

**D3Q7 ADE,**  
a supplementary material for  
**Lattice Boltzmann Method Analysis Tool (LBMAT)**

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## 1 Global definitions

In  $\mathbb{R}^3$ , the position and velocity vectors are given by  $\mathbf{x} = (x_1, x_2, x_3)^T$  and  $\mathbf{v} = (v_1, v_2, v_3)^T$ , respectively.

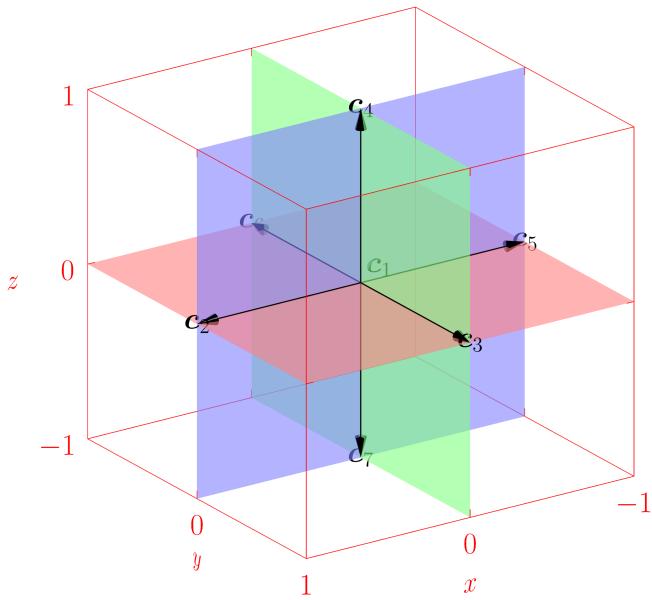
## 1.1 Discrete velocity vectors

Discrete velocity vectors and the lattice speed of sound are defined by

$$\{\mathbf{c}_i\}_{i=1}^7 = \left( \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix} \right),$$

$$c_s = \frac{1}{2},$$

respectively [1].



## 1.2 Raw and central moments

The raw and central moments are defined by

$$m_{\alpha} := \sum_{i=1}^7 f_i \mathbf{c}_i^{\alpha},$$

and

$$k_{\alpha} := \sum_{i=1}^7 f_i (\mathbf{c}_i - \mathbf{v})^{\alpha},$$

respectively, where  $\alpha = (\alpha_1, \alpha_2, \alpha_3) \in \mathbb{Z}^3$  denotes a multi-index (as a row vector) and  $\mathbf{c}_i^{\alpha} := \prod_{j=1}^3 [\mathbf{c}_i]_j^{\alpha_j}$ .

## 1.3 Transformation matrix M

Matrix  $\mathbf{M}$ , that defines macroscopic quantities (moments)  $\boldsymbol{\mu}$  by

$$\boldsymbol{\mu} = \mathbf{M} \mathbf{f},$$

with  $\mathbf{f} = (f_1, f_2, \dots, f_7)^T$ , is selected such that

$$\boldsymbol{\mu} = \left( m_{(0,0,0)}, m_{(1,0,0)}, m_{(0,1,0)}, m_{(0,0,1)}, m_{(2,0,0)}, m_{(0,2,0)}, m_{(0,0,2)} \right)^T,$$

i.e.,  $\mathbf{M}$  is given by

$$\mathbf{M} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 \end{pmatrix}.$$

## 1.4 Equilibrium

The corresponding equilibrium raw moments are defined using the continuous Maxwell–Boltzmann distribution function [1]

$$f^{(eq)}(\boldsymbol{\xi}) = \frac{\rho}{(2\pi c_s^2)^{\frac{3}{2}}} \exp\left(-\frac{||\boldsymbol{\xi} - \mathbf{v}||^2}{2c_s^2}\right)$$

as

$$m_{\boldsymbol{\alpha}}^{(eq)} = \int_{\mathbb{R}^3} \boldsymbol{\xi}^{\boldsymbol{\alpha}} f^{(eq)}(\boldsymbol{\xi}) d\boldsymbol{\xi},$$

where  $\alpha_i \in \{0, 1, 2\}$ ,  $i = 1, 2, 3$ . Hence, the equilibrium moments  $\boldsymbol{\mu}^{(eq)}$  satisfy

$$\boldsymbol{\mu}^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho(v_1^2 + c_s^2) \\ \rho(v_2^2 + c_s^2) \\ \rho(v_3^2 + c_s^2) \end{pmatrix}.$$

## 2 Spatial EPDEs

### 2.1 SRT

#### 2.1.1 Definitions

Collision operator  $\mathbf{C}$ :

$$\mathbf{C}(\mathbf{f}) = \omega \left( \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)} - \mathbf{f} \right),$$

$\omega \in (0, 2)$ .

#### 2.1.2 Conservation of mass equation

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$$\begin{aligned}
& + (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_1 v_2}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_4 \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
C_5 \frac{\delta_l^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 - \omega^2 + 3\omega) \frac{3\delta_l^2 \delta_t \rho v_2}{2\omega^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + \\
(34cs^2\omega^2 - 2cs^2\omega^3 - 2v_2^2\omega^2 + 60cs^2 + v_2^2\omega^3 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_1 v_2}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
C_6 \frac{\delta_l^4}{4\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + (-26cs^2\omega^2 + cs^2\omega^3 - 126v_2^2\omega + 50v_2^2\omega^2 - 48cs^2 - 4v_2^2\omega^3 + 84v_2^2 + 72cs^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_2^2} + \\
(-26cs^2\omega^2 + 84v_1^2 + cs^2\omega^3 - 48cs^2 + 72cs^2\omega + 50v_1^2\omega^2 - 4v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_7 \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2^3} + \\
(24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_1 v_2}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_8 \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
C_9 \frac{\delta_l^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{10} \frac{\delta_l^4}{24\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_2^4} + C_{11} \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 - \omega^2 + 3\omega) \frac{\delta_l \delta_t^2 \rho}{2\omega^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
(36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_3}{12\omega^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_1}{12\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
(-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_1 v_3}{6\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3} + (34cs^2\omega^2 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega - 2v_1^2\omega^2 + v_1^2\omega^3) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3} + \\
+ (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_1 v_3}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{12} \frac{\delta_l^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
C_{13} \frac{\delta_l^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_3}{12\omega^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_2}{12\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
(-20 + \omega^3 - 12\omega^2 + 30\omega) \frac{\delta_l^3 \rho v_3 v_2}{2\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + (-20 + \omega^3 - 12\omega^2 + 30\omega) \frac{\delta_l^3 \rho v_1 v_3}{2\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + \\
(-20 + \omega^3 - 12\omega^2 + 30\omega) \frac{\delta_l^3 \rho v_1 v_2}{2\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + \\
(-12cs^2\omega^2 + 40v_1^2 + cs^2\omega^3 - 20cs^2 + 30cs^2\omega + 24v_1^2\omega^2 - 2v_1^2\omega^3 - 60v_1^2\omega) \frac{\delta_l^4 v_3 v_2}{\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
(132 - 5\omega^3 + 76\omega^2 - 198\omega) \frac{\delta_l^4 \rho v_1 v_3 v_2}{6\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
(-56cs^2\omega^2 + 84v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega + 52v_1^2\omega^2 - 5v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
(-56cs^2\omega^2 + 84v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega + 52v_1^2\omega^2 - 5v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
(-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_3 v_2}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + (34cs^2\omega^2 - 2cs^2\omega^3 - 2v_2^2\omega^2 + 60cs^2 + v_2^2\omega^3 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + \\
+ (-12cs^2\omega^2 + cs^2\omega^3 - 60v_2^2\omega + 24v_2^2\omega^2 - 20cs^2 - 2v_2^2\omega^3 + 40v_2^2 + 30cs^2\omega) \frac{\delta_l^4 v_1 v_3}{\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\
(-56cs^2\omega^2 + 4cs^2\omega^3 - 126v_2^2\omega + 52v_2^2\omega^2 - 96cs^2 - 5v_2^2\omega^3 + 84v_2^2 + 144cs^2\omega) \frac{\delta_l^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
(132 - 5\omega^3 + 76\omega^2 - 198\omega) \frac{\delta_l^4 \rho v_1 v_3 v_2}{6\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
(-56cs^2\omega^2 + 4cs^2\omega^3 - 126v_2^2\omega + 52v_2^2\omega^2 - 96cs^2 - 5v_2^2\omega^3 + 84v_2^2 + 144cs^2\omega) \frac{\delta_l^4 \rho v_1 v_3}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
(24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_3 v_2}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{14} \frac{\delta_l^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + \\
C_{15} \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 - \omega^2 + 3\omega) \frac{3\delta_l^2 \delta_t \rho v_3}{2\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + \\
(34cs^2\omega^2 - 2v_3^2\omega^2 + v_3^2\omega^3 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_1 v_3}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
+ C_{16} \frac{\delta_l^4}{4\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-26cs^2\omega^2 + 50v_3^2\omega^2 - 4v_3^2\omega^3 + cs^2\omega^3 + 84v_3^2 - 48cs^2 + 72cs^2\omega - 126v_3^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
(-26cs^2\omega^2 + 84v_1^2 + cs^2\omega^3 - 48cs^2 + 72cs^2\omega + 50v_1^2\omega^2 - 4v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
(34cs^2\omega^2 - 2v_3^2\omega^2 + v_3^2\omega^3 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_3 v_2}{6\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + \\
+ (-12cs^2\omega^2 + 24v_3^2\omega^2 - 2v_3^2\omega^3 + cs^2\omega^3 + 40v_3^2 - 20cs^2 + 30cs^2\omega - 60v_3^2\omega) \frac{\delta_l^4 v_1 v_2}{\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
(-56cs^2\omega^2 + 52v_3^2\omega^2 - 5v_3^2\omega^3 + 4cs^2\omega^3 + 84v_3^2 - 96cs^2 + 144cs^2\omega - 126v_3^2\omega) \frac{\delta_l^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
(-56cs^2\omega^2 + 52v_3^2\omega^2 - 5v_3^2\omega^3 + 4cs^2\omega^3 + 84v_3^2 - 96cs^2 + 144cs^2\omega - 126v_3^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
(132 - 5\omega^3 + 76\omega^2 - 198\omega) \frac{\delta_l^4 \rho v_1 v_3 v_2}{6\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{17} \frac{\delta_l^4}{4\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} +
\end{aligned}$$

$$\begin{aligned}
& (-26cs^2\omega^2 + 50v_3^2\omega^2 - 4v_3^2\omega^3 + cs^2\omega^3 + 84v_3^2 - 48cs^2 + 72cs^2\omega - 126v_3^2\omega) \frac{\delta_t^4\rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (-26cs^2\omega^2 + cs^2\omega^3 - 126v_2^2\omega + 50v_2^2\omega^2 - 48cs^2 - 4v_2^2\omega^3 + 84v_2^2 + 72cs^2\omega) \frac{\delta_t^4\rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{18} \frac{\delta_t^3\rho}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_3^3} + \\
& (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_t^4 v_1 v_3}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{19} \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& C_{20} \frac{\delta_t^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_t^4 v_3 v_2}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& C_{21} \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{22} \frac{\delta_t^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{23} \frac{\delta_t^4}{24\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^4} + C_{24} \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$C_1 = -36 + 34cs^2\omega^2 + 72v_1^2 - 2cs^2\omega^3 + 60cs^2\omega + \omega^3 + 42v_1^2\omega^2 - 20\omega^2 - 3v_1^2\omega^3 + 54\omega - 108v_1^2\omega$$

$$C_2 = -14cs^2\omega^2 + 3v_1^4\omega^3 - 84v_1^2cs^2\omega^2 + 72v_1^2 - 42v_1^4\omega^2 + cs^2\omega^3 + 6v_1^2cs^2\omega^3 + 108v_1^4\omega - 24cs^2 + 216v_1^2cs^2\omega - 144v_1^2cs^2 + 36cs^2\omega + 42v_1^2\omega^2 - 3cs^4\omega^3 + 48cs^4 + 30cs^4\omega^2 - 3v_1^2\omega^3 - 72v_1^4 - 72cs^4\omega - 108v_1^2\omega$$

$$C_3 = 24 - 26cs^2\omega^2 - 36v_1^2 + cs^2\omega^3 - 48cs^2 + 72cs^2\omega - \omega^3 - 22v_1^2\omega^2 + 14\omega^2 + 2v_1^2\omega^3 - 36\omega + 54v_1^2\omega$$

$$C_4 = 12 - 56cs^2\omega^2 - 12v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 12v_1^2\omega^2 + 8\omega^2 + 3v_1^2\omega^3 - 18\omega + 18v_1^2\omega$$

$$C_5 = 36 - 56cs^2\omega^2 - 36v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 20v_1^2\omega^2 + 20\omega^2 + v_1^2\omega^3 - 54\omega + 54v_1^2\omega$$

$$C_6 = -14v_1^2cs^2\omega^2 - 84v_1^2v_2^2\omega + 36cs^2v_2^2\omega + v_1^2cs^2\omega^3 - 14cs^2v_2^2\omega^2 + 56v_1^2v_2^2 + 34v_1^2v_2^2\omega^2 + 36v_1^2cs^2\omega + cs^2v_2^2\omega^3 - 24v_1^2cs^2 - 3v_1^2v_2^2\omega^3 - cs^4\omega^3 + 16cs^4 + 10cs^4\omega^2 - 24cs^4\omega - 24cs^2v_2^2$$

$$C_7 = -36 + 34cs^2\omega^2 - 2cs^2\omega^3 - 108v_2^2\omega + 42v_2^2\omega^2 + 60cs^2 - 3v_2^2\omega^3 + 72v_2^2 - 90cs^2\omega + \omega^3 - 20\omega^2 + 54\omega$$

$$C_8 = 36 - 56cs^2\omega^2 + 4cs^2\omega^3 + 54v_2^2\omega - 20v_2^2\omega^2 - 96cs^2 + v_2^2\omega^3 - 36v_2^2 + 144cs^2\omega - \omega^3 + 20\omega^2 - 54\omega$$

$$C_9 = 12 - 56cs^2\omega^2 + 4cs^2\omega^3 + 18v_2^2\omega - 12v_2^2\omega^2 - 96cs^2 + 3v_2^2\omega^3 - 12v_2^2 + 144cs^2\omega - \omega^3 + 8\omega^2 - 18\omega$$

$$C_{10} = -14cs^2\omega^2 + cs^2\omega^3 - 108v_2^2\omega + 216cs^2v_2^2\omega + 42v_2^2\omega^2 - 84cs^2v_2^2\omega^2 - 24cs^2 + 6cs^2v_2^2\omega^3 - 3v_2^2\omega^3 + 72v_2^2 + 36cs^2\omega - 3cs^4\omega^3 + 48cs^4 + 108v_2^4\omega - 72v_2^4 + 30cs^4\omega^2 + 3v_2^4\omega^3 - 72cs^4\omega - 144cs^2v_2^2 - 42v_2^4\omega^2$$

$$C_{11} = 24 - 26cs^2\omega^2 + cs^2\omega^3 + 54v_2^2\omega - 22v_2^2\omega^2 - 48cs^2 + 2v_2^2\omega^3 - 36v_2^2 + 72cs^2\omega - \omega^3 + 14\omega^2 - 36\omega$$

$$C_{12} = 12 - 56cs^2\omega^2 - 12v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 12v_1^2\omega^2 + 8\omega^2 + 3v_1^2\omega^3 - 18\omega + 18v_1^2\omega$$

$$C_{13} = 36 - 56cs^2\omega^2 - 36v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 20v_1^2\omega^2 + 20\omega^2 + v_1^2\omega^3 - 54\omega + 54v_1^2\omega$$

$$C_{14} = 12 - 56cs^2\omega^2 + 4cs^2\omega^3 + 18v_2^2\omega - 12v_2^2\omega^2 - 96cs^2 + 3v_2^2\omega^3 - 12v_2^2 + 144cs^2\omega - \omega^3 + 8\omega^2 - 18\omega$$

$$C_{15} = 36 - 56cs^2\omega^2 + 4cs^2\omega^3 + 54v_2^2\omega - 20v_2^2\omega^2 - 96cs^2 + v_2^2\omega^3 - 36v_2^2 + 144cs^2\omega - \omega^3 + 20\omega^2 - 54\omega$$

$$C_{16} = -14cs^2v_3^2\omega^2 - 14v_1^2cs^2\omega^2 + 34v_1^2v_3^2\omega^2 + cs^2v_3^2\omega^3 - 3v_1^2v_3^2\omega^3 + v_1^2cs^2\omega^3 + 36v_1^2cs^2\omega - 84v_1^2v_3^2\omega - 24v_1^2cs^2 + 56v_1^2v_3^2 + 36cs^2v_3^2\omega - cs^4\omega^3 + 16cs^4 + cs^4\omega^3 + 16cs^4 + 10cs^4\omega^2 - 24cs^4\omega - 24cs^2v_3^2$$

$$C_{17} = -14cs^2v_3^2\omega^2 + cs^2v_3^2\omega^3 - 84v_3^2v_2^2\omega + 36cs^2v_2^2\omega + 34v_3^2v_2^2\omega^2 - 14cs^2v_2^2\omega^2 + cs^2v_2^2\omega^3 - 3v_3^2v_2^2\omega^3 + 36cs^2v_3^2\omega - cs^4\omega^3 + 16cs^4 + 10cs^4\omega^2 - 24cs^4\omega + 56v_3^2v_2^2 - 24cs^2v_2^2 - 24cs^2v_3^2$$

$$C_{18} = -36 + 34cs^2\omega^2 + 42v_3^2\omega^2 - 3v_3^2\omega^3 - 2cs^2\omega^3 + 72v_3^2 + 60cs^2 - 90cs^2\omega - 108v_3^2\omega + \omega^3 - 20\omega^2 + 54\omega$$

$$C_{19} = 36 - 56cs^2\omega^2 - 20v_3^2\omega^2 + v_3^2\omega^3 + 4cs^2\omega^3 - 36v_3^2 - 96cs^2 + 144cs^2\omega + 54v_3^2\omega - \omega^3 + 20\omega^2 - 54\omega$$

$$C_{20} = 12 - 56cs^2\omega^2 - 12v_3^2\omega^2 + 3v_3^2\omega^3 + 4cs^2\omega^3 - 12v_3^2 - 96cs^2 + 144cs^2\omega + 18v_3^2\omega - \omega^3 + 8\omega^2 - 18\omega$$

$$C_{21} = 36 - 56cs^2\omega^2 - 20v_3^2\omega^2 + v_3^2\omega^3 + 4cs^2\omega^3 - 36v_3^2 - 96cs^2 + 144cs^2\omega + 54v_3^2\omega - \omega^3 + 20\omega^2 - 54\omega$$

$$C_{22} = 12 - 56cs^2\omega^2 - 12v_3^2\omega^2 + 3v_3^2\omega^3 + 4cs^2\omega^3 - 12v_3^2 - 96cs^2 + 144cs^2\omega + 18v_3^2\omega - \omega^3 + 8\omega^2 - 18\omega$$

$$C_{23} = -84cs^2v_3^2\omega^2 - 14cs^2\omega^2 + 42v_3^2\omega^2 - 3v_3^2\omega^3 + cs^2\omega^3 + 6cs^2v_3^2\omega^3 + 72v_3^2 - 24cs^2 + 216cs^2v_3^2\omega + 36cs^2\omega - 108v_3^2\omega + 3v_3^4\omega^3 - 3cs^4\omega^3 - 72v_3^4 + 48cs^4 + 30cs^4\omega^2 - 42v_3^4\omega^2 - 72cs^4\omega + 108v_3^4\omega - 144cs^2v_3^2$$

$$C_{24} = 24 - 26cs^2\omega^2 - 22v_3^2\omega^2 + 2v_3^2\omega^3 + cs^2\omega^3 - 36v_3^2 - 48cs^2 + 72cs^2\omega + 54v_3^2\omega - \omega^3 + 14\omega^2 - 36\omega$$

## 2.2 MRT1

### 2.2.1 Definitions

Collision operator  $C$ :

$$C(\mathbf{f}) = \mathbf{M}^{-1} \mathbf{S} (\boldsymbol{\mu}^{(eq)} - \mathbf{M} \mathbf{f}),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2).$$

### 2.2.2 Conservation of mass equation

 attached text file: output\_d3q7\_ade\_mrt1\_symbolic\_pde\_00.txt

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\
& (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\delta_t \omega_2} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_1 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{\rho \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{\rho \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_2 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\
& (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho \delta_l^2}{2\omega_3 \delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{v_2 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{\rho \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + \\
& (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_3 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{v_3 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + \\
& (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\rho \delta_l^2}{2\delta_t \omega_4} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial t} \frac{\partial^2 v_1}{\partial x_1} + \\
& (-2 + \omega_2) \frac{cs^2 \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho \delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_2 v_1 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + \\
& (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho \delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + \\
& (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_3 v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + \\
& (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{v_3 v_2 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_4) \frac{cs^2 \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_3^2} + \\
& (-2 + \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_3}{\partial x_3^2} + (12 - 12\omega_2 + \omega_2^2) \frac{\delta_t \rho \delta_l}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_5 \omega_2 - 6\omega_5 - 6\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_5 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + C_1 \frac{v_1 \delta_l^3}{6\delta_t \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& C_2 \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^3} + (12 + \omega_3^2 - 12\omega_3) \frac{\delta_t \rho \delta_l}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + (3\omega_3^2 - 6\omega_3 + 9\omega_3 \omega_2 - 2\omega_3^2 \omega_2 - 6\omega_2) \frac{v_2 \rho \delta_l^2}{6\omega_3^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + \\
& (-2\omega_3 \omega_2^2 - 6\omega_3 + 9\omega_3 \omega_2 - 6\omega_2 + 3\omega_2^2) \frac{v_1 \rho \delta_l^2}{6\omega_3 \omega_2^2} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + C_3 \frac{v_2 \delta_l^3}{2\omega_3^2 \delta_t \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& (-6\omega_3 \omega_2^2 + 6\omega_3^2 - 6\omega_3 \omega_2 + \omega_3^2 \omega_2 + 6\omega_2^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (6v_1^2 \omega_2^2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 + 18cs^2 \omega_5 \omega_2 + 6cs^2 \omega_2^2 - 12v_1^2 \omega_2 + 12v_1^2 \omega_5 + v_1^2 \omega_5 \omega_2^2 - 6v_1^2 \omega_5 \omega_2 - 12cs^2 \omega_5) \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} \\
& + (12 - 6\omega_6 - 6\omega_3 + \omega_6 \omega_3) \frac{v_2 \rho \delta_l^2}{6\omega_6 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\omega_6 \omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-12\omega_6 cs^2 + 18\omega_6 \omega_3 cs^2 - 12\omega_3 v_2^2 + 6\omega_3^2 cs^2 + \\
& \omega_6 \omega_3^2 v_2^2 + 12\omega_6 v_2^2 - 6\omega_6 \omega_3 v_2^2 - 12\omega_3 cs^2 + 6\omega_3^2 v_2^2 - 3\omega_6 \omega_3^2 cs^2) \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-6\omega_3 \omega_2^2 + 6\omega_3^2 - 6\omega_3 \omega_2 + \omega_3^2 \omega_2 + 6\omega_2^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\delta_t \rho \delta_l}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (9\omega_4 \omega_2 - 6\omega_4 + 3\omega_4^2 - 6\omega_2 - 2\omega_4^2 \omega_2) \frac{v_3 \rho \delta_l^2}{6\omega_4^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (9\omega_4 \omega_2 - 2\omega_4 \omega_2^2 - 6\omega_4 - 6\omega_2 + 3\omega_2^2) \frac{v_1 \rho \delta_l^2}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3 \delta_l^3}{2\delta_t \omega_4^2 \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_4 \omega_2^2 + \omega_4^2 \omega_2^2 + 6\omega_4^2 - 6\omega_4^2 \omega_2 + 6\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\delta_t \omega_4^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (6v_1^2\omega_2^2 - 3cs^2\omega_5\omega_2^2 - 12cs^2\omega_2 + 18cs^2\omega_5\omega_2 + 6cs^2\omega_2^2 - 12v_1^2\omega_5 + v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_5\omega_2 - 12cs^2\omega_5) \frac{\rho\delta_l^3}{12\delta_t\omega_5\omega_2^2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} \\
& + (-6\omega_3 + 9\omega_3\omega_4 - 2\omega_3\omega_4^2 - 6\omega_4 + 3\omega_4^2) \frac{v_3\rho\delta_l^2}{6\omega_3\omega_4^2} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (3\omega_3^2 - 6\omega_3 + 9\omega_3\omega_4 - 6\omega_4 - 2\omega_3^2\omega_4) \frac{v_2\rho\delta_l^2}{6\omega_3^2\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_3\omega_4^2\omega_2 + \omega_3^2\omega_4\omega_2 - 2\omega_3^2\omega_4\omega_2^2 - 2\omega_3\omega_4^2\omega_2^2 + \omega_3\omega_4\omega_2^2 + \omega_3^2\omega_4^2 + \omega_4^2\omega_2^2 + \omega_3^2\omega_4^2\omega_2^2 - 2\omega_3^2\omega_4^2\omega_2 + \omega_3^2\omega_4^2) \frac{2v_3v_2v_1\delta_l^3}{\omega_3^2\delta_t\omega_4^2\omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (3\omega_3^2 + 6\omega_3\omega_4 - 6\omega_3\omega_4^2 + 2\omega_3^2\omega_4^2 + 3\omega_4^2 - 6\omega_3^2\omega_4) \frac{v_3v_2\rho\delta_l^3}{3\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (6\omega_4\omega_2 - 6\omega_4\omega_2^2 + 2\omega_4^2\omega_2^2 + 3\omega_4^2 - 6\omega_4^2\omega_2 + 3\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{3\delta_t\omega_4^2\omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_3\omega_2^2 + 3\omega_3^2 + 6\omega_3\omega_2 - 6\omega_3^2\omega_2 + 2\omega_3^2\omega_2^2 + 3\omega_2^2) \frac{v_2v_1\rho\delta_l^3}{3\omega_3^2\delta_t\omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (6\omega_3^2 - 6\omega_3\omega_4^2 + \omega_3^2\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4) \frac{v_3v_2\rho\delta_l^3}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + (-12\omega_6cs^2 + 18\omega_6\omega_3cs^2 - 12\omega_3v_2^2 + 6\omega_3^2cs^2 + \omega_6\omega_3^2v_2^2 + \\
& 12\omega_6v_2^2 - 6\omega_6\omega_3v_2^2 - 12\omega_3cs^2 + 6\omega_3^2v_2^2 - 3\omega_6\omega_3^2cs^2) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (12 - 6\omega_7 - 6\omega_4 + \omega_7\omega_4) \frac{v_3\rho\delta_l^2}{6\omega_7\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_3^2} + \\
& C_9 \frac{v_1\delta_l^3}{2\delta_t\omega_7\omega_4^2\omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-6v_3^2\omega_7\omega_4 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 + v_3^2\omega_7\omega_4^2 - 12v_3^2\omega_4 + 6v_3^2\omega_4^2 + 18\omega_7\omega_4cs^2 + \\
& 12v_3^2\omega_7 - 12\omega_4cs^2) \frac{\rho\delta_l^3}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-6\omega_4\omega_2^2 + \omega_4^2\omega_2^2 + 6\omega_4^2 - 6\omega_4^2\omega_2 + 6\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{6\delta_t\omega_4^2\omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + \\
& C_{10} \frac{v_2\delta_l^3}{2\omega_3^2\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + (-6v_3^2\omega_7\omega_4 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 + v_3^2\omega_7\omega_4^2 - 12v_3^2\omega_4 + 6v_3^2\omega_4^2 + 18\omega_7\omega_4cs^2 + \\
& 12v_3^2\omega_7 - 12\omega_4cs^2) \frac{\rho\delta_l^3}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (6\omega_3^2 - 6\omega_3\omega_4^2 + \omega_3^2\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4) \frac{v_3v_2\rho\delta_l^3}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3\delta_l^3}{6\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& C_{12} \frac{\rho\delta_l^3}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_3}{\partial x_3^3} + (-2 + 3\omega_2 - \omega_2^2) \frac{\delta_l^2\rho\delta_l}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + \\
& (-4\omega_5\omega_2 + 2\omega_5^2 - 2\omega_5\omega_3^2 + 8\omega_5\omega_2^2 - \omega_5^2\omega_2^2 + 2\omega_3^3 - \omega_5^2\omega_2 - 4\omega_2^2) \frac{\delta_t v_1 \rho \delta_l^2}{2\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\rho\delta_l^3}{12\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + \\
& C_{14} \frac{\delta_l^4}{24\delta_t\omega_5^2\omega_3^2} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{v_1\rho\delta_l^4}{12\delta_t\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3\omega_3) \frac{\delta_l^2\rho\delta_l}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (-24\omega_3\omega_2^2 + 12\omega_3^2 - 6\omega_3^3 + 12\omega_3\omega_2 - 24\omega_3^2\omega_2 - \omega_3^3\omega_2^2 + 7\omega_3^3\omega_2 + 13\omega_3^2\omega_2^2 + 12\omega_2^2) \frac{\delta_t v_2 \rho \delta_l^2}{12\omega_3^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-24\omega_3\omega_2^2 + 12\omega_3^2 + 7\omega_3\omega_3^2 + 12\omega_3\omega_2 - 24\omega_3^2\omega_2 - \omega_3^2\omega_3^2 - 6\omega_3^3 + 13\omega_3^2\omega_2^2 + 12\omega_2^2) \frac{\delta_t v_1 \rho \delta_l^2}{12\omega_3^2\omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& C_{16} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^2\omega_5\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{\rho\delta_l^3}{12\omega_3\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{18} \frac{v_2v_1\delta_l^4}{6\omega_3^2\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_2v_1\delta_l^4}{12\omega_3^2\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& C_{20} \frac{v_1\rho\delta_l^4}{12\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + (-4\omega_3^2 - 4\omega_6\omega_3 + 2\omega_3^3 + 2\omega_6^2 + 8\omega_6\omega_3^2 - 2\omega_6\omega_3^3 - \omega_6^2\omega_3^2 - \omega_6\omega_3) \frac{\delta_t v_2 \rho \delta_l^2}{2\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + \\
& C_{21} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^3\omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + C_{22} \frac{v_2v_1\rho\delta_l^3}{6\omega_6\omega_3^3\omega_2^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + C_{23} \frac{\delta_l^4}{4\omega_6^2\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{v_1\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& C_{25} \frac{v_2v_1\delta_l^4}{12\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^3} + C_{27} \frac{v_2v_1\delta_l^4}{6\omega_6^2\omega_3^3\delta_t\omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_{28} \frac{v_2v_1\delta_l^4}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{29} \frac{v_1\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} \\
& + C_{30} \frac{\delta_l^4}{24\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{31} \frac{v_2v_1\delta_l^4}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 + 3\omega_4 - \omega_4^2) \frac{\delta_l^2\rho\delta_l}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (12\omega_4\omega_2 - 24\omega_4\omega_2^2 + 7\omega_4^3\omega_2 - 6\omega_4^3 + 13\omega_4^2\omega_2^2 + 12\omega_4^2 - 24\omega_4^2\omega_2 - \omega_4^3\omega_2^2 + 12\omega_2^2) \frac{\delta_t v_3 \rho \delta_l^2}{12\omega_4^2\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (12\omega_4\omega_2 - 24\omega_4\omega_2^2 + 7\omega_4\omega_3^2 - \omega_4^2\omega_3^2 + 13\omega_4^2\omega_2^2 + 12\omega_4^2 - 6\omega_4^3 - 24\omega_4^2\omega_2 + 12\omega_2^2) \frac{\delta_t v_1 \rho \delta_l^2}{12\omega_4^2\omega_2^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& C_{32} \frac{v_3v_1\rho\delta_l^3}{6\omega_4^2\omega_5\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + C_{33} \frac{\rho\delta_l^3}{12\omega_4\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{34} \frac{v_3v_1\delta_l^4}{6\delta_t\omega_4^2\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{35} \frac{v_3\rho\delta_l^4}{12\delta_t\omega_4^2\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& C_{36} \frac{v_1\rho\delta_l^4}{12\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (12\omega_3^2 + 12\omega_3\omega_4 - 24\omega_3\omega_4^2 + 7\omega_3\omega_4^3 - \omega_3^2\omega_4^3 - 6\omega_4^3 + 13\omega_3^2\omega_4^2 + 12\omega_4^2 - 24\omega_3^2\omega_4) \frac{\delta_t v_3 \rho \delta_l^2}{12\omega_3^2\omega_4^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (12\omega_3^2 - 6\omega_3^3 + 12\omega_3\omega_4 - 24\omega_3\omega_4^2 + 7\omega_3\omega_4^3 + 13\omega_3^2\omega_4^2 + 12\omega_4^2 - 24\omega_3^2\omega_4 - \omega_3^3\omega_4) \frac{\delta_t v_2 \rho \delta_l^2}{12\omega_3^3\omega_4^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_3v_2\rho\delta_l^3}{6\omega_3^3\omega_5\omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{38} \frac{v_3v_1\rho\delta_l^3}{6\omega_3\omega_5^2\omega_2^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{39} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^2\omega_4\omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{40} \frac{v_3v_2\delta_l^4}{\omega_3^2\delta_t\omega_4^2\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{41} \frac{v_3v_2v_1\rho\delta_l^4}{6\omega_3^3\delta_t\omega_4^2\omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{42} \frac{v_3\rho\delta_l^4}{12\delta_t\omega_4^2\omega_5^2\omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{43} \frac{v_2v_1\delta_l^4}{12\omega_3^3\delta_t\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{44} \frac{v_3v_2\rho\delta_l^4}{6\omega_6\omega_3^3\omega_4^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^3\omega_4} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{46} \frac{v_3v_1\delta_l^4}{\omega_6^2\omega_3^3\delta_t\omega_4^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{47} \frac{v_3\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_4^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{48} \frac{v_3v_2v_1\rho\delta_l^4}{6\omega_3^3\delta_t\omega_4^2\omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{49} \frac{v_1\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{50} \frac{v_3v_2\delta_l^4}{6\omega_6^2\omega_3^3\delta_t\omega_4^2} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{51} \frac{v_3\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_4^2} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{52} \frac{v_2\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-\omega_7^2 \omega_4 - \omega_7^2 \omega_4^2 + 2\omega_4^3 - 2\omega_7 \omega_4^3 + 8\omega_7 \omega_4^2 - 4\omega_4^2 - 4\omega_7 \omega_4 + 2\omega_7^2) \frac{\delta_t v_3 \rho \delta_l^2}{2\omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + C_{53} \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3 \omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + \\
C_{54} & \frac{v_3 v_1 \rho \delta_l^3}{6\omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + C_{55} \frac{\delta_l^4}{4\delta_t \omega_7^2 \omega_3^2 \omega_5^2 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{56} \frac{v_1 \rho \delta_l^4}{12\delta_t \omega_7^2 \omega_3^2 \omega_5^2 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{57} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_4^3 \omega_5^2 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
C_{58} & \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + C_{59} \frac{v_3 v_2 \rho \delta_l^3}{6\omega_3^3 \omega_7 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + C_{60} \frac{v_2 v_1 \delta_l^4}{\omega_3^3 \delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{61} \frac{v_2 \rho \delta_l^4}{12\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
C_{62} & \frac{v_1 \rho \delta_l^4}{12\delta_t \omega_7^2 \omega_3^2 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{63} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{64} \frac{\delta_l^4}{4\omega_6^2 \omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{65} \frac{v_2 \rho \delta_l^4}{12\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
C_{66} & \frac{v_3 \rho \delta_l^4}{12\omega_6^2 \omega_3^3 \delta_t \omega_4^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{67} \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3^2} + C_{68} \frac{v_3 v_1 \delta_l^4}{6\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + C_{69} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{70} \frac{v_1 \rho \delta_l^4}{12\delta_t \omega_7^2 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^2} + \\
& + C_{71} \frac{v_3 v_2 \delta_l^4}{6\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^2} + C_{72} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2 \omega_3^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^2} + C_{73} \frac{v_2 \rho \delta_l^4}{12\omega_3^3 \delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^2} + C_{74} \frac{\delta_l^4}{24\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 \rho}{\partial x_3^2} + C_{75} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial x_3^2} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -3\omega_5 \omega_2 + 3v_1^2 \omega_2^2 - 3cs^2 \omega_5 \omega_2^2 - 6cs^2 \omega_2 + 15cs^2 \omega_5 \omega_2 + 3cs^2 \omega_2^2 + \omega_5 \omega_2^2 - 6v_1^2 \omega_2 - v_1^2 \omega_5 \omega_2^2 + 3v_1^2 \omega_5 \omega_2 + 6\omega_2 - 12cs^2 \omega_5 - 3\omega_2^2 \\
C_2 &= -6\omega_5 \omega_2 + 6v_1^2 \omega_2^2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 + 18cs^2 \omega_5 \omega_2 + 6cs^2 \omega_2^2 + 2\omega_5 \omega_2^2 - 12v_1^2 \omega_2 - 12v_1^2 \omega_5 - 5v_1^2 \omega_5 \omega_2^2 + 18v_1^2 \omega_5 \omega_2 + 12\omega_2 - 12cs^2 \omega_5 - 6\omega_2^2 \\
C_3 &= \omega_3^2 v_1^2 \omega_2^2 - 3\omega_3 v_1^2 \omega_5 \omega_2^2 - \omega_3^2 c s^2 \omega_5 \omega_2^2 - 2\omega_3^2 c s^2 \omega_2 + \omega_3^2 c s^2 \omega_2^2 + 4\omega_3^2 c s^2 \omega_5 \omega_2 + 2\omega_3 v_1^2 \omega_5 \omega_2 - 2\omega_3^2 v_1^2 \omega_2 + \omega_3 c s^2 \omega_5 \omega_2^2 + 4\omega_3^2 v_1^2 \omega_5 \\
&+ \omega_3^2 v_1^2 \omega_5 \omega_2^2 + 2v_1^2 \omega_5 \omega_2^2 - 4\omega_3^2 v_1^2 \omega_5 \omega_2 - 2\omega_3 c s^2 \omega_5 \omega_2 - 2\omega_3^2 c s^2 \omega_5 \\
C_4 &= -\omega_6 \omega_3^2 c s^2 \omega_2^2 + \omega_6 \omega_3^2 v_1^2 \omega_2^2 + \omega_3^2 c s^2 \omega_2^2 + \omega_3^2 v_2^2 \omega_2^2 - 3\omega_6 \omega_3^2 v_1^2 \omega_2^2 + \omega_6 \omega_3^2 c s^2 \omega_2 + 2\omega_6 \omega_3^2 v_2^2 - 2\omega_3 c s^2 \omega_2^2 - 2\omega_3 v_2^2 \omega_2^2 + 2\omega_6 \omega_3 v_2^2 \omega_2 - \\
&2\omega_6 \omega_3 c s^2 \omega_2 + 4\omega_6 \omega_3 c s^2 \omega_2^2 - 4\omega_6 \omega_3 v_2^2 \omega_2^2 + 4\omega_6 v_2^2 \omega_2^2 - 2\omega_6 c s^2 \omega_2^2 \\
C_5 &= -12\omega_6 c s^2 + 15\omega_6 \omega_3 c s^2 - 3\omega_3^2 + 6\omega_3 - 3\omega_6 \omega_3 - 6\omega_3 v_2^2 + \omega_6 \omega_3^2 + 3\omega_3^2 c s^2 - \omega_6 \omega_3^2 v_2^2 + 3\omega_6 \omega_3 v_2^2 - 6\omega_3 c s^2 + 3\omega_3^2 v_2^2 - 3\omega_6 \omega_3^2 c s^2 \\
C_6 &= -12\omega_6 c s^2 + 18\omega_6 \omega_3 c s^2 - 6\omega_3^2 + 12\omega_3 - 6\omega_6 \omega_3 - 12\omega_3 v_2^2 + 2\omega_6 \omega_3 + 6\omega_3^2 c s^2 - 5\omega_6 \omega_3^2 v_2^2 - 12\omega_6 v_2^2 + 18\omega_6 \omega_3 v_2^2 - 12\omega_3 c s^2 + 6\omega_3^2 v_2^2 - 3\omega_6 \omega_3^2 c s^2 \\
C_7 &= -2v_1^2 \omega_4^2 \omega_2 - 4v_1^2 \omega_4^2 \omega_5 \omega_2 - \omega_4^2 c s^2 \omega_5 \omega_2^2 + 4\omega_4^2 c s^2 \omega_5 \omega_2 + v_1^2 \omega_4^2 \omega_5 \omega_2^2 + v_1^2 \omega_4^2 \omega_2^2 - 2\omega_4^2 c s^2 \omega_5 - 3v_1^2 \omega_4 \omega_5 \omega_2^2 + \omega_4 c s^2 \omega_5 \omega_2^2 - 2\omega_4^2 c s^2 \omega_2 + \\
&2v_1^2 \omega_5 \omega_2^2 + \omega_4^2 c s^2 \omega_2^2 - 2\omega_4 c s^2 \omega_5 \omega_2 + 4v_1^2 \omega_4^2 \omega_5 + 2v_1^2 \omega_4 \omega_5 \omega_2 \\
C_8 &= \omega_3^2 v_2^2 \omega_4^2 + \omega_3^2 \omega_4^2 c s^2 - 3\omega_6 \omega_3^2 v_2^2 \omega_4 - 2\omega_6 \omega_3 \omega_4 c s^2 + 2\omega_6 \omega_3^2 v_2^2 + \omega_6 \omega_3^2 v_2^2 \omega_4^2 - \omega_6 \omega_3^2 \omega_4^2 c s^2 + \omega_6 \omega_3^2 \omega_4 c s^2 - 4\omega_6 \omega_3 v_2^2 \omega_4^2 - 2\omega_6 \omega_4^2 c s^2 + \\
&4\omega_6 \omega_3 \omega_4^2 c s^2 + 4\omega_6 v_2^2 \omega_4^2 - 2\omega_3 v_2^2 \omega_4^2 + 2\omega_6 \omega_3 v_2^2 \omega_4 - 2\omega_3 \omega_4^2 c s^2 \\
C_9 &= -2\omega_4 c s^2 \omega_2^2 - 2\omega_7 \omega_4 c s^2 \omega_2 + 4v_3^2 \omega_7 \omega_2^2 + v_3^2 \omega_7 \omega_4^2 \omega_2^2 - 3v_3^2 \omega_7 \omega_4^2 \omega_2 + 2v_3^2 \omega_7 \omega_4^2 \omega_2^2 + 4\omega_7 \omega_4 c s^2 \omega_2^2 - 2\omega_7 c s^2 \omega_2^2 + v_3^2 \omega_4^2 \omega_2^2 - 2v_3^2 \omega_4 \omega_2^2 + \\
&2v_3^2 \omega_7 \omega_4 \omega_2 - \omega_7 \omega_4^2 c s^2 \omega_2^2 + \omega_4^2 c s^2 \omega_2^2 - 4v_3^2 \omega_7 \omega_4 \omega_2^2 + \omega_7 \omega_4^2 c s^2 \omega_2 \\
C_{10} &= \omega_3^2 \omega_4^2 c s^2 - 4\omega_3^2 v_3^2 \omega_7 \omega_4 - \omega_3^2 \omega_7 \omega_4^2 c s^2 - 2\omega_3^2 \omega_7 c s^2 - 2\omega_3 \omega_7 \omega_4 c s^2 + 2v_3^2 \omega_7 \omega_4^2 + \omega_3^2 v_3^2 \omega_7 \omega_4^2 + 2\omega_3 v_3^2 \omega_7 \omega_4 - 2\omega_3^2 v_3^2 \omega_4 + \omega_3 \omega_7 \omega_4^2 c s^2 + \\
&4\omega_3^2 \omega_7 \omega_4 c s^2 + \omega_3^2 v_3^2 \omega_4^2 + 4\omega_3^2 v_3^2 \omega_7 - 3\omega_3 v_3^2 \omega_7 \omega_4^2 - 2\omega_3^2 \omega_4 c s^2 \\
C_{11} &= 3v_3^2 \omega_7 \omega_4 + 3\omega_4^2 c s^2 - 3\omega_7 \omega_4^2 c s^2 - 12\omega_7 c s^2 - v_3^2 \omega_7 \omega_4^2 + 6\omega_4 + \omega_7 \omega_4^2 - 6v_3^2 \omega_4 - 3\omega_4^2 - 3\omega_7 \omega_4 + 3v_3^2 \omega_4^2 + 15\omega_7 \omega_4 c s^2 - 6\omega_4 c s^2 \\
C_{12} &= 18v_3^2 \omega_7 \omega_4 + 6\omega_4^2 c s^2 - 3\omega_7 \omega_4^2 c s^2 - 12\omega_7 c s^2 - 5v_3^2 \omega_7 \omega_4^2 + 12\omega_4 + 2\omega_7 \omega_4^2 - 12v_3^2 \omega_4 - 6\omega_4^2 - 6\omega_7 \omega_4 + 6v_3^2 \omega_4^2 + 18\omega_7 \omega_4 c s^2 - 12v_3^2 \omega_7 - 12\omega_4 c s^2 \\
C_{13} &= -24\omega_5 \omega_2 + 12v_1^2 \omega_2^2 + 9c s^2 \omega_5 \omega_3^2 - 6v_1^2 \omega_3^2 - 42v_1^2 \omega_5 \omega_2^2 - 36c s^2 \omega_5 \omega_2^2 + 24c s^2 \omega_5 \omega_2 + 12c s^2 \omega_2^2 + 27v_1^2 \omega_5 \omega_2^2 - 9\omega_5 \omega_2^3 - 6c s^2 \omega_2^3 + 36\omega_5 \omega_2^2 - \\
&3v_1^2 \omega_5 \omega_2^3 + 15v_1^2 \omega_5 \omega_2^2 + 24c s^2 \omega_5^2 - 11\omega_5 \omega_2^2 - 48c s^2 \omega_5 \omega_2 + \omega_5^2 \omega_2^3 - 60v_1^2 \omega_5 \omega_2^2 + 48v_1^2 \omega_5 \omega_2 + 12v_1^2 \omega_5^2 + 25c s^2 \omega_5 \omega_2^2 + 6\omega_2^3 + 12\omega_5^2 \omega_2 - 12\omega_2^2 - 2c s^2 \omega_5 \omega_2^3 \\
C_{14} &= 24c s^4 \omega_5 \omega_2 + 24v_1^2 \omega_2^2 - 6c s^2 \omega_5 \omega_2^3 - 24v_1^2 \omega_5 \omega_2^2 - 12v_1^2 \omega_3^2 - 24v_1^2 \omega_5 \omega_2 + 3v_1^4 \omega_5 \omega_2^3 + 24c s^2 \omega_5 \omega_2^2 + 24c s^4 \omega_5^2 + 156v_1^2 c s^2 \omega_5 \omega_2^2 - \\
&24c s^2 \omega_5 \omega_2 - 72v_1^2 c s^2 \omega_5 \omega_2^2 - 96v_1^2 c s^2 \omega_5^2 + 24v_1^2 \omega_5 \omega_2^2 + 6c s^4 \omega_5 \omega_2^3 + 6v_1^2 c s^2 \omega_5 \omega_2^3 + 24v_1^2 \omega_5 \omega_2^2 - 3v_1^2 \omega_5 \omega_2^3 - 12v_1^2 c s^2 \omega_5 \omega_2^3 - \\
&24v_1^2 c s^2 \omega_5 \omega_2^2 + 12v_1^2 \omega_5^2 - 48v_1^2 \omega_5 \omega_2 + 18v_1^2 \omega_5 \omega_2^3 + 24c s^4 \omega_5 \omega_2^2 + 12c s^2 \omega_5 \omega_2^2 - 24v_1^2 \omega_5^2 + 12v_1^2 c s^2 \omega_5 \omega_2^3 + 48v_1^2 c s^2 \omega_5 \omega_2^2 - 3c s^4 \omega_5 \omega_2^3 - 72v_1^2 \omega_5 \omega_2^2 + \\
&48v_1^2 \omega_5 \omega_2 - 8c s^2 \omega_5 \omega_2^2 - 18v_1^2 \omega_5 \omega_2^3 - 24v_1^2 c s^2 \omega_5 \omega_2 - 48c s^4 \omega_5 \omega_2^2 + 72v_1^2 \omega_5 \omega_2^2 + c s^2 \omega_5 \omega_2^3 \\
C_{15} &= 12\omega_5 \omega_2 - 12v_1^2 \omega_2^2 - 6c s^2 \omega_5 \omega_2^3 + 6v_1^2 \omega_2^3 + 24v_1^2 \omega_5 \omega_2^2 + 24c s^2 \omega_5 \omega_2^2 - 12c s^2 \omega_5 \omega_2 - 12c s^2 \omega_2^2 - 16v_1^2 \omega_5 \omega_2^2 + 6\omega_5 \omega_2^3 + 6c s^2 \omega_2^2 - 24\omega_5 \omega_2^2 + \\
&2v_1^2 \omega_5 \omega_2^3 - 6v_1^2 \omega_5 \omega_2^2 - 24c s^2 \omega_5^2 + 8\omega_5 \omega_2^2 + 42c s^2 \omega_5 \omega_2 - \omega_5^2 \omega_2^3 + 24v_1^2 \omega_5 \omega_2^2 - 12v_1^2 \omega_5 \omega_2 - 12v_1^2 \omega_5^2 - 20c s^2 \omega_5 \omega_2^2 - 6\omega_5^2 \omega_2 + 12\omega_2^2 + c s^2 \omega_5 \omega_2^3 \\
C_{16} &= -12\omega_3^2 \omega_5 \omega_2 - 12\omega_3^2 \omega_5 \omega_3^2 - 7\omega_3^2 \omega_5 \omega_2^3 - 6\omega_5 \omega_2^3 + 12\omega_3^2 \omega_5 \omega_2^2 + 12\omega_3 \omega_5 \omega_2^3 + 3\omega_3^2 \omega_2^3 + 24\omega_3^2 \omega_5 \omega_2 - 6\omega_3^2 \omega_2^2 - 6\omega_3 \omega_5 \omega_2^2 - 10\omega_3^2 \omega_5 \omega_2^2 - \\
&6\omega_3^2 \omega_2^3 + \omega_3^2 \omega_5 \omega_2^3 + 12\omega_3^2 \omega_2^2 \\
C_{17} &= 9\omega_3 v_1^2 \omega_5 \omega_2^3 - 6c s^2 \omega_5 \omega_2^3 - 24\omega_3 v_1^2 \omega_5^2 - 12v_1^2 \omega_5 \omega_2^2 - 30\omega_3 v_1^2 \omega_5 \omega_2^2 + 12c s^2 \omega_5 \omega_2^2 - 30\omega_3 c s^2 \omega_5 \omega_2^2 + 22\omega_3 c s^2 \omega_5 \omega_2^2 + 12\omega_3 v_1^2 \omega_5 \omega_2 + \\
&6v_1^2 \omega_5 \omega_2^2 + 12\omega_3 c s^2 \omega_5^2 - 2\omega_3 c s^2 \omega_5 \omega_2^3 - v_1^2 \omega_5 \omega_2^3 + 12\omega_3 c s^2 \omega_5 \omega_2^2 + 9\omega_3 c s^2 \omega_5 \omega_2^3 - 6v_1^2 \omega_5 \omega_2^3 - 30\omega_3 c s^2 \omega_5 \omega_2^2 + 12c s^2 \omega_5 \omega_2^2 - 6\omega_3 c s^2 \omega_2^3 + \\
&36\omega_3 v_1^2 \omega_5 \omega_2^2 + 12v_1^2 \omega_5 \omega_2^2 + 12\omega_3 v_1^2 \omega_5 \omega_2^2 - 10\omega_3 v_1^2 \omega_5 \omega_2^2 - 18c s^2 \omega_5 \omega_2^2 + 12\omega_3 c s^2 \omega_5 \omega_2 + \omega_3 v_1^2 \omega_5 \omega_2^3 - 6\omega_3 v_1^2 \omega_2^3 + 3c s^2 \omega_5 \omega_2^3 \\
C_{18} &= -\omega_3^3 \omega_5 \omega_2^3 + 6\omega_3^2 c s^2 \omega_5 \omega_2^2 - 36\omega_3^2 c s^2 \omega_5^2 + 12\omega_3^2 v_1^2 \omega_5 \omega_2^2 + 7\omega_3^2 \omega_5 \omega_2^2 - 24\omega_3^2 c s^2 \omega_5 \omega_2^2 - 12\omega_3^2 c s^2 \omega_5 \omega_2^2 + 6\omega_3^2 v_1^2 \omega_5 \omega_2^2 - 12\omega_3 c s^2 \omega_5 \omega_2^2 + \\
&30\omega_3^2 v_1^2 \omega_5 \omega_2^2 + 42\omega_3^2 c s^2 \omega_5 \omega_2^2 - 6\omega_3^2 \omega_5 \omega_2^2 - 12\omega_3^2 v_1^2 \omega_5 \omega_2^2 - 3\omega_3^2 \omega_5 \omega_2^2 + 24\omega_3^2 v_1^2 \omega_5 \omega_2^2 + 6\omega_3 c s^2 \omega_5 \omega_2^2 + 6\omega_3^2 \omega_5 \omega_2^2 - 12\omega_3^2 c s^2 \omega_5 \omega_2^2 +
\end{aligned}$$





$$\begin{aligned}
C_{47} = & -12w_6^2w_3^2w_4cs^2 + 4w_6^2w_3^3w_4cs^2 - 90w_6^2w_3v_2^2w_4^3 + 36w_6w_3^2w_4^3cs^2 - 12w_3^2v_2^2w_4^3 - 24w_6^2w_3w_4^2cs^2 - 30w_6^2w_3^3v_2^2w_4 - 12w_6^2w_3^4cs^2 + \\
& 48w_6^2w_3v_2^2w_4^2 - 12w_3^2w_4^3cs^2 + 24w_6^2w_3^2v_2^2w_4^2 + 36w_6w_3^2v_2^2w_4^3 - 12w_6^2w_3^2w_4^2cs^2 + 48w_6^2v_2^2w_4^3 - 5w_6^2w_3^2v_2^2w_4^3 - 24w_6w_3^2v_2^2w_4^2 + 36w_6^2w_3w_4^3cs^2 - \\
& 24w_6w_3^2w_4^2cs^2 + 24w_6^2w_3^2v_2^2w_4 - 12w_6w_3v_2^2w_4^3 + 6w_3^2v_2^2w_4^3 - 12w_6w_3^2w_4^3cs^2 + 6w_6^2w_3^2w_4cs^2 - 32w_6^2w_3^2w_4^3cs^2 + 12w_6w_3^2w_4^2cs^2 + 12w_6w_3^3v_2^2w_4^2 + \\
& 40w_6^2w_3^2v_2^2w_4^3 + 48w_6^2w_3^2w_4^2cs^2 - 12w_6w_3w_4^3cs^2 - 12w_6w_3^2v_2^2w_4^3 + 6w_3^2w_4^3cs^2 - 60w_6^2w_3^2v_2^2w_4^2 + 12w_6^2w_3^2v_2^2
\end{aligned}$$

$$\begin{aligned} C_{48} = & -36w_3^3w_4^3w_2^3 - 42w_3^3w_4^2w_2^2 - 30w_3^3w_4^3w_2 + 24w_3^3w_4^2w_2^3 + 18w_3w_4^3w_2^2 + 24w_3^3w_4^3w_2^2 + 18w_3w_4^2w_2^3 + 6w_2^3w_4w_2^3 + 18w_3^3w_4^2w_2 - 5w_3^3w_4^3w_2^3 - \\ & 30w_2^3w_4^2w_2^3 + 6w_3^2w_4^3w_2 + 12w_3^3w_2^3 + 12w_2^3w_4^2w_2^2 - 30w_3^2w_4w_2^3 + 28w_3^2w_4^3w_2^3 + 12w_3^2w_4^3 + 12w_4^2w_2^3 - 30w_3^2w_4^3w_2^2 + 18w_3^2w_4w_2^2 \end{aligned}$$

$$\begin{aligned}
C_{49} = & 36w_6w_3^2cs^2w_3^2 + 24w_6^2w_3^3v_2^2w_2^2 - 12w_6^2w_3^3cs^2w_2^2 + 36w_6w_3^2v_2^2w_3^2 + 48w_6^2v_2^2w_3^2 - 12w_6^2cs^2w_3^2 - 5w_6^2w_3^3v_2^2w_3^2 - 24w_6w_3^2cs^2w_2^2 - \\
& 24w_6w_3^2v_2^2w_2^2 + 4w_6^2w_3^3cs^2w_3^2 + 36w_6^2w_3cs^2w_3^2 - 90w_6^2w_3v_2^2w_3^2 - 12w_3^2cs^2w_3^2 - 12w_3^2v_2^2w_3^2 + 6w_6^2w_3^3cs^2w_2^2 - 30w_6^2w_3^3v_2^2w_2 - 24w_6^2w_3cs^2w_2^2 + \\
& 48w_6^2w_3v_2^2w_2^2 + 12w_6w_3^3v_2^2w_2^2 - 32w_6^2w_3^2cs^2w_3^2 + 40w_6^2w_3^2v_2^2w_3^2 + 12w_6w_3^3cs^2w_2^2 + 48w_6^2w_3^2cs^2w_2^2 - 12w_6w_3^3v_2^2w_3^2 - 12w_6w_3^3cs^2w_3^2 - \\
& 60w_6^2v_3^2w_2^2 + 24w_6^2w_3^2v_2^2w_2 - 12w_6^2w_3^2cs^2w_2 - 12w_6w_3cs^2w_3^2 - 12w_6w_3v_2^2w_3^2 + 6w_3^3v_2^2w_3^2 + 12w_6^2w_3^3v_2^2
\end{aligned}$$

$$\begin{aligned}
C_{50} = & -12w_6^2w_3^2w_4cs^2 + 6w_6^2w_3^3w_4^2cs^2 - 30w_6^2w_3v_2^2w_4^3 + 6w_6w_3^2w_4^2 - 6w_6^2w_3w_4^3 + 42w_6w_2^2w_4^3cs^2 - 12w_2^2v_2^2w_4^3 - 24w_6^2w_3v_2^4cs^2 - 12w_6^2w_3^3v_2^2w_4 - \\
& 21w_6w_3^2w_4^3 - 36w_6^2w_3^4cs^2 + 12w_6^2w_3v_2^2w_4^2 - 3w_6w_3^2w_4^2 - 12w_3^2w_4^3cs^2 + 6w_6^2w_3^2v_2^2w_4^2 + 42w_6w_3^2v_2^2w_4^3 - 12w_6^2w_3^2w_4^2cs^2 + 24w_6^2v_2^2w_4^3 + 6w_6w_3^3w_4^3 - \\
& 12w_6w_3^2v_2^2w_4^4 + 78w_6^2w_3w_4^3cs^2 - 12w_6w_3^2w_4^2cs^2 + 6w_6^2w_3^2v_2^2w_4 + 6w_3^2w_4^3 + w_6^2w_3^2w_4^2 - 24w_6w_3v_2^2w_4^3 + 6w_3^2v_2^2w_4^3 - 12w_6w_3^2w_4^3cs^2 - w_6^2w_3^3w_4^3 + \\
& 6w_6^2w_3^2w_4cs^2 - 48w_6^2w_3^2w_4^3cs^2 + 6w_6w_3^2w_4^2cs^2 + 12w_6w_3w_4^3 - 3w_6^2w_3^2w_4^2 + 6w_6w_3^2v_2^2w_4^2 + 6w_6^2w_3^2v_2^2w_4^3 - 3w_3^2w_4^3 + 42w_6w_3^2w_4^2cs^2 - \\
& 24w_6w_3w_4^3cs^2 - 12w_6w_3^2v_2^2w_4^3 + 6w_3^2w_4^3cs^2 - 12w_6^2w_3^2v_2^2w_4 + 7w_6^2w_3^2w_4^3 + 6w_6^2w_3^2v_2^2
\end{aligned}$$

$$\begin{aligned} C_{51} = & -12w_6^2w_3^2w_4c s^2 + 4w_6^2w_3^3w_4c s^2 - 30w_6^2w_3v_2^2w_4^3 + 12w_6w_3^2w_4^4 + 36w_6w_3^2w_4^3c s^2 - 12w_3^2v_2^2w_3^3 - 24w_6^2w_3w_4^2c s^2 - 18w_6^2w_3^2v_2^2w_4 - 6w_6w_3^2w_3^4 - \\ & 12w_6^2w_3^4c s^2 - 6w_6w_3^2w_4^2 - 12w_3^2w_4^3c s^2 + 36w_6w_3^2v_2^2w_3^4 - 12w_6^2w_3^2w_4^2c s^2 + 24w_6^2v_2^2w_3^4 + 3w_6^2w_3^3v_2^2w_3^4 + 3w_6w_3^3w_4^3 - 24w_6w_3^2v_2^2w_4^2 + 36w_6^2w_3w_4^3c s^2 - \\ & 24w_6w_3^2w_4^2c s^2 + 2w_6^2w_3^3w_4^2 - 12w_6w_3v_2^2w_3^4 + 6w_3^2v_2^2w_3^4 - 12w_6w_3^2w_4^3c s^2 - w_6^2w_3^3w_4^3 + 6w_6^2w_3^2w_4c s^2 - 32w_6^2w_3^2w_4^3c s^2 + 12w_6w_3^2w_4^2c s^2 - \\ & 6w_6^2w_3^2w_4^2 + 12w_6w_3^2v_2^2w_4^2 + 48w_6^2w_3^2w_4^2c s^2 - 12w_6w_3w_4^3c s^2 - 12w_6w_3^2v_2^2w_4^3 + 6w_3^2w_4^3c s^2 + 12w_6^2w_3^2v_2^2w_4^2 + 3w_6^2w_3^2w_4^3 + 12w_6^2w_3^2v_2^2 \end{aligned}$$

$$C_{52} = 6w_3^3cs^2 - 36w_6w_3cs^2 + 12w_3^2 + 24w_6w_3 - 44w_6^2w_3^2cs^2 - 12w_6w_3^3v_2^2 - 6w_3^3 - 36w_6w_3^2 - 12w_3^2cs^2 + 12w_6^2v_2^2 + 48w_6w_3^2v_2^2 + 4w_6^2w_3^3cs^2 + 9w_6w_3^3 + 6w_3^2v_2^2 - 36w_6w_3v_2^2 - w_6^2w_3^3 - 8w_6^2w_3^2v_2^2 - 12w_6w_3^3cs^2 + 11w_6^2w_3^2 + 90w_6^2w_3cs^2 - 12w_6^2w_3 - 12w_3^2v_2^2 - 48w_6^2cs^2 + 48w_6w_3^2cs^2 + w_6^2w_3^3v_2^2$$

$$C_{53} = -12w_7w_4c_5 - 6w_4cs + 12w_3w_4w_2 + 12w_7w_4cs w_2 + 9w_3w_7w_4w_2 + 12w_7w_4cs w_2 + 22w_7w_4cs w_2 - 30w_3w_7w_4w_2 - 6v_3w_7w_4 - 6v_2^2w_3^2w_2 + 12v_3^2w_7w_4^2 + 36v_3w_7^2w_4w_2 + 9w_7w_3^4cs^2w_2 - 6w_7w_3^4cs^2 - 10v_3^2w_7^2w_4^2w_2 + 6v_3^2w_7^2w_4^2 - 30w_7w_4acs^2w_2 - v_3^2w_7^2w_4^3 + 12v_3^2w_7w_4w_2 - 24v_3^2w_7^2w_2 + 12w_4^2cs^2w_2 + 3w_7^2w_3^4cs^2 + 12w_7^2cs^2w_2 + v_3^2w_7^2w_4^2w_2 - 30w_7w_4acs^2w_2 - 18w_7w_4cs^2 - 2w_7^2w_3^4cs^2w_2 - 12v_3^2w_7^2w_4$$

$$C_{54}^4 = 24\omega_7\omega_4\omega_2 - 12\omega_7\omega_4\omega_2^2 - 6\omega_4^2\omega_2 + 12\omega_7\omega_4^2\omega_2^2 - 6\omega_7\omega_4^2 + 12\omega_4^2\omega_2^2 - 10\omega_7\omega_4^2\omega_2^2 + 12\omega_7\omega_4\omega_2 - 7\omega_7\omega_4^2\omega_2^2 - 12\omega_7\omega_2^2 + 3\omega_4^2\omega_2 + \omega_7\omega_4^3\omega_2^3 - 6\omega_7\omega_4^2\omega_2 - 6\omega_4^3\omega_2^2$$

$$\begin{aligned}
C_{55} = & 10v_3^2 v_1^7 w_7^3 w_4^2 w_5 w_2^2 + 4w_7^2 w_1^3 c s^4 w_5 w_2^2 - 3v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^3 + v_1^4 w_7 w_4^2 c s^4 w_5 w_2^3 + 20v_3^2 v_7^2 w_7^2 w_4^2 w_5 w_2^2 + 2v_1^4 w_7 w_4^2 c s^4 w_5 w_2^2 + w_7 w_4^3 c s^4 w_5 w_2^3 + \\
& 4w_7^2 w_4^2 c s^4 w_5 w_2^2 + 4v_3^2 w_7^2 w_4 c s^2 w_5 w_2^3 - 4v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 + 20v_2^2 v_7^2 w_7^2 w_4^2 w_5 w_2^2 - 4v_7^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 + 10v_2^3 w_7^2 w_4^3 c s^2 w_5 w_2^2 - w_7^2 c_3^4 c s^2 w_5 w_2^3 - \\
& 4v_3^2 w_7^2 w_4^2 w_5 w_2^3 - 3v_3^2 w_7^2 w_4^3 w_5 w_2^3 + 8v_2^3 w_7^2 w_4 c s^2 w_5 w_2^2 - 3v_1^2 w_7 w_4^3 c s^2 w_5 w_2^3 - 8v_1^2 w_7 w_4^2 c s^2 w_5 w_2^2 - 4v_1^2 w_7 c_3^4 c s^2 w_5 w_2^3 + \\
& 8v_2^2 w_7^2 c s^4 w_5 w_2^3 - 4v_3^2 w_7^2 w_4^2 c s^2 w_5 w_2^2 + 12v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 - 4v_2^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 - 8v_1^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 - 3v_2^2 v_1^2 w_7 w_4^3 w_5 w_2^3 + 10v_2^2 v_7 w_7^2 c s^2 w_5 w_2^3 - \\
& 36v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^2 + 4w_7 w_4^2 c s^4 w_5 w_2^2 + 2v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^3 - 8v_1^2 w_7^2 w_4^2 c s^2 w_5 w_2^3 + 2v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^3 - 12w_2^2 w_7^2 c s^4 w_5 w_2^2 - 4v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^2 - \\
& 2w_7 w_3^2 c s^4 w_5 w_2^2 - 2w_7 w_4^2 c s^4 w_5 w_2^3 - 4v_1^2 w_7 w_2^2 c s^2 w_5 w_2^2 + 2v_3^2 v_1^2 w_7 w_4^3 w_5 w_2^2 + 20v_3^2 v_1^2 w_7 w_4^2 w_5 w_2^3 + 4w_2^2 w_4^2 c s^4 w_5 w_2^2 - 2v_1^2 w_7 w_2^2 c s^2 w_5 w_2^3 - \\
& 4v_5^2 w_7^2 w_4^2 c s^2 w_5 w_2^3 - 38v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^2 + 2v_3^2 v_1^2 w_7 w_4^2 w_5 w_2^3 + 4v_3^2 w_7 w_4^3 c s^2 w_5 w_2^2 + 20v_3^2 v_1^2 w_7^2 w_4^2 w_5 w_2^3 + 20v_2^2 v_1^2 w_7 w_4^2 w_5 w_2^2 + 12v_2^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 + \\
& 4v_1^2 w_7 w_4^2 c s^4 w_5 w_2^2 - 2w_7^2 w_4^2 c s^4 w_5 w_2^3 - 4v_3^2 v_1^2 w_7 w_4^3 w_5 w_2^3 - 4v_3^2 v_1^2 w_7^2 w_4^2 w_5 w_2^2 + 10v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 - 2v_3^2 w_7 w_4^2 c s^2 w_5 w_2^3 + 2v_1^2 w_4^3 c s^4 w_5 w_2^2 + \\
& w_7^2 w_4^3 c s^4 w_5 w_2^3 - 2v_2^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 - 4v_2^2 w_7^2 w_4^2 c s^2 w_5 w_2^2 - 3v_2^2 v_1^2 w_7 w_4^3 w_5 w_2^2 - 4v_1^2 w_7 w_4 c s^2 w_5 w_2^2 - 4v_2^2 v_1^2 w_7 w_4^2 w_5 w_2^2 - \\
& 2w_7^2 w_4^4 c s^2 w_5 w_2^3 - 4v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^2 - 4v_3^2 v_1^2 w_7^2 w_4^2 c s^2 w_5 w_2^2 - 4v_1^2 w_7^2 w_4^3 c s^2 w_5 w_2^2 + v_3^2 w_7 w_4^2 c s^2 w_5 w_2^3 - 4v_3^2 w_7^2 w_4^2 c s^2 w_5 w_2^2 + 20v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^2 + \\
& 10v_3^2 v_1^2 w_7 w_2^2 w_5 w_2^3 + v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^3 + v_1^2 w_7 w_4^3 c s^2 w_5 w_2^3 + 2v_3^2 w_7^2 w_4^3 c s^2 w_5 w_2^3 - 4v_2^2 v_1^2 w_7^2 w_4^2 w_5 w_2^3 - 2w_7^2 w_4^3 c s^4 w_5 w_2^2 - 2v_3^2 w_7 w_4^3 c s^2 w_5 w_2^3 + \\
& 2v_3^2 v_1^2 w_7^2 w_4^3 w_5 w_2^3 + 10v_1^2 w_7^2 w_4 c s^2 w_5 w_2^3 + 4w_7^2 w_4 c s^4 w_5 w_2^2
\end{aligned}$$

$$\begin{aligned}
C_{56} = & 6v_3^2 w_4^3 w_3^2 + 24v_3^2 w_7 w_4^2 w_3^2 + 24v_3^2 w_7^2 w_4 w_2^2 - 14w_2^2 w_4^2 c s^2 w_3^2 - 6w_7 w_3^4 c s^2 w_3^2 + 12w_7^2 w_4^2 c s^2 w_2^2 - 78v_3^2 w_7 w_4 w_3^2 - 12w_7^2 w_4^2 c s^2 w_2^2 - 6v_3^2 w_7 w_4^3 w_3^2 - \\
& 12w_7 w_4 c s^2 w_3^2 - 12v_3^2 w_4^2 w_3^2 + 6w_4^3 c s^2 w_3^2 - 6w_7^2 w_4^3 c s^2 w_2^2 + 24v_3^2 w_7^2 w_4^2 w_2^2 + 24w_7 w_4^2 c s^2 w_3^2 - 4v_3^2 w_7^2 w_4^3 w_3^2 - 12w_7^2 c s^2 w_3^2 + 22v_3^2 w_7 w_4^3 w_2^2 + \\
& 12v_3^2 w_7 w_3^2 + w_7^2 w_4^3 c s^2 w_3^2 + 24w_7^2 w_4 c s^2 w_3^2 - 30v_3^2 w_7^2 w_4^3 w_2^2 + 34v_3^2 w_7^2 w_4^2 w_3^2 - 12w_4^2 c s^2 w_3^2 + 48v_3^2 w_7 w_3^2 - 48v_3^2 w_7^2 w_4^2 w_2^2 + 6w_7^2 w_4^3 c s^2 w_2^2 - 12v_3^2 w_7 w_4 w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{57} = & 6v_1^2 w_3^4 w_2^3 - 4v_1^2 w_3^3 w_5^2 w_2^3 + 34v_1^2 w_3^2 w_5^2 w_2^2 - 12w_4^3 c s^2 w_5 w_2 - 12v_1^2 w_3^2 w_2^3 + 24w_4^3 c s^2 w_5 w_2^2 - 78v_1^2 w_3^2 w_5^2 w_2 + 24v_1^2 w_4 w_5^2 w_2^2 - 12w_4 c s^2 w_5^2 w_2^3 + 6w_3^4 c s^2 w_2^3 - 30v_1^2 w_4 w_5^2 w_2^3 - 6w_4^3 c s^2 w_5 w_2^3 + 12v_1^2 w_5^2 w_2^3 - 12w_3^3 c s^2 w_2^2 + 6w_4 c s^2 w_5^2 w_2^3 - 48v_1^2 w_4 w_5^2 w_2^2 + 4^3 c s^2 w_5^2 w_2^3 - 12v_1^2 w_3^4 w_5 w_2 - 14w_4^3 c s^2 w_5^2 w_2^2 - 12w_4^3 c s^2 w_5^2 + 22v_1^2 w_4 w_5^2 w_2^3 + 12w_4^2 c s^2 w_5^2 w_2^2 + 24w_4^3 c s^2 w_5^2 w_2 + 24v_1^2 w_3^4 w_5 w_2^2 - 6w_4^2 c s^2 w_5^2 w_2^3 + 48v_1^2 w_4 w_5^2 w_2^2 + 24v_1^2 w_4^2 w_5^2 w_2 - 6v_1^2 w_3^4 w_5 w_2^3
\end{aligned}$$

