

D3Q7 ADE,

a supplementary material for

Lattice Boltzmann Method Analysis Tool (LBMAT)

Radek Fučík[†], Pavel Eichler[†], Jakub Klinkovský[†], Robert Straka^{‡,†}, and Tomáš Oberhuber[†]

[†]Faculty of Nuclear Sciences and Physical Engineering, Czech Technical University in Prague,
Trojanova 13, 120 00 Prague, Czech Republic

[‡]AGH University of Science and Technology, al. Mickiewicza 30, 30-059 Krakow, Poland

Contents

1	Global definitions	1
1.1	Discrete velocity vectors	2
1.2	Raw and central moments	2
1.3	Transformation matrix \mathbf{M}	2
1.4	Equilibrium	3
2	Spatial EPDEs	3
2.1	SRT	3
2.1.1	Definitions	3
2.1.2	Conservation of mass equation	3
2.2	MRT1	7
2.2.1	Definitions	7
2.2.2	Conservation of mass equation	7
2.3	MRT2	14
2.3.1	Definitions	14
2.3.2	Conservation of mass equation	15
2.4	CLBM1	21
2.4.1	Definitions	21
2.4.2	Conservation of mass equation	22
2.5	CLBM2	29
2.5.1	Definitions	29
2.5.2	Conservation of mass equation	30
3	Comparison of SRT, MRT, and CLBM	36
3.1	Conservation of mass equation	36

1 Global definitions

In \mathbb{R}^3 , the position and velocity vectors are given by $\mathbf{x} = (x_1, x_2, x_3)^T$ and $\mathbf{v} = (v_1, v_2, v_3)^T$, respectively.

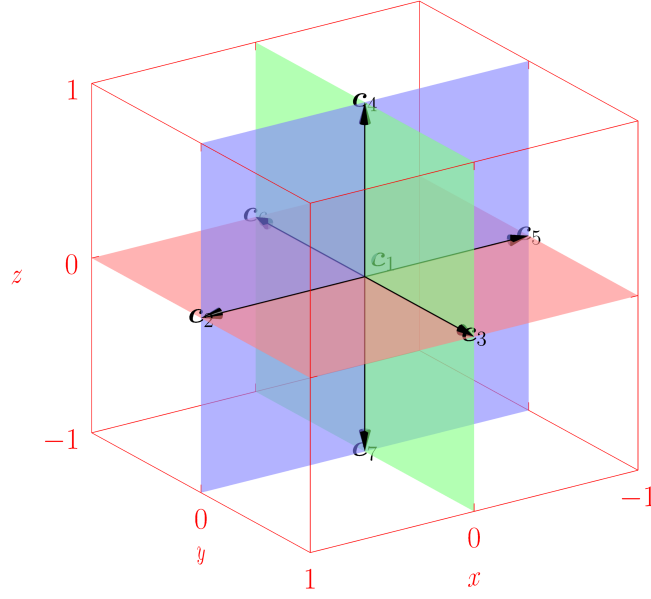
1.1 Discrete velocity vectors

Discrete velocity vectors and the lattice speed of sound are defined by

$$\{\mathbf{c}_i\}_{i=1}^7 = \left(\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix} \right),$$

$$c_s = \frac{1}{2},$$

respectively [1].



1.2 Raw and central moments

The raw and central moments are defined by

$$m_{\alpha} := \sum_{i=1}^7 f_i \mathbf{c}_i^{\alpha},$$

and

$$k_{\alpha} := \sum_{i=1}^7 f_i (\mathbf{c}_i - \mathbf{v})^{\alpha},$$

respectively, where $\alpha = (\alpha_1, \alpha_2, \alpha_3) \in \mathbb{Z}^3$ denotes a multi-index (as a row vector) and $\mathbf{c}_i^{\alpha} := \prod_{j=1}^3 [\mathbf{c}_i]_j^{\alpha_j}$.

1.3 Transformation matrix M

Matrix \mathbf{M} , that defines macroscopic quantities (moments) $\boldsymbol{\mu}$ by

$$\boldsymbol{\mu} = \mathbf{M} \mathbf{f},$$

with $\mathbf{f} = (f_1, f_2, \dots, f_7)^T$, is selected such that

$$\boldsymbol{\mu} = \left(m_{(0,0,0)}, m_{(1,0,0)}, m_{(0,1,0)}, m_{(0,0,1)}, m_{(2,0,0)}, m_{(0,2,0)}, m_{(0,0,2)} \right)^T,$$

i.e., \mathbf{M} is given by

$$\mathbf{M} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 \end{pmatrix}.$$

1.4 Equilibrium

The corresponding equilibrium raw moments are defined using the continuous Maxwell–Boltzmann distribution function [1]

$$f^{(eq)}(\boldsymbol{\xi}) = \frac{\rho}{(2\pi c_s^2)^{\frac{3}{2}}} \exp\left(-\frac{\|\boldsymbol{\xi} - \mathbf{v}\|^2}{2c_s^2}\right)$$

as

$$m_{\boldsymbol{\alpha}}^{(eq)} = \int_{\mathbb{R}^3} \boldsymbol{\xi}^{\boldsymbol{\alpha}} f^{(eq)}(\boldsymbol{\xi}) d\boldsymbol{\xi},$$

where $\alpha_i \in \{0, 1, 2\}$, $i = 1, 2, 3$. Hence, the equilibrium moments $\boldsymbol{\mu}^{(eq)}$ satisfy

$$\boldsymbol{\mu}^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho(v_1^2 + c_s^2) \\ \rho(v_2^2 + c_s^2) \\ \rho(v_3^2 + c_s^2) \end{pmatrix}.$$

2 Spatial EPDEs

2.1 SRT

2.1.1 Definitions

Collision operator \mathbf{C} :

$$\mathbf{C}(\mathbf{f}) = \omega \left(\mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)} - \mathbf{f} \right),$$

$\omega \in (0, 2)$.

2.1.2 Conservation of mass equation



attached text file: output_d3q7_ade_srt_symbolic_pde_00.txt

[illegible]

$$\begin{aligned}
& (24 + 180c_s^2\omega - 120c_s^2 - 36\omega + 6c_s^2\omega^3 - 72c_s^2\omega^2 + 14\omega^2 - \omega^3) \frac{\delta_t^4 v_1 v_2}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_4 \frac{\rho \delta_t^4 v_2}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_5 \frac{\rho \delta_t^4 v_1}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} \\
& + (-2 + 3\omega - \omega^2) \frac{3\delta_t \rho \delta_t^3 v_2}{2\omega^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + (-90c_s^2\omega - 2\omega^2 v_2^2 + 60c_s^2 - 2c_s^2\omega^3 + \omega^3 v_2^2 + 34c_s^2\omega^2) \frac{\rho \delta_t^3}{12\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (-24 + 36\omega - 14\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_1 v_2}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + C_6 \frac{\delta_t^4}{4\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^4 \partial x_2^2} + \\
& (72c_s^2\omega + 50\omega^2 v_2^2 - 48c_s^2 + c_s^2\omega^3 - 4\omega^3 v_2^2 - 26c_s^2\omega^2 + 84v_2^2 - 126\omega v_2^2) \frac{\rho \delta_t^4 v_1}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^4 \partial x_2^2} + \\
& (72c_s^2\omega + 50\omega^2 v_1^2 - 48c_s^2 - 4\omega^3 v_1^2 + c_s^2\omega^3 - 26c_s^2\omega^2 + 84v_1^2 - 126\omega v_1^2) \frac{\rho \delta_t^4 v_2}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1^4 \partial x_2^2} + C_7 \frac{\rho \delta_t^3}{12\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2^3} + \\
& (24 + 180c_s^2\omega - 120c_s^2 - 36\omega + 6c_s^2\omega^3 - 72c_s^2\omega^2 + 14\omega^2 - \omega^3) \frac{\delta_t^4 v_1 v_2}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_8 \frac{\rho \delta_t^4 v_2}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_9 \frac{\rho \delta_t^4 v_1}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} \\
& + C_{10} \frac{\delta_t^4}{24\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_2^4} + C_{11} \frac{\rho \delta_t^4 v_2}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 + 3\omega - \omega^2) \frac{\delta_t^4 \rho \delta_t}{2\omega^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + (36 - 54\omega + 20\omega^2 - \omega^3) \frac{\delta_t \rho \delta_t^2 v_3}{12\omega^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (36 - 54\omega + 20\omega^2 - \omega^3) \frac{\delta_t \rho \delta_t^2 v_1}{12\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + (-24 + 36\omega - 14\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_3 v_1}{6\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + \\
& (-90c_s^2\omega - 2\omega^2 v_1^2 + 60c_s^2 + \omega^3 v_1^2 - 2c_s^2\omega^3 + 34c_s^2\omega^2) \frac{\rho \delta_t^3}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + \\
& (24 + 180c_s^2\omega - 120c_s^2 - 36\omega + 6c_s^2\omega^3 - 72c_s^2\omega^2 + 14\omega^2 - \omega^3) \frac{\delta_t^4 v_3 v_1}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{12} \frac{\rho \delta_t^4 v_3}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& C_{13} \frac{\rho \delta_t^4 v_1}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + (36 - 54\omega + 20\omega^2 - \omega^3) \frac{\delta_t \rho \delta_t^2 v_3}{12\omega^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + (36 - 54\omega + 20\omega^2 - \omega^3) \frac{\delta_t \rho \delta_t^2 v_2}{12\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& (-20 + 30\omega - 12\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_3 v_2}{2\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + (-20 + 30\omega - 12\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_3 v_1}{2\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + \\
& (-20 + 30\omega - 12\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_1 v_2}{2\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + \\
& (30c_s^2\omega + 24\omega^2 v_1^2 - 20c_s^2 - 2\omega^3 v_1^2 + c_s^2\omega^3 - 12c_s^2\omega^2 + 40v_1^2 - 60\omega v_1^2) \frac{\delta_t^4 v_3 v_2}{\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (132 - 198\omega + 76\omega^2 - 5\omega^3) \frac{\rho \delta_t^4 v_3 v_1 v_2}{6\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (144c_s^2\omega + 52\omega^2 v_1^2 - 96c_s^2 - 5\omega^3 v_1^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 + 84v_1^2 - 126\omega v_1^2) \frac{\rho \delta_t^4 v_3}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (144c_s^2\omega + 52\omega^2 v_1^2 - 96c_s^2 - 5\omega^3 v_1^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 + 84v_1^2 - 126\omega v_1^2) \frac{\rho \delta_t^4 v_2}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-24 + 36\omega - 14\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_3 v_2}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + (-90c_s^2\omega - 2\omega^2 v_2^2 + 60c_s^2 - 2c_s^2\omega^3 + \omega^3 v_2^2 + 34c_s^2\omega^2) \frac{\rho \delta_t^3}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + \\
& (30c_s^2\omega + 24\omega^2 v_2^2 - 20c_s^2 + c_s^2\omega^3 - 2\omega^3 v_2^2 - 12c_s^2\omega^2 + 40v_2^2 - 60\omega v_2^2) \frac{\delta_t^4 v_3 v_1}{\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (144c_s^2\omega + 52\omega^2 v_2^2 - 96c_s^2 + 4c_s^2\omega^3 - 5\omega^3 v_2^2 - 56c_s^2\omega^2 + 84v_2^2 - 126\omega v_2^2) \frac{\rho \delta_t^4 v_3}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (132 - 198\omega + 76\omega^2 - 5\omega^3) \frac{\rho \delta_t^4 v_3 v_1 v_2}{6\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (144c_s^2\omega + 52\omega^2 v_2^2 - 96c_s^2 + 4c_s^2\omega^3 - 5\omega^3 v_2^2 - 56c_s^2\omega^2 + 84v_2^2 - 126\omega v_2^2) \frac{\rho \delta_t^4 v_1}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (24 + 180c_s^2\omega - 120c_s^2 - 36\omega + 6c_s^2\omega^3 - 72c_s^2\omega^2 + 14\omega^2 - \omega^3) \frac{\delta_t^4 v_3 v_2}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{14} \frac{\rho \delta_t^4 v_3}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + \\
& C_{15} \frac{\rho \delta_t^4 v_2}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 + 3\omega - \omega^2) \frac{3\delta_t \rho \delta_t^3 v_3}{2\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + \\
& (-90c_s^2\omega + \omega^3 v_3^2 + 60c_s^2 - 2\omega^2 v_3^2 - 2c_s^2\omega^3 + 34c_s^2\omega^2) \frac{\rho \delta_t^3}{12\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + (-24 + 36\omega - 14\omega^2 + \omega^3) \frac{\rho \delta_t^3 v_3 v_1}{6\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + \\
& C_{16} \frac{\delta_t^4}{4\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (72c_s^2\omega - 4\omega^3 v_3^2 - 48c_s^2 + 50\omega^2 v_3^2 + c_s^2\omega^3 - 26c_s^2\omega^2 - 126\omega v_3^2 + 84v_3^2) \frac{\rho \delta_t^4 v_1}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& (72c_s^2\omega + 50\omega^2 v_1^2 - 48c_s^2 - 4\omega^3 v_1^2 + c_s^2\omega^3 - 26c_s^2\omega^2 + 84v_1^2 - 126\omega v_1^2) \frac{\rho \delta_t$$

$$\begin{aligned}
& (72c_s^2\omega - 4\omega^3v_3^2 - 48c_s^2 + 50\omega^2v_3^2 + c_s^2\omega^3 - 26c_s^2\omega^2 - 126\omega v_3^2 + 84v_3^2) \frac{\rho\delta_t^4v_2}{12\delta_t\omega^3} \frac{\partial^4v_2}{\partial x_2^2\partial x_3^2} + \\
& (72c_s^2\omega + 50\omega^2v_2^2 - 48c_s^2 + c_s^2\omega^3 - 4\omega^3v_2^2 - 26c_s^2\omega^2 + 84v_2^2 - 126\omega v_2^2) \frac{\rho\delta_t^4v_3}{12\delta_t\omega^3} \frac{\partial^4v_3}{\partial x_2^2\partial x_3^2} + C_{18} \frac{\rho\delta_t^3}{12\omega^3} \frac{\partial^4v_3}{\partial t\partial x_3^3} + \\
& (24 + 180c_s^2\omega - 120c_s^2 - 36\omega + 6c_s^2\omega^3 - 72c_s^2\omega^2 + 14\omega^2 - \omega^3) \frac{\delta_t^4v_3v_1}{6\delta_t\omega^3} \frac{\partial^4\rho}{\partial x_1\partial x_3^3} + C_{19} \frac{\rho\delta_t^4v_3}{12\delta_t\omega^3} \frac{\partial^4v_1}{\partial x_1\partial x_3^3} + \\
& C_{20} \frac{\rho\delta_t^4v_1}{12\delta_t\omega^3} \frac{\partial^4v_3}{\partial x_1\partial x_3^3} + (24 + 180c_s^2\omega - 120c_s^2 - 36\omega + 6c_s^2\omega^3 - 72c_s^2\omega^2 + 14\omega^2 - \omega^3) \frac{\delta_t^4v_3v_2}{6\delta_t\omega^3} \frac{\partial^4\rho}{\partial x_2\partial x_3^3} + C_{21} \frac{\rho\delta_t^4v_3}{12\delta_t\omega^3} \frac{\partial^4v_2}{\partial x_2\partial x_3^3} \\
& + C_{22} \frac{\rho\delta_t^4v_2}{12\delta_t\omega^3} \frac{\partial^4v_3}{\partial x_2\partial x_3^3} + C_{23} \frac{\delta_t^4}{24\delta_t\omega^3} \frac{\partial^4\rho}{\partial x_3^4} + C_{24} \frac{\rho\delta_t^4v_3}{12\delta_t\omega^3} \frac{\partial^4v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -36 - 90c_s^2\omega + 42\omega^2v_1^2 + 60c_s^2 + 54\omega - 3\omega^3v_1^2 - 2c_s^2\omega^3 + 34c_s^2\omega^2 + 72v_1^2 - 20\omega^2 - 108\omega v_1^2 + \omega^3 \\
C_2 &= 36c_s^2\omega + 42\omega^2v_1^2 + 6c_s^2\omega^3v_1^2 + 108\omega v_1^4 - 144c_s^2v_1^2 - 24c_s^2 - 72v_1^4 - 3\omega^3v_1^2 + c_s^2\omega^3 - 84c_s^2\omega^2v_1^2 - 14c_s^2\omega^2 + 3\omega^3v_1^4 + 48c_s^4 + 72v_1^2 + \\
& 216c_s^2\omega v_1^2 - 72c_s^4\omega + 30c_s^4\omega^2 - 42\omega^2v_1^4 - 108\omega v_1^2 - 3c_s^4\omega^3 \\
C_3 &= 24 + 72c_s^2\omega - 22\omega^2v_1^2 - 48c_s^2 - 36\omega + 2\omega^3v_1^2 + c_s^2\omega^3 - 26c_s^2\omega^2 - 36v_1^2 + 14\omega^2 + 54\omega v_1^2 - \omega^3 \\
C_4 &= 12 + 144c_s^2\omega - 12\omega^2v_1^2 - 96c_s^2 - 18\omega + 3\omega^3v_1^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 - 12v_1^2 + 8\omega^2 + 18\omega v_1^2 - \omega^3 \\
C_5 &= 36 + 144c_s^2\omega - 20\omega^2v_1^2 - 96c_s^2 - 54\omega + \omega^3v_1^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 - 36v_1^2 + 20\omega^2 + 54\omega v_1^2 - \omega^3 \\
C_6 &= c_s^2\omega^3v_2^2 - 3\omega^3v_1^2v_2^2 - 24c_s^2v_2^2 + c_s^2\omega^3v_1^2 - 24c_s^2v_1^2 - 14c_s^2\omega^2v_2^2 - 84\omega v_1^2v_2^2 - 14c_s^2\omega^2v_1^2 + 16c_s^4 + 36c_s^2\omega v_1^2 + 34\omega^2v_1^2v_2^2 - 24c_s^4\omega + \\
& 36c_s^2\omega v_2^2 + 56v_1^2v_2^2 + 10c_s^4\omega^2 - c_s^4\omega^3 \\
C_7 &= -36 - 90c_s^2\omega + 42\omega^2v_2^2 + 60c_s^2 + 54\omega - 2c_s^2\omega^3 - 3\omega^3v_2^2 + 34c_s^2\omega^2 + 72v_2^2 - 108\omega v_2^2 - 20\omega^2 + \omega^3 \\
C_8 &= 36 + 144c_s^2\omega - 20\omega^2v_2^2 - 96c_s^2 - 54\omega + 4c_s^2\omega^3 + \omega^3v_2^2 - 56c_s^2\omega^2 - 36v_2^2 + 54\omega v_2^2 + 20\omega^2 - \omega^3 \\
C_9 &= 12 + 144c_s^2\omega - 12\omega^2v_2^2 - 96c_s^2 - 18\omega + 4c_s^2\omega^3 + 3\omega^3v_2^2 - 56c_s^2\omega^2 - 12v_2^2 + 18\omega v_2^2 + 8\omega^2 - \omega^3 \\
C_{10} &= 36c_s^2\omega + 6c_s^2\omega^3v_2^2 - 144c_s^2v_2^2 + 108\omega v_2^4 + 42\omega^2v_2^2 - 24c_s^2 - 84c_s^2\omega^2v_2^2 + c_s^2\omega^3 - 72v_2^4 - 3\omega^3v_2^2 - 14c_s^2\omega^2 + 48c_s^4 + 3\omega^3v_2^4 - 72c_s^4\omega + \\
& 216c_s^2\omega v_2^2 + 72v_2^2 - 108\omega v_2^2 + 30c_s^4\omega^2 - 3c_s^4\omega^3 - 42\omega^2v_2^4 \\
C_{11} &= 24 + 72c_s^2\omega - 22\omega^2v_2^2 - 48c_s^2 - 36\omega + c_s^2\omega^3 + 2\omega^3v_2^2 - 26c_s^2\omega^2 - 36v_2^2 + 54\omega v_2^2 + 14\omega^2 - \omega^3 \\
C_{12} &= 12 + 144c_s^2\omega - 12\omega^2v_1^2 - 96c_s^2 - 18\omega + 3\omega^3v_1^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 - 12v_1^2 + 8\omega^2 + 18\omega v_1^2 - \omega^3 \\
C_{13} &= 36 + 144c_s^2\omega - 20\omega^2v_1^2 - 96c_s^2 - 54\omega + \omega^3v_1^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 - 36v_1^2 + 20\omega^2 + 54\omega v_1^2 - \omega^3 \\
C_{14} &= 12 + 144c_s^2\omega - 12\omega^2v_2^2 - 96c_s^2 - 18\omega + 4c_s^2\omega^3 + 3\omega^3v_2^2 - 56c_s^2\omega^2 - 12v_2^2 + 18\omega v_2^2 + 8\omega^2 - \omega^3 \\
C_{15} &= 36 + 144c_s^2\omega - 20\omega^2v_2^2 - 96c_s^2 - 54\omega + 4c_s^2\omega^3 + \omega^3v_2^2 - 56c_s^2\omega^2 - 36v_2^2 + 54\omega v_2^2 + 20\omega^2 - \omega^3 \\
C_{16} &= c_s^2\omega^3v_1^2 - 14c_s^2\omega^2v_3^2 + 56v_3^2v_1^2 + 34\omega^2v_3^2v_1^2 - 24c_s^2v_1^2 - 24c_s^2v_3^2 + c_s^2\omega^3v_3^2 - 14c_s^2\omega^2v_1^2 - 3\omega^3v_3^2v_1^2 + 16c_s^4 + 36c_s^2\omega v_1^2 - 24c_s^4\omega + \\
& 36c_s^2\omega v_3^2 + 10c_s^4\omega^2 - 84\omega v_3^2v_1^2 - c_s^4\omega^3 \\
C_{17} &= 56v_3^2v_2^2 + c_s^2\omega^3v_2^2 + 34\omega^2v_3^2v_2^2 - 24c_s^2v_2^2 - 14c_s^2\omega^2v_3^2 - 14c_s^2\omega^2v_2^2 - 24c_s^2v_3^2 + c_s^2\omega^3v_3^2 + 16c_s^4 - 24c_s^4\omega - 3\omega^3v_3^2v_2^2 + 36c_s^2\omega v_2^2 + \\
& 36c_s^2\omega v_3^2 + 10c_s^4\omega^2 - 84\omega v_3^2v_2^2 - c_s^4\omega^3 \\
C_{18} &= -36 - 90c_s^2\omega - 3\omega^3v_3^2 + 60c_s^2 + 54\omega + 42\omega^2v_3^2 - 2c_s^2\omega^3 + 34c_s^2\omega^2 - 108\omega v_3^2 + 72v_3^2 - 20\omega^2 + \omega^3 \\
C_{19} &= 36 + 144c_s^2\omega + \omega^3v_3^2 - 96c_s^2 - 54\omega - 20\omega^2v_3^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 + 54\omega v_3^2 - 36v_3^2 + 20\omega^2 - \omega^3 \\
C_{20} &= 12 + 144c_s^2\omega + 3\omega^3v_3^2 - 96c_s^2 - 18\omega - 12\omega^2v_3^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 + 18\omega v_3^2 - 12v_3^2 + 8\omega^2 - \omega^3 \\
C_{21} &= 36 + 144c_s^2\omega + \omega^3v_3^2 - 96c_s^2 - 54\omega - 20\omega^2v_3^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 + 54\omega v_3^2 - 36v_3^2 + 20\omega^2 - \omega^3 \\
C_{22} &= 12 + 144c_s^2\omega + 3\omega^3v_3^2 - 96c_s^2 - 18\omega - 12\omega^2v_3^2 + 4c_s^2\omega^3 - 56c_s^2\omega^2 + 18\omega v_3^2 - 12v_3^2 + 8\omega^2 - \omega^3 \\
C_{23} &= 36c_s^2\omega - 3\omega^3v_3^2 - 72v_3^4 - 84c_s^2\omega^2v_3^2 - 24c_s^2 + 42\omega^2v_3^2 + c_s^2\omega^3 + 108\omega v_3^4 - 144c_s^2v_3^2 + 6c_s^2\omega^3v_3^2 - 14c_s^2\omega^2 - 42\omega^2v_3^4 + 48c_s^4 - 72c_s^4\omega - \\
& 108\omega v_3^2 + 72v_3^2 + 216c_s^2\omega v_3^2 + 30c_s^4\omega^2 + 3\omega^3v_3^4 - 3c_s^4\omega^3 \\
C_{24} &= 24 + 72c_s^2\omega + 2\omega^3v_3^2 - 48c_s^2 - 36\omega - 22\omega^2v_3^2 + c_s^2\omega^3 - 26c_s^2\omega^2 + 54\omega v_3^2 - 36v_3^2 + 14\omega^2 - \omega^3
\end{aligned}$$

2.2 MRT1

2.2.1 Definitions

Collision operator \mathcal{C} :

$$\mathcal{C}(f) = \mathbf{M}^{-1} \mathbf{S} \left(\mu^{(eq)} - \mathbf{M} f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2).$$

2.2.2 Conservation of mass equation



attached text file: output_d3q7_ade_mrt1_symbolic_pde_00.txt

$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\ & (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\delta_t \omega_2} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_1 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\ & (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{\rho \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\ & (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{\rho \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_2 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} \\ & + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho \delta_l^2}{2\omega_3 \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (\omega_3 + \omega_4 - \omega_3 \omega_4) \frac{v_2 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\ & (\omega_3 + \omega_4 - \omega_3 \omega_4) \frac{\rho \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_3 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} \\ & + (\omega_3 + \omega_4 - \omega_3 \omega_4) \frac{v_3 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\rho \delta_l^2}{2\delta_t \omega_4} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + \\ & (-2 + \omega_2) \frac{\rho \delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho \delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + \\ & (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_2 v_1 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\ & (-2 + \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho \delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_3 v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\ & (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (\omega_3 + \omega_4 - \omega_3 \omega_4) \frac{v_3 v_2 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + \\ & (-2 + \omega_4) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_3}{\partial x_3^2} + (12 - 12\omega_2 + \omega_2^2) \frac{\delta_t \rho \delta_l}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_5 \omega_2 - 6\omega_5 - 6\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_5 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} \\ & + C_1 \frac{v_1 \delta_l^3}{6\delta_t \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^3} + (12 - 12\omega_3 + \omega_3^2) \frac{\delta_t \rho \delta_l}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + \\ & (-6\omega_3 - 2\omega_3^2 \omega_2 + 9\omega_3 \omega_2 - 6\omega_2 + 3\omega_3^2) \frac{v_2 \rho \delta_l^2}{6\omega_3^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + (-6\omega_3 + 9\omega_3 \omega_2 - 6\omega_2 + 3\omega_2^2 - 2\omega_3 \omega_2^2) \frac{v_1 \rho \delta_l^2}{6\omega_3 \omega_2^2} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + \\ & C_3 \frac{v_2 \delta_l^3}{2\omega_3^2 \delta_t \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (\omega_3^2 \omega_2^2 - 6\omega_3^2 \omega_2 + 6\omega_2^2 + 6\omega_3^3 - 6\omega_3 \omega_2^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\ & (6v_1^2 \omega_2^2 + 6c_s^2 \omega_2^2 - 6v_1^2 \omega_5 \omega_2 + 18c_s^2 \omega_5 \omega_2 - 3c_s^2 \omega_5 \omega_2^2 + v_1^2 \omega_5 \omega_2^2 - 12v_1^2 \omega_2 - 12c_s^2 \omega_2 - 12c_s^2 \omega_5 + 12v_1^2 \omega_5) \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} \\ & + (12 - 6\omega_3 + \omega_3 \omega_6 - 6\omega_6) \frac{v_2 \rho \delta_l^2}{6\omega_3 \omega_6} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\omega_3^2 \delta_t \omega_2^2 \omega_6} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\ & (6\omega_3^2 c_s^2 + \omega_3^2 v_2^2 \omega_6 + 18\omega_3 c_s^2 \omega_6 - 12c_s^2 \omega_6 + 6\omega_3^2 v_2^2 + 12v_2^2 \omega_6 - 12\omega_3 v_2^2 - 3\omega_3^2 c_s^2 \omega_6 - 6\omega_3 v_2^2 \omega_6 - 12\omega_3 c_s^2) \frac{\rho \delta_l^3}{12\omega_3^2 \delta_t \omega_6} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} \\ & + (\omega_3^2 \omega_2^2 - 6\omega_3^2 \omega_2 + 6\omega_2^2 + 6\omega_3^3 - 6\omega_3 \omega_2^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\omega_3^2 \delta_t \omega_6} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho \delta_l^3}{12\omega_3^2 \delta_t \omega_6} \frac{\partial^3 v_2}{\partial x_2^3} + \\ & (12 - 12\omega_4 + \omega_4^2) \frac{\delta_t \rho \delta_l}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-2\omega_4^2 \omega_2 - 6\omega_4 + 3\omega_4^2 - 6\omega_2 + 9\omega_4 \omega_2) \frac{v_3 \rho \delta_l^2}{6\omega_4^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\ & (-6\omega_4 - 2\omega_4 \omega_2^2 - 6\omega_2 + 3\omega_2^2 + 9\omega_4 \omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3 \delta_l^3}{2\delta_t \omega_4^2 \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\ & (-6\omega_4^2 \omega_2 + 6\omega_4^2 + \omega_4^2 \omega_2^2 - 6\omega_4 \omega_2^2 + 6\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\delta_t \omega_4^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\ & (6v_1^2 \omega_2^2 + 6c_s^2 \omega_2^2 - 6v_1^2 \omega_5 \omega_2 + 18c_s^2 \omega_5 \omega_2 - 3c_s^2 \omega_5 \omega_2^2 + v_1^2 \omega_5 \omega_2^2 - 12v_1^2 \omega_2 - 12c_s^2 \omega_2 - 12c_s^2 \omega_5 + 12v_1^2 \omega_5) \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} \end{aligned}$$

$$\begin{aligned}
& + (-6\omega_3 - 2\omega_3\omega_4^2 - 6\omega_4 + 9\omega_3\omega_4 + 3\omega_4^2) \frac{v_3\rho\delta_l^2}{6\omega_3\omega_4^2} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-6\omega_3 - 6\omega_4 + 9\omega_3\omega_4 - 2\omega_3^2\omega_4 + 3\omega_3^2) \frac{v_2\rho\delta_l^2}{6\omega_3^2\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (-2\omega_3\omega_4^2\omega_2^2 - 2\omega_3^2\omega_4\omega_2^2 + \omega_3^2\omega_2^2 + \omega_3^2\omega_4\omega_2 + \omega_3\omega_4^2\omega_2 + \omega_4^2\omega_2^2 - 2\omega_3^2\omega_4^2\omega_2 + \omega_3^2\omega_4^2\omega_2^2 + \omega_3\omega_4\omega_2^2 + \omega_3^2\omega_4) \frac{2v_3v_2v_1\delta_l^3}{\omega_3^2\delta_l\omega_4^2\omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (-6\omega_3\omega_4^2 + 6\omega_3\omega_4 + 3\omega_4^2 - 6\omega_3^2\omega_4 + 3\omega_3^2 + 2\omega_3^2\omega_4^2) \frac{v_3v_2\rho\delta_l^3}{3\omega_3^2\delta_l\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_4^2\omega_2 + 3\omega_4^2 + 2\omega_4^2\omega_2^2 - 6\omega_4\omega_2^2 + 3\omega_2^2 + 6\omega_4\omega_2) \frac{v_3v_1\rho\delta_l^3}{3\delta_l\omega_4^2\omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (2\omega_3^2\omega_2^2 - 6\omega_3^2\omega_2 + 6\omega_3\omega_2 + 3\omega_2^2 + 3\omega_3^2 - 6\omega_3\omega_2^2) \frac{v_2v_1\rho\delta_l^3}{3\omega_3^2\delta_l\omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_3^2\delta_l\omega_4^2\omega_6} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_3\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4 + 6\omega_3^2 + \omega_3^2\omega_4^2) \frac{v_3v_2\rho\delta_l^3}{6\omega_3^2\delta_l\omega_4^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& (6\omega_3^2c_s^2 + \omega_3^2v_2^2\omega_6 + 18\omega_3c_s^2\omega_6 - 12c_s^2\omega_6 + 6\omega_3^2v_2^2 + 12v_2^2\omega_6 - 12\omega_3v_2^2 - 3\omega_3^2c_s^2\omega_6 - 6\omega_3v_2^2\omega_6 - 12\omega_3c_s^2) \frac{\rho\delta_l^3}{12\omega_3^2\delta_l\omega_6} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} \\
& + (12 - 6\omega_7 - 6\omega_4 + \omega_7\omega_4) \frac{v_3\rho\delta_l^2}{6\omega_7\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_3} + C_9 \frac{v_1\delta_l^3}{2\delta_l\omega_7\omega_4^2\omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3} + \\
& (-12c_s^2\omega_4 - 12c_s^2\omega_7 + 6c_s^2\omega_4^2 - 12v_3^2\omega_4 - 3c_s^2\omega_7\omega_4^2 + 12v_3^2\omega_7 + v_3^2\omega_7\omega_4^2 - 6v_3^2\omega_7\omega_4 + 18c_s^2\omega_7\omega_4 + 6v_3^2\omega_4^2) \frac{\rho\delta_l^3}{12\delta_l\omega_7\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3} \\
& + (-6\omega_4^2\omega_2 + 6\omega_4^2 + \omega_4^2\omega_2^2 - 6\omega_4\omega_2^2 + 6\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{6\delta_l\omega_4^2\omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_3} + C_{10} \frac{v_2\delta_l^3}{2\omega_3^2\delta_l\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3} + \\
& (-12c_s^2\omega_4 - 12c_s^2\omega_7 + 6c_s^2\omega_4^2 - 12v_3^2\omega_4 - 3c_s^2\omega_7\omega_4^2 + 12v_3^2\omega_7 + v_3^2\omega_7\omega_4^2 - 6v_3^2\omega_7\omega_4 + 18c_s^2\omega_7\omega_4 + 6v_3^2\omega_4^2) \frac{\rho\delta_l^3}{12\delta_l\omega_7\omega_4^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3} \\
& + (-6\omega_3\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4 + 6\omega_3^2 + \omega_3^2\omega_4^2) \frac{v_3v_2\rho\delta_l^3}{6\omega_3^2\delta_l\omega_4^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3} + C_{11} \frac{v_3\delta_l^3}{6\delta_l\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_3} + C_{12} \frac{\rho\delta_l^3}{12\delta_l\omega_7\omega_4^2} \frac{\partial^3 v_3}{\partial x_3} + \\
& (-2 + 3\omega_2 - \omega_2^2) \frac{\delta_l^2\rho\delta_l}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-4\omega_5\omega_2 + 8\omega_5\omega_2^2 - 2\omega_5\omega_2^2 + 2\omega_3^2 + 2\omega_5^2 - \omega_5^2\omega_2^2 - 4\omega_2^2 - \omega_5^2\omega_2) \frac{\delta_l v_1\rho\delta_l^2}{2\omega_3^2\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + \\
& C_{13} \frac{\rho\delta_l^3}{12\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_l^4}{24\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{v_1\rho\delta_l^4}{12\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 + 3\omega_3 - \omega_3^2) \frac{\delta_l^2\rho\delta_l}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (7\omega_3^3\omega_2 + 13\omega_3^2\omega_2^2 - 24\omega_3^2\omega_2 - \omega_3^3\omega_2^2 + 12\omega_3\omega_2 + 12\omega_2^2 + 12\omega_3^2 - 24\omega_3\omega_2^2 - 6\omega_3^3) \frac{v_2\delta_l\rho\delta_l^2}{12\omega_3^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-\omega_3^2\omega_2^3 + 13\omega_3^2\omega_2^2 - 24\omega_3^2\omega_2 - 6\omega_3^2 + 12\omega_3\omega_2 + 12\omega_2^2 + 12\omega_3^2 - 24\omega_3\omega_2^2 + 7\omega_3\omega_2^3) \frac{\delta_l v_1\rho\delta_l^2}{12\omega_3^2\omega_2^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& C_{16} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^3\omega_5\omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{\rho\delta_l^3}{12\omega_3\omega_5^2\omega_2^3} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{18} \frac{v_2v_1\delta_l^4}{6\omega_3^3\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& C_{20} \frac{v_1\rho\delta_l^4}{12\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-4\omega_3\omega_6 + 2\omega_6^2 - \omega_3\omega_6^2 - 2\omega_3^3\omega_6 - \omega_3^2\omega_6^2 + 8\omega_3^2\omega_6 - 4\omega_3^2 + 2\omega_3^3) \frac{v_2\delta_l\rho\delta_l^2}{2\omega_3^3\omega_6^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + \\
& C_{21} \frac{\rho\delta_l^3}{12\omega_3^3\omega_2\omega_6^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + C_{22} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^3\omega_3^2\omega_6^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + C_{23} \frac{\delta_l^4}{4\omega_3^3\delta_l\omega_5^2\omega_2^3\omega_6^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{v_1\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2\omega_2^3\omega_6^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& C_{25} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\rho\delta_l^3}{12\omega_3^3\omega_6^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + C_{27} \frac{v_2v_1\delta_l^4}{6\omega_3^3\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{28} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_l\omega_6^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{29} \frac{v_1\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2\omega_6^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} \\
& + C_{30} \frac{\delta_l^4}{24\omega_3^3\delta_l\omega_6^2} \frac{\partial^4 \rho}{\partial x_2^4} + C_{31} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_l\omega_6^2} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 + 3\omega_4 - \omega_4^2) \frac{\delta_l^2\rho\delta_l}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (-24\omega_4^2\omega_2 - \omega_4^3\omega_2^2 + 7\omega_4^3\omega_2 - 6\omega_4^3 + 12\omega_4^2 + 13\omega_4^2\omega_2^2 - 24\omega_4\omega_2^2 + 12\omega_2^2 + 12\omega_4\omega_2) \frac{v_3\delta_l\rho\delta_l^2}{12\omega_4^3\omega_2^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-24\omega_4^2\omega_2 - \omega_4^3\omega_2^2 + 12\omega_4^2 + 13\omega_4^2\omega_2^2 - 6\omega_4^2 - 24\omega_4\omega_2^2 + 7\omega_4\omega_2^3 + 12\omega_2^2 + 12\omega_4\omega_2) \frac{\delta_l v_1\rho\delta_l^2}{12\omega_4^2\omega_2^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& C_{32} \frac{v_3v_1\rho\delta_l^3}{6\omega_4^3\omega_5\omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + C_{33} \frac{\rho\delta_l^3}{12\omega_4\omega_5^2\omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{34} \frac{v_3v_1\delta_l^4}{6\delta_l\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{35} \frac{v_3\rho\delta_l^4}{12\delta_l\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& C_{36} \frac{v_1\rho\delta_l^4}{12\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-24\omega_3\omega_4^2 + 7\omega_3\omega_4^3 - 6\omega_4^3 + 12\omega_3\omega_4 + 12\omega_4^2 - 24\omega_3^2\omega_4 - \omega_3^2\omega_4^3 + 12\omega_3^2 + 13\omega_3^2\omega_4^2) \frac{v_3\delta_l\rho\delta_l^2}{12\omega_3^2\omega_4^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (-24\omega_3\omega_4^2 + 12\omega_3\omega_4 + 12\omega_4^2 - 24\omega_3^2\omega_4 - \omega_3^3\omega_4^2 + 7\omega_3^3\omega_4 + 12\omega_3^2 - 6\omega_3^3 + 13\omega_3^2\omega_4^2) \frac{v_2\delta_l\rho\delta_l^2}{12\omega_3^3\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_3v_2\rho\delta_l^3}{6\omega_3^3\omega_4^2\omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{38} \frac{v_3v_1\rho\delta_l^3}{6\omega_3\omega_4^3\omega_2^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{39} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^3\omega_4\omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{40} \frac{v_3v_2\delta_l^4}{\omega_3^3\delta_l\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{41} \frac{v_3v_2v_1\rho\delta_l^4}{6\omega_3^3\delta_l\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{42} \frac{v_3\rho\delta_l^4}{12\delta_l\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{43} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2\omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{44} \frac{v_3v_2\rho\delta_l^3}{6\omega_3^3\omega_4^3\omega_6} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\rho\delta_l^3}{12\omega_3^3\omega_4\omega_6^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{46} \frac{v_3v_1\delta_l^4}{\omega_3^3\delta_l\omega_4^3\omega_5^2\omega_6^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{47} \frac{v_3\rho\delta_l^4}{12\omega_3^3\delta_l\omega_4^3\omega_6^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{48} \frac{v_3v_2v_1\rho\delta_l^4}{6\omega_3^3\delta_l\omega_4^3\omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{49} \frac{v_1\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2\omega_6^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{50} \frac{v_3v_2\delta_l^4}{6\omega_3^3\delta_l\omega_4^3\omega_6^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{51} \frac{v_3\rho\delta_l^4}{12\omega_3^3\delta_l\omega_4^3\omega_6^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{52} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_l\omega_5^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& (8\omega_7\omega_4^2 - 2\omega_7\omega_4^3 + 2\omega_7^2 + 2\omega_4^2 - 4\omega_4^2 - 4\omega_7\omega_4 - \omega_7^2\omega_4 - \omega_7^2\omega_4^2) \frac{v_3\delta_l\rho\delta_l^2}{2\omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3} + C_{53} \frac{\rho\delta_l^3}{12\omega_7^2\omega_4^3\omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& C_{54} \frac{v_3 v_1 \rho \delta_1^3}{6\omega_7 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3} + C_{55} \frac{\delta_1^4}{4\delta_t \omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{56} \frac{v_1 \rho \delta_1^4}{12\delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + C_{57} \frac{v_3 \rho \delta_1^4}{12\delta_t \omega_7^3 \omega_5^2 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + \\
& C_{58} \frac{\rho \delta_1^3}{12\omega_3 \omega_7^2 \omega_4^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3} + C_{59} \frac{v_3 v_2 \rho \delta_1^3}{6\omega_3^3 \omega_7 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3} + C_{60} \frac{v_2 v_1 \delta_1^4}{\omega_3^3 \delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{61} \frac{v_2 \rho \delta_1^4}{12\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& C_{62} \frac{v_1 \rho \delta_1^4}{12\delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + C_{63} \frac{v_3 v_2 v_1 \rho \delta_1^4}{6\omega_3^3 \delta_t \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{64} \frac{\delta_1^4}{4\omega_3^3 \delta_t \omega_7^2 \omega_4^3 \omega_6^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{65} \frac{v_2 \rho \delta_1^4}{12\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& C_{66} \frac{v_3 \rho \delta_1^4}{12\omega_3^3 \delta_t \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{67} \frac{\rho \delta_1^3}{12\omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3} + C_{68} \frac{v_3 v_1 \delta_1^4}{6\delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + C_{69} \frac{v_3 \rho \delta_1^4}{12\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} + C_{70} \frac{v_1 \rho \delta_1^4}{12\delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} \\
& + C_{71} \frac{v_3 v_2 \delta_1^4}{6\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3} + C_{72} \frac{v_3 \rho \delta_1^4}{12\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + C_{73} \frac{v_2 \rho \delta_1^4}{12\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3} + C_{74} \frac{\delta_1^4}{24\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_3} + C_{75} \frac{v_3 \rho \delta_1^4}{12\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial x_3} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -3\omega_5\omega_2 + \omega_5\omega_2^2 + 3v_1^2\omega_2^2 + 3c_s^2\omega_2^2 + 3v_1^2\omega_5\omega_2 + 15c_s^2\omega_5\omega_2 + 6\omega_2 - 3\omega_2^2 - 3c_s^2\omega_5\omega_2^2 - v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_2 - 6c_s^2\omega_2 - 12c_s^2\omega_5 \\
C_2 &= -6\omega_5\omega_2 + 2\omega_5\omega_2^2 + 6v_1^2\omega_2^2 + 6c_s^2\omega_2^2 + 18v_1^2\omega_5\omega_2 + 18c_s^2\omega_5\omega_2 + 12\omega_2 - 6\omega_2^2 - 3c_s^2\omega_5\omega_2^2 - 5v_1^2\omega_5\omega_2^2 - 12v_1^2\omega_2 - 12c_s^2\omega_2 - 12c_s^2\omega_5 - 12v_1^2\omega_5 \\
C_3 &= \omega_3^2 c_s^2 \omega_2^2 + \omega_3^2 v_1^2 \omega_2^2 + \omega_3 c_s^2 \omega_5 \omega_2^2 - 3\omega_3 v_1^2 \omega_5 \omega_2^2 + 4\omega_3^2 v_1^2 \omega_5 - 2\omega_3^2 c_s^2 \omega_5 + 2\omega_3 v_1^2 \omega_5 \omega_2 - 2\omega_3 c_s^2 \omega_5 \omega_2 - 2\omega_3^2 c_s^2 \omega_2 - 2\omega_3^2 v_1^2 \omega_2 + \omega_3^2 v_1^2 \omega_5 \omega_2^2 - \\
& \omega_3^2 c_s^2 \omega_5 \omega_2^2 + 2v_1^2 \omega_5 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_5 \omega_2 - 4\omega_3^2 v_1^2 \omega_5 \omega_2 \\
C_4 &= 4v_2^2 \omega_2^2 \omega_6 + 2\omega_3 v_2^2 \omega_2 \omega_6 + \omega_3^2 c_s^2 \omega_2 \omega_6 - 2\omega_3 v_2^2 \omega_2^2 + \omega_3^2 c_s^2 \omega_2^2 + 2\omega_3^2 v_2^2 \omega_6 + 4\omega_3 c_s^2 \omega_2^2 \omega_6 + \omega_3^2 v_2^2 \omega_2^2 \omega_6 - 2\omega_3 c_s^2 \omega_2 \omega_6 - 3\omega_3^2 v_2^2 \omega_2 \omega_6 - \\
& 2c_s^2 \omega_2^2 \omega_6 - 2\omega_3 c_s^2 \omega_2^2 + \omega_3^2 v_2^2 \omega_2^2 - 4\omega_3 v_2^2 \omega_2^2 \omega_6 - \omega_3^2 c_s^2 \omega_2^2 \omega_6 \\
C_5 &= 6\omega_3 + 3\omega_3^2 c_s^2 - \omega_3^2 v_2^2 \omega_6 + 15\omega_3 c_s^2 \omega_6 - 3\omega_3 \omega_6 - 12c_s^2 \omega_6 + 3\omega_3^2 v_2^2 - 6\omega_3 v_2^2 + \omega_3^2 \omega_6 - 3\omega_3^2 - 3\omega_3^2 c_s^2 \omega_6 + 3\omega_3 v_2^2 \omega_6 - 6\omega_3 c_s^2 \\
C_6 &= 12\omega_3 + 6\omega_3^2 c_s^2 - 5\omega_3^2 v_2^2 \omega_6 + 18\omega_3 c_s^2 \omega_6 - 6\omega_3 \omega_6 - 12c_s^2 \omega_6 + 6\omega_3^2 v_2^2 - 12v_2^2 \omega_6 - 12\omega_3 v_2^2 + 2\omega_3^2 \omega_6 - 6\omega_3^2 - 3\omega_3^2 c_s^2 \omega_6 + 18\omega_3 v_2^2 \omega_6 - 12\omega_3 c_s^2 \\
C_7 &= -4v_1^2 \omega_2^2 \omega_5 \omega_2 + 4c_s^2 \omega_2^2 \omega_5 \omega_2 - c_s^2 \omega_4^2 \omega_5 \omega_2^2 + v_1^2 \omega_4^2 \omega_5 \omega_2^2 + c_s^2 \omega_4 \omega_5 \omega_2^2 - 3v_1^2 \omega_4 \omega_5 \omega_2^2 - 2v_1^2 \omega_4^2 \omega_2 - 2c_s^2 \omega_4^2 \omega_2 - 2c_s^2 \omega_4^2 \omega_5 + 4v_1^2 \omega_4^2 \omega_5 + \\
& 2v_1^2 \omega_5 \omega_2^2 + c_s^2 \omega_4^2 \omega_2^2 + v_1^2 \omega_4^2 \omega_2^2 + 2v_1^2 \omega_4 \omega_5 \omega_2 - 2c_s^2 \omega_4 \omega_5 \omega_2 \\
C_8 &= -2\omega_3 c_s^2 \omega_4 \omega_6 - 3\omega_3^2 v_2^2 \omega_4 \omega_6 - 2\omega_3 c_s^2 \omega_4^2 + \omega_3^2 v_2^2 \omega_4^2 - 2c_s^2 \omega_4^2 \omega_6 + 2\omega_3^2 v_2^2 \omega_6 - 4\omega_3 v_2^2 \omega_4^2 \omega_6 - \omega_3^2 c_s^2 \omega_4^2 \omega_6 + 4v_2^2 \omega_4^2 \omega_6 + 2\omega_3 v_2^2 \omega_4 \omega_6 + \\
& \omega_3^2 c_s^2 \omega_4 \omega_6 - 2\omega_3 v_2^2 \omega_4^2 + \omega_3^2 c_s^2 \omega_4^2 + 4\omega_3 c_s^2 \omega_4^2 \omega_6 + \omega_3^2 v_2^2 \omega_4^2 \omega_6 \\
C_9 &= -c_s^2 \omega_7 \omega_4^2 \omega_2^2 - 2c_s^2 \omega_4 \omega_2^2 - 2v_3^2 \omega_4 \omega_2^2 - 3v_3^2 \omega_7 \omega_4^2 \omega_2 + v_3^2 \omega_7 \omega_4^2 \omega_2^2 - 2c_s^2 \omega_7 \omega_2^2 + c_s^2 \omega_7 \omega_4^2 \omega_2 + 4v_3^2 \omega_7 \omega_2^2 - 2c_s^2 \omega_7 \omega_4 \omega_2 - 4v_3^2 \omega_7 \omega_4 \omega_2^2 + \\
& 2v_3^2 \omega_7 \omega_4^2 + v_3^2 \omega_4^2 \omega_2^2 + 2v_3^2 \omega_7 \omega_4 \omega_2 + 4c_s^2 \omega_7 \omega_4 \omega_2^2 + c_s^2 \omega_4^2 \omega_2^2 \\
C_{10} &= 4v_3^2 \omega_3^2 \omega_7 - 2\omega_3 c_s^2 \omega_7 \omega_4 - 3v_3^2 \omega_3 \omega_7 \omega_2^2 - 2v_3^2 \omega_3^2 \omega_4 + v_3^2 \omega_3^2 \omega_4^2 + \omega_3 c_s^2 \omega_7 \omega_4^2 + 2v_3^2 \omega_3 \omega_7 \omega_4 - 2\omega_3^2 c_s^2 \omega_7 + 4\omega_3^2 c_s^2 \omega_7 \omega_4 - 4v_3^2 \omega_3^2 \omega_7 \omega_4 - \\
& 2\omega_3^2 c_s^2 \omega_4 + 2v_3^2 \omega_7 \omega_4^2 + v_3^2 \omega_3 \omega_7 \omega_4^2 + \omega_3^2 c_s^2 \omega_4^2 - \omega_3^2 c_s^2 \omega_7 \omega_4^2 \\
C_{11} &= \omega_7 \omega_4^2 - 6c_s^2 \omega_4 - 12c_s^2 \omega_7 + 6\omega_4 + 3c_s^2 \omega_4^2 - 3\omega_4^2 - 3\omega_7 \omega_4 - 6v_3^2 \omega_4 - 3c_s^2 \omega_7 \omega_4^2 - v_3^2 \omega_7 \omega_4^2 + 3v_3^2 \omega_7 \omega_4 + 15c_s^2 \omega_7 \omega_4 + 3v_3^2 \omega_4^2 \\
C_{12} &= 2\omega_7 \omega_4^2 - 12c_s^2 \omega_4 - 12c_s^2 \omega_7 + 12\omega_4 + 6c_s^2 \omega_4^2 - 6\omega_4^2 - 6\omega_7 \omega_4 - 12v_3^2 \omega_4 - 3c_s^2 \omega_7 \omega_4^2 - 12v_3^2 \omega_7 - 5v_3^2 \omega_7 \omega_4^2 + 18v_3^2 \omega_7 \omega_4 + 18c_s^2 \omega_7 \omega_4 + 6v_3^2 \omega_4^2 \\
C_{13} &= -3v_1^2 \omega_5^2 \omega_2^3 - 2c_s^2 \omega_5^2 \omega_2^3 + 25c_s^2 \omega_5^2 \omega_2^2 + 27v_1^2 \omega_5^2 \omega_2^2 - 24\omega_5 \omega_2 + 36\omega_5 \omega_2^2 - 42v_1^2 \omega_5^2 \omega_2 - 48c_s^2 \omega_5^2 \omega_2 - 9\omega_5 \omega_2^3 - 6c_s^2 \omega_2^3 - 6v_1^2 \omega_2^3 + 24c_s^2 \omega_5^2 + \\
& 12v_1^2 \omega_5^2 + 6\omega_2^3 + \omega_5^2 \omega_2^2 + 12v_1^2 \omega_2^2 + 12c_s^2 \omega_2^2 + 48v_1^2 \omega_5 \omega_2 + 24c_s^2 \omega_5 \omega_2 - 11\omega_5^2 \omega_2^2 - 12\omega_2^2 + 12\omega_5^2 \omega_2 - 36c_s^2 \omega_5 \omega_2^2 - 60v_1^2 \omega_5 \omega_2^2 + 15v_1^2 \omega_5 \omega_2^2 + 9c_s^2 \omega_5 \omega_2^2 \\
C_{14} &= -3v_1^2 \omega_5^2 \omega_2^3 + c_s^2 \omega_5^2 \omega_2^3 - 72v_1^2 c_s^2 \omega_5^2 \omega_2^2 - 24v_1^4 \omega_2^2 - 48c_s^4 \omega_5^2 \omega_2 + 24v_1^4 \omega_5^2 \omega_2 + 12v_1^2 c_s^2 \omega_2^3 - 96v_1^2 c_s^2 \omega_5^2 + 12v_1^4 \omega_2^3 - 8c_s^2 \omega_5^2 \omega_2^2 + 24v_1^2 \omega_5^2 \omega_2^2 + \\
& 6v_1^2 c_s^2 \omega_5^2 \omega_2^3 + 24c_s^4 \omega_5^2 \omega_2^2 - 24v_1^2 c_s^2 \omega_2^2 - 3c_s^4 \omega_5^2 \omega_2^3 + 3v_1^4 \omega_5^2 \omega_2^3 - 24v_1^2 \omega_5^2 \omega_2 + 12c_s^2 \omega_5^2 \omega_2 - 24v_1^4 \omega_5^2 \omega_2^2 + 24c_s^4 \omega_5^2 \omega_2^2 + 156v_1^2 c_s^2 \omega_5^2 \omega_2 - 12v_1^2 \omega_2^3 + \\
& 72v_1^4 \omega_5 \omega_2^2 - 24c_s^4 \omega_5 \omega_2^2 - 24v_1^2 c_s^2 \omega_5 \omega_2 + 6c_s^4 \omega_5 \omega_2^2 - 18v_1^4 \omega_5 \omega_2^2 + 24v_1^2 \omega_2^2 + 48v_1^2 \omega_5 \omega_2 - 24c_s^2 \omega_5 \omega_2 - 12v_1^2 c_s^2 \omega_5 \omega_2^3 + 24c_s^2 \omega_5 \omega_2^2 - 72v_1^2 \omega_5 \omega_2^2 + \\
& 48v_1^2 c_s^2 \omega_5 \omega_2^2 + 18v_1^2 \omega_5 \omega_2^2 - 6c_s^2 \omega_5 \omega_2^2 + 24c_s^4 \omega_5 \omega_2 - 48v_1^4 \omega_5 \omega_2 \\
C_{15} &= 2v_1^2 \omega_5^2 \omega_2^3 + c_s^2 \omega_5^2 \omega_2^3 - 20c_s^2 \omega_5^2 \omega_2^2 - 16v_1^2 \omega_5^2 \omega_2^2 + 12\omega_5 \omega_2 - 24\omega_5 \omega_2^2 + 24v_1^2 \omega_5^2 \omega_2 + 42c_s^2 \omega_5^2 \omega_2 + 6\omega_5 \omega_2^3 + 6c_s^2 \omega_2^3 + 6v_1^2 \omega_2^3 - 24c_s^2 \omega_5^2 - \\
& 12v_1^2 \omega_5^2 - 6\omega_2^3 - \omega_5^2 \omega_2^2 - 12v_1^2 \omega_2^2 - 12c_s^2 \omega_2^2 - 12v_1^2 \omega_5 \omega_2 - 12c_s^2 \omega_5 \omega_2 + 8\omega_5^2 \omega_2^2 + 12\omega_2^2 - 6\omega_2^2 \omega_2 + 24c_s^2 \omega_5 \omega_2^2 + 24v_1^2 \omega_5 \omega_2^2 - 6v_1^2 \omega_5 \omega_2^2 - 6c_s^2 \omega_5 \omega_2^3 \\
C_{16} &= 12\omega_3 \omega_5 \omega_2^3 - 6\omega_2^3 \omega_2^3 + 24\omega_3^2 \omega_5 \omega_2 - 6\omega_3 \omega_5 \omega_2^2 - 12\omega_3^2 \omega_5 + 12\omega_3^2 \omega_2^2 + 3\omega_3^2 \omega_2^3 - 10\omega_3^2 \omega_5 \omega_2^2 - 6\omega_3^2 \omega_2^2 - 6\omega_5 \omega_2^3 + \omega_3^2 \omega_5 \omega_2^3 - 12\omega_3^2 \omega_5 \omega_2 - \\
& 7\omega_3^2 \omega_5 \omega_2^2 + 12\omega_3^2 \omega_5 \omega_2^2 \\
C_{17} &= -v_1^2 \omega_2^2 \omega_2^3 + 3c_s^2 \omega_5^2 \omega_2^3 + 9\omega_3 v_1^2 \omega_5 \omega_2^3 + 9\omega_3 c_s^2 \omega_5 \omega_2^3 - 18c_s^2 \omega_5^2 \omega_2^2 + 6v_1^2 \omega_5^2 \omega_2^2 - 30\omega_3 c_s^2 \omega_5 \omega_2^2 - 30\omega_3 v_1^2 \omega_5 \omega_2^2 + 12\omega_3 v_1^2 \omega_5 \omega_2 + \\
& 12\omega_3 c_s^2 \omega_5 \omega_2 - 12v_1^2 \omega_2^2 \omega_2 + 12c_s^2 \omega_5^2 \omega_2 + 36\omega_3 v_1^2 \omega_5^2 \omega_2 - 30\omega_3 c_s^2 \omega_5^2 \omega_2 + 12c_s^2 \omega_5 \omega_2^2 + 12v_1^2 \omega_5 \omega_2^2 + 12\omega_3 v_1^2 \omega_2^2 + 12\omega_3 c_s^2 \omega_2^2 + 22\omega_3 c_s^2 \omega_5^2 \omega_2^2 - \\
& 10\omega_3 v_1^2 \omega_5^2 \omega_2^2 - 6v_1^2 \omega_5 \omega_2^2 - 6c_s^2 \omega_5 \omega_2^2 + 12\omega_3 c_s^2 \omega_5^2 - 24\omega_3 v_1^2 \omega_5^2 + \omega_3 v_1^2 \omega_5^2 \omega_2^2 - 2\omega_3 c_s^2 \omega_5^2 \omega_2^2 - 6\omega_3 c_s^2 \omega_2^2 - 6\omega_3 v_1^2 \omega_2^2 \\
C_{18} &= -3\omega_3^2 \omega_5^2 \omega_2^2 + 6\omega_3^2 c_s^2 \omega_5^2 \omega_2^2 + 6v_1^2 \omega_5^2 \omega_2^3 + 12\omega_3^2 \omega_5 \omega_2 - 48\omega_3^2 c_s^2 \omega_5^2 \omega_2^2 + \omega_3^2 \omega_5^2 \omega_2^3 + 6\omega_3^2 v_1^2 \omega_5^2 \omega_2^2 - 24\omega_3^2 c_s^2 \omega_5^2 \omega_2^2 + 12\omega_3^2 v_1^2 \omega_5^2 \omega_2 - \\
& 12\omega_3^2 v_1^2 \omega_2^2 \omega_2^2 + 42\omega_3^2 c_s^2 \omega_5^2 \omega_2^2 - 3\omega_3^2 \omega_2^3 - 21\omega_3^2 \omega_5 \omega_2^2 - 30\omega_3^2 v_1^2 \omega_5^2 \omega_2 + 78\omega_3^2 c_s^2 \omega_5^2 \omega_2 + 6\omega_3^2 \omega_2^2 - 12\omega_3^2 c_s^2 \omega_5^2 \omega_2^3 + 6\omega_3^2 v_1^2 \omega_5^2 \omega_2^3 + 6\omega_3^2 \omega_5 \omega_2^3 + \\
& 6\omega_3^2 c_s^2 \omega_2^2 + 6\omega_3^2 v_1^2 \omega_2^2 + 6\omega_3^2 c_s^2 \omega_5 \omega_2^2 + 6\omega_3^2 v_1^2 \omega_5 \omega_2^2 - 36\omega_3^2 c_s^2 \omega_5^2 + 24\omega_3^2 v_1^2 \omega_5^2 - \omega_3^2 \omega_5^2 \omega_2^2 - 12\omega_3^2 v_1^2 \omega_5 \omega_2^2 - 12\omega_3^2 c_s^2 \omega_5 \omega_2^2 - 12\omega_3^2 v_1^2 \omega_2^2 -
\end{aligned}$$

$$C_{74} = 12c_s^2\omega_7^2\omega_4 - 3c_s^4\omega_7^2\omega_4^3 - 72v_3^2c_s^2\omega_7^2\omega_4^2 - 24v_3^4\omega_7^2\omega_4^2 - 24v_3^2\omega_7^2\omega_4 + 3v_3^4\omega_7^2\omega_4^3 + 6v_3^2c_s^2\omega_7^2\omega_4^3 + 24c_s^4\omega_7^2\omega_4^2 - 48c_s^4\omega_7^2\omega_4 + c_s^2\omega_7^2\omega_4^3 + 24v_3^2\omega_7^2\omega_4^2 - 24v_3^4\omega_4^2 + 156v_3^2c_s^2\omega_7^2\omega_4 + 24v_3^4\omega_7^2\omega_4 + 12v_3^4\omega_4^3 - 3v_3^2\omega_7^2\omega_4^3 - 8c_s^2\omega_7^2\omega_4^2 - 48v_3^4\omega_7\omega_4 - 24v_3^2c_s^2\omega_7\omega_4 + 18v_3^2\omega_7\omega_4^3 + 24c_s^2\omega_7\omega_4^2 + 24c_s^4\omega_7\omega_4 - 6c_s^2\omega_7\omega_4^3 - 72v_3^2\omega_7\omega_4^2 + 48v_3^2\omega_7\omega_4 - 12v_3^2c_s^2\omega_7\omega_4^3 - 12v_3^2\omega_4^3 - 18v_3^4\omega_7\omega_4^3 - 24c_s^4\omega_7\omega_4^2 - 24v_3^2c_s^2\omega_4^2 + 24c_s^4\omega_7^2 - 24c_s^2\omega_7\omega_4 + 6c_s^4\omega_7\omega_4^3 + 12v_3^2c_s^2\omega_4^3 - 96v_3^2c_s^2\omega_7^2 + 72v_3^4\omega_7\omega_4^2 + 24v_3^2\omega_4^2 + 48v_3^2c_s^2\omega_7\omega_4^2$$

$$C_{75} = 42c_s^2\omega_7^2\omega_4 - 24\omega_7\omega_4^2 + 6\omega_7\omega_4^3 + 24v_3^2\omega_7^2\omega_4 + 6c_s^2\omega_4^3 - 24c_s^2\omega_7^2 + c_s^2\omega_7^2\omega_4^3 - 6\omega_4^3 - 16v_3^2\omega_7^2\omega_4^2 - 12c_s^2\omega_4^2 + 2v_3^2\omega_7^2\omega_4^3 + 12\omega_4^2 + 12\omega_7\omega_4 - 20c_s^2\omega_7^2\omega_4^2 - 6v_3^2\omega_7\omega_4^3 + 24c_s^2\omega_7\omega_4^2 - 6\omega_7\omega_4 - 6c_s^2\omega_7\omega_4^3 + 24v_3^2\omega_7\omega_4^2 - \omega_7^2\omega_4^3 - 12v_3^2\omega_7\omega_4 + 6v_3^2\omega_4^3 - 12v_3^2\omega_7^2 + 8\omega_7^2\omega_4^2 - 12c_s^2\omega_7\omega_4 - 12v_3^2\omega_4^2$$

2.3 MRT2

2.3.1 Definitions

Collision operator C :

$$C(f) = \mathbf{M}_2^{-1} \mathbf{S} \left(\boldsymbol{\mu}_2^{(eq)} - \mathbf{M}_2 f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2)$.

Matrix \mathbf{M}_2 corresponds to the transformation matrix to the raw moment basis defined by

$$\boldsymbol{\mu}_2 = \begin{pmatrix} m_{(0,0,0)} \\ m_{(1,0,0)} \\ m_{(0,1,0)} \\ m_{(0,0,1)} \\ m_{(2,0,0)} + m_{(0,2,0)} + m_{(0,0,2)} \\ m_{(2,0,0)} - m_{(0,2,0)} \\ m_{(2,0,0)} - m_{(0,0,2)} \end{pmatrix},$$

and is given by

$$\mathbf{M}_2 = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & -1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & -1 & 1 & 0 & -1 \end{pmatrix}.$$

The equilibrium moments $\boldsymbol{\mu}_2^{(eq)}$ are defined by

$$\boldsymbol{\mu}_2^{(eq)} = \mathbf{M}_2 \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\mu}_2^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho(v_3^2 + v_2^2 + v_1^2 + 3c_s^2) \\ \rho(v_1^2 - v_2^2) \\ \rho(v_1^2 - v_3^2) \end{pmatrix}.$$

