_{10} \omega_5 \omega_{15} v_2^2 + 3\omega_5 \omega_{15} v_2^2 \\
C_7 &= 12\omega_{10} c_s^2 + \omega_{10}^2 c_s^4 - 12c_s^2 + 24\omega_{10}^2 c_s^2 v_2^2 - 7\omega_{10}^2 v_2^2 + 36v_2^4 - 36\omega_{10} v_2^4 - 144\omega_{10} c_s^2 v_2^2 + 7\omega_{10}^2 v_2^4 - 36v_2^2 + 144c_s^2 v_2^2 + 36\omega_{10} v_2^2 - 12\omega_{10} c_s^4 - \omega_{10}^2 c_s^2 + 12c_s^4 \\
C_8 &= \omega_{10}^2 \omega_7 v_2^2 + \omega_{10} \omega_7 + 3\omega_7 c_s^2 \omega_{16} - 3\omega_{10} \omega_7 c_s^2 \omega_{16} + \omega_7 v_2^2 \omega_{16} - \omega_{10} \omega_7 v_2^2 \omega_{16} + \omega_{10}^2 - \omega_{10}^2 v_2^2 - 3\omega_{10} \omega_7 c_s^2 - \omega_7 \omega_{16} + \omega_{10} \omega_7 \omega_{16} + \omega_{10} v_2^2 \omega_{16} + \\
& 3\omega_{10}^2 \omega_7 c_s^2 - \omega_{10}^2 \omega_7 - \omega_{10} \omega_7 v_2^2 + 3\omega_{10} c_s^2 \omega_{16} - 3\omega_{10}^2 c_s^2 - \omega_{10} \omega_{16} \\
C_9 &= 3\omega_{10}^2 \omega_7 v_2^2 + \omega_{10} \omega_7 + \omega_7 c_s^2 \omega_{16} - \omega_{10} \omega_7 c_s^2 \omega_{16} + 3\omega_7 v_2^2 \omega_{16} - 3\omega_{10} \omega_7 v_2^2 \omega_{16} + \omega_{10}^2 - 3\omega_{10}^2 v_2^2 - \omega_{10} \omega_7 c_s^2 - \omega_7 \omega_{16} + \omega_{10} \omega_7 \omega_{16} + \\
& 3\omega_{10} v_2^2 \omega_{16} + \omega_{10}^2 \omega_7 c_s^2 - \omega_{10}^2 \omega_7 - 3\omega_{10} \omega_7 v_2^2 + \omega_{10} c_s^2 \omega_{16} - \omega_{10}^2 c_s^2 - \omega_{10} \omega_{16} \\
C_{10} &= -3\omega_{10}^2 \omega_7 v_2^2 \omega_{16} - 12\omega_{10}^2 \omega_7 v_2^2 - 24\omega_{10}^2 c_s^2 \omega_{16} - 12\omega_{10} \omega_7 v_2^2 - 24\omega_{10} \omega_7 c_s^2 \omega_{16} - 6\omega_{10}^2 \omega_7 \omega_{16} + 12\omega_{10} \omega_7^2 + 12\omega_{10}^2 \omega_7^2 c_s^2 - 11\omega_{10}^2 \omega_7^2 c_s^2 \omega_{16} - \\
& 12\omega_7^2 \omega_{16} + 6\omega_{10} \omega_7^2 \omega_{16} + 12\omega_7^2 v_2^2 \omega_{16} - 12\omega_{10} \omega_7^2 c_s^2 - 6\omega_{10} \omega_7^2 v_2^2 \omega_{16} + 42\omega_{10}^2 \omega_7 c_s^2 \omega_{16} - 12\omega_{10}^2 \omega_7^2 + 3\omega_{10}^2 \omega_7^2 \omega_{16} - 12\omega_{10}^2 \omega_7 c_s^2 + 12\omega_{10}^2 \omega_7 +
\end{aligned}$$

$$12\omega_{10}^2\omega_5^3\omega_{15}\omega_{12}v_1^2 + 18\omega_{10}^2c_s^4\omega_5^3\omega_{21}\omega_{15}^2 + 12\omega_{10}c_s^4\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 6\omega_{10}^3\omega_5^2\omega_{15}\omega_{12}v_1^2 + 12\omega_{10}^3c_s^2\omega_5^2\omega_{15}\omega_{12}v_2^2 + 6\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_{12}v_2^2v_1^2 - 12\omega_{10}^3\omega_5^2\omega_{15}^2\omega_{12}v_2^2v_1^2 - 12\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_{12}v_2^2 + 18\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12}v_1^2 - 36\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{12}v_1^2 + 36\omega_{10}^3c_s^2\omega_5^2\omega_{15}^2 + 12\omega_{10}^3c_s^2\omega_5^2\omega_{15}^2v_2^2$$

$$\begin{aligned}
C_{22} = & -6w_{10}c_2^4w_3^5w_{21}w_{15}w_{12} - 36w_{10}^3w_2^4w_3w_{21}w_{12}w_2^2v_1^2 - 12w_{10}^3c_4^4w_5^4w_{15}w_{12} + 36w_{10}^2w_3^4w_5w_{15}w_{12}v_2^2v_1^2 - 12w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_1^2 - 36w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_2^2v_1^2 + \\
& -36w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_1^2 - 24w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_2^2 + 60w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_1^2 - 12w_{10}^3w_3^4w_5w_{21}w_{15}w_{12}v_2^2 - 24w_{10}^3w_3^4w_5w_{21}w_{15}w_{12}v_1^2 - 12w_{10}^3w_5^4w_{15}^2w_{12}v_1^2 - 12w_{10}^3w_5^4w_{15}^2w_{12}v_2^2 + \\
& -36w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_1^2 - 12w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_2^2 - 12w_{10}^3c_2^4w_5^2w_{15}^2w_{12}v_1^2 + 6w_{10}c_4^4w_5^4w_{21}w_{15}w_{12} + 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} + 24w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 + \\
& + 24w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 72w_{10}^2w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 - 12w_{10}w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 - 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 + 12w_{10}^2c_4^4w_5^4w_{21}w_{15}w_{12} + 12c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 + \\
& + 36w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 6w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 36w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 + 18w_{10}^3w_3^4w_5^4w_{15}w_{12}v_2^2v_1^2 + 18w_{10}^3c_4^4w_5^4w_{21}w_{15}w_{12} - 24w_{10}^3c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - \\
& - 12w_{10}^3c_2^4w_5^4w_{21}w_{15}w_{12} + 12w_{10}w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 54w_{10}w_3^4w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 - 132w_{10}^3c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 - 36w_{10}^3c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - \\
& - 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} - 6w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} + 12w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 36w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 18w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 18w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + \\
& + 72w_{10}w_3^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 24w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 72w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 - 18w_{10}^3c_2^4w_5^4w_{21}w_{15}w_{12} - 24w_{10}^3c_4^4w_5^4w_{21}w_{15}w_{12} - 12w_{10}^3w_3^4w_5^4w_{15}w_{12}v_1^2 + \\
& + 18w_{10}^3c_2^4w_5^4w_{15}w_{12}v_2^2 - 12w_{10}^2c_2^4w_5^4w_{15}w_{12} - 12w_{10}^2c_4^4w_5^4w_{15}w_{12} - 24w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 108w_{10}c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 60w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + \\
& + 24w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} - 12w_{10}^2c_4^4w_5^4w_{21}w_{15} - 6w_{10}^2c_2^4w_5^4w_{21}w_{15} + 6w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} + 12w_{10}^3w_5^4w_{21}w_{15}w_{12} - 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 + \\
& + 72w_{10}^2w_3^4w_{21}w_{15}w_{12}v_2^2v_1^2 - 6w_{10}^2c_2^4w_5^4w_{15}w_{12} - 6w_{10}^2c_2^4w_5^4w_{15}w_{12}v_2^2 - 36w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 36w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 + 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} + \\
& + 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 6w_{10}^2c_4^4w_5^4w_{21}w_{15}w_{12} - 6w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} - 24w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + \\
& + 6w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 + 6w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 - 48w_{10}^3c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} - 12w_{10}^2c_4^4w_5^4w_{21}w_{15}w_{12} + 12w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 + \\
& + 18w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 12w_{10}^3c_2^4w_5^4w_{15}w_{12} - 6w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12} - 144w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 + 36w_{10}w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 + \\
& + 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12} - 12w_{10}^2c_4^4w_5^4w_{21}w_{15}w_{12} + 24w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 + 12w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 - 18w_{10}^3w_5^4w_{15}w_{12}v_2^2v_1^2 + \\
& + 18w_{10}^2c_2^4w_5^4w_{15}w_{12}v_2^2 - 36w_{10}^2c_2^4w_5^4w_{15}w_{12}v_2^2 + 12w_{10}^3w_5^4w_{15}w_{12}v_1^2 - 6w_{10}^2w_3^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 12w_{10}^3c_2^4w_5^4w_{15}w_{12}v_1^2 - 36w_{10}w_3^4w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 + \\
& + 36w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 - 24w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 6w_{10}^3c_4^4w_5^4w_{15} - 4w_{10}^3c_4^4w_5^4w_{21}w_{15}w_{12} - 84w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_2^2 - 24w_{10}^3c_2^4w_5^4w_{21}w_{12}v_2^2 + \\
& + 108w_{10}^3w_5^4w_{21}w_{15}w_{12}v_2^2v_1^2 + 24w_{10}^2c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 18w_{10}c_2^4w_5^4w_{21}w_{15}w_{12}v_1^2 - 12w_5^4w_{21}w_{15}w_{12}v_1^2 - 36w_{10}^2w_5^4w_{15}w_{12}v_2^2v_1^2 + \\
& + 12w_{10}^2c_4^4w_5^4w_{15}w_{12} + 6w_{10}^2c_2^4w_5^4w_{15}w_{1$$

$$C_{48} = 12\omega_{10}\omega_7^3v_3w_{23}w_{20}\omega_{17}w_8^2\omega_5^2\omega_6^2\omega_{19}v_2^2v_{1\omega_{16}} - 12\omega_{10}\omega_7^3v_3^2w_{23}c_s^2w_{20}\omega_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19}\omega_{16} - 12\omega_7^3v_3w_{23}w_{20}\omega_{17}w_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19}v_2^2v_{1\omega_{16}} - 12\omega_{10}\omega_7^3v_3w_{23}c_s^2w_{20}\omega_{17}w_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19}v_2^2v_{1\omega_{16}} - 12\omega_{10}\omega_7^3v_3^2w_{23}w_{20}\omega_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19}v_2^2\omega_{16} + 6\omega_7^3w_{23}c_s^2w_{20}\omega_{17}w_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19}v_2^2\omega_{16} - 24\omega_{10}\omega_7^3v_3w_{23}w_{17}w_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19}v_2^2v_{1\omega_{16}} - 12\omega_{10}\omega_7^3v_3^2w_{23}c_s^2w_{20}\omega_8^2\omega_5^2\omega_{15}\omega_6^2\omega_{19} - 6\omega_{10}\omega_7^3w_{23}c_s^2w_{20}\omega_{17}w_8^2\omega_5^2\omega_6^2\omega_{19}v_2^2\omega_{16} -$$

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$$\begin{aligned}
C_{55} = & -24w_7c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19} - 36w_7c_s^2w_{20}w_{11}w_8w_5w_{18}w_6^2 - 42w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - 6w_7^2w_{20}w_{11}w_8w_5w_6w_{19}^2 - \\
& 6w_7^2c_s^2w_{11}w_8^2w_5w_{18}w_6w_{19} - 18w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7^2w_{11}w_8w_5w_{18}w_6w_{19}^2 - 12w_7c_s^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 + 12w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 12w_7^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 + 24w_7c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7w_{20}w_{11}w_8^2w_5w_6w_{19}^2 - 6w_7^2v_3^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7^2v_3^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - \\
& 12w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7w_{20}w_{11}w_8^2w_5w_{18}w_6^2 - 24w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 + 12w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 + 18w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 - \\
& 6w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7^2v_3^2w_{11}w_8w_5w_{18}w_6w_{19}^2 + 12w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 + 4w_7^2v_3^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - \\
& 12w_7v_3^2w_{20}w_{11}w_8^2w_5^2w_6w_{19}^2 + 12w_7^2v_3^2w_{11}w_8w_5^2w_{18}w_6w_{19}^2 + 12w_7c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 3w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 6w_7^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 9w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 18w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 24c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 + 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 + \\
& w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 24w_7c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 - 4w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - \\
& 36w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7^2c_s^2w_{11}w_8w_5^2w_{18}w_6w_{19}^2 - 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 - 6w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 12w_7c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 6w_7^2v_3^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - 6w_7w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 12w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 3w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 + 54w_7c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 36c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 + 12w_7^2v_3^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 6w_7^2v_3^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - 12w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 + 6w_7^2c_s^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 9w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 - \\
& 36c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 + 12v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - 9w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2v_3^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - \\
& 12w_7^2w_{11}w_8w_5w_{18}w_6w_{19}^2 + 18w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 + 12w_7^2c_s^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 + 30w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 + \\
& 6w_7^2w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 12w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 + 36w_7c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 3w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - \\
& 54w_7c_s^2w_{20}w_{11}w_8w_5w_{18}w_6w_{19}^2 - 12w_7w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 6w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 - 12w_7^2v_3^2w_{11}w_8w_5w_{18}w_6w_{19}^2 + 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_6w_{19}^2 - \\
& 12w_7w_{11}w_8w_5w_{18}w_6w_{19}^2 + 12w_7w_{20}w_{11}w_8^2w_5w_6w_{19}^2 - 6w_7^2v_3^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 - 18w_7w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 6w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + 12w_7^2c_s^2w_{11}w_8w_5w_{18}w_6w_{19}^2 - 6w_7^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 + 42w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6w_{19}^2 + \\
& 24w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18}w_6^2 - 12w_7^2w_{20}w_{11}w_8^2w_5w_6w_{19}$$

[illegible]

$$\begin{aligned}
& 6\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}v_2^2\omega_{16} + 36\omega_{10}\omega_7^2v_3^2c_s^2\omega_{11}^2\omega_{19}\omega_{16} - 18\omega_{10}\omega_7^3v_3^2\omega_{11}^2\omega_{19}v_2^2\omega_{16} + 12\omega_{10}\omega_7^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} + 12\omega_7^3c_s^4\omega_{11}^2\omega_{19}^2 - \\
& 12\omega_{10}\omega_7^3\omega_{23}\omega_{11}\omega_{19}^2v_2^2 - 12\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}^2 - 12\omega_{10}\omega_7\omega_{23}c_s^4\omega_{11}\omega_{19}\omega_{16} - 12\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}v_2^2\omega_{16} + 24\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} + \\
& 12\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2 - 6\omega_{10}\omega_7^3c_s^4\omega_{11}^2\omega_{19}\omega_{16} + 36\omega_{10}\omega_7^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 6\omega_{10}\omega_7^3\omega_{11}^2\omega_{19}v_2^2\omega_{16} - \omega_{10}\omega_7^3\omega_{23}c_s^4\omega_{11}^2\omega_{19}^2\omega_{16} + \\
& 36\omega_{10}\omega_7^3v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2 + 54\omega_{10}\omega_7^2v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} + 60\omega_{10}\omega_7v_3^2\omega_{23}c_s^2\omega_{11}^2\omega_{19}\omega_{16} + 6\omega_{10}\omega_7^3\omega_{23}\omega_{19}^2v_2^2\omega_{16} - 6\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{19}^2v_2^2\omega_{16} + \\
& 6\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}v_2^2\omega_{16} + 12\omega_{10}\omega_7^3c_s^2\omega_{11}^2\omega_{19}^2 + 36\omega_{10}\omega_7^2v_3^2\omega_{11}^2\omega_{19}^2v_2^2 - 6\omega_{10}\omega_7^3\omega_{23}\omega_{11}\omega_{19}v_2^2\omega_{16} + 18\omega_{10}\omega_7^2\omega_{23}c_s^4\omega_{11}\omega_{19}\omega_{16} - \\
& 36\omega_{10}\omega_7^3v_3^2c_s^2\omega_{11}^2\omega_{19}^2 - 12\omega_{10}\omega_7^2\omega_{23}c_s^4\omega_{11}\omega_{19}^2 - 6\omega_7^3c_s^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} + 12\omega_7^3c_s^2\omega_{11}^2\omega_{19}^2v_2^2 + 18\omega_{10}\omega_7^3v_3^2c_s^2\omega_{11}^2\omega_{19}\omega_{16} - 12\omega_7^3\omega_{23}\omega_{11}^2\omega_{19}v_2^2\omega_{16} - \\
& 18\omega_{10}\omega_7^3v_3^2\omega_{23}\omega_{19}^2v_2^2\omega_{16} - 72\omega_{10}\omega_7v_3^2\omega_{23}\omega_{11}\omega_{19}v_2^2\omega_{16} - 24\omega_{10}\omega_7\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 15\omega_{10}\omega_7^3v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} - 36\omega_{10}\omega_7^3v_3^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} - \\
& 6\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}^2\omega_{19}\omega_{16} - 6\omega_{10}\omega_7^3c_s^2\omega_{11}^2\omega_{19}\omega_{16} - 36\omega_7^3v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2 - 12\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}\omega_{16} - 12\omega_7^3c_s^2\omega_{11}^2\omega_{19}^2 - 48\omega_{10}\omega_7^2\omega_{23}\omega_{11}\omega_{19}v_2^2\omega_{16} + \\
& 12\omega_7^3\omega_{23}\omega_{11}\omega_{19}^2v_2^2 - 18\omega_{10}\omega_7^2\omega_{23}c_s^4\omega_{11}\omega_{19}\omega_{16} + 6\omega_7^3\omega_{23}c_s^4\omega_{11}\omega_{19}^2\omega_{16} - 12\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} + 12\omega_{10}\omega_7^2\omega_{23}\omega_{11}^2v_2^2\omega_{16} + 12\omega_{10}\omega_7^2c_s^4\omega_{11}^2\omega_{19}^2 + \\
& 18\omega_{10}\omega_7^3v_3^2\omega_{23}\omega_{11}\omega_{19}v_2^2\omega_{16} + 18\omega_7^3v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} + 5\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2\omega_{16} - 18\omega_7^3v_3^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} - 36\omega_{10}\omega_7^2v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2 - \\
& 48\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2\omega_{16} - 24\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11}\omega_{19}v_2^2\omega_{16} - 12\omega_{10}\omega_7^2v_3^2\omega_{23}c_s^2\omega_{11}\omega_{16} + 30\omega_{10}\omega_7^3v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} - 5\omega_{10}\omega_7^2\omega_{23}c_s^4\omega_{11}^2\omega_{19}^2\omega_{16} - \\
& 9\omega_{10}\omega_7^3\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 12\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}^2\omega_{16} - 12\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} + 9\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 24\omega_7^2\omega_{23}c_s^2\omega_{11}^2\omega_{19}v_2^2\omega_{16} - \\
& 36\omega_{10}\omega_7^2v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2 + 12\omega_{10}\omega_7^2\omega_{11}\omega_{19}^2v_2^2 + 36\omega_{10}\omega_7^2v_3^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} + 12\omega_{10}\omega_7^2\omega_{23}c_s^4\omega_{11}\omega_{19}^2 + 36\omega_{10}\omega_7^2v_3^2c_s^2\omega_{11}\omega_{19}^2 - \\
& 12\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2 - 12\omega_{10}\omega_7^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 18\omega_7^3v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 144\omega_{10}\omega_7^2v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 6\omega_7^3c_s^4\omega_{11}^2\omega_{19}^2\omega_{16} - \\
& 36\omega_{10}\omega_7^3v_3^2\omega_{11}\omega_{19}^2v_2^2 + 12\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2 + 27\omega_{10}\omega_7^2v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 12\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} - 72\omega_7^2v_3^2\omega_{23}\omega_{11}\omega_{19}v_2^2\omega_{16} - \\
& 36\omega_7^3v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2 - 18\omega_{10}\omega_7^3v_3^2c_s^2\omega_{11}\omega_{19}\omega_{16} + 12\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} - 24\omega_7^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 18\omega_{10}\omega_7^3v_3^2\omega_{23}\omega_{11}^2v_2^2\omega_{16} + \\
& 6\omega_7^3\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} - 12\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2 - 6\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 48\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 12\omega_7^2\omega_{11}^2\omega_{19}^2v_2^2 + 6\omega_{10}\omega_7^3c_s^2\omega_{11}^2\omega_{19}\omega_{16} + \\
& 6\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}^2v_2^2\omega_{16} - 6\omega_{10}\omega_7^3\omega_{23}\omega_{11}^2v_2^2\omega_{16} + 36\omega_{10}\omega_7^3v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2 - 18\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} - 12\omega_{10}\omega_{23}c_s^4\omega_{11}^2\omega_{19}^2\omega_{16} + \\
& 18\omega_7^3v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2\omega_{16} - 24\omega_{10}\omega_7^2v_3^2\omega_{23}c_s^2\omega_{11}\omega_{16} - 108\omega_{10}\omega_7^2v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 6\omega_{10}\omega_7^3c_s^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} + 6\omega_{10}\omega_7^3\omega_{23}c_s^4\omega_{11}^2\omega_{19}\omega_{16} - \\
& 12\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2 + 36\omega_7^3v_3^2\omega_{11}^2\omega_{19}^2v_2^2 + 15\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 18\omega_7^3v_3^2c_s^2\omega_{11}\omega_{19}^2\omega_{16} + 6\omega_{10}\omega_7^3c_s^4\omega_{11}^2\omega_{19}\omega_{16} - 12\omega_7^3\omega_{23}c_s^4\omega_{11}^2\omega_{19}^2 + \\
& 12\omega_{10}\omega_7^2c_s^2\omega_{11}^2\omega_{19}^2v_2^2 + 60\omega_{10}\omega_7v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} - 15\omega_{10}\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 24\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 18\omega_{10}\omega_7\omega_{23}c_s^4\omega_{11}^2\omega_{19}\omega_{16} + \\
& 36\omega_{10}\omega_7^2v_3^2\omega_{23}\omega_{19}^2v_2^2\omega_{16} + 12\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 36\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 12\omega_{10}\omega_7^2\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 12\omega_{10}\omega_7^2c_s^4\omega_{11}^2\omega_{19}\omega_{16} + \\
& 18\omega_{10}\omega_7^2v_3^2\omega_{11}^2\omega_{19}^2v_2^2\omega_{16} + 18\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11}^2\omega_{19}\omega_{16} - 6\omega_7^3\omega_{23}c_s^2\omega_{11}\omega_{19}^2\omega_{16} - 36\omega_{10}\omega_7v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}^2\omega_{16} + 12\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{19}^2v_2^2\omega_{16} + \\
& 12\omega_{10}\omega_7^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2 - 15\omega_{10}\omega_7^2v_3^2\omega_{23}c_s^2\omega_{11}\omega_{19}\omega_{16} - 45\omega_{10}\omega_7^3v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} + 72\omega_7^2v_3^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 36\omega_{10}\omega_7^2v_3^2c_s^2\omega_{11}^2\omega_{19}^2\omega_{16} + \\
& 24\omega_7^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 12\omega_{10}\omega_7^2\omega_{11}\omega_{19}^2v_2^2 - 5\omega_{10}\omega_7^2\omega_{23}c_s^4\omega_{11}\omega_{19}^2\omega_{16} + 12\omega_{10}\omega_7^2\omega_{23}\omega_{11}\omega_{19}^2v_2^2\omega_{16} - 6\omega_{10}\omega_7^3\omega_{11}\omega_{19}^2v_2^2\omega_{16}
\end{aligned}$$

$$\begin{aligned}
C_{61} = & -3\omega_7^3v_3^4\omega_{11}^2\omega_{19}^2 - 48\omega_7v_3^4\omega_{11}\omega_{19} - 24\omega_7v_3^4\omega_{11}^2 - 432\omega_7v_3^2c_s^2\omega_{11}\omega_{19}^2 + 24\omega_7c_s^2\omega_{11}^2 + \omega_7^2c_s^2\omega_{11}^2\omega_{19}^2 - 48v_3^4\omega_{11}\omega_{19} + 24c_s^2\omega_{11}^2\omega_{19} + 36\omega_7^2v_3^2\omega_{19}^2 - \\
& 12\omega_7^2c_s^4\omega_{19}^2 - 144\omega_7v_3^2c_s^2\omega_{11}^2 + 30\omega_7^2v_3^2\omega_{11}\omega_{19} - 48\omega_7c_s^4\omega_{11}\omega_{19} - 12\omega_7^2c_s^4\omega_{11}^2\omega_{19} + 150\omega_7^2v_3^2c_s^2\omega_{11}\omega_{19}^2 + 96\omega_7v_3^2\omega_{11}\omega_{19}^2 + 3\omega_7^2v_3^2\omega_{11}^2\omega_{19}^2 - \\
& \omega_7^2c_s^2\omega_{11}^2\omega_{19}^2 + 72\omega_7^2v_3^2c_s^2\omega_{11}\omega_{19} + 48\omega_7v_3^2\omega_{11}\omega_{19} + 288\omega_7v_3^2c_s^2\omega_{19} + 48v_3^2\omega_{11}^2\omega_{19} - 24c_s^4\omega_{11}^2\omega_{19} - 216v_3^2c_s^2\omega_{11}\omega_{19} + 12\omega_7^2c_s^4\omega_{11}^2 - 12\omega_7^2v_3^2\omega_{11}^2 + \\
& 48\omega_7c_s^2\omega_{11}\omega_{19} - 24\omega_7c_s^2\omega_{19} + 72\omega_7v_3^4\omega_{19} - 30\omega_7^2v_3^4\omega_{11}\omega_{19} - 96\omega_7v_3^4\omega_{11}\omega_{19} + 12\omega_7^2c_s^2\omega_{11}^2\omega_{19} - 144\omega_7v_3^2c_s^2\omega_{11}\omega_{19} + 48\omega_7^4\omega_{11}\omega_{19} - 24c_s^2\omega_{11}\omega_{19}^2 + \\
& 24\omega_7^2v_3^4\omega_{11}\omega_{19} + 432\omega_7v_3^2c_s^2\omega_{11}\omega_{19} + 48\omega_7c_s^4\omega_{11}\omega_{19} - 36\omega_7^2v_3^2\omega_{11}\omega_{19} + 72\omega_7^2v_3^2c_s^2\omega_{11}^2 + 24\omega_7v_3^2\omega_{11}^2 - 126\omega_7^2v_3^2c_s^2\omega_{11}\omega_{19} - 96\omega_7v_3^2\omega_{11}\omega_{19} + \\
& 14\omega_7^2c_s^4\omega_{11}\omega_{19} - 24\omega_7c_s^4\omega_{11}^2 - 36\omega_7^2v_3^4\omega_{19} + 12\omega_7^2c_s^2\omega_{19}^2 - 12\omega_7^2c_s^2\omega_{11}^2 - 48\omega_7\omega_{11}\omega_{19} + 12\omega_7^2v_3^4\omega_{11}^2 + 24c_s^4\omega_{11}\omega_{19}^2 + 24\omega_7c_s^4\omega_{19}^2 - 24\omega_7^2v_3^2\omega_{11}\omega_{19} - \\
& 72\omega_7v_3^2\omega_{19} - 144\omega_7^2v_3^2c_s^2\omega_{19} - 12\omega_7^2v_3^2c_s^2\omega_{11}^2\omega_{19} + 36\omega_7^2v_3^4\omega_{11}\omega_{19} - 48\omega_7c_s^2\omega_{11}\omega_{19} - 14\omega_7^2c_s^4\omega_{11}\omega_{19} + 96\omega_7v_3^4\omega_{11}\omega_{19} + 216v_3^2c_s^2\omega_{11}\omega_{19}
\end{aligned}$$

$$\begin{aligned}
C_{62} = & -24\omega_7c_s^2\omega_{19} - 48\omega_7v_3^4\omega_{19} + \omega_7^3c_s^2\omega_{19}^2 + 3\omega_7^3v_3^4\omega_{19} + 12\omega_7^2v_3^2c_s^2 - 24\omega_7^2v_3^4 + 24\omega_7^2v_3^2\omega_{19} + 24\omega_7^2c_s^4\omega_{19} + 24c_s^4\omega_{19}^2 - 24\omega_7v_3^2c_s^2\omega_{19} + \\
& 12\omega_7^3v_3^4 + 156\omega_7v_3^2c_s^2\omega_{19} - 72\omega_7^2v_3^2\omega_{19} - 24\omega_7^2c_s^4\omega_{19} + 12\omega_7^2c_s^2\omega_{19}^2 + 24\omega_7v_3^4\omega_{19} - 6\omega_7^3c_s^2\omega_{19} - 18\omega_7^3v_3^4\omega_{19} - 12\omega_7^3v_3^2 + 24\omega_7c_s^4\omega_{19} + \\
& 48\omega_7v_3^2\omega_{19} + 48\omega_7^2v_3^2c_s^2\omega_{19} - 3\omega_7^3c_s^4\omega_{19} - 3\omega_7^3v_3^2\omega_{19} - 24\omega_7^2v_3^2c_s^2 - 96v_3^2c_s^2\omega_{19} - 24\omega_7^2v_3^2\omega_{19} + 6\omega_7^3v_3^2c_s^2\omega_{19} - 8\omega_7^3c_s^2\omega_{19} + 24\omega_7^2v_3^2 - \\
& 12\omega_7^3v_3^2c_s^2\omega_{19} + 72\omega_7^2v_3^2\omega_{19} + 24\omega_7^2c_s^2\omega_{19} - 48\omega_7c_s^4\omega_{19} - 24\omega_7v_3^2\omega_{19} - 72\omega_7^2v_3^2c_s^2\omega_{19} + 6\omega_7^3c_s^4\omega_{19} + 18\omega_7^3v_3^2\omega_{19}
\end{aligned}$$

$$\begin{aligned}
C_{63} = & 72\omega_7\omega_{11}\omega_{19}^2 - 24\omega_7c_s^2\omega_{11}\omega_{19} - 48\omega_7c_s^2\omega_{11}^2 - 3\omega_7^2c_s^2\omega_{11}^2\omega_{19} - 60c_s^2\omega_{11}\omega_{19} - 60\omega_7^2v_3^2\omega_{19} + 2\omega_7^2\omega_{11}^2\omega_{19} + 24\omega_7^2\omega_{19}^2 - 51\omega_7^2v_3^2\omega_{11}\omega_{19} - \\
& 168\omega_7v_3^2\omega_{11}\omega_{19} - 5\omega_7^2v_3^2\omega_{11}\omega_{19} - 72\omega_7v_3^2\omega_{11}\omega_{19} - 12\omega_7^2\omega_{11}^2 - 84v_3^2\omega_{11}\omega_{19} + 21\omega_7^2\omega_{11}\omega_{19} + 24\omega_7^2v_3^2\omega_{11} + 36\omega_{11}^2\omega_{19} - 120\omega_7c_s^2\omega_{11}\omega_{19}^2 + \\
& 72\omega_7c_s^2\omega_{19} + 24\omega_7\omega_{11}\omega_{19} - 33\omega_7^2c_s^2\omega_{11}\omega_{19} + 60c_s^2\omega_{11}\omega_{19}^2 - 72\omega_7\omega_{11}\omega_{19} + 12\omega_7^2c_s^2\omega_{11}\omega_{19} + 61\omega_7^2v_3^2\omega_{11}\omega_{19} - 48\omega_7v_3^2\omega_{11} + 168\omega_7v_3^2\omega_{11}\omega_{19} + \\
& 24\omega_7\omega_{11}^2 - 36\omega_7^2c_s^2\omega_{19} - 12\omega_7^2\omega_{11}\omega_{19} + 24\omega_7^2c_s^2\omega_{11}^2 + 84v_3^2\omega_{11}\omega_{19} - 48\omega_7\omega_{19}^2 - 25\omega_7^2\omega_{11}\omega_{19} + 36\omega_7^2v_3^2\omega_{11}\omega_{19} + 120\omega_7v_3^2\omega_{19} + \\
& 120\omega_7c_s^2\omega_{11}\omega_{19} + 39\omega_7^2c_s^2\omega_{11}\omega_{19}^2 - 36\omega_{11}\omega_{19}^2
\end{aligned}$$

2.2.5 Conservation of momentum: ρv_3

$$\begin{aligned}
& v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 \delta_1 v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \delta_1 \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_1 \rho v_1}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_3 \delta_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \delta_1 \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_1 \rho v_2}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\
& \frac{2v_3 \delta_1 \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{c_s^2 \delta_1^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2 \delta_1^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{c_s^2 \delta_1^2}{2\omega_7 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{c_s^2 \delta_1^2}{2\omega_7 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& + (-2 - 3v_3^2\omega_{11} + 4c_s^2 + \omega_{11} + 6v_3^2 - 2c_s^2\omega_{11}) \frac{\delta_1^2}{\omega_{11} \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3v_3 \delta_1^2 \rho}{\omega_{11} \delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{c_s^2 \delta_1^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\
& (-2 + \omega_7) \frac{c_s^2 \delta_1^2 \rho}{2\omega_7 \delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{c_s^2 \delta_1^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{c_s^2 \delta_1^2 \rho}{2\omega_7 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\
& (-2 - v_3^2\omega_{11} + 6c_s^2 + \omega_{11} + 2v_3^2 - 3c_s^2\omega_{11}) \frac{v_3 \delta_1^2}{2\omega_{11} \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 - 3v_3^2\omega_{11} + 2c_s^2 + \omega_{11} + 6v_3^2 - c_s^2\omega_{11}) \frac{\delta_1^2 \rho}{2\omega_{11} \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& C_1 \frac{v_3 \delta_1^3 v_1}{12\omega_{13}\omega_9\omega_6 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{v_3 \delta_1^3 \rho}{12\omega_{13}\omega_9\omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{\delta_1^3 \rho v_1}{6\omega_{13}\omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^3} + \\
& (-6\omega_8\omega_6 + 6\omega_5\omega_6 - 6\omega_7\omega_5\omega_6 - \omega_7\omega_8\omega_5\omega_6 + 6\omega_7\omega_5 - 6\omega_7\omega_8 + 6\omega_7\omega_8\omega_6) \frac{v_3 c_s^2 \delta_1^3 \rho}{6\omega_7\omega_8\omega_5\omega_6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-\omega_8\omega_6 - \omega_7\omega_6^2 - \omega_7\omega_8 + \omega_6^2 + \omega_7\omega_6 + \omega_7\omega_8\omega_6) \frac{c_s^2 \delta_1^3 \rho v_2}{\omega_7\omega_8\omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} + \\
& (-6\omega_8\omega_6 + 6\omega_5\omega_6 - 6\omega_7\omega_5\omega_6 - \omega_7\omega_8\omega_5\omega_6 + 6\omega_7\omega_5 - 6\omega_7\omega_8 + 6\omega_7\omega_8\omega_6) \frac{v_3 c_s^2 \delta_1^3 \rho}{6\omega_7\omega_8\omega_5\omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} +
\end{aligned}$$

$$\begin{aligned}
& (-\omega_8\omega_6 - \omega_7^2\omega_6 + \omega_7^2 - \omega_7\omega_8 + \omega_7\omega_6 + \omega_7\omega_8\omega_6) \frac{c_s^2\delta_l^3\rho v_1}{\omega_7^2\omega_8\omega_6\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_2^2} + C_4 \frac{v_3\delta_l^3 v_2}{12\omega_{10}\omega_7\delta_t\omega_{16}} \frac{\partial^3 \rho}{\partial x_2^3} + C_5 \frac{v_3\delta_l^3 \rho}{12\omega_{10}\omega_7\delta_t\omega_{16}} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& C_6 \frac{\delta_l^3 \rho v_2}{6\omega_7^2\delta_t\omega_{16}} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4\delta_l^3}{6\omega_6^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_3} + (-2\omega_{13} + 2\omega_6 - \omega_6^2 + \omega_{13}\omega_6) \frac{c_s^2\delta_l^3\rho v_1}{\omega_{13}\omega_6^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2\partial x_3} + \\
& (-\omega_{11}\omega_{18}\omega_6^2 + 12\omega_{11}\omega_{18}\omega_6 - 12\omega_{11}\omega_{18} - 12\omega_{11}\omega_6 + 12\omega_{11}\omega_6^2 - 12\omega_{18}\omega_6) \frac{v_3c_s^2\delta_l^3\rho}{6\omega_{11}\omega_{18}\omega_6^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2\partial x_3} + \\
& (-\omega_8\omega_6 - \omega_7\omega_6^2 - \omega_7\omega_8 + \omega_6^2 + \omega_7\omega_6 + \omega_7\omega_8\omega_6) \frac{c_s^2\delta_l^3\rho v_2}{\omega_7\omega_8\omega_6^2\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_2\partial x_3} + \\
& (-\omega_8\omega_6 - \omega_7^2\omega_6 + \omega_7^2 - \omega_7\omega_8 + \omega_7\omega_6 + \omega_7\omega_8\omega_6) \frac{c_s^2\delta_l^3\rho v_1}{\omega_7^2\omega_8\omega_6\delta_t} \frac{\partial^3 v_2}{\partial x_1\partial x_2\partial x_3} + (-12 + 12\omega_7 - \omega_7^2) \frac{c_s^4\delta_l^3}{6\omega_7^2\delta_t} \frac{\partial^3 \rho}{\partial x_2^3\partial x_3} + \\
& (2\omega_7 - \omega_7^2 + \omega_7\omega_{16} - 2\omega_{16}) \frac{c_s^2\delta_l^3\rho v_2}{\omega_7^2\delta_t\omega_{16}} \frac{\partial^3 v_2}{\partial x_2^3\partial x_3} + \\
& (-12\omega_7^2\omega_{11} + 12\omega_7^2 + 12\omega_7\omega_{11}\omega_{19} - 12\omega_{11}\omega_{19} - 12\omega_7\omega_{19} - \omega_7^2\omega_{11}\omega_{19} + 12\omega_7\omega_{11}) \frac{v_3c_s^2\delta_l^3\rho}{6\omega_7^2\omega_{11}\omega_{19}\delta_t} \frac{\partial^3 v_3}{\partial x_2^2\partial x_3} + \\
& C_7 \frac{v_3\delta_l^3 v_1}{\omega_{11}^2\omega_{18}\omega_6\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_3^2} + C_8 \frac{v_3\delta_l^3 \rho}{12\omega_{11}^2\omega_{18}\omega_6^2\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_3^2} + C_9 \frac{\delta_l^3 \rho v_1}{\omega_{11}^2\omega_{18}\omega_6\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_3^2} + C_{10} \frac{v_3\delta_l^3 v_2}{\omega_7\omega_{11}^2\omega_{19}\delta_t} \frac{\partial^3 \rho}{\partial x_2\partial x_3^2} + \\
& C_{11} \frac{v_3\delta_l^3 \rho}{12\omega_7^2\omega_{11}^2\omega_{19}\delta_t} \frac{\partial^3 v_2}{\partial x_2\partial x_3^2} + C_{12} \frac{\delta_l^3 \rho v_2}{\omega_7\omega_{11}^2\omega_{19}\delta_t} \frac{\partial^3 v_3}{\partial x_2\partial x_3^2} + C_{13} \frac{\delta_l^3}{12\omega_{11}^2\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-24 - 60v_3^2\omega_{11} + 36c_s^2 + 24\omega_{11} + 11v_3^2\omega_{11}^2 + 60v_3^2 - 36c_s^2\omega_{11} + 5c_s^2\omega_{11}^2 - 4\omega_{11}^2) \frac{v_3\delta_l^3\rho}{6\omega_{11}^2\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{v_3\delta_l^4}{24\omega_{13}^2\omega_9^2\omega_6^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{v_3\delta_l^4 \rho v_1}{12\omega_{13}^2\omega_9^2\omega_6^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{\delta_l^4 \rho}{24\omega_{13}^2\omega_6^3\delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + C_{17} \frac{v_3\delta_l^4 v_2 v_1}{4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^3\partial x_2} + \\
& C_{18} \frac{v_3\delta_l^4 \rho v_2}{4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^3\partial x_2} + C_{19} \frac{v_3\delta_l^4 \rho v_1}{12\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_{12}\omega_6^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^3\partial x_2} + C_{20} \frac{\delta_l^4 \rho v_2 v_1}{2\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2\delta_t} \frac{\partial^4 v_3}{\partial x_1^3\partial x_2} + \\
& C_{21} \frac{v_3c_s^4\delta_l^4}{6\omega_7^2\omega_8^2\omega_6^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2\partial x_2^2} + C_{22} \frac{v_3c_s^2\delta_l^4 \rho v_1}{2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}\omega_6^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2^2} + C_{23} \frac{v_3c_s^2\delta_l^4 \rho v_2}{2\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}\omega_6^2\delta_t\omega_{16}} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2^2} + \\
& C_{24} \frac{c_s^2\delta_l^4 \rho}{2\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8^2\omega_6^3\delta_t\omega_{16}} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2^2} + C_{25} \frac{v_3\delta_l^4 v_2 v_1}{4\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15}\omega_6\delta_t\omega_{16}^2} \frac{\partial^4 \rho}{\partial x_1\partial x_2^2} + C_{26} \frac{v_3\delta_l^4 \rho v_2}{12\omega_{10}^2\omega_7^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}\omega_6^2\delta_t\omega_{16}^2} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2} + \\
& C_{27} \frac{v_3\delta_l^4 \rho v_1}{4\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15}\omega_6\delta_t\omega_{16}^2} \frac{\partial^4 v_2}{\partial x_1\partial x_2^2} + C_{28} \frac{\delta_l^4 \rho v_2 v_1}{2\omega_7^2\omega_{17}\omega_8^2\omega_6^2\delta_t\omega_{16}^2} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2} + C_{29} \frac{v_3\delta_l^4}{24\omega_{10}^2\omega_7^2\delta_t\omega_{16}^2} \frac{\partial^4 \rho}{\partial x_2^2} + C_{30} \frac{v_3\delta_l^4 \rho v_2}{12\omega_{10}^2\omega_7^2\delta_t\omega_{16}^2} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& C_{31} \frac{\delta_l^4 \rho}{24\omega_7^2\delta_t\omega_{16}^2} \frac{\partial^4 v_3}{\partial x_2^2} + C_{32} \frac{\delta_l^4 v_1}{12\omega_{13}^2\omega_{11}\omega_{18}\omega_9^2\omega_6^2\omega_{22}\delta_t} \frac{\partial^4 \rho}{\partial x_1^3\partial x_3} + C_{33} \frac{\delta_l^4 \rho}{12\omega_{13}^2\omega_{11}\omega_{18}\omega_9^2\omega_6^2\omega_{22}\delta_t} \frac{\partial^4 v_1}{\partial x_1^3\partial x_3} + \\
& C_{34} \frac{v_3\delta_l^4 \rho v_1}{12\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9^2\omega_6^2\omega_{22}\delta_t} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + C_{35} \frac{\delta_l^4}{2\omega_{13}\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2\omega_{18}\omega_9^2\omega_{22}\omega_{19}\delta_t} \frac{\partial^4 \rho}{\partial x_1^2\partial x_2\partial x_3} + \\
& C_{36} \frac{\delta_l^4 \rho}{2\omega_{13}^2\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2\omega_{18}\omega_9^2\omega_{22}\omega_{19}\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2\partial x_3} + C_{37} \frac{\delta_l^4 \rho}{12\omega_{13}\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2\omega_{18}\omega_9^2\omega_{22}\omega_{19}\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2\partial x_3} + \\
& C_{38} \frac{v_3\delta_l^4 \rho}{2\omega_{13}\omega_7^2\omega_{20}\omega_{11}^2\omega_{14}\omega_8^2\omega_{18}\omega_9^2\omega_{22}\omega_{19}\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2\partial x_3} + C_{39} \frac{\delta_l^4 \rho}{2\omega_7^2\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8^2\omega_{18}\omega_9^2\omega_{19}\delta_t\omega_{16}} \frac{\partial^4 \rho}{\partial x_1\partial x_2^2\partial x_3} + \\
& C_{40} \frac{\delta_l^4 \rho}{12\omega_7^2\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8^2\omega_{18}\omega_9^2\omega_{19}\delta_t\omega_{16}} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2\partial x_3} + C_{41} \frac{\delta_l^4 \rho v_2}{\omega_7^2\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8^2\omega_{18}\omega_9^2\omega_{19}\delta_t\omega_{16}^2} \frac{\partial^4 v_2}{\partial x_1\partial x_2^2\partial x_3} + \\
& C_{42} \frac{\delta_l^4 \rho}{2\omega_7^2\omega_{23}\omega_{20}\omega_{17}\omega_{11}^2\omega_8^2\omega_{18}\omega_9^2\omega_{19}\delta_t\omega_{16}} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2\partial x_3} + C_{43} \frac{\delta_l^4 v_2}{12\omega_{10}^2\omega_7^2\omega_{23}\omega_{11}\omega_{19}\delta_t\omega_{16}^2} \frac{\partial^4 \rho}{\partial x_2^2\partial x_3} + \\
& C_{44} \frac{\delta_l^4 \rho}{12\omega_{10}^2\omega_7^2\omega_{23}\omega_{11}\omega_{19}\delta_t\omega_{16}^2} \frac{\partial^4 v_2}{\partial x_2^2\partial x_3} + C_{45} \frac{v_3\delta_l^4 \rho v_2}{12\omega_{10}^2\omega_7^2\omega_{23}\omega_{11}^2\omega_{19}\delta_t\omega_{16}^2} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3} + C_{46} \frac{v_3\delta_l^4}{12\omega_{13}\omega_{11}^2\omega_{18}\omega_6^2\omega_{22}\delta_t} \frac{\partial^4 \rho}{\partial x_1^2\partial x_3^2} + \\
& C_{47} \frac{v_3\delta_l^4 \rho v_1}{2\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9\omega_6^2\omega_{22}\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + C_{48} \frac{\delta_l^4 \rho}{12\omega_{13}\omega_{11}^2\omega_{18}\omega_6^2\omega_{22}\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_3^2} + C_{49} \frac{v_3\delta_l^4 v_2 v_1}{\omega_7^2\omega_{20}\omega_{11}^2\omega_{18}\omega_9^2\omega_{19}\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{50} \frac{v_3\delta_l^4 \rho v_2}{2\omega_7^2\omega_{20}\omega_{11}^2\omega_{18}\omega_9^2\omega_{19}\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2\partial x_3^2} + C_{51} \frac{v_3\delta_l^4 \rho v_1}{2\omega_7^2\omega_{20}\omega_{11}^2\omega_{18}\omega_9^2\omega_{19}\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{52} \frac{\delta_l^4 \rho v_2 v_1}{\omega_7^2\omega_{20}\omega_{11}^2\omega_{18}\omega_9^2\omega_{19}\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_2\partial x_3^2} + C_{53} \frac{v_3\delta_l^4}{12\omega_7^2\omega_{23}\omega_{11}^2\omega_{19}\delta_t\omega_{16}} \frac{\partial^4 \rho}{\partial x_2^2\partial x_3^2} + C_{54} \frac{v_3\delta_l^4 \rho v_2}{2\omega_{10}\omega_7^2\omega_{23}\omega_{11}^2\omega_{19}\delta_t\omega_{16}^2} \frac{\partial^4 v_2}{\partial x_2^2\partial x_3^2} + \\
& C_{55} \frac{\delta_l^4 \rho}{12\omega_7^2\omega_{23}\omega_{11}^2\omega_{19}\delta_t\omega_{16}} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3^2} + C_{56} \frac{\delta_l^4 v_1}{4\omega_{11}^3\omega_{18}\omega_6^2\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^3} + C_{57} \frac{\delta_l^4 \rho}{12\omega_{11}^3\omega_{18}\omega_6^3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_3^3} + C_{58} \frac{v_3\delta_l^4 \rho v_1}{4\omega_{11}^3\omega_{18}\omega_6^2\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_3^3} + \\
& C_{59} \frac{\delta_l^4 v_2}{4\omega_{11}^2\omega_{19}\delta_t} \frac{\partial^4 \rho}{\partial x_2\partial x_3^3} + C_{60} \frac{\delta_l^4 \rho}{12\omega_7^2\omega_{11}^2\omega_{19}\delta_t} \frac{\partial^4 v_2}{\partial x_2\partial x_3^3} + C_{61} \frac{v_3\delta_l^4 \rho v_2}{4\omega_7^2\omega_{11}^2\omega_{19}\delta_t} \frac{\partial^4 v_3}{\partial x_2\partial x_3^3} + C_{62} \frac{v_3\delta_l^4}{12\omega_{11}^3\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{63} \frac{\delta_l^4 \rho}{12\omega_{11}^3\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -18\omega_{13}c_s^2\omega_6 - 6\omega_{13}\omega_6v_1^2 - 12\omega_{13} + 18c_s^2\omega_9\omega_6 + 6\omega_9\omega_6v_1^2 + 3\omega_{13}c_s^2\omega_9\omega_6 + \omega_{13}\omega_9\omega_6v_1^2 - 6\omega_9\omega_6 - 36c_s^2\omega_9 - 12\omega_9v_1^2 + 36\omega_{13}c_s^2 + 12\omega_9 + 12\omega_{13}v_1^2 + 6\omega_{13}\omega_6 - \omega_{13}\omega_9\omega_6 \\
C_2 &= -6\omega_{13}c_s^2\omega_6 - 18\omega_{13}\omega_6v_1^2 - 12\omega_{13} + 6c_s^2\omega_9\omega_6 + 18\omega_9\omega_6v_1^2 + \omega_{13}c_s^2\omega_9\omega_6 + 3\omega_{13}\omega_9\omega_6v_1^2 - 6\omega_9\omega_6 - 12c_s^2\omega_9 - 36\omega_9v_1^2 + 12\omega_{13}c_s^2 + 12\omega_9 + 36\omega_{13}v_1^2 - 6\omega_{13}\omega_6 - \omega_{13}\omega_9\omega_6 \\
C_3 &= 15\omega_{13}c_s^2\omega_6 + 3\omega_{13}\omega_6v_1^2 + 3\omega_6^2v_1^2 - 12\omega_{13}c_s^2 - 3\omega_{13}c_s^2\omega_6^2 + \omega_{13}\omega_6^2 - 6\omega_6v_1^2 - 6c_s^2\omega_6 + 3c_s^2\omega_6^2 + 6\omega_6 - 3\omega_6^2 - 3\omega_{13}\omega_6 - \omega_{13}\omega_6^2v_1^2
\end{aligned}$$

$$C_4 = -36\omega_{10}c_s^2 + 12\omega_{10} - 6\omega_{10}\omega_7 - 18\omega_7c_s^2\omega_{16} + 3\omega_{10}\omega_7c_s^2\omega_{16} - 6\omega_7v_2^2\omega_{16} + \omega_{10}\omega_7v_2^2\omega_{16} + 18\omega_{10}\omega_7c_s^2 + 6\omega_7\omega_{16} - \omega_{10}\omega_7\omega_{16} - 12\omega_{10}v_2^2 + 12v_2^2\omega_{16} + 6\omega_{10}\omega_7v_2^2 + 36c_s^2\omega_{16} - 12\omega_{16}$$

$$C_5 = -12\omega_{10}c_s^2 + 12\omega_{10} - 6\omega_{10}\omega_7 - 6\omega_7c_s^2\omega_{16} + \omega_{10}\omega_7c_s^2\omega_{16} - 18\omega_7v_2^2\omega_{16} + 3\omega_{10}\omega_7v_2^2\omega_{16} + 6\omega_{10}\omega_7c_s^2 + 6\omega_7\omega_{16} - \omega_{10}\omega_7\omega_{16} - 36\omega_{10}v_2^2 + 36v_2^2\omega_{16} + 18\omega_{10}\omega_7v_2^2 + 12c_s^2\omega_{16} - 12\omega_{16}$$

$$C_6 = 6\omega_7 + 3\omega_7^2v_2^2 + 15\omega_7c_s^2\omega_{16} + 3\omega_7v_2^2\omega_{16} - 3\omega_7^2 + \omega_7^2\omega_{16} - 6\omega_7c_s^2 - \omega_7^2v_2^2\omega_{16} - 3\omega_7\omega_{16} + 3\omega_7^2c_s^2 - 6\omega_7v_2^2 - 12c_s^2\omega_{16} - 3\omega_7^2c_s^2\omega_{16}$$

$$C_7 = v_3^2\omega_{11}^2\omega_6 - v_3\omega_{11}\omega_{18}\omega_6 + 3c_s^2\omega_{11}\omega_{18} - \omega_{11}^2\omega_6 + v_3^2\omega_{11}\omega_{18} - v_3\omega_{11}^2 + 3c_s^2\omega_{11}^2\omega_6 + \omega_{11}\omega_{18}\omega_6 - \omega_{11}\omega_{18} + 3c_s^2\omega_{18}\omega_6 - 3c_s^2\omega_{11}\omega_{18}\omega_6 - 3c_s^2\omega_{11}\omega_6 + \omega_{11}\omega_6 + v_3\omega_{18}\omega_6 - 3c_s^2\omega_{11}^2 - \omega_{18}\omega_6 - v_3\omega_{11}\omega_6 + \omega_{11}^2$$

$$C_8 = -12v_3^2\omega_{11}^2\omega_6 + 6\omega_{11}\omega_{18}\omega_6^2 + 12\omega_{11}^2\omega_6 + 12c_s^2\omega_{11}^2\omega_6^2 - 11c_s^2\omega_{11}^2\omega_{18}\omega_6^2 + 42c_s^2\omega_{11}^2\omega_{18}\omega_6 - 12\omega_{11}^2\omega_6^2 - 12c_s^2\omega_{11}^2\omega_6 + 12v_3^2\omega_{11}^2\omega_6^2 - 6v_3^2\omega_{11}\omega_{18}\omega_6^2 - 12\omega_{18}\omega_6^2 - 24c_s^2\omega_{11}\omega_{18}\omega_6 - 12v_3^2\omega_{11}\omega_6^2 - 3v_3^2\omega_{11}^2\omega_{18}\omega_6^2 - 6\omega_{11}^2\omega_{18}\omega_6 + 12\omega_{11}\omega_6^2 + 12v_3^2\omega_{18}\omega_6^2 - 12c_s^2\omega_{11}\omega_6^2 + 6v_3^2\omega_{11}^2\omega_{18}\omega_6 + 3\omega_{11}^2\omega_{18}\omega_6^2 + 36c_s^2\omega_{18}\omega_6^2 - 18c_s^2\omega_{11}\omega_{18}\omega_6^2 - 24c_s^2\omega_{11}^2\omega_{18}$$

$$C_9 = 3v_3^2\omega_{11}^2\omega_6 - 3v_3\omega_{11}\omega_{18}\omega_6 + c_s^2\omega_{11}\omega_{18} - \omega_{11}^2\omega_6 + 3v_3^2\omega_{11}\omega_{18} - 3v_3\omega_{11}^2 + c_s^2\omega_{11}^2\omega_6 + \omega_{11}\omega_{18}\omega_6 - \omega_{11}\omega_{18} + c_s^2\omega_{18}\omega_6 - c_s^2\omega_{11}\omega_{18}\omega_6 - c_s^2\omega_{11}\omega_6 + \omega_{11}\omega_6 + 3v_3\omega_{18}\omega_6 - c_s^2\omega_{11}^2 - \omega_{18}\omega_6 - 3v_3\omega_{11}\omega_6 + \omega_{11}^2$$

$$C_{10} = 3\omega_7c_s^2\omega_{19} - 3\omega_7c_s^2\omega_{11}\omega_{19} + 3\omega_7c_s^2\omega_{11}^2 - \omega_7v_3^2\omega_{11}\omega_{19} - v_3^2\omega_{11}^2 + \omega_7\omega_{11}\omega_{19} - 3\omega_7c_s^2\omega_{11} - \omega_{11}\omega_{19} + \omega_7v_3^2\omega_{19} + \omega_7v_3^2\omega_{11}^2 + v_3^2\omega_{11}\omega_{19} - \omega_7\omega_{11}^2 - \omega_7\omega_{19} + \omega_7\omega_{11} - \omega_7v_3^2\omega_{11} - 3c_s^2\omega_{11}^2 + \omega_{11}^2 + 3c_s^2\omega_{11}\omega_{19}$$

$$C_{11} = -24\omega_7c_s^2\omega_{11}\omega_{19} - 12\omega_7c_s^2\omega_{11}^2 - 12\omega_7^2v_3^2\omega_{11} - 24c_s^2\omega_{11}^2\omega_{19} + 12\omega_7^2\omega_{11} - 3\omega_7^2v_3^2\omega_{11}^2\omega_{19} - 12\omega_7^2\omega_{11}^2 + 3\omega_7^2\omega_{11}^2\omega_{19} - 12\omega_7^2\omega_{19} + 12\omega_7^2v_3^2\omega_{11}^2 + 12\omega_7^2v_3^2\omega_{19} - 11\omega_7^2c_s^2\omega_{11}^2\omega_{19} - 6\omega_7\omega_{11}^2\omega_{19} - 18\omega_7^2c_s^2\omega_{11}\omega_{19} - 12\omega_7v_3^2\omega_{11}^2\omega_{19} + 6\omega_7v_3^2\omega_{11}^2\omega_{19} - 12\omega_7^2c_s^2\omega_{11} + 12\omega_7\omega_{11}^2 + 6\omega_7^2\omega_{11}\omega_{19} + 12\omega_7^2c_s^2\omega_{11} + 36\omega_7^2c_s^2\omega_{19} - 6\omega_7^2v_3^2\omega_{11}\omega_{19} + 42\omega_7c_s^2\omega_{11}^2\omega_{19}$$

$$C_{12} = \omega_7c_s^2\omega_{19} - \omega_7c_s^2\omega_{11}\omega_{19} + \omega_7c_s^2\omega_{11}^2 - 3\omega_7v_3^2\omega_{11}\omega_{19} - 3v_3^2\omega_{11}^2 + \omega_7\omega_{11}\omega_{19} - \omega_7c_s^2\omega_{11} - \omega_{11}\omega_{19} + 3\omega_7v_3^2\omega_{19} + 3\omega_7v_3^2\omega_{11}^2 + 3v_3^2\omega_{11}\omega_{19} - \omega_7\omega_{11}^2 - \omega_7\omega_{19} + \omega_7\omega_{11} - 3\omega_7v_3^2\omega_{11} - c_s^2\omega_{11}^2 + \omega_{11}^2 + c_s^2\omega_{11}\omega_{19}$$

$$C_{13} = -12c_s^4\omega_{11} + 36v_3^2\omega_{11} - 12c_s^2 + c_s^4\omega_{11}^2 - 7v_3^2\omega_{11}^2 - 36v_3^2 + 12c_s^2\omega_{11} - 36v_3^4\omega_{11} + 144v_3^2c_s^2 + 36v_3^4 - 144v_3^2c_s^2\omega_{11} + 24v_3^2c_s^2\omega_{11}^2 + 12c_s^4 - c_s^2\omega_{11}^2 + 7v_3^4\omega_{11}^2$$

$$C_{14} = -432\omega_{13}^2c_s^2\omega_9\omega_6v_1^2 - \omega_{13}^2c_s^4\omega_9^2\omega_6^2 - 96\omega_{13}^2\omega_9\omega_6v_1^4 + 48\omega_{13}^2\omega_9^2v_1^2 + 72\omega_{13}^2\omega_6v_1^4 - 12\omega_9^2\omega_6^2v_1^2 - 144c_s^2\omega_9^2\omega_6v_1^2 - 126\omega_{13}^2c_s^2\omega_9^2\omega_6^2v_1^2 - 12\omega_{13}^2c_s^4\omega_6^2 + 36\omega_{13}^2\omega_6^2v_1^2 - 3\omega_{13}^2\omega_9^2\omega_6^2v_1^4 + 288\omega_{13}^2c_s^2\omega_6v_1^2 - 24\omega_{13}^2c_s^4\omega_9^2 - 24\omega_9^2\omega_6v_1^4 - 12\omega_{13}^2c_s^2\omega_9^2\omega_6^2v_1^2 - 24\omega_{13}^2c_s^2\omega_9 - 144\omega_{13}^2c_s^2\omega_9\omega_6v_1^2 - 36\omega_{13}^2\omega_9\omega_6^2v_1^2 - 48\omega_{13}^2\omega_9v_1^2 + 48\omega_{13}^2\omega_9\omega_6v_1^2 + \omega_{13}^2c_s^2\omega_9^2\omega_6^2 + 96\omega_{13}^2\omega_9^2\omega_6v_1^4 + 30\omega_{13}^2\omega_9^2\omega_6^2v_1^2 + 24\omega_{13}^2c_s^4\omega_6 + 24\omega_{13}^2\omega_9\omega_6^2v_1^4 + 24\omega_{13}^2c_s^2\omega_9 - 96\omega_{13}^2\omega_9^2\omega_6v_1^2 - 12\omega_{13}^2c_s^4\omega_9^2\omega_6^2 + 24\omega_{13}^2c_s^4\omega_9 - 48\omega_{13}^2\omega_9\omega_6v_1^4 - 24c_s^4\omega_9^2\omega_6 - 48\omega_{13}^2c_s^4\omega_9\omega_6 - 24\omega_{13}^2\omega_9\omega_6^2v_1^2 - 12c_s^2\omega_9^2\omega_6^2 - 48\omega_{13}^2c_s^2\omega_9^2\omega_6 - 14\omega_{13}^2c_s^2\omega_9\omega_6^2 - 216\omega_{13}^2c_s^2\omega_9^2v_1^2 - 30\omega_{13}^2\omega_9^2\omega_6^2v_1^4 + 12\omega_{13}^2c_s^2\omega_6^2 - 72\omega_{13}^2\omega_6v_1^2 - 48\omega_{13}^2\omega_6^2v_1^4 + 12\omega_9^2\omega_6^2v_1^2 + 24\omega_{13}^2c_s^2\omega_6 - 144\omega_{13}^2c_s^2\omega_6^2v_1^2 + 72\omega_{13}^2c_s^2\omega_9\omega_6^2v_1^2 + 216\omega_{13}^2c_s^2\omega_9v_1^2 + 12\omega_{13}^2c_s^2\omega_9^2\omega_6^2 + 24c_s^2\omega_9^2\omega_6 + 48\omega_{13}^2c_s^2\omega_9\omega_6 + 96\omega_{13}^2\omega_9\omega_6v_1^2 + 12c_s^4\omega_9^2\omega_6^2 + 48\omega_{13}^2c_s^4\omega_9^2\omega_6 + 150\omega_{13}^2c_s^2\omega_9\omega_6^2v_1^2 + 48\omega_{13}^2\omega_9v_1^4 + 36\omega_{13}^2\omega_9\omega_6^2v_1^4 + 14\omega_{13}^2c_s^4\omega_9\omega_6^2 + 3\omega_{13}^2\omega_9^2\omega_6^2v_1^2 - 36\omega_{13}^2\omega_6^2v_1^4 + 432\omega_{13}^2c_s^2\omega_9\omega_6v_1^2 + 24\omega_9^2\omega_6v_1^2 + 72c_s^2\omega_9^2\omega_6^2v_1^2$$

$$C_{15} = -84\omega_{13}^2\omega_9^2v_1^2 + 24\omega_9^2\omega_6^2v_1^2 - 72\omega_{13}^2\omega_9^2\omega_6 - 60\omega_{13}^2\omega_6^2v_1^2 + 12\omega_{13}^2c_s^2\omega_9\omega_6^2 + 60\omega_{13}^2c_s^2\omega_9 + 72\omega_{13}^2\omega_9\omega_6 - 48\omega_{13}^2\omega_6 + 61\omega_{13}^2\omega_9\omega_6^2v_1^2 + 84\omega_{13}^2\omega_9v_1^2 - 24\omega_{13}^2c_s^2\omega_9\omega_6 - 72\omega_{13}^2\omega_9\omega_6v_1^2 - 25\omega_{13}^2\omega_9\omega_6^2 + 24\omega_{13}^2\omega_6^2 - 3\omega_{13}^2c_s^2\omega_9^2\omega_6^2 + 36\omega_{13}^2\omega_9^2 - 51\omega_{13}^2\omega_9^2\omega_6^2v_1^2 + 21\omega_{13}^2\omega_9^2\omega_6^2 - 12\omega_{13}^2\omega_9\omega_6^2 - 60\omega_{13}^2c_s^2\omega_9^2 + 168\omega_{13}^2\omega_9^2\omega_6v_1^2 + 2\omega_{13}^2\omega_9^2\omega_6^2 + 36\omega_{13}^2\omega_9\omega_6^2v_1^2 + 24\omega_9^2\omega_6 + 24c_s^2\omega_9^2\omega_6^2 + 120\omega_{13}^2c_s^2\omega_9^2\omega_6 + 39\omega_{13}^2c_s^2\omega_9\omega_6^2 - 36\omega_{13}^2c_s^2\omega_6^2 - 36\omega_{13}^2\omega_9 + 120\omega_{13}^2\omega_6v_1^2 + 72\omega_{13}^2c_s^2\omega_6 - 33\omega_{13}^2c_s^2\omega_9^2\omega_6^2 - 12\omega_9^2\omega_6^2 - 48c_s^2\omega_9^2\omega_6 - 120\omega_{13}^2c_s^2\omega_9\omega_6 - 168\omega_{13}^2\omega_9\omega_6v_1^2 - 5\omega_{13}^2\omega_9^2\omega_6^2v_1^2 + 24\omega_{13}^2\omega_9\omega_6 - 48\omega_9^2\omega_6v_1^2$$

$$C_{16} = -24\omega_{13}^2c_s^2\omega_6 + 48\omega_{13}^2\omega_6v_1^2 - 12\omega_{13}^2c_s^2\omega_9^3v_1^2 - 12\omega_6^3v_1^2 + 24\omega_{13}^2\omega_6v_1^4 + 24\omega_{13}^2c_s^4\omega_6^2 + 24\omega_{13}^2\omega_6^2v_1^2 - 24c_s^2\omega_6^2v_1^2 + 156\omega_{13}^2c_s^2\omega_6v_1^2 - 3\omega_{13}^2c_s^4\omega_6^3 + 72\omega_{13}^2\omega_6^2v_1^4 + 24\omega_6^2v_1^2 + 48\omega_{13}^2c_s^2\omega_6^2v_1^2 - 6\omega_{13}^2c_s^2\omega_6^3 - 18\omega_{13}^2\omega_6^3v_1^4 + 24\omega_{13}^2c_s^4 - 48\omega_{13}^2c_s^4\omega_6 + 24\omega_{13}^2c_s^2\omega_6^2 - 3\omega_{13}^2\omega_6^3v_1^2 + 12c_s^2\omega_6^3v_1^2 - 24\omega_6^3v_1^4 + \omega_{13}^2c_s^2\omega_6^3 + 6\omega_{13}^2c_s^2\omega_6^2v_1^2 + 24\omega_{13}^2c_s^2\omega_6v_1^2 + 3\omega_{13}^2\omega_6^3v_1^2 - 8\omega_{13}^2c_s^2\omega_6^2 - 18\omega_{13}^2c_s^2\omega_6v_1^2 + 18\omega_{13}^2\omega_6^3v_1^2 - 8\omega_{13}^2c_s^2\omega_6^2 - 96\omega_{13}^2c_s^2v_1^2 - 24\omega_{13}^2\omega_6v_1^2 + 12\omega_{13}^2c_s^2\omega_6 - 72\omega_{13}^2c_s^2\omega_6^2v_1^2 - 24\omega_{13}^2c_s^4\omega_6^2 - 48\omega_{13}^2\omega_6v_1^4 + 12\omega_6^3v_1^4 - 72\omega_{13}^2\omega_6^2v_1^2 - 24\omega_{13}^2\omega_6^2v_1^4 + 6\omega_{13}^2c_s^4\omega_6^3$$

$$C_{17} = -4\omega_{13}^2\omega_7\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 - 12\omega_{13}^2\omega_7c_s^2\omega_5\omega_9^2\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12} - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_9^2\omega_6^2 - 6\omega_{13}\omega_7c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}^2c_s^2\omega_5\omega_9^2\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_7\omega_5\omega_9^2\omega_{12}\omega_6v_1^2 + 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_6 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2v_1^2 + 2\omega_{13}^2\omega_7\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2v_1^2 + 2\omega_{13}\omega_7\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 6\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_7\omega_5\omega_9^2\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_{12}\omega_6v_1^2 - 24\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 + 4\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12} + 6\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9^2\omega_6^2 - 12\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 2\omega_{13}^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2v_1^2 + 4\omega_{13}^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2v_1^2 - 12\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12} - 12\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_9^2\omega_6^2 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6 + 3\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2v_1^2 - 4\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6v_1^2 + 6\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_9^2\omega_6v_1^2 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12} + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7\omega_5\omega_9^2\omega_{12}\omega_6 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6v_1^2 + 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_6v_1^2 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_6 + 9\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9^2\omega_6 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6v_1^2 + 12\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 + 8\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6v_1^2 - 12\omega_{13}^2c_s^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7\omega_{14}\omega_5\omega_9\omega_{12}\omega_6 + 2\omega_{13}\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2v_1^2 + 12\omega_{13}^2\omega_7c_s^2\omega_5\omega_9^2\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5^2\omega_6 - 2\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2v_1^2 + 12\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 + 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2v_1^2 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_6v_1^2 + 6\omega_{13}^2\omega_7c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2v_1^2 + 2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 6\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 12\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 - 6\omega_{13}^2c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2v_1^2 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_{12}\omega_6^2v_1^2 - 3\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 2\omega_{13}^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_{12}\omega_6 + 24\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 9\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6^2 +$$

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$$6\omega_7 c_s^2 \omega_{11}^3 \omega_{19}^2 + 12\omega_7^3 v_3^2 \omega_{11}^2 + 162\omega_7^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{19}^2 - 306\omega_7^3 v_3^2 c_s^2 \omega_{11} \omega_{19}^2 + 12\omega_7^2 c_s^2 \omega_{11} \omega_{19}^2 + 12\omega_7^3 v_3^2 c_s^2 \omega_{11}^3 - 12\omega_7^2 v_3^4 \omega_{11}^3 - 48\omega_7 v_3^2 c_s^2 \omega_{11}^2 \omega_{19}^2 + 30\omega_7^2 v_3^2 c_s^2 \omega_{11}^3 \omega_{19} + 24\omega_7 v_3^2 \omega_{11}^3 \omega_{19} + 12\omega_7 c_s^4 \omega_{11}^3 \omega_{19} - 36\omega_7^3 v_3^4 \omega_{11} \omega_{19} - 12\omega_7^2 v_3^2 \omega_{11}^3$$

$$\begin{aligned} C_{61} = & -24\omega_7 \omega_{11} \omega_{19}^2 + 17\omega_7^2 \omega_{11}^3 \omega_{19} - 28v_3^2 \omega_{11}^3 \omega_{19} + 25\omega_7^2 c_s^2 \omega_{11}^2 \omega_{19} - 12\omega_{11}^2 \omega_{19}^2 + 80\omega_7^2 v_3^2 \omega_{19}^2 - 16\omega_7 c_s^2 \omega_{11}^3 + 28v_3^2 \omega_{11}^2 \omega_{19}^2 - 25\omega_7^2 c_s^2 \omega_{11}^3 \omega_{19} - \\ & 17\omega_7^2 \omega_{11}^2 \omega_{19}^2 - 32\omega_7^2 \omega_{19}^2 + 12\omega_{11}^3 \omega_{19} + 104\omega_7^2 v_3^2 \omega_{11}^2 \omega_{19} + 64\omega_7 v_3^2 \omega_{11} \omega_{19}^2 + 43\omega_7^2 v_3^2 \omega_{11}^2 \omega_{19}^2 - 20c_s^2 \omega_{11}^3 \omega_{19} + 16\omega_7^2 v_3^2 \omega_{11}^3 + 8\omega_7^2 \omega_{11}^2 - \\ & 40\omega_7^2 \omega_{11}^2 \omega_{19} - 16\omega_7^2 v_3^2 \omega_{11}^2 - 43\omega_7^2 v_3^2 \omega_{11}^3 \omega_{19} + 20c_s^2 \omega_{11}^2 \omega_{19}^2 + 32\omega_7 c_s^2 \omega_{11} \omega_{19}^2 + 56\omega_7^2 c_s^2 \omega_{11}^2 \omega_{19} - 8\omega_7^2 \omega_{11}^3 - 16\omega_7 v_3^2 \omega_{11}^3 + 16\omega_7 \omega_{11}^2 \omega_{19} - \\ & 44\omega_7 c_s^2 \omega_{11}^2 \omega_{19}^2 - 32\omega_7^2 c_s^2 \omega_{11} \omega_{19} + 8\omega_7 \omega_{11}^3 - 120\omega_7^2 v_3^2 \omega_{11} \omega_{19}^2 - 48\omega_7 v_3^2 \omega_{11}^2 \omega_{19} + 48\omega_7^2 c_s^2 \omega_{19}^2 + 24\omega_7^2 \omega_{11} \omega_{19} + 44\omega_7 c_s^2 \omega_{11}^3 \omega_{19} - 16\omega_7^2 c_s^2 \omega_{11}^2 + \\ & 48\omega_7^2 \omega_{11} \omega_{19}^2 - 28\omega_7 \omega_{11}^3 \omega_{19} - 64\omega_7^2 v_3^2 \omega_{11} \omega_{19} - 68\omega_7 v_3^2 \omega_{11}^2 \omega_{19}^2 - 16\omega_7 c_s^2 \omega_{11}^2 \omega_{19} + 28\omega_7 \omega_{11}^2 \omega_{19}^2 - 72\omega_7^2 c_s^2 \omega_{11} \omega_{19}^2 + 16\omega_7^2 c_s^2 \omega_{11}^3 + 68\omega_7 v_3^2 \omega_{11}^3 \omega_{19} \end{aligned}$$

$$C_{62} = 12 - 216c_s^4 \omega_{11} + 234v_3^2 \omega_{11} - 132c_s^2 + 82c_s^4 \omega_{11}^2 - 18\omega_{11} - 98v_3^2 \omega_{11}^2 - 156v_3^2 + 10v_3^2 \omega_{11}^3 - 5c_s^4 \omega_{11}^3 + 198c_s^2 \omega_{11} - 216v_3^4 \omega_{11} + 672v_3^2 c_s^2 + 144v_3^4 - 1008v_3^2 c_s^2 \omega_{11} + 404v_3^2 c_s^2 \omega_{11}^2 - 9v_3^4 \omega_{11}^3 - \omega_{11}^3 + 6c_s^2 \omega_{11}^3 - 34v_3^2 c_s^2 \omega_{11}^3 + 144c_s^4 - 78c_s^2 \omega_{11}^2 + 90v_3^4 \omega_{11}^2 + 8\omega_{11}^2$$

$$C_{63} = 12 - 36c_s^4 \omega_{11} + 378v_3^2 \omega_{11} - 36c_s^2 + 14c_s^4 \omega_{11}^2 - 18\omega_{11} - 154v_3^2 \omega_{11}^2 - 252v_3^2 + 14v_3^2 \omega_{11}^3 - c_s^4 \omega_{11}^3 + 54c_s^2 \omega_{11} - 756v_3^4 \omega_{11} + 432v_3^2 c_s^2 + 504v_3^4 - 648v_3^2 c_s^2 \omega_{11} + 252v_3^2 c_s^2 \omega_{11}^2 - 29v_3^4 \omega_{11}^3 - \omega_{11}^3 + 2c_s^2 \omega_{11}^3 - 18v_3^2 c_s^2 \omega_{11}^3 + 24c_s^4 - 22c_s^2 \omega_{11}^2 + 310v_3^4 \omega_{11}^2 + 8\omega_{11}^2$$

2.3 MRT2

2.3.1 Definitions

Collision operator C :

$$C(f) = \mathbf{M}_2^{-1} \mathbf{S} \left(\mu_2^{(eq)} - \mathbf{M}_2 f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \dots, \omega_{27}),$$

$$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2).$$

Matrix \mathbf{M}_2 corresponds to the transformation matrix to the raw moment basis defined by

$$\mu_2 = \left(\begin{array}{c} m_{(0,0,0)} \\ m_{(1,0,0)} \\ m_{(0,1,0)} \\ m_{(0,0,1)} \\ m_{(1,1,0)} \\ m_{(1,0,1)} \\ m_{(0,1,1)} \\ m_{(2,0,0)} - m_{(0,2,0)} \\ m_{(2,0,0)} - m_{(0,0,2)} \\ m_{(2,0,0)} + m_{(0,2,0)} + m_{(0,0,2)} \\ m_{(1,2,0)} + m_{(1,0,2)} \\ m_{(2,1,0)} + m_{(0,1,2)} \\ m_{(2,0,1)} + m_{(0,2,1)} \\ m_{(1,2,0)} - m_{(1,0,2)} \\ m_{(2,1,0)} - m_{(0,1,2)} \\ m_{(2,0,1)} - m_{(0,2,1)} \\ m_{(1,1,1)} \\ m_{(2,2,0)} - 2m_{(2,0,2)} + m_{(0,2,2)} \\ m_{(2,2,0)} + m_{(2,0,2)} - 2m_{(0,2,2)} \\ m_{(2,2,0)} + m_{(2,0,2)} + m_{(0,2,2)} \\ m_{(2,1,1)} \\ m_{(1,2,1)} \\ m_{(1,1,2)} \\ m_{(2,2,1)} \\ m_{(2,1,2)} \\ m_{(1,2,2)} \\ m_{(2,2,2)} \end{array} \right)$$

and is given by

The equilibrium moments $\mu_2^{(eq)}$ are defined by

$$\mu_2^{(eq)} = \mathbf{M}_2 \mathbf{M}^{-1} \mu^{(eq)},$$

i.e.,

$$\mu_2^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho v_1 v_2 \\ \rho v_1 v_3 \\ \rho v_2 v_3 \\ \rho(v_1^2 - v_2^2) \\ \rho(v_1^2 - v_3^2) \\ \rho(v_3^2 + v_2^2 + v_1^2 + 3c_s^2) \\ \rho(v_1 v_3^2 + v_1 v_2^2 + 2c_s^2 v_1) \\ \rho(v_2 v_3^2 + v_1^2 v_2 + 2c_s^2 v_2) \\ \rho(v_2^2 v_3 + v_1^2 v_3 + 2c_s^2 v_3) \\ \rho(v_1 v_2^2 - v_1 v_3^2) \\ \rho(v_1^2 v_2 - v_2 v_3^2) \\ \rho(v_1^2 v_3 - v_2^2 v_3) \\ \rho v_1 v_2 v_3 \\ \rho(v_2^2 v_3^2 - 2v_1^2 v_3^2 - c_s^2 v_3^2 + v_1^2 v_2^2 + 2c_s^2 v_2^2 - c_s^2 v_1^2) \\ \rho(-2v_2^2 v_3^2 + v_1^2 v_3^2 - c_s^2 v_3^2 + v_1^2 v_2^2 - c_s^2 v_2^2 + 2c_s^2 v_1^2) \\ \rho(v_2^2 v_3^2 + v_1^2 v_3^2 + 2c_s^2 v_3^2 + v_1^2 v_2^2 + 2c_s^2 v_2^2 + 2c_s^2 v_1^2 + 3c_s^4) \\ \rho(v_1^2 v_2 v_3 + c_s^2 v_2 v_3) \\ \rho(v_1 v_2^2 v_3 + c_s^2 v_1 v_3) \\ \rho(v_1 v_2 v_3^2 + c_s^2 v_1 v_2) \\ \rho(v_1^2 v_2^2 v_3 + c_s^2 v_2^2 v_3 + c_s^2 v_1^2 v_3 + c_s^4 v_3) \\ \rho(v_1^2 v_2 v_3^2 + c_s^2 v_2 v_3^2 + c_s^2 v_1^2 v_2 + c_s^4 v_2) \\ \rho(v_1 v_2^2 v_3^2 + c_s^2 v_1 v_3^2 + c_s^2 v_1 v_2^2 + c_s^4 v_1) \\ \rho(v_1^2 v_2^2 v_3^2 + c_s^2 v_2^2 v_3^2 + c_s^2 v_1^2 v_3^2 + c_s^4 v_3^2 + c_s^2 v_1^2 v_2^2 + c_s^4 v_2^2 + c_s^4 v_1^2 + c_s^6) \end{pmatrix}.$$

2.3.2 Conservation of mass: ρ

$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{v_1 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\rho c_s^2 \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\rho c_s^2 \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_2 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\ & \frac{\rho c_s^2 \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho c_s^2 \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\rho c_s^2 \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\rho c_s^2 \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + v_3^2 + 3c_s^2) \frac{v_3 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\ & + (-3v_1^4 \omega_9 - c_s^4 \omega_9 + 24v_1^2 c_s^2 - 2c_s^2 - 6v_1^2 + 6v_1^4 + 2c_s^4 + c_s^2 \omega_9 + 3v_1^2 \omega_9 - 12v_1^2 c_s^2 \omega_9) \frac{\delta_l^4}{24 \omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 + 6c_s^2 + 10v_1^2 - 3c_s^2 \omega_9 - 5v_1^2 \omega_9 + 2\omega_9) \frac{\rho v_1 \delta_l^4}{12 \omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (3c_s^2 \omega_{12} - 3c_s^2 \omega_9 + v_1^2 \omega_{12} - v_1^2 \omega_9 + \omega_9 - \omega_{12}) \frac{v_2 v_1 \delta_l^4}{4 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} \\ & + (c_s^2 \omega_{12} - c_s^2 \omega_9 + 3v_1^2 \omega_{12} - 3v_1^2 \omega_9 + \omega_9 - \omega_{12}) \frac{v_2 \rho \delta_l^4}{4 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + (v_1^2 \omega_5 \omega_9 \omega_{12} - \omega_5 \omega_{12} - 3c_s^2 \omega_5 \omega_9 - \omega_5 \omega_9 \omega_{12} - \\ & 6c_s^2 \omega_9 \omega_{12} + 3\omega_5 \omega_9 + 3c_s^2 \omega_5 \omega_{12} + 3c_s^2 \omega_5 \omega_9 \omega_{12} - 3v_1^2 \omega_5 \omega_9 + v_1^2 \omega_5 \omega_{12}) \frac{\rho v_1 \delta_l^4}{12 \omega_5 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_5) \frac{c_s^4 \delta_l^4}{6 \omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\ & (\omega_5 - \omega_{12}) \frac{\rho v_1 c_s^2 \delta_l^4}{2 \omega_5 \omega_{12} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + (\omega_5 - \omega_{15}) \frac{v_2 \rho c_s^2 \delta_l^4}{2 \omega_5 \omega_{15} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\ & (\omega_{10} - 3\omega_{10} c_s^2 - \omega_{10} v_2^2 + 3c_s^2 \omega_{15} + v_2^2 \omega_{15} - \omega_{15}) \frac{v_2 v_1 \delta_l^4}{4 \omega_{10} \omega_{15} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + (\omega_{10} v_2^2 \omega_5 \omega_{15} - 6\omega_{10} c_s^2 \omega_{15} - \omega_{10} \omega_5 \omega_{15} + \\ & 3\omega_{10} \omega_5 + 3c_s^2 \omega_5 \omega_{15} - \omega_5 \omega_{15} - 3\omega_{10} c_s^2 \omega_5 - 3\omega_{10} v_2^2 \omega_5 + 3\omega_{10} c_s^2 \omega_5 \omega_{15} + v_2^2 \omega_5 \omega_{15}) \frac{v_2 \rho \delta_l^4}{12 \omega_{10} \omega_5 \omega_{15} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\ & (\omega_{10} - \omega_{10} c_s^2 - 3\omega_{10} v_2^2 + c_s^2 \omega_{15} + 3v_2^2 \omega_{15} - \omega_{15}) \frac{\rho v_1 \delta_l^4}{4 \omega_{10} \omega_{15} \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\ & (-6v_2^2 + \omega_{10} c_s^2 - 2c_s^2 + 3\omega_{10} v_2^2 + 2c_s^4 - 3\omega_{10} v_2^4 - 12\omega_{10} v_2^2 c_s^2 + 24v_2^2 c_s^2 + 6v_2^4 - \omega_{10} c_s^4) \frac{\delta_l^4}{24 \omega_{10} \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \end{aligned}$$

$$\begin{aligned}
& (-4 + 2\omega_{10} + 10v_2^2 - 3\omega_{10}c_s^2 + 6c_s^2 - 5\omega_{10}v_2^2) \frac{v_2\rho\delta_l^4}{12\omega_{10}\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-\omega_{13} + \omega_{13}v_1^2 + 3\omega_{13}c_s^2 - 3c_s^2\omega_9 - v_1^2\omega_9 + \omega_9) \frac{v_3v_1\delta_l^4}{4\omega_{13}\omega_9\delta_t} \frac{\partial^4 \rho}{\partial x_1^3\partial x_3} + \\
& (-\omega_{13} + 3\omega_{13}v_1^2 + \omega_{13}c_s^2 - c_s^2\omega_9 - 3v_1^2\omega_9 + \omega_9) \frac{v_3\rho\delta_l^4}{4\omega_{13}\omega_9\delta_t} \frac{\partial^4 v_1}{\partial x_1^3\partial x_3} + (3\omega_{13}c_s^2\omega_9\omega_6 + \omega_{13}v_1^2\omega_6 + \omega_{13}v_1^2\omega_9\omega_6 - \\
& 6\omega_{13}c_s^2\omega_9 + 3\omega_{13}c_s^2\omega_6 - \omega_{13}\omega_9\omega_6 - 3c_s^2\omega_9\omega_6 + 3\omega_9\omega_6 - \omega_{13}\omega_6 - 3v_1^2\omega_9\omega_6) \frac{\rho v_1\delta_l^4}{12\omega_{13}\omega_9\omega_6\delta_t} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + \\
& (-\omega_8 + \omega_5) \frac{v_3\rho c_s^2\delta_l^4}{2\omega_8\omega_5\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2\partial x_3} + (-\omega_8 + \omega_6) \frac{v_2\rho c_s^2\delta_l^4}{2\omega_8\omega_6\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2\partial x_3} + (-\omega_8 + \omega_5) \frac{v_3\rho c_s^2\delta_l^4}{2\omega_8\omega_5\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2\partial x_3} + \\
& (\omega_7 - \omega_8) \frac{\rho v_1 c_s^2\delta_l^4}{2\omega_7\omega_8\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2\partial x_3} + (-\omega_{16} + \omega_{10} + 3\omega_{16}c_s^2 - 3\omega_{10}c_s^2 - \omega_{10}v_2^2 + \omega_{16}v_2^2) \frac{v_2v_3\delta_l^4}{4\omega_{16}\omega_{10}\delta_t} \frac{\partial^4 \rho}{\partial x_3^3\partial x_3} + \\
& (-\omega_{16} + \omega_{10} + \omega_{16}c_s^2 - \omega_{10}c_s^2 - 3\omega_{10}v_2^2 + 3\omega_{16}v_2^2) \frac{v_3\rho\delta_l^4}{4\omega_{16}\omega_{10}\delta_t} \frac{\partial^4 v_2}{\partial x_3^3\partial x_3} + (-6\omega_{16}\omega_{10}c_s^2 - \omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7 + 3\omega_{10}\omega_7 + \\
& \omega_{16}\omega_{10}v_2^2\omega_7 + \omega_{16}v_2^2\omega_7 + 3\omega_{16}\omega_{10}\omega_7c_s^2 + 3\omega_{16}\omega_7c_s^2 - 3\omega_{10}v_2^2\omega_7 - 3\omega_{10}\omega_7c_s^2) \frac{v_2\rho\delta_l^4}{12\omega_{16}\omega_{10}\omega_7\delta_t} \frac{\partial^4 v_3}{\partial x_3^3\partial x_3} + \\
& (-2 + \omega_6) \frac{c_s^4\delta_l^4}{6\omega_6\delta_t} \frac{\partial^4 \rho}{\partial x_1^2\partial x_3^2} + (-\omega_{13} + \omega_6) \frac{\rho v_1 c_s^2\delta_l^4}{2\omega_{13}\omega_6\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + (-\omega_{18} + \omega_6) \frac{v_3\rho c_s^2\delta_l^4}{2\omega_{18}\omega_6\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_3^2} + \\
& (-\omega_8 + \omega_6) \frac{v_2\rho c_s^2\delta_l^4}{2\omega_8\omega_6\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2\partial x_3^2} + (\omega_7 - \omega_8) \frac{\rho v_1 c_s^2\delta_l^4}{2\omega_7\omega_8\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + (-2 + \omega_7) \frac{c_s^4\delta_l^4}{6\omega_7\delta_t} \frac{\partial^4 \rho}{\partial x_3^2\partial x_3^2} + (-\omega_{16} + \omega_7) \frac{v_2\rho c_s^2\delta_l^4}{2\omega_{16}\omega_7\delta_t} \frac{\partial^4 v_2}{\partial x_3^2\partial x_3^2} \\
& + (\omega_7 - \omega_{19}) \frac{v_3\rho c_s^2\delta_l^4}{2\omega_7\omega_{19}\delta_t} \frac{\partial^4 v_3}{\partial x_3^2\partial x_3^2} + (-v_3^2\omega_{11} + 3c_s^2\omega_{18} + \omega_{11} - \omega_{18} - 3c_s^2\omega_{11} + v_3^2\omega_{18}) \frac{v_3v_1\delta_l^4}{4\omega_{11}\omega_{18}\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^3} + \\
& (v_3^2\omega_{18}\omega_6 - \omega_{18}\omega_6 - 6c_s^2\omega_{11}\omega_{18} + 3c_s^2\omega_{18}\omega_6 + v_3^2\omega_{11}\omega_{18}\omega_6 - \omega_{11}\omega_{18}\omega_6 + 3\omega_{11}\omega_6 - 3c_s^2\omega_{11}\omega_6 + 3c_s^2\omega_{11}\omega_{18}\omega_6 - \\
& 3v_3^2\omega_{11}\omega_6) \frac{v_3\rho\delta_l^4}{12\omega_{11}\omega_{18}\omega_6\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_3^3} + (-3v_3^2\omega_{11} + c_s^2\omega_{18} + \omega_{11} - \omega_{18} - c_s^2\omega_{11} + 3v_3^2\omega_{18}) \frac{\rho v_1\delta_l^4}{4\omega_{11}\omega_{18}\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_3^3} + \\
& (-v_3^2\omega_{11} + \omega_{11} + v_3^2\omega_{19} - 3c_s^2\omega_{11} + 3c_s^2\omega_{19} - \omega_{19}) \frac{v_2v_3\delta_l^4}{4\omega_{11}\omega_{19}\delta_t} \frac{\partial^4 \rho}{\partial x_2\partial x_3^3} + (-3v_3^2\omega_7\omega_{11} + 3\omega_7\omega_{11} + v_3^2\omega_7\omega_{19} - \omega_7\omega_{19} - \\
& \omega_7\omega_{11}\omega_{19} - 6c_s^2\omega_{11}\omega_{19} + 3\omega_7c_s^2\omega_{11}\omega_{19} - 3\omega_7c_s^2\omega_{11} + 3\omega_7c_s^2\omega_{19} + v_3^2\omega_7\omega_{11}\omega_{19}) \frac{v_3\rho\delta_l^4}{12\omega_7\omega_{11}\omega_{19}\delta_t} \frac{\partial^4 v_2}{\partial x_2\partial x_3^3} + \\
& (-3v_3^2\omega_{11} + \omega_{11} + 3v_3^2\omega_{19} - c_s^2\omega_{11} + c_s^2\omega_{19} - \omega_{19}) \frac{v_2\rho\delta_l^4}{4\omega_{11}\omega_{19}\delta_t} \frac{\partial^4 v_3}{\partial x_2\partial x_3^3} + \\
& (-c_s^4\omega_{11} - 6v_3^2 + 3v_3^2\omega_{11} - 2c_s^2 + 24v_3^2c_s^2 + 2c_s^4 - 12v_3^2c_s^2\omega_{11} - 3v_3^4\omega_{11} + c_s^2\omega_{11} + 6v_3^4) \frac{\delta_l^4}{24\omega_{11}\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 10v_3^2 - 5v_3^2\omega_{11} + 6c_s^2 + 2\omega_{11} - 3c_s^2\omega_{11}) \frac{v_3\rho\delta_l^4}{12\omega_{11}\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.3.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho v_1\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2v_1\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_2\rho\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho v_1\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3v_1\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3\rho\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\rho v_1\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + 4c_s^2 + 6v_1^2 - 2c_s^2\omega_9 - 3v_1^2\omega_9 + \omega_9) \frac{\delta_l^2}{\omega_9\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\rho v_1\delta_l^2}{\omega_9\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{c_s^2\delta_l^2}{2\omega_5\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{c_s^2\delta_l^2}{2\omega_5\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{c_s^2\delta_l^2}{2\omega_6\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2\delta_l^2}{2\omega_6\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + 6c_s^2 + 2v_1^2 - 3c_s^2\omega_9 - v_1^2\omega_9 + \omega_9) \frac{v_1\delta_l^2}{2\omega_9\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + 2c_s^2 + 6v_1^2 - c_s^2\omega_9 - 3v_1^2\omega_9 + \omega_9) \frac{\rho\delta_l^2}{2\omega_9\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{\rho c_s^2\delta_l^2}{2\omega_5\delta_t} \frac{\partial^2 v_2}{\partial x_1\partial x_2} + (-2 + \omega_5) \frac{\rho c_s^2\delta_l^2}{2\omega_5\delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{\rho c_s^2\delta_l^2}{2\omega_6\delta_t} \frac{\partial^2 v_3}{\partial x_1\partial x_3} + (-2 + \omega_6) \frac{\rho c_s^2\delta_l^2}{2\omega_6\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega_9^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 + 36c_s^2 + 60v_1^2 - 36c_s^2\omega_9 - 4\omega_9^2 - 60v_1^2\omega_9 + 24\omega_9 + 11v_1^2\omega_9^2 + 5c_s^2\omega_9^2) \frac{\rho v_1\delta_l^3}{6\omega_9^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{v_2v_1\delta_l^3}{\omega_5\omega_9^2\omega_{12}\delta_t} \frac{\partial^3 \rho}{\partial x_1^2\partial x_2} + \\
& C_3 \frac{v_2\rho\delta_l^3}{\omega_5\omega_9^2\omega_{12}\delta_t} \frac{\partial^3 v_1}{\partial x_2^2\partial x_2} + C_4 \frac{\rho v_1\delta_l^3}{12\omega_5^2\omega_9^2\omega_{12}\delta_t} \frac{\partial^3 v_2}{\partial x_1^2\partial x_2} + (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4\delta_l^3}{6\omega_5^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_2^2} + \\
& (12\omega_5^2 - \omega_5^2\omega_9\omega_{12} - 12\omega_5^2\omega_9 - 12\omega_9\omega_{12} - 12\omega_5\omega_{12} + 12\omega_5\omega_9\omega_{12} + 12\omega_5\omega_9) \frac{\rho v_1 c_s^2\delta_l^3}{6\omega_5^2\omega_9\omega_{12}\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_2^2} + \\
& (-\omega_5^2 + \omega_5\omega_{15} + 2\omega_5 - 2\omega_{15}) \frac{v_2\rho c_s^2\delta_l^3}{\omega_5^2\omega_{15}\delta_t} \frac{\partial^3 v_2}{\partial x_1\partial x_2^2} + C_5 \frac{v_2v_1\delta_l^3}{12\omega_{10}\omega_5\omega_{15}\delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + C_6 \frac{v_2\rho\delta_l^3}{6\omega_5^2\omega_{15}\delta_t} \frac{\partial^3 v_1}{\partial x_2^2} + C_7 \frac{\rho v_1\delta_l^3}{12\omega_{10}\omega_5\omega_{15}\delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + \\
& C_8 \frac{v_3v_1\delta_l^3}{\omega_{13}\omega_9^2\omega_6\delta_t} \frac{\partial^3 \rho}{\partial x_2^2\partial x_3} + C_9 \frac{v_3\rho\delta_l^3}{\omega_{13}\omega_9^2\omega_6\delta_t} \frac{\partial^3 v_1}{\partial x_2^2\partial x_3} + C_{10} \frac{\rho v_1\delta_l^3}{12\omega_{13}\omega_9^2\omega_6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2\partial x_3} + \\
& (\omega_8\omega_5\omega_6 + \omega_5^2 - \omega_5^2\omega_6 - \omega_8\omega_6 + \omega_5\omega_6 - \omega_8\omega_5) \frac{v_3\rho c_s^2\delta_l^3}{\omega_8\omega_5^2\omega_6\delta_t} \frac{\partial^3 v_2}{\partial x_1\partial x_2\partial x_3} + \\
& (\omega_8\omega_5\omega_6 - \omega_8\omega_6 + \omega_6^2 + \omega_5\omega_6 - \omega_5\omega_6^2 - \omega_8\omega_5) \frac{v_2\rho c_s^2\delta_l^3}{\omega_8\omega_5\omega_6^2\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_2\partial x_3} + \\
& (\omega_8\omega_5\omega_6 + \omega_5^2 - \omega_5^2\omega_6 - \omega_8\omega_6 + \omega_5\omega_6 - \omega_8\omega_5) \frac{v_3\rho c_s^2\delta_l^3}{\omega_8\omega_5^2\omega_6\delta_t} \frac{\partial^3 v_1}{\partial x_2^2\partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-\omega_7\omega_8\omega_5\omega_6 + 6\omega_8\omega_5\omega_6 + 6\omega_7\omega_6 - 6\omega_8\omega_6 + 6\omega_7\omega_5 - 6\omega_7\omega_5\omega_6 - 6\omega_8\omega_5) \frac{\rho v_1 c_s^2 \delta_l^3}{6\omega_7\omega_8\omega_5\omega_6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-12 - \omega_6^2 + 12\omega_6) \frac{c_s^4 \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (-\omega_{13}\omega_9\omega_6^2 + 12\omega_{13}\omega_9\omega_6 + 12\omega_6^2 + 12\omega_9\omega_6 - 12\omega_9\omega_6^2 - 12\omega_{13}\omega_6 - 12\omega_{13}\omega_9) \frac{\rho v_1 c_s^2 \delta_l^3}{6\omega_{13}\omega_9\omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3} + \\
& (\omega_{18}\omega_6 - \omega_6^2 - 2\omega_{18} + 2\omega_6) \frac{v_3 \rho c_s^2 \delta_l^3}{\omega_{18}\omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3} + (\omega_8\omega_5\omega_6 - \omega_8\omega_6 + \omega_6^2 + \omega_5\omega_6 - \omega_5\omega_6^2 - \omega_8\omega_5) \frac{v_2 \rho c_s^2 \delta_l^3}{\omega_8\omega_5\omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_2 \partial x_3} + \\
& (-\omega_7\omega_8\omega_5\omega_6 + 6\omega_8\omega_5\omega_6 + 6\omega_7\omega_6 - 6\omega_8\omega_6 + 6\omega_7\omega_5 - 6\omega_7\omega_5\omega_6 - 6\omega_8\omega_5) \frac{\rho v_1 c_s^2 \delta_l^3}{6\omega_7\omega_8\omega_5\omega_6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3} + \\
& C_{11} \frac{v_3 v_1 \delta_l^3}{12\omega_{11}\omega_{18}\omega_6\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{v_3 \rho \delta_l^3}{6\omega_{18}\omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + C_{13} \frac{\rho v_1 \delta_l^3}{12\omega_{11}\omega_{18}\omega_6\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{v_1 \delta_l^4}{12\omega_9^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\rho \delta_l^4}{12\omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& C_{16} \frac{v_2 \delta_l^4}{4\omega_5^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{17} \frac{v_2 \rho v_1 \delta_l^4}{4\omega_5^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{18} \frac{\rho \delta_l^4}{12\omega_5^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_1 \delta_l^4}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& C_{20} \frac{\rho \delta_l^4}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{21} \frac{v_2 \rho v_1 \delta_l^4}{2\omega_{10} \omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_2 \delta_l^4}{12\omega_{10}^2 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& C_{23} \frac{v_2 \rho v_1 \delta_l^4}{12\omega_{10}^2 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{24} \frac{\rho \delta_l^4}{12\omega_{10}^2 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{25} \frac{v_1 \delta_l^4}{24\omega_{10}^2 \omega_5^2 \omega_{15}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{26} \frac{\rho \delta_l^4}{24\omega_5^2 \omega_{15}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& C_{27} \frac{v_2 \rho v_1 \delta_l^4}{12\omega_{10}^2 \omega_5^2 \omega_{15}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_{28} \frac{v_3 \delta_l^4}{4\omega_{13}^2 \omega_9^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{29} \frac{v_3 \rho v_1 \delta_l^4}{4\omega_{13}^2 \omega_9^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{30} \frac{\rho \delta_l^4}{12\omega_{13}^2 \omega_9^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{31} \frac{v_2 v_3 v_1 \delta_l^4}{\omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{32} \frac{v_2 v_3 \rho \delta_l^4}{\omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{33} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{v_2 \rho v_1 \delta_l^4}{2\omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{35} \frac{2v_3 c_s^4 \delta_l^4}{\omega_5^2 \omega_9^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{36} \frac{v_3 \rho v_1 c_s^2 \delta_l^4}{2\omega_{13} \omega_7 \omega_{14} \omega_5^2 \omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{37} \frac{v_2 v_3 \rho c_s^2 \delta_l^4}{\omega_{17} \omega_8^2 \omega_3^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{38} \frac{\rho c_s^2 \delta_l^4}{12\omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8^2 \omega_3^2 \omega_{15} \omega_9 \omega_{12} \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{39} \frac{v_2 v_3 v_1 \delta_l^4}{4\omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + \\
& + C_{40} \frac{v_2 v_3 \rho \delta_l^4}{2\omega_{17} \omega_8^2 \omega_3^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^3 \partial x_3} + C_{41} \frac{v_3 \rho v_1 \delta_l^4}{4\omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{42} \frac{v_2 \rho v_1 \delta_l^4}{12\omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& C_{43} \frac{v_1 \delta_l^4}{12\omega_{13}^2 \omega_{18} \omega_9^2 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{44} \frac{\rho \delta_l^4}{12\omega_{13}^2 \omega_{18} \omega_9^2 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{45} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_{13}^2 \omega_{11} \omega_{18}^2 \omega_9^2 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{46} \frac{\rho \delta_l^4}{2\omega_{13} \omega_{20} \omega_{14} \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{47} \frac{\rho \delta_l^4}{2\omega_{13}^2 \omega_7 \omega_{20} \omega_{14} \omega_5^2 \omega_{18} \omega_9^2 \omega_{12} \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{48} \frac{\rho \delta_l^4}{12\omega_{13} \omega_7^2 \omega_{20} \omega_{14} \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{49} \frac{v_3 \rho \delta_l^4}{\omega_{13} \omega_{20} \omega_{14} \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{\delta_l^4}{12\omega_7^2 \omega_{20} \omega_{17} \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{51} \frac{\rho \delta_l^4}{4\omega_{20} \omega_{17} \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + \\
& C_{52} \frac{v_2 \rho \delta_l^4}{2\omega_{16} \omega_{10}^2 \omega_{20} \omega_{17} \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{\rho \delta_l^4}{4\omega_7^2 \omega_{20} \omega_{17} \omega_{11} \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{54} \frac{v_3 \delta_l^4}{12\omega_{13} \omega_{11}^2 \omega_{18}^2 \omega_9 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_{13}^2 \omega_{11}^2 \omega_{18}^2 \omega_9^2 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{56} \frac{\rho \delta_l^4}{12\omega_{13} \omega_{11}^2 \omega_{18}^2 \omega_9 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{57} \frac{v_2 v_3 v_1 \delta_l^4}{4\omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{58} \frac{v_2 v_3 \rho \delta_l^4}{2\omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} + C_{59} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2 \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{60} \frac{v_2 \rho v_1 \delta_l^4}{4\omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{v_1 \delta_l^4}{24\omega_{11}^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{62} \frac{\rho \delta_l^4}{24\omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + C_{63} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_{11}^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -36v_1^4\omega_9 - 12c_s^4\omega_9 + 144v_1^2c_s^2 - 12c_s^2 + c_s^4\omega_9^2 - 36v_1^2 + 7v_1^4\omega_9^2 + 36v_1^4 + 12c_s^4 + 12c_s^2\omega_9 + 24v_1^2c_s^2\omega_9^2 + 36v_1^2\omega_9 - 144v_1^2c_s^2\omega_9 - 7v_1^2\omega_9^2 - c_s^2\omega_9^2 \\
C_2 &= -v_1^2\omega_5\omega_9\omega_{12} - \omega_9\omega_{12} - \omega_5\omega_{12} - 3c_s^2\omega_5\omega_9 + \omega_5\omega_9\omega_{12} + 3c_s^2\omega_9\omega_{12} + \omega_5\omega_9 + 3c_s^2\omega_5\omega_{12} - 3c_s^2\omega_5\omega_9\omega_{12} + \omega_9^2 + v_1^2\omega_5\omega_9^2 - v_1^2\omega_9^2 - v_1^2\omega_5\omega_9 + v_1^2\omega_9\omega_{12} + v_1^2\omega_5\omega_{12} - 3c_s^2\omega_9^2 - \omega_5\omega_9^2 + 3c_s^2\omega_5\omega_9^2 \\
C_3 &= -3v_1^2\omega_5\omega_9\omega_{12} - \omega_9\omega_{12} - \omega_5\omega_{12} - c_s^2\omega_5\omega_9 + \omega_5\omega_9\omega_{12} + c_s^2\omega_9\omega_{12} + \omega_5\omega_9 + c_s^2\omega_5\omega_{12} - c_s^2\omega_5\omega_9\omega_{12} + \omega_9^2 + 3v_1^2\omega_5\omega_9^2 - 3v_1^2\omega_9^2 - 3v_1^2\omega_5\omega_9 + 3v_1^2\omega_9\omega_{12} + 3v_1^2\omega_5\omega_{12} - c_s^2\omega_9^2 - \omega_5\omega_9^2 + c_s^2\omega_5\omega_9^2 \\
C_4 &= -3v_1^2\omega_5^2\omega_9\omega_{12} - 12\omega_5^2\omega_9^2 + 12c_s^2\omega_5^2\omega_9^2 - 12v_1^2\omega_5^2\omega_9 + 12v_1^2\omega_5^2\omega_{12} + 42c_s^2\omega_5\omega_9^2\omega_{12} + 6\omega_5^2\omega_9\omega_{12} + 12v_1^2\omega_5^2\omega_9^2 - 6\omega_5\omega_9^2\omega_{12} - 12c_s^2\omega_5^2\omega_9 - 18c_s^2\omega_5^2\omega_9\omega_{12} - 12\omega_5^2\omega_{12} - 24c_s^2\omega_5^2\omega_{12} + 36c_s^2\omega_5^2\omega_{12} + 12\omega_5^2\omega_9 - 11c_s^2\omega_5^2\omega_9\omega_{12} + 3\omega_5^2\omega_9^2\omega_{12} - 24c_s^2\omega_5\omega_9\omega_{12} - 12v_1^2\omega_5\omega_9^2 + 6v_1^2\omega_5\omega_9^2\omega_{12} + 12\omega_5\omega_9^2 - 6v_1^2\omega_5\omega_9\omega_{12} - 12c_s^2\omega_5\omega_9^2 \\
C_5 &= 12\omega_{10} + \omega_{10}v_2^2\omega_5\omega_{15} - \omega_{10}\omega_5\omega_{15} - 36\omega_{10}c_s^2 - 6\omega_{10}\omega_5 - 12\omega_{10}\omega_5^2 - 18c_s^2\omega_5\omega_{15} + 6\omega_5\omega_{15} + 36c_s^2\omega_{15} + 18\omega_{10}c_s^2\omega_5 + 12v_2^2\omega_{15} + 6\omega_{10}v_2^2\omega_5 - 12\omega_{15} + 3\omega_{10}c_s^2\omega_5\omega_{15} - 6v_2^2\omega_5\omega_{15} \\
C_6 &= -6c_s^2\omega_5 - 3\omega_5^2 - v_2^2\omega_5^2\omega_{15} + 15c_s^2\omega_5\omega_{15} + 3c_s^2\omega_5^2 - 3\omega_5\omega_{15} - 12c_s^2\omega_{15} + 6\omega_5 - 3c_s^2\omega_5^2\omega_{15} + \omega_5^2\omega_{15} + 3v_2^2\omega_5^2 - 6v_2^2\omega_5 + 3v_2^2\omega_5\omega_{15} \\
C_7 &= 12\omega_{10} + 3\omega_{10}v_2^2\omega_5\omega_{15} - \omega_{10}\omega_5\omega_{15} - 12\omega_{10}c_s^2 - 6\omega_{10}\omega_5 - 36\omega_{10}\omega_5^2 - 6c_s^2\omega_5\omega_{15} + 6\omega_5\omega_{15} + 12c_s^2\omega_{15} + 6\omega_{10}c_s^2\omega_5 + 36v_2^2\omega_{15} + 18\omega_{10}v_2^2\omega_5 - 12\omega_{15} + \omega_{10}c_s^2\omega_5\omega_{15} - 18v_2^2\omega_5\omega_{15}
\end{aligned}$$

[illegible]

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$$C_{48} = 12w_{16}w_{10}v_2^3w_7^3w_{23}w_{17}w_8w_5^3w_{15}w_6^3w_{19} - 6w_{16}w_{10}w_7^3w_{23}c_s^4w_{20}w_{17}w_8^3w_5^3w_{15}w_6^3 - 6w_{16}w_{10}w_7^3w_{23}c_s^4w_{17}w_8^3w_5^3w_{15}w_6^3w_{19} + 12w_{16}w_3^3w_{23}c_4^4w_{20}w_{17}w_8^3w_5^3w_6^3w_{19} + 24v_2^3v_3w_7^3w_{23}v_1w_{20}w_{17}w_8^3w_5^3w_{15}w_6^3w_{19} + 24w_{10}v_2^3v_3w_7^3w_{23}v_1w_{20}w_8^3w_5^3w_{15}w_6^3w_{19} + 36w_{16}w_{10}v_2^3w_7^3w_{23}c_s^3w_{20}w_{17}w_8^3w_5^3w_{15}w_6^3w_{19} - 24v_3w_3^3v_1c_s^3w_{20}w_{17}w_8^3w_5^3w_{15}w_6^3w_{19} - 12w_{10}v_2^3v_3^3w_7^3w_{20}w_{17}w_8^3w_5^3w_{15}w_6^3w_{19} -$$

[illegible]

$$C_{62} = -48v_3^4\omega_7\omega_{19} - 24v_3^4\omega_7^2 + 12v_3^3\omega_7^3c_s^2 + 24c_s^2\omega_{19}^2 + 24\omega_7^2c_s^2\omega_{19} + 6\omega_7^3c_s^4\omega_{19} - 24v_3^3\omega_7\omega_{19}^2 - 72v_3^2\omega_7^2c_s^2\omega_{19} - 48\omega_7c_s^4\omega_{19} + 12v_3^4\omega_7^3 - 3\omega_7^3c_s^4\omega_{19} + 48v_3^3\omega_7^2c_s^2\omega_{19} + 48v_3^2\omega_7\omega_{19} - 24v_3^2\omega_7^2c_s^2 + 24\omega_7c_s^4\omega_{19} - 8\omega_7^2c_s^2\omega_{19}^2 + 24v_3^4\omega_7\omega_{19}^2 + 6v_3^3\omega_7^2c_s^2\omega_{19} - 24\omega_7^2c_s^4\omega_{19} - 3v_3^3\omega_7^3\omega_{19} - 24v_3^2\omega_7c_s^2\omega_{19} - 6\omega_7^2c_s^2\omega_{19} - 24v_3^4\omega_7^2\omega_{19} - 12v_3^3\omega_7^3 + 12\omega_7c_s^2\omega_{19}^2 - 72v_3^2\omega_7^2\omega_{19} - 96v_3^2c_s^2\omega_{19}^2 + 24v_3^4\omega_7^2 - 18v_3^4\omega_7^3\omega_{19} + 3v_3^4\omega_7^3\omega_{19}^2 + 24v_3^2\omega_7^2\omega_{19} + \omega_7^2c_s^2\omega_{19}^2 + 72v_3^4\omega_7\omega_{19} - 24\omega_7c_s^2\omega_{19} - 12v_3^3\omega_7^3c_s^2\omega_{19} + 24\omega_7^2c_s^4\omega_{19} + 156v_3^2\omega_7c_s^2\omega_{19} + 18v_3^3\omega_7^3\omega_{19}$$

$$\begin{aligned}
& C_6 \frac{v_2 \rho \delta_l^3}{6 \omega_{16} \omega_7^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 - \omega_6^2 + 12 \omega_6) \frac{c_s^4 \delta_l^3}{6 \omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + (-2 \omega_{13} - \omega_6^2 + \omega_{13} \omega_6 + 2 \omega_6) \frac{\rho v_1 c_s^2 \delta_l^3}{\omega_{13} \omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\
& (-12 \omega_{18} \omega_6 - 12 \omega_{11} \omega_{18} + 12 \omega_6^2 - \omega_{11} \omega_{18} \omega_6^2 - 12 \omega_{11} \omega_6^2 + 12 \omega_{11} \omega_{18} \omega_6 + 12 \omega_{11} \omega_6) \frac{v_3 \rho c_s^2 \delta_l^3}{6 \omega_{11} \omega_{18} \omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (\omega_7 \omega_6 - \omega_7 \omega_6^2 + \omega_7 \omega_8 \omega_6 - \omega_7 \omega_8 - \omega_8 \omega_6 + \omega_6^2) \frac{v_2 \rho c_s^2 \delta_l^3}{\omega_7 \omega_8 \omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (\omega_7 \omega_6 + \omega_7 \omega_8 \omega_6 - \omega_7 \omega_8 - \omega_8 \omega_6 + \omega_7^2 - \omega_7^2 \omega_6) \frac{\rho v_1 c_s^2 \delta_l^3}{\omega_7^2 \omega_8 \omega_6 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + (-12 + 12 \omega_7 - \omega_7^2) \frac{c_s^4 \delta_l^3}{6 \omega_7^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-2 \omega_{16} + 2 \omega_7 + \omega_{16} \omega_7 - \omega_7^2) \frac{v_2 \rho c_s^2 \delta_l^3}{\omega_{16} \omega_7^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& (12 \omega_7 \omega_{11} - \omega_7^2 \omega_{11} \omega_{19} + 12 \omega_7^2 - 12 \omega_7 \omega_{19} - 12 \omega_{11} \omega_{19} + 12 \omega_7 \omega_{11} \omega_{19} - 12 \omega_7^2 \omega_{11}) \frac{v_3 \rho c_s^2 \delta_l^3}{6 \omega_7^2 \omega_{11} \omega_{19} \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& C_7 \frac{v_3 v_1 \delta_l^3}{\omega_{11}^2 \omega_{18} \omega_6 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + C_8 \frac{v_3 \rho \delta_l^3}{12 \omega_{11}^2 \omega_{18} \omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_9 \frac{\rho v_1 \delta_l^3}{\omega_{11}^2 \omega_{18} \omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{v_2 v_3 \delta_l^3}{\omega_7 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& C_{11} \frac{v_3 \rho \delta_l^3}{12 \omega_7^2 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{12} \frac{v_2 \rho \delta_l^3}{\omega_7 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{13} \frac{\delta_l^3}{12 \omega_{11}^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-24 + 60 v_3^2 - 60 v_3^2 \omega_{11} + 36 c_s^2 + 11 v_3^2 \omega_{11}^2 + 24 \omega_{11} - 4 \omega_{11}^2 - 36 c_s^2 \omega_{11} + 5 c_s^2 \omega_{11}^2) \frac{v_3 \rho \delta_l^3}{6 \omega_{11}^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{v_3 \delta_l^4}{24 \omega_{13}^2 \omega_9^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{v_3 \rho v_1 \delta_l^4}{12 \omega_{13}^2 \omega_9^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{\rho \delta_l^4}{24 \omega_{13}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_{17} \frac{v_2 v_3 v_1 \delta_l^4}{4 \omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_{18} \frac{v_2 v_3 \rho \delta_l^4}{4 \omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_3 \rho v_1 \delta_l^4}{12 \omega_{13}^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12} \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{20} \frac{v_2 \rho v_1 \delta_l^4}{2 \omega_{13}^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_2} + \\
& C_{21} \frac{v_3 c_s^4 \delta_l^4}{6 \omega_7^2 \omega_8^2 \omega_5^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_3 \rho v_1 c_s^4 \delta_l^4}{2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12} \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{v_2 v_3 \rho c_s^2 \delta_l^4}{2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\
& C_{24} \frac{\rho c_s^4 \delta_l^4}{2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8^2 \omega_5^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + C_{25} \frac{v_2 v_3 v_1 \delta_l^4}{4 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{26} \frac{12 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_6^2 \delta_t}{\partial x_1 \partial x_2^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
& C_{27} \frac{v_3 \rho v_1 \delta_l^4}{4 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{28} \frac{v_2 \rho v_1 \delta_l^4}{2 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2} + C_{29} \frac{v_3 \delta_l^4}{24 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2} + C_{30} \frac{v_2 v_3 \rho \delta_l^4}{12 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2} + \\
& C_{31} \frac{\rho \delta_l^4}{24 \omega_{16}^2 \omega_7^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2} + C_{32} \frac{v_1 \delta_l^4}{12 \omega_{13}^2 \omega_{11} \omega_{18} \omega_5^2 \omega_6^2 \omega_{22} \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{33} \frac{\rho \delta_l^4}{12 \omega_{13}^2 \omega_{11} \omega_{18} \omega_5^2 \omega_6^2 \omega_{22} \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_{34} \frac{v_3 \rho v_1 \delta_l^4}{12 \omega_{13}^2 \omega_{11}^2 \omega_{18}^2 \omega_5^2 \omega_6^2 \omega_{22} \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{35} \frac{2 \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18} \omega_5^2 \omega_{22} \omega_{19} \delta_t}{\delta_l^4} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{36} \frac{\rho \delta_l^4}{2 \omega_{13}^2 \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18} \omega_5^2 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{37} \frac{\rho \delta_l^4}{12 \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18} \omega_5^2 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{v_3 \rho \delta_l^4}{2 \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18} \omega_5^2 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\delta_l^4}{2 \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18} \omega_5^2 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{40} \frac{\rho \delta_l^4}{12 \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18} \omega_5^2 \omega_{19} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{v_2 \rho \delta_l^4}{\omega_{16}^2 \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18} \omega_5^2 \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{42} \frac{\rho \delta_l^4}{2 \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18} \omega_5^2 \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{v_2 \delta_l^4}{12 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + \\
& C_{44} \frac{\rho \delta_l^4}{12 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{45} \frac{v_2 v_3 \rho \delta_l^4}{12 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{46} \frac{v_3 \delta_l^4}{12 \omega_{13} \omega_{11}^2 \omega_{18}^2 \omega_5^2 \omega_{22} \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& C_{47} \frac{v_3 \rho v_1 \delta_l^4}{2 \omega_{13}^2 \omega_{11}^2 \omega_{18}^2 \omega_9 \omega_5^2 \omega_{22} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{48} \frac{\rho \delta_l^4}{12 \omega_{13} \omega_{11}^2 \omega_{18}^2 \omega_5^2 \omega_{22} \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{49} \frac{v_2 v_3 v_1 \delta_l^4}{\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}^2 \omega_6^2 \omega_{19}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{v_2 v_3 \rho \delta_l^4}{2 \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{51} \frac{v_3 \rho v_1 \delta_l^4}{2 \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5 \omega_{18}^2 \omega_6^2 \omega_{19}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{52} \frac{v_2 \rho v_1 \delta_l^4}{\omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}^2 \omega_6^2 \omega_{19}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{53} \frac{v_3 \delta_l^4}{12 \omega_{16} \omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{54} \frac{v_2 v_3 \rho \delta_l^4}{2 \omega_{16}^2 \omega_{10} \omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{55} \frac{\rho \delta_l^4}{12 \omega_{16} \omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{56} \frac{v_1 \delta_l^4}{4 \omega_{11}^3 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{57} \frac{\rho \delta_l^4}{12 \omega_{11}^3 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{58} \frac{v_3 \rho v_1 \delta_l^4}{4 \omega_{11}^3 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{59} \frac{v_2 \delta_l^4}{4 \omega_{11}^2 \omega_{18}^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{60} \frac{\rho \delta_l^4}{12 \omega_7^2 \omega_{11}^3 \omega_{19}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{61} \frac{v_2 v_3 \rho \delta_l^4}{4 \omega_7^2 \omega_{11}^3 \omega_{19}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{62} \frac{v_3 \delta_l^4}{12 \omega_{11}^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{63} \frac{\rho \delta_l^4}{12 \omega_{11}^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 3 \omega_{13} c_s^2 \omega_9 \omega_6 - 12 \omega_{13} - 6 \omega_{13} v_1^2 \omega_6 + \omega_{13} v_1^2 \omega_9 \omega_6 - 18 \omega_{13} c_s^2 \omega_6 - \omega_{13} \omega_9 \omega_6 + 12 \omega_{13} v_1^2 + 36 \omega_{13} c_s^2 - 36 c_s^2 \omega_9 + 18 c_s^2 \omega_9 \omega_6 - 6 \omega_9 \omega_6 - \\
& 12 v_1^2 \omega_9 + 12 \omega_9 + 6 \omega_{13} \omega_6 + 6 v_1^2 \omega_9 \omega_6 \\
C_2 &= \omega_{13} c_s^2 \omega_9 \omega_6 - 12 \omega_{13} - 18 \omega_{13} v_1^2 \omega_6 + 3 \omega_{13} v_1^2 \omega_9 \omega_6 - 6 \omega_{13} c_s^2 \omega_6 - \omega_{13} \omega_9 \omega_6 + 36 \omega_{13} v_1^2 + 12 \omega_{13} c_s^2 - 12 c_s^2 \omega_9 + 6 c_s^2 \omega_9 \omega_6 - 6 \omega_9 \omega_6 - \\
& 36 v_1^2 \omega_9 + 12 \omega_9 + 6 \omega_{13} \omega_6 + 18 v_1^2 \omega_9 \omega_6 \\
C_3 &= -3 \omega_{13} c_s^2 \omega_6^2 - \omega_{13} v_1^2 \omega_6^2 + 3 \omega_{13} v_1^2 \omega_6 + 15 \omega_{13} c_s^2 \omega_6 - 12 \omega_{13} c_s^2 - 6 v_1^2 \omega_6 - 3 \omega_6^2 + \omega_{13} \omega_6^2 - 6 c_s^2 \omega_6 + 3 c_s^2 \omega_6^2 - 3 \omega_{13} \omega_6 + 6 \omega_6 + 3 v_1^2 \omega_6^2 \\
C_4 &= -12 \omega_{16} + 12 \omega_{10} + 36 \omega_{16} c_s^2 - 36 \omega_{10} c_s^2 - 12 \omega_{10} v_2^2 + 6 \omega_{16} \omega_7 - \omega_{16} \omega_{10} \omega_7 + 12 \omega_{16} v_2^2 - 6 \omega_{10} \omega_7 + \omega_{16} \omega_{10} v_2^2 \omega_7 - 6 \omega_{16} v_2^2 \omega_7 +
\end{aligned}$$

$$\begin{aligned}
& 3\omega_{16}\omega_{10}\omega_7c_s^2 - 18\omega_{16}\omega_7c_s^2 + 6\omega_{10}v_2^2\omega_7 + 18\omega_{10}\omega_7c_s^2 \\
C_5 = & -12\omega_{16} + 12\omega_{10} + 12\omega_{16}c_s^2 - 12\omega_{10}c_s^2 - 36\omega_{10}v_2^2 + 6\omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7 + 36\omega_{16}v_2^2 - 6\omega_{10}\omega_7 + 3\omega_{16}\omega_{10}v_2^2\omega_7 - 18\omega_{16}v_2^2\omega_7 + \\
& \omega_{16}\omega_{10}\omega_7c_s^2 - 6\omega_{16}\omega_7c_s^2 + 18\omega_{10}v_2^2\omega_7 + 6\omega_{10}\omega_7c_s^2 \\
C_6 = & -12\omega_{16}c_s^2 + 6\omega_7 + \omega_{16}\omega_7^2 - 3\omega_{16}\omega_7 - 3\omega_{16}\omega_7^2c_s^2 - 3\omega_7^2 + 3\omega_7^2c_s^2 - 6v_2^2\omega_7 - 6\omega_7c_s^2 + 3\omega_{16}v_2^2\omega_7 + 15\omega_{16}\omega_7c_s^2 - \omega_{16}v_2^2\omega_7^2 + 3v_2^2\omega_7^2 \\
C_7 = & v_3^2\omega_{18}\omega_6 + v_3^2\omega_{11}\omega_{18} + v_3^2\omega_{11}^2\omega_6 - \omega_{18}\omega_6 - \omega_{11}\omega_{18} - \omega_{11}^2\omega_6 + 3c_s^2\omega_{11}\omega_{18} + 3c_s^2\omega_{18}\omega_6 + 3c_s^2\omega_{11}^2\omega_6 - v_3^2\omega_{11}^2 + \omega_{11}^2 - v_3^2\omega_{11}\omega_{18}\omega_6 + \\
& \omega_{11}\omega_{18}\omega_6 + \omega_{11}\omega_6 - 3c_s^2\omega_{11}^2 - 3c_s^2\omega_{11}\omega_6 - 3c_s^2\omega_{11}\omega_{18}\omega_6 - v_3^2\omega_{11}\omega_6 \\
C_8 = & -6\omega_{11}^2\omega_{18}\omega_6 - 3v_3^2\omega_{11}^2\omega_{18}\omega_6^2 - 12v_3^2\omega_{11}^2\omega_6 + 42c_s^2\omega_{11}^2\omega_{18}\omega_6 + 12\omega_{11}^2\omega_6 - 12c_s^2\omega_{11}^2\omega_6 + 36c_s^2\omega_{18}\omega_6^2 + 12c_s^2\omega_{11}^2\omega_6^2 - 11c_s^2\omega_{11}^2\omega_{18}\omega_6^2 - \\
& 12\omega_{18}\omega_6^2 - 12\omega_{11}^2\omega_6^2 + 12v_3^2\omega_{18}\omega_6^2 + 6v_3^2\omega_{11}^2\omega_{18}\omega_6 + 12v_3^2\omega_{11}^2\omega_6^2 + 3\omega_{11}^2\omega_{18}\omega_6^2 - 12v_3^2\omega_{11}\omega_6^2 - 18c_s^2\omega_{11}\omega_{18}\omega_6^2 - 12c_s^2\omega_{11}\omega_6^2 + 6\omega_{11}\omega_{18}\omega_6^2 + \\
& 12\omega_{11}\omega_6^2 - 6v_3^2\omega_{11}\omega_{18}\omega_6^2 - 24c_s^2\omega_{11}^2\omega_{18} - 24c_s^2\omega_{11}\omega_{18}\omega_6 \\
C_9 = & 3v_3^2\omega_{18}\omega_6 + 3v_3^2\omega_{11}\omega_{18} + 3v_3^2\omega_{11}^2\omega_6 - \omega_{18}\omega_6 - \omega_{11}\omega_{18} - \omega_{11}^2\omega_6 + c_s^2\omega_{11}\omega_{18} + c_s^2\omega_{18}\omega_6 + c_s^2\omega_{11}^2\omega_6 - 3v_3^2\omega_{11}^2 + \omega_{11}^2 - 3v_3^2\omega_{11}\omega_{18}\omega_6 + \\
& \omega_{11}\omega_{18}\omega_6 + \omega_{11}\omega_6 - c_s^2\omega_{11}^2 - c_s^2\omega_{11}\omega_6 - c_s^2\omega_{11}\omega_{18}\omega_6 - 3v_3^2\omega_{11}\omega_6 \\
C_{10} = & -v_3^2\omega_7\omega_{11} + \omega_7\omega_{11} + v_3^2\omega_7\omega_{19} - v_3^2\omega_{11}^2 - \omega_7\omega_{11} + v_3^2\omega_7\omega_{11}^2 - \omega_7\omega_{19} - \omega_{11}\omega_{19} + \omega_{11}^2 + \omega_7\omega_{11}\omega_{19} + 3c_s^2\omega_{11}\omega_{19} - 3\omega_7c_s^2\omega_{11}\omega_{19} - \\
& 3\omega_7c_s^2\omega_{11} + v_3^2\omega_{11}\omega_{19} + 3\omega_7c_s^2\omega_{11}^2 - 3c_s^2\omega_{11}^2 + 3\omega_7c_s^2\omega_{19} - v_3^2\omega_7\omega_{11}\omega_{19} \\
C_{11} = & 12\omega_7^2c_s^2\omega_{11}^2 + 6v_3^2\omega_7\omega_{11}^2\omega_{19} + 36\omega_7^2c_s^2\omega_{19} - 18\omega_7^2c_s^2\omega_{11}\omega_{19} - 6v_3^2\omega_7\omega_{11}\omega_{19} + 42\omega_7c_s^2\omega_{11}^2\omega_{19} + 6\omega_7\omega_{11}\omega_{19} + 12\omega_7\omega_{11}^2 - 12v_3^2\omega_7\omega_{11}^2 - \\
& 6\omega_7\omega_{11}^2\omega_{19} - 24c_s^2\omega_{11}^2\omega_{19} - 12\omega_7^2c_s^2\omega_{11} + 12v_3^2\omega_7^2\omega_{11}^2 - 12\omega_7^2\omega_{19} + 12v_3^2\omega_7^2\omega_{19} - 24\omega_7c_s^2\omega_{11}\omega_{19} - 12\omega_7^2\omega_{11}^2 + 3\omega_7^2\omega_{11}^2\omega_{19} - 12\omega_7c_s^2\omega_{11}^2 + \\
& 12\omega_7^2\omega_{11} - 11\omega_7^2c_s^2\omega_{11}^2\omega_{19} - 3v_3^2\omega_7^2\omega_{11}^2\omega_{19} - 12v_3^2\omega_7^2\omega_{11} \\
C_{12} = & -3v_3^2\omega_7\omega_{11} + \omega_7\omega_{11} + 3v_3^2\omega_7\omega_{19} - 3v_3^2\omega_{11}^2 - \omega_7\omega_{11} + 3v_3^2\omega_7\omega_{11}^2 - \omega_7\omega_{19} - \omega_{11}\omega_{19} + \omega_{11}^2 + \omega_7\omega_{11}\omega_{19} + c_s^2\omega_{11}\omega_{19} - \omega_7c_s^2\omega_{11}\omega_{19} - \\
& \omega_7c_s^2\omega_{11} + 3v_3^2\omega_{11}\omega_{19} + \omega_7c_s^2\omega_{11}^2 - c_s^2\omega_{11}^2 + \omega_7c_s^2\omega_{19} - 3v_3^2\omega_7\omega_{11}\omega_{19} \\
C_{13} = & -12c_s^4\omega_{11} - 36v_3^4 + 36v_3^2\omega_{11} - 12c_s^2 - 7v_3^2\omega_{11}^2 + c_s^4\omega_{11}^2 + 144v_3^2c_s^2 + 12c_s^4 - 144v_3^2c_s^2\omega_{11} - 36v_3^4\omega_{11} + 12c_s^2\omega_{11} - c_s^2\omega_{11}^2 + 36v_3^4 + 24v_3^2c_s^2\omega_{11}^2 + 7v_3^4\omega_{11}^2 \\
C_{14} = & 24v_1^2\omega_9^2\omega_6 - 48\omega_{13}v_1^4\omega_9\omega_6 - 24c_s^4\omega_9^2\omega_6 + 48\omega_{13}^2v_1^4\omega_9 + \omega_{13}^2c_s^2\omega_9^2\omega_6^2 + 24\omega_{13}^2c_s^4\omega_6 + 150\omega_{13}^2v_1^2c_s^2\omega_9\omega_6^2 - 3\omega_{13}^2v_1^4\omega_9^2\omega_6^2 - 216\omega_{13}v_1^2c_s^2\omega_9^2 + \\
& 48\omega_{13}v_1^2\omega_9 + 24\omega_{13}^2c_s^4\omega_9 + 72\omega_{13}^2v_1^4\omega_6 - 12c_s^2\omega_9^2\omega_6^2 + 24\omega_{13}c_s^2\omega_9^2\omega_6^2 + 12v_1^4\omega_9^2\omega_6^2 + 72\omega_{13}v_1^2c_s^2\omega_9\omega_6^2 + 24c_s^2\omega_9^2\omega_6 - 24v_1^4\omega_9^2\omega_6 + \\
& 48\omega_{13}v_1^2\omega_9\omega_6 + 3\omega_{13}^2v_1^2\omega_9^2\omega_6^2 - 144\omega_{13}v_1^2c_s^2\omega_9\omega_6 - \omega_{13}^2c_s^4\omega_9^2\omega_6^2 - 36\omega_{13}^2v_1^4\omega_6^2 + 24\omega_{13}v_1^4\omega_9\omega_6^2 - 12v_1^4\omega_9^2\omega_6^2 + 12c_s^4\omega_9^2\omega_6^2 - 12\omega_{13}^2c_s^4\omega_6^2 - \\
& 432\omega_{13}^2v_1^2c_s^2\omega_9\omega_6 - 24\omega_{13}^2c_s^2\omega_9 - 72\omega_{13}^2v_1^4\omega_6 + 12\omega_{13}c_s^2\omega_9^2\omega_6^2 - 24\omega_{13}c_s^4\omega_9^2\omega_6^2 - 30\omega_{13}v_1^4\omega_9^2\omega_6^2 - 96\omega_{13}^2v_1^4\omega_9\omega_6 + 72v_1^2c_s^2\omega_9^2\omega_6^2 + 48\omega_{13}^2c_s^2\omega_9\omega_6 - \\
& 96\omega_{13}v_1^2\omega_9^2\omega_6 + 48\omega_{13}c_s^4\omega_9^2\omega_6 + 14\omega_{13}^2c_s^4\omega_9\omega_6^2 - 48\omega_{13}^2v_1^2\omega_9 + 432\omega_{13}v_1^2c_s^2\omega_9\omega_6 - 36\omega_{13}^2v_1^2\omega_9\omega_6^2 - 144\omega_{13}^2v_1^2c_s^2\omega_6^2 - 24\omega_{13}^2c_s^2\omega_6 - \\
& 48\omega_{13}v_1^4\omega_6^2 + 30\omega_{13}v_1^2\omega_9^2\omega_6^2 - 12\omega_{13}c_s^4\omega_9^2\omega_6^2 - 126\omega_{13}v_1^2c_s^2\omega_9^2\omega_6^2 - 48\omega_{13}^2c_s^4\omega_9\omega_6 + 12\omega_{13}^2c_s^2\omega_6^2 + 288\omega_{13}^2v_1^2c_s^2\omega_6 + 96\omega_{13}^2v_1^2\omega_9\omega_6 - \\
& 48\omega_{13}c_s^2\omega_9^2\omega_6 + 96\omega_{13}v_1^4\omega_9\omega_6 - 144v_1^2c_s^2\omega_9^2\omega_6 + 36\omega_{13}^2v_1^4\omega_9\omega_6^2 - 12\omega_{13}^2v_1^2c_s^2\omega_9^2\omega_6^2 - 14\omega_{13}^2c_s^2\omega_9\omega_6^2 + 216\omega_{13}^2v_1^2c_s^2\omega_9 + 36\omega_{13}^2v_1^2\omega_6^2 \\
C_{15} = & -48v_1^2\omega_9^2\omega_6 - 24\omega_{13}c_s^2\omega_9\omega_6 - 3\omega_{13}^2c_s^2\omega_9^2\omega_6^2 - 12\omega_{13}\omega_9\omega_6^2 - 36\omega_{13}^2\omega_9 - 84\omega_{13}v_1^2\omega_9^2 - 12\omega_9^2\omega_6^2 + 24c_s^2\omega_9^2\omega_6^2 - 60\omega_{13}c_s^2\omega_9^2 + 36\omega_{13}v_1^2\omega_9\omega_6^2 - \\
& 48\omega_{13}^2\omega_9 + 2\omega_{13}^2\omega_9^2\omega_6^2 - 48c_s^2\omega_9^2\omega_6 + 24\omega_{13}\omega_6 - 72\omega_{13}v_1^2\omega_9\omega_6 - 5\omega_{13}^2v_1^2\omega_9^2\omega_6^2 + 24\omega_9^2\omega_6 + 24\omega_{13}\omega_9\omega_6 + 24v_1^2\omega_9^2\omega_6^2 + 12\omega_{13}c_s^2\omega_9\omega_6^2 - 72\omega_{13}\omega_9^2\omega_6 + \\
& 36\omega_{13}\omega_9^2 + 60\omega_{13}^2c_s^2\omega_9 + 120\omega_{13}^2v_1^2\omega_6 - 33\omega_{13}c_s^2\omega_9^2\omega_6^2 - 120\omega_{13}^2c_s^2\omega_9\omega_6 + 168\omega_{13}v_1^2\omega_9^2\omega_6 + 84\omega_{13}^2v_1^2\omega_9 + 61\omega_{13}^2v_1^2\omega_9\omega_6^2 + 72\omega_{13}^2c_s^2\omega_6 + \\
& 72\omega_{13}^2\omega_9\omega_6 - 51\omega_{13}v_1^2\omega_9^2\omega_6^2 - 25\omega_{13}^2\omega_9\omega_6^2 - 36\omega_{13}^2c_s^2\omega_6^2 - 168\omega_{13}v_1^2\omega_9\omega_6 + 120\omega_{13}c_s^2\omega_9^2\omega_6 + 39\omega_{13}^2c_s^2\omega_9\omega_6^2 + 21\omega_{13}\omega_9^2\omega_6^2 - 60\omega_{13}^2v_1^2\omega_6^2 \\
C_{16} = & -48\omega_{13}^2c_s^4\omega_6 + 24\omega_{13}c_s^2\omega_6^2 - 12\omega_{13}v_1^2c_s^2\omega_6^3 + 18\omega_{13}v_1^2\omega_6^3 - 96\omega_{13}^2v_1^2c_s^2 + 24\omega_{13}^2v_1^4\omega_6 - 72\omega_{13}v_1^2\omega_6^2 + 48\omega_{13}v_1^2c_s^2\omega_6^2 - 6\omega_{13}c_s^2\omega_6^3 + \\
& 48\omega_{13}v_1^2\omega_6 + 24\omega_{13}^2c_s^4 - 24v_1^4\omega_6^2 - 24\omega_{13}v_1^2c_s^2\omega_6 - 3\omega_{13}^2c_s^4\omega_6^3 - 24\omega_{13}^2v_1^4\omega_6^2 - 24\omega_{13}c_s^2\omega_6 + 12v_1^4\omega_6^3 + 3\omega_{13}^2v_1^4\omega_6^3 + 24\omega_{13}^2c_s^4\omega_6^2 + 6\omega_{13}^2v_1^2c_s^2\omega_6^3 - \\
& 24\omega_{13}^2v_1^2\omega_6 + 72\omega_{13}v_1^4\omega_6^2 - 24v_1^2c_s^2\omega_6^2 + 6\omega_{13}c_s^4\omega_6^3 - 72\omega_{13}^2v_1^2c_s^2\omega_6^2 + 12\omega_{13}^2c_s^2\omega_6 - 24\omega_{13}c_s^4\omega_6^2 + 12v_1^2c_s^2\omega_6^3 - 18\omega_{13}v_1^4\omega_6^3 + 24\omega_{13}c_s^4\omega_6 - \\
& 12v_1^2\omega_6^3 - 3\omega_{13}^2v_1^4\omega_6^3 - 8\omega_{13}^2c_s^2\omega_6^2 + 156\omega_{13}^2v_1^2c_s^2\omega_6 - 48\omega_{13}v_1^4\omega_6 + 24v_1^4\omega_6^2 + \omega_{13}^2c_s^2\omega_6^3 + 24\omega_{13}^2v_1^2\omega_6^2 \\
C_{17} = & 4\omega_{13}^2\omega_7v_1^4\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}^2\omega_7c_s^2\omega_5\omega_9^2\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7v_1^2\omega_5\omega_9^2\omega_{12}\omega_6 - 3\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - \\
& 2\omega_{13}^2v_1^2\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 6\omega_{13}^2c_s^2\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 6\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_6^2 + 2\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9\omega_6^2 + 4\omega_{13}^2\omega_7\omega_8\omega_5\omega_9\omega_{12}\omega_6 - \\
& 24\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 - 8\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 - 6\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_{12}\omega_6^2 - \\
& 8\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_6 + 2\omega_{13}^2v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6^2 + 6\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6^2 + 4\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 - \\
& 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}\omega_7c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_9^2\omega_6 + 4\omega_{13}\omega_7v_1^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 - \\
& 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9\omega_6 - 4\omega_{13}\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12} - 12\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12} - 2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6 - \\
& 6\omega_{13}\omega_7c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}\omega_7v_1^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_9^2\omega_6 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_9^2\omega_6 + \\
& 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12} + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12} + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_{12}\omega_6 - 4\omega_{13}^2\omega_5\omega_9^2\omega_{12}\omega_6^2 + \\
& 4\omega_{13}^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 + 3\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_6^2 + 2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_7\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 4\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6^2 + \\
& 3\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 9\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6 + \\
& 8\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 - 12\omega_{13}^2\omega_7c_s^2\omega_5\omega_9^2\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7v_1^2\omega_5\omega_9^2\omega_{12}\omega_6^2 - 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_6 - 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9\omega_6 + \\
& 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_9\omega_{12}\omega_6^2 + 6\omega_{13}c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 2\omega_{13}v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 2\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - \\
& 6\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 12\omega_{13}^2\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6 + 4\omega_{13}^2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6 + 4\omega_{13}^2v_1^2\omega_5\omega_9^2\omega_{12}\omega_6^2 + 12\omega_{13}^2c_s^2\omega_5\omega_9^2\omega_{12}\omega_6^2 + \\
& 2\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_{12}\omega_6^2 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_9^2\omega_6^2 - 12\omega_{13}^2\omega_7c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 4\omega_{13}^2\omega_7v_1^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 12\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_9^2\omega_6^2 - \\
& 4\omega_{13}^2v_1^2\omega_{14}\omega_8\omega_9^2\omega_6^2 + 4\omega_{13}\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 4\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 + 4\omega_{13}^2v_1^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7\omega_5\omega_9^2\omega_{12}\omega_6^2 + \\
& 12\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 + 2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_6 - 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 + 2\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + \\
& 6\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6 - 12\omega_7c_s^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 + 4\omega_{13}^2\omega_7\omega_{14}\omega_5\omega_9\omega_{12}\omega_6 - 4\omega_7v_1^2\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 + \\
& 4\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_6 + 4\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12} + 6\omega_{13}^2\omega_7c_s^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 + 2\omega_{13}^2\omega_7v_1^2\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - 2\omega_{13}\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}\omega_6^2 - \\
& 12\omega_{13}^2c_s^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}^2v_1^2\omega_{14}\omega_5\omega_9\omega_{12}\omega_6^2 - 4\omega_{13}\omega_7\omega_8\omega_5\omega_9^2\omega_{12}\omega_6 - 6\omega_{13}^2c_s^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 + 2\omega_{13}^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12}\omega_6^2 -
\end{aligned}$$

$$C_{21} = 12\omega_7^2\omega_8\omega_5^2\omega_6^2 + 12\omega_7^2\omega_8^2\omega_6^2 + 12\omega_7\omega_5^2\omega_6^2 - 14\omega_7^2\omega_8^2\omega_5\omega_6^2 - 12\omega_7^2\omega_8^2\omega_6\omega_5 - 24\omega_7^2\omega_5^2\omega_6\omega_5 - 24\omega_7^2\omega_8\omega_5^2\omega_6 + 12\omega_7^2\omega_8\omega_5^2 - 24\omega_7\omega_8\omega_5^2\omega_6^2 + 12\omega_7^2\omega_5^2\omega_6 - 12\omega_8^2\omega_5\omega_6^2 + 24\omega_7\omega_8^2\omega_5\omega_6^2 + 12\omega_8\omega_5^2\omega_6^2 + \omega_7^2\omega_8^2\omega_5^2\omega_6^2 - 12\omega_7^2\omega_8^2\omega_5 - 12\omega_7\omega_8^2\omega_6^2 - 12\omega_7^2\omega_5^2\omega_6^2$$

$$\begin{aligned}
C_{23} = & -2w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_6 + 2w_{16}w_{10}w_7^2w_{17}w_8w_5^2w_{15} - 2w_{10}w_7^2w_{17}w_8^2w_5w_{15}w_6^2 - 2w_{16}w_{10}w_7^2w_8^2w_5^2w_{15}w_6^2 + 4w_{16}w_{10}w_{17}w_8w_5^2w_{15}w_6^2 + \\
& 4w_{16}w_{10}w_{17}w_8^2w_5^2w_{15}w_6^2 - 2w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_{15} - 4w_{16}w_{10}w_7^2w_{17}w_8^2w_{15}w_6 - 2w_{16}w_{10}w_7^2w_{17}w_8w_5^2w_{15}w_6^2 - 4w_{16}w_{10}w_{17}w_{17}w_8^2w_5^2w_6^2 + \\
& 4w_{16}w_{17}w_8^2w_5^2w_6^2 + 4w_{16}w_{10}w_7^2w_{17}w_8^2w_{15}w_6^2 + 2w_{10}w_7^2w_8^2w_{15}w_6^2 + 2w_{16}w_{10}w_7^2w_{17}w_8w_5^2w_{15}w_6 - 2w_{16}w_{10}w_{17}w_{17}w_8w_5^2w_{15}w_6^2 + \\
& 4w_{10}w_{17}w_{17}w_8^2w_5^2w_6^2 + 2w_{16}w_{10}w_7^2w_8^2w_5^2w_{15}w_6 + 3w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_6^2 - 2w_{16}w_7^2w_{17}w_8^2w_5^2w_{15}w_6 - 4w_{16}w_{10}w_{17}w_{17}w_8^2w_5^2w_6^2 - \\
& 4w_{16}w_{10}w_{17}w_{17}w_8^2w_{15}w_6^2 - 4w_{10}w_{17}w_8^2w_5^2w_{15}w_6^2 - 4w_{16}w_{10}w_7^2w_{17}w_8w_5^2w_{15}w_6^2 + 4w_{16}w_{10}w_7^2w_8w_5^2w_{15}w_6^2 - 4w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_6^2 - \\
& 6w_{16}w_{10}w_{17}w_{17}w_8w_5^2w_{15}w_6^2 + 4w_{16}w_{10}w_{17}w_{17}w_8^2w_5^2w_6^2 + 2w_{16}w_7^2w_{17}w_8^2w_5^2w_{15}w_6^2 - 3w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_{15}w_6^2 + 2w_{16}w_{10}w_7^2w_{17}w_8^2w_{15}w_6 - \\
& 2w_{16}w_{10}w_{17}w_{17}w_8^2w_5^2w_{15}w_6 - 4w_{16}w_{10}w_{17}w_8w_5^2w_{15}w_6^2 - 4w_{16}w_{10}w_{17}w_8^2w_5^2w_{15}w_6^2 + 6w_{16}w_{10}w_{17}w_{17}w_8^2w_5^2w_{15}w_6^2 + 4w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_{15}w_6 - \\
& 2w_{16}w_{10}w_7^2w_{17}w_8^2w_{15}w_6^2 + 2w_{16}w_{10}w_{17}w_{17}w_8w_5^2w_{15}w_6 + 4w_{16}w_{10}w_7^2w_{17}w_8^2w_5^2w_6 + 2w_{16}w_{10}w_{17}w_{17}w_8^2w_5^2w_{15}w_6^2 + 2w_{16}w_{10}w_7^2w_{17}w_8w_5^2w_{15}w_6^2 - \\
& 4w_{16}w_{10}w_7^2w_8w_5^2w_{15}w_6
\end{aligned}$$

[illegible]

[illegible]

$$28v_3^2\omega_{11}^2\omega_{19}^2 - 28\omega_7\omega_{11}^3\omega_{19} + 48\omega_7^2\omega_{11}\omega_{19}^2 + 12\omega_{11}^3\omega_{19} - 32\omega_7^2c_s^2\omega_{11}\omega_{19} - 44\omega_7c_s^2\omega_{11}^2\omega_{19} - 64v_3^2\omega_7^2\omega_{11}\omega_{19} - 16v_3^2\omega_7\omega_{11}^3 - 72\omega_7^2c_s^2\omega_{11}\omega_{19}^2 - 16\omega_7c_s^2\omega_{11}^2\omega_{19} + 68v_3^2\omega_7\omega_{11}^3\omega_{19} - 120v_3^2\omega_7^2\omega_{11}\omega_{19}^2 + 48\omega_7^2c_s^2\omega_{11}^2\omega_{19} + 24\omega_7^2\omega_{11}\omega_{19} - 68v_3^2\omega_7\omega_{11}^2\omega_{19}^2 + 8\omega_7\omega_{11}^3 + 16\omega_7\omega_{11}^2\omega_{19} - 43v_3^2\omega_7^2\omega_{11}^3\omega_{19} + 64v_3^2\omega_7\omega_{11}\omega_{19}^2 - 16v_3^2\omega_7^2\omega_{11}^2 - 25\omega_7^2c_s^2\omega_{11}\omega_{19} - 8\omega_7^2\omega_{11}^3 + 25\omega_7^2c_s^2\omega_{11}^2\omega_{19} + 16v_3^2\omega_7^2\omega_{11}^3 + 43v_3^2\omega_7^2\omega_{11}\omega_{19}^2 + 8\omega_7^2\omega_{11}^2 - 40\omega_7^2\omega_{11}\omega_{19} - 17\omega_7^2\omega_{11}\omega_{19}^2 + 56\omega_7^2c_s^2\omega_{11}\omega_{19} + 80v_3^2\omega_7^2\omega_{19}^2 + 104v_3^2\omega_7^2\omega_{11}\omega_{19} + 32\omega_7c_s^2\omega_{11}\omega_{19}^2 + 17\omega_7^2\omega_{11}^3\omega_{19} - 24\omega_7\omega_{11}\omega_{19}^2 - 32\omega_7^2\omega_{19}^2 - 16\omega_7c_s^2\omega_{11}^3$$

$$C_{62} = 12 - 216c_s^4\omega_{11} - 156v_3^2 + 234v_3^2\omega_{11} - 132c_s^2 - 98v_3^2\omega_{11}^2 - 5c_s^4\omega_{11}^3 - 18\omega_{11} + 10v_3^2\omega_{11}^3 + 82c_s^4\omega_{11}^2 + 672v_3^2c_s^2 + 8\omega_{11}^2 + 144c_s^4 - 1008v_3^2c_s^2\omega_{11} - 216v_3^4\omega_{11} - \omega_{11}^3 + 198c_s^2\omega_{11} - 9v_3^4\omega_{11}^3 - 34v_3^2c_s^2\omega_{11}^3 - 78c_s^2\omega_{11}^2 + 144v_3^4 + 404v_3^2c_s^2\omega_{11}^2 + 90v_3^4\omega_{11}^2 + 6c_s^2\omega_{11}^3$$

$$C_{63} = 12 - 36c_s^4\omega_{11} - 252v_3^2 + 378v_3^2\omega_{11} - 36c_s^2 - 154v_3^2\omega_{11}^2 - c_s^4\omega_{11}^3 - 18\omega_{11} + 14v_3^2\omega_{11}^3 + 14c_s^4\omega_{11}^2 + 432v_3^2c_s^2 + 8\omega_{11}^2 + 24c_s^4 - 648v_3^2c_s^2\omega_{11} - 756v_3^4\omega_{11} - \omega_{11}^3 + 54c_s^2\omega_{11} - 29v_3^4\omega_{11}^3 - 18v_3^2c_s^2\omega_{11}^3 - 22c_s^2\omega_{11}^2 + 504v_3^4 + 252v_3^2c_s^2\omega_{11}^2 + 310v_3^4\omega_{11}^2 + 2c_s^2\omega_{11}^3$$

2.4 CLBM1

2.4.1 Definitions

Collision operator C :

$$C(f) = \mathbf{K}^{-1}\mathbf{S}\left(\boldsymbol{\kappa}^{(eq)} - \mathbf{K}f\right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \dots, \omega_{27}),$$

$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2)$.

Matrix \mathbf{K} corresponds to the transformation matrix to the central moment basis defined by

$$\boldsymbol{\kappa} = \left(k_{(0,0,0)}, k_{(1,0,0)}, k_{(0,1,0)}, k_{(0,0,1)}, k_{(1,1,0)}, k_{(1,0,1)}, k_{(0,1,1)}, k_{(1,1,1)}, k_{(2,0,0)}, k_{(0,2,0)}, k_{(0,0,2)}, k_{(2,1,0)}, k_{(2,0,1)}, k_{(2,1,1)}, k_{(1,2,0)}, k_{(0,2,1)}, k_{(1,2,1)}, k_{(1,0,2)}, k_{(0,1,2)}, k_{(1,1,2)}, k_{(2,2,0)}, k_{(2,0,2)}, k_{(0,2,2)}, k_{(2,2,1)}, k_{(2,1,2)}, k_{(1,2,2)}, k_{(2,2,2)} \right)^T,$$

and is given by

$$\begin{array}{lll} \mathbf{K}_{1,i} = (\mathbf{c}_i - \mathbf{v})^{(0,0,0)}, & \mathbf{K}_{2,i} = (\mathbf{c}_i - \mathbf{v})^{(1,0,0)}, & \mathbf{K}_{3,i} = (\mathbf{c}_i - \mathbf{v})^{(0,1,0)}, \\ \mathbf{K}_{4,i} = (\mathbf{c}_i - \mathbf{v})^{(0,0,1)}, & \mathbf{K}_{5,i} = (\mathbf{c}_i - \mathbf{v})^{(1,1,0)}, & \mathbf{K}_{6,i} = (\mathbf{c}_i - \mathbf{v})^{(1,0,1)}, \\ \mathbf{K}_{7,i} = (\mathbf{c}_i - \mathbf{v})^{(0,1,1)}, & \mathbf{K}_{8,i} = (\mathbf{c}_i - \mathbf{v})^{(1,1,1)}, & \mathbf{K}_{9,i} = (\mathbf{c}_i - \mathbf{v})^{(2,0,0)}, \\ \mathbf{K}_{10,i} = (\mathbf{c}_i - \mathbf{v})^{(0,2,0)}, & \mathbf{K}_{11,i} = (\mathbf{c}_i - \mathbf{v})^{(0,0,2)}, & \mathbf{K}_{12,i} = (\mathbf{c}_i - \mathbf{v})^{(2,1,0)}, \\ \mathbf{K}_{13,i} = (\mathbf{c}_i - \mathbf{v})^{(2,0,1)}, & \mathbf{K}_{14,i} = (\mathbf{c}_i - \mathbf{v})^{(2,1,1)}, & \mathbf{K}_{15,i} = (\mathbf{c}_i - \mathbf{v})^{(1,2,0)}, \\ \mathbf{K}_{16,i} = (\mathbf{c}_i - \mathbf{v})^{(0,2,1)}, & \mathbf{K}_{17,i} = (\mathbf{c}_i - \mathbf{v})^{(1,2,1)}, & \mathbf{K}_{18,i} = (\mathbf{c}_i - \mathbf{v})^{(1,0,2)}, \\ \mathbf{K}_{19,i} = (\mathbf{c}_i - \mathbf{v})^{(0,1,2)}, & \mathbf{K}_{20,i} = (\mathbf{c}_i - \mathbf{v})^{(1,1,2)}, & \mathbf{K}_{21,i} = (\mathbf{c}_i - \mathbf{v})^{(2,2,0)}, \\ \mathbf{K}_{22,i} = (\mathbf{c}_i - \mathbf{v})^{(2,0,2)}, & \mathbf{K}_{23,i} = (\mathbf{c}_i - \mathbf{v})^{(0,2,2)}, & \mathbf{K}_{24,i} = (\mathbf{c}_i - \mathbf{v})^{(2,2,1)}, \\ \mathbf{K}_{25,i} = (\mathbf{c}_i - \mathbf{v})^{(2,1,2)}, & \mathbf{K}_{26,i} = (\mathbf{c}_i - \mathbf{v})^{(1,2,2)}, & \mathbf{K}_{27,i} = (\mathbf{c}_i - \mathbf{v})^{(2,2,2)}, \end{array}$$

$\forall i \in \{1, 2, \dots, 27\}$.

The equilibrium central moments are defined as

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K}\mathbf{M}^{-1}\boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left(\rho, 0, 0, 0, 0, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2, 0, 0, 0, 0, 0, 0, 0, 0, \rho c_s^4, \rho c_s^4, \rho c_s^4, 0, 0, 0, \rho c_s^6 \right)^T.$$

2.4.2 Conservation of mass: ρ

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + v_1^2 + 3c_s^2) \frac{v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-1 + 3v_1^2 + c_s^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{\delta_l^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\
& \frac{\delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} - \frac{\delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} - \frac{\delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\
& + (-3v_1^4 \omega_9 - 12v_1^2 \omega_9 c_s^2 + \omega_9 c_s^2 + 6v_1^4 + 2c_s^4 - 6v_1^2 - \omega_9 c_s^4 - 2c_s^2 + 3v_1^2 \omega_9 + 24v_1^2 c_s^2) \frac{\delta_l^4 \rho}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 2\omega_9 - 3\omega_9 c_s^2 + 10v_1^2 + 6c_s^2 - 5v_1^2 \omega_9) \frac{v_1 \delta_l^4 \rho}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& (3\omega_9 - \omega_{12} - 9\omega_9 c_s^2 + v_1^2 \omega_{12} + 3\omega_9 \omega_{12} c_s^2 + 3\omega_{12} c_s^2 - 3v_1^2 \omega_9 + v_1^2 \omega_9 \omega_{12} - \omega_9 \omega_{12}) \frac{v_1 \delta_l^4 \rho}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + \\
& (-2 + \omega_5) \frac{\delta_l^4 c_s^4}{6\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (-\omega_{15} - \omega_{15} \omega_{10} + 3\omega_{15} c_s^2 + 3\omega_{10} - 9\omega_{10} c_s^2 - 3v_2^2 \omega_{10} + v_2^2 \omega_{15} + 3\omega_{15} \omega_{10} c_s^2 + v_2^2 \omega_{15} \omega_{10}) \frac{\delta_l^4 v_2 \rho}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-12v_2^2 \omega_{10} c_s^2 - 3v_2^4 \omega_{10} - \omega_{10} c_s^4 + 6v_2^4 + 2c_s^4 + \omega_{10} c_s^2 + 24v_2^2 c_s^2 + 3v_2^2 \omega_{10} - 6v_2^2 - 2c_s^2) \frac{\delta_l^4}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 2\omega_{10} - 3\omega_{10} c_s^2 - 5v_2^2 \omega_{10} + 10v_2^2 + 6c_s^2) \frac{\delta_l^4 v_2 \rho}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& (3\omega_9 - 9\omega_9 c_s^2 + v_1^2 \omega_9 \omega_{13} - \omega_9 \omega_{13} - \omega_{13} - 3v_1^2 \omega_9 + 3\omega_9 \omega_{13} c_s^2 + 3\omega_{13} c_s^2 + v_1^2 \omega_{13}) \frac{v_1 \delta_l^4 \rho}{12\omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (v_2^2 \omega_{16} \omega_{10} + 3\omega_{16} \omega_{10} c_s^2 - \omega_{16} + 3\omega_{10} + v_2^2 \omega_{16} - 9\omega_{10} c_s^2 - 3v_2^2 \omega_{10} + 3\omega_{16} c_s^2 - \omega_{16} \omega_{10}) \frac{\delta_l^4 v_2 \rho}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{\delta_l^4 c_s^4}{6\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + (-2 + \omega_7) \frac{\delta_l^4 c_s^4}{6\delta_t \omega_7} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (v_3^2 \omega_{18} - \omega_{18} - 9c_s^2 \omega_{11} + 3\omega_{18} c_s^2 + v_3^2 \omega_{18} \omega_{11} - \omega_{18} \omega_{11} + 3\omega_{11} + 3\omega_{18} c_s^2 \omega_{11} - 3v_3^2 \omega_{11}) \frac{v_3 \delta_l^4 \rho}{12\omega_{18} \delta_t \omega_{11}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (-9c_s^2 \omega_{11} + 3\omega_{19} c_s^2 \omega_{11} - \omega_{19} + 3\omega_{19} c_s^2 + v_3^2 \omega_{19} + v_3^2 \omega_{19} \omega_{11} - \omega_{19} \omega_{11} + 3\omega_{11} - 3v_3^2 \omega_{11}) \frac{v_3 \delta_l^4 \rho}{12\omega_{19} \delta_t \omega_{11}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (6v_3^4 + c_s^2 \omega_{11} - 12v_3^2 c_s^2 \omega_{11} + 24v_3^2 c_s^2 - 3v_3^4 \omega_{11} + 2c_s^4 - c_s^4 \omega_{11} - 2c_s^2 - 6v_3^2 + 3v_3^2 \omega_{11}) \frac{\delta_l^4}{24\delta_t \omega_{11}} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 - 3c_s^2 \omega_{11} + 6c_s^2 + 10v_3^2 + 2\omega_{11} - 5v_3^2 \omega_{11}) \frac{v_3 \delta_l^4 \rho}{12\delta_t \omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.4.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2v_1 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l v_2 \rho}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{v_1 \delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{v_1 \delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_9 - 2\omega_9 c_s^2 + 6v_1^2 + 4c_s^2 - 3v_1^2 \omega_9) \frac{\delta_l^2 \rho}{\omega_9 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3v_1 \delta_l^2 \rho}{\omega_9 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + \omega_9 - 3\omega_9 c_s^2 + 2v_1^2 + 6c_s^2 - v_1^2 \omega_9) \frac{v_1 \delta_l^2}{2\omega_9 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_9 - \omega_9 c_s^2 + 6v_1^2 + 2c_s^2 - 3v_1^2 \omega_9) \frac{\delta_l^2 \rho}{2\omega_9 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{\delta_l^2 c_s^2 \rho}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{\delta_l^2 c_s^2 \rho}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega_9^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 + 24\omega_9 - 36\omega_9 c_s^2 + 60v_1^2 + 5\omega_9^2 c_s^2 + 36c_s^2 - 4\omega_9^2 - 60v_1^2 \omega_9 + 11v_1^2 \omega_9^2) \frac{v_1 \delta_l^3 \rho}{6\omega_9^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{v_1 \delta_l^3 \rho}{12\omega_5 \omega_9^2 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 + 12\omega_5 - \omega_5^2) \frac{\delta_l^3 c_s^4}{6\omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{v_1 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_1 \delta_l^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_3 \frac{\delta_l^3 v_2 \rho}{6\omega_5 \omega_{15} \delta_t} \frac{\partial^3 v_1}{\partial x_2^3} + \\
& (-1 + 3v_2^2 + c_s^2) \frac{v_1 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_4 \frac{v_1 \delta_l^3 \rho}{12\omega_9^2 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{v_1 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (-12 + 12\omega_6 - \omega_6^2) \frac{\delta_l^3 c_s^4}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \\
& \frac{v_1 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{v_1 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \delta_l^3 \rho}{6\omega_{18} \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{v_1 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_6 \frac{v_1 \delta_l^4}{12\omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_7 \frac{\delta_l^4 \rho}{12\omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_8 \frac{\delta_l^4 \rho}{12\omega_3^3 \omega_3^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_9 \frac{v_1 \delta_l^4 c_s^2}{12\omega_5^2 \omega_{21} \omega_{15} \omega_3^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& C_{10} \frac{\delta_l^4 c_s^2 \rho}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\delta_l^4 v_2 c_s^2}{12\omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& (-\omega_{15} - \omega_{15} \omega_{10} + 3\omega_{15} c_s^2 + 3\omega_{10} - 9\omega_{10} c_s^2 - 3v_2^2 \omega_{10} + v_2^2 \omega_{15} + 3\omega_{15} \omega_{10} c_s^2 + v_2^2 \omega_{15} \omega_{10}) \frac{v_1 \delta_l^4 v_2 \rho}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& C_{12} \frac{\delta_l^4 c_s^2 \rho}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} +
\end{aligned}$$

$$\begin{aligned}
& (-12v_2^2\omega_{10}c_s^2 - 3v_2^4\omega_{10} - \omega_{10}c_s^4 + 6v_2^4 + 2c_s^4 + \omega_{10}c_s^2 + 24v_2^2c_s^2 + 3v_2^2\omega_{10} - 6v_2^2 - 2c_s^2) \frac{v_1\delta_l^4}{24\delta_t\omega_{10}} \frac{\partial^4\rho}{\partial x_2^4} + \\
& C_{13} \frac{\delta_l^4\rho}{24\omega_5^3\omega_{15}^2\delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + (-4 + 2\omega_{10} - 3\omega_{10}c_s^2 - 5v_2^2\omega_{10} + 10v_2^2 + 6c_s^2) \frac{v_1\delta_l^4 v_2\rho}{12\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + C_{14} \frac{\delta_l^4\rho}{12\omega_5^3\omega_6^3\delta_t\omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + \\
& C_{15} \frac{\delta_l^4 c_s^4\rho}{12\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2\partial x_3} + \\
& (v_2^2\omega_{16}\omega_{10} + 3\omega_{16}\omega_{10}c_s^2 - \omega_{16} + 3\omega_{10} + v_2^2\omega_{16} - 9\omega_{10}c_s^2 - 3v_2^2\omega_{10} + 3\omega_{16}c_s^2 - \omega_{16}\omega_{10}) \frac{v_1\delta_l^4 v_2\rho}{12\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3} + \\
& C_{16} \frac{v_1\delta_l^4 c_s^2}{12\omega_{18}\omega_9^3\omega_6^2\omega_{22}\delta_t\omega_{13}} \frac{\partial^4\rho}{\partial x_1^2\partial x_3^2} + C_{17} \frac{\delta_l^4 c_s^2\rho}{12\omega_{18}\omega_9^3\omega_6^2\omega_{22}\delta_t\omega_{13}} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + C_{18} \frac{\delta_l^4}{2\omega_5\omega_{18}\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_{20}\omega_{14}\omega_8} \frac{\partial^4\rho}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{19} \frac{\delta_l^4\rho}{2\omega_5\omega_{18}\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_{20}\omega_{14}\omega_8} \frac{\partial^4 v_1}{\partial x_1\partial x_2\partial x_3^2} + C_{20} \frac{\delta_l^4\rho}{12\omega_5^2\omega_{18}\omega_9\omega_{12}\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_7\omega_{20}\omega_{14}\omega_8} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{21} \frac{v_3\delta_l^4\rho}{\omega_5\omega_{18}\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_{20}\omega_{14}\omega_8} \frac{\partial^4 v_3}{\partial x_1\partial x_2\partial x_3^2} + C_{22} \frac{\delta_l^4}{12\omega_5\omega_{18}\omega_{15}\omega_6\delta_t\omega_7\omega_{20}\omega_{17}\omega_8} \frac{\partial^4\rho}{\partial x_2^2\partial x_3^2} + \\
& C_{23} \frac{\delta_l^4\rho}{4\omega_5^2\omega_{18}\omega_{15}\omega_6^2\delta_t\omega_{20}\omega_{17}\omega_8} \frac{\partial^4 v_1}{\partial x_2^2\partial x_3^2} + C_{24} \frac{\delta_l^4 v_2\rho}{2\omega_5\omega_{18}\omega_{15}\omega_6\delta_t\omega_{20}\omega_{17}\omega_8} \frac{\partial^4 v_2}{\partial x_2^2\partial x_3^2} + C_{25} \frac{\delta_l^4\rho}{4\omega_5\omega_{18}\omega_{15}\omega_6\delta_t\omega_{20}\omega_{17}\omega_8} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3^2} + \\
& C_{26} \frac{v_3\delta_l^4 c_s^2}{12\omega_{18}^2\omega_9\omega_6^2\omega_{22}\delta_t\omega_{13}\omega_{11}} \frac{\partial^4\rho}{\partial x_1\partial x_3^2} + \\
& (v_3^2\omega_{18} - \omega_{18} - 9c_s^2\omega_{11} + 3\omega_{18}c_s^2 + v_3^2\omega_{18}\omega_{11} - \omega_{18}\omega_{11} + 3\omega_{11} + 3\omega_{18}c_s^2\omega_{11} - 3v_3^2\omega_{11}) \frac{v_3 v_1\delta_l^4\rho}{12\omega_{18}\delta_t\omega_{11}} \frac{\partial^4 v_1}{\partial x_1\partial x_3^2} + \\
& C_{27} \frac{\delta_l^4 c_s^2\rho}{12\omega_{18}\omega_9\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}} \frac{\partial^4 v_3}{\partial x_1\partial x_3^2} + \\
& (-9c_s^2\omega_{11} + 3\omega_{19}c_s^2\omega_{11} - \omega_{19} + 3\omega_{19}c_s^2 + v_3^2\omega_{19} + v_3^2\omega_{19}\omega_{11} - \omega_{19}\omega_{11} + 3\omega_{11} - 3v_3^2\omega_{11}) \frac{v_3 v_1\delta_l^4\rho}{12\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 v_2}{\partial x_2\partial x_3^2} + \\
& (6v_3^4 + c_s^2\omega_{11} - 12v_3^2c_s^2\omega_{11} + 24v_3^2c_s^2 - 3v_3^4\omega_{11} + 2c_s^4 - c_s^4\omega_{11} - 2c_s^2 - 6v_3^2 + 3v_3^2\omega_{11}) \frac{v_1\delta_l^4}{24\delta_t\omega_{11}} \frac{\partial^4\rho}{\partial x_3^4} + C_{28} \frac{\delta_l^4\rho}{24\omega_{18}^2\omega_6^3\delta_t} \frac{\partial^4 v_1}{\partial x_3^4} \\
& + (-4 - 3c_s^2\omega_{11} + 6c_s^2 + 10v_3^2 + 2\omega_{11} - 5v_3^2\omega_{11}) \frac{v_3 v_1\delta_l^4\rho}{12\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -36v_1^4\omega_9 - 144v_1^2\omega_9c_s^2 + 12\omega_9c_s^2 + 36v_1^4 + 7v_1^4\omega_9 + \omega_9^2c_s^4 + 12c_s^4 - 36v_1^2 - 12\omega_9c_s^4 + 24v_1^2\omega_9^2c_s^2 - \omega_9^2c_s^2 - 12c_s^2 + 36v_1^2\omega_9 - 7v_1^2\omega_9^2 + 144v_1^2c_s^2 \\
C_2 &= 12\omega_5v_1^2\omega_9^2 + 6\omega_5\omega_9\omega_{12} - 18\omega_5\omega_9\omega_{12}c_s^2 - 12\omega_5\omega_{12} + 6v_1^2\omega_9^2\omega_{12} - 6\omega_9^2\omega_{12} + 18\omega_5^2\omega_{12}c_s^2 - 6\omega_5v_1^2\omega_9\omega_{12} + 36\omega_5\omega_9^2c_s^2 + 36\omega_5\omega_{12}c_s^2 - \\
& 12\omega_5v_1^2\omega_9 + 12\omega_5v_1^2\omega_{12} - 36\omega_5\omega_9c_s^2 - 36\omega_9^2c_s^2 - 12\omega_5\omega_9 - 3\omega_5v_1^2\omega_9^2\omega_{12} + 12\omega_9^2 - 12v_1^2\omega_9^2 + 12\omega_5\omega_9 - 11\omega_5\omega_9^2\omega_{12}c_s^2 + 3\omega_5\omega_9^2\omega_{12} \\
C_3 &= 6 - 3\omega_5 - \omega_5v_2^2\omega_{15} - 3\omega_{15} + 9\omega_{15}c_s^2 - 3\omega_5\omega_{15}c_s^2 - 6v_2^2 - 18c_s^2 + 3\omega_5v_2^2 + 9\omega_5c_s^2 + \omega_5\omega_{15} + 3v_2^2\omega_{15} \\
C_4 &= 18\omega_9^2\omega_{13}c_s^2 - 18\omega_9\omega_6\omega_{13}c_s^2 + 12v_1^2\omega_9^2\omega_6 - 12\omega_9^2\omega_6 - 3v_1^2\omega_9^2\omega_6\omega_{13} + 3\omega_9^2\omega_6\omega_{13} + 36\omega_6\omega_{13}c_s^2 + 36\omega_9^2\omega_6c_s^2 - 6v_1^2\omega_9\omega_6\omega_{13} + 6v_1^2\omega_9^2\omega_{13} - \\
& 11\omega_9^2\omega_6\omega_{13}c_s^2 + 6\omega_9\omega_6\omega_{13} - 6\omega_9^2\omega_{13} - 36\omega_9\omega_6c_s^2 - 36\omega_9^2c_s^2 - 12\omega_6\omega_{13} + 12\omega_9^2 + 12v_1^2\omega_6\omega_{13} - 12v_1^2\omega_9\omega_6 - 12v_1^2\omega_9^2 + 12\omega_9\omega_6 \\
C_5 &= 6 + 3v_3^2\omega_{18} - 3\omega_{18} + 9\omega_{18}c_s^2 - 3\omega_{18}\omega_6c_s^2 - 3\omega_6 + 9\omega_6c_s^2 - 18c_s^2 - v_3^2\omega_{18}\omega_6 + \omega_{18}\omega_6 - 6v_3^2 + 3v_3^2\omega_6 \\
C_6 &= 12 - 216v_1^4\omega_9 - 5\omega_9^4c_s^4 - 18\omega_9 - 1008v_1^2\omega_9c_s^2 - 9v_1^4\omega_9^3 + 198\omega_9c_s^2 + 144v_1^4 + 90v_1^4\omega_9^2 + 82\omega_9^2c_s^4 + 144c_s^4 - 156v_1^2 - \omega_9^3 - 216\omega_9c_s^4 + \\
& 404v_1^2\omega_9^2c_s^2 - 78\omega_9^2c_s^2 - 132c_s^2 + 8\omega_9^2 + 234v_1^2\omega_9 - 98v_1^2\omega_9^2 + 672v_1^2c_s^2 + 10v_1^2\omega_9^3 + 6\omega_9^3c_s^2 - 34v_1^2\omega_9^3c_s^2 \\
C_7 &= 12 - 756v_1^4\omega_9 - \omega_9^4c_s^4 - 18\omega_9 - 648v_1^2\omega_9c_s^2 - 29v_1^4\omega_9^3 + 54\omega_9c_s^2 + 504v_1^4 + 310v_1^4\omega_9^2 + 14\omega_9^2c_s^4 + 24c_s^4 - 252v_1^2 - \omega_9^3 - 36\omega_9c_s^4 + \\
& 252v_1^2\omega_9^2c_s^2 - 22\omega_9^2c_s^2 - 36c_s^2 + 8\omega_9^2 + 378v_1^2\omega_9 - 154v_1^2\omega_9^2 + 432v_1^2c_s^2 + 14v_1^2\omega_9^3 + 2\omega_9^3c_s^2 - 18v_1^2\omega_9^3c_s^2 \\
C_8 &= 12\omega_5^3\omega_9\omega_{12}c_s^2 + 39\omega_5^3v_1^2\omega_9^2\omega_{12} - 3\omega_5^2v_1^2\omega_9^3\omega_{12}c_s^2 - 5\omega_5^2\omega_9^3\omega_{12}c_s^2 + 6\omega_5^2v_1^2\omega_9^3\omega_{12}^2 + 72\omega_5^3v_1^4\omega_9^2\omega_{12} + \omega_5^3\omega_9^2\omega_{12}^2c_s^4 - 18\omega_5^2\omega_9^3\omega_{12}c_s^4 + \\
& 252\omega_5^3v_1^2\omega_{12}c_s^2 + 12\omega_5^3\omega_{12}c_s^4 + 72\omega_5^3v_1^4\omega_{12} - 19\omega_5^3v_1^2\omega_9^2\omega_{12}^2 + 36\omega_5^2v_1^4\omega_9^3\omega_{12} + 6\omega_5^2\omega_9^3\omega_{12}c_s^2 + 4\omega_5^3v_1^4\omega_9^3\omega_{12}^2 - 99\omega_5^3v_1^2\omega_9^3\omega_{12}c_s^2 - \\
& 18\omega_5^3v_1^2\omega_9^2\omega_{12}c_s^2 - 36\omega_5^2v_1^4\omega_9^3 - 12\omega_5^2\omega_9^2\omega_{12}c_s^2 - 39\omega_5^3v_1^4\omega_9^3\omega_{12} - 108\omega_5^3v_1^2\omega_9\omega_{12}c_s^2 + 6\omega_5^3\omega_9^3\omega_{12}c_s^4 - 36\omega_5^3v_1^2\omega_9^3 - 6\omega_5^2v_1^4\omega_9^3\omega_{12}^2 - \\
& 72\omega_5^3v_1^2\omega_9^2\omega_{12} + 36\omega_5^2v_1^4\omega_9^2\omega_{12}c_s^2 - 24\omega_5\omega_9^3\omega_{12}c_s^4 + 60\omega_5^3v_1^2\omega_9^2\omega_{12}c_s^2 - 12\omega_5\omega_9^3\omega_{12}c_s^2 + 12\omega_5^2\omega_9\omega_{12}c_s^2 + 19\omega_5^3v_1^4\omega_9^2\omega_{12} - 36\omega_5^2v_1^2\omega_9^3\omega_{12} + \\
& 6\omega_5^2\omega_9^2\omega_{12}c_s^4 - 4\omega_5^3v_1^2\omega_9^3\omega_{12} - 36\omega_5^2v_1^2\omega_9\omega_{12}c_s^2 + 36\omega_5^3v_1^2\omega_9^2\omega_{12}c_s^2 + 198\omega_5^3v_1^2\omega_9^2\omega_{12}c_s^2 - 72\omega_5^3v_1^2\omega_{12}^2 - 90\omega_5^3v_1^4\omega_9\omega_{12} + 6\omega_5\omega_9^3\omega_{12}c_s^2 + 108\omega_5^3v_1^2\omega_9^3c_s^2 + \\
& 12\omega_5^2\omega_9^2\omega_{12}c_s^4 - 6\omega_5^3\omega_9\omega_{12}c_s^2 - 6\omega_5^2\omega_9^3\omega_{12}c_s^2 - 306\omega_5^3v_1^2\omega_9\omega_{12}c_s^2 - \omega_5^3\omega_9^3\omega_{12}c_s^4 + 12\omega_5\omega_9^3\omega_{12}c_s^4 - 12\omega_5^2\omega_9\omega_{12}c_s^4 + 18\omega_5^2v_1^2\omega_9^2\omega_{12}c_s^2 + \\
& 36\omega_5^3v_1^2\omega_9\omega_{12} + 12\omega_5^3\omega_{12}c_s^4 + 13\omega_5^2\omega_9^3\omega_{12}c_s^4 - 108\omega_5^3v_1^2\omega_9c_s^2 + 90\omega_5^3v_1^2\omega_9\omega_{12} - \omega_5^3\omega_9^2\omega_{12}c_s^2 + 12\omega_5^3v_1^2\omega_9^3\omega_{12}c_s^2 - 12\omega_5^3\omega_9\omega_{12}c_s^4 - 36\omega_5^3v_1^4\omega_9^2 + \\
& 36\omega_5^2v_1^2\omega_9^3\omega_{12}c_s^2 + 36\omega_5^2v_1^2\omega_9^3\omega_{12}c_s^2 + 54\omega_5^2v_1^2\omega_9^3\omega_{12}c_s^2 + 18\omega_5^2\omega_9^3\omega_{12}c_s^2 + 36\omega_5^3v_1^4\omega_9^3 - 12\omega_5^3\omega_{12}c_s^2 - 36\omega_5^3v_1^4\omega_9\omega_{12} - 6\omega_5^3\omega_9^2\omega_{12}c_s^4 - 108\omega_5^2v_1^2\omega_9^3c_s^2 \\
C_9 &= -\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 - 12\omega_5\omega_{21}v_1^2\omega_9^2\omega_{12}^2 + 12\omega_5^2\omega_{15}\omega_9^3\omega_{12} - 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^2 - 12\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 6\omega_5^2\omega_9^3\omega_{12}^2 + 36\omega_5\omega_{15}\omega_9^3\omega_{12}c_s^2 - \\
& 12\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^3 - 12\omega_5^2v_1^2\omega_{15}\omega_9^3\omega_{12} - 18\omega_5^2\omega_9^3\omega_{12}c_s^2 - 6\omega_5^2v_1^2\omega_9^3\omega_{12} + 6\omega_5^2\omega_{15}\omega_9^2\omega_{12}^2 - 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9\omega_{12} + 12\omega_5^2v_1^2\omega_{15}\omega_9^3\omega_{12} - \\
& 36\omega_5^2\omega_{15}\omega_9^3\omega_{12}c_s^2 + 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^3 + 36\omega_{21}\omega_{15}\omega_9^3\omega_{12}c_s^2 - 18\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12\omega_5^2\omega_{21}\omega_{15}\omega_{12}^2 + 12\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + \\
& 5\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}c_s^2 + 6\omega_5^2\omega_{21}v_1^2\omega_9^2\omega_{12} - 6\omega_5^2v_1^2\omega_{15}\omega_9^3\omega_{12} - 36\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2c_s^2 - 18\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^2v_1^2\omega_{15}\omega_9^2\omega_{12} - \\
& 12\omega_5^2\omega_{15}\omega_9^3\omega_{12} - 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9\omega_{12} + 36\omega_5^2\omega_{21}\omega_{15}\omega_{12}c_s^2 - 12\omega_5v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 12\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 40\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12}c_s^2 + \\
& 2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 6\omega_5^2v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 54\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}c_s^2 - 18\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 12\omega_5\omega_{21}\omega_{15}\omega_9^3 - 18\omega_5^2\omega_{15}\omega_9^3\omega_{12}c_s^2 + \\
& 6\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 6\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 + 12\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12\omega_5v_1^2\omega_9^3\omega_{12}^2 + 18\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12} - 6\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}c_s^2 + 36\omega_5\omega_9^3\omega_{12}c_s^2 + \\
& 12\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 36\omega_5^2\omega_{15}\omega_9^3\omega_{12}c_s^2 - 12\omega_5\omega_{15}\omega_9^3\omega_{12} - 36\omega_{21}\omega_{15}\omega_9^2\omega_{12}c_s^2 + \omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 18\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12}^2 -
\end{aligned}$$

$2w_5v_3^2v_{1w18}v_{2w9w6w22w13w20w14w8} - w_5w_{18}v_3^2w_{12w6w22w13c_s^2w20w14w8} - 4w_5v_{1w18}v_{2w9w12w22c_s^2w20w14w8} +$
 $2w_5v_3^2w_{18}v_3^2w_{12w6w22w20w14w8} - 2v_{1w18}v_{2w9w12w6w22w13c_s^2w14w8} + 4w_5v_3^2v_{1w18}v_{2w9w12w20w14w8} + w_5v_3^2w_{18}w_{6w22w13c_s^2w20w14w8} -$
 $2w_3^2w_{18}v_{2w9w12w6w22w13w14} + 2w_5v_3^2v_{1w18}v_{2w9w12w6w13w20w14w8} - 2w_5w_{18}v_3^2w_{9w12w22w13c_s^2w20} + 4w_5v_{1w18}v_{2w9w12w6w22w13c_s^2w20w14} +$
 $4w_5v_{1w18}v_{2w12w6w22c_s^2w20w8} + 2v_3^2w_{18}v_{2w9w12w6w22w13w20w14} + 2w_5v_3^2w_{9w12w22w13c_s^2w20w14w8} - 2w_5w_{18}v_3^2w_{9w12w22w13c_s^2w20w8} +$
 $4v_3^2v_{1w18}v_{2w9w6w22w13w20w8} + 2w_5w_{18}v_3^2w_{9w12w22c_s^2w20w14w8} + 2w_5w_{18}v_3^2w_{9w12w13c_s^2w20w14w8} - 2w_5v_3^2w_{18}w_{9w12w22c_s^2w20w8} +$
 $2w_5w_{18}v_3^2w_{9w6w22w13c_s^2w20w8} - 2v_3^2w_{18}w_{9w12w6w22w13c_s^2w20} - 2w_5w_{18}v_3^2w_{12w6w22c_s^2w20w8} + 4w_5v_{1w18}v_{2w9w12w22w13c_s^2w20} +$
 $w_5v_3^2w_{18}v_3^2w_{9w12w6w22w13w20w14w8} - 2w_5v_3^2w_{9w12w6w22w13c_s^2w14w8} + 4w_5v_{1w18}v_{2w9w12w22w13c_s^2w14w8} -$
 $2v_{1w18}v_{2w9w6w22w13c_s^2w20w14w8} - 2w_5v_3^2w_{18}w_{9w12w22w13c_s^2w20w14w8} - 2v_3^2w_{18}v_{2w9w12w22w13c_s^2w20w14w8} - 2w_5w_{18}v_3^2w_{9w12w6w22w13c_s^2w20w8} +$
 $v_3^2w_{18}w_{9w12w6w22w13c_s^2w14w8} + 2w_5w_{18}v_3^2w_{12w6w22w13c_s^2w20w8} + 2w_5w_{18}v_3^2w_{12w6w22w13c_s^2w20} + 2w_5v_3^2w_{18}w_{9w12w22w13c_s^2w20w14} -$
 $2w_5v_3^2w_{18}v_3^2w_{12w6w22w20w8} - 2w_5v_3^2w_{18}w_{6w22w13c_s^2w20w8} - 4w_5v_3^2v_{1w18}v_{2w9w12w22w13w20w14w8} + 2w_5v_3^2w_{18}v_3^2w_{9w12w13w20w14w8} -$
 $2w_5v_3^2v_{1w18}v_{2w9w12w6w22w13w20w14w8} - 4w_5v_{1w18}v_{2w12w6w22w13c_s^2w20w8} - 4w_5v_{1w18}v_{2w9w12w6w22w13c_s^2w20} +$
 $2w_5v_3^2w_{18}v_3^2w_{12w6w22w13w20w8} - 4w_5v_3^2v_{1w18}v_{2w9w12w13w20w14w8} - w_5v_3^2w_{18}v_3^2w_{12w6w22w13w20w14w8} +$
 $2w_5v_{1w18}v_{2w12w6w22w13c_s^2w20w14w8} + 2w_5v_3^2w_{18}w_{9w12w22w13c_s^2w20w8} + 2w_5v_3^2v_{1w18}v_{2w9w12w6w22w13w20w14w8} + 4v_{1w18}v_{2w9w12w6w22w13c_s^2w14} -$
 $2w_5w_{18}v_3^2w_{9w12w6w22w13c_s^2w20w14} - 4w_5v_{1w18}v_{2w9w12w22w13c_s^2w20w14w8} + w_5v_3^2v_3^2w_{9w12w6w13w20w14w8} + 2v_3^2w_{18}w_{9w12w6w22w13c_s^2w20w8} -$
 $4w_5w_{18}v_3^2w_{9w12w6w22w13c_s^2w14w8} - 4w_5v_{1w18}v_{2w9w12w6w22w13w20w14w8} + 2w_5w_{18}v_3^2w_{9w12w22w13c_s^2w20w14} + 2w_5v_3^2w_{18}w_{12w6w22w13c_s^2w20w8} +$
 $2w_5v_3^2v_{1w18}v_{2w9w12w22w13w20w14w8} - 2w_{18}v_3^2w_{9w6w22w13c_s^2w20w8} + 2w_5v_3^2w_{18}w_{9w12w6w22w13c_s^2w20} - 4w_5v_{1w18}v_{2w9w12w6w22w13c_s^2w20w8} -$
 $2w_5v_3^2w_{18}v_3^2w_{9w12w22w13w14} - 2w_5v_3^2w_{18}v_3^2w_{9w12w22w13w20w14w8} - 2w_5v_3^2w_{18}v_3^2w_{12w6w20w14w8} - w_5v_3^2v_3^2w_{9w12w6w22w13w20w14w8} +$
 $2w_5v_3^2w_{18}v_3^2w_{9w12w6w22w13w20w14} + 2w_5v_3^2w_{18}w_{9w12w6w22w13c_s^2w14w8} + 2w_5v_{1w18}v_{2w9w12w6w13c_s^2w20w14w8} -$
 $v_3^2w_{18}v_3^2w_{9w12w6w22w13w20w14w8} + 4w_5v_{1w18}v_{2w9w12w6w22w13w20w14w8} + 4w_5v_3^2v_{1w18}v_{2w9w12w22w13w14w8} + 2v_3^2w_{18}w_{9w12w6w22w13c_s^2w20w14} -$
 $4w_5v_3^2v_{1w18}v_{2w9w12w6w22w13w14} + 2w_5w_{18}v_3^2w_{9w12w22w13c_s^2w20w8} + 2w_5v_{1w18}v_{2w9w12w22w13c_s^2w20w14w8} -$
 $4w_5v_{1w18}v_{2w9w12w22w13c_s^2w20w14} + 4w_5v_{1w18}v_{2w9w12w22w13c_s^2w14w8} + 4v_3^2v_{1w18}v_{2w9w12w6w22w13w20} + 2w_5w_{18}v_3^2w_{9w12w6c_s^2w20w14w8} -$
 $4v_{1w18}v_{2w9w12w6w22w13c_s^2w20w8} - 2w_5w_{18}v_3^2w_{9w12c_s^2w20w14w8} - 2w_5v_3^2v_{1w18}v_{2w9w12w6w13w20w14w8} - w_5w_{18}v_3^2w_{9w6w22w13c_s^2w20w14w8} +$
 $w_5w_{18}v_3^2w_{6w22w13c_s^2w20w14w8} - 2w_5v_3^2w_{18}w_{12w6w22w13c_s^2w20w14w8} + w_5w_{18}v_3^2w_{9w12w6w13c_s^2w20w14w8} -$
 $2w_5v_3^2w_{18}v_3^2w_{6w22w13w20w8} + v_3^2w_{18}v_3^2w_{9w12w6w22w13w14w8} + 4w_5v_{1w18}v_{2w9w12w22w1c_s^2w20w14w8} + 2w_5w_{18}v_3^2w_{9w12w6w22c_s^2w20w14w8} -$
 $2w_5w_{18}v_3^2w_{9w12w6w22c_s^2w20w14w8} + 2w_5v_3^2w_{18}w_{9w6w22w13c_s^2w20w8} - 2w_5v_{1w18}v_{2w9w12w6w22w13c_s^2w20w14w8} -$
 $4w_5v_{1w18}v_{2w12w6w22c_s^2w20w14w8} - 2w_{18}v_3^2w_{9w12w6w22w13c_s^2w20} - 2w_5v_{1w18}v_{2w12w6w13c_s^2w20w14w8} - 4v_{1w18}v_{2w9w12w6w22w13c_s^2w20w14} +$
 $4w_5v_3^2v_{1w18}v_{2w9w12w22w20w8} + 4w_5v_{1w18}v_{2w9w12w13c_s^2w20w14w8} + 2w_5v_3^2v_3^2w_{9w12w22w13w20w14w8} - 2w_5v_{1w18}v_{2w6w22w13c_s^2w20w14w8} -$
 $2v_3^2v_{1w18}v_{2w9w6w22w13w20w14w8} - w_{18}v_3^2w_{9w12w6w22w13c_s^2w20w14w8} + 2w_5v_3^2w_{18}w_{9w12w6w2$

[illegible]

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$$\begin{aligned}
& 2\omega_5 v_3 v_{18} \omega_{15} c_s^2 \omega_{20} \omega_{17} \omega_8 + 4\omega_5 v_3^2 v_{18} \omega_{15} \omega_{17} - \omega_5 v_3 v_1^2 \omega_{15} \omega_6 \omega_{20} \omega_{17} \omega_8 - \omega_5 v_3 v_{18} \omega_6 c_s^2 \omega_{20} \omega_{17} \omega_8 - 4\omega_5 v_3 v_{18} \omega_{15} c_s^2 \omega_{17} + \\
& \omega_5 v_3^2 v_{18} \omega_{15} \omega_{20} \omega_{17} \omega_8 - 4\omega_5 v_3 v_1^2 \omega_{18} \omega_{15} \omega_{20} + \omega_5 v_3 v_1^2 \omega_{18} \omega_{15} \omega_6 \omega_{20} \omega_{17} \omega_8 + 2\omega_5 v_3 v_1^2 \omega_{15} \omega_{20} \omega_{17} \omega_8 + 4\omega_5 v_3 v_1^2 \omega_{18} \omega_{15} \omega_6 \omega_{17} - \\
& 2\omega_5 v_3 v_1^2 \omega_{18} \omega_{15} \omega_{20} \omega_{17} \omega_8 + 2\omega_5 v_3 v_{18} \omega_{15} c_s^2 \omega_{20} \omega_8 + 4\omega_5 v_3 v_1^2 \omega_{18} \omega_{15} \omega_{17} \omega_8 - 2v_{18} v_{15} \omega_6 c_s^2 \omega_{20} \omega_{17} + 2v_3 v_{18} \omega_{15} \omega_6 c_s^2 \omega_{20} \omega_{17} \omega_8 - \\
& 2\omega_5 v_3^2 v_{18} \omega_{15} \omega_6 \omega_{20} \omega_8 - 4v_3 v_1^2 \omega_{18} \omega_{15} \omega_6 \omega_{20} \omega_8 - 4v_3^2 v_{18} v_{15} \omega_6 \omega_{20} \omega_{17} - 4v_{18} \omega_{15} \omega_6 c_s^2 \omega_{20} \omega_{17} - 2\omega_5 v_3 v_{18} \omega_{15} \omega_6 \omega_{20} \omega_8 + \\
& 2\omega_5 v_{18} \omega_{15} \omega_6 c_s^2 \omega_{17} \omega_8 + 4\omega_5 v_3^2 v_{18} \omega_{15} \omega_{17} \omega_8 + 2\omega_5 v_3 v_{15} c_s^2 \omega_{20} \omega_{17} \omega_8 + 2\omega_5 v_3^2 v_{18} \omega_{15} \omega_6 \omega_{17} \omega_8 - 4\omega_5 v_3 v_{18} \omega_{15} \omega_6 c_s^2 \omega_{20} \omega_{17}
\end{aligned}$$

$$\begin{aligned}
C_{26} = & -36w_{18}^2w_{18}w_{6w}w_{22}c_s^2 + 3w_{18}w_{9w}w_{13}^2w_{22}w_{13}w_{11} - 12w_{18}^2w_{9w}w_{6w}w_{22}w_{13}w_{11} - 12w_{18}^2w_{18}w_{9w}w_{6w}w_{11} + 3w_{18}^2w_{9w}w_{6w}^2w_{22}w_{13}c_s^2w_{11} + 12w_{18}^2w_{9w}w_{6w}w_{22} - \\
& 12w_{18}^2w_{9w}w_{22}w_{13}w_{11} + 12w_{18}^2w_{18}w_{9w}w_{6w}w_{13}w_{11} + 18w_{18}^2w_{6w}^2w_{22}w_{13}c_s^2 - 18w_{18}^2w_{9w}w_{6w}^2w_{13}c_s^2w_{11} + 12w_{18}w_{9w}w_{22}w_{13}w_{11} - 12w_{18}^2w_{18}w_{9w}w_{6w}w_{13}w_{11} - \\
& 36w_{18}^2w_{9w}w_{6w}w_{22}w_{13}c_s^2w_{11} + w_{18}^2w_{18}w_{9w}w_{6w}^2w_{22}w_{13}w_{11} + 6w_{18}^2w_{18}w_{6w}^2w_{13}w_{11} - 36w_{18}^2w_{9w}w_{6w}^2c_s^2w_{11} - 6w_{9w}w_{18}^2w_{22}w_{13}w_{11} - 18w_{18}^2w_{9w}w_{6w}w_{22}w_{13} + \\
& 36w_{18}^2w_{6w}^2c_s^2w_{11} + 18w_{18}^2w_{9w}w_{6w}^2w_{13}c_s^2w_{11} - 6w_{18}^2w_{18}w_{6w}^2w_{13}w_{11} + 12w_{18}^2w_{18}^2w_{9w}w_{6w}w_{11} - 12w_{18}^2w_{18}w_{9w}w_{6w}w_{22} - 3w_{18}^2w_{18}w_{9w}w_{6w}^2w_{22}w_{13}w_{11} + \\
& 54w_{18}^2w_{9w}w_{6w}w_{22}w_{13}c_s^2 - 5w_{18}^2w_{18}w_{9w}w_{6w}^2w_{22}w_{13} - w_{18}^2w_{9w}w_{6w}^2w_{22}w_{13}w_{11} + 6w_{18}w_{18}^2w_{9w}w_{6w}^2w_{13}w_{11} - 6w_{18}^2w_{18}^2w_{6w}^2w_{13}w_{11} + 12w_{18}^2w_{9w}w_{6w}w_{13}w_{11} - \\
& 12w_{18}^2w_{18}w_{9w}w_{22}w_{13}w_{11} - 12w_{18}^2w_{18}w_{9w}w_{22}w_{13} - 36w_{9w}w_{6w}w_{22}w_{13}c_s^2w_{11} + 18w_{18}^2w_{18}w_{9w}w_{6w}w_{22}w_{13} - 18w_{18}w_{9w}w_{6w}w_{22}w_{13}w_{11} + 6w_{18}^2w_{9w}w_{6w}^2w_{22}w_{13}w_{11} - \\
& 6w_{18}^2w_{6w}^2w_{22}w_{13} - 36w_{18}w_{9w}w_{22}w_{13}c_s^2w_{11} - 18w_{18}^2w_{6w}^2w_{13}c_s^2w_{11} - 12w_{18}^2w_{18}w_{9w}w_{6w}^2w_{11} - 36w_{18}^2w_{6w}^2w_{22}c_s^2 + 18w_{9w}w_{6w}^2w_{22}w_{13}c_s^2w_{11} + 12w_{9w}w_{6w}w_{22}w_{13}w_{11} + \\
& 12w_{18}^2w_{18}w_{9w}w_{6w}^2w_{22} - 12w_{18}^2w_{18}w_{9w}w_{6w}w_{22}w_{13}w_{11} - 36w_{18}^2w_{9w}w_{22}w_{13}c_s^2 - 12w_{18}w_{9w}w_{6w}^2w_{13}w_{11} + 12w_{18}^2w_{18}w_{9w}w_{22}w_{13}w_{11} + 36w_{18}w_{9w}w_{6w}^2w_{13}c_s^2w_{11} + \\
& 12w_{18}^2w_{18}w_{9w}w_{22}w_{13} - 15w_{18}^2w_{18}w_{9w}w_{22}w_{13}c_s^2 - 12w_{18}^2w_{18}^2w_{11} + 6w_{18}^2w_{18}w_{6w}^2w_{22}w_{13} + 12w_{18}^2w_{6w}^2w_{22} + 36w_{18}^2w_{9w}w_{6w}^2w_{22}c_s^2 - 9w_{18}w_{9w}w_{6w}^2w_{22}w_{13}c_s^2w_{11} - \\
& 6w_{18}^2w_{18}w_{9w}w_{6w}^2w_{13}w_{11} + 18w_{18}^2w_{18}w_{9w}w_{6w}w_{22}w_{13}w_{11} - 36w_{18}^2w_{9w}w_{6w}w_{13}c_s^2w_{11} - 12w_{18}^2w_{18}w_{9w}w_{6w}w_{22} + 54w_{18}w_{9w}w_{6w}w_{22}w_{13}c_s^2w_{11} + 36w_{18}^2w_{18}w_{9w}w_{6w}^2c_s^2w_{11} + \\
& 6w_{18}^2w_{18}w_{9w}w_{6w}^2w_{13}w_{11} + 12w_{18}^2w_{18}^2w_{11} + 12w_{18}^2w_{18}w_{9w}w_{6w}w_{22}w_{13}w_{11} + 12w_{18}^2w_{18}w_{9w}w_{6w}^2w_{11} + 5w_{18}^2w_{18}w_{9w}w_{6w}w_{22}w_{13} + 36w_{18}^2w_{18}w_{9w}w_{22}w_{13}c_s^2w_{11} - 12w_{18}^2w_{18}w_{9w}w_{6w}^2w_{22}
\end{aligned}$$