$$\begin{aligned} C_{58} = & 12w_7^2w_4cs^2 + 12w_3v_3^2w_4^2 - 10w_3v_3^2w_2^2w_4^2 - 6w_3v_3^2w_4^3 - 2w_3w_7^2w_4^3cs^2 + 12w_7w_4^2cs^2 + w_3v_3^2w_2^2w_4^3 - 6v_3^2w_7w_4^3 - 24w_3v_3^2w_7^2 + \\ & 12w_3w_7w_4cs^2 + 12v_3^2w_7w_4^2 + 36w_3v_3^2w_7^2w_4 + 12w_3w_7^2cs^2 - 6w_7w_4^3cs^2 + 22w_3w_7^2w_2^2cs^2 + 6v_3^2w_7^2w_4^2 + 12w_3v_3^2w_7w_4 - 6w_3w_4^3cs^2 - \\ & 30w_3w_7^2w_4cs^2 - v_3^2w_7^2w_4^3 + 3w_7^2w_4^3cs^2 - 30w_3w_7w_4^2cs^2 + 12w_3w_4^2cs^2 + 9w_3v_3^2w_7w_4^3 + 9w_3w_7w_4^3cs^2 - 18w_7w_4^2cs^2 - 30w_3v_3^2w_7w_4^2 - 12v_3^2w_7^2w_4 \end{aligned}$$

$$C_{59} = -10\omega_3^3 w_7 w_4^2 + \omega_3^3 w_7 w_4^3 + 12w_3 w_7 w_4^3 + 24\omega_3^3 w_7 w_4 - 6w_3 w_7 w_4^2 - 6\omega_3^2 w_4^3 - 7w_3^2 w_7 w_4^3 - 6w_7 w_4^3 + 12w_3^2 w_4^2 + 12w_3^2 w_7 w_4^2 - 12\omega_3^2 w_7 w_4 + 3\omega_3^3 w_4^3 - 12w_3^2 w_7 - 6w_3^2 w_4^2$$

$$C_{60} = 6w_3^2 w_2^2 w_4 c s^2 w_2^3 - 2 w_3^2 v_2^2 w_7 w_4 w_2^3 + 6 w_3^3 w_2^2 w_4 c s^2 w_2^3 - 8 w_3^2 v_2^3 w_7^2 w_3^2 w_2 + 12 w_3^3 v_2^2 w_7^2 w_4 w_2^3 + 7 w_3^2 v_2^3 w_7^2 w_4 w_2^3 - 2 w_3^2 w_7^2 w_4 c s^2 w_2^2 + \\ v_2^2 w_7^2 w_4 c s^2 w_2^3 - 12 v_2^3 w_7^2 w_4^2 w_2^2 - 2 v_2^2 w_7^2 w_4^2 c s^2 w_2^3 + v_2^3 w_7^2 w_4^2 c s^2 w_2^2 - 2 v_2^3 w_7^2 w_4^2 w_2^3 - 2 v_2^3 w_7^2 w_4^2 c s^2 w_2^3 + v_2^3 w_7^2 w_4^2 c s^2 w_2^3 -$$

$$2w_3^2 w_7^4 w_4^4 c s^- w_2^2 + 4 w_3^4 v_3^2 w_7^2 w_4^4 w_2 + 6 w_3^2 \omega_7 w_4^2 c s^- w_2^3 - 2 w_3^2 v_3^2 w_7^2 w_4^3 w_2^3 + w_3^2 v_3^2 w_7 w_4^3 w_2^3 + 7 w_3^2 v_3^2 w_7^2 w_4^2 w_2^3 + w_3^2 v_3^2 w_4^3 w_2^3 + w_3^2 w_7^2 w_4^4 c s^- w_2^3 -$$

$$2\omega_3^2\omega_7w_4^2cs^2w_2^2 + 3\omega_3v_3^2\omega_7^2w_4^3w_2^2 + \omega_3w_7^2w_4^3cs^2w_2^2 + 3v_3^2\omega_7^2w_4^3w_2^2 - 2\omega_3^2\omega_7^2w_4^3cs^2w_2^2 - 2\omega_3^2v_3^2\omega_7w_4^3w_2^2 - 2\omega_3^2w_7^2w_4^3cs^2w_2^2 + 10\omega_3^3v_3^2\omega_7^2w_4^3w_2^2 - \\ 2\omega_3^2\omega_7w_4^2cs^2w_2^2 - 2\omega_3^2\omega_7w_4^2cs^2w_3^2 + \omega_3^2\omega_7^2w_4^3cs^2w_2^2 + 7\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 + \omega_3^2v_3^2\omega_7w_4^3w_2^2 - 8\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 - 2\omega_3^2w_7^2w_4^3cs^2w_2^2 + \\ 3\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 - 12\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 + 3\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 - 2\omega_3^2w_7^2w_4^3cs^2w_2^2 + 6\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 + 7\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 + 7\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 + \\ 4\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 - 2\omega_3^2w_7w_4^3cs^2w_2^2 + 6\omega_3^2\omega_7^2w_4^3cs^2w_2^2 + 4\omega_3v_3^2\omega_7^2w_4^3w_2^2 - 2\omega_3^2\omega_7^2w_4^3w_2^2 - 21\omega_3^2v_3^2\omega_7^2w_4^3w_2^2 - 2\omega_3^2v_3^2\omega_7w_4^3w_2^2$$

$$C_{61} = 36\omega_3^3v_3^2\omega_7w_4^2 - 24\omega_3^2\omega_7^2w_4^3cs^2 + 24\omega_3v_3^2\omega_7^2w_4^2 - 12\omega_3^2\omega_7w_4^3cs^2 - 12\omega_3^2\omega_7^2w_4^2cs^2 + 6\omega_3\omega_7^2w_4^3cs^2 + 48\omega_3^3v_3^2\omega_7^2w_4^2 - \\ 12\omega_3^2v_3^2\omega_7w_4^3 - 30\omega_3v_3^2\omega_7^2w_4^3 + 12\omega_3^2v_3^2\omega_7w_4^3 + 36\omega_3^3\omega_7w_4^2cs^2 + 6\omega_3^2v_3^2\omega_4^3 + 36\omega_3^3\omega_7^2w_4^2cs^2 - 24\omega_3^2v_3^2\omega_7w_4^2 - 12\omega_3^2v_3^2\omega_7^2w_4^2 - 12\omega_3^2v_3^2\omega_7w_4^2 - \\ 12\omega_3\omega_7^2w_4^2cs^2 + 12\omega_3^2\omega_7w_4^3cs^2 - 32\omega_3^2\omega_7^2w_4^2cs^2 - 60\omega_3^2v_3^2\omega_7^2w_4^2 - 90\omega_3^2v_3^2\omega_7^2w_4^2 + 24\omega_3^2v_3^2\omega_7^2w_4^2 + 12\omega_3^2v_3^2\omega_7^2w_4^2 - 12\omega_3^2\omega_7w_4^2cs^2 - \\ 12\omega_3^2\omega_7^2w_4^2cs^2 - 5\omega_3^2v_3^2\omega_7^2w_4^2 + 4\omega_3^2v_3^2\omega_7^2w_4^3 + 40\omega_3^2v_3^2\omega_7^2w_4^3 + 48\omega_3^2\omega_7^2w_4^3cs^2 + 6\omega_3^3\omega_4^3 + 48\omega_3^2v_3^2\omega_7^2w_4^2$$

$$C_{62} = 6v_2^2\omega_3^2w_2^3 + 36v_2^2\omega_7w_4^2w_2^3 + 48v_2^2\omega_3^2w_2^2w_4w_2^2 + 12\omega_7w_4^3cs^2w_2^2 - 32\omega_2^2\omega_7^2w_2^3cs^2w_2^2 - 12\omega_7w_4^3cs^2w_2^3 + 48\omega_2^2\omega_7^2w_2^2w_2^3 - \\ 90v_2^2\omega_7^2w_4^2w_2^3 - 24v_2^2\omega_7w_4^2w_2^3 - 12v_2^2\omega_7w_4^3w_2^3 - 12\omega_7w_4^2cs^2w_2^3 - 12v_2^2\omega_7^2w_2^3 + 6\omega_4^2cs^2w_2^3 + 12v_2^2\omega_7^2w_4^2w_2^3 - 12\omega_7w_4^2cs^2w_2^3 + 24v_2^2\omega_7^2w_4^2w_2^3 + \\ 36\omega_7w_4^2cs^2w_2^3 - 5v_2^2\omega_7^2w_2^3w_2^3 - 12\omega_7^2cs^2w_2^3 + 24v_2^2\omega_7^2w_4^3w_2^3 + 12v_2^2\omega_7^2w_4^3w_2^3 + 4\omega_7^2w_4^3cs^2w_2^3 - 24\omega_7w_4^2cs^2w_2^3 + 36\omega_7^2w_4^2cs^2w_2^3 - 30v_2^2\omega_7^2w_4^3w_2^3 + \\ 40v_2^2\omega_7w_4^2w_2^3 - 12\omega_4^2cs^2w_2^3 + 48v_2^2\omega_7w_2^3 - 60v_2^2\omega_7^2w_4^2w_2^2 + 6\omega_2^2\omega_7^2w_4^3cs^2w_2^2 - 12v_2^2\omega_7w_4^2w_2^3 - 24\omega_7w_4^2cs^2w_2^2$$

$$C_{63} = -30\omega_3w_4^3w_2^3 - 30\omega_3^2\omega_4^2w_2^2 - 30\omega_3^3w_4^3w_2 + 28\omega_3^2w_4^2w_2^3 + 18\omega_3w_4^3w_2^2 + 24\omega_3^2w_4^3w_2^2 + 6\omega_3w_4^2w_2^3 + 18\omega_3^2w_4w_2^3 + 6\omega_3^3w_4^2w_2 - 5\omega_3^3w_4^3w_2^3 - \\ 30\omega_3^2w_4^2w_2^3 + 18\omega_3^2w_4^3w_2 + 12\omega_3^2w_4^3w_2 + 12\omega_3^2w_4^2w_2^3 - 36\omega_3^3w_4w_2^3 + 24\omega_3^2w_4^3w_2^3 + 12\omega_4^3w_2^3 - 42\omega_3^2w_4^2w_2^2 + 18\omega_3^2w_4w_2^2$$

$$C_{64} = 2\omega_6w_3^3v_3^2\omega_7^2w_4^2cs^2 - 4\omega_6^2\omega_3^3v_3^2v_2^2w_7w_4 - 4\omega_3^2v_3^2\omega_7^2w_4^3cs^2 + 10\omega_6w_3^2v_2^2v_2^2w_7w_4^3 + 4\omega_6^2\omega_3^2w_2^2\omega_7w_4^3cs^4 + 2\omega_6^2\omega_3^2v_2^2w_7w_4^3cs^2 + \\ 20\omega_6^2w_3^2v_3^2v_2^2w_7^2w_2^2 + \omega_6^2\omega_3^2v_2^2w_7^2w_4^3cs^2 - 2\omega_6w_3^2v_2^2w_7^2w_4^2cs^2 - 4\omega_6w_3^2v_2^2v_2^2w_7w_4^2 + 2\omega_6^2w_3^2v_2^2w_7w_4^3cs^4 + \\ 4\omega_6w_3v_3^2v_2^2w_7w_4^3 + \omega_6^2\omega_3^2v_3^2w_2^2w_7w_4^3cs^2 + 20\omega_6^2w_3^2v_3^2v_2^2w_7w_4^2w_4 - 2\omega_6^2w_3^2v_2^2w_7w_4^3cs^4 - 8\omega_6^2w_3^2v_2^2w_7w_4^2w_4^2cs^2 - 4\omega_6^2w_3^2v_2^2w_7w_4^2w_4^2 - 36\omega_6^2w_2^2v_3^2v_2^2w_7w_4^2 - \\ 38\omega_6^2w_3^2v_2^2w_7w_4^2w_4^2 + 4\omega_6^2w_3^2v_2^2w_7w_4^3cs^4 - 4\omega_6^2w_3^2v_2^2w_7w_4^3cs^2 - 3\omega_6w_3^2v_2^2w_7w_4^3cs^2 + 2\omega_6^2v_3^2v_2^2w_7w_4^3cs^4 - 8\omega_6^2w_3^2v_2^2w_7w_4^3cs^2 - 2\omega_6^2w_3^2v_2^2w_7w_4^3cs^4 - \\ 3\omega_6^2w_3^2v_2^2w_7w_4^3 + 20\omega_6^2w_3^2v_2^2w_7w_4^3w_3 + 2\omega_6^2w_3^2v_2^2w_7w_4^3w_3 - 4\omega_6^2w_3^2v_2^2w_7w_4^3w_3 + 20\omega_6^2w_3^2v_2^2w_7w_4^3w_3 - 4\omega_6^2w_3^2v_2^2w_7w_4^3w_3 - 2\omega_6^2w_3^2v_2^2w_7w_4^3w_3 + \\ 10\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 + 4\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - 4\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 + 20\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 + 4\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - 20\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 + 4\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - \\ 4\omega_5^2v_2^2w_7w_4^2w_2^3 + 10\omega_6w_3^2v_3^2v_2^2w_7w_4^2w_2^3 + 2\omega_6^2w_3^2v_3^2v_2^2w_7w_4^2w_2^3 + 10\omega_6^2w_3^2v_3^2w_2^2w_7w_4^2w_2^3 - 4\omega_6^2w_3^2v_3^2w_2^2w_7w_4^2w_2^3 + 2\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - \\ 2\omega_6w_3^2w_2^2w_7w_4^2cs^4 + 20\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 + 12\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - 2\omega_6w_3^2v_2^2w_7w_4^2w_2^3 - 2\omega_6w_3^2v_2^2w_7w_4^2w_2^3 + 10\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - 2\omega_6w_3^2v_2^2w_7w_4^2w_2^3 + 4\omega_6^2w_3^2v_2^2w_7w_4^2w_2^3 - \\ 8\omega_6^2w_3^2v_2^2w_7w_4^2cs^2 - 2\omega_6^2w_3^2v_3^2w_2^2w_7w_4^2cs^2 - 4\omega_6^2w_3^2v_3^2v_2^2w_7w_4^2 - 4\omega_6w_3^2v_3^2v_2^2w_7w_4^2w_4 - 3\omega_6^2w_3^2v_3^2v_2^2w_7w_4^2w_4^2 + 12\omega_6^2w_3^2v_3^2w_2^2w_7w_4^2cs^2 - 4\omega_6^2w_3^2v_2^2w_7w_4^2w_3^2 - 3\omega_6w_3^2v_3^2w_2^2w_7w_4^2w_3^2 + \\ 2\omega_3^2v_3^2w_2^2w_7w_4^2cs^2 - 38\omega_6^2w_3^2v_3^2v_2^2w_7w_4^2w_2 - 8\omega_6^2w_3^2v_3^2w_2^2w_7w_4^2w_2 - 4\omega_6^2v_3^2w_2^2w_7w_4^2w_2^3 + 4\omega_6^2w_3v_2^2w_7w_4^2w_2^3 + 2\omega_6w_3^2v_3^2w_2^2w_7w_4^2w_2^3 + \\ 4\omega_6w_3^2w_7w_4^2cs^2 - \omega_6^2w_3^2w_7w_4^2w_3^2 + 4\omega_6w_3^2v_2^2w_7w_4^2w_3^2$$

$$C_{65} = 24\omega_3^2v_3^2\omega_7w_4^2 + 24\omega_3v_3^2w_7^2w_2^2 - 6\omega_3^2\omega_7w_4^3cs^2 - 12\omega_3^2w_7^2cs^2 + 6\omega_3w_7^2w_4^3cs^2 + 48\omega_3^2v_3^2w_7^2 - 6\omega_3^2v_3^2\omega_7w_4^3 - 30\omega_3v_3^2\omega_7^2w_4^3 + 24\omega_3^2\omega_7w_4^2cs^2 + \\ 6\omega_3^2v_3^2w_4^3 + 24\omega_3^2\omega_7w_4cs^2 - 12\omega_3^2v_3^2w_4^2 - 12\omega_3^2v_3^2\omega_7w_4 - 12\omega_3w_7^2w_4^2cs^2 - 14\omega_3^2\omega_7w_4^2w_2^3 - 48\omega_3^2v_3^2w_7w_4^2 - 78\omega_3^2v_3^2\omega_7^2w_4 + 22\omega_3^2v_3^2w_7w_4^2 + \\ 12\omega_3^2w_7w_4^2 - 12\omega_3^2\omega_7w_4cs^2 - 12\omega_3^2w_4^2cs^2 - 6\omega_3^2w_7w_4^2w_3^2 - 4\omega_3^2v_3^2w_7w_4^2w_3^2 + 34\omega_3^2v_3^2w_7w_4^2w_3^2 + 12\omega_3^2w_7w_4^2w_3^2 + 6\omega_3^3w_4^3cs^2 + 24\omega_3^2v_3^2w_7w_4^2w_3^2$$

$$C_{66} = -12\omega_6^2w_3^2w_4cs^2 + \omega_6^2\omega_3^2w_3^2cs^2 - 78\omega_6^2w_3v_2^2w_4^3 + 24\omega_6w_3^2v_2^2w_4^3cs^2 - 12\omega_6^2v_2^2w_4^3 - 30\omega_6^2w_3^2v_2^2w_4^3 - 12\omega_6^2w_3^2v_2^2w_4^3cs^2 + 24\omega_6^2w_3v_2^2w_4^3 - 12\omega_6^2w_3^2w_4^3cs^2 + \\ 22\omega_6^2w_3^2v_2^2w_4^2 + 24\omega_6w_3^2v_2^2w_4^2 - 6\omega_6^2w_3^2v_2^2w_4^2cs^2 + 48\omega_6^2v_2^2w_4^2 - 4\omega_6^2w_3^2v_2^2w_4^2w_3 + 24\omega_6^2w_3^2v_2^2w_4^2w_3 - 12\omega_6w_3^2v_2^2w_4^2w_3 + 6\omega_3^2v_2^2w_4^2 - 6\omega_6^2w_3^2w_4^3cs^2 + \\ 6\omega_6^2w_3^2w_4cs^2 - 14\omega_6^2w_3^2w_4^3cs^2 + 34\omega_6^2w_3^2v_2^2w_4^3 + 12\omega_6^2w_3^2w_4^3cs^2 - 6\omega_6w_3^2v_2^2w_4^3 + 6\omega_3^2w_4^3cs^2 - 48\omega_6^2w_3^2v_2^2w_4^3 + 12\omega_6^2w_3^2v_2^2w_4^3$$

$$C_{67} = -48\omega_2^2w_4cs^2 + 48v_2^2\omega_7w_4 + 12\omega_4^2cs^2 + 12\omega_2^2w_4 - 36\omega_7w_4^2cs^2 - 6\omega_4^3cs^2 + 15v_2^2\omega_7w_4^3 - 11\omega_2^2w_4^2 - 60v_2^2\omega_7w_4^2 + 9\omega_7w_4^3cs^2 + \omega_7w_4^3 + 27v_2^2w_7w_4^2 + \\ 6\omega_4^3 + 12v_2^2w_7^2 - 9\omega_7w_4^3 + 24\omega_7^2cs^2 - 3v_2^2w_7w_4^3 + 36\omega_7w_4^2 - 12\omega_4^2 - 2\omega_2^2w_4^3cs^2 - 24\omega_7w_4 + 12v_2^2w_4^2 + 24\omega_7w_4cs^2 + 25\omega_2^2w_4^2cs^2 - 6v_2^2w_4^3 - 42v_2^2w_7w_4^2$$

$$C_{68} = \omega_7^2w_3^2w_2^2 + 6v_2^2\omega_3^2w_4^3 + 42v_2^2\omega_7w_4^2w_3^2 + 12v_2^2\omega_7^2w_4w_2^2 + 6\omega_7w_3^2cs^2w_2^2 - 48\omega_7^2w_4^2cs^2w_3^2 - \omega_7^2w_3^2w_2^3 - 12\omega_7w_3^2cs^2w_2^3 + 42w_2^2w_3^2w_4^2cs^2w_2^2 - \\ 30v_2^2w_7w_4^2w_2^3 - 12v_2^2\omega_7w_2^2w_2^2 - 12\omega_7^2w_4^2cs^2w_2^2 - 12v_2^2\omega_7w_3^2w_2^3 - 24\omega_7w_4cs^2w_2^3 - 3v_2^2w_7w_4^2w_2^2 - 12v_2^2w_3^2w_4^2w_2^3 + 6\omega_4^2cs^2w_2^3 + \\ 6v_2^2w_7w_4^2w_2^2 + 7v_2^2w_7w_4^2w_2^3 - 12\omega_7^2w_4^2cs^2w_2^2 + 6v_2^2w_7w_4^2w_2^2 + 42\omega_7w_4^2cs^2w_2^2 + 6\omega_4^2w_2^2w_7w_4^2w_2^3 + 36\omega_7^2w_4^2cs^2w_2^2 - 6\omega_7w_4^2w_2^2 + 6\omega_7w_4^2w_2^3 + 6v_2^2w_7w_4^2w_2^3 + \\ 6v_2^2w_7w_4^2w_2^3 - 12\omega_7w_4^2cs^2w_2^2 - 21\omega_7w_4^2w_2^3 - 3\omega_7w_4^2w_2^3 + 78\omega_7w_4^2cs^2w_2^2 - 12v_2^2w_7w_4^2w_2^3 - 3v_2^2w_7w_4^2w_2^3 + 6v_2^2w_7w_4^2w_2^3 + 6\omega_7w_4^2w_2^3 - \\ 12\omega_4^2cs^2w_2^2 + 24v_2^2w_7w_4^2w_2^3 - 12v_2^2w_7w_4^2w_2^3 + 6\omega_7w_4^2cs^2w_2^2 - 24v_2^2w_7w_4^2w_2^3 - 24v_2^2w_7w_4^2w_2^3 - 24v_2^2w_7w_4^2w_2^3$$

$$C_{69} = 90\omega_7^2w_4cs^2 - 36v_2^2\omega_7w_4 - 12\omega_4^2cs^2 - 12\omega_2^2w_4 + 48\omega_7w_4^2cs^2 + 6\omega_3^2cs^2 - 12v_2^2\omega_7w_4^3 + 11\omega_2^2w_4^2 + 48v_2^2\omega_7w_4^2 - 12\omega_7w_4^3cs^2 - \omega_7w_4^3 - \\ 8v_2^2w_7w_4^2 - 6\omega_4^3 + 12v_2^2w_7^2 + 9\omega_7w_4^3 - 48\omega_7^2cs^2 + v_2^2w_7w_4^3 - 36\omega_7w_4^2 + 12\omega_4^2 + 4\omega_7w_4^3cs^2 + 24\omega_7w_4 - 12v_2^2w_4^2 + 36\omega_7w_4cs^2 - 44\omega_7w_4^2cs^2 + 6v_2^2w_4^3$$

$$C_{70} = 2\omega_7^2w_3^2w_2^2 + 6v_2^2\omega_3^2w_4^3 + 36v_2^2\omega_7w_4^2w_3^2 + 12\omega_7w_4^3cs^2w_2^2 - 32\omega_7^2w_4^2cs^2w_3^2 - \omega_7^2w_3^2w_2^3 - 12\omega_7w_3^2cs^2w_2^3 + 48\omega_7^2w_4^2cs^2w_2^2 - 30v_2^2w_7w_4^2w_3^2 - \\ 24v_2^2w_7w_4^2w_2^2 - 12\omega_7^2w_4^2cs^2w_2^2 - 12v_2^2\omega_7w_4^3w_2^2 - 6\omega_7^2w_4^2w_2^2 - 12v_2^2w_7w_4^2w_2^2 + 6\omega_4^2cs^2w_2^2 + 12v_2^2w_7w_4^2w_2^2 + 3w_7^2w_4^2w_2^2 - \\ 12\omega_7^2w_4^2cs^2w_2^2 + 36\omega_7w_4^2cs^2w_2^2 + 3v_2^2w_7w_4^2w_2^2 - 12\omega_7w_4^2cs^2w_2^2 + 12v_2^2w_7w_4^2w_2^2 + 4\omega_7w_4^2cs^2w_2^2 - 24\omega_7w_4^2cs^2w_2^2 - 6\omega_7w_4^2w_2^2 - 6\omega_7w_4^2w_2^3 + \\ 36\omega_7w_4^2cs^2w_2^2 - 18v_2^2w_7w_4^2w_2^2 + 3w_7w_4^2cs^2w_2^2 + 24v_2^2w_7w_4^2w_2^2 + 12v_2^2w_7w_4^2w_2^2 + 6\omega_7w_4^2cs^2w_2^2 - 12v_2^2w_7w_4^2w_2^2 - 24\omega_7w_4^2cs^2w_2^2$$

$$C_{71} = 42\omega_3^2v_3^2\omega_7w_4^2 - 21\omega_3^2w_7w_4^2 - 24\omega_3^2w_7w_4^3w_4^2cs^2 + 6\omega_3v_3^2w_7w_4^2w_4^2 - 12\omega_3^2w_7w_4^3cs^2 - 36\omega_3^2w_7w_4^3cs^2 - 12\omega_3^2w_7w_4^2cs^2 + 6\omega_3w_7^2w_4^3cs^2 + 24\omega_3^2v_3^2w_7^2 + \\ 6\omega_3^2\omega_7w_4^3 - 12\omega_3^2v_3^2w_7w_4^3 - 12\omega_3v_3^2w_7w_4^3 + 6\omega_3^2v_2^2w_7w_4^3 + 42\omega_3^2w_7w_4^3cs^2 - 3v_3^2w_7w_4^2w_4^2 + 6\omega_3^2v_2^2w_7w_4^3 + 78\omega_3^2w_7w_4^3cs^2 - 12\omega_3^2v_2^2w_7w_4^3 + 12\omega_3^2v_2^2w_7w_4^3 - \\ 12\omega_3^2v_3^2w_7w_4^3 - 24\omega_3^2v_3^2w_7w_4^3 - 12\omega_3v_3^2w_7w_4^3 + 6\omega_3^2w_7w_4^3 + 42\omega_3^2w_7w_4^3 - 12\omega_3^2v_3^2w_7w_4^3 - 6\omega_3^2w_7w_4^3 - 30\omega_3^2v_3^2w_7w_4^3 - 3v_3^2w_7w_4^3 + \\ 6\omega_3^2v_3^2w_7w_4^3 + 6v_3^2w_7w_4^3 - 24\omega_3^2w_7w_4^3cs^2 - 12\omega_3^2w_7w_4^3 - 6\omega_3^2w_7w_4^3 + 6\omega_3^2w_7w_4^3 - \omega_3^2w_7w_4^3 + 6\omega_3^2w_7w_4^3 + 6\omega_3^2v_3^2w_7w_4^3 + \\ 7\omega_3^2w_7w_4^3 + 42\omega_3^2w_7w_4^3cs^2 + 6\omega_3^2w_7w_4^3 + 6\omega_3^2w_7w_4^3 + 12\omega_3^2v_3^2w_7w_4^3$$

$$C_{72} = 90\omega_7^2w_4cs^2 - 36v_2^2\omega_7w_4 - 12\omega_4^2cs^2 - 12\omega_2^2w_4 + 48\omega_7w_4^2cs^2 + 6\omega_3^2cs^2 - 12v_2^2\omega_7w_4^3 + 11\omega_2^2w_4^2 + 48v_2^2\omega_7w_4^2 - 12\omega_7w_4^3cs^2 - \omega_7w_4^3 - \\ 8v_2^2w_7w_4^2 - 6\omega_4^3 + 12v_2^2w_7^2 + 9\omega_7w_4^3 - 48\omega_7^2cs^2 + v_2^2w_7w_4^3 - 36\omega_7w_4^2 + 12\omega_4^2 + 4\omega_7w_4^3cs^2 + 24\omega_7w_4 - 12v_2^2w_4^2 + 36\omega_7w_4cs^2 - 44\omega_7w_4^2cs^2 + 6v_2^2w_4^3$$

$$\begin{aligned}
C_{73} = & 36\omega_3^3 v_3^2 \omega_7 \omega_4^2 - 6\omega_3^3 \omega_7 \omega_4^2 - 24\omega_3^2 \omega_7^2 \omega_4^2 c s^2 - 12\omega_3^3 \omega_7 \omega_4^3 c s^2 - 12\omega_3^2 \omega_7^2 \omega_4^2 c s^2 + 24\omega_3^2 \omega_7 \omega_4^2 c s^2 + 6\omega_3 \omega_7^2 \omega_4^3 c s^2 + 24\omega_3^3 v_3^2 \omega_7^2 + 3\omega_3^3 \omega_7 \omega_4^3 - \\
& 12\omega_3^2 v_3^2 \omega_7 \omega_4^3 - 18\omega_3 v_3^2 \omega_7^2 \omega_4^3 + 12\omega_3^2 v_3^2 \omega_7 \omega_4^3 + 36\omega_3^3 \omega_7 \omega_4^2 c s^2 - 6\omega_3^2 \omega_7^2 \omega_4^2 + 6\omega_3^3 v_3^2 \omega_4^3 + 36\omega_3^3 \omega_7^2 \omega_4^2 c s^2 - 24\omega_3^2 v_3^2 \omega_7 \omega_4^2 - 12\omega_3^3 v_3^2 \omega_4^2 - \\
& 12\omega_3^3 v_3^2 \omega_7 \omega_4^2 - 12\omega_3 \omega_7^2 \omega_4^2 c s^2 + 12\omega_3^2 \omega_7 \omega_4^3 c s^2 + 2\omega_3^2 \omega_7^2 \omega_4^3 - 32\omega_3^2 \omega_7 \omega_4^2 c s^2 + 12\omega_3^2 v_3^2 \omega_7 \omega_4^2 - 30\omega_3^3 v_3^2 \omega_7 \omega_4^2 - 6\omega_3^2 \omega_7 \omega_4^3 + 12\omega_3^2 \omega_7^2 \omega_4^3 - \\
& 12\omega_3^3 \omega_7 \omega_4 c s^2 - 12\omega_3^2 \omega_7^2 \omega_4^3 c s^2 + 12\omega_3^2 \omega_7 \omega_4^2 - \omega_3^3 \omega_7^2 \omega_4^3 + 3\omega_3^3 v_3^2 \omega_7 \omega_4^3 + 4\omega_3^3 \omega_7^2 \omega_4^3 c s^2 + 3\omega_3^3 \omega_7^2 \omega_4^2 + 48\omega_3^2 \omega_7^2 \omega_4^2 c s^2 + 6\omega_3^3 \omega_4^3 c s^2 \\
C_{74} = & 12\omega_7^2 \omega_4 c s^2 - 18v_3^4 \omega_7 \omega_4^3 + 48v_3^2 \omega_7 \omega_4 + 24\omega_7 \omega_4 c s^4 + 6v_3^2 \omega_7^2 \omega_4^3 c s^2 + 72v_3^4 \omega_7 \omega_4^2 + 24\omega_7 \omega_4^2 c s^2 + 24\omega_7^2 \omega_4^2 c s^4 - 72v_3^2 \omega_7^2 \omega_4^2 c s^2 + 12v_3^4 \omega_3^3 + \\
& 18v_3^2 \omega_7 \omega_4^3 - 48v_3^4 \omega_7 \omega_4 - 72v_3^2 \omega_7 \omega_4^2 - 24v_3^4 \omega_4^2 - 3\omega_7^2 \omega_4^3 c s^4 - 24v_3^2 \omega_7 \omega_4 c s^2 - 6\omega_7 \omega_4^3 c s^2 + 24\omega_7^2 \omega_4^2 c s^4 - 96v_3^2 \omega_7^2 \omega_4^2 c s^2 + 24v_3^2 \omega_7^2 \omega_4^2 + \\
& 48v_3^2 \omega_7 \omega_4^2 c s^2 + 12v_3^2 \omega_7^2 \omega_4^3 c s^2 + 6\omega_7 \omega_4^3 c s^4 + 156v_3^2 \omega_7^2 \omega_4 c s^2 - 3v_3^2 \omega_7^2 \omega_4^3 + 24v_3^4 \omega_7^2 \omega_4 + \omega_7^2 \omega_4^3 c s^2 + 24v_3^2 \omega_7^2 \omega_4^2 - 24v_3^4 \omega_7^2 \omega_4^2 - 24v_3^2 \omega_7 \omega_4^2 c s^2 - \\
& 24\omega_7 \omega_4 c s^2 - 48\omega_7^2 \omega_4 c s^4 - 12v_3^2 \omega_7 \omega_4^3 c s^2 - 8\omega_7^2 \omega_4^2 c s^2 + 3v_3^4 \omega_7^2 \omega_4^3 - 12v_3^2 \omega_7^2 \omega_4^3 - 24v_3^2 \omega_7^2 \omega_4 - 24\omega_7 \omega_4^2 c s^4
\end{aligned}$$

## 2.3 MRT2

### 2.3.1 Definitions

Collision operator  $\mathbf{C}$ :

$$\mathbf{C}(\mathbf{f}) = \mathbf{M}_2^{-1} \mathbf{S} (\boldsymbol{\mu}_2^{(eq)} - \mathbf{M}_2 \mathbf{f}),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2)$ .

Matrix  $\mathbf{M}_2$  corresponds to the transformation matrix to the raw moment basis defined by

$$\boldsymbol{\mu}_2 = \begin{pmatrix} m_{(0,0,0)} \\ m_{(1,0,0)} \\ m_{(0,1,0)} \\ m_{(0,0,1)} \\ m_{(2,0,0)} + m_{(0,2,0)} + m_{(0,0,2)} \\ m_{(2,0,0)} - m_{(0,2,0)} \\ m_{(2,0,0)} - m_{(0,0,2)} \end{pmatrix},$$

and is given by

$$\mathbf{M}_2 = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & -1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & -1 & 1 & 0 & -1 \end{pmatrix}.$$

The equilibrium moments  $\boldsymbol{\mu}_2^{(eq)}$  are defined by

$$\boldsymbol{\mu}_2^{(eq)} = \mathbf{M}_2 \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\mu}_2^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho(v_3^2 + v_2^2 + v_1^2 + 3c_s^2) \\ \rho(v_1^2 - v_2^2) \\ \rho(v_1^2 - v_3^2) \end{pmatrix}.$$

### 2.3.2 Conservation of mass equation

 attached text file: output\_d3q7\_ade\_mrt2\_symbolic\_pde\_00.txt

$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\
& (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\delta_l^2 \rho}{2\omega_2 \delta_t} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{\delta_l^2 \rho}{\omega_2 \omega_3 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{\delta_l^2 \rho}{\omega_4 \omega_2 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} \\
& + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\delta_l^2 \rho}{2\omega_3 \delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{\delta_l^2 \rho}{\omega_4 \omega_3 \delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_3 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} \\
& + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_3 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l^2 \rho}{2\omega_4 \delta_t} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + \\
& (-2 + \omega_2) \frac{\delta_l \rho}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{cs^2 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \delta_l^2 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\delta_l \rho}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + \\
& (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \delta_l^2 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\
& (-2 + \omega_3) \frac{v_2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\delta_l \rho}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_3 v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \delta_l^2 \rho}{2\omega_4 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\
& (2 - \omega_2) \frac{v_1 \delta_l^2 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_3 v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \delta_l^2 \rho}{2\omega_4 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + \\
& (-2 + \omega_4) \frac{cs^2 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{v_3 \delta_l^2 \rho}{2\omega_4 \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + (12 + \omega_2^2 - 12\omega_2) \frac{\delta_l \rho \delta_t}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 - 6\omega_5 - 6\omega_2 + \omega_5 \omega_2) \frac{v_1 \delta_l^2 \rho}{6\omega_5 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_2^2} \\
& + C_1 \frac{v_1 \delta_l^3}{6\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_2^3} + (12 - 12\omega_3 + \omega_3^2) \frac{\delta_l \rho \delta_t}{12\omega_2^3} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + \\
& (-6\omega_2 - 2\omega_2 \omega_3^2 + 9\omega_2 \omega_3 - 6\omega_3 + 3\omega_3^2) \frac{v_2 \delta_l^2 \rho}{6\omega_2 \omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + (-2\omega_2^2 \omega_3 + 3\omega_2^2 - 6\omega_2 + 9\omega_2 \omega_3 - 6\omega_3) \frac{v_1 \delta_l^2 \rho}{6\omega_2^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + \\
& C_3 \frac{v_2 \delta_l^3}{2\omega_5 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (-6\omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 + 6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2) \frac{v_2 v_1 \delta_l^3 \rho}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + (-12\omega_2 v_1^2 + 6cs^2 \omega_2^2 - 6\omega_5 \omega_2 v_1^2 + 18cs^2 \omega_5 \omega_2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 - 12cs^2 \omega_5 + \omega_5 \omega_2^2 v_1^2 + 12\omega_5 v_1^2 + 6\omega_2^2 v_1^2) \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (12 - 6\omega_6 - 6\omega_3 + \omega_6 \omega_3) \frac{v_2 \delta_l^2 \rho}{6\omega_6 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\omega_2^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-3cs^2 \omega_6 \omega_3^2 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_6 \omega_3 + 18cs^2 \omega_6 \omega_3 + 6cs^2 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 - 12v_2^2 \omega_3 + 12v_2^2 \omega_6 - 12cs^2 \omega_6) \frac{\delta_l^3 \rho}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-6\omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 + 6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2) \frac{v_2 v_1 \delta_l^3 \rho}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\delta_l^3 \rho}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\delta_l \rho \delta_t}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-2\omega_4^2 \omega_2 - 6\omega_4 + 3\omega_4^2 - 6\omega_2 + 9\omega_4 \omega_2) \frac{v_3 \delta_l^2 \rho}{6\omega_4^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (-6\omega_4 + 3\omega_2^2 - 6\omega_2 - 2\omega_4 \omega_2^2 + 9\omega_4 \omega_2) \frac{v_1 \delta_l^2 \rho}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3 \delta_l^3}{2\omega_4^2 \omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (-6\omega_4^2 \omega_2 + 6\omega_4^2 + 6\omega_2^2 + \omega_4^2 \omega_2^2 - 6\omega_4 \omega_2^2) \frac{v_3 v_1 \delta_l^3 \rho}{6\omega_4^2 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + (-12\omega_2 v_1^2 + 6cs^2 \omega_2^2 - 6\omega_5 \omega_2 v_1^2 + 18cs^2 \omega_5 \omega_2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 - 12cs^2 \omega_5 + \omega_5 \omega_2^2 v_1^2 + 12\omega_5 v_1^2 + 6\omega_2^2 v_1^2) \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-6\omega_4 + 3\omega_4^2 + 9\omega_4\omega_3 - 2\omega_4^2\omega_3 - 6\omega_3) \frac{v_3\delta_l^2\rho}{6\omega_4^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-6\omega_4 - 2\omega_4\omega_3^2 + 9\omega_4\omega_3 - 6\omega_3 + 3\omega_3^2) \frac{v_2\delta_l^2\rho}{6\omega_4\omega_3^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_4^2\omega_2^2\omega_3^2 + \omega_4\omega_2\omega_3^2 + \omega_2^2\omega_3^2 - 2\omega_4^2\omega_2^2\omega_3 + \omega_4^2\omega_2^2 + \omega_4^2\omega_2\omega_3 + \omega_4\omega_2^2\omega_3 + \omega_4^2\omega_3^2 - 2\omega_4\omega_2^2\omega_3^2 - 2\omega_4^2\omega_2\omega_3^2) \frac{2v_3v_2v_1\delta_l^3}{\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\
& + (-6\omega_4\omega_3^2 + 3\omega_4^2 + 6\omega_4\omega_3 - 6\omega_4^2\omega_3 + 3\omega_3^2 + 2\omega_4^2\omega_3^2) \frac{v_3v_2\delta_l^3\rho}{3\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_4^2\omega_2 + 3\omega_4^2 + 3\omega_2^2 + 2\omega_4^2\omega_2^2 - 6\omega_4\omega_2^2 + 6\omega_4\omega_2) \frac{v_3v_1\delta_l^3\rho}{3\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2^2\omega_3 + 2\omega_2^2\omega_3^2 + 3\omega_2^2 - 6\omega_2\omega_3^2 + 6\omega_2\omega_3 + 3\omega_3^2) \frac{v_2v_1\delta_l^3\rho}{3\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_4^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_4\omega_3^2 + 6\omega_4^2 - 6\omega_4^2\omega_3 + 6\omega_3^2 + \omega_4^2\omega_3^2) \frac{v_3v_2\delta_l^3\rho}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + (-3cs^2\omega_6\omega_3^2 + v_2^2\omega_6\omega_3^2 - 6v_2^2\omega_6\omega_3 + 18cs^2\omega_6\omega_3 + \\
& 6cs^2\omega_3^2 + 6v_2^2\omega_3^2 - 12cs^2\omega_3 - 12v_2^2\omega_3 + 12v_2^2\omega_6 - 12cs^2\omega_6) \frac{\delta_l^3\rho}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (12 - 6\omega_7 - 6\omega_4 + \omega_7\omega_4) \frac{v_3\delta_l^2\rho}{6\omega_7\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_3^2} \\
& + C_9 \frac{v_1\delta_l^3}{2\omega_7\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 - 6\omega_7\omega_4v_3^2 - 12\omega_4v_3^2 + 6\omega_4^2v_3^2 + 12\omega_7v_3^2 + \omega_7\omega_4^2v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_4cs^2) \frac{\delta_l^3\rho}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} \\
& + (-6\omega_4^2\omega_2 + 6\omega_4^2 + 6\omega_2^2 + \omega_4^2\omega_2^2 - 6\omega_4\omega_2^2) \frac{v_3v_1\delta_l^3\rho}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{v_2\delta_l^3}{2\omega_7\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& (6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 - 6\omega_7\omega_4v_3^2 - 12\omega_4v_3^2 + 6\omega_4^2v_3^2 + 12\omega_7v_3^2 + \omega_7\omega_4^2v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_4cs^2) \frac{\delta_l^3\rho}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + (-6\omega_4\omega_3^2 + 6\omega_4^2 - 6\omega_4^2\omega_3 + 6\omega_3^2 + \omega_4^2\omega_3^2) \frac{v_3v_2\delta_l^3\rho}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3\delta_l^3}{6\omega_7\omega_4^2\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\delta_l^3\rho}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2 - \omega_2^2 + 3\omega_2) \frac{\delta_l\rho\delta_l^2}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-\omega_5^2\omega_2^2 + 2\omega_2^3 - \omega_5^2\omega_2 - 4\omega_2^2 + 2\omega_5^2 - 4\omega_5\omega_2 + 8\omega_5\omega_2^2 - 2\omega_5\omega_2^3) \frac{v_1\delta_l^2\rho\delta_t}{2\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_2} + \\
& C_{13} \frac{\delta_l^3\rho}{12\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_3^1} + C_{14} \frac{\delta_l^4}{24\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_4^1} + C_{15} \frac{v_1\delta_l^4\rho}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_4^1} + (-2 + 3\omega_3 - \omega_3^2) \frac{\delta_l\rho\delta_l^2}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (-24\omega_2^2\omega_3 + 13\omega_2^2\omega_3^2 + 12\omega_2^2 - \omega_2^2\omega_3^3 + 7\omega_2\omega_3^2 - 24\omega_2\omega_3^2 + 12\omega_2\omega_3 + 12\omega_3^2 - 6\omega_3^3) \frac{v_2\delta_l^2\rho\delta_t}{12\omega_2^2\omega_3^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-\omega_2^3\omega_3^2 - 24\omega_2^2\omega_3 - 6\omega_2^3 + 13\omega_2^2\omega_3^2 + 12\omega_2^2 + 7\omega_2^3\omega_3 - 24\omega_2\omega_3^2 + 12\omega_2\omega_3 + 12\omega_3^2) \frac{v_1\delta_l^2\rho\delta_t}{12\omega_2^2\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& C_{16} \frac{v_2v_1\delta_l^3\rho}{6\omega_5\omega_3^2\omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_2^2 \partial x_2} + C_{17} \frac{\delta_l^3\rho}{12\omega_5^2\omega_3^2\omega_3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_2} + C_{18} \frac{v_2v_1\delta_l^4}{6\omega_5^2\omega_3^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_3^1 \partial x_2} + C_{19} \frac{v_2\delta_l^4\rho}{12\omega_5^2\omega_3^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_3^1 \partial x_2} + \\
& C_{20} \frac{v_1\delta_l^4\rho}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-\omega_6^2\omega_3 - \omega_6^2\omega_3^2 - 2\omega_6\omega_3^3 + 8\omega_6\omega_3^2 - 4\omega_3^2 - 4\omega_6\omega_3 + 2\omega_6^2 + 2\omega_3^3) \frac{v_2\delta_l^2\rho\delta_t}{2\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2} + \\
& C_{21} \frac{\delta_l^3\rho}{12\omega_2\omega_6^2\omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_2 \partial x_2} + C_{22} \frac{v_2v_1\delta_l^3\rho}{6\omega_2^3\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2} + C_{23} \frac{\delta_l^4}{4\omega_2^2\omega_6^2\omega_3^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2} + C_{24} \frac{v_1\delta_l^4\rho}{12\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_2^1 \partial x_2} + \\
& C_{25} \frac{v_2\delta_l^4\rho}{12\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + C_{26} \frac{\delta_l^3\rho}{12\omega_2^2\omega_6^3} \frac{\partial^4 v_2}{\partial t \partial x_3^2} + C_{27} \frac{v_2v_1\delta_l^5}{6\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + C_{28} \frac{v_2\delta_l^4\rho}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{29} \frac{v_1\delta_l^4\rho}{12\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^2} \\
& + C_{30} \frac{\delta_l^4}{24\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{31} \frac{v_2\delta_l^4\rho}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 + 3\omega_4 - \omega_4^2) \frac{\delta_l\rho\delta_l^2}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (-24\omega_4^2\omega_2 - 6\omega_4^3 - \omega_4^2\omega_2^2 + 12\omega_4^2 + 7\omega_4^3\omega_2 + 12\omega_4^2 + 13\omega_4^2\omega_2^2 - 24\omega_4\omega_2^2 + 12\omega_4\omega_2) \frac{v_3\delta_l^2\rho\delta_t}{12\omega_4^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-24\omega_4^2\omega_2 + 12\omega_4^2 - 6\omega_2^3 - \omega_2^2\omega_3^2 + 12\omega_2^2 + 13\omega_4^2\omega_2^2 - 24\omega_4\omega_2^2 + 7\omega_4\omega_3^2 + 12\omega_4\omega_2) \frac{v_1\delta_l^2\rho\delta_t}{12\omega_4^2\omega_3^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& C_{32} \frac{v_3v_1\delta_l^3\rho}{6\omega_4^3\omega_5\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_2^2 \partial x_3} + C_{33} \frac{\delta_l^3\rho}{12\omega_4\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{34} \frac{v_3v_1\delta_l^4}{6\omega_4^2\omega_5^2\omega_2^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{35} \frac{v_3\delta_l^4\rho}{12\omega_4^3\omega_5^2\omega_2^3\delta_t} \frac{\partial^4 v_1}{\partial x_3^1 \partial x_3} + \\
& C_{36} \frac{v_1\delta_l^4\rho}{12\omega_5^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-6\omega_4^3 - 24\omega_4\omega_3^2 + 12\omega_4^2 + 12\omega_4\omega_3 - \omega_4^3\omega_3^2 - 24\omega_4^2\omega_3 + 12\omega_3^2 + 13\omega_4^2\omega_3^2 + 7\omega_4^3\omega_3) \frac{v_3\delta_l^2\rho\delta_t}{12\omega_4^3\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (7\omega_4\omega_3^3 - 24\omega_4\omega_3^2 + 12\omega_4^2 + 12\omega_4\omega_3 - 24\omega_4^2\omega_3 + 12\omega_3^2 + 13\omega_4^2\omega_3^2 - 6\omega_3^3 - \omega_4^2\omega_3^3) \frac{v_2\delta_l^2\rho\delta_t}{12\omega_4^2\omega_3^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_3v_2\delta_l^3\rho}{6\omega_4^3\omega_2\omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{38} \frac{v_3v_1\delta_l^3\rho}{6\omega_4^3\omega_2^3\omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{39} \frac{v_2v_1\delta_l^3\rho}{6\omega_4\omega_3^2\omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{40} \frac{v_3v_2\delta_l^4}{6\omega_4^3\omega_5^2\omega_3^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{41} \frac{v_3v_2v_1\delta_l^4\rho}{6\omega_4^3\omega_5^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_2 \partial x_3} + C_{42} \frac{v_3\delta_l^4\rho}{12\omega_4^3\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{43} \frac{v_2\delta_l^4\rho}{12\omega_4^2\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{44} \frac{v_3v_2\delta_l^3\rho}{6\omega_4^3\omega_6\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\delta_l^3\rho}{12\omega_4\omega_6^2\omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{46} \frac{v_3v_1\delta_l^4}{\omega_4^3\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{47} \frac{v_3\delta_l^4\rho}{12\omega_4^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{48} \frac{v_3v_2v_1\delta_l^4\rho}{6\omega_4^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& C_{49} \frac{v_1\delta_l^4\rho}{12\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{50} \frac{v_3v_2\delta_l^4}{6\omega_4^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{51} \frac{v_3\delta_l^4\rho}{12\omega_4^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{52} \frac{v_2\delta_l^4\rho}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (8\omega_7\omega_4^2 + 2\omega_4^3 - 2\omega_7\omega_4^3 - 4\omega_4^2 + 2\omega_7^2 - 4\omega_7\omega_4 - \omega_7^2\omega_4 - \omega_7^2\omega_4^2) \frac{v_3\delta_l^2\rho\delta_t}{2\omega_7^2\omega_4^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2} + C_{53} \frac{\delta_l^3\rho}{12\omega_7^2\omega_4^2\omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} +
\end{aligned}$$

$$\begin{aligned}
& C_{54} \frac{v_3 v_1 \delta_l^3 \rho}{6 \omega_7 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + C_{55} \frac{\delta_l^4}{4 \omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{56} \frac{v_1 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{57} \frac{v_3 \delta_l^4 \rho}{12 \omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{58} \frac{\delta_l^3 \rho}{12 \omega_7^2 \omega_4^3 \omega_3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + C_{59} \frac{v_3 v_2 \delta_l^3 \rho}{6 \omega_7 \omega_4^3 \omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + C_{60} \frac{v_2 v_1 \delta_l^4}{\omega_7^2 \omega_4^3 \omega_5^2 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{61} \frac{v_2 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{62} \frac{v_1 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{63} \frac{v_3 v_2 v_1 \delta_l^4 \rho}{6 \omega_4^3 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{64} \frac{\delta_l^4}{4 \omega_7^2 \omega_4^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{65} \frac{v_2 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{66} \frac{v_3 \delta_l^4 \rho}{12 \omega_4^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{67} \frac{\delta_l^3 \rho}{12 \omega_7^2 \omega_4^3 \partial t \partial x_3^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{68} \frac{v_3 v_1 \delta_l^4}{6 \omega_7^2 \omega_4^3 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{69} \frac{v_3 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{70} \frac{v_1 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& + C_{71} \frac{v_3 v_2 \delta_l^4}{6 \omega_7^2 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{72} \frac{v_3 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{73} \frac{v_2 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{74} \frac{\delta_l^4}{24 \omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{75} \frac{v_3 \delta_l^4 \rho}{12 \omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -6 \omega_2 v_1^2 + 3 c s^2 \omega_2^2 + 3 \omega_5 \omega_2 v_1^2 + 15 c s^2 \omega_5 \omega_2 - 3 c s^2 \omega_5 \omega_2^2 - 6 c s^2 \omega_2 - 3 \omega_2^2 + 6 \omega_2 - 12 c s^2 \omega_5 - 3 \omega_5 \omega_2 + \omega_5 \omega_2^2 - \omega_5 \omega_2^2 v_1^2 + 3 \omega_2^2 v_1^2 \\
C_2 &= -12 \omega_2 v_1^2 + 6 c s^2 \omega_2^2 + 18 \omega_5 \omega_2 v_1^2 + 18 c s^2 \omega_5 \omega_2 - 3 c s^2 \omega_5 \omega_2^2 - 12 c s^2 \omega_2 - 6 \omega_2^2 + 12 \omega_2 - 12 c s^2 \omega_5 - 6 \omega_5 \omega_2 + 2 \omega_5 \omega_2^2 - 5 \omega_5 \omega_2^2 v_1^2 - 12 \omega_5 v_1^2 + 6 \omega_2^2 v_1^2 \\
C_3 &= c s^2 \omega_5 \omega_2^2 \omega_3 - 3 \omega_5 \omega_2^2 v_1^2 \omega_3 + \omega_2^2 v_1^2 \omega_3^2 - 2 c s^2 \omega_2 \omega_3^2 + 4 \omega_5 v_1^2 \omega_3^2 + \omega_5 \omega_2^2 v_1^2 \omega_3^2 - c s^2 \omega_5 \omega_2^2 \omega_3^2 + 4 c s^2 \omega_5 \omega_2 \omega_3^2 - 4 \omega_5 \omega_2 v_1^2 \omega_3^2 + 2 \omega_5 \omega_2^2 v_1^2 + \\
c s^2 \omega_2^2 \omega_3^2 - 2 \omega_2 v_1^2 \omega_3^2 + 2 \omega_5 \omega_2 v_1^2 \omega_3 - 2 c s^2 \omega_5 \omega_2 \omega_3^2 - 2 c s^2 \omega_5 \omega_2 \omega_3 \\
C_4 &= 2 v_2^2 \omega_6 \omega_3^2 + c s^2 \omega_2 \omega_6 \omega_3^2 - 3 v_2^2 \omega_2 \omega_6 \omega_3^2 + 2 v_2^2 \omega_2 \omega_6 \omega_3 - 2 c s^2 \omega_2 \omega_6 \omega_3 - 2 c s^2 \omega_2^2 \omega_6 + 4 v_2^2 \omega_2^2 \omega_6 - 4 v_2^2 \omega_2^2 \omega_6 \omega_3 + 4 c s^2 \omega_2^2 \omega_6 \omega_3 - 2 v_2^2 \omega_2^2 \omega_3 - \\
2 c s^2 \omega_2^2 \omega_3 + c s^2 \omega_2^2 \omega_3^2 + v_2^2 \omega_2^2 \omega_3^2 - c s^2 \omega_2^2 \omega_6 \omega_3^2 + v_2^2 \omega_2^2 \omega_6 \omega_3 \\
C_5 &= -3 c s^2 \omega_6 \omega_3^2 - v_2^2 \omega_6 \omega_3^2 + 3 v_2^2 \omega_6 \omega_3 + 15 c s^2 \omega_6 \omega_3 + \omega_6 \omega_3^2 + 3 c s^2 \omega_3^2 + 3 v_2^2 \omega_3^2 - 6 c s^2 \omega_3 - 6 v_2^2 \omega_3 + 6 \omega_3 - 3 \omega_3^2 - 3 \omega_6 \omega_3 - 12 c s^2 \omega_6 \\
C_6 &= -3 c s^2 \omega_6 \omega_3^2 - 5 v_2^2 \omega_6 \omega_3^2 + 18 v_2^2 \omega_6 \omega_3 + 18 c s^2 \omega_6 \omega_3 + 2 \omega_6 \omega_3^2 + 6 c s^2 \omega_3^2 + 6 v_2^2 \omega_3^2 - 12 c s^2 \omega_3 - 12 v_2^2 \omega_3 + 12 \omega_3 - 6 \omega_3^2 - 6 \omega_6 \omega_3 - 12 v_2^2 \omega_6 - 12 c s^2 \omega_6 \\
C_7 &= -2 \omega_4^2 c s^2 \omega_2 - 2 \omega_4 c s^2 \omega_5 \omega_2 + 2 \omega_4 \omega_5 \omega_2 v_1^2 + \omega_4^2 \omega_5 \omega_2^2 v_1^2 - 2 \omega_4^2 \omega_2 v_1^2 + \omega_4 c s^2 \omega_5 \omega_2^2 + \omega_4^2 c s^2 \omega_2^2 + 4 \omega_4^2 \omega_5 v_1^2 + \omega_4^2 \omega_2^2 v_1^2 - 4 \omega_4^2 \omega_5 \omega_2 v_1^2 + \\
4 \omega_4^2 c s^2 \omega_5 \omega_2 - 2 \omega_4^2 c s^2 \omega_5 + 2 \omega_5 \omega_2^2 v_1^2 - 3 \omega_4 \omega_5 \omega_2^2 v_1^2 - \omega_4^2 c s^2 \omega_5 \omega_2^2 \\
C_8 &= \omega_4 c s^2 \omega_6 \omega_3^2 - 3 \omega_4 v_2^2 \omega_6 \omega_3^2 + 2 v_2^2 \omega_6 \omega_3^2 + 2 \omega_4 v_2^2 \omega_6 \omega_3 - 2 \omega_4 c s^2 \omega_6 \omega_3 - 2 \omega_4^2 v_2^2 \omega_3 - 2 \omega_4^2 c s^2 \omega_3 - 2 \omega_4^2 c s^2 \omega_6 + 4 \omega_4^2 v_2^2 \omega_6 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - \\
\omega_4^2 c s^2 \omega_6 \omega_3^2 + 4 \omega_4^2 c s^2 \omega_6 \omega_3 - 4 \omega_4^2 v_2^2 \omega_6 \omega_3 + \omega_4^2 v_2^2 \omega_3^2 + \omega_4^2 c s^2 \omega_3^2 \\
C_9 &= 4 \omega_7 v_3^2 \omega_2^2 - \omega_7 \omega_4^2 c s^2 \omega_2^2 + \omega_7 \omega_4^2 v_3^2 \omega_2^2 - 2 \omega_7 c s^2 \omega_2^2 - 3 \omega_7 \omega_4^2 v_3^2 \omega_2 + \omega_4^2 c s^2 \omega_2^2 + \omega_4^2 v_3^2 \omega_2^2 + \omega_7 \omega_4^2 c s^2 \omega_2 + 2 \omega_7 \omega_4 v_3^2 \omega_2 - 2 \omega_4 c s^2 \omega_2^2 - \\
2 \omega_4 v_3^2 \omega_2^2 + 2 \omega_7 \omega_4^2 v_3^2 - 2 \omega_7 \omega_4 c s^2 \omega_2 + 4 \omega_7 \omega_4 c s^2 \omega_2^2 - 4 \omega_7 \omega_4 v_3^2 \omega_2^2 \\
C_{10} &= -2 \omega_4 v_3^2 \omega_2^2 - 2 \omega_7 \omega_4 c s^2 \omega_3 + 2 \omega_7 \omega_4 v_3^2 \omega_3 - 2 \omega_4 c s^2 \omega_3^2 - 4 \omega_7 \omega_4 v_3^2 \omega_3^2 + 4 \omega_7 \omega_4 c s^2 \omega_3^2 + \omega_7 \omega_4^2 v_3^2 \omega_3^2 - 2 \omega_7 c s^2 \omega_3^2 + 4 \omega_7 v_3^2 \omega_3^2 - \\
\omega_7 \omega_4^2 c s^2 \omega_3^2 + 2 \omega_7 \omega_4^2 v_3^2 + \omega_4^2 v_3^2 \omega_3^2 + \omega_7 \omega_4^2 c s^2 \omega_3 - 3 \omega_7 \omega_4^2 v_3^2 \omega_3 + \omega_4^2 c s^2 \omega_3^2 \\
C_{11} &= \omega_7 \omega_4^2 + 3 \omega_4^2 c s^2 + 6 \omega_4 - 3 \omega_7 \omega_4^2 c s^2 - 3 \omega_4^2 - 12 \omega_7 c s^2 + 3 \omega_7 \omega_4 v_3^2 - 3 \omega_7 \omega_4 - 6 \omega_4 v_3^2 + 3 \omega_4^2 v_3^2 - \omega_7 \omega_4^2 v_3^2 + 15 \omega_7 \omega_4 c s^2 - 6 \omega_4 c s^2 \\
C_{12} &= 2 \omega_7 \omega_4^2 + 6 \omega_4^2 c s^2 + 12 \omega_4 - 3 \omega_7 \omega_4^2 c s^2 - 6 \omega_4^2 - 12 \omega_7 c s^2 + 18 \omega_7 \omega_4 v_3^2 - 6 \omega_7 \omega_4 - 12 \omega_4 v_3^2 + 6 \omega_4^2 v_3^2 - 12 \omega_7 v_3^2 - 5 \omega_7 \omega_4^2 v_3^2 + 18 \omega_7 \omega_4 c s^2 - 12 \omega_4 c s^2 \\
C_{13} &= \omega_5^2 \omega_3^2 + 12 c s^2 \omega_2^2 + 27 \omega_5^2 \omega_2^2 v_1^2 - 11 \omega_5^2 \omega_2^2 + 48 \omega_5 \omega_2 v_1^2 + 12 \omega_5^2 v_1^2 - 6 c s^2 \omega_2^2 + 24 c s^2 \omega_5 \omega_2 - 3 \omega_5^2 \omega_2^2 v_1^2 - 36 c s^2 \omega_5 \omega_2^2 + 6 \omega_2^2 + 12 \omega_5^2 \omega_2 + 9 c s^2 \omega_5 \omega_2^2 - \\
12 \omega_2^2 - 2 c s^2 \omega_5^2 \omega_2^2 + 15 \omega_5 \omega_2^2 v_1^2 + 25 c s^2 \omega_5^2 \omega_2^2 - 6 \omega_2^3 v_1^2 - 24 \omega_5 \omega_2 + 36 \omega_5 \omega_2^2 - 60 \omega_5 \omega_2^2 v_1^2 - 48 c s^2 \omega_5^2 \omega_2^2 - 9 \omega_5 \omega_2^3 + 12 \omega_2^2 v_1^2 - 42 \omega_5^2 \omega_2 v_1^2 + 24 c s^2 \omega_5^2 \\
C_{14} &= 72 \omega_5 \omega_2^2 v_1^4 - 24 c s^4 \omega_5 \omega_2^2 - 72 c s^2 \omega_5^2 \omega_2^2 v_1^2 + 24 \omega_5^2 \omega_2^2 v_1^2 + 6 c s^4 \omega_5 \omega_2^2 + 24 \omega_5^2 \omega_2^2 v_1^4 + 12 c s^2 \omega_5^2 \omega_2^2 v_1^2 + 48 \omega_5 \omega_2 v_1^2 - 24 c s^2 \omega_5 \omega_2 v_1^2 - 24 \omega_2^2 v_1^4 - \\
24 c s^2 \omega_5 \omega_2 - 3 \omega_5^2 \omega_2^2 v_1^2 + 6 c s^2 \omega_5^2 \omega_2^2 v_1^2 + 24 c s^2 \omega_5 \omega_2^2 - 18 \omega_5 \omega_2^2 v_1^4 + 24 c s^4 \omega_5^2 - 6 c s^2 \omega_5 \omega_2^2 + 12 \omega_3^2 v_1^4 - 24 c s^2 \omega_5^2 \omega_2^2 v_1^2 + 24 c s^4 \omega_5 \omega_2 - \\
12 c s^2 \omega_5^2 \omega_2^2 v_1^2 + c s^2 \omega_5^2 \omega_2^2 + 18 \omega_5 \omega_2^2 v_1^2 + 3 \omega_5^2 \omega_2^2 v_1^4 - 48 c s^4 \omega_5^2 \omega_2^2 - 8 c s^2 \omega_5^2 \omega_2^2 - 12 \omega_3^2 v_1^2 - 96 c s^2 \omega_5^2 \omega_2^2 v_1^2 - 3 c s^4 \omega_5^2 \omega_2^3 - 24 \omega_5^2 \omega_2^2 v_1^4 - 72 \omega_5 \omega_2 v_1^2 + 12 c s^2 \omega_5^2 \omega_2^2 + 48 c s^2 \omega_5 \omega_2^2 v_1^2 - 48 \omega_5 \omega_2 v_1^4 + 24 \omega_2^2 v_1^2 + 156 c s^2 \omega_5^2 \omega_2 v_1^2 - 24 \omega_5^2 \omega_2 v_1^2 \\
C_{15} &= -\omega_5^2 \omega_3^2 - 12 c s^2 \omega_2^2 - 16 \omega_5^2 \omega_2^2 v_1^2 + 8 \omega_5^2 \omega_2^2 - 12 \omega_5 \omega_2 v_1^2 - 12 \omega_5^2 v_1^2 + 6 c s^2 \omega_2^2 - 12 c s^2 \omega_5 \omega_2 + 2 \omega_5^2 \omega_2^2 v_1^2 + 24 c s^2 \omega_5 \omega_2^2 - 6 \omega_2^3 - 6 \omega_5^2 \omega_2 - 6 c s^2 \omega_5 \omega_2^3 + \\
12 \omega_2^2 + c s^2 \omega_5^2 \omega_2^2 - 6 \omega_5 \omega_2^2 v_1^2 - 20 c s^2 \omega_5^2 \omega_2^2 + 6 \omega_2^2 v_1^2 + 12 \omega_5 \omega_2 - 24 \omega_5 \omega_2^2 + 24 \omega_5 \omega_2^2 v_1^2 + 42 c s^2 \omega_5^2 \omega_2 + 6 \omega_5 \omega_2^3 - 12 \omega_2^2 v_1^2 + 24 \omega_5^2 \omega_2 v_1^2 - 24 c s^2 \omega_5^2 \\
C_{16} &= -6 \omega_2^3 \omega_3^2 - 6 \omega_5 \omega_2^2 \omega_3 + \omega_5 \omega_2^2 \omega_3^2 + 3 \omega_2^3 \omega_3^2 - 7 \omega_5 \omega_2^2 \omega_3^2 - 12 \omega_5 \omega_3^3 + 12 \omega_5 \omega_2^3 \omega_3 + 10 \omega_5 \omega_2^2 \omega_3^2 + 12 \omega_2^2 \omega_3^2 + 12 \omega_5 \omega_2^2 \omega_3^2 - 6 \omega_2^2 \omega_3^2 - \\
12 \omega_5 \omega_2 \omega_3^2 + 24 \omega_5 \omega_2 \omega_3^2 - 6 \omega_5 \omega_2^3 \\
C_{17} &= \omega_5^2 \omega_2^2 v_1^2 \omega_3 - 30 c s^2 \omega_5 \omega_2^2 \omega_3 + 6 \omega_5^2 \omega_2^2 v_1^2 - 30 \omega_5 \omega_2^2 v_1^2 \omega_3 - 30 c s^2 \omega_5^2 \omega_2 \omega_3 - \omega_5^2 \omega_2^2 v_1^2 + 9 c s^2 \omega_5 \omega_2^2 \omega_3 + 12 c s^2 \omega_5 \omega_2^2 - 12 \omega_2^2 v_1^2 \omega_3 - \\
6 c s^2 \omega_5 \omega_2^2 + 36 \omega_5^2 \omega_2 v_1^2 \omega_3 + 12 c s^2 \omega_5^2 \omega_2 \omega_3 + 3 c s^2 \omega_5^2 \omega_2^3 - 6 \omega_5^2 \omega_2^2 v_1^2 + 2 c s^2 \omega_5^2 \omega_2^2 \omega_3 + 9 \omega_5 \omega_2^2 v_1^2 \omega_3 - 18 c s^2 \omega_5^2 \omega_2^2 \omega_3 + 12 c s^2 \omega_5^2 \omega_2 \omega_3 - 10 \omega_5^2 \omega_2^2 v_1^2 \omega_3 + \\
22 c s^2 \omega_5^2 \omega_2^2 \omega_3 + 12 \omega_5 \omega_2^2 v_1^2 + 12 c s^2 \omega_5 \omega_2^2 \omega_3 - 6 \omega_2^2 v_1^2 \omega_3 - 6 c s^2 \omega_5^2 \omega_2^2 \omega_3 - 24 \omega_5 \omega_2 v_1^2 \omega_3 + 12 c s^2 \omega_5 \omega_2 \omega_3 - 12 \omega_5^2 \omega_2 v_1^2 \\
C_{18} &= -12 \omega_2^2 v_1^2 \omega_3^3 + 12 \omega_5^2 \omega_2 v_1^2 \omega_3^2 - 12 \omega_2^2 \omega_2^2 v_1^2 \omega_3 + 6 \omega_5 \omega_2^2 \omega_3^2 - 12 c s^2 \omega_5 \omega_2^2 \omega_3^2 - 36 c s^2 \omega_5^2 \omega_3^2 - 3 \omega_2^2 \omega_3^2 + 30 \omega_5^2 \omega_2 v_1^2 \omega_3^2 + 6 c s^2 \omega_5 \omega_2^2 \omega_3^2 - \\
3 \omega_5^2 \omega_2^2 + 42 c s^2 \omega_5 \omega_2 \omega_3^2 - 24 c s^2 \omega_5^2 \omega_2 \omega_3^2 + 6 \omega_5^2 \omega_2^2 v_1^2 - 21 \omega_5 \omega_2^2 \omega_3^2 - 12 \omega_5 \omega_2^2 v_1^2 \omega_3^2 + 6 \omega_5 \omega_2^2 \omega_3^2 - 6 \omega_2^2 \omega_3^2 + 78 c s^2 \omega_5^2 \omega_2 \omega_3^2 - 12 c s^2 \omega_5 \omega_2 \omega_3^2 + \\
6 \omega_2^2 \omega_3^3 + 6 \omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 42 \omega_5 \omega_2^2 v_1^2 \omega_3^2 + 7 \omega_5^2 \omega_2^2 \omega_3^2 + 6 c s^2 \omega_5^2 \omega_2^2 \omega_3^2 - 48 c s^2 \omega_5 \omega_2 \omega_3^2 + 42 c s^2 \omega_5^2 \omega_2^2 \omega_3^2 - 24 c s^2 \omega_5 \omega_2 \omega_3^2 + 12 \omega_5 \omega_2 \omega_3^2 + 24 \omega_5^2 v_1^2 \omega_3^2 +
\end{aligned}$$

$$6cs^2\omega_5^3\omega_3^3 - 3\omega_5^2\omega_5^2\omega_3^2 - 24\omega_5\omega_2v_1^2\omega_3^3 + 6\omega_5^3v_1^2\omega_3^3 + 6\omega_5^2\omega_2^2v_1^2\omega_3 - 12\omega_5\omega_2^3v_1^2\omega_3^3 - 12\omega_5^2\omega_2^2v_1^2\omega_3^2 - 12cs^2\omega_5^2\omega_2^2\omega_3 + 6cs^2\omega_5^2\omega_2^3\omega_3^3 - \omega_5^2\omega_3^3 + 6\omega_5\omega_2^3v_1^2\omega_3^2 + 6\omega_5^2\omega_2^2v_1^2\omega_3^3 + \omega_5^2\omega_3^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^2$$