2.3.2 Conservation of mass equation



attached text file: output_d3q7_ade_mrt2_symbolic_pde_00.txt

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{\delta_1 v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_1 \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_1 \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_1}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\
& (-2 + \omega_2) \frac{\delta_1^2 v_1}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\delta_1^2 \rho}{2\omega_2 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{\delta_1^2 v_2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{\delta_1^2 v_1}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{\delta_1^2 \rho}{\omega_2 \omega_3 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{\delta_1^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_2 + \omega_4 - \omega_2 \omega_4) \frac{\delta_1^2 v_1}{\omega_2 \delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_2 + \omega_4 - \omega_2 \omega_4) \frac{\delta_1^2 \rho}{\omega_2 \delta_t \omega_4} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_1}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{\delta_1^2 v_2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\
& (2 - \omega_2) \frac{\delta_1^2 v_1}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_3) \frac{\delta_1^2 v_2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\delta_1^2 \rho}{2\omega_3 \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{\delta_1^2 v_3}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{\delta_1^2 v_2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{\delta_1^2 \rho}{\omega_3 \delta_t \omega_4} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_1}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + \\
& (\omega_2 + \omega_4 - \omega_2 \omega_4) \frac{\delta_1^2 v_3}{\omega_2 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{\delta_1^2 v_1}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{\delta_1^2 v_3}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{\delta_1^2 v_2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\
& + (-2 + \omega_4) \frac{\delta_1^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_1^2 \rho}{2\delta_t \omega_4} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\delta_1 \rho}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{\delta_1^2 c_s^2}{2\omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + \\
& (-2 + \omega_2) \frac{\delta_1^2 v_1 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\delta_1 \rho}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{\delta_1^2 v_2 v_1}{\omega_2 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{\delta_1^2 v_2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (2 - \omega_2) \frac{\delta_1^2 v_1 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{\delta_1^2 c_s^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_3) \frac{\delta_1^2 v_2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\delta_1 \rho}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + \\
& (\omega_2 + \omega_4 - \omega_2 \omega_4) \frac{\delta_1^2 v_1 v_3}{\omega_2 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{\delta_1^2 \rho v_3}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (2 - \omega_2) \frac{\delta_1^2 v_1 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{\delta_1^2 v_2 v_3}{\omega_3 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + \\
& + (2 - \omega_4) \frac{\delta_1^2 \rho v_3}{2\delta_t \omega_4} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{\delta_1^2 v_2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_4) \frac{\delta_1^2 c_s^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{\delta_1^2 \rho v_3}{2\delta_t \omega_4} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (12 + \omega_2^2 - 12\omega_2) \frac{\delta_1 \delta_t \rho}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 - 6\omega_5 - 6\omega_2 + \omega_5 \omega_2) \frac{\delta_1^2 v_1 \rho}{6\omega_5 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1} + C_1 \frac{\delta_1^3 v_1}{6\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_1^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (12 + \omega_3^2 - 12\omega_3) \frac{\delta_1 \delta_t \rho}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + (9\omega_2 \omega_3 - 6\omega_2 - 2\omega_2 \omega_3^2 + 3\omega_3^2 - 6\omega_3) \frac{\delta_1^2 v_2 \rho}{6\omega_2 \omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + \\
& (9\omega_2 \omega_3 + 3\omega_2^2 - 6\omega_2 - 6\omega_3 - 2\omega_2^2 \omega_3) \frac{\delta_1^2 v_1 \rho}{6\omega_2^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + C_3 \frac{\delta_1^3 v_2}{2\omega_5 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& (6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3) \frac{\delta_1^3 v_2 v_1 \rho}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (-3\omega_5 \omega_2^2 c_s^2 - 12\omega_2 c_s^2 + 12\omega_5 v_1^2 - 6\omega_5 \omega_2 v_1^2 + 6\omega_2^2 v_1^2 - 12\omega_2 v_1^2 + \omega_5 \omega_2^2 v_1^2 - 12\omega_5 c_s^2 + 6\omega_2^2 c_s^2 + 18\omega_5 \omega_2 c_s^2) \frac{\delta_1^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& + (12 + \omega_6 \omega_3 - 6\omega_6 - 6\omega_3) \frac{\delta_1^2 v_2 \rho}{6\omega_6 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{\delta_1^3 v_1}{2\omega_2^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (\omega_6 \omega_3^2 v_2^2 - 12\omega_6 c_s^2 + 18\omega_6 \omega_3 c_s^2 - 12\omega_3 c_s^2 + 6\omega_3^2 v_2^2 - 12\omega_3 v_2^2 + 6\omega_3^2 c_s^2 + 12\omega_6 v_2^2 - 3\omega_6 \omega_3^2 c_s^2 - 6\omega_6 \omega_3 v_2^2) \frac{\delta_1^3 \rho}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& + (6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3) \frac{\delta_1^3 v_2 v_1 \rho}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{\delta_1^3 v_2}{6\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\delta_1^3 \rho}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 + \omega_4^2 - 12\omega_4) \frac{\delta_1 \delta_t \rho}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-6\omega_2 + 3\omega_4^2 - 2\omega_2 \omega_4^2 - 6\omega_4 + 9\omega_2 \omega_4) \frac{\delta_1^2 \rho v_3}{6\omega_2 \omega_4^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (-2\omega_2^2 \omega_4 + 3\omega_2^2 - 6\omega_2 - 6\omega_4 + 9\omega_2 \omega_4) \frac{\delta_1^2 v_1 \rho}{6\omega_2^2 \omega_4} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{\delta_1^3 v_3}{2\omega_5 \omega_2^2 \delta_t \omega_4^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (-6\omega_2^2 \omega_4 + 6\omega_2^2 + 6\omega_4^2 + \omega_2^2 \omega_4^2 - 6\omega_2 \omega_4^2) \frac{\delta_1^3 v_1 \rho v_3}{6\omega_2^2 \delta_t \omega_4^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\
& (-3\omega_5 \omega_2^2 c_s^2 - 12\omega_2 c_s^2 + 12\omega_5 v_1^2 - 6\omega_5 \omega_2 v_1^2 + 6\omega_2^2 v_1^2 - 12\omega_2 v_1^2 + \omega_5 \omega_2^2 v_1^2 - 12\omega_5 c_s^2 + 6\omega_2^2 c_s^2 + 18\omega_5 \omega_2 c_s^2) \frac{\delta_1^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& + (3\omega_4^2 - 6\omega_3 + 9\omega_3 \omega_4 - 2\omega_3 \omega_4^2 - 6\omega_4) \frac{\delta_1^2 \rho v_3}{6\omega_3 \omega_4^2} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-2\omega_3^2 \omega_4 + 3\omega_3^2 - 6\omega_3 + 9\omega_3 \omega_4 - 6\omega_4) \frac{\delta_1^2 v_2 \rho}{6\omega_3^2 \omega_4} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_2 \omega_3^2 \omega_4 + \omega_3^2 \omega_4^2 + \omega_2^2 \omega_3 \omega_4 - 2\omega_2^2 \omega_3 \omega_4^2 - 2\omega_2 \omega_3^2 \omega_4^2 + \omega_2^2 \omega_4^2 + \omega_2 \omega_3 \omega_4^2 + \omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2 \omega_4^2 - 2\omega_2^2 \omega_3^2 \omega_4) \frac{2\delta_1^3 v_2 v_1 v_3}{\omega_2^2 \omega_3^2 \delta_t \omega_4^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\
& + (2\omega_3^2 \omega_4^2 - 6\omega_3^2 \omega_4 + 3\omega_4^2 + 3\omega_3^2 + 6\omega_3 \omega_4 - 6\omega_3 \omega_4^2) \frac{\delta_1^3 v_2 \rho v_3}{3\omega_3^2 \delta_t \omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2^2 \omega_4 + 3\omega_2^2 + 3\omega_4^2 + 2\omega_2^2 \omega_4^2 - 6\omega_2 \omega_4^2 + 6\omega_2 \omega_4) \frac{\delta_1^3 v_1 \rho v_3}{3\omega_2^2 \delta_t \omega_4^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (6\omega_2 \omega_3 + 3\omega_2^2 - 6\omega_2 \omega_3^2 + 3\omega_3^2 + 2\omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3) \frac{\delta_1^3 v_2 v_1 \rho}{3\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{\delta_1^3 v_3}{2\omega_6 \omega_3^2 \delta_t \omega_4^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (\omega_3^2 \omega_4^2 - 6\omega_3^2 \omega_4 + 6\omega_4^2 + 6\omega_3^2 - 6\omega_3 \omega_4^2) \frac{\delta_1^3 v_2 \rho v_3}{6\omega_3^2 \delta_t \omega_4^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (\omega_6\omega_3^2v_2^2 - 12\omega_6c_s^2 + 18\omega_6\omega_3c_s^2 - 12\omega_3c_s^2 + 6\omega_3^2v_2^2 - 12\omega_3v_2^2 + 6\omega_3^2c_s^2 + 12\omega_6v_2^2 - 3\omega_6\omega_3^2c_s^2 - 6\omega_6\omega_3v_2^2) \frac{\delta_t^3\rho}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3v_3}{\partial x_2^2\partial x_3} \\
& + (12 + \omega_7\omega_4 - 6\omega_7 - 6\omega_4) \frac{\delta_t^3\rho v_3}{6\omega_7\omega_4} \frac{\partial^3v_3}{\partial t\partial x_3^2} + C_9 \frac{\delta_t^3v_1}{2\omega_3^2\delta_t\omega_7\omega_4^2} \frac{\partial^3\rho}{\partial x_1\partial x_3^2} + \\
& (18c_s^2\omega_7\omega_4 - 12\omega_4v_3^2 - 6\omega_7\omega_4v_3^2 - 3c_s^2\omega_7\omega_4^2 + 12\omega_7v_3^2 - 12c_s^2\omega_4 + 6\omega_4^2v_3^2 + \omega_7\omega_4^2v_3^2 + 6c_s^2\omega_4^2 - 12c_s^2\omega_7) \frac{\delta_t^3\rho}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3v_1}{\partial x_1\partial x_3^2} \\
& + (-6\omega_2^2\omega_4 + 6\omega_2^2 + 6\omega_4^2 + \omega_2^2\omega_4^2 - 6\omega_2\omega_4^2) \frac{\delta_t^3v_1\rho v_3}{6\omega_2^2\delta_t\omega_4^2} \frac{\partial^3v_3}{\partial x_1\partial x_3^2} + C_{10} \frac{\delta_t^3v_2}{2\omega_3^2\delta_t\omega_7\omega_4^2} \frac{\partial^3\rho}{\partial x_2\partial x_3^2} + \\
& (18c_s^2\omega_7\omega_4 - 12\omega_4v_3^2 - 6\omega_7\omega_4v_3^2 - 3c_s^2\omega_7\omega_4^2 + 12\omega_7v_3^2 - 12c_s^2\omega_4 + 6\omega_4^2v_3^2 + \omega_7\omega_4^2v_3^2 + 6c_s^2\omega_4^2 - 12c_s^2\omega_7) \frac{\delta_t^3\rho}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3v_2}{\partial x_2\partial x_3^2} \\
& + (\omega_3^2\omega_4^2 - 6\omega_3^2\omega_4 + 6\omega_4^2 + 6\omega_3^2 - 6\omega_3\omega_4^2) \frac{\delta_t^3v_2\rho v_3}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3v_3}{\partial x_2\partial x_3^2} + C_{11} \frac{\delta_t^3v_3}{6\delta_t\omega_7\omega_4^2} \frac{\partial^3\rho}{\partial x_3^2} + C_{12} \frac{\delta_t^3\rho}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3v_3}{\partial x_3^2} + \\
& (-2 - \omega_2^2 + 3\omega_2) \frac{\delta_t\delta_t^2\rho}{2\omega_3^2} \frac{\partial^4v_1}{\partial t^3\partial x_1} + (8\omega_5\omega_2^2 + 2\omega_2^2 - 2\omega_5\omega_2^2 - 4\omega_2^2 - 4\omega_5\omega_2 - \omega_5^2\omega_2 + 2\omega_5^2 - \omega_5^2\omega_2^2) \frac{\delta_t^2\delta_t v_1\rho}{2\omega_5^2\omega_2^2} \frac{\partial^4v_1}{\partial t^2\partial x_1^2} + \\
& C_{13} \frac{\delta_t^3\rho}{12\omega_5^2\omega_2^2} \frac{\partial^4v_1}{\partial t\partial x_1^3} + C_{14} \frac{\delta_t^4}{24\omega_5^2\omega_2^2\delta_t} \frac{\partial^4\rho}{\partial x_1^4} + C_{15} \frac{\delta_t^4v_1\rho}{12\omega_5^2\omega_2^2\delta_t} \frac{\partial^4v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3\omega_3) \frac{\delta_t\delta_t^2\rho}{2\omega_3^2} \frac{\partial^4v_2}{\partial t^3\partial x_2} + \\
& (12\omega_2\omega_3 + 12\omega_2^2 + 7\omega_2\omega_3^2 - 24\omega_2\omega_3^2 + 12\omega_3^2 + 13\omega_2^2\omega_3^2 - \omega_2^2\omega_3^3 - 6\omega_3^3 - 24\omega_2^2\omega_3) \frac{\delta_t^2\delta_t v_2\rho}{12\omega_2^2\omega_3^2} \frac{\partial^4v_1}{\partial t^2\partial x_1\partial x_2} + \\
& (12\omega_2\omega_3 - 6\omega_2^2 + 12\omega_2^2 - 24\omega_2\omega_3^2 + 12\omega_3^2 + 13\omega_2^2\omega_3^2 + 7\omega_2^2\omega_3 - \omega_2^2\omega_3^3 - 24\omega_2^2\omega_3) \frac{\delta_t^2\delta_t v_1\rho}{12\omega_2^2\omega_3^2} \frac{\partial^4v_2}{\partial t^2\partial x_1\partial x_2} + \\
& C_{16} \frac{\delta_t^3v_2v_1\rho}{6\omega_5\omega_2^2\omega_3^2} \frac{\partial^4v_1}{\partial t\partial x_1^2\partial x_2} + C_{17} \frac{\delta_t^3\rho}{12\omega_5^2\omega_2^2\omega_3} \frac{\partial^4v_2}{\partial t\partial x_1^2\partial x_2} + C_{18} \frac{\delta_t^4v_2v_1}{6\omega_5^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4\rho}{\partial x_1^3\partial x_2} + C_{19} \frac{\delta_t^4v_1\rho}{12\omega_5^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4v_1}{\partial x_1^3\partial x_2} + \\
& C_{20} \frac{\delta_t^4v_1\rho}{12\omega_5^2\omega_2^2\delta_t} \frac{\partial^4v_2}{\partial x_1^3\partial x_2} + (-4\omega_6\omega_3 - 2\omega_6\omega_3^2 + 8\omega_6\omega_3^2 - \omega_6^2\omega_3^2 - 4\omega_3^2 + 2\omega_6^2 + 2\omega_3^2 - \omega_6^2\omega_3) \frac{\delta_t^2\delta_t v_2\rho}{2\omega_6^2\omega_3^2} \frac{\partial^4v_2}{\partial t^2\partial x_2^2} + \\
& C_{21} \frac{\delta_t^3\rho}{12\omega_2\omega_6^2\omega_3^2} \frac{\partial^4v_1}{\partial t\partial x_1\partial x_2^2} + C_{22} \frac{\delta_t^3v_2v_1\rho}{6\omega_2^2\omega_6\omega_3^2} \frac{\partial^4v_2}{\partial t\partial x_1\partial x_2^2} + C_{23} \frac{\delta_t^4}{4\omega_2^2\omega_3^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4\rho}{\partial x_1^2\partial x_2^2} + C_{24} \frac{\delta_t^4v_1\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4v_1}{\partial x_1^2\partial x_2^2} + \\
& C_{25} \frac{\delta_t^4v_2\rho}{12\omega_2^2\omega_3^2\omega_6^2\delta_t} \frac{\partial^4v_2}{\partial x_1^2\partial x_2^2} + C_{26} \frac{\delta_t^3\rho}{12\omega_2^2\omega_6^2} \frac{\partial^4v_2}{\partial t\partial x_2^2} + C_{27} \frac{\delta_t^4v_2v_1}{6\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4\rho}{\partial x_1\partial x_2^2} + C_{28} \frac{\delta_t^4v_2\rho}{12\omega_2^2\omega_6^2\delta_t} \frac{\partial^4v_1}{\partial x_1\partial x_2^2} + C_{29} \frac{\delta_t^4v_1\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4v_2}{\partial x_1\partial x_2^2} \\
& + C_{30} \frac{\delta_t^4}{24\omega_6^2\omega_3^2\delta_t} \frac{\partial^4\rho}{\partial x_2^4} + C_{31} \frac{\delta_t^4v_2\rho}{12\omega_6^2\omega_3^2\delta_t} \frac{\partial^4v_2}{\partial x_2^4} + (-2 - \omega_4^2 + 3\omega_4) \frac{\delta_t\delta_t^2\rho}{2\omega_4^2} \frac{\partial^4v_3}{\partial t^3\partial x_3} + \\
& (-24\omega_2^2\omega_4 + 12\omega_2^2 - \omega_2^2\omega_4^3 - 6\omega_4^3 + 12\omega_4^2 + 13\omega_2^2\omega_4^2 - 24\omega_2\omega_4^2 + 7\omega_2\omega_4^3 + 12\omega_2\omega_4) \frac{\delta_t^2\delta_t\rho v_3}{12\omega_2^2\omega_4^2} \frac{\partial^4v_1}{\partial t^2\partial x_1\partial x_3} + \\
& (-24\omega_2^2\omega_4 - 6\omega_2^2 - \omega_2^2\omega_4^2 + 12\omega_2^2 + 7\omega_2^2\omega_4 + 12\omega_4^2 + 13\omega_2^2\omega_4^2 - 24\omega_2\omega_4^2 + 12\omega_2\omega_4) \frac{\delta_t^2\delta_t v_1\rho}{12\omega_2^2\omega_4^2} \frac{\partial^4v_3}{\partial t^2\partial x_1\partial x_3} + \\
& C_{32} \frac{\delta_t^3v_1\rho v_3}{6\omega_5\omega_3^2\omega_4^2} \frac{\partial^4v_1}{\partial t\partial x_1^2\partial x_3} + C_{33} \frac{\delta_t^3\rho}{12\omega_5^2\omega_2^2\omega_4} \frac{\partial^4v_3}{\partial t\partial x_1^2\partial x_3} + C_{34} \frac{\delta_t^4v_1v_3}{6\omega_5^2\omega_2^2\delta_t\omega_4^2} \frac{\partial^4\rho}{\partial x_1^3\partial x_3} + C_{35} \frac{\delta_t^4\rho v_3}{12\omega_5^2\omega_2^2\delta_t\omega_4^2} \frac{\partial^4v_1}{\partial x_1^3\partial x_3} + \\
& C_{36} \frac{\delta_t^4v_1\rho}{12\omega_5^2\omega_2^2\delta_t} \frac{\partial^4v_3}{\partial x_1^3\partial x_3} + \\
& (-\omega_3^2\omega_4^3 + 13\omega_3^2\omega_4^2 - 24\omega_3^2\omega_4 - 6\omega_4^3 + 12\omega_4^2 + 12\omega_3^2 + 12\omega_3\omega_4 - 24\omega_3\omega_4^2 + 7\omega_3\omega_4^3) \frac{\delta_t^2\delta_t\rho v_3}{12\omega_3^2\omega_4^2} \frac{\partial^4v_2}{\partial t^2\partial x_2\partial x_3} + \\
& (7\omega_3^2\omega_4 + 13\omega_3^2\omega_4^2 - 24\omega_3^2\omega_4 + 12\omega_4^2 - \omega_3^2\omega_4^2 + 12\omega_3^2 + 12\omega_3\omega_4 - 6\omega_3^3 - 24\omega_3\omega_4) \frac{\delta_t^2\delta_t v_2\rho}{12\omega_3^2\omega_4^2} \frac{\partial^4v_3}{\partial t^2\partial x_2\partial x_3} + \\
& C_{37} \frac{\delta_t^3v_2\rho v_3}{6\omega_2\omega_3^2\omega_4^2} \frac{\partial^4v_1}{\partial t\partial x_1\partial x_2\partial x_3} + C_{38} \frac{\delta_t^3v_1\rho v_3}{6\omega_2^2\omega_3\omega_4^2} \frac{\partial^4v_2}{\partial t\partial x_1\partial x_2\partial x_3} + C_{39} \frac{\delta_t^3v_2v_1\rho}{6\omega_2^2\omega_3^2\omega_4} \frac{\partial^4v_3}{\partial t\partial x_1\partial x_2\partial x_3} + C_{40} \frac{\delta_t^4v_2v_3}{\omega_2^2\omega_3^2\omega_4^2\delta_t\omega_4^2} \frac{\partial^4\rho}{\partial x_1^2\partial x_2\partial x_3} + \\
& C_{41} \frac{\delta_t^4v_2v_1\rho v_3}{6\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_1}{\partial x_1^2\partial x_2\partial x_3} + C_{42} \frac{\delta_t^4\rho v_3}{12\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_2}{\partial x_1^2\partial x_2\partial x_3} + C_{43} \frac{\delta_t^4v_2\rho}{12\omega_2^2\omega_3^2\omega_4^2\delta_t} \frac{\partial^4v_3}{\partial x_1^2\partial x_2\partial x_3} + C_{44} \frac{\delta_t^3\rho v_3}{6\omega_6\omega_3^2\omega_4^2} \frac{\partial^4v_2}{\partial t\partial x_2^2\partial x_3} + \\
& C_{45} \frac{\delta_t^3\rho}{12\omega_2^2\omega_3^2\omega_4} \frac{\partial^4v_3}{\partial t\partial x_2^2\partial x_3} + C_{46} \frac{\delta_t^4v_1v_3}{\omega_2^2\omega_6^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4\rho}{\partial x_1\partial x_2^2\partial x_3} + C_{47} \frac{\delta_t^4\rho v_3}{12\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_1}{\partial x_1\partial x_2^2\partial x_3} + C_{48} \frac{\delta_t^4v_2v_1\rho v_3}{6\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_2}{\partial x_1\partial x_2^2\partial x_3} + \\
& C_{49} \frac{\delta_t^4v_1\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4v_3}{\partial x_1\partial x_2^2\partial x_3} + C_{50} \frac{\delta_t^4v_2v_3}{6\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4\rho}{\partial x_2^2\partial x_3} + C_{51} \frac{\delta_t^4\rho v_3}{12\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_2}{\partial x_2^2\partial x_3} + C_{52} \frac{\delta_t^4v_2\rho}{12\omega_2^2\omega_3^2\delta_t} \frac{\partial^4v_3}{\partial x_2^2\partial x_3} + \\
& (-\omega_7^2\omega_4 + 2\omega_7^2 - \omega_7^2\omega_4^2 + 2\omega_4^3 - 4\omega_4^2 - 2\omega_7\omega_4^2 + 8\omega_7\omega_4 - 4\omega_7\omega_4) \frac{\delta_t^2\delta_t\rho v_3}{2\omega_7^2\omega_4^2} \frac{\partial^4v_3}{\partial t^2\partial x_2^2} + C_{53} \frac{\delta_t^3\rho}{12\omega_2\omega_7^2\omega_4^2} \frac{\partial^4v_1}{\partial t\partial x_1\partial x_2^2} + \\
& C_{54} \frac{\delta_t^3v_1\rho v_3}{6\omega_2^2\omega_7\omega_4^2} \frac{\partial^4v_3}{\partial t\partial x_1\partial x_2^2} + C_{55} \frac{\delta_t^4}{4\omega_2^2\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4\rho}{\partial x_1^2\partial x_2^2} + C_{56} \frac{\delta_t^4v_1\rho}{12\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_1}{\partial x_1^2\partial x_2^2} + C_{57} \frac{\delta_t^4\rho v_3}{12\omega_5^2\omega_2^2\delta_t\omega_4^2} \frac{\partial^4v_3}{\partial x_1^2\partial x_2^2} + \\
& C_{58} \frac{\delta_t^3\rho}{12\omega_3\omega_7^2\omega_4^2} \frac{\partial^4v_2}{\partial t\partial x_2\partial x_2^2} + C_{59} \frac{\delta_t^3v_2\rho v_3}{6\omega_3^2\omega_7\omega_4^2} \frac{\partial^4v_3}{\partial t\partial x_2\partial x_2^2} + C_{60} \frac{\delta_t^4v_2v_1}{\omega_2^2\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4\rho}{\partial x_1\partial x_2\partial x_2^2} + C_{61} \frac{\delta_t^4v_2\rho}{12\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_1}{\partial x_1\partial x_2\partial x_2^2} + \\
& C_{62} \frac{\delta_t^4v_1\rho}{12\omega_2^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_2}{\partial x_1\partial x_2\partial x_2^2} + C_{63} \frac{\delta_t^4v_2v_1\rho v_3}{6\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_3}{\partial x_1\partial x_2\partial x_2^2} + C_{64} \frac{\delta_t^4}{4\omega_2^2\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4\rho}{\partial x_2^2\partial x_2^2} + C_{65} \frac{\delta_t^4v_2\rho}{12\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_2}{\partial x_2^2\partial x_2^2} + \\
& C_{66} \frac{\delta_t^4\rho v_3}{12\omega_6^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^4v_3}{\partial x_2^2\partial x_2^2} + C_{67} \frac{\delta_t^3\rho}{12\omega_7^2\omega_4^2} \frac{\partial^4v_3}{\partial t\partial x_3^2} + C_{68} \frac{\delta_t^4v_1v_3}{6\omega_2^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4\rho}{\partial x_1\partial x_3^2} + C_{69} \frac{\delta_t^4\rho v_3}{12\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_1}{\partial x_1\partial x_3^2} + C_{70} \frac{\delta_t^4v_1\rho}{12\omega_2^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_3}{\partial x_1\partial x_3^2} \\
& + C_{71} \frac{\delta_t^4v_2v_3}{6\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4\rho}{\partial x_2\partial x_3^2} + C_{72} \frac{\delta_t^4\rho v_3}{12\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_2}{\partial x_2\partial x_3^2} + C_{73} \frac{\delta_t^4v_2\rho}{12\omega_3^2\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_3}{\partial x_2\partial x_3^2} + C_{74} \frac{\delta_t^4}{24\delta_t\omega_7^2\omega_4^2} \frac{\partial^4\rho}{\partial x_3^4} + C_{75} \frac{\delta_t^4\rho v_3}{12\delta_t\omega_7^2\omega_4^2} \frac{\partial^4v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -3\omega_5\omega_2^2c_s^2 + \omega_5\omega_2^2 - 6\omega_2c_s^2 + 3\omega_5\omega_2v_1^2 + 3\omega_2^2v_1^2 - 3\omega_2^2 + 6\omega_2 - 3\omega_5\omega_2 - 6\omega_2v_1^2 - \omega_5\omega_2^2v_1^2 - 12\omega_5c_s^2 + 3\omega_2^2c_s^2 + 15\omega_5\omega_2c_s^2 \\
C_2 &= -3\omega_5\omega_2^2c_s^2 + 2\omega_5\omega_2^2 - 12\omega_2c_s^2 - 12\omega_5v_1^2 + 18\omega_5\omega_2v_1^2 + 6\omega_2^2v_1^2 - 6\omega_2^2 + 12\omega_2 - 6\omega_5\omega_2 - 12\omega_2v_1^2 - 5\omega_5\omega_2^2v_1^2 - 12\omega_5c_s^2 + 6\omega_2^2c_s^2 + 18\omega_5\omega_2c_s^2 \\
C_3 &= \omega_5\omega_2^2\omega_3c_s^2 + 2\omega_5\omega_2\omega_3v_1^2 + \omega_5\omega_2^2\omega_3^2v_1^2 - 2\omega_2\omega_3^2v_1^2 + 4\omega_5\omega_2\omega_3^2c_s^2 + \omega_2^2\omega_3^2c_s^2 - 2\omega_5\omega_3^2c_s^2 + 4\omega_5\omega_3^2v_1^2 + 2\omega_5\omega_2^2v_1^2 - 3\omega_5\omega_2^2\omega_3v_1^2 - \\
& 2\omega_5\omega_2\omega_3c_s^2 - 2\omega_2\omega_3^2c_s^2 - \omega_5\omega_2^2\omega_3^2c_s^2 + \omega_2^2\omega_3^2v_1^2 - 4\omega_5\omega_2\omega_3^2v_1^2 \\
C_4 &= -2\omega_2^2\omega_3v_2^2 + \omega_2^2\omega_6\omega_3^2v_2^2 + 2\omega_6\omega_3^2v_2^2 + 4\omega_2^2\omega_6\omega_3c_s^2 + \omega_2^2\omega_3^2c_s^2 + \omega_2\omega_6\omega_3^2c_s^2 + 4\omega_2^2\omega_6v_2^2 + 2\omega_2\omega_6\omega_3v_2^2 - 2\omega_2^2\omega_6c_s^2 - 3\omega_2\omega_6\omega_3v_2^2 - \\
& 2\omega_2\omega_6\omega_3c_s^2 - 2\omega_2^2\omega_3c_s^2 - \omega_2^2\omega_6\omega_3^2c_s^2 - 4\omega_2^2\omega_6\omega_3v_2^2 + \omega_2^2\omega_3^2v_2^2 \\
C_5 &= -\omega_6\omega_3^2v_2^2 - 12\omega_6c_s^2 - 3\omega_6\omega_3 + 15\omega_6\omega_3c_s^2 - 6\omega_3c_s^2 + 3\omega_3^2v_2^2 + \omega_6\omega_3^2 - 6\omega_3v_2^2 - 3\omega_3^2 + 6\omega_3 + 3\omega_3^2c_s^2 - 3\omega_6\omega_3^2c_s^2 + 3\omega_6\omega_3v_2^2 \\
C_6 &= -5\omega_6\omega_3^2v_2^2 - 12\omega_6c_s^2 - 6\omega_6\omega_3 + 18\omega_6\omega_3c_s^2 - 12\omega_3c_s^2 + 6\omega_3^2v_2^2 + 2\omega_6\omega_3^2 - 12\omega_3v_2^2 - 6\omega_3^2 + 12\omega_3 + 6\omega_3^2c_s^2 - 12\omega_6v_2^2 - 3\omega_6\omega_3^2c_s^2 + 18\omega_6\omega_3v_2^2 \\
C_7 &= -2\omega_2v_1^2\omega_4^2 + \omega_5\omega_2^2v_1^2\omega_4^2 - 2\omega_5\omega_2c_s^2\omega_4^2 - 2\omega_5c_s^2\omega_4^2 + \omega_2^2c_s^2\omega_4^2 + 4\omega_5\omega_2c_s^2\omega_4^2 - 3\omega_5\omega_2^2v_1^2\omega_4 - \omega_5\omega_2^2c_s^2\omega_4^2 - 2\omega_2c_s^2\omega_4^2 + 2\omega_5\omega_2v_1^2\omega_4 + \\
& 4\omega_5v_1^2\omega_4^2 + 2\omega_5\omega_2^2v_1^2 - 4\omega_5\omega_2v_1^2\omega_4^2 + \omega_2^2v_1^2\omega_4^2 + \omega_5\omega_2^2c_s^2\omega_4 \\
C_8 &= 2\omega_6\omega_3^2v_2^2 + 4\omega_6v_2^2\omega_4^2 - 2\omega_3c_s^2\omega_4^2 - \omega_6\omega_3^2c_s^2\omega_4^2 + 2\omega_6\omega_3v_2^2\omega_4 + \omega_6\omega_3^2c_s^2\omega_4 - 4\omega_6\omega_3v_2^2\omega_4^2 + \omega_3^2v_2^2\omega_4^2 + \omega_6\omega_3^2v_2^2\omega_4^2 - 2\omega_6\omega_3c_s^2\omega_4 - \\
& 2\omega_3v_2^2\omega_4^2 - 2\omega_6c_s^2\omega_4^2 + \omega_3^2c_s^2\omega_4^2 - 3\omega_6\omega_3^2v_2^2\omega_4 + 4\omega_6\omega_3c_s^2\omega_4^2 \\
C_9 &= 4\omega_2^2\omega_7\omega_3^2 + 4\omega_3^2c_s^2\omega_7\omega_4 - 2\omega_3^2c_s^2\omega_4 - 4\omega_2^2\omega_7\omega_4v_3^2 + \omega_2^2\omega_4^2v_3^2 - 3\omega_2\omega_7\omega_4^2v_3^2 + \omega_2^2c_s^2\omega_4^2 - \omega_2^2c_s^2\omega_7\omega_4^2 - 2\omega_2^2c_s^2\omega_7 - 2\omega_2c_s^2\omega_7\omega_4 - 2\omega_2^2\omega_4v_3^2 + \\
& 2\omega_2\omega_7\omega_4v_3^2 + 2\omega_7\omega_4^2v_3^2 + \omega_2^2\omega_7\omega_4^2v_3^2 + \omega_2c_s^2\omega_7\omega_4^2 \\
C_{10} &= -\omega_3^2c_s^2\omega_7\omega_4^2 - 2\omega_3^2\omega_4v_3^2 - 3\omega_3\omega_7\omega_4^2v_3^2 - 4\omega_3^2\omega_7\omega_4v_3^2 + 4\omega_3^2c_s^2\omega_7\omega_4 + \omega_3c_s^2\omega_7\omega_4^2 - 2\omega_3^2c_s^2\omega_4 + \omega_3^2\omega_7\omega_4^2v_3^2 + 4\omega_3^2\omega_7v_3^2 - 2\omega_3^2c_s^2\omega_7 + \\
& 2\omega_7\omega_4^2v_3^2 + 2\omega_3\omega_7\omega_4v_3^2 + \omega_3^2c_s^2\omega_4^2 - 2\omega_3c_s^2\omega_7\omega_4 + \omega_3^2\omega_4^2v_3^2 \\
C_{11} &= 15c_s^2\omega_7\omega_4 - 6\omega_4v_3^2 + 3\omega_7\omega_4v_3^2 - 3c_s^2\omega_7\omega_4^2 - 3\omega_4^2 - 6c_s^2\omega_4 + \omega_7\omega_4^2 + 3\omega_4^2v_3^2 - 3\omega_7\omega_4 - \omega_7\omega_4^2v_3^2 + 3c_s^2\omega_4^2 + 6\omega_4 - 12c_s^2\omega_7 \\
C_{12} &= 18c_s^2\omega_7\omega_4 - 12\omega_4v_3^2 + 18\omega_7\omega_4v_3^2 - 3c_s^2\omega_7\omega_4^2 - 6\omega_4^2 - 12\omega_7v_3^2 - 12c_s^2\omega_4 + 2\omega_7\omega_4^2 + 6\omega_4^2v_3^2 - 6\omega_7\omega_4 - 5\omega_7\omega_4^2v_3^2 + 6c_s^2\omega_4^2 + 12\omega_4 - 12c_s^2\omega_7 \\
C_{13} &= -36\omega_5\omega_2^2c_s^2 + 36\omega_5\omega_2^2 + 27\omega_5^2\omega_2^2v_1^2 + 6\omega_2^3 + 48\omega_5\omega_2v_1^2 + 12\omega_2^2v_1^2 - 48\omega_5^2\omega_2c_s^2 - 9\omega_5\omega_2^3 + 24\omega_5^2c_s^2 - 12\omega_2^2 - 3\omega_2^2\omega_2^3v_1^2 + 9\omega_5\omega_2^3c_s^2 - 24\omega_5\omega_2 - \\
& 6\omega_2^3v_1^2 + 12\omega_5^2\omega_2 - 2\omega_5^2\omega_2^2c_s^2 + 15\omega_5\omega_2^2v_1^2 - 6\omega_2^3c_s^2 - 60\omega_5\omega_2^2v_1^2 + \omega_5^2\omega_2^2 + 25\omega_5^2\omega_2^2c_s^2 + 12\omega_2^2c_s^2 + 24\omega_5\omega_2c_s^2 - 11\omega_5^2\omega_2^2 - 42\omega_5^2\omega_2v_1^2 + 12\omega_5^2v_1^2 \\
C_{14} &= 24\omega_5\omega_2^2c_s^2 - 24\omega_5\omega_2c_s^2v_1^2 + 24\omega_5^2\omega_2^2v_1^2 - 24\omega_2^2c_s^2v_1^2 + 72\omega_5\omega_2^2v_1^4 + 24\omega_5^2\omega_2^2c_s^4 + 48\omega_5\omega_2v_1^2 + 24\omega_2^2v_1^2 + 12\omega_5^2\omega_2c_s^2 + 24\omega_5\omega_2c_s^4 + \\
& 24\omega_5^2\omega_2v_1^4 - 3\omega_5^2\omega_2^3c_s^4 - 18\omega_5\omega_2^3v_1^4 - 3\omega_5^2\omega_2^3v_1^2 - 6\omega_5\omega_2^3c_s^2 - 72\omega_5^2\omega_2^2c_s^2v_1^2 - 12\omega_5\omega_2^3c_s^2v_1^2 - 12\omega_2^3v_1^2 + 3\omega_5^2\omega_2^3v_1^4 + 6\omega_5\omega_2^3c_s^4 + 156\omega_5^2\omega_2c_s^2v_1^2 + \\
& \omega_5^2\omega_2^2c_s^2 + 18\omega_5\omega_2^3v_1^2 - 96\omega_5^2c_s^2v_1^2 + 12\omega_2^3v_1^4 + 12\omega_2^3c_s^2v_1^2 + 48\omega_5\omega_2^3c_s^2v_1^2 - 72\omega_5\omega_2^2v_1^2 - 8\omega_5^2\omega_2^2c_s^2 - 24\omega_5\omega_2^2c_s^4 - 24\omega_5^2\omega_2^2v_1^4 + 24\omega_5^2c_s^4 - \\
& 24\omega_5\omega_2c_s^2 + 6\omega_5^2\omega_2^3c_s^2v_1^2 - 24\omega_5^2\omega_2v_1^2 - 48\omega_5\omega_2v_1^4 - 24\omega_2^3v_1^4 - 48\omega_5^2\omega_2c_s^4 \\
C_{15} &= 24\omega_5\omega_2^2c_s^2 - 24\omega_5\omega_2^2 - 16\omega_5^2\omega_2^2v_1^2 - 6\omega_2^3 - 12\omega_5\omega_2v_1^2 - 12\omega_2^2v_1^2 + 42\omega_5^2\omega_2c_s^2 + 6\omega_5\omega_2^3 - 24\omega_5^2c_s^2 + 12\omega_2^2 + 2\omega_5^2\omega_2^3v_1^2 - 6\omega_5\omega_2^3c_s^2 + \\
& 12\omega_5\omega_2 + 6\omega_2^3v_1^2 - 6\omega_5^2\omega_2 + \omega_5^2\omega_2^2c_s^2 - 6\omega_5\omega_2^3v_1^2 + 6\omega_2^3c_s^2 + 24\omega_5\omega_2^2v_1^2 - \omega_5^2\omega_2^2 - 20\omega_5^2\omega_2^2c_s^2 - 12\omega_2^2c_s^2 - 12\omega_5\omega_2c_s^2 + 8\omega_5^2\omega_2^2 + 24\omega_5^2\omega_2v_1^2 - 12\omega_5^2v_1^2 \\
C_{16} &= -6\omega_5\omega_2^3\omega_3 + \omega_5\omega_2^3\omega_3^2 - 7\omega_5\omega_2^3\omega_3^2 - 6\omega_5\omega_2^3 + 12\omega_5\omega_2^3\omega_3 - 10\omega_5\omega_2^2\omega_3^2 + 12\omega_5\omega_2^2\omega_3^2 - 12\omega_5\omega_3^2 - 12\omega_5\omega_2\omega_3^2 + 12\omega_2^2\omega_3^2 + 24\omega_5\omega_2\omega_3^2 - \\
& 6\omega_2^2\omega_3^2 - 6\omega_2^2\omega_3^2 + 3\omega_2^3\omega_3^2 \\
C_{17} &= 12\omega_5\omega_2^2c_s^2 + 6\omega_5^2\omega_2^2v_1^2 - 30\omega_5\omega_2^2\omega_3c_s^2 + 12\omega_5\omega_2\omega_3v_1^2 + 12\omega_2^2\omega_3v_1^2 + 12\omega_5^2\omega_2c_s^2 - 2\omega_2^2\omega_2^3\omega_3c_s^2 - 30\omega_5^2\omega_2\omega_3c_s^2 - 10\omega_5^2\omega_2^2\omega_3v_1^2 - \omega_5^2\omega_2^3v_1^2 - \\
& 6\omega_5\omega_2^3c_s^2 + 9\omega_5\omega_2^3\omega_3v_1^2 - 6\omega_2^3\omega_3c_s^2 + 12\omega_5^2\omega_3c_s^2 + 36\omega_5^2\omega_2\omega_3v_1^2 + 22\omega_5^2\omega_2^2\omega_3c_s^2 + 3\omega_5^2\omega_2^3c_s^2 - 6\omega_5\omega_2^3v_1^2 + 9\omega_5\omega_2^3\omega_3c_s^2 - 6\omega_2^3\omega_3v_1^2 - 24\omega_5^2\omega_3v_1^2 + \\
& 12\omega_5\omega_2^2v_1^2 - 18\omega_5^2\omega_2^2c_s^2 - 30\omega_5\omega_2^2\omega_3v_1^2 + 12\omega_2^2\omega_3c_s^2 + 12\omega_5\omega_2\omega_3c_s^2 - 12\omega_5^2\omega_2v_1^2 + \omega_5^2\omega_2^3\omega_3v_1^2 \\
C_{18} &= 6\omega_5\omega_2^3\omega_3^2 + 24\omega_5^2\omega_2^3v_1^2 + 6\omega_2^3\omega_3^2v_1^2 - 12\omega_5\omega_2^3\omega_3^2c_s^2 + 6\omega_5^2\omega_2^3\omega_3^2v_1^2 - 3\omega_5\omega_2^3\omega_3^2 - 12\omega_5\omega_2^3\omega_3^2v_1^2 - 48\omega_5^2\omega_2^3\omega_3^2c_s^2 - 30\omega_5^2\omega_2\omega_3^2v_1^2 + \\
& 6\omega_5^2\omega_2^3\omega_3c_s^2 + 6\omega_5\omega_2^3\omega_3^2c_s^2 + 6\omega_5^2\omega_2^3\omega_3v_1^2 + 6\omega_5^2\omega_2^3v_1^2 - 21\omega_5\omega_2^3\omega_3^2 - 24\omega_5\omega_2\omega_3^2c_s^2 + 12\omega_5^2\omega_2\omega_3^2v_1^2 - 12\omega_2^3\omega_3^2c_s^2 + 42\omega_5\omega_2^3\omega_3^2v_1^2 + 42\omega_5^2\omega_2^3\omega_3^2c_s^2 + \\
& 6\omega_5\omega_2^3\omega_3^2 - 6\omega_5^2\omega_2\omega_3^2 + 6\omega_2^3\omega_3^2c_s^2 + 6\omega_5\omega_2^3\omega_3^2v_1^2 - 12\omega_5^2\omega_2\omega_3c_s^2 + 7\omega_5^2\omega_2^3\omega_3^2 - 24\omega_5^2\omega_2\omega_3^2c_s^2 - 12\omega_2^3\omega_3^2v_1^2 - 24\omega_5\omega_2\omega_3^2v_1^2 - 12\omega_2^2\omega_2^3\omega_3^2v_1^2 + \\
& 42\omega_5\omega_2^3\omega_3^2c_s^2 + 12\omega_5\omega_2\omega_3^2 + 6\omega_2^3\omega_3^2 - 3\omega_2^2\omega_2^3\omega_3^2 - \omega_5^2\omega_2^3\omega_3^2 - 36\omega_5^2\omega_3^2c_s^2 + 6\omega_2^3\omega_3^2c_s^2 - 12\omega_5^2\omega_2^3\omega_3^2c_s^2 - 12\omega_5\omega_2^3\omega_3^2v_1^2 - 3\omega_2^3\omega_3^2 + \omega_5^2\omega_2^3\omega_3^2 + \\
& 6\omega_5^2\omega_2^3\omega_3^2v_1^2 - 12\omega_5\omega_2^2\omega_3^2c_s^2 + 78\omega_5^2\omega_2\omega_3^2c_s^2 - 12\omega_5^2\omega_2^3\omega_3v_1^2 \\
C_{19} &= 3\omega_5\omega_2^3\omega_3^2 + 24\omega_5^2\omega_2^3v_1^2 + 6\omega_2^3\omega_3^2v_1^2 - 12\omega_5\omega_2^3\omega_3^2c_s^2 - 6\omega_5\omega_2^3\omega_3^2 - 24\omega_5\omega_2^3\omega_3^2v_1^2 - 32\omega_5^2\omega_2^3\omega_3^2c_s^2 - 30\omega_5^2\omega_2\omega_3^2v_1^2 + 6\omega_5^2\omega_2^3\omega_3c_s^2 + \\
& 12\omega_5\omega_2^3\omega_3^2c_s^2 + 3\omega_2^3\omega_2^3\omega_3^2v_1^2 + 12\omega_2^2\omega_2^3v_1^2 - 6\omega_5\omega_2^3\omega_3^2 - 12\omega_5\omega_2\omega_3^2c_s^2 - 12\omega_2^3\omega_3^2c_s^2 + 36\omega_5\omega_2^3\omega_3^2v_1^2 + 48\omega_5^2\omega_2^3\omega_3^2c_s^2 + 12\omega_5\omega_2^3\omega_3^2 + 4\omega_2^2\omega_2^3\omega_3^2c_s^2 + \\
& 12\omega_5\omega_2^3\omega_3^2v_1^2 - 12\omega_2^2\omega_2^3\omega_3c_s^2 + 3\omega_2^2\omega_2^3\omega_3^2 - 24\omega_5^2\omega_2\omega_3^2c_s^2 - 12\omega_2^2\omega_3^2v_1^2 - 12\omega_5\omega_2\omega_3^2v_1^2 + 12\omega_5^2\omega_2^3\omega_3^2v_1^2 + 36\omega_5\omega_2^3\omega_3^2c_s^2 - 6\omega_5^2\omega_2^2\omega_3^2 - \omega_5^2\omega_2^3\omega_3^2 - \\
& 12\omega_2^2\omega_3^2c_s^2 + 6\omega_2^3\omega_3^2c_s^2 - 12\omega_5^2\omega_2^3\omega_3^2c_s^2 - 12\omega_5\omega_2^3\omega_3^2v_1^2 + 2\omega_2^2\omega_2^3\omega_3^2 - 24\omega_5\omega_2^3\omega_3^2c_s^2 + 36\omega_5^2\omega_2\omega_3^2c_s^2 - 18\omega_5^2\omega_2^3\omega_3v_1^2 \\
C_{20} &= 48\omega_5\omega_2^2c_s^2 - 36\omega_5\omega_2^2 - 8\omega_5^2\omega_2^2v_1^2 - 6\omega_2^3 - 36\omega_5\omega_2v_1^2 - 12\omega_2^2v_1^2 + 90\omega_5^2\omega_2c_s^2 + 9\omega_5\omega_2^3 - 48\omega_5^2c_s^2 + 12\omega_2^2 + \omega_5^2\omega_2^3v_1^2 - 12\omega_5\omega_2^3c_s^2 + \\
& 24\omega_5\omega_2 + 6\omega_2^3v_1^2 - 12\omega_5^2\omega_2 + 4\omega_5^2\omega_2^2c_s^2 - 12\omega_5\omega_2^3v_1^2 + 6\omega_2^3c_s^2 + 48\omega_5\omega_2^2v_1^2 - \omega_5^2\omega_2^2 - 44\omega_5^2\omega_2^2c_s^2 - 12\omega_2^2c_s^2 - 36\omega_5\omega_2c_s^2 + 11\omega_5^2\omega_2^2 + 12\omega_5^2v_1^2 \\
C_{21} &= \omega_2\omega_2^3\omega_3^2v_2^2 + 12\omega_6\omega_3^2v_2^2 - 18\omega_6^2\omega_3^2c_s^2 + 9\omega_2\omega_6\omega_3^2c_s^2 - 12\omega_6^2\omega_3v_2^2 + 12\omega_2\omega_3^2v_2^2 + 3\omega_6^2\omega_3^2c_s^2 - 30\omega_2\omega_6\omega_3^2c_s^2 - 10\omega_2\omega_6^2\omega_3^2v_2^2 - 6\omega_6\omega_3^2v_2^2 - \\
& 24\omega_2\omega_6^2v_2^2 - 30\omega_2\omega_6^2\omega_3c_s^2 - 6\omega_2\omega_3^2v_2^2 + 12\omega_2\omega_6\omega_3v_2^2 + 22\omega_2\omega_6^2\omega_3^2c_s^2 - 6\omega_6\omega_3^2c_s^2 - \omega_6^2\omega_3^2v_2^2 - 30\omega_2\omega_6\omega_3^2v_2^2 + 12\omega_2\omega_6\omega_3c_s^2 - 6\omega_2\omega_3^2c_s^2 + \\
& 36\omega_2\omega_6^2\omega_3v_2^2 + 12\omega_2\omega_6^2c_s^2 + 6\omega_6^2\omega_3^2v_2^2 + 9\omega_2\omega_6\omega_3^2v_2^2 - 2\omega_2\omega_6^2\omega_3^2c_s^2 + 12\omega_6\omega_3^2c_s^2 + 12\omega_2\omega_3^2c_s^2 + 12\omega_6^2\omega_3c_s^2
\end{aligned}$$

$$C_{22} = 12\omega_2\omega_6\omega_3^3 - 6\omega_2\omega_6\omega_3^2 + 24\omega_2^3\omega_6\omega_3 - 6\omega_6\omega_3^3 - 10\omega_3^2\omega_6\omega_3^2 + \omega_3^3\omega_6\omega_3^3 - 12\omega_2^3\omega_6 - 12\omega_2^2\omega_6\omega_3 + 12\omega_2^2\omega_3^2 - 6\omega_2^2\omega_3^3 - 7\omega_2^2\omega_6\omega_3^3 - 6\omega_2^3\omega_3^2 + 3\omega_2^3\omega_3^3 + 12\omega_2^2\omega_6\omega_3^2$$

$$C_{23} = -38\omega_2^3\omega_6^3\omega_3^2v_1^2 + 2\omega_5\omega_3^2\omega_6^2\omega_3^2c_s^2v_2^2 - 2\omega_5\omega_2^2\omega_6^2\omega_3^3c_s^4 - 8\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 + 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^4 - 36\omega_5^2\omega_2^2\omega_6^2\omega_3^2v_1^2 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 - 3\omega_5^2\omega_2^3\omega_6^3\omega_3^2v_1^2 - 2\omega_5\omega_2^3\omega_6^3\omega_3^2c_s^2v_1^2 + 4\omega_5^2\omega_2^2\omega_6^3\omega_3^2c_s^2v_1^2 + 20\omega_5^2\omega_2\omega_6^2\omega_3^2v_1^2 - 4\omega_5^2\omega_2^3\omega_6\omega_3^2c_s^2v_1^2 + 2\omega_5^2\omega_6^3\omega_3^2v_1^2 + 4\omega_2^2\omega_5^2\omega_6^3\omega_3^2c_s^4 + 10\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^2v_2^2 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 + 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2v_1^2 - 2\omega_5\omega_2^3\omega_6^2\omega_3^2c_s^4 + \omega_5^2\omega_2^3\omega_6\omega_3^2c_s^2v_2^2 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 + 4\omega_5\omega_2^2\omega_6^2\omega_3^2c_s^4 - 3\omega_5^2\omega_2^3\omega_6\omega_3^2c_s^2v_1^2 - \omega_5^2\omega_2^3\omega_6^3\omega_3^2c_s^4 + 20\omega_5^2\omega_6^2\omega_3^2v_2^2 + 10\omega_5^2\omega_2\omega_6^3\omega_3^2v_1^2 + 20\omega_5^2\omega_2^2\omega_6^2\omega_3^2v_1^2 - 4\omega_5\omega_2\omega_6^2\omega_3^2c_s^2v_2^2 - 12\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^4 - 4\omega_5^2\omega_2^3\omega_6^2\omega_3^2c_s^2v_2^2 + \omega_5\omega_2^3\omega_6^2\omega_3^2c_s^4 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 + 10\omega_5\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2v_1^2 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 - 8\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 + 2\omega_5^2\omega_2^3\omega_6^2\omega_3^2v_1^2 - 2\omega_5\omega_2^3\omega_6^2\omega_3^2c_s^2v_1^2 - 3\omega_5^2\omega_2^3\omega_6^2\omega_3^2v_1^2 - 8\omega_5^2\omega_2^3\omega_6^2\omega_3^2c_s^2v_1^2 + 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^4 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2v_1^2 + 2\omega_5^2\omega_2\omega_6^3\omega_3^2c_s^2v_1^2 - 4\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^2v_2^2 + 2\omega_2^2\omega_5^2\omega_6^3\omega_3^2c_s^2v_1^2 - 38\omega_5^2\omega_2\omega_6^2\omega_3^2v_2^2 - 8\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^2v_1^2 - 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 + \omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^4 - 4\omega_5^2\omega_2^2\omega_6\omega_3^2v_1^2 + 12\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 - 2\omega_5^2\omega_2\omega_6^3\omega_3^2c_s^4 + 20\omega_5^2\omega_2^2\omega_6^3\omega_3^2v_1^2 + \omega_5\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 + 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 + 2\omega_5\omega_2^3\omega_6^2\omega_3^2v_1^2 + 4\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^4 - 3\omega_5\omega_2^3\omega_6^2\omega_3^2c_s^2v_2^2 + 10\omega_5^2\omega_2^3\omega_6^2\omega_3^2c_s^2v_1^2 + 12\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 - 2\omega_5^2\omega_2^3\omega_6\omega_3^2c_s^4 - 4\omega_5^2\omega_2^3\omega_6^2\omega_3^2v_1^2 + 4\omega_5\omega_2^2\omega_6^2\omega_3^2c_s^2v_1^2 + 10\omega_5\omega_2^2\omega_6^2\omega_3^2v_2^2 + 2\omega_5^2\omega_2^3\omega_6^2\omega_3^2c_s^2v_1^2 + \omega_5^2\omega_2^3\omega_6^2\omega_3^2c_s^2v_1^2 + 20\omega_5^2\omega_2^2\omega_6^2\omega_3^2v_2^2 + \omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 - 4\omega_5\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 + 20\omega_5^2\omega_2\omega_6^2\omega_3^2v_1^2 - 3\omega_5^2\omega_2\omega_6^2\omega_3^2v_1^2 + 10\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^2v_1^2 - 4\omega_2^2\omega_5^2\omega_6^3\omega_3^2v_1^2 - 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^4 - 4\omega_5^2\omega_2^2\omega_6^2c_s^2v_1^2 - 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^4 - 4\omega_5\omega_2\omega_6^2\omega_3^2v_2^2 + 4\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^4 - 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2c_s^2v_2^2 - 2\omega_5^2\omega_2\omega_6^2\omega_3^2c_s^2v_2^2$$

$$C_{24} = -30\omega_2\omega_6^2\omega_3^3v_2^2 + 6\omega_2^3\omega_3^3v_2^2 + 12\omega_2^2\omega_6^2\omega_3^2c_s^2 + 48\omega_3^3\omega_6^2v_2^2 + \omega_3^3\omega_2^2\omega_3^2c_s^2 + 24\omega_2^2\omega_6^2\omega_3v_2^2 - 6\omega_2^3\omega_6\omega_3^3v_2^2 - 78\omega_2^3\omega_6^2\omega_3v_2^2 - 6\omega_2^3\omega_6^2\omega_3^3c_s^2 - 12\omega_3^3\omega_2^3v_2^2 + 24\omega_2\omega_6^2\omega_3^2v_2^2 - 12\omega_2^3\omega_6\omega_3^2c_s^2 + 24\omega_3^3\omega_6\omega_3^2v_2^2 - 14\omega_3^3\omega_6^2\omega_3^2c_s^2 - 12\omega_2^3\omega_3^2c_s^2 - 12\omega_2\omega_6^2\omega_3^2c_s^2 - 12\omega_3^3\omega_6\omega_3v_2^2 + 22\omega_2^2\omega_6^2\omega_3^3v_2^2 + 24\omega_2^2\omega_6^2\omega_3^2c_s^2 + 12\omega_2^2\omega_3^3v_2^2 + 34\omega_3^3\omega_6^2\omega_3^2v_2^2 + 24\omega_2^2\omega_6^2\omega_3^2c_s^2 - 12\omega_2^2\omega_6^2c_s^2 - 48\omega_2^2\omega_6^2\omega_3^2v_2^2 + 6\omega_2\omega_6^2\omega_3^2c_s^2 + 6\omega_2^3\omega_3^2c_s^2 - 6\omega_2^3\omega_6\omega_3^2c_s^2 - 4\omega_2^3\omega_6^2\omega_3^3v_2^2$$

$$C_{25} = 48\omega_2^2\omega_3^3v_1^2 + 6\omega_2^3\omega_3^3v_1^2 - 6\omega_5\omega_2^3\omega_3^3c_s^2 + 22\omega_5^2\omega_3^3\omega_2^2v_1^2 - 14\omega_5^2\omega_2^3\omega_3^2c_s^2 - 78\omega_5^2\omega_2\omega_3^3v_1^2 + 6\omega_5^2\omega_2^3\omega_3^2c_s^2 - 4\omega_5^2\omega_2^3\omega_3^3v_1^2 + 24\omega_5^2\omega_2^2\omega_3^3v_1^2 + 12\omega_5^2\omega_2^3v_1^2 - 12\omega_5\omega_2\omega_3^3c_s^2 + 24\omega_5^2\omega_2\omega_3^3v_1^2 - 12\omega_2^3\omega_3^2c_s^2 + 24\omega_5\omega_2^2\omega_3^3v_1^2 + 12\omega_5^2\omega_2^2\omega_3^2c_s^2 + \omega_5^2\omega_2^3\omega_3^2c_s^2 - 12\omega_5^2\omega_2^3\omega_3^2c_s^2 - 12\omega_2^3\omega_3^3v_1^2 - 12\omega_5\omega_2\omega_3^3v_1^2 - 48\omega_5^2\omega_2^2\omega_3^3v_1^2 + 24\omega_5\omega_2^2\omega_3^3c_s^2 - 12\omega_5^2\omega_3^2c_s^2 + 6\omega_2^3\omega_3^2c_s^2 - 6\omega_5^2\omega_2^3\omega_3^2c_s^2 - 6\omega_5\omega_2^3\omega_3^2v_1^2 + 34\omega_5^2\omega_2^2\omega_3^3v_1^2 + 24\omega_5^2\omega_2\omega_3^3c_s^2 - 30\omega_5^2\omega_2^2\omega_3^3v_1^2$$

$$C_{26} = -60\omega_6\omega_3^3v_2^2 - 24\omega_6\omega_3 + 25\omega_2^2\omega_3^2c_s^2 - 42\omega_6^2\omega_3v_2^2 + 12\omega_6^2v_2^2 + 24\omega_6\omega_3c_s^2 - 6\omega_3^3v_2^2 - 2\omega_6^2\omega_3^2c_s^2 - 9\omega_6\omega_3^3 + 15\omega_6\omega_3^2v_2^2 + 12\omega_3^3v_2^2 + 36\omega_6\omega_3^2 - 11\omega_6^2\omega_3^3 + 9\omega_6\omega_3^2c_s^2 - 12\omega_3^3 - 3\omega_6^2\omega_3^3v_2^2 + \omega_6^2\omega_3^3 + 12\omega_3^2c_s^2 + 6\omega_3^3 + 27\omega_6^2\omega_3^2v_2^2 - 36\omega_6\omega_3^2c_s^2 - 6\omega_3^3c_s^2 + 48\omega_6\omega_3v_2^2 + 24\omega_6^2c_s^2 - 48\omega_6^2\omega_3^2c_s^2 + 12\omega_6^2\omega_3$$

$$C_{27} = -12\omega_2^2\omega_6\omega_3^2v_2^2 - 3\omega_2^3\omega_6^2\omega_3^2 - 12\omega_2\omega_6^2\omega_3^3v_2^2 + 6\omega_3^3\omega_3^3v_2^2 + 42\omega_2^2\omega_6^2\omega_3^2c_s^2 + 24\omega_3^3\omega_6^2v_2^2 + 6\omega_3^3\omega_6^2\omega_3^2c_s^2 + \omega_2^2\omega_6^2\omega_3^3 + 12\omega_3^3\omega_6\omega_3 + 12\omega_2^2\omega_6^2\omega_3v_2^2 - 12\omega_2^2\omega_6^2\omega_3^3v_2^2 - 30\omega_2^3\omega_6^2\omega_3^2v_2^2 - 12\omega_2^2\omega_6^2\omega_3^2c_s^2 - 12\omega_2^3\omega_3^3v_2^2 + 6\omega_2\omega_6^2\omega_3^2v_2^2 - 24\omega_2^3\omega_6\omega_3^2c_s^2 - 21\omega_2^3\omega_6\omega_3^2 + 6\omega_2^2\omega_6^2\omega_3^3v_2^2 + 6\omega_3^3\omega_6\omega_3^2 - 48\omega_2^3\omega_6^2\omega_3^2c_s^2 + 6\omega_2^2\omega_6^2\omega_3^3c_s^2 - 12\omega_2^3\omega_3^2c_s^2 - 12\omega_2\omega_6^2\omega_3^2c_s^2 - 24\omega_2^3\omega_6\omega_3^2v_2^2 + 6\omega_2^2\omega_6^2\omega_3^2v_2^2 - \omega_2^3\omega_6^2\omega_3^3 + 78\omega_2^2\omega_6^2\omega_3^2c_s^2 + 6\omega_6^2\omega_3^3v_2^2 + 6\omega_2^3\omega_6^2\omega_3^2c_s^2 + 42\omega_2^2\omega_6^2\omega_3^2c_s^2 + 7\omega_2^3\omega_6^2\omega_3^2 - 3\omega_2^3\omega_6\omega_3^2 + 6\omega_2^3\omega_3^2 - 36\omega_2^2\omega_6^2c_s^2 - 12\omega_2^2\omega_6^2\omega_3^2v_2^2 - 6\omega_2^2\omega_6\omega_3 + 6\omega_2\omega_6^2\omega_3^2c_s^2 + 6\omega_2^2\omega_3^2c_s^2 - 12\omega_2^2\omega_6\omega_3^2c_s^2 - 12\omega_2^2\omega_6\omega_3^3c_s^2 - 3\omega_3^3\omega_3^3 + 6\omega_2^2\omega_6\omega_3^2 - 24\omega_2^2\omega_6^2\omega_3^2c_s^2$$

$$C_{28} = 48\omega_6\omega_3^2v_2^2 + 24\omega_6\omega_3 - 44\omega_6^2\omega_3^2c_s^2 + 12\omega_6^2v_2^2 - 36\omega_6\omega_3c_s^2 + 6\omega_3^3v_2^2 + 4\omega_6^2\omega_3^2c_s^2 + 9\omega_6\omega_3^3 - 12\omega_6\omega_3^3v_2^2 - 12\omega_3^3v_2^2 - 36\omega_6\omega_3^2 + 11\omega_6^2\omega_3^3 - 12\omega_6\omega_3^2c_s^2 + 12\omega_3^3 + \omega_6^2\omega_3^3v_2^2 - \omega_6^2\omega_3^3 - 12\omega_3^2c_s^2 - 6\omega_3^3 - 8\omega_6^2\omega_3^2v_2^2 + 48\omega_6\omega_3^2c_s^2 + 6\omega_3^3c_s^2 - 36\omega_6\omega_3v_2^2 - 48\omega_6^2c_s^2 + 90\omega_6^2\omega_3^2c_s^2 - 12\omega_6^2\omega_3$$

$$C_{29} = -24\omega_2^3\omega_6\omega_3^3v_2^2 - 6\omega_2^2\omega_6^2\omega_3^2 - 18\omega_2\omega_6^2\omega_3^3v_2^2 + 6\omega_3^3\omega_3^3v_2^2 + 48\omega_2^2\omega_6^2\omega_3^2c_s^2 + 24\omega_2^2\omega_6^2v_2^2 + 4\omega_3^3\omega_6^2\omega_3^2c_s^2 + 2\omega_2^2\omega_6^2\omega_3^3 - 12\omega_2^3\omega_6\omega_3^3v_2^2 - 30\omega_2^3\omega_6\omega_3^2v_2^2 - 12\omega_2^2\omega_6^2\omega_3^3c_s^2 - 12\omega_3^3\omega_6\omega_3^2v_2^2 - 12\omega_2^3\omega_6\omega_3^2c_s^2 - 6\omega_2^3\omega_6\omega_3^2 + 12\omega_2^2\omega_6\omega_3^2v_2^2 + 36\omega_2^3\omega_6\omega_3^2v_2^2 + 3\omega_2^2\omega_6^2\omega_3^3c_s^2 + 12\omega_3^3\omega_6\omega_3^2c_s^2 - 12\omega_2^2\omega_6^2\omega_3^2c_s^2 - 12\omega_2^3\omega_6\omega_3^2v_2^2 - \omega_2^3\omega_6^2\omega_3^3 + 36\omega_2^2\omega_6^2\omega_3^2c_s^2 + 12\omega_6^2\omega_3^3v_2^2 + 36\omega_2^2\omega_6^2\omega_3^2c_s^2 + 3\omega_2^3\omega_6^2\omega_3^3 - 6\omega_2^2\omega_6\omega_3^3 - 12\omega_2^3\omega_6^2c_s^2 + 12\omega_2^2\omega_6^2\omega_3^2v_2^2 + 6\omega_2\omega_6^2\omega_3^2c_s^2 + 6\omega_2^3\omega_3^2c_s^2 - 24\omega_2^2\omega_6\omega_3^2c_s^2 - 12\omega_2^2\omega_6\omega_3^2c_s^2 + 12\omega_2^2\omega_6\omega_3^2 - 24\omega_2^2\omega_6^2\omega_3^2c_s^2 + 3\omega_2^2\omega_6^2\omega_3^3v_2^2$$

$$C_{30} = -24\omega_6\omega_3^4 - 72\omega_6\omega_3^2v_2^2 - 24\omega_6^2\omega_3^4v_2^2 - 8\omega_6^2\omega_3^2c_s^2 + 12\omega_3^3c_s^2v_2^2 + 156\omega_6^2\omega_3^2c_s^2v_2^2 - 24\omega_6^2\omega_3v_2^2 + 24\omega_6^2c_s^4 - 48\omega_6^2\omega_3^4c_s^4 - 24\omega_6\omega_3^2c_s^2 - 96\omega_6^2c_s^2v_2^2 - 12\omega_3^3v_2^2 - 48\omega_6\omega_3^4v_2^2 + \omega_6^2\omega_3^3c_s^2 + 3\omega_6^2\omega_3^3v_2^2 + 18\omega_6\omega_3^3v_2^2 + 6\omega_6^2\omega_3^2c_s^2v_2^2 + 6\omega_6\omega_3^3c_s^4 + 24\omega_3^3v_2^2 + 48\omega_6\omega_3^2c_s^2v_2^2 - 18\omega_6\omega_3^4v_2^2 - 6\omega_6\omega_3^2c_s^2 - 3\omega_6^2\omega_3^4c_s^4 - 3\omega_6^2\omega_3^2v_2^2 - 24\omega_3^2c_s^2v_2^2 - 24\omega_3^2v_2^2 - 24\omega_6\omega_3^2c_s^2v_2^2 + 24\omega_6^2\omega_3^2v_2^2 - 12\omega_6\omega_3^3c_s^2v_2^2 + 24\omega_6^2\omega_3^4c_s^4 + 24\omega_6\omega_3^2c_s^2v_2^2 + 72\omega_6\omega_3^4v_2^2 + 24\omega_6\omega_3^4c_s^4 + 48\omega_6\omega_3^2v_2^2 - 72\omega_6^2\omega_3^2c_s^2v_2^2 + 12\omega_3^3v_2^2 + 24\omega_6^2\omega_3^4v_2^2 + 12\omega_6^2\omega_3^2c_s^2$$

$$C_{31} = 24\omega_6\omega_3^2v_2^2 + 12\omega_6\omega_3 - 20\omega_6^2\omega_3^2c_s^2 + 24\omega_6^2\omega_3v_2^2 - 12\omega_6^2v_2^2 - 12\omega_6\omega_3^2c_s^2 + 6\omega_3^3v_2^2 + \omega_6^2\omega_3^2c_s^2 + 6\omega_6\omega_3^3 - 6\omega_6\omega_3^3v_2^2 - 12\omega_3^3v_2^2 - 24\omega_6\omega_3^2 + 8\omega_6^2\omega_3^3 - 6\omega_6\omega_3^2c_s^2 + 12\omega_3^3 + 2\omega_6^2\omega_3^2v_2^2 - \omega_6^2\omega_3^3 - 12\omega_3^2c_s^2 - 6\omega_3^3 - 16\omega_6^2\omega_3^2v_2^2 + 24\omega_6\omega_3^2c_s^2 + 6\omega_3^3c_s^2 - 12\omega_6\omega_3^2v_2^2 - 24\omega_6^2c_s^2 + 42\omega_6^2\omega_3^2c_s^2 - 6\omega_6^2\omega_3$$

$$C_{32} = 3\omega_2^3\omega_4^3 - 6\omega_2^3\omega_4^4 - 6\omega_5\omega_2^2 - 6\omega_2^2\omega_4^3 + 24\omega_5\omega_2\omega_4^3 - 12\omega_5\omega_4^3 + 12\omega_2^2\omega_4^4 - 12\omega_5\omega_2\omega_4^4 + 12\omega_5\omega_2^2\omega_4^4 + 12\omega_5\omega_2^3\omega_4 - 10\omega_5\omega_2^2\omega_4^3 - 7\omega_5\omega_2^3\omega_4^4 - 6\omega_5\omega_2^2\omega_4 + \omega_5\omega_2^3\omega_4^4$$

$$C_{33} = 12\omega_5\omega_2^2c_s^2 - 24\omega_5^2v_1^2\omega_4 + 6\omega_5^2\omega_2^2v_1^2 - 6\omega_2^3v_1^2\omega_4 + 12\omega_2^2c_s^2\omega_4 + 12\omega_5\omega_2c_s^2\omega_4 + 12\omega_5^2\omega_2c_s^2 + 36\omega_5^2\omega_2v_1^2\omega_4 + \omega_5^2\omega_2^3v_1^2\omega_4 - \omega_5^2\omega_2^3v_1^2 - 6\omega_5\omega_2^3c_s^2 + 9\omega_5\omega_2^3c_s^2\omega_4 - 30\omega_5\omega_2^2v_1^2\omega_4 + 22\omega_5^2\omega_2^2c_s^2\omega_4 + 12\omega_5^2c_s^2\omega_4 - 6\omega_2^3c_s^2\omega_4 + 3\omega_5^2\omega_2^3c_s^2 - 6\omega_5\omega_2^3v_1^2 + 12\omega_5\omega_2v_1^2\omega_4 + 12\omega_2^2v_1^2\omega_4 - 30\omega_2^2\omega_2c_s^2\omega_4 - 2\omega_2^2\omega_2^2c_s^2\omega_4 + 12\omega_5\omega_2^2v_1^2 - 18\omega_5^2\omega_2^2c_s^2 + 9\omega_5\omega_2^2v_1^2\omega_4 - 30\omega_5\omega_2^2c_s^2\omega_4 - 12\omega_5^2\omega_2v_1^2 - 10\omega_5^2\omega_2^2v_1^2\omega_4$$

$$C_{34} = -12\omega_5\omega_2^2c_s^2\omega_4^3 + 42\omega_5^2\omega_2^2c_s^2\omega_4^2 - 3\omega_2^3\omega_4^3 + \omega_5^2\omega_2^2\omega_4^2 - 12\omega_5\omega_2^2v_1^2\omega_4^2 - \omega_5^2\omega_2^2\omega_4^3 + 6\omega_5\omega_2^2c_s^2\omega_4^2 - 48\omega_5^2\omega_2^2c_s^2\omega_4^3 + 42\omega_5\omega_2^2v_1^2\omega_4^3 + 6\omega_5^2\omega_2^3v_1^2\omega_4^2 + 12\omega_5^2\omega_2v_1^2\omega_4^2 + 6\omega_2^3v_1^2\omega_4^2 - 12\omega_5^2\omega_2^3v_1^2\omega_4 + 6\omega_5^2\omega_2^3v_1^2 + 6\omega_2^3\omega_4^2 + 12\omega_5\omega_2\omega_4^3 - 3\omega_5^2\omega_2^2\omega_4^2 + 24\omega_5^2v_1^2\omega_4^3 - 30\omega_5^2\omega_2v_1^2\omega_4^3 - 12\omega_2^2\omega_2^2c_s^2\omega_4 + 7\omega_2^2\omega_2^2\omega_4^3 - 24\omega_5\omega_2c_s^2\omega_4^3 - 12\omega_2^2c_s^2\omega_4^3 - 12\omega_5^2\omega_2^2v_1^2\omega_4^2 - 12\omega_5\omega_2^3v_1^2\omega_4^3 + 6\omega_5^2\omega_2^3c_s^2\omega_4^3 + 6\omega_5\omega_2^2\omega_4^2 - 12\omega_5\omega_2^2c_s^2\omega_4^2 - 6\omega_5^2\omega_2^2\omega_4^3 + 6\omega_5^2\omega_2^2v_1^2\omega_4^3 + 6\omega_5\omega_2^3v_1^2\omega_4^2 - 21\omega_5\omega_2^3\omega_4^2 - 12\omega_5^2\omega_2^3c_s^2\omega_4^2 + 42\omega_5\omega_2^3c_s^2\omega_4^3 - 3\omega_5\omega_2^2\omega_4^2 + 6\omega_5^2\omega_2^2c_s^2\omega_4 + 6\omega_2^3c_s^2\omega_4^3 - 24\omega_5^2\omega_2c_s^2\omega_4^2 - 36\omega_5^2c_s^2\omega_4^3 + 78\omega_5^2\omega_2c_s^2\omega_4^3 + 6\omega_5\omega_2^2\omega_4^3 - 12\omega_2^2v_1^2\omega_4^3 - 24\omega_5\omega_2v_1^2\omega_4^3 + 6\omega_5^2\omega_2^2v_1^2\omega_4$$

$$C_{35} = -12\omega_5\omega_2^3c_s^2\omega_4^3 + 48\omega_5^2\omega_2^2c_s^2\omega_4^2 + 2\omega_5^2\omega_2^2\omega_4^2 - 24\omega_5\omega_2^2v_1^2\omega_4^2 + 3\omega_5^2\omega_2^3v_1^2\omega_4^3 - \omega_5^2\omega_2^3\omega_4^3 + 12\omega_5\omega_2^3c_s^2\omega_4^2 - 32\omega_5^2\omega_2^2c_s^2\omega_4^3 + 36\omega_5\omega_2^2v_1^2\omega_4^3 + 6\omega_2^3v_1^2\omega_4^3 - 18\omega_5^2\omega_2^3v_1^2\omega_4 + 12\omega_5^2\omega_2^3v_1^2 - 6\omega_5^2\omega_2^3\omega_4^2 + 24\omega_5^2v_1^2\omega_4^3 - 30\omega_5^2\omega_2v_1^2\omega_4^3 - 12\omega_5^2\omega_2^2c_s^2\omega_4 + 3\omega_5^2\omega_2^2\omega_4^3 - 12\omega_5\omega_2c_s^2\omega_4^2 - 12\omega_2^2c_s^2\omega_4^3 + 12\omega_5^2\omega_2^2v_1^2\omega_4^2 - 12\omega_5\omega_2^3v_1^2\omega_4^3 + 4\omega_5^2\omega_2^3c_s^2\omega_4^3 + 12\omega_5\omega_2^2\omega_4^2 - 24\omega_5\omega_2^2c_s^2\omega_4^2 + 12\omega_5\omega_2^2v_1^2\omega_4^2 - 6\omega_5\omega_2^2\omega_4^3 - 12\omega_5^2\omega_2^2c_s^2\omega_4^2 + 36\omega_5\omega_2^2c_s^2\omega_4^3 - 6\omega_5\omega_2^3\omega_4^2 + 6\omega_5^2\omega_2^3c_s^2\omega_4 + 6\omega_2^3c_s^2\omega_4^3 - 24\omega_5^2\omega_2c_s^2\omega_4^2 - 36\omega_5^2c_s^2\omega_4^3$$

$$\begin{aligned}
C_{51} = & -6\omega_6\omega_3^3\omega_4^2 - 12\omega_6\omega_3^3v_2^2\omega_4^3 - 12\omega_6^2\omega_3^3c_s^2\omega_4^2 + 12\omega_6^2\omega_3^3v_2^2\omega_4^2 + 36\omega_6\omega_3^2c_s^2\omega_4^3 + 4\omega_6^2\omega_3^3c_s^2\omega_4^3 + 12\omega_6\omega_3^3v_2^2\omega_4^2 - 24\omega_6\omega_3^2c_s^2\omega_4^2 + 3\omega_6\omega_3^3\omega_4^3 + \\
& 36\omega_6^2\omega_3^3c_s^2\omega_4^3 + 12\omega_6\omega_3^2\omega_4^2 - 12\omega_6^2c_s^2\omega_4^3 - 6\omega_6\omega_3^2\omega_4^3 - 12\omega_6\omega_3v_2^2\omega_4^3 - 24\omega_6^2\omega_3c_s^2\omega_4^2 + 6\omega_6^2\omega_3^3c_s^2\omega_4 - 12\omega_3^3v_2^2\omega_4^3 + 6\omega_3^3c_s^2\omega_4^2 - 6\omega_3^2\omega_2^2\omega_4^2 + \\
& 12\omega_6\omega_3^3c_s^2\omega_4^2 + 3\omega_3^2\omega_3^3v_2^2\omega_4^3 - 32\omega_6^2\omega_3^3c_s^2\omega_4^3 - 24\omega_6\omega_3^3v_2^2\omega_4^2 + 12\omega_6^2\omega_3^3v_2^2 - 12\omega_6\omega_3^3c_s^2\omega_4^3 + 36\omega_6\omega_3^3v_2^2\omega_4^3 + 48\omega_6^2\omega_3^3c_s^2\omega_4^2 + 3\omega_6^2\omega_3^3\omega_4^3 - \\
& 12\omega_3^3c_s^2\omega_4^3 + 6\omega_3^3v_2^2\omega_4^3 - 12\omega_6\omega_3c_s^2\omega_4^3 - 12\omega_6^2\omega_3^3c_s^2\omega_4 + 2\omega_6^2\omega_3^3\omega_4^2 - 18\omega_6^2\omega_3^3v_2^2\omega_4 + 24\omega_6^2v_2^2\omega_4^3 - \omega_6^2\omega_3^3\omega_4^3 - 30\omega_6^2\omega_3v_2^2\omega_4^3 \\
C_{52} = & 48\omega_6\omega_3^2v_2^2 + 24\omega_6\omega_3 - 44\omega_6^2\omega_3^2c_s^2 + 12\omega_6^2v_2^2 - 36\omega_6\omega_3c_s^2 + 6\omega_3^3v_2^2 + 4\omega_6^2\omega_3^3c_s^2 + 9\omega_6\omega_3^3 - 12\omega_6\omega_3^2v_2^2 - 12\omega_3^3v_2^2 - 36\omega_6\omega_3^2 + 11\omega_6^2\omega_3^2 - \\
& 12\omega_6\omega_3^3c_s^2 + 12\omega_3^3 + \omega_6^2\omega_3^3v_2^2 - \omega_6^2\omega_3^3 - 12\omega_3^3c_s^2 - 6\omega_3^3 - 8\omega_6^2\omega_3^3v_2^2 + 48\omega_6\omega_3^3c_s^2 + 6\omega_3^3c_s^2 - 36\omega_6\omega_3v_2^2 - 48\omega_6^2c_s^2 + 90\omega_6^2\omega_3c_s^2 - 12\omega_6^2\omega_3 \\
C_{53} = & 22\omega_2c_s^2\omega_7^2\omega_4^2 + 6\omega_7^2\omega_4^2v_3^2 + 9\omega_2\omega_7\omega_4^3v_3^2 - 24\omega_2\omega_7^2v_3^2 - 2\omega_2c_s^2\omega_7^2\omega_4^3 - \omega_7^2\omega_4^3v_3^2 - 30\omega_2\omega_7\omega_4^2v_3^2 - 6c_s^2\omega_7\omega_4^3 - 30\omega_2c_s^2\omega_7^2\omega_4 + 12c_s^2\omega_7\omega_4^2 + \\
& 36\omega_2\omega_7^2\omega_4v_3^2 - 18c_s^2\omega_7^2\omega_4^2 + 12\omega_2c_s^2\omega_7\omega_4 - 10\omega_2\omega_7^2\omega_4^2v_3^2 + 12\omega_2\omega_4^2v_3^2 - 6\omega_7\omega_4^2v_3^2 + 12\omega_2c_s^2\omega_4^2 + 12\omega_2\omega_7\omega_4v_3^2 + 3c_s^2\omega_7^2\omega_4^3 - 6\omega_2c_s^2\omega_4^3 + \\
& 12\omega_2c_s^2\omega_7^2 + \omega_2\omega_7^2\omega_4^3v_3^2 - 6\omega_2\omega_4^2v_3^2 + 12\omega_7\omega_4^2v_3^2 + 9\omega_2c_s^2\omega_7\omega_4^3 + 12c_s^2\omega_7^2\omega_4 - 30\omega_2c_s^2\omega_7\omega_4^2 - 12\omega_7^2\omega_4^2v_3^2 \\
C_{54} = & 3\omega_3^3\omega_4^3 - 12\omega_3^3\omega_7 - 7\omega_2^2\omega_7\omega_4^3 - 6\omega_2^2\omega_4^2 + 12\omega_2^2\omega_7\omega_4^2 - 12\omega_2^2\omega_7\omega_4 - 6\omega_2^2\omega_4^3 + 12\omega_2^2\omega_4^2 - 10\omega_3^3\omega_7\omega_4^2 - 6\omega_7\omega_4^3 + \omega_2^3\omega_7\omega_4^3 + 12\omega_2\omega_7\omega_4^3 + \\
& 24\omega_2^2\omega_7\omega_4 - 6\omega_2\omega_7\omega_4^3 \\
C_{55} = & 4\omega_5^2\omega_3^3c_s^4\omega_7^2\omega_4^2 + 20\omega_5^2\omega_3^3v_1^2\omega_7^2\omega_4^2v_3^2 + 4\omega_5\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^2 - 3\omega_5\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 - 8\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4v_3^2 + 2\omega_3^3v_1^2\omega_7^2\omega_4^3v_3^2 - 4\omega_5^2\omega_3^3c_s^2v_1^2\omega_7^2 + \\
& 4\omega_5^2\omega_2^2c_s^4\omega_7\omega_4^2 + \omega_5\omega_3^3c_s^4\omega_7^2\omega_4^2 - 4\omega_5^2\omega_2^2c_s^2v_1^2\omega_7\omega_4^2v_3^2 - 4\omega_5^2\omega_3^3v_1^2\omega_7\omega_4v_3^2 - 4\omega_5^2\omega_2^2c_s^2v_1^2\omega_7\omega_4v_3^2 - 2\omega_5\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + 20\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^2v_3^2 - 3\omega_5\omega_3^3v_1^2\omega_7^2\omega_4^3v_3^2 - 4\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^3 + \\
& 4\omega_5^2\omega_2^2c_s^4\omega_7^2\omega_4^3 + 2\omega_5^2\omega_2^2v_1^2\omega_7\omega_4^3v_3^2 - 4\omega_5^2\omega_2^2\omega_7^2\omega_4^3v_3^2 - 4\omega_5^2\omega_3^3c_s^2v_1^2\omega_7^2\omega_4^2v_3^2 + 10\omega_5^2\omega_2^2c_s^2v_1^2\omega_7\omega_4^2v_3^2 - 3\omega_5^2\omega_3^3v_1^2\omega_7^2\omega_4^3v_3^2 + 2\omega_5\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 + 4\omega_5\omega_3^3c_s^4\omega_7^2\omega_4^2 - \\
& 8\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^2 + 2\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^3 + \omega_5^2\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + 12\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^2 + 2\omega_5\omega_3^3v_1^2\omega_7^2\omega_4^2v_3^2 - 12\omega_5^2\omega_2^2c_s^4\omega_7^2\omega_4^2 - 2\omega_5\omega_3^3c_s^2\omega_7^2\omega_4^3 + \\
& 4\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^3 - 3\omega_5^2\omega_3^3c_s^2v_1^2\omega_7\omega_4^3 + 20\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^2v_3^2 - 2\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 + 10\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 + 20\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^3v_3^2 + \\
& 4\omega_5^2\omega_2^2c_s^4\omega_7\omega_4^2 - 4\omega_5^2\omega_2^2c_s^2v_1^2\omega_7\omega_4^2 - 4\omega_5\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 + 2\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^3 + \omega_5^2\omega_3^3c_s^2v_1^2\omega_7^2\omega_4^2 - 3\omega_5^2\omega_2^2v_1^2\omega_7\omega_4^3v_3^2 - 2\omega_5^2\omega_2^2c_s^2\omega_7\omega_4^3 + \\
& \omega_5^2\omega_3^3c_s^2\omega_7\omega_4^3v_3^2 + 2\omega_5^2\omega_2^2c_s^2v_1^2\omega_7\omega_4^3 - 8\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 - 4\omega_5\omega_2^2v_1^2\omega_7^2\omega_4^2v_3^2 - 8\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^2 - 38\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^3v_3^2 + 10\omega_5^2\omega_3^3v_1^2\omega_7\omega_4^2v_3^2 + \\
& 10\omega_5^2\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^2 - 4\omega_5^2v_1^2\omega_7^2\omega_4^3v_3^2 + \omega_5^2\omega_3^3c_s^4\omega_7\omega_4^2 - 4\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^3 - 2\omega_5\omega_3^3c_s^2v_1^2\omega_7^2\omega_4^2 - 36\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^3v_3^2 + 4\omega_5^2\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + \\
& 10\omega_5\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 - 4\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 - 2\omega_5^2\omega_2^2c_s^4\omega_7^2\omega_4^2 - 4\omega_5\omega_2^2v_1^2\omega_7^2\omega_4^3v_3^2 + 20\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^2v_3^2 - 2\omega_5^2\omega_2^2c_s^4\omega_7\omega_4^2 - 4\omega_5\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 + \\
& 12\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4^3v_3^2 + 10\omega_5\omega_2^2v_1^2\omega_7^2\omega_4^3v_3^2 - 38\omega_5^2\omega_2^2v_1^2\omega_7^2\omega_4^3v_3^2 - 4\omega_5^2c_s^2\omega_7^2\omega_4^3v_3^2 + 4\omega_5^2\omega_2^2c_s^2\omega_7^2\omega_4^2 + \omega_5\omega_2^2c_s^2v_1^2\omega_7^2\omega_4^3 - 2\omega_5^2\omega_2^2c_s^2\omega_7\omega_4^3v_3^2 \\
C_{56} = & 24\omega_3^3c_s^2\omega_7\omega_4^2 - 12\omega_2c_s^2\omega_7^2\omega_4^2 - 48\omega_2^2\omega_7^2\omega_4^2v_3^2 - 4\omega_3^3\omega_7^2\omega_4^3v_3^2 - 6\omega_3^3c_s^2\omega_7\omega_4^3 + 6\omega_2c_s^2\omega_7^2\omega_4^3 + 12\omega_7^2\omega_4^3v_3^2 + 48\omega_3^3\omega_2^2v_3^2 + 22\omega_2^2\omega_7^2\omega_4^3v_3^2 - \\
& 12\omega_3^3\omega_7\omega_4v_3^2 - 12\omega_3^3c_s^2\omega_7\omega_4 + 34\omega_3^3\omega_7^2\omega_4^2v_3^2 + 12\omega_2^2c_s^2\omega_7^2\omega_4^2 + 24\omega_2\omega_7^2\omega_4^2v_3^2 + 24\omega_2^2c_s^2\omega_7^2\omega_4 - 78\omega_3^3\omega_7^2\omega_4v_3^2 - 6\omega_2^2c_s^2\omega_7^2\omega_4^3 + 6\omega_3^3\omega_4^3v_3^2 + \\
& 24\omega_2^2\omega_7\omega_4^3v_3^2 - 12\omega_2^2c_s^2\omega_7^2 + 6\omega_2^2c_s^2\omega_4^3 + \omega_2^2c_s^2\omega_7^2\omega_4^3 - 30\omega_2\omega_7^2\omega_4^3v_3^2 - 12\omega_2^2c_s^2\omega_4^2 - 14\omega_2^2c_s^2\omega_7^2\omega_4 - 6\omega_2^2\omega_7\omega_4^3v_3^2 - 12\omega_2^2\omega_4^3v_3^2 + 24\omega_2^2\omega_7^2\omega_4v_3^2 \\
C_{57} = & -6\omega_5\omega_3^3c_s^2\omega_4^3 + 12\omega_5^2\omega_2^2c_s^2\omega_4^2 - 4\omega_5^2\omega_3^3v_1^2\omega_4^3 - 14\omega_5^2\omega_2^2c_s^2\omega_4^3 + 24\omega_5\omega_2^2v_1^2\omega_4^3 + 22\omega_5^2\omega_2^2v_1^2\omega_4^2 + 24\omega_5^2\omega_2^2v_1^2\omega_4^2 + 6\omega_3^3v_1^2\omega_4^3 - 30\omega_5^2\omega_2^2v_1^2\omega_4 + \\
& 12\omega_5^2\omega_3^3v_1^2 + 48\omega_5^2v_1^2\omega_4^3 - 78\omega_5^2\omega_2^2v_1^2\omega_4^3 - 12\omega_5^2\omega_2^2c_s^2\omega_4 - 12\omega_5\omega_2^2c_s^2\omega_4^3 - 48\omega_5^2\omega_2^2v_1^2\omega_4^2 - 6\omega_5\omega_3^3v_1^2\omega_4^3 + \omega_5^2\omega_3^3c_s^2\omega_4^3 + \\
& 34\omega_5^2\omega_2^2v_1^2\omega_4^2 - 6\omega_5^2\omega_2^2c_s^2\omega_4^2 + 24\omega_5\omega_2^2c_s^2\omega_4^3 + 6\omega_5^2\omega_2^2c_s^2\omega_4 + 6\omega_2^2c_s^2\omega_4^3 - 12\omega_5^2c_s^2\omega_4^2 + 24\omega_5^2\omega_2^2c_s^2\omega_4 - 12\omega_2^2v_1^2\omega_4^3 - 12\omega_5\omega_2^2v_1^2\omega_4^2 + 24\omega_5^2\omega_2^2v_1^2\omega_4 \\
C_{58} = & -6\omega_3^3c_s^2\omega_4^3 - 30\omega_3^3c_s^2\omega_7\omega_4 + 6\omega_7^2\omega_4^3v_3^2 + 36\omega_3\omega_7^2\omega_4v_3^2 + 12\omega_3c_s^2\omega_4^2 - 30\omega_3\omega_7\omega_4^2v_3^2 + 12\omega_3\omega_4^2v_3^2 - \omega_7^2\omega_4^3v_3^2 - 2\omega_3c_s^2\omega_7^2\omega_4^3 - 6c_s^2\omega_7\omega_4^3 + \\
& 22\omega_3c_s^2\omega_7^2\omega_4 + 12c_s^2\omega_7\omega_4^2 - 6\omega_3\omega_3^3v_2^2 + 9\omega_3\omega_7\omega_4^3v_3^2 + 12\omega_3c_s^2\omega_7^2 - 18c_s^2\omega_7^2\omega_4^2 - 30\omega_3c_s^2\omega_7\omega_4^2 - 24\omega_3\omega_7^2v_3^2 - 6\omega_7\omega_4^3v_3^2 + \omega_3\omega_7^2\omega_4^3v_3^2 + \\
& 3c_s^2\omega_7^2\omega_4^3 + 9\omega_3c_s^2\omega_7\omega_4^3 + 12\omega_7\omega_4^2v_3^2 + 12\omega_3\omega_7\omega_4v_3^2 + 12\omega_3c_s^2\omega_7\omega_4 + 12c_s^2\omega_7^2\omega_4 - 10\omega_3\omega_7^2\omega_4^2v_3^2 - 12\omega_7^2\omega_4^2v_3^2 \\
C_{59} = & -6\omega_3^3\omega_4^3 + \omega_3^3\omega_7\omega_4^3 + 12\omega_3^3\omega_4^2 - 10\omega_3^3\omega_7\omega_4^2 - 6\omega_3\omega_7\omega_4^2 + 24\omega_3^3\omega_7\omega_4 - 12\omega_3^3\omega_7 + 3\omega_3^3\omega_4^3 + 12\omega_3\omega_7\omega_4^2 - 6\omega_3^3\omega_4^2 + 12\omega_3^3\omega_7\omega_4^2 - 6\omega_7\omega_4^3 - \\
& 7\omega_3^3\omega_7\omega_4^2 - 12\omega_3^3\omega_7\omega_4 \\
C_{60} = & 6\omega_3^3\omega_3^3\omega_7^2\omega_4^2v_3^2 + \omega_3^3\omega_3^3c_s^2\omega_4^3 + 3\omega_2\omega_3^3\omega_7^2\omega_4^3v_3^2 - 12\omega_3^3\omega_3^3\omega_7^2\omega_4^2v_3^2 - 2\omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4^3 - 21\omega_3^3\omega_3^3\omega_7^2\omega_4v_3^2 + 3\omega_3^3\omega_7^2\omega_4^3v_3^2 - 8\omega_2^2\omega_3^3\omega_7^2\omega_4^3v_3^2 + \\
& 6\omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4 - 2\omega_3^3\omega_3^3\omega_7^2v_3^2 + 4\omega_2\omega_3^3\omega_7^2\omega_4^2v_3^2 + 4\omega_3^3\omega_3\omega_7^2\omega_4^2v_3^2 + 6\omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4^2 - 2\omega_3^3\omega_3^3c_s^2\omega_4^2 + \omega_3^3\omega_3^3\omega_7\omega_4^3v_3^2 - 2\omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4 + \\
& 7\omega_3^3\omega_7^2\omega_4^2v_3^2 + 7\omega_3^3\omega_3^3\omega_7^2\omega_4^2 + \omega_3^3\omega_3^3c_s^2\omega_7\omega_4^2 - 2\omega_3^3\omega_3^3\omega_7\omega_4^2v_3^2 + 3\omega_3^3\omega_7^2\omega_4^2v_3^2 - 6\omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4 - 2\omega_3^3\omega_3^3c_s^2\omega_7 - 2\omega_3^3\omega_3^3c_s^2\omega_7\omega_4 - \\
& 2\omega_3^3\omega_3^3\omega_7\omega_4^2v_3^2 - 8\omega_3^3\omega_3\omega_7^2\omega_4^2v_3^2 + 4\omega_2^2\omega_3^3\omega_7^2\omega_4^2v_3^2 + \omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4^3 - 8\omega_2\omega_3^3\omega_7^2\omega_4^2v_3^2 + \omega_3^3\omega_3^3\omega_4^3v_3^2 + 6\omega_2^2\omega_3^3c_s^2\omega_7^2\omega_4^2 + \omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4^3 + \\
& \omega_2^2\omega_3^3\omega_7\omega_4^3v_3^2 - 2\omega_3^3\omega_3^3c_s^2\omega_7\omega_4^3 + 10\omega_3^3\omega_3^3\omega_7^2v_3^2 + \omega_2\omega_3^3c_s^2\omega_7^2\omega_4^3 - 2\omega_3^3\omega_3^3\omega_7^2\omega_4^2v_3^2 - 2\omega_2^2\omega_3^3c_s^2\omega_7^2\omega_4^2 - 12\omega_2^2\omega_3^3\omega_7^2\omega_4^2v_3^2 - 2\omega_3^3\omega_3^3c_s^2\omega_7^2\omega_4^2 + \\
& 3\omega_2^2\omega_3\omega_7^2\omega_4^3v_3^2 - 2\omega_2\omega_3^3c_s^2\omega_7^2\omega_4^2 + 6\omega_2^2\omega_3^3c_s^2\omega_7\omega_4^2 + \omega_2^2\omega_3^3c_s^2\omega_7^2\omega_4^3 + 12\omega_3^3\omega_3^3\omega_7^2\omega_4^2v_3^2 - 2\omega_3^3\omega_3^3c_s^2\omega_7\omega_4 - 2\omega_2^2\omega_3^3\omega_7\omega_4^2v_3^2 - 2\omega_3^3\omega_3^3c_s^2\omega_7\omega_4^2 - \\
& 2\omega_2^2\omega_3^3c_s^2\omega_7^2\omega_4^2 - 2\omega_3^3\omega_3^3\omega_7\omega_4v_3^2 + 7\omega_2^2\omega_3^3\omega_7^2\omega_4^2v_3^2 - 2\omega_2^2\omega_3^3c_s^2\omega_7^2\omega_4 + \omega_2^2\omega_3^3c_s^2\omega_7\omega_4^3 + 7\omega_2^2\omega_3^3\omega_7^2\omega_4v_3^2 \\
C_{61} = & -12\omega_3^3c_s^2\omega_7\omega_4 - 12\omega_3^3c_s^2\omega_7^2 + 40\omega_3^3\omega_7^2\omega_4^2v_3^2 + 6\omega_3^3\omega_4^3v_3^2 - 24\omega_3^3c_s^2\omega_7\omega_4^2 - 12\omega_3^3\omega_7\omega_4v_3^2 + 12\omega_3^3c_s^2\omega_7\omega_4^3 + 24\omega_3^3\omega_7^2\omega_4^2v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + \\
& 6\omega_3^3c_s^2\omega_7^2\omega_4^2 - 12\omega_3^3\omega_4^2v_3^2 - 5\omega_3^3\omega_7^2\omega_4^3v_3^2 - 12\omega_3^3c_s^2\omega_7\omega_4^3 - 12\omega_3^3c_s^2\omega_4^2 - 12\omega_3c_s^2\omega_7^2\omega_4^2 - 60\omega_3^3\omega_7^2\omega_4^2v_3^2 + 6\omega_3^3c_s^2\omega_4^3 + 36\omega_3^3c_s^2\omega_7\omega_4^2 + 48\omega_3^3\omega_7^2\omega_4v_3^2 - \\
& 24\omega_3^3c_s^2\omega_7\omega_4 - 32\omega_3^3c_s^2\omega_7^2\omega_4 - 12\omega_3^3\omega_7\omega_4^3v_3^2 - 30\omega_3\omega_7^2\omega_4^2v_3^2 - 24\omega_3^3\omega_7\omega_4^2v_3^2 + 4\omega_3^3c_s^2\omega_7^2\omega_4^3 + 36\omega_3^3\omega_7\omega_4^2v_3^2 - 12\omega_3^3c_s^2\omega_7^2\omega_4^3 + 36\omega_3^3c_s^2\omega_7^2\omega_4 - \\
& 90\omega_3^3\omega_7^2\omega_4v_3^2 + 12\omega_3^3\omega_7\omega_4^3v_3^2 + 48\omega_3^3c_s^2\omega_7^2\omega_4^2 + 24\omega_3\omega_7^2\omega_4^2v_3^2 + 48\omega_3^3\omega_7^2v_3^2 \\
C_{62} = & 36\omega_3^3c_s^2\omega_7\omega_4^2 - 12\omega_2c_s^2\omega_7^2\omega_4^2 - 60\omega_2^2\omega_7^2\omega_4^2v_3^2 - 5\omega_3^3\omega_7^2\omega_4^3v_3^2 - 12\omega_3^3c_s^2\omega_7\omega_4^3 + 6\omega_2c_s^2\omega_7^2\omega_4^3 + 12\omega_2^2c_s^2\omega_7\omega_4^3 + 12\omega_7^2\omega_4^3v_3^2 + 48\omega_3^3\omega_7^2v_3^2 + \\
& 24\omega_2^2\omega_7^2\omega_4^3v_3^2 - 12\omega_3^3\omega_7\omega_4v_3^2 - 24\omega_2^2c_s^2\omega_7\omega_4^2 - 12\omega_2^2c_s^2\omega_7\omega_4^3 + 40\omega_3^3\omega_7^2\omega_4^2v_3^2 + 12\omega_2^2\omega_7\omega_4^3v_3^2 + 48\omega_2^2c_s^2\omega_7^2\omega_4^2 + 24\omega_2\omega_7^2\omega_4^2v_3^2 + 36\omega_2^2c_s^2\omega_7^2\omega_4 - \\
& 90\omega_3^3\omega_7^2\omega_4v_3^2 - 12\omega_2^2c_s^2\omega_7^2\omega_4^3 + 6\omega_3^3\omega_4^3v_3^2 + 36\omega_3^3\omega_7\omega_4^2v_3^2 - 12\omega_2^2c_s^2\omega_7^2 + 6\omega_3^3c_s^2\omega_4^3 + 4\omega_2^2c_s^2\omega_7^2\omega_4^3 - 30\omega_2\omega_7^2\omega_4^3v_3^2 - 24\omega_2^2\omega_7\omega_4^2v_3^2 - 12\omega_2^2c_s^2\omega_4^2 - \\
& 32\omega_2^2c_s^2\omega_7^2\omega_4^2 - 12\omega_2^2\omega_7\omega_4^2v_3^2 - 12\omega_2^2\omega_4^2v_3^2 + 48\omega_2^2\omega_7^2\omega_4v_3^2 - 24\omega_2^2c_s^2\omega_7^2\omega_4 \\
C_{63} = & 12\omega_3^3\omega_4^3 - 30\omega_3^3\omega_3^2\omega_4^2 - 30\omega_2\omega_3^3\omega_4^3 + 6\omega_2\omega_3^3\omega_4^2 - 36\omega_3^3\omega_3^3\omega_4 + 24\omega_3^3\omega_3^3\omega_4^3 + 18\omega_2\omega_3^3\omega_4^3 + 28\omega_3^3\omega_3^3\omega_4^2 + 12\omega_3^3\omega_4^3 + 18\omega_2^2\omega_3^3\omega_4 - \\
& 5\omega_2^2\omega_3^3\omega_4^3 + 18\omega_2^2\omega_3\omega_4^3 - 42\omega_2^2\omega_3^2\omega_4^3 + 18\omega_2^2\omega_3^3\omega_4 + 12\omega_2^2\omega_3^2\omega_4^2 + 24\omega_2^2\omega_3^3\omega_4^2 - 30\omega_2^2\omega_3\omega_4^3 + 12\omega_2^2\omega_3^3 + 6\omega_2^2\omega_3\omega_4^2 - 30\omega_2^2\omega_3^3\omega_4^2 \\
C_{64} = & -2\omega_6\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^2 + \omega_6^2\omega_3^3c_s^2\omega_7\omega_4^3v_3^2 + 2\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^3 + 2\omega_6^2\omega_3^3v_2^2\omega_7\omega_4^3v_3^2 + 4\omega_6\omega_3^3c_s^4\omega_7^2\omega_4^2 - 8\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + 10\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4 + \\
& 2\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 + 4\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^2 - 3\omega_6^2\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 - 4\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 - 2\omega_6^2\omega_3^3c_s^4\omega_7^2\omega_4 - 2\omega_6\omega_3^3c_s^4\omega_7^2\omega_4^3 + 10\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + 2\omega_6\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 -
\end{aligned}$$