2.4.4 Conservation of momentum: ρv_2

$$\begin{aligned}
& v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_1 \delta_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 v_2 \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_1 \rho}{\delta_t} \frac{\partial v_2}{\partial x_1} + (v_2^2 + c_s^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2 \delta_1 v_2 \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_1 \rho}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\
& \frac{\delta_1 v_2 \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2}{2 \omega_5 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2}{2 \omega_5 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\
& (-2 + \omega_{10} - 2 \omega_{10} c_s^2 - 3 v_2^2 \omega_{10} + 6 v_2^2 + 4 c_s^2) \frac{\delta_1^2}{\delta_t \omega_{10}} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_{10}) \frac{3 \delta_1^2 v_2 \rho}{\delta_t \omega_{10}} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2 \delta_t \omega_7} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + \\
& (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2 \delta_t \omega_7} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2 \rho}{2 \omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2 \rho}{2 \omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (-2 + \omega_{10} - 3 \omega_{10} c_s^2 - v_2^2 \omega_{10} + 2 v_2^2 + 6 c_s^2) \frac{\delta_1^2 v_2}{2 \delta_t \omega_{10}} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_{10} - \omega_{10} c_s^2 - 3 v_2^2 \omega_{10} + 6 v_2^2 + 2 c_s^2) \frac{\delta_1^2 \rho}{2 \delta_t \omega_{10}} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_7) \frac{\delta_1^2 c_s^2 \rho}{2 \delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_7) \frac{\delta_1^2 c_s^2 \rho}{2 \delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_3^2} + (-1 + v_1^2 + 3 c_s^2) \frac{v_1 \delta_1^3 v_2}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3 v_1^2 + c_s^2) \frac{\delta_1^3 v_2 \rho}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& C_1 \frac{v_1 \delta_1^3 \rho}{6 \omega_5 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 + 12 \omega_5 - \omega_5^2) \frac{\delta_1^3 c_s^2 \rho}{6 \omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \frac{\delta_1^3 v_2 c_s^2 \rho}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_2 \frac{\delta_1^3 v_2 \rho}{12 \omega_5 \omega_{15} \delta_t \omega_{10}^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_3 \frac{\delta_1^3}{12 \delta_t \omega_{10}^2} \frac{\partial^3 \rho}{\partial x_2^2} + \\
& (-24 + 5 \omega_{10}^2 c_s^2 + 24 \omega_{10} - 36 \omega_{10} c_s^2 - 60 v_2^2 \omega_{10} + 60 v_2^2 + 36 c_s^2 - 4 \omega_{10}^2 + 11 v_2^2 \omega_{10}^2) \frac{\delta_1^3 v_2 \rho}{6 \delta_t \omega_{10}^2} \frac{\partial^3 v_2}{\partial x_2^2} - \frac{\delta_1^3 v_2 c_s^2 \rho}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} + \\
& C_4 \frac{\delta_1^3 v_2 \rho}{12 \delta_t \omega_{16} \omega_{10}^2 \omega_7} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\delta_1^3 v_2 c_s^2 \rho}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + (-12 + 12 \omega_7 - \omega_7^2) \frac{\delta_1^3 c_s^4}{6 \delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{\delta_1^3 v_2 c_s^2 \rho}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& (-1 + 3 c_s^2 + v_3^2) \frac{v_3 \delta_1^3 \rho}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \delta_1^3 \rho}{6 \omega_{19} \delta_t \omega_7} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3 v_3^2) \frac{\delta_1^3 v_2 \rho}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-3 v_1^4 \omega_9 - 12 v_1^2 \omega_9 c_s^2 + \omega_9 c_s^2 + 6 v_1^4 + 2 c_s^4 - 6 v_1^2 - \omega_9 c_s^4 - 2 c_s^2 + 3 v_1^2 \omega_9 + 24 v_1^2 c_s^2) \frac{\delta_1^4 v_2}{24 \omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 2 \omega_9 - 3 \omega_9 c_s^2 + 10 v_1^2 + 6 c_s^2 - 5 v_1^2 \omega_9) \frac{v_1 \delta_1^4 v_2 \rho}{12 \omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\delta_1^4 \rho}{24 \omega_5^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_7 \frac{v_1 \delta_1^4 c_s^2}{12 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12}^2 \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_8 \frac{\delta_1^4 c_s^2 \rho}{12 \omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& (3 \omega_9 - \omega_{12} - 9 \omega_9 c_s^2 + v_1^2 \omega_{12} + 3 \omega_9 \omega_{12} c_s^2 + 3 \omega_{12} c_s^2 - 3 v_1^2 \omega_9 + v_1^2 \omega_9 \omega_{12} - \omega_9 \omega_{12}) \frac{v_1 \delta_1^4 v_2 \rho}{12 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& C_9 \frac{\delta_1^4 v_2 c_s^2}{12 \omega_5^2 \omega_{21} \omega_{15} \omega_{12} \delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_2^2} + C_{10} \frac{\delta_1^4 c_s^2 \rho}{12 \omega_5^3 \omega_{21} \omega_{15} \omega_{12} \delta_t \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\delta_1^4 \rho}{12 \omega_5^3 \omega_{15}^2 \delta_t \omega_{10}^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{12} \frac{\delta_1^4 v_2}{12 \delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_2^2} + \\
& C_{13} \frac{\delta_1^4 \rho}{12 \delta_t \omega_{10}^3} \frac{\partial^4 v_2}{\partial x_2^2} + (3 \omega_9 - 9 \omega_9 c_s^2 + v_1^2 \omega_9 \omega_{13} - \omega_9 \omega_{13} - \omega_{13} - 3 v_1^2 \omega_9 + 3 \omega_9 \omega_{13} c_s^2 + 3 \omega_{13} c_s^2 + v_1^2 \omega_{13}) \frac{v_1 \delta_1^4 v_2 \rho}{12 \omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + \\
& C_{14} \frac{\delta_1^4 c_s^4 \rho}{12 \omega_5^3 \omega_{15} \omega_{12} \omega_6 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{14} \omega_8} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_2 \partial x_3} + C_{15} \frac{\delta_1^4 \rho}{12 \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^3} \frac{\partial^4 v_3}{\partial x_3^3 \partial x_3} + C_{16} \frac{\delta_1^4}{12 \omega_5 \omega_{12} \omega_6 \omega_{19} \delta_t \omega_7 \omega_{20} \omega_{14} \omega_8} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& C_{17} \frac{\delta_1^4 \rho}{4 \omega_5 \omega_{12} \omega_{19} \delta_t \omega_7 \omega_{20} \omega_{14} \omega_8} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{18} \frac{\delta_1^4 \rho}{4 \omega_5^2 \omega_{12} \omega_{19} \delta_t \omega_7^2 \omega_{20} \omega_{14} \omega_8} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{19} \frac{v_3 \delta_1^4 \rho}{2 \omega_5 \omega_{12} \omega_{19} \delta_t \omega_7 \omega_{20} \omega_{14} \omega_8} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{20} \frac{\delta_1^4}{2 \omega_5 \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_8} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{21} \frac{\delta_1^4 \rho}{12 \omega_5^2 \omega_{15} \omega_6 \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{22} \frac{\delta_1^4 v_2 \rho}{\omega_5 \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_8} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{23} \frac{\delta_1^4 \rho}{2 \omega_5 \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_8} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{24} \frac{\delta_1^4 v_2 c_s^2}{12 \omega_{19} \delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\delta_1^4 c_s^2 \rho}{12 \omega_{19} \delta_t \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{23}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (v_3^2 \omega_{18} - \omega_{18} - 9 c_s^2 \omega_{11} + 3 \omega_{18} c_s^2 + v_3^2 \omega_{18} \omega_{11} - \omega_{18} \omega_{11} + 3 \omega_{11} + 3 \omega_{18} c_s^2 \omega_{11} - 3 v_3^2 \omega_{11}) \frac{v_3 \delta_1^4 v_2 \rho}{12 \omega_{18} \delta_t \omega_{11}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& C_{26} \frac{v_3 \delta_1^4 c_s^2}{12 \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& (-9 c_s^2 \omega_{11} + 3 \omega_{19} c_s^2 \omega_{11} - \omega_{19} + 3 \omega_{19} c_s^2 + v_3^2 \omega_{19} + v_3^2 \omega_{19} \omega_{11} - \omega_{19} \omega_{11} + 3 \omega_{11} - 3 v_3^2 \omega_{11}) \frac{v_3 \delta_1^4 v_2 \rho}{12 \omega_{19} \delta_t \omega_{11}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{27} \frac{\delta_1^4 c_s^2 \rho}{12 \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& (6 v_3^4 + c_s^2 \omega_{11} - 12 v_3^2 c_s^2 \omega_{11} + 24 v_3^2 c_s^2 - 3 v_3^4 \omega_{11} + 2 c_s^4 - c_s^4 \omega_{11} - 2 c_s^2 - 6 v_3^2 + 3 v_3^2 \omega_{11}) \frac{\delta_1^4 v_2}{24 \delta_t \omega_{11}} \frac{\partial^4 \rho}{\partial x_3^4} + C_{28} \frac{\delta_1^4 \rho}{24 \omega_{19}^2 \delta_t \omega_7^3} \frac{\partial^4 v_2}{\partial x_3^4} + \\
& + (-4 - 3 c_s^2 \omega_{11} + 6 c_s^2 + 10 v_3^2 + 2 \omega_{11} - 5 v_3^2 \omega_{11}) \frac{v_3 \delta_1^4 v_2 \rho}{12 \delta_t \omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 3 \omega_5 + \omega_5 \omega_{12} - 3 \omega_{12} + 3 v_1^2 \omega_{12} - 3 \omega_5 \omega_{12} c_s^2 - \omega_5 v_1^2 \omega_{12} - 6 v_1^2 + 3 \omega_5 v_1^2 + 9 \omega_{12} c_s^2 - 18 c_s^2 + 9 \omega_5 c_s^2 \\
C_2 &= -3 \omega_5 v_2^2 \omega_{15} \omega_{10}^2 - 6 \omega_{15} \omega_{10}^2 + 18 \omega_{15} \omega_{10}^2 c_s^2 + 12 \omega_5 v_2^2 \omega_{10}^2 + 12 \omega_5 v_2^2 \omega_{15} - 12 \omega_5 v_2^2 \omega_{10} - 36 \omega_5 \omega_{10} c_s^2 - 6 \omega_5 v_2^2 \omega_{15} \omega_{10} - 18 \omega_5 \omega_{15} \omega_{10} c_s^2 - \\
& 36 \omega_{10}^2 c_s^2 - 11 \omega_5 \omega_{15} \omega_{10}^2 c_s^2 + 6 v_2^2 \omega_{15} \omega_{10}^2 + 36 \omega_5 \omega_{15} c_s^2 + 6 \omega_5 \omega_{15} \omega_{10} + 12 \omega_5 \omega_{10} + 36 \omega_5 \omega_{10}^2 c_s^2 - 12 \omega_5 \omega_{10}^2 - 12 \omega_5 \omega_{15} + 12 \omega_{10}^2 + 3 \omega_5 \omega_{15} \omega_{10}^2 - 12 v_2^2 \omega_{10}^2 \\
C_3 &= -144 v_2^2 \omega_{10} c_s^2 - 36 v_2^4 \omega_{10} - 12 \omega_{10} c_s^4 + 7 v_2^4 \omega_{10}^2 - \omega_{10}^2 c_s^2 + 36 v_2^4 + 12 c_s^4 + 12 \omega_{10} c_s^2 + 144 v_2^2 c_s^2 + 36 v_2^2 \omega_{10} - 36 v_2^2 + \omega_{10}^2 c_s^4 - 12 c_s^2 + 24 v_2^2 \omega_{10}^2 c_s^2 - 7 v_2^2 \omega_{10}^2
\end{aligned}$$

$$\begin{aligned}
& 6w_5v_3^2w_{12}w_{6c_s^2}w_{20}w_{14}w_8 + 12w_5v_1v_2^2w_{12}w_{6w_{19}w_7c_s^2}w_{20} - 6v_1v_2^2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8 + 12v_3^2v_1^2v_{2w_{12}w_{6w_{19}w_7}w_{20}} + \\
& 3w_5v_3^2v_{2w_{12}w_{6w_7c_s^2}w_{20}w_{14}w_8} + 12w_5v_3^2v_1v_2^2w_{12}w_{6w_{19}w_7}w_{20} + 12w_5v_3^2v_1w_{12}w_{6w_{19}c_s^2}w_{20}w_{14} + 12v_3^2v_1w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_8 + \\
& 6w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} + 12w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}} - 6w_5v_1^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{14}w_8} - 6v_3^2v_{1w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} + \\
& 6w_5v_3^2v_{1w_{12}w_{6w_{19}w_7c_s^2}w_{14}w_8} - 6w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} + 6w_5v_3^2v_1v_2^2w_{12}w_{6w_{20}w_{14}w_8} + 12w_5v_3^2v_1v_2^2w_{12}w_{6w_{20}w_{14}w_8} + \\
& 6w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} - 6w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} + 12v_3^2v_1w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14} + 12w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}} - \\
& 3w_5v_3^2v_1w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8 - 6v_1^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} + 3w_5v_3^2v_1v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}w_8} - 12w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{20}w_{14}} - \\
& 6v_3^2v_1v_2^2w_{12}w_{6w_{19}w_7}w_{20}w_{14}w_8 + 12w_5v_3^2v_{2w_{12}w_{6w_{19}w_7c_s^2}w_{14}w_8} - 12v_3^2v_1v_2^2w_{6w_{19}w_7}w_{20}w_{14}w_8 - 6w_5v_3^2v_1v_{2w_{12}w_{6w_{19}w_7}w_{20}w_{14}w_8} + 6w_5v_3^2v_1v_2^2w_{12}w_{6w_{19}w_7}w_{20}w_8
\end{aligned}$$

$$\begin{aligned}
1 &= 2\omega_2^2\omega_{12}w_7c_{14}^4\omega_{14}w_8 - 8\omega_5v_3^2v_1v_2w_{19}w_7^2w_{20}w_8 - 4\omega_3^2v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{20} - 2\omega_5^2v_3^2v_1^2w_{12}w_7w_{20}w_{14}w_8 - 4\omega_5w_{12}w_{19}w_7^2c_{14}^4w_{14} + 4\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7w_{14} - \\
&+ 4\omega_5^2v_1^2w_{12}w_{19}w_7c_{14}^2w_{14}w_8 + 4\omega_5v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{14}w_8 - 8\omega_5v_3^2v_1v_2w_{12}w_{19}w_7^2w_{20} + \omega_5^2v_3^2w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 - 4\omega_5^2w_{12}w_{19}w_7^2c_{14}^2w_{20} - \\
&2w_{12}w_{19}w_7^2c_{14}^3w_{20}w_{14}w_8 - 2\omega_5v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{14}w_8 - \omega_5^2v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 - 8\omega_3^2v_1v_2w_{12}w_{19}w_7c_{14}^2w_{20} + 4\omega_5v_3^2v_1^2w_{12}w_{19}w_7^2w_{14} + \\
&4\omega_5v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20} + 2\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{14}w_8 + 2\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_8 + 4\omega_5^2v_3^2w_{12}w_{19}w_7c_{14}^2w_{20} - 2\omega_5^2w_{12}w_{19}w_7^2c_{14}^2w_{14}w_8 + \\
&4w_{12}w_{19}w_7c_{14}^3w_{20}w_{14}w_8 + 4\omega_5w_{12}w_{19}w_7^2c_{14}^3w_{20}w_{14}w_8 + 8\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7w_{20}w_{14} + 2\omega_5^2v_1^2w_{12}w_{19}w_7c_{14}^2w_{20}w_{14}w_8 - 2\omega_5^2v_3^2v_1v_2w_{12}w_7^2w_{20}w_{14}w_8 - \\
&4\omega_5v_1v_2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + 4\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} + 2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 + 2\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14}w_8 + \\
&8\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14} - 2\omega_5^2v_1^2w_{12}w_7^2c_{14}^2w_{14}w_8 + 4\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{14}w_8 + 4\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7w_{20}w_8 - 8\omega_5^2v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} - \\
&8\omega_5v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{20} - 4\omega_5^2v_1v_2w_{12}w_{19}w_7c_{14}^2w_{20}w_{14}w_8 - 2\omega_5^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_8 + 4\omega_5w_{19}w_7c_{14}^2w_{20}w_{14}w_8 - 2\omega_5^2v_1^2w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 + \\
&4\omega_5v_1v_2w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 + \omega_5^2v_3^2v_1^2w_{19}w_7^2w_{20}w_{14}w_8 + 4\omega_5v_1^2w_{19}w_7^2c_{14}^2w_{20}w_8 - \omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + 2\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_8 - \\
&2\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{14}w_8 - 2\omega_5^2v_3^2v_1^2w_{19}w_7^2w_{20}w_8 + 2\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{14}w_8 + 4\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_8 - 2\omega_5^2v_1^2w_{12}w_7c_{14}^2w_{20}w_{14}w_8 + \\
&8\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7w_{14}w_8 - 4\omega_5^2v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_8 - 4\omega_5^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} + 4\omega_5^2v_1v_2w_{19}w_7^2c_{14}^2w_{20}w_8 - 4\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{14} - \\
&4\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20} + 4\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14} - 8\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14}w_8 - 2\omega_5^2v_3^2w_{19}w_7^2c_{14}^2w_{20}w_8 - 4\omega_5v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} + \\
&\omega_5^2v_1^2w_{12}w_7^2c_{14}^2w_{20}w_{14}w_8 + 8\omega_5^2v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{14} - 8\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7w_{20} - 2\omega_5^2v_1v_2w_{19}w_7^2w_{20}w_{14}w_8 + 2\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + \\
&2\omega_5^2w_{12}w_{19}w_7c_{14}^2w_{20}w_{14}w_8 - 4\omega_5^2v_1^2w_{12}w_{19}w_7c_{14}^2w_{20}w_{14} - 4\omega_5v_3^2v_1v_2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + 8\omega_5v_1v_2w_{12}w_{19}w_7^2w_{20}w_{14} + 4\omega_5^2w_{12}w_{19}w_7^2c_{14}^2w_{14} - \\
&4\omega_5v_1w_{12}w_{19}w_7^2c_{14}^2w_{20}w_8 + 4\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} + 4\omega_5v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 - 8\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14}w_8 - 2\omega_5^2v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{14} - \\
&2\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + 2\omega_5^2v_3^2v_1^2w_{19}w_7^2w_{20}w_{14}w_8 + 4\omega_5v_3^2v_1^2w_{19}w_7^2c_{14}^2w_{20}w_8 - 4\omega_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14} + \\
&4\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14}w_8 - \omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 - 2\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 + 4\omega_5v_3^2v_1^2w_{12}w_{19}w_7^2w_{20} + 4\omega_5v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{14} - \\
&4\omega_5^2w_{12}w_{19}w_7c_{14}^2w_{14}w_8 + 4\omega_5w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} - 4\omega_5^2v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14}w_8 - 8\omega_5v_3^2v_1v_2w_{12}w_{19}w_7^2w_{14} - 4\omega_5^2w_{12}w_{19}w_7^2c_{14}^2w_{14} + \\
&8\omega_5^2v_1v_2w_{12}w_{19}w_7^2c_{14}^2w_{14}w_8 - 4\omega_5v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} + \omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 + 2\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14}w_8 + 4\omega_5v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_8 - \\
&4\omega_5^2v_3^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} - 8\omega_5^2v_1^2w_{12}w_{19}w_7^2c_{14}^2w_{20}w_{14} + 4\omega_5^2v_1^2w_{12}w_{19$$

$$\begin{aligned}
& 4w_5v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_8 + 4w_5v_3^2v_1^2w_{19}w_7^2w_{20}w_{14}w_8 + 2w_5^2w_{12}w_{19}w_7^4w_{20}w_8 + 8w_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_8 - 2w_5^2v_3^2v_1^2w_{19}w_7^2w_{20}w_{14}w_8 - \\
& 8w_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14} + 2w_5w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + 4w_5^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 - 2w_5^2w_{12}w_{19}w_7^2w_{20}w_{14}w_8 + 2w_5^2v_1^2w_{12}w_{19}w_7^2w_{20}w_8 - \\
& 4w_5^2v_3^2w_{12}w_{19}w_7^2w_{20} - 4w_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{14} - 4w_5^2v_3^2v_1^2w_{12}w_{19}w_7w_{14}w_8 + 4w_5^2v_1^2w_{12}w_{19}w_7^2w_{14}w_8 - 8w_5v_1^2w_{12}w_{19}w_7^2w_{14} - \\
& 4w_5^2v_3^2v_1^2w_{12}w_{19}w_7^2w_{20}w_8 + 4w_5^2v_1^2w_{12}w_{19}w_7^2w_{20}w_{14} + 4w_5w_{12}w_{19}w_7^4w_{20}w_{14}w_8 - 2w_5^2v_3^2v_1^2w_{19}w_7^2w_{20}w_{14}w_8 - 12w_5w_{12}w_{19}w_7^4w_{20}w_{14}w_8
\end{aligned}$$

[illegible]

[illegible]

[illegible]

$$C_{25} = 36v_2^2\omega_{19}\omega_{10}\omega_7^2\omega_{23} - 6\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 36v_2^2\omega_{19}\omega_{16}\omega_{10}^2\omega_7^2 + 18v_2^2\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 36v_2^2\omega_{19}\omega_{10}^2\omega_7\omega_{23} + 18v_2^2\omega_{19}\omega_{16}\omega_{10}^2\omega_7^3 + 12\omega_{19}\omega_{16}\omega_7^2\omega_{23} + 12\omega_{19}\omega_{10}^2\omega_7^2\omega_{23} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 36v_2^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 6\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 6\omega_{19}\omega_{16}\omega_{10}^2\omega_7^3 + 12\omega_{19}\omega_{10}^2\omega_7^3 - 36v_2^2\omega_{19}\omega_{16}\omega_7^2\omega_{23} - 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 36v_2^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 36v_2^2\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 36v_2^2\omega_{19}\omega_{10}^2\omega_7^2 + 12\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 4\omega_{19}\omega_{16}\omega_{10}^2\omega_7^2\omega_{23}c_s^2 - 24\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{19}\omega_{16}\omega_7^2\omega_{23}c_s^2 - 12\omega_{19}\omega_{10}^2\omega_7^2 - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 18v_2^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}^2\omega_7^2 - 36v_2^2\omega_{19}\omega_{10}^2\omega_7^3 - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^3c_s^2 - 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3c_s^2 - 24\omega_{19}\omega_{10}^2\omega_7^2\omega_{23}c_s^2 + 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} - 12\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 6\omega_{19}\omega_{16}\omega_{10}^2\omega_7^2\omega_{23}c_s^2 + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 72v_2^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7^3 + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3 + 24\omega_{19}\omega_{10}^2\omega_7^2\omega_{23} + 18\omega_{19}\omega_{16}\omega_{10}^2\omega_7^2\omega_{23}c_s^2 + 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 18v_2^2\omega_{19}\omega_{16}\omega_{10}\omega_7^3 - 72v_2^2\omega_{19}\omega_{10}^2\omega_7^2\omega_{23} - \omega_{19}\omega_{16}\omega_{10}^2\omega_7^3\omega_{23}c_s^2 + 12\omega_{16}\omega_{10}^2\omega_7^2c_s^2 + 6\omega_{16}\omega_{10}\omega_7^3 + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}c_s^2 + 12\omega_{19}\omega_{10}^2\omega_7^2c_s^2 + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 18v_2^2\omega_{16}\omega_{10}^2\omega_7^2 - 12\omega_{19}\omega_{16}\omega_{10}^2\omega_7^2c_s^2 - 18v_2^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{16}\omega_{10}^2\omega_7^2 - 12\omega_{19}\omega_{10}^2\omega_7^2\omega_{23} + 24\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2$$

$$C_{26} = -12v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_{23}\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{23} - 12\omega_{19}^2\omega_7^2\omega_{11} - 6v_3^2\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 18v_3^2\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23} + 12\omega_{19}^2\omega_{10}\omega_7\omega_{23} - 3v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 36\omega_{19}\omega_{16}\omega_{10}\omega_7c_s^2\omega_{11} + 6v_3^2\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{11} - 36v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 + 12\omega_{19}^2\omega_{10}\omega_7^2\omega_{11} - 36\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11} + 12v_3^2\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 36v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 + 36v_3^2\omega_{19}\omega_{10}\omega_7c_s^2\omega_{11} - 12v_3^2\omega_{19}^2\omega_{10}\omega_7\omega_{23} - 12v_3^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 12v_3^2\omega_{19}^2\omega_{10}\omega_7^2\omega_{11} + 5\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23} + 54\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - 12v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_{23} + 3\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 18\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 6\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{11} - 9\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{11} - 36v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 18\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} + 18\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 36\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} + 6v_3^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23} - 15\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 18\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 12v_3^2\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 3\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 18\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23} - 6\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 6\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{11} - 12v_3^2\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 18\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} + 12v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{11} - 12v_3^2\omega_{19}^2\omega_7^2\omega_{23} + 36\omega_{19}^2\omega_{10}\omega_7^2\omega_{23}c_s^2 - 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} + 18v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 36\omega_{19}^2\omega_7^2c_s^2\omega_{11} + 36\omega_{19}\omega_{16}\omega_{10}\omega_{23}c_s^2\omega_{11} + 6v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{23} + 12\omega_{19}^2\omega_7^2\omega_{23} + 12\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 36v_3^2\omega_{19}\omega_{10}\omega_7^2c_s^2\omega_{11} - 12\omega_{19}^2\omega_{10}\omega_7^2\omega_{23} - 5v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{19}^2\omega_{10}\omega_7\omega_{11} - 36v_3^2\omega_{19}^2\omega_7^2\omega_{23}c_s^2 - 12v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{11} + 54\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11}$$

$$C_{27} = -\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 3v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 6\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} + 12\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11} - 36v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} + 18v_3^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - 36v_3^2\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 36v_3^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 + \omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 36v_3^2\omega_{19}\omega_7^3\omega_{23} + 36v_3^2\omega_{19}\omega_{10}\omega_7^3\omega_{23} - 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} + 12\omega_{19}\omega_7^3\omega_{23} + 18v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{11} - 12\omega_{19}\omega_{10}\omega_7^3c_s^2\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{11} - 18\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} - 54v_3^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 36v_3^2\omega_{19}\omega_{10}\omega_7^2\omega_{11} - 6\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11} + 6\omega_{19}\omega_{16}\omega_7^3\omega_{11} - 15v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 12\omega_{19}\omega_7^3\omega_{11} + 12\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} - 12\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 36v_3^2\omega_{19}\omega_7^3\omega_{11} - 18v_3^2\omega_{16}\omega_{10}\omega_7^3\omega_{11} + 12\omega_{19}\omega_{10}\omega_7^2c_s^2\omega_{11} + 54v_3^2\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 18v_3^2\omega_{19}\omega_{16}\omega_7^3\omega_{11} - 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{11} - 12\omega_{19}\omega_7^3\omega_{23}c_s^2 + 36v_3^2\omega_{19}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2\omega_{11} + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}c_s^2 + 12\omega_{19}\omega_{10}\omega_7^3\omega_{11} + 36v_3^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 12\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 6\omega_{16}\omega_{10}\omega_7^3\omega_{11} + 6\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2\omega_{11} + 12\omega_{19}\omega_7^3c_s^2\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^3c_s^2\omega_{11} + 18\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2\omega_{11} + 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2$$

$$C_{28} = 72v_3^2\omega_7^2 + 30v_3^2\omega_{19}\omega_7^2 - 72v_3^2\omega_{19}\omega_7^2c_s^2 - 3\omega_{19}^2\omega_7^3c_s^4 - 36v_3^2\omega_7^3 - 216v_3^2\omega_7^2c_s^2 - 6\omega_{19}\omega_7^3c_s^2 - 72v_3^2\omega_{19}\omega_7^2 + 144v_3^2\omega_{19}\omega_7^2c_s^2 + 12\omega_{19}^2\omega_7c_s^2 + 24\omega_{19}^2c_s^4 - 30v_3^4\omega_{19}\omega_7^3 + 24\omega_{19}\omega_7^4c_s^4 + 24\omega_{19}\omega_7^2c_s^2 + 108v_3^2\omega_7^3c_s^2 - 36v_3^2\omega_{19}\omega_7c_s^2 + 24\omega_{19}^2\omega_7^2c_s^4 + 72v_3^4\omega_{19}\omega_7^2 - 12v_3^2\omega_{19}\omega_7^2c_s^2 - 24\omega_{19}\omega_7c_s^2 + 36v_3^4\omega_7^3 - 48\omega_{19}\omega_7^4c_s^4 - 12v_3^4\omega_{19}\omega_7^2 - 8\omega_{19}^2\omega_7^2c_s^2 - 72v_3^2\omega_7^2 + 72v_3^2\omega_{19}\omega_7c_s^2 + 3v_3^4\omega_{19}\omega_7^2 - 24\omega_{19}\omega_7^2c_s^4 + 6v_3^2\omega_{19}\omega_7^3c_s^2 + 12v_3^2\omega_{19}\omega_7^2 + 6\omega_{19}\omega_7^3c_s^4 - 3v_3^2\omega_{19}\omega_7^3 + \omega_{19}\omega_7^3c_s^2$$

2.4.5 Conservation of momentum: ρv_3

$$v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_3 \delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_2 \rho}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{2v_3 \delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (-2 - 2c_s^2\omega_{11} + 4c_s^2 + 6v_3^2 + \omega_{11} - 3v_3^2\omega_{11}) \frac{\delta_l^2}{\delta_t \omega_{11}} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3v_3 \delta_l^2 \rho}{\delta_t \omega_{11}} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{\delta_l^2 c_s^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2 \rho}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2 \rho}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (-2 - 3c_s^2\omega_{11} + 6c_s^2 + 2v_3^2 + \omega_{11} - v_3^2\omega_{11}) \frac{v_3 \delta_l^2}{2\delta_t \omega_{11}} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 - c_s^2\omega_{11} + 2c_s^2 + 6v_3^2 + \omega_{11} - 3v_3^2\omega_{11}) \frac{\delta_l^2 \rho}{2\delta_t \omega_{11}} \frac{\partial^2 v_3}{\partial x_3^2} + (-1 + v_1^2 + 3c_s^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_3 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{v_1 \delta_l^3 \rho}{6\omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{v_3 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{v_3 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_3 \delta_l^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{v_3 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_2 \frac{\delta_l^3 v_2 \rho}{6\delta_t \omega_{16} \omega_7} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega_6 - \omega_6^2) \frac{\delta_l^3 c_s^4}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \frac{v_3 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 + 12\omega_7 - \omega_7^2) \frac{\delta_l^3 c_s^4}{6\delta_t \omega_7} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{v_3 \delta_l^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_3 \frac{v_3 \delta_l^3 \rho}{12\omega_{18} \omega_6 \delta_t \omega_{11}^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_4 \frac{v_3 \delta_l^3 \rho}{12\omega_{19} \delta_t \omega_7 \omega_{11}^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_5 \frac{\delta_l^3}{12\delta_t \omega_{11}^2} \frac{\partial^3 \rho}{\partial x_3^3} + (-24 - 36c_s^2\omega_{11} + 5c_s^2\omega_{11}^2 - 4\omega_{11}^2 + 11v_3^2\omega_{11}^2 + 36c_s^2 + 60v_3^2 + 24\omega_{11} - 60v_3^2\omega_{11}) \frac{v_3 \delta_l^3 \rho}{6\delta_t \omega_{11}^2} \frac{\partial^3 v_3}{\partial x_3^3} + (-3v_1^4\omega_9 - 12v_1^2\omega_9c_s^2 + \omega_9c_s^2 + 6v_1^4 + 2c_s^4 - 6v_1^2 - \omega_9c_s^4 - 2c_s^2 + 3v_1^2\omega_9 + 24v_1^2c_s^2) \frac{v_3 \delta_l^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + (-4 + 2\omega_9 - 3\omega_9c_s^2 + 10v_1^2 + 6c_s^2 - 5v_1^2\omega_9) \frac{v_3 v_1 \delta_l^4 \rho}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\delta_l^4 \rho}{24\omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^4} +$$

$$\begin{aligned}
& (3\omega_9 - \omega_{12} - 9\omega_9 c_s^2 + v_1^2 \omega_{12} + 3\omega_9 \omega_{12} c_s^2 + 3\omega_{12} c_s^2 - 3v_2^2 \omega_9 + v_1^2 \omega_9 \omega_{12} - \omega_9 \omega_{12}) \frac{v_3 v_1 \delta_l^4 \rho}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + \omega_5) \frac{v_3 \delta_l^4 c_s^4}{6\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_7 \frac{\delta_l^4 c_s^4 \rho}{2\omega_6^2 \delta_t \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (-\omega_{15} - \omega_{15} \omega_{10} + 3\omega_{15} c_s^2 + 3\omega_{10} - 9\omega_{10} c_s^2 - 3v_2^2 \omega_{10} + v_2^2 \omega_{15} + 3\omega_{15} \omega_{10} c_s^2 + v_2^2 \omega_{15} \omega_{10}) \frac{v_3 \delta_l^4 v_2 \rho}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
& (-12v_2^2 \omega_{10} c_s^2 - 3v_2^4 \omega_{10} - \omega_{10} c_s^4 + 6v_2^4 + 2c_s^4 + \omega_{10} c_s^2 + 24v_2^2 c_s^2 + 3v_2^2 \omega_{10} - 6v_2^2 - 2c_s^2) \frac{v_3 \delta_l^4}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^2} + \\
& (-4 + 2\omega_{10} - 3\omega_{10} c_s^2 - 5v_2^2 \omega_{10} + 10v_2^2 + 6c_s^2) \frac{v_3 \delta_l^4 v_2 \rho}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^2} + C_8 \frac{\delta_l^4 \rho}{24\delta_t \omega_{16}^2 \omega_7^3} \frac{\partial^4 v_3}{\partial x_2^4} + C_9 \frac{v_1 \delta_l^4 c_s^2}{12\omega_{18} \omega_9 \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{11}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_{10} \frac{\delta_l^4 c_s^2 \rho}{12\omega_{18} \omega_9 \omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& (3\omega_9 - 9\omega_9 c_s^2 + v_1^2 \omega_9 \omega_{13} - \omega_9 \omega_{13} - \omega_{13} - 3v_1^2 \omega_9 + 3\omega_9 \omega_{13} c_s^2 + 3\omega_{13} c_s^2 + v_1^2 \omega_{13}) \frac{v_3 v_1 \delta_l^4 \rho}{12\omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{11} \frac{\delta_l^4}{2\omega_{18} \omega_6 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7 \omega_{20} \omega_{11} \omega_{14} \omega_8} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{12} \frac{\delta_l^4 \rho}{2\omega_{18} \omega_6 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7 \omega_{20} \omega_{11} \omega_{14} \omega_8} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{13} \frac{\delta_l^4 \rho}{12\omega_5 \omega_{18} \omega_6^3 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{14} \frac{v_3 \delta_l^4 \rho}{\omega_{18} \omega_6 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7 \omega_{20} \omega_{11} \omega_{14} \omega_8} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{15} \frac{\delta_l^4}{2\omega_{18} \omega_6 \omega_{19} \delta_t \omega_{16} \omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{16} \frac{\delta_l^4 \rho}{12\omega_5 \omega_{18} \omega_6^3 \omega_{19} \delta_t \omega_{16} \omega_7^3 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{17} \frac{\delta_l^4 v_2 \rho}{\omega_{18} \omega_6 \omega_{19} \delta_t \omega_{16} \omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{18} \frac{\delta_l^4 \rho}{2\omega_{18} \omega_6 \omega_{19} \delta_t \omega_{16} \omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{19} \frac{\delta_l^4 v_2 c_s^2}{12\omega_{19} \delta_t \omega_{16}^2 \omega_{10} \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + C_{20} \frac{\delta_l^4 c_s^2 \rho}{12\omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^3 \omega_{23} \omega_{11}} \frac{\partial^4 v_2}{\partial x_3^3 \partial x_3} + \\
& (v_2^2 \omega_{16} \omega_{10} + 3\omega_{16} \omega_{10} c_s^2 - \omega_{16} + 3\omega_{10} + v_2^2 \omega_{16} - 9\omega_{10} c_s^2 - 3v_2^2 \omega_{10} + 3\omega_{16} c_s^2 - \omega_{16} \omega_{10}) \frac{v_3 \delta_l^4 v_2 \rho}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_3^3 \partial x_3} + \\
& C_{21} \frac{v_3 \delta_l^4 c_s^2}{12\omega_{18}^2 \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{11}^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{22} \frac{\delta_l^4 c_s^2 \rho}{12\omega_{18} \omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{23} \frac{v_3 \delta_l^4 c_s^2}{12\omega_{19}^2 \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{11}^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{24} \frac{\delta_l^4 c_s^2 \rho}{12\omega_{19} \delta_t \omega_{16} \omega_7^3 \omega_{23} \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\delta_l^4 \rho}{12\omega_{18}^2 \omega_6^3 \delta_t \omega_{11}^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{26} \frac{\delta_l^4 \rho}{12\omega_{19}^2 \delta_t \omega_7^3 \omega_{11}^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{27} \frac{v_3 \delta_l^4}{12\delta_t \omega_{11}^3} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\delta_l^4 \rho}{12\delta_t \omega_{11}^3} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 3\omega_6 - 3\omega_6 \omega_{13} c_s^2 + 3v_1^2 \omega_6 + 9\omega_6 c_s^2 - 6v_1^2 - 3\omega_{13} - 18c_s^2 + \omega_6 \omega_{13} - v_1^2 \omega_6 \omega_{13} + 9\omega_{13} c_s^2 + 3v_1^2 \omega_{13} \\
C_2 &= 6 - v_2^2 \omega_{16} \omega_7 - 3\omega_{16} \omega_7 c_s^2 - 3\omega_{16} + 3v_2^2 \omega_{16} + \omega_{16} \omega_7 - 3\omega_7 - 6v_2^2 - 18c_s^2 + 9\omega_{16} c_s^2 + 3v_2^2 \omega_7 + 9\omega_7 c_s^2 \\
C_3 &= -18\omega_{18} \omega_6 c_s^2 \omega_{11} + 12\omega_6 \omega_{11} - 12v_3^2 \omega_6 \omega_{11} + 36\omega_{18} \omega_6 c_s^2 + 12v_3^2 \omega_6 \omega_{11} - 36c_s^2 \omega_{11} - 12\omega_6 \omega_{11} - 11\omega_{18} \omega_6 c_s^2 \omega_{11}^2 + 12\omega_{11}^2 - 12v_3^2 \omega_{11}^2 - \\
& 36\omega_6 c_s^2 \omega_{11} + 3\omega_{18} \omega_6 \omega_{11}^2 + 18\omega_{18} c_s^2 \omega_{11}^2 + 12v_3^2 \omega_{18} \omega_6 - 3v_3^2 \omega_{18} \omega_6 \omega_{11}^2 - 12\omega_{18} \omega_6 - 6v_3^2 \omega_{18} \omega_6 \omega_{11} - 6\omega_{18} \omega_{11}^2 + 36\omega_6 c_s^2 \omega_{11}^2 + 6\omega_{18} \omega_6 \omega_{11} + 6v_3^2 \omega_{18} \omega_{11}^2 \\
C_4 &= -6v_3^4 \omega_{19} \omega_7 \omega_{11} + 12v_3^2 \omega_7 \omega_{11}^2 - 36\omega_7 c_s^2 \omega_{11} + 18\omega_{19} c_s^2 \omega_{11}^2 - 12\omega_7 \omega_{11}^2 + 6\omega_{19} \omega_7 \omega_{11} + 12v_3^2 \omega_{19} \omega_7 + 3\omega_{19} \omega_7 \omega_{11}^2 - 36c_s^2 \omega_{11}^2 - 12\omega_{19} \omega_7 + \\
& 36\omega_7 c_s^2 \omega_{11}^2 + 12\omega_7 \omega_{11} + 12\omega_{11}^2 - 12v_3^2 \omega_7 \omega_{11} - 3v_3^2 \omega_{19} \omega_7 \omega_{11}^2 - 12v_3^2 \omega_{11}^2 + 36\omega_{19} \omega_7 c_s^2 - 18\omega_{19} \omega_7 c_s^2 \omega_{11} - 6\omega_{19} \omega_{11}^2 + 6v_3^2 \omega_{19} \omega_{11}^2 - 11\omega_{19} \omega_7 c_s^2 \omega_{11}^2 \\
C_5 &= 36v_3^4 + 7v_3^2 \omega_{11}^2 + 12c_s^2 \omega_{11} - 144v_3^2 c_s^2 \omega_{11} + 24v_3^2 c_s^2 \omega_{11}^2 + 144v_3^2 c_s^2 - 36v_3^4 \omega_{11} - c_s^2 \omega_{11}^2 + 12c_s^4 - 12c_s^4 \omega_{11} - 7v_3^2 \omega_{11}^2 - 12c_s^2 - 36v_3^2 + c_s^2 \omega_{11}^2 + 36v_3^2 \omega_{11} \\
C_6 &= 30v_1^2 \omega_6^3 \omega_{13} - 36v_1^2 \omega_6^3 - 3\omega_6^3 \omega_{13} c_s^4 + 72v_1^4 \omega_6^2 \omega_{13} - 6\omega_6^3 \omega_{13} c_s^2 + 12v_1^2 \omega_6^2 \omega_{13} + 72v_1^2 \omega_6^2 - 72v_1^2 \omega_6^3 \omega_{13} c_s^2 + 108v_1^2 \omega_6^3 c_s^2 + 3v_1^4 \omega_6^3 \omega_{13} - \\
& 24\omega_6^2 \omega_{13} c_s^4 - 30v_1^4 \omega_6^3 \omega_{13} + 72v_1^2 \omega_6 \omega_{13} c_s^2 - 24\omega_6 \omega_{13} c_s^2 - 72v_1^2 \omega_6^2 \omega_{13} - 12v_1^2 \omega_6^2 \omega_{13} c_s^2 - 12v_1^4 \omega_6^2 \omega_{13}^2 - 216v_1^2 \omega_6^2 c_s^2 - 48\omega_6 \omega_{13}^2 c_s^4 - 8\omega_6^2 \omega_{13}^2 c_s^2 - \\
& 3v_1^2 \omega_6^2 \omega_{13}^2 + 144v_1^2 \omega_6^2 \omega_{13} c_s^2 + 24\omega_6 \omega_{13} c_s^4 - 72v_1^4 \omega_6^2 + 24\omega_6^2 \omega_{13} c_s^2 + 36v_1^4 \omega_6^3 + 24\omega_6^2 \omega_{13}^2 c_s^4 - 36v_1^2 \omega_6^2 \omega_{13}^2 c_s^2 + 12\omega_6 \omega_{13}^2 c_s^2 + \omega_6^3 \omega_{13}^2 c_s^2 + \\
& 6v_1^2 \omega_6^3 \omega_{13}^2 c_s^2 + 24\omega_{13}^2 c_s^4 + 6\omega_6^3 \omega_{13} c_s^4 \\
C_7 &= \omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} \omega_8 + 2\omega_6 \omega_{16} \omega_7 \omega_{17} \omega_{14} \omega_8 - 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{14} + \omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8 + \omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 - 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{17} - \\
& \omega_6 \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 - \omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} + \omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 + \omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_8 - \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 - \\
& \omega_6^2 \omega_{16} \omega_7 \omega_{17} \omega_{14} \omega_8 - 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} + \omega_6^2 \omega_{16} \omega_7^2 \omega_{17} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} - 2\omega_6 \omega_{16} \omega_7^2 \omega_{17} \omega_8 - 2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} + \\
& 2\omega_6 \omega_{16} \omega_{13} \omega_{17} \omega_{14} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{14} \omega_8 - \omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_8 + 2\omega_6 \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 - \omega_6^2 \omega_{16} \omega_{13} \omega_{17} \omega_{14} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} + \\
& 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} + 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_8 - 2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 + 2\omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 - 6\omega_6 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 - 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} \\
C_8 &= -48\omega_{16}^2 \omega_7 c_s^4 - 12v_2^2 \omega_{16}^2 \omega_7 c_s^2 - 24\omega_{16} \omega_7 c_s^2 - 30v_2^4 \omega_{16} \omega_7^3 + 72v_2^2 \omega_{16} \omega_7 c_s^2 - 24\omega_{16} \omega_7^3 c_s^4 - 8\omega_{16}^2 \omega_7^2 c_s^2 + 72v_2^4 \omega_{16} \omega_7^2 + 36v_2^4 \omega_7^3 + \\
& 6v_2^2 \omega_{16}^2 \omega_7^3 c_s^2 + 30v_2^2 \omega_{16} \omega_7^3 + \omega_{16}^2 \omega_7^3 c_s^2 - 72v_2^4 \omega_7^2 - 72v_2^2 \omega_{16} \omega_7^2 + 6\omega_{16} \omega_7^3 c_s^4 + 24\omega_{16}^2 c_s^4 - 72v_2^2 \omega_{16} \omega_7^3 c_s^2 + 12v_2^2 \omega_{16} \omega_7^2 - 6\omega_{16} \omega_7^3 c_s^2 - 3\omega_{16}^2 \omega_7^3 c_s^4 - \\
& 3v_2^2 \omega_{16} \omega_7^3 - 216v_2^2 \omega_7^2 c_s^2 + 24\omega_{16} \omega_7 c_s^4 + 144v_2^2 \omega_{16} \omega_7^2 c_s^2 + 72v_2^2 \omega_7^2 - 12v_2^4 \omega_{16}^2 \omega_7^2 + 12\omega_{16}^2 \omega_7 c_s^2 + 108v_2^2 \omega_7^3 c_s^2 - 36v_2^2 \omega_7^3 - 36v_2^2 \omega_{16} \omega_7 c_s^2 + \\
& 24\omega_{16}^2 \omega_7^2 c_s^4 + 24\omega_{16} \omega_7^2 c_s^2 + 3v_2^4 \omega_{16} \omega_7^3 \\
C_9 &= -36\omega_6 \omega_{22} \omega_{13}^2 c_s^2 \omega_{11} + 12\omega_{18} \omega_{22} \omega_{13}^2 \omega_{11} - 12\omega_9 \omega_{13}^2 \omega_{11}^2 + 3\omega_{18} \omega_9 \omega_6^2 \omega_{22} \omega_{13} \omega_{11} - 15\omega_{18} \omega_6^2 \omega_{22} \omega_{13}^2 c_s^2 \omega_{11} + 18v_1^2 \omega_{18} \omega_9 \omega_6 \omega_{22} \omega_{13} \omega_{11} + \\
& 6v_1^2 \omega_{18} \omega_9 \omega_6^2 \omega_{22} \omega_{11} + 12v_1^2 \omega_9 \omega_6^2 \omega_{13} - 12v_1^2 \omega_{18} \omega_9 \omega_6 \omega_{13} \omega_{11} + 3\omega_{18} \omega_9 \omega_6^2 \omega_{22} \omega_{13}^2 c_s^2 \omega_{11} - 5v_1^2 \omega_{18} \omega_6^2 \omega_{22} \omega_{13}^2 \omega_{11} + 36\omega_9 \omega_6^2 \omega_{13}^2 c_s^2 - \\
& 18\omega_{18} \omega_9 \omega_6^2 \omega_{13} c_s^2 \omega_{11} + 12\omega_{18} \omega_9 \omega_{22} \omega_{13} \omega_{11} - 12v_1^2 \omega_{18} \omega_{22} \omega_{13}^2 \omega_{11} - 36\omega_{18} \omega_9 \omega_6 \omega_{22} \omega_{13}^2 c_s^2 \omega_{11} - 6v_1^2 \omega_{18} \omega_9 \omega_6^2 \omega_{13} \omega_{11} + 36\omega_6^2 \omega_{22} \omega_{13}^2 c_s^2 \omega_{11} -
\end{aligned}$$

$$\begin{aligned}
& 18\omega_{18}\omega_6\omega_6^2\omega_{13}^2c_s^2 + 54\omega_{18}\omega_6\omega_{22}\omega_{13}^2c_s^2\omega_{11} - 12\omega_9\omega_6\omega_{13}^2\omega_{11} + 36\omega_9\omega_6\omega_{13}^2c_s^2\omega_{11} - 6\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{11} + 36\omega_{18}\omega_9\omega_{22}\omega_{13}^2c_s^2\omega_{11} + \\
& 12\omega_{18}\omega_9\omega_6\omega_{13}^2\omega_{11} + 6\omega_{17}^2\omega_{18}\omega_6^2\omega_{22}\omega_{13}^2 + 12\omega_{17}^2\omega_6^2\omega_{22}\omega_{13}^2\omega_{11} + 12\omega_{17}^2\omega_9\omega_6\omega_{13}^2\omega_{11} + 5\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}^2\omega_{11} + 18\omega_{18}\omega_9\omega_6^2\omega_{22}c_s^2\omega_{11} - \\
& 12\omega_{17}^2\omega_{18}\omega_9\omega_{22}\omega_{13}\omega_{11} + \omega_{17}^2\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}\omega_{11} + 12\omega_{18}\omega_9\omega_6\omega_6^2\omega_{22}\omega_{13}\omega_{11} - 36\omega_{18}\omega_9\omega_6\omega_6^2c_s^2\omega_{11} + 6\omega_{18}\omega_9\omega_6^2\omega_{13}\omega_{11} - 6\omega_{18}\omega_6^2\omega_{22}\omega_{13} - \\
& 12\omega_6^2\omega_{22}\omega_{13}\omega_{11} + 6\omega_{18}\omega_9\omega_6^2\omega_{13} - 3\omega_{17}^2\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}\omega_{11} + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11} + 12\omega_{17}^2\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}\omega_{11} - 6\omega_{18}\omega_9\omega_6^2\omega_{13}\omega_{11} - \\
& 18\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}\omega_{11} + 12\omega_{18}\omega_9\omega_6\omega_{22}\omega_{11} - 36\omega_{18}\omega_9\omega_{22}\omega_{13}^2c_s^2\omega_{11} - 6\omega_{17}^2\omega_{18}\omega_9\omega_6^2\omega_{13}^2 - 12\omega_{17}^2\omega_9\omega_6^2\omega_{13}^2\omega_{11} + 18\omega_{17}^2\omega_{18}\omega_6\omega_{22}\omega_{13}^2\omega_{11} - \\
& 12\omega_{18}\omega_9\omega_6\omega_{13}\omega_{11} + 36\omega_{18}\omega_9\omega_6\omega_{13}c_s^2\omega_{11} - 12\omega_{17}^2\omega_6\omega_{22}\omega_{13}^2\omega_{11} + 18\omega_{18}\omega_6^2\omega_{22}\omega_{13}^2c_s^2 - 12\omega_{18}\omega_9\omega_{22}\omega_{13}^2\omega_{11} - 36\omega_9\omega_6^2\omega_{13}^2c_s^2\omega_{11} - \\
& 9\omega_{18}\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11} + 6\omega_{17}^2\omega_{18}\omega_9\omega_6^2\omega_{13}^2\omega_{11} - 36\omega_6^2\omega_{22}\omega_{13}^2c_s^2 - 12\omega_{17}^2\omega_{18}\omega_9\omega_6\omega_{22}\omega_{11} - 36\omega_{18}\omega_{22}\omega_{13}^2c_s^2\omega_{11} + 54\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}^2c_s^2\omega_{11} - \\
& 12\omega_{17}^2\omega_6^2\omega_{22}\omega_{13} + 12\omega_6\omega_{22}\omega_{13}\omega_{11} + 18\omega_{18}\omega_9\omega_6^2\omega_{13}^2c_s^2\omega_{11} + \omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}^2\omega_{11} + 12\omega_6^2\omega_{22}\omega_{13} - 12\omega_{17}^2\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}\omega_{11} + \\
& 12\omega_{17}^2\omega_{18}\omega_9\omega_6\omega_{13}\omega_{11} - 18\omega_{18}\omega_6\omega_{22}\omega_{13}\omega_{11} - 36\omega_{18}\omega_9\omega_6\omega_{22}c_s^2\omega_{11}
\end{aligned}$$

[illegible]

[illegible]

$$6v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 - 12\omega_{19}\omega_{16}\omega_7\omega_{11}^3 + 12v_3^2\omega_{19}\omega_{16}\omega_{23}\omega_{11}^3 + 36\omega_{19}\omega_{16}\omega_{23}c_s^2\omega_{11}^3 - 6v_3^2\omega_{19}\omega_7^2\omega_{11}^3 + 2\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 18\omega_{19}\omega_7^2c_s^2\omega_{11}^3 - 36\omega_{19}\omega_7\omega_{23}c_s^2\omega_{11}^2 + 12\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 54\omega_{19}\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11}^2 + 12v_3^2\omega_{19}\omega_7\omega_{11}^3 + 12\omega_{19}\omega_{16}\omega_7^2\omega_{11}^3 - 12\omega_{16}\omega_7^2\omega_{23}\omega_{11}^3 - \omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11}^3 - 12\omega_{19}\omega_7\omega_{11}^3 - 12\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 + 12\omega_{19}\omega_{16}\omega_{23}\omega_{11}^3 - 18\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 12v_3^2\omega_{19}\omega_{16}\omega_7\omega_{11}^3 - 12\omega_{19}\omega_{16}\omega_7^2\omega_{23} - 12v_3^2\omega_{19}\omega_7\omega_{23}\omega_{11}^2 + 12\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11} - 12v_3^2\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11}^2 + 54\omega_{19}\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11}^2 - 12v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{11}^3 - 12v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 36\omega_{19}\omega_{16}\omega_7c_s^2\omega_{11}^3 + 12v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 + 12\omega_{19}\omega_{16}\omega_7\omega_{11}^3 - 12v_3^2\omega_{19}\omega_{16}\omega_{23}\omega_{11}^3 + 12v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{23} - 40\omega_{19}\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11}^3 + 12\omega_{19}\omega_7\omega_{23}\omega_{11}^2 + 18v_3^2\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 36\omega_{19}\omega_{16}\omega_7c_s^2\omega_{11}^3 + 12\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11} + 18v_3^2\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11}^3 + 12v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^3 - 36\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11}^3$$

$$C_{24} = 12\omega_{16}\omega_7^2c_s^2\omega_{11}^2 + 36v_3^2\omega_{16}\omega_7^2\omega_{11}^2 - 12\omega_{16}\omega_7^3\omega_{11} + 12\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11} + 36v_3^2\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 36v_3^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} + 12\omega_{16}\omega_7^3\omega_{23}c_s^2\omega_{11}^2 - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}c_s^2\omega_{11} + 18v_3^2\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 18v_3^2\omega_{19}\omega_7^3\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_7^2\omega_{23} - 12\omega_{16}\omega_7^2\omega_{11}^2 + 36v_3^2\omega_{16}\omega_7^2\omega_{11} + 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 4\omega_{19}\omega_{16}\omega_7^2\omega_{23}c_s^2\omega_{11}^2 + 12\omega_{16}\omega_7^2\omega_{23}c_s^2\omega_{11} + 6\omega_{19}\omega_7^2\omega_{23}c_s^2\omega_{11} - 12\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 12\omega_{19}\omega_{16}\omega_7^2c_s^2\omega_{11}^2 - 12\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 24\omega_{16}\omega_7^2\omega_{23}c_s^2\omega_{11}^2 + 24\omega_{19}\omega_{16}\omega_7^2\omega_{23}c_s^2\omega_{11} + 12\omega_{16}\omega_7^3\omega_{23}\omega_{11} - 12\omega_{19}\omega_7^3\omega_{23}c_s^2\omega_{11} - \omega_{19}\omega_{16}\omega_7^3\omega_{23}c_s^2\omega_{11}^2 - 12\omega_{16}\omega_7^3\omega_{23}c_s^2\omega_{11} - 36v_3^2\omega_{16}\omega_7^3\omega_{11}^2 + 72v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 12\omega_{19}\omega_{16}\omega_{23}c_s^2\omega_{11}^2 - 12\omega_{19}\omega_{16}\omega_7^2\omega_{23}c_s^2 + 36v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 6\omega_{19}\omega_{16}\omega_7^2\omega_{23} + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}\omega_{11} + 12\omega_{16}\omega_7^3\omega_{11}^2 - 6\omega_{19}\omega_7^3\omega_{23}\omega_{11} - 36v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{23} - 6\omega_{19}\omega_7^3c_s^2\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_7^3c_s^2\omega_{11}^2 + 24\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_7^2\omega_{11} - 36v_3^2\omega_{19}\omega_7^2\omega_{23}\omega_{11} + 36v_3^2\omega_{19}\omega_7^2\omega_{11}^2 + 18\omega_{19}\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11}^2 + 36v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 36v_3^2\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 - 12\omega_{19}\omega_7^2\omega_{11}^2 + 18v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{11} - 24\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11} + 12\omega_{16}\omega_7^3c_s^2\omega_{11} - 18v_3^2\omega_{19}\omega_7^3\omega_{11} - 18v_3^2\omega_{19}\omega_{16}\omega_7^3\omega_{11} + 12\omega_{19}\omega_7^2\omega_{23}\omega_{11} + 12\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11}^2 - 12\omega_{19}\omega_{16}\omega_7\omega_{23}c_s^2\omega_{11} - 18v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 72v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}c_s^2 - 36v_3^2\omega_{19}\omega_{16}\omega_7^2\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^3\omega_{11} + 6\omega_{19}\omega_7^3\omega_{11}^2 - 6\omega_{19}\omega_{16}\omega_7^3c_s^2\omega_{11} - 12\omega_{16}\omega_7^2\omega_{23}\omega_{11}$$

$$C_{25} = 12\omega_{18}\omega_6^2c_s^4\omega_{11}^2 - 72v_3^2\omega_{18}\omega_6^3\omega_{11}^2 - \omega_{18}\omega_6^3c_s^4\omega_{11}^3 - 36v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^2 - 72v_3^2\omega_{18}\omega_6^3 + 36v_3^2\omega_{18}\omega_6c_s^2\omega_{11}^3 + 6\omega_{18}\omega_6^3c_s^2\omega_{11}^2 + 252v_3^2\omega_{18}\omega_6^3c_s^2 - 5\omega_{18}\omega_6^2c_s^2\omega_{11}^3 - 108v_3^2\omega_6^2c_s^2\omega_{11}^3 + 39v_3^2\omega_{18}\omega_6^3\omega_{11}^3 - 18\omega_{18}\omega_6^2c_s^4\omega_{11}^3 + \omega_{18}\omega_6^3c_s^4\omega_{11}^3 - 6\omega_{18}\omega_6^3c_s^2\omega_{11}^3 - 6\omega_{18}\omega_6^2c_s^2\omega_{11}^2 - 12\omega_{18}\omega_6^3c_s^2 - 6v_3^2\omega_{18}\omega_6^3\omega_{11}^3 - 90v_3^4\omega_{18}\omega_6^3\omega_{11} - 108v_3^2\omega_{18}\omega_6^3c_s^2\omega_{11} + 12\omega_{18}\omega_6^2c_s^2\omega_{11}^2 - 12\omega_{18}\omega_6c_s^2\omega_{11}^3 + 198v_3^2\omega_{18}\omega_6^3c_s^2\omega_{11}^2 + 19v_3^4\omega_{18}\omega_6^3\omega_{11}^2 - 3v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^3 + 72v_3^4\omega_{18}\omega_6^3 - 12\omega_{18}\omega_6^3c_s^4\omega_{11} - 99v_3^2\omega_{18}\omega_6^3c_s^2\omega_{11}^2 + 18v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^2 + 4v_3^4\omega_{18}\omega_6^3\omega_{11}^3 - 24\omega_{18}\omega_6^2c_s^4\omega_{11}^3 + 36v_3^2\omega_{18}\omega_6^3\omega_{11} - 36v_3^2\omega_{18}\omega_6^2\omega_{11}^3 + 72v_3^4\omega_{18}\omega_6^3\omega_{11}^2 - 18v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^3 - \omega_{18}\omega_6^3c_s^2\omega_{11}^2 + 36v_3^2\omega_6^3\omega_{11}^3 + 18\omega_{18}\omega_6^2c_s^2\omega_{11}^3 + 6\omega_{18}\omega_6^2c_s^4\omega_{11}^3 + 6\omega_{18}\omega_6^3c_s^4\omega_{11}^3 + 108v_3^2\omega_6^3c_s^2\omega_{11}^3 + 36v_3^4\omega_6^3\omega_{11}^3 - 306v_3^2\omega_{18}\omega_6^3c_s^2\omega_{11} - 12\omega_{18}\omega_6^2c_s^2\omega_{11}^3 - 39v_3^4\omega_{18}\omega_6^3\omega_{11}^3 + 6v_3^2\omega_{18}\omega_6^2\omega_{11}^3 + 90v_3^2\omega_{18}\omega_6^3\omega_{11} - 36v_3^4\omega_6^3\omega_{11}^3 - 108v_3^2\omega_6^3c_s^2\omega_{11}^2 + 13\omega_{18}\omega_6^2c_s^4\omega_{11}^3 - 6\omega_{18}\omega_6^3c_s^4\omega_{11}^3 - 36v_3^4\omega_6^3\omega_{11}^3 - 19v_3^2\omega_{18}\omega_6^3\omega_{11}^3 + 6\omega_{18}\omega_6^2c_s^2\omega_{11}^3 + 60v_3^2\omega_{18}\omega_6^3c_s^2\omega_{11}^2 + 54v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^3 + 12\omega_{18}\omega_6^2c_s^4\omega_{11}^3 - 36v_3^2\omega_6^3\omega_{11}^3 - 12\omega_{18}\omega_6^2c_s^4\omega_{11} + 12\omega_{18}\omega_6^3c_s^4\omega_{11}^3 - 4v_3^2\omega_{18}\omega_6^3\omega_{11}^3 - 36v_3^4\omega_{18}\omega_6^3\omega_{11} + 36v_3^2\omega_6^3\omega_{11}^3 + 36v_3^4\omega_{18}\omega_6^3\omega_{11} + 12\omega_{18}\omega_6^2c_s^2\omega_{11}^2 + 12v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^3 + 36v_3^2\omega_{18}\omega_6^2c_s^2\omega_{11}^2$$

$$C_{26} = -19v_3^2\omega_{19}\omega_7^3\omega_{11}^2 + 6\omega_{19}\omega_7^3c_s^4\omega_{11}^2 + 6\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 18v_3^2\omega_{19}\omega_7^2c_s^3\omega_{11}^2 + 18\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - \omega_{19}\omega_7^3c_s^2\omega_{11}^2 + 108v_3^2\omega_7^3c_s^2\omega_{11}^3 - 6\omega_{19}\omega_7^3c_s^4\omega_{11}^2 - 4v_3^2\omega_{19}\omega_7^3\omega_{11}^2 + 13\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 12\omega_{19}\omega_7^3c_s^4 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 108v_3^2\omega_7^3c_s^2\omega_{11}^3 - 36v_3^4\omega_{19}\omega_7^3\omega_{11}^2 - 306v_3^2\omega_{19}\omega_7^3c_s^2\omega_{11} + 6\omega_{19}\omega_7^2c_s^3\omega_{11}^2 + 54v_3^2\omega_{19}\omega_7^2c_s^3\omega_{11}^2 + 72v_3^4\omega_{19}\omega_7^2c_s^3\omega_{11}^2 + 60v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 36v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 12v_3^2\omega_{19}\omega_7^3\omega_{11}^2 + 6v_3^2\omega_{19}\omega_7^2\omega_{11}^3 + 36v_3^2\omega_{19}\omega_7^2c_s^3\omega_{11}^2 + 19v_3^4\omega_{19}\omega_7^2\omega_{11}^2 - 5\omega_{19}\omega_7^2c_s^2\omega_{11}^3 - 36v_3^4\omega_7^3\omega_{11}^3 + 6\omega_{19}\omega_7^3c_s^2\omega_{11}^2 - 36v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - \omega_{19}\omega_7^3c_s^4\omega_{11}^2 + 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 36v_3^2\omega_7^3c_s^4\omega_{11}^2 - 108v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11} - 108v_3^2\omega_7^2c_s^2\omega_{11}^3 - 6\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 6\omega_{19}\omega_7^3c_s^3\omega_{11}^2 + 4v_3^4\omega_{19}\omega_7^3\omega_{11}^2 - 36v_3^2\omega_{19}\omega_7^3\omega_{11}^2 + 72v_3^4\omega_{19}\omega_7^3 + 36v_3^2\omega_7^3\omega_{11}^3 + 36v_3^2\omega_{19}\omega_7^3\omega_{11} + \omega_{19}\omega_7^3c_s^4\omega_{11}^2 - 18\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 36v_3^2\omega_7^3\omega_{11}^3 - 72v_3^2\omega_{19}\omega_7^3\omega_{11}^2 - 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 12\omega_{19}\omega_7c_s^2\omega_{11}^3 + 252v_3^2\omega_{19}\omega_7^2c_s^2 - 3v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 198v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 12\omega_{19}\omega_7^2c_s^2\omega_{11} + 36v_3^4\omega_7^3\omega_{11}^3 + 39v_3^2\omega_{19}\omega_7^3\omega_{11}^2 - 24\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 90v_3^4\omega_{19}\omega_7^2\omega_{11}^2 - 72v_3^2\omega_{19}\omega_7^2 - 36v_3^4\omega_7^3\omega_{11}^3 - 6v_3^4\omega_{19}\omega_7^2\omega_{11}^2 + 18v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 99v_3^2\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 12\omega_{19}\omega_7^2c_s^2$$

$$C_{27} = 12 - 9v_3^4\omega_{11}^3 + 144v_3^4 + 90v_3^4\omega_{11}^2 + 198c_s^2\omega_{11} - 1008v_3^2c_s^2\omega_{11} + 404v_3^2c_s^2\omega_{11}^2 + 672v_3^2c_s^2 - 216v_3^4\omega_{11} - 78c_s^2\omega_{11}^2 - \omega_{11}^3 - 34v_3^2c_s^2\omega_{11}^3 + 6c_s^2\omega_{11}^3 + 8\omega_{11}^3 + 144c_s^4 - 216c_s^4\omega_{11} - 98v_3^2\omega_{11}^2 + 10v_3^2\omega_{11}^3 - 132c_s^2 - 156v_3^2 - 5c_s^4\omega_{11}^3 - 18\omega_{11} + 82c_s^4\omega_{11}^2 + 234v_3^2\omega_{11}$$

$$C_{28} = 12 - 29v_3^4\omega_{11}^3 + 504v_3^4 + 310v_3^4\omega_{11}^2 + 54c_s^2\omega_{11} - 648v_3^2c_s^2\omega_{11} + 252v_3^2c_s^2\omega_{11}^2 + 432v_3^2c_s^2 - 756v_3^4\omega_{11} - 22c_s^2\omega_{11}^2 - \omega_{11}^3 - 18v_3^2c_s^2\omega_{11}^3 + 2c_s^2\omega_{11}^3 + 8\omega_{11}^3 + 24c_s^4 - 36c_s^4\omega_{11} - 154v_3^2\omega_{11}^2 + 14v_3^2\omega_{11}^3 - 36c_s^2 - 252v_3^2 - c_s^4\omega_{11}^3 - 18\omega_{11} + 14c_s^4\omega_{11}^2 + 378v_3^2\omega_{11}$$

2.5 CLBM2

2.5.1 Definitions

Collision operator C :

$$C(f) = \mathbf{K}^{-1}\mathbf{S}(\boldsymbol{\kappa}^{(eq)} - \mathbf{K}f),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \dots, \omega_{27}),$$

$$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2).$$

Matrix \mathbf{K} corresponds to the transformation matrix to the central moment basis defined by

$$\boldsymbol{\kappa} = \begin{pmatrix} k_{(0,0,0)} \\ k_{(1,0,0)} \\ k_{(0,1,0)} \\ k_{(0,0,1)} \\ k_{(1,1,0)} \\ k_{(1,0,1)} \\ k_{(0,1,1)} \\ k_{(2,0,0)} - k_{(0,2,0)} \\ k_{(2,0,0)} - k_{(0,0,2)} \\ k_{(2,0,0)} + k_{(0,2,0)} + k_{(0,0,2)} \\ k_{(1,2,0)} + k_{(1,0,2)} \\ k_{(2,1,0)} + k_{(0,1,2)} \\ k_{(2,0,1)} + k_{(0,2,1)} \\ k_{(1,2,0)} - k_{(1,0,2)} \\ k_{(2,1,0)} - k_{(0,1,2)} \\ k_{(2,0,1)} - k_{(0,2,1)} \\ k_{(1,1,1)} \\ k_{(2,2,0)} - 2k_{(2,0,2)} + k_{(0,2,2)} \\ k_{(2,2,0)} + k_{(2,0,2)} - 2k_{(0,2,2)} \\ k_{(2,2,0)} + k_{(2,0,2)} + k_{(0,2,2)} \\ k_{(2,1,1)} \\ k_{(1,2,1)} \\ k_{(1,1,2)} \\ k_{(2,2,1)} \\ k_{(2,1,2)} \\ k_{(1,2,2)} \\ k_{(2,2,2)} \end{pmatrix},$$

The transformation matrix \mathbf{K} satisfies

$$\begin{aligned}
\mathbf{K}_{1,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,0)} \\
\mathbf{K}_{2,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,0)} \\
\mathbf{K}_{3,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,0)} \\
\mathbf{K}_{4,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,1)} \\
\mathbf{K}_{5,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,0)} \\
\mathbf{K}_{6,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,1)} \\
\mathbf{K}_{7,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,1)} \\
\mathbf{K}_{8,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} \\
\mathbf{K}_{9,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,0,2)} \\
\mathbf{K}_{10,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,0,2)} \\
\mathbf{K}_{11,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(1,0,2)} \\
\mathbf{K}_{12,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,1,2)} \\
\mathbf{K}_{13,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,1)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,1)} \\
\mathbf{K}_{14,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)} - (\mathbf{c}_i - \mathbf{v})^{(1,0,2)} \\
\mathbf{K}_{15,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,1,2)} \\
\mathbf{K}_{16,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,1)} \\
\mathbf{K}_{17,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,1)} \\
\mathbf{K}_{18,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)} - 2(\mathbf{c}_i - \mathbf{v})^{(2,0,2)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,2)} \\
\mathbf{K}_{19,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(2,0,2)} - 2(\mathbf{c}_i - \mathbf{v})^{(0,2,2)} \\
\mathbf{K}_{20,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(2,0,2)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,2)} \\
\mathbf{K}_{21,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,1)} \\
\mathbf{K}_{22,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,1)} \\
\mathbf{K}_{23,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,2)} \\
\mathbf{K}_{24,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,1)} \\
\mathbf{K}_{25,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,2)} \\
\mathbf{K}_{26,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,2)} \\
\mathbf{K}_{27,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,2)},
\end{aligned}$$

$\forall i \in \{1, 2, \dots, 27\}$. The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K} \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left(\rho, 0, 0, 0, 0, 0, 0, 0, 0, 3\rho c_s^2, 0, 0, 0, 0, 0, 0, 0, 3\rho c_s^4, 0, 0, 0, 0, 0, 0, 0, 3\rho c_s^6 \right)^T.$$

2.5.2 Conservation of mass: ρ

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{\delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{\delta_l^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{\delta_l^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\
& \frac{\rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} - \frac{\rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_1^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_l^3 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\
& + (-2c_s^2 - 6v_1^2 - 3\omega_9 v_1^4 + 24c_s^2 v_1^2 - \omega_9 c_s^4 + 3\omega_9 v_1^2 + \omega_9 c_s^2 - 12\omega_9 c_s^2 v_1^2 + 2c_s^4 + 6v_1^4) \frac{\delta_l^4 \rho}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 6c_s^2 + 10v_1^2 + 2\omega_9 - 5\omega_9 v_1^2 - 3\omega_9 c_s^2) \frac{\rho \delta_l^4 v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& (3\omega_9 \omega_{12} c_s^2 + \omega_9 \omega_{12} v_1^2 + 3\omega_9 - \omega_{12} - 3\omega_9 v_1^2 - 9\omega_9 c_s^2 + 3\omega_{12} c_s^2 - \omega_9 \omega_{12} + \omega_{12} v_1^2) \frac{\rho \delta_l^4 v_1}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + \omega_5) \frac{\delta_l^4 c_s^4}{6\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (3\omega_{15} \omega_{10} c_s^2 + \omega_{15} \omega_{10} v_2^2 - \omega_{15} \omega_{10} - \omega_{15} + 3\omega_{15} c_s^2 + \omega_{15} v_2^2 + 3\omega_{10} - 9\omega_{10} c_s^2 - 3\omega_{10} v_2^2) \frac{\rho \delta_l^4 v_2}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-6v_2^2 - 2c_s^2 - \omega_{10} c_s^4 - 3\omega_{10} v_2^4 - 12\omega_{10} v_2^2 c_s^2 + 24v_2^2 c_s^2 + 6v_2^4 + 2c_s^4 + \omega_{10} c_s^2 + 3\omega_{10} v_2^2) \frac{\delta_l^4}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 10v_2^2 + 6c_s^2 + 2\omega_{10} - 3\omega_{10} c_s^2 - 5\omega_{10} v_2^2) \frac{\rho \delta_l^4 v_2}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (3\omega_{13} c_s^2 + \omega_{13} v_1^2 + 3\omega_9 + 3\omega_9 \omega_{13} c_s^2 - \omega_9 \omega_{13} - 3\omega_9 v_1^2 + \omega_9 \omega_{13} v_1^2 - 9\omega_9 c_s^2 - \omega_{13}) \frac{\rho \delta_l^4 v_1}{12\omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-\omega_{16} \omega_{10} + 3\omega_{16} \omega_{10} c_s^2 + \omega_{16} \omega_{10} v_2^2 - \omega_{16} + 3\omega_{10} + 3\omega_{16} c_s^2 + \omega_{16} v_2^2 - 9\omega_{10} c_s^2 - 3\omega_{10} v_2^2) \frac{\rho \delta_l^4 v_2}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{\delta_l^4 c_s^4}{6\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-2 + \omega_7) \frac{\delta_l^4 c_s^4}{6\delta_t \omega_7} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (3\omega_{11} + \omega_{18} v_3^2 - 9\omega_{11} c_s^2 - \omega_{11} \omega_{18} + 3\omega_{18} c_s^2 - 3\omega_{11} v_3^2 - \omega_{18} + \omega_{11} \omega_{18} v_3^2 + 3\omega_{11} \omega_{18} c_s^2) \frac{\rho \delta_l^4 v_3}{12\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (3\omega_{11} - 9\omega_{11} c_s^2 + 3\omega_{11} \omega_{19} c_s^2 - 3\omega_{11} v_3^2 + \omega_{11} \omega_{19} v_3^2 + 3\omega_{19} c_s^2 - \omega_{19} - \omega_{11} \omega_{19} + \omega_{19} v_3^2) \frac{\rho \delta_l^4 v_3}{12\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-12\omega_{11} v_3^2 c_s^2 - 2c_s^2 + \omega_{11} c_s^2 + 3\omega_{11} v_3^2 - 6v_3^2 - 3\omega_{11} v_3^4 + 24v_3^2 c_s^2 + 6v_3^4 + 2c_s^4 - \omega_{11} c_s^4) \frac{\delta_l^4}{24\omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 2\omega_{11} + 6c_s^2 - 3\omega_{11} c_s^2 - 5\omega_{11} v_3^2 + 10v_3^2) \frac{\rho \delta_l^4 v_3}{12\omega_{11} \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.5.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho \delta_l v_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2 v_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l v_2}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho \delta_l v_1}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_3 v_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l v_3}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\rho \delta_l v_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + 4c_s^2 + 6v_1^2 + \omega_9 - 3\omega_9 v_1^2 - 2\omega_9 c_s^2) \frac{\delta_l^2}{\omega_9 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\rho \delta_l^2 v_1}{\omega_9 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + 6c_s^2 + 2v_1^2 + \omega_9 - \omega_9 v_1^2 - 3\omega_9 c_s^2) \frac{\delta_l^2 v_1}{2\omega_9 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + 2c_s^2 + 6v_1^2 + \omega_9 - 3\omega_9 v_1^2 - \omega_9 c_s^2) \frac{\rho \delta_l^2}{2\omega_9 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{\rho \delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{\rho \delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega_9^3 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 - 4\omega_9^2 + 36c_s^2 + 60v_1^2 + 5\omega_9^2 c_s^2 + 24\omega_9 + 11\omega_9^2 v_1^2 - 60\omega_9 v_1^2 - 36\omega_9 c_s^2) \frac{\rho \delta_l^3 v_1}{6\omega_9^3 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{\rho \delta_l^3 v_1}{12\omega_5 \omega_9^3 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 + 12\omega_5 - \omega_5^2) \frac{\delta_l^3 c_s^4}{6\omega_5^3 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{\rho \delta_l^3 c_s^2 v_1}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{\delta_l^3 v_2 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + C_3 \frac{\rho \delta_l^3 v_2}{6\omega_5 \omega_{15} \delta_t} \frac{\partial^3 v_1}{\partial x_2^2} + \\
& (-1 + 3v_2^2 + c_s^2) \frac{\rho \delta_l^3 v_1}{12\delta_t} \frac{\partial^3 v_2}{\partial x_3^2} + C_4 \frac{\rho \delta_l^3 v_1}{12\omega_9^3 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2 v_1}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (-12 - \omega_6^2 + 12\omega_6) \frac{\delta_l^3 c_s^4}{6\omega_6^3 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \\
& \frac{\rho \delta_l^3 c_s^2 v_1}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\rho \delta_l^3 c_s^2 v_1}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_l^3 v_3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^2} + C_5 \frac{\rho \delta_l^3 v_3}{6\omega_{18} \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_3^2} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3 v_1}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^2} + \\
& C_6 \frac{\delta_l^4 v_1}{12\omega_9^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_7 \frac{\rho \delta_l^4}{12\omega_9^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_8 \frac{\rho \delta_l^4}{12\omega_5^3 \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_9 \frac{\delta_l^4 c_s^2 v_1}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& C_{10} \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\delta_l^4 v_2 c_s^2}{12\omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& (3\omega_{15} \omega_{10} c_s^2 + \omega_{15} \omega_{10} v_2^2 - \omega_{15} \omega_{10} - \omega_{15} + 3\omega_{15} c_s^2 + \omega_{15} v_2^2 + 3\omega_{10} - 9\omega_{10} c_s^2 - 3\omega_{10} v_2^2) \frac{\rho \delta_l^4 v_2 v_1}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& C_{12} \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} +
\end{aligned}$$

$$\begin{aligned}
& (-6v_2^2 - 2c_s^2 - \omega_{10}c_s^4 - 3\omega_{10}v_2^4 - 12\omega_{10}v_2^2c_s^2 + 24v_2^2c_s^2 + 6v_2^4 + 2c_s^4 + \omega_{10}c_s^2 + 3\omega_{10}v_2^2) \frac{\delta_t^4 v_1}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& C_{13} \frac{\rho \delta_t^4}{24\omega_5^3 \omega_{15}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + (-4 + 10v_2^2 + 6c_s^2 + 2\omega_{10} - 3\omega_{10}c_s^2 - 5\omega_{10}v_2^2) \frac{\rho \delta_t^4 v_2 v_1}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + C_{14} \frac{\rho \delta_t^4}{12\omega_5^3 \omega_6^3 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{15} \frac{\rho \delta_t^4 c_s^4}{12\omega_{17} \omega_{14} \omega_8 \omega_5^3 \omega_{15} \omega_9 \omega_{12} \omega_6^2 \delta_t \omega_{13} \omega_7} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (-\omega_{16} \omega_{10} + 3\omega_{16} \omega_{10} c_s^2 + \omega_{16} \omega_{10} v_2^2 - \omega_{16} + 3\omega_{10} + 3\omega_{16} c_s^2 + \omega_{16} v_2^2 - 9\omega_{10} c_s^2 - 3\omega_{10} v_2^2) \frac{\rho \delta_t^4 v_2 v_1}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{16} \frac{\delta_t^4 c_s^2 v_1}{12\omega_{18} \omega_9^3 \omega_6^2 \omega_{22}^2 \delta_t \omega_{13}^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{17} \frac{\rho \delta_t^4 c_s^2}{12\omega_{18} \omega_9^3 \omega_6^2 \omega_{22}^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{18} \frac{\delta_t^4}{2\omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} \omega_6 \omega_{22}^2 \delta_t \omega_{13} \omega_{20}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{19} \frac{\rho \delta_t^4}{2\omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} \omega_6 \omega_{22}^2 \delta_t \omega_{13} \omega_{20}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{20} \frac{\rho \delta_t^4}{12\omega_{14} \omega_8 \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^3 \omega_{22}^2 \delta_t \omega_{13} \omega_7 \omega_{20}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{21} \frac{\rho \delta_t^4 v_3}{\omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} \omega_6 \omega_{22}^2 \delta_t \omega_{13} \omega_{20}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{22} \frac{\delta_t^4}{12\omega_{17} \omega_8 \omega_5 \omega_{18} \omega_{15} \omega_6 \delta_t \omega_7 \omega_{20}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{23} \frac{\rho \delta_t^4}{4\omega_{17} \omega_8 \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t \omega_{20}} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + C_{24} \frac{\rho \delta_t^4 v_2}{2\omega_{17} \omega_8 \omega_5 \omega_{18} \omega_{15} \omega_6 \delta_t \omega_{20}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\rho \delta_t^4}{4\omega_{17} \omega_8 \omega_5 \omega_{18} \omega_{15} \omega_6 \delta_t \omega_{20}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{26} \frac{\delta_t^4 v_3 c_s^2}{12\omega_{11} \omega_{18}^3 \omega_9 \omega_6^2 \omega_{22}^2 \delta_t \omega_{13}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + \\
& (3\omega_{11} + \omega_{18} v_3^2 - 9\omega_{11} c_s^2 - \omega_{11} \omega_{18} + 3\omega_{18} c_s^2 - 3\omega_{11} v_3^2 - \omega_{18} + \omega_{11} \omega_{18} v_3^2 + 3\omega_{11} \omega_{18} c_s^2) \frac{\rho \delta_t^4 v_3 v_1}{12\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& C_{27} \frac{\rho \delta_t^4 c_s^2}{12\omega_{11} \omega_{18} \omega_9 \omega_6^2 \omega_{22}^2 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (3\omega_{11} - 9\omega_{11} c_s^2 + 3\omega_{11} \omega_{19} c_s^2 - 3\omega_{11} v_3^2 + \omega_{11} \omega_{19} v_3^2 + 3\omega_{19} c_s^2 - \omega_{19} - \omega_{11} \omega_{19} + \omega_{19} v_3^2) \frac{\rho \delta_t^4 v_3 v_1}{12\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-12\omega_{11} v_3^2 c_s^2 - 2c_s^2 + \omega_{11} c_s^2 + 3\omega_{11} v_3^2 - 6v_3^2 - 3\omega_{11} v_3^4 + 24v_3^2 c_s^2 + 6v_3^4 + 2c_s^4 - \omega_{11} c_s^4) \frac{\delta_t^4 v_1}{24\omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho \delta_t^4}{24\omega_{18}^2 \omega_6^3 \delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + (-4 + 2\omega_{11} + 6c_s^2 - 3\omega_{11} c_s^2 - 5\omega_{11} v_3^2 + 10v_3^2) \frac{\rho \delta_t^4 v_3 v_1}{12\omega_{11} \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 24\omega_9^2 c_s^2 v_1^2 - 12c_s^2 - 36v_1^2 - 36\omega_9 v_1^4 + 144c_s^2 v_1^2 - \omega_9^2 c_s^2 - 12\omega_9 c_s^4 - 7\omega_9^2 v_1^2 + \omega_9^2 c_s^4 + 36\omega_9 v_1^2 + 7\omega_9^2 v_1^4 + 12\omega_9 c_s^2 - 144\omega_9 c_s^2 v_1^2 + 12c_s^4 + 36v_1^4 \\
C_2 &= 12\omega_5 \omega_9^3 v_1^2 - 6\omega_5^2 \omega_{12} + 12\omega_9 + 36\omega_5 \omega_9^2 c_s^2 - 36\omega_9^2 c_s^2 - 3\omega_5 \omega_9^2 \omega_{12} v_1^2 + 3\omega_5 \omega_9^2 \omega_{12} - 12\omega_9^2 v_1^2 - 11\omega_5 \omega_9^2 \omega_{12} c_s^2 + 18\omega_9^2 \omega_{12} c_s^2 + 12\omega_5 \omega_{12} v_1^2 + \\
& 6\omega_5 \omega_9 \omega_{12} - 6\omega_5 \omega_9 \omega_{12} v_1^2 - 12\omega_5 \omega_{12} + 6\omega_9^2 \omega_{12} v_1^2 + 12\omega_5 \omega_9 + 36\omega_5 \omega_{12} c_s^2 - 18\omega_5 \omega_9 \omega_{12} c_s^2 - 36\omega_5 \omega_9 c_s^2 - 12\omega_5 \omega_9^2 - 12\omega_5 \omega_9 v_1^2 \\
C_3 &= 6 - 6v_2^2 - 18c_s^2 - 3\omega_5 - 3\omega_{15} + 9\omega_{15} c_s^2 + 3\omega_{15} v_2^2 + \omega_5 \omega_{15} + 3\omega_5 v_2^2 + 9\omega_5 c_s^2 - \omega_5 \omega_{15} v_2^2 - 3\omega_5 \omega_{15} c_s^2 \\
C_4 &= 12\omega_9^2 - 6\omega_9 \omega_6 \omega_{13} v_1^2 - 12\omega_9^2 \omega_6 + 36\omega_6 \omega_{13} c_s^2 - 18\omega_9 \omega_6 \omega_{13} c_s^2 + 12\omega_6 \omega_{13} v_1^2 - 12\omega_9 \omega_6 v_1^2 + 18\omega_9^2 \omega_{13} c_s^2 - 36\omega_9^2 c_s^2 + 6\omega_9 \omega_6 \omega_{13} - \\
& 36\omega_9 \omega_6 c_s^2 + 6\omega_9^2 \omega_{13} v_1^2 - 6\omega_9^2 \omega_{13} - 12\omega_9^2 v_1^2 + 12\omega_9^2 \omega_6 v_1^2 + 3\omega_9^2 \omega_6 \omega_{13} - 3\omega_9^2 \omega_6 \omega_{13} v_1^2 + 36\omega_9^2 \omega_6 c_s^2 - 11\omega_9^2 \omega_6 \omega_{13} c_s^2 - 12\omega_6 \omega_{13} + 12\omega_9 \omega_6 \\
C_5 &= 6 + \omega_{18} \omega_6 - 18c_s^2 + 3\omega_{18} v_3^2 + 9\omega_{18} c_s^2 - 3\omega_{18} - 6v_3^2 - 3\omega_6 - 3\omega_{18} \omega_6 c_s^2 + 3\omega_6 v_3^2 - \omega_{18} \omega_6 v_3^2 + 9\omega_6 c_s^2 \\
C_6 &= 12 + 6\omega_9^2 c_s^2 + 404\omega_5^2 c_s^2 v_1^2 + 8\omega_9^2 - 132c_s^2 + 10\omega_3^3 v_1^2 - \omega_9^3 - 156v_1^2 - 216\omega_9 v_1^4 + 672c_s^2 v_1^2 - 78\omega_9^2 c_s^2 - 18\omega_9 - 216\omega_9 c_s^4 - 98\omega_9^2 v_1^2 + \\
& 82\omega_9^2 c_s^4 + 234\omega_9 v_1^2 + 90\omega_9^2 v_1^4 - 34\omega_9^2 c_s^2 v_1^2 + 198\omega_9 c_s^2 - 1008\omega_9 c_s^2 v_1^2 + 144c_s^4 - 5\omega_9^3 c_s^4 + 144v_1^4 - 9\omega_9^3 v_1^4 \\
C_7 &= 12 + 2\omega_9^2 c_s^2 + 252\omega_5^2 c_s^2 v_1^2 + 8\omega_9^2 - 36c_s^2 + 14\omega_9^3 v_1^2 - \omega_9^3 - 252v_1^2 - 756\omega_9 v_1^4 + 432c_s^2 v_1^2 - 22\omega_9^2 c_s^2 - 18\omega_9 - 36\omega_9 c_s^4 - 154\omega_9^2 v_1^2 + 14\omega_9^2 c_s^4 + \\
& 378\omega_9 v_1^2 + 310\omega_9^2 v_1^4 - 18\omega_9^2 c_s^2 v_1^2 + 54\omega_9 c_s^2 - 648\omega_9 c_s^2 v_1^2 + 24c_s^4 - \omega_9^3 c_s^4 + 504v_1^4 - 29\omega_9^3 v_1^4 \\
C_8 &= 12\omega_5^3 \omega_9^3 \omega_{12}^2 c_s^2 v_1^2 + 12\omega_5^3 \omega_{12}^2 c_s^4 - 6\omega_5^2 \omega_9^2 \omega_{12}^2 c_s^2 - \omega_5^3 \omega_9^3 \omega_{12}^2 c_s^4 - 108\omega_5^3 \omega_9^2 c_s^2 v_1^2 - 72\omega_5^3 \omega_{12}^2 v_1^2 + 54\omega_5^2 \omega_9^3 \omega_{12}^2 c_s^2 v_1^2 + 12\omega_5 \omega_9^3 \omega_{12}^2 c_s^4 + \\
& 39\omega_5^3 \omega_9 \omega_{12} v_1^2 - 12\omega_5^2 \omega_9 \omega_{12} c_s^4 + 36\omega_5 \omega_9^3 \omega_{12} c_s^2 v_1^2 - 36\omega_5^3 \omega_9^3 v_1^2 + 4\omega_5^3 \omega_9^3 \omega_{12}^2 v_1^4 + 6\omega_5 \omega_9^3 \omega_{12}^2 c_s^2 - 36\omega_5^2 \omega_9 \omega_{12}^2 c_s^2 v_1^2 + 12\omega_5^2 \omega_9 \omega_{12} c_s^4 - \\
& 12\omega_5^3 \omega_{12}^2 c_s^2 - 108\omega_5^3 \omega_9 \omega_{12} c_s^2 v_1^2 - 6\omega_5^3 \omega_9^3 \omega_{12} c_s^2 - 36\omega_5^2 \omega_9^3 v_1^4 - 6\omega_5^2 \omega_9^3 \omega_{12}^2 v_1^4 - 19\omega_5^3 \omega_9^2 \omega_{12}^2 v_1^2 - 90\omega_5^3 \omega_9 \omega_{12}^2 v_1^4 + 18\omega_5^2 \omega_9^3 \omega_{12} c_s^2 - 6\omega_5^2 \omega_9^2 \omega_{12} c_s^4 + \\
& 13\omega_5^3 \omega_9^2 \omega_{12} c_s^4 + 36\omega_5^3 \omega_9 \omega_{12} v_1^2 + 60\omega_5^2 \omega_9^2 \omega_{12}^2 c_s^2 v_1^2 - \omega_5^2 \omega_9^2 \omega_{12}^2 c_s^2 - 36\omega_5^2 \omega_9^3 \omega_{12} v_1^2 - 12\omega_5^3 \omega_9 \omega_{12}^2 c_s^4 + 72\omega_5^2 \omega_9^3 \omega_{12} v_1^4 + 36\omega_5^2 \omega_9^2 \omega_{12} c_s^2 v_1^2 + \\
& 36\omega_5^3 \omega_9 v_1^2 + 90\omega_5^3 \omega_9 \omega_{12}^2 v_1^2 - 18\omega_5^2 \omega_9^2 \omega_{12} c_s^4 + 6\omega_5^3 \omega_9^2 \omega_{12} c_s^2 + 36\omega_5^2 \omega_9^3 v_1^2 + 6\omega_5^2 \omega_9^3 \omega_{12}^2 v_1^2 + 19\omega_5^3 \omega_9^2 \omega_{12}^2 v_1^4 + 198\omega_5^3 \omega_9 \omega_{12} c_s^2 v_1^2 + 36\omega_5^2 \omega_9^3 \omega_{12} v_1^4 + \\
& 12\omega_5^3 \omega_9^2 \omega_{12} c_s^2 - 72\omega_5^3 \omega_9^2 \omega_{12} v_1^2 - 36\omega_5^2 \omega_9^3 v_1^4 - 5\omega_5^2 \omega_9^3 \omega_{12} c_s^2 - 36\omega_5^2 \omega_9 \omega_{12} v_1^4 + 18\omega_5^2 \omega_9^2 \omega_{12} c_s^2 v_1^2 + 108\omega_5^3 \omega_9^2 c_s^2 v_1^2 + \omega_5^3 \omega_9^2 \omega_{12} c_s^4 + 72\omega_5^3 \omega_{12} v_1^4 - \\
& 12\omega_5^3 \omega_9 \omega_{12} c_s^2 - 39\omega_5^3 \omega_9 \omega_{12} v_1^4 - 99\omega_5^3 \omega_9^2 \omega_{12} c_s^2 v_1^2 + 12\omega_5^2 \omega_9 \omega_{12} c_s^2 + 6\omega_5^2 \omega_9^2 \omega_{12} c_s^4 - 108\omega_5^2 \omega_9^3 c_s^2 v_1^2 - 3\omega_5^2 \omega_9^3 \omega_{12} c_s^2 v_1^2 + 252\omega_5^3 \omega_{12} c_s^2 v_1^2 - \\
& 12\omega_5^2 \omega_9^2 \omega_{12} c_s^2 + 12\omega_5^3 \omega_{12} c_s^4 - 18\omega_5 \omega_9^2 \omega_{12} c_s^2 v_1^2 + 6\omega_5^3 \omega_9^2 \omega_{12} c_s^2 - 306\omega_5^3 \omega_9 \omega_{12}^2 c_s^2 v_1^2 + 36\omega_5^3 \omega_9^3 v_1^4 - 4\omega_5^3 \omega_9^3 \omega_{12}^2 v_1^2 - 24\omega_5 \omega_9^3 \omega_{12}^2 c_s^4 \\
C_9 &= 18\omega_5 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} v_1^2 + 36\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12} c_s^2 - 36\omega_5 \omega_{21} \omega_{15} \omega_9^3 c_s^2 + 36\omega_5 \omega_{15} \omega_9^3 \omega_{12} c_s^2 + 12\omega_5 \omega_9^3 \omega_{12}^2 v_1^2 + 12\omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 v_1^2 - \\
& 6\omega_5^2 \omega_{21} \omega_9^2 \omega_{12} - 12\omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} v_1^2 - 6\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12} c_s^2 - \omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 - 12\omega_5^2 \omega_{15} \omega_9^3 \omega_{12} v_1^2 + 12\omega_5^2 \omega_{21} \omega_{15} \omega_9^3 v_1^2 + \\
& 54\omega_5 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} c_s^2 + 12\omega_5 \omega_{15} \omega_9^3 \omega_{12} v_1^2 + 36\omega_5 \omega_9^3 \omega_{12} c_s^2 + 12\omega_5^2 \omega_{21} \omega_{15} \omega_{12} v_1^2 - 12\omega_5 \omega_{21} \omega_{15} \omega_9^3 v_1^2 + 12\omega_5 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 + 36\omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 c_s^2 - \\
& 18\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12} - 36\omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} c_s^2 + 36\omega_5^2 \omega_{21} \omega_{15} \omega_9^3 c_s^2 - 36\omega_5^2 \omega_{15} \omega_9^3 \omega_{12} c_s^2 + 12\omega_5 \omega_{15} \omega_9^3 \omega_{12}^2 - 2\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 v_1^2 - \\
& 12\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 v_1^2 + 2\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 \omega_{12} - 18\omega_5^2 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} c_s^2 - 6\omega_5^2 \omega_{15} \omega_9^3 \omega_{12} v_1^2 + 12\omega_5 \omega_{21} \omega_{15} \omega_9^3 - 12\omega_5 \omega_{15} \omega_9^3 \omega_{12} + 18\omega_5 \omega_{21} \omega_{15} \omega_9^2 \omega_{12} v_1^2 - \\
& 18\omega_5 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} - 12\omega_5 \omega_9^3 \omega_{12} - 36\omega_5^2 \omega_{21} \omega_{15} \omega_9^2 c_s^2 - 18\omega_5^2 \omega_{15} \omega_9^2 \omega_{12} c_s^2 + 6\omega_5^2 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} - 6\omega_5^2 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} v_1^2 - 18\omega_5 \omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 + \\
& 54\omega_5 \omega_{21} \omega_{15} \omega_9^2 \omega_{12} c_s^2 - 36\omega_{21} \omega_{15} \omega_9^2 \omega_{12} c_s^2 - 36\omega_5 \omega_{21} \omega_9^2 \omega_{12} c_s^2 + \omega_5^2 \omega_{21} \omega_{15} \omega_9^3 \omega_{12} v_1^2 + 12\omega_{21} \omega_{15} \omega_9^2 \omega_{12} + 36\omega_5^2 \omega_{15} \omega_9^2 \omega_{12} c_s^2 - 12\omega_5^2 \omega_{15} \omega_9^2 \omega_{12} + \\
& 12\omega_5 \omega_{21} \omega_9^2 \omega_{12} + 6\omega_5^2 \omega_9^2 \omega_{12} - 6\omega_5^2 \omega_9^2 \omega_{12} v_1^2 + 6\omega_5^2 \omega_{21} \omega_9^2 \omega_{12} v_1^2 + 12\omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 12\omega_{21} \omega_{15} \omega_9^3 \omega_{12} - 12\omega_{21} \omega_{15} \omega_9^2 \omega_{12}^2 - 6\omega_5^2 \omega_{15} \omega_9^3 \omega_{12}^2 +
\end{aligned}$$

$$\begin{aligned}
& 4w_{14}w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_2c_s^2w_{20}v_1 + 4w_8w_5w_{18}w_9w_{12}w_6w_{22}v_3^2v_{2w_{20}}v_1 - 4w_{14}w_8w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_2v_1 + \\
& 4w_8w_5w_{18}w_6w_{22}w_{13}v_2c_s^2w_{20}v_1 + 4w_{14}w_8w_5w_{18}w_9w_{12}v_2c_s^2w_{20}v_1 + 2w_{14}w_8w_5w_{18}w_9w_{12}w_{22}v_2^2c_s^2w_{20} + 2w_{14}w_8w_5w_{18}w_9w_{12}w_{13}v_3^2v_2^2w_{20} - \\
& 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 + w_{14}w_8w_5w_{18}w_6w_{22}w_{13}v_2^2c_s^2w_{20} - 4w_{14}w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_{2w_{20}}v_1 - \\
& 4w_8w_5w_{18}w_9w_6w_{22}w_{13}v_2c_s^2w_{20}v_1 + 4w_8w_5w_{18}w_{12}w_6w_{22}v_3^2v_{2w_{20}}v_1 - 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}v_3^2v_2^2w_{20} - w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{13}v_2^2c_s^2w_{20} + \\
& 2w_{14}w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_2^2c_s^2 - w_{14}w_8w_5w_{18}w_{12}w_6w_{22}w_{13}v_2^2c_s^2w_{20} - 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}v_3^2c_s^2w_{20} + \\
& 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2v_1 + 4w_{14}w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_2v_1 + 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{13}v_2c_s^2w_{20}v_1 - \\
& w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} + 2w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} - 2w_{14}w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2c_s^2 - w_{14}w_8w_5w_{18}w_9w_6w_{22}w_{13}v_2^2c_s^2w_{20} + \\
& 4w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 - 2w_{14}w_8w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_2^2 + 2w_{14}w_8w_5w_{18}w_{12}w_6w_{22}v_3^2v_2^2w_{20} + 2w_{14}w_8w_5w_9w_{12}w_{22}w_{13}v_3^2c_s^2w_{20} + \\
& 4w_{14}w_8w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_{2w_{20}}v_1 + w_{14}w_8w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2 + w_{14}w_8w_5w_{18}w_{12}w_6w_{13}v_2^2c_s^2w_{20} + 2w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} - \\
& w_{14}w_8w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2c_s^2w_{20} - 2w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2c_s^2w_{20} + 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}v_3^2c_s^2w_{20} + w_{14}w_8w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2c_s^2 - \\
& 2w_{14}w_8w_5w_9w_{12}w_{22}w_{13}v_3^2c_s^2 + 2w_{14}w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} - 2w_{14}w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2 + 2w_{14}w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} + \\
& 2w_{14}w_8w_{18}w_9w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 + w_{14}w_8w_5w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2 - 2w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2c_s^2w_{20} - 2w_8w_{18}w_9w_6w_{22}w_{13}v_2^2c_s^2w_{20} + \\
& 4w_{14}w_8w_5w_9w_{12}w_{13}v_2c_s^2w_{20}v_1 - w_{14}w_8w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} + 2w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2c_s^2w_{20} + w_{14}w_8w_5w_9w_{12}w_6w_{22}w_{13}v_3^2c_s^2 + \\
& 2w_{14}w_8w_5w_9w_{12}w_{22}w_{13}v_3^2v_2^2w_{20} - 4w_{14}w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2v_1 + 2w_{14}w_8w_5w_{18}w_{12}w_6w_{22}v_3^2c_s^2w_{20} - 4w_8w_5w_{18}w_{12}w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 - \\
& 2w_{14}w_8w_5w_{18}w_{12}w_6w_{22}v_3^2c_s^2w_{20} - 4w_8w_{18}w_9w_{12}w_6w_{22}w_{13}v_2^2c_s^2w_{20} - 2w_8w_5w_{18}w_{12}w_6w_{22}v_2^2c_s^2w_{20} + w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2c_s^2w_{20} + \\
& w_{14}w_8w_{18}w_9w_6w_{22}w_{13}v_3^2c_s^2w_{20} + 2w_{14}w_5w_{18}w_9w_{12}w_{22}w_{13}v_2^2c_s^2w_{20} - 2w_{14}w_8w_{18}w_9w_{12}w_6w_{22}w_{13}v_2c_s^2v_1 + 4w_{14}w_8w_5w_9w_{12}w_{22}w_{13}v_2c_s^2v_1 + \\
& 2w_8w_5w_{18}w_{12}w_6w_{22}w_{13}v_2^2c_s^2w_{20} + 2w_8w_5w_{18}w_9w_{12}w_6w_{22}v_2^2c_s^2w_{20} - 2w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_2^2c_s^2w_{20} - 2w_{18}w_9w_{12}w_6w_{22}w_{13}v_2^2c_s^2w_{20} - \\
& 2w_{14}w_8w_5w_9w_{12}w_6w_{13}v_3^2v_{2w_{20}}v_1 + 4w_8w_5w_{18}w_9w_{12}w_{22}v_3^2v_{2w_{20}}v_1 + 4w_{18}w_9w_{12}w_6w_{22}w_{13}v_2c_s^2w_{20}v_1 + 4w_{14}w_{18}w_9w_{12}w_6w_{22}w_{13}v_2c_s^2v_1 + \\
& 2w_{14}w_8w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_2^2 + 4w_{14}w_8w_5w_{18}w_9w_{12}v_3^2v_{2w_{20}}v_1 - 4w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_2c_s^2w_{20}v_1 - 4w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 - \\
& 2w_{14}w_8w_5w_{18}w_9w_{12}w_{22}w_{13}v_2^2c_s^2w_{20} + 4w_{14}w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 - 2w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} - \\
& 2w_{14}w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2c_s^2 + 2w_8w_5w_{18}w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} - 2w_{14}w_5w_{18}w_9w_{12}w_{22}w_{13}v_3^2v_2^2 - 4w_8w_5w_{18}w_9w_6w_{22}w_{13}v_3^2v_{2w_{20}}v_1 + \\
& 4w_8w_5w_{18}w_{12}w_6w_{22}v_2^2c_s^2w_{20}v_1 + 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_2^2c_s^2 - 4w_{14}w_5w_{18}w_9w_{12}w_{22}w_{13}v_2^2c_s^2w_{20}v_1 + w_{14}w_8w_{18}w_9w_6w_{22}w_{13}v_3^2v_2^2w_{20} - \\
& 2w_{14}w_8w_5w_{18}w_9w_{12}w_6w_{22}w_{13}v_2c_s^2w_{20}v_1 + w_{14}w_8w_5w_9w_{12}w_6w_{22}w_{13}v_3^2v_2^2w_{20} - 2w_8w_5w_{18}w_9w_{$$

$$C_{21} = 2\omega_8\omega_{18}\omega_{912}\omega_{622}\omega_{13}v_2^2\omega_{20}v_1 - 2\omega_{18}\omega_{912}\omega_{622}\omega_{13}c_s^2\omega_{20}v_1 + 2\omega_{18}\omega_{912}\omega_{622}\omega_{13}v_2c_s^2\omega_{20} - 2\omega_8\omega_{518}\omega_{912}\omega_{622}v_2c_s^2\omega_{20} + 2\omega_8\omega_{518}\omega_{912}\omega_{622}c_s^2\omega_{20}v_1 + 2\omega_8\omega_{518}\omega_{12}\omega_{622}v_2c_s^2\omega_{20} - 2\omega_8\omega_{518}\omega_{12}\omega_{622}c_s^2\omega_{20}v_1 + \omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}c_s^2\omega_{20}v_1 - \omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2c_s^2\omega_{20} + 2\omega_{14}\omega_{518}\omega_{912}\omega_{622}\omega_{13}c_s^2\omega_{20}v_1 - 2\omega_{14}\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2c_s^2\omega_{20} - \omega_{14}\omega_8\omega_{18}\omega_{912}\omega_{622}\omega_{13}v_2\omega_{20}v_1^2 - 2\omega_8\omega_{518}\omega_{12}\omega_{622}\omega_{13}v_2\omega_{20}v_1^2 + 2\omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2c_s^2\omega_{20} - 2\omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}c_s^2\omega_{20}v_1 + 2\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2\omega_{20}v_1^2 - 2\omega_{14}\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2^2\omega_{20}v_1 + 2\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2^2\omega_{20}v_1^2 + 2\omega_{14}\omega_8\omega_{18}\omega_{912}\omega_{622}\omega_{13}v_2c_s^2\omega_{20} - 2\omega_{14}\omega_8\omega_{18}\omega_{912}\omega_{622}\omega_{13}c_s^2\omega_{20}v_1 - 2\omega_{14}\omega_{18}\omega_{912}\omega_{622}\omega_{13}c_s^2v_1 + 2\omega_{14}\omega_{18}\omega_{912}\omega_{622}\omega_{13}v_2\omega_{20}v_1^2 + \omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}c_s^2v_1 - \omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2^2\omega_{20}v_1^2 + 2\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2^2\omega_{20}v_1^2 - \omega_{14}\omega_8\omega_{518}\omega_{912}\omega_{622}\omega_{13}v_2\omega_{20}v_1^2 +$$

$$4\omega_{17}\omega_{518}\omega_{15}\omega_{6v_3^2}v_1 - 4\omega_{17}\omega_{518}\omega_{15}v_3c_s^2 + 4\omega_{18}\omega_{15}\omega_{6v_3^2}c_s^2\omega_{20}v_1 + 4\omega_{17}\omega_{518}\omega_{15}v_3\omega_{20}v_1^2 - 4\omega_{818}\omega_{15}\omega_{6v_3^2}c_s^2\omega_{20}v_1 - \omega_{17}\omega_{818}\omega_{518}\omega_{6v_3^2}c_s^2\omega_{20} + \omega_{17}\omega_{818}\omega_{518}\omega_{6v_3^2}\omega_{20}v_1 + 2\omega_{17}\omega_{818}\omega_{18}\omega_{6v_3^2}c_s^2\omega_{20} + 4\omega_{17}\omega_{818}\omega_{518}\omega_{15}v_3c_s^2 + 2\omega_{17}\omega_{818}\omega_{15}\omega_{6v_3^2}\omega_{20}v_1 - 4\omega_{17}\omega_{518}\omega_{15}v_3v_1^2$$

$$\begin{aligned}
C_{26} = & 3\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 - 6\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{13}v_3^2 + 36\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}c_s^2 + 12\omega_{18}\omega_6^2\omega_{22} - 3\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}v_3^2 - 18\omega_{11}\omega_{18}\omega_6^2\omega_{13}c_s^2 \\
& - 12\omega_{11}\omega_{18}\omega_6\omega_6 - 12\omega_{11}\omega_{18}\omega_6\omega_6\omega_{13} + 5\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13} + 18\omega_{11}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 + 36\omega_{18}\omega_6\omega_6^2\omega_{22}c_s^2 - 36\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}c_s^2 - 12\omega_{11}\omega_{18}\omega_6^2 \\
& + 6\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{13}v_3^2 + 54\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 - 12\omega_{18}\omega_6\omega_{22}\omega_{13}v_3^2 - 12\omega_{11}\omega_{18}\omega_6\omega_6^2v_3^2 + 12\omega_{18}\omega_6\omega_6^2\omega_{22}v_3^2 - \omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13} \\
& - 12\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}v_3^2 + 6\omega_{11}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 - 36\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}c_s^2 - 36\omega_{11}\omega_{18}\omega_6\omega_6^2c_s^2 - 6\omega_{11}\omega_6\omega_6^2\omega_{22}\omega_{13} + 18\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{13}c_s^2 - 12\omega_{18}\omega_6\omega_6^2\omega_{22} \\
& - 12\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}v_3^2 + 18\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 + 12\omega_{11}\omega_{18}\omega_6\omega_6^2 - 9\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 - 6\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13}v_3^2 - 6\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{13} + \\
& \omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}v_3^2 + 12\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}v_3^2 - 18\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{13}c_s^2 + 3\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13} + 12\omega_{11}\omega_{18}\omega_6\omega_6\omega_{13} + 12\omega_{11}\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13} \\
& - 36\omega_{18}\omega_6^2\omega_{22}c_s^2 - 12\omega_{18}\omega_6\omega_6\omega_{22}v_3^2 - 36\omega_{11}\omega_{18}\omega_6\omega_6\omega_{13}c_s^2 + 12\omega_{11}\omega_{18}\omega_6^2v_3^2 + 18\omega_{11}\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13}v_3^2 + 12\omega_{11}\omega_6\omega_6\omega_{22}\omega_{13} - \\
& 36\omega_{11}\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13}c_s^2 + 6\omega_{18}\omega_6^2\omega_{22}\omega_{13}v_3^2 + 36\omega_{11}\omega_{18}\omega_6\omega_6\omega_{13}c_s^2 - 15\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}c_s^2 - 6\omega_{18}\omega_6^2\omega_{22}\omega_{13} + 36\omega_{11}\omega_{18}\omega_6\omega_6c_s^2 - \\
& 18\omega_{11}\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13} + 12\omega_{18}\omega_6\omega_6\omega_{22} - 36\omega_{11}\omega_6\omega_6\omega_{22}\omega_{13}c_s^2 - 5\omega_{18}\omega_6\omega_6^2\omega_{22}\omega_{13}v_3^2 + 12\omega_{11}\omega_{18}\omega_6\omega_6\omega_{13}v_3^2 + 6\omega_{11}\omega_{18}\omega_6^2\omega_{13} - 18 \\
& 18\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13} + 12\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13} - 12\omega_{11}\omega_6\omega_6\omega_{22}\omega_{13}v_3^2 + 12\omega_{11}\omega_{18}\omega_6\omega_6^2v_3^2 + 12\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13} - 36\omega_{18}\omega_6\omega_6\omega_{22}c_s^2 - 12\omega_{18}\omega_6^2\omega_{22}v_3^2 - \\
& 12\omega_{11}\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13}v_3^2 + 18\omega_{18}\omega_6^2\omega_{22}\omega_{13}c_s^2 - 12\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}v_3^2 + 36\omega_{11}\omega_{18}\omega_6^2c_s^2 + 54\omega_{11}\omega_{18}\omega_6\omega_6\omega_{22}\omega_{13}c_s^2 + 6\omega_{11}\omega_{18}\omega_6\omega_6^2\omega_{13}
\end{aligned}$$

$$C_{28} = -72\omega_{18}\omega_6^2v_3^2 - 12\omega_{18}^2\omega_6^2v_3^4 - 12\omega_{18}^2\omega_6^2v_3^2c_s^2 - 3\omega_{18}^2\omega_6^3c_s^4 - 36\omega_3^3v_3^3 - 72\omega_{18}\omega_6^3v_3^3c_s^2 - 6\omega_{18}\omega_3^3c_s^2 + 12\omega_{18}^2\omega_6c_s^2 + 72\omega_{18}\omega_6v_3^3c_s^2 + 3\omega_{18}^2\omega_6^3v_3^4 + 30\omega_{18}\omega_3^3v_3^3 + 24\omega_{18}\omega_6c_s^4 + 24\omega_{18}\omega_6^2c_s^2 - 216\omega_3^2v_3^2c_s^2 + 24\omega_{18}^2c_s^4 + 72\omega_6^2v_3^2 + 24\omega_{18}^2\omega_6^2c_s^4 - 30\omega_{18}\omega_6^3v_3^3 - 24\omega_{18}\omega_6c_s^2 + 144\omega_{18}\omega_6^2v_3^2c_s^2 - 48\omega_{18}^2\omega_6c_s^4 - 3\omega_{18}^2\omega_6^3v_3^2 + 6\omega_{18}^2\omega_3^3v_3^2c_s^2 - 72\omega_6^2v_3^4 - 8\omega_{18}^2\omega_6^2c_s^2 - 24\omega_{18}\omega_6^2c_s^4 + 12\omega_{18}^2\omega_6^2v_3^2 - 36\omega_{18}\omega_6v_3^2c_s^2 + 72\omega_{18}\omega_6^2v_3^4 + 108\omega_3^3v_3^2c_s^2 + 6\omega_{18}\omega_6^2c_s^4 + \omega_{18}^2\omega_6^2c_s^2 + 36\omega_6^3v_3^3$$

$$\begin{aligned}
& (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (-2 + 2v_2^2 + 6c_s^2 + \omega_{10} - 3\omega_{10}c_s^2 - \omega_{10}v_2^2) \frac{\delta_l^2 v_2}{2\delta_t \omega_{10}} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + 6v_2^2 + 2c_s^2 + \omega_{10} - \omega_{10}c_s^2 - 3\omega_{10}v_2^2) \frac{\rho \delta_l^2}{2\delta_t \omega_{10}} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_7) \frac{\rho \delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_7) \frac{\rho \delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_3^2} + (-1 + 3c_s^2 + v_1^2) \frac{\delta_l^3 v_2 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3 v_2}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& C_1 \frac{\rho \delta_l^3 v_1}{6\omega_5 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 + 12\omega_5 - \omega_5^2) \frac{\delta_l^3 c_s^4}{6\omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \frac{\rho \delta_l^3 v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_2 \frac{\rho \delta_l^3 v_2}{12\omega_5 \omega_{15} \delta_t \omega_{10}^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_3 \frac{\delta_l^3}{12\delta_t \omega_{10}^2} \frac{\partial^3 \rho}{\partial x_2^2} + \\
& (-24 + 5\omega_{10}^2 c_s^2 + 11\omega_{10}^2 v_2^2 + 60v_2^2 + 36c_s^2 - 4\omega_{10}^2 + 24\omega_{10} - 36\omega_{10}c_s^2 - 60\omega_{10}v_2^2) \frac{\rho \delta_l^3 v_2}{6\delta_t \omega_{10}^2} \frac{\partial^3 v_2}{\partial x_2^2} - \frac{\rho \delta_l^3 v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^3 \partial x_3} + \\
& C_4 \frac{\rho \delta_l^3 v_2}{12\delta_t \omega_{16} \omega_{10}^2 \omega_7} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\rho \delta_l^3 v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + (-12 - \omega_7^2 + 12\omega_7) \frac{\delta_l^3 c_s^4}{6\delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{\rho \delta_l^3 v_2 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& (-1 + 3c_s^2 + v_3^2) \frac{\delta_l^3 v_3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{\rho \delta_l^3 v_3}{6\omega_{19} \delta_t \omega_7} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3 v_2}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2c_s^2 - 6v_1^2 - 3\omega_9 v_1^4 + 24c_s^2 v_1^2 - \omega_9 c_s^4 + 3\omega_9 v_1^2 + \omega_9 c_s^2 - 12\omega_9 c_s^2 v_1^2 + 2c_s^4 + 6v_1^4) \frac{\delta_l^4 v_2}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 6c_s^2 + 10v_1^2 + 2\omega_9 - 5\omega_9 v_1^2 - 3\omega_9 c_s^2) \frac{\rho \delta_l^4 v_2 v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_l^4}{24\omega_5^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_7 \frac{\delta_l^4 c_s^2 v_1}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12}^2 \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_8 \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& (3\omega_9 \omega_{12} c_s^2 + \omega_9 \omega_{12} v_1^2 + 3\omega_9 - \omega_{12} - 3\omega_9 v_1^2 - 9\omega_9 c_s^2 + 3\omega_{12} c_s^2 - \omega_9 \omega_{12} + \omega_{12} v_1^2) \frac{\rho \delta_l^4 v_2 v_1}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& C_9 \frac{\delta_l^4 v_2 c_s^2}{12\omega_5^2 \omega_{21} \omega_{15}^2 \omega_{12} \delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{10} \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_{12} \delta_t \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\rho \delta_l^4}{12\omega_5^3 \omega_{15}^2 \delta_t \omega_{10}^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{12} \frac{\delta_l^4 v_2}{12\delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_2^2} + \\
& C_{13} \frac{\rho \delta_l^4}{12\delta_t \omega_{10}^3} \frac{\partial^4 v_2}{\partial x_2^2} + (3\omega_{13} c_s^2 + \omega_{13} v_1^2 + 3\omega_9 + 3\omega_9 \omega_{13} c_s^2 - \omega_9 \omega_{13} - 3\omega_9 v_1^2 + \omega_9 \omega_{13} v_1^2 - 9\omega_9 c_s^2 - \omega_{13}) \frac{\rho \delta_l^4 v_2 v_1}{12\omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{14} \frac{\rho \delta_l^4 c_s^4}{12\omega_{17} \omega_{14} \omega_8 \omega_{12}^2 \omega_{15} \omega_{12} \omega_6 \delta_t \omega_{16} \omega_{10} \omega_7^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{15} \frac{\rho \delta_l^4}{12\delta_t \omega_{16} \omega_{10}^3 \omega_7^3} \frac{\partial^4 v_3}{\partial x_3^3} + C_{16} \frac{\delta_l^4}{12\omega_{14} \omega_8 \omega_{12} \omega_{15} \omega_{12} \omega_6 \omega_{19} \delta_t \omega_7 \omega_{20}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& C_{17} \frac{\rho \delta_l^4}{4\omega_{14} \omega_8 \omega_{12} \omega_{15} \omega_{12} \omega_{19} \delta_t \omega_7 \omega_{20}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{18} \frac{\rho \delta_l^4}{4\omega_{14} \omega_8 \omega_{12} \omega_{15} \omega_{12} \omega_{19} \delta_t \omega_7 \omega_{20}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + C_{19} \frac{\rho \delta_l^4 v_3}{2\omega_{14} \omega_8 \omega_{12} \omega_{15} \omega_{12} \omega_{19} \delta_t \omega_7 \omega_{20}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{20} \frac{\delta_l^4}{2\omega_{17} \omega_8 \omega_{15} \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{21} \frac{\rho \delta_l^4}{12\omega_{17} \omega_8 \omega_{15} \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{22} \frac{\rho \delta_l^4 v_2}{\omega_{17} \omega_8 \omega_{15} \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{23} \frac{\rho \delta_l^4}{2\omega_{17} \omega_8 \omega_{15} \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23} \omega_{20}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{24} \frac{\delta_l^4 v_2 c_s^2}{12\omega_{19} \delta_t \omega_{16} \omega_{10}^2 \omega_{23}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\rho \delta_l^4 c_s^2}{12\omega_{19} \delta_t \omega_{16} \omega_{10}^2 \omega_{23}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (3\omega_{11} + \omega_{18} v_3^2 - 9\omega_{11} c_s^2 - \omega_{11} \omega_{18} + 3\omega_{18} c_s^2 - 3\omega_{11} v_3^2 - \omega_{18} + \omega_{11} \omega_{18} v_3^2 + 3\omega_{11} \omega_{18} c_s^2) \frac{\rho \delta_l^4 v_3 v_2}{12\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + \\
& C_{26} \frac{\delta_l^4 v_3 c_s^2}{12\omega_{11} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^2} + \\
& (3\omega_{11} - 9\omega_{11} c_s^2 + 3\omega_{11} \omega_{19} c_s^2 - 3\omega_{11} v_3^2 + \omega_{11} \omega_{19} v_3^2 + 3\omega_{19} c_s^2 - \omega_{19} - \omega_{11} \omega_{19} + \omega_{19} v_3^2) \frac{\rho \delta_l^4 v_3 v_2}{12\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^2} + \\
& C_{27} \frac{\rho \delta_l^4 c_s^2}{12\omega_{11} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{23}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^2} + \\
& (-12\omega_{11} v_3^2 c_s^2 - 2c_s^2 + \omega_{11} c_s^2 + 3\omega_{11} v_3^2 - 6v_3^2 - 3\omega_{11} v_3^4 + 24v_3^2 c_s^2 + 6v_3^4 + 2c_s^4 - \omega_{11} c_s^4) \frac{\delta_l^4 v_2}{24\omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho \delta_l^4}{24\omega_{19}^2 \delta_t \omega_7^3} \frac{\partial^4 v_2}{\partial x_3^4} + (-4 + 2\omega_{11} + 6c_s^2 - 3\omega_{11} c_s^2 - 5\omega_{11} v_3^2 + 10v_3^2) \frac{\rho \delta_l^4 v_3 v_2}{12\omega_{11} \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 18c_s^2 - 3\omega_5 - 6v_1^2 - 3\omega_{12} - \omega_5 \omega_{12} v_1^2 + \omega_5 \omega_{12} - 3\omega_5 \omega_{12} c_s^2 + 9\omega_5 c_s^2 + 9\omega_{12} c_s^2 + 3\omega_5 v_1^2 + 3\omega_{12} v_1^2 \\
C_2 &= 12\omega_5 \omega_{10} - 36\omega_{10}^2 c_s^2 - 12\omega_{10}^2 v_2^2 - 3\omega_5 \omega_{15} \omega_{10}^2 v_2^2 - 11\omega_5 \omega_{15} \omega_{10}^2 c_s^2 + 6\omega_5 \omega_{15} \omega_{10} - 6\omega_{15} \omega_{10}^2 + 3\omega_5 \omega_{15} \omega_{10}^2 - 12\omega_5 \omega_{10}^2 v_2^2 + 12\omega_5 \omega_{10}^2 v_2^2 + \\
& 36\omega_5 \omega_{10}^2 c_s^2 - 12\omega_5 \omega_{10} v_2^2 - 36\omega_5 \omega_{10} c_s^2 + 12\omega_{10}^2 - 12\omega_5 \omega_{15} + 18\omega_{15} \omega_{10}^2 c_s^2 + 6\omega_{15} \omega_{10}^2 v_2^2 + 12\omega_5 \omega_{15} v_2^2 - 6\omega_5 \omega_{15} \omega_{10} v_2^2 - 18\omega_5 \omega_{15} \omega_{10} c_s^2 + 36\omega_5 \omega_{15} c_s^2 \\
C_3 &= -\omega_{10}^2 c_s^2 - 7\omega_{10}^2 v_2^2 - 36v_2^2 - 12c_s^2 - 12\omega_{10} c_s^4 - 36\omega_{10} v_2^4 - 144\omega_{10} v_2^2 c_s^2 + 144v_2^2 c_s^2 + 24\omega_{10}^2 v_2^2 c_s^2 + 36v_2^4 + 12c_s^4 + \omega_{10}^2 c_s^4 + 7\omega_{10}^2 v_2^4 + 12\omega_{10} c_s^2 + 36\omega_{10} v_2^2 \\
C_4 &= -36\omega_{10}^2 c_s^2 - 12\omega_{10}^2 v_2^2 - 11\omega_{16} \omega_{10}^2 \omega_7 c_s^2 - 36\omega_{10} \omega_7 c_s^2 - 12\omega_{10} \omega_7 v_2^2 - 3\omega_{16} \omega_{10} \omega_7 v_2^2 - 12\omega_{10}^2 \omega_7 + 3\omega_{16} \omega_{10}^2 \omega_7 + 36\omega_{16} \omega_7 c_s^2 + 12\omega_{16} \omega_7 v_2^2 + \\
& 18\omega_{16} \omega_{10}^2 c_s^2 + 6\omega_{16} \omega_{10}^2 v_2^2 - 6\omega_{16} \omega_{10}^2 + 12\omega_{10}^2 + 6\omega_{16} \omega_{10} \omega_7 + 12\omega_{10} \omega_7 - 6\omega_{16} \omega_{10} \omega_7 v_2^2 + 12\omega_{10}^2 \omega_7 v_2^2 + 36\omega_{10}^2 \omega_7 c_s^2 - 18\omega_{16} \omega_{10} \omega_7 c_s^2 - 12\omega_{16} \omega_7 \\
C_5 &= 6 - 18c_s^2 + 9\omega_7 c_s^2 + 3\omega_7 v_3^2 - 6v_3^2 + 9\omega_{19} c_s^2 - 3\omega_{19} - \omega_{19} \omega_7 v_3^2 + \omega_{19} \omega_7 - 3\omega_{19} \omega_7 c_s^2 - 3\omega_7 + 3\omega_{19} v_3^2 \\
C_6 &= 6\omega_5^3 \omega_{12} c_s^4 + 72\omega_5^3 v_1^2 - 72\omega_5^3 \omega_{12} c_s^2 v_1^2 - 3\omega_5^3 \omega_{12}^2 v_1^2 - 30\omega_5^3 \omega_{12} v_1^4 - 36\omega_5 \omega_{12}^2 c_s^2 v_1^2 + \omega_5^3 \omega_{12}^2 c_s^2 - 72\omega_5^3 \omega_{12} v_1^2 + 12\omega_5 \omega_{12}^2 c_s^2 + 24\omega_5^2 \omega_{12}^2 c_s^4 - 36\omega_5^3 v_1^2 + \\
& 108\omega_5^3 c_s^2 v_1^2 + 24\omega_5^2 \omega_{12} c_s^2 - 12\omega_5^2 \omega_{12}^2 v_1^4 + 24\omega_5 \omega_{12} c_s^4 + 144\omega_5^2 \omega_{12} c_s^2 v_1^2 + 36\omega_5^3 v_1^4 - 8\omega_5^2 \omega_{12}^2 c_s^2 + 72\omega_5^2 \omega_{12} v_1^4 - 48\omega_5 \omega_{12}^2 c_s^4 + 12\omega_5^2 \omega_{12}^2 v_1^2 - 24\omega_5 \omega_{12} c_s^2 - \\
& 12\omega_5^2 \omega_{12}^2 c_s^2 v_1^2 - 24\omega_5^2 \omega_{12} c_s^4 + 3\omega_5^3 \omega_{12}^2 v_1^4 - 6\omega_5^3 \omega_{12} c_s^2 - 72\omega_5^2 v_1^4 + 6\omega_5^2 \omega_{12}^2 c_s^2 v_1^2 - 216\omega_5^2 c_s^2 v_1^2 + 24\omega_{12}^2 c_s^4 - 3\omega_5^2 \omega_{12}^2 c_s^4 + 72\omega_5 \omega_{12} c_s^2 v_1^2 + 30\omega_5^3 \omega_{12} v_1^2
\end{aligned}$$

$$\begin{aligned}
& 12w_1w_7w_8w_5^3w_{15}w_6w_{16}w_{10}w_7^2 - 12w_1w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 - 12w_1w_7w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7 - 12w_1w_7w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 + \\
& 12w_1w_7w_{14}w_8w_5w_{15}w_{12}w_{16}w_{10}w_7^2 - 6w_1w_7w_{14}w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10} - 18w_1w_7w_{14}w_8w_5^2w_{15}w_{12}w_6w_{16}w_{10}w_7 - 6w_1w_7w_{14}w_8w_5^3w_{15}w_6w_{16}w_{10}w_7 - \\
& w_{17}w_{14}w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 + 10w_1w_7w_{14}w_8w_5^3w_{15}w_{12}w_{16}w_{10}w_7^2 + 12w_1w_7w_{14}w_8w_5^3w_{15}w_{16}w_7^2 - 24w_1w_7w_{14}w_8w_{15}w_{12}w_6w_{16}w_{10}w_7^2 - \\
& 12w_1w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10} - 12w_1w_7w_{14}w_8w_5^3w_{15}w_{12}w_{10}w_7^2 - 6w_1w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 - 12w_1w_4w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 + \\
& 12w_1w_7w_{14}w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7 + 12w_1w_4w_8w_5^3w_{12}w_6w_{16}w_{10}w_7^2 + 12w_1w_7w_{14}w_8w_5w_{15}w_{12}w_6w_{16}w_{10}w_7 - 12w_1w_7w_{14}w_8w_5^3w_{15}w_{12}w_{16}w_7^2 + \\
& 12w_1w_7w_{14}w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 - 12w_1w_4w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7 + 12w_1w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 + 12w_1w_4w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 + \\
& 6w_1w_7w_8w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7 - 12w_1w_7w_{14}w_5^3w_{15}w_{12}w_6w_{16}w_{10}w_7^2 + 12w_1w_4w_8w_5^3w_{15}w_{12}w_6w_{16}w_7^2 + 12w_1w_7w_{14}w_8w_5^3w_{15}w_6w_{16}w_{10}w_7 + \\
& 24w_1w_7w_{14}w_8w_5w_{15}w_{12}w_6w_{16}w_{10}w_7^2 - 12w_1w_7w_{14}w_8w_5^3w_{12}w_{16}w_{10}w_7^2 + 12w_1w_7w_{14}w_8w_5^3w_{15}w_{12}w_{10}w_7 + 6w_1w_7w_8w_5^3w_{15}w_6w_{16}w_{10}w_7^2 - \\
& 18w_1w_7w_{14}w_8w_5^3w_{15}w_{12}w_{16}w_{10}w_7 + 12w_1w_4w_8w_5^3w_{15}w_{12}w_6w_{10}w_7^2
\end{aligned}$$

C₁₆ = 12w₁₄w₅w₁₂w₆w₁₉w₇v₃²c_s²w₂₀ - 12w₁₄w₈w₅w₁₂w₆w₁₉v₂c_s²v₁ - 3w₁₄w₈w₅w₁₂w₆w₁₉v₃²v₂w₂₀v₁ - 12w₁₄w₅w₁₂w₆w₁₉w₇v₃²c_s²w₂₀v₁ - 3w₁₄w₈w₅w₁₂w₆w₁₉v₂c_s²w₂₀v₁ - 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²v₁ - 6w₈w₅w₁₂w₆w₁₉v₃²v₂c_s²w₂₀ + 6w₈w₅w₁₂w₆w₁₉v₃²c_s²w₂₀v₁ + 12w₁₄w₁₂w₆w₁₉w₇v₃²v₂c_s² + 6w₈w₅w₁₂w₆w₁₉w₇v₂c_s²w₂₀v₁ + 12w₁₄w₈w₅w₁₂w₆w₁₉v₂c_s²v₁ + 12w₁₄w₅w₁₂w₆w₁₉v₃²c_s² + 12w₈w₁₂w₆w₁₉w₇v₃²c_s²w₂₀v₁ - 12w₈w₁₂w₆w₁₉w₇v₂c_s²w₂₀v₁ - 12w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²w₂₀v₁ - 3w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²w₂₀v₁ - 3w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²w₂₀v₁ + 12w₁₂w₆w₁₉w₇v₃²c_s²w₂₀v₁ + 12w₁₂w₆w₁₉w₇v₃²v₂c_s²w₂₀ + 3w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²w₂₀v₁ - 3w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²v₂c_s²w₂₀ + 12w₅w₁₂w₆w₁₉v₃²c_s²w₂₀ - 12w₅w₁₂w₆w₁₉v₃²v₂c_s²w₂₀v₁ + 2w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²w₂₀ + 12w₈w₆w₁₉w₇v₃²v₂c_s²w₂₀ - 12w₈w₆w₁₉w₇v₃²c_s²w₂₀v₁ + 12w₁₄w₈w₅w₁₂w₆w₁₉v₃²c_s²v₁ - 12w₈w₆w₁₉w₇v₂c_s²v₁ - 12w₈w₆w₁₉w₇v₃²c_s²w₂₀v₁ - 12w₈w₆w₁₉w₇v₃²v₂w₂₀v₁ - 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²w₂₀v₁ - 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²v₁ - 12w₅w₁₂w₆w₁₉v₃²c_s²v₁ - 12w₅w₁₂w₆w₁₉v₃²v₂c_s²w₂₀v₁ - 12w₅w₁₂w₆w₁₉v₂c_s²w₂₀v₁ + 3w₁₄w₈w₅w₁₂w₆w₁₉v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₃²v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₃²v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₃²v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉w₇v₂c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆w₁₉v₃²c_s²v₁ + 6w₁₄w₈w₅w₁₂w₆

$$\begin{aligned}
& 2w_8w_5w_{19}w_7v_2w_{20}v_1^2 + 4w_8w_{12}w_{19}w_7v_2^2w_{20}v_1 - 4w_{14}w_5w_{12}w_{19}v_2c_s^2w_{20} + 4w_{14}w_5w_{12}w_{19}c_s^2w_{20}v_1 + 2w_{14}w_8w_5w_{12}w_{19}w_7v_2v_1^2 + \\
& -4w_{14}w_8w_5w_{12}v_2v_1^2 - 2w_8w_5w_{12}w_{19}w_7v_2^2w_{20}v_1 - 2w_{14}w_8w_5w_{12}w_{19}v_2^2w_{20}v_1 + 2w_{14}w_8w_5w_{12}v_2^2w_{20}v_1 + 4w_{14}w_8w_5w_{12}w_{19}c_s^2v_1 + 4w_8w_{19}w_7v_2c_s^2w_{20} - \\
& 4w_8w_{19}w_7c_s^2w_{20}v_1 + 4w_5w_{12}w_{19}w_7v_2^2w_{20}v_1 + w_{14}w_8w_5w_{19}w_7v_2c_s^2w_{20} - w_{14}w_8w_5w_{19}w_7c_s^2w_{20}v_1 + 4w_{14}w_8w_5w_{12}w_{19}v_2^2v_1 - 4w_{14}w_5w_{12}w_{19}w_7v_2c_s^2 + \\
& 4w_{14}w_8w_5w_{12}v_2c_s^2 - 4w_{14}w_{12}w_{19}w_7v_2^2v_1 - w_{14}w_8w_5w_{19}w_7v_2^2w_{20}v_1 - 2w_{14}w_8w_{19}w_7v_2w_{20}v_1^2 + 2w_{14}w_8w_{12}w_{19}w_7v_2w_{20}v_1^2 - 4w_5w_{12}w_{19}w_7v_2c_s^2w_{20} + \\
& 4w_5w_{12}w_{19}w_7c_s^2w_{20}v_1 - 4w_8w_{19}w_7v_2^2w_{20}v_1 - 2w_{14}w_8w_5w_{12}v_2c_s^2w_{20} + 2w_{14}w_8w_5w_{12}c_s^2w_{20}v_1 - 4w_{14}w_{12}w_{19}w_7v_2^2v_1 - 2w_{14}w_8w_5w_{12}w_{19}c_s^2w_{20}v_1 + \\
& 2w_{14}w_8w_5w_{12}w_{19}v_2c_s^2w_{20} + 2w_8w_5w_{12}w_{19}w_7v_2c_s^2w_{20} - 2w_8w_5w_{12}w_{19}w_7c_s^2w_{20}v_1 - 4w_{14}w_5w_{12}w_{19}w_7v_2v_1^2 + 2w_8w_5w_{12}w_{19}c_s^2w_{20}v_1 - \\
& 2w_8w_5w_{12}w_{19}v_2c_s^2w_{20} - 2w_{14}w_8w_{12}w_{19}w_7v_2v_1^2 + 4w_{14}w_5w_{12}w_{19}v_2c_s^2 - 4w_5w_{12}w_{19}c_s^2w_{20}v_1 + 4w_5w_{12}w_{19}v_2c_s^2w_{20} - 4w_5w_{12}w_{19}w_7v_2w_{20}v_1^2 + \\
& 2w_8w_5w_{19}w_7v_2^2w_{20}v_1 + 4w_{14}w_5w_{12}w_{19}w_7v_2c_s^2w_{20} - 4w_{14}w_5w_{12}w_{19}w_7c_s^2w_{20}v_1 + 4w_{14}w_{12}w_{19}w_7v_2^2w_{20}v_1 - w_{14}w_8w_5w_{12}w_{19}w_7v_2w_{20}v_1^2 + \\
& 4w_{12}w_{19}w_7v_2w_{20}v_1^2 + w_{14}w_8w_5w_{12}w_7v_2w_{20}v_1^2 - 2w_{14}w_8w_{12}w_{19}w_7v_2c_s^2 + 2w_{14}w_8w_5w_{12}w_7v_2^2v_1 + 4w_{14}w_5w_{12}w_{19}v_2v_1^2 - \\
& 2w_{14}w_8w_5w_{12}w_{19}w_7v_2^2v_1 - 4w_{14}w_{12}w_{19}w_7v_2c_s^2w_{20} + 4w_{14}w_{12}w_{19}w_7v_2c_s^2v_1 - 4w_{14}w_5w_{12}w_{19}w_7v_2^2w_{20}v_1 - 2w_8w_5w_{19}w_7v_2c_s^2w_{20} + \\
& 2w_8w_5w_{19}w_7c_s^2w_{20}v_1 - 2w_{14}w_8w_5w_{12}w_{19}w_7c_s^2v_1 - 4w_5w_{12}w_{19}v_2^2w_{20}v_1 - 4w_{14}w_5w_{12}w_{19}v_2w_{20}v_1^2 + 2w_{14}w_8w_5w_{12}w_7c_s^2v_1 + 2w_8w_5w_{12}w_{19}v_2^2w_{20}v_1
\end{aligned}$$

$$C_{22} = -\omega_{17}\omega_8\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}\omega_{20}v_1^2 + 2\omega_{17}\omega_8\omega_{15}\omega_{16}\omega_{10}v_3\omega_{23}\omega_{20}v_1^2 + 2\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{10}v_3^2\omega_{23}\omega_{20}v_1 + 2\omega_8\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23}\omega_{20}v_1 - 2\omega_{17}\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_{23}C_s^2\omega_{20}v_1 + 2\omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{10}v_3^2\omega_{20}v_1 + \omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}\omega_{20}v_1^2 + 2\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}v_3\omega_{23}C_s^2\omega_{20}v_1 - 2\omega_{17}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}C_s^2\omega_{20}v_1 - 2\omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{20}v_1 + 2\omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}v_3\omega_{23}C_s^2\omega_{20}v_1 + 2\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}\omega_{20}v_1^2 + 2\omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{16}\omega_{10}\omega_{23}C_s^2v_1 - \omega_{17}\omega_8\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}C_s^2v_1 - 2\omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{16}\omega_{10}v_3\omega_{23}^2v_1 + \omega_{17}\omega_8\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}^2v_1 + 2\omega_{17}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}C_s^2v_1 + 2\omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}\omega_{20}v_1 + \omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23}\omega_{20}v_1 + 2\omega_8\omega_{15}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23}\omega_{20}v_1 - 2\omega_{17}\omega_{15}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3\omega_{23}^2v_1 + \omega_{17}\omega_8\omega_{15}\omega_{15}\omega_{16}\omega_{10}\omega_7v_3C_s^2\omega_{20} -$$

$$\begin{aligned}
& 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7 + 18\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23} - 3\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^2v_3^2\omega_{23} - 36\omega_{11}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 + 12\omega_{11}\omega_{16}\omega_{10}\omega_7\omega_{23} + \\
& 36\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7c_s^2 + 12\omega_{19}\omega_{10}\omega_7\omega_{23} - 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} + 54\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - \\
& 15\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 6\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2 - 12\omega_{19}\omega_7^2v_3^2\omega_{23} - 12\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_{23} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{11}\omega_{19}\omega_7^2 + 3\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - \\
& 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2 - 6\omega_{11}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - \omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23} - 12\omega_{19}\omega_{10}\omega_7v_3^2\omega_{23} - 12\omega_{11}\omega_{19}\omega_{10}\omega_7 - \\
& 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} + 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2 - 12\omega_{11}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23} + 12\omega_{11}\omega_{19}\omega_{10}\omega_7v_3^2 + 54\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - 9\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + \\
& 36\omega_{11}\omega_{19}\omega_7^2c_s^2 + 36\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 18\omega_{11}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23} + 6\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2 + 3\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + \\
& 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_{23} + 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_{23} - 6\omega_{19}\omega_{16}\omega_7^2\omega_{23} + 12\omega_{11}\omega_{19}\omega_{10}\omega_7^2 + 36\omega_{11}\omega_{19}\omega_{10}\omega_7c_s^2 + 12\omega_{11}\omega_{19}\omega_7^2v_3^2 + 6\omega_{19}\omega_{16}\omega_7^2v_3^2\omega_{23} - \\
& 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_{23} + 12\omega_{19}\omega_7^2\omega_{23} - 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7 + 6\omega_{11}\omega_{19}\omega_{16}\omega_7^2 + 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 6\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2 \\
C_{27} = & -\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 6\omega_{11}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 36\omega_{19}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23} + 6\omega_{11}\omega_{19}\omega_{16}\omega_7^3 - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} - \\
& 12\omega_{11}\omega_{19}\omega_{10}\omega_7^2 + 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 12\omega_{11}\omega_{19}\omega_7^3c_s^2 + 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^3\omega_{23}c_s^2 + 12\omega_{11}\omega_{19}\omega_{10}\omega_7^3 - \\
& 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_{23}c_s^2 + 36\omega_{11}\omega_{19}\omega_7^3v_3^2 - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{11}\omega_{19}\omega_7^3 - 36\omega_{19}\omega_{10}\omega_7^2v_3^2\omega_{23} + 18\omega_{19}\omega_{16}\omega_7^3v_3^2\omega_{23} - \\
& 54\omega_{11}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} - 3\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} + 12\omega_{19}\omega_7^3\omega_{23} + 12\omega_{11}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - 12\omega_{11}\omega_{16}\omega_{10}\omega_7\omega_{23} - 12\omega_{19}\omega_7^3\omega_{23}c_s^2 - \\
& 15\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} + 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 - 12\omega_{11}\omega_{16}\omega_{10}\omega_7^2 + 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23}c_s^2 + \\
& \omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 12\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2 - 36\omega_{11}\omega_{19}\omega_{10}\omega_7^2v_3^2 + 18\omega_{11}\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 18\omega_{11}\omega_{16}\omega_{10}\omega_7^2v_3^2 + \\
& 18\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2 + 12\omega_{11}\omega_{19}\omega_{10}\omega_7^2c_s^2 + 36\omega_{11}\omega_{16}\omega_{10}\omega_7v_3^2\omega_{23} - 36\omega_{19}\omega_7^3v_3^2\omega_{23} + 6\omega_{11}\omega_{16}\omega_{10}\omega_7^3 - 5\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23}c_s^2 - \\
& 6\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^3 - 5\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 - 6\omega_{11}\omega_{19}\omega_{16}\omega_7^2c_s^2 - 18\omega_{11}\omega_{16}\omega_{10}\omega_7^2\omega_{23}c_s^2 + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}c_s^2 + 54\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} - \\
& 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 6\omega_{11}\omega_{16}\omega_{10}\omega_7^2c_s^2 - 6\omega_{11}\omega_{16}\omega_{10}\omega_7^3\omega_{23} + 36\omega_{11}\omega_{19}\omega_{10}\omega_7^2v_3^2 + 6\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2c_s^2 + 18\omega_{11}\omega_{16}\omega_{10}\omega_7^2v_3^2\omega_{23} - \\
& 18\omega_{11}\omega_{19}\omega_{16}\omega_7^3v_3^2 - 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}c_s^2 + 36\omega_{19}\omega_{10}\omega_7^3v_3^2\omega_{23} + 36\omega_{11}\omega_{16}\omega_{10}\omega_7^2v_3^2 - 12\omega_{11}\omega_{19}\omega_{10}\omega_7^3c_s^2 - 36\omega_{11}\omega_{19}\omega_{16}\omega_{10}\omega_7^2v_3^2 \\
C_{28} = & 3\omega_{19}\omega_7^3v_3^4 + 12\omega_{19}\omega_7c_s^2 + 144\omega_{19}\omega_7^2v_3^2c_s^2 + 24\omega_{19}\omega_7c_s^4 + 30\omega_{19}\omega_7^3v_3^2 + 24\omega_{19}\omega_7^2c_s^2 + 36\omega_7^3v_3^4 + 24\omega_{19}\omega_7^2c_s^4 + 6\omega_{19}\omega_7^3v_3^2c_s^2 - 72\omega_{19}\omega_7^2v_3^2 - \\
& 36\omega_{19}\omega_7^3c_s^2 + 108\omega_7^2v_3^2c_s^2 - 12\omega_{19}\omega_7^2v_3^4 - 3\omega_{19}\omega_7^3c_s^4 - 72\omega_7^2v_3^4 - 6\omega_{19}\omega_7^2c_s^2 - 12\omega_{19}\omega_7^2v_3^2c_s^2 + 12\omega_{19}\omega_7^2v_3^4 + 72\omega_{19}\omega_7^2v_3^4 + 6\omega_{19}\omega_7^3c_s^4 - 72\omega_{19}\omega_7^3v_3^2c_s^2 + \\
& 24\omega_{19}^2c_s^4 + 72\omega_7^2v_3^2 + \omega_{19}\omega_7^3c_s^2 - 24\omega_{19}\omega_7c_s^2 - 30\omega_{19}\omega_7^3v_3^4 - 3\omega_{19}\omega_7^3v_3^2 - 48\omega_{19}\omega_7c_s^4 + 72\omega_{19}\omega_7v_3^2c_s^2 - 8\omega_{19}\omega_7^2c_s^2 - 36\omega_7^3v_3^2 - 216\omega_7^2v_3^2c_s^2 - 24\omega_{19}\omega_7^2c_s^4
\end{aligned}$$

2.5.5 Conservation of momentum: ρv_3

$$\begin{aligned}
& v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{\delta_1 v_3 v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_1 v_3}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho \delta_1 v_1}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{\delta_1 v_3 v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_1 v_3}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\rho \delta_1 v_2}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\
& \frac{2\rho \delta_1 v_3}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{\delta_1^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_1^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\
& + (-2 + \omega_{11} + 4c_s^2 - 2\omega_{11}c_s^2 - 3\omega_{11}v_3^2 + 6v_3^2) \frac{\delta_1^2}{\omega_{11}\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3\rho \delta_1^2 v_3}{\omega_{11}\delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{\rho \delta_1^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\
& (-2 + \omega_7) \frac{\rho \delta_1^2 c_s^2}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{\rho \delta_1^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{\rho \delta_1^2 c_s^2}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\
& (-2 + \omega_{11} + 6c_s^2 - 3\omega_{11}c_s^2 - \omega_{11}v_3^2 + 2v_3^2) \frac{\delta_1^2 v_3}{2\omega_{11}\delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_{11} + 2c_s^2 - \omega_{11}c_s^2 - 3\omega_{11}v_3^2 + 6v_3^2) \frac{\rho \delta_1^2}{2\omega_{11}\delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (-1 + 3c_s^2 + v_1^2) \frac{\delta_1^3 v_3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_1^3 v_3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{\rho \delta_1^3 v_1}{6\omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{\rho \delta_1^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_2} - \frac{\rho \delta_1^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-1 + v_2^2 + 3c_s^2) \frac{\delta_1^3 v_3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\rho \delta_1^3 v_3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_2 \frac{\rho \delta_1^3 v_2}{6\delta_t \omega_{16} \omega_7} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 - \omega_6^2 + 12\omega_6) \frac{\delta_1^3 c_s^4}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\
& \frac{\rho \delta_1^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 - \omega_7^2 + 12\omega_7) \frac{\delta_1^3 c_s^4}{6\delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{\rho \delta_1^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_3 \frac{\rho \delta_1^3 v_3}{12\omega_{11}^2 \omega_{18} \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
C_4 = & \frac{\rho \delta_1^3 v_3}{12\omega_{11}^2 \omega_{19} \delta_t \omega_7} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_5 \frac{\delta_1^3}{12\omega_{11}^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-24 + 24\omega_{11} + 36c_s^2 - 36\omega_{11}c_s^2 - 60\omega_{11}v_3^2 + 60v_3^2 + 11\omega_{11}^2v_3^2 + 5\omega_{11}^2c_s^2 - 4\omega_{11}^2) \frac{\rho \delta_1^3 v_3}{6\omega_{11}^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2c_s^2 - 6v_1^2 - 3\omega_9v_1^4 + 24c_s^2v_1^2 - \omega_9c_s^4 + 3\omega_9v_1^2 + \omega_9c_s^2 - 12\omega_9c_s^2v_1^2 + 2c_s^4 + 6v_1^4) \frac{\delta_1^4 v_3}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 6c_s^2 + 10v_1^2 + 2\omega_9 - 5\omega_9v_1^2 - 3\omega_9c_s^2) \frac{\rho \delta_1^4 v_3 v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_1^4}{24\omega_6^3 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^4} + \\
& (3\omega_9\omega_{12}c_s^2 + \omega_9\omega_{12}v_1^2 + 3\omega_9 - \omega_{12} - 3\omega_9v_1^2 - 9\omega_9c_s^2 + 3\omega_{12}c_s^2 - \omega_9\omega_{12} + \omega_{12}v_1^2) \frac{\rho \delta_1^4 v_3 v_1}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + \\
& (-2 + \omega_5) \frac{\delta_1^4 v_3 c_s^4}{6\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_7 \frac{\rho \delta_1^4 c_s^4}{2\omega_{17} \omega_{14} \omega_8 \omega_6^2 \delta_t \omega_{16} \omega_{13} \omega_7^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (3\omega_{15}\omega_{10}c_s^2 + \omega_{15}\omega_{10}v_2^2 - \omega_{15}\omega_{10} - \omega_{15} + 3\omega_{15}c_s^2 + \omega_{15}v_2^2 + 3\omega_{10} - 9\omega_{10}c_s^2 - 3\omega_{10}v_2^2) \frac{\rho \delta_1^4 v_3 v_2}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
& (-6v_2^2 - 2c_s^2 - \omega_{10}c_s^4 - 3\omega_{10}v_2^4 - 12\omega_{10}v_2^2c_s^2 + 24v_2^2c_s^2 + 6v_2^4 + 2c_s^4 + \omega_{10}c_s^2 + 3\omega_{10}v_2^2) \frac{\delta_1^4 v_3}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 10v_2^2 + 6c_s^2 + 2\omega_{10} - 3\omega_{10}c_s^2 - 5\omega_{10}v_2^2) \frac{\rho \delta_1^4 v_3 v_2}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^2} + C_8 \frac{\rho \delta_1^4}{24\delta_t \omega_{16}^2 \omega_7^2} \frac{\partial^4 v_3}{\partial x_2^4} + C_9 \frac{\delta_1^4 c_s^4 v_1}{12\omega_{11} \omega_{18} \omega_9 \omega_6^2 \omega_{22} \delta_t \omega_{13}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
C_{10} = & \frac{\rho \delta_1^4 c_s^2}{12\omega_{11} \omega_{18} \omega_9 \omega_6^2 \omega_{22} \delta_t \omega_{13}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& (3\omega_{13}c_s^2 + \omega_{13}v_1^2 + 3\omega_9 + 3\omega_9\omega_{13}c_s^2 - \omega_9\omega_{13} - 3\omega_9v_1^2 + \omega_9\omega_{13}v_1^2 - 9\omega_9c_s^2 - \omega_{13}) \frac{\rho \delta_1^4 v_3 v_1}{12\omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& C_{11} \frac{\delta_1^4}{2\omega_{11}\omega_{14}\omega_8\omega_{18}\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{12} \frac{\rho \delta_1^4}{2\omega_{11}\omega_{14}\omega_8\omega_{18}\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{13} \frac{\rho \delta_1^4}{12\omega_{11}\omega_{14}\omega_8\omega_{18}\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{14} \frac{\rho \delta_1^4 v_3}{\omega_{11}\omega_{14}\omega_8\omega_{18}\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{15} \frac{\delta_1^4}{2\omega_{17}\omega_{11}\omega_8\omega_{18}\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{16} \frac{\rho \delta_1^4}{12\omega_{17}\omega_{11}\omega_8\omega_{18}\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{17} \frac{\rho \delta_1^4 v_2}{\omega_{17}\omega_{11}\omega_8\omega_{18}\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{18} \frac{\rho \delta_1^4}{2\omega_{17}\omega_{11}\omega_8\omega_{18}\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{19} \frac{\delta_1^4 v_2 c_s^2}{12\omega_{11}\omega_{19}\delta_t\omega_{16}^2\omega_{10}\omega_7^2\omega_{23}} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + C_{20} \frac{\rho \delta_1^4 c_s^2}{12\omega_{11}\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7^2\omega_{23}} \frac{\partial^4 v_2}{\partial x_3^3 \partial x_3} + \\
& (-\omega_{16}\omega_{10} + 3\omega_{16}\omega_{10}c_s^2 + \omega_{16}\omega_{10}v_2^2 - \omega_{16} + 3\omega_{10} + 3\omega_{16}c_s^2 + \omega_{16}v_2^2 - 9\omega_{10}c_s^2 - 3\omega_{10}v_2^2) \frac{\rho \delta_1^4 v_3 v_2}{12\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 v_3}{\partial x_3^2 \partial x_3} + \\
& C_{21} \frac{\delta_1^4 v_3 c_s^2}{12\omega_{11}^3\omega_{18}\omega_6^2\omega_{22}\delta_t\omega_{13}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{22} \frac{\rho \delta_1^4 c_s^2}{12\omega_{11}^3\omega_{18}\omega_6^2\omega_{22}\delta_t\omega_{13}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{23} \frac{\delta_1^4 v_3 c_s^2}{12\omega_{11}^3\omega_{19}^2\delta_t\omega_{16}\omega_7^2\omega_{23}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{24} \frac{\rho \delta_1^4 c_s^2}{12\omega_{11}^2\omega_{19}\delta_t\omega_{16}\omega_7^3\omega_{23}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\rho \delta_1^4}{12\omega_{11}^3\omega_{18}\omega_6^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{26} \frac{\rho \delta_1^4}{12\omega_{11}^3\omega_{19}^2\delta_t\omega_7^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{27} \frac{\delta_1^4 v_3}{12\omega_{11}^3\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho \delta_1^4}{12\omega_{11}^3\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 + 9\omega_{13}c_s^2 - 18c_s^2 - 3\omega_6\omega_{13}c_s^2 + 3\omega_{13}v_1^2 - \omega_6\omega_{13}v_1^2 - 6v_1^2 - 3\omega_6 - 3\omega_{13} + \omega_6\omega_{13} + 3\omega_6v_1^2 + 9\omega_6c_s^2 \\
C_2 &= 6 - 6v_2^2 - 18c_s^2 + 9\omega_7c_s^2 + 3\omega_7v_2^2 - 3\omega_{16}\omega_7c_s^2 - \omega_{16}\omega_7v_2^2 - 3\omega_{16} + 9\omega_{16}c_s^2 + 3\omega_{16}v_2^2 - 3\omega_7 + \omega_{16}\omega_7 \\
C_3 &= -12\omega_{18}\omega_6 - 3\omega_{11}^2\omega_{18}\omega_6v_3^2 + 18\omega_{11}^2\omega_{18}c_s^2 - 12\omega_{11}\omega_6v_3^2 + 6\omega_{11}^2\omega_{18}v_3^2 - 11\omega_{11}^2\omega_{18}\omega_6c_s^2 - 36\omega_{11}\omega_6c_s^2 + 12\omega_{11}\omega_6 + 3\omega_{11}^2\omega_{18}\omega_6 - 12\omega_{11}^2\omega_6 + 36\omega_{18}\omega_6c_s^2 + 36\omega_{11}^2\omega_6c_s^2 + 6\omega_{11}\omega_{18}\omega_6 - 12\omega_{11}^2v_3^2 - 6\omega_{11}\omega_{18}\omega_6v_3^2 - 36\omega_{11}^2c_s^2 + 12\omega_{11}^2 - 18\omega_{11}\omega_{18}\omega_6c_s^2 - 6\omega_{11}^2\omega_{18} + 12\omega_{18}\omega_6v_3^2 + 12\omega_{11}^2\omega_6v_3^2 \\
C_4 &= 12\omega_{11}\omega_7 - 11\omega_{11}^2\omega_{19}\omega_7c_s^2 + 6\omega_{11}\omega_{19}\omega_7 + 12\omega_{11}^2\omega_7v_3^2 - 6\omega_{11}^2\omega_{19} + 36\omega_{11}^2\omega_7c_s^2 - 3\omega_{11}^2\omega_{19}\omega_7v_3^2 + 6\omega_{11}^2\omega_{19}v_3^2 - 36\omega_{11}\omega_7c_s^2 - 18\omega_{11}\omega_{19}\omega_7c_s^2 + 12\omega_{19}\omega_7v_3^2 - 12\omega_{11}^2v_3^2 - 12\omega_{19}\omega_7 - 36\omega_{11}^2c_s^2 + 12\omega_{11}^2 + 3\omega_{11}^2\omega_{19}\omega_7 + 36\omega_{19}\omega_7c_s^2 - 12\omega_{11}^2\omega_7 + 18\omega_{11}^2\omega_{19}c_s^2 - 12\omega_{11}\omega_7v_3^2 - 6\omega_{11}\omega_{19}\omega_7v_3^2 \\
C_5 &= -144\omega_{11}v_3^2c_s^2 + \omega_{11}^2c_s^4 - 12c_s^2 + 12\omega_{11}c_s^2 + 36\omega_{11}v_3^2 - 36v_3^2 + 7\omega_{11}^2v_3^4 - 36\omega_{11}v_3^4 + 144v_3^2c_s^2 + 36v_3^4 - 7\omega_{11}^2v_3^2 - \omega_{11}^2c_s^2 + 24\omega_{11}^2v_3^2c_s^2 + 12c_s^4 - 12\omega_{11}c_s^4 \\
C_6 &= -24\omega_6^2\omega_{13}c_s^4 + 144\omega_6^2\omega_{13}c_s^2v_1^2 + 12\omega_6^2\omega_{13}v_1^2 - 24\omega_6\omega_{13}c_s^2 + 72\omega_6^2\omega_{13}v_1^4 - 48\omega_6\omega_{13}c_s^4 + 108\omega_6^3c_s^2v_1^2 + 24\omega_{13}^3c_s^4 - 8\omega_6^2\omega_{13}^2c_s^2 + 72\omega_6^2v_1^2 - 36\omega_6\omega_{13}^2c_s^2v_1^2 + 30\omega_6^2\omega_{13}v_1^4 - 3\omega_6^2\omega_{13}c_s^4 - 6\omega_6^2\omega_{13}c_s^2 - 36\omega_6^3v_1^2 + 3\omega_6^3\omega_{13}v_1^4 - 72\omega_6^3\omega_{13}c_s^2v_1^2 + \omega_6^3\omega_{13}^2c_s^2 + 72\omega_6\omega_{13}c_s^2v_1^2 - 30\omega_6^3\omega_{13}v_1^4 - 216\omega_6^3c_s^2v_1^2 - 3\omega_6^3\omega_{13}^2v_1^2 + 6\omega_6^3\omega_{13}^2c_s^2v_1^2 + 6\omega_6^3\omega_{13}c_s^4 + 36\omega_6^3v_1^4 - 12\omega_6^2\omega_{13}^2v_1^4 + 24\omega_6\omega_{13}c_s^4 + 24\omega_6^2\omega_{13}c_s^2 - 12\omega_6^2\omega_{13}^2c_s^2v_1^2 + 24\omega_6^2\omega_{13}^3c_s^4 - 72\omega_6^2v_1^4 - 72\omega_6^2\omega_{13}v_1^2 + 12\omega_6\omega_{13}^2c_s^2 \\
C_7 &= -\omega_{17}\omega_{14}\omega_8\omega_{16}\omega_{13}\omega_7^2 + 2\omega_{17}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7^2 - 2\omega_{17}\omega_8\omega_6\omega_{16}\omega_7^2 - \omega_{17}\omega_{14}\omega_8\omega_6^2\omega_{16}\omega_7 + 2\omega_{17}\omega_6^2\omega_{16}\omega_{13}\omega_7^2 - 6\omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7 - \omega_{17}\omega_{14}\omega_8\omega_6^2\omega_{16}\omega_{13} + 2\omega_{17}\omega_{14}\omega_8\omega_6\omega_{13}\omega_7 - \omega_{14}\omega_8\omega_6^2\omega_{16}\omega_{13}\omega_7^2 + 2\omega_{17}\omega_{14}\omega_6\omega_{16}\omega_{13}\omega_7^2 - 2\omega_{14}\omega_6\omega_{16}\omega_{13}\omega_7^2 + 2\omega_{14}\omega_8\omega_6^2\omega_{16}\omega_{13}\omega_7 - \omega_{17}\omega_{14}\omega_8\omega_6\omega_{13}\omega_7^2 + 2\omega_{17}\omega_{14}\omega_8\omega_6\omega_{13}\omega_7 + \omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7 - \omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7 - \omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7^2 - 2\omega_{17}\omega_{14}\omega_6^2\omega_{16}\omega_{13}\omega_7 - 2\omega_{17}\omega_{14}\omega_6\omega_{16}\omega_{13}\omega_7^2 - 2\omega_{14}\omega_8\omega_6^2\omega_{13}\omega_7 + \omega_{14}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7^2 + 2\omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_{13}\omega_7 + \omega_{17}\omega_8\omega_6^2\omega_{16}\omega_{13}\omega_7 + 2\omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_7 + \omega_{14}\omega_8\omega_6^2\omega_{13}\omega_7^2 + 2\omega_{14}\omega_6^2\omega_{16}\omega_{13}\omega_7^2 + 2\omega_{17}\omega_{14}\omega_8\omega_6\omega_{16}\omega_{13} + \omega_{17}\omega_8\omega_6^2\omega_{16}\omega_{13}\omega_7 \\
C_8 &= -72\omega_7^2v_4^2 + \omega_{16}^2\omega_7^3c_s^2 - 216\omega_7^2v_2^2c_s^2 - 3\omega_{16}^2\omega_7^3v_2^2 + 72\omega_{16}\omega_7v_2^2c_s^2 - 30\omega_{16}\omega_7^3v_4^2 + 6\omega_{16}\omega_7^3c_s^4 - 48\omega_{16}\omega_7c_s^4 - 24\omega_{16}\omega_7c_s^2 - 72\omega_{16}\omega_7^3v_2^2c_s^2 + 36\omega_7^3v_4^2 - 24\omega_{16}\omega_7^2c_s^4 + 72\omega_{16}\omega_7^2v_4^2 + 12\omega_{16}^2\omega_7^2v_2^2 - 12\omega_{16}^2\omega_7^2v_2^2c_s^2 - 8\omega_{16}^2\omega_7^2c_s^2 + 24\omega_{16}\omega_7c_s^4 - 36\omega_7^3v_2^2 + 12\omega_{16}^2\omega_7c_s^2 + 108\omega_7^3v_2^2c_s^2 - 12\omega_{16}^2\omega_7^2v_4^2 + 24\omega_{16}\omega_7^2c_s^4 - 36\omega_{16}^2\omega_7v_2^2c_s^2 + 24\omega_{16}\omega_7^2c_s^2 - 72\omega_{16}\omega_7^2v_2^2 + 6\omega_{16}^2\omega_7^3v_2^2c_s^2 + 72\omega_7^2v_2^2 + 30\omega_{16}\omega_7^2v_2^2 + 144\omega_{16}\omega_7^2v_2^2c_s^2 - 6\omega_{16}\omega_7^3c_s^2 - 3\omega_{16}^2\omega_7^3c_s^4 + 24\omega_{16}^2c_s^4 + 3\omega_{16}^2\omega_7^3v_4^2 \\
C_9 &= 36\omega_9\omega_6^2\omega_{13}c_s^2 + 6\omega_{18}\omega_6^2\omega_{22}\omega_{13}v_1^2 - \omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}^2 - 12\omega_{11}\omega_{18}\omega_9\omega_{22}\omega_{13}^2v_1^2 - 12\omega_{11}\omega_{18}\omega_9\omega_{22}\omega_{13}v_1^2 - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{13} - 36\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}^2c_s^2 + 12\omega_9\omega_6^2\omega_{13}v_1^2 + 6\omega_{18}\omega_9\omega_6^2\omega_{13} + 18\omega_{18}\omega_6^2\omega_{22}\omega_{13}c_s^2 - 36\omega_{11}\omega_{18}\omega_9\omega_{22}\omega_{13}^2c_s^2 + 12\omega_{11}\omega_6\omega_{22}\omega_{13} - 36\omega_{11}\omega_{18}\omega_9\omega_{22}\omega_{13}c_s^2 - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}^2v_1^2 - 18\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13} - 36\omega_{11}\omega_{18}\omega_9\omega_6\omega_{13}^2c_s^2 + 12\omega_{11}\omega_9\omega_6\omega_{13}^2v_1^2 - 3\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}v_1^2 - 6\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}v_1^2 + 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}c_s^2 + 36\omega_{11}\omega_6^2\omega_{22}\omega_{13}^2c_s^2 - 5\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13}v_1^2 - 6\omega_{18}\omega_6^2\omega_{22}\omega_{13}^2 - 12\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}v_1^2 + 6\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22} - 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}^2c_s^2 - 15\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13}^2c_s^2 + 12\omega_{11}\omega_6^2\omega_{22}\omega_{13}^2v_1^2 + 3\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13} - 12\omega_{11}\omega_9\omega_6\omega_{13}^2 + 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{13}v_1^2 + 3\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}^2c_s^2 - 36\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}c_s^2 + 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}^2c_s^2 + 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22} - 12\omega_{11}\omega_9\omega_6^2\omega_{13}v_1^2 - 6\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}^2 + 12\omega_{11}\omega_9\omega_6^2\omega_{13} - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}v_1^2 + 12\omega_{11}\omega_9\omega_6^2\omega_{13}^2 + 12\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}^2c_s^2 - 18\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13} - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}^2 - 12\omega_{11}\omega_9\omega_6^2\omega_{13}^2 - 36\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}^2c_s^2 + 6\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}^2 + 12\omega_{11}\omega_9\omega_6^2\omega_{13}^2 - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13} - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}^2 - 12\omega_{11}\omega_9\omega_6^2\omega_{13}^2 - 18\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}v_1^2 - 18\omega_{18}\omega_9\omega_6^2\omega_{13}^2c_s^2 - 12\omega_{11}\omega_6^2\omega_{22}\omega_{13}^2 + 54\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}^2c_s^2 - 12\omega_{11}\omega_6\omega_{22}\omega_{13}^2v_1^2 + 5\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13}^2 + 12\omega_{11}\omega_{18}\omega_9\omega_{22}\omega_{13}^2v_1^2 - 36\omega_6^2\omega_{22}\omega_{13}^2c_s^2 - 6\omega_{18}\omega_9\omega_6^2\omega_{13}^2v_1^2 + 54\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}\omega_{13}c_s^2 + 6\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13} \\
C_{10} &= -\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{22}\omega_{13}c_s^2 + 6\omega_{18}\omega_9\omega_6^3\omega_{13} - 12\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}c_s^2 - 12\omega_{11}\omega_6^3\omega_{22}\omega_{13} - 36\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13}v_1^2 - 12\omega_{11}\omega_{18}\omega_9\omega_{22}\omega_{13}c_s^2 + 5\omega_{11}\omega_{18}\omega_6^3\omega_{22}\omega_{13} - 6\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{22} - 3\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}v_1^2 - 36\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}v_1^2 - 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}c_s^2 + 12\omega_{11}\omega_{18}\omega_6\omega_{22}\omega_{13} + 12\omega_{11}\omega_9\omega_6^2\omega_{13}c_s^2 - 36\omega_6^3\omega_{22}\omega_{13}v_1^2 + 12\omega_9\omega_6^3\omega_{13}c_s^2 - 5\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13}c_s^2 + 36\omega_{11}\omega_9\omega_6^2\omega_{13}v_1^2 - 54\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}v_1^2 + 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22} - 12\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}c_s^2 - 12\omega_6^3\omega_{22}\omega_{13}c_s^2 + 12\omega_6^3\omega_{22}\omega_{13} + 36\omega_9\omega_6^3\omega_{13}v_1^2 + \omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}\omega_{13} + 6\omega_{11}\omega_{18}\omega_9\omega_6^3 - 18\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13} + 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}c_s^2 - 12\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{13}v_1^2 - 6\omega_{18}\omega_9\omega_6^3\omega_{13}c_s^2 - 6\omega_{11}\omega_{18}\omega_9\omega_6^3c_s^2 + 12\omega_{11}\omega_6^2\omega_{22}\omega_{13} - 36\omega_{11}\omega_6^2\omega_{22}\omega_{13}v_1^2 + 18\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13}c_s^2 - 6\omega_{18}\omega_6^3\omega_{22}\omega_{13} + 36\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}v_1^2 - 6\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{13} + 6\omega_{18}\omega_6^3\omega_{22}\omega_{13}c_s^2 - 12\omega_{11}\omega_{18}\omega_9\omega_6^2 - 18\omega_{18}\omega_9\omega_6^3\omega_{13}v_1^2 - 18\omega_{11}\omega_{18}\omega_9\omega_6^3v_1^2 + 12\omega_{11}\omega_9\omega_6^3\omega_{13} + 54\omega_{11}\omega_{18}\omega_6^2\omega_{22}\omega_{13}v_1^2 - 12\omega_{11}\omega_6^2\omega_{22}\omega_{13}c_s^2 +
\end{aligned}$$

$$\begin{aligned}
C_{25} = & -306\omega_{11}\omega_{18}\omega_6^3v_3^2c_s^2 + 36\omega_{11}\omega_{18}\omega_6^3v_3^2 + 36\omega_{11}\omega_{18}\omega_6v_3^2c_s^2 - 5\omega_{11}^3\omega_{18}^2\omega_6^2c_s^2 - 18\omega_{11}^3\omega_{18}\omega_6^2c_s^4 - 108\omega_{11}^2\omega_6^3v_3^2c_s^2 - 90\omega_{11}\omega_{18}\omega_6^3v_3^4 + 36\omega_{11}^2\omega_{18}\omega_6^2v_3^2c_s^2 - \\
& 39\omega_{11}^3\omega_{18}\omega_6^3v_3^4 + 12\omega_{18}^2\omega_6^3c_s^4 - 6\omega_{11}^2\omega_{18}\omega_6^3c_s^4 - 12\omega_{11}^3\omega_{18}\omega_6c_s^2 + 36\omega_{11}^3\omega_6^3v_3^4 - 12\omega_{11}\omega_{18}^2\omega_6^2c_s^4 + 60\omega_{11}^2\omega_{18}\omega_6^3v_3^2c_s^2 - 24\omega_{11}^2\omega_{18}\omega_6c_s^4 - \omega_{11}^2\omega_{18}\omega_6^3c_s^2 - \\
& 4\omega_{11}^3\omega_{18}\omega_6^3v_3^2 + 36\omega_{11}^2\omega_6^3v_3^2 + 6\omega_{11}^3\omega_{18}\omega_6^3c_s^4 + 72\omega_{11}^2\omega_{18}\omega_6^3v_3^4 + 72\omega_{18}^2\omega_6^3v_3^4 - 19\omega_{11}^2\omega_{18}\omega_6^3v_3^2 - 3\omega_{11}^3\omega_{18}\omega_6^2v_3^2c_s^2 - 6\omega_{11}^2\omega_{18}\omega_6^2c_s^2 + 6\omega_{11}^3\omega_{18}\omega_6^2v_3^2 - \\
& 12\omega_{11}^2\omega_{18}\omega_6^3c_s^2 - 99\omega_{11}^3\omega_{18}\omega_6^3v_3^2c_s^2 + 36\omega_{11}^3\omega_{18}\omega_6^2v_3^4 - 36\omega_{11}^3\omega_6^2v_3^4 + 108\omega_{11}^2\omega_6^3v_3^2c_s^2 + 12\omega_{11}^2\omega_{18}\omega_6^2c_s^4 + 19\omega_{11}^2\omega_{18}\omega_6^3v_3^4 - \omega_{11}^3\omega_{18}\omega_6^3c_s^4 + \\
& 18\omega_{11}^2\omega_{18}\omega_6^3v_3^2c_s^2 - 36\omega_{11}^2\omega_6^3v_3^4 - 18\omega_{11}^3\omega_{18}\omega_6^2v_3^2c_s^2 - 6\omega_{11}^3\omega_{18}\omega_6^3c_s^2 - 108\omega_{11}\omega_{18}\omega_6^3v_3^2c_s^2 - 72\omega_{18}^2\omega_6^3v_3^2 - 72\omega_{11}^2\omega_{18}\omega_6^3v_3^2 + 12\omega_{11}\omega_{18}\omega_6^3c_s^2 + \\
& 198\omega_{11}^2\omega_{18}\omega_6^3v_3^2c_s^2 + 252\omega_{18}^2\omega_6^3v_3^2c_s^2 - 36\omega_{11}^3\omega_{18}\omega_6^2v_3^2 + 12\omega_{11}^2\omega_{18}^2c_s^4 + 36\omega_{11}^2\omega_6^2v_3^2 - 12\omega_{11}^2\omega_{18}\omega_6^2c_s^2 + 6\omega_{11}^2\omega_{18}\omega_6^2c_s^4 - 36\omega_{11}\omega_{18}\omega_6^2v_3^2c_s^2 - \\
& 6\omega_{11}^3\omega_{18}\omega_6^2v_3^4 + 18\omega_{11}^3\omega_{18}\omega_6^2c_s^2 + 54\omega_{11}^3\omega_{18}\omega_6^2v_3^2c_s^2 + 90\omega_{11}\omega_{18}\omega_6^3v_3^2 - 108\omega_{11}^2\omega_6^2v_3^2c_s^2 - 36\omega_{11}\omega_{18}\omega_6^3v_3^4 + 13\omega_{11}^2\omega_{18}\omega_6^2c_s^4 + \omega_{11}^2\omega_{18}\omega_6^3c_s^4 + \\
& 6\omega_{11}^3\omega_{18}\omega_6c_s^2 + 12\omega_{11}^2\omega_{18}\omega_6^3v_3^2c_s^2 + 4\omega_{11}^3\omega_{18}\omega_6^2v_3^4 + 39\omega_{11}^3\omega_{18}\omega_6^3v_3^2 + 12\omega_{11}^2\omega_{18}\omega_6^2c_s^4 + 6\omega_{11}^2\omega_{18}\omega_6^3c_s^2 - 12\omega_{18}^2\omega_6^3c_s^2 - 36\omega_{11}^3\omega_6^3v_3^2 + 12\omega_{11}\omega_{18}\omega_6^2c_s^2 \\
C_{26} = & 72\omega_{11}^2\omega_{19}\omega_7^3v_3^4 + 72\omega_{19}^2\omega_7^3v_3^4 - 108\omega_{11}\omega_{19}\omega_7^3v_3^2c_s^2 + 6\omega_{11}^3\omega_{19}\omega_7^3c_s^4 - 18\omega_{11}^3\omega_{19}^2\omega_7^2v_3^2c_s^2 + 18\omega_{11}^2\omega_{19}^2\omega_7^2v_3^2c_s^2 - 19\omega_{11}^2\omega_{19}\omega_7^3v_3^2 + 6\omega_{11}^3\omega_{19}\omega_7^2v_3^2 - \\
& 36\omega_{11}\omega_{19}^2\omega_7^2v_3^2c_s^2 - 6\omega_{11}^2\omega_{19}\omega_7^2c_s^2 - 36\omega_{11}^3\omega_7^3v_3^2 + 12\omega_{11}^2\omega_{19}\omega_7^2c_s^4 + 198\omega_{11}^2\omega_{19}\omega_7^2v_3^2c_s^2 + 252\omega_{19}^2\omega_7^2v_3^2c_s^2 + 36\omega_{11}^3\omega_{19}\omega_7^2v_3^2 - 12\omega_{11}\omega_{19}\omega_7^3c_s^4 - \\
& 5\omega_{11}^3\omega_{19}\omega_7^2c_s^2 - 108\omega_{11}^2\omega_7^2v_3^2c_s^2 + 36\omega_{11}\omega_{19}\omega_7^3v_3^2 - 36\omega_{11}^2\omega_7^3v_3^4 - 90\omega_{11}\omega_{19}^2\omega_7^3v_3^4 + 54\omega_{11}^3\omega_{19}\omega_7^2v_3^2c_s^2 - 18\omega_{11}^3\omega_{19}\omega_7^2c_s^4 - 12\omega_{11}\omega_{19}^2\omega_7^2c_s^4 + \\
& 12\omega_{11}^3\omega_{19}^2c_s^4 + 12\omega_{19}^2\omega_7^2c_s^4 - 6\omega_{11}^2\omega_{19}\omega_7^3c_s^4 + 36\omega_{11}^3\omega_7^2v_3^2 - 12\omega_{11}^3\omega_{19}\omega_7^2c_s^2 - 39\omega_{11}^3\omega_{19}\omega_7^2v_3^4 - 4\omega_{11}^3\omega_{19}\omega_7^3v_3^2 - 24\omega_{11}^3\omega_{19}\omega_7^2c_s^4 + 12\omega_{11}^3\omega_{19}\omega_7^2v_3^2c_s^2 - \\
& \omega_{11}^2\omega_{19}\omega_7^3c_s^2 + 36\omega_{11}^2\omega_{19}\omega_7^2v_3^2c_s^2 + 90\omega_{11}\omega_{19}^2\omega_7^3v_3^2 + 36\omega_{11}^2\omega_7^3v_3^2 + 18\omega_{11}^3\omega_{19}\omega_7^2c_s^2 + 13\omega_{11}^3\omega_{19}\omega_7^2c_s^4 + 36\omega_{11}^3\omega_{19}\omega_7^2v_3^2c_s^2 - 36\omega_{11}\omega_{19}\omega_7^3v_3^4 - \\
& 108\omega_{11}^2\omega_7^2v_3^2c_s^2 - 306\omega_{11}\omega_{19}\omega_7^3v_3^2c_s^2 + 4\omega_{11}^3\omega_{19}\omega_7^3v_3^4 + \omega_{11}^2\omega_{19}\omega_7^3c_s^4 + 6\omega_{11}^3\omega_{19}\omega_7^2c_s^2 + 60\omega_{11}^2\omega_{19}\omega_7^3v_3^2c_s^2 + 12\omega_{11}\omega_{19}\omega_7^2c_s^2 + 12\omega_{11}^3\omega_{19}\omega_7^2c_s^4 - \\
& 36\omega_{11}^3\omega_7^2v_3^4 + 6\omega_{11}^2\omega_{19}\omega_7^2c_s^2 - 12\omega_{19}^2\omega_7^2c_s^2 + 39\omega_{11}^3\omega_{19}\omega_7^3v_3^2 - 3\omega_{11}^3\omega_{19}\omega_7^2v_3^2c_s^2 - \omega_{11}^3\omega_{19}\omega_7^3c_s^4 + 19\omega_{11}^2\omega_{19}\omega_7^3v_3^4 - 72\omega_{19}^2\omega_7^3v_3^2 - 72\omega_{11}^2\omega_{19}\omega_7^3v_3^2 - \\
& 6\omega_{11}^3\omega_{19}\omega_7^2c_s^2 - 12\omega_{11}^2\omega_{19}\omega_7^2c_s^2 + 36\omega_{11}^3\omega_7^3v_3^4 - 36\omega_{11}^3\omega_{19}\omega_7^2v_3^2 + 12\omega_{11}\omega_{19}\omega_7^2c_s^2 - 99\omega_{11}^3\omega_{19}\omega_7^3v_3^2c_s^2 + 108\omega_{11}^3\omega_7^3v_3^2c_s^2 - 6\omega_{11}^3\omega_{19}\omega_7^2v_3^4 + 6\omega_{11}^2\omega_{19}\omega_7^2c_s^4 \\
C_{27} = & 12 - 1008\omega_{11}v_3^2c_s^2 - 18\omega_{11} + 82\omega_{11}^2c_s^4 - 132c_s^2 - 9\omega_{11}^3v_3^4 + 198\omega_{11}c_s^2 - 5\omega_{11}^3c_s^4 + 234\omega_{11}v_3^2 - 34\omega_{11}^2v_3^2c_s^2 - 156v_3^2 + 90\omega_{11}^2v_3^4 + 6\omega_{11}^3c_s^2 - \\
& 216\omega_{11}v_3^4 + 672v_3^2c_s^2 + 144v_3^4 - 98\omega_{11}^2v_3^2 - 78\omega_{11}^2c_s^2 + 404\omega_{11}^3v_3^2c_s^2 + 8\omega_{11}^4 + 144c_s^4 - \omega_{11}^3 + 10\omega_{11}^3v_3^2 - 216\omega_{11}c_s^4 \\
C_{28} = & 12 - 648\omega_{11}v_3^2c_s^2 - 18\omega_{11} + 14\omega_{11}^2c_s^4 - 36c_s^2 - 29\omega_{11}^3v_3^4 + 54\omega_{11}c_s^2 - \omega_{11}^3c_s^4 + 378\omega_{11}v_3^2 - 18\omega_{11}^2v_3^2c_s^2 - 252v_3^2 + 310\omega_{11}^2v_3^4 + 2\omega_{11}^3c_s^2 - \\
& 756\omega_{11}v_3^4 + 432v_3^2c_s^2 + 504v_3^4 - 154\omega_{11}^2v_3^2 - 22\omega_{11}^2c_s^2 + 252\omega_{11}^3v_3^2c_s^2 + 8\omega_{11}^4 + 24c_s^4 - \omega_{11}^3 + 14\omega_{11}^3v_3^2 - 36\omega_{11}c_s^4
\end{aligned}$$