$$\begin{aligned} C_{19} = & -12\omega_5^2v_1^2\omega_3^3 - 18\omega_5^2\omega_5^2\omega_3^2v_1^2\omega_3 + 3\omega_5\omega_2^3\omega_3^3 - 12cs^2\omega_5\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^3 - 30\omega_5^2\omega_2v_1^2\omega_3^3 + 12cs^2\omega_5\omega_3^2\omega_2^3 - 6\omega_5\omega_3^2\omega_2^3 + 36cs^2\omega_5\omega_2^3\omega_3^3 - \\ & 24cs^2\omega_5^2\omega_2\omega_3^2 + 12\omega_5^2\omega_3^2v_1^2 - 6\omega_5\omega_2^3\omega_3^3 + 3\omega_5^2\omega_3^2v_1^2\omega_3^3 - 24\omega_5\omega_2^3v_1^2\omega_3^2 + 12\omega_5\omega_2^3\omega_3^2 + 36cs^2\omega_5\omega_2^3\omega_3^3 - 24cs^2\omega_5\omega_2^3\omega_3^2 + 36\omega_5\omega_2^2v_1^2\omega_3^3 + \\ & 3\omega_5^2\omega_2^3\omega_3^3 + 6cs^2\omega_5^2\omega_2^3\omega_3^3 - 32cs^2\omega_5^2\omega_2^3\omega_3^3 + 48cs^2\omega_5^2\omega_2^3\omega_3^2 - 12cs^2\omega_5\omega_2\omega_3^3 + 24\omega_5^2v_1^2\omega_3^3 + 6cs^2\omega_5^2\omega_3^3 - 6\omega_5^2\omega_2^3\omega_3^2 - 12\omega_5\omega_2v_1^2\omega_3^3 + 6\omega_3^2v_1^2\omega_3^3 - \\ & 12\omega_5\omega_2^3v_1^2\omega_3^3 + 12\omega_5^2\omega_2^2v_1^2\omega_3^2 - 12cs^2\omega_5^2\omega_2^2\omega_3 + 4cs^2\omega_5^2\omega_2^3\omega_3^3 - \omega_5^2\omega_3^3\omega_3^3 + 12\omega_5\omega_2^3v_1^2\omega_3^2 + 2\omega_5^2\omega_3^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^2 \end{aligned}$$

$$C_{20} = -\omega_5^2\omega_3^3 - 12cs^2\omega_5^2 - 8\omega_5^2\omega_2^2v_1^2 + 11\omega_5^2\omega_2^2 - 36\omega_5\omega_2v_1^2 + 12\omega_5^2v_1^2 + 6cs^2\omega_5^2\omega_2^2 + \omega_5^2\omega_3^2v_1^2 + 48cs^2\omega_5\omega_2^2 - 6\omega_2^3 - 12\omega_5^2\omega_2^2 - \\ 12cs^2\omega_5\omega_2^3 + 12\omega_2^2 + 4cs^2\omega_5^2\omega_2^3 - 12\omega_5\omega_2^3v_1^2 - 44cs^2\omega_5^2\omega_2^2 + 6\omega_2^3v_1^2 + 24\omega_5\omega_2^2 - 36\omega_5\omega_2^2 + 48\omega_5\omega_2^2v_1^2 + 90cs^2\omega_5^2\omega_2^2 + 9\omega_5\omega_2^3 - 12\omega_2^2v_1^2 - 48cs^2\omega_5^2\omega_2^2$$

$$C_{21} = -6v_2^2\omega_6\omega_3^3 - 6cs^2\omega_6\omega_3^3 - 24v_2^2\omega_2\omega_6^2 + 12cs^2\omega_2\omega_6^2 - 6v_2^2\omega_2\omega_6^3 - 6cs^2\omega_2\omega_6\omega_3^3 + 9cs^2\omega_2\omega_6\omega_3^3 + 9v_2^2\omega_2\omega_6\omega_3^3 + 12cs^2\omega_6\omega_3^3 + 12v_2^2\omega_6\omega_3^3 - \\ 30cs^2\omega_2\omega_6\omega_3^3 - 30v_2^2\omega_2\omega_6\omega_3^3 + 12cs^2\omega_2\omega_6^2 + 12v_2^2\omega_2\omega_6^3 + 12cs^2\omega_2\omega_6\omega_3 - 30cs^2\omega_2\omega_6\omega_3^3 + 36v_2^2\omega_2\omega_6\omega_3^3 - 12v_2^2\omega_6\omega_3 + \\ 12cs^2\omega_6\omega_3 - 18cs^2\omega_6\omega_3^3 + 6v_2^2\omega_6\omega_3^3 - 10v_2^2\omega_2\omega_6\omega_3^3 + 22cs^2\omega_2\omega_6\omega_3^3 - v_2^2\omega_6\omega_3^3 + 3cs^2\omega_6\omega_3^3 + v_2^2\omega_2\omega_6\omega_3^3 - 2cs^2\omega_2\omega_6\omega_3^3$$

$$C_{22} = -6\omega_2^3\omega_3^3 + 12\omega_2\omega_6\omega_3^3 + 3\omega_2^3\omega_3^3 + 24\omega_2^3\omega_6\omega_3 - 6\omega_2\omega_6\omega_3^2 - 10\omega_2^3\omega_6\omega_3^2 - 12\omega_2^3\omega_6\omega_3 + 12\omega_2^2\omega_3^2 + \omega_2^3\omega_6\omega_3^3 - 6\omega_2^2\omega_3^3 - 12\omega_2^2\omega_6\omega_3 - 6\omega_6\omega_3^3 - \\ 7\omega_2^2\omega_6\omega_3^3 + 12\omega_2^2\omega_6\omega_3^2$$

$$\begin{aligned} C_{23} = & -4\omega_5v_2^2\omega_2^2v_1^2\omega_6^2 + 12cs^2\omega_5^2\omega_2^2v_1^2\omega_6^2 + 4cs^2\omega_5^2\omega_2^2v_1^2\omega_6^2 + 10cs^2\omega_5^2v_2^2\omega_2\omega_6^2 + 20\omega_5^2v_2^2\omega_3^2v_1^2\omega_6^2 + 20\omega_5^2v_2^2\omega_2^2v_1^2\omega_6^2 + \\ & 2cs^2\omega_5\omega_2^2v_2^2\omega_6\omega_3^3 + 10cs^2\omega_5^2\omega_2^3v_1^2\omega_6^3 - 2cs^4\omega_5^2\omega_2\omega_6\omega_3^3 - 4cs^2\omega_5^2\omega_2^2\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^2\omega_6\omega_3^2 - 4cs^2\omega_5^2v_2^2\omega_2\omega_6\omega_3^2 - 3\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^3 - \\ & 2cs^2\omega_5^2v_2^2\omega_2\omega_6\omega_3^3 + 4cs^2\omega_5^2v_2^2\omega_3^2\omega_6\omega_3^3 - 4cs^2\omega_5^2\omega_2^2v_1^2\omega_6\omega_3^3 + 10\omega_5v_2^2\omega_3^2v_1^2\omega_6\omega_3^3 - 4cs^2\omega_5^2v_2^2\omega_2\omega_6\omega_3^3 - 2cs^4\omega_5^2\omega_2^2\omega_6\omega_3^3 + 4cs^2\omega_5\omega_2^2v_1^2\omega_6\omega_3^3 + \\ & 4cs^4\omega_5^2\omega_2^2\omega_6\omega_3^3 - 2cs^4\omega_5^2\omega_2^3\omega_6\omega_3^3 - 4cs^2\omega_5^2\omega_2^2\omega_6\omega_3^2 - 3cs^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 3\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^3 + cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^3 + 2cs^2\omega_5\omega_2^3v_1^2\omega_6\omega_3^3 + \\ & 4cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 + 20\omega_5^2v_2^2\omega_2^2v_1^2\omega_6\omega_3^3 - 4cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 - 2cs^4\omega_5\omega_2^2\omega_6\omega_3^2 - 4cs^2\omega_5^2v_2^2\omega_2^3\omega_6\omega_3^2 - \\ & cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 + 4cs^2\omega_5\omega_2^3\omega_6\omega_3^2 - 36\omega_5^2v_2^2\omega_2^2v_1^2\omega_6\omega_3^2 + 2cs^2\omega_5^2v_2^2\omega_2^3\omega_6\omega_3^2 - 8cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 + 2\omega_5v_2^2\omega_2^3v_1^2\omega_6\omega_3^2 - \\ & 4cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 + cs^2\omega_5\omega_2^3v_1^2\omega_6\omega_3^2 - 38\omega_5^2v_2^2\omega_2^3v_1^2\omega_6\omega_3^2 + 20\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^2 + 2\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^3 - 4\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^2 + \\ & cs^4\omega_5^2\omega_3^2\omega_6\omega_3^3 + 4cs^4\omega_5^2\omega_2^2\omega_6\omega_3^3 + 10cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^3 + cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 - 4\omega_5^2\omega_2^3\omega_3^2v_1^2\omega_6\omega_3^3 + 2cs^2\omega_5^2\omega_2^3\omega_6\omega_3^3 - 8cs^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - \\ & 8cs^2\omega_5^2\omega_2v_1^2\omega_6\omega_3^2 + 20\omega_5^2v_2^2v_1^2\omega_6\omega_3^3 - 3cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 + 2\omega_5^2v_2^2\omega_2^2v_1^2\omega_6\omega_3^3 - 2cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 + 2v_2^2\omega_3^2v_1^2\omega_6\omega_3^3 + 4cs^2\omega_5^2\omega_2v_1^2\omega_6\omega_3^2 - \\ & 4\omega_5v_2^2\omega_2v_1^2\omega_6\omega_3^2 - 2cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 - 8cs^2\omega_5^2\omega_2^2\omega_6\omega_3^2 - 4v_2^2\omega_2^2v_1^2\omega_6\omega_3^3 - 3\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^3 + 2cs^2\omega_5^2\omega_2^2v_1^2\omega_6\omega_3^2 - 2cs^4\omega_5\omega_2^3\omega_6\omega_3^2 - \\ & 38\omega_5^2v_2^2\omega_2v_1^2\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 - 4cs^2\omega_5^2\omega_2^2\omega_6\omega_3^2 - 4cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 + 10\omega_5^2v_2^2\omega_3^2v_1^2\omega_6\omega_3^2 + 12cs^2\omega_5^2v_2^2\omega_2^2\omega_6\omega_3^2 + \\ & 10cs^2\omega_5^2\omega_2^2\omega_6\omega_3^2 + cs^4\omega_5\omega_2^3\omega_6\omega_3^3 - 12cs^4\omega_5^2\omega_2^2\omega_6\omega_3^2 + 20\omega_5^2v_2^2\omega_2v_1^2\omega_6\omega_3^2 - 4cs^2\omega_5^2\omega_2^3v_1^2\omega_6\omega_3^2 \end{aligned}$$

$$C_{24} = -48v_2^2\omega_2^2\omega_6\omega_3^3 + 12cs^2\omega_2^2\omega_6\omega_3^3 + 22v_2^2\omega_2^2\omega_6\omega_3^3 - 6cs^2\omega_2^2\omega_6\omega_3^3 - 12v_2^2\omega_2^3\omega_6\omega_3 + 24v_2^2\omega_2^3\omega_6\omega_3^2 + 24cs^2\omega_2^3\omega_6\omega_3^2 - \\ 6v_2^2\omega_2^3\omega_6\omega_3^3 - 6cs^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^2\omega_6\omega_3 + cs^2\omega_2^3\omega_6\omega_3^3 - 4v_2^2\omega_2^3\omega_6\omega_3^2 - 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - 14cs^2\omega_2^3\omega_6\omega_3^2 + 48v_2^2\omega_2^3\omega_6\omega_3^2 + \\ 6cs^2\omega_2^3\omega_6\omega_3^3 + 6v_2^2\omega_2^3\omega_6\omega_3^2 + 34v_2^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2\omega_6\omega_3^2 - 12cs^2\omega_2\omega_6\omega_3^2 - 78v_2^2\omega_2^3\omega_6\omega_3^2 + 24cs^2\omega_2^3\omega_6\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2\omega_6\omega_3^2 +$$

$$C_{25} = -12\omega_2^2v_1^2\omega_3^3 + 24\omega_5^2\omega_2v_1^2\omega_3^2 - 30\omega_5^2\omega_2^2v_1^2\omega_3 - 6cs^2\omega_5\omega_2\omega_3^3 - 12cs^2\omega_5^2\omega_3^3 - 78\omega_5^2\omega_2v_1^2\omega_3^3 + 24cs^2\omega_5\omega_2\omega_3^3 + 12\omega_5^2\omega_3^2v_1^2\omega_3^2 + 4\omega_5^2\omega_2^2v_1^2\omega_3^3 + \\ 24cs^2\omega_5^2\omega_2\omega_3^3 + 22\omega_5^2\omega_3^2v_1^2\omega_3^2 + 24\omega_5\omega_2v_1^2\omega_3^2 + 6cs^2\omega_5^2\omega_2^3\omega_3^3 - 4cs^2\omega_5^2\omega_2^2\omega_3^2 + 12cs^2\omega_5^2\omega_2\omega_3^3 + 48\omega_5^2v_1^2\omega_3^3 + 6cs^2\omega_5^2\omega_3^3 - \\ 12\omega_5\omega_2v_1^2\omega_3^3 + 6\omega_5^2v_1^2\omega_3^3 + 24\omega_5^2\omega_2v_1^2\omega_3^2 - 48\omega_5^2\omega_2^2v_1^2\omega_3^2 - 12cs^2\omega_5^2\omega_2\omega_3^2 + cs^2\omega_5^2\omega_2^3\omega_3^3 + 34\omega_5^2\omega_2v_1^2\omega_3^2 - 12cs^2\omega_5^2\omega_2\omega_3^2 - 6cs^2\omega_5^2\omega_2\omega_3^2$$

$$C_{26} = 15v_2^2\omega_6\omega_3^3 + 9cs^2\omega_6\omega_3^3 - 36cs^2\omega_6\omega_3^3 - 60v_2^2\omega_6\omega_3^2 + 12\omega_6^2\omega_3 - 11\omega_6^2\omega_3^2 + 48v_2^2\omega_6\omega_3 + 24cs^2\omega_6\omega_3 + \omega_6^2\omega_3^3 - 6v_2^2\omega_3^3 - 6cs^2\omega_6\omega_3^3 + 12v_2^2\omega_6^2 + 24cs^2\omega_6^2 + 36\omega_6\omega_3^2 + 12v_2^2\omega_6\omega_3^2 + 12v_2^2\omega_6\omega_3^3 + 27v_2^2\omega_6^2\omega_3^2 - 12\omega_3^2 - 24\omega_6\omega_3 - 3v_2^2\omega_6\omega_3^2 - 2cs^2\omega_6\omega_3^2 + 6\omega_3^3$$

$$\begin{aligned} C_{27} = & 6\omega_2^3\omega_3^2 - 3\omega_2^2\omega_6\omega_3^2 - 12v_2^2\omega_2^2\omega_6\omega_3^2 + 42cs^2\omega_2^2\omega_6\omega_3^2 - 3\omega_2^3\omega_3^3 + 12\omega_2^3\omega_6\omega_3 + 6v_2^2\omega_2^2\omega_6\omega_3^2 - 12cs^2\omega_2^2\omega_6\omega_3^2 - 24cs^2\omega_2^2\omega_6\omega_3^2 + \\ & 24v_2^2\omega_6\omega_3^2 + \omega_2^2\omega_6\omega_3^3 - 21v_2^2\omega_6\omega_3^2 + 42v_2^2\omega_2^3\omega_6\omega_3^2 + 42cs^2\omega_2^3\omega_6\omega_3^2 - 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - 24cs^2\omega_2^2\omega_6\omega_3^2 + 6\omega_2^3\omega_6\omega_3^2 + \\ & 12v_2^2\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2^3\omega_6\omega_3^2 - 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - 3\omega_2^3\omega_6\omega_3^2 + 7\omega_2^3\omega_6\omega_3^2 - 36cs^2\omega_2^3\omega_6\omega_3^2 - 48cs^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2^3\omega_6\omega_3^2 + \\ & 6v_2^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2^3\omega_6\omega_3^2 - 6\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - 30v_2^2\omega_2^3\omega_6\omega_3^2 - 3\omega_2^3\omega_6\omega_3^2 + 78cs^2\omega_2^3\omega_6\omega_3^2 + \\ & 6v_2^2\omega_6\omega_3^2 + 6\omega_2^2\omega_6\omega_3^2 - 12v_2^2\omega_2\omega_6\omega_3^2 + 6cs^2\omega_2\omega_6\omega_3^2 - 12cs^2\omega_2^2\omega_6\omega_3^2 - 12v_2^2\omega_2^2\omega_6\omega_3^2 \end{aligned}$$

$$C_{28} = -12v_2^2\omega_6\omega_3^3 - 12cs^2\omega_6\omega_3^3 + 48cs^2\omega_6\omega_3^3 + 48v_2^2\omega_6\omega_3^2 - 12\omega_6^2\omega_3 + 11\omega_6^2\omega_3^2 - 36v_2^2\omega_6\omega_3 - 36cs^2\omega_6\omega_3 - \omega_6^2\omega_3^3 + 9\omega_6\omega_3^3 + 6v_2^2\omega_3^3 + 6cs^2\omega_3^3 + \\ 12v_2^2\omega_6^2 - 48cs^2\omega_6^2 - 36\omega_6\omega_3^2 - 12cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6\omega_3^2 - 44cs^2\omega_6\omega_3^2 - 8v_2^2\omega_6\omega_3^2 + 12\omega_3^2 + 24\omega_6\omega_3 + v_2^2\omega_6\omega_3^3 + 4cs^2\omega_6\omega_3^3 - 6\omega_3^3$$

$$C_{29} = -6\omega_2^2\omega_6\omega_3^3 + 12v_2^2\omega_2^2\omega_6\omega_3^3 + 48cs^2\omega_2^2\omega_6\omega_3^3 - 12cs^2\omega_2^2\omega_6\omega_3^3 - 12cs^2\omega_2^3\omega_6\omega_3^3 - 24cs^2\omega_2^2\omega_6\omega_3^2 + 3w_2^3\omega_6\omega_3^3 + 4cs^2\omega_2^3\omega_6\omega_3^2 + 3v_2^2\omega_2^3\omega_6\omega_3^2 - 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - \\ w_2^3\omega_6\omega_3^3 + 3w_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - 32cs^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6\omega_3^2 + 12cs^2\omega_2^2\omega_6\omega_3^2 + 12v_2^2\omega_2^2\omega_6\omega_3^2 - 12cs^2\omega_2^2\omega_6\omega_3^2 - \\ 30v_2^2\omega_2^3\omega_6\omega_3^2 - 6w_2^2\omega_6\omega_3^2 + 36cs^2\omega_2^3\omega_6\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 + 12\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2\omega_6\omega_3^2 - 24v_2^2\omega_2^2\omega_6\omega_3^2 - 24v_2^2\omega_2^3\omega_6\omega_3^2$$

$$C_{30} = 18v_2^2\omega_6\omega_3^3 - 6cs^2\omega_6\omega_3^3 - 12cs^2\omega_2^2\omega_6\omega_3^3 - 24v_2^4\omega_3^2 - 96cs^2\omega_2^2\omega_6\omega_3^2 + 24cs^4\omega_6\omega_3^2 + 12v_2^2\omega_2^2\omega_6\omega_3^2 + 12cs^2\omega_2^3\omega_6\omega_3^2 - 6\omega_2^3\omega_6\omega_3^2 + 36v_2^2\omega_2^3\omega_6\omega_3^2 + \\ 72v_2^2\omega_6\omega_3^2 - 24cs^2\omega_2^2\omega_3^2 + 24cs^4\omega_6\omega_3^2 + 12v_2^4\omega_3^2 + 6cs^2\omega_6\omega_3^2 - 18v_2^4\omega_6\omega_3^2 - 24cs^2\omega_2^2\omega_6\omega_3^2 + 48v_2^2\omega_2\omega_6\omega_3^2 - 24cs^2\omega_2^3\omega_6\omega_3^2 + 72v_2^2\omega_2\omega_6\omega_3^2 - 24cs^4\omega_6\omega_3^2 - \\ 24v_2^4\omega_2\omega_3^2 + 24cs^4\omega_6\omega_3^2 - 12v_2^2\omega_3^2 + 3cs^4\omega_6\omega_3^2 + 3v_2^2\omega_2\omega_3^2 + 24v_2^2\omega_2^2\omega_3^2 + 156cs^2\omega_2^2\omega_6\omega_3^2 - 24v_2^2\omega_2^2\omega_6\omega_3^2 - 12cs^2\omega_2^2\omega_6\omega_3^2 - 72cs^2\omega_2^2\omega_6\omega_3^2 - \\ 8cs^2\omega_6\omega_3^2 + 24v_2^2\omega_6\omega_3^2 - 3v_2^2\omega_6\omega_3^2 + cs^2\omega_6\omega_3^2 + 6cs^2\omega_2^2\omega_6\omega_3^2 - 48cs^4\omega_6\omega_3^2 + 24v_2^4\omega_6\omega_3^2$$

$$C_{31} = -6v_2^2\omega_6\omega_3^3 - 6cs^2\omega_6\omega_3^3 + 24cs^2\omega_6\omega_3^3 + 24v_2^2\omega_6\omega_3^2 - 6\omega_6^2\omega_3 + 8\omega_6^2\omega_3^2 - 12v_2^2\omega_6\omega_3 - 12cs^2\omega_6\omega_3 - \omega_6^2\omega_3^3 + 6\omega_6\omega_3^3 + 6v_2^2\omega_3^3 + 6cs^2\omega_6\omega_3^3 - 12v_2^2\omega_6\omega_3^2 - \\ 24cs^2\omega_6\omega_3^2 - 24\omega_6\omega_3^2 - 12cs^2\omega_3^2 - 12v_2^2\omega_3^2 + 24v_2^2\omega_6\omega_3 + 42cs^2\omega_6\omega_3^2 - 20cs^2\omega_6\omega_3^2 - 16v_2^2\omega_6\omega_3^2 + 12\omega_3^2 + 12\omega_6\omega_3 + 2v_2^2\omega_6\omega_3^3 + cs^2\omega_6\omega_3^3 - 6\omega_3^3$$



$$\begin{aligned}
C_{47} = & -5w_3^4v_2^2w_6^2w_3 + 4w_3^4c_2s^2w_6^2w_3 - 24w_4^2c_2s^2w_6^2w_3 + 48w_4^2v_2^2w_6^2w_3 - 32w_4^3c_2s^2w_6^2w_3 + 40w_4^3v_2^2w_6^2w_3 - 90w_4^3v_2^2w_6^2w_3 + 36w_4^3c_2s^2w_6^2w_3 - \\
& 12w_4^3c_2s^2w_3^2 - 12w_4^3v_2^2w_3^2 - 60w_4^2v_2^2w_6^2w_3^2 + 48w_4^2c_2s^2w_6^2w_3^2 + 48w_4^3v_2^2w_6^2w_3^2 - 12w_4^3c_2s^2w_6^2w_3^2 + 6w_4^3v_2^2w_3^3 + 6w_4^3c_2s^2w_3^3 - 12w_4^2c_2s^2w_6^2w_3^3 + 24w_4^2v_2^2w_6^2w_3^3 + \\
& 12w_4^2c_2s^2w_6w_3^3 + 12w_4^2v_2^2w_6w_3^3 - 12w_4^3c_2s^2w_6w_3 - 12w_4^3c_2s^2w_6w_3^2 - 24w_4^2v_2^2w_6w_3^2 - 24w_4^2c_2s^2w_6w_3^2 - 12w_4c_2s^2w_6^2w_3^2 + 24w_4v_2^2w_6^2w_3^2 + \\
& 36w_4^3c_2s^2w_6w_3^3 + 36w_4^2v_2^2w_6w_3^3 + 12v_2^2w_6^2w_3^3 - 30w_4v_2^2w_6^2w_3^3 + 6w_4c_2s^2w_6^2w_3^3 - 12w_4^3v_2^2w_6w_3^3 - 12w_4^3c_2s^2w_6w_3^3
\end{aligned}$$

$$\begin{aligned} C_{48} = & 12w_4^3w_2^3 + 12w_4^2w_2^2w_3 + 12w_3^2w_3^3 - 42w_4^2w_2^2w_3^3 + 18w_4^2w_2^3w_3 + 6w_4^3w_2w_3^2 - 30w_4^2w_3^3w_3^2 + 24w_4^2w_3^2w_3^3 - 30w_4^3w_2w_3^3 + 6w_4w_3^3w_2^3 - \\ & 36w_4^3w_2^3w_3 + 24w_4^3w_2^2w_3^3 - 30w_4^3w_2^2w_3^2 + 12w_4^3w_3^3 - 30w_4w_2^3w_3^3 + 18w_4^3w_2^2w_3^3 - 5w_4^3w_3^2w_3^3 + 18w_4^2w_2w_3^3 + 18w_4w_2^2w_3^3 + 28w_4^3w_3^2w_2^3 \end{aligned}$$

$$\begin{aligned} C_{49} = & -60v_2^2w_2^2w_6^2w_3^2 + 48cs^2w_2^2w_6^2w_3^2 + 24v_2^2w_2^2w_6^2w_3^2 - 12cs^2w_2^2w_6^2w_3^2 - 12cs^2w_2^3w_6w_3 - 12v_2^2w_2^3w_6w_3 + 36v_2^2w_2^3w_6w_3^2 + 36cs^2w_2^3w_6w_3^2 - \\ & 12v_2^2w_2^3w_6w_3^2 - 12cs^2w_2^3w_6w_3^2 - 24cs^2w_2^2w_6^2w_3 + 48v_2^2w_2^2w_6^2w_3 + 4cs^2w_3^2w_2^2w_3^2 - 5v_2^2w_3^2w_2^2w_3^2 - 12v_2^2w_3^2w_2^2w_3^2 - 12cs^2w_3^2w_2^2w_3^2 - \\ & 32cs^2w_3^2w_2^2w_3^2 + 48v_2^2w_3^2w_2^2 + 6cs^2w_3^2w_3^3 + 6v_2^2w_3^2w_3^3 + 40v_2^2w_3^2w_6^2w_3^2 + 12cs^2w_2^2w_6w_3^2 + 12v_2^2w_2^2w_6w_3^2 + 24v_2^2w_2^2w_6w_3^2 - 12cs^2w_2^2w_6w_3^2 - \\ & 90v_2^2w_2^3w_6w_3 + 36cs^2w_2^3w_6w_3 + 12v_2^2w_6^2w_3^2 - 30v_2^2w_2w_6^2w_3^2 + 6cs^2w_2w_6^2w_3^2 - 24cs^2w_2^2w_6w_3^2 - 24v_2^2w_2^2w_6w_3^2 \end{aligned}$$

$$\begin{aligned} C_{50} = & -3\omega_4^2 w_6^2 w_3^2 + 6\omega_3^3 c s^2 w_6^2 w_3^3 + 12\omega_4^3 w_6 w_3 - 24\omega_4^2 c s^2 w_6^2 w_3 + \omega_4^2 w_6^2 w_3^3 + 12\omega_4^2 v_2^2 w_6^2 w_3 - 48\omega_4^3 c s^2 w_6^2 w_3^2 + 6\omega_4^3 v_2^2 w_6^2 w_3^2 - 30\omega_3^3 v_2^2 w_6^2 w_3 + \\ & 78\omega_4^3 c s^2 w_6^2 w_3 - 12w_3^3 c s^2 w_3^2 - 12\omega_4^3 v_2^2 w_3^2 - 21\omega_4^3 w_6 w_3^2 - 12\omega_4^2 v_2^2 w_6^2 w_3^2 + 42\omega_4^2 c s^2 w_6^2 w_3^2 + 24\omega_4^3 v_2^2 w_6^2 - 36\omega_4^3 c s^2 w_6^2 + 6\omega_3^3 v_2^2 w_3^3 + 6\omega_4^3 c s^2 w_3^3 - \\ & 12\omega_4^2 c s^2 w_6^2 w_3^3 + 6\omega_4^2 v_2^2 w_6^2 w_3^3 + 6\omega_4^3 w_6 w_3^3 + 6\omega_3^3 w_3^2 + 6\omega_4^2 c s^2 w_6 w_3^3 + 6\omega_4^2 v_2^2 w_6 w_3^3 - \omega_4^3 w_6^2 w_3^3 - 3\omega_4^3 w_3^3 - 24\omega_4^3 v_2^2 w_6 w_3 - 24\omega_4^3 c s^2 w_6 w_3 + \\ & 7\omega_3^3 w_2^2 w_3^2 - 12\omega_4^2 v_2^2 w_6 w_3^2 - 12\omega_4^2 c s^2 w_6 w_3^2 - 6\omega_4^3 w_2^2 w_3 - 12w_4 c s^2 w_2^2 w_3^2 + 6w_4 v_2^2 w_6 w_3^2 - 3\omega_4^2 w_6 w_3^2 + 42\omega_4^3 c s^2 w_6 w_3^2 + 42\omega_4^3 v_2^2 w_6 w_3^2 + 6w_4^2 w_6 w_3^2 + \\ & 6v_2^2 w_6^2 w_3^3 - 12w_4 v_2^2 w_6^2 w_3^3 + 6w_4 c s^2 w_6^2 w_3^3 - 12\omega_4^3 v_2^2 w_6 w_3^3 - 12\omega_4^3 c s^2 w_6 w_3^3 \end{aligned}$$

$$\begin{aligned} C_{51} = & -6w_4^2 w_6^2 w_3^2 + 3w_3^3 v_2^2 w_6^2 w_3^3 + 4w_4^3 c s^2 w_6^2 w_3^3 - 24w_4^2 c s^2 w_6^2 w_3 + 2w_4^2 w_6^2 w_3^3 - 32w_4^3 c s^2 w_6^2 w_3^3 - 30w_4^3 v_2^2 w_6^2 w_3 + 36w_3^3 c s^2 w_6^2 w_3^3 - 12w_4^3 c s^2 w_6^2 w_3^2 - 12w_3^3 v_2^2 w_6^2 w_3^2 - 6w_3^3 w_6^2 w_3^2 + 12w_4^2 v_2^2 w_6^2 w_3^2 + 48w_4^2 c s^2 w_6^2 w_3^2 + 24w_4^3 v_2^2 w_6^2 - 12w_4^3 c s^2 w_6^2 + 6w_4^3 v_2^2 w_6^3 + 6w_3^4 c s^2 w_6^3 - 12w_4^2 c s^2 w_6^2 w_3^3 + 3w_4^3 w_6 w_3^3 + 12w_4^2 c s^2 w_6 w_3^3 + 12w_4^2 v_2^2 w_6 w_3^3 - w_3^4 w_6^2 w_3^3 - 12w_4^3 v_2^2 w_6 w_3 - 12w_4^3 c s^2 w_6 w_3 + 3w_4^3 w_6^2 w_3^2 - 24w_4^2 v_2^2 w_6 w_3^2 - 24w_4^2 c s^2 w_6 w_3^2 - 12w_4 c s^2 w_6^2 w_3^2 - 6w_4^2 w_6 w_3^3 + 36w_3^4 c s^2 w_6 w_3^2 + 36w_3^4 v_2^2 w_6 w_3^3 + 12w_4^2 w_6 w_3^2 + 12v_2^2 w_6^2 w_3^3 - 18w_4 v_2^2 w_6^2 w_3^3 + 6w_4 c s^2 w_6^2 w_3^3 - 12w_4^3 v_2^2 w_6 w_3^3 - 12w_4^3 c s^2 w_6 w_3^2 \end{aligned}$$

$$\textcolor{red}{C_{52}} = -12v_2^2w_6\omega_3^3 - 12cs^2w_6\omega_3^3 + 48cs^2w_6\omega_3^2 + 48v_2^2w_6\omega_3^2 - 12\omega_6^2\omega_3 + 11\omega_6^2\omega_3^2 - 36v_2^2w_6\omega_3 - 36cs^2w_6\omega_3 - \omega_6^2\omega_3^3 + 9w_6\omega_3^3 + 6v_2^2\omega_3^3 + 6cs^2\omega_3^3 + 12v_2^2\omega_6^2 - 48cs^2\omega_6^2 - 36w_6\omega_3^2 - 12cs^2\omega_3^2 - 12v_2^2w_3^2 + 90cs^2w_6^2\omega_3 - 44cs^2w_6^2\omega_3^2 - 8v_2^2w_6^2\omega_3^2 + 12w_3^2 + 24w_6\omega_3 + v_2^2w_6^2\omega_3^3 + 4cs^2w_6^2\omega_3^3 - 6\omega_3^3$$

$$\begin{aligned} C_{53} = & 12w_7^2w_4c_8s^2 + 12w_4^2v_3^2w_2 + 36w_2^2w_4v_3^2w_2 - w_7^2w_4^3v_3^2 + 12w_2^4c_8s^2w_2 + 12w_7w_4^2c_8s^2 - 30w_7w_4^2v_3^2w_2 - 30w_7w_4^2v_3^2w_2 - 2w_7^2w_4^3c_8s^2w_2 + \\ & w_7^2w_4^3v_3^2w_2 - 6w_7w_4^3c_8s^2 - 30w_7w_4^2c_8s^2w_2 + 6w_7^2w_4^2v_3^2 + 12w_2^2c_8s^2w_2 + 12w_7w_4v_3^2w_2 - 6w_4^3c_8s^2w_2 - 12w_7w_4v_3^2 - 6w_4^3v_3^2w_2 + 12w_7w_4^2v_3^2 + \\ & 12w_7w_4c_8s^2w_2 + 3w_7^2w_4^3c_8s^2 - 24w_7^2v_3^2w_2 + 9w_7w_4^3c_8s^2w_2 - 10w_7^2w_4^2v_3^2w_2 - 18w_7^2w_4^2c_8s^2 - 22w_7w_4^2c_8s^2w_2 - 6w_7w_4^3v_3^2 + 9w_7w_4^3v_3^2w_2 \end{aligned}$$

$$C_{54} = -7\omega_7\omega_4^3\omega_2^2 + 3\omega_4^3\omega_3^2 - 6\omega_7\omega_4^3 - 6\omega_7\omega_4^2\omega_2 - 6\omega_4^3\omega_2^2 + \omega_7\omega_4^3\omega_2^3 + 12\omega_7\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2^3 - 12\omega_7\omega_4^3 + 12\omega_4^2\omega_2^2 + 12\omega_7\omega_4^3\omega_2 - 10\omega_7\omega_4^2\omega_3^2 + 24\omega_7\omega_4\omega_2^3 - 12\omega_7\omega_4\omega_2^2$$

$$\begin{aligned}
C_{55} = & -4w_7w_4c^8s^2w_5^2w_3^2v_1^2 + 20w_7^2w_4^2w_5^2v_3^2w_2v_1^2 - 3w_7w_4w_5^2v_3^2w_2^2v_1^2 - 4w_7w_4^2c^8s^2w_5v_3^2w_2^2 + 4w_7^2w_4^2c^8s^4w_5w_2^2 + 12w_7^2w_4^2c^8s^2w_5^2w_2^2v_1^2 - \\
& 8w_7w_3^3c^8s^2w_5^2v_3^2w_2^2 - 2w_7^2w_4^3c^8s^2w_5w_2^2v_1^2 + 2w_7^2w_3^3v_3^2w_2^2v_1^2 - 4w_7^2w_4^3c^8s^2w_5v_3^2 + 2w_7w_2^2w_5^2v_3^2w_2^3v_1^2 - 2w_7^2w_4^2c^8s^4w_5w_3^2 + 2w_7^2w_4^2c^8s^2w_5v_3^2w_3^2 + \\
& 4w_7^2w_3^3c^8s^2w_5^2w_2v_1^2 + 10w_7w_4^2c^8s^2w_5^2w_3^2v_1^2 + w_7^2w_4^3c^8s^2w_5^2v_3^2w_3^2 + 20w_7^2w_3^4w_5^2v_3^2w_2^2v_1^2 - 4w_7^2w_4c^8s^2w_5^2w_2^2v_1^2 + 20w_7^2w_5^2v_3^2w_2^3v_1^2 + w_7^2w_4^3c^8s^2w_5w_3^2v_1^2 - \\
& 4w_7^2w_4^2w_5v_2^2w_2v_1^2 + w_7^2w_3^3c^8s^4w_5w_3^2 - 2w_7^2w_4c^8s^4w_5^2w_3^2 - 8w_7^2w_4c^8s^2w_5^2w_3^2v_1^2 + 2w_7^2w_4^2c^8s^2w_5^2v_3^2w_2^2v_1^2 + 2w_7w_4^2w_5^2v_3^2w_2^3v_1^2 + w_7w_4^3c^8s^2w_5^2v_3^2w_3^2 + \\
& 10w_7w_4c^8s^2w_5^2w_2^3v_1^2 + 10w_7^2w_3^2c^8s^2w_5^2w_3^2 - 3w_7w_4w_5^2v_3^2w_2^3v_1^2 - 4w_7c^8s^2w_5^2w_3^2v_1^2 - 4w_7w_4c^8s^2w_5^2w_2^2v_1^2 - 2w_7^2w_4^2c^8s^4w_5w_2^2 - 2w_7w_3^3c^8s^2w_5^2v_3^2w_2^2 + \\
& 4w_7w_4c^8s^4w_5^2w_2^2 - 4w_7^2w_3^2v_3^2w_2^2v_1^2 - 4w_7w_4^2w_5^2v_3^2w_2^2v_1^2 - 4w_7w_4^2w_5^2v_3^2w_2^3v_1^2 - 2w_7w_4^2c^8s^2w_5^2v_3^2w_3^2 + w_7^2w_4^3c^8s^2w_5^2w_3^2v_1^2 + \\
& 4w_7^2w_3^4c^8s^2w_5^2w_3^2 - 38w_7^2w_4w_5^2v_3^2w_2^3v_1^2 + w_7^2w_4^3c^8s^4w_5^2w_3^2 + 4w_7^2w_4^2c^8s^4w_5^2w_2^2 - 7w_7^2w_4^2c_5^8s^2w_5^2w_3^2v_1^2 - w_7^2w_4^3c^8s^4w_5^2w_2^3 + 10w_7^2w_3^4w_5^2v_3^2w_2^2v_1^2 + \\
& 20w_7^2w_5^2v_3^2w_2^3v_1^2 + 4w_7w_4^2w_5^2v_3^2w_2^3v_1^2 - 4w_7^2w_3^2c^8s^2w_5^2v_3^2w_2^2 + 2w_7w_4^2c^8s^2w_5^2w_2^2v_1^2 + 2w_7^2w_4^2c^8s^2w_5^2w_3^2v_1^2 - 4w_7^2w_4^2c^8s^2w_5^2v_3^2w_2^2 + 20w_7^2w_4^2w_5^2v_2^2w_3^2v_1^2 - \\
& 2w_7w_3^3c^8s^2w_5^2w_2^2 + 4w_7^2w_4^2c^8s^2w_5w_2^2v_1^2 - 4w_7w_4^2c^8s^2v_3^2w_2^2 + 4w_7^2w_4^2c^8s^4w_5w_3^2 + 12w_7w_4^2c^8s^2w_5^2v_3^2w_2^2 + 4w_7^2w_4c^8s^2w_5^2v_3^2w_3^2 + 4w_7w_4^2c^8s^4w_5^2w_2^2 - \\
& 4w_7^2c^8s^2w_5^2w_3^2v_1^2 + 20w_7^2w_4w_5^2v_3^2w_2^2v_1^2 - 4w_7w_3^2c^8s^2w_5^2w_2^2v_1^2 + 10w_7w_3^2c^8s^2w_5v_3^2w_2^2 + 10w_7w_3^2w_5^2v_3^2w_2^3v_1^2 - 38w_7w_3^2w_5^2v_3^2w_2^2v_1^2 - 12w_7^2w_4^2c^8s^4w_5^2w_2^2 - \\
& 4w_7^2w_4^2c^8s^2w_5^2v_3^2w_3^2 - 36w_7w_4w_5^2v_3^2w_2^2v_1^2 + 2w_7^2w_3^2c^8s^2v_3^2w_2^3 - 3w_7w_4^2c^8s^2w_5^2w_2^3v_1^2 - 8w_7w_4^2c^8s^2w_5^2w_2v_1^2 - 4w_7w_4w_5^2v_3^2w_2^3v_1^2 - 3w_7w_4^2c^8s^2w_5v_3^2w_3^2 - \\
& 8w_7w_4c^8s^2w_5^2v_3^2w_2^2 - 3w_7^2w_4^3w_5^2v_3^2w_2^3v_1^2 - 2w_7w_4^3c^8s^4w_5^2w_2 - 2w_7w_4^2c^8s^4w_5^2w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{56} = & w_7^2 w_3^3 c s^2 w_3^3 + 24 w_7 w_4^2 v_3^2 w_3^3 + 22 w_7 w_3^3 v_3^2 w_2^2 + 24 w_7 w_4^2 c s^2 w_3^2 + 12 w_7 w_3^3 v_3^2 - 6 w_7^2 w_4^3 c s^2 w_2^2 - 4 w_7^2 w_4^3 v_3^2 w_3^2 - 78 w_7^2 w_4 v_3^2 w_3^2 - 12 w_4^2 v_3^2 w_3^2 + \\
& 6 w_7 w_3^3 c s^2 w_2^2 + 24 w_7 w_4 v_3^2 w_2^2 - 30 w_7 w_3^4 v_3^2 w_2 + 24 w_7^2 w_4 c s^2 w_3^2 - 12 w_4^2 c s^2 w_3^2 + 34 w_7^2 w_4^2 v_3^2 w_3^2 + 12 w_7^2 w_4^2 c s^2 w_2^2 - 6 w_7 w_4^3 c s^2 w_3^2 - 48 w_7^2 w_4^2 v_3^2 w_2^2 - \\
& 6 w_7 w_4^2 v_3^2 w_2^2 - 14 w_7^2 w_4^2 c s^2 w_3^2 + 6 w_3^4 c s^2 w_3^2 - 12 w_7 w_4 v_3^2 w_3^2 + 24 w_7^2 w_4^2 v_3^2 w_2 - 12 w_7^2 c s^2 w_3^2 - 12 w_7^2 w_4^2 c s^2 w_2 + 48 w_7^2 v_3^2 w_3^2 - 12 w_7 w_4 c s^2 w_3^2 + 6 w_4^3 v_3^2 w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{57} = & -12w_4^3cs^2w_5^2 - 78w_4^3w_5^2w_2v_1^2 - 12w_4^3w_2^2v_1^2 + 24w_4w_2^2w_2^2v_1^2 - 6w_4^2cs^2w_5^2w_3^2 + 24w_4^3cs^2w_5^2w_2 + 24w_4^3w_5w_2^2v_1^2 + 12w_2^2cs^2w_5^2w_2^2 + 12w_5^2w_3^2v_1^2 + \\
& 6w_3^2w_3^2v_1^2 - 30w_4w_5^2w_3^2v_1^2 - 14w_4^3cs^2w_5^2w_2^2 + 24w_4^2w_5^2w_2v_1^2 - 6w_4^3w_5w_3^2v_1^2 + w_3^4cs^2w_5^2w_3^2 - 48w_4^2w_5^2w_2^2v_1^2 + 6w_4cs^2w_5^2w_3^2 - 6w_4^3cs^2w_5w_3^2 - \\
& 12w_4cs^2w_5^2w_2^2 + 24w_4^3cs^2w_5w_2^2 - 4w_3^4w_5^2w_3^2v_1^2 - 12w_4^3cs^2w_5w_2 + 6w_4^3cs^2w_3^2 + 48w_3^2w_5^2v_1^2 - 12w_4^3w_5w_2v_1^2 + 22w_4^2w_5^2w_3^2v_1^2 + 34w_4^3w_5^2w_2^2v_1^2 - 12w_4^3cs^2w_2^2
\end{aligned}$$

$$\begin{aligned} C_{58} = & -6w_3^4v_3^2w_3 + 12w_7^2w_4cs^2 + 12w_7w_4cs^2w_3 - 24w_7^2v_3^2w_3 + 12w_7^2cs^2w_3 - w_7^2w_3^3v_3^2 + 12w_7w_4v_3^2w_3 + 12w_7w_4^2cs^2 - 6w_3^4cs^2w_3 + \\ & 22w_2^2w_4^2cs^2w_3 + 9w_7w_4^2v_3^2w_3 + 9w_7w_4^2cs^2w_3 - 6w_7w_4^2cs^2 + 6w_2^2w_4^2v_3^2 - 10w_7w_4^2v_3^2w_3 - 30w_7w_4cs^2w_3 + 12w_2^4cs^2w_3 - 12w_7w_4v_3^2 + 12w_7w_4^2v_3^2 + \\ & 36w_7w_4v_3^2w_3 + 12w_2^4v_3^2w_3 + 3w_7^2w_3^3cs^2 + w_7^2w_3^3v_3^2w_3 - 30w_7w_4^2cs^2w_3 - 18w_7w_4^2cs^2 - 30w_7w_4v_3^2w_3 - 6w_7w_4^2v_3^2 - 2w_7^2w_3^4cs^2w_3 \end{aligned}$$

$$C_{59} = -12\omega_7\omega_4\omega_3^2 - 6\omega_7\omega_3^4 + 24\omega_7\omega_4\omega_3^3 + \omega_7\omega_4^3\omega_3^3 - 6\omega_4^3\omega_3^2 - 6\omega_7\omega_4^2\omega_3 + 3\omega_4^3\omega_3^3 - 7\omega_7\omega_4^3\omega_3^2 - 12\omega_7\omega_3^3 - 10\omega_7\omega_4^2\omega_3^3 + 12\omega_7\omega_4^3\omega_3 + 12\omega_4^2\omega_3^2 - 6\omega_4^2\omega_3^3 + 12\omega_7\omega_4^2\omega_3^2$$

$$\begin{aligned} C_{60} = & -8w_2^3 w_3^3 w_2^3 w_3^3 - 2w_2 w_4 c_2 s_2^2 w_3^3 + 7w_2^2 w_4^2 s_2^2 w_3^3 + 10w_2^2 w_3^2 w_3^3 - 2w_2^2 w_4 c_2 s_2^2 w_3^3 - 2w_2^2 w_4^2 c_2 s_2^2 w_3^3 + w_3^2 w_4^2 s_2^2 w_3^3 + 3w_2^2 w_3^4 c_2^2 w_3 \\ & - 3w_2^2 s_2^2 c_2^2 w_3^3 - 2w_2^2 s_2^2 c_2^2 w_3^3 + w_2^2 s_2^2 c_2^2 w_3^3 - 2w_2^2 s_2^2 c_2^2 w_3^3 + w_2^2 s_2^2 c_2^2 w_3^3 + w_2^2 s_2^2 c_2^2 w_3^3 - 2w_2^2 s_2^2 c_2^2 w_3^3 + w_2^2 s_2^2 c_2^2 w_3^3 \end{aligned}$$

$$7\omega_7^2\omega_4v_3^2\omega_2^3\omega_3^2 + 4\omega_7^2\omega_4^2v_3^2\omega_2\omega_3^3 + \omega_7^2\omega_4^3cs^2\omega_2\omega_3^3 - 2\omega_7\omega_4v_3^2\omega_2^3\omega_3^3 - 12\omega_7^2\omega_4^2v_3^2\omega_2^2\omega_3^3 - 2\omega_7\omega_4^3v_3^2\omega_2^3\omega_3^3 + 6\omega_7^2\omega_4^2cs^2\omega_2^3\omega_3^2 + 4\omega_7^2\omega_4^2v_3^2\omega_2^3\omega_3 +$$

$$6w_7w_4^2cs^2w_3^3w_3 + 7w_7w_3^2v_3^2w_2w_2^2 + w_7^2w_3^4cs^2w_3^2w_3 + 3w_7w_3^4v_3^2w_3^3 - 2w_7^2w_4^4cs^2w_2^2w_3^3 - 6w_7^2w_4^2cs^2w_3^2w_3 + w_7w_3^4v_3^2w_3^2w_3^2 + 4w_7w_4^2v_3^2w_2w_2^2 - 2w_7w_4^2v_3^2w_2^2w_3^3 + 3w_7^2w_3^4v_3^2w_2^2w_3 + w_7w_3^4cs^2w_2^2w_3^2 - 2w_7w_4^2v_3^2w_2^2w_3^3 - 2w_7w_4^2cs^2w_3^3w_2^2 - 8w_7w_3^2v_3^2w_2^2w_3^2 - 2w_7w_4^2cs^2w_2^2w_3^3 - 2w_7w_4^2v_3^2w_2^2w_3^2w_3 + w_7w_3^4v_3^2w_2^2w_3^3 + 12w_7^2w_4^2v_3^2w_2^2w_3^3 - 2w_7^2w_4^2cs^2w_2^2w_3^2 + w_7w_3^4v_3^2w_2^2w_3^3 - 8w_7w_4^2v_3^2w_2^2w_3^2 - 2w_7w_4^2cs^2w_2^2w_3^2 + 6w_7w_4^2v_3^2w_2^2w_3^3 + 7w_7w_3^2v_3^2w_2^2w_3^3 + 6w_7^2w_4^2cs^2w_2^2w_3^3 - 2w_7^2w_4^2cs^2w_2^2w_3^2 - 12w_7w_4^2v_3^2w_2^2w_3^2 - 2w_7w_4^2cs^2w_2^2w_3^3$$

$$\begin{aligned} C_{61} = & -12\omega_7^3\omega_4^3\omega_3^3 - 60\omega_7^2\omega_4^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^2 + 12\omega_7\omega_4^3v_3^2\omega_3^2 + 40\omega_7^2\omega_4^2v_3^2\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^2 + \\ & 48\omega_7^2\omega_4^2cs^2\omega_3^2 + 48\omega_7^2\omega_4^3v_3^2\omega_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3^2 - 12\omega_7\omega_4cs^2\omega_3^2 + 6\omega_7^3\omega_4^3\omega_3^3 + 6\omega_7^3cs^2\omega_3^2 - 12\omega_7\omega_4v_3^2\omega_3^2 - 12\omega_7^2cs^2\omega_3^2 + 24\omega_7^2\omega_4^2v_3^2\omega_3^2 - \\ & 12\omega_7^2\omega_4^3cs^2\omega_3^2 + 36\omega_7\omega_4^2cs^2\omega_3^2 - 5\omega_7^2\omega_4^3\omega_3^3\omega_3^3 - 24\omega_7\omega_4^2v_3^2\omega_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^2 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 24\omega_7^2\omega_4^3v_3^2\omega_3^2 + 36\omega_7\omega_4^2v_3^2\omega_3^2 + 48\omega_7^2\omega_4v_3^2\omega_3^2 - \\ & 30\omega_7^2\omega_4^3v_3^2\omega_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3^2 + 36\omega_7^2\omega_4cs^2\omega_3^2 - 12\omega_7^2\omega_4^3v_3^2\omega_3^2 - 90\omega_7^2\omega_4v_3^2\omega_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3^2 - 24\omega_7^2\omega_4cs^2\omega_3^2 \end{aligned}$$

$$\begin{aligned} C_{62} = & -24\omega_7 w_2^4 c s^2 w_2^2 + 4\omega_7^2 w_3^4 c s^2 w_2^3 + 36w_7 w_2^4 v_3^2 w_2^3 + 24w_7^2 w_3^4 v_3^2 w_2^2 + 36w_7 w_2^4 c s^2 w_2^3 + 12w_7^2 w_3^4 v_3^2 w_2^2 - 12w_7^2 w_3^4 c s^2 w_2^2 - 24w_7 w_2^4 v_3^2 w_2^2 - \\ & 5w_7^2 w_3^4 v_3^2 w_2^2 - 90w_7^2 w_4 v_3^2 w_2^3 - 12w_2^4 v_3^2 w_2^3 + 6w_7^2 w_3^4 c s^2 w_2 - 24w_7^2 w_4 c s^2 w_2^2 + 48w_7^2 w_4 v_3^2 w_2^2 - 30w_7^2 w_3^4 v_3^2 w_2 + 36w_7^2 w_4 c s^2 w_2^3 - 12w_4^2 c s^2 w_2^3 + \\ & 40w_7^2 w_4^2 v_3^2 w_2^3 + 12w_7 w_3^4 v_3^2 w_2^2 + 48w_7^2 w_4^2 c s^2 w_2^2 - 12w_7 w_3^4 c s^2 w_2^3 - 60w_7^2 w_4 v_3^2 w_2^2 - 12w_7 w_3^4 v_3^2 w_2^3 - 32w_7^2 w_4^2 c s^2 w_2^3 + 12w_7 w_3^4 c s^2 w_2^2 + 6w_3^4 c s^2 w_2^3 - \\ & 12w_7 w_4 v_3^2 w_2^3 + 24w_7^2 w_4^2 v_3^2 w_2 - 12w_7^2 c s^2 w_2^3 - 12w_7^2 w_4^2 c s^2 w_2 + 48w_7^2 v_3^2 w_2^3 - 12w_7 w_4 c s^2 w_2^3 + 6w_3^4 v_3^2 w_2^3 \end{aligned}$$

$$\begin{aligned} C_{63} = & 12w_4^3w_2^3 + 12w_2^4w_2^2w_3^2 + 12w_3^3w_2^3 - 30w_4^2w_2^2w_3 + 6w_4^2w_2^3w_3 + 18w_3^3w_2w_3^2 - 30w_4^2w_3^2w_3 + 28w_4^2w_3^2w_3^3 - 30w_4^3w_2w_3^3 + 18w_4w_2^3w_3^2 - \\ & 30w_3^3w_2^3w_3 + 24w_4^3w_2^2w_3^2 - 42w_4^3w_2^2w_3^2 + 12w_4^3w_3^3 - 36w_4w_2^3w_3^2 + 18w_4^3w_2^2w_3 - 5w_4^3w_2^3w_3 + 6w_4^2w_2w_3^3 + 18w_4w_2^3w_3^3 + 24w_4^3w_2^3w_3^2 \end{aligned}$$

$$\begin{aligned}
C_{64} = & 10w_7^2w_4^3v_2^2v_2^2w_6w_3^2 + 10w_7^2w_4^3cs^2v_3^2w_6^2w_3 - 4w_7^2w_3^3cs^2v_2^2w_6^2w_3^2 + 20w_7^2w_3^3v_3^2v_2^2w_6^2 - 2w_7^2w_3^3cs^4w_6w_3^2 + 2w_7^2w_4^3v_2^2v_2^2w_3^3 + \\
& 20w_7^2w_4^3v_2^3v_2^2w_6^2w_3^2 - 2w_7^2w_4^2cs^2v_2^2w_6w_3^3 + 2w_4^3cs^2v_2^2w_6^2w_3^3 - 2w_7w_4^3cs^2v_3^2w_2^2w_3^2 + 4w_7^2w_4cs^4w_6^2w_3^2 - 38w_7^2w_4v_2^2v_2^2w_6^2w_3^3 - 4w_7^2w_4^3v_2^2v_2^2w_3^2 + \\
& w_7^2w_4^3cs^4w_6w_3^3 + w_7^2w_4^3cs^2v_2^2w_6^2w_3^3 - 3w_7^2w_4v_3^2v_2^2w_6w_3^3 - 4w_4^2v_3^2v_2^2w_6^2w_3^3 - 2w_7^2w_4cs^4w_6^2w_3^3 + w_7w_4^3cs^2v_3^2w_2^2w_6^2w_3^3 + 4w_7^2w_4^2cs^2v_2^2w_6w_3^2 - \\
& 36w_7^2w_4^2v_2^2v_2^2w_6^2w_3^2 + 2w_7^2w_4^3cs^2v_3^2w_3^3 - 4w_7w_4^3cs^2v_2^2w_6^2w_3^2 - 4w_7w_4v_3^2v_2^2w_6^2w_3^3 - 3w_7w_4^3cs^2v_2^2w_2^2w_3^3 - 2w_7^2w_4^2cs^4w_6w_3^3 - 4w_7^2w_4^3cs^2v_3^2w_6w_3^2 + \\
& 20w_7^2w_4^3v_3^2v_2^2w_6^2w_3^3 - 4w_7w_4^3v_2^2v_2^2w_6^2w_3^2 + w_7^2w_4^3cs^2v_2^2w_6^2w_3^3 + 2w_7w_4^3cs^2v_3^2w_6w_3^2 + 2w_7w_4^2cs^2v_2^2w_6^2w_3^2 + 4w_7^2w_4^2cs^4w_6w_3^2 - 4w_7^2w_4^3cs^2v_3^2w_6^2w_3^2 + \\
& 4w_7^2w_4^3cs^2v_2^2w_6^2w_3^2 - 4w_7^2w_4v_3^2v_2^2w_6w_3^3 - 8w_7w_4^3cs^2v_3^2w_6^2w_3^2 - 4w_7w_4^3cs^2v_2^2w_6^2w_3^3 + 10w_7w_4^2v_3^2v_2^2w_6^2w_3^3 - 12w_7w_4^2cs^4w_6^2w_3^2 + \\
& 4w_7^2w_4^2cs^2v_2^2w_6^2w_3^2 + 10w_7w_4^2cs^2v_2^2w_6^2w_3^3 + 20w_7^2w_3^2v_2^2w_6^2w_3^2 - 38w_7^2w_4v_3^2v_2^2w_6^2w_3^3 + 10w_7^2w_4^3cs^2v_3^2w_6w_3^2 - 8w_7w_4cs^2v_3^2w_6^2w_3^2 - 2w_7w_4^3cs^4w_6^2w_3^2 - \\
& 2w_7^2w_4^3cs^4w_6^2w_3^3 - 4w_7w_4cs^2v_2^2w_6^2w_3^3 + 12w_7w_4^2cs^2v_3^2w_6^2w_3^2 - 8w_7^2w_4^2cs^2v_2^2w_6^2w_3^2 + 4w_7^2w_4^2cs^4w_6^2w_3^2 - 3w_7w_4^3v_3^2v_2^2w_6^2w_3^3 + 4w_7w_4^3cs^4w_6^2w_3^2 + \\
& 4w_7^2w_4cs^2v_2^2w_6^2w_3^2 - 3w_7w_4^3cs^2v_3^2w_6w_3^3 - 4w_7w_4^2cs^2v_2^2w_6^2w_3^2 - \bar{w}_7w_4^3cs^4w_6^2w_3^2 + 10w_7w_4^2cs^2v_2^2w_6^2w_3^3 - 4w_7w_4^2cs^2v_2^2w_6^2w_3^2 + \bar{w}_7w_4^3cs^2v_2^2w_6w_3^2 - \\
& 3w_7w_4^3v_3^2v_2^2w_6^2w_3^3 + 4w_7w_4^2cs^2v_3^2w_6^2w_3^2 + 12w_7w_4^2cs^2v_2^2w_6^2w_3^2 - 4w_7w_4^2cs^2v_2^2w_6^2w_3^2 - 4w_7^2w_4^2v_3^2v_2^2w_6^2w_3^3 - 2w_7w_4^3cs^4w_6^2w_3^2 - 2w_7w_4^2cs^2v_3^2w_6^2w_3^2 + \\
& 20w_7^2w_4^3v_3^2v_2^2w_6^2w_3^2 - 4w_7^2w_4^3cs^2v_3^2w_6w_3^3 - 2w_7w_4^3cs^2v_2^2w_6w_3^3 - 4w_7^2w_4cs^2v_2^2w_6^2w_3^2 + 4w_7^2w_4^3cs^4w_6^2w_3^2 + w_7w_4^3cs^4w_6^2w_3^2 + \\
& 2w_7^2w_4^3v_2^2w_6^2w_3^3 + 2w_7w_4^2v_3^2v_2^2w_6w_3^3 - 8w_7w_4^2cs^2v_2^2w_6^2w_3^3
\end{aligned}$$

$$\begin{aligned} C_{65} = & -6w_7w_4^3v_2^3w_3^3 - 48w_2^2w_4^2v_2^3w_3^2 - 14w_2^2w_4^2cs^2w_3^3 + 34w_7^2w_4^2v_2^3w_3^3 + 12w_7^2w_4^3v_2^3 - 6w_7w_4^3cs^2w_3^3 + 12w_7^2w_4^2cs^2w_3^2 + 48w_2^2v_2^3w_3^3 - 12w_7w_4^2cs^2w_3^3 + 6w_3^4v_2^3w_3^3 + 6w_3^4cs^2w_3^3 - 12w_7w_4v_2^3w_3^3 - 12w_7^2cs^2w_3^3 + 24w_7^2w_4^2v_2^3w_3 - 6w_7^2w_4^3cs^2w_3^2 + 24w_7w_4^2cs^2w_3^3 - 4w_7^2w_4^3v_2^3w_3 + w_7w_4^3cs^2w_3^3 + 22w_7^2w_4^3v_2^3w_3^2 + 24w_7w_4^2v_2^3w_3^3 + 24w_7^2w_4v_2^3w_3^2 - 30w_7^2w_4^3v_2^3w_3 - 12w_4^2cs^2w_3^3 + 24w_7^2w_4cs^2w_3^3 - 12w_4^2v_2^3w_3^3 - 78w_7^2w_4v_2^3w_3^3 + 6w_7^2w_4^3cs^2w_3 \end{aligned}$$

$$\begin{aligned} C_{66} = & -4w_3^3 v_2^2 w_6^2 w_3^3 + w_3^4 c s^2 w_6^2 w_3^3 + 24 w_4^2 v_2^2 w_6^2 w_3 - 14 w_4^3 c s^2 w_6^2 w_3^2 + 34 w_3^3 v_2^2 w_6^2 w_3^2 - 78 w_3^3 v_2^2 w_6^2 w_3 + 24 w_3^3 c s^2 w_6^2 w_3 - 12 w_3^3 c s^2 w_3^2 - 12 w_4^3 v_2^2 w_3^2 - \\ & 48 w_4^2 v_2^2 w_6^2 w_3^2 + 12 w_4^2 c s^2 w_6^2 w_3^2 + 48 w_3^4 v_2^2 w_6^2 - 12 w_3^4 c s^2 w_6^2 + 6 w_4^3 v_2^2 w_3^3 + 6 w_4^3 c s^2 w_3^3 - 6 w_4^2 c s^2 w_6^2 w_3^3 + 22 w_4^2 v_2^2 w_6^2 w_3^3 - 12 w_4^3 v_2^2 w_6 w_3 - 12 w_4^3 c s^2 w_6 w_3 - \\ & 12 w_4 c s^2 w_6^2 w_3^2 + 24 w_4 v_2^2 w_6^2 w_3^2 + 24 w_3^4 c s^2 w_6 w_3^2 + 24 w_3^4 v_2^2 w_6 w_3^2 + 12 v_2^2 w_6^2 w_3^3 - 30 w_4 v_2^2 w_6^2 w_3^3 + 6 w_4 c s^2 w_6^2 w_3^3 - 6 w_3^3 v_2^2 w_6 w_3^3 - 6 w_3^4 c s^2 w_6 w_3^3 \end{aligned}$$

$$C_{67} = 36w_7w_4^2 + 12w_2^2cs^2 - 48w_7^2w_4cs^2 + 6w_4^3 - 3w_7w_3^3v_3^2 - 9w_7w_4^3 - 36w_7w_3^2cs^2 - 12w_4^2 + 12w_2^2v_3^2 + 48w_7w_4v_3^2 - 6w_3^4cs^2 + 9w_7w_3^3cs^2 - 24w_7w_4 + 27w_7^2w_4^2v_3^2 + 12w_7^2w_4 + 12w_2^4v_3^2 - 42w_2^2w_4v_3^2 - 60w_7w_4^2v_3^2 - 2w_7w_3^3cs^2 - 6w_3^4v_3^2 + 24w_7w_4cs^2 + w_7^2w_4^3 + 24w_7^2cs^2 + 25w_7^2w_4^2cs^2 - 11w_7^2w_4^2 + 15w_7w_4^3v_3^2$$

$$\begin{aligned}
C_{68} = & -3w_7w_4^3w_2^2 - 3w_3^2w_3^2 - 12w_7w_4^2cs^2w_2^2 + 6w_7^2w_3^4cs^2w_3^2 + 42w_7w_4^2v_3^2w_3^2 + 6w_7^2w_3^4v_3^2w_2^2 + 42w_7w_4^2cs^2w_3^2 + 6w_7^2w_3^4v_3^2w_3^2 - 12w_7w_4^2v_3^2w_2^2 - 30w_7^2w_4v_3^2w_3^2 - 12w_4^2v_3^2w_3^2 + 6w_7^2w_3^4cs^2w_2^2 + 6w_7w_4^2w_2^2 + 6w_4^2w_3^2 - 24w_7^2w_4cs^2w_3^2 - 6w_7^2w_4w_2^3 + 12w_7^2w_4v_3^2w_2^2 - 12w_2^2w_4^3v_3^2w_2^2 + 78w_7w_4acs^2w_3^2 - 12w_4^2cs^2w_3^2 - 21w_7w_4^2w_3^2 + 6w_7^2w_4v_3^2w_3^2 + 6w_7w_4^3v_3^2w_2^2 + 12w_7w_4w_2^3 + 42w_7^2w_4^2cs^2w_2^2 - 12w_7w_4^3cs^2w_3^2 - 3w_7^2w_4^2w_2^2 - 12w_7^2w_4^2v_3^2w_2^2 - 12w_7w_3^4v_3^2w_3^2 + 7w_7^2w_4^2w_3^2 - 48w_7w_4^2cs^2w_3^2 + 6w_7w_3^4cs^2w_2^2 + 6w_4^3cs^2w_3^2 + w_7w_3^2w_2^2 - 24w_7w_4v_3^2w_3^2 + 6w_2^2w_4^2v_3^2w_2 - 36w_7^2cs^2w_3^2 - w_7^2w_3^4w_2^3 - 12w_7w_4^2cs^2w_2^2 + 24w_7^2v_3^2w_3^2 - 24w_7w_4cs^2w_3^2 + 6w_3^2v_3^2w_2^3
\end{aligned}$$

$$\begin{aligned} C_{69} = & -36w_7\tau w_4^2 - 12w_4^2cs^2 + 90w_7^2w_4cs^2 - 6w_4^3 + w_2^2w_3^3v_3^2 + 9w_7\tau w_4^3 + 48w_7w_4^2cs^2 + 12w_4^2 + 12w_7^2v_3^2 - 36w_7w_4v_3^2 + 6w_3^3cs^2 - 12w_7w_3^3cs^2 + \\ & 24w_7w_4 - 8w_2^2w_4^2v_3^2 - 12w_7^2w_4 - 12w_4^2v_3^2 + 48w_7w_4v_3^2 + 4w_7^2w_3^4cs^2 + 6w_3^4v_3^2 - 36w_7w_4cs^2 - w_7^2w_4^3 - 48w_7^2cs^2 - 44w_7^2w_4^2cs^2 + 11w_7^2w_4^2 - 12w_7w_4^3v_3^2 \end{aligned}$$

$$\begin{aligned} C_{70} = & -6w_7w_4^3w_2^2 - 24w_7w_4^2cs^2w_2^2 + 4w_7w_3^3cs^2w_2^3 + 36w_7w_4^2v_3^2w_3^2 + 12w_7w_3^4v_3^2 - 12w_7w_4^3cs^2w_2^2 + 3w_7w_3^4v_3^2w_2^3 - 30w_7w_4v_3^2w_2^3 - 12w_7w_3^2v_3^2w_2^3 + 6w_7w_4^3cs^2w_2 + 12w_7w_2^2w_2^2 - 24w_7w_4cs^2w_2^2 - 18w_7w_3^3v_2^2w_2 + 36w_7w_4cs^2w_2^3 - 12w_4^2cs^2w_2^3 - 6w_7w_2^3w_2^3 + 12w_7w_3^4v_3^2w_2^2 + 48w_7w_4^2cs^2w_2^2 - 12w_7w_3^4cs^2w_2^3 - 6w_7w_4^2w_2^2 + 12w_7w_2^4v_3^2w_2^2 - 12w_7w_3^4v_3^2w_2^3 + 3w_7w_4^2w_2^3 - 32w_7w_4^2cs^2w_2^3 + 12w_7w_4^3cs^2w_2^2 + 6w_4^3cs^2w_2^3 + 2w_7w_3^2w_2^2 - 12w_7w_4v_3^2w_2^3 - 12w_7^2cs^2w_2^3 - w_7^2w_4^3w_2^3 - 12w_7w_2^4cs^2w_2 + 24w_7w_3^2w_2^3 - 12w_7w_4cs^2w_2^3 + 6w_4^3v_3^2w_2^3 \end{aligned}$$

$$\begin{aligned}
C_{71} = & -12w_7^3 w_4^2 v_3^2 w_3^3 - 12w_7^2 w_4^2 v_3^2 w_3^2 + 6w_7 w_4^3 c s^2 w_3^2 - 48w_7^2 w_4^2 c s^2 w_3^3 + 7w_7^2 w_4^2 w_3^3 + 6w_7 w_4^3 v_3^2 w_3^2 + 6w_7^2 w_4^2 v_3^2 w_3^3 + 6w_7^2 w_4^3 v_3^2 - 3w_7^2 w_4^2 w_3^2 - \\
& 12w_7 w_4^3 c s^2 w_3^3 + 42w_7^2 w_4^2 c s^2 w_3^2 + 12w_7 w_4 w_3^3 + 24w_7^2 v_3^2 w_3^3 - 12w_7^2 w_4^2 c s^2 w_3 - w_7 w_4^2 w_3^3 - 24w_7 w_4 c s^2 w_3 + 6w_4^3 v_3^2 w_3^3 + 6w_4^3 c s^2 w_3^3 + w_7^2 w_4^3 w_3^2 - \\
& 24w_7 w_4 v_3^2 w_3^3 - 36w_7^2 c s^2 w_3^3 + 6w_7 w_4^2 v_3^2 w_3 - 12w_7^2 w_4^3 c s^2 w_3^2 + 42w_7 w_4^2 c s^2 w_3^3 + 6w_7 w_4^3 w_3^3 - 12w_7 w_4^2 v_3^2 w_3^2 - 3w_4^3 w_3^3 - 3w_7 w_4^3 w_3^2 + 6w_7^2 w_4^3 c s^2 w_3^3 - \\
& 12w_7 w_4^2 c s^2 w_3^3 + 6w_7^2 w_4^3 v_3^2 w_3^2 + 42w_7 w_4^2 v_3^2 w_3^3 + 12w_7^2 w_4 v_3^2 w_3^2 - 12w_7^2 w_4^3 v_3^2 w_3 - 21w_7 w_4^2 w_3^3 - 12w_4^2 c s^2 w_3^3 + 78w_7^2 w_4 c s^2 w_3^3 - 12w_4^2 v_3^2 w_3^3 - \\
& 30w_7^2 w_4 v_3^2 w_3^3 + 6w_7^2 w_4^3 c s^2 w_3 + 6w_4^2 w_3^3 - 6w_7^2 w_4 w_3^3 - 24w_7^2 w_4 c s^2 w_3^2 + 6w_7 w_4^2 w_3^2
\end{aligned}$$

$$\begin{aligned} C_{72} = & -36w_7w_4^2 - 12w_4^2cs^2 + 90w_7^2w_4cs^2 - 6w_4^3 + w_7^2w_3^3v_3^2 + 9w_7w_4^3 + 48w_7w_4^2cs^2 + 12w_4^2 + 12w_7^2v_3^2 - 36w_7w_4v_3^2 + 6w_3^3cs^2 - 12w_7w_3^3cs^2 + \\ & 24w_7w_4 - 8w_7^2w_4^2v_3^2 - 12w_7^2w_4 - 12w_4^2v_3^2 + 48w_7w_4v_3^2 + 4w_7^2w_3^4cs^2 + 6w_3^4v_3^2 - 36w_7w_4cs^2 - w_7^2w_4 - 48w_7^2cs^2 - 44w_7^2w_4^2cs^2 + 11w_7^2w_4^2 - 12w_7w_4^3v_3^2 \end{aligned}$$

$$C_{73} = -12\omega_7\omega_4^3v_3^2\omega_3^3 + 12\omega_7^2\omega_4^2v_3^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^3 + 3\omega_7^2\omega_4^2\omega_3^3 + 12\omega_7\omega_4^3v_3^2\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 6\omega_7^2\omega_4^2\omega_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^3 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 + 24\omega_7^2v_3^2\omega_3^3 - 12\omega_7^2\omega_4^2cs^2\omega_3 - \omega_7^2\omega_4^3\omega_3^3 - 12\omega_7\omega_4cs^2\omega_3^3 + 6\omega_7^3v_3^2\omega_3^3 + 6\omega_7^3cs^2\omega_3^2 + 2\omega_7^2\omega_4^3\omega_3^2 - 12\omega_7\omega_4v_3^2\omega_3^3 - 12\omega_7^2cs^2\omega_3^3 - 12\omega_7\omega_4^3cs^2\omega_3^2 + 36\omega_7\omega_4^2cs^2\omega_3^3 + 3\omega_7\omega_4^3\omega_3^3 + 3\omega_7^2\omega_4^3v_3^2\omega_3^3 - 24\omega_7\omega_4^2v_3^2\omega_3^2 - 6\omega_7\omega_4^3\omega_3^2 + 4\omega_7^2\omega_4^2cs^2\omega_3^3 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 36\omega_7\omega_4^3v_3^2\omega_3^3 - 18\omega_7^2\omega_4^3v_3^2\omega_3 - 6\omega_7\omega_4^2\omega_3^3 - 12\omega_4^2cs^2\omega_3^3 + 36\omega_7^2\omega_4cs^2\omega_3^3 - 12\omega_4^2v_3^2\omega_3^3 - 30\omega_7^2\omega_4v_3^2\omega_3^3 + 6\omega_7^2\omega_4^3cs^2\omega_3 - 24\omega_7^2\omega_4cs^2\omega_3^2 + 12\omega_7\omega_4^2\omega_3^2$$

$$C_{74} = 24\omega_7^2cs^4 + 12\omega_4^3cs^2v_3^2 + 12\omega_7^2\omega_4cs^2 + 12\omega_4^3v_3^4 - 96\omega_7^2cs^2v_3^2 + 24\omega_7\omega_4cs^4 - 3\omega_7^2\omega_4^3v_3^2 + 24\omega_7\omega_4^2cs^2 - 24\omega_7\omega_4cs^2v_3^2 + 24\omega_7^2\omega_4^2cs^4 - 18\omega_7\omega_4^3v_3^4 + 24\omega_7^2\omega_4v_3^4 - 24\omega_7^2v_3^4 - 12\omega_7\omega_4^3cs^2v_3^2 + 48\omega_7\omega_4v_3^2 + 72\omega_7\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3cs^4 - 6\omega_7\omega_4^3cs^2 - 72\omega_7^2\omega_4^2cs^2v_3^2 + 24\omega_7^2\omega_4^2v_3^2 - 48\omega_7\omega_4v_3^4 + 24\omega_7^2\omega_4v_3^2 - 24\omega_7^2\omega_4v_3^4 + 6\omega_7\omega_4^3cs^4 - 24\omega_7^2\omega_4^2v_3^4 - 72\omega_7\omega_4^2v_3^2 - 24\omega_7^2\omega_4^2cs^2v_3^2 + 156\omega_7^2\omega_4cs^2v_3^2 + \omega_7^2\omega_4^3cs^2 - 12\omega_7\omega_4^2v_3^2 - 24\omega_7\omega_4cs^2 + 6\omega_7^2\omega_4^3cs^2v_3^2 - 48\omega_7^2\omega_4cs^4 - 8\omega_7^2\omega_4^2cs^2 + 48\omega_7\omega_4^2cs^2v_3^2 + 18\omega_7\omega_4^3v_3^2 + 3\omega_7^2\omega_4^3v_3^4 - 24\omega_7\omega_4^2cs^4$$

$$C_{75} = -24\omega_7\omega_4^2 - 12\omega_4^2cs^2 + 42\omega_7^2\omega_4cs^2 - 6\omega_4^3 + 2\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3 + 24\omega_7\omega_4^2cs^2 + 12\omega_4^2 - 12\omega_7^2v_3^2 - 12\omega_7\omega_4v_3^2 + 6\omega_7^2\omega_4^3cs^2 - 6\omega_7\omega_4^3cs^2 + 12\omega_7\omega_4 - 16\omega_7^2\omega_4^2v_3^2 - 6\omega_7^2\omega_4 - 12\omega_7^2v_3^2 + 24\omega_7^2\omega_4v_3^2 + \omega_7^2\omega_4^3cs^2 + 6\omega_7^2\omega_4v_3^2 - 12\omega_7\omega_4cs^2 - \omega_7^2\omega_4^3 - 24\omega_7^2\omega_4^2cs^2 - 20\omega_7^2\omega_4^2cs^2 + 8\omega_7^2\omega_4^2 - 6\omega_7\omega_4^3v_3^2$$

## 2.4 CLBM1

### 2.4.1 Definitions

Collision operator  $C$ :

$$C(f) = \mathbf{K}^{-1}\mathbf{S}(\kappa^{(eq)} - \mathbf{K}f),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2)$ .