$$\begin{aligned}
& 4\omega_6\omega_3c_s^2v_2^2\omega_2^2 + \omega_6\omega_3c_s^2v_2^2\omega_7\omega_3^3 - 4\omega_6\omega_3c_s^2\omega_7\omega_1^2v_3^2 - 12\omega_6\omega_3c_s^4\omega_7^2\omega_4^2 + 20\omega_6\omega_3^3v_2^2\omega_7^2\omega_4^2v_3^2 - 4\omega_6\omega_3c_s^2\omega_7\omega_4^3v_3^2 + 12\omega_6\omega_3^2c_s^2\omega_7\omega_1^2v_3^2 + \omega_6\omega_3^3c_s^4\omega_7\omega_1^3 + \\
& 4\omega_6^2\omega_3^3c_s^4\omega_7^2\omega_4^2 + \omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^3 - 4\omega_6^2\omega_3^3v_2^2\omega_7\omega_4^2v_3^2 + 4\omega_6^2\omega_3^3c_s^4\omega_7^2\omega_4^2 + 20\omega_6^2\omega_3^3v_2^2\omega_7^2v_3^2 - 2\omega_6^2\omega_3^3c_s^2\omega_7\omega_4^2v_3^2 - 4\omega_6^2\omega_3^3c_s^2v_2^2\omega_7\omega_4^2 - 2\omega_6\omega_3^3c_s^4\omega_7^2\omega_4^2 - \\
& 4\omega_6^2c_s^2\omega_7^2\omega_4^3v_3^2 - 8\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^2 - 4\omega_6^2\omega_3^3v_2^2\omega_7\omega_4^2v_3^2 + 2\omega_6^2\omega_3^3c_s^2v_2^2\omega_7\omega_4^3 + 10\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + 4\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^2v_3^2 - 3\omega_6\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 - \\
& 4\omega_6^2c_s^3\omega_7^2\omega_4^2v_3^2 + 20\omega_6^2\omega_3^3v_2^2\omega_7^2\omega_4^2v_3^2 - 4\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2 - \omega_6^2\omega_3^3c_s^4\omega_7^2\omega_4^3 + 10\omega_6^2\omega_3^3c_s^2v_2^2\omega_7\omega_4^2 + 4\omega_6^2\omega_3^3c_s^2\omega_7\omega_4^2v_3^2 + 10\omega_6^2\omega_3^3v_2^2\omega_7\omega_4^2v_3^2 - \\
& 2\omega_6^2\omega_3^3c_s^4\omega_7^2\omega_4^2 - 8\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^2 - 4\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_1^2v_3^2 - 4\omega_6\omega_3^3v_2^2\omega_7^2\omega_1^3v_3^2 - 4\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^3 + \omega_6^2\omega_3^3c_s^4\omega_7\omega_4^3 - 36\omega_6^2\omega_3^3v_2^2\omega_7^2\omega_1^2v_3^2 - \\
& 38\omega_6^2\omega_3^3v_2^2\omega_7\omega_4^2v_3^2 + 10\omega_6\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 + 4\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^3c_s^4\omega_7^2\omega_4^2 - 3\omega_6^2\omega_3^3c_s^2v_2^2\omega_7\omega_4^3 - 8\omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^2v_3^2 - 3\omega_6\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 + \\
& 20\omega_6^2\omega_3^3v_2^2\omega_7^2\omega_1^2v_3^2 - 2\omega_6^2\omega_3^3c_s^2\omega_7\omega_4^2v_3^2 + 2\omega_6^2\omega_3^3v_2^2\omega_4^3v_3^2 + 20\omega_6^2v_2^2\omega_7^2\omega_4^3v_3^2 + 12\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^2 + 2\omega_3^3c_s^2\omega_7^2\omega_1^2v_3^2 + 20\omega_6^2\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 - \\
& 4\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 - 4\omega_6^2\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^2 + \omega_6^2\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 - 3\omega_6^2\omega_3^3v_2^2\omega_7\omega_4^2v_3^2 + 4\omega_6^2\omega_3^3c_s^4\omega_7\omega_4^2 + 4\omega_6\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^2 - 2\omega_6^2\omega_3^3c_s^2\omega_7\omega_4^3v_3^2 - \\
& 4\omega_6^2\omega_3^3v_2^2\omega_4^3v_3^2 - 2\omega_6\omega_3^3c_s^2v_2^2\omega_7^2\omega_4^3 - 38\omega_6^2\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2 + 2\omega_6\omega_3^3c_s^2\omega_7^2\omega_4^3v_3^2 - 2\omega_6^2\omega_3^3c_s^4\omega_7\omega_4^3 - 4\omega_6^2\omega_3^3c_s^2v_2^2\omega_7\omega_4^3 - 4\omega_6\omega_3^3v_2^2\omega_7^2\omega_4^3v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{65} = & -12\omega_3^3c_s^2\omega_7\omega_4 - 12\omega_3^3c_s^2\omega_7^2 + 34\omega_3^3\omega_7^2\omega_1^2v_3^2 + 6\omega_3^3\omega_3^3v_3^2 - 12\omega_3^3\omega_7\omega_4v_3^2 + 22\omega_3^3\omega_7^2\omega_4^2v_3^2 + 12\omega_7^2\omega_3^3v_3^2 + 6\omega_3c_s^2\omega_7^2\omega_4^3 - 12\omega_3^3\omega_4^2v_3^2 - \\
& 4\omega_3^3\omega_7^2\omega_4^3v_3^2 - 6\omega_3^3c_s^2\omega_7\omega_4^3 - 12\omega_3^3c_s^2\omega_4^2 - 12\omega_3c_s^2\omega_7^2\omega_4^2 - 48\omega_3^3\omega_7^2\omega_1^2v_3^2 + 6\omega_3^3c_s^2\omega_4^3 + 24\omega_3^3c_s^2\omega_7\omega_4^2 + 24\omega_7^2\omega_4^2v_3^2 - 14\omega_3^3c_s^2\omega_7^2\omega_4^2 - 6\omega_3^3\omega_7\omega_4^3v_3^2 - \\
& 30\omega_3\omega_7^2\omega_4^3v_3^2 + \omega_3^3c_s^2\omega_7^2\omega_4^3 + 24\omega_3^3\omega_7\omega_4^2v_3^2 - 6\omega_3^3c_s^2\omega_7^2\omega_4^3 + 24\omega_3^3c_s^2\omega_7\omega_4^2 - 78\omega_3^3\omega_7^2\omega_4^2v_3^2 + 12\omega_3^3c_s^2\omega_7^2\omega_4^3 + 24\omega_3\omega_7^2\omega_1^2v_3^2 + 48\omega_3^3\omega_7^2v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{66} = & -6\omega_6\omega_3^3v_2^2\omega_4^3 - 6\omega_6^2\omega_3^3c_s^2\omega_4^2 - 48\omega_6^2\omega_3^3v_2^2\omega_4^2 + 24\omega_6\omega_3^3c_s^2\omega_4^3 + \omega_6^2\omega_3^3c_s^2\omega_4^3 + 34\omega_6^2\omega_3^3v_2^2\omega_4^3 + 24\omega_6^2\omega_3c_s^2\omega_4^3 - 12\omega_6^2c_s^2\omega_4^3 - 12\omega_6\omega_3^3v_2^2\omega_4^3 + \\
& 24\omega_6^2\omega_3^3v_2^2\omega_4^2 + 6\omega_6^2\omega_3^3c_s^2\omega_4^2 - 12\omega_6^2v_2^2\omega_4^3 + 6\omega_3^3c_s^2\omega_4^3 - 4\omega_6^2\omega_3^3v_2^2\omega_4^3 - 14\omega_6^2\omega_3^3c_s^2\omega_4^3 + 12\omega_6^2\omega_3^3v_2^2\omega_4^2 - 6\omega_6\omega_3^3c_s^2\omega_4^3 + 24\omega_6\omega_3^3v_2^2\omega_4^3 + \\
& 12\omega_6^2\omega_3^3c_s^2\omega_4^2 - 12\omega_6^2c_s^2\omega_4^3 + 6\omega_3^3v_2^2\omega_4^3 + 24\omega_6^2\omega_3^3v_2^2\omega_4^2 - 12\omega_6\omega_3^3c_s^2\omega_4^3 - 12\omega_6^2\omega_3^3c_s^2\omega_4^2 - 30\omega_6^2\omega_3^3v_2^2\omega_4^2 + 48\omega_6^2v_2^2\omega_4^3 - 78\omega_6^2\omega_3^3v_2^2\omega_4^3
\end{aligned}$$

$$\begin{aligned}
C_{67} = & 24c_s^2\omega_7\omega_4 + 27\omega_7^2\omega_4^2v_3^2 + 12\omega_7^2\omega_4 + 48\omega_7\omega_4v_3^2 - 3\omega_7^2\omega_4^3v_3^2 + 9c_s^2\omega_7\omega_4^3 - 11\omega_7^2\omega_4^2 + 6\omega_4^3 - 36c_s^2\omega_7\omega_4^2 - 12\omega_4^2 + 12\omega_7^2v_3^2 + \omega_7^2\omega_4^3 + 25c_s^2\omega_7^2\omega_4^2 + \\
& 24c_s^2\omega_7^2 + 15\omega_7\omega_4^3v_3^2 - 6\omega_4^3v_3^2 - 9\omega_7\omega_4^3 - 2c_s^2\omega_7^2\omega_4^3 + 36\omega_7\omega_4^2 + 12\omega_4^2v_3^2 - 24\omega_7\omega_4 - 60\omega_7\omega_4^2v_3^2 + 12c_s^2\omega_4^2 - 48c_s^2\omega_7\omega_4 - 6c_s^2\omega_4^3 - 42\omega_7^2\omega_4^2v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{68} = & 42\omega_3^3c_s^2\omega_7\omega_4^2 - 3\omega_3^3\omega_4^3 - 6\omega_3^3\omega_7^2\omega_4 - 12\omega_2^2c_s^2\omega_7^2\omega_4^2 - 12\omega_2^2\omega_7^2\omega_4^2v_3^2 - 3\omega_2^2\omega_7\omega_4^3 + 6\omega_3^3\omega_4^2 - 12\omega_3^3c_s^2\omega_7\omega_4^3 + 6\omega_2^2\omega_7\omega_4^2 + 6\omega_2^2c_s^2\omega_7^2\omega_4^3 + \\
& 6\omega_2^2c_s^2\omega_7\omega_4^3 + 6\omega_7^2\omega_3^3v_3^2 + 24\omega_2^2\omega_7^2v_3^2 + 6\omega_2^2\omega_7^2\omega_4^3v_3^2 - \omega_2^2\omega_7^2\omega_4^3 - 24\omega_2^2\omega_7\omega_4^3v_3^2 + 7\omega_3^3\omega_7^2\omega_4^2 - 12\omega_2^2c_s^2\omega_7\omega_4^2 - 24\omega_2^2c_s^2\omega_7\omega_4 + 6\omega_2^2\omega_7^2\omega_4^3v_3^2 + \\
& 6\omega_2^2\omega_7\omega_4^3v_3^2 - 21\omega_2^2\omega_7\omega_4^2 + 42\omega_2^2c_s^2\omega_7^2\omega_4^2 + 6\omega_2^2\omega_7^2\omega_4^3v_3^2 + 78\omega_2^2c_s^2\omega_7^2\omega_4^2 - 30\omega_2^2\omega_7^2\omega_4^3v_3^2 - 12\omega_2^2c_s^2\omega_7^2\omega_4^3 + 6\omega_3^3\omega_7\omega_4^2 + 6\omega_2^2\omega_4^3v_3^2 + 42\omega_2^2\omega_7\omega_4^2v_3^2 - \\
& 36\omega_3^3c_s^2\omega_7^2 + 6\omega_2^2c_s^2\omega_4^3 + 6\omega_2^2c_s^2\omega_7^2\omega_4^3 - 12\omega_2\omega_7^2\omega_4^3v_3^2 - 3\omega_2^2\omega_7^2\omega_4^2 - 12\omega_2^2\omega_7\omega_4^3v_3^2 - 12\omega_2^2c_s^2\omega_4^2 - 48\omega_2^2c_s^2\omega_7^2\omega_4^2 - 12\omega_3^3\omega_7\omega_4^3v_3^2 - 12\omega_3^3\omega_4^2v_3^2 + \\
& 12\omega_2^2\omega_7\omega_4 + 12\omega_2^2\omega_7^2\omega_4^3v_3^2 - 24\omega_2^2c_s^2\omega_7^2\omega_4 + \omega_2^2\omega_7^2\omega_4^3
\end{aligned}$$

$$\begin{aligned}
C_{69} = & -36c_s^2\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 12\omega_7^2\omega_4 - 36\omega_7\omega_4v_3^2 + \omega_7^2\omega_4^3v_3^2 - 12c_s^2\omega_7\omega_4^3 + 11\omega_7^2\omega_4^2 - 6\omega_4^3 + 48c_s^2\omega_7\omega_4^2 + 12\omega_4^2 + 12\omega_7^2v_3^2 - \omega_7^2\omega_4^3 - \\
& 44c_s^2\omega_7^2\omega_4^2 - 48c_s^2\omega_7^2 - 12\omega_7\omega_4^3v_3^2 + 6\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 4c_s^2\omega_7^2\omega_4^3 - 36\omega_7\omega_4^2 - 12\omega_4^2v_3^2 + 24\omega_7\omega_4 + 48\omega_7\omega_4^2v_3^2 - 12c_s^2\omega_4^2 + 90c_s^2\omega_7^2\omega_4 + 6c_s^2\omega_4^3
\end{aligned}$$

$$\begin{aligned}
C_{70} = & 36\omega_3^3c_s^2\omega_7\omega_4^2 - 12\omega_2^2c_s^2\omega_7^2\omega_4^2 + 12\omega_2^2\omega_7^2\omega_4^2v_3^2 - 6\omega_2^2\omega_7\omega_4^3 + 3\omega_2^2\omega_7^2\omega_4^3v_3^2 - 12\omega_3^3c_s^2\omega_7\omega_4^3 + 12\omega_2^2\omega_7\omega_4^2 + 6\omega_2^2c_s^2\omega_7^2\omega_4^3 + 12\omega_2^2c_s^2\omega_7\omega_4^3 + \\
& 12\omega_2^2\omega_4^3v_3^2 + 24\omega_2^2\omega_7^2v_3^2 - \omega_2^2\omega_7^2\omega_4^3 - 12\omega_2^2\omega_7\omega_4^3v_3^2 + 3\omega_2^2\omega_7^2\omega_4^2 - 24\omega_2^2c_s^2\omega_7\omega_4^2 - 12\omega_2^2c_s^2\omega_7\omega_4 + 12\omega_2^2\omega_7\omega_4^3v_3^2 - 6\omega_2^2\omega_7\omega_4^2 + 48\omega_2^2c_s^2\omega_7^2\omega_4^2 + \\
& 36\omega_2^2c_s^2\omega_7^2\omega_4 - 30\omega_2^2\omega_7^2\omega_4^3v_3^2 - 12\omega_2^2c_s^2\omega_7^2\omega_4^3 + 3\omega_2^2\omega_7\omega_4^3 + 6\omega_2^2\omega_4^3v_3^2 + 36\omega_2^2\omega_7\omega_4^2v_3^2 - 12\omega_2^2c_s^2\omega_7^2 + 6\omega_2^2c_s^2\omega_4^3 + 4\omega_2^2c_s^2\omega_7^2\omega_4^3 - 18\omega_2^2\omega_7^2\omega_4^3v_3^2 - \\
& 6\omega_2^2\omega_7^2\omega_4^2 - 24\omega_2^2\omega_7\omega_4^3v_3^2 - 12\omega_2^2c_s^2\omega_4^2 - 32\omega_2^2c_s^2\omega_7^2\omega_4^2 - 12\omega_2^2\omega_7\omega_4^3v_3^2 - 12\omega_2^2\omega_4^3v_3^2 - 24\omega_2^2c_s^2\omega_7^2\omega_4 + 2\omega_2^2\omega_7^2\omega_4^3
\end{aligned}$$

$$\begin{aligned}
C_{71} = & -24\omega_3^3c_s^2\omega_7\omega_4 - 36\omega_3^3c_s^2\omega_7^2 + 6\omega_3^3\omega_7^2\omega_4^2v_3^2 + 6\omega_3^3\omega_4^3v_3^2 + 6\omega_3^3\omega_7\omega_4^3 - 12\omega_3^3c_s^2\omega_7\omega_4^2 - 24\omega_3^3\omega_7\omega_4^3v_3^2 + 6\omega_3^3c_s^2\omega_7\omega_4^3 - 21\omega_3^3\omega_7\omega_4^2 + \\
& 6\omega_3^3\omega_7^2\omega_4^3v_3^2 + \omega_3^3\omega_7^2\omega_4^3 + 6\omega_7^2\omega_4^3v_3^2 + 6\omega_3c_s^2\omega_7^2\omega_4^3 - 12\omega_3^3\omega_7^2v_3^2 + 12\omega_3^3\omega_7\omega_4 - 3\omega_3^3\omega_4^3 - 12\omega_3^3c_s^2\omega_7\omega_4^3 - 12\omega_3^3\omega_4^2 - 12\omega_3c_s^2\omega_7^2\omega_4^2 - \\
& 12\omega_3^3\omega_7^2\omega_4^3v_3^2 - 3\omega_3^3\omega_7^2\omega_4^2 + 6\omega_3^3c_s^2\omega_4^3 + 42\omega_3^3c_s^2\omega_7\omega_4^2 + 6\omega_3^3\omega_4^2 + 12\omega_3^3\omega_7^2\omega_4^3v_3^2 + 6\omega_3^3\omega_7\omega_4^2 - 24\omega_3^3c_s^2\omega_7^2\omega_4 - 48\omega_3^3c_s^2\omega_7^2\omega_4^2 - 12\omega_3^3\omega_7\omega_4^3v_3^2 - \\
& 12\omega_3\omega_7^2\omega_4^3v_3^2 - 3\omega_3^3\omega_7\omega_4^3 - 6\omega_3^3\omega_7^2\omega_4 - 12\omega_3^3\omega_7\omega_4^2v_3^2 + 6\omega_3^3c_s^2\omega_7^2\omega_4^3 + 42\omega_3^3\omega_7\omega_4^2v_3^2 - 12\omega_3^3c_s^2\omega_7^2\omega_4^3 + 7\omega_3^3\omega_7^2\omega_4^2 + 78\omega_3^3c_s^2\omega_7\omega_4 - 30\omega_3^3\omega_7^2\omega_4^3v_3^2 + \\
& 6\omega_3^3\omega_7\omega_4^3v_3^2 - \omega_3^3\omega_7^2\omega_4^3 + 42\omega_3^3c_s^2\omega_7^2\omega_4^2 + 6\omega_3\omega_7^2\omega_4^3v_3^2 + 24\omega_3^3\omega_7^2v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{72} = & -36c_s^2\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 12\omega_7^2\omega_4 - 36\omega_7\omega_4v_3^2 + \omega_7^2\omega_4^3v_3^2 - 12c_s^2\omega_7\omega_4^3 + 11\omega_7^2\omega_4^2 - 6\omega_4^3 + 48c_s^2\omega_7\omega_4^2 + 12\omega_4^2 + 12\omega_7^2v_3^2 - \omega_7^2\omega_4^3 - \\
& 44c_s^2\omega_7^2\omega_4^2 - 48c_s^2\omega_7^2 - 12\omega_7\omega_4^3v_3^2 + 6\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 4c_s^2\omega_7^2\omega_4^3 - 36\omega_7\omega_4^2 - 12\omega_4^2v_3^2 + 24\omega_7\omega_4 + 48\omega_7\omega_4^2v_3^2 - 12c_s^2\omega_4^2 + 90c_s^2\omega_7^2\omega_4 + 6c_s^2\omega_4^3
\end{aligned}$$

$$\begin{aligned}
C_{73} = & -12\omega_3^3c_s^2\omega_7\omega_4 - 12\omega_3^3c_s^2\omega_7^2 + 6\omega_3^3\omega_4^3v_3^2 + 3\omega_3^3\omega_7\omega_4^3 - 24\omega_3^3c_s^2\omega_7\omega_4^2 - 12\omega_3^3\omega_7\omega_4^3v_3^2 + 12\omega_3^3c_s^2\omega_7\omega_4^3 - 6\omega_3^3\omega_7\omega_4^2 + 2\omega_2^2\omega_7^2\omega_4^3 + \\
& 12\omega_7^2\omega_4^3v_3^2 + 6\omega_3c_s^2\omega_7^2\omega_4^3 - 12\omega_3^3\omega_4^2v_3^2 + 3\omega_3^3\omega_7^2\omega_4^3v_3^2 - 12\omega_3^3c_s^2\omega_7\omega_4^3 - 12\omega_3^3c_s^2\omega_4^2 - 12\omega_3c_s^2\omega_7^2\omega_4^2 + 12\omega_3^3\omega_7^2\omega_4^3v_3^2 - 6\omega_3^3\omega_7^2\omega_4^2 + 6\omega_3^3c_s^2\omega_4^3 + \\
& 36\omega_3^3c_s^2\omega_7\omega_4^2 + 12\omega_2^2\omega_7\omega_4^2 - 24\omega_3^3c_s^2\omega_7^2\omega_4 - 32\omega_3^3c_s^2\omega_7^2\omega_4^2 - 12\omega_3^3\omega_7\omega_4^3v_3^2 - 18\omega_3\omega_7^2\omega_4^3v_3^2 - 6\omega_2^2\omega_7\omega_4^3 - 24\omega_2^2\omega_7\omega_4^2v_3^2 + 4\omega_3^3c_s^2\omega_7^2\omega_4^3 + \\
& 36\omega_3^3\omega_7\omega_4^2v_3^2 - 12\omega_3^3c_s^2\omega_7^2\omega_4^3 + 3\omega_3^3\omega_7^2\omega_4^2 + 36\omega_3^3c_s^2\omega_7^2\omega_4 - 30\omega_3^3\omega_7^2\omega_4^3v_3^2 + 12\omega_3^3\omega_7\omega_4^3v_3^2 - \omega_3^3\omega_7^2\omega_4^3 + 48\omega_3^3c_s^2\omega_7^2\omega_4^2 + 24\omega_3^3\omega_7^2v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{74} = & 72\omega_7\omega_4^2v_3^4 + 6c_s^4\omega_7\omega_4^3 - 24c_s^2\omega_1^2v_3^2 - 24\omega_1^2v_3^4 - 24c_s^2\omega_7\omega_4 + 24\omega_7^2\omega_4^2v_3^2 - 24c_s^4\omega_7\omega_4^2 - 12c_s^2\omega_7\omega_4^3v_3^2 + 24\omega_7^2\omega_4^4v_3^2 + 24c_s^4\omega_7^2 + 48\omega_7\omega_4^2v_3^2 - \\
& 3\omega_7^2\omega_4^3v_3^2 + 12\omega_4^3v_3^4 + 12c_s^2\omega_4^3v_3^2 - 6c_s^2\omega_7\omega_4^3 + 24c_s^4\omega_7\omega_4 + 156c_s^2\omega_7^2\omega_4^3v_3^2 - 18\omega_7\omega_4^3v_3^4 + 24c_s^2\omega_7\omega_4^2 + 48c_s^2\omega_7\omega_4^2v_3^2 - 8c_s^2\omega_7^2\omega_4^2 + 18\omega_7\omega_4^3v_3^2 + \\
& 3\omega_7^2\omega_4^3v_3^2 - 24c_s^2\omega_7\omega_4^2v_3^2 - 12\omega_4^2v_3^2 - 96c_s^2\omega_7^2v_3^2 + c_s^2\omega_7^2\omega_4^3 - 48c_s^4\omega_7^2\omega_4 - 72c_s^2\omega_7^2\omega_4^3v_3^2 + 24\omega_4^2v_3^2 + 24c_s^4\omega_7^2\omega_4^2 - 24\omega_7^2\omega_4^2v_3^2 - 72\omega_7\omega_4^2v_3^2 - \\
& 48\omega_7\omega_4^2v_3^4 + 6c_s^2\omega_7^2\omega_4^3v_3^2 - 3c_s^4\omega_7^2\omega_4^3 + 12c_s^2\omega_7^2\omega_4 - 24\omega_7^2\omega_4^2v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{75} = & -12c_s^2\omega_7\omega_4 - 16\omega_7^2\omega_4^2v_3^2 - 6\omega_7^2\omega_4 - 12\omega_7\omega_4v_3^2 + 2\omega_7^2\omega_4^3v_3^2 - 6c_s^2\omega_7\omega_4^3 + 8\omega_7^2\omega_4^2 - 6\omega_4^3 + 24c_s^2\omega_7\omega_4^2 + 12\omega_4^2 - 12\omega_7^2v_3^2 - \omega_7^2\omega_4^3 - 20c_s^2\omega_7^2\omega_4^2 - \\
& 24c_s^2\omega_7^2 - 6\omega_7\omega_4^3v_3^2 + 6\omega_4^3v_3^2 + 6\omega_7\omega_4^3 + c_s^2\omega_7^2\omega_4^3 - 24\omega_7\omega_4^2 - 12\omega_4^2v_3^2 + 12\omega_7\omega_4 + 24\omega_7\omega_4^2v_3^2 - 12c_s^2\omega_4^2 + 42c_s^2\omega_7^2\omega_4 + 6c_s^2\omega_4^3 + 24\omega_7\omega_4^2v_3^2
\end{aligned}$$

2.4 CLBM1

2.4.1 Definitions

Collision operator C :

$$C(f) = \mathbf{K}^{-1}\mathbf{S}\left(\kappa^{(eq)} - \mathbf{K}f\right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2).$$

Matrix \mathbf{K} corresponds to the transformation matrix to the central moment basis defined as

$$\boldsymbol{\kappa} = (k_{(0,0,0)}, k_{(1,0,0)}, k_{(0,1,0)}, k_{(0,0,1)}, k_{(2,0,0)}, k_{(0,2,0)}, k_{(0,0,2)})^T,$$

and is given by

$$\mathbf{K} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ -v_1 & 1-v_1 & -v_1 & -v_1 & -v_1-1 & -v_1 & -v_1 \\ -v_2 & -v_2 & 1-v_2 & -v_2 & -v_2 & -v_2-1 & -v_2 \\ -v_3 & -v_3 & -v_3 & 1-v_3 & -v_3 & -v_3 & -v_3-1 \\ v_1^2 & (1-v_1)^2 & v_1^2 & v_1^2 & (v_1+1)^2 & v_1^2 & v_1^2 \\ v_2^2 & v_2^2 & (1-v_2)^2 & v_2^2 & v_2^2 & (v_2+1)^2 & v_2^2 \\ v_3^2 & v_3^2 & v_3^2 & (1-v_3)^2 & v_3^2 & v_3^2 & (v_3+1)^2 \end{pmatrix}.$$

The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K}\mathbf{M}^{-1}\boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = (\rho, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2)^T.$$

2.4.2 Conservation of mass equation



attached text file: output_d3q7_ade_clbm1_symbolic_pde_00.txt

$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{\delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\ & (-2 + \omega_2) \frac{\delta_l^2 v_1}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\delta_l^2 \rho}{2\omega_2 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{\delta_l^2 v_2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{\delta_l^2 v_1}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\ & (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{\delta_l^2 \rho}{\omega_2 \omega_3 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{\delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_2 - \omega_2 \omega_4 + \omega_4) \frac{\delta_l^2 v_1}{\omega_2 \delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\ & (\omega_2 - \omega_2 \omega_4 + \omega_4) \frac{\delta_l^2 \rho}{\omega_2 \delta_t \omega_4} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{\delta_l^2 v_2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{\delta_l^2 v_1}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + \\ & + (-2 + \omega_3) \frac{\delta_l^2 v_2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\delta_l^2 \rho}{2\omega_3 \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{\delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (-\omega_3 \omega_4 + \omega_3 + \omega_4) \frac{\delta_l^2 v_2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\ & + (-\omega_3 \omega_4 + \omega_3 + \omega_4) \frac{\delta_l^2 \rho}{\omega_3 \delta_t \omega_4} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + (\omega_2 - \omega_2 \omega_4 + \omega_4) \frac{\delta_l^2 v_3}{\omega_2 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + \\ & (2 - \omega_2) \frac{\delta_l^2 v_1}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-\omega_3 \omega_4 + \omega_3 + \omega_4) \frac{\delta_l^2 v_3}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{\delta_l^2 v_2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{\delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + \\ & (-2 + \omega_4) \frac{\delta_l^2 \rho}{2\delta_t \omega_4} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\delta_l \rho}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{\delta_l^2 c_s^2}{2\omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{\delta_l^2 v_1 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\delta_l \rho}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + \\ & + (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{\delta_l^2 v_1 v_2}{\omega_2 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{\delta_l^2 v_2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{\delta_l^2 v_1 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{\delta_l^2 c_s^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\ & (-2 + \omega_3) \frac{\delta_l^2 v_2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\delta_l \rho}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + (\omega_2 - \omega_2 \omega_4 + \omega_4) \frac{\delta_l^2 v_1 v_3}{\omega_2 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{\delta_l^2 v_3 \rho}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\ & (2 - \omega_2) \frac{\delta_l^2 v_1 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-\omega_3 \omega_4 + \omega_3 + \omega_4) \frac{\delta_l^2 v_2 v_3}{\omega_3 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{\delta_l^2 v_3 \rho}{2\delta_t \omega_4} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{\delta_l^2 v_2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + \\ & (-2 + \omega_4) \frac{\delta_l^2 c_s^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{\delta_l^2 v_3 \rho}{2\delta_t \omega_4} \frac{\partial^2 v_3}{\partial x_3^2} + (12 - 12\omega_2 + \omega_2^2) \frac{\delta_l \delta_t \rho}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 - 12\omega_2 + \omega_2^2) \frac{\delta_l^2 v_1 \rho}{6\omega_2^2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + \\ & C_1 \frac{\delta_l^3 v_1}{6\omega_5 \omega_2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + (12 - 12\omega_3 + \omega_3^2) \frac{\delta_l \delta_t \rho}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + \end{aligned}$$

$$\begin{aligned}
& (-6\omega_2 - 6\omega_3 - 2\omega_2\omega_3^2 + 3\omega_3^2 + 9\omega_2\omega_3) \frac{\delta_l^2 v_2 \rho}{6\omega_2\omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + (-2\omega_2^2\omega_3 - 6\omega_2 + 3\omega_2^2 - 6\omega_3 + 9\omega_2\omega_3) \frac{\delta_l^2 v_1 \rho}{6\omega_2^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + \\
& C_3 \frac{\delta_l^3 v_2}{2\omega_5\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (-6\omega_2^2\omega_3 + \omega_2^2\omega_3^2 + 6\omega_2^2 - 6\omega_2\omega_3^2 + 6\omega_3^2) \frac{\delta_l^3 v_1 v_2 \rho}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (-12\omega_5 v_1^2 + 6\omega_2^2 c_s^2 - 3\omega_5\omega_2^2 c_s^2 - 12\omega_5 c_s^2 - 6\omega_2^2 v_1^2 + \omega_5\omega_2^2 v_1^2 + 6\omega_5\omega_2 v_1^2 + 12\omega_2 v_1^2 + 18\omega_5\omega_2 c_s^2 - 12\omega_2 c_s^2) \frac{\delta_l^3 \rho}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} \\
& + (12 - 12\omega_3 + \omega_3^2) \frac{\delta_l^2 v_2 \rho}{6\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{\delta_l^3 v_1}{2\omega_2^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (-12\omega_6 c_s^2 + 6\omega_6\omega_3 v_2^2 + 6\omega_3^2 c_s^2 - 6\omega_3^2 v_2^2 + 18\omega_6\omega_3 c_s^2 - 12\omega_6 v_2^2 + 12\omega_3 v_2^2 - 3\omega_6\omega_3^2 c_s^2 + \omega_6\omega_3^2 v_2^2 - 12\omega_3 c_s^2) \frac{\delta_l^3 \rho}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} \\
& + (-6\omega_2^2\omega_3 + \omega_2^2\omega_3^2 + 6\omega_2^2 - 6\omega_2\omega_3^2 + 6\omega_3^2) \frac{\delta_l^3 v_1 v_2 \rho}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{\delta_l^3 v_2}{6\omega_6\omega_3\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\delta_l^3 \rho}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 + \omega_4^2 - 12\omega_4) \frac{\delta_l \delta_t \rho}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-2\omega_2\omega_4^2 - 6\omega_2 + 3\omega_4^2 + 9\omega_2\omega_4 - 6\omega_4) \frac{\delta_l^2 v_3 \rho}{6\omega_2\omega_4^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (-6\omega_2 + 3\omega_2^2 + 9\omega_2\omega_4 - 2\omega_2^2\omega_4 - 6\omega_4) \frac{\delta_l^2 v_1 \rho}{6\omega_2^2\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{\delta_l^3 v_3}{2\omega_5\omega_2^2\delta_t\omega_4^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (-6\omega_2\omega_4^2 + 6\omega_2^2 + 6\omega_4^2 - 6\omega_2^2\omega_4 + \omega_2^2\omega_4^2) \frac{\delta_l^3 v_1 v_3 \rho}{6\omega_2^2\delta_t\omega_4^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\
& (-12\omega_5 v_1^2 + 6\omega_2^2 c_s^2 - 3\omega_5\omega_2^2 c_s^2 - 12\omega_5 c_s^2 - 6\omega_2^2 v_1^2 + \omega_5\omega_2^2 v_1^2 + 6\omega_5\omega_2 v_1^2 + 12\omega_2 v_1^2 + 18\omega_5\omega_2 c_s^2 - 12\omega_2 c_s^2) \frac{\delta_l^3 \rho}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} \\
& + (-2\omega_3\omega_4^2 + 9\omega_3\omega_4 + 3\omega_4^2 - 6\omega_3 - 6\omega_4) \frac{\delta_l^2 v_3 \rho}{6\omega_3\omega_4^2} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (9\omega_3\omega_4 - 6\omega_3 - 2\omega_3^2\omega_4 + 3\omega_3^2 - 6\omega_4) \frac{\delta_l^2 v_2 \rho}{6\omega_3^2\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (-2\omega_2^2\omega_3^2\omega_4 + \omega_2^2\omega_3^2 + \omega_2\omega_3\omega_4^2 + \omega_2^2\omega_3^2\omega_4^2 - 2\omega_2^2\omega_3\omega_4^2 - 2\omega_2\omega_3^2\omega_4^2 + \omega_2\omega_3^2\omega_4 + \omega_3^2\omega_4^2 + \omega_2^2\omega_3\omega_4 + \omega_2^2\omega_4^2) \frac{2\delta_l^3 v_1 v_2 v_3}{\omega_2^2\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (-6\omega_3\omega_4^2 + 6\omega_3\omega_4 + 3\omega_4^2 - 6\omega_3^2\omega_4 + 3\omega_3^2 + 2\omega_3^2\omega_4^2) \frac{\delta_l^3 v_2 v_3 \rho}{3\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2\omega_4^2 + 3\omega_2^2 + 3\omega_4^2 + 6\omega_2\omega_4 - 6\omega_2^2\omega_4 + 2\omega_2^2\omega_4^2) \frac{\delta_l^3 v_1 v_3 \rho}{3\omega_2^2\delta_t\omega_4^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2^2\omega_3 + 2\omega_2^2\omega_3^2 + 3\omega_2^2 - 6\omega_2\omega_3^2 + 3\omega_3^2 + 6\omega_2\omega_3) \frac{\delta_l^3 v_1 v_2 \rho}{3\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{\delta_l^3 v_3}{2\omega_6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_3\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4 + 6\omega_3^2 + \omega_3^2\omega_4^2) \frac{\delta_l^3 v_2 v_3 \rho}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& (-12\omega_6 c_s^2 + 6\omega_6\omega_3 v_2^2 + 6\omega_3^2 c_s^2 - 6\omega_3^2 v_2^2 + 18\omega_6\omega_3 c_s^2 - 12\omega_6 v_2^2 + 12\omega_3 v_2^2 - 3\omega_6\omega_3^2 c_s^2 + \omega_6\omega_3^2 v_2^2 - 12\omega_3 c_s^2) \frac{\delta_l^3 \rho}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} \\
& + (12 + \omega_4^2 - 12\omega_4) \frac{\delta_l^2 v_3 \rho}{6\omega_4^2} \frac{\partial^3 v_3}{\partial t \partial x_3^2} + C_9 \frac{\delta_l^3 v_1}{2\omega_2^2\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (-12v_3^2\omega_7 - 12c_s^2\omega_7 + 12v_3^2\omega_4 - 12c_s^2\omega_4 + 6c_s^2\omega_4^2 - 6v_3^2\omega_4^2 + 6v_3^2\omega_7\omega_4 + 18c_s^2\omega_7\omega_4 - 3c_s^2\omega_7\omega_4^2 + v_3^2\omega_7\omega_4^2) \frac{\delta_l^3 \rho}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} \\
& + (-6\omega_2\omega_4^2 + 6\omega_2^2 + 6\omega_4^2 - 6\omega_2^2\omega_4 + \omega_2^2\omega_4^2) \frac{\delta_l^3 v_1 v_3 \rho}{6\omega_2^2\delta_t\omega_4^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{\delta_l^3 v_2}{2\omega_3^2\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& (-12v_3^2\omega_7 - 12c_s^2\omega_7 + 12v_3^2\omega_4 - 12c_s^2\omega_4 + 6c_s^2\omega_4^2 - 6v_3^2\omega_4^2 + 6v_3^2\omega_7\omega_4 + 18c_s^2\omega_7\omega_4 - 3c_s^2\omega_7\omega_4^2 + v_3^2\omega_7\omega_4^2) \frac{\delta_l^3 \rho}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + (-6\omega_3\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4 + 6\omega_3^2 + \omega_3^2\omega_4^2) \frac{\delta_l^3 v_2 v_3 \rho}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{\delta_l^3 v_3}{6\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\delta_l^3 \rho}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2 + 3\omega_2 - \omega_2^2) \frac{\delta_l \delta_t^2 \rho}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-2 + 3\omega_2 - \omega_2^2) \frac{3\delta_l^2 v_1 \delta_t \rho}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\delta_l^3 \rho}{12\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_l^4}{24\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{\delta_l^4 v_1 \rho}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 + 3\omega_3 - \omega_3^2) \frac{\delta_l \delta_t^2 \rho}{2\omega_3^2} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (-24\omega_2^2\omega_3 + 13\omega_2^2\omega_3^2 + 12\omega_2^2 - \omega_2^2\omega_3^3 + 7\omega_2\omega_3^3 - 24\omega_2\omega_3^2 + 12\omega_3^2 + 12\omega_2\omega_3 - 6\omega_3^3) \frac{\delta_l^2 v_2 \delta_t \rho}{12\omega_2^2\omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-\omega_3^2\omega_3^2 - 24\omega_2^2\omega_3 + 13\omega_2^2\omega_3^2 + 12\omega_2^2 + 7\omega_2^3\omega_3 - 6\omega_2^2 - 24\omega_2\omega_3^2 + 12\omega_3^2 + 12\omega_2\omega_3) \frac{\delta_l^2 v_1 \delta_t \rho}{12\omega_2^2\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-7\omega_3^2\omega_3^2 - 6\omega_2^2\omega_3 + \omega_3^2\omega_3^3 + 6\omega_2^2\omega_3^2 + 12\omega_3^2\omega_3 - 7\omega_2^2\omega_3^3 - 6\omega_2^2 + 18\omega_2\omega_3^3 - 12\omega_3^3) \frac{\delta_l^3 v_1 v_2 \rho}{6\omega_2^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + \\
& C_{16} \frac{\delta_l^3 \rho}{12\omega_5^2\omega_2^2\omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{\delta_l^4 v_1 v_2}{6\omega_5^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{18} \frac{\delta_l^4 v_2 \rho}{12\omega_5^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{\delta_l^4 v_1 \rho}{12\omega_5^2\omega_2^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + 3\omega_3 - \omega_3^2) \frac{3\delta_l^2 v_2 \delta_t \rho}{2\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + C_{20} \frac{\delta_l^3 \rho}{12\omega_2\omega_6^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (-7\omega_3^2\omega_3^2 + \omega_3^2\omega_3^3 + 6\omega_2^2\omega_3^2 + 18\omega_2^2\omega_3 - 7\omega_2^2\omega_3^3 - 12\omega_2^2 + 12\omega_2\omega_3^3 - 6\omega_2\omega_3^2 - 6\omega_3^3) \frac{\delta_l^3 v_1 v_2 \rho}{6\omega_2^2\omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{21} \frac{\delta_l^4}{4\omega_2^2\omega_2^2\omega_3^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{\delta_l^4 v_1 \rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{\delta_l^4 v_2 \rho}{12\omega_2^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{\delta_l^3 \rho}{12\omega_6^2\omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + \\
& C_{25} \frac{\delta_l^4 v_1 v_2}{6\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{26} \frac{\delta_l^4 v_2 \rho}{12\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{27} \frac{\delta_l^4 v_1 \rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{28} \frac{\delta_l^4}{24\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{29} \frac{\delta_l^4 v_2 \rho}{12\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} +
\end{aligned}$$

$$\begin{aligned}
& (-2 - \omega_4^2 + 3\omega_4) \frac{\delta_l \delta_t^2 \rho}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (-24\omega_2\omega_4^2 + 7\omega_2\omega_4^3 - 6\omega_4^3 + 12\omega_2^2 + 12\omega_4^2 + 12\omega_2\omega_4 - 24\omega_2^2\omega_4 - \omega_2^2\omega_4^3 + 13\omega_2^2\omega_4^2) \frac{\delta_l^2 \delta_t v_3 \rho}{12\omega_2^2\omega_4^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-24\omega_2\omega_4^2 + 12\omega_2^2 + 12\omega_4^2 - 6\omega_2^3 + 12\omega_2\omega_4 - 24\omega_2^2\omega_4 - \omega_2^2\omega_4^2 + 7\omega_2^3\omega_4 + 13\omega_2^2\omega_4^2) \frac{\delta_l^2 v_1 \delta_t \rho}{12\omega_2^2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& (18\omega_2\omega_4^3 - 12\omega_4^3 - 6\omega_2^3 - 6\omega_2^2\omega_4 + \omega_2^2\omega_4^3 - 7\omega_2^3\omega_4^2 + 12\omega_2^2\omega_4 - 7\omega_2^2\omega_4^3 + 6\omega_2^2\omega_4^2) \frac{\delta_l^3 v_1 v_3 \rho}{6\omega_2^3\omega_4^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + \\
& C_{30} \frac{\delta_l^3 \rho}{12\omega_5^2\omega_2^3\omega_4} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{31} \frac{\delta_l^4 v_1 v_3}{6\omega_5^2\omega_2^3\delta_t \omega_4^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{32} \frac{\delta_l^4 v_3 \rho}{12\omega_5^2\omega_2^3\delta_t \omega_4^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{33} \frac{\delta_l^4 v_1 \rho}{12\omega_5^2\omega_2^3\delta_t \omega_4^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (7\omega_3\omega_4^3 - 24\omega_3\omega_4^2 + 12\omega_3\omega_4 - 6\omega_4^3 + 12\omega_4^2 - 24\omega_3^2\omega_4 + 12\omega_3^2 + 13\omega_3^2\omega_4^2 - \omega_3^2\omega_4^3) \frac{\delta_l^2 \delta_t v_3 \rho}{12\omega_3^2\omega_4^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (-24\omega_3\omega_4^2 + 12\omega_3\omega_4 + 12\omega_4^2 - \omega_3^2\omega_4^2 - 24\omega_3^2\omega_4 + 12\omega_3^2 + 13\omega_3^2\omega_4^2 - 6\omega_3^3 + 7\omega_3^3\omega_4) \frac{\delta_l^2 v_2 \delta_t \rho}{12\omega_3^2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{\delta_l^3 v_2 v_3 \rho}{6\omega_2\omega_3^3\omega_4^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{35} \frac{\delta_l^3 v_1 v_3 \rho}{6\omega_2^3\omega_3\omega_4^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{36} \frac{\delta_l^3 v_1 v_2 \rho}{6\omega_2^3\omega_3^3\omega_4} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{37} \frac{\delta_l^4 v_2 v_3}{\omega_2^3\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{\delta_l^4 v_1 v_2 v_3 \rho}{6\omega_2^3\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\delta_l^4 v_3 \rho}{12\omega_5^2\omega_2^3\delta_t \omega_4^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{40} \frac{\delta_l^4 v_2 \rho}{12\omega_5^2\omega_2^3\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (18\omega_3\omega_4^3 - 12\omega_4^3 - 7\omega_3^3\omega_4^2 + \omega_3^3\omega_4^3 - 6\omega_2^3\omega_4 + 6\omega_2^3\omega_4^2 - 6\omega_3^3 - 7\omega_2^3\omega_4^3 + 12\omega_3^3\omega_4) \frac{\delta_l^3 v_2 v_3 \rho}{6\omega_3^3\omega_4^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{41} \frac{\delta_l^3 \rho}{12\omega_6^2\omega_3^3\omega_4} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{42} \frac{\delta_l^4 v_1 v_3}{\omega_2^3\omega_6^2\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{\delta_l^4 v_3 \rho}{12\omega_6^2\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{44} \frac{\delta_l^4 v_1 v_2 v_3 \rho}{6\omega_2^3\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\delta_l^4 v_1 \rho}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{46} \frac{\delta_l^4 v_2 v_3}{6\omega_6^2\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + C_{47} \frac{\delta_l^4 v_3 \rho}{12\omega_6^2\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_2}{\partial x_3^3 \partial x_3} + C_{48} \frac{\delta_l^4 v_2 \rho}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_3^3 \partial x_3} + \\
& (-2 - \omega_4^2 + 3\omega_4) \frac{3\delta_l^2 \delta_t v_3 \rho}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3} + C_{49} \frac{\delta_l^3 \rho}{12\omega_2\omega_7^2\omega_3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (-6\omega_2\omega_4^2 + 12\omega_2\omega_4^3 - 6\omega_4^3 - 12\omega_2^3 + \omega_2^3\omega_4^3 - 7\omega_2^3\omega_4^2 + 18\omega_2^3\omega_4 - 7\omega_2^2\omega_4^3 + 6\omega_2^2\omega_4^2) \frac{\delta_l^3 v_1 v_3 \rho}{6\omega_2^3\omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3} + \\
& C_{50} \frac{\delta_l^4}{4\omega_2^3\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{51} \frac{\delta_l^4 v_1 \rho}{12\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + C_{52} \frac{\delta_l^4 v_3 \rho}{12\omega_2^3\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + C_{53} \frac{\delta_l^3 \rho}{12\omega_3\omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3} + \\
& (12\omega_3\omega_4^3 - 6\omega_3\omega_4^2 - 6\omega_4^3 - 7\omega_3^3\omega_4^2 + \omega_3^3\omega_4^3 + 6\omega_2^3\omega_4^2 - 12\omega_3^3 - 7\omega_2^3\omega_4^3 + 18\omega_3^3\omega_4) \frac{\delta_l^3 v_2 v_3 \rho}{6\omega_3^3\omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3} + \\
& C_{54} \frac{\delta_l^4 v_1 v_2}{\omega_2^3\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{55} \frac{\delta_l^4 v_2 \rho}{12\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{56} \frac{\delta_l^4 v_1 \rho}{12\omega_2^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + C_{57} \frac{\delta_l^4 v_1 v_2 v_3 \rho}{6\omega_2^3\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + \\
& C_{58} \frac{\delta_l^4}{4\omega_2^3\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{59} \frac{\delta_l^4 v_2 \rho}{12\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{60} \frac{\delta_l^4 v_3 \rho}{12\omega_6^2\omega_3^3\delta_t \omega_4^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{61} \frac{\delta_l^3 \rho}{12\omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3} + \\
& C_{62} \frac{\delta_l^4 v_1 v_3}{6\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + C_{63} \frac{\delta_l^4 v_3 \rho}{12\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} + C_{64} \frac{\delta_l^4 v_1 \rho}{12\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} + C_{65} \frac{\delta_l^4 v_2 v_3}{6\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3} + \\
& C_{66} \frac{\delta_l^4 v_3 \rho}{12\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + C_{67} \frac{\delta_l^4 v_2 \rho}{12\omega_3^3\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3} + C_{68} \frac{\delta_l^4}{24\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_3} + C_{69} \frac{\delta_l^4 v_3 \rho}{12\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial x_3} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 + 3\omega_5 v_1^2 - 3\omega_5 - 3\omega_2 + 9\omega_5 c_s^2 - 18c_s^2 - \omega_5 \omega_2 v_1^2 + 3\omega_2 v_1^2 - 6v_1^2 - 3\omega_5 \omega_2 c_s^2 + 9\omega_2 c_s^2 + \omega_5 \omega_2 \\
C_2 &= 12\omega_5 v_1^2 + 6\omega_2 c_s^2 - 3\omega_5 \omega_2 c_s^2 + 12\omega_2 - 12\omega_5 c_s^2 + 18\omega_2 v_1^2 - 5\omega_5 \omega_2 v_1^2 - 6\omega_2^2 + 2\omega_5 \omega_2^2 + 6\omega_5 \omega_2 v_1^2 - 36\omega_2 v_1^2 + 18\omega_5 \omega_2 c_s^2 - 12\omega_2 c_s^2 - 6\omega_5 \omega_2 \\
C_3 &= -2\omega_5 \omega_2 v_1^2 \omega_3^2 + 2\omega_3 v_1^2 \omega_3^2 - 2\omega_5 \omega_3^2 c_s^2 - 2\omega_2 \omega_3^2 c_s^2 + 2\omega_5 \omega_2^2 v_1^2 + 2\omega_5 \omega_2 v_1^2 \omega_3 + 4\omega_5 \omega_2 \omega_3^2 c_s^2 + \omega_5 \omega_2^2 \omega_3 c_s^2 - \omega_5 \omega_2^2 \omega_3^2 c_s^2 - 3\omega_5 \omega_2^2 v_1^2 \omega_3 + \\
& \omega_2^2 \omega_3^2 c_s^2 - 2\omega_5 \omega_2 \omega_3 c_s^2 - \omega_2^2 v_1^2 \omega_3^2 + \omega_5 \omega_2^2 v_1^2 \omega_3^2 \\
C_4 &= 2\omega_2^2 \omega_3 v_2^2 - 3\omega_2 \omega_6 \omega_3^2 v_2^2 + 4\omega_2^2 \omega_6 \omega_3^2 c_s^2 + \omega_2 \omega_6 \omega_3^2 c_s^2 - 2\omega_2^2 \omega_6 \omega_3 v_2^2 - 2\omega_2^2 \omega_3 c_s^2 - 2\omega_2 \omega_6 \omega_3 c_s^2 + \omega_2^2 \omega_6 \omega_3^2 v_2^2 + \omega_2^2 \omega_3^2 c_s^2 - 2\omega_2^2 \omega_6 c_s^2 + \\
& 2\omega_6 \omega_3^2 v_2^2 - \omega_2^2 \omega_3^2 v_2^2 + 2\omega_2 \omega_6 \omega_3 v_2^2 - \omega_2^2 \omega_6 \omega_3^2 c_s^2 \\
C_5 &= 6 + 9\omega_6 c_s^2 + \omega_6 \omega_3 - \omega_6 \omega_3 v_2^2 - 3\omega_6 \omega_3 c_s^2 + 3\omega_6 v_2^2 - 3\omega_6 - 18c_s^2 - 3\omega_3 + 3\omega_3 v_2^2 + 9\omega_3 c_s^2 - 6v_2^2 \\
C_6 &= -12\omega_6 c_s^2 - 6\omega_6 \omega_3 + 6\omega_6 \omega_3 v_2^2 + 6\omega_3^2 c_s^2 + 18\omega_3^2 v_2^2 + 18\omega_6 \omega_3 c_s^2 + 2\omega_6 \omega_3^2 + 12\omega_6 v_2^2 + 12\omega_3 - 36\omega_3 v_2^2 - 3\omega_6 \omega_3^2 c_s^2 - 6\omega_3^2 - 5\omega_6 \omega_3^2 v_2^2 - 12\omega_3 c_s^2 \\
C_7 &= 4\omega_5 \omega_2 c_s^2 \omega_4^2 - 2\omega_2 c_s^2 \omega_4^2 - 3\omega_5 \omega_2^2 v_1^2 \omega_4 - 2\omega_5 c_s^2 \omega_4^2 - \omega_2^2 v_1^2 \omega_4^2 + \omega_5 \omega_2^2 v_1^2 \omega_4^2 + 2\omega_5 \omega_2^2 v_1^2 - 2\omega_5 \omega_2 c_s^2 \omega_4 - 2\omega_5 \omega_2 v_1^2 \omega_4^2 + 2\omega_2 v_1^2 \omega_4^2 + \\
& \omega_5 \omega_2^2 c_s^2 \omega_4 + \omega_2^2 c_s^2 \omega_4^2 - \omega_5 \omega_2^2 c_s^2 \omega_4^2 + 2\omega_5 \omega_2 v_1^2 \omega_4 \\
C_8 &= -3\omega_6 \omega_3^2 v_2^2 \omega_4 - 2\omega_6 \omega_3 c_s^2 \omega_4 - 2\omega_3 c_s^2 \omega_4^2 + 4\omega_6 \omega_3 c_s^2 \omega_4^2 + \omega_6 \omega_3^2 v_2^2 \omega_4^2 - \omega_3^2 v_2^2 \omega_4^2 + \omega_3^2 c_s^2 \omega_4^2 - \omega_6 \omega_3^2 c_s^2 \omega_4^2 - 2\omega_6 \omega_3 v_2^2 \omega_4^2 + 2\omega_3 v_2^2 \omega_4^2 - \\
& 2\omega_6 c_s^2 \omega_4^2 + 2\omega_6 \omega_3 v_2^2 \omega_4 + 2\omega_6 \omega_3^2 v_2^2 + \omega_6 \omega_3^2 c_s^2 \omega_4 \\
C_9 &= \omega_2 c_s^2 \omega_7 \omega_4^2 - 3\omega_2 v_3^2 \omega_7 \omega_4^2 + 2\omega_2 v_3^2 \omega_7 \omega_4 - 2\omega_2 c_s^2 \omega_7 \omega_4 - \omega_2^2 c_s^2 \omega_7 \omega_4^2 + 2\omega_2^2 v_3^2 \omega_4 - 2\omega_2^2 c_s^2 \omega_4 + \omega_2^2 v_3^2 \omega_7 \omega_4^2 - 2\omega_2^2 c_s^2 \omega_7 - 2\omega_2^2 v_3^2 \omega_7 \omega_4 + \\
& 2v_3^2 \omega_7 \omega_4^2 + \omega_2^2 c_s^2 \omega_4^2 + 4\omega_2^2 c_s^2 \omega_7 \omega_4 - \omega_2^2 v_3^2 \omega_4^2
\end{aligned}$$

$$C_{10} = 4\omega_3^2 c_s^2 \omega_7 \omega_4 - 2\omega_3^2 v_3^2 \omega_7 \omega_4 + \omega_3^2 v_3^2 \omega_7 \omega_4^2 - \omega_3^2 c_s^2 \omega_7 \omega_4^2 - \omega_3^2 v_3^2 \omega_4^2 - 2\omega_3 c_s^2 \omega_7 \omega_4 + \omega_3^2 c_s^2 \omega_4^2 + 2\omega_3 v_3^2 \omega_7 \omega_4 - 2\omega_3^2 c_s^2 \omega_7 - 3\omega_3 v_3^2 \omega_7 \omega_4^2 + 2v_3^2 \omega_7 \omega_4^2 + \omega_3 c_s^2 \omega_7 \omega_4^2 - 2\omega_3^2 c_s^2 \omega_4 + 2\omega_3^2 v_3^2 \omega_4$$

$$C_{11} = 6 + 3v_3^2 \omega_7 + 9c_s^2 \omega_7 + 3v_3^2 \omega_4 + 9c_s^2 \omega_4 + \omega_7 \omega_4 - 18c_s^2 - 6v_3^2 - v_3^2 \omega_7 \omega_4 - 3c_s^2 \omega_7 \omega_4 - 3\omega_7 - 3\omega_4$$

$$C_{12} = 12v_3^2 \omega_7 - 12c_s^2 \omega_7 - 36v_3^2 \omega_4 - 12c_s^2 \omega_4 + 2\omega_7 \omega_4 + 6c_s^2 \omega_4^2 - 6\omega_7 \omega_4 + 18v_3^2 \omega_4^2 - 6\omega_4^2 + 6v_3^2 \omega_7 \omega_4 + 18c_s^2 \omega_7 \omega_4 - 3c_s^2 \omega_7 \omega_4^2 + 12\omega_4 - 5v_3^2 \omega_7 \omega_4^2$$

$$C_{13} = 12\omega_3^2 c_s^2 - 36\omega_5 \omega_2^2 c_s^2 - 18\omega_3^2 v_1^2 + 27\omega_5 \omega_2^3 v_1^2 + 12\omega_2^2 \omega_2 - 48\omega_5^2 \omega_2 c_s^2 + \omega_5^2 \omega_2^3 + 36\omega_2^2 v_1^2 - 108\omega_5 \omega_2^2 v_1^2 - 12\omega_2^2 - 6\omega_3^2 c_s^2 + 9\omega_5 \omega_2^3 c_s^2 - 11\omega_5^2 \omega_2^2 + 6\omega_2^2 + 18\omega_5^2 \omega_2 v_1^2 + 36\omega_5 \omega_2^2 - 2\omega_5^2 \omega_2^2 c_s^2 + 15\omega_5^2 \omega_2^2 v_1^2 - 9\omega_5 \omega_2^3 + 72\omega_5 \omega_2 v_1^2 + 24\omega_5^2 c_s^2 - 3\omega_5^2 \omega_2^2 v_1^2 + 25\omega_5^2 \omega_2^2 c_s^2 + 24\omega_5 \omega_2 c_s^2 - 36\omega_5^2 v_1^2 - 24\omega_5 \omega_2$$

$$C_{14} = 24\omega_5 \omega_2^2 c_s^2 - 36\omega_3^2 v_1^2 + 30\omega_5 \omega_2^3 v_1^2 + 3\omega_5^2 \omega_2^3 v_1^4 - 72\omega_5 \omega_2^3 v_1^2 c_s^2 + 24\omega_5^2 \omega_2^2 c_s^4 + 108\omega_3^3 v_1^2 c_s^2 + 12\omega_5^2 \omega_2 c_s^2 + 24\omega_5 \omega_2 c_s^4 - 12\omega_5^2 \omega_2^2 v_1^2 c_s^2 - 3\omega_5^2 \omega_2^3 c_s^4 - 12\omega_5^2 \omega_2^3 v_1^4 + 72\omega_3^2 v_1^2 - 72\omega_5 \omega_2^2 v_1^2 - 6\omega_5 \omega_2^3 c_s^2 + 24\omega_5^2 c_s^4 + 72\omega_5 \omega_2 v_1^2 c_s^2 - 72\omega_3^2 v_1^4 + 72\omega_5 \omega_2^3 v_1^4 + 6\omega_5^2 \omega_2^3 v_1^2 c_s^2 + 6\omega_5 \omega_2^3 c_s^4 + \omega_5^2 \omega_2^3 c_s^2 + 12\omega_5^2 \omega_2^2 v_1^2 + 144\omega_5 \omega_2^2 v_1^2 c_s^2 - 216\omega_2^2 v_1^2 c_s^2 - 3\omega_5^2 \omega_2^3 v_1^2 - 8\omega_5^2 \omega_2^2 c_s^2 - 24\omega_5 \omega_2^2 c_s^4 + 36\omega_3^2 v_1^4 - 30\omega_5 \omega_2^3 v_1^4 - 24\omega_5 \omega_2 c_s^2 - 36\omega_5^2 \omega_2 v_1^2 c_s^2 - 48\omega_5^2 \omega_2 c_s^4$$

$$C_{15} = -60\omega_3^2 c_s^2 + 72\omega_5 \omega_2^3 c_s^2 + 42\omega_3^2 v_1^2 - 24\omega_5 \omega_2^3 v_1^2 + 6\omega_5^2 \omega_2 - 30\omega_5^2 \omega_2 c_s^2 - \omega_5^2 \omega_2^3 - 84\omega_2^2 v_1^2 + 24\omega_5 \omega_2^2 v_1^2 + 36\omega_2^2 + 30\omega_3^2 c_s^2 - 24\omega_5 \omega_2^3 c_s^2 + 2\omega_5^2 \omega_2^2 - 18\omega_3^2 - 12\omega_5^2 \omega_2 v_1^2 - 24\omega_5 \omega_2^2 + \omega_5^2 \omega_2^3 c_s^2 + 2\omega_5^2 \omega_2^2 v_1^2 + 12\omega_5 \omega_2^2 + 60\omega_5 \omega_2 v_1^2 + 24\omega_5^2 c_s^2 + 2\omega_5^2 \omega_2^3 v_1^2 - 2\omega_5^2 \omega_2^2 c_s^2 - 12\omega_5 \omega_2 c_s^2 - 12\omega_5^2 v_1^2 - 12\omega_5 \omega_2$$

$$C_{16} = 8\omega_5^2 \omega_2^2 v_1^2 \omega_3 + 12\omega_5 \omega_2^2 c_s^2 + 6\omega_5 \omega_2^3 v_1^2 + 12\omega_5^2 \omega_3 c_s^2 + 6\omega_3^2 v_1^2 \omega_3 - 30\omega_5^2 \omega_2 \omega_3 c_s^2 - 9\omega_5 \omega_3^2 v_1^2 \omega_3 + 12\omega_5^2 \omega_2 c_s^2 - 12\omega_5 \omega_2^2 v_1^2 - 12\omega_5 \omega_2 v_1^2 \omega_3 - 2\omega_5^2 \omega_2^3 \omega_3 c_s^2 - 6\omega_5 \omega_2^3 c_s^2 - 30\omega_5 \omega_2^3 \omega_3 c_s^2 + 12\omega_2^2 \omega_3 c_s^2 + 12\omega_5^2 \omega_2 v_1^2 + 3\omega_5^2 \omega_3 c_s^2 - 12\omega_3^2 v_1^2 \omega_3 - 6\omega_5^2 \omega_2^2 v_1^2 + 30\omega_5 \omega_2^2 v_1^2 \omega_3 + \omega_5^2 \omega_2^3 v_1^2 \omega_3 + 12\omega_5 \omega_2 \omega_3 c_s^2 + 9\omega_5 \omega_2^3 \omega_3 c_s^2 - \omega_5^2 \omega_2^3 v_1^2 - 18\omega_5^2 \omega_2^2 c_s^2 - 6\omega_3^2 \omega_3 c_s^2 - 36\omega_5^2 \omega_2 v_1^2 \omega_3 + 22\omega_5^2 \omega_2^3 \omega_3 c_s^2 + 24\omega_5^2 v_1^2 \omega_3$$

$$C_{17} = 6\omega_5^2 \omega_2^2 v_1^2 \omega_3 - 24\omega_5 \omega_2 \omega_3^2 c_s^2 - 24\omega_5 \omega_2 v_1^2 \omega_3^2 + 36\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 - 3\omega_5 \omega_2^3 \omega_3^2 + 12\omega_5 \omega_2^3 \omega_3^2 c_s^2 + 6\omega_5 \omega_2^3 \omega_3^2 - 3\omega_2^3 \omega_3^2 - 6\omega_5^2 \omega_2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - 36\omega_2^2 \omega_2^3 \omega_3^2 c_s^2 + 6\omega_2^2 \omega_2^3 \omega_3^2 c_s^2 - 6\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 - 21\omega_5 \omega_2^2 \omega_3^2 + 6\omega_2^2 \omega_3^2 - 6\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 18\omega_2^3 \omega_3^2 c_s^2 - 6\omega_3^2 v_1^2 \omega_3^2 - 24\omega_5 \omega_2^3 \omega_3^2 c_s^2 - 3\omega_5^2 \omega_2^2 \omega_3^2 + 12\omega_5 \omega_2 \omega_3^2 - 24\omega_5 \omega_2^2 \omega_3^2 c_s^2 + 12\omega_2^2 \omega_2 v_1^2 \omega_3^2 + 36\omega_5^2 \omega_2 \omega_3^2 c_s^2 + 7\omega_5^2 \omega_2^2 \omega_3^2 - 12\omega_2^2 \omega_3^2 c_s^2 - 12\omega_5^2 \omega_2^3 v_1^2 \omega_3 - 12\omega_2^2 \omega_2^3 \omega_3^2 c_s^2 + 6\omega_5^2 \omega_2^3 v_1^2 + 12\omega_5 \omega_2^2 v_1^2 \omega_3^2 - 12\omega_5^2 \omega_2 \omega_3^2 c_s^2 - 36\omega_2^2 \omega_3^2 c_s^2 + 6\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 12\omega_2^2 v_1^2 \omega_3^2 + 72\omega_5 \omega_2^2 \omega_3^2 c_s^2 + \omega_5^2 \omega_2^2 \omega_3^2 + 6\omega_5^2 \omega_2^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 \omega_3 c_s^2 - \omega_5^2 \omega_2^2 \omega_3^2$$

$$C_{18} = -12\omega_5 \omega_2 \omega_3^2 c_s^2 + 12\omega_5 \omega_2 v_1^2 \omega_3^2 + 48\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 - 6\omega_5 \omega_2^3 \omega_3^2 + 12\omega_5 \omega_2^3 \omega_3^2 c_s^2 + 3\omega_5 \omega_2^3 \omega_3^2 + 12\omega_5 \omega_2^2 \omega_3^2 - 32\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 + 6\omega_5^2 \omega_2^2 \omega_3 c_s^2 - 12\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 12\omega_5 \omega_2^2 \omega_3^2 + 12\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3^2 c_s^2 - 6\omega_2^2 \omega_3^2 - 24\omega_5 \omega_2^2 \omega_3^2 c_s^2 + 30\omega_5^2 \omega_2 v_1^2 \omega_3^2 + 36\omega_2^2 \omega_3^2 c_s^2 - 24\omega_5^2 v_1^2 \omega_3^2 + 3\omega_5^2 \omega_2^2 \omega_3^2 - 12\omega_5^2 \omega_3^2 c_s^2 - 18\omega_5^2 \omega_2^2 v_1^2 \omega_3 - 12\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 + 12\omega_5^2 \omega_2^2 v_1^2 - 12\omega_5 \omega_2^2 v_1^2 \omega_3^2 - 24\omega_5^2 \omega_2 \omega_3^2 c_s^2 - 12\omega_2^2 \omega_3^2 c_s^2 + 12\omega_2^2 v_1^2 \omega_3^2 + 36\omega_5 \omega_2^2 \omega_3^2 c_s^2 + 2\omega_5^2 \omega_2^2 \omega_3^2 + 4\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 - 24\omega_5 \omega_2^2 v_1^2 \omega_3^2 + 3\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 \omega_3 c_s^2 - \omega_5^2 \omega_2^2 \omega_3^2$$