2.6 CuLBM1

2.6.1 Definitions

Based on [2], collision operator \mathcal{C} :

$$\mathcal{C}(f) = \mathbf{M}^{-1}\mathbf{G}^{-1}\left(\mathbf{S}\left(\gamma^{(eq)} - \mathbf{G}(\mathbf{M}f)\right)\right),$$

where

$$\mathbf{S} = \text{diag}(0, 0, 0, 0, \omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7, \omega_8, \omega_9, \omega_{10}, \omega_{11}, \omega_{12}, \omega_{13}, \omega_{14}, \omega_{15}, \omega_{16}, \omega_{17}, \omega_{18}, \omega_{19}, \omega_{20}, \omega_{21}, \omega_{22}, \omega_{23}),$$

$$\omega_1, \omega_2, \dots, \omega_{10} \in (0, 2).$$

The nonlinear operator \mathbf{G} (with its inverse \mathbf{G}^{-1}) transforms the raw moment vector $\boldsymbol{\mu}$ defined by matrix \mathbf{M} to the cumulant vector

$$\boldsymbol{\gamma} = \mathbf{G}(\boldsymbol{\mu}) = (\gamma_{(0,0,0)}, \gamma_{(1,0,0)}, \gamma_{(0,1,0)}, \dots, \gamma_{(2,2,2)})^T$$

as:

$$\gamma_{(0,0,0)} = m_{(0,0,0)}$$

$$\gamma_{(1,0,0)} = m_{(1,0,0)} - v_1 m_{(0,0,0)}$$

$$\gamma_{(0,1,0)} = m_{(0,1,0)} - v_2 m_{(0,0,0)}$$

$$\gamma_{(0,0,1)} = m_{(0,0,1)} - v_3 m_{(0,0,0)}$$

$$\gamma_{(1,1,0)} = m_{(1,1,0)} - v_1 m_{(0,1,0)} - v_2 m_{(1,0,0)} - v_1 v_2 m_{(0,0,0)}$$

$$\gamma_{(1,0,1)} = m_{(1,0,1)} - v_1 m_{(0,0,1)} - v_3 m_{(1,0,0)} - v_1 v_3 m_{(0,0,0)}$$

$$\gamma_{(0,1,1)} = m_{(0,1,1)} - v_3 m_{(0,1,0)} - v_2 m_{(0,0,1)} - v_3 v_2 m_{(0,0,0)}$$

$$\gamma(2,0,0) = m_{(2,0,0)} - 2v_1m_{(1,0,0)} + v_1v_1m_{(0,0,0)}$$

$$\gamma(0,2,0) = m_{(0,2,0)} - 2v_2m_{(0,1,0)} + v_2v_2m_{(0,0,0)}$$

$$\gamma(0,0,2) = m_{(0,0,2)} - 2v_3m_{(0,0,1)} + v_3v_3m_{(0,0,0)}$$

$$\gamma(1,2,0) = m_{(1,2,0)} - 2v_2m_{(1,1,0)} + v_2v_2m_{(1,0,0)} - v_1m_{(0,2,0)} + 2v_1v_2m_{(0,1,0)} - v_1v_2v_2m_{(0,0,0)}$$

$$\gamma(1,0,2) = m_{(1,0,2)} - 2v_3m_{(1,0,1)} + v_3v_3m_{(1,0,0)} - v_1m_{(0,0,2)} + 2v_1v_3m_{(0,0,1)} - v_1v_3v_3m_{(0,0,0)}$$

$$\gamma(0,1,2) = m_{(0,1,2)} - 2v_3m_{(0,1,1)} + v_3v_3m_{(0,1,0)} - v_2m_{(0,0,2)} + 2v_2v_3m_{(0,0,1)} - v_2v_3v_3m_{(0,0,0)}$$

$$\gamma(2,1,0) = m_{(2,1,0)} - 2v_1m_{(1,1,0)} + v_1v_1m_{(0,1,0)} - v_2m_{(2,0,0)} + 2v_1v_2m_{(1,0,0)} - v_1v_1v_2m_{(0,0,0)}$$

$$\gamma(2,0,1) = m_{(2,0,1)} - 2v_1m_{(1,0,1)} + v_1v_1m_{(0,0,1)} - v_3m_{(2,0,0)} + 2v_1v_3m_{(1,0,0)} - v_1v_1v_3m_{(0,0,0)}$$

$$\gamma(0,2,1) = m_{(0,2,1)} - 2v_2m_{(0,1,1)} + v_2v_2m_{(0,0,1)} - v_3m_{(0,2,0)} + 2v_2v_3m_{(0,1,0)} - v_2v_2v_3m_{(0,0,0)}$$

$$\gamma(1,1,1) = m_{(1,1,1)} - v_3m_{(1,1,0)} - v_2m_{(1,0,1)} + v_2v_3m_{(1,0,0)} - v_1m_{(0,1,1)} + v_1v_3m_{(0,1,0)} + v_1v_2m_{(0,0,1)} - v_1v_2v_3m_{(0,0,0)}$$

$$\begin{aligned} \gamma(2,2,0) = & -2v_2m_{(2,1,0)} - 2m_{(0,0,0)}v_1^2v_2^2 - 4m_{(1,0,0)}v_1v_2^2 - \frac{2m_{(1,0,0)}^2v_2^2}{m_{(0,0,0)}} - 4m_{(0,1,0)}v_1^2v_2 + 8m_{(1,1,0)}v_1v_2 - \\ & \frac{8m_{(0,1,0)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} - \frac{2m_{(0,1,0)}^2v_1^2}{m_{(0,0,0)}} - 2m_{(1,2,0)}v_1 + \frac{4m_{(0,1,0)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \\ & \frac{2m_{(0,2,0)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,2,0)} - \frac{m_{(0,2,0)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{2m_{(1,1,0)}^2}{m_{(0,0,0)}} \end{aligned}$$

$$\begin{aligned} \gamma(2,0,2) = & -2v_3m_{(2,0,1)} - 2m_{(0,0,0)}v_1^2v_3^2 - 4m_{(1,0,0)}v_1v_3^2 - \frac{2m_{(1,0,0)}^2v_3^2}{m_{(0,0,0)}} - 4m_{(0,0,1)}v_1^2v_3 + 8m_{(1,0,1)}v_1v_3 - \\ & \frac{8m_{(0,0,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} + \frac{2m_{(0,0,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}} - \frac{2m_{(0,0,1)}^2v_1^2}{m_{(0,0,0)}} - 2m_{(1,0,2)}v_1 + \frac{4m_{(0,0,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \\ & \frac{2m_{(0,0,2)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,0,2)} - \frac{m_{(0,0,2)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,1)}^2}{m_{(0,0,0)}} \end{aligned}$$

$$\begin{aligned} \gamma(0,2,2) = & -2v_3m_{(0,2,1)} - 2m_{(0,0,0)}v_2^2v_3^2 - 4m_{(0,1,0)}v_2v_3^2 - \frac{2m_{(0,1,0)}^2v_3^2}{m_{(0,0,0)}} - 4m_{(0,0,1)}v_2^2v_3 + 8m_{(0,1,1)}v_2v_3 - \\ & \frac{8m_{(0,0,1)}m_{(0,1,0)}v_2v_3}{m_{(0,0,0)}} + \frac{2m_{(0,0,1)}m_{(0,2,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(0,1,1)}v_3}{m_{(0,0,0)}} - \frac{2m_{(0,0,1)}^2v_2^2}{m_{(0,0,0)}} - 2m_{(0,1,2)}v_2 + \frac{4m_{(0,0,1)}m_{(0,1,1)}v_2}{m_{(0,0,0)}} + \\ & \frac{2m_{(0,0,2)}m_{(0,1,0)}v_2}{m_{(0,0,0)}} + m_{(0,2,2)} - \frac{m_{(0,0,2)}m_{(0,2,0)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,1)}^2}{m_{(0,0,0)}} \end{aligned}$$

$$\begin{aligned} \gamma(2,1,1) = & -8m_{(1,0,0)}v_1v_2v_3 + 2m_{(2,0,0)}v_2v_3 - \frac{2m_{(1,0,0)}^2v_2v_3}{m_{(0,0,0)}} - 2m_{(0,1,0)}v_1^2v_3 + 4m_{(1,1,0)}v_1v_3 - \frac{4m_{(0,1,0)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} - \\ & m_{(2,1,0)}v_3 + \frac{m_{(0,1,0)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} - 2m_{(0,0,1)}v_1^2v_2 + 4m_{(1,0,1)}v_1v_2 - \frac{4m_{(0,0,1)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} - m_{(2,0,1)}v_2 + \\ & \frac{m_{(0,0,1)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} - \frac{2m_{(0,0,1)}m_{(0,1,0)}v_1^2}{m_{(0,0,0)}} - 2m_{(1,1,1)}v_1 + \frac{2m_{(0,0,1)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \\ & \frac{2m_{(0,1,1)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,1,1)} - \frac{m_{(0,1,1)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,1)}m_{(1,1,0)}}{m_{(0,0,0)}} \end{aligned}$$

$$\begin{aligned} \gamma(1,2,1) = & -2m_{(1,0,0)}v_2^2v_3 - 8m_{(0,1,0)}v_1v_2v_3 + 4m_{(1,1,0)}v_2v_3 - \frac{4m_{(0,1,0)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}} + 2m_{(0,2,0)}v_1v_3 - \\ & \frac{2m_{(0,1,0)}^2v_1v_3}{m_{(0,0,0)}} - m_{(1,2,0)}v_3 + \frac{2m_{(0,1,0)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} + \frac{m_{(0,2,0)}m_{(1,0,0)}v_3}{m_{(0,0,0)}} - 2m_{(0,0,1)}v_1v_2^2 - \frac{2m_{(0,0,1)}m_{(1,0,0)}v_2^2}{m_{(0,0,0)}} + 4m_{(0,1,1)}v_1v_2 - \\ & \frac{4m_{(0,0,1)}m_{(0,1,0)}v_1v_2}{m_{(0,0,0)}} - 2m_{(1,1,1)}v_2 + \frac{2m_{(0,0,1)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,1)}m_{(1,0,0)}v_2}{m_{(0,0,0)}} - m_{(0,2,1)}v_1 + \\ & \frac{m_{(0,0,1)}m_{(0,2,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(0,1,1)}v_1}{m_{(0,0,0)}} + m_{(1,2,1)} - \frac{2m_{(0,1,1)}m_{(1,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(1,0,1)}}{m_{(0,0,0)}} \end{aligned}$$

$$\begin{aligned}
\gamma_{(1,1,2)} = & -2m_{(1,0,0)}v_2v_3^2 - 2m_{(0,1,0)}v_1v_3^2 - \frac{2m_{(0,1,0)}m_{(1,0,0)}v_3^2}{m_{(0,0,0)}} - 8m_{(0,0,1)}v_1v_2v_3 + 4m_{(1,0,1)}v_2v_3 - \frac{4m_{(0,0,1)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}} + \\
& 4m_{(0,1,1)}v_1v_3 - \frac{4m_{(0,0,1)}m_{(0,1,0)}v_1v_3}{m_{(0,0,0)}} - 2m_{(1,1,1)}v_3 + \frac{2m_{(0,0,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,1,1)}m_{(1,0,0)}v_3}{m_{(0,0,0)}} + \\
& 2m_{(0,0,2)}v_1v_2 - \frac{2m_{(0,0,1)}^2v_1v_2}{m_{(0,0,0)}} \\
& - m_{(1,0,2)}v_2 + \frac{2m_{(0,0,1)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} + \frac{m_{(0,0,2)}m_{(1,0,0)}v_2}{m_{(0,0,0)}} - m_{(0,1,2)}v_1 + \frac{2m_{(0,0,1)}m_{(0,1,1)}v_1}{m_{(0,0,0)}} + \frac{m_{(0,0,2)}m_{(0,1,0)}v_1}{m_{(0,0,0)}} + m_{(1,1,2)} - \\
& \frac{m_{(0,0,2)}m_{(1,1,0)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,1)}m_{(1,0,1)}}{m_{(0,0,0)}} \\
\gamma_{(1,2,2)} = & -m_{(0,0,0)}v_1^2v_2^2v_3^2 - 6m_{(0,0,0)}v_1v_2^2v_3^2 - m_{(1,0,0)}v_2^2v_3^2 + 2m_{(0,1,0)}v_1v_2v_3^2 - 2m_{(1,1,0)}v_2v_3^2 + \\
& \frac{12m_{(0,1,0)}m_{(1,0,0)}v_2v_3^2}{m_{(0,0,0)}} - m_{(0,2,0)}v_1v_3^2 + \frac{6m_{(0,1,0)}^2v_1v_3^2}{m_{(0,0,0)}} - \frac{6m_{(0,1,0)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} - \frac{3m_{(0,2,0)}m_{(1,0,0)}v_3^2}{m_{(0,0,0)}} + 2m_{(0,0,1)}v_1v_2^2v_3 - \\
& 2m_{(1,0,1)}v_2^2v_3 + \frac{12m_{(0,0,1)}m_{(1,0,0)}v_2^2v_3}{m_{(0,0,0)}} - 12m_{(0,1,1)}v_1v_2v_3 + \frac{24m_{(0,0,1)}m_{(0,1,0)}v_1v_2v_3}{m_{(0,0,0)}} + 8m_{(1,1,1)}v_2v_3 - \frac{12m_{(0,0,1)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}} - \\
& \frac{12m_{(0,1,0)}m_{(1,0,1)}v_2v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,1)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}} + 4m_{(0,2,1)}v_1v_3 - \frac{6m_{(0,0,1)}m_{(0,2,0)}v_1v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,0)}m_{(0,1,1)}v_1v_3}{m_{(0,0,0)}} - 2m_{(1,2,1)}v_3 + \\
& \frac{2m_{(0,0,1)}m_{(1,2,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(1,1,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,2,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,2,1)}m_{(1,0,0)}v_3}{m_{(0,0,0)}} - m_{(0,0,2)}v_1v_2^2 + \\
& \frac{6m_{(0,0,1)}^2v_1v_2^2}{m_{(0,0,0)}} - \frac{6m_{(0,0,1)}m_{(1,0,1)}v_2^2}{m_{(0,0,0)}} - \frac{3m_{(0,0,2)}m_{(1,0,0)}v_2^2}{m_{(0,0,0)}} + 4m_{(0,1,2)}v_1v_2 - \frac{12m_{(0,0,1)}m_{(0,1,1)}v_1v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,2)}m_{(0,1,0)}v_1v_2}{m_{(0,0,0)}} - \\
& 2m_{(1,1,2)}v_2 + \frac{4m_{(0,0,1)}m_{(1,1,1)}v_2}{m_{(0,0,0)}} + \frac{4m_{(0,0,2)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,2)}v_2}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,2)}m_{(1,0,0)}v_2}{m_{(0,0,0)}} - \\
& m_{(0,2,2)}v_1 + \frac{2m_{(0,0,1)}m_{(0,2,1)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,0,2)}m_{(0,2,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(0,1,2)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,1,1)}^2v_1}{m_{(0,0,0)}} + m_{(1,2,2)} - \frac{m_{(0,0,2)}m_{(1,2,0)}}{m_{(0,0,0)}} - \\
& \frac{4m_{(0,1,1)}m_{(1,1,1)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,2)}m_{(1,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(1,0,2)}}{m_{(0,0,0)}} - \frac{2m_{(0,2,1)}m_{(1,0,1)}}{m_{(0,0,0)}} \\
\gamma_{(2,1,2)} = & -m_{(0,0,0)}v_1^2v_2^2v_3^2 - 6m_{(0,0,0)}v_1^2v_2v_3^2 + 2m_{(1,0,0)}v_1v_2v_3^2 - m_{(2,0,0)}v_2v_3^2 + \frac{6m_{(1,0,0)}^2v_2v_3^2}{m_{(0,0,0)}} - \\
& m_{(0,1,0)}v_1^2v_3^2 - 2m_{(1,1,0)}v_1v_3^2 + \frac{12m_{(0,1,0)}m_{(1,0,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{3m_{(0,1,0)}m_{(2,0,0)}v_3^2}{m_{(0,0,0)}} - \frac{6m_{(1,0,0)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} + 2m_{(0,0,1)}v_1^2v_2v_3 - \\
& 12m_{(1,0,1)}v_1v_2v_3 + \frac{24m_{(0,0,1)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}} + 4m_{(2,0,1)}v_2v_3 - \frac{6m_{(0,0,1)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}} - \frac{12m_{(1,0,0)}m_{(1,0,1)}v_2v_3}{m_{(0,0,0)}} - 2m_{(0,1,1)}v_1^2v_3 + \\
& \frac{12m_{(0,0,1)}m_{(0,1,0)}v_1^2v_3}{m_{(0,0,0)}} + 8m_{(1,1,1)}v_1v_3 - \frac{12m_{(0,0,1)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,0)}m_{(1,0,1)}v_1v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} - 2m_{(2,1,1)}v_3 + \\
& \frac{2m_{(0,0,1)}m_{(2,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,1)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,1,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(1,0,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} - m_{(0,0,2)}v_1^2v_2 + \\
& \frac{6m_{(0,0,1)}^2v_1^2v_2}{m_{(0,0,0)}} + 4m_{(1,0,2)}v_1v_2 - \frac{12m_{(0,0,1)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,2)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} - m_{(2,0,2)}v_2 + \frac{2m_{(0,0,1)}m_{(2,0,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,0,2)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,0,2)}v_2}{m_{(0,0,0)}} + \frac{4m_{(1,0,1)}^2v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,1)}m_{(0,1,1)}v_1^2}{m_{(0,0,0)}} - \frac{3m_{(0,0,2)}m_{(0,1,0)}v_1^2}{m_{(0,0,0)}} - 2m_{(1,1,2)}v_1 + \\
& \frac{4m_{(0,0,1)}m_{(1,1,1)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,0,2)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,2)}v_1}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,2)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,1,2)} - \\
& \frac{m_{(0,0,2)}m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,1)}m_{(2,0,1)}}{m_{(0,0,0)}} - \frac{m_{(0,1,2)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{4m_{(1,0,1)}m_{(1,1,1)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,2)}m_{(1,1,0)}}{m_{(0,0,0)}} \\
\gamma_{(2,2,1)} = & -m_{(0,0,0)}v_1^2v_2^2v_3^2 - 6m_{(0,0,0)}v_1^2v_2^2v_3 + 2m_{(1,0,0)}v_1v_2^2v_3 - m_{(2,0,0)}v_2^2v_3 + \frac{6m_{(1,0,0)}^2v_2^2v_3}{m_{(0,0,0)}} + 2m_{(0,1,0)}v_1^2v_2v_3 - \\
& 12m_{(1,1,0)}v_1v_2v_3 \\
& + \frac{24m_{(0,1,0)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}} + 4m_{(2,1,0)}v_2v_3 - \frac{6m_{(0,1,0)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}} - \frac{12m_{(1,0,0)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}} - m_{(0,2,0)}v_1^2v_3 + \frac{6m_{(0,1,0)}^2v_1^2v_3}{m_{(0,0,0)}} + \\
& 4m_{(1,2,0)}v_1v_3 \\
& - \frac{12m_{(0,1,0)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}} - \frac{6m_{(0,2,0)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} - m_{(2,2,0)}v_3 + \frac{2m_{(0,1,0)}m_{(2,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,2,0)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,2,0)}v_3}{m_{(0,0,0)}} + \\
& \frac{4m_{(1,1,0)}^2v_3}{m_{(0,0,0)}} - m_{(0,0,1)}v_1^2v_2^2 - 2m_{(1,0,1)}v_1v_2^2 + \frac{12m_{(0,0,1)}m_{(1,0,0)}v_1v_2^2}{m_{(0,0,0)}} - \frac{3m_{(0,0,1)}m_{(2,0,0)}v_2^2}{m_{(0,0,0)}} - \frac{6m_{(1,0,0)}m_{(1,0,1)}v_2^2}{m_{(0,0,0)}} - \\
& 2m_{(0,1,1)}v_1^2v_2 + \frac{12m_{(0,0,1)}m_{(0,1,0)}v_1^2v_2}{m_{(0,0,0)}} + 8m_{(1,1,1)}v_1v_2 - \frac{12m_{(0,0,1)}m_{(1,1,0)}v_1v_2}{m_{(0,0,0)}} - \frac{12m_{(0,1,0)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}} - \\
& \frac{12m_{(0,1,1)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} - 2m_{(2,1,1)}v_2 + \frac{2m_{(0,0,1)}m_{(2,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,1)}v_2}{m_{(0,0,0)}} + \frac{4m_{(0,1,1)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,1,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{8m_{(1,0,1)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} - \frac{3m_{(0,0,1)}m_{(0,2,0)}v_1^2}{m_{(0,0,0)}} - \frac{6m_{(0,1,0)}m_{(0,1,1)}v_1^2}{m_{(0,0,0)}} - 2m_{(1,2,1)}v_1 + \frac{2m_{(0,0,1)}m_{(1,2,0)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(1,1,1)}v_1}{m_{(0,0,0)}} +
\end{aligned}$$

$$\begin{aligned}
& \frac{8m_{(0,1,1)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,2,0)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,2,1)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,2,1)} - \frac{2m_{(0,1,1)}m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(2,0,1)}}{m_{(0,0,0)}} - \frac{m_{(0,2,1)}m_{(2,0,0)}}{m_{(0,0,0)}} - \\
& \frac{2m_{(1,0,1)}m_{(1,2,0)}}{m_{(0,0,0)}} - \frac{4m_{(1,1,0)}m_{(1,1,1)}}{m_{(0,0,0)}} \\
\gamma(2,2,2) = & 2v_2^2v_3m_{(2,0,1)} - \frac{4m_{(0,1,0)}v_2v_3m_{(2,0,1)}}{m_{(0,0,0)}} + \frac{2m_{(0,2,0)}v_3m_{(2,0,1)}}{m_{(0,0,0)}} + 2v_1^2v_3m_{(0,2,1)} - \frac{4m_{(1,0,0)}v_1v_3m_{(0,2,1)}}{m_{(0,0,0)}} + \\
& \frac{2m_{(2,0,0)}v_3m_{(0,2,1)}}{m_{(0,0,0)}} - 4m_{(0,0,0)}v_1v_2v_3^4 - 4m_{(1,0,0)}v_2v_3^4 - 4m_{(0,1,0)}v_1v_3^4 + 4m_{(1,1,0)}v_3^4 + 16m_{(0,0,1)}v_1v_2v_3^3 + \\
& \frac{16m_{(0,0,1)}m_{(1,0,0)}v_2v_3^3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}v_1v_3^3}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(1,1,0)}v_3^3}{m_{(0,0,0)}} + 2v_2m_{(2,1,0)}v_3^2 - 7m_{(0,0,0)}v_1^2v_2^2v_3^2 + v_1^2v_2^2v_3^2 - \\
& 20m_{(1,0,0)}v_1v_2^2v_3^2 + 4m_{(2,0,0)}v_2^2v_3^2 - \frac{26m_{(1,0,0)}^2v_2^2v_3^2}{m_{(0,0,0)}} - 20m_{(0,1,0)}v_1^2v_2v_3^2 + 16m_{(1,1,0)}v_1v_2v_3^2 - \frac{128m_{(0,1,0)}m_{(1,0,0)}v_1v_2v_3^2}{m_{(0,0,0)}} - \\
& 8m_{(0,0,2)}v_1v_2v_3^2 - \frac{16m_{(0,0,1)}^2v_1v_2v_3^2}{m_{(0,0,0)}} - 4m_{(2,1,0)}v_2v_3^2 + \frac{18m_{(0,1,0)}m_{(2,0,0)}v_2v_3^2}{m_{(0,0,0)}} + \frac{44m_{(1,0,0)}m_{(1,1,0)}v_2v_3^2}{m_{(0,0,0)}} - \\
& \frac{24m_{(0,1,0)}m_{(1,0,0)}^2v_2v_3^2}{m_{(0,0,0)}} - \frac{8m_{(0,0,2)}m_{(1,0,0)}v_2v_3^2}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}^2m_{(1,0,0)}v_2v_3^2}{m_{(0,0,0)}} + 4m_{(0,2,0)}v_1^2v_3^2 - \frac{26m_{(0,1,0)}^2v_1^2v_3^2}{m_{(0,0,0)}} - 2m_{(1,2,0)}v_1v_3^2 + \\
& \frac{44m_{(0,1,0)}m_{(1,1,0)}v_1v_3^2}{m_{(0,0,0)}} + \frac{18m_{(0,0,1)}^2m_{(1,0,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{24m_{(0,1,0)}^2m_{(1,0,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{8m_{(0,0,2)}m_{(0,1,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}^2m_{(0,1,0)}v_1v_3^2}{m_{(0,0,0)}} - \\
& \frac{6m_{(0,1,0)}m_{(2,1,0)}v_3^2}{m_{(0,0,0)}} - \frac{2m_{(0,2,0)}m_{(2,0,0)}v_3^2}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}^2m_{(2,0,0)}v_3^2}{m_{(0,0,0)}} - \frac{6m_{(1,0,0)}m_{(1,2,0)}v_3^2}{m_{(0,0,0)}} - \frac{8m_{(1,1,0)}^2v_3^2}{m_{(0,0,0)}} + \frac{16m_{(0,1,0)}m_{(1,0,0)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} + \\
& \frac{8m_{(0,0,2)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}^2m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} + \frac{4m_{(0,2,0)}m_{(1,0,0)}^2v_3^2}{m_{(0,0,0)}} - \frac{4m_{(0,0,1)}v_2m_{(2,1,0)}v_3}{m_{(0,0,0)}} - 4m_{(0,0,1)}v_1^2v_2^2v_3 + 8m_{(1,0,1)}v_1v_2^2v_3 - \\
& \frac{104m_{(0,0,1)}m_{(1,0,0)}v_1v_2^2v_3}{m_{(0,0,0)}} - 4m_{(2,0,1)}v_2^2v_3 + \frac{18m_{(0,0,1)}m_{(2,0,0)}v_2^2v_3}{m_{(0,0,0)}} + \frac{36m_{(1,0,0)}m_{(1,0,1)}v_2^2v_3}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(1,0,0)}^2v_2^2v_3}{m_{(0,0,0)}} + \\
& 8m_{(0,1,1)}v_1^2v_2v_3 - \frac{104m_{(0,0,1)}m_{(0,1,0)}v_1^2v_2v_3}{m_{(0,0,0)}} - 24m_{(1,1,1)}v_1v_2v_3 + \frac{88m_{(0,0,1)}m_{(1,1,0)}v_1v_2v_3}{m_{(0,0,0)}} + \frac{104m_{(0,1,0)}m_{(1,0,1)}v_1v_2v_3}{m_{(0,0,0)}} + \\
& \frac{104m_{(0,1,1)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}} - \frac{80m_{(0,0,1)}m_{(0,1,0)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}^2} + \frac{16m_{(0,0,1)}m_{(0,0,2)}v_1v_2v_3}{m_{(0,0,0)}} + 8m_{(2,1,1)}v_2v_3 - \frac{8m_{(0,0,1)}m_{(2,1,0)}v_2v_3}{m_{(0,0,0)}} - \\
& \frac{8m_{(0,1,0)}m_{(2,0,1)}v_2v_3}{m_{(0,0,0)}} - \frac{24m_{(0,1,1)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}^2} - \frac{24m_{(1,0,0)}m_{(1,1,1)}v_2v_3}{m_{(0,0,0)}} - \frac{48m_{(1,0,1)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}} + \\
& \frac{16m_{(0,0,1)}m_{(1,0,0)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}^2} + \frac{32m_{(0,1,0)}m_{(1,0,0)}m_{(1,0,1)}v_2v_3}{m_{(0,0,0)}^2} + \frac{16m_{(0,1,1)}m_{(1,0,0)}^2v_2v_3}{m_{(0,0,0)}^2} + \frac{16m_{(0,0,1)}m_{(0,0,2)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}^2} - \\
& 4m_{(0,2,1)}v_1^2v_3 + \frac{18m_{(0,0,1)}m_{(0,2,0)}v_1^2v_3}{m_{(0,0,0)}} + \frac{36m_{(0,1,0)}m_{(0,1,1)}v_1^2v_3}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(0,1,0)}^2v_1^2v_3}{m_{(0,0,0)}^2} + 8m_{(1,2,1)}v_1v_3 - \\
& \frac{12m_{(0,0,1)}m_{(1,2,0)}v_1v_3}{m_{(0,0,0)}} - \frac{24m_{(0,1,0)}m_{(1,1,1)}v_1v_3}{m_{(0,0,0)}} - \frac{48m_{(0,1,1)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}^2} - \frac{24m_{(0,2,0)}m_{(1,0,1)}v_1v_3}{m_{(0,0,0)}} + \\
& \frac{16m_{(0,1,0)}^2m_{(1,0,1)}v_1v_3}{m_{(0,0,0)}^2} - \frac{8m_{(0,2,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,2,0)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}^2} + \frac{32m_{(0,1,0)}m_{(0,1,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}^2} + \\
& \frac{16m_{(0,0,1)}m_{(0,0,2)}m_{(0,1,0)}v_1v_3}{m_{(0,0,0)}^2} - 2m_{(2,2,1)}v_3 + \frac{2m_{(0,0,1)}m_{(2,2,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(2,1,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(2,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,2,0)}m_{(2,0,1)}v_3}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,2,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} - \frac{4m_{(0,0,1)}m_{(0,2,0)}m_{(2,0,0)}v_3}{m_{(0,0,0)}^2} - \frac{8m_{(0,1,0)}m_{(0,1,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}^2} + \frac{4m_{(1,0,0)}m_{(1,2,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(1,0,1)}m_{(1,2,0)}v_3}{m_{(0,0,0)}} + \\
& \frac{16m_{(1,1,0)}m_{(1,1,1)}v_3}{m_{(0,0,0)}} - \frac{16m_{(0,1,0)}m_{(1,0,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}^2} - \frac{16m_{(0,1,1)}m_{(1,0,0)}m_{(1,1,0)}v_3}{m_{(0,0,0)}^2} - \frac{16m_{(0,0,1)}m_{(0,0,2)}m_{(1,1,0)}v_3}{m_{(0,0,0)}^2} - \\
& \frac{8m_{(0,2,0)}m_{(1,0,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}^2} + \frac{2m_{(0,0,2)}v_2m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{22m_{(0,0,1)}^2v_1^2v_2^2}{m_{(0,0,0)}} - 2m_{(1,0,2)}v_1v_2^2 + \frac{36m_{(0,0,1)}m_{(1,0,1)}v_1v_2^2}{m_{(0,0,0)}} + \\
& \frac{10m_{(0,0,2)}m_{(1,0,0)}v_1v_2^2}{m_{(0,0,0)}} - \frac{24m_{(0,0,1)}^2m_{(1,0,0)}v_1v_2^2}{m_{(0,0,0)}^2} - \frac{6m_{(0,0,1)}m_{(2,0,1)}v_2^2}{m_{(0,0,0)}} - \frac{2m_{(0,0,2)}m_{(2,0,0)}v_2^2}{m_{(0,0,0)}} + \frac{4m_{(0,0,1)}^2m_{(2,0,0)}v_2^2}{m_{(0,0,0)}^2} - \\
& \frac{6m_{(1,0,0)}m_{(1,0,2)}v_2^2}{m_{(0,0,0)}} - \frac{4m_{(1,0,1)}^2v_2^2}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(1,0,0)}m_{(1,0,1)}v_2^2}{m_{(0,0,0)}^2} - 2m_{(0,1,2)}v_1^2v_2 + \frac{36m_{(0,0,1)}m_{(0,1,1)}v_1^2v_2}{m_{(0,0,0)}} + \\
& \frac{10m_{(0,0,2)}m_{(0,1,0)}v_1^2v_2}{m_{(0,0,0)}} - \frac{24m_{(0,0,1)}^2m_{(0,1,0)}v_1^2v_2}{m_{(0,0,0)}^2} + 8m_{(1,1,2)}v_1v_2 - \frac{24m_{(0,0,1)}m_{(1,1,1)}v_1v_2}{m_{(0,0,0)}} - \frac{16m_{(0,0,2)}m_{(1,1,0)}v_1v_2}{m_{(0,0,0)}} + \\
& \frac{16m_{(0,0,1)}^2m_{(1,1,0)}v_1v_2}{m_{(0,0,0)}^2} - \frac{12m_{(0,1,0)}m_{(1,0,2)}v_1v_2}{m_{(0,0,0)}} - \frac{48m_{(0,1,1)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}} + \frac{32m_{(0,0,1)}m_{(0,1,0)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}^2} - \frac{12m_{(0,1,2)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} + \\
& \frac{32m_{(0,0,1)}m_{(0,1,1)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}^2} + \frac{8m_{(0,0,2)}m_{(0,1,0)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,2)}^2v_1v_2}{m_{(0,0,0)}} - 2m_{(2,1,2)}v_2 + \frac{4m_{(0,0,1)}m_{(2,1,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,0,2)}m_{(2,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,2)}v_2}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(2,0,1)}v_2}{m_{(0,0,0)}} + \frac{4m_{(0,1,2)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} - \frac{8m_{(0,0,1)}m_{(0,1,1)}m_{(2,0,0)}v_2}{m_{(0,0,0)}^2} - \\
& \frac{4m_{(0,0,2)}m_{(0,1,0)}m_{(2,0,0)}v_2}{m_{(0,0,0)}^2} + \frac{4m_{(1,0,0)}m_{(1,1,2)}v_2}{m_{(0,0,0)}} + \frac{16m_{(1,0,1)}m_{(1,1,1)}v_2}{m_{(0,0,0)}} + \frac{8m_{(1,0,2)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(1,0,1)}m_{(1,1,0)}v_2}{m_{(0,0,0)}^2} - \\
& \frac{8m_{(0,1,0)}m_{(1,0,1)}^2v_2}{m_{(0,0,0)}^2} - \frac{16m_{(0,1,1)}m_{(1,0,0)}m_{(1,0,1)}v_2}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,2)}^2m_{(1,0,0)}v_2}{m_{(0,0,0)}^2} - \frac{6m_{(0,0,1)}m_{(0,2,1)}v_1^2}{m_{(0,0,0)}} - \frac{2m_{(0,0,2)}m_{(0,2,0)}v_1^2}{m_{(0,0,0)}} + \\
& \frac{4m_{(0,0,1)}^2m_{(0,2,0)}v_1^2}{m_{(0,0,0)}^2} - \frac{6m_{(0,1,0)}m_{(0,1,2)}v_1^2}{m_{(0,0,0)}} - \frac{4m_{(0,1,1)}^2v_1^2}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}m_{(0,1,1)}v_1^2}{m_{(0,0,0)}^2} - 2m_{(1,2,2)}v_1 + \frac{4m_{(0,0,1)}m_{(1,2,1)}v_1}{m_{(0,0,0)}} +
\end{aligned}$$

$$\begin{aligned}
& \frac{4m_{(0,0,2)}m_{(1,2,0)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(1,1,2)}v_1}{m_{(0,0,0)}} + \frac{16m_{(0,1,1)}m_{(1,1,1)}v_1}{m_{(0,0,0)}} + \frac{8m_{(0,1,2)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(0,1,1)}m_{(1,1,0)}v_1}{m_{(0,0,0)}^2} + \\
& \frac{4m_{(0,2,0)}m_{(1,0,2)}v_1}{m_{(0,0,0)}} + \frac{8m_{(0,2,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} - \frac{8m_{(0,0,1)}m_{(0,2,0)}m_{(1,0,1)}v_1}{m_{(0,0,0)}^2} - \frac{16m_{(0,1,0)}m_{(0,1,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}^2} + \frac{2m_{(0,2,2)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} - \\
& \frac{4m_{(0,0,2)}m_{(0,2,0)}m_{(1,0,0)}v_1}{m_{(0,0,0)}^2} - \frac{8m_{(0,1,1)}^2m_{(1,0,0)}v_1}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,2)}^2m_{(0,1,0)}v_1}{m_{(0,0,0)}^2} + m_{(2,2,2)} - \frac{m_{(0,0,2)}m_{(2,2,0)}}{m_{(0,0,0)}} - \frac{4m_{(0,1,1)}m_{(2,1,1)}}{m_{(0,0,0)}} - \\
& \frac{2m_{(0,1,2)}m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(2,0,2)}}{m_{(0,0,0)}} - \frac{2m_{(0,2,1)}m_{(2,0,1)}}{m_{(0,0,0)}} - \frac{m_{(0,2,2)}m_{(2,0,0)}}{m_{(0,0,0)}} + \frac{2m_{(0,0,2)}m_{(0,2,0)}m_{(2,0,0)}}{m_{(0,0,0)}^2} + \frac{4m_{(0,1,1)}^2m_{(2,0,0)}}{m_{(0,0,0)}^2} - \\
& \frac{4m_{(1,0,1)}m_{(1,2,1)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,2)}m_{(1,2,0)}}{m_{(0,0,0)}} - \frac{4m_{(1,1,0)}m_{(1,1,2)}}{m_{(0,0,0)}} - \frac{4m_{(1,1,1)}^2}{m_{(0,0,0)}} + \frac{16m_{(0,1,1)}m_{(1,0,1)}m_{(1,1,0)}}{m_{(0,0,0)}^2} + \frac{4m_{(0,0,2)}^2m_{(1,1,0)}}{m_{(0,0,0)}^2} + \\
& \frac{4m_{(0,2,0)}m_{(1,0,1)}^2}{m_{(0,0,0)}^2}.
\end{aligned}$$

The equilibrium cumulant vector $\gamma^{(eq)}$ is defined by

$$\gamma^{(eq)} = (\rho, 0, 0, 0, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2, 0, 0, \dots, 0)^T.$$

2.6.2 Conservation of mass: ρ

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + v_1^2 + 3c_s^2) \frac{v_1 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-1 + 3v_1^2 + c_s^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_2 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\
& \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (-1 + v_3^2 + 3c_s^2) \frac{v_3 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\
& + (2c_s^4 + 3v_1^2 \omega_4 + 24v_1^2 c_s^2 + 6v_1^4 - \omega_4 c_s^4 - 12v_1^2 \omega_4 c_s^2 + \omega_4 c_s^2 - 6v_1^2 - 2c_s^2 - 3v_1^4 \omega_4) \frac{\delta_l^4}{24 \omega_4 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 2\omega_4 - 5v_1^2 \omega_4 - 3\omega_4 c_s^2 + 10v_1^2 + 6c_s^2) \frac{v_1 \rho \delta_l^4}{12 \omega_4 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& (3\omega_4 + v_1^2 \omega_9 + 3\omega_4 c_s^2 \omega_9 - 3v_1^2 \omega_4 - 9\omega_4 c_s^2 - \omega_9 + 3c_s^2 \omega_9 - \omega_4 \omega_9 + v_1^2 \omega_4 \omega_9) \frac{v_1 \rho \delta_l^4}{12 \omega_4 \omega_9 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_1) \frac{c_s^4 \delta_l^4}{6 \omega_1 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} \\
& + (-\omega_7 \omega_5 - \omega_7 + 3\omega_7 c_s^2 \omega_5 - 9c_s^2 \omega_5 + 3\omega_5 + \omega_7 v_2^2 - 3v_2^2 \omega_5 + 3\omega_7 c_s^2 + \omega_7 v_2^2 \omega_5) \frac{v_2 \rho \delta_l^4}{12 \omega_7 \omega_5 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (2c_s^4 - 12v_2^2 c_s^2 \omega_5 - 3v_2^4 \omega_5 + c_s^2 \omega_5 + 24v_2^2 c_s^2 + 6v_2^4 + 3v_2^2 \omega_5 - 6v_2^2 - 2c_s^2 - c_s^4 \omega_5) \frac{\delta_l^4}{24 \omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 - 3c_s^2 \omega_5 + 2\omega_5 - 5v_2^2 \omega_5 + 10v_2^2 + 6c_s^2) \frac{v_2 \rho \delta_l^4}{12 \omega_5 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& (3\omega_4 c_s^2 \omega_{12} + v_1^2 \omega_{12} + 3\omega_4 - 3v_1^2 \omega_4 - 9\omega_4 c_s^2 - \omega_{12} + v_1^2 \omega_4 \omega_{12} - \omega_4 \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_1 \rho \delta_l^4}{12 \omega_4 \omega_{12} \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (3c_s^2 \omega_{11} - \omega_{11} \omega_5 - \omega_{11} - 9c_s^2 \omega_5 + v_2^2 \omega_{11} \omega_5 + 3\omega_5 - 3v_2^2 \omega_5 + v_2^2 \omega_{11} + 3c_s^2 \omega_{11} \omega_5) \frac{v_2 \rho \delta_l^4}{12 \omega_{11} \omega_5 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_2) \frac{c_s^4 \delta_l^4}{6 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-2 + \omega_3) \frac{c_s^4 \delta_l^4}{6 \omega_3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (3c_s^2 \omega_8 \omega_6 + 3c_s^2 \omega_8 + v_3^2 \omega_8 \omega_6 - \omega_8 - 3v_3^2 \omega_6 + v_3^2 \omega_8 + 3\omega_6 - 9c_s^2 \omega_6 - \omega_8 \omega_6) \frac{v_3 \rho \delta_l^4}{12 \omega_8 \omega_6 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (3c_s^2 \omega_6 \omega_{10} + v_3^2 \omega_6 \omega_{10} + 3c_s^2 \omega_{10} - 3v_3^2 \omega_6 + 3\omega_6 - 9c_s^2 \omega_6 - \omega_6 \omega_{10} - \omega_{10} + v_3^2 \omega_{10}) \frac{v_3 \rho \delta_l^4}{12 \omega_6 \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (2c_s^4 + 24v_3^2 c_s^2 - 12v_3^2 c_s^2 \omega_6 - c_s^4 \omega_6 + 6v_3^4 + 3v_3^2 \omega_6 - 6v_3^2 - 2c_s^2 - 3v_3^4 \omega_6 + c_s^2 \omega_6) \frac{\delta_l^4}{24 \omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 - 5v_3^2 \omega_6 + 10v_3^2 + 2\omega_6 + 6c_s^2 - 3c_s^2 \omega_6) \frac{v_3 \rho \delta_l^4}{12 \omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_3^2} = 0.
\end{aligned}$$

2.6.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2v_1 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_2 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{v_1 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{v_1 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4 - 3v_1^2 \omega_4 - 2\omega_4 c_s^2 + 6v_1^2 + 4c_s^2) \frac{\delta_l^2}{\omega_4 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_4) \frac{3v_1 \rho \delta_l^2}{\omega_4 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2 \omega_1 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2 \omega_1 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + \omega_4 - v_1^2 \omega_4 - 3\omega_4 c_s^2 + 2v_1^2 + 6c_s^2) \frac{v_1 \delta_l^2}{2 \omega_4 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_4 - 3v_1^2 \omega_4 - \omega_4 c_s^2 + 6v_1^2 + 2c_s^2) \frac{\rho \delta_l^2}{2 \omega_4 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2 \omega_1 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2 \omega_1 \delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_2) \frac{c_s^2 \rho \delta_l^2}{2 \omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_2) \frac{c_s^2 \rho \delta_l^2}{2 \omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12 \omega_4^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} +
\end{aligned}$$

$$\begin{aligned}
& (-24 + 24\omega_4 + 11v_1^2\omega_4^2 + 5\omega_4^2c_s^2 - 60v_1^2\omega_4 - 36\omega_4c_s^2 + 60v_1^2 - 4\omega_4^2 + 36c_s^2) \frac{v_1\rho\delta_l^3}{6\omega_4^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{v_1\rho\delta_l^3}{12\omega_4^2\omega_1\omega_9\delta_t} \frac{\partial^3 v_2}{\partial x_1^2\partial x_2} + \\
& (-12 + 12\omega_1 - \omega_1^2) \frac{c_s^4\delta_l^3}{6\omega_1^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_2^2} - \frac{v_1c_s^2\rho\delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_2v_1\delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_3 \frac{v_2\rho\delta_l^3}{6\omega_7\omega_1\delta_t} \frac{\partial^3 v_1}{\partial x_2^3} + \\
& (-1 + 3v_2^2 + c_s^2) \frac{v_1\rho\delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_4 \frac{v_1\rho\delta_l^3}{12\omega_4^2\omega_2\omega_{12}\delta_t} \frac{\partial^3 v_3}{\partial x_1^2\partial x_3} - \frac{v_1c_s^2\rho\delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2\partial x_3} + (-12 + 12\omega_2 - \omega_2^2) \frac{c_s^4\delta_l^3}{6\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_3^2} - \\
& \frac{v_1c_s^2\rho\delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_3^2} - \frac{v_1c_s^2\rho\delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2\partial x_3^2} + (-1 + v_3^2 + 3c_s^2) \frac{v_3v_1\delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3\rho\delta_l^3}{6\omega_8\omega_2\delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{v_1\rho\delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_6 \frac{v_1\delta_l^4}{12\omega_4^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_7 \frac{\rho\delta_l^4}{12\omega_4^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_8 \frac{\rho\delta_l^4}{12\omega_4^2\omega_1^2\omega_9^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^3\partial x_2} + C_9 \frac{v_1c_s^2\delta_l^4}{12\omega_4^2\omega_1^2\omega_9^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2\partial x_2^2} + C_{10} \frac{c_s^2\rho\delta_l^4}{12\omega_4^2\omega_1^2\omega_9\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2^2} + \\
& C_{11} \frac{v_2c_s^2\delta_l^4}{12\omega_7^2\omega_1^2\omega_5\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^2} + (-\omega_7\omega_5 - \omega_7 + 3\omega_7c_s^2\omega_5 - 9c_s^2\omega_5 + 3\omega_5 + \omega_7v_2^2 - 3v_2^2\omega_5 + 3\omega_7c_s^2 + \omega_7v_2^2\omega_5) \frac{v_2v_1\rho\delta_l^4}{12\omega_7\omega_5\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_3^2} \\
& + C_{12} \frac{c_s^2\rho\delta_l^4}{12\omega_7\omega_1^2\omega_5\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_3^2} + \\
& (2c_s^4 - 12v_2^2c_s^2\omega_5 - 3v_2^4\omega_5 + c_s^2\omega_5 + 24v_2^2c_s^2 + 6v_2^4 + 3v_2^2\omega_5 - 6v_2^2 - 2c_s^2 - c_s^4\omega_5) \frac{v_1\delta_l^4}{24\omega_5\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{13} \frac{\rho\delta_l^4}{24\omega_7^2\omega_1^2\delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (-4 - 3c_s^2\omega_5 + 2\omega_5 - 5v_2^2\omega_5 + 10v_2^2 + 6c_s^2) \frac{v_2v_1\rho\delta_l^4}{12\omega_5\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_{14} \frac{\rho\delta_l^4}{12\omega_4^2\omega_2^2\omega_{12}^2\delta_t} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + C_{15} \frac{c_s^4\delta_l^4}{12\omega_{13}\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2\partial x_3} + \\
& (3c_s^2\omega_{11} - \omega_{11}\omega_5 - \omega_{11} - 9c_s^2\omega_5 + v_2^2\omega_{11}\omega_5 + 3\omega_5 - 3v_2^2\omega_5 + v_2^2\omega_{11} + 3c_s^2\omega_{11}\omega_5) \frac{v_2v_1\rho\delta_l^4}{12\omega_{11}\omega_5\delta_t} \frac{\partial^4 v_3}{\partial x_3^3} + \\
& C_{16} \frac{v_1c_s^2\delta_l^4}{12\omega_4^2\omega_2^2\omega_{12}^2\delta_t} \frac{\partial^4 \rho}{\partial x_2^2\partial x_3^2} + C_{17} \frac{c_s^2\rho\delta_l^4}{12\omega_4^2\omega_2^2\omega_{12}\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + C_{18} \frac{c_s^4\rho\delta_l^4}{12\omega_{13}\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + (-2 + \omega_3) \frac{v_1c_s^4\delta_l^4}{6\omega_3\delta_t} \frac{\partial^4 \rho}{\partial x_2^2\partial x_3^2} + \\
& (-\omega_{13}\omega_1\omega_2 - 2\omega_1\omega_2 + 2\omega_1\omega_2^2 - \omega_2^2 + \omega_{13}\omega_1 - \omega_1^2\omega_2^2 + 2\omega_1^2\omega_2 - \omega_1^2 + \omega_{13}\omega_2) \frac{c_s^4\rho\delta_l^4}{\omega_{13}\omega_1^2\omega_2^2\delta_t} \frac{\partial^4 v_1}{\partial x_2^2\partial x_3^2} + \\
& C_{19} \frac{v_3c_s^2\delta_l^4}{12\omega_8^2\omega_6\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^2} + (3c_s^2\omega_8\omega_6 + 3c_s^2\omega_8 + v_3^2\omega_8\omega_6 - \omega_8 - 3v_3^2\omega_6 + v_3^2\omega_8 + 3\omega_6 - 9c_s^2\omega_6 - \omega_8\omega_6) \frac{v_3v_1\rho\delta_l^4}{12\omega_8\omega_6\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_3^2} \\
& + C_{20} \frac{c_s^2\rho\delta_l^4}{12\omega_8\omega_3^2\omega_6\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_3^2} + \\
& (3c_s^2\omega_6\omega_{10} + v_3^2\omega_6\omega_{10} + 3c_s^2\omega_{10} - 3v_3^2\omega_6 + 3\omega_6 - 9c_s^2\omega_6 - \omega_6\omega_{10} - \omega_{10} + v_3^2\omega_{10}) \frac{v_3v_1\rho\delta_l^4}{12\omega_6\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_2\partial x_3^2} + \\
& (2c_s^4 + 24v_3^2c_s^2 - 12v_3^2c_s^2\omega_6 - c_s^4\omega_6 + 6v_3^4 + 3v_3^2\omega_6 - 6v_3^2 - 2c_s^2 - 3v_3^4\omega_6 + c_s^2\omega_6) \frac{v_1\delta_l^4}{24\omega_6\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{21} \frac{\rho\delta_l^4}{24\omega_8^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + \\
& (-4 - 5v_3^2\omega_6 + 10v_3^2 + 2\omega_6 + 6c_s^2 - 3c_s^2\omega_6) \frac{v_3v_1\rho\delta_l^4}{12\omega_6\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 12c_s^4 - 7v_1^2\omega_4^2 - \omega_4^2c_s^2 + 36v_1^2\omega_4 + 144v_1^2c_s^2 + 24v_1^2\omega_4^2c_s^2 + 36v_1^4 - 12\omega_4c_s^4 - 144v_1^2\omega_4c_s^2 + \omega_4^2c_s^4 + 7v_1^4\omega_4^2 + 12\omega_4c_s^2 - 36v_1^2 - 12c_s^2 - 36v_1^4\omega_4 \\
C_2 &= -3v_1^2\omega_4^2\omega_1\omega_9 - 36\omega_4c_s^2\omega_1 + 6v_1^2\omega_4^2\omega_9 - 12\omega_4^2\omega_1 - 6\omega_4^2\omega_9 - 12v_1^2\omega_4^2 + 12v_1^2\omega_4^2\omega_1 - 36\omega_4^2c_s^2 + 3\omega_4^2\omega_1\omega_9 + 12v_1^2\omega_1\omega_9 - 18\omega_4c_s^2\omega_1\omega_9 - \\
& 12\omega_1\omega_9 + 6\omega_4\omega_1\omega_9 + 36c_s^2\omega_1\omega_9 + 12\omega_4^2 + 36\omega_4^2c_s^2\omega_1 - 6v_1^2\omega_4\omega_1\omega_9 - 12v_1^2\omega_4\omega_1 + 18\omega_4^2c_s^2\omega_9 - 11\omega_4^2c_s^2\omega_1\omega_9 + 12\omega_4\omega_1 \\
C_3 &= 6 - 3\omega_7 + 3v_2^2\omega_1 - 3\omega_1 - \omega_7v_2^2\omega_1 + 3\omega_7v_2^2 - 3\omega_7c_s^2\omega_1 - 6v_2^2 + \omega_7\omega_1 - 18c_s^2 + 9\omega_7c_s^2 + 9c_s^2\omega_1 \\
C_4 &= -11\omega_4^2c_s^2\omega_2\omega_{12} - 6\omega_4^2\omega_{12} + 6v_1^2\omega_4^2\omega_{12} - 12v_1^2\omega_4^2 - 6v_1^2\omega_4\omega_2\omega_{12} - 36\omega_4^2c_s^2 + 12v_1^2\omega_4^2\omega_2 + 36c_s^2\omega_2\omega_{12} - 36\omega_4c_s^2\omega_2 + 6\omega_4\omega_2\omega_{12} - \\
& 12\omega_4^2\omega_2 - 12\omega_2\omega_{12} + 12\omega_4\omega_2 - 18\omega_4c_s^2\omega_2\omega_{12} + 36\omega_4^2c_s^2\omega_2 + 12v_1^2\omega_2\omega_{12} + 3\omega_4^2\omega_2\omega_{12} - 12v_1^2\omega_4\omega_2 + 12\omega_4^2 + 18\omega_4^2c_s^2\omega_{12} - 3v_1^2\omega_4^2\omega_2\omega_{12} \\
C_5 &= 6 + 3v_3^2\omega_2 + 9c_s^2\omega_8 - v_3^2\omega_8\omega_2 - 3\omega_8 - 3c_s^2\omega_8\omega_2 - 3\omega_2 - 6v_3^2 + \omega_8\omega_2 + 9c_s^2\omega_2 + 3v_3^2\omega_8 - 18c_s^2 \\
C_6 &= 12 + 10v_1^2\omega_4^3 + 144c_s^4 + 6\omega_4^3c_s^2 - 18\omega_4 - 98v_1^2\omega_4^2 - 34v_1^2\omega_4^3c_s^2 - 78\omega_4^2c_s^2 + 234v_1^2\omega_4 + 672v_1^2c_s^2 + 404v_1^2\omega_4^2c_s^2 + 144v_1^4 - 216\omega_4c_s^4 - \\
& 1008v_1^2\omega_4c_s^2 - \omega_4^3 + 82\omega_4^2c_s^4 + 90v_1^4\omega_4^2 + 198\omega_4c_s^2 - 9v_1^4\omega_4^3 - 156v_1^2 + 8\omega_4^2 - 132c_s^2 - 5\omega_4^3c_s^4 - 216v_1^4\omega_4 \\
C_7 &= 12 + 14v_1^2\omega_4^3 + 24c_s^4 + 2\omega_4^3c_s^2 - 18\omega_4 - 154v_1^2\omega_4^2 - 18v_1^2\omega_4^3c_s^2 - 22\omega_4^2c_s^2 + 378v_1^2\omega_4 + 432v_1^2c_s^2 + 252v_1^2\omega_4^2c_s^2 + 504v_1^4 - 36\omega_4c_s^4 - \\
& 648v_1^2\omega_4c_s^2 - \omega_4^3 + 14\omega_4^2c_s^4 + 310v_1^4\omega_4^2 + 54\omega_4c_s^2 - 29v_1^4\omega_4^3 - 252v_1^2 + 8\omega_4^2 - 36c_s^2 - \omega_4^3c_s^4 - 756v_1^4\omega_4 \\
C_8 &= 36v_1^2\omega_4^3c_s^2\omega_1\omega_9 + 90v_1^2\omega_4\omega_1^3\omega_9^2 + 39v_1^2\omega_4^3\omega_1^3\omega_9 - 5\omega_4^3c_s^2\omega_1^2\omega_9^2 - 6\omega_4^3c_s^4\omega_1^3\omega_9 - \omega_4^3c_s^4\omega_1^3\omega_9^2 - 12\omega_4^2c_s^2\omega_1^2\omega_9 + 12c_s^4\omega_1^3\omega_9^2 + 36v_1^2\omega_4^3\omega_1^2 + 252v_1^2c_s^2\omega_1^3\omega_9^2 + \\
& 6v_1^2\omega_4^3\omega_1^2\omega_9^2 - 36v_1^4\omega_4^2\omega_1^3 + 6\omega_4^4c_s^4\omega_1^2\omega_9^2 - 6\omega_4^3c_s^2\omega_1^3\omega_9 + 72v_1^4\omega_1^2\omega_1^3\omega_9 - 306v_1^2\omega_4c_s^2\omega_1^3\omega_9^2 - \omega_4^2c_s^2\omega_1^3\omega_9^2 - 18\omega_4^3c_s^4\omega_1^2\omega_9 - 36v_1^2\omega_4^3\omega_1^3 + 19v_1^4\omega_4^2\omega_1^3\omega_9^2 - \\
& 108v_1^2\omega_4c_s^2\omega_1^3\omega_9 + 13\omega_4^3c_s^4\omega_1^2\omega_9^2 + 6\omega_4^2c_s^2\omega_1^3\omega_9 - 108v_1^2\omega_4^3c_s^2\omega_1^2 - 36v_1^2\omega_4^3\omega_1^2\omega_9 - 36v_1^4\omega_4^3\omega_1^2 + 12\omega_4^2c_s^4\omega_1^2\omega_9 - 12c_s^2\omega_1^3\omega_9^2 + 108v_1^2\omega_4^3c_s^2\omega_1^2 + 36v_1^2\omega_4^3\omega_1^2 - \\
& 6\omega_4^2c_s^2\omega_1^2\omega_9^2 + 6\omega_4^3c_s^4\omega_1^2\omega_9 - 36v_1^2\omega_4c_s^2\omega_1^2\omega_9^2 - 18v_1^2\omega_4^3c_s^2\omega_1\omega_9^2 + 36v_1^2\omega_4\omega_1^3\omega_9 - 4v_1^2\omega_4^3\omega_1^3\omega_9^2 + \omega_4^2c_s^4\omega_1^3\omega_9^2 + 18\omega_4^3c_s^2\omega_1^2\omega_9 + 36v_1^4\omega_1^3\omega_1^3 - 39v_1^4\omega_1^3\omega_1^3\omega_9 - \\
& 90v_1^4\omega_4\omega_1^3\omega_9^2 + 36v_1^2\omega_4^3c_s^2\omega_1^2\omega_9 + 12\omega_4^3c_s^4\omega_1^2\omega_9^2 - 72v_1^2\omega_1^3\omega_9^2 - 3v_1^2\omega_4^3c_s^2\omega_1^2\omega_9^2 - 12\omega_4^3c_s^2\omega_1\omega_9 + 12\omega_4c_s^2\omega_1^3\omega_9^2 + 60v_1^2\omega_4^2c_s^2\omega_1^3\omega_9^2 - 6v_1^4\omega_4^3\omega_1^2\omega_9^2 - \\
& 24\omega_4^3c_s^4\omega_1\omega_9^2 - 72v_1^2\omega_4^3\omega_1^3\omega_9 - 99v_1^2\omega_4^3c_s^2\omega_1^3\omega_9 - 12\omega_4^4c_s^4\omega_1^2\omega_9^2 + 12v_1^2\omega_4^3c_s^2\omega_1^2\omega_9^2 - 19v_1^2\omega_1^3\omega_1^3\omega_9^2 + 198v_1^2\omega_4^2c_s^2\omega_1^3\omega_9 - 108v_1^2\omega_4^2c_s^2\omega_1^3 + 72v_1^4\omega_1^3\omega_9^2 + \\
& 36v_1^4\omega_4^3\omega_1^2\omega_9 + 12\omega_4^3c_s^4\omega_1\omega_9 - 12\omega_4c_s^4\omega_1^3\omega_9^2 + 54v_1^2\omega_4^3c_s^2\omega_1^2\omega_9 + 6\omega_4^3c_s^2\omega_1\omega_9^2 + 4v_1^4\omega_4^3\omega_1^3\omega_9^2 - 36v_1^4\omega_4\omega_1^3\omega_9 + 18v_1^2\omega_4^2c_s^2\omega_1^2\omega_9^2 + 12\omega_4c_s^2\omega_1^2\omega_9^2 - \\
C_9 &= -12\omega_4^3\omega_9^2 + 12v_1^2\omega_4^2\omega_1\omega_9 + 36\omega_4^3c_s^2\omega_1^2 + 36c_s^2\omega_1^2\omega_9^2 + 5\omega_4^3c_s^2\omega_1^2\omega_9^2 + 18\omega_4^2c_s^2\omega_1^2\omega_9 + 12v_1^2\omega_4^3\omega_1^2 + 18\omega_4\omega_1^2\omega_9^2 + 6\omega_4^3\omega_1^2\omega_9 + v_1^2\omega_4^3\omega_1^2\omega_9^2 + \\
& 12v_1^2\omega_4^3\omega_9^2 + 36\omega_4^3c_s^2\omega_9^2 - 12\omega_4^3\omega_1^2 - 6\omega_4^2\omega_1\omega_9^2 + 12\omega_4^3\omega_1 - 36\omega_4^3c_s^2\omega_9 - 12\omega_4^2\omega_1\omega_9 - 12v_1^2\omega_4^2\omega_1^2 - 6v_1^2\omega_4^3\omega_1^2\omega_9 - 12v_1^2\omega_4^3\omega_9 - 18v_1^2\omega_4\omega_1^2\omega_9^2 + \\
& 12\omega_4^2\omega_9^2 + 12\omega_4^2c_s^2\omega_1^2\omega_9 - 12v_1^2\omega_4^2\omega_1 + 12\omega_4^2\omega_1^2 - \omega_4^2\omega_1^2\omega_9^2 - 36\omega_4^3c_s^2\omega_1 + 6v_1^2\omega_4^2\omega_1\omega_9^2 + 12\omega_4^3\omega_9 - 18\omega_4^3c_s^2\omega_1^2\omega_9 - 12v_1^2\omega_4^2\omega_9^2 + 18\omega_4^2c_s^2\omega_1\omega_9^2 -
\end{aligned}$$

$$36\omega_2^2 c_s^2 \omega_9^2 + 12\omega_4^3 \omega_1 \omega_9^2 + 4v_1^2 \omega_4^2 \omega_9^2 + 54\omega_4^3 c_s^2 \omega_1 \omega_9 - 6\omega_2^2 \omega_1^2 \omega_9 - 36\omega_4^2 c_s^2 \omega_1^2 + 18v_1^2 \omega_4^3 \omega_1 \omega_9 - 12v_1^2 \omega_4^3 \omega_1 \omega_9^2 + 12v_1^2 \omega_1^2 \omega_9^2 - 4\omega_4^2 \omega_1^2 \omega_9^2 + 6v_1^2 \omega_4^2 \omega_1^2 \omega_9 - 40\omega_4^3 c_s^2 \omega_1 \omega_9^2 - 12\omega_1^2 \omega_9^2 + 36\omega_4^2 c_s^2 \omega_1 \omega_9 - 18\omega_4^2 \omega_1 \omega_9 - 54\omega_4^2 c_s^2 \omega_1^2 \omega_9^2$$

$$C_{10} = -4\omega_4^2 c_s^2 \omega_1^2 \omega_9 - 12\omega_2^2 \omega_1 + 36v_1^2 \omega_4 \omega_1^2 \omega_9 + 36v_1^2 \omega_4^2 \omega_1 - 12\omega_4^2 \omega_1^3 - \omega_4^2 c_s^2 \omega_1^3 \omega_9 + 36v_1^2 \omega_1^3 - 72v_1^2 \omega_4^2 \omega_1^2 - 24\omega_4^2 c_s^2 \omega_1^3 + 36v_1^2 \omega_1^2 \omega_1^3 - 12\omega_4 \omega_1^2 \omega_9 + 24\omega_4^2 c_s^2 \omega_1 \omega_9 + 24\omega_4^2 c_s^2 \omega_1^2 - 12c_s^2 \omega_1^2 \omega_9 + 12\omega_4 \omega_1 \omega_9 - 72v_1^2 \omega_4 \omega_1^3 + 12\omega_4^2 c_s^2 \omega_1^2 \omega_9 - 24\omega_4 \omega_1^2 + 12\omega_4^2 c_s^2 \omega_1^3 + 12\omega_1^2 \omega_9 + 24\omega_4 \omega_1^3 + 72v_1^2 \omega_4 \omega_1^2 + 12c_s^2 \omega_1^3 - 24\omega_4^2 c_s^2 \omega_1^2 - 36v_1^2 \omega_1^2 \omega_9 + 12\omega_4^2 c_s^2 \omega_1 - 12\omega_1^3 - 36v_1^2 \omega_4 \omega_1 \omega_9 - 12\omega_4^2 c_s^2 \omega_9 + 18\omega_4^2 c_s^2 \omega_1 \omega_9$$

$$C_{11} = \omega_7^2 v_2^2 \omega_1^2 \omega_5 + 12\omega_7 \omega_5 - 36\omega_7^2 c_s^2 - 36c_s^2 \omega_1 \omega_5 - 6\omega_1^2 \omega_5 + 3\omega_7^2 c_s^2 \omega_1^2 - \omega_7^2 \omega_1^2 - 36\omega_7 c_s^2 \omega_5 - 9\omega_7 c_s^2 \omega_1^2 \omega_5 + 12\omega_7^2 v_2^2 \omega_5 - 6\omega_7 v_2^2 \omega_1^2 + 6v_2^2 \omega_1^2 \omega_5 + 12\omega_7 v_2^2 \omega_1 - 6\omega_2^2 \omega_1 + 12\omega_2^2 \omega_1 \omega_5 + 18\omega_2^2 c_s^2 \omega_1 - 36\omega_2^2 c_s^2 \omega_1 \omega_5 - 12\omega_2^2 v_2^2 + 18\omega_7 v_2^2 \omega_1 \omega_5 + 3\omega_7 \omega_1^2 \omega_5 + 6\omega_2^2 v_2^2 \omega_1 + 12\omega_7^2 - 3\omega_7 v_2^2 \omega_1^2 \omega_5 - 18\omega_7 \omega_1 \omega_5 + 36\omega_7 c_s^2 \omega_1 - 12v_2^2 \omega_1 \omega_5 + 3\omega_7^2 c_s^2 \omega_1^2 \omega_5 - 12\omega_7 \omega_1 - \omega_7^2 \omega_1^2 \omega_5 + 6\omega_7 \omega_1^2 + 54\omega_7 c_s^2 \omega_1 \omega_5 - 12\omega_7^2 v_2^2 \omega_1 \omega_5 + 36\omega_7^2 c_s^2 \omega_5 - 12\omega_7^2 \omega_5 - 18\omega_7 c_s^2 \omega_1^2 + 12\omega_1 \omega_5 + 18c_s^2 \omega_1^2 \omega_5 + \omega_7^2 v_2^2 \omega_1^2 - 12\omega_7 v_2^2 \omega_5$$

$$C_{12} = 12c_s^2 \omega_1 \omega_5 + 18\omega_2^2 \omega_5 + 18v_2^2 \omega_1^2 \omega_5 + 3\omega_7 v_2^2 \omega_1^2 - 12\omega_7 c_s^2 \omega_5 - 5\omega_7 c_s^2 \omega_1^2 \omega_5 + 18\omega_7 v_2^2 \omega_1^2 - 54v_2^2 \omega_1^2 \omega_5 - 36\omega_7 v_2^2 \omega_1 - 6\omega_1^3 \omega_5 + 36v_2^2 \omega_1^2 - \omega_7 c_s^2 \omega_1^2 \omega_5 - 18v_2^2 \omega_1^3 + \omega_7 \omega_1^2 \omega_5 + 12c_s^2 \omega_1^2 - 3\omega_7 v_2^2 \omega_1^2 \omega_5 - 12\omega_7 c_s^2 \omega_1 + 36v_2^2 \omega_1 \omega_5 + 6c_s^2 \omega_1^2 \omega_5 - 6c_s^2 \omega_1^3 + 12\omega_7 \omega_1 + \omega_7 c_s^2 \omega_1^3 - 6\omega_7 \omega_1^2 + 6\omega_1^3 + 18\omega_7 c_s^2 \omega_1 \omega_5 - 12\omega_1^2 - \omega_7 \omega_1^2 + 6\omega_7 c_s^2 \omega_1^2 - 12\omega_1 \omega_5 - 18c_s^2 \omega_1^2 \omega_5$$

$$C_{13} = 144\omega_7 v_2^2 c_s^2 \omega_1^2 + \omega_7^2 c_s^2 \omega_1^3 + 30\omega_7 v_2^2 \omega_1^3 - 8\omega_7^2 c_s^2 \omega_1^2 - 72\omega_7 v_2^2 c_s^2 \omega_1^3 - 72\omega_7 v_2^2 \omega_1^2 + 24\omega_7 c_s^4 \omega_1 - 24\omega_7 c_s^4 \omega_1^2 + 12\omega_7^2 c_s^2 \omega_1 - 12\omega_2^2 v_2^4 \omega_1^2 + 72v_2^2 \omega_1^2 + 6\omega_7 c_s^4 \omega_1^3 - 36v_2^2 \omega_1^3 + 3\omega_2^2 v_2^2 \omega_1^3 + 72\omega_7 v_2^2 c_s^2 \omega_1 + 24\omega_2^2 c_s^2 \omega_1^2 - 12\omega_2^2 v_2^2 c_s^2 \omega_1^2 + 72\omega_7 v_2^2 \omega_1^2 - 24\omega_7 c_s^2 \omega_1 - 3\omega_2^2 c_s^4 \omega_1^3 - 30\omega_7 v_2^2 \omega_1^3 + 6\omega_7^2 v_2^2 c_s^2 \omega_1^3 - 6\omega_7 c_s^2 \omega_1^3 - 216v_2^2 c_s^2 \omega_1^2 - 3\omega_2^2 v_2^2 \omega_1^3 + 36v_2^4 \omega_1^3 + 24\omega_7^2 c_s^4 - 36\omega_7^2 v_2^2 c_s^2 \omega_1 + 24\omega_7 c_s^2 \omega_1^2 - 48\omega_7^2 c_s^4 \omega_1 - 72v_2^4 \omega_1^2 + 108v_2^2 c_s^2 \omega_1^3 + 12\omega_7^2 v_2^2 \omega_1^2$$

$$C_{14} = 4v_1^4 \omega_4^3 \omega_2^3 \omega_{12} + 108v_1^2 \omega_4^3 c_s^2 \omega_2^3 + 36v_1^2 \omega_4^2 \omega_2^3 + 12\omega_4^2 c_s^2 \omega_2^3 \omega_{12} + 18v_1^2 \omega_4^2 c_s^2 \omega_2^3 \omega_{12} - 36v_1^4 \omega_4 \omega_2^3 \omega_{12} + 54v_1^2 \omega_4^2 c_s^2 \omega_2^3 \omega_{12} - 12\omega_4^2 c_s^2 \omega_2^3 \omega_{12}^2 + 6\omega_4^2 c_s^2 \omega_2 \omega_{12} + 36v_1^4 \omega_1^3 \omega_2^3 + 198v_1^2 \omega_1^2 c_s^2 \omega_2^3 \omega_{12} + 72v_1^4 \omega_2^3 \omega_{12} - 108v_1^2 \omega_1^3 c_s^2 \omega_2^3 + 36v_1^4 \omega_1^2 \omega_2^3 \omega_{12} + 12\omega_4^2 c_s^2 \omega_2 \omega_{12} - 36v_1^4 \omega_4^2 \omega_2^3 + 12v_1^4 \omega_1^2 c_s^2 \omega_2^3 \omega_{12} - 19v_1^2 \omega_4^2 \omega_2^3 \omega_{12} - 36v_1^4 \omega_1^2 \omega_2^3 - 72v_1^2 \omega_1^2 \omega_2^3 \omega_{12} - 12\omega_4^2 c_s^4 \omega_2^3 \omega_{12} - 99v_1^2 \omega_1^3 c_s^2 \omega_2^3 \omega_{12} + 60v_1^2 \omega_1^2 c_s^2 \omega_2^3 \omega_{12} + 12\omega_4^2 c_s^2 \omega_2^3 \omega_{12} - 6v_1^4 \omega_1^3 \omega_2^3 \omega_{12} - 24\omega_1^2 c_s^4 \omega_2 \omega_{12} - 36v_1^2 \omega_1^2 \omega_2^3 - 72v_1^2 \omega_1^2 \omega_2^3 \omega_{12} - 3v_1^2 \omega_1^2 c_s^2 \omega_2^3 \omega_{12} - 12\omega_1^3 c_s^2 \omega_2 \omega_{12} - 39v_1^2 \omega_1^2 \omega_2^3 \omega_{12} + 36v_1^2 \omega_1^2 \omega_2^3 + 36v_1^2 \omega_1^2 c_s^2 \omega_2^3 \omega_{12} - 90v_1^4 \omega_4 \omega_2^3 \omega_{12} + 36v_1^2 \omega_4 \omega_2^3 \omega_{12} - 18v_1^2 \omega_1^3 c_s^2 \omega_2 \omega_{12} - 4v_1^2 \omega_1^3 \omega_2^3 \omega_{12} + 18\omega_1^3 c_s^2 \omega_2^3 \omega_{12} + \omega_1^2 c_s^4 \omega_2^3 \omega_{12} - 36v_1^2 \omega_4 c_s^2 \omega_2^3 \omega_{12} + 6\omega_4^2 c_s^4 \omega_2^3 \omega_{12} - 6\omega_1^2 c_s^2 \omega_2^3 \omega_{12} - 36v_1^2 \omega_1^2 \omega_2^3 \omega_{12} + 12\omega_1^2 c_s^4 \omega_2^3 \omega_{12} - 12c_s^2 \omega_2^3 \omega_{12}^2 + 12\omega_4^2 c_s^2 \omega_2^3 - 108v_1^2 \omega_1^2 c_s^2 \omega_2^3 + 19v_1^4 \omega_1^2 \omega_2^3 \omega_{12} + 6\omega_1^2 c_s^2 \omega_2^3 \omega_{12} + 13\omega_1^4 c_s^2 \omega_2^3 \omega_{12} - 108v_1^2 \omega_1^2 c_s^2 \omega_2^3 \omega_{12} + 72v_1^4 \omega_1^2 \omega_2^3 \omega_{12} - 18\omega_1^3 c_s^4 \omega_2^3 \omega_{12} - \omega_1^2 c_s^2 \omega_2^3 \omega_{12}^2 - 306v_1^2 \omega_4 c_s^2 \omega_2^3 \omega_{12} + 6v_1^2 \omega_4^3 \omega_2^3 \omega_{12} - 6\omega_4^2 c_s^2 \omega_2^3 \omega_{12} + 6\omega_4^2 c_s^4 \omega_2^3 \omega_{12} - 12\omega_4^2 c_s^2 \omega_2^3 \omega_{12} - \omega_4^2 c_s^4 \omega_2^3 \omega_{12} + 12c_s^2 \omega_2^3 \omega_{12}^2 + 252v_1^2 c_s^2 \omega_2^3 \omega_{12} + 90v_1^4 \omega_4 \omega_2^3 \omega_{12} + 36v_1^2 \omega_4^3 c_s^2 \omega_2 \omega_{12} + 39v_1^2 \omega_4^3 \omega_2^3 \omega_{12} - 6\omega_4^2 c_s^4 \omega_2^3 \omega_{12} - 5\omega_4^2 c_s^2 \omega_2^3 \omega_{12}^2$$

$$C_{15} = -\omega_{13} \omega_1^2 \omega_2^3 \omega_3 - 12\omega_1^2 \omega_2 \omega_3 - 12\omega_1^3 \omega_3 - 12\omega_1^3 \omega_2^3 \omega_3 - 6\omega_{13} \omega_1^2 \omega_2 \omega_3 + 24\omega_{13} \omega_1 \omega_2^3 \omega_3 + 12\omega_{13} \omega_1 \omega_2^2 - 24\omega_{13} \omega_2^3 \omega_3 - 12\omega_1^3 \omega_2 - 6\omega_{13} \omega_1^2 \omega_2^2 + 12\omega_{13} \omega_1 \omega_2 \omega_3 + 24\omega_1^2 \omega_2 \omega_3 - 2\omega_{13} \omega_1^2 \omega_2^3 \omega_3 - 6\omega_{13} \omega_1^2 \omega_2 - 12\omega_1^2 \omega_2^2 - 2\omega_{13} \omega_1^3 \omega_2^2 + 12\omega_{13} \omega_1^3 + 12\omega_1^3 \omega_2^2 + 12\omega_1^2 \omega_2^3 \omega_3$$

$$C_{16} = -12v_1^2 \omega_4^2 \omega_2 + 36\omega_4^2 c_s^2 \omega_2 \omega_{12} - 54\omega_4^2 c_s^2 \omega_2^2 \omega_{12} - 18\omega_4^2 \omega_2 \omega_{12} + 36\omega_4^2 c_s^2 \omega_{12}^2 + 12\omega_2^2 \omega_{12} + 6v_1^2 \omega_4^2 \omega_2^2 \omega_{12} - 36\omega_4^2 c_s^2 \omega_2 - 40\omega_4^2 c_s^2 \omega_2 \omega_{12}^2 + 12v_1^2 \omega_4^3 \omega_{12} - 12\omega_2^3 \omega_{12} + 12\omega_4^2 \omega_2 - 12v_1^2 \omega_4^2 \omega_2^2 - 4\omega_4^2 \omega_2^3 \omega_{12} - 12v_1^2 \omega_4^2 \omega_{12}^2 + 12v_1^2 \omega_2^2 \omega_{12}^2 - 12\omega_4^2 \omega_{12} - 12v_1^2 \omega_4^2 \omega_{12}^2 + 18v_1^2 \omega_4^2 \omega_2 \omega_{12} + 12\omega_4^2 \omega_{12} - 12\omega_2^2 \omega_{12} - 6\omega_4^2 \omega_2^3 \omega_{12} + 4v_1^2 \omega_4^2 \omega_2^3 \omega_{12} + 36\omega_4^2 c_s^2 \omega_2^2 + 12\omega_4^2 \omega_{12}^2 - 12v_1^2 \omega_4^2 \omega_{12} + 54\omega_4^2 c_s^2 \omega_2 \omega_{12} + 12v_1^2 \omega_4^2 \omega_2^2 + 18\omega_4^2 c_s^2 \omega_2 \omega_{12}^2 + 12\omega_2^3 \omega_2 \omega_{12} - 36\omega_4^2 c_s^2 \omega_{12} + 6v_1^2 \omega_4^2 \omega_2 \omega_{12} - 18\omega_4^2 c_s^2 \omega_2^2 \omega_{12} + 12\omega_2^2 c_s^2 \omega_2^2 \omega_{12} - \omega_4^2 \omega_2^3 \omega_{12} - 6v_1^2 \omega_4^2 \omega_2^3 \omega_{12} - 18v_1^2 \omega_4 \omega_2^3 \omega_{12} - 36\omega_4^2 c_s^2 \omega_{12}^2 - 12\omega_4^2 \omega_2 \omega_{12} - 6\omega_4^2 \omega_2 \omega_{12}^2 - 36\omega_4^2 c_s^2 \omega_2^2 + v_1^2 \omega_4^2 \omega_2^2 \omega_{12} + 18\omega_4^2 c_s^2 \omega_2^2 \omega_{12} + 18\omega_4 \omega_2^2 \omega_{12} + 6\omega_4^2 \omega_2^2 \omega_{12} + 12v_1^2 \omega_4^2 \omega_2 \omega_{12} + 36c_s^2 \omega_2^2 \omega_{12}^2 + 5\omega_4^2 c_s^2 \omega_2^2 \omega_{12}^2$$

$$C_{17} = 36v_1^2 \omega_4^2 \omega_3^2 + 18\omega_4^2 c_s^2 \omega_2 \omega_{12} + 24\omega_4^2 \omega_2^2 + 24\omega_4^2 c_s^2 \omega_2^2 - 12\omega_2^2 \omega_3^2 - 72v_1^2 \omega_4^2 \omega_2^2 + 36v_1^2 \omega_3^2 - 24\omega_4^2 c_s^2 \omega_3^2 - 36v_1^2 \omega_4 \omega_2 \omega_{12} - 36v_1^2 \omega_2^2 \omega_{12} + 36v_1^2 \omega_4^2 \omega_2 + 12\omega_2^2 \omega_{12} + 12\omega_4 \omega_2 \omega_{12} + 12\omega_4^2 c_s^2 \omega_2^2 \omega_{12} - 12\omega_4^2 \omega_2 - 12c_s^2 \omega_2^2 \omega_{12} - 12\omega_4 \omega_2^2 \omega_{12} - 12\omega_4^2 c_s^2 \omega_2 \omega_{12} + 12\omega_4^2 c_s^2 \omega_2 - 12\omega_2^3 - \omega_4^2 c_s^2 \omega_2^2 \omega_{12} + 24\omega_4 \omega_2^2 - 12\omega_4^2 c_s^2 \omega_{12} + 12c_s^2 \omega_2^2 + 72v_1^2 \omega_4 \omega_2^2 - 24\omega_4^2 c_s^2 \omega_2^2 + 36v_1^2 \omega_4 \omega_2^3 \omega_{12} - 4\omega_4^2 c_s^2 \omega_2^2 \omega_{12} - 72v_1^2 \omega_4 \omega_2^2 - 24\omega_4 \omega_2^2 + 12\omega_4^2 c_s^2 \omega_2^2$$

$$C_{18} = -12\omega_1 \omega_2^2 \omega_3 - 24\omega_{13} \omega_1^2 \omega_3 + 24\omega_{13} \omega_1^2 \omega_2 \omega_3 - 6\omega_{13} \omega_1 \omega_3^2 + 24\omega_1 \omega_3^2 \omega_3 - 12\omega_1 \omega_3^2 - 6\omega_{13} \omega_1 \omega_2^3 \omega_3 + 12\omega_2^3 \omega_3^2 - 6\omega_{13} \omega_1^2 \omega_2^2 + 12\omega_{13} \omega_1 \omega_2 \omega_3 - 12\omega_1^2 \omega_2^3 \omega_3 + 12\omega_{13} \omega_3^2 - 2\omega_{13} \omega_1^2 \omega_3^2 - 2\omega_{13} \omega_1^2 \omega_2^3 \omega_3 - 12\omega_1^2 \omega_2^2 - \omega_{13} \omega_1^2 \omega_2^3 \omega_3 + 12\omega_{13} \omega_1^2 \omega_2 + 12\omega_1^2 \omega_2^3 \omega_3 - 12\omega_2^3 \omega_3$$

$$C_{19} = -\omega_8^2 \omega_2^2 - 12v_3^2 \omega_8^2 \omega_2 \omega_6 - 18c_s^2 \omega_8 \omega_2^2 - 36c_s^2 \omega_8 \omega_6 - 12\omega_8^2 \omega_6 - 3v_3^2 \omega_8 \omega_2^2 \omega_6 - 12v_3^2 \omega_8 \omega_6 + 12\omega_8^2 - 6v_3^2 \omega_8 \omega_2^2 - 12v_3^2 \omega_2 \omega_6 + 12v_3^2 \omega_8 \omega_2 - \omega_8^2 \omega_2^3 \omega_6 - 9c_s^2 \omega_8 \omega_2^2 \omega_6 - 36c_s^2 \omega_8^2 - 36c_s^2 \omega_8^2 \omega_2 \omega_6 - 6\omega_8^2 \omega_2 + 36c_s^2 \omega_8 \omega_2 - 6\omega_2^2 \omega_6 - 18\omega_8 \omega_2 \omega_6 - 36c_s^2 \omega_2 \omega_6 + 18c_s^2 \omega_8^2 \omega_2 - 12\omega_8 \omega_2 + 3c_s^2 \omega_8^2 \omega_2 \omega_6 + 18c_s^2 \omega_2^2 \omega_6 + 12\omega_2 \omega_6 + 3\omega_8 \omega_2^2 \omega_6 + 6v_3^2 \omega_2^2 \omega_6 + 6v_3^2 \omega_8^2 \omega_2 + 12\omega_8^2 \omega_2 \omega_6 + 54c_s^2 \omega_8 \omega_2 \omega_6 - 12v_3^2 \omega_8^2 + 18v_3^2 \omega_8 \omega_2 \omega_6 + 12v_3^2 \omega_8^2 \omega_6 + v_3^2 \omega_2^2 \omega_2^2 + 3c_s^2 \omega_8^2 \omega_2^2 + v_3^2 \omega_8^2 \omega_2^2 \omega_6 + 6\omega_8 \omega_2^2 + 12\omega_8 \omega_6 + 36c_s^2 \omega_8^2 \omega_6$$

$$C_{20} = -c_s^2 \omega_8 \omega_2^3 \omega_6 + 6c_s^2 \omega_8 \omega_2^2 - 12c_s^2 \omega_8 \omega_6 + 3v_3^2 \omega_8 \omega_2^3 - 6\omega_2^3 \omega_6 + c_s^2 \omega_8 \omega_2^3 - 3v_3^2 \omega_8 \omega_2^2 \omega_6 + 18v_3^2 \omega_8 \omega_2^2 + 36v_3^2 \omega_2 \omega_6 - 36v_3^2 \omega_8 \omega_2 - 18v_3^2 \omega_2^3 - 5c_s^2 \omega_8 \omega_2^2 \omega_6 - 12c_s^2 \omega_8 \omega_2 + 36v_3^2 \omega_2^2 + 18\omega_2^3 \omega_6 + 12c_s^2 \omega_2^2 \omega_6 - 12\omega_2^2 + 12\omega_8 \omega_2 - 18c_s^2 \omega_2^2 \omega_6 - 12\omega_2 \omega_6 + \omega_8 \omega_2^2 \omega_6 - 54v_3^2 \omega_2^2 \omega_6 + 6\omega_2^3 + 18c_s^2 \omega_8 \omega_2 \omega_6 + 6c_s^2 \omega_2^2 \omega_6 - 6c_s^2 \omega_2^2 - \omega_8 \omega_2^2 + 12c_s^2 \omega_2^2 - 6\omega_8 \omega_2^2 + 18v_3^2 \omega_2^2 \omega_6$$

$$C_{21} = 24c_s^2 \omega_8 \omega_2^2 + 30v_3^2 \omega_8 \omega_2^3 + 108v_3^2 c_s^2 \omega_2^3 - 36v_3^2 c_s^2 \omega_2^2 \omega_2 - 6c_s^2 \omega_8 \omega_2^3 + 24c_s^4 \omega_8 \omega_2 - 72v_3^2 \omega_8 \omega_2^2 - 216v_3^2 c_s^2 \omega_2^2 - 24c_s^4 \omega_8 \omega_2^3 - 30v_3^4 \omega_8 \omega_2^3 - 36v_3^2 \omega_2^3 - 12v_3^2 c_s^2 \omega_8^2 \omega_2^2 + 6c_s^4 \omega_8 \omega_2^3 - 24c_s^2 \omega_8 \omega_2 + 72v_3^2 \omega_2^2 + 72v_3^4 \omega_8 \omega_2^2 + 6v_3^2 c_s^2 \omega_8 \omega_2^3 - 3c_s^4 \omega_8^2 \omega_2^3 + 12c_s^2 \omega_8^2 \omega_2 - 72v_3^2 c_s^2 \omega_8 \omega_2^3 - 12v_3^4 \omega_8 \omega_2^2 + 24c_s^4 \omega_8 \omega_2^2 + 144v_3^2 c_s^2 \omega_8 \omega_2^2 + 3v_3^4 \omega_8^2 \omega_2^2 + 72v_3^2 c_s^2 \omega_8 \omega_2 + c_s^2 \omega_8^2 \omega_2^2 - 48c_s^4 \omega_8 \omega_2 - 72v_3^2 \omega_2^2 + 12v_3^2 \omega_8^2 \omega_2^2 - 8c_s^2 \omega_8^2 \omega_2^2 + 36v_3^2 \omega_2^3 - 3v_3^2 \omega_8^2 \omega_2^2 + 24c_s^4 \omega_8^2$$

2.6.4 Conservation of momentum: ρv_2

$$v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_2 v_1 \delta_L}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_2 \rho \delta_L}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \rho \delta_L}{\delta_t} \frac{\partial v_2}{\partial x_1} + (v_2^2 + c_s^2) \frac{\delta_L}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2v_2 \rho \delta_L}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_2 \delta_L}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_L}{\delta_t} \frac{\partial v_2}{\partial x_3} + \frac{v_2 \rho \delta_L}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_L^2}{2\omega_1 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2 \delta_L^2}{2\omega_1 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-2 - 2c_s^2 \omega_5 + \omega_5 - 3v_2^2 \omega_5 + 6v_2^2 + 4c_s^2) \frac{\delta_L^2}{\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_5) \frac{3v_2 \rho \delta_L^2}{\omega_5 \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_3) \frac{c_s^2 \delta_L^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} +$$

$$\begin{aligned}
& (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\omega_1 \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\omega_1 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (-2 - 3c_s^2 \omega_5 + \omega_5 - v_2^2 \omega_5 + 2v_2^2 + 6c_s^2) \frac{v_2 \delta_l^2}{2\omega_5 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 - c_s^2 \omega_5 + \omega_5 - 3v_2^2 \omega_5 + 6v_2^2 + 2c_s^2) \frac{\rho \delta_l^2}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_3) \frac{c_s^2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_3) \frac{c_s^2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-1 + v_1^2 + 3c_s^2) \frac{v_2 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_2 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& C_1 \frac{v_1 \rho \delta_l^3}{6\omega_1 \omega_9 \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 + 12\omega_1 - \omega_1^2) \frac{c_s^4 \delta_l^3}{6\omega_1^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \frac{v_2 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_2 \frac{v_2 \rho \delta_l^3}{12\omega_7 \omega_1 \omega_5^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_3 \frac{\delta_l^3}{12\omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + \\
& (-24 + 5c_s^2 \omega_5^2 - 36c_s^2 \omega_5 - 4\omega_5^2 + 24\omega_5 - 60v_2^2 \omega_5 + 60v_2^2 + 36c_s^2 + 11v_2^2 \omega_5^2) \frac{v_2 \rho \delta_l^3}{6\omega_5^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \frac{v_2 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& C_4 \frac{v_2 \rho \delta_l^3}{12\omega_{11} \omega_5^2 \omega_3 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{v_2 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + (-12 - \omega_3^2 + 12\omega_3) \frac{c_s^4 \delta_l^3}{6\omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{v_2 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& (-1 + v_3^2 + 3c_s^2) \frac{v_3 v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \rho \delta_l^3}{6\omega_3 \delta_t \omega_{10}} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{v_2 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (2c_s^4 + 3v_1^2 \omega_4 + 24v_1^2 c_s^2 + 6v_1^4 - \omega_4 c_s^4 - 12v_1^4 \omega_4 c_s^2 + \omega_4 c_s^2 - 6v_1^2 - 2c_s^2 - 3v_1^4 \omega_4) \frac{v_2 \delta_l^4}{24\omega_4 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 2\omega_4 - 5v_1^2 \omega_4 - 3\omega_4 c_s^2 + 10v_1^2 + 6c_s^2) \frac{v_2 v_1 \rho \delta_l^4}{12\omega_4 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_l^4}{24\omega_1^2 \omega_5^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_7 \frac{v_1 c_s^2 \delta_l^4}{12\omega_4 \omega_1^2 \omega_9^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_8 \frac{c_s^2 \rho \delta_l^4}{12\omega_4 \omega_1^3 \omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + (3\omega_4 + v_1^2 \omega_9 + 3\omega_4 c_s^2 \omega_9 - 3v_1^2 \omega_4 - 9\omega_4 c_s^2 - \omega_9 + 3c_s^2 \omega_9 - \omega_4 \omega_9 + v_1^2 \omega_4 \omega_9) \frac{v_2 v_1 \rho \delta_l^4}{12\omega_4 \omega_9 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& C_9 \frac{v_2 c_s^2 \delta_l^4}{12\omega_7^2 \omega_1^2 \omega_5^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{10} \frac{c_s^2 \rho \delta_l^4}{12\omega_7 \omega_1^2 \omega_5^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\rho \delta_l^4}{12\omega_7^2 \omega_1^2 \omega_5^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{12} \frac{v_2 \delta_l^4}{12\omega_5^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{13} \frac{\rho \delta_l^4}{12\omega_5^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (3\omega_4 c_s^2 \omega_{12} + v_1^2 \omega_{12} + 3\omega_4 - 3v_1^2 \omega_4 - 9\omega_4 c_s^2 - \omega_{12} + v_1^2 \omega_4 \omega_{12} - \omega_4 \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_2 v_1 \rho \delta_l^4}{12\omega_4 \omega_{12} \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{14} \frac{c_s^4 \rho \delta_l^4}{12\omega_{13} \omega_1^2 \omega_2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{15} \frac{\rho \delta_l^4}{12\omega_{11}^2 \omega_3^3 \omega_5^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 + \omega_2) \frac{v_2 c_s^4 \delta_l^4}{6\omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (-\omega_1^2 \omega_3^2 - \omega_3^2 + \omega_{13} \omega_3 + 2\omega_1^2 \omega_3 - 2\omega_1 \omega_3 + \omega_{13} \omega_1 - \omega_{13} \omega_1 \omega_3 - \omega_1^2 + 2\omega_1 \omega_3^2) \frac{c_s^4 \rho \delta_l^4}{\omega_{13} \omega_1^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + \\
& C_{16} \frac{c_s^4 \rho \delta_l^4}{12\omega_{13} \omega_1^2 \omega_2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{17} \frac{v_2 c_s^2 \delta_l^4}{12\omega_{11}^2 \omega_3^3 \omega_5^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{18} \frac{c_s^2 \rho \delta_l^4}{12\omega_{11} \omega_5^2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (3c_s^2 \omega_8 \omega_6 + 3c_s^2 \omega_8 + v_3^2 \omega_8 \omega_6 - \omega_8 - 3v_3^2 \omega_6 + v_3^2 \omega_8 + 3\omega_6 - 9c_s^2 \omega_6 - \omega_8 \omega_6) \frac{v_2 v_3 \rho \delta_l^4}{12\omega_8 \omega_6 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{19} \frac{v_3 c_s^2 \delta_l^4}{12\omega_6 \omega_3^3 \delta_t \omega_{10}^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& (3c_s^2 \omega_6 \omega_{10} + v_3^2 \omega_6 \omega_{10} + 3c_s^2 \omega_{10} - 3v_3^2 \omega_6 + 3\omega_6 - 9c_s^2 \omega_6 - \omega_6 \omega_{10} - \omega_{10} + v_3^2 \omega_{10}) \frac{v_3 v_2 \rho \delta_l^4}{12\omega_6 \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{20} \frac{c_s^2 \rho \delta_l^4}{12\omega_6 \omega_3^3 \delta_t \omega_{10}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + (2c_s^4 + 24v_3^2 c_s^2 - 12v_3^2 c_s^2 \omega_6 - c_s^4 \omega_6 + 6v_3^4 + 3v_3^2 \omega_6 - 6v_3^2 - 2c_s^2 - 3v_3^4 \omega_6 + c_s^2 \omega_6) \frac{v_2 \delta_l^4}{24\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4 \partial x_3^3} + \\
& + C_{21} \frac{\rho \delta_l^4}{24\omega_3^3 \delta_t \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_3^4} + (-4 - 5v_3^2 \omega_6 + 10v_3^2 + 2\omega_6 + 6c_s^2 - 3c_s^2 \omega_6) \frac{v_3 v_2 \rho \delta_l^4}{12\omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 + 3v_1^2 \omega_1 + 3v_1^2 \omega_9 - 3\omega_1 - v_1^2 \omega_1 \omega_9 + \omega_1 \omega_9 - 3c_s^2 \omega_1 \omega_9 - 3\omega_9 - 6v_1^2 + 9c_s^2 \omega_9 - 18c_s^2 + 9c_s^2 \omega_1 \\
C_2 &= -3\omega_7 v_2^2 \omega_1 \omega_5^2 - 36c_s^2 \omega_1 \omega_5 - 36c_s^2 \omega_5^2 + 12\omega_7 v_2^2 \omega_1 + 18\omega_7 c_s^2 \omega_5^2 + 12\omega_5^2 + 36c_s^2 \omega_1 \omega_5^2 - 6\omega_7 v_2^2 \omega_1 \omega_5 - 6\omega_7 \omega_5^2 - 12\omega_1 \omega_5^2 + 6\omega_7 v_2^2 \omega_5^2 + \\
& 6\omega_7 \omega_1 \omega_5 + 36\omega_7 c_s^2 \omega_1 - 12v_2^2 \omega_1 \omega_5 - 12\omega_7 \omega_1 - 11\omega_7 c_s^2 \omega_1 \omega_5^2 - 18\omega_7 c_s^2 \omega_1 \omega_5 + 12v_2^2 \omega_1 \omega_5^2 - 12v_2^2 \omega_5^2 + 3\omega_7 \omega_1 \omega_5^2 + 12\omega_1 \omega_5 \\
C_3 &= 12c_s^4 - 144v_2^2 c_s^2 \omega_5 - 36v_2^2 \omega_5 - c_s^2 \omega_5^2 + 7v_2^2 \omega_5^2 + 12c_s^2 \omega_5 + 24v_2^2 c_s^2 \omega_5^2 + 144v_2^2 c_s^2 + 36v_2^4 + 36v_2^2 \omega_5 + c_s^4 \omega_5^2 - 36v_2^2 - 12c_s^2 - 7v_2^2 \omega_5^2 - 12c_s^4 \omega_5 \\
C_4 &= -36c_s^2 \omega_5 \omega_3 - 6v_2^2 \omega_{11} \omega_5 \omega_3 - 12\omega_5^2 \omega_3 + 12v_2^2 \omega_{11} \omega_3 + 6v_2^2 \omega_{11} \omega_5^2 - 36c_s^2 \omega_5^2 + 12v_2^2 \omega_5^2 \omega_3 + 3\omega_{11} \omega_5^2 \omega_3 + 12\omega_5^2 - 12\omega_{11} \omega_3 - 6\omega_{11} \omega_5^2 - \\
& 18c_s^2 \omega_{11} \omega_5 \omega_3 + 36c_s^2 \omega_{11} \omega_3 + 18c_s^2 \omega_{11} \omega_5^2 - 11c_s^2 \omega_{11} \omega_5^2 \omega_3 - 12v_2^2 \omega_5 \omega_3 + 6\omega_{11} \omega_5 \omega_3 - 12v_2^2 \omega_5^2 + 12\omega_5 \omega_3 - 3v_2^2 \omega_{11} \omega_5^2 \omega_3 + 36c_s^2 \omega_5^2 \omega_3 \\
C_5 &= 6 + 9c_s^2 \omega_3 + \omega_3 \omega_{10} + 9c_s^2 \omega_{10} - 6v_3^2 - v_3^2 \omega_3 \omega_{10} + 3v_3^2 \omega_3 - 3c_s^2 \omega_3 \omega_{10} - 18c_s^2 - 3\omega_3 - 3\omega_{10} + 3v_3^2 \omega_{10} \\
C_6 &= -8c_s^2 \omega_1^2 \omega_9^2 + 24c_s^4 \omega_9^2 - 3c_s^4 \omega_1^3 \omega_9^2 + 6v_1^2 c_s^2 \omega_1^3 \omega_9^2 - 6c_s^2 \omega_1^3 \omega_9 + 144v_1^2 c_s^2 \omega_1^2 \omega_9 - 24c_s^4 \omega_1^2 \omega_9 - 12v_1^2 c_s^2 \omega_1^2 \omega_9^2 + 24c_s^4 \omega_1^2 \omega_9^2 - 36v_1^2 \omega_1^3 + c_s^2 \omega_1^3 \omega_9^2 + \\
& 6c_s^4 \omega_1^3 \omega_9 + 72v_1^2 \omega_1^2 - 72v_1^2 c_s^2 \omega_1^3 \omega_9 + 24c_s^2 \omega_1^2 \omega_9 + 108v_1^2 c_s^2 \omega_1^3 - 12v_1^4 \omega_1^2 \omega_9^2 - 3v_1^2 \omega_1^3 \omega_9^2 - 24c_s^2 \omega_1 \omega_9 - 216v_1^2 c_s^2 \omega_1^2 - 30v_1^4 \omega_1^3 \omega_9 - 36v_1^2 c_s^2 \omega_1 \omega_9^2 - \\
& 48c_s^4 \omega_1 \omega_9^2 - 72v_1^2 \omega_1^2 \omega_9 - 72v_1^4 \omega_1^2 + 12v_1^2 \omega_1^2 \omega_9^2 + 72v_1^2 c_s^2 \omega_1 \omega_9 + 3v_1^4 \omega_1^3 \omega_9^2 + 24c_s^4 \omega_1 \omega_9 + 30v_1^2 \omega_1^3 \omega_9 + 12c_s^2 \omega_1 \omega_9^2 + 36v_1^4 \omega_1^3 + 72v_1^4 \omega_1^2 \omega_9 \\
C_7 &= -6\omega_1 \omega_9^2 - 36\omega_4 c_s^2 \omega_1 + 3c_s^2 \omega_1^2 \omega_9^2 - \omega_4 \omega_1^2 \omega_9^2 - 36\omega_4 c_s^2 \omega_1 \omega_9^2 - 3v_1^2 \omega_4 \omega_1^2 \omega_9 + 6v_1^2 \omega_1 \omega_9^2 - 36\omega_4 c_s^2 \omega_9 + 36\omega_4 c_s^2 \omega_9^2 - 12v_1^2 \omega_9^2 + v_1^2 \omega_4 \omega_1^2 \omega_9^2 + \\
& 12v_1^2 \omega_1 \omega_9 + 3\omega_4 \omega_1^2 \omega_9 + 54\omega_4 c_s^2 \omega_1 \omega_9 + 18\omega_4 c_s^2 \omega_1^2 - 12\omega_1 \omega_9 - 18c_s^2 \omega_1^2 \omega_9 - 18\omega_4 \omega_1 \omega_9 - 9\omega_4 c_s^2 \omega_1^2 \omega_9 - 6\omega_4 \omega_1^2 + 36c_s^2 \omega_1 \omega_9 + 12v_1^2 \omega_4 \omega_9^2 + \\
& 6\omega_1^2 \omega_9 + 6v_1^2 \omega_4 \omega_1^2 - 36c_s^2 \omega_9^2 - 6v_1^2 \omega_1^2 \omega_9 - 12\omega_4 \omega_9^2 - 12v_1^2 \omega_4 \omega_1 \omega_9^2 + v_1^2 \omega_1^2 \omega_9^2 + 18v_1^2 \omega_4 \omega_1 \omega_9 + 12\omega_4 \omega_9 + 12\omega_9^2 - 12v_1^2 \omega_4 \omega_1 - 12v_1^2 \omega_4 \omega_9 + \\
& 18c_s^2 \omega_1 \omega_9^2 - \omega_1^2 \omega_9^2 + 12\omega_4 \omega_1 \omega_9^2 + 3\omega_4 c_s^2 \omega_1^2 \omega_9^2 + 12\omega_4 \omega_1 \\
C_8 &= 12\omega_4 c_s^2 \omega_1 + c_s^2 \omega_1^3 \omega_9 - 3v_1^2 \omega_4 \omega_1^2 \omega_9 - 12\omega_4 c_s^2 \omega_9 - 18v_1^2 \omega_1^3 + 6\omega_4 c_s^2 \omega_1^3 - 36v_1^2 \omega_1 \omega_9 + 36v_1^2 \omega_1^2 + \omega_4 \omega_1^2 \omega_9 + 18\omega_4 c_s^2 \omega_1 \omega_9 - 18\omega_4 c_s^2 \omega_1^2 + \\
& 12\omega_1 \omega_9 + 6c_s^2 \omega_1^2 \omega_9 + 12c_s^2 \omega_1^2 + 18v_1^2 \omega_4 \omega_1^3 - 5\omega_4 c_s^2 \omega_1^2 \omega_9 + 18\omega_4 \omega_1^2 - 12c_s^2 \omega_1 \omega_9 - 6\omega_1^2 \omega_9 - 6\omega_4 \omega_1^3 - 54v_1^2 \omega_4 \omega_1^2 - 6c_s^2 \omega_1^3 + 18v_1^2 \omega_1^2 \omega_9 - \omega_1^3 \omega_9 + \\
& 6\omega_1^3 - \omega_4 c_s^2 \omega_1^3 \omega_9 + 36v_1^2 \omega_4 \omega_1 + 3v_1^2 \omega_1^3 \omega_9 - 12\omega_1^2 - 12\omega_4 \omega_1
\end{aligned}$$

$$C_9 = -18\omega_7^2 v_2^2 \omega_1^2 \omega_5 - 6\omega_7 \omega_1^2 \omega_5^2 + 12\omega_7 v_2^2 \omega_1 \omega_5^2 - 40\omega_7^2 c_s^2 \omega_1 \omega_5^3 + 12\omega_7^2 \omega_1 \omega_5^3 + 12v_2^2 \omega_1^2 \omega_5^3 + 36\omega_7^2 c_s^2 \omega_1^2 - 12\omega_7^2 \omega_1^2 - 6\omega_7^2 \omega_1 \omega_5^2 + 18\omega_7 v_2^2 \omega_1 \omega_5^3 + 6\omega_7 \omega_1^2 \omega_5^3 + 18\omega_7^2 c_s^2 \omega_1 \omega_5^2 - 12v_2^2 \omega_1^2 \omega_5^2 - 12\omega_7^2 v_2^2 \omega_5^2 - 12\omega_1^2 \omega_5^3 - 36c_s^2 \omega_1 \omega_5^3 + 12\omega_7 \omega_5^3 + 18\omega_7 c_s^2 \omega_1^2 \omega_5^2 + \omega_7^2 v_2^2 \omega_1^2 \omega_5^2 + 12\omega_1^2 \omega_5^2 + 12\omega_7^2 v_2^2 \omega_5^3 - 18\omega_7 c_s^2 \omega_1^2 \omega_5^3 + 4\omega_7^2 v_2^2 \omega_1^2 \omega_5^2 - 36\omega_7 c_s^2 \omega_5^3 - 36c_s^2 \omega_1^2 \omega_5^2 + 6\omega_7^2 v_2^2 \omega_1 \omega_5^2 + 54\omega_7 c_s^2 \omega_1 \omega_5^3 + 12\omega_7^2 \omega_5^2 - 36\omega_7^2 c_s^2 \omega_5^2 - 12\omega_7 v_2^2 \omega_5^3 + 36c_s^2 \omega_1^2 \omega_5^3 + 12\omega_1 \omega_5^3 - 54\omega_7^2 c_s^2 \omega_1^2 \omega_5 - 12\omega_7^2 \omega_5^3 + 36\omega_7^2 c_s^2 \omega_5^3 + 18\omega_7^2 \omega_1^2 \omega_5 - 12\omega_7^2 v_2^2 \omega_1 \omega_5^3 + 36\omega_7 c_s^2 \omega_1 \omega_5^2 + 12\omega_7^2 c_s^2 \omega_1^2 \omega_5^2 - 6\omega_7 v_2^2 \omega_1^2 \omega_5^3 - 18\omega_7 \omega_1 \omega_5^3 - 4\omega_7^2 \omega_1^2 \omega_5^2 - \omega_7^2 \omega_1^2 \omega_5^2 + 5\omega_7^2 c_s^2 \omega_1^2 \omega_5^3 - 12\omega_7 \omega_1 \omega_5^2 + 6\omega_7 v_2^2 \omega_1^2 \omega_5^2 - 12v_2^2 \omega_1 \omega_5^3 + 12\omega_7^2 v_2^2 \omega_1^2$$

$$C_{10} = -\omega_7 c_s^2 \omega_1^3 \omega_5^2 - 24\omega_1^2 \omega_5 - 72v_2^2 \omega_1^3 \omega_5 + 12\omega_7 c_s^2 \omega_1^2 \omega_5 - 72v_2^2 \omega_1^2 \omega_5^2 - 36\omega_7 v_2^2 \omega_1^2 - 12\omega_1^3 \omega_5^2 + 72v_2^2 \omega_1^2 \omega_5 + 24\omega_1^3 \omega_5 - 12\omega_7 c_s^2 \omega_5^2 - 4\omega_7 c_s^2 \omega_1^2 \omega_5^2 + 12c_s^2 \omega_1 \omega_5^2 + 24\omega_1^2 \omega_5^2 + 36v_2^2 \omega_1^3 \omega_5^2 + 36v_2^2 \omega_3^3 - 36\omega_7 v_2^2 \omega_1 \omega_5 - 12\omega_7 \omega_1^2 \omega_5 - 12\omega_1 \omega_5^2 - 24c_s^2 \omega_1^2 \omega_5^2 + 36\omega_7 v_2^2 \omega_1^2 \omega_5 + 12\omega_7 \omega_1 \omega_5 - 24c_s^2 \omega_3^3 \omega_5 + 12c_s^2 \omega_1^3 + 18\omega_7 c_s^2 \omega_1 \omega_5^2 + 12\omega_7 \omega_1^2 - 12\omega_1^3 - 12\omega_7 c_s^2 \omega_1 \omega_5 + 36v_2^2 \omega_1 \omega_5^2 + 12c_s^2 \omega_1^3 \omega_5^2 - 12\omega_7 c_s^2 \omega_1^2 + 24c_s^2 \omega_1^2 \omega_5$$

$$C_{11} = -4\omega_7^2 v_2^2 \omega_1^3 \omega_5^3 - 108v_2^2 c_s^2 \omega_1^2 \omega_5^3 + 36v_2^4 \omega_1^3 \omega_5^3 + 6\omega_7 c_s^2 \omega_1^3 \omega_5^2 + 6\omega_7^2 c_s^2 \omega_1 \omega_5^3 - 12\omega_7^2 c_s^2 \omega_1^2 + 12\omega_7^2 c_s^4 \omega_5^3 - 90\omega_7^2 v_2^4 \omega_1^3 \omega_5 + 12\omega_7 c_s^4 \omega_1^2 \omega_5^2 - 6\omega_7^2 v_2^4 \omega_1^2 \omega_5^3 + 36v_2^2 \omega_1^2 \omega_5^3 - 36v_2^4 \omega_1^3 \omega_5^2 - 19\omega_7^2 v_2^2 \omega_1^3 \omega_5^2 - 6\omega_7 c_s^2 \omega_1^3 \omega_5^3 - 18\omega_7 c_s^4 \omega_1^2 \omega_5^3 - 36v_2^2 \omega_1^3 \omega_5^3 + 4\omega_7^2 v_2^4 \omega_1^3 \omega_5^3 - 6\omega_7 c_s^4 \omega_1^3 \omega_5^2 - 24\omega_7^2 c_s^4 \omega_1 \omega_5^3 - 12\omega_7 c_s^2 \omega_1^2 \omega_5^2 - 36v_2^2 \omega_1^2 \omega_5^3 + 6\omega_7^2 v_2^2 \omega_1^2 \omega_5^3 + 108v_2^2 c_s^2 \omega_1^2 \omega_5^3 + 36\omega_7 v_2^2 c_s^2 \omega_1 \omega_5^3 + 90\omega_7^2 v_2^4 \omega_1^3 \omega_5^2 + 19\omega_7^2 v_2^4 \omega_1^3 \omega_5^2 + 36v_2^2 \omega_1^3 \omega_5^2 + 6\omega_7 c_s^4 \omega_1^3 \omega_5^3 - 18\omega_7^2 v_2^2 \omega_1^3 \omega_5^3 - 108\omega_7^2 c_s^2 \omega_1^3 \omega_5^2 - 36\omega_7 v_2^4 \omega_1^3 \omega_5^2 + 6\omega_7^2 c_s^4 \omega_1^2 \omega_5^2 + 36\omega_7 v_2^2 \omega_1^2 \omega_5^3 - 3\omega_7^2 v_2^2 c_s^2 \omega_1^2 \omega_5^3 - 306\omega_7^2 v_2^2 c_s^2 \omega_1^2 \omega_5^3 - 12\omega_7 c_s^2 \omega_1 \omega_5^3 + 36\omega_7 v_2^2 c_s^2 \omega_1^2 \omega_5^2 + 39\omega_7 v_2^2 \omega_1^3 \omega_5^3 - \omega_7^2 c_s^2 \omega_1^3 \omega_5^2 + 18\omega_7^2 v_2^2 c_s^2 \omega_1^2 \omega_5^2 + 13\omega_7^2 c_s^4 \omega_1^2 \omega_5^3 - 12\omega_7^2 c_s^4 \omega_1^3 \omega_5 + 12\omega_7^2 c_s^4 \omega_1^3 + 12\omega_7^2 c_s^2 \omega_1^2 \omega_5^2 - 72\omega_7 v_2^2 \omega_1^3 \omega_5^2 + 54\omega_7 v_2^2 c_s^2 \omega_1^2 \omega_5^3 + 252\omega_7^2 v_2^2 c_s^2 \omega_1^2 - 108\omega_7 v_2^2 c_s^2 \omega_1^2 \omega_5 - 6\omega_7^2 c_s^2 \omega_1^2 \omega_5^2 - 36\omega_7 v_2^2 \omega_1^3 \omega_5^3 + 36\omega_7 v_2^2 \omega_1^3 \omega_5 + 198\omega_7 v_2^2 c_s^2 \omega_1^3 \omega_5^2 + 12\omega_7^2 v_2^2 c_s^2 \omega_1^3 \omega_5^3 - 72\omega_7^2 v_2^2 \omega_1^3 - 36\omega_7^2 v_2^2 c_s^2 \omega_1^2 \omega_5^2 + 12\omega_7 c_s^4 \omega_1 \omega_5^3 - 39\omega_7 v_2^4 \omega_1^3 \omega_5^3 + \omega_7^2 c_s^4 \omega_1^3 \omega_5^2 - 99\omega_7 v_2^2 c_s^2 \omega_1^3 \omega_5^3 + 12\omega_7^2 c_s^2 \omega_1^3 \omega_5 - 5\omega_7^2 c_s^2 \omega_1^3 \omega_5^3 + 72\omega_7 v_2^4 \omega_1^3 \omega_5^2 - \omega_7^2 c_s^4 \omega_1^3 \omega_5^3 - 12\omega_7^2 c_s^4 \omega_1^2 \omega_5 + 60\omega_7^2 v_2^2 c_s^2 \omega_1^3 \omega_5^2$$

$$C_{12} = 12 + 6c_s^2 \omega_5^3 + 144c_s^4 - 1008v_2^2 c_s^2 \omega_5 - 216v_2^4 \omega_5 - 78c_s^2 \omega_5^2 + 90v_2^4 \omega_5^2 - 34v_2^2 c_s^2 \omega_5^3 + 198c_s^2 \omega_5 + 8\omega_5^2 + 404v_2^2 c_s^2 \omega_5^2 - 9v_2^4 \omega_5^3 - 18\omega_5 - \omega_5^3 + 672v_2^2 c_s^2 + 144v_2^4 + 234v_2^2 \omega_5 + 82c_s^4 \omega_5^2 - 156v_2^2 - 5c_s^4 \omega_5^3 - 132c_s^2 + 10v_2^2 \omega_5^3 - 98v_2^2 \omega_5^2 - 216c_s^4 \omega_5$$

$$C_{13} = 12 + 2c_s^2 \omega_5^3 + 24c_s^4 - 648v_2^2 c_s^2 \omega_5 - 756v_2^4 \omega_5 - 22c_s^2 \omega_5^2 + 310v_2^4 \omega_5^2 - 18v_2^2 c_s^2 \omega_5^3 + 54c_s^2 \omega_5 + 8\omega_5^2 + 252v_2^2 c_s^2 \omega_5^2 - 29v_2^4 \omega_5^3 - 18\omega_5 - \omega_5^3 + 432v_2^2 c_s^2 + 504v_2^4 + 378v_2^2 \omega_5 + 14c_s^4 \omega_5^2 - 252v_2^2 - c_s^4 \omega_5^3 - 36c_s^2 + 14v_2^2 \omega_5^3 - 154v_2^2 \omega_5^2 - 36c_s^4 \omega_5$$

$$C_{14} = -24\omega_{13}\omega_2\omega_3^2 - 6\omega_{13}\omega_1^2\omega_3 - 12\omega_1^2\omega_3^2 - 12\omega_1^2\omega_2\omega_3 - 2\omega_{13}\omega_1^2\omega_2\omega_3^2 - 12\omega_3^3\omega_3 - 6\omega_{13}\omega_1^2\omega_3^2 + 12\omega_1^3\omega_3^2 - 6\omega_{13}\omega_1^2\omega_2\omega_3 - 2\omega_{13}\omega_1^3\omega_3^2 + 12\omega_1^2\omega_2\omega_3^2 - 12\omega_1^3\omega_2 - \omega_{13}\omega_1^3\omega_2\omega_3^2 + 12\omega_{13}\omega_1\omega_2\omega_3 + 24\omega_1^3\omega_2\omega_3 + 12\omega_{13}\omega_1^3 + 12\omega_{13}\omega_1\omega_3^2 - 12\omega_1^3\omega_2\omega_3^2 + 24\omega_{13}\omega_1\omega_2\omega_3^2$$

$$C_{15} = 12c_s^4 \omega_{11}^2 \omega_5^3 - c_s^2 \omega_{11}^2 \omega_5^2 \omega_3^3 - 90v_2^4 \omega_{11}^2 \omega_5 \omega_3^3 + 6c_s^2 \omega_{11}^2 \omega_5^2 \omega_3 + 36v_2^4 \omega_3^3 \omega_3^3 - 108v_2^2 c_s^2 \omega_{11}^2 \omega_5^2 \omega_3^3 + 12v_2^2 c_s^2 \omega_{11}^2 \omega_3^3 \omega_3^3 + 36v_2^2 \omega_5^2 \omega_3^3 + 6v_2^2 \omega_{11}^2 \omega_3^3 \omega_3^2 + 6c_s^2 \omega_{11} \omega_5^3 \omega_3^3 - 36v_2^4 \omega_3^2 \omega_3^3 - 3v_2^2 c_s^2 \omega_{11}^2 \omega_5^3 \omega_3^2 + 72v_2^4 \omega_{11} \omega_5^2 \omega_3^3 - 6c_s^2 \omega_{11}^2 \omega_5^2 \omega_3^2 - 18c_s^4 \omega_{11} \omega_5^3 \omega_3^2 - 4v_2^2 \omega_{11}^2 \omega_5^3 \omega_3^2 - 12c_s^2 \omega_{11}^2 \omega_3^3 - 12c_s^4 \omega_{11} \omega_5 \omega_3^2 + 12c_s^4 \omega_{11} \omega_5^3 \omega_3 + 36v_2^2 \omega_{11} \omega_5 \omega_3^3 - 6c_s^4 \omega_{11} \omega_5^2 \omega_3^3 - 36v_2^2 \omega_5^2 \omega_3^3 + 60v_2^2 c_s^2 \omega_{11}^2 \omega_5^2 \omega_3^3 + 108v_2^2 c_s^2 \omega_5^2 \omega_3^3 - 36v_2^2 \omega_5^2 \omega_3^3 - 18v_2^2 c_s^2 \omega_{11}^2 \omega_3^3 \omega_3 + 36v_2^4 \omega_{11} \omega_5^2 \omega_3^2 + 12c_s^4 \omega_{11}^2 \omega_5^2 \omega_3^2 - 12c_s^4 \omega_{11}^2 \omega_5 \omega_3^3 - 19v_2^2 \omega_{11}^2 \omega_5^2 \omega_3^3 - 19v_2^2 \omega_{11}^2 \omega_5^2 \omega_3^3 - 39v_2^2 \omega_{11} \omega_5^3 \omega_3^3 - 5c_s^2 \omega_{11}^2 \omega_5^3 \omega_3^3 - 108v_2^2 c_s^2 \omega_{11} \omega_5 \omega_3^3 + 18v_2^2 c_s^2 \omega_{11}^2 \omega_5^2 \omega_3^2 + 12c_s^4 \omega_{11}^2 \omega_5^2 \omega_3^2 - 12c_s^4 \omega_{11}^2 \omega_5 \omega_3^3 + 90v_2^2 c_s^2 \omega_{11}^2 \omega_5 \omega_3^3 + c_s^4 \omega_{11}^2 \omega_5^2 \omega_3^3 - 72v_2^2 \omega_{11}^2 \omega_3^3 - 24c_s^4 \omega_{11}^2 \omega_3^3 - 6v_2^4 \omega_{11}^2 \omega_5^2 \omega_3^2 + 252v_2^2 c_s^2 \omega_{11}^2 \omega_3^3 - 6c_s^2 \omega_{11} \omega_5^3 \omega_3^3 + 36v_2^2 c_s^2 \omega_{11} \omega_5^2 \omega_3^3 - 36v_2^2 c_s^2 \omega_{11}^2 \omega_5 \omega_3^3 + 198v_2^2 c_s^2 \omega_{11} \omega_5^2 \omega_3^3 - 72v_2^2 \omega_{11} \omega_5^2 \omega_3^3 + 6c_s^4 \omega_{11}^2 \omega_5^2 \omega_3^2 + 36v_2^2 c_s^2 \omega_{11} \omega_5^2 \omega_3^2 - 306v_2^2 c_s^2 \omega_{11}^2 \omega_5 \omega_3^3 + 18c_s^4 \omega_{11} \omega_5^2 \omega_3^2 + 4v_2^2 \omega_{11}^2 \omega_3^3 \omega_3^3 - 99v_2^2 c_s^2 \omega_{11} \omega_5^2 \omega_3^3 - 12c_s^4 \omega_{11} \omega_3^3 \omega_3^3 + 72v_2^4 \omega_{11}^2 \omega_3^3 + 12c_s^2 \omega_{11}^2 \omega_5 \omega_3^2 + 6c_s^4 \omega_{11} \omega_5^2 \omega_3^2 - 36v_2^2 \omega_{11} \omega_5 \omega_3^3 - c_s^4 \omega_{11}^2 \omega_5^3 \omega_3^3 - 36v_2^2 \omega_{11} \omega_5^2 \omega_3^2 - 12c_s^2 \omega_{11} \omega_5^2 \omega_3^2 + 19v_2^4 \omega_{11}^2 \omega_5^2 \omega_3^3 + 12c_s^2 \omega_{11}^2 \omega_5 \omega_3^3 + 54v_2^2 c_s^2 \omega_{11} \omega_5^2 \omega_3^3 + 39v_2^2 \omega_{11} \omega_5^3 \omega_3^3 + 13c_s^4 \omega_{11}^2 \omega_3^3 \omega_3^3$$

$$C_{16} = 12\omega_{13}\omega_3^3 - \omega_{13}\omega_1^2\omega_2\omega_3^3 - 2\omega_{13}\omega_1^2\omega_3^3 - 12\omega_1^2\omega_3^3 - 12\omega_2\omega_3^3 - 2\omega_{13}\omega_1^2\omega_2\omega_3^3 + 12\omega_1^2\omega_3^3 - 6\omega_{13}\omega_1^2\omega_3^3 - 12\omega_1^2\omega_2\omega_3^3 + 12\omega_{13}\omega_1^2\omega_3 + 24\omega_{13}\omega_1^2\omega_2\omega_3 + 12\omega_1^2\omega_2\omega_3^3 + 24\omega_1\omega_2\omega_3^3 + 12\omega_{13}\omega_1\omega_2\omega_3 - 12\omega_1\omega_2\omega_3^3 - 12\omega_1\omega_3^3 - 6\omega_{13}\omega_1\omega_2\omega_3^3 - 24\omega_{13}\omega_1^2\omega_2 - 6\omega_{13}\omega_1\omega_3^3$$

$$C_{17} = -40c_s^2 \omega_{11}^2 \omega_5^3 \omega_3 + 18\omega_{11}^2 \omega_5 \omega_3^2 - 18\omega_{11} \omega_5^3 \omega_3 - 12v_2^2 \omega_5^2 \omega_3 - 12v_2^2 \omega_{11} \omega_5^3 + 36c_s^2 \omega_{11}^2 \omega_3^2 + v_2^2 \omega_{11}^2 \omega_5^3 \omega_3^2 - 6\omega_{11} \omega_5^2 \omega_3^2 + 12c_s^2 \omega_{11}^2 \omega_5^2 \omega_3^2 + 6v_2^2 \omega_{11}^2 \omega_5^2 \omega_3 - 12\omega_5^2 \omega_3^2 - 12v_2^2 \omega_5^2 \omega_3^2 + 12\omega_{11} \omega_5^2 + 4v_2^2 \omega_{11}^2 \omega_5^2 \omega_3^2 + 36c_s^2 \omega_{11}^2 \omega_5^2 + 12\omega_5^2 \omega_3 - 12\omega_{11} \omega_5^2 \omega_3 + 18c_s^2 \omega_{11}^2 \omega_5^2 \omega_3 + 12v_2^2 \omega_5^2 \omega_3^2 - 36c_s^2 \omega_{11}^2 \omega_5^2 \omega_3 - 12v_2^2 \omega_{11}^2 \omega_5^2 \omega_3 + 12\omega_5^2 \omega_3^2 + 6\omega_{11} \omega_5^2 \omega_3^2 + 12\omega_{11}^2 \omega_5^2 - 36c_s^2 \omega_5^2 \omega_3^2 + 6v_2^2 \omega_{11} \omega_5^2 \omega_3^2 + 36c_s^2 \omega_{11} \omega_5^2 \omega_3 - 6\omega_{11}^2 \omega_5^2 \omega_3 + 12v_2^2 \omega_{11}^2 \omega_3 - 36c_s^2 \omega_{11} \omega_3^2 - 36c_s^2 \omega_5^2 \omega_3 - 18v_2^2 \omega_{11} \omega_5 \omega_3^2 + 18v_2^2 \omega_{11} \omega_3^2 \omega_3 - 12\omega_{11}^2 \omega_3^2 - \omega_{11}^2 \omega_5^2 \omega_3^2 - 18c_s^2 \omega_{11} \omega_3^2 \omega_3^2 + 12\omega_{11}^2 \omega_3^2 \omega_3 + 54c_s^2 \omega_{11} \omega_5^2 \omega_3 - 54c_s^2 \omega_{11}^2 \omega_5 \omega_3^2 - 6v_2^2 \omega_{11} \omega_5^2 \omega_3^2 + 36c_s^2 \omega_5^2 \omega_3^2 - 12v_2^2 \omega_{11}^2 \omega_5^2 + 18c_s^2 \omega_{11} \omega_5^2 \omega_3 - 4\omega_{11}^2 \omega_5^2 \omega_3^2 + 12v_2^2 \omega_{11}^2 \omega_5^2 - 12\omega_{11}^2 \omega_3^2 + 12v_2^2 \omega_{11} \omega_5^2 \omega_3$$

$$C_{18} = 12c_s^2 \omega_{11} \omega_5 \omega_3^2 - 12\omega_3^3 + 12\omega_{11} \omega_5^2 \omega_3^2 + 36v_2^2 \omega_5^2 \omega_3^3 - 36v_2^2 \omega_{11} \omega_5 \omega_3 - 12\omega_5^2 \omega_3 - 72v_2^2 \omega_5^2 \omega_3^2 - 12\omega_5^2 \omega_3^3 - 24c_s^2 \omega_5 \omega_3^3 - 36v_2^2 \omega_{11} \omega_3^2 + 36v_2^2 \omega_{11} \omega_5 \omega_3^2 + 24c_s^2 \omega_5 \omega_3^2 + 12c_s^2 \omega_3^3 + 24\omega_5^2 \omega_3^2 - 12c_s^2 \omega_{11} \omega_5 \omega_3 - 24\omega_5 \omega_3^2 - 24c_s^2 \omega_5^2 \omega_3^2 - 12c_s^2 \omega_{11} \omega_5^2 + 18c_s^2 \omega_{11} \omega_5^2 \omega_3 + 12c_s^2 \omega_5^2 \omega_3^2 + 24\omega_5 \omega_3^2 + 36v_2^2 \omega_3^3 + 12\omega_{11} \omega_5 \omega_3 - 12\omega_{11} \omega_5 \omega_3^2 - c_s^2 \omega_{11} \omega_5^2 \omega_3^2 + 72v_2^2 \omega_5 \omega_3^2 - 4c_s^2 \omega_{11} \omega_5^2 \omega_3^2 - 12c_s^2 \omega_{11} \omega_3^2 - 72v_2^2 \omega_5 \omega_3^2 + 12c_s^2 \omega_5^2 \omega_3$$

$$C_{19} = -36c_s^2 \omega_6 \omega_{10} - 36c_s^2 \omega_6 \omega_3 \omega_{10}^2 + 18v_2^2 \omega_6 \omega_3 \omega_{10} - 36c_s^2 \omega_{10}^2 + 6v_2^2 \omega_6 \omega_3^2 + v_2^2 \omega_3^2 \omega_{10}^2 - 6\omega_3 \omega_{10}^2 + 3c_s^2 \omega_3^2 \omega_{10}^2 + 18c_s^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_6 \omega_{10} - \omega_6 \omega_3^2 \omega_{10}^2 + 3\omega_6 \omega_3^2 \omega_{10} + 12v_2^2 \omega_6 \omega_{10}^2 - 12\omega_3 \omega_{10} - 18c_s^2 \omega_3^2 \omega_{10} - 36c_s^2 \omega_6 \omega_3 - 12v_2^2 \omega_6 \omega_3 \omega_{10} + 54c_s^2 \omega_6 \omega_3 \omega_{10} - 12v_2^2 \omega_6 \omega_3 - 6v_2^2 \omega_3^2 \omega_{10} + 12\omega_{10}^2 + 36c_s^2 \omega_6 \omega_{10}^2 + v_2^2 \omega_6 \omega_3^2 \omega_{10}^2 - 9c_s^2 \omega_6 \omega_3^2 \omega_{10} + 12v_2^2 \omega_3 \omega_{10} - 12v_2^2 \omega_{10}^2 - 12\omega_6 \omega_{10} - 18\omega_6 \omega_3 \omega_{10} + 36c_s^2 \omega_3 \omega_{10} + 6\omega_3^2 \omega_{10} + 12\omega_6 \omega_3 + 18c_s^2 \omega_3 \omega_{10}^2 - \omega_3^2 \omega_{10}^2 - 6\omega_6 \omega_3^2 + 12\omega_6 \omega_3 \omega_{10} + 12\omega_6 \omega_{10} + 3c_s^2 \omega_6 \omega_3^2 \omega_{10} - 3v_2^2 \omega_6 \omega_3^2 \omega_{10} + 6v_2^2 \omega_3 \omega_{10}^2$$

$$C_{20} = 6c_s^2 \omega_6 \omega_3^3 - 12c_s^2 \omega_6 \omega_{10} + 6\omega_3^3 + c_s^2 \omega_3^3 \omega_{10} - 54v_2^2 \omega_6 \omega_3^2 - 12\omega_3^2 - 18c_s^2 \omega_6 \omega_3^2 + 3v_2^2 \omega_3^3 \omega_{10} + 18v_2^2 \omega_6 \omega_3^3 + \omega_6 \omega_3^2 \omega_{10} + 12c_s^2 \omega_3^2 + 12\omega_3 \omega_{10} + 6c_s^2 \omega_3^2 \omega_{10} + 12c_s^2 \omega_6 \omega_3 + 18c_s^2 \omega_6 \omega_3 \omega_{10} + 36v_2^2 \omega_6 \omega_3 - 6c_s^2 \omega_3^3 + 18v_2^2 \omega_3^2 \omega_{10} - 5c_s^2 \omega_6 \omega_3^2 \omega_{10} - 36v_2^2 \omega_3 \omega_{10} - 12c_s^2 \omega_3 \omega_{10} - 6\omega_3^2 \omega_{10} - 12\omega_6 \omega_3 + 18\omega_6 \omega_3^2 + 36v_2^2 \omega_3^2 - c_s^2 \omega_6 \omega_3^2 \omega_{10} - 6\omega_6 \omega_3^2 - \omega_3^3 \omega_{10} - 3v_2^2 \omega_6 \omega_3^2 \omega_{10} - 18v_2^2 \omega_3^3$$

$$C_{21} = 3v_2^3 \omega_3^3 \omega_{10}^2 + 72v_2^3 c_s^2 \omega_3 \omega_{10} - 6c_s^2 \omega_3^3 \omega_{10} - 24c_s^4 \omega_3^3 \omega_{10} + 12v_2^3 \omega_3^2 \omega_{10}^2 - 8c_s^2 \omega_3^2 \omega_{10}^2 + 72v_2^4 \omega_3^2 \omega_{10} + 30v_2^3 \omega_3^3 \omega_{10} - 3c_s^4 \omega_3^3 \omega_{10}^2 - 3v_2^3 \omega_3^3 \omega_{10}^2 + 6c_s^4 \omega_3^3 \omega_{10} + 24c_s^2 \omega_3^2 \omega_{10} + 36v_2^3 \omega_3^3 - 12v_2^4 \omega_3^2 \omega_{10}^2 + 24c_s^4 \omega_3^2 \omega_{10}^2 - 72v_2^3 \omega_3^2 \omega_{10} - 30v_2^4 \omega_3^3 \omega_{10} - 36v_2^3 c_s^2 \omega_3 \omega_{10}^2 - 72v_2^4 \omega_3^2 + c_s^2 \omega_3^2 \omega_{10}^2 - 48c_s^4 \omega_3 \omega_{10}^2 - 12v_2^3 c_s^2 \omega_3^2 \omega_{10}^2 - 216v_2^3 c_s^2 \omega_3^2 + 24c_s^4 \omega_{10}^2 + 108v_2^3 c_s^2 \omega_3^3 - 24c_s^2 \omega_3 \omega_{10} - 72v_2^3 c_s^2 \omega_3^2 \omega_{10} + 12c_s^2 \omega_3 \omega_{10} + 6v_2^3 c_s^2 \omega_3^2 \omega_{10}^2 + 72v_2^3 \omega_3^2 + 144v_2^3 c_s^2 \omega_3^2 \omega_{10} + 24c_s^4 \omega_3 \omega_{10} - 36v_2^3 \omega_3^3$$

2.6.5 Conservation of momentum: ρv_3

$$\begin{aligned}
& v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_3 v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_2} + (v_3^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\
& \frac{2v_3 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\
& + (-2 - 3v_3^2 \omega_6 + 6v_3^2 + \omega_6 + 4c_s^2 - 2c_s^2 \omega_6) \frac{\delta_l^2}{\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_6) \frac{3v_3 \rho \delta_l^2}{\omega_6 \delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{c_s^2 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\
& (-2 + \omega_3) \frac{c_s^2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_2) \frac{c_s^2 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_3) \frac{c_s^2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\
& (-2 - v_3^2 \omega_6 + 2v_3^2 + \omega_6 + 6c_s^2 - 3c_s^2 \omega_6) \frac{v_3 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 - 3v_3^2 \omega_6 + 6v_3^2 + \omega_6 + 2c_s^2 - c_s^2 \omega_6) \frac{\rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (-1 + v_1^2 + 3c_s^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{v_1 \rho \delta_l^3}{6\omega_2 \omega_{12} \delta_t} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{v_3 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{v_3 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-1 + v_2^2 + 3c_s^2) \frac{v_3 v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_2 \frac{v_2 \rho \delta_l^3}{6\omega_{11} \omega_3 \delta_t} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega_2 - \omega_2^2) \frac{c_s^4 \delta_l^3}{6\omega_2^3 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\
& \frac{v_3 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 - \omega_3^2 + 12\omega_3) \frac{c_s^4 \delta_l^3}{6\omega_3^3 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{v_3 c_s^2 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_3 \frac{v_3 \rho \delta_l^3}{12\omega_8 \omega_2 \omega_6^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_4 \frac{v_3 \rho \delta_l^3}{12\omega_6^2 \omega_3 \delta_t \omega_{10}} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + C_5 \frac{\delta_l^3}{12\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-24 + 11v_3^2 \omega_6^2 - 60v_3^2 \omega_6 + 60v_3^2 + 5c_s^2 \omega_6^2 + 24\omega_6 + 36c_s^2 - 36c_s^2 \omega_6 - 4\omega_6^2) \frac{v_3 \rho \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (2c_s^4 + 3v_1^2 \omega_4 + 24v_1^2 c_s^2 + 6v_1^4 - \omega_4 c_s^4 - 12v_1^2 \omega_4 c_s^2 + \omega_4 c_s^2 - 6v_1^2 - 2c_s^2 - 3v_1^4 \omega_4) \frac{v_3 \delta_l^4}{24\omega_4 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 2\omega_4 - 5v_1^2 \omega_4 - 3\omega_4 c_s^2 + 10v_1^2 + 6c_s^2) \frac{v_3 v_1 \rho \delta_l^4}{12\omega_4 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_l^4}{24\omega_2^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + \\
& (3\omega_4 + v_1^2 \omega_9 + 3\omega_4 c_s^2 \omega_9 - 3v_1^2 \omega_4 - 9\omega_4 c_s^2 - \omega_9 + 3c_s^2 \omega_9 - \omega_4 \omega_9 + v_1^2 \omega_4 \omega_9) \frac{v_3 v_1 \rho \delta_l^4}{12\omega_4 \omega_9 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_1) \frac{v_3 c_s^4 \delta_l^4}{6\omega_1 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} \\
& + (-\omega_3^2 + 2\omega_2 \omega_3^2 - 2\omega_2 \omega_3 + \omega_{13} \omega_3 - \omega_{13} \omega_2 \omega_3 - \omega_2^2 + 2\omega_2^2 \omega_3 - \omega_2^2 \omega_3^2 + \omega_{13} \omega_2) \frac{c_s^4 \rho \delta_l^4}{\omega_{13} \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (-\omega_7 \omega_5 - \omega_7 + 3\omega_7 c_s^2 \omega_5 - 9c_s^2 \omega_5 + 3\omega_5 + \omega_7 v_2^2 - 3v_2^2 \omega_5 + 3\omega_7 c_s^2 + \omega_7 v_2^2 \omega_5) \frac{v_3 v_2 \rho \delta_l^4}{12\omega_7 \omega_5 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + \\
& (2c_s^4 - 12v_2^2 c_s^2 \omega_5 - 3v_2^4 \omega_5 + c_s^2 \omega_5 + 24v_2^2 c_s^2 + 6v_2^4 + 3v_2^2 \omega_5 - 6v_2^2 - 2c_s^2 - c_s^4 \omega_5) \frac{v_3 \delta_l^4}{24\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 - 3c_s^2 \omega_5 + 2\omega_5 - 5v_2^2 \omega_5 + 10v_2^2 + 6c_s^2) \frac{v_3 v_2 \rho \delta_l^4}{12\omega_5 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_7 \frac{\rho \delta_l^4}{24\omega_{11}^3 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^4} + C_8 \frac{v_1 c_s^2 \delta_l^4}{12\omega_4 \omega_2^2 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_9 \frac{c_s^2 \rho \delta_l^4}{12\omega_4 \omega_2^2 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& (3\omega_4 c_s^2 \omega_{12} + v_1^2 \omega_{12} + 3\omega_4 - 3v_1^2 \omega_4 - 9\omega_4 c_s^2 - \omega_{12} + v_1^2 \omega_4 \omega_{12} - \omega_4 \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_3 v_1 \rho \delta_l^4}{12\omega_4 \omega_{12} \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{10} \frac{c_s^4 \rho \delta_l^4}{12\omega_{13} \omega_1 \omega_3^2 \omega_5^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{11} \frac{c_s^4 \rho \delta_l^4}{12\omega_{13} \omega_1 \omega_2^2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{12} \frac{v_2 c_s^2 \delta_l^4}{12\omega_{11}^2 \omega_5 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{13} \frac{c_s^2 \rho \delta_l^4}{12\omega_{11} \omega_5 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& (3c_s^2 \omega_{11} - \omega_{11} \omega_5 - \omega_{11} - 9c_s^2 \omega_5 + v_2^2 \omega_{11} \omega_5 + 3\omega_5 - 3v_2^2 \omega_5 + v_2^2 \omega_{11} + 3c_s^2 \omega_{11} \omega_5) \frac{v_3 v_2 \rho \delta_l^4}{12\omega_{11} \omega_5 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{14} \frac{v_3 c_s^2 \delta_l^4}{12\omega_8^2 \omega_2^2 \omega_6^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{15} \frac{c_s^2 \rho \delta_l^4}{12\omega_8 \omega_3^2 \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{16} \frac{v_3 c_s^2 \delta_l^4}{12\omega_6^2 \omega_3^2 \delta_t \omega_{10}^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{17} \frac{c_s^2 \rho \delta_l^4}{12\omega_6^2 \omega_3^3 \delta_t \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{18} \frac{\rho \delta_l^4}{12\omega_8^2 \omega_3^2 \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{19} \frac{\rho \delta_l^4}{12\omega_6^3 \omega_3^3 \delta_t \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{20} \frac{v_3 \delta_l^4}{12\omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{21} \frac{\rho \delta_l^4}{12\omega_6^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 + 3v_1^2 \omega_{12} - 3c_s^2 \omega_2 \omega_{12} + 3v_1^2 \omega_2 - 3\omega_2 + \omega_2 \omega_{12} + 9c_s^2 \omega_2 - v_1^2 \omega_2 \omega_{12} - 3\omega_{12} - 6v_1^2 - 18c_s^2 + 9c_s^2 \omega_{12} \\
C_2 &= 6 + 9c_s^2 \omega_{11} - v_2^2 \omega_{11} \omega_3 + 9c_s^2 \omega_3 - 3\omega_{11} + \omega_{11} \omega_3 - 3c_s^2 \omega_{11} \omega_3 - 6v_2^2 - 18c_s^2 - 3\omega_3 + 3v_2^2 \omega_{11} + 3v_2^2 \omega_3 \\
C_3 &= -12v_3^2 \omega_6^2 + 3\omega_8 \omega_2 \omega_6^2 + 36c_s^2 \omega_2 \omega_6^2 + 12v_3^2 \omega_2 \omega_6^2 + 6v_3^2 \omega_8 \omega_6^2 - 12v_3^2 \omega_2 \omega_6 + 12v_3^2 \omega_8 \omega_2 + 36c_s^2 \omega_8 \omega_2 + 18c_s^2 \omega_8 \omega_6^2 + 6\omega_8 \omega_2 \omega_6 - 36c_s^2 \omega_2 \omega_6 - 12\omega_8 \omega_2 - 6\omega_8 \omega_6^2 - 36c_s^2 \omega_6^2 + 12\omega_2 \omega_6 - 3v_3^2 \omega_8 \omega_2 \omega_6^2 - 18c_s^2 \omega_8 \omega_2 \omega_6 - 11c_s^2 \omega_8 \omega_2 \omega_6^2 - 6v_3^2 \omega_8 \omega_2 \omega_6 - 12\omega_2 \omega_6^2 + 12\omega_6^2 \\
C_4 &= -12v_3^2 \omega_6^2 - 6\omega_6^2 \omega_{10} - 6v_3^2 \omega_6 \omega_3 \omega_{10} - 12\omega_3 \omega_{10} - 12\omega_6^2 \omega_3 - 36c_s^2 \omega_6 \omega_3 - 18c_s^2 \omega_6 \omega_3 \omega_{10} - 12v_3^2 \omega_6 \omega_3 + 3\omega_6^2 \omega_3 \omega_{10} + 12v_3^2 \omega_6^2 \omega_3 + 12v_3^2 \omega_3 \omega_{10} - 36c_s^2 \omega_6^2 + 6\omega_6 \omega_3 \omega_{10} - 11c_s^2 \omega_6^2 \omega_3 \omega_{10} + 36c_s^2 \omega_3 \omega_{10} + 36c_s^2 \omega_6^2 \omega_3 + 12\omega_6 \omega_3 + 6v_3^2 \omega_6^2 \omega_{10} - 3v_3^2 \omega_6^2 \omega_3 \omega_{10} + 18c_s^2 \omega_6^2 \omega_{10} + 12\omega_6^2 \\
C_5 &= -7v_3^2 \omega_6^2 + 12c_s^4 + 144v_3^2 c_s^2 - 144v_3^2 c_s^2 \omega_6 + c_s^4 \omega_6^2 + 24v_3^2 c_s^2 \omega_6^2 - 12c_s^4 \omega_6 + 36v_3^4 + 36v_3^2 \omega_6 - 36v_3^2 - c_s^2 \omega_6^2 + 7v_3^4 \omega_6^2 - 12c_s^2 - 36v_3^4 \omega_6 + 12c_s^2 \omega_6 \\
C_6 &= 72v_1^2 \omega_2^2 + 72v_1^4 \omega_2^2 \omega_{12} + 30v_1^2 \omega_2^3 \omega_{12} + 12c_s^2 \omega_2 \omega_{12}^2 + 72v_1^2 c_s^2 \omega_2 \omega_{12} + 3v_1^4 \omega_2^3 \omega_{12} - 36v_1^2 \omega_2^3 + 24c_s^4 \omega_2 \omega_{12} + 24c_s^4 \omega_{12}^2 + 12v_1^2 \omega_2^2 \omega_{12}^2 - 72v_1^2 \omega_2^2 \omega_{12} - 30v_1^4 \omega_2^3 \omega_{12} - 36v_1^2 c_s^2 \omega_2 \omega_{12}^2 - 48c_s^4 \omega_2 \omega_{12}^2 - 3v_1^2 \omega_2^3 \omega_{12}^2 - 24c_s^2 \omega_2 \omega_{12}^2 - 12v_1^4 \omega_2^3 \omega_{12} + 36v_1^4 \omega_2^3 + 24c_s^2 \omega_2^2 \omega_{12} + 6c_s^4 \omega_2^2 \omega_{12} - 72v_1^2 c_s^2 \omega_2^2 \omega_{12} - 72v_1^4 \omega_2^2 + c_s^2 \omega_3^2 \omega_{12}^2 - 12v_1^2 c_s^2 \omega_2^2 \omega_{12} + 24c_s^4 \omega_2^2 \omega_{12} + 144v_1^2 c_s^2 \omega_2^2 \omega_{12} - 216v_1^2 c_s^2 \omega_2^2 - 24c_s^4 \omega_2^2 \omega_{12} - 6c_s^2 \omega_3^2 \omega_{12} - 3c_s^4 \omega_3^2 \omega_{12} + 6v_1^2 c_s^2 \omega_3^2 \omega_{12} + 108v_1^2 c_s^2 \omega_2^2 - 8c_s^2 \omega_3^2 \omega_{12}^2
\end{aligned}$$

$$C_7 = 72v_2^4\omega_{11}\omega_3^2 + 36v_2^4\omega_3^3 - 216v_2^3c_s^2\omega_3^2 - 8c_s^2\omega_{11}\omega_3^2 - 48c_s^4\omega_{11}^2\omega_3 + 72v_2^3c_s^2\omega_{11}\omega_3 - 30v_2^4\omega_{11}\omega_3^3 + c_s^2\omega_{11}^2\omega_3^3 + 108v_2^3c_s^2\omega_3^3 - 72v_2^4\omega_3^3 - 72v_2^2\omega_{11}\omega_3^2 + 24c_s^4\omega_{11}^2\omega_3^2 + 144v_2^3c_s^2\omega_{11}\omega_3^2 + 12c_s^2\omega_{11}^2\omega_3^2 + 30v_2^3\omega_{11}\omega_3^3 - 72v_2^2c_s^2\omega_{11}\omega_3^3 - 3c_s^4\omega_{11}^2\omega_3^3 - 24c_s^2\omega_{11}\omega_3^3 - 3v_2^3\omega_{11}^2\omega_3^3 + 6v_2^3c_s^2\omega_{11}^2\omega_3^3 + 6c_s^4\omega_{11}\omega_3^3 + 72v_2^2\omega_3^3 + 12v_2^2\omega_{11}^2\omega_3^3 - 36v_2^2\omega_3^3 - 24c_s^4\omega_{11}\omega_3^3 - 12v_2^3c_s^2\omega_{11}^2\omega_3^3 + 24c_s^4\omega_{11}\omega_3^3 + 3v_2^4\omega_{11}^2\omega_3^3 - 36v_2^2c_s^2\omega_{11}\omega_3^3 + 24c_s^4\omega_{11}^2 - 6c_s^2\omega_{11}\omega_3^3 - 12v_2^4\omega_{11}^2\omega_3^3 + 24c_s^2\omega_{11}\omega_3^2$$

$$C_8 = 12\omega_4\omega_2\omega_{12}^2 - 36\omega_4c_s^2\omega_{12} + 3\omega_4c_s^2\omega_2^2\omega_{12}^2 + 18c_s^2\omega_2\omega_{12}^2 - \omega_2^2\omega_{12}^2 + 18\omega_4c_s^2\omega_2^2 + v_1^2\omega_2^2\omega_{12}^2 + 18v_1^2\omega_4\omega_2\omega_{12} - 6v_1^2\omega_2^2\omega_{12} - 12v_1^2\omega_4\omega_2\omega_{12}^2 + 36c_s^2\omega_2\omega_{12} - 36\omega_4c_s^2\omega_2 + 6\omega_2^2\omega_{12} - 12v_1^2\omega_{12}^2 - 18\omega_4\omega_2\omega_{12} + 36\omega_4c_s^2\omega_{12}^2 - 9\omega_4c_s^2\omega_2^2\omega_{12} - 12\omega_4\omega_{12}^2 - 12\omega_2\omega_{12} - 36c_s^2\omega_{12}^2 - 18c_s^2\omega_2^2\omega_{12} + 3\omega_4\omega_2^2\omega_{12} + 12\omega_4\omega_2 + 54\omega_4c_s^2\omega_2\omega_{12} + 12v_1^2\omega_4\omega_{12}^2 + v_1^2\omega_4\omega_2^2\omega_{12} + 12v_1^2\omega_2\omega_{12} - 12v_1^2\omega_4\omega_2 + 6v_1^2\omega_4\omega_2^2 - 12v_1^2\omega_4\omega_{12} - 3v_1^2\omega_4\omega_2^2\omega_{12} + 6v_1^2\omega_2\omega_{12}^2 - \omega_4\omega_2^2\omega_{12}^2 - 6\omega_4\omega_2^2 + 12\omega_{12}^2 - 36\omega_4c_s^2\omega_2\omega_{12} + 12\omega_4\omega_{12} - 6\omega_2\omega_{12}^2 + 3c_s^2\omega_2^2\omega_{12}^2$$

$$C_9 = -12\omega_4c_s^2\omega_{12} + 36v_1^2\omega_2^2 + 3v_1^2\omega_3^2\omega_{12} - 18\omega_4c_s^2\omega_2^2 - \omega_4c_s^2\omega_3^2\omega_{12} - 18v_1^2\omega_3^2 + 6\omega_4c_s^2\omega_3^2 - \omega_3^2\omega_{12} + 18v_1^2\omega_2^2\omega_{12} - 12c_s^2\omega_2\omega_{12} + 12\omega_4c_s^2\omega_2 - 6\omega_2^3\omega_{12} - 5\omega_4c_s^2\omega_2^3\omega_{12} - 12\omega_2^2 + 12\omega_2\omega_{12} + 6c_s^2\omega_2^3\omega_{12} + \omega_4\omega_2^3\omega_{12} - 12\omega_4\omega_2 + 18\omega_4c_s^2\omega_2\omega_{12} - 36v_1^2\omega_2\omega_{12} + 6\omega_2^3 + 36v_1^2\omega_4\omega_2 - 6\omega_4\omega_2^3 - 6c_s^2\omega_2^3 - 54v_1^2\omega_4\omega_2^3 + c_s^2\omega_2^3\omega_{12} - 3v_1^2\omega_4\omega_2^3\omega_{12} + 18v_1^2\omega_4\omega_2^3 + 12c_s^2\omega_2^3 + 18\omega_4\omega_2^3$$

$$C_{10} = -2\omega_{13}\omega_1\omega_2^2\omega_3^2 + 12\omega_{13}\omega_2\omega_3^2 - 12\omega_1\omega_3^2\omega_3^2 - 12\omega_1\omega_2^2\omega_3 + 12\omega_1\omega_2^2\omega_3^2 - \omega_{13}\omega_1\omega_2^2\omega_3^2 + 24\omega_1\omega_2^2\omega_3 - 12\omega_1\omega_2^3 - 6\omega_{13}\omega_1\omega_2^2\omega_3 + 12\omega_2^3\omega_3^2 + 12\omega_{13}\omega_1\omega_2\omega_3 - 2\omega_{13}\omega_2^2\omega_3^2 + 12\omega_{13}\omega_2^2 - 12\omega_2^2\omega_3^2 - 24\omega_{13}\omega_1\omega_2^3 - 6\omega_{13}\omega_2^2\omega_3 + 24\omega_{13}\omega_1\omega_2\omega_3^2 - 6\omega_{13}\omega_2^2\omega_3^2 - 12\omega_2^3\omega_3$$

$$C_{11} = 12\omega_{13}\omega_3^3 - 2\omega_{13}\omega_1\omega_2^2\omega_3^2 - 12\omega_2\omega_3^3 - \omega_{13}\omega_1\omega_2^2\omega_3^2 - 6\omega_{13}\omega_2\omega_3^3 + 12\omega_1\omega_2^2\omega_3^2 - 12\omega_1\omega_2^2\omega_3^3 + 24\omega_{13}\omega_1\omega_2^2\omega_3 - 24\omega_{13}\omega_1\omega_2^2 + 12\omega_{13}\omega_2^2\omega_3 + 24\omega_1\omega_2\omega_3^3 + 12\omega_{13}\omega_1\omega_2\omega_3 - 12\omega_1\omega_2\omega_3^2 - 12\omega_1\omega_3^3 - 12\omega_2^2\omega_3^2 - 2\omega_{13}\omega_2^2\omega_3^2 - 6\omega_{13}\omega_1\omega_2\omega_3^2 - 6\omega_{13}\omega_2^2\omega_3^2 + 12\omega_2^2\omega_3^3$$

$$C_{12} = -9c_s^2\omega_{11}\omega_5\omega_3^2 - \omega_{11}^2\omega_5\omega_3^2 + 12\omega_{11}^2 + 6\omega_{11}\omega_3^2 + 3c_s^2\omega_{11}^2\omega_3^2 - 36c_s^2\omega_5\omega_3 + 36c_s^2\omega_{11}^2\omega_5 + 18v_2^2\omega_{11}\omega_5\omega_3 + 12\omega_{11}\omega_5 + 12v_2^2\omega_{11}\omega_3 - 6v_2^2\omega_{11}\omega_3^2 - 12v_2^2\omega_{11}\omega_5 - 12\omega_{11}\omega_3 + 18c_s^2\omega_{11}^2\omega_3 - 3v_2^2\omega_{11}\omega_5\omega_3^2 + 18c_s^2\omega_5\omega_3^2 - 36c_s^2\omega_{11}^2 + 54c_s^2\omega_{11}\omega_5\omega_3 + 12\omega_{11}^2\omega_5\omega_3 + 36c_s^2\omega_{11}\omega_3 - 6\omega_{11}^2\omega_3 - 6\omega_5\omega_3^2 + v_2^2\omega_{11}^2\omega_3^2 + v_2^2\omega_{11}^2\omega_5\omega_3^2 + 12v_2^2\omega_{11}^2\omega_5 - 12v_2^2\omega_5\omega_3 - 12v_2^2\omega_{11}^2 - 18\omega_{11}\omega_5\omega_3 - 36c_s^2\omega_{11}^2\omega_5\omega_3 + 3\omega_{11}\omega_5\omega_3^2 + 3c_s^2\omega_{11}^2\omega_5\omega_3^2 + 6v_2^2\omega_{11}^2\omega_3 - 12v_2^2\omega_{11}^2\omega_5\omega_3 + 6v_2^2\omega_5\omega_3^2 - 18c_s^2\omega_{11}\omega_3^2 - \omega_{11}^2\omega_3^2 - 12\omega_{11}^2\omega_5 + 12\omega_5\omega_3 - 36c_s^2\omega_{11}\omega_5$$

$$C_{13} = -5c_s^2\omega_{11}\omega_5\omega_3^2 + 6\omega_3^3 - 6\omega_{11}\omega_3^3 + 12c_s^2\omega_5\omega_3 - 12\omega_3^2 - c_s^2\omega_{11}\omega_5\omega_3^2 - 36v_2^2\omega_{11}\omega_3 - \omega_{11}\omega_3^3 + 12c_s^2\omega_3^2 + 6c_s^2\omega_5\omega_3^2 + 18v_2^2\omega_{11}\omega_3^2 + 12\omega_{11}\omega_3 - 3v_2^2\omega_{11}\omega_5\omega_3^2 + 3v_2^2\omega_{11}\omega_3^3 - 18c_s^2\omega_5\omega_3^2 - 6c_s^2\omega_3^3 + 18c_s^2\omega_{11}\omega_5\omega_3 - 12c_s^2\omega_{11}\omega_3 + 18\omega_5\omega_3^2 + 36v_2^2\omega_3^2 - 6\omega_5\omega_3^2 + 36v_2^2\omega_5\omega_3 - 18v_2^2\omega_3^3 + \omega_{11}\omega_5\omega_3^2 - 54v_2^2\omega_5\omega_3^2 + c_s^2\omega_{11}\omega_3^3 + 6c_s^2\omega_{11}\omega_3^2 + 18v_2^2\omega_5\omega_3^2 - 12\omega_5\omega_3 - 12c_s^2\omega_{11}\omega_5$$

$$C_{14} = -12\omega_2^2\omega_6^2 + 18c_s^2\omega_8\omega_2^2\omega_6^2 - 18c_s^2\omega_8\omega_2^2\omega_6^3 - 12\omega_8\omega_2\omega_6^2 + 12\omega_2^2\omega_6^2 - \omega_2^2\omega_2^2\omega_6^3 - 12v_3^2\omega_2\omega_6^3 - 36c_s^2\omega_2\omega_6^3 - 4\omega_8^2\omega_2^2\omega_6^2 - 18\omega_8\omega_2\omega_6^3 - 12\omega_2^2\omega_6^3 + 18c_s^2\omega_8\omega_2^2\omega_6^2 - 40c_s^2\omega_8^2\omega_2\omega_6^3 + 18\omega_8^2\omega_2\omega_6^2 - 12\omega_8^2\omega_6^2 - 36c_s^2\omega_8\omega_6^3 + 6v_3^2\omega_8\omega_2^2\omega_6^2 - 12v_3^2\omega_8^2\omega_2\omega_6^3 - 12v_3^2\omega_8\omega_6^3 + 6v_3^2\omega_8^2\omega_2\omega_6^2 - 6v_3^2\omega_8\omega_2^2\omega_6^3 + 12\omega_8^2\omega_6^2 + 12v_3^2\omega_8^2\omega_6^2 + 18v_3^2\omega_8\omega_2\omega_6^3 - 54c_s^2\omega_8^2\omega_2\omega_6^2 + 4v_3^2\omega_8^2\omega_2\omega_6^2 - 36c_s^2\omega_8^2\omega_6^2 - 12v_3^2\omega_8^2\omega_6^2 + 36c_s^2\omega_8^2\omega_6^3 + 12\omega_8\omega_6^2 + v_3^2\omega_8^2\omega_2^2\omega_6^3 + 12v_3^2\omega_8\omega_2\omega_6^2 + 6\omega_8\omega_2^2\omega_6^3 + 12\omega_2\omega_6^3 - 6\omega_8^2\omega_2\omega_6^2 + 36c_s^2\omega_2^2\omega_6^3 + 5c_s^2\omega_8^2\omega_2^2\omega_6^3 + 36c_s^2\omega_8\omega_2\omega_6^2 - 12v_3^2\omega_2^2\omega_6^2 + 12v_3^2\omega_8^2\omega_2^2 + 36c_s^2\omega_8^2\omega_2^2 + 54c_s^2\omega_8\omega_2\omega_6^3 - 18v_3^2\omega_8^2\omega_2\omega_6^2 + 12c_s^2\omega_8^2\omega_2^2\omega_6^2 + 12\omega_8^2\omega_2\omega_6^3 - 36c_s^2\omega_2^2\omega_6^2 - 6\omega_8\omega_2^2\omega_6^2 + 12v_3^2\omega_2^2\omega_6^3$$

$$C_{15} = -12c_s^2\omega_8\omega_2^2 + 24\omega_2^2\omega_6^2 + 12c_s^2\omega_2\omega_6^2 + 24\omega_2^3\omega_6 - 4c_s^2\omega_8\omega_2^2\omega_6^2 + 36v_3^2\omega_8\omega_2^2\omega_6 + 36v_3^2\omega_2\omega_6^2 - 36v_3^2\omega_8\omega_2^2 - 12\omega_2^3\omega_6^2 + 36v_3^2\omega_2^3 + 12c_s^2\omega_8\omega_2^2\omega_6 - c_s^2\omega_8\omega_2^2\omega_6^2 - 12c_s^2\omega_8\omega_6^2 - 24\omega_2^2\omega_6 + 12\omega_8\omega_2\omega_6 + 36v_3^2\omega_2^2\omega_6^2 + 24c_s^2\omega_2^2\omega_6 - 12\omega_8\omega_2^2\omega_6 + 72v_3^2\omega_2^2\omega_6 - 12\omega_2^3 + 12c_s^2\omega_2^2\omega_6^2 - 12c_s^2\omega_8\omega_2\omega_6 - 24c_s^2\omega_2^3\omega_6 + 12c_s^2\omega_2^3 + 18c_s^2\omega_8\omega_2\omega_6^2 - 36v_3^2\omega_8\omega_2\omega_6 - 72v_3^2\omega_2^2\omega_6^2 + 12\omega_8\omega_2^2 - 24c_s^2\omega_2^2\omega_6^2 - 12\omega_2\omega_6^2 - 72v_3^2\omega_2^2\omega_6$$

$$C_{16} = 12\omega_6^3\omega_3 - 12v_3^2\omega_6^3\omega_3\omega_{10} + 54c_s^2\omega_6^3\omega_3\omega_{10} - 6\omega_6^3\omega_3\omega_{10} + 12v_3^2\omega_3^2\omega_{10} - 12\omega_6^3\omega_{10} + 36c_s^2\omega_3^2\omega_{10} + 12\omega_6^2\omega_3^2 + 18\omega_6\omega_3^2\omega_{10} + 6\omega_6^3\omega_3\omega_{10} - 6v_3^2\omega_6^2\omega_3\omega_{10} + 12c_s^2\omega_6^2\omega_3\omega_{10} + 18c_s^2\omega_6^2\omega_3\omega_{10} + 4v_3^2\omega_6^2\omega_3\omega_{10} - \omega_6^2\omega_3\omega_{10} + 12\omega_6^3\omega_{10} - 12\omega_6^2\omega_3\omega_{10} - 40c_s^2\omega_6^2\omega_3\omega_{10} + 18v_3^2\omega_6^2\omega_3\omega_{10} - 12\omega_6^3\omega_3^2 + 12\omega_6^2\omega_{10} - 18v_3^2\omega_6\omega_3\omega_{10} + 5c_s^2\omega_6^2\omega_3\omega_{10} - 6v_3^2\omega_6^2\omega_3\omega_{10} - 12v_3^2\omega_6^3\omega_{10} - 6\omega_6^2\omega_3\omega_{10} + 36c_s^2\omega_6^2\omega_3^2 - 36c_s^2\omega_6^2\omega_{10} - 12v_3^2\omega_6^2\omega_{10} + 12v_3^2\omega_6^3\omega_3 + 12\omega_6^2\omega_3\omega_{10} + 36c_s^2\omega_6^2\omega_3\omega_{10} - 6v_3^2\omega_6^2\omega_3\omega_{10} - 36c_s^2\omega_6^2\omega_3\omega_{10} - 36c_s^2\omega_6^2\omega_3\omega_{10} - 12v_3^2\omega_6^2\omega_{10} - 12v_3^2\omega_6^3\omega_3 + 12v_3^2\omega_6^2\omega_3\omega_{10} + 18c_s^2\omega_6^2\omega_3\omega_{10} - 18\omega_6^2\omega_3\omega_{10} - 36c_s^2\omega_6^2\omega_3 - 12v_3^2\omega_6^2\omega_3 - 54c_s^2\omega_6\omega_3\omega_{10} - 4\omega_6^2\omega_3\omega_{10} + v_3^2\omega_6^2\omega_3\omega_{10} - 18c_s^2\omega_6^2\omega_3\omega_{10} + 12v_3^2\omega_6^2\omega_{10}$$

$$C_{17} = -24c_s^2\omega_6\omega_3^3 - 12\omega_6^2\omega_3^3 - 12\omega_3^3 - 36v_3^2\omega_6\omega_3\omega_{10} - c_s^2\omega_6^2\omega_3^3\omega_{10} + 72v_3^2\omega_6\omega_3^2 + 24\omega_6^2\omega_3^2 + 24c_s^2\omega_6\omega_3^2 - 72v_3^2\omega_6\omega_3^3 - 12\omega_6\omega_3^2\omega_{10} - 4c_s^2\omega_6^2\omega_3\omega_{10} - 12c_s^2\omega_6^2\omega_{10} - 12\omega_6^2\omega_3 - 12c_s^2\omega_6\omega_3\omega_{10} + 12c_s^2\omega_3^3 - 36v_3^2\omega_3^2\omega_{10} + 36v_3^2\omega_6^2\omega_3 + 12c_s^2\omega_6\omega_3^2\omega_{10} + 12\omega_6\omega_3\omega_{10} + 18c_s^2\omega_6^2\omega_3\omega_{10} + 12\omega_2^3\omega_{10} + 12c_s^2\omega_6^2\omega_3 - 24c_s^2\omega_6^2\omega_3^2 - 24\omega_6\omega_3^2 + 36v_3^2\omega_6^2\omega_3^3 + 24\omega_6\omega_3^3 + 12c_s^2\omega_6^2\omega_3^2 - 12c_s^2\omega_6^2\omega_{10} - 72v_3^2\omega_6^2\omega_3^2 + 36v_3^2\omega_6\omega_2^2\omega_{10} + 36v_3^2\omega_3^3$$

$$C_{18} = -72v_3^2\omega_8\omega_3^2\omega_6^2 - 108v_3^2c_s^2\omega_3^2\omega_6^2 + 18c_s^2\omega_8\omega_2^2\omega_6^3 - c_s^4\omega_2^2\omega_3^2\omega_6^3 + 198v_3^2c_s^2\omega_8\omega_2^2\omega_6^2 - 12c_s^4\omega_8^2\omega_2^2\omega_6 - 12c_s^2\omega_8\omega_2^2\omega_6^2 + 108v_3^2c_s^2\omega_3^2\omega_6^3 + 39v_3^2\omega_8\omega_2^2\omega_6^3 + 6c_s^2\omega_8\omega_2\omega_6^3 - 6v_3^4\omega_8^2\omega_2^2\omega_6^3 - 90v_3^4\omega_8\omega_2^2\omega_6 - 99v_3^2c_s^2\omega_8\omega_2^2\omega_6^3 + c_s^4\omega_8^2\omega_2^2\omega_6^2 + 36v_3^2c_s^2\omega_8\omega_2^2\omega_6^2 + 13c_s^4\omega_8^2\omega_2^2\omega_6^3 - 18v_3^2c_s^2\omega_8\omega_2\omega_6^3 - 12c_s^4\omega_8^2\omega_2^2\omega_6 + 19v_3^4\omega_8^2\omega_2^2\omega_6^2 - 6c_s^2\omega_8\omega_2^2\omega_6^3 + 12c_s^4\omega_8\omega_2\omega_6^3 + 4v_3^4\omega_8^2\omega_2^2\omega_6^3 - 108v_3^2c_s^2\omega_8\omega_2^2\omega_6 + 6c_s^4\omega_8^2\omega_2^2\omega_6^2 + 54v_3^2c_s^2\omega_8\omega_2^2\omega_6^3 + 36v_3^2\omega_8\omega_2^2\omega_6 + 6c_s^2\omega_8\omega_2^2\omega_6^2 - 108v_3^2c_s^2\omega_2^2\omega_6^3 - 36v_3^2\omega_8\omega_2^2\omega_6^3 + 252v_3^2c_s^2\omega_8\omega_2^2 + 36v_3^2\omega_3^2\omega_6^2 + 36v_3^2c_s^2\omega_8\omega_2\omega_6^3 + 72v_3^4\omega_8\omega_2^2\omega_6^2 + 12c_s^4\omega_8^2\omega_3^2 - 18c_s^4\omega_8\omega_2^2\omega_6^3 + 18v_3^2c_s^2\omega_8\omega_2^2\omega_6^2 + 12c_s^2\omega_8^2\omega_2^2\omega_6^2 + 12c_s^4\omega_8\omega_2^2\omega_6^2 - 36v_3^2\omega_8\omega_2^2\omega_6^2 - 24c_s^4\omega_8^2\omega_2\omega_6^3 - 39v_3^4\omega_8\omega_2^2\omega_6^3 - 306v_3^2c_s^2\omega_8^2\omega_2^2\omega_6 + 72v_3^4\omega_8\omega_2^2 + 6v_3^2\omega_8\omega_2^2\omega_6^3 - 36v_3^4\omega_2^2\omega_6^3 - c_s^2\omega_8\omega_2^2\omega_6^2 + 90v_3^2\omega_8\omega_2^2\omega_6 - 5c_s^2\omega_8\omega_2^2\omega_6^3 - 36v_3^4\omega_2^2\omega_6^2 - 19v_3^2\omega_8^2\omega_2^2\omega_6^2 + 12c_s^2\omega_8^2\omega_2^2\omega_6 - 12c_s^2\omega_8^2\omega_6^2 + 60v_3^2c_s^2\omega_2^2\omega_6^2\omega_6^2 + 6c_s^4\omega_8\omega_2^2\omega_6^3 - 4v_3^2\omega_2^2\omega_6^2\omega_6^3 + 36v_3^4\omega_2^2\omega_6^3 - 12c_s^2\omega_8\omega_2\omega_6^3 - 6c_s^2\omega_8\omega_2^2\omega_6^2 + 12c_s^4\omega_8\omega_3^2 - 72v_3^2\omega_8\omega_2^2 - 6c_s^4\omega_8\omega_2\omega_6^2 - 36v_3^2\omega_8\omega_2^2\omega_6 + 12v_3^2c_s^2\omega_8\omega_2^2\omega_6^3 + 36v_3^2\omega_8\omega_2^2\omega_6^3 - 36v_3^2c_s^2\omega_8\omega_2^2\omega_6 + 36v_3^2\omega_2^2\omega_6^3$$

$$C_{19} = 72v_3^4\omega_3^3\omega_{10}^2 - 18v_3^2c_s^2\omega_6^3\omega_3\omega_{10}^2 + 36v_3^4\omega_6^3\omega_3\omega_{10} + 13c_s^4\omega_6^3\omega_3\omega_{10}^2 + 60v_3^2c_s^2\omega_6^2\omega_3\omega_{10}^2 + 108v_3^2c_s^2\omega_6^3\omega_3^3 - 19v_3^2\omega_6^2\omega_3\omega_{10}^2 + 6c_s^2\omega_6^2\omega_3\omega_{10} - 12c_s^2\omega_6^3\omega_3\omega_{10} + 36v_3^2c_s^2\omega_6^2\omega_3\omega_{10} - 108v_3^2c_s^2\omega_6^2\omega_3^2 - 12c_s^4\omega_6\omega_3\omega_{10} - 36v_3^4\omega_6\omega_3\omega_{10} + 4v_3^4\omega_6^2\omega_3\omega_{10}^2 + 6c_s^4\omega_6^3\omega_3\omega_{10} + 12c_s^4\omega_3^3\omega_{10} - 6c_s^2\omega_6^2\omega_3\omega_{10} - 72v_3^2\omega_3^2\omega_{10} - 12c_s^2\omega_6^2\omega_3\omega_{10} - 108v_3^2c_s^2\omega_6^2\omega_3 - 18v_3^2c_s^2\omega_6^2\omega_3^2 - 90v_3^4\omega_6\omega_3\omega_{10} - c_s^4\omega_6^3\omega_3\omega_{10} - 39v_3^4\omega_6^3\omega_3\omega_{10} - c_s^2\omega_6^2\omega_3\omega_{10}^2 - 72v_3^2\omega_6^2\omega_3\omega_{10} + 6c_s^2\omega_6^2\omega_3\omega_{10} + 36v_3^2c_s^2\omega_6^2\omega_3\omega_{10} - 18c_s^4\omega_6^2\omega_3\omega_{10} - 12c_s^4\omega_3^3\omega_{10} + 12c_s^4\omega_6^3\omega_{10} - 36v_3^2\omega_6^3\omega_3^3 - 5c_s^2\omega_6^2\omega_3\omega_{10}^2 - 36v_3^2\omega_6^2\omega_3\omega_{10} + 12c_s^4\omega_6\omega_3\omega_{10} + 54v_3^2c_s^2\omega_6^2\omega_3\omega_{10} - 6c_s^4\omega_6^2\omega_3\omega_{10} + 19v_3^4\omega_6^2\omega_3\omega_{10} - 36v_3^4\omega_6^2\omega_3^3 - 36v_3^2c_s^2\omega_6\omega_3\omega_{10}^2 - 6c_s^2\omega_6^2\omega_3\omega_{10} - 4v_3^2\omega_6^2\omega_3\omega_{10}^2 + 36v_3^2\omega_3^3\omega_{10} + 36v_3^2\omega_6\omega_3\omega_{10} + 12c_s^2\omega_6\omega_3\omega_{10}^2 + 6c_s^4\omega_6^2\omega_3\omega_{10} - 108v_3^2c_s^2\omega_6\omega_3\omega_{10} + 12v_3^2c_s^2\omega_6^2\omega_3\omega_{10} + 36v_3^4\omega_6\omega_3\omega_{10} + 12c_s^4\omega_6^2\omega_3\omega_{10} - 306v_3^2c_s^2\omega_6\omega_3\omega_{10}^2 + 252v_3^2c_s^2\omega_3^3\omega_{10} - 99v_3^2c_s^2\omega_6^2\omega_3\omega_{10} + 39v_3^2\omega_6^2\omega_3\omega_{10} + 36v_3^2\omega_6^2\omega_3^3 + 90v_3^2\omega_6\omega_3\omega_{10}^2 - 24c_s^4\omega_6\omega_3\omega_{10} - 3v_3^2c_s^2\omega_6^2\omega_3\omega_{10}^2 + 72v_3^4\omega_6^2\omega_3\omega_{10} + c_s^4\omega_6^2\omega_3\omega_{10} - 36v_3^4\omega_6^2\omega_3^3 + 12c_s^2\omega_6\omega_3\omega_{10}^2 + 6v_3^2\omega_6^2\omega_3\omega_{10}^2 + 18c_s^2\omega_6^2\omega_3\omega_{10}$$

$$\begin{aligned}
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_2\delta_l^4}{12\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_2^3} + C_3 \frac{v_2\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2^3} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2^3} + C_4 \frac{\delta_l^4}{72\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4\omega_1 + 6c_s^2\omega_1 + 10v_2^2\omega_1 + 6\omega_1\omega_2 - 8\omega_2 - 15v_2^2\omega_1\omega_2 + 20v_2^2\omega_2 - 9c_s^2\omega_1\omega_2 + 12c_s^2\omega_2) \frac{v_2\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_1v_3\delta_l^4}{12\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_1^3\partial x_3} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^3\partial x_3} + C_5 \frac{v_1\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + C_6 \frac{v_3\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2\partial x_3} \\
& + C_7 \frac{v_2\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2\partial x_3} + C_8 \frac{v_3\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2\partial x_3} + C_9 \frac{v_1\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2\partial x_3} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_2v_3\delta_l^4}{12\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_2^3\partial x_3} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_2^3\partial x_3} + C_{10} \frac{v_2\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_2^3\partial x_3} + \\
& (3v_1^2\omega_1 - 2\omega_1 + 2c_s^2\omega_1 + 2\omega_2 - 3v_3^2\omega_2 + 3\omega_1v_3^2 + 6c_s^2\omega_1\omega_2 - 14c_s^2\omega_2 - 3v_1^2\omega_2) \frac{c_s^2\delta_l^4}{36\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2\partial x_3^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_3^2} + C_{11} \frac{v_2\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{12} \frac{v_1\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + \\
& (-2\omega_1 + 2c_s^2\omega_1 + 3v_2^2\omega_1 + 2\omega_2 - 3v_3^2\omega_2 + 3\omega_1v_3^2 - 3v_2^2\omega_2 + 6c_s^2\omega_1\omega_2 - 14c_s^2\omega_2) \frac{c_s^2\delta_l^4}{36\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_2^2\partial x_3^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_2^2\partial x_3^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_3\delta_l^4}{12\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^3} + C_{13} \frac{v_3\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_3^3} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_3^3} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2v_3\delta_l^4}{12\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_2\partial x_3^3} + C_{14} \frac{v_3\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_2\partial x_3^3} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_2\partial x_3^3} + C_{15} \frac{\delta_l^4}{72\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4\omega_1 + 6c_s^2\omega_1 + 6\omega_1\omega_2 - 8\omega_2 + 20v_3^2\omega_2 + 10\omega_1v_3^2 - 9c_s^2\omega_1\omega_2 + 12c_s^2\omega_2 - 15\omega_1v_3^2\omega_2) \frac{v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$C_1 = -6v_1^2\omega_1 - 2c_s^2\omega_1 + 12v_1^4\omega_2 + 48v_1^2c_s^2\omega_2 + 4c_s^4\omega_2 + 2c_s^4\omega_1 - 36v_1^2c_s^2\omega_1\omega_2 + 6v_1^4\omega_1 + 24v_1^2c_s^2\omega_1 - 9v_1^4\omega_1\omega_2 + 3c_s^2\omega_1\omega_2 - 4c_s^2\omega_2 - 12v_1^2\omega_2 - 3c_s^4\omega_1\omega_2 + 9v_1^2\omega_1\omega_2$$

$$C_2 = 4v_1^2\omega_4\omega_2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 18\omega_4v_2^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 - 9v_1^2\omega_4\omega_1\omega_2 + 6\omega_4c_s^2\omega_2\omega_3 + 18\omega_4v_2^2\omega_1\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9v_1^2\omega_1\omega_2\omega_3 + 6v_1^2\omega_4\omega_1\omega_2\omega_3 + 2v_1^2\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$C_3 = 6\omega_4v_2^2\omega_1\omega_2\omega_3 - 18v_1^2\omega_4\omega_2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 - 9\omega_4v_2^2\omega_1\omega_2 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 4\omega_4v_2^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 - 9v_2^2\omega_1\omega_2\omega_3 + 2\omega_4v_2^2\omega_1\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 + 18v_1^2\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$C_4 = 12v_2^4\omega_2 - 2c_s^2\omega_1 - 9v_2^4\omega_1\omega_2 - 6v_2^2\omega_1 + 4c_s^4\omega_2 + 9v_2^2\omega_1\omega_2 + 48c_s^2v_2^2\omega_2 + 2c_s^4\omega_1 + 24c_s^2v_2^2\omega_1 - 12v_2^2\omega_2 + 3c_s^2\omega_1\omega_2 - 4c_s^2\omega_2 - 36c_s^2v_2^2\omega_1\omega_2 + 6v_2^4\omega_1 - 3c_s^4\omega_1\omega_2$$

$$C_5 = 4v_1^2\omega_4\omega_2\omega_3 + 18\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 12\omega_4c_s^2\omega_1\omega_3 - 9v_1^2\omega_4\omega_1\omega_2 + 6\omega_4c_s^2\omega_2\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9v_1^2\omega_1\omega_2\omega_3 + 6v_1^2\omega_4\omega_1\omega_2\omega_3 + 2v_1^2\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 - 18\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$C_6 = 2\omega_4\omega_1v_3^2\omega_3 + 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 6\omega_4c_s^2\omega_1\omega_3 - 6\omega_4c_s^2\omega_2\omega_3 - 9\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 + 9\omega_1v_3^2\omega_2\omega_3 - 2\omega_4v_3^2\omega_2\omega_3 - 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$\begin{aligned}
C_7 &= 27c_s^2\omega_1\omega_2\omega_3 - 9\omega_4v_2^2\omega_1\omega_2 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 2\omega_4v_2^2\omega_2\omega_3 + 6\omega_4c_s^2\omega_1\omega_3 - 6\omega_4c_s^2\omega_2\omega_3 + 9v_2^2\omega_1\omega_2\omega_3 + 2\omega_4v_2^2\omega_1\omega_3 - 9\omega_1\omega_2\omega_3 - \\
& 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_8 &= 2\omega_4\omega_1v_3^2\omega_3 + 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 6\omega_4c_s^2\omega_1\omega_3 - 6\omega_4c_s^2\omega_2\omega_3 - 9\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 + 9\omega_1v_3^2\omega_2\omega_3 - 2\omega_4v_3^2\omega_2\omega_3 - \\
& 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_9 &= -2v_1^2\omega_4\omega_2\omega_3 + 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 6\omega_4c_s^2\omega_1\omega_3 - 9v_1^2\omega_4\omega_1\omega_2 - 6\omega_4c_s^2\omega_2\omega_3 - 9\omega_1\omega_2\omega_3 + 9v_1^2\omega_1\omega_2\omega_3 + \\
& 2v_1^2\omega_4\omega_1\omega_3 - 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_{10} &= 6\omega_4v_2^2\omega_1\omega_2\omega_3 + 18\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 - 9\omega_4v_2^2\omega_1\omega_2 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 4\omega_4v_2^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 - \\
& 9v_2^2\omega_1\omega_2\omega_3 + 2\omega_4v_2^2\omega_1\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 - 18\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_{11} &= 27c_s^2\omega_1\omega_2\omega_3 - 9\omega_4v_2^2\omega_1\omega_2 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 2\omega_4v_2^2\omega_2\omega_3 + 6\omega_4c_s^2\omega_1\omega_3 - 6\omega_4c_s^2\omega_2\omega_3 + 9v_2^2\omega_1\omega_2\omega_3 + 2\omega_4v_2^2\omega_1\omega_3 - 9\omega_1\omega_2\omega_3 - \\
& 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_{12} &= -2v_1^2\omega_4\omega_2\omega_3 + 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 6\omega_4c_s^2\omega_1\omega_3 - 9v_1^2\omega_4\omega_1\omega_2 - 6\omega_4c_s^2\omega_2\omega_3 - 9\omega_1\omega_2\omega_3 + 9v_1^2\omega_1\omega_2\omega_3 + \\
& 2v_1^2\omega_4\omega_1\omega_3 - 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_{13} &= -18v_1^2\omega_4\omega_2\omega_3 + 2\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 + 9\omega_1\omega_2\omega_3 + \\
& 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 - 9\omega_1v_3^2\omega_2\omega_3 + 18v_1^2\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 + 4\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_{14} &= 2\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 18\omega_4v_2^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 + 18\omega_4v_2^2\omega_1\omega_3 + \\
& 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 - 9\omega_1v_3^2\omega_2\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 + 4\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2 \\
C_{15} &= -2c_s^2\omega_1 - 36c_s^2\omega_1v_3^2\omega_2 - 9\omega_1v_3^4\omega_2 + 6\omega_1v_3^4 + 24c_s^2\omega_1v_3^2 + 4c_s^4\omega_2 - 12v_3^2\omega_2 + 2c_s^4\omega_1 - 6\omega_1v_3^2 + 48c_s^2v_3^2\omega_2 + 3c_s^2\omega_1\omega_2 - 4c_s^2\omega_2 + \\
& 12v_3^4\omega_2 + 9\omega_1v_3^4\omega_2 - 3c_s^4\omega_1\omega_2
\end{aligned}$$

2.7.3 Conservation of momentum: ρv_1

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2v_1\delta_l\rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1v_3\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_2\delta_l\rho}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{v_1\delta_l\rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_1v_3\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3\delta_l\rho}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{v_1\delta_l\rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (6v_1^2\omega_1 - 2\omega_1 + 4c_s^2\omega_1 + 3\omega_1\omega_2 - 4\omega_2 - 6c_s^2\omega_1\omega_2 + 8c_s^2\omega_2 + 12v_1^2\omega_2 - 9v_1^2\omega_1\omega_2) \frac{\delta_l^2}{3\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + \\
& (2\omega_1 - 3\omega_1\omega_2 + 4\omega_2) \frac{v_1\delta_l^2\rho}{\omega_1\omega_2\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (-\omega_1 + c_s^2\omega_1 + 3v_2^2\omega_1 + \omega_2 - 3v_2^2\omega_2 - c_s^2\omega_2) \frac{\delta_l^2}{3\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& (\omega_1 - \omega_2) \frac{2v_2\delta_l^2\rho}{\omega_1\omega_2\delta_t} \frac{\partial v_2}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (-\omega_1 + c_s^2\omega_1 + \omega_2 - 3v_3^2\omega_2 + 3\omega_1v_3^2 - c_s^2\omega_2) \frac{\delta_l^2}{3\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (\omega_1 - \omega_2) \frac{2v_3\delta_l^2\rho}{\omega_1\omega_2\delta_t} \frac{\partial v_3}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (-2\omega_1 + 6c_s^2\omega_1 + 6v_2^2\omega_1 + 2\omega_2 - 6v_2^2\omega_2 + 3c_s^2\omega_1\omega_2 - 12c_s^2\omega_2) \frac{\delta_l^2}{6\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2\delta_l^2}{2\omega_1\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + \\
& (-2\omega_1 + 6c_s^2\omega_1 + 2\omega_2 - 6v_3^2\omega_2 + 6\omega_1v_3^2 + 3c_s^2\omega_1\omega_2 - 12c_s^2\omega_2) \frac{\delta_l^2}{6\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2\delta_l^2}{2\omega_1\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (2v_1^2\omega_1 - 2\omega_1 + 6c_s^2\omega_1 + 3\omega_1\omega_2 - 4\omega_2 - 9c_s^2\omega_1\omega_2 + 12c_s^2\omega_2 + 4v_1^2\omega_2 - 3v_1^2\omega_1\omega_2) \frac{v_1\delta_l^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + \\
& (6v_1^2\omega_1 - 2\omega_1 + 2c_s^2\omega_1 + 3\omega_1\omega_2 - 4\omega_2 - 3c_s^2\omega_1\omega_2 + 4c_s^2\omega_2 + 12v_1^2\omega_2 - 9v_1^2\omega_1\omega_2) \frac{\delta_l^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2\delta_l^2\rho}{3\omega_1\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1\partial x_2} + \\
& (-2\omega_1 + 2c_s^2\omega_1 + 6v_2^2\omega_1 + 2\omega_2 - 6v_2^2\omega_2 + 3c_s^2\omega_1\omega_2 - 8c_s^2\omega_2) \frac{\delta_l^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 v_2}{\partial x_1\partial x_2} + (-2 + \omega_1) \frac{c_s^2\delta_l^2\rho}{2\omega_1\delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_3\delta_l^2\rho}{3\omega_1\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1\partial x_3} + \\
& (-2\omega_1 + 2c_s^2\omega_1 + 2\omega_2 - 6v_3^2\omega_2 + 6\omega_1v_3^2 + 3c_s^2\omega_1\omega_2 - 8c_s^2\omega_2) \frac{\delta_l^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 v_3}{\partial x_1\partial x_3} + (-2 + \omega_1) \frac{c_s^2\delta_l^2\rho}{2\omega_1\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} \\
& + C_2 \frac{v_1\delta_l^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{v_1v_2\delta_l^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2\partial x_2} + C_4 \frac{v_2\delta_l^3\rho}{6\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_1^2\partial x_2} + C_5 \frac{v_1\delta_l^3\rho}{12\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_2}{\partial x_1^2\partial x_2} + C_6 \frac{\delta_l^3}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_2^2} - \\
& \frac{v_1c_s^2\delta_l^3\rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_2^2} + C_7 \frac{v_2\delta_l^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1\partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_1v_2\delta_l^3\rho}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + C_8 \frac{v_2\delta_l^3\rho}{12\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_2^2} + (-1 + 3v_2^2 + c_s^2) \frac{v_1\delta_l^3\rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^2} \\
& + C_9 \frac{v_1v_3\delta_l^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2\partial x_3} + C_{10} \frac{v_3\delta_l^3\rho}{6\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_1^2\partial x_3} + C_{11} \frac{v_1\delta_l^3\rho}{12\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_1^2\partial x_3} + C_{12} \frac{v_2v_3\delta_l^3\rho}{3\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_2\partial x_3} + \\
& C_{13} \frac{v_3\delta_l^3\rho}{6\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_2}{\partial x_1\partial x_2\partial x_3} + C_{14} \frac{v_2\delta_l^3\rho}{6\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_2\partial x_3} + C_{15} \frac{v_3\delta_l^3\rho}{4\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_2^2\partial x_3} - \frac{v_1c_s^2\delta_l^3\rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2\partial x_3} + \\
& C_{16} \frac{\delta_l^3}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1\partial x_3^2} - \frac{v_1c_s^2\delta_l^3\rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_3^2} + C_{17} \frac{v_3\delta_l^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_3^2} + C_{18} \frac{v_2\delta_l^3\rho}{4\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_2\partial x_3^2} - \frac{v_1c_s^2\delta_l^3\rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2\partial x_3^2} + \\
& (-1 + v_3^2 + 3c_s^2) \frac{v_1v_3\delta_l^3\rho}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^2} + C_{19} \frac{v_3\delta_l^3\rho}{12\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_3^2} + (-1 + 3v_3^2 + c_s^2) \frac{v_1\delta_l^3\rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^2} + C_{20} \frac{v_1\delta_l^4\rho}{36\omega_1^3\omega_2^2\omega_3\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{21} \frac{\delta_l^4\rho}{36\omega_1^3\omega_2^2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{22} \frac{v_2\delta_l^4\rho}{36\omega_1^3\omega_2^2\omega_3\delta_t} \frac{\partial^4 \rho}{\partial x_1^3\partial x_2} + C_{23} \frac{v_1v_2\delta_l^4\rho}{18\omega_1^3\omega_2^2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1^3\partial x_2} + C_{24} \frac{\delta_l^4\rho}{72\omega_4^3\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_1^3\partial x_2} +
\end{aligned}$$

$$\begin{aligned}
& C_{25} \frac{v_1 \delta_l^4}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\delta_l^4 \rho}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{27} \frac{v_1 v_2 \delta_l^4 \rho}{18\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{28} \frac{v_2 \delta_l^4}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& C_{29} \frac{v_1 v_2 \delta_l^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{30} \frac{\delta_l^4 \rho}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{31} \frac{v_1 \delta_l^4}{72\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{32} \frac{\delta_l^4 \rho}{24\omega_4 \omega_1^3 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (-4\omega_1 + 6c_s^2 \omega_1 + 10v_2^2 \omega_1 + 6\omega_1 \omega_2 - 8\omega_2 - 15v_2^2 \omega_1 \omega_2 + 20v_2^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 + 12c_s^2 \omega_2) \frac{v_1 v_2 \delta_l^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& C_{33} \frac{v_3 \delta_l^4}{36\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{34} \frac{v_1 v_3 \delta_l^4 \rho}{18\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{35} \frac{\delta_l^4 \rho}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{36} \frac{v_1 v_2 v_3 \delta_l^4}{6\omega_1^3 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_2 v_3 \delta_l^4 \rho}{6\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{38} \frac{v_1 v_3 \delta_l^4 \rho}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{v_1 v_2 \delta_l^4 \rho}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{40} \frac{v_3 \delta_l^4}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{v_1 v_3 \delta_l^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{42} \frac{v_2 v_3 \delta_l^4 \rho}{6\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{43} \frac{\delta_l^4 \rho}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (-\omega_1 + 3c_s^2 \omega_1 + \omega_2 - v_2^2 \omega_2 + \omega_1 v_3^2 - 3c_s^2 \omega_2) \frac{v_1 v_2 v_3 \delta_l^4}{12\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + \\
& C_{44} \frac{v_2 v_3 \delta_l^4 \rho}{8\omega_2^2 \omega_1 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3} + (-\omega_1 + 3c_s^2 \omega_1 + \omega_2 - v_2^2 \omega_2 + \omega_1 v_3^2 - 3c_s^2 \omega_2) \frac{v_1 v_3 \delta_l^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{45} \frac{v_1 v_2 \delta_l^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{46} \frac{v_1 \delta_l^4}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{47} \frac{\delta_l^4 \rho}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + C_{48} \frac{v_1 v_3 \delta_l^4 \rho}{18\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{49} \frac{v_2 \delta_l^4}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{v_1 v_2 \delta_l^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{51} \frac{\delta_l^4 \rho}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{52} \frac{v_2 v_3 \delta_l^4 \rho}{6\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (-2\omega_1 + 2c_s^2 \omega_1 + 3v_2^2 \omega_1 + 2\omega_2 - 3v_2^2 \omega_2 + 3\omega_1 v_3^2 - 3v_2^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 14c_s^2 \omega_2) \frac{v_1 c_s^2 \delta_l^4}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{53} \frac{\delta_l^4 \rho}{8\omega_2^2 \omega_1^3 \omega_5 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + (-\omega_1 + 3c_s^2 \omega_1 + v_2^2 \omega_1 + \omega_2 - v_2^2 \omega_2 - 3c_s^2 \omega_2) \frac{v_1 v_2 \delta_l^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (-\omega_1 + 3c_s^2 \omega_1 + \omega_2 - v_2^2 \omega_2 + \omega_1 v_3^2 - 3c_s^2 \omega_2) \frac{v_1 v_3 \delta_l^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{54} \frac{v_3 \delta_l^4}{72\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + C_{55} \frac{v_1 v_3 \delta_l^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + \\
& C_{56} \frac{\delta_l^4 \rho}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^2} + (-\omega_1 + 3c_s^2 \omega_1 + v_2^2 \omega_1 + \omega_2 - v_2^2 \omega_2 - 3c_s^2 \omega_2) \frac{v_1 v_2 v_3 \delta_l^4}{12\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^2} + C_{57} \frac{v_2 v_3 \delta_l^4 \rho}{8\omega_4^2 \omega_1 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^2} + \\
& C_{58} \frac{v_1 v_3 \delta_l^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^2} + (-\omega_1 + 3c_s^2 \omega_1 + v_2^2 \omega_1 + \omega_2 - v_2^2 \omega_2 - 3c_s^2 \omega_2) \frac{v_1 v_2 \delta_l^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^2} + C_{59} \frac{v_1 \delta_l^4}{72\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{60} \frac{\delta_l^4 \rho}{24\omega_4^2 \omega_1^3 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + \\
& (-4\omega_1 + 6c_s^2 \omega_1 + 6\omega_1 \omega_2 - 8\omega_2 + 20v_2^2 \omega_2 + 10\omega_1 v_3^2 - 9c_s^2 \omega_1 \omega_2 + 12c_s^2 \omega_2 - 15\omega_1 v_3^2 \omega_2) \frac{v_1 v_3 \delta_l^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 12v_1^2 \omega_1^2 \omega_2 - 4c_s^4 \omega_1^2 \omega_2 + 8c_s^4 \omega_2^2 + 24v_1^2 c_s^2 \omega_1^2 \omega_2^2 + 72v_1^2 c_s^2 \omega_2^2 - c_s^2 \omega_1^2 \omega_2^2 + 7v_1^4 \omega_1^2 \omega_2^2 + 16v_1^4 \omega_2^2 - 4c_s^2 \omega_1^2 + 4c_s^2 \omega_2^2 \omega_2 - 12v_1^4 \omega_1^2 \omega_2 - \\
& 7v_1^2 \omega_1^2 \omega_2^2 - 48v_1^2 c_s^2 \omega_1^2 \omega_2 + c_s^4 \omega_1^2 \omega_2^2 - 4v_1^4 \omega_1^2 - 8c_s^4 \omega_1 \omega_2^2 + 48v_1^2 c_s^2 \omega_1 \omega_2 + 24v_1^2 \omega_1 \omega_2^2 - 16v_1^2 \omega_2^2 + 16v_1^4 \omega_1 \omega_2 - 8c_s^2 \omega_2^2 + 24v_1^2 c_s^2 \omega_1^2 - 24v_1^4 \omega_1 \omega_2^2 + \\
& 8c_s^2 \omega_1 \omega_2^2 + 4v_1^4 \omega_1^2 + 4c_s^2 \omega_1^2 - 96v_1^2 c_s^2 \omega_1 \omega_2^2 - 16v_1^2 \omega_1 \omega_2 \\
C_2 &= 16\omega_1 \omega_2^2 - 20v_2^2 \omega_1^2 \omega_2 + 5c_s^2 \omega_1^2 \omega_2^2 + 8c_s^2 \omega_1^2 - 4\omega_1^2 - 12c_s^2 \omega_1^2 \omega_2 - 8\omega_1 \omega_2 + 11v_1^2 \omega_1^2 \omega_2^2 + 8v_1^2 \omega_1^2 + 8\omega_1^2 \omega_2 - 40v_1^2 \omega_1 \omega_2^2 + 28v_1^2 \omega_2^2 - 12\omega_2^2 + \\
& 8c_s^2 \omega_1 \omega_2 + 20c_s^2 \omega_2^2 - 24c_s^2 \omega_1 \omega_2^2 - 4\omega_1^2 \omega_2^2 + 24v_1^2 \omega_1 \omega_2 \\
C_3 &= -3\omega_1 \omega_2^2 + 3v_2^2 \omega_1 \omega_2^2 + 2v_2^2 \omega_1^2 + 12c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_1 \omega_2 + 2v_2^2 \omega_1 \omega_2 + 2v_1^2 \omega_1^2 + 3\omega_1^2 \omega_2 - 3v_2^2 \omega_1^2 \omega_2 + 2v_1^2 \omega_2^2 + 2\omega_2^2 - \\
& 6c_s^2 \omega_1 \omega_2 - 6c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 4v_2^2 \omega_2^2 - 4v_1^2 \omega_1 \omega_2 \\
C_4 &= -2\omega_1 \omega_2^2 + 2v_2^2 \omega_1 \omega_2^2 - 4\omega_1^2 \omega_3 - 4c_s^2 \omega_2^2 \omega_3 - 4c_s^2 \omega_1 \omega_2 \omega_3 + 2v_2^2 \omega_1^2 \omega_3 - v_2^2 \omega_1^2 \omega_2 \omega_3 - 6c_s^2 \omega_1^2 \omega_2 + \omega_1^2 \omega_2 \omega_3 + v_2^2 \omega_1 \omega_2^2 \omega_3 + 6v_1^2 \omega_2^2 \omega_3 - \\
& \omega_1 \omega_2^2 \omega_3 + 2\omega_1^2 \omega_2 - 2v_2^2 \omega_1^2 \omega_2 + 4\omega_1 \omega_2 \omega_3 - 12v_1^2 \omega_1 \omega_2 \omega_3 + 6v_1^2 \omega_1^2 \omega_3 + 3c_s^2 \omega_1 \omega_2^2 \omega_3 + 6c_s^2 \omega_1 \omega_2^2 - 3c_s^2 \omega_1^2 \omega_2 \omega_3 - 2v_2^2 \omega_2^2 \omega_3 + 8c_s^2 \omega_1^2 \omega_3 \\
C_5 &= -8v_1^2 \omega_4 \omega_1 \omega_2^2 + 12\omega_4 v_2^2 \omega_1 \omega_2 \omega_3 - 8\omega_4 \omega_1^2 \omega_3 + 18c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 8\omega_4 \omega_1^2 \omega_2 \omega_3 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 8\omega_4 \omega_1 \omega_2^2 \omega_3 + 8\omega_4 \omega_1 \omega_2^2 + 4v_1^2 \omega_4 \omega_1^2 \omega_3 - \\
& 12v_1^2 \omega_1 \omega_2^2 \omega_3 + 12\omega_4 c_s^2 \omega_1 \omega_2^2 \omega_3 + 2v_1^2 \omega_4 \omega_1 \omega_2^2 \omega_3 + 16\omega_4 c_s^2 \omega_2^2 \omega_3 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 12\omega_4 v_2^2 \omega_1^2 \omega_3 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 \omega_3 + 12\omega_1 \omega_2^2 \omega_3 - 2v_1^2 \omega_4 \omega_1^2 \omega_2 \omega_3 + \\
& 6v_1^2 \omega_1^2 \omega_2^2 \omega_3 - 11\omega_4 c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 - 3v_1^2 \omega_4 \omega_1^2 \omega_2^2 \omega_3 - 4v_1^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_4 \omega_1^2 \omega_2 + 4\omega_4 c_s^2 \omega_1 \omega_2 \omega_3 - 24\omega_4 v_2^2 \omega_2^2 \omega_3 + 16\omega_4 c_s^2 \omega_1^2 \omega_3 - \\
& 6\omega_1^2 \omega_2^2 \omega_3 - 36c_s^2 \omega_1 \omega_2^2 \omega_3 - 18\omega_4 v_2^2 \omega_1^2 \omega_2 \omega_3 - 6\omega_4 \omega_1^2 \omega_2^2 - 4\omega_4 \omega_1 \omega_2 \omega_3 + 6v_1^2 \omega_4 \omega_1^2 \omega_2^2 + 18\omega_4 v_2^2 \omega_1 \omega_2^2 \omega_3 + 8v_1^2 \omega_4 \omega_2^2 \omega_3 + 3\omega_4 \omega_1^2 \omega_2^2 \omega_3 \\
C_6 &= -18c_s^2 v_2^2 \omega_2^2 - 3v_2^2 \omega_1 \omega_2^2 - 2c_s^4 \omega_1^2 \omega_2 - 14c_s^4 \omega_2^2 + 2v_2^4 \omega_1 \omega_2 - 15c_s^2 v_2^2 \omega_1^2 \omega_2 - 2v_2^2 \omega_1^2 - 2c_s^2 \omega_1^2 + 2c_s^2 \omega_1^2 \omega_2 + 3v_2^4 \omega_1 \omega_2^2 - 2v_2^2 \omega_1 \omega_2 - c_s^4 \omega_1^2 \omega_2^2 - \\
& 4v_2^4 \omega_2^2 + 3v_2^2 \omega_1^2 \omega_2 + 14c_s^4 \omega_1 \omega_2^2 + 2v_2^4 \omega_1^2 + 15c_s^2 v_2^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 - 3v_2^4 \omega_1^2 \omega_2 + 4v_2^2 \omega_2^2 + 6c_s^2 v_2^2 \omega_1 \omega_2 + 12c_s^2 v_2^2 \omega_1^2 + 2c_s^4 \omega_1^2 \\
C_7 &= \\
& -5\omega_1 \omega_2^2 + 11v_2^2 \omega_1 \omega_2^2 + 8v_2^2 \omega_1^2 + 8c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 - 2\omega_1 \omega_2 + 6v_2^2 \omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 11v_2^2 \omega_1^2 \omega_2 + 6\omega_2^2 + 2c_s^2 \omega_1 \omega_2 - 10c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 14v_2^2 \omega_2^2 \\
C_8 &= 9\omega_4 c_s^2 \omega_1 - 6v_2^2 \omega_3 + 6\omega_4 + 9c_s^2 \omega_1 \omega_3 + 6\omega_4 v_2^2 \omega_3 + 18\omega_4 c_s^2 \omega_3 - 6\omega_4 c_s^2 \omega_1 \omega_3 + 3\omega_4 v_2^2 \omega_1 - 18c_s^2 \omega_3 - 18\omega_4 c_s^2 - 2\omega_4 v_2^2 \omega_1 \omega_3 - 6\omega_4 \omega_3 + \\
& 6\omega_3 - 6\omega_4 v_2^2 - 3\omega_1 \omega_3 + 3v_2^2 \omega_1 \omega_3 - 3\omega_4 \omega_1 + 2\omega_4 \omega_1 \omega_3 \\
C_9 &= -4v_3^2 \omega_2^2 - 3\omega_1 \omega_2^2 - 3\omega_1^2 v_3^2 \omega_2 + 12c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_1^2 v_3^2 + 2\omega_1 \omega_2 + 2v_1^2 \omega_1^2 + 3\omega_1^2 \omega_2 + 3\omega_1 v_3^2 \omega_2^2 + 2v_1^2 \omega_2^2 + 2\omega_2^2 - 6c_s^2 \omega_1 \omega_2 - \\
& 6c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 + 2\omega_1 v_3^2 \omega_2 - 4v_1^2 \omega_1 \omega_2
\end{aligned}$$

$$C_{10} = -2\omega_1\omega_2^2 - 4\omega_1^2\omega_3 - \omega_1^2v_3^2\omega_2\omega_3 - 4c_s^2\omega_2^2\omega_3 - 4c_s^2\omega_1\omega_2\omega_3 - 2\omega_1^2v_3^2\omega_2 - 2v_3^2\omega_2^2\omega_3 - 6c_s^2\omega_1^2\omega_2 + \omega_1^2\omega_2\omega_3 + \omega_1v_3^2\omega_2^2\omega_3 + 6v_1^2\omega_2^2\omega_3 - \omega_1\omega_2^2\omega_3 + 2\omega_1^2\omega_2 + 2\omega_1v_3^2\omega_2^2 + 4\omega_1\omega_2\omega_3 + 2\omega_1^2v_3^2\omega_3 - 12v_1^2\omega_1\omega_2\omega_3 + 6v_1^2\omega_1^2\omega_3 + 3c_s^2\omega_1\omega_2^2\omega_3 + 6c_s^2\omega_1\omega_2^2 - 3c_s^2\omega_1^2\omega_2\omega_3 + 8c_s^2\omega_1^2\omega_3$$

$$C_{11} = -8v_1^2\omega_4\omega_1\omega_2^2 - 24\omega_4v_3^2\omega_2^2\omega_3 - 8\omega_4\omega_1^2\omega_3 + 18c_s^2\omega_1^2\omega_2^2\omega_3 + 8\omega_4\omega_1^2\omega_2\omega_3 - 12\omega_4c_s^2\omega_1^2\omega_2 - 8\omega_4\omega_1\omega_2^2\omega_3 + 8\omega_4\omega_1\omega_2^2 + 4v_1^2\omega_4\omega_1^2\omega_3 + 12\omega_4\omega_1v_3^2\omega_2\omega_3 - 12v_1^2\omega_1\omega_2^2\omega_3 + 12\omega_4c_s^2\omega_1\omega_2^2\omega_3 + 2v_1^2\omega_4\omega_1\omega_2^2\omega_3 + 16\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 + 18\omega_4c_s^2\omega_1^2\omega_2^2 - 12\omega_4c_s^2\omega_1^2\omega_2\omega_3 + 12\omega_1\omega_2^2\omega_3 - 2v_1^2\omega_4\omega_1^2\omega_2\omega_3 + 6v_1^2\omega_1^2\omega_2^2\omega_3 - 11\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 24\omega_4c_s^2\omega_1\omega_2^2 - 3v_1^2\omega_4\omega_1^2\omega_2^2\omega_3 - 4v_1^2\omega_4\omega_1^2\omega_2 + 4\omega_4\omega_1^2\omega_2 + 4\omega_4c_s^2\omega_1\omega_2\omega_3 - 18\omega_4\omega_1^2v_3^2\omega_2\omega_3 + 16\omega_4c_s^2\omega_1^2\omega_3 - 6\omega_1^2\omega_2^2\omega_3 - 36c_s^2\omega_1\omega_2^2\omega_3 - 6\omega_4\omega_1^2\omega_2^2 - 4\omega_4\omega_1\omega_2\omega_3 + 18\omega_4\omega_1v_3^2\omega_2^2\omega_3 + 12\omega_4\omega_1v_3^2\omega_3 + 6v_1^2\omega_4\omega_1^2\omega_2^2 + 8v_1^2\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_1^2\omega_2^2\omega_3$$

$$C_{12} = v_3^2\omega_2^2 + v_2^2\omega_1^2 + 6c_s^2\omega_1^2 - 2\omega_1^2 + \omega_1^2v_3^2 + 4\omega_1\omega_2 - 2v_2^2\omega_1\omega_2 - 2\omega_2^2 - 12c_s^2\omega_1\omega_2 + 6c_s^2\omega_2^2 + v_2^2\omega_2^2 - 2\omega_1v_3^2\omega_2$$

$$C_{13} = -12\omega_4v_2^2\omega_1\omega_2\omega_3 - 2\omega_4v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_1^2\omega_3 + 3\omega_4\omega_1^2v_3^2\omega_2^2 - 9c_s^2\omega_1^2\omega_2^2\omega_3 + \omega_4\omega_1^2\omega_2\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2 - \omega_4\omega_1\omega_2^2\omega_3 + 4\omega_4\omega_1\omega_2^2 + 3\omega_4c_s^2\omega_1\omega_2^2\omega_3 + 6\omega_1v_3^2\omega_2^2\omega_3 - 4\omega_4c_s^2\omega_2^2\omega_3 + 9\omega_4c_s^2\omega_1^2\omega_2^2 + 6\omega_4v_2^2\omega_1^2\omega_3 - 3\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 6\omega_1\omega_2^2\omega_3 - 2\omega_4\omega_1^2v_3^2\omega_2 - 12\omega_4c_s^2\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_4c_s^2\omega_1\omega_2\omega_3 - \omega_4\omega_1^2v_3^2\omega_2\omega_3 + 6\omega_4v_2^2\omega_2^2\omega_3 + 8\omega_4c_s^2\omega_1^2\omega_3 + 3\omega_1^2\omega_2^2\omega_3 + 18c_s^2\omega_1\omega_2^2\omega_3 - 4\omega_4\omega_1v_3^2\omega_2^2 - 3\omega_1^2v_3^2\omega_2^2\omega_3 - 3\omega_4\omega_1^2\omega_2^2 + 4\omega_4\omega_1\omega_2\omega_3 + \omega_4\omega_1v_3^2\omega_2^2\omega_3 + 2\omega_4\omega_1^2v_3^2\omega_3$$

$$C_{14} = 6\omega_4v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_1^2\omega_3 - 9c_s^2\omega_1^2\omega_2^2\omega_3 + \omega_4\omega_1^2\omega_2\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2 - \omega_4\omega_1\omega_2^2\omega_3 + 4\omega_4\omega_1\omega_2^2 - 12\omega_4\omega_1v_3^2\omega_2\omega_3 + 3\omega_4c_s^2\omega_1\omega_2^2\omega_3 - 4\omega_4v_2^2\omega_1\omega_2^2\omega_3 + 6v_2^2\omega_1\omega_2^2\omega_3 - 4\omega_4c_s^2\omega_2^2\omega_3 + 9\omega_4c_s^2\omega_1^2\omega_2^2 + 2\omega_4v_2^2\omega_1^2\omega_3 - 3\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 6\omega_1\omega_2^2\omega_3 - 12\omega_4c_s^2\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_4c_s^2\omega_1\omega_2\omega_3 - 3v_2^2\omega_1^2\omega_2^2\omega_3 - 2\omega_4v_2^2\omega_2^2\omega_3 + 3\omega_4v_2^2\omega_1^2\omega_2^2 + 8\omega_4c_s^2\omega_1^2\omega_3 + 3\omega_1^2\omega_2^2\omega_3 + 18c_s^2\omega_1\omega_2^2\omega_3 - 2\omega_4v_2^2\omega_1^2\omega_2 - \omega_4v_2^2\omega_1^2\omega_2\omega_3 - 3\omega_4\omega_1^2\omega_2^2 + 4\omega_4\omega_1\omega_2\omega_3 + 6\omega_4\omega_1^2v_3^2\omega_3 + \omega_4v_2^2\omega_1\omega_2^2\omega_3$$

$$C_{15} = 3\omega_4c_s^2\omega_1 + 2\omega_4 - 3c_s^2\omega_1\omega_3 - \omega_1v_3^2\omega_3 + 6c_s^2\omega_3 - 6\omega_4c_s^2 + \omega_4\omega_1v_3^2 - 2\omega_3 + \omega_1\omega_3 - 2\omega_4v_3^2 + 2v_3^2\omega_3 - \omega_4\omega_1$$

$$C_{16} = 4v_3^2\omega_2^2 - 2c_s^4\omega_1^2\omega_2 - 14c_s^4\omega_2^2 + 3\omega_1v_3^4\omega_2^2 + 15c_s^2\omega_1v_3^2\omega_2^2 + 3\omega_1^2v_3^2\omega_2 + 6c_s^2\omega_1v_3^2\omega_2 - 2c_s^2\omega_1^2 + 2\omega_1v_3^4\omega_2 + 2c_s^2\omega_1^2\omega_2 - 2\omega_1^2v_3^2 - c_s^4\omega_1^2\omega_2^2 - 3\omega_1v_3^2\omega_2^2 + 14c_s^4\omega_1\omega_2^2 - 15c_s^2\omega_1^2v_3^2\omega_2 - 3\omega_1^2v_3^4\omega_2 - 4v_3^4\omega_2^2 + 2\omega_1^2v_3^4 + 12c_s^2\omega_1^2v_3^2 + 2c_s^2\omega_2^2 - 2c_s^2\omega_1\omega_2^2 - 18c_s^2v_3^2\omega_2^2 - 2\omega_1v_3^2\omega_2 + 2c_s^4\omega_1^2$$

$$C_{17} = -14v_3^2\omega_2^2 - 5\omega_1\omega_2^2 - 11\omega_1^2v_3^2\omega_2 + 8c_s^2\omega_1^2 - 4\omega_1^2 - 9c_s^2\omega_1^2\omega_2 + 8\omega_1^2v_3^2 - 2\omega_1\omega_2 + 5\omega_1^2\omega_2 + 11\omega_1v_3^2\omega_2^2 + 6\omega_2^2 + 2c_s^2\omega_1\omega_2 - 10c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 6\omega_1v_3^2\omega_2$$

$$C_{18} = 3\omega_4c_s^2\omega_1 + 2v_2^2\omega_3 + 2\omega_4 - 3c_s^2\omega_1\omega_3 + \omega_4v_2^2\omega_1 + 6c_s^2\omega_3 - 6\omega_4c_s^2 - 2\omega_3 - 2\omega_4v_2^2 + \omega_1\omega_3 - v_2^2\omega_1\omega_3 - \omega_4\omega_1$$

$$C_{19} = 9\omega_4c_s^2\omega_1 + 6\omega_4 - 2\omega_4\omega_1v_3^2\omega_3 + 9c_s^2\omega_1\omega_3 + 18\omega_4c_s^2\omega_3 + 3\omega_1v_3^2\omega_3 - 6\omega_4c_s^2\omega_1\omega_3 - 18c_s^2\omega_3 - 18\omega_4c_s^2 - 6\omega_4\omega_3 + 3\omega_4\omega_1v_3^2 + 6\omega_3 - 3\omega_1\omega_3 - 6\omega_4v_3^2 - 6v_3^2\omega_3 - 3\omega_4\omega_1 + 2\omega_4\omega_1\omega_3 + 6\omega_4v_3^2\omega_3$$

$$C_{20} = -8c_s^2\omega_1^3\omega_2 - 264v_4^4\omega_1^2\omega_2^2\omega_3 + 8\omega_1^3\omega_2^2\omega_3 + 152c_s^4\omega_1^2\omega_2^2\omega_3 - 372c_s^4\omega_1\omega_2^3\omega_3 + 328v_1^2\omega_1\omega_2^3\omega_3 - 16v_1^2c_s^2\omega_1^2\omega_2^2 + 16c_s^2\omega_1^2\omega_2^2 - 28\omega_1\omega_2^3\omega_3 + 82c_s^4\omega_1^3\omega_2^2\omega_3 - 464v_1^2c_s^2\omega_1^2\omega_2\omega_3 + 8v_1^2c_s^2\omega_1^3\omega_2 + 216c_s^4\omega_2^2\omega_3 + 808v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 98v_1^2\omega_1^3\omega_2^2\omega_3 - 160v_1^2\omega_1^2\omega_2^2\omega_3 + 176v_1^2\omega_1\omega_2^2\omega_3 + 24c_s^4\omega_1^3\omega_2 + 760v_1^2c_s^2\omega_1^2\omega_2\omega_3 + 72c_s^4\omega_1\omega_2^2\omega_3 - 3\omega_1^3\omega_2\omega_3 - 84v_1^4\omega_1^2\omega_2\omega_3 - 156c_s^2\omega_1^2\omega_2\omega_3 + 180v_1^4\omega_1^2\omega_2^2\omega_3 + 8\omega_1^2\omega_2\omega_3 + 122c_s^4\omega_1^2\omega_2\omega_3 + 72c_s^4\omega_1^2\omega_2\omega_3 + 30v_1^4\omega_1^3\omega_2^2\omega_3 - 1088v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 15c_s^4\omega_1^3\omega_2^2\omega_3 - 48c_s^4\omega_1^2\omega_2^2 - 104v_1^2\omega_1^2\omega_2\omega_3 + 8\omega_1\omega_2^2\omega_3 + 4\omega_1^3\omega_3 + 144v_1^4\omega_2^2\omega_3 - 184c_s^2\omega_2^2\omega_3 + 440v_1^2c_s^2\omega_1^2\omega_2\omega_3 - 120c_s^4\omega_1^2\omega_2^2\omega_3 + 280v_1^2\omega_1^2\omega_2^2\omega_3 - 102v_1^2c_s^2\omega_1^3\omega_2^2\omega_3 + 160v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 300v_1^4\omega_1\omega_2^2\omega_3 + 320c_s^2\omega_1\omega_2^2\omega_3 - 52c_s^2\omega_1^3\omega_3 + 24c_s^4\omega_1\omega_2^2 + 16\omega_2^2\omega_3 + 24v_1^4\omega_1^3\omega_3 + 656v_1^2c_s^2\omega_1\omega_2^2\omega_3 + 90v_1^4\omega_1^2\omega_2^2\omega_3 - 78c_s^2\omega_1^3\omega_2^2\omega_3 - 16\omega_1^2\omega_2^2\omega_3 - 80c_s^2\omega_1\omega_2^2\omega_3 + 168v_1^4\omega_1\omega_2^2\omega_3 + 404v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 196v_1^2\omega_1^2\omega_2^2\omega_3 + 8\omega_1^2c_s^2\omega_1\omega_2^2\omega_3 - 156c_s^4\omega_1\omega_2\omega_3 + 94v_1^4\omega_1^2\omega_2\omega_3 + 164c_s^4\omega_1^2\omega_2\omega_3 + 18c_s^2\omega_1^3\omega_2^2\omega_3 - 8c_s^2\omega_1\omega_2^2 - 28v_1^2\omega_1^3\omega_3 + 72c_s^4\omega_1^3\omega_3 + 96v_1^4\omega_1^2\omega_2\omega_3 + 16\omega_2^2\omega_3 - 80c_s^2\omega_1^2\omega_2\omega_3 - 10\omega_1^3\omega_2\omega_3 - 27v_1^4\omega_1^3\omega_2^2\omega_3 - 1472v_1^2c_s^2\omega_1\omega_2^2\omega_3$$

$$C_{21} = -8c_s^2\omega_1^3\omega_2 - 888v_1^4\omega_1^2\omega_2^2\omega_3 + 8\omega_1^3\omega_2^2\omega_3 + 24c_s^2\omega_1^2\omega_2^2\omega_3 - 68c_s^4\omega_1\omega_2^3\omega_3 + 552v_1^2\omega_1\omega_2^3\omega_3 - 48v_1^2c_s^2\omega_1^2\omega_2^2 + 16c_s^2\omega_1^2\omega_2^2 - 28\omega_1\omega_2^3\omega_3 + 14c_s^4\omega_1^3\omega_2^2\omega_3 - 360v_1^2c_s^2\omega_1^2\omega_2\omega_3 + 24v_1^2c_s^2\omega_1^3\omega_2 + 40c_s^4\omega_2^2\omega_3 + 504v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 154v_1^4\omega_1^2\omega_2^2\omega_3 - 288v_1^2\omega_1^2\omega_2^2\omega_3 - 240v_1^2\omega_1\omega_2^2\omega_3 + 8c_s^4\omega_1^2\omega_2 + 552v_1^2c_s^2\omega_1^2\omega_2\omega_3 + 8c_s^4\omega_1\omega_2^2\omega_3 - 3\omega_1^3\omega_2\omega_3 - 312v_1^4\omega_1^3\omega_2\omega_3 - 44c_s^2\omega_1^2\omega_2^2\omega_3 + 620v_1^4\omega_1^2\omega_2^2\omega_3 + 8\omega_1^2\omega_2\omega_3 + 42c_s^2\omega_1^2\omega_2\omega_3 + 8c_s^4\omega_1^2\omega_2\omega_3 + 42v_1^4\omega_1^3\omega_2^2\omega_3 - 576v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 3c_s^4\omega_1^3\omega_2^2\omega_3 - 16c_s^4\omega_1^2\omega_2^2 - 168v_1^4\omega_1^2\omega_2\omega_3 + 8\omega_1\omega_2^2\omega_3 + 4\omega_1^3\omega_3 + 528v_1^4\omega_2^2\omega_3 - 56c_s^2\omega_2^2\omega_3 + 264v_1^2c_s^2\omega_1^2\omega_2\omega_3 - 8c_s^4\omega_1^2\omega_2^2\omega_3 + 408v_1^2\omega_1^2\omega_2^2\omega_3 - 54v_1^4c_s^2\omega_1^3\omega_2^2\omega_3 + 144v_1^2c_s^2\omega_1^3\omega_3 - 1068v_1^4\omega_1\omega_2^2\omega_3 + 96c_s^2\omega_1\omega_2^2\omega_3 - 20c_s^2\omega_1^3\omega_3 + 8c_s^4\omega_1\omega_2^2 + 16\omega_2^2\omega_3 + 96v_1^4\omega_1^3\omega_3 + 336v_1^2c_s^2\omega_1\omega_2^2\omega_3 + 310v_1^4\omega_1^2\omega_2^2\omega_3 - 22c_s^2\omega_1^3\omega_2^2\omega_3 - 16\omega_1^2\omega_2^2\omega_3 - 16c_s^2\omega_1\omega_2^2\omega_3 + 552v_1^4\omega_1\omega_2^2\omega_3 + 252v_1^2c_s^2\omega_1^2\omega_2^2\omega_3 - 308v_1^2\omega_1^2\omega_2^2\omega_3 + 24v_1^2c_s^2\omega_1\omega_2^2\omega_3 - 32c_s^4\omega_1^3\omega_2\omega_3 + 174v_1^4\omega_1^3\omega_2\omega_3 + 28c_s^4\omega_1^2\omega_2^2\omega_3 + 6c_s^2\omega_1^3\omega_2^2\omega_3 - 8c_s^2\omega_1\omega_2^2 - 60v_1^4\omega_1^3\omega_3 + 16c_s^4\omega_1^3\omega_3 + 336v_1^4\omega_1^2\omega_2\omega_3 + 16\omega_1^2\omega_2^2\omega_3 - 16c_s^2\omega_1^2\omega_2\omega_3 - 10\omega_1^3\omega_2\omega_3 - 87v_1^4\omega_1^3\omega_2^2\omega_3 - 1008v_1^2c_s^2\omega_1\omega_2^2\omega_3$$

$$C_{22} = -4v_2^2\omega_1^3\omega_3 + 24v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 8\omega_1\omega_2^2\omega_3^2 - 12c_s^2\omega_1^2\omega_2^2\omega_3^2 + 48v_1^4\omega_2^2\omega_3^2 + 4\omega_1^3\omega_3^2 + 2c_s^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 4c_s^2\omega_1^2\omega_2^2\omega_3^2 + 20c_s^2\omega_2^3\omega_3^2 - 12c_s^2v_2^2\omega_1^2\omega_2^2 + 24c_s^4\omega_1\omega_2^2\omega_3 - 8v_2^2\omega_1\omega_2^2\omega_3^2 - 36c_s^4\omega_1^2\omega_2\omega_3^2 + 216v_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 24v_1^2\omega_1^2\omega_2\omega_3^2 - 36v_1^4\omega_1^3\omega_2\omega_3^2 + 96v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 + 5c_s^2\omega_1^2\omega_2^2\omega_3^2 - 4\omega_1^2\omega_2\omega_3^2 + 22c_s^2v_2^2\omega_1\omega_2^2\omega_3^2 + 56c_s^2\omega_1^2\omega_2\omega_3^2 + 54c_s^4\omega_1^3\omega_2\omega_3^2 - 36c_s^4\omega_1^2\omega_2\omega_3^2 + 48v_1^2\omega_1\omega_2^2\omega_3^2 + 24v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 4v_2^2\omega_1^2\omega_2\omega_3^2 + 36c_s^4\omega_1^2\omega_2^2 + 6c_s^4\omega_1^2\omega_2^2\omega_3^2 - 324v_1^4c_s^2\omega_1^2\omega_2\omega_3^2 - 8v_2^2\omega_1\omega_2^2\omega_3^2 - 36c_s^4\omega_2^3\omega_3^2 + 24v_1^2\omega_2^3\omega_3^2 - 24v_1^2\omega_1^3\omega_2^2\omega_3^2 - 72v_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 24v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 + 18c_s^2\omega_1^2\omega_2^2\omega_3^2 + 8\omega_1\omega_2^2\omega_3^2 + 8c_s^2v_2^2\omega_1\omega_2^2\omega_3^2 - 4c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 + 4c_s^2\omega_1^2\omega_2\omega_3^2 + 42c_s^4\omega_1\omega_2^2\omega_3^2 + 12c_s^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - v_2^2\omega_1^2\omega_2^2\omega_3^2 - 60v_1^2\omega_1\omega_2^2\omega_3^2 - 20c_s^2v_2^2\omega_2^2\omega_3^2 + 12c_s^2\omega_1^2\omega_2^2 + 72v_1^4\omega_1^2\omega_2^2\omega_3^2 + 8c_s^2v_2^2\omega_1\omega_2^2\omega_3^2 + 18c_s^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 24v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 + \omega_1^2\omega_2^2\omega_3^2 - 34c_s^2\omega_1^2\omega_2^2\omega_3^2 + 108v_1^2c_s^2\omega_1\omega_2^2\omega_3^2 + v_2^2\omega_1^2\omega_2^2\omega_3^2 - 12c_s^4\omega_2^2\omega_3^2 + 4v_2^2\omega_1^3\omega_2\omega_3^2 - 48v_1^4\omega_1^3\omega_2^2\omega_3^2 - \omega_1^2\omega_2^2\omega_3^2 - 18c_s^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 72c_s^4\omega_1^3\omega_2^2\omega_3^2 + 40c_s^2\omega_1^2\omega_2\omega_3^2 - 8c_s^2\omega_1\omega_2^2\omega_3^2 - 4c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 - 4\omega_1^3\omega_2\omega_3^2 + 24v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 84c_s^4\omega_1^2\omega_2\omega_3^2 + 84v_1^2v_2^2\omega_2^2\omega_3^2 - 6c_s^4\omega_1^2\omega_2^2\omega_3^2 - 8c_s^2\omega_1\omega_2^2\omega_3^2 + 16c_s^2v_2^2\omega_1^3\omega_2^2\omega_3^2 - 48v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 18c_s^2\omega_1^3\omega_2\omega_3^2 - 72v_1^4\omega_1\omega_2^2\omega_3^2 - 2c_s^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 5c_s^2\omega_1^3\omega_2^2\omega_3^2 - 4c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 - 4\omega_1^2\omega_2^2\omega_3^2 - 52c_s^2\omega_1^3\omega_2^2\omega_3^2 + 24v_1^4\omega_1^3\omega_2^2\omega_3^2 - 12c_s^4\omega_1^3\omega_2\omega_3^2 - 8\omega_2^2\omega_3^2 - 216v_1^2c_s^2\omega_1\omega_2^2\omega_3^2 - 54c_s^4\omega_1^2\omega_2^2\omega_3^2 + 8v_2^2\omega_2^2\omega_3^2 + 4v_2^2\omega_1^2\omega_2^2\omega_3^2 - 48v_1^2v_2^2\omega_1^2\omega_2\omega_3^2 - 36v_1^4\omega_1\omega_2^2\omega_3^2 - 2c_s^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 216v_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 22c_s^2\omega_1\omega_2^2\omega_3^2 - 72v_1^2v_2^2\omega_2^2\omega_3^2 - 20c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 - 24v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 42c_s^4\omega_1^2\omega_2^2\omega_3^2 - 24v_1^2\omega_1^2\omega_2^2\omega_3^2$$

$$C_{23} = -18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^2 - 5\omega_1^3\omega_2^2\omega_3 + 81c_s^2\omega_1^2\omega_2^2\omega_3 + 5v_2^2\omega_1^3\omega_2^2\omega_3 - 66v_1^2\omega_1\omega_2^2\omega_3 - 18c_s^2\omega_1^2\omega_2^2 + 3\omega_1\omega_2^2\omega_3 + 12v_2^2\omega_1\omega_2^2 - 12\omega_1\omega_2^2 + 27v_2^2\omega_1\omega_2^2\omega_3 + 84v_1^2\omega_2^2\omega_3 - 120v_1^2\omega_1\omega_2^2\omega_3 + 6v_2^2\omega_1^2\omega_2\omega_3 - 15c_s^2\omega_1^2\omega_2^2\omega_3 + 6\omega_1^2\omega_2\omega_3 - 108c_s^2\omega_1^3\omega_2\omega_3 + 6v_2^2\omega_1\omega_2^2\omega_3 - 12v_1^2\omega_1\omega_2^2\omega_3 + 42\omega_1\omega_2^2\omega_3 + 27c_s^2\omega_1^3\omega_2^2 + 12v_2^2\omega_2^2\omega_3 - 36\omega_1^3\omega_3 - 12c_s^2\omega_2^2\omega_3 + 132v_2^2\omega_1^2\omega_2^2\omega_3 + 27c_s^2\omega_1\omega_2^2\omega_3 + 9v_2^2\omega_1^2\omega_2^2 + 84c_s^2\omega_1^3\omega_3 - 12\omega_2^2\omega_3 - 9\omega_1^3\omega_2^2 -$$

$$24v_2^2\omega_3^2\omega_3 - 9v_2^2\omega_1^2\omega_2^2\omega_3 + 15c_s^2\omega_1^2\omega_2^2\omega_3 - 51\omega_1^2\omega_2^2\omega_3 - 54c_s^2\omega_1\omega_2^2\omega_3 - 6v_2^2\omega_1^2\omega_2 - 9v_2^2\omega_1^2\omega_2^2 - 66v_1^2\omega_1^2\omega_2\omega_3 + 6\omega_1^3\omega_2 + 9\omega_1^2\omega_2^2 + 36c_s^2\omega_1\omega_2^2 + 48v_1^2\omega_1^3\omega_3 + 5\omega_1^2\omega_3^2\omega_3 - 18c_s^2\omega_1^2\omega_2\omega_3 + 48\omega_1^3\omega_2\omega_3 + 6\omega_1^2\omega_2^2 - 5v_2^2\omega_1^2\omega_3^2\omega_3 - 6v_2^2\omega_1^2\omega_2^2 - 18v_2^2\omega_3^2\omega_2\omega_3$$