Matrix  $\mathbf{K}$  corresponds to the transformation matrix to the central moment basis defined as

$$\kappa = (k_{(0,0,0)}, k_{(1,0,0)}, k_{(0,1,0)}, k_{(0,0,1)}, k_{(2,0,0)}, k_{(0,2,0)}, k_{(0,0,2)})^T,$$

and is given by

$$\mathbf{K} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ -v_1 & 1-v_1 & -v_1 & -v_1 & -v_1-1 & -v_1 & -v_1 \\ -v_2 & -v_2 & 1-v_2 & -v_2 & -v_2 & -v_2-1 & -v_2 \\ -v_3 & -v_3 & -v_3 & 1-v_3 & -v_3 & -v_3 & -v_3-1 \\ v_1^2 & (1-v_1)^2 & v_1^2 & v_1^2 & (v_1+1)^2 & v_1^2 & v_1^2 \\ v_2^2 & v_2^2 & (1-v_2)^2 & v_2^2 & v_2^2 & (v_2+1)^2 & v_2^2 \\ v_3^2 & v_3^2 & v_3^2 & (1-v_3)^2 & v_3^2 & v_3^2 & (v_3+1)^2 \end{pmatrix}.$$

The equilibrium central moments are defined by

$$\kappa^{(eq)} = \mathbf{KM}^{-1}\mu^{(eq)},$$

i.e.,

$$\kappa^{(eq)} = (\rho, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2)^T.$$

### 2.4.2 Conservation of mass equation

 attached text file: `output_d3q7_ade_clbm1_symbolic_pde_00.txt`

$$\frac{\partial \rho}{\partial t} + \frac{v_1\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2+\omega_2)\frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + (-2+\omega_2)\frac{v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2+\omega_2)\frac{\rho\delta_l^2}{2\omega_2\delta_t} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2-\omega_3)\frac{v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-\omega_2\omega_3 + \omega_2 + \omega_3)\frac{v_1\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} +$$

$$\begin{aligned}
& (-\omega_2\omega_3 + \omega_2 + \omega_3) \frac{\rho\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{v_1\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{\rho\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (-\omega_2\omega_3 + \omega_2 + \omega_3) \frac{v_2\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\
& (2 - \omega_2) \frac{v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_3) \frac{v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho\delta_l^2}{2\omega_3\delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{v_2\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{\rho\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_4}{\partial t} + \\
& (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{v_3\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{v_3\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} \\
& + (-2 + \omega_4) \frac{v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\rho\delta_l^2}{2\omega_4\delta_t} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\rho\delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{cs^2\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + \\
& (-2 + \omega_2) \frac{\rho v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho\delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + (-\omega_2\omega_3 + \omega_2 + \omega_3) \frac{v_2v_1\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{\rho v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (2 - \omega_2) \frac{\rho v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_3) \frac{\rho v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho\delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + \\
& (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{v_1v_3\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{\rho v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (2 - \omega_2) \frac{\rho v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{v_2v_3\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} \\
& + (2 - \omega_4) \frac{\rho v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{\rho v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_4) \frac{cs^2\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{\rho v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (12 + \omega_2^2 - 12\omega_2) \frac{\rho\delta_l\delta_t}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_2^2 - 12\omega_2) \frac{\rho v_1\delta_l^2}{6\omega_2^2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + C_1 \frac{v_1\delta_l^3}{6\omega_5\omega_2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (12 + \omega_3^2 - 12\omega_3) \frac{\rho\delta_l\delta_t}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + (-2\omega_2\omega_3^2 + 3\omega_3^2 + 9\omega_2\omega_3 - 6\omega_2 - 6\omega_3) \frac{\rho v_2\delta_l^2}{6\omega_2\omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + \\
& (3\omega_2^2 + 9\omega_2\omega_3 - 6\omega_2 - 2\omega_2^2\omega_3 - 6\omega_3) \frac{\rho v_1\delta_l^2}{6\omega_2^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + C_3 \frac{v_2\delta_l^3}{2\omega_5\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& (-6\omega_2\omega_3^2 + 6\omega_3^2 + 6\omega_2^2 - 6\omega_2^2\omega_3 + \omega_2^2\omega_3^2) \frac{\rho v_2v_1\delta_l^3}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (v_1^2\omega_5\omega_2^2 - 3cs^2\omega_5\omega_2^2 + 6v_1^2\omega_5\omega_2 + 18cs^2\omega_5\omega_2 - 6v_1^2\omega_2^2 + 6cs^2\omega_2^2 - 12cs^2\omega_5 - 12v_1^2\omega_5 + 12v_1^2\omega_2 - 12cs^2\omega_2) \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} \\
& + (12 + \omega_3^2 - 12\omega_3) \frac{\rho v_2\delta_l^2}{6\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2} + C_4 \frac{v_1\delta_l^3}{2\omega_2^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-3cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6 - 12cs^2\omega_6 + 18cs^2\omega_6\omega_3 + \\
& v_2^2\omega_6\omega_3^2 - 12cs^2\omega_3 - 6v_2^2\omega_3^2 + 12v_2^2\omega_3 + 6cs^2\omega_3^2 + 6v_2^2\omega_6\omega_3) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-6\omega_2\omega_3^2 + 6\omega_3^2 + 6\omega_2^2 - 6\omega_2^2\omega_3 + \omega_2^2\omega_3^2) \frac{\rho v_2v_1\delta_l^3}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2\delta_l^3}{6\omega_6\omega_3\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\rho\delta_l\delta_t}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-6\omega_4 - 2\omega_4^2\omega_2 - 6\omega_2 + 3\omega_4^2 + 9\omega_4\omega_2) \frac{\rho v_3\delta_l^2}{6\omega_4^2\omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (-6\omega_4 + 3\omega_2^2 - 6\omega_2 + 9\omega_4\omega_2 - 2\omega_4\omega_2^2) \frac{\rho v_1\delta_l^2}{6\omega_4\omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3\delta_l^3}{2\omega_4^2\omega_5\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2 + 6\omega_2^2 + 6\omega_4^2 - 6\omega_4\omega_2^2) \frac{\rho v_1v_3\delta_l^3}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\
& (v_1^2\omega_5\omega_2^2 - 3cs^2\omega_5\omega_2^2 + 6v_1^2\omega_5\omega_2 + 18cs^2\omega_5\omega_2 - 6v_1^2\omega_2^2 + 6cs^2\omega_2^2 - 12cs^2\omega_5 - 12v_1^2\omega_5 + 12v_1^2\omega_2 - 12cs^2\omega_2) \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} \\
& + (-6\omega_4 - 2\omega_4^2\omega_3 + 3\omega_4^2 - 6\omega_3 + 9\omega_4\omega_3) \frac{\rho v_3\delta_l^2}{6\omega_4^2\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-6\omega_4 + 3\omega_3^2 - 2\omega_4\omega_3^2 - 6\omega_3 + 9\omega_4\omega_3) \frac{\rho v_2\delta_l^2}{6\omega_4\omega_3^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_4^2\omega_2\omega_3 + \omega_4^2\omega_2^2 + \omega_4\omega_2^2\omega_3 + \omega_4^2\omega_3^2 - 2\omega_4\omega_2\omega_3^2 - 2\omega_4^2\omega_2\omega_3 + \omega_4^2\omega_2^2\omega_3 + \omega_4\omega_2\omega_3^2 + \omega_4^2\omega_2^2 - 2\omega_4^2\omega_2\omega_3) \frac{2v_2v_1v_3\delta_l^3}{\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (-6\omega_4^2\omega_3 + 3\omega_3^2 + 2\omega_4^2\omega_3^2 + 3\omega_4^2 - 6\omega_4\omega_3^2 + 6\omega_4\omega_3) \frac{\rho v_2v_3\delta_l^3}{3\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (2\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2 + 3\omega_2^2 + 3\omega_4^2 + 6\omega_4\omega_2 - 6\omega_4\omega_2^2) \frac{\rho v_1v_3\delta_l^3}{3\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2\omega_3^2 + 3\omega_3^2 + 3\omega_2^2 + 6\omega_2\omega_3 - 6\omega_2^2\omega_3 + 2\omega_2^2\omega_3^2) \frac{\rho v_2v_1\delta_l^3}{3\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_2^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_4^2\omega_3 + 6\omega_3^2 + \omega_4^2\omega_3^2 + 6\omega_4^2 - 6\omega_4\omega_3^2) \frac{\rho v_2v_3\delta_l^3}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + (-3cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6 - 12cs^2\omega_6 + 18cs^2\omega_6\omega_3 + \\
& v_2^2\omega_6\omega_3^2 - 12cs^2\omega_3 - 6v_2^2\omega_3^2 + 12v_2^2\omega_3 + 6cs^2\omega_3^2 + 6v_2^2\omega_6\omega_3) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (12 - 12\omega_4 + \omega_4^2) \frac{\rho v_3\delta_l^2}{6\omega_4^2} \frac{\partial^3 v_3}{\partial t \partial x_2^2} + \\
& C_9 \frac{v_1\delta_l^3}{2\omega_7\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (\omega_7\omega_4^2v_3^2 + 18\omega_7\omega_4\omega_4cs^2 - 12\omega_7\omega_4cs^2 - 12\omega_4\omega_4cs^2 - 6\omega_4^2v_3^2 + 12\omega_4v_3^2 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 + 6\omega_7\omega_4v_3^2 - 12\omega_7v_3^2) \frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} \\
& + (\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2 + 6\omega_2^2 + 6\omega_4^2 - 6\omega_4\omega_2^2) \frac{\rho v_1v_3\delta_l^3}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + C_{10} \frac{v_2\delta_l^3}{2\omega_7\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_2^2}
\end{aligned}$$

$$\begin{aligned}
& (\omega_7 \omega_4^2 v_3^2 + 18 \omega_7 \omega_4 c s^2 - 12 \omega_4 c s^2 - 12 \omega_4 c s^2 - 6 \omega_4^2 v_3^2 + 12 \omega_4 v_3^2 + 6 \omega_4^2 c s^2 - 3 \omega_7 \omega_4^2 c s^2 + 6 \omega_7 \omega_4 v_3^2 - 12 \omega_7 v_3^2) \frac{\rho \delta_l^3}{12 \omega_7 \omega_4^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + (-6 \omega_4^2 \omega_3 + 6 \omega_3^2 + \omega_4^2 \omega_3^2 + 6 \omega_4^2 - 6 \omega_4 \omega_3^2) \frac{\rho v_2 v_3 \delta_l^3}{6 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3 \delta_l^3}{6 \omega_7 \omega_4 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\rho \delta_l^3}{12 \omega_7 \omega_4^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2 - \omega_2^2 + 3 \omega_2) \frac{\rho \delta_l \delta_t^2}{2 \omega_2^3} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-2 - \omega_2^2 + 3 \omega_2) \frac{3 \rho v_1 \delta_l^2 \delta_t}{2 \omega_2^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\rho \delta_l^3}{12 \omega_5^2 \omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_l^4}{24 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{\rho v_1 \delta_l^4}{12 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3 \omega_3) \frac{\rho \delta_l \delta_t^2}{2 \omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (7 \omega_2 \omega_3^3 - 6 \omega_3^3 - 24 \omega_2 \omega_3^2 + 12 \omega_3^2 + 12 \omega_2^2 + 12 \omega_2 \omega_3 - 24 \omega_2^2 \omega_3 + 13 \omega_2^2 \omega_3^2 - \omega_2^2 \omega_3^3) \frac{\rho v_2 \delta_l^2 \delta_t}{12 \omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-24 \omega_2 \omega_3^2 + 12 \omega_3^2 + 12 \omega_2^2 + 12 \omega_2 \omega_3 - 6 \omega_3^3 - \omega_2^3 \omega_3^2 - 24 \omega_2^2 \omega_3 + 13 \omega_2^2 \omega_3^2 + 7 \omega_2^3 \omega_3) \frac{\rho v_1 \delta_l^2 \delta_t}{12 \omega_3^2 \omega_2^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& (18 \omega_2 \omega_3^3 - 12 \omega_3^3 - 6 \omega_3^3 - 7 \omega_2^3 \omega_3^2 - 6 \omega_2^2 \omega_3 + \omega_2^3 \omega_3^3 + 6 \omega_2^2 \omega_3^2 + 12 \omega_2^3 \omega_3 - 7 \omega_2^2 \omega_3^3) \frac{\rho v_2 v_1 \delta_l^3}{6 \omega_2^3 \omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + \\
& C_{16} \frac{\rho \delta_l^3}{12 \omega_5^2 \omega_3^2 \omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{v_2 v_1 \delta_l^4}{6 \omega_5^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{18} \frac{\rho v_2 \delta_l^4}{12 \omega_5^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{\rho v_1 \delta_l^4}{12 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 - \omega_3^2 + 3 \omega_3) \frac{3 \rho v_2 \delta_l^2 \delta_t}{2 \omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + C_{20} \frac{\rho \delta_l^3}{12 \omega_2 \omega_6^2 \omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (12 \omega_2 \omega_3^3 - 6 \omega_3^3 - 6 \omega_2 \omega_3^2 - 12 \omega_2^3 - 7 \omega_3^2 \omega_3^2 + \omega_2^3 \omega_3^3 + 6 \omega_2^2 \omega_3^2 + 18 \omega_3^2 \omega_3 - 7 \omega_2^2 \omega_3^3) \frac{\rho v_2 v_1 \delta_l^3}{6 \omega_2^3 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{21} \frac{\delta_l^4}{4 \omega_2^2 \omega_2^3 \omega_6^2 \omega_3^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{\rho v_1 \delta_l^4}{12 \omega_2^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{\rho v_2 \delta_l^4}{12 \omega_5^2 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{\rho \delta_l^3}{12 \omega_6^2 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^3} + \\
& C_{25} \frac{v_2 v_1 \delta_l^4}{6 \omega_2^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{26} \frac{\rho v_2 \delta_l^4}{12 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{27} \frac{\rho v_1 \delta_l^4}{12 \omega_2^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^2} + C_{28} \frac{\delta_l^4}{24 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{29} \frac{\rho v_2 \delta_l^4}{12 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-2 + 3 \omega_4 - \omega_4^2) \frac{\rho \delta_l \delta_t^2}{2 \omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (7 \omega_4^2 \omega_2 + 13 \omega_4^2 \omega_2^2 - 24 \omega_4^2 \omega_2 + 12 \omega_2^2 - \omega_4^3 \omega_2^2 + 12 \omega_4^2 + 12 \omega_4 \omega_2 - 6 \omega_4^3 - 24 \omega_4 \omega_2^2) \frac{\rho v_3 \delta_l^2 \delta_t}{12 \omega_4^3 \omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-\omega_4^2 \omega_3^3 + 13 \omega_4^2 \omega_2^2 - 24 \omega_4^2 \omega_2 + 12 \omega_2^2 - 6 \omega_3^2 + 12 \omega_4^2 + 12 \omega_4 \omega_2 - 24 \omega_4 \omega_2^2 + 7 \omega_4 \omega_3^3) \frac{\rho v_1 \delta_l^2 \delta_t}{12 \omega_4^2 \omega_2^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-7 \omega_4^2 \omega_3^3 + 18 \omega_4^2 \omega_2 + 6 \omega_4^2 \omega_2^2 + \omega_4^3 \omega_2^3 - 6 \omega_3^2 - 7 \omega_4^2 \omega_2^2 - 12 \omega_4^3 - 6 \omega_4 \omega_2^2 + 12 \omega_4 \omega_3^3) \frac{\rho v_1 v_3 \delta_l^3}{6 \omega_4^3 \omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + \\
& C_{30} \frac{\rho \delta_l^3}{12 \omega_4 \omega_5^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{31} \frac{v_1 v_3 \delta_l^4}{6 \omega_3^3 \omega_4^2 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{32} \frac{\rho v_3 \delta_l^4}{12 \omega_3^2 \omega_4^2 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{33} \frac{\rho v_1 \delta_l^4}{12 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-\omega_4^3 \omega_3^3 - 24 \omega_4^2 \omega_3 + 12 \omega_3^2 + 13 \omega_4^2 \omega_3^2 + 7 \omega_4^3 \omega_3 + 12 \omega_4^2 - 24 \omega_4 \omega_3^2 - 6 \omega_4^3 + 12 \omega_4 \omega_3) \frac{\rho v_3 \delta_l^2 \delta_t}{12 \omega_3^3 \omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (-6 \omega_3^3 - 24 \omega_4^2 \omega_3 + 12 \omega_3^2 + 13 \omega_4^2 \omega_3^2 - \omega_4^2 \omega_3^3 + 7 \omega_4 \omega_3^3 + 12 \omega_4^2 - 24 \omega_4 \omega_3^2 + 12 \omega_4 \omega_3) \frac{\rho v_2 \delta_l^2 \delta_t}{12 \omega_4^2 \omega_3^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{\rho v_2 v_3 \delta_l^3}{6 \omega_4^3 \omega_2 \omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{35} \frac{\rho v_1 v_3 \delta_l^3}{6 \omega_3^3 \omega_4^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{36} \frac{\rho v_2 v_1 \delta_l^3}{6 \omega_4 \omega_3^2 \omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{37} \frac{v_2 v_3 \delta_l^4}{w_3^3 \omega_5^2 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{\rho v_2 v_1 v_3 \delta_l^4}{6 \omega_4^3 \omega_2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\rho v_3 \delta_l^4}{12 \omega_4^3 \omega_2 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{40} \frac{\rho v_2 \delta_l^4}{12 \omega_5^2 \omega_3^2 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-6 \omega_3^3 - 7 \omega_4^2 \omega_3^2 + \omega_4^3 \omega_3^3 + 6 \omega_4^2 \omega_3^2 + 18 \omega_3^2 \omega_3 - 7 \omega_4^2 \omega_3^3 + 12 \omega_4 \omega_3^3 - 6 \omega_4 \omega_3^2 - 12 \omega_4^3) \frac{\rho v_2 v_3 \delta_l^3}{6 \omega_4^3 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{41} \frac{\rho \delta_l^3}{12 \omega_4 \omega_6^2 \omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{42} \frac{v_1 v_3 \delta_l^4}{w_4^3 \omega_3^2 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{\rho v_3 \delta_l^4}{12 \omega_3^3 \omega_4^2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{44} \frac{\rho v_2 v_1 v_3 \delta_l^4}{6 \omega_4^3 \omega_2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\rho v_1 \delta_l^4}{12 \omega_3^2 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{46} \frac{v_2 v_3 \delta_l^4}{6 \omega_4^3 \omega_2 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{47} \frac{\rho v_3 \delta_l^4}{12 \omega_3^3 \omega_4^2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{48} \frac{\rho v_2 \delta_l^4}{12 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + 3 \omega_4 - \omega_4^2) \frac{3 \rho v_3 \delta_l^2 \delta_t}{2 \omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2^3} + C_{49} \frac{\rho \delta_l^3}{12 \omega_2^2 \omega_4^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^3} + \\
& (-7 \omega_4^2 \omega_3^3 + 12 \omega_4^2 \omega_2 + 6 \omega_4^2 \omega_2^2 + \omega_4^3 \omega_2^3 - 6 \omega_4^2 \omega_2 - 12 \omega_3^3 - 7 \omega_4^2 \omega_2^2 - 6 \omega_4^3 + 18 \omega_4 \omega_3^2) \frac{\rho v_1 v_3 \delta_l^3}{6 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{50} \frac{\delta_l^4}{4 \omega_2^2 \omega_3^2 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{51} \frac{\rho v_1 \delta_l^4}{12 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + C_{52} \frac{\rho v_3 \delta_l^4}{12 \omega_3^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{\rho \delta_l^3}{12 \omega_2^2 \omega_4^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
& (-12 \omega_3^3 - 7 \omega_4^2 \omega_3^2 - 6 \omega_4^2 \omega_3 + \omega_4^3 \omega_3^3 + 6 \omega_4^2 \omega_3^2 + 12 \omega_4^3 \omega_3^3 - 7 \omega_4^2 \omega_3^3 + 18 \omega_4 \omega_3^3 - 6 \omega_4^3) \frac{\rho v_2 v_3 \delta_l^3}{6 \omega_4^3 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
& C_{54} \frac{v_2 v_1 \delta_l^4}{w_7^2 \omega_4^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{55} \frac{\rho v_2 \delta_l^4}{12 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{56} \frac{\rho v_1 \delta_l^4}{12 \omega_2^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{57} \frac{\rho v_2 v_1 v_3 \delta_l^4}{6 \omega_4^3 \omega_2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{58} \frac{\delta_l^4}{4 \omega_2^2 \omega_3^2 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{59} \frac{\rho v_2 \delta_l^4}{12 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{60} \frac{\rho v_3 \delta_l^4}{12 \omega_3^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{61} \frac{\rho \delta_l^3}{12 \omega_2^2 \omega_4^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_3^3} + \\
& C_{62} \frac{v_1 v_3 \delta_l^4}{6 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{63} \frac{\rho v_3 \delta_l^4}{12 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{64} \frac{\rho v_1 \delta_l^4}{12 \omega_2^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{65} \frac{v_2 v_3 \delta_l^4}{6 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& C_{66} \frac{\rho v_3 \delta_l^4}{12 \omega_2^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{67} \frac{\rho v_2 \delta_l^4}{12 \omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{68} \frac{\delta_l^4}{24 \omega_2^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{69} \frac{\rho v_3 \delta_l^4}{12 \omega_2^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
& 12cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 4v_2^2cs^2\omega_5^2\omega_6^2\omega_3^3 + cs^4\omega_5\omega_2^3\omega_6^2\omega_3^2 - 4v_2^2cs^2\omega_5^2\omega_2\omega_6^2\omega_3^2 + 2v_2^2cs^2\omega_5^2\omega_2^2\omega_6\omega_3^3 + 4v_2^2v_1^2\omega_5^2\omega_6^2\omega_3^2 - 4cs^2v_1^2\omega_5^2\omega_6^2\omega_3^2 + \\
& 4cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 2v_2^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^3 - 2cs^4\omega_5\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + 2v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 14v_2^2v_1^2\omega_5^2\omega_3^2\omega_6^2\omega_3^2 - 2v_2^2v_1^2\omega_5^2\omega_6^2\omega_3^2 + \\
& 10cs^2v_1^2\omega_5^2\omega_3^2\omega_6^2\omega_3^2 - 4v_2^2cs^2\omega_5^2\omega_2^2\omega_6\omega_3^3 + 2cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^3 + 10v_2^2cs^2\omega_5^2\omega_2\omega_6^2\omega_3^2 + 4cs^2v_1^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 2v_2^2v_1^2\omega_5^2\omega_3^2\omega_6^2\omega_3^2 - 2cs^4\omega_5^2\omega_2\omega_6^2\omega_3^2 + \\
& 14v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 2cs^4\omega_5^2\omega_2^3\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_3^2\omega_6\omega_3^3 - 4cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^3 - 3v_2^2cs^2\omega_5\omega_2^3\omega_6^2\omega_3^2 - 2cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + 8v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + \\
& 2cs^2v_1^2\omega_5^2\omega_3^2\omega_6^2\omega_3^2 + 3v_2^2v_1^2\omega_5\omega_2^3\omega_6^2\omega_3^2 - 28v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + 4cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 2cs^4\omega_5^2\omega_2\omega_6^2\omega_3^2 + 2v_2^2cs^2\omega_5\omega_2^3\omega_6^2\omega_3^2 + 8cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - \\
& 8v_2^2cs^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - cs^2v_1^2\omega_5\omega_2^3\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 4cs^2v_1^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 3cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^3 + 2v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_2\omega_6^2\omega_3^2 + \\
& 4cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - cs^4\omega_5^2\omega_2^3\omega_6^2\omega_3^2 + 3v_2^2v_1^2\omega_5^2\omega_3^2\omega_6\omega_3^3 - 4v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + 12v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + 10cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - v_2^2cs^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - \\
& 4cs^2v_1^2\omega_5^2\omega_3^2\omega_6^2 - 4v_2^2cs^2\omega_5\omega_2\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 - 2cs^4\omega_5^2\omega_2\omega_6^2\omega_3^2 - 10v_2^2v_1^2\omega_5^2\omega_3^2\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^3\omega_6^2\omega_3^2 \\
C_{22} = & 12v_2^2\omega_5^2\omega_2^2\omega_3^2 - 4v_2^2\omega_5^2\omega_6^2\omega_3^2 + cs^2\omega_5^2\omega_6^2\omega_3^2 - 14cs^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 6v_2^2\omega_5^2\omega_3^2 + 22v_2^2\omega_5^2\omega_6^2\omega_3^2 + 12v_2^2\omega_5^2\omega_6^2\omega_3^2 + 24cs^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 18v_2^2\omega_5^2\omega_6^2\omega_3^2 - \\
& 12cs^2\omega_2\omega_6^2\omega_3^2 + 24v_2^2\omega_2\omega_6^2\omega_3^2 - 30v_2^2\omega_2\omega_6^2\omega_3^2 + 6cs^2\omega_2\omega_6^2\omega_3^2 - 12cs^2\omega_5^2\omega_6^2\omega_3^2 - 48v_2^2\omega_2\omega_6^2\omega_3^2 + 12cs^2\omega_2\omega_6^2\omega_3^2 + 6cs^2\omega_5^2\omega_6^2\omega_3^2 + \\
& 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - 6cs^2\omega_2^3\omega_6\omega_3^2 + 22v_2^2\omega_2^3\omega_6\omega_3^2 + 24cs^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^3\omega_6\omega_3^2 + 24v_2^2\omega_2^3\omega_6\omega_3^2 + 6v_2^2\omega_2^3\omega_6\omega_3^2 + \\
C_{23} = & 22v_2^2\omega_5^2\omega_2^2\omega_3^2 - 30v_2^2\omega_5^2\omega_3^2\omega_3^2 - 14cs^2\omega_5^2\omega_2^2\omega_3^2 + 6cs^2\omega_5^2\omega_3^2\omega_3^2 + 12v_2^2\omega_5\omega_2\omega_3^2 - 48v_2^2\omega_5^2\omega_2^2\omega_3^2 - 12cs^2\omega_5\omega_2\omega_3^2 + 12cs^2\omega_5^2\omega_2^2\omega_3^2 + \\
& cs^2\omega_5^2\omega_2^3\omega_3^2 - 12cs^2\omega_5^2\omega_2^2\omega_3^2 - 4v_2^2\omega_5^2\omega_3^2\omega_3^2 + 24v_2^2\omega_5^2\omega_2^2\omega_3^2 - 6cs^2\omega_5^2\omega_3^2\omega_3^2 + 6v_2^2\omega_5\omega_3^2\omega_3^2 + 6cs^2\omega_5^2\omega_3^2\omega_3^2 - \\
& 6v_2^2\omega_5^2\omega_3^2\omega_3^2 - 12cs^2\omega_5^2\omega_3^2\omega_3^2 + 24v_2^2\omega_5^2\omega_2\omega_3^2 - 24v_2^2\omega_5\omega_2\omega_3^2 + 24cs^2\omega_5\omega_2\omega_3^2 + 12v_2^2\omega_5^2\omega_3^2 - 18v_2^2\omega_5\omega_2\omega_3^2 + 12v_2^2\omega_5^2\omega_3^2 + 24cs^2\omega_5^2\omega_2\omega_3^2 - 12cs^2\omega_5^2\omega_3^2 \\
C_{24} = & -36cs^2\omega_6\omega_3^2 + 24cs^2\omega_6^2 + 6\omega_3^3 + 18v_2^2\omega_6^2\omega_3 + 36\omega_6\omega_3^2 + 9cs^2\omega_6\omega_3^2 - 9\omega_6\omega_3^3 - 12\omega_3^2 - 3v_2^2\omega_6^2\omega_3^2 - 36v_2^2\omega_6^2\omega_3^2 + 15v_2^2\omega_6^2\omega_3^2 - 24\omega_6\omega_3 + 24cs^2\omega_6\omega_3^2 - \\
& 108v_2^2\omega_6\omega_3^2 - 18v_2^2\omega_6^3 - 12\omega_6^2\omega_3 - 48cs^2\omega_6^2\omega_3 + 36v_2^2\omega_6^2\omega_3 + 27v_2^2\omega_6\omega_3^2 - 6cs^2\omega_6^2\omega_3^2 - 2cs^2\omega_6^2\omega_3^2 + \omega_6^2\omega_3^3 + 25cs^2\omega_6^2\omega_3^2 + 12cs^2\omega_6^2\omega_3^2 + 72v_2^2\omega_6\omega_3^2 - 11\omega_6^2\omega_3^2 \\
C_{25} = & 12v_2^2\omega_5^2\omega_3^2 + 6cs^2\omega_5^2\omega_2^2\omega_3^2 + 7\omega_2^2\omega_6^2\omega_3^2 - 36cs^2\omega_5^2\omega_3^2\omega_3^2 - 6v_2^2\omega_5^2\omega_3^2\omega_3^2 - 6v_2^2\omega_5^2\omega_6^2\omega_3^2 - \omega_2^2\omega_6^2\omega_3^2 + 6w_2^2\omega_6\omega_3^2 + 6v_2^2\omega_6^2\omega_3^2 + 36cs^2\omega_5^2\omega_6\omega_3^2 + \\
& 12v_2^2\omega_5^2\omega_6^2\omega_3^2 - 12cs^2\omega_5^2\omega_6\omega_3^2 + 12cs^2\omega_5^2\omega_6^2\omega_3^2 + 6v_2^2\omega_5^2\omega_6^2\omega_3^2 - 6\omega_2^2\omega_6^2\omega_3^2 - 3v_2^2\omega_5^2\omega_6^2\omega_3^2 - 12v_2^2\omega_5^2\omega_6^2\omega_3^2 - 24cs^2\omega_5^2\omega_6\omega_3^2 + 6cs^2\omega_5^2\omega_6^2\omega_3^2 - \\
& 12cs^2\omega_5^2\omega_6^2\omega_3^2 + 12\omega_2^2\omega_6\omega_3 - 36cs^2\omega_5^2\omega_3^2 + \omega_2^2\omega_6^2\omega_3^2 - 6\omega_2^2\omega_6^2\omega_3^2 - 6v_2^2\omega_5^2\omega_6^2\omega_3^2 + 36cs^2\omega_5^2\omega_6^2\omega_3^2 - 3v_2^2\omega_5^2\omega_6^2\omega_3^2 - 24v_2^2\omega_5^2\omega_6\omega_3^2 - \\
& 24cs^2\omega_5^2\omega_6\omega_3 - 12cs^2\omega_5^2\omega_6^2\omega_3^2 + 6v_2^2\omega_5^2\omega_6^2\omega_3^2 - 3\omega_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_5^2\omega_6\omega_3^2 + 72cs^2\omega_5^2\omega_6\omega_3^2 + 6\omega_2^2\omega_6\omega_3^2 - 12cs^2\omega_5^2\omega_6^2\omega_3^2 - 24cs^2\omega_5^2\omega_6\omega_3^2 - 21\omega_2^2\omega_6\omega_3^2 \\
C_{26} = & 96cs^2\omega_6\omega_3^2 - 6\omega_3^3 + 12v_2^2\omega_6^2\omega_3 - 36\omega_6\omega_3^2 - 30cs^2\omega_6\omega_3^2 + 9\omega_6\omega_3^3 + 12\omega_3^2 + v_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 - 14v_2^2\omega_6^2\omega_3^2 + 24\omega_6\omega_3 - 36cs^2\omega_6\omega_3^2 + \\
& 48v_2^2\omega_6\omega_3^2 - 6\omega_2^2\omega_3^2 - 12\omega_6^2\omega_3 + 18cs^2\omega_6^2\omega_3 + 12v_2^2\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^2 + 30cs^2\omega_6^2\omega_3^2 + 4cs^2\omega_6^2\omega_3^2 - \omega_6^2\omega_3^3 - 26cs^2\omega_6^2\omega_3^2 - 60cs^2\omega_6^2\omega_3^2 - 60v_2^2\omega_6\omega_3 + 11\omega_6^2\omega_3^2 \\
C_{27} = & 12v_2^2\omega_5^2\omega_3^2 + 3v_2^2\omega_5^2\omega_6^2\omega_3^2 + 4cs^2\omega_5^2\omega_6^2\omega_3^2 + 3\omega_2^2\omega_6^2\omega_3^2 - 32cs^2\omega_5^2\omega_6^2\omega_3^2 - 6v_2^2\omega_5^2\omega_6^2\omega_3^2 - 12v_2^2\omega_5^2\omega_6^2\omega_3^2 - \omega_2^2\omega_6^2\omega_3^2 + 12\omega_2^2\omega_6\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 + \\
& 36cs^2\omega_5^2\omega_6^2\omega_3^2 + 30v_2^2\omega_5^2\omega_6^2\omega_3^2 + 12v_2^2\omega_5^2\omega_6\omega_3^2 - 12cs^2\omega_5^2\omega_6\omega_3^2 + 12cs^2\omega_5^2\omega_6^2\omega_3^2 - 6\omega_2^2\omega_6\omega_3^2 - 18v_2^2\omega_5^2\omega_6\omega_3^2 - 24cs^2\omega_5^2\omega_6\omega_3^2 + 6cs^2\omega_5^2\omega_6^2\omega_3^2 - \\
& 12cs^2\omega_5^2\omega_6^2\omega_3^2 - 24v_2^2\omega_5^2\omega_6\omega_3^2 - 12cs^2\omega_5^2\omega_6^2\omega_3^2 + 2w_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_5^2\omega_6^2\omega_3^2 + 48cs^2\omega_5^2\omega_6^2\omega_3^2 - 6\omega_2^2\omega_6^2\omega_3^2 + 6cs^2\omega_5^2\omega_6^2\omega_3^2 + 12v_2^2\omega_5^2\omega_6\omega_3^2 - \\
& 12cs^2\omega_5^2\omega_6\omega_3^2 - 12cs^2\omega_5^2\omega_6^2\omega_3^2 - 12v_2^2\omega_5^2\omega_6\omega_3^2 + 36cs^2\omega_5^2\omega_6\omega_3^2 + 3\omega_2^2\omega_6\omega_3^2 - 24cs^2\omega_5^2\omega_6^2\omega_3^2 - 6\omega_2^2\omega_6\omega_3^2 - 24v_2^2\omega_5^2\omega_6^2\omega_3^2 \\
C_{28} = & 24cs^2\omega_6\omega_3^2 - 72v_2^2\omega_3^2 + 3v_2^2\omega_6^2\omega_3^2 - 72v_2^2cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6^2\omega_3^2 + 36v_2^2\omega_6^2\omega_3^2 - 6cs^2\omega_6\omega_3^2 + 144v_2^2cs^2\omega_6\omega_3^2 + 24cs^4\omega_6\omega_3 + 72v_2^2cs^2\omega_6\omega_3^2 - 24cs^4\omega_6\omega_3^2 - \\
& 3v_2^2\omega_6^2\omega_3^2 + 108v_2^2cs^2\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 + 216v_2^2cs^2\omega_6^2\omega_3^2 - 24cs^2\omega_6\omega_3^2 - 72v_2^2\omega_6\omega_3^2 - 36v_2^2\omega_6^2\omega_3^2 - 3cs^2\omega_6^2\omega_3^2 + 12cs^2\omega_6^2\omega_3^2 + 24cs^4\omega_6^2\omega_3^2 - \\
& 36v_2^2cs^2\omega_6^2\omega_3^2 + 72v_2^2\omega_6^2\omega_3^2 + 30v_2^2\omega_6\omega_3^2 + 24cs^4\omega_6^2\omega_3^2 + 72v_2^2\omega_6\omega_3^2 - 48cs^4\omega_6^2\omega_3^2 - 12v_2^2cs^2\omega_6^2\omega_3^2 - 8cs^2\omega_6^2\omega_3^2 - 30v_2^4\omega_6\omega_3^2 + 6v_2^2cs^2\omega_6^2\omega_3^2 \\
C_{29} = & 72cs^2\omega_6\omega_3^2 + 24cs^2\omega_6^2 - 18\omega_3^3 - 12v_2^2\omega_6^2\omega_3 - 24\omega_6\omega_3^2 - 24cs^2\omega_6\omega_3^2 + 12\omega_6\omega_3^3 + 36\omega_3^2 + 2v_2^2\omega_6^2\omega_3^2 - 12v_2^2\omega_6^2\omega_3^2 - 12\omega_6\omega_3 - 12cs^2\omega_6\omega_3^2 + \\
& 24v_2^2\omega_6\omega_3^2 + 42v_2^2\omega_6^2\omega_3^2 + 6\omega_6^2\omega_3 - 30cs^2\omega_6^2\omega_3^2 - 84v_2^2\omega_6^2\omega_3^2 - 24v_2^2\omega_6\omega_3^2 + 30cs^2\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^2 - \omega_6^2\omega_3^3 - 2cs^2\omega_6^2\omega_3^2 - 60cs^2\omega_6^2\omega_3^2 + 60v_2^2\omega_6\omega_3 + 2\omega_6^2\omega_3^2 \\
C_{30} = & -12\omega_4v_1^2\omega_2^2 + 12\omega_4cs^2\omega_2^2 + 30\omega_4v_1^2\omega_5\omega_2^2 - 12v_2^2\omega_5\omega_2^2 - 30\omega_4cs^2\omega_5\omega_2^2 + 12cs^2\omega_5\omega_2^2 - 6\omega_4cs^2\omega_2^2 + 6\omega_4v_1^2\omega_2^2 + 12\omega_4cs^2\omega_5\omega_2^2 - \\
& 24\omega_4v_1^2\omega_5^2 + 9\omega_4cs^2\omega_5\omega_2^2 - 6cs^2\omega_5\omega_2^2 - 9\omega_4v_1^2\omega_5\omega_2^2 + 6v_1^2\omega_5\omega_2^2 - 12\omega_4v_1^2\omega_5\omega_2^2 + 12\omega_4cs^2\omega_5\omega_2^2 - 36\omega_4v_1^2\omega_5^2\omega_2^2 + 12v_1^2\omega_5\omega_2^2 - 30\omega_4cs^2\omega_5\omega_2^2 + \\
& 12cs^2\omega_5^2\omega_2^2 + 3cs^2\omega_5^2\omega_2^2 - 2\omega_4cs^2\omega_5\omega_2^2 - v_1^2\omega_5\omega_2^2 + \omega_4v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_5\omega_2^2 + 8\omega_4v_1^2\omega_5\omega_2^2 - 18cs^2\omega_5\omega_2^2 + 22\omega_4cs^2\omega_5\omega_2^2 \\
C_{32} = & -12\omega_4v_1^2\omega_5\omega_2^2 - 32\omega_4cs^2\omega_5\omega_2^2 - 24\omega_4cs^2\omega_5\omega_2^2 + 3\omega_4v_1^2\omega_5\omega_2^2 + 3\omega_4v_1^2\omega_5\omega_2^2 - \omega_4v_1^2\omega_5\omega_2^2 - 12\omega_4cs^2\omega_5\omega_2^2 + 12\omega_4\omega_5\omega_2^2 - \\
& 12\omega_4cs^2\omega_5^2\omega_2^2 - 3\omega_4v_1^2\omega_5^2\omega_2^2 + 18\omega_4cs^2\omega_5^2\omega_2^2 - 6\omega_4v_1^2\omega_5^2\omega_2^2 - 3v_4^2\omega_5\omega_2^2 + 36\omega_4cs^2\omega_5^2\omega_2^2 - 6\omega_4v_1^2\omega_5^2\omega_2^2 - 12\omega_4v_1^2\omega_5\omega_2^2 + 12\omega_4\omega_5\omega_2^2 + \\
& 36\omega_4cs^2\omega_5^2\omega_2^2 - 24\omega_4cs^2\omega_5\omega_2^2 + 2\omega_4v_1^2\omega_5\omega_2^2 - 24\omega_4v_1^2\omega_5\omega_2^2 + 12\omega_4v_1^2\omega_5\omega_2^2 - 24\omega_4v_1^2\omega_5\omega_2^2 - 3\omega_4v_1^2\omega_5\omega_2^2 + 12\omega_4v_1^2\omega_5\omega_2^2 - 6\omega_4v_1^2\omega_5\omega_2^2 + 12\omega_4cs^2\omega_5\omega_2^2 - \\
& 12\omega_4cs^2\omega_5\omega_2^2 + 6\omega_4cs^2\omega_5\omega_2^2 + 3\omega_4v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_5\omega_2^2 - 12\omega_4v_1^2\omega_5\omega_2^2 + 12\omega_4v_1^2\omega_5\omega_2^2 + 72\omega_4cs^2\omega_5\omega_2^2 + 6\omega_4v_1^2\omega_5\omega_2^2 - 21\omega_4v_1^2\omega_5\omega_2^2 - 12\omega_4cs^2\omega_5\omega_2^2 \\
C_{33} = & -36\omega_5\omega_2^2 + 48v_1^2\omega_5\omega_2^2 + 96cs^2\omega_5\omega_2^2 + 9\omega_5\omega_2^3 - 30cs^2\omega_5\omega_2^3 - 6v_1^2\omega_5\omega_2^3 + 12\omega_2^2 - 60v_1^2\omega_5\omega_2^3 - 36cs^2\omega_5\omega_2^3 - 6\omega_2^3 + 24\omega_5\omega_2 + 12v_1^2\omega_5\omega_2^2 + \\
& 12v_1^2\omega_5\omega_2^2 + 18cs^2\omega_5\omega_2^2 - 60cs^2\omega_5\omega_2^2 - 12\omega_5\omega_2 + 30cs^2\omega_5\omega_2^3 - 6v_1^2\omega_5\omega_2^3 + 12v_1^2\omega_5\omega_2^2 - \omega_5^2\omega_2^3 + 4cs^2\omega_5\omega_2^3 + v_1^2\omega_5\omega_2^3 + 11\omega_5\omega_2^2 - 14v_1^2\omega_5\omega_2^2 - 26cs^2\omega_5\omega_2^2 \\
C_{34} = & -6\omega_2\omega_3^3 - 6\omega_4^3\omega_2 - 12\omega_4^2\omega_2\omega_3 + 12\omega_4^3\omega_2^2\omega_3^2 - 4\omega_4^3\omega_2^3 - 12\omega_4^2\omega_2\omega_3^2 - 16\omega_4^2\omega_2\omega_3^2 + 30\omega_4^2\omega_2\omega_3^2 - 6\omega_4^3\omega_2 + 12\omega_4^2\omega_2\omega_3^2 + 18\omega_4\omega_2\omega_3^2 - 6\omega_4^3\omega_2 + 12\omega_4^2\omega_2\omega_3^2 + \\
& 18\omega_4^3\omega_2\omega_3^2 - 12\omega_4\omega_2\omega_3^2 - 16\omega_4^2\omega_2\omega_3^2 + 3\omega_4^3\omega_2\omega_3^2 \\
C_{35} = & 12\omega_4^2\omega_2^3 - 6\omega_4^3\omega_2 - 12\omega_4^2\omega_2\omega_3 + 3\omega_4^3\omega_2^2\omega_3 - 12\omega_4^2\omega_2^2 - 12\omega_4\omega_2\omega_3 - 16\omega_4^2\omega_2\omega_3^2 - 4\omega_4^3\omega_2^3 + 18\omega_4\omega_2\omega_3^2 - 6\omega_4^3\omega_2 + 12\omega_4^2\omega_2\omega_3^2 + \\
& 18\omega_4^3\omega_2\omega_3 - 16\omega_4^2\omega_2\omega_3^2 - 6\omega_4^3\omega_2\omega_3^2 + 30\omega_4^2\omega_2\omega_3^2 \\
C_{36} = & -6\omega_2\omega_3^3 - 16\omega_4\omega_2\omega_3^2 - 12\omega_4\omega_2\omega_3^2 + 3\omega_4\omega_2\omega_3^2 + 30\omega_4\omega_2\omega_3^2 + 18\omega_4\omega_2\omega_3^2 - 16\omega_4\omega_2\omega_3^2 + 18\omega_4\omega_2\omega_3^2 - 6\omega_4\omega_3 + 12\omega_4\omega_2\omega_3^2 + \\
& 4\omega_3^2\omega_3^2 - 12\omega_2^2\omega_3^2 - 6\omega_2^3\omega_3 - 12\omega_2^2\omega_3^2 + 6\omega_2^3\omega_3 + 30\omega_2^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{37} = & -2w_4^2cs^2w_5^2w_2^2w_3^2 + 2w_4^3v_1^2w_2^2w_3^3 + 4w_4v_1^2w_5^2w_2^2w_3^3 - 7w_4^3v_1^2w_2^2w_2w_3^3 - 2w_4^2cs^2w_5^2w_2^3 + 2w_4^3v_1^2w_5w_2^2w_3^2 + 6w_4^3cs^2w_5^2w_2w_3^3 - \\
& 2w_4^3cs^2w_5w_2w_3^2 + 4w_4^2v_1^2w_5^2w_2^2w_3^2 - 2w_4cs^2w_5^2w_2^2w_3^3 - 6w_4^3v_1^2w_5w_2w_3^2 + 3w_4^3v_2^2w_5^2w_2w_3^2 + 3w_4^3v_1^2w_5w_2^2w_3^2 + 6w_4^2cs^2w_5^2w_2^2w_3^2 + 3w_4^2v_1^2w_5w_2w_3^2 - \\
& 10w_4^2v_1^2w_5^2w_2^2w_3^3 + 6w_4^3cs^2w_5w_2^2w_3^3 - 2w_4^3cs^2w_5w_2w_3^2 - 2w_3^2cs^2w_5^2w_2^2w_3^2 - 8w_4^2v_1^2w_5^2w_3^2w_2^2 + w_4cs^2w_5^2w_2^2w_3^2 + 2w_3^2v_1^2w_5^2w_3^2w_2^2 + \\
& w_4^3cs^2w_5^2w_3^2w_2^2 - w_4^3v_1^2w_5w_3^2w_2^2 + w_4^2cs^2w_5^2w_3^2w_2^3 + 3w_4^2v_1^2w_5^2w_3^2w_2^3 - w_4^2v_1^2w_5w_3^2w_2^3 - 8w_4v_1^2w_5^2w_3^2w_2^3 - 2w_4^3cs^2w_5w_3^2w_2^3 + 7w_4^2v_1^2w_5^2w_3^2w_2^3 + \\
& 3w_4^3v_2^2w_5^2w_3^2w_2^2 - 2w_4^2cs^2w_5^2w_3^2w_2^3 + 2w_4^3v_1^2w_5^2w_3^2w_2^3 - 2w_4^2cs^2w_5^2w_3^2w_2^3 + 7w_4^3v_2^2w_5^2w_3^2w_2^3 - w_4^2v_1^2w_5w_3^2w_2^3 - 2w_4^2cs^2w_5^2w_3^2w_2^3 + w_4^2cs^2w_5^2w_3^2w_2^3 + \\
& 4w_4^3v_1^2w_5^2w_2^2w_3 - 2w_4^3v_1^2w_5^2w_3^2w_2^3 + w_4^2cs^2w_5w_3^2w_2^2w_3^3 - 10w_4^3v_1^2w_5^2w_2^2w_3^2 + 2w_4^3v_1^2w_5w_2w_3^2w_2^3 - 2w_4^2cs^2w_5^2w_2w_3^2 + 3w_4^2v_1^2w_5^2w_2w_3^2 + 6w_4^3cs^2w_5^2w_2^2w_3^2 - \\
& 2w_4^3cs^2w_5w_2w_3^2 - 2w_4^2cs^2w_5w_2^2w_3^3 - 8w_4^2v_1^2w_5^2w_2^2w_3^3 + 8w_4^3v_1^2w_5^2w_2^2w_3^3 + w_4^2cs^2w_5^2w_2^2w_3^2 - 6w_4^3cs^2w_5^2w_2^2w_3^2 + 2w_4^2v_1^2w_5w_2w_3^2
\end{aligned}$$

$$C_{38} = 18w_4w_3^2w_2^3 - 30w_4^3w_2^3w_3 + 28w_4^3w_2^2w_3^2 - 30w_4^3w_2^2w_3^2 + 12w_4^3w_2^3 - 30w_4w_3^2w_2^3 + 6w_4^3w_2^2w_3 - 5w_4^3w_2^3w_3^2 + 18w_4^2w_2w_3^3 + 12w_4^3w_2^3 + 6w_4w_2^2w_3^2 + 24w_4^3w_2^2w_3^2 + 12w_4^2w_2^2w_3^2 - 30w_4^2w_2^2w_3^2 + 18w_4^2w_2^3w_3 + 12w_3^2w_2^3 + 18w_4^3w_2w_3^2 - 42w_4^2w_2^3w_3^2 + 24w_4^2w_3^2w_3^2 - 36w_4^3w_2w_3^2$$

$$\begin{aligned} C_{39} = & 16w_4^3v_1^2w_5^2\omega_2^2 - 32w_4^3cs^2\omega_5^2\omega_2^2 - 24w_4^2cs^2\omega_5^2w_2 + 4w_4^3cs^2\omega_5^2\omega_3^2 - 5w_3^3v_1^2w_5^2\omega_3^2 + 24w_4^2v_1^2w_5^2\omega_3^2 - 12w_4^2cs^2\omega_5^2\omega_3^2 - 12w_4^3cs^2\omega_5^2\omega_5^2 + \\ & 6w_4^3cs^2\omega_3^2 - 6w_4^3v_1^2\omega_3^2 + 48w_4^2cs^2\omega_5^2\omega_2^2 - 36w_4^2v_1^2w_5^2\omega_2^2 + 12w_4^3v_1^2\omega_2^2 - 6w_3^3v_1^2w_5^2\omega_2 - 12w_4^3cs^2\omega_2^2 + 36w_4^3cs^2\omega_5^2\omega_2 - 24w_4^2cs^2\omega_5^2\omega_2^2 + \\ & 24w_4^2v_1^2w_5\omega_2^2 + 12w_4^3v_1^2\omega_5\omega_2 - 12w_4^3cs^2\omega_5\omega_2 - 12w_4^2v_1^2\omega_5\omega_3^2 + 12w_4^2cs^2\omega_5\omega_3^2 - 12w_4^3cs^2\omega_5\omega_3^2 + 12w_4^3v_1^2\omega_5\omega_3^2 + 6w_4cs^2\omega_5^2\omega_3^2 + 12v_1^2\omega_5^2\omega_3^2 - \\ & 30w_4v_1^2\omega_5^2\omega_3^2 - 36w_4^3v_1^2\omega_5\omega_2^2 + 36w_4^3cs^2\omega_5\omega_2^2 + 24w_4v_1^2\omega_5^2\omega_2^2 - 12w_4cs^2\omega_5^2\omega_2^2 \end{aligned}$$

$$\begin{aligned} C_{40} = & 16v_1^2 w_5^2 w_2^2 w_3^3 - 30v_1^2 w_5^2 w_2^3 w_3 - 32c s^2 w_5^2 w_2^2 w_3 + 6c s^2 w_5^2 w_3^2 w_3 + 12v_1^2 w_5 w_2 w_3^3 - 36v_1^2 w_5^2 w_2^2 w_3^2 - 12c s^2 w_5 w_2 w_3^3 + 48c s^2 w_5^2 w_2^2 w_3^2 + \\ & 4c s^2 w_5^2 w_3^2 w_3^3 - 12c s^2 w_5^2 w_2^2 w_3 - 5v_1^2 w_5^2 w_3^2 w_3^3 + 24v_1^2 w_5^2 w_2^2 w_3 - 12c s^2 w_5^2 w_3^2 w_3^2 + 24v_1^2 w_5^2 w_3^2 w_3^3 - 12c s^2 w_5 w_3^2 w_3^3 + 12v_1^2 w_5 w_3^2 w_3^3 + 12c s^2 w_5 w_3^2 w_3^2 + \\ & 6c s^2 w_5^2 w_3^2 w_3^3 - 6v_1^2 w_5^2 w_3^2 w_3^3 - 12c s^2 w_5^2 w_3^2 - 12v_1^2 w_5 w_2 w_3^2 w_3^3 - 36v_1^2 w_5 w_2^2 w_3^2 - 24c s^2 w_5^2 w_2 w_3^2 + 36c s^2 w_5 w_2^2 w_3^2 + 12v_1^2 w_5^2 w_2^2 + 24v_1^2 w_5 w_2^2 w_3^2 - \\ & 6v_1^2 w_5^2 w_2 w_3^2 + 12v_1^2 w_5^2 w_3^2 - 24c s^2 w_5^2 w_2^2 w_3^2 + 36c s^2 w_5^2 w_2 w_3^2 - 12c s^2 w_5^2 w_3^2 \end{aligned}$$

$$C_{41} = 12c^2w_6w_3^2 - 30w_4c^2s^2w_6w_3 + 6w_4v_2^2w_3^3 - 36w_4v_2^2w_6^2w_3 + 12v_2^2w_6^2w_3 - 12w_4v_2^2w_3^2 - 6c^2s^2w_6w_3^3 + 9w_4c^2s^2w_6w_3^2 - 6w_4c^2s^2w_3^3 - v_2^2w_6^2w_3^3 + w_4v_2^2w_6^2w_3^2 - 6v_2^2w_6^2w_3^2 + 8w_4v_2^2w_6^2w_3^2 + 12w_4c^2s^2w_3^2 + 12w_4cs^2w_6w_3 + 30w_4v_2^2w_6w_3^2 - 12v_2^2w_6w_3^2 + 12w_4c^2s^2w_6^2 + 12cs^2w_6^2w_3 - 30w_4c^2s^2w_6w_3 - 9w_4v_2^2w_6w_3^2 + 6v_2^2w_6w_3^3 - 2w_4c^2s^2w_6w_3^3 + 3cs^2w_6w_3^3 + 24w_4v_2^2w_6^2 + 22w_4cs^2w_6w_3^2 - 18c^2s^2w_6w_3^2 - 12w_4v_2^2w_6w_3$$

$$\begin{aligned}
C_{42} = & 2w_3^4 v_2^2 w_3^2 w_6^2 + 2w_3^3 v_2^2 w_3^2 w_6 w_3^2 - 2w_3^4 c s^2 w_3^2 w_6 w_3^3 + w_4 c s^2 w_3^2 w_6^2 w_3^3 + 3v_2^2 w_3^2 w_6^2 w_3^3 - 2w_3^4 c s^2 w_2^2 w_6^2 w_3 - 8w_4 v_2^2 w_3^2 w_6^2 w_3^3 + 3w_4^3 v_2^2 w_2^2 w_6^2 w_3^3 - \\
& 10w_2^2 v_2^2 w_3^2 w_6^2 w_3^2 + 6w_2^4 c s^2 w_3^2 w_6^2 w_3^2 + 4w_4 v_2^2 w_3^2 w_6^2 w_3^2 - 2w_4 c s^2 w_3^2 w_6^2 w_3^2 + 6w_4^3 c s^2 w_3^2 w_6 w_3^2 - 6w_4^3 v_2^2 w_3^2 w_6 w_3^2 - 2w_4 c s^2 w_3^2 w_6^2 w_3^2 + 7w_4^2 v_2^2 w_3^2 w_6^2 w_3^2 + \\
& 3w_4^2 v_2^2 w_2 w_6^2 w_3^2 + w_4^3 c s^2 w_3^2 w_3^2 + 7w_3^4 v_2^2 w_2^2 w_6^2 w_3^2 - 2w_3^4 c s^2 w_2^2 w_6^2 w_3^2 - 2w_3^4 c s^2 w_3^2 w_6 w_3 + 2w_3^4 v_2^2 w_3^2 w_6 w_3 + 3w_4^2 v_2^2 w_3^2 w_6^2 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6^2 w_3^2 + \\
& 6w_3^4 c s^2 w_2^2 w_6^2 w_3^2 - 2w_3^4 c s^2 w_2^2 w_3^2 - 10w_4^3 v_2^2 w_2^2 w_6^2 w_3^2 - 2w_4^3 c s^2 w_3^2 w_6^2 - 8w_4^2 v_2^2 w_2^2 w_6^2 w_3^2 + w_4^2 c s^2 w_2^2 w_6^2 w_3^2 + 2w_4^3 v_2^2 w_2^2 w_6 w_3^2 + w_4^3 c s^2 w_2 w_6^2 w_3^2 - \\
& 2w_4^2 c s^2 w_2^2 w_6 w_3^2 - 8w_4^2 v_2^2 w_2 w_6^2 w_3^2 - 2w_4^2 c s^2 w_2^2 w_6^2 w_3^2 + 4w_4^2 v_2^2 w_2^2 w_6^2 w_3^2 + 4w_4^3 v_2^2 w_2 w_6^2 w_3^2 + w_4^3 c s^2 w_2^2 w_6 w_3^2 - 2w_4^3 c s^2 w_2 w_6^2 w_3^2 - w_4^3 v_2^2 w_2^2 w_6^2 w_3^2 + \\
& 3w_4^2 v_2^2 w_2^2 w_6^2 w_3^2 - 7w_3^4 v_2^2 w_2^2 w_6^2 w_3^2 + 6w_3^4 c s^2 w_3^2 w_6^2 w_3^2 + 3w_4^3 v_2^2 w_3^2 w_6^2 w_3^2 + 8w_3^4 v_2^2 w_3^2 w_6^2 w_3^2 - 6w_4^3 c s^2 w_3^2 w_6^2 w_3^2 - w_4^3 v_2^2 w_3^2 w_6^2 w_3^2 - w_4^2 v_2^2 w_3^2 w_6 w_3^2 + \\
& w_4^2 c s^2 w_3^2 w_6 w_3^2 + w_4^3 c s^2 w_3^2 w_6^2 w_3^2 - 2w_4^3 v_2^2 w_3^2 w_6^2 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6 w_3^2 + 2w_4^2 v_2^2 w_3^2 w_6 w_3^2 + 2w_4^3 v_2^2 w_3^2 w_6^2 w_3^2
\end{aligned}$$

$$\begin{aligned} C_{43} = & 12w_4^3v_2^2w_6w_3 - 24w_4^2c^2s^2w_6^2w_3 - 32w_3^3cs^2w_2^2w_3^2 - 12w_3^4cs^2w_3^2 + 24w_4^2v_2^2w_6w_3^2 - 12w_4^2v_2^2w_6w_3^3 + 4w_4^3cs^2w_6^2w_3^3 + 6w_4^3cs^2w_3^3 + 12w_2^2w_6^2w_3^3 - \\ & 30w_4v_2^2w_6^2w_3^3 - 12w_4^2cs^2w_6^2w_3^3 + 12w_4^3v_2^2w_3^2 + 12w_4^3v_2^2w_6w_3^3 + 36w_3^3cs^2w_6^2w_3^2 + 24w_4v_2^2w_6^2w_3^2 - 36w_4^2v_2^2w_6w_3^2 + 48w_4^2cs^2w_6^2w_3^2 - 6w_4^3v_2^2w_3^2 - \\ & 12w_4^3cs^2w_6w_3 + 16w_4^3v_2^2w_6^2w_3^2 - 24w_4^2cs^2w_6w_3^2 + 12w_4^2cs^2w_6w_3^3 - 5w_4^3v_2^2w_6^2w_3^3 + 6w_4cs^2w_6^2w_3^3 + 24w_4^2v_2^2w_6^2w_3^2 - 12w_3^3cs^2w_6w_3^2 - 6w_4^3v_2^2w_6^2w_3 - \\ & 12w_4cs^2w_6^2w_3^2 - 12w_4^3cs^2w_6^2 + 36w_3^3cs^2w_6w_3^2 - 36w_4^2v_2^2w_6^2w_3^2 \end{aligned}$$

$$\begin{aligned} C_{44} = & 6w_4 w_3^2 w_2^3 - 36w_4^3 w_3^2 w_2 + 24w_4^3 w_2^2 w_3^3 - 30w_4^3 w_2^2 w_3^2 + 12w_4^3 w_2^3 w_3 - 30w_4 w_3^2 w_2^3 + 18w_4^3 w_2^2 w_3 - 5w_4^3 w_2^3 w_3^2 + 18w_4^2 w_2 w_3^3 + 12w_4^3 w_3^2 w_2^3 + \\ & 18w_4 w_2^2 w_3^3 + 28w_4^3 w_2^3 w_3 + 12w_4^2 w_2^2 w_3^2 - 42w_4^2 w_2^2 w_3^3 + 18w_4^2 w_2^3 w_3 + 12w_3^2 w_3^3 + 6w_4^3 w_2 w_3^2 - 30w_4^2 w_2^3 w_3^2 + 24w_4^2 w_2^3 w_3^3 - 30w_4^3 w_2 w_3^2 \end{aligned}$$

$$C_{45} = 12v_2^2w_3^2w_3^2 - 5v_2^2w_3^2w_6^2w_3 + 4cs^2w_3^2w_6^2w_3^3 - 32cs^2w_3^2w_6^2w_3^2 - 6v_2^2w_3^2w_6^2w_3^3 + 16v_2^2w_3^2w_6^2w_3^2 + 12v_2^2w_6^2w_3^3 + 36cs^2w_3^2w_6^2w_3 - 6v_2^2w_3^2w_6^2w_3 - 12v_2^2w_2^2w_6w_3^3 - 12cs^2w_2w_6^2w_3^2 + 12cs^2w_2^2w_6w_3^3 + 24v_2^2w_2w_6^2w_3^2 - 30v_2^2w_2w_6^2w_3^3 - 24cs^2w_2^2w_6w_3^2 + 6cs^2w_2w_6^2w_3^3 - 12cs^2w_3^2w_6^2 + 24v_2^2w_2^2w_6w_3^2 - 12cs^2w_3^2w_6^2w_3^3 - 36v_2^2w_2^2w_6^2w_3^2 + 48cs^2w_2^2w_6^2w_3^3 + 6cs^2w_3^2w_6^2w_3^3 + 12v_2^2w_3^2w_6w_3 - 12cs^2w_3^2w_6w_3 - 12cs^2w_2^2w_6^2w_3^3 + 24v_2^2w_2^2w_6^2w_3^3 - 36v_2^2w_2^2w_6w_3^2 + 36cs^2w_3^2w_6w_3^2 - 24cs^2w_2^2w_6^2w_3 - 12cs^2w_3^2w_6w_3 + 12v_2^2w_3^2w_6w_3^3$$

$$\begin{aligned} C_{46} = & -24w_4^3v_2^2w_6w_3 + 7w_4^3w_6^2w_3^2 - 12w_4^2cs^2w_6^2w_3 - 36w_4^3cs^2w_6^2w_3^2 - 36w_4^3cs^2w_3^2 + 6w_4^3w_3^2 - w_4^3w_6^2w_3^3 - 3w_4^3w_3^3 + 6w_4^3cs^2w_6^2w_3^3 + 18w_4^3cs^2w_3^3 + \\ & 6v_2^2w_6^2w_3^3 - 12w_4v_2^2w_6^2w_3^3 - 12w_4^2cs^2w_6^2w_3^3 + 12w_4^3v_2^2w_3^2 + 6w_4^2w_6w_2^3 + 36w_4^3cs^2w_6^2w_3 + 6w_4v_2^2w_6^2w_3^2 - 6w_4^3w_6^2w_3 + 12w_4^3v_2^2w_6w_3^2 - 3w_4^2w_6w_3^3 + \\ & 36w_4^2cs^2w_6^2w_3^2 - 6w_4^3v_2^2w_3^3 - 24w_4^3cs^2w_6w_3 + 12w_4^3w_6w_3 - 6w_4^3v_2^2w_6^2w_3^2 - 24w_4^2cs^2w_6w_3^2 + w_4^2w_6^2w_3^3 - 3w_4^2w_6^2w_3^2 + 12w_4^2cs^2w_6w_3^3 + 6w_4cs^2w_6^2w_3^2 + \\ & 6w_4^3w_6w_3^3 + 6w_4^2v_2^2w_6^2w_3^2 - 24w_4^3cs^2w_6w_3^2 + 12w_4^3v_2^2w_6^2w_3^2 - 21w_4^3w_6w_3^2 - 12w_4cs^2w_6^2w_3^2 - 12w_4^3cs^2w_6^2 + 72w_4^3cs^2w_6w_3^2 - 6w_4^2v_2^2w_6^2w_3^2 \end{aligned}$$

$$\begin{aligned}
C_{47} = & 12w_4^3v_2^2w_6w_3 + 3w_4^3w_6^2w_3^2 - 24w_4^2cs^2w_6^2w_3 - 32w_3^3cs^2w_6^2w_3^2 - 12w_3^3cs^2w_3^2 - 24w_4^2v_2^2w_6w_3^2 - w_3^3w_6^2w_3^3 + 12w_4^2v_2^2w_6w_3^3 + 4w_4^3cs^2w_6^2w_3^3 + \\
& 6w_4^3cs^2w_3^3 + 12v_2^3w_6^2w_3^3 - 18w_4v_2^2w_6^2w_3^3 - 12w_4^2cs^2w_6^2w_3^3 + 12w_4^3v_2^2w_3^3 + 12w_4^2w_6w_3^3 + 36w_3^3cs^2w_6^2w_3^3 - 12w_3^3v_2^2w_6w_3^2 - 6w_4^2w_6w_3^3 + 48w_4^2cs^2w_6^2w_3^2 - \\
& 6w_4^3v_2^2w_3^3 - 12w_4^3cs^2w_6w_3^3 - 12w_4^3v_2^2w_6^2w_3^3 - 24w_4^2cs^2w_6w_3^2 + 2w_4^2w_6^2w_3^3 - 24w_4^3v_2^2w_6^2 - 6w_4^2w_6^2w_3^3 + 12w_4^2cs^2w_6w_3^3 + 3w_4^3v_2^2w_6w_3^3 + \\
& 6w_4^2cs^2w_6^2w_3^3 + 3w_4^3w_6w_3^3 - 12w_3^3cs^2w_6w_3^3 + 30w_4^3v_2^2w_6^2w_3 - 6w_4^3w_6w_3^2 - 12w_4^2cs^2w_6^2w_3^2 - 12w_4^3cs^2w_6^2w_3^2 + 36w_3^3cs^2w_6w_3^2 + 12w_4^2v_2^2w_6^2w_3^2
\end{aligned}$$