$$C_{19} = -60\omega_2^2 c_s^2 + 96\omega_5 \omega_2^2 c_s^2 - 6\omega_3^2 v_1^2 - 6\omega_5 \omega_2^3 v_1^2 - 12\omega_2^2 \omega_2 + 18\omega_5^2 \omega_2 c_s^2 - \omega_5^2 \omega_2^2 + 12\omega_2^2 v_1^2 + 48\omega_5 \omega_2^2 v_1^2 + 12\omega_2^2 + 30\omega_3^2 c_s^2 - 30\omega_5 \omega_2^3 c_s^2 + 11\omega_5^2 \omega_2^2 - 6\omega_3^2 + 12\omega_5^2 \omega_2 v_1^2 - 36\omega_5 \omega_2^2 + 4\omega_5^2 \omega_2^2 c_s^2 - 14\omega_5^2 \omega_2^2 v_1^2 + 9\omega_5 \omega_2^2 - 60\omega_5 \omega_2 v_1^2 + \omega_5^2 \omega_2^2 v_1^2 - 26\omega_5^2 \omega_2^2 c_s^2 - 36\omega_5 \omega_2 c_s^2 + 12\omega_5^2 v_1^2 + 24\omega_5 \omega_2$$

$$C_{20} = -6\omega_2^2 \omega_3^2 v_2^2 - 6\omega_2 \omega_3^2 c_s^2 + 30\omega_2 \omega_6 \omega_3^2 v_2^2 - 12\omega_2 \omega_3^2 v_2^2 + 3\omega_2^2 \omega_3^2 c_s^2 - 36\omega_2 \omega_6^2 \omega_3^2 v_2^2 + 9\omega_2 \omega_6 \omega_3^2 c_s^2 - 9\omega_2 \omega_6 \omega_3^2 v_2^2 - 30\omega_2 \omega_6^2 \omega_3^2 c_s^2 + 12\omega_2^2 \omega_3^2 c_s^2 - \omega_6^2 \omega_3^2 v_2^2 - 30\omega_2 \omega_6 \omega_3^2 c_s^2 - 18\omega_6^2 \omega_3^2 c_s^2 + 6\omega_2 \omega_6^2 v_2^2 + 12\omega_2 \omega_6 \omega_3^2 c_s^2 + \omega_2 \omega_6^2 \omega_3^2 v_2^2 + 6\omega_6 \omega_3^2 v_2^2 + 12\omega_6^2 \omega_3^2 c_s^2 + 12\omega_2 \omega_6^2 c_s^2 + 22\omega_2 \omega_6^2 \omega_3^2 c_s^2 + 12\omega_6 \omega_3^2 c_s^2 - 12\omega_2 \omega_3^2 v_2^2 + 8\omega_2 \omega_6^2 \omega_3^2 v_2^2 + 12\omega_6^2 \omega_3^2 v_2^2 - 6\omega_6 \omega_3^2 c_s^2 + 24\omega_2 \omega_6^2 v_2^2 - 2\omega_2 \omega_6^2 \omega_3^2 c_s^2 - 12\omega_2 \omega_6 \omega_3^2 v_2^2$$

$$C_{21} = 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 c_s^4 - 2\omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 + 2\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 \omega_3^2 c_s^2 + 10\omega_5 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 - 2\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 2\omega_5^2 \omega_2 \omega_6^2 \omega_3^2 c_s^4 + 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_2^2 - 8\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 + 4\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 v_2^2 - \omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 - 4\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 + 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_2^2 c_s^4 + 4\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_2^2 c_s^2 - 4\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 c_s^4 - 4\omega_5 \omega_2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 - 4\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 + \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_2^2 c_s^2 + 2\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 + 3\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + 12\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + 4\omega_5^2 \omega_2 \omega_6^2 \omega_3^2 c_s^4 - 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 \omega_3^2 c_s^2 - 2\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 c_s^4 + 10\omega_5^2 \omega_2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 + 2\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 - 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 \omega_3^2 c_s^2 - 2\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 8\omega_2^2 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 - 2\omega_2^2 \omega_2^2 \omega_6 \omega_3^2 c_s^4 + 14\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 2\omega_5^2 \omega_2^2 \omega_6 v_1^2 \omega_3^2 v_2^2 + 2\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 - 10\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 \omega_3^2 v_2^2 - 10\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 10\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^4 + 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 c_s^4 + 2\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_2^2 c_s^2 - 2\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 - 4\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + 4\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 c_s^4 - 4\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 - 2\omega_5 \omega_2^2 \omega_6 \omega_3^2 c_s^4 - 2\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 v_2^2 + 3\omega_5^2 \omega_2^2 \omega_6 v_1^2 \omega_3^2 v_2^2 + 4\omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 28\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 + 4\omega_5 \omega_2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 4\omega_5 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 + 8\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 + \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 c_s^4 - 12\omega_2^2 \omega_2^2 \omega_6^2 \omega_3^2 c_s^4 + 4\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 - 3\omega_5 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 - 3\omega_5^2 \omega_2^2 \omega_6 v_1^2 \omega_3^2 c_s^2 + 8\omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 - 14\omega_5^2 \omega_2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + 2\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 c_s^2 - 4\omega_5^2 \omega_2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 + 2\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 c_s^2 + 14\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 v_2^2 + 4\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 v_2^2 + 2\omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_2^2 c_s^2 - 10\omega_5^2 \omega_2^2 \omega_6 v_1^2 \omega_3^2 v_2^2 - \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 c_s^4 + 10\omega_5^2 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2 + 4\omega_5 \omega_2^2 \omega_6^2 \omega_3^2 c_s^4 + 2\omega_5 \omega_2^2 \omega_6^2 v_1^2 \omega_3^2 c_s^2$$

$$C_{22} = 12\omega_3^2 \omega_6 \omega_3 v_2^2 + \omega_2^2 \omega_6^2 \omega_3^2 c_s^2 - 6\omega_3^2 \omega_3^2 v_2^2 + 22\omega_3^2 \omega_6^2 \omega_3^2 v_2^2 - 12\omega_3^2 \omega_3^2 c_s^2 + 22\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 + 12\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 - 48\omega_3^2 \omega_6^2 \omega_3^2 v_2^2 + 12\omega_3^2 \omega_3^2 v_2^2 + 12\omega_6^2 \omega_3^2 v_2^2 - 14\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 - 6\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 - 4\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 + 6\omega_3^2 \omega_3^2 c_s^2 - 12\omega_2^2 \omega_6 \omega_3^2 c_s^2 - 30\omega_2 \omega_6^2 \omega_3^2 v_2^2 + 24\omega_2^2 \omega_6 \omega_3^2 c_s^2 + 24\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 - 12\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 + 24\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 + 6\omega_3^2 \omega_6 \omega_3^2 v_2^2 - 6\omega_3^2 \omega_6 \omega_3^2 c_s^2 - 18\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 + 24\omega_2 \omega_6^2 \omega_3^2 v_2^2 - 12\omega_2^2 \omega_6^2 c_s^2 - 24\omega_3^2 \omega_6 \omega_3^2 v_2^2 + 6\omega_2 \omega_6^2 \omega_3^2 c_s^2$$

$$C_{23} = 24\omega_5^2 \omega_2^2 v_1^2 \omega_3 - 12\omega_5 \omega_2 \omega_3^2 c_s^2 + 12\omega_5 \omega_2 v_1^2 \omega_3^2 + 12\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 - 14\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 + 6\omega_5^2 \omega_3^2 \omega_3 c_s^2 + 22\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 - 48\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 6\omega_5 \omega_2^3 v_1^2 \omega_3^2 + 6\omega_2^2 \omega_3^2 c_s^2 - 6\omega_2^2 v_1^2 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3^2 c_s^2 - 18\omega_5^2 \omega_2 v_1^2 \omega_3^2 + 24\omega_5^2 \omega_2 \omega_3^2 c_s^2 - 12\omega_5^2 \omega_3^2 c_s^2 - 30\omega_5^2 \omega_2^2 v_1^2 \omega_3 + 24\omega_5^2 \omega_2 v_1^2 \omega_3 - 6\omega_5^2 \omega_2^2 \omega_3^2 c_s^2 + 12\omega_5^2 \omega_2^2 v_1^2 - 24\omega_5 \omega_2^2 v_1^2 \omega_3^2 - 12\omega_2^2 \omega_3^2 c_s^2 + 22\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 12\omega_2^2 v_1^2 \omega_3^2 + 24\omega_5 \omega_2^2 \omega_3^2 c_s^2 + \omega_5^2 \omega_2^2 \omega_3^2 c_s^2 - 4\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 \omega_3^2 c_s^2$$

$$C_{24} = 15\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 - 18\omega_3^3 v_2^2 - 24\omega_6 \omega_3 - 2\omega_6^2 \omega_3^2 c_s^2 + 72\omega_6 \omega_3 v_2^2 + 12\omega_3^2 c_s^2 + 36\omega_3^2 v_2^2 + 24\omega_6 \omega_3 c_s^2 + 36\omega_6 \omega_3 - 3\omega_6^2 \omega_3^2 v_2^2 - 6\omega_3^2 c_s^2 + 25\omega_6^2 \omega_3^2 c_s^2 - 9\omega_6 \omega_3^2 - 36\omega_6^2 v_2^2 + \omega_6^2 \omega_3^2 + 27\omega_6 \omega_3^2 v_2^2 - 48\omega_6^2 \omega_3 c_s^2 - 11\omega_6^2 \omega_3^2 - 36\omega_6 \omega_3^2 c_s^2 - 12\omega_3^2 - 108\omega_6 \omega_3^2 v_2^2 + 12\omega_6^2 \omega_3 + 18\omega_6^2 \omega_3 v_2^2 + 6\omega_3^2 + 9\omega_6 \omega_3^2 c_s^2 + 24\omega_6^2 c_s^2$$

$$C_{25} = -24\omega_3^2 \omega_6 \omega_3 v_2^2 + 6\omega_3^2 \omega_6^2 \omega_3^2 c_s^2 - 6\omega_3^2 \omega_3^2 v_2^2 + 6\omega_3^2 \omega_3^2 + 6\omega_2^2 \omega_6^2 \omega_3^2 v_2^2 - 3\omega_2^2 \omega_6^2 \omega_3^2 - 36\omega_3^2 \omega_3^2 c_s^2 - 6\omega_3^2 \omega_6^2 \omega_3^2 v_2^2 + \omega_2^2 \omega_6^2 \omega_3^2 + 36\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 - 3\omega_3^2 \omega_3^2 + 12\omega_2^2 \omega_6 \omega_3 - 6\omega_3^2 \omega_2^2 \omega_3^2 v_2^2 - 21\omega_3^2 \omega_6^2 \omega_3^2 + 12\omega_3^2 \omega_3^2 v_2^2 + 6\omega_6^2 \omega_3^2 v_2^2 - 36\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 + 6\omega_3^2 \omega_6 \omega_3^2 - 12\omega_2^2 \omega_6^2 \omega_3^2 c_s^2 + 18\omega_3^2 \omega_3^2 c_s^2 - 24\omega_3^2 \omega_6 \omega_3 c_s^2 - 12\omega_2 \omega_6^2 \omega_3^2 v_2^2 - \omega_2^2 \omega_6^2 \omega_3^2 + 72\omega_3^2 \omega_6 \omega_3^2 c_s^2 + 12\omega_2^2 \omega_6 \omega_3^2 c_s^2 - 12\omega_2 \omega_6^2 \omega_3^2 c_s^2 + 7\omega_3^2 \omega_6 \omega_3^2 + 36\omega_3^2 \omega_6 \omega_3 c_s^2 - 24\omega_3^2 \omega_6 \omega_3^2 c_s^2 + 12\omega_3^2 \omega_6^2 \omega_3 v_2^2 - 12\omega_2^2 \omega_6^2 \omega_3 c_s^2 - 3\omega_2^2 \omega_6 \omega_3^2 - 6\omega_3^2 \omega_6 \omega_3 + 6\omega_2 \omega_6^2 \omega_3^2 v_2^2 - 12\omega_2^2 \omega_6^2 c_s^2 + 12\omega_3^2 \omega_6 \omega_3^2 v_2^2 + 6\omega_2 \omega_6^2 \omega_3^2 c_s^2 + 6\omega_2^2 \omega_6 \omega_3^2 - 24\omega_2^2 \omega_6 \omega_3^2 c_s^2$$

$$C_{26} = -14\omega_2^2\omega_3^2v_2^2 - 6\omega_3^3v_2^2 + 24\omega_6\omega_3 + 4\omega_6^2\omega_3^2c_s^2 - 60\omega_6\omega_3v_2^2 - 60\omega_3^2c_s^2 + 12\omega_2^2v_2^2 - 36\omega_6\omega_3c_s^2 - 36\omega_6\omega_3 + \omega_6^2\omega_3^2v_2^2 + 30\omega_3^3c_s^2 - 26\omega_6^2\omega_3^2c_s^2 + 9\omega_6\omega_3^3 + 12\omega_6^2v_2^2 - \omega_6^2\omega_3^3 - 6\omega_6\omega_3^3v_2^2 + 18\omega_6^2\omega_3c_s^2 + 11\omega_6^2\omega_3 + 96\omega_6\omega_3^2c_s^2 + 12\omega_3^3 + 48\omega_6\omega_3^2v_2^2 - 12\omega_6^2\omega_3 + 12\omega_6^2\omega_3v_2^2 - 6\omega_3^3 - 30\omega_6\omega_3^2c_s^2$$

$$C_{27} = 12\omega_2^3\omega_6\omega_3v_2^2 + 4\omega_2^3\omega_6^2\omega_3^2c_s^2 - 6\omega_2^3\omega_3^3v_2^2 - 6\omega_2^3\omega_6^2\omega_3^2 - 12\omega_2^3\omega_3^2c_s^2 - 12\omega_2^3\omega_6^2\omega_3^2v_2^2 + 2\omega_2^3\omega_6^2\omega_3^3 + 48\omega_2^3\omega_6^2\omega_3^2c_s^2 + 12\omega_2^3\omega_6^2\omega_3^2v_2^2 - 6\omega_2^3\omega_6\omega_3^3 + 12\omega_2^3\omega_3^3v_2^2 + 12\omega_2^3\omega_6^3v_2^2 - 32\omega_2^3\omega_6^2\omega_3^2c_s^2 + 3\omega_2^3\omega_6\omega_3^3 - 12\omega_2^3\omega_6^2\omega_3^2c_s^2 + 3\omega_2^3\omega_6^2\omega_3^3v_2^2 + 6\omega_2^3\omega_3^3c_s^2 - 12\omega_2^3\omega_6\omega_3c_s^2 - 18\omega_2\omega_6^2\omega_3^3v_2^2 - \omega_2^3\omega_6^3\omega_3^3 - 24\omega_2^3\omega_6\omega_3^2v_2^2 + 36\omega_2^3\omega_6\omega_3^2c_s^2 - 24\omega_2^3\omega_6^2v_2^2 + 12\omega_2^3\omega_6\omega_3^2c_s^2 - 12\omega_2\omega_6^2\omega_3^2c_s^2 + 3\omega_2^3\omega_6^2\omega_3^3 + 36\omega_2^3\omega_6^2\omega_3c_s^2 - 12\omega_2^3\omega_6\omega_3^3c_s^2 + 30\omega_2^3\omega_6^2\omega_3v_2^2 + 12\omega_2^3\omega_6\omega_3^2v_2^2 - 24\omega_2^3\omega_6^2\omega_3c_s^2 - 6\omega_2^3\omega_6\omega_3^3 - 12\omega_2^3\omega_6^2c_s^2 - 12\omega_2^3\omega_6\omega_3^2v_2^2 + 6\omega_2\omega_6^2\omega_3^2c_s^2 + 12\omega_2^3\omega_6\omega_3^3 - 24\omega_2^3\omega_6\omega_3^2c_s^2$$

$$C_{28} = -12\omega_2^2\omega_3^2v_2^2c_s^2 + 12\omega_6^2\omega_3^2v_2^2 - 36\omega_3^3v_2^2 + 72\omega_6\omega_3^2v_2^4 + 24\omega_6^2c_s^4 + \omega_6^2\omega_3^2c_s^2 + 108\omega_3^3v_2^2c_s^2 - 72\omega_6\omega_3^3v_2^2c_s^2 + 6\omega_6\omega_3^3c_s^4 - 30\omega_6\omega_3^3v_2^4 - 48\omega_6^2\omega_3^3c_s^4 + 72\omega_3^3v_2^2 + 72\omega_6\omega_3v_2^2c_s^2 - 24\omega_6\omega_3^2c_s^2 - 3\omega_6^2\omega_3^3v_2^2 - 24\omega_6\omega_3^2c_s^4 - 8\omega_6^2\omega_3^2c_s^2 + 24\omega_6\omega_3c_s^4 + 3\omega_6^2\omega_3^3v_2^2 + 30\omega_6\omega_3^3v_2^2 + 12\omega_6^2\omega_3c_s^2 - 72\omega_3^3v_2^4 - 216\omega_3^3v_2^2c_s^2 + 144\omega_6\omega_3^3v_2^2c_s^2 + 24\omega_6^2\omega_3^3c_s^4 + 6\omega_6^2\omega_3^3v_2^2c_s^2 + 24\omega_6\omega_3^2c_s^2 + 36\omega_3^3v_2^4 - 36\omega_6^2\omega_3v_2^2c_s^2 - 72\omega_6\omega_3^2v_2^2 - 12\omega_6^2\omega_3^2v_2^4 - 6\omega_6\omega_3^3c_s^2 - 3\omega_6^2\omega_3^3c_s^4$$

$$C_{29} = 2\omega_6^2\omega_3^2v_2^2 + 42\omega_3^3v_2^2 - 12\omega_6\omega_3 + \omega_6^2\omega_3^2c_s^2 + 60\omega_6\omega_3v_2^2 - 60\omega_3^2c_s^2 - 84\omega_3^3v_2^2 - 12\omega_6\omega_3c_s^2 - 24\omega_6\omega_3^2 + 2\omega_6^2\omega_3^2v_2^2 + 30\omega_3^3c_s^2 - 2\omega_6^2\omega_3^2c_s^2 + 12\omega_6\omega_3^3 - 12\omega_6^2v_2^2 - \omega_6^2\omega_3^3 - 24\omega_6\omega_3^3v_2^2 - 30\omega_6^2\omega_3^2c_s^2 + 2\omega_6^2\omega_3^2 + 72\omega_6\omega_3^2c_s^2 + 36\omega_3^3 + 24\omega_6\omega_3^2v_2^2 + 6\omega_6^2\omega_3 - 12\omega_6^2\omega_3v_2^2 - 18\omega_3^3 - 24\omega_6\omega_3^3c_s^2 + 24\omega_6^2c_s^2$$

$$C_{30} = 22\omega_2^2\omega_2^2c_s^2\omega_4 + 12\omega_5\omega_2^2c_s^2 + 6\omega_5\omega_2^3v_1^2 + \omega_5^2\omega_2^3v_1^2\omega_4 - 6\omega_2^3c_s^2\omega_4 + 9\omega_5\omega_2^2c_s^2\omega_4 + 12\omega_2^2\omega_2c_s^2 - 12\omega_2^2v_1^2\omega_4 + 30\omega_5\omega_2^2v_1^2\omega_4 - 12\omega_5\omega_2^3v_1^2 + 12\omega_5\omega_2^2c_s^2\omega_4 + 24\omega_5^2v_1^2\omega_4 - 6\omega_5\omega_2^3c_s^2 - 36\omega_5^2\omega_2v_1^2\omega_4 + 12\omega_5^2\omega_2v_1^2\omega_4 + 12\omega_5\omega_2^2v_1^2\omega_4 - 9\omega_5\omega_2^3v_1^2\omega_4 + 3\omega_5^2\omega_2^2c_s^2 + 12\omega_2^2c_s^2\omega_4 - 6\omega_5^2\omega_2^2v_1^2 - 30\omega_5\omega_2^2c_s^2\omega_4 + 8\omega_5^2\omega_2^2v_1^2\omega_4 - 2\omega_5^2\omega_2^2c_s^2\omega_4 - \omega_5^2\omega_2^3v_1^2 - 18\omega_5^2\omega_2^2c_s^2 - 30\omega_5^2\omega_2c_s^2\omega_4 - 12\omega_5\omega_2v_1^2\omega_4 + 12\omega_5^2c_s^2\omega_4$$

$$C_{31} = -12\omega_2^2\omega_2^2c_s^2\omega_4 - 24\omega_5\omega_2^2c_s^2\omega_4^3 + 7\omega_5^2\omega_2^2\omega_4^3 - 12\omega_5^2\omega_2^3v_1^2\omega_4 - 3\omega_5^2\omega_2^2\omega_4^3 + 12\omega_5\omega_2\omega_4^3 + 12\omega_5^2\omega_2v_1^2\omega_4^3 - \omega_5^2\omega_2^3\omega_4^3 - 36\omega_2^2\omega_2^2c_s^2\omega_4^3 + 12\omega_5\omega_2^2c_s^2\omega_4 + 6\omega_2^2\omega_2^3v_1^2\omega_4 + 12\omega_5\omega_2^2v_1^2\omega_4^3 + 12\omega_2^2v_1^2\omega_4^3 + 36\omega_2^2\omega_2^2c_s^2\omega_4^3 + \omega_5^2\omega_2^3\omega_4^3 + 18\omega_2^2c_s^2\omega_4^3 + 36\omega_5^2\omega_2c_s^2\omega_4^3 + 6\omega_5\omega_2^2\omega_4^3 - 3\omega_2^3\omega_4^3 - 12\omega_5^2c_s^2\omega_4^3 + 6\omega_5^2\omega_2^2v_1^2\omega_4 - 24\omega_5\omega_2v_1^2\omega_4^3 - 3\omega_5\omega_2^2\omega_4^3 + 6\omega_5^2\omega_2^2c_s^2\omega_4 - 12\omega_5^2\omega_2c_s^2\omega_4^3 + 6\omega_5^2\omega_2^3v_1^2 - 21\omega_5\omega_2^2\omega_4^3 + 6\omega_2^2\omega_4^3 + 72\omega_5\omega_2^2c_s^2\omega_4^3 - 12\omega_5^2\omega_2^2c_s^2\omega_4^3 - 36\omega_2^2c_s^2\omega_4^3 - 6\omega_5^2\omega_2^2v_1^2\omega_4^3 - 6\omega_2^3v_1^2\omega_4^3 - 24\omega_5\omega_2^2c_s^2\omega_4^3 - 6\omega_5^2\omega_2\omega_4^3 + 6\omega_5^2\omega_2^2c_s^2\omega_4^3 + 6\omega_5\omega_2^2\omega_4^3 - 6\omega_5^2\omega_2^2v_1^2\omega_4^3$$

$$C_{32} = -24\omega_2^2v_1^2\omega_4^3 - 12\omega_5^2\omega_2^2c_s^2\omega_4 - 12\omega_5\omega_2^2c_s^2\omega_4^3 + 3\omega_5^2\omega_2^2\omega_4^3 - 18\omega_5^2\omega_2^3v_1^2\omega_4 - 6\omega_5^2\omega_2^2\omega_4^3 + 30\omega_5^2\omega_2v_1^2\omega_4^3 + 3\omega_5^2\omega_2^3v_1^2\omega_4^3 - 24\omega_5\omega_2^2v_1^2\omega_4^2 - \omega_5^2\omega_2^3\omega_4^3 - 32\omega_5^2\omega_2^2c_s^2\omega_4^3 + 12\omega_5\omega_2^2c_s^2\omega_4^3 - 12\omega_5\omega_2^2v_1^2\omega_4^3 + 12\omega_2^2v_1^2\omega_4^3 + 48\omega_5^2\omega_2^2c_s^2\omega_4^3 - 12\omega_5\omega_2^2c_s^2\omega_4^3 + 2\omega_5^2\omega_2^2\omega_4^3 + 6\omega_5^2c_s^2\omega_4^3 + 36\omega_5^2\omega_2c_s^2\omega_4^3 + 3\omega_5\omega_2^2\omega_4^3 - 12\omega_5^2c_s^2\omega_4^3 + 12\omega_5\omega_2v_1^2\omega_4^3 - 6\omega_5\omega_2^2\omega_4^3 + 6\omega_5^2\omega_2^2c_s^2\omega_4 - 24\omega_5^2\omega_2c_s^2\omega_4^3 + 12\omega_5^2\omega_2^2v_1^2 - 6\omega_5\omega_2^2\omega_4^3 + 36\omega_5\omega_2^2c_s^2\omega_4^3 - 12\omega_5^2\omega_2^2c_s^2\omega_4^3 - 12\omega_2^2c_s^2\omega_4^3 + 12\omega_5^2\omega_2^2v_1^2\omega_4^3 - 6\omega_2^3v_1^2\omega_4^3 - 24\omega_5\omega_2^2c_s^2\omega_4^3 + 4\omega_5^2\omega_2^2c_s^2\omega_4^3 + 12\omega_5\omega_2^2\omega_4^3 + 12\omega_5\omega_2^3v_1^2\omega_4^3 - 12\omega_5^2\omega_2^2v_1^2\omega_4^3$$

$$C_{33} = -60\omega_2^2c_s^2 + 96\omega_5\omega_2^2c_s^2 - 6\omega_2^3v_1^2 - 6\omega_5\omega_2^3v_1^2 - 12\omega_2^2\omega_2 + 18\omega_2^2\omega_2c_s^2 - \omega_5^2\omega_2^3 + 12\omega_2^3v_1^2 + 48\omega_5\omega_2^2v_1^2 + 12\omega_2^2 + 30\omega_2^3c_s^2 - 30\omega_5\omega_2^3c_s^2 + 11\omega_5^2\omega_2^2 - 6\omega_2^3 + 12\omega_5^2\omega_2v_1^2 - 36\omega_5\omega_2^2 + 4\omega_5^2\omega_2^2c_s^2 - 14\omega_5^2\omega_2v_1^2 + 9\omega_5\omega_2^3 - 60\omega_5\omega_2v_1^2 + \omega_5^2\omega_2^3v_1^2 - 26\omega_5^2\omega_2^2c_s^2 - 36\omega_5\omega_2c_s^2 + 12\omega_5^2v_1^2 + 24\omega_5\omega_2$$

$$C_{34} = -6\omega_3\omega_4^3 - 6\omega_2\omega_4^3 - 12\omega_2\omega_3\omega_4^3 + 18\omega_2\omega_3\omega_4^3 - 6\omega_2\omega_3^3 + 12\omega_3^3\omega_4^3 + 18\omega_2\omega_3^3\omega_4 - 16\omega_2\omega_3^3\omega_4^3 - 4\omega_3^3\omega_4^3 + 30\omega_2\omega_3^3\omega_4^3 - 12\omega_2\omega_3^3\omega_4 + 3\omega_2\omega_3^3\omega_4^3 - 12\omega_3^3\omega_4^3 - 16\omega_2\omega_3^3\omega_4^3 + 12\omega_3^3\omega_4^3 - 6\omega_3^3\omega_4$$

$$C_{35} = 3\omega_2^3\omega_3\omega_4^3 - 6\omega_3\omega_4^3 - 6\omega_2\omega_4^3 - 16\omega_2^3\omega_3\omega_4^3 + 18\omega_2^3\omega_3\omega_4 - 12\omega_2\omega_3\omega_4^3 - 6\omega_2^3\omega_3 + 18\omega_2\omega_3\omega_4^3 + 30\omega_2^2\omega_3\omega_4^3 - 4\omega_2^3\omega_4^3 + 12\omega_2^3\omega_4^3 - 16\omega_2^2\omega_3\omega_4^3 - 6\omega_2^3\omega_4 + 12\omega_2^2\omega_4^3 - 12\omega_2^2\omega_3\omega_4 - 12\omega_2^2\omega_4^3$$

$$C_{36} = 30\omega_2^2\omega_3^2\omega_4 + 12\omega_2^2\omega_3^2 - 4\omega_2^3\omega_3^3 - 12\omega_2^2\omega_3^2 + 18\omega_2^3\omega_3\omega_4 - 16\omega_2^2\omega_3^3\omega_4 - 6\omega_2^3\omega_3 + 12\omega_2^2\omega_3^3 - 6\omega_2\omega_3^3 + 18\omega_2\omega_3^3\omega_4 - 16\omega_2^3\omega_3^3\omega_4 - 6\omega_2^3\omega_4 - 12\omega_2\omega_3^3\omega_4 - 12\omega_2^2\omega_3\omega_4 + 3\omega_2^3\omega_3^3\omega_4 - 6\omega_3^3\omega_4$$

$$C_{37} = 4\omega_5^2\omega_2^2v_1^2\omega_3^2\omega_4^3 - \omega_5\omega_2^3v_1^2\omega_3^2\omega_4^3 + \omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 - 2\omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 + \omega_5\omega_2^3\omega_3^2c_s^2\omega_4^3 - 2\omega_2^2\omega_2^3v_1^2\omega_3^2\omega_4^3 + 3\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4 + 2\omega_5\omega_2^3v_1^2\omega_3^2\omega_4^3 + \omega_2^3v_1^2\omega_3^2\omega_4^3 + 4\omega_5^2\omega_2^2v_1^2\omega_3^2\omega_4 - 2\omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 + 2\omega_5\omega_2^3v_1^2\omega_3^2\omega_4^3 - 10\omega_5^2\omega_2^2v_1^2\omega_3^2\omega_4^3 - 2\omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 + 7\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4^3 - 2\omega_5\omega_2^3\omega_3^2c_s^2\omega_4^3 - \omega_2^3v_1^2\omega_3^2\omega_4^3 + 7\omega_5^2\omega_2^2v_1^2\omega_3^2\omega_4^3 - 2\omega_2^2\omega_3^2c_s^2\omega_4^3 - 2\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4^3 + 6\omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 + 3\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4 + 3\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4^3 + 6\omega_5\omega_2^2\omega_3^2c_s^2\omega_4^3 - 10\omega_5^2\omega_2^2v_1^2\omega_3^2\omega_4^3 + \omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 + 2\omega_2^2v_1^2\omega_3^2\omega_4^3 - 6\omega_5^2\omega_2^2\omega_3^2c_s^2\omega_4^3 + 2\omega_5\omega_2^3v_1^2\omega_3^2\omega_4^3 - 8\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4^3 - \omega_5\omega_2^3v_1^2\omega_3^2\omega_4^3 + 8\omega_5^2\omega_2^3v_1^2\omega_3^2\omega_4^3 - 2\omega_5\omega_2^2\omega_3^2c_s^2\omega_4^3 + \omega_5^2\omega_2^2\omega_3^2c_s^2\omega_4^3 + \omega_5\omega_2^2\omega_3^2c_s^2\omega_4^3 + 3\omega_5^2\omega_2^3v_1^2\omega_3\omega_4^2 + 2\omega_5^2v_1^2\omega_3^2\omega_4^3 - 2\omega_5^2\omega_3^2c_s^2\omega_4^3 + \omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^2 - 8\omega_5^2\omega_2^3v_1^2\omega_3\omega_4^3 - 2\omega_5^2\omega_2^3\omega_3^2c_s^2\omega_4^3 + 3\omega_5^2\omega_2v_1^2\omega_3^2\omega_4^3 + 3\omega_5^2\omega_2v_1^2\omega_3^2\omega_4^3 - 2\omega_5\omega_2\omega_3^2c_s^2\omega_4^3 + 4\omega_5^2\omega_2^2v_1^2\omega_3\omega_4^3 + 6\omega_5^2\omega_2^2\omega_3^2c_s^2\omega_4^3 - 2\omega_5^2\omega_2\omega_3^2c_s^2\omega_4^3 + 2\omega_5\omega_2v_1^2\omega_3^2\omega_4^3 + 3\omega_5^2\omega_2^2v_1^2\omega_3^2\omega_4^3 - 7\omega_5^2\omega_2v_1^2\omega_3^2\omega_4^3 - 2\omega_5\omega_2^2\omega_3^2c_s^2\omega_4^3 - 2\omega_5^2\omega_2^2\omega_3^2c_s^2\omega_4^3 + 6\omega_5^2\omega_2\omega_3^2c_s^2\omega_4^3$$

$$C_{38} = 28\omega_2^2\omega_3^3\omega_4^3 - 30\omega_2^3\omega_3\omega_4^3 + 18\omega_2^3\omega_3\omega_4^2 - 30\omega_2^2\omega_3^3\omega_4^3 + 12\omega_2^3\omega_3^3 - 30\omega_2^2\omega_3^3\omega_4 + 6\omega_2^3\omega_3^3\omega_4 + 12\omega_2^2\omega_3^2\omega_4^3 + 18\omega_2\omega_3^2\omega_4^3 + 24\omega_2^3\omega_3^3\omega_4^3 + 12\omega_2^3\omega_4^3 + 12\omega_2^3\omega_4^3 + 18\omega_2^3\omega_3\omega_4 - 5\omega_2^3\omega_3^3\omega_4^3 + 6\omega_2^2\omega_3\omega_4^3 - 42\omega_2^2\omega_3^3\omega_4^3 - 36\omega_2\omega_3^3\omega_4^3 + 18\omega_2\omega_3^3\omega_4^3 - 30\omega_2^3\omega_3\omega_4 + 24\omega_2^3\omega_3^3\omega_4^3$$

$$C_{39} = -12\omega_2^2\omega_2^2c_s^2\omega_4 - 12\omega_5\omega_2^2c_s^2\omega_4^3 - 30\omega_5^2\omega_2^2v_1^2\omega_4 - 6\omega_5^2\omega_2^2v_1^2\omega_4^3 - 5\omega_2^2\omega_2^2v_1^2\omega_4^3 + 24\omega_5\omega_2^2v_1^2\omega_4^2 - 32\omega_2^2\omega_2^2c_s^2\omega_4^3 + 12\omega_5\omega_2^2c_s^2\omega_4^3 + 24\omega_2^2\omega_2^3v_1^2\omega_4^2 - 36\omega_5\omega_2^2v_1^2\omega_4^3 + 12\omega_5^2v_1^2\omega_4^3 + 48\omega_5^2\omega_2^2c_s^2\omega_4^3 - 12\omega_5\omega_2^3c_s^2\omega_4^3 + 6\omega_2^2c_s^2\omega_4^3 + 36\omega_5^2\omega_2c_s^2\omega_4^3 - 12\omega_5^2\omega_2^2v_1^2\omega_4 + 12\omega_5\omega_2v_1^2\omega_4^3 + 6\omega_2^2\omega_2^3c_s^2\omega_4 - 24\omega_2^2\omega_2c_s^2\omega_4^3 + 12\omega_5^2\omega_2^2v_1^2 + 36\omega_5\omega_2^2c_s^2\omega_4^3 - 12\omega_2^2\omega_2^3c_s^2\omega_4^3 - 12\omega_2^2c_s^2\omega_4^3 + 12\omega_5\omega_2^2v_1^2\omega_4^3 - 36\omega_2^2\omega_2^2v_1^2\omega_4^3 - 6\omega_2^2v_1^2\omega_4^3 - 24\omega_5\omega_2^2c_s^2\omega_4^3 + 4\omega_5^2\omega_2^2c_s^2\omega_4^3 - 12\omega_5\omega_2^2v_1^2\omega_4^3 + 16\omega_5^2\omega_2^2v_1^2\omega_4^3$$

$$C_{40} = 24\omega_5^2\omega_2^2v_1^2\omega_3 - 12\omega_5\omega_2\omega_3^2c_s^2 + 12\omega_5\omega_2v_1^2\omega_3^3 + 48\omega_5^2\omega_2^2\omega_3^2c_s^2 + 12\omega_5\omega_2^2\omega_3^2c_s^2 - 32\omega_5^2\omega_2^2\omega_3^3c_s^2 + 6\omega_5^2\omega_2^2\omega_3c_s^2 + 16\omega_5^2\omega_2^2v_1^2\omega_3^3 - 12\omega_5\omega_2^2v_1^2\omega_3^3 - 36\omega_5^2\omega_2^2v_1^2\omega_3^3 + 12\omega_5\omega_2^3v_1^2\omega_3^3 + 6\omega_2^3\omega_3^3c_s^2 - 6\omega_2^3v_1^2\omega_3^3 - 12\omega_5\omega_2^3\omega_3^3c_s^2 - 24\omega_5\omega_2^2\omega_3^3c_s^2 - 6\omega_5^2\omega_2v_1^2\omega_3^3 + 36\omega_5^2\omega_2\omega_3^3c_s^2 - 12\omega_5^2\omega_3^3c_s^2 - 30\omega_2^2\omega_3^3v_1^2\omega_3 - 12\omega_5^2\omega_2^3\omega_3^2c_s^2 + 12\omega_5^2\omega_2^3v_1^2 - 36\omega_5\omega_2^2v_1^2\omega_3^3 - 24\omega_5^2\omega_2\omega_3^2c_s^2 - 12\omega_2^2\omega_3^3c_s^2 + 24\omega_5^2\omega_2^2v_1^2\omega_3^3 + 12\omega_2^2v_1^2\omega_3^3 + 36\omega_5\omega_2^2\omega_3^3c_s^2 + 4\omega_5^2\omega_2^3\omega_3^3c_s^2 + 24\omega_5\omega_2^2v_1^2\omega_3^3 - 5\omega_5^2\omega_2^3v_1^2\omega_3^3 - 12\omega_5^2\omega_2^3\omega_3c_s^2$$

$$C_{41} = -12\omega_2^3v_2^2\omega_4 + 30\omega_6\omega_3^2v_2^2\omega_4 - 6\omega_6^2\omega_3^2v_2^2 + 12\omega_6\omega_3c_s^2\omega_4 + 3\omega_6^2\omega_3^2c_s^2 + \omega_6^2\omega_3^3v_2^2\omega_4 - 36\omega_6^2\omega_3v_2^2\omega_4 + 9\omega_6\omega_3^3c_s^2\omega_4 - 6\omega_3^3c_s^2\omega_4 - \omega_6^2\omega_3^3v_2^2 - 18\omega_2^2\omega_3^2c_s^2 + 22\omega_6^2\omega_3^2c_s^2\omega_4 + 12\omega_6^2c_s^2\omega_4 + 6\omega_6\omega_3^3v_2^2 + 24\omega_6^2v_2^2\omega_4 + 12\omega_6^2\omega_3c_s^2 + 8\omega_6^2\omega_3^2v_2^2\omega_4 + 6\omega_3^3v_2^2\omega_4 - 9\omega_6\omega_3^3v_2^2\omega_4 - 30\omega_6^2\omega_3c_s^2\omega_4 + 12\omega_6\omega_3^3c_s^2 - 2\omega_6^2\omega_3^2c_s^2\omega_4 - 12\omega_6\omega_3v_2^2\omega_4 - 12\omega_6\omega_3^2v_2^2 + 12\omega_6^2\omega_3v_2^2 - 6\omega_6\omega_3^3c_s^2 - 30\omega_6\omega_3^2c_s^2\omega_4 + 12\omega_2^2c_s^2\omega_4$$

$$\begin{aligned} & 7\omega_2^3\omega_3^2v_3^2\omega_7^4\omega_4^3 + \omega_3^3\omega_2^3c_s^2\omega_7^4\omega_4^3 + 6\omega_2^3\omega_3^2c_s^2\omega_7^4\omega_4^3 + 8\omega_3^3\omega_3^2v_3^2\omega_7^4\omega_4^2 + 3\omega_2^3\omega_3^2v_3^2\omega_7^4\omega_4^3 + \omega_2^3\omega_3^2c_s^2\omega_7^4\omega_4^3 - \omega_2^3\omega_3^2v_3^3\omega_7^4\omega_4^3 - 2\omega_2^3\omega_3^2c_s^3\omega_7^4\omega_4^3 + \\ & 3\omega_3^3\omega_3^2v_3^2\omega_7^4\omega_4^3 - 6\omega_2^3\omega_3^2c_s^3\omega_7^4\omega_4^3 - 2\omega_2^3\omega_3^2v_3^3\omega_7^4\omega_4^3 + \omega_2^3\omega_3^2c_s^2\omega_7^4\omega_4^3 + 2\omega_2^3\omega_3^2v_3^3\omega_7^4\omega_4^3 - 2\omega_2^3\omega_3^2c_s^2\omega_7^4\omega_4^3 + 7\omega_2^3\omega_3^2v_3^3\omega_7^4\omega_4^3 + 6\omega_2^3\omega_3^2c_s^2\omega_7^4\omega_4^3 + \\ & 6\omega_2^3\omega_3^2c_s^3\omega_7^4\omega_4^3 - 2\omega_2^3\omega_3^2c_s^3\omega_7^4\omega_4^3 - 10\omega_2^3\omega_3^2v_3^2\omega_7^4\omega_4^3 - 7\omega_2^3\omega_3^2v_3^3\omega_7^4\omega_4^3 + 3\omega_3^3v_3^2\omega_7^4\omega_4^3 \end{aligned}$$

$$C_{56} = -5\omega_3^3 v_3^2 \omega_7^2 \omega_4^3 - 32\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 24\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 4\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 12v_3^3 \omega_7^2 \omega_4^3 + 16\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 + 12\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 - 36\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 - 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 6\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 + 48\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 24\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 - 6\omega_2^3 v_3^3 \omega_4^3 - 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 36\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 6\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 24\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 12\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 - 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 24\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 + 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 12\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 - 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 36\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 + 6\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 + 24\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 + 12\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 + 36\omega_2^3 c_s^2 \omega_7^2 \omega_4^3 - 30\omega_2^3 v_3^3 \omega_7^2 \omega_4^3 - 12\omega_2^3 c_s^2 \omega_7^2 \omega_4^3$$

$$C_{58} = 4\omega_6^2\omega_3^2c_4^2\omega_7\omega_2^4 - 4\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4 + \omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 + 4\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^2v_2^2v_3^2\omega_7\omega_4 - 10\omega_6\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 - 4\omega_6\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^2 - 4\omega_6^2\omega_3^2c_s^2v_3^2\omega_7\omega_4^2 - 2\omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^2 + 4\omega_6\omega_3v_2^2v_3^2\omega_7^2\omega_4^3 - 2\omega_6\omega_3v_2^2v_3^2\omega_7^2\omega_4^3 + 10\omega_6^2\omega_3^2v_2^2c_s^2\omega_7\omega_4^3 + 4\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 + \omega_6^2\omega_3^2c_s^4\omega_7\omega_4^3 + 3\omega_6^2v_2^2v_3^2\omega_7^2\omega_4^3 - 2\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 - 2\omega_6^2\omega_3c_4^2\omega_7^2\omega_4^3 - 28\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 - 10\omega_6^2v_2^2v_3^2\omega_7^2\omega_4^3 - 2\omega_6^2\omega_3^2c_s^2\omega_7\omega_4^3 - 3\omega_6\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 + 12\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 - 3\omega_6^2\omega_3^2v_2^2c_s^2\omega_7\omega_4^3 + 14\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3c_4^2\omega_7^2\omega_4^3 + 8\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 - 4\omega_6\omega_3c_s^2v_3^2\omega_7^2\omega_4^3 + 14\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 - 4\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 + \omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^2c_s^2\omega_7\omega_4^3 + 4\omega_6^2\omega_3^2c_s^2\omega_7^2\omega_4^3 + \omega_6\omega_3^2c_s^4\omega_7\omega_4^3 - 2\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 - 4\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 - \omega_6^2\omega_3^2c_4^2\omega_7^2\omega_4^3 - 4\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 - 8\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 - 3\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 2\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 + 10\omega_6\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 2\omega_6^2\omega_3^2v_2^2c_s^2\omega_7\omega_4^3 + 4\omega_6^2\omega_3^2v_2^2v_3^2\omega_7\omega_4^3 + 2\omega_6^2\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 + 2\omega_6\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 - 4\omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 - 2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 4\omega_6^2\omega_3^2v_2^2\omega_7^2\omega_4^3 + 3\omega_6\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 4\omega_6\omega_3^2c_s^2\omega_7^2\omega_4^3 - 8\omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 + 10\omega_6^2\omega_3^2v_2^2c_s^2\omega_7\omega_4^3 - 4\omega_6^2c_s^2v_3^2\omega_7^2\omega_4^3 - 2\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 - 12\omega_6^2\omega_3^2c_s^4\omega_7\omega_4^3 + 10\omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 - \omega_6^2\omega_3^2c_s^2v_3^2\omega_7\omega_4^3 - \omega_6\omega_3^2v_2^2c_s^2\omega_7^2\omega_4^3 - 14\omega_6^2\omega_3^2v_2^2v_3^2\omega_7^2\omega_4^3 + 8\omega_6^2\omega_3^2c_s^2v_3^2\omega_7^2\omega_4^3 - 2\omega_6\omega_3^2c_4^2\omega_7^2\omega_4^3 - 2\omega_6^2\omega_3^2c_s^4\omega_7\omega_4^3 - 2\omega_6^2\omega_3^2c_s^4\omega_7^2\omega_4^3$$

$$C_{60} = -6\omega_6\omega_3c_s^2\omega_4^3 + 6\omega_3^2c_s^2\omega_4^3 + 12\omega_6^2\omega_3^2c_s^2\omega_4^2 - 18\omega_6^2\omega_3v_2^2\omega_4^3 + 24\omega_6^2\omega_3v_2^2\omega_4^2 - 12\omega_6^2c_s^2\omega_4^3 - 30\omega_6^2\omega_3^2v_2^2\omega_4 - 14\omega_6^2\omega_3^2c_s^2\omega_4^3 + 22\omega_6^2\omega_3^3v_2^2\omega_4^2 + 12\omega_3^2v_2^2\omega_4^3 - 24\omega_6\omega_3^2v_2^2\omega_4^3 + 12\omega_6^2\omega_3^2v_2^2 - 4\omega_6^2\omega_3^2v_2^2\omega_4^3 - 12\omega_6^2\omega_3^2c_s^2\omega_4 - 12\omega_6\omega_3c_s^2\omega_4^3 + 12\omega_6\omega_3v_2^2\omega_4^3 + 24\omega_6^2\omega_3^2v_2^2\omega_4 + \omega_6^2\omega_3^2c_s^2\omega_4 - 6\omega_6^2\omega_3^2c_s^2\omega_4^2 + 24\omega_6\omega_3^2c_s^2\omega_4^3 - 12\omega_3^2c_s^2\omega_4^3 + 22\omega_6^2\omega_3^2v_2^2\omega_4^3 + 6\omega_6^2\omega_3^2c_s^2\omega_4 + 24\omega_6^2\omega_3c_s^2\omega_4^3 - 6\omega_3^2v_2^2\omega_4^3 + 6\omega_6\omega_3^2v_2^2\omega_4^3 - 48\omega_6^2\omega_3^2v_2^2\omega_4^2$$

$$C_{62} = 6\omega_3^2\omega_7\omega_4^3 - 36\omega_3^2c_s^2\omega_7^2\omega_4^2 - 12\omega_3^2c_s^2\omega_7^2\omega_4 + 6\omega_3^2c_s^2\omega_7^2\omega_4^3 + 6v_3^2\omega_7^2\omega_4^3 - 6\omega_3^2v_3^2\omega_7^2\omega_4^2 - 21\omega_3^2\omega_7\omega_4^2 + 12\omega_3^2v_3^2\omega_7^2 - 6\omega_3^2v_3^2\omega_7^2\omega_4 - 12\omega_3^2c_s^2\omega_7^2\omega_4^3 - 36\omega_3^2c_s^2\omega_7^2\omega_4^2 + \omega_3^2\omega_7^2\omega_4^3 + 12\omega_3^2v_3^2\omega_7^2\omega_4 + 12\omega_3^2\omega_7\omega_4 + 36\omega_3^2c_s^2\omega_7^2\omega_4^2 + 6\omega_3^2v_3^2\omega_7^2\omega_4^3 - 6\omega_3^2v_3^2\omega_7^2\omega_4^2 - 12\omega_3^2c_s^2\omega_7^2 + 36\omega_3^2c_s^2\omega_7^2\omega_4 - 3\omega_3^2\omega_7^2\omega_4^2 + 18\omega_3^2c_s^2\omega_7^2\omega_4 - 24\omega_3^2c_s^2\omega_7\omega_4^2 + 6\omega_3^2\omega_7\omega_4^2 - 24\omega_3^2c_s^2\omega_7\omega_4 - 3\omega_3^2\omega_4^3 + 12\omega_3^2c_s^2\omega_7\omega_4^3 - 3\omega_3^2\omega_7\omega_4^3 + 6\omega_3^2\omega_4^2 - 24\omega_3^2v_3^2\omega_7\omega_4 - 6\omega_3^2\omega_7^2\omega_4 - 24\omega_3^2c_s^2\omega_7\omega_4^3 + 12\omega_3^2v_3^2\omega_7\omega_4^2 + 7\omega_3^2\omega_7^2\omega_4^2 + 6\omega_3^2c_s^2\omega_7^2\omega_4^3 + 6\omega_3^2v_3^2\omega_7^2\omega_4^2 - \omega_3^2\omega_7^2\omega_4^3 + 72\omega_3^2c_s^2\omega_7\omega_4^2 - 12\omega_3^2v_3^2\omega_7^2\omega_4^3 - 12\omega_3^2c_s^2\omega_7^2\omega_4^2$$

$$C_{64} = 3\omega_3^2\omega_7\omega_4^3 + 3\omega_3^3v_3^2\omega_7^2\omega_4^3 - 32\omega_3^2c_s^2\omega_7^2\omega_4^3 - 24\omega_3^2c_s^2\omega_7\omega_4^3 + 4\omega_3^3c_s^2\omega_7^2\omega_4^3 + 12v_3^2\omega_7\omega_4^3 - 12\omega_3^2v_3^2\omega_7\omega_4^3 - 6\omega_3^2\omega_7\omega_4^3 + 12\omega_3^2v_3^2\omega_4^3 + 12\omega_3^2v_3^2\omega_7\omega_4^3 - 12\omega_3^2c_s^2\omega_7^2\omega_4^3 - 12\omega_3^2c_s^2\omega_7\omega_4^3 + 2\omega_3^2\omega_7^2\omega_4^3 + 30\omega_3^3v_3^2\omega_7^2\omega_4^3 - 24\omega_3^3v_3^2\omega_7^2 - 48\omega_3^2c_s^2\omega_7^2\omega_4^3 - 6\omega_3^3v_3^2\omega_4^3 - 12\omega_3^3c_s^2\omega_7^2 + 36\omega_3^2c_s^2\omega_7^2\omega_4^3 - 6\omega_3^2\omega_7^2\omega_4^3 + 6\omega_3^2c_s^2\omega_4^3 - 24\omega_3^2c_s^2\omega_7\omega_4^3 + 12\omega_3^2v_3^2\omega_7\omega_4^3 + 12\omega_3^2\omega_7\omega_4^3 - 12\omega_3^2c_s^2\omega_7\omega_4^3 - 24\omega_3^2v_3^2\omega_7\omega_4^3 + 12\omega_3^2c_s^2\omega_7\omega_4^3 - 6\omega_3^2\omega_7\omega_4^3 + 12\omega_3^2v_3^2\omega_7\omega_4^3 - 12\omega_3^2c_s^2\omega_7\omega_4^3 - 12\omega_3^2v_3^2\omega_7\omega_4^3 + 3\omega_3^3\omega_7^2\omega_4^3 + 6\omega_3^2c_s^2\omega_7^2\omega_4^3 - \omega_3^2\omega_7^2\omega_4^3 + 36\omega_3^3c_s^2\omega_7\omega_4^3 - 18\omega_3^2v_3^2\omega_7\omega_4^3 - 12\omega_3^2c_s^2\omega_7^2\omega_4^3$$

$$C_{66} = -14c_s^2\omega_7^2\omega_4^2 + 4c_s^2\omega_7^2\omega_4^3 + 9\omega_7^2\omega_4^3 - 26c_s^2\omega_7^2\omega_4^2 + v_s^2\omega_7^2\omega_4^3 - 36\omega_7\omega_4^2 - 6\omega_4^3 - 60c_s^2\omega_4^2 + 24\omega_7\omega_4 + 18c_s^2\omega_7^2\omega_4 + 12v_s^2\omega_4^2 + 30c_s^2\omega_4^3 + 12\omega_4^2 + 12v_s^2\omega_7^2 + 12v_s^2\omega_7^2\omega_4 - 6v_s^2\omega_4^3 - 60v_s^2\omega_7\omega_4 - 12\omega_7^2\omega_4 - 36c_s^2\omega_7\omega_4 + 96c_s^2\omega_7\omega_4^2 - 6v_s^2\omega_7\omega_4^3 + 11\omega_7^2\omega_4^2 + 48v_s^2\omega_7\omega_4^2 - 30c_s^2\omega_7\omega_4^3 - \omega_7^2\omega_3^3$$

$$C_{68} = 12v_3^2\omega_7^2\omega_4^2 + c_s^2\omega_7^2\omega_4^3 - 48c_s^4\omega_7^2\omega_4 + 144c_s^2v_3^2\omega_7\omega_4^2 - 8c_s^2\omega_7^2\omega_4^2 - 3v_3^2\omega_7^2\omega_4^3 - 72c_s^2v_3^2\omega_7\omega_4^3 - 12v_3^4\omega_7^2\omega_4^2 - 3c_s^4\omega_7^2\omega_4^3 + 12c_s^2\omega_7^2\omega_4 + 72v_3^2\omega_4^2 + 24c_s^4\omega_7^2\omega_4^2 + 72c_s^2v_3^2\omega_7\omega_4 + 3v_3^4\omega_7^2\omega_4^3 - 36v_3^2\omega_4^3 - 24c_s^4\omega_7\omega_4^2 + 108c_s^2v_3^2\omega_4^3 - 30v_3^4\omega_7\omega_4^3 - 36c_s^2v_3^2\omega_7^2\omega_4 + 72v_3^4\omega_7\omega_4^2 + 6c_s^4\omega_7\omega_4^3 - 216c_s^2v_3^2\omega_4^2 - 24c_s^2\omega_7\omega_4 + 24c_s^2\omega_7\omega_4^2 + 24c_s^4\omega_7^2 + 30v_3^2\omega_7\omega_4^3 + 6c_s^2v_3^2\omega_7^2\omega_4^3 + 36v_3^4\omega_4^3 - 72v_3^2\omega_7\omega_4^2 - 6c_s^2\omega_7\omega_4^3 - 72v_3^4\omega_4^2 + 24c_s^4\omega_7\omega_4 - 12c_s^2v_3^2\omega_7^2\omega_4^2$$

$$C_{69} = 2v_3^2\omega_7^2\omega_4^2 + c_s^2\omega_7^2\omega_4^3 + 12\omega_7\omega_4^3 - 2c_s^2\omega_7^2\omega_4^2 + 2v_3^2\omega_7^2\omega_4^3 - 24\omega_7\omega_4^2 - 18\omega_4^3 - 60c_s^2\omega_4^2 - 12\omega_7\omega_4 - 30c_s^2\omega_7^2\omega_4 - 84v_3^2\omega_4^2 + 24c_s^2\omega_7^2 + 30c_s^2\omega_4^3 + 36\omega_4^2 - 12v_3^2\omega_7^2 - 12v_3^2\omega_7^2\omega_4 + 42v_3^2\omega_4^3 + 60v_3^2\omega_7\omega_4 + 6\omega_7^2\omega_4 - 12c_s^2\omega_7\omega_4 + 72c_s^2\omega_7\omega_4^2 - 24v_3^2\omega_7\omega_4^3 + 2\omega_7^2\omega_4^2 + 24v_3^2\omega_7\omega_4^2 - 24c_s^2\omega_7\omega_4^3 - \omega_7^2\omega_4^3$$

2.5 CLBM2

2.5.1 Definitions

Collision operator \mathbf{C} :

$$\mathbf{C}(\mathbf{f}) = \mathbf{K}^{-1}\mathbf{S}\left(\boldsymbol{\kappa}^{(eq)} - \mathbf{K}\mathbf{f}\right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2)$.

Matrix \mathbf{K} corresponds to the transformation matrix to the central moment basis defined by

$$\boldsymbol{\kappa} = \begin{pmatrix} k_{(0,0,0)} \\ k_{(1,0,0)} \\ k_{(0,1,0)} \\ k_{(0,0,1)} \\ k_{(2,0,0)} + k_{(0,2,0)} + k_{(0,0,2)} \\ k_{(2,0,0)} - k_{(0,2,0)} \\ k_{(2,0,0)} - k_{(0,0,2)} \end{pmatrix},$$

Thus, the transformation matrix \mathbf{K} satisfies

$$\begin{aligned} \mathbf{K}_{1,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,0)}, \\ \mathbf{K}_{2,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,0)}, \\ \mathbf{K}_{3,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,0)}, \\ \mathbf{K}_{4,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,1)}, \\ \mathbf{K}_{5,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,0,2)}, \\ \mathbf{K}_{6,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,0)}, \\ \mathbf{K}_{7,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,0,2)}, \end{aligned}$$

$\forall i \in \{1, 2, \dots, 7\}$.

The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K}\mathbf{M}^{-1}\boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left(\rho, 0, 0, 0, 3\rho c_s^2, 0, 0\right)^T.$$

2.5.2 Conservation of mass equation



attached text file: output_d3q7_ade_clbm2_symbolic_pde_00.txt

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\
& (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\delta_t \omega_2} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\delta_t \omega_3} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{v_1 \delta_l^2}{\delta_t \omega_2 \omega_3} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{\rho \delta_l^2}{\delta_t \omega_2 \omega_3} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{\delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{\rho \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{v_2 \delta_l^2}{\delta_t \omega_2 \omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\
& (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\delta_t \omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho \delta_l^2}{2\delta_t \omega_3} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{\delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\delta_t \omega_4 \omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{\rho \delta_l^2}{\delta_t \omega_4 \omega_3} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + \\
& (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{\delta_l^2 v_3}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{\delta_l^2 v_3}{\delta_t \omega_4 \omega_3} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + \\
& (2 - \omega_3) \frac{v_2 \delta_l^2}{2\delta_t \omega_3} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{\delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\rho \delta_l^2}{2\delta_t \omega_4} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\rho \delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + \\
& (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho \delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{v_2 v_1 \delta_l^2}{\delta_t \omega_2 \omega_3} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + \\
& (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\delta_t \omega_3} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_3} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_3) \frac{v_2 \rho \delta_l^2}{2\delta_t \omega_3} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho \delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + \\
& + (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_2 \delta_l^2 v_3}{\delta_t \omega_4 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{\rho \delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + \\
& (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2 \delta_l^2 v_3}{\delta_t \omega_4 \omega_3} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{\rho \delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\delta_t \omega_3} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_4) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_3^2} + \\
& (-2 + \omega_4) \frac{\rho \delta_l^2 v_3}{2\delta_t \omega_4} \frac{\partial^2 v_3}{\partial x_3^2} + (12 + \omega_2^2 - 12\omega_2) \frac{\delta_t \rho \delta_l}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_2^2 - 12\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_2^2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + C_1 \frac{v_1 \delta_l^3}{6\delta_t \omega_5 \omega_2} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& C_2 \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^3} + (12 + \omega_3^2 - 12\omega_3) \frac{\delta_t \rho \delta_l}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + (9\omega_2 \omega_3 - 2\omega_2 \omega_3^2 + 3\omega_3^2 - 6\omega_2 - 6\omega_3) \frac{v_2 \rho \delta_l^2}{6\omega_2 \omega_3} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + \\
& (9\omega_2 \omega_3 + 3\omega_2^2 - 6\omega_2 - 2\omega_2^2 \omega_3 - 6\omega_3) \frac{v_1 \rho \delta_l^2}{6\omega_2^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + C_3 \frac{v_2 \delta_l^3}{2\delta_t \omega_5 \omega_2^2 \omega_3} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& (6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3) \frac{v_2 v_1 \rho \delta_l^3}{6\delta_t \omega_2^2 \omega_3^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (-3c_s^2 \omega_5 \omega_2^2 + 18c_s^2 \omega_5 \omega_2 - 12\omega_5 v_1^2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 + 12v_1^2 \omega_2 + 6\omega_5 v_1^2 \omega_2 + \omega_5 v_1^2 \omega_2^2 - 6v_1^2 \omega_2^2 - 12c_s^2 \omega_2) \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& + (12 + \omega_3^2 - 12\omega_3) \frac{v_2 \rho \delta_l^2}{6\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\delta_t \omega_2^2 \omega_6 \omega_3} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (-12v_2^2 \omega_6 - 12c_s^2 \omega_6 - 6v_2^2 \omega_3^2 + 6c_s^2 \omega_3^2 + 12v_2^2 \omega_3 - 12c_s^2 \omega_3 - 3c_s^2 \omega_6 \omega_3^2 + v_2^2 \omega_6 \omega_3^2 + 18c_s^2 \omega_6 \omega_3 + 6v_2^2 \omega_6 \omega_3) \frac{\rho \delta_l^3}{12\delta_t \omega_6 \omega_3^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& + (6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3) \frac{v_2 v_1 \rho \delta_l^3}{6\delta_t \omega_2^2 \omega_3^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\delta_t \omega_6 \omega_3} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho \delta_l^3}{12\delta_t \omega_6 \omega_3^2} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\delta_t \rho \delta_l}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (9\omega_4 \omega_2 - 6\omega_4 - 6\omega_2 - 2\omega_4^2 \omega_2 + 3\omega_4^2) \frac{\rho \delta_l^2 v_3}{6\omega_4^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (3\omega_2^2 + 9\omega_4 \omega_2 - 6\omega_4 - 2\omega_4 \omega_2^2 - 6\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{\delta_l^3 v_3}{2\delta_t \omega_4^2 \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (6\omega_2^2 - 6\omega_4 \omega_2^2 + \omega_4^2 \omega_2^2 - 6\omega_4^2 \omega_2 + 6\omega_4^2) \frac{v_1 \rho \delta_l^3 v_3}{6\delta_t \omega_4^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\
& (-3c_s^2 \omega_5 \omega_2^2 + 18c_s^2 \omega_5 \omega_2 - 12\omega_5 v_1^2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 + 12v_1^2 \omega_2 + 6\omega_5 v_1^2 \omega_2 + \omega_5 v_1^2 \omega_2^2 - 6v_1^2 \omega_2^2 - 12c_s^2 \omega_2) \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& + (-6\omega_4 - 2\omega_4^2 \omega_3 + 9\omega_4 \omega_3 + 3\omega_4^2 - 6\omega_3) \frac{\rho \delta_l^2 v_3}{6\omega_4^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-6\omega_4 + 3\omega_3^2 + 9\omega_4 \omega_3 - 6\omega_3 - 2\omega_4 \omega_3^2) \frac{v_2 \rho \delta_l^2}{6\omega_4 \omega_3^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (-2\omega_4 \omega_2^2 \omega_3^2 + \omega_4^2 \omega_3^2 - 2\omega_4^2 \omega_2 \omega_3^2 + \omega_4^2 \omega_2 \omega_3 + \omega_4 \omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 - 2\omega_4^2 \omega_2^2 \omega_3 + \omega_4^2 \omega_2^2 + \omega_4^2 \omega_2^2 \omega_3^2 + \omega_4 \omega_2 \omega_3^2) \frac{2v_2 v_1 \delta_l^3 v_3}{\delta_t \omega_4^2 \omega_2^2 \omega_3^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\
& + (2\omega_4^2 \omega_3^2 - 6\omega_4^2 \omega_3 + 3\omega_3^2 + 6\omega_4 \omega_3 + 3\omega_4^2 - 6\omega_4 \omega_3^2) \frac{v_2 \rho \delta_l^2 v_3}{3\delta_t \omega_4^2 \omega_3^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (3\omega_2^2 + 6\omega_4 \omega_2 - 6\omega_4 \omega_2^2 + 2\omega_4^2 \omega_2^2 - 6\omega_4^2 \omega_2 + 3\omega_4^2) \frac{v_1 \rho \delta_l^2 v_3}{3\delta_t \omega_4^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (6\omega_2 \omega_3 + 3\omega_2^2 - 6\omega_2 \omega_3^2 + 3\omega_3^2 + 2\omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3) \frac{v_2 v_1 \rho \delta_l^2}{3\delta_t \omega_2^2 \omega_3^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{\delta_l^3 v_3}{2\delta_t \omega_4^2 \omega_6 \omega_3^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (\omega_4^2 \omega_3^2 - 6\omega_4^2 \omega_3 + 6\omega_3^2 + 6\omega_4^2 - 6\omega_4 \omega_3^2) \frac{v_2 \rho \delta_l^2 v_3}{6\delta_t \omega_4^2 \omega_3^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-12v_2^2\omega_6 - 12c_s^2\omega_6 - 6v_2^2\omega_3^2 + 6c_s^2\omega_3^2 + 12v_2^2\omega_3 - 12c_s^2\omega_3 - 3c_s^2\omega_6\omega_3^2 + v_2^2\omega_6\omega_3^2 + 18c_s^2\omega_6\omega_3 + 6v_2^2\omega_6\omega_3) \frac{\rho\delta_l^3}{12\delta_t\omega_6\omega_3^2} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} \\
& + (12 - 12\omega_4 + \omega_4^2) \frac{\rho\delta_l^2 v_3}{6\omega_4^2} \frac{\partial^3 v_3}{\partial t \partial x_3^2} + C_9 \frac{v_1 \rho\delta_l^3}{2\delta_t \omega_7 \omega_4^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (6\omega_7 \omega_4 v_3^2 - 6\omega_4^2 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 - 12c_s^2 \omega_4 + 6c_s^2 \omega_4^2 - 12\omega_7 v_3^2 + 18c_s^2 \omega_7 \omega_4 + 12\omega_4 v_3^2 + \omega_7 \omega_4^2 v_3^2 - 12c_s^2 \omega_7) \frac{\rho\delta_l^3}{12\delta_t \omega_7 \omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} \\
& + (6\omega_2^2 - 6\omega_4 \omega_2^2 + \omega_4^2 \omega_2^2 - 6\omega_4^2 \omega_2 + 6\omega_4^2) \frac{v_1 \rho\delta_l^3 v_3}{6\delta_t \omega_2^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{v_2 \rho\delta_l^3}{2\delta_t \omega_7 \omega_4^2 \omega_3^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& (6\omega_7 \omega_4 v_3^2 - 6\omega_4^2 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 - 12c_s^2 \omega_4 + 6c_s^2 \omega_4^2 - 12\omega_7 v_3^2 + 18c_s^2 \omega_7 \omega_4 + 12\omega_4 v_3^2 + \omega_7 \omega_4^2 v_3^2 - 12c_s^2 \omega_7) \frac{\rho\delta_l^3}{12\delta_t \omega_7 \omega_4^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + (\omega_4^2 \omega_3^2 - 6\omega_4^2 \omega_3 + 6\omega_3^2 + 6\omega_4^2 - 6\omega_4 \omega_3^2) \frac{v_2 \rho\delta_l^3 v_3}{6\delta_t \omega_2^2 \omega_3^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{\delta_l^3 v_3}{6\delta_t \omega_7 \omega_4} \frac{\partial^3 \rho}{\partial x_3^2} + C_{12} \frac{\rho\delta_l^3}{12\delta_t \omega_7 \omega_4^2} \frac{\partial^3 v_3}{\partial x_3^2} + \\
& (-2 - \omega_2^2 + 3\omega_2) \frac{\delta_l^2 \rho\delta_l}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-2 - \omega_2^2 + 3\omega_2) \frac{3\delta_t v_1 \rho\delta_l^2}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\rho\delta_l^3}{12\omega_5^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_l^4}{24\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3\omega_3) \frac{\delta_l^2 \rho\delta_l}{2\omega_3^2} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (12\omega_2 \omega_3 + 12\omega_2^2 + 7\omega_2 \omega_3^2 - 24\omega_2 \omega_3^2 + 12\omega_3^2 + 13\omega_2^2 \omega_3^2 - 6\omega_3^3 - \omega_2^2 \omega_3^3 - 24\omega_2^2 \omega_3) \frac{\delta_t v_2 \rho\delta_l^2}{12\omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-6\omega_2^3 + 12\omega_2 \omega_3 + 12\omega_2^2 - 24\omega_2 \omega_3^2 + 12\omega_3^2 + 13\omega_2^2 \omega_3^2 + 7\omega_2^2 \omega_3 - \omega_2^2 \omega_3^2 - 24\omega_2^2 \omega_3) \frac{\delta_t v_1 \rho\delta_l^2}{12\omega_2^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-6\omega_2^3 + 18\omega_2 \omega_3^2 + 6\omega_2^2 \omega_3^2 - 12\omega_3^3 + 12\omega_2^2 \omega_3 - 7\omega_2^2 \omega_3^2 - 7\omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + \omega_2^2 \omega_3^2) \frac{v_2 v_1 \rho\delta_l^3}{6\omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + \\
& C_{16} \frac{\rho\delta_l^3}{12\omega_5^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{v_2 v_1 \delta_l^4}{6\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{18} \frac{v_2 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 - \omega_3^2 + 3\omega_3) \frac{3\delta_t v_2 \rho\delta_l^2}{2\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + C_{20} \frac{\rho\delta_l^3}{12\omega_2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (-12\omega_2^3 + 12\omega_2 \omega_3^2 - 6\omega_2 \omega_3^2 + 6\omega_2^2 \omega_3^2 - 6\omega_3^3 + 18\omega_2^2 \omega_3 - 7\omega_2^2 \omega_3^2 - 7\omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2) \frac{v_2 v_1 \rho\delta_l^3}{6\omega_2^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{21} \frac{\delta_l^4}{4\delta_t \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{v_2 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{\rho\delta_l^3}{12\omega_6^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + \\
& C_{25} \frac{v_2 v_1 \delta_l^4}{6\delta_t \omega_5^2 \omega_6^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{26} \frac{v_2 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{27} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{28} \frac{\delta_l^4}{24\delta_t \omega_6^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_2^4} + C_{29} \frac{v_2 \rho\delta_l^4}{12\delta_t \omega_6^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-2 + 3\omega_4 - \omega_4^2) \frac{\delta_t^2 \rho\delta_l}{2\omega_4^2} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (12\omega_2^2 + 12\omega_4 \omega_2 - 24\omega_4 \omega_2^2 + 7\omega_4^3 \omega_2 + 13\omega_4^2 \omega_2^2 - 6\omega_4^3 - 24\omega_4^2 \omega_2 - \omega_4^3 \omega_2^2 + 12\omega_4^2) \frac{\delta_t \rho\delta_l^2 v_3}{12\omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-6\omega_2^3 + 12\omega_2^2 + 12\omega_4 \omega_2 - 24\omega_4 \omega_2^2 + 7\omega_4^3 \omega_2 - \omega_4^2 \omega_2^2 + 13\omega_4^2 \omega_2^2 - 24\omega_4^2 \omega_2 + 12\omega_4^2) \frac{\delta_t v_1 \rho\delta_l^2}{12\omega_2^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-6\omega_2^3 - 6\omega_4 \omega_2^2 + 12\omega_4 \omega_3^2 - 7\omega_4^2 \omega_3^2 + 18\omega_4^3 \omega_2 + 6\omega_4^2 \omega_2^2 - 12\omega_4^3 + \omega_4^3 \omega_3^2 - 7\omega_4^3 \omega_2^2) \frac{v_1 \rho\delta_l^3 v_3}{6\omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + \\
& C_{30} \frac{\rho\delta_l^3}{12\omega_4 \omega_2^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{31} \frac{v_1 \delta_l^4 v_3}{6\delta_t \omega_2^2 \omega_3^2 \omega_2^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{32} \frac{\rho\delta_l^4 v_3}{12\delta_t \omega_2^2 \omega_3^2 \omega_2^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + C_{33} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_2^2 \omega_3^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + \\
& (13\omega_4^2 \omega_3^2 + 7\omega_4^3 \omega_3 - \omega_4^3 \omega_3^2 - 24\omega_4^2 \omega_3 + 12\omega_3^2 + 12\omega_4 \omega_3 - 6\omega_4^3 + 12\omega_4^2 - 24\omega_4 \omega_3) \frac{\delta_t \rho\delta_l^2 v_3}{12\omega_4^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (13\omega_4^2 \omega_3^2 - \omega_4^2 \omega_3^2 - 24\omega_4^2 \omega_3 + 12\omega_3^2 + 12\omega_4 \omega_3 - 6\omega_3^3 + 7\omega_4 \omega_3^2 + 12\omega_4^2 - 24\omega_4 \omega_3) \frac{\delta_t v_2 \rho\delta_l^2}{12\omega_4^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{v_2 \rho\delta_l^3 v_3}{6\omega_4^2 \omega_2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{35} \frac{v_1 \rho\delta_l^3 v_3}{6\omega_4^2 \omega_2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{36} \frac{v_2 v_1 \rho\delta_l^3}{6\omega_4 \omega_2^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{37} \frac{v_2 \delta_l^4 v_3}{\delta_t \omega_4^2 \omega_5^2 \omega_2^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{v_2 v_1 \rho\delta_l^4 v_3}{6\delta_t \omega_4^2 \omega_5^2 \omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\rho\delta_l^4 v_3}{12\delta_t \omega_4^2 \omega_5^2 \omega_2^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{40} \frac{v_2 \rho\delta_l^4}{12\delta_t \omega_5^2 \omega_2^2 \omega_3^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (6\omega_4^2 \omega_3^2 - 7\omega_4^2 \omega_3^2 + 18\omega_4^3 \omega_3 - 7\omega_4^3 \omega_3^2 + \omega_4^3 \omega_3^2 - 6\omega_3^3 - 12\omega_4^3 + 12\omega_4 \omega_3^2 - 6\omega_4 \omega_3^2) \frac{v_2 \rho\delta_l^3 v_3}{6\omega_4^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{41} \frac{\rho\delta_l^3}{12\omega_4 \omega_6^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{42} \frac{v_1 \delta_l^4 v_3}{\delta_t \omega_4^2 \omega_2^2 \omega_6^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{\rho\delta_l^4 v_3}{12\delta_t \omega_4^2 \omega_2^2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{44} \frac{v_2 v_1 \rho\delta_l^4 v_3}{6\delta_t \omega_4^2 \omega_2^2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_2^2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{46} \frac{v_2 \delta_l^4 v_3}{6\delta_t \omega_4^2 \omega_6^2 \omega_3^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{47} \frac{\rho\delta_l^4 v_3}{12\delta_t \omega_4^2 \omega_6^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{48} \frac{v_2 \rho\delta_l^4}{12\delta_t \omega_6^2 \omega_3^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& (-2 + 3\omega_4 - \omega_4^2) \frac{3\delta_t \rho\delta_l^2 v_3}{2\omega_4^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + C_{49} \frac{\rho\delta_l^3}{12\omega_7^2 \omega_4^2 \omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + \\
& (-12\omega_2^3 + 18\omega_4 \omega_2^3 - 7\omega_4^2 \omega_2^3 + 12\omega_4^3 \omega_2 + 6\omega_4^2 \omega_2^2 - 6\omega_4^3 + \omega_4^3 \omega_2^2 - 6\omega_4^2 \omega_2 - 7\omega_4^3 \omega_2^2) \frac{v_1 \rho\delta_l^3 v_3}{6\omega_4^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + \\
& C_{50} \frac{\delta_l^4}{4\delta_t \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{51} \frac{v_1 \rho\delta_l^4}{12\delta_t \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{52} \frac{\rho\delta_l^4 v_3}{12\delta_t \omega_4^2 \omega_5^2 \omega_2^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{53} \frac{\rho\delta_l^3}{12\omega_2^2 \omega_4^2 \omega_3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
& (6\omega_4^2 \omega_3^2 - 7\omega_4^2 \omega_3^2 + 12\omega_4^3 \omega_3 - 7\omega_4^3 \omega_3^2 + \omega_4^3 \omega_3^2 - 6\omega_4^2 \omega_3 - 12\omega_3^3 - 6\omega_4^3 + 18\omega_4 \omega_3^2) \frac{v_2 \rho\delta_l^3 v_3}{6\omega_4^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} +
\end{aligned}$$