[illegible]

$$12\omega_1^2\omega_2\omega_3 - 9v_1^3\omega_1\omega_2\omega_3 + 6\omega_1^3\omega_2 - 18c_s^2\omega_1\omega_2^3 + 12v_1^2\omega_1^3\omega_3 + 23\omega_1^2\omega_2^3\omega_3 - 18c_s^2\omega_1^2\omega_2\omega_3 + 48\omega_1^3\omega_2\omega_3 - 12\omega_1^2\omega_2^2 - 50v_2^2\omega_2^3\omega_3 - 75v_2^2\omega_1^3\omega_2\omega_3$$

$$\begin{aligned} C_{28} = & 160\omega_4^2v_2^2\omega_2^3\omega_3^2 + 56\omega_4^2c_s^2\omega_1\omega_2\omega_3^2 + 120\omega_4^2v_4^4\omega_1^2\omega_2\omega_3^2 + 320\omega_4^2c_s^2v_2^2\omega_1^3\omega_3^2 - 104\omega_4^2c_s^2\omega_1^3\omega_3^2 + 36\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2 - 36\omega_4^2c_s^2v_2^2\omega_1^3\omega_2\omega_3^2 - \\ & 276\omega_4^2c_s^4\omega_1^3\omega_2\omega_3^2 - 8\omega_4^2\omega_1^2\omega_2^3\omega_3^2 + 9\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3^2 - 56\omega_4^2c_s^2v_2^2\omega_1\omega_2^3\omega_3^2 + 54c_s^4\omega_1^3\omega_2^3\omega_3^2 - 342\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 + 6v_1^4\omega_4^2\omega_1^2\omega_2^3\omega_3^2 + 36c_s^2\omega_1^2\omega_2^3\omega_3^2 - \\ & 6\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3^2 + 108\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 - 88\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2 - 24\omega_4^2v_4^4\omega_1\omega_2\omega_3^2 + 56\omega_4^2c_s^2\omega_1\omega_2\omega_3^2 - 56\omega_4^2c_s^2v_2^2\omega_1\omega_2\omega_3^2 + 92\omega_4^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + \\ & 120\omega_4^2c_s^4\omega_1\omega_2^3\omega_3^2 + 448\omega_4^2c_s^2v_2^2\omega_1\omega_2\omega_3^2 - 6v_1^4\omega_4^2\omega_1^2\omega_2^3\omega_3^2 + 6\omega_4^2c_s^2v_2^2\omega_1^3\omega_2^3\omega_3^2 + 152\omega_4^2v_2^2\omega_1^2\omega_2\omega_3^2 - 16\omega_4^2\omega_2^3\omega_3^2 + 12\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 - 144\omega_4^2v_4^4\omega_1^2\omega_2^3\omega_3^2 + \\ & 1232\omega_4^2c_s^2v_2^2\omega_1\omega_2^3\omega_3^2 - 20\omega_4^2\omega_1^3\omega_2\omega_3^2 - 18v_1^2\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 - 9\omega_4^2c_s^2v_2^2\omega_1^3\omega_2^3\omega_3^2 + 144\omega_4^2c_s^4\omega_1^3\omega_3^2 - 14\omega_4^2\omega_1^2\omega_2^3\omega_3^2 + 18c_s^2v_2^2\omega_1^3\omega_2^3\omega_3^2 + 9\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3^2 + \\ & 78\omega_4^2v_2^2\omega_1^2\omega_2^3\omega_3^2 - 9\omega_4^2c_s^2v_2^2\omega_1^3\omega_2^3\omega_3^2 - 368\omega_4^2c_s^2\omega_1\omega_2^3\omega_3^2 + 394\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 48\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 + 216\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 + 104\omega_4^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + \\ & 228\omega_4^2v_4^4\omega_1\omega_2^3\omega_3^2 - 118\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 + 28\omega_4^2\omega_1\omega_2^3\omega_3^2 - 712\omega_4^2c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 - 108\omega_4^2c_s^4\omega_1^3\omega_2\omega_3^2 - 18\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3^2 + 18\omega_4^2c_s^2v_2^2\omega_1^3\omega_2^3\omega_3^2 - \\ & 136\omega_4^2v_2^2\omega_1^2\omega_2\omega_3^2 - 144\omega_4^2c_s^4\omega_1\omega_2^3\omega_3^2 - 460\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 184\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 - 288\omega_4^2c_s^4\omega_2^3\omega_3^2 - 18c_s^2\omega_1^3\omega_2^3\omega_3^2 - 108\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 + \\ & 208\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2 + 48\omega_4^2v_4^4\omega_1^2\omega_2\omega_3^2 - 27\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3^2 - 36\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 + 14\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 168\omega_4^2c_s^4\omega_1\omega_2^3\omega_3^2 + 32\omega_4^2v_2^2\omega_1\omega_2^3\omega_3^2 + 72\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 + \\ & 40\omega_4^2c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 + 18v_1^2\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 + 18\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3^2 - 108c_s^4\omega_1^3\omega_2^3\omega_3^2 - 132\omega_4^2v_2^2\omega_1^3\omega_2\omega_3^2 - 40\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 - 78\omega_4^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 54\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3^2 - \\ & 6v_1^2\omega_4^2\omega_1^2\omega_2^3\omega_3^2 + 52\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 - 36\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 208\omega_4^2c_s^2\omega_2^3\omega_3^2 - 412\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 588\omega_4^2c_s^4\omega_1\omega_2^3\omega_3^2 - 56\omega_4^2v_2^2\omega_1^2\omega_2^3\omega_3^2 - 8\omega_4^2\omega_1\omega_2^3\omega_3^2 - \\ & 784\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 - 92\omega_4^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 36\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 + 6v_1^4\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 27\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3^2 - 96\omega_4^2v_4^4\omega_1^2\omega_2^3\omega_3^2 - 72\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 - 36c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + \\ & 8\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 16\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 + 36\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 + 16\omega_4^2\omega_1^2\omega_2\omega_3^2 + 16\omega_4^2c_s^2v_2^2\omega_1^2\omega_2\omega_3^2 + 144\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 + 72\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3\omega_3^2 - 256\omega_4^2v_2^2\omega_1\omega_2^3\omega_3^2 \end{aligned}$$

$$C_{29} = 6\omega_4v_2^2\omega_1\omega_2\omega_3 - 18v_1^2\omega_4\omega_2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 - 9\omega_4v_2^2\omega_1\omega_2 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 4\omega_4v_2^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 - 9v_2^2\omega_1\omega_2\omega_3 + 2\omega_4v_2^2\omega_1\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 + 18v_1^2\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$\begin{aligned} C_{30} = & 10\omega_4c_s^4\omega_1^2\omega_2\omega_3 - 18\omega_4c_s^4\omega_1^2\omega_2^2 + 8\omega_4c_s^4\omega_1^3\omega_2 + 24\omega_4c_s^2v_2^2\omega_1\omega_2^3 - 3v_1^2\omega_4c_s^2\omega_1^2\omega_2^3\omega_3 - 60\omega_4c_s^2v_2^2\omega_1\omega_2^3\omega_3 + 36c_s^4\omega_1\omega_2^3\omega_3 + \\ & 138\omega_4v_2^2\omega_1^3\omega_2^3\omega_3 + 8\omega_4\omega_1^2\omega_2\omega_3 - 54\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4c_s^2\omega_1^3\omega_2^2 - v_2^2\omega_4\omega_1^2\omega_2^2\omega_3 + 27c_s^2v_2^2\omega_1^2\omega_2^2\omega_3 + 120\omega_4c_s^2v_2^2\omega_1\omega_2\omega_3 + 84\omega_4v_2^2\omega_1^2\omega_2^2\omega_3 + \\ & 20\omega_4c_s^4\omega_1^2\omega_2^2 + 18\omega_4c_s^2\omega_1^3\omega_2^2 - 60\omega_4v_2^2\omega_1^3\omega_3 - 4\omega_4\omega_1\omega_2^3\omega_3 + v_1^4\omega_4\omega_1^2\omega_2^3\omega_3 + 408\omega_4v_4^4\omega_1\omega_2^3\omega_3 - 24\omega_4c_s^2\omega_1^3\omega_2^3\omega_3 + 40\omega_4c_s^2\omega_2^3\omega_3 - 8\omega_4c_s^2\omega_1^3\omega_2 + \\ & 18\omega_4c_s^2\omega_1^2\omega_2^3 + 144\omega_4c_s^2v_2^2\omega_1^3\omega_3 + 192\omega_4v_2^4\omega_1^2\omega_2\omega_3 + 32\omega_4c_s^2\omega_1\omega_2^3\omega_3 + 7\omega_4\omega_1^3\omega_2^3\omega_3 - 32\omega_4c_s^4\omega_1^2\omega_2\omega_3 + 432\omega_4c_s^2v_2^2\omega_1\omega_2^3\omega_3 + 36c_s^2\omega_1^2\omega_2^3\omega_3 + \\ & 4\omega_4\omega_1^3\omega_3 + 108c_s^2v_2^2\omega_1\omega_2^3\omega_3 + 9\omega_4c_s^4\omega_1^3\omega_2^2 - 29\omega_4c_s^4\omega_1^2\omega_2^3\omega_3 + 14\omega_4\omega_1\omega_2^3\omega_3 - 20\omega_4c_s^2\omega_1^2\omega_2^2 + 9c_s^4\omega_1^3\omega_2^3\omega_3 - 24\omega_4v_4^4\omega_1\omega_2^3\omega_3 - 16\omega_4c_s^2\omega_1^2\omega_2\omega_3 + \\ & 81\omega_4v_2^2\omega_1^2\omega_2^3\omega_3 + 153\omega_4c_s^2v_2^2\omega_1^2\omega_2^3\omega_3 + 96\omega_4v_2^2\omega_1^3\omega_3 - 18\omega_4c_s^4\omega_1^3\omega_2^2 - 68\omega_4c_s^4\omega_2^3\omega_3 + 138\omega_4v_2^2\omega_1^3\omega_2\omega_3 - 8\omega_4\omega_2^3\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - \\ & 288\omega_4c_s^2v_2^2\omega_1^2\omega_2\omega_3 - 108c_s^2v_2^2\omega_1^2\omega_2^3\omega_3 - 54\omega_4c_s^2v_2^2\omega_1^3\omega_2^2 + 94\omega_4c_s^4\omega_1\omega_2^3\omega_3 - 153\omega_4c_s^2v_2^2\omega_1^2\omega_2^3\omega_3 - 36c_s^2\omega_1\omega_2^3\omega_3 - 312\omega_4c_s^2v_2^2\omega_1^2\omega_2^3\omega_3 - \\ & 81\omega_4v_2^2\omega_1^2\omega_2^3\omega_3 - 168\omega_4v_4^4\omega_1\omega_2^3\omega_3 - 8\omega_4c_s^2\omega_1\omega_2^3 - 7\omega_4\omega_1^2\omega_2^3\omega_3 + 16\omega_4c_s^4\omega_1^3\omega_3 - 264\omega_4v_4^4\omega_2^3\omega_3 - 10\omega_4\omega_1^3\omega_2\omega_3 + 17\omega_4c_s^4\omega_1^2\omega_2^3\omega_3 + \\ & 27\omega_4c_s^2v_2^2\omega_1^2\omega_2^2 - 222\omega_4v_2^2\omega_1\omega_2^3\omega_3 - 90\omega_4c_s^2v_2^2\omega_1^2\omega_2^3\omega_3 - 28\omega_4c_s^4\omega_1\omega_2^3\omega_3 - 96\omega_4v_2^2\omega_1^2\omega_2\omega_3 + 60\omega_4c_s^2v_2^2\omega_1^2\omega_2^2 + v_1^4\omega_4\omega_1^2\omega_2^3\omega_3 + 24\omega_4c_s^2\omega_1^2\omega_2^3\omega_3 - \\ & v_1^4\omega_4\omega_1^2\omega_2^3\omega_3 + 42\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 36c_s^4\omega_1^2\omega_2^3\omega_3 - 54\omega_4c_s^2v_2^2\omega_1^2\omega_2^2 - 9c_s^2\omega_1^2\omega_2^3\omega_3 - 20\omega_4c_s^2\omega_1^3\omega_3 + 24\omega_4c_s^2v_2^2\omega_1^2\omega_2 + 8\omega_4c_s^4\omega_1^2\omega_2\omega_3 + \\ & 8\omega_4c_s^4\omega_1\omega_2^3 + 12\omega_4v_2^2\omega_1\omega_2^3\omega_3 + 3v_1^2\omega_4c_s^2\omega_1^2\omega_2^3\omega_3 - 3\omega_4c_s^2\omega_1^3\omega_2^3\omega_3 + 144\omega_4v_2^2\omega_2^3\omega_3 - 240\omega_4v_2^2\omega_1^2\omega_2\omega_3 - 138\omega_4v_2^2\omega_1^2\omega_2^3\omega_3 - 4\omega_4\omega_1^2\omega_2^3\omega_3 \end{aligned}$$

$$C_{31} = 12v_2^2\omega_2 - 2c_s^2\omega_1 - 9v_1^4\omega_1\omega_2 - 6v_2^2\omega_1 + 4c_s^4\omega_2 + 9v_2^2\omega_1\omega_2 + 48c_s^2v_2^2\omega_2 + 2c_s^4\omega_1 + 24c_s^2v_2^2\omega_1 - 12v_2^2\omega_2 + 3c_s^2\omega_1\omega_2 - 4c_s^2\omega_2 - 36c_s^2v_2^2\omega_1\omega_2 + 6v_2^4\omega_1 - 3c_s^4\omega_1\omega_2$$

$$\begin{aligned} C_{32} = & -9v_2^3\omega_1^3\omega_3 - 15\omega_4v_4^4\omega_1^3\omega_2^3 + 6\omega_4^2c_s^2v_2^2\omega_1^3\omega_3^2 + \omega_4^2c_s^2\omega_1^3\omega_2^2 + 24\omega_4^2c_s^4\omega_1^2\omega_2^2 + 27\omega_4^2c_s^2v_2^2\omega_1^3 - 36\omega_4v_2^2\omega_1^2\omega_2^3 - 18v_1^2\omega_1^2\omega_2^3 - \\ & 108\omega_4c_s^2v_2^2\omega_1^3\omega_3 + 12\omega_4^2c_s^2\omega_1^3\omega_2^2 - 36\omega_4v_4^4\omega_1^3\omega_2^3 - 12\omega_4c_s^2\omega_1^3\omega_2^2 + 72\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3 - 18\omega_4v_2^2\omega_1^3\omega_2^3 - 36\omega_4c_s^2v_2^2\omega_1^2\omega_2^2 + 54c_s^4\omega_1^2\omega_2^2\omega_3 + \\ & 3\omega_4^2c_s^2\omega_1^3\omega_3 + 15\omega_4v_2^2\omega_1^2\omega_2^3 + 54\omega_4c_s^2v_2^2\omega_1^3\omega_3 + 9v_1^2\omega_1^3\omega_2^2 - 3\omega_4^2c_s^4\omega_1^3\omega_3 + 24\omega_4^2c_s^4\omega_2^3 - 8\omega_4^2c_s^2\omega_1^2\omega_2^3 + 18v_2^2\omega_1^2\omega_2^3 + 9\omega_4v_4^4\omega_1^2\omega_2^2 - 12\omega_4^2c_s^2v_2^2\omega_1^2\omega_2^3 + \\ & 36\omega_4v_2^2\omega_1^2\omega_2^3 - 12\omega_4^2c_s^4\omega_1^2\omega_2^2 + 12\omega_4c_s^4\omega_1\omega_2^3 + 36\omega_4v_2^2\omega_1^2\omega_2^3 + 72\omega_4c_s^2v_2^2\omega_1^2\omega_2^3 - 36\omega_4^2c_s^2v_2^2\omega_1^3\omega_3 - 18\omega_4^2v_4^4\omega_1^2\omega_2^3 + 18\omega_4v_4^4\omega_1^2\omega_2^3 - 3\omega_4^2c_s^2\omega_1^3\omega_3 + \\ & 12\omega_4^2c_s^4\omega_1\omega_3 + 12\omega_4^2v_2^2\omega_1^2\omega_2^3 + 36\omega_4c_s^2v_2^2\omega_1\omega_2^3 - 12\omega_4c_s^2\omega_1^2\omega_2^3 - 3\omega_4c_s^2\omega_1^3\omega_2^2 + 3\omega_4^2v_2^2\omega_1^2\omega_2^3 + 15\omega_4^2v_2^2\omega_1^2\omega_2^3 + 27c_s^2v_2^2\omega_1^3\omega_2^3 + 36\omega_4^2v_2^2\omega_1^2\omega_2^3 + \\ & 12\omega_4^2c_s^2\omega_1\omega_2^3 - 36\omega_4^2c_s^2v_2^2\omega_1\omega_2^3 - 12\omega_4^2v_2^2\omega_1^2\omega_2^3 - 12\omega_4^2c_s^2\omega_1\omega_3 + 36\omega_4^2c_s^2v_2^2\omega_1\omega_3 + 12\omega_4c_s^4\omega_1^2\omega_2^3 + 3\omega_4c_s^4\omega_1^3\omega_2^3 + 18\omega_4^2v_2^2\omega_1^2 - 3\omega_4^2v_2^2\omega_1^3\omega_2^3 - \\ & 54c_s^2v_2^2\omega_1^2\omega_2^3 - 15\omega_4^2v_2^2\omega_1^3\omega_3 - 48\omega_4^2c_s^2\omega_1\omega_2^3 - 36\omega_4^2v_2^2\omega_1^2\omega_2^3 - 9\omega_4^2v_2^2\omega_1^3 \end{aligned}$$

$$\begin{aligned} C_{33} = & 8\omega_1\omega_2^3\omega_3 - 12c_s^2\omega_1^2\omega_2^3 + 48v_1^4\omega_2^3\omega_3 + 4\omega_1^3\omega_2^3 + 4c_s^2\omega_1^2\omega_2^3\omega_3 + 20c_s^2\omega_2^3\omega_3 + 24c_s^4\omega_1\omega_2^3\omega_3 - 36c_s^4\omega_1^2\omega_2\omega_3 + 216v_1^2c_s^2\omega_1^2\omega_2^3\omega_3 + 22c_s^2\omega_1v_2^3\omega_2^3\omega_3 - \\ & 24v_1^2\omega_2^3\omega_3 + 96v_1^4\omega_1v_2^3\omega_2^3\omega_3 - 36v_1^4\omega_1^2\omega_2\omega_3 + 5c_s^2\omega_1^2\omega_2\omega_3 - 4\omega_1^2\omega_2\omega_3 - 4c_s^2\omega_1^3v_2^3\omega_2\omega_3 + 56c_s^2\omega_1^3\omega_2\omega_3 - 8\omega_1v_2^3\omega_2^3\omega_3 + 54c_s^4\omega_1^2\omega_2^2\omega_3 - \\ & 4c_s^2\omega_1^2v_2^3\omega_2\omega_3 - 36c_s^4\omega_1^2\omega_2^2 + 48v_1^4\omega_1\omega_2^3\omega_3 + 24v_1^4\omega_1^2v_2^3\omega_2\omega_3 + 4\omega_1^3v_2^3\omega_2\omega_3 + 36c_s^4\omega_1^2\omega_2^2 + 6c_s^4\omega_1^3\omega_2^2\omega_3 + 24v_1^4\omega_1v_2^3\omega_2^3\omega_3 - 324v_1^4c_s^2\omega_1^3\omega_2\omega_3 - \\ & 12c_s^2\omega_1^3v_2^3\omega_2 - 36c_s^4\omega_2^3\omega_3 + 8c_s^2\omega_1v_2^3\omega_2^3\omega_3 + 24v_1^4\omega_2^3\omega_3 - 24v_1^4\omega_1^3\omega_2\omega_3 - 72v_1^2c_s^2\omega_1^2\omega_2^3\omega_3 + 4\omega_1^2v_2^3\omega_2\omega_3 - 48v_1^4\omega_1^3v_2^3\omega_2\omega_3 + 18c_s^2\omega_1^3\omega_2^3\omega_3 + 8\omega_1\omega_2^3\omega_3 - \\ & 4\omega_1^3v_2^3\omega_3 + 4c_s^2\omega_1^3\omega_2\omega_3 - 72v_1^2v_2^3\omega_2^3\omega_3 - 20c_s^2\omega_1^3v_2^3\omega_2\omega_3 + 42c_s^4\omega_1\omega_2^3\omega_3 + 8c_s^2\omega_1v_2^3\omega_2\omega_3 + 8v_2^3\omega_2^3\omega_3 - 60v_1^2\omega_1\omega_2^3\omega_3 + 24v_1^4\omega_1^2v_2^3\omega_2^3 + 12c_s^2\omega_1^3\omega_2^2 + \\ & 72v_1^4\omega_1^2\omega_2^3\omega_3 - 8\omega_1v_2^3\omega_2^3\omega_3 + \omega_1^3\omega_2^3\omega_3 - 34c_s^2\omega_1^2\omega_2^3\omega_3 + 108v_1^2c_s^2\omega_1\omega_2^3\omega_3 - 24v_1^2\omega_1^2v_2^3\omega_2^3\omega_3 - 12c_s^4\omega_1^2\omega_2\omega_3 - 2c_s^2\omega_1^2v_2^3\omega_2^3\omega_3 - 48v_1^4\omega_1^3\omega_2^2 - \omega_2^2\omega_2^3\omega_3 + \\ & 72c_s^4\omega_1^3\omega_2^2 + 40c_s^2\omega_1^2\omega_2\omega_3 - 8c_s^2\omega_1\omega_2^3\omega_3 - 4\omega_1^3\omega_2\omega_3 + 24v_1^4\omega_1^2\omega_2^3\omega_3 + 72v_1^4c_s^2\omega_1^2\omega_2^3\omega_3 - 84c_s^4\omega_1^3\omega_2\omega_3 - 4c_s^2\omega_1^2v_2^3\omega_2^3\omega_3 + 84v_1^4\omega_1^3\omega_2\omega_3 - 6c_s^4\omega_1^3\omega_2^2\omega_3 + \\ & 24v_1^4\omega_1^3v_2^3\omega_2^3\omega_3 - 8c_s^2\omega_1\omega_2^3\omega_3 + 4\omega_1^2v_2^3\omega_2^3\omega_3 + 2c_s^2\omega_1^3v_2^3\omega_2^3\omega_3 - 18c_s^2\omega_1^3\omega_2^3\omega_3 - 72v_1^4\omega_1\omega_2^3\omega_3 - 5c_s^2\omega_1^3\omega_2^3\omega_3 + 18c_s^2\omega_1^3v_2^3\omega_2^3\omega_3 - 4\omega_1^2\omega_2^3\omega_3 + \\ & 12c_s^2\omega_1^3v_2^3\omega_3 - 52c_s^2\omega_1^2\omega_2^3\omega_3 + 24v_1^4\omega_1^2\omega_2^3\omega_3 - 2c_s^2\omega_1^2v_2^3\omega_2^3\omega_3 - 12c_s^4\omega_1^3\omega_2\omega_3 - 8\omega_2^3\omega_3 - 216v_1^2c_s^2\omega_1\omega_2^3\omega_3 - 20c_s^2v_2^3\omega_2^3\omega_3 - \omega_1^3v_2^3\omega_2^3\omega_3 - 54c_s^4\omega_1^2\omega_2^3\omega_3 - \\ & 48v_1^4\omega_1^3v_2^3\omega_2^3\omega_3 - 36v_1^4\omega_1\omega_2^3\omega_3 + 216v_1^2c_s^2\omega_1^2\omega_2^3\omega_3 - 22c_s^2\omega_1\omega_2^3\omega_3 + 16c_s^2\omega_1^3v_2^3\omega_3 + \omega_1^3v_2^3\omega_2^3\omega_3 + 42c_s^4\omega_1^2\omega_2^3\omega_3 - 24v_1^4\omega_1^2\omega_2^3\omega_3 - 18c_s^2\omega_1^2v_2^3\omega_2^3\omega_3 \end{aligned}$$

$$\begin{aligned} C_{34} = & -18c_s^2\omega_1^3\omega_2 + 27\omega_1v_2^3\omega_2^3\omega_3 - 27c_s^2\omega_1^2\omega_2^2 - 5\omega_1^2\omega_2^2\omega_3 + 81c_s^2\omega_1^2\omega_2^3\omega_3 - 24v_2^3\omega_2^3\omega_3 - 66v_1^2\omega_1\omega_2^3\omega_3 + 6\omega_1^2v_2^3\omega_2\omega_3 + 12\omega_1^3v_2^3\omega_3 - \\ & 18c_s^2\omega_1^2\omega_2^2 + 3\omega_1\omega_2^3\omega_3 - 12\omega_1\omega_2^2\omega_3 + 84v_1^4\omega_2^3\omega_3 - 120v_1^2\omega_1\omega_2^3\omega_3 - 6\omega_1^2v_2^3\omega_2 - 18\omega_1^2v_2^3\omega_2\omega_3 - 15c_s^2\omega_1^2\omega_2^3\omega_3 + 6\omega_1^2\omega_2\omega_3 + 6\omega_1v_2^3\omega_2^3\omega_3 - \\ & 108c_s^2\omega_1^3\omega_2\omega_3 - 9\omega_1^2v_2^3\omega_2 - 12v_1^2\omega_1^2\omega_2\omega_3 + 42\omega_1\omega_2^3\omega_3 + 27c_s^2\omega_1^2\omega_2^2 - 36\omega_1^2\omega_2^2 - 12c_s^2\omega_2^3\omega_3 + 132v_1^2\omega_1^2\omega_2^3\omega_3 - 6\omega_1^2v_2^3\omega_2 + 27c_s^2\omega_1\omega_2^3\omega_3 - \\ & 5\omega_1^2v_2^3\omega_2\omega_3 + 84c_s^2\omega_1^3\omega_3 - 12\omega_2^3\omega_3 + 5\omega_1^3v_2^3\omega_2^3\omega_3 - 9\omega_1^3\omega_2^2 + 12\omega_1v_2^3\omega_2^3 + 15c_s^2\omega_1^3\omega_2^3\omega_3 - 51\omega_1^2\omega_2^3\omega_3 - 54c_s^2\omega_1\omega_2^3\omega_3 - 9\omega_1^2v_2^3\omega_2^3\omega_3 - \\ & 66v_1^4\omega_1^3\omega_2\omega_3 + 6\omega_1^2\omega_2 + 9\omega_1\omega_2^2 + 36c_s^2\omega_1\omega_2^2 + 48v_1^4\omega_1^3\omega_3 + 5\omega_1\omega_2^3\omega_3 - 18c_s^2\omega_1^2\omega_2\omega_3 + 48\omega_1^3\omega_2\omega_3 + 6\omega_1^2\omega_2^2 + 9\omega_1^3v_2^3\omega_2 \end{aligned}$$

$$\begin{aligned} C_{35} = & 24\omega_2^2\omega_1^3v_2^3\omega_2^3\omega_3^2 - 32\omega_4^2c_s^2\omega_1\omega_2^3\omega_3^2 - 540v_1^2\omega_4c_s^2\omega_1^2\omega_2^3\omega_3^2 + 72v_2^2\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 40\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3^2 + 117v_1^2\omega_4\omega_1^3\omega_2^3\omega_3^2 - 96\omega_4^2c_s^2\omega_1v_2^3\omega_2^3\omega_3^2 + \\ & 60v_1^2\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 48v_1^2\omega_4^2\omega_2^3\omega_3^2 + 36\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 - 28\omega_4^2c_s^4\omega_1^3\omega_2\omega_3^2 - 8\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 18\omega_4c_s^2\omega_1^3\omega_2^3\omega_3^2 - 54v_1^2\omega_1^3\omega_2^3\omega_3^2 + 576v_1^2\omega_4^2\omega_1v_2^3\omega_2^3\omega_3^2 + \\ & 86\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 - 60v_1^4\omega_4^2\omega_1^2\omega_2^3\omega_3^2 - 117v_4^4\omega_4\omega_1^3\omega_2^3\omega_3^2 - 492v_1^2\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3^2 + 36v_1^2\omega_4\omega_1^3\omega_2^3\omega_3^2 + 8v_1^2\omega_4^2\omega_1^2\omega_2^3\omega_3^2 + 48\omega_4^2c_s^2\omega_1v_2^3\omega_2^3\omega_3^2 - \\ & 72\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3^2 - 108\omega_4^2\omega_1^3\omega_2^3\omega_3^2 + 64\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2 + 204v_1^2\omega_4^2\omega_1^2\omega_2\omega_3^2 - 16\omega_4^2c_s^2\omega_1\omega_2^3\omega_3^2 - 108v_1^2\omega_4c_s^2\omega_1^2\omega_2^3\omega_3^2 + 40\omega_4^2c_s^4$$

$$\begin{aligned}
& 24v_1^4w_4w_1^3w_2w_3 + 144v_1^2w_1^2w_1v_3^2w_2^2w_3^2 + 32w_2^2c_s^4w_1^3w_3^2 - 492v_1^2w_4^2c_s^2w_1^3w_2w_3^2 - 2w_4^2w_1^3w_3^2w_3^2 - 324v_1^2c_s^2w_1^3w_2^2w_3^2 - 36v_1^2w_4w_1^3w_2^2w_3^2 - 18w_2^2c_s^2w_1^3w_3^2w_3^2 - \\
& 216v_1^2w_1^2w_1^3w_3^2w_3^2 + 6w_4^2w_1^3v_3^2w_2^2w_3^2 + 48v_1^4w_4^2w_1^3w_3^2 - 96w_4^2c_s^2w_1^3v_3^2w_2w_3^2 - 54v_1^2w_4^2w_1^3w_3^2 + 24v_1^2w_4^2w_1^3w_2w_3 + 48w_4^2c_s^2w_1w_3^2w_3^2 + 24w_1^2c_s^2w_1^3v_3^2w_3^2 - \\
& 288v_1^2w_1^2w_1^3v_3^2w_2w_3^2 + 16w_4^2c_s^4w_1^3w_2w_3 + 264v_1^2w_4^2c_s^2w_1^3w_3^2 - 72v_1^4w_4w_1w_3^2w_3^2 - 144v_1^4w_4^2w_1^3w_2^2w_3^2 - 36w_4^2c_s^4w_1^3w_2^2w_3 + 24w_4^2c_s^2v_3^2w_3^2w_3^2 - \\
& 108v_1^2w_4^2c_s^2w_1^3w_2^2w_3 - 6w_4^2w_1^3v_3^2w_2^2w_3^2 - 72w_4^2c_s^2w_1w_3^2w_3^2 + 108v_1^4w_4w_1^3w_2^2w_3 + 72v_1^2w_4w_1w_3^2w_3^2 + 36v_1^2w_4^2w_1^3w_2^2 + 648v_1^2w_4c_s^2w_1^3w_2^2w_3^2 - \\
& 108v_1^2w_4w_1^3w_3^2w_3^2 - 12w_4^2c_s^2w_1v_3^2w_2^2w_3^2 + 240v_1^2w_4^2w_1^3w_2^2w_3^2 - 24w_4^2w_1^3v_3^2w_2^2w_3^2 + 16w_4^2w_1^3w_2^2w_3^2 - 297v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 - 36w_4^2c_s^4w_1^3w_2^2w_3 + 24v_1^4w_4^2w_1^3w_2^2w_3^2 + \\
& 192v_1^4w_1^2w_3^2w_3^2 + 24w_1^2w_1^3v_3^2w_2w_3^2 - 852v_1^2w_4^2c_s^2w_1w_3^2w_3^2 - 24v_1^4w_4^2w_1w_3^2w_3^2 - 72v_1^4w_4^2w_1^3w_2^2w_3^2 + 16w_4^2c_s^4w_1w_3^2w_3^2 - 144v_1^2w_4^2w_1^3v_3^2w_2^2w_3^2 + 96v_1^4w_4^2w_1^3w_2^2w_3^2 - \\
& 36w_4^2c_s^2w_1^3w_2^2w_3^2 + 80w_4^2c_s^4w_1^3w_2^2w_3^2 - 24v_1^2w_4^2w_1^3w_2^2w_3^2 + 72w_4^2c_s^2w_1^3v_3^2w_2^2w_3^2 - 144v_1^2w_4^2w_1^3w_2w_3^2 + 108v_1^2w_4c_s^2w_1^3w_2^2w_3^2 + 24v_1^2w_4^2w_1^3w_2^2w_3 + 36w_4^2c_s^2w_1^3w_2w_3^2 - \\
& 48w_4^2w_1v_3^2w_2^2w_3^2 + 54v_1^4w_1^3w_2^2w_3^2 + 18w_4^2c_s^4w_1^3w_2^2w_3^2 + 108v_1^2w_1^3w_2^2w_3^2 - 72w_4^2c_s^2w_1^3v_3^2w_2^2w_3^2 + 72w_4^2c_s^2w_1^3w_2^2w_3^2 + 2w_4^2w_1^3w_2^2w_3^2 + 96v_1^4w_4^2w_1^3w_2^2w_3^2 + \\
& 16w_4^2c_s^4w_1w_3^2w_3^2 - 56w_4^2c_s^4w_1^3w_2w_3^2 + 288v_1^4w_4w_1^3w_2^2w_3^2 + 168v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 - 6w_4^2c_s^4w_1^3w_2^2w_3^2 + 108v_1^4w_4^2w_1^3w_2^2w_3^2 + 324v_1^2w_4c_s^2w_1^3w_2^2w_3^2 - \\
& 144v_1^2w_4^2w_1w_3^2w_3^2 + 48w_4^2v_3^2w_2^2w_3^2 - 216v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 + 144v_1^2w_4^2w_1^3v_3^2w_2^2w_3^2 - 40w_4^2c_s^2w_1^3w_2^2w_3^2 - 108v_1^2w_4^2w_1^3w_2^2w_3^2 + 24w_4^2c_s^2w_1^3v_3^2w_2^2w_3^2 - \\
& 288v_1^4w_4w_1^3w_2^2w_3^2 + 432v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 - 108v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 - 48w_4^2w_1v_3^2w_2^2w_3^2 - 297v_1^2w_4c_s^2w_1^3w_2^2w_3^2 - 86v_1^2w_4^2w_1^3w_2^2w_3^2 - 12w_4^2c_s^2w_1^3w_2^2w_3^2 + \\
& 48w_4^2c_s^2w_1^3v_3^2w_2^2w_3^2 + 180v_1^2w_4w_1^3w_2^2w_3^2 + 336v_1^2w_4^2c_s^2w_1w_3^2w_3^2 - 12w_4^2c_s^2w_1^3v_3^2w_2^2w_3^2 - 96v_1^2w_4^2w_1^3w_2^2w_3^2 + 8w_4^2c_s^2w_3^2w_3^2 - 288v_1^2w_4^2w_1^3v_3^2w_2^2w_3^2 - \\
& 172w_4^2c_s^4w_1w_3^2w_3^2 + 54v_1^4w_4^2w_1^3w_2^2w_3^2 + 288v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 + 16w_4^2w_1w_3^2w_3^2 - 432v_1^2w_4^2v_3^2w_2^2w_3^2 - 180v_1^4w_4w_1^3w_2^2w_3^2 + 38v_1^4w_4^2w_1^3w_2^2w_3^2 + \\
& 18w_4^2c_s^4w_1^3w_2^2w_3^2 + 117v_1^2w_4^2w_1^3w_2^2w_3^2 + 36w_4^2c_s^2w_1^3w_2^2w_3^2 + 72w_4^2c_s^4w_1w_3^2w_3^2 + 24w_4^2w_1^3v_3^2w_2^2w_3^2 + 8w_4^2w_3^2w_3^2 + 36v_1^2w_4w_1^3w_2^2w_3^2 + 12w_4^2c_s^2w_1^3v_3^2w_2^2w_3^2 + \\
& 96v_1^4w_4^2w_1^3w_2^2w_3^2 - 16w_4^2c_s^2w_1^3w_2w_3^2 - 108v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 + 144v_1^2w_4^2w_1^3v_3^2w_2^2w_3^2 + 162v_1^2w_4^2c_s^2w_3^2w_3^2 + 72v_1^2w_4^2c_s^2w_1^3w_2^2w_3^2 - 36v_1^4w_4^2w_1^3w_2^2w_3^2 - \\
& 8w_4^2w_1^3w_2w_3^2 - 117v_1^4w_4^2w_1^3w_2^2w_3^2 - 2w_4^2c_s^4w_3^2w_3^2 + 162v_1^2c_s^2w_1^3w_2^2w_3^2 + 72v_1^2w_4^2c_s^2w_1w_3^2w_3^2 - 36v_1^4w_4^2w_1^3w_2^2w_3^2 + 264v_1^2w_4^2c_s^2w_1^3w_2w_3^2 - 288v_1^4w_4^2w_1w_3^2w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{36} = & -18c_s^5w_1^3w_2 + 4v_1^2w_1^3 - 12w_1w_2^2 - 12v_1^2w_1^3w_2 + 2v_3^2w_3^2 + 36c_s^2w_1^2w_2^2 - 3v_1^2w_1w_3^2 + 4w_1^3v_3^2 + 6w_1w_3^2 - 6w_1^2v_3^2w_2 + 6w_1^2v_3^2w_2^2 - 72c_s^2w_1^2w_2 + 4v_1^2w_1^3 - 12w_1^3 + \\
& 36c_s^2w_1^3 + 24w_1^2w_2 - 6v_1^2w_1^2w_2 - 3w_1^3v_3^2w_2 + 12v_1^2w_1w_3^2 - 3w_1^3v_3^2w_2 - 4v_1^2w_3^2 + 36c_s^2w_1w_2^2 - 3v_1^2w_1^3w_2 + 6w_1^3w_2 - 18c_s^5w_1w_2^2 - 12w_1^2w_2^2 + 2v_3^2w_3^2 + 6v_1^2w_1^3w_2^2
\end{aligned}$$

$$\begin{aligned}
C_{37} = & -36v_1^2w_4w_1^3w_2w_3^2 - 3w_4v_2^2w_1^3w_2w_3^2 - 6w_1^3w_2^2w_3 + 4w_4w_1^3v_3^2w_3^2 - 3w_4w_1^2v_3^2w_3^2w_3 + 3v_3^2w_1^3w_2^2w_3 + 6w_4w_1w_3^2w_3^2 + 6w_4c_s^2w_1w_3^2w_3 + \\
& 12v_1^2w_4w_1^3w_3^2 - 36w_4c_s^2w_1^3w_2w_3^2 + 3w_4w_1^2v_3^2w_3^2 + 18c_s^2w_1^3w_2^2w_3^2 + 36v_1^2w_4w_1w_3^2w_3^2 + 4w_4v_3^2w_2^2w_3^2 + w_4v_2^2w_1^3w_2^2w_3^2 - 12w_4w_3^2w_3^2 + 3w_4w_3^2v_3^2w_2^2w_3^2 + \\
& 6w_4w_1^2v_3^2w_2^2w_3^2 - 18w_4c_s^2w_1^3w_2^2w_3^2 - 12w_4c_s^2w_1w_3^2w_3^2 + 18w_4c_s^2w_1^3w_2^2w_3^2 - 4w_4w_1w_3^2w_3^2 + 4w_4v_2^2w_1^3w_3^2 + w_4w_1^2v_3^2w_2^2w_3^2 + 18w_4c_s^2w_1^3w_2^2w_3^2 - 3v_1^2w_1^3w_2^2w_3^2 - \\
& 6w_4w_1^3w_2^2w_3 + 20w_4c_s^2w_3^2w_3^2 - 18c_s^2w_1^3w_2^2w_3^2 + 6w_4v_2^2w_1^3w_2^2w_3^2 + 6w_1w_2^2w_3^2 - 2w_4w_1w_3^2w_3^2 - 3v_2^2w_1^3w_2^2w_3^2 + 20w_4w_1^2w_2w_3^2 - 18w_4c_s^2w_1w_3^2w_3^2 - \\
& 3w_4v_2^2w_1^3w_2^2w_3^2 - 3w_1v_3^2w_2^2w_3^2 + 6w_1^3w_2^2w_3^2 - 2w_4v_2^2w_1^3w_2^2w_3^2 + 18c_s^2w_1^3w_2^2w_3^2 + w_4w_1v_3^2w_2^2w_3^2 + 3v_2^2w_1^3w_2^2w_3^2 + 6w_4w_1^3w_2^2w_3^2 + 6w_4c_s^2w_1^3w_2^2w_3^2 - \\
& 12w_4w_2^2w_3^2 + 28w_4c_s^2w_1^3w_3^2 - 6w_1^2w_2^2w_3^2 + 3w_4v_2^2w_1^3w_2^2w_3^2 - 4w_4v_2^2w_1w_3^2w_3^2 + 4w_4v_2^2w_3^2w_3^2 + 3w_4v_2^2w_1^3w_2^2w_3^2 - 3w_1^2v_3^2w_2^2w_3^2 + 6w_4w_1^3w_3^2w_3^2 - \\
& 18w_4c_s^2w_1^3w_2^2w_3^2 + 3w_1^3v_3^2w_2^2w_3^2 - 4w_4w_1v_3^2w_2^2w_3^2 + 4w_4w_3^2w_2w_3^2 + 3w_1^2v_3^2w_2^2w_3^2 + 18c_s^2w_1^3w_2^2w_3^2 - 3w_4w_1^3v_3^2w_2w_3^2 - 3w_4w_1^3v_3^2w_2^2w_3^2 + w_4v_2^2w_1w_3^2w_3^2 - \\
& 4w_4v_2^2w_1^3w_2w_3^2 - 12v_1^2w_1^3w_2^2w_3^2 - 2w_4c_s^2w_1^3w_2^2w_3^2 - 2w_4w_1^3v_3^2w_2w_3^2 - 6w_1^2w_2^2w_3^2 - 3w_4v_2^2w_1w_3^2w_3^2 - 18w_4c_s^2w_1^3w_2^2w_3^2 - 4w_4w_1^2v_3^2w_2w_3^2 - \\
& 12w_4c_s^2w_1^3w_2w_3^2 - 3w_1^3v_3^2w_2^2w_3^2 + 6w_4w_1^2w_2w_3^2 + 3v_2^2w_1^3w_2^2w_3^2 - 3w_4v_2^2w_1^3w_2^2w_3^2 + 6w_1^2w_2^2w_3^2 - 18c_s^2w_1w_3^2w_3^2 + 3w_1^2v_3^2w_2^2w_3^2 - 3w_4w_1v_3^2w_2^2w_3^2 - \\
& 3v_2^2w_1^3w_2^2w_3^2 - 4w_4w_3^2w_3^2 + 36w_4c_s^2w_1^3w_2^2w_3^2 - 6w_4w_1^3w_2^2w_3^2 - 2w_4w_1^2w_2^2w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{38} = & -36w_1^2w_1^3v_3^2w_2^2w_3^2 + 72w_4^2v_2^2w_3^2w_3^2 - 72w_4^2c_s^2w_1w_2^2w_3^2 + 63w_4w_1^3v_3^2w_3^2w_3^2 - 72v_1^2w_4^2w_1^3w_2^2w_3^2 + 336w_1^2c_s^2w_1^3w_3^2 + 12v_1^2w_1^2w_1^3w_2^2w_3^2 + \\
& 48v_1^2w_4^2w_3^2w_3^2 + 54w_4^2w_1^3v_3^2w_2^2w_3^2 + 324w_4^2c_s^2w_1^3w_2^2w_3^2 + 108w_4w_3^2w_3^2w_3^2 - 108w_4^2w_1^3w_2^2w_3^2 + 189w_4c_s^2w_1^3w_2^2w_3^2 + 54v_1^2w_1^3w_2^2w_3^2 - 36w_4w_1^3v_3^2w_2^2w_3^2 - \\
& 36w_4w_1w_3^2w_3^2 + 72w_4^2w_1^3v_3^2w_2^2w_3^2 + 36v_1^2w_4w_1^3w_2^2w_3^2 - 36w_4^2w_1^3v_3^2w_2^2w_3^2 + 144w_4^2w_1^3v_3^2w_2^2w_3^2 - 144w_4^2c_s^2w_1^3w_2w_3^2 - 36v_1^2w_4^2w_1^3w_2w_3^2 - 36w_4^2c_s^2w_1w_2^2w_3^2 + \\
& 36w_4w_1^3v_3^2w_2^2w_3^2 + 36w_4w_1^3v_3^2w_2^2w_3^2 + 144w_4^2w_1^3w_2^2w_3^2 + 48w_4^2w_1^3w_2w_3^2 - 108w_4^2v_2^2w_1^3w_2^2w_3^2 + 72w_4w_1^3w_2^2w_3^2 + 24w_4^2w_3^2w_3^2 + 216w_4c_s^2w_1^3w_2^2w_3^2 - \\
& 108w_4^2w_1^3w_2^2w_3^2 + 72w_4^2w_1^3w_2w_3^2 - 63w_4^2w_1^3v_3^2w_2^2w_3^2 - 72w_4w_1^3w_2^2w_3^2 - 216w_4c_s^2w_1^3w_2^2w_3^2 + 20w_4^2w_1^3w_2^2w_3^2 - 36v_1^2w_4w_1^3w_2^2w_3^2 - \\
& 189w_4c_s^2w_1^3w_3^2w_3^2 - 36v_1^2w_4^2w_1^3w_2^2w_3^2 - 20w_4^2w_1^3v_3^2w_2^2w_3^2 + 54v_1^2w_4^2w_1^3w_2^2w_3^2 - 24v_1^2w_4^2w_1^3w_2w_3^2 - 36w_4w_1^3v_3^2w_2^2w_3^2 + 180w_4^2c_s^2w_1^3w_2^2w_3^2 - 63w_4w_1^3w_3^2w_3^2 + \\
& 48w_4^2w_1^3w_2^2w_3^2 - 324w_4c_s^2w_1^3w_2^2w_3^2 - 108w_4^2w_1^3v_3^2w_2^2w_3^2 + 216w_4^2v_2^2w_1^3w_2^2w_3^2 - 180w_4w_1^3v_3^2w_2^2w_3^2 + 20w_4^2w_1^3v_3^2w_2^2w_3^2 + 108w_4c_s^2w_1^3w_2^2w_3^2 - \\
& 36v_1^2w_4w_1w_3^2w_3^2 - 36v_1^2w_4^2w_1^3w_2^2w_3^2 - 60w_4^2w_1^3v_3^2w_2^2w_3^2 - 108v_1^2w_4^2w_1^3w_2^2w_3^2 + 60w_4^2c_s^2w_1^3w_2^2w_3^2 + 72v_1^2w_4^2w_1^3w_2^2w_3^2 - 54w_1^3v_3^2w_2^2w_3^2 + 48w_4^2w_1^3v_3^2w_2^2w_3^2 - \\
& 36w_4^2w_1w_3^2w_3^2 + 324w_4^2c_s^2w_1^3w_2^2w_3^2 + 72w_4^2w_1^3v_3^2w_2^2w_3^2 + 63w_4^2w_1^3w_2^2w_3^2 - 72w_4w_1^3w_2^2w_3^2 - 216w_4^2v_2^2w_1^3w_2w_3^2 - 60w_4^2c_s^2w_1^3w_2^2w_3^2 - 48v_1^2w_4^2w_1^3w_2w_3^2 + \\
& 12v_1^2w_4^2w_1^3w_2^2w_3^2 - 360w_4^2c_s^2w_1^3w_2w_3^2 + 24w_4^2w_1v_3^2w_2^2w_3^2 - 108v_1^2w_4^2w_1^3w_2^2w_3^2 - 432w_4^2c_s^2w_1^3w_2^2w_3^2 - 20w_4^2w_1^3w_2^2w_3^2 - 144w_4w_1^3w_2^2w_3^2 - 216w_4^2c_s^2w_1^3w_2^2w_3^2 - \\
& 48v_1^2w_4^2w_1w_3^2w_3^2 - 96w_4^2v_2^2w_3^2w_3^2 - 24w_4^2w_1v_3^2w_2^2w_3^2 - 144w_4^2c_s^2w_1^3w_2^2w_3^2 - 72w_4w_1^3v_3^2w_2^2w_3^2 + 36v_1^2w_4^2w_1^3w_2^2w_3^2 + 36v_1^2w_4w_1^3w_2^2w_3^2 + 108w_4^2w_1v_3^2w_2^2w_3^2 + \\
& 180w_4^2c_s^2w_1^3w_2^2w_3^2 + 180v_1^2w_4w_1^3w_2^2w_3^2 + 432w_4^2c_s^2w_1^3w_2^2w_3^2 - 108w_4^2w_1^3w_2^2w_3^2 + 48v_1^2w_4^2w_1^3w_2^2w_3^2 - 120w_4^2c_s^2w_1^3w_2^2w_3^2 + 144w_4w_1^3w_2^2w_3^2 + 144w_4^2v_2^2w_1^3w_2^2w_3^2 + \\
& 24w_4^2w_1w_3^2w_3^2 - 432w_4^2c_s^2w_1^3w_2^2w_3^2 + 324w_4^2c_s^2w_1^3w_2^2w_3^2 + 24w_4^2w_1^3v_3^2w_2^2w_3^2 - 144w_4^2w_3^2w_3^2 + 36v_1^2w_4w_1^3w_2^2w_3^2 - 36v_1^2w_4^2w_1^3w_2^2w_3^2 - 144w_4^2c_s^2w_1^3w_2w_3^2 + \\
& 108w_1^2v_3^2w_2^2w_3^2 + 12w_4^2w_1w_2^2w_3^2 + 72w_4w_1v_3^2w_2^2w_3^2 + 96w_4^2w_1^3w_2w_3^2 + 216w_4^2c_s^2w_1^3w_2^2w_3^2 - 24w_4^2w_1^3v_3^2w_2w_3^2 - 108w_4^2v_2^2w_1w_2^2w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{39} = & 216w_4^2w_1^3v_3^2w_2^2w_3^2 - 180w_4v_2^2w_1^3w_2^2w_3^2 - 96w_4^2v_2^2w_3^2w_3^2 - 72w_4^2c_s^2w_1w_2^2w_3^2 - 72v_1^2w_4^2w_1^3w_2^2w_3^2 + 336w_4^2c_s^2w_1^3w_3^2 + 12v_1^2w_4^2w_1^3w_2^2w_3^2 - \\
& 72w_4^2v_2^2w_1^3w_2^2w_3^2 + 48v_1^2w_4^2w_2^2w_3^2 + 324w_4^2c_s^2w_1^3w_2^2w_3^2 + 108w_4w_3^2w_3^2w_3^2 - 108w_4^2w_1^3w_2^2w_3^2 + 189w_4c_s^2w_1^3w_2^2w_3^2 + 54v_1^2w_1^3w_2^2w_3^2 - 60w_4^2v_2^2w_1^3w_2^2w_3^2 - \\
& 36w_4w_1w_3^2w_3^2 + 36v_1^2w_4^2w_1^3w_2^2w_3^2 - 144w_4^2c_s^2w_1^3w_2w_3^2 - 36v_1^2w_4^2w_1^3w_2w_3^2 - 36w_4^2c_s^2w_1w_3^2w_3^2 - 20w_4^2v_2^2w_1^3w_2^2w_3^2 + 144w_4^2w_1^3w_2^2w_3^2 - 54v_2^2w_1^3w_2^2w_3^2 + \\
& 48w_4^2w_1^3w_2w_3^2 - 72w_4^2v_2^2w_1^3w_2w_3^2 + 72w_4w_1^3w_2^2w_3^2 + 24w_4^2w_3^2w_3^2 + 216w_4c_s^2w_1^3w_2^2w_3^2 - 108w_4^2w_1^3w_2^2w_3^2 + 144w_4^2v_2^2w_1^3w_2^2w_3^2 + 72w_4^2w_1^3w_2^2w_3^2 + \\
& 144w_4^2w_1^3w_2w_3^2 - 24w_4^2v_2^2w_1^3w_2w_3^2 - 72w_4w_1^3w_2^2w_3^2 - 216w_4^2c_s^2w_1^3w_2^2w_3^2 + 20w_4^2w_1^3w_2^2w_3^2 - 36v_1^2w_4w_1^3w_2^2w_3^2 - 189w_4^2c_s^2w_1^3w_2^2w_3^2 + 54w_4^2v_2^2w_1^3w_2^2w_3^2 - \\
& 36v_1^2w_4^2w_1^3w_2^2w_3^2 + 36w_4v_2^2w_1^3w_2^2w_3^2 + 54v_2^2w_4^2w_1^3w_2^2w_3^2 - 24v_1^2w_4^2w_1^3w_2w_3^2 - 180w_4^2c_s^2w_1^3w_2w_3^2 - 63w_4w_1^3w_2^2w_3^2 + 48w_4^2w_1^3w_2^2w_3^2 - 324w_4^2c_s^2w_1^3w_2w_3^2 - \\
& 108w_4^2w_1^3w_2^2w_3^2 - 36w_4^2v_2^2w_1^3w_2^2w_3^2 + 108w_4c_s^2w_1w_3^2w_3^2 - 36w_4v_2^2w_1^3w_2^2w_3^2 - 36v_1^2w_4^2w_1^3w_2^2w_3^2 - 108v_1^2w_4w_1^3w_2^2w_3^2 + 60w_4^2c_s^2w_1^3w_2^2w_3^2 + 72v_1^2w_4^2w_1^3w_2^2w_3^2 + 144w_4^2w_1^3v_3^2w_2^2w_3^2 - 36w_4^2w_1w_3^2w_3^2 + 108v_3^2w_1^3w_2^2w_3^2 + 324w_4^2c_s^2w_1^3w_2^2w_3^2 - 108w_4^2w_1^3v_3^2w_2w_3^2 + 63w_4^2w_1^3w_2^2w_3^2 - \\
& 72w_4w_1^3w_2^2w_3^2 + 24w_4^2v_2^2w_1^3w_2w_3^2 - 24w_4^2v_2^2w_1w_3^2w_3^2 - 60w_4^2c_s^2w_1^3w_2^2w_3^2 - 48v_1^2w_4^2w_1^3w_2w_3^2 + 12v_1^2w_4^2w_1w_3^2w_3^2 - 360w_4^2c_s^2w_1^3w_2w_3^2 + \\
& 36w_4v_2^2w_1^3w_2^2w_3^2 - 108v_1^2w_1^3w_2^2w_3^2 - 432w_4^2c_s^2w_1^3w_2^2w_3^2 - 20w_4^2w_1^3w_2^2w_3^2 - 144w_4w_1^3w_2^2w_3^2 + 24w_4^2v_2^2w_1w_3^2w_3^2 - 216w_4^2c_s^2w_1^3w_2^2w_3^2 + 72w_4^2v_2^2w_1^3w_2^2w_3^2 - \\
& 48v_1^2w_4^2w_1w_3^2w_3^2 + 72w_4^2v_2^2w_3^2w_3^2 + 63w_4v_2^2w_1^3w_2^2w_3^2 - 144w_4^2c_s^2w_1^3w_2^2w_3^2 + 36v_1^2w_4^2w_1^3w_2^2w_3^2 + 36v_1^2w_4w_1^3w_2^2w_3^2 - 108w_4^2w_1v_3^2w_2^2w_3^2 + \\
& 180w_4^2c_s^2w_1^3w_2^2w_3^2 + 72w_4v_2^2w_1w_3^2w_3^2 + 180v_1^2w_4w_1^3w_2^2w_3^2 + 432w_4^2c_s^2w_1^3w_2^2w_3^2 - 108w_4^2w_1^3w_2^2w_3^2 + 48v_1^2w_4^2w_1^3w_2^2w_3^2 - 120w_4^2c_s^2w_1^3w_2^2w_3^2 + 144w_4w_1^3w_2^2w_3^2 + \\
& 48w_4^2v_2^2w_1^3w_2^2w_3^2 + 24w_4^2w_1w_3^2w_3^2 + 20w_4^2v_2^2w_1^3w_2^2w_3^2 - 432w_4^2c_s^2w_1^3w_2^2w_3^2 + 324w_4^2c_s^2w_1^3w_2^2w_3^2 - 216w_4^2w_1^3v_3^2w_2w_3^2 - 144w_4^2w_3^2w_3^2 + 36v_1^2w_4w_1^3w_2^2w_3^2 - \\
& 36v_1^2w_4^2w_1w_3^2w_3^2 - 144w_4^2c_s^2w_1^3w_2w_3^2 - 36w_4v_2^2w_3^2w_3^2 + 12w_4^2w_1w_3^2w_3^2 + 96w_4^2w_1^3w_2w_3^2 - 63w_4^2v_2^2w_1^3w_2^2w_3^2 + 216w_4^2c_s^2w_1^3w_2^2w_3^2 + 108w_4^2v_2^2w_1w_3^2w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{40} = & -16w_4^2w_1^2v_3^2w_2^2w_3^2 - 96w_4^2v_2^2w_3^2w_3^2 + 128w_4^2c_s^2w_1w_2^2w_3^2 - 72w_4^2v_1^4w_1^2w_2w_3^2 + 432w_4^2c_s^2v_2^2w_1^3w_3^2 - 104w_4^2c_s^2w_1^3w_3^2 - 56w_4^2c_s^2w_1v_3^2w_2^2w_3^2 - \\
& 168w_4^2c_s^4w_1^3w_2w_3^2 + 16w_4^2w_1^2w_3^2w_3^2 - 27w_4^2c_s^2w_1^3w_2^2w_3^2 - 432w_4^2c_s^2v_2^2w_1w_2^2w_3^2 - 162c_s^4w_1^3w_2^2w_3^2 - 30w_4^2c_s^4w_1^3w_2^2w_3^2 - 24w_4^2v_2^2w_1^3v_3^2w_2w$$

$$\begin{aligned}
& 42\omega_1^2\omega_1^3\omega_2^3\omega_3^2 - 9v_1^2\omega_4c_2^2\omega_1^3\omega_3^2\omega_3 + 54\omega_4^2c_4^4\omega_1^3\omega_3^2 - 16\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 - 36\omega_4\omega_3^3v_3^4\omega_2\omega_3^2 - 28v_1^2\omega_1^2c_s^2\omega_1\omega_2^2\omega_3^2 + 138\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - 4v_1^2\omega_4\omega_1^3\omega_3^2 + \\
& 20\omega_1^2c_s^2\omega_3^3\omega_3^2 + 60v_1^2\omega_1^2\omega_2^2v_1^2\omega_2^2\omega_3^2 + 78\omega_4^2c_s^2\omega_1\omega_2^2\omega_3^2 - 4\omega_4^2\omega_1\omega_2^2\omega_3^2 + 36v_1^2\omega_1^2v_3^3\omega_3^2 + 24\omega_4^2c_s^2\omega_1^2\omega_3^2 + 36\omega_4\omega_1v_3^4\omega_2^2\omega_3^2 - 27\omega_1^2c_s^4\omega_3^3\omega_3 - \\
& 36\omega_1^2c_s^2\omega_1^2\omega_3^2\omega_3 + 12\omega_4^2\omega_1^2v_3^3\omega_2\omega_3^2 + 4\omega_1^2\omega_1^3\omega_3^2 - 138\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 4v_1^2\omega_4^2\omega_1\omega_2^2\omega_3^2 + 4\omega_4^2c_s^2\omega_1^3\omega_2\omega_3 + 24v_1^2\omega_1^2\omega_1^3v_3^2\omega_3^2 + 18v_1^2\omega_4^2c_s^2\omega_3^3\omega_3^2 - \\
& 36\omega_4^2c_s^4\omega_1^3\omega_2^2 + 3v_1^2\omega_4^2c_s^2\omega_1^3\omega_2^2\omega_3^2 - 4\omega_4^2\omega_1^2\omega_2\omega_3^2 - 60\omega_4^2v_3^4\omega_2^2\omega_3^2 + 35\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 18v_1^2c_s^2\omega_1^3\omega_2^2\omega_3^2 - 28v_1^2\omega_4^2c_s^2\omega_1\omega_2^2\omega_3 - 4v_1^2\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{47} = & 56\omega_4c_s^4\omega_1^2\omega_2^2\omega_3 + 12v_1^2\omega_4\omega_1^2\omega_2\omega_3^2 - 36v_1^2\omega_4\omega_1^2v_3^2\omega_2\omega_3^2 + 6\omega_4\omega_1^2v_3^4\omega_2^2\omega_3 - 126v_1^2\omega_4c_s^2\omega_1^2\omega_3^2\omega_3 - 68\omega_4c_s^4\omega_3^2\omega_3^2 + 24v_1^2\omega_4c_s^2\omega_1^2\omega_2\omega_3 + 54c_s^2\omega_1v_3^2\omega_3^2\omega_3^2 - \\
& 48\omega_4\omega_1^3v_3^2\omega_3^2 + 9\omega_4\omega_1^3v_3^4\omega_2^2\omega_3^2 + 36\omega_4\omega_1^2v_3^3\omega_2^2\omega_3 + 18c_s^4\omega_1^3\omega_3^2\omega_3^2 - 18\omega_4\omega_1^3v_3^4\omega_2^2\omega_3^2 + 150\omega_4c_s^2\omega_1v_3^2\omega_3^2\omega_3^2 - 4\omega_4\omega_1\omega_2^2\omega_3^2 - 8\omega_4c_s^2\omega_1\omega_2^2\omega_3 - 12v_1^2\omega_4\omega_1^3\omega_3^2 + \\
& 32\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 - 18\omega_4\omega_1^2v_3^2\omega_2^2\omega_3^2 - 36\omega_4c_s^2\omega_1^3v_3^2\omega_2\omega_3 - 14\omega_4c_s^4\omega_1^2\omega_2\omega_3^2 - 90v_1^2\omega_4\omega_1^2v_3^2\omega_2^2\omega_3^2 + 72c_s^2\omega_1^2\omega_2^2\omega_3^2 - 96v_1^2\omega_4c_s^2\omega_2^2\omega_3^2 - 14\omega_4c_s^4\omega_1^2\omega_2^2\omega_3^2 + \\
& 12v_1^2\omega_4\omega_1\omega_2^2\omega_3^2 + 12\omega_4v_3^3\omega_2^2\omega_3^2 + 4\omega_4\omega_1^3\omega_3^2 - 9\omega_4\omega_1^2v_3^4\omega_2^2\omega_3^2 - 36\omega_4\omega_1^2v_3^2\omega_2^2\omega_3 + 66v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 - 42\omega_4\omega_1^2v_3^3\omega_2^2\omega_3^2 + 18\omega_1v_3^4\omega_2^2\omega_3^2 + \\
& 32\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 + 36\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 12\omega_4c_s^2\omega_1^2v_3^2\omega_2\omega_3^2 - 12\omega_4c_s^2\omega_1v_3^2\omega_2^2\omega_3^2 - 4\omega_4\omega_1\omega_2^2\omega_3^2 + 108v_1^2\omega_4v_3^2\omega_2^2\omega_3^2 - 6\omega_4\omega_1^2v_3^2\omega_2^2\omega_3 + v_1^4\omega_4\omega_1^3\omega_2^2\omega_3^2 + \\
& 28\omega_4c_s^2\omega_2^2\omega_3^2 - 2\omega_4c_s^2\omega_1^3\omega_2^2\omega_3^2 - 216v_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 8\omega_4c_s^4\omega_1^3\omega_2\omega_3 - v_1^4\omega_4\omega_1^3\omega_2^2\omega_3^2 - 174\omega_4c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 + 54\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 36\omega_4c_s^4\omega_1^2\omega_2^2\omega_3^2 + \\
& 132v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 9\omega_4\omega_1^2v_3^2\omega_2^2\omega_3^2 - 36\omega_4\omega_1^2v_3^4\omega_2^2\omega_3 - 108\omega_4c_s^2v_3^2\omega_2^2\omega_3^2 + 72c_s^4\omega_1\omega_2^2\omega_3^2 - 18\omega_4c_s^2\omega_1^3\omega_2^2\omega_3^2 - 18\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3 + 4\omega_4\omega_2^2\omega_2\omega_3^2 + \\
& 9\omega_4\omega_1^2v_3^3\omega_2^2\omega_3^2 + 36\omega_4\omega_1^2v_3^4\omega_2^2\omega_3^2 - 90v_1^2\omega_4\omega_1^2v_3^2\omega_2\omega_3^2 + 132\omega_4c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - 48\omega_4v_3^4\omega_2^2\omega_3^2 - 18\omega_4c_s^2\omega_1\omega_2^2\omega_3^2 + 12v_1^2\omega_4\omega_1\omega_2^2\omega_3^2 + 28\omega_4c_s^4\omega_1^2\omega_2^2\omega_3^2 + \\
& 72v_1^2\omega_4\omega_1^3v_3^2\omega_2^2\omega_3^2 - 6v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 - 18\omega_1v_3^3\omega_2^2\omega_3^2 - 18\omega_4\omega_1^2v_3^4\omega_2^2\omega_3^2 - 144v_1^2\omega_4\omega_1v_3^2\omega_2^2\omega_3^2 - 6v_1^2\omega_4c_s^2\omega_3^3\omega_2\omega_3^2 - 6\omega_4\omega_1v_3^3\omega_2^2\omega_3 + 18\omega_4\omega_1^2v_3^4\omega_2^2 - \\
& 30\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 216v_1^2c_s^2\omega_1\omega_2^2\omega_3^2 - 56\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 + 8\omega_4\omega_1^2\omega_2^2\omega_3^2 - 12\omega_4\omega_1^2v_3^3\omega_2\omega_3 - 54c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 20\omega_4c_s^2\omega_1^3\omega_3^2 - 18c_s^2\omega_1^3\omega_2^2\omega_3^2 + \\
& 12\omega_4\omega_1^2v_3^3\omega_2\omega_3^2 - 28\omega_4c_s^4\omega_1^2\omega_2\omega_3^2 + 8\omega_4c_s^4\omega_1\omega_2^2\omega_3 + 6v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 - 3\omega_4c_s^4\omega_1^2\omega_2^2\omega_3^2 + 18\omega_1^2v_3^4\omega_2^2\omega_3^2 + 18\omega_1^2v_3^2\omega_2^2\omega_3^2 + 2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 + \\
& 18\omega_4c_s^2\omega_1^3\omega_2\omega_3^2 - 18\omega_1^2v_3^3\omega_2^2\omega_3^2 + 18\omega_1^2v_3^2\omega_2^2\omega_3 + 36\omega_4\omega_1v_3^2\omega_2^2\omega_3^2 + 54\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - v_1^4\omega_4\omega_1^3\omega_2^2\omega_3^2 - 72c_s^4\omega_1^2\omega_2^2\omega_3^2 + 54v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 + \\
& 30\omega_4c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - 36\omega_4c_s^4\omega_1^3\omega_2^2\omega_3 + 18\omega_1^2v_3^2\omega_2^2\omega_3^2 + 12v_1^2\omega_4\omega_1^3\omega_2\omega_3^2 + 54\omega_4\omega_1v_3^4\omega_2^2\omega_3^2 + 48v_1^2\omega_4c_s^2\omega_1\omega_2^2\omega_3^2 + 54c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 + 24\omega_4\omega_1^2v_3^3\omega_2^2\omega_3^2 + \\
& 66\omega_4\omega_1^2v_3^2\omega_2^2\omega_3^2 + 18\omega_4\omega_1^2v_3^3\omega_2^2\omega_3 + v_1^4\omega_4\omega_1^3\omega_2^2\omega_3^2 - 28\omega_4c_s^4\omega_1\omega_2^2\omega_3^2 - 12v_1^2\omega_4\omega_2^2\omega_3^2 + 6\omega_4\omega_1v_3^4\omega_2^2\omega_3 + 2\omega_4c_s^2\omega_1^3\omega_2^2\omega_3^2 + 90\omega_4c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 + \\
& 12\omega_4\omega_1^3v_3^2\omega_2\omega_3^2 - 48v_1^2\omega_4c_s^2\omega_1^2\omega_2\omega_3^2 - 54c_s^2\omega_1^3v_3^2\omega_2^2\omega_3 + 60v_1^2\omega_4c_s^2\omega_1\omega_2^2\omega_3^2 - 54\omega_4c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 + 36\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 + 16\omega_4c_s^4\omega_1^3\omega_3^2 - 54c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + \\
& 24\omega_4c_s^2\omega_1^3\omega_2^2\omega_3^2 - 8\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 18\omega_1^2v_3^2\omega_2^2\omega_3^2 + 18\omega_1^2v_3^2\omega_2^2\omega_3 + 18\omega_1^2v_3^2\omega_2^2\omega_3 - 84v_1^2\omega_4c_s^2\omega_1\omega_2^2\omega_3^2 - 76\omega_4c_s^4\omega_1\omega_2^2\omega_3^2 - 24v_1^2\omega_4\omega_1^3\omega_2^2\omega_3^2 + \\
& 180v_1^2\omega_4\omega_1^2v_3^2\omega_2^2\omega_3^2 - 72c_s^2\omega_1\omega_2^2\omega_3^2 - 90v_1^2\omega_4c_s^2\omega_1^2\omega_2\omega_3^2 + 12\omega_4\omega_1v_3^4\omega_2^2\omega_3^2 + 18\omega_1^2v_3^3\omega_2^2\omega_3^2 - 18\omega_1^2v_3^4\omega_2^2\omega_3 + 18\omega_4c_s^4\omega_1^3\omega_2^2\omega_3 - 90\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - \\
& 24\omega_4\omega_1v_3^2\omega_2^2\omega_3^2 - 18\omega_1^2v_3^3\omega_2^2\omega_3^2 + 4\omega_4\omega_2^2\omega_3^2 + 54v_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 36\omega_4c_s^2\omega_1^2\omega_2^2\omega_3^2 + 12v_1^2\omega_4c_s^2\omega_1^3\omega_2^2\omega_3^2 + 54c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 36\omega_4\omega_1v_3^3\omega_2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{48} = & -18c_s^2\omega_1^3\omega_2 + 141\omega_1v_3^2\omega_2^2\omega_3 - 23\omega_1^2\omega_2^2\omega_3 - 114v_3^2\omega_2^2\omega_3 - 9v_1^2\omega_1\omega_2^2\omega_3 + 6\omega_1^2v_3^2\omega_2\omega_3 + 48\omega_1^3v_3^2\omega_3 + 36c_s^2\omega_1^2\omega_2^2\omega_3 - 60\omega_1\omega_2^2\omega_3 + 6\omega_1\omega_2^2 + \\
& 12v_1^2\omega_3^2\omega_3 - 6v_1^2\omega_3^2\omega_2 - 12v_1^2\omega_1\omega_2^2\omega_3 - 75\omega_1^3v_3^2\omega_2\omega_3 - 42c_s^2\omega_1^2\omega_2^2\omega_3 + 6\omega_1^2\omega_2\omega_3 + 60\omega_1v_3^2\omega_2^2\omega_3 - 108c_s^2\omega_1^3\omega_2\omega_3 + 12v_1^2\omega_1^2\omega_2^2\omega_3 - 12v_1^2\omega_1^2\omega_2\omega_3 - \\
& 12\omega_1\omega_2^2\omega_3 - 36\omega_1^3\omega_3 - 66c_s^2\omega_2^2\omega_3 + 18v_1^2\omega_1^2\omega_2^2\omega_3 + 108c_s^2\omega_1\omega_2^2\omega_3 - 50\omega_1^2v_3^2\omega_2^2\omega_3 + 84c_s^2\omega_1^3\omega_3 - 6v_1^2\omega_1\omega_2^2 + 42\omega_3^2\omega_3 + 50\omega_1^3v_3^2\omega_2^2\omega_3 + \\
& 42c_s^2\omega_1^2\omega_2^2\omega_3 + 12\omega_1^2\omega_2^2\omega_3 - 66\omega_1^2v_3^2\omega_2^2\omega_3 - 9v_1^2\omega_1^2\omega_2\omega_3 + 6\omega_1^2\omega_2 - 18c_s^2\omega_1\omega_2^2 + 12v_1^2\omega_1^2\omega_3 + 23\omega_1^2\omega_2^2\omega_3 - 18c_s^2\omega_1^2\omega_2\omega_3 + 48\omega_1^2\omega_2\omega_3 - 12\omega_1^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{49} = & -192\omega_1^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 8\omega_1^2v_3^2\omega_2^2\omega_3^2 + 128\omega_1^2c_s^2\omega_1\omega_2^2\omega_3^2 + 32\omega_4^2c_s^2v_3^2\omega_1^2\omega_3^2 - 104\omega_4^2c_s^2\omega_3^3\omega_3^2 - 168\omega_1^2c_s^4\omega_1^2\omega_2\omega_3^2 + 16\omega_1^2\omega_1^2\omega_2^2\omega_3^2 - \\
& 27\omega_4c_s^2\omega_1^3\omega_3^2\omega_3^2 - 56\omega_4^2c_s^2v_3^2\omega_1\omega_2^2\omega_3^2 - 162c_s^4\omega_3^3\omega_2^2\omega_3^2 - 30\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 - 24\omega_1^2v_3^2\omega_1^2v_3^2\omega_2\omega_3^2 + 48\omega_4\omega_1^3v_3^4\omega_2^2\omega_3^2 - 108c_s^2\omega_1^2\omega_3^2\omega_3^2 - \\
& 432\omega_1^2c_s^2\omega_1v_3^2\omega_2^2\omega_3^2 - 324\omega_4c_s^4\omega_1^2\omega_2^2\omega_3^2 + 80\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 56\omega_1^2c_s^2\omega_1\omega_2^2\omega_3^2 - 56\omega_1^2c_s^2v_3^2\omega_1\omega_2^2\omega_3 + 192\omega_1^2c_s^4\omega_1^2\omega_2^2\omega_3 - 8\omega_1^2c_s^2v_3^2\omega_1^2\omega_2\omega_3^2 - \\
& 432\omega_4^2c_s^2\omega_1^3v_3^2\omega_2\omega_3^2 + 8\omega_4^2v_3^2\omega_1^2\omega_2\omega_3^2 + 8\omega_4^2\omega_2^2\omega_3^2 - 60\omega_4^2v_3^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 192\omega_1^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 8\omega_4^2c_s^2v_3^2\omega_1\omega_2^2\omega_3^2 - 8\omega_4^2\omega_1^2\omega_2\omega_3^2 + 72\omega_4^2\omega_1^2v_3^4\omega_2^2\omega_3^2 - \\
& 27\omega_1^2c_s^2\omega_2^2\omega_1^2\omega_2^2\omega_3 + 144\omega_1^2c_s^4\omega_1^3\omega_3^2 - 54c_s^2v_3^2\omega_1^3\omega_2^2\omega_3^2 + 27\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 432\omega_1^2c_s^2\omega_1^2v_3^2\omega_2\omega_3^2 + 27\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 64\omega_1^2c_s^2\omega_1\omega_2^2\omega_3^2 + \\
& 432\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 + 10\omega_4^2c_s^2v_3^2\omega_1^3\omega_2^2\omega_3^2 - 24\omega_4^2c_s^4\omega_1^3\omega_2\omega_3^2 - 96\omega_1^2v_3^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 324\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 - 16\omega_4^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 432\omega_4^2c_s^2v_3^2\omega_1^3\omega_2^2\omega_3^2 - \\
& 60\omega_1^2v_3^2\omega_1^2v_3^2\omega_2\omega_3^2 - 10\omega_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 432\omega_4^2c_s^2\omega_1v_3^2\omega_2^2\omega_3^2 - 96\omega_4^2v_3^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 8\omega_4^2\omega_1^2\omega_2^2\omega_3^2 - 40\omega_1^2c_s^2v_3^2\omega_1^2\omega_2\omega_3^2 - 36\omega_4^2\omega_1v_3^4\omega_2^2\omega_3^2 - \\
& 54\omega_1^2c_s^2\omega_1^3\omega_3^2 + 96\omega_4\omega_1^3v_3^2\omega_2\omega_3^2 + 54\omega_1^2c_s^2v_3^2\omega_1^3\omega_2^2\omega_3^2 + 8\omega_4^2v_3^2\omega_1^2\omega_2\omega_3^2 - 216\omega_4^2c_s^4\omega_1\omega_2^2\omega_3^2 - 10\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 10\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 144\omega_4^2c_s^4\omega_3^3\omega_3^2 + \\
& 54c_s^2\omega_1^3\omega_2^2\omega_3^2 - 252\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 112\omega_4^2c_s^2\omega_1^3\omega_2\omega_3^2 + 96\omega_4^2\omega_1v_3^2\omega_2^2\omega_3^2 + 81\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 - 72\omega_4^2\omega_1^2v_3^4\omega_2\omega_3^2 + 108\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 24\omega_1^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 - \\
& 168\omega_4^2c_s^4\omega_1\omega_2^2\omega_3^2 + 8\omega_4^2v_3^2\omega_1\omega_2^2\omega_3^2 - 72\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 + 64\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 24\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 324c_s^2\omega_1^2\omega_2^2\omega_3^2 - 96\omega_1^2v_3^2\omega_1^3\omega_2^2\omega_3^2 - 64\omega_1^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + \\
& 864\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 162\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 - 176\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 - 36\omega_4^2\omega_1^2v_3^4\omega_2\omega_3^2 + 72\omega_4^2v_3^2\omega_1^2\omega_2^2\omega_3^2 - 84\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 - \\
& 104\omega_4^2c_s^2\omega_2^2\omega_3^2 + 32\omega_4^2c_s^2v_3^2\omega_1^2\omega_2\omega_3^2 - 24\omega_4^2c_s^4\omega_1\omega_2^2\omega_3^2 - 8\omega_1^2v_3^2\omega_1^2\omega_2^2\omega_3^2 - 8\omega_4^2\omega_1\omega_2^2\omega_3^2 + 32\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 84\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 81\omega_4^2c_s^4\omega_3^3\omega_3^2 - \\
& 108\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 96\omega_4^2\omega_1^2v_3^2\omega_2\omega_3^2 + 108c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 8\omega_4^2\omega_1^3\omega_3^2 + 8\omega_4^2c_s^2\omega_1^3\omega_2\omega_3^2 - 108\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 - 72\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 - 8\omega_4^2\omega_1^2\omega_2\omega_3^2 - \\
& 8\omega_4^2c_s^2v_3^2\omega_1^2\omega_2\omega_3^2 + 24\omega_4^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 30\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 108\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^2\omega_3^2 + 8\omega_4^2v_3^2\omega_1\omega_2^2\omega_3^2 + 120\omega_4^2v_3^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 48\omega_4^2v_3^2\omega_1^2v_3^2\omega_2^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{50} = & 27c_s^2\omega_1\omega_2\omega_3 - 9\omega_4v_3^2\omega_1\omega_2 + 2\omega_4\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 2\omega_4v_3^2\omega_2\omega_3 + 6\omega_4c_s^2\omega_1\omega_3 - 6\omega_4c_s^2\omega_2\omega_3 + 9v_3^2\omega_1\omega_2\omega_3 + 2\omega_4v_3^2\omega_1\omega_3 - 9\omega_1\omega_2\omega_3 - \\
& 2\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{51} = & 48\omega_1^2\omega_1^3v_3^4\omega_5\omega_3^2 + 132\omega_1^2\omega_1^3v_3^2\omega_5\omega_2\omega_3^2 + 648\omega_4c_s^2v_3^2\omega_1^2\omega_5\omega_3^2\omega_3^2 + 144\omega_4\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 72\omega_4^2c_s^2\omega_1^3v_3^2\omega_5\omega_2\omega_3 + 72\omega_4^2\omega_1v_3^2\omega_5\omega_2^2\omega_3^2 - \\
& 216\omega_4^2c_s^2v_3^2\omega_5\omega_2^2\omega_3^2 - 108\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 36\omega_4\omega_1^3v_3^4\omega_5\omega_2^2\omega_3^2 - 168\omega_1^2c_s^2v_3^2\omega_1\omega_5\omega_2^2\omega_3^2 + 108\omega_4c_s^2\omega_1^3v_3^2\omega_5\omega_2^2\omega_3^2 + 288\omega_4c_s^2\omega_1\omega_5\omega_2^2\omega_3^2 + \\
& 24\omega_1^2v_3^2\omega_1^2\omega_5\omega_2\omega_3^2 + 160\omega_4^2c_s^4\omega_1\omega_5\omega_2^2\omega_3 - 36\omega_4^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3 - 162c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3 + 16\omega_4^2\omega_1^2\omega_5\omega_2^2\omega_3^2 - 288\omega_4c_s^4\omega_1\omega_5\omega_2^2\omega_3^2 - \\
& 160\omega_4^2c_s^2\omega_1\omega_5\omega_2^2\omega_3 - 216\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3 + 288\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 72\omega_4^2\omega_1^3v_3^2\omega_5\omega_2^2\omega_3 - 60\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 12\omega_1^2c_s^2v_3^2\omega_1^2\omega_5\omega_2\omega_3^2 - \\
& 72\omega_1^2v_3^2\omega_1^2v_3^2\omega_5\omega_2\omega_3^2 + 36\omega_4^2c_s^2\omega_1^2\omega_5\omega_2\omega_3^2 - 12\omega_1^2\omega_1v_3^2\omega_5\omega_2^2\omega_3 + 336\omega_1^2c_s^2v_3^2\omega_1\omega_5\omega_2^2\omega_3 - 108\omega_4c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3 - 56\omega_1^2c_s^2\omega_1\omega_5\omega_2^2\omega_3^2 + \\
& 24\omega_1^2v_3^2\omega_1\omega_5\omega_2^2\omega_3^2 + 300\omega_4^2c_s^2\omega_1v_3^2\omega_5\omega_2^2\omega_3^2 + 64\omega_4^2c_s^2\omega_1\omega_5\omega_2^2\omega_3 - 36\omega_4\omega_1v_3^2\omega_5\omega_2^2\omega_3^2 - 28\omega_4^2c_s^4\omega_1^2\omega_5\omega_2\omega_3^2 + 108\omega_1^2c_s^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3 - \\
& 84\omega_1^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 96\omega_1^2v_3^4\omega_5\omega_2^2\omega_3^2 - 54\omega_1^2\omega_1^3v_3^4\omega_5\omega_2^2\omega_3 - 27v_1^2\omega_1^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3 + 48\omega_1^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 16\omega_4^2c_s^4\omega_1^2\omega_5\omega_2\omega_3^2 - 96\omega_1^2\omega_1^3v_3^2\omega_5\omega_2^2\omega_3^2 - \\
& 12\omega_1^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3 + 24\omega_4^2c_s^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3 + 216\omega_4^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 64\omega_1^2c_s^2\omega_1^2\omega_5\omega_2\omega_3^2 - 16\omega_4^2c_s^2\omega_1^3\omega_5\omega_2\omega_3^2 - 48\omega_4^2\omega_1v_3^2\omega_5\omega_2^2\omega_3^2 + 24\omega_4^2\omega_1^2v_3^4\omega_5\omega_2\omega_3^2 - \\
& 40\omega_1^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3 + 27v_1^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 108\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 120\omega_4^2c_s^2v_3^2\omega_1\omega_5\omega_2^2\omega_3^2 + 54\omega_4\omega_1^3v_3^4\omega_5\omega_2^2\omega_3^2 - 56\omega_4^2c_s^4\omega_1^2\omega_5\omega_2\omega_3^2 - \\
& 108\omega_4^2c_s^2\omega_1^3v_3^2\omega_5\omega_2^2\omega_3 - 54\omega_1^3v_3^4\omega_5\omega_2^2\omega_3^2 - 6v_1^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 36\omega_4\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 180\omega_1^2c_s^2\omega_1v_3^2\omega_5\omega_2^2\omega_3 + 18\omega_1^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + \\
& 24\omega_1^2v_3^2\omega_1^2\omega_5\omega_2\omega_3^2 + 240\omega_4^$$

$$\begin{aligned}
& 8\omega_4^2\omega_5\omega_3^2\omega_2^2 + 108\omega_4c_s^2\omega_1^2v_3^2\omega_5\omega_3^2\omega_2^2 - 9v_1^4\omega_2^2\omega_1^3\omega_5\omega_3^2\omega_2^2 - 72\omega_4c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 12\omega_4^2\omega_1v_3^4\omega_5\omega_3^2\omega_2^2 - 72\omega_4c_s^4\omega_1^3\omega_3^2\omega_2^2 - 2v_1^2\omega_4^2\omega_1^3\omega_5\omega_2^2\omega_3^2 - \\
& 180\omega_4^2v_3^2\omega_1v_3^2\omega_5\omega_3^2\omega_2^2 - 36\omega_4^2v_3^2\omega_1^3\omega_5\omega_2^2\omega_3^2 + 24\omega_4^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 - 108\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_3^2\omega_2^2 + 72\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 72\omega_4^2c_s^2\omega_1^2\omega_5\omega_3^2\omega_2^2 + \\
& 144\omega_4^2v_3^2\omega_1^3\omega_3^2\omega_5\omega_2^2\omega_3^2 - 468\omega_4^2c_s^2\omega_1^2\omega_1^3\omega_5\omega_2^2\omega_3^2 + 36\omega_4\omega_1v_3^4\omega_5\omega_2^2\omega_3^2 + 56\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2\omega_3^2 + 12\omega_4^2\omega_1^2v_3^4\omega_5\omega_2^2\omega_3^2 - 9v_1^2\omega_4\omega_1^3\omega_5\omega_2^2\omega_3^2 - \\
& 4\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 360\omega_4^2v_3^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 54\omega_4^2\omega_1^3v_3^2\omega_5\omega_2^2\omega_3^2 + 54\omega_4^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 324c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 112\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2\omega_3^2 - \\
& 6\omega_4^2c_s^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 54\omega_4^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 162\omega_4^2c_s^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 4\omega_4^2c_s^4\omega_1^3\omega_5\omega_2^2\omega_3^2 - 8\omega_4^2\omega_1\omega_5\omega_2^2\omega_3^2 - 216\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - \\
& 288\omega_4^2c_s^2\omega_1^2\omega_1^2\omega_2^2\omega_3^2 - 36\omega_4\omega_1^2v_3^4\omega_5\omega_2^2\omega_3^2 - 24\omega_4^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 - 112\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 108\omega_4^2\omega_1v_3^4\omega_5\omega_2^2\omega_3^2 - 54\omega_4\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 32\omega_4^2c_s^4\omega_1^3\omega_5\omega_2^2\omega_3^2 - \\
& 72\omega_4^2\omega_1^2v_3^4\omega_5\omega_2^2\omega_3^2 - 18\omega_4^2\omega_1^3v_3^2\omega_5\omega_2^2\omega_3^2 + 36\omega_4^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 28\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2\omega_3^2 + 264\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 108\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - \\
& 18\omega_4^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 48\omega_4^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 9v_1^4\omega_4\omega_1^3\omega_5\omega_2^2\omega_3^2 - 72\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 180\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 72\omega_4^2c_s^4\omega_1^3\omega_5\omega_2^2\omega_3^2 - \\
& 8\omega_4^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 152\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2\omega_3^2 + 4\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + 36\omega_4\omega_1^3v_3^2\omega_5\omega_2^2\omega_3^2 - 24\omega_4^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 - 288\omega_4^2v_3^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 6\omega_4^2c_s^2v_3^2\omega_1^2\omega_5\omega_2^2\omega_3^2 + \\
& 264\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 - 180\omega_4^2v_3^2\omega_1^2v_3^2\omega_5\omega_2^2\omega_3^2 + 72\omega_4^2c_s^4\omega_1^3\omega_5\omega_2^2\omega_3^2 + 72\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2\omega_3^2 - 24\omega_4^2\omega_1^3v_3^4\omega_5\omega_2^2\omega_3^2 + 36\omega_4\omega_1^2v_3^4\omega_5\omega_2^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{52} = & -6c_s^2\omega_1^3\omega_2 - 13\omega_1v_3^2\omega_3^2\omega_2 + 48c_s^2\omega_1^2\omega_2^2\omega_3 + 10v_3^2\omega_2^2\omega_3 - 22\omega_1^2v_3^2\omega_2\omega_3 + 16\omega_1^3v_3^2\omega_3 + 12c_s^2\omega_1^2\omega_2^2 + 10\omega_1\omega_2^2\omega_3 - 2v_2^2\omega_1\omega_3^2 + 2\omega_1\omega_2^3 - \\
& 3v_3^2\omega_1\omega_3^2\omega_3 - 4v_2^2\omega_1^2\omega_2\omega_3 - 13\omega_1^2v_3^2\omega_2\omega_3 + 14\omega_1^2\omega_2\omega_3 - 4\omega_1v_3^2\omega_2^2\omega_3 - 24c_s^2\omega_1^2\omega_2\omega_3 - 4v_3^2\omega_1\omega_2^2\omega_3 + 8\omega_1\omega_2^2\omega_3 + 4v_3^2\omega_1^3\omega_3 - 12\omega_1^3\omega_3 + \\
& 26c_s^2\omega_2\omega_3 - 24c_s^2\omega_1\omega_2^2\omega_3 + 28c_s^2\omega_1^2\omega_3 - 10\omega_2^2\omega_3 + 4v_2^2\omega_1^2\omega_3 - 20\omega_1^2\omega_2^2\omega_3 - 24c_s^2\omega_1\omega_2^2\omega_3 + 26\omega_1^2v_3^2\omega_2^2\omega_3 - 2v_2^2\omega_1^2\omega_2 + 2\omega_1^3\omega_2 - \\
& 6c_s^2\omega_1\omega_2^2 - 30c_s^2\omega_1^2\omega_2\omega_3 + 10\omega_1^3\omega_2\omega_3 - 4\omega_1^2\omega_2^2 + 4v_2^2\omega_1^2\omega_2^2 - 3v_2^2\omega_1^3\omega_2\omega_3
\end{aligned}$$

$$\begin{aligned}
C_{53} = & -3\omega_4^2v_3^4\omega_1^3\omega_5\omega_3 + 32\omega_4^2c_s^4\omega_1^2\omega_3^2 + 6\omega_4\omega_1^2v_3^2\omega_5\omega_3^2 - 8\omega_4^2c_s^4\omega_1^2\omega_5\omega_3 + 8\omega_4c_s^2\omega_1\omega_5\omega_3^2 + 6\omega_4^2\omega_1^2v_3^4\omega_5\omega_3 - 6\omega_4^2\omega_1^2v_3^4\omega_5 - 9c_s^2v_2^2\omega_1^3\omega_5\omega_3^2 - 2\omega_4^2c_s^2\omega_1^3\omega_5\omega_3 + \\
& 3\omega_4^2v_3^4\omega_1^3\omega_5 + 6\omega_4c_s^2v_2^2\omega_1^3\omega_5\omega_3^2 + 3\omega_4\omega_1^3v_3^2\omega_5\omega_3^2 - 6\omega_4^2v_3^2\omega_1^3\omega_5\omega_3 + 6\omega_4^2v_3^2\omega_1^2\omega_5 + 3\omega_4^2\omega_1^2v_3^2\omega_5\omega_3 - 3\omega_4^2\omega_1^2v_3^2\omega_5 - 6\omega_4^2c_s^2v_2^2\omega_1^3\omega_5\omega_3 + 3v_2^2\omega_1^3\omega_5\omega_3^2 + \\
& 12\omega_4^2c_s^2v_2^2\omega_1\omega_5\omega_3 - 8\omega_4^2c_s^4\omega_1^3\omega_3^2 + 3\omega_4^2v_3^2\omega_1^3\omega_5\omega_3^2 - 12\omega_4^2c_s^2v_2^2\omega_1\omega_5\omega_3^2 - 6\omega_4^2\omega_1^2v_3^2\omega_5\omega_3 + 8\omega_4c_s^4\omega_1^2\omega_5\omega_3^2 - 6\omega_4\omega_1^2v_3^4\omega_5\omega_3^2 - 8\omega_4^2c_s^2\omega_1\omega_5\omega_3 - \\
& 18\omega_4^2c_s^2\omega_1^2\omega_5\omega_3 + 2\omega_4c_s^2\omega_1^2\omega_5\omega_3^2 - 12\omega_4c_s^2\omega_1v_3^2\omega_5\omega_3^2 - 3\omega_4^2v_3^2\omega_1^2\omega_5 + 6\omega_4v_3^2\omega_1^2\omega_5\omega_3^2 - 3\omega_4^2\omega_1^2v_3^2\omega_5\omega_3 - 6\omega_4^2v_3^2\omega_1^2\omega_5 - 3\omega_4\omega_1^2v_3^2\omega_5\omega_3^2 + 6v_2^2\omega_1^2\omega_5\omega_3^2 + \\
& 12\omega_4^2c_s^2\omega_1v_3^2\omega_5\omega_3 + 6\omega_4^2\omega_1^2v_3^2\omega_5 + 3\omega_4^2v_2^2\omega_1^3\omega_5\omega_3 - 6\omega_4^2c_s^2\omega_1^3v_3^2\omega_5\omega_3 + 6\omega_4^2c_s^2v_2^2\omega_1^2\omega_5\omega_3 - 9c_s^2\omega_1^3v_3^2\omega_5\omega_3^2 + 8\omega_4^2c_s^2\omega_1^2\omega_5\omega_3 + 3\omega_4^2\omega_1^3v_3^4\omega_5 + \\
& 18c_s^2v_2^2\omega_1^2\omega_5\omega_3^2 - 8\omega_4c_s^4\omega_1\omega_5\omega_3^2 - 6\omega_4c_s^2v_2^2\omega_1^2\omega_5\omega_3^2 + 6\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_3^2 - 6\omega_4^2v_3^2\omega_1^2\omega_5\omega_3^2 - 8\omega_4^2c_s^4\omega_1\omega_5\omega_3^2 + 2\omega_4^2c_s^4\omega_1^2\omega_5\omega_3 + 9\omega_4^2c_s^2v_2^2\omega_1^2\omega_5 - \\
& 3\omega_1^3v_3^4\omega_5\omega_3^2 + 6\omega_4^2v_3^4\omega_1^2\omega_5\omega_3 - 3\omega_4v_3^2\omega_1^3\omega_5\omega_3^2 - 3v_3^4\omega_1^3\omega_5\omega_3^2 - 8\omega_4c_s^2\omega_1^2\omega_5\omega_3^2 + 8\omega_4^2c_s^4\omega_1\omega_5\omega_3 + 6\omega_4^2v_3^4\omega_1\omega_5\omega_3^2 + 16\omega_4^2c_s^4\omega_1\omega_5\omega_3^2 + 6\omega_4^2c_s^2\omega_1^2v_3^2\omega_5\omega_3 + \\
& 9\omega_4^2c_s^2\omega_1^2v_3^2\omega_5 - 18\omega_4^2c_s^2v_2^2\omega_1^2\omega_5 - 2\omega_4c_s^4\omega_1^2\omega_5\omega_3^2 - 32\omega_4^2c_s^4\omega_1\omega_3^2 - 6\omega_4c_s^2\omega_1^2v_3^2\omega_5\omega_3^2 + 3\omega_1^3v_3^4\omega_5\omega_3^2 - 6v_2^2\omega_1^2\omega_5\omega_3^2 - 6\omega_4v_3^2\omega_1^2\omega_5\omega_3^2 + 18c_s^2\omega_1^2v_3^2\omega_5\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{54} = & 104\omega_4^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 56\omega_4^2c_s^2\omega_1\omega_2^2\omega_3^2 - 104\omega_4^2c_s^2\omega_1^3\omega_2^2\omega_3^2 - 56\omega_4^2c_s^2\omega_1v_3^2\omega_2^2\omega_3 + 36\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 276\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 - 8\omega_4^2\omega_1^2\omega_2^2\omega_3^2 + \\
& 9\omega_4^2c_s^2\omega_1^3\omega_2^2\omega_3^2 + 54c_s^4\omega_1^2\omega_2^2\omega_3^2 - 342\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 - 78\omega_4^2\omega_1^2v_3^4\omega_2^2\omega_3^2 + 48\omega_4^2\omega_1^3v_3^4\omega_2^2\omega_3^2 + 6v_1^2\omega_4^2\omega_1^2\omega_2^2\omega_3^2 + 36c_s^2\omega_1^2\omega_2^2\omega_3^2 - 56\omega_4^2c_s^2\omega_1^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - \\
& 6\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 108\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 78\omega_4^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - 88\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 56\omega_4^2c_s^2\omega_1\omega_2^2\omega_3^2 + 120\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 - 6v_1^4\omega_4^2\omega_1^2\omega_2^2\omega_3^2 - \\
& 712\omega_4^2c_s^2\omega_1^3v_3^2\omega_2\omega_3^2 - 16\omega_4^2\omega_2^2\omega_3^2 + 12\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 16\omega_4^2c_s^2\omega_1^3v_3^2\omega_2\omega_3^2 - 20\omega_4^2\omega_1^3\omega_2\omega_3^2 - 18v_1^2\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 96\omega_4^2\omega_1^2v_3^4\omega_2^2\omega_3^2 + 144\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 - \\
& 14\omega_4^2\omega_1^2\omega_2^2\omega_3^2 + 9\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 92\omega_4^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 448\omega_4^2c_s^4\omega_1^2v_3^2\omega_2^2\omega_3^2 - 368\omega_4^2c_s^2\omega_1\omega_2^2\omega_3^2 + 320\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 48\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 - 36\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2 + \\
& 216\omega_4^2c_s^4\omega_1^2\omega_3^2\omega_3^2 - 784\omega_4^2c_s^2v_3^2\omega_2^2\omega_3^2 - 92\omega_4^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - 118\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 1232\omega_4^2c_s^2\omega_1v_3^2\omega_2^2\omega_3^2 - 56\omega_4^2\omega_1^3v_3^2\omega_2^2\omega_3^2 + 36\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + \\
& 28\omega_4^2\omega_1\omega_2^2\omega_3^2 - 108\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 228\omega_4^2\omega_1v_3^2\omega_2^2\omega_3^2 - 18\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 152\omega_4^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 6\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 144\omega_4^2c_s^4\omega_1\omega_2^2\omega_3^2 - 36c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + \\
& 184\omega_4^2c_s^2\omega_1^2\omega_3^2\omega_3^2 - 288\omega_4^2c_s^4\omega_2^2\omega_3^2 - 18c_s^2\omega_1^3\omega_2^2\omega_3^2 + 72\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 108\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 208\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2 + 32\omega_4^2\omega_1v_3^2\omega_2^2\omega_3^2 - 27\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 + \\
& 120\omega_4^2\omega_1^2v_3^4\omega_2\omega_3^2 - 36\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 36\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 14\omega_4^2\omega_1^2\omega_2^2\omega_3^2 - 168\omega_4^2c_s^4\omega_1\omega_2^2\omega_3^2 + 72\omega_4^2c_s^4\omega_1^2\omega_2\omega_3^2 + 18v_1^2\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + \\
& 18\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 - 108\omega_4^2\omega_1^2\omega_2^2\omega_3^2 + 160\omega_4^2v_3^2\omega_2^2\omega_3^2 - 40\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 412\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 256\omega_4^2\omega_1v_3^2\omega_2^2\omega_3^2 + 54\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 - 6v_1^2\omega_4^2\omega_1^2\omega_2^2\omega_3^2 + \\
& 52\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 - 132\omega_4^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 40\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 18\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 394\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 208\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 588\omega_4^2c_s^4\omega_1\omega_2^2\omega_3^2 - \\
& 8\omega_4^2\omega_1\omega_2^2\omega_3^2 + 36\omega_4^2c_s^2\omega_2^2\omega_3^2 - 24\omega_4^2\omega_1v_3^4\omega_2^2\omega_3^2 + 6v_1^4\omega_4^2\omega_1^3\omega_2^2\omega_3^2 - 27\omega_4^2c_s^4\omega_1^3\omega_2^2\omega_3^2 - 72\omega_4^2c_s^2\omega_1^2\omega_2^2\omega_3^2 + 18c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2 - 136\omega_4^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + \\
& 8\omega_4^2\omega_1^2\omega_2^2\omega_3^2 - 460\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 - 16\omega_4^2c_s^2\omega_1^2\omega_2\omega_3^2 - 9\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^2\omega_3^2 + 16\omega_4^2\omega_1^2\omega_2\omega_3^2 - 144\omega_4^2v_3^4\omega_2^2\omega_3^2 + 144\omega_4^2c_s^4\omega_1^2\omega_2^2\omega_3^2 - 9\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{55} = & -18v_1^4\omega_4\omega_2\omega_3 + 2\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 + 9\omega_1\omega_2\omega_3 + \\
& 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 - 9\omega_1v_3^2\omega_2\omega_3 + 18v_1^4\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 + 4\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{56} = & 10\omega_4c_s^4\omega_1^2\omega_2^2\omega_3 - 18\omega_4c_s^4\omega_1^2\omega_2^2 + 8\omega_4c_s^4\omega_1^3\omega_2 - 168\omega_4\omega_1^2v_3^4\omega_2^2\omega_3 - 3v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 + 36c_s^4\omega_1\omega_2^2\omega_3 + 81\omega_4\omega_1^2v_3^2\omega_2^2\omega_3 + 8\omega_4\omega_1^2\omega_2\omega_3 - \\
& 54\omega_4c_s^2\omega_1\omega_3^2\omega_3 - 264\omega_4v_3^4\omega_2^2\omega_3 + 144\omega_4c_s^2\omega_1^3v_3^2\omega_2\omega_3 - 9\omega_4c_s^2\omega_1^3\omega_2^2 - 288\omega_4c_s^2\omega_1^3v_3^2\omega_2\omega_3 - v_1^2\omega_4\omega_1^3\omega_2^2\omega_3 - 312\omega_4c_s^2v_3^2\omega_2^2\omega_3 + 20\omega_4c_s^4\omega_1^2\omega_2^2 - \\
& 81\omega_4\omega_1^3v_3^2\omega_2^2\omega_3 + 18\omega_4c_s^2\omega_1^3\omega_2^2 - 60\omega_4c_s^2\omega_1v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_1\omega_2^2\omega_3 + v_1^4\omega_4\omega_1^3\omega_2^2\omega_3 - 24\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 + 40\omega_4c_s^2\omega_2^2\omega_3 - 8\omega_4c_s^2\omega_1^3\omega_2 + \\
& 84\omega_4\omega_1^2v_3^2\omega_2^2\omega_3 + 18\omega_4c_s^2\omega_1^2\omega_2^2 + 32\omega_4c_s^2\omega_1\omega_2^2\omega_3 + 7\omega_4\omega_1^3\omega_2^2\omega_3 + 120\omega_4c_s^2\omega_1^2v_3^2\omega_2\omega_3 - 32\omega_4c_s^4\omega_1^2\omega_2\omega_3 - 54\omega_4c_s^2\omega_1^2v_3^2\omega_2^2 + 36c_s^2\omega_1^2\omega_2^2\omega_3 + \\
& 144\omega_4v_3^2\omega_2^2\omega_3 + 4\omega_4\omega_1^3\omega_3 + 9\omega_4c_s^4\omega_1^3\omega_2^2 - 29\omega_4c_s^4\omega_1^2\omega_2^2\omega_3 - 138\omega_4\omega_1^2v_3^4\omega_2^2\omega_3 + 108c_s^2\omega_1v_3^2\omega_2^2\omega_3 + 432\omega_4c_s^2\omega_1v_3^2\omega_2^2\omega_3 + 14\omega_4\omega_1\omega_2^2\omega_3 - \\
& 20\omega_4c_s^2\omega_1^2\omega_2^2 - 60\omega_4\omega_1^2v_3^2\omega_2\omega_3 + 9c_s^4\omega_1^3\omega_2^2\omega_3 + 138\omega_4\omega_1^2v_3^2\omega_2^2\omega_3 - 16\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 18\omega_4c_s^4\omega_1^2\omega_2^2 + 60\omega_4c_s^2\omega_1^2v_3^2\omega_2^2 - 68\omega_4c_s^4\omega_1^2\omega_2^2\omega_3 - \\
& 222\omega_4\omega_1v_3^2\omega_2^2\omega_3 - 8\omega_4\omega_2^2\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 240\omega_4\omega_1^3v_3^4\omega_2\omega_3 + 27c_s^2\omega_1^3v_3^2\omega_2^2\omega_3 + 94\omega_4c_s^2\omega_1\omega_2^2\omega_3 + 24\omega_4c_s^2\omega_1v_3^2\omega_2^2 - 36c_s^2\omega_1\omega_2^2\omega_3 - \\
& 24\omega_4\omega_1v_3^2\omega_2^2\omega_3 - 8\omega_4c_s^2\omega_1\omega_2^2 - 7\omega_4\omega_1^2\omega_2^2\omega_3 - 96\omega_4\omega_1^2v_3^2\omega_2\omega_3 + 16\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 90\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3 - 10\omega_4\omega_1^2\omega_2\omega_3 + 17\omega_4c_s^4\omega_1^3\omega_2^2\omega_3 + \\
& 24\omega_4c_s^2\omega_1^3v_3^2\omega_2 + 408\omega_4\omega_1v_3^4\omega_2^2\omega_3 + 153\omega_4c_s^2\omega_1^3v_3^2\omega_2\omega_3 + 138\omega_4c_s^2v_3^2\omega_2\omega_3 + 96\omega_4c_s^2\omega_1^3v_3^4\omega_2\omega_3 - 28\omega_4c_s^4\omega_1\omega_2^2\omega_3 - 54\omega_4c_s^2\omega_1^3v_3^2\omega_2^2 + v_1^2\omega_4\omega_1^2\omega_2^2\omega_3 + \\
& 24\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - v_1^4\omega_4\omega_1^3\omega_2^2\omega_3 + 12\omega_4\omega_1v_3^2\omega_2^2\omega_3 + 42\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 36c_s^4\omega_1^2\omega_2^2\omega_3 - 9c_s^2\omega_1^3\omega_2^2\omega_3 + 192\omega_4\omega_1^2v_3^4\omega_2\omega_3 + 27\omega_4c_s^2\omega_1^3v_3^2\omega_2^2 - \\
& 20\omega_4c_s^2\omega_1^3\omega_3 + 8\omega_4c_s^4\omega_1^2\omega_2\omega_3 + 8\omega_4c_s^4\omega_1\omega_2^2 + 3v_1^2\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 3\omega_4c_s^4\omega_1^3\omega_2^2\omega_3 - 153\omega_4c_s^2\omega_1^2v_3^2\omega_2^2\omega_3 - 108c_s^2\omega_1^2v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_2^2\omega_2^2\omega_3
\end{aligned}$$

$$\begin{aligned}
C_{57} = & -6\omega_4\omega_1v_3^2\omega_3 - 2\omega_4^2v_2^2\omega_1\omega_3 + 3\omega_1v_3^2\omega_3^2 + 2\omega_4^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_1\omega_3^2 - 6\omega_4^2v_3^2 - 6\omega_4^2\omega_1 - 18\omega_4c_s^2\omega_3^2 + 36\omega_4c_s^2\omega_2\omega_3 - 6\omega_4v_2^2\omega_2^2 - 6\omega_4^2v_2^2 - \\
& 18\omega_4c_s^2\omega_1\omega_3 + 3\omega_2^2\omega_1v_3^2 - 36\omega_4^2c_s^2 + 12\omega_4^2 + 6v_2^2\omega_3^2 - 6\omega_4^2\omega_3 + 18\omega_4^2c_s^2\omega_3 - 12\omega_4\omega_3 - 2\omega_4\omega_1\omega_3^2 + 3\omega_4^2v_3^2\omega_1 - 6v_3^2\omega_3^2 - 3v_2^2\omega_1\omega_3^2 - \\
& 6\omega_4^2c_s^2\omega_1\omega_3 + 18\omega_4^2c_s^2\omega_1 + 6\omega_4\omega_2^2 + 6\omega_4\omega_1\omega_3 + 6\omega_4^2v_2^2\omega_3 + 2\omega_4v_2^2\omega_1\omega_3^2 + 12\omega_4v_3^2\omega_3
\end{aligned}$$

$$\begin{aligned}
C_{58} = & 2\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 18\omega_4v_2^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 + 18\omega_4v_2^2\omega_1\omega_3 + \\
& 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 - 9\omega_1v_3^2\omega_2\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 + 4\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{59} = & -2c_s^2\omega_1 - 36c_s^2\omega_1v_3^2\omega_2 - 9\omega_1v_3^4\omega_2 + 6\omega_$$

$$\begin{aligned}
& 3\omega_4\omega_1^3v_3^4\omega_3^2 - 36\omega_4^2c_s^2\omega_1v_3^2\omega_3^2 - 12\omega_4c_s^2\omega_1\omega_3^2 - 36\omega_4^2c_s^2\omega_1^3v_3^2\omega_3 + 12\omega_4\omega_1^2v_3^2\omega_3^2 + 27\omega_4^2c_s^2\omega_1^3v_3^2 + 3\omega_4^2c_s^4\omega_1^3\omega_3 - 36\omega_4^2\omega_1^2v_3^2\omega_3 - 3\omega_4^2c_s^4\omega_1^3\omega_3 - \\
& 18\omega_1^2v_3^4\omega_3^2 - 15\omega_4^2\omega_1^3v_3^4\omega_3 + 24\omega_4^2c_s^4\omega_1^3\omega_3^2 - 8\omega_4^2c_s^2\omega_1^2\omega_3^2 + 36\omega_4^2c_s^2\omega_1v_3^2\omega_3 - 9\omega_1^3v_3^2\omega_3^2 - 54c_s^2\omega_1^2v_3^2\omega_3^2 + 6\omega_4^2c_s^2\omega_1^3v_3^2\omega_3^2 - 18\omega_1^2\omega_3^2v_3^4 - \\
& 54\omega_1^2c_s^2\omega_1^3v_3^2 - 12\omega_4^2c_s^4\omega_1^3\omega_3 + 12\omega_4c_s^4\omega_1\omega_3^2 - 18\omega_4\omega_1^3v_3^2\omega_3 - 36\omega_4c_s^2\omega_1^3v_3^2\omega_3 - 3\omega_4^2c_s^2\omega_1^3\omega_3 - 36\omega_4\omega_1^2v_3^4\omega_3 - 3\omega_4^2\omega_1^3v_3^2\omega_3^2 + 12\omega_4^2c_s^4\omega_1\omega_3 + \\
& 18\omega_1^2\omega_3^2v_3^2 - 12\omega_4c_s^4\omega_1^2\omega_3^2 - 3\omega_4c_s^2\omega_1^3\omega_3^2 - 12\omega_4^2\omega_1^2v_3^4\omega_3^2 + 72\omega_4^2c_s^2\omega_1^2v_3^2\omega_3 - 108\omega_4c_s^2\omega_1^2v_3^2\omega_3 - 36\omega_4\omega_1^2v_3^2\omega_3^2 + 12\omega_4^2c_s^2\omega_1\omega_3^2 - 15\omega_4\omega_1^3v_3^4\omega_3^2 - \\
& 12\omega_1^2c_s^2\omega_1\omega_3 + 18\omega_4\omega_1^3v_3^4\omega_3 + 12\omega_4c_s^2\omega_1^2\omega_3^2 + 3\omega_4^2c_s^4\omega_1^3\omega_3^2 - 9\omega_1^2\omega_3^2v_3^2 + 72\omega_4c_s^2\omega_1^2v_3^2\omega_3^2 + 36\omega_4\omega_1^2v_3^2\omega_3 + 36\omega_4^2\omega_1^3v_3^4\omega_3 - 12\omega_4^2c_s^2\omega_1^2v_3^2\omega_3^2 + \\
& 27c_s^2\omega_1^3v_3^2\omega_3^2 + 18\omega_1^2v_3^2\omega_3^2 - 48\omega_4^2c_s^4\omega_1\omega_3^2 + 15\omega_4^2\omega_1^3v_3^2\omega_3 + 9\omega_1^3v_3^4\omega_3^2
\end{aligned}$$

2.7.4 Conservation of momentum: ρv_2

$$\begin{aligned}
& v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_1 v_2 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_2 \delta_t \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_t \rho}{\delta_t} \frac{\partial v_2}{\partial x_1} + (v_2^2 + c_s^2) \frac{\delta_t}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2v_2 \delta_t \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 v_3 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_t \rho}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\
& \frac{v_2 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_t^2}{2\omega_1 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (6v_1^2 \omega_1 - 2\omega_1 + 6c_s^2 \omega_1 + 2\omega_2 + 3c_s^2 \omega_1 \omega_2 - 12c_s^2 \omega_2 - 6v_1^2 \omega_2) \frac{\delta_t^2}{6\omega_1 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\
& (\omega_1 - \omega_2) \frac{2v_1 \delta_t^2 \rho}{\omega_1 \omega_2 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (3v_1^2 \omega_1 - \omega_1 + c_s^2 \omega_1 + \omega_2 - c_s^2 \omega_2 - 3v_1^2 \omega_2) \frac{\delta_t^2}{3\omega_1 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\
& (-2\omega_1 + 4c_s^2 \omega_1 + 6v_2^2 \omega_1 + 3\omega_1 \omega_2 - 4\omega_2 - 9v_2^2 \omega_1 \omega_2 + 12v_2^2 \omega_2 - 6c_s^2 \omega_1 \omega_2 + 8c_s^2 \omega_2) \frac{\delta_t^2}{3\omega_1 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + \\
& (2\omega_1 - 3\omega_1 \omega_2 + 4\omega_2) \frac{v_2 \delta_t^2 \rho}{\omega_1 \omega_2 \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-\omega_1 + c_s^2 \omega_1 + \omega_2 - 3v_3^2 \omega_2 + 3\omega_1 v_3^2 - c_s^2 \omega_2) \frac{\delta_t^2}{3\omega_1 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_1 - \omega_2) \frac{2v_3 \delta_t^2 \rho}{\omega_1 \omega_2 \delta_t} \frac{\partial v_3}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2\omega_1 + 6c_s^2 \omega_1 + 2\omega_2 - 6v_3^2 \omega_2 + 6\omega_1 v_3^2 + 3c_s^2 \omega_1 \omega_2 - 12c_s^2 \omega_2) \frac{\delta_t^2}{6\omega_1 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\
& (-2 + \omega_1) \frac{c_s^2 \delta_t^2}{2\omega_1 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_t^2 \rho}{2\omega_1 \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + (v_1^2 \omega_1 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 - v_1^2 \omega_2) \frac{v_1 \delta_t^2}{3\omega_1 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + \\
& (6v_1^2 \omega_1 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 + 3c_s^2 \omega_1 \omega_2 - 8c_s^2 \omega_2 - 6v_1^2 \omega_2) \frac{\delta_t^2 \rho}{6\omega_1 \omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (-2\omega_1 + 6c_s^2 \omega_1 + 2v_2^2 \omega_1 + 3\omega_1 \omega_2 - 4\omega_2 - 3v_2^2 \omega_1 \omega_2 + 4v_2^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 + 12c_s^2 \omega_2) \frac{v_2 \delta_t^2}{6\omega_1 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\
& (-2\omega_1 + 2c_s^2 \omega_1 + 6v_2^2 \omega_1 + 3\omega_1 \omega_2 - 4\omega_2 - 9v_2^2 \omega_1 \omega_2 + 12v_2^2 \omega_2 - 3c_s^2 \omega_1 \omega_2 + 4c_s^2 \omega_2) \frac{\delta_t^2 \rho}{6\omega_1 \omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-\omega_1 + 3c_s^2 \omega_1 + \omega_2 - v_3^2 \omega_2 + \omega_1 v_3^2 - 3c_s^2 \omega_2) \frac{v_3 \delta_t^2}{3\omega_1 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + \\
& (-2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 6v_3^2 \omega_2 + 6\omega_1 v_3^2 + 3c_s^2 \omega_1 \omega_2 - 8c_s^2 \omega_2) \frac{\delta_t^2 \rho}{6\omega_1 \omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_t^2 \rho}{2\omega_1 \delta_t} \frac{\partial^2 v_2}{\partial x_3^2} + \\
& (-1 + v_1^2 + 3c_s^2) \frac{v_1 v_2 \delta_t^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_2 \delta_t^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{v_1 \delta_t^3 \rho}{12\omega_4 \omega_1 \omega_3 \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + C_2 \frac{\delta_t^3}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& C_3 \frac{v_1 \delta_t^3 \rho}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} - \frac{c_s^2 v_2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_4 \frac{v_1 v_2 \delta_t^3}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_t^3 \rho}{12\omega_4 \omega_1^2 \omega_2^2 \omega_3 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_6 \frac{v_1 \delta_t^3 \rho}{6\omega_1^2 \omega_2^2 \omega_3 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + \\
& C_7 \frac{\delta_t^3}{12\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + C_8 \frac{v_2 \delta_t^3 \rho}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + C_9 \frac{v_3 \delta_t^3 \rho}{4\omega_4 \omega_1 \omega_3 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} - \frac{c_s^2 v_2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + C_{10} \frac{v_1 v_3 \delta_t^3}{3\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\
& C_{11} \frac{v_3 \delta_t^3 \rho}{6\omega_4 \omega_1^2 \omega_2^2 \omega_3 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{12} \frac{v_1 \delta_t^3 \rho}{6\omega_4 \omega_1^2 \omega_2^2 \omega_3 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{13} \frac{v_2 v_3 \delta_t^3}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_{14} \frac{v_3 \delta_t^3 \rho}{6\omega_1^2 \omega_2^2 \omega_3 \delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& C_{15} \frac{v_2 \delta_t^3 \rho}{12\omega_4 \omega_1^2 \omega_2^2 \omega_3 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{c_s^2 v_2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_{16} \frac{v_1 \delta_t^3 \rho}{4\omega_4 \omega_1 \omega_3 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_3^2} + C_{17} \frac{\delta_t^3}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{c_s^2 v_2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& C_{18} \frac{v_3 \delta_t^3 \rho}{6\omega_1^2 \omega_2^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + (-1 + v_3^2 + 3c_s^2) \frac{v_2 v_3 \delta_t^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{19} \frac{v_3 \delta_t^3 \rho}{12\omega_4 \omega_1 \omega_3 \delta_t} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{v_2 \delta_t^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_{20} \frac{v_2 \delta_t^4}{72\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + (10v_1^2 \omega_1 - 4\omega_1 + 6c_s^2 \omega_1 + 6\omega_1 \omega_2 - 8\omega_2 - 9c_s^2 \omega_1 \omega_2 + 12c_s^2 \omega_2 + 20v_1^2 \omega_2 - 15v_1^2 \omega_1 \omega_2) \frac{v_1 v_2 \delta_t^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& + C_{21} \frac{\delta_t^4 \rho}{24\omega_4^2 \omega_1^3 \omega_2^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_{22} \frac{v_1 \delta_t^4}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{23} \frac{\delta_t^4 \rho}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{24} \frac{v_1 v_2 \delta_t^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& C_{25} \frac{v_2 \delta_t^4}{36\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{v_1 v_2 \delta_t^4 \rho}{18\omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{27} \frac{\delta_t^4 \rho}{36\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{28} \frac{v_1 \delta_t^4}{36\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + \\
& C_{29} \frac{\delta_t^4 \rho}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{30} \frac{v_1 v_2 \delta_t^4 \rho}{18\omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{31} \frac{v_2 \delta_t^4}{36\omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2} + C_{32} \frac{\delta_t^4 \rho}{36\omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& (-\omega_1 + 3c_s^2 \omega_1 + \omega_2 - v_3^2 \omega_2 + \omega_1 v_3^2 - 3c_s^2 \omega_2) \frac{v_1 v_2 v_3 \delta_t^4}{12\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& (-\omega_1 + 3c_s^2 \omega_1 + \omega_2 - v_3^2 \omega_2 + \omega_1 v_3^2 - 3c_s^2 \omega_2) \frac{v_2 v_3 \delta_t^4 \rho}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{33} \frac{v_1 v_3 \delta_t^4 \rho}{8\omega_4^2 \omega_1^3 \omega_2^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_3} + C_{34} \frac{v_1 v_2 \delta_t^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{35} \frac{v_3 \delta_t^4}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{36} \frac{v_1 v_3 \delta_t^4 \rho}{6\omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{37} \frac{v_2 v_3 \delta_t^4 \rho}{72\omega_4 \omega_1 \omega_2 \omega_3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{\delta_t^4 \rho}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{v_1 v_2 v_3 \delta_t^4}{6\omega_1^3 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{40} \frac{v_2 v_3 \delta_t^4 \rho}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{v_1 v_3 \delta_t^4 \rho}{6\omega_4 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& + C_{42} \frac{v_1 v_2 \delta_t^4 \rho}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{v_3 \delta_t^4}{36\omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{44} \frac{v_2 v_3 \delta_t^4 \rho}{18\omega_1^3 \omega_2^3 \omega_3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{45} \frac{\delta_t^4 \rho}{72\omega_4^2 \omega_1^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& (3v_1^2 \omega_1 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 3v_3^2 \omega_2 + 3\omega_1 v_3^2 + 6c_s^2 \omega_1 \omega_2 - 14c_s^2 \omega_2 - 3v_1^2 \omega_2) \frac{c_s^2 v_2 \delta_t^4}{36\omega_1 \omega_2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} +
\end{aligned}$$

$$\begin{aligned}
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_2\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + C_{46} \frac{\delta_l^4\rho}{8\omega_1^2\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_3^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + \omega_2 - v_3^2\omega_2 + \omega_1v_3^2 - 3c_s^2\omega_2) \frac{v_2v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_3^2} + C_{47} \frac{v_1\delta_l^4\rho}{72\omega_1^2\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{48} \frac{\delta_l^4\rho}{72\omega_1^2\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2\partial x_3^2} + C_{49} \frac{v_1v_2\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + C_{50} \frac{v_1v_3\delta_l^4\rho}{6\omega_1^3\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_2\partial x_3^2} + C_{51} \frac{v_2\delta_l^4\rho}{36\omega_4^2\omega_1^3\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_2^2\partial x_3^2} + \\
& + C_{52} \frac{\delta_l^4\rho}{36\omega_4\omega_1^3\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_2^2\partial x_3^2} + C_{53} \frac{v_2v_3\delta_l^4\rho}{18\omega_1^3\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3^2} + (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_2v_3\delta_l^4\rho}{12\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^3} + \\
& C_{54} \frac{v_2v_3\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_3^3} + C_{55} \frac{v_1v_3\delta_l^4\rho}{8\omega_1^2\omega_1\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_3^3} + (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_2\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_1\partial x_3^3} + \\
& C_{56} \frac{v_3\delta_l^4\rho}{72\omega_1^2\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_2\partial x_3^3} + C_{57} \frac{v_2v_3\delta_l^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_2\partial x_3^3} + C_{58} \frac{\delta_l^4\rho}{36\omega_4\omega_1^3\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_2\partial x_3^3} + C_{59} \frac{v_2\delta_l^4\rho}{72\omega_1\omega_2\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{60} \frac{\delta_l^4\rho}{24\omega_1^4\omega_3^3\omega_5\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4\omega_1 + 6c_s^2\omega_1 + 6\omega_1\omega_2 - 8\omega_2 + 20v_3^2\omega_2 + 10\omega_1v_3^2 - 9c_s^2\omega_1\omega_2 + 12c_s^2\omega_2 - 15\omega_1v_3^2\omega_2) \frac{v_2v_3\delta_l^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 9\omega_4c_s^2\omega_1 + 6v_1^2\omega_4\omega_3 + 6\omega_4 + 9c_s^2\omega_1\omega_3 - 6v_1^2\omega_4 + 3v_1^2\omega_4\omega_1 - 6v_1^2\omega_3 + 18\omega_4c_s^2\omega_3 + 3v_1^2\omega_1\omega_3 - 6\omega_4c_s^2\omega_1\omega_3 - 18c_s^2\omega_3 - 18\omega_4c_s^2 - \\
& 6\omega_4\omega_3 + 6\omega_3 - 3\omega_1\omega_3 - 2v_1^2\omega_4\omega_1\omega_3 - 3\omega_4\omega_1 + 2\omega_4\omega_1\omega_3 \\
C_2 &= 3v_1^2\omega_1^2\omega_2 - 2c_s^4\omega_1^2\omega_2 - 14c_s^4\omega_2^2 - 18v_1^2c_s^2\omega_2^2 - 4v_1^4\omega_2^2 - 2c_s^2\omega_1^2 + 2c_s^2\omega_1^2\omega_2 - 3v_1^4\omega_1^2\omega_2 - 15v_1^2c_s^2\omega_1^2\omega_2 - c_s^4\omega_1^2\omega_2^2 - 2v_1^2\omega_1^2 + 14c_s^4\omega_1\omega_2^2 + \\
& 6v_1^2c_s^2\omega_1\omega_2 - 3v_1^2\omega_1\omega_2^2 + 4v_1^4\omega_2^2 + 2v_1^4\omega_1\omega_2 + 2c_s^2\omega_2^2 + 12v_1^2c_s^2\omega_1^2 + 3v_1^4\omega_1\omega_2^2 - 2c_s^2\omega_1\omega_2^2 + 2v_1^4\omega_1^2 + 2c_s^4\omega_1^2 + 15v_1^2c_s^2\omega_1\omega_2^2 - 2v_1^2\omega_1\omega_2 \\
C_3 &= -5\omega_1\omega_2^2 - 11v_1^2\omega_1^2\omega_2 + 8c_s^2\omega_1^2 - 4\omega_1^2 - 9c_s^2\omega_1^2\omega_2 - 2\omega_1\omega_2 + 8v_1^2\omega_1^2 + 5\omega_1^2\omega_2 + 11v_1^2\omega_1\omega_2^2 - 14v_1^2\omega_2^2 + 6\omega_2^2 + 2c_s^2\omega_1\omega_2 - 10c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 6v_1^2\omega_1\omega_2 \\
C_4 &= -3\omega_1\omega_2^2 - 3v_1^2\omega_1^2\omega_2 + 2v_2^2\omega_2^2 + 12c_s^2\omega_1^2 - 4\omega_1^2 - 9c_s^2\omega_1^2\omega_2 + 2\omega_1\omega_2 - 4v_2^2\omega_1\omega_2 + 2v_1^2\omega_1^2 + 3\omega_1^2\omega_2 + 3v_1^2\omega_1\omega_2^2 - 4v_1^2\omega_2^2 + 2\omega_2^2 - \\
& 6c_s^2\omega_1\omega_2 - 6c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2v_2^2\omega_2^2 + 2v_1^2\omega_1\omega_2 \\
C_5 &= -8\omega_4\omega_1^2\omega_3 + 18c_s^2\omega_1^2\omega_2\omega_3 + 8\omega_4\omega_1^2\omega_2\omega_3 - 12\omega_4c_s^2\omega_1^2\omega_2 - 3\omega_4v_2^2\omega_1^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_2^2\omega_3 + 8\omega_4\omega_1\omega_2^2 + 12v_1^2\omega_4\omega_1^2\omega_3 + 12\omega_4c_s^2\omega_1\omega_2^2\omega_3 + \\
& 18v_1^2\omega_4\omega_1\omega_2^2\omega_3 - 8\omega_4v_2^2\omega_1\omega_2^2 - 12v_2^2\omega_1\omega_2^2\omega_3 + 16\omega_4c_s^2\omega_1^2\omega_2\omega_3 + 18\omega_4c_s^2\omega_1^2\omega_2^2 + 4\omega_4v_2^2\omega_1^2\omega_2\omega_3 - 12\omega_4c_s^2\omega_1^2\omega_2\omega_3 + 12\omega_1\omega_2^2\omega_3 - 18v_1^2\omega_4\omega_1^2\omega_2\omega_3 - \\
& 11\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 24\omega_4c_s^2\omega_1\omega_2^2 + 4\omega_4\omega_1^2\omega_2 + 4\omega_4c_s^2\omega_1\omega_2\omega_3 + 6v_2^2\omega_1^2\omega_2^2\omega_3 + 8\omega_4v_2^2\omega_2^2\omega_3 + 6\omega_4v_2^2\omega_1^2\omega_2^2 + 16\omega_4c_s^2\omega_1^2\omega_3 - 6\omega_1^2\omega_2^2\omega_3 + \\
& 12v_1^2\omega_4\omega_1\omega_2\omega_3 - 36c_s^2\omega_1\omega_2^2\omega_3 - 4\omega_4v_2^2\omega_1^2\omega_2 - 2\omega_4v_2^2\omega_1^2\omega_2\omega_3 - 6\omega_4\omega_1^2\omega_2^2 - 4\omega_4\omega_1\omega_2\omega_3 + 2\omega_4v_2^2\omega_1\omega_2^2\omega_3 - 24v_1^2\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_1^2\omega_2^2\omega_3 \\
C_6 &= -2\omega_1\omega_2^2 - 2v_1^2\omega_1^2\omega_2 - 4\omega_1^2\omega_3 - 4c_s^2\omega_2^2\omega_3 - 4c_s^2\omega_1\omega_2\omega_3 + 6v_2^2\omega_2^2\omega_3 + v_1^2\omega_1\omega_2^2\omega_3 - 6c_s^2\omega_1^2\omega_2 + \omega_1^2\omega_2\omega_3 - 2v_1^2\omega_2^2\omega_3 - v_1^2\omega_1^2\omega_2\omega_3 - \\
& \omega_1\omega_2^2\omega_3 + 2\omega_1^2\omega_2 - 12v_2^2\omega_1\omega_2\omega_3 + 2v_1^2\omega_1\omega_2^2 + 4\omega_1\omega_2\omega_3 + 2v_1^2\omega_1^2\omega_3 + 3c_s^2\omega_1\omega_2^2\omega_3 + 6c_s^2\omega_1\omega_2^2 - 3c_s^2\omega_1^2\omega_2\omega_3 + 6v_2^2\omega_2^2\omega_3 + 8c_s^2\omega_1^2\omega_3 \\
C_7 &= 72c_s^2v_2^2\omega_2^2 + 24v_2^2\omega_1\omega_2^2 - 4c_s^4\omega_1^2\omega_2 + 8c_s^4\omega_2^2 - c_s^2\omega_1^2\omega_2^2 + 16v_2^2\omega_1\omega_2 - 48c_s^2v_2^2\omega_1^2\omega_2 - 4v_2^2\omega_1^2 + 24c_s^2v_2^2\omega_1^2\omega_2^2 - 4c_s^2\omega_1^2 + 4c_s^2\omega_1^2\omega_2 - \\
& 24v_2^4\omega_1\omega_2^2 - 16v_2^2\omega_1\omega_2 + c_s^4\omega_1^2\omega_2^2 + 16v_2^4\omega_2^2 + 12v_2^2\omega_1^2\omega_2^2 - 8c_s^4\omega_1\omega_2^2 + 4v_2^4\omega_1^2 - 96c_s^2v_2^2\omega_1\omega_2^2 - 8c_s^2\omega_2^2 + 7v_2^4\omega_1^2\omega_2^2 + 8c_s^2\omega_1\omega_2^2 - 12v_2^4\omega_1^2\omega_2^2 - \\
& 16v_2^2\omega_2^2 + 48c_s^2v_2^2\omega_1\omega_2 + 24c_s^2v_2^2\omega_1^2 + 4c_s^4\omega_1^2 - 7v_2^2\omega_1^2\omega_2^2 \\
C_8 &= 16\omega_1\omega_2^2 - 40v_2^2\omega_1\omega_2^2 + 5c_s^2\omega_1^2\omega_2^2 + 8v_2^2\omega_1^2 + 8c_s^2\omega_1^2 - 4\omega_1^2 - 12c_s^2\omega_1^2\omega_2 - 8\omega_1\omega_2 + 24v_2^2\omega_1\omega_2 + 8\omega_1^2\omega_2 - 20v_2^2\omega_1^2\omega_2 - 12\omega_2^2 + 8c_s^2\omega_1\omega_2 + \\
& 20c_s^2\omega_2^2 - 24c_s^2\omega_1\omega_2^2 + 28v_2^2\omega_2^2 - 4\omega_1^2\omega_2^2 + 11v_2^2\omega_1^2\omega_2^2 \\
C_9 &= 3\omega_4c_s^2\omega_1 + 2\omega_4 - 3c_s^2\omega_1\omega_3 - \omega_1v_3^2\omega_3 + 6c_s^2\omega_3 - 6\omega_4c_s^2 + \omega_4\omega_1v_3^2 - 2\omega_3 + \omega_1\omega_3 - 2\omega_4v_3^2 + 2v_3^2\omega_3 - \omega_4\omega_1 \\
C_{10} &= v_3^2\omega_2^2 + 6c_s^2\omega_1^2 - 2\omega_1^2 + \omega_1^2v_3^2 + 4\omega_1\omega_2 + v_1^2\omega_1^2 + v_1^2\omega_2^2 - 2\omega_2^2 - 12c_s^2\omega_1\omega_2 + 6c_s^2\omega_2^2 - 2\omega_1v_3^2\omega_2 - 2v_1^2\omega_1\omega_2 \\
C_{11} &= -2\omega_4v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_1^2\omega_3 + 3\omega_4\omega_1^2v_3^2\omega_2^2 - 9c_s^2\omega_1^2\omega_2^2\omega_3 + \omega_4\omega_1^2\omega_2\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2 - \omega_4\omega_1\omega_2^2\omega_3 + 4\omega_4\omega_1\omega_2^2 + 6v_1^2\omega_4\omega_1^2\omega_3 + \\
& 3\omega_4c_s^2\omega_1\omega_2^2\omega_3 + 6\omega_1v_3^2\omega_2^2\omega_3 - 4\omega_4c_s^2\omega_1^2\omega_2^2 + 9\omega_4c_s^2\omega_1^2\omega_2^2 - 3\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 6\omega_1\omega_2^2\omega_3 - 2\omega_4\omega_1^2v_3^2\omega_2 - 12\omega_4c_s^2\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - \\
& 4\omega_4c_s^2\omega_1\omega_2\omega_3 - \omega_4\omega_1^2v_3^2\omega_2\omega_3 + 8\omega_4c_s^2\omega_1^2\omega_3 + 3\omega_1^2\omega_2^2\omega_3 - 12v_1^2\omega_4\omega_1\omega_2\omega_3 + 18c_s^2\omega_1\omega_2^2\omega_3 - 4\omega_4\omega_1v_3^2\omega_2^2 - 3\omega_1^2v_3^2\omega_2^2\omega_3 - 3\omega_4\omega_1^2\omega_2^2 + \\
& 4\omega_4\omega_1\omega_2\omega_3 + \omega_4\omega_1v_3^2\omega_2^2\omega_3 + 2\omega_4\omega_1^2v_3^2\omega_3 + 6v_1^2\omega_4\omega_2^2\omega_3 \\
C_{12} &= -4v_1^2\omega_4\omega_1\omega_2^2 + 6\omega_4v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_1^2\omega_3 - 9c_s^2\omega_1^2\omega_2^2\omega_3 + \omega_4\omega_1^2\omega_2\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2 - \omega_4\omega_1\omega_2^2\omega_3 + 4\omega_4\omega_1\omega_2^2 + 2v_1^2\omega_4\omega_1^2\omega_3 - 12\omega_4\omega_1v_3^2\omega_2\omega_3 + \\
& 6v_1^2\omega_1\omega_2^2\omega_3 + 3\omega_4c_s^2\omega_1\omega_2^2\omega_3 + v_1^2\omega_4\omega_1\omega_2^2\omega_3 - 4\omega_4c_s^2\omega_2^2\omega_3 + 9\omega_4c_s^2\omega_1^2\omega_2^2 - 3\omega_4c_s^2\omega_1^2\omega_2\omega_3 - 6\omega_1\omega_2^2\omega_3 - v_1^2\omega_4\omega_1^2\omega_2\omega_3 - 3v_1^2\omega_1^2\omega_2^2\omega_3 - 12\omega_4c_s^2\omega_1\omega_2^2 - \\
& 2v_1^2\omega_4\omega_1^2\omega_2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_4c_s^2\omega_1\omega_2\omega_3 + 8\omega_4c_s^2\omega_1^2\omega_3 + 3\omega_1^2\omega_2^2\omega_3 + 18c_s^2\omega_1\omega_2^2\omega_3 - 3\omega_4\omega_1^2\omega_2^2 + 4\omega_4\omega_1\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_3 + 3v_1^2\omega_4\omega_1^2\omega_2^2 - 2v_1^2\omega_4\omega_2^2\omega_3 \\
C_{13} &= -4v_3^2\omega_2^2 - 3\omega_1\omega_2^2 + 2v_2^2\omega_1^2 - 3\omega_1^2v_3^2\omega_2 + 12c_s^2\omega_1^2 - 4\omega_1^2 - 9c_s^2\omega_1^2\omega_2 + 2\omega_1^2v_3^2 + 2\omega_1\omega_2 - 4v_2^2\omega_1\omega_2 + 3\omega_1^2\omega_2 + 3\omega_1v_3^2\omega_2^2 + 2\omega_2^2 - \\
& 6c_s^2\omega_1\omega_2 - 6c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2v_2^2\omega_2^2 + 2\omega_1v_3^2\omega_2 \\
C_{14} &= -2\omega_1\omega_2^2 - 4\omega_1^2\omega_3 - \omega_1^2v_3^2\omega_2\omega_3 - 4c_s^2\omega_2^2\omega_3 - 4c_s^2\omega_1\omega_2\omega_3 + 6v_2^2\omega_1^2\omega_3 - 2\omega_1^2v_3^2\omega_2 - 2v_3^2\omega_2^2\omega_3 - 6c_s^2\omega_1^2\omega_2 + \omega_1^2\omega_2\omega_3 + \omega_1v_3^2\omega_2^2\omega_3 - \\
& \omega_1\omega_2^2\omega_3 + 2\omega_1^2\omega_2 + 2\omega_1v_3^2\omega_2^2 - 12v_2^2\omega_1\omega_2\omega_3 + 4\omega_1\omega_2\omega_3 + 2\omega_1^2v_3^2\omega_3 + 3c_s^2\omega_1\omega_2^2\omega_3 + 6c_s^2\omega_1\omega_2^2 - 3c_s^2\omega_1^2\omega_2\omega_3 + 6v_2^2\omega_2^2\omega_3 + 8c_s^2\omega_1^2\omega_3 \\
C_{15} &= -24\omega_4v_3^2\omega_2^2\omega_3 - 8\omega_4\omega_1^2\omega_3 + 18c_s^2\omega_1^2\omega_2^2\omega_3 + 8\omega_4\omega_1^2\omega_2\omega_3 - 12\omega_4c_s^2\omega_1^2\omega_2 - 3\omega_4v_2^2\omega_1^2\omega_2^2\omega_3 - 8\omega_4\omega_1\omega_2^2\omega_3 + 8\omega_4\omega_1\omega_2^2 + 12\omega_4\omega_1v_3^2\omega_2\omega_3 + \\
& 12\omega_4c_s^2\omega_1\omega_2^2\omega_3 - 8\omega_4v_2^2\omega_1\omega_2^2 - 12v_2^2\omega_1\omega_2^2\omega_3 + 16\omega_4c_s^2\omega_2^2\omega_3 + 18\omega_4c_s^2\omega_1^2\omega_2^2 + 4\omega_4v_2^2\omega_1^2\omega_2^2\omega_3 - 12\omega_4c_s^2\omega_1^2\omega_2\omega_3 + 12\omega_1\omega_2^2\omega_3 - 11\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 -
\end{aligned}$$

$$C_{26} = -18c_s^3\omega_1^3\omega_2 - 23\omega_1^3\omega_2^2\omega_3 + 141v_1^2\omega_1\omega_3^2\omega_3 + 36c_s^2\omega_1^2\omega_2^2 - 60\omega_1\omega_1^3\omega_3 - 6v_1^2\omega_1\omega_2^2 + 6\omega_1\omega_2^2 - 9v_1^2\omega_1\omega_3^2\omega_3 + 50v_1^2\omega_1^2\omega_2^2\omega_3 - 114v_1^2\omega_1^2\omega_3^2 + 60v_1^2\omega_1\omega_2^2\omega_3 - 12v_2^2\omega_1^2\omega_2\omega_3 - 42c_s^2\omega_1^2\omega_2^2\omega_3 + 6\omega_1^2\omega_2\omega_3 - 108c_s^3\omega_1^2\omega_2\omega_3 - 12v_2^2\omega_1\omega_2^2\omega_3 + 6\omega_1^2\omega_2^2\omega_3 - 12\omega_1\omega_2^2\omega_3 + 12v_2^2\omega_1^3\omega_3 - 36\omega_1^3\omega_3 - 66c_s^3\omega_1^3\omega_3 - 66v_1^2\omega_1^2\omega_2^2\omega_3 + 108c_s^2\omega_1\omega_2^2\omega_3 + 84c_s^2\omega_1^3\omega_3 + 42\omega_2^3\omega_3 + 12v_2^2\omega_3^2\omega_3 + 18v_2^2\omega_1^2\omega_2^2\omega_3 + 42c_s^3\omega_1^3\omega_2^2\omega_3 + 12\omega_1^2\omega_2^2\omega_3 - 6v_2^2\omega_1^3\omega_2 - 50v_1^2\omega_1^2\omega_2^2\omega_3 - 75v_1^2\omega_1^3\omega_2\omega_3 + 6\omega_1^3\omega_2 - 18c_s^2\omega_1\omega_2^2 + 48\omega_1^2\omega_3^2 + 23\omega_1^2\omega_2^2\omega_3 - 18c_s^2\omega_1^2\omega_2\omega_3 + 48\omega_1^2\omega_3\omega_3 - 12\omega_1^2\omega_2^2 + 12v_2^2\omega_1^2\omega_2^2 - 9v_2^2\omega_1^2\omega_2\omega_3$$

$$\begin{aligned}
C_{28} = & -48v_2^2\omega_1^3\omega_3^2 + 24v_1^2v_2^2\omega_1^3\omega_3^2 + 8\omega_1\omega_2^2\omega_3^2 - 36v_2^4\omega_1^3\omega_2\omega_3 - 12c_s^2\omega_1^2\omega_3^2 + 4\omega_1^4\omega_3^2 + 72c_2^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 4c_2^4\omega_1^2\omega_2^2\omega_3 + 20c_2^2\omega_1^3\omega_3^2 + 24c_4^4\omega_1\omega_2^3\omega_3 + \\
& 48v_2^2\omega_1\omega_2^2\omega_3^2 - 36c_4^4\omega_1^2\omega_2\omega_3^2 - 2v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 + 4v_1^2\omega_1^4\omega_2\omega_3^2 + 96v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 + 5c_2^2\omega_1^2\omega_2^2\omega_3^2 - 4\omega_1^4\omega_2\omega_3^2 + 108c_2^2v_2^2\omega_1\omega_2^2\omega_3^2 + 56c_2^2\omega_1^2\omega_2\omega_3^2 + \\
& 54c_4^4\omega_1^3\omega_2^2\omega_3 + 12v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 - 36c_4^4\omega_1^3\omega_2^2\omega_3 - 8v_1^2\omega_1^2\omega_2^2\omega_3^2 - 4v_1^2c_2^2\omega_1^2\omega_2\omega_3^2 + 24v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 24v_2^2\omega_1^2\omega_2^2\omega_3^2 - 20v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 + 18v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 + 36c_4^4\omega_1\omega_2^3\omega_3 + \\
& 6c_2^4\omega_1^2\omega_2^2\omega_3^2 - 12v_1^2c_2^2\omega_1^2\omega_2\omega_3^2 - 20v_1^2c_2^2\omega_1^2\omega_2\omega_3^2 + 24v_2^4\omega_1^3\omega_2\omega_3 - 36c_2^4\omega_1^2\omega_2^2\omega_3^2 + 8v_1^2\omega_1^2\omega_2^2\omega_3^2 - v_1^2\omega_1^4\omega_2^2\omega_3^2 - 2v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 + 24v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 + \\
& 72v_2^4\omega_1^2\omega_2^2\omega_3^2 + 18c_2^4\omega_1^2\omega_2^3\omega_3 + 8\omega_1\omega_2^3\omega_3^2 + 4c_2^4\omega_1^2\omega_2\omega_3^2 + 42c_4^4\omega_1\omega_2^3\omega_3^2 - 4v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 - 24v_2^2\omega_1^2\omega_2^2\omega_3^2 - 8v_1^2\omega_1\omega_2^3\omega_3^2 + 12c_2^2\omega_1^2\omega_2^2\omega_3^2 - 216c_2^2v_2^2\omega_1\omega_2^2\omega_3^2 + \\
& 24v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 + \omega_1^3\omega_2^2\omega_3^2 - 34c_2^2\omega_1^2\omega_2^2\omega_3^2 + 22v_1^2c_2^2\omega_1\omega_2^2\omega_3^2 + 24v_2^2\omega_1^2\omega_2^2\omega_3^2 - 12c_2^4\omega_1^2\omega_2^2\omega_3 + 84v_2^4\omega_1^3\omega_2\omega_3 - 4v_1^2\omega_1^4\omega_2^2\omega_3^2 - \omega_1^2\omega_2^3\omega_3^2 + 72c_4^4\omega_1^2\omega_3^2 + \\
& 40c_2^2\omega_1^2\omega_2\omega_3^2 - 72v_2^2\omega_1\omega_2^2\omega_3^2 - 8c_2^4\omega_1\omega_2^3\omega_3 + 48v_1^2\omega_2^3\omega_3^2 - 4\omega_1^4\omega_2\omega_3^2 + v_1^2\omega_1^4\omega_2^2\omega_3^2 + 2v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 - 84c_2^4\omega_1^3\omega_2\omega_3^2 + 4v_1^2\omega_1^2\omega_2\omega_3^2 - 6c_2^4\omega_1^2\omega_2\omega_3^2 - \\
& 8c_2^4\omega_1\omega_2^3\omega_3^2 + 216c_2^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 48v_2^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 18c_2^4\omega_1^2\omega_2^2\omega_3^2 + 216c_2^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 36v_2^4\omega_1\omega_2^3\omega_3^2 - 5c_2^4\omega_1^2\omega_2^2\omega_3^2 - 4\omega_1^4\omega_2^2\omega_3^2 + 18v_1^2c_2^2\omega_1^2\omega_2^2\omega_3^2 - \\
& 52c_2^2\omega_1^2\omega_2^2\omega_3^2 - 12c_2^4\omega_1^2\omega_2\omega_3^2 - 8\omega_2^3\omega_3^2 + 8v_1^2c_2^2\omega_1\omega_2^2\omega_3^2 - 54c_2^4\omega_1^2\omega_2^2\omega_3^2 + 24v_2^4\omega_1^2\omega_2^2\omega_3^2 - 24v_2^4\omega_1^2\omega_2^2\omega_3^2 - 48v_1^2v_2^2\omega_1\omega_2^2\omega_3^2 - 72c_2^2v_2^2\omega_1\omega_2^2\omega_3^2 + \\
& 16v_1^2c_2^2\omega_1^2\omega_3^2 - 22c_2^2\omega_1\omega_2^3\omega_3^2 - 72v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 - 324c_2^2v_2^2\omega_1^2\omega_2\omega_3^2 - 24v_1^2v_2^2\omega_1^2\omega_2^2\omega_3^2 + 8v_1^2c_2^2\omega_1\omega_2^3\omega_3^2 - 4v_1^2c_2^2\omega_1^2\omega_2\omega_3^2 + 42c_4^4\omega_1^2\omega_2^2\omega_3^2 + 4v_1^2\omega_1^2\omega_2^2\omega_3^2
\end{aligned}$$

$$C_{30} = -18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_3 - 5\omega_1^3\omega_2^2\omega_3 + 81c_s^2\omega_1^2\omega_2^2\omega_3 + 27v_1^2\omega_1\omega_3^2\omega_3 - 18c_s^2\omega_1^2\omega_2^2 + 3\omega_1\omega_3^2\omega_3 + 9v_1^2\omega_1^3\omega_2^2 - 12\omega_1\omega_3^2 - 66v_1^2\omega_1\omega_2^2\omega_3 + 5v_1^2\omega_1^3\omega_2^2\omega_3 - 24v_1^2\omega_2^2\omega_3 - 6v_1^2\omega_1^3\omega_2 + 6v_1^2\omega_1\omega_2^2\omega_3 - 9v_1^2\omega_1^2\omega_3^2 - 12v_1^2\omega_1^2\omega_2\omega_3 - 15c_s^2\omega_1^2\omega_3^2\omega_3 + 6\omega_1^2\omega_2\omega_3 - 108c_s^2\omega_1^2\omega_2\omega_3 - 120v_1^2\omega_1\omega_2^2\omega_3 - 6v_1^2\omega_1^2\omega_3^2 + 6v_1^2\omega_1^2\omega_2\omega_3 + 42\omega_1\omega_2^2\omega_3 + 27c_s^2\omega_1^3\omega_2^2 + 48v_1^2\omega_1^3\omega_3 - 36\omega_1^3\omega_3 - 12c_s^2\omega_1^3\omega_3 - 9v_1^2\omega_1^2\omega_2^2\omega_3 + 27c_s^2\omega_1\omega_3^2\omega_3 + 84c_s^2\omega_1^3\omega_3 + 12v_1^2\omega_1\omega_3^2 -$$

$$36\omega_1^3\omega_3 - 66c_s^2\omega_2^3\omega_3 + 108c_s^2\omega_1\omega_2^3\omega_3 - 50\omega_1^2v_3^2\omega_2^3\omega_3 + 84c_s^2\omega_1^3\omega_3 + 42\omega_2^3\omega_3 + 50\omega_1^3v_3^2\omega_2^2\omega_3 + 12v_2^2\omega_3^3\omega_3 + 18v_2^2\omega_1^2\omega_2^3\omega_3 + 42c_s^2\omega_1^3\omega_2^3\omega_3 + 12\omega_1^2\omega_2^3\omega_3 - 66\omega_1^2v_3^2\omega_2^3\omega_3 - 6v_2^2\omega_1^3\omega_2 + 6\omega_1^3\omega_2 - 18c_s^2\omega_1\omega_2^3 + 23\omega_1^2\omega_2^3\omega_3 - 18c_s^2\omega_1^2\omega_2\omega_3 + 48\omega_1^3\omega_2\omega_3 - 12\omega_1^2\omega_2^2 + 12v_2^2\omega_1^2\omega_2^2 - 9v_2^2\omega_1^2\omega_2\omega_3$$

$$C_{54} = -18v_1^2\omega_4\omega_2\omega_3 + 2\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 - 9\omega_1v_3^2\omega_2\omega_3 + 18v_1^2\omega_4\omega_1\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 + 4\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$C_{55} = -6\omega_4\omega_1v_3^2\omega_3 - 2v_1^2\omega_2^2\omega_1\omega_3 + 3\omega_1v_3^2\omega_2^3 + 2\omega_4^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_1\omega_2^2 - 3v_1^2\omega_1\omega_2^2 - 6\omega_4^2v_3^2 - 6\omega_4^2\omega_1 + 6v_1^2\omega_2^2 - 18\omega_4c_s^2\omega_2^2 + 36\omega_4c_s^2\omega_3 - 6v_1^2\omega_4^2 - 18\omega_4c_s^2\omega_1\omega_3 + 3\omega_4^2\omega_1v_3^2 - 36\omega_4^2c_s^2 + 12\omega_4^2 - 6\omega_4^2\omega_3 - 6v_1^2\omega_4\omega_3 + 18\omega_1^2c_s^2\omega_3 - 12\omega_4\omega_3 - 2\omega_4\omega_1\omega_3 + 3v_1^2\omega_4^2\omega_1 + 2v_1^2\omega_4\omega_1\omega_3 - 6v_3^2\omega_3^2 - 6\omega_4^2c_s^2\omega_1\omega_3 + 18\omega_4^2c_s^2\omega_1 + 6\omega_4\omega_3^2 + 6\omega_4\omega_1\omega_3 + 6v_1^2\omega_4^2\omega_3 + 12\omega_4v_3^2\omega_3$$

$$C_{56} = 104\omega_4^2\omega_1^2v_3^2\omega_2^3\omega_3 + 56\omega_4^2c_s^2\omega_1\omega_2^3\omega_3 - 104\omega_4^2c_s^2\omega_1^3\omega_3 - 56\omega_4^2c_s^2\omega_1v_3^2\omega_2^3\omega_3 + 36\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 - 276\omega_4^2c_s^4\omega_1^3\omega_2\omega_3 - 8\omega_4^2\omega_1^2\omega_2^3\omega_3 + 9\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 + 54c_s^4\omega_1^3\omega_2^3\omega_3 - 342\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3 - 78\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 + 48\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 + 36c_s^2\omega_1^2\omega_2^3\omega_3 - 56\omega_4^2c_s^2\omega_1v_3^2\omega_2^3\omega_3 - 6\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 + 108\omega_4^2c_s^4\omega_1\omega_2^3\omega_3 + 78\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 - 88\omega_4^2c_s^2\omega_1^2\omega_2\omega_3 + 56\omega_4^2c_s^2\omega_1\omega_2^3\omega_3 + 6\omega_4^2v_3^2\omega_1^2\omega_2^3\omega_3 + 120\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3 - 712\omega_4^2c_s^2\omega_1v_3^2\omega_2^3\omega_3 - 16\omega_4^2\omega_1^3\omega_2^3\omega_3 + 12\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 + 16\omega_4^2c_s^2\omega_1^3v_3^2\omega_2\omega_3 - 20\omega_4^2\omega_1^3v_3^2\omega_2\omega_3 - 96\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 + 144\omega_4^2c_s^4\omega_1^3\omega_3 - 14\omega_4^2\omega_1^2\omega_2^3\omega_3 + 9\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 + 6\omega_4^2v_3^2\omega_1^3\omega_2^3\omega_3 + 92\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 + 448\omega_4^2c_s^2\omega_1^2v_3^2\omega_2\omega_3 - 368\omega_4^2c_s^2\omega_1\omega_2^3\omega_3 + 320\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 + 18\omega_4^2c_s^2v_3^2\omega_1^2\omega_2^3\omega_3 + 48\omega_4^2c_s^4\omega_1^2\omega_2\omega_3 - 36\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 + 216\omega_4^2c_s^4\omega_1^2v_3^2\omega_2^3\omega_3 - 784\omega_4^2c_s^2v_3^2\omega_2^3\omega_3 - 92\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 - 118\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 + 1232\omega_4^2c_s^2\omega_1v_3^2\omega_2^3\omega_3 - 56\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 + 36\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 + 28\omega_4^2\omega_1^2\omega_2^3\omega_3 - 108\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3 + 228\omega_4^2\omega_1v_3^2\omega_2^3\omega_3 - 18\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 + 152\omega_4^2\omega_1^3v_3^2\omega_2\omega_3 + 6\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 - 144\omega_4^2c_s^2\omega_1\omega_2^3\omega_3 - 36c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 - 18\omega_4^2c_s^2v_3^2\omega_2^3\omega_3 + 184\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 - 288\omega_4^2c_s^4\omega_2^3\omega_3 - 18c_s^2\omega_1^3\omega_2^3\omega_3 + 72\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 - 108\omega_4^2c_s^4\omega_1^2\omega_3 + 208\omega_4^2c_s^2\omega_1^2\omega_2\omega_3 + 32\omega_4^2\omega_1v_3^2\omega_2^3\omega_3 - 27\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 + 120\omega_4^2\omega_1^2v_3^2\omega_2\omega_3 - 36\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 - 36\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 + 14\omega_4^2\omega_1^2\omega_2^3\omega_3 - 168\omega_4^2c_s^4\omega_1\omega_2^3\omega_3 + 72\omega_4^2c_s^4\omega_1^2\omega_2\omega_3 + 18\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3 - 108\omega_4^2\omega_1^2\omega_2^3\omega_3 + 160\omega_4^2v_3^2\omega_2^3\omega_3 - 40\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 - 6\omega_4^2v_3^2\omega_1^2\omega_2^3\omega_3 - 412\omega_4^2c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 - 256\omega_4^2\omega_1^3v_3^2\omega_2^3\omega_3 + 54\omega_4^2c_s^4\omega_1^3\omega_2^3\omega_3 + 52\omega_4^2\omega_1^2\omega_2^3\omega_3 - 132\omega_4^2\omega_1^3v_3^2\omega_2\omega_3 + 40\omega_4^2c_s^2\omega_1^2v_3^2\omega_2\omega_3 + 18\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 + 394\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 + 208\omega_4^2c_s^2\omega_2^3\omega_3 + 588\omega_4^2c_s^4\omega_1\omega_2^3\omega_3 - 8\omega_4^2\omega_1\omega_2^3\omega_3 - 6\omega_4^2v_3^2\omega_1^3\omega_2^3\omega_3 + 36\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 - 24\omega_4^2\omega_1v_3^2\omega_2^3\omega_3 - 27\omega_4^2c_s^2\omega_1^3\omega_2^3\omega_3 - 72\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 + 18c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 - 136\omega_4^2\omega_1^2v_3^2\omega_2\omega_3 + 8\omega_4^2\omega_1^2\omega_2^3\omega_3 - 460\omega_4^2c_s^2\omega_1^2\omega_2^3\omega_3 - 16\omega_4^2c_s^2\omega_1^2\omega_2\omega_3 - 9\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 + 16\omega_4^2\omega_1^2\omega_2\omega_3 - 144\omega_4^2v_3^2\omega_2^3\omega_3 + 144\omega_4^2c_s^4\omega_1^2\omega_2^3\omega_3 - 9\omega_4^2c_s^2\omega_1^3v_3^2\omega_2^3\omega_3$$

$$C_{57} = 2\omega_4\omega_1v_3^2\omega_3 - 27c_s^2\omega_1\omega_2\omega_3 + 2\omega_4\omega_2\omega_3 + 6\omega_4\omega_1v_3^2\omega_2\omega_3 + 9\omega_4\omega_1\omega_2 - 18\omega_4v_3^2\omega_2\omega_3 + 12\omega_4c_s^2\omega_1\omega_3 + 6\omega_4c_s^2\omega_2\omega_3 + 18\omega_4v_3^2\omega_1\omega_3 + 9\omega_1\omega_2\omega_3 + 18\omega_4c_s^2\omega_1\omega_2\omega_3 - 9\omega_4\omega_1v_3^2\omega_2 - 9\omega_1v_3^2\omega_2\omega_3 - 6\omega_4\omega_1\omega_2\omega_3 + 4\omega_4v_3^2\omega_2\omega_3 - 8\omega_4\omega_1\omega_3 - 27\omega_4c_s^2\omega_1\omega_2$$

$$C_{58} = 10\omega_4^4c_s^4\omega_1^2\omega_2^3\omega_3 - 18\omega_4^4c_s^4\omega_1^2\omega_3^2 + 8\omega_4^4c_s^4\omega_1^3\omega_2 - 168\omega_4\omega_1^2v_3^4\omega_2^3\omega_3 + 36c_s^4\omega_1\omega_2^3\omega_3 + \omega_4v_3^4\omega_1^3\omega_2^3\omega_3 + 81\omega_4\omega_1^2v_3^3\omega_2^3\omega_3 + 8\omega_4\omega_1^2\omega_2\omega_3 - 54\omega_4c_s^2\omega_1\omega_3^3\omega_3 - 264\omega_4v_3^4\omega_2^3\omega_3 + 144\omega_4c_s^2\omega_1^3v_3^3\omega_3 - 9\omega_4c_s^2\omega_1^3\omega_2^2 - 288\omega_4c_s^2\omega_1^3v_3^2\omega_2\omega_3 - 312\omega_4c_s^2v_3^2\omega_2^3\omega_3 + 20\omega_4c_s^4\omega_1^2\omega_2^2 - 81\omega_4\omega_1^3v_3^2\omega_2^3\omega_3 + 18\omega_4c_s^2\omega_1^3\omega_2^2 - 60\omega_4c_s^2\omega_1v_3^2\omega_2^2\omega_3 - 4\omega_4\omega_1\omega_2^3\omega_3 - 24\omega_4c_s^2\omega_1^3\omega_2^3\omega_3 + 40\omega_4c_s^2\omega_2^3\omega_3 - 8\omega_4c_s^2\omega_1^3\omega_2 + 84\omega_4\omega_1^2v_3^2\omega_2^3\omega_3 + 18\omega_4c_s^2\omega_1^2\omega_3^2 + 32\omega_4c_s^2\omega_1^2\omega_2^3\omega_3 + 7\omega_4\omega_1^3\omega_2^3\omega_3 + 120\omega_4c_s^2\omega_1^2v_3^2\omega_2\omega_3 - 32\omega_4c_s^4\omega_1^3\omega_2\omega_3 - 54\omega_4c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 + 36c_s^2\omega_1^2\omega_2^3\omega_3 + 144\omega_4v_3^2\omega_2^3\omega_3 + 4\omega_4\omega_1^3\omega_3 + 9\omega_4^4\omega_1^3\omega_2^2 - 29\omega_4^4c_s^2\omega_1^3\omega_2^2\omega_3 - 138\omega_4\omega_1^3v_3^2\omega_2^3\omega_3 + 108c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 + 432\omega_4c_s^2\omega_1v_3^2\omega_2^3\omega_3 + 14\omega_4\omega_1^2\omega_2^3\omega_3 - 20\omega_4c_s^2\omega_1^2\omega_2^2 - 60\omega_4\omega_1^3v_3^2\omega_3 + 9c_s^4\omega_1^3\omega_2^3 + 138\omega_4\omega_1^3v_3^4\omega_2^3\omega_3 - 16\omega_4c_s^2\omega_1^3\omega_2\omega_3 + \omega_4v_3^2\omega_1^2\omega_2^3\omega_3 + 3\omega_4c_s^2v_3^2\omega_1^2\omega_2^3\omega_3 - 18\omega_4c_s^4\omega_1^3\omega_2^2 + 60\omega_4c_s^2\omega_1^2v_3^2\omega_2^2 - 68\omega_4c_s^4\omega_3^3\omega_3 - 222\omega_4\omega_1v_3^2\omega_2^3\omega_3 - 8\omega_4\omega_2^3\omega_3 - 6\omega_4c_s^2\omega_1^2\omega_2^2\omega_3 - 240\omega_4\omega_1^3v_3^2\omega_2\omega_3 + 27c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 + 94\omega_4c_s^4\omega_1\omega_2^3\omega_3 + 24\omega_4c_s^2\omega_1v_3^2\omega_2^2 - 3\omega_4c_s^2v_3^2\omega_1^2\omega_2^3\omega_3 - 36c_s^2\omega_1^2\omega_2^3\omega_3 - \omega_4v_3^2\omega_1^2\omega_2^3\omega_3 - 24\omega_4\omega_1v_3^4\omega_2^3\omega_3 - 8\omega_4c_s^2\omega_1v_3^4\omega_2^3\omega_3 - 7\omega_4\omega_1^2\omega_2^3\omega_3 - 96\omega_4\omega_1^2v_3^2\omega_2\omega_3 + 16\omega_4c_s^4\omega_1^3\omega_3 - 90\omega_4c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 - 10\omega_4\omega_1^3\omega_2\omega_3 + 17\omega_4c_s^4\omega_1^3\omega_2^3\omega_3 + 24\omega_4c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 + 408\omega_4\omega_1v_3^4\omega_2^3\omega_3 + 153\omega_4c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 + 138\omega_4\omega_1^3v_3^2\omega_2\omega_3 + 96\omega_4\omega_1^3v_3^4\omega_3 - 28\omega_4c_s^4\omega_1\omega_2^3\omega_3 - 54\omega_4c_s^2\omega_1^3v_3^2\omega_2^2 + 24\omega_4c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 + 12\omega_4\omega_1v_3^4\omega_2^3\omega_3 + 42\omega_4c_s^2\omega_1^3\omega_2\omega_3 - 36c_s^4\omega_1^2\omega_2^3\omega_3 - 9c_s^2\omega_1^3\omega_2^3\omega_3 + 192\omega_4\omega_1^2v_3^4\omega_2\omega_3 + 27\omega_4c_s^2\omega_1^2v_3^4\omega_2^2 - 20\omega_4c_s^2\omega_1^3\omega_3 + 8\omega_4c_s^4\omega_1^2\omega_2\omega_3 + 8\omega_4c_s^4\omega_1\omega_2^3 - 3\omega_4c_s^4\omega_1^3\omega_2^3\omega_3 - 153\omega_4c_s^2\omega_1^3v_3^2\omega_2^3\omega_3 - \omega_4v_3^4\omega_1^2\omega_2^3\omega_3 - 108c_s^2\omega_1^2v_3^2\omega_2^3\omega_3 - 4\omega_4\omega_1^2\omega_2^3\omega_3$$

$$C_{59} = -2c_s^2\omega_1 - 36c_s^2\omega_1v_3^2\omega_2 - 9\omega_1v_3^4\omega_2 + 6\omega_1v_3^4 + 24c_s^2\omega_1v_3^2 + 4c_s^4\omega_2 - 12v_3^2\omega_2 + 2c_s^4\omega_1 - 6\omega_1v_3^2 + 48c_s^2v_3^2\omega_2 + 3c_s^2\omega_1\omega_2 - 4c_s^2\omega_2 + 12v_3^4\omega_2 + 9\omega_1v_3^2\omega_2 - 3c_s^4\omega_1\omega_2$$

$$C_{60} = 9\omega_2^2\omega_1^3v_3^4 + \omega_2^2c_s^2\omega_1^3\omega_3^2 + 36\omega_4\omega_1^3v_3^4\omega_3^2 + 24\omega_2^2c_s^4\omega_1^2\omega_3^2 + 36\omega_4c_s^2\omega_1^2v_3^2\omega_3^2 + 15\omega_4\omega_1^3v_3^2\omega_3^2 + 54\omega_4c_s^2\omega_1^3v_3^2\omega_3 + 12\omega_2^2c_s^2\omega_1^2\omega_3 + 3\omega_4^2\omega_1^3v_3^4\omega_2^2 - 36\omega_4^2c_s^2\omega_1^3v_3^2\omega_3 - 12\omega_4c_s^2\omega_1^3\omega_3^2 - 36\omega_4^2c_s^2\omega_1^3v_3^2\omega_3 + 12\omega_4^2c_s^2\omega_1^3\omega_3^2 + 27\omega_4^2c_s^2\omega_1^3v_3^2\omega_3 + 3\omega_4^2c_s^4\omega_1^3\omega_3 - 36\omega_2^2\omega_1^4v_3^3\omega_3 - 3\omega_4^2c_s^4\omega_1^3\omega_3^2 - 18\omega_1^2v_3^4\omega_3^2 - 15\omega_4^2\omega_1^3v_3^4\omega_3 + 24\omega_4^2c_s^4\omega_3^2 - 8\omega_4^2c_s^2\omega_1^2\omega_3^2 + 36\omega_4^2c_s^2\omega_1v_3^2\omega_3 - 9\omega_1^3v_3^2\omega_3^2 - 54c_s^2\omega_2^2v_3^2\omega_3^2 + 6\omega_4^2c_s^2\omega_1^3v_3^2\omega_3^2 - 18\omega_4^2\omega_1^2v_3^4 - 54\omega_2^2c_s^2\omega_1^2v_3^2 - 12\omega_4^2c_s^4\omega_1^2\omega_3 + 12\omega_4c_s^4\omega_1\omega_3^2 - 18\omega_4\omega_1^3v_3^2\omega_3 - 36\omega_4c_s^2\omega_1^2v_3^2\omega_3^2 - 3\omega_4^2c_s^2\omega_1^2\omega_3 - 36\omega_4\omega_1^2v_3^2\omega_3 - 3\omega_4^2\omega_1^3v_3^2\omega_3 + 12\omega_4^2c_s^4\omega_1\omega_3 + 18\omega_2^2\omega_1^2v_3^2 - 12\omega_4c_s^4\omega_1^2\omega_3^2 - 3\omega_4c_s^2\omega_1^3\omega_3^2 - 12\omega_4^2\omega_1^2v_3^4\omega_3^2 + 72\omega_4^2c_s^2\omega_1^2v_3^2\omega_3 - 108\omega_4c_s^2\omega_1^2v_3^2\omega_3 - 36\omega_4\omega_1^2v_3^2\omega_3 + 12\omega_4^2c_s^2\omega_1\omega_3^2 - 15\omega_4\omega_1^3v_3^4\omega_3^2 - 12\omega_2^2c_s^2\omega_1\omega_3 + 18\omega_4\omega_1^3v_3^4\omega_3 + 12\omega_4c_s^2\omega_1^2\omega_3^2 + 3\omega_4c_s^4\omega_1^3\omega_3^2 - 9\omega_2^2\omega_1^3v_3^2\omega_3^2 + 72\omega_4c_s^2\omega_1^2v_3^2\omega_3 + 36\omega_4\omega_1^2v_3^2\omega_3 + 36\omega_4\omega_1^2v_3^4\omega_3 - 12\omega_4^2c_s^2\omega_1^2v_3^2\omega_3 + 27c_s^2\omega_1^3v_3^2\omega_3^2 + 18\omega_1^2v_3^2\omega_3^2 - 48\omega_1^2c_s^4\omega_1\omega_3^2 + 15\omega_4^2\omega_1^3v_3^2\omega_3 + 9\omega_1^3v_3^4\omega_3^2$$