$$C_{48} = 96c^2w_6w_3^2 - 6w_3^3 + 12v_2^2w_6^2w_3 - 36w_6w_3^2 - 30c^2s^2w_6w_3^3 + 9w_6w_3^3 + 12w_3^2 + v_2^2w_6^2w_3^3 + 12v_2^2w_6^2 - 14v_2^2w_6^2w_3^2 + 24w_6w_3 - 36c^2s^2w_6w_3 + 48v_2^2w_6w_3^2 - 6v_2^2w_3^3 - 12w_6^2w_3 + 18c^2s^2w_6^2w_3 + 12v_2^2w_3^2 - 6v_2^2w_6w_3^3 + 30c^2s^2w_3^3 + 4c^2s^2w_6^2w_3^3 - w_6^2w_3^3 - 26c^2s^2w_6^2w_3^2 - 60c^2s^2w_3^2 - 60v_2^2w_6w_3 + 11w_2^2w_3^2$$

$$C_{49} = -12w_7w_2^4v_3^2 - 6w_3^4cs^2w_2 - 30w_7^2w_4cs^2w_2 - 18w_7^2w_4^2cs^2 - 12w_7w_4v_3^2w_2 + 12w_7^2w_4v_3^2 - 12w_7^2v_2^2w_2 + 12w_7^2cs^2w_2 + 8w_7^2w_4^2v_3^2w_2 + 3w_7^2w_3^4cs^2 - 30w_7w_4^2cs^2w_2 + 6w_7w_3^3v_3^2 - 9w_7w_3^4v_2^2w_2 - 2w_7^2w_3^4cs^2w_2 - 36w_7^2w_4v_3^2w_2 + 6w_4^3v_3^2w_2 - w_7^2w_3^4v_3^2 + 12w_7w_4cs^2w_2 - 6w_7w_4^3cs^2 + 12w_4^2cs^2w_2 + 12w_7w_4^2cs^2 + 22w_7^2w_4^2cs^2w_2 - 6w_7^2w_3^2v_3^2 + 24w_7^2v_2^2w_2 + 30w_7w_4^2v_3^2w_2 + 12w_7^2w_4cs^2 + 9w_7w_3^4cs^2w_2 + w_7^2w_3^4v_3^2w_2$$

$$C_{50} = -2w_2^2 w_4^2 c s^2 v_3^2 w_5^2 w_3^2 - 4w_7^2 w_4 c s^2 v_1^2 w_5^2 w_2^2 - 2w_3^2 v_1^2 v_3^2 w_5^2 w_3^2 + 12w_7^2 w_4 v_1^2 v_3^2 w_5^2 w_2^2 + 2w_3^4 c s^2 v_1^2 w_5^2 w_3^2 + 4w_7^2 w_4^3 v_1^2 v_3^2 w_5^2 w_2^2 - 2w_7^2 w_4^2 c s^4 w_5^2 w_3^2 - 4w_7^2 w_4^3 c s^2 v_3^2 w_5^2 w_2^2 - 10w_7^2 w_4^3 v_2^2 w_5^2 w_2^2 - 4w_7^2 c s^2 v_1^2 w_5^2 w_3^2 + 2w_7^2 w_3^2 c s^2 v_1^2 w_5^2 w_2^2 + 4w_7^2 v_2^2 v_3^2 w_5^2 w_3^2 + 10w_7^2 w_3^2 c s^2 v_3^2 w_5^2 w_2^2 + 14w_7^2 w_4^2 v_1^2 v_3^2 w_5^2 w_3^2 -$$

$$\begin{aligned}
& 8w_7^2w_4^2cs^2v_1^2w_5^2w_3 - w_7^2w_4^3cs^2v_1^2w_5w_3^2 + 4w_7^2w_4^3v_1^2v_3^2w_5^2 + 4w_7^2w_4^2cs^4w_5w_2^2 + 2w_7w_3^4cs^2v_3^2w_3^2 + 3w_7w_3^4v_1^2v_3^2w_5w_3^2 - 14w_7^2w_4v_1^2v_3^2w_2^2w_3^2 - \\
& 2w_7w_3^4v_1^2v_3^2w_3^2 + 8w_7w_2^2cs^2v_3^2w_5w_2^2 - 4w_7w_3^4cs^2v_3^2w_2^2 + 10w_7^2w_4cs^2v_1^2w_5^2w_3^2 + 8w_7^2w_4^2cs^2v_1^2w_2^2w_2^2 - 28w_7^2w_4v_1^2v_3^2w_5w_2^2 - 3w_7^2w_4^3cs^2v_3^2w_5w_3^2 + \\
& 12w_7^2w_4^2v_2^2v_3^2w_3^2w_2 - 2w_7^2w_4^3cs^4w_5w_2^2 - 4w_7w_2^2cs^2v_2^2w_5w_2^2 - 4w_7w_4cs^2v_1^2w_5^2w_3^2 + 4w_7w_4v_1^2v_3^2w_5w_2^2 + 4w_7w_4^2v_1^2v_3^2w_5w_2^2 - 4w_7w_4^2cs^2v_1^2w_5^2w_2^2 + \\
& 4w_7w_4cs^4w_5w_2^2 - 4w_7^2w_4cs^2v_2^2w_5w_2^2 - 4w_7w_2^3cs^2v_3^2w_5w_2^2 + 2w_7w_4^2cs^2v_3^2w_5w_2^2 + 4w_7w_3^4cs^4w_5w_2^2 - 2w_7^2w_4cs^4w_2^2w_3^2 + 4w_7w_3^4v_1^2v_3^2w_5w_2^2 + \\
& 10w_7w_4cs^2v_1^2w_5w_3^2 - 10w_7w_4v_1^2v_3^2w_5w_3^2 - w_7^2w_4^3cs^4w_5w_3^2 + 10w_7w_4^2cs^2v_3^2w_2^2w_2^2 - 2w_7w_4v_1^2v_3^2w_5w_2^2 + 2w_7w_4^2cs^2v_1^2w_5w_2^2 + 2w_7w_4^3cs^2v_3^2w_5w_2^2 - \\
& 2w_7w_3^4cs^4w_5w_2^2 - 14w_7^2w_3^4v_1^2v_3^2w_5w_2^2 - 3w_7w_3^4cs^2v_2^2w_5w_2^2 + 3w_7w_3^4v_1^2v_3^2w_5w_3^2 + 4w_7w_3^4v_1^2v_3^2w_5w_2^2 + 4w_7w_4^2cs^4w_5w_2^2 + w_7w_3^4cs^4w_5w_3^2 - \\
& w_7w_4^3cs^2v_3^2w_5w_2^2 - 3w_7w_4^2v_1^2v_3^2w_5w_2^2 - 12w_7w_2^2cs^4w_5w_2^2 + w_7w_3^4cs^2v_1^2w_5w_2^2 - 4w_7w_2^2cs^2v_3^2w_5w_2^2 + 4w_7w_4v_1^2v_3^2w_5w_2^2 - 4w_7w_2^2cs^2v_1^2w_5w_2^2 + \\
& 4w_7^2v_2^2v_3^2w_5w_3^2 + w_7w_3^4cs^2v_3^2w_5w_3^2 - 2w_7w_4^2cs^4w_5w_2^2 - 2w_7w_3^4cs^4w_2^2w_3^2 - 4w_7w_4^2cs^2v_1^2w_5w_3^2 + 2w_7w_4^2cs^2v_3^2w_5w_3^2 - 2w_7^2w_4^3cs^2v_1^2w_5w_2^2 + \\
& 14w_7w_4^3v_1^2v_3^2w_5w_2^2 + 4w_7w_4^2cs^4w_5w_3^2 + 4w_7w_4^2cs^4w_5w_2^2 - 8w_7w_4^3cs^2v_3^2w_5w_2^2 + 2w_7w_4^2cs^2v_1^2w_5w_3^2 - 2w_7w_4^2v_1^2v_3^2w_5w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{51} = & -6w_2^2w_3^4c^2s^2\omega_2^2 + 24w_7w_2^4c^2s^2\omega_3^2 + 22w_7w_2^4v_2^2\omega_3^2 - 12w_2^2c^2s^2\omega_3^2 + w_7^2w_3^4c^2s^2\omega_3^2 + 6w_7w_3^4v_2^3\omega_3^2 - 48w_2^2w_4^2v_2^3\omega_3^2 + 12w_7w_4c^2v_3^2\omega_3^2 + 24w_2^2w_4^2v_3^2\omega_2 + \\
& 24w_2^2w_4c^2s^2\omega_3^2 + 6w_3^4c^2s^2\omega_3^2 + 12w_4^2v_2^3\omega_3^2 + 6w_7w_3^4c^2s^2\omega_2 + 22w_2^2w_3^4v_2^3\omega_2^2 - 24w_7w_2^4v_3^2\omega_3^2 + 12w_2^2w_3^4v_3^2 - 14w_7w_2^4c^2s^2\omega_3^2 - 4w_7^2w_3^3v_2^3\omega_3^2 - \\
& 6w_7w_3^4c^2s^2\omega_3^2 + 12w_7^2w_2^4c^2s^2\omega_2^2 - 12w_7w_2^4c^2s^2\omega_2 - 12w_7w_4c^2s^2\omega_3^2 - 6w_4^2v_3^2\omega_3^2 - 18w_7w_4v_3^2\omega_3^2 - 12w_2^2c^2s^2\omega_3^2 + 24w_7w_4v_3^2\omega_2^2 - 30w_7w_4^2v_3^2\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{52} = & 22w_4^3v_2^2w_5^2w_2^2 - 14w_4^3cs^2w_5^2w_2^2 + 24w_4^2v_1^2w_5^2w_2 + w_4^3cs^2w_5^2w_3^2 - 4w_3^3v_1^2w_5^2w_3^3 + 22w_2^2v_1^2w_5^2w_3^2 - 6w_2^4cs^2w_5^2w_3^3 - 12w_3^4cs^2w_5^2 + 6w_3^4cs^2w_3^2 - \\
& 6w_3^2v_2^2w_3^2 + 12w_2^4cs^2w_5^2w_2^2 - 48w_4^2v_1^2w_5^2w_2^2 + 12w_3^4v_1^2w_2^2 - 18w_3^3v_1^2w_5^2w_2 - 12w_3^4cs^2w_2^2 + 24w_4^3cs^2w_5^2w_2 + 12w_4^3v_1^2w_5^2w_2 - 12w_3^4cs^2w_5^2w_2^2 - \\
& 6w_3^4cs^2w_5^2w_3^2 + 6w_3^4v_1^2w_5^2w_3^2 + 6w_4cs^2w_5^2w_3^2 + 12v_2^2w_5^2w_3^2 - 30w_4v_1^2w_5^2w_3^2 - 24w_3^3v_1^2w_5^2w_2^2 + 24w_4^3cs^2w_5^2w_2^2 + 24w_4v_1^2w_5^2w_2^2 - 12w_4cs^2w_5^2w_2^2
\end{aligned}$$

$$\begin{aligned} C_{53} = & -9\omega_7 w_4^3 v_2^2 w_3 - 12\omega_7 w_4^2 v_3^2 - 18w_7^2 w_4^2 c s^2 - 2w_7^2 w_3^3 c s^2 w_3 + 12w_7^2 c s^2 w_3 + 8w_7^2 w_4^2 v_3^2 w_3 + 12w_7^2 w_4 v_3^2 - 30\omega_7 w_7^2 c s^2 w_3 + 3w_7^2 w_4^3 c s^2 - \\ & - 12w_4^2 v_3^2 w_3 + 6\omega_7 w_3^3 v_3^2 - 6w_3^4 c s^2 w_3 - 30w_7^2 w_4 c s^2 w_3 - 12\omega_7 w_4 v_3^2 w_3 + 9\omega_7 w_4^3 c s^2 w_3 - w_7^2 w_4^3 v_3^2 + w_7^2 w_4^3 w_3 - 6\omega_7 w_4^3 c s^2 + 22w_7^2 w_4^2 c s^2 w_3 + \\ & + 24w_7^2 v_3^2 w_3 + 30\omega_7 w_4^2 v_3^2 w_3 + 12w_7 w_4^2 c s^2 - 6w_7^2 w_4^2 v_3^2 + 12w_4^2 c s^2 w_3 - 36w_7^2 w_4 v_3^2 w_3 + 6w_4^3 v_3^2 w_3 + 12w_7^2 w_4 c s^2 + 12w_7 w_4 c s^2 w_3 \end{aligned}$$

$$\begin{aligned}
C_{54} = & w_2^2 w_3^3 c s^2 w_2 w_3^3 + 3 w_2^7 w_4 v_3^2 w_2^2 w_3^3 - 8 w_2^7 w_4^3 v_3^2 w_2 w_3^3 - 2 w_2^7 w_4 c s^2 w_2^2 w_3^3 + 2 w_2^4 v_3^2 w_2^3 w_3^3 + 3 w_2^4 w_3^3 v_3^2 w_2 w_3^3 - 2 w_2^2 c s^2 w_3^2 w_2^3 - w_3^4 v_3^2 w_2^3 w_3^3 + \\
& 6 w_7^2 w_4 c s^2 w_2^3 w_3^3 + w_4^3 c s^2 w_3^2 w_3^3 - 7 w_7^2 w_4 v_3^2 w_3^2 w_3^3 - 2 w_7^2 w_4^2 c s^2 w_3^2 w_3^3 + 2 w_7 w_4 v_3^2 w_3^2 w_3^3 - 2 w_7^2 w_4 c s^2 w_3^2 w_3^3 + 4 w_7^2 w_4^2 v_3^2 w_2 w_3^3 - 2 w_7 w_4 c s^2 w_3^2 w_3^3 + \\
& 3 w_7^2 w_4 v_3^2 w_2^3 w_3^3 - 2 w_7 w_4^3 c s^2 w_3^2 w_3^3 - 2 w_2^2 w_4^2 c s^2 w_3^2 w_3^3 + 6 w_7^2 w_4^2 c s^2 w_2^2 w_3^3 + 7 w_7^2 w_4^3 v_3^2 w_3^2 w_3^3 + 4 w_7^2 w_4^2 v_3^2 w_3^2 w_3^3 + 2 w_7 w_4^3 v_3^2 w_3^2 w_3^3 - 10 w_7^2 w_4^2 v_3^2 w_2^2 w_3^3 - \\
& 2 w_7 w_4^3 c s^2 w_3^2 w_3^3 + 3 w_2^2 w_4^3 v_3^2 w_3^2 - 2 w_7 w_4^3 c s^2 w_3^2 w_3^3 + 3 w_2^7 w_4^3 v_3^2 w_2^2 w_3 + 2 w_7 w_4^3 v_3^2 w_2^2 w_3^3 - 2 w_7^2 w_4 c s^2 w_2^2 w_3^3 + w_7 w_4^3 c s^2 w_3^2 w_2^2 + w_7^2 w_4^3 c s^2 w_3^2 w_3^3 - \\
& 2 w_7 w_4 c s^2 w_2^3 w_3^3 + 4 w_7^2 w_4^2 v_3^2 w_3^2 w_3^3 - w_7 w_4^3 v_3^2 w_3^2 w_3^3 - 2 w_7 w_4 c s^2 w_3^2 w_3^3 + w_7^2 w_4^3 c s^2 w_2^2 w_3^3 + 3 w_2^2 w_4^3 v_3^2 w_3^2 w_3^3 + 2 w_7^2 v_3^2 w_3^2 w_3^3 - w_7 w_4^3 v_3^2 w_2^2 w_3^3 + \\
& 8 w_7^2 w_4^3 v_3^2 w_2^3 w_3^3 + 2 w_7 w_4^2 v_3^2 w_3^2 w_3^3 - 2 w_2^2 c s^2 w_3^2 w_3^3 - 8 w_2^7 w_4^3 v_3^2 w_2^2 w_3^3 + w_7 w_4^3 c s^2 w_2^2 w_3^3 - 6 w_7^2 w_4 c s^2 w_3^2 w_3^3 - 10 w_7^2 w_4^3 v_3^2 w_3^2 w_3^2 - 2 w_7^2 w_4^3 c s^2 w_2^2 w_3^3 + \\
& w_7^2 w_4^3 c s^2 w_3^2 w_3^3 + 6 w_7 w_4^2 c s^2 w_3^2 w_3^3 + 6 w_7^2 w_4^2 c s^2 w_3^2 w_3^2 + 7 w_7^2 w_4^3 v_3^2 w_2^2 w_3^3 - 6 w_7 w_4^2 v_3^2 w_3^2 w_3^3 - 8 w_2^7 w_4^3 v_3^2 w_2^2 w_3^3
\end{aligned}$$

$$C_{55} = 12w_4^2v_3^2\omega_3^3 + 6w_7^2\omega_3^3cs^2\omega_3 - 24w_7^2w_4cs^2\omega_3^2 + 12w_7w_4v_3^2\omega_3^3 + 24w_7^2w_4^2v_3^2\omega_3 + 36w_7^2w_4cs^2\omega_3^3 + 6w_3^4cs^2\omega_3^3 - 24w_7w_4^2cs^2\omega_3^2 + 4w_7^2w_3^4cs^2\omega_3^3 - 36w_2^2\omega_4^2v_3^2\omega_3^2 + 12w_7w_4^3v_3^2\omega_3^3 + 36w_7w_4^2cs^2\omega_3^3 - 12w_7^2w_4^3cs^2\omega_3^2 + 16w_7^2w_4^2v_3^2\omega_3^3 - 12w_7w_4^3v_3^2\omega_3^2 - 12w_7^2cs^2\omega_3^3 - 12w_4^2cs^2\omega_3^3 + 12w_2^2\omega_4^3v_3^2 - 30w_7^2w_4^3\omega_3^2\omega_3 - 12w_7^2w_4^2cs^2\omega_3^2 - 12w_7w_4cs^2\omega_3^3 - 6w_3^4v_3^2\omega_3^3 - 6w_7^2w_4v_3^2\omega_3^3 + 24w_7w_4^2v_3^2\omega_3^2 - 5w_7^2w_4^3v_3^2\omega_3^3 + 48w_7^2w_4^2cs^2\omega_3^2 - 12w_7w_4^3cs^2\omega_3^3 - 36w_7w_4^2v_3^2\omega_3^3 + 24w_7^2w_4^3v_3^2\omega_3^2 - 32w_7^2w_4^2cs^2\omega_3^3 + 12w_7w_4^3cs^2\omega_3^2$$

$$\begin{aligned}
C_{56} = & -12w_7^2w_3^4cs^2w_2^2 + 36w_7w_4^2cs^2w_3^2 - 12w_7w_3^4v_3^2w_2^2 + 16w_7^2w_4^2v_3^2w_3^2 - 12w_7^2cs^2w_3^3 + 4w_7^2w_3^4cs^2w_3^3 - 24w_7w_4^2cs^2w_2^2 + 12w_7w_4^3v_3^2w_3^2 - \\
& 36w_7^2w_4^2v_3^2w_2^2 + 12w_7w_4v_3^2w_3^2 + 24w_7w_2^2v_3^2w_2 + 36w_7^2w_4cs^2w_3^2 + 6w_4^3cs^2w_3^2 + 12w_4^2v_3^2w_3^2 + 6w_2^2w_4^3cs^2w_2 - 24w_7^2w_4cs^2w_2^2 + 24w_7w_3^3v_3^2w_2^2 - \\
& 36w_7w_4^2v_3^2w_2^3 + 12w_7w_3^3v_3^2 + 12w_7w_4^3cs^2w_2^2 - 32w_7^2w_4^2cs^2w_3^2 - 5w_7w_3^3v_3^2w_2^3 + 24w_7w_4^2v_3^2w_2^2 - 12w_7w_4^3cs^2w_3^2 + 48w_7w_4^2cs^2w_2^2 - 12w_7^2w_4^2cs^2w_2 - \\
& 12w_7w_4cs^2w_3^2 - 6w_4^3v_3^2w_2^3 - 6w_7^2w_4v_3^2w_3^2 - 12w_4^2cs^2w_3^2 - 30w_7w_4^3v_3^2w_2
\end{aligned}$$

$$C_{57} = 18w_4w_3^2w_2^3 - 30w_4^3w_3^2w_3 + 24w_4^2w_2^2w_3^3 - 42w_4^3w_2^2w_3^2 + 12w_3^4w_3^3 - 36w_4w_3^2w_3^3 + 18w_4^3w_2^2w_3 + 18w_4^2w_2w_3^3 + 24w_4^3w_2^3w_3 + 12w_2^4w_2^2w_3^2 - 30w_2^2w_2^3w_3^3 + 6w_2^4w_3^2w_3 + 12w_3^2w_3^3 + 18w_4^3w_2w_2^3 - 30w_2^2w_3^2w_3^3 + 28w_4^2w_3^2w_3^3 - 30w_3^4w_2w_3^3$$

$$\begin{aligned}
C_{58} = & 12w_7^2w_4v_2^2v_3^2w_6^2w_3^2 - 2w_3^3v_2^2v_3^2w_6^2w_3^3 + 4w_2^2v_2^2v_3^2w_6^2w_3^3 + 10w_7^2w_3^4cs^2v_3^2w_6w_3^2 - 8w_7^2w_4^2v_3^2cs^2w_6^2w_3^3 - 10w_7^2w_3^4v_2^2v_3^2w_6w_3^2 - 2w_7^2w_4^2cs^4w_6w_3^3 - \\
& 4w_7^2w_4v_2^2cs^2w_6^2w_3^3 + 4w_7^2w_3^4v_2^2v_3^2w_6^3 + 2w_3^4v_3^2cs^2w_6^2w_3^3 - 4w_7^2v_2^2cs^2w_6^2w_3^3 - 2w_7^2v_4^2cs^2v_3^2w_6^2w_3^3 + 2w_7^2w_3^4v_2^2cs^2w_6w_3^3 + 14w_7^2w_4^2v_2^2v_3^2w_6^2w_3^3 + \\
& 3w_7^2w_3^4v_2^2v_3^2w_6w_3^3 + 8w_7^2w_4^2v_2^2cs^2w_6^2w_3^3 - 3w_7^2w_3^4cs^2v_3^2w_6w_3^3 - 14w_7^2w_4v_2^2v_3^2w_6^2w_3^3 - 28w_7^2v_4^2v_2^2v_3^2w_6^2w_3^2 - w_7^2w_3^4v_2^2cs^2w_6w_3^3 + 8w_7^2w_4^2cs^2v_3^2w_6^2w_3^3 + \\
& 10w_7^2w_4v_2^2cs^2w_6^2w_3^3 + 4w_7^2w_4^2cs^4w_6w_3^3 + 4w_7^2w_4cs^4w_6^2w_3^3 + 2w_7^2w_4^2cs^2v_3^2w_6^2w_3^3 + 12w_7^2w_4^2v_2^2v_3^2w_6^2w_3^3 - 4w_7^2w_4^2v_2^2cs^2w_6^2w_3^3 - 4w_7^2w_4^2cs^2v_3^2w_6^2w_3^3 + \\
& 4w_7w_4v_2^2v_3^2w_6^2w_3^3 - 2w_7^2w_4^2cs^4w_6w_3^3 - 4w_7w_4v_2^2v_3^2w_6^2w_3^3 + 4w_7w_4v_2^2v_3^2w_6^2w_3^2 - 4w_7w_4v_2^2cs^2w_6^2w_3^3 + 10w_7w_4^2v_2^2cs^2w_6^2w_3^3 - 4w_7^2w_3^4cs^2v_3^2w_3^3 - \\
& 2w_7^2w_4cs^4w_6w_3^3 - 10w_7^2v_4^2v_2^2v_3^2w_6w_3^3 - 4w_7^2w_3^4cs^2v_3^2w_6w_3^3 + 2w_7^2w_4^2cs^2v_3^2w_6w_3^3 + 4w_7^2w_3^4v_2^2v_3^2w_6w_3^3 - 2w_7w_4^2cs^4w_6w_3^3 + \\
& 2w_7w_3^4cs^2v_3^2w_6^2w_3^2 - 2w_7w_4^2v_2^2v_3^2w_6^2w_3^2 - 4w_7^2w_3^4cs^2v_3^2w_6^2w_3^2 - 14w_7^2v_4^2v_2^2v_3^2w_6^2w_3^2 - w_7^2w_3^4cs^4w_6^2w_3^3 + 10w_7w_4^2v_3^2w_6^2w_3^3 + 2w_7w_4^2v_2^2cs^2w_6^2w_3^2 + \\
& 3w_7w_4^2v_2^2v_3^2w_6^2w_3^3 - w_7w_4^2cs^2v_3^2w_6^2w_3^3 + 4w_7^2w_4^2cs^2w_6^2w_3^3 + w_7w_4^2cs^2v_3^2w_6^2w_3^2 - 3w_7w_4^2v_2^2v_3^2cs^2w_6^2w_3^3 + 4w_7^2w_3^4cs^4w_6^2w_3^2 + w_7^2w_3^4cs^2v_3^2w_6^2w_3^2 - \\
& 2w_7w_3^4v_2^2v_3^2w_6^2w_3^3 - 3w_7w_3^4v_2^2v_3^2w_6^2w_3^2 - 2w_7w_4^2cs^4w_6^2w_3^3 - 2w_7w_3^4cs^4w_6^2w_3^2 - 4w_7^2w_2^2v_2^2cs^2w_6^2w_3^3 - 4w_7^2w_4^2v_2^2cs^2v_3^2w_6^2w_3^2 + \\
& 4w_7w_2^2v_2^2v_3^2w_6w_3^2 + w_7w_4^2v_2^2v_3^2cs^2w_6^2w_3^3 - 12w_7w_2^2w_4^2cs^4w_6^2w_3^3 + 4w_4^2v_2^2v_3^2w_6^2w_3^3 + 2w_7w_4^2v_2^2cs^2w_6w_3^3 + 4w_7w_4^2cs^4w_6^2w_3^3 + 14w_7^2w_3^4v_2^2v_3^2w_6^2w_3^2 - \\
& 8w_7w_3^4cs^2v_3^2w_6^2w_3^3 + 4w_7w_4^2w_3^4v_2^2v_3^2w_3^3 + 4w_7^2w_4^2v_3^4w_6^2w_3^3 - 2w_7w_4^2v_2^2v_3^2w_6w_3^3 + 2w_7w_4^2v_2^2cs^2v_3^2w_6w_3^3
\end{aligned}$$

$$C_{59} = 12w_4^2v_3^2w_3^3 + 6w_7^2w_4^3cs^2w_3 + 12w_7w_4v_3^2w_3^3 + 24w_7^2w_2^2v_3^2w_3 + 24w_7^2w_4cs^2w_3^3 + 6w_4^3cs^2w_3^3 + w_7^2w_3^3cs^2w_3 - 48w_2^2w_4v_3^2w_3^2 + 6w_7w_3^4v_3^2w_3^3 + 24w_7w_4^2cs^2w_3^3 - 6w_7w_3^2cs^2w_3^2 + 22w_2^2w_4^2v_3^2w_3^3 - 12w_7^2cs^2w_3^3 - 12w_4^2cs^2w_3^3 + 24w_7^2w_4v_3^2w_3^2 + 12w_7^2w_4^3v_3^2 - 30w_7w_3^2v_3^2w_3 - 12w_7w_4^2cs^2w_3 - 12w_7w_4cs^2w_3^3 - 6w_4^3v_3^2w_3^3 - 18w_7^2w_4v_3^2w_3^3 - 4w_7w_4^3v_3^2w_3^3 + 12w_7^2w_4^2cs^2w_3^2 - 6w_7w_4^3cs^2w_3^3 - 24w_7w_4^2v_3^2w_3^3 + 22w_7^2w_4^3v_3^2w_3^2 - 14w_7^2w_4^2cs^2w_3^3$$

$$\begin{aligned} C_{60} = & 12w_4^3v_2^2w_6w_3 - 14w_4^3c^2s^2w_6^2w_3^2 - 12w_3^3c^2s^2w_3^2 + w_3^3c^2s^2w_6^2w_3^3 + 6w_3^3c^2s^2w_3^3 + 12w_2^2s^2w_6^2w_3^3 - 30w_4v_2^3w_6^2w_3^3 - 6w_4^2c^2s^2w_6^2w_3^3 + 12w_4^3v_2^2w_3^2 + \\ & 6w_4^3v_2^2w_6w_3^3 + 24w_4^3c^2s^2w_6^2w_3 + 24w_4v_2^2w_6^2w_3^2 - 24w_4^3v_2^2w_6w_3^3 + 12w_4^2c^2s^2w_6^2w_3^2 - 6w_4^3v_2^2w_3^3 - 12w_4^3c^2s^2w_6w_3 + 24w_4^2v_2^2w_6^2w_3 + 22w_3^3v_2^2w_6^2w_3^2 - \\ & 4w_4^3v_2^2w_6^2w_3^3 + 6w_4c^2s^2w_6^2w_3^3 + 22w_4^2v_2^2w_6^2w_3^3 - 6w_4^3c^2s^2w_6w_3^3 - 18w_3^3v_2^2w_6^2w_3^3 - 12w_4c^2s^2w_6^2w_3^3 + 24w_4^3c^2s^2w_6w_3^2 - 48w_4^2v_2^2w_6^2w_3^2 \end{aligned}$$

$$C_{61} = -108w_7w_2^2v_3^2 - 36w_7^2v_2^2 + 25w_7^2w_4^2cs^2 - 24w_7w_4 + 24w_7w_4cs^2 - 18w_3^2v_3^2 + 18w_7^2w_4v_2^2 - 9w_7w_4^3 - 2w_7^2w_4^3cs^2 + 27w_7w_4^3v_3^2 + 36w_4^2v_3^2 + 36w_7w_4^2 - 3w_7^2w_3^2v_3^2 - 12w_4^2 + 9w_7w_4^3cs^2 - 11w_7^2w_4^2 + 6w_4^3 + 12w_4^2cs^2 + w_7^2w_4^3 - 36w_7w_4^2cs^2 + 15w_7^2w_4^2v_3^2 + 24w_7^2cs^2 + 72w_7w_4v_2^2 + 12w_7^2w_4 - 48w_7^2w_4cs^2 - 6w_4^3cs^2$$

$$\begin{aligned}
C_{62} = & -12w_7^2w_3^4cs^2w_2^2 + 72w_7w_4^2cs^2w_3^2 + 6w_4^2w_3^2 - 3w_7w_4^3w_2^2 - 6w_7^2w_4^2v_3^2w_3^2 - 12w_7^2cs^2w_3^2 + 6w_7w_3^3w_2^3 + 6w_2^2w_3^4cs^2w_2^2 - \\
& 6w_7w_4^2v_3^2w_2^2 - 24w_7w_4v_3^2w_3^2 + 6w_7^2w_4^2v_3^2w_2 + 6w_7w_4^2v_2^2 + 36w_7^2w_4cs^2w_3^2 - 3w_3^3w_2^3 - 6w_7^2w_4w_3^2 + 18w_4^3cs^2w_3^2 + 12w_4^2v_3^2w_3^2 + 6w_7^2w_4^3cs^2w_2 - \\
& 21w_7w_4^2w_3^2 - 12w_7^2w_4cs^2w_2^2 + 6w_7^2w_4^3v_3^2w_2^2 + 12w_7w_4^2v_3^2w_3^2 + 6w_7^2w_4v_3^2 + 12w_7w_4w_3^2 + 12w_7w_3^4cs^2w_2^2 - 3w_7^2w_4^2w_2^2 - 36w_7w_4^2cs^2w_3^2 + 7w_7^2w_4^3w_3^2 - \\
& 24w_7w_4^3cs^2w_3^2 + 36w_7^2w_4^2cs^2w_2^2 - 12w_7^2w_4^2cs^2w_2 + w_7^2w_4^3w_2^2 - 24w_7w_4cs^2w_2^3 - 6w_3^2v_3^2w_3^2 + 12w_7^2w_4v_3^2w_3^2 - w_7^2w_4^3w_3^2 - 36w_7^2w_4^2cs^2w_3^2 - 12w_7^2w_4^3v_3^2w_2
\end{aligned}$$

$$\begin{aligned} \textcolor{red}{C_{63}} = & 48w_7w_4^2v_3^2 + 12w_7^2v_3^2 - 26w_7^2w_4^2cs^2 + 24w_7w_4 - 36w_7w_4cs^2 - 6w_3^3v_3^2 + 12w_7^2w_4v_3^2 + 9w_7w_4^3 + 4w_2^2w_4^3cs^2 - 6w_7w_4^3v_3^2 + 12w_2^2v_3^2 - 36w_7w_4^2 + \\ & w_7^2w_4^3v_3^2 + 12w_4^2 - 30w_7w_4^3cs^2 + 11w_7^2w_4^2 - 6w_4^3 - 60w_4^2cs^2 - w_7^2w_4^3 + 96w_7w_4^2cs^2 - 14w_7^2w_4^3v_3^2 - 60w_7w_4v_3^2 - 12w_7^2w_4 + 18w_7^2w_4cs^2 + 30w_4^3cs^2 \end{aligned}$$

$$\begin{aligned}
C_{64} = & -12w_7^2w_4^3cs^2w_2^2 + 36w_7w_4^2cs^2w_3^2 - 6w_7w_4^3w_2^2 + 12w_7w_4^3v_3^2w_2^2 - 12w_7w_2^2v_3^2w_3^2 - 12w_7^2cs^2w_3^2 + 3w_7w_3^4w_3^2 + 4w_7^2w_3^4cs^2w_2^2 - 24w_7w_4^2cs^2w_2^2 + \\
& 12w_7w_4^2v_3^2w_2^2 + 12w_7w_4v_3^2w_3^2 + 12w_7w_4^2w_2^2 + 36w_7^2w_4cs^2w_3^2 + 6w_7^3cs^2w_2^2 + 12w_4^2v_3^2w_3^2 + 6w_7^2w_3^4cs^2w_2 - 6w_7w_4^2w_2^2 - 24w_7^2w_4cs^2w_2^2 - \\
& 12w_7w_4^2v_3^2w_3^2 - 24w_7^2v_3^2w_3^2 + 12w_7^2w_4^3v_3^2 + 12w_7w_4^3cs^2w_2^2 - 6w_7w_4^2w_2^2 - 32w_7^2w_4^2cs^2w_3^2 + 3w_7w_4^2v_3^2w_3^2 - 24w_7w_4^2v_3^2w_2^2 + 3w_7^2w_4^2w_3^2 - \\
& 12w_7w_4^3cs^2w_3^2 + 48w_7^2w_4cs^2w_2^2 - 12w_7^2w_4^2cs^2w_2 + 2w_7^2w_4^3w_2^2 - 12w_7w_4cs^2w_3^2 - 6w_4^3v_3^2w_3^2 + 30w_7w_4v_3^2w_3^2 - w_7^2w_4^3w_3^2 - 12w_4^2cs^2w_3^2 - 18w_7^2w_4^3v_3^2w_2
\end{aligned}$$

$$\begin{aligned}
C_{65} = & 12w_4^2v_3^2w_3^3 + 6w_7^2w_3^3cs^2w_3 - 12w_7^2w_4cs^2w_3^2 - 21w_7w_2^2w_3^3 - 24w_7w_4v_2^2w_3^3 + 6w_7^2w_4^2v_3^2w_3 - 6w_7^2w_4w_3^3 + 36w_7^2w_4cs^2w_3^3 - 3w_4^3w_3^3 + 6w_7w_4^2w_3^3 + \\
& 18w_4^3cs^2w_3^3 + 6w_7w_4^3w_3^3 - 24w_7w_4^2cs^2w_3^2 + 6w_2^2w_4^3cs^2w_3^3 - 6w_2^2w_4^2v_3^2w_3^2 + 72w_7w_4^2cs^2w_3^3 - 12w_2^2w_4^3cs^2w_3^2 - 3w_7w_4^3w_3^2 + 6w_2^2w_3^3 - 6w_7w_4^2v_3^2w_3^3 - \\
& 12w_2^2cs^2w_3^3 - 36w_4^2cs^2w_3^3 - w_7^2w_3^4w_3^3 + 6w_7^2w_4^3v_3^2 - 12w_2^2w_4^3v_3^2w_3 + w_7^2w_3^4w_3^2 - 12w_7^2w_4^2cs^2w_3 - 24w_7w_4cs^2w_3^3 - 6w_4^2v_3^2w_3^3 + 12w_7^2w_4v_3^2w_3^3 + \\
& 36w_7^2w_4^2cs^2w_3^2 + 7w_2^2w_4^2w_3^3 - 24w_7w_4^3cs^2w_3^3 + 12w_7w_4^2v_3^2w_3^3 + 6w_7^2w_4^3v_3^2w_3^2 - 36w_7^2w_4^2cs^2w_3^3 + 12w_7w_4^3cs^2w_3^2 - 3w_7^2w_4^2w_3^3 + 12w_7w_4w_3^3
\end{aligned}$$

$$\begin{aligned} \textcolor{red}{C_{66}} = & 48w_7w_4^2v_3^2 + 12w_7^2v_3^2 - 26w_7^2w_4^2cs^2 + 24w_7w_4 - 36w_7w_4cs^2 - 6w_3^3v_3^2 + 12w_7^2w_4v_3^2 + 9w_7w_3^4 + 4w_7^2w_4^3cs^2 - 6w_7w_3^2v_3^2 + 12w_2^2v_3^2 - 36w_7w_4^2 + \\ & w_7^2w_3^4v_3^2 + 12w_4^2 - 30w_7w_4^3cs^2 + 11w_7^2w_4^2 - 6w_4^3 - 60w_4^2cs^2 - w_7^2w_3^4 + 96w_7w_4^2cs^2 - 14w_7^2w_4v_3^2 - 60w_7w_4v_3^2 - 12w_7^2w_4 + 18w_7^2w_4cs^2 + 30w_4^3cs^2 \end{aligned}$$

$$\begin{aligned}
C_{67} = & 12w_4^2v_3^2w_3^3 + 6w_7^2w_4^3cs^2w_3 - 24w_7^2w_4cs^2w_3^2 - 6w_7w_4^2w_3^3 + 12w_7w_4v_3^2w_3^3 + 36w_7^2w_4cs^2w_3^3 + 12w_7w_4^2w_3^2 + 6w_4^3cs^2w_3^3 + 3w_7w_4^3w_3^3 - \\
& 24w_7w_4^2cs^2w_3^2 + 4w_7w_4^3cs^2w_3^3 + 12w_7^2w_4^2v_3^2w_3^3 + 36w_7w_4^2cs^2w_3^3 - 12w_7^3w_4^3cs^2w_3^2 - 6w_7w_4^3w_3^2 - 12w_7^2w_4^2v_3^2w_3^3 + 12w_7w_4^3v_3^2w_3^2 - 12w_7^2cs^2w_3^3 - \\
& 12w_4^2cs^2w_3^3 - w_7^2w_3^3w_3^3 + 12w_7^2w_3^3v_3^2 - 18w_7w_4^3v_3^2w_3 + 2w_7^2w_4^2w_3^2 - 12w_7^2w_4^2cs^2w_3 - 12w_7w_4cs^2w_3^2 - 6w_4^3v_3^2w_3^3 + 30w_7^2w_4v_3^2w_3^3 - 24w_7w_4^2v_3^2w_3^2 + \\
& 3w_7w_4^3v_3^2w_3^3 + 48w_7^2w_4^2cs^2w_3^2 + 3w_7^2w_4^2w_3^3 - 12w_7w_4^3cs^2w_3^3 - 12w_7w_4^2v_3^2w_3^3 - 24w_7^2v_3^2w_3^3 - 32w_7^2w_4^2cs^2w_3^2 + 12w_7w_4^3cs^2w_3^2 - 6w_7^2w_4^2w_3^2
\end{aligned}$$

$$\begin{aligned} C_{68} = & -72\omega_7^2\omega_4^2v_3^2 - 8\omega_7^2\omega_4^2cs^2 - 24\omega_7\omega_4^2cs^4 - 12\omega_7^2\omega_4^2v_3^4 + 24\omega_7^2cs^4 + 108\omega_4^3cs^2v_3^2 - 24\omega_7\omega_4cs^2 - 36\omega_7^2\omega_4cs^2v_3^2 - 36\omega_4^3v_3^2 - 48\omega_7^2\omega_4cs^4 + 3\omega_7^2\omega_4^3v_3^4 + \\ & 6\omega_7\omega_4^3cs^4 + 6\omega_7^2\omega_4^3cs^2v_3^2 + \omega_7^2\omega_4^3cs^2 + 30\omega_7\omega_4^2v_3^2 + 72\omega_4^2v_3^2 + 144\omega_7\omega_4^2cs^2v_3^2 - 3\omega_7^2\omega_4^3cs^4 - 30\omega_7\omega_4^3v_3^2 - 3\omega_7^2\omega_4^3v_3^2 - 216\omega_4^2cs^2v_3^2 - 6\omega_7\omega_4^3cs^2 - \\ & 72\omega_4^2v_3^4 + 72\omega_7\omega_4cs^2v_3^2 + 24\omega_7\omega_4^2cs^2 + 12\omega_7^2\omega_4^2v_3^2 - 72\omega_7\omega_4^2cs^2v_3^2 + 72\omega_7\omega_4^2v_3^4 + 24\omega_7^2\omega_4^2cs^4 - 12\omega_7^2\omega_4^2cs^2v_3^2 + 12\omega_7^2\omega_4cs^2 + 24\omega_7\omega_4cs^4 + 36\omega_4^3v_3^4 \end{aligned}$$

$$\begin{aligned}
C_{69} = & 24w_7w_4^2v_3^2 - 12w_7^2v_3^2 - 2w_7^2w_4^2cs^2 - 12w_7w_4 - 12w_7w_4cs^2 + 42w_4^3v_3^2 - 12w_7^2w_4v_3^2 + 12w_7w_3^4 + w_7^2w_4^3cs^2 - 24w_7w_3v_3^2 - 84w_4^2v_3^2 - 24w_7w_4^2 + \\
& 2w_7^2w_4^3v_3^2 + 36w_4^2 - 24w_7w_4^3cs^2 + 2w_7^2w_4^2 - 18w_4^3 - 60w_4^2cs^2 - w_7^2w_4^3 + 72w_7w_4^2cs^2 + 2w_7^2w_4^2v_3^2 + 24w_7cs^2 + 60w_7w_4v_3^2 + 6w_7^2w_4 - 30w_7^2w_4cs^2 + 30w_4^3cs^2
\end{aligned}$$

## 2.5 CLBM2

### 2.5.1 Definitions

Collision operator  $C$ :

$$C(f) = \mathbf{K}^{-1} \mathbf{S} \left( \boldsymbol{\kappa}^{(eq)} - \mathbf{K} f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2).$$

Matrix  $\mathbf{K}$  corresponds to the transformation matrix to the central moment basis defined by

$$\kappa = \begin{pmatrix} k_{(0,0,0)} \\ k_{(1,0,0)} \\ k_{(0,1,0)} \\ k_{(0,0,1)} \\ k_{(2,0,0)} + k_{(0,2,0)} + k_{(0,0,2)} \\ k_{(2,0,0)} - k_{(0,2,0)} \\ k_{(2,0,0)} - k_{(0,0,2)} \end{pmatrix},$$

Thus, the transformation matrix  $\mathbf{K}$  satisfies

$$\begin{aligned}\mathbf{K}_{1,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,0)}, \\ \mathbf{K}_{2,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,0)}, \\ \mathbf{K}_{3,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,0)}, \\ \mathbf{K}_{4,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,1)}, \\ \mathbf{K}_{5,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,0,2)}, \\ \mathbf{K}_{6,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,0)}, \\ \mathbf{K}_{7,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,0,2)},\end{aligned}$$

$\forall i \in \{1, 2, \dots, 7\}$ .

The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{KM}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left( \rho, 0, 0, 0, 3\rho c_s^2, 0, 0 \right)^T.$$

### 2.5.2 Conservation of mass equation

attached text file: `output_d3q7_ade_clbm2_symbolic_pde_00.txt`

$$\begin{aligned}& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\& (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\omega_2 \delta_t} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\& (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{\rho \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\& (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{\rho \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + \\& + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho \delta_l^2}{2\omega_3 \delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\& + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{\rho \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + \\& (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_3 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + \\& (-2 + \omega_4) \frac{\rho \delta_l^2}{2\omega_4 \delta_t} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\rho \delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{cs^2 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho \delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + \\& + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\& (-2 + \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho \delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3 v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\& (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_3 v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + \\& (-2 + \omega_4) \frac{cs^2 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{v_3 \rho \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + (12 + \omega_2^2 - 12\omega_2) \frac{\rho \delta_l \delta_t}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_2^2 - 12\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_2^2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + \\& C_1 \frac{v_1 \delta_l^3}{6\omega_5 \omega_2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\rho \delta_l^3}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + (12 + \omega_2^2 - 12\omega_2) \frac{\rho \delta_l \delta_t}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + \\& (3\omega_3^2 - 6\omega_2 + 9\omega_2 \omega_3 - 6\omega_3 - 2\omega_2 \omega_3^2) \frac{v_2 \rho \delta_l^2}{6\omega_2 \omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + (3\omega_2^2 - 2\omega_2^2 \omega_3 - 6\omega_2 + 9\omega_2 \omega_3 - 6\omega_3) \frac{v_1 \rho \delta_l^2}{6\omega_2^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + \\& C_3 \frac{v_2 \delta_l^3}{2\omega_5 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (6\omega_2^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + (-12cs^2 \omega_5 - 12cs^2 \omega_2 + 6cs^2 \omega_2^2 + \\& 12v_1^2 \omega_2 - 3cs^2 \omega_5 \omega_2^2 + 6v_1^2 \omega_5 \omega_2 - 12v_1^2 \omega_5 + v_1^2 \omega_5 \omega_2^2 + 18cs^2 \omega_5 \omega_2 - 6v_1^2 \omega_2^2) \frac{\rho \delta_l^3}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_2} +\end{aligned}$$

$$\begin{aligned}
& (12 + \omega_3^2 - 12\omega_3) \frac{v_2\rho\delta_l^2}{6\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1\delta_l^3}{2\omega_2^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (6v_2^2\omega_6\omega_3 + 6cs^2\omega_3^2 - 12cs^2\omega_3 - 12v_2^2\omega_6 + v_2^2\omega_6\omega_3^2 + 12v_2^2\omega_3 - 3cs^2\omega_6\omega_3^2 - 12cs^2\omega_6 + 18cs^2\omega_6\omega_3 - 6v_2^2\omega_3^2) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& + (6\omega_2^2 + \omega_2^2\omega_3^2 - 6\omega_2^2\omega_3 + 6\omega_3^2 - 6\omega_2\omega_3^2) \frac{v_2v_1\rho\delta_l^3}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2\delta_l^3}{6\omega_6\omega_3\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\rho\delta_l\delta_t}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-6\omega_4 + 9\omega_4\omega_2 - 6\omega_2 - 2\omega_4^2\omega_2 + 3\omega_4^2) \frac{v_3\rho\delta_l^2}{6\omega_4^2\omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (3\omega_2^2 - 2\omega_4\omega_2^2 - 6\omega_4 + 9\omega_4\omega_2 - 6\omega_2) \frac{v_1\rho\delta_l^2}{6\omega_4\omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3\delta_l^3}{2\omega_4^2\omega_5\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (6\omega_2^2 - 6\omega_4\omega_2^2 - 6\omega_4^2\omega_2 + 6\omega_4^2 + \omega_4^2\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_2^2 \partial x_3} + (-12cs^2\omega_5 - 12cs^2\omega_2 + 6cs^2\omega_2^2 + 12v_1^2\omega_2 - 3cs^2\omega_5\omega_2^2 + \\
& 6v_1^2\omega_5\omega_2 - 12v_1^2\omega_5 + v_1^2\omega_5\omega_2^2 + 18cs^2\omega_5\omega_2 - 6v_1^2\omega_2^2) \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (9\omega_4\omega_3 - 6\omega_4 - 6\omega_3 + 3\omega_4^2 - 2\omega_4^2\omega_3) \frac{v_3\rho\delta_l^2}{6\omega_4^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (9\omega_4\omega_3 - 6\omega_4 + 3\omega_3^2 - 2\omega_4\omega_3^2 - 6\omega_3) \frac{v_2\rho\delta_l^2}{6\omega_4\omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_4\omega_2\omega_3^2 + \omega_2^2\omega_3^2 + \omega_4^2\omega_2^2\omega_3^2 - 2\omega_4^2\omega_2^2\omega_3 + \omega_4^2\omega_3^2 + \omega_4\omega_2^2\omega_3 + \omega_4^2\omega_2\omega_3 - 2\omega_4^2\omega_2\omega_3^2 - 2\omega_4\omega_2^2\omega_3^2 + \omega_4^2\omega_2^2) \frac{2v_3v_2v_1\delta_l^3}{\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\
& + (6\omega_4\omega_3 + 3\omega_3^2 - 6\omega_4\omega_3^2 + 2\omega_4^2\omega_3^2 + 3\omega_4^2 - 6\omega_4^2\omega_3) \frac{v_3v_2\rho\delta_l^3}{3\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (3\omega_2^2 - 6\omega_4\omega_2^2 + 6\omega_4\omega_2 - 6\omega_4^2\omega_2 + 3\omega_4^2 + 2\omega_4^2\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{3\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (3\omega_2^2 + 2\omega_2^2\omega_3^2 - 6\omega_2^2\omega_3 + 3\omega_3^2 + 6\omega_2\omega_3 - 6\omega_2\omega_3^2) \frac{v_2v_1\rho\delta_l^3}{3\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_4^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (6\omega_3^2 - 6\omega_4\omega_3^2 + \omega_4^2\omega_3^2 + 6\omega_4^2 - 6\omega_4^2\omega_3) \frac{v_3v_2\omega_2^2\delta_t}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& (6v_2^2\omega_6\omega_3 + 6cs^2\omega_3^2 - 12cs^2\omega_3 - 12v_2^2\omega_6 + v_2^2\omega_6\omega_3^2 + 12v_2^2\omega_3 - 3cs^2\omega_6\omega_3^2 - 12cs^2\omega_6 + 18cs^2\omega_6\omega_3 - 6v_2^2\omega_3^2) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& + (12 - 12\omega_4 + \omega_4^2) \frac{v_3\rho\delta_l^2}{6\omega_4^2} \frac{\partial^3 v_3}{\partial t \partial x_3} + C_9 \frac{v_1\delta_l^3}{2\omega_7\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (6\omega_4^2cs^2 + \omega_7\omega_4^2v_3^2 - 3\omega_7\omega_4^2cs^2 - 6\omega_4^2v_3^2 + 6\omega_7\omega_4v_3^2 - 12\omega_4cs^2 + 12\omega_4v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_7v_3^2 - 12\omega_7cs^2) \frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& + (6\omega_2^2 - 6\omega_4\omega_2^2 - 6\omega_4^2\omega_2 + 6\omega_4^2 + \omega_4^2\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + C_{10} \frac{v_2\delta_l^3}{2\omega_7\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& (6\omega_4^2cs^2 + \omega_7\omega_4^2v_3^2 - 3\omega_7\omega_4^2cs^2 - 6\omega_4^2v_3^2 + 6\omega_7\omega_4v_3^2 - 12\omega_4cs^2 + 12\omega_4v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_7v_3^2 - 12\omega_7cs^2) \frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& + (6\omega_3^2 - 6\omega_4\omega_3^2 + \omega_4^2\omega_3^2 + 6\omega_4^2 - 6\omega_4^2\omega_3) \frac{v_3v_2\rho\delta_l^3}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3\delta_l^3}{6\omega_7\omega_4\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2 - \omega_2^2 + 3\omega_2) \frac{\rho\delta_l\delta_t}{2\omega_2^3} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-2 - \omega_2^2 + 3\omega_2) \frac{3v_1\rho\delta_l^2\delta_t}{2\omega_2^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\rho\delta_l^3}{12\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_4^4}{24\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{v_1\rho\delta_l^4}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3\omega_3) \frac{\rho\delta_l\delta_t^2}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (12\omega_2^2 + 13\omega_2^2\omega_3^2 - \omega_2^2\omega_3^3 - 6\omega_3^3 - 24\omega_2^2\omega_3 + 12\omega_3^2 + 12\omega_2\omega_3 + 7\omega_2\omega_3^2 - 24\omega_2\omega_3^2) \frac{v_2\rho\delta_l^2\delta_t}{12\omega_2^2\omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (12\omega_2^2 + 13\omega_2^2\omega_3^2 - 6\omega_3^2 + 7\omega_3^2\omega_3 - \omega_2^2\omega_3^2 - 24\omega_2^2\omega_3 + 12\omega_3^2 + 12\omega_2\omega_3 - 24\omega_2\omega_3^2) \frac{v_1\rho\delta_l^2\delta_t}{12\omega_2^2\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& (6\omega_2^2\omega_3^2 - 6\omega_2^3 + 12\omega_2^3\omega_3 - 7\omega_2^2\omega_3^2 - 7\omega_2^3\omega_3^2 - 12\omega_3^3 - 6\omega_2^2\omega_3 + \omega_2^3\omega_3^3 + 18\omega_2\omega_3^3) \frac{v_2v_1\rho\delta_l^3}{6\omega_2^3\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial t \partial x_2^2 \partial x_2} + \\
& C_{16} \frac{\rho\delta_l^3}{12\omega_5^2\omega_2^3\omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2} + C_{17} \frac{v_2v_1\delta_l^4}{6\omega_5^2\omega_2^3\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2} + C_{18} \frac{v_2\rho\delta_l^4}{12\omega_5^2\omega_2^3\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_1\rho\delta_l^4}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 - \omega_3^2 + 3\omega_3) \frac{3v_2\rho\delta_l^2}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + C_{20} \frac{\rho\delta_l^3}{12\omega_2\omega_6^2\omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (6\omega_2^2\omega_3^2 - 12\omega_2^3 + 18\omega_2^3\omega_3 - 7\omega_2^3\omega_3^2 - 7\omega_2^3\omega_3^2 - 6\omega_3^3 + \omega_2^3\omega_3^3 + 12\omega_2\omega_3^3 - 6\omega_2\omega_3^2) \frac{v_2v_1\rho\delta_l^3}{6\omega_2^3\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{21} \frac{\delta_4^4}{4\omega_2^2\omega_3^2\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_1\rho\delta_l^4}{12\omega_3^2\omega_2^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{v_2\rho\delta_l^4}{12\omega_5^2\omega_2^3\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_3^2} + \\
& C_{25} \frac{v_2v_1\delta_l^4}{6\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_{26} \frac{v_2\rho\delta_l^4}{12\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{27} \frac{v_1\rho\delta_l^4}{12\omega_2^3\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{28} \frac{\delta_4^4}{24\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{29} \frac{v_2\rho\delta_l^4}{12\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-2 + 3\omega_4 - \omega_4^2) \frac{\rho\delta_l\delta_t^2}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (12\omega_2^2 - 24\omega_4\omega_2^2 + 12\omega_4\omega_2 - 24\omega_4^2\omega_2 - \omega_4^3\omega_2^2 + 12\omega_4^2 + 7\omega_4^3\omega_2 - 6\omega_4^3 + 13\omega_4^2\omega_2^2) \frac{v_3\rho\delta_l^2\delta_t}{12\omega_4^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (12\omega_2^2 - 24\omega_4\omega_2^2 - 6\omega_3^2 + 7\omega_4\omega_2^3 + 12\omega_4\omega_2 - 24\omega_4^2\omega_2 + 12\omega_4^2 - \omega_4^2\omega_2^3 + 13\omega_4^2\omega_2^2) \frac{v_1\rho\delta_l^2\delta_t}{12\omega_4^2\omega_3^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-6\omega_4\omega_2^2 - 6\omega_2^3 + 12\omega_4\omega_2^3 + \omega_4^3\omega_2^3 - 7\omega_4^3\omega_2^2 - 7\omega_4^2\omega_2^3 + 18\omega_4^3\omega_2 - 12\omega_4^3 + 6\omega_4^2\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^3 \omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + \\
& C_{30} \frac{\rho \delta_l^3}{12\omega_4 \omega_5^2 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{31} \frac{v_3 v_1 \delta_l^4}{6\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{32} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{33} \frac{v_1 \rho \delta_l^4}{12\omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (12\omega_4\omega_3 + 12\omega_2^2 - 24\omega_4\omega_3^2 + 13\omega_4^2\omega_3^2 + 7\omega_4^3\omega_3 + 12\omega_4^2 - \omega_4^3\omega_3^2 - 24\omega_4^2\omega_3 - 6\omega_4^3) \frac{v_3 \rho \delta_l^2 \delta_t}{12\omega_4^3 \omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (12\omega_4\omega_3 - 6\omega_3^3 + 7\omega_4\omega_3^3 + 12\omega_3^2 - 24\omega_4\omega_3^2 + 13\omega_4^2\omega_3^2 - \omega_4^2\omega_3^3 + 12\omega_4^2 - 24\omega_4^2\omega_3) \frac{v_2 \rho \delta_l^2 \delta_t}{12\omega_4^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^3 \omega_2 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{35} \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^3 \omega_2^2 \omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{36} \frac{v_2 v_1 \rho \delta_l^3}{6\omega_4 \omega_2^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{37} \frac{v_3 v_2 \delta_l^4}{\omega_4^3 \omega_5^2 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_4^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{40} \frac{v_2 \rho \delta_l^4}{12\omega_5^2 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-6\omega_3^3 + 12\omega_4\omega_3^3 - 6\omega_4\omega_3^2 + 6\omega_4^2\omega_3^2 + 18\omega_4^3\omega_3 - 7\omega_4^2\omega_3^2 - 7\omega_4^3\omega_3^2 - 12\omega_4^3 + \omega_4^3\omega_3^3) \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^3 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{41} \frac{\rho \delta_l^3}{12\omega_4 \omega_6^2 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{42} \frac{v_3 v_1 \delta_l^4}{\omega_4^3 \omega_2^3 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{v_3 \rho \delta_l^4}{12\omega_3^2 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{44} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_4^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{v_1 \rho \delta_l^4}{12\omega_2^2 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{46} \frac{v_3 v_2 \delta_l^4}{6\omega_4^3 \omega_2^2 \omega_6^3 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{47} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{48} \frac{v_2 \rho \delta_l^4}{12\omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + 3\omega_4 - \omega_4^2) \frac{3v_3 \rho \delta_l^2 \delta_t}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2^2} + C_{49} \frac{\rho \delta_l^3}{12\omega_2^2 \omega_3^2 \omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (-12\omega_2^3 + 18\omega_4\omega_2^3 + \omega_4^3\omega_2^3 - 6\omega_4^2\omega_2 - 7\omega_4^3\omega_2^2 - 7\omega_4^2\omega_3^2 + 12\omega_4^3\omega_2 - 6\omega_4^3 + 6\omega_4^2\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{50} \frac{\delta_l^4}{4\omega_2^2 \omega_4^2 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{51} \frac{v_1 \rho \delta_l^4}{12\omega_2^2 \omega_4^2 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{52} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + C_{53} \frac{\rho \delta_l^3}{12\omega_2^2 \omega_4^3 \omega_3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
& (-12\omega_3^3 + 18\omega_4\omega_3^3 + 6\omega_4^2\omega_3^2 + 12\omega_3^2\omega_3 - 7\omega_4^2\omega_3^2 - 7\omega_4^3\omega_3^2 - 6\omega_4^2\omega_3 - 6\omega_4^3 + \omega_4^3\omega_3^3) \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^3 \omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + \\
& C_{54} \frac{v_2 v_1 \delta_l^4}{\omega_7^2 \omega_4^2 \omega_5^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{55} \frac{v_2 \rho \delta_l^4}{12\omega_7^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{56} \frac{v_1 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{57} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_4^3 \omega_2^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{58} \frac{\delta_l^4}{4\omega_2^2 \omega_4^2 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{59} \frac{v_2 \rho \delta_l^4}{12\omega_7^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{60} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{61} \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3^3} + \\
& C_{62} \frac{v_3 v_1 \delta_l^4}{6\omega_7^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{63} \frac{v_3 \rho \delta_l^4}{12\omega_7^2 \omega_4^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{64} \frac{v_1 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{65} \frac{v_3 v_2 \delta_l^4}{6\omega_7^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& C_{66} \frac{v_3 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{67} \frac{v_2 \rho \delta_l^4}{12\omega_7^2 \omega_4^2 \omega_3^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{68} \frac{\delta_l^4}{24\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{69} \frac{v_3 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 + 9cs^2\omega_5 + 9cs^2\omega_2 - 6v_1^2 - 3\omega_5 - 3\omega_2 + 3v_1^2\omega_2 - 18cs^2 + \omega_5\omega_2 - v_1^2\omega_5\omega_2 + 3v_1^2\omega_5 - 3cs^2\omega_5\omega_2 \\
C_2 &= -6\omega_2^2 - 12cs^2\omega_5 - 12cs^2\omega_2 + 6cs^2\omega_2^2 + 12\omega_2 - 36v_1^2\omega_2 - 3cs^2\omega_5\omega_2^2 - 6\omega_5\omega_2 + 6v_1^2\omega_5\omega_2 + 12v_1^2\omega_5 - 5v_1^2\omega_5\omega_2^2 + 18cs^2\omega_5\omega_2 + 2\omega_5\omega_2^2 + 18v_1^2\omega_2^2 \\
C_3 &= -3v_1^2\omega_5\omega_2^2\omega_3 + 4cs^2\omega_5\omega_2\omega_3^2 - v_1^2\omega_2^2\omega_3^2 + cs^2\omega_2^2\omega_3^2 - 2cs^2\omega_5\omega_2\omega_3 + v_1^2\omega_5\omega_2^2\omega_3^2 - 2v_1^2\omega_5\omega_2\omega_3^2 - 2cs^2\omega_2\omega_3 + cs^2\omega_5\omega_2^2\omega_3 + 2v_1^2\omega_2\omega_3^2 + \\
& 2v_1^2\omega_5\omega_2^2 - cs^2\omega_5\omega_2\omega_3^2 + 2v_1^2\omega_5\omega_2\omega_3 - 2cs^2\omega_5\omega_3 \\
C_4 &= -cs^2\omega_2^2\omega_6\omega_3^2 - 2cs^2\omega_2^2\omega_3 + 2v_2^2\omega_2\omega_6\omega_3 - 3v_2^2\omega_2\omega_6\omega_3^2 + cs^2\omega_2^2\omega_3^2 + 4cs^2\omega_2^2\omega_6\omega_3 + 2v_2^2\omega_6\omega_3^2 + v_2^2\omega_2^2\omega_6\omega_3^2 - v_2^2\omega_2^2\omega_3^2 - 2cs^2\omega_2\omega_6\omega_3 + \\
& cs^2\omega_2\omega_6\omega_3^2 + 2v_2^2\omega_2^2\omega_3 - 2cs^2\omega_2^2\omega_6 - 2v_2^2\omega_2^2\omega_6\omega_3 \\
C_5 &= 6 - v_2^2\omega_6\omega_3 + 9cs^2\omega_3 + 3v_2^2\omega_6 - 6v_2^2 - 18cs^2 + 3v_2^2\omega_3 - 3\omega_6 + 9cs^2\omega_6 + \omega_6\omega_3 - 3\omega_3 - 3cs^2\omega_6\omega_3 \\
C_6 &= 6v_2^2\omega_6\omega_3 + 6cs^2\omega_3^2 - 12cs^2\omega_3 + 12v_2^2\omega_6 - 6\omega_3^2 - 5v_2^2\omega_6\omega_3^2 - 36v_2^2\omega_3 - 3cs^2\omega_6\omega_3^2 - 12cs^2\omega_6 - 6\omega_6\omega_3 + 12\omega_3 + 18cs^2\omega_6\omega_3 + 2\omega_6\omega_3^2 + 18v_2^2\omega_3^2 \\
C_7 &= -2\omega_4cs^2\omega_5\omega_2 - 2\omega_4^2cs^2\omega_2 - 2\omega_2^2cs^2\omega_5 - 3\omega_4v_1^2\omega_5\omega_2^2 + 2\omega_4v_1^2\omega_5\omega_2 + \omega_4^2cs^2\omega_2^2 + \omega_4cs^2\omega_5\omega_2^2 + 4\omega_4^2cs^2\omega_5\omega_2 + \omega_4^2v_1^2\omega_5\omega_2^2 + 2\omega_4^2v_1^2\omega_2 - \\
& \omega_4^2v_1^2\omega_2^2 + 2v_1^2\omega_5\omega_2^2 - 2\omega_4^2v_1^2\omega_5\omega_2 - \omega_4^2cs^2\omega_5\omega_2^2 \\
C_8 &= \omega_7^2 v_2^2 \omega_6 \omega_3^2 + \omega_4^2 c s^2 \omega_3^2 - 2 \omega_4 c s^2 \omega_6 \omega_3 + \omega_4 c s^2 \omega_6 \omega_3^2 - 2 \omega_4^2 v_2^2 \omega_6 \omega_3 - 2 \omega_4^2 c s^2 \omega_3 + 2 v_2^2 \omega_6 \omega_3^2 - 2 \omega_4^2 c s^2 \omega_6 + 2 \omega_4^2 v_2^2 \omega_3 - 3 \omega_4 v_2^2 \omega_6 \omega_3^2 + \\
& 4 \omega_4^2 c s^2 \omega_6 \omega_3 - \omega_4^2 c s^2 \omega_6 \omega_3^2 + 2 \omega_4 v_2^2 \omega_6 \omega_3 - \omega_4^2 v_2^2 \omega_3^2 \\
C_9 &= -3 \omega_7 \omega_4^2 v_3^2 \omega_2 + \omega_7 \omega_4^2 c s^2 \omega_2 - 2 \omega_7 c s^2 \omega_2^2 - \omega_7^2 v_3^2 \omega_2^2 - \omega_7 \omega_4^2 c s^2 \omega_2^2 + \omega_7 \omega_4^2 v_3^2 \omega_2^2 + \omega_4^2 c s^2 \omega_2^2 + 4 \omega_7 \omega_4 c s^2 \omega_2^2 + 2 \omega_4 v_3^2 \omega_2^2 - \\
& 2 \omega_4 c s^2 \omega_2^2 - 2 \omega_7 \omega_4 v_3^2 \omega_2^2 + 2 \omega_7 \omega_4 v_3^2 \omega_2 - 2 \omega_7 \omega_4 c s^2 \omega_2^2 \\
C_{10} &= \omega_7 \omega_4^2 v_3^2 \omega_3^2 + \omega_4^2 c s^2 \omega_3^2 - 2 \omega_7 c s^2 \omega_3^2 - \omega_7^2 v_3^2 \omega_3^2 - \omega_7 \omega_4^2 c s^2 \omega_3^2 + \omega_7 \omega_4^2 v_3^2 \omega_3^2 - 3 \omega_7 \omega_4^2 v_3^2 \omega_3 - 2 \omega_7 \omega_4 c s^2 \omega_3^2 + 2 \omega_7 \omega_4 v_3^2 \omega_3 - \\
& 2 \omega_4 c s^2 \omega_3^2 - 2 \omega_7 \omega_4 v_3^2 \omega_3^2 + 4 \omega_7 \omega_4 c s^2 \omega_3^2 + 2 \omega_4 v_3^2 \omega_3^2 \\
C_{11} &= 6 - 3\omega_7 - 3\omega_4 - \omega_7 \omega_4 v_3^2 + 9\omega_4 c s^2 - 6v_3^2 + 3\omega_4 v_3^2 - 18cs^2 - 3\omega_7 \omega_4 c s^2 + \omega_7 \omega_4 + 3\omega_7 v_3^2 + 9\omega_7 c s^2 \\
C_{12} &= 12\omega_4 + 6\omega_4^2 c s^2 - 5\omega_7 \omega_4^2 v_3^2 - 3\omega_7 \omega_4^2 c s^2 + 18\omega_4^2 v_3^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_4 c s^2 - 36\omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 + 2\omega_7 \omega_4^2 - 6\omega_4^2 - 6\omega_7 \omega_4 + 12\omega_7 v_3^2 - 12\omega_7 c s^2
\end{aligned}$$



$$12c s^2 \omega_2^2 \omega_6^2 \omega_3^3 - 6 \omega_2^2 \omega_6 \omega_3^3 - 12 c s^2 \omega_3^2 \omega_6^2 - 12 c s^2 \omega_2^3 \omega_6 \omega_3 - 12 v_2^2 \omega_2^3 \omega_6^2 \omega_3^2 - 6 v_2^2 \omega_2^3 \omega_3^3 + 12 \omega_2^2 \omega_6 \omega_3^3 + 48 c s^2 \omega_2^2 \omega_6^2 \omega_3^2 + 12 v_2^2 \omega_3^2 \omega_6^3 + 3 v_2^2 \omega_2^3 \omega_3^2 \omega_6^3$$

$$\begin{aligned}
C_{28} = & -36c^2s^2v_2^2\omega_6^2\omega_3 - 30v_4^2\omega_6\omega_3^3 + 24cs^4\omega_6^2\omega_3^2 + 12cs^2\omega_6^2\omega_3 - 3cs^4\omega_6^2\omega_3^3 + 72v_4^2\omega_6\omega_3^2 + 30v_2^2\omega_6\omega_3^3 + 36v_4^2\omega_6^2\omega_3^3 + 6cs^2v_2^2\omega_6^2\omega_3^2 - 8cs^2\omega_6^2\omega_3^2 - 48cs^4\omega_6^2\omega_3 + \\
& - 36c^4\omega_6^2 - 12cs^2v_2^2\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^3 - 72v_2^2\omega_6^2\omega_3^2 - 72v_2^2\omega_6\omega_3^2 + 108cs^4v_2^2\omega_6^2\omega_3^2 + 24cs^4\omega_6\omega_3 - 6cs^2\omega_6\omega_3^3 + 144cs^2v_2^2\omega_6\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 - 216cs^4v_2^2\omega_6^2\omega_3^2 - \\
& - 3v_2^2\omega_6^2\omega_3^3 + 24cs^2\omega_6^2\omega_3^2 - 72cs^2v_2^2\omega_6\omega_3^2 - 24cs^2\omega_6\omega_3 + 6cs^4\omega_6\omega_3^3 + 72v_2^2\omega_6^2\omega_3^2 - 12v_2^2\omega_6^2\omega_3^2 + 72cs^2v_2^2\omega_6\omega_3 + 3v_2^2\omega_6^2\omega_3^3 - 36v_2^2\omega_6^2\omega_3^2 - 24cs^4\omega_6\omega_3^2
\end{aligned}$$

$$\begin{aligned} C_{29} = & -\omega_6^2 w_3^3 + 60 v_2^2 \omega_6 w_3 + 30 c s^2 w_3^3 + 2 w_6^2 w_3^2 - 12 v_2^2 w_6^2 - 30 c s^2 w_6^2 w_3 - 60 c s^2 w_3^2 - 18 w_3^3 - 24 v_2^2 \omega_6 w_3^3 + 6 w_6^2 w_3 - 2 c s^2 w_6^2 w_3^2 + 36 w_3^2 + c s^2 w_6^2 w_3^3 + 24 v_2^2 \omega_6 w_3^2 - 24 c s^2 w_6 w_3^3 + 2 v_2^2 w_6^2 w_3^2 + 2 v_2^2 w_6^2 w_3^3 + 72 c s^2 \omega_6 w_3^2 - 12 w_6 w_3 + 24 c s^2 w_6^2 - 12 c s^2 w_6 w_3 - 24 w_6 w_3^2 - 84 v_2^2 w_3^2 + 12 w_6 w_3^3 - 12 v_2^2 w_6^2 w_3 + 42 v_2^2 w_3^3 \end{aligned}$$