$$\begin{aligned}
& C_{54} \frac{v_2 v_1 \delta_l^4}{\delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{55} \frac{v_2 \rho \delta_l^4}{12 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{56} \frac{v_1 \rho \delta_l^4}{12 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + C_{57} \frac{v_2 v_1 \rho \delta_l^4 v_3}{6 \delta_t \omega_4^3 \omega_3^2 \omega_3^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + \\
& C_{58} \frac{\delta_l^4}{4 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3} + C_{59} \frac{v_2 \rho \delta_l^4}{12 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + C_{60} \frac{\rho \delta_l^4 v_3}{12 \delta_t \omega_4^3 \omega_3^2 \omega_3^2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3} + C_{61} \frac{\rho \delta_l^4}{12 \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3} + \\
& C_{62} \frac{v_1 \delta_l^4 v_3}{6 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + C_{63} \frac{\rho \delta_l^4 v_3}{12 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} + C_{64} \frac{v_1 \rho \delta_l^4}{12 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} + C_{65} \frac{v_2 \delta_l^4 v_3}{6 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3} + \\
& C_{66} \frac{\rho \delta_l^4 v_3}{12 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + C_{67} \frac{v_2 \rho \delta_l^4}{12 \delta_t \omega_7^2 \omega_4^3 \omega_3^2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3} + C_{68} \frac{\delta_l^4}{24 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_3^4} + C_{69} \frac{\rho \delta_l^4 v_3}{12 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 6v_1^2 - 3c_s^2 \omega_5 \omega_2 + 3\omega_5 v_1^2 + \omega_5 \omega_2 - 18c_s^2 - 3\omega_5 + 9c_s^2 \omega_5 + 3v_1^2 \omega_2 - 3\omega_2 - \omega_5 v_1^2 \omega_2 + 9c_s^2 \omega_2 \\
C_2 &= 2\omega_5 \omega_2^2 - 6\omega_2^2 - 3c_s^2 \omega_5 \omega_2^2 + 18c_s^2 \omega_5 \omega_2 + 12\omega_5 v_1^2 - 6\omega_5 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 36v_1^2 \omega_2 + 12\omega_2 + 6\omega_5 v_1^2 \omega_2 - 5\omega_5 v_1^2 \omega_2^2 + 18v_1^2 \omega_2^2 - 12c_s^2 \omega_2 \\
C_3 &= 4c_s^2 \omega_5 \omega_2 \omega_3^2 - v_1^2 \omega_2^2 \omega_3^2 + \omega_5 v_1^2 \omega_3^2 \omega_3^2 - 2c_s^2 \omega_2 \omega_3^2 - 3\omega_5 v_1^2 \omega_2 \omega_3 - 2c_s^2 \omega_5 \omega_2 \omega_3 - 2c_s^2 \omega_5 \omega_3^2 + c_s^2 \omega_5 \omega_2^2 \omega_3 + c_s^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 + \\
& 2\omega_5 v_1^2 \omega_2^2 - 2\omega_5 v_1^2 \omega_2 \omega_3^2 - c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 2v_1^2 \omega_2 \omega_3^2 \\
C_4 &= 2v_2^2 \omega_2 \omega_6 \omega_3 - 2c_s^2 \omega_2 \omega_6 \omega_3 + c_s^2 \omega_2 \omega_6 \omega_3^2 - 3v_2^2 \omega_2 \omega_6 \omega_3^2 - 2c_s^2 \omega_2^2 \omega_6 + c_s^2 \omega_2^2 \omega_3^2 - c_s^2 \omega_2^2 \omega_6 \omega_3^2 - v_2^2 \omega_2^2 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + v_2^2 \omega_2^2 \omega_6 \omega_3^2 - \\
& 2v_2^2 \omega_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_2^2 \omega_3 + 2v_2^2 \omega_2^2 \omega_3 + 4c_s^2 \omega_2^2 \omega_6 \omega_3 \\
C_5 &= 6 + 3v_2^2 \omega_6 + 9c_s^2 \omega_6 + 3v_2^2 \omega_3 + 9c_s^2 \omega_3 - 6v_2^2 - 18c_s^2 - 3c_s^2 \omega_6 \omega_3 - v_2^2 \omega_6 \omega_3 - 3\omega_6 - 3\omega_3 + \omega_6 \omega_3 \\
C_6 &= 12v_2^2 \omega_6 - 12c_s^2 \omega_6 + 18v_2^2 \omega_3^2 + 6c_s^2 \omega_3^2 - 36v_2^2 \omega_3 - 12c_s^2 \omega_3 + 2\omega_6 \omega_3^2 - 6\omega_3^2 - 3c_s^2 \omega_6 \omega_3^2 - 5v_2^2 \omega_6 \omega_3^2 + 18c_s^2 \omega_6 \omega_3 + 6v_2^2 \omega_6 \omega_3 + 12\omega_3 - 6\omega_6 \omega_3 \\
C_7 &= -2\omega_4^2 \omega_5 v_1^2 \omega_2 - c_s^2 \omega_4^2 \omega_5 \omega_2^2 + 4c_s^2 \omega_4^2 \omega_5 \omega_2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - \omega_4^2 v_1^2 \omega_2^2 + c_s^2 \omega_4^2 \omega_2^2 - 2c_s^2 \omega_4 \omega_5 \omega_2 - 2c_s^2 \omega_4^2 \omega_5 + 2\omega_5 v_1^2 \omega_2^2 + \\
& c_s^2 \omega_4 \omega_5 \omega_2^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4^2 v_1^2 \omega_2 - 2c_s^2 \omega_4^2 \omega_2 \\
C_8 &= -2c_s^2 \omega_4^2 \omega_6 - 2c_s^2 \omega_4 \omega_6 \omega_3 + 2\omega_4^2 v_2^2 \omega_3 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + c_s^2 \omega_4^2 \omega_3^2 - 2c_s^2 \omega_4^2 \omega_3 - 2\omega_4^2 v_2^2 \omega_6 \omega_3 + c_s^2 \omega_4 \omega_6 \omega_3^2 - \omega_4^2 v_2^2 \omega_3^2 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 - \\
& c_s^2 \omega_4^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + 4c_s^2 \omega_4^2 \omega_6 \omega_3 + 2\omega_4 v_2^2 \omega_6 \omega_3 \\
C_9 &= 2\omega_4 \omega_2^2 v_3^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 - c_s^2 \omega_7 \omega_4^2 \omega_2^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 + c_s^2 \omega_7 \omega_4^2 \omega_2 - 2c_s^2 \omega_4 \omega_2^2 + c_s^2 \omega_4^2 \omega_2^2 - 2c_s^2 \omega_7 \omega_4 \omega_2 - 2c_s^2 \omega_7 \omega_2^2 - 2\omega_7 \omega_4 \omega_2^2 v_3^2 - \omega_4^2 \omega_2^2 v_3^2 + \\
& 4c_s^2 \omega_7 \omega_4 \omega_2^2 + 2\omega_7 \omega_4^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2 \\
C_{10} &= -2c_s^2 \omega_7 \omega_4 \omega_3 + c_s^2 \omega_4^2 \omega_3^2 + 2\omega_4 \omega_3^2 v_3^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 - 2c_s^2 \omega_7 \omega_3^2 + 4c_s^2 \omega_7 \omega_4 \omega_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 - 2\omega_7 \omega_4 \omega_3^2 v_3^2 - c_s^2 \omega_7 \omega_4^2 \omega_3^2 - \omega_4^2 \omega_3^2 v_3^2 - \\
& 3\omega_7 \omega_4^2 \omega_3 v_3^2 - 2c_s^2 \omega_4 \omega_3^2 + 2\omega_7 \omega_4^2 v_3^2 + c_s^2 \omega_7 \omega_4^2 \omega_3 \\
C_{11} &= 6 - \omega_7 \omega_4 v_3^2 - 3\omega_7 + 9c_s^2 \omega_4 - 3\omega_4 + \omega_7 \omega_4 + 3\omega_7 v_3^2 - 3c_s^2 \omega_7 \omega_4 - 18c_s^2 - 6v_3^2 + 3\omega_4 v_3^2 + 9c_s^2 \omega_7 \\
C_{12} &= 6\omega_7 \omega_4 v_3^2 + 18\omega_4^2 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 + 2\omega_7 \omega_4^2 - 12c_s^2 \omega_4 + 12\omega_4 + 6c_s^2 \omega_4^2 - 6\omega_7 \omega_4 + 12\omega_7 v_3^2 + 18c_s^2 \omega_7 \omega_4 - 36\omega_4 v_3^2 - 5\omega_7 \omega_4^2 v_3^2 - 12c_s^2 \omega_7 - 6\omega_4^2 \\
C_{13} &= 9c_s^2 \omega_5 \omega_3^2 + 6\omega_3^2 + 15\omega_5^2 v_1^2 \omega_2^2 + 36\omega_5 \omega_2^2 - 3\omega_5^2 v_1^2 \omega_3^2 - 12\omega_2^2 - 36c_s^2 \omega_5 \omega_2^2 - 9\omega_5 \omega_3^2 + 24c_s^2 \omega_5 \omega_2 - 24\omega_5 \omega_2 + 18\omega_5^2 v_1^2 \omega_2 + 12\omega_5^2 \omega_2 - 36\omega_5^2 v_1^2 + \\
& 12c_s^2 \omega_2^2 - 6c_s^2 \omega_3^2 + 72\omega_5 v_1^2 \omega_2 - 48c_s^2 \omega_5 \omega_2 - 108\omega_5 v_1^2 \omega_2^2 + 25c_s^2 \omega_5^2 \omega_2^2 + 36v_1^2 \omega_2^2 + \omega_2^2 \omega_3^2 - 2c_s^2 \omega_5^2 \omega_3^2 + 24c_s^2 \omega_5^2 + 27\omega_5 v_1^2 \omega_3^2 - 11\omega_5^2 \omega_2^2 - 18v_1^2 \omega_3^2 \\
C_{14} &= -6c_s^2 \omega_5 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2^2 + 24c_s^4 \omega_5 \omega_2 - 36c_s^2 \omega_5^2 v_1^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_3^2 + 24c_s^2 \omega_5 \omega_2^2 + 6c_s^2 \omega_5^2 v_1^2 \omega_3^2 + 6c_s^4 \omega_5 \omega_3^2 + 24c_s^4 \omega_5^2 - 30\omega_5 v_1^4 \omega_3^2 + 36v_1^4 \omega_3^2 - \\
& 24c_s^2 \omega_5 \omega_2 + 72\omega_5 v_1^4 \omega_3^2 - 24c_s^2 \omega_5 \omega_2^2 - 12c_s^2 \omega_5^2 v_1^2 \omega_2^2 - 72v_1^4 \omega_2^2 + 3\omega_5^2 v_1^4 \omega_3^2 + 24c_s^4 \omega_5^2 \omega_2^2 - 72c_s^2 \omega_5 v_1^2 \omega_3^2 + 144c_s^2 \omega_5 v_1^2 \omega_3^2 - 3c_s^4 \omega_5^2 \omega_3^2 - 12\omega_5^2 v_1^4 \omega_2^2 + \\
& 12c_s^2 \omega_5^2 \omega_2 - 72\omega_5 v_1^2 \omega_2^2 - 8c_s^2 \omega_5^2 \omega_2^2 + 108c_s^2 v_1^2 \omega_3^2 + 72c_s^2 \omega_5 v_1^2 \omega_2 + 72v_1^2 \omega_2^2 - 216c_s^2 v_1^2 \omega_2^2 + c_s^2 \omega_5^2 \omega_3^2 + 30\omega_5 v_1^2 \omega_3^2 - 48c_s^4 \omega_5^2 \omega_2 - 36v_1^2 \omega_3^2 \\
C_{15} &= -24c_s^2 \omega_5 \omega_3^2 - 18\omega_3^2 + 2\omega_5^2 v_1^2 \omega_2^2 - 24\omega_5 \omega_2^2 + 2\omega_5^2 v_1^2 \omega_3^2 + 36\omega_2^2 + 72c_s^2 \omega_5 \omega_2^2 + 12\omega_5 \omega_3^2 - 12c_s^2 \omega_5 \omega_2 - 12\omega_5 \omega_2 - 12\omega_5^2 v_1^2 \omega_2 + 6\omega_5^2 \omega_2 - \\
& 12\omega_5^2 v_1^2 - 60c_s^2 \omega_2^2 + 30c_s^2 \omega_3^2 + 60\omega_5 v_1^2 \omega_2 - 30c_s^2 \omega_5^2 \omega_2 + 24\omega_5 v_1^2 \omega_2^2 - 2c_s^2 \omega_5^2 \omega_2^2 - 84v_1^2 \omega_2^2 - \omega_5^2 \omega_3^2 + c_s^2 \omega_5^2 \omega_3^2 + 24c_s^2 \omega_5^2 - 24\omega_5 v_1^2 \omega_3^2 + 2\omega_5^2 \omega_2^2 + 42v_1^2 \omega_3^2 \\
C_{16} &= -6c_s^2 \omega_5 \omega_3^2 - 2c_s^2 \omega_5^2 \omega_3^2 \omega_3 - 6\omega_5^2 v_1^2 \omega_2^2 - 9\omega_5 v_1^2 \omega_3^2 \omega_3 + 12c_s^2 \omega_5^2 \omega_3 - \omega_5^2 v_1^2 \omega_2^2 + 12c_s^2 \omega_5 \omega_2^2 + 6v_1^2 \omega_3^2 \omega_3 - 36\omega_5^2 v_1^2 \omega_2 \omega_3 + 30\omega_5 v_1^2 \omega_2^2 \omega_3 + \\
& 22c_s^2 \omega_5^2 \omega_3^2 \omega_3 - 12v_1^2 \omega_2^2 \omega_3 + 12c_s^2 \omega_5 \omega_2 \omega_3 + 12\omega_5^2 v_1^2 \omega_2 - 6c_s^2 \omega_3^2 \omega_3 + \omega_5^2 v_1^2 \omega_2^2 \omega_3 - 30c_s^2 \omega_5 \omega_2^2 \omega_3 - 12\omega_5 v_1^2 \omega_2 \omega_3 + 12c_s^2 \omega_5^2 \omega_2 - 30c_s^2 \omega_5^2 \omega_2 \omega_3 - \\
& 12\omega_5 v_1^2 \omega_2^2 + 9c_s^2 \omega_5 \omega_2^2 \omega_3 - 18c_s^2 \omega_5^2 \omega_2^2 + 8\omega_5^2 v_1^2 \omega_3^2 \omega_3 + 12c_s^2 \omega_2^2 \omega_3 + 24\omega_5^2 v_1^2 \omega_3 + 3c_s^2 \omega_5^2 \omega_2^2 + 6\omega_5 v_1^2 \omega_3^2 \\
C_{17} &= -36c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 + 6c_s^2 \omega_5^2 \omega_3^2 \omega_3 + \omega_5^2 \omega_2^2 \omega_3^2 + 12\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 6\omega_5^2 v_1^2 \omega_3^2 - 24c_s^2 \omega_5 \omega_2 \omega_3^2 + 36c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 - \omega_5^2 \omega_2^2 \omega_3^2 - \\
& 12c_s^2 \omega_5^2 \omega_3^2 + 12\omega_5 \omega_2 \omega_3^2 - 3\omega_5^2 \omega_2^2 \omega_3^2 + 6c_s^2 \omega_5^2 \omega_3^2 \omega_3 - 12c_s^2 \omega_5^2 \omega_2^2 \omega_3 + 7\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 6v_1^2 \omega_2^2 \omega_3^2 - 12c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - \\
& 6\omega_5^2 \omega_2 \omega_3^2 - 12\omega_5^2 v_1^2 \omega_3^2 \omega_3 - 36c_s^2 \omega_2^2 \omega_3^2 - 6\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 24c_s^2 \omega_5 \omega_2^2 \omega_3^2 - 6\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 21\omega_5 \omega_2^2 \omega_3^2 + 12c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 6\omega_2^2 \omega_3^2 - 12c_s^2 \omega_5^2 \omega_2 \omega_3^2 + \\
& 72c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 6\omega_5^2 v_1^2 \omega_2^2 \omega_3 + 18c_s^2 \omega_2^2 \omega_3^2 - 3\omega_5 \omega_2^2 \omega_3^2 - 24c_s^2 \omega_5 \omega_2^2 \omega_3^2 - 3\omega_2^2 \omega_3^2 + 36c_s^2 \omega_5^2 \omega_2 \omega_3^2 - 24\omega_5 v_1^2 \omega_2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 + 6\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 \\
C_{18} &= -32c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 + 6c_s^2 \omega_5^2 \omega_3^2 \omega_3 + 2\omega_5^2 \omega_2^2 \omega_3^2 - 12\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_3^2 - 12c_s^2 \omega_5 \omega_2 \omega_3^2 + 48c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 - \omega_5^2 \omega_2^2 \omega_3^2 - \\
& 24\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 12c_s^2 \omega_5^2 \omega_3^2 - 6\omega_5^2 \omega_2^2 \omega_3^2 + 4c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 - 12c_s^2 \omega_5^2 \omega_2^2 \omega_3 + 12\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 3\omega_5^2 \omega_2^2 \omega_3^2 + 30\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 6v_1^2 \omega_2^2 \omega_3^2 - 12c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 - \\
& 24\omega_2^2 v_1^2 \omega_3^2 + 12\omega_5 \omega_2^2 \omega_3^2 - 18\omega_5^2 v_1^2 \omega_3^2 \omega_3 - 12c_s^2 \omega_2^2 \omega_3^2 - 12\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 12c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2^2 \omega_2^2 - 6\omega_5 \omega_2^2 \omega_3^2 + 12c_s^2 \omega_5 \omega_2^2 \omega_3^2 - \\
& 24c_s^2 \omega_5^2 \omega_2 \omega_3^2 + 36c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 3\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 + 6c_s^2 \omega_2^2 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3^2 - 24c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 36c_s^2 \omega_5^2 \omega_2 \omega_3^2 + 12\omega_5 v_1^2 \omega_2 \omega_3^2 + 3\omega_5 \omega_2^2 \omega_3^2 \\
C_{19} &= -30c_s^2 \omega_5 \omega_3^2 - 6\omega_3^2 - 14\omega_5^2 v_1^2 \omega_2^2 - 36\omega_5 \omega_2^2 + \omega_5^2 v_1^2 \omega_3^2 + 12\omega_2^2 + 96c_s^2 \omega_5 \omega_2^2 + 9\omega_5 \omega_3^2 - 36c_s^2 \omega_5 \omega_2 + 24\omega_5 \omega_2 + 12\omega_5^2 v_1^2 \omega_2 - 12\omega_5^2 \omega_2 + \\
& 12\omega_5^2 v_1^2 - 60c_s^2 \omega_2^2 + 30c_s^2 \omega_3^2 - 60\omega_5 v_1^2 \omega_2 + 18c_s^2 \omega_5^2 \omega_2 + 48\omega_5 v_1^2 \omega_2^2 - 26c_s^2 \omega_5^2 \omega_2^2 + 12v_1^2 \omega_2^2 - \omega_5^2 \omega_2^2 + 4c_s^2 \omega_5^2 \omega_2^2 - 6\omega_5 v_1^2 \omega_3^2 + 11\omega_5^2 \omega_2^2 - 6v_1^2 \omega_3^2
\end{aligned}$$

$$C_{20} = -12v_2^2\omega_2\omega_6\omega_3 + 12c_s^2\omega_2\omega_6\omega_3 + 24v_2^2\omega_2\omega_6^2 + 12c_s^2\omega_2\omega_6^2 + 12c_s^2\omega_2^3\omega_3 + 12v_2^2\omega_6^2\omega_3 + 12c_s^2\omega_2\omega_3^2 + 9c_s^2\omega_2\omega_6\omega_3^2 - 12v_2^2\omega_2\omega_3^2 - 18c_s^2\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^2 - 9v_2^2\omega_2\omega_6\omega_3^2 + 6v_2^2\omega_2\omega_3^3 - 30c_s^2\omega_2\omega_6\omega_3^2 - 6c_s^2\omega_2\omega_3^3 - v_2^2\omega_6^2\omega_3^3 + 30v_2^2\omega_2\omega_6\omega_3^2 + 3c_s^2\omega_6^2\omega_3^2 + 22c_s^2\omega_2\omega_6^2\omega_3^2 + 8v_2^2\omega_2\omega_6^2\omega_3^2 + 6v_2^2\omega_6\omega_3^3 - 6c_s^2\omega_6\omega_3^3 - 2c_s^2\omega_2\omega_6^2\omega_3^3 + 12c_s^2\omega_6\omega_3^3 + v_2^2\omega_2\omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3^3 - 36v_2^2\omega_2\omega_6^2\omega_3 - 30c_s^2\omega_2\omega_6^2\omega_3$$

$$C_{21} = -3v_2^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^2 + 2c_s^2v_2^2\omega_2^3\omega_6^2\omega_3^2 + 10c_s^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3 + 2c_s^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 - 2c_s^4\omega_2^3\omega_3^2\omega_6\omega_3^2 + 2c_s^2\omega_5^2v_1^2\omega_2^3\omega_3^2 + 10c_s^2v_2^2\omega_5^2\omega_2\omega_6^2\omega_3^2 + 4v_2^2\omega_5^2v_1^2\omega_2^3\omega_3^2 - 4c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2v_2^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^2 - 4c_s^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 - 4c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 14v_2^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^2 + 3v_2^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 + 4c_s^4\omega_5^2\omega_2^3\omega_6\omega_3^2 + 2c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4c_s^2v_2^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 2v_2^2\omega_5^2v_1^2\omega_2^3\omega_3^2 - 4c_s^2\omega_5^2v_1^2\omega_2^3\omega_3^2 + c_s^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 12c_s^4\omega_2^3\omega_3^2\omega_6\omega_3^2 + c_s^4\omega_5\omega_2^3\omega_6^2\omega_3^2 + 10c_s^2v_2^2\omega_5\omega_2^3\omega_6^2\omega_3^2 + 2c_s^2\omega_5v_1^2\omega_2^3\omega_6^2\omega_3^2 - 2v_2^2v_1^2\omega_2^3\omega_6^2\omega_3^2 - 2c_s^2v_2^2\omega_5^2\omega_2^3\omega_6^2\omega_3^2 + 4v_2^2\omega_5v_1^2\omega_2\omega_6^2\omega_3^2 + 4v_2^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^2 - 2v_2^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 + c_s^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^2 - c_s^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 + 4c_s^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2c_s^4\omega_5\omega_2^3\omega_6^2\omega_3^2 - 8c_s^2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^2 - 14v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 4v_2^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 - 10v_2^2\omega_5v_1^2\omega_2\omega_6^2\omega_3^2 - 2c_s^4\omega_5^2\omega_2^3\omega_6^2\omega_3^2 - 4c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2c_s^4\omega_5^2\omega_2\omega_6^2\omega_3^2 + 4c_s^4\omega_5^2\omega_2\omega_6\omega_3^2 - c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 10c_s^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 - 28v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 2c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2c_s^4\omega_5^2\omega_2\omega_6^2\omega_3^2 + 4c_s^4\omega_5^2\omega_2\omega_6\omega_3^2 + 4v_2^2\omega_5v_1^2\omega_2\omega_6^2\omega_3^2 - 4c_s^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 - 4c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 14v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 4v_2^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 - 3c_s^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 8c_s^2\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^2 - 10v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 4c_s^4\omega_5\omega_2^3\omega_6^2\omega_3^2 - c_s^4\omega_5^2\omega_2^3\omega_6\omega_3^2 + 2c_s^2\omega_5v_1^2\omega_2\omega_6^2\omega_3^2 - 8c_s^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 2c_s^2v_2^2\omega_5\omega_2^3\omega_6^2\omega_3^2 - 4c_s^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 3v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 12v_2^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 - 2c_s^2\omega_5^2v_1^2\omega_2\omega_6^2\omega_3^2 + 8c_s^2v_2^2\omega_5^2\omega_2^3\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_2\omega_6^2\omega_3^2 - 4c_s^2\omega_5v_1^2\omega_2\omega_6^2\omega_3^2 - 3c_s^2v_2^2\omega_5\omega_2^3\omega_6\omega_3^2 - 2c_s^4\omega_5\omega_2^3\omega_6^2\omega_3^2 + 4c_s^4\omega_5^2\omega_2^3\omega_6\omega_3^2$$

$$C_{22} = -24v_2^2\omega_2^3\omega_6\omega_3^2 + 24c_s^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^2\omega_6^2\omega_3 - 6c_s^2\omega_2^3\omega_6\omega_3^2 + 12c_s^2\omega_2^2\omega_6^2\omega_3^2 - 48v_2^2\omega_2^2\omega_6^2\omega_3^2 - 6c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12\omega_5^2v_1^2\omega_2^3\omega_3^2 + c_s^2\omega_2^3\omega_6\omega_3^2 + 12c_s^2\omega_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^2\omega_6^2\omega_3^2 - 18v_2^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6^2\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 + 6c_s^2\omega_2\omega_6^2\omega_3^2 - 30v_2^2\omega_2\omega_6^2\omega_3^2 - 4v_2^2\omega_2^3\omega_6\omega_3^2 + c_s^2\omega_2^3\omega_6\omega_3^2 + 6c_s^2\omega_2^2\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^2 + 22v_2^2\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_3^2 - 14c_s^2\omega_2^3\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_3^2$$

$$C_{23} = -14c_s^2\omega_5^2\omega_2^3\omega_3^2 + 6c_s^2\omega_5^2\omega_3^3\omega_3 - 24\omega_5v_1^2\omega_2^3\omega_3^2 + 12\omega_5^2v_1^2\omega_3^3 - 12c_s^2\omega_5\omega_2\omega_3^2 + 12c_s^2\omega_5^2\omega_2^3\omega_3^2 + 12v_1^2\omega_2^3\omega_3^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 - 12c_s^2\omega_5^2\omega_3^3 + 6\omega_5v_1^2\omega_2^3\omega_3^2 + c_s^2\omega_2^3\omega_6\omega_3^2 + 12c_s^2\omega_2^2\omega_6^2\omega_3^2 - 18\omega_5^2v_1^2\omega_2\omega_3^2 - 6c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6^2\omega_3^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 - 4\omega_5^2v_1^2\omega_2^3\omega_3^2 + 6c_s^2\omega_2^3\omega_3^2 + 24c_s^2\omega_5^2\omega_2\omega_3^2 + 12\omega_5v_1^2\omega_2\omega_3^2 + 22\omega_5^2v_1^2\omega_2^3\omega_3^2 - 48\omega_5^2v_1^2\omega_2^3\omega_3^2 + 24c_s^2\omega_5\omega_2^3\omega_3^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 - 4\omega_5^2v_1^2\omega_2^3\omega_3^2 + 6c_s^2\omega_2^3\omega_3^2 + 24c_s^2\omega_5^2\omega_2\omega_3^2 + 12\omega_5v_1^2\omega_2\omega_3^2 + 22\omega_5^2v_1^2\omega_2^3\omega_3^2$$

$$C_{24} = -6c_s^2\omega_3^3 - 18v_2^2\omega_3^3 + 12\omega_6^2\omega_3 - 48c_s^2\omega_6^2\omega_3 + 36v_2^2\omega_3^2 + 12c_s^2\omega_3^2 + 18v_2^2\omega_6^2\omega_3 + \omega_6^2\omega_3^2 + 25c_s^2\omega_6^2\omega_3^2 + 15v_2^2\omega_6^2\omega_3^2 - 11\omega_6^2\omega_3^2 - 3v_2^2\omega_6^2\omega_3^2 - 36v_2^2\omega_6^2 + 24c_s^2\omega_6^2 - 2c_s^2\omega_6^2\omega_3^2 + 36\omega_6\omega_3^2 - 12\omega_3^2 + 27v_2^2\omega_6\omega_3^2 + 9c_s^2\omega_6\omega_3^2 + 6\omega_3^3 - 9\omega_6\omega_3^2 - 36c_s^2\omega_6\omega_3^2 - 108v_2^2\omega_6\omega_3^2 + 24c_s^2\omega_6\omega_3 + 72v_2^2\omega_6\omega_3 - 24\omega_6\omega_3$$

$$C_{25} = \omega_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 + 12\omega_3^3\omega_6\omega_3 + 72c_s^2\omega_2^3\omega_6\omega_3^2 - 3\omega_2^2\omega_6^2\omega_3^2 - 24c_s^2\omega_2^3\omega_6\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^3\omega_6^2\omega_3^2 + 6\omega_3^3\omega_6\omega_3^2 - 6v_2^2\omega_2^3\omega_6^2\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 - 24c_s^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6^2\omega_3^2 - 21\omega_2^3\omega_6\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 + 12c_s^2\omega_2^3\omega_6\omega_3^2 + 36c_s^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6^2\omega_3^2 + 7\omega_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^2 + 6c_s^2\omega_2\omega_6^2\omega_3^2 - \omega_3^3\omega_6\omega_3^2 - 12v_2^2\omega_2\omega_6^2\omega_3^2 + 6\omega_3^2\omega_3^2 + 6\omega_2^2\omega_6\omega_3^2 + 6c_s^2\omega_2^3\omega_6\omega_3^2 + 18c_s^2\omega_2^2\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^2 - 3\omega_2^2\omega_6\omega_3^2 - 3\omega_2^3\omega_3^2 - 6\omega_2^2\omega_6\omega_3^2 - 6v_2^2\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_3^2 - 36c_s^2\omega_2^3\omega_6^2\omega_3^2 - 36c_s^2\omega_2^3\omega_3^2$$

$$C_{26} = 30c_s^2\omega_3^3 - 6v_2^2\omega_3^3 - 12\omega_6^2\omega_3 + 18c_s^2\omega_6^2\omega_3 + 12v_2^2\omega_3^2 - 60c_s^2\omega_3^2 + 12v_2^2\omega_6^2\omega_3 - \omega_6^2\omega_3^2 - 26c_s^2\omega_6^2\omega_3^2 - 14v_2^2\omega_6^2\omega_3^2 + 11\omega_6^2\omega_3^2 + v_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2 + 4c_s^2\omega_6^2\omega_3^2 - 36\omega_6\omega_3^2 + 12\omega_3^2 - 6v_2^2\omega_6\omega_3^2 - 30c_s^2\omega_6\omega_3^2 - 6\omega_3^3 + 9\omega_6\omega_3^2 + 96c_s^2\omega_6\omega_3^2 + 48v_2^2\omega_6\omega_3^2 - 36c_s^2\omega_6\omega_3 - 60v_2^2\omega_6\omega_3 + 24\omega_6\omega_3$$

$$C_{27} = 2\omega_2^2\omega_6^2\omega_3^2 - 12v_2^2\omega_2^3\omega_6\omega_3^2 + 36c_s^2\omega_2^3\omega_6\omega_3^2 - 6\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^2 - 24c_s^2\omega_2^2\omega_6^2\omega_3^2 + 48c_s^2\omega_2^3\omega_6^2\omega_3^2 + 3\omega_2^3\omega_6\omega_3^2 + 12v_2^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 - 6\omega_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 + 30v_2^2\omega_2^3\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6^2\omega_3^2 - 24c_s^2\omega_2^2\omega_6^2\omega_3^2 - 24v_2^2\omega_2^3\omega_6^2\omega_3^2 + 6c_s^2\omega_2\omega_6^2\omega_3^2 - \omega_3^3\omega_6\omega_3^2 - 18v_2^2\omega_2\omega_6^2\omega_3^2 - 24v_2^2\omega_2^3\omega_6\omega_3^2 + 3v_2^2\omega_2^3\omega_6^2\omega_3^2 + 12\omega_2^2\omega_6\omega_3^2 + 4c_s^2\omega_2^3\omega_6\omega_3^2 + 6c_s^2\omega_2^2\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^2 - 6\omega_2^2\omega_6\omega_3^2 - 12v_2^2\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_3^2 - 32c_s^2\omega_2^3\omega_6^2\omega_3^2 - 12c_s^2\omega_2^2\omega_6^2\omega_3^2$$

$$C_{28} = -36v_2^2\omega_3^3 + 6c_s^2v_2^2\omega_6^2\omega_3^2 + 24c_s^4\omega_6^2\omega_3^2 - 12v_1^4\omega_6^2\omega_3^2 - 216c_s^2v_2^2\omega_6^2\omega_3^2 + 12c_s^2\omega_6^2\omega_3^2 + 72v_2^2\omega_3^2 + 108c_s^2v_2^2\omega_3^2 + 3v_1^4\omega_6^2\omega_3^2 - 3c_s^4\omega_6^2\omega_3^2 - 12c_s^2v_2^2\omega_6^2\omega_3^2 - 36c_s^2v_2^2\omega_6^2\omega_3^2 - 8c_s^2\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 - 48c_s^4\omega_6^2\omega_3^2 - 3v_2^2\omega_6^2\omega_3^2 + c_s^2\omega_6^2\omega_3^2 + 24c_s^4\omega_6\omega_3 - 72v_2^4\omega_3^2 + 30v_2^2\omega_6\omega_3^2 - 6c_s^2\omega_6\omega_3^2 + 36v_2^4\omega_3^2 + 72c_s^2v_2^2\omega_6\omega_3 + 24c_s^2\omega_6\omega_3^2 - 72v_2^2\omega_6\omega_3^2 - 24c_s^2\omega_6\omega_3 - 30v_1^4\omega_6\omega_3^2 + 24c_s^4\omega_6^2 + 6c_s^4\omega_6\omega_3^2 + 144c_s^2v_2^2\omega_6\omega_3^2 - 72c_s^2v_2^2\omega_6\omega_3^2 - 24c_s^4\omega_6\omega_3^2 + 72v_2^4\omega_6\omega_3^2$$

$$C_{29} = 30c_s^2\omega_3^3 + 42v_2^2\omega_3^3 + 6\omega_6^2\omega_3 - 30c_s^2\omega_6^2\omega_3 - 84v_2^2\omega_3^2 - 60c_s^2\omega_3^2 - 12v_2^2\omega_6^2\omega_3 - \omega_6^2\omega_3^2 - 2c_s^2\omega_6^2\omega_3^2 + 2v_2^2\omega_6^2\omega_3^2 + 2\omega_6^2\omega_3^2 + 2v_2^2\omega_6^2\omega_3^2 - 12v_2^2\omega_6^2 + 24c_s^2\omega_6^2 + c_s^2\omega_6^2\omega_3^2 - 24\omega_6\omega_3^2 + 36\omega_3^2 - 24v_2^2\omega_6\omega_3^2 - 24c_s^2\omega_6\omega_3^2 - 18\omega_3^3 + 12\omega_6\omega_3^2 + 72c_s^2\omega_6\omega_3^2 + 24v_2^2\omega_6\omega_3^2 - 12c_s^2\omega_6\omega_3 + 60v_2^2\omega_6\omega_3 - 12\omega_6\omega_3$$

$$C_{30} = -6c_s^2\omega_5\omega_2^3 + 22c_s^2\omega_4\omega_5^2\omega_2^2 - 6\omega_5^2v_1^2\omega_2^2 + 12c_s^2\omega_4\omega_5^2 + \omega_4\omega_5^2v_1^2\omega_2^2 + 24\omega_4\omega_5^2v_1^2 - \omega_5^2v_1^2\omega_2^3 - 2c_s^2\omega_4\omega_5^2\omega_2^2 + 12c_s^2\omega_5\omega_2^2 + 8\omega_4\omega_5^2v_1^2\omega_2^2 - 6c_s^2\omega_4\omega_2^3 - 12\omega_4v_1^2\omega_2^2 - 36\omega_4\omega_5^2v_1^2\omega_2 + 6\omega_4v_1^2\omega_2^3 + 12c_s^2\omega_4\omega_2^2 - 30c_s^2\omega_4\omega_5^2\omega_2 + 12\omega_5^2v_1^2\omega_2 - 12\omega_4\omega_5v_1^2\omega_2 + 12c_s^2\omega_4\omega_5\omega_2 + 12c_s^2\omega_5^2\omega_2 - 12\omega_5v_1^2\omega_2^2 + 9c_s^2\omega_4\omega_5\omega_2^2 - 18c_s^2\omega_5^2\omega_2^2 - 9\omega_4\omega_5v_1^2\omega_2^2 + 3c_s^2\omega_5^2\omega_2^2 - 30c_s^2\omega_4\omega_5\omega_2^2 + 6\omega_5v_1^2\omega_2^2 + 30\omega_4\omega_5v_1^2\omega_2^2$$

$$C_{31} = -12c_s^2\omega_4\omega_5^2\omega_2^2 + 12\omega_4^3\omega_5v_1^2\omega_2^2 + 12c_s^2\omega_4^2\omega_5\omega_2^2 + 36c_s^2\omega_4^3\omega_5^2\omega_2 - 12\omega_4\omega_5^2v_1^2\omega_2^2 + 7\omega_4^3\omega_5^2\omega_2^2 - 6\omega_4^3v_1^2\omega_2^2 + 6\omega_5^2v_1^2\omega_2^2 - 24c_s^2\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 + 6\omega_4\omega_5^2v_1^2\omega_2^2 + 6\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4^2\omega_5^2\omega_2^2 - 3\omega_4^2\omega_5\omega_2^2 - 6\omega_4^3\omega_5^2\omega_2 - 24\omega_4^3\omega_5v_1^2\omega_2 - 36c_s^2\omega_4^3\omega_5^2\omega_2^2 + \omega_4^2\omega_5^2\omega_2^2 + 6\omega_4^2\omega_5^2v_1^2\omega_2^2 + 12\omega_4^2\omega_5\omega_2 + 72c_s^2\omega_4^2\omega_5\omega_2^2 - 6\omega_4^2\omega_5^2v_1^2\omega_2^2 - 3\omega_4^2\omega_5^2\omega_2^2 - 12c_s^2\omega_4^2\omega_5^2 - 24c_s^2\omega_4^2\omega_5\omega_2^2 + 12\omega_4^2\omega_5^2v_1^2\omega_2 - 12c_s^2\omega_4^2\omega_5^2\omega_2 - 3\omega_4^2\omega_2^2 - 6\omega_4^2\omega_5^2v_1^2\omega_2^2 + 36c_s^2\omega_4^2\omega_5^2\omega_2^2 + 6\omega_4^2\omega_5\omega_2^2 - 36c_s^2\omega_4^2\omega_2^2 - 12c_s^2\omega_4^2\omega_5^2\omega_2^2 + 6\omega_4^2\omega_2^2 - 24c_s^2\omega_4^2\omega_5\omega_2 + 18c_s^2\omega_4^2\omega_2^2 - 21\omega_4^2\omega_5\omega_2^2$$

$$C_{32} = -12c_s^2\omega_4\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5v_1^2\omega_2^2 + 12c_s^2\omega_4^2\omega_5\omega_2^2 + 36c_s^2\omega_4^3\omega_5^2\omega_2 - 18\omega_4\omega_5^2v_1^2\omega_2^2 + 3\omega_4^3\omega_5^2\omega_2^2 - 6\omega_4^3v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2^2 - 24c_s^2\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^2\omega_5v_1^2\omega_2^2 + 12\omega_4^2\omega_5\omega_2^2 + 4c_s^2\omega_4^2\omega_5^2\omega_2^2 - 6\omega_4^2\omega_5\omega_2^2 - 24\omega_4^2\omega_5v_1^2\omega_2^2 - 24\omega_4^2\omega_5^2v_1^2\omega_2^2 + 12\omega_4^2\omega_5v_1^2\omega_2 - 32c_s^2\omega_4^2\omega_5^2\omega_2^2 + 2\omega_4^2\omega_5^2\omega_2^2 + 36c_s^2\omega_4^2\omega_5\omega_2^2 + 12\omega_4^2\omega_5v_1^2\omega_2^2 - 6\omega_4^2\omega_5^2\omega_2^2 - 12c_s^2\omega_4^2\omega_5^2 - 12c_s^2\omega_4^2\omega_5\omega_2^2 + 30\omega_4^2\omega_5^2v_1^2\omega_2 - 24c_s^2\omega_4^2\omega_5^2\omega_2 - 12\omega_4^2\omega_5^2v_1^2\omega_2^2 + 48c_s^2\omega_4^2\omega_5^2\omega_2^2 + 3\omega_4^2\omega_5\omega_2^2 - 12c_s^2\omega_4^2\omega_2^2 - 12c_s^2\omega_4^2\omega_5^2\omega_2^2 + 3\omega_4^2\omega_5^2v_1^2\omega_2^2 - 12c_s^2\omega_4^2\omega_5\omega_2 + 6c_s^2\omega_4^2\omega_2^2 - 6\omega_4^2\omega_5\omega_2^2$$

$$C_{33} = -30c_s^2\omega_5\omega_2^3 - 6\omega_3^3 - 14\omega_5^2v_1^2\omega_2^2 - 36\omega_5\omega_2^2 + \omega_5^2v_1^2\omega_2^2 + 12\omega_2^2 + 96c_s^2\omega_5\omega_2^2 + 9\omega_5\omega_2^3 - 36c_s^2\omega_5\omega_2 + 24\omega_5\omega_2 + 12\omega_5^2v_1^2\omega_2 - 12\omega_5^2\omega_2 + 12\omega_5^2v_1^2 - 60c_s^2\omega_2^2 + 30c_s^2\omega_2^3 - 60\omega_5v_1^2\omega_2 + 18c_s^2\omega_5^2\omega_2 + 48\omega_5v_1^2\omega_2^2 - 26c_s^2\omega_5^2\omega_2^2 + 12v_1^2\omega_2^2 - \omega_5^2\omega_2^2 + 4c_s^2\omega_5^2\omega_2^2 - 6\omega_5v_1^2\omega_2^2 + 11\omega_5^2\omega_2^2 - 6v_1^2\omega_2^3$$

$$\begin{aligned}
C_{60} &= 24c_s^2\omega_3^3\omega_6\omega_3^2 + 12\omega_3^3v_2^2\omega_6\omega_3 - 6c_s^2\omega_3^3\omega_6\omega_3^3 - 12c_s^2\omega_3^3\omega_6^2 - 30\omega_4v_2^2\omega_6^2\omega_3 + 12c_s^2\omega_4^2\omega_6^2\omega_3 + 6\omega_4^3v_2^2\omega_6\omega_3 + 6c_s^2\omega_4^3\omega_3^3 + 24\omega_4v_2^2\omega_6^2\omega_3^2 + \\
& 12v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_3^3\omega_6\omega_3 - 12c_s^2\omega_4^3\omega_3^3 - 6c_s^2\omega_4^3\omega_6^2\omega_3 - 24\omega_4^3v_2^2\omega_6\omega_3 + 24\omega_4^3v_2^2\omega_6^2\omega_3 + 22\omega_4^3v_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_4\omega_3^3\omega_3^2 + \\
& 6c_s^2\omega_4\omega_6^2\omega_3^3 - 4\omega_4^3v_2^2\omega_6\omega_3^3 + c_s^2\omega_4^3\omega_6^2\omega_3^3 + 12\omega_4^3v_2^2\omega_3^3 + 22\omega_4^3v_2^2\omega_6^2\omega_3^3 - 6\omega_4^3v_2^2\omega_3^3 - 14c_s^2\omega_4^3\omega_6^2\omega_3^3 - 18\omega_4^3v_2^2\omega_6\omega_3 - 48\omega_4^3v_2^2\omega_6^2\omega_3^2 \\
C_{61} &= 72\omega_7\omega_4v_3^2 + 36\omega_4^2v_3^2 - 9\omega_7\omega_4^3 - 36c_s^2\omega_7\omega_4^2 + 36\omega_7\omega_4^2 + 15\omega_7^2\omega_4^2v_3^2 + 9c_s^2\omega_7\omega_4^3 + 12c_s^2\omega_4^2 - 24\omega_7\omega_4 - 18\omega_4^3v_3^2 + 24c_s^2\omega_7\omega_4 - 6c_s^2\omega_4^3 - \\
& 3\omega_7^2\omega_4^3v_3^2 - 48c_s^2\omega_7^2\omega_4 + 24c_s^2\omega_7^2 + 12\omega_7^2\omega_4 - 36\omega_7^2v_3^2 + 27\omega_7\omega_4^3v_3^2 + 6\omega_4^3 - 11\omega_7^2\omega_4^2 + 18\omega_7^2\omega_4v_3^2 - 2c_s^2\omega_7^2\omega_4^3 - 108\omega_7\omega_4^2v_3^2 + \omega_7^2\omega_4^3 - 12\omega_4^3 + 25c_s^2\omega_7^2\omega_4 \\
C_{62} &= -3\omega_7\omega_4^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4\omega_2^2 + 72c_s^2\omega_7\omega_4^3\omega_2^2 + 12\omega_7^2\omega_4\omega_3^2v_3^2 - 12c_s^2\omega_7^2\omega_2^2 + 6\omega_7\omega_4^3\omega_3^2 - 6\omega_4^3\omega_3^2v_3^2 - 24c_s^2\omega_7\omega_4^3\omega_2^2 + 6\omega_7^2\omega_3^3\omega_2^2v_3^2 + \\
& 36c_s^2\omega_7^2\omega_4\omega_2^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 - 24c_s^2\omega_7\omega_4^3\omega_2^2 + 6\omega_7\omega_4^3\omega_2^2 - 6\omega_7^2\omega_4\omega_2^2 + 12c_s^2\omega_7\omega_4^3\omega_2^2 + 6\omega_7^2\omega_2^2v_3^2 + 6\omega_7^2\omega_4^3v_3^2 - 21\omega_7\omega_4^3\omega_2^2 - 24\omega_7\omega_4\omega_2^2v_3^2 + \\
& 6c_s^2\omega_7^2\omega_3^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 + 12\omega_7^2\omega_3^3v_3^2 - 6\omega_7^2\omega_4^3\omega_2^2v_3^2 + 12\omega_7\omega_4\omega_2^2 + 6\omega_4^3\omega_2^2 - 3\omega_7^2\omega_4^3\omega_2^2 - 36c_s^2\omega_4^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 + 7\omega_7^2\omega_4\omega_2^2 - 3\omega_4^3\omega_2^2 + \\
& \omega_7^2\omega_3^3\omega_2^2 - 6\omega_7^2\omega_2^2v_3^2 - 36c_s^2\omega_7^2\omega_4^3\omega_2^2 + 6c_s^2\omega_7^2\omega_4^3\omega_2 - 12\omega_7^2\omega_3^3\omega_2^2v_3^2 - \omega_7^2\omega_4^3\omega_2^2 - 24c_s^2\omega_7\omega_4\omega_2^2 + 36c_s^2\omega_7^2\omega_4^3\omega_2^2 + 18c_s^2\omega_4^3\omega_2^2 \\
C_{63} &= -60\omega_7\omega_4v_3^2 + 12\omega_4^2v_3^2 + 9\omega_7\omega_4^3 + 96c_s^2\omega_7\omega_4^2 - 36\omega_7\omega_4^2 - 14\omega_7^2\omega_4^2v_3^2 - 30c_s^2\omega_7\omega_4^3 - 60c_s^2\omega_4^2 + 24\omega_7\omega_4 - 6\omega_4^3v_3^2 - 36c_s^2\omega_7\omega_4 + 30c_s^2\omega_4^3 + \\
& \omega_7^2\omega_4^3v_3^2 + 18c_s^2\omega_7^2\omega_4 - 12\omega_7^2\omega_4 + 12\omega_7^2v_3^2 - 6\omega_7\omega_4^3v_3^2 - 6\omega_4^3 + 11\omega_7^2\omega_4^2 + 12\omega_7^2\omega_4v_3^2 + 4c_s^2\omega_7^2\omega_4^3 + 48\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 + 12\omega_4^3 - 26c_s^2\omega_7^2\omega_4 \\
C_{64} &= -6\omega_7\omega_4^3\omega_2^2 - 24c_s^2\omega_7^2\omega_4\omega_2^2 + 36c_s^2\omega_7\omega_4^3\omega_2^2 - 24\omega_7\omega_4^3\omega_2^2v_3^2 + 30\omega_7^2\omega_4\omega_2^2v_3^2 - 12c_s^2\omega_7^2\omega_2^2 + 3\omega_7\omega_4^3\omega_2^2 - 6\omega_4^3\omega_2^2v_3^2 - 24c_s^2\omega_7\omega_4^3\omega_2^2 + \\
& 36c_s^2\omega_7^2\omega_4\omega_2^2 - 12\omega_7\omega_4^3\omega_2^2v_3^2 - 12c_s^2\omega_7\omega_4^3\omega_2^2 + 12\omega_7^2\omega_3^3\omega_2^2 + 12\omega_7^2\omega_4^3\omega_2^2 + 12\omega_7^2\omega_3^3v_3^2 - 6\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4\omega_2^2v_3^2 + \\
& 4c_s^2\omega_7^2\omega_3^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 + 12\omega_7^2\omega_3^3v_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 6\omega_7^2\omega_4^3\omega_2^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 - 12c_s^2\omega_4^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 + 3\omega_7^2\omega_4^3\omega_2^2 + 2\omega_7^2\omega_3^3\omega_2^2 - \\
& 12\omega_7^2\omega_4^3v_3^2 - 32c_s^2\omega_7^2\omega_4^3\omega_2^2 + 6c_s^2\omega_7^2\omega_4^3\omega_2 - 18\omega_7^2\omega_4^3\omega_2v_3^2 - \omega_7^2\omega_4^3\omega_2^2 - 12c_s^2\omega_7\omega_4\omega_2^2 + 48c_s^2\omega_7^2\omega_4^3\omega_2^2 + 6c_s^2\omega_4^3\omega_2^2 - 24\omega_7^2\omega_3^3v_3^2 \\
C_{65} &= -36c_s^2\omega_4^3\omega_3^3 - 12c_s^2\omega_7^2\omega_3^3\omega_2^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 + 7\omega_7^2\omega_4^3\omega_3^3 + 6c_s^2\omega_7^2\omega_4^3\omega_3^3 - 12c_s^2\omega_7^2\omega_2^2\omega_3 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2 + 12\omega_7\omega_4\omega_3^3 + 6\omega_4^3\omega_3^3 - 3\omega_7^2\omega_4^3\omega_3^3 - \\
& \omega_7^2\omega_3^3\omega_3^3 - 24c_s^2\omega_7\omega_4\omega_3^3 + 36c_s^2\omega_7^2\omega_4^3\omega_3^3 + 18c_s^2\omega_4^3\omega_3^3 + 12\omega_7^2\omega_4\omega_3^3v_3^2 - 3\omega_4^3\omega_3^3 + \omega_7^2\omega_4^3\omega_3^3 - 6\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_4^3v_3^2 - 36c_s^2\omega_7^2\omega_4^3\omega_3^3 + \\
& 6\omega_7^2\omega_4^3\omega_3^2v_3^2 + 6c_s^2\omega_7^2\omega_4^3\omega_3^3 + 6\omega_7\omega_4^3\omega_3^3 - 6\omega_7^2\omega_4^3\omega_3^3v_3^2 - 24c_s^2\omega_7\omega_4^3\omega_2^2 - 12\omega_7^2\omega_4^3\omega_3^2v_3^2 + 36c_s^2\omega_7^2\omega_4^3\omega_3^3 - 3\omega_7\omega_4^3\omega_3^3 - 12c_s^2\omega_7^2\omega_4^3\omega_3^3 + \\
& 72c_s^2\omega_7\omega_4^3\omega_3^3 - 12c_s^2\omega_7^2\omega_3^3 + 12c_s^2\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4\omega_3^3v_3^2 + 12\omega_4^3\omega_3^3v_3^2 - 6\omega_7^2\omega_4^3\omega_3^3v_3^2 - 21\omega_7\omega_4^3\omega_3^3 - 24c_s^2\omega_7\omega_4^3\omega_3^3 + 6\omega_7\omega_4^3\omega_3^3 - 6\omega_7^2\omega_4\omega_3^3 \\
C_{66} &= -60\omega_7\omega_4v_3^2 + 12\omega_4^2v_3^2 + 9\omega_7\omega_4^3 + 96c_s^2\omega_7\omega_4^2 - 36\omega_7\omega_4^2 - 14\omega_7^2\omega_4^2v_3^2 - 30c_s^2\omega_7\omega_4^3 - 60c_s^2\omega_4^2 + 24\omega_7\omega_4 - 6\omega_4^3v_3^2 - 36c_s^2\omega_7\omega_4 + 30c_s^2\omega_4^3 + \\
& \omega_7^2\omega_4^3v_3^2 + 18c_s^2\omega_7^2\omega_4 - 12\omega_7^2\omega_4 + 12\omega_7^2v_3^2 - 6\omega_7\omega_4^3v_3^2 - 6\omega_4^3 + 11\omega_7^2\omega_4^2 + 12\omega_7^2\omega_4v_3^2 + 4c_s^2\omega_7^2\omega_4^3 + 48\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 + 12\omega_4^3 - 26c_s^2\omega_7^2\omega_4 \\
C_{67} &= -12c_s^2\omega_4^3\omega_3^3 - 12c_s^2\omega_7^2\omega_3^3\omega_2^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 + 3\omega_7^2\omega_4^3\omega_3^3 + 3\omega_7^2\omega_3^3\omega_2^2 + 4c_s^2\omega_7^2\omega_4^3\omega_3^3 - 12c_s^2\omega_7^2\omega_2^2\omega_3 - 6\omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_3^3 - \\
& 12c_s^2\omega_7\omega_4\omega_3^3 - 24\omega_7\omega_4^3\omega_2^2v_3^2 + 48c_s^2\omega_7^2\omega_4^3\omega_2^2 + 6c_s^2\omega_3^3\omega_3^3 + 30\omega_7^2\omega_4\omega_3^3v_3^2 + 2\omega_7^2\omega_3^3\omega_2^2 - 6\omega_4^3\omega_3^3v_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 32c_s^2\omega_7^2\omega_4^3\omega_3^3 + 6c_s^2\omega_7^2\omega_3^3\omega_3^3 + \\
& 3\omega_7\omega_4^3\omega_3^3 - 12\omega_7^2\omega_4^3\omega_3^2v_3^2 - 24c_s^2\omega_7\omega_4^3\omega_2^2 - 18\omega_7^2\omega_4^3\omega_3^2v_3^2 + 36c_s^2\omega_7^2\omega_4^3\omega_3^3 - 6\omega_7\omega_4^3\omega_3^3 - 24c_s^2\omega_7^2\omega_4^3\omega_2^2 + 36c_s^2\omega_7\omega_4^3\omega_3^3 - 24\omega_7^2\omega_3^3v_3^2 - 12c_s^2\omega_7^2\omega_3^3 + \\
& 12c_s^2\omega_7\omega_4^3\omega_3^3 + 12\omega_7\omega_4\omega_3^3v_3^2 + 12\omega_4^3\omega_3^3v_3^2 + 12\omega_7^2\omega_4^3\omega_3^3v_3^2 - 6\omega_7\omega_4^3\omega_3^3 + 12\omega_7\omega_4^3\omega_3^2v_3^2 - 12c_s^2\omega_7\omega_4^3\omega_3^3 + 12\omega_7\omega_4^3\omega_3^3 \\
C_{68} &= 72\omega_2^2v_3^2 + 24c_s^2\omega_7\omega_4^2 + 6c_s^2\omega_7^2\omega_4^3\omega_3^2 + 24c_s^4\omega_7\omega_4 + 12\omega_7^2\omega_2^2v_3^2 + 72\omega_7\omega_4^2v_3^4 - 216c_s^2\omega_4^2v_3^2 + 24c_s^4\omega_7^2 - 6c_s^2\omega_7\omega_4^3 - 12c_s^2\omega_7^2\omega_4^2v_3^2 - 24c_s^4\omega_7\omega_4^2 - \\
& 36\omega_3^3v_3^2 - 24c_s^2\omega_7\omega_4 + 72c_s^2\omega_7\omega_4v_3^2 - 30\omega_7\omega_4^3v_3^2 + 108c_s^2\omega_3^3v_3^2 - 3\omega_7^2\omega_4^3v_3^2 + 6c_s^4\omega_7\omega_4^2 + 144c_s^2\omega_7\omega_4^2v_3^2 + 12c_s^2\omega_7^2\omega_4 + 36\omega_4^3v_3^4 - 3c_s^4\omega_7^2\omega_3^3 + \\
& 3\omega_7^2\omega_4^3v_3^4 - 36c_s^2\omega_7^2\omega_4v_3^2 + 24c_s^4\omega_7^2\omega_4 + 30\omega_7\omega_4^3v_3^2 - 48c_s^4\omega_7\omega_4 - 72\omega_4^2v_3^4 + c_s^2\omega_7^2\omega_4^3 - 72c_s^2\omega_7\omega_4^3v_3^2 - 72\omega_7\omega_4^2v_3^2 - 8c_s^2\omega_7^2\omega_4^2 - 12\omega_7^2\omega_4^2v_3^4 \\
C_{69} &= 60\omega_7\omega_4v_3^2 - 84\omega_4^2v_3^2 + 12\omega_7\omega_4^3 + 72c_s^2\omega_7\omega_4^2 - 24\omega_7\omega_4^2 + 2\omega_7^2\omega_4^2v_3^2 - 24c_s^2\omega_7\omega_4^3 - 60c_s^2\omega_4^2 - 12\omega_7\omega_4 + 42\omega_3^3v_3^2 - 12c_s^2\omega_7\omega_4 + 30c_s^2\omega_4^3 + \\
& 2\omega_7^2\omega_4^3v_3^2 - 30c_s^2\omega_7^2\omega_4 + 24c_s^2\omega_7^2 + 6\omega_7^2\omega_4 - 12\omega_7^2v_3^2 - 24\omega_7\omega_4^3v_3^2 - 18\omega_4^3 + 2\omega_7^2\omega_4^2 - 12\omega_7^2\omega_4v_3^2 + c_s^2\omega_7^2\omega_4^3 + 24\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 + 36\omega_4^3 - 2c_s^2\omega_7^2\omega_4^2
\end{aligned}$$

3 Comparison of SRT, MRT, and CLBM

3.1 Conservation of mass equation

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + v_1 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \rho \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + v_2 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \rho \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + v_3 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \rho \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + C_{D_x \rho, D_t v_1}^{(0)} \delta_l \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + C_{D_x \rho, D_x v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} \\
& + C_{D_x v_1, D_x v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + C_{D_x \rho, D_y v_1}^{(0)} \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + C_{D_x \rho, D_y v_2}^{(0)} \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + C_{D_x v_1, D_y v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& C_{D_x \rho, D_z v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + C_{D_x \rho, D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + C_{D_x v_1, D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + C_{D_y \rho, D_t v_2}^{(0)} \delta_l \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + \\
& C_{D_y \rho, D_x v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + C_{D_y \rho, D_x v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + C_{D_y \rho, D_y v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + C_{D_y v_2, D_y v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + \\
& C_{D_y \rho, D_z v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + C_{D_y \rho, D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + C_{D_y v_2, D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + C_{D_z \rho, D_t v_3}^{(0)} \delta_l \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + \\
& C_{D_z \rho, D_x v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + C_{D_z \rho, D_x v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + C_{D_z \rho, D_y v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + C_{D_z \rho, D_y v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\
& C_{D_z \rho, D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + C_{D_z v_3, D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + C_{D_t D_x v_1}^{(0)} \delta_l \frac{\partial^2 v_1}{\partial t \partial x_1} + C_{D_z^2 \rho}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + C_{D_x^2 v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& C_{D_t D_y v_2}^{(0)} \delta_l \frac{\partial^2 v_2}{\partial t \partial x_2} + C_{D_x D_y \rho}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + C_{D_x D_y v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + C_{D_x D_y v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + C_{D_y^2 \rho}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + C_{D_y^2 v_2}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_2}{\partial x_2^2} \\
& + C_{D_t D_z v_3}^{(0)} \delta_l \frac{\partial^2 v_3}{\partial t \partial x_3} + C_{D_x D_z \rho}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + C_{D_x D_z v_1}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + C_{D_x D_z v_3}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + C_{D_y D_z \rho}^{(0)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} +
\end{aligned}$$

[illegible]

coefficient $C_{D_{x\rho}, D_t v_1}^{(0)}$ at $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t}$:

$$C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{1}{2\omega_2}$$

$$C_{D_x \rho, D_t v_1}^{(0), \text{CLBM1}} = C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_t v_1}^{(0), \text{CLBM2}} = C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x \rho, D_x v_1}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_x \rho, D_x v_1}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_1}{2\omega}$$

$$C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_x \rho, D_x v_1}^{(0), \text{MRT2}} = C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_1}^{(0), \text{CLBM1}} = C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_1}^{(0), \text{CLBM2}} = C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x v_1, D_x v_1}^{(0)}$ **at** $\left(\frac{\partial v_1}{\partial x_1}\right)^2$:

$$C_{D_x v_1, D_x v_1}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{\rho}{2\omega_2}$$

$$C_{D_x v_1, D_x v_1}^{(0), \text{MRT2}} = C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_x v_1, D_x v_1}^{(0), \text{CLBM1}} = C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_x v_1, D_x v_1}^{(0), \text{CLBM2}} = C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x \rho, D_y v_1}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2}$:

$$C_{D_x \rho, D_y v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{2\omega}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{MRT2}} = C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{CLBM1}} = C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{CLBM2}} = C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x \rho, D_y v_2}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_x \rho, D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{\omega}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}} = (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_1}{\omega_2 \omega_3}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{MRT2}} = C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{CLBM1}} = C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{CLBM2}} = C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_x v_1, D_y v_2}^{(0)}$ **at** $\frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_x v_1, D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{MRT1}} = (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{\rho}{\omega_2 \omega_3}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{MRT}2} = C_{D_x v_1, D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{CLBM}1} = C_{D_x v_1, D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{CLBM}2} = C_{D_x v_1, D_y v_2}^{(0), \text{MRT}1}$$

coefficient $C_{D_x \rho, D_z v_1}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3}$:

$$C_{D_x \rho, D_z v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{2\omega}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{MRT}1} = (2 - \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{MRT}2} = C_{D_x \rho, D_z v_1}^{(0), \text{MRT}1}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{CLBM}1} = C_{D_x \rho, D_z v_1}^{(0), \text{MRT}1}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{CLBM}2} = C_{D_x \rho, D_z v_1}^{(0), \text{MRT}1}$$

coefficient $C_{D_x \rho, D_z v_3}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_x \rho, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{\omega}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{MRT}1} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1}{\omega_4 \omega_2}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{MRT}2} = C_{D_x \rho, D_z v_3}^{(0), \text{MRT}1}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{CLBM}1} = C_{D_x \rho, D_z v_3}^{(0), \text{MRT}1}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{CLBM}2} = C_{D_x \rho, D_z v_3}^{(0), \text{MRT}1}$$

coefficient $C_{D_x v_1, D_z v_3}^{(0)}$ **at** $\frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_x v_1, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{MRT}1} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{\rho}{\omega_4 \omega_2}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{MRT}2} = C_{D_x v_1, D_z v_3}^{(0), \text{MRT}1}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{CLBM}1} = C_{D_x v_1, D_z v_3}^{(0), \text{MRT}1}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{CLBM}2} = C_{D_x v_1, D_z v_3}^{(0), \text{MRT}1}$$

coefficient $C_{D_y \rho, D_t v_2}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t}$:

$$C_{D_y \rho, D_t v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{MRT}1} = (-2 + \omega_3) \frac{1}{2\omega_3}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{MRT}2} = C_{D_y \rho, D_t v_2}^{(0), \text{MRT}1}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{CLBM}1} = C_{D_y \rho, D_t v_2}^{(0), \text{MRT}1}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{CLBM}2} = C_{D_y \rho, D_t v_2}^{(0), \text{MRT}1}$$

coefficient $C_{D_y \rho, D_x v_1}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_y \rho, D_x v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{\omega}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}} = (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2}{\omega_2 \omega_3}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{MRT2}} = C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{CLBM1}} = C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{CLBM2}} = C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_y \rho, D_x v_2}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1}$:

$$C_{D_y \rho, D_x v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{2\omega}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y \rho, D_y v_2}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_y \rho, D_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_2}{2\omega}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y v_2, D_y v_2}^{(0)}$ **at** $\left(\frac{\partial v_2}{\partial x_2} \right)^2$:

$$C_{D_y v_2, D_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{\rho}{2\omega_3}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{MRT2}} = C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{CLBM1}} = C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{CLBM2}} = C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y \rho, D_z v_2}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_y \rho, D_z v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{2\omega}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y \rho, D_z v_3}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_y \rho, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{\omega}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}} = (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_2}{\omega_4 \omega_3}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{MRT2}} = C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{CLBM1}} = C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{CLBM2}} = C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_y v_2, D_z v_3}^{(0)}$ **at** $\frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_y v_2, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}} = (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{\rho}{\omega_4 \omega_3}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{MRT2}} = C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{CLBM1}} = C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{CLBM2}} = C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_z \rho, D_t v_3}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t}$:

$$C_{D_z \rho, D_t v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{1}{2\omega_4}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_z \rho, D_x v_1}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_z \rho, D_x v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{\omega}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3}{\omega_4 \omega_2}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{MRT2}} = C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{CLBM1}} = C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{CLBM2}} = C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_z \rho, D_x v_3}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1}$:

$$C_{D_z \rho, D_x v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{2\omega}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_z \rho, D_y v_2}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_z \rho, D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{\omega}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}} = (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_3}{\omega_4 \omega_3}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{MRT2}} = C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{CLBM1}} = C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{CLBM2}} = C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_z \rho, D_y v_3}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2}$:

$$C_{D_z \rho, D_y v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{2\omega}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_z \rho, D_z v_3}^{(0)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_z \rho, D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_3}{2\omega}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_z v_3, D_z v_3}^{(0)}$ **at** $\left(\frac{\partial v_3}{\partial x_3} \right)^2$:

$$C_{D_z v_3, D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho}{2\omega_4}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{MRT2}} = C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{CLBM1}} = C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{CLBM2}} = C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x v_1}^{(0)}$ **at** $\frac{\partial^2 v_1}{\partial t \partial x_1}$:

$$C_{D_t D_x v_1}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_x v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{\rho}{2\omega_2}$$

$$C_{D_t D_x v_1}^{(0), \text{MRT2}} = C_{D_t D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x v_1}^{(0), \text{CLBM1}} = C_{D_t D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x v_1}^{(0), \text{CLBM2}} = C_{D_t D_x v_1}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_x \rho}^{(0)} \text{ at } \frac{\partial^2 \rho}{\partial x_1^2} :$$

$$C_{D_x \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_x \rho}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_x \rho}^{(0), \text{MRT2}} = C_{D_x \rho}^{(0), \text{MRT1}}$$

$$C_{D_x \rho}^{(0), \text{CLBM1}} = C_{D_x \rho}^{(0), \text{MRT1}}$$

$$C_{D_x \rho}^{(0), \text{CLBM2}} = C_{D_x \rho}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_x v_1}^{(0)} \text{ at } \frac{\partial^2 v_1}{\partial x_1^2} :$$

$$C_{D_x v_1}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho v_1}{2\omega}$$

$$C_{D_x v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{\rho v_1}{2\omega_2}$$

$$C_{D_x v_1}^{(0), \text{MRT2}} = C_{D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_x v_1}^{(0), \text{CLBM1}} = C_{D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_x v_1}^{(0), \text{CLBM2}} = C_{D_x v_1}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_t D_y v_2}^{(0)} \text{ at } \frac{\partial^2 v_2}{\partial t \partial x_2} :$$

$$C_{D_t D_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{\rho}{2\omega_3}$$

$$C_{D_t D_y v_2}^{(0), \text{MRT2}} = C_{D_t D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y v_2}^{(0), \text{CLBM1}} = C_{D_t D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y v_2}^{(0), \text{CLBM2}} = C_{D_t D_y v_2}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_x D_y \rho}^{(0)} \text{ at } \frac{\partial^2 \rho}{\partial x_1 \partial x_2} :$$

$$C_{D_x D_y \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 v_1}{\omega}$$

$$C_{D_x D_y \rho}^{(0), \text{MRT1}} = (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 v_1}{\omega_2 \omega_3}$$

$$C_{D_x D_y \rho}^{(0), \text{MRT2}} = C_{D_x D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y \rho}^{(0), \text{CLBM1}} = C_{D_x D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y \rho}^{(0), \text{CLBM2}} = C_{D_x D_y \rho}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_x D_y v_1}^{(0)} \text{ at } \frac{\partial^2 v_1}{\partial x_1 \partial x_2} :$$

$$C_{D_x D_y v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_x D_y v_1}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_x D_y v_1}^{(0), \text{MRT2}} = C_{D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(0), \text{CLBM1}} = C_{D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(0), \text{CLBM2}} = C_{D_x D_y v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_y v_2}^{(0)}$ **at** $\frac{\partial^2 v_2}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho v_1}{2\omega}$$

$$C_{D_x D_y v_2}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{\rho v_1}{2\omega_2}$$

$$C_{D_x D_y v_2}^{(0), \text{MRT2}} = C_{D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(0), \text{CLBM1}} = C_{D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(0), \text{CLBM2}} = C_{D_x D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y^2 \rho}^{(0)}$ **at** $\frac{\partial^2 \rho}{\partial x_2^2}$:

$$C_{D_y^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{MRT2}} = C_{D_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 \rho}^{(0), \text{CLBM1}} = C_{D_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 \rho}^{(0), \text{CLBM2}} = C_{D_y^2 \rho}^{(0), \text{MRT1}}$$

coefficient $C_{D_y^2 v_2}^{(0)}$ **at** $\frac{\partial^2 v_2}{\partial x_2^2}$:

$$C_{D_y^2 v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_y^2 v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(0), \text{CLBM1}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_z v_3}^{(0)}$ **at** $\frac{\partial^2 v_3}{\partial t \partial x_3}$:

$$C_{D_t D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho}{2\omega_4}$$

$$C_{D_t D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_z \rho}^{(0)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3 v_1}{\omega}$$

$$C_{D_x D_z \rho}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3 v_1}{\omega_4 \omega_2}$$

$$C_{D_x D_z \rho}^{(0), \text{MRT2}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z \rho}^{(0), \text{CLBM1}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z \rho}^{(0), \text{CLBM2}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_z v_1}^{(0)}$ **at** $\frac{\partial^2 v_1}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3 \rho}{2\omega}$$

$$C_{D_x D_z v_1}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{v_3 \rho}{2\omega_4}$$

$$C_{D_x D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_z v_3}^{(0)}$ **at** $\frac{\partial^2 v_3}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho v_1}{2\omega}$$

$$C_{D_x D_z v_3}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{\rho v_1}{2\omega_2}$$

$$C_{D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(0), \text{CLBM1}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(0), \text{CLBM2}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_y D_z \rho}^{(0)}$ **at** $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 v_3}{\omega}$$

$$C_{D_y D_z \rho}^{(0), \text{MRT1}} = (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_2 v_3}{\omega_4 \omega_3}$$

$$C_{D_y D_z \rho}^{(0), \text{MRT2}} = C_{D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y D_z \rho}^{(0), \text{CLBM1}} = C_{D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y D_z \rho}^{(0), \text{CLBM2}} = C_{D_y D_z \rho}^{(0), \text{MRT1}}$$

coefficient $C_{D_y D_z v_2}^{(0)}$ **at** $\frac{\partial^2 v_2}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3 \rho}{2\omega}$$

$$C_{D_y D_z v_2}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{v_3 \rho}{2\omega_4}$$

$$C_{D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_y D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y D_z v_3}^{(0)}$ **at** $\frac{\partial^2 v_3}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_y D_z v_3}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_y D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_z^2 \rho}^{(0)}$ **at** $\frac{\partial^2 \rho}{\partial x_3^2}$:

$$C_{D_z^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{c_s^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), \text{MRT2}} = C_{D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_z^2 \rho}^{(0), \text{CLBM1}} = C_{D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_z^2 \rho}^{(0), \text{CLBM2}} = C_{D_z^2 \rho}^{(0), \text{MRT1}}$$

coefficient $C_{D_z^2 v_3}^{(0)}$ **at** $\frac{\partial^2 v_3}{\partial x_3^2}$:

$$C_{D_z^2 v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_3 \rho}{2\omega}$$

$$C_{D_z^2 v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{v_3 \rho}{2\omega_4}$$

$$C_{D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_t^2 D_x v_1}^{(0)}$ **at** $\frac{\partial^3 v_1}{\partial t^2 \partial x_1}$:

$$C_{D_t^2 D_x v_1}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{MRT1}} = (12 + \omega_2^2 - 12\omega_2) \frac{\rho}{12\omega_2^2}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{MRT2}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x^2 v_1}^{(0)}$ **at** $\frac{\partial^3 v_1}{\partial t \partial x_1^2}$:

$$C_{D_t D_x^2 v_1}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{\rho v_1}{6\omega^2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{MRT1}} = (12 - 6\omega_5 - 6\omega_2 + \omega_5 \omega_2) \frac{\rho v_1}{6\omega_5 \omega_2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{CLBM1}} = (12 + \omega^2 - 12\omega_2) \frac{\rho v_1}{6\omega_2^2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 v_1}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^3 \rho}^{(0)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^3} :$$

$$C_{D_x^3 \rho}^{(0), \text{SRT}} = (6 - 6v_1^2 + \omega^2 - 6\omega + 6\omega v_1^2 - \omega^2 v_1^2 - 3c_s^2 \omega^2 + 18c_s^2 \omega - 18c_s^2) \frac{v_1}{6\omega^2}$$

$$C_{D_x^3 \rho}^{(0), \text{MRT1}} = (3\omega_5 \omega_2 v_1^2 + 3\omega_2^2 v_1^2 - 6c_s^2 \omega_2 + 3c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 3\omega_2^2 + 6\omega_2 - 3c_s^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 - 3\omega_5 \omega_2 - \omega_5 \omega_2^2 v_1^2 - 6\omega_2 v_1^2 + 15c_s^2 \omega_5 \omega_2) \frac{v_1}{6\omega_5 \omega_2^2}$$

$$C_{D_x^3 \rho}^{(0), \text{MRT2}} = C_{D_x^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(0), \text{CLBM1}} = (6 + 3\omega_5 v_1^2 - 6v_1^2 - \omega_5 \omega_2 v_1^2 + 9c_s^2 \omega_2 + 9c_s^2 \omega_5 - 3\omega_5 - 3\omega_2 + \omega_5 \omega_2 + 3\omega_2 v_1^2 - 3c_s^2 \omega_5 \omega_2 - 18c_s^2) \frac{v_1}{6\omega_5 \omega_2}$$

$$C_{D_x^3 \rho}^{(0), \text{CLBM2}} = C_{D_x^3 \rho}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^3 v_1}^{(0)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^3} :$$

$$C_{D_x^3 v_1}^{(0), \text{SRT}} = (12 - 24v_1^2 + 2\omega^2 - 12\omega + 24\omega v_1^2 - 5\omega^2 v_1^2 - 3c_s^2 \omega^2 + 24c_s^2 \omega - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^3 v_1}^{(0), \text{MRT1}} = (-12\omega_5 v_1^2 + 18\omega_5 \omega_2 v_1^2 + 6\omega_2^2 v_1^2 - 12c_s^2 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 6\omega_2^2 + 12\omega_2 - 3c_s^2 \omega_5 \omega_2^2 + 2\omega_5 \omega_2^2 - 6\omega_5 \omega_2 - 5\omega_5 \omega_2^2 v_1^2 - 12\omega_2 v_1^2 + 18c_s^2 \omega_5 \omega_2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^3 v_1}^{(0), \text{MRT2}} = C_{D_x^3 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(0), \text{CLBM1}} = (12\omega_5 v_1^2 + 6\omega_5 \omega_2 v_1^2 + 18\omega_2^2 v_1^2 - 12c_s^2 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 6\omega_2^2 + 12\omega_2 - 3c_s^2 \omega_5 \omega_2^2 + 2\omega_5 \omega_2^2 - 6\omega_5 \omega_2 - 5\omega_5 \omega_2^2 v_1^2 - 36\omega_2 v_1^2 + 18c_s^2 \omega_5 \omega_2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^3 v_1}^{(0), \text{CLBM2}} = C_{D_x^3 v_1}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t^2 D_y v_2}^{(0)} \text{ at } \frac{\partial^3 v_2}{\partial t^2 \partial x_2} :$$

$$C_{D_t^2 D_y v_2}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{MRT1}} = (12 + \omega_3^2 - 12\omega_3) \frac{\rho}{12\omega_3^2}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{MRT2}} = C_{D_t^2 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{CLBM1}} = C_{D_t^2 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{CLBM2}} = C_{D_t^2 D_y v_2}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_t D_x D_y v_1}^{(0)} \text{ at } \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} :$$

$$C_{D_t D_x D_y v_1}^{(0), \text{SRT}} = (-6 - \omega^2 + 6\omega) \frac{v_2 \rho}{3\omega^2}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{MRT1}} = (3\omega_3^2 - 6\omega_2 + 9\omega_2\omega_3 - 2\omega_2\omega_3^2 - 6\omega_3) \frac{v_2 \rho}{6\omega_2 \omega_3^2}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{CLBM1}} = C_{D_t D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{CLBM2}} = C_{D_t D_x D_y v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x D_y v_2}^{(0)}$ **at** $\frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2}$:

$$C_{D_t D_x D_y v_2}^{(0), \text{SRT}} = (-6 - \omega^2 + 6\omega) \frac{\rho v_1}{3\omega^2}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{MRT1}} = (-2\omega_2^2\omega_3 + 3\omega_2^2 - 6\omega_2 + 9\omega_2\omega_3 - 6\omega_3) \frac{\rho v_1}{6\omega_2^2 \omega_3}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{MRT2}} = C_{D_t D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{CLBM1}} = C_{D_t D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{CLBM2}} = C_{D_t D_x D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_x^2 D_y \rho}^{(0)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y \rho}^{(0), \text{SRT}} = (6v_1^2 - 6\omega v_1^2 + \omega^2 v_1^2 - c_s^2 \omega^2 + 6c_s^2 \omega - 6c_s^2) \frac{v_2}{2\omega^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{MRT1}} = (4c_s^2 \omega_5 \omega_2 \omega_3^2 - 2c_s^2 \omega_5 \omega_3^2 + \omega_5 \omega_2^2 \omega_3^2 v_1^2 - 2\omega_2 \omega_3^2 v_1^2 + c_s^2 \omega_2^2 \omega_3^2 + 2\omega_5 \omega_2 \omega_3 v_1^2 - 2c_s^2 \omega_5 \omega_2 \omega_3 + 4\omega_5 \omega_3^2 v_1^2 + c_s^2 \omega_5 \omega_2^2 \omega_3 - 4\omega_5 \omega_2 \omega_3^2 v_1^2 - 2c_s^2 \omega_2 \omega_3^2 + 2\omega_5 \omega_2^2 v_1^2 + \omega_2^2 \omega_3^2 v_1^2 - 3\omega_5 \omega_2^2 \omega_3 v_1^2 - c_s^2 \omega_5 \omega_2^2 \omega_3^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{MRT2}} = C_{D_x^2 D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{CLBM1}} = (4c_s^2 \omega_5 \omega_2 \omega_3^2 - 2c_s^2 \omega_5 \omega_3^2 + \omega_5 \omega_2^2 \omega_3^2 v_1^2 + 2\omega_2 \omega_3^2 v_1^2 + c_s^2 \omega_2^2 \omega_3^2 + 2\omega_5 \omega_2 \omega_3 v_1^2 - 2c_s^2 \omega_5 \omega_2 \omega_3 + c_s^2 \omega_5 \omega_2^2 \omega_3 - 2\omega_5 \omega_2 \omega_3^2 v_1^2 - 2c_s^2 \omega_2 \omega_3^2 + 2\omega_5 \omega_2^2 v_1^2 - \omega_2^2 \omega_3^2 v_1^2 - 3\omega_5 \omega_2^2 \omega_3 v_1^2 - c_s^2 \omega_5 \omega_2^2 \omega_3^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{CLBM2}} = C_{D_x^2 D_y \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^2 D_y v_1}^{(0)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_1}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_2 \rho v_1}{6\omega^2}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{MRT1}} = (6\omega_3^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 6\omega_2^2 - 6\omega_2 \omega_3^2) \frac{v_2 \rho v_1}{6\omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{CLBM1}} = C_{D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{CLBM2}} = C_{D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x^2 D_y v_2}^{(0)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_2}^{(0), \text{SRT}} = (\omega^2 v_1^2 - 3c_s^2 \omega^2 + 24c_s^2 \omega - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{MRT1}} = (12\omega_5 v_1^2 - 6\omega_5 \omega_2 v_1^2 + 6\omega_2^2 v_1^2 - 12c_s^2 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 3c_s^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 v_1^2 - 12\omega_2 v_1^2 + 18c_s^2 \omega_5 \omega_2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{MRT2}} = C_{D_x^2 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{CLBM1}} = (-12\omega_5 v_1^2 + 6\omega_5 \omega_2 v_1^2 - 6\omega_2^2 v_1^2 - 12c_s^2 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 3c_s^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 v_1^2 + 12\omega_2 v_1^2 + 18c_s^2 \omega_5 \omega_2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{CLBM2}} = C_{D_x^2 D_y v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t D_y^2 v_2}^{(0)}$ **at** $\frac{\partial^3 v_2}{\partial t \partial x_2^2}$:

$$C_{D_t D_y^2 v_2}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_2 \rho}{6\omega^2}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{MRT1}} = (12 + \omega_6 \omega_3 - 6\omega_6 - 6\omega_3) \frac{v_2 \rho}{6\omega_6 \omega_3}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_t D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{CLBM1}} = (12 + \omega_3^2 - 12\omega_3) \frac{v_2 \rho}{6\omega_3^2}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_t D_y^2 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x D_y^2 \rho}^{(0)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 \rho}^{(0), \text{SRT}} = (-6\omega v_2^2 + 6v_2^2 - c_s^2 \omega^2 + 6c_s^2 \omega + \omega^2 v_2^2 - 6c_s^2) \frac{v_1}{2\omega^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{MRT1}} = (\omega_2^2 v_2^2 \omega_3^2 + c_s^2 \omega_2^2 \omega_3^2 + 4c_s^2 \omega_2^2 \omega_6 \omega_3 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 + 4\omega_2^2 v_2^2 \omega_6 - 4\omega_2^2 v_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_2^2 \omega_3 + 2v_2^2 \omega_6 \omega_3^2 - c_s^2 \omega_2^2 \omega_6 \omega_3^2 - 2\omega_2^2 v_2^2 \omega_3 - 2c_s^2 \omega_2^2 \omega_6 + c_s^2 \omega_2 \omega_6 \omega_3^2 - 3\omega_2 v_2^2 \omega_6 \omega_3^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{MRT2}} = C_{D_x D_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{CLBM1}} = (-\omega_2^2 v_2^2 \omega_3^2 + c_s^2 \omega_2^2 \omega_3^2 + 4c_s^2 \omega_2^2 \omega_6 \omega_3 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2\omega_2^2 v_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_2^2 \omega_3 + 2v_2^2 \omega_6 \omega_3^2 - c_s^2 \omega_2^2 \omega_6 \omega_3^2 + 2\omega_2^2 v_2^2 \omega_3 - 2c_s^2 \omega_2^2 \omega_6 + c_s^2 \omega_2 \omega_6 \omega_3^2 - 3\omega_2 v_2^2 \omega_6 \omega_3^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{CLBM2}} = C_{D_x D_y^2 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x D_y^2 v_1}^{(0)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 v_1}^{(0), \text{SRT}} = (-3c_s^2 \omega^2 + 24c_s^2 \omega + \omega^2 v_2^2 - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{MRT1}} = (-6v_2^2 \omega_6 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_3 + 6v_2^2 \omega_3^2 + 18c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_3 + 6c_s^2 \omega_3^2 + 12v_2^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{MRT2}} = C_{D_x D_y^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{CLBM1}} = (6v_2^2 \omega_6 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_3 - 6v_2^2 \omega_3^2 + 18c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3 + 6c_s^2 \omega_3^2 - 12v_2^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{CLBM2}} = C_{D_x D_y^2 v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x D_y^2 v_2}^{(0)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 v_2}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_2 \rho v_1}{6\omega^2}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{MRT1}} = (6\omega_3^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 6\omega_2^2 - 6\omega_2 \omega_3^2) \frac{v_2 \rho v_1}{6\omega_2^2 \omega_3^2}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_x D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{CLBM1}} = C_{D_x D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_x D_y^2 v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y^3 \rho}^{(0)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{D_y^3 \rho}^{(0), \text{SRT}} = (6 + 6\omega v_2^2 + \omega^2 - 6\omega - 6v_2^2 - 3c_s^2 \omega^2 + 18c_s^2 \omega - \omega^2 v_2^2 - 18c_s^2) \frac{v_2}{6\omega^2}$$

$$C_{D_y^3 \rho}^{(0), \text{MRT1}} = (3v_2^2 \omega_6 \omega_3 - 3\omega_3^2 - v_2^2 \omega_6 \omega_3^2 - 6c_s^2 \omega_3 + 3v_2^2 \omega_3^2 - 3\omega_6 \omega_3 + 15c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3 + \omega_6 \omega_3^2 + 3c_s^2 \omega_3^2 + 6\omega_3) \frac{v_2}{6\omega_6 \omega_3^2}$$

$$C_{D_y^3 \rho}^{(0), \text{MRT2}} = C_{D_y^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(0), \text{CLBM1}} = (6 - v_2^2 \omega_6 \omega_3 - 6v_2^2 + 9c_s^2 \omega_3 + \omega_6 \omega_3 - 3c_s^2 \omega_6 \omega_3 + 9c_s^2 \omega_6 + 3v_2^2 \omega_3 - 3\omega_6 + 3v_2^2 \omega_6 - 3\omega_3 - 18c_s^2) \frac{v_2}{6\omega_6 \omega_3}$$

$$C_{D_y^3 \rho}^{(0), \text{CLBM2}} = C_{D_y^3 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_y^3 v_2}^{(0)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^3}$:

$$C_{D_y^3 v_2}^{(0), \text{SRT}} = (12 + 24\omega v_2^2 + 2\omega^2 - 12\omega - 24v_2^2 - 3c_s^2 \omega^2 + 24c_s^2 \omega - 5\omega^2 v_2^2 - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_y^3 v_2}^{(0), \text{MRT1}} =$$

$$(18v_2^2 \omega_6 \omega_3 - 6\omega_3^2 - 5v_2^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_3 + 6v_2^2 \omega_3^2 - 6\omega_6 \omega_3 + 18c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_3 + 2\omega_6 \omega_3^2 + 6c_s^2 \omega_3^2 - 12v_2^2 \omega_6 + 12\omega_3) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^3 v_2}^{(0), \text{MRT2}} = C_{D_y^3 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(0), \text{CLBM1}} =$$

$$(6v_2^2 \omega_6 \omega_3 - 6\omega_3^2 - 5v_2^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_3 + 18v_2^2 \omega_3^2 - 6\omega_6 \omega_3 + 18c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 - 36v_2^2 \omega_3 + 2\omega_6 \omega_3^2 + 6c_s^2 \omega_3^2 + 12v_2^2 \omega_6 + 12\omega_3) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^3 v_2}^{(0), \text{CLBM2}} = C_{D_y^3 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t^2 D_z v_3}^{(0)}$ **at** $\frac{\partial^3 v_3}{\partial t^2 \partial x_3}$:

$$C_{D_t^2 D_z v_3}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{MRT1}} = (12 - 12\omega_4 + \omega_4^2) \frac{\rho}{12\omega_4^2}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{CLBM1}} = C_{D_t^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{CLBM2}} = C_{D_t^2 D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x D_z v_1}^{(0)}$ **at** $\frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3}$:

$$C_{D_t D_x D_z v_1}^{(0), \text{SRT}} = (-6 - \omega^2 + 6\omega) \frac{v_3 \rho}{3\omega^2}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{MRT1}} = (-6\omega_4 + 3\omega_4^2 - 2\omega_4^2 \omega_2 + 9\omega_4 \omega_2 - 6\omega_2) \frac{v_3 \rho}{6\omega_4^2 \omega_2}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_t D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_t D_x D_z v_1}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_t D_x D_z v_3}^{(0)} \text{ at } \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} :$$

$$C_{D_t D_x D_z v_3}^{(0), \text{SRT}} = (-6 - \omega^2 + 6\omega) \frac{\rho v_1}{3\omega^2}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{MRT1}} = (-6\omega_4 + 9\omega_4\omega_2 + 3\omega_2^2 - 6\omega_2 - 2\omega_4\omega_2^2) \frac{\rho v_1}{6\omega_4\omega_2^2}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_x D_z v_3}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_x^2 D_z \rho}^{(0)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z \rho}^{(0), \text{SRT}} = (6v_1^2 - 6\omega v_1^2 + \omega^2 v_1^2 - c_s^2 \omega^2 + 6c_s^2 \omega - 6c_s^2) \frac{v_3}{2\omega^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{MRT1}} = (c_s^2 \omega_4^2 \omega_2^2 - 3\omega_4 \omega_5 \omega_2^2 v_1^2 - 2c_s^2 \omega_4^2 \omega_5 - c_s^2 \omega_4^2 \omega_5 \omega_2^2 + 4c_s^2 \omega_4^2 \omega_5 \omega_2 - 4\omega_4^2 \omega_5 \omega_2 v_1^2 - 2\omega_4^2 \omega_2 v_1^2 - 2c_s^2 \omega_4^2 \omega_2 + \omega_4^2 \omega_5 \omega_2^2 v_1^2 + \omega_4^2 \omega_2^2 v_1^2 - 2c_s^2 \omega_4 \omega_5 \omega_2 + 4\omega_4^2 \omega_5 v_1^2 + 2\omega_5 \omega_2^2 v_1^2 + c_s^2 \omega_4 \omega_5 \omega_2^2 + 2\omega_4 \omega_5 \omega_2 v_1^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{MRT2}} = C_{D_x^2 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{CLBM1}} = (c_s^2 \omega_4^2 \omega_2^2 - 3\omega_4 \omega_5 \omega_2^2 v_1^2 - 2c_s^2 \omega_4^2 \omega_5 - c_s^2 \omega_4^2 \omega_5 \omega_2^2 + 4c_s^2 \omega_4^2 \omega_5 \omega_2 - 2\omega_4^2 \omega_5 \omega_2 v_1^2 + 2\omega_4^2 \omega_2 v_1^2 - 2c_s^2 \omega_4^2 \omega_2 + \omega_4^2 \omega_5 \omega_2^2 v_1^2 - \omega_4^2 \omega_2^2 v_1^2 - 2c_s^2 \omega_4 \omega_5 \omega_2 + 2\omega_5 \omega_2^2 v_1^2 + c_s^2 \omega_4 \omega_5 \omega_2^2 + 2\omega_4 \omega_5 \omega_2 v_1^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{CLBM2}} = C_{D_x^2 D_z \rho}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^2 D_z v_1}^{(0)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z v_1}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_3 \rho v_1}{6\omega^2}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{MRT1}} = (\omega_4^2 \omega_2^2 + 6\omega_4^2 - 6\omega_4^2 \omega_2 + 6\omega_2^2 - 6\omega_4 \omega_2^2) \frac{v_3 \rho v_1}{6\omega_4^2 \omega_2^2}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{CLBM1}} = C_{D_x^2 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{CLBM2}} = C_{D_x^2 D_z v_1}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_x^2 D_z v_3}^{(0)} \text{ at } \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z v_3}^{(0), \text{SRT}} = (\omega^2 v_1^2 - 3c_s^2 \omega^2 + 24c_s^2 \omega - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{MRT1}} = (12\omega_5 v_1^2 - 6\omega_5 \omega_2 v_1^2 + 6\omega_2^2 v_1^2 - 12c_s^2 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 3c_s^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 v_1^2 - 12\omega_2 v_1^2 + 18c_s^2 \omega_5 \omega_2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_x^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{CLBM1}} = (-12\omega_5 v_1^2 + 6\omega_5 \omega_2 v_1^2 - 6\omega_2^2 v_1^2 - 12c_s^2 \omega_2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_5 - 3c_s^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 v_1^2 + 12\omega_2 v_1^2 + 18c_s^2 \omega_5 \omega_2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{CLBM2}} = C_{D_x^2 D_z v_3}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_y D_z v_2}^{(0)} \text{ at } \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} :$$

$$C_{D_t D_y D_z v_2}^{(0), \text{SRT}} = (-6 - \omega^2 + 6\omega) \frac{v_3 \rho}{3\omega^2}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{MRT1}} = (9\omega_4 \omega_3 - 6\omega_4 + 3\omega_4^2 - 2\omega_4^2 \omega_3 - 6\omega_3) \frac{v_3 \rho}{6\omega_4^2 \omega_3}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_t D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_t D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_t D_y D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_y D_z v_3}^{(0)}$ at $\frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3}$:

$$C_{D_t D_y D_z v_3}^{(0), \text{SRT}} = (-6 - \omega^2 + 6\omega) \frac{v_2 \rho}{3\omega^2}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{MRT1}} = (9\omega_4 \omega_3 + 3\omega_3^2 - 6\omega_4 - 2\omega_4 \omega_3^2 - 6\omega_3) \frac{v_2 \rho}{6\omega_4 \omega_3^2}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_y D_z \rho}^{(0)}$ at $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z \rho}^{(0), \text{SRT}} = (6 + \omega^2 - 6\omega) \frac{2v_2 v_3 v_1}{\omega^2}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{MRT1}} = (\omega_4^2 \omega_2 \omega_3 + \omega_4^2 \omega_2^2 + \omega_4 \omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 - 2\omega_4 \omega_2^2 \omega_3^2 - 2\omega_4^2 \omega_2 \omega_3^2 + \omega_4^2 \omega_2^2 \omega_3^2 + \omega_4^2 \omega_3^2 + \omega_4 \omega_2 \omega_3^2 - 2\omega_4^2 \omega_2^2 \omega_3) \frac{2v_2 v_3 v_1}{\omega_4^2 \omega_2^2 \omega_3^2}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{MRT2}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{CLBM1}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{CLBM2}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_y D_z v_1}^{(0)}$ at $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_1}^{(0), \text{SRT}} = (6 + \omega^2 - 6\omega) \frac{2v_2 v_3 \rho}{3\omega^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT1}} = (6\omega_4 \omega_3 + 3\omega_3^2 - 6\omega_4 \omega_3^2 + 3\omega_4^2 + 2\omega_4^2 \omega_3 - 6\omega_4^2 \omega_3) \frac{v_2 v_3 \rho}{3\omega_4^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_y D_z v_2}^{(0)}$ at $\frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_2}^{(0), \text{SRT}} = (6 + \omega^2 - 6\omega) \frac{2v_3 \rho v_1}{3\omega^2}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT1}} = (2\omega_4^2 \omega_2^2 + 3\omega_4^2 - 6\omega_4^2 \omega_2 + 6\omega_4 \omega_2 + 3\omega_2^2 - 6\omega_4 \omega_2^2) \frac{v_3 \rho v_1}{3\omega_4^2 \omega_2^2}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_y D_z v_3}^{(0)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_3}^{(0), \text{SRT}} = (6 + \omega^2 - 6\omega) \frac{2v_2 \rho v_1}{3\omega^2}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{MRT1}} = (3\omega_3^2 + 2\omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 3\omega_2^2 + 6\omega_2 \omega_3 - 6\omega_2 \omega_3^2) \frac{v_2 \rho v_1}{3\omega_2^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_y^2 D_z \rho}^{(0)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z \rho}^{(0), \text{SRT}} = (-6\omega v_2^2 + 6v_2^2 - c_s^2 \omega^2 + 6c_s^2 \omega + \omega^2 v_2^2 - 6c_s^2) \frac{v_3}{2\omega^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{MRT1}} = (\omega_4^2 v_2^2 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + 4c_s^2 \omega_4^2 \omega_6 \omega_3 - c_s^2 \omega_4^2 \omega_6 \omega_3^2 + 4\omega_4^2 v_2^2 \omega_6 + 2v_2^2 \omega_6 \omega_3^2 - 4\omega_4^2 v_2^2 \omega_6 \omega_3 - 2\omega_4^2 v_2^2 \omega_3 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + c_s^2 \omega_4 \omega_6 \omega_3^2 + c_s^2 \omega_4^2 \omega_3^2 - 2c_s^2 \omega_4^2 \omega_3 - 2c_s^2 \omega_4 \omega_6 \omega_3 + 2\omega_4 v_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_4^2 \omega_6) \frac{v_3}{2\omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{MRT2}} = C_{D_y^2 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{CLBM1}} = (-\omega_4^2 v_2^2 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + 4c_s^2 \omega_4^2 \omega_6 \omega_3 - c_s^2 \omega_4^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 - 2\omega_4^2 v_2^2 \omega_6 \omega_3 + 2\omega_4^2 v_2^2 \omega_3 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + c_s^2 \omega_4 \omega_6 \omega_3^2 + c_s^2 \omega_4^2 \omega_3^2 - 2c_s^2 \omega_4^2 \omega_3 - 2c_s^2 \omega_4 \omega_6 \omega_3 + 2\omega_4 v_2^2 \omega_6 \omega_3 - 2c_s^2 \omega_4^2 \omega_6) \frac{v_3}{2\omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{CLBM2}} = C_{D_y^2 D_z \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_y^2 D_z v_2}^{(0)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_2}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_2 v_3 \rho}{6\omega^2}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{MRT1}} = (6\omega_3^2 - 6\omega_4 \omega_3^2 + 6\omega_4^2 + \omega_4^2 \omega_3^2 - 6\omega_4^2 \omega_3) \frac{v_2 v_3 \rho}{6\omega_4^2 \omega_3^2}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{MRT2}} = C_{D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{CLBM1}} = C_{D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{CLBM2}} = C_{D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_y^2 D_z v_3}^{(0)}$ **at** $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_3}^{(0), \text{SRT}} = (-3c_s^2 \omega^2 + 24c_s^2 \omega + \omega^2 v_2^2 - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{MRT1}} = (-6v_2^2 \omega_6 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_3 + 6v_2^2 \omega_3^2 + 18c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_3 + 6c_s^2 \omega_3^2 + 12v_2^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_y^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{CLBM1}} = (6v_2^2 \omega_6 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_3 - 6v_2^2 \omega_3^2 + 18c_s^2 \omega_6 \omega_3 - 12c_s^2 \omega_6 - 3c_s^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3 + 6c_s^2 \omega_3^2 - 12v_2^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{CLBM2}} = C_{D_y^2 D_z v_3}^{(0), \text{CLBM1}}$$

coefficient $C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0)}$ **at** $\frac{\partial^3 v_3}{\partial t \partial x_3^2}$:

$$C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_3 \rho}{6\omega^2}$$

$$C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}} = (12 - 6\omega_7 - 6\omega_4 + \omega_7 \omega_4) \frac{v_3 \rho}{6\omega_7 \omega_4}$$

$$C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}} = (12 - 12\omega_4 + \omega_4^2) \frac{v_3 \rho}{6\omega_4^2}$$

$$C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}}$$

coefficient $C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_3^2}$:

$$C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{SRT}} = (-6\omega v_3^2 + 6v_3^2 - c_s^2 \omega^2 + \omega^2 v_3^2 + 6c_s^2 \omega - 6c_s^2) \frac{v_1}{2\omega^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{MRT1}} = (c_s^2 \omega_4^2 \omega_2^2 + 4c_s^2 \omega_7 \omega_4 \omega_2^2 - 2\omega_4 \omega_2^2 v_3^2 + 2\omega_7 \omega_4^2 v_3^2 - 2c_s^2 \omega_7 \omega_2^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - 2c_s^2 \omega_7 \omega_4 \omega_2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2 + c_s^2 \omega_7 \omega_4^2 \omega_2 - 4\omega_7 \omega_4 \omega_2^2 v_3^2 + 4\omega_7 \omega_2^2 v_3^2 + \omega_4^2 \omega_2^2 v_3^2 - 2c_s^2 \omega_4 \omega_2^2 - c_s^2 \omega_7 \omega_4^2 \omega_2^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{MRT2}} = C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{CLBM1}} = (c_s^2 \omega_4^2 \omega_2^2 + 4c_s^2 \omega_7 \omega_4 \omega_2^2 + 2\omega_4 \omega_2^2 v_3^2 + 2\omega_7 \omega_4^2 v_3^2 - 2c_s^2 \omega_7 \omega_2^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - 2c_s^2 \omega_7 \omega_4 \omega_2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2 + c_s^2 \omega_7 \omega_4^2 \omega_2 - 2\omega_7 \omega_4 \omega_2^2 v_3^2 - \omega_4^2 \omega_2^2 v_3^2 - 2c_s^2 \omega_4 \omega_2^2 - c_s^2 \omega_7 \omega_4^2 \omega_2^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{CLBM2}} = C_{\mathbf{D}_x \mathbf{D}_z^2 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{SRT}} = (-3c_s^2 \omega^2 + \omega^2 v_3^2 + 24c_s^2 \omega - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{MRT1}} = (-12c_s^2 \omega_7 - 12\omega_4 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 18c_s^2 \omega_7 \omega_4 + 6c_s^2 \omega_4^2 + 12\omega_7 v_3^2 - 6\omega_7 \omega_4 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 + 6\omega_4^2 v_3^2 - 12c_s^2 \omega_4) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{MRT2}} = C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{CLBM1}} = (-12c_s^2 \omega_7 + 12\omega_4 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 18c_s^2 \omega_7 \omega_4 + 6c_s^2 \omega_4^2 - 12\omega_7 v_3^2 + 6\omega_7 \omega_4 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 - 6\omega_4^2 v_3^2 - 12c_s^2 \omega_4) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{CLBM2}} = C_{\mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_3^2}$:

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_3 \rho v_1}{6\omega^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}} = (\omega_4^2 \omega_2^2 + 6\omega_4^2 - 6\omega_4^2 \omega_2 + 6\omega_2^2 - 6\omega_4 \omega_2^2) \frac{v_3 \rho v_1}{6\omega_4^2 \omega_2^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}} = C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}}$$

coefficient $C_{\mathbf{D}_y \mathbf{D}_z^2 \rho}^{(0)}$ **at** $\frac{\partial^3 \rho}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 \rho}^{(0), \text{SRT}} = (-6\omega v_3^2 + 6v_3^2 - c_s^2 \omega^2 + \omega^2 v_3^2 + 6c_s^2 \omega - 6c_s^2) \frac{v_2}{2\omega^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{MRT}1} = (2\omega_7 \omega_4^2 v_3^2 + c_s^2 \omega_7 \omega_4^2 \omega_3 + 4\omega_7 v_3^2 \omega_3^2 - 4\omega_7 \omega_4 v_3^2 \omega_3^2 + 2\omega_7 \omega_4 v_3^2 \omega_3 + \omega_4^2 v_3^2 \omega_3^2 - 2c_s^2 \omega_4 \omega_3^2 - c_s^2 \omega_7 \omega_4^2 \omega_3^2 - 2\omega_4 v_3^2 \omega_3^2 - 3\omega_7 \omega_4^2 v_3^2 \omega_3 - 2c_s^2 \omega_7 \omega_3^2 + c_s^2 \omega_4^2 \omega_3^2 + 4c_s^2 \omega_7 \omega_4 \omega_3^2 - 2c_s^2 \omega_7 \omega_4 \omega_3 + \omega_7 \omega_4^2 v_3^2 \omega_3^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{MRT}2} = C_{D_y D_z^2 \rho}^{(0), \text{MRT}1}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{CLBM}1} = (2\omega_7 \omega_4^2 v_3^2 + c_s^2 \omega_7 \omega_4^2 \omega_3 - 2\omega_7 \omega_4 v_3^2 \omega_3^2 + 2\omega_7 \omega_4 v_3^2 \omega_3 - \omega_4^2 v_3^2 \omega_3^2 - 2c_s^2 \omega_4 \omega_3^2 - c_s^2 \omega_7 \omega_4^2 \omega_3^2 + 2\omega_4 v_3^2 \omega_3^2 - 3\omega_7 \omega_4^2 v_3^2 \omega_3 - 2c_s^2 \omega_7 \omega_3^2 + c_s^2 \omega_4^2 \omega_3^2 + 4c_s^2 \omega_7 \omega_4 \omega_3^2 - 2c_s^2 \omega_7 \omega_4 \omega_3 + \omega_7 \omega_4^2 v_3^2 \omega_3^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{CLBM}2} = C_{D_y D_z^2 \rho}^{(0), \text{CLBM}1}$$

$$\text{coefficient } C_{D_y D_z^2 v_2}^{(0)} \text{ at } \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} :$$

$$C_{D_y D_z^2 v_2}^{(0), \text{SRT}} = (-3c_s^2 \omega^2 + \omega^2 v_3^2 + 24c_s^2 \omega - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{MRT}1} = (-12c_s^2 \omega_7 - 12\omega_4 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 18c_s^2 \omega_7 \omega_4 + 6c_s^2 \omega_4^2 + 12\omega_7 v_3^2 - 6\omega_7 \omega_4 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 + 6\omega_4^2 v_3^2 - 12c_s^2 \omega_4) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{MRT}2} = C_{D_y D_z^2 v_2}^{(0), \text{MRT}1}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{CLBM}1} = (-12c_s^2 \omega_7 + 12\omega_4 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 18c_s^2 \omega_7 \omega_4 + 6c_s^2 \omega_4^2 - 12\omega_7 v_3^2 + 6\omega_7 \omega_4 v_3^2 - 3c_s^2 \omega_7 \omega_4^2 - 6\omega_4^2 v_3^2 - 12c_s^2 \omega_4) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{CLBM}2} = C_{D_y D_z^2 v_2}^{(0), \text{CLBM}1}$$

$$\text{coefficient } C_{D_y D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} :$$

$$C_{D_y D_z^2 v_3}^{(0), \text{SRT}} = (12 + \omega^2 - 12\omega) \frac{v_2 v_3 \rho}{6\omega^2}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{MRT}1} = (6\omega_3^2 - 6\omega_4 \omega_3^2 + 6\omega_4^2 + \omega_4^2 \omega_3^2 - 6\omega_4^2 \omega_3) \frac{v_2 v_3 \rho}{6\omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{MRT}2} = C_{D_y D_z^2 v_3}^{(0), \text{MRT}1}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{CLBM}1} = C_{D_y D_z^2 v_3}^{(0), \text{MRT}1}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{CLBM}2} = C_{D_y D_z^2 v_3}^{(0), \text{MRT}1}$$

$$\text{coefficient } C_{D_z^3 \rho}^{(0)} \text{ at } \frac{\partial^3 \rho}{\partial x_3^3} :$$

$$C_{D_z^3 \rho}^{(0), \text{SRT}} = (6 + 6\omega v_3^2 + \omega^2 - 6\omega - 6v_3^2 - 3c_s^2 \omega^2 - \omega^2 v_3^2 + 18c_s^2 \omega - 18c_s^2) \frac{v_3}{6\omega^2}$$

$$C_{D_z^3 \rho}^{(0), \text{MRT}1} = (-12c_s^2 \omega_7 - 6\omega_4 v_3^2 - \omega_7 \omega_4^2 v_3^2 + 6\omega_4 - 3\omega_4^2 + 15c_s^2 \omega_7 \omega_4 + 3c_s^2 \omega_4^2 - 3\omega_7 \omega_4 + 3\omega_7 \omega_4 v_3^2 + \omega_7 \omega_4^2 - 3c_s^2 \omega_7 \omega_4^2 + 3\omega_4^2 v_3^2 - 6c_s^2 \omega_4) \frac{v_3}{6\omega_7 \omega_4^2}$$

$$C_{D_z^3 \rho}^{(0), \text{MRT}2} = C_{D_z^3 \rho}^{(0), \text{MRT}1}$$

$$C_{D_z^3 \rho}^{(0), \text{CLBM}1} = (6 + 9c_s^2 \omega_7 + 3\omega_4 v_3^2 - 3\omega_7 - 3\omega_4 - 6v_3^2 - 3c_s^2 \omega_7 \omega_4 + \omega_7 \omega_4 + 3\omega_7 v_3^2 - \omega_7 \omega_4 v_3^2 - 18c_s^2 + 9c_s^2 \omega_4) \frac{v_3}{6\omega_7 \omega_4}$$

$$C_{D_z^3 \rho}^{(0), \text{CLBM}2} = C_{D_z^3 \rho}^{(0), \text{CLBM}1}$$

$$\text{coefficient } C_{D_z^3 v_3}^{(0)} \text{ at } \frac{\partial^3 v_3}{\partial x_3^3} :$$

$$C_{D_z^3 v_3}^{(0), \text{SRT}} = (12 + 24\omega v_3^2 + 2\omega^2 - 12\omega - 24v_3^2 - 3c_s^2 \omega^2 - 5\omega^2 v_3^2 + 24c_s^2 \omega - 24c_s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_2^3 v_3}^{(0), \text{MRT}1} = (-12c_s^2\omega_7 - 12\omega_4v_3^2 - 5\omega_7\omega_4v_3^2 + 12\omega_4 - 6\omega_4^2 + 18c_s^2\omega_7\omega_4 + 6c_s^2\omega_4^2 - 6\omega_7\omega_4 - 12\omega_7v_3^2 + 18\omega_7\omega_4v_3^2 + 2\omega_7\omega_4^2 - 3c_s^2\omega_7\omega_4^2 + 6\omega_4^2v_3^2 - 12c_s^2\omega_4) \frac{\rho}{12\omega_7\omega_4^2}$$

$$C_{D_2^3 v_3}^{(0), \text{MRT}2} = C_{D_2^3 v_3}^{(0), \text{MRT}1}$$

$$C_{D_2^3 v_3}^{(0), \text{CLBM}1} = (-12c_s^2\omega_7 - 36\omega_4v_3^2 - 5\omega_7\omega_4v_3^2 + 12\omega_4 - 6\omega_4^2 + 18c_s^2\omega_7\omega_4 + 6c_s^2\omega_4^2 - 6\omega_7\omega_4 + 12\omega_7v_3^2 + 6\omega_7\omega_4v_3^2 + 2\omega_7\omega_4^2 - 3c_s^2\omega_7\omega_4^2 + 18\omega_4^2v_3^2 - 12c_s^2\omega_4) \frac{\rho}{12\omega_7\omega_4^2}$$

$$C_{D_2^3 v_3}^{(0), \text{CLBM}2} = C_{D_2^3 v_3}^{(0), \text{CLBM}1}$$

$$\text{coefficient } C_{D_t^3 D_x v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t^3 \partial x_1} :$$

$$C_{D_t^3 D_x v_1}^{(0), \text{SRT}} = (-2 - \omega^2 + 3\omega) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3 D_x v_1}^{(0), \text{MRT}1} = (-2 - \omega_2^2 + 3\omega_2) \frac{\rho}{2\omega_2^3}$$

$$C_{D_t^3 D_x v_1}^{(0), \text{MRT}2} = C_{D_t^3 D_x v_1}^{(0), \text{MRT}1}$$

$$C_{D_t^3 D_x v_1}^{(0), \text{CLBM}1} = C_{D_t^3 D_x v_1}^{(0), \text{MRT}1}$$

$$C_{D_t^3 D_x v_1}^{(0), \text{CLBM}2} = C_{D_t^3 D_x v_1}^{(0), \text{MRT}1}$$

$$\text{coefficient } C_{D_t^2 D_x^2 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} :$$

$$C_{D_t^2 D_x^2 v_1}^{(0), \text{SRT}} = (-2 - \omega^2 + 3\omega) \frac{3\rho v_1}{2\omega^3}$$

$$C_{D_t^2 D_x^2 v_1}^{(0), \text{MRT}1} = (-\omega_5^2\omega_2 - \omega_5^2\omega_2^2 - 4\omega_2^2 - 2\omega_5\omega_2^3 + 8\omega_5\omega_2^2 + 2\omega_2^3 - 4\omega_5\omega_2 + 2\omega_5^2) \frac{\rho v_1}{2\omega_5^2\omega_2^3}$$

$$C_{D_t^2 D_x^2 v_1}^{(0), \text{MRT}2} = C_{D_t^2 D_x^2 v_1}^{(0), \text{MRT}1}$$

$$C_{D_t^2 D_x^2 v_1}^{(0), \text{CLBM}1} = (-2 - \omega_2^2 + 3\omega_2) \frac{3\rho v_1}{2\omega_2^3}$$

$$C_{D_t^2 D_x^2 v_1}^{(0), \text{CLBM}2} = C_{D_t^2 D_x^2 v_1}^{(0), \text{CLBM}1}$$

$$\text{coefficient } C_{D_t D_x^3 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t \partial x_1^3} :$$

$$C_{D_t D_x^3 v_1}^{(0), \text{SRT}} = (-36 + 72v_1^2 - 20\omega^2 + 54\omega + \omega^3 - 108\omega v_1^2 + 42\omega^2 v_1^2 + 34c_s^2\omega^2 - 2c_s^2\omega^3 - 3\omega^3 v_1^2 - 90c_s^2\omega + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x^3 v_1}^{(0), \text{MRT}1} = (27\omega_5^2\omega_2^2 v_1^2 + 48\omega_5\omega_2 v_1^2 + 12\omega_5^2\omega_2 + 24c_s^2\omega_5^2 + 12\omega_2^2 v_1^2 - 48c_s^2\omega_5^2\omega_2 + 25c_s^2\omega_5^2\omega_2^2 + 12c_s^2\omega_2^2 - 3\omega_5^2\omega_2^3 v_1^2 - 11\omega_5^2\omega_2^2 - 6c_s^2\omega_2^3 - 2c_s^2\omega_5^2\omega_2^3 - 6\omega_2^3 v_1^2 + \omega_5^2\omega_2^3 + 9c_s^2\omega_5\omega_2^3 - 12\omega_2^2 + 15\omega_5\omega_2^3 v_1^2 - 9\omega_5\omega_2^3 - 36c_s^2\omega_5\omega_2^2 + 36\omega_5\omega_2^2 + 6\omega_2^3 - 24\omega_5\omega_2 - 60\omega_5\omega_2^2 v_1^2 + 24c_s^2\omega_5\omega_2 + 12\omega_5^2 v_1^2 - 42\omega_5^2\omega_2 v_1^2) \frac{\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_t D_x^3 v_1}^{(0), \text{MRT}2} = C_{D_t D_x^3 v_1}^{(0), \text{MRT}1}$$

$$C_{D_t D_x^3 v_1}^{(0), \text{CLBM}1} = (15\omega_5^2\omega_2^2 v_1^2 + 72\omega_5\omega_2 v_1^2 + 12\omega_5^2\omega_2 + 24c_s^2\omega_5^2 + 36\omega_2^2 v_1^2 - 48c_s^2\omega_5^2\omega_2 + 25c_s^2\omega_5^2\omega_2^2 + 12c_s^2\omega_2^2 - 3\omega_5^2\omega_2^3 v_1^2 - 11\omega_5^2\omega_2^2 - 6c_s^2\omega_2^3 - 2c_s^2\omega_5^2\omega_2^3 - 18\omega_2^3 v_1^2 + \omega_5^2\omega_2^3 + 9c_s^2\omega_5\omega_2^3 - 12\omega_2^2 + 27\omega_5\omega_2^3 v_1^2 - 9\omega_5\omega_2^3 - 36c_s^2\omega_5\omega_2^2 + 36\omega_5\omega_2^2 + 6\omega_2^3 - 24\omega_5\omega_2 - 108\omega_5\omega_2^2 v_1^2 + 24c_s^2\omega_5\omega_2 - 36\omega_5^2 v_1^2 + 18\omega_5^2\omega_2 v_1^2) \frac{\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_t D_x^3 v_1}^{(0), \text{CLBM}2} = C_{D_t D_x^3 v_1}^{(0), \text{CLBM}1}$$

$$\text{coefficient } C_{D_x^4 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^4} :$$

$$C_{D_x^4 \rho}^{(0), \text{SRT}} = (3\omega^3 v_1^4 - 3c_s^4 \omega^3 + 72v_1^2 + 48c_s^4 + 30c_s^4 \omega^2 - 72c_s^4 \omega - 42\omega^2 v_1^4 - 108\omega v_1^2 + 216c_s^2 \omega v_1^2 + 42\omega^2 v_1^2 - 84c_s^2 \omega^2 v_1^2 - 14c_s^2 \omega^2 + c_s^2 \omega^3 + 108\omega v_1^4 + 6c_s^2 \omega^3 v_1^2 - 3\omega^3 v_1^2 + 36c_s^2 \omega - 72v_1^4 - 24c_s^2 - 144c_s^2 v_1^2) \frac{1}{24\omega^3}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT1}} = (24\omega_5^2 \omega_2^2 v_1^2 + 24c_s^4 \omega_5^2 \omega_2^2 + 72\omega_5 \omega_2^2 v_1^4 - 24c_s^2 \omega_5 \omega_2 v_1^2 - 3c_s^4 \omega_5^2 \omega_2^3 + 48\omega_5 \omega_2 v_1^2 + 24\omega_2^2 v_1^2 - 24c_s^2 \omega_2^2 v_1^2 - 72c_s^2 \omega_5^2 \omega_2^2 v_1^2 + 12c_s^2 \omega_5^2 \omega_2 + 24\omega_5^2 \omega_2 v_1^4 - 8c_s^2 \omega_5^2 \omega_2^2 - 18\omega_5 \omega_2^3 v_1^4 - 3\omega_5^2 \omega_2^3 v_1^2 + c_s^2 \omega_5^2 \omega_2^3 + 6c_s^2 \omega_5^2 \omega_2^3 v_1^2 + 12c_s^2 \omega_2^3 v_1^2 - 12\omega_2^3 v_1^2 - 48c_s^4 \omega_5^2 \omega_2 + 3\omega_5^2 \omega_2^3 v_1^4 - 6c_s^2 \omega_5 \omega_2^3 + 24c_s^4 \omega_5^2 + 24c_s^4 \omega_5 \omega_2 + 18\omega_5 \omega_2^3 v_1^2 - 12c_s^2 \omega_5 \omega_2^3 v_1^2 + 12\omega_2^3 v_1^4 + 24c_s^2 \omega_5 \omega_2^2 + 6c_s^4 \omega_5 \omega_2^3 - 72\omega_5 \omega_2^2 v_1^2 + 156c_s^2 \omega_5^2 \omega_2 v_1^2 - 24\omega_5^2 \omega_2^2 v_1^4 - 24c_s^2 \omega_5 \omega_2 - 24c_s^4 \omega_5 \omega_2 - 24\omega_5^2 \omega_2 v_1^2 - 48\omega_5 \omega_2 v_1^4 - 96c_s^2 \omega_5^2 v_1^2 - 24\omega_2^2 v_1^4 + 48c_s^2 \omega_5 \omega_2^2 v_1^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT2}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM1}} = (12\omega_5^2 \omega_2^2 v_1^2 + 24c_s^4 \omega_5^2 \omega_2^2 + 72\omega_5 \omega_2^2 v_1^4 + 72c_s^2 \omega_5 \omega_2 v_1^2 - 3c_s^4 \omega_5^2 \omega_2^3 + 72\omega_2^2 v_1^2 - 216c_s^2 \omega_2^2 v_1^2 - 12c_s^2 \omega_5^2 \omega_2^2 v_1^2 + 12c_s^2 \omega_5^2 \omega_2 - 8c_s^2 \omega_5^2 \omega_2^2 - 30\omega_5^2 \omega_2^3 v_1^4 - 3\omega_5^2 \omega_2^3 v_1^2 + c_s^2 \omega_5^2 \omega_2^3 + 6c_s^2 \omega_5^2 \omega_2^3 v_1^2 + 108c_s^2 \omega_2^3 v_1^2 - 36\omega_2^3 v_1^2 - 48c_s^4 \omega_5^2 \omega_2 + 3\omega_5^2 \omega_2^3 v_1^4 - 6c_s^2 \omega_5 \omega_2^3 + 24c_s^4 \omega_5^2 + 24c_s^4 \omega_5 \omega_2 + 30\omega_5 \omega_2^3 v_1^2 - 72c_s^2 \omega_5 \omega_2^3 v_1^2 + 36\omega_2^3 v_1^4 + 24c_s^2 \omega_5 \omega_2^2 + 6c_s^4 \omega_5 \omega_2^3 - 72\omega_5 \omega_2^2 v_1^2 - 36c_s^2 \omega_5^2 \omega_2 v_1^2 - 12\omega_5^2 \omega_2^2 v_1^4 - 24c_s^2 \omega_5 \omega_2 - 24c_s^4 \omega_5 \omega_2^2 - 72\omega_2^2 v_1^4 + 144c_s^2 \omega_5 \omega_2^2 v_1^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM2}} = C_{D_x^4 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^4 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^4}$:

$$C_{D_x^4 v_1}^{(0), \text{SRT}} = (24 - 36v_1^2 + 14\omega^2 - 36\omega - \omega^3 + 54\omega v_1^2 - 22\omega^2 v_1^2 - 26c_s^2 \omega^2 + c_s^2 \omega^3 + 2\omega^3 v_1^2 + 72c_s^2 \omega - 48c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT1}} = (-16\omega_5^2 \omega_2^2 v_1^2 - 12\omega_5 \omega_2 v_1^2 - 6\omega_5^2 \omega_2 - 24c_s^2 \omega_5^2 - 12\omega_2^2 v_1^2 + 42c_s^2 \omega_5^2 \omega_2 - 20c_s^2 \omega_5^2 \omega_2^2 - 12c_s^2 \omega_2^2 + 2\omega_5^2 \omega_2^3 v_1^2 + 8\omega_5^2 \omega_2^2 + 6c_s^2 \omega_2^3 + c_s^2 \omega_5^2 \omega_2^3 + 6\omega_2^3 v_1^2 - \omega_5^2 \omega_2^3 - 6c_s^2 \omega_5 \omega_2^3 + 12\omega_2^2 - 6\omega_5 \omega_2^3 v_1^2 + 6\omega_5 \omega_2^3 + 24c_s^2 \omega_5 \omega_2^2 - 24\omega_5 \omega_2^2 - 6\omega_2^3 + 12\omega_5 \omega_2 + 24\omega_5 \omega_2^2 v_1^2 - 12c_s^2 \omega_5 \omega_2 - 12\omega_5^2 v_1^2 + 24\omega_5^2 \omega_2 v_1^2) \frac{\rho v_1}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT2}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM1}} = (2\omega_5^2 \omega_2^2 v_1^2 + 60\omega_5 \omega_2 v_1^2 + 6\omega_5^2 \omega_2 + 24c_s^2 \omega_5^2 - 84\omega_2^2 v_1^2 - 30c_s^2 \omega_5^2 \omega_2 - 2c_s^2 \omega_5^2 \omega_2^2 - 60c_s^2 \omega_2^2 + 2\omega_5^2 \omega_2^3 v_1^2 + 2\omega_5^2 \omega_2^2 + 30c_s^2 \omega_2^3 + c_s^2 \omega_5^2 \omega_2^3 + 42\omega_2^3 v_1^2 - \omega_5^2 \omega_2^3 - 24c_s^2 \omega_5 \omega_2^3 + 36\omega_2^2 - 24\omega_5 \omega_2^3 v_1^2 + 12\omega_5 \omega_2^3 + 72c_s^2 \omega_5 \omega_2^2 - 24\omega_5 \omega_2^2 - 18\omega_2^3 - 12\omega_5 \omega_2 + 24\omega_5 \omega_2^2 v_1^2 - 12c_s^2 \omega_5 \omega_2 - 12\omega_5^2 v_1^2 - 12\omega_5^2 \omega_2 v_1^2) \frac{\rho v_1}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM2}} = C_{D_x^4 v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t^3 D_y v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial t^3 \partial x_2}$:

$$C_{D_t^3 D_y v_2}^{(0), \text{SRT}} = (-2 - \omega^2 + 3\omega) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{MRT1}} = (-2 - \omega_3^2 + 3\omega_3) \frac{\rho}{2\omega_3^3}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{MRT2}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{CLBM1}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{CLBM2}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_t^2 D_x D_y v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2}$:

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{SRT}} = (36 + 20\omega^2 - 54\omega - \omega^3) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}} = (-\omega_2^2 \omega_3^3 - 6\omega_3^3 + 12\omega_3^2 + 13\omega_2^2 \omega_3^2 - 24\omega_2^2 \omega_3 + 12\omega_2^2 + 12\omega_2 \omega_3 - 24\omega_2 \omega_3^2 + 7\omega_2 \omega_3^3) \frac{v_2 \rho}{12\omega_2^2 \omega_3^3}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_t^2 D_x D_y v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2}$:

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{SRT}} = (36 + 20\omega^2 - 54\omega - \omega^3) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}} = (7\omega_2^3 \omega_3 + 12\omega_3^2 + 13\omega_2^2 \omega_3^2 - 24\omega_2^2 \omega_3 - \omega_2^3 \omega_3^2 + 12\omega_2^2 + 12\omega_2 \omega_3 - 6\omega_2^3 - 24\omega_2 \omega_3^2) \frac{\rho v_1}{12\omega_2^3 \omega_3^2}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x^2 D_y v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2}$:

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{SRT}} = (-24 - 14\omega^2 + 36\omega + \omega^3) \frac{v_2 \rho v_1}{6\omega^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{MRT1}} = (-6\omega_2^2 \omega_3^3 + 24\omega_5 \omega_2 \omega_3^3 - 12\omega_5 \omega_2 \omega_3^2 + 12\omega_2^2 \omega_3^2 - 12\omega_5 \omega_3^3 + 3\omega_2^3 \omega_3^3 - 6\omega_2^2 \omega_3^2 - 7\omega_5 \omega_2^3 \omega_3^2 - 6\omega_5 \omega_2^3 + \omega_5 \omega_2^2 \omega_3^3 - 6\omega_5 \omega_2^2 \omega_3 + 12\omega_5 \omega_2^2 \omega_3^2 - 10\omega_5 \omega_2^2 \omega_3^3 + 12\omega_5 \omega_2^3 \omega_3) \frac{v_2 \rho v_1}{6\omega_5 \omega_2^3 \omega_3^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{CLBM1}} = (-7\omega_2^2 \omega_3^3 + 12\omega_2^2 \omega_3 - 12\omega_3^3 + 6\omega_2^2 \omega_3^2 + \omega_2^3 \omega_3^3 - 6\omega_2^2 \omega_3 - 7\omega_2^3 \omega_3^2 - 6\omega_2^3 + 18\omega_2 \omega_3^3) \frac{v_2 \rho v_1}{6\omega_2^3 \omega_3^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 D_y v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t D_x^2 D_y v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2}$:

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{SRT}} = (-2\omega^2 v_1^2 + 34c_s^2 \omega^2 - 2c_s^2 \omega^3 + \omega^3 v_1^2 - 90c_s^2 \omega + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{MRT1}} = (-6c_s^2 \omega_2^3 \omega_3 + 6\omega_5^2 \omega_2^2 v_1^2 - 2c_s^2 \omega_5^2 \omega_2^3 \omega_3 + 12\omega_5 \omega_2 \omega_3 v_1^2 + 12c_s^2 \omega_5^2 \omega_2 + 12\omega_2^2 \omega_3 v_1^2 - 18c_s^2 \omega_5^2 \omega_2^2 - \omega_5^2 \omega_2^3 v_1^2 + 22c_s^2 \omega_5^2 \omega_2^2 \omega_3 + 12c_s^2 \omega_2^2 \omega_3 + 9\omega_5 \omega_2^3 \omega_3 v_1^2 + 3c_s^2 \omega_5^2 \omega_2^3 - 10\omega_5^2 \omega_2^2 \omega_3 v_1^2 + 12c_s^2 \omega_5 \omega_2 \omega_3 - 6c_s^2 \omega_5 \omega_2^3 - 6\omega_2^3 \omega_3 v_1^2 + 12c_s^2 \omega_5^2 \omega_3 - 30c_s^2 \omega_5 \omega_2^2 \omega_3 - 6\omega_5 \omega_2^3 v_1^2 - 24\omega_5^2 \omega_3 v_1^2 + 12c_s^2 \omega_5 \omega_2^2 - 30c_s^2 \omega_5^2 \omega_2 \omega_3 + 36\omega_5^2 \omega_2 \omega_3 v_1^2 + \omega_5^2 \omega_2^3 \omega_3 v_1^2 + 9c_s^2 \omega_5 \omega_2^3 \omega_3 + 12\omega_5 \omega_2^2 v_1^2 - 30\omega_5 \omega_2^2 \omega_3 v_1^2 - 12\omega_5^2 \omega_2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3 \omega_3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{MRT2}} = C_{D_t D_x^2 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{CLBM1}} = (-6c_s^2 \omega_2^3 \omega_3 - 6\omega_5^2 \omega_2^2 v_1^2 - 2c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 12\omega_5 \omega_2 \omega_3 v_1^2 + 12c_s^2 \omega_5^2 \omega_2 - 12\omega_2^2 \omega_3 v_1^2 - 18c_s^2 \omega_5^2 \omega_2^2 - \omega_5^2 \omega_2^3 v_1^2 + 22c_s^2 \omega_5^2 \omega_2^2 \omega_3 + 12c_s^2 \omega_2^2 \omega_3 - 9\omega_5 \omega_2^3 \omega_3 v_1^2 + 3c_s^2 \omega_5^2 \omega_2^2 + 8\omega_5^2 \omega_2^2 \omega_3 v_1^2 + 12c_s^2 \omega_5 \omega_2 \omega_3 - 6c_s^2 \omega_5 \omega_2^3 + 6\omega_2^3 \omega_3 v_1^2 + 12c_s^2 \omega_5^2 \omega_3 - 30c_s^2 \omega_5 \omega_2^2 \omega_3 + 6\omega_5 \omega_2^3 v_1^2 + 24\omega_5^2 \omega_3 v_1^2 + 12c_s^2 \omega_5 \omega_2^2 - 30c_s^2 \omega_5^2 \omega_2 \omega_3 - 36\omega_5^2 \omega_2 \omega_3 v_1^2 + \omega_5^2 \omega_2^3 \omega_3 v_1^2 + 9c_s^2 \omega_5 \omega_2^3 \omega_3 - 12\omega_5 \omega_2^2 v_1^2 + 30\omega_5 \omega_2^2 \omega_3 v_1^2 + 12\omega_5^2 \omega_2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3 \omega_3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{CLBM2}} = C_{D_t D_x^2 D_y v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^3 D_y \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y \rho}^{(0), \text{SRT}} = (24 + 14\omega^2 - 36\omega - \omega^3 - 72c_s^2 \omega^2 + 6c_s^2 \omega^3 + 180c_s^2 \omega - 120c_s^2) \frac{v_2 v_1}{6\omega^3}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{MRT1}} = (-30\omega_5^2 \omega_2 \omega_3^3 v_1^2 + 6c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 12c_s^2 \omega_2^2 \omega_3^3 - 48c_s^2 \omega_5^2 \omega_2^2 \omega_3^3 - 12\omega_5 \omega_2^2 \omega_3^2 v_1^2 + 6\omega_2^2 \omega_3^3 + 24\omega_5^2 \omega_3^3 v_1^2 - 3\omega_5^2 \omega_2^2 \omega_3^2 + 12\omega_5 \omega_2 \omega_3^3 + 6\omega_5^2 \omega_3^3 v_1^2 + 42c_s^2 \omega_5^2 \omega_2^3 \omega_3^2 - 24c_s^2 \omega_5 \omega_2 \omega_3^3 + 6\omega_2^3 \omega_3^3 v_1^2 + 7\omega_2^2 \omega_2^3 \omega_3^3 + \omega_5^2 \omega_2^3 \omega_3^2 - 3\omega_2^3 \omega_3^3 + 6\omega_2^2 \omega_3^3 v_1^2 - 12c_s^2 \omega_5^2 \omega_2^2 \omega_3 + 6c_s^2 \omega_5^2 \omega_2^3 \omega_3^3 + 42\omega_5 \omega_2^2 \omega_3^3 v_1^2 + 6c_s^2 \omega_2^3 \omega_3^3 + 12\omega_5 \omega_2 \omega_3^2 v_1^2 - \omega_5^2 \omega_2^3 \omega_3^3 + 6\omega_2^2 \omega_2^3 \omega_3^3 - 12c_s^2 \omega_5^2 \omega_2^3 \omega_3^2 - 12\omega_2^2 \omega_3^3 v_1^2 - 3\omega_5 \omega_2^3 \omega_3^2 - 12\omega_5^2 \omega_2^2 \omega_3^2 v_1^2 - 24\omega_5 \omega_2 \omega_3^3 v_1^2 - 12c_s^2 \omega_5 \omega_2^3 \omega_3^3 + 6\omega_5 \omega_2^3 \omega_3^3 v_1^2 + 6c_s^2 \omega_5 \omega_2^2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^3 v_1^2 + 42c_s^2 \omega_5 \omega_2^2 \omega_3^2 - 24c_s^2 \omega_5^2 \omega_2 \omega_3^2 - 12\omega_5^2 \omega_2^3 \omega_3 v_1^2 - 36c_s^2 \omega_5^2 \omega_3^3 + 6\omega_5^2 \omega_2^2 \omega_3^3 v_1^2 - 6\omega_5^2 \omega_2 \omega_3^3 + 6\omega_5 \omega_2^2 \omega_3^2 - 12\omega_5 \omega_2^3 \omega_3^3 v_1^2 + 78c_s^2 \omega_5^2 \omega_2 \omega_3^3 - 12c_s^2 \omega_5 \omega_2^2 \omega_3^2 - 21\omega_5 \omega_2^2 \omega_3^3) \frac{v_2 v_1}{6\omega_5^2 \omega_2^3 \omega_3^3}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{MRT}2} = C_{D_x^3 D_y \rho}^{(0), \text{MRT}1}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CLBM1}} = (12\omega_5^2\omega_2\omega_3^3v_1^2 + 6c_s^2\omega_5^2\omega_2^3\omega_3 - 36c_s^2\omega_2^2\omega_3^3 - 36c_s^2\omega_5^2\omega_2^2\omega_3^3 + 6\omega_2^2\omega_3^3 - 3\omega_5^2\omega_2^2\omega_3^2 + 12\omega_5\omega_2\omega_3^3 + 6\omega_5^2\omega_2^3\omega_3^2v_1^2 + 36c_s^2\omega_5^2\omega_2^2\omega_3^2 - 24c_s^2\omega_5\omega_2\omega_3^3 - 6\omega_3^3\omega_3^3v_1^2 + 7\omega_5^2\omega_2^2\omega_3^3 + \omega_5^2\omega_2^2\omega_3^2 - 3\omega_2^3\omega_3^3 + 6\omega_5^2\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_2^2\omega_3 + 6c_s^2\omega_5^2\omega_2^3\omega_3^3 + 12\omega_5\omega_2^2\omega_3^3v_1^2 + 18c_s^2\omega_2^3\omega_3^3 - \omega_5^2\omega_2^2\omega_3^3 + 6\omega_5^2\omega_2^2\omega_3^2v_1^2 - 12c_s^2\omega_5^2\omega_2^3\omega_3^2 + 12\omega_5^2\omega_3^3v_1^2 - 3\omega_5\omega_2^3\omega_3^2 - 6\omega_5^2\omega_2^2\omega_3^3v_1^2 - 24\omega_5\omega_2\omega_3^3v_1^2 - 24c_s^2\omega_5\omega_2^3\omega_3^3 + 6\omega_5\omega_2^3\omega_3^3 + 12c_s^2\omega_5\omega_2^3\omega_3^2 + 72c_s^2\omega_5\omega_2\omega_3^3 - 12c_s^2\omega_5^2\omega_2\omega_3^2 - 12\omega_5^2\omega_2^3\omega_3v_1^2 - 12c_s^2\omega_5^2\omega_3^3 - 6\omega_5^2\omega_2^2\omega_3^3v_1^2 - 6\omega_5^2\omega_2\omega_3^3 + 6\omega_5\omega_2^2\omega_3^3 + 36c_s^2\omega_5^2\omega_2\omega_3^3 - 24c_s^2\omega_5\omega_2^2\omega_3^2 - 21\omega_5\omega_2^2\omega_3^3) \frac{v_2v_1}{6\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CLBM2}} = C_{D_x^3 D_y \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^3 D_y v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_1}^{(0), \text{SRT}} = (12 - 12v_1^2 + 8\omega^2 - 18\omega - \omega^3 + 18\omega v_1^2 - 12\omega^2 v_1^2 - 56c_s^2\omega^2 + 4c_s^2\omega^3 + 3\omega^3 v_1^2 + 144c_s^2\omega - 96c_s^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{MRT}1} = (-30\omega_5^2\omega_2\omega_3^3v_1^2 + 6c_s^2\omega_5^2\omega_2^3\omega_3 - 12c_s^2\omega_2^2\omega_3^3 - 32c_s^2\omega_5^2\omega_2^2\omega_3^3 - 24\omega_5\omega_2^2\omega_3^3v_1^2 + 24\omega_5^2\omega_3^3v_1^2 - 6\omega_5^2\omega_2^2\omega_3^2 + 48c_s^2\omega_5^2\omega_2^2\omega_3^2 - 12c_s^2\omega_5\omega_2\omega_3^3 + 6\omega_3^3\omega_3^3v_1^2 + 3\omega_5^2\omega_2^2\omega_3^3 + 2\omega_5^2\omega_2^3\omega_3^2 + 12\omega_5^2\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_2^2\omega_3 + 4c_s^2\omega_5^2\omega_2^3\omega_3^3 + 36\omega_5\omega_2^2\omega_3^3v_1^2 + 6c_s^2\omega_2^3\omega_3^3 - \omega_5^2\omega_2^2\omega_3^3 - 12c_s^2\omega_5^2\omega_2^3\omega_3^2 + 3\omega_5^2\omega_2^3\omega_3^3v_1^2 - 12\omega_2^2\omega_3^3v_1^2 - 6\omega_5\omega_2^3\omega_3^2 + 12\omega_5^2\omega_2^2\omega_3^3v_1^2 - 12\omega_5\omega_2\omega_3^3v_1^2 - 12c_s^2\omega_5\omega_2^3\omega_3^3 + 3\omega_5\omega_2^3\omega_3^3 + 12c_s^2\omega_5\omega_2^3\omega_3^2 + 12\omega_5\omega_2^2\omega_3^3v_1^2 + 36c_s^2\omega_5\omega_2^2\omega_3^3 - 24c_s^2\omega_5^2\omega_2\omega_3^2 - 18\omega_5^2\omega_2^3\omega_3v_1^2 - 12c_s^2\omega_5^2\omega_3^3 + 12\omega_5\omega_2^2\omega_3^2 - 12\omega_5\omega_2^3\omega_3^3v_1^2 + 36c_s^2\omega_5^2\omega_2\omega_3^3 - 24c_s^2\omega_5\omega_2^2\omega_3^2 - 6\omega_5\omega_2^2\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{MRT}2} = C_{D_x^3 D_y v_1}^{(0), \text{MRT}1}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{CLBM1}} = (30\omega_5^2\omega_2\omega_3^3v_1^2 + 6c_s^2\omega_5^2\omega_2^3\omega_3 - 12c_s^2\omega_2^2\omega_3^3 - 32c_s^2\omega_5^2\omega_2^2\omega_3^3 - 24\omega_5\omega_2^2\omega_3^3v_1^2 - 24\omega_5^2\omega_3^3v_1^2 - 6\omega_5^2\omega_2^2\omega_3^2 + 48c_s^2\omega_5^2\omega_2^2\omega_3^2 - 12c_s^2\omega_5\omega_2\omega_3^3 - 6\omega_3^3\omega_3^3v_1^2 + 3\omega_5^2\omega_2^2\omega_3^3 + 2\omega_5^2\omega_2^3\omega_3^2 + 12\omega_5^2\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_2^2\omega_3 + 4c_s^2\omega_5^2\omega_2^3\omega_3^3 - 12\omega_5\omega_2^2\omega_3^3v_1^2 + 6c_s^2\omega_2^3\omega_3^3 - \omega_5^2\omega_2^2\omega_3^3 - 12c_s^2\omega_5^2\omega_2^3\omega_3^2 + 3\omega_5^2\omega_2^3\omega_3^3v_1^2 + 12\omega_2^2\omega_3^3v_1^2 - 6\omega_5\omega_2^3\omega_3^2 + 12\omega_5^2\omega_2^2\omega_3^3v_1^2 + 12\omega_5\omega_2\omega_3^3v_1^2 - 12c_s^2\omega_5\omega_2^3\omega_3^3 + 3\omega_5\omega_2^3\omega_3^3 + 12c_s^2\omega_5\omega_2^3\omega_3^2 + 12\omega_5\omega_2^2\omega_3^3v_1^2 + 36c_s^2\omega_5\omega_2^2\omega_3^3 - 24c_s^2\omega_5^2\omega_2\omega_3^2 - 18\omega_5^2\omega_2^3\omega_3v_1^2 - 12c_s^2\omega_5^2\omega_3^3 - 12\omega_5^2\omega_2^2\omega_3^3v_1^2 + 12\omega_5\omega_2^2\omega_3^2 + 36c_s^2\omega_5^2\omega_2\omega_3^3 - 24c_s^2\omega_5\omega_2^2\omega_3^2 - 6\omega_5\omega_2^2\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{CLBM2}} = C_{D_x^3 D_y v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^3 D_y v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_2}^{(0), \text{SRT}} = (36 - 36v_1^2 + 20\omega^2 - 54\omega - \omega^3 + 54\omega v_1^2 - 20\omega^2 v_1^2 - 56c_s^2\omega^2 + 4c_s^2\omega^3 + \omega^3 v_1^2 + 144c_s^2\omega - 96c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{MRT}1} = (-8\omega_5^2\omega_2^2v_1^2 - 36\omega_5\omega_2v_1^2 - 12\omega_5^2\omega_2 - 48c_s^2\omega_5^2 - 12\omega_2^2v_1^2 + 90c_s^2\omega_5^2\omega_2 - 44c_s^2\omega_5^2\omega_2^2 - 12c_s^2\omega_2^2 + \omega_5^2\omega_2^3v_1^2 + 11\omega_5^2\omega_2^2 + 6c_s^2\omega_2^3 + 4c_s^2\omega_5^2\omega_2^3 + 6\omega_2^3v_1^2 - \omega_5^2\omega_2^2 - 12c_s^2\omega_5\omega_2^2 + 12\omega_2^2 - 12\omega_5\omega_2^3v_1^2 + 9\omega_5\omega_2^2 + 48c_s^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5\omega_2^2v_1^2 - 36c_s^2\omega_5\omega_2 + 12\omega_5^2v_1^2) \frac{\rho v_1}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{MRT}2} = C_{D_x^3 D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CLBM1}} = (-14\omega_5^2\omega_2^2v_1^2 - 60\omega_5\omega_2v_1^2 - 12\omega_5^2\omega_2 + 12\omega_2^2v_1^2 + 18c_s^2\omega_5^2\omega_2 - 26c_s^2\omega_5^2\omega_2^2 - 60c_s^2\omega_2^2 + \omega_5^2\omega_2^3v_1^2 + 11\omega_5^2\omega_2^2 + 30c_s^2\omega_2^3 + 4c_s^2\omega_5^2\omega_2^3 - 6\omega_2^3v_1^2 - \omega_5^2\omega_2^2 - 30c_s^2\omega_5\omega_2^2 + 12\omega_2^2 - 6\omega_5\omega_2^3v_1^2 + 9\omega_5\omega_2^2 + 96c_s^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5\omega_2^2v_1^2 - 36c_s^2\omega_5\omega_2 + 12\omega_5^2v_1^2 + 12\omega_5^2\omega_2v_1^2) \frac{\rho v_1}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CLBM2}} = C_{D_x^3 D_y v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t^2 D_y^2 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial t^2 \partial x_2^2}$:

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{SRT}} = (-2 - \omega^2 + 3\omega) \frac{3v_2\rho}{2\omega^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{MRT}1} = (2\omega_6^2 + 2\omega_3^3 - 4\omega_3^2 - \omega_6^2\omega_3^2 - \omega_6^2\omega_3 - 4\omega_6\omega_3 + 8\omega_6\omega_3^2 - 2\omega_6\omega_3^3) \frac{v_2\rho}{2\omega_6^2\omega_3^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{MRT}2} = C_{D_t^2 D_y^2 v_2}^{(0), \text{MRT}1}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{CLBM1}} = (-2 - \omega_3^2 + 3\omega_3) \frac{3v_2\rho}{2\omega_3^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_t^2 D_y^2 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t D_x D_y^2 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2}$:

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{SRT}} = (34c_s^2 \omega^2 + \omega^3 v_2^2 - 2c_s^2 \omega^3 - 90c_s^2 \omega - 2\omega^2 v_2^2 + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{MRT1}} = (3c_s^2 \omega_6^2 \omega_3^3 - 30c_s^2 \omega_2 \omega_6^2 \omega_3 - 18c_s^2 \omega_6^2 \omega_3^2 + 36\omega_2 v_2^2 \omega_6^2 \omega_3 - 10\omega_2 v_2^2 \omega_6^2 \omega_3^2 - 2c_s^2 \omega_2 \omega_6^2 \omega_3^3 + 12v_2^2 \omega_6 \omega_3^2 + 12c_s^2 \omega_6^2 \omega_3 + \omega_2 v_2^2 \omega_6^2 \omega_3^3 + 22c_s^2 \omega_2 \omega_6^2 \omega_3^2 - 6v_2^2 \omega_6 \omega_3^3 + 9\omega_2 v_2^2 \omega_6 \omega_3^2 - v_2^2 \omega_6^2 \omega_3^3 - 30c_s^2 \omega_2 \omega_6 \omega_3^2 - 30\omega_2 v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_6^2 \omega_3^2 + 9c_s^2 \omega_2 \omega_6 \omega_3^2 + 12c_s^2 \omega_2 \omega_3^2 + 12c_s^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_6^2 \omega_3 + 12\omega_2 v_2^2 \omega_6 \omega_3 + 12\omega_2 v_2^2 \omega_3^2 + 12c_s^2 \omega_2 \omega_6 \omega_3 + 12c_s^2 \omega_2 \omega_6^2 - 6c_s^2 \omega_6 \omega_3^3 - 6c_s^2 \omega_2 \omega_3^3 - 6\omega_2 v_2^2 \omega_3^3 - 24\omega_2 v_2^2 \omega_6^2) \frac{\rho}{12\omega_2 \omega_6^2 \omega_3^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_y^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{CLBM1}} = (3c_s^2 \omega_6^2 \omega_3^3 - 30c_s^2 \omega_2 \omega_6^2 \omega_3 - 18c_s^2 \omega_6^2 \omega_3^2 - 36\omega_2 v_2^2 \omega_6^2 \omega_3 + 8\omega_2 v_2^2 \omega_6^2 \omega_3^2 - 2c_s^2 \omega_2 \omega_6^2 \omega_3^3 - 12v_2^2 \omega_6 \omega_3^2 + 12c_s^2 \omega_6^2 \omega_3 + \omega_2 v_2^2 \omega_6^2 \omega_3^3 + 22c_s^2 \omega_2 \omega_6^2 \omega_3^2 + 6v_2^2 \omega_6 \omega_3^3 - 9\omega_2 v_2^2 \omega_6 \omega_3^2 - v_2^2 \omega_6^2 \omega_3^3 - 30c_s^2 \omega_2 \omega_6 \omega_3^2 + 30\omega_2 v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_6^2 \omega_3^2 + 9c_s^2 \omega_2 \omega_6 \omega_3^2 + 12c_s^2 \omega_2 \omega_3^2 + 12c_s^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3 - 12\omega_2 v_2^2 \omega_6 \omega_3 - 12\omega_2 v_2^2 \omega_3^2 + 12c_s^2 \omega_2 \omega_6 \omega_3 + 12c_s^2 \omega_2 \omega_6^2 - 6c_s^2 \omega_6 \omega_3^3 - 6c_s^2 \omega_2 \omega_3^3 + 6\omega_2 v_2^2 \omega_3^3 + 24\omega_2 v_2^2 \omega_6^2) \frac{\rho}{12\omega_2 \omega_6^2 \omega_3^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{CLBM2}} = C_{D_t D_x D_y^2 v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t D_x D_y^2 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2}$:

$$C_{D_t D_x D_y^2 v_2}^{(0), \text{SRT}} = (-24 - 14\omega^2 + 36\omega + \omega^3) \frac{v_2 \rho v_1}{6\omega^3}$$

$$C_{D_t D_x D_y^2 v_2}^{(0), \text{MRT1}} = (-6\omega_2^2 \omega_3^3 - 12\omega_2^2 \omega_6 \omega_3 - 12\omega_2^3 \omega_6 + 12\omega_2^2 \omega_3^2 - 7\omega_2^2 \omega_6 \omega_3^2 + 3\omega_2^3 \omega_3^2 + 12\omega_2^2 \omega_6 \omega_3^2 - 6\omega_2^3 \omega_3^2 + 12\omega_2 \omega_6 \omega_3^2 + 24\omega_2^3 \omega_6 \omega_3 - 6\omega_2 \omega_6 \omega_3^2 - 10\omega_2^2 \omega_6 \omega_3^2 - 6\omega_6 \omega_3^3 + \omega_2^3 \omega_6 \omega_3^3) \frac{v_2 \rho v_1}{6\omega_2^2 \omega_6 \omega_3^3}$$

$$C_{D_t D_x D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_t D_x D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y^2 v_2}^{(0), \text{CLBM1}} = (-7\omega_2^2 \omega_3^3 + 18\omega_2^3 \omega_3 - 6\omega_3^3 + 6\omega_2^2 \omega_3^2 + \omega_2^3 \omega_3^2 - 7\omega_2^3 \omega_3^2 - 12\omega_2^3 - 6\omega_2 \omega_3^2 + 12\omega_2 \omega_3^3) \frac{v_2 \rho v_1}{6\omega_2^2 \omega_3^3}$$

$$C_{D_t D_x D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_t D_x D_y^2 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^2 D_y^2 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{SRT}} = (36c_s^2 \omega v_2^2 - c_s^4 \omega^3 + 16c_s^4 + 10c_s^4 \omega^2 - 24c_s^4 \omega + 34\omega^2 v_2^2 v_1^2 + 36c_s^2 \omega v_1^2 - 84\omega v_2^2 v_1^2 - 24c_s^2 v_2^2 - 14c_s^2 \omega^2 v_1^2 + 56v_2^2 v_1^2 + c_s^2 \omega^3 v_2^2 + c_s^2 \omega^3 v_1^2 - 14c_s^2 \omega^2 v_2^2 - 24c_s^2 v_1^2 - 3\omega^3 v_2^2 v_1^2) \frac{1}{4\omega^3}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT1}} = (c_s^2 \omega_5^2 \omega_3^2 v_2^2 \omega_6 \omega_3^3 + 2c_s^2 \omega_5^2 \omega_3^2 \omega_3^3 v_1^2 + 10c_s^2 \omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^3 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 + 20\omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 2c_s^4 \omega_5 \omega_2^2 \omega_6^2 \omega_3^3 - 3c_s^2 \omega_5^2 \omega_3^2 \omega_6 \omega_3^3 v_1^2 - 38\omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 v_1^2 + 10\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^3 v_1^2 - 2c_s^2 \omega_5^2 \omega_3^2 v_2^2 \omega_6 \omega_3^2 + 2\omega_5^2 \omega_3^2 v_2^2 \omega_3^3 v_1^2 - c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^3 + 10\omega_5^2 \omega_3^2 v_2^2 \omega_6 \omega_3^2 v_1^2 + 4c_s^4 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 - 4c_s^2 \omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3 v_1^2 + 20\omega_5^2 \omega_3^2 v_2^2 \omega_6^2 v_1^2 - 4\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 - 8c_s^2 \omega_5^2 \omega_2 \omega_6^2 \omega_3^2 v_1^2 + 4c_s^4 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 - 2c_s^4 \omega_5^2 \omega_2 \omega_6^2 \omega_3^2 - 38\omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 2c_s^2 \omega_5^2 \omega_2^2 \omega_6 \omega_3^3 v_1^2 - 4\omega_5^2 v_2^2 \omega_6^2 \omega_3^3 v_1^2 - 4c_s^2 \omega_5^2 \omega_3^2 \omega_6^2 v_1^2 + 10c_s^2 \omega_5^2 \omega_3^2 \omega_6 \omega_3^2 v_1^2 - 2c_s^4 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 + 4c_s^4 \omega_5^2 \omega_2 \omega_6^2 \omega_3^2 - 3\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 20\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 2c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 - 2c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 4\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 10c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 4c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 3\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 20\omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 8c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 3c_s^2 \omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + c_s^4 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 - 12c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 4c_s^2 \omega_5^2 v_2^2 \omega_6^2 \omega_3^3 + 2\omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 v_1^2 - 2c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 - 8c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 + 10c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 4c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 3\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 20\omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 8c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 3c_s^2 \omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + c_s^4 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 + 4c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 + c_s^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 + c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 - 4\omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 v_1^2 + 2c_s^2 \omega_5^2 v_2^2 \omega_6^2 \omega_3^2 + c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 - 2c_s^4 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 + 2c_s^2 \omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 20\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2) \frac{1}{4\omega_5^2 \omega_2^2 \omega_6^2 \omega_3^3}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT2}} = C_{D_x^2 D_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CLBM1}} = (-c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^3 + 2c_s^2 \omega_5^2 \omega_2^2 \omega_3^3 v_1^2 + 10c_s^2 \omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^3 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 + 12\omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 - 14\omega_5^2 \omega_3^2 v_2^2 \omega_6^2 \omega_3 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 v_1^2 - 10\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^3 v_1^2 + 4\omega_5^2 v_2^2 \omega_6^2 \omega_3^3 v_1^2 + 4c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 2c_s^4 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 - 3c_s^2 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 - 28\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 - 4c_s^2 \omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 4\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 2c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2\omega_5^2 \omega_2^2 v_2^2 \omega_3^3 v_1^2 - c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 10\omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 v_1^2 + 4c_s^4 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 - 4c_s^2 \omega_5^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3 v_1^2 + 4\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 4\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 4c_s^4 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 - 14\omega_5 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 + 2c_s^2 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 v_1^2 + 4\omega_5^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 v_1^2 - 4c_s^2 \omega_5^2 \omega_2^2 \omega_3^2 v_1^2 + 10c_s^2 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 v_1^2 - 2c_s^4 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 + 4c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 + 3\omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 v_1^2 + 2c_s^2 \omega_5^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2c_s^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 + 4\omega_5^2 \omega_2^2 v_2^2 \omega_3^3 v_1^2 +$$

$$10c_s^2\omega_5^2\omega_6^3\omega_3^2v_1^2+14\omega_5^2\omega_2^2\omega_6^2\omega_3^3v_1^2-2c_s^2\omega_5^2\omega_2^2\omega_6^2\omega_3^3v_1^2+2c_s^2\omega_5\omega_3^3\omega_6^2\omega_2^2v_1^2-2c_s^4\omega_5\omega_3^3\omega_6^2\omega_2^2-4c_s^2\omega_5^2v_2^2\omega_6^2\omega_3^3+4c_s^4\omega_5^2\omega_2^2\omega_6^2\omega_3^3-8c_s^2\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^3-4c_s^2\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^3-2\omega_5^3v_2^2\omega_6^2\omega_3^3v_1^2-2\omega_5\omega_2^3v_2^2\omega_6^2\omega_3^3v_1^2-4c_s^2\omega_5^2\omega_2^3\omega_6\omega_3v_1^2+8c_s^2\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^3-3\omega_5^2\omega_2^3v_2^2\omega_6^2\omega_3^3v_1^2+c_s^4\omega_5\omega_2^3\omega_6^2\omega_3^3-12c_s^4\omega_5^2\omega_2^2\omega_6^2\omega_3^3-4c_s^2\omega_5^2v_2^2\omega_6^2\omega_3^3-2\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^3v_1^2+2c_s^2\omega_5\omega_2^2\omega_6^2\omega_3^3v_1^2-8c_s^2\omega_5^2\omega_2^3\omega_6^2\omega_3^3v_1^2+10c_s^2\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^3+3\omega_5\omega_2^3v_2^2\omega_6^2\omega_3^3v_1^2+12\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^3v_1^2-2c_s^2\omega_5^3v_2^2\omega_6^2\omega_3^3-3c_s^2\omega_5\omega_2^3v_2^2\omega_6^2\omega_3^3+4\omega_5^2\omega_2^3v_2^2\omega_6\omega_3v_1^2+c_s^4\omega_5^2\omega_2^3\omega_6\omega_3^3+4c_s^4\omega_5^2\omega_2^2\omega_6^2\omega_3^3+8c_s^2\omega_5^2\omega_2^2\omega_6^2\omega_3^3v_1^2-c_s^2\omega_5\omega_2^3\omega_6^2\omega_3^3v_1^2+c_s^2\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^3-4c_s^2\omega_5\omega_2^2\omega_6^2\omega_3^3v_1^2+4\omega_5^2\omega_2^2v_2^2\omega_6\omega_3^3v_1^2+2c_s^2\omega_5^2v_2^2\omega_6^2\omega_3^3+c_s^2\omega_5^2\omega_2^2\omega_6^2\omega_3^3v_1^2-2c_s^2\omega_5^2\omega_2^3\omega_6\omega_3^3+2c_s^2\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^3+14\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^3v_1^2)\frac{1}{4\omega_5^2\omega_2^2\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CLBM2}} = C_{D_x^2 D_y^2 \rho}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{SRT}} = (-126\omega v_2^2 + 84v_2^2 - 26c_s^2\omega^2 - 4\omega^3 v_2^2 + c_s^2\omega^3 + 72c_s^2\omega + 50\omega^2 v_2^2 - 48c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}} = (-14c_s^2\omega_2^3\omega_6^2\omega_3^3 + c_s^2\omega_2^3\omega_6^2\omega_3^3 - 12\omega_2^3v_2^2\omega_6\omega_3 + 24\omega_2v_2^2\omega_6^2\omega_3^3 + 24\omega_2^3v_2^2\omega_6\omega_3^3 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 30\omega_2v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_3^3 + 24c_s^2\omega_2^3\omega_6^2\omega_3^3 - 6\omega_2^3v_2^2\omega_6\omega_3^3 + 48\omega_2^3v_2^2\omega_6^2 + 6\omega_2^3v_2^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 - 6c_s^2\omega_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6\omega_3 - 4\omega_2^3v_2^2\omega_6^2\omega_3^3 - 12\omega_2^3v_2^2\omega_3^3 + 24\omega_2^2v_2^2\omega_6^2\omega_3^3 + 34\omega_2^2v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6^2\omega_3^3 - 6c_s^2\omega_2^2\omega_6\omega_3^3 - 78\omega_2^2v_2^2\omega_6\omega_3 - 48\omega_2^2v_2^2\omega_6^2\omega_3^3 + 24c_s^2\omega_2^2\omega_6\omega_3^3 + 22\omega_2^2v_2^2\omega_6^2\omega_3^3) \frac{\rho v_1}{12\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM1}} = (-14c_s^2\omega_2^3\omega_6^2\omega_3^3 + c_s^2\omega_2^3\omega_6^2\omega_3^3 + 12\omega_2^3v_2^2\omega_6\omega_3 + 24\omega_2v_2^2\omega_6^2\omega_3^3 - 24\omega_2^3v_2^2\omega_6\omega_3^3 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 30\omega_2v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_3^3 + 24c_s^2\omega_2^3\omega_6^2\omega_3^3 + 6\omega_2^3v_2^2\omega_6\omega_3^3 - 6\omega_2^3v_2^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 - 6c_s^2\omega_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6\omega_3 - 4\omega_2^3v_2^2\omega_6^2\omega_3^3 + 12\omega_2^3v_2^2\omega_3^3 + 24\omega_2^2v_2^2\omega_6^2\omega_3^3 + 22\omega_2^2v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6^2\omega_3^3 - 6c_s^2\omega_2^2\omega_6\omega_3^3 - 18\omega_2^2v_2^2\omega_6\omega_3 - 48\omega_2^2v_2^2\omega_6^2\omega_3^3 + 24c_s^2\omega_2^2\omega_6\omega_3^3 + 22\omega_2^2v_2^2\omega_6^2\omega_3^3) \frac{\rho v_1}{12\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM2}} = C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{SRT}} = (84v_1^2 - 126\omega v_1^2 + 50\omega^2 v_1^2 - 26c_s^2\omega^2 + c_s^2\omega^3 - 4\omega^3 v_1^2 + 72c_s^2\omega - 48c_s^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}} = (-78\omega_5^2\omega_2\omega_3^3v_1^2 + 6c_s^2\omega_5^2\omega_2\omega_3^3 - 12c_s^2\omega_2^2\omega_3^3 - 14c_s^2\omega_5^2\omega_2\omega_3^3 + 48\omega_5^2\omega_3^3v_1^2 + 22\omega_5^2\omega_2^2\omega_3^3v_1^2 + 12c_s^2\omega_5^2\omega_2^2\omega_3^3 - 12c_s^2\omega_5\omega_2\omega_3^3 + 6\omega_5^3\omega_3^3v_1^2 + 12\omega_5^2\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_2\omega_3^3 + c_s^2\omega_5^2\omega_2^2\omega_3^3 + 24\omega_5\omega_2^3\omega_3^3v_1^2 + 6c_s^2\omega_2^3\omega_3^3 + 24\omega_5^2\omega_2\omega_3^3v_1^2 + 24\omega_5^2\omega_2^2\omega_3^3v_1^2 - 6c_s^2\omega_5^2\omega_2^2\omega_3^3 - 4\omega_5^2\omega_2^3\omega_3^3v_1^2 - 12\omega_2^2\omega_3^3v_1^2 - 48\omega_5^2\omega_2^2\omega_3^3v_1^2 - 12\omega_5\omega_2\omega_3^3v_1^2 - 6c_s^2\omega_5\omega_2^2\omega_3^3 + 24c_s^2\omega_5\omega_2^2\omega_3^3 - 30\omega_5^2\omega_2^3\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_3^3 + 34\omega_5^2\omega_2^2\omega_3^3v_1^2 - 6\omega_5\omega_2^3\omega_3^3v_1^2 + 24c_s^2\omega_5^2\omega_2\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM1}} = (-18\omega_5^2\omega_2\omega_3^3v_1^2 + 6c_s^2\omega_5^2\omega_2\omega_3^3 - 12c_s^2\omega_2^2\omega_3^3 - 14c_s^2\omega_5^2\omega_2\omega_3^3 + 22\omega_5^2\omega_2^2\omega_3^3v_1^2 + 12c_s^2\omega_5^2\omega_2^2\omega_3^3 - 12c_s^2\omega_5\omega_2\omega_3^3 - 6\omega_5^3\omega_3^3v_1^2 + 12\omega_5^2\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_2\omega_3^3 + c_s^2\omega_5^2\omega_2^2\omega_3^3 - 24\omega_5\omega_2^3\omega_3^3v_1^2 + 6c_s^2\omega_2^3\omega_3^3 + 24\omega_5^2\omega_2\omega_3^3v_1^2 + 24\omega_5^2\omega_2^2\omega_3^3v_1^2 - 6c_s^2\omega_5^2\omega_2^2\omega_3^3 - 4\omega_5^2\omega_2^3\omega_3^3v_1^2 + 12\omega_2^2\omega_3^3v_1^2 - 48\omega_5^2\omega_2^2\omega_3^3v_1^2 + 12\omega_5\omega_2\omega_3^3v_1^2 - 6c_s^2\omega_5\omega_2^2\omega_3^3 + 24c_s^2\omega_5\omega_2^2\omega_3^3 - 30\omega_5^2\omega_2^3\omega_3^3v_1^2 - 12c_s^2\omega_5^2\omega_3^3 + 22\omega_5^2\omega_2^2\omega_3^3v_1^2 + 6\omega_5\omega_2^3\omega_3^3v_1^2 + 24c_s^2\omega_5^2\omega_2\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_y^3 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial t \partial x_2^2} :$$