2.7.5 Conservation of momentum: ρv_3

$$v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_1 v_3 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \delta_t \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_2 v_3 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \delta_t \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_2} + (v_3^2 + c_s^2) \frac{\delta_t}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{2v_3 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_t^2}{2\omega_1 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (6v_1^2\omega_1 - 2\omega_1 + 6c_s^2\omega_1 + 2\omega_2 + 3c_s^2\omega_1\omega_2 - 12c_s^2\omega_2 - 6v_1^2\omega_2) \frac{\delta_t^2}{6\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_1 - \omega_2) \frac{2v_1 \delta_t^2 \rho}{\omega_1\omega_2\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_t^2}{2\omega_1 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2\omega_1 + 6c_s^2\omega_1 + 6v_2^2\omega_1 + 2\omega_2 - 6v_2^2\omega_2 + 3c_s^2\omega_1\omega_2 - 12c_s^2\omega_2) \frac{\delta_t^2}{6\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (\omega_1 - \omega_2) \frac{2v_2 \delta_t^2 \rho}{\omega_1\omega_2\delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (3v_1^2\omega_1 - \omega_1 + c_s^2\omega_1 + \omega_2 - c_s^2\omega_2 - 3v_1^2\omega_2) \frac{\delta_t^2}{3\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (-\omega_1 + c_s^2\omega_1 + 3v_2^2\omega_1 + \omega_2 - 3v_2^2\omega_2 - c_s^2\omega_2) \frac{\delta_t^2}{3\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (-2\omega_1 + 4c_s^2\omega_1 + 3\omega_1\omega_2 - 4\omega_2 + 12v_3^2\omega_2 + 6\omega_1v_3^2 - 6c_s^2\omega_1\omega_2 + 8c_s^2\omega_2 - 9\omega_1v_3^2\omega_2) \frac{\delta_t^2}{3\omega_1\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} +$$

$$\begin{aligned}
& (2\omega_1 - 3\omega_1\omega_2 + 4\omega_2) \frac{v_3\delta_1^2\rho}{\omega_1\omega_2\delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_1) \frac{c_s^2\delta_1^2\rho}{2\omega_1\delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + (-2 + \omega_1) \frac{c_s^2\delta_1^2\rho}{2\omega_1\delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1\delta_1^2\rho}{3\omega_1\omega_2\delta_t} \frac{\partial^2\rho}{\partial x_1\partial x_3} + \\
& (6v_1^2\omega_1 - 2\omega_1 + 2c_s^2\omega_1 + 2\omega_2 + 3c_s^2\omega_1\omega_2 - 8c_s^2\omega_2 - 6v_1^2\omega_2) \frac{\delta_1^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 v_1}{\partial x_1\partial x_3} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2\delta_1^2\rho}{3\omega_1\omega_2\delta_t} \frac{\partial^2\rho}{\partial x_2\partial x_3} + \\
& (-2\omega_1 + 2c_s^2\omega_1 + 6v_2^2\omega_1 + 2\omega_2 - 6v_2^2\omega_2 + 3c_s^2\omega_1\omega_2 - 8c_s^2\omega_2) \frac{\delta_1^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 v_2}{\partial x_2\partial x_3} + \\
& (-2\omega_1 + 6c_s^2\omega_1 + 3\omega_1\omega_2 - 4\omega_2 + 4v_3^2\omega_2 + 2\omega_1v_3^2 - 9c_s^2\omega_1\omega_2 + 12c_s^2\omega_2 - 3\omega_1v_3^2\omega_2) \frac{v_3\delta_1^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2\rho}{\partial x_3^2} + \\
& (-2\omega_1 + 2c_s^2\omega_1 + 3\omega_1\omega_2 - 4\omega_2 + 12v_3^2\omega_2 + 6\omega_1v_3^2 - 3c_s^2\omega_1\omega_2 + 4c_s^2\omega_2 - 9\omega_1v_3^2\omega_2) \frac{\delta_1^2\rho}{6\omega_1\omega_2\delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (-1 + v_1^2 + 3c_s^2) \frac{v_1v_3\delta_1^3\rho}{12\delta_t} \frac{\partial^3\rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_3\delta_1^3\rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{v_1\delta_1^3\rho}{12\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{c_s^2v_3\delta_1^3\rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2\partial x_2} + \\
& C_2 \frac{v_2\delta_1^3\rho}{4\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_1^2\partial x_2} - \frac{c_s^2v_3\delta_1^3\rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_2^2} + C_3 \frac{v_1\delta_1^3\rho}{4\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_2v_3\delta_1^3\rho}{12\delta_t} \frac{\partial^3\rho}{\partial x_2^2\partial x_3} + \\
& (-1 + 3v_2^2 + c_s^2) \frac{v_3\delta_1^3\rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + C_4 \frac{v_2\delta_1^3\rho}{12\omega_4\omega_1\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_2^2} + C_5 \frac{\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3\rho}{\partial x_1^2\partial x_3} + C_6 \frac{v_1\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2\partial x_3} - \frac{c_s^2v_3\delta_1^3\rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2\partial x_3} + \\
& C_7 \frac{v_1v_2\delta_1^3\rho}{3\omega_1^2\omega_2^2\delta_t} \frac{\partial^3\rho}{\partial x_1\partial x_2\partial x_3} + C_8 \frac{v_2\delta_1^3\rho}{6\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_2\partial x_3} + C_9 \frac{v_1\delta_1^3\rho}{6\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_2}{\partial x_1\partial x_2\partial x_3} + C_{10} \frac{\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3\rho}{\partial x_2^2\partial x_3} + \\
& C_{11} \frac{v_2\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^2\partial x_3} - \frac{c_s^2v_3\delta_1^3\rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2\partial x_3} + C_{12} \frac{v_1v_3\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3\rho}{\partial x_1\partial x_3^2} + C_{13} \frac{v_3\delta_1^3\rho}{12\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_3^2} + C_{14} \frac{v_1\delta_1^3\rho}{6\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_1\partial x_3^2} + \\
& C_{15} \frac{v_2v_3\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3\rho}{\partial x_2\partial x_3^2} + C_{16} \frac{v_3\delta_1^3\rho}{12\omega_4\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_2}{\partial x_2\partial x_3^2} + C_{17} \frac{v_2\delta_1^3\rho}{6\omega_1^2\omega_2^2\omega_3\delta_t} \frac{\partial^3 v_3}{\partial x_2\partial x_3^2} + C_{18} \frac{\delta_1^3\rho}{12\omega_1^2\omega_2^2\delta_t} \frac{\partial^3\rho}{\partial x_3^3} + C_{19} \frac{v_3\delta_1^3\rho}{6\omega_1^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_{20} \frac{v_3\delta_1^4\rho}{72\omega_1\omega_2\delta_t} \frac{\partial^4\rho}{\partial x_1^4} + (10v_1^2\omega_1 - 4\omega_1 + 6c_s^2\omega_1 + 6\omega_1\omega_2 - 8\omega_2 - 9c_s^2\omega_1\omega_2 + 12c_s^2\omega_2 + 20v_1^2\omega_2 - 15v_1^2\omega_1\omega_2) \frac{v_1v_3\delta_1^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} \\
& + C_{21} \frac{\delta_1^4\rho}{24\omega_1^2\omega_3^2\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_1v_2v_3\delta_1^4\rho}{12\omega_1\omega_2\delta_t} \frac{\partial^4\rho}{\partial x_1^2\partial x_2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2v_3\delta_1^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2} + C_{22} \frac{v_1v_3\delta_1^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2} + C_{23} \frac{v_1v_2\delta_1^4\rho}{8\omega_4^2\omega_1\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2} + \\
& (3v_1^2\omega_1 - 2\omega_1 + 2c_s^2\omega_1 + 3v_2^2\omega_1 + 2\omega_2 - 3v_2^2\omega_2 + 6c_s^2\omega_1\omega_2 - 14c_s^2\omega_2 - 3v_1^2\omega_2) \frac{c_s^2v_3\delta_1^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4\rho}{\partial x_1^2\partial x_2^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_3\delta_1^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2^2} + \\
& (-\omega_1 + 3c_s^2\omega_1 + v_2^2\omega_1 + \omega_2 - v_2^2\omega_2 - 3c_s^2\omega_2) \frac{v_2v_3\delta_1^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2^2} + C_{24} \frac{\delta_1^4\rho}{8\omega_4^2\omega_1^3\omega_5\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_2v_3\delta_1^4\rho}{12\omega_1\omega_2\delta_t} \frac{\partial^4\rho}{\partial x_1\partial x_2^2} + C_{25} \frac{v_2v_3\delta_1^4\rho}{72\omega_4\omega_1\omega_2\omega_3\delta_t} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2} + \\
& (v_1^2\omega_1 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 - v_1^2\omega_2) \frac{v_1v_3\delta_1^4\rho}{36\omega_1\omega_2\delta_t} \frac{\partial^4 v_2}{\partial x_1\partial x_2^2} + C_{26} \frac{v_1v_2\delta_1^4\rho}{8\omega_4^2\omega_1\omega_3\delta_t} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2} + C_{27} \frac{v_3\delta_1^4\rho}{72\omega_1\omega_2\delta_t} \frac{\partial^4\rho}{\partial x_2^4} + \\
& (-4\omega_1 + 6c_s^$$

$$\begin{aligned}
C_1 &= 9\omega_4 c_s^2 \omega_1 + 6v_1^2 \omega_4 \omega_3 + 6\omega_4 + 9c_s^2 \omega_1 \omega_3 - 6v_1^2 \omega_4 + 3v_1^2 \omega_4 \omega_1 - 6v_1^2 \omega_3 + 18\omega_4 c_s^2 \omega_3 + 3v_1^2 \omega_1 \omega_3 - 6\omega_4 c_s^2 \omega_1 \omega_3 - 18c_s^2 \omega_3 - 18\omega_4 c_s^2 - 6\omega_4 \omega_3 + 6\omega_3 - 3\omega_1 \omega_3 - 2v_1^2 \omega_4 \omega_1 \omega_3 - 3\omega_4 \omega_1 + 2\omega_4 \omega_1 \omega_3 \\
C_2 &= 3\omega_4 c_s^2 \omega_1 + 2v_2^2 \omega_3 + 2\omega_4 - 3c_s^2 \omega_1 \omega_3 + \omega_4 v_2^2 \omega_1 + 6c_s^2 \omega_3 - 6\omega_4 c_s^2 - 2\omega_3 - 2\omega_4 v_2^2 + \omega_1 \omega_3 - v_2^2 \omega_1 \omega_3 - \omega_4 \omega_1 \\
C_3 &= 3\omega_4 c_s^2 \omega_1 + 2\omega_4 - 3c_s^2 \omega_1 \omega_3 - 2v_1^2 \omega_4 + v_1^2 \omega_4 \omega_1 + 2v_1^2 \omega_3 - v_1^2 \omega_1 \omega_3 + 6c_s^2 \omega_3 - 6\omega_4 c_s^2 - 2\omega_3 + \omega_1 \omega_3 - \omega_4 \omega_1 \\
C_4 &= 9\omega_4 c_s^2 \omega_1 - 6v_2^2 \omega_3 + 6\omega_4 + 9c_s^2 \omega_1 \omega_3 + 6\omega_4 v_2^2 \omega_3 + 18\omega_4 c_s^2 \omega_3 - 6\omega_4 c_s^2 \omega_1 \omega_3 + 3\omega_4 v_2^2 \omega_1 - 18c_s^2 \omega_3 - 18\omega_4 c_s^2 - 2\omega_4 v_2^2 \omega_1 \omega_3 - 6\omega_4 \omega_3 + 6\omega_3 - 6\omega_4 v_2^2 - 3\omega_1 \omega_3 + 3v_2^2 \omega_1 \omega_3 - 3\omega_4 \omega_1 + 2\omega_4 \omega_1 \omega_3 \\
C_5 &= 3v_1^2 \omega_1^2 \omega_2 - 2c_s^4 \omega_1^2 \omega_2 - 14c_s^4 \omega_2^2 - 18v_1^2 c_s^2 \omega_2^2 - 4v_1^4 \omega_2^2 - 2c_s^2 \omega_1^2 + 2c_s^2 \omega_1^2 \omega_2 - 3v_1^4 \omega_1^2 \omega_2 - 15v_1^2 c_s^2 \omega_1^2 \omega_2 - c_s^4 \omega_1^2 \omega_2^2 - 2v_1^2 \omega_1^2 + 14c_s^4 \omega_1 \omega_2^2 + 6v_1^2 c_s^2 \omega_1 \omega_2 - 3v_1^2 \omega_1 \omega_2^2 + 4v_1^2 \omega_2^2 + 2v_1^4 \omega_1 \omega_2 + 2c_s^2 \omega_2^2 + 12v_1^2 c_s^2 \omega_1^2 + 3v_1^4 \omega_1^2 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 + 2v_1^4 \omega_1^2 + 2c_s^4 \omega_1^2 + 15v_1^2 c_s^2 \omega_1 \omega_2^2 - 2v_1^2 \omega_1 \omega_2 \\
C_6 &= -5\omega_1 \omega_2^2 - 11v_1^2 \omega_1^2 \omega_2 + 8c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 - 2\omega_1 \omega_2 + 8v_1^2 \omega_1^2 + 5\omega_1^2 \omega_2 + 11v_1^2 \omega_1 \omega_2^2 - 14v_1^2 \omega_2^2 + 6\omega_2^2 + 2c_s^2 \omega_1 \omega_2 - 10c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 + 6v_1^2 \omega_1 \omega_2 \\
C_7 &= v_2^2 \omega_1^2 + 6c_s^2 \omega_1^2 - 2\omega_1^2 + 4\omega_1 \omega_2 - 2v_2^2 \omega_1 \omega_2 + v_1^2 \omega_1^2 + v_1^2 \omega_2^2 - 2\omega_2^2 - 12c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_2^2 + v_2^2 \omega_2^2 - 2v_1^2 \omega_1 \omega_2 \\
C_8 &= -4\omega_4 \omega_1^2 \omega_3 - 9c_s^2 \omega_1^2 \omega_2^2 \omega_3 + \omega_4 \omega_1^2 \omega_2 \omega_3 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 - \omega_4 \omega_1 \omega_2^2 \omega_3 + 4\omega_4 \omega_1 \omega_2^2 + 6v_1^2 \omega_4 \omega_1^2 \omega_3 + 3\omega_4 c_s^2 \omega_1 \omega_2^2 \omega_3 - 4\omega_4 v_2^2 \omega_1 \omega_2^2 + 6v_2^2 \omega_1 \omega_2^2 \omega_3 - 4\omega_4 c_s^2 \omega_2^2 \omega_3 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 2\omega_4 v_2^2 \omega_1^2 \omega_3 - 3\omega_4 c_s^2 \omega_1^2 \omega_2 \omega_3 - 6\omega_1 \omega_2^2 \omega_3 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2 - 4\omega_4 c_s^2 \omega_1 \omega_2 \omega_3 - 3v_2^2 \omega_1^2 \omega_2^2 \omega_3 - 2\omega_4 v_2^2 \omega_2^2 \omega_3 + 3\omega_4 v_2^2 \omega_1^2 \omega_2^2 + 8\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 3\omega_1^2 \omega_2^2 \omega_3 - 12v_1^2 \omega_4 \omega_1 \omega_2 \omega_3 + 18c_s^2 \omega_1 \omega_2^2 \omega_3 - 2\omega_4 v_2^2 \omega_1^2 \omega_2 - \omega_4 v_2^2 \omega_1^2 \omega_2 \omega_3 - 3\omega_4 \omega_1^2 \omega_2^2 + 4\omega_4 \omega_1 \omega_2 \omega_3 + \omega_4 v_2^2 \omega_1 \omega_2^2 \omega_3 + 6v_1^2 \omega_4 \omega_2^2 \omega_3 \\
C_9 &= -4v_1^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_4 v_2^2 \omega_1 \omega_2 \omega_3 - 4\omega_4 \omega_1^2 \omega_3 - 9c_s^2 \omega_1^2 \omega_2^2 \omega_3 + \omega_4 \omega_1^2 \omega_2 \omega_3 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 - \omega_4 \omega_1 \omega_2^2 \omega_3 + 4\omega_4 \omega_1 \omega_2^2 + 2v_1^2 \omega_4 \omega_1^2 \omega_3 + 6v_1^2 \omega_1 \omega_2^2 \omega_3 + 3\omega_4 c_s^2 \omega_1 \omega_2^2 \omega_3 + v_1^2 \omega_4 \omega_1 \omega_2^2 \omega_3 - 4\omega_4 c_s^2 \omega_2^2 \omega_3 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 6\omega_4 v_2^2 \omega_1^2 \omega_3 - 3\omega_4 c_s^2 \omega_1^2 \omega_2 \omega_3 - 6\omega_1 \omega_2^2 \omega_3 - v_1^2 \omega_4 \omega_1^2 \omega_2 \omega_3 - 3v_1^2 \omega_1^2 \omega_2^2 \omega_3 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 - 2v_1^2 \omega_4 \omega_1^2 \omega_2 + 2\omega_4 \omega_1^2 \omega_2 - 4\omega_4 c_s^2 \omega_1 \omega_2 \omega_3 + 6\omega_4 v_2^2 \omega_2^2 \omega_3 + 8\omega_4 c_s^2 \omega_1^2 \omega_3 + 3\omega_1^2 \omega_2^2 \omega_3 + 18c_s^2 \omega_1 \omega_2^2 \omega_3 - 3\omega_4 \omega_1^2 \omega_2^2 + 4\omega_4 \omega_1 \omega_2 \omega_3 + 3v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 2v_1^2 \omega_4 \omega_2^2 \omega_3 \\
C_{10} &= -18c_s^2 v_2^2 \omega_2^2 - 3v_2^2 \omega_1 \omega_2^2 - 2c_s^4 \omega_1^2 \omega_2 - 14c_s^4 \omega_2^2 + 2v_2^4 \omega_1 \omega_2 - 15c_s^2 v_2^2 \omega_1^2 \omega_2 - 2v_2^2 \omega_1^2 - 2c_s^2 \omega_1^2 + 2c_s^2 \omega_1^2 \omega_2 + 3v_2^4 \omega_1 \omega_2^2 - 2v_2^2 \omega_1 \omega_2 - c_s^4 \omega_1^2 \omega_2^2 - 4v_2^4 \omega_2^2 + 3v_2^2 \omega_1^2 \omega_2 + 14c_s^4 \omega_1 \omega_2^2 + 2v_2^4 \omega_1^2 + 15c_s^2 v_2^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 - 3v_2^4 \omega_1^2 \omega_2 + 4v_2^2 \omega_2^2 + 6c_s^2 v_2^2 \omega_1 \omega_2 + 12c_s^2 v_2^2 \omega_1^2 + 2c_s^4 \omega_1^2 \\
C_{11} &= -5\omega_1 \omega_2^2 + 11v_2^2 \omega_1 \omega_2^2 + 8v_2^2 \omega_1^2 + 8c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 - 2\omega_1 \omega_2 + 6v_2^2 \omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 11v_2^2 \omega_1^2 \omega_2 + 6\omega_2^2 + 2c_s^2 \omega_1 \omega_2 - 10c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 14v_2^2 \omega_2^2 \\
C_{12} &= 2v_3^2 \omega_2^2 - 3\omega_1 \omega_2^2 - 3v_1^2 \omega_1^2 \omega_2 + 12c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_1^2 v_3^2 + 2\omega_1 \omega_2 + 2v_2^2 \omega_1^2 + 3\omega_1^2 \omega_2 + 3v_1^2 \omega_1 \omega_2^2 - 4v_1^2 \omega_2^2 + 2\omega_2^2 - 6c_s^2 \omega_1 \omega_2 - 6c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 4\omega_1 v_3^2 \omega_2 + 2v_1^2 \omega_1 \omega_2 \\
C_{13} &= 8\omega_4 v_3^2 \omega_2^2 \omega_3 - 8\omega_4 \omega_1^2 \omega_3 + 6\omega_4 \omega_1^2 v_3^2 \omega_2^2 + 18c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 8\omega_4 \omega_1^2 \omega_2 \omega_3 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 8\omega_4 \omega_1 \omega_2^2 \omega_3 + 8\omega_4 \omega_1 \omega_2^2 + 12v_2^2 \omega_4 \omega_1^2 \omega_3 - 3\omega_4 \omega_1^2 v_3^2 \omega_2^2 \omega_3 + 12\omega_4 c_s^2 \omega_1 \omega_2^2 \omega_3 + 18v_1^2 \omega_4 \omega_1 \omega_2^2 \omega_3 - 12\omega_1 v_3^2 \omega_2^2 \omega_3 + 16\omega_4 c_s^2 \omega_2^2 \omega_3 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 \omega_3 + 12\omega_1 \omega_2^2 \omega_3 - 4\omega_4 \omega_1^2 v_3^2 \omega_2 - 18v_1^2 \omega_4 \omega_1^2 \omega_2 \omega_3 - 4\omega_4 \omega_1^2 v_3^2 \omega_2 - 11\omega_4 c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 + 4\omega_4 c_s^2 \omega_1 \omega_2 \omega_3 - 2\omega_4 \omega_1^2 v_3^2 \omega_2 \omega_3 + 16\omega_4 c_s^2 \omega_1^2 \omega_3 - 6\omega_1^2 \omega_2^2 \omega_3 + 12v_1^2 \omega_4 \omega_1 \omega_2 \omega_3 - 36c_s^2 \omega_1 \omega_2^2 \omega_3 - 8\omega_4 \omega_1 v_3^2 \omega_2^2 + 6\omega_1^2 v_3^2 \omega_2^2 \omega_3 - 6\omega_4 \omega_1^2 \omega_2^2 - 4\omega_4 \omega_1 \omega_2 \omega_3 + 2\omega_4 \omega_1 v_3^2 \omega_2^2 \omega_3 + 4\omega_4 \omega_1^2 v_3^2 \omega_3 - 24v_1^2 \omega_4 \omega_2^2 \omega_3 + 3\omega_4 \omega_1^2 \omega_2^2 \omega_3 \\
C_{14} &= -2\omega_1 \omega_2^2 - 2v_1^2 \omega_1^2 \omega_2 - 4\omega_1^2 \omega_3 - 4c_s^2 \omega_2^2 \omega_3 - 4c_s^2 \omega_1 \omega_2 \omega_3 + 6v_3^2 \omega_2^2 \omega_3 + v_1^2 \omega_1 \omega_2^2 \omega_3 - 6c_s^2 \omega_1^2 \omega_2 + \omega_1^2 \omega_2 \omega_3 - 2v_1^2 \omega_2^2 \omega_3 - v_1^2 \omega_1^2 \omega_2 \omega_3 - \omega_1 \omega_2^2 \omega_3 + 2\omega_1^2 \omega_2 + 2v_1^2 \omega_1 \omega_2^2 + 4\omega_1 \omega_2 \omega_3 + 6\omega_1^2 v_3^2 \omega_3 + 2v_1^2 \omega_1^2 \omega_3 - 12\omega_1 v_3^2 \omega_2 \omega_3 + 3c_s^2 \omega_1 \omega_2^2 \omega_3 + 6c_s^2 \omega_1 \omega_2^2 - 3c_s^2 \omega_1^2 \omega_2 \omega_3 + 8c_s^2 \omega_1^2 \omega_3 \\
C_{15} &= 2v_3^2 \omega_2^2 - 3\omega_1 \omega_2^2 + 3v_2^2 \omega_1 \omega_2^2 + 2v_2^2 \omega_1^2 + 12c_s^2 \omega_1^2 - 4\omega_1^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_1^2 v_3^2 + 2\omega_1 \omega_2 + 2v_2^2 \omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 3v_2^2 \omega_1^2 \omega_2 + 2\omega_2^2 - 6c_s^2 \omega_1 \omega_2 - 6c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 4v_2^2 \omega_2^2 - 4\omega_1 v_3^2 \omega_2 \\
C_{16} &= 12\omega_4 v_2^2 \omega_1 \omega_2 \omega_3 + 8\omega_4 v_3^2 \omega_2^2 \omega_3 - 8\omega_4 \omega_1^2 \omega_3 + 6\omega_4 \omega_1^2 v_3^2 \omega_2^2 + 18c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 8\omega_4 \omega_1^2 \omega_2 \omega_3 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 8\omega_4 \omega_1 \omega_2^2 \omega_3 + 8\omega_4 \omega_1 \omega_2^2 - 3\omega_4 \omega_1^2 v_3^2 \omega_2^2 \omega_3 + 12\omega_4 c_s^2 \omega_1 \omega_2^2 \omega_3 - 12\omega_1 v_3^2 \omega_2^2 \omega_3 + 16\omega_4 c_s^2 \omega_2^2 \omega_3 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 12\omega_4 v_2^2 \omega_1^2 \omega_3 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 \omega_3 + 12\omega_1 \omega_2^2 \omega_3 - 4\omega_4 \omega_1^2 v_3^2 \omega_2 - 11\omega_4 c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 + 4\omega_4 c_s^2 \omega_1 \omega_2 \omega_3 - 2\omega_4 \omega_1^2 v_3^2 \omega_2 \omega_3 - 24\omega_4 v_2^2 \omega_2^2 \omega_3 + 16\omega_4 c_s^2 \omega_1^2 \omega_3 - 6\omega_1^2 \omega_2^2 \omega_3 - 36c_s^2 \omega_1 \omega_2^2 \omega_3 - 8\omega_4 \omega_1 v_3^2 \omega_2^2 + 6\omega_1^2 v_3^2 \omega_2^2 \omega_3 - 18\omega_4 v_2^2 \omega_1^2 \omega_2 \omega_3 - 6\omega_4 \omega_1^2 \omega_2^2 - 4\omega_4 \omega_1 \omega_2 \omega_3 + 2\omega_4 \omega_1 v_3^2 \omega_2^2 \omega_3 + 4\omega_4 \omega_1^2 v_3^2 \omega_3 + 18\omega_4 v_2^2 \omega_1 \omega_2^2 \omega_3 + 3\omega_4 \omega_1^2 \omega_2^2 \omega_3 \\
C_{17} &= -2\omega_1 \omega_2^2 + 2v_2^2 \omega_1 \omega_2^2 - 4\omega_1^2 \omega_3 - 4c_s^2 \omega_2^2 \omega_3 - 4c_s^2 \omega_1 \omega_2 \omega_3 + 2v_2^2 \omega_1^2 \omega_3 + 6v_3^2 \omega_2^2 \omega_3 - v_2^2 \omega_1^2 \omega_2 \omega_3 - 6c_s^2 \omega_1^2 \omega_2 + \omega_1^2 \omega_2 \omega_3 + v_2^2 \omega_1 \omega_2^2 \omega_3 - \omega_1 \omega_2^2 \omega_3 + 2\omega_1^2 \omega_2 - 2v_2^2 \omega_1^2 \omega_2 + 4\omega_1 \omega_2 \omega_3 + 6\omega_1^2 v_3^2 \omega_3 - 12\omega_1 v_3^2 \omega_2 \omega_3 + 3c_s^2 \omega_1 \omega_2^2 \omega_3 + 6c_s^2 \omega_1 \omega_2^2 - 3c_s^2 \omega_1^2 \omega_2 \omega_3 - 2v_2^2 \omega_2^2 \omega_3 + 8c_s^2 \omega_1^2 \omega_3 \\
C_{18} &= -16v_3^2 \omega_2^2 - 4c_s^4 \omega_1^2 \omega_2 + 8c_s^4 \omega_2^2 - 24\omega_1 v_3^4 \omega_2^2 - c_s^2 \omega_1^2 \omega_2^2 - 96c_s^2 \omega_1 v_3^2 \omega_2^2 + 12\omega_1^2 v_3^2 \omega_2 + 48c_s^2 \omega_1 v_3^2 \omega_2 - 7\omega_1^2 v_3^2 \omega_2^2 - 4c_s^2 \omega_1^2 + 16\omega_1 v_3^4 \omega_2 + 4c_s^2 \omega_1^2 \omega_2 - 4\omega_1^2 v_3^2 + c_s^4 \omega_1^2 \omega_2^2 + 24\omega_1 v_3^2 \omega_2^2 - 8c_s^4 \omega_1 \omega_2^2 - 48c_s^2 \omega_1^2 v_3^2 \omega_2 - 12\omega_1^2 v_3^4 \omega_2 + 16v_3^4 \omega_2^2 + 4\omega_1^2 v_3^4 + 24c_s^2 \omega_1^2 v_3^2 - 8c_s^2 \omega_2^2 + 8c_s^2 \omega_1 \omega_2^2 + 72c_s^2 v_3^2 \omega_2^2 + 7\omega_1^2 v_3^4 \omega_2^2 - 16\omega_1 v_3^4 \omega_2 + 4c_s^4 \omega_1^2 + 24c_s^2 \omega_1^2 v_3^2 \omega_2^2 \\
C_{19} &= 28v_3^2 \omega_2^2 + 16\omega_1 \omega_2^2 + 5c_s^2 \omega_1^2 \omega_2^2 - 20\omega_1^2 v_3^2 \omega_2 + 11\omega_1^2 v_3^2 \omega_2^2 + 8c_s^2 \omega_1^2 - 4\omega_1^2 - 12c_s^2 \omega_1^2 \omega_2 + 8\omega_1^2 v_3^2 - 8\omega_1 \omega_2 + 8\omega_1^2 \omega_2 - 40\omega_1 v_3^2 \omega_2^2 - 12\omega_2^2 + 8c_s^2 \omega_1 \omega_2 + 20c_s^2 \omega_2^2 - 24c_s^2 \omega_1 \omega_2^2 + 24\omega_1 v_3^2 \omega_2 - 4\omega_1^2 \omega_2^2 \\
C_{20} &= -6v_1^2 \omega_1 - 2c_s^2 \omega_1 + 12v_4^4 \omega_2 + 48v_1^2 c_s^2 \omega_2 + 4c_s^4 \omega_2 + 2c_s^4 \omega_1 - 36v_1^2 c_s^2 \omega_1 \omega_2 + 6v_1^4 \omega_1 + 24v_1^2 c_s^2 \omega_1 - 9v_1^4 \omega_1 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 4c_s^2 \omega_2 - 12v_1^2 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 9v_1^2 \omega_1 \omega_2 \\
C_{21} &= -12v_1^4 \omega_4^2 \omega_1^2 \omega_3^2 + \omega_4^2 c_s^2 \omega_1^3 \omega_3^2 - 36v_1^2 \omega_4^2 c_s^2 \omega_1^3 \omega_3 + 24\omega_4^2 c_s^4 \omega_1^2 \omega_3^2 + 15v_1^2 \omega_4 \omega_1^3 \omega_3^2 + 12\omega_4^2 c_s^2 \omega_1^2 \omega_3 - 15v_1^4 \omega_4^2 \omega_1^3 \omega_3 - 12\omega_4 c_s^2 \omega_1 \omega_3^2 + 36v_1^2 \omega_4 \omega_1^2 \omega_3 - 12v_1^2 \omega_4^2 c_s^2 \omega_1^2 \omega_3^2 + 3\omega_4^2 c_s^4 \omega_1^3 \omega_3 - 36v_1^2 \omega_4 \omega_1^2 \omega_3^2 + 36v_1^2 \omega_4 c_s^2 \omega_1^2 \omega_3 + 72v_1^2 \omega_4^2 c_s^2 \omega_1^2 \omega_3 - 3\omega_4^2 c_s^4 \omega_1^3 \omega_3 + 24\omega_4^2 c_s^4 \omega_3 - 8\omega_4^2 c_s^2 \omega_1^2 \omega_3^2 + 3v_1^4 \omega_4^2 \omega_1^3 \omega_3^2 + 6v_1^2 \omega_4^2 c_s^2 \omega_1^3 \omega_3^2 - 12\omega_4^2 c_s^4 \omega_1^2 \omega_3^2 + 12\omega_4 c_s^4 \omega_1 \omega_3^2 - 18v_1^2 \omega_4 \omega_1^2 \omega_3 + 36v_1^2 \omega_4^2 \omega_1^2 \omega_3 - 3\omega_4^2 c_s^2 \omega_1^2 \omega_3 + 12\omega_4^2 c_s^4 \omega_1 \omega_3 - 54v_1^2 \omega_4^2 c_s^2 \omega_1^2 + 54v_1^2 \omega_4 c_s^2 \omega_1^3 \omega_3 + 12v_1^2 \omega_4^2 \omega_1^2 \omega_3^2 - 18v_1^4 \omega_1^2 \omega_3^2 - 12\omega_4 c_s^4 \omega_1^2 \omega_3^2 - 9v_1^2 \omega_1^3 \omega_3^2 - 3\omega_4 c_s^2 \omega_1^3 \omega_3^2 - 18v_1^4 \omega_4^2 \omega_1^2 - 15v_1^4 \omega_4 \omega_1^3 \omega_3^2 + 72v_1^2 \omega_4 c_s^2 \omega_1^2 \omega_3^2 +
\end{aligned}$$

$$\begin{aligned}
& 72\omega_4 c_s^2 \omega_1^2 \omega_3^2 \omega_2^2 + 2\omega_4 \omega_1^3 \omega_2^2 \omega_3^2 + 16\omega_2^4 c_s^4 \omega_1 \omega_3^2 \omega_2 - 48\omega_2^2 v_2^2 \omega_1 \omega_2^2 \omega_3^2 - 144\omega_4^2 v_2^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - 56\omega_4^2 c_s^4 \omega_1^2 \omega_2 \omega_3^2 + 48\omega_4^2 c_s^2 v_2^2 \omega_1^2 \omega_2^2 \omega_3 - 108\omega_1^4 v_3^4 \omega_2^2 \omega_3^2 - \\
& 6\omega_4^2 c_s^4 \omega_1^3 \omega_2^2 \omega_3^2 + 54\omega_4^2 \omega_1^3 \omega_2^4 \omega_3^2 - 48\omega_4^2 v_3^2 \omega_2^2 \omega_3^2 + 24\omega_4^2 \omega_1 v_3^2 \omega_2^2 \omega_3^2 + 108\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - 72\omega_4 \omega_1 v_3^4 \omega_2^2 \omega_3^2 - 40\omega_4^2 c_s^2 \omega_1^2 \omega_2^2 \omega_3^2 + 72\omega_2^2 \omega_1^2 v_3^2 \omega_2^2 - \\
& 492\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - 24\omega_4^2 \omega_1^3 v_3^4 \omega_2 \omega_3 + 96\omega_4^2 \omega_1 v_3^2 \omega_2^2 \omega_3^2 + 54\omega_1^3 v_3^4 \omega_2^2 \omega_3^2 - 108\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - 12\omega_4^2 c_s^2 \omega_1^2 \omega_2^2 \omega_3^2 - 108\omega_4^2 \omega_1^3 v_3^4 \omega_2 \omega_3^2 - \\
& 432\omega_4^2 v_3^2 \omega_2^2 \omega_3^2 \omega_3^2 - 108\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 162\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 168\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 8\omega_4^2 c_s^2 \omega_2^2 \omega_3^2 + 24\omega_4^2 c_s^2 v_2^2 \omega_1^2 \omega_2^2 \omega_3^2 - 172\omega_4^2 c_s^4 \omega_1 \omega_2^2 \omega_3^2 - \\
& 24\omega_4^2 v_2^2 \omega_1^3 \omega_3^2 - 108\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 16\omega_4^2 \omega_1 \omega_2^2 \omega_3^2 + 24\omega_4^2 c_s^2 v_2^2 \omega_2^2 \omega_3^2 - 6\omega_4^2 v_2^2 \omega_1^2 \omega_2^2 \omega_3^2 + 96\omega_4^2 \omega_1 v_3^4 \omega_2^2 \omega_3^2 + 18\omega_4^2 c_s^4 \omega_1^3 \omega_2^2 \omega_3^2 + 36\omega_4^2 c_s^2 \omega_1^2 \omega_2^2 \omega_3^2 + \\
& 162\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 72\omega_4^2 c_s^4 \omega_1 \omega_2^2 \omega_3^2 - 144\omega_4^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 8\omega_4^2 \omega_1^3 \omega_2^2 \omega_3^2 + 174\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - 16\omega_4^2 c_s^2 \omega_1^2 \omega_2^2 \omega_3^2 + 108\omega_4^2 v_3^2 \omega_2^2 \omega_3^2 - 297\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - \\
& 540\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 72\omega_4 \omega_1 v_3^2 \omega_2^2 \omega_3^2 - 8\omega_4^2 \omega_1^2 \omega_2^2 \omega_3^2 - 24\omega_4^2 \omega_1 v_3^4 \omega_2^2 \omega_3^2 + 48\omega_4^2 c_s^2 v_2^2 \omega_1^2 \omega_2^2 \omega_3^2 + 192\omega_4^2 v_3^4 \omega_2^2 \omega_3^2 - 2\omega_4^2 c_s^4 \omega_1^3 \omega_2^2 \omega_3^2 - \\
& 297\omega_4^2 c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 + 24\omega_4^2 c_s^2 v_2^2 \omega_1^2 \omega_2^2 \omega_3^2 - 48\omega_4^2 v_2^2 \omega_1^2 \omega_2^2 \omega_3^2 - 288\omega_4^2 v_2^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3^2 - 108\omega_4^2 c_s^2 v_3^2 \omega_2^2 \omega_3^2 + 144\omega_4^2 v_2^2 \omega_1^3 v_3^2 \omega_2^2 \omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{58} = & -18c_s^2 \omega_1^2 \omega_2 - 66\omega_1 v_3^2 \omega_2^2 \omega_3 - 27c_s^2 \omega_1^2 \omega_3^2 - 5\omega_1^2 \omega_2^2 \omega_3 + 81c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 84v_3^2 \omega_2^2 \omega_3 + 5v_2^2 \omega_1^2 \omega_2^2 \omega_3 - 12\omega_1^2 v_3^2 \omega_2 \omega_3 + 48\omega_1^3 v_3^2 \omega_3 - \\
& 18c_s^2 \omega_2^2 \omega_3^2 + 3\omega_1 \omega_2^2 \omega_3 + 12v_3^2 \omega_1 \omega_2^2 \omega_3 - 12\omega_1 \omega_2^2 \omega_3 + 27v_2^2 \omega_1 \omega_2^2 \omega_3 + 6v_2^2 \omega_2^2 \omega_3 - 66\omega_1^3 v_3^2 \omega_2 \omega_3 - 15c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 6\omega_1^2 \omega_2 \omega_3 - 120\omega_1 v_3^2 \omega_2^2 \omega_3 - \\
& 108c_s^2 \omega_1^2 \omega_2 \omega_3 + 6v_2^2 \omega_1 \omega_2^2 \omega_3 + 42\omega_1 \omega_2^2 \omega_3 + 27c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 12v_2^2 \omega_1 \omega_2^2 \omega_3 - 36\omega_1^3 \omega_3 - 12c_s^2 \omega_1^2 \omega_3^2 + 27c_s^2 \omega_1 \omega_2^2 \omega_3 + 9v_2^2 \omega_1^2 \omega_2^2 + 84c_s^2 \omega_1^3 \omega_3 - 12\omega_2^2 \omega_3 - \\
& 9\omega_1^3 \omega_2^2 - 24v_2^2 \omega_2^2 \omega_3 - 9v_2^2 \omega_1^2 \omega_2^2 \omega_3 + 15c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 51\omega_1^2 \omega_2^2 \omega_3 - 54c_s^2 \omega_1 \omega_2^2 \omega_3 + 132\omega_1^2 v_3^2 \omega_2^2 \omega_3 - 6v_2^2 \omega_1^2 \omega_2 - 9v_2^2 \omega_1^2 \omega_2^2 + 6\omega_1^3 \omega_2 + 9\omega_1^2 \omega_2^2 + \\
& 36c_s^2 \omega_1 \omega_2^2 + 5\omega_1^2 \omega_2^2 \omega_3 - 18c_s^2 \omega_1^2 \omega_2 \omega_3 + 48\omega_1^2 \omega_2 \omega_3 + 6\omega_1^2 \omega_2^2 - 5v_2^2 \omega_1^2 \omega_2^2 \omega_3 - 6v_2^2 \omega_1^2 \omega_2^2 - 18v_2^2 \omega_1^2 \omega_2 \omega_3
\end{aligned}$$

$$\begin{aligned}
C_{59} = & -8c_s^2 \omega_1^2 \omega_2 + 328\omega_1 v_3^2 \omega_2^2 \omega_3 + 8\omega_1^2 \omega_2^2 \omega_3 - 84\omega_1^3 v_3^4 \omega_2 \omega_3 + 152c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 372c_s^4 \omega_1 \omega_2^2 \omega_3 + 168\omega_1 v_3^4 \omega_2^2 \omega_3 - 160v_3^2 \omega_2^2 \omega_3 + 8c_s^2 \omega_1 v_3^2 \omega_2^2 - \\
& 104\omega_1^2 v_3^2 \omega_2 \omega_3 - 28\omega_1^3 v_3^2 \omega_3 + 16c_s^2 \omega_2^2 \omega_3^2 - 28\omega_1 \omega_2^2 \omega_3 - 464c_s^4 \omega_1^3 v_3^2 \omega_2 \omega_3 + 82c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 216c_s^4 \omega_2^2 \omega_3 + 8c_s^2 \omega_1^3 v_3^2 \omega_2^2 \omega_3 + 656c_s^2 \omega_1 v_3^2 \omega_2^2 \omega_3 + \\
& 440c_s^2 \omega_1^2 v_3^2 \omega_2 \omega_3 - 300\omega_1^2 v_3^2 \omega_2^2 \omega_3 + 24c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 72c_s^4 \omega_1 \omega_2^2 \omega_3 + 94\omega_1^2 v_3^2 \omega_2 \omega_3 - 3\omega_1^2 \omega_2^2 \omega_3 - 156c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 8\omega_1^2 \omega_2 \omega_3 - 176\omega_1 v_3^2 \omega_2^2 \omega_3 + \\
& 122c_s^2 \omega_1^2 \omega_2 \omega_3 + 144v_3^4 \omega_2^2 \omega_3 + 72c_s^4 \omega_1^2 \omega_2^2 \omega_3 - 1472c_s^2 \omega_1 v_3^2 \omega_2^2 \omega_3 + 96\omega_1^2 v_3^4 \omega_2 \omega_3 - 15c_s^4 \omega_1^3 \omega_2^2 \omega_3 - 48c_s^4 \omega_1^2 \omega_2^2 + 8\omega_1 \omega_2^2 \omega_3 + 4\omega_1^3 \omega_3 - \\
& 184c_s^2 \omega_2^2 \omega_3 - 264\omega_1^2 v_3^2 \omega_2^2 \omega_3 - 120c_s^2 \omega_1^2 \omega_2^2 \omega_3 + 24\omega_1^3 v_3^2 \omega_3 - 102c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 + 160c_s^2 \omega_1^2 v_3^2 \omega_3 + 320c_s^2 \omega_1 \omega_2^2 \omega_3 - 196\omega_1^2 v_3^2 \omega_2^2 \omega_3 - 52c_s^2 \omega_1^3 \omega_3 + \\
& 24c_s^4 \omega_1 \omega_2^2 \omega_3 + 16\omega_2^2 \omega_3 - 1088c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 - 98\omega_1^3 v_3^2 \omega_2^2 \omega_3 + 760c_s^2 v_3^2 \omega_2^2 \omega_3 - 27\omega_1^3 v_3^4 \omega_2^2 \omega_3 - 78c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 16\omega_1^2 \omega_2^2 \omega_3 - 80c_s^2 \omega_1 \omega_2^2 \omega_3 + \\
& 280\omega_1^2 v_3^2 \omega_2^2 \omega_3 + 404c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 - 156c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 180\omega_1^2 v_3^2 \omega_2^2 \omega_3 + 164c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 18c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 8c_s^2 \omega_1 \omega_2^2 + 72c_s^4 \omega_1 \omega_3 + 16\omega_1^2 \omega_2^2 \omega_3 - \\
& 80c_s^2 \omega_1^2 \omega_2 \omega_3 - 10\omega_1^2 \omega_2 \omega_3 + 90\omega_1^3 v_3^4 \omega_2^2 \omega_3 + 30\omega_1^3 v_3^2 \omega_2^2 \omega_3 + 808c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 - 16c_s^2 \omega_1^2 v_3^2 \omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{60} = & -8c_s^2 \omega_1^3 \omega_2 + 552\omega_1 v_3^2 \omega_2^2 \omega_3 + 8\omega_1^2 \omega_2^2 \omega_3 - 312\omega_1^3 v_3^4 \omega_2 \omega_3 + 24c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 68c_s^4 \omega_1 \omega_2^2 \omega_3 + 552\omega_1 v_3^4 \omega_2^2 \omega_3 - 288v_3^2 \omega_2^2 \omega_3 + 24c_s^2 \omega_1 v_3^2 \omega_2^2 - \\
& 168\omega_1^2 v_3^2 \omega_2 \omega_3 - 60\omega_1^3 v_3^2 \omega_3 + 16c_s^2 \omega_2^2 \omega_3^2 - 28\omega_1 \omega_2^2 \omega_3 - 360c_s^2 \omega_1^3 v_3^2 \omega_2 \omega_3 + 14c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 40c_s^4 \omega_2^2 \omega_3 + 24c_s^2 \omega_1^3 v_3^2 \omega_2^2 + 336c_s^2 \omega_1 v_3^2 \omega_2^2 \omega_3 + \\
& 264c_s^2 \omega_1^2 v_3^2 \omega_2 \omega_3 - 1068\omega_1 v_3^4 \omega_2^2 \omega_3 + 8c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 8c_s^4 \omega_1 \omega_2^2 \omega_3 + 174\omega_1^3 v_3^2 \omega_2 \omega_3 - 3\omega_1^2 \omega_2^2 \omega_3 - 44c_s^2 \omega_2^2 \omega_3^2 + 8\omega_1^2 \omega_2 \omega_3 - 240\omega_1 v_3^2 \omega_2^2 \omega_3 + \\
& 42c_s^2 \omega_1^2 \omega_2 \omega_3 + 528v_3^4 \omega_2^2 \omega_3 + 8c_s^4 \omega_1^2 \omega_2^2 \omega_3 - 1008c_s^2 \omega_1 v_3^2 \omega_2^2 \omega_3 + 336\omega_1^2 v_3^4 \omega_2 \omega_3 - 3c_s^4 \omega_1^3 \omega_2^2 \omega_3 - 16c_s^4 \omega_1^2 \omega_2^2 + 8\omega_1 \omega_2^2 \omega_3 + 4\omega_1^3 \omega_3 - 56c_s^2 \omega_2^2 \omega_3 - \\
& 888\omega_1^2 v_3^4 \omega_2^2 \omega_3 - 8c_s^4 \omega_2^2 \omega_3^2 + 96\omega_1^3 v_3^4 \omega_3 - 54c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 + 144c_s^2 \omega_1^2 v_3^2 \omega_3 + 96c_s^2 \omega_1 \omega_2^2 \omega_3 - 308\omega_1^2 v_3^2 \omega_2^2 \omega_3 - 20c_s^2 \omega_2^2 \omega_3 + 8c_s^4 \omega_1 \omega_2^2 + \\
& 16\omega_2^2 \omega_3 - 576c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 - 154\omega_1^3 v_3^2 \omega_2^2 \omega_3 + 552c_s^2 v_3^2 \omega_2^2 \omega_3 - 87\omega_1^2 v_3^4 \omega_2^2 \omega_3 - 22c_s^2 \omega_1^2 \omega_2^2 \omega_3 - 16\omega_1^2 \omega_2^2 \omega_3 - 16c_s^2 \omega_1 \omega_2^2 \omega_3 + 408\omega_1^2 v_3^2 \omega_2^2 \omega_3 + \\
& 252c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 - 32c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 620\omega_1^2 v_3^4 \omega_2^2 \omega_3 + 28c_s^4 \omega_1^2 \omega_2^2 \omega_3 + 6c_s^2 \omega_1^3 \omega_2^2 \omega_3 - 8c_s^2 \omega_1 \omega_2^2 + 16c_s^4 \omega_1 \omega_3 + 16\omega_1^2 \omega_2^2 \omega_3 - 16c_s^2 \omega_1^2 \omega_2 \omega_3 - \\
& 10\omega_1^2 \omega_2 \omega_3 + 310\omega_1^3 v_3^4 \omega_2^2 \omega_3 + 42\omega_1^2 v_3^2 \omega_2^2 \omega_3 + 504c_s^2 \omega_1^2 v_3^2 \omega_2^2 \omega_3 - 48c_s^2 \omega_1^2 v_3^2 \omega_2^2
\end{aligned}$$

3 Comparison of SRT, MRT, CLBM, and CuLBM

3.1 Conservation of mass: ρ

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + v_1 \frac{\delta_l}{\delta t} \frac{\partial \rho}{\partial x_1} + \rho \frac{\delta_l}{\delta t} \frac{\partial v_1}{\partial x_1} + v_2 \frac{\delta_l}{\delta t} \frac{\partial \rho}{\partial x_2} + \rho \frac{\delta_l}{\delta t} \frac{\partial v_2}{\partial x_2} + v_3 \frac{\delta_l}{\delta t} \frac{\partial \rho}{\partial x_3} + \rho \frac{\delta_l}{\delta t} \frac{\partial v_3}{\partial x_3} + (-1 + v_1^2 + 3c_s^2) \frac{v_1}{12} \frac{\delta_l^3}{\delta t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-1 + 3v_1^2 + c_s^2) \frac{\rho}{12} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{c_s^2 \rho}{6} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \rho}{6} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2}{12} \frac{\delta_l^3}{\delta t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho}{12} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_2}{\partial x_2^3} \\
& - \frac{c_s^2 \rho}{6} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \rho}{6} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{c_s^2 \rho}{6} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho}{6} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3}{12} \frac{\delta_l^3}{\delta t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-1 + c_s^2 + 3v_3^2) \frac{\rho}{12} \frac{\delta_l^3}{\delta t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{D_x^4 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{D_x^4 v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{D_x^3 D_y \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{D_x^3 D_y v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& C_{D_x^3 D_y v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{D_x^2 D_y^2 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{D_x D_y^3 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& C_{D_x D_y^3 v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{D_y^4 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{D_y^4 v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_2^4} + C_{D_x^3 D_z \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_{D_x^3 D_z v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{D_x^2 D_y D_z v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{D_x D_y^2 D_z v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_y^3 D_z \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + \\
& C_{D_y^3 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_x^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{D_x D_y D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{D_x D_y D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_y^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{D_x D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + \\
& C_{D_x D_z^3 v_1}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{D_y D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_2}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& C_{D_z^4 \rho}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{D_z^4 v_3}^{(0)} \frac{\delta_l^4}{\delta t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

coefficient $C_{D_x^4 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^4}$:

$$C_{D_x^4 \rho}^{(0), \text{SRT}} = (-6v_1^2 + c_s^2 \omega - 12c_s^2 \omega v_1^2 + 24c_s^2 v_1^2 + 2c_s^4 - 3\omega v_1^4 + 3\omega v_1^2 - c_s^4 \omega - 2c_s^2 + 6v_1^4) \frac{1}{24\omega}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT1}} = (-6v_1^2 - c_s^4 \omega_9 + 24c_s^2 v_1^2 - 12c_s^2 v_1^2 \omega_9 + 2c_s^4 - 3v_1^4 \omega_9 + c_s^2 \omega_9 - 2c_s^2 + 6v_1^4 + 3v_1^2 \omega_9) \frac{1}{24\omega_9}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT2}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM1}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM2}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CuLBM1}} = (-6v_1^2 - 12\omega_4 c_s^2 v_1^2 + \omega_4 c_s^2 + 24c_s^2 v_1^2 + 2c_s^4 - 3\omega_4 v_1^4 + 3\omega_4 v_1^2 - 2c_s^2 - \omega_4 c_s^4 + 6v_1^4) \frac{1}{24\omega_4}$$

$$C_{D_x^4 \rho}^{(0), \text{CuLBM2}} = (12v_1^4 \omega_2 + 48c_s^2 v_1^2 \omega_2 - 36c_s^2 \omega_1 v_1^2 \omega_2 + 2c_s^4 \omega_1 + 6\omega_1 v_1^4 + 24c_s^2 \omega_1 v_1^2 + 9\omega_1 v_1^2 \omega_2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 - 12v_1^2 \omega_2 - 2c_s^2 \omega_1 - 9\omega_1 v_1^4 \omega_2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 6\omega_1 v_1^2) \frac{1}{72\omega_1 \omega_2}$$

coefficient $C_{D_x^4 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^4}$:

$$C_{D_x^4 v_1}^{(0), \text{SRT}} = (-4 + 10v_1^2 - 3c_s^2 \omega + 2\omega - 5\omega v_1^2 + 6c_s^2) \frac{\rho v_1}{12\omega}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT1}} = (-4 + 10v_1^2 - 3c_s^2 \omega_9 + 6c_s^2 - 5v_1^2 \omega_9 + 2\omega_9) \frac{\rho v_1}{12\omega_9}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT2}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM1}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM2}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CuLBM1}} = (-4 + 10v_1^2 - 3\omega_4 c_s^2 + 2\omega_4 - 5\omega_4 v_1^2 + 6c_s^2) \frac{\rho v_1}{12\omega_4}$$

$$C_{D_x^4 v_1}^{(0), \text{CuLBM2}} = (-15\omega_1 v_1^2 \omega_2 + 6\omega_1 \omega_2 - 4\omega_1 + 20v_1^2 \omega_2 + 6c_s^2 \omega_1 - 8\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 + 10\omega_1 v_1^2) \frac{\rho v_1}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_y \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_y \rho}^{(0), \text{MRT1}} = (-3c_s^2 \omega_9 + 3c_s^2 \omega_{12} + v_1^2 \omega_{12} - v_1^2 \omega_9 + \omega_9 - \omega_{12}) \frac{v_1 v_2}{4\omega_9 \omega_{12}}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{MRT2}} = C_{D_x^3 D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CuLBM2}} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{v_1 v_2}{12\omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_y v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_y v_1}^{(0), \text{MRT}1} = (-c_s^2 \omega_9 + c_s^2 \omega_{12} + 3v_1^2 \omega_{12} - 3v_1^2 \omega_9 + \omega_9 - \omega_{12}) \frac{\rho v_2}{4\omega_9 \omega_{12}}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{MRT}2} = C_{D_x^3 D_y v_1}^{(0), \text{MRT}1}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{CLBM}1} = 0$$

$$C_{D_x^3 D_y v_1}^{(0), \text{CLBM}2} = 0$$

$$C_{D_x^3 D_y v_1}^{(0), \text{CuLBM}1} = 0$$

$$C_{D_x^3 D_y v_1}^{(0), \text{CuLBM}2} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{\rho v_2}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^3 D_y v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} :$$

$$C_{D_x^3 D_y v_2}^{(0), \text{SRT}} = (2 - 2v_1^2 + 3c_s^2 \omega - \omega + \omega v_1^2 - 6c_s^2) \frac{\rho v_1}{12\omega}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{MRT}1} = (v_1^2 \omega_5 \omega_9 \omega_{12} + 3\omega_5 \omega_9 - \omega_5 \omega_{12} - 3v_1^2 \omega_5 \omega_9 + v_1^2 \omega_5 \omega_{12} - \omega_5 \omega_9 \omega_{12} + 3c_s^2 \omega_5 \omega_{12} - 3c_s^2 \omega_5 \omega_9 - 6c_s^2 \omega_9 \omega_{12} + 3c_s^2 \omega_5 \omega_9 \omega_{12}) \frac{\rho v_1}{12\omega_5 \omega_9 \omega_{12}}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{MRT}2} = C_{D_x^3 D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CLBM}1} = (-\omega_9 \omega_{12} + v_1^2 \omega_9 \omega_{12} + 3c_s^2 \omega_9 \omega_{12} - 9c_s^2 \omega_9 + 3c_s^2 \omega_{12} + v_1^2 \omega_{12} - 3v_1^2 \omega_9 + 3\omega_9 - \omega_{12}) \frac{\rho v_1}{12\omega_9 \omega_{12}}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CLBM}2} = C_{D_x^3 D_y v_2}^{(0), \text{CLBM}1}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CuLBM}1} = (-9\omega_4 c_s^2 - \omega_4 \omega_9 + 3\omega_4 + \omega_4 v_1^2 \omega_9 + 3c_s^2 \omega_9 - 3\omega_4 v_1^2 + v_1^2 \omega_9 - \omega_9 + 3\omega_4 c_s^2 \omega_9) \frac{\rho v_1}{12\omega_4 \omega_9}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CuLBM}2} = (2\omega_3 \omega_4 \omega_1 v_1^2 + 6\omega_3 \omega_4 c_s^2 \omega_2 + 18\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 12\omega_3 \omega_4 c_s^2 \omega_1 + 4\omega_3 \omega_4 v_1^2 \omega_2 - 27\omega_4 c_s^2 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 - 18\omega_3 \omega_4 v_2^2 \omega_2 + 6\omega_3 \omega_4 \omega_1 v_1^2 \omega_2 + 9\omega_3 \omega_1 \omega_2 - 9\omega_3 \omega_1 v_1^2 \omega_2 - 9\omega_4 \omega_1 v_1^2 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 18\omega_3 \omega_4 \omega_1 v_2^2) \frac{\rho v_1}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y^2 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^4}{6\omega}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT}1} = (-2 + \omega_5) \frac{c_s^4}{6\omega_5}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT}2} = C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT}1}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CLBM}1} = C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT}1}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CLBM}2} = C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT}1}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CuLBM}1} = (-2 + \omega_1) \frac{c_s^4}{6\omega_1}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CuLBM}2} = (3\omega_1 v_2^2 - 3v_2^2 \omega_2 - 2\omega_1 - 3v_1^2 \omega_2 + 2c_s^2 \omega_1 + 2\omega_2 - 14c_s^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 + 3\omega_1 v_1^2) \frac{c_s^2}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT}1} = (\omega_5 - \omega_{12}) \frac{c_s^2 \rho v_1}{2\omega_5 \omega_{12}}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT}2} = C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT}1}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{\rho v_1}{36 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}} = (\omega_5 - \omega_{15}) \frac{c_s^2 \rho v_2}{2 \omega_5 \omega_{15}}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CuLBM2}} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{\rho v_2}{36 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_y^3 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} :$$

$$C_{D_x D_y^3 \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT1}} = (v_2^2 \omega_{15} + \omega_{10} + 3c_s^2 \omega_{15} - 3\omega_{10} c_s^2 - \omega_{10} v_2^2 - \omega_{15}) \frac{v_1 v_2}{4 \omega_{10} \omega_{15}}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT2}} = C_{D_x D_y^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{v_1 v_2}{12 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_y^3 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} :$$

$$C_{D_x D_y^3 v_1}^{(0), \text{SRT}} = (2 + 3c_s^2 \omega + \omega v_2^2 - \omega - 6c_s^2 - 2v_2^2) \frac{\rho v_2}{12 \omega}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT1}} =$$

$$(-\omega_{10} \omega_5 \omega_{15} - \omega_5 \omega_{15} - 3\omega_{10} c_s^2 \omega_5 - 3\omega_{10} \omega_5 v_2^2 + 3\omega_{10} \omega_5 + \omega_5 v_2^2 \omega_{15} - 6\omega_{10} c_s^2 \omega_{15} + \omega_{10} \omega_5 v_2^2 \omega_{15} + 3c_s^2 \omega_5 \omega_{15} + 3\omega_{10} c_s^2 \omega_5 \omega_{15}) \frac{\rho v_2}{12 \omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT2}} = C_{D_x D_y^3 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM1}} = (v_2^2 \omega_{15} + \omega_{10} v_2^2 \omega_{15} + 3\omega_{10} + 3c_s^2 \omega_{15} + 3\omega_{10} c_s^2 \omega_{15} - 9\omega_{10} c_s^2 - \omega_{10} \omega_{15} - 3\omega_{10} v_2^2 - \omega_{15}) \frac{\rho v_2}{12 \omega_{10} \omega_{15}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM2}} = C_{D_x D_y^3 v_1}^{(0), \text{CLBM1}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CuLBM1}} = (-\omega_7 \omega_5 - 9c_s^2 \omega_5 - 3\omega_5 v_2^2 - \omega_7 + \omega_7 \omega_5 v_2^2 + 3\omega_7 c_s^2 \omega_5 + \omega_7 v_2^2 + 3\omega_5 + 3\omega_7 c_s^2) \frac{\rho v_2}{12\omega_7 \omega_5}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CuLBM2}} = (-9\omega_3 \omega_1 v_2^2 \omega_2 + 18\omega_3 \omega_4 \omega_1 v_1^2 - 9\omega_4 \omega_1 v_2^2 \omega_2 + 6\omega_3 \omega_4 c_s^2 \omega_2 + 18\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 12\omega_3 \omega_4 c_s^2 \omega_1 + 6\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 18\omega_3 \omega_4 v_1^2 \omega_2 - 27\omega_4 c_s^2 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 4\omega_3 \omega_4 v_2^2 \omega_2 + 9\omega_3 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 2\omega_3 \omega_4 \omega_1 v_2^2) \frac{\rho v_2}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x D_y^3 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT1}} = (3v_2^2 \omega_{15} + \omega_{10} + c_s^2 \omega_{15} - \omega_{10} c_s^2 - 3\omega_{10} v_2^2 - \omega_{15}) \frac{\rho v_1}{4\omega_{10} \omega_{15}}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT2}} = C_{D_x D_y^3 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{\rho v_1}{36\omega_1 \omega_2}$$

coefficient $C_{D_y^4 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_2^4}$:

$$C_{D_y^4 \rho}^{(0), \text{SRT}} = (c_s^2 \omega + 6v_2^4 + 3\omega v_2^2 + 2c_s^4 - 3\omega v_2^4 + 24c_s^2 v_2^2 - c_s^4 \omega - 2c_s^2 - 6v_2^2 - 12c_s^2 \omega v_2^2) \frac{1}{24\omega}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT1}} = (6v_2^4 - 3\omega_{10} v_2^4 - \omega_{10} c_s^4 + 2c_s^4 + \omega_{10} c_s^2 + 24c_s^2 v_2^2 - 12\omega_{10} c_s^2 v_2^2 - 2c_s^2 - 6v_2^2 + 3\omega_{10} v_2^2) \frac{1}{24\omega_{10}}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT2}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CLBM1}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CLBM2}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CuLBM1}} = (c_s^2 \omega_5 + 6v_2^4 + 3\omega_5 v_2^2 + 2c_s^4 - 12c_s^2 \omega_5 v_2^2 - c_s^4 \omega_5 + 24c_s^2 v_2^2 - 2c_s^2 - 6v_2^2 - 3\omega_5 v_2^4) \frac{1}{24\omega_5}$$

$$C_{D_y^4 \rho}^{(0), \text{CuLBM2}} = (-6\omega_1 v_2^2 - 9\omega_1 v_2^4 \omega_2 + 2c_s^4 \omega_1 - 12v_2^2 \omega_2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 9\omega_1 v_2^2 \omega_2 + 24c_s^2 \omega_1 v_2^2 - 2c_s^2 \omega_1 + 12v_2^4 \omega_2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 36c_s^2 \omega_1 v_2^2 \omega_2 + 48c_s^2 v_2^2 \omega_2 + 6\omega_1 v_2^4) \frac{1}{72\omega_1 \omega_2}$$

coefficient $C_{D_y^4 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_2^4}$:

$$C_{D_y^4 v_2}^{(0), \text{SRT}} = (-4 - 3c_s^2 \omega - 5\omega v_2^2 + 2\omega + 6c_s^2 + 10v_2^2) \frac{\rho v_2}{12\omega}$$

$$C_{D_y^4 v_2}^{(0), \text{MRT1}} = (-4 + 2\omega_{10} - 3\omega_{10} c_s^2 + 6c_s^2 + 10v_2^2 - 5\omega_{10} v_2^2) \frac{\rho v_2}{12\omega_{10}}$$

$$C_{D_y^4 v_2}^{(0), \text{MRT2}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CLBM1}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CLBM2}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CuLBM1}} = (-4 - 3c_s^2 \omega_5 - 5\omega_5 v_2^2 + 2\omega_5 + 6c_s^2 + 10v_2^2) \frac{\rho v_2}{12\omega_5}$$

$$C_{D_y^4 v_2}^{(0), \text{CuLBM2}} = (10\omega_1 v_2^2 + 20v_2^2 \omega_2 + 6\omega_1 \omega_2 - 4\omega_1 - 15\omega_1 v_2^2 \omega_2 + 6c_s^2 \omega_1 - 8\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2) \frac{\rho v_2}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_z \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{MRT1}} = (\omega_{13} v_1^2 - \omega_{13} + 3\omega_{13} c_s^2 - 3c_s^2 \omega_9 - v_1^2 \omega_9 + \omega_9) \frac{v_1 v_3}{4\omega_{13} \omega_9}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{MRT2}} = C_{D_x^3 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{v_1 v_3}{12\omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_z v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{MRT1}} = (3\omega_{13} v_1^2 - \omega_{13} + \omega_{13} c_s^2 - c_s^2 \omega_9 - 3v_1^2 \omega_9 + \omega_9) \frac{\rho v_3}{4\omega_{13} \omega_9}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{MRT2}} = C_{D_x^3 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{\rho v_3}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z v_3}^{(0), \text{SRT}} = (2 - 2v_1^2 + 3c_s^2 \omega - \omega + \omega v_1^2 - 6c_s^2) \frac{\rho v_1}{12\omega}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT1}} = (\omega_6 \omega_{13} v_1^2 + 3\omega_6 \omega_{13} c_s^2 \omega_9 - 3\omega_6 c_s^2 \omega_9 - \omega_6 \omega_{13} + 3\omega_6 \omega_{13} c_s^2 - 6\omega_{13} c_s^2 \omega_9 + 3\omega_6 \omega_9 - \omega_6 \omega_{13} \omega_9 - 3\omega_6 v_1^2 \omega_9 + \omega_6 \omega_{13} v_1^2 \omega_9) \frac{\rho v_1}{12\omega_6 \omega_{13} \omega_9}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT2}} = C_{D_x^3 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM1}} = (\omega_{13} v_1^2 - \omega_{13} + 3\omega_{13} c_s^2 + \omega_{13} v_1^2 \omega_9 - 9c_s^2 \omega_9 - \omega_{13} \omega_9 + 3\omega_{13} c_s^2 \omega_9 - 3v_1^2 \omega_9 + 3\omega_9) \frac{\rho v_1}{12\omega_{13} \omega_9}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM2}} = C_{D_x^3 D_z v_3}^{(0), \text{CLBM1}}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CuLBM1}} = (-9\omega_4 c_s^2 - \omega_4 \omega_{12} + 3\omega_4 + \omega_4 v_1^2 \omega_{12} - 3\omega_4 v_1^2 + 3c_s^2 \omega_{12} + v_1^2 \omega_{12} + 3\omega_4 c_s^2 \omega_{12} - \omega_{12}) \frac{\rho v_1}{12\omega_4 \omega_{12}}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CuLBM2}} = (2\omega_3 \omega_4 \omega_1 v_1^2 - 18\omega_3 \omega_4 \omega_2 v_3^2 + 6\omega_3 \omega_4 c_s^2 \omega_2 + 18\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 12\omega_3 \omega_4 c_s^2 \omega_1 + 4\omega_3 \omega_4 v_1^2 \omega_2 - 27\omega_4 c_s^2 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 6\omega_3 \omega_4 \omega_1 v_1^2 \omega_2 + 9\omega_3 \omega_1 \omega_2 - 9\omega_3 \omega_1 v_1^2 \omega_2 - 9\omega_4 \omega_1 v_1^2 \omega_2 + 18\omega_3 \omega_4 \omega_1 v_3^2 + 2\omega_3 \omega_4 \omega_2) \frac{\rho v_1}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y D_z v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3}$:

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT1}} = (-\omega_8 + \omega_5) \frac{c_s^2 \rho v_3}{2\omega_8 \omega_5}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CuLBM2}} = (-2\omega_3\omega_4\omega_2v_3^2 - 6\omega_3\omega_4c_s^2\omega_2 + 9\omega_4\omega_1\omega_2 + 6\omega_3\omega_4c_s^2\omega_1 - 27\omega_4c_s^2\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 - 9\omega_4\omega_1\omega_2v_3^2 + 9\omega_3\omega_1\omega_2v_3^2 - 9\omega_3\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_3^2 + 2\omega_3\omega_4\omega_2) \frac{\rho v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3}:$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT1}} = (\omega_6 - \omega_8) \frac{c_s^2 \rho v_2}{2\omega_6\omega_8}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CuLBM2}} = (9\omega_3\omega_1v_2^2\omega_2 - 9\omega_4\omega_1v_2^2\omega_2 - 6\omega_3\omega_4c_s^2\omega_2 + 9\omega_4\omega_1\omega_2 + 6\omega_3\omega_4c_s^2\omega_1 - 27\omega_4c_s^2\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 - 2\omega_3\omega_4v_2^2\omega_2 - 9\omega_3\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 2\omega_3\omega_4\omega_1v_2^2) \frac{\rho v_2}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3}:$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{MRT1}} = (-\omega_8 + \omega_5) \frac{c_s^2 \rho v_3}{2\omega_8\omega_5}$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_y^2 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CuLBM2}} = (-2\omega_3\omega_4\omega_2v_3^2 - 6\omega_3\omega_4c_s^2\omega_2 + 9\omega_4\omega_1\omega_2 + 6\omega_3\omega_4c_s^2\omega_1 - 27\omega_4c_s^2\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 - 9\omega_4\omega_1\omega_2v_3^2 + 9\omega_3\omega_1\omega_2v_3^2 - 9\omega_3\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_3^2 + 2\omega_3\omega_4\omega_2) \frac{\rho v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3}:$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}} = (\omega_7 - \omega_8) \frac{c_s^2 \rho v_1}{2\omega_7\omega_8}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CuLBM2}} = (2\omega_3\omega_4\omega_1 v_1^2 - 6\omega_3\omega_4 c_s^2 \omega_2 + 9\omega_4\omega_1 \omega_2 + 6\omega_3\omega_4 c_s^2 \omega_1 - 2\omega_3\omega_4 v_1^2 \omega_2 - 27\omega_4 c_s^2 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 2\omega_3\omega_4 \omega_1 - 9\omega_3\omega_1 \omega_2 + 9\omega_3\omega_1 v_1^2 \omega_2 - 9\omega_4\omega_1 v_1^2 \omega_2 + 2\omega_3\omega_4 \omega_2) \frac{\rho v_1}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT1}} = (\omega_{16} v_2^2 - \omega_{16} + \omega_{10} + 3\omega_{16} c_s^2 - 3\omega_{10} c_s^2 - \omega_{10} v_2^2) \frac{v_2 v_3}{4\omega_{16}\omega_{10}}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT2}} = C_{D_y^3 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{v_2 v_3}{12\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT1}} = (3\omega_{16} v_2^2 - \omega_{16} + \omega_{10} + \omega_{16} c_s^2 - \omega_{10} c_s^2 - 3\omega_{10} v_2^2) \frac{\rho v_3}{4\omega_{16}\omega_{10}}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT2}} = C_{D_y^3 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{\rho v_3}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z v_3}^{(0), \text{SRT}} = (2 + 3c_s^2 \omega + \omega v_2^2 - \omega - 6c_s^2 - 2v_2^2) \frac{\rho v_2}{12\omega}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT1}} = (3\omega_{16}\omega_7 c_s^2 + \omega_{16}\omega_{10}\omega_7 v_2^2 - \omega_{16}\omega_7 + 3\omega_{16}\omega_{10}\omega_7 c_s^2 - \omega_{16}\omega_{10}\omega_7 - 6\omega_{16}\omega_{10} c_s^2 + \omega_{16}\omega_7 v_2^2 + 3\omega_{10}\omega_7 - 3\omega_{10}\omega_7 v_2^2 - 3\omega_{10}\omega_7 c_s^2) \frac{\rho v_2}{12\omega_{16}\omega_{10}\omega_7}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT2}} = C_{D_y^3 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM1}} = (\omega_{16} v_2^2 + \omega_{16}\omega_{10} v_2^2 - \omega_{16} + 3\omega_{10} + 3\omega_{16} c_s^2 + 3\omega_{16}\omega_{10} c_s^2 - \omega_{16}\omega_{10} - 9\omega_{10} c_s^2 - 3\omega_{10} v_2^2) \frac{\rho v_2}{12\omega_{16}\omega_{10}}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM2}} = C_{D_y^3 D_z v_3}^{(0), \text{CLBM1}}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{CuLBM1}} = (-9c_s^2 \omega_5 - \omega_{11} \omega_5 - 3\omega_5 v_2^2 + 3c_s^2 \omega_{11} + 3c_s^2 \omega_{11} \omega_5 - \omega_{11} + \omega_{11} v_2^2 + \omega_{11} \omega_5 v_2^2 + 3\omega_5) \frac{\rho v_2}{12\omega_{11} \omega_5}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{CuLBM2}} = (-9\omega_3 \omega_1 v_2^2 \omega_2 - 9\omega_4 \omega_1 v_2^2 \omega_2 - 18\omega_3 \omega_4 \omega_2 v_3^2 + 6\omega_3 \omega_4 c_s^2 \omega_2 + 18\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 12\omega_3 \omega_4 c_s^2 \omega_1 + 6\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 27\omega_4 c_s^2 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 4\omega_3 \omega_4 v_2^2 \omega_2 + 9\omega_3 \omega_1 \omega_2 + 18\omega_3 \omega_4 \omega_1 v_3^2 + 2\omega_3 \omega_4 \omega_2 + 2\omega_3 \omega_4 \omega_1 v_2^2) \frac{\rho v_2}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2}$:

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^4}{6\omega}$$

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^4}{6\omega_6}$$

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{MRT2}} = C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{CLBM1}} = C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{CLBM2}} = C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^4}{6\omega_2}$$

$$C_{\text{D}_x^2 \text{D}_z^2 \rho}^{(0), \text{CuLBM2}} = (3\omega_1 v_3^2 - 2\omega_1 - 3v_1^2 \omega_2 + 2c_s^2 \omega_1 + 2\omega_2 - 3\omega_2 v_3^2 - 14c_s^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 + 3\omega_1 v_1^2) \frac{c_s^2}{36\omega_1 \omega_2}$$

coefficient $C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2}$:

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{SRT}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{MRT1}} = (\omega_6 - \omega_{13}) \frac{c_s^2 \rho v_1}{2\omega_6 \omega_{13}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{MRT2}} = C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_1}^{(0), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{\rho v_1}{36\omega_1 \omega_2}$$

coefficient $C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2}$:

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{SRT}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{MRT1}} = (\omega_6 - \omega_{18}) \frac{c_s^2 \rho v_3}{2\omega_6 \omega_{18}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{\text{D}_x^2 \text{D}_z^2 v_3}^{(0), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{\rho v_3}{36\omega_1 \omega_2}$$

coefficient $C_{D_x D_y D_z^2 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2}$:

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT1}} = (\omega_6 - \omega_8) \frac{c_s^2 \rho v_2}{2 \omega_6 \omega_8}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CuLBM2}} = (9\omega_3\omega_1 v_2^2 \omega_2 - 9\omega_4\omega_1 v_2^2 \omega_2 - 6\omega_3\omega_4 c_s^2 \omega_2 + 9\omega_4\omega_1 \omega_2 + 6\omega_3\omega_4 c_s^2 \omega_1 - 27\omega_4 c_s^2 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 2\omega_3\omega_4 \omega_1 - 2\omega_3\omega_4 v_2^2 \omega_2 - 9\omega_3\omega_1 \omega_2 + 2\omega_3\omega_4 \omega_2 + 2\omega_3\omega_4 \omega_1 v_2^2) \frac{\rho v_2}{72\omega_3\omega_4\omega_1\omega_2}$$

coefficient $C_{D_x D_y D_z^2 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2}$:

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}} = (\omega_7 - \omega_8) \frac{c_s^2 \rho v_1}{2 \omega_7 \omega_8}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CuLBM2}} = (2\omega_3\omega_4\omega_1 v_1^2 - 6\omega_3\omega_4 c_s^2 \omega_2 + 9\omega_4\omega_1 \omega_2 + 6\omega_3\omega_4 c_s^2 \omega_1 - 2\omega_3\omega_4 v_1^2 \omega_2 - 27\omega_4 c_s^2 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 2\omega_3\omega_4 \omega_1 - 9\omega_3\omega_1 \omega_2 + 9\omega_3\omega_1 v_1^2 \omega_2 - 9\omega_4\omega_1 v_1^2 \omega_2 + 2\omega_3\omega_4 \omega_2) \frac{\rho v_1}{72\omega_3\omega_4\omega_1\omega_2}$$

coefficient $C_{D_y^2 D_z^2 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2}$:

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^4}{6\omega}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^4}{6\omega_7}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT2}} = C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CLBM1}} = C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CLBM2}} = C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^4}{6\omega_3}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CuLBM2}} = (3\omega_1 v_2^2 + 3\omega_1 v_3^2 - 3v_2^2 \omega_2 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 3\omega_2 v_3^2 - 14c_s^2 \omega_2 + 6c_s^2 \omega_1 \omega_2) \frac{c_s^2}{36\omega_1 \omega_2}$$

coefficient $C_{D_y^2 D_z^2 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2}$:

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT1}} = (-\omega_{16} + \omega_7) \frac{c_s^2 \rho v_2}{2\omega_{16}\omega_7}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT2}} = C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CuLBM2}} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{\rho v_2}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y^2 D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT1}} = (-\omega_{19} + \omega_7) \frac{c_s^2 \rho v_3}{2\omega_{19}\omega_7}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{\rho v_3}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_z^3 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT1}} = (-3c_s^2 \omega_{11} + v_3^2 \omega_{18} + \omega_{11} - \omega_{11} v_3^2 - \omega_{18} + 3c_s^2 \omega_{18}) \frac{v_1 v_3}{4\omega_{11} \omega_{18}}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT2}} = C_{D_x D_z^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{v_1 v_3}{12\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_z^3 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_1}^{(0), \text{SRT}} = (2 + 3c_s^2 \omega + \omega v_3^2 - \omega - 6c_s^2 - 2v_3^2) \frac{\rho v_3}{12\omega}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{MRT1}} = (3\omega_6 c_s^2 \omega_{11} \omega_{18} + 3\omega_6 \omega_{11} - 3\omega_6 c_s^2 \omega_{11} - 6c_s^2 \omega_{11} \omega_{18} + \omega_6 v_3^2 \omega_{18} - 3\omega_6 \omega_{11} v_3^2 + \omega_6 \omega_{11} v_3^2 \omega_{18} - \omega_6 \omega_{18} - \omega_6 \omega_{11} \omega_{18} + 3\omega_6 c_s^2 \omega_{18}) \frac{\rho v_3}{12\omega_6 \omega_{11} \omega_{18}}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{MRT2}} = C_{D_x D_z^3 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{CLBM1}} = (3c_s^2 \omega_{11} \omega_{18} - 9c_s^2 \omega_{11} + v_3^2 \omega_{18} + 3\omega_{11} - 3\omega_{11} v_3^2 - \omega_{18} - \omega_{11} \omega_{18} + 3c_s^2 \omega_{18} + \omega_{11} v_3^2 \omega_{18}) \frac{\rho v_3}{12\omega_{11} \omega_{18}}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{CLBM2}} = C_{D_x D_z^3 v_1}^{(0), \text{CLBM1}}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{CuLBM1}} = (3\omega_6 + 3c_s^2\omega_8 + 3\omega_6 c_s^2\omega_8 - \omega_6\omega_8 + \omega_6\omega_8 v_3^2 + \omega_8 v_3^2 - 9\omega_6 c_s^2 - \omega_8 - 3\omega_6 v_3^2) \frac{\rho v_3}{12\omega_6\omega_8}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{CuLBM2}} = (18\omega_3\omega_4\omega_1 v_1^2 + 4\omega_3\omega_4\omega_2 v_3^2 + 6\omega_3\omega_4 c_s^2\omega_2 + 18\omega_3\omega_4 c_s^2\omega_1\omega_2 + 9\omega_4\omega_1\omega_2 + 12\omega_3\omega_4 c_s^2\omega_1 - 18\omega_3\omega_4 v_1^2\omega_2 - 27\omega_4 c_s^2\omega_1\omega_2 - 27\omega_3 c_s^2\omega_1\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_4\omega_1\omega_2 v_3^2 - 9\omega_3\omega_1\omega_2 v_3^2 + 9\omega_3\omega_1\omega_2 + 6\omega_3\omega_4\omega_1\omega_2 v_3^2 + 2\omega_3\omega_4\omega_1 v_3^2 + 2\omega_3\omega_4\omega_2) \frac{\rho v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_z^3 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{MRT1}} = (-c_s^2\omega_{11} + 3v_3^2\omega_{18} + \omega_{11} - 3\omega_{11} v_3^2 - \omega_{18} + c_s^2\omega_{18}) \frac{\rho v_1}{4\omega_{11}\omega_{18}}$$

$$C_{D_x D_z^3 v_3}^{(0), \text{MRT2}} = C_{D_x D_z^3 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CuLBM2}} = (-\omega_1 - v_1^2\omega_2 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 + \omega_1 v_1^2) \frac{\rho v_1}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y D_z^3 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_z^3 \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_y D_z^3 \rho}^{(0), \text{MRT1}} = (-\omega_{19} + 3\omega_{19}c_s^2 + \omega_{19}v_3^2 - 3c_s^2\omega_{11} + \omega_{11} - \omega_{11}v_3^2) \frac{v_2 v_3}{4\omega_{19}\omega_{11}}$$

$$C_{D_y D_z^3 \rho}^{(0), \text{MRT2}} = C_{D_y D_z^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y D_z^3 \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y D_z^3 \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y D_z^3 \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^3 \rho}^{(0), \text{CuLBM2}} = (\omega_1 v_2^2 - v_2^2\omega_2 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2) \frac{v_2 v_3}{12\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y D_z^3 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_z^3 v_2}^{(0), \text{SRT}} = (2 + 3c_s^2\omega + \omega v_3^2 - \omega - 6c_s^2 - 2v_3^2) \frac{\rho v_3}{12\omega}$$

$$C_{D_y D_z^3 v_2}^{(0), \text{MRT1}} =$$

$$(-3\omega_7\omega_{11}v_3^2 - \omega_{19}\omega_7 - \omega_{19}\omega_7\omega_{11} + \omega_{19}\omega_7\omega_{11}v_3^2 - 6\omega_{19}c_s^2\omega_{11} + 3\omega_7\omega_{11} + \omega_{19}\omega_7v_3^2 + 3\omega_{19}\omega_7c_s^2\omega_{11} + 3\omega_{19}\omega_7c_s^2 - 3\omega_7c_s^2\omega_{11}) \frac{\rho v_3}{12\omega_{19}\omega_7\omega_{11}}$$

$$C_{D_y D_z^3 v_2}^{(0), \text{MRT2}} = C_{D_y D_z^3 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y D_z^3 v_2}^{(0), \text{CLBM1}} = (-\omega_{19} + 3\omega_{19}c_s^2 + 3\omega_{19}c_s^2\omega_{11} + \omega_{19}v_3^2 - 9c_s^2\omega_{11} + 3\omega_{11} + \omega_{19}\omega_{11}v_3^2 - \omega_{19}\omega_{11} - 3\omega_{11}v_3^2) \frac{\rho v_3}{12\omega_{19}\omega_{11}}$$

$$C_{D_y D_z^3 v_2}^{(0), \text{CLBM2}} = C_{D_y D_z^3 v_2}^{(0), \text{CLBM1}}$$

$$C_{D_y D_z^3 v_2}^{(0), \text{CuLBM1}} = (3\omega_6 - \omega_{10} - \omega_6\omega_{10} + 3\omega_6\omega_{10}c_s^2 - 9\omega_6c_s^2 + 3\omega_{10}c_s^2 + \omega_6\omega_{10}v_3^2 - 3\omega_6v_3^2 + \omega_{10}v_3^2) \frac{\rho v_3}{12\omega_6\omega_{10}}$$

$$C_{\text{DyD}_2^3v_2}^{(0),\text{CuLBM2}} = (4\omega_3\omega_4\omega_2v_3^2 + 6\omega_3\omega_4c_s^2\omega_2 + 18\omega_3\omega_4c_s^2\omega_1\omega_2 + 9\omega_4\omega_1\omega_2 + 12\omega_3\omega_4c_s^2\omega_1 - 27\omega_4c_s^2\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 18\omega_3\omega_4v_2^2\omega_2 - 9\omega_4\omega_1\omega_2v_3^2 - 9\omega_3\omega_1\omega_2v_3^2 + 9\omega_3\omega_1\omega_2 + 6\omega_3\omega_4\omega_1\omega_2v_3^2 + 2\omega_3\omega_4\omega_1v_3^2 + 2\omega_3\omega_4\omega_2 + 18\omega_3\omega_4\omega_1v_2^2) \frac{\rho v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

coefficient $C_{\text{DyD}_2^3v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_2 \partial x_3^3}$:

$$C_{\text{DyD}_2^3v_3}^{(0),\text{SRT}} = 0$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{MRT1}} = (-\omega_{19} + \omega_{19}c_s^2 + 3\omega_{19}v_3^2 - c_s^2\omega_{11} + \omega_{11} - 3\omega_{11}v_3^2) \frac{\rho v_2}{4\omega_{19}\omega_{11}}$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{MRT2}} = C_{\text{DyD}_2^3v_3}^{(0),\text{MRT1}}$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{CLBM1}} = 0$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{CLBM2}} = 0$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{CuLBM1}} = 0$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{CuLBM2}} = (\omega_1v_2^2 - v_2^2\omega_2 - \omega_1 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2) \frac{\rho v_2}{36\omega_1\omega_2}$$

coefficient $C_{\text{D}_z^4\rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_3^4}$:

$$C_{\text{D}_z^4\rho}^{(0),\text{SRT}} = (c_s^2\omega + 6v_3^4 + 3\omega v_3^2 + 2c_s^4 - 3\omega v_3^4 + 24c_s^2v_3^2 - c_s^4\omega - 2c_s^2 - 12c_s^2\omega v_3^2 - 6v_3^2) \frac{1}{24\omega}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{MRT1}} = (-12c_s^2\omega_{11}v_3^2 + 6v_3^4 - 3\omega_{11}v_3^4 + c_s^2\omega_{11} + 2c_s^4 + 24c_s^2v_3^2 + 3\omega_{11}v_3^2 - 2c_s^2 - c_s^4\omega_{11} - 6v_3^2) \frac{1}{24\omega_{11}}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{MRT2}} = C_{\text{D}_z^4\rho}^{(0),\text{MRT1}}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{CLBM1}} = C_{\text{D}_z^4\rho}^{(0),\text{MRT1}}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{CLBM2}} = C_{\text{D}_z^4\rho}^{(0),\text{MRT1}}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{CuLBM1}} = (6v_3^4 - 3\omega_6v_3^4 + 2c_s^4 - \omega_6c_s^4 - 12\omega_6c_s^2v_3^2 + \omega_6c_s^2 + 24c_s^2v_3^2 - 2c_s^2 + 3\omega_6v_3^2 - 6v_3^2) \frac{1}{24\omega_6}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{CuLBM2}} = (12\omega_2v_3^4 + 2c_s^4\omega_1 - 6\omega_1v_3^2 + 9\omega_1\omega_2v_3^2 - 36c_s^2\omega_1\omega_2v_3^2 + 48c_s^2\omega_2v_3^2 + 4c_s^4\omega_2 - 3c_s^4\omega_1\omega_2 + 24c_s^2\omega_1v_3^2 - 2c_s^2\omega_1 + 6\omega_1v_3^4 - 9\omega_1\omega_2v_3^4 - 12\omega_2v_3^2 - 4c_s^2\omega_2 + 3c_s^2\omega_1\omega_2) \frac{1}{72\omega_1\omega_2}$$

coefficient $C_{\text{D}_z^4v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_3^4}$:

$$C_{\text{D}_z^4v_3}^{(0),\text{SRT}} = (-4 - 3c_s^2\omega - 5\omega v_3^2 + 2\omega + 6c_s^2 + 10v_3^2) \frac{\rho v_3}{12\omega}$$

$$C_{\text{D}_z^4v_3}^{(0),\text{MRT1}} = (-4 - 3c_s^2\omega_{11} + 2\omega_{11} - 5\omega_{11}v_3^2 + 6c_s^2 + 10v_3^2) \frac{\rho v_3}{12\omega_{11}}$$

$$C_{\text{D}_z^4v_3}^{(0),\text{MRT2}} = C_{\text{D}_z^4v_3}^{(0),\text{MRT1}}$$

$$C_{\text{D}_z^4v_3}^{(0),\text{CLBM1}} = C_{\text{D}_z^4v_3}^{(0),\text{MRT1}}$$

$$C_{\text{D}_z^4v_3}^{(0),\text{CLBM2}} = C_{\text{D}_z^4v_3}^{(0),\text{MRT1}}$$

$$C_{\text{D}_z^4v_3}^{(0),\text{CuLBM1}} = (-4 + 2\omega_6 - 3\omega_6c_s^2 + 6c_s^2 - 5\omega_6v_3^2 + 10v_3^2) \frac{\rho v_3}{12\omega_6}$$

$$C_{\text{D}_z^4v_3}^{(0),\text{CuLBM2}} = (10\omega_1v_3^2 - 15\omega_1\omega_2v_3^2 + 6\omega_1\omega_2 - 4\omega_1 + 6c_s^2\omega_1 - 8\omega_2 + 20\omega_2v_3^2 + 12c_s^2\omega_2 - 9c_s^2\omega_1\omega_2) \frac{\rho v_3}{36\omega_1\omega_2}$$

coefficient $C_{D_x v_1, D_x v_1}^{(1)}$ **at** $\left(\frac{\partial v_1}{\partial x_1}\right)^2$:

$$C_{D_x v_1, D_x v_1}^{(1), \text{SRT}} = (2 - \omega) \frac{3\rho v_1}{\omega}$$

$$C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}} = (2 - \omega_9) \frac{3\rho v_1}{\omega_9}$$

$$C_{D_x v_1, D_x v_1}^{(1), \text{MRT2}} = C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}}$$

$$C_{D_x v_1, D_x v_1}^{(1), \text{CLBM1}} = C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}}$$

$$C_{D_x v_1, D_x v_1}^{(1), \text{CLBM2}} = C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}}$$

$$C_{D_x v_1, D_x v_1}^{(1), \text{CuLBM1}} = (2 - \omega_4) \frac{3\rho v_1}{\omega_4}$$

$$C_{D_x v_1, D_x v_1}^{(1), \text{CuLBM2}} = (-3\omega_1\omega_2 + 2\omega_1 + 4\omega_2) \frac{\rho v_1}{\omega_1\omega_2}$$

coefficient $C_{D_x \rho, D_y v_2}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_x \rho, D_y v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{MRT1}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{MRT2}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CuLBM2}} = (3\omega_1 v_2^2 - 3v_2^2\omega_2 - \omega_1 + c_s^2\omega_1 + \omega_2 - c_s^2\omega_2) \frac{1}{3\omega_1\omega_2}$$

coefficient $C_{D_x v_2, D_y v_2}^{(1)}$ **at** $\frac{\partial v_2}{\partial x_1} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_x v_2, D_y v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{MRT1}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{MRT2}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2\rho v_2}{\omega_1\omega_2}$$

coefficient $C_{D_x \rho, D_z v_3}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_x \rho, D_z v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{MRT1}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{MRT2}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CuLBM2}} = (3\omega_1 v_3^2 - \omega_1 + c_s^2 \omega_1 + \omega_2 - 3\omega_2 v_3^2 - c_s^2 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_x v_3, D_z v_3}^{(1)}$ **at** $\frac{\partial v_3}{\partial x_1} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_x v_3, D_z v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{MRT1}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{MRT2}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2\rho v_3}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_x v_2}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1}$:

$$C_{D_y \rho, D_x v_2}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2}{2\omega_5}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{MRT2}} = C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CLBM1}} = C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CLBM2}} = C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CuLBM2}} = (6\omega_1 v_2^2 - 6v_2^2 \omega_2 - 2\omega_1 + 6c_s^2 \omega_1 + 2\omega_2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{1}{6\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_y v_1}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2}$:

$$C_{D_y \rho, D_y v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2}{2\omega_5}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{MRT2}} = C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CLBM1}} = C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CLBM2}} = C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CuLBM2}} = C_{D_y \rho, D_y v_1}^{(1), \text{CuLBM1}}$$

coefficient $C_{D_z \rho, D_x v_3}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1}$:

$$C_{D_z \rho, D_x v_3}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2}{2\omega_6}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{MRT2}} = C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CLBM1}} = C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CLBM2}} = C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CuLBM2}} = (6\omega_1 v_3^2 - 2\omega_1 + 6c_s^2 \omega_1 + 2\omega_2 - 6\omega_2 v_3^2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{1}{6\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_z v_1}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3}$:

$$C_{D_z \rho, D_z v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2}{2\omega_6}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{MRT2}} = C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CLBM1}} = C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CLBM2}} = C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_x^2 \rho}^{(1)}$ **at** $\frac{\partial^2 \rho}{\partial x_1^2}$:

$$C_{D_x^2 \rho}^{(1), \text{SRT}} = (-2 + 2v_1^2 - 3c_s^2 \omega + \omega - \omega v_1^2 + 6c_s^2) \frac{v_1}{2\omega}$$

$$C_{D_x^2 \rho}^{(1), \text{MRT1}} = (-2 + 2v_1^2 - 3c_s^2 \omega_9 + 6c_s^2 - v_1^2 \omega_9 + \omega_9) \frac{v_1}{2\omega_9}$$

$$C_{D_x^2 \rho}^{(1), \text{MRT2}} = C_{D_x^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 \rho}^{(1), \text{CLBM1}} = C_{D_x^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 \rho}^{(1), \text{CLBM2}} = C_{D_x^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 \rho}^{(1), \text{CuLBM1}} = (-2 + 2v_1^2 - 3\omega_4 c_s^2 + \omega_4 - \omega_4 v_1^2 + 6c_s^2) \frac{v_1}{2\omega_4}$$

$$C_{D_x^2 \rho}^{(1), \text{CuLBM2}} = (-3\omega_1 v_1^2 \omega_2 + 3\omega_1 \omega_2 - 2\omega_1 + 4v_1^2 \omega_2 + 6c_s^2 \omega_1 - 4\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 + 2\omega_1 v_1^2) \frac{v_1}{6\omega_1 \omega_2}$$

coefficient $C_{D_x^2 v_1}^{(1)}$ **at** $\frac{\partial^2 v_1}{\partial x_1^2}$:

$$C_{D_x^2 v_1}^{(1), \text{SRT}} = (-2 + 6v_1^2 - c_s^2 \omega + \omega - 3\omega v_1^2 + 2c_s^2) \frac{\rho}{2\omega}$$

$$C_{D_x^2 v_1}^{(1), \text{MRT1}} = (-2 + 6v_1^2 - c_s^2 \omega_9 + 2c_s^2 - 3v_1^2 \omega_9 + \omega_9) \frac{\rho}{2\omega_9}$$

$$C_{D_x^2 v_1}^{(1), \text{MRT2}} = C_{D_x^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(1), \text{CLBM1}} = C_{D_x^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(1), \text{CLBM2}} = C_{D_x^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(1), \text{CuLBM1}} = (-2 + 6v_1^2 - \omega_4 c_s^2 + \omega_4 - 3\omega_4 v_1^2 + 2c_s^2) \frac{\rho}{2\omega_4}$$

$$C_{D_x^2 v_1}^{(1), \text{CuLBM2}} = (-9\omega_1 v_1^2 \omega_2 + 3\omega_1 \omega_2 - 2\omega_1 + 12v_1^2 \omega_2 + 2c_s^2 \omega_1 - 4\omega_2 + 4c_s^2 \omega_2 - 3c_s^2 \omega_1 \omega_2 + 6\omega_1 v_1^2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_x D_y \rho}^{(1)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{MRT1}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{MRT2}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CuLBM2}} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{v_2}{3\omega_1 \omega_2}$$

coefficient $C_{D_x D_y v_2}^{(1)}$ **at** $\frac{\partial^2 v_2}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y v_2}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_y v_2}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_x D_y v_2}^{(1), \text{MRT2}} = C_{D_x D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(1), \text{CLBM1}} = C_{D_x D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(1), \text{CLBM2}} = C_{D_x D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_x D_y v_2}^{(1), \text{CuLBM2}} = (6\omega_1 v_2^2 - 6v_2^2 \omega_2 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_y^2 v_1}^{(1)}$ **at** $\frac{\partial^2 v_1}{\partial x_2^2}$:

$$C_{D_y^2 v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y^2 v_1}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_y^2 v_1}^{(1), \text{MRT2}} = C_{D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 v_1}^{(1), \text{CLBM1}} = C_{D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 v_1}^{(1), \text{CLBM2}} = C_{D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_y^2 v_1}^{(1), \text{CuLBM2}} = C_{D_y^2 v_1}^{(1), \text{CuLBM1}}$$

coefficient $C_{D_x D_z \rho}^{(1)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{MRT1}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{MRT2}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{v_3}{3\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_z v_3}^{(1)} \text{ at } \frac{\partial^2 v_3}{\partial x_1 \partial x_3} :$$

$$C_{D_x D_z v_3}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_z v_3}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_x D_z v_3}^{(1), \text{MRT2}} = C_{D_x D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(1), \text{CLBM1}} = C_{D_x D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(1), \text{CLBM2}} = C_{D_x D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_x D_z v_3}^{(1), \text{CuLBM2}} = (6\omega_1 v_3^2 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 6\omega_2 v_3^2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_z^2 v_1}^{(1)} \text{ at } \frac{\partial^2 v_1}{\partial x_3^2} :$$

$$C_{D_z^2 v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_z^2 v_1}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_z^2 v_1}^{(1), \text{MRT2}} = C_{D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^2 v_1}^{(1), \text{CLBM1}} = C_{D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^2 v_1}^{(1), \text{CLBM2}} = C_{D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^2 v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_z^2 v_1}^{(1), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$\text{coefficient } C_{D_x^3 \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^3} :$$

$$C_{D_x^3 \rho}^{(1), \text{SRT}} = (-36v_1^2 + 12c_s^2 \omega - 144c_s^2 \omega v_1^2 - 7\omega^2 v_1^2 + 144c_s^2 v_1^2 - c_s^2 \omega^2 + 12c_s^4 - 36\omega v_1^4 + 7\omega^2 v_1^4 + 36\omega v_1^2 - 12c_s^4 \omega - 12c_s^2 + c_s^4 \omega^2 + 36v_1^4 + 24c_s^2 \omega^2 v_1^2) \frac{1}{12\omega^2}$$

$$C_{D_x^3 \rho}^{(1), \text{MRT1}} = (-36v_1^2 - 12c_s^4 \omega_9 + 7v_1^4 \omega_9^2 + 24c_s^2 v_1^2 \omega_9^2 + 144c_s^2 v_1^2 - 144c_s^2 v_1^2 \omega_9 + 12c_s^4 + c_s^4 \omega_9^2 - 36v_1^4 \omega_9 + 12c_s^2 \omega_9 - 7v_1^2 \omega_9^2 - 12c_s^2 + 36v_1^4 - c_s^2 \omega_9^2 + 36v_1^2 \omega_9) \frac{1}{12\omega_9^2}$$

$$C_{D_x^3 \rho}^{(1), \text{MRT2}} = C_{D_x^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(1), \text{CLBM1}} = C_{D_x^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(1), \text{CLBM2}} = C_{D_x^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(1), \text{CuLBM1}} = (-36v_1^2 - 144\omega_4 c_s^2 v_1^2 + 12\omega_4 c_s^2 + \omega_4^2 c_s^4 - 7\omega_4^2 v_1^2 + 144c_s^2 v_1^2 + 12c_s^4 - 36\omega_4 v_1^4 + 7\omega_4^2 v_1^4 + 36\omega_4 v_1^2 - 12c_s^2 + 24\omega_4^2 c_s^2 v_1^2 - 12\omega_4 c_s^4 + 36v_1^4 - \omega_4^2 c_s^2) \frac{1}{12\omega_4^2}$$

$$C_{D_x^3 \rho}^{(1), \text{CuLBM2}} = (c_s^4 \omega_1^2 \omega_2^2 + 8c_s^4 \omega_2^2 - 12\omega_1^2 v_1^4 \omega_2 - 4\omega_1^2 v_1^2 + 48c_s^2 \omega_1 v_1^2 \omega_2 + 24\omega_1 v_1^2 \omega_2^2 + 4c_s^2 \omega_1^2 \omega_2 - c_s^2 \omega_1^2 \omega_2^2 - 96c_s^2 \omega_1 v_1^2 \omega_2^2 + 72c_s^2 v_1^2 \omega_2^2 + 4c_s^4 \omega_1^2 - 16\omega_1 v_1^2 \omega_2 - 4c_s^4 \omega_1^2 \omega_2 + 7\omega_1^2 v_1^4 \omega_2^2 + 16v_1^4 \omega_2^2 + 8c_s^2 \omega_1 \omega_2^2 - 8c_s^2 \omega_2^2 + 12\omega_1^2 v_1^2 \omega_2 + 24c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 24c_s^2 \omega_1^2 v_1^2 - 24\omega_1 v_1^4 \omega_2^2 + 16\omega_1 v_1^4 \omega_2 - 4c_s^2 \omega_1^2 + 4\omega_1^2 v_1^4 - 16v_1^2 \omega_2^2 - 7\omega_1^2 v_1^2 \omega_2^2 - 48c_s^2 \omega_1^2 v_1^2 \omega_2 - 8c_s^4 \omega_1 \omega_2^2) \frac{1}{12\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^3 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^3}$:

$$C_{D_x^3 v_1}^{(1), \text{SRT}} = (-24 + 60v_1^2 - 36c_s^2 \omega - 4\omega^2 + 11\omega^2 v_1^2 + 5c_s^2 \omega^2 + 24\omega - 60\omega v_1^2 + 36c_s^2) \frac{\rho v_1}{6\omega^2}$$

$$C_{D_x^3 v_1}^{(1), \text{MRT1}} = (-24 + 60v_1^2 - 4\omega_9^2 - 36c_s^2 \omega_9 + 11v_1^2 \omega_9^2 + 36c_s^2 + 5c_s^2 \omega_9^2 - 60v_1^2 \omega_9 + 24\omega_9) \frac{\rho v_1}{6\omega_9^2}$$

$$C_{D_x^3 v_1}^{(1), \text{MRT2}} = C_{D_x^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(1), \text{CLBM1}} = C_{D_x^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(1), \text{CLBM2}} = C_{D_x^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(1), \text{CuLBM1}} = (-24 + 60v_1^2 - 36\omega_4 c_s^2 + 11\omega_4^2 v_1^2 + 24\omega_4 - 60\omega_4 v_1^2 - 4\omega_4^2 + 36c_s^2 + 5\omega_4^2 c_s^2) \frac{\rho v_1}{6\omega_4^2}$$

$$C_{D_x^3 v_1}^{(1), \text{CuLBM2}} = (8\omega^2 v_1^2 - 40\omega_1 v_1^2 \omega_2^2 + 16\omega_1 \omega_2^2 - 12c_s^2 \omega_1^2 \omega_2 + 5c_s^2 \omega_2^2 \omega_2^2 + 24\omega_1 v_1^2 \omega_2 - 8\omega_1 \omega_2 + 8\omega_2^2 \omega_2 - 4\omega_1^2 - 24c_s^2 \omega_1 \omega_2^2 + 20c_s^2 \omega_2^2 - 20\omega_1^2 v_1^2 \omega_2 + 8c_s^2 \omega_1^2 + 8c_s^2 \omega_1 \omega_2 + 28v_1^2 \omega_2^2 + 11\omega_1^2 v_1^2 \omega_2^2 - 12\omega_2^2 - 4\omega_1^2 \omega_2^2) \frac{\rho v_1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_y \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{MRT1}} = (-v_1^2 \omega_5 \omega_9 \omega_{12} + v_1^2 \omega_5 \omega_9^2 - \omega_9 \omega_{12} + \omega_5 \omega_9 - \omega_5 \omega_{12} - \omega_5 \omega_9^2 + v_1^2 \omega_9 \omega_{12} - v_1^2 \omega_5 \omega_9 + v_1^2 \omega_5 \omega_{12} + \omega_9^2 + \omega_5 \omega_9 \omega_{12} + 3c_s^2 \omega_5 \omega_{12} - 3c_s^2 \omega_5 \omega_9 + 3c_s^2 \omega_9 \omega_{12} - v_1^2 \omega_9^2 - 3c_s^2 \omega_9^2 + 3c_s^2 \omega_5 \omega_9^2 - 3c_s^2 \omega_5 \omega_9 \omega_{12}) \frac{v_1 v_2}{\omega_5 \omega_9^2 \omega_{12}}$$

$$C_{D_x^2 D_y \rho}^{(1), \text{MRT2}} = C_{D_x^2 D_y \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CuLBM2}} = (2\omega_1^2 v_1^2 - 4v_2^2 \omega_2^2 - 3\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 - 3\omega_1^2 v_2^2 \omega_2 - 4\omega_1 v_1^2 \omega_2 + 2\omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 6c_s^2 \omega_2^2 + 2\omega_1 v_2^2 \omega_2 + 12c_s^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 + 2v_1^2 \omega_2^2 + 3\omega_1 v_2^2 \omega_2^2 + 2\omega_1^2 v_2^2 + 2\omega_2^2) \frac{v_1 v_2}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_y v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{MRT1}} = (-3v_1^2 \omega_5 \omega_9 \omega_{12} + 3v_1^2 \omega_5 \omega_9^2 - \omega_9 \omega_{12} + \omega_5 \omega_9 - \omega_5 \omega_{12} - \omega_5 \omega_9^2 + 3v_1^2 \omega_9 \omega_{12} - 3v_1^2 \omega_5 \omega_9 + 3v_1^2 \omega_5 \omega_{12} + \omega_9^2 + \omega_5 \omega_9 \omega_{12} + c_s^2 \omega_5 \omega_{12} - c_s^2 \omega_5 \omega_9 + c_s^2 \omega_9 \omega_{12} - 3v_1^2 \omega_9^2 - c_s^2 \omega_9^2 + c_s^2 \omega_5 \omega_9^2 - c_s^2 \omega_5 \omega_9 \omega_{12}) \frac{\rho v_2}{\omega_5 \omega_9^2 \omega_{12}}$$

$$C_{D_x^2 D_y v_1}^{(1), \text{MRT2}} = C_{D_x^2 D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CuLBM2}} = (3\omega_3 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 - 2\omega_1 \omega_2^2 - 6c_s^2 \omega_1^2 \omega_2 + 2\omega_3 \omega_1^2 \omega_2^2 + \omega_3 \omega_1^2 \omega_2 - 2\omega_1^2 v_2^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 - 4\omega_3 c_s^2 \omega_2^2 + \omega_3 \omega_1 v_2^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2 - 2\omega_3 v_2^2 \omega_2^2 - 12\omega_3 \omega_1 v_1^2 \omega_2 - \omega_3 \omega_1^2 v_2^2 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 6\omega_3 \omega_1^2 v_1^2 + 2\omega_1 v_2^2 \omega_2^2 - 4\omega_3 \omega_1^2) \frac{\rho v_2}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_y v_2}^{(1)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_2}^{(1), \text{SRT}} = (12 - 12v_1^2 + 36c_s^2 \omega + 3\omega^2 - 3\omega^2 v_1^2 - 11c_s^2 \omega^2 - 12\omega + 12\omega v_1^2 - 36c_s^2) \frac{\rho v_1}{12\omega^2}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{MRT1}} = (12c_s^2 \omega_5^2 \omega_9^2 + 42c_s^2 \omega_5 \omega_9^2 \omega_{12} - 12v_1^2 \omega_5 \omega_9^2 - 3v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 18c_s^2 \omega_5^2 \omega_9 \omega_{12} + 6\omega_5^2 \omega_9 \omega_{12} + 12\omega_5 \omega_9^2 - 6\omega_5 \omega_9^2 \omega_{12} + 36c_s^2 \omega_5^2 \omega_{12} - 12c_s^2 \omega_5^2 \omega_9 - 24c_s^2 \omega_9^2 \omega_{12} - 12v_1^2 \omega_5^2 \omega_9 + 12v_1^2 \omega_5^2 \omega_{12} + 3\omega_5^2 \omega_9^2 \omega_{12} - 12\omega_5^2 \omega_9^2 - 6v_1^2 \omega_5^2 \omega_9 \omega_{12} + 12\omega_5^2 \omega_9 - 12\omega_5^2 \omega_{12} - 11c_s^2 \omega_5^2 \omega_9^2 \omega_{12} - 12c_s^2 \omega_5 \omega_9^2 + 6v_1^2 \omega_5 \omega_9^2 \omega_{12} - 24c_s^2 \omega_5 \omega_9 \omega_{12} + 12v_1^2 \omega_5^2 \omega_9^2) \frac{\rho v_1}{12\omega_5^2 \omega_9^2 \omega_{12}}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{MRT2}} = C_{D_x^2 D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{CLBM1}} = (-6v_1^2 \omega_5 \omega_9 \omega_{12} - 11c_s^2 \omega_5 \omega_9^2 \omega_{12} + 12v_1^2 \omega_5 \omega_9^2 + 12\omega_5 \omega_9 - 12\omega_5 \omega_{12} - 12\omega_5 \omega_9^2 + 3\omega_5 \omega_9^2 \omega_{12} - 12v_1^2 \omega_5 \omega_9 + 12v_1^2 \omega_5 \omega_{12} + 18c_s^2 \omega_9^2 \omega_{12} + 6v_1^2 \omega_9^2 \omega_{12} + 12\omega_9^2 + 6\omega_5 \omega_9 \omega_{12} + 36c_s^2 \omega_5 \omega_{12} - 36c_s^2 \omega_5 \omega_9 - 12v_1^2 \omega_9^2 - 6\omega_9^2 \omega_{12} - 36c_s^2 \omega_9^2 + 36c_s^2 \omega_5 \omega_9^2 - 3v_1^2 \omega_5 \omega_9^2 \omega_{12} - 18c_s^2 \omega_5 \omega_9 \omega_{12}) \frac{\rho v_1}{12\omega_5^2 \omega_9^2 \omega_{12}}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{CLBM2}} = C_{D_x^2 D_y v_2}^{(1), \text{CLBM1}}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{CuLBM1}} = (12\omega_1 v_1^2 \omega_9 - 18\omega_4 c_s^2 \omega_1 \omega_9 - 12\omega_1 \omega_9 + 36\omega_4^2 c_s^2 \omega_1 + 18\omega_1^2 c_s^2 \omega_9 - 3\omega_4^2 \omega_1 v_1^2 \omega_9 - 12\omega_4^2 v_1^2 + 12\omega_4 \omega_1 + 6\omega_4 \omega_1 \omega_9 + 6\omega_4^2 v_1^2 \omega_9 + 12\omega_4^2 \omega_1 v_1^2 + 3\omega_4^2 \omega_1 \omega_9 - 11\omega_4^2 c_s^2 \omega_1 \omega_9 - 12\omega_4^2 \omega_1 + 36c_s^2 \omega_1 \omega_9 - 6\omega_4 \omega_1 v_1^2 \omega_9 - 6\omega_4^2 \omega_9 + 12\omega_4^2 - 12\omega_4 \omega_1 v_1^2 - 36\omega_4 c_s^2 \omega_1 - 36\omega_4^2 c_s^2) \frac{\rho v_1}{12\omega_4^2 \omega_1 \omega_9}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{CuLBM2}} = (-36\omega_3 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 \omega_4 \omega_1^2 v_2^2 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 - 4\omega_4 \omega_1^2 v_1^2 \omega_2 - 3\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2^2 + 8\omega_3 \omega_4 v_1^2 \omega_2^2 + 18\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1^2 + 8\omega_4 \omega_1 \omega_2^2 - 2\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 + 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 + 12\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 + 6\omega_4 \omega_1^2 v_1^2 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 18\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 - 6\omega_4 \omega_1^2 \omega_2^2 - 8\omega_4 \omega_1 v_1^2 \omega_2^2 - 12\omega_3 \omega_1 v_1^2 \omega_2^2 - 11\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 + 12\omega_3 \omega_1 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 + 2\omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 - 24\omega_3 \omega_4 v_2^2 \omega_2^2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_1}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y^2 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 \rho}^{(1), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x D_y^2 \rho}^{(1), \text{MRT1}} = (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4}{6\omega_5^2}$$

$$C_{D_x D_y^2 \rho}^{(1), \text{MRT2}} = C_{D_x D_y^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 \rho}^{(1), \text{CLBM1}} = C_{D_x D_y^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 \rho}^{(1), \text{CLBM2}} = C_{D_x D_y^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 \rho}^{(1), \text{CuLBM1}} = (-12 + 12\omega_1 - \omega_1^2) \frac{c_s^4}{6\omega_1^2}$$

$$C_{D_x D_y^2 \rho}^{(1), \text{CuLBM2}} = (-c_s^4 \omega_1^2 \omega_2^2 - 14c_s^4 \omega_2^2 + 2\omega_1 v_2^4 \omega_2 + 4v_2^2 \omega_2^2 - 15c_s^2 \omega_1^2 v_2^2 \omega_2 + 2c_s^2 \omega_1^2 \omega_2 + 2\omega_1^2 v_2^4 + 12c_s^2 \omega_1^2 v_2^2 + 3\omega_1^2 v_2^2 \omega_2 + 2c_s^4 \omega_1^2 - 2c_s^4 \omega_1^2 \omega_2 + 3\omega_1 v_2^4 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 - 18c_s^2 v_2^2 \omega_2^2 + 15c_s^2 \omega_1 v_2^2 \omega_2^2 - 2\omega_1 v_2^2 \omega_2 - 4v_2^4 \omega_2^2 - 3\omega_1^2 v_2^4 \omega_2 - 2c_s^2 \omega_1^2 + 6c_s^2 \omega_1 v_2^2 \omega_2 - 3\omega_1 v_2^2 \omega_2^2 + 14c_s^4 \omega_1 \omega_2^2 - 2\omega_1^2 v_2^2) \frac{1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y^2 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 v_1}^{(1), \text{SRT}} = \frac{-c_s^2 \rho v_1}{6}$$

$$C_{D_x D_y^2 v_1}^{(1), \text{MRT1}} = (12\omega_5^2 - 12\omega_9 \omega_{12} + 12\omega_5 \omega_9 - 12\omega_5 \omega_{12} - \omega_5^2 \omega_9 \omega_{12} + 12\omega_5 \omega_9 \omega_{12} - 12\omega_5^2 \omega_9) \frac{c_s^2 \rho v_1}{6\omega_5^2 \omega_9 \omega_{12}}$$

$$C_{D_x D_y^2 v_1}^{(1), \text{MRT2}} = C_{D_x D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 v_1}^{(1), \text{CLBM1}} = C_{D_x D_y^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(1), \text{CLBM2}} = C_{D_x D_y^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(1), \text{CuLBM1}} = C_{D_x D_y^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(1), \text{CuLBM2}} = C_{D_x D_y^2 v_1}^{(1), \text{SRT}}$$

$$\text{coefficient } C_{D_x D_y^2 v_2}^{(1)} \text{ at } \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{MRT1}} = (-\omega_5^2 + \omega_5 \omega_{15} + 2\omega_5 - 2\omega_{15}) \frac{c_s^2 \rho v_2}{\omega_5^2 \omega_{15}}$$

$$C_{D_x D_y^2 v_2}^{(1), \text{MRT2}} = C_{D_x D_y^2 v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CuLBM2}} = (-14v_2^2 \omega_2^2 - 5\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 - 11\omega_1^2 v_2^2 \omega_2 - 2\omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 10c_s^2 \omega_2^2 + 6\omega_1 v_2^2 \omega_2 + 8c_s^2 \omega_1^2 + 2c_s^2 \omega_1 \omega_2 + 11\omega_1 v_2^2 \omega_2^2 + 8\omega_1^2 v_2^2 + 6\omega_2^2) \frac{\rho v_2}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_y^3 \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_2^3} :$$

$$C_{D_y^3 \rho}^{(1), \text{SRT}} = (-1 + 3c_s^2 + v_2^2) \frac{v_1 v_2}{12}$$

$$C_{D_y^3 \rho}^{(1), \text{MRT1}} = (-\omega_{10} \omega_5 \omega_{15} + 6\omega_5 \omega_{15} + 18\omega_{10} c_s^2 \omega_5 + 12v_2^2 \omega_{15} + 6\omega_{10} \omega_5 v_2^2 + 12\omega_{10} - 6\omega_{10} \omega_5 - 6\omega_5 v_2^2 \omega_{15} + 36c_s^2 \omega_{15} + \omega_{10} \omega_5 v_2^2 \omega_{15} - 18c_s^2 \omega_5 \omega_{15} - 36\omega_{10} c_s^2 + 3\omega_{10} c_s^2 \omega_5 \omega_{15} - 12\omega_{10} v_2^2 - 12\omega_{15}) \frac{v_1 v_2}{12\omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_y^3 \rho}^{(1), \text{MRT2}} = C_{D_y^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(1), \text{CLBM1}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(1), \text{CLBM2}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(1), \text{CuLBM1}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(1), \text{CuLBM2}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$\text{coefficient } C_{D_y^3 v_1}^{(1)} \text{ at } \frac{\partial^3 v_1}{\partial x_2^3} :$$

$$C_{D_y^3 v_1}^{(1), \text{SRT}} = (6 + 18c_s^2 \omega + \omega^2 + 6\omega v_2^2 - 3c_s^2 \omega^2 - 6\omega - \omega^2 v_2^2 - 18c_s^2 - 6v_2^2) \frac{\rho v_2}{6\omega^2}$$

$$C_{D_y^3 v_1}^{(1), \text{MRT1}} = (-3\omega_5^2 - 3\omega_5 \omega_{15} - 6c_s^2 \omega_5 - 6\omega_5 v_2^2 - 3c_s^2 \omega_5^2 \omega_{15} - \omega_5^2 v_2^2 \omega_{15} + 3c_s^2 \omega_5^2 + 3\omega_5 v_2^2 \omega_{15} - 12c_s^2 \omega_{15} + 15c_s^2 \omega_5 \omega_{15} + 6\omega_5 + 3\omega_5^2 v_2^2 + \omega_5^2 \omega_{15}) \frac{\rho v_2}{6\omega_5^2 \omega_{15}}$$

$$C_{D_y^3 v_1}^{(1), \text{MRT2}} = C_{D_y^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^3 v_1}^{(1), \text{CLBM1}} = (6 + \omega_5 \omega_{15} + 3v_2^2 \omega_{15} + 9c_s^2 \omega_5 + 3\omega_5 v_2^2 - \omega_5 v_2^2 \omega_{15} + 9c_s^2 \omega_{15} - 3c_s^2 \omega_5 \omega_{15} - 3\omega_5 - 18c_s^2 - 6v_2^2 - 3\omega_{15}) \frac{\rho v_2}{6\omega_5 \omega_{15}}$$

$$C_{D_y^3 v_1}^{(1), \text{CLBM2}} = C_{D_y^3 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_y^3 v_1}^{(1), \text{CuLBM1}} = (6 - 3\omega_7 c_s^2 \omega_1 + 3\omega_1 v_2^2 - 3\omega_7 - 3\omega_1 + \omega_7 \omega_1 + 3\omega_7 v_2^2 + 9c_s^2 \omega_1 - \omega_7 \omega_1 v_2^2 - 18c_s^2 - 6v_2^2 + 9\omega_7 c_s^2) \frac{\rho v_2}{6\omega_7 \omega_1}$$

$$C_{D_y^3 v_1}^{(1), \text{CuLBM2}} = (6\omega_3 - 18\omega_4 c_s^2 - 6\omega_4 v_2^2 - 3\omega_4 \omega_1 - 6\omega_3 \omega_4 c_s^2 \omega_1 + 3\omega_4 \omega_1 v_2^2 + 9\omega_3 c_s^2 \omega_1 + 6\omega_4 - 3\omega_3 \omega_1 - 6\omega_3 v_2^2 + 6\omega_3 \omega_4 v_2^2 + 2\omega_3 \omega_4 \omega_1 - 6\omega_3 \omega_4 + 18\omega_3 \omega_4 c_s^2 + 3\omega_3 \omega_1 v_2^2 - 18\omega_3 c_s^2 + 9\omega_4 c_s^2 \omega_1 - 2\omega_3 \omega_4 \omega_1 v_2^2) \frac{\rho v_2}{12\omega_3 \omega_4 \omega_1}$$

$$\text{coefficient } C_{D_y^3 v_2}^{(1)} \text{ at } \frac{\partial^3 v_2}{\partial x_2^3} :$$

$$C_{D_y^3 v_2}^{(1), \text{SRT}} = (-1 + c_s^2 + 3v_2^2) \frac{\rho v_1}{12}$$

$$C_{D_y^3 v_2}^{(1), \text{MRT1}} = (-\omega_{10} \omega_5 \omega_{15} + 6\omega_5 \omega_{15} + 6\omega_{10} c_s^2 \omega_5 + 36v_2^2 \omega_{15} + 18\omega_{10} \omega_5 v_2^2 + 12\omega_{10} - 6\omega_{10} \omega_5 - 18\omega_5 v_2^2 \omega_{15} + 12c_s^2 \omega_{15} + 3\omega_{10} \omega_5 v_2^2 \omega_{15} - 6c_s^2 \omega_5 \omega_{15} - 12\omega_{10} c_s^2 + \omega_{10} c_s^2 \omega_5 \omega_{15} - 36\omega_{10} v_2^2 - 12\omega_{15}) \frac{\rho v_1}{12\omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_y^3 v_2}^{(1), \text{MRT2}} = C_{D_y^3 v_2}^{(1), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(1), \text{CLBM1}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(1), \text{CLBM2}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(1), \text{CuLBM1}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(1), \text{CuLBM2}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$\text{coefficient } C_{D_x^2 D_z \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{MRT1}} = (\omega_6 \omega_{13} v_1^2 + \omega_6 v_1^2 \omega_9^2 + \omega_9^2 - 3\omega_6 \omega_{13} c_s^2 \omega_9 - 3\omega_6 c_s^2 \omega_9 - \omega_6 \omega_{13} - \omega_6 \omega_9^2 + 3\omega_6 \omega_{13} c_s^2 + \omega_{13} v_1^2 \omega_9 - v_1^2 \omega_9^2 - \omega_{13} \omega_9 - 3c_s^2 \omega_9^2 + 3\omega_{13} c_s^2 \omega_9 + \omega_6 \omega_9 + \omega_6 \omega_{13} \omega_9 - \omega_6 v_1^2 \omega_9 - \omega_6 \omega_{13} v_1^2 \omega_9 + 3\omega_6 c_s^2 \omega_9^2) \frac{v_1 v_3}{\omega_6 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z \rho}^{(1), \text{MRT2}} = C_{D_x^2 D_z \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CuLBM2}} = (2\omega_1^2 v_1^2 + 2\omega_1 \omega_2 v_3^2 - 3\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 - 4\omega_2^2 v_3^2 - 4\omega_1 v_1^2 \omega_2 + 2\omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 6c_s^2 \omega_2^2 + 12c_s^2 \omega_1^2 - 3\omega_1^2 \omega_2 v_3^2 - 6c_s^2 \omega_1 \omega_2 + 2v_1^2 \omega_2^2 + 2\omega_2^2 + 2\omega_1^2 v_3^2 + 3\omega_1 \omega_2^2 v_3^2) \frac{v_1 v_3}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_z v_1}^{(1)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{MRT1}} = (3\omega_6 \omega_{13} v_1^2 + 3\omega_6 v_1^2 \omega_9^2 + \omega_9^2 - \omega_6 \omega_{13} c_s^2 \omega_9 - \omega_6 c_s^2 \omega_9 - \omega_6 \omega_{13} - \omega_6 \omega_9^2 + \omega_6 \omega_{13} c_s^2 + 3\omega_{13} v_1^2 \omega_9 - 3v_1^2 \omega_9^2 - \omega_{13} \omega_9 - c_s^2 \omega_9^2 + \omega_{13} c_s^2 \omega_9 + \omega_6 \omega_9 + \omega_6 \omega_{13} \omega_9 - 3\omega_6 v_1^2 \omega_9 - 3\omega_6 \omega_{13} v_1^2 \omega_9 + \omega_6 c_s^2 \omega_9^2) \frac{\rho v_3}{\omega_6 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z v_1}^{(1), \text{MRT2}} = C_{D_x^2 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CuLBM2}} = (3\omega_3 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 - 2\omega_1 \omega_2^2 + 2\omega_3 \omega_1^2 v_3^2 - 6c_s^2 \omega_1^2 \omega_2 + \omega_3 \omega_1^2 \omega_2 + \omega_3 \omega_1 \omega_2^2 v_3^2 - \omega_3 \omega_1^2 \omega_2 v_3^2 - 4\omega_3 c_s^2 \omega_1 \omega_2 - 4\omega_3 c_s^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2 - 12\omega_3 \omega_1 v_1^2 \omega_2 - \omega_3 \omega_1 \omega_2^2 - 2\omega_1^2 \omega_2 v_3^2 + 6\omega_3 \omega_1^2 v_1^2 - 2\omega_3 \omega_2^2 v_3^2 - 4\omega_3 \omega_1^2 + 2\omega_1 \omega_2^2 v_3^2) \frac{\rho v_3}{6\omega_3 \omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_z v_3}^{(1)} \text{ at } \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z v_3}^{(1), \text{SRT}} = (12 - 12v_1^2 + 36c_s^2 \omega + 3\omega^2 - 3\omega^2 v_1^2 - 11c_s^2 \omega^2 - 12\omega + 12\omega v_1^2 - 36c_s^2) \frac{\rho v_1}{12\omega^2}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{MRT1}} = (12\omega_6 \omega_9 - 18\omega_6 \omega_{13} c_s^2 \omega_9 - 3\omega_6^2 \omega_{13} v_1^2 \omega_9^2 + 6\omega_6^2 \omega_{13} \omega_9 + 12\omega_6^2 c_s^2 \omega_9^2 - 12\omega_6^2 v_1^2 \omega_9 - 12\omega_6^2 c_s^2 \omega_9 + 12\omega_6^2 v_1^2 \omega_9^2 + 3\omega_6^2 \omega_{13} \omega_9^2 - 11\omega_6^2 \omega_{13} c_s^2 \omega_9^2 + 36\omega_6^2 \omega_{13} c_s^2 - 6\omega_6^2 \omega_{13} v_1^2 \omega_9 - 12\omega_6^2 \omega_{13} - 12\omega_6^2 \omega_9^2 - 12\omega_6 v_1^2 \omega_9^2 + 6\omega_6 \omega_{13} v_1^2 \omega_9^2 - 24\omega_6 \omega_{13} c_s^2 \omega_9 - 6\omega_6 \omega_{13} \omega_9^2 + 12\omega_6 \omega_9^2 - 24\omega_{13} c_s^2 \omega_9^2 + 12\omega_6^2 \omega_{13} v_1^2 + 42\omega_6 \omega_{13} c_s^2 \omega_9^2 - 12\omega_6 c_s^2 \omega_9^2) \frac{\rho v_1}{12\omega_6^2 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{MRT2}} = C_{D_x^2 D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CLBM1}} = (12\omega_6 \omega_{13} v_1^2 + 12\omega_6 v_1^2 \omega_9^2 + 12\omega_9^2 - 3\omega_6 \omega_{13} v_1^2 \omega_9^2 - 18\omega_6 \omega_{13} c_s^2 \omega_9 - 36\omega_6 c_s^2 \omega_9 - 12\omega_6 \omega_{13} + 3\omega_6 \omega_{13} \omega_9^2 - 12\omega_6 \omega_9^2 + 36\omega_6 \omega_{13} c_s^2 - 12v_1^2 \omega_9^2 + 18\omega_{13} c_s^2 \omega_9^2 - 6\omega_{13} \omega_9^2 - 36c_s^2 \omega_9^2 + 6\omega_{13} v_1^2 \omega_9^2 + 12\omega_6 \omega_9 + 6\omega_6 \omega_{13} \omega_9 - 12\omega_6 v_1^2 \omega_9 - 6\omega_6 \omega_{13} v_1^2 \omega_9 - 11\omega_6 \omega_{13} c_s^2 \omega_9^2 + 36\omega_6 c_s^2 \omega_9^2) \frac{\rho v_1}{12\omega_6 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CLBM2}} = C_{D_x^2 D_z v_3}^{(1), \text{CLBM1}}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CuLBM1}} = (12\omega_4 \omega_2 + 18\omega_4 c_s^2 \omega_{12} - 6\omega_4 v_1^2 \omega_2 \omega_{12} + 12\omega_4^2 v_1^2 \omega_2 + 36\omega_4^2 c_s^2 \omega_2 - 12\omega_4^2 v_1^2 + 6\omega_4^2 v_1^2 \omega_{12} - 11\omega_4^2 c_s^2 \omega_2 \omega_{12} + 3\omega_4^2 \omega_2 \omega_{12} + 36c_s^2 \omega_2 \omega_{12} + 12v_1^2 \omega_2 \omega_{12} - 36\omega_4 c_s^2 \omega_2 + 6\omega_4 \omega_2 \omega_{12} - 3\omega_4^2 v_1^2 \omega_2 \omega_{12} - 6\omega_4^2 \omega_{12} + 12\omega_4^2 - 12\omega_4^2 \omega_2 - 12\omega_2 \omega_{12} - 18\omega_4 c_s^2 \omega_2 \omega_{12} - 12\omega_4 v_1^2 \omega_2 - 36\omega_4^2 c_s^2) \frac{\rho v_1}{12\omega_4^2 \omega_2 \omega_{12}}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CuLBM2}} = (-36\omega_3 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 18\omega_3 \omega_4 \omega_1 \omega_2^2 v_3^2 + 12\omega_3 \omega_4 \omega_1^2 v_3^2 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 - 4\omega_4 \omega_1^2 v_1^2 \omega_2 - 3\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2^2 + 8\omega_3 \omega_4 v_1^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 - 18\omega_3 \omega_4 \omega_1^2 \omega_2 v_3^2 + 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1^2 + 8\omega_4 \omega_1 \omega_2^2 - 2\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_2^2 + 12\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 + 6\omega_4 \omega_1^2 v_1^2 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 6\omega_4 \omega_1^2 \omega_2^2 - 8\omega_4 \omega_1 v_1^2 \omega_2^2 - 12\omega_3 \omega_1 v_1^2 \omega_2^2 - 11\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 + 12\omega_3 \omega_1 \omega_2^2 - 24\omega_3 \omega_4 \omega_2^2 v_3^2 + 4\omega_4 \omega_1^2 \omega_2 + 12\omega_3 \omega_4 \omega_1 \omega_2 v_3^2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 + 2\omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_1}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x D_y D_z \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} :$$

$$C_{D_x D_y D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{MRT1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{MRT2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CuLBM2}} = (v_2^2 \omega_2^2 - 2\omega_1 \omega_2 v_3^2 + \omega_2^2 v_3^2 + 4\omega_1 \omega_2 - 2\omega_1^2 + 6c_s^2 \omega_2^2 - 2\omega_1 v_2^2 \omega_2 + 6c_s^2 \omega_1^2 - 12c_s^2 \omega_1 \omega_2 + \omega_1^2 v_2^2 - 2\omega_2^2 + \omega_1^2 v_3^2) \frac{v_2 v_3}{3\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x D_y D_z v_2}^{(1)} \text{ at } \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} :$$

$$C_{D_x D_y D_z v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{MRT1}} = (\omega_5^2 - \omega_6 \omega_5^2 - \omega_6 \omega_8 + \omega_6 \omega_5 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5) \frac{c_s^2 \rho v_3}{\omega_6 \omega_8 \omega_5^2}$$

$$C_{D_x D_y D_z v_2}^{(1), \text{MRT2}} = C_{D_x D_y D_z v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CuLBM2}} = (18\omega_3 c_s^2 \omega_1 \omega_2^2 + \omega_3 \omega_4 \omega_1 \omega_2^2 v_3^2 + 2\omega_3 \omega_4 \omega_1^2 v_3^2 + 6\omega_3 \omega_4 \omega_1^2 v_2^2 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - \omega_3 \omega_4 \omega_1^2 \omega_2 v_3^2 - 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 8\omega_3 \omega_4 c_s^2 \omega_1^2 + 4\omega_4 \omega_1 \omega_2^2 - 4\omega_4 \omega_1 \omega_2^2 v_3^2 - 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 4\omega_3 \omega_4 c_s^2 \omega_2^2 + 6\omega_3 \omega_1 \omega_2^2 v_3^2 + 3\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 2\omega_4 \omega_1^2 \omega_2 v_3^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 + 3\omega_4 \omega_1^2 \omega_2^2 v_3^2 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - 3\omega_3 \omega_1^2 \omega_2^2 v_3^2 - 3\omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 6\omega_3 \omega_1 \omega_2^2 - 2\omega_3 \omega_4 \omega_2^2 v_3^2 + 2\omega_4 \omega_1^2 \omega_2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 + 6\omega_3 \omega_4 v_2^2 \omega_2^2 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2) \frac{\rho v_3}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{MRT1}} = (-\omega_6 \omega_8 + \omega_6 \omega_5 + \omega_6^2 - \omega_6^2 \omega_5 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5) \frac{c_s^2 \rho v_2}{\omega_6^2 \omega_8 \omega_5}$$

$$C_{D_x D_y D_z v_3}^{(1), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CuLBM2}} = (18\omega_3 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 \omega_1^2 v_3^2 + 2\omega_3 \omega_4 \omega_1^2 v_2^2 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 + \omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 8\omega_3 \omega_4 c_s^2 \omega_1^2 + 4\omega_4 \omega_1 \omega_2^2 - 4\omega_3 \omega_4 c_s^2 \omega_2^2 + 3\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 4\omega_4 \omega_1 v_2^2 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 \omega_1 v_2^2 \omega_2^2 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - \omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_4 \omega_1^2 v_2^2 \omega_2^2 - 3\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 6\omega_3 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 \omega_2^2 v_3^2 + 2\omega_4 \omega_1^2 \omega_2 - 2\omega_4 \omega_1^2 v_2^2 \omega_2 - 12\omega_3 \omega_4 \omega_1 \omega_2 v_3^2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 - 2\omega_3 \omega_4 v_2^2 \omega_2^2 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2) \frac{\rho v_2}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{MRT1}} = (\omega_5^2 - \omega_6 \omega_5^2 - \omega_6 \omega_8 + \omega_6 \omega_5 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5) \frac{c_s^2 \rho v_3}{\omega_6 \omega_8 \omega_5^2}$$

$$C_{D_y^2 D_z v_1}^{(1), \text{MRT2}} = C_{D_y^2 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CuLBM2}} = (-2\omega_3 - 6\omega_4 c_s^2 - \omega_4 \omega_1 + \omega_4 \omega_1 v_3^2 - 2\omega_4 v_3^2 - 3\omega_3 c_s^2 \omega_1 + 2\omega_4 + \omega_3 \omega_1 + 2\omega_3 v_3^2 - \omega_3 \omega_1 v_3^2 + 6\omega_3 c_s^2 + 3\omega_4 c_s^2 \omega_1) \frac{\rho v_3}{4\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_y^2 D_z v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_3}^{(1), \text{SRT}} = \frac{-c_s^2 \rho v_1}{6}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{MRT1}} = (-6\omega_6 \omega_7 \omega_5 - \omega_6 \omega_7 \omega_8 \omega_5 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_7 + 6\omega_6 \omega_8 \omega_5 - 6\omega_8 \omega_5) \frac{c_s^2 \rho v_1}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{MRT2}} = C_{D_y^2 D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CLBM1}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CLBM2}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CuLBM1}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CuLBM2}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

coefficient $C_{D_x D_z^2 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 \rho}^{(1), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{MRT1}} = (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4}{6\omega_6^2}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{MRT2}} = C_{D_x D_z^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CLBM1}} = C_{D_x D_z^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CLBM2}} = C_{D_x D_z^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CuLBM1}} = (-12 + 12\omega_2 - \omega_2^2) \frac{c_s^4}{6\omega_2^2}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CuLBM2}} = (-3\omega_1^2 \omega_2 v_3^4 - c_s^4 \omega_1^2 \omega_2^2 - 14c_s^4 \omega_2^2 - 2\omega_1 \omega_2 v_3^2 + 2\omega_1^2 v_3^4 + 3\omega_1 \omega_2^2 v_3^4 + 2c_s^2 \omega_1^2 \omega_2 + 4\omega_2^2 v_3^2 + 12c_s^2 \omega_1^2 v_3^2 + 2c_s^4 \omega_1^2 + 6c_s^2 \omega_1 \omega_2 v_3^2 - 2c_s^4 \omega_1^2 \omega_2 - 18c_s^2 \omega_2^2 v_3^2 + 15c_s^2 \omega_1 \omega_2^2 v_3^2 - 15c_s^2 \omega_1^2 \omega_2 v_3^2 - 2c_s^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 - 2c_s^2 \omega_1^2 + 2\omega_1 \omega_2 v_3^4 + 3\omega_1^2 \omega_2 v_3^2 + 14c_s^4 \omega_1 \omega_2^2 - 4\omega_2^2 v_3^4 - 2\omega_1^2 v_3^2 - 3\omega_1 \omega_2^2 v_3^2) \frac{1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_1}^{(1), \text{SRT}} = \frac{-c_s^2 \rho v_1}{6}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{MRT1}} = (-12\omega_6^2 \omega_9 - \omega_6^2 \omega_{13} \omega_9 + 12\omega_6^2 - 12\omega_6 \omega_{13} - 12\omega_{13} \omega_9 + 12\omega_6 \omega_9 + 12\omega_6 \omega_{13} \omega_9) \frac{c_s^2 \rho v_1}{6\omega_6^2 \omega_{13} \omega_9}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{MRT2}} = C_{D_x D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CLBM1}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CLBM2}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CuLBM1}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CuLBM2}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

coefficient $C_{D_x D_z^2 v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{MRT1}} = (2\omega_6 - \omega_6^2 + \omega_6 \omega_{18} - 2\omega_{18}) \frac{c_s^2 \rho v_3}{\omega_6^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_3}^{(1), \text{MRT2}} = C_{D_x D_z^2 v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CuLBM2}} = (6\omega_1\omega_2v_3^2 - 5\omega_1\omega_2^2 - 9c_s^2\omega_1^2\omega_2 - 14\omega_2^2v_3^2 - 2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 4\omega_1^2 + 9c_s^2\omega_1\omega_2^2 - 10c_s^2\omega_2^2 + 8c_s^2\omega_1^2 - 11\omega_1^2\omega_2v_3^2 + 2c_s^2\omega_1\omega_2 + 6\omega_2^2 + 8\omega_1^2v_3^2 + 11\omega_1\omega_2^2v_3^2) \frac{\rho v_3}{6\omega_1^2\omega_2^2}$$

coefficient $C_{D_y D_z^2 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_y D_z^2 v_1}^{(1), \text{MRT1}} = (-\omega_6\omega_8 + \omega_6\omega_5 + \omega_6^2 - \omega_6^2\omega_5 + \omega_6\omega_8\omega_5 - \omega_8\omega_5) \frac{c_s^2 \rho v_2}{\omega_6^2\omega_8\omega_5}$$

$$C_{D_y D_z^2 v_1}^{(1), \text{MRT2}} = C_{D_y D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y D_z^2 v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^2 v_1}^{(1), \text{CuLBM2}} = (-2\omega_3 - 6\omega_4c_s^2 - 2\omega_4v_2^2 - \omega_4\omega_1 + \omega_4\omega_1v_2^2 - 3\omega_3c_s^2\omega_1 + 2\omega_4 + \omega_3\omega_1 + 2\omega_3v_2^2 - \omega_3\omega_1v_2^2 + 6\omega_3c_s^2 + 3\omega_4c_s^2\omega_1) \frac{\rho v_2}{4\omega_3\omega_4\omega_1}$$

coefficient $C_{D_y D_z^2 v_2}^{(1)}$ **at** $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_2}^{(1), \text{SRT}} = \frac{-c_s^2 \rho v_1}{6}$$

$$C_{D_y D_z^2 v_2}^{(1), \text{MRT1}} = (-6\omega_6\omega_7\omega_5 - \omega_6\omega_7\omega_8\omega_5 + 6\omega_7\omega_5 - 6\omega_6\omega_8 + 6\omega_6\omega_7 + 6\omega_6\omega_8\omega_5 - 6\omega_8\omega_5) \frac{c_s^2 \rho v_1}{6\omega_6\omega_7\omega_8\omega_5}$$

$$C_{D_y D_z^2 v_2}^{(1), \text{MRT2}} = C_{D_y D_z^2 v_2}^{(1), \text{MRT1}}$$

$$C_{D_y D_z^2 v_2}^{(1), \text{CLBM1}} = C_{D_y D_z^2 v_2}^{(1), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(1), \text{CLBM2}} = C_{D_y D_z^2 v_2}^{(1), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(1), \text{CuLBM1}} = C_{D_y D_z^2 v_2}^{(1), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(1), \text{CuLBM2}} = C_{D_y D_z^2 v_2}^{(1), \text{SRT}}$$

coefficient $C_{D_z^3 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{D_z^3 \rho}^{(1), \text{SRT}} = (-1 + 3c_s^2 + v_3^2) \frac{v_1 v_3}{12}$$

$$C_{D_z^3 \rho}^{(1), \text{MRT1}} = (3\omega_6c_s^2\omega_{11}\omega_{18} - 6\omega_6\omega_{11} + 18\omega_6c_s^2\omega_{11} - 6\omega_6v_3^2\omega_{18} - 36c_s^2\omega_{11} + 12v_3^2\omega_{18} + 12\omega_{11} + 6\omega_6\omega_{11}v_3^2 + \omega_6\omega_{11}v_3^2\omega_{18} - 12\omega_{11}v_3^2 + 6\omega_6\omega_{18} - \omega_6\omega_{11}\omega_{18} - 12\omega_{18} - 18\omega_6c_s^2\omega_{18} + 36c_s^2\omega_{18}) \frac{v_1 v_3}{12\omega_6\omega_{11}\omega_{18}}$$

$$C_{D_z^3 \rho}^{(1), \text{MRT2}} = C_{D_z^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_z^3 \rho}^{(1), \text{CLBM1}} = C_{D_z^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(1), \text{CLBM2}} = C_{D_z^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(1), \text{CuLBM1}} = C_{D_z^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(1), \text{CuLBM2}} = C_{D_z^3 \rho}^{(1), \text{SRT}}$$

coefficient $C_{D_z^3 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_3^3}$:

$$C_{D_z^3 v_1}^{(1), \text{SRT}} = (6 + 18c_s^2\omega + \omega^2 + 6\omega v_3^2 - 3c_s^2\omega^2 - 6\omega - \omega^2 v_3^2 - 18c_s^2 - 6v_3^2) \frac{\rho v_3}{6\omega^2}$$

$$C_{D_z^3 v_1}^{(1), \text{MRT1}} = (3\omega_6^2 v_3^2 + 6\omega_6 - 3\omega_6^2 c_s^2 \omega_{18} + 3\omega_6^2 c_s^2 + 3\omega_6 v_3^2 \omega_{18} + \omega_6^2 \omega_{18} - 3\omega_6^2 - \omega_6^2 v_3^2 \omega_{18} - 6\omega_6 c_s^2 - 3\omega_6 \omega_{18} + 15\omega_6 c_s^2 \omega_{18} - 6\omega_6 v_3^2 - 12c_s^2 \omega_{18}) \frac{\rho v_3}{6\omega_6^2 \omega_{18}}$$

$$C_{D_z^3 v_1}^{(1), \text{MRT2}} = C_{D_z^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^3 v_1}^{(1), \text{CLBM1}} = (6 - 3\omega_6 - \omega_6 v_3^2 \omega_{18} + 3v_3^2 \omega_{18} + 9\omega_6 c_s^2 + \omega_6 \omega_{18} - 18c_s^2 - 3\omega_{18} - 3\omega_6 c_s^2 \omega_{18} + 3\omega_6 v_3^2 + 9c_s^2 \omega_{18} - 6v_3^2) \frac{\rho v_3}{6\omega_6 \omega_{18}}$$

$$C_{D_z^3 v_1}^{(1), \text{CLBM2}} = C_{D_z^3 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_z^3 v_1}^{(1), \text{CuLBM1}} = (6 + 9c_s^2 \omega_8 + \omega_8 \omega_2 + 3\omega_8 v_3^2 - 3\omega_8 - 3c_s^2 \omega_8 \omega_2 - 18c_s^2 - 3\omega_2 + 3\omega_2 v_3^2 + 9c_s^2 \omega_2 - \omega_8 \omega_2 v_3^2 - 6v_3^2) \frac{\rho v_3}{6\omega_8 \omega_2}$$

$$C_{D_z^3 v_1}^{(1), \text{CuLBM2}} = (6\omega_3 - 18\omega_4 c_s^2 - 3\omega_4 \omega_1 - 6\omega_3 \omega_4 c_s^2 \omega_1 + 3\omega_4 \omega_1 v_3^2 - 6\omega_4 v_3^2 + 9\omega_3 c_s^2 \omega_1 + 6\omega_4 - 3\omega_3 \omega_1 + 6\omega_3 \omega_4 v_3^2 + 2\omega_3 \omega_4 \omega_1 - 6\omega_3 v_3^2 - 6\omega_3 \omega_4 + 3\omega_3 \omega_1 v_3^2 + 18\omega_3 \omega_4 c_s^2 - 18\omega_3 c_s^2 - 2\omega_3 \omega_4 \omega_1 v_3^2 + 9\omega_4 c_s^2 \omega_1) \frac{\rho v_3}{12\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_z^3 v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_3^3}$:

$$C_{D_z^3 v_3}^{(1), \text{SRT}} = (-1 + c_s^2 + 3v_3^2) \frac{\rho v_1}{12}$$

$$C_{D_z^3 v_3}^{(1), \text{MRT1}} = (\omega_6 c_s^2 \omega_{11} \omega_{18} - 6\omega_6 \omega_{11} + 6\omega_6 c_s^2 \omega_{11} - 18\omega_6 v_3^2 \omega_{18} - 12c_s^2 \omega_{11} + 36v_3^2 \omega_{18} + 12\omega_{11} + 18\omega_6 \omega_{11} v_3^2 + 3\omega_6 \omega_{11} v_3^2 \omega_{18} - 36\omega_{11} v_3^2 - 6\omega_6 \omega_{18} - \omega_6 \omega_{11} \omega_{18} - 12\omega_{18} - 6\omega_6 c_s^2 \omega_{18} + 12c_s^2 \omega_{18}) \frac{\rho v_1}{12\omega_6 \omega_{11} \omega_{18}}$$

$$C_{D_z^3 v_3}^{(1), \text{MRT2}} = C_{D_z^3 v_3}^{(1), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(1), \text{CLBM1}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(1), \text{CLBM2}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(1), \text{CuLBM1}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(1), \text{CuLBM2}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

coefficient $C_{D_x^4 \rho}^{(1)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^4}$:

$$C_{D_x^4 \rho}^{(1), \text{SRT}} = (12 - 156v_1^2 + 10\omega^3 v_1^2 + 198c_s^2 \omega - 1008c_s^2 \omega v_1^2 - \omega^3 + 8\omega^2 + 6c_s^2 \omega^3 - 98\omega^2 v_1^2 + 672c_s^2 v_1^2 - 78c_s^2 \omega^2 + 144c_s^4 - 216\omega v_1^4 + 90\omega^2 v_1^4 - 18\omega - 34c_s^2 \omega^3 v_1^2 + 234\omega v_1^2 - 216c_s^4 \omega - 132c_s^2 - 9\omega^3 v_1^4 + 82c_s^4 \omega^2 + 144v_1^4 - 5c_s^4 \omega^3 + 404c_s^2 \omega^2 v_1^2) \frac{v_1}{12\omega^3}$$

$$C_{D_x^4 \rho}^{(1), \text{MRT1}} = (12 - 156v_1^2 - 216c_s^4 \omega_9 + 90v_1^4 \omega_9^2 + 404c_s^2 v_1^2 \omega_9^2 - 9v_1^4 \omega_9^3 - 34c_s^2 v_1^2 \omega_9^3 + 672c_s^2 v_1^2 - 5c_s^4 \omega_9^3 - 1008c_s^2 v_1^2 \omega_9 + 144c_s^4 + 82c_s^4 \omega_9^2 - 216v_1^4 \omega_9 + 8\omega_9^2 + 10v_1^2 \omega_9^3 + 198c_s^2 \omega_9 - 98v_1^2 \omega_9^2 - \omega_9^3 - 132c_s^2 + 144v_1^4 - 78c_s^2 \omega_9^2 + 234v_1^2 \omega_9 - 18\omega_9 + 6c_s^2 \omega_9^3) \frac{v_1}{12\omega_9^3}$$

$$C_{D_x^4 \rho}^{(1), \text{MRT2}} = C_{D_x^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(1), \text{CLBM1}} = C_{D_x^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(1), \text{CLBM2}} = C_{D_x^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(1), \text{CuLBM1}} = (12 - 156v_1^2 - 1008\omega_4 c_s^2 v_1^2 + 10\omega_4^3 v_1^2 + 198\omega_4 c_s^2 + 82\omega_4^2 c_s^4 - 98\omega_4^2 v_1^2 + 672c_s^2 v_1^2 - 18\omega_4 + 144c_s^4 - 216\omega_4 v_1^4 - 5\omega_4^3 c_s^4 - 34\omega_4^3 c_s^2 v_1^2 + 90\omega_4^2 v_1^4 - \omega_4^3 + 234\omega_4 v_1^2 + 6\omega_4^3 c_s^2 + 8\omega_4^2 - 132c_s^2 + 404\omega_4^2 c_s^2 v_1^2 - 9\omega_4^3 v_1^4 - 216\omega_4 c_s^4 + 144v_1^4 - 78\omega_4^2 c_s^2) \frac{v_1}{12\omega_4^3}$$

$$C_{D_x^4 \rho}^{(1), \text{CuLBM2}} = (-80\omega_3 c_s^2 \omega_1 \omega_2^2 - 10\omega_3 \omega_1^3 \omega_2 - 1472\omega_3 c_s^2 \omega_1 v_1^2 \omega_2^3 + 16\omega_3 \omega_1^2 \omega_2^3 - 48c_s^4 \omega_1^2 \omega_2^2 - 104\omega_3 \omega_1^2 v_1^2 \omega_2 + 168\omega_3 \omega_1 v_1^4 \omega_2^2 - 84\omega_3 \omega_1^3 v_1^4 \omega_2 - 464\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2 - 160\omega_3 v_1^2 \omega_2^3 - 16\omega_3 \omega_1^2 \omega_2^2 + 656\omega_3 c_s^2 \omega_1 v_1^2 \omega_2^2 + 320\omega_3 c_s^2 \omega_1 \omega_2^3 + 24c_s^4 \omega_1^3 \omega_2 - 52\omega_3 c_s^2 \omega_1^3 - 300\omega_3 \omega_1 v_1^4 \omega_2^3 + 16c_s^2 \omega_1^2 \omega_2^2 + 72\omega_3 c_s^4 \omega_1 \omega_2^2 - 27\omega_3 \omega_1^3 v_1^4 \omega_2^3 + 160\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2^2 + 8c_s^2 \omega_1 v_1^2 \omega_2^3 + 404\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2^2 - 196\omega_3 \omega_1^2 v_1^2 \omega_2^3 + 24\omega_3 \omega_1^3 v_1^4 + 8\omega_3 \omega_1^2 \omega_2 - 184\omega_3 c_s^2 \omega_2^3 - 3\omega_3 \omega_1^3 \omega_2^3 + 90\omega_3 \omega_1^3 v_1^4 \omega_2^2 - 372\omega_3 c_s^4 \omega_1 \omega_2^3 + 8c_s^2 \omega_1^3 v_1^2 \omega_2 - 8c_s^2 \omega_1^3 \omega_2 + 8\omega_3 \omega_1^3 \omega_2^2 + 280\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 102\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2^3 - 28\omega_3 \omega_1^3 v_1^2 + 144\omega_3 v_1^4 \omega_2^3 - 8c_s^2 \omega_1 \omega_2^3 - 156\omega_3 c_s^4 \omega_1^3 \omega_2 + 164\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^3 \omega_2^3 - 80\omega_3 c_s^2 \omega_1^2 \omega_2 + 440\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2 + 72\omega_3 c_s^4 \omega_1^3 + 328\omega_3 \omega_1 v_1^2 \omega_2^3 - 120\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 16c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 96\omega_3 \omega_1^2 v_1^4 \omega_2 - 176\omega_3 \omega_1 v_1^2 \omega_2^2 + 94\omega_3 \omega_1^3 v_1^2 \omega_2 - 78\omega_3 c_s^2 \omega_1^3 \omega_2^2 + 16\omega_3 \omega_2^3 + 808\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2^3 - 156\omega_3 c_s^2 \omega_1^2 \omega_2^3 -$$

$$98\omega_3\omega_1^3v_1^2\omega_2^2 + 8\omega_3\omega_1\omega_2^2 + 24c_s^4\omega_1\omega_2^3 + 122\omega_3c_s^2\omega_1^3\omega_2 + 72\omega_3c_s^4\omega_1^2\omega_2 - 15\omega_3c_s^4\omega_1^3\omega_2^3 + 4\omega_3\omega_1^3 - 264\omega_3\omega_1^2v_1^4\omega_2^2 - 28\omega_3\omega_1\omega_2^3 + 152\omega_3c_s^2\omega_1^2\omega_2^2 + 30\omega_3\omega_1^3v_1^2\omega_2^3 - 1088\omega_3c_s^2\omega_1^2v_1^2\omega_2^2 + 760\omega_3c_s^2v_1^2\omega_2^3 + 180\omega_3\omega_1^2v_1^4\omega_2^2 + 216\omega_3c_s^4\omega_1^3\omega_2^3 + 82\omega_3c_s^4\omega_1^3\omega_2^2) \frac{v_1}{36\omega_3\omega_1^3\omega_2^3}$$

coefficient $C_{D_x^4 v_1}^{(1)}$ at $\frac{\partial^4 v_1}{\partial x_1^4}$:

$$C_{D_x^4 v_1}^{(1), \text{SRT}} = (12 - 252v_1^2 + 14\omega^3v_1^2 + 54c_s^2\omega - 648c_s^2\omega v_1^2 - \omega^3 + 8\omega^2 + 2c_s^2\omega^3 - 154\omega^2v_1^2 + 432c_s^2v_1^2 - 22c_s^2\omega^2 + 24c_s^4 - 756\omega v_1^4 + 310\omega^2v_1^4 - 18\omega - 18c_s^2\omega^3v_1^2 + 378\omega v_1^2 - 36c_s^4\omega - 36c_s^2 - 29\omega^3v_1^4 + 14c_s^4\omega^2 + 504v_1^4 - c_s^4\omega^3 + 252c_s^2\omega^2v_1^2) \frac{\rho}{12\omega^3}$$

$$C_{D_x^4 v_1}^{(1), \text{MRT1}} = (12 - 252v_1^2 - 36c_s^4\omega_9 + 310v_1^4\omega_9^2 + 252c_s^2v_1^2\omega_9^2 - 29v_1^4\omega_9^3 - 18c_s^2v_1^2\omega_9^3 + 432c_s^2v_1^2 - c_s^4\omega_9^3 - 648c_s^2v_1^2\omega_9 + 24c_s^4 + 14c_s^4\omega_9^2 - 756v_1^4\omega_9 + 8\omega_9^2 + 14v_1^2\omega_9^3 + 54c_s^2\omega_9 - 154v_1^2\omega_9^2 - \omega_9^3 - 36c_s^2 + 504v_1^4 - 22c_s^2\omega_9^2 + 378v_1^2\omega_9 - 18\omega_9 + 2c_s^2\omega_9^3) \frac{\rho}{12\omega_9^3}$$

$$C_{D_x^4 v_1}^{(1), \text{MRT2}} = C_{D_x^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(1), \text{CLBM1}} = C_{D_x^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(1), \text{CLBM2}} = C_{D_x^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(1), \text{CuLBM1}} = (12 - 252v_1^2 - 648\omega_4c_s^2v_1^2 + 14\omega_4^3v_1^2 + 54\omega_4c_s^2 + 14\omega_4^2c_s^4 - 154\omega_4^2v_1^2 + 432c_s^2v_1^2 - 18\omega_4 + 24c_s^4 - 756\omega_4v_1^4 - \omega_4^3c_s^4 - 18\omega_4^3c_s^2v_1^2 + 310\omega_4^2v_1^4 - \omega_4^4 + 378\omega_4v_1^2 + 2\omega_4^3c_s^2 + 8\omega_4^2 - 36c_s^2 + 252\omega_4^2c_s^2v_1^2 - 29\omega_4^3v_1^4 - 36\omega_4c_s^4 + 504v_1^4 - 22\omega_4^2c_s^2) \frac{\rho}{12\omega_4^3}$$

$$C_{D_x^4 v_1}^{(1), \text{CuLBM2}} = (-16\omega_3c_s^2\omega_1\omega_2^2 - 10\omega_3\omega_1^3\omega_2 - 1008\omega_3c_s^2\omega_1v_1^2\omega_2^3 + 16\omega_3\omega_1^2\omega_2^3 - 16c_s^4\omega_1^2\omega_2^2 - 168\omega_3\omega_1^2v_1^2\omega_2 + 552\omega_3\omega_1v_1^4\omega_2^2 - 312\omega_3\omega_1^3v_1^4\omega_2 - 360\omega_3c_s^2\omega_1^3v_1^2\omega_2 - 288\omega_3v_1^2\omega_2^3 - 16\omega_3\omega_1^2\omega_2^2 + 336\omega_3c_s^2\omega_1v_1^2\omega_2^2 + 96\omega_3c_s^2\omega_1\omega_2^3 + 8c_s^4\omega_1^3\omega_2 - 20\omega_3c_s^2\omega_1^3 - 1068\omega_3\omega_1v_1^4\omega_2^3 + 16c_s^2\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_1\omega_2^2 - 87\omega_3\omega_1^3v_1^4\omega_2^3 + 144\omega_3c_s^2\omega_1^3v_1^2 - 24c_s^2\omega_1v_1^2\omega_2^3 + 252\omega_3c_s^2\omega_1^3v_1^2\omega_2^2 - 308\omega_3\omega_1^2v_1^2\omega_2^3 + 96\omega_3\omega_1^3v_1^4 + 8\omega_3\omega_1^2\omega_2 - 56\omega_3c_s^2\omega_2^3 - 3\omega_3\omega_1^3\omega_2^3 + 310\omega_3\omega_1^3v_1^4\omega_2^2 - 68\omega_3c_s^4\omega_1\omega_2^3 + 24c_s^2\omega_1^3v_1^2\omega_2 - 8c_s^2\omega_1^3\omega_2 + 8\omega_3\omega_1^3\omega_2^2 + 408\omega_3\omega_1^2v_1^2\omega_2^2 - 54\omega_3c_s^2\omega_1^3v_1^2\omega_2^3 - 60\omega_3\omega_1^3v_1^2 + 528\omega_3v_1^4\omega_2^3 - 8c_s^2\omega_1\omega_2^3 - 32\omega_3c_s^4\omega_1^3\omega_2 + 28\omega_3c_s^4\omega_1^2\omega_2^3 + 6\omega_3c_s^2\omega_1^3\omega_2^3 - 16\omega_3c_s^2\omega_1^2\omega_2 + 264\omega_3c_s^2\omega_1^2v_1^2\omega_2 + 16\omega_3c_s^4\omega_1^3 + 552\omega_3\omega_1v_1^2\omega_2^3 - 8\omega_3c_s^4\omega_1^2\omega_2^2 - 48c_s^2\omega_1^2v_1^2\omega_2^2 + 336\omega_3\omega_1^2v_1^2\omega_2 - 240\omega_3\omega_1v_1^2\omega_2^2 + 174\omega_3\omega_1^3v_1^2\omega_2 - 22\omega_3c_s^2\omega_1^3\omega_2^2 + 16\omega_3\omega_2^3 + 504\omega_3c_s^2\omega_1^2v_1^2\omega_2^3 - 44\omega_3c_s^2\omega_1^2\omega_2^3 - 154\omega_3\omega_1^3v_1^2\omega_2^2 + 8\omega_3\omega_1\omega_2^2 + 8c_s^4\omega_1\omega_2^3 + 42\omega_3c_s^2\omega_1^3\omega_2 + 8\omega_3c_s^4\omega_1^2\omega_2 - 3\omega_3c_s^4\omega_1^3\omega_2^3 + 4\omega_3\omega_1^3 - 888\omega_3\omega_1^2v_1^4\omega_2^2 - 28\omega_3\omega_1\omega_2^3 + 24\omega_3c_s^2\omega_1^2\omega_2^2 + 42\omega_3\omega_1^3v_1^2\omega_2^2 - 576\omega_3c_s^2\omega_1^2v_1^2\omega_2^2 + 552\omega_3c_s^2v_1^2\omega_2^3 + 620\omega_3\omega_1^2v_1^4\omega_2^2 + 40\omega_3c_s^4\omega_2^2 + 14\omega_3c_s^4\omega_1^3\omega_2^2) \frac{\rho}{36\omega_3\omega_1^3\omega_2^3}$$

coefficient $C_{D_x^3 D_y \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^3 D_y \rho}^{(1), \text{MRT1}} = (4c_s^2\omega_5^2\omega_9^2 - 4c_s^2\omega_9^2\omega_{12}^2 - 4c_s^4\omega_5^2\omega_3\omega_{12} + 4c_s^4\omega_5\omega_9\omega_{12}^2 - 48c_s^2v_1^2\omega_5\omega_9^2\omega_{12} - 8c_s^2\omega_5^2\omega_{12}^2 - 20v_1^4\omega_5\omega_9^2\omega_{12}^2 + 4c_s^4\omega_5^2\omega_9^2\omega_{12}^2 + 4c_s^2\omega_9^3\omega_{12} - 72c_s^2v_1^2\omega_5^2\omega_9\omega_{12} - 32v_1^2\omega_5^2\omega_9^2\omega_{12} - 4c_s^2\omega_5^2\omega_9^3 + 4v_1^2\omega_5\omega_9^3 + 20v_1^4\omega_5\omega_9^3\omega_{12} - 36v_1^4\omega_5^2\omega_9\omega_{12}^2 + 4c_s^2\omega_5^2\omega_9\omega_{12} - 24c_s^2v_1^2\omega_5\omega_9^3 - 4c_s^4\omega_5^2\omega_9^2 - 20v_1^4\omega_5^2\omega_9\omega_{12} + 12c_s^2\omega_5^2\omega_9\omega_{12}^2 + 4c_s^4\omega_9^2\omega_{12}^2 - 8c_s^2\omega_5\omega_9^3\omega_{12} + 8c_s^4\omega_5^2\omega_9^2\omega_{12} + 84c_s^2v_1^2\omega_5\omega_9^3\omega_{12} - 144c_s^2v_1^2\omega_5^2\omega_9\omega_{12} - 13v_1^2\omega_5^2\omega_9^2\omega_{12} + 8c_s^4\omega_5^2\omega_{12} - 4c_s^4\omega_5^3\omega_{12} + 8c_s^2\omega_5\omega_9^2\omega_{12}^2 + 4c_s^4\omega_5^2\omega_9^2 - 16v_1^4\omega_5\omega_9^2\omega_{12} - 4v_1^4\omega_5\omega_9^3 - 20v_1^2\omega_5\omega_9\omega_{12}^2 + 13v_1^2\omega_5^2\omega_9^3\omega_{12} - 84c_s^2v_1^2\omega_5\omega_9^2\omega_{12}^2 - 4c_s^2\omega_5\omega_9\omega_{12}^2 + 4c_s^2\omega_5^2\omega_9^3\omega_{12} + 36c_s^2v_1^2\omega_9^2\omega_{12} - 4c_s^4\omega_5\omega_9^3 - 24c_s^2v_1^2\omega_5^2\omega_9^2 + 96c_s^2v_1^2\omega_5^2\omega_{12}^2 + 4v_1^4\omega_5^2\omega_9^3 + 20v_1^2\omega_5\omega_9^3\omega_{12}^2 - 51c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12} + 72c_s^2v_1^2\omega_5\omega_9\omega_{12}^2 - 8v_1^4\omega_9^3\omega_{12} + 32v_1^4\omega_5^2\omega_9^2\omega_{12} + 24v_1^4\omega_5^2\omega_{12}^2 + 24c_s^2v_1^2\omega_5^2\omega_9^3 - 4c_s^2\omega_5^2\omega_9^2\omega_{12}^2 - 36c_s^2v_1^2\omega_9^3\omega_{12} + 51c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12}^2 - 4c_s^4\omega_5^2\omega_9\omega_{12} + 8v_1^4\omega_9^2\omega_{12}^2 - 4v_1^4\omega_5^2\omega_9^2 + 36v_1^2\omega_5\omega_9\omega_{12}^2 - 20v_1^2\omega_5\omega_9^3\omega_{12} + 120c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12} + 8c_s^4\omega_5\omega_9^3\omega_{12} - 12c_s^4\omega_5^2\omega_9\omega_{12}^2 + 4c_s^2\omega_5\omega_9^3 + 20v_1^2\omega_5^2\omega_9\omega_{12} + 13v_1^4\omega_5^2\omega_9^2\omega_{12} - 4v_1^2\omega_5^2\omega_9^3 - 8c_s^2\omega_5^2\omega_9^2\omega_{12} + 8v_1^2\omega_9^3\omega_{12} - 24v_1^2\omega_5^2\omega_{12}^2 + 16v_1^2\omega_5\omega_9^2\omega_{12} - 8c_s^4\omega_5\omega_9^2\omega_{12}^2 - 8v_1^2\omega_9^2\omega_{12}^2 - 13v_1^4\omega_5^2\omega_9^3\omega_{12} + 20v_1^4\omega_5\omega_9\omega_{12}^2 + 4v_1^2\omega_5^2\omega_9^2) \frac{v_2^3}{4\omega_5^2\omega_9^2\omega_{12}^2}$$

$$C_{D_x^3 D_y \rho}^{(1), \text{MRT2}} = C_{D_x^3 D_y \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CuLBM2}} = (8\omega_3^2\omega_1\omega_2^2 - 18\omega_3c_s^2\omega_1^2v_2^2\omega_2^3 + \omega_3^2\omega_1^2v_2^2\omega_2^3 - 60\omega_3\omega_1v_1^2\omega_2^3 - 24\omega_3\omega_1^2v_1^2v_2^2\omega_2^3 + 40\omega_3c_s^2\omega_1^2\omega_2 - 324\omega_3^2c_s^2\omega_1^3v_1^2\omega_2 - 84\omega_3^2c_s^4\omega_1^3\omega_2 - 6\omega_3^2c_s^4\omega_1^2\omega_2^3 + 12c_s^2\omega_3^2\omega_2^2 - 216\omega_3^2c_s^2\omega_1v_1^2\omega_2^2 - 2\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^2 + 84\omega_3^2\omega_1^3v_1^2\omega_2 + 8\omega_3^2v_2^2\omega_2^3 - 5\omega_3^2c_s^2\omega_1^3\omega_2^2 - 48\omega_3^2\omega_1^2v_1^2v_2^2\omega_2^2 + 48\omega_3^2\omega_1v_1^2\omega_2^2 + 36c_s^4\omega_1^2\omega_2^3 - 4\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 - 8\omega_3c_s^2\omega_1\omega_2^3 + 8\omega_3^2\omega_1\omega_2^3 + 4\omega_3^2\omega_1^2v_2^2\omega_2^2 + 16\omega_3^2c_s^2\omega_1^3v_2^2 - 2\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^3 - 36\omega_3^2c_s^4\omega_1^3 + 108\omega_3^2c_s^2\omega_1v_1^2\omega_2^3 - 48\omega_3^2\omega_1^3v_1^2v_2^2\omega_2 + 4\omega_3^2\omega_1^3 + 42\omega_3^2c_s^4\omega_1^2\omega_2^2 - 72\omega_3^2v_1^2v_2^2\omega_2^3 + 24\omega_3^2\omega_1^3v_1^2v_2^2\omega_2^2 + 24\omega_3^2\omega_1^3v_1^2v_2^2 + 72\omega_3^2\omega_1^2v_1^4\omega_2^2 + 48\omega_3^2v_1^4\omega_2^3 - 36\omega_3^2c_s^4\omega_1^2\omega_2 + 12c_s^2\omega_3^2\omega_1^2v_2^2\omega_2^3 - 48\omega_3^2\omega_1^3v_1^2 - 24\omega_3^2\omega_1^3v_1^2\omega_2^2 + 5\omega_3^2c_s^2\omega_1^2\omega_2^3 + 72\omega_3^2c_s^4\omega_1^3 + 56\omega_3^2c_s^2\omega_1^3\omega_2 - 8\omega_3^2\omega_2^3 + 24\omega_3^2\omega_1^2v_1^2v_2^2\omega_2 - 36c_s^4\omega_1^3\omega_2^2 + 4\omega_3^2\omega_1^2v_2^2\omega_2 + 6\omega_3^2c_s^2\omega_1^2\omega_2^2 + 72\omega_3^2c_s^2\omega_1^2v_1^2\omega_2^2 + 24\omega_3^2c_s^2\omega_1\omega_2^3 - 4\omega_3^2c_s^2\omega_1^2v_2^2\omega_2 - 12c_s^2\omega_1^2\omega_2^2 - 34\omega_3^2c_s^2\omega_1^2\omega_2^2 - 36\omega_3^2\omega_1^3v_1^2\omega_2 - 12\omega_3c_s^4\omega_1^3\omega_2 -$$

$$72\omega_3^2\omega_1v_1^4\omega_2^2 - 54\omega_3c_s^4\omega_1^2\omega_2^3 - 4\omega_3^2\omega_1^2\omega_2 - 24\omega_3^2\omega_1^2v_1^2\omega_2 + 20\omega_3^2c_s^2\omega_2^3 - 8\omega_3^2c_s^2\omega_1\omega_2^2 - \omega_3^2\omega_1^3v_2^2\omega_2^2 + 18\omega_3c_s^2\omega_1^3v_2^2\omega_2^2 + 96\omega_3^2\omega_1v_1^2v_2^2\omega_2^3 + 24\omega_3^2\omega_1^3v_1^4 - 12\omega_3c_s^4\omega_1^2\omega_2^2 - 36\omega_3^2\omega_1v_1^4\omega_2^3 + 2\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 - 4\omega_3^2\omega_1^3v_2 + 24\omega_3^2\omega_1v_1^2v_2^2\omega_2^2 - 22\omega_3^2c_s^2\omega_1\omega_2^3 - 20\omega_3^2c_s^2v_2^2\omega_2^3 - 18\omega_3c_s^2\omega_1^3\omega_2^2 + \omega_3^2\omega_1^3\omega_2^2 + 24\omega_3^2\omega_1^3v_1^2\omega_2^3 + 18\omega_3c_s^2\omega_1^2\omega_2^3 - \omega_3^2\omega_1^2\omega_2^3 + 8\omega_3c_s^2\omega_1v_2^2\omega_2^3 - 4\omega_3^2\omega_1^3\omega_2 + 4\omega_3c_s^2\omega_1^3\omega_2 - 8\omega_3^2\omega_1v_2^2\omega_2^3 - 12c_s^2\omega_1^3v_2^2\omega_2^2 + 8\omega_3^2c_s^2\omega_1v_2^2\omega_2^2 + 216\omega_3^2c_s^2\omega_1^3v_1^2 + 216\omega_3^2c_s^2\omega_1^2v_1^2\omega_2^2 - 20\omega_3^2c_s^2\omega_1^3v_2^2\omega_2 - 8\omega_3^2\omega_1v_2^2\omega_2^2 - 24\omega_3^2\omega_1^3v_1^2\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2^2 + 4\omega_3c_s^2\omega_1^2\omega_2^2 - 4\omega_3c_s^2\omega_1^3v_2^2\omega_2 + 24\omega_3^2v_1^2\omega_2^3 + 4\omega_3^2\omega_1^3v_2^2\omega_2 + 42\omega_3^2c_s^4\omega_1\omega_2^3 - 52\omega_3^2c_s^2\omega_1^3 - 72\omega_3^2c_s^2\omega_1^2v_1^2\omega_2^3 + 54\omega_3c_s^4\omega_1^3\omega_2^2 + 22\omega_3^2c_s^2\omega_1v_2^2\omega_2^3) \frac{v_2}{36\omega_3^3\omega_1^3\omega_2^3}$$

coefficient $C_{D_x^3 D_y v_1}^{(1)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x^3 D_y v_1}^{(1), \text{MRT1}} = (-16c_s^2\omega_5^2\omega_9^2 + 20c_s^2\omega_5^2\omega_{12}^2 + 28\omega_5\omega_9^2\omega_{12}^2 - 16c_s^2\omega_5\omega_9^2\omega_{12} + 48c_s^2\omega_5^2\omega_{12}^2 - 20c_s^2\omega_9^3\omega_{12} + 104v_1^2\omega_5^2\omega_9^2\omega_{12} + 16c_s^2\omega_5^2\omega_9^3 - 16v_1^7\omega_5\omega_9^3 + 48\omega_5^2\omega_9\omega_{12}^2 - 28\omega_5\omega_9^3\omega_{12} - 32c_s^2\omega_5^2\omega_9\omega_{12} + 24\omega_5^2\omega_9\omega_{12} - 72c_s^2\omega_5^2\omega_9\omega_{12}^2 + 44c_s^2\omega_5\omega_9^3\omega_{12} + 43v_1^7\omega_5^2\omega_9^2\omega_{12}^2 + 16\omega_5\omega_9^2\omega_{12} - 44c_s^2\omega_5\omega_9^2\omega_{12}^2 + 64v_1^7\omega_5\omega_9\omega_{12}^2 - 43v_1^7\omega_5^2\omega_9^3\omega_{12} + 8\omega_5\omega_9^3 + 32c_s^2\omega_5\omega_9\omega_{12}^2 - 25c_s^2\omega_5^2\omega_9^3\omega_{12} - 8\omega_5^2\omega_9^3 - 68v_1^7\omega_5\omega_9^2\omega_{12}^2 + 12\omega_9^3\omega_{12} - 32\omega_5^2\omega_{12}^2 + 25c_s^2\omega_5^2\omega_9^2\omega_{12} - 40\omega_5^2\omega_9^2\omega_{12} - 12\omega_9^2\omega_{12}^2 - 120v_1^7\omega_5^2\omega_9\omega_{12}^2 + 8\omega_5^2\omega_9^2 + 68v_1^7\omega_5\omega_9^3\omega_{12} - 16c_s^2\omega_5\omega_9^3 - 64v_1^7\omega_5^2\omega_9\omega_{12} + 16v_1^7\omega_5^2\omega_9^3 + 56c_s^2\omega_5^2\omega_9^2\omega_{12} - 28v_1^7\omega_9^3\omega_{12} - 17\omega_5^2\omega_9^2\omega_{12}^2 + 80v_1^7\omega_5^2\omega_{12}^2 - 48v_1^7\omega_5\omega_9^2\omega_{12} + 28v_1^7\omega_5^2\omega_{12}^2 - 24\omega_5\omega_9\omega_{12}^2 + 17\omega_5^2\omega_9\omega_{12} - 16v_1^7\omega_5^2\omega_9^2) \frac{\rho v_1 v_2}{4\omega_5^3\omega_9^3\omega_{12}^2}$$

$$C_{D_x^3 D_y v_1}^{(1), \text{MRT2}} = C_{D_x^3 D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CuLBM2}} = (-54\omega_3c_s^2\omega_1\omega_2^2 + 5\omega_3\omega_1^3v_2^2\omega_2^2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^3 - 12\omega_3\omega_1^2v_1^2\omega_2 - 6\omega_1^2v_2^2\omega_2^2 + 27c_s^2\omega_1^3\omega_2^2 + 84\omega_3v_1^2\omega_2^3 - 51\omega_3\omega_1^2\omega_2^2 + 27\omega_3c_s^2\omega_1\omega_2^3 - 12\omega_1\omega_2^3 + 84\omega_3c_s^2\omega_1^3 - 9\omega_1^2v_2^2\omega_2^3 - 18c_s^2\omega_1^2\omega_2^2 + 27\omega_3\omega_1v_2^2\omega_2^3 + 6\omega_3\omega_1^2\omega_2 - 12\omega_3c_s^2\omega_2^3 + 12\omega_3\omega_1^3v_2^2 - 18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^3 - 5\omega_3\omega_1^2\omega_2^2 - 18\omega_3\omega_1^3v_2^2\omega_2 + 6\omega_3\omega_1v_2^2\omega_2^2 + 132\omega_3\omega_1^2v_1^2\omega_2^2 + 48\omega_3\omega_1^3v_1^2 + 36c_s^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 - 5\omega_3\omega_1^2v_2^2\omega_2^3 - 66\omega_3\omega_1v_1^2\omega_2^3 - 9\omega_1^3\omega_2^2 + 9\omega_1^2v_2^2\omega_2^2 - 120\omega_3\omega_1v_1^2\omega_2^2 - 9\omega_3\omega_1^2v_2^2\omega_2^2 - 66\omega_3\omega_1^3v_1^2\omega_2 + 15\omega_3c_s^2\omega_1^3\omega_2^2 - 12\omega_3\omega_2^3 + 6\omega_3\omega_1^2v_2^2\omega_2 - 15\omega_3c_s^2\omega_1^2\omega_2^3 + 42\omega_3\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 + 6\omega_1^3\omega_2 + 9\omega_1^2\omega_2^2 - 6\omega_1^3v_2^2\omega_2 - 36\omega_3\omega_1^3 + 3\omega_3\omega_1\omega_2^3 + 81\omega_3c_s^2\omega_1^2\omega_2^2 - 24\omega_3v_2^2\omega_2^3 + 12\omega_1v_2^2\omega_2^3 + 6\omega_1^2\omega_2^2) \frac{\rho v_1 v_2}{18\omega_3\omega_1^3\omega_2^3}$$

coefficient $C_{D_x^3 D_y v_2}^{(1)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_2}^{(1), \text{SRT}} = (36v_1^2 - 4\omega^3v_1^2 + 36c_s^2\omega + 54c_s^2\omega v_1^2 + 26\omega^2v_1^2 - 36c_s^2v_1^2 - 12c_s^2\omega^2 + 36c_s^4 + 54\omega v_1^4 - 26\omega^2v_1^4 + 12c_s^2\omega^3v_1^2 - 54\omega v_1^2 - 54c_s^4\omega - 24c_s^2 + 4\omega^3v_1^4 + 20c_s^4\omega^2 - 36v_1^4 - c_s^4\omega^3 - 42c_s^2\omega^2v_1^2) \frac{\rho}{12\omega^3}$$

$$C_{D_x^3 D_y v_2}^{(1), \text{MRT1}} = (18v_1^2\omega_5^2\omega_9^3\omega_{12}^2 + 12c_s^4\omega_5^3\omega_{12}^2 + 60c_s^2v_1^2\omega_5^3\omega_9^2\omega_{12}^2 - 18c_s^4\omega_5^2\omega_9^3\omega_{12} + 90v_1^4\omega_5^3\omega_9\omega_{12}^2 + 60v_1^4\omega_5^3\omega_9^2\omega_{12} + 12c_s^4\omega_9^3\omega_{12}^2 - c_s^2\omega_5^3\omega_9^2\omega_{12}^2 + 6c_s^4\omega_5^2\omega_9^2\omega_{12}^2 + 102c_s^2v_1^2\omega_5\omega_9^3\omega_{12}^2 + 24v_1^2\omega_5^2\omega_9^2\omega_{12} - 21c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12} - 24v_1^4\omega_5\omega_9^3\omega_{12} - 6c_s^2\omega_5^3\omega_9^3\omega_{12} + 6c_s^2\omega_5\omega_9^3\omega_{12}^2 + 4v_1^4\omega_5^3\omega_9^3\omega_{12}^2 - 12c_s^2\omega_5^3\omega_{12}^2 + 12v_1^4\omega_5\omega_9^3\omega_{12}^2 + 12c_s^2\omega_5^2\omega_9\omega_{12}^2 - 27v_1^4\omega_5^2\omega_9^3\omega_{12} - 12c_s^2\omega_5\omega_9^3\omega_{12} + 12c_s^4\omega_5^2\omega_9^2\omega_{12} - 12c_s^2v_1^2\omega_5\omega_9^3\omega_{12} - 108c_s^2v_1^2\omega_5^2\omega_9\omega_{12}^2 - 12v_1^2\omega_5^2\omega_9^2\omega_{12}^2 + 12c_s^2v_1^2\omega_5^3\omega_9^2\omega_{12}^2 + 19v_1^4\omega_5^3\omega_9^2\omega_{12} + 6c_s^2\omega_5^3\omega_9^2\omega_{12} - 12c_s^4\omega_5^3\omega_9\omega_{12}^2 - 48v_1^2\omega_5^2\omega_9^3\omega_{12} + 54c_s^2v_1^2\omega_5^3\omega_9^2\omega_{12} + 36v_1^2\omega_5^3\omega_9\omega_{12} + 13c_s^4\omega_5^2\omega_9^2\omega_{12}^2 - 48c_s^2v_1^2\omega_5\omega_9^2\omega_{12}^2 - 90v_1^4\omega_5^2\omega_9\omega_{12}^2 + 18c_s^2\omega_5^2\omega_9^3\omega_{12} - 12v_1^2\omega_5^3\omega_9^3 - 18v_1^4\omega_5^2\omega_9^3\omega_{12} - 36c_s^2v_1^2\omega_5^3\omega_9\omega_{12} + c_s^4\omega_5^3\omega_9^2\omega_{12}^2 - 12v_1^4\omega_5^2\omega_9^3 + 30c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12} - 60v_1^2\omega_5^3\omega_9^2\omega_{12} - 24v_1^4\omega_5^2\omega_9^2\omega_{12} + 12v_1^2\omega_5^3\omega_9^2 - 12c_s^2v_1^2\omega_5^2\omega_9^3 - 6c_s^2\omega_5^2\omega_9^2\omega_{12}^2 + 162c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12}^2 - 4v_1^2\omega_5^3\omega_9^3\omega_{12}^2 - 24c_s^4\omega_5\omega_9^3\omega_{12}^2 - 72v_1^2\omega_5^3\omega_{12}^2 + 6c_s^4\omega_5^3\omega_9^3\omega_{12} + 24v_1^2\omega_5\omega_9^3\omega_{12} - 12c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12} + 12c_s^4\omega_5\omega_9^3\omega_{12} + 27v_1^2\omega_5^2\omega_9^3\omega_{12} - 12c_s^4\omega_5^2\omega_9\omega_{12}^2 - 12v_1^2\omega_5\omega_9^3\omega_{12}^2 + 12v_1^4\omega_5^3\omega_9^3 - c_s^4\omega_5^3\omega_9^3\omega_{12}^2 + 252c_s^2v_1^2\omega_5^3\omega_{12}^2 + 12v_1^4\omega_5^2\omega_9^2\omega_{12}^2 - 12c_s^2v_1^2\omega_5^3\omega_9^2 + 12v_1^2\omega_5^2\omega_9^3 - 12c_s^2\omega_5^2\omega_9^2\omega_{12}^2 - 48c_s^2v_1^2\omega_5^3\omega_{12}^2 - 306c_s^2v_1^2\omega_5^3\omega_9\omega_{12}^2 - 12v_1^4\omega_5^3\omega_9^2 - 6c_s^4\omega_5^3\omega_9^2\omega_{12}^2 - 81c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12}^2 - 19v_1^2\omega_5^3\omega_9^2\omega_{12}^2 - 5c_s^2\omega_5^2\omega_9^3\omega_{12}^2 - 36v_1^4\omega_5^3\omega_9\omega_{12} + 48v_1^4\omega_5^2\omega_9^3\omega_{12} + 12c_s^2\omega_5^3\omega_9\omega_{12}^2 + 12c_s^2v_1^2\omega_5^3\omega_9^2 + 72v_1^4\omega_5^3\omega_{12}^2) \frac{\rho}{12\omega_5^3\omega_9^3\omega_{12}^2}$$

$$C_{D_x^3 D_y v_2}^{(1), \text{MRT2}} = C_{D_x^3 D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_y v_2}^{(1), \text{CLBM1}} = (6v_1^2\omega_5^2\omega_9^3\omega_{12}^2 + 12c_s^4\omega_5^3\omega_{12}^2 + 60c_s^2v_1^2\omega_5^3\omega_9^2\omega_{12}^2 - 18c_s^4\omega_5^2\omega_9^3\omega_{12} + 90v_1^4\omega_5^3\omega_9\omega_{12}^2 + 72v_1^4\omega_5^3\omega_9^2\omega_{12} + 12c_s^4\omega_9^3\omega_{12}^2 - c_s^2\omega_5^3\omega_9^2\omega_{12}^2 + 6c_s^4\omega_5^2\omega_9^2\omega_{12}^2 - 18c_s^2v_1^2\omega_5\omega_9^3\omega_{12}^2 - 99c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12} - 6c_s^2\omega_5^3\omega_9^3\omega_{12} + 6c_s^2\omega_5\omega_9^3\omega_{12}^2 + 4v_1^4\omega_5^3\omega_9^3\omega_{12}^2 - 12c_s^2\omega_5^3\omega_{12}^2 + 12c_s^2\omega_5^2\omega_9\omega_{12}^2 - 39v_1^4\omega_5^3\omega_9^3\omega_{12} - 12c_s^2\omega_5\omega_9^3\omega_{12} + 12c_s^4\omega_5^2\omega_9^2\omega_{12} + 36c_s^2v_1^2\omega_5\omega_9^3\omega_{12} - 36c_s^2v_1^2\omega_5^2\omega_9\omega_{12}^2 + 12c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12}^2 + 19v_1^4\omega_5^3\omega_9^2\omega_{12} + 6c_s^2\omega_5^3\omega_9^2\omega_{12} - 12c_s^4\omega_5^3\omega_9\omega_{12}^2 - 36v_1^2\omega_5^3\omega_9^2\omega_{12} + 198c_s^2v_1^2\omega_5^3\omega_9\omega_{12} + 36v_1^2\omega_5^3\omega_9\omega_{12} + 13c_s^4\omega_5^2\omega_9^2\omega_{12}^2 - 90v_1^4\omega_5^2\omega_9^3\omega_{12} + 18c_s^2\omega_5^2\omega_9^3\omega_{12} - 12v_1^2\omega_5^3\omega_9^3 - 18v_1^4\omega_5^2\omega_9^3\omega_{12} - 36c_s^2v_1^2\omega_5^3\omega_9\omega_{12} + c_s^4\omega_5^3\omega_9^2\omega_{12}^2 - 12v_1^4\omega_5^2\omega_9^3 + 30c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12} - 60v_1^2\omega_5^3\omega_9^2\omega_{12} - 24c_s^4\omega_5\omega_9^3\omega_{12}^2 - 72v_1^2\omega_5^3\omega_{12}^2 + 6c_s^4\omega_5^3\omega_9^3\omega_{12} + 252c_s^2v_1^2\omega_5^3\omega_{12}^2 - 108c_s^2v_1^2\omega_5^3\omega_9^2 + 36v_1^2\omega_5^2\omega_9^3 - 12c_s^2\omega_5^2\omega_9^2\omega_{12}^2 - 306c_s^2v_1^2\omega_5^3\omega_9\omega_{12}^2 - 36v_1^4\omega_5^3\omega_9^2 - 6c_s^4\omega_5^3\omega_9^2\omega_{12}^2 - 3c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12}^2 - 19v_1^2\omega_5^3\omega_9^2\omega_{12}^2 - 5c_s^2\omega_5^2\omega_9^3\omega_{12}^2 - 36v_1^4\omega_5^3\omega_9\omega_{12} + 36v_1^4\omega_5^2\omega_9^3\omega_{12} + 12c_s^2\omega_5^3\omega_9\omega_{12}^2 + 108c_s^2v_1^2\omega_5^3\omega_9^2 + 72v_1^4\omega_5^3\omega_{12}^2) \frac{\rho}{12\omega_5^3\omega_9^3\omega_{12}^2}$$

$$C_{D_x^3 D_y v_2}^{(1), \text{CLBM2}} = C_{D_x^3 D_y v_2}^{(1), \text{CLBM1}}$$

$$C_{\text{D}_3\text{D}_{xy}v_2}^{(1), \text{CuLBMI}} = (18\omega_4^3 c_s^2 \omega_1^2 \omega_9 + \omega_2^2 c_s^5 \omega_1^3 \omega_9^2 - 90\omega_4 \omega_1^3 v_1^4 \omega_9^2 - 306\omega_4 c_s^2 \omega_3^3 v_1^2 \omega_9^2 - 36\omega_4^2 \omega_3^3 v_1^4 + 6\omega_3^4 c_s^4 \omega_3 \omega_9 - 6\omega_4^2 c_s^2 \omega_2^2 \omega_9^2 - 72\omega_3^3 v_1^2 \omega_9^2 + 54\omega_3^4 c_s^3 v_1^2 \omega_9 + 39\omega_3^3 \omega_1^3 v_1^2 \omega_9 + 36\omega_3^3 \omega_1^2 v_1^2 + 12\omega_4^2 c_s^4 \omega_2^2 \omega_9 + 12c_s^4 \omega_3^3 \omega_9^2 + 6\omega_4^2 c_s^2 \omega_1^3 \omega_9 + 13\omega_4^2 c_s^4 \omega_2^2 \omega_9^2 - 19\omega_2^2 \omega_1^3 v_1^2 \omega_9^2 + 36\omega_3^3 \omega_1^4 v_1 \omega_9 + 60\omega_4^2 c_s^2 \omega_1^3 v_1^2 \omega_9 - 18\omega_3^4 c_s^4 \omega_2^2 \omega_9 - \omega_4^2 c_s^5 \omega_3^3 \omega_9^2 - 72\omega_4^2 \omega_1^3 v_1^2 \omega_9 + 198\omega_4^2 c_s^2 \omega_1^3 v_1^2 \omega_9 - 6\omega_3^4 \omega_1^4 v_1 \omega_9^2 - 3\omega_4^2 c_s^2 \omega_1^2 v_1 \omega_9^2 + 12\omega_4^3 c_s^4 \omega_9^2 - 4\omega_4^3 \omega_1^3 v_1^2 \omega_9^2 - 6\omega_3^4 c_s^2 \omega_1^2 \omega_9 + 6\omega_4^2 c_s^4 \omega_1^2 \omega_9^2 - 12\omega_4^2 c_s^5 \omega_1^2 \omega_9 - \omega_4^3 c_s^5 \omega_1^3 \omega_9^2 + 252c_s^2 \omega_1^3 v_1^2 \omega_9^2 - 12c_s^2 \omega_3^3 \omega_9^2 - 36\omega_3^3 \omega_1^3 v_1^2 - 6\omega_4^2 c_s^4 \omega_3^3 \omega_9 - 5\omega_4^3 c_s^5 \omega_1^2 \omega_9^2 - 18\omega_4^2 c_s^3 \omega_1^2 v_1 \omega_9 - 36\omega_4^3 c_s^3 \omega_1^4 \omega_9 + 12\omega_4^2 c_s^2 \omega_1^2 \omega_9^2 - 39\omega_3^3 \omega_1^4 v_1 \omega_9 + 18\omega_2^2 \omega_1^3 v_1^2 \omega_9^2 + 6\omega_4^2 c_s^2 \omega_1^2 v_1 \omega_9^2 + 19\omega_2^2 \omega_1^3 v_1^2 \omega_9^2 - 99\omega_3^3 c_s^5 \omega_1^2 v_1 \omega_9^2 - 108\omega_4^2 c_s^3 \omega_1^2 \omega_9^2 - 12\omega_4^2 c_s^4 \omega_3^3 \omega_9^2 - 36\omega_4^3 c_s^3 \omega_1^2 \omega_9 + 36\omega_4^3 c_s^4 \omega_1^2 \omega_9 + 12\omega_4^2 c_s^5 \omega_1^2 \omega_9^2 + 108\omega_4^2 c_s^3 \omega_1^2 v_1^2 - 12\omega_4^2 c_s^4 \omega_1^2 \omega_9^2 - 24\omega_4^3 c_s^4 \omega_1 \omega_9^2 + 12\omega_4^2 c_s^2 \omega_1^3 \omega_9^2 + 36\omega_4 \omega_1^3 v_1^2 \omega_9 - 12\omega_4^2 c_s^2 \omega_1 \omega_9 + 12\omega_4^2 c_s^3 \omega_3^3 v_1^2 \omega_9^2 + 72\omega_4^3 v_1^4 \omega_9 + 6\omega_4^3 \omega_1^4 v_1 \omega_9^2 + 36\omega_4^2 c_s^2 \omega_1^4 v_1 \omega_9 - 108\omega_4^2 c_s^2 \omega_1^2 v_1^2 + 36\omega_4^2 c_s^2 \omega_1^2 v_1 \omega_9 + 4\omega_4^3 \omega_1^4 v_1 \omega_9^2 - 36\omega_4^3 \omega_1^4 v_1^2) \frac{\rho}{12\omega_4^3 \omega_1^3 \omega_9^2}$$

coefficient $C_{D_x^2 D_y^2 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2}$:

[illegible]

$$\begin{aligned}
& 180c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 12c_s^2\omega_5^3v_2^2\omega_{15}\omega_9^2\omega_{12} + 12c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 - 18c_s^2v_1^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 12\omega_5^2v_2^2\omega_{21}\omega_9^2\omega_{12}^2 - 12c_s^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - \\
& 36v_1^2\omega_5^2v_2^2\omega_{15}\omega_9^3\omega_{12}^2 - 12c_s^4\omega_5^2\omega_{21}\omega_9^2\omega_{12}^2 - 84c_s^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 108v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12c_s^4\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - \\
& 36v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 36c_s^2v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 + 24\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 18c_s^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 6c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2 - 36c_s^2v_1^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} + \\
& 12\omega_5^2v_2^2\omega_{15}\omega_9^3\omega_{12}^2 + 12c_s^2\omega_5^2\omega_{21}\omega_9^2\omega_{12}^2 + 6c_s^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 6c_s^4\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2 - 132c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 18c_s^4\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + \\
& 6c_s^2\omega_5^3v_2^2\omega_{15}\omega_9^3\omega_{12}^2 - 12\omega_5^2v_2^2\omega_{15}\omega_9^3\omega_{12}^2 + 18c_s^2v_1^2\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2 - 12\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_{12}^2 + 24c_s^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 6c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - \\
& 72v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 42c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2\omega_5^3v_2^2\omega_{15}\omega_9^3\omega_{12} + 36v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_{12}^2 + 36v_1^2\omega_5^2v_2^2\omega_{15}\omega_9^3\omega_{12} + \\
& 6c_s^4\omega_5^3\omega_9^2\omega_{12} + 6c_s^4\omega_5^2\omega_{21}\omega_9^2\omega_{12} + 12c_s^4\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2\omega_5^3v_2^2\omega_{15}\omega_9^3\omega_{12} + 36v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_{12}^2 + 36v_1^2\omega_5^2v_2^2\omega_{15}\omega_9^3\omega_{12} + \\
& 24c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 24c_s^4\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 54v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 6c_s^2\omega_5^3\omega_{21}\omega_9^2\omega_{12}^2 + 72c_s^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 12c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + \\
& 12\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36c_s^2v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 60c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9^3 + \\
& 24\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 6c_s^4\omega_5^3\omega_{15}\omega_9^3\omega_{12}^2 - 12\omega_5^2v_2^2\omega_9^3\omega_{12}^2 - 6c_s^2\omega_5^3v_2^2\omega_{15}\omega_9^2\omega_{12}^2 - 12c_s^4\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 12c_s^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + \\
& 36c_s^2v_1^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 6c_s^4\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 36c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12}^2 - 12c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 36v_1^2\omega_5^2v_2^2\omega_9^3\omega_{12}^2 + 72v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + \\
& 18c_s^2v_1^2\omega_5^3\omega_{21}\omega_9^2\omega_{12}^2 - 12c_s^2\omega_5^2\omega_9^3\omega_{12}^2 - 12\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9^3 - 6c_s^2\omega_5^3\omega_{15}\omega_9^3\omega_{12}^2 - 36v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 84c_s^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 - \\
& 24c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 12c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 + 18\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 24c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^3) \frac{\rho}{12\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2}
\end{aligned}$$

$$C_{D_x^2 D_y^2 v_1}^{(1), \text{MRT}^2} = C_{D_x^2 D_y^2 v_1}^{(1), \text{MRT}^1}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 v_1}^{(1), \text{CLBM}^1} = & (-12c_s^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 36v_1^2\omega_5^3\omega_{15}\omega_9 + 6\omega_5^3\omega_9^2\omega_{12} - 12c_s^2\omega_5^2\omega_{21}\omega_9\omega_{12} + 36v_1^2\omega_5^2\omega_9^2\omega_{12} + 6c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 24c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2 - \\
& 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + 12c_s^2\omega_5^2\omega_{15}\omega_9^2 - 6\omega_5^3\omega_{15}\omega_9^2\omega_{12} - 6c_s^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 18v_1^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} - 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2 - 12\omega_5^3\omega_{15}\omega_9^2 + \\
& 6c_s^2\omega_5^2\omega_{21}\omega_9\omega_{12} - 36v_1^2\omega_5^2\omega_{15}\omega_9\omega_{12} - c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 36v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^2 + 12\omega_5^2\omega_{15}\omega_9^2\omega_{12} - 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} + 12c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - \\
& 12\omega_5\omega_{21}\omega_{15}\omega_9^2 + 6\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 24c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 6c_s^2\omega_5^3\omega_9^2\omega_{12} - 18v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 36v_1^2\omega_5^3\omega_{15}\omega_9^2 - 12\omega_5^3\omega_{15}\omega_9 - \\
& 12c_s^2\omega_5^3\omega_{15}\omega_9^2 - 4c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 36v_1^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 18v_1^2\omega_5^3\omega_9^2\omega_{12} + 36v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2 - 36v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} - \\
& 6\omega_5^3\omega_{21}\omega_9\omega_{12} - 12\omega_5^3\omega_{21}\omega_{15}\omega_9^2 + 12\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 72v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 18v_1^2\omega_5^3\omega_{21}\omega_9\omega_{12} - 12\omega_5^2\omega_9^2\omega_{12} - 12c_s^2\omega_5^2\omega_{15}\omega_9^2\omega_{12} - \\
& 6c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^2 - 12\omega_5^2\omega_{21}\omega_{15}\omega_9 - 24\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 18c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 36v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 36v_1^2\omega_5^2\omega_{21}\omega_9\omega_{12} + \\
& 36v_1^2\omega_5^2\omega_{15}\omega_9^2 + 24\omega_5^2\omega_{21}\omega_{15}\omega_9^2 - 6\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 12\omega_5^2\omega_{21}\omega_9\omega_{12} - 72v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2 + 18v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 6\omega_5^3\omega_{15}\omega_9\omega_{12} - \\
& 36v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 18v_1^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 12c_s^2\omega_5^2\omega_9^2\omega_{12} + 12\omega_5^3\omega_{21}\omega_{15}\omega_9 + 6c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 12\omega_5^3\omega_{15}\omega_9^2 + 12c_s^2\omega_5^3\omega_{15}\omega_9) \frac{c_s^2\rho}{12\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12}}
\end{aligned}$$

$$C_{D_x^2 D_y^2 v_1}^{(1), \text{CLBM}^2} = C_{D_x^2 D_y^2 v_1}^{(1), \text{CLBM}^1}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 v_1}^{(1), \text{CuLBM}^1} = & (-72\omega_4\omega_1^3v_1^2 - 12\omega_4c_s^2\omega_1\omega_9 + 24\omega_4\omega_1^3 + 12\omega_4^2c_s^2\omega_1 - 12\omega_4^2c_s^2\omega_9 - \omega_4^2c_s^2\omega_1^3\omega_9 - 24\omega_4\omega_1^2 - 12c_s^2\omega_1^2\omega_9 + 12\omega_4\omega_1\omega_9 + \\
& 72\omega_4\omega_1^2v_1^2 - 24\omega_4^2c_s^2\omega_1^2 + 36\omega_1^3v_1^2 - 4\omega_4^2c_s^2\omega_1^2\omega_9 + 36\omega_4\omega_1^2v_1^2\omega_9 + 36\omega_4^2\omega_1v_1^2 + 12\omega_4^2c_s^2\omega_1^3 + 18\omega_4^2c_s^2\omega_1\omega_9 - 72\omega_4^2\omega_1^2v_1^2 + 24\omega_4c_s^2\omega_1^2 - 12\omega_4^2\omega_1 - \\
& 12\omega_4\omega_1^2\omega_9 - 36\omega_4\omega_1v_1^2\omega_9 - 24\omega_4c_s^2\omega_1^3 - 12\omega_1^3 + 36\omega_4^2\omega_1^3v_1^2 + 24\omega_4^2\omega_1^2 - 36\omega_1^2v_1^2\omega_9 + 12c_s^2\omega_1^3 + 12\omega_4c_s^2\omega_1^2\omega_9 + 12\omega_1^2\omega_9 - 12\omega_4^2\omega_1^3) \frac{c_s^2\rho}{12\omega_4^2\omega_1^3\omega_9}
\end{aligned}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 v_1}^{(1), \text{CuLBM}^2} = & (54\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 + 18\omega_3\omega_1^3v_2^2\omega_2^2 + 24\omega_3^2\omega_4\omega_1^3v_2^4 + 18\omega_3^2\omega_1^2v_2^2\omega_2^3 + 76\omega_3^2\omega_4c_s^4\omega_1\omega_2^3 + 4\omega_3^2\omega_4\omega_1^3 + \omega_3^2\omega_4\omega_1^3v_1^4\omega_2^2 - 18\omega_3^2c_s^2\omega_3^3\omega_2^3 + \\
& 12\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 - 6\omega_3\omega_4\omega_1v_2^3\omega_2^3 + 150\omega_3^2\omega_4c_s^2\omega_1v_2^3\omega_2^3 - 24\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^2 + 36\omega_3^2\omega_4\omega_1v_2^2\omega_2^2 - 6\omega_3^2\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 - 72\omega_3^2c_s^4\omega_1^2\omega_2^3 + 18\omega_4\omega_1^3v_2^2\omega_2^3 + \\
& 66\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 - 54\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^2 + 90\omega_3\omega_4c_s^2\omega_1^3v_2^3\omega_2^3 + 12\omega_3^2\omega_4c_s^2\omega_1^3v_1^2 - 28\omega_3^2\omega_4c_s^4\omega_1\omega_2^2 + 54\omega_4c_s^2\omega_1^2v_2^2\omega_2^3 + 18\omega_3^2\omega_1^2v_2^2\omega_2^3 + 18\omega_4\omega_1^2v_2^4\omega_2^3 + \\
& 16\omega_3^2\omega_4c_s^4\omega_1^3 + 12\omega_3\omega_4\omega_1^3v_2^2\omega_2 - 54\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^3 + 216\omega_3^2c_s^2\omega_1v_2^3\omega_2^3 + 8\omega_3\omega_4c_s^4\omega_1\omega_2^3 - 174\omega_3^2\omega_4c_s^2\omega_1^3v_2^2\omega_2 - 12\omega_3^2\omega_4\omega_1^3v_1^2 + 18\omega_3\omega_1^2v_2^4\omega_2^3 + \\
& 66\omega_3^2\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 - 24\omega_3^2\omega_4\omega_1v_2^3\omega_2^3 + 18\omega_3^2\omega_1^3v_2^3\omega_2^3 + \omega_3^2\omega_4\omega_1^2v_2^3\omega_2^3 - 12\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_2^2 - 18\omega_3^2\omega_4c_s^2\omega_1\omega_2^3 + 30\omega_3^2\omega_4c_s^2\omega_1^3v_2^2\omega_2^2 + \\
& 6\omega_3\omega_4\omega_1^2v_2^4\omega_2^2 - 48\omega_3^2\omega_4c_s^2\omega_1^2v_1^2\omega_2 + 18\omega_3^2c_s^4\omega_1^3\omega_2^3 + 54\omega_3^2c_s^2\omega_1^2v_1^2\omega_2^3 - 108\omega_3^2\omega_4c_s^2v_2^2\omega_2^3 - 68\omega_3^2\omega_4c_s^4\omega_2^3 - 36\omega_3\omega_4c_s^2\omega_1^2v_2^2\omega_2 + 72\omega_3^2c_s^2\omega_1^2\omega_2^3 - \\
& 4\omega_3^2\omega_4\omega_1\omega_2^3 - 9\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^3 + 12\omega_3^2\omega_4v_2^2\omega_2^3 - 144\omega_3^2\omega_4\omega_1v_1^2v_2^2\omega_2^3 - 36\omega_3\omega_4\omega_1^3v_2^2\omega_2^3 + 132\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 + 12\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^2 - \\
& 36\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 + 4\omega_3^2\omega_4\omega_2^3 + 18\omega_3^2\omega_1v_2^4\omega_2^3 - 9\omega_3^2\omega_4\omega_1^3v_2^3\omega_2^2 + 32\omega_3^2\omega_4c_s^2\omega_1\omega_2^3 - 126\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 - 8\omega_3\omega_4c_s^2\omega_1\omega_2^3 - 90\omega_3^2\omega_4\omega_1v_1^2v_2^2\omega_2^3 - \\
& 18\omega_3\omega_4c_s^2\omega_1v_2^2\omega_2^3 - 18\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1\omega_2^2 - 12\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_2 - 96\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^3 - 36\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^3 + 18\omega_3\omega_4c_s^4\omega_1^3\omega_2^3 - 18\omega_4\omega_1^2v_2^2\omega_2^3 - \\
& 20\omega_3^2\omega_4c_s^2\omega_1^3 - 18\omega_3^2\omega_1^2v_2^4\omega_2^2 - 12\omega_3\omega_4\omega_1^3v_2^4\omega_2 + 6\omega_3^2\omega_4c_s^2\omega_1^3v_1^2\omega_2^2 - 12\omega_3^2\omega_4v_1^2\omega_2^3 - 8\omega_3\omega_4c_s^2\omega_1^3\omega_2 + 2\omega_3^2\omega_4c_s^4\omega_1^3\omega_2^3 + 54\omega_3\omega_4c_s^2\omega_1^2v_2^2\omega_2^2 + \\
& 36\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 + 24\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2 - 18\omega_3^2\omega_3^3v_2^2\omega_2^2 - 54\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 - 18\omega_3\omega_1^3v_2^2\omega_2^3 + 54\omega_3^2\omega_4\omega_1v_2^2\omega_2^3 - \omega_3^2\omega_4\omega_1^2v_1^4\omega_2^3 + 8\omega_3^2\omega_4\omega_1^2\omega_2^2 + \\
& 18\omega_3^2\omega_4c_s^2\omega_1^3\omega_2 - 18\omega_3^2\omega_1^2v_2^4\omega_2^3 - 18\omega_3\omega_1^3v_2^4\omega_2^3 - 36\omega_3\omega_4c_s^4\omega_1^3\omega_2^3 - \omega_3^2\omega_4\omega_1^3v_1^2\omega_2^2 + 2\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^3 + 54\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^3 + 6\omega_3\omega_4\omega_1v_2^4\omega_2^3 + \\
& 72\omega_3^2\omega_4\omega_1^3v_2^2\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2 - 72\omega_3^2c_s^2\omega_1\omega_2^3 - 18\omega_4\omega_1^3v_2^2\omega_2^2 - 36\omega_3^2\omega_4\omega_1^2v_1^2v_2^2\omega_2 + 12\omega_3^2\omega_4\omega_1v_2^2\omega_2^2 + 108\omega_3^2\omega_4v_1^2v_2^2\omega_2^3 - 54\omega_4c_s^2\omega_1^3v_2^2\omega_2^2 - \\
& 56\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 - 90\omega_3\omega_4c_s^2\omega_1^2v_2^2\omega_2^3 - 3\omega_3^2\omega_4c_s^4\omega_1^3\omega_2^3 + 60\omega_3\omega_4c_s^2\omega_1v_1^2\omega_2^3 - 28\omega_3^2\omega_4c_s^4\omega_1^2\omega_2 - 36\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 + 180\omega_3^2\omega_4\omega_1v_1^2v_2^2\omega_2^2 + \\
& 54\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2^3 + 132\omega_3^2\omega_4c_s^2\omega_1^3v_2^2 + 36\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 - 18\omega_3\omega_4c_s^2\omega_1^3\omega_2^3 + 9\omega_3^2\omega_4\omega_1^3v_2^2\omega_2^2 + 28\omega_3^2\omega_4c_s^4\omega_1^2\omega_2^2 - 18\omega_3^2\omega_1v_2^2\omega_2^3 - \\
& 36\omega_3\omega_4c_s^4\omega_1^2\omega_2^3 - 48\omega_3^2\omega_4\omega_1^3v_2^2 - 2\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^2 + 12\omega_3^2\omega_4\omega_1^3v_1^2\omega_2 + 8\omega_3\omega_4c_s^4\omega_1^3\omega_2 - 42\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^2 + 48\omega_3^2\omega_4c_s^2\omega_1v_1^2\omega_2^3 - \\
& 90\omega_3^2\omega_4\omega_1^3v_1^2v_2^2\omega_2 - 30\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_2^3 + 12\omega_3^2\omega_4\omega_1v_1^2\omega_2 - 14\omega_3^2\omega_4c_s^4\omega_1^2\omega_2^3 + 36\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 - 14\omega_3^2\omega_4c_s^4\omega_1^3\omega_2 - 6\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 - \\
& 90\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2^2 + 28\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^3 - 4\omega_3^2\omega_4\omega_1^2\omega_2 + 72\omega_3^2c_s^4\omega_1\omega_2^3 + 12\omega_3^2\omega_4\omega_1v_1^2\omega_2^3 + 24\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_2^2 - 84\omega_3^2\omega_4c_s^2\omega_1v_1^2\omega_2^2 + 9\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^3 - \\
& 48\omega_3^2\omega_4v_2^2\omega_2^3 - 216\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^3 + 32\omega_3^2\omega_4c_s^2\omega_1^2\omega_2 - 6\omega_3^2\omega_4c_s^2\omega_1^3v_2^2\omega_2 + 36\omega_3\omega_4\omega_1^3v_2^4\omega_2^2 + 54\omega_3^2c_s^2\omega_1v_2^2\omega_2^3 + 56\omega_3\omega_4c_s^4\omega_1^2\omega_2^2) \frac{\rho}{36\omega_3^2\omega_4\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y^2 v_2}^{(1), \text{MRT}^1} = & (-5\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2 - 5\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 2\omega_{10}v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 4\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3 + \\
& 2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 9\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 4\omega_{10}v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 + 2\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 3\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} -
\end{aligned}$$

$$\begin{aligned}
& 4w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3 - 6w_{10}v_7^2w_5w_{21}w_{15}w_9^3w_{12} - 4w_{10}c_s^2w_5^3w_{15}w_9^3w_{12} + 2w_{10}w_5^3w_{15}w_9^3w_{12} - 7w_{10}w_5^3w_{21}w_{15}w_9^3w_{12} - 4w_{10}c_s^2w_5^3w_{15}w_9^3w_{12} + \\
& 8w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 3w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 4w_{10}w_5^3w_{15}w_9^3w_{12}^2 + 4w_{10}c_s^2w_5^3w_{15}w_9^3w_{12}^2 - \\
& 2w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12} - 4w_{10}w_5^3w_{21}w_{15}w_9^3w_{12} + 13w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12} + 2w_{10}v_7^2w_5w_{21}w_{15}w_9^3w_{12} - w_{10}w_5^3w_{21}w_{15}w_9^3w_{12} - 4c_s^2w_5w_{21}w_{15}w_9^3w_{12}^2 + \\
& 12w_{10}c_s^2w_5w_{21}w_{15}w_9^3w_{12}^2 + 2w_{10}c_s^2w_5^3w_{15}w_9^3w_{12}^2 - 4w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 4w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 2w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + \\
& 2c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 24w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 4w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 2w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 + w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 3w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 + \\
& 4w_{10}c_s^2w_5^3w_{15}w_9^3w_{12}^2 - 2c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 8w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 16w_{10}c_s^2w_{21}w_{15}w_9^3w_{12}^2 + 3w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 + \\
& 2w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}w_5^3w_{15}w_9^3w_{12}^2 + 26w_{10}c_s^2w_5w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}w_5^3w_{15}w_9^3w_{12}^2 - 2w_{10}c_s^2w_5^3w_{15}w_9^3w_{12}^2 + \\
& 4w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 + 7w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 6w_{10}w_5w_{21}w_{15}w_9^3w_{12}^2 + 4c_s^2w_5w_{21}w_{15}w_9^3w_{12}^2 - 8w_{10}c_s^2w_5w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 - \\
& 2w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 9w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 2w_{10}w_5w_{21}w_{15}w_9^3w_{12}^2 - 8w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 8w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + \\
& 6w_{10}c_s^2w_5^3w_{15}w_9^3w_{12}^2 + 5w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 2w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 - 8w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 15w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 4w_{10}w_5^3w_{15}w_9^3w_{12}^2 - \\
& 2w_{10}c_s^2w_5w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 3w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 4w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 - 4w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 + \\
& 11w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 2w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 12w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 6w_{10}w_5^3w_5w_{21}w_{15}w_9^3w_{12}^2 - \\
& 2w_{10}w_5^3w_{15}w_9^3w_{12}^2 + w_{10}v_7^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 2w_{10}v_7^2w_5^3w_{15}w_9^3w_{12}^2 - 2w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 4w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 - 2w_{10}w_5w_{21}w_{15}w_9^3w_{12}^2 + \\
& 8w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 2w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}^2 - w_{10}c_s^2w_5^3w_{21}w_{15}w_9^3w_{12}^2 + 4w_{10}c_s^2w_5^3w_{15}w_9^3w_{12}^2 - 4w_{10}w_5^3w_{15}w_9^3w_{12}^2) \frac{\rho v_1 v_2}{2w_{10}w_5^3w_{21}w_{15}w_9^3w_{12}}
\end{aligned}$$

coefficient $C_{D_x D_y^3 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$:

$$6\omega_{10}\omega_5^3\omega_{15}\omega_9\omega_{12} + 6\omega_{10}\omega_5^3\omega_9\omega_{12} - 3\omega_{10}\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 18\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12}) \frac{c_s^2\rho}{12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CLBM2}} = C_{D_x D_y^3 v_2}^{(1), \text{CLBM1}}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CuLBM1}} = (-12\omega_7 c_s^2 \omega_1 + 3\omega_7 \omega_1^3 v_2^2 - 6\omega_3^3 \omega_5 + 12c_s^2 \omega_1 \omega_5 - 54\omega_1^2 \omega_5 v_2^2 + 18\omega_7 c_s^2 \omega_1 \omega_5 - 3\omega_7 \omega_1^2 \omega_5 v_2^2 + 18\omega_7 \omega_1^2 v_2^2 + \omega_7 c_s^2 \omega_1^3 + 18\omega_1^2 \omega_5 + 6\omega_7 c_s^2 \omega_1^2 + 18\omega_1^3 \omega_5 v_2^2 + 6c_s^2 \omega_1^3 \omega_5 - 12\omega_1^2 - 12\omega_1 \omega_5 - 12\omega_7 c_s^2 \omega_5 - 5\omega_7 c_s^2 \omega_1^2 \omega_5 + 12\omega_7 \omega_1 - 18\omega_1^3 v_2^2 + 6\omega_1^3 - 36\omega_7 \omega_1 v_2^2 - 6\omega_7 \omega_1^2 + 12c_s^2 \omega_1^2 + \omega_7 \omega_1^2 \omega_5 - 18c_s^2 \omega_1^2 \omega_5 - 6c_s^2 \omega_1^3 + 36\omega_1^2 v_2^2 - \omega_7 \omega_1^3 + 36\omega_1 \omega_5 v_2^2 - \omega_7 c_s^2 \omega_1^3 \omega_5) \frac{c_s^2 \rho}{12\omega_7 \omega_1^3 \omega_5}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CuLBM2}} = (60\omega_4 c_s^2 \omega_1^2 v_2^2 \omega_2^2 - 108\omega_3 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 4\omega_3 \omega_4 \omega_1^2 \omega_2^2 - 222\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^3 + \omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2^3 - 20\omega_3 \omega_4 c_s^2 \omega_1^3 - 28\omega_3 \omega_4 c_s^4 \omega_1 \omega_2^3 + 153\omega_3 \omega_4 c_s^2 \omega_1^3 v_2^2 \omega_2^2 + 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 - 7\omega_3 \omega_4 \omega_1^2 \omega_2^3 - 10\omega_3 \omega_4 \omega_1^3 \omega_2 - 54\omega_4 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 36\omega_3 c_s^2 \omega_1 \omega_2^3 + 138\omega_3 \omega_4 \omega_1^3 v_2^2 \omega_2 + 94\omega_3 \omega_4 c_s^4 \omega_1 \omega_2^3 + \omega_3 \omega_4 \omega_1^3 v_4^2 \omega_2^2 - 8\omega_4 c_s^2 \omega_1 \omega_2^3 + 192\omega_3 \omega_4 \omega_1^2 v_2^4 \omega_2 - 168\omega_3 \omega_4 \omega_1^2 v_2^4 \omega_2^2 - 60\omega_3 \omega_4 \omega_1^3 v_2^2 - 288\omega_3 \omega_4 c_s^2 \omega_1^3 v_2^2 \omega_2 - 60\omega_3 \omega_4 c_s^2 \omega_1 v_2^2 \omega_2^2 + 32\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 81\omega_3 \omega_4 \omega_1^3 v_2^2 \omega_2^2 + 7\omega_3 \omega_4 \omega_1^3 \omega_2^2 - 264\omega_3 \omega_4 v_2^4 \omega_2^3 - 138\omega_3 \omega_4 \omega_1^2 v_2^4 \omega_2^3 + 36\omega_3 c_s^4 \omega_1 \omega_2^3 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 54\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^3 + 40\omega_3 \omega_4 c_s^2 \omega_2^3 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 + 432\omega_3 \omega_4 c_s^2 \omega_1 v_2^2 \omega_2^3 - 312\omega_3 \omega_4 c_s^2 v_2^2 \omega_2^3 + 8\omega_4 c_s^4 \omega_1 \omega_2^3 - 24\omega_3 \omega_4 \omega_1 v_2^4 \omega_2^2 - 9\omega_4 c_s^2 \omega_1^3 \omega_2^3 - 3\omega_3 \omega_4 c_s^4 \omega_1^3 \omega_2^3 + 8\omega_3 \omega_4 c_s^4 \omega_1^2 \omega_2 - 240\omega_3 \omega_4 \omega_1^3 v_2^4 \omega_2 - 36\omega_3 c_s^4 \omega_1^2 \omega_2^3 - 9\omega_3 c_s^2 \omega_1^3 \omega_2^3 + 42\omega_3 \omega_4 c_s^2 \omega_1^3 \omega_2 - 90\omega_3 \omega_4 c_s^2 \omega_1^2 v_2^2 \omega_2^2 + 24\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^3 - \omega_3 \omega_4 \omega_1^3 v_1^2 \omega_2^2 - 96\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 - 18\omega_4 c_s^4 \omega_1^2 \omega_2^3 + 27\omega_4 c_s^2 \omega_1^3 v_2^2 \omega_2^3 + 96\omega_3 \omega_4 \omega_1^3 v_2^4 + 8\omega_4 c_s^4 \omega_1^3 \omega_2 + 17\omega_3 \omega_4 c_s^4 \omega_1^3 \omega_2^2 + 408\omega_3 \omega_4 \omega_1 v_2^4 \omega_2^3 + 18\omega_4 c_s^2 \omega_1^3 \omega_2^2 - 8\omega_3 \omega_4 \omega_2^3 - \omega_3 \omega_4 \omega_1^2 v_1^4 \omega_2^3 + 20\omega_4 c_s^4 \omega_1^2 \omega_2^2 - 54\omega_4 c_s^2 \omega_1^3 v_2^2 \omega_2^2 + 27\omega_3 c_s^2 \omega_1^3 v_2^2 \omega_2^3 + 16\omega_3 \omega_4 c_s^4 \omega_1^3 - 6\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 153\omega_3 \omega_4 c_s^2 \omega_1^2 v_2^2 \omega_2^3 + 9\omega_4 c_s^4 \omega_1^3 \omega_2^3 + 144\omega_3 \omega_4 v_2^2 \omega_2^3 + 24\omega_4 c_s^2 \omega_1^3 v_2^2 \omega_2 - 81\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2^3 - 16\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1^3 + 36\omega_3 c_s^2 \omega_1^2 \omega_2^3 + 108\omega_3 c_s^2 \omega_1 v_2^2 \omega_2^3 + 14\omega_3 \omega_4 \omega_1 \omega_2^3 - 29\omega_3 \omega_4 c_s^4 \omega_1^2 \omega_2^3 + 9\omega_3 c_s^4 \omega_1^3 \omega_2^3 - 68\omega_3 \omega_4 c_s^4 \omega_2^3 + 32\omega_3 \omega_4 c_s^4 \omega_1^2 \omega_2 - 8\omega_4 c_s^2 \omega_1^3 \omega_2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^3 + 24\omega_4 c_s^2 \omega_1 v_2^2 \omega_2^3 - 24\omega_3 \omega_4 c_s^2 \omega_1^3 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2^2 + 120\omega_3 \omega_4 c_s^2 \omega_1^2 v_2^2 \omega_2 + 84\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2^2 + 3\omega_3 \omega_4 c_s^2 \omega_1^3 v_1^2 \omega_2^2 - 18\omega_4 c_s^4 \omega_1^3 \omega_2^2 - 20\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 144\omega_3 \omega_4 c_s^2 \omega_1^3 v_2^2 + 138\omega_3 \omega_4 \omega_1^3 v_2^2 \omega_2^2 + 10\omega_3 \omega_4 c_s^4 \omega_1^2 \omega_2^2) \frac{\rho}{36\omega_3 \omega_4 \omega_1^3 \omega_2^3}$$

$$\text{coefficient } C_{D_y^4 \rho}^{(1)} \text{ at } \frac{\partial^4 \rho}{\partial x^2}:$$

$$C_{D_y^4 \rho}^{(1), \text{SRT}} = (c_s^2 \omega + 6v_2^4 + 3\omega v_2^2 + 2c_s^4 - 3\omega v_2^4 + 24c_s^2 v_2^2 - c_s^4 \omega - 2c_s^2 - 6v_2^2 - 12c_s^2 \omega v_2^2) \frac{v_1}{24\omega}$$

$$C_{D_y^4 \rho}^{(1), \text{MRT1}} = (-96\omega_{10}^2 \omega_5 v_2^2 \omega_{15} - 144\omega_{10}^2 c_s^2 \omega_5 v_2^2 + 72\omega_{10} c_s^2 \omega_5^2 v_2^2 \omega_{15} - 216\omega_{10}^2 c_s^2 v_2^2 \omega_{15} - 12\omega_{10}^2 \omega_5^2 v_2^2 - 3\omega_{10}^2 \omega_5^2 v_2^4 \omega_{15} - 48\omega_{10}^2 c_s^2 \omega_5 \omega_{15} - 36\omega_{10} \omega_5^2 v_2^2 \omega_{15}^2 - 24\omega_{10}^2 \omega_5 v_2^4 - 14\omega_{10} c_s^2 \omega_5^2 \omega_{15}^2 + 12c_s^2 \omega_5^2 \omega_{15}^2 - 48\omega_{10} \omega_5 v_2^4 \omega_{15} - 126\omega_{10}^2 c_s^2 \omega_5^2 v_2^2 \omega_{15} + 36\omega_5^2 v_2^2 \omega_{15}^2 + 12\omega_{10}^2 c_s^4 \omega_5^2 - 48\omega_{10}^2 v_2^4 \omega_{15} - 12\omega_{10}^2 c_s^2 \omega_5^2 v_2^2 \omega_{15}^2 + 24\omega_{10} c_s^4 \omega_{15}^2 - 144c_s^2 \omega_5^2 v_2^2 \omega_{15}^2 - 96\omega_{10} \omega_5 v_2^4 \omega_{15}^2 - 24\omega_{10}^2 c_s^4 \omega_5 + 72\omega_5 v_2^4 \omega_{15}^2 + 24\omega_{10} c_s^2 \omega_{15} - 24\omega_{10} \omega_5^2 v_2^2 \omega_{15} - 48\omega_{10} v_2^2 \omega_{15}^2 + 48\omega_{10}^2 c_s^4 \omega_5 \omega_{15} + 14\omega_{10} c_s^4 \omega_5^2 \omega_{15} - 30\omega_{10}^2 \omega_5^2 v_2^4 \omega_{15} - 12c_s^4 \omega_5^2 \omega_{15} + 150\omega_{10} c_s^2 \omega_5^2 v_2^2 \omega_{15}^2 - 12\omega_{10}^2 c_s^4 \omega_5^2 \omega_{15} + 288c_s^2 \omega_5^2 v_2^2 \omega_{15}^2 + 36\omega_{10} \omega_5^2 v_2^4 \omega_{15} - 48\omega_{10} c_s^2 \omega_5 \omega_{15}^2 + 24c_s^4 \omega_5 \omega_{15}^2 + 48\omega_{10} \omega_5 v_2^4 \omega_{15} - 36\omega_5^2 v_2^4 \omega_{15} - 12\omega_{10}^2 c_s^2 \omega_5^2 + 96\omega_{10}^2 \omega_5 v_2^4 \omega_{15} + \omega_{10}^2 c_s^2 \omega_5^2 \omega_{15}^2 - 432\omega_{10} c_s^2 \omega_5 v_2^2 \omega_{15}^2 + 3\omega_{10}^2 \omega_5^2 v_2^2 \omega_{15}^2 - 144\omega_{10} c_s^2 \omega_5 v_2^2 \omega_{15} + 12\omega_{10}^2 c_s^2 \omega_5^2 \omega_{15} + 48\omega_{10} c_s^2 \omega_5 \omega_{15}^2 + 12\omega_{10}^2 \omega_5^2 v_2^4 + 30\omega_{10}^2 \omega_5^2 v_2^2 \omega_{15} - 24c_s^2 \omega_5 \omega_{15}^2 + 72\omega_{10}^2 c_s^2 \omega_5^2 v_2^2 + 48\omega_{10}^2 v_2^2 \omega_{15} + 96\omega_{10} \omega_5 v_2^2 \omega_{15}^2 - 24\omega_{10} c_s^2 \omega_{15}^2 + 24\omega_{10}^2 c_s^2 \omega_5 - 72\omega_5 v_2^2 \omega_{15}^2 + 216\omega_{10} c_s^2 v_2^2 \omega_{15}^2 - \omega_{10}^2 c_s^4 \omega_5^2 \omega_{15}^2 + 24\omega_{10} \omega_5^2 v_2^4 \omega_{15} - 24\omega_{10}^2 c_s^4 \omega_{15} + 432\omega_{10}^2 c_s^2 \omega_5 v_2^2 \omega_{15} + 24\omega_{10}^2 \omega_5 v_2^2 + 48\omega_{10} v_2^4 \omega_{15}^2) \frac{v_1}{24\omega_{10}^2 \omega_5^2 \omega_{15}^2}$$

$$C_{D_y^4 \rho}^{(1), \text{MRT2}} = C_{D_y^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(1), \text{CLBM1}} = (6v_2^4 - 3\omega_{10} v_2^4 - \omega_{10} c_s^4 + 2c_s^4 + \omega_{10} c_s^2 + 24c_s^2 v_2^2 - 12\omega_{10} c_s^2 v_2^2 - 2c_s^2 - 6v_2^2 + 3\omega_{10} v_2^2) \frac{v_1}{24\omega_{10}}$$

$$C_{D_y^4 \rho}^{(1), \text{CLBM2}} = C_{D_y^4 \rho}^{(1), \text{CLBM1}}$$

$$C_{D_y^4 \rho}^{(1), \text{CuLBM1}} = (c_s^2 \omega_5 + 6v_2^4 + 3\omega_5 v_2^2 + 2c_s^4 - 12c_s^2 \omega_5 v_2^2 - c_s^4 \omega_5 + 24c_s^2 v_2^2 - 2c_s^2 - 6v_2^2 - 3\omega_5 v_2^4) \frac{v_1}{24\omega_5}$$

$$C_{D_y^4 \rho}^{(1), \text{CuLBM2}} = (-6\omega_1 v_2^2 - 9\omega_1 v_2^4 \omega_2 + 2c_s^4 \omega_1 - 12v_2^2 \omega_2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 9\omega_1 v_2^2 \omega_2 + 24c_s^2 \omega_1 v_2^2 - 2c_s^2 \omega_1 + 12v_2^4 \omega_2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 36c_s^2 \omega_1 v_2^2 \omega_2 + 48c_s^2 v_2^2 \omega_2 + 6\omega_1 v_2^4) \frac{v_1}{72\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x^2}:$$

$$C_{D_y v_1}^{(1), \text{SRT}} = (-84c_s^2 \omega^2 v_2^2 + 36c_s^2 \omega + 3\omega^3 v_2^4 - 72v_2^4 + c_s^2 \omega^3 - 108\omega v_2^2 + 6c_s^2 \omega^3 v_2^2 - 14c_s^2 \omega^2 + 48c_s^4 - 42\omega^2 v_2^4 + 108\omega v_2^4 + 42\omega^2 v_2^2 - 144c_s^2 v_2^2 - 72c_s^4 \omega - 24c_s^2 + 30c_s^4 \omega^2 + 72v_2^2 - 3c_s^4 \omega^3 + 216c_s^2 \omega v_2^2 - 3\omega^3 v_2^2) \frac{\rho}{24\omega^3}$$

$$C_{D_y v_1}^{(1), \text{MRT1}} = (-24c_s^4 \omega_5^2 \omega_{15} - 24\omega_5^2 v_2^4 - 6c_s^2 \omega_5^3 \omega_{15} - 48\omega_5 v_2^4 \omega_{15} - 3c_s^4 \omega_5^3 \omega_{15}^2 + 3\omega_5^3 v_2^4 \omega_{15}^2 - 8c_s^2 \omega_5^2 \omega_{15}^2 + 48c_s^2 \omega_5^2 v_2^2 \omega_{15} + 12c_s^2 \omega_5^3 v_2^2 + 24\omega_5^2 v_2^2 \omega_{15}^2 + 24c_s^2 \omega_5^2 \omega_{15} + 24c_s^4 \omega_{15}^2 - 72c_s^2 \omega_5^2 v_2^2 \omega_{15}^2 - 72\omega_5^2 v_2^2 \omega_{15} + 12\omega_5^3 v_2^4 + 24\omega_5 v_2^4 \omega_{15}^2 - 18\omega_5^3 v_2^4 \omega_{15} + 6c_s^4 \omega_5^3 \omega_{15} - 24c_s^2 \omega_5^2 v_2^2 + c_s^2 \omega_5^3 \omega_{15}^2 + 24c_s^4 \omega_5^2 \omega_{15}^2 - 12\omega_5^3 v_2^2 + 48\omega_5 v_2^2 \omega_{15} + 156c_s^2 \omega_5 v_2^2 \omega_{15}^2 - 3\omega_5^3 v_2^2 \omega_{15}^2 - 12c_s^2 \omega_5^3 v_2^2 \omega_{15} - 48c_s^4 \omega_5 \omega_{15}^2 - 24\omega_5^2 v_2^4 \omega_{15}^2 - 24c_s^2 \omega_5 \omega_{15} + 12c_s^2 \omega_5 \omega_{15}^2 + 24\omega_5^2 v_2^2 + 24c_s^4 \omega_5 \omega_{15} - 96c_s^2 v_2^2 \omega_{15}^2 + 72\omega_5^2 v_2^4 \omega_{15} - 24\omega_5 v_2^2 \omega_{15}^2 - 24c_s^2 \omega_5 v_2^2 \omega_{15} + 18\omega_5^3 v_2^2 \omega_{15} + 6c_s^2 \omega_5^3 v_2^2 \omega_{15}^2) \frac{\rho}{24\omega_5^3 \omega_{15}^2}$$

$$C_{D_y v_1}^{(1), \text{MRT2}} = C_{D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^4 v_1}^{(1), \text{CLBM1}} = (-24c_s^4 \omega_5 \omega_{15} - 72\omega_5^2 v_2^4 - 6c_s^2 \omega_5^3 \omega_{15} - 3c_s^4 \omega_5^2 \omega_{15}^2 + 3\omega_5^3 v_2^4 \omega_{15} - 8c_s^2 \omega_5^2 \omega_{15}^2 + 144c_s^2 \omega_5^2 v_2^2 \omega_{15} + 108c_s^2 \omega_5^3 v_2^2 + 12\omega_5^2 v_2^2 \omega_{15}^2 + 24c_s^2 \omega_5^2 \omega_{15} + 24c_s^4 \omega_{15}^2 - 12c_s^2 \omega_5^2 v_2^2 \omega_{15} - 72\omega_5^2 v_2^2 \omega_{15} + 36\omega_5^3 v_2^4 - 30\omega_5^3 v_2^4 \omega_{15} + 6c_s^4 \omega_5^3 \omega_{15} - 216c_s^2 \omega_5^2 v_2^2 + c_s^2 \omega_5^3 \omega_{15} + 24c_s^4 \omega_5^2 \omega_{15} - 36\omega_5^3 v_2^2 - 36c_s^2 \omega_5^2 v_2^2 \omega_{15} - 3\omega_5^3 v_2^2 \omega_{15} - 72c_s^2 \omega_5^3 v_2^2 \omega_{15} - 48c_s^4 \omega_5^2 \omega_{15} - 12\omega_5^2 v_2^4 \omega_{15} - 24c_s^2 \omega_5 \omega_{15} + 12c_s^2 \omega_5 \omega_{15}^2 + 72\omega_5^2 v_2^2 + 24c_s^4 \omega_5 \omega_{15} + 72\omega_5^2 v_2^4 \omega_{15} + 72c_s^2 \omega_5^2 v_2^2 \omega_{15} + 30\omega_5^3 v_2^2 \omega_{15} + 6c_s^2 \omega_5^2 v_2^2 \omega_{15}^2) \frac{\rho}{24\omega_5^2 \omega_{15}^2}$$

$$C_{D_y^4 v_1}^{(1), \text{CLBM2}} = C_{D_y^4 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_y^4 v_1}^{(1), \text{CuLBM1}} = (-24\omega_7 c_s^2 \omega_1 + 30\omega_7 \omega_1^3 v_2^2 + 108c_s^2 \omega_1^3 v_2^2 + 3\omega_7^2 \omega_1^3 v_2^4 + 24\omega_7^2 c_s^4 \omega_1^2 - 3\omega_7^2 c_s^4 \omega_1^3 + 144\omega_7 c_s^2 \omega_1^2 v_2^2 - 72\omega_1^2 v_2^4 - 12\omega_7^2 \omega_1^2 v_2^4 - 36\omega_7^2 c_s^2 \omega_1 v_2^2 - 216c_s^2 \omega_1^2 v_2^2 - 72\omega_7 \omega_1^2 v_2^2 - 6\omega_7 c_s^2 \omega_1^3 - 72\omega_7 c_s^2 \omega_1^3 v_2^2 + 36\omega_1^3 v_2^4 - 48\omega_7^2 c_s^4 \omega_1 + 24\omega_7 c_s^2 \omega_1^2 + 72\omega_7 \omega_1^2 v_2^4 + \omega_7^2 c_s^2 \omega_1^3 + 12\omega_7^2 \omega_1^2 v_2^2 - 12\omega_7^2 c_s^2 \omega_1^2 v_2^2 + 24\omega_7 c_s^2 \omega_1 - 36\omega_1^2 v_2^2 - 8\omega_7^2 c_s^2 \omega_1^2 + 12\omega_7^2 c_s^2 \omega_1 - 3\omega_7^2 \omega_1^3 v_2^2 - 24\omega_7 c_s^4 \omega_1^2 - 30\omega_7 \omega_1^3 v_2^2 + 24\omega_7^2 c_s^4 + 72\omega_7 c_s^2 \omega_1 v_2^2 + 72\omega_1^2 v_2^2 + 6\omega_7^2 c_s^2 \omega_1^2 v_2^2 + 6\omega_7 c_s^4 \omega_1^3) \frac{\rho}{24\omega_7^2 \omega_1^3}$$

$$C_{D_y^4 v_1}^{(1), \text{CuLBM2}} = (-12\omega_3^2 \omega_4 c_s^4 \omega_1^2 - 15\omega_3^2 \omega_4 \omega_1^3 v_2^4 - 12\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_2^2 + 36\omega_3 \omega_4^2 \omega_1^2 v_2^4 + 36\omega_3 \omega_4 \omega_1^2 v_2^2 - 3\omega_3^2 \omega_4^2 \omega_1^3 v_2^2 + 12\omega_3^2 \omega_4^2 c_s^2 \omega_1 - 9\omega_1^2 \omega_3^3 v_2^2 - 18\omega_3^2 \omega_1^2 v_2^4 + 12\omega_3 \omega_4^2 c_s^4 \omega_1 + 27\omega_4^2 c_s^2 \omega_1^3 v_2^2 + 3\omega_3^2 \omega_4 c_s^4 \omega_1^3 + 27\omega_3^2 c_s^2 \omega_1^3 v_2^2 + 24\omega_3^2 \omega_4^2 c_s^4 + 72\omega_3 \omega_4^2 c_s^2 \omega_1^2 v_2^2 + \omega_3^2 \omega_4^2 c_s^2 \omega_1^3 + 12\omega_3^2 \omega_4^2 \omega_1^2 v_2^2 - 18\omega_3 \omega_4 \omega_1^3 v_2^2 - 15\omega_3 \omega_4^2 \omega_1^3 v_2^4 - 12\omega_3 \omega_4^2 c_s^4 \omega_1^2 + 36\omega_3^2 \omega_4 \omega_1^2 v_2^4 + 6\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 v_2^2 - 54\omega_3^2 c_s^2 \omega_1^2 v_2^2 - 36\omega_3 \omega_4^2 c_s^2 \omega_1^2 v_2^2 - 8\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 + 12\omega_3^2 \omega_4^2 c_s^4 \omega_1 + 9\omega_3^2 \omega_1^3 v_2^4 + 18\omega_1^2 \omega_3^3 v_2^2 + 36\omega_3^2 \omega_4 c_s^2 \omega_1 v_2^2 + 3\omega_3 \omega_4^2 c_s^4 \omega_1^3 - 54\omega_4^2 c_s^2 \omega_1^3 v_2^2 - 12\omega_3 \omega_4^2 c_s^2 \omega_1 + 15\omega_3 \omega_4^2 \omega_1^3 v_2^2 - 36\omega_3^2 \omega_4 \omega_1^2 v_2^2 - 3\omega_3^2 \omega_4 c_s^2 \omega_1^3 - 12\omega_3^2 \omega_4^2 \omega_1^2 v_2^4 + 18\omega_3 \omega_4 \omega_1^3 v_2^4 + 72\omega_3^2 \omega_4 c_s^2 \omega_1^2 v_2^2 + 12\omega_3^2 \omega_4 c_s^2 \omega_1^2 - 18\omega_4^2 \omega_1^2 v_2^4 - 9\omega_3^2 \omega_1^3 v_2^2 - 108\omega_3 \omega_4 c_s^2 \omega_1^2 v_2^2 - 48\omega_3^2 \omega_4 c_s^4 \omega_1 - 36\omega_3 \omega_4 \omega_1^2 v_2^4 - 36\omega_3^2 \omega_4 c_s^2 \omega_1^2 v_2^2 + 3\omega_3^2 \omega_1^3 v_2^4 + 24\omega_3^2 \omega_4^2 c_s^4 \omega_1^2 + 36\omega_3 \omega_4^2 c_s^2 \omega_1 v_2^2 + 15\omega_3^2 \omega_4 \omega_1^3 v_2^2 - 12\omega_3^2 \omega_4 c_s^2 \omega_1 - 3\omega_3 \omega_4^2 c_s^2 \omega_1^3 - 36\omega_3 \omega_4^2 \omega_1^2 v_2^2 - 3\omega_3^2 \omega_4^2 c_s^4 \omega_1^3 - 36\omega_3^2 \omega_4^2 c_s^2 \omega_1 v_2^2 + 18\omega_3^2 \omega_1^3 v_2^2 + 9\omega_4^2 \omega_1^3 v_2^4 + 12\omega_3 \omega_4^2 c_s^2 \omega_1^2 + 54\omega_3 \omega_4 c_s^2 \omega_1^3 v_2^2) \frac{\rho}{24\omega_3^2 \omega_4^2 \omega_1^3}$$

$$\text{coefficient } C_{D_y^4 v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^4} :$$

$$C_{D_y^4 v_2}^{(1), \text{SRT}} = (-4 - 3c_s^2 \omega - 5\omega v_2^2 + 2\omega + 6c_s^2 + 10v_2^2) \frac{\rho v_1 v_2}{12\omega^2}$$

$$C_{D_y^4 v_2}^{(1), \text{MRT1}} = (168\omega_{10}^2 \omega_5 v_2^2 \omega_{15} + 24\omega_{10} \omega_5 \omega_{15} + 24\omega_{10}^2 \omega_5^2 v_2^2 + 120\omega_{10}^2 c_s^2 \omega_5 \omega_{15} + 61\omega_{10} \omega_5^2 v_2^2 \omega_{15}^2 + 36\omega_{10}^2 \omega_{15} + 39\omega_{10} c_s^2 \omega_5^2 \omega_{15}^2 - 36c_s^2 \omega_5^2 \omega_{15}^2 - 60\omega_{10}^2 \omega_5^2 \omega_{15}^2 + 21\omega_{10}^2 \omega_5^2 \omega_{15} + 2\omega_{10}^2 \omega_5^2 \omega_{15}^2 - 60\omega_{10}^2 c_s^2 \omega_{15} + 36\omega_{10} \omega_5^2 v_2^2 \omega_{15} + 12\omega_{10} c_s^2 \omega_5^2 \omega_{15} + 84\omega_{10} v_2^2 \omega_{15}^2 + 72\omega_{10} \omega_5 \omega_{15}^2 - 48\omega_5 \omega_{15}^2 - 25\omega_{10} \omega_5^2 \omega_{15} + 24\omega_5^2 \omega_{15} + 24\omega_{10}^2 \omega_5 - 72\omega_{10} \omega_5 v_2^2 \omega_{15} + 24\omega_{10}^2 c_s^2 \omega_5^2 - 3\omega_{10}^2 c_s^2 \omega_5^2 \omega_{15}^2 - 24\omega_{10} c_s^2 \omega_5 \omega_{15} - 36\omega_{10} \omega_{15}^2 - 5\omega_{10}^2 \omega_5^2 v_2^2 \omega_{15}^2 - 33\omega_{10}^2 c_s^2 \omega_5^2 \omega_{15} - 120\omega_{10} c_s^2 \omega_5 \omega_{15}^2 - 51\omega_{10}^2 \omega_5^2 v_2^2 \omega_{15} + 72c_s^2 \omega_5 \omega_{15}^2 - 72\omega_{10}^2 \omega_5 \omega_{15} - 12\omega_{10}^2 \omega_5^2 - 84\omega_{10}^2 v_2^2 \omega_{15} - 168\omega_{10} \omega_5 v_2^2 \omega_{15}^2 + 60\omega_{10} c_s^2 \omega_{15}^2 - 48\omega_{10}^2 c_s^2 \omega_5 + 120\omega_5 v_2^2 \omega_{15}^2 - 12\omega_{10} \omega_5^2 \omega_{15} - 48\omega_{10}^2 \omega_5 v_2^2) \frac{\rho v_1 v_2}{12\omega_{10}^2 \omega_5^2 \omega_{15}^2}$$

$$C_{D_y^4 v_2}^{(1), \text{MRT2}} = C_{D_y^4 v_2}^{(1), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(1), \text{CLBM1}} = (-4 + 2\omega_{10} - 3\omega_{10} c_s^2 + 6c_s^2 + 10v_2^2 - 5\omega_{10} v_2^2) \frac{\rho v_1 v_2}{12\omega_{10}}$$

$$C_{D_y^4 v_2}^{(1), \text{CLBM2}} = C_{D_y^4 v_2}^{(1), \text{CLBM1}}$$

$$C_{D_y^4 v_2}^{(1), \text{CuLBM1}} = (-4 - 3c_s^2 \omega_5 - 5\omega_5 v_2^2 + 2\omega_5 + 6c_s^2 + 10v_2^2) \frac{\rho v_1 v_2}{12\omega_5^2}$$

$$C_{D_y^4 v_2}^{(1), \text{CuLBM2}} = (10\omega_1 v_2^2 + 20v_2^2 \omega_2 + 6\omega_1 \omega_2 - 4\omega_1 - 15\omega_1 v_2^2 \omega_2 + 6c_s^2 \omega_1 - 8\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2) \frac{\rho v_1 v_2}{36\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^3 D_z \rho}^{(1)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{MRT1}} = (-36\omega_6^2 \omega_{13}^2 v_1^4 \omega_9 + 20\omega_6 \omega_{13} v_1^4 \omega_9^3 - 72\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9 + 4\omega_6^2 \omega_{13}^2 c_s^4 \omega_9^2 - 4\omega_6 v_1^4 \omega_9^3 + 4\omega_6^2 \omega_{13} c_s^2 \omega_9 - 8\omega_{13}^2 v_1^2 \omega_9^2 - 32\omega_6^2 \omega_{13} v_1^2 \omega_9^2 - 4\omega_6^2 c_s^2 \omega_9^3 - 4\omega_{13} c_s^4 \omega_9^3 - 16\omega_6 \omega_{13} v_1^4 \omega_9^2 + 96\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 + 4\omega_6^2 c_s^2 \omega_9^2 + 13\omega_6^2 \omega_{13} v_1^2 \omega_9^3 - 24\omega_6^2 \omega_{13}^2 v_1^2 + 8\omega_6 \omega_{13}^2 c_s^2 \omega_9^2 - 20\omega_6^2 \omega_{13}^2 v_1^2 \omega_9 - 4\omega_6 \omega_{13}^2 c_s^2 \omega_9 - 48\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9^2 + 20\omega_6 \omega_{13}^2 v_1^2 \omega_9^2 + 4\omega_6^2 v_1^2 \omega_9^2 + 4\omega_6^2 \omega_{13} c_s^2 \omega_9^3 - 51\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9^3 - 8\omega_{13} v_1^4 \omega_9^3 + 8\omega_6^2 \omega_{13}^2 c_s^4 - 8\omega_6^2 \omega_{13} c_s^2 \omega_9^2 - 4\omega_6^2 v_1^2 \omega_9^3 + 84\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9^3 - 4\omega_{13}^2 c_s^2 \omega_9^2 - 24\omega_6 c_s^2 v_1^2 \omega_9^3 + 20\omega_6^2 \omega_{13} v_1^2 \omega_9 + 13\omega_6^2 \omega_{13}^2 v_1^4 \omega_9^2 - 4\omega_6 c_s^4 \omega_9^3 + 36\omega_{13}^2 c_s^2 v_1^2 \omega_9^2 + 8\omega_6 \omega_{13} c_s^4 \omega_9^3 + 120\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9^2 - 12\omega_6^2 \omega_{13}^2 c_s^4 \omega_9 + 4\omega_{13} c_s^2 \omega_9^3 + 16\omega_6 \omega_{13} v_1^2 \omega_9^2 - 8\omega_6^2 \omega_{13}^2 c_s^2 - 4\omega_6^2 c_s^4 \omega_9^2 - 13\omega_6^2 \omega_{13} v_1^4 \omega_9^3 - 144\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9 - 8\omega_6 \omega_{13}^2 c_s^4 \omega_9^2 + 20\omega_6 \omega_{13}^2 v_1^4 \omega_9 + 72\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9 + 36\omega_6^2 \omega_{13} v_1^2 \omega_9 - 20\omega_6 \omega_{13} v_1^2 \omega_9^3 - 4\omega_6^2 \omega_{13} c_s^2 \omega_9^2 + 4\omega_6 v_1^2 \omega_9^3 - 4\omega_6^2 \omega_{13} c_s^4 \omega_9 + 8\omega_{13}^2 v_1^4 \omega_9^2 + 32\omega_6^2 \omega_{13} v_1^4 \omega_9^2 + 4\omega_6^2 c_s^4 \omega_9^3 + 8\omega_6^2 \omega_{13} c_s^4 \omega_9^2 + 4\omega_6^2 v_1^4 \omega_9^3 + 4\omega_{13}^2 c_s^4 \omega_9^2 - 36\omega_{13} c_s^2 v_1^2 \omega_9^3 - 20\omega_6^2 \omega_{13} v_1^4 \omega_9 - 13\omega_6^2 \omega_{13}^2 v_1^2 \omega_9^2 + 4\omega_6 c_s^2 \omega_9^3 - 84\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9^2 - 8\omega_6 \omega_{13} c_s^2 \omega_9^3 - 24\omega_6^2 c_s^2 v_1^2 \omega_9^2 + 12\omega_6^2 \omega_{13} c_s^2 \omega_9 + 51\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 \omega_9^2 + 24\omega_6^2 \omega_{13}^2 v_1^4 + 4\omega_6 \omega_{13}^2 c_s^2 \omega_9 - 20\omega_6 \omega_{13}^2 v_1^4 \omega_9^2 - 4\omega_6^2 v_1^4 \omega_9^2 - 4\omega_6^2 \omega_{13} c_s^4 \omega_9^3 + 24\omega_6^2 c_s^2 v_1^2 \omega_9^3 + 8\omega_{13} v_1^2 \omega_9^3) \frac{v_3}{4\omega_6^2 \omega_{13}^2 \omega_9^3}$$

$$C_{D_x^3 D_z \rho}^{(1), \text{MRT2}} = C_{D_x^3 D_z \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{D_x^3 D_z \rho}^{(1), \text{CuLBM2}} = & (8\omega_2^2 \omega_1 \omega_2^2 - 60\omega_3^2 \omega_1 v_1^2 \omega_2^3 - 48\omega_3^2 \omega_1^2 v_1^2 \omega_2^2 v_3^2 - 4\omega_3 c_s^2 \omega_1^2 \omega_2^2 v_3^2 + 40\omega_3^2 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_1^2 \omega_2^2 v_3^2 - 324\omega_3^2 c_s^2 \omega_1^3 v_1^2 \omega_2 - \\ & 84\omega_3^2 c_s^4 \omega_1^3 \omega_2 - 72\omega_3^2 v_1^2 \omega_2^3 v_3^2 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 12c_s^2 \omega_1^3 \omega_2^2 - 216\omega_3^2 c_s^2 \omega_1 v_1^2 \omega_2^2 + 12c_s^2 \omega_1^2 \omega_2^3 v_3^2 + 84\omega_3^2 \omega_1^3 v_1^2 \omega_2 - 5\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 + 48\omega_3^2 \omega_1 v_1^2 \omega_2^2 + \\ & 36c_s^4 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 + 16\omega_3^2 c_s^2 \omega_1^3 v_3^2 + 8\omega_3^2 \omega_1 \omega_2^3 - 36\omega_3^2 c_s^4 \omega_2^3 + 108\omega_3^2 c_s^2 \omega_1 v_1^2 \omega_2^3 + 4\omega_3^2 \omega_1^3 + 42\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 2\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 v_3^2 + 72\omega_3^2 \omega_1^2 v_1^4 \omega_2^2 + \\ & 48\omega_3^2 v_1^4 \omega_2^3 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 48\omega_3^2 \omega_1^3 v_1^2 - 24\omega_3^2 \omega_1^2 v_1^2 \omega_2^3 v_3^2 - 24\omega_3^2 \omega_1^3 v_1^2 \omega_2^2 + 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + \omega_3^2 \omega_1^2 \omega_2^3 v_3^2 + 72\omega_3^2 c_s^4 \omega_1^3 + 56\omega_3^2 c_s^2 \omega_1^3 \omega_2 - \\ & 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 - 8\omega_3^2 \omega_2^3 + 24\omega_3^2 \omega_1^3 v_1^2 v_3^2 - 36c_s^4 \omega_1^3 \omega_2^2 - 4\omega_3^2 c_s^2 \omega_1^3 \omega_2 v_3^2 + 4\omega_3^2 \omega_1^3 \omega_2 v_3^2 + 6\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 + 72\omega_3^2 c_s^2 \omega_1^3 v_1^2 \omega_2^2 + 24\omega_3^2 \omega_1^3 v_1^2 \omega_2^3 v_3^2 - \\ & 2\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 + 24\omega_3^2 c_s^4 \omega_1 \omega_2^3 - 20\omega_3^2 c_s^2 \omega_1^3 \omega_2 v_3^2 - 12c_s^4 \omega_1^2 \omega_2^3 + 8\omega_3^2 \omega_2^3 v_3^2 - 34\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 48\omega_3^2 \omega_1^3 v_1^2 \omega_2 v_3^2 - 36\omega_3^2 \omega_1^3 v_1^4 \omega_2 + 2\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 v_3^2 - \\ & 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 72\omega_3^2 \omega_1 v_1^4 \omega_2^2 - 54\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 + 24\omega_3^2 \omega_1 v_1^2 \omega_2^2 v_3^2 - 4\omega_3^2 \omega_1^2 \omega_2^2 - 24\omega_3^2 \omega_1^2 v_1^2 \omega_2^2 + 20\omega_3^2 c_s^2 \omega_2^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^2 - 8\omega_3^2 \omega_1 \omega_2^3 v_3^2 + \\ & 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 v_3^2 + 24\omega_3^2 \omega_1^3 v_1^2 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 36\omega_3^2 \omega_1 v_1^4 \omega_2^2 + 22\omega_3^2 c_s^2 \omega_1 \omega_2^3 v_3^2 - 4\omega_3^2 \omega_1^3 v_3^2 - 22\omega_3^2 c_s^2 \omega_1 \omega_2^3 - \omega_3^2 \omega_1^2 \omega_2^3 v_3^2 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 - \\ & 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 + \omega_3^2 \omega_1^3 \omega_2^2 - 8\omega_3^2 \omega_1 \omega_2^3 v_3^2 + 24\omega_3^2 v_1^2 \omega_2^2 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - \omega_3^2 \omega_1^2 \omega_2^2 + 96\omega_3^2 \omega_1 v_1^2 \omega_2^3 v_3^2 - 4\omega_3^2 \omega_1^3 \omega_2 + 4\omega_3^2 c_s^2 \omega_1^3 \omega_2 + 216\omega_3^2 c_s^2 \omega_1^3 v_1^2 + \\ & 216\omega_3^2 c_s^2 \omega_1^3 v_1^2 \omega_2^2 - 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 - 24\omega_3^2 \omega_1^2 v_1^2 \omega_2^2 - 4\omega_3^2 \omega_1^2 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + 4\omega_3^2 \omega_1^2 \omega_2 v_3^2 + 24\omega_3^2 v_1^2 \omega_2^2 - 20\omega_3^2 c_s^2 \omega_2^3 v_3^2 + 24\omega_3^2 \omega_1^2 v_1^2 \omega_2 v_3^2 + \\ & 42\omega_3^2 c_s^4 \omega_1 \omega_2^2 - 12c_s^2 \omega_1^2 \omega_2^3 v_3^2 + 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 v_3^2 - 52\omega_3^2 c_s^2 \omega_1^3 - 72\omega_3^2 c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 54\omega_3^2 c_s^4 \omega_1^3 \omega_2^2) \frac{v_3}{36\omega_3^2 \omega_1^3 \omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{D_x^3 D_z v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z v_1}^{(1), \text{SRT}} = 0$$

$$\begin{aligned} C_{D_x^3 D_z v_1}^{(1), \text{MRT1}} = & (-32\omega_6^2 \omega_{13}^2 - 24\omega_6 \omega_{13} \omega_9 - 32\omega_6^2 \omega_{13} c_s^2 \omega_9 + 28\omega_{13}^2 v_1^2 \omega_9^2 + 104\omega_6^2 \omega_{13} v_1^2 \omega_9^2 + 16\omega_6^2 c_s^2 \omega_9^3 + 24\omega_6^2 \omega_{13} \omega_9 - 16\omega_6^2 c_s^2 \omega_9^2 - \\ & 43\omega_6^2 \omega_{13} v_1^2 \omega_9^3 + 80\omega_6^2 \omega_{13}^2 v_1^2 - 44\omega_6 \omega_{13}^2 c_s^2 \omega_9^2 + 64\omega_6 \omega_{13}^2 v_1^2 \omega_9 + 32\omega_6 \omega_{13} c_s^2 \omega_9 - 68\omega_6 \omega_{13}^2 v_1^2 \omega_9^2 - 16\omega_6^2 v_1^2 \omega_9^2 - 25\omega_6^2 \omega_{13} c_s^2 \omega_9^3 - 40\omega_6^2 \omega_{13} \omega_9^2 - \\ & 12\omega_{13}^2 \omega_9^2 - 8\omega_6^2 \omega_9^3 + 56\omega_6^2 \omega_{13} c_s^2 \omega_9^2 + 16\omega_6^2 v_1^2 \omega_9^3 + 20\omega_{13}^2 c_s^2 \omega_9^2 - 64\omega_6^2 \omega_{13} v_1^2 \omega_9 + 8\omega_6^2 \omega_9^2 + 28\omega_6 \omega_{13}^2 \omega_9^2 + 17\omega_6^2 \omega_{13} \omega_9^2 - 20\omega_{13} c_s^2 \omega_9^3 - \\ & 48\omega_6 \omega_{13} v_1^2 \omega_9^2 + 48\omega_6^2 \omega_{13}^2 c_s^2 + 12\omega_{13}^2 \omega_9^3 + 16\omega_6 \omega_{13} \omega_9^2 - 120\omega_6^2 \omega_{13}^2 v_1^2 \omega_9 + 68\omega_6 \omega_{13} v_1^2 \omega_9^3 + 25\omega_6^2 \omega_{13}^2 c_s^2 \omega_9^2 - 16\omega_6 v_1^2 \omega_9^3 - 28\omega_6 \omega_{13} \omega_9^3 + 8\omega_6 \omega_9^3 - \\ & 17\omega_6^2 \omega_{13} \omega_9^2 + 48\omega_6^2 \omega_{13} \omega_9 + 43\omega_6^2 \omega_{13}^2 v_1^2 \omega_9^2 - 16\omega_6 c_s^2 \omega_9^3 + 44\omega_6 \omega_{13} c_s^2 \omega_9^3 - 72\omega_6^2 \omega_{13}^2 c_s^2 \omega_9 - 28\omega_{13} v_1^2 \omega_9^3 - 16\omega_6 \omega_{13} c_s^2 \omega_9^2) \frac{\rho v_1 v_3}{4\omega_6^2 \omega_{13}^2 \omega_9^3} \end{aligned}$$

$$C_{D_x^3 D_z v_1}^{(1), \text{MRT2}} = C_{D_x^3 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{D_x^3 D_z v_1}^{(1), \text{CuLBM2}} = & (27\omega_3 \omega_1 \omega_2^3 v_3^2 - 54\omega_3 c_s^2 \omega_1 \omega_2^2 + 48\omega_3 \omega_1^3 \omega_2 + 5\omega_3 \omega_1^2 \omega_2^3 - 12\omega_3 \omega_1^2 v_1^2 \omega_2 + 27c_s^2 \omega_1^3 \omega_2^2 + 5\omega_3 \omega_1^2 \omega_2^2 v_3^2 + 84\omega_3 v_1^2 \omega_2^3 - 51\omega_3 \omega_1^2 \omega_2^2 + \\ & 27\omega_3^2 c_s^2 \omega_1 \omega_2^2 - 6\omega_3^2 \omega_2^3 v_3^2 - 12\omega_1 \omega_2^3 + 84\omega_3 c_s^2 \omega_1^3 - 18c_s^2 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_1^2 \omega_2^2 - 12\omega_3 c_s^2 \omega_2^3 + 6\omega_3 \omega_1 \omega_2^2 v_3^2 - 6\omega_1^2 \omega_2 v_3^2 - 9\omega_1^2 \omega_2^3 v_3^2 - 18c_s^2 \omega_1^3 \omega_2 - \\ & 27c_s^2 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_1^2 \omega_2 v_3^2 - 5\omega_3 \omega_1^3 \omega_2^2 + 12\omega_3 \omega_1^3 v_3^2 + 132\omega_3 \omega_1^2 v_1^2 \omega_2^2 + 48\omega_3 \omega_1^3 v_1^2 + 9\omega_1^3 \omega_2^2 v_3^2 + 36c_s^2 \omega_1 \omega_2^3 - 18\omega_3 c_s^2 \omega_1^2 \omega_2 - 9\omega_3 \omega_1^2 \omega_2^2 v_3^2 - \\ & 66\omega_3 \omega_1 v_1^2 \omega_2^2 - 9\omega_1^2 \omega_2^2 + 12\omega_1 \omega_2^3 v_3^2 - 120\omega_3 \omega_1 v_1^2 \omega_2^2 - 66\omega_3 \omega_1^3 v_1^2 \omega_2 - 24\omega_3 \omega_2^3 v_3^2 + 15\omega_3 c_s^2 \omega_1^3 \omega_2^2 - 12\omega_3 \omega_2^3 - 18\omega_3 \omega_1^2 \omega_2 v_3^2 - 15\omega_3 c_s^2 \omega_1^2 \omega_2^2 + \\ & 42\omega_3 \omega_1 \omega_2^2 - 5\omega_3 \omega_1^2 \omega_2^3 v_3^2 - 108\omega_3 c_s^2 \omega_1^3 \omega_2 + 6\omega_1^3 \omega_2 + 9\omega_1^2 \omega_2^2 - 36\omega_3 \omega_1^3 + 3\omega_3 \omega_1 \omega_2^2 + 81\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 6\omega_1^2 \omega_2^2) \frac{\rho v_1 v_3}{18\omega_3 \omega_1^3 \omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{D_x^3 D_z v_3}^{(1)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} :$$

$$\begin{aligned} C_{D_x^3 D_z v_3}^{(1), \text{SRT}} = & (36v_1^2 - 4\omega^3 v_1^2 + 36c_s^2 \omega + 54c_s^2 \omega v_1^2 + 26\omega^2 v_1^2 - 36c_s^2 v_1^2 - 12c_s^2 \omega^2 + 36c_s^4 + 54\omega v_1^4 - 26\omega^2 v_1^4 + 12c_s^2 \omega^3 v_1^2 - 54\omega v_1^2 - 54c_s^4 \omega - \\ & 24c_s^5 + 4\omega^3 v_1^4 + 20c_s^4 \omega^2 - 36v_1^4 - c_s^4 \omega^3 - 42c_s^2 \omega^2 v_1^2) \frac{\rho}{12\omega^3} \end{aligned}$$

$$\begin{aligned} C_{D_x^3 D_z v_3}^{(1), \text{MRT1}} = & (36\omega_6^3 \omega_{13} v_1^2 \omega_9 - 24\omega_6 \omega_{13} v_1^4 \omega_9^3 + 6\omega_6^2 \omega_{13}^2 c_s^4 \omega_9^2 + 6\omega_6^3 \omega_{13} c_s^2 \omega_9^2 - 12\omega_6^2 \omega_{13}^2 c_s^4 \omega_9 + 12\omega_6^3 \omega_{13}^2 c_s^2 v_1^2 \omega_9^3 + 6\omega_6 \omega_{13}^2 c_s^2 \omega_9^3 + 19\omega_6^3 \omega_{13}^2 v_1^4 \omega_9^2 + \\ & 24\omega_6^2 \omega_{13} v_1^2 \omega_9^2 + 13\omega_6^2 \omega_{13}^2 c_s^4 \omega_9^3 - 6\omega_6^2 \omega_{13} c_s^2 \omega_9^3 + 4\omega_6^3 \omega_{13} v_1^4 \omega_9^3 - 48\omega_6^2 \omega_{13} v_1^2 \omega_9^3 + 60\omega_6^3 \omega_{13}^2 c_s^2 v_1^2 \omega_9^2 - 12\omega_6^3 \omega_{13}^2 c_s^2 + 252\omega_6^3 \omega_{13}^2 c_s^2 v_1^2 - \\ & 306\omega_6^3 \omega_{13}^2 c_s^2 v_1^2 \omega_9 - \omega_6^3 \omega_{13}^2 c_s^4 \omega_9^3 + 18\omega_6^2 \omega_{13} c_s^2 \omega_9^3 + 72\omega_6^3 \omega_{13}^2 v_1^4 + 30\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9^3 - 12\omega_6^3 v_1^4 \omega_9^2 - 18\omega_6^2 \omega_{13} v_1^4 \omega_9^3 + 27\omega_6^3 \omega_{13} v_1^2 \omega_9^3 - 48\omega_{13}^2 c_s^2 v_1^2 \omega_9^3 + \\ & \omega_6^3 \omega_{13}^2 c_s^4 \omega_9^2 - 12\omega_6^2 \omega_{13} c_s^2 \omega_9^2 + 12\omega_6^2 v_1^2 \omega_9^3 - 12\omega_6 \omega_{13}^2 v_1^2 \omega_9^3 - 12\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9^3 - 90\omega_6^3 \omega_{13}^2 v_1^4 \omega_9 + 12\omega_6^2 \omega_{13}^2 v_1^4 \omega_9^2 - 60\omega_6^3 \omega_{13} v_1^2 \omega_9^2 + 12\omega_6 \omega_{13} c_s^4 \omega_9^3 + \\ & 12\omega_6^3 v_1^4 \omega_9^3 - 12\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9^2 - 12\omega_6^2 \omega_{13}^2 c_s^4 \omega_9 + 6\omega_6^3 \omega_{13} c_s^4 \omega_9^3 - 5\omega_6^2 \omega_{13}^2 c_s^2 \omega_9^3 - 72\omega_6^3 \omega_{13}^2 v_1^2 - 21\omega_6^3 \omega_{13} c_s^2 v_1^2 \omega_9^3 + 48\omega_6^2 \omega_{13} v_1^4 \omega_9^3 - 4\omega_6^3 \omega_{13}^2 v_1^2 \omega_9^3 - \\ & 108\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 \omega_9 + 12\omega_6^3 c_s^2 v_1^2 \omega_9^3 - 36\omega_6^3 \omega_{13} v_1^4 \omega_9 + 54\omega_6^3 \omega_{13} c_s^2 v_1^2 \omega_9^2 + 24\omega_6 \omega_{13} v_1^2 \omega_9^3 - 6\omega_6^3 \omega_{13} c_s^4 \omega_9^2 - 6\omega_6^2 \omega_{13}^2 c_s^2 \omega_9^2 + 12\omega_6^3 \omega_{13}^2 c_s^2 \omega_9 - 12\omega_6^3 c_s^2 v_1^2 \omega_9^2 - \\ & 24\omega_6 \omega_{13} c_s^4 \omega_9^3 - 24\omega_6^2 \omega_{13} v_1^4 \omega_9^2 - 19\omega_6^3 \omega_{13} v_1^2 \omega_9^2 + 12\omega_6^2 \omega_{13} c_s^4 \omega_9^2 - 12\omega_6^2 v_1^4 \omega_9^3 - \omega_6^3 \omega_{13} c_s^2 \omega_9^2 + 12\omega_6 \omega_{13}^2 v_1^2 \omega_9^3 + 90\omega_6^3 \omega_{13}^2 v_1^2 \omega_9 - 81\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 \omega_9^3 - \\ & 36\omega_6^3 \omega_{13} c_s^2 v_1^2 \omega_9 + 60\omega_6^3 \omega_{13} v_1^4 \omega_9^2 - 12\omega_6^2 \omega_{13}^2 v_1^2 \omega_9^2 - 48\omega_6 \omega_{13}^2 c_s^2 v_1^2 \omega_9^2 - 12\omega_6^3 v_1^4 \omega_9^3 - 12\omega_6 \omega_{13} c_s^2 \omega_9^3 + 12\omega_6^2 \omega_{13}^2 c_s^2 \omega_9 + 162\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 \omega_9^2 + \\ & 12\omega_{13}^2 c_s^4 \omega_9^3 + 12\omega_6^2 \omega_{13}^2 c_s^4 - 18\omega_6^2 \omega_{13} c_s^2 \omega_9^3 - 12\omega_6^2 c_s^2 v_1^2 \omega_9^3 + 12\omega_6^3 v_1^4 \omega_9^3 - 27\omega_6^3 \omega_{13} v_1^4 \omega_9^3 + 102\omega_6 \omega_{13}^2 c_s^2 v_1^2 \omega_9^3 + 18\omega_6^2 \omega_{13}^2 v_1^2 \omega_9^3) \frac{\rho}{12\omega_6^2 \omega_{13}^2 \omega_9^3} \end{aligned}$$

$$C_{D_x^3 D_z v_3}^{(1), \text{MRT2}} = C_{D_x^3 D_z v_3}^{(1), \text{MRT1}}$$

$$\begin{aligned}
C_{D_x^2 D_y D_z \rho}^{(1), \text{MRT2}} &= C_{D_x^2 D_y D_z \rho}^{(1), \text{MRT1}} \\
C_{D_x^2 D_y D_z \rho}^{(1), \text{CLBM1}} &= 0 \\
C_{D_x^2 D_y D_z \rho}^{(1), \text{CLBM2}} &= 0 \\
C_{D_x^2 D_y D_z \rho}^{(1), \text{CuLBM1}} &= 0 \\
C_{D_x^2 D_y D_z \rho}^{(1), \text{CuLBM2}} &= (6\omega_1^2 v_2^2 \omega_2^2 + 12\omega_1 v_1^2 \omega_2^2 - 12\omega_1 \omega_2^2 - 72c_s^2 \omega_1^2 \omega_2 + 6\omega_1^2 \omega_2^2 v_3^2 + 6\omega_1 \omega_3^2 + 2v_2^2 \omega_2^3 + 36c_s^2 \omega_1^2 \omega_2^2 + 4\omega_1^3 v_1^2 - 6\omega_1^2 v_2^2 \omega_2 - 3\omega_1^3 \omega_2 v_3^2 + \\
&\quad 2\omega_3^3 v_2^2 - 18c_s^2 \omega_1^3 \omega_2 - 18c_s^2 \omega_1 \omega_2^3 + 24\omega_1^2 \omega_2 + 36c_s^2 \omega_1 \omega_2^2 - 3\omega_1 \omega_2^3 v_3^2 - 12\omega_1^2 v_1^2 \omega_2 + 4\omega_1^3 v_3^2 + 4\omega_1^3 v_2^2 - 12\omega_1^3 + 6\omega_1^3 \omega_2 - 6\omega_1^2 \omega_2 v_3^2 - 3\omega_1^3 v_2^2 \omega_2 + \\
&\quad 36c_s^2 \omega_1^3 - 3\omega_1 v_2^2 \omega_2^2 - 4v_1^2 \omega_2^3 - 12\omega_1^2 \omega_2^2) \frac{v_1 v_2 v_3}{6\omega_1^3 \omega_2^2}
\end{aligned}$$

[illegible]

$$C_{\text{D}_x \text{D}_y \text{D}_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{\text{D}_x \text{D}_y \text{D}_z v_3}^{(1), \text{CuLBM2}} = & (144\omega_3^2\omega_4^3\omega_1^3v_3^2 + 12\omega_3\omega_4^2\omega_1\omega_2^3 + 108\omega_3^2\omega_1^2v_2^2\omega_2^3 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 144\omega_3\omega_4^2c_s^2\omega_1^3\omega_2 + 180\omega_3\omega_4\omega_1^2v_1^2\omega_2^3 + 36\omega_3\omega_4^2\omega_1^3v_1^2\omega_2^2 + \\ & 324\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 + 180\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2 + 36\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^2 - 72\omega_4^2\omega_1^2v_2^2\omega_2^3 - 108\omega_4^2\omega_1^3\omega_2^3 + 48\omega_3^2\omega_4^2\omega_1^3v_2^2 + 324\omega_4^2c_s^2\omega_1^3\omega_2^3 - 120\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 + \\ & 96\omega_3^2\omega_4^2\omega_1^3\omega_2 - 144\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 - 144\omega_3\omega_4\omega_1^2\omega_2^3 - 108\omega_3^2\omega_4^2\omega_1^3\omega_2v_3^2 + 24\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2 - 216\omega_4^2c_s^2\omega_1^3\omega_2^2 + 72\omega_4^2\omega_1^3\omega_2^2 - 360\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2 + \\ & 72\omega_3^2\omega_4\omega_1v_2^2\omega_2^3 - 60\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3 + 36\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^3 + 144\omega_4^2\omega_1^2\omega_2^3 + 336\omega_3^2\omega_4^2c_s^2\omega_1^3 - 36\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 108\omega_3^2\omega_4c_s^2\omega_1\omega_2^3 + 63\omega_3^2\omega_4\omega_1^3v_2^2\omega_2^3 - \\ & 432\omega_4^2c_s^2\omega_1^2\omega_2^3 - 36\omega_4^2\omega_1^3v_1^2\omega_2^3 - 48\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 + 60\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 - 108\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 189\omega_3\omega_4^2c_s^2\omega_1^3\omega_2^3 - 36\omega_3^2\omega_4\omega_1\omega_2^3 + \\ & 12\omega_3^2\omega_4\omega_1v_1^2\omega_2^3 + 36\omega_3\omega_4\omega_1^2v_2^2\omega_2^2 + 48\omega_3^2\omega_4^2v_1^2\omega_2^3 + 144\omega_3\omega_4^2\omega_1^2v_2^2\omega_2^3 - 72\omega_3\omega_4\omega_1^3\omega_2^2 + 216\omega_3^2\omega_4^2\omega_1^2\omega_2^2v_3^2 - 144\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2 + 54\omega_4^2\omega_1^3v_1^2\omega_2^3 - \\ & 36\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 20\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 - 36\omega_3^2\omega_4\omega_1^3v_2^2\omega_2^2 + 108\omega_3\omega_4\omega_1^3\omega_2^3 - 60\omega_3\omega_4^2\omega_1^2v_2^2\omega_2^3 + 324\omega_3\omega_4^2c_s^2\omega_1^3\omega_2^2 + 144\omega_3^2\omega_4^2\omega_1^3\omega_2 + 20\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - \\ & 24\omega_3\omega_4^2\omega_1^3v_1^2\omega_2 + 54\omega_3^2\omega_1^3v_1^2\omega_2^3 + 24\omega_3^2\omega_4^2\omega_2^3 - 72\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2 - 216\omega_3^2\omega_4^2\omega_1^2\omega_2v_3^2 + 216\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 + 72\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2 - \\ & 36\omega_4^2\omega_1^3v_2^2\omega_2^2 - 24\omega_3\omega_4^2\omega_1v_2^2\omega_2^3 - 108\omega_3\omega_4^2\omega_1^3\omega_2^2 - 36\omega_3\omega_4^2\omega_1^2v_1^2\omega_2^3 - 96\omega_3^2\omega_4^2v_2^2\omega_2^3 + 432\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 + 36\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1\omega_2^3 - \\ & 72\omega_3^2\omega_4\omega_1^2\omega_2^2 + 108\omega_3^2\omega_4\omega_1v_2^2\omega_2^2 + 54\omega_4^2\omega_1^3v_2^2\omega_2^3 - 36\omega_3^2\omega_4\omega_1^3v_1^2\omega_2^2 - 432\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^3 + 144\omega_3^2\omega_4\omega_1^2\omega_2^3 - 54\omega_3^2\omega_1^3v_2^2\omega_2^3 - 24\omega_3\omega_4^2\omega_1^3v_2^2\omega_2 + \\ & 24\omega_3^2\omega_4^2\omega_1\omega_2^2 + 12\omega_3\omega_4^2\omega_1^2v_1^2\omega_2^2 - 108\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 + 63\omega_3\omega_4^2\omega_1^3\omega_2^3 + 72\omega_3^2\omega_4^2\omega_2^3v_3^2 + 72\omega_3\omega_4^2\omega_1^3v_2^2\omega_2^2 + 72\omega_3^2\omega_4\omega_1^3\omega_2^2 - 36\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 + \\ & 48\omega_3\omega_4^2\omega_2^2\omega_2^2 - 108\omega_3^2\omega_1^2v_1^2\omega_2^3 - 324\omega_3\omega_4c_s^2\omega_1^3\omega_2^3 - 216\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^2 + 36\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^2 + 180\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^3 - 72\omega_4^2\omega_1^2v_1^2\omega_2^3 + 48\omega_3\omega_4^2\omega_1^3\omega_2 - \\ & 144\omega_3^2\omega_4^2\omega_1^3 + 216\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 - 108\omega_3\omega_4^2\omega_1^2\omega_2^3 - 63\omega_3\omega_4^2\omega_1^3v_2^2\omega_2^3 - 36\omega_3\omega_4^2c_s^2\omega_1\omega_2^3 - 63\omega_3^2\omega_4\omega_1^3\omega_2^3 - 36\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 - 180\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^2 + \\ & 20\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 108\omega_3^2\omega_4\omega_1\omega_2^3v_3^2 - 72\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^2 - 48\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 + 48\omega_3^2\omega_4^2\omega_1^3v_1^2 + 189\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^3) \frac{\rho v_1 v_2}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{\text{D}_x \text{D}_y \text{D}_z \rho}^{(1)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{MRT1}} =$$

$$(\omega_6^2\omega_8\omega_5 - \omega_6\omega_8^2\omega_5 + \omega_6\omega_5^3 + 2\omega_6\omega_8^2\omega_5^2 + \omega_6^2\omega_8\omega_5^3 - 2\omega_6^2\omega_8\omega_5^2 - \omega_8^2\omega_5^2 - 2\omega_6\omega_8\omega_5^3 - \omega_6^2\omega_8^2\omega_5^2 + \omega_8\omega_5^3 - 2\omega_6^2\omega_8^2 - \omega_6^2\omega_5^3 + 3\omega_6^2\omega_8^2\omega_5 + \omega_6^2\omega_5^2) \frac{2c_s^4 v_3}{\omega_6^2\omega_8^2\omega_5^3}$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{MRT2}} = C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{MRT1}}$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{\text{D}_x \text{D}_y^2 \text{D}_z \rho}^{(1), \text{CuLBM2}} = & (-252\omega_4^2c_s^4\omega_1^2\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1v_2^4\omega_2^3 - 8\omega_3^2\omega_4^2\omega_3^3v_3^2 - 432\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2 - 8\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2v_3^2 + 54\omega_3^2c_s^2\omega_1^3\omega_2^3 + 8\omega_3\omega_2^2c_s^2\omega_1^3\omega_2 - \\ & 432\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 - 108\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 + 30\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^2 - 81\omega_3\omega_4^2c_s^4\omega_3^3\omega_2^3 - 176\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2 - 56\omega_3\omega_4^2c_s^2\omega_1\omega_3^3v_3^2 + 324\omega_3^2c_s^4\omega_1^2\omega_2^3 - \\ & 96\omega_3^2\omega_4^2\omega_3^3v_2^2 - 54\omega_4^2c_s^2\omega_1^3\omega_2^3 - 432\omega_3^2\omega_1^2c_s^2\omega_1^2v_2^2\omega_2^3 - 104\omega_3^2\omega_4^2c_s^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2 - 64\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 - 36\omega_3^2\omega_1^2\omega_3^3v_4^2\omega_2 - 72\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2 - \\ & 56\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 + 8\omega_3^2\omega_4^2\omega_1^2\omega_2v_3^2 + 96\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 24\omega_4^2c_s^2\omega_1^3\omega_2^3 + 24\omega_3^2\omega_4^2v_2^2\omega_2^3 + 112\omega_3^2\omega_4^2c_s^2\omega_3^3\omega_2 + 10\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3 + 27\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^3v_3^2 + \\ & 120\omega_3^2\omega_1^2v_2^2\omega_2^3v_3^2 - 104\omega_3^2\omega_4^2c_s^2\omega_1^3 - 192\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 32\omega_3^2\omega_4^2c_s^2\omega_1^3v_3^2 + 84\omega_4^2c_s^2\omega_1^2\omega_2^3 - 84\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 - 10\omega_3^2\omega_1^2c_s^2\omega_1^3\omega_2^2 + \\ & 324\omega_3\omega_4^2c_s^4\omega_1^2\omega_2^3 - 162\omega_3^2c_s^4\omega_1^3\omega_2^3 - 24\omega_3\omega_4^2c_s^4\omega_1^3\omega_2 + 16\omega_3^2\omega_4^2\omega_1^2\omega_2^3 - 108\omega_3^2c_s^2\omega_1^2\omega_2^3 + 192\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^3 + 27\omega_3\omega_4^2c_s^2\omega_3^3\omega_2^3 + 10\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^3v_3^2 + \\ & 162\omega_4^2c_s^4\omega_1^3\omega_2^3 + 432\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 - 16\omega_3^2\omega_4^2\omega_1^2\omega_2^3v_3^2 + 80\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2 + 108\omega_3^2c_s^2\omega_1^2\omega_2^3v_3^2 + 192\omega_3\omega_4^2c_s^4\omega_1^2\omega_2^3 - 27\omega_3\omega_4^2c_s^2\omega_1^3\omega_2^3v_3^2 - 72\omega_4^2c_s^4\omega_1^3\omega_2^3 + \\ & 8\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^3v_3^2 - 30\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2 - 168\omega_3^2\omega_4^2c_s^4\omega_3^3\omega_2 + 8\omega_3^2\omega_4^2\omega_2^3 + 32\omega_3^2\omega_4^2c_s^2\omega_2^3v_3^2 - 60\omega_3^2\omega_4\omega_1v_2^2\omega_2^3 + 144\omega_3^2\omega_4^2c_s^4\omega_2^3 + \\ & 96\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2 + 64\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 + 8\omega_3^2\omega_4^2\omega_1^2\omega_2v_3^2 - 108\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 + 96\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^3 - 72\omega_3^2\omega_4^2\omega_1^2v_2^4\omega_2 - 96\omega_3^2\omega_4^2v_2^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 - \\ & 24\omega_3^2\omega_4^2c_s^4\omega_1\omega_2^3 + 96\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^3 - 24\omega_4^2c_s^2\omega_1^3\omega_2^3v_3^2 + 108\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3 - 24\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2v_3^2 + 8\omega_3^2\omega_4^2\omega_1\omega_2^2v_3^2 - 168\omega_3\omega_4^2c_s^4\omega_1\omega_2^3 - \\ & 40\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2v_3^2 - 216\omega_3^2\omega_4^2c_s^4\omega_1\omega_2^2 - 432\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 - 10\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 + 81\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^3 - 8\omega_3^2\omega_4^2\omega_3^3v_3^2 + \\ & 864\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 - 60\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2v_3^2 + 48\omega_3^2\omega_4^2\omega_1^3v_4^2 - 54\omega_3^2c_s^2\omega_1^3\omega_2^3v_3^2 - 8\omega_3\omega_4^2c_s^2\omega_3^3\omega_2v_3^2 + 432\omega_3^2\omega_4^2c_s^2\omega_2^3v_2^2 - 96\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + \\ & 64\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^3 + 108\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 + 32\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 - 324\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3 + 8\omega_3^2\omega_4^2\omega_1^3 + 144\omega_3^2\omega_4^2c_s^4\omega_1^3 + 72\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + \\ & 56\omega_3\omega_4^2c_s^2\omega_1\omega_2^3 + 72\omega_3^2\omega_4^2v_2^2\omega_2^3v_3^2 + 8\omega_3^2\omega_4^2\omega_1\omega_2^3v_3^2 + 128\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^2 - 27\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^3 + 48\omega_3^2\omega_4^2\omega_1^3v_2^2v_3^2 + 54\omega_4^2c_s^2\omega_1^3\omega_2^3v_3^2) \frac{v_3}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{\text{D}_x \text{D}_y^2 \text{D}_z v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z v_1}^{(1), \text{SRT}} = 0$$

$$\begin{aligned} C_{\text{D}_x \text{D}_y^2 \text{D}_z v_1}^{(1), \text{MRT1}} = & (2\omega_6^2\omega_{13}\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12}^2 - 4\omega_6\omega_7\omega_8^2\omega_5^3\omega_9\omega_{12}^2 + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_9\omega_{12} + 4\omega_6^2\omega_{13}\omega_7\omega_8^2\omega_5^3\omega_9\omega_{12}^2 + 4\omega_6\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}^2 - \\ & 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}^2 + 12\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12}^2 + 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_5^2\omega_9\omega_{12}^2 + 4\omega_6\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 4\omega_6^2\omega_{13}\omega_7\omega_8^2\omega_5^2\omega_9\omega_{12} + \\ & 8\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}^2 + 4\omega_6^2\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}^2 + 4\omega_6\omega_{13}\omega_7\omega_8^2\omega_5^2\omega_9\omega_{12}^2 - 2\omega_6^2\omega_{13}\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12}^2 + \\ & 4\omega_6\omega_{13}\omega_7\omega_8^2\omega_5^2\omega_9\omega_{12}^2 + 8\omega_6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} - 10\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12}^2 - 4\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}^2 + 2\omega_6\omega_{13}\omega_7\omega_{14}\omega_5^2\omega_9\omega_{12}^2 + \\ & 4\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12}^2 + 4\omega_6\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 4\omega_6^2\omega_{13}\omega_7\omega_8^2\omega_5^3\omega_9\omega_{12} - 8\omega_6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}^2 + 4\omega_6^2\omega_{13}\omega_7\omega_8\omega_5^3\omega_9\omega_{12}^2 + \\ & 2\omega_6\omega_{13}\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12}^2 + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 4\omega_6^2\omega_7\omega_8^2\omega_5^3\omega_9\omega_{12}^2 - 4\omega_6\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_9\omega_{12} + 4\omega_6^2\omega_{13}\omega_7\omega_8^2\omega_5^3\omega_9\omega_{12} + \end{aligned}$$

$$6\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9^2\omega_{12}^2 + 2\omega_6^2\omega_{13}\omega_{14}\omega_8^2\omega_5^2\omega_9^2\omega_{12}^2 - 4\omega_6\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9^2\omega_{12}^2 + 4\omega_6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}^2 + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_{12} - 4\omega_6^2\omega_7\omega_8^2\omega_5^3\omega_9\omega_{12}^2 + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_9 - 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^3\omega_9^2\omega_{12}^2 - 8\omega_6\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}^2 - 4\omega_6\omega_{13}\omega_7\omega_8\omega_5^3\omega_9^2\omega_{12}^2 - 8\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_{14}\omega_8\omega_5^3\omega_9^2\omega_{12}^2 - 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}^2 + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9^2\omega_{12}^2 - 5\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9^2\omega_{12}^2 - 4\omega_6^2\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9^2\omega_{12}^2 + 2\omega_6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^2\omega_9^2\omega_{12}^2 - 4\omega_6^2\omega_{13}\omega_7\omega_8\omega_5^2\omega_9^2\omega_{12}^2 - 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_9^2\omega_{12}^2 - 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 8\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_9\omega_{12} - 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}^2 + 5\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9^2\omega_{12}^2) \frac{c_s^2 \rho v_1 v_3}{2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^3\omega_9^2\omega_{12}^2}$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{MRT}2} = C_{D_x D_y^2 D_z v_1}^{(1), \text{MRT}1}$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CLBM}1} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CLBM}2} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CuLBM}1} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CuLBM}2} = (-2\omega_3\omega_4\omega_2v_3^2 - 6\omega_3\omega_4c_s^2\omega_2 + 9\omega_4\omega_1\omega_2 + 6\omega_3\omega_4c_s^2\omega_1 - 27\omega_4c_s^2\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 - 9\omega_4\omega_1\omega_2v_3^2 + 9\omega_3\omega_1\omega_2v_3^2 - 9\omega_3\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_3^2 + 2\omega_3\omega_4\omega_2) \frac{\rho v_1 v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{MRT}1} = (2\omega_6\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6^2\omega_{17}\omega_5^2\omega_{15}^2 + 2\omega_6^2\omega_8\omega_5^3\omega_{15}^2 - 4\omega_6^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} - \omega_6^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}^2 - \omega_6^2\omega_{17}\omega_5^3\omega_{15}^2 + \omega_{17}\omega_8\omega_5^3\omega_{15}^2 - \omega_6\omega_{17}\omega_8^3\omega_5^3\omega_{15} - 4\omega_6^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} + 3\omega_6^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + \omega_6\omega_8^2\omega_5^3\omega_{15}^2 + 2\omega_6\omega_{17}\omega_8^2\omega_5^2\omega_{15}^2 - 2\omega_6^2\omega_8\omega_5^2\omega_{15}^2 - 4\omega_6^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 3\omega_6\omega_{17}\omega_8^2\omega_5\omega_{15}^2 + \omega_6^2\omega_8^3\omega_5^3\omega_{15} + 5\omega_6^2\omega_{17}\omega_8\omega_5\omega_{15}^2 + 2\omega_6\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 2\omega_6^2\omega_8^2\omega_5^2\omega_{15}^2 - 2\omega_6\omega_8\omega_5^3\omega_{15}^2 - 2\omega_6^2\omega_8^2\omega_5^2\omega_{15} - \omega_6^2\omega_{17}\omega_8^3\omega_5^3 + \omega_6\omega_{17}\omega_8^3\omega_5^2\omega_{15} - \omega_{17}\omega_8^2\omega_5^2\omega_{15}^2 + 2\omega_6^2\omega_{17}\omega_8^2\omega_5\omega_{15} + \omega_6^2\omega_{17}\omega_8\omega_5^3\omega_{15}^2 + 2\omega_6^2\omega_{17}\omega_8^2\omega_5^2 - 2\omega_6\omega_{17}\omega_8\omega_5^3\omega_{15}^2 - \omega_6^2\omega_8^2\omega_5^3\omega_{15}^2) \frac{c_s^2 \rho v_2 v_3}{\omega_6^2\omega_{17}\omega_8^2\omega_5^3\omega_{15}^2}$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{MRT}2} = C_{D_x D_y^2 D_z v_2}^{(1), \text{MRT}1}$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{CLBM}1} = 0$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{CLBM}2} = 0$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{CuLBM}1} = 0$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{CuLBM}2} = (-3\omega_3\omega_1\omega_2^3v_3^2 - 24\omega_3c_s^2\omega_1\omega_2^2 + 10\omega_3\omega_1^3\omega_2 - 20\omega_3\omega_1^2\omega_2^2 - 24\omega_3c_s^2\omega_1\omega_2^3 + 4\omega_1^2\omega_2^2v_3^2 + 2\omega_1\omega_2^3 + 28\omega_3c_s^2\omega_1^3 + 12c_s^2\omega_1^2\omega_2^2 - 13\omega_3\omega_1v_2^2\omega_2^3 + 14\omega_3\omega_1^2\omega_2 + 26\omega_3c_s^2\omega_2^3 - 4\omega_3\omega_1\omega_2^2v_3^2 - 2\omega_1^3\omega_2v_3^2 + 16\omega_3\omega_1^3v_2^2 - 6c_s^2\omega_1^3\omega_2 - 4\omega_3\omega_1^2\omega_2v_3^2 - 13\omega_3\omega_1^3v_2^2\omega_2 + 4\omega_3\omega_1^3v_3^2 - 4\omega_3\omega_1v_2^2\omega_2^3 - 6c_s^2\omega_1\omega_2^3 - 30\omega_3c_s^2\omega_1^2\omega_2 + 6\omega_3\omega_1^2\omega_2^2v_3^2 - 2\omega_1\omega_2^3v_3^2 + 26\omega_3\omega_1^2v_2^2\omega_2^3 + 4\omega_3\omega_2^3v_3^2 - 10\omega_3\omega_2^3 - 22\omega_3\omega_1^2v_2^2\omega_2 - 3\omega_3\omega_1^3\omega_2v_3^2 + 8\omega_3\omega_1\omega_2^2 - 24\omega_3c_s^2\omega_1^3\omega_2 + 2\omega_1^3\omega_2 - 12\omega_3\omega_1^3 + 10\omega_3\omega_1\omega_2^3 + 48\omega_3c_s^2\omega_1^2\omega_2^2 + 10\omega_3v_2^2\omega_2^3 - 4\omega_1^2\omega_2^2) \frac{\rho v_2 v_3}{6\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_3}^{(1)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{D_x D_y^2 D_z v_3}^{(1), \text{SRT}} = (-36 - \omega^3 - 16\omega^2 + 54\omega) \frac{c_s^4 \rho}{12\omega^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(1), \text{MRT}1} = (-18\omega_6^3\omega_{13}\omega_7c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^2\omega_{15}\omega_9\omega_{12} + 36\omega_6^3\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_8^2v_1^2\omega_5^2\omega_{15}\omega_9\omega_{12} + 24\omega_6^2\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8^2\omega_5^2v_2^2\omega_{15}\omega_9\omega_{12} + 6\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_8^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_8\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_8\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} + 6\omega_6\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_8^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_8^2\omega_5^3v_1^2\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 30\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8v_1^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 6\omega_6^3\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} - 2\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_{15}\omega_9\omega_{12} - 12\omega_6^2\omega_7^2\omega_{17}\omega_{14}\omega_8^2v_1^2\omega_5^3\omega_{15}\omega_9\omega_{12} - 24\omega_6^2\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8^2v_1^2\omega_5^3\omega_{15}\omega_{12} - 24\omega_6^2\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8^2\omega_5v_2^2\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_{15}\omega_{12} - 12\omega_1\omega_3\omega_7^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12} - 24\omega_6\omega_{13}\omega_7c_s^2\omega_{17}\omega_{14}\omega_8^2v_1^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_{15}\omega_9\omega_{12} - \omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8^2v_1^2\omega_5^3\omega_{15}\omega_{12} - 12\omega_6^3\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2v_2^2\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_{14}\omega_8^2\omega_5^3\omega_9\omega_{12} + 12\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}\omega_9\omega_{12} - 48\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8\omega_5^2\omega_{15}\omega_9\omega_{12} - 48\omega_6^3\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8\omega_5^2\omega_{15}\omega_9\omega_{12} +$$

coefficient $C_{D^3_D, v_3}^{(1)}$ at $\frac{\partial^4 v_3}{\partial x_3^3 \partial x_2}$:

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{MRT2}} = C_{D_x^2 D_z^2 v_3}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{CuLBM1}} = 0$$

coefficient $C_{D_x D_y D_z^2 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2}$:

$$C_{\mathbf{D}_x \mathbf{D}_y \mathbf{D}_z^2 \rho}^{(1), \text{SRT}} = (36\omega v_1 v_2^2 v_3^2 + 24c_s^2 v_1^2 v_2 + 36c_s^2 \omega v_1 v_3^2 + 14c_s^2 \omega^2 v_2 v_3^2 + 36c_s^2 \omega v_1 v_2^2 - 36\omega v_1^2 v_2 v_3^2 + 24c_s^2 v_2 v_3^2 + 14c_s^2 \omega^2 v_1^2 v_2 + c_s^2 \omega^3 v_1 v_2^2 + c_s^2 \omega^3 v_1 v_3^2 - 36c_s^2 \omega v_2^2 v_2 - 24c_s^2 v_1 v_2^3 - 24c_s^2 v_1 v_2^2 - 24v_1 v_2^2 v_3^2 - 14\omega^2 v_1 v_2^2 v_3^2 + 14\omega^2 v_1^2 v_2 v_3^2 - c_s^2 \omega^3 v_2 v_3^2 + 24v_1^2 v_2 v_3^2 - 36c_s^2 \omega v_2 v_3^2 - 14c_s^2 \omega^2 v_1 v_3^2 - 14c_s^2 \omega^2 v_1 v_2^2 - \omega^3 v_1^2 v_2 v_3^2 + \omega^3 v_1 v_2^2 v_3^2 - c_s^2 \omega^3 v_1^2 v_2) \frac{1}{2\omega^3}$$

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[illegible]

[illegible]

$$C_{D_x D_y D_z^2 v_3}^{(1), \text{CLBM2}} = C_{D_x D_y D_z^2 v_3}^{(1), \text{CLBM1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_3}^{(1), \text{CuLBM2}} = (-13\omega_3\omega_1\omega_2^3v_3^2 - 24\omega_3c_s^2\omega_1\omega_2^2 + 10\omega_3\omega_1^3\omega_2 + 4\omega_1^2v_2^2\omega_2^2 - 20\omega_3\omega_1^2\omega_2^2 - 24\omega_3c_s^2\omega_1\omega_2^3 + 2\omega_1\omega_2^3 + 28\omega_3c_s^2\omega_1^3 + 12c_s^2\omega_1^2\omega_2^2 - 3\omega_3\omega_1v_2^2\omega_2^3 + 14\omega_3\omega_1^2\omega_2 + 26\omega_3c_s^2\omega_2^3 - 4\omega_3\omega_1\omega_2^2v_3^2 + 4\omega_3\omega_1^2v_2^2 - 6c_s^2\omega_1^3\omega_2 - 22\omega_3\omega_1^2\omega_2v_3^2 - 3\omega_3\omega_1^3v_2^2\omega_2 + 16\omega_3\omega_1^2v_3^2 - 4\omega_3\omega_1v_2^2\omega_2^2 - 6c_s^2\omega_1\omega_2^3 - 30\omega_3c_s^2\omega_1^2\omega_2 + 26\omega_3\omega_1^2\omega_2^2v_3^2 + 6\omega_3\omega_1^2v_2^2\omega_2^2 + 10\omega_3\omega_2^3v_3^2 - 10\omega_3\omega_2^3 - 4\omega_3\omega_1^2v_2^2\omega_2 - 13\omega_3\omega_1^2\omega_2v_3^2 + 8\omega_3\omega_1\omega_2^2 - 24\omega_3c_s^2\omega_1^3\omega_2 + 2\omega_1^3\omega_2 - 2\omega_1^3v_2^2\omega_2 - 12\omega_3\omega_1^3 + 10\omega_3\omega_1\omega_2^3 + 48\omega_3c_s^2\omega_1^2\omega_2^2 + 4\omega_3v_2^2\omega_2^3 - 2\omega_1v_2^2\omega_2^3 - 4\omega_1^2\omega_2^3) \frac{\rho v_2 v_3}{6\omega_3\omega_1^2\omega_2^3}$$

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$$C_{D_2^2 v_1}^{(1), \text{CuLBM2}} = (-6\omega_3^2\omega_1^2\omega_5v_2^2 - 8\omega_3^2\omega_4c_s^2\omega_1^2\omega_5 - 18\omega_4^2c_s^2\omega_1^2\omega_5v_3^2 + 8\omega_3\omega_4^2c_s^3\omega_1\omega_5 + 6\omega_4^2\omega_1^2\omega_5v_3^2 - 12\omega_3^2\omega_4c_s^2\omega_1\omega_5v_3^2 - 12\omega_3^2\omega_4c_s^2\omega_1\omega_5v_2^2 + 6\omega_4^2\omega_1^2\omega_5v_2^2 - 6\omega_3^2\omega_1^2\omega_5v_3^2 - 18\omega_4^2c_s^2\omega_1^2\omega_5v_2^2 - 2\omega_3^2\omega_4c_s^4\omega_1^3\omega_5 - 6\omega_3\omega_4^2c_s^2\omega_1^2\omega_5v_3^2 - 3\omega_3\omega_4^2\omega_1^2\omega_5v_4^2 - 6\omega_3^2\omega_4\omega_1^2\omega_5v_4^2 + 16\omega_3^2\omega_4^2c_s^4\omega_5 + 18\omega_3^2c_s^2\omega_1^2\omega_5v_3^2 + 18\omega_3^2c_s^2\omega_1^2\omega_5v_2^2 - 3\omega_3\omega_4^2\omega_1^3\omega_5v_4^2 - 6\omega_3^2\omega_4\omega_1^2\omega_5v_4^3 - 8\omega_3^2\omega_4^2c_s^4\omega_1\omega_5 - 6\omega_3\omega_4^2c_s^2\omega_1^3\omega_5v_2^2 - 3\omega_3^2\omega_4\omega_1^3\omega_5v_2^2 - 6\omega_3\omega_4^2\omega_1^3\omega_5v_3^2 + 8\omega_3^2\omega_4c_s^2\omega_1^2\omega_5 + 12\omega_3^2\omega_4^2c_s^2\omega_1\omega_5v_2^2 - 8\omega_3\omega_4^2c_s^2\omega_1\omega_5 + 2\omega_3^2\omega_4c_s^2\omega_1^3\omega_5 + 12\omega_3\omega_4^2c_s^2\omega_1\omega_5v_3^2 - 3\omega_3^2\omega_4\omega_1^2\omega_5v_3^2 - 6\omega_3\omega_4^2\omega_1^2\omega_5v_2^2 - 3\omega_3^2\omega_4\omega_1^2\omega_5v_4^2 + 6\omega_3^2\omega_4c_s^2\omega_1^2\omega_5v_3^2 + 3\omega_4^2\omega_1^3\omega_5v_4^2 + 3\omega_4^2c_s^2\omega_1^3\omega_5v_2^2 + 6\omega_3^2\omega_4c_s^2\omega_1^2\omega_5v_2^2 + 6\omega_3^2\omega_4c_s^2\omega_1^2\omega_5v_3^2 - 9\omega_3^2c_s^2\omega_1^3\omega_5v_2^2 + 6\omega_3\omega_4^2c_s^2\omega_1\omega_5v_2^2 + 6\omega_3\omega_4^2c_s^2\omega_1\omega_5v_3^2 + 6\omega_3\omega_4^2c_s^2\omega_1\omega_5v_4^2 + 3\omega_3^2\omega_4\omega_1^2\omega_5v_4^3 + 3\omega_3^2\omega_4\omega_1^2\omega_5v_4^2 + 6\omega_3^2\omega_4c_s^2\omega_1\omega_5 + 3\omega_3^2\omega_4^2\omega_1\omega_5v_3^2 +$$

$$\begin{aligned} & 8\omega_3\omega_4^2c_s^2\omega_1^2\omega_5 + 9\omega_4^2c_s^2\omega_1^3\omega_5v_2^2 + 2\omega_3\omega_4^2c_s^4\omega_1^3\omega_5 + 3\omega_3^2\omega_1^3\omega_5v_2^2 + 9\omega_4^2c_s^2\omega_1^3\omega_5v_3^2 - 3\omega_2^2\omega_1^3\omega_5v_3^2 - 32\omega_3^2\omega_4^2c_s^4\omega_1 - 6\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_3^2 - \\ & 6\omega_4^2c_s^2\omega_1^2\omega_5v_4^2 + 6\omega_3^2\omega_1^2\omega_5v_4^3 + 32\omega_3^2\omega_4^2c_s^4\omega_1 + 6\omega_3^2\omega_1^2\omega_5v_4^2 - 6\omega_4^2c_s^2\omega_1^2\omega_5v_4^3 - 6\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2 - 8\omega_3^2\omega_4^2c_s^4\omega_1^3 + 8\omega_3^2\omega_4^2c_s^2\omega_1\omega_5 + 6\omega_3^2\omega_4^2\omega_1^2\omega_5v_3^2 + \\ & 3\omega_3\omega_4^2\omega_1^3\omega_5v_2^2 - 8\omega_3\omega_4^2c_s^2\omega_1^2\omega_5 - 2\omega_3\omega_4^2c_s^2\omega_1^3\omega_5 + 6\omega_3^2\omega_4^2\omega_1^2\omega_5v_2^2 + 3\omega_3\omega_4^2\omega_1^3\omega_5v_3^2 \bigg) \frac{\rho}{8\omega_2^2\omega_4^2\omega_1^3\omega_5} \end{aligned}$$

$$C_{D_2^2 D_2^2 v_2}^{(1), \text{SRT}} = (-\omega^3 v_1 v_3^2 + c_s^2 \omega^3 v_3 - 14\omega^2 v_1^2 v_3 + 24c_s^2 v_1 + 24v_1 v_3^2 - 36c_s^2 \omega v_1 - 14c_s^2 \omega^2 v_3 - 36\omega v_1 v_3^2 + 14c_s^2 \omega^2 v_1 + \omega^3 v_1^2 v_3 + 36c_s^2 \omega v_3 - 24v_1^2 v_3 + 14\omega^2 v_1 v_3^2 - c_s^2 \omega^3 v_1 - 24c_s^2 v_3 + 36\omega v_1^2 v_3) \frac{\rho v_2}{2\omega^3}$$

$$C_{D_y^2 D_z^2 v_2}^{(1), \text{MRT2}} = C_{D_y^2 D_z^2 v_2}^{(1), \text{MRT1}}$$

[illegible]

$$\begin{aligned}
& 5\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 24\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9 + 9\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}^2 - 12\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_9 + \\
& 6\omega_6^3\omega_{13}c_s^2\omega_{11}^2\omega_{18}\omega_9 - 12\omega_6^3c_s^2\omega_{11}^2v_1^2\omega_{18}^2\omega_9 + 24\omega_6\omega_{22}\omega_{13}\omega_{11}^2v_1^2\omega_{18}\omega_9 - 15\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}^2v_1^2\omega_{18}\omega_9 + 18\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}v_3^2\omega_{18}^2 + \\
& 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}^2v_3^2\omega_9 - 12\omega_{22}\omega_{13}c_s^4\omega_{11}^2\omega_{18}\omega_9 - 12\omega_6^2c_s^2\omega_{11}^2\omega_{18}^2\omega_9 - 12\omega_6^2\omega_{22}c_s^4\omega_{11}\omega_{18}^2\omega_9 - 108\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}^2\omega_9 - \\
& 18\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}^2\omega_9 - 6\omega_6^3\omega_{13}\omega_{11}^2v_1^2\omega_{18}^2\omega_9 - 36\omega_6^2\omega_{22}\omega_{11}v_1^2v_3^2\omega_{18}^2\omega_9 + 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}^2v_1^2v_3^2\omega_9 - 36\omega_6^3\omega_{11}^2v_1^2v_3^2\omega_{18}\omega_9 - \\
& 45\omega_6^3\omega_{22}\omega_{13}\omega_{11}^2v_1^2v_3^2\omega_{18}\omega_9 + 24\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2v_1^2\omega_{18} - 72\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2v_1^2v_3^2\omega_{18} + 36\omega_6^3\omega_{22}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 - 24\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}^2v_1^2\omega_{18} - \\
& 12\omega_6^3\omega_{22}c_s^2\omega_{11}\omega_{18}\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}^2v_1^2\omega_{18}^2 - 36\omega_6^3\omega_{13}\omega_{11}^2v_1^2v_3^2\omega_{18}\omega_9 + 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9 - \omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}^2\omega_{18}\omega_9 + \\
& 24\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}^2v_1^2\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 12\omega_6^3\omega_{13}c_s^2\omega_{11}^2v_1^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{11}v_1^2\omega_{18}^2\omega_9 + 36\omega_6^2\omega_{13}c_s^2\omega_{11}^2v_3^2\omega_{18}\omega_9 + \\
& 12\omega_6^3\omega_{11}^2v_1^2\omega_{18}\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}c_s^4\omega_{11}\omega_{18}^2 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{13}c_s^4\omega_{11}^2\omega_{18}\omega_9 - 102\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}^2v_3^2\omega_{18}\omega_9) \frac{\rho}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}^2\omega_{18}\omega_9}
\end{aligned}$$

$$C_{D_x D_x^3 v_3}^{(1), \text{MRT2}} = C_{D_x D_x^3 v_3}^{(1), \text{MRT1}}$$

$$\begin{aligned}
C_{D_x D_x^3 v_3}^{(1), \text{CLBM1}} = & (36\omega_6^3\omega_{22}v_3^2\omega_{18}\omega_9 - 18\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{18}\omega_9 - 12\omega_6^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 18\omega_6^3\omega_{13}\omega_{11}v_3^2\omega_9 + \\
& 54\omega_6^2\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9 - 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_9 + 12\omega_6^3\omega_{22}c_s^2\omega_{18}\omega_9 - 12\omega_6^3c_s^2\omega_{11}\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_9 - 18\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_9 + \\
& 18\omega_6^2\omega_{22}\omega_{13}v_3^2\omega_{18} + 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + \omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_9 + 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9 - 18\omega_6^3\omega_{13}\omega_{11}v_3^2\omega_{18} + 12\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 + \\
& 6\omega_6^3\omega_{13}\omega_{11}\omega_9 - 36\omega_6^3\omega_{22}v_3^2\omega_{18} - 36\omega_6^3\omega_{11}v_3^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{13}c_s^2\omega_{11}\omega_9 - 12\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9 + \\
& 12\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 36\omega_6\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{18} - 54\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_9 - 12\omega_6^3\omega_{22}\omega_{18}\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_9 + 12\omega_6^2\omega_{22}\omega_{18} - \\
& 6\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9 - 15\omega_6^3\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9 - 5\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_9 + 36\omega_6^2\omega_{11}v_3^2\omega_{18}\omega_9 - 12\omega_6^3\omega_{11}\omega_{18} - \\
& 12\omega_6^2\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 + 12\omega_6^3\omega_{11}\omega_{18}\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{18} - 12\omega_6^2\omega_{22}c_s^2\omega_{18}\omega_9 + 36\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_9 - 12\omega_6^2\omega_{11}\omega_{18}\omega_9 - 36\omega_6^2\omega_{22}v_3^2\omega_{18}\omega_9 + \\
& 5\omega_6^3\omega_{22}\omega_{13}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{18}\omega_9 - 6\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_{18} - 12\omega_6^2\omega_{22}c_s^2\omega_{18} + 36\omega_6\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_9 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_9 + 12\omega_6^2c_s^2\omega_{11}\omega_{18} + \\
& 18\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 36\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9 + 12\omega_6^2c_s^2\omega_{11}\omega_{18}\omega_9) \frac{c_s^2\rho}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9}
\end{aligned}$$

$$C_{D_x D_x^3 v_3}^{(1), \text{CLBM2}} = C_{D_x D_x^3 v_3}^{(1), \text{CLBM1}}$$

$$\begin{aligned}
C_{D_x D_x^3 v_3}^{(1), \text{CuLBM1}} = & (18\omega_8\omega_2^2v_3^2 + 12\omega_8\omega_2 - 54\omega_6\omega_2^2v_3^2 - 12\omega_6c_s^2\omega_8 + 36\omega_2^2v_3^2 + 18\omega_6\omega_2^3v_3^2 - \omega_8\omega_2^3 + \omega_6\omega_8\omega_2^2 + 3\omega_8\omega_2^3v_3^2 - 3\omega_6\omega_8\omega_2^2v_3^2 - 6\omega_8\omega_2^2 - \\
& 18\omega_3^3v_3^2 - 6c_s^2\omega_2^2 - 5\omega_6c_s^2\omega_8\omega_2^2 - 18\omega_6c_s^2\omega_2^2 - 12\omega_6\omega_2 - \omega_6c_s^2\omega_8\omega_2^2 + 6\omega_6c_s^2\omega_2^3 + 12c_s^2\omega_2^2 - 12c_s^2\omega_8\omega_2 - 6\omega_6\omega_2^2 + 6c_s^2\omega_8\omega_2^2 + 6\omega_2^3 - 36\omega_8\omega_2v_3^2 + \\
& 18\omega_6\omega_2^2 + c_s^2\omega_8\omega_2^2 - 12\omega_2^3 + 36\omega_6\omega_2v_3^2 + 18\omega_6c_s^2\omega_8\omega_2 + 12\omega_6c_s^2\omega_2) \frac{c_s^2\rho}{12\omega_6\omega_8\omega_2^3}
\end{aligned}$$

$$\begin{aligned}
C_{D_x D_x^3 v_3}^{(1), \text{CuLBM2}} = & (153\omega_3\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 - 4\omega_3\omega_4\omega_1^2\omega_2^2 + 12\omega_3\omega_4\omega_1\omega_2^2v_3^2 + \omega_3\omega_4\omega_1^2v_1^2\omega_2^3 - 20\omega_3\omega_4c_s^2\omega_1^3 - 28\omega_3\omega_4c_s^4\omega_1\omega_2^2 - 168\omega_3\omega_4\omega_1^2\omega_2^2v_3^4 + \\
& 432\omega_3\omega_4c_s^2\omega_1\omega_2^3v_3^2 + 60\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 - 7\omega_3\omega_4\omega_1^2\omega_2^3 - 312\omega_3\omega_4c_s^2\omega_1^3v_3^2 - 10\omega_3\omega_4\omega_1^3\omega_2 - 36\omega_3c_s^2\omega_1\omega_2^3 - 96\omega_3\omega_4\omega_1^2\omega_2v_3^2 + 94\omega_3\omega_4c_s^4\omega_1\omega_2^3 + \\
& \omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 8\omega_4c_s^2\omega_1\omega_2^3 - 138\omega_3\omega_4\omega_1^2\omega_2^3v_3^4 - 264\omega_3\omega_4\omega_1^3v_3^4 - 240\omega_3\omega_4\omega_1^3\omega_2v_3^4 + 120\omega_3\omega_4c_s^2\omega_1^2\omega_2v_3^2 - 108\omega_3c_s^2\omega_1^2\omega_2^3v_3^2 - 60\omega_3\omega_4\omega_1^3v_3^2 - \\
& 222\omega_3\omega_4\omega_1\omega_2^3v_3^2 + 32\omega_3\omega_4c_s^2\omega_1\omega_2^2 + 7\omega_3\omega_4\omega_1^3\omega_2^2 + 36\omega_3c_s^4\omega_1\omega_2^3 + 24\omega_4c_s^2\omega_1^3\omega_2v_3^2 - 3\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 - 54\omega_3\omega_4c_s^2\omega_1\omega_2^3 + 40\omega_3\omega_4c_s^2\omega_1^3 + \\
& 8\omega_3\omega_4\omega_1^2\omega_2 - 54\omega_4c_s^2\omega_1^2\omega_2^3v_3^2 - 60\omega_3\omega_4c_s^2\omega_1\omega_2^2v_3^2 - 81\omega_3\omega_4\omega_1^2\omega_2^2v_3^2 + 8\omega_4c_s^4\omega_1\omega_2^3 + 96\omega_3\omega_4\omega_1^3v_3^2 - 9\omega_4c_s^2\omega_1^2\omega_2^3 - 3\omega_3\omega_4c_s^4\omega_1^3\omega_2^3 + \\
& 8\omega_3\omega_4c_s^2\omega_1^2\omega_2 + 408\omega_3\omega_4\omega_1\omega_2^3v_3^4 - 36\omega_3c_s^4\omega_1^2\omega_2^3 + 81\omega_3\omega_4\omega_1^2\omega_2^3v_3^2 - 9\omega_3c_s^2\omega_1^2\omega_2^3 + 42\omega_3\omega_4c_s^2\omega_1^3\omega_2 + 144\omega_3\omega_4\omega_2^3v_3^2 - 54\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + \\
& 24\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 - \omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 18\omega_4c_s^4\omega_1^2\omega_2^3 + 108\omega_3c_s^2\omega_1\omega_2^2v_3^2 + 138\omega_3\omega_4\omega_1^2\omega_2v_3^2 + 8\omega_4c_s^4\omega_1^2\omega_2 + 17\omega_3\omega_4c_s^4\omega_1^2\omega_2^2 + 18\omega_4c_s^2\omega_1^2\omega_2^2 - 8\omega_3\omega_4\omega_2^3 + \\
& 138\omega_3\omega_4\omega_1^3\omega_2^2v_3^4 - \omega_3\omega_4\omega_1^2v_1^4\omega_2^2 + 20\omega_4c_s^4\omega_1^2\omega_2^2 - 90\omega_3\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 + 24\omega_4c_s^2\omega_1\omega_2^3v_3^2 + 16\omega_3\omega_4c_s^4\omega_1^3 - 6\omega_3\omega_4c_s^2\omega_1^2\omega_2^2 + 9\omega_4c_s^4\omega_1^3\omega_2^2 - \\
& 16\omega_3\omega_4c_s^2\omega_1^2\omega_2 + 4\omega_3\omega_4\omega_2^3 + 36\omega_3c_s^2\omega_1^2\omega_2^3 + 84\omega_3\omega_4\omega_1^2\omega_2^2v_3^2 + 27\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 14\omega_3\omega_4\omega_1\omega_2^3 - 29\omega_3\omega_4c_s^4\omega_1^2\omega_2^2 + 9\omega_3c_s^4\omega_1^2\omega_2^2 - 24\omega_3\omega_4\omega_1\omega_2^2v_3^4 - \\
& 68\omega_3\omega_4c_s^4\omega_2^3 - 32\omega_3\omega_4c_s^4\omega_1^3\omega_2 - 8\omega_4c_s^2\omega_1^3\omega_2 + 18\omega_4c_s^2\omega_1^2\omega_2^3 + 27\omega_3c_s^2\omega_1^3\omega_2^3v_3^2 - 24\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2^2 - 288\omega_3\omega_4c_s^4\omega_1^2\omega_2v_3^2 + \\
& 144\omega_3\omega_4c_s^2\omega_1^2v_3^2 + 3\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 - 153\omega_3\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 - 18\omega_4c_s^4\omega_1^2\omega_2^2 - 20\omega_4c_s^2\omega_1^2\omega_2^2 + 192\omega_3\omega_4\omega_1^2\omega_2v_3^4 + 10\omega_3\omega_4c_s^4\omega_1^2\omega_2^2) \frac{\rho}{36\omega_3\omega_4\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_y D_x^3 \rho}^{(1)} \text{ at } \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_x^3 \rho}^{(1), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_y D_x^3 \rho}^{(1), \text{MRT1}} = & (4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5v_3^2 - 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{11}^2\omega_8\omega_5\omega_{18} + \\
& 12\omega_6^3\omega_{19}\omega_7c_s^2\omega_{11}^2\omega_{18} - 4\omega_6^2\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} - 4\omega_6\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 12\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_5\omega_{18} + 9\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - \\
& 4\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_{18} + 12\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 4\omega_6^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8v_3^2\omega_{18} + 8\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - \\
& 4\omega_6^2\omega_{20}\omega_{11}^2\omega_8v_3^2\omega_{18}^2 - 2\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5\omega_{18} - 2\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_8v_3^2\omega_{18} - 4\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 + 4\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_5v_3^2\omega_{18} - \\
& 12\omega_6\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_8\omega_5\omega_{18} - 4\omega_6^2\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_{18} + 12\omega_6^2\omega_{19}c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18} - 4\omega_6\omega_{20}\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} - \\
& 24\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5 + 12\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_8\omega_5\omega_{18} - 4\omega_6\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} - 9\omega_6^2\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18}^2 + \\
& 4\omega_6\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 6\omega_6^2\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18} - 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 4\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_5\omega_{18} - \\
& 4\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}v_3^2\omega_{18}^2 - 12\omega_6c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18}^2 - 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18}^2 + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8v_3^2\omega_{18} + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + \\
& 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} + 12\omega_6\omega_{19}\omega_7c_s^2\omega_{11}\omega_5\omega_{18}^2 - 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5 + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} - \\
& 2\omega_6^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18}^2 + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} + 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{11}^2\omega_8\omega_5\omega_{18}^2 - 12\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_{18} + \\
& 4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_5v_3^2\omega_{18} + 4\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_5\omega_{18} + 4\omega_6^2\omega_{19}\omega_7\omega_{11}^2v_3^2\omega_{18} + 4\omega_6\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_5\omega_{18} - \\
& 12\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_5\omega_{18}^2 - 4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5\omega_{18} - 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2 - 12\omega_6^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18}^2 - 2\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} - \\
& 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} + 12\omega_6\omega_{19}\omega_7c_s^2\omega_{11}\omega_8\omega_5\omega_{18} + 12\omega_6^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 2\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} - 12\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_5 + \\
& 4\omega_6\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 + 6\omega_6^2\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5 + 12\omega_6\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18}^2 - 12\omega_6^2\omega_{19}\omega_7c_s^2\omega_{11}\omega_5\omega_{18}^2 - \\
& 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_8\omega_5\omega_{18}^2 - 4\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} - 3\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 - 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8v_3^2\omega_{18} - 4\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_5v_3^2\omega_{18} -
\end{aligned}$$

$$\begin{aligned}
& 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_5v_3^2\omega_{18}^2 + 8\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} - 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_{18} + 12\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18}^2 + 4\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + \\
& 4\omega_6^2\omega_{19}\omega_{11}^2\omega_8\omega_{18}^2 - 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} - 12\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} - 8\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 4\omega_6\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18}^2 + \\
& 2\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_{18}^2 - 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8v_3^2\omega_{18} + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_8\omega_5v_3^2\omega_{18}^2 + 4\omega_6^2\omega_{19}\omega_{20}\omega_{11}\omega_8v_3^2\omega_{18}^2 + 4\omega_6^2\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 - \\
& 12\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_{18}^2 + 3\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18}^2 - 12\omega_6^2\omega_{19}c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18}^2 + 24\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5\omega_{18}^2 - \\
& 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{11}^2\omega_8\omega_{18}^2 + 2\omega_6^2\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} - 4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_5\omega_{18}^2 + 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_{18} - 12\omega_6\omega_{19}\omega_7c_s^2\omega_{11}^2\omega_8\omega_5\omega_{18}^2 + \\
& 4\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18}^2 - 6\omega_6^2\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 2\omega_6^2\omega_7\omega_{20}\omega_{11}^2\omega_8v_3^2\omega_{18}^2 + 3\omega_6^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18}^2 + 2\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_8\omega_5\omega_{18}^2 - \\
& 8\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18}^2 + 4\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_{18}^2 + 4\omega_6^2\omega_{20}\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18}^2 - 4\omega_6\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18}^2) \frac{v_1v_2v_3}{4\omega_6^2\omega_{19}\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18}^2}
\end{aligned}$$

$$C_{D_y D_x^2 \rho}^{(1), \text{MRT}^2} = C_{D_y D_x^2 \rho}^{(1), \text{MRT}^1}$$

$$C_{D_y D_x^2 \rho}^{(1), \text{CLBM}^1} = 0$$

$$C_{D_y D_x^2 \rho}^{(1), \text{CLBM}^2} = 0$$

$$C_{D_y D_x^2 \rho}^{(1), \text{CuLBM}^1} = 0$$

$$C_{D_y D_x^2 \rho}^{(1), \text{CuLBM}^2} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{v_1 v_2 v_3}{12 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y D_x^2 v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_x^2 v_1}^{(1), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_y D_x^2 v_1}^{(1), \text{MRT}^1} = & (-\omega_6^3 \omega_8^2 \omega_5 v_3^2 \omega_{18}^2 - 6\omega_6 c_s^2 \omega_{20} \omega_8^2 \omega_5 \omega_{18}^2 - 2\omega_6 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + 2\omega_6^3 c_s^2 \omega_8 \omega_5 \omega_{18}^2 - 2\omega_6^2 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} - 7\omega_6^3 c_s^2 \omega_{20} \omega_8 \omega_5 \omega_{18}^2 + \\
& \omega_6^3 \omega_{20} \omega_8^2 \omega_5 v_3^2 \omega_{18} + \omega_6^2 \omega_{20} \omega_8 \omega_5^2 \omega_{18}^2 - 2\omega_6^2 \omega_8 \omega_5^2 \omega_{18}^2 + 2\omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 - \omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 \omega_{18} - 2\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 - \omega_6^2 \omega_{20} \omega_8^2 \omega_5 \omega_{18} + 6\omega_6 c_s^2 \omega_{20} \omega_8 \omega_5^2 \omega_{18}^2 + \\
& \omega_6^3 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 + \omega_6^3 \omega_{20} \omega_8 \omega_5 \omega_{18}^2 + \omega_6^3 c_s^2 \omega_8^2 \omega_5^2 \omega_{18}^2 + \omega_6^3 \omega_{20} \omega_8 \omega_5^2 v_3^2 \omega_{18} - 2\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 - \omega_6^2 \omega_{20} \omega_8^2 \omega_5 \omega_{18} + 2\omega_6^2 c_s^2 \omega_8 \omega_5^2 \omega_{18}^2 + 2\omega_6^2 \omega_{20} \omega_8^2 \omega_5 \omega_{18} - \\
& 11\omega_6^2 c_s^2 \omega_{20} \omega_8 \omega_5^2 \omega_{18}^2 - \omega_6^3 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} - \omega_6^3 c_s^2 \omega_8^2 \omega_5^2 \omega_{18} - 2\omega_6^3 \omega_8 \omega_5^2 v_3^2 \omega_{18} + \omega_6^3 \omega_8^2 \omega_5 \omega_{18}^2 + 2\omega_6^2 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + 4\omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + \\
& 7\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_5 \omega_{18} - \omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 + 2\omega_6^2 \omega_8 \omega_5^2 \omega_{18}^2 - 2\omega_6^3 c_s^2 \omega_{20} \omega_8^2 \omega_{18} + \omega_6 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + \omega_6^3 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} - \omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 \omega_{18} - \\
& 5\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18}^2 + 2\omega_6^2 \omega_8 \omega_5^2 v_3^2 \omega_{18} + 2\omega_6^2 c_s^2 \omega_8^2 \omega_5^2 \omega_{18} + 2\omega_6 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} - 2\omega_6^3 \omega_8 \omega_5 \omega_{18}^2 - \omega_6^3 \omega_{20} \omega_8^2 \omega_5 \omega_{18} + 2\omega_6^3 \omega_8 \omega_5 v_3^2 \omega_{18}^2 - 2\omega_6 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} + \\
& 2\omega_6^3 c_s^2 \omega_{20} \omega_5 \omega_{18} + 4\omega_6^3 c_s^2 \omega_{20} \omega_8 \omega_5 \omega_{18}^2 - 2\omega_6^2 \omega_{20} \omega_8^2 \omega_5 v_3^2 \omega_{18} - 2\omega_6^2 \omega_8^2 \omega_5^2 \omega_{18} + 2\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} - 4\omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} + \omega_6^3 c_s^2 \omega_{20} \omega_8^2 \omega_5 \omega_{18} - \\
& 8c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18}^2 - \omega_6^3 \omega_8^2 \omega_5^2 \omega_{18} - \omega_6^3 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} - \omega_6^3 \omega_{20} \omega_8 \omega_5^2 \omega_{18}^2 - \omega_6^3 c_s^2 \omega_8^2 \omega_5 \omega_{18}^2 + \omega_6^3 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + \omega_6^3 \omega_8^2 \omega_5^2 \omega_{18} + 2\omega_6^3 c_s^2 \omega_{20} \omega_8 \omega_{18}^2 + \\
& 2\omega_6^2 \omega_8^2 \omega_5^2 \omega_{18} + \omega_6^2 \omega_{20} \omega_8^2 \omega_5 v_3^2 \omega_{18} + \omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} - \omega_6^3 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 \omega_{18} - \omega_6 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18}^2 - 2\omega_6^3 c_s^2 \omega_8 \omega_5^2 \omega_{18} + \omega_6^3 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 - 2\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_{18}^2 + \\
& 13\omega_6 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} + 5\omega_6^3 c_s^2 \omega_{20} \omega_8 \omega_5^2 \omega_{18} + 4\omega_6^2 c_s^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18} - 2\omega_6^2 \omega_{20} \omega_8^2 \omega_5^2 v_3^2 - \omega_6^3 \omega_{20} \omega_8 \omega_5 v_3^2 \omega_{18} - 2\omega_6^2 c_s^2 \omega_8^2 \omega_5^2 \omega_{18}) \frac{\rho v_2 v_3}{2\omega_8^2 \omega_{20} \omega_8^2 \omega_5^2 \omega_{18}^2}
\end{aligned}$$

$$C_{D_y D_x^2 v_1}^{(1), \text{MRT}^2} = C_{D_y D_x^2 v_1}^{(1), \text{MRT}^1}$$

$$C_{D_y D_x^2 v_1}^{(1), \text{CLBM}^1} = 0$$

$$C_{D_y D_x^2 v_1}^{(1), \text{CLBM}^2} = 0$$

$$C_{D_y D_x^2 v_1}^{(1), \text{CuLBM}^1} = 0$$

$$\begin{aligned}
C_{D_y D_x^2 v_1}^{(1), \text{CuLBM}^2} = & (-18\omega_3^2 \omega_4 c_s^2 + 3\omega_3^2 \omega_1 v_3^2 - 3\omega_3^2 \omega_1 v_2^2 + 18\omega_4^2 c_s^2 \omega_1 + 18\omega_3 \omega_4^2 c_s^2 - 2\omega_3 \omega_4^2 \omega_1 v_2^2 + 6\omega_3^2 \omega_4 - 18\omega_3 \omega_4 c_s^2 \omega_1 - 2\omega_3^2 \omega_4 \omega_1 - 6\omega_3^2 \omega_4 v_2^2 + \\
& 6\omega_3^2 v_2^2 + 2\omega_3^2 \omega_4 \omega_1 v_2^2 + 2\omega_3 \omega_4^2 \omega_1 + 6\omega_3 \omega_4^2 v_2^2 - 6\omega_3^2 v_3^2 + 3\omega_4^2 \omega_1 v_3^2 - 6\omega_3 \omega_4^2 c_s^2 \omega_1 + 12\omega_3 \omega_4 v_3^2 + 6\omega_3 \omega_4 \omega_1 + 3\omega_4^2 \omega_1 v_2^2 - 6\omega_4^2 \omega_1 - 6\omega_4^2 v_2^2 - \\
& 12\omega_3 \omega_4 + 12\omega_4^2 - 6\omega_4^2 v_3^2 + 36\omega_3 \omega_4 c_s^2 + 6\omega_3^2 \omega_4 c_s^2 \omega_1 - 6\omega_3 \omega_4^2 - 6\omega_3 \omega_4 \omega_1 v_3^2 - 36\omega_4^2 c_s^2) \frac{\rho v_2 v_3}{8\omega_3^2 \omega_4^2 \omega_1}
\end{aligned}$$

$$\text{coefficient } C_{D_y D_x^2 v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_x^2 v_2}^{(1), \text{SRT}} = (2 + 3c_s^2 \omega + \omega v_3^2 - \omega - 6c_s^2 - 2v_3^2) \frac{\rho v_1 v_3}{12 \omega}$$

$$\begin{aligned}
C_{D_y D_x^2 v_2}^{(1), \text{MRT}^1} = & (6\omega_6^2 \omega_{19} \omega_7 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2 - 3\omega_6^2 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 v_3^2 \omega_{18} + 6\omega_6^2 \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 v_3^2 \omega_{18}^2 + 12\omega_6^2 \omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 v_3^2 \omega_{18}^2 + \\
& 12\omega_6 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 - 9\omega_6^2 \omega_{19} \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + 3\omega_6^2 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18} + 12\omega_6^2 \omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + 12\omega_6 \omega_7 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2 + \\
& 12\omega_6^2 \omega_{19} \omega_7^2 c_s^2 \omega_{11}^2 \omega_8 \omega_5 \omega_{18} - 6\omega_6^2 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8^2 \omega_5 v_3^2 \omega_{18} - 12\omega_6^2 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8 \omega_5 \omega_{18} - 24\omega_6 \omega_{19} \omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} - 6\omega_6^2 \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + \\
& 18\omega_6 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} - 36\omega_{19} \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} - 12\omega_6 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18} - 6\omega_6^2 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 v_3^2 \omega_{18} - 6\omega_6^2 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18} - \\
& 12\omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + 12\omega_6 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + 6\omega_6^2 \omega_{19} \omega_7^2 c_s^2 \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + 12\omega_6^2 \omega_{19} \omega_7 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} - 12\omega_6 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18}^2 + \\
& 6\omega_6^2 \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5 \omega_{18} + 12\omega_6^2 \omega_7 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 + 6\omega_6 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18} + 54\omega_6 \omega_{19} \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} - 6\omega_6^2 \omega_{19} \omega_7^2 c_s^2 \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + \\
& 6\omega_6^2 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} - 12\omega_6 \omega_{19} \omega_7^2 \omega_{11}^2 \omega_8^2 \omega_5^2 v_3^2 \omega_{18} + 6\omega_6^2 \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + 12\omega_6 \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18} + 4\omega_6^2 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 v_3^2 \omega_{18} + \\
& 12\omega_6 \omega_{19} \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18} + 6\omega_6^2 \omega_{19} \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 v_3^2 - 42\omega_6 \omega_{19} \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 + 42\omega_6^2 \omega_{19} \omega_7^2 c_s^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}^2 +
\end{aligned}$$

$$C_{D_y D_z^3 v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^2 v_3}^{(1), \text{CuLBM2}} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{\rho v_1 v_2}{36 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_z^4 \rho}^{(1)} \text{ at } \frac{\partial^4 \rho}{\partial x^3}:$$

$$C_{D_z^4 \rho}^{(1), \text{SRT}} = (c_s^2 \omega + 6v_3^4 + 3\omega v_3^2 + 2c_s^4 - 3\omega v_3^4 + 24c_s^2 v_3^2 - c_s^4 \omega - 2c_s^2 - 12c_s^2 \omega v_3^2 - 6v_3^2) \frac{v_1}{24\omega}$$

$$\begin{aligned} C_{D_z^4 \rho}^{(1), \text{MRT1}} = & (-48\omega_6 \omega_{11} v_3^4 \omega_{18} + 24\omega_6 c_s^4 \omega_{18}^2 + \omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 + 72\omega_6^2 c_s^2 \omega_{11} v_3^2 \omega_{18} + 72\omega_6^2 c_s^2 \omega_{11}^2 v_3^2 - 3\omega_6^2 \omega_{11}^2 v_3^4 \omega_{18}^2 - 144\omega_6 c_s^2 \omega_{11} v_3^2 \omega_{18} - 24c_s^2 \omega_{11} \omega_{18}^2 + \\ & 48\omega_{11} v_3^4 \omega_{18}^2 - 72\omega_6 v_3^2 \omega_{18}^2 - 48\omega_6 c_s^4 \omega_{11} \omega_{18}^2 - 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 48\omega_{11}^2 v_3^2 \omega_{18} + 24\omega_6 c_s^2 \omega_{11}^2 - 24\omega_6^2 \omega_{11} v_3^2 \omega_{18} - \omega_6^2 c_s^4 \omega_{11}^2 \omega_{18}^2 - 36\omega_6^2 v_3^4 \omega_{18}^2 - \\ & 36\omega_6^2 \omega_{11} v_3^2 \omega_{18}^2 - 216c_s^2 \omega_{11}^2 v_3^2 \omega_{18} - 30\omega_6^2 \omega_{11}^2 v_3^4 \omega_{18} - 432\omega_6 c_s^2 \omega_{11} v_3^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 + 150\omega_6^2 c_s^2 \omega_{11} v_3^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{18}^2 + 12\omega_6^2 \omega_{11}^2 v_3^4 + 24c_s^4 \omega_{11} \omega_{18}^2 - \\ & 96\omega_6 \omega_{11}^2 v_3^2 \omega_{18} + 48\omega_6 c_s^2 \omega_{11} \omega_{18}^2 - 96\omega_6 \omega_{11} v_3^4 \omega_{18}^2 + 24\omega_6 \omega_{11}^2 v_3^2 - 144\omega_6^2 c_s^2 v_3^2 \omega_{18}^2 + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 3\omega_6^2 \omega_{11}^2 v_3^2 \omega_{18}^2 - 48\omega_{11} v_3^2 \omega_{18}^2 + 72\omega_6 v_3^4 \omega_{18}^2 - \\ & 48\omega_{11}^2 v_3^4 \omega_{18} + 24\omega_6^2 \omega_{11} v_3^4 \omega_{18} - 24\omega_6 c_s^4 \omega_{11}^2 + 48\omega_6 c_s^4 \omega_{11}^2 \omega_{18} + 48\omega_6 \omega_{11} v_3^2 \omega_{18} - 24\omega_6 c_s^2 \omega_{18}^2 - 24\omega_6 \omega_{11}^2 v_3^4 - 12\omega_6^2 c_s^2 \omega_{11}^2 v_3^2 \omega_{18}^2 + 14\omega_6^2 c_s^4 \omega_{11} \omega_{18}^2 + \\ & 24c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 \omega_{11}^2 v_3^2 - 144\omega_6 c_s^2 \omega_{11}^2 v_3^2 - 12\omega_6^2 c_s^4 \omega_{18}^2 + 96\omega_6 \omega_{11}^2 v_3^4 \omega_{18} + 96\omega_6 \omega_{11} v_3^2 \omega_{18}^2 - 126\omega_6^2 c_s^2 \omega_{11}^2 v_3^2 \omega_{18} + 288\omega_6 c_s^2 v_3^2 \omega_{18}^2 - 48\omega_6 c_s^2 \omega_{11}^2 \omega_{18} - \\ & 14\omega_6^2 c_s^2 \omega_{11} \omega_{18}^2 + 36\omega_6^2 v_3^2 \omega_{18}^2 + 36\omega_6^2 \omega_{11} v_3^2 \omega_{18} + 432\omega_6 c_s^2 \omega_{11}^2 v_3^2 \omega_{18} + 216c_s^2 \omega_{11} v_3^2 \omega_{18}^2 - 12\omega_6^2 c_s^2 \omega_{11}^2 + 30\omega_6^2 \omega_{11}^2 v_3^2 \omega_{18} - 24c_s^4 \omega_{11}^2 \omega_{18}) \frac{v_1}{24\omega_6^2 \omega_{11} \omega_{18}} \end{aligned}$$

$$C_{D_z^4 \rho}^{(1), \text{MRT2}} = C_{D_z^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(1), \text{CLBM1}} = (-12c_s^2 \omega_{11} v_3^2 + 6v_3^4 - 3\omega_{11} v_3^4 + c_s^2 \omega_{11} + 2c_s^4 + 24c_s^2 v_3^2 + 3\omega_{11} v_3^2 - 2c_s^2 - c_s^4 \omega_{11} - 6v_3^2) \frac{v_1}{24\omega_{11}}$$

$$C_{D_z^4 \rho}^{(1), \text{CLBM2}} = C_{D_z^4 \rho}^{(1), \text{CLBM1}}$$

$$C_{D_z^4 \rho}^{(1), \text{CuLBM1}} = (6v_3^4 - 3\omega_6 v_3^4 + 2c_s^4 - \omega_6 c_s^4 - 12\omega_6 c_s^2 v_3^2 + \omega_6 c_s^2 + 24c_s^2 v_3^2 - 2c_s^2 + 3\omega_6 v_3^2 - 6v_3^2) \frac{v_1}{24\omega_6}$$

$$\begin{aligned} C_{D_z^4 \rho}^{(1), \text{CuLBM2}} = & (12\omega_2 v_3^4 + 2c_s^4 \omega_1 - 6\omega_1 v_3^2 + 9\omega_1 \omega_2 v_3^2 - 36c_s^2 \omega_1 \omega_2 v_3^2 + 48c_s^2 \omega_2 v_3^2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 24c_s^2 \omega_1 v_3^2 - 2c_s^2 \omega_1 + 6\omega_1 v_3^4 - \\ & 9\omega_1 \omega_2 v_3^4 - 12\omega_2 v_3^2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{v_1}{72\omega_1 \omega_2} \end{aligned}$$

$$\text{coefficient } C_{D_z^4 v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x^3}:$$

$$C_{D_z^4 v_1}^{(1), \text{SRT}} = (-84c_s^2 \omega^2 v_3^2 + 36c_s^2 \omega - 72v_3^4 + 3\omega^3 v_3^4 + c_s^2 \omega^3 + 6c_s^2 \omega^3 v_3^2 - 108\omega v_3^2 - 42\omega^2 v_3^4 - 14c_s^2 \omega^2 + 48c_s^4 + 108\omega v_3^4 - 144c_s^2 v_3^2 + 42\omega^2 v_3^2 - 72c_s^4 \omega - 24c_s^2 + 30c_s^4 \omega^2 - 3\omega^3 v_3^2 - 3c_s^4 \omega^3 + 216c_s^2 \omega v_3^2 + 72v_3^2) \frac{\rho}{24\omega^3}$$

$$\begin{aligned} C_{D_z^4 v_1}^{(1), \text{MRT1}} = & (6\omega_6^3 c_s^4 \omega_{18} + 24\omega_6^2 v_3^2 - 48\omega_6 c_s^4 \omega_{18}^2 + 48\omega_6^2 c_s^2 v_3^2 \omega_{18} + 6\omega_6^3 c_s^2 v_3^2 \omega_{18}^2 + 24\omega_6^2 c_s^2 \omega_{18} + 24c_s^4 \omega_{18}^2 - 24\omega_6 v_3^2 \omega_{18}^2 + 18\omega_6^3 v_3^2 \omega_{18} + \\ & 72\omega_6^2 v_3^4 \omega_{18} - 24\omega_6^2 c_s^2 v_3^2 - 24\omega_6^2 v_3^4 \omega_{18}^2 + 48\omega_6 v_3^2 \omega_{18} - 12\omega_6^3 v_3^2 - 3\omega_6^3 v_3^2 \omega_{18}^2 - 12\omega_6^2 c_s^2 v_3^2 \omega_{18} - 8\omega_6^2 c_s^2 \omega_{18}^2 - 3\omega_6^3 c_s^4 \omega_{18}^2 + 24\omega_6 c_s^4 \omega_{18} - \\ & 72\omega_6^2 c_s^2 v_3^2 \omega_{18}^2 + 24\omega_6 v_3^2 \omega_{18}^2 + 12\omega_6^3 v_3^4 - 18\omega_6^3 v_3^2 \omega_{18} - 24\omega_6 c_s^2 v_3^2 \omega_{18} - 72\omega_6^2 v_3^2 \omega_{18} - 6\omega_6^3 c_s^2 \omega_{18} + 12\omega_6 c_s^2 \omega_{18}^2 - 24\omega_6^2 c_s^4 \omega_{18} - 96c_s^2 v_3^2 \omega_{18}^2 + \\ & 24\omega_6^2 c_s^4 \omega_{18}^2 - 24\omega_6^2 v_3^4 + \omega_6^2 c_s^2 \omega_{18}^2 - 24\omega_6 c_s^2 \omega_{18} + 156\omega_6 c_s^2 v_3^2 \omega_{18}^2 + 24\omega_6^2 v_3^2 \omega_{18}^2 - 48\omega_6 v_3^4 \omega_{18} + 3\omega_6^3 v_3^4 \omega_{18}^2 + 12\omega_6^3 c_s^2 v_3^2) \frac{\rho}{24\omega_6^3 \omega_{18}^2} \end{aligned}$$

$$C_{D_z^4 v_1}^{(1), \text{MRT2}} = C_{D_z^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^4 v_1}^{(1), \text{CLBM1}} =$$

$$\begin{aligned} & (6\omega_6^3 c_s^4 \omega_{18} + 72\omega_6^2 v_3^2 - 48\omega_6 c_s^4 \omega_{18}^2 + 144\omega_6^2 c_s^2 v_3^2 \omega_{18} + 6\omega_6^3 c_s^2 v_3^2 \omega_{18}^2 + 24\omega_6^2 c_s^2 \omega_{18} + 24c_s^4 \omega_{18}^2 + 30\omega_6^3 v_3^2 \omega_{18} + 72\omega_6^2 v_3^4 \omega_{18} - 216\omega_6^2 c_s^2 v_3^2 - 12\omega_6^2 v_3^4 \omega_{18}^2 - \\ & 36\omega_6^3 v_3^2 - 3\omega_6^3 v_3^2 \omega_{18}^2 - 72\omega_6^2 c_s^2 v_3^2 \omega_{18} - 8\omega_6^2 c_s^2 \omega_{18}^2 - 3\omega_6^3 c_s^4 \omega_{18}^2 + 24\omega_6 c_s^4 \omega_{18} - 12\omega_6^2 c_s^2 v_3^2 \omega_{18}^2 + 36\omega_6^3 v_3^4 - 30\omega_6^3 v_3^2 \omega_{18} + 72\omega_6 c_s^2 v_3^2 \omega_{18} - 72\omega_6^2 v_3^2 \omega_{18} - \\ & 6\omega_6^3 c_s^2 \omega_{18} + 12\omega_6 c_s^2 \omega_{18}^2 - 24\omega_6^2 c_s^4 \omega_{18} + 24\omega_6^2 c_s^4 \omega_{18}^2 - 72\omega_6^2 v_3^4 + \omega_6^2 c_s^2 \omega_{18}^2 - 24\omega_6 c_s^2 \omega_{18} - 36\omega_6 c_s^2 v_3^2 \omega_{18}^2 + 12\omega_6^2 v_3^2 \omega_{18}^2 + 3\omega_6^3 v_3^4 \omega_{18}^2 + 108\omega_6^3 c_s^2 v_3^2) \frac{\rho}{24\omega_6^3 \omega_{18}^2} \end{aligned}$$

$$C_{D_z^4 v_1}^{(1), \text{CLBM2}} = C_{D_z^4 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_z^4 v_1}^{(1), \text{CuLBM1}} =$$

$$\begin{aligned} & (-48c_s^4 \omega_8^2 \omega_2 - 72\omega_8 \omega_2^2 v_3^2 - 12\omega_8^2 \omega_2^2 v_3^4 + c_s^2 \omega_8^2 \omega_2^3 - 72c_s^2 \omega_8 \omega_2^3 v_3^2 + 72\omega_2^2 v_3^2 - 8c_s^2 \omega_8^2 \omega_2^2 + 12c_s^2 \omega_8^2 \omega_2 + 3\omega_8^2 \omega_2^3 v_3^4 - 36c_s^2 \omega_8^2 \omega_2 v_3^2 - 3c_s^4 \omega_8^2 \omega_2^3 + \\ & 30\omega_8 \omega_2^3 v_3^2 - 36\omega_8^3 v_3^2 + 144c_s^2 \omega_8 \omega_2^2 v_3^2 + 24c_s^4 \omega_8^2 \omega_2^2 - 30\omega_8 \omega_2^3 v_3^4 - 216c_s^2 \omega_2^2 v_3^2 - 24c_s^4 \omega_8 \omega_2^2 - 3\omega_8^2 \omega_2^3 v_3^2 + 72c_s^2 \omega_8 \omega_2 v_3^2 - 24c_s^2 \omega_8 \omega_2 - 12c_s^2 \omega_8^2 \omega_2^2 v_3^2 + \\ & 6c_s^4 \omega_8 \omega_2^3 + 36\omega_2^3 v_3^4 + 12\omega_8^2 \omega_2^2 v_3^2 + 108c_s^2 \omega_2^2 v_3^2 + 24c_s^4 \omega_8^2 + 72\omega_8 \omega_2^2 v_3^4 + 24c_s^2 \omega_8 \omega_2^2 - 72\omega_2^2 v_3^4 + 24c_s^4 \omega_8 \omega_2 + 6c_s^2 \omega_8^2 \omega_2^3 v_3^2 - 6c_s^2 \omega_8 \omega_2^3) \frac{\rho}{24\omega_8^2 \omega_2^3} \end{aligned}$$

$$\begin{aligned} C_{D_z^4 v_1}^{(1), \text{CuLBM2}} = & (-3\omega_3^2 \omega_4^2 \omega_3^3 v_3^2 - 12\omega_3^2 \omega_4 c_s^4 \omega_1^2 + 36\omega_3 \omega_4 \omega_1^2 v_3^2 + 36\omega_3 \omega_4 \omega_1^2 v_3^4 - 12\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_3^2 + 12\omega_3^2 \omega_4^2 c_s^2 \omega_1 - 15\omega_3^2 \omega_4 \omega_1^3 v_3^4 + \\ & 12\omega_3 \omega_4 c_s^4 \omega_1 + 72\omega_3 \omega_4 c_s^2 \omega_1^2 v_3^2 + 27\omega_3^2 c_s^2 \omega_1^3 v_3^2 + 3\omega_3^2 \omega_4 c_s^4 \omega_1^3 + 24\omega_3^2 \omega_4 c_s^4 + 27\omega_1^2 c_s^2 \omega_1^3 v_3^2 - 9\omega_1^2 \omega_1^3 v_3^2 - 18\omega_3^2 \omega_1^3 v_3^4 + \omega_3^2 \omega_1^2 c_s^2 \omega_1^3 + \end{aligned}$$

$$6\omega_3\omega_4^2c_s^2\omega_1^3v_3^2 + 36\omega_3\omega_4\omega_1^2v_3^4 - 15\omega_3\omega_4^2\omega_1^3v_3^4 - 12\omega_3\omega_4^2c_s^4\omega_1^2 - 18\omega_3\omega_4\omega_1^3v_3^2 + 12\omega_3^2\omega_4^2\omega_1^2v_3^2 - 54\omega_4^2c_s^2\omega_1^2v_3^2 + 9\omega_3^2\omega_1^4v_3^4 + 18\omega_4^2\omega_1^2v_3^2 + 36\omega_3^2\omega_4c_s^2\omega_1v_3^2 - 8\omega_3^2\omega_4^2c_s^2\omega_1^2 + 12\omega_3^2\omega_4c_s^4\omega_1 - 36\omega_3\omega_4^2c_s^2\omega_1^3v_3^2 - 54\omega_3^2c_s^2\omega_1^2v_3^2 + 3\omega_3\omega_4^2c_s^4\omega_1^3 + 72\omega_3\omega_4c_s^2\omega_1^3v_3^4 - 12\omega_3\omega_4^2c_s^2\omega_1 - 12\omega_3^2\omega_4^2\omega_1^2v_3^4 - 3\omega_3^2\omega_4c_s^2\omega_1^3 - 36\omega_3^2\omega_4\omega_1^2v_3^2 + 15\omega_3\omega_4^2\omega_1^3v_3^2 + 12\omega_3^2\omega_4c_s^2\omega_1^2 - 108\omega_3\omega_4c_s^2\omega_1^3v_3^2 - 18\omega_4^2\omega_1^4v_3^4 - 9\omega_3^2\omega_1^3v_3^2 - 48\omega_3^2\omega_4c_s^4\omega_1 - 36\omega_3\omega_4^2\omega_1^3v_3^2 + 36\omega_3\omega_4^2c_s^2\omega_1v_3^2 + 15\omega_3^2\omega_4\omega_1^3v_3^2 + 24\omega_3^2\omega_4c_s^4\omega_1^2 - 12\omega_3^2\omega_4c_s^2\omega_1 + 3\omega_3^2\omega_4^2\omega_1^3v_3^2 - 3\omega_3\omega_4^2c_s^2\omega_1^3 - 36\omega_3\omega_4c_s^2\omega_1^3v_3^2 - 36\omega_3\omega_4\omega_1^2v_3^4 - 3\omega_3^2\omega_4^2c_s^4\omega_1^3 + 54\omega_3\omega_4c_s^2\omega_1^3v_3^2 + 18\omega_3^2\omega_1^2v_3^2 + 9\omega_4^2\omega_1^3v_3^2 + 12\omega_3\omega_4^2c_s^2\omega_1^2 - 36\omega_3^2\omega_4c_s^2\omega_1v_3^2) \frac{\rho v_1 v_3}{24\omega_3^2\omega_4^2\omega_1^3}$$

coefficient $C_{D_z^4 v_3}^{(1)}$ at $\frac{\partial^4 v_3}{\partial x_3^4}$:

$$C_{D_z^4 v_3}^{(1), \text{SRT}} = (-4 - 3c_s^2\omega - 5\omega v_3^2 + 2\omega + 6c_s^2 + 10v_3^2) \frac{\rho v_1 v_3}{12\omega}$$

$$C_{D_z^4 v_3}^{(1), \text{MRT1}} = (-24\omega_6c_s^2\omega_{11}\omega_{18} + 36\omega_{11}^2\omega_{18} - 3\omega_6^2c_s^2\omega_{11}\omega_{18} - 12\omega_6^2\omega_{11}\omega_{18} + 60c_s^2\omega_{11}\omega_{18}^2 - 72\omega_6\omega_{11}^2\omega_{18} + 120\omega_6v_3^2\omega_{18}^2 + 24\omega_6^2\omega_{18}^2 - 84\omega_{11}^2v_3^2\omega_{18} - 48\omega_6c_s^2\omega_{11}^2 + 36\omega_6\omega_{11}^2v_3^2\omega_{18} + 61\omega_6\omega_{11}v_3^2\omega_{18}^2 + 24\omega_6\omega_{11}^2 - 36\omega_6^2c_s^2\omega_{18} + 168\omega_6\omega_{11}^2v_3^2\omega_{18} - 120\omega_6c_s^2\omega_{11}\omega_{18}^2 - 48\omega_6\omega_{11}^2v_3^2 - 25\omega_6^2\omega_{11}\omega_{18}^2 - 33\omega_6^2c_s^2\omega_{11}^2\omega_{18} - 5\omega_6^2\omega_{11}^2v_3^2\omega_{18} + 84\omega_{11}^2v_3^2\omega_{18}^2 + 12\omega_6^2c_s^2\omega_{11}\omega_{18} - 36\omega_{11}^2\omega_{18}^2 + 2\omega_6^2\omega_{11}^2\omega_{18} - 72\omega_6\omega_{11}^2v_3^2\omega_{18} + 72\omega_6c_s^2\omega_{18}^2 + 72\omega_6\omega_{11}\omega_{18} - 60c_s^2\omega_{11}^2\omega_{18} + 24\omega_6^2\omega_{11}^2v_3^2 - 12\omega_6^2\omega_{11}^2 + 24\omega_6\omega_{11}\omega_{18} - 48\omega_6\omega_{18}^2 - 168\omega_6\omega_{11}^2v_3^2\omega_{18} + 120\omega_6c_s^2\omega_{11}^2\omega_{18} + 21\omega_6^2\omega_{11}^2\omega_{18} + 39\omega_6^2c_s^2\omega_{11}\omega_{18} - 60\omega_6^2v_3^2\omega_{18} + 24\omega_6^2c_s^2\omega_{11}^2 - 51\omega_6^2\omega_{11}^2v_3^2\omega_{18}) \frac{\rho v_1 v_3}{12\omega_6^2\omega_{11}^2\omega_{18}^2}$$

$$C_{D_z^4 v_3}^{(1), \text{MRT2}} = C_{D_z^4 v_3}^{(1), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(1), \text{CLBM1}} = (-4 - 3c_s^2\omega_{11} + 2\omega_{11} - 5\omega_{11}v_3^2 + 6c_s^2 + 10v_3^2) \frac{\rho v_1 v_3}{12\omega_{11}}$$

$$C_{D_z^4 v_3}^{(1), \text{CLBM2}} = C_{D_z^4 v_3}^{(1), \text{CLBM1}}$$

$$C_{D_z^4 v_3}^{(1), \text{CuLBM1}} = (-4 + 2\omega_6 - 3\omega_6c_s^2 + 6c_s^2 - 5\omega_6v_3^2 + 10v_3^2) \frac{\rho v_1 v_3}{12\omega_6}$$

$$C_{D_z^4 v_3}^{(1), \text{CuLBM2}} = (10\omega_1v_3^2 - 15\omega_1\omega_2v_3^2 + 6\omega_1\omega_2 - 4\omega_1 + 6c_s^2\omega_1 - 8\omega_2 + 20\omega_2v_3^2 + 12c_s^2\omega_2 - 9c_s^2\omega_1\omega_2) \frac{\rho v_1 v_3}{36\omega_1\omega_2}$$

3.3 Conservation of momentum: ρv_2

$$\begin{aligned} & v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + v_1 v_2 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \rho v_2 \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \rho v_1 \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_1} + (c_s^2 + v_2^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + 2\rho v_2 \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + v_2 v_3 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \rho v_3 \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\ & \rho v_2 \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + C_{D_x \rho, D_x v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + C_{D_x \rho, D_y v_1}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + C_{D_x v_1, D_y v_1}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_2} + C_{D_y \rho, D_x v_1}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\ & C_{D_y \rho, D_y v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + C_{D_y v_2, D_y v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + C_{D_y \rho, D_z v_3}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + C_{D_y v_3, D_z v_3}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial v_3}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\ & C_{D_z \rho, D_y v_3}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + C_{D_z \rho, D_z v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + C_{D_z^2 v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_1^2} + C_{D_x D_y \rho}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + C_{D_x D_y v_1}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\ & C_{D_y^2 \rho}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_2^2} + C_{D_y^2 v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_2}{\partial x_2^2} + C_{D_y D_z \rho}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + C_{D_y D_z v_3}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + C_{D_z^2 v_2}^{(2)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_2}{\partial x_3^2} + C_{D_x^3 \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & C_{D_x^3 v_1}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1^3} + C_{D_x^3 v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1^3} + C_{D_x^2 D_y \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + C_{D_x^2 D_y v_1}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + C_{D_x^2 D_y v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\ & C_{D_x D_y^2 \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + C_{D_x D_y^2 v_1}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_{D_x D_y^2 v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_{D_y^3 \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_2^3} + C_{D_y^3 v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_2^3} + \\ & C_{D_x^2 D_z v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} + C_{D_x^2 D_z v_3}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + C_{D_x D_y D_z \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{D_x D_y D_z v_1}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\ & C_{D_x D_y D_z v_3}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{D_y^2 D_z \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z v_3}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_{D_x D_z^2 v_1}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & C_{D_x D_z^2 v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_{D_y D_z^2 \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + C_{D_y D_z^2 v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{D_y D_z^2 v_3}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{D_x^3 \rho}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & C_{D_x^3 v_2}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1^3} + C_{D_x^3 v_3}^{(2)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_1^3} + C_{D_x^4 \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1^4} + C_{D_x^4 v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1^4} + C_{D_x^4 v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1^4} + C_{D_x^3 D_y \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\ & C_{D_x^3 D_y v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{D_x^3 D_y v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{D_x^2 D_y^2 \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\ & C_{D_x D_y^3 \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{D_y^4 \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_2^4} + C_{D_y^4 v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_2^4} + C_{D_x^3 D_z \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} \\ & + C_{D_x^3 D_z v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_3}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{D_x^2 D_y D_z \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\ & C_{D_x^2 D_y D_z v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_3}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x D_y^2 D_z \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\ & C_{D_x D_y^2 D_z v_1}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_2}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_3}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_y^3 D_z \rho}^{(2)} \frac{\delta_l^4}{\delta_t^4} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + \end{aligned}$$

$$\begin{aligned}
& C_{D_y^3 D_z v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_x^2 D_z^2 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{D_x^2 D_z^2 v_1}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + C_{D_x^2 D_z^2 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3} + \\
& C_{D_x^2 D_z^2 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + C_{D_x D_y D_z^2 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{D_x D_y D_z^2 v_1}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{D_x D_y D_z^2 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& C_{D_x D_y D_z^2 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{D_y^2 D_z^2 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z^2 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z^2 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{D_x D_z^3 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + \\
& C_{D_x D_z^3 v_1}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} + C_{D_x D_z^3 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_3} + C_{D_x D_z^3 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} + C_{D_y D_z^3 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3} + C_{D_y D_z^3 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + \\
& C_{D_y D_z^3 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3} + C_{D_z^4 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3} + C_{D_z^4 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_3} + C_{D_z^4 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3} = 0,
\end{aligned}$$

where:

coefficient $C_{D_x \rho, D_x v_2}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1}$:

$$\begin{aligned}
C_{D_x \rho, D_x v_2}^{(2), \text{SRT}} &= (-2 + \omega) \frac{c_s^2}{2\omega} \\
C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}} &= (-2 + \omega_5) \frac{c_s^2}{2\omega_5} \\
C_{D_x \rho, D_x v_2}^{(2), \text{MRT2}} &= C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}} \\
C_{D_x \rho, D_x v_2}^{(2), \text{CLBM1}} &= C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}} \\
C_{D_x \rho, D_x v_2}^{(2), \text{CLBM2}} &= C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}} \\
C_{D_x \rho, D_x v_2}^{(2), \text{CuLBM1}} &= (-2 + \omega_1) \frac{c_s^2}{2\omega_1} \\
C_{D_x \rho, D_x v_2}^{(2), \text{CuLBM2}} &= C_{D_x \rho, D_x v_2}^{(2), \text{CuLBM1}}
\end{aligned}$$

coefficient $C_{D_x \rho, D_y v_1}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2}$:

$$\begin{aligned}
C_{D_x \rho, D_y v_1}^{(2), \text{SRT}} &= (-2 + \omega) \frac{c_s^2}{2\omega} \\
C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}} &= (-2 + \omega_5) \frac{c_s^2}{2\omega_5} \\
C_{D_x \rho, D_y v_1}^{(2), \text{MRT2}} &= C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}} \\
C_{D_x \rho, D_y v_1}^{(2), \text{CLBM1}} &= C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}} \\
C_{D_x \rho, D_y v_1}^{(2), \text{CLBM2}} &= C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}} \\
C_{D_x \rho, D_y v_1}^{(2), \text{CuLBM1}} &= (-2 + \omega_1) \frac{c_s^2}{2\omega_1} \\
C_{D_x \rho, D_y v_1}^{(2), \text{CuLBM2}} &= (-2\omega_1 - 6v_1^2\omega_2 + 6c_s^2\omega_1 + 2\omega_2 - 12c_s^2\omega_2 + 3c_s^2\omega_1\omega_2 + 6\omega_1v_1^2) \frac{1}{6\omega_1\omega_2}
\end{aligned}$$

coefficient $C_{D_x v_1, D_y v_1}^{(2)}$ **at** $\frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_2}$:

$$\begin{aligned}
C_{D_x v_1, D_y v_1}^{(2), \text{SRT}} &= 0 \\
C_{D_x v_1, D_y v_1}^{(2), \text{MRT1}} &= 0 \\
C_{D_x v_1, D_y v_1}^{(2), \text{MRT2}} &= 0 \\
C_{D_x v_1, D_y v_1}^{(2), \text{CLBM1}} &= 0 \\
C_{D_x v_1, D_y v_1}^{(2), \text{CLBM2}} &= 0 \\
C_{D_x v_1, D_y v_1}^{(2), \text{CuLBM1}} &= 0
\end{aligned}$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2\rho v_1}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_x v_1}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_y \rho, D_x v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{MRT1}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{MRT2}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CuLBM2}} = (-\omega_1 - 3v_1^2 \omega_2 + c_s^2 \omega_1 + \omega_2 - c_s^2 \omega_2 + 3\omega_1 v_1^2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_y v_2}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_y \rho, D_y v_2}^{(2), \text{SRT}} = (-2 - 2c_s^2 \omega - 3\omega v_2^2 + \omega + 4c_s^2 + 6v_2^2) \frac{1}{\omega}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}} = (-2 + \omega_{10} - 2\omega_{10} c_s^2 + 4c_s^2 + 6v_2^2 - 3\omega_{10} v_2^2) \frac{1}{\omega_{10}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{MRT2}} = C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CLBM1}} = C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CLBM2}} = C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CuLBM1}} = (-2 - 2c_s^2 \omega_5 - 3\omega_5 v_2^2 + \omega_5 + 4c_s^2 + 6v_2^2) \frac{1}{\omega_5}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CuLBM2}} = (6\omega_1 v_2^2 + 12v_2^2 \omega_2 + 3\omega_1 \omega_2 - 2\omega_1 - 9\omega_1 v_2^2 \omega_2 + 4c_s^2 \omega_1 - 4\omega_2 + 8c_s^2 \omega_2 - 6c_s^2 \omega_1 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_y v_2, D_y v_2}^{(2)}$ **at** $\left(\frac{\partial v_2}{\partial x_2} \right)^2$:

$$C_{D_y v_2, D_y v_2}^{(2), \text{SRT}} = (2 - \omega) \frac{3\rho v_2}{\omega}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}} = (2 - \omega_{10}) \frac{3\rho v_2}{\omega_{10}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{MRT2}} = C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CLBM1}} = C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CLBM2}} = C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CuLBM1}} = (2 - \omega_5) \frac{3\rho v_2}{\omega_5}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CuLBM2}} = (-3\omega_1 \omega_2 + 2\omega_1 + 4\omega_2) \frac{\rho v_2}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_z v_3}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_y \rho, D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{MRT1}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{MRT2}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CuLBM2}} = (3\omega_1 v_3^2 - \omega_1 + c_s^2 \omega_1 + \omega_2 - 3\omega_2 v_3^2 - c_s^2 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_y v_3, D_z v_3}^{(2)}$ **at** $\frac{\partial v_3}{\partial x_2} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_y v_3, D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{MRT1}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{MRT2}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2\rho v_3}{\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_y v_3}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2}$:

$$C_{D_z \rho, D_y v_3}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{MRT2}} = C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CLBM1}} = C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CLBM2}} = C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CuLBM2}} = (6\omega_1 v_3^2 - 2\omega_1 + 6c_s^2 \omega_1 + 2\omega_2 - 6\omega_2 v_3^2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{1}{6\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_z v_2}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_z \rho, D_z v_2}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{MRT2}} = C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CLBM1}} = C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CLBM2}} = C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_x^2 v_2}^{(2)}$ **at** $\frac{\partial^2 v_2}{\partial x_1^2}$:

$$C_{D_x^2 v_2}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x^2 v_2}^{(2), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_x^2 v_2}^{(2), \text{MRT2}} = C_{D_x^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 v_2}^{(2), \text{CLBM1}} = C_{D_x^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 v_2}^{(2), \text{CLBM2}} = C_{D_x^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 v_2}^{(2), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_x^2 v_2}^{(2), \text{CuLBM2}} = C_{D_x^2 v_2}^{(2), \text{CuLBM1}}$$

coefficient $C_{D_x D_y \rho}^{(2)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y \rho}^{(2), \text{MRT1}} = 0$$

$$C_{D_x D_y \rho}^{(2), \text{MRT2}} = 0$$

$$C_{D_x D_y \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(2), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{v_1}{3\omega_1 \omega_2}$$

coefficient $C_{D_x D_y v_1}^{(2)}$ **at** $\frac{\partial^2 v_1}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y v_1}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_y v_1}^{(2), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_x D_y v_1}^{(2), \text{MRT2}} = C_{D_x D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(2), \text{CLBM1}} = C_{D_x D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(2), \text{CLBM2}} = C_{D_x D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(2), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_x D_y v_1}^{(2), \text{CuLBM2}} = (-2\omega_1 - 6v_1^2 \omega_2 + 2c_s^2 \omega_1 + 2\omega_2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 + 6\omega_1 v_1^2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_y^2 \rho}^{(2)}$ **at** $\frac{\partial^2 \rho}{\partial x_2^2}$:

$$C_{D_y^2 \rho}^{(2), \text{SRT}} = (-2 - 3c_s^2 \omega - \omega v_2^2 + \omega + 6c_s^2 + 2v_2^2) \frac{v_2}{2\omega}$$

$$C_{D_y^2 \rho}^{(2), \text{MRT1}} = (-2 + \omega_{10} - 3\omega_{10} c_s^2 + 6c_s^2 + 2v_2^2 - \omega_{10} v_2^2) \frac{v_2}{2\omega_{10}}$$

$$C_{D_y^2 \rho}^{(2), \text{MRT2}} = C_{D_y^2 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^2 \rho}^{(2), \text{CLBM1}} = C_{D_y^2 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^2 \rho}^{(2), \text{CLBM2}} = C_{D_y^2 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^2 \rho}^{(2), \text{CuLBM1}} = (-2 - 3c_s^2 \omega_5 - \omega_5 v_2^2 + \omega_5 + 6c_s^2 + 2v_2^2) \frac{v_2}{2\omega_5}$$

$$C_{D_y^2 \rho}^{(2), \text{CuLBM2}} = (2\omega_1 v_2^2 + 4v_2^2 \omega_2 + 3\omega_1 \omega_2 - 2\omega_1 - 3\omega_1 v_2^2 \omega_2 + 6c_s^2 \omega_1 - 4\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2) \frac{v_2}{6\omega_1 \omega_2}$$

coefficient $C_{D_y^2 v_2}^{(2)}$ **at** $\frac{\partial^2 v_2}{\partial x_2^2}$:

$$C_{D_y^2 v_2}^{(2), \text{SRT}} = (-2 - c_s^2 \omega - 3\omega v_2^2 + \omega + 2c_s^2 + 6v_2^2) \frac{\rho}{2\omega}$$

$$C_{D_y^2 v_2}^{(2), \text{MRT1}} = (-2 + \omega_{10} - \omega_{10} c_s^2 + 2c_s^2 + 6v_2^2 - 3\omega_{10} v_2^2) \frac{\rho}{2\omega_{10}}$$

$$C_{D_y^2 v_2}^{(2), \text{MRT2}} = C_{D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(2), \text{CLBM1}} = C_{D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(2), \text{CLBM2}} = C_{D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(2), \text{CuLBM1}} = (-2 - c_s^2 \omega_5 - 3\omega_5 v_2^2 + \omega_5 + 2c_s^2 + 6v_2^2) \frac{\rho}{2\omega_5}$$

$$C_{D_y^2 v_2}^{(2), \text{CuLBM2}} = (6\omega_1 v_2^2 + 12v_2^2 \omega_2 + 3\omega_1 \omega_2 - 2\omega_1 - 9\omega_1 v_2^2 \omega_2 + 2c_s^2 \omega_1 - 4\omega_2 + 4c_s^2 \omega_2 - 3c_s^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_y D_z \rho}^{(2)}$ **at** $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{MRT1}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{MRT2}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{v_3}{3\omega_1 \omega_2}$$

coefficient $C_{D_y D_z v_3}^{(2)}$ **at** $\frac{\partial^2 v_3}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z v_3}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y D_z v_3}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_y D_z v_3}^{(2), \text{MRT2}} = C_{D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(2), \text{CLBM1}} = C_{D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(2), \text{CLBM2}} = C_{D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_3}^{(2), \text{CuLBM2}} = (6\omega_1 v_3^2 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 6\omega_2 v_3^2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_z^2 v_2}^{(2)}$ **at** $\frac{\partial^2 v_2}{\partial x_3^2}$:

$$C_{D_z^2 v_2}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_z^2 v_2}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_z^2 v_2}^{(2), \text{MRT2}} = C_{D_z^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_z^2 v_2}^{(2), \text{CLBM1}} = C_{D_z^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_z^2 v_2}^{(2), \text{CLBM2}} = C_{D_z^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_z^2 v_2}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_z^2 v_2}^{(2), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_x^3 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^3}$:

$$C_{D_x^3 \rho}^{(2), \text{SRT}} = (-1 + v_1^2 + 3c_s^2) \frac{v_1 v_2}{12}$$

$$C_{D_x^3 \rho}^{(2), \text{MRT1}} = (v_1^2 \omega_5 \omega_9 \omega_{12} - 6\omega_5 \omega_9 + 6\omega_5 \omega_{12} + 6v_1^2 \omega_5 \omega_9 - 6v_1^2 \omega_5 \omega_{12} - \omega_5 \omega_9 \omega_{12} - 18c_s^2 \omega_5 \omega_{12} + 18c_s^2 \omega_5 \omega_9 - 36c_s^2 \omega_9 + 36c_s^2 \omega_{12} + 12v_1^2 \omega_{12} - 12v_1^2 \omega_9 + 3c_s^2 \omega_5 \omega_9 \omega_{12} + 12\omega_9 - 12\omega_{12}) \frac{v_1 v_2}{12\omega_5 \omega_9 \omega_{12}}$$

$$C_{D_x^3 \rho}^{(2), \text{MRT2}} = C_{D_x^3 \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(2), \text{CLBM1}} = C_{D_x^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(2), \text{CLBM2}} = C_{D_x^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(2), \text{CuLBM1}} = C_{D_x^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(2), \text{CuLBM2}} = C_{D_x^3 \rho}^{(2), \text{SRT}}$$

coefficient $C_{D_x^3 v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^3}$:

$$C_{D_x^3 v_1}^{(2), \text{SRT}} = (-1 + 3v_1^2 + c_s^2) \frac{\rho v_2}{12}$$

$$C_{D_x^3 v_1}^{(2), \text{MRT1}} = (3v_1^2 \omega_5 \omega_9 \omega_{12} - 6\omega_5 \omega_9 + 6\omega_5 \omega_{12} + 18v_1^2 \omega_5 \omega_9 - 18v_1^2 \omega_5 \omega_{12} - \omega_5 \omega_9 \omega_{12} - 6c_s^2 \omega_5 \omega_{12} + 6c_s^2 \omega_5 \omega_9 - 12c_s^2 \omega_9 + 12c_s^2 \omega_{12} + 36v_1^2 \omega_{12} - 36v_1^2 \omega_9 + c_s^2 \omega_5 \omega_9 \omega_{12} + 12\omega_9 - 12\omega_{12}) \frac{\rho v_2}{12\omega_5 \omega_9 \omega_{12}}$$

$$C_{D_x^3 v_1}^{(2), \text{MRT2}} = C_{D_x^3 v_1}^{(2), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(2), \text{CLBM1}} = C_{D_x^3 v_1}^{(2), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(2), \text{CLBM2}} = C_{D_x^3 v_1}^{(2), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(2), \text{CuLBM1}} = C_{D_x^3 v_1}^{(2), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(2), \text{CuLBM2}} = C_{D_x^3 v_1}^{(2), \text{SRT}}$$

coefficient $C_{D_x^3 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^3}$:

$$C_{D_x^3 v_2}^{(2), \text{SRT}} = (6 - 6v_1^2 + 18c_s^2 \omega + \omega^2 - \omega^2 v_1^2 - 3c_s^2 \omega^2 - 6\omega + 6\omega v_1^2 - 18c_s^2) \frac{\rho v_1}{6\omega^2}$$

$$C_{D_x^3 v_2}^{(2), \text{MRT1}} = (-3\omega_5^2 + 3v_1^2 \omega_5^2 - 6c_s^2 \omega_5 - 3\omega_5 \omega_{12} - 6v_1^2 \omega_5 + 3c_s^2 \omega_5^2 - 3c_s^2 \omega_5^2 \omega_{12} + 3v_1^2 \omega_5 \omega_{12} + 15c_s^2 \omega_5 \omega_{12} - v_1^2 \omega_5^2 \omega_{12} + 6\omega_5 - 12c_s^2 \omega_{12} + \omega_5^2 \omega_{12}) \frac{\rho v_1}{6\omega_5^2 \omega_{12}}$$

$$C_{D_x^3 v_2}^{(2), \text{MRT2}} = C_{D_x^3 v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^3 v_2}^{(2), \text{CLBM1}} = (6 - 6v_1^2 + 9c_s^2 \omega_5 + \omega_5 \omega_{12} + 3v_1^2 \omega_5 - v_1^2 \omega_5 \omega_{12} - 3c_s^2 \omega_5 \omega_{12} - 3\omega_5 + 9c_s^2 \omega_{12} - 18c_s^2 + 3v_1^2 \omega_{12} - 3\omega_{12}) \frac{\rho v_1}{6\omega_5 \omega_{12}}$$

$$C_{D_x^3 v_2}^{(2), \text{CLBM2}} = C_{D_x^3 v_2}^{(2), \text{CLBM1}}$$

$$C_{D_x^3 v_2}^{(2), \text{CuLBM1}} = (6 - 6v_1^2 - \omega_1 v_1^2 \omega_9 + \omega_1 \omega_9 - 3\omega_1 - 3c_s^2 \omega_1 \omega_9 + 9c_s^2 \omega_9 + 9c_s^2 \omega_1 - 18c_s^2 + 3v_1^2 \omega_9 + 3\omega_1 v_1^2 - 3\omega_9) \frac{\rho v_1}{6\omega_1 \omega_9}$$

$$C_{D_x^3 v_2}^{(2), \text{CuLBM2}} = (-2\omega_3 \omega_4 \omega_1 v_1^2 + 6\omega_3 - 18\omega_4 c_s^2 + 3\omega_3 \omega_1 v_1^2 - 3\omega_4 \omega_1 - 6\omega_3 \omega_4 c_s^2 \omega_1 - 6\omega_3 v_1^2 + 9\omega_3 c_s^2 \omega_1 + 6\omega_4 + 6\omega_3 \omega_4 v_1^2 - 3\omega_3 \omega_1 + 2\omega_3 \omega_4 \omega_1 - 6\omega_4 v_1^2 - 6\omega_3 \omega_4 + 3\omega_4 \omega_1 v_1^2 + 18\omega_3 \omega_4 c_s^2 - 18\omega_3 c_s^2 + 9\omega_4 c_s^2 \omega_1) \frac{\rho v_1}{12\omega_3 \omega_4 \omega_1}$$

$$\text{coefficient } C_{D_x^2 D_y \rho}^{(2)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y \rho}^{(2), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{MRT1}} = (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4}{6\omega_5^2}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{MRT2}} = C_{D_x^2 D_y \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CLBM1}} = C_{D_x^2 D_y \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CLBM2}} = C_{D_x^2 D_y \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CuLBM1}} = (-12 + 12\omega_1 - \omega_1^2) \frac{c_s^4}{6\omega_1^2}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CuLBM2}} = (-c_s^4 \omega_1^2 \omega_2^2 - 14c_s^4 \omega_2^2 - 3\omega_1^2 v_1^4 \omega_2 - 2\omega_1^2 v_1^2 + 6c_s^2 \omega_1 v_1^2 \omega_2 - 3\omega_1 v_1^2 \omega_2^2 + 2c_s^2 \omega_1^2 \omega_2 + 15c_s^2 \omega_1 v_1^2 \omega_2^2 - 18c_s^2 v_1^2 \omega_2^2 + 2c_s^4 \omega_1^2 - 2\omega_1 v_1^2 \omega_2 - 2c_s^2 \omega_1^2 \omega_2 - 4v_1^4 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 + 3\omega_1^2 v_1^2 \omega_2 + 12c_s^2 \omega_1^2 v_1^2 + 3\omega_1 v_1^4 \omega_2^2 + 2\omega_1 v_1^4 \omega_2 - 2c_s^2 \omega_1^2 + 2\omega_1^2 v_1^4 + 4v_1^2 \omega_2^2 - 15c_s^2 \omega_1^2 v_1^2 \omega_2 + 14c_s^4 \omega_1 \omega_2^2) \frac{1}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_y v_1}^{(2)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{MRT1}} = (-\omega_5^2 + \omega_5 \omega_{12} + 2\omega_5 - 2\omega_{12}) \frac{c_s^2 \rho v_1}{\omega_5^2 \omega_{12}}$$

$$C_{D_x^2 D_y v_1}^{(2), \text{MRT2}} = C_{D_x^2 D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CuLBM2}} = (8\omega_1^2 v_1^2 + 11\omega_1 v_1^2 \omega_2^2 - 5\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 + 6\omega_1 v_1^2 \omega_2 - 2\omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 10c_s^2 \omega_2^2 - 11\omega_1^2 v_1^2 \omega_2 + 8c_s^2 \omega_1^2 + 2c_s^2 \omega_1 \omega_2 - 14v_1^2 \omega_2^2 + 6\omega_2^2) \frac{\rho v_1}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_y v_2}^{(2)} \text{ at } \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_2}^{(2), \text{SRT}} = \frac{-c_s^2 \rho v_2}{6}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{MRT1}} = (-12\omega_{10} \omega_5^2 + 12\omega_5^2 + 12\omega_{10} \omega_5 \omega_{15} - 12\omega_5 \omega_{15} + 12\omega_{10} \omega_5 - 12\omega_{10} \omega_{15} - \omega_{10} \omega_5^2 \omega_{15}) \frac{c_s^2 \rho v_2}{6\omega_{10} \omega_5^2 \omega_{15}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{MRT2}} = C_{D_x^2 D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{CLBM1}} = C_{D_x^2 D_y v_2}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{CLBM2}} = C_{D_x^2 D_y v_2}^{(2), \text{SRT}}$$

$$C_{D_x D_y v_2}^{(2), \text{CuLBM1}} = C_{D_x D_y v_2}^{(2), \text{SRT}}$$

$$C_{D_x D_y v_2}^{(2), \text{CuLBM2}} = C_{D_x D_y v_2}^{(2), \text{SRT}}$$

$$\text{coefficient } C_{D_x D_y \rho}^{(2)} \text{ at } \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{MRT1}} = (-\omega_{10}^2 v_2^2 + \omega_{10} \omega_5 \omega_{15} - \omega_5 \omega_{15} - 3\omega_{10} c_s^2 \omega_5 + \omega_{10} v_2^2 \omega_{15} - \omega_{10} \omega_5 v_2^2 - 3\omega_{10}^2 c_s^2 + \omega_{10} \omega_5 + \omega_5 v_2^2 \omega_{15} - \omega_{10}^2 \omega_5 + 3\omega_{10} c_s^2 \omega_{15} - \omega_{10} \omega_5 v_2^2 \omega_{15} + 3c_s^2 \omega_5 \omega_{15} - 3\omega_{10} c_s^2 \omega_5 \omega_{15} - \omega_{10} \omega_{15} + \omega_{10}^2 + 3\omega_{10}^2 c_s^2 \omega_5 + \omega_{10}^2 \omega_5 v_2^2) \frac{v_1 v_2}{\omega_{10}^2 \omega_5 \omega_{15}}$$

$$C_{D_x D_y^2 \rho}^{(2), \text{MRT2}} = C_{D_x D_y^2 \rho}^{(2), \text{MRT1}}$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CuLBM2}} = (2\omega_1^2 v_1^2 + 2v_2^2 \omega_2^2 + 3\omega_1 v_1^2 \omega_2^2 - 3\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_1 v_1^2 \omega_2 + 2\omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 6c_s^2 \omega_2^2 - 3\omega_1^2 v_1^2 \omega_2 - 4\omega_1 v_2^2 \omega_2 + 12c_s^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 - 4v_1^2 \omega_2^2 + 2\omega_1^2 v_2^2 + 2\omega_2^2) \frac{v_1 v_2}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x D_y^2 v_1}^{(2)} \text{ at } \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_1}^{(2), \text{SRT}} = (12 + 36c_s^2 \omega + 3\omega^2 + 12\omega v_2^2 - 11c_s^2 \omega^2 - 12\omega - 3\omega^2 v_2^2 - 36c_s^2 - 12v_2^2) \frac{\rho v_2}{12\omega^2}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{MRT1}} = (6\omega_{10}^2 \omega_5 v_2^2 \omega_{15} + 12\omega_{10} \omega_5^2 + 12\omega_{10}^2 \omega_5^2 v_2^2 + 42\omega_{10}^2 c_s^2 \omega_5 \omega_{15} + 3\omega_{10}^2 \omega_5^2 \omega_{15} + 36c_s^2 \omega_5^2 \omega_{15} + 12\omega_5^2 v_2^2 \omega_{15} - 12\omega_{10} c_s^2 \omega_5^2 - 24\omega_{10}^2 c_s^2 \omega_{15} - 6\omega_{10} \omega_5^2 v_2^2 \omega_{15} - 18\omega_{10} c_s^2 \omega_5^2 \omega_{15} + 12\omega_{10}^2 \omega_5 + 12\omega_{10}^2 c_s^2 \omega_5^2 - 24\omega_{10} c_s^2 \omega_5 \omega_{15} - 11\omega_{10}^2 c_s^2 \omega_5^2 \omega_{15} - 3\omega_{10}^2 \omega_5^2 v_2^2 \omega_{15} - 12\omega_{10} \omega_5^2 v_2^2 - 6\omega_{10}^2 \omega_5 \omega_{15} - 12\omega_{10}^2 \omega_5^2 - 12\omega_{10}^2 c_s^2 \omega_5 + 6\omega_{10} \omega_5^2 \omega_{15} - 12\omega_{10}^2 \omega_5 v_2^2 - 12\omega_5^2 \omega_{15}) \frac{\rho v_2}{12\omega_{10}^2 \omega_5^2 \omega_{15}}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{MRT2}} = C_{D_x D_y^2 v_1}^{(2), \text{MRT1}}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CLBM1}} = (-3\omega_{10}^2 \omega_5 v_2^2 \omega_{15} - 12\omega_{10}^2 v_2^2 + 6\omega_{10} \omega_5 \omega_{15} - 12\omega_5 \omega_{15} - 36\omega_{10} c_s^2 \omega_5 - 11\omega_{10}^2 c_s^2 \omega_5 \omega_{15} - 6\omega_{10}^2 \omega_{15} - 12\omega_{10} \omega_5 v_2^2 + 18\omega_{10}^2 c_s^2 \omega_{15} - 36\omega_{10}^2 c_s^2 + 12\omega_{10} \omega_5 + 12\omega_5 v_2^2 \omega_{15} - 12\omega_{10}^2 \omega_5 - 6\omega_{10} \omega_5 v_2^2 \omega_{15} + 36c_s^2 \omega_5 \omega_{15} - 18\omega_{10} c_s^2 \omega_5 \omega_{15} + 3\omega_{10}^2 \omega_5 \omega_{15} + 12\omega_{10}^2 v_2^2 \omega_{15} + 36\omega_{10}^2 c_s^2 \omega_5 + 12\omega_{10}^2 \omega_5 v_2^2) \frac{\rho v_2}{12\omega_{10}^2 \omega_5 \omega_{15}}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CLBM2}} = C_{D_x D_y^2 v_1}^{(2), \text{CLBM1}}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CuLBM1}} = (36\omega_7 c_s^2 \omega_1 + 12\omega_5^2 + 12\omega_1 \omega_5^2 v_2^2 + 6\omega_7 \omega_1 \omega_5 - 36c_s^2 \omega_1 \omega_5 - 11\omega_7 c_s^2 \omega_1 \omega_5^2 - 18\omega_7 c_s^2 \omega_1 \omega_5 + 3\omega_7 \omega_1 \omega_5^2 - 6\omega_7 \omega_5^2 + 36c_s^2 \omega_1 \omega_5^2 - 36c_s^2 \omega_5^2 + 6\omega_7 \omega_5^2 v_2^2 - 3\omega_7 \omega_1 \omega_5^2 v_2^2 + 12\omega_1 \omega_5 - 6\omega_7 \omega_1 \omega_5 v_2^2 - 12\omega_7 \omega_1 + 12\omega_7 \omega_1 v_2^2 - 12\omega_5^2 v_2^2 - 12\omega_1 \omega_5^2 + 18\omega_7 c_s^2 \omega_5^2 - 12\omega_1 \omega_5 v_2^2) \frac{\rho v_2}{12\omega_7 \omega_1 \omega_5^2}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CuLBM2}} = (-36\omega_3 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1^2 v_2^2 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 - 24\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 2\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1^2 + 8\omega_4 \omega_1 \omega_2^2 - 18\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_2^2 + 12\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 8\omega_4 \omega_1 v_2^2 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 12\omega_3 \omega_1 v_2^2 \omega_2^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 + 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 6\omega_4 \omega_1^2 \omega_2^2 + 6\omega_4 \omega_1^2 v_2^2 \omega_2^2 + 6\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 11\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 + 12\omega_3 \omega_1 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 - 4\omega_4 \omega_1^2 v_2^2 \omega_2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 - 3\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2^2 + 18\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 + 8\omega_3 \omega_4 v_2^2 \omega_2^2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 12\omega_3 \omega_4 \omega_1^2 v_2^2) \frac{\rho v_2}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x D_y^2 v_2}^{(2)} \text{ at } \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{MRT1}} = (-3\omega_{10}^2 v_2^2 + \omega_{10} \omega_5 \omega_{15} - \omega_5 \omega_{15} - \omega_{10} c_s^2 \omega_5 + 3\omega_{10} v_2^2 \omega_{15} - 3\omega_{10} \omega_5 v_2^2 - \omega_{10}^2 c_s^2 + \omega_{10} \omega_5 + 3\omega_5 v_2^2 \omega_{15} - \omega_{10}^2 \omega_5 + \omega_{10} c_s^2 \omega_{15} - 3\omega_{10} \omega_5 v_2^2 \omega_{15} + c_s^2 \omega_5 \omega_{15} - \omega_{10} c_s^2 \omega_5 \omega_{15} - \omega_{10} \omega_{15} + \omega_{10}^2 + \omega_{10}^2 c_s^2 \omega_5 + 3\omega_{10}^2 \omega_5 v_2^2) \frac{\rho v_1}{\omega_{10}^2 \omega_5 \omega_{15}}$$

$$C_{D_x D_y^2 v_2}^{(2), \text{MRT}^2} = C_{D_x D_y^2 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CuLBM}^2} = (3\omega_3 c_s^2 \omega_1 \omega_2^2 - 12\omega_3 \omega_1 v_2^2 \omega_2 - 2\omega_3 v_1^2 \omega_2^2 - \omega_3 \omega_1^2 v_1^2 \omega_2 + 2\omega_1 v_1^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 - 2\omega_1 \omega_2^2 - 6c_s^2 \omega_1^2 \omega_2 + 6\omega_3 \omega_1^2 v_2^2 + \omega_3 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 - 4\omega_3 c_s^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1^2 v_1^2 \omega_2 + \omega_3 \omega_1 v_1^2 \omega_2^2 + 4\omega_3 \omega_1 \omega_2 + 6\omega_3 v_2^2 \omega_2^2 - \omega_3 \omega_1 \omega_2^2 + 2\omega_3 \omega_1^2 v_1^2 - 4\omega_3 \omega_1^2) \frac{\rho v_1}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^3 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x^3}$:

$$C_{D_y^3 \rho}^{(2), \text{SRT}} = (24c_s^2 \omega^2 v_2^2 + 12c_s^2 \omega + 36v_2^4 + 36\omega v_2^2 - c_s^2 \omega^2 + 12c_s^4 + 7\omega^2 v_2^4 - 36\omega v_2^4 - 7\omega^2 v_2^2 + 144c_s^2 v_2^2 - 12c_s^4 \omega - 12c_s^2 + c_s^4 \omega^2 - 36v_2^2 - 144c_s^2 \omega v_2^2) \frac{1}{12\omega^2}$$

$$C_{D_y^3 \rho}^{(2), \text{MRT}^1} = (-7\omega_{10}^2 v_2^2 + 36v_2^4 - 36\omega_{10} v_2^4 - \omega_{10}^2 c_s^2 - 12\omega_{10} c_s^4 + 12c_s^4 + 24\omega_{10}^2 c_s^2 v_2^2 + \omega_{10}^2 c_s^4 + 12\omega_{10} c_s^2 + 144c_s^2 v_2^2 - 144\omega_{10} c_s^2 v_2^2 - 12c_s^2 + 7\omega_{10}^2 v_2^4 - 36v_2^2 + 36\omega_{10} v_2^2) \frac{1}{12\omega_{10}^2}$$

$$C_{D_y^3 \rho}^{(2), \text{MRT}^2} = C_{D_y^3 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y^3 \rho}^{(2), \text{CLBM}^1} = C_{D_y^3 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y^3 \rho}^{(2), \text{CLBM}^2} = C_{D_y^3 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y^3 \rho}^{(2), \text{CuLBM}^1} = (7\omega_5^2 v_2^4 + 12c_s^2 \omega_5 + 36v_2^4 + 36\omega_5 v_2^2 - c_s^2 \omega_5^2 + 24c_s^2 \omega_5^2 v_2^2 + 12c_s^4 - 144c_s^2 \omega_5 v_2^2 - 12c_s^4 \omega_5 + 144c_s^2 v_2^2 - 12c_s^2 - 7\omega_5^2 v_2^2 - 36v_2^2 - 36\omega_5 v_2^4 + c_s^4 \omega_5^2) \frac{1}{12\omega_5^2}$$

$$C_{D_y^3 \rho}^{(2), \text{CuLBM}^2} = (c_s^4 \omega_1^2 \omega_2^2 + 8c_s^4 \omega_2^2 + 16\omega_1 v_2^4 \omega_2 - 16v_2^2 \omega_2^2 - 7\omega_1^2 v_2^2 \omega_2^2 - 48c_s^2 \omega_1^2 v_2^2 \omega_2 + 4c_s^2 \omega_1^2 \omega_2 + 4\omega_1^2 v_2^4 - c_s^2 \omega_1^2 \omega_2^2 + 24c_s^2 \omega_1^2 v_2^2 + 12\omega_1^2 v_2^2 \omega_2 + 4c_s^4 \omega_1^2 + 24c_s^2 \omega_1^2 v_2^2 \omega_2^2 - 4c_s^4 \omega_1^2 \omega_2 - 24\omega_1 v_2^4 \omega_2^2 + 8c_s^2 \omega_1 \omega_2^2 - 8c_s^2 \omega_2^2 + 72c_s^2 v_2^2 \omega_2^2 - 96c_s^2 \omega_1 v_2^2 \omega_2^2 - 16\omega_1 v_2^2 \omega_2 + 7\omega_1^2 v_2^4 \omega_2^2 + 16v_2^2 \omega_2^2 - 12\omega_1^2 v_2^4 \omega_2 - 4c_s^2 \omega_1^2 + 48c_s^2 \omega_1 v_2^2 \omega_2 + 24\omega_1 v_2^2 \omega_2^2 - 8c_s^4 \omega_1 \omega_2^2 - 4\omega_1^2 v_2^2) \frac{1}{12\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^3 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x^3}$:

$$C_{D_y^3 v_2}^{(2), \text{SRT}} = (-24 - 36c_s^2 \omega - 4\omega^2 - 60\omega v_2^2 + 5c_s^2 \omega^2 + 24\omega + 11\omega^2 v_2^2 + 36c_s^2 + 60v_2^2) \frac{\rho v_2}{6\omega^2}$$

$$C_{D_y^3 v_2}^{(2), \text{MRT}^1} = (-24 + 11\omega_{10}^2 v_2^2 + 24\omega_{10} + 5\omega_{10}^2 c_s^2 - 36\omega_{10} c_s^2 + 36c_s^2 - 4\omega_{10}^2 + 60v_2^2 - 60\omega_{10} v_2^2) \frac{\rho v_2}{6\omega_{10}^2}$$

$$C_{D_y^3 v_2}^{(2), \text{MRT}^2} = C_{D_y^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_y^3 v_2}^{(2), \text{CLBM}^1} = C_{D_y^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_y^3 v_2}^{(2), \text{CLBM}^2} = C_{D_y^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_y^3 v_2}^{(2), \text{CuLBM}^1} = (-24 - 4\omega_5^2 - 36c_s^2 \omega_5 - 60\omega_5 v_2^2 + 5c_s^2 \omega_5^2 + 24\omega_5 + 36c_s^2 + 11\omega_5^2 v_2^2 + 60v_2^2) \frac{\rho v_2}{6\omega_5^2}$$

$$C_{D_y^3 v_2}^{(2), \text{CuLBM}^2} = (28v_2^2 \omega_2^2 + 11\omega_1^2 v_2^2 \omega_2^2 + 16\omega_1 \omega_2^2 - 12c_s^2 \omega_1^2 \omega_2^2 + 5c_s^2 \omega_1^2 \omega_2^2 - 20\omega_1^2 v_2^2 \omega_2^2 - 8\omega_1 \omega_2 + 8\omega_1^2 \omega_2 - 4\omega_1^2 - 24c_s^2 \omega_1 \omega_2^2 + 20c_s^2 \omega_2^2 + 24\omega_1 v_2^2 \omega_2 + 8c_s^2 \omega_1^2 + 8c_s^2 \omega_1 \omega_2 - 40\omega_1 v_2^2 \omega_2^2 + 8\omega_1^2 v_2^2 - 12\omega_2^2 - 4\omega_1^2 \omega_2^2) \frac{\rho v_2}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_z v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{MRT}1} = (\omega_5^2 - \omega_7 \omega_8 + \omega_7 \omega_5 - \omega_7 \omega_5^2 + \omega_7 \omega_8 \omega_5 - \omega_8 \omega_5) \frac{c_s^2 \rho v_3}{\omega_7 \omega_8 \omega_5^2}$$

$$C_{D_x^2 D_z v_2}^{(2), \text{MRT}2} = C_{D_x^2 D_z v_2}^{(2), \text{MRT}1}$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CLBM}1} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CLBM}2} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CuLBM}1} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CuLBM}2} = (-2\omega_3 - 6\omega_4 c_s^2 - \omega_4 \omega_1 + \omega_4 \omega_1 v_3^2 - 2\omega_4 v_3^2 - 3\omega_3 c_s^2 \omega_1 + 2\omega_4 + \omega_3 \omega_1 + 2\omega_3 v_3^2 - \omega_3 \omega_1 v_3^2 + 6\omega_3 c_s^2 + 3\omega_4 c_s^2 \omega_1) \frac{\rho v_3}{4\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_x^2 D_z v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_3}^{(2), \text{SRT}} = \frac{-c_s^2 \rho v_2}{6}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{MRT}1} = (-6\omega_6 \omega_7 \omega_5 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_7 \omega_8 \omega_5 + 6\omega_6 \omega_5 + 6\omega_6 \omega_7 - 6\omega_8 \omega_5) \frac{c_s^2 \rho v_2}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{MRT}2} = C_{D_x^2 D_z v_3}^{(2), \text{MRT}1}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CLBM}1} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CLBM}2} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CuLBM}1} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CuLBM}2} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

coefficient $C_{D_x D_y D_z \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{MRT}1} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{MRT}2} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CLBM}1} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CLBM}2} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CuLBM}1} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CuLBM}2} = (\omega_1^2 v_1^2 - 2\omega_1 \omega_2 v_3^2 + \omega_2^2 v_3^2 - 2\omega_1 v_1^2 \omega_2 + 4\omega_1 \omega_2 - 2\omega_1^2 + 6c_s^2 \omega_2^2 + 6c_s^2 \omega_1^2 - 12c_s^2 \omega_1 \omega_2 + v_1^2 \omega_2^2 - 2\omega_2^2 + \omega_1^2 v_3^2) \frac{v_1 v_3}{3\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{MRT}1} = (\omega_5^2 - \omega_7 \omega_8 + \omega_7 \omega_5 - \omega_7 \omega_5^2 + \omega_7 \omega_8 \omega_5 - \omega_8 \omega_5) \frac{c_s^2 \rho v_3}{\omega_7 \omega_8 \omega_5^2}$$

$$C_{D_x D_y D_z v_1}^{(2), \text{MRT}2} = C_{D_x D_y D_z v_1}^{(2), \text{MRT}1}$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CLBM}1} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CLBM}2} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CuLBM2}} = (18\omega_3 c_s^2 \omega_1 \omega_2^2 + \omega_3 \omega_4 \omega_1 \omega_2^2 v_3^2 + 2\omega_3 \omega_4 \omega_1^2 v_3^2 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 v_1^2 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - \omega_3 \omega_4 \omega_1^2 \omega_2 v_3^2 - 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 8\omega_3 \omega_4 c_s^2 \omega_1^2 + 4\omega_4 \omega_1 \omega_2^2 - 4\omega_4 \omega_1 \omega_2^2 v_3^2 - 4\omega_3 \omega_4 c_s^2 \omega_2^2 + 6\omega_3 \omega_1 \omega_2^2 v_3^2 + 3\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 2\omega_4 \omega_1^2 \omega_2 v_3^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 + 3\omega_4 \omega_1^2 \omega_2^2 v_3^2 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - 3\omega_3 \omega_2^2 \omega_2^2 v_3^2 - 12\omega_3 \omega_4 \omega_1 v_1^2 \omega_2 - 3\omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 6\omega_3 \omega_1 \omega_2^2 - 2\omega_3 \omega_4 \omega_2^2 v_3^2 + 2\omega_4 \omega_1^2 \omega_2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_3}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{MRT1}} = (-\omega_7 \omega_8 + \omega_7 \omega_5 + \omega_7 \omega_8 \omega_5 - \omega_7^2 \omega_5 + \omega_7^2 - \omega_8 \omega_5) \frac{c_s^2 \rho v_1}{\omega_7^2 \omega_8 \omega_5}$$

$$C_{D_x D_y D_z v_3}^{(2), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CuLBM2}} = (18\omega_3 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 \omega_1^2 v_3^2 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 - 2\omega_4 \omega_1^2 v_1^2 \omega_2 - 2\omega_3 \omega_4 v_1^2 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 8\omega_3 \omega_4 c_s^2 \omega_1^2 + 4\omega_4 \omega_1 \omega_2^2 - \omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 - 4\omega_3 \omega_4 c_s^2 \omega_2^2 + 3\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 + 3\omega_4 \omega_1^2 v_1^2 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - 3\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - 3\omega_4 \omega_1^2 \omega_2^2 - 4\omega_4 \omega_1 v_1^2 \omega_2^2 + 6\omega_3 \omega_1 v_1^2 \omega_2^2 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 6\omega_3 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 \omega_2^2 v_3^2 + 2\omega_4 \omega_1^2 \omega_2 - 12\omega_3 \omega_4 \omega_1 \omega_2 v_3^2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 + \omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 2\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_1}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{MRT1}} = (-\omega_{10}^2 v_2^2 + \omega_{16} \omega_{10} v_2^2 + 3\omega_{16} \omega_7 c_s^2 + 3\omega_{10}^2 \omega_7 c_s^2 - \omega_{16} \omega_{10} \omega_7 v_2^2 - \omega_{16} \omega_7 - \omega_{10}^2 \omega_7 - 3\omega_{10}^2 c_s^2 - 3\omega_{16} \omega_{10} \omega_7 c_s^2 + \omega_{10}^2 \omega_7 v_2^2 + \omega_{16} \omega_{10} \omega_7 + 3\omega_{16} \omega_{10} c_s^2 + \omega_{16} \omega_7 v_2^2 - \omega_{16} \omega_{10} + \omega_{10} \omega_7 - \omega_{10} \omega_7 v_2^2 - 3\omega_{10} \omega_7 c_s^2 + \omega_{10}^2) \frac{v_2 v_3}{\omega_{16} \omega_{10}^2 \omega_7}$$

$$C_{D_y^2 D_z \rho}^{(2), \text{MRT2}} = C_{D_y^2 D_z \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CuLBM2}} = (2v_2^2 \omega_2^2 + 2\omega_1 \omega_2 v_3^2 - 3\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 - 4\omega_2^2 v_3^2 + 2\omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 6c_s^2 \omega_2^2 - 4\omega_1 v_2^2 \omega_2 + 12c_s^2 \omega_1^2 - 3\omega_1^2 \omega_2 v_3^2 - 6c_s^2 \omega_1 \omega_2 + 2\omega_1^2 v_2^2 + 2\omega_2^2 + 2\omega_1^2 v_3^2 + 3\omega_1 \omega_2^2 v_3^2) \frac{v_2 v_3}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{MRT1}} = (-3\omega_{10}^2 v_2^2 + 3\omega_{16} \omega_{10} v_2^2 + \omega_{16} \omega_7 c_s^2 + \omega_{10}^2 \omega_7 c_s^2 - 3\omega_{16} \omega_{10} \omega_7 v_2^2 - \omega_{16} \omega_7 - \omega_{10}^2 \omega_7 - \omega_{10}^2 c_s^2 - \omega_{16} \omega_{10} \omega_7 c_s^2 + 3\omega_{10}^2 \omega_7 v_2^2 + \omega_{16} \omega_{10} \omega_7 + \omega_{16} \omega_{10} c_s^2 + 3\omega_{16} \omega_7 v_2^2 - \omega_{16} \omega_{10} + \omega_{10} \omega_7 - 3\omega_{10} \omega_7 v_2^2 - \omega_{10} \omega_7 c_s^2 + \omega_{10}^2) \frac{\rho v_3}{\omega_{16} \omega_{10}^2 \omega_7}$$

$$C_{D_y^2 D_z v_2}^{(2), \text{MRT2}} = C_{D_y^2 D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CuLBM2}} = (3\omega_3 c_s^2 \omega_1 \omega_2^2 - 12\omega_3 \omega_1 v_2^2 \omega_2 + 8\omega_3 c_s^2 \omega_1^2 - 2\omega_1 \omega_2^2 + 2\omega_3 \omega_1^2 v_3^2 - 6c_s^2 \omega_1^2 \omega_2 + 6\omega_3 \omega_1^2 v_2^2 + \omega_3 \omega_1^2 \omega_2 + \omega_3 \omega_1 \omega_2^2 v_3^2 - \omega_3 \omega_1^2 \omega_2 v_3^2 - 4\omega_3 c_s^2 \omega_1 \omega_2 - 4\omega_3 c_s^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2 + 6\omega_3 v_2^2 \omega_2^2 - \omega_3 \omega_1 \omega_2^2 - 2\omega_1^2 \omega_2 v_3^2 - 2\omega_3 \omega_2^2 v_3^2 - 4\omega_3 \omega_1^2 + 2\omega_1 \omega_2^2 v_3^2) \frac{\rho v_3}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_3}^{(2), \text{SRT}} = (12 + 36c_s^2 \omega + 3\omega^2 + 12\omega v_2^2 - 11c_s^2 \omega^2 - 12\omega - 3\omega^2 v_2^2 - 36c_s^2 - 12v_2^2) \frac{\rho v_2}{12\omega^2}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{MRT1}} = (-12\omega_{10} \omega_7^2 c_s^2 - 3\omega_{16} \omega_{10}^2 \omega_7^2 v_2^2 + 6\omega_{16} \omega_{10} \omega_7^2 - 12\omega_{16} \omega_7^2 - 12\omega_{10}^2 \omega_7^2 - 12\omega_{10}^2 \omega_7 c_s^2 + 12\omega_{10}^2 \omega_7 - 11\omega_{16} \omega_{10}^2 \omega_7^2 c_s^2 - 12\omega_{10} \omega_7^2 v_2^2 - 24\omega_{16} \omega_{10} \omega_7 c_s^2 - 12\omega_{10}^2 \omega_7 v_2^2 - 18\omega_{16} \omega_{10} \omega_7^2 c_s^2 + 12\omega_{10}^2 \omega_7^2 v_2^2 + 12\omega_{16} \omega_7^2 v_2^2 - 24\omega_{16} \omega_{10}^2 c_s^2 - 6\omega_{16} \omega_{10}^2 \omega_7 + 42\omega_{16} \omega_{10}^2 \omega_7 c_s^2 + 12\omega_{10} \omega_7^2 + 36\omega_{16} \omega_7^2 c_s^2 + 12\omega_{10}^2 \omega_7^2 c_s^2 - 6\omega_{16} \omega_{10} \omega_7^2 v_2^2 + 6\omega_{16} \omega_{10}^2 \omega_7 v_2^2 + 3\omega_{16} \omega_{10}^2 \omega_7^2) \frac{\rho v_2}{12\omega_{16} \omega_{10}^2 \omega_7^2}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{MRT2}} = C_{D_y^2 D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CLBM1}} = (-6\omega_{16} \omega_{10}^2 - 12\omega_{10}^2 v_2^2 + 36\omega_{16} \omega_7 c_s^2 + 36\omega_{10}^2 \omega_7 c_s^2 - 6\omega_{16} \omega_{10} \omega_7 v_2^2 - 12\omega_{16} \omega_7 - 12\omega_{10}^2 \omega_7 - 36\omega_{10}^2 c_s^2 - 18\omega_{16} \omega_{10} \omega_7 c_s^2 + 12\omega_{10}^2 \omega_7 v_2^2 + 6\omega_{16} \omega_{10} \omega_7 + 12\omega_{16} \omega_7 v_2^2 + 18\omega_{16} \omega_{10}^2 c_s^2 + 3\omega_{16} \omega_{10}^2 \omega_7 + 12\omega_{10} \omega_7 - 11\omega_{16} \omega_{10}^2 \omega_7 c_s^2 - 12\omega_{10} \omega_7 v_2^2 + 6\omega_{16} \omega_{10}^2 v_2^2 - 36\omega_{10} \omega_7 c_s^2 + 12\omega_{10}^2 - 3\omega_{16} \omega_{10}^2 \omega_7 v_2^2) \frac{\rho v_2}{12\omega_{16} \omega_{10}^2 \omega_7}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CLBM2}} = C_{D_y^2 D_z v_3}^{(2), \text{CLBM1}}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CuLBM1}} = (12\omega_3 \omega_5^2 v_2^2 + 12\omega_5^2 - 6\omega_3 \omega_{11} \omega_5 v_2^2 + 12\omega_3 \omega_5 - 18\omega_3 c_s^2 \omega_{11} \omega_5 - 6\omega_{11} \omega_5^2 + 6\omega_{11} \omega_5^2 v_2^2 - 12\omega_3 \omega_{11} - 11\omega_3 c_s^2 \omega_{11} \omega_5^2 - 36c_s^2 \omega_5^2 - 12\omega_3 \omega_5^2 + 12\omega_3 \omega_{11} v_2^2 + 36\omega_3 c_s^2 \omega_5^2 + 3\omega_3 \omega_{11} \omega_5^2 + 36\omega_3 c_s^2 \omega_{11} - 12\omega_5^2 v_2^2 + 6\omega_3 \omega_{11} \omega_5 - 12\omega_3 \omega_5 v_2^2 - 3\omega_3 \omega_{11} \omega_5^2 v_2^2 + 18c_s^2 \omega_{11} \omega_5^2 - 36\omega_3 c_s^2 \omega_5) \frac{\rho v_2}{12\omega_3 \omega_{11} \omega_5^2}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CuLBM2}} = (-36\omega_3 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 18\omega_3 \omega_4 \omega_1 \omega_2^2 v_3^2 + 12\omega_3 \omega_4 \omega_1^2 v_3^2 + 4\omega_3 \omega_4 \omega_1^2 v_2^2 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 + 2\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 - 18\omega_3 \omega_4 \omega_1^2 \omega_2 v_3^2 + 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1^2 + 8\omega_4 \omega_1 \omega_2^2 + 16\omega_3 \omega_4 c_s^2 \omega_2^2 + 12\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 8\omega_4 \omega_1 v_2^2 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 12\omega_3 \omega_1 v_2^2 \omega_2^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 - 6\omega_4 \omega_1^2 \omega_2^2 + 6\omega_4 \omega_1^2 v_2^2 \omega_2^2 + 6\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 11\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 + 12\omega_3 \omega_1 \omega_2^2 - 24\omega_3 \omega_4 \omega_1^2 v_3^2 + 4\omega_4 \omega_1^2 \omega_2 - 4\omega_4 \omega_1^2 v_2^2 \omega_2 + 12\omega_3 \omega_4 \omega_1 \omega_2 v_3^2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 - 3\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2^2 + 8\omega_3 \omega_4 v_2^2 \omega_2^2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2) \frac{\rho v_2}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_1}^{(2), \text{SRT}} = \frac{-c_s^2 \rho v_2}{6}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{MRT1}} = (-6\omega_6 \omega_7 \omega_5 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_7 \omega_8 \omega_5 + 6\omega_6 \omega_5 + 6\omega_6 \omega_7 - 6\omega_8 \omega_5) \frac{c_s^2 \rho v_2}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{MRT2}} = C_{D_x D_z^2 v_1}^{(2), \text{MRT1}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CLBM1}} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CLBM2}} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CuLBM1}} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CuLBM2}} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

coefficient $C_{D_x D_z^2 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{MRT1}} = (-\omega_7 \omega_8 + \omega_7 \omega_5 + \omega_7 \omega_8 \omega_5 - \omega_7^2 \omega_5 + \omega_7^2 - \omega_8 \omega_5) \frac{c_s^2 \rho v_1}{\omega_7^2 \omega_8 \omega_5}$$

$$C_{D_x D_z^2 v_2}^{(2), \text{MRT}^2} = C_{D_x D_z^2 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CuLBM}^2} = (-2\omega_3 - 6\omega_4 c_s^2 - \omega_3 \omega_1 v_1^2 - \omega_4 \omega_1 + 2\omega_3 v_1^2 - 3\omega_3 c_s^2 \omega_1 + 2\omega_4 + \omega_3 \omega_1 - 2\omega_4 v_1^2 + \omega_4 \omega_1 v_1^2 + 6\omega_3 c_s^2 + 3\omega_4 c_s^2 \omega_1) \frac{\rho v_1}{4\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_y D_z^2 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 \rho}^{(2), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1} = (-12 + 12\omega_7 - \omega_7^2) \frac{c_s^4}{6\omega_7^2}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{MRT}^2} = C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CLBM}^1} = C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CLBM}^2} = C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CuLBM}^1} = (-12 + 12\omega_3 - \omega_3^2) \frac{c_s^4}{6\omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CuLBM}^2} = (-3\omega_1^2 \omega_2 v_3^4 - c_s^4 \omega_1^2 \omega_2^2 - 14c_s^4 \omega_2^2 - 2\omega_1 \omega_2 v_3^2 + 2\omega_1^2 v_3^4 + 3\omega_1 \omega_2^2 v_3^4 + 2c_s^2 \omega_1^2 \omega_2 + 4\omega_2^2 v_3^2 + 12c_s^2 \omega_1^2 v_3^2 + 2c_s^4 \omega_1^2 + 6c_s^2 \omega_1 \omega_2 v_3^2 - 2c_s^4 \omega_1^2 \omega_2 - 18c_s^2 \omega_2^2 v_3^2 + 15c_s^2 \omega_1 \omega_2^2 v_3^2 - 15c_s^2 \omega_1^2 \omega_2 v_3^2 - 2c_s^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 - 2c_s^2 \omega_1^2 + 2\omega_1 \omega_2 v_3^4 + 3\omega_1^2 \omega_2 v_3^2 + 14c_s^4 \omega_1 \omega_2^2 - 4\omega_2^2 v_3^4 - 2\omega_1^2 v_3^2 - 3\omega_1 \omega_2^2 v_3^2) \frac{1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_2}^{(2), \text{SRT}} = \frac{-c_s^2 \rho v_2}{6}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{MRT}^1} = (-\omega_{16} \omega_{10} \omega_7^2 - 12\omega_{16} \omega_7 + 12\omega_{16} \omega_{10} \omega_7 - 12\omega_{16} \omega_{10} + 12\omega_{10} \omega_7 - 12\omega_{10} \omega_7^2 + 12\omega_7^2) \frac{c_s^2 \rho v_2}{6\omega_{16} \omega_{10} \omega_7^2}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{MRT}^2} = C_{D_y D_z^2 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CLBM}^1} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CLBM}^2} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CuLBM}^1} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CuLBM}^2} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

coefficient $C_{D_y D_z^2 v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{MRT}^1} = (\omega_{19} \omega_7 - 2\omega_{19} + 2\omega_7 - \omega_7^2) \frac{c_s^2 \rho v_3}{\omega_{19} \omega_7^2}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{MRT}^2} = C_{D_y D_z^2 v_3}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CuLBM2}} = (6\omega_1\omega_2v_3^2 - 5\omega_1\omega_2^2 - 9c_s^2\omega_1^2\omega_2 - 14\omega_2^2v_3^2 - 2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 4\omega_1^2 + 9c_s^2\omega_1\omega_2^2 - 10c_s^2\omega_2^2 + 8c_s^2\omega_1^2 - 11\omega_1^2\omega_2v_3^2 + 2c_s^2\omega_1\omega_2 + 6\omega_2^2 + 8\omega_1^2v_3^2 + 11\omega_1\omega_2^2v_3^2) \frac{\rho v_3}{6\omega_1^2\omega_2^2}$$

coefficient $C_{D_z^3 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{D_z^3 \rho}^{(2), \text{SRT}} = (-1 + 3c_s^2 + v_3^2) \frac{v_2 v_3}{12}$$

$$C_{D_z^3 \rho}^{(2), \text{MRT1}} = (6\omega_7\omega_{11}v_3^2 + 6\omega_{19}\omega_7 - 12\omega_{19} + 36\omega_{19}c_s^2 - \omega_{19}\omega_7\omega_{11} + \omega_{19}\omega_7\omega_{11}v_3^2 + 12\omega_{19}v_3^2 - 6\omega_7\omega_{11} - 36c_s^2\omega_{11} - 6\omega_{19}\omega_7v_3^2 + 3\omega_{19}\omega_7c_s^2\omega_{11} + 12\omega_{11} - 12\omega_{11}v_3^2 - 18\omega_{19}\omega_7c_s^2 + 18\omega_7c_s^2\omega_{11}) \frac{v_2 v_3}{12\omega_{19}\omega_7\omega_{11}}$$

$$C_{D_z^3 \rho}^{(2), \text{MRT2}} = C_{D_z^3 \rho}^{(2), \text{MRT1}}$$

$$C_{D_z^3 \rho}^{(2), \text{CLBM1}} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(2), \text{CLBM2}} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(2), \text{CuLBM1}} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(2), \text{CuLBM2}} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

coefficient $C_{D_z^3 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_3^3}$:

$$C_{D_z^3 v_2}^{(2), \text{SRT}} = (6 + 18c_s^2\omega + \omega^2 + 6\omega v_3^2 - 3c_s^2\omega^2 - 6\omega - \omega^2v_3^2 - 18c_s^2 - 6v_3^2) \frac{\rho v_3}{6\omega^2}$$

$$C_{D_z^3 v_2}^{(2), \text{MRT1}} = (3\omega_7^2c_s^2 - 3\omega_{19}\omega_7 - 12\omega_{19}c_s^2 - 3\omega_{19}\omega_7^2c_s^2 + 3\omega_7^2v_3^2 + 6\omega_7 + \omega_{19}\omega_7^2 - \omega_{19}\omega_7^2v_3^2 + 3\omega_{19}\omega_7v_3^2 - 6\omega_7v_3^2 + 15\omega_{19}\omega_7c_s^2 - 3\omega_7^2 - 6\omega_7c_s^2) \frac{\rho v_3}{6\omega_{19}\omega_7^2}$$

$$C_{D_z^3 v_2}^{(2), \text{MRT2}} = C_{D_z^3 v_2}^{(2), \text{MRT1}}$$

$$C_{D_z^3 v_2}^{(2), \text{CLBM1}} = (6 + \omega_{19}\omega_7 - 3\omega_{19} + 9\omega_{19}c_s^2 - 3\omega_7 + 3\omega_{19}v_3^2 - \omega_{19}\omega_7v_3^2 + 3\omega_7v_3^2 - 18c_s^2 - 3\omega_{19}\omega_7c_s^2 + 9\omega_7c_s^2 - 6v_3^2) \frac{\rho v_3}{6\omega_{19}\omega_7}$$

$$C_{D_z^3 v_2}^{(2), \text{CLBM2}} = C_{D_z^3 v_2}^{(2), \text{CLBM1}}$$

$$C_{D_z^3 v_2}^{(2), \text{CuLBM1}} = (6 - 3\omega_3 - \omega_3\omega_{10}v_3^2 - 3\omega_{10} - 3\omega_3\omega_{10}c_s^2 + 3\omega_3v_3^2 + 9\omega_{10}c_s^2 - 18c_s^2 + 9\omega_3c_s^2 + \omega_3\omega_{10} + 3\omega_{10}v_3^2 - 6v_3^2) \frac{\rho v_3}{6\omega_3\omega_{10}}$$

$$C_{D_z^3 v_2}^{(2), \text{CuLBM2}} = (6\omega_3 - 18\omega_4c_s^2 - 3\omega_4\omega_1 - 6\omega_3\omega_4c_s^2\omega_1 + 3\omega_4\omega_1v_3^2 - 6\omega_4v_3^2 + 9\omega_3c_s^2\omega_1 + 6\omega_4 - 3\omega_3\omega_1 + 6\omega_3\omega_4v_3^2 + 2\omega_3\omega_4\omega_1 - 6\omega_3v_3^2 - 6\omega_3\omega_4 + 3\omega_3\omega_1v_3^2 + 18\omega_3\omega_4c_s^2 - 18\omega_3c_s^2 - 2\omega_3\omega_4\omega_1v_3^2 + 9\omega_4c_s^2\omega_1) \frac{\rho v_3}{12\omega_3\omega_4\omega_1}$$

coefficient $C_{D_z^3 v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_3^3}$:

$$C_{D_z^3 v_3}^{(2), \text{SRT}} = (-1 + c_s^2 + 3v_3^2) \frac{\rho v_2}{12}$$

$$C_{D_z^3 v_3}^{(2), \text{MRT1}} = (18\omega_7\omega_{11}v_3^2 + 6\omega_{19}\omega_7 - 12\omega_{19} + 12\omega_{19}c_s^2 - \omega_{19}\omega_7\omega_{11} + 3\omega_{19}\omega_7\omega_{11}v_3^2 + 36\omega_{19}v_3^2 - 6\omega_7\omega_{11} - 12c_s^2\omega_{11} - 18\omega_{19}\omega_7v_3^2 + \omega_{19}\omega_7c_s^2\omega_{11} + 12\omega_{11} - 36\omega_{11}v_3^2 - 6\omega_{19}\omega_7c_s^2 + 6\omega_7c_s^2\omega_{11}) \frac{\rho v_2}{12\omega_{19}\omega_7\omega_{11}}$$

$$C_{D_z^3 v_3}^{(2), \text{MRT2}} = C_{D_z^3 v_3}^{(2), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(2), \text{CLBM1}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(2), \text{CLBM2}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(2), \text{CuLBM1}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(2), \text{CuLBM2}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$\text{coefficient } C_{D_x^4 \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x^4} :$$

$$C_{D_x^4 \rho}^{(2), \text{SRT}} = (-6v_1^2 + c_s^2 \omega - 12c_s^2 \omega v_1^2 + 24c_s^2 v_1^2 + 2c_s^4 - 3\omega v_1^4 + 3\omega v_1^2 - c_s^4 \omega - 2c_s^2 + 6v_1^4) \frac{v_2}{24\omega}$$

$$C_{D_x^4 \rho}^{(2), \text{MRT1}} = (48v_1^2 \omega_5 \omega_9 \omega_{12} - 72v_1^2 \omega_5 \omega_{12}^2 - 12c_s^2 \omega_5^2 \omega_9^2 - 48c_s^4 \omega_5 \omega_9 \omega_{12}^2 + 432c_s^2 v_1^2 \omega_5 \omega_9^2 \omega_{12} - 48c_s^2 \omega_5 \omega_9^2 \omega_{12} - 48v_1^2 \omega_9 \omega_{12}^2 + 24v_1^2 \omega_5 \omega_9^2 + 12c_s^2 \omega_5^2 \omega_{12}^2 - c_s^4 \omega_5^2 \omega_9^2 \omega_{12}^2 + 72c_s^2 v_1^2 \omega_5^2 \omega_9 \omega_{12} + 30v_1^2 \omega_5^2 \omega_9^2 \omega_{12} + 36v_1^4 \omega_5^2 \omega_9 \omega_{12}^2 - 24c_s^4 \omega_9^2 \omega_{12} + 72v_1^4 \omega_5 \omega_{12}^2 + 12c_s^4 \omega_5^2 \omega_9^2 + 24v_1^4 \omega_5^2 \omega_9 \omega_{12} - 14c_s^2 \omega_5^2 \omega_9 \omega_{12}^2 + 48v_1^4 \omega_9 \omega_{12}^2 - 12c_s^4 \omega_5^2 \omega_9^2 \omega_{12} + 150c_s^2 v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 + 3v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 24v_1^4 \omega_5 \omega_9^2 - 12c_s^4 \omega_5^2 \omega_{12}^2 + 216c_s^2 v_1^2 \omega_9 \omega_{12}^2 - 144c_s^2 v_1^2 \omega_5 \omega_9^2 + 96v_1^4 \omega_5 \omega_9^2 \omega_{12} + 288c_s^2 v_1^2 \omega_5 \omega_{12}^2 + 96v_1^2 \omega_5 \omega_9 \omega_{12}^2 + 24c_s^2 \omega_9^2 \omega_{12} + 48c_s^2 \omega_5 \omega_9 \omega_{12}^2 + 48v_1^2 \omega_9^2 \omega_{12} - 48v_1^4 \omega_5 \omega_9 \omega_{12} + 72c_s^2 v_1^2 \omega_5^2 \omega_9^2 - 144c_s^2 v_1^2 \omega_5^2 \omega_{12}^2 - 432c_s^2 v_1^2 \omega_5 \omega_9 \omega_{12}^2 + 48c_s^4 \omega_5 \omega_9^2 \omega_{12} - 30v_1^4 \omega_5^2 \omega_9^2 \omega_{12} - 24c_s^4 \omega_5 \omega_9^2 - 36v_1^4 \omega_5^2 \omega_{12}^2 + c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 24c_s^4 \omega_9 \omega_{12}^2 - 12c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 24c_s^4 \omega_5 \omega_{12}^2 + 12v_1^4 \omega_5^2 \omega_9^2 - 36v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 - 126c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 48v_1^4 \omega_9^2 \omega_{12} + 14c_s^4 \omega_5^2 \omega_9 \omega_{12}^2 - 24v_1^2 \omega_5^2 \omega_9 \omega_{12} - 3v_1^4 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 24c_s^2 \omega_5 \omega_9^2 + 36v_1^2 \omega_5^2 \omega_{12}^2 - 96v_1^2 \omega_5 \omega_9^2 \omega_{12} - 144c_s^2 v_1^2 \omega_5 \omega_9 \omega_{12} - 24c_s^2 \omega_9 \omega_{12}^2 - 216c_s^2 v_1^2 \omega_9^2 \omega_{12} - 96v_1^4 \omega_5 \omega_9 \omega_{12}^2 - 24c_s^2 \omega_5 \omega_{12}^2 - 12v_1^2 \omega_5^2 \omega_9^2) \frac{v_2}{24\omega_5^2 \omega_9^2 \omega_{12}^2}$$

$$C_{D_x^4 \rho}^{(2), \text{MRT2}} = C_{D_x^4 \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(2), \text{CLBM1}} = (-6v_1^2 - c_s^4 \omega_9 + 24c_s^2 v_1^2 - 12c_s^2 v_1^2 \omega_9 + 2c_s^4 - 3v_1^4 \omega_9 + c_s^2 \omega_9 - 2c_s^2 + 6v_1^4 + 3v_1^2 \omega_9) \frac{v_2}{24\omega_9}$$

$$C_{D_x^4 \rho}^{(2), \text{CLBM2}} = C_{D_x^4 \rho}^{(2), \text{CLBM1}}$$

$$C_{D_x^4 \rho}^{(2), \text{CuLBM1}} = (-6v_1^2 - 12\omega_4 c_s^2 v_1^2 + \omega_4 c_s^2 + 24c_s^2 v_1^2 + 2c_s^4 - 3\omega_4 v_1^4 + 3\omega_4 v_1^2 - 2c_s^2 - \omega_4 c_s^4 + 6v_1^4) \frac{v_2}{24\omega_4}$$

$$C_{D_x^4 \rho}^{(2), \text{CuLBM2}} = (12v_1^4 \omega_2 + 48c_s^2 v_1^2 \omega_2 - 36c_s^2 \omega_1 v_1^2 \omega_2 + 2c_s^4 \omega_1 + 6\omega_1 v_1^4 + 24c_s^2 \omega_1 v_1^2 + 9\omega_1 v_1^2 \omega_2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 - 12v_1^2 \omega_2 - 2c_s^2 \omega_1 - 9\omega_1 v_1^4 \omega_2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 6\omega_1 v_1^2) \frac{v_2}{72\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^4 v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x^4} :$$

$$C_{D_x^4 v_1}^{(2), \text{SRT}} = (-4 + 10v_1^2 - 3c_s^2 \omega + 2\omega - 5\omega v_1^2 + 6c_s^2) \frac{\rho v_1 v_2}{12\omega}$$

$$C_{D_x^4 v_1}^{(2), \text{MRT1}} = (-72v_1^2 \omega_5 \omega_9 \omega_{12} + 120v_1^2 \omega_5 \omega_{12}^2 + 24c_s^2 \omega_5^2 \omega_9^2 + 120c_s^2 \omega_5 \omega_9^2 \omega_{12} + 84v_1^2 \omega_9 \omega_{12}^2 - 48v_1^2 \omega_5 \omega_9^2 - 36c_s^2 \omega_5^2 \omega_{12}^2 - 51v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 25\omega_5^2 \omega_9 \omega_{12}^2 + 12c_s^2 \omega_5^2 \omega_9 \omega_{12}^2 - 48\omega_5 \omega_{12}^2 - 12\omega_5^2 \omega_9 \omega_{12} + 39c_s^2 \omega_5^2 \omega_9 \omega_{12}^2 - 36\omega_9 \omega_{12}^2 - 5v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 24\omega_5 \omega_9^2 - 72\omega_5 \omega_9^2 \omega_{12} - 168v_1^2 \omega_5 \omega_9 \omega_{12}^2 - 60c_s^2 \omega_9^2 \omega_{12} - 120c_s^2 \omega_5 \omega_9 \omega_{12}^2 - 84v_1^2 \omega_9^2 \omega_{12} + 24\omega_5 \omega_9 \omega_{12} + 24\omega_5^2 \omega_{12}^2 - 3c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 21\omega_5^2 \omega_9^2 \omega_{12} + 61v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 - 12\omega_5^2 \omega_9^2 + 36\omega_9^2 \omega_{12} + 36v_1^2 \omega_5^2 \omega_9 \omega_{12} - 33c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 2\omega_5^2 \omega_9^2 \omega_{12}^2 - 48c_s^2 \omega_5 \omega_9^2 - 60v_1^2 \omega_5^2 \omega_{12}^2 + 168v_1^2 \omega_5 \omega_9^2 \omega_{12} + 60c_s^2 \omega_9 \omega_{12}^2 - 24c_s^2 \omega_5 \omega_9 \omega_{12} + 72\omega_5 \omega_9 \omega_{12}^2 + 72c_s^2 \omega_5 \omega_{12}^2 + 24v_1^2 \omega_5^2 \omega_9^2) \frac{\rho v_1 v_2}{12\omega_5^2 \omega_9^2 \omega_{12}^2}$$

$$C_{D_x^4 v_1}^{(2), \text{MRT2}} = C_{D_x^4 v_1}^{(2), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(2), \text{CLBM1}} = (-4 + 10v_1^2 - 3c_s^2 \omega_9 + 6c_s^2 - 5v_1^2 \omega_9 + 2\omega_9) \frac{\rho v_1 v_2}{12\omega_9}$$

$$C_{D_x^4 v_1}^{(2), \text{CLBM2}} = C_{D_x^4 v_1}^{(2), \text{CLBM1}}$$

$$C_{D_x^4 v_1}^{(2), \text{CuLBM1}} = (-4 + 10v_1^2 - 3\omega_4 c_s^2 + 2\omega_4 - 5\omega_4 v_1^2 + 6c_s^2) \frac{\rho v_1 v_2}{12\omega_4}$$

$$C_{D_x^4 v_1}^{(2), \text{CuLBM2}} = (-15\omega_1 v_1^2 \omega_2 + 6\omega_1 \omega_2 - 4\omega_1 + 20v_1^2 \omega_2 + 6c_s^2 \omega_1 - 8\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 + 10\omega_1 v_1^2) \frac{\rho v_1 v_2}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^4 v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x^4} :$$

$$C_{D_x^4 v_2}^{(2), \text{SRT}} = (72v_1^2 - 3\omega^3 v_1^2 + 36c_s^2 \omega + 216c_s^2 \omega v_1^2 + c_s^2 \omega^3 + 42\omega^2 v_1^2 - 144c_s^2 v_1^2 - 14c_s^2 \omega^2 + 48c_s^4 + 108\omega v_1^4 - 42\omega^2 v_1^4 + 6c_s^2 \omega^3 v_1^2 - 108\omega v_1^2 - 72c_s^4 \omega - 24c_s^2 + 3\omega^3 v_1^4 + 30c_s^4 \omega^2 - 72v_1^4 - 3c_s^4 \omega^3 - 84c_s^2 \omega^2 v_1^2) \frac{\rho}{24\omega^3}$$

$$C_{D_x^4 v_2}^{(2), \text{MRT1}} = (-24c_s^2 v_1^2 \omega_5 \omega_{12} - 3c_s^4 \omega_5^3 \omega_{12}^2 - 24v_1^2 \omega_5 \omega_{12}^2 - 96c_s^2 v_1^2 \omega_{12}^2 - 12v_1^2 \omega_5^3 - 8c_s^2 \omega_5^2 \omega_{12}^2 + 24v_1^2 \omega_5^2 - 24c_s^4 \omega_5^2 \omega_{12} - 48v_1^4 \omega_5 \omega_{12} - 6c_s^2 \omega_5^3 \omega_{12} + 24v_1^4 \omega_5 \omega_{12}^2 + c_s^2 \omega_5^3 \omega_{12}^2 + 24c_s^4 \omega_5^2 \omega_{12}^2 + 24c_s^4 \omega_{12}^2 + 24c_s^2 \omega_5^2 \omega_{12} + 156c_s^2 v_1^2 \omega_5 \omega_{12}^2 + 6c_s^4 \omega_5^3 \omega_{12} + 48v_1^2 \omega_5 \omega_{12} - 24v_1^4 \omega_5^2 - 18v_1^4 \omega_5^3 \omega_{12} - 24c_s^2 \omega_5 \omega_{12} - 72v_1^2 \omega_5^2 \omega_{12} - 72c_s^2 v_1^2 \omega_5^2 \omega_{12}^2 - 24c_s^2 v_1^2 \omega_5^2 - 24v_1^4 \omega_5^2 \omega_{12}^2 + 12v_1^4 \omega_5^3 + 12c_s^2 v_1^2 \omega_5^3 - 48c_s^4 \omega_5 \omega_{12}^2 - 3v_1^2 \omega_5^3 \omega_{12}^2 - 12c_s^2 v_1^2 \omega_5^3 \omega_{12} + 24c_s^4 \omega_5 \omega_{12} + 18v_1^2 \omega_5^3 \omega_{12} + 6c_s^2 v_1^2 \omega_5^3 \omega_{12}^2 + 72v_1^4 \omega_5^2 \omega_{12} + 24v_1^2 \omega_5^2 \omega_{12}^2 + 48c_s^2 v_1^2 \omega_5^2 \omega_{12} + 3v_1^4 \omega_5^3 \omega_{12}^2 + 12c_s^2 \omega_5 \omega_{12}^2) \frac{\rho}{24\omega_5^3 \omega_{12}^2}$$