$$\begin{aligned} C_{30} = & -12\omega_4 v_1^2 \omega_2^2 + 12cs^2 \omega_5^2 \omega_2 + 12\omega_4 cs^2 \omega_5 \omega_2 - 9\omega_4 v_1^2 \omega_5 \omega_2^3 - v_1^2 \omega_5^2 \omega_3^2 + 6\omega_4 v_1^2 \omega_2^3 - 6v_1^2 \omega_5^2 \omega_2^2 + 30\omega_4 v_1^2 \omega_5 \omega_2^2 + 24\omega_4 v_1^2 \omega_5^2 - \\ & 12\omega_4 v_1^2 \omega_5 \omega_2 + 12v_1^2 \omega_5^2 \omega_2 + 3cs^2 \omega_5^2 \omega_2^3 + 9\omega_4 cs^2 \omega_5 \omega_2^3 - 30\omega_4 cs^2 \omega_5 \omega_2^2 - 18cs^2 \omega_5^2 \omega_2^2 - 6\omega_4 cs^2 \omega_3^2 + 12\omega_4 cs^2 \omega_5^2 + 22\omega_4 cs^2 \omega_5^2 \omega_2^2 + 12cs^2 \omega_5 \omega_2^2 - \\ & 36\omega_4 v_1^2 \omega_5^2 \omega_2 + 12\omega_4 cs^2 \omega_2^2 - 6cs^2 \omega_5 \omega_2^3 - 2\omega_4 cs^2 \omega_2^2 \omega_3^2 - 12v_1^2 \omega_5 \omega_2^2 + 8\omega_4 v_1^2 \omega_5^2 \omega_2^2 - 30\omega_4 cs^2 \omega_5^2 \omega_2 + \omega_4 v_1^2 \omega_5^2 \omega_3^2 + 6v_1^2 \omega_5 \omega_2^3 \end{aligned}$$

$$\begin{aligned}
C_{31} = & 36w_4^2c_5^2s_5^2w_2^2 + 12w_3^3w_5w_2 + 6w_1^2w_5^2w_3^2 + w_4^2w_5^2w_3^3 + 36w_4^3c_5^2s_5^2w_2^2 - 6w_3^3v_1^2w_5^2w_2^2 - 12w_4^2c_5^2s_5^2w_2^3 - 3w_4^2w_5^2w_2^2 + 6w_3^3c_5^2s_5^2w_2^3 - \\
& 6w_4^2v_1^2w_5^2w_2^2 + 6w_3^4w_5w_3^2 - 6w_3^4v_1^2w_3^2 + 12w_4^3v_1^2w_5^2w_2 + 6w_4^2v_1^2w_5^2w_3^2 - 21w_3^3w_5w_2^2 - 36w_4^3c_5^2s_5^2w_2^2 - 12w_4^2c_5^2s_5^2w_2^3 + 12w_3^3v_1^2w_2^2 + 7w_3^4w_5^2w_2^2 - \\
& 3w_4^3w_3^2 + 72w_4^3c_5^2s_5^2w_2^2 - 12w_4c_5^2s_5^2w_2^2 - 24w_4^3c_5^2s_5^2w_3^2 - w_4^3w_5^2w_3^2 + 6w_3^4w_2^2 - 24w_4^3v_1^2w_5w_2 + 6w_4c_5s_5^2w_2^3 + 12w_4^3v_1^2w_5w_2^2 + 12w_4^2c_5^2s_5^2w_3^2 + \\
& 6w_4^2w_5w_2^2 + 6w_4v_1^2w_5^2w_2^2 - 36w_4^3c_5^2s_5^2w_2^2 - 12w_4^3c_5^2s_5^2w_3^2 - 24w_4^2c_5^2s_5^2w_5w_2^2 - 6w_4^3w_5^2w_2 + 18w_4^3c_5^2s_5^2w_3^2 - 24w_4^3c_5^2s_5^2w_5w_2 - 12w_4v_1^2w_5^2w_3^2 - 3w_4^2w_5w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{32} = & 48w_4^2c^2s^2w_5^2w_2^2 + 3w_4^3v_1^2w_5^2w_3^2 + 12v_1^2w_5^2w_3^3 + 2w_4^2w_5^2w_3^2 + 36w_4^3c^2s^2w_5^2w_2 - 12w_4^3v_1^2w_5^2w_2^2 - 12w_4^2c^2s^2w_5^2w_3^2 - 6w_4^2w_5^2w_2^2 + 4w_3^4c^2s^2w_5^2w_3^2 - \\
& 24w_4^3v_1^2w_5^2 + 12w_4^2v_1^2w_5^2w_2^2 + 3w_4^3w_5w_2^3 - 6w_4^3v_1^2w_3^2 + 30w_4^3v_1^2w_5^2w_2 - 6w_3^4w_5w_2^2 - 32w_4^3c^2s^2w_5^2w_2^2 - 24w_4^2c^2s^2w_5^2w_2 + 12w_3^4v_1^2w_2^2 + 3w_4^3w_5w_2^2 + \\
& 12w_4^2v_1^2w_5w_2^3 + 36w_4^3c^2s^2w_5w_2^2 - 12w_4c^2s^2w_5^2w_2^2 - 12w_4^3c^2s^2w_5w_2^3 - w_4^3w_5w_2^3 - 24w_4^2v_1^2w_5w_2^2 + 12w_3^4v_1^2w_5w_2 + 6w_4c^2s^2w_5^2w_3^2 - 12w_4^3v_1^2w_5w_2^2 + \\
& 12w_4^2c^2s^2w_5w_2^3 + 12w_4^2w_5w_2^2 - 12w_4^3c^2s^2w_2^2 - 12w_4^3c^2s^2w_5^2 - 24w_4^2c^2s^2w_5w_2^2 + 6w_4^3c^2s^2w_3^2 - 12w_4^3c^2s^2w_5w_2 - 18w_4v_1^2w_5^2w_3^2 - 6w_4^2w_5w_2^3
\end{aligned}$$

$$\begin{aligned} C_{33} = & 11w_5^2 w_2^2 + 12w_2^2 + 18cs^2 w_5^2 w_2 + v_1^2 w_5^2 w_3^2 - 6w_3^2 - w_5^2 w_3^2 - 14v_1^2 w_5^2 w_2^2 + 12v_1^2 w_5^2 w_2 - 60cs^2 w_2^2 + 4cs^2 w_5^2 w_3^2 - 12w_5^2 w_2 - 26cs^2 w_5^2 w_2^2 + \\ & 30cs^2 w_3^2 + 96cs^2 w_5 w_2^2 + 24w_5 w_2 - 60v_1^2 w_5 w_2 - 30cs^2 w_5 w_3^2 + 9w_5 w_3^2 + 12v_1^2 w_5^2 + 48v_1^2 w_5 w_2^2 - 6v_1^2 w_3^2 - 36cs^2 w_5 w_2 - 36w_5 w_2^2 + 12v_1^2 w_2^2 - 6v_1^2 w_5 w_3^2 \end{aligned}$$

$$C_{34} = 18\omega_4^3\omega_2\omega_3 - 12\omega_4\omega_2\omega_3^2 + 18\omega_4\omega_2\omega_3^3 - 6\omega_4\omega_3^3 + 3\omega_4^3\omega_2\omega_3^3 - 16\omega_4^3\omega_2\omega_3^2 - 12\omega_4^2\omega_3^2 - 12\omega_4^2\omega_2\omega_3 - 6\omega_4^3\omega_3 + 12\omega_4^2\omega_3^3 + 30\omega_4^2\omega_2\omega_3^2 + 12\omega_4^3\omega_3^2 - 6\omega_2\omega_3^3 - 6\omega_4^3\omega_2 - 4\omega_4^3\omega_3^3 - 16\omega_4^2\omega_2\omega_3^3$$

$$\begin{aligned} C_{35} = & 18w_4^3w_2w_3 - 16w_4^2w_2^3w_3 - 6w_3^2w_3 - 6w_4w_3^2 + 30w_4^2w_2^2w_3 - 4w_4^3w_2^3 - 12w_4w_2^2w_3 + 12w_4^3w_2^2 - 12w_4^2w_2w_3 + 3w_4^3w_2^3w_3 - 6w_4^3w_3 + \\ & 18w_4w_2^3w_3 + 12w_4^2w_2^3 - 6w_3^4w_2 - 16w_4^3w_2^2w_3 - 12w_4^2w_2^2 \end{aligned}$$

$$C_{36} = -12\omega_4\omega_2\omega_3^2 - 12\omega_2^2\omega_3^2 + 18\omega_4\omega_2\omega_3^3 - 6\omega_3^2\omega_3 + 12\omega_2^2\omega_3^3 - 6\omega_4\omega_2^3 + 12\omega_2^3\omega_3^2 - 6\omega_4\omega_3^3 - 4\omega_2^3\omega_3^3 - 12\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_2^3\omega_3^3 - 16\omega_4\omega_2^3\omega_3^2 + 18\omega_4\omega_3^2\omega_3 - 16\omega_4\omega_2^2\omega_3^3 - 6\omega_2\omega_3^3 + 30\omega_4\omega_2^2\omega_3^2$$

$$\begin{aligned}
C_{37} = & -2w_1^2c^2s^2w_5^2w_2w_3^3 - 8w_4^4v_1^2w_5^2w_3^2w_3 + w_4^4c^2s^2w_3^2w_3^3 + 3w_3^4v_2^2w_5^2w_2^2w_3^2 - w_3^4v_2^2w_5w_3^2w_3^2 - 2w_3^4c^2s^2w_5w_2w_3^3 + 2w_3^4v_2^2w_2^2w_3^3 - \\
& 8w_4^4v_1^2w_5^2w_3^2 - 2w_4^4c^2s^2w_5w_3^2w_3^3 - 2w_4^4c^2s^2w_5^2w_3^2w_3^3 + 7w_3^4v_2^2w_5^2w_3^2w_3^3 + 3w_4v_1^2w_5^2w_3^2w_3^4 + w_4^4c^2s^2w_5^2w_3^2w_3 + 2w_4^4v_1^2w_5w_3^2w_3^2 - 6w_3^4c^2s^2w_5^2w_2w_3^3 + \\
& 4w_4^4v_1^2w_5^2w_3^2w_3 - w_4^4v_1^2w_5^2w_3^3 + 2w_3^4v_1^2w_5w_3^2w_3^2 - 2w_3^4c^2s^2w_5^2w_3^2w_3^2 - 7w_3^4v_1^2w_5^2w_2^2w_3^2 - 2w_4^4c^2s^2w_5^2w_3^2w_3 + 4w_4^4v_1^2w_5^2w_3^2w_3^2 + 3w_4^4v_1^2w_5^2w_2^2w_3^2 - \\
& 2w_3^4c^2s^2w_5^2w_3^2w_3^2 + w_4^4c^2s^2w_5^2w_3^2w_3^3 - 6w_4^4v_1^2w_5^2w_3^2w_3^3 + 2w_4^4v_1^2w_5^2w_3^2w_3^3 - 10w_3^4v_1^2w_5^2w_3^2w_3^2 + w_4^4c^2s^2w_5^2w_3^2w_3^3 + w_4^4c^2s^2w_5^2w_3^2w_3^3 + 4w_3^4c^2s^2w_5^2w_3^2w_3^3 + w_7^4c^2s^2w_5^2w_3^2w_3^3 + 3w_4^4v_1^2w_5^2w_3^2w_3^3 + 2w_4^4v_1^2w_5^2w_3^2w_3^3 + 2w_3^4c^2s^2w_5^2w_3^2w_3^3 + 8w_4^4v_1^2w_5^2w_3^2w_3^3 - 8w_4^4v_1^2w_5^2w_3^2w_3^3 + \\
& 2w_4^4v_1^2w_5w_3^2w_3^3 - 2w_4^4c^2s^2w_5^2w_3^2w_3^3 - 2w_4^4c^2s^2w_5^2w_3^2w_3^3 - 2w_4^4c^2s^2w_5^2w_3^2w_3^3 + 3w_3^4v_2^2w_5^2w_3^2w_3^3 + 6w_4^4c^2s^2w_5^2w_3^2w_3^3 - 2w_4^4c^2s^2w_5w_3^2w_3^3 + 7w_3^4v_1^2w_5^2w_3^2w_3^3 + 6w_4^4c^2s^2w_5^2w_3^2w_3^3 - w_4^4v_1^2w_5w_3^2w_3^3 - 2w_3^4c^2s^2w_5^2w_3^2w_3^2
\end{aligned}$$

$$\begin{aligned} C_{38} = & -30\omega_4^2\omega_2^2\omega_3^3 + 18\omega_4^2\omega_3^2\omega_3 + 12\omega_4^2\omega_2^2\omega_3^2 + 24\omega_4^2\omega_3^2\omega_3^3 - 36\omega_4^3\omega_2\omega_3^3 + 12\omega_3^2\omega_3^3 + 18\omega_4^3\omega_2\omega_3^2 - 42\omega_4^2\omega_3^2\omega_3^2 + 12\omega_4^3\omega_2^3 - 30\omega_4^3\omega_2^2\omega_3^2 - \\ & 30\omega_4\omega_2^3\omega_3^3 + 18\omega_4\omega_2^2\omega_3^2 - 30\omega_3^3\omega_2^3\omega_3 + 28\omega_3^4\omega_2^2\omega_3^3 + 6\omega_4\omega_2^2\omega_3^3 + 24\omega_4^3\omega_2^3\omega_3^2 + 6\omega_4^3\omega_2^2\omega_3 + 12\omega_4^3\omega_3^3 - 5\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4^2\omega_2\omega_3^2 \end{aligned}$$

$$C_{39} = 48w_4^4cs^2w_5^2w_2^2 - 5w_4^3v_1^2w_5^2w_2^3 + 12v_1^2w_5^2w_2^3 + 36w_4^3cs^2w_5^2w_2 + 16w_4^3v_1^2w_5^2w_2^2 - 12w_4^2cs^2w_5^2w_2^3 + 4w_4^3cs^2w_5^2w_2^3 - 36w_4^2v_1^2w_5^2w_2^2 - 6w_4^3v_1^2w_3^2 - 6w_4^3v_1^2w_5^2w_2 + 24w_4^2v_1^2w_5^2w_2^3 - 32w_4^3cs^2w_5^2w_2^2 - 24w_4^2cs^2w_5^2w_2 + 12w_4^3v_1^2w_2^2 - 12w_4^2v_1^2w_5w_2^3 + 36w_4^3cs^2w_5^2w_2^2 - 12w_4cs^2w_5^2w_2^2 - 12w_4^3cs^2w_5w_2^3 + 24w_4^3v_1^2w_5w_2^2 + 12w_4^3v_1^2w_5w_2 + 6w_4cs^2w_5^2w_2^3 - 36w_4^2v_1^2w_5w_2^2 + 12w_4^3cs^2w_5w_2^3 + 24w_4v_1^2w_5^2w_2^2 - 12w_4^3cs^2w_2^2 - 12w_4^3cs^2w_5^2 - 24w_4^2cs^2w_5w_2^2 + 12w_4^3v_1^2w_5w_2^3 + 6w_4^3cs^2w_2^3 - 12w_4^3cs^2w_5w_2 - 30w_4v_1^2w_5^2w_2^3$$

$$\begin{aligned} C_{40} = & 12v_1^2w_2^2w_3^3 - 32cs^2w_2^2w_2^3w_3 + 12v_1^2w_5w_2^3w_3^3 + 12v_1^2w_5^2w_2^3 + 6cs^2w_3^2w_3^3 + 6cs^2w_5^2w_2^3w_3 - 12cs^2w_5w_2w_3^3 - 12v_1^2w_5w_2^3w_3^2 + 48cs^2w_5^2w_2^2w_3^2 - \\ & 12cs^2w_5^2w_3^3 - 12cs^2w_2^2w_3^3 - 36v_1^2w_5w_2^3w_3^3 + 4cs^2w_5^2w_3^2w_3^3 - 12cs^2w_5^2w_2^3w_3 - 6v_1^2w_2^3w_3^3 - 6v_1^2w_5^2w_2w_3^3 - 12cs^2w_5^2w_2^3w_3^2 + 24v_1^2w_5w_2^2w_3^2 - \\ & 30v_1^2w_5^2w_3^2w_3 + 16v_1^2w_5^2w_2^2w_3^3 - 12cs^2w_5w_3^2w_3^3 + 12cs^2w_5w_3^2w_3^2 - 36v_1^2w_5^2w_2^2w_3^2 + 12v_1^2w_5w_2w_3^3 + 24v_1^2w_5^2w_2^2w_3 - 24cs^2w_5^2w_2w_3^2 + \\ & 36cs^2w_5w_2^2w_3^3 - 5v_1^2w_5^2w_2^3w_3 + 24v_1^2w_5^2w_3^2w_3^2 - 24cs^2w_5w_2w_3^2 + 36cs^2w_5^2w_2w_3^3 \end{aligned}$$

$$\begin{aligned} C_{41} = & 6w_4v_2^2w_3^3 - 36w_4v_2^2w_6^2w_3 - 12w_4v_2^2w_3^3 + 12w_4cs^2w_6w_3 + 12cs^2w_6^2w_3 + 12w_4cs^2w_6^2w_3 + w_4v_2^2w_6^2w_3^3 + 6w_2^2w_6w_3^3 - 18cs^2w_6^2w_3^3 - \\ & 30w_4cs^2w_6w_3^3 + 9w_4cs^2w_6w_3^3 + 3cs^2w_6^2w_3^3 - 12v_2^2w_6w_3^2 + 8w_4v_2^2w_6^2w_3^2 - 2w_4cs^2w_6^2w_3^3 - 6cs^2w_6w_3^3 - 6v_2^2w_6^2w_3^2 + 30w_4v_2^2w_6w_3^2 - 9w_4v_2^2w_6w_3^3 - \\ & v_2^2w_6^2w_3^3 + 12cs^2w_6w_3^2 + 22w_4cs^2w_6^2w_3^2 + 12w_4cs^2w_6^2w_3^3 - 30w_4cs^2w_6^2w_3 + 24w_4v_2^2w_6^2 - 12w_4v_2^2w_6w_3 + 12v_2^2w_6^2w_3^3 - 6w_4cs^2w_3^3 \end{aligned}$$

$$\begin{aligned}
C_{42} = & -2w_3^4 c s^2 w_2 w_6^2 w_3^2 + 7w_4^2 v_2^2 w_3^2 \omega_6^2 w_3^3 + w_3^4 c s^2 w_2 w_6 w_3^3 + w_4^3 c s^2 w_3^2 \omega_6^2 w_3 - 6w_3^4 v_2^2 w_3^2 w_6 w_3^2 - 2w_4^2 c s^2 w_2^2 \omega_6^2 w_3^2 + \\
& 4w_4 v_2^2 w_3^2 w_6 w_3^2 + 2w_3^4 v_2^2 w_3^2 \omega_6^2 - 2w_3^4 c s^2 w_3^2 \omega_6^2 - 2w_4^3 c s^2 w_2^2 \omega_6 w_3^2 - 10w_4^2 v_2^2 w_3^2 \omega_6^2 w_3^2 + w_4^3 c s^2 w_2 w_6^2 w_3^3 - 8w_4 v_2^2 w_3^2 \omega_6^2 w_3^3 + 3w_4^3 v_2^2 w_2^2 \omega_6^2 w_3^2 + \\
& w_4^2 c s^2 w_2^2 w_6^2 w_3^3 + 2w_3^4 v_2^2 w_3^2 w_6 w_3^3 - 10w_4^3 v_2^2 w_2^2 \omega_6^2 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6 w_3^2 + w_4^3 c s^2 w_3^2 w_6^2 w_3^3 + 3w_4^2 v_2^2 w_3^2 \omega_6^2 w_3^2 + 2w_4^3 v_2^2 w_3^2 w_6 w_3 + w_2^2 c s^2 w_3^2 w_6 w_3^3 + \\
& 7w_4^3 v_2^2 w_2^2 w_6^2 w_3^3 - 6w_4^3 c s^2 w_3^2 w_6^2 w_3^3 + 3w_4^2 v_2^2 w_3^2 w_6^2 w_3^3 + 3w_4 v_2^2 w_3^2 w_6^2 w_3^3 - 7w_4^3 v_2^2 w_3^2 \omega_6^2 w_3^3 + 4w_4^3 v_2^2 w_2 w_6^2 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6^2 w_3^3 - w_4^3 v_2^2 w_2^2 \omega_6^2 w_3^3 - \\
& 2w_4 c s^2 w_3^2 w_6^2 w_3^3 + 6w_4^3 c s^2 w_3^2 w_6 w_3^2 + 4w_4^2 v_2^2 w_3^2 \omega_6^2 w_3^2 + 2w_4^3 v_2^2 w_2 w_6 w_3^2 + 6w_4^2 c s^2 w_3^2 w_6^2 w_3^3 + 3w_4^3 v_2^2 w_3^2 \omega_6^2 w_3^3 - 8w_4^3 v_2^2 w_2 w_6^2 w_3^3 - 8w_4^2 v_2^2 w_2^2 \omega_6^2 w_3^3 -
\end{aligned}$$

$$\begin{aligned}
& 2w_4^3cs^2w_3^2w_6w_3^3 + w_4cs^2w_3^2w_6^2w_3^3 - 2w_4^3cs^2w_3^2w_6^2w_3 + 6w_3^3cs^2w_2^2w_6^2w_3^3 - w_4^3v_2^2w_3^2w_3^3 + 2w_4^2v_2^2w_3^2w_6w_3^2 - 2w_4^2cs^2w_3^2w_6^2w_3 - 2w_3^3cs^2w_3^2w_3^2w_6^2 - \\
& 2w_4^3v_2^2w_3^2w_6^2w_3^3 - w_4^2v_2^2w_3^2w_6w_3^3 + 2w_3^2v_2^2w_3^2w_3^2 - 2w_4^3cs^2w_2^2w_6^2w_3^3 - 2w_3^4cs^2w_3^2w_6w_3 + 8w_3^4v_2^2w_3^2w_6^2w_3^3 + 3v_2^2w_3^2w_6^2w_3^3
\end{aligned}$$

$$\begin{aligned} C_{43} = & 24\omega_4^2 v_2^2 w_6 w_3^2 - 12\omega_4^2 c s^2 \omega_6^2 w_3^3 + 12\omega_3^3 v_2^2 w_6 w_3 + 48\omega_4^2 c s^2 \omega_6^2 w_3^2 - 12\omega_4^2 v_2^2 w_6 w_3^3 + 36w_3^3 c s^2 \omega_6^2 w_3 - 12\omega_3^3 c s^2 \omega_6^2 + 12\omega_3^3 v_2^2 w_6 w_3^3 - \\ & 32w_3^4 c s^2 \omega_6^2 w_3^2 - 30w_4 v_2^2 w_6^2 w_3^3 - 24\omega_4^2 c s^2 \omega_6^2 w_3 + 12\omega_3^3 v_2^2 w_6^2 w_3^2 + 4\omega_3^4 c s^2 \omega_6^2 w_3^3 - 36w_3^4 v_2^2 w_6 w_3^2 - 6w_3^3 v_2^2 w_3^3 + 24w_4 v_2^2 w_6^2 w_3^2 - 12w_3^4 c s^2 w_6 w_3^3 + \\ & 16w_3^4 c s^2 \omega_6^2 w_3^2 + 6w_3^3 c s^2 w_3^3 + 6w_4 c s^2 \omega_6^2 w_3^3 - 5w_3^4 v_2^2 w_6^2 w_3^3 + 36w_3^4 c s^2 w_6 w_3^2 + 12v_2^2 w_6^2 w_3^3 - 12w_4 c s^2 w_6^2 w_3 - 12w_3^4 c s^2 w_3^2 - 24\omega_4^2 c s^2 w_6 w_3^2 + \\ & 24w_4^2 v_2^2 w_6^2 w_3^3 - 12w_3^4 c s^2 w_6 w_3 - 36w_4 v_2^2 w_6^2 w_3^2 + 12w_4^2 c s^2 w_6 w_3^3 - 6w_3^4 v_2^2 w_6^2 w_3 \end{aligned}$$

$$\begin{aligned} C_{44} = & -42\omega_4^2\omega_2^2w_3^3 + 18\omega_4^2w_3^2w_3 + 12w_2^2\omega_2^2w_3^2 + 24\omega_4^2w_3^2w_3^3 - 30w_4^3\omega_2w_3^3 + 12w_3^2\omega_3^3 + 6w_3^4\omega_2w_3^2 - 30\omega_4^2w_3^2w_3^2 + 12w_4^3\omega_3^2 - 30w_3^4\omega_2^2w_3^2 - \\ & 30w_4\omega_3^2w_3^3 + 6w_4\omega_3^2w_3^2 - 36w_4^3\omega_2^2w_3 + 24w_4^3\omega_2^2w_3^3 + 18w_4\omega_2^2w_3^3 + 28w_4^3\omega_2^3w_3^2 + 18w_4^2\omega_2^2w_3 + 12w_3^4w_3^3 - 5w_3^4\omega_2^3w_3^3 + 18w_4^2\omega_2w_3^3 \end{aligned}$$

$$\begin{aligned} C_{45} = & 6cs^2w_2w_6^2w_3^3 - 24cs^2w_2^2w_6w_3^2 + 6cs^2w_2^3w_3^3 + 12v_2^2w_3^2w_6w_3^3 + 12cs^2w_2^2w_6w_3^3 - 12cs^2w_2w_6^2w_3^2 + 36cs^2w_3^2w_6^2w_3 - 36v_2^2w_3^2w_6w_3^2 - \\ & 12cs^2w_3^2w_3^2 + 12v_2^2w_3^2w_6w_3 + 24v_2^2w_2^2w_6^2w_3^3 - 32cs^2w_3^2w_6^2w_3^2 - 36v_2^2w_2^2w_6^2w_3^2 + 4cs^2w_3^2w_6^2w_3^3 - 30v_2^2w_2w_6^2w_3^3 + 24v_2^2w_2^2w_6w_3^2 - 12cs^2w_3^2w_6w_3^2 - \\ & 24cs^2w_2^2w_6^2w_3 - 6v_2^2w_3^2w_6^2w_3^2 - 12v_2^2w_2^2w_6w_3^3 + 24v_2^2w_2w_6^2w_3^2 + 12v_2^2w_6^2w_3^3 + 36cs^2w_3^2w_6w_3^2 - 12cs^2w_2^2w_6^2w_3^2 - 12cs^2w_2^3w_6w_3 + \\ & 16v_2^2w_3^2w_6^2w_3^2 - 6v_2^2w_3^2w_3^3 + 48cs^2w_2^2w_6^2w_3^2 + 12v_2^2w_3^2w_3^2 - 5v_2^2w_3^2w_6^2w_3^2 \end{aligned}$$

$$\begin{aligned}
C_{46} = & -12w_4^2cs^2w_6^2w_3^3 - 3w_4^2w_6^2w_3^2 - 24w_4^3v_2^2w_6w_3 + 36w_4^2cs^2w_6^2w_3^2 + 12w_4^3w_6w_3 + w_4^2w_6^2w_3^3 + 36w_4^3cs^2w_6^2w_3 - 12w_4^3cs^2w_6^2 - 21w_4^3w_6w_3^2 - \\
& 36w_4^3cs^2w_6^2w_3^2 - 12w_4v_2^2w_6^2w_3^3 - 12w_4^2cs^2w_6^2w_3 + 12w_4^3v_2^2w_3^2 + 6w_4^3cs^2w_6^2w_3^3 + 6w_4^3w_6w_3^2 + 12w_4^3v_2^2w_6w_3^2 - 6w_4^3v_2^2w_3^3 + 6w_4v_2^2w_6^2w_3^2 - \\
& 24w_4^3cs^2w_6w_3^3 - 6w_3^3v_2^2w_6^2w_3^2 - w_4^3w_6^2w_3^3 + 18w_3^3cs^2w_3^3 + 6w_4cs^2w_6^2w_3^3 + 7w_4^2v_2^2w_6^2w_3^2 + 72w_4^3cs^2w_6w_3^2 + 6v_2^2w_6^2w_3^3 - 12w_4cs^2w_6^2w_3^2 - 36w_4^3cs^2w_3^2 - \\
& 24w_4^2cs^2w_6w_3^2 + 6w_4v_2^2w_6^2w_3^3 + 6w_4^3w_3^2 - 6w_4^3w_6^2w_3 - 24w_4^3cs^2w_6w_3 - 3w_4^2w_6w_3^3 - 3w_4^3w_3^3 - 6w_4v_2^2w_6^2w_3^2 + 12w_4^2cs^2w_6w_3^3 + 6w_4^2w_6w_3^2 + 12w_4^3v_2^2w_6w_3
\end{aligned}$$

$$\begin{aligned} \textcolor{red}{C_{47}} = & -24w_4^2v_2^2w_6w_3^2 - 12w_4^2cs^2w_6^2w_3^3 - 6w_4^2w_6^2w_3^2 + 12w_3^3v_2^2w_6w_3 + 48w_4^2cs^2w_6^2w_3^2 + 12w_4^2v_2^2w_6w_3^3 + 2w_4^2w_6^2w_3^3 + 36w_4^3cs^2w_6^2w_3 - 12w_4^3cs^2w_6^2w_3^2 - 6w_3^4w_6w_3^2 - 32w_4^3cs^2w_6^2w_3^3 - 18w_4v_2^2w_6^2w_3^3 - 24w_4^2cs^2w_6^2w_3 + 12w_3^3v_2^2w_6^2w_3^2 + 4w_4^3cs^2w_6^2w_3^3 + 3w_4^3w_6w_3^3 - 12w_4^2v_2^2w_6w_3^2 - 6w_4^3v_2^2w_6^2w_3^3 - 12w_3^3cs^2w_6w_3^3 - 12w_3^2v_2^2w_6^2w_3^2 - w_4^3w_6^2w_3^3 + 6w_4^3cs^2w_3^3 + 6w_4^2cs^2w_6^2w_3^3 - 24w_4^3v_2^2w_6^2 + 3w_4^3w_2^2w_3^3 + 3w_4^3v_2^2w_6^2w_3^3 + 36w_4^3cs^2w_6w_3^2 + 12v_2^2w_6^2w_3^3 - 12w_4cs^2w_6^2w_3^2 - 12w_4^3cs^2w_3^3 - 24w_4^2cs^2w_6w_3^2 - 12w_4^3cs^2w_6w_3 - 6w_4^2w_6w_3^3 + 12w_4^2v_2^2w_6^2w_3^2 + 12w_4^2cs^2w_6w_3^3 + 12w_4^2w_6w_3^3 + 30w_4^3v_2^2w_6^2w_3 \end{aligned}$$

$$\textcolor{red}{C_{48}} = -\omega_6^2 w_3^3 - 60 v_2^2 w_6 w_3 + 30 c_5^2 w_3^3 + 11 \omega_6^2 w_3^2 + 12 v_2^2 w_6^2 + 18 c_5^2 w_6^2 w_3 - 60 c_5^2 w_3^2 - 6 w_3^3 - 6 v_2^2 w_6 w_3 - 12 w_6^2 w_3 - 26 c_5^2 w_6^2 w_3 + 12 w_6^3 + 4 c_5^2 w_6^2 w_3^3 + 48 v_2^2 w_6 w_3^2 - 30 c_5^2 w_6 w_3^3 - 14 v_2^2 w_6^2 w_3^2 + v_2^2 w_6^2 w_3^3 + 96 c_5^2 w_6 w_3^2 + 24 w_6 w_3 - 36 c_5^2 w_6 w_3 - 36 w_6 w_3^2 + 12 v_2^2 w_3^2 + 9 w_6 w_3^3 + 12 v_2^2 w_6^2 w_3 - 6 v_2^2 w_3^3$$

$$\begin{aligned} C_{49} = & -2w_2^2 w_4^3 c s^2 w_2 + 30 w_7 w_4^2 v_3^2 w_2 + 12 w_4^2 c s^2 w_2 - 6 w_7 w_3^3 c s^2 - 12 w_4^2 v_3^2 w_2 - 30 w_7 w_4^2 c s^2 w_2 + w_7 w_3^3 v_3^2 w_2 + 6 w_7 w_3^4 v_3^2 - 36 w_7^2 w_4 v_3^2 w_2 + 12 w_7^2 w_4 v_3^2 + 12 w_7^2 w_4 c s^2 - 12 w_7 w_4^2 v_3^2 - 30 w_7^2 w_4 c s^2 w_2 + 12 w_7 w_4^2 c s^2 + 8 w_7^2 w_4^2 v_3^2 w_2 + 6 w_4^3 v_3^2 w_2 + 9 w_7 w_3^3 c s^2 w_2 - 9 w_7 w_4^2 v_3^2 w_2 - 6 w_4^3 c s^2 w_2 - 6 w_7 w_4^2 v_3^2 + 22 w_7^2 w_4^2 c s^2 w_2 - 18 w_7^2 w_4^2 c s^2 + 24 w_7^2 v_3^2 w_2 - 12 w_7 w_4 v_3^2 w_2 + 12 w_7 w_4 c s^2 w_2 + 3 w_7^2 w_4^3 c s^2 - w_7^2 w_4^3 v_3^2 + 12 w_7^2 c s^2 w_2 \end{aligned}$$

$$\begin{aligned}
C_{50} = & 2w_7^7 w_4^3 c s^2 v_2^2 a_5^2 w_2^2 - 2w_7 w_4^2 c s^4 a_5^2 w_2^3 - 2w_2^2 w_4^3 c s^4 a_2^2 w_2 + 4w_7 w_4^2 v_3^2 v_1^2 a_5^2 w_2^2 - 4w_4^2 c s^2 v_2^2 a_5^2 w_2^3 + 10w_7^2 w_4^3 c s^2 v_2^3 a_5^2 w_2 + 4w_7 w_4 v_3^2 v_1^2 w_5^2 w_2^3 - \\
& 12w_2^2 w_2^3 c s^4 a_5^2 w_2^2 - 3w_7 w_4^3 c s^2 v_2^2 w_5^2 w_2^3 + 12w_7^2 w_4^2 v_3^2 v_1^2 w_5^2 w_2^2 - 10w_7 w_4^2 v_3^2 v_2^2 w_5^2 w_2^3 + 4w_7^2 w_3^3 v_3^2 v_1^2 w_5 w_2 + 4w_7 w_4^2 c s^4 a_5^2 w_2^2 - w_7 w_4^3 c s^2 v_3^2 w_5^2 w_2^3 + \\
& 4w_7^2 w_2^2 c s^4 a_5^2 w_2^3 - 2w_3^3 v_3^2 v_2^2 w_5^2 w_2^3 + 2w_7 w_4^3 c s^2 v_2^2 w_5^2 w_2^3 + 14w_7^2 w_4^2 v_3^2 v_1^2 w_5^2 w_2^2 - 2w_7 w_4^3 c s^4 a_5^2 w_2^2 + 4w_7^2 v_3^2 v_2^2 w_5^2 w_2^3 + w_2^2 w_4^3 c s^2 v_2^2 w_5^2 w_2^3 + \\
& 2w_7 w_4^2 c s^2 v_2^2 w_5^2 w_2^3 - w_7^2 w_4^3 c s^4 a_5^2 w_2^3 - 10w_2^2 w_4^3 v_3^2 v_1^2 w_5^2 w_2^2 + 12w_7 w_4^2 v_3^2 v_1^2 w_5^2 w_2^2 - 4w_7^2 w_4^2 c s^2 v_2^2 w_5^2 w_2^3 - 4w_7^2 w_4^3 c s^2 v_2^2 w_5^2 w_2^2 - \\
& 4w_2^2 w_4^2 c s^2 v_2^2 w_5^2 w_2^2 - 8w_2^2 w_4^3 c s^2 v_3^2 w_5^2 w_2^2 - 4w_2^2 w_4^3 c s^4 v_2^2 w_5^2 w_2^3 + 4w_7^2 w_4^2 c s^4 a_5^2 w_2^2 + w_7 w_4^3 c s^4 v_2^2 w_5^2 w_2^3 - 28w_2^2 w_4^2 v_3^2 v_1^2 w_5^2 w_2^2 + w_7^2 w_4^3 c s^2 v_2^2 w_5^2 w_2^3 + \\
& 2w_7 w_4^2 c s^2 v_2^2 w_5^2 w_2^2 + 2w_7^2 w_4^2 c s^2 v_3^2 w_5^2 w_2^2 - 14w_7 w_4 v_3^2 v_1^2 w_5^2 w_2^3 + 4w_2^2 w_4^3 c s^4 a_5^2 w_2^2 + 3w_7^2 w_4^3 v_3^2 v_1^2 w_5 w_2 + 8w_7^2 w_4^2 c s^2 v_1^2 w_5^2 w_2^2 + 10w_7^2 w_4^3 c s^2 v_2^2 w_5 w_2^2 + \\
& 4w_7^2 w_4 c s^4 a_5^2 w_2^2 + 4w_7^2 w_4^2 v_3^2 v_1^2 w_5 w_2 + 4w_7^2 w_3^3 v_3^2 v_1^2 w_5^2 w_2^2 - w_7 w_4^3 c s^2 v_1^2 w_5 w_2^2 - 2w_7^2 w_4^2 c s^2 v_2^2 w_5^2 w_2^3 + 10w_7^2 w_4 c s^2 v_1^2 w_5^2 w_2^3 - 2w_7^2 w_4^3 v_3^2 v_1^2 w_5^2 w_2^2 - \\
& 3w_7^2 w_4^3 v_3^2 v_2^2 a_5^2 w_2^3 - 2w_7^2 w_4^3 c s^4 a_5 w_2^2 - 2w_7^2 w_4^2 v_3^2 v_1^2 w_5 w_2^3 - 2w_7^2 w_4 c s^4 a_5^2 w_2^3 - 4w_7^2 c s^2 v_2^2 w_5^2 w_2^3 - 3w_7^2 w_4^3 c s^2 v_3^2 w_5 w_2^3 - 8w_7^2 w_4^2 c s^2 v_1^2 w_5^2 w_2^3 + \\
& 14w_7^2 w_4^3 v_3^2 v_2^2 v_1^2 w_5^2 w_2^2 + w_7^2 w_4^3 c s^4 a_5 w_2^3 + 4w_7^2 w_4^3 c s^4 w_5 w_2^3 + 4w_7^2 w_4^3 v_3^2 v_1^2 w_5^2 w_2^2 - 4w_7^2 w_4 c s^2 v_1^2 w_5^2 w_2^2 + 8w_7^2 w_4^2 c s^2 v_3^2 w_5^2 w_2^2 + 2w_7^2 w_4^3 c s^2 v_1^2 w_5 w_2^2 - 14w_7^2 w_4^3 v_3^2 v_1^2 w_5^2 w_2^2 - \\
& 4w_7^2 w_4^2 c s^2 v_2^2 w_5^2 w_2^2 + 10w_7 w_4^2 c s^2 v_1^2 w_5^2 w_2^3 - 2w_7 w_4^3 v_3^2 v_1^2 w_5^2 w_2^2 + 2w_7^2 c s^2 v_1^2 w_5^2 w_2^3 - 4w_7 w_4^3 c s^2 v_3^2 w_5 w_2^2 - 2w_7^2 w_4^2 c s^4 w_5 w_2^2 + 4w_7^2 v_3^2 v_1^2 w_5^2 w_2^3 - \\
& 4w_7 w_4^2 c s^2 v_1^2 w_5^2 w_2^2 + 2w_7 w_4^2 c s^2 v_3^2 w_5^2 w_2^3 + 4w_7^2 w_4^2 c s^4 w_5 w_2^2 - 4w_7^2 w_4^2 c s^2 v_3^2 w_5 w_2 + 3w_7 w_4^3 v_3^2 v_1^2 w_5^2 w_2^3 - 4w_7 w_4 c s^2 v_1^2 w_5^2 w_2^3
\end{aligned}$$

$$\begin{aligned} C_{51} = & 6w_7^2 w_4^3 c s^2 w_2 - 18w_7^2 v_4^3 w_3^2 + 24w_7^2 w_4 c s^2 w_3^2 + 24w_7^2 v_4^3 w_2^2 - 30w_7^2 v_4^3 w_2^2 - 12w_4^7 c s^2 w_3^2 - 24w_7^2 w_4^2 v_3^2 w_3^2 + 22w_7^2 w_4^3 v_3^2 w_2^2 + w_7^2 w_4^3 c s^2 w_2^2 - \\ & 4w_7^2 w_3^3 v_3^2 w_3^2 - 6w_7^2 w_4^2 c s^2 w_2^2 + 24w_7 w_2^2 c s^2 w_3^2 + 12w_2^2 v_3^2 w_3^2 + 12w_7 w_4 v_3^2 w_3^2 + 24w_7 w_2^2 v_3^2 w_2^2 - 12w_7^2 c s^2 w_3^2 - 12w_2^2 w_4^2 c s^2 w_2^2 - 12w_7^2 w_4 c s^2 w_3^2 - \\ & 6w_7 w_4^3 c s^2 w_2^2 + 12w_7^2 w_4^2 c s^2 w_2^2 - 6w_3^4 v_3^2 w_3^2 + 22w_7 w_2^2 v_3^2 w_2^2 - 14w_7^2 w_4^2 c s^2 w_3^2 + 12w_7^2 w_4^3 v_3^2 + 6w_4^3 c s^2 w_3^2 - 48w_7^2 w_4^2 v_3^2 w_2^2 + 6w_7 w_4^3 v_3^2 w_3^2 \end{aligned}$$

$$\begin{aligned}
& \text{C52} = 12w_4^2cs^2w_5^2w_2^2 - 4w_4^3v_1^2w_5^2w_3^2 + 12v_1^2w_5^2w_3^2 + 24w_4^3cs^2w_5^2w_2 + 22w_4^3v_1^2w_5^2w_2^2 - 6w_4^4cs^2w_5^2w_3^2 + 24w_2^2v_1^2w_5^2w_2 + w_4^4cs^2w_5^2w_3^2 - 48w_2^4v_1^1w_5^2w_2^2 - 6w_3^4v_1^2w_3^2 - 18w_3^4v_1^2w_5^2w_2 + 22w_4^2v_1^2w_5^2w_3^2 - 14w_3^4cs^2w_5^2w_2^2 + 12w_3^4v_2^2w_2^2 + 24w_4^3cs^2w_5^2w_2 - 12w_4^4cs^2w_5^2w_3^2 - 6w_3^3cs^2w_5w_3^2 + 12w_3^3v_1^2w_5w_2 + 6w_4^4cs^2w_5^2w_3^2 - 24w_4^3v_1^2w_5w_2^2 + 24w_4v_1^2w_5^2w_2^2 - 12w_4^3cs^2w_5^2w_2^2 - 12w_4^3cs^2w_5^2w_3^2 + 6w_3^4v_1^2w_5w_2^2 + 6w_4^4cs^2w_5^2w_3^2 - 12w_3^4cs^2w_5w_2 - 30w_4v_1^2w_5^2w_3^2
\end{aligned}$$

$$\text{C}_{53} = -30w_7^2 w_4 c s^2 w_3 - 6w_7 w_3^4 c s^2 - 36w_7^2 w_4 v_3^2 w_3 + 6w_7 w_4^3 v_3^2 - 12w_4^2 v_3^2 w_3 - 30w_7 w_4^2 c s^2 w_3 + 12w_7^2 w_4 v_3^2 + 12w_2^2 w_4 c s^2 + w_7^2 w_4^3 v_3^2 w_3 - 2w_7^2 w_3^4 c s^2 w_3 - 12w_7 w_2^2 v_3^2 + 30w_7 w_4^2 v_3^2 w_3 + 12w_7 w_4^2 c s^2 + 12w_4^2 c s^2 w_3 + 12w_7 w_4 c s^2 w_3 + 12w_7^2 c s^2 w_3 - 6w_7^2 w_4^2 v_3^2 + 24w_2^2 v_3^2 w_3 - 18w_7 w_4^2 c s^2 - 12w_7 w_4 v_3^2 w_3 - 9w_7 w_4^3 v_3^2 w_3 - 6w_4^3 c s^2 w_3 + 22w_7^2 w_4^2 c s^2 w_3 + 8w_7^2 w_4 v_3^2 w_3 + 3w_7^2 w_4^3 c s^2 - w_7^2 w_4^3 v_3^2 + 6w_4^3 v_3^2 w_3 + 9w_7 w_4^3 c s^2 w_3$$

$$\begin{aligned}
C_{54} = & -2w_2^2w_3^3c_8^2w_2w_3^3 + 3w_2^2w_3^4v_3^2w_2^3 + 7w_2^2w_3^4v_3^2w_2^3w_2^2 + 6w_7w_4^2c_8^2w_2^3w_3^3 + w_7^2w_3^3c_8^2w_2^3w_3 + w_3^2c_8^2w_2^3w_3^3 + 2w_4^2c_8^2w_2^3w_3^3 - 10w_2^2w_4^2c_8^2w_2^3w_3^3 + \\
& 6w_7w_2^2c_8^2w_2^3w_3^2 + 2w_7w_2^2v_3^2w_2^3w_3^3 + 4w_7^2w_2^2v_3^2w_2^3w_3^2 + 2w_7w_2^2v_3^2w_2^3w_3^2 - 2w_7w_2^2c_8^2w_2^3w_3^2 + 3w_7^2w_3^2v_3^2w_2^3w_3^2 - 2w_7w_2^2v_3^2w_2^3w_3^3 + w_7^2w_4^2c_8^2w_2^3w_3^2 + \\
& w_7w_4^2c_8^2w_2^3w_3^2 - w_7w_3^2v_3^2w_2^3w_3^2 - 6w_7^2w_4^2c_8^2w_2^3w_3^3 + 4w_7^2w_4^2c_8^2w_2^3w_3^2 - 2w_7^2w_4^2c_8^2w_2^3w_2^2 + 8w_7^2w_4^2c_8^2w_2^3w_3^3 + w_7w_3^2c_8^2w_2^3w_3^2 - w_7w_3^2v_3^2w_2^3w_3^2 - \\
& w_8^2w_3^2v_3^2w_2^3w_3^2 + w_7^2w_3^2c_8^2w_2^3w_3^3 + 2w_7w_2^2v_3^2w_2^3w_3^2 - 2w_7w_4^2c_8^2w_2^3w_3^2 - 2w_4^2c_8^2w_2^3w_3^2 + 3w_7^2w_3^2v_3^2w_2^3w_3^2 - 2w_7w_3^2c_8^2w_2^3w_3^2 - \\
& 10w_7w_2^2v_3^2w_2^3w_3^2 + 6w_7w_2^2c_8^2w_2^3w_3^3 - 8w_2^2w_3^4v_3^2w_2^3w_2^3 - 6w_7w_2^2v_3^2w_2^3w_3^2 - 2w_7w_3^2c_8^2w_2^3w_3^2 + 7w_7w_3^2v_3^2w_2^3w_3^3 - w_4^2v_3^2w_2^3w_3^3 - 2w_2^2w_4c_8^2w_2^3w_3^2 + \\
& 3w_7w_4^2v_3^2w_2^3w_3^2 - 2w_7w_2^2c_8^2w_2^3w_3^3 - 8w_7w_2^2v_3^2w_2^3w_3^2 - 2w_7w_4c_8^2w_2^3w_3^3 + 6w_7^2w_4c_8^2w_2^3w_3^2 - 2w_7^2c_8^2w_2^3w_3^3 + 3w_7^2w_3^2v_3^2w_2^3w_3^2 + 2w_7^2v_3^2w_2^3w_3^3 - \\
& 7w_7w_4^2v_3^2w_2^3w_3^3 + w_7^2w_3^2c_8^2w_2^3w_3^3 + 2w_7w_4v_3^2w_2^3w_3^2 - 2w_7w_4c_8^2w_2^3w_3^2 + 3w_7w_4v_3^2w_2^3w_3^2 + 4w_7w_4^2v_3^2w_2^3w_3^3
\end{aligned}$$

$$\begin{aligned}
C_{55} = & -5\omega_7^2\omega_4^3v_3^2w_3 + 24\omega_7w_2^2v_3^2w_3^2 + 36\omega_7w_2^4cs^2w_3^3 - 12\omega_7^2w_4^3cs^2w_3^2 + 12\omega_4^2v_3^2w_3^3 - 12\omega_4^2cs^2w_3^3 + 24\omega_7^2w_4^3v_3^2w_3^2 - 36\omega_7w_4^2v_3^2w_3^3 - \\
& 24\omega_7w_2^4cs^2w_3^2 + 4\omega_2^2w_3^2cs^2w_3^3 + 36\omega_7^2w_4cs^2w_3^3 - 30\omega_7^2w_4^3v_3^2w_3 + 6\omega_7^2w_4^3cs^2w_3 - 24\omega_7^2w_4cs^2w_3^2 - 6\omega_7^2w_4v_3^2w_3^3 - 32\omega_7^2w_4^2cs^2w_3^3 + 12\omega_7w_4^3cs^2w_3^2 + \\
& 6\omega_4^3cs^2w_3^3 + 12\omega_7w_4^3v_3^2w_3^3 - 36\omega_7^2w_4^2v_3^2w_3^2 + 48\omega_7^2w_4^2cs^2w_3^2 - 12\omega_7w_4^3cs^2w_3^3 - 6\omega_4^3v_3^2w_3^3 - 12\omega_7w_4^3v_3^2w_3^2 + 16\omega_7^2w_4^2v_3^2w_3^3 - 12\omega_7^2cs^2w_3^3 - \\
& 12\omega_7^2w_4^2cs^2w_3 - 12\omega_7w_4cs^2w_3^3 + 12\omega_7w_4^3v_3^2w_3^2 + 24\omega_7^2w_4^2v_3^2w_3 + 12\omega_2^2w_3^2v_3^2
\end{aligned}$$

$$\begin{aligned}
C_{56} = & 6w_2^2 w_4^3 c s^2 w_2 - 24w_2^7 w_4 c s^2 w_2^2 - 6w_2^7 w_4 v_3^2 w_3^3 + 36w_2^7 w_4 c s^2 w_3^2 - 30w_2^7 w_4^3 v_3^2 w_2 - 12w_4^2 c s^2 w_3^2 - 36w_7 w_4^2 v_3^2 w_2^3 + 24w_2^7 w_4^3 v_3^2 w_2^2 + \\
& 4w_7^2 w_4^3 c s^2 w_2^3 - 24w_7 w_4^2 c s^2 w_2^2 + 24w_7 w_4^2 v_3^2 w_2^2 - 5w_7^2 w_4^3 v_3^2 w_2^3 - 12w_7^2 w_4^3 c s^2 w_2^2 + 36w_7 w_4^2 c s^2 w_2^3 + 12w_4^2 v_3^2 w_2^3 + 12w_7 w_4 v_3^2 w_2^3 + 24w_2^7 w_4^2 v_3^2 w_2 - \\
& 12w_2^7 c s^2 w_3^2 - 12w_2^7 w_2^2 c s^2 w_2 - 12w_7 w_4 c s^2 w_2^3 - 12w_7 w_4^3 c s^2 w_3^2 + 48w_7^2 w_4^2 c s^2 w_2^2 - 6w_4^3 v_3^2 w_2^3 + 16w_2^7 w_4^2 v_3^2 w_2^3 - 12w_7 w_4^3 v_3^2 w_2^2 + 12w_7 w_4^3 c s^2 w_2^2 - \\
& 32w_2^7 w_4^2 c s^2 w_3^2 + 12w_2^7 w_4^3 v_3^2 + 6w_4^3 c s^2 w_2^3 - 36w_2^7 w_4^2 v_3^2 w_2^2 + 12w_7 w_4^3 v_3^2 w_2^3
\end{aligned}$$

$$\begin{aligned} C_{57} = & -30w_2^2 w_2^2 w_3^3 + 6w_2^4 w_3^2 w_3 + 12w_2^4 w_3^2 w_3^2 + 28w_2^4 w_3^2 w_3^3 - 30w_3^4 w_2 w_3^3 + 12w_3^5 w_3^3 + 18w_3^3 w_2 w_3^2 - 30w_2^4 w_3^2 w_3^2 + 12w_3^4 w_3^2 - 42w_3^4 w_2^2 w_3^2 - \\ & 36w_4 w_2^3 w_3^3 + 18w_4 w_2^3 w_3^2 - 30w_3^4 w_3^2 w_3 + 24w_4^3 w_2^2 w_3^3 + 18w_4 w_2^2 w_3^3 + 24w_3^4 w_3^2 w_3^2 + 18w_3^4 w_2^2 w_3 + 12w_3^4 w_3^3 - 5w_3^4 w_2^3 w_3^3 + 6w_2^4 w_2 w_3^3 \end{aligned}$$

$$\begin{aligned}
C_{58} = & 4w_7w_4^2cs^4w_6^2w_3^2 - 8w_7w_4^2cs^2v_3^2w_6^3w_3^3 - w_7w_4^3cs^2v_3^2w_6^2w_3^3 - 2w_7w_4^2v_3^2v_2^2w_6w_3^3 - 4w_7^2cs^2v_3^2w_6^2w_3^3 + 2w_7^2w_3^3cs^2v_2^2w_3^3 + 2w_7w_3^3cs^2v_2^2w_6w_3^2 + \\
& 4w_7^2w_4^2cs^4w_6^2w_3^3 - 4w_7w_4cs^2v_2^2w_6^2w_2^3 + 14w_7w_4^3v_3^2v_2^2w_6^2w_3^3 + 4w_7^2w_4^2v_3^2v_2^2w_6w_3^2 + 2w_7w_4^3cs^2v_3^2w_6^2w_3^2 + 8w_7^2w_4^2cs^2v_2^2w_6^2w_3^2 - 2w_7w_4^2cs^4w_6^2w_3^2 - \\
& 2w_7w_4^3cs^4w_6^2w_3^3 - 3w_7w_4^3v_3^2v_2^2w_6^2w_3^3 + 10w_7w_4^3cs^2v_3^2w_6^2w_3 + 10w_7w_4cs^2v_2^2w_6^2w_3^3 - 12w_7w_4^2cs^4w_6^2w_3^2 - 4w_7w_4^3cs^2v_3^2w_6^2w_3^2 - w_7w_4^3cs^2v_2^2w_6w_3^2 - \\
& 8w_7w_4^2cs^2v_3^2w_6^2w_3^2 + 4w_7w_4^2cs^4w_6^2w_3 + w_7w_4^3cs^4w_6^2w_3^3 - 4w_7w_4^2cs^2v_2^2w_6^2w_3^2 + 4w_4^2v_3^2v_2^2w_6^2w_3^3 + 2w_7w_4^2cs^2v_3^2w_6w_3^3 - 4w_7w_4cs^2v_2^2w_6^2w_3^2 + \\
& 3w_7w_4^3v_3^2v_2^2w_6^2w_3^3 + 4w_7w_4^3cs^4w_6^2w_3^2 + 10w_7w_4^2cs^2v_3^2w_6^2w_3^3 + 4w_7w_4^3v_3^2v_2^2w_6^2w_3^2 - 2w_7w_4^2cs^4w_6^2w_3^2 + w_7w_4^3cs^2v_3^2w_6^2w_3^2 - 14w_7w_4^3v_3^2v_2^2w_6w_3^2 - \\
& w_7w_4^3cs^4w_6^2w_3^2 + 2w_4^2cs^2v_2^2w_6^2w_3^2 - 2w_7w_4^3v_3^2v_2^2w_6^2w_3^2 - 2w_7w_4^2cs^4w_6^2w_3^2 - 3w_7w_4^2cs^2v_3^2w_6w_3^2 - \\
& 10w_7w_4^2v_3^2v_2^2w_6^2w_3^2 + w_7w_4^3cs^4w_6^2w_3^3 + 2w_7w_4^3cs^2v_2^2w_6^2w_3^2 - 2w_7w_4^3v_3^2v_2^2w_6^2w_3^2 + 4w_7w_4^3v_3^2v_2^2w_6^2w_3^2 + 8w_7w_4^2cs^2v_3^2w_6^2w_3^2 - 4w_4^2cs^2v_2^2w_6^2w_3^2 + \\
& 4w_7w_4^2v_3^2v_2^2w_6^2w_3^2 + 10w_7w_4^3cs^2v_3^2w_6w_3^3 + 4w_7w_4^2w_4cs^2v_6^2w_3^2 + 12w_7w_4^2v_3^2v_2^2w_6^2w_3^2 - 2w_7w_4^2cs^2v_3^2w_6^2w_3^2 - 2w_7w_4^3v_3^2v_2^2w_6^2w_3^2 - 3w_7w_4^3cs^2v_2^2w_6^2w_3^2 - \\
& 2w_7w_4^3cs^4w_6^2w_3^2 + 4w_7w_4v_3^2v_2^2w_6^2w_3^2 - 4w_7w_4^3cs^2v_3^2w_6^2w_3^2 - 28w_7w_4^2v_3^2v_2^2w_6^2w_3^2 - 4w_7w_4^2cs^2v_2^2w_6w_3^2 + 4w_7w_4^2cs^2v_3^2w_6^2w_3^2 + 2w_7w_4^2cs^2v_2^2w_6^2w_3^2 - \\
& 4w_7w_4^3cs^2v_3^2w_6w_3^3 + 3w_7w_4^3v_3^2v_2^2w_6w_3^3 - 14w_7w_4^2v_3^2v_2^2w_6^2w_3^3 + w_7w_4^3cs^2v_2^2w_6^2w_3^3 + 4w_7w_4^2v_3^2v_2^2w_6^2w_3^3 + 2w_7w_4^2cs^2v_2^2w_6w_3^2 - 4w_7w_4^2cs^2v_3^2w_6^2w_3^2 + \\
& 14w_7w_4^2v_3^2v_2^2w_6^2w_3^2 - 2w_7w_4^3cs^2v_2^2w_6^2w_3^2 + 12w_7w_4^2v_3^2v_2^2w_6^2w_3^2 - 10w_7w_4^3v_3^2v_2^2w_6w_3^2 - 2w_7w_4^2cs^4w_6w_3^2 - 4w_7w_4^2cs^2v_3^2w_6^2w_3^2 +
\end{aligned}$$

$$\begin{aligned} C_{59} = & -4w_7^2 w_4^3 v_3^2 w_3^3 + 24w_7 w_4^2 c s^2 w_3^3 - 6w_7 w_4^3 c s^2 w_3^2 + 12w_4^2 v_3^2 w_3^3 - 12w_4^2 c s^2 w_3^3 + 22w_2^2 w_3^2 v_3^2 w_3^2 - 24w_7 w_4^2 v_3^2 w_3^3 + w_7^2 w_4^3 c s^2 w_3^3 + 24w_7^2 w_4 c s^2 w_3^3 + 24w_7^2 w_4 v_3^2 w_3^3 - 30w_7^2 w_4^3 v_3^2 w_3 + 6w_7^2 w_4^3 c s^2 w_3 - 18w_7^2 w_4 v_3^2 w_3^3 - 14w_7^2 w_4^2 c s^2 w_3^3 + 6w_4^3 c s^2 w_3^3 + 6w_7 w_4^3 v_3^2 w_3^3 - 48w_7^2 w_4^2 v_3^2 w_3^2 + 12w_7^2 w_4^2 c s^2 w_3^2 - 6w_7 w_4^3 c s^2 w_3^3 - 6w_4^3 v_3^2 w_3^3 + 22w_7^2 w_4^2 v_3^2 w_3^3 - 12w_7^2 c s^2 w_3^3 - 12w_7^2 w_4^2 c s^2 w_3^3 - 12w_7 w_4 c s^2 w_3^3 + 12w_7 w_4 v_3^2 w_3^3 + 24w_7^2 w_4^2 v_3^2 w_3 + 12w_7^2 w_4^3 v_3^2 \end{aligned}$$

$$\begin{aligned} C_{60} = & -6w_4^2cs^2w_2^2w_3^3 + 12w_3^2v_2^2w_6w_3 + 12w_4^2cs^2w_2^2w_3^2 + 24w_3^3cs^2w_2^2w_3 - 12w_3^2cs^2w_2^2 + 6w_3^3v_2^2w_6w_3^3 - 14w_4^3cs^2w_2^2w_3^2 - 30w_4v_2^2w_2^2w_3^3 + \\ & 12w_3^4v_2^2w_3^2 + w_3^3cs^2w_2^2w_3^2 - 24w_3^4v_2^2w_6w_3^2 - 6w_3^4v_2^2w_3^3 + 24w_4v_2^2w_2^2w_3^2 - 6w_4^3cs^2w_6w_3^3 + 22w_3^4v_2^2w_2^2w_3^2 + 6w_4^3cs^2w_3^3 + 6w_4cs^2w_2^2w_3^3 + 24w_2^2v_2^2w_2^2w_3 - \\ & 4w_3^4v_2^2w_6w_3^3 + 24w_3^4cs^2w_6w_3^2 + 12v_2^2w_6w_3^3 - 12w_4cs^2w_2^2w_3^2 - 12w_3^4cs^2w_2^2w_3^2 + 22w_4^2v_2^2w_2^2w_3^3 - 12w_3^4cs^2w_6w_3 - 48w_4^2v_2^2w_2^2w_3^2 - 18w_3^4v_2^2w_2^2w_3 \end{aligned}$$

$$\begin{aligned} C_{61} = & -36\omega_7^2 v_3^2 + 24\omega_7^2 c s^2 + 9\omega_7 w_4^3 c s^2 - 18w_4^3 v_3^2 + 12\omega_7^2 w_4 - 6\omega_3^3 c s^2 + 27\omega_7 w_3^3 v_3^2 - 11\omega_7^2 w_4^2 + 18\omega_7^2 w_4 v_3^2 - 48\omega_7^2 w_4 c s^2 + 12\omega_4^2 c s^2 - 108\omega_7 w_4^2 v_3^2 + \\ & \omega_7^2 w_4^3 - 36\omega_7 w_4^2 c s^2 + 36\omega_4^2 v_3^2 + 72\omega_7 w_4 v_3^2 - 9\omega_7 w_4^3 + 24\omega_7 w_4 c s^2 + 36\omega_7 w_4^2 + 15\omega_7^2 w_4^2 v_3^2 + 25\omega_7^2 w_4^2 c s^2 - 12\omega_4^2 - 24\omega_7 w_4 + 6w_4^3 - 2\omega_7^2 w_4^3 c s^2 - 3\omega_7^2 w_4^2 v_3^2 \end{aligned}$$

$$\begin{aligned}
C_{62} = & 6w_2^2 w_4^3 c s^2 w_2 - 12w_2^2 w_4 c s^2 w_2^2 + 7w_2^2 w_4^2 w_3^2 + 12w_2^2 w_4 v_3^2 w_3^2 - 3w_2^2 w_4^2 w_2^2 + 12w_7 w_4 w_3^2 + 36w_7 w_4 c s^2 w_3^2 - 12w_2^2 w_4^3 v_3^2 w_2 - 36w_4^2 c s^2 w_2^3 + \\
& 12w_7 w_4^2 v_3^2 w_2^3 + 6w_2^2 w_3^3 v_3^2 w_2^2 - w_7 w_3^4 w_3^2 + 6w_7 w_4^3 c s^2 w_3^2 - 24w_7 w_4^2 c s^2 w_2^2 - 12w_7 w_4^3 c s^2 w_2^2 + 72w_7 w_4^2 c s^2 w_3^2 + 12w_4^2 v_3^2 w_3^2 + w_7 w_4^3 w_2^2 - 3w_4^3 w_3^2 - \\
& 24w_7 w_4 v_3^2 w_3^2 + 6w_2^2 w_4^3 v_3^2 w_2 + 6w_7 w_4^3 w_3^2 - 12w_7^2 c s^2 w_3^2 - 12w_7^2 w_4^2 c s^2 w_2^2 - 3w_7 w_4^3 w_2^2 - 24w_7 w_4 c s^2 w_3^2 - 21w_7 w_4^2 w_3^2 - 24w_7 w_4^3 c s^2 w_3^2 + \\
& 36w_7^2 w_4^2 c s^2 w_2^2 - 6w_3^4 v_3^2 w_2^3 - 6w_2^2 w_4^2 v_3^2 w_3^2 + 6w_4^2 w_3^2 + 12w_7 w_4^3 c s^2 w_2^2 - 6w_7 w_4 w_3^2 - 36w_7^2 w_4^2 c s^2 w_3^2 + 6w_7 w_4^2 w_2^2 + 6w_7^2 w_4^3 v_3^2 + 18w_4^3 c s^2 w_3^2 - 6w_7^2 w_4^2 v_3^2 w_2^2
\end{aligned}$$

$$\begin{aligned} \textcolor{red}{C_{63}} = & 12w_7^2v_3^2 - 30w_7w_3^4cs^2 - 6w_3^4v_3^2 - 12w_7w_4 + 30w_3^4cs^2 - 6w_7w_3^4v_3^2 + 11w_7^2w_4^2 + 12w_7^2w_4v_3^2 + 18w_7^2w_4cs^2 - 60w_4^2cs^2 + 48w_7w_2^4v_3^2 - w_7^2w_4^3 + \\ & 96w_7w_2^4cs^2 + 12w_2^4v_3^2 - 60w_7w_4v_3^2 + 9w_7w_3^4 - 36w_7w_4cs^2 - 36w_7w_4^2 - 14w_7^2w_4v_3^2 - 26w_7^2w_4cs^2 + 12w_4^2 + 24w_7w_4 - 6w_4^3 + 4w_7^2w_4^3cs^2 + w_7^2w_4^3v_3^2 \end{aligned}$$

$$\begin{aligned}
C_{64} = & 6w_7^2 w_4^3 c s^2 w_2 - 24w_7^2 w_4 c s^2 w_2^2 + 3w_7^2 w_4^2 w_3^2 + 30w_7^2 w_4 v_3^2 w_3^2 - 6w_7^2 w_4^2 w_2^2 + 36w_7^2 w_4 c s^2 w_3^2 - 18w_7^2 w_3^3 v_3^2 w_2 - 12w_4^2 c s^2 w_3^2 - 12w_7 w_2^4 v_3^2 w_2^3 - \\
& w_7^2 w_4^3 w_2^3 + 4w_7^2 w_4 c s^2 w_3^2 - 24w_7 w_2^4 c s^2 w_2^2 - 24w_7 w_2^4 v_3^2 w_2^2 + 3w_7^2 w_3^3 v_3^2 w_2^3 - 12w_7^2 w_3^3 c s^2 w_2^2 + 36w_7 w_4^2 c s^2 w_3^2 + 12w_4^2 v_2^2 w_3^2 + 2w_7 w_3^3 w_2^2 + \\
& 12w_7 w_4 v_3^2 w_2^3 - 24w_7^2 v_3^2 w_3^2 + 3w_7 w_3^3 w_2^3 - 12w_7^2 c s^2 w_3^2 - 12w_2^2 w_4^2 c s^2 w_2 - 6w_7 w_4^3 w_2^2 - 12w_7 w_4 c s^2 w_3^2 - 6w_7 w_4^2 w_3^2 - 12w_7 w_3^3 c s^2 w_3^2 + 48w_7 w_4^2 c s^2 w_2^2 - \\
& 6w_3^4 v_3^2 w_2^3 - 12w_7^2 w_4^2 v_3^2 w_2^3 + 12w_7 w_4^3 v_3^2 w_2^2 + 12w_7 w_4 c s^2 w_2^2 - 32w_2^2 w_4^2 c s^2 w_3^2 + 12w_7 w_4^2 w_2^2 + 12w_7^2 w_4^3 v_3^2 + 6w_4^3 c s^2 w_3^2 + 12w_7^2 w_4^2 v_3^2 w_2^2
\end{aligned}$$

$$\begin{aligned}
C_{65} = & 72w_7w_4^2cs^2w_3 - 12w_7^2w_4^3cs^2w_3 + w_7^2w_4^3w_3^2 + 12w_4^2v_2^2w_3^3 - 36w_2^2cs^2w_3 + 6w_7w_4^3v_3^2w_3^2 + 12w_7w_4^2v_3^2w_3^3 - w_7w_3^3w_3^3 - 24w_7w_4^2cs^2w_3^2 + \\
& 6w_7w_3^3cs^2w_3^3 + 36w_7w_4cs^2w_3^3 + 12w_7w_4w_3^3 - 3w_7w_4^2w_3^2 - 12w_7^2w_4^3v_3^2w_3 + 6w_7w_4^3cs^2w_3 + 7w_7^2w_4^2w_3^3 - 12w_7w_4cs^2w_3^2 + 12w_7w_4v_3^2w_3^3 + \\
& 6w_7w_2^2w_3^2 - 36w_7w_4^2cs^2w_3^3 - 6w_7^2w_4w_3^3 + 12w_7w_4^3cs^2w_3^2 + 18w_4^3cs^2w_3^3 - 6w_7^2w_4^3v_3^2w_3^2 + 36w_7w_4^2cs^2w_3^2 - 24w_7w_4^3cs^2w_3^3 - 21w_7w_4^2w_3^3 - 6w_4^3v_3^2w_3^3 - \\
& 6w_7w_4^2v_3^2w_3^3 + 6w_4^2w_3^3 - 12w_7^2cs^2w_3^3 - 3w_7w_4^3w_3^2 - 12w_7w_4^2cs^2w_3 - 24w_7w_4cs^2w_3^3 - 24w_7w_4v_3^2w_3^3 - 3w_4^3w_3^3 + 6w_2^2w_4^2v_3^2w_3 + 6w_7w_4^3v_3^2 + 6w_7w_4^3w_3^3
\end{aligned}$$

$$C_{66} = 12w_7^2v_3^2 - 30w_7w_4^3cs^2 - 6w_4^3v_3^2 - 12w_7^2w_4 + 30w_4^3cs^2 - 6w_7w_4^3v_3^2 + 11w_7^2w_4^2 + 12w_7^2w_4v_3^2 + 18w_7^2w_4cs^2 - 60w_4^2cs^2 + 48w_7w_4^2v_3^2 - w_7^2w_4^3 + 96w_7w_4^2cs^2 + 12w_4^2v_3^2 - 60w_7w_4v_3^2 + 9w_7w_4^3 - 36w_7w_4cs^2 - 36w_7w_4^2 - 14w_7^2w_4^2v_3^2 - 26w_7^2w_4^2cs^2 + 12w_4^2 + 24w_7w_4 - 6w_4^3 + 4w_7^2w_4^3cs^2 + w_7^2w_4^3v_3^2$$

$$+ 24w_7w_2^2cs^2w_3^3 + 4w_7w_2^3cs^2w_3^3 + 36w_7^2w_4cs^2w_3^3 - 6w_7^2w_4^2w_3^2 - 18w_7^2w_4^3v_2^2w_3 + 6w_7w_2^3cs^2w_3 + 3w_7^2w_4^2w_3^2 - 24w_7^2w_4cs^2w_3^2 + 30w_7^2w_4v_3w_3^3 + \\ 12w_7w_2^2w_3^2 - 32w_7^2w_4^2cs^2w_3^3 + 12w_7w_4^3cs^2w_3^2 + 6w_7^2w_4^2v_2^2w_3^2 + 12w_7^2w_4^2v_3^2w_3^2 + 48w_7^2w_4^2cs^2w_3^2 - 12w_7w_4^3cs^2w_3^2 - 6w_7w_4^2w_3^3 - 6w_4^3v_2^2w_3^3 + \\ 12w_7w_4^3v_3^2w_3^2 - 12w_7^2w_4^2v_2^2w_3^3 - 12w_7^2w_4^2cs^2w_3^3 - 6w_7w_4^3w_3^2 - 12w_7^2w_4^2cs^2w_3 - 12w_7w_4cs^2w_3^2 + 12w_7w_4v_2^2w_3^3 + 12w_7^2w_4^3v_3^2 - 24w_7^2v_3^2w_3^3 + 3w_7w_4^3w_3^2$$

$$\begin{aligned} C_{68} = & -12w_7w_4cs^2v_3 - 6w_7w_4cs + 3w_7w_4v_3 - 3w_7w_4c_3 - 3w_7w_4cs + 3w_7w_4c_3 - 12w_7w_4cs \\ & v_3 + 24w_7w_4cs + 12w_7w_4cs + 108w_4cs^2v_3 - \\ & 72w_7w_3^2cs^2v_3^2 - 72w_7w_4v_3^2 + 24w_2^2w_4^2cs^4 - 12w_7w_4^2v_4^2 + 24w_7w_4cs^2 + 72w_4^2v_3^2 - 36w_7w_4cs^2v_3^2 - 48w_7w_4cs^4 - 24w_7w_4cs^2 - 24w_7w_4^2cs^4 + 12w_7w_4^2v_3^2 - \\ & 72w_4^2v_3^2 - 8w_7w_4^2cs^2 + 72w_7w_4v_3^2 + 24w_7w_4^2cs^4 + 144w_7w_4cs^2v_3^2 - 216w_4^2cs^2v_3^2 - 30w_7w_4^2v_3^2 + w_7w_4^2cs^2 - 3w_7w_4^2v_3^2 + 6w_7w_4^2cs^4 + 36w_4^2v_3^2 + 6w_7w_4^2cs^2v_3^2 \end{aligned}$$