$$C_{D_t D_y^3 v_2}^{(0), \text{SRT}} = (-36 - 108\omega v_2^2 - 20\omega^2 + 54\omega + 72v_2^2 + \omega^3 + 34c_s^2\omega^2 - 3\omega^3 v_2^2 - 2c_s^2\omega^3 - 90c_s^2\omega + 42\omega^2 v_2^2 + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{MRT1}} = (-2c_s^2\omega_6^2\omega_3^3 + 6\omega_3^3 + \omega_6^2\omega_3^3 + 48v_2^2\omega_6\omega_3 + 25c_s^2\omega_6^2\omega_3^3 - 12\omega_3^3 - 11\omega_6^2\omega_3^3 + 12\omega_6^2\omega_3 - 60v_2^2\omega_6\omega_3^3 - 48c_s^2\omega_6^2\omega_3 + 15v_2^2\omega_6\omega_3^3 + 12v_2^2\omega_6^2 - 6v_2^2\omega_3^3 - 3v_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_3^3 - 24\omega_6\omega_3 + 24c_s^2\omega_6\omega_3 + 27v_2^2\omega_6^2\omega_3^3 - 6c_s^2\omega_3^3 - 36c_s^2\omega_6\omega_3^3 - 42v_2^2\omega_6^2\omega_3 + 24c_s^2\omega_6^2 + 36\omega_6\omega_3^3 + 9c_s^2\omega_6\omega_3^3 + 12c_s^2\omega_3^3 - 9\omega_6\omega_3^3) \frac{\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{MRT2}} = C_{D_t D_y^3 v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{CLBM1}} =$$

$$(-2c_s^2\omega_6^2\omega_3^3 + 6\omega_3^3 + \omega_6^2\omega_3^3 + 72v_2^2\omega_6\omega_3 + 25c_s^2\omega_6^2\omega_3^2 - 12\omega_3^2 - 11\omega_6^2\omega_3^2 + 12\omega_6^2\omega_3 - 108v_2^2\omega_6\omega_3^2 - 48c_s^2\omega_6^2\omega_3 + 27v_2^2\omega_6\omega_3^3 - 36v_2^2\omega_6^2 - 18v_2^2\omega_3^3 - 3v_2^2\omega_6^2\omega_3^3 + 36v_2^2\omega_3^2 - 24\omega_6\omega_3 + 24c_s^2\omega_6\omega_3 + 15v_2^2\omega_6^2\omega_3^2 - 6c_s^2\omega_3^3 - 36c_s^2\omega_6\omega_3^2 + 18v_2^2\omega_6^2\omega_3 + 24c_s^2\omega_6^2 + 36\omega_6\omega_3^2 + 9c_s^2\omega_6\omega_3^3 + 12c_s^2\omega_3^2 - 9\omega_6\omega_3^3) \frac{\rho}{12\omega_6^3\omega_3^3}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{CLBM2}} = C_{D_t D_y^3 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x D_y^3 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 \rho}^{(0), \text{SRT}} = (24 + 14\omega^2 - 36\omega - \omega^3 - 72c_s^2\omega^2 + 6c_s^2\omega^3 + 180c_s^2\omega - 120c_s^2) \frac{v_2 v_1}{6\omega^3}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT1}} = (-48c_s^2\omega_2^3\omega_6^2\omega_3^2 + 6\omega_2^2v_2^2\omega_6\omega_3^3 - \omega_3^3\omega_6^2\omega_3^3 + 6c_s^2\omega_2^3\omega_6^2\omega_3^3 - 24\omega_3^3v_2^2\omega_6\omega_3 + 7\omega_3^3\omega_6^2\omega_3^2 - 12\omega_2^2v_2^2\omega_6\omega_3^2 + 6\omega_2v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3\omega_6^2\omega_3 - 3\omega_2^3\omega_6^3 - 3\omega_3^3\omega_3^3 + 42\omega_2^3v_2^2\omega_6\omega_3^2 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 36c_s^2\omega_3^3\omega_6^2 - 12c_s^2\omega_2^2\omega_6\omega_3^2 + 6\omega_2^3\omega_6\omega_3^2 + 6\omega_3^3\omega_3^2 - 12\omega_2v_2^2\omega_6^2\omega_3^3 + 6c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^2 - 12c_s^2\omega_3^3\omega_3^2 + 78c_s^2\omega_2^3\omega_6^2\omega_3 - 12\omega_3^3v_2^2\omega_6\omega_3^3 - 3\omega_3^3\omega_6^2\omega_3^2 + 24\omega_2^3v_2^2\omega_6^2 + 6\omega_2^3v_2^2\omega_3^3 + 6v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^2\omega_6^2\omega_3^3 - 24c_s^2\omega_2^3\omega_6\omega_3 + 12\omega_3^3\omega_6\omega_3 - 12\omega_3^3v_2^2\omega_3^2 + 12\omega_2^2v_2^2\omega_6^2\omega_3 + \omega_2^2\omega_6^2\omega_3^3 + 6\omega_3^3v_2^2\omega_6^2\omega_3^2 + 42c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^3 - 30\omega_3^3v_2^2\omega_6\omega_3 - 24c_s^2\omega_2^2\omega_6\omega_3 - 21\omega_3^3\omega_6\omega_3^2 - 12\omega_2^2v_2^2\omega_6^2\omega_3^2 + 42c_s^2\omega_2^2\omega_6\omega_3^2 + 6\omega_2^2v_2^2\omega_6^2\omega_3^3 + 6\omega_2^3\omega_6\omega_3^3) \frac{v_2 v_1}{6\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT2}} = C_{D_x D_y^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM1}} = (-36c_s^2\omega_2^3\omega_6^2\omega_3^2 - \omega_2^3\omega_6^2\omega_3^3 + 6c_s^2\omega_2^3\omega_6^2\omega_3^3 - 24\omega_3^3v_2^2\omega_6\omega_3 + 7\omega_3^3\omega_6^2\omega_3^2 + 6\omega_2v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3\omega_6^2\omega_3 - 3\omega_2^3\omega_6\omega_3^3 - 3\omega_3^3\omega_3^3 + 12\omega_3^3v_2^2\omega_6\omega_3^2 + 18c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 24c_s^2\omega_2^2\omega_6\omega_3^2 + 6\omega_2^3\omega_6\omega_3^2 + 6\omega_3^3\omega_3^2 - 12\omega_2v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^2 - 36c_s^2\omega_3^3\omega_6^2\omega_3 + 3\omega_2^3\omega_6^2\omega_3^2 - 6\omega_3^3v_2^2\omega_3^3 + 6v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^2\omega_6^2\omega_3^3 - 24c_s^2\omega_2^3\omega_6\omega_3 + 12\omega_3^3\omega_6\omega_3 + 12\omega_3^3v_2^2\omega_3^2 + \omega_2^2\omega_6^2\omega_3^3 - 6\omega_3^3v_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^2\omega_6^2\omega_3^2 - 24c_s^2\omega_2^3\omega_6\omega_3^3 + 12\omega_3^3v_2^2\omega_6^2\omega_3 - 12c_s^2\omega_2^2\omega_6^2\omega_3 - 21\omega_3^3\omega_6\omega_3^2 - 6\omega_2^2v_2^2\omega_6^2\omega_3^2 + 72c_s^2\omega_2^3\omega_6\omega_3^2 + 6\omega_2^2v_2^2\omega_6^2\omega_3^3 + 6\omega_3^3\omega_6\omega_3^3) \frac{v_2 v_1}{6\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM2}} = C_{D_x D_y^3 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x D_y^3 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 v_1}^{(0), \text{SRT}} = (36 + 54\omega v_2^2 + 20\omega^2 - 54\omega - 36v_2^2 - \omega^3 - 56c_s^2\omega^2 + \omega^3 v_2^2 + 4c_s^2\omega^3 + 144c_s^2\omega - 20\omega^2 v_2^2 - 96c_s^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT1}} = (4c_s^2\omega_2^3\omega_3^3 - 6\omega_3^3 - \omega_6^2\omega_3^3 - 36v_2^2\omega_6\omega_3 - 44c_s^2\omega_6^2\omega_3^2 + 12\omega_3^2 + 11\omega_6^2\omega_3^2 - 12\omega_6^2\omega_3 + 48v_2^2\omega_6\omega_3^2 + 90c_s^2\omega_6^2\omega_3 - 12v_2^2\omega_6\omega_3^3 + 12v_2^2\omega_6^2 + 6v_2^2\omega_3^3 + v_2^2\omega_6^2\omega_3^3 - 12v_2^2\omega_3^2 + 24\omega_6\omega_3 - 36c_s^2\omega_6\omega_3 - 8v_2^2\omega_6^2\omega_3^2 + 6c_s^2\omega_3^3 + 48c_s^2\omega_6\omega_3^2 - 48c_s^2\omega_6^2 - 36\omega_6\omega_3^2 - 12c_s^2\omega_6\omega_3^3 - 12c_s^2\omega_3^2 + 9\omega_6\omega_3^3) \frac{v_2 \rho}{12\omega_6^3\omega_3^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT2}} = C_{D_x D_y^3 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM1}} = (4c_s^2\omega_6^2\omega_3^3 - 6\omega_3^3 - \omega_6^2\omega_3^3 - 60v_2^2\omega_6\omega_3 - 26c_s^2\omega_6^2\omega_3^2 + 12\omega_3^2 + 11\omega_6^2\omega_3^2 - 12\omega_6^2\omega_3 + 48v_2^2\omega_6\omega_3^2 + 18c_s^2\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^3 + 12v_2^2\omega_6^2 - 6v_2^2\omega_3^3 + v_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_3^2 + 24\omega_6\omega_3 - 36c_s^2\omega_6\omega_3 - 14v_2^2\omega_6^2\omega_3^2 + 30c_s^2\omega_3^3 + 96c_s^2\omega_6\omega_3^2 + 12v_2^2\omega_6^2\omega_3 - 36\omega_6\omega_3^2 - 30c_s^2\omega_6\omega_3^3 - 60c_s^2\omega_3^2 + 9\omega_6\omega_3^3) \frac{v_2 \rho}{12\omega_6^3\omega_3^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM2}} = C_{D_x D_y^3 v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x D_y^3 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 v_2}^{(0), \text{SRT}} = (12 + 18\omega v_2^2 + 8\omega^2 - 18\omega - 12v_2^2 - \omega^3 - 56c_s^2\omega^2 + 3\omega^3 v_2^2 + 4c_s^2\omega^3 + 144c_s^2\omega - 12\omega^2 v_2^2 - 96c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT1}} = (-32c_s^2\omega_2^3\omega_6^2\omega_3^2 + 12\omega_2^2v_2^2\omega_6\omega_3^3 - \omega_2^3\omega_6^2\omega_3^3 + 4c_s^2\omega_2^3\omega_6^2\omega_3^3 - 12\omega_3^3v_2^2\omega_6\omega_3 + 3\omega_3^3\omega_6^2\omega_3^2 - 24\omega_2^2v_2^2\omega_6\omega_3^2 - 6\omega_2^3\omega_6\omega_3^3 + 36\omega_3^3v_2^2\omega_6\omega_3^2 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 24c_s^2\omega_2^2\omega_6\omega_3^2 + 12\omega_2^3\omega_6\omega_3^2 - 18\omega_2v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^2 - 12c_s^2\omega_3^3\omega_3^2 + 36c_s^2\omega_2^3\omega_6^2\omega_3 - 12\omega_3^3v_2^2\omega_6\omega_3^3 - 6\omega_3^3\omega_6^2\omega_3^2 + 24\omega_2^3v_2^2\omega_6^2 + 6\omega_2^3v_2^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6\omega_3 + 3\omega_3^3v_2^2\omega_6^2\omega_3^2 - 12\omega_3^3v_2^2\omega_3^2 + 2\omega_2^2\omega_6^2\omega_3^3 + 48c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^3 - 30\omega_3^3v_2^2\omega_6^2\omega_3 - 24c_s^2\omega_2^2\omega_6\omega_3^2 - 6\omega_3^3\omega_6\omega_3^2 + 12\omega_3^3v_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^3\omega_6\omega_3^2 + 3\omega_3^3\omega_6\omega_3^3) \frac{\rho v_1}{12\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT2}} = C_{D_x D_y^3 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM1}} = (-32c_s^2\omega_2^3\omega_6^2\omega_3^2 + 12\omega_2^2v_2^2\omega_6\omega_3^3 - \omega_2^3\omega_6^2\omega_3^3 + 4c_s^2\omega_2^3\omega_6^2\omega_3^3 + 12\omega_3^3v_2^2\omega_6\omega_3 + 3\omega_3^3\omega_6^2\omega_3^2 - 24\omega_2^2v_2^2\omega_6\omega_3^2 - 6\omega_2^3\omega_6\omega_3^3 - 12\omega_3^3v_2^2\omega_6\omega_3^2 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 24c_s^2\omega_2^2\omega_6\omega_3^2 + 12\omega_2^3\omega_6\omega_3^2 - 18\omega_2v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^2 - 12c_s^2\omega_3^3\omega_3^2 +$$

$$36c_s^2\omega_3^3\omega_6^2\omega_3 - 6\omega_2^2\omega_6^2\omega_3^2 - 24\omega_2^3v_2^2\omega_6^2 - 6\omega_2^3v_2^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6\omega_3 + 3\omega_2^3v_2^2\omega_6^2\omega_3^3 + 12\omega_2^3v_2^2\omega_3^2 + 2\omega_2^2\omega_6^2\omega_3^3 - 12\omega_2^2v_2^2\omega_6^2\omega_3^2 + 48c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^3 + 30\omega_2^3v_2^2\omega_6^2\omega_3 - 24c_s^2\omega_2^2\omega_6^2\omega_3 - 6\omega_2^3\omega_6\omega_3^2 + 12\omega_2^2v_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^3\omega_6\omega_3^2 + 3\omega_2^3\omega_6\omega_3^3) \frac{\rho v_1}{12\omega_2^2\omega_6^2\omega_3^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM2}} = C_{D_x D_y^3 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_y^4 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x^2}$:

$$C_{D_y^4 \rho}^{(0), \text{SRT}} = (216c_s^2\omega v_2^2 - 108\omega v_2^2 - 3c_s^4\omega^3 - 42\omega^2 v_2^4 + 48c_s^4 + 30c_s^4\omega^2 - 72c_s^4\omega + 72v_2^2 + 3\omega^3 v_2^4 - 144c_s^2 v_2^2 - 72v_2^4 - 14c_s^2\omega^2 - 3\omega^3 v_2^2 + 6c_s^2\omega^3 v_2^2 + c_s^2\omega^3 + 108\omega v_2^4 - 84c_s^2\omega^2 v_2^2 + 36c_s^2\omega + 42\omega^2 v_2^2 - 24c_s^2) \frac{1}{24\omega^3}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT1}} = (-24v_2^4\omega^3 + c_s^2\omega_6^2\omega_3^3 - 24c_s^2v_2^2\omega_6\omega_3 - 48c_s^4\omega_6^2\omega_3 + 72v_2^4\omega_6\omega_3^2 + 48v_2^2\omega_6\omega_3 + 12v_2^4\omega_3^3 - 8c_s^2\omega_6^2\omega_3^2 - 18v_2^4\omega_6\omega_3^3 - 3c_s^4\omega_6^2\omega_3^3 - 12c_s^2v_2^2\omega_6\omega_3^3 - 72v_2^2\omega_6\omega_3^2 + 12c_s^2\omega_6^2\omega_3 + 48c_s^2v_2^2\omega_6\omega_3^2 + 24c_s^4\omega_6^2\omega_3^2 + 24c_s^4\omega_6^2 - 48v_2^4\omega_6\omega_3 + 18v_2^2\omega_6\omega_3^3 - 72c_s^2v_2^2\omega_6^2\omega_3^2 + 24v_2^4\omega_6^2\omega_3 - 24c_s^4\omega_6\omega_3^2 - 12v_2^2\omega_3^3 - 3v_2^2\omega_6^2\omega_3^3 + 12c_s^2v_2^2\omega_3^3 - 96c_s^2v_2^2\omega_6^2 + 6c_s^4\omega_6\omega_3^3 + 24v_2^2\omega_3^2 + 6c_s^2v_2^2\omega_6^2\omega_3^3 - 24c_s^2\omega_6\omega_3 + 24v_2^2\omega_6^2\omega_3^2 - 24c_s^2v_2^2\omega_3^2 + 24c_s^2\omega_6\omega_3^2 - 24v_2^2\omega_6^2\omega_3 + 3v_2^4\omega_6^2\omega_3^3 - 6c_s^2\omega_6\omega_3^3 + 156c_s^2v_2^2\omega_6^2\omega_3 - 24v_2^4\omega_6^2\omega_3^2 + 24c_s^4\omega_6\omega_3) \frac{1}{24\omega_6^2\omega_3^3}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT2}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CLBM1}} = (-72v_2^4\omega_3^3 + c_s^2\omega_6^2\omega_3^3 + 72c_s^2v_2^2\omega_6\omega_3 - 48c_s^4\omega_6^2\omega_3 + 72v_2^4\omega_6\omega_3^2 + 36v_2^4\omega_3^3 - 8c_s^2\omega_6^2\omega_3^2 - 30v_2^4\omega_6\omega_3^3 - 3c_s^4\omega_6^2\omega_3^3 - 72c_s^2v_2^2\omega_6\omega_3^3 - 72v_2^2\omega_6\omega_3^2 + 12c_s^2\omega_6^2\omega_3 + 144c_s^2v_2^2\omega_6\omega_3^2 + 24c_s^4\omega_6^2\omega_3^2 + 24c_s^4\omega_6^2 + 30v_2^2\omega_6\omega_3^3 - 12c_s^2v_2^2\omega_6^2\omega_3^2 - 24c_s^4\omega_6\omega_3^2 - 36v_2^2\omega_3^3 - 3v_2^2\omega_6^2\omega_3^3 + 108c_s^2v_2^2\omega_3^3 + 6c_s^4\omega_6\omega_3^3 + 72v_2^2\omega_3^2 + 6c_s^2v_2^2\omega_6^2\omega_3^3 - 24c_s^2\omega_6\omega_3 + 12v_2^2\omega_6^2\omega_3^2 - 216c_s^2v_2^2\omega_3^3 + 24c_s^2\omega_6\omega_3^2 + 3v_2^4\omega_6^2\omega_3^3 - 6c_s^2\omega_6\omega_3^3 - 36c_s^2v_2^2\omega_6^2\omega_3 - 12v_2^4\omega_6^2\omega_3^2 + 24c_s^4\omega_6\omega_3) \frac{1}{24\omega_6^2\omega_3^3}$$

$$C_{D_y^4 \rho}^{(0), \text{CLBM2}} = C_{D_y^4 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_y^4 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x^2}$:

$$C_{D_y^4 v_2}^{(0), \text{SRT}} = (24 + 54\omega v_2^2 + 14\omega^2 - 36\omega - 36v_2^2 - \omega^3 - 26c_s^2\omega^2 + 2\omega^3 v_2^2 + c_s^2\omega^3 + 72c_s^2\omega - 22\omega^2 v_2^2 - 48c_s^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_y^4 v_2}^{(0), \text{MRT1}} = (c_s^2\omega_6^2\omega_3^3 - 6\omega_3^3 - \omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3 - 20c_s^2\omega_6^2\omega_3^2 + 12\omega_3^2 + 8\omega_6^2\omega_3^2 - 6\omega_6^2\omega_3 + 24v_2^2\omega_6\omega_3^2 + 42c_s^2\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^3 - 12v_2^2\omega_6^2 + 6v_2^2\omega_3^3 + 2v_2^2\omega_6^2\omega_3^3 - 12v_2^2\omega_3^2 + 12\omega_6\omega_3 - 12c_s^2\omega_6\omega_3 - 16v_2^2\omega_6^2\omega_3^2 + 6c_s^2\omega_3^3 + 24c_s^2\omega_6\omega_3^2 + 24v_2^2\omega_6^2\omega_3 - 24c_s^2\omega_6^2 - 24\omega_6\omega_3^2 - 6c_s^2\omega_6\omega_3^3 - 12c_s^2\omega_3^2 + 6\omega_6\omega_3) \frac{v_2 \rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4 v_2}^{(0), \text{MRT2}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CLBM1}} = (c_s^2\omega_6^2\omega_3^3 - 18\omega_3^3 - \omega_6^2\omega_3^3 + 60v_2^2\omega_6\omega_3 - 2c_s^2\omega_6^2\omega_3^2 + 36\omega_3^2 + 2\omega_6^2\omega_3^2 + 6\omega_6^2\omega_3 + 24v_2^2\omega_6\omega_3^2 - 30c_s^2\omega_6^2\omega_3 - 24v_2^2\omega_6\omega_3^3 - 12v_2^2\omega_6^2 + 42v_2^2\omega_3^3 + 2v_2^2\omega_6^2\omega_3^3 - 84v_2^2\omega_3^2 - 12\omega_6\omega_3 - 12c_s^2\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^2 + 30c_s^2\omega_3^3 + 72c_s^2\omega_6\omega_3^2 - 12v_2^2\omega_6^2\omega_3 + 24c_s^2\omega_6^2 - 24\omega_6\omega_3^2 - 24c_s^2\omega_6\omega_3^3 - 60c_s^2\omega_3^2 + 12\omega_6\omega_3) \frac{v_2 \rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4 v_2}^{(0), \text{CLBM2}} = C_{D_y^4 v_2}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t^3 D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial t^3 \partial x_3}$:

$$C_{D_t^3 D_z v_3}^{(0), \text{SRT}} = (-2 - \omega^2 + 3\omega) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3 D_z v_3}^{(0), \text{MRT1}} = (-2 + 3\omega_4 - \omega_4^2) \frac{\rho}{2\omega_4^3}$$

$$C_{D_t^3 D_z v_3}^{(0), \text{MRT2}} = C_{D_t^3 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_z v_3}^{(0), \text{CLBM1}} = C_{D_t^3 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_z v_3}^{(0), \text{CLBM2}} = C_{D_t^3 D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_t^2 D_x D_z v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3}$:

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{SRT}} = (36 + 20\omega^2 - 54\omega - \omega^3) \frac{v_3 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT1}} = (13\omega_4^2 \omega_2^2 + 7\omega_4^3 \omega_2 - \omega_4^3 \omega_2^2 + 12\omega_4^2 - 24\omega_4^2 \omega_2 - 6\omega_4^3 + 12\omega_4 \omega_2 + 12\omega_2^2 - 24\omega_4 \omega_2^2) \frac{v_3 \rho}{12\omega_4^3 \omega_2^2}$$

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_t^2 D_x D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3}$:

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{SRT}} = (36 + 20\omega^2 - 54\omega - \omega^3) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}} = (13\omega_4^2 \omega_2^2 - \omega_4^2 \omega_3^2 + 12\omega_4^2 - 24\omega_4^2 \omega_2 + 12\omega_4 \omega_2 + 12\omega_2^2 - 6\omega_2^3 + 7\omega_4 \omega_2^3 - 24\omega_4 \omega_2^2) \frac{\rho v_1}{12\omega_4^3 \omega_2^3}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x^2 D_z v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3}$:

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{SRT}} = (-24 - 14\omega^2 + 36\omega + \omega^3) \frac{v_3 \rho v_1}{6\omega^3}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{MRT1}} = (12\omega_4^2 \omega_5 \omega_2^2 + 12\omega_4^2 \omega_2^2 - 6\omega_4^2 \omega_3^2 - 7\omega_4^2 \omega_5 \omega_3^2 - 6\omega_4^3 \omega_2^2 - 12\omega_4^3 \omega_5 - 12\omega_4^2 \omega_5 \omega_2 + 3\omega_4^3 \omega_2^2 + \omega_4^3 \omega_5 \omega_2^2 - 6\omega_5 \omega_2^3 - 10\omega_4^3 \omega_5 \omega_2^2 + 24\omega_4^3 \omega_5 \omega_2 - 6\omega_4 \omega_5 \omega_2^2 + 12\omega_4 \omega_5 \omega_2^3) \frac{v_3 \rho v_1}{6\omega_4^3 \omega_5 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{CLBM1}} = (6\omega_4^2 \omega_2^2 - 7\omega_4^2 \omega_3^2 + 18\omega_4^3 \omega_2 - 7\omega_4^3 \omega_2^2 + \omega_4^3 \omega_2^3 - 12\omega_4^3 - 6\omega_2^3 + 12\omega_4 \omega_2^3 - 6\omega_4 \omega_2^2) \frac{v_3 \rho v_1}{6\omega_4^3 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 D_z v_1}^{(0), \text{CLBM1}}$$

coefficient $C_{D_t D_x^2 D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3}$:

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{SRT}} = (-2\omega^2 v_1^2 + 34c_s^2 \omega^2 - 2c_s^2 \omega^3 + \omega^3 v_1^2 - 90c_s^2 \omega + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{MRT1}} = (22c_s^2 \omega_4 \omega_5^2 \omega_2^2 + 6\omega_5^2 \omega_2^2 v_1^2 - 6\omega_4 \omega_2^3 v_1^2 - 30\omega_4 \omega_5 \omega_2^2 v_1^2 - 2c_s^2 \omega_4 \omega_5^2 \omega_2^3 + 36\omega_4 \omega_5^2 \omega_2 v_1^2 + 12c_s^2 \omega_5^2 \omega_2 + 12\omega_4 \omega_2^2 v_1^2 + 9\omega_4 \omega_5 \omega_2^3 v_1^2 - 18c_s^2 \omega_5^2 \omega_2^2 - \omega_5^2 \omega_2^3 v_1^2 + 3c_s^2 \omega_5^2 \omega_2^3 - 30c_s^2 \omega_4 \omega_5^2 \omega_2 - 6c_s^2 \omega_5 \omega_2^3 + 12c_s^2 \omega_4 \omega_5^2 + \omega_4 \omega_5^2 \omega_2^3 v_1^2 - 24\omega_4 \omega_5^2 v_1^2 + 12c_s^2 \omega_4 \omega_5 \omega_2 - 6\omega_5 \omega_2^3 v_1^2 + 12c_s^2 \omega_5 \omega_2^2 - 6c_s^2 \omega_4 \omega_2^3 + 12\omega_5 \omega_2^2 v_1^2 + 9c_s^2 \omega_4 \omega_5 \omega_2^3 - 10\omega_4 \omega_5^2 \omega_2^2 v_1^2 - 30c_s^2 \omega_4 \omega_5 \omega_2^2 - 12\omega_5^2 \omega_2 v_1^2 + 12c_s^2 \omega_4 \omega_2^2 + 12\omega_4 \omega_5 \omega_2 v_1^2) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_x^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{CLBM1}} = (22c_s^2 \omega_4 \omega_5^2 \omega_2^2 - 6\omega_5^2 \omega_2^2 v_1^2 + 6\omega_4 \omega_2^3 v_1^2 + 30\omega_4 \omega_5 \omega_2^2 v_1^2 - 2c_s^2 \omega_4 \omega_5^2 \omega_2^3 - 36\omega_4 \omega_5^2 \omega_2 v_1^2 + 12c_s^2 \omega_5^2 \omega_2 - 12\omega_4 \omega_2^2 v_1^2 - 9\omega_4 \omega_5 \omega_2^3 v_1^2 - 18c_s^2 \omega_5^2 \omega_2^2 - \omega_5^2 \omega_2^3 v_1^2 + 3c_s^2 \omega_5^2 \omega_2^3 - 30c_s^2 \omega_4 \omega_5^2 \omega_2 - 6c_s^2 \omega_5 \omega_2^3 + 12c_s^2 \omega_4 \omega_5^2 + \omega_4 \omega_5^2 \omega_2^3 v_1^2 + 24\omega_4 \omega_5^2 v_1^2 + 12c_s^2 \omega_4 \omega_5 \omega_2 + 6\omega_5 \omega_2^3 v_1^2 + 12c_s^2 \omega_5 \omega_2^2 - 6c_s^2 \omega_4 \omega_2^3 - 12\omega_5 \omega_2^2 v_1^2 + 9c_s^2 \omega_4 \omega_5 \omega_2^3 + 8\omega_4 \omega_5^2 \omega_2^2 v_1^2 - 30c_s^2 \omega_4 \omega_5 \omega_2^2 + 12\omega_5^2 \omega_2 v_1^2 + 12c_s^2 \omega_4 \omega_2^2 - 12\omega_4 \omega_5 \omega_2 v_1^2) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_x^2 D_z v_3}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^3 D_z \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z \rho}^{(0), \text{SRT}} = (24 + 14\omega^2 - 36\omega - \omega^3 - 72c_s^2\omega^2 + 6c_s^2\omega^3 + 180c_s^2\omega - 120c_s^2) \frac{v_3 v_1}{6\omega^3}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{MRT}^1} = (-12c_s^2\omega_4\omega_5^2\omega_2^2 + 6c_s^2\omega_4^2\omega_5\omega_2^3 + 78c_s^2\omega_4^3\omega_5^2\omega_2 - 24\omega_4^3\omega_5\omega_2v_1^2 + 6\omega_4^2\omega_5\omega_2^2 + 6\omega_4^2\omega_5^2\omega_2^3v_1^2 + 6\omega_4^3\omega_5^2\omega_2^2v_1^2 - 12c_s^2\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4\omega_5^2\omega_2^3 - 36c_s^2\omega_4^3\omega_5^2 - 12\omega_4^3\omega_5^2v_1^2 - 3\omega_4^2\omega_5\omega_2^3 + 7\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^2\omega_5^2\omega_2^2v_1^2 + 6\omega_4^3\omega_5^2 - 12c_s^2\omega_4^3\omega_2^2 + 6\omega_5^2\omega_2^3v_1^2 + 6c_s^2\omega_4^3\omega_5^2\omega_2^3 + 6\omega_4^3\omega_2^3v_1^2 - 3\omega_4^3\omega_2^3 - \omega_4^3\omega_5^2\omega_2^3 - 48c_s^2\omega_4^3\omega_5^2\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 - 12\omega_4^2\omega_5\omega_2^3v_1^2 + 6\omega_4^3\omega_5\omega_2^3 - 12\omega_4\omega_5^2\omega_2^3v_1^2 + 42c_s^2\omega_4^3\omega_5\omega_2^3 - 21\omega_4^3\omega_5\omega_2^3 + 12\omega_4^2\omega_5\omega_2^3v_1^2 - 12c_s^2\omega_4^3\omega_5\omega_2^3 - 12\omega_4^3\omega_5\omega_2^3v_1^2 - 24c_s^2\omega_4^2\omega_5^2\omega_2 - 30\omega_4^3\omega_5^2\omega_2v_1^2 + 42c_s^2\omega_4^2\omega_5^2\omega_2^2 + 6\omega_4\omega_5^2\omega_2^2v_1^2 + 12\omega_4^3\omega_5\omega_2 + \omega_4^2\omega_5^2\omega_2^3 + 6\omega_4^2\omega_5\omega_2^3v_1^2 - 12c_s^2\omega_4^2\omega_5^2\omega_2^2 + 42\omega_4^2\omega_5\omega_2^3v_1^2 - 24c_s^2\omega_4^3\omega_5\omega_2 + 24\omega_4^3\omega_5^2v_1^2 - 3\omega_4^2\omega_5^2\omega_2^2) \frac{v_3 v_1}{6\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{MRT}^2} = C_{D_x^3 D_z \rho}^{(0), \text{MRT}^1}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CLBM}^1} = (-12c_s^2\omega_4\omega_5^2\omega_2^2 + 12c_s^2\omega_4^2\omega_5\omega_2^3 + 36c_s^2\omega_4^3\omega_5^2\omega_2 - 24\omega_4^3\omega_5\omega_2v_1^2 + 6\omega_4^2\omega_5\omega_2^2 + 6\omega_4^2\omega_5^2\omega_2^3v_1^2 - 6\omega_4^3\omega_5^2\omega_2^2v_1^2 - 24c_s^2\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4\omega_5^2\omega_2^3 - 36c_s^2\omega_4^3\omega_5^2 + 12\omega_4^3\omega_2^3v_1^2 - 3\omega_4^2\omega_5\omega_2^3 + 7\omega_4^3\omega_5^2\omega_2^2 - 6\omega_4^2\omega_5^2\omega_2^2v_1^2 + 6\omega_4^3\omega_2^2 - 36c_s^2\omega_4^3\omega_2^2 + 6\omega_5^2\omega_2^3v_1^2 + 6c_s^2\omega_4^3\omega_5^2\omega_2^3 - 6\omega_4^3\omega_2^3v_1^2 - 3\omega_4^3\omega_2^3 - \omega_4^3\omega_5^2\omega_2^3 - 36c_s^2\omega_4^3\omega_5^2\omega_2^2 + 18c_s^2\omega_4^3\omega_2^3 + 6\omega_4^3\omega_5\omega_2^3 - 12\omega_4\omega_5^2\omega_2^3v_1^2 + 72c_s^2\omega_4^3\omega_5\omega_2^3 - 21\omega_4^3\omega_5\omega_2^3 - 24c_s^2\omega_4^3\omega_5\omega_2^3 - 12c_s^2\omega_4^2\omega_5^2\omega_2 - 12\omega_4^2\omega_5\omega_2^3v_1^2 + 36c_s^2\omega_4^2\omega_5^2\omega_2^2 + 6\omega_4\omega_5^2\omega_2^3v_1^2 + 12\omega_4^3\omega_5\omega_2 + \omega_4^2\omega_5^2\omega_2^3 - 12c_s^2\omega_4^2\omega_5^2\omega_2^3 + 12\omega_4^3\omega_5\omega_2^2v_1^2 - 24c_s^2\omega_4^3\omega_5\omega_2 - 3\omega_4^2\omega_5^2\omega_2^2) \frac{v_3 v_1}{6\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CLBM}^2} = C_{D_x^3 D_z \rho}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{D_x^3 D_z v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z v_1}^{(0), \text{SRT}} = (12 - 12v_1^2 + 8\omega^2 - 18\omega - \omega^3 + 18\omega v_1^2 - 12\omega^2 v_1^2 - 56c_s^2\omega^2 + 4c_s^2\omega^3 + 3\omega^3 v_1^2 + 144c_s^2\omega - 96c_s^2) \frac{v_3 \rho}{12\omega^3}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{MRT}^1} = (-12c_s^2\omega_4\omega_5^2\omega_2^2 + 12c_s^2\omega_4^2\omega_5\omega_2^3 + 36c_s^2\omega_4^3\omega_5^2\omega_2 - 12\omega_4^3\omega_5\omega_2v_1^2 + 12\omega_4^2\omega_5\omega_2^2 - 24c_s^2\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4\omega_5^2\omega_2^3 - 12c_s^2\omega_4^3\omega_5^2 - 12\omega_4^3\omega_2^3v_1^2 - 6\omega_4^2\omega_5\omega_2^3 + 3\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2^2v_1^2 - 12c_s^2\omega_4^3\omega_2^2 + 12\omega_5^2\omega_2^3v_1^2 + 4c_s^2\omega_4^3\omega_5^2\omega_2^3 + 6\omega_4^3\omega_2^3v_1^2 - \omega_4^3\omega_5^2\omega_2^3 - 32c_s^2\omega_4^3\omega_5^2\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 + 3\omega_4^3\omega_2^3v_1^2 - 24\omega_4^2\omega_5\omega_2^3v_1^2 + 3\omega_4^3\omega_5\omega_2^3 - 18\omega_4\omega_5^2\omega_2^3v_1^2 + 36c_s^2\omega_4^3\omega_5\omega_2^3 - 6\omega_4^3\omega_5\omega_2^3 - 12c_s^2\omega_4^3\omega_5\omega_2^3 - 12\omega_4^3\omega_5\omega_2^3v_1^2 - 24c_s^2\omega_4^2\omega_5^2\omega_2 - 30\omega_4^3\omega_5^2\omega_2v_1^2 + 48c_s^2\omega_4^2\omega_5^2\omega_2^2 + 2\omega_4^2\omega_5^2\omega_2^3 + 12\omega_4^3\omega_5\omega_2^3v_1^2 - 12c_s^2\omega_4^2\omega_5^2\omega_2^3 + 36\omega_4^3\omega_5\omega_2^2v_1^2 - 12c_s^2\omega_4^3\omega_5\omega_2 + 24\omega_4^3\omega_5^2v_1^2 - 6\omega_4^2\omega_5^2\omega_2^2) \frac{v_3 \rho}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{MRT}^2} = C_{D_x^3 D_z v_1}^{(0), \text{MRT}^1}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CLBM}^1} = (-12c_s^2\omega_4\omega_5^2\omega_2^2 + 12c_s^2\omega_4^2\omega_5\omega_2^3 + 36c_s^2\omega_4^3\omega_5^2\omega_2 + 12\omega_4^3\omega_5\omega_2v_1^2 + 12\omega_4^2\omega_5\omega_2^2 - 12\omega_4^3\omega_5^2\omega_2^2v_1^2 - 24c_s^2\omega_4^2\omega_5\omega_2^2 + 6c_s^2\omega_4\omega_5^2\omega_2^3 - 12c_s^2\omega_4^3\omega_5^2 + 12\omega_4^3\omega_2^3v_1^2 - 6\omega_4^2\omega_5\omega_2^3 + 3\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2^2v_1^2 - 12c_s^2\omega_4^3\omega_2^2 + 12\omega_5^2\omega_2^3v_1^2 + 4c_s^2\omega_4^3\omega_5^2\omega_2^3 - 6\omega_4^3\omega_2^3v_1^2 - \omega_4^3\omega_5^2\omega_2^3 - 32c_s^2\omega_4^3\omega_5^2\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 + 3\omega_4^3\omega_2^3v_1^2 - 24\omega_4^2\omega_5\omega_2^3v_1^2 + 3\omega_4^3\omega_5\omega_2^3 - 18\omega_4\omega_5^2\omega_2^3v_1^2 + 36c_s^2\omega_4^3\omega_5\omega_2^3 - 6\omega_4^3\omega_5\omega_2^3 - 12c_s^2\omega_4^3\omega_5\omega_2^3 - 24c_s^2\omega_4^2\omega_5^2\omega_2 - 30\omega_4^3\omega_5^2\omega_2v_1^2 + 48c_s^2\omega_4^2\omega_5^2\omega_2^2 + 2\omega_4^2\omega_5^2\omega_2^3 + 12\omega_4^3\omega_5\omega_2^3v_1^2 - 12c_s^2\omega_4^2\omega_5^2\omega_2^3 - 12\omega_4^3\omega_5\omega_2^2v_1^2 - 12c_s^2\omega_4^3\omega_5\omega_2 - 24\omega_4^3\omega_5^2v_1^2 - 6\omega_4^2\omega_5^2\omega_2^2) \frac{v_3 \rho}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CLBM}^2} = C_{D_x^3 D_z v_1}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{D_x^3 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z v_3}^{(0), \text{SRT}} = (36 - 36v_1^2 + 20\omega^2 - 54\omega - \omega^3 + 54\omega v_1^2 - 20\omega^2 v_1^2 - 56c_s^2\omega^2 + 4c_s^2\omega^3 + \omega^3 v_1^2 + 144c_s^2\omega - 96c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT}^1} = (-8\omega_5^2\omega_2^3v_1^2 - 36\omega_5\omega_2v_1^2 - 12\omega_5^2\omega_2 - 48c_s^2\omega_5^2 - 12\omega_2^2v_1^2 + 90c_s^2\omega_5^2\omega_2 - 44c_s^2\omega_5^2\omega_2^2 - 12c_s^2\omega_2^2 + \omega_5^2\omega_2^3v_1^2 + 11\omega_5^2\omega_2^2 + 6c_s^2\omega_2^3 + 4c_s^2\omega_5^2\omega_2^3 + 6\omega_2^3v_1^2 - \omega_5^2\omega_2^3 - 12c_s^2\omega_5\omega_2^3 + 12\omega_2^2 - 12\omega_5\omega_2^3v_1^2 + 9\omega_5\omega_2^3 + 48c_s^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5\omega_2^2v_1^2 - 36c_s^2\omega_5\omega_2 + 12\omega_5^2v_1^2) \frac{\rho v_1}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT}^2} = C_{D_x^3 D_z v_3}^{(0), \text{MRT}^1}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^1} = (-14\omega_5^2\omega_2^3v_1^2 - 60\omega_5\omega_2v_1^2 - 12\omega_5^2\omega_2 + 12\omega_2^2v_1^2 + 18c_s^2\omega_5^2\omega_2 - 26c_s^2\omega_5^2\omega_2^2 - 60c_s^2\omega_2^2 + \omega_5^2\omega_2^3v_1^2 + 11\omega_5^2\omega_2^2 + 30c_s^2\omega_2^3 + 4c_s^2\omega_5^2\omega_2^3 - 6\omega_2^3v_1^2 - \omega_5^2\omega_2^3 - 30c_s^2\omega_5\omega_2^3 + 12\omega_2^2 - 6\omega_5\omega_2^3v_1^2 + 9\omega_5\omega_2^3 + 96c_s^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5\omega_2^2v_1^2 - 36c_s^2\omega_5\omega_2 + 12\omega_5^2v_1^2 + 12\omega_5^2\omega_2v_1^2) \frac{\rho v_1}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^2} = C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{D_t^2 D_y D_z v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} :$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{SRT}} = (36 + 20\omega^2 - 54\omega - \omega^3) \frac{v_3 \rho}{12\omega^3}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}} = (12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4\omega_3^2 + 12\omega_4^2 - 6\omega_4^3 + 7\omega_4^3\omega_3 + 13\omega_4^2\omega_3^2 - 24\omega_4^2\omega_3 - \omega_4^3\omega_3^2) \frac{v_3\rho}{12\omega_4^3\omega_3^2}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_t^2 D_y D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3}$:

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{SRT}} = (36 + 20\omega^2 - 54\omega - \omega^3) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}} = (-6\omega_3^3 + 12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4\omega_3^2 + 12\omega_4^2 + 7\omega_4\omega_3^3 - \omega_4^2\omega_3^3 + 13\omega_4^2\omega_3^2 - 24\omega_4^2\omega_3) \frac{v_2\rho}{12\omega_4^2\omega_3^3}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x D_y D_z v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{SRT}} = (-20 - 12\omega^2 + 30\omega + \omega^3) \frac{v_2 v_3 \rho}{2\omega^3}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}} = (-12\omega_4^2\omega_2\omega_3 - 6\omega_4^3\omega_2 - 16\omega_4^2\omega_2\omega_3^3 + 30\omega_4^2\omega_2\omega_3^2 - 6\omega_4\omega_3^3 + 12\omega_4^2\omega_3^3 + 18\omega_4\omega_2\omega_3^3 - 6\omega_4^3\omega_3 - 12\omega_4^2\omega_3^2 - 12\omega_4\omega_2\omega_3^2 + 18\omega_4^3\omega_2\omega_3 - 4\omega_4^3\omega_3^3 - 16\omega_4^2\omega_2\omega_3^2 + 3\omega_4^3\omega_2\omega_3^3 + 12\omega_4^3\omega_3^2 - 6\omega_2\omega_3^3) \frac{v_2 v_3 \rho}{6\omega_4^3\omega_2\omega_3^3}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{CLBM1}} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{CLBM2}} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x D_y D_z v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{SRT}} = (-20 - 12\omega^2 + 30\omega + \omega^3) \frac{v_3\rho v_1}{2\omega^3}$$

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{MRT1}} = (3\omega_4^3\omega_2^3\omega_3 - 12\omega_4^2\omega_2\omega_3 - 6\omega_2^3\omega_3 - 12\omega_4^2\omega_2^2 - 12\omega_4\omega_2^2\omega_3 + 12\omega_4^2\omega_2^3 - 6\omega_4^3\omega_2 + 12\omega_4^3\omega_2^2 - 16\omega_4^3\omega_2^2\omega_3 - 4\omega_4^3\omega_2^3 + 18\omega_4\omega_2^3\omega_3 - 6\omega_4^3\omega_3 - 16\omega_4^2\omega_2^3\omega_3 + 18\omega_4^3\omega_2\omega_3 - 6\omega_4\omega_2^3 + 30\omega_4^2\omega_2^2\omega_3) \frac{v_3\rho v_1}{6\omega_4^3\omega_2^3\omega_3}$$

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_t D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_t D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_t D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_t D_x D_y D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_t D_x D_y D_z v_3}^{(0), \text{SRT}} = (-20 - 12\omega^2 + 30\omega + \omega^3) \frac{v_2\rho v_1}{2\omega^3}$$

$$C_{D_t D_x D_y D_z v_3}^{(0), \text{MRT1}} = (-16\omega_4\omega_3^3\omega_2^2 + 12\omega_2^2\omega_3^3 - 6\omega_2^3\omega_3 - 12\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_3^3\omega_2^3 - 12\omega_2^2\omega_3^2 - 4\omega_2^3\omega_3^3 + 30\omega_4\omega_2^2\omega_3^2 + 12\omega_2^3\omega_3^2 + 18\omega_4\omega_2^3\omega_3 - 16\omega_4\omega_2^2\omega_3^3 - 6\omega_4\omega_3^3 + 18\omega_4\omega_2\omega_3^3 - 12\omega_4\omega_2\omega_3^2 - 6\omega_4\omega_2^3 - 6\omega_2\omega_3^3) \frac{v_2\rho v_1}{6\omega_4\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM1}} = (-12c_s^2 \omega_4 \omega_5^2 \omega_2^2 + 12c_s^2 \omega_4^2 \omega_5 \omega_2^3 + 36c_s^2 \omega_4^3 \omega_5^2 \omega_2 + 12\omega_4^3 \omega_5 \omega_2 v_1^2 + 24\omega_4^2 \omega_5^2 \omega_2^3 v_1^2 + 16\omega_4^3 \omega_5^2 \omega_2^2 v_1^2 - 24c_s^2 \omega_4^2 \omega_5 \omega_2^2 + 6c_s^2 \omega_4 \omega_5^2 \omega_2^3 - 12c_s^2 \omega_4^3 \omega_5^2 + 12\omega_4^3 \omega_5^2 v_1^2 - 36\omega_4^2 \omega_5^2 \omega_2^2 v_1^2 - 12c_s^2 \omega_4^3 \omega_2^2 + 12\omega_5^2 \omega_2^3 v_1^2 + 4c_s^2 \omega_4^3 \omega_5^2 \omega_2^2 - 6\omega_4^3 \omega_5^3 v_1^2 - 32c_s^2 \omega_4^3 \omega_5^2 \omega_2^2 + 6c_s^2 \omega_4^3 \omega_2^2 - 5\omega_4^3 \omega_5^2 \omega_2^3 v_1^2 + 24\omega_4^2 \omega_5 \omega_2^3 v_1^2 - 30\omega_4 \omega_5^2 \omega_2^3 v_1^2 + 36c_s^2 \omega_4^3 \omega_5 \omega_2^2 - 12c_s^2 \omega_4^3 \omega_5 \omega_2^3 + 12\omega_4^3 \omega_5 \omega_2^3 v_1^2 - 24c_s^2 \omega_4^2 \omega_5^2 \omega_2 - 6\omega_4^3 \omega_5^2 \omega_2 v_1^2 + 48c_s^2 \omega_4^2 \omega_5^2 \omega_2^2 + 24\omega_4 \omega_5^2 \omega_2^3 v_1^2 - 12\omega_4^2 \omega_5 \omega_2^3 v_1^2 - 12c_s^2 \omega_4^2 \omega_5^2 \omega_2^3 - 36\omega_4^2 \omega_5 \omega_2^3 v_1^2 - 12c_s^2 \omega_4^3 \omega_5 \omega_2) \frac{v_3 \rho}{12\omega_4^3 \omega_5^2 \omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^2 D_y D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} :$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{SRT}} = (84v_1^2 - 126\omega v_1^2 + 52\omega^2 v_1^2 - 56c_s^2 \omega^2 + 4c_s^2 \omega^3 - 5\omega^3 v_1^2 + 144c_s^2 \omega - 96c_s^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT1}} = (-90\omega_5^2 \omega_2 \omega_3^3 v_1^2 + 6c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 12c_s^2 \omega_5^2 \omega_2^3 - 32c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 24\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 48\omega_5^2 \omega_3^3 v_1^2 + 24\omega_5^2 \omega_2^3 \omega_3^2 v_1^2 + 48c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 12c_s^2 \omega_5 \omega_2 \omega_3^3 + 6\omega_5^3 \omega_3^3 v_1^2 + 12\omega_5^2 \omega_3^3 v_1^2 - 12c_s^2 \omega_5^2 \omega_2^3 \omega_3 + 4c_s^2 \omega_5^2 \omega_2^3 \omega_3^2 + 36\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 6c_s^2 \omega_5^3 \omega_3^2 + 48\omega_5^2 \omega_2 \omega_3^2 v_1^2 + 24\omega_5^2 \omega_2^3 \omega_3 v_1^2 - 12c_s^2 \omega_5^2 \omega_2^3 \omega_3^2 - 5\omega_5^2 \omega_3^3 \omega_3^2 v_1^2 - 12\omega_5^2 \omega_3^3 v_1^2 - 60\omega_5^2 \omega_2^3 \omega_3^2 v_1^2 - 12\omega_5 \omega_2 \omega_3^3 v_1^2 - 12c_s^2 \omega_5 \omega_2^3 \omega_3^2 + 12c_s^2 \omega_5 \omega_3^2 \omega_3^2 + 12\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 36c_s^2 \omega_5 \omega_2^3 \omega_3^2 - 24c_s^2 \omega_5^2 \omega_2 \omega_3^2 - 30\omega_5^2 \omega_2 \omega_3^2 v_1^2 - 12c_s^2 \omega_5^2 \omega_3^2 + 40\omega_5^2 \omega_2^3 \omega_3^2 v_1^2 - 12\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 36c_s^2 \omega_5^2 \omega_2 \omega_3^2 - 24c_s^2 \omega_5 \omega_2^3 \omega_3^2) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM1}} = (-6\omega_5^2 \omega_2 \omega_3^3 v_1^2 + 6c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 12c_s^2 \omega_5^2 \omega_2^3 - 32c_s^2 \omega_5^2 \omega_2^3 \omega_3 + 24\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 24\omega_5^2 \omega_2^3 \omega_3^2 v_1^2 + 48c_s^2 \omega_5^2 \omega_2^3 \omega_3 - 12c_s^2 \omega_5 \omega_2 \omega_3^3 - 6\omega_5^3 \omega_3^3 v_1^2 + 12\omega_5^2 \omega_3^3 v_1^2 - 12c_s^2 \omega_5^2 \omega_2^3 \omega_3 + 4c_s^2 \omega_5^2 \omega_2^3 \omega_3^2 - 36\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 6c_s^2 \omega_5^3 \omega_3^2 + 24\omega_5^2 \omega_2 \omega_3^2 v_1^2 - 12c_s^2 \omega_5^2 \omega_2^3 \omega_3^2 - 5\omega_5^2 \omega_2^3 \omega_3^3 v_1^2 + 12\omega_5^2 \omega_3^3 v_1^2 - 36\omega_5^2 \omega_2^3 \omega_3^2 v_1^2 + 12\omega_5 \omega_2 \omega_3^3 v_1^2 - 12c_s^2 \omega_5 \omega_2^3 \omega_3^2 + 12c_s^2 \omega_5 \omega_3^2 \omega_3^2 + 12\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 36c_s^2 \omega_5 \omega_2^3 \omega_3^2 - 24c_s^2 \omega_5^2 \omega_2 \omega_3^2 - 30\omega_5^2 \omega_2 \omega_3^2 v_1^2 - 12c_s^2 \omega_5^2 \omega_3^2 + 16\omega_5^2 \omega_2^3 \omega_3^2 v_1^2 + 12\omega_5 \omega_2^3 \omega_3^2 v_1^2 + 36c_s^2 \omega_5^2 \omega_2 \omega_3^2 - 24c_s^2 \omega_5 \omega_2^3 \omega_3^2) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_y^2 D_z v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} :$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{SRT}} = (-24 - 14\omega^2 + 36\omega + \omega^3) \frac{v_2 v_3 \rho}{6\omega^3}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{MRT1}} = (-12\omega_4^2 \omega_6 \omega_3 - 7\omega_4^2 \omega_6 \omega_3^3 + 12\omega_4^2 \omega_6 \omega_3^2 + 12\omega_4 \omega_6 \omega_3^3 - 6\omega_4^2 \omega_3^3 + 24\omega_4^3 \omega_6 \omega_3 + 12\omega_4^2 \omega_3^2 - 12\omega_4^3 \omega_6 - 6\omega_4 \omega_6 \omega_3^2 + 3\omega_4^3 \omega_3^3 - 10\omega_4^3 \omega_6 \omega_3^2 + \omega_4^3 \omega_6 \omega_3^3 - 6\omega_4^3 \omega_3^2 - 6\omega_6 \omega_3^3) \frac{v_2 v_3 \rho}{6\omega_4^3 \omega_6 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{MRT2}} = C_{D_t D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{CLBM1}} = (-6\omega_3^3 - 6\omega_4 \omega_3^2 - 12\omega_4^3 + 12\omega_4 \omega_3^3 - 7\omega_4^2 \omega_3^3 + 18\omega_4^3 \omega_3 + 6\omega_4^2 \omega_3^2 + \omega_4^3 \omega_3^3 - 7\omega_4^3 \omega_3^2) \frac{v_2 v_3 \rho}{6\omega_4^3 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{CLBM2}} = C_{D_t D_y^2 D_z v_2}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_y^2 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} :$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{SRT}} = (34c_s^2 \omega^2 + \omega^3 v_2^2 - 2c_s^2 \omega^3 - 90c_s^2 \omega - 2\omega^2 v_2^2 + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{MRT1}} = (3c_s^2 \omega_6^2 \omega_3^3 - 30c_s^2 \omega_4 \omega_6^2 \omega_3 + 36\omega_4 v_2^2 \omega_6^2 \omega_3 - 18c_s^2 \omega_6^2 \omega_3^2 - 2c_s^2 \omega_4 \omega_6^2 \omega_3^2 + \omega_4 v_2^2 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_4 \omega_3^2 + 12v_2^2 \omega_6 \omega_3^2 + 12c_s^2 \omega_6^2 \omega_3 - 6c_s^2 \omega_4 \omega_3^3 - 10\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 22c_s^2 \omega_4 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_4 \omega_6^2 - 6v_2^2 \omega_6 \omega_3^3 - 30\omega_4 v_2^2 \omega_6 \omega_3^2 - 30c_s^2 \omega_4 \omega_6 \omega_3^2 - v_2^2 \omega_6^2 \omega_3^3 + 9c_s^2 \omega_4 \omega_6 \omega_3^3 + 9\omega_4 v_2^2 \omega_6 \omega_3^3 + 6v_2^2 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_6^2 \omega_3 + 12\omega_4 v_2^2 \omega_3^2 - 6\omega_4 v_2^2 \omega_3^3 - 6c_s^2 \omega_6 \omega_3^3 - 24\omega_4 v_2^2 \omega_6^2 + 12c_s^2 \omega_4 \omega_6 \omega_3 + 12\omega_4 v_2^2 \omega_6 \omega_3) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_y^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{CLBM1}} = (3c_s^2 \omega_6^2 \omega_3^3 - 30c_s^2 \omega_4 \omega_6^2 \omega_3 - 36\omega_4 v_2^2 \omega_6^2 \omega_3 - 18c_s^2 \omega_6^2 \omega_3^2 - 2c_s^2 \omega_4 \omega_6^2 \omega_3^2 + \omega_4 v_2^2 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_4 \omega_3^2 - 12v_2^2 \omega_6 \omega_3^2 + 12c_s^2 \omega_6^2 \omega_3 - 6c_s^2 \omega_4 \omega_3^3 + 8\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 22c_s^2 \omega_4 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_4 \omega_6^2 + 6v_2^2 \omega_6 \omega_3^3 + 30\omega_4 v_2^2 \omega_6 \omega_3^2 - 30c_s^2 \omega_4 \omega_6 \omega_3^2 - v_2^2 \omega_6^2 \omega_3^3 + 9c_s^2 \omega_4 \omega_6 \omega_3^3 - 9\omega_4 v_2^2 \omega_6 \omega_3^3 - 6v_2^2 \omega_6^2 \omega_3^2 + 12c_s^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3 - 12\omega_4 v_2^2 \omega_3^2 + 6\omega_4 v_2^2 \omega_3^3 - 6c_s^2 \omega_6 \omega_3^3 + 24\omega_4 v_2^2 \omega_6^2 + 12c_s^2 \omega_4 \omega_6 \omega_3 - 12\omega_4 v_2^2 \omega_6 \omega_3) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^2 D_z v_2}^{(0), \text{CLBM1}} = C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_2}^{(0), \text{CLBM2}} = C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

coefficient $C_{D_x D_y^2 D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3}$:

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{SRT}} = (-126\omega v_2^2 + 84v_2^2 - 56c_s^2\omega^2 - 5\omega^3 v_2^2 + 4c_s^2\omega^3 + 144c_s^2\omega + 52\omega^2 v_2^2 - 96c_s^2) \frac{\rho v_1}{12\omega_3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}} = (-32c_s^2\omega_2^3\omega_6^2\omega_3^2 + 12\omega_2^2 v_2^2\omega_6\omega_3^3 + 4c_s^2\omega_2^3\omega_6^2\omega_3^3 - 12\omega_2^3 v_2^2\omega_6\omega_3 - 24\omega_2^2 v_2^2\omega_6\omega_3^2 + 24\omega_2 v_2^2\omega_6^2\omega_3^2 + 36\omega_2^3 v_2^2\omega_6\omega_3^2 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 24c_s^2\omega_2^2\omega_6\omega_3^2 - 30\omega_2 v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_3^3 + 36c_s^2\omega_2^3\omega_6^2\omega_3 - 12\omega_2^3 v_2^2\omega_6\omega_3^3 + 48\omega_2^3 v_2^2\omega_6^2 + 6\omega_2^3 v_2^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2^3\omega_6\omega_3 - 5\omega_2^3 v_2^2\omega_6^2\omega_3^3 - 12\omega_2^3 v_2^2\omega_3^3 + 48\omega_2^2 v_2^2\omega_6^2\omega_3 + 40\omega_2^3 v_2^2\omega_6^2\omega_3^2 + 48c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^3 - 90\omega_2^3 v_2^2\omega_6^2\omega_3 - 24c_s^2\omega_2^2\omega_6^2\omega_3 - 60\omega_2^2 v_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^3\omega_6\omega_3^2 + 24\omega_2^2 v_2^2\omega_6^2\omega_3^3) \frac{\rho v_1}{12\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM1}} = (-32c_s^2\omega_2^3\omega_6^2\omega_3^2 - 12\omega_2^2 v_2^2\omega_6\omega_3^3 + 4c_s^2\omega_2^3\omega_6^2\omega_3^3 + 12\omega_2^3 v_2^2\omega_6\omega_3 + 24\omega_2^2 v_2^2\omega_6\omega_3^2 + 24\omega_2 v_2^2\omega_6^2\omega_3^2 - 36\omega_2^3 v_2^2\omega_6\omega_3^2 + 6c_s^2\omega_2^3\omega_3^3 + 6c_s^2\omega_2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^3\omega_6^2 - 24c_s^2\omega_2^2\omega_6\omega_3^2 - 30\omega_2 v_2^2\omega_6^2\omega_3^3 + 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_3^3 + 36c_s^2\omega_2^3\omega_6^2\omega_3 + 12\omega_2^3 v_2^2\omega_6\omega_3^3 - 6\omega_2^3 v_2^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_2^2\omega_6\omega_3^3 - 12c_s^2\omega_2^3\omega_6\omega_3 - 5\omega_2^3 v_2^2\omega_6^2\omega_3^3 + 12\omega_2^3 v_2^2\omega_3^3 + 16\omega_2^2 v_2^2\omega_6^2\omega_3^2 + 48c_s^2\omega_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_2^3\omega_6\omega_3^3 - 6\omega_2^3 v_2^2\omega_6^2\omega_3 - 24c_s^2\omega_2^2\omega_6^2\omega_3 - 36\omega_2^2 v_2^2\omega_6^2\omega_3^2 + 36c_s^2\omega_2^3\omega_6\omega_3^2 + 24\omega_2^2 v_2^2\omega_6^2\omega_3^3) \frac{\rho v_1}{12\omega_2^3\omega_6^2\omega_3^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM2}} = C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM1}}$$

coefficient $C_{D_y^3 D_z \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_2^3 \partial x_3}$:

$$C_{D_y^3 D_z \rho}^{(0), \text{SRT}} = (24 + 14\omega^2 - 36\omega - \omega^3 - 72c_s^2\omega^2 + 6c_s^2\omega^3 + 180c_s^2\omega - 120c_s^2) \frac{v_2 v_3}{6\omega^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT1}} = (-24\omega_4^3 v_2^2\omega_6\omega_3 - \omega_4^3\omega_6^2\omega_3^3 - 12\omega_4^2 v_2^2\omega_6\omega_3^2 - 48c_s^2\omega_4^3\omega_6^2\omega_3^2 + 7\omega_4^3\omega_6^2\omega_3^2 + 6c_s^2\omega_4^3\omega_6^2\omega_3^3 + 6\omega_4^2 v_2^2\omega_6\omega_3^3 + 6c_s^2\omega_4\omega_6^2\omega_3^3 - 12\omega_4 v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_4^2\omega_6\omega_3^2 - 6\omega_4^3\omega_6^2\omega_3 - 3\omega_4^2\omega_6\omega_3^3 - 12\omega_4^3 v_2^2\omega_6\omega_3^3 + 6c_s^2\omega_4^2\omega_6\omega_3^3 + 6\omega_4 v_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_4^2\omega_6^2\omega_3^2 + 78c_s^2\omega_4^3\omega_6^2\omega_3 + 42\omega_4^3 v_2^2\omega_6\omega_3^3 + 6\omega_4^2\omega_6\omega_3^3 - 12c_s^2\omega_4^2\omega_6^2\omega_3^3 - 24c_s^2\omega_4^3\omega_6\omega_3^2 + 12\omega_4^2 v_2^2\omega_6^2\omega_3 + 24\omega_4^3 v_2^2\omega_6^2 + 6v_2^2\omega_6^2\omega_3^3 + 6\omega_4^3 v_2^2\omega_6^2\omega_3 - 3\omega_4^3\omega_6^2\omega_3^3 + 6\omega_4^3 v_2^2\omega_3^3 + 42c_s^2\omega_4^3\omega_6^2\omega_3^2 + 12\omega_4^3\omega_6\omega_3^2 - 12\omega_4^3 v_2^2\omega_3^2 + \omega_4^3\omega_6^2\omega_3^3 - 3\omega_4^3\omega_3^3 - 21\omega_4^3\omega_6\omega_3^2 + 6\omega_4^2 v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_4^3\omega_6\omega_3^3 - 36c_s^2\omega_4^3\omega_6^2 - 24c_s^2\omega_4^2\omega_6^2\omega_3 + 6c_s^2\omega_4^3\omega_3^3 - 30\omega_4^3 v_2^2\omega_6^2\omega_3 + 6\omega_4^3\omega_6\omega_3^2 + 6\omega_4^3\omega_3^2 - 12c_s^2\omega_4^3\omega_3^2 + 42c_s^2\omega_4^3\omega_6\omega_3^2 - 12\omega_4^2 v_2^2\omega_6^2\omega_3^3) \frac{v_2 v_3}{6\omega_4^3\omega_6^2\omega_3^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT2}} = C_{D_y^3 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM1}} = (-24\omega_4^3 v_2^2\omega_6\omega_3 - \omega_4^3\omega_6^2\omega_3^3 - 36c_s^2\omega_4^3\omega_6^2\omega_3^2 + 7\omega_4^3\omega_6^2\omega_3^2 + 6c_s^2\omega_4^3\omega_6^2\omega_3^3 + 6c_s^2\omega_4\omega_6^2\omega_3^3 - 12\omega_4 v_2^2\omega_6^2\omega_3^3 - 24c_s^2\omega_4^2\omega_6\omega_3^2 - 6\omega_4^3\omega_6^2\omega_3 - 3\omega_4^2\omega_6\omega_3^3 + 12c_s^2\omega_4^2\omega_6\omega_3^3 + 6\omega_4 v_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_4^2\omega_6^2\omega_3^2 + 36c_s^2\omega_4^3\omega_6^2\omega_3 + 12\omega_4^2 v_2^2\omega_6\omega_3^2 + 6\omega_4^3 v_2^2\omega_6^2\omega_3^2 - 12c_s^2\omega_4^3\omega_6^2\omega_3^2 - 24c_s^2\omega_4^3\omega_6\omega_3^2 + 6v_2^2\omega_6^2\omega_3^3 - 6\omega_4^3 v_2^2\omega_6^2\omega_3^3 - 3\omega_4^3\omega_6^2\omega_3^3 + 36c_s^2\omega_4^2\omega_6^2\omega_3^3 + 12\omega_4^3\omega_6\omega_3^2 + 12\omega_4^3 v_2^2\omega_3^2 + \omega_4^3\omega_6^2\omega_3^3 - 3\omega_4^3\omega_3^3 - 21\omega_4^3\omega_6\omega_3^2 + 6\omega_4^2 v_2^2\omega_6^2\omega_3^3 - 12c_s^2\omega_4^3\omega_6\omega_3^3 - 36c_s^2\omega_4^3\omega_6^2 - 24c_s^2\omega_4^2\omega_6^2\omega_3 + 12c_s^2\omega_4^3\omega_6^2 - 12c_s^2\omega_4^2\omega_6\omega_3^2 + 18c_s^2\omega_4^3\omega_3^3 + 12\omega_4^3 v_2^2\omega_6^2\omega_3 + 6\omega_4^3\omega_6\omega_3^2 + 6\omega_4^3\omega_3^2 - 36c_s^2\omega_4^3\omega_3^2 + 72c_s^2\omega_4^3\omega_6\omega_3^2 - 6\omega_4^2 v_2^2\omega_6^2\omega_3^3) \frac{v_2 v_3}{6\omega_4^3\omega_6^2\omega_3^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM2}} = C_{D_y^3 D_z \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_y^3 D_z v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_2^3 \partial x_3}$:

$$C_{D_y^3 D_z v_2}^{(0), \text{SRT}} = (12 + 18\omega v_2^2 + 8\omega^2 - 18\omega - 12v_2^2 - \omega^3 - 56c_s^2\omega^2 + 3\omega^3 v_2^2 + 4c_s^2\omega^3 + 144c_s^2\omega - 12\omega^2 v_2^2 - 96c_s^2) \frac{v_3 \rho}{12\omega_3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT1}} = (-12\omega_4^3 v_2^2\omega_6\omega_3 - \omega_4^3\omega_6^2\omega_3^3 - 24\omega_4^2 v_2^2\omega_6\omega_3^2 - 32c_s^2\omega_4^3\omega_6^2\omega_3^2 + 3\omega_4^3\omega_6^2\omega_3^2 + 4c_s^2\omega_4^3\omega_6^2\omega_3^3 + 12\omega_4^2 v_2^2\omega_6\omega_3^3 + 6c_s^2\omega_4\omega_6^2\omega_3^3 - 18\omega_4 v_2^2\omega_6^2\omega_3^3 - 24c_s^2\omega_4^2\omega_6\omega_3^2 - 6\omega_4^3\omega_6\omega_3^3 - 12\omega_4^3 v_2^2\omega_6\omega_3^3 + 12c_s^2\omega_4^2\omega_6\omega_3^3 - 12c_s^2\omega_4^3\omega_6^2\omega_3^2 + 36c_s^2\omega_4^3\omega_6^2\omega_3 + 36\omega_4^3 v_2^2\omega_6\omega_3^2 + 12\omega_4^2 v_2^2\omega_6\omega_3^2 - 12c_s^2\omega_4^2\omega_6^2\omega_3^3 - 12c_s^2\omega_4^3\omega_6\omega_3^2 + 24\omega_4^3 v_2^2\omega_6^2 + 12v_2^2\omega_6^2\omega_3^3 - 6\omega_4^3\omega_6^2\omega_3^3 + 6\omega_4^3 v_2^2\omega_3^3 + 48c_s^2\omega_4^2\omega_6^2\omega_3^2 - 12\omega_4^3 v_2^2\omega_3^2 + 2\omega_4^3\omega_6^2\omega_3^3 + 3\omega_4^3 v_2^2\omega_6^2\omega_3^3 - 6\omega_4^3\omega_6\omega_3^3 - 12c_s^2\omega_4^3\omega_6\omega_3^3 - 12c_s^2\omega_4^2\omega_6^2\omega_3^2 - 24c_s^2\omega_4^3\omega_6^2\omega_3 + 6c_s^2\omega_4^3\omega_3^3 - 30\omega_4^3 v_2^2\omega_6^2\omega_3 + 3\omega_4^3\omega_6\omega_3^2 - 12c_s^2\omega_4^3\omega_3^2 + 36c_s^2\omega_4^3\omega_6\omega_3^2 + 12\omega_4^2 v_2^2\omega_6^2\omega_3^3) \frac{v_3 \rho}{12\omega_4^3\omega_6^2\omega_3^3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT2}} = C_{D_y^3 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM1}} = (12\omega_4^3 v_2^2 \omega_6 \omega_3 - \omega_4^3 \omega_6^2 \omega_3^3 - 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 32c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 4c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 6c_s^2 \omega_4 \omega_6^2 \omega_3^3 - 18\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 24c_s^2 \omega_4^2 \omega_6 \omega_3^2 - 6\omega_4^2 \omega_6 \omega_3^3 + 12c_s^2 \omega_4^2 \omega_6 \omega_3^3 - 12c_s^2 \omega_4 \omega_6^2 \omega_3^2 + 36c_s^2 \omega_4^3 \omega_6^2 \omega_3 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 12\omega_4^2 \omega_6 \omega_3^2 - 12c_s^2 \omega_4^2 \omega_6^2 \omega_3^3 - 12c_s^2 \omega_4^3 \omega_6 \omega_3 - 24\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_3^3 + 48c_s^2 \omega_4^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_3^2 + 2\omega_4^2 \omega_6^2 \omega_3^3 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 - 6\omega_4^3 \omega_6 \omega_3^2 - 12c_s^2 \omega_4^3 \omega_6 \omega_3^2 - 12c_s^2 \omega_4^2 \omega_6^2 \omega_3 - 24c_s^2 \omega_4^2 \omega_6^2 \omega_3 + 6c_s^2 \omega_4^3 \omega_3^3 + 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 3\omega_4^3 \omega_6 \omega_3^3 - 12c_s^2 \omega_4^3 \omega_3^2 + 36c_s^2 \omega_4^3 \omega_6 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2) \frac{v_3 \rho}{12\omega_4^2 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM2}} = C_{D_y^3 D_z v_2}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_y^3 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_3^2 \partial x_3^2} :$$

$$C_{D_y^3 D_z v_3}^{(0), \text{SRT}} = (36 + 54\omega v_2^2 + 20\omega^2 - 54\omega - 36v_2^2 - \omega^3 - 56c_s^2 \omega^2 + \omega^3 v_2^2 + 4c_s^2 \omega^3 + 144c_s^2 \omega - 20\omega^2 v_2^2 - 96c_s^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT1}} = (4c_s^2 \omega_6^2 \omega_3^3 - 6\omega_3^3 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 - 44c_s^2 \omega_6^2 \omega_3^2 + 12\omega_3^2 + 11\omega_6^2 \omega_3^2 - 12\omega_6^2 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 + 90c_s^2 \omega_6^2 \omega_3 - 12v_2^2 \omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 + 6v_2^2 \omega_3^3 + v_2^2 \omega_6^2 \omega_3^3 - 12v_2^2 \omega_3^2 + 24\omega_6 \omega_3 - 36c_s^2 \omega_6 \omega_3 - 8v_2^2 \omega_6^2 \omega_3^2 + 6c_s^2 \omega_3^3 + 48c_s^2 \omega_6 \omega_3^2 - 48c_s^2 \omega_6^2 - 36\omega_6 \omega_3^2 - 12c_s^2 \omega_6 \omega_3^3 - 12c_s^2 \omega_3^2 + 9\omega_6 \omega_3^3) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT2}} = C_{D_y^3 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM1}} = (4c_s^2 \omega_6^2 \omega_3^3 - 6\omega_3^3 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 - 26c_s^2 \omega_6^2 \omega_3^2 + 12\omega_3^2 + 11\omega_6^2 \omega_3^2 - 12\omega_6^2 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 + 18c_s^2 \omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 - 6v_2^2 \omega_3^3 + v_2^2 \omega_6^2 \omega_3^3 + 12v_2^2 \omega_3^2 + 24\omega_6 \omega_3 - 36c_s^2 \omega_6 \omega_3 - 14v_2^2 \omega_6^2 \omega_3^2 + 30c_s^2 \omega_3^3 + 96c_s^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3 - 36\omega_6 \omega_3^2 - 30c_s^2 \omega_6 \omega_3^3 - 60c_s^2 \omega_3^2 + 9\omega_6 \omega_3^3) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM2}} = C_{D_y^3 D_z v_3}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t^2 D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} :$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{SRT}} = (-2 - \omega^2 + 3\omega) \frac{3v_3 \rho}{2\omega^3}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{MRT1}} = (-\omega_7^2 \omega_4^2 - 4\omega_4^2 - \omega_7^2 \omega_4 + 2\omega_4^3 - 4\omega_7 \omega_4 + 2\omega_7^2 - 2\omega_7 \omega_4^3 + 8\omega_7 \omega_4^2) \frac{v_3 \rho}{2\omega_7^2 \omega_4^3}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{CLBM1}} = (-2 + 3\omega_4 - \omega_4^2) \frac{3v_3 \rho}{2\omega_4^3}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_t^2 D_z^2 v_3}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_x D_z^2 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} :$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{SRT}} = (\omega^3 v_3^2 + 34c_s^2 \omega^2 - 2c_s^2 \omega^3 - 2\omega^2 v_3^2 - 90c_s^2 \omega + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{MRT1}} = (-12\omega_7^2 \omega_4 v_3^2 - 2c_s^2 \omega_7^2 \omega_4^3 \omega_2 - 18c_s^2 \omega_7^2 \omega_4^2 - 10\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 6c_s^2 \omega_4^3 \omega_2 + 12\omega_7 \omega_4^2 v_3^2 + 12\omega_4^2 \omega_2 v_3^2 + 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 3c_s^2 \omega_7^2 \omega_4^3 + 22c_s^2 \omega_7^2 \omega_4^2 \omega_2 + 12\omega_7 \omega_4 \omega_2 v_3^2 + 12c_s^2 \omega_7 \omega_4 \omega_2 + 12c_s^2 \omega_7^2 \omega_4 + 12c_s^2 \omega_4^2 \omega_2 - 6\omega_7 \omega_4^3 v_3^2 - 30\omega_7 \omega_4^2 \omega_2 v_3^2 - 30c_s^2 \omega_7 \omega_4^2 \omega_2 - 6\omega_4^3 \omega_2 v_3^2 - 24\omega_7^2 \omega_2 v_3^2 + 12c_s^2 \omega_7^2 \omega_2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 - 30c_s^2 \omega_7^2 \omega_4 \omega_2 - \omega_7^2 \omega_4^3 v_3^2 + 36\omega_7^2 \omega_4 \omega_2 v_3^2 - 6c_s^2 \omega_7 \omega_4^3 + 9c_s^2 \omega_7 \omega_4^3 \omega_2 + 6\omega_7^2 \omega_4^2 v_3^2 + 12c_s^2 \omega_7 \omega_4^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{CLBM1}} = (12\omega_7^2 \omega_4 v_3^2 - 2c_s^2 \omega_7^2 \omega_4^3 \omega_2 - 18c_s^2 \omega_7^2 \omega_4^2 + 8\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 6c_s^2 \omega_4^3 \omega_2 - 12\omega_7 \omega_4^2 v_3^2 - 12\omega_4^2 \omega_2 v_3^2 - 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 3c_s^2 \omega_7^2 \omega_4^3 + 22c_s^2 \omega_7^2 \omega_4^2 \omega_2 - 12\omega_7 \omega_4 \omega_2 v_3^2 + 12c_s^2 \omega_7 \omega_4 \omega_2 + 12c_s^2 \omega_7^2 \omega_4 + 12c_s^2 \omega_4^2 \omega_2 + 6\omega_7 \omega_4^3 v_3^2 + 30\omega_7 \omega_4^2 \omega_2 v_3^2 - 30c_s^2 \omega_7 \omega_4^2 \omega_2 + 6\omega_4^3 \omega_2 v_3^2 + 24\omega_7^2 \omega_2 v_3^2 + 12c_s^2 \omega_7^2 \omega_2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 - 30c_s^2 \omega_7^2 \omega_4 \omega_2 - \omega_7^2 \omega_4^3 v_3^2 - 36\omega_7^2 \omega_4 \omega_2 v_3^2 - 6c_s^2 \omega_7 \omega_4^3 + 9c_s^2 \omega_7 \omega_4^3 \omega_2 - 6\omega_7^2 \omega_4^2 v_3^2 + 12c_s^2 \omega_7 \omega_4^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{CLBM2}} = C_{D_t D_x D_z^2 v_1}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_x D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} :$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{MRT}^1} = (24\omega_7\omega_4\omega_2^3 - 12\omega_7\omega_2^3 + 12\omega_4^2\omega_2^2 - 12\omega_7\omega_4\omega_2^2 - 6\omega_4^2\omega_2^2 - 6\omega_4^3\omega_2^2 + 3\omega_4^3\omega_2^3 - 7\omega_7\omega_4^3\omega_2^2 + \omega_7\omega_4^3\omega_2^3 - 6\omega_7\omega_4^2\omega_2 - 6\omega_7\omega_4^3 + 12\omega_7\omega_4^2\omega_2^2 - 10\omega_7\omega_4^3\omega_2^2 + 12\omega_7\omega_4^3\omega_2) \frac{v_3 \rho v_1}{6\omega_7\omega_4^3\omega_2^3}$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_t D_x D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_1 D_x D_z^2 v_3}^{(0), \text{CLBM1}} = (6\omega_4^2\omega_2^2 - 7\omega_4^2\omega_2^3 + 12\omega_4^3\omega_2 - 7\omega_4^3\omega_2^2 + \omega_4^3\omega_2^3 - 6\omega_4^2\omega_2 - 6\omega_4^3 - 12\omega_2^3 + 18\omega_4\omega_2^3) \frac{v_3\rho v_1}{6\omega_4^3\omega_2^3}$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_t D_x D_z^2 v_3}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^2 D_z^2 \rho}^{(0)}$ at $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2}$:

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{SRT}} = (34\omega^2 v_3^2 v_1^2 - c_s^4 \omega^3 + 16c_s^4 + 36c_s^2 \omega v_3^2 + 10c_s^4 \omega^2 - 24c_s^4 \omega + 36c_s^2 \omega v_1^2 - 14c_s^2 \omega^2 v_1^2 + c_s^2 \omega^3 v_3^2 - 24c_s^2 v_3^2 - 3\omega^3 v_3^2 v_1^2 - 14c_s^2 \omega^2 v_3^2 + c_s^2 \omega^3 v_1^2 - 84\omega v_3^2 v_1^2 + 56v_3^2 v_1^2 - 24c_s^2 v_1^2) \frac{1}{4\omega^3}$$

$$C_{D_2^2 D_2^2 \rho}^{(0), \text{MRT1}} = (10c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_3^2 + c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_1^2 + 2\omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_3^2 v_1^2 - 4c_s^2 \omega_7 \omega_4 \omega_5^2 \omega_2^2 v_1^2 - 4c_s^2 \omega_7^2 \omega_5^2 \omega_2^2 v_1^2 + 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 - 2c_s^4 \omega_7 \omega_4^2 \omega_5^2 \omega_2^3 + 2\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 8c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2 v_1^2 - c_s^4 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 + 4c_s^4 \omega_7 \omega_4^2 \omega_5^2 \omega_2^2 - 36\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 v_1^2 + 10c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2 v_1^2 - 3\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 38\omega_7^2 \omega_4^2 \omega_5^2 \omega_2 v_3^2 v_1^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 v_3^2 v_1^2 + 4c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_1^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 v_3^2 v_1^2 + 2c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 v_3^2 - 8c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 v_3^2 - 4c_s^2 \omega_7^2 \omega_3^2 \omega_5^2 v_3^2 + 10c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 v_1^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 v_3^2 v_1^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2 v_3^2 - 3\omega_7^2 \omega_3^2 \omega_5^2 \omega_2 v_3^2 v_1^2 - 2c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_1^2 - 2c_s^4 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 - 3c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_3^2 + 4c_s^4 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_1^2 + 2c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 v_3^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 v_1^2 + 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 + 10\omega_7^2 \omega_3^2 \omega_5 \omega_2^2 v_3^2 v_1^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_3^2 - 2c_s^2 \omega_7^2 \omega_3^2 \omega_5 \omega_2^2 v_1^2 - 2c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^3 + 4c_s^2 \omega_7^2 \omega_3^2 \omega_5^2 \omega_2 v_1^2 + 4c_s^4 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 - 2c_s^4 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2 + 2\omega_7^2 \omega_3^2 \omega_5^2 v_3^2 v_1^2 + 10c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_1^2 + 20\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 + 4c_s^2 \omega_7 \omega_3^2 \omega_5^2 \omega_2^2 v_1^2 - 2c_s^4 \omega_7^2 \omega_3^2 \omega_5^2 \omega_2^2 + c_s^2 \omega_7^2 \omega_3^2 \omega_5^2 v_3^2 + 4c_s^4 \omega_7^2 \omega_1^2 \omega_5^2 \omega_2^2 + 2\omega_7^2 \omega_3^2 \omega_5^2 \omega_2^2 v_3^2 + 12c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 + 20\omega_7^2 \omega_3^2 \omega_5^2 \omega_2^2 v_3^2 v_1^2 - 8c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 38\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 + c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 + 2c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_1^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_1^2 + c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 + 12c_s^4 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 + c_s^4 \omega_7^2 \omega_3^2 \omega_5^2 \omega_2^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 + 4c_s^4 \omega_7^2 \omega_1^2 \omega_5^2 \omega_2^2 - 2c_s^2 \omega_7^2 \omega_3^2 \omega_5^2 \omega_2^3 v_3^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_1^2 - 8c_s^2 \omega_7^2 \omega_3^2 \omega_5^2 \omega_2^2 v_3^2 + c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_1^2 - 3\omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_3^2 v_1^2 + 20\omega_7^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5 \omega_2^2 v_3^2 + 20\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 2c_s^2 \omega_7^2 \omega_3^2 \omega_5 \omega_2^2 + 2\omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 + 10\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 + 12c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_1^2 - 4c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 + 20\omega_7^2 \omega_3^2 \omega_5^2 \omega_2^3 v_3^2 v_1^2 - 3c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_1^2 - 2c_s^2 \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2) \frac{1}{4\omega_7^2 \omega_3^2 \omega_5^2 \omega_2^3}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT2}} = C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$\begin{aligned} C(0, \text{CLB}M1) = & \frac{1}{D_x^2 D_y^2 \rho} = \\ & (10c_s^2 w_4^2 w_5 w_2^2 v_3^2 - c_s^2 w_2^2 w_5 w_3^2 v_1^2 - 2w_2^2 w_4^2 w_5 w_3^2 v_3^2 v_1^2 - 4c_s^2 w_7 w_4 w_2^2 w_3^2 v_1^2 - 4c_s^2 w_7^2 w_2^2 w_5^2 v_1^2 + 4c_s^4 w_2^2 w_3^2 w_5^2 w_2^2 - 2c_s^4 w_7 w_4^2 w_5^2 w_3^2 + 2c_s^2 w_3^2 w_5^2 w_2^2 v_1^2 + \\ & 12w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - c_s^4 w_2^2 w_3^2 w_5^2 w_2^2 + 4c_s^4 w_7 w_4^2 w_5^2 w_3^2 - 28w_2^2 w_3^2 w_5^2 w_2^2 v_3^2 v_1^2 + 10c_s^2 w_7^2 w_2^2 w_5^2 w_3^2 + 3w_7 w_4^2 w_5^2 w_3^2 v_3^2 v_1^2 - 14w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 + \\ & 4w_2^2 w_4^2 w_5^2 v_3^2 v_1^2 - 4c_s^2 w_7^2 w_2^2 w_5^2 w_3^2 v_1^2 + 4w_2^2 w_5^2 w_3^2 v_3^2 v_1^2 + 2c_s^2 w_7^2 w_4^2 w_5^2 w_3^2 v_3^2 - 4c_s^2 w_7^2 w_4^2 w_5^2 w_3^2 v_3^2 + 10c_s^2 w_7^2 w_4^2 w_5^2 w_3^2 v_1^2 + 4w_7 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - 4c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 - \\ & 3w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 + 2c_s^2 w_2^2 w_3^2 w_5^2 w_2^2 v_1^2 - 2c_s^4 w_2^2 w_4^2 w_5^2 w_3^2 - 3c_s^2 w_2^2 w_3^2 w_5^2 w_2^2 v_3^2 + 4c_s^4 w_2^2 w_4^2 w_5^2 w_2^2 - 4c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_1^2 + 2c_s^2 w_2^2 w_3^2 w_5^2 w_3^2 v_3^2 - 4c_s^2 w_2^2 w_3^2 w_5^2 w_3^2 v_1^2 - \\ & 10w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - 4c_s^2 w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 + 2c_s^2 w_7^2 w_2^2 w_5^2 w_3^2 v_1^2 - 2c_s^4 w_2^2 w_4^2 w_5^2 w_3^2 + 4c_s^4 w_2^2 w_4^2 w_5^2 w_2^2 - 2c_s^2 w_7^2 w_3^2 w_5^2 w_2^2 - 2w_2^2 w_3^2 w_5^2 v_3^2 v_1^2 + 10c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_1^2 + \\ & 14w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - 4c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_1^2 - 2c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 - 2c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 + 4c_s^4 w_7^2 w_2^2 w_5^2 w_3^2 - 2w_7 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 + \\ & 8c_s^2 w_7^2 w_2^2 w_5^2 w_2^2 v_3^2 + 4w_7^2 w_3^2 w_5^2 w_2^2 v_3^2 v_1^2 - 8c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_1^2 - 14w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - c_s^2 w_7^2 w_3^2 w_5^2 w_2^2 v_3^2 + 2c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_1^2 + 4w_7^2 w_3^2 w_5^2 w_2^2 v_3^2 v_1^2 + \\ & c_s^4 w_7 w_4^2 w_5^2 w_3^2 - 12c_s^4 w_2^2 w_4^2 w_5^2 w_2^2 + 4w_2^2 w_4^2 w_5^2 w_3^2 v_3^2 v_1^2 + c_s^4 w_2^2 w_4^2 w_5^2 w_3^2 + 4w_7 w_4^2 w_5^2 w_3^2 v_3^2 v_1^2 + 4c_s^4 w_2^2 w_4^2 w_5^2 w_2^2 + 2c_s^2 w_7^2 w_4^2 w_5^2 w_3^2 v_3^2 - 4c_s^2 w_7^2 w_3^2 w_5^2 w_2^2 v_1^2 - \\ & 8c_s^2 w_7^2 w_3^2 w_5^2 w_2^2 v_3^2 + c_s^2 w_7^2 w_3^2 w_5^2 w_2^2 v_1^2 + 3w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 + 4w_2^2 w_5^2 w_3^2 v_3^2 v_1^2 - 4c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 + 12w_2^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - 2c_s^4 w_7^2 w_4^2 w_5^2 w_2^2 - 2w_4^2 w_5^2 w_3^2 v_3^2 v_1^2 - \\ & 4c_s^2 w_7^2 w_4^2 w_5^2 v_3^2 - 10w_7 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 + 8c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_1^2 - 2c_s^2 w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 + 14w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 v_1^2 - 3c_s^2 w_7 w_4^2 w_5^2 w_2^2 v_1^2 + 2c_s^2 w_7 w_4^2 w_5^2 w_2^2 v_3^2) \frac{1}{4w_2^2 w_3^2 w_5^2 w_3^2} \end{aligned}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{CLBM2}} = C_{D_x^2 D_z^2 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_x^2 D_z^2 v_1}^{(0)}$ at $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2}$:

$$C_{\text{D}_2^2\text{D}_2^2v_1}^{(0),\text{SRT}} = (-126\omega v_3^2 + 84v_3^2 - 4\omega^3 v_3^2 - 26c_s^2\omega^2 + c_s^2\omega^3 + 50\omega^2 v_3^2 + 72c_s^2\omega - 48c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$\begin{aligned} \mathcal{D}_{\mathbb{C}_2^3 \mathbb{D}_2^2 v_1}^{(0), \text{MRT}1} = & (-4\omega_7^2 \omega_3^3 \omega_2^3 v_3^2 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_2 - 14c_s^2 \omega_7^2 \omega_4^2 \omega_2^2 + 24\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 12c_s^2 \omega_4^4 \omega_2^3 + 24\omega_7^2 \omega_4 \omega_2^3 v_3^2 + 6\omega_4^3 \omega_2^3 v_3^2 + 48\omega_7^2 \omega_2^3 v_3^2 + 12c_s^2 \omega_7^2 \omega_4^2 \omega_2^2 - \\ & 12c_s^2 \omega_7 \omega_4 \omega_2^3 + 24\omega_7 \omega_4^2 \omega_2^3 v_3^2 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_2 + 22\omega_7^2 \omega_4^3 \omega_2^2 v_3^2 + c_s^2 \omega_7^2 \omega_3^3 \omega_2^2 - 6c_s^2 \omega_7^2 \omega_4^3 \omega_2^2 - 78\omega_7^2 \omega_4 \omega_2^3 v_3^2 + 6c_s^2 \omega_3^3 \omega_2^3 - 6c_s^2 \omega_7 \omega_3^3 \omega_2^2 - 6\omega_7 \omega_4^3 \omega_2^3 v_3^2 - \\ & 12\omega_4^2 \omega_2^3 v_3^2 + 34\omega_7^2 \omega_4^2 \omega_2^3 v_3^2 - 30\omega_7^2 \omega_4^2 \omega_2^2 v_3^2 + 12\omega_7^2 \omega_4^3 v_3^2 + 24c_s^2 \omega_7 \omega_4^2 \omega_2^3 + 24c_s^2 \omega_7^2 \omega_4 \omega_2^3 - 12\omega_7 \omega_4 \omega_2^3 v_3^2 - 12c_s^2 \omega_7^2 \omega_2^3 - 48\omega_7^2 \omega_4^2 \omega_2^3 v_3^2) \frac{\nu v}{12\omega_7^2 \omega_3^3 \omega_2^3} \end{aligned}$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_2^2 D_2^2 v_1}^{(0), \text{CLB} \text{M1}} = (-4\omega_7^2 \omega_4^3 \omega_2^3 v_3^2 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_2 - 14c_s^2 \omega_7^2 \omega_4^2 \omega_2^3 + 24\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 12c_s^2 \omega_4^2 \omega_2^3 + 24\omega_7^2 \omega_4 \omega_2^2 v_3^2 - 6\omega_4^3 \omega_2^3 v_3^2 + 12c_s^2 \omega_7^2 \omega_4^2 \omega_2^2 -$$

$$12c_s^2\omega_7\omega_4\omega_2^3 - 24\omega_7\omega_4^2\omega_2^3v_3^2 - 12c_s^2\omega_7^2\omega_2^2\omega_2 + 22\omega_7^2\omega_4^3\omega_2^3v_3^2 + c_s^2\omega_7^2\omega_4^3\omega_2^3 - 6c_s^2\omega_7^2\omega_4^3\omega_2^3 - 18\omega_7^2\omega_4\omega_2^3v_3^2 + 6c_s^2\omega_4^3\omega_2^3 - 6c_s^2\omega_7\omega_4^3\omega_2^3 + 6\omega_7\omega_4^3\omega_2^3v_3^2 + 12\omega_4^3\omega_2^3v_3^2 + 22\omega_7^2\omega_4^3\omega_2^3v_3^2 - 30\omega_7^2\omega_4^3\omega_2^3v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 24c_s^2\omega_7\omega_4^3\omega_2^3 + 24c_s^2\omega_7^2\omega_4\omega_2^3 + 12\omega_7\omega_4\omega_2^3v_3^2 - 12c_s^2\omega_7^2\omega_2^3 - 48\omega_7^2\omega_4^3\omega_2^3v_3^2) \frac{\rho v_1}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{CLBM2}} = C_{D_x^2 D_z^2 v_1}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x^2 D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} :$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{SRT}} = (84v_1^2 - 126\omega v_1^2 + 50\omega^2 v_1^2 - 26c_s^2\omega^2 + c_s^2\omega^3 - 4\omega^3 v_1^2 + 72c_s^2\omega - 48c_s^2) \frac{v_3\rho}{12\omega^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT1}} = (-12c_s^2\omega_4\omega_5^2\omega_2^2 + 24c_s^2\omega_4^3\omega_5^2\omega_2 - 12\omega_4^3\omega_5\omega_2v_1^2 + 22\omega_4^2\omega_5^2\omega_2^3v_1^2 + 34\omega_4^3\omega_5^2\omega_2^3v_1^2 + 6c_s^2\omega_4\omega_5^2\omega_2^3 - 12c_s^2\omega_4^3\omega_5^2 - 12\omega_4^3\omega_5^2v_1^2 - 48\omega_4^2\omega_5^2\omega_2^3v_1^2 - 12c_s^2\omega_4^3\omega_2^2 + 12\omega_5^2\omega_2^3v_1^2 + c_s^2\omega_4^3\omega_5^2\omega_2^3 + 6\omega_4^3\omega_2^3v_1^2 - 14c_s^2\omega_4^3\omega_5^2\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 - 4\omega_4^3\omega_5^2\omega_2^3v_1^2 - 30\omega_4\omega_5^2\omega_2^3v_1^2 + 24c_s^2\omega_4^3\omega_5\omega_2^2 + 24\omega_4^2\omega_5^2\omega_2v_1^2 - 6c_s^2\omega_4^3\omega_5\omega_2^2 - 6\omega_4^3\omega_5\omega_2^3v_1^2 - 78\omega_4^3\omega_5^2\omega_2v_1^2 + 12c_s^2\omega_4^3\omega_5^2\omega_2^2 + 24\omega_4\omega_5^2\omega_2^3v_1^2 - 6c_s^2\omega_4^3\omega_5^2\omega_2^3 + 24\omega_4^3\omega_5\omega_2^3v_1^2 - 12c_s^2\omega_4^3\omega_5\omega_2 + 48\omega_4^3\omega_5^2v_1^2) \frac{\rho v_1}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM1}} = (-12c_s^2\omega_4\omega_5^2\omega_2^2 + 24c_s^2\omega_4^3\omega_5^2\omega_2 + 12\omega_4^3\omega_5\omega_2v_1^2 + 22\omega_4^2\omega_5^2\omega_2^3v_1^2 + 22\omega_4^3\omega_5^2\omega_2^3v_1^2 + 6c_s^2\omega_4\omega_5^2\omega_2^3 - 12c_s^2\omega_4^3\omega_5^2 + 12\omega_4^3\omega_5^2v_1^2 - 48\omega_4^2\omega_5^2\omega_2^3v_1^2 - 12c_s^2\omega_4^3\omega_2^2 + 12\omega_5^2\omega_2^3v_1^2 + c_s^2\omega_4^3\omega_5^2\omega_2^3 - 6\omega_4^3\omega_2^3v_1^2 - 14c_s^2\omega_4^3\omega_5^2\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 - 4\omega_4^3\omega_5^2\omega_2^3v_1^2 - 30\omega_4\omega_5^2\omega_2^3v_1^2 + 24c_s^2\omega_4^3\omega_5\omega_2^2 + 24\omega_4^2\omega_5^2\omega_2v_1^2 - 6c_s^2\omega_4^3\omega_5\omega_2^2 + 6\omega_4^3\omega_5\omega_2^3v_1^2 - 18\omega_4^3\omega_5^2\omega_2v_1^2 + 12c_s^2\omega_4^3\omega_5^2\omega_2^2 + 24\omega_4\omega_5^2\omega_2^3v_1^2 - 6c_s^2\omega_4^3\omega_5^2\omega_2^3 + 24\omega_4^3\omega_5\omega_2^3v_1^2 - 12c_s^2\omega_4^3\omega_5\omega_2 + 48\omega_4^3\omega_5^2v_1^2) \frac{v_3\rho}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_y D_z^2 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} :$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{SRT}} = (\omega^3 v_3^2 + 34c_s^2\omega^2 - 2c_s^2\omega^3 - 2\omega^2 v_3^2 - 90c_s^2\omega + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{MRT1}} = (12c_s^2\omega_7^2\omega_3 - 30c_s^2\omega_7^2\omega_4\omega_3 - 12\omega_7^2\omega_4v_3^2 - 10\omega_7^2\omega_1^2v_3^2\omega_3 - 18c_s^2\omega_7^2\omega_4^2 + 12\omega_7\omega_4^2v_3^2 - 30c_s^2\omega_7\omega_4^2\omega_3 + 3c_s^2\omega_7^2\omega_4^3 + 12\omega_4^2v_3^2\omega_3 + 9\omega_7\omega_4^3v_3^2\omega_3 + 12\omega_7\omega_4v_3^2\omega_3 + 12c_s^2\omega_7^2\omega_4 + 9c_s^2\omega_7\omega_4^3\omega_3 - 6\omega_7\omega_4^3v_3^2 - 6c_s^2\omega_4^3\omega_3 - 30\omega_7\omega_4^2v_3^2\omega_3 - 24\omega_7^2v_3^2\omega_3 - 6\omega_4^3v_3^2\omega_3 + \omega_7^2\omega_4^3v_3^2\omega_3 - 2c_s^2\omega_7^2\omega_4^3\omega_3 - \omega_7^2\omega_4^3v_3^2 + 12c_s^2\omega_7\omega_4\omega_3 + 12c_s^2\omega_4^2\omega_3 + 36\omega_7^2\omega_4v_3^2\omega_3 - 6c_s^2\omega_7\omega_4^3 + 6\omega_7^2\omega_4^2v_3^2 + 22c_s^2\omega_7^2\omega_4^2\omega_3 + 12c_s^2\omega_7\omega_4^2) \frac{\rho}{12\omega_7^2\omega_4^3\omega_3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{MRT2}} = C_{D_t D_y D_z^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{CLBM1}} = (12c_s^2\omega_7^2\omega_3 - 30c_s^2\omega_7^2\omega_4\omega_3 + 12\omega_7^2\omega_4v_3^2 + 8\omega_7^2\omega_4^2v_3^2\omega_3 - 18c_s^2\omega_7^2\omega_4^2 - 12\omega_7\omega_4^2v_3^2 - 30c_s^2\omega_7\omega_4^2\omega_3 + 3c_s^2\omega_7^2\omega_4^3 - 12\omega_4^2v_3^2\omega_3 - 9\omega_7\omega_4^3v_3^2\omega_3 - 12\omega_7\omega_4v_3^2\omega_3 + 12c_s^2\omega_7^2\omega_4 + 9c_s^2\omega_7\omega_4^3\omega_3 + 6\omega_7\omega_4^3v_3^2 - 6c_s^2\omega_4^3\omega_3 + 30\omega_7\omega_4^2v_3^2\omega_3 + 24\omega_7^2v_3^2\omega_3 + 6\omega_4^3v_3^2\omega_3 + \omega_7^2\omega_4^3v_3^2\omega_3 - 2c_s^2\omega_7^2\omega_4^3\omega_3 - \omega_7^2\omega_4^3v_3^2 + 12c_s^2\omega_7\omega_4\omega_3 + 12c_s^2\omega_4^2\omega_3 - 36\omega_7^2\omega_4v_3^2\omega_3 - 6c_s^2\omega_7\omega_4^3 - 6\omega_7^2\omega_4^2v_3^2 + 22c_s^2\omega_7^2\omega_4^2\omega_3 + 12c_s^2\omega_7\omega_4^2) \frac{\rho}{12\omega_7^2\omega_4^3\omega_3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{CLBM2}} = C_{D_t D_y D_z^2 v_2}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_t D_y D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} :$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{SRT}} = (-24 - 14\omega^2 + 36\omega + \omega^3) \frac{v_2 v_3 \rho}{6\omega^3}$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{MRT1}} = (\omega_7\omega_4^3\omega_3^3 - 6\omega_7\omega_4^2\omega_3 - 7\omega_7\omega_4^3\omega_3^2 - 10\omega_7\omega_4^2\omega_3^3 + 12\omega_7\omega_4^3\omega_3 + 12\omega_7\omega_4^2\omega_3^2 - 12\omega_7\omega_4\omega_3^2 - 6\omega_4^3\omega_3^3 - 12\omega_7\omega_3^3 + 24\omega_7\omega_4\omega_3^3 + 12\omega_4^3\omega_3^3 - 6\omega_7\omega_4^3 + 3\omega_4^3\omega_3^3 - 6\omega_4^3\omega_3^2) \frac{v_2 v_3 \rho}{6\omega_7\omega_4^3\omega_3^3}$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_t D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{CLBM1}} = (-12\omega^3 - 6\omega^4 + 18\omega_4\omega^3 - 7\omega_4^3\omega^3 + 12\omega_4^3\omega_3 + 6\omega_4^2\omega_3^2 + \omega_4^3\omega_3^3 - 6\omega_4^2\omega_3 - 7\omega_4^3\omega_3^2) \frac{v_2 v_3 \rho}{6\omega_4^3\omega_3^3}$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_t D_y D_z^2 v_3}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x D_y D_z^2 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} :$$

$$C_{\text{D}_x \text{D}_y \text{D}_z^2 \rho}^{(0), \text{SRT}} = (-60\omega v_3^2 + 40v_3^2 - 2\omega^3 v_3^2 - 12c_s^2 \omega^2 + c_s^2 \omega^3 + 24\omega^2 v_3^2 + 30c_s^2 \omega - 20c_s^2) \frac{v_2 v_1}{\omega^3}$$

$$C_{D_x D_y D_z^2 \rho}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 \rho}^{(0), \text{CLBM2}} = C_{D_x D_y D_z^2 \rho}^{(0), \text{CLBM1}}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM2}} = C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM1}}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}}$$

$$36c_s^2\omega_7^2\omega_4\omega_2^3 + 12\omega_7\omega_4\omega_2^3v_3^2 - 24c_s^2\omega_7\omega_4^2\omega_2^2 - 12c_s^2\omega_7^2\omega_2^3 - 36\omega_7^2\omega_4^2\omega_2^2v_3^2) \frac{\rho v_1}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM2}} = C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_x D_y D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} :$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{SRT}} = (132 + 76\omega^2 - 198\omega - 5\omega^3) \frac{v_2 v_3 \rho v_1}{6\omega^3}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}} = (-30\omega_4^3\omega_2^3\omega_3 + 24\omega_4^3\omega_2^2\omega_3^3 + 18\omega_4\omega_2^3\omega_3^2 - 36\omega_4\omega_2^2\omega_3^3 - 42\omega_4^3\omega_2^2\omega_3^2 + 12\omega_2^3\omega_3^3 + 6\omega_4^2\omega_2\omega_3^3 + 18\omega_4^3\omega_2\omega_3 - 5\omega_4^3\omega_2^3\omega_3^3 + 12\omega_4^3\omega_2^3 + 24\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4\omega_2^3\omega_3^3 + 12\omega_4^2\omega_2^2\omega_3^2 - 30\omega_4^2\omega_2^2\omega_3^3 + 6\omega_4^3\omega_2^2\omega_3 + 12\omega_4^3\omega_2^3 - 30\omega_4^2\omega_2^2\omega_3^2 + 18\omega_4^3\omega_2\omega_3^2 - 30\omega_4^3\omega_2\omega_3^3 + 28\omega_4^2\omega_2^3\omega_3^3) \frac{v_2 v_3 \rho v_1}{6\omega_4^3\omega_2^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$\text{coefficient } C_{D_y D_z^2 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y D_z^2 \rho}^{(0), \text{SRT}} = (36c_s^2\omega v_2^2 + 34\omega^2 v_2^2 v_3^2 - c_s^4\omega^3 + 16c_s^4 + 36c_s^2\omega v_3^2 + 10c_s^4\omega^2 - 24c_s^4\omega - 24c_s^2 v_2^2 + c_s^2\omega^3 v_3^2 - 24c_s^2 v_3^2 - 3\omega^3 v_2^2 v_3^2 + c_s^2\omega^3 v_2^2 - 14c_s^2\omega^2 v_3^2 - 84\omega^2 v_2^2 v_3^2 - 14c_s^2\omega^2 v_2^2 + 56v_2^2 v_3^2) \frac{1}{4\omega^3}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{MRT1}} = (-3\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^3 - 38\omega_7^2\omega_4 v_2^2 v_3^2 \omega_6^2 \omega_3^3 + c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 4c_s^4\omega_7^2\omega_4 \omega_6^2 \omega_3^2 + 2c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 36\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^4\omega_7^2\omega_4^3 \omega_6 \omega_3^3 + 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^3 - 2c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^2 - 4\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_3^2 + 20\omega_7^2\omega_4 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 + 10\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 - 4c_s^4\omega_7^2\omega_4^3 \omega_6 \omega_3^2 - 3c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 2c_s^4\omega_7^2\omega_4 \omega_6^2 \omega_3^3 + 20\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 - 8c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 20\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^3 + 2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^3 + 4c_s^4\omega_7\omega_4^2 \omega_6^2 \omega_3^2 - 8c_s^2\omega_7^2\omega_4 v_3^2 \omega_6^2 \omega_3^2 - c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^3 + 12c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 20\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^3 + 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 + 10c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 10c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 + 10\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 - 4\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 20\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 - 8c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 2c_s^4\omega_7\omega_4^3 \omega_6^2 \omega_3^3 - 4\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 + 4c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^2 - 4\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 3c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 3\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 4\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 + c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 + c_s^4\omega_7^2\omega_4^3 \omega_6 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_3^2 + 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 2\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + c_s^2\omega_7\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 + 4c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3 - 8c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 38\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3 + 10c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 2c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 20\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 2c_s^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 2\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 12c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 12c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^2 + c_s^4\omega_7\omega_4^3 \omega_6^2 \omega_3^2 - 3\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 + c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 4c_s^2\omega_7\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 + 4c_s^4\omega_7^2\omega_4 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^4\omega_7\omega_4^3 \omega_6^2 \omega_3^2 - 4\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 10c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2) \frac{1}{4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{MRT2}} = C_{D_y D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{CLBM1}} = (3\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^3 - 14\omega_7^2\omega_4 v_2^2 v_3^2 \omega_6^2 \omega_3^3 + c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 4c_s^4\omega_7^2\omega_4 \omega_6^2 \omega_3^2 + 2c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 28\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^4\omega_7^2\omega_4^3 \omega_6 \omega_3^3 + 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^3 - 2c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^2 + 4\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_3^2 + 12\omega_7^2\omega_4 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 + 10\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 - 2\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 4c_s^4\omega_7\omega_4^2 \omega_6^2 \omega_3^2 - c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^3 + 8c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 4\omega_7^2 v_2^2 v_3^2 \omega_6^2 \omega_3^2 + 10c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 10c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 10\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 4\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 12\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 8c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 2c_s^4\omega_7\omega_4^3 \omega_6^2 \omega_3^2 + 4\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 + 4c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^2 + 4\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 3c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 4c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_7\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 8c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 14\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 + 10c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 + 2c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 14\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 2c_s^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 4c_s^2\omega_7\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 8c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12c_s^4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^2 + c_s^4\omega_7\omega_4^3 \omega_6^2 \omega_3^2 - 3\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6^2 \omega_3^2 - c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 4c_s^2\omega_7\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 + 4c_s^4\omega_7^2\omega_4 \omega_6^2 \omega_3^2 - 2c_s^2\omega_7^2\omega_4^3 v_3^2 \omega_6^2 \omega_3^2 - 2c_s^4\omega_7\omega_4^3 \omega_6^2 \omega_3^2 + 4\omega_7^2\omega_4^3 v_2^2 v_3^2 \omega_6 \omega_3^2 + 10c_s^2\omega_7^2\omega_4^3 v_2^2 \omega_6^2 \omega_3^2) \frac{1}{4\omega_7^2\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{CLBM2}} = C_{D_y D_z^2 \rho}^{(0), \text{CLBM1}}$$

$$\text{coefficient } C_{D_y D_z^2 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y D_z^2 v_2}^{(0), \text{SRT}} = (-126\omega v_2^3 + 84v_2^3 - 4\omega^3 v_3^2 - 26c_s^2\omega^2 + c_s^2\omega^3 + 50\omega^2 v_3^2 + 72c_s^2\omega - 48c_s^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT}^1} = (24\omega_7^2 \omega_2^2 v_3 \omega_3 - 12\omega_7 \omega_4 v_3^2 \omega_3^3 - 6c_s^2 \omega_7 \omega_4 \omega_3^3 + 34\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 24c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_3^3 - 6\omega_7 \omega_4^3 v_3^2 \omega_3^3 - 48\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 - 12\omega_4^2 v_3^2 \omega_3^3 + 24c_s^2 \omega_7 \omega_4^3 \omega_3^3 - 78\omega_7^2 \omega_4 v_3^2 \omega_3^3 - 12c_s^2 \omega_4^2 \omega_3^3 + 12c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7 \omega_4 \omega_3^3 - 30\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 24\omega_7^2 \omega_4 v_3^2 \omega_3^3 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 + 12\omega_7^2 \omega_4^3 \omega_3^3 - 14c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 6c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 + 6\omega_4^3 v_3^2 \omega_3^3 + 48\omega_7^2 v_3^2 \omega_3^3 + 22\omega_7^2 \omega_4^3 v_3^2 \omega_3^3 + 24\omega_7 \omega_4^2 v_3^2 \omega_3^3 + 6c_s^2 \omega_4^3 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 + c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 - 4\omega_7^2 \omega_4^3 v_3^2 \omega_3^3) \frac{v_2 \rho}{12\omega_7^2 \omega_4^3 \omega_3^3}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT}^2} = C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT}^1}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM}^1} = (24\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 12\omega_7 \omega_4 v_3^2 \omega_3^3 - 6c_s^2 \omega_7 \omega_4^3 \omega_3^3 + 22\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 24c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_3^3 + 6\omega_7 \omega_4^3 v_3^2 \omega_3^3 - 48\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 12\omega_4^2 v_3^2 \omega_3^3 + 24c_s^2 \omega_7 \omega_4^3 \omega_3^3 - 18\omega_7^2 \omega_4 v_3^2 \omega_3^3 - 12c_s^2 \omega_4^2 \omega_3^3 + 12c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7 \omega_4 \omega_3^3 - 30\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 24\omega_7^2 \omega_4 v_3^2 \omega_3^3 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 + 12\omega_7^2 \omega_4^3 \omega_3^3 - 14c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 6c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 - 6\omega_4^3 v_3^2 \omega_3^3 + 22\omega_7^2 \omega_4^3 v_3^2 \omega_3^3 - 24\omega_7 \omega_4^2 v_3^2 \omega_3^3 + 6c_s^2 \omega_4^3 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 + c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 - 4\omega_7^2 \omega_4^3 v_3^2 \omega_3^3) \frac{v_2 \rho}{12\omega_7^2 \omega_4^3 \omega_3^3}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM}^2} = C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{D_y^2 D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{SRT}} = (-126\omega v_2^2 + 84v_2^2 - 26c_s^2 \omega^2 - 4\omega^3 v_2^2 + c_s^2 \omega^3 + 72c_s^2 \omega + 50\omega^2 v_2^2 - 48c_s^2) \frac{v_3 \rho}{12\omega^3}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT}^1} = (-12\omega_4^3 v_2^2 \omega_6 \omega_3 - 14c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 + c_s^2 \omega_4^3 \omega_6 \omega_3^3 + 6c_s^2 \omega_4 \omega_6^2 \omega_3^3 - 30\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 6\omega_4^3 v_2^2 \omega_6 \omega_3^3 + 24\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 12c_s^2 \omega_4 \omega_6^2 \omega_3^2 + 24c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 + 24\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 6c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 - 12c_s^2 \omega_4^3 \omega_6 \omega_3^2 + 24\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 48\omega_4^3 v_2^2 \omega_6^2 + 12v_2^2 \omega_6^2 \omega_3^3 + 34\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4^3 v_2^2 \omega_3^3 + 12c_s^2 \omega_4^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_3^2 - 4\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 22\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 6c_s^2 \omega_4^3 \omega_6 \omega_3^2 - 12c_s^2 \omega_4^3 \omega_6^2 + 6c_s^2 \omega_4^3 \omega_3^3 - 78\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12c_s^2 \omega_4^3 \omega_3^2 + 24c_s^2 \omega_4^3 \omega_6 \omega_3^2 - 48\omega_4^3 v_2^2 \omega_6^2 \omega_3^2) \frac{v_3 \rho}{12\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT}^2} = C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT}^1}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM}^1} = (12\omega_4^3 v_2^2 \omega_6 \omega_3 - 14c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 + c_s^2 \omega_4^3 \omega_6 \omega_3^3 + 6c_s^2 \omega_4 \omega_6^2 \omega_3^3 - 30\omega_4 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_4^3 v_2^2 \omega_6 \omega_3^3 + 24\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 12c_s^2 \omega_4 \omega_6^2 \omega_3^2 + 24c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 - 24\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 6c_s^2 \omega_4^3 \omega_6^2 \omega_3^2 - 12c_s^2 \omega_4^3 \omega_6 \omega_3^2 + 24\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^3 + 22\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_3^3 + 12c_s^2 \omega_4^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_3^2 - 4\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 22\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 6c_s^2 \omega_4^3 \omega_6 \omega_3^2 - 12c_s^2 \omega_4^3 \omega_6^2 + 6c_s^2 \omega_4^3 \omega_3^3 - 18\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12c_s^2 \omega_4^3 \omega_3^2 + 24c_s^2 \omega_4^3 \omega_6 \omega_3^2 - 48\omega_4^3 v_2^2 \omega_6^2 \omega_3^2) \frac{v_3 \rho}{12\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM}^2} = C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{D_t D_z^3 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial t \partial x_3^3} :$$

$$C_{D_t D_z^3 v_3}^{(0), \text{SRT}} = (-36 - 108\omega v_3^2 - 20\omega^2 + 54\omega + \omega^3 + 72v_3^2 - 3\omega^3 v_3^2 + 34c_s^2 \omega^2 - 2c_s^2 \omega^3 + 42\omega^2 v_3^2 - 90c_s^2 \omega + 60c_s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_z^3 v_3}^{(0), \text{MRT}^1} = (-11\omega_7^2 \omega_4^2 - 42\omega_7^2 \omega_4 v_3^2 + 25c_s^2 \omega_7^2 \omega_4^2 + \omega_7^2 \omega_4^3 - 60\omega_7 \omega_4^2 v_3^2 + 12\omega_7^2 v_3^2 - 2c_s^2 \omega_7^2 \omega_4^3 - 12\omega_4^2 + 24c_s^2 \omega_7^2 - 48c_s^2 \omega_7^2 \omega_4 + 12\omega_7^2 \omega_4 + 6\omega_4^3 + 15\omega_7 \omega_4^3 v_3^2 + 24c_s^2 \omega_7 \omega_4 + 12c_s^2 \omega_4^2 - 24\omega_7 \omega_4 - 6c_s^2 \omega_4^3 - 6\omega_4^3 v_3^2 - 3\omega_7^2 \omega_4^3 v_3^2 - 9\omega_7 \omega_4^3 + 48\omega_7 \omega_4 v_3^2 + 9c_s^2 \omega_7 \omega_4^3 + 27\omega_7^2 \omega_4^2 v_3^2 + 36\omega_7 \omega_4^2 - 36c_s^2 \omega_7 \omega_4^2 + 12\omega_4^2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3}$$

$$C_{D_t D_z^3 v_3}^{(0), \text{MRT}^2} = C_{D_t D_z^3 v_3}^{(0), \text{MRT}^1}$$

$$C_{D_t D_z^3 v_3}^{(0), \text{CLBM}^1} = (-11\omega_7^2 \omega_4^2 + 18\omega_7^2 \omega_4 v_3^2 + 25c_s^2 \omega_7^2 \omega_4^2 + \omega_7^2 \omega_4^3 - 108\omega_7 \omega_4^2 v_3^2 - 36\omega_7^2 v_3^2 - 2c_s^2 \omega_7^2 \omega_4^3 - 12\omega_4^2 + 24c_s^2 \omega_7^2 - 48c_s^2 \omega_7^2 \omega_4 + 12\omega_7^2 \omega_4 + 6\omega_4^3 + 27\omega_7 \omega_4^3 v_3^2 + 24c_s^2 \omega_7 \omega_4 + 12c_s^2 \omega_4^2 - 24\omega_7 \omega_4 - 6c_s^2 \omega_4^3 - 18\omega_4^3 v_3^2 - 3\omega_7^2 \omega_4^3 v_3^2 - 9\omega_7 \omega_4^3 + 72\omega_7 \omega_4 v_3^2 + 9c_s^2 \omega_7 \omega_4^3 + 15\omega_7^2 \omega_4^2 v_3^2 + 36\omega_7 \omega_4^2 - 36c_s^2 \omega_7 \omega_4^2 + 36\omega_4^2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3}$$

$$C_{D_t D_z^3 v_3}^{(0), \text{CLBM}^2} = C_{D_t D_z^3 v_3}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{D_x D_z^3 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 \rho}^{(0), \text{SRT}} = (24 + 14\omega^2 - 36\omega - \omega^3 - 72c_s^2 \omega^2 + 6c_s^2 \omega^3 + 180c_s^2 \omega - 120c_s^2) \frac{v_3 v_1}{6\omega^3}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT}^1} = (-3\omega_7^2 \omega_4^2 \omega_2^2 + 12\omega_7 \omega_4 \omega_3^2 + 6c_s^2 \omega_7^2 \omega_4^2 \omega_2 - 48c_s^2 \omega_7^2 \omega_4^2 \omega_3^2 + 6\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 12c_s^2 \omega_4^2 \omega_2^3 + 7\omega_7^2 \omega_4^2 \omega_2^3 + 12\omega_7^2 \omega_4 \omega_2^2 v_3^2 + 6\omega_4^3 \omega_3^2 v_3^2 + 6\omega_4^2 \omega_3^3 + 24\omega_7^2 \omega_3^2 v_3^2 + 42c_s^2 \omega_7^2 \omega_4^2 \omega_2^2 - 24c_s^2 \omega_7 \omega_4 \omega_3^2 + 42\omega_7 \omega_4^2 \omega_3^2 v_3^2 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_2 + 6\omega_7^2 \omega_4^3 \omega_2^2 v_3^2 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3^2 + \omega_7^2 \omega_4^3 \omega_2^2 - 12c_s^2 \omega_7^2 \omega_4^3 \omega_2^2 - 3\omega_4^3 \omega_2^2 - 12\omega_7 \omega_4^2 \omega_2^2 v_3^2 - 30\omega_7^2 \omega_4 \omega_2^2 v_3^2 - \omega_7^2 \omega_4^3 \omega_2^2 + 6c_s^2 \omega_4^3 \omega_2^2 - 12c_s^2 \omega_7 \omega_4^2 \omega_2^2 - 12\omega_7 \omega_4^3 \omega_2^2 v_3^2 - 12\omega_4^2 \omega_2^2 v_3^2 - 3\omega_7 \omega_4^3 \omega_2^2 + 6\omega_7^2 \omega_4^2 \omega_2^2 v_3^2 +$$

$$6c_s^2\omega_7\omega_4^3\omega_2^2 - 12\omega_7^2\omega_4^3\omega_2v_3^2 + 6\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3\omega_2^3 - 6\omega_7^2\omega_4\omega_2^3 + 6\omega_7\omega_4^2\omega_2^2 + 6\omega_7\omega_4^3\omega_2^2v_3^2 + 42c_s^2\omega_7\omega_4^2\omega_2^3 - 24c_s^2\omega_7^2\omega_4\omega_2^2 - 21\omega_7\omega_4^2\omega_2^3 + 78c_s^2\omega_7^2\omega_4\omega_2^3 - 24\omega_7\omega_4\omega_2^3v_3^2 - 12c_s^2\omega_7\omega_4^2\omega_2^2 - 36c_s^2\omega_7^2\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^2v_3^2) \frac{v_3v_1}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3\rho}^{(0),\text{MRT2}} = C_{\mathbf{D}_x\mathbf{D}_z^3\rho}^{(0),\text{MRT1}}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3\rho}^{(0),\text{CLBM1}} = (-3\omega_7^2\omega_4^2\omega_2^2 + 12\omega_7\omega_4\omega_2^3 + 6c_s^2\omega_7^2\omega_4^3\omega_2 - 36c_s^2\omega_7^2\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^2\omega_2v_3^2 - 36c_s^2\omega_4^2\omega_2^3 + 7\omega_7^2\omega_4^2\omega_2^3 - 6\omega_4^3\omega_3^2v_3^2 + 6\omega_4^2\omega_2^3 + 36c_s^2\omega_7^2\omega_4^2\omega_2^2 - 24c_s^2\omega_7\omega_4\omega_2^3 + 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12c_s^2\omega_7^2\omega_4^2\omega_2 + 6\omega_7^2\omega_4^3\omega_2^2v_3^2 + 6c_s^2\omega_7^2\omega_4^3\omega_2^2 + \omega_7^2\omega_4^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 - 3\omega_4^3\omega_2^3 + 12\omega_7^2\omega_4\omega_2^3v_3^2 - \omega_7^2\omega_4^3\omega_2^3 + 18c_s^2\omega_4^3\omega_2^3 - 24c_s^2\omega_7\omega_4^3\omega_2^3 + 12\omega_4^2\omega_2^3v_3^2 - 3\omega_7\omega_4^3\omega_2^2 - 6\omega_7^2\omega_4^2\omega_2^3v_3^2 + 12c_s^2\omega_7\omega_4^3\omega_2^2 - 12\omega_7^2\omega_4^3\omega_2v_3^2 + 6\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3\omega_2^3 - 6\omega_7^2\omega_4\omega_2^3 + 6\omega_7\omega_4^2\omega_2^2 + 72c_s^2\omega_7\omega_4^2\omega_2^2 - 12c_s^2\omega_7^2\omega_4\omega_2^2 - 21\omega_7\omega_4^2\omega_2^3 + 36c_s^2\omega_7^2\omega_4\omega_2^2 - 24\omega_7\omega_4\omega_2^3v_3^2 - 24c_s^2\omega_7\omega_4^2\omega_2^2 - 12c_s^2\omega_7^2\omega_2^3 - 6\omega_7^2\omega_4^2\omega_2^2v_3^2) \frac{v_3v_1}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3\rho}^{(0),\text{CLBM2}} = C_{\mathbf{D}_x\mathbf{D}_z^3\rho}^{(0),\text{CLBM1}}$$

$$\text{coefficient } C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} :$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{SRT}} = (36 + 54\omega v_3^2 + 20\omega^2 - 54\omega - \omega^3 - 36v_3^2 + \omega^3v_3^2 - 56c_s^2\omega^2 + 4c_s^2\omega^3 - 20\omega^2v_3^2 + 144c_s^2\omega - 96c_s^2) \frac{v_3\rho}{12\omega^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{MRT1}} = (11\omega_7^2\omega_4^2 - 44c_s^2\omega_7^2\omega_4^2 - \omega_7^2\omega_4^3 + 48\omega_7\omega_4^2v_3^2 + 12\omega_7^2v_3^2 + 4c_s^2\omega_7^2\omega_4^3 + 12\omega_4^2 - 48c_s^2\omega_7^2 + 90c_s^2\omega_7^2\omega_4 - 12\omega_7^2\omega_4 - 6\omega_4^3 - 12\omega_7\omega_4^3v_3^2 - 36c_s^2\omega_7\omega_4 - 12c_s^2\omega_4^2 + 24\omega_7\omega_4 + 6c_s^2\omega_4^3 + 6\omega_4^3v_3^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 - 36\omega_7\omega_4v_3^2 - 12c_s^2\omega_7\omega_4^3 - 8\omega_7^2\omega_4^2v_3^2 - 36\omega_7\omega_4^2 + 48c_s^2\omega_7\omega_4^2 - 12\omega_4^2v_3^2) \frac{v_3\rho}{12\omega_7^2\omega_4^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{MRT2}} = C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{MRT1}}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{CLBM1}} = (11\omega_7^2\omega_4^2 + 12\omega_7^2\omega_4v_3^2 - 26c_s^2\omega_7^2\omega_4^2 - \omega_7^2\omega_4^3 + 48\omega_7\omega_4^2v_3^2 + 12\omega_7^2v_3^2 + 4c_s^2\omega_7^2\omega_4^3 + 12\omega_4^2 + 18c_s^2\omega_7^2\omega_4 - 12\omega_7^2\omega_4 - 6\omega_4^3 - 6\omega_7\omega_4^3v_3^2 - 36c_s^2\omega_7\omega_4 - 60c_s^2\omega_4^2 + 24\omega_7\omega_4 + 30c_s^2\omega_4^3 - 6\omega_4^3v_3^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 - 60\omega_7\omega_4v_3^2 - 30c_s^2\omega_7\omega_4^3 - 14\omega_7^2\omega_4^2v_3^2 - 36\omega_7\omega_4^2 + 96c_s^2\omega_7\omega_4^2 + 12\omega_4^2v_3^2) \frac{v_3\rho}{12\omega_7^2\omega_4^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{CLBM2}} = C_{\mathbf{D}_x\mathbf{D}_z^3v_1}^{(0),\text{CLBM1}}$$

$$\text{coefficient } C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} :$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{SRT}} = (12 + 18\omega v_3^2 + 8\omega^2 - 18\omega - \omega^3 - 12v_3^2 + 3\omega^3v_3^2 - 56c_s^2\omega^2 + 4c_s^2\omega^3 - 12\omega^2v_3^2 + 144c_s^2\omega - 96c_s^2) \frac{\rho v_1}{12\omega^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{MRT1}} = (-6\omega_7^2\omega_4^2\omega_2^2 + 3\omega_7^2\omega_4^3\omega_2^2v_3^2 + 6c_s^2\omega_7^2\omega_4^3\omega_2 - 32c_s^2\omega_7^2\omega_4^2\omega_2^3 - 12c_s^2\omega_4^2\omega_2^3 + 3\omega_7^2\omega_4^2\omega_2^3 + 6\omega_4^3\omega_2^3v_3^2 + 24\omega_7^2\omega_2^3v_3^2 + 48c_s^2\omega_7^2\omega_4^2\omega_2^2 - 12c_s^2\omega_7\omega_4\omega_2^3 + 36\omega_7\omega_4^2\omega_2^3v_3^2 - 12c_s^2\omega_7^2\omega_4^2\omega_2 + 4c_s^2\omega_7^2\omega_4^3\omega_2^2 + 2\omega_7^2\omega_4^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 - 24\omega_7\omega_4^2\omega_2^3v_3^2 - 30\omega_7^2\omega_4\omega_2^3v_3^2 - \omega_7^2\omega_4^3\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 - 12c_s^2\omega_7\omega_4^3\omega_2^3 - 12\omega_7\omega_4^3\omega_2^3v_3^2 - 12\omega_4^2\omega_2^3v_3^2 - 6\omega_7\omega_4^3\omega_2^2 + 12c_s^2\omega_7\omega_4^3\omega_2^2 - 18\omega_7^2\omega_4^3\omega_2v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 3\omega_7\omega_4^3\omega_2^3 + 12\omega_7\omega_4^2\omega_2^3 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36c_s^2\omega_7\omega_4^3\omega_2^3 - 24c_s^2\omega_7^2\omega_4\omega_2^2 - 6\omega_7\omega_4^2\omega_2^3 + 36c_s^2\omega_7^2\omega_4\omega_2^3 - 12\omega_7\omega_4\omega_2^3v_3^2 - 24c_s^2\omega_7\omega_4^2\omega_2^2 - 12c_s^2\omega_7^2\omega_2^3 + 12\omega_7^2\omega_4^2\omega_2^2v_3^2) \frac{\rho v_1}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{MRT2}} = C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{MRT1}}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{CLBM1}} = (-6\omega_7^2\omega_4^2\omega_2^2 + 3\omega_7^2\omega_4^3\omega_2^2v_3^2 + 6c_s^2\omega_7^2\omega_4^3\omega_2 - 32c_s^2\omega_7^2\omega_4^2\omega_2^3 - 12c_s^2\omega_4^2\omega_2^3 + 3\omega_7^2\omega_4^2\omega_2^3 - 6\omega_4^3\omega_2^3v_3^2 - 24\omega_7^2\omega_2^3v_3^2 + 48c_s^2\omega_7^2\omega_4^2\omega_2^2 - 12c_s^2\omega_7\omega_4\omega_2^3 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12c_s^2\omega_7^2\omega_4^2\omega_2 + 4c_s^2\omega_7^2\omega_4^3\omega_2^2 + 2\omega_7^2\omega_4^3\omega_2^2 - 12c_s^2\omega_7^2\omega_4^3\omega_2^2 - 24\omega_7\omega_4^2\omega_2^3v_3^2 + 30\omega_7^2\omega_4\omega_2^3v_3^2 - \omega_7^2\omega_4^3\omega_2^2 + 6c_s^2\omega_4^3\omega_2^3 - 12c_s^2\omega_7\omega_4^3\omega_2^3 + 12\omega_4^2\omega_2^3v_3^2 - 6\omega_7\omega_4^3\omega_2^2 - 12\omega_7^2\omega_4^3\omega_2^3v_3^2 + 12c_s^2\omega_7\omega_4^3\omega_2^2 - 18\omega_7^2\omega_4^3\omega_2v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 3\omega_7\omega_4^3\omega_2^3 + 12\omega_7\omega_4^2\omega_2^3 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36c_s^2\omega_7\omega_4^3\omega_2^3 - 24c_s^2\omega_7^2\omega_4\omega_2^2 - 6\omega_7\omega_4^2\omega_2^3 + 36c_s^2\omega_7^2\omega_4\omega_2^3 + 12\omega_7\omega_4\omega_2^3v_3^2 - 24c_s^2\omega_7\omega_4^2\omega_2^2 - 12c_s^2\omega_7^2\omega_2^3 + 12\omega_7^2\omega_4^2\omega_2^2v_3^2) \frac{\rho v_1}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{CLBM2}} = C_{\mathbf{D}_x\mathbf{D}_z^3v_3}^{(0),\text{CLBM1}}$$

$$\text{coefficient } C_{\mathbf{D}_y\mathbf{D}_z^3\rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} :$$

$$C_{\mathbf{D}_y\mathbf{D}_z^3\rho}^{(0),\text{SRT}} = (24 + 14\omega^2 - 36\omega - \omega^3 - 72c_s^2\omega^2 + 6c_s^2\omega^3 + 180c_s^2\omega - 120c_s^2) \frac{v_2v_3}{6\omega^3}$$

$$C_{\mathbf{D}_y\mathbf{D}_z^3\rho}^{(0),\text{MRT1}} = (6c_s^2\omega_7\omega_4^3\omega_2^3 + 6\omega_7^2\omega_4^2v_3^2\omega_3 + 6\omega_7\omega_4^3\omega_2^3 - 24\omega_7\omega_4v_3^2\omega_3^3 - 12c_s^2\omega_7\omega_4^3\omega_2^3 - 3\omega_7\omega_4^3\omega_2^3 - 21\omega_7\omega_4^2\omega_3^3 + 6\omega_7\omega_4^3v_3^2\omega_2^3 + 6\omega_7^2\omega_4^2v_3^2\omega_3^3 + 78c_s^2\omega_7^2\omega_4\omega_2^3 - 12c_s^2\omega_7\omega_4^2\omega_2^3 - 36c_s^2\omega_7^2\omega_2^3 - 12\omega_7\omega_4^3v_3^2\omega_3^3 - 12\omega_7^2\omega_4^2v_3^2\omega_2^3 - 12\omega_4^2v_3^2\omega_3^3 - 6\omega_7^2\omega_4\omega_2^3 + 6\omega_7\omega_4^2\omega_2^3 + 42c_s^2\omega_7\omega_4^2\omega_2^3 - 24c_s^2\omega_7^2\omega_4\omega_2^3 - 30\omega_7^2\omega_4v_3^2\omega_2^3 - 12c_s^2\omega_4^2\omega_2^3 + 7\omega_7^2\omega_4^2\omega_2^3 + 6\omega_4^3\omega_2^3 + 42c_s^2\omega_7^2\omega_4^2\omega_2^3 - 24c_s^2\omega_7\omega_4\omega_2^3 - 3\omega_7^2\omega_4^2\omega_2^3 - 12\omega_7^2\omega_4^3v_3^2\omega_3 + 12\omega_7\omega_4\omega_2^3 + 12\omega_7^2\omega_4v_3^2\omega_2^3 + 6c_s^2\omega_7^2\omega_3^3\omega_2 + 6\omega_7^2\omega_4^3v_3^2 - 48c_s^2\omega_7^2\omega_4^2\omega_2^3 - 12c_s^2\omega_7^2\omega_4^3\omega_2^3 - 3\omega_4^3\omega_2^3 + 6\omega_4^3v_3^2\omega_2^3 + 24\omega_7^2v_3^2\omega_2^3 + 6\omega_7\omega_4^3v_3^2\omega_2^3 - \omega_7^2\omega_4^3\omega_2^3 + 42\omega_7\omega_4^2v_3^2\omega_2^3 + 6c_s^2\omega_4^3\omega_2^3 - 12c_s^2\omega_7^2\omega_4^3\omega_2^3 + 6c_s^2\omega_7^2\omega_4^2\omega_2^3 + \omega_7^2\omega_4^2\omega_2^3 - 12\omega_7\omega_4^2v_3^2\omega_2^3) \frac{v_2v_3}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{\text{D}_y \text{D}_z^3 \rho}^{(0), \text{MRT}^2} = C_{\text{D}_y \text{D}_z^3 \rho}^{(0), \text{MRT}^1}$$

$$C_{\text{D}_y \text{D}_z^3 \rho}^{(0), \text{CLBM}^1} = (12c_s^2 \omega_7 \omega_4^3 \omega_3^2 + 6\omega_7^2 \omega_4^2 v_3^2 \omega_3 + 6\omega_7 \omega_4^3 \omega_3^3 - 24\omega_7 \omega_4 v_3^2 \omega_3^3 - 24c_s^2 \omega_7 \omega_4^3 \omega_3^3 - 3\omega_7 \omega_4^3 \omega_3^2 - 21\omega_7 \omega_4^2 \omega_3^3 - 6\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 36c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 24c_s^2 \omega_7 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_3^3 - 6\omega_7^2 \omega_4^2 v_3^2 \omega_3^2 + 12\omega_4^2 v_3^2 \omega_3^3 - 6\omega_7^2 \omega_4 \omega_3^3 + 6\omega_7 \omega_4^2 \omega_3^2 + 72c_s^2 \omega_7 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4 \omega_3^2 + 12\omega_7^2 \omega_4 v_3^2 \omega_3^3 - 36c_s^2 \omega_4^2 \omega_3^3 + 7\omega_7^2 \omega_4^3 \omega_3^3 + 6\omega_4^3 \omega_3^3 + 36c_s^2 \omega_7^2 \omega_4^2 \omega_3^2 - 24c_s^2 \omega_7 \omega_4 \omega_3^3 - 3\omega_7^2 \omega_4^2 \omega_3^2 - 12\omega_7^2 \omega_4^3 v_3^2 \omega_3 + 12\omega_7 \omega_4 \omega_3^3 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3 + 6\omega_7^2 \omega_4^3 v_3^2 - 36c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 - 3\omega_4^3 \omega_3^3 - 6\omega_4^2 v_3^2 \omega_3^3 + 6\omega_7^2 \omega_4^3 v_3^2 \omega_3^2 - \omega_7^2 \omega_4^3 \omega_3^3 + 12\omega_7 \omega_4^3 v_3^2 \omega_3^3 + 18c_s^2 \omega_4^3 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_3 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 + \omega_7^2 \omega_4^3 \omega_3^2) \frac{v_2 v_3}{6\omega_7^2 \omega_4^3 \omega_3^3}$$

$$C_{\text{D}_y \text{D}_z^3 \rho}^{(0), \text{CLBM}^2} = C_{\text{D}_y \text{D}_z^3 \rho}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{\text{D}_y \text{D}_z^3 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} :$$

$$C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{SRT}} = (36 + 54\omega v_3^2 + 20\omega^2 - 54\omega - \omega^3 - 36v_3^2 + \omega^3 v_3^2 - 56c_s^2 \omega^2 + 4c_s^2 \omega^3 - 20\omega^2 v_3^2 + 144c_s^2 \omega - 96c_s^2) \frac{v_3 \rho}{12\omega^3}$$

$$C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{MRT}^1} = (11\omega_7^2 \omega_4^2 - 44c_s^2 \omega_7^2 \omega_4^2 - \omega_7^2 \omega_4^3 + 48\omega_7 \omega_4^2 v_3^2 + 12\omega_7^2 v_3^2 + 4c_s^2 \omega_7^2 \omega_4^3 + 12\omega_4^2 - 48c_s^2 \omega_7^2 + 90c_s^2 \omega_7 \omega_4 - 12\omega_7^2 \omega_4 - 6\omega_4^3 - 12\omega_7 \omega_4^3 v_3^2 - 36c_s^2 \omega_7 \omega_4 - 12c_s^2 \omega_4^2 + 24\omega_7 \omega_4 + 6c_s^2 \omega_4^3 + 6\omega_4^3 v_3^2 + \omega_7^2 \omega_4^3 v_3^2 + 9\omega_7 \omega_4^3 - 36\omega_7 \omega_4 v_3^2 - 12c_s^2 \omega_7 \omega_4^3 - 8\omega_7^2 \omega_4^2 v_3^2 - 36\omega_7 \omega_4^2 + 48c_s^2 \omega_7 \omega_4^2 - 12\omega_4^2 v_3^2) \frac{v_3 \rho}{12\omega_7^2 \omega_4^3}$$

$$C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{MRT}^2} = C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{MRT}^1}$$

$$C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{CLBM}^1} = (11\omega_7^2 \omega_4^2 + 12\omega_7^2 \omega_4 v_3^2 - 26c_s^2 \omega_7^2 \omega_4^2 - \omega_7^2 \omega_4^3 + 48\omega_7 \omega_4^2 v_3^2 + 12\omega_7^2 v_3^2 + 4c_s^2 \omega_7^2 \omega_4^3 + 12\omega_4^2 + 18c_s^2 \omega_7^2 \omega_4 - 12\omega_7^2 \omega_4 - 6\omega_4^3 - 6\omega_7 \omega_4^3 v_3^2 - 36c_s^2 \omega_7 \omega_4 - 60c_s^2 \omega_4^2 + 24\omega_7 \omega_4 + 30c_s^2 \omega_4^3 - 6\omega_4^3 v_3^2 + \omega_7^2 \omega_4^3 v_3^2 + 9\omega_7 \omega_4^3 - 60\omega_7 \omega_4 v_3^2 - 30c_s^2 \omega_7 \omega_4^3 - 14\omega_7^2 \omega_4^2 v_3^2 - 36\omega_7 \omega_4^2 + 96c_s^2 \omega_7 \omega_4^2 + 12\omega_4^2 v_3^2) \frac{v_3 \rho}{12\omega_7^2 \omega_4^3}$$

$$C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{CLBM}^2} = C_{\text{D}_y \text{D}_z^3 v_2}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{\text{D}_y \text{D}_z^3 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} :$$

$$C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{SRT}} = (12 + 18\omega v_3^2 + 8\omega^2 - 18\omega - \omega^3 - 12v_3^2 + 3\omega^3 v_3^2 - 56c_s^2 \omega^2 + 4c_s^2 \omega^3 - 12\omega^2 v_3^2 + 144c_s^2 \omega - 96c_s^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{MRT}^1} = (12c_s^2 \omega_7 \omega_4^3 \omega_3^2 + 3\omega_7 \omega_4^3 \omega_3^3 - 12\omega_7 \omega_4 v_3^2 \omega_3^3 - 12c_s^2 \omega_7 \omega_4^3 \omega_3^3 - 6\omega_7 \omega_4^3 \omega_3^2 - 6\omega_7 \omega_4^2 \omega_3^3 + 12\omega_7 \omega_4^3 v_3^2 \omega_3^2 + 36c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 24c_s^2 \omega_7 \omega_4^2 \omega_3^2 - 12c_s^2 \omega_7^2 \omega_3^3 - 12\omega_7 \omega_4^3 v_3^2 \omega_3^3 + 12\omega_7^2 \omega_4^2 v_3^2 \omega_3^2 - 12\omega_4^2 v_3^2 \omega_3^3 + 12\omega_7 \omega_4^2 \omega_3^3 + 36c_s^2 \omega_7 \omega_4^2 \omega_3^3 - 24c_s^2 \omega_7^2 \omega_4 \omega_3^2 - 30\omega_7^2 \omega_4 v_3^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_3^3 + 3\omega_7^2 \omega_4^2 \omega_3^3 + 48c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 12c_s^2 \omega_7 \omega_4 \omega_3^3 - 6\omega_7^2 \omega_4^2 \omega_3^3 - 18\omega_7^2 \omega_4^3 v_3^2 \omega_3 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3 + 12\omega_7^2 \omega_4^3 v_3^2 - 32c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4 \omega_3^2 + 6\omega_4^3 v_3^2 \omega_3^3 + 24\omega_7^2 v_3^2 \omega_3^3 - \omega_7^2 \omega_4^3 \omega_3^3 + 36\omega_7 \omega_4^3 v_3^2 \omega_3^3 + 6c_s^2 \omega_4^3 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_3 + 4c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 + 3\omega_7^2 \omega_4^3 v_3^2 \omega_3^3 + 2\omega_7^2 \omega_4^3 \omega_3^2 - 24\omega_7 \omega_4^3 v_3^2 \omega_3^2) \frac{v_2 \rho}{12\omega_7^2 \omega_4^3 \omega_3^3}$$

$$C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{MRT}^2} = C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{MRT}^1}$$

$$C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{CLBM}^1} = (12c_s^2 \omega_7 \omega_4^3 \omega_3^2 + 3\omega_7 \omega_4^3 \omega_3^3 + 12\omega_7 \omega_4 v_3^2 \omega_3^3 - 12c_s^2 \omega_7 \omega_4^3 \omega_3^3 - 6\omega_7 \omega_4^3 \omega_3^2 - 6\omega_7 \omega_4^2 \omega_3^3 + 12\omega_7 \omega_4^3 v_3^2 \omega_3^2 - 12\omega_7^2 \omega_4^2 v_3^2 \omega_3^3 + 36c_s^2 \omega_7^2 \omega_4 \omega_3^3 - 24c_s^2 \omega_7 \omega_4^2 \omega_3^2 - 12c_s^2 \omega_7^2 \omega_3^3 + 12\omega_7^2 \omega_4^2 v_3^2 \omega_3^2 + 12\omega_4^2 v_3^2 \omega_3^3 + 12\omega_7 \omega_4^2 \omega_3^3 + 36c_s^2 \omega_7 \omega_4^2 \omega_3^3 - 24c_s^2 \omega_7^2 \omega_4 \omega_3^2 + 30\omega_7^2 \omega_4 v_3^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4 \omega_3^2 + 3\omega_7^2 \omega_4^2 \omega_3^3 + 48c_s^2 \omega_7^2 \omega_4^2 \omega_3^2 - 12c_s^2 \omega_7 \omega_4 \omega_3^3 - 6\omega_7^2 \omega_4^2 \omega_3^2 - 18\omega_7^2 \omega_4^3 v_3^2 \omega_3 + 6c_s^2 \omega_7^2 \omega_4^3 \omega_3 + 12\omega_7^2 \omega_4^3 v_3^2 - 32c_s^2 \omega_7^2 \omega_4^2 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4 \omega_3^2 - 12c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 - 6\omega_4^3 v_3^2 \omega_3^3 + 24\omega_7^2 v_3^2 \omega_3^3 - 6\omega_4^3 v_3^2 \omega_3^3 - 24\omega_7^2 v_3^2 \omega_3^3 - \omega_7^2 \omega_4^3 \omega_3^3 - 12\omega_7 \omega_4^2 v_3^2 \omega_3^3 + 6c_s^2 \omega_4^3 \omega_3^3 - 12c_s^2 \omega_7^2 \omega_4^2 \omega_3 + 4c_s^2 \omega_7^2 \omega_4^3 \omega_3^3 + 3\omega_7^2 \omega_4^3 v_3^2 \omega_3^3 + 2\omega_7^2 \omega_4^3 \omega_3^2 - 24\omega_7 \omega_4^3 v_3^2 \omega_3^2) \frac{v_2 \rho}{12\omega_7^2 \omega_4^3 \omega_3^3}$$

$$C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{CLBM}^2} = C_{\text{D}_y \text{D}_z^3 v_3}^{(0), \text{CLBM}^1}$$

$$\text{coefficient } C_{\text{D}_z^4 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_3^4} :$$

$$C_{\text{D}_z^4 \rho}^{(0), \text{SRT}} = (-42\omega^2 v_3^4 - 3c_s^4 \omega^3 + 48c_s^4 + 216c_s^2 \omega v_3^2 - 108\omega v_3^2 + 30c_s^4 \omega^2 - 72c_s^4 \omega + 3\omega^3 v_3^4 + 72v_3^2 - 3\omega^3 v_3^2 + 6c_s^2 \omega^3 v_3^2 - 14c_s^2 \omega^2 - 144c_s^2 v_3^2 - 72v_3^4 + c_s^2 \omega^3 - 84c_s^2 \omega^2 v_3^2 + 42\omega^2 v_3^2 + 108\omega v_3^4 + 36c_s^2 \omega - 24c_s^2) \frac{1}{24\omega^3}$$

$$C_{\text{D}_z^4 \rho}^{(0), \text{MRT}^1} = (-24\omega_7^2 \omega_4 v_3^2 - 48\omega_7 \omega_4 v_3^4 - 8c_s^2 \omega_7^2 \omega_4^2 + 48c_s^2 \omega_7 \omega_4^2 v_3^2 - 48c_s^4 \omega_7^2 \omega_4 - 72\omega_7 \omega_4^2 v_3^2 - 24\omega_4^2 v_3^4 + 156c_s^2 \omega_7^2 \omega_4 v_3^2 + c_s^2 \omega_7^2 \omega_4^3 - 24\omega_7^2 \omega_4^2 v_3^4 - 96c_s^2 \omega_7^2 v_3^2 - 12c_s^2 \omega_7 \omega_4^3 v_3^2 + 24c_s^4 \omega_7^2 \omega_4^2 + 3\omega_7^2 \omega_4^3 v_3^4 + 12c_s^2 \omega_7^2 \omega_4 + 12\omega_4^3 v_3^4 - 3c_s^4 \omega_7^2 \omega_4^3 + 18\omega_7 \omega_4^3 v_3^2 - 24c_s^2 \omega_7 \omega_4 + 6c_s^2 \omega_7^2 \omega_4^3 v_3^2 + 6c_s^4 \omega_7 \omega_4^3 - 12\omega_4^3 v_3^2 - 18\omega_7 \omega_4^3 v_3^4 - 3\omega_7^2 \omega_4^3 v_3^2 - 24c_s^4 \omega_7 \omega_4^2 + 12c_s^2 \omega_4^3 v_3^2 + 24c_s^4 \omega_7^2 + 48\omega_7 \omega_4 v_3^2 + 24c_s^4 \omega_7 \omega_4 - 72c_s^2 \omega_7^2 \omega_4^2 v_3^2 - 6c_s^2 \omega_7 \omega_4^3 + 24\omega_7^2 \omega_4 v_3^4 - 24c_s^2 \omega_4^2 v_3^2 + 24\omega_7^2 \omega_4^2 v_3^2 + 24c_s^2 \omega_7 \omega_4^2 + 72\omega_7 \omega_4^2 v_3^4 - 24c_s^2 \omega_7 \omega_4 v_3^2 + 24\omega_4^2 v_3^2) \frac{1}{24\omega_7^2 \omega_4^3}$$

$$C_{\text{D}_z^4 \rho}^{(0), \text{MRT}^2} = C_{\text{D}_z^4 \rho}^{(0), \text{MRT}^1}$$

$$C_{D_z^4 \rho}^{(0), \text{CLBM1}} = (-8c_s^2 \omega_7^2 \omega_4^2 + 144c_s^2 \omega_7 \omega_4^2 v_3^2 - 48c_s^4 \omega_7^2 \omega_4 - 72\omega_7 \omega_4^2 v_3^2 - 72\omega_4^2 v_3^4 - 36c_s^2 \omega_7^2 \omega_4 v_3^2 + c_s^2 \omega_7^2 \omega_4^3 - 12\omega_7^2 \omega_4^2 v_3^4 - 72c_s^2 \omega_7 \omega_4^3 v_3^2 + 24c_s^4 \omega_7^2 \omega_4^2 + 3\omega_7^2 \omega_4^3 v_3^4 + 12c_s^2 \omega_7^2 \omega_4 + 36\omega_4^3 v_3^4 - 3c_s^4 \omega_7^2 \omega_4^3 + 30\omega_7 \omega_4^3 v_3^2 - 24c_s^2 \omega_7 \omega_4 + 6c_s^2 \omega_7^2 \omega_4^3 v_3^2 + 6c_s^4 \omega_7 \omega_4^3 - 36\omega_4^3 v_3^2 - 30\omega_7 \omega_4^3 v_3^4 - 3\omega_7^2 \omega_4^3 v_3^2 - 24c_s^4 \omega_7 \omega_4^2 + 108c_s^2 \omega_4^3 v_3^2 + 24c_s^4 \omega_7^2 + 24c_s^4 \omega_7 \omega_4 - 12c_s^2 \omega_7^2 \omega_4^2 v_3^2 - 6c_s^2 \omega_7 \omega_4^3 - 216c_s^2 \omega_4^2 v_3^2 + 12\omega_7^2 \omega_4^2 v_3^2 + 24c_s^2 \omega_7 \omega_4^2 + 72\omega_7 \omega_4^2 v_3^4 + 72c_s^2 \omega_7 \omega_4 v_3^2 + 72\omega_4^2 v_3^2) \frac{1}{24\omega_7^2 \omega_4^3}$$

$$C_{D_z^4 \rho}^{(0), \text{CLBM2}} = C_{D_z^4 \rho}^{(0), \text{CLBM1}}$$

coefficient $C_{D_z^4 v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_3^4}$:

$$C_{D_z^4 v_3}^{(0), \text{SRT}} = (24 + 54\omega v_3^2 + 14\omega^2 - 36\omega - \omega^3 - 36v_3^2 + 2\omega^3 v_3^2 - 26c_s^2 \omega^2 + c_s^2 \omega^3 - 22\omega^2 v_3^2 + 72c_s^2 \omega - 48c_s^2) \frac{v_3 \rho}{12\omega^3}$$

$$C_{D_z^4 v_3}^{(0), \text{MRT1}} = (8\omega_7^2 \omega_4^2 + 24\omega_7^2 \omega_4 v_3^2 - 20c_s^2 \omega_7^2 \omega_4^2 - \omega_7^2 \omega_4^3 + 24\omega_7 \omega_4^2 v_3^2 - 12\omega_7^2 v_3^2 + c_s^2 \omega_7^2 \omega_4^3 + 12\omega_4^2 - 24c_s^2 \omega_7^2 + 42c_s^2 \omega_7^2 \omega_4 - 6\omega_7^2 \omega_4 - 6\omega_4^3 - 6\omega_7 \omega_4^3 v_3^2 - 12c_s^2 \omega_7 \omega_4 - 12c_s^2 \omega_4^2 + 12\omega_7 \omega_4 + 6c_s^2 \omega_4^3 + 6\omega_4^3 v_3^2 + 2\omega_7^2 \omega_4^3 v_3^2 + 6\omega_7 \omega_4^3 - 12\omega_7 \omega_4 v_3^2 - 6c_s^2 \omega_7 \omega_4^3 - 16\omega_7^2 \omega_4^2 v_3^2 - 24\omega_7 \omega_4^2 + 24c_s^2 \omega_7 \omega_4^2 - 12\omega_4^2 v_3^2) \frac{v_3 \rho}{12\omega_7^2 \omega_4^3}$$

$$C_{D_z^4 v_3}^{(0), \text{MRT2}} = C_{D_z^4 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(0), \text{CLBM1}} = (2\omega_7^2 \omega_4^2 - 12\omega_7^2 \omega_4 v_3^2 - 2c_s^2 \omega_7^2 \omega_4^2 - \omega_7^2 \omega_4^3 + 24\omega_7 \omega_4^2 v_3^2 - 12\omega_7^2 v_3^2 + c_s^2 \omega_7^2 \omega_4^3 + 36\omega_4^2 + 24c_s^2 \omega_7^2 - 30c_s^2 \omega_7^2 \omega_4 + 6\omega_7^2 \omega_4 - 18\omega_4^3 - 24\omega_7 \omega_4^3 v_3^2 - 12c_s^2 \omega_7 \omega_4 - 60c_s^2 \omega_4^2 - 12\omega_7 \omega_4 + 30c_s^2 \omega_4^3 + 42\omega_4^3 v_3^2 + 2\omega_7^2 \omega_4^3 v_3^2 + 12\omega_7 \omega_4^3 + 60\omega_7 \omega_4 v_3^2 - 24c_s^2 \omega_7 \omega_4^3 + 2\omega_7^2 \omega_4^2 v_3^2 - 24\omega_7 \omega_4^2 + 72c_s^2 \omega_7 \omega_4^2 - 84\omega_4^2 v_3^2) \frac{v_3 \rho}{12\omega_7^2 \omega_4^3}$$

$$C_{D_z^4 v_3}^{(0), \text{CLBM2}} = C_{D_z^4 v_3}^{(0), \text{CLBM1}}$$

References

- [1] T. Krüger, H. Kusumaatmaja, A. Kuzmin, O. Shardt, G. Silva, E. M. Viggien, The lattice Boltzmann method, Springer International Publishing 10 (978-3) (2017) 4–15.