[illegible]

$$45\omega_{10}v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 24\omega_{10}c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 6\omega_{10}c_s^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_{12} - 18v_1^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 36\omega_{10}v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9^2 + 36v_1^2\omega_5^3v_2^2\omega_{12}^2 - 36\omega_{10}c_s^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} + 6\omega_{10}c_s^4\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 24\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12\omega_{10}\omega_5^3v_2^2\omega_9^2\omega_{12} - 24\omega_{10}\omega_5v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12\omega_{10}c_s^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 6c_s^2\omega_5^3v_2^2\omega_{15}\omega_9^2\omega_{12} + 24c_s^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 6c_s^4\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 48\omega_{10}c_s^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 54\omega_{10}c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 18\omega_{10}v_1^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12}^2 - 12\omega_{10}c_s^2\omega_5^2v_2^2\omega_{15}\omega_9^2\omega_{12} - 108\omega_{10}v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 12\omega_{10}\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 72v_1^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 6\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 12\omega_{10}\omega_5^2v_2^2\omega_{15}\omega_9^2\omega_{12} + 18\omega_{10}c_s^4\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2) \frac{\rho}{12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2}$$

$$C_{D_x^3 D_y v_1}^{(2), \text{MRT}^2} = C_{D_x^3 D_y v_1}^{(2), \text{MRT}^1}$$

$$C_{D_x^3 D_y v_1}^{(2), \text{CLBM}^1} = (12\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_{12} + 12\omega_{10}c_s^2\omega_5^2\omega_9\omega_{12} - 12\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9 - 36\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{12} + 12\omega_5^3\omega_{21}\omega_{12} + 18\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} - 12\omega_{10}\omega_5^3\omega_{15}\omega_9 + 6c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 12\omega_{10}c_s^2\omega_5^2\omega_{15}\omega_9\omega_{12} - 18\omega_{10}v_1^2\omega_5^3\omega_{15}\omega_9 - 18\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 6c_s^2\omega_5^3\omega_{15}\omega_9\omega_{12} - 12\omega_{10}\omega_5^3\omega_{21}\omega_{12} + 36\omega_{10}v_1^2\omega_5\omega_{21}\omega_{15}\omega_9 - 36\omega_{10}v_1^2\omega_5^3\omega_9\omega_{12} - 5\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 12c_s^2\omega_5^3\omega_{21}\omega_{12} - 12\omega_{10}\omega_5^2\omega_9\omega_{12} + 6\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 36\omega_{10}v_1^2\omega_5\omega_{21}\omega_{15}\omega_{12} + 6\omega_{10}c_s^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 12\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{12} - 3\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12\omega_{10}c_s^2\omega_5^3\omega_{15}\omega_9 + 36v_1^2\omega_5^2\omega_9\omega_{12} - \omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 36\omega_{10}v_1^2\omega_5^2\omega_{15}\omega_9 + 18\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9 - 12\omega_{10}c_s^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12c_s^2\omega_5^3\omega_9\omega_{12} + 12\omega_{10}\omega_5^2\omega_{21}\omega_{12} + 12\omega_{10}\omega_5^2\omega_{15}\omega_9\omega_{12} + 18\omega_{10}c_s^2\omega_5\omega_{21}\omega_{15}\omega_9 - 15\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 18\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 12\omega_{10}c_s^2\omega_5^3\omega_9\omega_{12} - 12\omega_{10}c_s^2\omega_5\omega_{21}\omega_{15}\omega_{12} + 18\omega_{10}v_1^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 54\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} - 6\omega_{10}c_s^2\omega_5^3\omega_{15}\omega_9 - 6\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 18v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 6\omega_5^3\omega_{15}\omega_9\omega_{12} - 36\omega_{10}v_1^2\omega_5^2\omega_{15}\omega_9\omega_{12} - 12\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{12} - 54\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 18v_1^2\omega_5^3\omega_{15}\omega_9\omega_{12} + \omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 6\omega_{10}\omega_5^3\omega_{15}\omega_9\omega_{12} + 12\omega_{10}\omega_5^3\omega_9\omega_{12} - 6\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 5\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 12\omega_5^3\omega_9\omega_{12} + 36\omega_{10}v_1^2\omega_5^2\omega_9\omega_{12}) \frac{c_s^2\rho}{12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}}$$

$$C_{D_x^3 D_y v_1}^{(2), \text{CLBM}^2} = C_{D_x^3 D_y v_1}^{(2), \text{CLBM}^1}$$

$$C_{D_x^3 D_y v_1}^{(2), \text{CuLBM}^1} = (36\omega_1^2v_1^2 + 18\omega_4\omega_3^3v_1^2 - 36\omega_1v_1^2\omega_9 + 18\omega_4c_s^2\omega_1\omega_9 - 6\omega_4\omega_1^3 + c_s^2\omega_3^3\omega_9 + 12\omega_1\omega_9 + 18\omega_4\omega_1^2 + 6c_s^2\omega_2^2\omega_9 - 12\omega_4\omega_1 - 54\omega_4\omega_1^2v_1^2 - 18\omega_3^3v_1^2 - 3\omega_4\omega_1^2v_2^2\omega_9 + 3\omega_1^3v_1^2\omega_9 - 12\omega_1^2 - 18\omega_4c_s^2\omega_1^2 + \omega_4\omega_1^2\omega_9 - \omega_3^3\omega_9 - 12c_s^2\omega_1\omega_9 - \omega_4c_s^2\omega_1^3\omega_9 + 6\omega_4c_s^2\omega_1^3 + 36\omega_4\omega_1v_1^2 + 6\omega_1^3 + 12c_s^2\omega_1^2 + 18\omega_1^2v_1^2\omega_9 - 6c_s^2\omega_1^3 + 12\omega_4c_s^2\omega_1 - 5\omega_4c_s^2\omega_1^2\omega_9 - 6\omega_1^2\omega_9 - 12\omega_4c_s^2\omega_9) \frac{c_s^2\rho}{12\omega_4\omega_1^3\omega_9}$$

$$C_{D_x^3 D_y v_1}^{(2), \text{CuLBM}^2} = (-4\omega_3\omega_4\omega_2^2\omega_2^2 + 108\omega_3c_s^2\omega_1v_1^2\omega_3^2 + 144\omega_3\omega_4v_1^2\omega_3^2 + 81\omega_3\omega_4v_1^2\omega_2^2 + 24\omega_4c_s^2\omega_1^3v_1^2\omega_2 + 144\omega_3\omega_4c_s^2\omega_1^3v_1^2 - 20\omega_3\omega_4c_s^2\omega_1^3 - 28\omega_3\omega_4c_s^4\omega_1\omega_2^2 + 3\omega_3\omega_4c_s^2\omega_1^3v_2^2\omega_2^2 + 84\omega_3\omega_4\omega_2^2v_1^2\omega_2^2 - 7\omega_3\omega_4\omega_2^2\omega_2^2 + 24\omega_4c_s^2\omega_1v_1^2\omega_2^2 - 10\omega_3\omega_4\omega_1^3\omega_2 - 36\omega_3c_s^2\omega_1\omega_2^2 + 120\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 + 94\omega_3\omega_4c_s^4\omega_1\omega_2^2 + 138\omega_3\omega_4\omega_1^3v_1^4\omega_2^2 - 8\omega_4c_s^2\omega_1\omega_2^3 - 240\omega_3\omega_4\omega_1^3v_1^4\omega_2 - 24\omega_3\omega_4\omega_1v_1^4\omega_2^2 + 27\omega_4c_s^2\omega_1^3v_1^2\omega_2^3 - 96\omega_3\omega_4\omega_1^2v_1^2\omega_2 + 32\omega_3\omega_4c_s^2\omega_1\omega_2^2 - \omega_3\omega_4\omega_1^3v_2^2\omega_2^2 - 90\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 + 7\omega_3\omega_4\omega_1^3\omega_2^2 + 408\omega_3\omega_4\omega_1v_1^4\omega_2^2 - \omega_3\omega_4\omega_1^2v_1^4\omega_2^2 + 36\omega_3c_s^4\omega_1\omega_2^3 - 153\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 - 54\omega_3\omega_4c_s^2\omega_1\omega_2^3 + 40\omega_3\omega_4c_s^2\omega_2^2 + 8\omega_3\omega_4\omega_2^2\omega_2 - 54\omega_4c_s^2\omega_1^3v_1^2\omega_2^2 + 27\omega_3c_s^2\omega_1^3v_1^2\omega_2^3 + 96\omega_3\omega_4\omega_1^3v_1^4 + 8\omega_4c_s^4\omega_1\omega_2^3 - 168\omega_3\omega_4\omega_1^2v_1^4\omega_2^2 - 9\omega_4c_s^2\omega_1^3\omega_2^3 - 3\omega_3\omega_4c_s^4\omega_1^3\omega_2^3 + 8\omega_3\omega_4c_s^2\omega_1^2\omega_2 - 36\omega_3c_s^2\omega_1^2\omega_2^3 - 60\omega_3\omega_4c_s^2\omega_1v_1^2\omega_2^2 - 9\omega_3c_s^2\omega_1^2\omega_2^3 + 42\omega_3\omega_4c_s^2\omega_1^2\omega_2 + 24\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 - 81\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 288\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2 - 18\omega_4c_s^4\omega_1^2\omega_2^3 + 8\omega_4c_s^4\omega_1^2\omega_2 + 17\omega_3\omega_4c_s^4\omega_1^3\omega_2^2 - 264\omega_3\omega_4v_1^4\omega_2^3 + 18\omega_4c_s^2\omega_1^3\omega_2^2 - 8\omega_3\omega_4\omega_2^3 - 60\omega_3\omega_4\omega_1^3v_1^2 - 138\omega_3\omega_4v_1^4\omega_2^3 + 20\omega_4c_s^4\omega_2^2\omega_2^2 - 312\omega_3\omega_4c_s^2v_1^2\omega_2^3 + 16\omega_3\omega_4c_s^4\omega_1^3 - 6\omega_3\omega_4c_s^2\omega_1^2\omega_2^2 - 3\omega_3\omega_4c_s^2\omega_1^2v_2^2\omega_2^3 + 432\omega_3\omega_4c_s^2\omega_1v_1^2\omega_2^3 - 222\omega_3\omega_4\omega_1v_1^2\omega_2^3 + 9\omega_4c_s^2\omega_1^3\omega_2^3 + \omega_3\omega_4\omega_1^2v_2^2\omega_2^3 - 16\omega_3\omega_4c_s^2\omega_1^2\omega_2 + 4\omega_3\omega_4\omega_1^3 + 60\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 - 108\omega_3c_s^2\omega_1^2v_1^2\omega_2^3 + 36\omega_3c_s^2\omega_1^2\omega_2^3 + 14\omega_3\omega_4\omega_1\omega_2^3 - 29\omega_3\omega_4c_s^4\omega_1^2\omega_2^3 + 9\omega_3c_s^4\omega_1^3\omega_2^3 - 68\omega_3\omega_4c_s^4\omega_2^3 - 32\omega_3\omega_4c_s^2\omega_1^2\omega_2 - 8\omega_4c_s^2\omega_1^2\omega_2 + 18\omega_4c_s^2\omega_1^2\omega_2^3 - 24\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 - 4\omega_3\omega_4\omega_1\omega_2^3 + 138\omega_3\omega_4\omega_1^2v_1^2\omega_2 - 54\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 + 153\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2^2 + 12\omega_3\omega_4\omega_1v_1^2\omega_2^2 - 18\omega_4c_s^4\omega_1^3\omega_2^2 + 192\omega_3\omega_4\omega_2^2v_1^4\omega_2 - 20\omega_4c_s^2\omega_1^2\omega_2^2 + \omega_3\omega_4\omega_1^3v_2^2\omega_2^2 + 10\omega_3\omega_4c_s^4\omega_1^2\omega_2^2) \frac{\rho}{36\omega_3\omega_4\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_x^3 D_y v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} :$$

$$C_{D_x^3 D_y v_2}^{(2), \text{SRT}} = (2 - 2v_1^2 + 3c_s^2\omega - \omega + \omega v_1^2 - 6c_s^2) \frac{\rho v_1 v_2}{12\omega}$$

$$C_{D_x^3 D_y v_2}^{(2), \text{MRT}^1} = (156\omega_{10}^2c_s^2\omega_5\omega_{21}\omega_{15}^2\omega_9^2\omega_{12} - 12\omega_{10}c_s^2\omega_5^3\omega_{15}^2\omega_9^2\omega_{12} + 18\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 24\omega_{10}^2c_s^2\omega_5^2\omega_{15}^2\omega_9^2\omega_{12} + 12\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 12\omega_{10}^2c_s^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} - 18\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 24c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5^2\omega_{15}\omega_9\omega_{12} + 24\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2 + 60\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 24\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2 - 24\omega_{10}^2\omega_5^2\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + \omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 66\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 24c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 48\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - \omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 90\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 24\omega_{10}^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2 + 18\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 24\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 6\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 6\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 18\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12\omega_{10}^2c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} - 36\omega_{10}^2c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 24\omega_{10}\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 6\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 24\omega_{10}^2c_s^2\omega_5^2\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 66\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 24\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 24\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 12\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 24\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 6\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 24\omega_{10}^2c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} - 36\omega_{10}^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 24\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 96\omega_{10}^2c_s^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 6\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 18\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 24\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 24\omega_{10}^2c_s^2\omega_5^2\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 4\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 24\omega_{10}^2c_s^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} - 72\omega_{10}c_s^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 48\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 72\omega_{10}^2c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 36\omega_{10}^2c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 42\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 24\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 4\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 12\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{10}^2c_s^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 24\omega_{10}^2\omega_5^2\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}v_1^2\omega_5^2\omega_{15}\omega_9^2\omega_{12} + 3\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} -$$

$$84\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 24\omega_{10}v_1^2\omega_5^2\omega_{15}\omega_9^2\omega_{12}^2 - 12\omega_{10}v_1^2\omega_5^3\omega_{15}\omega_9^2\omega_{12} + 24\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 84\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 12\omega_{10}\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2 - 132\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 12\omega_{10}^2\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2$$

$$C_{D_x^3 D_y v_2}^{(2), \text{MRT2}} = C_{D_x^3 D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^3 D_y v_2}^{(2), \text{CLBM1}} = (-\omega_9 \omega_{12} + v_1^2 \omega_9 \omega_{12} + 3c_s^2 \omega_9 \omega_{12} - 9c_s^2 \omega_9 + 3c_s^2 \omega_{12} + v_1^2 \omega_{12} - 3v_1^2 \omega_9 + 3\omega_9 - \omega_{12}) \frac{\rho v_1 v_2}{12 \omega_9 \omega_{12}}$$

$$C_{D_x^3 D_y v_2}^{(2), \text{CLBM2}} = C_{D_x^3 D_y v_2}^{(2), \text{CLBM1}}$$

$$C_{D_x^3 D_y v_2}^{(2), \text{CuLBM1}} = (-9\omega_4 c_s^2 - \omega_4 \omega_9 + 3\omega_4 + \omega_4 v_1^2 \omega_9 + 3c_s^2 \omega_9 - 3\omega_4 v_1^2 + v_1^2 \omega_9 - \omega_9 + 3\omega_4 c_s^2 \omega_9) \frac{\rho v_1 v_2}{12\omega_4 \omega_9}$$

$$6\omega_3\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 18\omega_3\omega_4v_2^2\omega_2 + 6\omega_3\omega_4\omega_1v_1^2\omega_2 + 9\omega_3\omega_1\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 + 2\omega_3\omega_4\omega_2 + 18\omega_3\omega_4\omega_1v_2^2) \frac{\rho v_1 v_2}{72\omega_3\omega_4\omega_1\omega_2}$$

$$C_{D_x^2 D_y^2 \rho}^{(2), \text{SRT}} = (24 + 108c_s^2\omega - \omega^3 + 14\omega^2 + 5c_s^2\omega^3 + 36\omega v_2^2 - 46c_s^2\omega^2 - 36\omega - 14\omega^2 v_2^2 - 72c_s^2 - 24v_2^2 + \omega^3 v_2^2) \frac{c_s^2 v_2}{12\omega^3}$$

$$C_{D_x^2 D_y^2 \rho}^{(2), \text{MRT2}} = C_{D_x^2 D_y^2 \rho}^{(2), \text{MRT1}}$$

$$36\omega_{10}^2c_s^2\omega_{21}\omega_{15}\omega_{12} - 36\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{12} + 12\omega_{10}^3v_2^2\omega_{21}\omega_{15}\omega_{12} - 18\omega_{10}^3\omega_5\omega_{21}\omega_{15}\omega_{12} - 12\omega_{10}\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_{12} - 12\omega_{10}^3\omega_5v_2^2\omega_{15}\omega_{12} + 18\omega_{10}^3\omega_5v_2^2\omega_{21}\omega_{15}\omega_{12} + 12\omega_{10}^3\omega_5\omega_{15}\omega_{12} - 36\omega_{10}^3c_s^2\omega_5\omega_{21}\omega_{12} - 12\omega_{10}^3\omega_5^2v_2^2\omega_{21}\omega_{12} - 18\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 6\omega_{10}^3\omega_5^2\omega_{15}^2) \frac{c_s^2v_2}{12\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}^2\omega_{12}}$$

$$C_{D_x^2D_y^2\rho}^{(2),\text{CLBM2}} = C_{D_x^2D_y^2\rho}^{(2),\text{CLBM1}}$$

$$C_{D_x^2D_y^2\rho}^{(2),\text{CuLBM1}} = (12\omega_1^2\omega_5^2 + 36\omega_7^2c_s^2\omega_5^2 + 18\omega_7^2\omega_1^2\omega_5 + 54\omega_7c_s^2\omega_1\omega_5^3 + 18\omega_7\omega_1\omega_5^3v_2^2 - 36\omega_7^2c_s^2\omega_5^2 - 12\omega_7^2\omega_1^2 + 4\omega_7^2\omega_1^2\omega_5^2v_2^2 - 12\omega_1^2\omega_5^3 + 36\omega_7c_s^2\omega_1\omega_5^2 - 12\omega_7\omega_5^3v_2^2 - 54\omega_7^2c_s^2\omega_1^2\omega_5 - 12\omega_1\omega_5^3v_2^2 + 12\omega_7^2c_s^2\omega_1^2\omega_5^2 - 12\omega_7\omega_1\omega_5^2 - \omega_7^2\omega_1^2\omega_5^3 + 5\omega_7^2c_s^2\omega_1^2\omega_5^3 - 36c_s^2\omega_1\omega_5^3 + 12\omega_7\omega_1\omega_5^3v_2^2 + 12\omega_7\omega_1\omega_5^3v_2^2 - 4\omega_7^2\omega_1^2\omega_5^2 - 18\omega_7\omega_1\omega_5^3 + 12\omega_1^2\omega_5^3v_2^2 - 40\omega_7^2c_s^2\omega_1\omega_5^3 - 12\omega_7^2\omega_5^3 + 36c_s^2\omega_1^2\omega_5^3 + 12\omega_7^2\omega_1^2v_2^2 + 6\omega_7\omega_1^2\omega_5^3 - 6\omega_7^2\omega_1\omega_5^2 - 12\omega_7^2\omega_5^2v_2^2 + 18\omega_7^2c_s^2\omega_1\omega_5^2 + 12\omega_7^2\omega_1\omega_5^3 + 6\omega_7\omega_1^2\omega_5^2v_2^2 - 6\omega_7\omega_1^2\omega_5^2 - 36c_s^2\omega_1^2\omega_5^2 - 12\omega_7^2\omega_1\omega_5^3v_2^2 + 36\omega_7^2c_s^2\omega_1^2 + 12\omega_7^2\omega_5^2 - 36\omega_7c_s^2\omega_5^3 + 12\omega_1\omega_5^3 - 18\omega_7^2\omega_1^2\omega_5^2v_2^2 + 18\omega_7c_s^2\omega_1^2\omega_5^2 - 12\omega_1^2\omega_5^2v_2^2 + 6\omega_7^2\omega_1\omega_5^2v_2^2 - 6\omega_7\omega_1^2\omega_5^3v_2^2 + 12\omega_7^2\omega_5^3v_2^2 - 18\omega_7c_s^2\omega_1^2\omega_5^3) \frac{c_s^2v_2}{12\omega_7^2\omega_1^2\omega_5^3}$$

$$C_{D_x^2D_y^2\rho}^{(2),\text{CuLBM2}} = (-72\omega_4^2c_s^4\omega_1^2\omega_2^3 - 20\omega_3^2\omega_2^2c_s^2\omega_1^3v_2^2\omega_2 - 27\omega_3^2\omega_2^2\omega_1^2v_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 + 4\omega_3\omega_4^2c_s^2\omega_1^2\omega_2 - 28\omega_3^2\omega_2^2c_s^2\omega_1^2v_2^2\omega_2^2 - 36\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 + 35\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^2 - 27\omega_3\omega_4^2c_s^4\omega_1^3\omega_2^3 - 16\omega_3^2\omega_2^2c_s^2\omega_1^2\omega_2^2 - 108\omega_3^2c_s^4\omega_1^2\omega_2^3 - 216\omega_3^2\omega_4^2c_s^2v_1^2\omega_2^3 - 4\omega_3^2\omega_4^2\omega_1^3v_2^2 - 24\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 - 18\omega_4^2c_s^2\omega_1^3\omega_2^3 + 4\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 + 20\omega_3^2\omega_4^2c_s^2\omega_2^3 - 4\omega_3^2\omega_4^2\omega_1^2\omega_2 + 15\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^3 - 32\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^2 - 138\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1^3v_1^2v_2^2 + 24\omega_3^2\omega_4^2\omega_1^3v_1^2 + 36\omega_3^2\omega_4^2v_1^2v_2^2\omega_2^3 + 4\omega_3^2\omega_1^2v_2^2\omega_2 + 12\omega_4^2c_s^2\omega_1^3\omega_2^2 - 36\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^3 + 74\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2 + 49\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3 - 27\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 - 9\omega_3^2\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^3 - 52\omega_3^2\omega_4^2c_s^2\omega_1^3 - 8\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 30\omega_3^2\omega_4^2\omega_1^2v_1^2v_2^2\omega_2^3 + 24\omega_4^2c_s^2\omega_1^3\omega_2^3 - 28\omega_3\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 + 12\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 25\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 + 108\omega_3\omega_4^2c_s^4\omega_1^2\omega_2^3 + 54\omega_3^2c_s^4\omega_1^3\omega_2^3 - 12\omega_3\omega_4^2c_s^4\omega_1^3\omega_2 + 66\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 + 8\omega_3^2\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3^2c_s^2\omega_1^2\omega_2^3 + 24\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^2 + 9\omega_3\omega_4^2c_s^2\omega_1^3\omega_2^3 + 3\omega_3^2\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^3 + 54\omega_4^2c_s^2\omega_1^3\omega_2^3 + 24\omega_3^2\omega_1^2v_1^2\omega_2^3 + 16\omega_3^2\omega_1^2c_s^2\omega_1^3v_2^2 - 4\omega_3\omega_4^2c_s^2\omega_1^2v_2^2\omega_2 + 4\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2 + 96\omega_3\omega_4^2c_s^4\omega_1^2\omega_2^2 - 102\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 - 9\omega_3^2\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^3 - 42\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 48\omega_3^2\omega_4^2\omega_1^2v_1^2v_2^2\omega_2^2 + 8\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 + 8\omega_3^2\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^2 - 119\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^3 - 4\omega_3^2\omega_4^2\omega_1^3\omega_2 - 102\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2 + 4\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2 - 12\omega_3^2\omega_4^2\omega_1^2v_1^2v_2^2\omega_2^3 + 18\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^3 + 36\omega_3\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 - 24\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 4\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 4\omega_3^2\omega_4^2v_2^2\omega_2^3 - 4\omega_3^2\omega_1^2\omega_2^3 + 27\omega_3^2\omega_1^2v_1^2\omega_2^2 + 78\omega_3^2\omega_4^2c_s^4\omega_1\omega_2^3 + 4\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 32\omega_3\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^2 - 36\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 + 27\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_2^3 + 18\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^3 - 84\omega_3\omega_4^2c_s^4\omega_1\omega_2^3 - 72\omega_3^2\omega_4^2c_s^4\omega_1\omega_2^2 - 4\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2 - 4\omega_3^2\omega_4^2\omega_1\omega_2^2 - 27\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^3 + 216\omega_3^2\omega_4^2c_s^2\omega_1^3v_1^2\omega_2^2 + 138\omega_3^2\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^2 + 16\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^2 + 72\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 324\omega_3^2\omega_4^2c_s^2\omega_1^3v_2^2\omega_2^2 + 16\omega_3^2\omega_4^2c_s^2v_2^2\omega_2^3 - 58\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^3 + 36\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 + 108\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^2 + 4\omega_3^2\omega_4^2\omega_1^3 + 72\omega_3^2\omega_4^2c_s^4\omega_1^3 + 36\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 28\omega_3\omega_4^2c_s^2\omega_1^2\omega_2^3 - 30\omega_3^2\omega_4^2\omega_1^2v_1^2v_2^2\omega_2 + 324\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_2^3 - 32\omega_3^2\omega_4^2c_s^2\omega_1^2v_2^2\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 28\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^2 + 60\omega_3^2\omega_4^2\omega_1^2v_1^2v_2^2\omega_2^2 + 12\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 48\omega_3^2\omega_4^2\omega_1^3v_1^2 + 9\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 - 60\omega_3^2\omega_4^2v_1^2\omega_2^3) \frac{v_2^2}{36\omega_3^2\omega_4^2\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_x^2D_y^2v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{SRT}} = 0$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{MRT1}} = (3\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^3\omega_5^2v_2^2\omega_{15}\omega_9\omega_{12} - 8\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^3\omega_5^3\omega_{21}\omega_9\omega_{12}^2 + 3\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 8\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 4\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - 7\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^3\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - \omega_{10}^3\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 2\omega_{10}c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 9\omega_{10}^2c_s^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + \omega_{10}^3\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 4\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + \omega_{10}^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 8\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_9\omega_{12}^2 - 2\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 6\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 6\omega_{10}^3c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^2c_s^2\omega_5^3\omega_{15}\omega_9\omega_{12}^2 + 6\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^2\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^2c_s^2\omega_5^2\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^3\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^3c_s^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 2\omega_{10}^3\omega_5^3\omega_{15}\omega_9\omega_{12}^2 + 11\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^2c_s^2v_2^2\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 26\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^3c_s^2\omega_5^2\omega_{15}\omega_9\omega_{12}^2 - 3\omega_{10}^3\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^3\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^2\omega_5^3\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^2\omega_5^3v_2^2\omega_{21}\omega_9\omega_{12}^2 + 3\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 8\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^3\omega_5^2\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^3\omega_5^2v_2^2\omega_{15}\omega_9\omega_{12}^2 - 5\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + \omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^3\omega_5^2\omega_{15}\omega_9\omega_{12}^2 - 8\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 5\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 13\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^3\omega_5^3\omega_{15}\omega_9\omega_{12}^2 - 15\omega_{10}c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 24\omega_{10}^2c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^3\omega_5^3v_2^2\omega_{21}\omega_9\omega_{12}^2 - \omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^2\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12}^2 + 4\omega_{10}^2\omega_5^3\omega_{21}\omega_9\omega_{12}^2 + 4\omega_{10}^3\omega_5^2\omega_{15}\omega_9\omega_{12}^2 - 4\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 2\omega_{10}^3\omega_5^3v_2^2\omega_{15}\omega_9\omega_{12}^2 - \omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 6\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 8\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_9\omega_{12}^2 + 2\omega_{10}^2\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 16\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - \omega_{10}^3\omega_5^2v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 12\omega_{10}^2c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 7\omega_{10}^3\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 4\omega_{10}^3c_s^2\omega_5^3\omega_{15}\omega_9\omega_{12}^2 - 5\omega_{10}\omega_5^3v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2) \frac{\rho v_1 v_2}{2\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12}^2}$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{MRT2}} = C_{D_x^2D_y^2v_1}^{(2),\text{MRT1}}$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{CLBM1}} = 0$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{CLBM2}} = 0$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{CuLBM1}} = 0$$

$$C_{D_x^2D_y^2v_1}^{(2),\text{CuLBM2}} = (48\omega_3\omega_1^3\omega_2 + 23\omega_3\omega_1^2\omega_2^3 + 6\omega_3\omega_1^2v_1^2\omega_2 + 12\omega_1^2v_2^2\omega_2^2 - 114\omega_3v_1^2\omega_2^3 + 12\omega_3\omega_1^2\omega_2^2 + 108\omega_3c_s^2\omega_1\omega_2^3 + 6\omega_1\omega_2^3 + 84\omega_3c_s^2\omega_1^3 + 36c_s^2\omega_1^2\omega_2^2 - 50\omega_3\omega_1^2v_1^2\omega_2^2 - 9\omega_3\omega_1^2v_2^2\omega_2^2 + 6\omega_3\omega_1^2\omega_2 - 66\omega_3c_s^2\omega_2^2 + 12\omega_3\omega_1^3v_2^2 - 18c_s^2\omega_1^3\omega_2 - 23\omega_3\omega_1^3\omega_2^2 - 9\omega_3\omega_1^3v_2^2\omega_2 - 12\omega_3\omega_1^2v_2^2\omega_2^2 - 66\omega_3\omega_1^2v_1^2\omega_2^2 +$$

$$\begin{aligned}
& 68\omega_3^2\omega_4c_s^4\omega_3^2 + 54\omega_3^2\omega_4\omega_1v_1^4\omega_3^2 - 54\omega_3c_s^2\omega_3^3v_1^2\omega_3^2 - 18\omega_3\omega_1^2v_2^2\omega_3^2 + 24\omega_3\omega_4c_s^2\omega_3^3v_2^2\omega_2 - 18\omega_3^3\omega_1^2v_1^2\omega_2^2 + 72\omega_3^2c_s^2\omega_1^2\omega_3^2 - 4\omega_3^2\omega_4\omega_1\omega_3^2 - \\
& \omega_3^2\omega_4\omega_1^2v_2^3\omega_3^2 - 12\omega_3^2\omega_4v_2^3\omega_3^2 - 144\omega_3^2\omega_4\omega_1v_1^2v_2^2\omega_3^2 + 54\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_3^2 + 6\omega_3\omega_4\omega_1v_1^4\omega_3^2 + 54\omega_3^2c_s^2\omega_1^3v_1^2\omega_3^2 - 18\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_3^2 - \\
& 18\omega_3^2\omega_1^4v_1^4\omega_3^2 - \omega_3^2\omega_4\omega_1^3v_2^2\omega_3^2 + 32\omega_3^2\omega_4c_s^2\omega_1\omega_3^2 - 90\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_3^2 - 8\omega_3\omega_4c_s^2\omega_1\omega_3^2 - 90\omega_3^2\omega_4\omega_1v_1^2v_2^2\omega_3^2 - 36\omega_3^2\omega_4\omega_1^3v_1^4\omega_3^2 + 60\omega_3\omega_4c_s^2\omega_1v_2^2\omega_3^2 - \\
& 4\omega_3^2\omega_4\omega_1\omega_3^2 - 54\omega_4c_s^2\omega_3^3v_1^2\omega_3^2 + 12\omega_3^2\omega_4\omega_1v_1^4\omega_3^2 - 18\omega_4\omega_1^3v_1^4\omega_3^2 - 48\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_3^2 + 6\omega_3\omega_4\omega_1^2v_1^4\omega_3^2 - 108\omega_3^2\omega_4c_s^2v_1^2\omega_3^2 + 54\omega_3^2c_s^2\omega_3^3v_2^2\omega_3^2 - \\
& 36\omega_3^2\omega_4c_s^2\omega_1^2\omega_3^2 + 18\omega_3\omega_4c_s^4\omega_1^3\omega_3^2 - 20\omega_3^2\omega_4c_s^2\omega_3^3 + 30\omega_3^2\omega_4c_s^2\omega_1^3v_1^2\omega_3^2 + 12\omega_3^2\omega_4v_1^2\omega_3^2 - 8\omega_3\omega_4c_s^2\omega_1^3\omega_2 + 2\omega_3^2\omega_4c_s^4\omega_1^3\omega_3^2 + 132\omega_3\omega_4c_s^2\omega_1^2v_2^2\omega_3^2 + \\
& 36\omega_3\omega_4c_s^2\omega_1^2\omega_3^3 - 36\omega_3\omega_4\omega_1^3v_1^2\omega_3^2 - 36\omega_3\omega_4c_s^2\omega_3^3v_1^2\omega_2 - 9\omega_3^2\omega_4\omega_1^2v_1^4\omega_3^2 + 8\omega_3^2\omega_4\omega_1^2\omega_3^2 + 18\omega_3^2\omega_4c_s^2\omega_1^3\omega_2 - 36\omega_3\omega_4c_s^4\omega_1^3\omega_3^2 - 9\omega_3^2\omega_4\omega_1^3v_1^2\omega_3^2 + \\
& 2\omega_3^2\omega_4c_s^2\omega_1^2\omega_3^2 + 18\omega_3^2\omega_1v_1^4\omega_3^2 + 12\omega_3^2\omega_4\omega_1^2v_2^2\omega_3^2 - 36\omega_3\omega_4\omega_1^2v_1^4\omega_3^2 - 18\omega_3^2\omega_4\omega_1^3v_1^4\omega_3^2 + 72\omega_3^2\omega_4\omega_1^3v_1^2v_2^2 - 4\omega_3^2\omega_4\omega_1^3\omega_2 - 72\omega_3^2c_s^2\omega_1\omega_3^2 - \\
& 36\omega_3^2\omega_4\omega_1^3v_1^2v_2^2\omega_2 + 108\omega_3^2\omega_4v_1^2v_2^2\omega_3^2 - 56\omega_3\omega_4c_s^2\omega_1^2\omega_3^2 - 126\omega_3\omega_4c_s^2\omega_1^2v_2^2\omega_3^2 - 3\omega_3^2\omega_4c_s^4\omega_1^3\omega_3^2 - 18\omega_3\omega_4c_s^2\omega_1v_1^2\omega_3^2 - 28\omega_3^2\omega_4c_s^4\omega_1^2\omega_2 - \\
& 6\omega_3\omega_4\omega_1v_1^2\omega_3^2 + 12\omega_3^2\omega_4\omega_1^3v_1^4\omega_2 + 180\omega_3^2\omega_4\omega_1^3v_1^2v_2^2\omega_3^2 + 12\omega_3^2\omega_4c_s^2\omega_1^3v_2^2 + 18\omega_3^2\omega_1^3v_1^2\omega_3^2 + 54\omega_3c_s^2\omega_1^2v_1^2\omega_3^2 + 18\omega_3\omega_1^3v_1^2\omega_3^2 - 18\omega_3\omega_4c_s^2\omega_3^3\omega_2^2 + \\
& \omega_3^2\omega_4\omega_1^3v_2^3\omega_3^2 + 28\omega_3^2\omega_4c_s^2\omega_1^2\omega_3^2 - 36\omega_3\omega_4c_s^4\omega_1^3\omega_3^2 - 12\omega_3^2\omega_4\omega_1^3v_2^2 - 2\omega_3^2\omega_4c_s^2\omega_3^3\omega_2^2 - 54\omega_3^2c_s^2\omega_1^2v_1^2\omega_3^2 + 66\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 8\omega_3\omega_4c_s^4\omega_1^3\omega_2 - \\
& 24\omega_3^2\omega_4\omega_1^3v_2^2\omega_3^2 + 150\omega_3^2\omega_4c_s^2\omega_1v_1^2\omega_3^2 - 90\omega_3^2\omega_4\omega_1^3v_1^2v_2^2\omega_2 + 18\omega_4\omega_1^3v_1^2\omega_3^2 - 6\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_3^2 + 36\omega_3^2\omega_4\omega_1v_1^2\omega_3^2 - 14\omega_3^2\omega_4c_s^4\omega_1^3\omega_3^2 + \\
& 36\omega_3\omega_4c_s^2\omega_3^3\omega_2^2 + 12\omega_3\omega_4\omega_1^3v_1^2\omega_2 - 14\omega_3^2\omega_4c_s^4\omega_1^3\omega_2 + 18\omega_3^2\omega_1^3v_1^2\omega_2^2 + 18\omega_4\omega_1^3v_1^4\omega_3^2 + 24\omega_3^2\omega_4\omega_1^3v_1^4 + 54\omega_4c_s^2\omega_1^3v_1^2\omega_3^2 + 90\omega_3\omega_4c_s^2\omega_3^3v_1^2\omega_2^2 + \\
& 28\omega_3^2\omega_4c_s^2\omega_3^3 - 4\omega_3^2\omega_4\omega_1^3\omega_2 + 72\omega_3^2c_s^4\omega_1\omega_3^2 + 18\omega_3^2\omega_1^3v_1^4\omega_3^2 - 24\omega_3^2\omega_4\omega_1v_1^2\omega_3^2 + 18\omega_3\omega_1^3v_1^4\omega_3^2 + 66\omega_3^2\omega_4c_s^2\omega_1^2v_2^2\omega_3^2 - 12\omega_3^2\omega_4c_s^2\omega_1v_1^2\omega_3^2 + \\
& \omega_3^2\omega_4\omega_1^3v_2^3\omega_3^2 - 54\omega_3^2c_s^2\omega_1^2v_1^2\omega_3^2 + 32\omega_3^2\omega_4c_s^2\omega_1^2\omega_2 - 174\omega_3^2\omega_4c_s^2\omega_1^3v_1^2\omega_2 + 216\omega_3^2c_s^2\omega_1v_2^2\omega_3^2 + 56\omega_3\omega_4c_s^4\omega_1^3\omega_2^2) \frac{\rho}{36\omega_3^2\omega_4\omega_1^3\omega_3^2}
\end{aligned}$$

coefficient $C_{D_x D_y^3 \rho}^{(2)}$ **at** $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 \rho}^{(2), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x D_y^3 \rho}^{(2), \text{MRT1}} = & (-13\omega_{10}^3\omega_5^2v_2^4\omega_{15} + 16\omega_{10}^2\omega_5v_2^2\omega_{15} - 72\omega_{10}c_s^2\omega_5^2v_2^2\omega_{15} + 8\omega_{10}^3c_s^4\omega_5\omega_{15} - 8\omega_{10}^2c_s^4\omega_5\omega_{15}^2 - 4\omega_{10}c_s^4\omega_5^2\omega_{15} + 4\omega_{10}^2\omega_5^2v_2^2 + \\
& 13\omega_{10}^2c_s^2v_2^4\omega_{15}^2 + 36\omega_{10}\omega_5^2v_2^2\omega_{15}^2 - 4\omega_{10}^2c_s^2\omega_{15}^2 - 4\omega_{10}^3c_s^2\omega_5^2 + 84\omega_{10}^3c_s^2\omega_5v_2^2\omega_{15} + 12\omega_{10}c_s^2\omega_5^2\omega_{15}^2 + 8\omega_{10}^2v_2^4\omega_{15} - 8c_s^2\omega_5^2\omega_{15}^2 + \\
& 120\omega_{10}^2c_s^2\omega_5^2v_2^2\omega_{15} - 24\omega_5^2v_2^2\omega_{15}^2 - 4\omega_{10}^2c_s^4\omega_5^2 - 4\omega_{10}^3c_s^4\omega_{15} + 51\omega_{10}^2c_s^2\omega_5^2v_2^2\omega_{15} + 96c_s^2\omega_5^2v_2^2\omega_{15}^2 + 4\omega_{10}^3\omega_5v_2^2 + 20\omega_{10}\omega_5v_2^4\omega_{15} - 8\omega_{10}^3c_s^2\omega_5\omega_{15} + \\
& 8\omega_{10}^2c_s^2\omega_5\omega_{15} + 8\omega_{10}^3v_2^2\omega_{15} + 20\omega_{10}\omega_5^2v_2^2\omega_{15} + 4\omega_{10}c_s^2\omega_5 + 4\omega_{10}c_s^2\omega_5^2\omega_{15} + 36\omega_{10}^2c_s^2v_2^2\omega_{15} - 12\omega_{10}c_s^2\omega_5^2\omega_{15} - 24\omega_{10}^3c_s^2\omega_5v_2^2 + \\
& 32\omega_{10}^2c_s^2v_2^4\omega_{15} - 20\omega_{10}^3\omega_5v_2^2\omega_{15} + 20\omega_{10}^2\omega_5v_2^2\omega_{15}^2 + 8c_s^4\omega_5^2\omega_{15} - 36\omega_{10}^2c_s^2v_2^2\omega_{15} - 144\omega_{10}c_s^2\omega_5^2v_2^2\omega_{15} + 4\omega_{10}^3\omega_5^2v_2^2 + 8\omega_{10}^2c_s^4\omega_5^2\omega_{15} - \\
& 84\omega_{10}^2c_s^2\omega_5v_2^2\omega_{15} + 4\omega_{10}^3c_s^4\omega_{15} - 36\omega_{10}\omega_5^2v_2^2\omega_{15} + 4\omega_{10}^3c_s^4\omega_5 + 4\omega_{10}c_s^4\omega_5\omega_{15} + 24\omega_{10}^2c_s^2\omega_5^2v_2^2 - 8\omega_{10}^3v_2^2\omega_{15} - 4\omega_{10}^2\omega_5v_2^2 + 24\omega_5^2v_2^2\omega_{15}^2 + \\
& 4\omega_{10}^2c_s^2\omega_5^2 - 16\omega_{10}^2\omega_5v_2^4\omega_{15} + 13\omega_{10}^3\omega_5^2v_2^2\omega_{15} + 4\omega_{10}^3c_s^2\omega_5^2\omega_{15} - 4\omega_{10}^3\omega_5^2v_2^2 - 4\omega_{10}^2c_s^2\omega_5^2\omega_{15} + 72\omega_{10}c_s^2\omega_5v_2^2\omega_{15}^2 - 13\omega_{10}^2\omega_5^2v_2^2\omega_{15} - \\
& 8\omega_{10}^3c_s^2\omega_5^2\omega_{15} - 4\omega_{10}c_s^2\omega_5\omega_{15}^2 - 4\omega_{10}^3\omega_5^2v_2^4 + 20\omega_{10}^3\omega_5v_2^3\omega_{15} - 32\omega_{10}^2\omega_5^2v_2^2\omega_{15} - 20\omega_{10}^2\omega_5v_2^2\omega_{15}^2 - 24\omega_{10}^2c_s^2\omega_5^2v_2^2 - 51\omega_{10}^3c_s^2\omega_5^2v_2^2\omega_{15} + \\
& 4\omega_{10}^3c_s^2\omega_{15} - 20\omega_{10}\omega_5v_2^2\omega_{15}^2 - 4\omega_{10}^3c_s^4\omega_5^2\omega_{15} + 4\omega_{10}^2c_s^4\omega_5^2\omega_{15}^2 - 20\omega_{10}\omega_5^2v_2^4\omega_{15} - 8\omega_{10}^3v_2^4\omega_{15} - 48\omega_{10}^2c_s^2\omega_5v_2^2\omega_{15} - 4\omega_{10}^3c_s^4\omega_5) \frac{v_1}{4\omega_{10}^3\omega_5^2\omega_{15}^2}
\end{aligned}$$

$$C_{D_x D_y^3 \rho}^{(2), \text{MRT2}} = C_{D_x D_y^3 \rho}^{(2), \text{MRT1}}$$

$$C_{D_x D_y^3 \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y^3 \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y^3 \rho}^{(2), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x D_y^3 \rho}^{(2), \text{CuLBM2}} = & (8\omega_3^2\omega_1\omega_2^2 + 24\omega_3^2\omega_1^2v_2^2\omega_3^2 - 8\omega_3^2\omega_1v_1^2\omega_3^2 - 24\omega_3^2\omega_1^2v_1^2v_2^2\omega_3^2 + 8\omega_3c_s^2\omega_1v_1^2\omega_3^2 + 40\omega_3^2c_s^2\omega_1^2\omega_2 - 20\omega_3^2c_s^2\omega_3^3v_1^2\omega_2 - 84\omega_3^2c_s^4\omega_1^3\omega_2 - \\
& 6\omega_3^2c_s^4\omega_1^2\omega_3^2 + 12c_s^2\omega_1^3\omega_3^2 + 8\omega_3^2c_s^2\omega_1v_1^2\omega_3^2 - 12c_s^2\omega_1^3v_1^2\omega_3^2 + 216\omega_3^2c_s^2\omega_1^2v_2^2\omega_3^2 + 4\omega_3^2\omega_1^3v_1^2\omega_2 + 24\omega_3^2v_2^3\omega_3^2 - 4\omega_3c_s^2\omega_1^3v_1^2\omega_2 - 5\omega_3^2c_s^2\omega_1^3\omega_2^2 - \\
& 48\omega_3^2\omega_1^2v_1^2v_2^2\omega_3^2 - 8\omega_3^2\omega_1v_1^2\omega_3^2 + 36c_s^4\omega_1^2\omega_3^2 - 8\omega_3c_s^2\omega_1\omega_3^2 + 8\omega_3^2\omega_1\omega_3^2 - 24\omega_3^2\omega_1^2v_2^2\omega_3^2 + 216\omega_3^2c_s^2\omega_1^3v_2^2 - 72\omega_3^2c_s^2\omega_1^2v_2^2\omega_3^2 - 36\omega_3^2c_s^4\omega_3^2 + \\
& 22\omega_3^2c_s^2\omega_1v_1^2\omega_3^2 - 48\omega_3^2\omega_1^3v_1^2v_2^2\omega_2 + 4\omega_3^2\omega_1^3 + 42\omega_3^2c_s^4\omega_1^2\omega_2 - 72\omega_3^2\omega_1v_1^4\omega_2 - 72\omega_3^2v_1^2v_2^2\omega_3^2 + 24\omega_3^2\omega_1^3v_1^2v_2^2\omega_2 + 24\omega_3^2c_s^4\omega_1^3\omega_2 - \\
& 36\omega_3^2\omega_1^3v_1^4\omega_2 - 4\omega_3^2\omega_1^3v_1^2 + 18\omega_3c_s^2\omega_1^3v_1^2\omega_2 - \omega_3^2\omega_1^3v_1^2\omega_3^2 + 5\omega_3^2c_s^2\omega_1^2\omega_3^2 + 72\omega_3^2c_s^4\omega_1^3 + 56\omega_3^2c_s^2\omega_1^3\omega_2 - 8\omega_3^2\omega_3^2 + 24\omega_3^2\omega_1^2v_1^2v_2^2\omega_2 - 36c_s^4\omega_1^3\omega_2^2 - \\
& 24\omega_3^2\omega_1^2v_2^2\omega_2 + 6\omega_3^2c_s^4\omega_1^3\omega_2^2 + 2\omega_3^2c_s^2\omega_3^3v_1^2\omega_2^2 + 24\omega_3c_s^4\omega_1\omega_3^2 - 36\omega_3^2\omega_1v_1^4\omega_3^2 - 12c_s^2\omega_1^2\omega_3^2 - 20\omega_3^2c_s^2v_1^2\omega_3^2 + 24\omega_3^2\omega_1^3v_1^4 - 34\omega_3^2c_s^2\omega_1^2\omega_2^2 + \\
& 12c_s^2\omega_1^2v_1^2\omega_3^2 + 48\omega_3^2v_2^3\omega_3^2 - 12\omega_3c_s^2\omega_1^3\omega_2 + 72\omega_3^2\omega_1^2v_2^2\omega_3^2 - 54\omega_3c_s^4\omega_1^2\omega_3^2 - 4\omega_3^2\omega_1^2\omega_2 + 4\omega_3^2\omega_1^2v_1^2\omega_2 + 20\omega_3^2c_s^2\omega_3^2 - 8\omega_3^2c_s^2\omega_1\omega_3^2 - 24\omega_3^2\omega_1^3v_2^2\omega_2 + \\
& 96\omega_3^2\omega_1v_1^2v_2^2\omega_3^2 - 12\omega_3c_s^4\omega_1^2\omega_2 - 4\omega_3^2c_s^2\omega_1^2v_1^2\omega_2 + 72\omega_3^2c_s^2\omega_1^2v_2^2\omega_2 - 48\omega_3^2\omega_1^3v_2^2 + 24\omega_3^2\omega_1v_1^2v_2^2\omega_2 - 22\omega_3^2c_s^2\omega_1\omega_3^2 - 18\omega_3c_s^2\omega_3^3\omega_2^2 + \omega_3^3\omega_1^2\omega_2^2 + \\
& \omega_3^2\omega_1^2v_1^2\omega_3^2 - 18\omega_3c_s^2\omega_1^2v_1^2\omega_3^2 + 18\omega_3c_s^2\omega_1^2\omega_3^2 - \omega_3^2\omega_1^2\omega_3^2 - 4\omega_3^2\omega_1^3\omega_2 + 4\omega_3c_s^2\omega_1^3\omega_2 - 60\omega_3^2\omega_1v_2^2\omega_3^2 - 216\omega_3^2c_s^2\omega_1v_2^2\omega_2^2 + 16\omega_3^2c_s^2\omega_1^3v_1^2 - \\
& 2\omega_3^2c_s^2\omega_1^2v_1^2\omega_2 - 324\omega_3^2c_s^2\omega_3^3v_2^2\omega_2 + 48\omega_3^2\omega_1v_2^2\omega_2 + 4\omega_3^2\omega_1^2v_1^2\omega_2 - 4\omega_3^2\omega_1^2\omega_3^2 + 4\omega_3c_s^2\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_1^2v_1^2\omega_2 + 8\omega_3^2v_1^2\omega_3^2 + 84\omega_3^2\omega_1^3v_2^2\omega_2 + \\
& 42\omega_3^2c_s^4\omega_1\omega_3^2 - 52\omega_3^2c_s^2\omega_1^3 - 2\omega_3^2c_s^2\omega_1^2v_1^2\omega_3^2 + 54\omega_3c_s^4\omega_1^2\omega_3^2 + 108\omega_3^2c_s^2\omega_1v_2^2\omega_3^2) \frac{v_1}{36\omega_3^2\omega_1^3\omega_3^2}
\end{aligned}$$

coefficient $C_{D_x D_y^3 v_1}^{(2)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^3}$:

$$\begin{aligned}
C_{D_x D_y^3 v_1}^{(2), \text{SRT}} = & (-42c_s^2\omega^2v_2^2 + 36c_s^2\omega + 4\omega^3v_2^4 - 36v_2^4 - 54\omega v_2^2 + 12c_s^2\omega^3v_2^2 - 12c_s^2\omega^2 + 36c_s^4 - 26\omega^2v_2^4 + 54\omega v_2^4 + 26\omega^2v_2^2 - 36c_s^2v_2^2 - 54c_s^4\omega - \\
& 24c_s^4 + 20c_s^4\omega^2 + 36v_2^2 - c_s^4\omega^3 + 54c_s^2\omega v_2^2 - 4\omega^3v_2^2) \frac{\rho}{12\omega^3}
\end{aligned}$$

$$\begin{aligned}
C_{D_x D_y^3 v_1}^{(2), \text{MRT1}} = & (48\omega_{10}^3\omega_5^2v_2^4\omega_{15} - 48\omega_{10}^3c_s^2v_2^2\omega_{15}^2 - 19\omega_{10}^2\omega_5^2v_2^2\omega_{15} + 12\omega_{10}^3c_s^4\omega_5\omega_{15} + 27\omega_{10}^3\omega_5^3v_2^2\omega_{15} - 12\omega_{10}^3\omega_5^2v_2^2\omega_{15} + 12\omega_{10}^2\omega_5^2v_2^4\omega_{15} + \\
& 12\omega_{10}^3c_s^2\omega_5^2v_2^2\omega_{15} + 12\omega_{10}^3\omega_5^3v_2^4 + 12c_s^4\omega_5^2\omega_{15}^2 + 72\omega_{10}^3v_2^4\omega_{15} - 12\omega_{10}^3c_s^2\omega_5^2v_2^2\omega_{15} + 12\omega_{10}c_s^2\omega_5^2\omega_{15}^2 - 12\omega_{10}c_s^4\omega_5^3\omega_{15} - 90\omega_{10}\omega_5^3v_2^4\omega_{15} + \\
& 12\omega_{10}^3c_s^4\omega_{15}^2 - 12\omega_{10}^2c_s^2\omega_5^2v_2^2\omega_{15} + 6\omega_{10}^3c_s^2\omega_5\omega_{15} + 12\omega_{10}^2\omega_5^3v_2^2 - 36\omega_{10}\omega_5^3v_2^4\omega_{15} + 162\omega_{10}^2c_s^2\omega_5^2v_2^2\omega_{15} - 12\omega_{10}^3c_s^2\omega_5\omega_{15} - 21\omega_{10}^2c_s^2\omega_5^3v_2^2\omega_{15} +
\end{aligned}$$

$$80\omega_5^2v_2^2\omega_{15}^2 - 40\omega_{10}^2\omega_5^2\omega_{15} - 16\omega_{10}^3\omega_5v_2^2 - 17\omega_{10}^2\omega_5^2\omega_{15}^2 + 44\omega_{10}^3c_s^2\omega_5\omega_{15} - 44\omega_{10}^2c_s^2\omega_5\omega_{15}^2 - 28\omega_{10}^3v_2^2\omega_{15} - 64\omega_{10}\omega_5^2v_2^2\omega_{15} - 12\omega_{10}^2\omega_{15}^2 - 16\omega_{10}^3c_s^2\omega_5 - 32\omega_{10}c_s^2\omega_5^2\omega_{15} - 24\omega_{10}\omega_5\omega_{15}^2 + 68\omega_{10}^3\omega_5v_2^2\omega_{15} - 28\omega_{10}^2\omega_5\omega_{15} - 68\omega_{10}^2\omega_5v_2^2\omega_{15}^2 + 12\omega_{10}^3\omega_{15} + 48\omega_{10}\omega_5^2\omega_{15}^2 + 17\omega_{10}^3\omega_5^2\omega_{15} - 32\omega_5^2\omega_{15}^2 + 28\omega_{10}^2v_2^2\omega_{15}^2 - 16\omega_{10}^2c_s^2\omega_5^2 - 43\omega_{10}^3\omega_5v_2^2\omega_{15} - 25\omega_{10}^3c_s^2\omega_5^2\omega_{15} + 28\omega_{10}^2\omega_5\omega_{15}^2 + 16\omega_{10}^3\omega_5^2v_2^2 + 25\omega_{10}^2c_s^2\omega_5^2\omega_{15} - 8\omega_{10}^3\omega_5^2 + 43\omega_{10}^2\omega_5^2v_2^2\omega_{15} + 56\omega_{10}^2c_s^2\omega_5^2\omega_{15} + 32\omega_{10}c_s^2\omega_5\omega_{15}^2 + 8\omega_{10}^3\omega_5 + 104\omega_{10}^2\omega_5^2v_2^2\omega_{15} + 16\omega_{10}^2\omega_5\omega_{15} + 8\omega_{10}^2\omega_5^2 - 20\omega_{10}^3c_s^2\omega_{15} + 64\omega_{10}\omega_5v_2^2\omega_{15}^2 + 24\omega_{10}\omega_5^2\omega_{15}) \frac{\rho v_1 v_2}{4\omega_{10}^3\omega_5^2\omega_{15}^2}$$

$$C_{D_x D_y^3 v_2}^{(2), \text{MRT}2} = C_{D_x D_y^3 v_2}^{(2), \text{MRT}1}$$

$$C_{D_x D_y^3 v_2}^{(2), \text{CLBM}1} = 0$$

$$C_{D_x D_y^3 v_2}^{(2), \text{CLBM}2} = 0$$

$$C_{D_x D_y^3 v_2}^{(2), \text{CuLBM}1} = 0$$

$$C_{D_x D_y^3 v_2}^{(2), \text{CuLBM}2} = (-54\omega_3c_s^2\omega_1\omega_2^2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^3 + 6\omega_3\omega_1^2v_1^2\omega_2 + 27c_s^2\omega_1^3\omega_2^2 - 6\omega_1^3v_1^2\omega_2 - 24\omega_3v_1^2\omega_2^3 - 51\omega_3\omega_1^2\omega_2^2 + 27\omega_3c_s^2\omega_1\omega_2^3 - 12\omega_1\omega_2^3 + 12\omega_1v_1^2\omega_2^3 + 84\omega_3c_s^2\omega_1^3 - 18c_s^2\omega_1^2\omega_2^2 - 5\omega_3\omega_1^2v_1^2\omega_2^3 - 66\omega_3\omega_1v_2^2\omega_2^3 + 6\omega_3\omega_1^2\omega_2 - 12\omega_3c_s^2\omega_2^3 + 48\omega_3\omega_1^3v_2^2 - 18c_s^2\omega_1^3\omega_2 + 9\omega_1^3v_1^2\omega_2^2 - 27c_s^2\omega_1^2\omega_2^3 - 5\omega_3\omega_1^3\omega_2^2 - 66\omega_3\omega_1^3v_2^2\omega_2 - 120\omega_3\omega_1v_2^2\omega_2^2 - 9\omega_3\omega_1^2v_1^2\omega_2^2 + 12\omega_3\omega_1^3v_1^2 + 36c_s^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 + 27\omega_3\omega_1v_1^2\omega_2^3 - 9\omega_1^3\omega_2^2 + 6\omega_3\omega_1v_1^2\omega_2^2 + 132\omega_3\omega_1^2v_2^2\omega_2^2 - 18\omega_3\omega_1^3v_1^2\omega_2 + 15\omega_3c_s^2\omega_1^3\omega_2^2 - 12\omega_3\omega_2^3 - 12\omega_3\omega_1^2v_1^2\omega_2 - 15\omega_3c_s^2\omega_1^2\omega_2^3 + 5\omega_3\omega_1^3v_1^2\omega_2^2 + 42\omega_3\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 + 6\omega_1^3\omega_2 + 9\omega_1^2\omega_2^3 - 6\omega_1^2v_1^2\omega_2^2 - 36\omega_3\omega_1^3 + 3\omega_3\omega_1\omega_2^3 + 81\omega_3c_s^2\omega_1^2\omega_2^2 + 84\omega_3v_2^2\omega_2^3 - 9\omega_1^2v_1^2\omega_2^3 + 6\omega_1^2\omega_2^2) \frac{\rho v_1 v_2}{18\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_y^4 \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_3^2}:$$

$$C_{D_y^4 \rho}^{(2), \text{SRT}} = (12 + 404c_s^2\omega^2v_2^2 + 198c_s^2\omega - \omega^3 - 9\omega^3v_2^4 + 8\omega^2 + 144v_2^4 + 6c_s^2\omega^3 + 234\omega v_2^2 - 34c_s^2\omega^3v_2^2 - 78c_s^2\omega^2 + 144c_s^4 + 90\omega^2v_2^4 - 216\omega v_2^4 - 18\omega - 98\omega^2v_2^2 + 672c_s^2v_2^2 - 216c_s^4\omega - 132c_s^2 + 82c_s^4\omega^2 - 156v_2^2 - 5c_s^4\omega^3 - 1008c_s^2\omega v_2^2 + 10\omega^3v_2^2) \frac{v_2}{12\omega^3}$$

$$C_{D_y^4 \rho}^{(2), \text{MRT}1} = (12 + 6\omega_{10}^3c_s^2 - 98\omega_{10}^2v_2^2 + 144v_2^4 - 216\omega_{10}v_2^4 - 18\omega_{10} - 78\omega_{10}^2c_s^2 + 10\omega_{10}^3v_2^2 - 216\omega_{10}c_s^4 + 144c_s^4 + 404\omega_{10}^2c_s^2v_2^2 + 82\omega_{10}^2c_s^4 - 9\omega_{10}^3v_2^4 + 198\omega_{10}c_s^2 + 672c_s^2v_2^2 - 1008\omega_{10}c_s^2v_2^2 - 132c_s^2 - 34\omega_{10}^3c_s^2v_2^2 - \omega_{10}^3 - 5\omega_{10}^3c_s^4 + 90\omega_{10}^2v_2^4 + 8\omega_{10}^2 - 156v_2^2 + 234\omega_{10}v_2^2) \frac{v_2}{12\omega_{10}^3}$$

$$C_{D_y^4 \rho}^{(2), \text{MRT}2} = C_{D_y^4 \rho}^{(2), \text{MRT}1}$$

$$C_{D_y^4 \rho}^{(2), \text{CLBM}1} = C_{D_y^4 \rho}^{(2), \text{MRT}1}$$

$$C_{D_y^4 \rho}^{(2), \text{CLBM}2} = C_{D_y^4 \rho}^{(2), \text{MRT}1}$$

$$C_{D_y^4 \rho}^{(2), \text{CuLBM}1} = (12 + 8\omega_5^2 + 90\omega_5^2v_2^4 - \omega_5^3 + 198c_s^2\omega_5 + 144v_2^4 - 34c_s^2\omega_5^3v_2^2 + 234\omega_5v_2^2 - 9\omega_5^3v_2^4 - 78c_s^2\omega_5^2 + 404c_s^2\omega_5^2v_2^2 + 144c_s^4 + 6c_s^2\omega_5^3 + 10\omega_5^2v_2^2 - 1008c_s^2\omega_5v_2^2 - 216c_s^4\omega_5 + 672c_s^2v_2^2 - 18\omega_5 - 132c_s^2 - 5c_s^4\omega_5^3 - 98\omega_5^2v_2^2 - 156v_2^2 - 216\omega_5v_2^4 + 82c_s^4\omega_5^2) \frac{v_2}{12\omega_5^3}$$

$$C_{D_y^4 \rho}^{(2), \text{CuLBM}2} = (808\omega_3c_s^2\omega_1^2v_2^2\omega_2^3 - 80\omega_3c_s^2\omega_1\omega_2^2 - 98\omega_3\omega_1^3v_2^2\omega_2^2 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 48c_s^4\omega_1^2\omega_2^2 - 264\omega_3\omega_1^2v_2^4\omega_2^2 + 760\omega_3c_s^2v_2^2\omega_2^3 - 16\omega_3\omega_1^2\omega_2^2 + 30\omega_3\omega_1^3v_2^2\omega_2^3 - 1088\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 + 320\omega_3c_s^2\omega_1\omega_2^3 + 24c_s^4\omega_1^3\omega_2 + 180\omega_3\omega_1^2v_2^4\omega_2^3 - 52\omega_3c_s^2\omega_1^3 + 16c_s^2\omega_1^2\omega_2^2 + 72\omega_3c_s^4\omega_1\omega_2^2 + 144\omega_3v_2^4\omega_2^3 + 328\omega_3\omega_1v_2^2\omega_2^3 + 8\omega_3\omega_1^2\omega_2 - 184\omega_3c_s^2\omega_2^3 - 3\omega_3\omega_1^3\omega_2^3 + 440\omega_3c_s^2\omega_1^2v_2^2\omega_2 - 28\omega_3\omega_1^3v_2^2 + 96\omega_3\omega_1^2v_2^4\omega_2 - 16c_s^2\omega_1^2v_2^2\omega_2^2 - 372\omega_3c_s^4\omega_1\omega_2^3 - 8c_s^2\omega_1^3\omega_2 + 8\omega_3\omega_1^3\omega_2^2 + 94\omega_3\omega_1^3v_2^2\omega_2 - 176\omega_3\omega_1v_2^2\omega_2^2 + 8c_s^2\omega_1v_2^2\omega_2^3 - 8c_s^2\omega_1\omega_2^3 - 156\omega_3c_s^4\omega_1^3\omega_2 - 27\omega_3\omega_1^3v_2^4\omega_2^3 + 164\omega_3c_s^4\omega_1^2\omega_2^3 + 18\omega_3c_s^2\omega_1^3\omega_2^2 - 80\omega_3c_s^2\omega_1^2\omega_2 + 72\omega_3c_s^4\omega_1^3 + 404\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 - 196\omega_3\omega_1^2v_2^2\omega_2^3 - 120\omega_3c_s^4\omega_1^2\omega_2^2 + 8c_s^2\omega_1^2v_2^2\omega_2 + 90\omega_3\omega_1^3v_2^4\omega_2^2 + 160\omega_3c_s^2\omega_1^3v_2^2 + 24\omega_3\omega_1^3v_2^4 + 280\omega_3\omega_1^2v_2^2\omega_2^2 - 102\omega_3c_s^2\omega_1^3v_2^2\omega_2^2 - 78\omega_3c_s^2\omega_1^3\omega_2^2 + 16\omega_3\omega_2^3 - 104\omega_3\omega_1^2v_2^2\omega_2 - 156\omega_3c_s^2\omega_1^2\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 24c_s^4\omega_1\omega_2^3 - 1472\omega_3c_s^2\omega_1v_2^2\omega_2^3 + 122\omega_3c_s^2\omega_1^3\omega_2 - 84\omega_3\omega_1^3v_2^4\omega_2 + 72\omega_3c_s^4\omega_1^2\omega_2 - 15\omega_3c_s^4\omega_1^3\omega_2^3 + 168\omega_3\omega_1v_2^4\omega_2^2 + 4\omega_3\omega_1^3 + 656\omega_3c_s^2\omega_1v_2^2\omega_2^2 - 28\omega_3\omega_1\omega_2^3 + 152\omega_3c_s^2\omega_1^2\omega_2^2 - 464\omega_3c_s^2\omega_1^3v_2^2\omega_2 - 160\omega_3v_2^2\omega_2^3 - 300\omega_3\omega_1v_2^4\omega_2^3 + 216\omega_3c_s^4\omega_2^3 + 82\omega_3c_s^4\omega_1^3\omega_2^2) \frac{v_2}{36\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_y^4 v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_3^2}:$$

$$C_{D_y^4 v_2}^{(2), \text{SRT}} = (12 + 252c_s^2\omega^2v_2^2 + 54c_s^2\omega - \omega^3 - 29\omega^3v_2^4 + 8\omega^2 + 504v_2^4 + 2c_s^2\omega^3 + 378\omega v_2^2 - 18c_s^2\omega^3v_2^2 - 22c_s^2\omega^2 + 24c_s^4 + 310\omega^2v_2^4 - 756\omega v_2^4 - 18\omega - 154\omega^2v_2^2 + 432c_s^2v_2^2 - 36c_s^4\omega - 36c_s^2 + 14c_s^4\omega^2 - 252v_2^2 - c_s^4\omega^3 - 648c_s^2\omega v_2^2 + 14\omega^3v_2^2) \frac{\rho}{12\omega^3}$$

$$C_{D_y^4 v_2}^{(2), \text{MRT}1} = (12 + 2\omega_{10}^3c_s^2 - 154\omega_{10}^2v_2^2 + 504v_2^4 - 756\omega_{10}v_2^4 - 18\omega_{10} - 22\omega_{10}^2c_s^2 + 14\omega_{10}^3v_2^2 - 36\omega_{10}c_s^4 + 24c_s^4 + 252\omega_{10}^2c_s^2v_2^2 + 14\omega_{10}^2c_s^4 - 29\omega_{10}^3v_2^4 + 54\omega_{10}c_s^2 + 432c_s^2v_2^2 - 648\omega_{10}c_s^2v_2^2 - 36c_s^2 - 18\omega_{10}^3c_s^2v_2^2 - \omega_{10}^3 - \omega_{10}^3c_s^4 + 310\omega_{10}^2v_2^4 + 8\omega_{10}^2 - 252v_2^2 + 378\omega_{10}v_2^2) \frac{\rho}{12\omega_{10}^3}$$

$$C_{D_y^4 v_2}^{(2), \text{MRT}2} = C_{D_y^4 v_2}^{(2), \text{MRT}1}$$

$$C_{D_y^4 v_2}^{(2), \text{CLBM1}} = C_{D_y^4 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(2), \text{CLBM2}} = C_{D_y^4 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(2), \text{CuLBM1}} = (12 + 8\omega_5^2 + 310\omega_5^2 v_4^2 - \omega_5^3 + 54c_s^2 \omega_5 + 504v_4^2 - 18c_s^2 \omega_5^3 v_2^2 + 378\omega_5 v_2^2 - 29\omega_5^3 v_4^2 - 22c_s^2 \omega_5^2 + 252c_s^2 \omega_5^2 v_2^2 + 24c_s^4 + 2c_s^2 \omega_5^3 + 14\omega_5^3 v_2^2 - 648c_s^2 \omega_5 v_2^2 - 36c_s^4 \omega_5 + 432c_s^2 v_2^2 - 18\omega_5 - 36c_s^2 - c_s^4 \omega_5^3 - 154\omega_5^2 v_2^2 - 252v_2^2 - 756\omega_5 v_2^4 + 14c_s^4 \omega_5^2) \frac{\rho}{12\omega_5^3}$$

$$C_{D_y^4 v_2}^{(2), \text{CuLBM2}} = (504\omega_3 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 16\omega_3 c_s^2 \omega_1 \omega_2^2 - 154\omega_3 \omega_1^3 v_2^2 \omega_2^2 - 10\omega_3 \omega_1^3 \omega_2 + 16\omega_3 \omega_1^2 \omega_2^3 - 16c_s^4 \omega_1^2 \omega_2^2 - 888\omega_3 \omega_1^3 v_2^4 \omega_2^2 + 552\omega_3 c_s^2 v_2^2 \omega_2^3 - 16\omega_3 \omega_1^2 \omega_2^2 + 42\omega_3 \omega_1^3 v_2^2 \omega_2^3 - 576\omega_3 c_s^2 \omega_1^2 v_2^2 \omega_2^2 + 96\omega_3 c_s^2 \omega_1 \omega_2^3 + 8c_s^4 \omega_1^3 \omega_2 + 620\omega_3 \omega_1^2 v_2^4 \omega_2^3 - 20\omega_3 c_s^2 \omega_1^3 + 16c_s^2 \omega_1^2 \omega_2^2 + 8\omega_3 c_s^4 \omega_1 \omega_2^2 + 528\omega_3 v_2^4 \omega_2^3 + 552\omega_3 \omega_1 v_2^2 \omega_2^3 + 8\omega_3 \omega_1^3 \omega_2 - 56\omega_3 c_s^2 \omega_2^3 - 3\omega_3 \omega_1^3 \omega_2^3 + 264\omega_3 c_s^2 \omega_1^2 v_2^2 \omega_2 - 60\omega_3 \omega_1^3 v_2^2 + 336\omega_3 \omega_1^2 v_2^2 \omega_2 - 48c_s^2 \omega_1^3 v_2^2 \omega_2^2 - 68\omega_3 c_s^4 \omega_1 \omega_2^3 - 8c_s^2 \omega_1^3 \omega_2 + 8\omega_3 \omega_1^3 \omega_2^2 + 174\omega_3 \omega_1^3 v_2^2 \omega_2 - 240\omega_3 \omega_1 v_2^2 \omega_2^2 + 24c_s^2 \omega_1 v_2^2 \omega_2^3 - 8c_s^2 \omega_1 \omega_2^3 - 32\omega_3 c_s^4 \omega_1^3 \omega_2 - 87\omega_3 \omega_1^3 v_2^4 \omega_2^3 + 28\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 6\omega_3 c_s^2 \omega_1^3 \omega_2^3 - 16\omega_3 c_s^2 \omega_1^2 \omega_2 + 16\omega_3 c_s^4 \omega_1^3 + 252\omega_3 c_s^2 \omega_1^3 v_2^2 \omega_2^2 - 308\omega_3 \omega_1^2 v_2^2 \omega_2^3 - 8\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 24c_s^2 \omega_1^3 v_2^2 \omega_2 + 310\omega_3 \omega_1^3 v_2^4 \omega_2^2 + 144\omega_3 c_s^2 \omega_1^3 v_2^2 + 96\omega_3 \omega_1^3 v_2^4 + 408\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 54\omega_3 c_s^2 \omega_1^3 v_2^2 \omega_2^3 - 22\omega_3 c_s^2 \omega_1^3 \omega_2^2 + 16\omega_3 \omega_2^3 - 168\omega_3 \omega_1^2 v_2^2 \omega_2 - 44\omega_3 c_s^2 \omega_1^2 \omega_2^3 + 8\omega_3 \omega_1 \omega_2^2 + 8c_s^4 \omega_1 \omega_2^3 - 1008\omega_3 c_s^2 \omega_1 v_2^2 \omega_2^3 + 42\omega_3 c_s^2 \omega_1^2 \omega_2 - 312\omega_3 \omega_1^3 v_2^4 \omega_2 + 8\omega_3 c_s^4 \omega_1^2 \omega_2 - 3\omega_3 c_s^4 \omega_1^3 \omega_2^3 + 552\omega_3 \omega_1 v_2^4 \omega_2^2 + 4\omega_3 \omega_1^3 + 336\omega_3 c_s^2 \omega_1 v_2^2 \omega_2^2 - 28\omega_3 \omega_1 \omega_2^3 + 24\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 360\omega_3 c_s^2 \omega_1^3 v_2^2 \omega_2 - 288\omega_3 v_2^2 \omega_2^3 - 1068\omega_3 \omega_1 v_2^4 \omega_2^2 + 40\omega_3 c_s^4 \omega_2^3 + 14\omega_3 c_s^4 \omega_1^3 \omega_2^2) \frac{\rho}{36\omega_3 \omega_1^3 \omega_2^3}$$

$$\text{coefficient } C_{D_x^3 D_z \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x^3 D_z \rho}^{(2), \text{MRT1}} = (-4\omega_6 \omega_{13} \omega_7 \omega_8 v_1^2 \omega_5 \omega_9^2 \omega_{12}^2 + 2\omega_6 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_5^2 \omega_9^2 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 24\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} - 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12\omega_6 \omega_{13} c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} - 4\omega_6 \omega_{13} \omega_7 \omega_{14} v_1^2 \omega_5 \omega_9^2 \omega_{12}^2 + 12\omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_7 \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9^2 \omega_{12} + 9\omega_6 \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 2\omega_6 \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 + 12\omega_6 \omega_{13} c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9 \omega_{12} + 4\omega_6 \omega_{13} \omega_7 v_1^2 \omega_5 \omega_9^2 \omega_{12}^2 - 6\omega_6 \omega_{13} c_s^2 \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 6\omega_6 \omega_{13} \omega_7 c_s^2 \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 12\omega_6 \omega_{13} c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_6 \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9^2 \omega_{12}^2 - 3\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9^2 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_6 \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5 \omega_{12}^2 - 12\omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 6\omega_6 \omega_{13} \omega_7 c_s^2 \omega_8 \omega_5^2 \omega_9^2 \omega_{12} - 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_9 \omega_{12}^2 - 6\omega_6 \omega_{13} c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} + 9\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 8\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} + 4\omega_6 \omega_{13} \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} + 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_9 \omega_{12}^2 - 12c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_8 \omega_5^2 \omega_9^2 \omega_{12} + 4\omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9 \omega_{12}^2 - 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} - 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9 \omega_{12} - 4\omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12}^2 + 6\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 + 3\omega_6 \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 6\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_{12} - 24\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12}^2 + 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_8 \omega_5 \omega_9^2 \omega_{12} + 12\omega_6 \omega_{13} c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_{12} + 4\omega_6 \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} - 4\omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_7 \omega_8 \omega_5 \omega_9^2 \omega_{12} + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} + 4\omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9 \omega_{12} - 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9 \omega_{12} + 4\omega_{13} \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_7 \omega_5 \omega_9^2 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_8 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 6\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_5 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_8 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} + 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_5 \omega_9^2 \omega_{12}^2 - 4\omega_6 \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9 \omega_{12}^2 + 12\omega_6 \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12} + 4\omega_6 \omega_{13} \omega_7 \omega_8 \omega_5 \omega_9^2 \omega_{12} - 12\omega_7 c_s^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_{12}^2 + 6\omega_6 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 8\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9^2 \omega_{12} - 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_8 \omega_5 \omega_9^2 \omega_{12} - 4\omega_6 \omega_{13} \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9^2 \omega_{12} - 4\omega_6 \omega_{13} \omega_7 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} + 4\omega_6 \omega_{13} v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_{14} \omega_8 v_1^2 \omega_5 \omega_9 \omega_{12}^2 - 12\omega_6 \omega_{13} \omega_7 c_s^2 \omega_{14} \omega_5 \omega_9 \omega_{12}^2 - 3\omega_6 \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} + 6\omega_6 \omega_7 c_s^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 v_1^2 \omega_5^2 \omega_9) \frac{v_1 v_2 v_3}{4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2}$$

$$C_{D_x^3 D_z \rho}^{(2), \text{MRT2}} = C_{D_x^3 D_z \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^3 D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(2), \text{CuLBM2}} = (\omega_1 v_3^2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - \omega_2 v_3^2 - 3c_s^2 \omega_2) \frac{v_1 v_2 v_3}{12\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^3 D_z v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_3 D_2 v_2}^{(2), \text{CuLBM2}} = (-18\omega_3\omega_4c_s^2 - 3\omega_3^2\omega_1v_3^2 - 6\omega_3\omega_4\omega_1v_1^2 + 18\omega_4^2c_s^2\omega_1 - 2\omega_3\omega_4^2\omega_1v_3^2 + 18\omega_3\omega_4^2c_s^2 + 6\omega_3^2\omega_4 - 6\omega_3^2\omega_4v_3^2 - 6\omega_4^2v_1^2 - 18\omega_3\omega_4c_s^2\omega_1 - 2\omega_3^2\omega_4\omega_1 + 6\omega_3\omega_4^2v_3^2 + 2\omega_3\omega_4^2\omega_1 + 2\omega_3^2\omega_4\omega_1v_3^2 + 12\omega_3\omega_4v_1^2 + 3\omega_3^2\omega_1v_1^2 + 6\omega_3^2v_3^2 + 3\omega_3^2\omega_1v_3^2 - 6\omega_3^2v_1^2 - 6\omega_3\omega_4^2c_s^2\omega_1 + 6\omega_3\omega_4\omega_1 - 6\omega_4^2\omega_1 -$$

$$C_{D_x^2 D_y D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y D_z \rho}^{(2), \text{CuLBM2}} = & (-252\omega_4 c_s^4 \omega_1^2 \omega_2^3 - 8\omega_3 \omega_2^2 \omega_1^3 v_3^2 - 8\omega_3 \omega_4 c_s^2 \omega_2^2 \omega_2 v_3^2 + 54\omega_3 c_s^2 \omega_1^3 \omega_2^3 + 864\omega_3^2 \omega_4 c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 8\omega_3 \omega_4 c_s^2 \omega_3 \omega_2 - 108\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^3 + \\
& 30\omega_3^2 \omega_4 c_s^4 \omega_1^2 \omega_2^2 - 81\omega_3 \omega_4 c_s^4 \omega_1^3 \omega_2^3 - 176\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 56\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^3 v_3^2 - 60\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2^3 v_3^2 + 324\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 + 432\omega_3^2 \omega_4 c_s^2 \omega_1^2 \omega_2^3 - \\
& 54\omega_4^2 c_s^2 \omega_1^3 \omega_2^3 - 104\omega_3 \omega_2^2 c_s^2 \omega_3^2 - 8\omega_3 \omega_4^2 \omega_1^2 \omega_2 - 64\omega_3 \omega_4 c_s^2 \omega_2^2 \omega_2^2 - 72\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2 + 72\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2^2 + 48\omega_3^2 \omega_4^2 \omega_3^3 v_1^4 - 56\omega_3^2 \omega_4^2 c_s^2 \omega_1 \omega_2^3 v_3^2 - \\
& 24\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2 v_3^2 + 8\omega_3^2 \omega_4^2 \omega_1^3 \omega_2 v_3^2 + 24\omega_4^2 c_s^2 \omega_1^3 \omega_2^2 + 48\omega_3^2 \omega_1^3 v_1^2 v_3^2 + 112\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 \omega_2 + 10\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 27\omega_3^2 \omega_4 c_s^2 \omega_1^3 \omega_2^3 v_3^2 - 104\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 + \\
& 32\omega_3^2 \omega_4 c_s^3 \omega_1^3 v_3^2 + 84\omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 96\omega_3^2 \omega_4 \omega_1 v_1^2 \omega_2^3 - 84\omega_4^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 - 10\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^2 + 324\omega_3 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 - 162\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 - 24\omega_3 \omega_4^2 c_s^4 \omega_1^3 \omega_2 - \\
& 96\omega_3^2 \omega_4 \omega_1 v_1^2 \omega_2^3 v_3^2 + 96\omega_3^2 \omega_4^2 \omega_1^3 v_1^2 \omega_2 + 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 108\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 + 192\omega_3^2 \omega_4^2 c_s^4 \omega_1^2 \omega_2^2 + 27\omega_3 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 + 10\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 v_3^2 - \\
& 72\omega_3^2 \omega_4^2 \omega_1^2 v_1^4 \omega_2 + 162\omega_4^2 c_s^4 \omega_1^3 \omega_2^3 - 96\omega_3^2 \omega_4^2 v_1^2 \omega_2^3 - 60\omega_3^2 \omega_4^2 \omega_1^3 v_1^2 \omega_2 v_3^2 - 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 v_3^2 + 80\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2 + 108\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 + 192\omega_3 \omega_4^2 c_s^4 \omega_1^2 \omega_2^2 - \\
& 27\omega_3 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 v_3^2 + 96\omega_3^2 \omega_4^2 \omega_1 v_1^2 \omega_2^3 - 72\omega_4^2 c_s^4 \omega_1^3 \omega_2^2 + 8\omega_3^2 \omega_4^2 c_s^2 \omega_1 \omega_2^3 v_3^2 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_1^2 \omega_2 - 30\omega_3^2 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1^3 \omega_2 + \\
& 72\omega_3^2 \omega_4^2 v_1^2 \omega_2^3 v_3^2 - 168\omega_3^2 \omega_4^2 c_s^4 \omega_1^3 \omega_2 + 8\omega_3^2 \omega_4^2 \omega_2^3 + 32\omega_3^2 \omega_4^2 c_s^2 \omega_2^3 v_3^2 + 144\omega_3^2 \omega_4^2 c_s^4 \omega_2^3 + 64\omega_3 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 + 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2 v_3^2 - 108\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 - \\
& 192\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2^2 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 - 24\omega_3^2 \omega_4^2 c_s^4 \omega_1 \omega_2^3 - 24\omega_4^2 c_s^2 \omega_1^3 \omega_2^3 v_3^2 + 108\omega_3^2 \omega_4 c_s^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 v_3^2 - 168\omega_3 \omega_4^2 c_s^4 \omega_1 \omega_2^3 - 40\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2 v_3^2 - \\
& 216\omega_3^2 \omega_4^2 c_s^4 \omega_1 \omega_2^2 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 - 10\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 + 81\omega_3^2 \omega_4^2 c_s^4 \omega_1^3 \omega_2^3 + 432\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 v_1^2 - 8\omega_3^2 \omega_4^2 \omega_2^3 v_3^2 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1 v_1^2 \omega_2^2 - \\
& 36\omega_3^2 \omega_4^2 \omega_1^4 \omega_2^3 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_1^2 \omega_2 - 54\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 v_3^2 - 8\omega_3^2 c_s^2 \omega_1^2 \omega_2 v_3^2 + 120\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2^3 v_3^2 + 64\omega_3^2 \omega_4^2 c_s^2 \omega_1 \omega_2^3 + 108\omega_3 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 + \\
& 32\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 v_3^2 - 324\omega_3^2 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^3 + 144\omega_3^2 \omega_4^2 c_s^4 \omega_1^3 + 56\omega_3 \omega_4^2 c_s^2 \omega_1 \omega_2^3 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1 v_1^2 \omega_2^3 - 36\omega_3^2 \omega_4^2 \omega_1^3 v_1^2 \omega_2 + \\
& 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 v_3^2 + 128\omega_3^2 \omega_4^2 c_s^2 \omega_1 \omega_2^2 + 96\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2 - 96\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 - 27\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 24\omega_3^2 \omega_4^2 v_1^4 \omega_2^3 + 54\omega_4^2 c_s^2 \omega_1^3 \omega_2^3 v_3^2) \frac{v_3}{72\omega_3^2 \omega_4^2 \omega_1^3 \omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y D_z v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} :$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y D_z v_1}^{(2), \text{MRT1}} = & (2\omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2 + \omega_7^2 \omega_{14} \omega_8^2 \omega_3 \omega_{12} + 3\omega_7^2 \omega_{14} \omega_8 \omega_5 \omega_{12}^2 - \omega_7 \omega_{14} \omega_8^2 \omega_5^3 \omega_{12} + 2\omega_7^2 \omega_8 \omega_5^3 \omega_{12}^2 - \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2 - \\
& 4\omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12} + 2\omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 + \omega_{14} \omega_8 \omega_5^3 \omega_{12}^2 + \omega_7 \omega_{14} \omega_5^3 \omega_{12}^2 - \omega_7^2 \omega_{14} \omega_8^2 \omega_5^3 + \omega_7 \omega_8^2 \omega_5^3 \omega_{12}^2 - 2\omega_7^2 \omega_8 \omega_5^2 \omega_{12}^2 + 2\omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12} + \omega_7^2 \omega_8^2 \omega_5^3 \omega_{12} - \\
& 2\omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_{12}^2 + \omega_7^2 \omega_{14} \omega_5^2 \omega_{12}^2 + 2\omega_7^2 \omega_{14} \omega_8 \omega_5 \omega_{12} + \omega_7^2 \omega_{14} \omega_8 \omega_5^3 \omega_{12}^2 + 2\omega_7^2 \omega_8^2 \omega_5^2 \omega_{12}^2 - 2\omega_7 \omega_8 \omega_5^3 \omega_{12}^2 - \omega_7^2 \omega_{14} \omega_5^3 \omega_{12}^2 + 2\omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_{12}^2 + \\
& 5\omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12}^2 - 2\omega_7^2 \omega_8^2 \omega_5^2 \omega_{12}^2 - \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2 - 4\omega_7^2 \omega_{14} \omega_8^2 \omega_{12}^2 - 3\omega_7 \omega_{14} \omega_8^2 \omega_5 \omega_{12}^2 - 4\omega_7^2 \omega_{14} \omega_8 \omega_5^2 \omega_{12}^2 - \omega_7^2 \omega_8^2 \omega_5^3 \omega_{12}^2) \frac{c_s^2 \rho v_1 v_3}{\omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2}
\end{aligned}$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{MRT2}} = C_{D_x^2 D_y D_z v_1}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y D_z v_1}^{(2), \text{CuLBM2}} = & (-3\omega_3 \omega_1 \omega_3^3 v_3^2 - 24\omega_3 c_s^2 \omega_1 \omega_2^2 + 10\omega_3 \omega_1^3 \omega_2 - 22\omega_3 \omega_1^2 v_1^2 \omega_2 + 10\omega_3 v_1^2 \omega_2^3 - 20\omega_3 \omega_1^2 \omega_2^2 - 24\omega_3 c_s^2 \omega_1 \omega_2^3 + 4\omega_2^2 \omega_2^2 v_3^2 + 2\omega_1 \omega_2^3 + \\
& 28\omega_3 c_s^2 \omega_1^3 + 12c_s^2 \omega_1^2 \omega_2^2 + 14\omega_3 \omega_1^2 \omega_2 + 26\omega_3 c_s^2 \omega_2^3 - 4\omega_3 \omega_1 \omega_2^2 v_3^2 - 2\omega_1^3 \omega_2 v_3^2 - 6c_s^2 \omega_1^3 \omega_2 - 4\omega_3 \omega_1^2 \omega_2 v_3^2 + 4\omega_3 \omega_1^3 v_3^2 + 26\omega_3 \omega_1^2 v_1^2 \omega_2^2 + 16\omega_3 \omega_1^3 v_1^2 - \\
& 6c_s^2 \omega_1 \omega_2^3 - 30\omega_3 c_s^2 \omega_1^2 \omega_2 + 6\omega_3 \omega_1^2 \omega_2^2 v_3^2 - 13\omega_3 \omega_1 v_1^2 \omega_2^3 - 2\omega_1 \omega_2^3 v_3^2 - 4\omega_3 \omega_1 v_1^2 \omega_2^3 - 13\omega_3 \omega_2^3 v_1^2 \omega_2 + 4\omega_3 \omega_2^2 v_3^2 - 10\omega_3 \omega_2^2 - 3\omega_3 \omega_1^2 \omega_2 v_3^2 + \\
& 8\omega_3 \omega_1 \omega_2^2 - 24\omega_3 c_s^2 \omega_1^3 \omega_2 + 2\omega_1^3 \omega_2 - 12\omega_3 \omega_1^3 + 10\omega_3 \omega_1 \omega_2^3 + 48\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_1^2 \omega_2^2) \frac{\rho v_1 v_3}{6\omega_3 \omega_1^3 \omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y D_z v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} :$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y D_z v_2}^{(2), \text{MRT1}} = & (4\omega_6 \omega_{16} \omega_{10}^2 \omega_2^2 \omega_{17} \omega_8^2 \omega_5^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 4\omega_6 \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5 \omega_{15}^2 - \\
& 4\omega_6 \omega_{16} \omega_{10}^2 \omega_8^2 \omega_5^3 \omega_{15}^2 - 2\omega_{16} \omega_{10}^2 \omega_2^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 5\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15} + \\
& 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 2\omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 - 8\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + \\
& 2\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 10\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + \\
& 2\omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5 \omega_{15}^2 - 2\omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15}^2 + \\
& 12\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5 \omega_{15}^2 + 2\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 2\omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 + \\
& 4\omega_6 \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 5\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + \\
& 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 + 6\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8 \omega_5 \omega_{15}^2 - 4\omega_6 \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} - \\
& 2\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_{15}^2 - 2\omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 4\omega_6 \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 8\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 8\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5 \omega_{15}^2 + \\
& 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} - 8\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - \\
& 8\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 8\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 2\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - \\
& 8\omega_6 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2) \frac{c_s^2 \rho v_2 v_3}{2\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2}
\end{aligned}$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{MRT2}} = C_{D_x^2 D_y D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{CLBM1}} = 0$$

[illegible]

$$6\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2\omega_{18} - 24\omega_6\omega_{19}^2\omega_7c_s^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18} + 12\omega_6^2\omega_{19}^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2v_3^2\omega_{18} - 12\omega_6\omega_{19}^2\omega_7c_s^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2) \frac{\rho v_2 v_3}{12\omega_6^2\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18}}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{MRT}^2} = C_{D_x D_z^3 v_1}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CLBM}^1} = (3c_s^2\omega_{11}\omega_{18} - 9c_s^2\omega_{11} + v_3^2\omega_{18} + 3\omega_{11} - 3\omega_{11}v_3^2 - \omega_{18} - \omega_{11}\omega_{18} + 3c_s^2\omega_{18} + \omega_{11}v_3^2\omega_{18}) \frac{\rho v_2 v_3}{12\omega_{11}\omega_{18}}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CLBM}^2} = C_{D_x D_z^3 v_1}^{(2), \text{CLBM}^1}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CuLBM}^1} = (3\omega_6 + 3c_s^2\omega_8 + 3\omega_6c_s^2\omega_8 - \omega_6\omega_8 + \omega_6\omega_8v_3^2 + \omega_8v_3^2 - 9\omega_6c_s^2 - \omega_8 - 3\omega_6v_3^2) \frac{\rho v_2 v_3}{12\omega_6\omega_8}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CuLBM}^2} = (18\omega_3\omega_4\omega_1v_1^2 + 4\omega_3\omega_4\omega_2v_3^2 + 6\omega_3\omega_4c_s^2\omega_2 + 18\omega_3\omega_4c_s^2\omega_1\omega_2 + 9\omega_4\omega_1\omega_2 + 12\omega_3\omega_4c_s^2\omega_1 - 18\omega_3\omega_4v_1^2\omega_2 - 27\omega_4c_s^2\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_4\omega_1\omega_2v_3^2 - 9\omega_3\omega_1\omega_2v_3^2 + 9\omega_3\omega_1\omega_2 + 6\omega_3\omega_4\omega_1\omega_2v_3^2 + 2\omega_3\omega_4\omega_1v_3^2 + 2\omega_3\omega_4\omega_2) \frac{\rho v_2 v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_z^3 v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{MRT}^1} = (\omega_{19}^2\omega_{19}^2\omega_{20}\omega_8^2\omega_5v_3^2 - \omega_{19}^2\omega_7\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2\omega_7^3c_s^2\omega_8\omega_5^2 - 2\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2 - 8\omega_{19}^2c_s^2\omega_{20}\omega_8^2\omega_5^2 + 5\omega_{19}^2\omega_7^3c_s^2\omega_{20}\omega_8\omega_5^2 + 2\omega_{19}^2\omega_7^3c_s^2\omega_{20}\omega_8 - \omega_{19}^2\omega_7^3\omega_{20}\omega_8\omega_5v_3^2 - \omega_{19}^2\omega_7^3\omega_{20}\omega_8\omega_5^2 + \omega_{19}^2\omega_7^3\omega_8^2\omega_5^2v_3^2 + 13\omega_{19}^2\omega_7c_s^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2 - \omega_{19}^2\omega_7^2\omega_{20}\omega_8\omega_5^2v_3^2 - \omega_{19}^2\omega_7^2\omega_{20}\omega_8\omega_5^2 - 5\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2\omega_7^2\omega_8\omega_5v_3^2 + 2\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2\omega_7\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8\omega_5^2 - 2\omega_{19}^2\omega_7^2\omega_8\omega_5^2 + 2\omega_{19}^2\omega_7^2\omega_8\omega_5^2v_3^2 - 2\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2\omega_5^2 + 4\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2\omega_5^2 + 4\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8\omega_5^2 - \omega_{19}^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2v_3^2 + 7\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2\omega_5^2 + \omega_{19}^2\omega_{20}\omega_8^2\omega_5^2v_3^2 + 2\omega_{19}^2\omega_7^2c_s^2\omega_8\omega_5^2 - 7\omega_{19}^2\omega_7^3c_s^2\omega_{20}\omega_8\omega_5 - 2\omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5v_3^2 + \omega_{19}^2\omega_7^3\omega_{20}\omega_8\omega_5 - 6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_8^2\omega_5 - \omega_{19}^2\omega_7^3\omega_8^2\omega_5^2 - 2\omega_{19}^2\omega_7^2\omega_8^2\omega_5^2v_3^2 + \omega_{19}^2\omega_7^2\omega_{20}\omega_8\omega_5^2 - 2\omega_{19}^2\omega_7c_s^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2\omega_7^3c_s^2\omega_8\omega_5 + 4\omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2v_3^2 - 2\omega_{19}^2\omega_{20}\omega_8^2\omega_5^2v_3^2 - 2\omega_{19}^2\omega_7^2c_s^2\omega_8\omega_5^2 + 2\omega_{19}^2\omega_7^2\omega_8\omega_5^2 + \omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2\omega_7^3\omega_8\omega_5^2v_3^2 + 2\omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + \omega_{19}^2\omega_7\omega_{20}\omega_8^2\omega_5^2v_3^2 - \omega_{19}^2\omega_7^3c_s^2\omega_8\omega_5^2 + 2\omega_{19}^2\omega_7^2\omega_8^2\omega_5^2 + \omega_{19}^2\omega_7^3c_s^2\omega_{20}\omega_8\omega_5 - \omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5 - \omega_{19}^2\omega_7\omega_{20}\omega_8^2\omega_5^2v_3^2 + \omega_{19}^2\omega_7^3c_s^2\omega_8\omega_5^2 + \omega_{19}^2\omega_7^2\omega_{20}\omega_8\omega_5^2v_3^2 + \omega_{19}^2\omega_7^3\omega_8\omega_5^2 - 2\omega_{19}^2\omega_7^3\omega_8\omega_5) \frac{\rho v_1 v_3}{2\omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2}$$

$$C_{D_x D_z^3 v_2}^{(2), \text{MRT}^2} = C_{D_x D_z^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CuLBM}^2} = (-18\omega_3^2\omega_4c_s^2 + 3\omega_3^2\omega_1v_3^2 + 18\omega_4^2c_s^2\omega_1 + 18\omega_3\omega_4^2c_s^2 + 6\omega_3^2\omega_4 - 6\omega_4^2v_1^2 - 18\omega_3\omega_4c_s^2\omega_1 - 2\omega_3^2\omega_4\omega_1 + 2\omega_3\omega_4^2\omega_1 + 3\omega_4^2\omega_1v_1^2 - 6\omega_3^2v_3^2 + 3\omega_4^2\omega_1v_3^2 + 6\omega_3^2v_1^2 - 6\omega_3\omega_4^2c_s^2\omega_1 + 2\omega_3^2\omega_4\omega_1v_1^2 + 12\omega_3\omega_4v_3^2 + 6\omega_3\omega_4^2v_1^2 + 6\omega_3\omega_4\omega_1 - 6\omega_4^2\omega_1 - 12\omega_3\omega_4 + 12\omega_4^2 - 6\omega_4^2v_3^2 - 6\omega_3^2\omega_4v_1^2 + 36\omega_3\omega_4c_s^2 + 6\omega_3^2\omega_4c_s^2\omega_1 - 6\omega_3\omega_4^2 - 2\omega_3\omega_4^2\omega_1v_1^2 - 6\omega_3\omega_4\omega_1v_3^2 - 3\omega_3^2\omega_1v_1^2 - 36\omega_4^2c_s^2) \frac{\rho v_1 v_3}{8\omega_3^2\omega_4^2\omega_1}$$

$$\text{coefficient } C_{D_x D_z^3 v_3}^{(2)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_3}^{(2), \text{MRT}^1} = (4\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5 + 12\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5v_3^2\omega_{18} - 12\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_5v_3^2\omega_{18} + 4\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5 - 2\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{11}\omega_8\omega_{18} + 12\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} - 6\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_8\omega_5v_3^2\omega_{18} - 4\omega_6\omega_{19}^2\omega_7^2\omega_{11}^2\omega_{18} - 3\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5 - 4\omega_6\omega_{19}^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 4\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 2\omega_6\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 2\omega_6\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 3\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 4\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_{18} - 2\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18} - 24\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} - 4\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_8\omega_5\omega_{18} + 2\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}^2\omega_{18} - 2\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5 + 2\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{11}\omega_8\omega_5\omega_{18} + 12\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5v_3^2 - 4\omega_6\omega_{19}^2\omega_7c_s^2\omega_{20}\omega_{11}\omega_5\omega_{18} - 4\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{18} + 4\omega_6\omega_{19}^2\omega_7^2\omega_{11}\omega_5\omega_{18} + 12\omega_6\omega_{19}^2\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} - 9\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5v_3^2 + 12\omega_6\omega_{19}^2\omega_7^2\omega_{11}^2v_3^2\omega_{18} + 4\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_{18} - 4\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{11}\omega_5\omega_{18} - 2\omega_6\omega_{19}\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_{18} + 4\omega_{19}^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5 + 4\omega_6\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 12\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5v_3^2 + 4\omega_6\omega_{19}^2\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_5\omega_{18} - 4\omega_6\omega_{19}^2\omega_7c_s^2\omega_{11}\omega_8\omega_5\omega_{18} + 12\omega_6\omega_{19}\omega_7^2\omega_{20}\omega_{11}\omega_5v_3^2\omega_{18} + 12\omega_6\omega_{19}\omega_7^2\omega_{20}\omega_8\omega_5v_3^2\omega_{18} - 4\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_{18} + 12\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_5v_3^2\omega_{18} + 4\omega_6\omega_{19}\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5 + 6\omega_6\omega_{19}\omega_{20}\omega_{11}\omega_8\omega_5v_3^2\omega_{18} + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} + 4\omega_6\omega_{19}\omega_7c_s^2\omega_{11}\omega_5\omega_{18} + 4\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18} - 4\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5 + 6\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8v_3^2 - 4\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8\omega_{18} + 4\omega_6\omega_{19}\omega_7c_s^2\omega_{20}\omega_8\omega_5\omega_{18} + 4\omega_6\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_5\omega_{18} - 4\omega_6\omega_{19}\omega_7\omega_{11}^2\omega_8\omega_5\omega_{18} - 4\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 4\omega_6\omega_{19}\omega_7c_s^2\omega_{11}\omega_8\omega_5\omega_{18} +$$

$$C_{D_z^4 v_3}^{(2), \text{CuLBM1}} = (72\omega_3\omega_{10}c_s^2v_3^2 + 108\omega_3^3c_s^2v_3^2 + 12\omega_3^2\omega_{10}^2v_3^2 - 6\omega_3^3\omega_{10}c_s^2 - 36\omega_3^3v_3^2 - 3\omega_3^3\omega_{10}c_s^4 + 72\omega_3^2\omega_{10}v_3^4 + 6\omega_3^3\omega_{10}^2c_s^2v_3^2 - 8\omega_3^2\omega_{10}^2c_s^2 - 12\omega_3^3\omega_{10}^2c_s^2v_3^2 - 48\omega_3\omega_{10}^2c_s^4 + 30\omega_3^3\omega_{10}v_3^2 - 24\omega_3\omega_{10}c_s^2 + 3\omega_3^3\omega_{10}^2v_3^4 - 24\omega_3^2\omega_{10}c_s^4 + 72\omega_3^2v_3^2 + 12\omega_3\omega_{10}^2c_s^2 + 24\omega_{10}^2c_s^4 - 30\omega_3^3\omega_{10}v_3^4 + 24\omega_3^3\omega_{10}^2c_s^4 + 144\omega_3^2\omega_{10}^2c_s^2v_3^2 - 72\omega_3^2v_3^4 + 24\omega_3^3\omega_{10}c_s^2 + 24\omega_3\omega_{10}c_s^4 - 216\omega_3^2c_s^2v_3^2 - 3\omega_3^3\omega_{10}^2v_3^2 + 6\omega_3^3\omega_{10}c_s^4 - 36\omega_3\omega_{10}^2c_s^2v_3^2 - 12\omega_3^2\omega_{10}^2v_3^4 - 72\omega_3^3\omega_{10}v_3^2 - 72\omega_3^3\omega_{10}^2c_s^2v_3^2 + 36\omega_3^3v_3^4 + \omega_3^3\omega_{10}^2c_s^2) \frac{\rho}{24\omega_3^3\omega_{10}^2}$$

$$C_{D_z^4 v_3}^{(2), \text{CuLBM2}} = (-3\omega_3^2\omega_4^2\omega_1^2v_3^2 - 12\omega_3^2\omega_4c_s^4\omega_1^2 + 36\omega_3\omega_4\omega_1^2v_3^2 + 36\omega_3\omega_4\omega_1^2v_3^4 - 12\omega_3^2\omega_4^2c_s^2\omega_1^2v_3^2 + 12\omega_3^2\omega_4^2c_s^2\omega_1 - 15\omega_3^2\omega_4\omega_1^3v_3^4 + 12\omega_3\omega_4^2c_s^4\omega_1 + 72\omega_3\omega_4^2c_s^2\omega_1^2v_3^2 + 27\omega_3^2c_s^2\omega_1^2v_3^2 + 3\omega_3^2\omega_4c_s^4\omega_1^3 + 24\omega_3^2\omega_4^2c_s^4 + 27\omega_1^2c_s^2\omega_1^3v_3^2 - 9\omega_1^2\omega_1^3v_3^2 - 18\omega_3^2\omega_1^2v_3^4 + \omega_3^2\omega_1^2c_s^2\omega_1^3 + 6\omega_3^2\omega_4^2c_s^2\omega_1^3v_3^2 + 36\omega_3^2\omega_4\omega_1^2v_3^4 - 15\omega_3\omega_4^2\omega_1^3v_3^4 - 12\omega_3\omega_4^2c_s^4\omega_1^2 - 18\omega_3\omega_4\omega_1^3v_3^2 + 12\omega_3^2\omega_4^2\omega_1^2v_3^2 - 54\omega_1^2c_s^2\omega_1^2v_3^2 + 9\omega_3^2\omega_1^3v_3^4 + 18\omega_4^2\omega_1^2v_3^2 + 36\omega_3^2\omega_4c_s^2\omega_1^2v_3^2 - 8\omega_3^2\omega_4^2c_s^2\omega_1^2 + 12\omega_3^2\omega_4c_s^4\omega_1 - 36\omega_3\omega_4^2c_s^2\omega_1^3v_3^2 - 54\omega_3^2c_s^2\omega_1^2v_3^2 + 3\omega_3\omega_4^2c_s^4\omega_1^3 + 72\omega_3^2\omega_4c_s^2\omega_1^2v_3^2 + 18\omega_3\omega_4\omega_1^3v_3^4 - 12\omega_3\omega_4^2c_s^2\omega_1 - 12\omega_3^2\omega_4\omega_1^2v_3^4 - 3\omega_3^2\omega_4c_s^2\omega_1^3 - 36\omega_3^2\omega_4\omega_1^2v_3^2 + 15\omega_3\omega_4\omega_1^3v_3^2 + 12\omega_3^2\omega_4^2\omega_1^2 - 108\omega_3\omega_4c_s^2\omega_1^2v_3^2 - 18\omega_4^2\omega_1^2v_3^4 - 9\omega_3^2\omega_1^3v_3^2 - 48\omega_3^2\omega_4^2c_s^4\omega_1 - 36\omega_3\omega_4^2\omega_1^2v_3^2 + 36\omega_3\omega_4^2c_s^2\omega_1^2v_3^2 + 15\omega_3^2\omega_4\omega_1^3v_3^2 + 24\omega_3^2\omega_4^2c_s^4\omega_1^2 - 12\omega_3^2\omega_4c_s^2\omega_1 + 3\omega_3^2\omega_4\omega_1^3v_3^4 - 3\omega_3\omega_4^2c_s^2\omega_1^3 - 36\omega_3^2\omega_4c_s^2\omega_1^2v_3^2 - 36\omega_3\omega_4\omega_1^2v_3^4 - 3\omega_3^2\omega_4^2c_s^4\omega_1^3 + 54\omega_3\omega_4^2c_s^2\omega_1^3v_3^2 + 18\omega_3^2\omega_1^2v_3^2 + 9\omega_4^2\omega_1^3v_3^4 + 12\omega_3\omega_4^2c_s^2\omega_1^2 - 36\omega_3^2\omega_4^2c_s^2\omega_1^2v_3^2) \frac{\rho}{24\omega_3^3\omega_4^2\omega_1^3}$$

coefficient $C_{D_z^4 v_3}^{(2)}$ at $\frac{\partial^4 v_3}{\partial x_3^4}$:

$$C_{D_z^4 v_3}^{(2), \text{SRT}} = (-4 - 3c_s^2\omega - 5\omega v_3^2 + 2\omega + 6c_s^2 + 10v_3^2) \frac{\rho v_2 v_3}{12\omega}$$

$$C_{D_z^4 v_3}^{(2), \text{MRT1}} = (72\omega_{19}^2\omega_7c_s^2 - 120\omega_{19}^2\omega_7c_s^2\omega_{11} + 24\omega_7\omega_{11}^2 + 61\omega_{19}^2\omega_7\omega_{11}v_3^2 + 2\omega_{19}^2\omega_7^2\omega_{11}^2 + 24\omega_7^2\omega_{11}^2v_3^2 - 33\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 72\omega_{19}\omega_7\omega_{11}^2 - 60\omega_{19}c_s^2\omega_{11}^2 + 24\omega_{19}\omega_7\omega_{11} - 72\omega_{19}\omega_7\omega_{11}v_3^2 + 12\omega_{19}^2\omega_7v_3^2 - 36\omega_{19}^2\omega_{11} + 84\omega_{19}\omega_{11}v_3^2 + 12\omega_{19}\omega_7^2c_s^2\omega_{11} - 51\omega_{19}\omega_7^2\omega_{11}^2v_3^2 - 25\omega_{19}^2\omega_{11}^2 + 24\omega_7^2c_s^2\omega_{11}^2 - 84\omega_{19}\omega_{11}^2v_3^2 + 60\omega_{19}^2c_s^2\omega_{11} + 72\omega_{19}^2\omega_7\omega_{11} + 36\omega_{19}\omega_7^2\omega_{11}v_3^2 - 24\omega_{19}\omega_7c_s^2\omega_{11} - 60\omega_{19}^2\omega_7^2v_3^2 - 48\omega_7c_s^2\omega_{11}^2 + 168\omega_{19}\omega_7\omega_{11}^2v_3^2 - 12\omega_{19}\omega_7^2\omega_{11} + 24\omega_{19}^2\omega_7 - 3\omega_{19}^2\omega_7^2c_s^2\omega_{11} - 48\omega_{19}\omega_7 + 39\omega_{19}^2\omega_7^2c_s^2\omega_{11} + 21\omega_{19}\omega_7^2\omega_{11} + 36\omega_{19}\omega_{11} - 168\omega_{19}^2\omega_7\omega_{11}v_3^2 + 120\omega_{19}\omega_7c_s^2\omega_{11}^2 - 48\omega_7\omega_{11}^2v_3^2 - 36\omega_{19}^2\omega_7^2c_s^2 - 5\omega_{19}^2\omega_7^2\omega_{11}^2v_3^2 - 12\omega_7^2\omega_{11}^2) \frac{\rho v_2^2 v_3}{12\omega_{19}^2\omega_7^2\omega_{11}^2}$$

$$C_{D_z^4 v_3}^{(2), \text{MRT2}} = C_{D_z^4 v_3}^{(2), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(2), \text{CLBM1}} = (-4 - 3c_s^2\omega_{11} + 2\omega_{11} - 5\omega_{11}v_3^2 + 6c_s^2 + 10v_3^2) \frac{\rho v_2 v_3}{12\omega_{11}}$$

$$C_{D_z^4 v_3}^{(2), \text{CLBM2}} = C_{D_z^4 v_3}^{(2), \text{CLBM1}}$$

$$C_{D_z^4 v_3}^{(2), \text{CuLBM1}} = (-4 + 2\omega_6 - 3\omega_6c_s^2 + 6c_s^2 - 5\omega_6v_3^2 + 10v_3^2) \frac{\rho v_2 v_3}{12\omega_6}$$

$$C_{D_z^4 v_3}^{(2), \text{CuLBM2}} = (10\omega_1v_3^2 - 15\omega_1\omega_2v_3^2 + 6\omega_1\omega_2 - 4\omega_1 + 6c_s^2\omega_1 - 8\omega_2 + 20\omega_2v_3^2 + 12c_s^2\omega_2 - 9c_s^2\omega_1\omega_2) \frac{\rho v_2 v_3}{36\omega_1\omega_2}$$

3.4 Conservation of momentum: ρv_3

$$\begin{aligned} & v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + v_1 v_3 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \rho v_3 \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \rho v_1 \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_1} + v_2 v_3 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \rho v_3 \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \rho v_2 \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\ & 2\rho v_3 \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + C_{D_x \rho, D_x v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + C_{D_x \rho, D_z v_1}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + C_{D_x v_1, D_z v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + C_{D_y \rho, D_y v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + \\ & C_{D_y \rho, D_z v_2}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + C_{D_y v_2, D_z v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + C_{D_z \rho, D_x v_1}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + C_{D_z \rho, D_y v_2}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + \\ & C_{D_z \rho, D_z v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + C_{D_z v_3, D_z v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + C_{D_z^2 v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + C_{D_y^2 v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + C_{D_x D_z \rho}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + \\ & C_{D_x D_z v_1}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + C_{D_y D_z \rho}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + C_{D_y D_z v_2}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + C_{D_z^2 \rho}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + C_{D_z^2 v_3}^{(3)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + C_{D_x^2 \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1^2} + \\ & C_{D_x^2 v_1}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1^2} + C_{D_x^2 v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1^2} + C_{D_x D_y v_2}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_{D_x^2 D_y v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} + C_{D_x D_z^2 v_1}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & C_{D_x D_y^2 v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + C_{D_y^2 \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + C_{D_y^2 v_2}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + C_{D_y^2 v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_2^2} + C_{D_x^2 D_z \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + C_{D_x^2 D_z v_1}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\ & C_{D_x^2 D_z v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + C_{D_x D_y D_z \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{D_x D_y D_z v_1}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{D_x D_y D_z v_2}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\ & C_{D_y^2 D_z \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z v_2}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_{D_x D_z^2 \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + C_{D_x D_z^2 v_1}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\ & C_{D_x D_z^2 v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{D_y D_z^2 \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + C_{D_y D_z^2 v_2}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{D_y D_z^2 v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{D_z^3 \rho}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\ & C_{D_z^3 v_3}^{(3)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{D_x^4 \rho}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{D_x^4 v_1}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{D_x^4 v_3}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + C_{D_x^3 D_y \rho}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{D_x^3 D_y v_1}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\ & C_{D_x^3 D_y v_2}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{D_x^3 D_y v_3}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_2} + C_{D_x^2 D_y^2 \rho}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_1}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_2}^{(4)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \end{aligned}$$

$$\begin{aligned}
& C_{D_x^2 D_y^3 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + C_{D_x D_y^3 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^3} + \\
& C_{D_y^4 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{D_y^4 v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_{D_y^4 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^4} + C_{D_x^3 D_z \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{D_x^2 D_y D_z \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{D_x D_y^2 D_z \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{D_y^3 D_z \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_x^2 D_z \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& C_{D_x^2 D_z v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{D_x D_y D_z^2 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{D_x D_y D_z^2 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_y^2 D_z^2 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{D_x D_z^3 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + \\
& C_{D_x D_z^3 v_1}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{D_y D_z^3 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_2}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& C_{D_x^2 \rho}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{D_x^2 v_3}^{(3)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

coefficient $C_{D_x \rho, D_x v_3}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1}$:

$$\begin{aligned}
C_{D_x \rho, D_x v_3}^{(3), \text{SRT}} &= (-2 + \omega) \frac{c_s^2}{2\omega} \\
C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}} &= (-2 + \omega_6) \frac{c_s^2}{2\omega_6} \\
C_{D_x \rho, D_x v_3}^{(3), \text{MRT2}} &= C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}} \\
C_{D_x \rho, D_x v_3}^{(3), \text{CLBM1}} &= C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}} \\
C_{D_x \rho, D_x v_3}^{(3), \text{CLBM2}} &= C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}} \\
C_{D_x \rho, D_x v_3}^{(3), \text{CuLBM1}} &= (-2 + \omega_2) \frac{c_s^2}{2\omega_2} \\
C_{D_x \rho, D_x v_3}^{(3), \text{CuLBM2}} &= (-2 + \omega_1) \frac{c_s^2}{2\omega_1}
\end{aligned}$$

coefficient $C_{D_x \rho, D_z v_1}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3}$:

$$\begin{aligned}
C_{D_x \rho, D_z v_1}^{(3), \text{SRT}} &= (-2 + \omega) \frac{c_s^2}{2\omega} \\
C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}} &= (-2 + \omega_6) \frac{c_s^2}{2\omega_6} \\
C_{D_x \rho, D_z v_1}^{(3), \text{MRT2}} &= C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}} \\
C_{D_x \rho, D_z v_1}^{(3), \text{CLBM1}} &= C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}} \\
C_{D_x \rho, D_z v_1}^{(3), \text{CLBM2}} &= C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}} \\
C_{D_x \rho, D_z v_1}^{(3), \text{CuLBM1}} &= (-2 + \omega_2) \frac{c_s^2}{2\omega_2} \\
C_{D_x \rho, D_z v_1}^{(3), \text{CuLBM2}} &= (-2\omega_1 - 6v_1^2\omega_2 + 6c_s^2\omega_1 + 2\omega_2 - 12c_s^2\omega_2 + 3c_s^2\omega_1\omega_2 + 6\omega_1v_1^2) \frac{1}{6\omega_1\omega_2}
\end{aligned}$$

coefficient $C_{D_x v_1, D_z v_1}^{(3)}$ **at** $\frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_3}$:

$$\begin{aligned}
C_{D_x v_1, D_z v_1}^{(3), \text{SRT}} &= 0 \\
C_{D_x v_1, D_z v_1}^{(3), \text{MRT1}} &= 0 \\
C_{D_x v_1, D_z v_1}^{(3), \text{MRT2}} &= 0
\end{aligned}$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2\rho v_1}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_y v_3}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2}$:

$$C_{D_y \rho, D_y v_3}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{MRT2}} = C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CLBM1}} = C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CLBM2}} = C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_y \rho, D_z v_2}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_y \rho, D_z v_2}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{MRT2}} = C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CLBM1}} = C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CLBM2}} = C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CuLBM2}} = (6\omega_1 v_2^2 - 6v_2^2 \omega_2 - 2\omega_1 + 6c_s^2 \omega_1 + 2\omega_2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{1}{6\omega_1 \omega_2}$$

coefficient $C_{D_y v_2, D_z v_2}^{(3)}$ **at** $\frac{\partial v_2}{\partial x_2} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_y v_2, D_z v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{MRT1}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{MRT2}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2\rho v_2}{\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_x v_1}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_z \rho, D_x v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{MRT1}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{MRT2}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CuLBM2}} = (-\omega_1 - 3v_1^2 \omega_2 + c_s^2 \omega_1 + \omega_2 - c_s^2 \omega_2 + 3\omega_1 v_1^2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_y v_2}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_z \rho, D_y v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{MRT1}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{MRT2}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CuLBM2}} = (3\omega_1 v_2^2 - 3v_2^2 \omega_2 - \omega_1 + c_s^2 \omega_1 + \omega_2 - c_s^2 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_z v_3}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_z \rho, D_z v_3}^{(3), \text{SRT}} = (-2 - 2c_s^2 \omega - 3\omega v_3^2 + \omega + 4c_s^2 + 6v_3^2) \frac{1}{\omega}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}} = (-2 - 2c_s^2 \omega_{11} + \omega_{11} - 3\omega_{11} v_3^2 + 4c_s^2 + 6v_3^2) \frac{1}{\omega_{11}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{MRT2}} = C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CLBM1}} = C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CLBM2}} = C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_6 - 2\omega_6 c_s^2 + 4c_s^2 - 3\omega_6 v_3^2 + 6v_3^2) \frac{1}{\omega_6}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CuLBM2}} = (6\omega_1 v_3^2 - 9\omega_1 \omega_2 v_3^2 + 3\omega_1 \omega_2 - 2\omega_1 + 4c_s^2 \omega_1 - 4\omega_2 + 12\omega_2 v_3^2 + 8c_s^2 \omega_2 - 6c_s^2 \omega_1 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_z v_3, D_z v_3}^{(3)}$ **at** $\left(\frac{\partial v_3}{\partial x_3}\right)^2$:

$$C_{D_z v_3, D_z v_3}^{(3), \text{SRT}} = (2 - \omega) \frac{3\rho v_3}{\omega}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}} = (2 - \omega_{11}) \frac{3\rho v_3}{\omega_{11}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{MRT2}} = C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CLBM1}} = C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CLBM2}} = C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CuLBM1}} = (2 - \omega_6) \frac{3\rho v_3}{\omega_6}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CuLBM2}} = (-3\omega_1\omega_2 + 2\omega_1 + 4\omega_2) \frac{\rho v_3}{\omega_1\omega_2}$$

coefficient $C_{D_x^2 v_3}^{(3)}$ **at** $\frac{\partial^2 v_3}{\partial x_1^2}$:

$$C_{D_x^2 v_3}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x^2 v_3}^{(3), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_x^2 v_3}^{(3), \text{MRT2}} = C_{D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 v_3}^{(3), \text{CLBM1}} = C_{D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 v_3}^{(3), \text{CLBM2}} = C_{D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_x^2 v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_y^2 v_3}^{(3)}$ **at** $\frac{\partial^2 v_3}{\partial x_2^2}$:

$$C_{D_y^2 v_3}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y^2 v_3}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_y^2 v_3}^{(3), \text{MRT2}} = C_{D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 v_3}^{(3), \text{CLBM1}} = C_{D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 v_3}^{(3), \text{CLBM2}} = C_{D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_y^2 v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_x D_z \rho}^{(3)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{MRT1}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{MRT2}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CuLBM2}} = (-\omega_1 - v_1^2 \omega_2 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2 + \omega_1 v_1^2) \frac{v_1}{3\omega_1 \omega_2}$$

coefficient $C_{D_x D_z v_1}^{(3)}$ **at** $\frac{\partial^2 v_1}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z v_1}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_z v_1}^{(3), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_x D_z v_1}^{(3), \text{MRT}2} = C_{D_x D_z v_1}^{(3), \text{MRT}1}$$

$$C_{D_x D_z v_1}^{(3), \text{CLBM}1} = C_{D_x D_z v_1}^{(3), \text{MRT}1}$$

$$C_{D_x D_z v_1}^{(3), \text{CLBM}2} = C_{D_x D_z v_1}^{(3), \text{MRT}1}$$

$$C_{D_x D_z v_1}^{(3), \text{CuLBM}1} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_x D_z v_1}^{(3), \text{CuLBM}2} = (-2\omega_1 - 6v_1^2\omega_2 + 2c_s^2\omega_1 + 2\omega_2 - 8c_s^2\omega_2 + 3c_s^2\omega_1\omega_2 + 6\omega_1v_1^2) \frac{\rho}{6\omega_1\omega_2}$$

coefficient $C_{D_y D_z \rho}^{(3)}$ **at** $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{MRT}1} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{MRT}2} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CLBM}1} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CLBM}2} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CuLBM}1} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CuLBM}2} = (\omega_1 v_2^2 - v_2^2 \omega_2 - \omega_1 + 3c_s^2 \omega_1 + \omega_2 - 3c_s^2 \omega_2) \frac{v_2}{3\omega_1 \omega_2}$$

coefficient $C_{D_y D_z v_2}^{(3)}$ **at** $\frac{\partial^2 v_2}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z v_2}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y D_z v_2}^{(3), \text{MRT}1} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_y D_z v_2}^{(3), \text{MRT}2} = C_{D_y D_z v_2}^{(3), \text{MRT}1}$$

$$C_{D_y D_z v_2}^{(3), \text{CLBM}1} = C_{D_y D_z v_2}^{(3), \text{MRT}1}$$

$$C_{D_y D_z v_2}^{(3), \text{CLBM}2} = C_{D_y D_z v_2}^{(3), \text{MRT}1}$$

$$C_{D_y D_z v_2}^{(3), \text{CuLBM}1} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_2}^{(3), \text{CuLBM}2} = (6\omega_1 v_2^2 - 6v_2^2 \omega_2 - 2\omega_1 + 2c_s^2 \omega_1 + 2\omega_2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_z^2 \rho}^{(3)}$ **at** $\frac{\partial^2 \rho}{\partial x_3^2}$:

$$C_{D_z^2 \rho}^{(3), \text{SRT}} = (-2 - 3c_s^2 \omega - \omega v_3^2 + \omega + 6c_s^2 + 2v_3^2) \frac{v_3}{2\omega}$$

$$C_{D_z^2 \rho}^{(3), \text{MRT}1} = (-2 - 3c_s^2 \omega_{11} + \omega_{11} - \omega_{11} v_3^2 + 6c_s^2 + 2v_3^2) \frac{v_3}{2\omega_{11}}$$

$$C_{D_z^2 \rho}^{(3), \text{MRT}2} = C_{D_z^2 \rho}^{(3), \text{MRT}1}$$

$$C_{D_z^2 \rho}^{(3), \text{CLBM}1} = C_{D_z^2 \rho}^{(3), \text{MRT}1}$$

$$C_{D_z^2 \rho}^{(3), \text{CLBM}2} = C_{D_z^2 \rho}^{(3), \text{MRT}1}$$

$$C_{D_z^2 \rho}^{(3), \text{CuLBM}1} = (-2 + \omega_6 - 3\omega_6 c_s^2 + 6c_s^2 - \omega_6 v_3^2 + 2v_3^2) \frac{v_3}{2\omega_6}$$

$$C_{D_z^2 \rho}^{(3), \text{CuLBM}2} = (2\omega_1 v_3^2 - 3\omega_1 \omega_2 v_3^2 + 3\omega_1 \omega_2 - 2\omega_1 + 6c_s^2 \omega_1 - 4\omega_2 + 4\omega_2 v_3^2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2) \frac{v_3}{6\omega_1 \omega_2}$$

coefficient $C_{D_z^2 v_3}^{(3)}$ **at** $\frac{\partial^2 v_3}{\partial x_3^2}$:

$$C_{D_z^2 v_3}^{(3), \text{SRT}} = (-2 - c_s^2 \omega - 3\omega v_3^2 + \omega + 2c_s^2 + 6v_3^2) \frac{\rho}{2\omega}$$

$$C_{D_z^2 v_3}^{(3), \text{MRT1}} = (-2 - c_s^2 \omega_{11} + \omega_{11} - 3\omega_{11} v_3^2 + 2c_s^2 + 6v_3^2) \frac{\rho}{2\omega_{11}}$$

$$C_{D_z^2 v_3}^{(3), \text{MRT2}} = C_{D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(3), \text{CLBM1}} = C_{D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(3), \text{CLBM2}} = C_{D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_6 - \omega_6 c_s^2 + 2c_s^2 - 3\omega_6 v_3^2 + 6v_3^2) \frac{\rho}{2\omega_6}$$

$$C_{D_z^2 v_3}^{(3), \text{CuLBM2}} = (6\omega_1 v_3^2 - 9\omega_1 \omega_2 v_3^2 + 3\omega_1 \omega_2 - 2\omega_1 + 2c_s^2 \omega_1 - 4\omega_2 + 12\omega_2 v_3^2 + 4c_s^2 \omega_2 - 3c_s^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_x^3 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^3}$:

$$C_{D_x^3 \rho}^{(3), \text{SRT}} = (-1 + v_1^2 + 3c_s^2) \frac{v_1 v_3}{12}$$

$$C_{D_x^3 \rho}^{(3), \text{MRT1}} = (-6\omega_6 \omega_{13} v_1^2 + 12\omega_{13} v_1^2 - 12\omega_{13} + 3\omega_6 \omega_{13} c_s^2 \omega_9 + 36\omega_{13} c_s^2 + 18\omega_6 c_s^2 \omega_9 + 6\omega_6 \omega_{13} - 18\omega_6 \omega_{13} c_s^2 - 36c_s^2 \omega_9 - 12v_1^2 \omega_9 - 6\omega_6 \omega_9 - \omega_6 \omega_{13} \omega_9 + 6\omega_6 v_1^2 \omega_9 + 12\omega_9 + \omega_6 \omega_{13} v_1^2 \omega_9) \frac{v_1 v_3}{12\omega_6 \omega_{13} \omega_9}$$

$$C_{D_x^3 \rho}^{(3), \text{MRT2}} = C_{D_x^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(3), \text{CLBM1}} = C_{D_x^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(3), \text{CLBM2}} = C_{D_x^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(3), \text{CuLBM1}} = C_{D_x^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(3), \text{CuLBM2}} = C_{D_x^3 \rho}^{(3), \text{SRT}}$$

coefficient $C_{D_x^3 v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^3}$:

$$C_{D_x^3 v_1}^{(3), \text{SRT}} = (-1 + 3v_1^2 + c_s^2) \frac{\rho v_3}{12}$$

$$C_{D_x^3 v_1}^{(3), \text{MRT1}} = (-18\omega_6 \omega_{13} v_1^2 + 36\omega_{13} v_1^2 - 12\omega_{13} + \omega_6 \omega_{13} c_s^2 \omega_9 + 12\omega_{13} c_s^2 + 6\omega_6 c_s^2 \omega_9 + 6\omega_6 \omega_{13} - 6\omega_6 \omega_{13} c_s^2 - 12c_s^2 \omega_9 - 36v_1^2 \omega_9 - 6\omega_6 \omega_9 - \omega_6 \omega_{13} \omega_9 + 18\omega_6 v_1^2 \omega_9 + 12\omega_9 + 3\omega_6 \omega_{13} v_1^2 \omega_9) \frac{\rho v_3}{12\omega_6 \omega_{13} \omega_9}$$

$$C_{D_x^3 v_1}^{(3), \text{MRT2}} = C_{D_x^3 v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(3), \text{CLBM1}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(3), \text{CLBM2}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(3), \text{CuLBM1}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(3), \text{CuLBM2}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

coefficient $C_{D_x^3 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^3}$:

$$C_{D_x^3 v_3}^{(3), \text{SRT}} = (6 - 6v_1^2 + 18c_s^2 \omega + \omega^2 - \omega^2 v_1^2 - 3c_s^2 \omega^2 - 6\omega + 6\omega v_1^2 - 18c_s^2) \frac{\rho v_1}{6\omega^2}$$

$$C_{D_x^3 v_3}^{(3), \text{MRT1}} = (6\omega_6 - 6\omega_6 v_1^2 + 3\omega_6 \omega_{13} v_1^2 + 3\omega_6^2 c_s^2 - 3\omega_6^2 - 3\omega_6^2 \omega_{13} c_s^2 + \omega_6^2 \omega_{13} - 12\omega_{13} c_s^2 - 3\omega_6 \omega_{13} + 15\omega_6 \omega_{13} c_s^2 - 6\omega_6 c_s^2 - \omega_6^2 \omega_{13} v_1^2 + 3\omega_6^2 v_1^2) \frac{\rho v_1}{6\omega_6^2 \omega_{13}}$$

$$C_{D_x^3 v_3}^{(3),\text{MRT}2} = C_{D_x^3 v_3}^{(3),\text{MRT}1}$$

$$C_{D_x^3 v_3}^{(3),\text{CLBM}1} = (6 - 6v_1^2 - 3\omega_6 + 3\omega_6 v_1^2 - \omega_6 \omega_{13} v_1^2 + 3\omega_{13} v_1^2 - 3\omega_{13} + 9\omega_{13} c_s^2 + \omega_6 \omega_{13} - 3\omega_6 \omega_{13} c_s^2 + 9\omega_6 c_s^2 - 18c_s^2) \frac{\rho v_1}{6\omega_6 \omega_{13}}$$

$$C_{D_x^3 v_3}^{(3),\text{CLBM}2} = C_{D_x^3 v_3}^{(3),\text{CLBM}1}$$

$$C_{D_x^3 v_3}^{(3),\text{CuLBM}1} = (6 - 6v_1^2 - 3c_s^2 \omega_2 \omega_{12} - v_1^2 \omega_2 \omega_{12} + 3v_1^2 \omega_2 + 9c_s^2 \omega_{12} - 18c_s^2 + \omega_2 \omega_{12} + 3v_1^2 \omega_{12} - 3\omega_2 + 9c_s^2 \omega_2 - 3\omega_{12}) \frac{\rho v_1}{6\omega_2 \omega_{12}}$$

$$C_{D_x^3 v_3}^{(3),\text{CuLBM}2} = (-2\omega_3 \omega_4 \omega_1 v_1^2 + 6\omega_3 - 18\omega_4 c_s^2 + 3\omega_3 \omega_1 v_1^2 - 3\omega_4 \omega_1 - 6\omega_3 \omega_4 c_s^2 \omega_1 - 6\omega_3 v_1^2 + 9\omega_3 c_s^2 \omega_1 + 6\omega_4 + 6\omega_3 \omega_4 v_1^2 - 3\omega_3 \omega_1 + 2\omega_3 \omega_4 \omega_1 - 6\omega_4 v_1^2 - 6\omega_3 \omega_4 + 3\omega_4 \omega_1 v_1^2 + 18\omega_3 \omega_4 c_s^2 - 18\omega_3 c_s^2 + 9\omega_4 c_s^2 \omega_1) \frac{\rho v_1}{12\omega_3 \omega_4 \omega_1}$$

$$\text{coefficient } C_{D_x^2 D_y v_2}^{(3)} \text{ at } \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_2}^{(3),\text{SRT}} = \frac{-c_s^2 \rho v_3}{6}$$

$$C_{D_x^2 D_y v_2}^{(3),\text{MRT}1} = (-6\omega_6 \omega_7 \omega_5 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_6 \omega_7 \omega_8 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_5) \frac{c_s^2 \rho v_3}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x^2 D_y v_2}^{(3),\text{MRT}2} = C_{D_x^2 D_y v_2}^{(3),\text{MRT}1}$$

$$C_{D_x^2 D_y v_2}^{(3),\text{CLBM}1} = C_{D_x^2 D_y v_2}^{(3),\text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(3),\text{CLBM}2} = C_{D_x^2 D_y v_2}^{(3),\text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(3),\text{CuLBM}1} = C_{D_x^2 D_y v_2}^{(3),\text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(3),\text{CuLBM}2} = C_{D_x^2 D_y v_2}^{(3),\text{SRT}}$$

$$\text{coefficient } C_{D_x^2 D_y v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_3}^{(3),\text{SRT}} = 0$$

$$C_{D_x^2 D_y v_3}^{(3),\text{MRT}1} = (-\omega_7 \omega_8 + \omega_6 \omega_7 \omega_8 - \omega_6 \omega_8 - \omega_6^2 \omega_7 + \omega_6^2 + \omega_6 \omega_7) \frac{c_s^2 \rho v_2}{\omega_6^2 \omega_7 \omega_8}$$

$$C_{D_x^2 D_y v_3}^{(3),\text{MRT}2} = C_{D_x^2 D_y v_3}^{(3),\text{MRT}1}$$

$$C_{D_x^2 D_y v_3}^{(3),\text{CLBM}1} = 0$$

$$C_{D_x^2 D_y v_3}^{(3),\text{CLBM}2} = 0$$

$$C_{D_x^2 D_y v_3}^{(3),\text{CuLBM}1} = 0$$

$$C_{D_x^2 D_y v_3}^{(3),\text{CuLBM}2} = (-2\omega_3 - 6\omega_4 c_s^2 - 2\omega_4 v_2^2 - \omega_4 \omega_1 + \omega_4 \omega_1 v_2^2 - 3\omega_3 c_s^2 \omega_1 + 2\omega_4 + \omega_3 \omega_1 + 2\omega_3 v_2^2 - \omega_3 \omega_1 v_2^2 + 6\omega_3 c_s^2 + 3\omega_4 c_s^2 \omega_1) \frac{\rho v_2}{4\omega_3 \omega_4 \omega_1}$$

$$\text{coefficient } C_{D_x D_y^2 v_1}^{(3)} \text{ at } \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_1}^{(3),\text{SRT}} = \frac{-c_s^2 \rho v_3}{6}$$

$$C_{D_x D_y^2 v_1}^{(3),\text{MRT}1} = (-6\omega_6 \omega_7 \omega_5 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_6 \omega_7 \omega_8 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_5) \frac{c_s^2 \rho v_3}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x D_y^2 v_1}^{(3),\text{MRT}2} = C_{D_x D_y^2 v_1}^{(3),\text{MRT}1}$$

$$C_{D_x D_y^2 v_1}^{(3),\text{CLBM}1} = C_{D_x D_y^2 v_1}^{(3),\text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CLBM2}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CuLBM1}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CuLBM2}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$\text{coefficient } C_{D_x D_y^2 v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{MRT1}} = (-\omega_7 \omega_8 + \omega_6 \omega_7 \omega_8 - \omega_6 \omega_8 + \omega_6 \omega_7 + \omega_7^2 - \omega_6 \omega_7^2) \frac{c_s^2 \rho v_1}{\omega_6 \omega_7^2 \omega_8}$$

$$C_{D_x D_y^2 v_3}^{(3), \text{MRT2}} = C_{D_x D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CuLBM2}} = (-2\omega_3 - 6\omega_4 c_s^2 - \omega_3 \omega_1 v_1^2 - \omega_4 \omega_1 + 2\omega_3 v_1^2 - 3\omega_3 c_s^2 \omega_1 + 2\omega_4 + \omega_3 \omega_1 - 2\omega_4 v_1^2 + \omega_4 \omega_1 v_1^2 + 6\omega_3 c_s^2 + 3\omega_4 c_s^2 \omega_1) \frac{\rho v_1}{4\omega_3 \omega_4 \omega_1}$$

$$\text{coefficient } C_{D_y^3 \rho}^{(3)} \text{ at } \frac{\partial^3 \rho}{\partial x_2^3} :$$

$$C_{D_y^3 \rho}^{(3), \text{SRT}} = (-1 + 3c_s^2 + v_2^2) \frac{v_2 v_3}{12}$$

$$C_{D_y^3 \rho}^{(3), \text{MRT1}} = (12\omega_{16} v_2^2 - 18\omega_{16} \omega_7 c_s^2 + \omega_{16} \omega_{10} \omega_7 v_2^2 - 12\omega_{16} + 12\omega_{10} + 6\omega_{16} \omega_7 + 36\omega_{16} c_s^2 + 3\omega_{16} \omega_{10} \omega_7 c_s^2 - \omega_{16} \omega_{10} \omega_7 - 6\omega_{16} \omega_7 v_2^2 - 36\omega_{10} c_s^2 - 6\omega_{10} \omega_7 + 6\omega_{10} \omega_7 v_2^2 + 18\omega_{10} \omega_7 c_s^2 - 12\omega_{10} v_2^2) \frac{v_2 v_3}{12\omega_{16} \omega_{10} \omega_7}$$

$$C_{D_y^3 \rho}^{(3), \text{MRT2}} = C_{D_y^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(3), \text{CLBM1}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(3), \text{CLBM2}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(3), \text{CuLBM1}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(3), \text{CuLBM2}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$\text{coefficient } C_{D_y^3 v_2}^{(3)} \text{ at } \frac{\partial^3 v_2}{\partial x_2^3} :$$

$$C_{D_y^3 v_2}^{(3), \text{SRT}} = (-1 + c_s^2 + 3v_2^2) \frac{\rho v_3}{12}$$

$$C_{D_y^3 v_2}^{(3), \text{MRT1}} = (36\omega_{16} v_2^2 - 6\omega_{16} \omega_7 c_s^2 + 3\omega_{16} \omega_{10} \omega_7 v_2^2 - 12\omega_{16} + 12\omega_{10} + 6\omega_{16} \omega_7 + 12\omega_{16} c_s^2 + \omega_{16} \omega_{10} \omega_7 c_s^2 - \omega_{16} \omega_{10} \omega_7 - 18\omega_{16} \omega_7 v_2^2 - 12\omega_{10} c_s^2 - 6\omega_{10} \omega_7 + 18\omega_{10} \omega_7 v_2^2 + 6\omega_{10} \omega_7 c_s^2 - 36\omega_{10} v_2^2) \frac{\rho v_3}{12\omega_{16} \omega_{10} \omega_7}$$

$$C_{D_y^3 v_2}^{(3), \text{MRT2}} = C_{D_y^3 v_2}^{(3), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(3), \text{CLBM1}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(3), \text{CLBM2}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(3), \text{CuLBM1}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(3), \text{CuLBM2}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$\text{coefficient } C_{D_y^3 v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_2^3} :$$

$$C_{D_y^3 v_3}^{(3), \text{SRT}} = (6 + 18c_s^2\omega + \omega^2 + 6\omega v_2^2 - 3c_s^2\omega^2 - 6\omega - \omega^2 v_2^2 - 18c_s^2 - 6v_2^2) \frac{\rho v_2}{6\omega^2}$$

$$C_{D_y^3 v_3}^{(3), \text{MRT1}} = (3\omega_7^2 c_s^2 + \omega_{16}\omega_7^2 + 15\omega_{16}\omega_7 c_s^2 + 3\omega_7^2 v_2^2 - 3\omega_{16}\omega_7 - 12\omega_{16}c_s^2 + 6\omega_7 + 3\omega_{16}\omega_7 v_2^2 - \omega_{16}\omega_7^2 v_2^2 - 6\omega_7 v_2^2 - 3\omega_{16}\omega_7^2 c_s^2 - 3\omega_7^2 - 6\omega_7 c_s^2) \frac{\rho v_2}{6\omega_{16}\omega_7^2}$$

$$C_{D_y^3 v_3}^{(3), \text{MRT2}} = C_{D_y^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^3 v_3}^{(3), \text{CLBM1}} = (6 + 3\omega_{16}v_2^2 - 3\omega_{16}\omega_7 c_s^2 - 3\omega_{16} + \omega_{16}\omega_7 + 9\omega_{16}c_s^2 - 3\omega_7 - \omega_{16}\omega_7 v_2^2 + 3\omega_7 v_2^2 - 18c_s^2 - 6v_2^2 + 9\omega_7 c_s^2) \frac{\rho v_2}{6\omega_{16}\omega_7}$$

$$C_{D_y^3 v_3}^{(3), \text{CLBM2}} = C_{D_y^3 v_3}^{(3), \text{CLBM1}}$$

$$C_{D_y^3 v_3}^{(3), \text{CuLBM1}} = (6 - 3\omega_3 + \omega_3\omega_{11} + 9c_s^2\omega_{11} - \omega_3\omega_{11}v_2^2 + 3\omega_3v_2^2 - 3\omega_{11} + 3\omega_{11}v_2^2 - 3\omega_3c_s^2\omega_{11} - 18c_s^2 + 9\omega_3c_s^2 - 6v_2^2) \frac{\rho v_2}{6\omega_3\omega_{11}}$$

$$C_{D_y^3 v_3}^{(3), \text{CuLBM2}} = (6\omega_3 - 18\omega_4c_s^2 - 6\omega_4v_2^2 - 3\omega_4\omega_1 - 6\omega_3\omega_4c_s^2\omega_1 + 3\omega_4\omega_1v_2^2 + 9\omega_3c_s^2\omega_1 + 6\omega_4 - 3\omega_3\omega_1 - 6\omega_3v_2^2 + 6\omega_3\omega_4v_2^2 + 2\omega_3\omega_4\omega_1 - 6\omega_3\omega_4 + 18\omega_3\omega_4c_s^2 + 3\omega_3\omega_1v_2^2 - 18\omega_3c_s^2 + 9\omega_4c_s^2\omega_1 - 2\omega_3\omega_4\omega_1v_2^2) \frac{\rho v_2}{12\omega_3\omega_4\omega_1}$$

$$\text{coefficient } C_{D_x^2 D_z \rho}^{(3)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z \rho}^{(3), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{MRT1}} = (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4}{6\omega_6^2}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{MRT2}} = C_{D_x^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CLBM1}} = C_{D_x^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CLBM2}} = C_{D_x^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CuLBM1}} = (-12 + 12\omega_2 - \omega_2^2) \frac{c_s^4}{6\omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CuLBM2}} = (-c_s^4\omega_1^2\omega_2^2 - 14c_s^4\omega_2^2 - 3\omega_1^2v_1^4\omega_2 - 2\omega_1^2v_1^2 + 6c_s^2\omega_1v_1^2\omega_2 - 3\omega_1v_1^2\omega_2^2 + 2c_s^2\omega_1^2\omega_2 + 15c_s^2\omega_1v_1^2\omega_2^2 - 18c_s^2v_1^2\omega_2^2 + 2c_s^4\omega_1^2 - 2\omega_1v_1^2\omega_2 - 2c_s^4\omega_1^2\omega_2 - 4v_1^4\omega_2^2 - 2c_s^2\omega_1\omega_2^2 + 2c_s^2\omega_2^2 + 3\omega_1^2v_1^2\omega_2 + 12c_s^2\omega_1^2v_1^2 + 3\omega_1v_1^4\omega_2^2 + 2\omega_1v_1^4\omega_2 - 2c_s^2\omega_1^2 + 2\omega_1^2v_1^4 + 4v_1^2\omega_2^2 - 15c_s^2\omega_1^2v_1^2\omega_2 + 14c_s^4\omega_1\omega_2^2) \frac{1}{6\omega_1^2\omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_z v_1}^{(3)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{MRT1}} = (2\omega_6 - 2\omega_{13} - \omega_6^2 + \omega_6\omega_{13}) \frac{c_s^2 \rho v_1}{\omega_6^2 \omega_{13}}$$

$$C_{D_x^2 D_z v_1}^{(3), \text{MRT2}} = C_{D_x^2 D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CuLBM2}} = (8\omega_1^2v_1^2 + 11\omega_1v_1^2\omega_2^2 - 5\omega_1\omega_2^2 - 9c_s^2\omega_1^2\omega_2 + 6\omega_1v_1^2\omega_2 - 2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 4\omega_1^2 + 9c_s^2\omega_1\omega_2^2 - 10c_s^2\omega_2^2 - 11\omega_1^2v_1^2\omega_2 + 8c_s^2\omega_1^2 + 2c_s^2\omega_1\omega_2 - 14v_1^2\omega_2^2 + 6\omega_2^2) \frac{\rho v_1}{6\omega_1^2\omega_2^2}$$

coefficient $C_{D_x^2 D_z v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_3}^{(3), \text{SRT}} = \frac{-c_s^2 \rho v_3}{6}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{MRT1}} = (-\omega_6^2 \omega_{11} \omega_{18} + 12\omega_6 \omega_{11} + 12\omega_6^2 - 12\omega_6 \omega_{18} + 12\omega_6 \omega_{11} \omega_{18} - 12\omega_6^2 \omega_{11} - 12\omega_{11} \omega_{18}) \frac{c_s^2 \rho v_3}{6\omega_6^2 \omega_{11} \omega_{18}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{MRT2}} = C_{D_x^2 D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CLBM1}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CLBM2}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CuLBM1}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CuLBM2}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

coefficient $C_{D_x D_y D_z \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{MRT1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{MRT2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CuLBM2}} = (\omega_1^2 v_1^2 + v_2^2 \omega_2^2 - 2\omega_1 v_1^2 \omega_2 + 4\omega_1 \omega_2 - 2\omega_1^2 + 6c_s^2 \omega_2^2 - 2\omega_1 v_2^2 \omega_2 + 6c_s^2 \omega_1^2 - 12c_s^2 \omega_1 \omega_2 + v_1^2 \omega_2^2 + \omega_1^2 v_2^2 - 2\omega_2^2) \frac{v_1 v_2}{3\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{MRT1}} = (-\omega_7 \omega_8 + \omega_6 \omega_7 \omega_8 - \omega_6 \omega_8 - \omega_6^2 \omega_7 + \omega_6^2 + \omega_6 \omega_7) \frac{c_s^2 \rho v_2}{\omega_6^2 \omega_7 \omega_8}$$

$$C_{D_x D_y D_z v_1}^{(3), \text{MRT2}} = C_{D_x D_y D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CuLBM2}} = (18\omega_3 c_s^2 \omega_1 \omega_2^2 + 2\omega_3 \omega_4 \omega_1^2 v_2^2 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 v_1^2 \omega_2^2 + \omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 8\omega_3 \omega_4 c_s^2 \omega_1^2 + 4\omega_4 \omega_1 \omega_2^2 - 4\omega_3 \omega_4 c_s^2 \omega_2^2 + 3\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 4\omega_4 \omega_1 v_2^2 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 \omega_1 v_2^2 \omega_2^2 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - \omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 - 12\omega_3 \omega_4 \omega_1 v_1^2 \omega_2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_4 \omega_1^2 v_2^2 \omega_2^2 - 3\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 6\omega_3 \omega_1 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2 - 2\omega_4 \omega_1^2 v_2^2 \omega_2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 - 2\omega_3 \omega_4 v_2^2 \omega_2^2 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_2}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_2}^{(3)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{MRT1}} = (-\omega_7 \omega_8 + \omega_6 \omega_7 \omega_8 - \omega_6 \omega_8 + \omega_6 \omega_7 + \omega_7^2 - \omega_6 \omega_7^2) \frac{c_s^2 \rho v_1}{\omega_6 \omega_7^2 \omega_8}$$

$$C_{D_x D_y D_z v_2}^{(3), \text{MRT}2} = C_{D_x D_y D_z v_2}^{(3), \text{MRT}1}$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CLBM}1} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CLBM}2} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CuLBM}1} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CuLBM}2} = (18\omega_3 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 \omega_4 \omega_1^2 v_2^2 - 12\omega_4 c_s^2 \omega_1 \omega_2^2 - 2\omega_4 \omega_1^2 v_1^2 \omega_2 - 2\omega_3 \omega_4 v_1^2 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 8\omega_3 \omega_4 c_s^2 \omega_1^2 + 4\omega_4 \omega_1 \omega_2^2 - \omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 - 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 4\omega_3 \omega_4 c_s^2 \omega_2^2 + 3\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 + 3\omega_4 \omega_1^2 v_1^2 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - 3\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 6\omega_4 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - 3\omega_4 \omega_1^2 \omega_2^2 - 4\omega_4 \omega_1 v_1^2 \omega_2^2 + 6\omega_3 \omega_1 v_1^2 \omega_2^2 - 3\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 6\omega_3 \omega_1 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 + \omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 + 6\omega_3 \omega_4 v_2^2 \omega_2^2 + 9\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 2\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_1}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_y^2 D_z \rho}^{(3)} \text{ at } \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} :$$

$$C_{D_y^2 D_z \rho}^{(3), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{MRT}1} = (-12 + 12\omega_7 - \omega_7^2) \frac{c_s^4}{6\omega_7^2}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{MRT}2} = C_{D_y^2 D_z \rho}^{(3), \text{MRT}1}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CLBM}1} = C_{D_y^2 D_z \rho}^{(3), \text{MRT}1}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CLBM}2} = C_{D_y^2 D_z \rho}^{(3), \text{MRT}1}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CuLBM}1} = (-12 + 12\omega_3 - \omega_3^2) \frac{c_s^4}{6\omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CuLBM}2} = (-c_s^4 \omega_1^2 \omega_2^2 - 14c_s^4 \omega_2^2 + 2\omega_1 v_2^2 \omega_2 + 4v_2^2 \omega_2^2 - 15c_s^2 \omega_1^2 v_2^2 \omega_2 + 2c_s^2 \omega_1^2 \omega_2 + 2\omega_1^2 v_2^4 + 12c_s^2 \omega_1^2 v_2^2 + 3\omega_1^2 v_2^2 \omega_2 + 2c_s^4 \omega_1^2 - 2c_s^4 \omega_1^2 \omega_2 + 3\omega_1 v_2^4 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_2^2 - 18c_s^2 v_2^2 \omega_2^2 + 15c_s^2 \omega_1 v_2^2 \omega_2^2 - 2\omega_1 v_2^2 \omega_2 - 4v_2^4 \omega_2^2 - 3\omega_1^2 v_2^4 \omega_2 - 2c_s^2 \omega_1^2 + 6c_s^2 \omega_1 v_2^2 \omega_2 - 3\omega_1 v_2^2 \omega_2^2 + 14c_s^4 \omega_1 \omega_2^2 - 2\omega_1^2 v_2^2) \frac{1}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_y^2 D_z v_2}^{(3)} \text{ at } \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} :$$

$$C_{D_y^2 D_z v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{MRT}1} = (-2\omega_{16} + \omega_{16} \omega_7 + 2\omega_7 - \omega_7^2) \frac{c_s^2 \rho v_2}{\omega_{16} \omega_7^2}$$

$$C_{D_y^2 D_z v_2}^{(3), \text{MRT}2} = C_{D_y^2 D_z v_2}^{(3), \text{MRT}1}$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CLBM}1} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CLBM}2} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CuLBM}1} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CuLBM}2} = (-14v_2^2 \omega_2^2 - 5\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 - 11\omega_1^2 v_2^2 \omega_2 - 2\omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 10c_s^2 \omega_2^2 + 6\omega_1 v_2^2 \omega_2 + 8c_s^2 \omega_1^2 + 2c_s^2 \omega_1 \omega_2 + 11\omega_1 v_2^2 \omega_2^2 + 8\omega_1^2 v_2^2 + 6\omega_2^2) \frac{\rho v_2}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_y^2 D_z v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} :$$

$$C_{D_y^2 D_z v_3}^{(3), \text{SRT}} = \frac{-c_s^2 \rho v_3}{6}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{MRT}1} = (-12\omega_{19} \omega_7 + 12\omega_{19} \omega_7 \omega_{11} + 12\omega_7 \omega_{11} - 12\omega_7^2 \omega_{11} - \omega_{19} \omega_7^2 \omega_{11} - 12\omega_{19} \omega_{11} + 12\omega_7^2) \frac{c_s^2 \rho v_3}{6\omega_{19} \omega_7^2 \omega_{11}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{MRT}^2} = C_{D_y^2 D_z v_3}^{(3), \text{MRT}^1}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CLBM}^1} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CLBM}^2} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CuLBM}^1} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CuLBM}^2} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

coefficient $C_{D_x D_z^2 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{MRT}^1} = (-3\omega_6 c_s^2 \omega_{11} \omega_{18} - 3c_s^2 \omega_{11}^2 + \omega_6 \omega_{11} + 3\omega_6 c_s^2 \omega_{11}^2 + \omega_{11}^2 - 3\omega_6 c_s^2 \omega_{11} + 3c_s^2 \omega_{11} \omega_{18} - \omega_{11}^2 v_3^2 + \omega_6 v_3^2 \omega_{18} - \omega_6 \omega_{11}^2 + \omega_6 \omega_{11}^2 v_3^2 - \omega_6 \omega_{11} v_3^2 - \omega_6 \omega_{11} v_3^2 \omega_{18} - \omega_6 \omega_{18} + \omega_6 \omega_{11} \omega_{18} + 3\omega_6 c_s^2 \omega_{18} - \omega_{11} \omega_{18} + \omega_{11} v_3^2 \omega_{18}) \frac{v_1 v_3}{\omega_6 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 \rho}^{(3), \text{MRT}^2} = C_{D_x D_z^2 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CLBM}^1} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CLBM}^2} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CuLBM}^1} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CuLBM}^2} = (2\omega_1^2 v_1^2 + 3\omega_1 v_1^2 \omega_2^2 - 4\omega_1 \omega_2 v_3^2 - 3\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_2^2 v_3^2 + 2\omega_1 v_1^2 \omega_2 + 2\omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 6c_s^2 \omega_2^2 - 3\omega_1^2 v_1^2 \omega_2 + 12c_s^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 - 4v_1^2 \omega_2^2 + 2\omega_2^2 + 2\omega_1^2 v_3^2) \frac{v_1 v_3}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_1}^{(3), \text{SRT}} = (12 + 36c_s^2 \omega + 3\omega^2 + 12\omega v_3^2 - 11c_s^2 \omega^2 - 12\omega - 3\omega^2 v_3^2 - 36c_s^2 - 12v_3^2) \frac{\rho v_3}{12\omega^2}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{MRT}^1} = (-24\omega_6 c_s^2 \omega_{11} \omega_{18} + 6\omega_6^2 \omega_{11} \omega_{18} + 36\omega_6^2 c_s^2 \omega_{18} - 6\omega_6 \omega_{11}^2 \omega_{18} - 12\omega_6 c_s^2 \omega_{11}^2 - 6\omega_6^2 \omega_{11} v_3^2 \omega_{18} - 12\omega_6^2 \omega_{11} v_3^2 + 12\omega_6 \omega_{11}^2 - 12\omega_6^2 \omega_{18} + 6\omega_6 \omega_{11}^2 v_3^2 \omega_{18} - 12\omega_6 \omega_{11}^2 v_3^2 - 11\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11} + 12\omega_6^2 v_3^2 \omega_{18} - 18\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 24c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 \omega_{11}^2 v_3^2 - 12\omega_6^2 \omega_{11}^2 + 12\omega_6^2 \omega_{11} + 42\omega_6 c_s^2 \omega_{11}^2 \omega_{18} + 3\omega_6^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 - 3\omega_6^2 \omega_{11}^2 v_3^2 \omega_{18}) \frac{\rho v_3}{12\omega_6^2 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{MRT}^2} = C_{D_x D_z^2 v_1}^{(3), \text{MRT}^1}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CLBM}^1} =$$

$$(-18\omega_6 c_s^2 \omega_{11} \omega_{18} - 6\omega_{11}^2 \omega_{18} - 36c_s^2 \omega_{11}^2 + 3\omega_6 \omega_{11}^2 \omega_{18} + 12\omega_6 \omega_{11} + 6\omega_{11}^2 v_3^2 \omega_{18} + 36\omega_6 c_s^2 \omega_{11}^2 + 12\omega_{11}^2 - 36\omega_6 c_s^2 \omega_{11} - 12\omega_{11}^2 v_3^2 + 12\omega_6 v_3^2 \omega_{18} - 12\omega_6 \omega_{11}^2 - 3\omega_6 \omega_{11}^2 v_3^2 \omega_{18} + 12\omega_6 \omega_{11}^2 v_3^2 - 12\omega_6 \omega_{11} v_3^2 - 6\omega_6 \omega_{11} v_3^2 \omega_{18} + 18c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6 \omega_{18} + 6\omega_6 \omega_{11} \omega_{18} + 36\omega_6 c_s^2 \omega_{18} - 11\omega_6 c_s^2 \omega_{11}^2 \omega_{18}) \frac{\rho v_3}{12\omega_6 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CLBM}^2} = C_{D_x D_z^2 v_1}^{(3), \text{CLBM}^1}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CuLBM}^1} = (-12\omega_6^2 v_3^2 - 12\omega_8 \omega_2 - 3\omega_6^2 \omega_8 \omega_2 v_3^2 + 12\omega_6^2 \omega_2 v_3^2 + 36\omega_6^2 c_s^2 \omega_2 + 6\omega_6 \omega_8 \omega_2 - 36\omega_6^2 c_s^2 - 11\omega_6^2 c_s^2 \omega_8 \omega_2 + 12\omega_6^2 - 12\omega_6^2 \omega_2 + 6\omega_6^2 \omega_8 v_3^2 + 12\omega_6 \omega_2 - 6\omega_6^2 \omega_8 + 36c_s^2 \omega_8 \omega_2 - 6\omega_6 \omega_8 \omega_2 v_3^2 + 12\omega_8 \omega_2 v_3^2 + 18\omega_6^2 c_s^2 \omega_8 + 3\omega_6^2 \omega_8 \omega_2 - 12\omega_6 \omega_2 v_3^2 - 18\omega_6 c_s^2 \omega_8 \omega_2 - 36\omega_6 c_s^2 \omega_2) \frac{\rho v_3}{12\omega_6^2 \omega_8 \omega_2}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CuLBM}^2} =$$

$$(-36\omega_3 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 2\omega_3 \omega_4 \omega_1 \omega_2^2 v_3^2 + 4\omega_3 \omega_4 \omega_1^2 v_3^2 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 - 24\omega_3 \omega_4 v_1^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 - 2\omega_3 \omega_4 \omega_1^2 \omega_2 v_3^2 + 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1^2 + 8\omega_4 \omega_1 \omega_2^2 - 8\omega_4 \omega_1 \omega_2^2 v_3^2 - 18\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_2^2 - 12\omega_3 \omega_1 \omega_2^2 v_3^2 + 12\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 4\omega_4 \omega_1^2 \omega_2 v_3^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_4 \omega_1^2 \omega_2 v_3^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1 \omega_2 + 6\omega_3 \omega_1^2 \omega_2^2 v_3^2 + 12\omega_3 \omega_4 \omega_1 v_1^2 \omega_2 - 6\omega_4 \omega_1^2 \omega_2^2 - 11\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 v_3^2 + 12\omega_3 \omega_1 \omega_2^2 + 8\omega_3 \omega_4 \omega_2^2 v_3^2 + 4\omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 + 18\omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2 + 12\omega_3 \omega_4 \omega_1^2 v_1^2) \frac{\rho v_3}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{MRT1}} = (-\omega_6 c_s^2 \omega_{11} \omega_{18} - c_s^2 \omega_{11}^2 + \omega_6 \omega_{11} + \omega_6 c_s^2 \omega_{11}^2 + \omega_{11}^2 - \omega_6 c_s^2 \omega_{11} + c_s^2 \omega_{11} \omega_{18} - 3\omega_{11}^2 v_3^2 + 3\omega_6 v_3^2 \omega_{18} - \omega_6 \omega_{11}^2 + 3\omega_6 \omega_{11}^2 v_3^2 - 3\omega_6 \omega_{11} v_3^2 - 3\omega_6 \omega_{11} v_3^2 \omega_{18} - \omega_6 \omega_{18} + \omega_6 \omega_{11} \omega_{18} + \omega_6 c_s^2 \omega_{18} - \omega_{11} \omega_{18} + 3\omega_{11} v_3^2 \omega_{18}) \frac{\rho v_1}{\omega_6 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_3}^{(3), \text{MRT2}} = C_{D_x D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CuLBM2}} = (3\omega_3 c_s^2 \omega_1 \omega_2^2 - 2\omega_3 v_1^2 \omega_2^2 - \omega_3 \omega_1^2 v_1^2 \omega_2 + 2\omega_1 v_1^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 - 2\omega_1 \omega_2^2 + 6\omega_3 \omega_1^2 v_3^2 - 6c_s^2 \omega_1^2 \omega_2 + \omega_3 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 - 4\omega_3 c_s^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1^2 v_1^2 \omega_2 + \omega_3 \omega_1 v_1^2 \omega_2^2 - 12\omega_3 \omega_1 \omega_2 v_3^2 + 4\omega_3 \omega_1 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 2\omega_3 \omega_1^2 v_1^2 + 6\omega_3 \omega_2^2 v_3^2 - 4\omega_3 \omega_1^2) \frac{\rho v_1}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{MRT1}} = (-\omega_7 \omega_{11} v_3^2 - \omega_7 \omega_{11}^2 - 3c_s^2 \omega_{11}^2 - \omega_{19} \omega_7 + \omega_{19} \omega_7 \omega_{11} + \omega_{11}^2 - \omega_{19} \omega_7 \omega_{11} v_3^2 + 3\omega_{19} c_s^2 \omega_{11} - \omega_{11}^2 v_3^2 + \omega_7 \omega_{11} + \omega_{19} \omega_7 v_3^2 - 3\omega_{19} \omega_7 c_s^2 \omega_{11} + \omega_{19} \omega_{11} v_3^2 + 3\omega_7 c_s^2 \omega_{11}^2 - \omega_{19} \omega_{11} + 3\omega_{19} \omega_7 c_s^2 - 3\omega_7 c_s^2 \omega_{11} + \omega_7 \omega_{11}^2 v_3^2) \frac{v_2 v_3}{\omega_{19} \omega_7 \omega_{11}^2}$$

$$C_{D_y D_z^2 \rho}^{(3), \text{MRT2}} = C_{D_y D_z^2 \rho}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CuLBM2}} = (-4v_2^2 \omega_2^2 - 4\omega_1 \omega_2 v_3^2 - 3\omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 + 2\omega_2^2 v_3^2 - 3\omega_1^2 v_2^2 \omega_2 + 2\omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 4\omega_1^2 + 9c_s^2 \omega_1 \omega_2^2 - 6c_s^2 \omega_2^2 + 2\omega_1 v_2^2 \omega_2 + 12c_s^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 + 3\omega_1 v_3^2 \omega_2^2 + 2\omega_1^2 v_2^2 + 2\omega_2^2 + 2\omega_1^2 v_3^2) \frac{v_2 v_3}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 v_2}^{(3)}$ **at** $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_2}^{(3), \text{SRT}} = (12 + 36c_s^2 \omega + 3\omega^2 + 12\omega v_3^2 - 11c_s^2 \omega^2 - 12\omega - 3\omega^2 v_3^2 - 36c_s^2 - 12v_3^2) \frac{\rho v_3}{12\omega^2}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{MRT1}} = (12\omega_7 \omega_{11}^2 - 12\omega_7^2 c_s^2 \omega_{11} + 12\omega_7^2 \omega_{11}^2 v_3^2 + 36\omega_{19} \omega_7^2 c_s^2 - 11\omega_{19} \omega_7^2 c_s^2 \omega_{11}^2 - 6\omega_{19} \omega_7 \omega_{11}^2 - 24\omega_{19} c_s^2 \omega_{11}^2 - 12\omega_{19} \omega_7^2 - 18\omega_{19} \omega_7^2 c_s^2 \omega_{11} - 3\omega_{19} \omega_7^2 \omega_{11}^2 v_3^2 + 12\omega_{19} \omega_7^2 v_3^2 + 12\omega_7^2 c_s^2 \omega_{11}^2 + 12\omega_7^2 \omega_{11} - 6\omega_{19} \omega_7^2 \omega_{11} v_3^2 - 24\omega_{19} \omega_7 c_s^2 \omega_{11} - 12\omega_7 c_s^2 \omega_{11}^2 + 6\omega_{19} \omega_7 \omega_{11}^2 v_3^2 + 6\omega_{19} \omega_7^2 \omega_{11} - 12\omega_7^2 \omega_{11} v_3^2 + 3\omega_{19} \omega_7^2 \omega_{11}^2 + 42\omega_{19} \omega_7 c_s^2 \omega_{11}^2 - 12\omega_7 \omega_{11}^2 v_3^2 - 12\omega_7^2 \omega_{11}^2) \frac{\rho v_3}{12\omega_{19} \omega_7^2 \omega_{11}^2}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{MRT2}} = C_{D_y D_z^2 v_2}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CLBM1}} =$$

$$(-12\omega_7 \omega_{11} v_3^2 - 12\omega_7 \omega_{11}^2 - 36c_s^2 \omega_{11}^2 - 12\omega_{19} \omega_7 + 3\omega_{19} \omega_7 \omega_{11}^2 + 18\omega_{19} c_s^2 \omega_{11}^2 + 6\omega_{19} \omega_7 \omega_{11} + 12\omega_{11}^2 - 6\omega_{19} \omega_7 \omega_{11} v_3^2 - 12\omega_{11}^2 v_3^2 + 12\omega_7 \omega_{11} + 6\omega_{19} \omega_{11}^2 v_3^2 + 12\omega_{19} \omega_7 v_3^2 - 18\omega_{19} \omega_7 c_s^2 \omega_{11} + 36\omega_7 c_s^2 \omega_{11}^2 - 3\omega_{19} \omega_7 \omega_{11}^2 v_3^2 + 36\omega_{19} \omega_7 c_s^2 - 36\omega_7 c_s^2 \omega_{11} - 6\omega_{19} \omega_{11}^2 - 11\omega_{19} \omega_7 c_s^2 \omega_{11}^2 + 12\omega_7 \omega_{11}^2 v_3^2) \frac{\rho v_3}{12\omega_{19} \omega_7 \omega_{11}^2}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CLBM2}} = C_{D_y D_z^2 v_2}^{(3), \text{CLBM1}}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CuLBM1}} = (-12\omega_6^2 v_3^2 + 6\omega_6^2 \omega_{10} v_3^2 + 3\omega_6^2 \omega_3 \omega_{10} + 12\omega_3 \omega_{10} v_3^2 - 18\omega_6 \omega_3 \omega_{10} c_s^2 + 12\omega_6 \omega_3 + 36\omega_6^2 \omega_3 c_s^2 - 36\omega_6^2 c_s^2 + 18\omega_6^2 \omega_{10} c_s^2 + 36\omega_3 \omega_{10} c_s^2 + 12\omega_6^2 - 6\omega_6^2 \omega_{10} - 6\omega_6 \omega_3 \omega_{10} v_3^2 + 12\omega_6^2 \omega_3 v_3^2 - 11\omega_6^2 \omega_3 \omega_{10} c_s^2 - 12\omega_6 \omega_3 v_3^2 + 6\omega_6 \omega_3 \omega_{10} - 12\omega_6^2 \omega_3 - 3\omega_6^2 \omega_3 \omega_{10} v_3^2 - 12\omega_3 \omega_{10} - 36\omega_6 \omega_3 c_s^2) \frac{\rho v_3}{12\omega_6^2 \omega_3 \omega_{10}}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CuLBM2}} = (-36\omega_3 c_s^2 \omega_1 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 2\omega_3 \omega_4 \omega_1 \omega_2^2 v_3^2 + 4\omega_3 \omega_4 \omega_1^2 v_3^2 + 12\omega_3 \omega_4 \omega_1^2 v_2^2 - 24\omega_4 c_s^2 \omega_1 \omega_2^2 + 18\omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 - 2\omega_3 \omega_4 \omega_1^2 \omega_2 v_3^2 + 4\omega_3 \omega_4 c_s^2 \omega_1 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_1^2 + 8\omega_4 \omega_1 \omega_2^2 - 8\omega_4 \omega_1 \omega_2^2 v_3^2 + 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 + 16\omega_3 \omega_4 c_s^2 \omega_2^2 - 12\omega_3 \omega_1 \omega_2^2 v_3^2 + 12\omega_3 \omega_4 c_s^2 \omega_1 \omega_2^2 - 4\omega_4 \omega_1^2 \omega_2 v_3^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 6\omega_4 \omega_1^2 \omega_2^2 v_3^2 - 12\omega_4 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1 \omega_2 + 6\omega_3 \omega_1^2 \omega_2^2 v_3^2 - 18\omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 - 6\omega_4 \omega_1^2 \omega_2^2 - 11\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_4 c_s^2 \omega_1^2 \omega_2 - 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 v_3^2 + 12\omega_3 \omega_1 \omega_2^2 + 8\omega_3 \omega_4 \omega_2^2 v_3^2 + 4\omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 - 24\omega_3 \omega_4 v_2^2 \omega_2^2 + 18\omega_4 c_s^2 \omega_1^2 \omega_2^2) \frac{\rho v_3}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{MRT1}} = (-3\omega_7 \omega_{11} v_3^2 - \omega_7 \omega_{11}^2 - c_s^2 \omega_{11}^2 - \omega_{19} \omega_7 + \omega_{19} \omega_7 \omega_{11} + \omega_{11}^2 - 3\omega_{19} \omega_7 \omega_{11} v_3^2 + \omega_{19} c_s^2 \omega_{11} - 3\omega_{11}^2 v_3^2 + \omega_7 \omega_{11} + 3\omega_{19} \omega_7 v_3^2 - \omega_{19} \omega_7 c_s^2 \omega_{11} + 3\omega_{19} \omega_{11} v_3^2 + \omega_7 c_s^2 \omega_{11}^2 - \omega_{19} \omega_{11} + \omega_{19} \omega_7 c_s^2 - \omega_7 c_s^2 \omega_{11} + 3\omega_7 \omega_{11}^2 v_3^2) \frac{\rho v_2}{\omega_{19} \omega_7 \omega_{11}^2}$$

$$C_{D_y D_z^2 v_3}^{(3), \text{MRT2}} = C_{D_y D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CuLBM2}} = (3\omega_3 c_s^2 \omega_1 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 - 2\omega_1 \omega_2^2 + 6\omega_3 \omega_1^2 v_3^2 - 6c_s^2 \omega_1^2 \omega_2 + 2\omega_3 \omega_1^2 v_2^2 + \omega_3 \omega_1^2 \omega_2 - 2\omega_1^2 v_2^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 - 4\omega_3 c_s^2 \omega_2^2 + \omega_3 \omega_1 v_2^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 12\omega_3 \omega_1 \omega_2 v_3^2 + 4\omega_3 \omega_1 \omega_2 - 2\omega_3 v_2^2 \omega_2^2 - \omega_3 \omega_1^2 v_2^2 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 2\omega_1 v_2^2 \omega_2^2 + 6\omega_3 \omega_2^2 v_3^2 - 4\omega_3 \omega_1^2) \frac{\rho v_2}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_z^3 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{D_z^3 \rho}^{(3), \text{SRT}} = (24c_s^2 \omega^2 v_3^2 + 12c_s^2 \omega + 36v_3^4 + 36\omega v_3^2 + 7\omega^2 v_3^4 - c_s^2 \omega^2 + 12c_s^4 - 36\omega v_3^4 + 144c_s^2 v_3^2 - 7\omega^2 v_3^2 - 12c_s^4 \omega - 12c_s^2 + c_s^4 \omega^2 - 144c_s^2 \omega v_3^2 - 36v_3^2) \frac{1}{12\omega^2}$$

$$C_{D_z^3 \rho}^{(3), \text{MRT1}} = (-144c_s^2 \omega_{11} v_3^2 - c_s^2 \omega_{11}^2 + 36v_3^4 - 7\omega_{11}^2 v_3^2 - 36\omega_{11} v_3^4 + 12c_s^2 \omega_{11} + 12c_s^4 + 7\omega_{11}^2 v_3^4 + 144c_s^2 v_3^2 + 36\omega_{11} v_3^2 + c_s^4 \omega_{11}^2 - 12c_s^2 - 12c_s^4 \omega_{11} + 24c_s^2 \omega_{11}^2 v_3^2 - 36v_3^2) \frac{1}{12\omega_{11}^2}$$

$$C_{D_z^3 \rho}^{(3), \text{MRT2}} = C_{D_z^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_z^3 \rho}^{(3), \text{CLBM1}} = C_{D_z^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_z^3 \rho}^{(3), \text{CLBM2}} = C_{D_z^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_z^3 \rho}^{(3), \text{CuLBM1}} = (-7\omega_6^2 v_3^2 + 36v_3^4 - 36\omega_6 v_3^4 - \omega_6^2 c_s^2 + 24\omega_6^2 c_s^2 v_3^2 + 12c_s^4 - 12\omega_6 c_s^4 - 144\omega_6 c_s^2 v_3^2 + \omega_6^2 c_s^4 + 12\omega_6 c_s^2 + 144c_s^2 v_3^2 - 12c_s^2 + 7\omega_6^2 v_3^4 + 36\omega_6 v_3^2 - 36v_3^2) \frac{1}{12\omega_6^2}$$

$$C_{D_z^3 \rho}^{(3), \text{CuLBM2}} = (-12\omega_1^2 \omega_2 v_3^4 + c_s^4 \omega_1^2 \omega_2^2 + 8c_s^4 \omega_2^2 - 16\omega_1 \omega_2 v_3^2 + 4\omega_1^2 v_3^4 - 24\omega_1 \omega_2^2 v_3^4 + 4c_s^2 \omega_1^2 \omega_2 - 7\omega_1^2 \omega_2^2 v_3^2 - 16\omega_2^2 v_3^2 - c_s^2 \omega_1^2 \omega_2^2 + 24c_s^2 \omega_1^2 \omega_2^2 v_3^2 + 24c_s^2 \omega_1^2 v_3^2 + 4c_s^4 \omega_1^2 + 48c_s^2 \omega_1 \omega_2 v_3^2 - 4c_s^4 \omega_1^2 \omega_2 + 72c_s^2 \omega_2^2 v_3^2 - 96c_s^2 \omega_1 \omega_2^2 v_3^2 - 48c_s^2 \omega_1^2 \omega_2 v_3^2 + 8c_s^2 \omega_1 \omega_2^2 - 8c_s^2 \omega_2^2 - 4c_s^2 \omega_1^2 + 16\omega_1 \omega_2 v_3^4 + 12\omega_1^2 \omega_2 v_3^2 - 8c_s^4 \omega_1 \omega_2^2 + 7\omega_1^2 \omega_2^2 v_3^4 + 16\omega_2^2 v_3^4 - 4\omega_1^2 v_3^2 + 24\omega_1 \omega_2^2 v_3^2) \frac{1}{12\omega_1^2 \omega_2^2}$$