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$$\begin{aligned} \textcolor{red}{C_{69}} = & -12\omega_7^2 v_3^2 + 24\omega_7^2 c s^2 - 24\omega_7 w_4^3 c s^2 + 42\omega_3^3 v_3^2 + 6\omega_7^2 w_4 + 30w_4^3 c s^2 - 24\omega_7 w_4^3 v_3^2 + 2w_7^2 w_4^2 - 12\omega_7^2 w_4 v_3^2 - 30\omega_7^2 w_4 c s^2 - 60\omega_7^2 c s^2 + 24\omega_7 w_4^2 v_3^2 - \\ & \omega_7^2 w_4^3 + 72\omega_7 w_4^2 c s^2 - 84\omega_4^2 v_3^2 + 60\omega_7 w_4 v_3^2 + 12\omega_7 w_4^3 - 12\omega_7 w_4 c s^2 - 24\omega_7 w_4^2 + 2w_7^2 w_4^2 v_3^2 - 2w_7^2 w_4^2 c s^2 + 36w_4^2 - 12\omega_7 w_4 - 18w_4^3 + \omega_7^2 w_4^3 c s^2 + 2w_7^2 w_4^3 v_3^2 \end{aligned}$$

### 3 Comparison of SRT, MRT, and CLBM

### 3.1 Conservation of mass equation

$$\begin{aligned}
& + C_{D_x^2 D_y D_z v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_t D_y^2 D_z v_2}^{(0)} \delta_l^3 \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + C_{D_t D_y^2 D_z v_3}^{(0)} \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + \\
C_{D_x D_y^2 D_z \rho}^{(0)} & \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
C_{D_y^3 D_z \rho}^{(0)} & \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_t^2 D_z^2 v_3}^{(0)} \delta_l^2 \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + C_{D_t D_x D_z^2 v_1}^{(0)} \delta_l^3 \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + \\
C_{D_t D_x D_z^2 v_3}^{(0)} & \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + C_{D_x^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{D_t D_y D_z^2 v_2}^{(0)} \delta_l^3 \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
+ C_{D_t D_y D_z^2 v_3}^{(0)} & \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
C_{D_x D_y D_z^2 v_3}^{(0)} & \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_y^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{D_t D_z^3 v_3}^{(0)} \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_3^3} + \\
C_{D_x D_z^3 \rho}^{(0)} & \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{D_y D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
C_{D_y D_z^3 v_3}^{(0)} & \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{D_z^4 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{D_z^4 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

**coefficient**  $C_{D_x \rho, D_t v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t}$ :

$$C_{D_x \rho, D_t v_1}^{(0), SRT} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{D_x \rho, D_t v_1}^{(0), MRT1} = (-2 + \omega_2) \frac{1}{2\omega_2}$$

$$C_{D_x \rho, D_t v_1}^{(0), MRT2} = C_{D_x \rho, D_t v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_t v_1}^{(0), CLB1} = C_{D_x \rho, D_t v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_t v_1}^{(0), CLB2} = C_{D_x \rho, D_t v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x \rho, D_x v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1}$ :

$$C_{D_x \rho, D_x v_1}^{(0), SRT} = (-2 + \omega) \frac{v_1}{2\omega}$$

$$C_{D_x \rho, D_x v_1}^{(0), MRT1} = (-2 + \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_x \rho, D_x v_1}^{(0), MRT2} = C_{D_x \rho, D_x v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_x v_1}^{(0), CLB1} = C_{D_x \rho, D_x v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_x v_1}^{(0), CLB2} = C_{D_x \rho, D_x v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x v_1, D_x v_1}^{(0)}$  **at**  $\left(\frac{\partial v_1}{\partial x_1}\right)^2$ :

$$C_{D_x v_1, D_x v_1}^{(0), SRT} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_x v_1, D_x v_1}^{(0), MRT1} = (-2 + \omega_2) \frac{\rho}{2\omega_2}$$

$$C_{D_x v_1, D_x v_1}^{(0), MRT2} = C_{D_x v_1, D_x v_1}^{(0), MRT1}$$

$$C_{D_x v_1, D_x v_1}^{(0), CLB1} = C_{D_x v_1, D_x v_1}^{(0), MRT1}$$

$$C_{D_x v_1, D_x v_1}^{(0), CLB2} = C_{D_x v_1, D_x v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x \rho, D_y v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2}$ :

$$C_{D_x \rho, D_y v_1}^{(0), SRT} = (2 - \omega) \frac{v_2}{2\omega}$$

$$C_{D_x \rho, D_y v_1}^{(0), MRT1} = (2 - \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_x \rho, D_y v_1}^{(0), MRT2} = C_{D_x \rho, D_y v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_y v_1}^{(0), CLBM1} = C_{D_x \rho, D_y v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_y v_1}^{(0), CLBM2} = C_{D_x \rho, D_y v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x \rho, D_y v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2}$ :

$$C_{D_x \rho, D_y v_2}^{(0), SRT} = (2 - \omega) \frac{v_1}{\omega}$$

$$C_{D_x \rho, D_y v_2}^{(0), MRT1} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{v_1}{\omega_2 \omega_3}$$

$$C_{D_x \rho, D_y v_2}^{(0), MRT2} = C_{D_x \rho, D_y v_2}^{(0), MRT1}$$

$$C_{D_x \rho, D_y v_2}^{(0), CLBM1} = C_{D_x \rho, D_y v_2}^{(0), MRT1}$$

$$C_{D_x \rho, D_y v_2}^{(0), CLBM2} = C_{D_x \rho, D_y v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_x v_1, D_y v_2}^{(0)}$  **at**  $\frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2}$ :

$$C_{D_x v_1, D_y v_2}^{(0), SRT} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_x v_1, D_y v_2}^{(0), MRT1} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{\rho}{\omega_2 \omega_3}$$

$$C_{D_x v_1, D_y v_2}^{(0), MRT2} = C_{D_x v_1, D_y v_2}^{(0), MRT1}$$

$$C_{D_x v_1, D_y v_2}^{(0), CLBM1} = C_{D_x v_1, D_y v_2}^{(0), MRT1}$$

$$C_{D_x v_1, D_y v_2}^{(0), CLBM2} = C_{D_x v_1, D_y v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_x \rho, D_z v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3}$ :

$$C_{D_x \rho, D_z v_1}^{(0), SRT} = (2 - \omega) \frac{v_3}{2\omega}$$

$$C_{D_x \rho, D_z v_1}^{(0), MRT1} = (2 - \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_x \rho, D_z v_1}^{(0), MRT2} = C_{D_x \rho, D_z v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_z v_1}^{(0), CLBM1} = C_{D_x \rho, D_z v_1}^{(0), MRT1}$$

$$C_{D_x \rho, D_z v_1}^{(0), CLBM2} = C_{D_x \rho, D_z v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x \rho, D_z v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_x \rho, D_z v_3}^{(0), SRT} = (2 - \omega) \frac{v_1}{\omega}$$

$$C_{D_x \rho, D_z v_3}^{(0), MRT1} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1}{\omega_4 \omega_2}$$

$$C_{D_x \rho, D_z v_3}^{(0), MRT2} = C_{D_x \rho, D_z v_3}^{(0), MRT1}$$

$$C_{D_x \rho, D_z v_3}^{(0), CLBM1} = C_{D_x \rho, D_z v_3}^{(0), MRT1}$$

$$C_{D_x \rho, D_z v_3}^{(0), CLBM2} = C_{D_x \rho, D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_x v_1, D_z v_3}^{(0)}$  **at**  $\frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3}$ :

$$C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{\rho}{\omega_4 \omega_2}$$

$$C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{MRT2}} = C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{CLBM1}} = C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{CLBM2}} = C_{\text{D}_x v_1, \text{D}_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\text{D}_y \rho, \text{D}_t v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t}$ :

$$C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{1}{2\omega_3}$$

$$C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{MRT2}} = C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{CLBM1}} = C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{CLBM2}} = C_{\text{D}_y \rho, \text{D}_t v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\text{D}_y \rho, \text{D}_x v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1}$ :

$$C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{\omega}$$

$$C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{MRT1}} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{v_2}{\omega_2 \omega_3}$$

$$C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{MRT2}} = C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{CLBM1}} = C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{CLBM2}} = C_{\text{D}_y \rho, \text{D}_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\text{D}_y \rho, \text{D}_x v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1}$ :

$$C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{2\omega}$$

$$C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{MRT2}} = C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{CLBM1}} = C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{CLBM2}} = C_{\text{D}_y \rho, \text{D}_x v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\text{D}_y \rho, \text{D}_y v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2}$ :

$$C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_2}{2\omega}$$

$$C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{MRT2}} = C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{CLBM1}} = C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{CLBM2}} = C_{\text{D}_y \rho, \text{D}_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y v_2, D_y v_2}^{(0)}$  **at**  $\left(\frac{\partial v_2}{\partial x_2}\right)^2$ :

$$C_{D_y v_2, D_y v_2}^{(0), SRT} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_y v_2, D_y v_2}^{(0), MRT1} = (-2 + \omega_3) \frac{\rho}{2\omega_3}$$

$$C_{D_y v_2, D_y v_2}^{(0), MRT2} = C_{D_y v_2, D_y v_2}^{(0), MRT1}$$

$$C_{D_y v_2, D_y v_2}^{(0), CLBM1} = C_{D_y v_2, D_y v_2}^{(0), MRT1}$$

$$C_{D_y v_2, D_y v_2}^{(0), CLBM2} = C_{D_y v_2, D_y v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_y \rho, D_z v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3}$ :

$$C_{D_y \rho, D_z v_2}^{(0), SRT} = (2 - \omega) \frac{v_3}{2\omega}$$

$$C_{D_y \rho, D_z v_2}^{(0), MRT1} = (2 - \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_y \rho, D_z v_2}^{(0), MRT2} = C_{D_y \rho, D_z v_2}^{(0), MRT1}$$

$$C_{D_y \rho, D_z v_2}^{(0), CLBM1} = C_{D_y \rho, D_z v_2}^{(0), MRT1}$$

$$C_{D_y \rho, D_z v_2}^{(0), CLBM2} = C_{D_y \rho, D_z v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_y \rho, D_z v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_y \rho, D_z v_3}^{(0), SRT} = (2 - \omega) \frac{v_2}{\omega}$$

$$C_{D_y \rho, D_z v_3}^{(0), MRT1} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2}{\omega_4 \omega_3}$$

$$C_{D_y \rho, D_z v_3}^{(0), MRT2} = C_{D_y \rho, D_z v_3}^{(0), MRT1}$$

$$C_{D_y \rho, D_z v_3}^{(0), CLBM1} = C_{D_y \rho, D_z v_3}^{(0), MRT1}$$

$$C_{D_y \rho, D_z v_3}^{(0), CLBM2} = C_{D_y \rho, D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_y v_2, D_z v_3}^{(0)}$  **at**  $\frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_y v_2, D_z v_3}^{(0), SRT} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_y v_2, D_z v_3}^{(0), MRT1} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{\rho}{\omega_4 \omega_3}$$

$$C_{D_y v_2, D_z v_3}^{(0), MRT2} = C_{D_y v_2, D_z v_3}^{(0), MRT1}$$

$$C_{D_y v_2, D_z v_3}^{(0), CLBM1} = C_{D_y v_2, D_z v_3}^{(0), MRT1}$$

$$C_{D_y v_2, D_z v_3}^{(0), CLBM2} = C_{D_y v_2, D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_z \rho, D_t v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t}$ :

$$C_{D_z \rho, D_t v_3}^{(0), SRT} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{D_z \rho, D_t v_3}^{(0), MRT1} = (-2 + \omega_4) \frac{1}{2\omega_4}$$

$$C_{D_z \rho, D_t v_3}^{(0), MRT2} = C_{D_z \rho, D_t v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_t v_3}^{(0), CLBM1} = C_{D_z \rho, D_t v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_x v_3}^{(0), CLBM2} = C_{D_z \rho, D_x v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_z \rho, D_x v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1}$ :

$$C_{D_z \rho, D_x v_1}^{(0), SRT} = (2 - \omega) \frac{v_3}{\omega}$$

$$C_{D_z \rho, D_x v_1}^{(0), MRT1} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3}{\omega_4 \omega_2}$$

$$C_{D_z \rho, D_x v_1}^{(0), MRT2} = C_{D_z \rho, D_x v_1}^{(0), MRT1}$$

$$C_{D_z \rho, D_x v_1}^{(0), CLBM1} = C_{D_z \rho, D_x v_1}^{(0), MRT1}$$

$$C_{D_z \rho, D_x v_1}^{(0), CLBM2} = C_{D_z \rho, D_x v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_z \rho, D_x v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1}$ :

$$C_{D_z \rho, D_x v_3}^{(0), SRT} = (2 - \omega) \frac{v_1}{2\omega}$$

$$C_{D_z \rho, D_x v_3}^{(0), MRT1} = (2 - \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_z \rho, D_x v_3}^{(0), MRT2} = C_{D_z \rho, D_x v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_x v_3}^{(0), CLBM1} = C_{D_z \rho, D_x v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_x v_3}^{(0), CLBM2} = C_{D_z \rho, D_x v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_z \rho, D_y v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2}$ :

$$C_{D_z \rho, D_y v_2}^{(0), SRT} = (2 - \omega) \frac{v_3}{\omega}$$

$$C_{D_z \rho, D_y v_2}^{(0), MRT1} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_3}{\omega_4 \omega_3}$$

$$C_{D_z \rho, D_y v_2}^{(0), MRT2} = C_{D_z \rho, D_y v_2}^{(0), MRT1}$$

$$C_{D_z \rho, D_y v_2}^{(0), CLBM1} = C_{D_z \rho, D_y v_2}^{(0), MRT1}$$

$$C_{D_z \rho, D_y v_2}^{(0), CLBM2} = C_{D_z \rho, D_y v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_z \rho, D_y v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2}$ :

$$C_{D_z \rho, D_y v_3}^{(0), SRT} = (2 - \omega) \frac{v_2}{2\omega}$$

$$C_{D_z \rho, D_y v_3}^{(0), MRT1} = (2 - \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_z \rho, D_y v_3}^{(0), MRT2} = C_{D_z \rho, D_y v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_y v_3}^{(0), CLBM1} = C_{D_z \rho, D_y v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_y v_3}^{(0), CLBM2} = C_{D_z \rho, D_y v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_z \rho, D_z v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_z \rho, D_z v_3}^{(0), SRT} = (-2 + \omega) \frac{v_3}{2\omega}$$

$$C_{D_z \rho, D_z v_3}^{(0), MRT1} = (-2 + \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_z \rho, D_z v_3}^{(0), MRT2} = C_{D_z \rho, D_z v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_z v_3}^{(0), CLBM1} = C_{D_z \rho, D_z v_3}^{(0), MRT1}$$

$$C_{D_z \rho, D_z v_3}^{(0), CLBM2} = C_{D_z \rho, D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_z v_3, D_z v_3}^{(0)}$  **at**  $\left(\frac{\partial v_3}{\partial x_3}\right)^2$ :

$$C_{D_z v_3, D_z v_3}^{(0), SRT} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_z v_3, D_z v_3}^{(0), MRT1} = (-2 + \omega_4) \frac{\rho}{2\omega_4}$$

$$C_{D_z v_3, D_z v_3}^{(0), MRT2} = C_{D_z v_3, D_z v_3}^{(0), MRT1}$$

$$C_{D_z v_3, D_z v_3}^{(0), CLBM1} = C_{D_z v_3, D_z v_3}^{(0), MRT1}$$

$$C_{D_z v_3, D_z v_3}^{(0), CLBM2} = C_{D_z v_3, D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_t D_x v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial t \partial x_1}$ :

$$C_{D_t D_x v_1}^{(0), SRT} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_x v_1}^{(0), MRT1} = (-2 + \omega_2) \frac{\rho}{2\omega_2}$$

$$C_{D_t D_x v_1}^{(0), MRT2} = C_{D_t D_x v_1}^{(0), MRT1}$$

$$C_{D_t D_x v_1}^{(0), CLBM1} = C_{D_t D_x v_1}^{(0), MRT1}$$

$$C_{D_t D_x v_1}^{(0), CLBM2} = C_{D_t D_x v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x^2 \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_1^2}$ :

$$C_{D_x^2 \rho}^{(0), SRT} = (-2 + \omega) \frac{cs^2}{2\omega}$$

$$C_{D_x^2 \rho}^{(0), MRT1} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

$$C_{D_x^2 \rho}^{(0), MRT2} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

$$C_{D_x^2 \rho}^{(0), CLBM1} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

$$C_{D_x^2 \rho}^{(0), CLBM2} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

**coefficient**  $C_{D_x^2 v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial x_1^2}$ :

$$C_{D_x^2 v_1}^{(0), SRT} = (-2 + \omega) \frac{v_1 \rho}{2\omega}$$

$$C_{D_x^2 v_1}^{(0), MRT1} = (-2 + \omega_2) \frac{v_1 \rho}{2\omega_2}$$

$$C_{D_x^2 v_1}^{(0), MRT2} = C_{D_x^2 v_1}^{(0), MRT1}$$

$$C_{D_x^2 v_1}^{(0), CLBM1} = C_{D_x^2 v_1}^{(0), MRT1}$$

$$C_{D_x^2 v_1}^{(0), CLBM2} = C_{D_x^2 v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_t D_y v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial t \partial x_2}$ :

$$C_{D_t D_y v_2}^{(0), SRT} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{\rho}{2\omega_3}$$

$$C_{D_t D_y v_2}^{(0), \text{MRT2}} = C_{D_t D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y v_2}^{(0), \text{CLBM1}} = C_{D_t D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y v_2}^{(0), \text{CLBM2}} = C_{D_t D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 v_2}{\omega}$$

$$C_{D_x D_y \rho}^{(0), \text{MRT1}} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{v_1 v_2}{\omega_2 \omega_3}$$

$$C_{D_x D_y \rho}^{(0), \text{MRT2}} = C_{D_x D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y \rho}^{(0), \text{CLBM1}} = C_{D_x D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y \rho}^{(0), \text{CLBM2}} = C_{D_x D_y \rho}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_x D_y v_1}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_x D_y v_1}^{(0), \text{MRT2}} = C_{D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(0), \text{CLBM1}} = C_{D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_1}^{(0), \text{CLBM2}} = C_{D_x D_y v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 \rho}{2\omega}$$

$$C_{D_x D_y v_2}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1 \rho}{2\omega_2}$$

$$C_{D_x D_y v_2}^{(0), \text{MRT2}} = C_{D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(0), \text{CLBM1}} = C_{D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(0), \text{CLBM2}} = C_{D_x D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y^2 \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_2^2}$ :

$$C_{D_y^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{cs^2}{2\omega}$$

$$C_{D_y^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{MRT2}} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{CLBM1}} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{CLBM2}} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

**coefficient**  $C_{D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial x_2^2}$ :

$$C_{D_y^2 v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_y^2 v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(0), \text{CLBM1}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_z v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial t \partial x_3}$ :

$$C_{D_t D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho}{2\omega_4}$$

$$C_{D_t D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_z \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$ :

$$C_{D_x D_z \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 v_3}{\omega}$$

$$C_{D_x D_z \rho}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1 v_3}{\omega_4 \omega_2}$$

$$C_{D_x D_z \rho}^{(0), \text{MRT2}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z \rho}^{(0), \text{CLBM1}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z \rho}^{(0), \text{CLBM2}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_z v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial x_1 \partial x_3}$ :

$$C_{D_x D_z v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho v_3}{2\omega}$$

$$C_{D_x D_z v_1}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{\rho v_3}{2\omega_4}$$

$$C_{D_x D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_z v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial x_1 \partial x_3}$ :

$$C_{D_x D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 \rho}{2\omega}$$

$$C_{D_x D_z v_3}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1 \rho}{2\omega_2}$$

$$C_{D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(0), CLBM1} = C_{D_x D_z v_3}^{(0), MRT1}$$

$$C_{D_x D_z v_3}^{(0), CLBM2} = C_{D_x D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_y D_z \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$ :

$$C_{D_y D_z \rho}^{(0), SRT} = (2 - \omega) \frac{v_2 v_3}{\omega}$$

$$C_{D_y D_z \rho}^{(0), MRT1} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2 v_3}{\omega_4 \omega_3}$$

$$C_{D_y D_z \rho}^{(0), MRT2} = C_{D_y D_z \rho}^{(0), MRT1}$$

$$C_{D_y D_z \rho}^{(0), CLBM1} = C_{D_y D_z \rho}^{(0), MRT1}$$

$$C_{D_y D_z \rho}^{(0), CLBM2} = C_{D_y D_z \rho}^{(0), MRT1}$$

**coefficient**  $C_{D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial x_2 \partial x_3}$ :

$$C_{D_y D_z v_2}^{(0), SRT} = (2 - \omega) \frac{\rho v_3}{2\omega}$$

$$C_{D_y D_z v_2}^{(0), MRT1} = (2 - \omega_4) \frac{\rho v_3}{2\omega_4}$$

$$C_{D_y D_z v_2}^{(0), MRT2} = C_{D_y D_z v_2}^{(0), MRT1}$$

$$C_{D_y D_z v_2}^{(0), CLBM1} = C_{D_y D_z v_2}^{(0), MRT1}$$

$$C_{D_y D_z v_2}^{(0), CLBM2} = C_{D_y D_z v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial x_2 \partial x_3}$ :

$$C_{D_y D_z v_3}^{(0), SRT} = (2 - \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_y D_z v_3}^{(0), MRT1} = (2 - \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_3}^{(0), MRT2} = C_{D_y D_z v_3}^{(0), MRT1}$$

$$C_{D_y D_z v_3}^{(0), CLBM1} = C_{D_y D_z v_3}^{(0), MRT1}$$

$$C_{D_y D_z v_3}^{(0), CLBM2} = C_{D_y D_z v_3}^{(0), MRT1}$$

**coefficient**  $C_{D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_2^2}$ :

$$C_{D_z^2 \rho}^{(0), SRT} = (-2 + \omega) \frac{c s^2}{2\omega}$$

$$C_{D_z^2 \rho}^{(0), MRT1} = (-2 + \omega_4) \frac{c s^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), MRT2} = (-2 + \omega_4) \frac{c s^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), CLBM1} = (-2 + \omega_4) \frac{c s^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), CLBM2} = (-2 + \omega_4) \frac{c s^2}{2\omega_4}$$

**coefficient**  $C_{D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial x_2^2}$ :

$$C_{D_z^2 v_3}^{(0), SRT} = (-2 + \omega) \frac{\rho v_3}{2\omega}$$

$$C_{D_z^2 v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho v_3}{2\omega_4}$$

$$C_{D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t^2 D_x v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial t^2 \partial x_1}$ :

$$C_{D_t^2 D_x v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{MRT1}} = (12 + \omega_2^2 - 12\omega_2) \frac{\rho}{12\omega_2^2}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{MRT2}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x^2 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial t \partial x_2^2}$ :

$$C_{D_t D_x^2 v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 \rho}{6\omega^2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{MRT1}} = (12 + \omega_5 \omega_2 - 6\omega_5 - 6\omega_2) \frac{v_1 \rho}{6\omega_5 \omega_2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{CLBM1}} = (12 + \omega_2^2 - 12\omega_2) \frac{v_1 \rho}{6\omega_2^2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 v_1}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_x^3 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1^3}$ :

$$C_{D_x^3 \rho}^{(0), \text{SRT}} = (6 - 3\omega^2 cs^2 - \omega^2 v_1^2 - 6v_1^2 - 18cs^2 - 6\omega + \omega^2 + 6\omega v_1^2 + 18\omega cs^2) \frac{v_1}{6\omega^2}$$

$$C_{D_x^3 \rho}^{(0), \text{MRT1}} = (15\omega_5 \omega_2 cs^2 + \omega_5 \omega_2^2 + 3\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2 + 3\omega_2^2 cs^2 - \omega_5 v_1^2 \omega_2^2 - 3\omega_2^2 - 6v_1^2 \omega_2 + 6\omega_2 - 6\omega_2 cs^2 + 3v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2) \frac{v_1}{6\omega_5 \omega_2^2}$$

$$C_{D_x^3 \rho}^{(0), \text{MRT2}} = (-3cs^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 + 3\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2 + 15cs^2 \omega_5 \omega_2 - \omega_5 v_1^2 \omega_2^2 - 3\omega_2^2 - 6cs^2 \omega_2 - 6v_1^2 \omega_2 + 6\omega_2 - 12cs^2 \omega_5 + 3v_1^2 \omega_2^2 + 3cs^2 \omega_2^2) \frac{v_1}{6\omega_5 \omega_2^2}$$

$$C_{D_x^3 \rho}^{(0), \text{CLBM1}} = (6 + 3\omega_5 v_1^2 - \omega_5 v_1^2 \omega_2 + 9\omega_5 cs^2 + \omega_5 \omega_2 - 6v_1^2 + 9\omega_2 cs^2 - 18cs^2 - 3\omega_5 + 3v_1^2 \omega_2 - 3\omega_2 - 3\omega_5 \omega_2 cs^2) \frac{v_1}{6\omega_5 \omega_2}$$

$$C_{D_x^3 \rho}^{(0), \text{CLBM2}} = (6 + 3\omega_5 v_1^2 - \omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2 cs^2 + \omega_5 \omega_2 - 6v_1^2 - 3\omega_5 + 3v_1^2 \omega_2 - 3\omega_2 + 9\omega_2 cs^2 - 18cs^2 + 9\omega_5 cs^2) \frac{v_1}{6\omega_5 \omega_2}$$

**coefficient**  $C_{D_x^3 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1^3}$ :

$$C_{D_x^3 v_1}^{(0), \text{SRT}} = (12 - 3\omega^2 cs^2 - 5\omega^2 v_1^2 - 24v_1^2 - 24cs^2 - 12\omega + 2\omega^2 + 24\omega v_1^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^3 v_1}^{(0), \text{MRT1}} =$$

$$(18\omega_5 \omega_2 cs^2 - 12\omega_5 v_1^2 + 2\omega_5 \omega_2^2 + 18\omega_5 v_1^2 \omega_2 - 6\omega_5 \omega_2 + 6\omega_2^2 cs^2 - 5\omega_5 v_1^2 \omega_2^2 - 6\omega_2^2 - 12v_1^2 \omega_2 + 12\omega_2 - 12\omega_2 cs^2 + 6v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$\begin{aligned}
C_{D_x^3 v_1}^{(0), \text{MRT2}} &= \\
(-12\omega_5 v_1^2 - 3cs^2\omega_5\omega_2^2 + 2\omega_5\omega_2^2 + 18\omega_5 v_1^2\omega_2 - 6\omega_5\omega_2 + 18cs^2\omega_5\omega_2 - 5\omega_5 v_1^2\omega_2^2 - 6\omega_2^2 - 12cs^2\omega_2 - 12v_1^2\omega_2 + 12\omega_2 - 12cs^2\omega_5 + 6v_1^2\omega_2^2 + 6cs^2\omega_2^2) \frac{\rho}{12\omega_5\omega_2^2} \\
C_{D_x^3 v_1}^{(0), \text{CLBM1}} &= \\
(12\omega_5 v_1^2 + 2\omega_5\omega_2^2 + 6\omega_5 v_1^2\omega_2 - 3\omega_5\omega_2^2cs^2 - 12\omega_5cs^2 - 6\omega_5\omega_2 - 5\omega_5 v_1^2\omega_2^2 - 6\omega_2^2 - 12\omega_2cs^2 + 6\omega_2^2cs^2 - 36v_1^2\omega_2 + 12\omega_2 + 18\omega_5\omega_2cs^2 + 18v_1^2\omega_2^2) \frac{\rho}{12\omega_5\omega_2^2} \\
C_{D_x^3 v_1}^{(0), \text{CLBM2}} &= \\
(12\omega_5 v_1^2 + 2\omega_5\omega_2^2 + 6\omega_5 v_1^2\omega_2 + 18\omega_5\omega_2cs^2 - 6\omega_5\omega_2 - 5\omega_5 v_1^2\omega_2^2 - 6\omega_2^2 + 6\omega_2^2cs^2 - 36v_1^2\omega_2 + 12\omega_2 - 12\omega_2cs^2 - 3\omega_5\omega_2^2cs^2 - 12\omega_5cs^2 + 18v_1^2\omega_2^2) \frac{\rho}{12\omega_5\omega_2^2} \\
\text{coefficient } C_{D_t^2 D_y v_2}^{(0)} \text{ at } \frac{\partial^3 v_2}{\partial t^2 \partial x_2} &: \\
C_{D_t^2 D_y v_2}^{(0), \text{SRT}} &= (12 - 12\omega + \omega^2) \frac{\rho}{12\omega^2} \\
C_{D_t^2 D_y v_2}^{(0), \text{MRT1}} &= (12 + \omega_3^2 - 12\omega_3) \frac{\rho}{12\omega_3^2} \\
C_{D_t^2 D_y v_2}^{(0), \text{MRT2}} &= C_{D_t^2 D_y v_2}^{(0), \text{MRT1}} \\
C_{D_t^2 D_y v_2}^{(0), \text{CLBM1}} &= C_{D_t^2 D_y v_2}^{(0), \text{MRT1}} \\
C_{D_t^2 D_y v_2}^{(0), \text{CLBM2}} &= C_{D_t^2 D_y v_2}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_t D_x D_y v_1}^{(0)} \text{ at } \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} &: \\
C_{D_t D_x D_y v_1}^{(0), \text{SRT}} &= (-6 + 6\omega - \omega^2) \frac{v_2 \rho}{3\omega^2} \\
C_{D_t D_x D_y v_1}^{(0), \text{MRT1}} &= (3\omega_3^2 - 2\omega_2\omega_3^2 - 6\omega_2 - 6\omega_3 + 9\omega_2\omega_3) \frac{v_2 \rho}{6\omega_2\omega_3^2} \\
C_{D_t D_x D_y v_1}^{(0), \text{MRT2}} &= C_{D_t D_x D_y v_1}^{(0), \text{MRT1}} \\
C_{D_t D_x D_y v_1}^{(0), \text{CLBM1}} &= C_{D_t D_x D_y v_1}^{(0), \text{MRT1}} \\
C_{D_t D_x D_y v_1}^{(0), \text{CLBM2}} &= C_{D_t D_x D_y v_1}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_t D_x D_y v_2}^{(0)} \text{ at } \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} &: \\
C_{D_t D_x D_y v_2}^{(0), \text{SRT}} &= (-6 + 6\omega - \omega^2) \frac{v_1 \rho}{3\omega^2} \\
C_{D_t D_x D_y v_2}^{(0), \text{MRT1}} &= (-2\omega_2^2\omega_3 + 3\omega_2^2 - 6\omega_2 - 6\omega_3 + 9\omega_2\omega_3) \frac{v_1 \rho}{6\omega_2^2\omega_3} \\
C_{D_t D_x D_y v_2}^{(0), \text{MRT2}} &= C_{D_t D_x D_y v_2}^{(0), \text{MRT1}} \\
C_{D_t D_x D_y v_2}^{(0), \text{CLBM1}} &= C_{D_t D_x D_y v_2}^{(0), \text{MRT1}} \\
C_{D_t D_x D_y v_2}^{(0), \text{CLBM2}} &= C_{D_t D_x D_y v_2}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_x^2 D_y \rho}^{(0)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} &: \\
C_{D_x^2 D_y \rho}^{(0), \text{SRT}} &= (-\omega^2 cs^2 + \omega^2 v_1^2 + 6v_1^2 - 6cs^2 - 6\omega v_1^2 + 6\omega cs^2) \frac{v_2}{2\omega^2} \\
C_{D_x^2 D_y \rho}^{(0), \text{MRT1}} &= (-\omega_5\omega_2^2\omega_3^2 cs^2 - 2\omega_5\omega_2\omega_3 cs^2 - 2\omega_5\omega_3^2 cs^2 + \omega_5 v_1^2\omega_2^2\omega_3^2 + v_1^2\omega_2^2\omega_3^2 + 2\omega_5 v_1^2\omega_2^2 - 3\omega_5 v_1^2\omega_2^2\omega_3 + \omega_2^2\omega_3^2 cs^2 - 2\omega_2\omega_3^2 cs^2 + 4\omega_5 v_1^2\omega_2\omega_3^2 + 2\omega_5 v_1^2\omega_2\omega_3^2 - 2v_1^2\omega_2\omega_3^2 + 4\omega_5\omega_2\omega_3^2 cs^2 - 4\omega_5 v_1^2\omega_2\omega_3^2 + \omega_5\omega_2^2\omega_3 cs^2) \frac{v_2}{2\omega_5\omega_2^2\omega_3^2}
\end{aligned}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{MRT2}} = (\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 4c s^2 \omega_5 \omega_2 \omega_3^2 - 2c s^2 \omega_5 \omega_2 \omega_3 + v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 + c s^2 \omega_2^2 \omega_3^2 - 2c s^2 \omega_2 \omega_3^2 + c s^2 \omega_5 \omega_2^2 \omega_3 + 4\omega_5 v_1^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 - 2v_1^2 \omega_2 \omega_3^2 - 2c s^2 \omega_5 \omega_3^2 - 4\omega_5 v_1^2 \omega_2 \omega_3^2 - c s^2 \omega_5 \omega_2^2 \omega_3^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{CLBIM1}} = (4\omega_5 \omega_2 c s^2 \omega_3^2 + \omega_5 v_1^2 \omega_2^2 \omega_3^2 - v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 - 2\omega_5 \omega_2 c s^2 \omega_3 - 2\omega_2 c s^2 \omega_3^2 + \omega_2^2 c s^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 + \omega_5 \omega_2^2 c s^2 \omega_3 + 2v_1^2 \omega_2 \omega_3^2 - 2\omega_5 v_1^2 \omega_2 \omega_3^2 - \omega_5 \omega_2^2 c s^2 \omega_3^2 - 2\omega_5 c s^2 \omega_3^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{CLBIM2}} = (-2\omega_5 \omega_2 \omega_3 c s^2 - 2\omega_5 \omega_3^2 c s^2 - \omega_5 \omega_2^2 \omega_3^2 c s^2 + \omega_5 v_1^2 \omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2 c s^2 - v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 - 2\omega_2 \omega_3^2 c s^2 + \omega_2^2 c s^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 + 2v_1^2 \omega_2 \omega_3^2 + \omega_5 \omega_2^2 \omega_3 c s^2 - 2\omega_5 v_1^2 \omega_2 \omega_3^2 + 4\omega_5 \omega_2 \omega_3^2 c s^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

**coefficient**  $C_{D_x^2 D_y v_1}^{(0)}$  at  $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_2}$ :

$$C_{D_x^2 D_y v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 v_2 \rho}{6\omega^2}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{MRT1}} = (-6\omega_2^2 \omega_3 + 6\omega_2^2 + \omega_2^2 \omega_3^2 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_1 v_2 \rho}{6\omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{CLBIM1}} = C_{D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{CLBIM2}} = C_{D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x^2 D_y v_2}^{(0)}$  at  $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_2}$ :

$$C_{D_x^2 D_y v_2}^{(0), \text{SRT}} = (-3\omega^2 c s^2 + \omega^2 v_1^2 - 24c s^2 + 24\omega c s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{MRT1}} = (18\omega_5 \omega_2 c s^2 + 12\omega_5 v_1^2 - 6\omega_5 v_1^2 \omega_2 + 6\omega_2^2 c s^2 + \omega_5 v_1^2 \omega_2^2 - 12v_1^2 \omega_2 - 12\omega_2 c s^2 + 6v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 c s^2 - 12\omega_5 c s^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{MRT2}} = (12\omega_5 v_1^2 - 3c s^2 \omega_5 \omega_2^2 - 6\omega_5 v_1^2 \omega_2 + 18c s^2 \omega_5 \omega_2 + \omega_5 v_1^2 \omega_2^2 - 12c s^2 \omega_2 - 12v_1^2 \omega_2 - 12c s^2 \omega_5 + 6v_1^2 \omega_2^2 + 6c s^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{CLBIM1}} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2^2 c s^2 - 12\omega_5 c s^2 + \omega_5 v_1^2 \omega_2^2 - 12\omega_2 c s^2 + 6\omega_2^2 c s^2 + 12v_1^2 \omega_2 + 18\omega_5 \omega_2 c s^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{CLBIM2}} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 + 18\omega_5 \omega_2 c s^2 + \omega_5 v_1^2 \omega_2^2 + 6\omega_2^2 c s^2 + 12v_1^2 \omega_2 - 12\omega_2 c s^2 - 3\omega_5 \omega_2^2 c s^2 - 12\omega_5 c s^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

**coefficient**  $C_{D_t D_y^2 v_2}^{(0)}$  at  $\frac{\partial^3 v_2}{\partial t \partial x_2}$ :

$$C_{D_t D_y^2 v_2}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_2 \rho}{6\omega^2}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{MRT1}} = (12 + \omega_6 \omega_3 - 6\omega_6 - 6\omega_3) \frac{v_2 \rho}{6\omega_6 \omega_3}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_t D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{CLBIM1}} = (12 + \omega_3^2 - 12\omega_3) \frac{v_2 \rho}{6\omega_3^2}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{CLBIM2}} = C_{D_t D_y^2 v_2}^{(0), \text{CLBIM1}}$$

**coefficient**  $C_{D_x D_y^2 \rho}^{(0)}$  at  $\frac{\partial^3 \rho}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y^2 \rho}^{(0), \text{SRT}} = (-\omega^2 c s^2 + \omega^2 v_2^2 - 6c s^2 + 6v_2^2 + 6\omega c s^2 - 6\omega v_2^2) \frac{v_1}{2\omega^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{MRT1}} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 + \omega_2 \omega_6 \omega_3^2 c s^2 - 2\omega_2^2 \omega_6 c s^2 + 2v_2^2 \omega_6 \omega_3^2 + 4\omega_2^2 \omega_6 \omega_3 c s^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 + \omega_2^2 \omega_3^2 c s^2 + 4\omega_2^2 v_2^2 \omega_6 - \omega_2^2 \omega_6 \omega_3^2 c s^2 - 2\omega_2^2 \omega_3 c s^2 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 + \omega_2^2 v_2^2 \omega_3^2 - 2\omega_2^2 v_2^2 \omega_3 - 4\omega_2^2 v_2^2 \omega_6 \omega_3 - 2\omega_2 \omega_6 \omega_3 c s^2) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), MRT2} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 - cs^2 \omega_2^2 \omega_6 \omega_3^2 - 2cs^2 \omega_2^2 \omega_3 + 2v_2^2 \omega_6 \omega_3^2 - 2cs^2 \omega_2^2 \omega_6 + 4cs^2 \omega_2^2 \omega_6 \omega_3 + cs^2 \omega_2^2 \omega_3^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 + 4\omega_2^2 v_2^2 \omega_6 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 + \omega_2^2 v_2^2 \omega_3^2 - 2cs^2 \omega_2 \omega_6 \omega_3 - 2\omega_2^2 v_2^2 \omega_3 + cs^2 \omega_2 \omega_6 \omega_3^2 - 4\omega_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), CLBM1} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 + \omega_2 cs^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 - 2\omega_2 cs^2 \omega_6 \omega_3 + 2\omega_2 v_2^2 \omega_6 \omega_3 - 2\omega_2^2 cs^2 \omega_6 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 - \omega_2^2 v_2^2 \omega_3^2 - \omega_2^2 cs^2 \omega_6 \omega_3^2 - 2\omega_2^2 cs^2 \omega_3 + 4\omega_2^2 cs^2 \omega_6 \omega_3 + 2\omega_2^2 v_2^2 \omega_6 \omega_3 - 2\omega_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), CLBM2} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 - 2\omega_2^2 \omega_6 cs^2 + \omega_2 \omega_6 \omega_3^2 cs^2 + 2v_2^2 \omega_6 \omega_3^2 + 4\omega_2^2 \omega_6 \omega_3 cs^2 + \omega_2^2 \omega_3^2 cs^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 - \omega_2^2 v_2^2 \omega_3^2 - \omega_2^2 \omega_6 \omega_3^2 cs^2 - 2\omega_2^2 \omega_3 cs^2 - 2\omega_2 \omega_6 \omega_3 cs^2 + 2\omega_2^2 v_2^2 \omega_3 - 2\omega_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

**coefficient**  $C_{D_x D_y^2 v_1}^{(0)}$  at  $\frac{\partial^3 v_1}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y^2 v_1}^{(0), SRT} = (-3\omega^2 cs^2 + \omega^2 v_2^2 - 24cs^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x D_y^2 v_1}^{(0), MRT1} = (-6v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 3\omega_6 \omega_3^2 cs^2 + 12v_2^2 \omega_6 - 12\omega_3 cs^2 + 6\omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 - 12\omega_6 cs^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), MRT2} = (6cs^2 \omega_3^2 - 12cs^2 \omega_6 - 6v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 + 12v_2^2 \omega_6 + 18cs^2 \omega_6 \omega_3 - 3cs^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), CLBM1} = (18cs^2 \omega_6 \omega_3 - 12cs^2 \omega_3 + 6v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^2 + 6cs^2 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_6 - 12cs^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), CLBM2} = (6v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^2 - 12\omega_3 cs^2 - 12v_2^2 \omega_6 - 3\omega_6 \omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 + 6\omega_3^2 cs^2 - 12\omega_6 cs^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

**coefficient**  $C_{D_x D_y^2 v_2}^{(0)}$  at  $\frac{\partial^3 v_2}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y^2 v_2}^{(0), SRT} = (12 - 12\omega + \omega^2) \frac{v_1 v_2 \rho}{6\omega^2}$$

$$C_{D_x D_y^2 v_2}^{(0), MRT1} = (-6\omega_2^2 \omega_3 + 6\omega_2^2 + \omega_2^2 \omega_3^2 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_1 v_2 \rho}{6\omega_2^2 \omega_3^2}$$

$$C_{D_x D_y^2 v_2}^{(0), MRT2} = C_{D_x D_y^2 v_2}^{(0), MRT1}$$

$$C_{D_x D_y^2 v_2}^{(0), CLBM1} = C_{D_x D_y^2 v_2}^{(0), MRT1}$$

$$C_{D_x D_y^2 v_2}^{(0), CLBM2} = C_{D_x D_y^2 v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_y^3 \rho}^{(0)}$  at  $\frac{\partial^3 \rho}{\partial x_2^3}$ :

$$C_{D_y^3 \rho}^{(0), SRT} = (6 - 3\omega^2 cs^2 - \omega^2 v_2^2 - 18cs^2 - 6\omega - 6v_2^2 + \omega^2 + 18\omega cs^2 + 6\omega v_2^2) \frac{v_2}{6\omega^2}$$

$$C_{D_y^3 \rho}^{(0), MRT1} = (3v_2^2 \omega_6 \omega_3 - 6v_2^2 \omega_3 - v_2^2 \omega_6 \omega_3^2 + 3v_2^2 \omega_3^2 - 3\omega_6 \omega_3^2 cs^2 - 6\omega_3 cs^2 - 3\omega_3^2 - 3\omega_6 \omega_3 + 3\omega_3^2 cs^2 + 15\omega_6 \omega_3 cs^2 - 12\omega_6 cs^2 + 6\omega_3 + \omega_6 \omega_3^2) \frac{v_2}{6\omega_6 \omega_3^2}$$

$$C_{D_y^3 \rho}^{(0), MRT2} = (3cs^2 \omega_3^2 - 12cs^2 \omega_6 + 3v_2^2 \omega_6 \omega_3 - 6v_2^2 \omega_3 - v_2^2 \omega_6 \omega_3^2 + 3v_2^2 \omega_3^2 - 6cs^2 \omega_3 - 3\omega_3^2 + 15cs^2 \omega_6 \omega_3 - 3\omega_6 \omega_3 + 6\omega_3 + \omega_6 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2) \frac{v_2}{6\omega_6 \omega_3^2}$$

$$C_{D_y^3 \rho}^{(0), CLBM1} = (6 - 3cs^2 \omega_6 \omega_3 + 9cs^2 \omega_3 - v_2^2 \omega_6 \omega_3 + 3v_2^2 \omega_3 + 3v_2^2 \omega_6 - 6v_2^2 + 9cs^2 \omega_6 - 18cs^2 + \omega_6 \omega_3 - 3\omega_6 - 3\omega_3) \frac{v_2}{6\omega_6 \omega_3}$$

$$C_{D_y^3 \rho}^{(0), CLBM2} = (6 - v_2^2 \omega_6 \omega_3 + 3v_2^2 \omega_3 + 9\omega_3 cs^2 + 3v_2^2 \omega_6 - 6v_2^2 + \omega_6 \omega_3 - 3\omega_6 \omega_3 cs^2 - 18cs^2 - 3\omega_6 - 3\omega_3 + 9\omega_6 cs^2) \frac{v_2}{6\omega_6 \omega_3}$$

**coefficient**  $C_{D_y^3 v_2}^{(0)}$  at  $\frac{\partial^3 v_2}{\partial x_2^3}$ :

$$C_{D_y^3 v_2}^{(0), SRT} = (12 - 3\omega^2 cs^2 - 5\omega^2 v_2^2 - 24cs^2 - 12\omega - 24v_2^2 + 2\omega^2 + 24\omega cs^2 + 24\omega v_2^2) \frac{\rho}{12\omega^2}$$

$$\begin{aligned}
C_{D_t^3 v_2}^{(0), \text{MRT1}} &= \\
(18v_2^2\omega_6\omega_3 - 12v_2^2\omega_3 - 5v_2^2\omega_6\omega_3^2 + 6v_2^2\omega_3^2 - 3\omega_6\omega_3^2cs^2 - 12v_2^2\omega_6 - 12\omega_3cs^2 - 6\omega_3^2 - 6\omega_6\omega_3 + 6\omega_3^2cs^2 + 18\omega_6\omega_3cs^2 - 12\omega_6cs^2 + 12\omega_3 + 2\omega_6\omega_3^2) \frac{\rho}{12\omega_6\omega_3^2} \\
C_{D_t^3 v_2}^{(0), \text{MRT2}} &= \\
(6cs^2\omega_3^2 - 12cs^2\omega_6 + 18v_2^2\omega_6\omega_3 - 12v_2^2\omega_3 - 5v_2^2\omega_6\omega_3^2 + 6v_2^2\omega_3^2 - 12cs^2\omega_3 - 12v_2^2\omega_6 - 6\omega_3^2 + 18cs^2\omega_6\omega_3 - 6\omega_6\omega_3 + 12\omega_3 + 2\omega_6\omega_3^2 - 3cs^2\omega_6\omega_3^2) \frac{\rho}{12\omega_6\omega_3^2} \\
C_{D_t^3 v_2}^{(0), \text{CLBM1}} &= \\
(18cs^2\omega_6\omega_3 - 12cs^2\omega_3 + 6v_2^2\omega_6\omega_3 - 36v_2^2\omega_3 - 5v_2^2\omega_6\omega_3^2 + 18v_2^2\omega_3^2 + 6cs^2\omega_3^2 - 3cs^2\omega_6\omega_3^2 + 12v_2^2\omega_6 - 12cs^2\omega_6 - 6\omega_3^2 - 6\omega_6\omega_3 + 12\omega_3 + 2\omega_6\omega_3^2) \frac{\rho}{12\omega_6\omega_3^2} \\
C_{D_t^3 v_2}^{(0), \text{CLBM2}} &= \\
(6v_2^2\omega_6\omega_3 - 36v_2^2\omega_3 - 5v_2^2\omega_6\omega_3^2 + 18v_2^2\omega_3^2 - 12\omega_3cs^2 + 12v_2^2\omega_6 - 3\omega_6\omega_3^2cs^2 - 6\omega_3^2 - 6\omega_6\omega_3 + 18\omega_6\omega_3cs^2 + 6\omega_3^2cs^2 + 12\omega_3 - 12\omega_6cs^2 + 2\omega_6\omega_3^2) \frac{\rho}{12\omega_6\omega_3^2} \\
\text{coefficient } C_{D_t^2 D_z v_3}^{(0)} \text{ at } \frac{\partial^3 v_3}{\partial t^2 \partial x_3}: \\
C_{D_t^2 D_z v_3}^{(0), \text{SRT}} &= (12 - 12\omega + \omega^2) \frac{\rho}{12\omega^2} \\
C_{D_t^2 D_z v_3}^{(0), \text{MRT1}} &= (12 + \omega_4^2 - 12\omega_4) \frac{\rho}{12\omega_4^2} \\
C_{D_t^2 D_z v_3}^{(0), \text{MRT2}} &= C_{D_t^2 D_z v_3}^{(0), \text{MRT1}} \\
C_{D_t^2 D_z v_3}^{(0), \text{CLBM1}} &= C_{D_t^2 D_z v_3}^{(0), \text{MRT1}} \\
C_{D_t^2 D_z v_3}^{(0), \text{CLBM2}} &= C_{D_t^2 D_z v_3}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_t D_x D_z v_1}^{(0)} \text{ at } \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3}: \\
C_{D_t D_x D_z v_1}^{(0), \text{SRT}} &= (-6 + 6\omega - \omega^2) \frac{\rho v_3}{3\omega^2} \\
C_{D_t D_x D_z v_1}^{(0), \text{MRT1}} &= (3\omega_4^2 - 6\omega_4 - 2\omega_4^2\omega_2 + 9\omega_4\omega_2 - 6\omega_2) \frac{\rho v_3}{6\omega_4^2\omega_2} \\
C_{D_t D_x D_z v_1}^{(0), \text{MRT2}} &= C_{D_t D_x D_z v_1}^{(0), \text{MRT1}} \\
C_{D_t D_x D_z v_1}^{(0), \text{CLBM1}} &= C_{D_t D_x D_z v_1}^{(0), \text{MRT1}} \\
C_{D_t D_x D_z v_1}^{(0), \text{CLBM2}} &= C_{D_t D_x D_z v_1}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_t D_x D_z v_3}^{(0)} \text{ at } \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3}: \\
C_{D_t D_x D_z v_3}^{(0), \text{SRT}} &= (-6 + 6\omega - \omega^2) \frac{v_1 \rho}{3\omega^2} \\
C_{D_t D_x D_z v_3}^{(0), \text{MRT1}} &= (-6\omega_4 + 3\omega_2^2 + 9\omega_4\omega_2 - 6\omega_2 - 2\omega_4\omega_2^2) \frac{v_1 \rho}{6\omega_4\omega_2^2} \\
C_{D_t D_x D_z v_3}^{(0), \text{MRT2}} &= C_{D_t D_x D_z v_3}^{(0), \text{MRT1}} \\
C_{D_t D_x D_z v_3}^{(0), \text{CLBM1}} &= C_{D_t D_x D_z v_3}^{(0), \text{MRT1}} \\
C_{D_t D_x D_z v_3}^{(0), \text{CLBM2}} &= C_{D_t D_x D_z v_3}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_x^2 D_z \rho}^{(0)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3}: \\
C_{D_x^2 D_z \rho}^{(0), \text{SRT}} &= (-\omega^2 cs^2 + \omega^2 v_1^2 + 6v_1^2 - 6cs^2 - 6\omega v_1^2 + 6\omega cs^2) \frac{v_3}{2\omega^2}
\end{aligned}$$

$$C_{D_x^2 D_z \rho}^{(0), MRT1} = (-2\omega_4^2 \omega_5 c s^2 - \omega_4^2 \omega_5 \omega_2^2 c s^2 + \omega_4^2 v_1^2 \omega_2^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - 2\omega_4^2 \omega_2 c s^2 + 2\omega_5 v_1^2 \omega_2^2 - 2\omega_4 \omega_5 \omega_2 c s^2 - 2\omega_4^2 v_1^2 \omega_2 +$$

$$\omega_4^2 \omega_5 \omega_2^2 c s^2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + \omega_4^2 \omega_2^2 c s^2 - 4\omega_4^2 \omega_5 v_1^2 \omega_2 + 4\omega_4^2 \omega_5 v_1^2 + 4\omega_4^2 \omega_5 \omega_2 c s^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(0), MRT2} = (\omega_4^2 c s^2 \omega_2^2 + \omega_4^2 v_1^2 \omega_2^2 - 2\omega_4 c s^2 \omega_5 \omega_2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + \omega_4 c s^2 \omega_5 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - 2\omega_4^2 c s^2 \omega_5 + 2\omega_5 v_1^2 \omega_2^2 - 2\omega_4^2 v_1^2 \omega_2 - 2\omega_4^2 c s^2 \omega_2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + 4\omega_4^2 c s^2 \omega_5 \omega_2 - 4\omega_4^2 \omega_5 v_1^2 \omega_2 - \omega_4^2 c s^2 \omega_5 \omega_2^2 + 4\omega_4^2 \omega_5 v_1^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_1}^{(0), CLBM1} = (-\omega_4^2 v_1^2 \omega_2^2 + 4\omega_4^2 \omega_5 \omega_2 c s^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 + \omega_4 \omega_5 \omega_2^2 c s^2 + 2\omega_5 v_1^2 \omega_2^2 + \omega_4^2 \omega_2^2 c s^2 + 2\omega_4^2 v_1^2 \omega_2 - 2\omega_4^2 \omega_2 c s^2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 - 2\omega_4 \omega_5 \omega_2 c s^2 - 2\omega_4^2 \omega_5 c s^2 - 2\omega_4^2 \omega_5 v_1^2 \omega_2 - \omega_4^2 \omega_5 \omega_2^2 c s^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_1}^{(0), CLBM2} = (-\omega_4^2 v_1^2 \omega_2^2 - 2\omega_4^2 \omega_5 c s^2 - \omega_4^2 \omega_5 \omega_2^2 c s^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - 2\omega_4 \omega_5 \omega_2 c s^2 + 2\omega_5 v_1^2 \omega_2^2 - 2\omega_4^2 \omega_2 c s^2 + 2\omega_4^2 v_1^2 \omega_2 + \omega_4^2 \omega_5 \omega_2^2 c s^2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + \omega_4 \omega_5 \omega_2^2 c s^2 - 2\omega_4^2 \omega_5 v_1^2 \omega_2 + 4\omega_4^2 \omega_5 \omega_2 c s^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

**coefficient**  $C_{D_x^2 D_z v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_3}$ :

$$C_{D_x^2 D_z v_1}^{(0), SRT} = (12 - 12\omega + \omega^2) \frac{v_1 \rho v_3}{6\omega^2}$$

$$C_{D_x^2 D_z v_1}^{(0), MRT1} = (\omega_4^2 \omega_2^2 + 6\omega_4^2 + 6\omega_2^2 - 6\omega_4^2 \omega_2 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_4^2 \omega_2^2}$$

$$C_{D_x^2 D_z v_1}^{(0), MRT2} = C_{D_x^2 D_z v_1}^{(0), MRT1}$$

$$C_{D_x^2 D_z v_1}^{(0), CLBM1} = C_{D_x^2 D_z v_1}^{(0), MRT1}$$

$$C_{D_x^2 D_z v_1}^{(0), CLBM2} = C_{D_x^2 D_z v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_x^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$ :

$$C_{D_x^2 D_z v_3}^{(0), SRT} = (-3\omega^2 c s^2 + \omega^2 v_1^2 - 24c s^2 + 24\omega c s^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^2 D_z v_3}^{(0), MRT1} = (18\omega_5 \omega_2 c s^2 + 12\omega_5 v_1^2 - 6\omega_5 v_1^2 \omega_2 + 6\omega_2^2 c s^2 + \omega_5 v_1^2 \omega_2^2 - 12v_1^2 \omega_2 - 12\omega_2 c s^2 + 6v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 c s^2 - 12\omega_5 c s^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), MRT2} = (12\omega_5 v_1^2 - 3c s^2 \omega_5 \omega_2^2 - 6\omega_5 v_1^2 \omega_2 + 18c s^2 \omega_5 \omega_2 + \omega_5 v_1^2 \omega_2^2 - 12c s^2 \omega_2 - 12v_1^2 \omega_2 - 12c s^2 \omega_5 + 6v_1^2 \omega_2^2 + 6c s^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), CLBM1} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2^2 c s^2 - 12\omega_5 c s^2 + \omega_5 v_1^2 \omega_2^2 - 12\omega_2 c s^2 + 6\omega_2^2 c s^2 + 12v_1^2 \omega_2 + 18\omega_5 \omega_2 c s^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), CLBM2} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 + 18\omega_5 \omega_2 c s^2 + \omega_5 v_1^2 \omega_2^2 + 6\omega_2^2 c s^2 + 12v_1^2 \omega_2 - 12\omega_2 c s^2 - 3\omega_5 \omega_2^2 c s^2 - 12\omega_5 c s^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

**coefficient**  $C_{D_t D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3}$ :

$$C_{D_t D_y D_z v_2}^{(0), SRT} = (-6 + 6\omega - \omega^2) \frac{\rho v_3}{3\omega^2}$$

$$C_{D_t D_y D_z v_2}^{(0), MRT1} = (3\omega_4^2 - 6\omega_4 + 9\omega_4 \omega_3 - 2\omega_4^2 \omega_3 - 6\omega_3) \frac{\rho v_3}{6\omega_4^2 \omega_3}$$

$$C_{D_t D_y D_z v_2}^{(0), MRT2} = C_{D_t D_y D_z v_2}^{(0), MRT1}$$

$$C_{D_t D_y D_z v_2}^{(0), CLBM1} = C_{D_t D_y D_z v_2}^{(0), MRT1}$$

$$C_{D_t D_y D_z v_2}^{(0), CLBM2} = C_{D_t D_y D_z v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_t D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3}$ :

$$C_{D_t D_y D_z v_3}^{(0), SRT} = (-6 + 6\omega - \omega^2) \frac{v_2 \rho}{3\omega^2}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{MRT1}} = (-2\omega_4\omega_3^2 - 6\omega_4 + 9\omega_4\omega_3 + 3\omega_3^2 - 6\omega_3) \frac{v_2\rho}{6\omega_4\omega_3^2}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z \rho}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_1 v_2 v_3}{\omega^2}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{MRT1}} = (\omega_4^2 \omega_3^2 + \omega_4^2 \omega_2 \omega_3 + \omega_4 \omega_2^2 \omega_3 - 2\omega_4 \omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2 - 2\omega_4^2 \omega_2 \omega_3^2 + \omega_4^2 \omega_2^2 \omega_3^2 + \omega_4 \omega_2 \omega_3^2 - 2\omega_4^2 \omega_2^2 \omega_3 + \omega_4^2 \omega_3^2) \frac{2v_1 v_2 v_3}{\omega_4^2 \omega_2^2 \omega_3^2}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{MRT2}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{CLBM1}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{CLBM2}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_1}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_2 \rho v_3}{3\omega^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT1}} = (-6\omega_4\omega_3^2 + 3\omega_4^2 + 6\omega_4\omega_3 + 3\omega_3^2 - 6\omega_4^2\omega_3 + 2\omega_4^2\omega_3^2) \frac{v_2 \rho v_3}{3\omega_4^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_2}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_1 \rho v_3}{3\omega^2}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT1}} = (2\omega_4^2 \omega_2^2 + 3\omega_4^2 + 3\omega_2^2 - 6\omega_4^2 \omega_2 + 6\omega_4 \omega_2 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{3\omega_4^2 \omega_2^2}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_3}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_1 v_2 \rho}{3\omega^2}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{MRT1}} = (-6\omega_2^2 \omega_3 + 3\omega_2^2 + 2\omega_2^2 \omega_3^2 + 3\omega_3^2 - 6\omega_2 \omega_3^2 + 6\omega_2 \omega_3) \frac{v_1 v_2 \rho}{3\omega_2^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y^2 D_z \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_2^2 \partial x_3}$ :

$$C_{D_y^2 D_z \rho}^{(0), SRT} = (-\omega^2 c s^2 + \omega^2 v_2^2 - 6 c s^2 + 6 v_2^2 + 6 \omega c s^2 - 6 \omega v_2^2) \frac{v_3}{2 \omega^2}$$

$$C_{D_y^2 D_z \rho}^{(0), MRT1} = (-3 \omega_4 v_2^2 \omega_6 \omega_3^2 + \omega_4 \omega_6 \omega_3^2 c s^2 - 2 \omega_4^2 \omega_6 c s^2 + 2 v_2^2 \omega_6 \omega_3^2 + 4 \omega_4^2 \omega_6 \omega_3 c s^2 + 2 \omega_4 v_2^2 \omega_6 \omega_3 + \omega_4^2 \omega_3^2 c s^2 - 2 \omega_4^2 \omega_3 c s^2 + 4 \omega_4^2 v_2^2 \omega_6 - \omega_4^2 \omega_6 \omega_3^2 c s^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_3^2 - 2 \omega_4^2 v_2^2 \omega_3 - 4 \omega_4^2 v_2^2 \omega_6 \omega_3 - 2 \omega_4 \omega_6 \omega_3 c s^2) \frac{v_3}{2 \omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), MRT2} = (-\omega_4^2 c s^2 \omega_6 \omega_3^2 - 3 \omega_4 v_2^2 \omega_6 \omega_3^2 + 2 v_2^2 \omega_6 \omega_3^2 + 2 \omega_4 v_2^2 \omega_6 \omega_3 + 4 \omega_4^2 c s^2 \omega_6 \omega_3 + 4 \omega_4^2 v_2^2 \omega_6 - 2 \omega_4^2 c s^2 \omega_3 + \omega_4 c s^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_3^2 - 2 \omega_4^2 v_2^2 \omega_3 - 4 \omega_4^2 v_2^2 \omega_6 \omega_3 - 2 \omega_4^2 c s^2 \omega_6 + \omega_4^2 c s^2 \omega_3^2 - 2 \omega_4 c s^2 \omega_6 \omega_3) \frac{v_3}{2 \omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), CLBM1} = (\omega_4 c s^2 \omega_6 \omega_3^2 - 3 \omega_4 v_2^2 \omega_6 \omega_3^2 + 2 v_2^2 \omega_6 \omega_3^2 + 2 \omega_4 v_2^2 \omega_6 \omega_3 - 2 \omega_4 c s^2 \omega_6 \omega_3 - 2 \omega_4^2 c s^2 \omega_6 - \omega_4^2 c s^2 \omega_6 \omega_3^2 + \omega_4^2 c s^2 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - \omega_4^2 v_2^2 \omega_3^2 + 2 \omega_4^2 v_2^2 \omega_3 - 2 \omega_4^2 c s^2 \omega_3 + 4 \omega_4^2 c s^2 \omega_6 \omega_3) \frac{v_3}{2 \omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), CLBM2} = (\omega_4 \omega_6 \omega_3^2 c s^2 - 2 \omega_4^2 \omega_6 c s^2 - 3 \omega_4 v_2^2 \omega_6 \omega_3^2 + 2 v_2^2 \omega_6 \omega_3^2 + \omega_4^2 \omega_3^2 c s^2 + 2 \omega_4 v_2^2 \omega_6 \omega_3 + 4 \omega_4^2 \omega_6 \omega_3 c s^2 - \omega_4^2 \omega_6 \omega_3^2 c s^2 - 2 \omega_4^2 \omega_3 c s^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - \omega_4^2 v_2^2 \omega_3^2 + 2 \omega_4^2 v_2^2 \omega_3 - 2 \omega_4^2 v_2^2 \omega_6 \omega_3 - 2 \omega_4 \omega_6 \omega_3 c s^2) \frac{v_3}{2 \omega_4^2 \omega_6 \omega_3^2}$$

**coefficient**  $C_{D_y^2 D_z v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_2^2 \partial x_3}$ :

$$C_{D_y^2 D_z v_2}^{(0), SRT} = (12 - 12\omega + \omega^2) \frac{v_2 \rho v_3}{6 \omega^2}$$

$$C_{D_y^2 D_z v_2}^{(0), MRT1} = (-6 \omega_4 \omega_3^2 + 6 \omega_4^2 + 6 \omega_3^2 - 6 \omega_4^2 \omega_3 + \omega_4^2 \omega_3^2) \frac{v_2 \rho v_3}{6 \omega_4^2 \omega_3^2}$$

$$C_{D_y^2 D_z v_2}^{(0), MRT2} = C_{D_y^2 D_z v_2}^{(0), MRT1}$$

$$C_{D_y^2 D_z v_2}^{(0), CLBM1} = C_{D_y^2 D_z v_2}^{(0), MRT1}$$

$$C_{D_y^2 D_z v_2}^{(0), CLBM2} = C_{D_y^2 D_z v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_y^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$ :

$$C_{D_y^2 D_z v_3}^{(0), SRT} = (-3 \omega^2 c s^2 + \omega^2 v_2^2 - 24 c s^2 + 24 \omega c s^2) \frac{\rho}{12 \omega^2}$$

$$C_{D_y^2 D_z v_3}^{(0), MRT1} = (-6 v_2^2 \omega_6 \omega_3 - 12 v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6 v_2^2 \omega_3^2 - 3 \omega_6 \omega_3^2 c s^2 + 12 v_2^2 \omega_6 - 12 \omega_3 c s^2 + 6 \omega_3^2 c s^2 + 18 \omega_6 \omega_3 c s^2 - 12 \omega_6 c s^2) \frac{\rho}{12 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), MRT2} = (6 c s^2 \omega_3^2 - 12 c s^2 \omega_6 - 6 v_2^2 \omega_6 \omega_3 - 12 v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6 v_2^2 \omega_3^2 - 12 c s^2 \omega_3 + 12 v_2^2 \omega_6 + 18 c s^2 \omega_6 \omega_3 - 3 c s^2 \omega_6 \omega_3^2) \frac{\rho}{12 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), CLBM1} = (18 c s^2 \omega_6 \omega_3 - 12 c s^2 \omega_3 + 6 v_2^2 \omega_6 \omega_3 + 12 v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6 v_2^2 \omega_3^2 + 6 c s^2 \omega_6 \omega_3^2 - 3 c s^2 \omega_6 \omega_3 - 12 v_2^2 \omega_6 - 12 c s^2 \omega_6) \frac{\rho}{12 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), CLBM2} = (6 v_2^2 \omega_6 \omega_3 + 12 v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6 v_2^2 \omega_3^2 - 12 \omega_3 c s^2 - 12 v_2^2 \omega_6 - 3 \omega_6 \omega_3^2 c s^2 + 18 \omega_6 \omega_3 c s^2 + 6 \omega_3^2 c s^2 - 12 \omega_6 c s^2) \frac{\rho}{12 \omega_6 \omega_3^2}$$

**coefficient**  $C_{D_t D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial t \partial x_3}$ :

$$C_{D_t D_z^2 v_3}^{(0), SRT} = (12 - 12\omega + \omega^2) \frac{\rho v_3}{6 \omega^2}$$

$$C_{D_t D_z^2 v_3}^{(0), MRT1} = (12 - 6\omega_7 - 6\omega_4 + \omega_7 \omega_4) \frac{\rho v_3}{6 \omega_7 \omega_4}$$

$$C_{D_t D_z^2 v_3}^{(0), MRT2} = C_{D_t D_z^2 v_3}^{(0), MRT1}$$

$$C_{D_t D_z^2 v_3}^{(0), CLBM1} = (12 + \omega_4^2 - 12\omega_4) \frac{\rho v_3}{6 \omega_4^2}$$

$$C_{\text{D}_t \text{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\text{D}_t \text{D}_z^2 v_3}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{\text{D}_x \text{D}_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{\text{D}_x \text{D}_z^2 \rho}^{(0), \text{SRT}} = (-\omega^2 c s^2 - 6\omega v_3^2 - 6c s^2 + 6v_3^2 + 6\omega c s^2 + \omega^2 v_3^2) \frac{v_1}{2\omega^2}$$

$$C_{\text{D}_x \text{D}_z^2 \rho}^{(0), \text{MRT1}} = (-2\omega_7 \omega_4 \omega_2 c s^2 - 2\omega_7 \omega_2^2 c s^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - \omega_7 \omega_4^2 \omega_2^2 c s^2 - 2\omega_4 \omega_2^2 v_3^2 - 2\omega_4 \omega_2^2 c s^2 + \omega_4^2 \omega_2^2 v_3^2 + 2\omega_4 \omega_2^2 v_3^2 + \omega_7 \omega_4^2 \omega_2 c s^2 - 4\omega_7 \omega_4 \omega_2^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2 + 4\omega_7 \omega_4 \omega_2^2 c s^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{\text{D}_x \text{D}_z^2 \rho}^{(0), \text{MRT2}} = (\omega_4^2 c s^2 \omega_2^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 - 2\omega_7 \omega_4 c s^2 \omega_2 + 4\omega_7 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - 2\omega_4 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 c s^2 \omega_2^2 + \omega_4^2 \omega_2^2 v_3^2 - \omega_7 \omega_4^2 c s^2 \omega_2^2 - 2\omega_7 c s^2 \omega_2^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_4 c s^2 \omega_2^2 - 4\omega_7 \omega_4 \omega_2^2 v_3^2 + \omega_7 \omega_4^2 c s^2 \omega_2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{\text{D}_x \text{D}_z^2 \rho}^{(0), \text{CLBM1}} = (\omega_7 \omega_4^2 \omega_2 c s^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 + 4\omega_7 \omega_4 \omega_2^2 c s^2 + 2\omega_4 \omega_2^2 v_3^2 + \omega_4^2 \omega_2^2 c s^2 - \omega_4^2 \omega_2^2 v_3^2 - 2\omega_4 \omega_2^2 c s^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 \omega_2^2 v_3^2 - 2\omega_7 \omega_4 c s^2 - \omega_7 \omega_4^2 \omega_2^2 c s^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{\text{D}_x \text{D}_z^2 \rho}^{(0), \text{CLBM2}} = (-\omega_7 \omega_4^2 \omega_2 c s^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - 2\omega_7 \omega_4 c s^2 - 2\omega_7 \omega_2^2 c s^2 - 2\omega_4 \omega_2^2 c s^2 + 2\omega_4 \omega_2^2 v_3^2 - \omega_4^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4^2 \omega_2^2 c s^2 - 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_2^2 c s^2 + \omega_7 \omega_4^2 \omega_2 c s^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

**coefficient**  $C_{\text{D}_x \text{D}_z^2 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{\text{D}_x \text{D}_z^2 v_1}^{(0), \text{SRT}} = (-3\omega^2 c s^2 - 24c s^2 + 24\omega c s^2 + \omega^2 v_3^2) \frac{\rho}{12\omega^2}$$

$$C_{\text{D}_x \text{D}_z^2 v_1}^{(0), \text{MRT1}} = (-12\omega_4 v_3^2 - 12\omega_4 c s^2 - 6\omega_7 \omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\text{D}_x \text{D}_z^2 v_1}^{(0), \text{MRT2}} = (-12\omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 - 12\omega_4 c s^2 - 6\omega_7 \omega_4 v_3^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\text{D}_x \text{D}_z^2 v_1}^{(0), \text{CLBM1}} = (12\omega_4 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 v_3^2 + 18\omega_7 \omega_4 c s^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 - 12\omega_4 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