coefficient $C_{D_z^3 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_3^3}$:

$$C_{D_z^3 v_3}^{(3), \text{SRT}} = (-24 - 36c_s^2 \omega - 4\omega^2 - 60\omega v_3^2 + 5c_s^2 \omega^2 + 24\omega + 11\omega^2 v_3^2 + 36c_s^2 + 60v_3^2) \frac{\rho v_3}{6\omega^2}$$

$$C_{D_z^3 v_3}^{(3), \text{MRT1}} = (-24 + 5c_s^2 \omega_{11}^2 - 4\omega_{11}^2 + 11\omega_{11}^2 v_3^2 - 36c_s^2 \omega_{11} + 24\omega_{11} - 60\omega_{11} v_3^2 + 36c_s^2 + 60v_3^2) \frac{\rho v_3}{6\omega_{11}^2}$$

$$C_{D_z^3 v_3}^{(3), \text{MRT2}} = C_{D_z^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(3), \text{CLBM1}} = C_{D_z^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(3), \text{CLBM2}} = C_{D_z^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(3), \text{CuLBM1}} = (-24 + 11\omega_6^2 v_3^2 + 24\omega_6 + 5\omega_6^2 c_s^2 - 4\omega_6^2 - 36\omega_6 c_s^2 + 36c_s^2 - 60\omega_6 v_3^2 + 60v_3^2) \frac{\rho v_3}{6\omega_6}$$

$$C_{D_z^3 v_3}^{(3), \text{CuLBM2}} = (24\omega_1 \omega_2 v_3^2 + 16\omega_1 \omega_2^2 - 12c_s^2 \omega_1^2 \omega_2 + 11\omega_1^2 \omega_2^2 v_3^2 + 28\omega_2^2 v_3^2 + 5c_s^2 \omega_1^2 \omega_2^2 - 8\omega_1 \omega_2 + 8\omega_1^2 \omega_2 - 4\omega_1^2 - 24c_s^2 \omega_1 \omega_2^2 + 20c_s^2 \omega_2^2 + 8c_s^2 \omega_1^2 - 20\omega_1^2 \omega_2 v_3^2 + 8c_s^2 \omega_1 \omega_2 - 12\omega_2^2 + 8\omega_1^2 v_3^2 - 4\omega_1^2 \omega_2^2 - 40\omega_1 \omega_2^2 v_3^2) \frac{\rho v_3}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^4 \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^4}:$$

$$C_{D_x^4 \rho}^{(3), \text{SRT}} = (-6v_1^2 + c_s^2 \omega - 12c_s^2 \omega v_1^2 + 24c_s^2 v_1^2 + 2c_s^4 - 3\omega v_1^4 + 3\omega v_1^2 - c_s^4 \omega - 2c_s^2 + 6v_1^4) \frac{v_3}{24\omega}$$

$$C_{D_x^4 \rho}^{(3), \text{MRT1}} = (216\omega_{13}^2 c_s^2 v_2^2 \omega_9 + 36\omega_6^2 \omega_{13}^2 v_1^4 \omega_9 - 24\omega_{13} c_s^4 \omega_9^2 + 72\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9 - \omega_6^2 \omega_{13} c_s^4 \omega_9^2 - 24\omega_{13}^2 c_s^2 \omega_9 + 30\omega_6^2 \omega_{13} v_1^2 \omega_9^2 - 24\omega_6 v_1^4 \omega_9^2 + 96\omega_6 \omega_{13} v_1^4 \omega_9^2 + 72\omega_6 \omega_{13}^2 v_1^4 - 144\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 - 12\omega_6^2 c_s^2 \omega_9^2 + 36\omega_6^2 \omega_{13}^2 v_1^2 + 96\omega_6 \omega_{13}^2 v_1^2 \omega_9 - 144\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9 - 144\omega_6 c_s^2 v_1^2 \omega_9^2 + 48\omega_6 \omega_{13}^2 c_s^2 \omega_9 - 24\omega_6 \omega_{13}^2 c_s^2 + 432\omega_6 \omega_{13} c_s^2 v_1^2 \omega_9^2 - 12\omega_6^2 v_1^2 \omega_9^2 - 48\omega_6 \omega_{13} v_1^4 \omega_9 + 48\omega_6 \omega_{13} c_s^4 \omega_9^2 - 12\omega_6^2 \omega_{13}^2 c_s^4 - 24\omega_6 c_s^4 \omega_9^2 + 12\omega_6^2 \omega_{13} c_s^2 \omega_9^2 - 48\omega_{13}^2 v_1^2 \omega_9 - 24\omega_6^2 \omega_{13} v_1^2 \omega_9 - 3\omega_6^2 \omega_{13}^2 v_1^4 \omega_9^2 - 48\omega_{13} v_1^4 \omega_9^2 - 126\omega_6^2 \omega_{13} c_s^2 v_1^2 \omega_9^2 + 14\omega_6^2 \omega_{13}^2 c_s^4 \omega_9 + 24\omega_6 v_1^2 \omega_9^2 - 96\omega_6 \omega_{13} v_1^2 \omega_9^2 + 12\omega_6^2 \omega_{13}^2 c_s^2 + 12\omega_6^2 c_s^4 \omega_9^2 + 150\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 \omega_9 + 24\omega_6 \omega_{13}^2 c_s^4 - 96\omega_6 \omega_{13}^2 v_1^4 \omega_9 - 432\omega_6 \omega_{13}^2 c_s^2 v_1^2 \omega_9 - 36\omega_6^2 \omega_{13}^2 v_1^2 \omega_9 + 24\omega_{13} c_s^2 \omega_9^2 + \omega_6^2 \omega_{13}^2 c_s^2 \omega_9^2 + 288\omega_6 \omega_{13}^2 c_s^2 v_1^2 + 24\omega_{13}^2 c_s^4 \omega_9 - 30\omega_6^2 \omega_{13} v_1^4 \omega_9^2 - 12\omega_6^2 \omega_{13} c_s^4 \omega_9^2 + 48\omega_{13}^2 v_1^4 \omega_9 + 24\omega_6^2 \omega_{13} v_1^4 \omega_9 + 3\omega_6^2 \omega_{13}^2 v_1^2 \omega_9^2 + 48\omega_{13} v_1^2 \omega_9^2 + 72\omega_6^2 c_s^2 v_1^2 \omega_9^2 - 14\omega_6^2 \omega_{13}^2 c_s^2 \omega_9 - 12\omega_6^2 \omega_{13}^2 c_s^2 v_1^2 \omega_9^2 - 36\omega_6^2 \omega_{13}^2 v_1^4 - 48\omega_6 \omega_{13}^2 c_s^4 \omega_9 - 216\omega_{13} c_s^2 v_1^2 \omega_9^2 + 12\omega_6^2 v_1^4 \omega_9^2 + 48\omega_6 \omega_{13} v_1^4 \omega_9 - 72\omega_6 \omega_{13}^2 v_1^2 - 48\omega_6 \omega_{13} c_s^2 \omega_9^2 + 24\omega_6 c_s^2 \omega_9^2) \frac{v_3}{24\omega_6^2 \omega_{13}^2 \omega_9^2}$$

$$C_{D_x^4 \rho}^{(3), \text{MRT2}} = C_{D_x^4 \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(3), \text{CLBM1}} = (-6v_1^2 - c_s^4 \omega_9 + 24c_s^2 v_1^2 - 12c_s^2 v_1^2 \omega_9 + 2c_s^4 - 3v_1^4 \omega_9 + c_s^2 \omega_9 - 2c_s^2 + 6v_1^4 + 3v_1^2 \omega_9) \frac{v_3}{24\omega_9}$$

$$C_{D_x^4 \rho}^{(3), \text{CLBM2}} = C_{D_x^4 \rho}^{(3), \text{CLBM1}}$$

$$C_{D_x^4 \rho}^{(3), \text{CuLBM1}} = (-6v_1^2 - 12\omega_4 c_s^2 v_1^2 + \omega_4 c_s^2 + 24c_s^2 v_1^2 + 2c_s^4 - 3\omega_4 v_1^4 + 3\omega_4 v_1^2 - 2c_s^2 - \omega_4 c_s^4 + 6v_1^4) \frac{v_3}{24\omega_4}$$

$$C_{D_x^4 \rho}^{(3), \text{CuLBM2}} = (12v_1^4 \omega_2 + 48c_s^2 v_1^2 \omega_2 - 36c_s^2 \omega_1 v_1^2 \omega_2 + 2c_s^4 \omega_1 + 6\omega_1 v_1^4 + 24c_s^2 \omega_1 v_1^2 + 9\omega_1 v_1^2 \omega_2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 - 12v_1^2 \omega_2 - 2c_s^2 \omega_1 - 9\omega_1 v_1^4 \omega_2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 6\omega_1 v_1^2) \frac{v_3}{72\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^3 v_1}^{(3)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^4}:$$

$$C_{D_x^3 v_1}^{(3), \text{SRT}} = (-4 + 10v_1^2 - 3c_s^2 \omega + 2\omega - 5\omega v_1^2 + 6c_s^2) \frac{\rho v_1 v_3}{12\omega}$$

$$C_{D_x^3 v_1}^{(3), \text{MRT1}} = (24\omega_6^2 \omega_{13}^2 + 72\omega_6 \omega_{13}^2 \omega_9 + 12\omega_6^2 \omega_{13} c_s^2 \omega_9 + 60\omega_{13}^2 c_s^2 \omega_9 - 51\omega_6^2 \omega_{13} v_1^2 \omega_9^2 - 36\omega_{13}^2 \omega_9 - 12\omega_6^2 \omega_{13} \omega_9 + 24\omega_6^2 c_s^2 \omega_9^2 - 60\omega_6^2 \omega_{13}^2 v_1^2 - 168\omega_6 \omega_{13}^2 v_1^2 \omega_9 - 120\omega_6 \omega_{13}^2 c_s^2 \omega_9 + 72\omega_6 \omega_{13}^2 c_s^2 + 24\omega_6^2 v_1^2 \omega_9^2 + 21\omega_6^2 \omega_{13} \omega_9^2 - 33\omega_6^2 \omega_{13} c_s^2 \omega_9^2 + 84\omega_{13}^2 v_1^2 \omega_9 + 36\omega_6^2 \omega_{13} v_1^2 \omega_9 - 12\omega_6^2 \omega_9^2 - 48\omega_6 v_1^2 \omega_9^2 + 168\omega_6 \omega_{13} v_1^2 \omega_9^2 - 24\omega_6 \omega_{13} c_s^2 \omega_9 - 36\omega_6^2 \omega_{13}^2 c_s^2 - 72\omega_6 \omega_{13} \omega_9^2 + 24\omega_6 \omega_9^2 + 61\omega_6^2 \omega_{13} v_1^2 \omega_9 - 60\omega_{13} c_s^2 \omega_9^2 - 3\omega_6^2 \omega_{13}^2 c_s^2 \omega_9^2 + 36\omega_{13} \omega_9^2 + 2\omega_6^2 \omega_{13} \omega_9^2 - 25\omega_6^2 \omega_{13}^2 \omega_9 - 5\omega_6^2 \omega_{13} v_1^2 \omega_9^2 - 84\omega_{13} v_1^2 \omega_9^2 + 39\omega_6^2 \omega_{13}^2 c_s^2 \omega_9 - 48\omega_6 \omega_{13}^2 + 24\omega_6 \omega_{13} \omega_9 - 72\omega_6 \omega_{13} v_1^2 \omega_9 + 120\omega_6 \omega_{13}^2 v_1^2 + 120\omega_6 \omega_{13} c_s^2 \omega_9^2 - 48\omega_6 c_s^2 \omega_9^2) \frac{\rho v_1 v_3}{12\omega_6^2 \omega_{13}^2 \omega_9^2}$$

$$C_{D_x^3 v_1}^{(3), \text{MRT2}} = C_{D_x^3 v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(3), \text{CLBM1}} = (-4 + 10v_1^2 - 3c_s^2 \omega_9 + 6c_s^2 - 5v_1^2 \omega_9 + 2\omega_9) \frac{\rho v_1 v_3}{12\omega_9}$$

$$C_{D_x^3 v_1}^{(3), \text{CLBM2}} = C_{D_x^3 v_1}^{(3), \text{CLBM1}}$$

$$C_{D_x^3 v_1}^{(3), \text{CuLBM1}} = (-4 + 10v_1^2 - 3\omega_4 c_s^2 + 2\omega_4 - 5\omega_4 v_1^2 + 6c_s^2) \frac{\rho v_1 v_3}{12\omega_4}$$

$$C_{D_x^3 v_1}^{(3), \text{CuLBM2}} = (-15\omega_1 v_1^2 \omega_2 + 6\omega_1 \omega_2 - 4\omega_1 + 20v_1^2 \omega_2 + 6c_s^2 \omega_1 - 8\omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 + 10\omega_1 v_1^2) \frac{\rho v_1 v_3}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^4 v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^4}:$$

$$C_{D_x^4 v_3}^{(3), \text{SRT}} = (72v_1^2 - 3\omega^3 v_1^2 + 36c_s^2 \omega + 216c_s^2 \omega v_1^2 + c_s^2 \omega^3 + 42\omega^2 v_1^2 - 144c_s^2 v_1^2 - 14c_s^2 \omega^2 + 48c_s^4 + 108\omega v_1^4 - 42\omega^2 v_1^4 + 6c_s^2 \omega^3 v_1^2 - 108\omega v_1^2 - 72c_s^4 \omega - 24c_s^2 \omega + 3\omega^3 v_1^4 + 30c_s^4 \omega^2 - 72v_1^4 - 3c_s^4 \omega^3 - 84c_s^2 \omega^2 v_1^2) \frac{\rho}{24\omega^3}$$

$$C_{D_x^3 D_y \rho}^{(3), \text{CLBM1}} = 0$$

$$\begin{aligned}
& 18\omega_6\omega_{13}\omega_7\omega_{14}\omega_5^2\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} + 6\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_{12} + 36\omega_6\omega_{13}\omega_7c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_{12} + 24\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} - \\
& 12\omega_6^2\omega_{13}\omega_7\omega_8v_1^2\omega_5^2\omega_9\omega_{12} + 6\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5\omega_9\omega_{12} - 36\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_{12} + 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7c_s^2\omega_8^2\omega_5^2\omega_9\omega_{12} - \\
& 6\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8v_1^2\omega_5^2\omega_9\omega_{12} - 24\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_{12} - 6\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} - 54\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + \\
& 54\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 12\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_5^2\omega_9\omega_{12} + 12\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 12\omega_6^2\omega_{13}c_s^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9 - \\
& 12\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_9 - 18\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5\omega_9\omega_{12} + \\
& 12\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} + 12\omega_6\omega_{13}\omega_7^2c_s^2\omega_8^2\omega_5^2\omega_9\omega_{12} + 12\omega_6\omega_{13}\omega_7^2\omega_8^2\omega_5^2\omega_9\omega_{12} + 18\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 9\omega_6^2\omega_{13}\omega_7c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} + \\
& 6\omega_6^2\omega_{13}\omega_7^2\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} + 12\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} + 12\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5\omega_9\omega_{12} - 12\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9 + 30\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + \\
& 12\omega_6^2\omega_{13}\omega_7c_s^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 12\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 6\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 54\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + \\
& 12\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 3\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 12\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} - 12\omega_6^2\omega_{13}c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 12\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9 - \\
& 12\omega_6^2\omega_{13}\omega_7\omega_8\omega_5^2\omega_9\omega_{12} - 6\omega_6^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} - 12\omega_6\omega_{13}\omega_7^2\omega_8^2\omega_5^2\omega_9\omega_{12} - 6\omega_6^2\omega_{13}\omega_7\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} + 18\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} - \\
& 24\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 12\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2v_1^2\omega_5\omega_9 - 6\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9 + 12\omega_6^2\omega_{13}\omega_7\omega_8v_1^2\omega_5^2\omega_9\omega_{12} + 6\omega_6^2\omega_{13}\omega_7\omega_8v_1^2\omega_5^2\omega_9\omega_{12} + \\
& 12\omega_6\omega_{13}\omega_7^2\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12} - 54\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 12\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_9 + 9\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9 - \\
& 36\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 6\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 6\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_8^2\omega_5^2\omega_9\omega_{12} - 12\omega_6^2\omega_{13}\omega_7c_s^2\omega_{14}\omega_8^2\omega_5\omega_9 + 12\omega_6\omega_{13}\omega_7^2c_s^2\omega_8\omega_5^2\omega_9\omega_{12} + \\
& 12\omega_6^2\omega_{13}\omega_7\omega_8\omega_5^2\omega_9\omega_{12} + 36\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} + 12\omega_6^2\omega_{13}\omega_7c_s^2\omega_{14}\omega_5^2\omega_9\omega_{12} - 3\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2\omega_5^2\omega_9\omega_{12}) \frac{\rho v_1 v_3}{12\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}}
\end{aligned}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{MRT2}} = C_{D_x^3 D_y v_2}^{(3), \text{MRT1}}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CLBM1}} = (-\omega_9\omega_{12} + v_1^2\omega_9\omega_{12} + 3c_s^2\omega_9\omega_{12} - 9c_s^2\omega_9 + 3c_s^2\omega_{12} + v_1^2\omega_{12} - 3v_1^2\omega_9 + 3\omega_9 - \omega_{12}) \frac{\rho v_1 v_3}{12\omega_9\omega_{12}}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CLBM2}} = C_{D_x^3 D_y v_2}^{(3), \text{CLBM1}}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CuLBM1}} = (-9\omega_4c_s^2 - \omega_4\omega_9 + 3\omega_4 + \omega_4v_1^2\omega_9 + 3c_s^2\omega_9 - 3\omega_4v_1^2 + v_1^2\omega_9 - \omega_9 + 3\omega_4c_s^2\omega_9) \frac{\rho v_1 v_3}{12\omega_4\omega_9}$$

$$\begin{aligned}
C_{D_x^3 D_y v_2}^{(3), \text{CuLBM2}} &= (2\omega_3\omega_4\omega_1v_1^2 + 6\omega_3\omega_4c_s^2\omega_2 + 18\omega_3\omega_4c_s^2\omega_1\omega_2 + 9\omega_4\omega_1\omega_2 + 12\omega_3\omega_4c_s^2\omega_1 + 4\omega_3\omega_4v_1^2\omega_2 - 27\omega_4c_s^2\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - \\
& 6\omega_3\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 18\omega_3\omega_4v_2^2\omega_2 + 6\omega_3\omega_4\omega_1v_1^2\omega_2 + 9\omega_3\omega_1\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 + 2\omega_3\omega_4\omega_2 + 18\omega_3\omega_4\omega_1v_2^2) \frac{\rho v_1 v_3}{72\omega_3\omega_4\omega_1\omega_2}
\end{aligned}$$

$$\text{coefficient } C_{D_x^3 D_y v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^3 \partial x_2} :$$

$$C_{D_x^3 D_y v_3}^{(3), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^3 D_y v_3}^{(3), \text{MRT1}} &= (-\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2 + 4\omega_6^2\omega_{13}\omega_7c_s^2\omega_{14}\omega_8 - 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2v_1^2 + \omega_6^3\omega_7^2\omega_{14}\omega_8^2v_1^2 + 2\omega_6^3\omega_{13}\omega_7\omega_8v_1^2 - 2\omega_6^2\omega_{13}c_s^2\omega_{14}\omega_8^2 - \\
& 6\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2 - 2\omega_6^3\omega_{13}\omega_7\omega_8 + 2\omega_6^2\omega_{13}\omega_7^2\omega_8v_1^2 + \omega_6^3\omega_{13}\omega_7^2\omega_8^2v_1^2 - 2\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{14} - \omega_6^3\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2 + \omega_6^3\omega_{13}\omega_7^2c_s^2\omega_8^2 + \\
& 5\omega_6^3\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8 - 2\omega_6^2\omega_{13}\omega_7^2\omega_8^2 + \omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2v_1^2 + \omega_6^3\omega_{13}\omega_7^2\omega_8^2 + \omega_6^3\omega_7^2c_s^2\omega_{14}\omega_8^2 - 2\omega_6^2\omega_{13}\omega_7c_s^2\omega_{14}\omega_8^2 - \omega_6^3\omega_{13}\omega_7\omega_{14}\omega_8^2v_1^2 + \omega_6^3\omega_{13}\omega_7\omega_8^2 + \\
& 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_8 + 2\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_8 - \omega_6^3\omega_{13}\omega_7^2\omega_8^2 + 13\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2 + \omega_6^3\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^2\omega_{13}\omega_7^2\omega_8 + \\
& 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2 + 2\omega_6^3\omega_{13}\omega_7c_s^2\omega_8 + 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2 - \omega_6^3\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^2\omega_7^2c_s^2\omega_{14}\omega_8^2 - 11\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8 - \omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2 + \\
& 2\omega_6^3\omega_{13}c_s^2\omega_{14}\omega_8 + \omega_6^3\omega_{13}\omega_7\omega_{14}\omega_8 - \omega_6^3\omega_{13}\omega_7^2c_s^2\omega_8^2 - 7\omega_6^3\omega_{13}\omega_7c_s^2\omega_{14}\omega_8 - \omega_6^3\omega_{13}\omega_7^2\omega_8^2v_1^2 + \omega_6^3\omega_{13}\omega_7\omega_{14}\omega_8^2v_1^2 + \omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8 - \\
& 2\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2 + \omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2 + \omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 8\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2 - 2\omega_6^2\omega_7^2\omega_{14}\omega_8^2v_1^2 + 4\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2 + \\
& 2\omega_6^2\omega_{13}\omega_7^2\omega_8^2 - \omega_6^3\omega_{13}\omega_7c_s^2\omega_8^2 + 2\omega_6^3\omega_{13}\omega_7c_s^2\omega_{14} - 5\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2 - \omega_6^3\omega_{13}\omega_7\omega_8^2v_1^2 + \omega_6^3\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2 - 2\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_8^2 + \omega_6^3\omega_{13}\omega_7c_s^2\omega_{14}\omega_8^2 + \\
& 2\omega_6^2\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1^2 - 2\omega_6^2\omega_{13}\omega_7^2\omega_8^2v_1^2 + 2\omega_6^3\omega_{13}\omega_7^2\omega_8 + 6\omega_6\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8 + 2\omega_6^2\omega_{13}\omega_7^2c_s^2\omega_{14} - \omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2) \frac{\rho v_1 v_2}{2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2}
\end{aligned}$$

$$C_{D_x^3 D_y v_3}^{(3), \text{MRT2}} = C_{D_x^3 D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x^3 D_y v_3}^{(3), \text{CuLBM2}} &= (-18\omega_3^2\omega_4c_s^2 - 6\omega_3\omega_4\omega_1v_1^2 - 3\omega_3\omega_1v_2^2 + 18\omega_4^2c_s^2\omega_1 + 18\omega_3\omega_4^2c_s^2 - 2\omega_3\omega_4^2\omega_1v_2^2 + 6\omega_3^2\omega_4 - 6\omega_4^2v_1^2 - 18\omega_3\omega_4c_s^2\omega_1 - 2\omega_3^2\omega_4\omega_1 - \\
& 6\omega_3^2\omega_4v_2^2 + 6\omega_3^2v_2^2 + 2\omega_3^2\omega_4\omega_1v_2^2 + 2\omega_3\omega_4^2\omega_1 + 6\omega_3\omega_4^2v_2^2 + 12\omega_3\omega_4v_1^2 + 3\omega_4^2\omega_1v_1^2 - 6\omega_3^2v_1^2 - 6\omega_3\omega_4^2c_s^2\omega_1 + 6\omega_3\omega_4\omega_1 + 3\omega_4^2\omega_1v_2^2 - 6\omega_4^2\omega_1 - \\
& 6\omega_4^2v_2^2 - 12\omega_3\omega_4 + 12\omega_4^2 + 36\omega_3\omega_4c_s^2 + 6\omega_3^2\omega_4c_s^2\omega_1 - 6\omega_3\omega_4^2 + 3\omega_3^2\omega_1v_1^2 - 36\omega_4^2c_s^2) \frac{\rho v_1 v_2}{8\omega_3^2\omega_4^2\omega_1}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y \rho}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^4 v_3}{6\omega}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{MRT}^1} = (24\omega_6\omega_7^2\omega_8^2\omega_5 + 12\omega_6^2\omega_7^2\omega_8\omega_5^2 - 12\omega_6^2\omega_7^2\omega_5^2 - 12\omega_7^2\omega_8^2\omega_5 + 24\omega_6^2\omega_7\omega_8^2\omega_5 + 12\omega_6^2\omega_8\omega_5^2 + 12\omega_6^2\omega_7^2\omega_8^2 + 12\omega_6\omega_7^2\omega_5^2 - 12\omega_6^2\omega_7\omega_8^2 - 12\omega_6\omega_7^2\omega_8^2 - 24\omega_6\omega_7^2\omega_8\omega_5^2 - 14\omega_6^2\omega_7^2\omega_8^2\omega_5 + 12\omega_6^2\omega_7\omega_5^2 + \omega_6^2\omega_7^2\omega_8^2\omega_5^2 - 24\omega_6^2\omega_7\omega_8\omega_5^2 + 12\omega_7^2\omega_8\omega_5^2 - 12\omega_6^2\omega_8^2\omega_5^2) \frac{c_s^4 v_3}{6\omega_6^2\omega_7^2\omega_8^2\omega_5^2}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{MRT}^2} = C_{D_x^2 D_y^2 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CLBM}^1} = (-2 + \omega_5) \frac{c_s^4 v_3}{6\omega_5^2}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CLBM}^2} = C_{D_x^2 D_y^2 \rho}^{(3), \text{CLBM}^1}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CuLBM}^1} = (-2 + \omega_1) \frac{c_s^4 v_3}{6\omega_1^2}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CuLBM}^2} = (3\omega_1 v_2^2 - 3v_2^2\omega_2 - 2\omega_1 - 3v_1^2\omega_2 + 2c_s^2\omega_1 + 2\omega_2 - 14c_s^2\omega_2 + 6c_s^2\omega_1\omega_2 + 3\omega_1 v_1^2) \frac{c_s^2 v_3}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_1}^{(3)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{MRT}^1} = (2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_{12} - 4\omega_6\omega_7^2\omega_8^2\omega_5^2\omega_9\omega_{12} + 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12} + 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_9\omega_{12} - 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9 - 2\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9 - 4\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9 + 2\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 4\omega_6^2\omega_{13}\omega_7\omega_8\omega_5^2\omega_9\omega_{12} + 2\omega_6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 2\omega_6^2\omega_7^2\omega_8^2\omega_5^2\omega_9\omega_{12} - 4\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12} + 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 6\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 2\omega_6^2\omega_{13}\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 4\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2 - 4\omega_6\omega_{13}\omega_7^2\omega_8\omega_5^2\omega_9\omega_{12} + 2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} + 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5^2\omega_9 - 4\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_{12} - 2\omega_6^2\omega_{13}\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2\omega_5\omega_9 - 4\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9 - 4\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} - 2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8\omega_5\omega_9\omega_{12} - 3\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5\omega_9\omega_{12} + 3\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9 + 4\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2) \frac{c_s^2 \rho v_1 v_3}{2\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}}$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{MRT}^2} = C_{D_x^2 D_y^2 v_1}^{(3), \text{MRT}^1}$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CLBM}^1} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CLBM}^2} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CuLBM}^1} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CuLBM}^2} = (-\omega_1 - v_1^2\omega_2 + 3c_s^2\omega_1 + \omega_2 - 3c_s^2\omega_2 + \omega_1 v_1^2) \frac{\rho v_1 v_3}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{MRT}^1} = (4\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_8\omega_5^2\omega_{15} + 4\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5 + 2\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6\omega_{16}\omega_{10}\omega_7^2\omega_8^2\omega_5^2\omega_{15} - 2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5 + 4\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 4\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_8\omega_5^2\omega_{15} - 2\omega_6\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5\omega_{15} + 2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5^2\omega_{15} - 4\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5\omega_{15} - 2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5\omega_{15} - 4\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 4\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5 - 4\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_{15} + 2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5^2\omega_{15} - 2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5 - 4\omega_6\omega_{16}\omega_{10}\omega_7^2\omega_8\omega_5^2\omega_{15} - 2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_8\omega_5\omega_{15} + 6\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5\omega_{15} + 2\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5\omega_{15} - 3\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6^2\omega_{10}\omega_7^2\omega_8^2\omega_5^2\omega_{15} - 6\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} - 4\omega_6\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_{15} + 3\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5^2) \frac{c_s^2 \rho v_2 v_3}{2\omega_6^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}}$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{MRT}^2} = C_{D_x^2 D_y^2 v_2}^{(3), \text{MRT}^1}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{SRT}} = 0$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{MRT1}} = (-2\omega_6^2 \omega_{16}^2 \omega_7^3 c_s^2 \omega_{17} - 7\omega_6 \omega_{16}^2 \omega_7^3 c_s^2 \omega_{17} \omega_8 + 2\omega_6^2 \omega_{16} \omega_7^2 c_s^2 \omega_8^2 - \omega_6^2 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8^2 v_2^2 - \omega_6^2 \omega_7^3 \omega_{17} \omega_8^2 - 11\omega_6^2 \omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} \omega_8 - \omega_6^2 \omega_{16}^2 \omega_7^3 \omega_8^2 + 2\omega_6 \omega_{16}^2 \omega_7^3 c_s^2 \omega_8^2 v_2^2 - \omega_6 \omega_{16}^2 \omega_7^3 c_s^2 \omega_8^2 + 7\omega_6 \omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} \omega_8^2 + \omega_6 \omega_{16}^2 \omega_7^3 \omega_{17} \omega_8 - 2\omega_6^2 \omega_{16}^2 \omega_7^3 \omega_8^2 v_2^2 - 2\omega_6^2 \omega_{16}^2 \omega_7^2 \omega_8 - \omega_6^2 \omega_{16} \omega_7^3 c_s^2 \omega_{17} \omega_8^2 - \omega_6^2 \omega_{16}^2 \omega_7 \omega_{17} \omega_8^2 + \omega_6^2 \omega_{16}^2 \omega_7^3 c_s^2 \omega_8^2 - 8\omega_6^2 \omega_{16}^2 c_s^2 \omega_{17} \omega_8^2 - 2\omega_6 \omega_{16} \omega_7^2 c_s^2 \omega_{17} \omega_8^2 - \omega_6^2 \omega_{16}^2 \omega_7^3 \omega_{17} \omega_8 + \omega_6 \omega_{16} \omega_7^3 \omega_{17} \omega_8^2 v_2^2 + 2\omega_6 \omega_{16}^2 \omega_7^3 c_s^2 \omega_{17} + 4\omega_6^2 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 v_2^2 + 2\omega_6 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 + 2\omega_{16}^2 \omega_7^3 c_s^2 \omega_{17} \omega_8 + \omega_6 \omega_{16} \omega_7^3 c_s^2 \omega_{17} \omega_8^2 + 4\omega_6^2 \omega_{16} \omega_7^2 c_s^2 \omega_{17} \omega_8^2 + 2\omega_6^2 \omega_{16}^2 \omega_7^3 \omega_8^2 - \omega_6^2 \omega_{16} \omega_7^3 \omega_{17} \omega_8^2 v_2^2 - 2\omega_6^2 \omega_{16}^2 \omega_7^3 c_s^2 \omega_8 - \omega_6^2 \omega_{16} \omega_7^3 \omega_8^2 v_2^2 - 2\omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} \omega_8^2 - 2\omega_6 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 v_2^2 + 5\omega_6^2 \omega_{16}^2 \omega_7^3 c_s^2 \omega_{17} \omega_8 + 2\omega_6 \omega_{16}^2 \omega_7^3 c_s^2 \omega_8 + \omega_6 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8^2 v_2^2 + 4\omega_6 \omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} \omega_8 - 2\omega_6^2 \omega_{16}^2 \omega_7^2 \omega_8^2 v_2^2 - 4\omega_6^2 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 - 5\omega_6^2 \omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} \omega_8^2 + 2\omega_6^2 \omega_{16}^2 \omega_7^3 \omega_8 + \omega_6^2 \omega_{16}^2 \omega_7^3 \omega_{17} \omega_8 v_2^2 - 6\omega_6 \omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} \omega_8^2 + \omega_6^2 \omega_{16}^2 \omega_7 \omega_{17} \omega_8^2 v_2^2 + 6\omega_6^2 \omega_{16}^2 \omega_7 c_s^2 \omega_{17} \omega_8 + 2\omega_6^2 \omega_{16}^2 \omega_7^2 \omega_8^2 v_2^2 + \omega_6 \omega_{16}^2 \omega_7^3 \omega_8^2 + \omega_6^2 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8^2 - 2\omega_6^2 \omega_{16}^2 \omega_7^2 \omega_8^2 v_2^2 + 2\omega_6^2 \omega_{16}^2 \omega_7^2 c_s^2 \omega_{17} + 2\omega_6^2 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8^2 + 2\omega_6^2 \omega_{16} \omega_7 \omega_{17} \omega_8^2 + \omega_6^2 \omega_{16}^2 c_s^2 \omega_{17} \omega_8^2 + \omega_6^2 \omega_{16} \omega_7^3 \omega_8^2 + \omega_6^2 \omega_{16} \omega_7^3 \omega_{17} \omega_8^2 + \omega_6^2 \omega_{16}^2 \omega_7^3 \omega_8^2 v_2^2 + \omega_6^2 \omega_7^3 \omega_{17} \omega_8^2 v_2^2 - 2\omega_6^2 \omega_7^2 c_s^2 \omega_{17} \omega_8^2 - 2\omega_6^2 \omega_{16} \omega_7 c_s^2 \omega_{17} \omega_8^2 - \omega_6 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8^2 + 13\omega_6^2 \omega_{16}^2 \omega_7 c_s^2 \omega_{17} \omega_8^2 - \omega_6 \omega_{16}^2 \omega_7^3 \omega_{17} \omega_8^2 v_2^2 - 2\omega_6 \omega_{16}^2 \omega_7^3 \omega_8 + 2\omega_6 \omega_{16} \omega_7^2 \omega_8^2 v_2^2 + \omega_6^2 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8 + 2\omega_6^2 \omega_{16}^2 \omega_7^2 c_s^2 \omega_8 - \omega_6^2 \omega_{16}^2 \omega_7^2 \omega_{17} \omega_8 v_2^2 - \omega_6 \omega_{16}^2 \omega_7^3 \omega_8^2 v_2^2 - \omega_6 \omega_{16} \omega_7^3 \omega_{17} \omega_8^2) \frac{\rho v_1 v_2}{2\omega_6^2 \omega_{16}^2 \omega_7^3 \omega_{17} \omega_8^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{MRT2}} = C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{MRT1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_3}^{(3), \text{CuLBM2}} = (-18\omega_3^2 \omega_4 c_s^2 + 3\omega_3^2 \omega_1 v_2^2 + 18\omega_4^2 c_s^2 \omega_1 + 18\omega_3 \omega_4^2 c_s^2 + 6\omega_3^2 \omega_4 - 6\omega_4^2 v_1^2 - 18\omega_3 \omega_4 c_s^2 \omega_1 - 2\omega_3^2 \omega_4 \omega_1 - 6\omega_3^2 v_2^2 + 2\omega_3 \omega_4^2 \omega_1 + 3\omega_4^2 \omega_1 v_1^2 + 6\omega_3^2 v_1^2 - 6\omega_3 \omega_4^2 c_s^2 \omega_1 + 2\omega_3^2 \omega_4 \omega_1 v_1^2 + 6\omega_3 \omega_4^2 v_1^2 + 12\omega_3 \omega_4 v_2^2 + 6\omega_3 \omega_4 \omega_1 + 3\omega_4^2 \omega_1 v_2^2 - 6\omega_4^2 \omega_1 - 6\omega_4^2 v_2^2 - 12\omega_3 \omega_4 + 12\omega_4^2 - 6\omega_3^2 \omega_4 v_1^2 + 36\omega_3 \omega_4 c_s^2 + 6\omega_3^2 \omega_4 c_s^2 \omega_1 - 6\omega_3 \omega_4^2 - 2\omega_3 \omega_4^2 \omega_1 v_1^2 - 3\omega_3^2 \omega_1 v_1^2 - 6\omega_3 \omega_4 \omega_1 v_2^2 - 36\omega_4^2 c_s^2) \frac{\rho v_1 v_2}{8\omega_3^2 \omega_4^2 \omega_1}$$

$$\text{coefficient } C_{\mathbf{D}_y^4}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_2^4} :$$

$$C_{\mathbf{D}_y^4}^{(3), \text{SRT}} = (c_s^2 \omega + 6v_2^4 + 3\omega v_2^2 + 2c_s^4 - 3\omega v_2^4 + 24c_s^2 v_2^2 - c_s^4 \omega - 2c_s^2 - 6v_2^2 - 12c_s^2 \omega v_2^2) \frac{v_3}{24\omega}$$

$$C_{\mathbf{D}_y^4}^{(3), \text{MRT1}} = (-432\omega_{16}^2 \omega_{10} \omega_7 c_s^2 v_2^2 + 30\omega_{16} \omega_{10}^2 \omega_7^2 v_2^2 + 288\omega_{16}^2 \omega_7 c_s^2 v_2^2 - 14\omega_{16}^2 \omega_{10} \omega_7^2 c_s^2 + 12\omega_{16}^2 \omega_7^2 c_s^2 - \omega_{16}^2 \omega_{10}^2 \omega_7^2 c_s^4 - 48\omega_{16} \omega_{10}^2 v_2^4 + 24\omega_{16} \omega_{10} \omega_7^2 v_2^4 + 12\omega_{10}^2 \omega_7^2 c_s^4 + 24\omega_{10}^2 \omega_7 c_s^2 + 48\omega_{16} \omega_{10} \omega_7 v_2^2 + 96\omega_{16} \omega_{10}^2 \omega_7 v_2^4 - 144\omega_{16} \omega_{10} \omega_7 c_s^2 v_2^2 + 24\omega_{16}^2 \omega_7 c_s^4 + 48\omega_{16}^2 \omega_{10} v_2^4 - 48\omega_{16}^2 \omega_{10} \omega_7 c_s^4 + 12\omega_{10}^2 \omega_7^2 v_2^4 + 72\omega_{10}^2 \omega_7^2 c_s^2 v_2^2 - 24\omega_{16} \omega_{10}^2 c_s^4 - 3\omega_{16}^2 \omega_{10}^2 \omega_7^2 v_2^4 - 36\omega_{16}^2 \omega_{10} \omega_7^2 v_2^2 - 12\omega_{16}^2 \omega_{10}^2 \omega_7^2 c_s^2 v_2^2 + 36\omega_{16}^2 \omega_7^2 v_2^2 + 12\omega_{16} \omega_{10}^2 \omega_7^2 c_s^2 + 72\omega_{16}^2 \omega_7 v_2^4 - 96\omega_{16}^2 \omega_{10} \omega_7 v_2^4 - 126\omega_{16} \omega_{10}^2 \omega_7^2 c_s^2 v_2^2 + 24\omega_{16}^2 \omega_{10} c_s^4 + 48\omega_{16} \omega_{10}^2 \omega_7 c_s^4 + 24\omega_{10}^2 \omega_7^2 v_2^2 + 36\omega_{16}^2 \omega_{10} \omega_7^2 v_2^4 - 144\omega_{10}^2 \omega_7^2 c_s^2 v_2^2 - 36\omega_{16}^2 \omega_7^2 v_2^2 - 12\omega_{16} \omega_{10}^2 \omega_7^2 c_s^4 - 12\omega_{10}^2 \omega_7^2 v_2^2 + 24\omega_{16} \omega_{10}^2 c_s^2 + 3\omega_{16}^2 \omega_{10}^2 \omega_7^2 v_2^2 - 24\omega_{10}^2 \omega_7 v_2^4 + 432\omega_{16} \omega_{10}^2 \omega_7 c_s^2 v_2^2 - 72\omega_{16}^2 \omega_7 v_2^2 + 216\omega_{16}^2 \omega_{10} c_s^2 v_2^2 + 96\omega_{16}^2 \omega_{10} \omega_7 v_2^2 - 24\omega_{16}^2 \omega_{10} c_s^2 - 48\omega_{16} \omega_{10}^2 \omega_7 c_s^2 + \omega_{16}^2 \omega_{10}^2 \omega_7^2 c_s^2 - 144\omega_{16}^2 \omega_7^2 c_s^2 v_2^2 + 48\omega_{16} \omega_{10}^2 v_2^2 - 12\omega_{10}^2 \omega_7^2 c_s^2 - 24\omega_{16} \omega_{10} \omega_7^2 v_2^2 + 150\omega_{16}^2 \omega_{10} \omega_7^2 c_s^2 v_2^2 - 30\omega_{16} \omega_{10}^2 \omega_7^2 v_2^4 + 14\omega_{16} \omega_{10} \omega_7^2 c_s^4 - 12\omega_{16}^2 \omega_7^2 c_s^4 - 96\omega_{16} \omega_{10}^2 \omega_7 v_2^2 - 216\omega_{16} \omega_{10}^2 c_s^2 v_2^2 - 24\omega_{16}^2 \omega_7 c_s^2 - 48\omega_{16}^2 \omega_{10} v_2^2 + 48\omega_{16}^2 \omega_{10} \omega_7 c_s^2 - 48\omega_{16} \omega_{10} \omega_7 v_2^4 - 24\omega_{10}^2 \omega_7 c_s^4 + 72\omega_{16} \omega_{10} \omega_7^2 c_s^2 v_2^2) \frac{v_3}{24\omega_{16}^2 \omega_{10}^2 \omega_7^2}$$

$$C_{\mathbf{D}_y^4}^{(3), \text{MRT2}} = C_{\mathbf{D}_y^4}^{(3), \text{MRT1}}$$

$$C_{\mathbf{D}_y^4}^{(3), \text{CLBM1}} = (6v_2^4 - 3\omega_{10} v_2^4 - \omega_{10} c_s^4 + 2c_s^4 + \omega_{10} c_s^2 + 24c_s^2 v_2^2 - 12\omega_{10} c_s^2 v_2^2 - 2c_s^2 - 6v_2^2 + 3\omega_{10} v_2^2) \frac{v_3}{24\omega_{10}}$$

$$C_{\mathbf{D}_y^4}^{(3), \text{CLBM2}} = C_{\mathbf{D}_y^4}^{(3), \text{CLBM1}}$$

$$C_{\mathbf{D}_y^4}^{(3), \text{CuLBM1}} = (c_s^2 \omega_5 + 6v_2^4 + 3\omega_5 v_2^2 + 2c_s^4 - 12c_s^2 \omega_5 v_2^2 - c_s^4 \omega_5 + 24c_s^2 v_2^2 - 2c_s^2 - 6v_2^2 - 3\omega_5 v_2^4) \frac{v_3}{24\omega_5}$$

$$C_{\mathbf{D}_y^4}^{(3), \text{CuLBM2}} = (-6\omega_1 v_2^2 - 9\omega_1 v_2^4 \omega_2 + 2c_s^4 \omega_1 - 12v_2^2 \omega_2 + 4c_s^4 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 9\omega_1 v_2^2 \omega_2 + 24c_s^2 \omega_1 v_2^2 - 2c_s^2 \omega_1 + 12v_2^4 \omega_2 - 4c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 36c_s^2 \omega_1 v_2^2 \omega_2 + 48c_s^2 v_2^2 \omega_2 + 6\omega_1 v_2^4) \frac{v_3}{72\omega_1 \omega_2}$$

$$\text{coefficient } C_{\mathbf{D}_y^2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^2} :$$

$$C_{\mathbf{D}_y^2}^{(3), \text{SRT}} = (-4 - 3c_s^2 \omega - 5\omega v_2^2 + 2\omega + 6c_s^2 + 10v_2^2) \frac{\rho v_2 v_3}{12\omega}$$

$$C_{\mathbf{D}_y^2}^{(3), \text{MRT1}} = (-51\omega_{16} \omega_{10}^2 \omega_7^2 v_2^2 + 39\omega_{16}^2 \omega_{10} \omega_7^2 c_s^2 - 12\omega_{16} \omega_{10} \omega_7^2 + 36\omega_{16} \omega_{10}^2 - 36\omega_{16}^2 \omega_7^2 c_s^2 + 2\omega_{16}^2 \omega_{10}^2 \omega_7^2 - 12\omega_{10}^2 \omega_7^2 - 48\omega_{10}^2 \omega_7 c_s^2 - 72\omega_{16} \omega_{10} \omega_7 v_2^2 + 61\omega_{16}^2 \omega_{10} \omega_7^2 v_2^2 + 24\omega_{10}^2 \omega_7 - 60\omega_{16}^2 \omega_7^2 v_2^2 - 33\omega_{16} \omega_{10}^2 \omega_7^2 c_s^2 - 24\omega_{16} \omega_{10} \omega_7 c_s^2 - 48\omega_{10}^2 \omega_7 v_2^2 + 24\omega_{16} \omega_{10} \omega_7 + 12\omega_{16} \omega_{10} \omega_7^2 c_s^2 +$$

coefficient $C_{D_x^3 D_z v_1}^{(3)}$ at $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z v_1}^{(3), \text{SRT}} = (-12 + 36v_1^2 - 6\omega^2 - c_s^2\omega^3 + 18\omega^2v_1^2 + 2c_s^2\omega^2 + 18\omega - 54\omega v_1^2) \frac{c_s^2 \rho}{12\omega^3}$$

$$C_{D_x^3 D_z v_1}^{(3), \text{MRT1}} =$$

$$(-36\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_9^2 + 60\omega_6\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 - 48\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 - 12\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_9 - 6\omega_6^3\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 - 48\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 - 18\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_{18}\omega_9 + 12\omega_6\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}c_s^2v_3^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3\omega_9 + 48\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_9 - 12\omega_6^3\omega_{13}^2c_s^4\omega_{11}\omega_9^2 + 12\omega_6^2\omega_{13}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9 + 24\omega_6^2\omega_{22}\omega_{13}^2c_s^2v_3^2\omega_{18}\omega_9 - 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18} - 12\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 18\omega_6^3\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 + 18\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 + 30\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 + 36\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_9 + 36\omega_6^2\omega_{13}^2v_1^2v_3^2\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{11}v_3^2\omega_{18}\omega_9^2 + 6\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{13}^2c_s^4\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}^2v_3^2\omega_{18}\omega_9 + 36\omega_6^3\omega_{13}^2c_s^2v_1^2\omega_9^2 - 15\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9 + 18\omega_6\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 + 18\omega_6^3\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_9 + 144\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{13}c_s^4\omega_{11}\omega_{18}\omega_9^2 + 36\omega_6^2\omega_{22}\omega_{13}^2\omega_{11}v_3^2\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18} + 12\omega_6^2\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 - 108\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9 - 36\omega_6^3\omega_{13}\omega_{11}v_1^2v_3^2\omega_9^2 + 12\omega_6^3\omega_{13}^2c_s^2\omega_{11}\omega_9^2 - 24\omega_6^2\omega_{22}\omega_{13}c_s^2v_3^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{13}^2c_s^4\omega_9^2 - 6\omega_6^3\omega_{13}^2c_s^2v_3^2\omega_{18}\omega_9^2 + 5\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 - 36\omega_6^3\omega_{22}\omega_{13}^2c_s^2v_1^2\omega_9 + 60\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9 + 24\omega_6^2\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{13}^2v_3^2\omega_{18}\omega_9^2 + 15\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 - 36\omega_6^3\omega_{22}\omega_{13}v_1^2v_3^2\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 + 6\omega_6^2\omega_{22}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 - 36\omega_6\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 + 36\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_9 + 6\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 + \omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{22}\omega_{13}^2v_3^2\omega_{18}\omega_9 - 24\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}^2c_s^4\omega_9 - 12\omega_6^2\omega_{13}^2c_s^2\omega_{11}\omega_9^2 - 18\omega_6^3\omega_{13}^2c_s^2v_1^2\omega_{18}\omega_9^2 - 12\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{11}v_3^2\omega_{18}\omega_9^2 + 18\omega_6^2\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9 - 24\omega_6\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9 + 27\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18} - 18\omega_6^3\omega_{13}^2v_1^2v_3^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 - 15\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 - 45\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}^2v_3^2\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}^2c_s^2v_1^2\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_9 + 12\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_9 + 12\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 + 36\omega_6^2\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_9^2 - 12\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 - 18\omega_6^3\omega_{22}\omega_{13}v_1^2v_3^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{13}^2c_s^4\omega_{11}\omega_9^2 + 72\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9 - 12\omega_6^3\omega_{13}^2c_s^2\omega_9^2 - 18\omega_6^2\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2\omega_{13}^2c_s^2v_3^2\omega_9^2 - 12\omega_6^3\omega_{13}^2c_s^2\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_9^2 - 15\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 + 72\omega_6^2\omega_{22}\omega_{13}^2v_1^2v_3^2\omega_{18}\omega_9 - 72\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}v_3^2\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 + 9\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_{18} + 54\omega_6^2\omega_{22}\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9 - 5\omega_6^3\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_{18}\omega_9 + 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2v_3^2\omega_{18}\omega_9 + 36\omega_6^2\omega_{13}\omega_{11}v_1^2v_3^2\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_9 - 102\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 18\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_3^2\omega_{18} - 12\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_3^2\omega_9^2 - 5\omega_6^2\omega_{22}\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{13}^2c_s^4\omega_{11}\omega_{18}\omega_9^2 + 36\omega_6^3\omega_{13}^2c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{13}\omega_{11}v_3^2\omega_9^2 + 24\omega_6^2\omega_{22}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{13}^2c_s^2\omega_{11}\omega_{18}\omega_9^2 + 36\omega_6^3\omega_{22}\omega_{13}v_1^2v_3^2\omega_{18}\omega_9^2) \frac{c_s^2 \rho}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9}$$

$$C_{D_x^3 D_z v_1}^{(3), \text{MRT2}} = C_{D_x^3 D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^3 D_z v_1}^{(3), \text{CLBM1}} = (36\omega_6^3\omega_{13}v_1^2\omega_9 + 36\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2 - 12\omega_6^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^3\omega_{22}c_s^2\omega_{11}\omega_{18}\omega_9 + 6\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 54\omega_6^2\omega_{22}\omega_{11}v_1^2\omega_{18}\omega_9 - 36\omega_6^2\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9 - 12\omega_6^3\omega_{22}\omega_{13}\omega_{11} - 12\omega_6\omega_{22}\omega_{13}^2c_s^2\omega_{11}\omega_{18} - 6\omega_6^3c_s^2\omega_{11}\omega_{18}\omega_9 + 12\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11} - 6\omega_6^3\omega_{22}\omega_{11}\omega_{18}\omega_9 - 36\omega_6^2\omega_{22}\omega_{13}v_1^2 + 54\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} + \omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 36\omega_6^2\omega_{13}\omega_{11}v_1^2\omega_9 - 5\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 36\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} + 6\omega_6^3\omega_{13}\omega_{18}\omega_9 + 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18} - \omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 + 36\omega_6^2\omega_{11}v_1^2\omega_{18}\omega_9 + 12\omega_6^3\omega_{22}\omega_{13} - 12\omega_6^3\omega_{22}\omega_{13}c_s^2 - 12\omega_6^3\omega_{13}\omega_9 - 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9 - 15\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} - 6\omega_6^3\omega_{13}^2c_s^2\omega_{18}\omega_9 + 5\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18} + 18\omega_6^3\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{11}v_1^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{13}c_s^2\omega_{11}\omega_9 - 12\omega_6^2\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 + 6\omega_6^3\omega_{11}\omega_{18}\omega_9 - 18\omega_6^2\omega_{22}c_s^2\omega_{11}\omega_{18}\omega_9 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{18} + 18\omega_6^2\omega_{22}\omega_{13}v_1^2\omega_{18} - 12\omega_6\omega_{22}\omega_{11}\omega_{18}\omega_9 - 5\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18} - 12\omega_6^2\omega_{11}\omega_{18}\omega_9 - 36\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2 + 12\omega_6\omega_{22}c_s^2\omega_{11}\omega_{18}\omega_9 - 36\omega_6^3\omega_{13}\omega_{11}v_1^2\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11} + 18\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2c_s^2\omega_{11}\omega_{18}\omega_9) \frac{c_s^2 \rho}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9}$$

$$C_{D_x^3 D_z v_1}^{(3), \text{CLBM2}} = C_{D_x^3 D_z v_1}^{(3), \text{CLBM1}}$$

$$C_{D_x^3 D_z v_1}^{(3), \text{CuLBM1}} = (-12\omega_4\omega_2 - 6\omega_2^2\omega_{12} - 5\omega_4c_s^2\omega_2^2\omega_{12} + 3v_1^2\omega_2^3\omega_{12} + 18\omega_4\omega_2^2 + 18v_1^2\omega_2^2\omega_{12} - \omega_4c_s^2\omega_2^3\omega_{12} - 6\omega_4\omega_2^3 - 12c_s^2\omega_2\omega_{12} - \omega_2^3\omega_{12} + \omega_4\omega_2^2\omega_{12} - 54\omega_4v_1^2\omega_2^2 - 36v_1^2\omega_2\omega_{12} - 6c_s^2\omega_2^3 + 12\omega_4c_s^2\omega_2 + 6c_s^2\omega_2^2\omega_{12} + 12c_s^2\omega_2^2 + 18\omega_4v_1^2\omega_2^3 + 12\omega_2\omega_{12} + c_s^2\omega_2^2\omega_{12} + 18\omega_4c_s^2\omega_2\omega_{12} + 6\omega_4c_s^2\omega_2^3 - 3\omega_4v_1^2\omega_2^2\omega_{12} + 36v_1^2\omega_2^2 + 6\omega_2^3 - 12\omega_4c_s^2\omega_{12} - 12\omega_2^2 + 36\omega_4v_1^2\omega_2 - 18v_1^2\omega_2^3 - 18\omega_4c_s^2\omega_2^2) \frac{c_s^2 \rho}{12\omega_4\omega_2^3\omega_{12}}$$

$$C_{D_x^3 D_z v_1}^{(3), \text{CuLBM2}} = (3\omega_3\omega_4c_s^2\omega_1^3\omega_2^3v_3^2 - 4\omega_3\omega_4\omega_1^2\omega_2^2 + 108\omega_3c_s^2\omega_1v_1^2\omega_2^3 + 144\omega_3\omega_4v_1^2\omega_2^3 + 81\omega_3\omega_4\omega_1^2v_1^2\omega_2^3 + 24\omega_4c_s^2\omega_1^3v_1^2\omega_2 + 144\omega_3\omega_4c_s^2\omega_1^3v_1^2 - 20\omega_3\omega_4c_s^2\omega_1^3 - 28\omega_3\omega_4c_s^4\omega_1\omega_2^2 + 84\omega_3\omega_4\omega_1^2v_1^2\omega_2^2 - 7\omega_3\omega_4\omega_1^2\omega_2^3 + 24\omega_4c_s^2\omega_1v_1^2\omega_2^3 - 10\omega_3\omega_4\omega_1^3\omega_2 - 36\omega_3c_s^2\omega_1\omega_2^3 + 120\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2 + 94\omega_3\omega_4c_s^4\omega_1\omega_2^3 + 138\omega_3\omega_4\omega_1^3v_1^4\omega_2^2 - 8\omega_4c_s^2\omega_1\omega_2^3 - \omega_3\omega_4\omega_1^2\omega_2^3v_4^2 - 240\omega_3\omega_4\omega_1^3v_1^4\omega_2 - 24\omega_3\omega_4\omega_1v_1^4\omega_2^2 + 27\omega_4c_s^2\omega_1^3v_1^2\omega_2^3 - 96\omega_3\omega_4\omega_1^2v_1^2\omega_2 + 32\omega_3\omega_4c_s^2\omega_1\omega_2^3 - 90\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 + 7\omega_3\omega_4\omega_1^3\omega_2^2 + 408\omega_3\omega_4\omega_1v_1^4\omega_2^3 + 36\omega_3c_s^4\omega_1\omega_2^3 - 153\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2^3 - 54\omega_3\omega_4c_s^2\omega_1\omega_2^3 + 40\omega_3\omega_4c_s^2\omega_2^3 + 8\omega_3\omega_4\omega_1^2\omega_2 - 54\omega_4c_s^2\omega_1^3v_1^2\omega_2^3 + 27\omega_3c_s^2\omega_1^3v_1^2\omega_2^3 - \omega_3\omega_4\omega_1^3\omega_2^3v_3^2 + 96\omega_3\omega_4\omega_1^3v_1^4 + 8\omega_4c_s^4\omega_1\omega_2^3 - 168\omega_3\omega_4\omega_1^2v_1^4\omega_2^2 - 9\omega_4c_s^2\omega_1^3\omega_2^3 - 3\omega_3\omega_4c_s^4\omega_1^3\omega_2^3 + 8\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 - 36\omega_3c_s^4\omega_1^3\omega_2^3 + \omega_3\omega_4\omega_1^3\omega_2^3v_3^2 - 60\omega_3\omega_4c_s^2\omega_1v_1^2\omega_2^2 - 9\omega_3c_s^2\omega_1^3\omega_2^3 + 42\omega_3\omega_4c_s^2\omega_1^3\omega_2^3 + 24\omega_3\omega_4c_s^2\omega_1^3\omega_2^3 - 81\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 288\omega_3\omega_4c_s^2\omega_1^3v_1^2\omega_2^2 - 18\omega_4c_s^4\omega_1^3\omega_2^2 + 8\omega_4c_s^4\omega_1^3\omega_2^2 + 17\omega_3\omega_4c_s^4\omega_1^3\omega_2^2 - 264\omega_3\omega_4v_1^4\omega_2^3 + 18\omega_4c_s^2\omega_1^3\omega_2^2 - 8\omega_3\omega_4\omega_2^3 + \omega_3\omega_4\omega_1^3\omega_2^3v_3^2 -$$

$$60\omega_3\omega_4\omega_1^3v_1^2 - 138\omega_3\omega_4\omega_1v_1^4\omega_2^3 + 20\omega_4c_s^4\omega_1^2\omega_2^2 - 312\omega_3\omega_4c_s^2v_1^2\omega_2^3 + 16\omega_3\omega_4c_s^4\omega_1^3 - 6\omega_3\omega_4c_s^2\omega_1^2\omega_2^2 + 432\omega_3\omega_4c_s^2\omega_1v_1^2\omega_2^3 - 222\omega_3\omega_4\omega_1v_1^2\omega_2^3 + 9\omega_4c_s^4\omega_1^3\omega_2^3 - 16\omega_3\omega_4c_s^2\omega_1^2\omega_2^2 + 4\omega_3\omega_4\omega_1^3 + 60\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 - 108\omega_3c_s^2\omega_1^2v_1^2\omega_2^3 + 36\omega_3c_s^2\omega_1^2\omega_2^3 + 14\omega_3\omega_4\omega_1\omega_2^3 - 29\omega_3\omega_4c_s^4\omega_1^2\omega_2^3 + 9\omega_3c_s^4\omega_1^3\omega_2^3 - 68\omega_3\omega_4c_s^4\omega_2^3 - 32\omega_3\omega_4c_s^4\omega_1^3\omega_2 - 8\omega_4c_s^2\omega_1^3\omega_2 + 18\omega_4c_s^2\omega_1^2\omega_2^2 - 24\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2^2 + 138\omega_3\omega_4\omega_1^3v_1^2\omega_2 - 54\omega_4c_s^2\omega_1^2v_1^2\omega_2^3 + 153\omega_3\omega_4c_s^2\omega_1^2v_1^2\omega_2^2 - 3\omega_3\omega_4c_s^2\omega_1^2\omega_2^3 + 12\omega_3\omega_4\omega_1v_1^2\omega_2^2 - 18\omega_4c_s^4\omega_1^2\omega_2^2 + 192\omega_3\omega_4\omega_1^2v_1^4\omega_2 - 20\omega_4c_s^2\omega_1^2\omega_2^2 + 10\omega_3\omega_4c_s^4\omega_1^2\omega_2^2) \frac{\rho}{36\omega_3\omega_4\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_x^3 D_z v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^4 \partial x_3} :$$

$$C_{D_x^3 D_z v_3}^{(3), \text{SRT}} = (2 - 2v_1^2 + 3c_s^2\omega - \omega + \omega v_1^2 - 6c_s^2) \frac{\rho v_1 v_3}{12\omega}$$

$$C_{D_x^3 D_z v_3}^{(3), \text{MRT1}} = (-24\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{18}\omega_9^2 + 36\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}^2 - 24\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 84\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9 - 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 96\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{22}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}^2 - 24\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 4\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 3\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - \omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 24\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 72\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 36\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 66\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{22}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{18}\omega_9^2 + 12\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 90\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 66\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 36\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}^2 + 72\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^3\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 48\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^3\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 18\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 84\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 66\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 156\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{13}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 132\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 4\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 18\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + \omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 18\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 60\omega_6^2\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 48\omega_6^2\omega_{22}c_s^2\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 12\omega_6\omega_{22}\omega_{13}c_s^2\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 18\omega_6^3\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2) \frac{\rho v_1 v_3}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2}$$

$$C_{D_x^3 D_z v_3}^{(3), \text{MRT2}} = C_{D_x^3 D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^3 D_z v_3}^{(3), \text{CLBM1}} = (\omega_{13}v_1^2 - \omega_{13} + 3\omega_{13}c_s^2 + \omega_{13}v_1^2\omega_9 - 9c_s^2\omega_9 - \omega_{13}\omega_9 + 3\omega_{13}c_s^2\omega_9 - 3v_1^2\omega_9 + 3\omega_9) \frac{\rho v_1 v_3}{12\omega_{13}\omega_9}$$

$$C_{D_x^3 D_z v_3}^{(3), \text{CLBM2}} = C_{D_x^3 D_z v_3}^{(3), \text{CLBM1}}$$

$$C_{D_x^3 D_z v_3}^{(3), \text{CuLBM1}} = (-9\omega_4c_s^2 - \omega_4\omega_{12} + 3\omega_4 + \omega_4v_1^2\omega_{12} - 3\omega_4v_1^2 + 3c_s^2\omega_{12} + v_1^2\omega_{12} + 3\omega_4c_s^2\omega_{12} - \omega_{12}) \frac{\rho v_1 v_3}{12\omega_4\omega_{12}}$$

$$C_{D_x^3 D_z v_3}^{(3), \text{CuLBM2}} = (2\omega_3\omega_4\omega_1v_1^2 - 18\omega_3\omega_4\omega_2v_3^2 + 6\omega_3\omega_4c_s^2\omega_2 + 18\omega_3\omega_4c_s^2\omega_1\omega_2 + 9\omega_4\omega_1\omega_2 + 12\omega_3\omega_4c_s^2\omega_1 + 4\omega_3\omega_4v_1^2\omega_2 - 27\omega_4c_s^2\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 6\omega_3\omega_4\omega_1v_1^2\omega_2 + 9\omega_3\omega_1\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 + 18\omega_3\omega_4\omega_1v_3^2 + 2\omega_3\omega_4\omega_2) \frac{\rho v_1 v_3}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^2 D_y D_z \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} :$$

$$C_{D_x^2 D_y D_z \rho}^{(3), \text{SRT}} = (36\omega v_1v_2^2v_3^2 + 24c_s^2v_1^2v_2 + 36c_s^2\omega v_1v_3^2 + 14c_s^2\omega^2v_2v_3^2 + 36c_s^2\omega v_1v_2^2 - 36\omega v_1^2v_2v_3^2 + 24c_s^2v_2v_3^2 + 14c_s^2\omega^2v_1^2v_2 + c_s^2\omega^3v_1v_2^2 + c_s^2\omega^3v_1v_3^2 - 36c_s^2\omega v_1^2v_2 - 24c_s^2v_1v_3^2 - 24c_s^2v_1v_2^2 - 24v_1v_2^2v_3^2 - 14\omega^2v_1v_2^2v_3^2 + 14\omega^2v_1^2v_2v_3^2 - c_s^2\omega^3v_2v_3^2 + 24v_1^2v_2v_3^2 - 36c_s^2\omega v_2v_3^2 - 14c_s^2\omega^2v_1v_3^2 - 14c_s^2\omega^2v_1v_2^2 - \omega^3v_1^2v_2v_3^2 + \omega^3v_1v_2^2v_3^2 - c_s^2\omega^3v_1^2v_2) \frac{1}{2\omega^3}$$

$$C_{D_x^2 D_y D_z \rho}^{(3), \text{MRT1}} = (2\omega_6^2\omega_{19}\omega_{13}\omega_7\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2v_3\omega_{18} - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{14}\omega_8^2v_2v_3^2 - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8v_1v_2^2\omega_{18} + 2\omega_6^3\omega_{19}\omega_{13}\omega_7^2\omega_{20}\omega_{14}\omega_8^2v_1^2v_2v_3^2 - 2\omega_6^2\omega_{22}\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1^2v_2\omega_{18} - \omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2\omega_{20}\omega_{14}\omega_8^2v_1v_3^2\omega_{18} + 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2\omega_{11}\omega_{14}\omega_8v_1v_2^2v_3^2\omega_{18} + 2\omega_6^2\omega_{22}\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8^2v_2v_2^2\omega_{18} + \omega_6^3\omega_{22}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{14}\omega_8^2v_1v_3^2\omega_{18} - 2\omega_6^3\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{14}\omega_8^2v_1v_2^2 - \omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8^2v_1v_2^2\omega_{18} + 4\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7c_s^2\omega_{20}\omega_{11}\omega_{14}v_2\omega_{18} + 2\omega_6^2\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_2v_3^2\omega_{18} + 2\omega_6^2\omega_{22}\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2\omega_{14}\omega_8^2v_1v_2^2v_3^2 + 2\omega_6^3\omega_{22}\omega_{13}\omega_7^2c_s^2\omega_{11}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} + \omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{14}\omega_8^2v_1^2v_2\omega_{18} - \omega_6^3\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} + 2\omega_6^2\omega_{22}\omega_{19}\omega_{13}\omega_7^2\omega_{14}\omega_8v_1v_2^2\omega_{18} + 2\omega_6^2\omega_{22}\omega_{19}\omega_{13}\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8v_1v_2^2v_3^2\omega_{18} - \omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_3^2\omega_{18} - 2\omega_6^2\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2 - 2\omega_6^2\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8v_1v_3^2\omega_{18} - 2\omega_6^2\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8v_1v_3^2\omega_{18} - 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8v_1v_2^2v_3^2\omega_{18} + \omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_8v_1^2v_2\omega_{18} + 2\omega_6^3\omega_{22}\omega_{13}\omega_7^2c_s^2\omega_{14}\omega_8^2v_2v_3^2\omega_{18} + 2\omega_6^2\omega_{22}\omega_{19}\omega_7^2c_s^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2v_1v_2^2\omega_{18} + 2\omega_6^3\omega_{22}\omega_{19}\omega_{13}\omega_7c_s^2\omega_{20}\omega_{11}\omega_8v_1^2v_2\omega_{18} -$$

[illegible]

$$\begin{aligned}
C_{D_x^2 D_y D_z \rho}^{(3), \text{CLBMM2}} &= C_{D_x^2 D_y D_z \rho}^{(3), \text{CLBMM1}} \\
C_{D_x^2 D_y D_z \rho}^{(3), \text{CuLBMM1}} &= 0 \\
C_{D_x^2 D_y D_z \rho}^{(3), \text{CuLBMM2}} &= (-252\omega_4^2 c_s^4 \omega_1^2 \omega_2^3 - 40\omega_3^2 \omega_4^2 c_s^3 \omega_1^3 v_2^2 \omega_2 + 54\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 + 864\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 8\omega_3 \omega_4^2 c_s^2 \omega_1^3 \omega_2 - 56\omega_3^2 \omega_4^2 c_s^2 \omega_1 v_2^2 \omega_2^3 - \\
&108\omega_3 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 30\omega_3^2 \omega_4^4 c_s^4 \omega_1^3 \omega_2^3 - 81\omega_3 \omega_4^4 c_s^4 \omega_1^3 \omega_2^3 - 176\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 324\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 + 432\omega_3^2 \omega_4^2 c_s^2 v_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1^3 v_2^2 - 84\omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - \\
&54\omega_4^2 c_s^2 \omega_1^3 \omega_2^3 + 8\omega_3^2 \omega_4^2 c_s^4 \omega_1 v_2^2 \omega_2^3 - 104\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 64\omega_3 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 - 72\omega_3^2 \omega_4^4 c_s^4 \omega_1 v_1^4 \omega_2 + 72\omega_3^2 \omega_4^2 \omega_1^3 v_1^4 \omega_2 + 48\omega_3^2 \omega_4^4 \omega_1^3 v_1^2 \omega_2 + \\
&48\omega_3^2 \omega_4^2 v_1^4 v_2^2 \omega_2^3 + 72\omega_3^2 \omega_4^2 v_1^2 v_2^2 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^2 v_2^2 \omega_2 + 24\omega_4^2 c_s^2 \omega_1^3 v_2^2 \omega_2 + 108\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2 + 112\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2 + 10\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 - 27\omega_3 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - \\
&104\omega_3^2 \omega_2^2 c_s^2 \omega_1^3 \omega_2^3 - 16\omega_3^2 \omega_4^2 \omega_1^2 v_2^2 \omega_2^3 - 60\omega_3^2 \omega_4^2 \omega_1 v_1^2 v_2^2 \omega_2^3 + 84\omega_4^2 c_s^2 \omega_1^3 \omega_2^3 - 56\omega_3 \omega_4^2 c_s^2 \omega_1 v_2^2 \omega_2^3 + 96\omega_3^2 \omega_4^2 \omega_1 v_1^2 \omega_2^3 - 10\omega_3^2 \omega_2^2 c_s^2 \omega_1^2 \omega_2^3 + \\
&324\omega_3 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 - 162\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 - 24\omega_3^2 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 + 96\omega_3^2 \omega_4^2 c_s^4 \omega_1 v_1^2 \omega_2^3 + 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 108\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 + 192\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 27\omega_3 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 - \\
&72\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2^3 - 162\omega_4^2 c_s^4 \omega_1^3 \omega_2^3 - 96\omega_3^2 \omega_4^2 v_1^2 v_2^2 \omega_2^3 + 32\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 8\omega_3 \omega_4^2 c_s^2 \omega_1^3 v_2^2 \omega_2 + 80\omega_3^2 \omega_2^2 c_s^2 \omega_1^2 \omega_2^3 + 192\omega_3 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 + 27\omega_3 \omega_4^2 c_s^2 \omega_1^3 v_2^2 \omega_2^3 + \\
&96\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2^3 - 162\omega_3^2 \omega_4^2 \omega_1 v_1^2 v_2^2 \omega_2^3 - 72\omega_4^2 c_s^4 \omega_1^3 \omega_2^3 + 10\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 v_2^2 \omega_2^3 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_1^2 \omega_2^3 - 30\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2 - \\
&168\omega_3^2 \omega_2^2 c_s^4 \omega_1^3 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_2^3 + 144\omega_3^2 \omega_4^2 c_s^4 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^3 v_2^2 \omega_2 - 24\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 v_2^2 \omega_2 - 24\omega_4^2 c_s^2 \omega_1^3 v_2^2 \omega_2^3 - 54\omega_3^2 c_s^2 \omega_1^3 v_2^2 \omega_2^3 + 108\omega_3 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - \\
&192\omega_3^2 \omega_4^2 \omega_1^2 v_1^2 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1 v_2^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 v_2^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 - 24\omega_3^2 \omega_4^2 c_s^4 \omega_1 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1 v_2^2 \omega_2^3 + 64\omega_3 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 + 108\omega_3 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 + \\
&54\omega_4^2 c_s^2 \omega_1^3 \omega_2^3 - 168\omega_3 \omega_4^2 c_s^4 \omega_1^3 \omega_2^3 - 216\omega_3^2 \omega_4^2 c_s^4 \omega_1 \omega_2^3 - 8\omega_3^2 \omega_4^2 c_s^2 \omega_1^3 v_2^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 + 81\omega_3^2 \omega_4^2 c_s^4 \omega_1^3 \omega_2^3 + 432\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + \\
&32\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1 v_1^2 \omega_2^3 - 36\omega_3^2 \omega_4^2 \omega_1 v_1^4 \omega_2^3 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 + 32\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 \omega_2^3 + 64\omega_3^2 \omega_4^2 c_s^2 \omega_1 \omega_2^3 - 108\omega_3^2 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - \\
&324\omega_3^2 \omega_4^2 c_s^4 \omega_1^2 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^3 + 144\omega_3^2 \omega_4^2 c_s^4 \omega_1^3 + 56\omega_3 \omega_4^2 c_s^2 \omega_1 \omega_2^3 - 60\omega_3^2 \omega_4^2 \omega_1 v_1^2 v_2^2 \omega_2^3 - 432\omega_3^2 \omega_4^2 c_s^2 \omega_1 v_1^2 \omega_2^3 - 10\omega_3 \omega_4^2 c_s^2 \omega_1^2 v_2^2 \omega_2^3 - \\
&36\omega_3^2 \omega_4^2 \omega_1 v_1^4 \omega_2 + 128\omega_3^2 \omega_4^2 c_s^2 \omega_1 \omega_2^3 + 120\omega_3^2 \omega_4^2 \omega_1 v_1^2 v_2^2 \omega_2^3 + 96\omega_3^2 \omega_4^2 \omega_1 v_1^2 \omega_2 - 96\omega_3^2 \omega_4^2 \omega_1 v_1 - 27\omega_3 \omega_4^2 c_s^2 \omega_1^3 \omega_2^3 + 24\omega_3^2 \omega_4^2 v_1^4 \omega_2^3) \frac{v_2}{72\omega_3^2 \omega_4^2 \omega_1^3 \omega_2^3}
\end{aligned}$$

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$$C_{D_x^2 D_y D_z v_1}^{(3), \text{SRT}} = (-14c_s^2 \omega^2 v_3^2 - 2\omega^3 v_1 v_2 v_3^2 - 14c_s^2 \omega^2 v_2^2 - 24v_2^2 v_3^2 - 2c_s^2 \omega^3 v_1 v_2 + \omega^3 v_2^2 v_3^2 + c_s^2 \omega^3 v_2^2 + 36\omega v_2^2 v_3^2 + c_s^2 \omega^3 v_3^2 - 72c_s^2 \omega v_1 v_2 + 48v_1 v_2 v_3^2 + 28\omega^2 v_1 v_2 v_3^2 - 14\omega^2 v_2^2 v_3^2 + 28c_s^2 \omega^2 v_1 v_2 - 24c_s^2 v_3^2 - 24c_s^2 v_2^2 + 48c_s^2 v_1 v_2 - 72\omega v_1 v_2 v_3^2 + 36c_s^2 \omega v_3^2 + 36c_s^2 \omega v_2^2) \frac{\rho}{2\omega_3}$$

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$$\begin{aligned}
C(3, MRT_1) &= (12w_6w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8w_5^2v_2^2w_{18} - 24w_6^3w_{16}w_7^2w_{23}w_{17}w_{11}w_8^2v_{15}w_5^2v_3^2w_{18} - 24w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{17}w_{18}w_5^2v_3 - \\
D_{x_1}D_{y_1}D_{z_1}v_1 &= 24w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} - 6w_6^2w_{19}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} + 12w_6^2w_{19}w_{16}w_7^2w_{23}c_5^2w_{17}w_{11}w_8w_5^2v_2^2w_{18} - \\
&12w_6^2w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} - 60w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8w_5^2v_3^2w_{18} - 12w_6^3w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5w_{18} - \\
&24w_6^3w_{19}w_{16}w_7^2w_{23}w_{17}w_8^2v_{15}w_5^2v_2^2v_3 + 12w_6^2w_{19}w_{16}w_7^2w_{23}c_5^2w_{17}w_{11}w_8^2w_5^2v_2^2 + 12w_6^2w_{16}w_7^2w_{23}w_{17}w_8^2w_5^2v_2^2v_3w_{18} + \\
&12w_6^2w_{19}w_{16}w_7^2w_{23}c_5^2w_{17}w_{11}w_8^2w_5^2 + 24w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} - 12w_6^3w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} + \\
&12w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{17}w_{11}w_8w_5^2v_2^2v_3w_{18} - 24w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_3w_{18} - 24w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} - \\
&12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} - 12w_6^3w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} + 6w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2v_3w_{18} + \\
&12w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{11}w_8w_5^2v_2^2v_3w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{17}w_8^2w_5^2v_2^2w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{11}w_8w_5^2v_3w_{18} - \\
&24w_6^3w_{16}w_7^2w_{23}w_{20}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} + 12w_6^3w_{16}w_7^2w_{23}c_5^2w_{20}w_{11}w_8^2w_5^2v_3w_{18} + 24w_6^3w_{19}w_{16}w_7^2w_{23}w_{17}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} + \\
&24w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{11}w_8v_{15}w_5^2v_2^2v_3w_{18} - 6w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} + 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_3 - \\
&24w_6^3w_{19}w_7^2w_{23}w_{20}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} - 18w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5w_{18} + 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} - \\
&12w_6^3w_{19}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} - 12w_6^3w_{16}w_7^2c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_3^2w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_3^2w_{18} - \\
&12w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{11}w_8^2w_5^2v_2^2v_3w_{18} - 24w_6^3w_{19}w_7^2c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} + 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_8^2w_5^2v_3^2w_{18} - \\
&12w_6^3w_{19}w_7^2w_{23}c_5^2w_{20}w_{11}w_8^2w_5^2v_2^2w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2 - 12w_6^3w_{16}w_7^2w_{23}c_5^2w_{17}w_8^2w_5^2w_{18} + \\
&12w_6^3w_{16}w_7^2w_{23}w_{20}w_{11}w_8^2w_5^2v_2^2v_3w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} - 12w_6^3w_{16}w_7^2c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} + \\
&6w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2 - 18w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_3w_{18} + 6w_6^3w_{19}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2v_3w_{18} - \\
&24w_6^3w_{19}w_{16}w_7^2w_{23}w_{17}w_{11}w_8v_{15}w_5^2v_2^2v_3w_{18} - 12w_6^3w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_3w_{18} + 12w_6^3w_{19}w_7^2w_{23}w_{20}w_{11}w_8^2w_5^2v_2^2w_{18} + \\
&24w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2w_5^2v_2^2v_3w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2w_5^2v_3w_{18} + \\
&24w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8v_{15}w_5^2v_2^2v_3w_{18} + 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8w_5^2v_3w_{18} - 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{11}w_8^2w_5^2v_2^2w_{18} + \\
&12w_6^3w_{19}w_{16}w_7^2w_{23}w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_2^2v_3w_{18} - 12w_6^3w_{19}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} + 24w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} - \\
&12w_6^3w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8^2v_3w_{18} + 24w_6^3w_{19}w_{16}w_7^2c_5^2w_{20}w_{17}w_{11}w_8^2v_{15}w_5^2v_3w_{18} + 12w_6^3w_{19}w_{16}w_7^2w_{23}c_5^2w_{20}w_{17}w_{11}w_8w_5^2w_{18} + \\
&24w$$

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$$C_{\text{D}_x \text{D}_y^2 \text{D}_z v_1}^{(3), \text{CLB} \text{M} 2} = C_{\text{D}_x \text{D}_y^2 \text{D}_z v_1}^{(3), \text{CLB} \text{M} 1}$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z v_1}^{(3), \text{CuLB} \text{M} 1} = (12\omega_2^3 \omega_1 \omega_2^2 + 12\omega_3 \omega_{13} \omega_2^2 - 6\omega_3^3 \omega_{13} \omega_2 + 12\omega_3^3 \omega_2^2 - 6\omega_3^2 \omega_{13} \omega_1 \omega_2 - \omega_3^3 \omega_{13} \omega_1 \omega_2^2 - 12\omega_3^3 \omega_1 + 12\omega_3^3 \omega_{13} - 12\omega_3^3 \omega_2 - 2\omega_3^2 \omega_{13} \omega_1 \omega_2^2 - 24\omega_{13} \omega_1 \omega_2^2 - 2\omega_3^3 \omega_{13} \omega_2^2 - 12\omega_3^2 \omega_1 \omega_2 - 12\omega_3^2 \omega_2^2 + 12\omega_3 \omega_{13} \omega_1 \omega_2 - 12\omega_3^3 \omega_1 \omega_2^2 + 24\omega_3^3 \omega_1 \omega_2 + 24\omega_3 \omega_{13} \omega_1 \omega_2^2 - 6\omega_3^2 \omega_{13} \omega_2^2) \frac{c_s^4 \rho}{12\omega_3^3 \omega_{13} \omega_1 \omega_2^2}$$

$$\begin{aligned}
C_{D_x D_z D_z v_1}(3, CuLBm2) = & (108\omega_3^2\omega_4^2\omega_1\omega_5v_4^2\omega_2^2 - 56\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_5\omega_2 - 72\omega_3\omega_4^2c_s^2\omega_1^3\omega_5\omega_2^2 + 54\omega_4^2\omega_1^3\omega_5v_4^2\omega_2^2 + 264\omega_3\omega_4^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^2 + 48\omega_3^2\omega_4^2\omega_1^3\omega_5v_4^2 - \\
& 8\omega_3^2\omega_4^2\omega_1^2\omega_5\omega_2 + 144\omega_3^2\omega_4^2\omega_1^2\omega_5v_2^2\omega_2^2 - 72\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5v_2^2\omega_2 + 132\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2 - 348\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5v_2^2\omega_2 - 24\omega_3^2\omega_4^2v_1^2\omega_5\omega_2^2 + \\
& 48\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 84\omega_3^2\omega_4^2\omega_1^2\omega_5v_2^2\omega_2^2 + 112\omega_3\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2 + 48\omega_3\omega_4^2c_s^2\omega_1^3v_1^2\omega_5\omega_2 + 36\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5\omega_2^2 - 648\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^2 + \\
& 108\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5v_2^2\omega_2^2 - 72\omega_3\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 - 72\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^2 + 36\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 + 288\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 - 36\omega_4^2\omega_1^3\omega_5v_4^2\omega_2^2 - 54\omega_3^2\omega_1^3\omega_5v_2^2\omega_2^2 + \\
& 72\omega_3\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 - 468\omega_3\omega_4^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1^3\omega_5v_4^2\omega_2^2 + 36\omega_3\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 - 9\omega_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2v_3^2 + 54\omega_3\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 + \\
& 108\omega_3\omega_4^2c_s^2\omega_1^3\omega_5v_2^2\omega_2^2 + 36\omega_3^2\omega_4^2\omega_1^2\omega_5v_4^2\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^2 + 64\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 + 18\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 - 60\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - \\
& 216\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2 + 36\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5\omega_2^2 + 108\omega_3^2\omega_1^3\omega_5v_4^2\omega_2^2 + 162\omega_3\omega_4^2c_s^2\omega_1^3v_1^2\omega_5\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 - 288\omega_3^2\omega_1^3v_1^2\omega_5v_2^2\omega_2^2 - \\
& 216\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 4\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5\omega_2^2 + 72\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 - 168\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^2 + 6\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5\omega_2^2v_3^2 - \\
& 2\omega_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2v_3^2 + 264\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5v_2^2\omega_2^2 - 16\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 - 36\omega_3\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 - 216\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 28\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_5\omega_2^2 - \\
& 24\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5v_2^2\omega_2^2 + 12\omega_3\omega_4^2\omega_1^2\omega_5v_4^2\omega_2^2 - 180\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5v_2^2\omega_2^2 - 54\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 + 9\omega_3\omega_4^2\omega_1^3\omega_5\omega_2^2v_3^2 + 27\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2v_3^2 - \\
& 72\omega_3^2\omega_4^2\omega_1^3\omega_5v_4^2\omega_2^2 + 180\omega_3\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 180\omega_3\omega_4^2c_s^2\omega_1^3v_1^2\omega_5\omega_2^2 + 24\omega_3\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 - 96\omega_3^2\omega_4^2\omega_1^3\omega_5v_4^2\omega_2^2 + 288\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 + 2\omega_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2v_3^2 - \\
& 6\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2v_3^2 - 36\omega_3\omega_4^2\omega_1^2\omega_5v_2^2\omega_2^2 - 108\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 12\omega_3\omega_4^2\omega_1^2\omega_5v_2^2\omega_2^2 + 56\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 + 60\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5v_2^2\omega_2^2 - \\
& 18\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^2 - 120\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 + 288\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^2 + 360\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^2 + 16\omega_3^2\omega_4^2\omega_1^2\omega_5\omega_2^2 - \\
& 160\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_5\omega_2^2 + 8\omega_3^2\omega_4^2\omega_1^3\omega_5 - 36\omega_3^2\omega_4^2\omega_1^2\omega_5v_4^2\omega_2^2 + 648\omega_3^2\omega_4^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^2 + 32\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_5 + 324\omega_3^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 + 2\omega_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2v_4^2 + \\
& 64\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5\omega_2^2 + 54\omega_3^2\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 + 36\omega_3^2\omega_1^3\omega_5v_2^2\omega_2^2 + 72\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 24\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_5v_2^2\omega_2^2 - 36\omega_3\omega_4^2\omega_1^3\omega_5v_2^2\omega_2^2 + 72\omega_3\omega_4^2c_s^4\omega_1^3\omega_5\omega_2^2 +
\end{aligned}$$

$$\text{coefficient } C_{\text{D}_x \text{D}_y^2 \text{D}_z \text{v}_2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z \text{v}_2}^{(3), \text{SRT}} = (-\omega^3 v_1 v_3^2 + c_s^2 \omega^3 v_3 - 14\omega^2 v_1^2 v_3 + 24c_s^2 v_1 + 24v_1 v_3^2 - 36c_s^2 \omega v_1 - 14c_s^2 \omega^2 v_3 - 36\omega v_1 v_3^2 + 14c_s^2 \omega^2 v_1 + \omega^3 v_1^2 v_3 + 36c_s^2 \omega v_3 - 24v_1^2 v_3 + 14\omega^2 v_1 v_3^2 - c_s^2 \omega^3 v_1 - 24c_s^2 v_3 + 36\omega v_1^2 v_3) \frac{\rho v_2}{\omega^3}$$

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$-2w_{6w19w16w23c_s^2w20w17w11v1w18} - 2w_{6w19w16w7w23c_s^2w17w11w8v1} - 2w_{6w19w16w23c_s^2w20w11w8v1w18} + 2w_{19w16w7w23w17w11w8v1^2v3w18} -$
 $-2w_{6w19w16w23w17w11w8v1v3^2w18} - 2w_{6w19w16w23w17w11v1^2v3w18} + w_{6w19w7w20w17w11w8v1^2v3w18} + 2w_{6w16w23w17w11w8v1v3^2w18} -$
 $-w_{19w16w7w23c_s^2w20w11w8v1w18} - w_{19w16w23w20w17w11w8v1v3^2} - 2w_{19w16w7w23c_s^2w20w17w11v1w18} + 2w_{19w16w7w23c_s^2w17w11w8v1} -$
 $-w_{6w19w16w7c_s^2w20w17w11w8v3w18} - 2w_{6w19w16w7w23c_s^2w20w17w11w8v3w18} + 2w_{6w16w7w23w17w11w8v3w18} - w_{6w19w7w23w20w17w11w8v1w18} -$
 $-w_{6w19w7w23c_s^2w20w17w11w8v1w18} - 2w_{6w19w16w7w23c_s^2w17w8v1w18} - 2w_{6w16w23w17w11w8v1^2v3w18} - 2w_{6w19w16w23w20w11v3w18} -$
 $-2w_{6w19w16w23c_s^2w20w11v3w18} - 2w_{19w16w7w23w17w11w8v1v3^2w18} - w_{6w19w16w7w23w20w17w11w8v1v3^2w18} +$
 $-2w_{6w19w16w23w17w11w8v1^2v3w18} - w_{6w19w16w7w23w20w17w11w8v1v3^2} + 2w_{6w16w7w23c_s^2w17w8v1w18} + 2w_{6w19w16w23w17w11v1w18} +$
 $-2w_{6w19w16w7w23w17w11v1v3^2w18} - 2w_{6w19w16w7w23w17w11w8v1v3^2w18} + 2w_{6w16w7w23c_s^2w20w17w11w8v1w18} + w_{19w16w7w23c_s^2w20w17w11w8v3} +$
 $-2w_{6w19w23w20w17w11w8v1^2v3w18} + 2w_{6w16w7w23w20w17w11w8v1v3^2w18} - 2w_{6w16c_s^2w20w17w11w8v3w18} + 2w_{19w16w7w23c_s^2w20w11v1w18} +$
 $-w_{6w19w7w23w20w11w8v1^2v3w18} + 2w_{19w16w7w23w17w11w8v1v3^2} + 2w_{6w16w7w23w17w11w8v1v3^2w18} + w_{6w19w16w7w23w20w17w11w8v1^2v3w18} +$
 $-2w_{6w19w16c_s^2w20w17w11w8v3w18} - 2w_{19w16w7w23c_s^2w17w11v3w18} + 2w_{6w19w16w7w23w20w11v1^2v3w18} + 2w_{19w16w7w23w20w11v1v3^2w18} -$
 $-2w_{6w19w16w23c_s^2w20w17w11w8v3w18} + 2w_{6w16w7w23c_s^2w17w11w8v3w18} - 2w_{6w16w7c_s^2w20w17w11w8v3w18} - w_{6w19w7w23c_s^2w20w17w11w8v3w18} +$
 $-2w_{6w19w16w7w23w17w11w8v1v3^2w18} - w_{6w19w16w7w23c_s^2w20w17w11w8v1w18} - 2w_{6w19w23c_s^2w20w17w11w8v1w18} +$
 $-w_{6w19w16w7c_s^2w20w17w1w8v3w18} + w_{6w19w16w7w23w20w17w11w8v1v3^2} + w_{6w19w16w7w23c_s^2w20w11w8v1w18} + 2w_{6w19w23c_s^2w20w11w8v1w18} +$
 $-2w_{6w19w16w7w23c_s^2w17w11v3w18} - 2w_{6w19w16w7w23c_s^2w17w11w8v3w18} + 2w_{6w16w23w20w17w11w8v1v3^2w18} - 2w_{19w16w7w23w20w11v1^2v3w18} -$
 $-2w_{6w19w16w7w23w20w11w8v1v3^2w18} - 2w_{6w19w16w7w23c_s^2w20w17w11w8v1w18} + w_{6w19w7w23w20w17w11w8v1v3^2w18} - 2w_{6w19w16w7w23w17w11v1^2v3w18} -$
 $-2w_{19w16w7w23w17w11v1^2v3w18} - w_{6w19w16w7w23w20w11w8v1w18} + 2w_{6w19w23w20w11w8v1v3^2w18} + 2w_{6w19w16w23w20w17w11w8v1v3^2w18} -$
 $-2w_{6w19w16w7w23w20w17w11w8v1v3^2w18} + 2w_{6w19w16w7w23c_s^2w20w11v3w18} + 2w_{6w19w16w7w23w20w17w11v1^2v3w18} -$
 $-w_{6w19w7w23c_s^2w20w11w8v1w18} + 2w_{6w19w16w23c_s^2w20w17w11w8v1w18} - 2w_{6w16w7w23c_s^2w17w11w8v1w18} - 2w_{6w16w23w20w17w11w8v1v3^2w18} +$
 $-2w_{6w19w16w7w23w20w17w11w8v1v3^2w18} + w_{6w19w16w23c_s^2w20w17w11w8v1w18} - 2w_{6w16w7w23c_s^2w20w17w8v1^2v3w18} + 2w_{6w16w7c_s^2w20w17w8v1w18} +$
 $-w_{6w19w16w7w23w20w17w11w8v3w18} + 2w_{6w19w16w7w23c_s^2w20w17w11w8v3w18} - w_{6w19w16w7w23w20w17w11w8v1v3^2w18} - 2w_{6w16w7w23w20w17w8v1^2v3w18} -$
 $-2w_{6w16w20w17w11w8v1v3^2w18} - 2w_{6w16w7w23c_s^2w20w17w11w8v3w18} + w_{19w16w7w23w20w17w11w8v1^2v3} + 2w_{6w16w7w23w20w17w11w8v1v3^2w18} -$
 $-w_{6w19w16w7w23w20w17w11w8v1v3^2w18} - 2w_{6w19w16c_s^2w20w17w11w8v1w18} - w_{6w19w16w7w23w20w17w11w8v1v3^2w18} - 2w_{6w16w7w23w20w17w8v1^2v3w18} +$
 $-2w_{6w16w20w17w11w8v1v3^2w18} - 2w_{6w16w7w23c_s^2w20w17w11w8v3w18} + w_{19w16w7w23w20w17w11w8v1^2v3} + 2w_{6w16w7w23w20w17w11w8v1v3^2w18} +$
 $-2w_{6w19w16w7w23w17w8v1v3^2} - 2w_{6w19w16w20w17w11w8v1v3^2w18} - w_{6w19w16w7w20w17w8v1v3^2w18} + 2w_{6w19w16w7w23w17w8v1^2v3w18} -$
 $-2w_{6w16w7c_s^2w20w17w11w8v1w18} + 2w_{6w19w20w17w11w8v1v3^2w18} + w_{6w19w16w7w23c_s^2w20w17w11w8v1v3^2w18} + w_{6w19w16w7w20w17w11w8v1v3^2w18} -$
 $-w_{6w19w16w7w23w20w17w11w8v1v3^2w18} - 2w_{6w16w7w23w20w17w11w8v1v3^2w18} + w_{19w16w7w23c_s^2w20w11w8v3w18} + 2w_{6w19w16w23w20w11w8v1^2v3w18} -$
 $-w_{19w16w7w23w20w11w8v1v3^2w18} - 2w_{6w19w16w7w23c_s^2w20w17w11v3w18} + w_{6w19w16w7w23c_s^2w20w17w8v1^2v3w18} + w_{6w19w16w7c_s^2w20w17w11w8v1w18} -$
 $-2w_{19w16w7w23w20w17w11v1v3^2w18} + w_{19w16w7w23w20w17w11w8v1v3^2w18} + w_{6w19w7c_s^2w20w17w11w8v3w18} + 2w_{6w16w7w23w20w17w8v1^2v3w18} +$
 $-2w_{6w19w16w23w20w17w11v1^2v3w18} - w_{6w19w16w7w23w20w17w11w8v1v3^2} - w_{6w19w16w7w20w17w11w8v1v3^2w18} - 2w_{6w19w16w7w23w17w8v1v3^2w18} -$
 $-2w$

[illegible]

$$\begin{aligned}
& 54w_{19}w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} + 12w_{16}w_{10}w_7^2w_{23}c_s^4w_{11}v_2^2 + 6w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 36w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} - 36w_{16}w_{10}w_7^2w_{23}c_s^2v_3^2 + \\
& 18w_{19}w_{10}w_7^2w_{23}c_s^4w_{11}v_2^2 - 12w_{19}w_{16}w_{10}w_7w_{23}c_s^2w_{11} + 12w_{19}w_{10}w_7^2w_{23}w_{11}v_2^2 + 144w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 + 24w_{19}w_{16}w_{10}w_7w_{23}w_{11}v_2^2v_3^2 + \\
& 36w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 + 12w_{19}w_{16}^2w_7^2w_{23}w_{11}v_2^2v_3^2 + 12w_{16}w_{10}w_7^3v_2^2v_3^2 + w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 + 12w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 - \\
& 6w_{19}w_{16}w_{10}w_7^2v_2^2v_3^2 + 36w_{16}^2w_{10}w_7^2c_s^4 - 6w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 - 12w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 - 12w_{19}w_{16}w_{10}w_7^2w_{11}v_2^2v_3^2 + 36w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} + \\
& 12w_{19}w_{16}w_{10}^2w_7^2w_{11}v_3^2 - 96w_{19}w_{16}w_{10}^2w_{23}c_s^4w_{11} + 18w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 + 12w_{16}w_{10}^2w_7^2w_{11}v_2^2v_3^2 + 12w_{19}w_{16}w_{10}w_7w_{23}c_s^2w_{11} + \\
& 6w_{19}w_{16}w_{10}w_7^2v_2^2 - 15w_{19}w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} - 6w_{19}w_{16}w_{10}w_7^2w_{11}v_2^2v_3^2 - 6w_{19}w_{10}w_7^2w_{23}c_s^2w_{11} - 12w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 + \\
& 72w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2v_3^2 - 42w_{19}w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} + 6w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 12w_{19}w_{16}w_{10}w_7^2w_{11}v_2^2v_3^2 + 36w_{19}w_{16}w_{10}w_7^3w_{23}c_s^2v_3^2 + \\
& 3w_{19}w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} - 12w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 - 12w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 36w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - \\
& 72w_{19}w_{16}w_{10}w_7w_{23}c_s^2w_{11}v_2^2 - 12w_{19}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 + 15w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 - 12w_{16}w_{10}^2w_7^2c_s^2w_{11} - 3w_{19}w_{16}w_{10}w_7^3w_{23}c_s^2w_{11}v_2^2 + \\
& 12w_{19}w_{16}w_{10}w_7^2c_s^2w_{11} - 6w_{19}w_{16}w_{10}w_7^2w_{23}v_2^2v_3^2 - 12w_{16}w_{10}w_7^2w_{23}v_2^2v_3^2 + 24w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_3^2 + 18w_{19}w_{16}w_{10}w_7^2c_s^4w_{11} - \\
& 12w_{19}w_{16}w_{10}^2w_7^2w_{23}c_s^2w_{11}v_2^2 + 12w_{19}w_{10}w_7^2w_{23}c_s^2w_{11} - 18w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11} - 36w_{16}w_{10}w_7^3c_s^4w_{11} + 12w_{16}w_{10}w_7^2w_{23}c_s^2w_{11} - \\
& 6w_{19}w_{16}w_{10}^2w_{23}w_{11}v_2^2v_3^2 + 156w_{19}w_{16}w_{10}w_7w_{23}c_s^4w_{11} - 45w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_3^2 - 12w_{16}w_{10}^2w_7^2c_s^2 + 12w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 + \\
& 6w_{19}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 18w_{19}w_{16}w_{10}w_7^2c_s^4w_{11} + 24w_{19}w_{16}w_{10}w_7^2w_{23}v_3^2 + 12w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11} + 18w_{19}w_{16}w_{10}w_7^3c_s^2w_{11}v_2^2 - \\
& 36w_{16}w_{10}^2w_7^2c_s^2w_{11}v_3^2 + 9w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 + 3w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11} + 36w_{19}w_{16}w_{10}w_7^2c_s^2w_{11}v_3^2 - 36w_{19}w_{16}w_{10}w_7w_{23}c_s^4w_{11} + \\
& 12w_{19}w_{16}w_{10}^2w_7^2w_{11}v_2^2 + 12w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 12w_{19}w_{16}w_{10}w_7^2c_s^2w_{11} - 12w_{16}w_{10}w_7^2c_s^2w_{11} + 12w_{16}w_{10}w_7^3w_{23}v_2^2 + \\
& 6w_{19}w_{16}w_{10}w_7^2c_s^2w_{11}v_2^2 - 12w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 24w_{19}w_{16}w_{10}w_7^2w_{23}v_2^2v_3^2 + 6w_{19}w_{16}w_{10}w_7^2w_{23}v_2^2 - 18w_{19}w_{16}w_{10}^2w_7^2c_s^2w_{11}v_3^2 - \\
& 18w_{19}w_{16}w_{10}w_7^2w_{23}c_s^4w_{11} - 12w_{19}w_{16}w_{10}w_7w_{23}c_s^2w_{11}v_2^2 + 36w_{16}w_{10}w_7^2c_s^2w_{11}v_3^2 - 36w_{19}w_{16}w_{10}w_7^2c_s^2w_{11}v_3^2 - w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11} - \\
& 18w_{19}w_{16}w_{10}^2w_7^2c_s^4 + 12w_{19}w_{16}w_{10}w_7^2w_{23}v_2^2v_3^2 + 6w_{19}w_{16}w_{10}w_7^2w_{11}v_3^2 - 12w_{19}w_{16}w_{10}w_7^2c_s^2w_{11}v_2^2 + 36w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 - 12w_{16}w_{10}^2w_7^2v_3^2 + \\
& 72w_{19}w_{16}w_{10}w_7w_{23}c_s^2w_{11}v_3^2 + 48w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 + 12w_{16}w_{10}w_7^2c_s^2w_{11}v_2^2 - 6w_{19}w_{16}w_{10}w_7^2c_s^2w_{11}v_2^2 - 24w_{19}w_{16}w_{10}w_7w_{23}w_{11}v_3^2 - \\
& 6w_{19}w_{16}w_{10}w_7^2w_{11}v_2^2 + 12w_{16}w_{10}w_7^2c_s^2v_2^2 - 36w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 - 6w_{19}w_{16}w_{10}w_7^2c_s^2v_2^2 + 12w_{16}w_{10}w_7^2w_{11}v_3^2 + 24w_{19}w_{16}w_{10}w_7^2w_{23}v_2^2v_3^2 - \\
& 24w_{19}w_{16}w_{10}w_7^2w_{23}w_{11}v_2^2v_3^2 - 108w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_3^2 - 12w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 - 36w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_3^2 - 12w_{16}w_{10}w_7^2w_{23}c_s^2w_{11} + \\
& 18w_{19}w_{16}w_{10}w_7^2w_{23}c_s^2w_{11}v_2^2 - 12w_{19}w_{10}w_7^2w_{23$$

$$C_{D_3^3 D_z \rho}^{(3), \text{CLBM2}} = C_{D_3^3 D_z \rho}^{(3), \text{CLBM1}}$$

$$C_{D_3^3 D_z \rho}^{(3), \text{CuLBM1}} = (12\omega_3\omega_{11}^2\omega_5 + 3\omega_3^2c_s^2\omega_{11}^2 + 18\omega_3\omega_{11}\omega_5v_2^2 - 36c_s^2\omega_{11}^2 + 12\omega_3\omega_5 - 6\omega_3\omega_{11}^2 + 6\omega_3^2\omega_5v_2^2 + 3\omega_3^2\omega_{11}\omega_5 + 54\omega_3c_s^2\omega_{11}\omega_5 + 18\omega_3^2c_s^2\omega_5 + 12\omega_{11}\omega_5 + 12\omega_{11}^2 + \omega_3^2\omega_{11}^2\omega_5v_2^2 - 12\omega_{11}^2v_2^2 + \omega_3^2\omega_{11}^2v_2^2 - 12\omega_3\omega_{11} + 3\omega_3^2c_s^2\omega_{11}^2\omega_5 + 36c_s^2\omega_{11}^2\omega_5 - 18\omega_3^2c_s^2\omega_{11} + 12\omega_{11}^2\omega_5v_2^2 + 12\omega_3\omega_{11}v_2^2 - 3\omega_3^2\omega_{11}\omega_5v_2^2 - 36c_s^2\omega_{11}\omega_5 + 6\omega_3\omega_{11}^2v_2^2 - 9\omega_3^2c_s^2\omega_{11}\omega_5 + 6\omega_3^2\omega_{11} + 36\omega_3c_s^2\omega_{11} - 12\omega_{11}\omega_5v_2^2 - 6\omega_3^2\omega_{11}v_2^2 - \omega_3^2\omega_{11}^2 + 18\omega_3c_s^2\omega_{11}^2 - \omega_3^2\omega_{11}^2\omega_5 - 36\omega_3c_s^2\omega_{11}^2\omega_5 - 12\omega_{11}^2\omega_5 - 12\omega_3\omega_{11}^2\omega_5v_2^2 - 18\omega_3\omega_{11}\omega_5 - 12\omega_3\omega_5v_2^2 - 36\omega_3c_s^2\omega_5 - 6\omega_3^2\omega_5) \frac{c_s^2v_2^2}{12\omega_3^2\omega_{11}^2\omega_5}$$

[illegible]

$$\begin{aligned}
C_{D_x D_y D_z^2 \rho}^{(3), \text{MRT2}} &= C_{D_x D_y D_z^2 \rho}^{(3), \text{MRT1}} \\
C_{D_x D_y D_z^2 \rho}^{(3), \text{CLBM1}} &= 0 \\
C_{D_x D_y D_z^2 \rho}^{(3), \text{CLBM2}} &= 0 \\
C_{D_x D_y D_z^2 \rho}^{(3), \text{CuLBM1}} &= 0 \\
C_{D_x D_y D_z^2 \rho}^{(3), \text{CuLBM2}} &= (6\omega_1^2 v_2^2 \omega_2^2 - 3\omega_1^3 v_1^2 \omega_2 - 12\omega_1 \omega_2^2 - 72c_s^2 \omega_1^2 \omega_2 + 6\omega_1 \omega_2^3 - 3\omega_1 v_1^2 \omega_2^3 + 2v_2^2 \omega_2^3 + 36c_s^2 \omega_1^2 \omega_2^2 + 4\omega_1^3 v_1^2 - 6\omega_1^2 v_2^2 \omega_2 - 4\omega_2^3 v_3^2 - \\
&\quad 18c_s^2 \omega_1^3 \omega_2 - 18c_s^2 \omega_1 \omega_2^3 + 24\omega_1^2 \omega_2 + 36c_s^2 \omega_1 \omega_2^2 - 6\omega_1^2 v_1^2 \omega_2 + 4\omega_1^3 v_3^2 + 4\omega_1^3 v_2^2 - 12\omega_1^3 + 6\omega_1^3 \omega_2 - 12\omega_1^2 \omega_2 v_3^2 - 3\omega_1^3 v_2^2 \omega_2 + 6\omega_1^2 v_1^2 \omega_2^2 + 36c_s^2 \omega_1^3 - \\
&\quad 3\omega_1 v_2^2 \omega_2^3 + 2v_1^2 \omega_2^3 - 12\omega_1^2 \omega_2^2 + 12\omega_1 \omega_2^2 v_3^2) \frac{v_1 v_2 v_3}{6\omega_1^3 \omega_2^3}
\end{aligned}$$

$$C_{D_x D_y D_z^2 v_1}^{(3), \text{SRT}} = 0$$

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C(3), MRT1

$$\begin{aligned} D_{\times}D_yD_zv_2 = & (-2w_6^2w_{19}w_7c_s^2w_{20}w_{11}w_8^2w_{18} - 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 2w_6w_2w_{19}w_7^2w_{11}w_8w_5w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} - \\ & 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{11}w_8w_5w_{18} + 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5 + w_6^2w_{19}w_7^2w_{20}w_{11}w_8w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} + \\ & 9w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 4w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & 8w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8w_5w_{18} + 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} + \\ & 2w_6w_{19}w_7^2c_s^2w_{11}w_8^2w_5w_{18} - w_6w_{19}w_7^2w_{11}w_8w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8w_5v_3^2w_{18} + 4w_6w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5v_3^2w_{18} - 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 8w_6^2w_{19}c_s^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} + w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} + 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8w_{18} - 4w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 3w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 8w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - \\ & w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} - 4w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 6w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 9w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} + 11w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{11}w_8^2w_5w_{18} - \\ & 9w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 6w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - w_6^2w_{19}w_7^2w_{20}w_{11}w_8w_5w_{18} - 2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} - 3w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} - \\ & w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 3w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} + 4w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2c_s^2w_{11}w_8^2w_5w_{18} - \\ & 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5v_3^2w_{18} + 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 5w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5v_3^2w_{18} + 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} + \\ & 3w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 4w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2c_s^2w_{11}w_8^2w_5w_{18} + 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5 - \\ & 3w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5v_3^2w_{18} + 2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} + 2w_6^2w_{19}w_7^2w_{11}w_8^2w_5w_{18} + 12w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - \\ & 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_5w_{18} + 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 6w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 5w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} - \\ & 8w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 6w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5 + 3w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_{18} - \\ & 2w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} - 4w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - \\ & 3w_6^2w_{19}w_7^2w_{20}w_{11}w_8^2w_5w_{18} + 2w_6^2w_{19}w_7^2w_{11}w_8w_5v_3^2w_{18} - 6w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} - 4w_6^2w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & 2w_6w_{19}w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18} + 4w_6w_{19}w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18} + 2w_6w_{19}w_7^2c_s^2w_{11}w_8w_5w_{18} + 2w_6w_{19}w_7^2c_s^2w_{20}w_{11}w_8^2w_5w_{18} + \\ & 2w_6w_{19}w_7^2c_s^2w_{20}w_{11}w_8w_5w_{18} - 2w_6w_{19}w_7^2w_{20}w_{11}w_8^2w_5v_3^2w_{18} + 2w_6w_{19}w$$

[illegible]

$$C_{D_y^2 D_z^2 v_2}^{(3), \text{MRT2}} = C_{D_y^2 D_z^2 v_2}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_2^2 D_2^2}^{(3), CuLB M2} = (-9\omega_3\omega_1\omega_3^2v_3^2 + 50\omega_3\omega_1^2v_2^2\omega_2^2 + 48\omega_3\omega_3^2\omega_2 + 23\omega_3\omega_1^2\omega_3^2 + 12\omega_3\omega_2^2\omega_2^2 + 108\omega_3c_s^2\omega_1\omega_3^2 + 12\omega_1^2\omega_2^2v_3^2 + 6\omega_1\omega_3^2 + 84\omega_3c_s^2\omega_1^3 + 36c_s^2\omega_2^2\omega_2^2 + 141\omega_3\omega_1v_2^2\omega_3^2 + 6\omega_3\omega_1^2\omega_2 - 66\omega_3c_s^2\omega_2^2 - 12\omega_3\omega_1\omega_2v_3^2 - 6\omega_1^2\omega_2v_3^2 + 48\omega_3\omega_1^2v_2^2 - 18c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_1^2\omega_2v_3^2 - 23\omega_3\omega_1^2\omega_2^2 - 75\omega_3\omega_1^2v_2^2\omega_2 + 12\omega_3\omega_3^2v_3 + 60\omega_3\omega_1v_2^2\omega_2^2 - 18c_s^2\omega_1\omega_3^2 - 18\omega_3c_s^2\omega_1^2\omega_2 + 18\omega_3\omega_1^2\omega_2^2v_3^2 - 50\omega_3\omega_2^2v_2^2\omega_3^2 - 6\omega_1\omega_2^2v_3^2 - 66\omega_3\omega_1^2v_2^2\omega_2^2 + 12\omega_3\omega_2^2v_3 + 42\omega_3c_s^2\omega_1^2\omega_2^2 + 42\omega_3\omega_2^2 + 6\omega_3\omega_1^2v_2^2\omega_2 - 9\omega_3\omega_1^2\omega_2v_3^2 - 42\omega_3c_s^2\omega_1^2\omega_2^2 - 12\omega_3\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^2\omega_2 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3 - 60\omega_3\omega_1\omega_2^2 - 114\omega_3v_2^2\omega_2^2 - 12\omega_1^2\omega_2^2) \frac{v_2v_3}{18\omega_3\omega_1^3\omega_2^2}$$

coefficient $C_{D_y^2 D_z^2 v_3}^{(3)}$ at $\frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2}$:

$$C_{D_y^2 D_z^2 v_3}^{(3), \text{SRT}} = (-24 - 18c_s^2\omega - 12\omega^2 - c_s^2\omega^3 - 108\omega v_3^2 + 8c_s^2\omega^2 + 36\omega + 36\omega^2 v_3^2 + 12c_s^2 + 72v_3^2) \frac{c_s^2 \rho}{12\omega^3}$$

[illegible]

$$C_{D_y^2 D_z^2 v_3}^{(3), \text{MRT2}} = C_{D_y^2 D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_2^2 v_3}^{(3), CLBM1} = (-18\omega_{19} \omega_{16} \omega_{23}^2 \omega_{23} \omega_{11} v_3^2 - 12\omega_{19} \omega_{16} \omega_{23} c_s^2 \omega_{11}^2 - 36\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11} v_3^2 - 36\omega_{16} \omega_{16}^2 \omega_{11}^2 v_3^2 + 36\omega_{16} \omega_{16} \omega_{23} \omega_{11}^2 v_3^2 - 12\omega_{16} \omega_{16}^2 \omega_{11}^2 - 12\omega_{19} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 + 12\omega_{19} \omega_{16} \omega_{16} \omega_{23} \omega_{11}^2 - 36\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 - 6\omega_{19} \omega_{16} \omega_{16}^2 \omega_{11}^2 - 12\omega_{19} \omega_{16} \omega_{16} \omega_{23} c_s^2 \omega_{11}^2 + 24\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 + 12\omega_{19} \omega_{16}^2 c_s^2 \omega_{11}^2 - 6\omega_{19} \omega_{16}^2 \omega_{23} \omega_{11}^2 - 36\omega_{19} \omega_{16} \omega_{16}^2 \omega_{11}^2 v_3^2 + 12\omega_{16} \omega_{16}^2 c_s^2 \omega_{11}^2 - 12\omega_{16} \omega_{16}^2 \omega_{11}^2 - 12\omega_{16} \omega_{16}^2 c_s^2 \omega_{11}^2 + 12\omega_{16} \omega_{16} \omega_{23} c_s^2 \omega_{11}^2 - 12\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 + 18\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 + 6\omega_{19} \omega_{16} \omega_{16}^2 \omega_{11}^2 - 12\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 + 6\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 + 12\omega_{16} \omega_{16}^2 \omega_{11}^2 v_3^2 + 36\omega_{19} \omega_{16}^2 \omega_{11}^2 v_3^2 + 36\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 + 72\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 - 18\omega_{19} \omega_{16} \omega_{16}^2 \omega_{11}^2 v_3^2 + 6\omega_{19} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 - 12\omega_{19} \omega_{16} \omega_{16}^2 c_s^2 \omega_{11}^2 + 12\omega_{19} \omega_{16} \omega_{16}^2 \omega_{11}^2 + 12\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 - 72\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 + 6\omega_{19} \omega_{16}^2 \omega_{11}^2 - 12\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 - 6\omega_{19} \omega_{16}^2 c_s^2 \omega_{11}^2 - \omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 + 12\omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 + 18\omega_{19} \omega_{16}^2 \omega_{11}^2 v_3^2 + 18\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} v_3^2 - 6\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} + 12\omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 - 6\omega_{19} \omega_{16} \omega_{16}^2 c_s^2 \omega_{11}^2 + 36\omega_{16} \omega_{16}^2 \omega_{11}^2 v_3^2 + 24\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 - 36\omega_{19} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 - 24\omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 - 4\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 + 6\omega_{19} \omega_{16} \omega_{16}^2 c_s^2 \omega_{11}^2 - 6\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 - 12\omega_{16} \omega_{16}^2 \omega_{23} c_s^2 \omega_{11}^2 - 12\omega_{19} \omega_{16}^2 \omega_{11}^2 - 24\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 - 18\omega_{19} \omega_{16}^2 \omega_{11}^2 v_3^2 + 36\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 + 12\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 - 12\omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 + 6\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} c_s^2 + 36\omega_{16} \omega_{16}^2 \omega_{11}^2 v_3^2 + 12\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} - 36\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2 v_3^2 + 12\omega_{16} \omega_{16}^2 c_s^2 \omega_{11}^2) \frac{c_s^2 \rho}{12\omega_{19} \omega_{16} \omega_{16}^2 \omega_{23} \omega_{11}^2}$$

$$C_{D_y^2 D_z^2 v_3}^{(3), \text{CLBM2}} = C_{D_y^2 D_z^2 v_3}^{(3), \text{CLBM1}}$$

coefficient $C_{D_x D_z^3 v_1}^{(3)}$ at $\frac{\partial^4 v_1}{\partial x_1 \partial x_3^3}$:

$$C_{\mathbf{D}_x \mathbf{D}_2^2 v_1}^{(3), \text{SRT}} = (-42c_s^2 \omega^2 v_3^2 + 36c_s^2 \omega - 36v_3^4 + 4\omega^3 v_3^4 + 12c_s^2 \omega^3 v_3^2 - 54\omega v_3^2 - 26\omega^2 v_3^4 - 12c_s^2 \omega^2 + 36c_s^4 + 54\omega v_3^4 - 36c_s^2 v_3^2 + 26\omega^2 v_3^2 - 54c_s^4 \omega - 24c_s^2 + 20c_s^4 \omega^2 - 4\omega^3 v_3^2 - c_s^4 \omega^3 + 54c_s^2 \omega v_3^2 + 36v_3^2) \frac{\rho}{12\omega^3}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{MRT1}} = (12\omega_3^2 \omega_{11}^2 v_3^2 + 54\omega_3^2 c_s^2 \omega_{11}^2 v_3^2 \omega_{18} + 12\omega_6 \omega_{11}^3 v_3^4 \omega_{18} + 6\omega_3^2 c_s^4 \omega_{11}^3 \omega_{18} - 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 + 252\omega_6^2 c_s^2 v_3^2 \omega_{18} + 6\omega_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 - 81\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} + 90\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 12\omega_6^2 \omega_{11}^3 v_3^4 \omega_{18} + 18\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + \omega_6^3 c_s^4 \omega_{11}^2 \omega_{18} + 27\omega_6^3 \omega_{11}^3 v_3^2 \omega_{18} + 102\omega_6^2 c_s^4 \omega_{11}^3 v_3^2 \omega_{18} + 18\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 60\omega_3^2 \omega_{11}^3 v_3^4 \omega_{18} - 12\omega_6^2 \omega_{11}^3 v_3^4 - 48\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} - 6\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + 6\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 + 19\omega_6^2 \omega_{11}^3 v_3^4 \omega_{18} - 24\omega_6^2 \omega_{11}^3 v_3^4 \omega_{18} + 36\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} - 6\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} - 5\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 4\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} - 12\omega_6^2 \omega_{11}^3 v_3^2 - 72\omega_6^2 v_3^2 \omega_{18} - 18\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - \omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 108\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} + 30\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 60\omega_3^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 - 24\omega_6^2 \omega_{11}^3 v_3^4 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - \omega_6^3 c_s^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} - 90\omega_6^2 \omega_{11}^3 v_3^4 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 27\omega_6^3 \omega_{11}^3 v_3^2 \omega_{18} + 12\omega_3^2 c_s^4 v_3^4 - 48\omega_6^2 c_s^4 \omega_{11}^2 v_3^2 \omega_{18} - 24\omega_6^2 c_s^4 \omega_{11}^2 v_3^2 - 18\omega_6^2 \omega_{11}^3 v_3^4 \omega_{18} - 48\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 60\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 162\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 12\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 21\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 30\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} - 36\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} + 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 \omega_{11}^3 v_3^4 - 12\omega_6^2 c_s^2 \omega_{18} + 12c_s^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^3 v_3^2 \omega_{18} + 24\omega_6 \omega_{11}^3 v_3^2 \omega_{18} + 48\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 \omega_{11}^3 v_3^2 - 19\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} - 36\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 24\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 4\omega_6^2 \omega_{11}^3 v_3^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 72\omega_6^2 v_3^2 \omega_{18}) \frac{\rho}{12\omega_6^3 \omega_{11}^2 \omega_{18}^2}$$

$$C_{D_x D_z^3 v_1}^{(3), \text{MRT2}} = C_{D_x D_z^3 v_1}^{(3), \text{MRT1}}$$

$$C_{D\mathbf{x}D^3\mathbf{v}_1}^{(3),\text{CLBMM1}} = (36\omega_6^2\omega_{11}^2v_3^3 + 198\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} + 6\omega_6^2c_s^4\omega_{11}^3\omega_{18} - 6\omega_6^2c_s^2\omega_{11}^2\omega_{18}^2 + 252\omega_6^2c_s^2v_3^2\omega_{18}^2 + 6\omega_6^2c_s^2\omega_{11}\omega_{18} + 13\omega_6^2c_s^4\omega_{11}^3\omega_{18}^2 + 108\omega_6^2c_s^3\omega_{11}^3v_3^2 - 3\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18}^2 + 90\omega_6^2\omega_{11}^2v_3^2\omega_{18}^2 + 18\omega_6^2c_s^2\omega_{11}^3\omega_{18} + \omega_6^2c_s^4\omega_{11}^2\omega_{18} + 39\omega_6^2\omega_{11}^2v_3^2\omega_{18} - 18\omega_6^2c_s^2\omega_{11}^3v_3^2\omega_{18} + 6\omega_6^2\omega_{11}^3v_3^2\omega_{18} + 12\omega_6^2c_s^4\omega_{11}^2\omega_{18} + 72\omega_6^2\omega_{11}^2v_3^2\omega_{18} - 36\omega_6^2\omega_{11}^3v_3^4 - 36\omega_6^2\omega_{11}^2v_3^2\omega_{18} - 6\omega_6^2c_s^3\omega_{11}^3\omega_{18} + 6\omega_6^2c_s^4\omega_{11}^2\omega_{18} - 108\omega_6^2c_s^2\omega_{11}^2v_3^2 + 19\omega_6^2\omega_{11}^3v_3^4\omega_{18} + 36\omega_6^2\omega_{11}^2v_3^2\omega_{18} - 6\omega_6^2c_s^4\omega_{11}^2\omega_{18} - 5\omega_6^2c_s^2\omega_{11}^3\omega_{18} + 36\omega_6^2c_s^3\omega_{11}^2v_3^2\omega_{18} - 4\omega_6^2\omega_{11}^3v_3^2\omega_{18} - 36\omega_6^2\omega_{11}^3v_3^2 - 72\omega_6^2v_3^2\omega_{18} - 18\omega_6^2c_s^4\omega_{11}^3\omega_{18} - \omega_6^2c_s^2\omega_{11}^3\omega_{18} - 36\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} + 54\omega_6^2c_s^3\omega_{11}^2v_3^2\omega_{18} + 12\omega_6^2c_s^4\omega_{11}^2 + 60\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} - 108\omega_6^2c_s^2\omega_{11}^3v_3^2 - 12\omega_6^2c_s^2\omega_{11}^2\omega_{18} - \omega_6^2c_s^4\omega_{11}^3\omega_{18} - 90\omega_6^2\omega_{11}^3v_3^4\omega_{18} + 12\omega_6^2c_s^2\omega_{11}^2\omega_{18} - 39\omega_6^2\omega_{11}^3v_3^2\omega_{18} + 36\omega_6^2\omega_{11}^3v_3^4 - 24\omega_6^2c_s^4\omega_{11}^2\omega_{18} - 6\omega_6^2\omega_{11}^3v_3^2\omega_{18} - 72\omega_6^2\omega_{11}^2v_3^2\omega_{18} + 18\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} - 12\omega_6^2c_s^4\omega_{11}^2\omega_{18} - 99\omega_6^2c_s^3\omega_{11}^2v_3^2\omega_{18} - 306\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} - 12\omega_6^2c_s^3\omega_{11}^3\omega_{18} - 12\omega_6^2c_s^4\omega_{11}^2\omega_{18} + 12\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} - 108\omega_6^2c_s^2\omega_{11}^2\omega_{18} - 6\omega_6^2c_s^3\omega_{11}^3\omega_{18} - 36\omega_6^2\omega_{11}^3v_3^4 - 12\omega_6^2c_s^2\omega_{18} + 12c_s^4\omega_{11}^2\omega_{18} + 36\omega_6^2c_s^2\omega_{11}^2v_3^2\omega_{18} + 36\omega_6^2\omega_{11}^2v_3^4\omega_{18} + 12\omega_6^2c_s^2\omega_{11}\omega_{18}^2 + 36\omega_6^2\omega_{11}^3v_3^2 - 19\omega_6^2\omega_{11}^2v_3^2\omega_{18} - 36\omega_6^2\omega_{11}^2v_3^4\omega_{18} + 4\omega_6^2\omega_{11}^3v_3^4\omega_{18} + 12\omega_6^2c_s^2\omega_{11}^3\omega_{18} + 72\omega_6^2v_3^4\omega_{18}) \frac{\rho}{12\omega_6^2\omega_{11}^2\omega_{18}^2}$$

$$C_{D_x D_z^3 v_1}^{(3), \text{CLBM2}} = C_{D_x D_z^3 v_1}^{(3), \text{CLBM1}}$$

$$\begin{aligned} C_{\mathbf{D} \times \mathbf{D}^2 \times \mathbf{v}_1}^{(3), \text{CuLBM1}} = & (-12\omega_6 c_s^4 \omega_8^2 \omega_3^2 + 36\omega_6 \omega_8 \omega_3^2 v_3^2 - 12\omega_6^3 c_s^2 \omega_8 \omega_2 + 6\omega_6^3 c_s^4 \omega_3 \omega_2^2 - 12\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 36\omega_6 c_s^2 \omega_8^2 \omega_2^2 v_3^2 - 12c_s^5 \omega_2^2 \omega_3^2 - 18\omega_6^3 c_s^2 \omega_8^2 \omega_2 v_3^2 - \\ & 90\omega_6^2 c_s^2 \omega_8^2 \omega_3^2 v_3^4 - 108\omega_6^2 c_s^2 \omega_3^2 v_3^2 - 39\omega_6^3 \omega_8 \omega_3^2 v_3^4 + 18\omega_6^2 c_s^2 \omega_2^2 \omega_3^2 v_3^2 - 108\omega_6^3 c_s^2 \omega_2^2 v_3^2 - 12\omega_6 c_s^4 \omega_8^2 \omega_2^2 + 54\omega_6^3 c_s^2 \omega_8 \omega_2^2 v_3^2 + 6\omega_6^3 c_s^2 \omega_8 \omega_2^2 - 36\omega_6^3 \omega_3^2 v_3^2 - \\ & 18\omega_6^3 c_s^4 \omega_8 \omega_2^2 - 4\omega_6^3 \omega_8^2 \omega_3^2 v_3^2 + 12\omega_6 c_s^2 \omega_8^2 \omega_2^2 + 72\omega_6^2 \omega_3^2 v_3^4 + 72\omega_6^2 \omega_8 \omega_3^2 v_3^4 - 306\omega_6 c_s^2 \omega_8^2 \omega_3^2 v_3^2 + 12\omega_6^3 c_s^4 \omega_8 \omega_2 + 12\omega_6^3 c_s^4 \omega_8 \omega_2^2 - 19\omega_6^2 \omega_2^2 \omega_3^2 v_3^2 + \\ & 12c_s^4 \omega_2^2 \omega_3^2 - 6\omega_6^3 c_s^2 \omega_8 \omega_2^2 - 36\omega_6^2 \omega_3^2 v_3^4 + 36\omega_6^2 \omega_2^2 v_3^2 + 6\omega_6^3 \omega_2^2 \omega_3^2 v_3^2 - 99\omega_6^3 c_s^2 \omega_8 \omega_2^2 v_3^2 + 12\omega_6 c_s^2 \omega_2^2 \omega_3^2 + 108\omega_6^3 c_s^2 \omega_3^2 v_3^2 + 36\omega_6^3 \omega_8 \omega_2^2 v_3^4 + \\ & 18\omega_6^3 c_s^2 \omega_8 \omega_2^2 - 6\omega_6^2 c_s^4 \omega_8 \omega_2^2 + 60\omega_6^2 c_s^2 \omega_8^2 \omega_3^2 v_3^2 - 108\omega_6^2 c_s^2 \omega_8 \omega_3^2 v_3^2 + 19\omega_6^2 \omega_8^2 \omega_3^2 v_3^4 + 12\omega_6^3 c_s^4 \omega_8^2 + 36\omega_6^2 \omega_3^2 v_3^2 + 6\omega_6^3 c_s^4 \omega_3^2 - 72\omega_6^2 \omega_3^2 v_3^2 - \\ & 72\omega_6^2 \omega_8 \omega_3^2 v_3^2 - 5\omega_6^3 c_s^2 \omega_8 \omega_2^2 + 12\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 24\omega_6^3 c_s^4 \omega_8 \omega_2^2 - 36\omega_6^3 \omega_8 \omega_2^2 v_3^2 + 198\omega_6^2 c_s^2 \omega_8 \omega_2^2 v_3^2 - 36\omega_6^2 \omega_3^2 v_3^4 - 6\omega_6^3 c_s^2 \omega_2^2 v_3^4 + 6\omega_6^3 c_s^2 \omega_2^2 \omega_3^2 + \\ & 90\omega_6^2 \omega_8^2 \omega_3^2 v_3^2 + 36\omega_6^3 c_s^2 \omega_8 \omega_2^2 v_3^2 - 36\omega_6^2 \omega_8^2 \omega_3^2 v_3^4 + 13\omega_6^3 c_s^4 \omega_8 \omega_2^2 - \omega_6^2 c_s^2 \omega_2^2 \omega_3^2 + 36\omega_6^3 \omega_3^2 v_3^4 + 36\omega_6^2 c_s^2 \omega_8 \omega_2^2 v_3^2 + 6\omega_6^3 c_s^2 \omega_8 \omega_2 + 4\omega_6^3 \omega_8^2 \omega_3^2 v_3^4 + \\ & 252c_s^2 \omega_8^2 \omega_3^2 v_3^2 - 6\omega_6^2 c_s^2 \omega_8 \omega_2^2 + 39\omega_6^3 \omega_8 \omega_2^2 v_3^2 - \omega_6^2 c_s^4 \omega_8 \omega_2^2 - 3\omega_6^3 c_s^2 \omega_8 \omega_2^2 v_3^2) \frac{\rho}{12\omega_6^2 \omega_8^2 \omega_3^2} \end{aligned}$$

$$\begin{aligned}
C(3), \text{CuLBM2} &= (-108\omega_3\omega_4c_2^5\omega_1^2\omega_3^2 + 24\omega_3\omega_4^2\omega_1^3\omega_2\omega_3^2 - 96\omega_3^2\omega_1^4\omega_1^3\omega_3^2 + 264\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 + 72\omega_3^2\omega_4c_4^5\omega_1\omega_3^2 + 38\omega_3^2\omega_4^2\omega_1^3\omega_2^2\omega_3^2 - \\
D_{\mathbb{P}} \mathbf{x}_2^2 \mathbf{v}_1 &216\omega_3\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 24\omega_3^2\omega_1^4c_2^5\omega_1^2\omega_3^2 + 2\omega_3^2\omega_1^3\omega_1^2\omega_3^2 - 16\omega_3\omega_4^2c_2^5\omega_1^3\omega_2 + 72\omega_3^2\omega_1^4c_2^5\omega_1^3\omega_3^2 + 36\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2 - 2\omega_3^2\omega_4^2c_4^5\omega_1^3\omega_3^2 + 18\omega_3\omega_4^2c_4^5\omega_1^3\omega_3^2 + \\
&192\omega_3^2\omega_1^2\omega_3^2\omega_3^2 - 12\omega_3^2\omega_1^4c_2^5\omega_1^2\omega_3^2 + 72\omega_3\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 - 24\omega_3\omega_4^2\omega_1\omega_3^2\omega_3^2 + 576\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 + 117\omega_3^2\omega_4\omega_1\omega_3^2\omega_3^2 + 24\omega_3^2\omega_4^2c_2^5\omega_1\omega_3^2 + 8\omega_3^2\omega_1^2c_2^5\omega_3^2 - \\
&8\omega_3^2\omega_1^4\omega_1^2\omega_2 - 6\omega_3^2\omega_4^2c_4^5\omega_1^2\omega_3^2 - 40\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2 + 54\omega_4^2\omega_1^3\omega_2^2\omega_3^2 - 108\omega_3\omega_4\omega_1^3\omega_2^2\omega_3^2 - 288\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 + 12\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 - 56\omega_3^2\omega_4^2c_4^5\omega_1^2\omega_2 \\
&36\omega_3^2\omega_4\omega_1^2\omega_3^2\omega_3^2 + 336\omega_3^2\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 + 144\omega_3^2\omega_1^2\omega_1^2\omega_3^2\omega_3^2 + 204\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 288\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2 + 54\omega_3^2\omega_1^2\omega_3^2\omega_3^2 + 144\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + \\
&108\omega_3\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 36\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 + 8\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 36\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 36\omega_3\omega_4^2c_4^5\omega_1^3\omega_3^2 - 297\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 - 40\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 - \\
&180\omega_3\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 72\omega_3^2\omega_1^2\omega_3^2\omega_3^2 + 72\omega_3\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 + 264\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 - 72\omega_3^2\omega_4^2c_2^5\omega_1\omega_3^2 - 48\omega_3^2\omega_4\omega_1\omega_3^2\omega_3^2 - 216\omega_3^2c_2^5\omega_1\omega_3^2\omega_3^2 - \\
&36\omega_3\omega_4^2c_4^5\omega_1^2\omega_3^2 + 16\omega_3\omega_4^2c_4^5\omega_1^3\omega_2 + 144\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 + 24\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 36\omega_3^2\omega_4\omega_1^3\omega_3^2\omega_3^2 - 8\omega_3^2\omega_4^2\omega_1^2\omega_3^2 + 60\omega_3\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 20\omega_3^2\omega_4^2c_4^5\omega_1^2\omega_3^2 + \\
&108\omega_3^2\omega_1^2\omega_3^2\omega_3^2 - 18\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2 + 168\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 96\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 + 324\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 24\omega_3^2\omega_4^2\omega_1^3\omega_3^2\omega_3^2 + 48\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - \\
&288\omega_3^2\omega_1^2\omega_3^2\omega_3^2 + 240\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 64\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 + 108\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 - 324\omega_3^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 40\omega_3\omega_4^2c_4^5\omega_1^2\omega_3^2 - 297\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 - \\
&48\omega_3^2\omega_4\omega_1\omega_3^2\omega_3^2 - 117\omega_3\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 72\omega_3^2\omega_4\omega_1\omega_3^2\omega_3^2 + 48\omega_3\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 + 288\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 - 852\omega_3^2\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 + 36\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2 - \\
&96\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 86\omega_3^2\omega_4^2c_4^5\omega_1^2\omega_3^2 - 8\omega_3^2\omega_1^2\omega_3^2\omega_3^2 - 432\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 2\omega_3^2\omega_4^2\omega_1^2\omega_3^2 - 28\omega_3^2\omega_4^2c_4^5\omega_1^3\omega_2 + 36\omega_3\omega_4\omega_1^3\omega_3^2\omega_3^2 + 96\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 - \\
&36\omega_4^2\omega_1^3\omega_3^2\omega_3^2 - 16\omega_3^2\omega_4^2\omega_3^2 + 432\omega_3^2\omega_4^2c_2^5\omega_3^2\omega_3^2 - 60\omega_3\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 80\omega_3^2\omega_4^2c_4^5\omega_3^2 - 108\omega_3^2\omega_2^2\omega_3^2\omega_3^2 - 108\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 - 144\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 + \\
&64\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 24\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 - 144\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 24\omega_3^2\omega_1^2\omega_3^2\omega_3^2 - 96\omega_3\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 + 180\omega_3\omega_4\omega_1^2\omega_3^2\omega_3^2 - 72\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + \\
&16\omega_3^2\omega_4\omega_1\omega_3^2 + 36\omega_3^2\omega_4\omega_1^2\omega_3^2\omega_3^2 - 172\omega_3^2\omega_4^2c_4^5\omega_1\omega_3^2 - 288\omega_3^2\omega_4\omega_1^2\omega_3^2\omega_3^2 - 108\omega_4^2c_2^5\omega_1^2\omega_3^2 + 72\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 + 6\omega_3^2\omega_4^2\omega_1^2\omega_3^2 + 48\omega_3\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 - \\
&36\omega_3\omega_4\omega_1^2\omega_3^2\omega_3^2 - 144\omega_3^2\omega_4^2\omega_1\omega_3^2\omega_3^2 + 16\omega_3\omega_4^2c_4^5\omega_1\omega_3^2 + 36\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 492\omega_3^2\omega_4^2c_2^5\omega_1\omega_3^2\omega_3^2 - 144\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 + 16\omega_3^2\omega_4^2c_2^5\omega_1\omega_3^2 + 16\omega_3^2\omega_4\omega_1\omega_3^2 + \\
&174\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 18\omega_3^2\omega_4^2c_4^5\omega_1^2\omega_3^2 + 24\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2 + 144\omega_3^2\omega_4^2\omega_1^2\omega_3^2\omega_3^2 - 12\omega_3^2\omega_4^2c_2^5\omega_1^2\omega_3^2\omega_3^2 + 117\omega_3\omega_4^2\omega_1^2\omega_$$

$$96\omega_3^2\omega_4\omega_1\omega_2^3v_3^2 - 32\omega_3^2\omega_1^2c_s^2\omega_1\omega_2^2 + 36\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 + 24\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 24\omega_3^2\omega_4^2\omega_1^3v_1^2 - 18\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^3 + 162\omega_4^2c_s^2\omega_1^3\omega_2^3v_3) \frac{\rho}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3}$$

coefficient $C_{D_x D_z^3 v_3}^{(3)}$ at $\frac{\partial^4 v_3}{\partial x_1 \partial x_3^3}$:

$$C_{D_x D_z^3 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_3}^{(3), \text{MRT1}} = (25\omega_6^2c_s^2\omega_{11}^2\omega_{18}^2 + 24\omega_6^2\omega_{11}\omega_{18} - 16\omega_6c_s^2\omega_{11}^3 - 68\omega_6\omega_{11}^2v_3^2\omega_{18}^2 - 16\omega_6\omega_{11}^3v_3^2 + 16\omega_6\omega_{11}^2\omega_{18} - 25\omega_6^2c_s^2\omega_{11}^3\omega_{18} - 32\omega_6^2\omega_{18}^2 - 64\omega_6^2\omega_{11}v_3^2\omega_{18} - 43\omega_6^2\omega_{11}^2v_3^2\omega_{18} + 28\omega_{11}^2v_3^2\omega_{18}^2 - 120\omega_6^2\omega_{11}v_3^2\omega_{18}^2 + 28\omega_6\omega_{11}^2\omega_{18} + 12\omega_{11}^3\omega_{18} + 48\omega_6^2c_s^2\omega_{18}^2 - 48\omega_6\omega_{11}^2v_3^2\omega_{18} + 8\omega_6\omega_{11}^3 + 32\omega_6c_s^2\omega_{11}\omega_{18}^2 + 48\omega_6^2\omega_{11}\omega_{18} + 56\omega_6^2c_s^2\omega_{11}^2\omega_{18} - 12\omega_{11}^2\omega_{18} - 28\omega_6\omega_{11}^3\omega_{18} + 43\omega_6\omega_{11}^2v_3^2\omega_{18} - 28\omega_{11}^2v_3^2\omega_{18} - 44\omega_6c_s^2\omega_{11}^2\omega_{18} - 8\omega_6^2\omega_{11}^3 - 32\omega_6^2c_s^2\omega_{11}\omega_{18} - 17\omega_6^2\omega_{11}^2\omega_{18} - 24\omega_6\omega_{11}\omega_{18} + 17\omega_6^2\omega_{11}^2\omega_{18} - 16\omega_6^2\omega_{11}^2v_3^2 + 8\omega_6^2\omega_{11}^2 + 44\omega_6c_s^2\omega_{11}^3\omega_{18} + 20c_s^2\omega_{11}^2\omega_{18} + 64\omega_6\omega_{11}^2v_3^2\omega_{18} + 16\omega_6^2c_s^2\omega_{11}^3 + 68\omega_6\omega_{11}^2v_3^2\omega_{18} - 16\omega_6c_s^2\omega_{11}^2\omega_{18} - 40\omega_6^2\omega_{11}^2\omega_{18} - 72\omega_6^2c_s^2\omega_{11}\omega_{18} + 80\omega_6^2v_3^2\omega_{18} + 16\omega_6^2\omega_{11}^2v_3^2 - 20c_s^2\omega_{11}^3\omega_{18} - 16\omega_6^2c_s^2\omega_{11}^2 + 104\omega_6^2\omega_{11}^2v_3^2\omega_{18}) \frac{\rho v_1 v_3}{4\omega_6^2\omega_{11}^3\omega_{18}^2}$$

$$C_{D_x D_z^3 v_3}^{(3), \text{MRT2}} = C_{D_x D_z^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x D_z^3 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_z^3 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_z^3 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^3 v_3}^{(3), \text{CuLBM2}} = (-66\omega_3\omega_1\omega_2^3v_3^2 - 54\omega_3c_s^2\omega_1\omega_2^2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^3 + 6\omega_3\omega_1^2v_1^2\omega_2 + 27c_s^2\omega_1^3\omega_2^2 - 6\omega_1^3v_1^2\omega_2 - 24\omega_3v_1^2\omega_2^3 - 51\omega_3\omega_1^2\omega_2^2 + 27\omega_3c_s^2\omega_1\omega_2^3 - 12\omega_1\omega_2^3 + 12\omega_1v_1^2\omega_2^3 + 84\omega_3c_s^2\omega_1^3 - 18c_s^2\omega_1^2\omega_2^2 - 5\omega_3\omega_1^2v_1^2\omega_2^3 + 6\omega_3\omega_1^2\omega_2 - 12\omega_3c_s^2\omega_2^3 - 120\omega_3\omega_1\omega_2^2v_3^2 - 18c_s^2\omega_1^3\omega_2 + 9\omega_1^3v_1^2\omega_2^2 - 27c_s^2\omega_1^2\omega_2^3 - 12\omega_3\omega_1^2\omega_2v_3^2 - 5\omega_3\omega_1^3\omega_2^2 + 48\omega_3\omega_1^3v_3^2 - 9\omega_3\omega_1^2v_1^2\omega_2^2 + 12\omega_3\omega_1^3v_1^2 + 36c_s^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 + 132\omega_3\omega_1^2\omega_2^2v_3^2 + 27\omega_3\omega_1v_1^2\omega_2^2 - 9\omega_1^3\omega_2^2 + 6\omega_3\omega_1v_1^2\omega_2^2 - 18\omega_3\omega_1^3v_1^2\omega_2 + 84\omega_3\omega_2^3v_3^2 + 15\omega_3c_s^2\omega_1^3\omega_2^2 - 12\omega_3\omega_2^3 - 66\omega_3\omega_1^3\omega_2v_3^2 - 15\omega_3c_s^2\omega_1^2\omega_2^3 + 5\omega_3\omega_1^3v_1^2\omega_2^2 + 42\omega_3\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 + 6\omega_1^3\omega_2 + 9\omega_1^2\omega_2^2 - 6\omega_1^2v_1^2\omega_2^2 - 36\omega_3\omega_1^3 + 3\omega_3\omega_1\omega_2^2 + 81\omega_3c_s^2\omega_1^2\omega_2^2 - 9\omega_1^2v_1^2\omega_2^2 + 6\omega_1^2\omega_2^2) \frac{\rho v_1 v_3}{18\omega_3\omega_1^3\omega_2^3}$$

coefficient $C_{D_y D_z^3 \rho}^{(3)}$ at $\frac{\partial^4 \rho}{\partial x_2 \partial x_3^3}$:

$$C_{D_y D_z^3 \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z^3 \rho}^{(3), \text{MRT1}} = (4\omega_{19}\omega_7^2c_s^2\omega_{11}^3 - 48\omega_{19}\omega_7c_s^2\omega_{11}^2v_3^2 - 4\omega_{19}\omega_7c_s^2\omega_{11} + 20\omega_{19}\omega_7\omega_{11}v_3^4 + 96\omega_{19}\omega_7^2c_s^2v_3^2 + 4\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 36\omega_{19}\omega_7^2\omega_{11}v_3^2 + 4\omega_{19}c_s^2\omega_{11}^3 - 24\omega_7^2c_s^2\omega_{11}^2v_3^2 + 13\omega_{19}\omega_7^2\omega_{11}^3v_3^2 + 8\omega_{19}\omega_{11}^3v_3^2 + 4\omega_7^2\omega_{11}^3v_3^2 - 4\omega_7c_s^4\omega_{11}^3 + 20\omega_{19}\omega_7\omega_{11}^3v_3^4 - 8\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 36\omega_{19}c_s^2\omega_{11}^2v_3^2 + 13\omega_{19}\omega_7^2\omega_{11}^3v_3^2 - 84\omega_{19}\omega_7c_s^2\omega_{11}^2v_3^2 + 8\omega_{19}\omega_7^2c_s^4 + 20\omega_{19}\omega_7\omega_{11}^2v_3^2 - 4\omega_7^2c_s^2\omega_{11}^3 + 24\omega_7^2c_s^2\omega_{11}^2v_3^2 - 144\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 4\omega_{19}c_s^4\omega_{11}^2 + 4\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 84\omega_{19}\omega_7c_s^2\omega_{11}^3v_3^2 - 12\omega_{19}\omega_7^2c_s^4\omega_{11} - 32\omega_{19}\omega_7^2\omega_{11}^2v_3^2 + 8\omega_{19}\omega_7c_s^4\omega_{11}^3 + 8\omega_{19}\omega_{11}^3v_3^4 + 4\omega_7^2c_s^2\omega_{11}^2 - 4\omega_7\omega_{11}^3v_3^4 + 24\omega_{19}\omega_7^2v_3^4 - 4\omega_7^2\omega_{11}^3v_3^2 - 16\omega_{19}\omega_7\omega_{11}^3v_3^4 + 8\omega_{19}\omega_7c_s^2\omega_{11}^2 - 72\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 8\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 20\omega_{19}\omega_7^2\omega_{11}v_3^2 + 4\omega_7c_s^2\omega_{11}^3 + 120\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 - 4\omega_{19}\omega_7^2c_s^4\omega_{11}^3 - 24\omega_{19}\omega_7^2v_3^2 + 4\omega_7^2\omega_{11}^3v_3^4 + 16\omega_{19}\omega_7\omega_{11}^2v_3^2 + 4\omega_{19}\omega_7c_s^4\omega_{11} + 51\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 - 4\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 32\omega_{19}\omega_7^2\omega_{11}^3v_3^4 - 4\omega_{19}c_s^4\omega_{11}^3 + 4\omega_7\omega_{11}^3v_3^2 - 8\omega_{19}\omega_{11}^2v_3^2 + 12\omega_{19}\omega_7c_s^2\omega_{11} - 51\omega_{19}\omega_7^2c_s^2\omega_{11}^3v_3^2 - 36\omega_{19}\omega_7^2\omega_{11}v_3^4 - 4\omega_7^2c_s^4\omega_{11}^2 - 8\omega_{19}\omega_7c_s^2\omega_{11}^3 + 72\omega_{19}\omega_7c_s^2\omega_{11}^2v_3^2 - 8\omega_{19}\omega_7c_s^4\omega_{11}^2 - 20\omega_{19}\omega_7\omega_{11}v_3^2 - 24\omega_7c_s^2\omega_{11}^3 - 13\omega_{19}\omega_7^2\omega_{11}^3v_3^4 - 8\omega_{19}\omega_7^2c_s^2 - 20\omega_{19}\omega_7\omega_{11}^3v_3^4 - 13\omega_{19}\omega_7^2\omega_{11}^2v_3^2 - 36\omega_{19}c_s^2\omega_{11}^3v_3^2 - 4\omega_7^2\omega_{11}^3v_3^4 - 8\omega_{19}\omega_{11}^3v_3^4 - 4\omega_{19}c_s^2\omega_{11}^2 - 20\omega_{19}\omega_7\omega_{11}^3v_3^2 - 4\omega_{19}\omega_7^2c_s^4\omega_{11}) \frac{v_2}{4\omega_{19}^2\omega_7^2\omega_{11}^3}$$

$$C_{D_y D_z^3 \rho}^{(3), \text{MRT2}} = C_{D_y D_z^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^3 \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^3 \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^3 \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^3 \rho}^{(3), \text{CuLBM2}} = (8\omega_3^2\omega_1\omega_2^2 - 18\omega_3c_s^2\omega_1^2v_2^2\omega_2^3 + \omega_3^2\omega_1^2v_2^2\omega_2^3 + 24\omega_3^2\omega_1v_2^2\omega_2^3v_3^2 + 40\omega_3^2c_s^2\omega_1^2\omega_2 - 24\omega_3^2\omega_1^2\omega_2^2v_3^2 - 72\omega_3^2\omega_1\omega_2^2v_3^4 - 84\omega_3^2c_s^4\omega_1^3\omega_2 - 48\omega_3^2\omega_1^3v_2^2\omega_2v_3^2 - 6\omega_3^2c_s^4\omega_1^2\omega_2^3 + 12c_s^2\omega_1^3\omega_2^2 - 2\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^2 + 8\omega_3^2v_2^2\omega_2^3 - 5\omega_3^2c_s^2\omega_1^3\omega_2^2 + 36c_s^4\omega_1^2\omega_2^3 - 4\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 - 8\omega_3c_s^2\omega_1\omega_2^3 + 216\omega_3^2c_s^2\omega_1^3v_3^2 + 8\omega_3^2\omega_1\omega_2^3 + 4\omega_3^2\omega_1^2v_2^2\omega_2^2 + 16\omega_3^2c_s^2\omega_1^3v_2^2 - 2\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^2 - 36\omega_3^2c_s^4\omega_2^3 + 4\omega_3^2\omega_1^3 + 42\omega_3^2c_s^4\omega_1^2\omega_2^2 + 216\omega_3^2c_s^2\omega_1^2\omega_2^2v_3^2 - 36\omega_3^2c_s^4\omega_1^2\omega_2 - 36\omega_3^2\omega_1\omega_2^3v_3^2 + 12c_s^2\omega_1^2v_2^2\omega_2^3 + 5\omega_3^2c_s^2\omega_1^2\omega_2^3 + 24\omega_3^2\omega_1^2\omega_2^2v_3^2 + 72\omega_3^2c_s^4\omega_1^3 + 56\omega_3^2c_s^2\omega_1^3\omega_2 - 8\omega_3^2\omega_2^3 - 36c_s^4\omega_1^3\omega_2^2 + 4\omega_3^2\omega_1^2v_2^2\omega_2 + 96\omega_3^2\omega_1v_2^2\omega_2^3v_3^2 + 84\omega_3^2\omega_1^2\omega_2v_3^2 + 6\omega_3^2c_s^4\omega_1^2\omega_2^2 + 24\omega_3^2\omega_1^3v_3^4 - 72\omega_3^2c_s^2\omega_1^2\omega_2^3v_3^2 + 24\omega_3c_s^4\omega_1\omega_2^3 - 4\omega_3^2c_s^2\omega_1^2v_2^2\omega_2 - 324\omega_3^2c_s^2\omega_1^3\omega_2v_3^2 - 12c_s^2\omega_1^2\omega_2^3 + 24\omega_3^2\omega_2^3v_3^2 + 24\omega_3^2\omega_1^2v_2^2\omega_2v_3^2 - 34\omega_3^2c_s^2\omega_1^2\omega_2^2 - 72\omega_3^2v_2^2\omega_2^3v_3^2 + 72\omega_3^2c_s^2\omega_1^3\omega_2^2v_3^2 - 12\omega_3c_s^4\omega_1^3\omega_2 - 36\omega_3^2\omega_1^3\omega_2v_3^4 - 54\omega_3c_s^4\omega_1^2\omega_2^2 + 24\omega_3^2\omega_1^3v_2^2v_3^2 - 4\omega_3^2\omega_1^2\omega_2 + 20\omega_3^2c_s^2\omega_2^3 - 8\omega_3^2c_s^2\omega_1\omega_2^2 - 60\omega_3^2\omega_1\omega_2^3v_3^2 - \omega_3^2\omega_1^3v_2^2\omega_2^2 + 18\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 - 48\omega_3^2\omega_1^2v_2^2\omega_2^2v_3^2 - 12\omega_3c_s^4\omega_1^2\omega_2^2 + 48\omega_3^2\omega_2^3v_3^4 + 108\omega_3^2c_s^2\omega_1\omega_2^3v_3^2 + 2\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 - 4\omega_3^2\omega_2^3v_2^2 - 48\omega_3^2\omega_1^3v_3^2 - 22\omega_3^2c_s^2\omega_1\omega_2^3 - 24\omega_3^2\omega_1^3v_2^2\omega_2^2 - 20\omega_3^2c_s^2v_2^2\omega_2^2 - 18\omega_3c_s^2\omega_1^3\omega_2^2 + \omega_3^2\omega_1^3\omega_2^2 +$$

$$48\omega_3^2\omega_1\omega_2^2v_3^2 - 24\omega_3^2\omega_1^2v_2^2\omega_3^2v_3^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 - \omega_3^2\omega_2^2\omega_3^2 + 8\omega_3c_s^2\omega_1v_2^2\omega_3^2 - 4\omega_3^2\omega_1^3\omega_2 + 4\omega_3c_s^2\omega_1^3\omega_2 - 8\omega_3^2\omega_1v_2^2\omega_3^2 - 12c_s^2\omega_1^3v_2^2\omega_2^2 + 8\omega_3^2c_s^2\omega_1v_2^2\omega_2^2 - 20\omega_3^2c_s^2\omega_1^2v_2^2\omega_2 + 72\omega_3^2\omega_1^2\omega_2^2v_3^4 - 8\omega_3^2\omega_1v_2^2\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2^2 + 4\omega_3c_s^2\omega_1^3v_2^2\omega_2 - 4\omega_3c_s^2\omega_1^3v_2^2\omega_2 - 24\omega_3^2\omega_1^2\omega_2v_3^2 + 4\omega_3^2\omega_1^3v_2^2\omega_2 + 42\omega_3^2c_s^4\omega_1\omega_2^2 + 24\omega_3^2\omega_1^3v_2^2\omega_2^2v_3^2 - 216\omega_3^2c_s^2\omega_1\omega_2^2v_3^2 - 52\omega_3^2c_s^2\omega_1^3 + 54\omega_3c_s^4\omega_1^3\omega_2^2 + 22\omega_3^2c_s^2\omega_1v_2^2\omega_2^2) \frac{v_2}{36\omega_3^2\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_y D_2^2 v_2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_2^2 v_2}^{(3), \text{SRT}} = (-42c_s^2\omega^2v_3^2 + 36c_s^2\omega - 36v_3^4 + 4\omega^3v_3^4 + 12c_s^2\omega^3v_3^2 - 54\omega v_3^2 - 26\omega^2v_3^4 - 12c_s^2\omega^2 + 36c_s^4 + 54\omega v_3^4 - 36c_s^2v_3^2 + 26\omega^2v_3^2 - 54c_s^4\omega - 24c_s^2 + 20c_s^4\omega^2 - 4\omega^3v_3^2 - c_s^4\omega^3 + 54c_s^2\omega v_3^2 + 36v_3^2) \frac{\rho}{12\omega^3}$$

$$C_{D_y D_2^2 v_2}^{(3), \text{MRT}^1} = (-\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 + 18\omega_{19}\omega_7^2c_s^2\omega_{11}^3 + 60\omega_{19}\omega_7^2\omega_{11}^2v_3^4 + 12\omega_7^2\omega_{11}^3v_3^4 + 6\omega_{19}^2\omega_7^2c_s^4\omega_{11}^2 - 36\omega_{19}\omega_7^3c_s^2\omega_{11}v_3^2 + 6\omega_{19}\omega_7^3c_s^4\omega_{11}^3 - 4\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 + 12\omega_{19}^2\omega_7^2\omega_{11}^3v_3^4 - 306\omega_{19}^2\omega_7^3c_s^2\omega_{11}v_3^2 + 12\omega_7^2c_s^2\omega_{11}^3v_3^2 + 72\omega_{19}^2\omega_7^3v_3^4 - 24\omega_{19}\omega_7\omega_{11}^3v_3^4 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 48\omega_{19}\omega_7^3\omega_{11}^2v_3^2 - 48\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2v_3^2 + 36\omega_{19}\omega_7^2\omega_{11}^3v_3^2 + 13\omega_{19}^2\omega_7^2c_s^4\omega_{11}^2 - 6\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 12\omega_7^2c_s^2\omega_{11}^3v_3^2 - 19\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 - 108\omega_{19}^2\omega_7^2c_s^2\omega_{11}v_3^2 - 12\omega_7^2\omega_{11}^3v_3^4 - 27\omega_{19}\omega_7^3\omega_{11}^2v_3^4 + 6\omega_{19}^2\omega_7^2c_s^2\omega_{11}^3 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^3v_3^2 - 12\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 - 12\omega_{19}^2\omega_7^2c_s^4\omega_{11} + 24\omega_{19}\omega_7^2\omega_{11}^2v_3^2 - 48\omega_{19}^2c_s^2\omega_{11}^3v_3^2 + 12\omega_{19}^2\omega_7^3c_s^4 + 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 102\omega_{19}^2\omega_7^2c_s^2\omega_{11}^3v_3^2 - 90\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 + 12\omega_7^2\omega_{11}^3v_3^2 - 12\omega_7^2c_s^2\omega_{11}^3v_3^2 + 12\omega_{19}^2\omega_7^3c_s^2\omega_{11} + 12\omega_{19}^2c_s^4\omega_{11}^3 - 18\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 + 27\omega_{19}\omega_7^3\omega_{11}^2v_3^2 + 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - \omega_{19}\omega_7^2c_s^4\omega_{11}^3 + 19\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 + 6\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 12\omega_{19}\omega_7^2c_s^2\omega_{11}^3v_3^2 - 5\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 12\omega_7^2\omega_{11}^3v_3^2 - 18\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 90\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 + \omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 12\omega_7^2\omega_{11}^3v_3^4 - 21\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 18\omega_{19}\omega_7^2\omega_{11}^3v_3^2 + 162\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2v_3^2 - 6\omega_{19}\omega_7^2c_s^2\omega_{11}^3 - 6\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 + 12\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 - 24\omega_{19}\omega_7^2\omega_{11}^3v_3^4 + 252\omega_{19}^2\omega_7^2c_s^2v_3^2 - 12\omega_{19}^2\omega_7^3c_s^2 + 60\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2v_3^2 + 12\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 - 12\omega_7^2\omega_{11}^3v_3^2 + 30\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 4\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 12\omega_{19}^2\omega_7^3c_s^4\omega_{11} - 60\omega_{19}\omega_7^2\omega_{11}^2v_3^2 + 48\omega_{19}\omega_7^2\omega_{11}^3v_3^4 - 36\omega_{19}\omega_7^3\omega_{11}^2v_3^2 + 54\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 - 12\omega_{19}^2\omega_7^2\omega_{11}^3v_3^2 - 81\omega_{19}^2\omega_7^2c_s^2\omega_{11}^3v_3^2 - 24\omega_{19}^2\omega_7^2c_s^4\omega_{11}^2 - 72\omega_{19}^2\omega_7^3v_3^2 + 24\omega_{19}\omega_7\omega_{11}^3v_3^2) \frac{\rho}{12\omega_{19}^2\omega_7^2\omega_{11}^3}$$

$$C_{D_y D_2^2 v_2}^{(3), \text{MRT}^2} = C_{D_y D_2^2 v_2}^{(3), \text{MRT}^1}$$

$$C_{D_y D_2^2 v_2}^{(3), \text{CLBM}^1} = (-\omega_{19}^2\omega_7^3c_s^2\omega_{11}^2 + 18\omega_{19}\omega_7^2c_s^2\omega_{11}^3 + 72\omega_{19}\omega_7^3\omega_{11}^2v_3^4 + 36\omega_7^3\omega_{11}^3v_3^4 + 6\omega_{19}^2\omega_7^2c_s^4\omega_{11}^2 - 108\omega_{19}\omega_7^3c_s^2\omega_{11}v_3^2 + 6\omega_{19}\omega_7^3c_s^4\omega_{11}^3 - 4\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 - 306\omega_{19}^2\omega_7^3c_s^2\omega_{11}v_3^2 + 108\omega_7^3c_s^2\omega_{11}^3v_3^2 + 72\omega_{19}^2\omega_7^3v_3^4 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 36\omega_{19}\omega_7^3\omega_{11}^2v_3^2 + 36\omega_{19}\omega_7^3\omega_{11}^3v_3^2 + 13\omega_{19}^2\omega_7^2c_s^4\omega_{11}^2 - 108\omega_{19}^2c_s^2\omega_{11}^3v_3^2 - 19\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 - 36\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2v_3^2 - 36\omega_7^3\omega_{11}^3v_3^4 - 39\omega_{19}\omega_7^3\omega_{11}^2v_3^4 + 6\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 36\omega_{19}\omega_7^2c_s^2\omega_{11}^3v_3^2 - 12\omega_{19}\omega_7^2c_s^4\omega_{11} + 12\omega_{19}^2\omega_7^2c_s^4 + 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 18\omega_{19}^2\omega_7^3c_s^2\omega_{11}^2v_3^2 - 90\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 + 36\omega_7^3\omega_{11}^3v_3^2 - 108\omega_7^2c_s^2\omega_{11}^3v_3^2 + 12\omega_{19}^2\omega_7^3c_s^2\omega_{11} + 12\omega_{19}^2c_s^4\omega_{11}^3 - 6\omega_{19}\omega_7^3\omega_{11}^2v_3^4 + 39\omega_{19}\omega_7^3\omega_{11}^2v_3^2 + 12\omega_{19}\omega_7^2c_s^4\omega_{11}^2 - \omega_{19}\omega_7^2c_s^4\omega_{11}^3 + 19\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 + 6\omega_{19}\omega_7^2c_s^2\omega_{11}^2 + 12\omega_{19}\omega_7^2c_s^2\omega_{11}^3v_3^2 - 5\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 12\omega_7^3\omega_{11}^3v_3^2 + 36\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 36\omega_7^3\omega_{11}^3v_3^2 - 18\omega_{19}\omega_7^2c_s^4\omega_{11}^2 + 90\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 + \omega_{19}\omega_7^2c_s^4\omega_{11}^2 - 36\omega_7^3\omega_{11}^3v_3^4 - 36\omega_7^2\omega_{11}^3v_3^4 - 99\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 6\omega_{19}^2\omega_7^3\omega_{11}^2v_3^2 + 18\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2v_3^2 - 6\omega_{19}\omega_7^2c_s^2\omega_{11}^3 - 6\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 + 252\omega_{19}^2\omega_7^2c_s^2v_3^2 - 12\omega_{19}^2\omega_7^3c_s^2 + 60\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2v_3^2 + 12\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 - 36\omega_7^3\omega_{11}^3v_3^2 + 54\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 + 4\omega_{19}^2\omega_7^3\omega_{11}^2v_3^4 - 12\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 12\omega_{19}^2\omega_7^3c_s^4\omega_{11} - 72\omega_{19}\omega_7^2\omega_{11}^2v_3^2 + 36\omega_{19}\omega_7^2\omega_{11}^3v_3^4 - 36\omega_{19}\omega_7^3\omega_{11}^2v_3^2 + 198\omega_{19}\omega_7^2c_s^2\omega_{11}^2v_3^2 - 3\omega_{19}^2\omega_7^2c_s^2\omega_{11}^3v_3^2 - 24\omega_{19}^2\omega_7^2c_s^4\omega_{11}^2 - 72\omega_{19}^2\omega_7^3v_3^2) \frac{\rho}{12\omega_{19}^2\omega_7^2\omega_{11}^3}$$

$$C_{D_y D_2^2 v_2}^{(3), \text{CLBM}^2} = C_{D_y D_2^2 v_2}^{(3), \text{CLBM}^1}$$

$$C_{D_y D_2^2 v_2}^{(3), \text{CuLBM}^1} = (-6\omega_6^2\omega_3^2\omega_{10}c_s^4 + 18\omega_6^2\omega_3^2\omega_{10}c_s^2 + 36\omega_6\omega_3^2\omega_{10}v_3^2 + 36\omega_6^2\omega_3^2\omega_{10}c_s^2v_3^2 - 36\omega_6^2\omega_3^2v_3^4 + 12\omega_6^2\omega_3\omega_{10}c_s^4 - 108\omega_6^2\omega_3^2c_s^2v_3^2 - 3\omega_6^2\omega_3^2\omega_{10}c_s^2v_3^2 + 12\omega_6\omega_3^2\omega_{10}c_s^2 - 4\omega_6^2\omega_3^2\omega_{10}v_3^2 + 6\omega_6^2\omega_3\omega_{10}c_s^2 - 39\omega_6^2\omega_3^2\omega_{10}v_3^4 + 36\omega_6^2\omega_3^2v_3^2 + 12\omega_3^2\omega_{10}c_s^4 - \omega_6^2\omega_3^2\omega_{10}c_s^2 - 90\omega_6\omega_3^2\omega_{10}v_3^4 + 13\omega_6^2\omega_3^2\omega_{10}c_s^4 + 252\omega_6^2\omega_3^2\omega_{10}c_s^2v_3^2 + 72\omega_6^2\omega_3^2\omega_{10}v_3^4 - 36\omega_6^2\omega_3^2\omega_{10}v_3^2 + 36\omega_6^2\omega_3\omega_{10}c_s^2v_3^2 - 108\omega_6\omega_3^2\omega_{10}c_s^2v_3^2 + 6\omega_6^2\omega_3^2\omega_{10}c_s^4 + 198\omega_6^2\omega_3^2\omega_{10}c_s^2v_3^2 - 12\omega_6^2\omega_3\omega_{10}c_s^2 + 72\omega_6^2\omega_3\omega_{10}v_3^2 + 6\omega_6^2\omega_3^2\omega_{10}c_s^4 - 19\omega_6^2\omega_3^2\omega_{10}v_3^2 + 12\omega_6^2\omega_3^2\omega_{10}c_s^2v_3^2 - 36\omega_6^2\omega_3^2v_3^2 - 6\omega_6^2\omega_3^2\omega_{10}v_3^4 - 12\omega_6\omega_3^2\omega_{10}c_s^4 - 6\omega_6^2\omega_3^2\omega_{10}c_s^2 - 18\omega_6^2\omega_3\omega_{10}c_s^2v_3^2 - \omega_6^2\omega_3^2\omega_{10}c_s^4 - 72\omega_6^2\omega_3^2\omega_{10}v_3^2 - 306\omega_6\omega_3^2\omega_{10}c_s^2v_3^2 + 36\omega_6^2\omega_3^2\omega_{10}v_3^4 + 19\omega_6^2\omega_3^2\omega_{10}v_3^4 + 108\omega_6^2\omega_3^2c_s^2v_3^2 + 36\omega_6^2\omega_3^2v_3^4 + 6\omega_6^2\omega_3^2\omega_{10}v_3^4 + 12\omega_6\omega_3^2\omega_{10}c_s^2 + 60\omega_6\omega_3^2\omega_{10}c_s^2v_3^2 + 12\omega_6^2\omega_3\omega_{10}c_s^4 - 72\omega_6^2\omega_3\omega_{10}c_s^2 - 6\omega_6^2\omega_3^2\omega_{10}c_s^2 + 36\omega_6\omega_3^2\omega_{10}c_s^2v_3^2 + 18\omega_6\omega_3^2\omega_{10}c_s^2v_3^2 - 12\omega_6^2\omega_3\omega_{10}c_s^2 - 12\omega_6\omega_3^2\omega_{10}c_s^4 - 108\omega_6^2\omega_3^2c_s^2v_3^2 + 4\omega_6^2\omega_3^2\omega_{10}v_3^4 + 6\omega_6^2\omega_3^2\omega_{10}c_s^2 + 12\omega_6^2\omega_{10}c_s^4 + 54\omega_6^2\omega_3^2\omega_{10}c_s^2v_3^2 - 18\omega_6^2\omega_3\omega_{10}c_s^4 - 36\omega_6\omega_3^2\omega_{10}v_3^4 + \omega_6^2\omega_3^2\omega_{10}c_s^4 + 90\omega_6\omega_3^2\omega_{10}v_3^2 - 5\omega_6^2\omega_3^2\omega_{10}c_s^2 - 24\omega_6^2\omega_3^2\omega_{10}c_s^4 - 36\omega_6\omega_3^2\omega_{10}c_s^2v_3^2 + 39\omega_6^2\omega_3^2\omega_{10}v_3^2 - 36\omega_6^2\omega_3^2v_3^4 - 12\omega_3^2\omega_{10}c_s^2) \frac{\rho}{12\omega_6^2\omega_3^2\omega_{10}^2}$$

$$C_{D_y D_2^2 v_2}^{(3), \text{CuLBM}^2} = (-108\omega_3\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 + 24\omega_3\omega_4\omega_1^3\omega_2^2v_3^2 - 96\omega_3^2\omega_1^2\omega_2^2v_3^2 - 12\omega_3^2\omega_1^2c_s^2\omega_1^3v_2^2\omega_2 + 264\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 + 72\omega_3^2\omega_4c_s^4\omega_1\omega_2^3 + 38\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^4 - 216\omega_3\omega_4\omega_1^2\omega_2^2v_3^2 + 2\omega_3^2\omega_4\omega_1^3\omega_2^2 - 16\omega_3\omega_4c_s^2\omega_1^3\omega_2 + 48\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 + 72\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 36\omega_3\omega_4c_s^2\omega_1^2\omega_2^2 - 2\omega_3^2\omega_4c_s^4\omega_1^3\omega_2^2 + 18\omega_3\omega_4c_s^4\omega_1^3\omega_2^2 + 192\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^4 - 12\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 + 72\omega_3\omega_4c_s^2\omega_1\omega_2^3v_3^2 - 72\omega_3\omega_4c_s^2\omega_1^2\omega_2^2 - 24\omega_3\omega_4\omega_1^3\omega_2^2v_3^4 + 117\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 - 144\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 24\omega_3^2\omega_4\omega_1^3v_3^2 - 12\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 + 8\omega_3^2\omega_4c_s^2\omega_1^3v_3^2 - 8\omega_3^2\omega_4\omega_1^2\omega_2 - 6\omega_3^2\omega_4c_s^4\omega_1^3\omega_2^2 - 40\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 + 54\omega_3^2\omega_4\omega_1^3v_3^4 - 108\omega_3\omega_4\omega_1^3\omega_2^2v_3^2 - 288\omega_3^2\omega_4\omega_1\omega_2^3v_3^4 - 56\omega_3^2\omega_4c_s^4\omega_1^2\omega_2 - 36\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^4 + 336\omega_3^2\omega_4c_s^2\omega_1\omega_2^2v_3^2 + 144\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 + 204\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 + 24\omega_3^2\omega_4\omega_1^2\omega_2^2 + 288\omega_3\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 54\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^4 + 108\omega_3\omega_4\omega_1^2\omega_2^3v_3^4 + 36\omega_3^2\omega_4c_s^2\omega_1^2\omega_2 + 8\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 36\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 - 36\omega_3\omega_4c_s^4\omega_1^3\omega_2^2 - 297\omega_3\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 - 288\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 40\omega_3^2\omega_4c_s^2\omega_1^3 + 24\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 180\omega_3\omega_4\omega_1^2\omega_2^2v_3^4 + 72\omega_4\omega_1^2\omega_2^2v_3^2 + 264\omega_3^2\omega_4c_s^2\omega_1^3v_3^2 - 72\omega_3^2\omega_4c_s^2\omega_1\omega_2^2v_3^2 - 96\omega_3\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 - 216\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 - 36\omega_3\omega_4c_s^4\omega_1^3\omega_2^2 + 16\omega_3\omega_4c_s^4\omega_1^3\omega_2 - 36\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 - 8\omega_3^2\omega_4\omega_1^2\omega_2^2 + 60\omega_3\omega_4\omega_1^2\omega_2^2v_3^2 + 20\omega_3^2\omega_4c_s^4\omega_1^2\omega_2^2 + 108\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 - 18\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 + 168\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 96\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^4 + 324\omega_3\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 24\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^4 + 24\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2 + 240\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 + 48\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 + 64\omega_3^2\omega_4c_s^2\omega_1^2\omega_2 + 108\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 - 324\omega_3^2c_s^2\omega_1^2\omega_2^2v_3^2 + 40\omega_3\omega_4c_s^4\omega_1^2\omega_2^2 - 297\omega_3\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 6\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 117\omega_3\omega_4\omega_1^3\omega_2^2v_3^4 + 72\omega_3^2\omega_4\omega_1\omega_2^3v_3^2 + 288\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 12\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 - 852\omega_3^2\omega_4c_s^2\omega_1\omega_2^3v_3^2 + 36\omega_3\omega_4c_s^2\omega_1^3\omega_2^2 + 86\omega_3^2\omega_4c_s^4\omega_1^2\omega_2 - 8\omega_3^2\omega_4\omega_1^3\omega_2 - 2\omega_3^2\omega_4\omega_1^2\omega_2 - 28\omega_3^2\omega_4c_s^4\omega_1^3\omega_2 + 36\omega_3\omega_4\omega_1^3\omega_2^2v_3^2 + 96\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^4 - 36\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 - 16\omega_3^2\omega_4\omega_2^3 + 432\omega_3^2\omega_4c_s^2\omega_2^3v_3^2 + 576\omega_3^2\omega_4\omega_1^2\omega_2^3v_3^2 - 60\omega_3\omega_4\omega_1^2\omega_2^3v_3^4 + 80\omega_3^2\omega_4c_s^4\omega_2^3 + 24\omega_3^2\omega_4\omega_1^3\omega_2^2\omega_2 - 108\omega_3^2\omega_4\omega_2^3v_3^4 - 108\omega_3\omega_4c_s^2\omega_2^3\omega_2^2v_3^2 - 144\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 + 72\omega_3\omega_4c_s^2\omega_2^3\omega_2^2v_3^2 + 648\omega_3^2\omega_4c_s^2\omega_2^3\omega_2^2v_3^2 - 48\omega_3^2\omega_4\omega_1^3\omega_2^2\omega_2^2 - 24\omega_3^2\omega_4\omega_1^3\omega_2^2v_3^2 + 180\omega_3\omega_4\omega_1^2\omega_2^3v_3^2 - 72\omega_3^2\omega_4\omega_1^3\omega_2^3v_3^4 + 48\omega_3^2\omega_4\omega_2^3\omega_2^2v_3^2 + 16\omega_3^2\omega_4\omega_1\omega_2^3 + 36\omega_3\omega_4\omega_1^2\omega_2^3v_3^4 - 172\omega_3^2\omega_4c_s^4\omega_1\omega_2^3 - 48\omega_3^2\omega_4\omega_1^2\omega_2^3 - 288\omega_3^2\omega_4\omega_1^2\omega_2^3v_3^2 + 48\omega_3\omega_4c_s^2\omega_1^3\omega_2^2\omega_2^2 - 108\omega_4c_s^2\omega_1^3\omega_2^2v_3^2 + 72\omega_3^2\omega_4c_s^2\omega_1^3\omega_2^3 + 144\omega_3^2\omega_4\omega_1^2\omega_2^2v_3^2 - 36\omega_3\omega_4\omega_1^2\omega_2^3v_3^4 - 144\omega_3^2\omega_4\omega_1\omega_2^2\omega_2^3 + 16\omega_3\omega_4c_s^4\omega_1\omega_2^3 + 36\omega_4\omega_1^2\omega_2^2v_3^2 - 492\omega_3^2\omega_4c_s^2\omega_1^2\omega_2^2v_3^2 - 144\omega_3^2\omega_4\omega_1^2\omega_2^3 +$$

$$16\omega_3^2\omega_4^2c_s^4\omega_1\omega_2^2 - 96\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2 + 16\omega_3^2\omega_4^2\omega_1\omega_2^2 + 174\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 + 18\omega_3^2\omega_4^2c_s^4\omega_1^3\omega_2^3 + 117\omega_3^2\omega_4^2\omega_1^3\omega_2^3v_3^2 - 72\omega_3^2\omega_4^2\omega_1\omega_2^3v_3^4 - 48\omega_3^2\omega_4^2\omega_1^3\omega_2^3v_3^2 + 24\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1\omega_2^3v_3^2 - 117\omega_3^2\omega_4^2\omega_1^3\omega_2^3v_3^4 - 288\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2v_3^2 + 162\omega_3^2c_s^2\omega_1^3\omega_2^3v_3^2 - 108\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2v_3^2 - 24\omega_3^2\omega_4^2\omega_1^3\omega_2v_3^4 + 48\omega_3^2\omega_4^2\omega_1^3v_3^4 - 72\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2v_3^2 + 24\omega_3^2\omega_4^2c_s^2v_2^2\omega_2^2 - 86\omega_3^2\omega_4^2\omega_1^3\omega_2^2v_3^2 + 216\omega_3^2\omega_4^2\omega_1^2\omega_2^3v_3^4 + 144\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2v_3^2 + 48\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^2 + 468\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2v_3^2 - 492\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2v_3^2 - 72\omega_3^2\omega_4^2c_s^4\omega_1^2\omega_2^2 + 8\omega_3^2\omega_4^2\omega_1^3 - 108\omega_3^2\omega_4^2\omega_1^3\omega_2v_3^4 - 54\omega_3^2\omega_4^2\omega_1^3\omega_2^2v_3^2 + 32\omega_3^2\omega_4^2c_s^4\omega_1^3 - 108\omega_3^2\omega_4^2\omega_1^3\omega_2^2v_3^2 - 16\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^2 + 40\omega_3^2\omega_4^2\omega_1^2\omega_2^2v_3^4 + 12\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^2v_3^2 - 540\omega_3^2\omega_4^2c_s^2\omega_1^2\omega_2^3v_3^2 - 432\omega_3^2\omega_1^2\omega_2^3v_3^2 - 54\omega_4^2\omega_1^3\omega_2^3v_3^2 + 108\omega_3^2\omega_4^2\omega_1^3\omega_2^3v_3^4 - 6\omega_3^2\omega_4^2\omega_1^3\omega_2^2v_3^2 + 96\omega_3^2\omega_4^2\omega_1\omega_2^2v_3^2 - 32\omega_3^2\omega_4^2c_s^2\omega_1\omega_2^2 + 36\omega_3^2\omega_4^2\omega_1^2\omega_2^2v_3^2 - 18\omega_3^2\omega_4^2c_s^2\omega_1^3\omega_2^2 + 144\omega_3^2\omega_4^2\omega_1^3v_2^2v_3^2 + 162\omega_4^2c_s^2\omega_1^3\omega_2^2v_3^2) \frac{\rho}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3}$$

coefficient $C_{D_y D_z^3 v_3}^{(3)}$ **at** $\frac{\partial^4 v_3}{\partial x_2 \partial x_3^3}$:

$$C_{D_y D_z^3 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z^3 v_3}^{(3), \text{MRT1}} = (-25\omega_{19}\omega_7^2c_s^2\omega_{11}^3 + 32\omega_{19}^2\omega_7c_s^2\omega_{11} - 120\omega_{19}\omega_7^2\omega_{11}v_3^2 - 20\omega_{19}c_s^2\omega_{11}^3 - 17\omega_{19}^2\omega_7^2\omega_{11}^2 - 28\omega_{19}\omega_7\omega_{11}^3 - 28\omega_{19}\omega_{11}^3v_3^2 - 16\omega_7^2\omega_{11}^2v_3^2 + 56\omega_{19}\omega_7^2c_s^2\omega_{11}^2 - 43\omega_{19}\omega_7^2\omega_{11}^3v_3^2 + 16\omega_{19}\omega_7\omega_{11}^2 - 68\omega_{19}^2\omega_7\omega_{11}^2v_3^2 - 12\omega_{19}^2\omega_{11}^2 + 8\omega_7\omega_{11}^3 + 16\omega_7^2c_s^2\omega_{11}^3 - 32\omega_{19}\omega_7^2c_s^2\omega_{11} + 104\omega_{19}\omega_7^2\omega_{11}^2v_3^2 + 48\omega_{19}^2\omega_7\omega_{11} - 16\omega_7^2c_s^2\omega_{11}^2 + 16\omega_7^2\omega_{11}^3v_3^2 - 44\omega_{19}\omega_7c_s^2\omega_{11} - 24\omega_{19}^2\omega_7\omega_{11} - 64\omega_{19}\omega_7^2\omega_{11}v_3^2 - 16\omega_7^2c_s^2\omega_{11}^3 + 80\omega_{19}^2\omega_7^2v_3^2 - 48\omega_{19}\omega_7\omega_{11}^2v_3^2 + 24\omega_{19}\omega_7^2\omega_{11} - 32\omega_{19}^2\omega_7^2 + 25\omega_{19}^2\omega_7^2c_s^2\omega_{11}^2 - 16\omega_7\omega_{11}^3v_3^2 + 28\omega_{19}^2\omega_{11}^2v_3^2 - 72\omega_{19}^2\omega_7^2c_s^2\omega_{11} + 44\omega_{19}\omega_7c_s^2\omega_{11}^3 - 40\omega_{19}\omega_7^2\omega_{11}^2 - 8\omega_7^2\omega_{11}^3 + 64\omega_{19}^2\omega_7\omega_{11}^2v_3^2 - 16\omega_{19}\omega_7c_s^2\omega_{11}^2 + 48\omega_{19}^2\omega_7^2c_s^2 + 43\omega_{19}\omega_7^2\omega_{11}^2v_3^2 + 8\omega_7^2\omega_{11}^2 + 12\omega_{19}\omega_{11}^3 + 17\omega_{19}\omega_7^2\omega_{11}^3 + 20\omega_{19}^2c_s^2\omega_{11}^2 + 68\omega_{19}\omega_7\omega_{11}^3v_3^2 + 28\omega_{19}^2\omega_7\omega_{11}^2) \frac{\rho v_2 v_3}{4\omega_{19}^2\omega_7^2\omega_{11}^3}$$

$$C_{D_y D_z^3 v_3}^{(3), \text{MRT2}} = C_{D_y D_z^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^3 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^3 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^3 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^3 v_3}^{(3), \text{CuLBM2}} = (-66\omega_3\omega_1\omega_2^3v_3^2 - 54\omega_3c_s^2\omega_1\omega_2^2 + 5\omega_3\omega_1^3v_2^2\omega_2^2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^3 - 6\omega_1^2v_2^2\omega_2^2 + 27c_s^2\omega_1^3\omega_2^2 - 51\omega_3\omega_1^2\omega_2^2 + 27\omega_3c_s^2\omega_1\omega_2^3 - 12\omega_1\omega_2^3 + 84\omega_3c_s^2\omega_1^3 - 9\omega_1^2v_2^2\omega_2^3 - 18c_s^2\omega_1^2\omega_2^2 + 27\omega_3\omega_1v_2^2\omega_2^3 + 6\omega_3\omega_1^2\omega_2 - 12\omega_3c_s^2\omega_2^3 - 120\omega_3\omega_1\omega_2^2v_3^2 + 12\omega_3\omega_1^3v_2^2 - 18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^3 - 12\omega_3\omega_2^2\omega_2v_3^2 - 5\omega_3\omega_1^3\omega_2^2 - 18\omega_3\omega_1^3v_2^2\omega_2 + 48\omega_3\omega_1^3v_3^2 + 6\omega_3\omega_1v_2^2\omega_2^2 + 36c_s^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 + 132\omega_3\omega_1^2\omega_2^2v_3^2 - 5\omega_3\omega_1^2v_2^2\omega_2^3 - 9\omega_1^3\omega_2^2 + 9\omega_1^3v_2^2\omega_2^2 - 9\omega_3\omega_1^2v_2^2\omega_2^2 + 84\omega_3\omega_2^3v_3^2 + 15\omega_3c_s^2\omega_1^3\omega_2^2 - 12\omega_3\omega_2^3 + 6\omega_3\omega_1^2v_2^2\omega_2 - 66\omega_3\omega_1^3\omega_2v_3^2 - 15\omega_3c_s^2\omega_1^2\omega_2^2 + 42\omega_3\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 + 6\omega_1^3\omega_2 + 9\omega_1^2\omega_2^3 - 6\omega_1^3v_2^2\omega_2 - 36\omega_3\omega_1^3 + 3\omega_3\omega_1\omega_2^2 + 81\omega_3c_s^2\omega_1^2\omega_2^2 - 24\omega_3v_2^2\omega_2^2 + 12\omega_1v_2^2\omega_2^2 + 6\omega_1^2\omega_2^2) \frac{\rho v_2 v_3}{18\omega_3\omega_1^3\omega_2^3}$$

coefficient $C_{D_z^4 \rho}^{(3)}$ **at** $\frac{\partial^4 \rho}{\partial x_3^4}$:

$$C_{D_z^4 \rho}^{(3), \text{SRT}} = (12 + 404c_s^2\omega^2v_3^2 + 198c_s^2\omega - \omega^3 + 144v_3^4 + 8\omega^2 - 9\omega^3v_3^4 + 6c_s^2\omega^3 - 34c_s^2\omega^3v_3^2 + 234\omega v_3^2 + 90\omega^2v_3^4 - 78c_s^2\omega^2 + 144c_s^4 - 216\omega v_3^4 - 18\omega + 672c_s^2v_3^2 - 98\omega^2v_3^2 - 216c_s^4\omega - 132c_s^2\omega^2 + 82c_s^4\omega^2 + 10\omega^3v_3^2 - 5c_s^4\omega^3 - 1008c_s^2\omega v_3^2 - 156v_3^2) \frac{v_3}{12\omega^3}$$

$$C_{D_z^4 \rho}^{(3), \text{MRT1}} = (12 + 10\omega_{11}^3v_3^2 - 1008c_s^2\omega_{11}v_3^2 - 78c_s^2\omega_{11}^2 + 144v_3^4 + 6c_s^2\omega_{11}^3 + 8\omega_{11}^2 - 98\omega_{11}^2v_3^2 - 216\omega_{11}v_3^4 + 198c_s^2\omega_{11} - \omega_{11}^3 + 144c_s^4 + 90\omega_{11}^2v_3^4 - 18\omega_{11} - 5c_s^4\omega_{11}^3 + 672c_s^2v_3^2 - 34c_s^2\omega_{11}^3v_3^2 + 234\omega_{11}v_3^2 + 82c_s^4\omega_{11}^2 - 132c_s^2 - 216c_s^4\omega_{11} - 9\omega_{11}^3v_3^4 + 404c_s^2\omega_{11}^2v_3^2 - 156v_3^2) \frac{v_3}{12\omega_{11}^3}$$

$$C_{D_z^4 \rho}^{(3), \text{MRT2}} = C_{D_z^4 \rho}^{(3), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(3), \text{CLBM1}} = C_{D_z^4 \rho}^{(3), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(3), \text{CLBM2}} = C_{D_z^4 \rho}^{(3), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(3), \text{CuLBM1}} = (12 - 98\omega_6^2v_3^2 - 18\omega_6 + 6\omega_6^3c_s^2 + 144v_3^4 - 216\omega_6v_3^4 - \omega_6^3 - 78\omega_6^2c_s^2 + 404\omega_6^2c_s^2v_3^2 + 10\omega_6^3v_3^2 + 8\omega_6^2 + 144c_s^4 - 216\omega_6c_s^4 - 1008\omega_6c_s^2v_3^2 - 9\omega_6^3v_3^4 + 82\omega_6^2c_s^4 + 198\omega_6c_s^2 + 672c_s^2v_3^2 - 132c_s^2 - 5\omega_6^3c_s^4 + 90\omega_6^2v_3^4 + 234\omega_6v_3^2 - 156v_3^2 - 34\omega_6^3c_s^2v_3^2) \frac{v_3}{12\omega_6^3}$$

$$C_{D_z^4 \rho}^{(3), \text{CuLBM2}} = (328\omega_3\omega_1\omega_2^3v_3^2 - 80\omega_3c_s^2\omega_1\omega_2^2 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 48c_s^4\omega_1^2\omega_2^2 - 1088\omega_3c_s^2\omega_1^2\omega_2^2v_3^2 + 8c_s^2\omega_1^3\omega_2v_3^2 - 84\omega_3\omega_1^3\omega_2v_3^4 + 180\omega_3\omega_1^2\omega_2^3v_3^4 - 98\omega_3\omega_1^3\omega_2^2v_3^2 - 16\omega_3\omega_1^2\omega_2^2 + 320\omega_3c_s^2\omega_1\omega_2^3 + 24c_s^4\omega_1^3\omega_2 - 52\omega_3c_s^2\omega_1^3 + 16c_s^2\omega_1^2\omega_2^2 + 72\omega_3c_s^4\omega_1\omega_2^2 - 16c_s^2\omega_1^2\omega_2^2v_3^2 - 264\omega_3\omega_1^2\omega_2^3v_3^4 + 808\omega_3c_s^2\omega_1^2\omega_2^2v_3^2 + 8\omega_3\omega_1^2\omega_2 - 184\omega_3c_s^2\omega_2^3 - 176\omega_3\omega_1\omega_2^2v_3^2 - 3\omega_3\omega_1^3\omega_2^2 - 464\omega_3c_s^2\omega_1^3\omega_2v_3^2 - 372\omega_3c_s^4\omega_1\omega_2^3 - 8c_s^2\omega_1^3\omega_2 + 144\omega_3\omega_1^3v_3^2 - 104\omega_3\omega_1^2\omega_2v_3^2 + 8\omega_3\omega_1^3\omega_2^2 + 760\omega_3c_s^2\omega_2^3v_3^2 - 28\omega_3\omega_1^3v_3^2 + 30\omega_3\omega_1^3\omega_2^2v_3^2 - 8c_s^2\omega_1\omega_2^2 - 156\omega_3c_s^4\omega_1^3\omega_2 + 168\omega_3\omega_1\omega_2^2v_3^4 + 164\omega_3c_s^4\omega_1^2\omega_2^3 + 18\omega_3c_s^2\omega_1^2\omega_2^3 - 80\omega_3c_s^2\omega_1^2\omega_2 + 280\omega_3\omega_1^2\omega_2^2v_3^2 + 72\omega_3c_s^4\omega_1^3 - 1472\omega_3c_s^2\omega_1\omega_2^3v_3^2 + 96\omega_3\omega_1^2\omega_2v_3^4 - 120\omega_3c_s^4\omega_1\omega_2^2 + 24\omega_3\omega_1^3v_3^4 - 27\omega_3\omega_1^3\omega_2^3v_3^4 + 160\omega_3c_s^2\omega_1^3v_3^2 - 160\omega_3\omega_2^3v_3^2 + 404\omega_3c_s^2\omega_1^3\omega_2^2v_3^2 - 78\omega_3c_s^2\omega_1^3\omega_2^2 + 16\omega_3\omega_2^3 + 656\omega_3c_s^2\omega_1\omega_2^2v_3^2 + 94\omega_3\omega_1\omega_2v_3^2 - 156\omega_3c_s^2\omega_1^2\omega_2^2 + 8\omega_3\omega_1\omega_2^2 + 24c_s^4\omega_1\omega_2^2 - 196\omega_3\omega_1^2\omega_2^2v_3^2 + 122\omega_3c_s^2\omega_1^3\omega_2 - 300\omega_3\omega_1\omega_2^3v_3^4 + 8c_s^2\omega_1\omega_2^2v_3^2 + 72\omega_3c_s^4\omega_1\omega_2 - 15\omega_3c_s^4\omega_1^3\omega_2^2 + 4\omega_3\omega_1^3 - 102\omega_3c_s^2\omega_1^2\omega_2^2v_3^2 - 28\omega_3\omega_1\omega_2^2 + 152\omega_3c_s^2\omega_1^2\omega_2^2 + 440\omega_3c_s^2\omega_1^2\omega_2v_3^2 + 90\omega_3\omega_1^2\omega_2^2v_3^2 + 216\omega_3c_s^4\omega_2^2 + 82\omega_3c_s^4\omega_1^2\omega_2^2) \frac{v_3}{36\omega_3\omega_1^3\omega_2^3}$$

coefficient $C_{D_z^4 v_3}^{(3)}$ at $\frac{\partial^4 v_3}{\partial x_1^4}$:

$$C_{D_z^4 v_3}^{(3), \text{SRT}} = (12 + 252c_s^2\omega^2v_3^2 + 54c_s^2\omega - \omega^3 + 504v_3^4 + 8\omega^2 - 29\omega^3v_3^4 + 2c_s^2\omega^3 - 18c_s^2\omega^3v_3^2 + 378\omega v_3^2 + 310\omega^2v_3^4 - 22c_s^2\omega^2 + 24c_s^4 - 756\omega v_3^4 - 18\omega + 432c_s^2v_3^2 - 154\omega^2v_3^2 - 36c_s^4\omega - 36c_s^2 + 14c_s^4\omega^2 + 14\omega^3v_3^2 - c_s^4\omega^3 - 648c_s^2\omega v_3^2 - 252v_3^2) \frac{\rho}{12\omega^3}$$

$$C_{D_z^4 v_3}^{(3), \text{MRT1}} = (12 + 14\omega_{11}^3v_3^2 - 648c_s^2\omega_{11}v_3^2 - 22c_s^2\omega_{11}^2 + 504v_3^4 + 2c_s^2\omega_{11}^3 + 8\omega_{11}^2 - 154\omega_{11}^2v_3^2 - 756\omega_{11}v_3^4 + 54c_s^2\omega_{11} - \omega_{11}^3 + 24c_s^4 + 310\omega_{11}^2v_3^4 - 18\omega_{11} - c_s^4\omega_{11}^3 + 432c_s^2v_3^2 - 18c_s^2\omega_{11}^3v_3^2 + 378\omega_{11}v_3^2 + 14c_s^4\omega_{11}^2 - 36c_s^2 - 36c_s^4\omega_{11} - 29\omega_{11}^3v_3^4 + 252c_s^2\omega_{11}^2v_3^2 - 252v_3^2) \frac{\rho}{12\omega_{11}^3}$$

$$C_{D_z^4 v_3}^{(3), \text{MRT2}} = C_{D_z^4 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(3), \text{CLBM1}} = C_{D_z^4 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(3), \text{CLBM2}} = C_{D_z^4 v_3}^{(3), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(3), \text{CuLBM1}} = (12 - 154\omega_6^2v_3^2 - 18\omega_6 + 2\omega_6^3c_s^2 + 504v_3^4 - 756\omega_6v_3^4 - \omega_6^3 - 22\omega_6^2c_s^2 + 252\omega_6^2c_s^2v_3^2 + 14\omega_6^3v_3^2 + 8\omega_6^2 + 24c_s^4 - 36\omega_6c_s^4 - 648\omega_6c_s^2v_3^2 - 29\omega_6^3v_3^4 + 14\omega_6^2c_s^4 + 54\omega_6c_s^2 + 432c_s^2v_3^2 - 36c_s^2 - \omega_6^3c_s^4 + 310\omega_6^2v_3^4 + 378\omega_6v_3^2 - 252v_3^2 - 18\omega_6^3c_s^2v_3^2) \frac{\rho}{12\omega_6^3}$$

$$C_{D_z^4 v_3}^{(3), \text{CuLBM2}} = (552\omega_3\omega_1\omega_2^3v_3^2 - 16\omega_3c_s^2\omega_1\omega_2^2 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 16c_s^4\omega_1^2\omega_2^2 - 576\omega_3c_s^2\omega_1^2\omega_2^2v_3^2 + 24c_s^2\omega_1^3\omega_2v_3^2 - 312\omega_3\omega_1^3\omega_2v_3^4 + 620\omega_3\omega_1^2\omega_2^3v_3^4 - 154\omega_3\omega_1^3\omega_2^2v_3^2 - 16\omega_3\omega_1^2\omega_2^2 + 96\omega_3c_s^2\omega_1\omega_2^3 + 8c_s^4\omega_1^3\omega_2 - 20\omega_3c_s^2\omega_1^3 + 16c_s^2\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_1\omega_2^2 - 48c_s^2\omega_1^2\omega_2^2v_3^2 - 888\omega_3\omega_1^2\omega_2^2v_3^4 + 504\omega_3c_s^2\omega_1^2\omega_2^3v_3^2 + 8\omega_3\omega_1^2\omega_2 - 56\omega_3c_s^2\omega_1^3 - 240\omega_3\omega_1\omega_2^2v_3^2 - 3\omega_3\omega_1^3\omega_2^3 - 360\omega_3c_s^2\omega_1^3\omega_2v_3^2 - 68\omega_3c_s^4\omega_1\omega_2^3 - 8c_s^2\omega_1^3\omega_2 + 528\omega_3\omega_2^3v_3^4 - 168\omega_3\omega_1^2\omega_2v_3^2 + 8\omega_3\omega_1^3\omega_2^2 + 552\omega_3c_s^2\omega_2^3v_3^2 - 60\omega_3\omega_1^3v_3^2 + 42\omega_3\omega_1^3\omega_2^3v_3^2 - 8c_s^2\omega_1\omega_2^3 - 32\omega_3c_s^4\omega_1^3\omega_2 + 552\omega_3\omega_1\omega_2^3v_3^4 + 28\omega_3c_s^4\omega_1^2\omega_2^3 + 6\omega_3c_s^2\omega_1^3\omega_2^3 - 16\omega_3c_s^2\omega_1^2\omega_2 + 408\omega_3\omega_1^2\omega_2^2v_3^2 + 16\omega_3c_s^4\omega_1^3 - 1008\omega_3c_s^2\omega_1\omega_2^3v_3^2 + 336\omega_3\omega_1^2\omega_2v_3^4 - 8\omega_3c_s^4\omega_1^2\omega_2^2 + 96\omega_3\omega_1^3v_3^4 - 87\omega_3\omega_1^3\omega_2^3v_3^4 + 144\omega_3c_s^2\omega_1^3v_3^2 - 288\omega_3\omega_2^3v_3^2 + 252\omega_3c_s^2\omega_1^3\omega_2^3v_3^2 - 22\omega_3c_s^2\omega_1^3\omega_2^2 + 16\omega_3\omega_2^3 + 336\omega_3c_s^2\omega_1\omega_2^3v_3^2 + 174\omega_3\omega_1^3\omega_2v_3^2 - 44\omega_3c_s^2\omega_1^2\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 8c_s^4\omega_1\omega_2^3 - 308\omega_3\omega_1^2\omega_2^3v_3^2 + 42\omega_3c_s^2\omega_1^3\omega_2 - 1068\omega_3\omega_1\omega_2^3v_3^4 + 24c_s^2\omega_1\omega_2^3v_3^2 + 8\omega_3c_s^4\omega_1\omega_2 - 3\omega_3c_s^4\omega_1^3\omega_2^3 + 4\omega_3\omega_1^3 - 54\omega_3c_s^2\omega_1^3\omega_2^3v_3^2 - 28\omega_3\omega_1\omega_2^3 + 24\omega_3c_s^2\omega_1^2\omega_2^2 + 264\omega_3c_s^2\omega_1^2\omega_2v_3^2 + 310\omega_3\omega_1^3\omega_2^3v_3^4 + 40\omega_3c_s^4\omega_2^3 + 14\omega_3c_s^4\omega_1^3\omega_2^2) \frac{\rho}{36\omega_3\omega_1^3\omega_2^3}$$

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