**coefficient**  $C_{\text{D}_x \text{D}_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 \rho v_3}{6\omega^2}$$

$$C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{MRT1}} = (\omega_4^2 \omega_2^2 + 6\omega_4^2 + 6\omega_2^2 - 6\omega_4^2 \omega_2 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_4^2 \omega_2^2}$$

$$C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{CLBM1}} = C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\text{D}_x \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\text{D}_y \text{D}_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_2 \partial x_3 \partial x_3}$ :

$$C_{\text{D}_y \text{D}_z^2 \rho}^{(0), \text{SRT}} = (-\omega^2 c s^2 - 6\omega v_3^2 - 6c s^2 + 6v_3^2 + 6\omega c s^2 + \omega^2 v_3^2) \frac{v_2}{2\omega^2}$$

$$C_{\text{D}_y \text{D}_z^2 \rho}^{(0), \text{MRT1}} = (\omega_7 \omega_4^2 \omega_3 c s^2 - 4\omega_7 \omega_4 \omega_3^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 + 4\omega_7 \omega_4 \omega_3^2 c s^2 + \omega_4^2 \omega_3^2 v_3^2 + \omega_4^2 \omega_3^2 c s^2 - 2\omega_4 \omega_3^2 v_3^2 - 2\omega_4 \omega_3^2 c s^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_3^2 c s^2 - 2\omega_7 \omega_4 \omega_3 c s^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4 \omega_3^2 v_3^2 + 4\omega_7 \omega_3^2 v_3^2 - \omega_7 \omega_4^2 \omega_3^2 c s^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{\text{D}_y \text{D}_z^2 \rho}^{(0), \text{MRT2}} = (\omega_7 \omega_4^2 c s^2 \omega_3 - 4\omega_7 \omega_4 \omega_3^2 v_3^2 - 2\omega_4 c s^2 \omega_3^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 + \omega_4^2 \omega_3^2 v_3^2 - 2\omega_7 c s^2 \omega_3^2 - \omega_7 \omega_4^2 c s^2 \omega_3^2 - 2\omega_4 \omega_3^2 v_3^2 + 4\omega_7 \omega_4 c s^2 \omega_3^2 + 2\omega_7 \omega_4 \omega_3^2 v_3^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + \omega_4^2 c s^2 \omega_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 + 4\omega_7 \omega_3^2 v_3^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{\text{D}_y \text{D}_z^2 \rho}^{(0), \text{CLBM1}} = (-2\omega_7 \omega_4 \omega_3^2 v_3^2 - 2\omega_7 c s^2 \omega_3^2 - \omega_7 \omega_4^2 c s^2 \omega_3^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 + \omega_7 \omega_4^2 c s^2 \omega_3 - \omega_4^2 \omega_3^2 v_3^2 - 2\omega_4 c s^2 \omega_3^2 + 2\omega_4 \omega_3^2 v_3^2 - 2\omega_7 \omega_4 c s^2 \omega_3 + \omega_4^2 c s^2 \omega_3^2 + 2\omega_7 \omega_4^2 v_3^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 + 4\omega_7 \omega_4 c s^2 \omega_3^2) \frac{v_3}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{\text{D}_y \text{D}_z^2 \rho}^{(0), \text{CLBM2}} = (-2\omega_7 \omega_4 \omega_3^2 v_3^2 + 4\omega_7 \omega_4 \omega_3^2 c s^2 + \omega_7 \omega_4^2 \omega_3 c s^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 - \omega_4^2 \omega_3^2 v_3^2 + \omega_4^2 \omega_3^2 c s^2 - 2\omega_4 \omega_3^2 c s^2 + 2\omega_4 \omega_3^2 v_3^2 + 2\omega_7 \omega_4^2 v_3^2 - \omega_7 \omega_4^2 \omega_3^2 c s^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 - 2\omega_7 \omega_3^2 c s^2 - 2\omega_7 \omega_4 \omega_3 c s^2) \frac{v_3}{2\omega_7 \omega_4^2 \omega_3^2}$$

**coefficient**  $C_{\text{D}_y \text{D}_z^2 v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_2 \partial x_3}$ :

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(0), \text{SRT}} = (-3\omega^2 c s^2 - 24c s^2 + 24\omega c s^2 + \omega^2 v_2^2) \frac{\rho}{12\omega^2}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(0), \text{MRT1}} = (-12\omega_4 v_3^2 - 12\omega_4 c s^2 - 6\omega_7 \omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(0), \text{MRT2}} = (-12\omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 - 12\omega_4 c s^2 - 6\omega_7 \omega_4 v_3^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(0), \text{CLBM1}} = (12\omega_4 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 v_3^2 + 18\omega_7 \omega_4 c s^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 - 12\omega_4 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(0), \text{CLBM2}} = (12\omega_4 v_3^2 - 12\omega_4 c s^2 + 18\omega_7 \omega_4 c s^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 c s^2 - 12\omega_7 v_3^2 - 3\omega_7 \omega_4^2 c s^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 + 6\omega_4^2 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

**coefficient**  $C_{\text{D}_y \text{D}_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_2 \partial x_3}$ :

$$C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_2 \rho v_3}{6\omega^2}$$

$$C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{MRT1}} = (-6\omega_4 \omega_3^2 + 6\omega_4^2 + 6\omega_3^2 - 6\omega_4^2 \omega_3 + \omega_4^2 \omega_3^2) \frac{v_2 \rho v_3}{6\omega_4^2 \omega_3^2}$$

$$C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{CLBM1}} = C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\text{D}_y \text{D}_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\text{D}_z^3 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_3^3}$ :

$$C_{\text{D}_z^3 \rho}^{(0), \text{SRT}} = (6 - 3\omega^2 c s^2 + 6\omega v_3^2 - 18c s^2 - 6\omega - 6v_3^2 + \omega^2 + 18\omega c s^2 - \omega^2 v_3^2) \frac{v_3}{6\omega^2}$$

$$C_{\text{D}_z^3 \rho}^{(0), \text{MRT1}} = (-6\omega_4 v_3^2 + \omega_7 \omega_4^2 - 3\omega_4^2 + 6\omega_4 - 6\omega_4 c s^2 + 3\omega_7 \omega_4 v_3^2 - 3\omega_7 \omega_4 + 15\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 - \omega_7 \omega_4^2 v_3^2 + 3\omega_4^2 c s^2 + 3\omega_4^2 v_3^2) \frac{v_3}{6\omega_7 \omega_4^2}$$

$$C_{\text{D}_z^3 \rho}^{(0), \text{MRT2}} = (-6\omega_4 v_3^2 + 15\omega_7 \omega_4 c s^2 + \omega_7 \omega_4^2 - 3\omega_4^2 + 6\omega_4 - 6\omega_4 c s^2 + 3\omega_7 \omega_4 v_3^2 - 3\omega_7 \omega_4 - \omega_7 \omega_4^2 v_3^2 + 3\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 3\omega_4^2 v_3^2) \frac{v_3}{6\omega_7 \omega_4^2}$$

$$C_{\text{D}_z^3 \rho}^{(0), \text{CLBM1}} = (6 + 3\omega_4 v_3^2 - 3\omega_7 - 3\omega_4 + 9\omega_7 c s^2 - \omega_7 \omega_4 v_3^2 + \omega_7 \omega_4 - 18c s^2 - 6v_3^2 + 3\omega_7 v_3^2 - 3\omega_7 \omega_4 c s^2 + 9\omega_4 c s^2) \frac{v_3}{6\omega_7 \omega_4}$$

$$C_{\text{D}_z^3 \rho}^{(0), \text{CLBM2}} = (6 + 3\omega_4 v_3^2 - 3\omega_7 + 9\omega_4 c s^2 - 3\omega_4 - 3\omega_7 \omega_4 c s^2 - \omega_7 \omega_4 v_3^2 + \omega_7 \omega_4 - 6v_3^2 - 18c s^2 + 9\omega_7 c s^2 + 3\omega_7 v_3^2) \frac{v_3}{6\omega_7 \omega_4}$$

**coefficient**  $C_{\text{D}_z^3 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_3^3}$ :

$$C_{\text{D}_z^3 v_3}^{(0), \text{SRT}} = (12 - 3\omega^2 c s^2 + 24\omega v_3^2 - 24c s^2 - 12\omega - 24v_3^2 + 2\omega^2 + 24\omega c s^2 - 5\omega^2 v_3^2) \frac{\rho}{12\omega^2}$$

$$C_{\text{D}_z^3 v_3}^{(0), \text{MRT1}} = (-12\omega_4 v_3^2 + 2\omega_7 \omega_4^2 - 6\omega_4^2 + 12\omega_4 - 12\omega_4 c s^2 + 18\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 + 18\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 - 12\omega_7 v_3^2 - 5\omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\text{D}_z^3 v_3}^{(0), \text{MRT2}} =$$

$$(-12\omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 + 2\omega_7 \omega_4^2 - 6\omega_4^2 + 12\omega_4 - 12\omega_4 c s^2 + 18\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 - 12\omega_7 v_3^2 - 5\omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$\begin{aligned}
C_{D_t^3 v_3}^{(0), \text{CLBM1}} &= \\
(-36\omega_4 v_3^2 + 2\omega_7 \omega_4^2 + 6\omega_4^2 c s^2 - 6\omega_4^2 + 12\omega_4 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 + 12\omega_7 v_3^2 + 18\omega_7 \omega_4 c s^2 - 5\omega_7 \omega_4^2 v_3^2 + 18\omega_4^2 v_3^2 - 12\omega_4 c s^2) \frac{\rho}{12\omega_7 \omega_4^2} \\
C_{D_t^3 v_3}^{(0), \text{CLBM2}} &= \\
(-36\omega_4 v_3^2 + 2\omega_7 \omega_4^2 - 12\omega_4 c s^2 - 6\omega_4^2 + 12\omega_4 + 18\omega_7 \omega_4 c s^2 + 6\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 - 12\omega_7 c s^2 + 12\omega_7 v_3^2 - 3\omega_7 \omega_4^2 c s^2 - 5\omega_7 \omega_4^2 v_3^2 + 18\omega_4^2 v_3^2 + 6\omega_4^2 c s^2) \frac{\rho}{12\omega_7 \omega_4^2} \\
\text{coefficient } C_{D_t^3 D_x v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t^3 \partial x_1}: \\
C_{D_t^3 D_x v_1}^{(0), \text{SRT}} &= (-2 + 3\omega - \omega^2) \frac{\rho}{2\omega^3} \\
C_{D_t^3 D_x v_1}^{(0), \text{MRT1}} &= (-2 - \omega_2^2 + 3\omega_2) \frac{\rho}{2\omega_2^3} \\
C_{D_t^3 D_x v_1}^{(0), \text{MRT2}} &= C_{D_t^3 D_x v_1}^{(0), \text{MRT1}} \\
C_{D_t^3 D_x v_1}^{(0), \text{CLBM1}} &= C_{D_t^3 D_x v_1}^{(0), \text{MRT1}} \\
C_{D_t^3 D_x v_1}^{(0), \text{CLBM2}} &= C_{D_t^3 D_x v_1}^{(0), \text{MRT1}} \\
\text{coefficient } C_{D_t^2 D_x^2 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2}: \\
C_{D_t^2 D_x^2 v_1}^{(0), \text{SRT}} &= (-2 + 3\omega - \omega^2) \frac{3v_1 \rho}{2\omega^3} \\
C_{D_t^2 D_x^2 v_1}^{(0), \text{MRT1}} &= (-2\omega_5 \omega_2^3 + 8\omega_5 \omega_2^2 + 2\omega_5^2 + 2\omega_2^3 - 4\omega_5 \omega_2 - 4\omega_2^2 - \omega_5^2 \omega_2 - \omega_5^2 \omega_2^2) \frac{v_1 \rho}{2\omega_5^2 \omega_2^3} \\
C_{D_t^2 D_x^2 v_1}^{(0), \text{MRT2}} &= C_{D_t^2 D_x^2 v_1}^{(0), \text{MRT1}} \\
C_{D_t^2 D_x^2 v_1}^{(0), \text{CLBM1}} &= (-2 - \omega_2^2 + 3\omega_2) \frac{3v_1 \rho}{2\omega_2^3} \\
C_{D_t^2 D_x^2 v_1}^{(0), \text{CLBM2}} &= C_{D_t^2 D_x^2 v_1}^{(0), \text{CLBM1}} \\
\text{coefficient } C_{D_t D_x^3 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial t \partial x_1^3}: \\
C_{D_t D_x^3 v_1}^{(0), \text{SRT}} &= (-36 + 34\omega^2 c s^2 + 42\omega^2 v_1^2 + 72v_1^2 - 2\omega^3 c s^2 - 3\omega^3 v_1^2 + 60c s^2 + 54\omega + \omega^3 - 20\omega^2 - 108\omega v_1^2 - 90\omega c s^2) \frac{\rho}{12\omega^3} \\
C_{D_t D_x^3 v_1}^{(0), \text{MRT1}} &= (24\omega_5 \omega_2 c s^2 - 9\omega_5 \omega_2^3 - 6\omega_2^3 c s^2 + 24\omega_5^2 c s^2 + 25\omega_5^2 \omega_2^2 c s^2 + 36\omega_5 \omega_2^2 + 48\omega_5 v_1^2 \omega_2 + 6\omega_2^3 - 24\omega_5 \omega_2 + 12\omega_2^2 c s^2 - 60\omega_5 v_1^2 \omega_2^2 - 12\omega_2^2 + 15\omega_5 v_1^2 \omega_2^3 + 27\omega_5^2 v_1^2 \omega_2^2 - 48\omega_5^2 \omega_2 c s^2 - 6v_1^2 \omega_2^3 + 12v_1^2 \omega_2^2 - 42\omega_5^2 v_1^2 \omega_2 + \\
12\omega_2^2 \omega_2^3 - 36\omega_5 \omega_2^2 c s^2 + 12\omega_5^2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3} \\
C_{D_t D_x^3 v_1}^{(0), \text{MRT2}} &= \\
(9c s^2 \omega_5 \omega_2^3 - 9\omega_5 \omega_2^3 - 36c s^2 \omega_5 \omega_2^2 + 36\omega_5 \omega_2^2 + 48\omega_5 v_1^2 \omega_2 + 6\omega_2^3 - 24\omega_5 \omega_2 + 24c s^2 \omega_5 \omega_2 - 60\omega_5 v_1^2 \omega_2^2 - 12\omega_2^2 + 15\omega_5 v_1^2 \omega_2^3 + 27\omega_5^2 v_1^2 \omega_2^2 - 48c s^2 \omega_5^2 \omega_2 + \\
12\omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 - 11\omega_5^2 \omega_2^2 + 25c s^2 \omega_5^2 \omega_2^2 - 6v_1^2 \omega_2^3 - 6c s^2 \omega_2^3 + 24c s^2 \omega_5^2 + 12v_1^2 \omega_2^2 - 42\omega_5^2 v_1^2 \omega_2 + \omega_5^2 \omega_2^3 - 2c s^2 \omega_5^2 \omega_2^3 + 12\omega_5^2 v_1^2 + 12c s^2 \omega_5^2) \frac{\rho}{12\omega_5^2 \omega_2^3} \\
C_{D_t D_x^3 v_1}^{(0), \text{CLBM1}} &= \\
(-48\omega_5^2 \omega_2 c s^2 - 9\omega_5 \omega_2^3 + 36\omega_5 \omega_2^2 + 72\omega_5 v_1^2 \omega_2 - 36\omega_5 \omega_2^2 c s^2 + 6\omega_2^3 - 24\omega_5 \omega_2 - 108\omega_5 v_1^2 \omega_2^2 - 12\omega_2^2 + 9\omega_5 \omega_2^3 c s^2 + 27\omega_5 v_1^2 \omega_2^3 + 12\omega_2^2 c s^2 + 15\omega_5^2 v_1^2 \omega_2^2 + \\
12\omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 - 2\omega_5^2 \omega_2^2 c s^2 - 11\omega_5^2 \omega_2^2 - 6\omega_2^3 c s^2 + 24\omega_5 \omega_2 c s^2 - 18v_1^2 \omega_2^3 + 24\omega_5^2 c s^2 + 36v_1^2 \omega_2^2 + 18\omega_5^2 v_1^2 \omega_2 + 25\omega_5^2 \omega_2^2 c s^2 + \omega_5^2 \omega_2^3 - 36\omega_5^2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3} \\
C_{D_t D_x^3 v_1}^{(0), \text{CLBM2}} &= (25\omega_5^2 \omega_2^2 c s^2 - 9\omega_5 \omega_2^3 + 36\omega_5 \omega_2^2 + 72\omega_5 v_1^2 \omega_2 - 6\omega_2^3 c s^2 + 24\omega_5 \omega_2 c s^2 + 24\omega_5^2 c s^2 + 6\omega_2^3 - 24\omega_5 \omega_2 - 108\omega_5 v_1^2 \omega_2^2 - 2\omega_5^2 \omega_2^3 c s^2 - \\
12\omega_2^2 + 12\omega_2^2 c s^2 + 27\omega_5 v_1^2 \omega_2^3 + 9\omega_5 \omega_2^3 c s^2 + 15\omega_5^2 v_1^2 \omega_2^2 + 12\omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 - 11\omega_5^2 \omega_2^2 - 36\omega_5 \omega_2^2 c s^2 - 18v_1^2 \omega_2^3 - 48\omega_5^2 \omega_2 c s^2 + 36v_1^2 \omega_2^2 + \\
18\omega_5^2 v_1^2 \omega_2 + \omega_5^2 \omega_2^3 - 36\omega_5^2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3} \\
\text{coefficient } C_{D_x^4 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^4}: \\
\end{aligned}$$

$$C_{D_x^4 \rho}^{(0), \text{SRT}} = (-14\omega^2 cs^2 - 84\omega^2 v_1^2 cs^2 + 108\omega v_1^4 - 72\omega cs^4 + 42\omega^2 v_1^2 + 72v_1^2 + \omega^3 cs^2 - 3\omega^3 v_1^2 - 24cs^2 - 72v_1^4 - 3\omega^3 cs^4 + 3\omega^3 v_1^4 + 6\omega^3 v_1^2 cs^2 + 48cs^4 + 216\omega v_1^2 cs^2 + 30\omega^2 cs^4 - 108\omega v_1^2 + 36\omega cs^2 - 42\omega^2 v_1^4 - 144v_1^2 cs^2) \frac{1}{24\omega^3}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT1}} = (-24\omega_5 \omega_2 cs^2 - 48\omega_5^2 \omega_2 cs^4 + 48\omega_5 v_1^2 \omega_2^2 cs^2 + 3\omega_5^2 v_1^4 \omega_2^3 - 8\omega_5^2 \omega_2^2 cs^2 + 48\omega_5 v_1^2 \omega_2 - 24\omega_5^2 v_1^4 \omega_2^2 + 12v_1^2 \omega_2^3 cs^2 - 24\omega_5 \omega_2^2 cs^4 - 24v_1^4 \omega_2^2 + 24\omega_5^2 v_1^4 \omega_2 - 12\omega_5 v_1^2 \omega_2^3 cs^2 - 96\omega_5^2 v_1^2 cs^2 - 72\omega_5 v_1^2 \omega_2^2 - 24v_1^2 \omega_2^2 cs^2 + 6\omega_5 \omega_2^3 cs^4 + 156\omega_5^2 v_1^2 \omega_2 cs^2 + 12v_1^4 \omega_2^3 + 18\omega_5 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 - 48\omega_5 v_1^4 \omega_2 - 72\omega_5^2 v_1^2 \omega_2^2 cs^2 + 24\omega_5^2 v_1^2 \omega_2^2 - 3\omega_5^2 \omega_2^3 cs^4 - 6\omega_5 \omega_2^3 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + 12\omega_5^2 \omega_2 cs^2 + 24\omega_5^2 cs^4 - 12v_1^2 \omega_2^3 - 18\omega_5 v_1^4 \omega_2^3 + 6\omega_5^2 v_1^2 \omega_2^3 cs^2 + 24\omega_5 \omega_2 cs^4 + 24v_1^2 \omega_2^2 - 24\omega_5^2 v_1^2 \omega_2 + 24\omega_5 \omega_2^2 cs^2 + 24\omega_5^2 \omega_2^2 cs^4 - 24\omega_5 v_1^2 \omega_2 cs^2 + 72\omega_5 v_1^4 \omega_2^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT2}} = (-6cs^2 \omega_5 \omega_2^3 + 24cs^4 \omega_5 \omega_2 + 3\omega_5^2 v_1^4 \omega_2^3 + 24cs^2 \omega_5 \omega_2^2 + 48\omega_5 v_1^2 \omega_2 - 24cs^2 \omega_5 v_1^2 \omega_2 - 24\omega_5^2 v_1^4 \omega_2^2 - 24v_1^4 \omega_2^2 + 24\omega_5^2 v_1^4 \omega_2 + 6cs^4 \omega_5 \omega_2^3 - 24cs^2 \omega_5 \omega_2 - 72\omega_5 v_1^2 \omega_2^2 + 48cs^2 \omega_5 v_1^2 \omega_2^2 - 24cs^4 \omega_5 \omega_2^2 + 12v_1^4 \omega_2^3 - 12cs^2 \omega_5 v_1^2 \omega_2^3 + 18\omega_5 v_1^2 \omega_2^3 + 24cs^4 \omega_5^2 + 24cs^4 \omega_5^2 \omega_2^2 - 48\omega_5 v_1^4 \omega_2 - 72cs^2 \omega_5^2 v_1^2 \omega_2^2 + 24\omega_5^2 v_1^2 \omega_2^2 - 3cs^4 \omega_5^2 \omega_2^3 + 12cs^2 \omega_5^2 \omega_2^2 - 3\omega_5^2 v_1^2 \omega_2^3 + 6cs^2 \omega_5^2 v_1^2 \omega_2^3 - 8cs^2 \omega_5^2 \omega_2^2 - 12v_1^2 \omega_2^3 + 12cs^2 v_1^2 \omega_2^3 - 18\omega_5 v_1^4 \omega_2^3 + 24v_1^2 \omega_2^2 - 24cs^2 v_1^2 \omega_2^2 + 156cs^2 \omega_5^2 v_1^2 \omega_2 - 24\omega_5^2 v_1^2 \omega_2 + cs^2 \omega_5^2 \omega_2^3 - 96cs^2 \omega_5^2 v_1^2 - 48cs^4 \omega_5^2 \omega_2 + 72\omega_5 v_1^4 \omega_2^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM1}} = (12\omega_5^2 \omega_2 cs^2 + 24\omega_5^2 cs^4 + 6\omega_5^2 v_1^2 \omega_2^3 cs^2 + 3\omega_5^2 v_1^4 \omega_2^3 + 24\omega_5 \omega_2 cs^4 + 24\omega_5 \omega_2^2 cs^2 - 12\omega_5^2 v_1^4 \omega_2^2 + 72\omega_5 v_1^2 \omega_2 cs^2 + 24\omega_5^2 \omega_2^2 cs^4 - 72v_1^4 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2^2 cs^2 - 72\omega_5 v_1^2 \omega_2^2 - 3\omega_5^2 \omega_2^3 cs^4 + 36v_1^4 \omega_2^3 - 6\omega_5 \omega_2^3 cs^2 + 30\omega_5 v_1^2 \omega_2^3 - 72\omega_5 v_1^2 \omega_2^3 cs^2 + 12v_1^2 \omega_2^3 + 6\omega_5 \omega_2^3 cs^4 - 216v_1^2 \omega_2^2 cs^2 - 36\omega_5^2 v_1^2 \omega_2 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 - 24\omega_5 \omega_2 cs^2 - 36v_1^2 \omega_2^3 + 144\omega_5 v_1^2 \omega_2^2 cs^2 - 48\omega_5^2 \omega_2 cs^4 - 30\omega_5 v_1^4 \omega_2^3 + 72v_1^2 \omega_2^3 - 8\omega_5^2 \omega_2^2 cs^2 + 72\omega_5 v_1^4 \omega_2^2 - 24\omega_5 \omega_2^2 cs^4 + 108v_1^2 \omega_2^3 cs^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM2}} = (-8\omega_5^2 \omega_2 cs^2 + 3\omega_5^2 v_1^4 \omega_2^3 - 24\omega_5 \omega_2^2 cs^4 + 108v_1^2 \omega_2^3 cs^2 - 24\omega_5 \omega_2 cs^2 - 48\omega_5^2 \omega_2 cs^4 + 144\omega_5 v_1^2 \omega_2^2 cs^2 - 12\omega_5^2 v_1^4 \omega_2^2 + 6\omega_5 \omega_2^3 cs^4 - 72v_1^4 \omega_2^2 - 216v_1^2 \omega_2^2 cs^2 - 36\omega_5^2 v_1^2 \omega_2^2 cs^2 - 72\omega_5 v_1^2 \omega_2^2 + \omega_5^2 \omega_2^3 cs^2 - 72\omega_5 v_1^2 \omega_2^3 cs^2 + 36v_1^4 \omega_2^3 + 30\omega_5 v_1^2 \omega_2^3 - 3\omega_5^2 \omega_2^3 cs^4 - 6\omega_5 \omega_2^3 cs^2 + 12\omega_5^2 v_1^2 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2^2 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + 24\omega_5 \omega_2^2 cs^2 - 36v_1^2 \omega_2^3 - 30\omega_5 v_1^4 \omega_2^3 + 24\omega_5^2 \omega_2^2 cs^4 + 72\omega_5 v_1^2 \omega_2^2 cs^2 + 12\omega_5^2 \omega_2^2 cs^2 + 72v_1^2 \omega_2^2 + 24\omega_5^2 cs^4 + 6\omega_5^2 v_1^2 \omega_2^2 cs^2 + 72\omega_5 v_1^4 \omega_2^2 + 24\omega_5 \omega_2^2 cs^4) \frac{1}{24\omega_5^2 \omega_2^3}$$

coefficient  $C_{D_x^4 v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1^4}$ :

$$C_{D_x^4 v_1}^{(0), \text{SRT}} = (24 - 26\omega^2 cs^2 - 22\omega^2 v_1^2 - 36v_1^2 + \omega^3 cs^2 + 2\omega^3 v_1^2 - 48cs^2 - 36\omega - \omega^3 + 14\omega^2 + 54\omega v_1^2 + 72\omega cs^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT1}} = (-12\omega_5 \omega_2 cs^2 + 6\omega_5 \omega_2^3 + 6\omega_2^3 cs^2 - 24\omega_5^2 \omega_2^2 cs^2 - 20\omega_5^2 \omega_2^2 - 24\omega_5 \omega_2^2 - 12\omega_5 v_1^2 \omega_2 - 6\omega_2^3 + 12\omega_5 \omega_2 - 12\omega_2^2 cs^2 + 24\omega_5 v_1^2 \omega_2^2 + 12\omega_2^2 - 6\omega_5 v_1^2 \omega_2^2 + 12\omega_2^2 - 6\omega_5 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 - 16\omega_5^2 v_1^2 \omega_2^2 - 6\omega_5^2 \omega_2 - 24\omega_5 \omega_2^2 - 36v_1^2 \omega_2^3 - 6\omega_5 \omega_2^3 cs^2 + 24\omega_5^2 \omega_2^2 cs^2 - 36v_1^2 \omega_2^3 + 30\omega_5 v_1^2 \omega_2^3 - 72\omega_5 v_1^2 \omega_2^3 cs^2 + 12v_1^2 \omega_2^3 + 6\omega_5 \omega_2^3 cs^4 - 6\omega_5 \omega_2^3 + 12\omega_5^2 v_1^2 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2^2 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + 24\omega_5 \omega_2^2 cs^2 - 36v_1^2 \omega_2^3 - 30\omega_5 v_1^4 \omega_2^3 + 24\omega_5^2 \omega_2^2 cs^4 + 72\omega_5 v_1^2 \omega_2^2 cs^2 + 12\omega_5^2 \omega_2^2 cs^2 + 72v_1^2 \omega_2^2 + 24\omega_5^2 cs^4 + 6\omega_5^2 v_1^2 \omega_2^2 cs^2 + 72\omega_5 v_1^4 \omega_2^2 + 24\omega_5 \omega_2^2 cs^4) \frac{1}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT2}} = (-6cs^2 \omega_5 \omega_2^3 + 6\omega_5 \omega_2^3 + 24cs^2 \omega_5 \omega_2^2 - 24\omega_5 \omega_2^2 - 12\omega_5 v_1^2 \omega_2 - 6\omega_2^3 + 12\omega_5 \omega_2 - 12\omega_2^2 cs^2 + 24\omega_5 v_1^2 \omega_2^2 + 12\omega_2^2 - 6\omega_5 v_1^2 \omega_2^3 - 16\omega_5^2 v_1^2 \omega_2^2 + 42cs^2 \omega_5^2 \omega_2 - 6\omega_5 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^3 + 8\omega_5^2 \omega_2^2 + 24\omega_5^2 \omega_2 cs^2 + 6v_1^2 \omega_2^3 - 12v_1^2 \omega_2^2 + 24\omega_5^2 v_1^2 \omega_2 - \omega_5^2 \omega_2^3 + cs^2 \omega_5^2 \omega_2^3 - 12\omega_5^2 v_1^2 - 12cs^2 \omega_2^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM1}} = (-30\omega_5^2 \omega_2 cs^2 + 12\omega_5 \omega_2^3 - 24\omega_5 \omega_2^2 + 60\omega_5 v_1^2 \omega_2 + 72\omega_5 \omega_2^2 cs^2 - 18\omega_2^3 - 12\omega_5 \omega_2 + 24\omega_5 v_1^2 \omega_2^2 + 36\omega_2^2 - 24\omega_5 \omega_2^3 cs^2 - 24\omega_5 v_1^2 \omega_2^3 - 60\omega_2^2 cs^2 + 2\omega_5^2 v_1^2 \omega_2^2 + 6\omega_5^2 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 + 2\omega_5^2 \omega_2^2 + 30\omega_2^3 cs^2 - 12\omega_5 \omega_2 cs^2 + 42v_1^2 \omega_2^3 + 24\omega_5^2 cs^2 - 84v_1^2 \omega_2^3 - 12\omega_5^2 v_1^2 \omega_2 - 2\omega_5^2 \omega_2^2 cs^2 - \omega_5^2 \omega_2^3 - 12\omega_5^2 v_1^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM2}} = (-2\omega_5^2 \omega_2 cs^2 + 12\omega_5 \omega_2^3 - 24\omega_5 \omega_2^2 + 60\omega_5 v_1^2 \omega_2 + 30\omega_2^3 cs^2 - 12\omega_5 \omega_2 cs^2 + 24\omega_5^2 cs^2 - 18\omega_2^3 - 12\omega_5 \omega_2 + 24\omega_5 v_1^2 \omega_2^2 + 36\omega_2^2 - 24\omega_5 \omega_2^3 cs^2 - 24\omega_5 v_1^2 \omega_2^3 - 60\omega_2^2 cs^2 + 2\omega_5^2 v_1^2 \omega_2^2 + 6\omega_5^2 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^3 + 8\omega_5^2 \omega_2^2 + 24\omega_5^2 \omega_2 cs^2 + 2\omega_5^2 v_1^2 \omega_2^2 + 6\omega_5^2 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^3 + 2\omega_5^2 \omega_2^2 + 72\omega_5 \omega_2^2 cs^2 + 42v_1^2 \omega_2^3 - 30\omega_5 \omega_2 cs^2 - 84v_1^2 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2 - \omega_5^2 \omega_2^3 - 12\omega_5^2 v_1^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

coefficient  $C_{D_t^3 D_y v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t^3 \partial x_2}$ :

$$C_{D_t^3 D_y v_2}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{MRT1}} = (-2 - \omega_3^2 + 3\omega_3) \frac{\rho}{2\omega_3^3}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{MRT2}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{CLBM1}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_y v_2}^{(0), CLBM2} = C_{D_t^3 D_y v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_t^2 D_x D_y v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2}$ :

$$C_{D_t^2 D_x D_y v_1}^{(0), SRT} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), MRT1} = (-24\omega_2^2\omega_3 - \omega_2^2\omega_3^3 + 12\omega_2^2 + 13\omega_2^2\omega_3^2 + 12\omega_3^2 - 24\omega_2\omega_3^2 + 7\omega_2\omega_3^3 - 6\omega_3^3 + 12\omega_2\omega_3) \frac{v_2 \rho}{12\omega_2^2\omega_3^3}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), MRT2} = C_{D_t^2 D_x D_y v_1}^{(0), MRT1}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), CLBM1} = C_{D_t^2 D_x D_y v_1}^{(0), MRT1}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), CLBM2} = C_{D_t^2 D_x D_y v_1}^{(0), MRT1}$$

**coefficient**  $C_{D_t^2 D_x D_y v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2}$ :

$$C_{D_t^2 D_x D_y v_2}^{(0), SRT} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), MRT1} = (-24\omega_2^2\omega_3 - \omega_2^3\omega_3^2 + 7\omega_2^3\omega_3 - 6\omega_2^3 + 12\omega_2^2 + 13\omega_2^2\omega_3^2 + 12\omega_3^2 - 24\omega_2\omega_3^2 + 12\omega_2\omega_3) \frac{v_1 \rho}{12\omega_2^3\omega_3^2}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), MRT2} = C_{D_t^2 D_x D_y v_2}^{(0), MRT1}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), CLBM1} = C_{D_t^2 D_x D_y v_2}^{(0), MRT1}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), CLBM2} = C_{D_t^2 D_x D_y v_2}^{(0), MRT1}$$

**coefficient**  $C_{D_t D_x^2 D_y v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2}$ :

$$C_{D_t D_x^2 D_y v_1}^{(0), SRT} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 v_2 \rho}{6\omega^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), MRT1} = (-6\omega_5\omega_3^3 + 3\omega_2^3\omega_3^3 + 24\omega_5\omega_2\omega_3^3 - 12\omega_5\omega_2\omega_3^2 - 6\omega_2^3\omega_3^2 - 6\omega_2^2\omega_3^3 + 12\omega_2^2\omega_3^2 - 7\omega_5\omega_2^3\omega_3^2 + \omega_5\omega_2^3\omega_3^3 - 6\omega_5\omega_2^2\omega_3 + 12\omega_5\omega_2^2\omega_3^2 - 12\omega_5\omega_3^3 - 10\omega_5\omega_2^2\omega_3^3 + 12\omega_5\omega_2^3\omega_3) \frac{v_1 v_2 \rho}{6\omega_5\omega_2^3\omega_3^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), MRT2} = C_{D_t D_x^2 D_y v_1}^{(0), MRT1}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), CLBM1} = (\omega_2^3\omega_3^3 - 6\omega_2^2\omega_3 - 7\omega_2^3\omega_3^2 - 7\omega_2^2\omega_3^3 + 12\omega_2^3\omega_3 - 6\omega_2^3 + 6\omega_2^2\omega_3^2 + 18\omega_2\omega_3^3 - 12\omega_3) \frac{v_1 v_2 \rho}{6\omega_2^3\omega_3^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), CLBM2} = C_{D_t D_x^2 D_y v_1}^{(0), CLBM1}$$

**coefficient**  $C_{D_t D_x^2 D_y v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2}$ :

$$C_{D_t D_x^2 D_y v_2}^{(0), SRT} = (34\omega^2 cs^2 - 2\omega^2 v_1^2 - 2\omega^3 cs^2 + \omega^3 v_1^2 + 60cs^2 - 90\omega cs^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), MRT1} = (12\omega_5^2\omega_3 cs^2 + 9\omega_5 v_1^2\omega_2^3\omega_3 - 24\omega_5^2 v_1^2\omega_3 + 12\omega_5\omega_2\omega_3 cs^2 - 18\omega_5^2\omega_2^2 cs^2 + 36\omega_5^2 v_1^2\omega_2\omega_3 + 12v_1^2\omega_2^2\omega_3 - 6\omega_2^3\omega_3 cs^2 + 12\omega_5 v_1^2\omega_2^2 + 9\omega_5\omega_2^3\omega_3 cs^2 - 30\omega_5 v_1^2\omega_2^2\omega_3 - 6v_1^2\omega_2^3\omega_3 + 22\omega_5^2\omega_2^2\omega_3 cs^2 - 6\omega_5 v_1^2\omega_2^3 + 3\omega_5^2\omega_2^3 cs^2 + 6\omega_5^2 v_1^2\omega_2^2 + 12\omega_2^2\omega_3 cs^2 + \omega_5^2 v_1^2\omega_2^3\omega_3 - 6\omega_5\omega_2^3 cs^2 - 30\omega_5^2\omega_2\omega_3 cs^2 + 12\omega_5 v_1^2\omega_2\omega_3 - \omega_5^2 v_1^2\omega_2^3 + 12\omega_5^2\omega_2 cs^2 - 10\omega_5^2 v_1^2\omega_2^2\omega_3 - 12\omega_5^2 v_1^2\omega_2 - 30\omega_5\omega_2^2\omega_3 cs^2 + 12\omega_5\omega_2^2 cs^2) \frac{\rho}{12\omega_5^2\omega_2^3\omega_3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), MRT2} = (9\omega_5 v_1^2\omega_2^3\omega_3 - 24\omega_5^2 v_1^2\omega_3 - 6cs^2\omega_5\omega_2^3 + 12cs^2\omega_2^2\omega_3 + 36\omega_5^2 v_1^2\omega_2\omega_3 + 12cs^2\omega_5\omega_2^2 + 12v_1^2\omega_2^2\omega_3 - 2cs^2\omega_5^2\omega_2^3\omega_3 - 6cs^2\omega_5\omega_2^3\omega_3 + 12cs^2\omega_5^2\omega_3 + 12\omega_5 v_1^2\omega_2^2 - 30\omega_5 v_1^2\omega_2^2\omega_3 + 22cs^2\omega_5^2\omega_2^2\omega_3 - 6v_1^2\omega_2^3\omega_3 - 6\omega_5 v_1^2\omega_2^3 + 30cs^2\omega_5^2\omega_2\omega_3 + 6\omega_5^2 v_1^2\omega_2^2 + \omega_5^2 v_1^2\omega_2^3\omega_3 - 30cs^2\omega_5\omega_2^2\omega_3 + 12cs^2\omega_5^2\omega_2\omega_3 + 12\omega_5 v_1^2\omega_2^2 + 12\omega_5 v_1^2\omega_2\omega_3 - \omega_5^2 v_1^2\omega_2^3 - 18cs^2\omega_5^2\omega_2^2 - 10\omega_5^2 v_1^2\omega_2^2\omega_3 - 12\omega_5^2 v_1^2\omega_2 - 3cs^2\omega_5^2\omega_2^2 + 9cs^2\omega_5\omega_2^3\omega_3) \frac{\rho}{12\omega_5^2\omega_2^3\omega_3}$$

$$C_{\substack{D_1^0 D_2^0 D_3 v_2}}^{(0), \text{CLBM1}} = (12w_5^2 w_2 c s^2 - 9w_5 v_1^2 w_2^3 w_3 + 24w_5^2 v_1^2 w_3 + 9w_5 w_2^3 c s^2 w_3 - 36w_5^2 v_1^2 w_2 w_3 + 22w_5^2 w_2^2 c s^2 w_3 + 12w_5 w_2^2 c s^2 - 12v_1^2 w_2^2 w_3 + 12w_5^2 c s^2 w_3 - 12w_5 v_1^2 w_2^2 + 30w_5 v_2^2 w_2^2 w_3 + 12w_5 w_2 c s^2 w_3 - 6w_5 w_2^3 c s^2 + 6v_1^2 w_3^2 w_3 + 6w_5 v_1^2 w_3^3 - 6w_2^3 c s^2 w_3 - 2w_5^2 w_2^3 c s^2 w_3 - 6w_5^2 v_1^2 w_2^2 + w_5^2 v_1^2 w_3^2 w_3 - 12w_5 v_1^2 w_2 w_3 - w_5^2 v_1^2 w_2^3 - 30w_5 w_2^2 c s^2 w_3 + 3w_5^2 w_2^3 c s^2 + 8w_5^2 v_1^2 w_2^2 w_3 + 12w_2^2 c s^2 w_3 + 12w_5^2 v_1^2 w_2 - 18w_5 w_2^2 c s^2 - 30w_5^2 w_2 c s^2 w_3) \frac{\rho}{12w_5^2 w_3^2 w_3}$$

$$C_{\substack{D_1 D_2 \\ D_3 v_2}}^{(0), \text{CLBM2}} = (12w_5 w_2 w_3 c s^2 - 9w_5 v_1^2 w_3^2 w_3 + 24w_5^2 v_1^2 w_3 - 18w_5^2 w_2^2 c s^2 - 6w_2^3 w_3 c s^2 - 36w_5^2 v_1^2 w_2 w_3 + 12w_5^2 w_3 c s^2 - 12v_1^2 w_2^2 w_3 + 22w_5^2 w_2^2 w_3 c s^2 - 12w_5 v_1^2 w_2^2 + 3w_5^2 w_3^2 c s^2 + 30w_5 v_1^2 w_2^2 w_3 + 6v_1^2 w_3^2 w_3 + 6w_5 v_1^2 w_2^3 + 9w_5 w_2^3 w_3 c s^2 - 6w_5 w_2^3 c s^2 - 6w_5^2 v_1^2 w_2^2 - 30w_5^2 w_2 w_3 c s^2 + w_5^2 v_1^2 w_3^2 w_3 - 12w_5 v_1^2 w_2 w_3 - w_5^2 v_1^2 w_2^3 + 12w_2^2 w_3 c s^2 + 8w_5^2 v_1^2 w_2^2 w_3 - 30w_5 w_2^2 w_3 c s^2 + 12w_5 w_2 c s^2 + 12w_5^2 w_2 c s^2 + 12w_5^2 v_1^2 w_2 - 2w_5^2 w_3^2 w_3 c s^2) \frac{\rho}{12w_5^2 w_3^2 w_3}$$

coefficient  $C_{D_x^3 D_y \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$ :

$$C_{\mathrm{D}_x^0 \mathrm{D}_y \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_1 v_2}{6\omega^3}$$

$$\begin{aligned} C_{D_x^3 D_y \rho}^{(0), MRT1} = & (42\omega_5 v_1^2 \omega_2^2 w_3^3 + 78\omega_5^2 w_2 w_3^3 c s^2 - 12\omega_5 w_2^2 w_3^3 c s^2 - 3w_2^3 w_3^3 - 3w_2^2 w_2^2 w_3^2 + 12\omega_5 w_2 w_3^3 - 12w_5^2 w_3^2 w_3^2 c s^2 - \\ & 12w_5^2 w_2^2 w_3^2 c s^2 + 6v_1^2 w_3^2 w_3^3 + 7w_2^5 w_2^2 w_3^3 + w_2^5 w_3^2 w_3^2 + 6w_2^2 w_3^3 + 42\omega_5 w_2^2 w_3^2 c s^2 + 12w_5^2 v_1^2 w_2 w_3^2 - 12w_5 v_1^2 w_3^2 w_3^3 + 24w_5^2 v_1^2 w_3^3 - 24w_5^2 w_3 w_3^2 c s^2 - \\ & w_5^2 w_3^2 w_3^3 - 12v_1^2 w_2^2 w_3^3 - 12w_5^2 w_2^2 w_3 c s^2 + 6w_5 v_1^2 w_3^2 w_3^3 - 30w_2^2 v_1^2 w_2 w_3^2 + 6w_5^2 w_3^2 w_3^3 c s^2 - 3w_5 w_3^2 w_3^2 + 6w_3^2 w_3^3 c s^2 + 42w_5^2 w_2^2 w_3^2 c s^2 + 6w_5^2 v_1^2 w_2^2 w_3^3 - \\ & 24w_5 w_2 w_3^3 c s^2 - 12w_5^2 v_1^2 w_2^2 w_3 + 6w_5 w_2^2 w_3^3 - 12w_5^2 v_1^2 w_2^2 w_3^2 + 6w_2^2 v_1^2 w_2^2 w_3^2 + 6w_5 w_2^2 w_3^2 c s^2 - 36w_5^2 w_3^2 c s^2 + 6w_2^2 w_2^2 w_3 c s^2 + 6w_5^2 v_1^2 w_2^2 w_3 - \\ & 48w_5^2 w_2 w_3^2 c s^2 - 6w_2^2 w_2 w_3^3 + 6w_5 w_2^2 w_3^2 - 24w_5 v_1^2 w_2 w_3^3 - 12w_5 w_2^2 w_3^2 c s^2 + 6w_5^2 v_1^2 w_2^2 w_3^2 - 21w_5 w_2^2 w_3^3) \frac{v_1^2 w_3^3}{6w_5^2 w_2^2 w_3^3} \end{aligned}$$

$$C_{\substack{D_5^3 D_4 \gamma \rho}}^{(0), \text{MRT2}} = (42w_5v_1^2w_2^2w_3^3 - 36cs^2w_5^2w_3^3 - 24cs^2w_5w_2w_3^3 - 3w_2^3w_3^3 - 3w_5^2w_2^2w_3^2 + 6cs^2w_3^2w_3^3 + 12w_5w_2w_3^3 + 42cs^2w_5^2w_2^2w_3^2 - 12w_5v_1^2w_2^2w_3^2 + 6v_1^2w_3^3w_3^3 - 48cs^2w_5^2w_2^2w_3^3 + 7w_5^2w_2^2w_3^3 + 6cs^2w_5^2w_3^3w_3 - 12cs^2w_3^2w_3^3 + w_5^2w_3^3w_3^2 + 6w_2^2w_3^3 - 12cs^2w_5^2w_3^2w_3^2 + 12w_5^2v_1^2w_2w_3^2 - 12w_5v_1^2w_2^3w_3^3 + 24w_5^2v_1^2w_3^3 + 6cs^2w_5^2w_2^3w_3^3 - 12cs^2w_5^2w_2^2w_3^3 - w_5^2w_2^3w_3^3 - 12v_1^2w_2^2w_3^3 + 6w_5v_1^2w_2^3w_3^2 - 30w_5^2v_1^2w_2w_3^3 + 6cs^2w_5w_3^3w_3^2 - 3w_5w_3^3w_3^2 + 6w_5^2v_1^2w_2^2w_3^3 - 12w_5^2w_1^2w_2^3w_3 + 6w_5w_2^3w_3^3 - 12cs^2w_5w_3^3w_3^3 - 12w_5^2v_1^2w_2^2w_3^2 + 6w_5^2v_1^2w_3^2w_3^3 + 6w_5^2v_1^2w_2^2w_3^3 - 6w_5^2w_2w_3^3 - 12cs^2w_5w_2^2w_3^2 + 78cs^2w_5^2w_2w_3^3 + 6w_5w_2^2w_3^2 - 24w_5v_1^2w_2w_3^3 + 6w_5^2v_1^2w_2^3w_3^2 - 21w_5w_2^2w_3^3 - 24cs^2w_5^2w_2w_3^2 + 42cs^2w_5w_2^2w_3^2) \frac{v_1v_2}{6w_5^2w_2^3w_3^3}$$

$$\begin{aligned} C_{\text{D}_3^{\text{D}_3}\text{Y}_3^{\text{D}_3}}^{(0),\text{CLBM1}} = & (12w_5v_1^2w_2^2w_3^3 - 12w_5^2cs^2w_3^3 - 3w_3^2w_3^3 - 3w_5^2w_2^2w_3^2 + 12w_5w_2w_3^3 + 18w_3^2cs^2w_3^3 - 12w_5^2w_2^2cs^2w_3 - 24w_5w_2cs^2w_3^3 - 6v_1^2w_3^2w_3^3 + \\ & 7w_5^2w_2^2w_3^3 + w_2^2w_3^2w_3^2 + 6w_2^2w_3^3 - 24w_5w_2^3cs^2w_3^3 + 36w_5^2w_2^2cs^2w_3^2 - w_2^2w_3^2w_3^3 + 12v_1^2w_2^2w_3^3 + 12w_5w_3^2cs^2w_3^2 - 36w_5^2w_2^2cs^2w_3^3 + 12w_5^2v_1^2w_2w_3^3 - 3w_5w_3^2w_3^2 + \\ & 6w_5^2w_3^3cs^2w_3^2 - 36w_2^2cs^2w_3^3 - 6w_5^2v_1^2w_2^2w_3^3 - 12w_5^2w_2cs^2w_3^2 - 12w_5^2v_1^2w_2^2w_3^3 + 6w_5w_3^2w_3^3 + 36w_5^2w_2cs^2w_3^3 - 6w_5^2v_1^2w_2^2w_3^2 + 6w_5^2v_1^2w_2^3 + 6w_5^2w_2^2w_3^2 + \\ & 6w_5^2w_2^2cs^2w_3^3 - 24w_5w_2^3cs^2w_3^2 - 6w_5^2w_2w_3^3 + 6w_5w_2^2w_3^2 - 12w_5^2w_2^2cs^2w_3^2 + 72w_5w_2^2cs^2w_3^3 - 24w_5v_1^2w_2w_3^3 + 6w_5^2v_1^2w_2^2w_3^2 - 21w_5w_2^2w_3^3) \frac{v_1^2v_2^2}{6w_5^2w_2^2w_3^3} \end{aligned}$$

$$C_{D_x^2 D_y}^{(0), \text{CLBM2}} = (-12 w_5^2 w_3^2 w_3^2 c s^2 - 36 w_2^2 w_3^3 c s^2 + 12 w_5 v_1^2 w_2^2 w_3^3 - 3 w_3^2 w_3^3 - 3 w_5^2 w_2^2 w_3^2 + 12 w_5 w_2 w_3^3 + 36 w_5^2 w_3^2 w_3^3 c s^2 - 24 w_5 w_2^2 w_3^2 c s^2 - 6 v_1^2 w_3^2 w_3^3 + 7 w_2^2 w_3^2 w_3^3 + w_5^2 w_3^2 w_3^2 + 6 w_2^2 w_3^3 - 12 w_5^2 w_2^2 w_3 c s^2 + 6 w_5^2 w_3^2 w_3^2 c s^2 - w_5^2 w_3^2 w_3^3 + 12 w_1^2 w_2^2 w_3^3 + 72 w_5 w_2^2 w_3^3 c s^2 - 12 w_5^2 w_2 w_3^2 c s^2 + 12 w_5^2 v_1^2 w_2 w_3^3 - 3 w_5 w_3^2 w_3^2 - 12 w_5^2 w_3^2 c s^2 + 12 w_5 w_3^2 w_3^2 c s^2 - 6 w_5^2 v_1^2 w_2^2 w_3^3 - 12 w_5^2 v_1^2 w_3^2 w_3^3 + 6 w_5 w_3^2 w_3^3 + 18 w_3^2 w_3^2 c s^2 + 36 w_5^2 w_2^2 w_3^2 c s^2 - 6 w_5^2 v_1^2 w_2^2 w_3^2 - 24 w_5 w_2 w_3^3 c s^2 + 6 w_5^2 v_1^2 w_3^2 w_3^3 - 24 w_5 w_3^2 w_3^2 c s^2 + 6 w_5^2 v_1^2 w_2^2 w_3 - 6 w_5^2 w_2 w_3^3 + 6 w_5 w_2^2 w_3^2 - 24 w_5 v_1^2 w_2 w_3^3 + 6 w_5^2 w_2^3 w_3 c s^2 - 36 w_5^2 w_2^2 w_3^2 c s^2 + 6 w_5^2 v_1^2 w_2^3 w_3^2 - 21 w_5 w_2 w_3^3) \frac{v_1 v_2^2}{6 w_5^2 w_2^2 w_3^3}$$

coefficient  $C_{D_x^3 D_y v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_2}$ :

$$C_{\substack{D_3^{(0),\text{SRT}} \\ D_x^3 D_y v_1}} = (12 - 56\omega^2 cs^2 - 12\omega^2 v_1^2 - 12v_1^2 + 4\omega^3 cs^2 + 3\omega^3 v_1^2 - 96cs^2 - 18\omega - \omega^3 + 8\omega^2 + 18\omega v_1^2 + 144\omega cs^2) \frac{v_2 \rho}{12w^3}$$

$$\begin{aligned} C_{\text{D}_3^2 \text{D}_3^2 \text{v}_1^2}^{(0), \text{MRT1}} = & (36w_5 v_1^2 w_2^2 w_3^3 + 36w_5^2 w_2 w_3^3 c s^2 - 24w_5 w_2^2 w_3^2 c s^2 - 6w_5^2 w_2^2 w_3^2 - 12w_5^2 w_3^2 w_2^3 c s^2 - 12w_2^2 w_3^3 c s^2 - 24w_5 v_1^2 w_2^2 w_3^2 + 6v_1^2 w_3^2 w_3^3 + \\ & 3w_5^2 w_2^2 w_3^3 + 2w_5^2 w_3^2 w_3^3 + 36w_5 w_2^2 w_3^3 c s^2 - 12w_5 v_1^2 w_3^2 w_3^3 + 24w_5^2 v_1^2 w_3^2 - 24w_5^2 w_2 w_3^2 c s^2 - w_5^2 w_3^2 w_3^3 - 12v_1^2 w_2^2 w_3^3 - 12w_2^2 w_2^2 w_3 c s^2 + 12w_5 v_1^2 w_3^2 w_3^3 - \\ & 30w_5^2 v_1^2 w_2 w_3^3 + 4w_5^2 w_3^2 w_3^3 c s^2 - 6w_5 w_2^2 w_3^3 + 6w_3^2 w_3^3 c s^2 + 48w_5^2 w_2^2 w_3^2 c s^2 - 12w_5 w_2 w_3^3 c s^2 - 18w_2^2 v_1^2 w_3^2 w_3 + 3w_5 w_3^2 w_3^3 + 12w_5^2 v_1^2 w_2^2 w_3^2 + 12w_5^2 w_2^2 w_3^2 w_3^3 + \\ & 12w_5 w_3^2 w_3^3 c s^2 - 12w_5^2 w_3^2 c s^2 + 3w_5^2 v_1^2 w_3^2 w_3^3 + 6w_5^2 w_3^2 w_3 c s^2 - 32w_5^2 w_2^2 w_3^3 c s^2 + 12w_5 w_2^2 w_3^2 - 12w_5 v_1^2 w_3^2 w_3^3 - 12w_5 w_3^2 w_3 c s^2 - 6w_5 w_2^2 w_3^3) \frac{v_2^2 \rho}{12w_5^2 w_3^2 w_3^3} \end{aligned}$$

$$C_{\substack{D_3^0 D_2^0 v_1}}^{(0), \text{MRT2}} = (36w_5^2 v_1^2 w_2^2 w_3^3 - 12c s^2 w_5^2 w_3^3 - 12c s^2 w_5 w_2 w_3^3 - 6w_5^2 w_2^2 w_3^2 + 6c s^2 w_3^2 w_3^3 + 48c s^2 w_5^2 w_2^2 w_3^2 - 24w_5 v_1^2 w_2^2 w_3^2 + 6v_1^2 w_3^2 w_3^3 - 32c s^2 w_5^2 w_2^2 w_3^3 + 3w_5^2 w_2^2 w_3^3 + 6c s^2 w_5^2 w_2^2 w_3^3 - 12c s^2 w_2^2 w_3^3 + 2w_5^2 w_3^2 w_3^3 - 12c s^2 w_5^2 w_3^2 w_3^3 - 12w_5 v_1^2 w_2^3 w_3^3 + 24w_5^2 v_1^2 w_3^3 + 4c s^2 w_5^2 w_3^3 - 12c s^2 w_5^2 w_2^2 w_3 - w_5^2 w_3^2 w_3^3 - 12v_1^2 w_2^2 w_3^3 + 12w_5 v_1^2 w_3^2 w_3^3 - 30w_5^2 v_1^2 w_2 w_3^3 + 12c s^2 w_5 w_3^2 w_3^3 - 6w_5 w_2^3 w_3^2 - 18w_5^2 v_1^2 w_3^2 w_3 + 3w_5 w_3^2 w_3^3 - 12c s^2 w_5 w_3^2 w_3^3 + 12w_5^2 v_1^2 w_2^2 w_3^2 + 12w_5^2 w_2^2 w_3^2 + 3w_5^2 v_1^2 w_2^3 w_3^3 - 24c s^2 w_5 w_2^2 w_3^2 + 36c s^2 w_5^2 w_2 w_3^2 + 12w_5 w_2^2 w_3^2 - 12w_5 v_1^2 w_2 w_3^3 - 6w_5 w_2^2 w_3^3 - 24c s^2 w_5 w_2 w_3^2 + 36c s^2 w_5 w_2 w_3^3) \frac{v_2 \rho}{12w_5^2 w_2^2 w_3^3}$$

$$\begin{aligned}
C_{\text{D}^3 \text{Y}^1 v_1}^{(0), \text{CLBM}} = & (-12w_5v_1^2w_2^2w_3^3 - 12w_5^2cs^2w_3^3 - 6w_5^2w_2^2w_3^2 + 6w_3^2cs^2w_3^3 - 12w_5^2w_2^2cs^2w_3 - 12w_5w_2cs^2w_3^3 - 24w_5v_1^2w_2^2w_3^2 - 6v_1^2w_3^2w_3^3 + 3w_5^2w_2^2w_3^3 + \\
& 2w_5^2w_3^2w_3^3 - 12w_5w_3^2cs^2w_3^3 + 48w_5^2w_2^2cs^2w_3^2 - 24w_5^2v_1^2w_3^3 - w_5^2w_3^2w_3^3 + 12v_1^2w_2^2w_3^3 + 12w_5v_1^2w_3^2w_3^2 + 12w_5w_3^2cs^2w_3^2 - 32w_5^2w_2^2cs^2w_3^3 + 30w_5^2v_1^2w_2w_3^3 - \\
& 6w_5w_3^2w_3^3 + 6w_5^2w_3^2cs^2w_3^2 - 12w_2^2cs^2w_3^3 - 12w_5^2v_1^2w_2^2w_3^3 - 24w_5^2w_2^2cs^2w_3^2 - 18w_5^2v_1^2w_3^2w_3^3 + 3w_5w_3^2w_3^3 + 36w_5^2w_2^2cs^2w_3^3 + 12w_5^2v_1^2w_2^2w_3^3 + \\
& 12w_5^2v_1^2w_3^2w_3^3 + 3w_5^2v_1^2w_2^2w_3^2 + 4w_5^2w_3^2cs^2w_3^3 - 24w_5w_3^2cs^2w_3^2 + 12w_5w_2^2w_3^2 - 12w_5^2w_3^2cs^2w_3^2 + 36w_5w_2^2cs^2w_3^3 + 12w_5v_1^2w_2w_3^3 - 6w_5w_2^2w_3^3) \frac{v_2 \rho}{12w_5^2w_3^2w_3^3}
\end{aligned}$$

$$G_{\frac{C}{D}, \frac{CLMBM}{Dyv_1}}^{\frac{O}{D}} = (-12w_5^2w_3^2w_3^2cs^2 - 12w_2^2w_3^3cs^2 - 12w_5v_1^2w_2^2w_3^3 - 6w_5^2w_2^2w_3^2 + 36w_5^2w_2w_3^3cs^2 - 24w_5w_2^2w_3^2cs^2 - 24w_5v_1^2w_2^2w_3^2 - 6v_1^2w_2^3w_3^3 +$$

$$3\omega_5^2\omega_2^2\omega_3^3 + 2\omega_5^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3cs^2 - 24\omega_5^2v_1^2\omega_3^3 + 4\omega_5^2\omega_2^3\omega_3^2cs^2 - \omega_5^2\omega_2^3\omega_3^3 + 12v_1^2\omega_2^2\omega_3^2 + 36\omega_5\omega_2^2\omega_3^2cs^2 + 12\omega_5v_1^2\omega_2^3\omega_3^2 - 24\omega_5^2\omega_2^3\omega_3^2 + 30\omega_5^2v_1^2\omega_2\omega_3^3 - 6\omega_5\omega_2^3\omega_3^2 - 12\omega_5^2\omega_3^2cs^2 + 12\omega_5\omega_2^2\omega_3^2cs^2 - 12\omega_5^2v_1^2\omega_2^2\omega_3^2 - 18\omega_5^2v_1^2\omega_2^3\omega_3^2 + 3\omega_5\omega_2^3\omega_3^3 + 6\omega_5^2\omega_3^2cs^2 + 48\omega_5^2\omega_2^2\omega_3^2cs^2 + 12\omega_5^2v_1^2\omega_2^2\omega_3^2 - 12\omega_5\omega_2\omega_3^2cs^2 + 12\omega_5^2v_1^2\omega_2^3 + 3\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5\omega_2^2\omega_3^2cs^2 + 12\omega_5\omega_2^2\omega_3^2 + 12\omega_5v_1^2\omega_2\omega_3^3 + 6\omega_5^2\omega_2^3\omega_3^2cs^2 - 32\omega_5^2\omega_2^2\omega_3^2cs^2 - 6\omega_5\omega_2^2\omega_3^3) \frac{v_1\rho}{12\omega_5^2\omega_2^3\omega_3^2}$$

**coefficient  $C_{D_x^3 D_y v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1^3 \partial x_2}$ :**

$$C_{D_x^3 D_y v_2}^{(0), SRT} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_1^2 - 36v_1^2 + 4\omega^3 cs^2 + \omega^3 v_1^2 - 96cs^2 - 54\omega - \omega^3 + 20\omega^2 + 54\omega v_1^2 + 144\omega cs^2) \frac{v_1\rho}{12\omega^3}$$

$$C_{D_x^3 D_y v_2}^{(0), MRT1} = (-36\omega_5\omega_2cs^2 + 9\omega_5\omega_3^2 + 6\omega_3^2cs^2 - 48\omega_5^2\omega_2^2cs^2 - 44\omega_5^2\omega_2^3cs^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 12\omega_2^2cs^2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^3 + 4\omega_5^2\omega_2^3cs^2 - 8\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 - 12\omega_5\omega_2^3cs^2 + \omega_5^2v_1^2\omega_2^3 + 11\omega_5^2\omega_2^2 + 90\omega_5^2\omega_2cs^2 + 6v_1^2\omega_2^3 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 48\omega_5\omega_2^2cs^2 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), MRT2} = (-12cs^2\omega_5\omega_3^2 + 9\omega_5\omega_3^3 + 48cs^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 36cs^2\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^3 - 8\omega_5^2\omega_2^3v_1^2 + 90\omega_5^2\omega_2cs^2 + 6v_1^2\omega_2^3 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 4cs^2\omega_5^2\omega_2^3 + 12\omega_5^2v_1^2 - 12cs^2\omega_5^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), CLBM1} = (18\omega_5^2\omega_2cs^2 + 9\omega_5\omega_3^2 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 96\omega_5\omega_2^2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 30\omega_5\omega_2^3cs^2 - 6\omega_5v_1^2\omega_2^3 - 60\omega_2^2cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_3^2 + 4\omega_5^2\omega_2^3cs^2 + 11\omega_5^2\omega_2^2 + 30\omega_5^2\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6v_1^2\omega_2^3 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - 26\omega_5^2\omega_2^2cs^2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), CLBM2} = (-26\omega_5^2\omega_2^2cs^2 + 9\omega_5\omega_3^2 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 30\omega_5^3cs^2 - 36\omega_5\omega_2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 4\omega_5^2\omega_2^3cs^2 + 12\omega_2^2 - 60\omega_2^2cs^2 - 30\omega_5\omega_2^3cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_3^2 + 11\omega_5^2\omega_2^2 + 96\omega_5\omega_2^2cs^2 - 6v_1^2\omega_2^3 + 18\omega_5^2\omega_2cs^2 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

**coefficient  $C_{D_t^2 D_y^2 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t^2 \partial x_2^2}$ :**

$$C_{D_t^2 D_y^2 v_2}^{(0), SRT} = (-2 + 3\omega - \omega^2) \frac{3v_2\rho}{2\omega^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), MRT1} = (-\omega_6^2\omega_3^2 - \omega_6^2\omega_3 - 4\omega_3^2 - 4\omega_6\omega_3 + 2\omega_3^3 - 2\omega_6\omega_3^2 + 2\omega_6^2 + 8\omega_6\omega_3^2) \frac{v_2\rho}{2\omega_6^2\omega_3^2}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), MRT2} = C_{D_t^2 D_y v_2}^{(0), MRT1}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), CLBM1} = (-2 - \omega_3^2 + 3\omega_3) \frac{3v_2\rho}{2\omega_3^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), CLBM2} = C_{D_t^2 D_y v_2}^{(0), CLBM1}$$

**coefficient  $C_{D_t D_x D_y^2 v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2}$ :**

$$C_{D_t D_x D_y^2 v_1}^{(0), SRT} = (34\omega^2 cs^2 - 2\omega^2 v_2^2 + \omega^3 v_2^2 - 2\omega^3 cs^2 + 60cs^2 - 90\omega cs^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), MRT1} = (-30\omega_2v_2^2\omega_6\omega_3^2 + 12\omega_2\omega_6^2cs^2 - 6\omega_6\omega_3^3cs^2 - 30\omega_2\omega_6\omega_3^2cs^2 + 9\omega_2v_2^2\omega_6\omega_3^3 - 30\omega_2\omega_6^2\omega_3cs^2 - 24\omega_2v_2^2\omega_6^2 + 12v_2^2\omega_6\omega_3^2 - 6\omega_2v_2^2\omega_3^3 + 9\omega_2\omega_6\omega_3^3cs^2 + 12\omega_6\omega_3^2cs^2 + 12\omega_2v_2^2\omega_3^2 - 6\omega_2\omega_6\omega_3^3 + 12\omega_2v_2^2\omega_6\omega_3 + 12\omega_6\omega_3^2cs^2 - 2\omega_2\omega_6\omega_3^3cs^2 - v_2^2\omega_6\omega_3^3 + 36\omega_2v_2^2\omega_6^2\omega_3 - 18\omega_6\omega_3^2cs^2 + 6v_2^2\omega_6\omega_3^2 + 12\omega_2\omega_6\omega_3^2cs^2 + 3\omega_6\omega_3^2cs^2 + \omega_2v_2^2\omega_6^2\omega_3^2 - 12v_2^2\omega_6^2\omega_3 + 22\omega_2\omega_6\omega_3^2cs^2 - 10\omega_2v_2^2\omega_6^2\omega_3^2 - 6\omega_2\omega_6\omega_3^3cs^2 + 12\omega_2\omega_6\omega_3^2cs^2) \frac{\rho}{12\omega_2\omega_6^2\omega_3^2}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), MRT2} = (-30\omega_2v_2^2\omega_6\omega_3^2 - 2cs^2\omega_2\omega_6\omega_3^3 - 18cs^2\omega_6\omega_3^2 + 9\omega_2v_2^2\omega_6\omega_3^3 + 3cs^2\omega_6\omega_3^3 + 22cs^2\omega_2\omega_6\omega_3^2 - 24\omega_2v_2^2\omega_6^2 + 12v_2^2\omega_6\omega_3^2 - 6\omega_2v_2^2\omega_3^3 - 30cs^2\omega_2\omega_6\omega_3^2 + 12\omega_2v_2^2\omega_6\omega_3^3 + 12cs^2\omega_6\omega_3^2 + 12\omega_2v_2^2\omega_6\omega_3 + 12cs^2\omega_2\omega_6\omega_3^2 - 12v_2^2\omega_6\omega_3^2 - 6cs^2\omega_6\omega_3^3 - 30cs^2\omega_2\omega_6\omega_3^2 - 10\omega_2v_2^2\omega_6\omega_3^2 + 9cs^2\omega_2\omega_6\omega_3^3 + 12cs^2\omega_6\omega_3^2) \frac{\rho}{12\omega_2\omega_6^2\omega_3^2}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), CLBM1} = (30\omega_2v_2^2\omega_6\omega_3^2 + 9\omega_2cs^2\omega_6\omega_3^3 - 30\omega_2cs^2\omega_6\omega_3^2 + 12\omega_2cs^2\omega_6^2 - 9\omega_2v_2^2\omega_6\omega_3^3 + 24\omega_2v_2^2\omega_6^2 - 12v_2^2\omega_6\omega_3^2 + 6\omega_2v_2^2\omega_3^3 - 6\omega_2cs^2\omega_6\omega_3^3 + 12cs^2\omega_6\omega_3^2 - 12\omega_2v_2^2\omega_3^2 + 6v_2^2\omega_6\omega_3^3 - 12\omega_2v_2^2\omega_6\omega_3 + 12\omega_2cs^2\omega_6\omega_3^2 - 18cs^2\omega_6\omega_3^2 - v_2^2\omega_6\omega_3^3 - 36\omega_2v_2^2\omega_6\omega_3^2 - 6v_2^2\omega_6\omega_3^2 + 3cs^2\omega_6\omega_3^3 - 30\omega_2cs^2\omega_6\omega_3^2 + 22\omega_2cs^2\omega_6\omega_3^2 + \omega_2v_2^2\omega_6\omega_3^3 + 12v_2^2\omega_6\omega_3^2 + 8\omega_2v_2^2\omega_6\omega_3^2 - 2\omega_2cs^2\omega_6\omega_3^3 + 12cs^2\omega_6\omega_3^2) \frac{\rho}{12\omega_2\omega_6^2\omega_3^2}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), CLBM2} = (30\omega_2v_2^2\omega_6\omega_3^2 - 30\omega_2\omega_6^2\omega_3cs^2 + 12\omega_2\omega_6^2cs^2 - 6\omega_6\omega_3^3cs^2 - 9\omega_2v_2^2\omega_6\omega_3^3 - 30\omega_2\omega_6\omega_3^2cs^2 + 24\omega_2v_2^2\omega_6^2 - 12v_2^2\omega_6\omega_3^2 + 6\omega_2v_2^2\omega_3^3 - 12\omega_2v_2^2\omega_6\omega_3^2 + 6v_2^2\omega_6\omega_3^3 + 9\omega_2\omega_6\omega_3^3cs^2 - 12\omega_2v_2^2\omega_6\omega_3 + 12\omega_2\omega_6\omega_3^2cs^2 - 36\omega_2v_2^2\omega_6\omega_3^2 - 2\omega_2\omega_6^2\omega_3^3) \frac{\rho}{12\omega_2\omega_6^2\omega_3^2}$$

$$6v_2^2\omega_6^2\omega_3^2 - 18\omega_6^2\omega_3^2cs^2 + \omega_2v_2^2\omega_6^2\omega_3^3 - 6\omega_2\omega_3^3cs^2 + 12\omega_2\omega_6\omega_3cs^2 + 12v_2^2\omega_6^2\omega_3 + 3\omega_6^2\omega_3^3cs^2 + 8\omega_2v_2^2\omega_6^2\omega_3^2 + 22\omega_2\omega_6^2\omega_3^2cs^2) \frac{\rho}{12\omega_2\omega_6^2\omega_3^3}$$

**coefficient**  $C_{D_t D_x D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2}$ :

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y^2 v_2}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 v_2 \rho}{6\omega^3}$$

$$C_{\substack{D_1 D_2 D_3 \\ D_4 D_5 D_6}}^{(0), \text{MRT1}} = (12\omega_2^2\omega_6\omega_3^2 + 3\omega_2^3\omega_3^3 - 12\omega_2^3\omega_6 - 6\omega_2^3\omega_3^2 - 7\omega_2^2\omega_6\omega_3^2 - 6\omega_2^2\omega_3^3 - 12\omega_2^2\omega_6\omega_3 + 12\omega_2^2\omega_3^2 + \omega_2^3\omega_6\omega_3^3 - 10\omega_2^3\omega_6\omega_3^2 + 24\omega_2^3\omega_6\omega_3 - 6\omega_6\omega_3^3 - 6\omega_2\omega_6\omega_3^2 + 12\omega_2\omega_6\omega_3^3) \frac{\nu_1 \nu_2 \rho}{6\omega_2^3\omega_6\omega_3^3}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y^2 v_2}^{(0), \text{MRT2}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{\substack{D_1 D_2 D_3 v_2}}^{(0), \text{CLBM1}} = (\omega_2^3 \omega_3^3 - 7\omega_2^3 \omega_3^2 - 7\omega_2^2 \omega_3^3 + 18\omega_2^3 \omega_3 - 12\omega_2^3 + 6\omega_2^2 \omega_3^2 - 6\omega_2 \omega_3^2 + 12\omega_2 \omega_3^3 - 6\omega_3^3) \frac{\nu_1 2 \nu_2 \rho}{6\omega_2^3 \omega_3^3}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y^2 v_2}^{(0), \text{CLBM2}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y^2 v_2}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_x^2 D_y^2 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2}$ :

$$C_{\frac{D_2}{D_2} \frac{D_2}{y} \rho}^{(0), \text{SRT}} = (-14\omega^2 v_1^2 cs^2 + 34\omega^2 v_1^2 v_2^2 - 24\omega cs^4 - 14\omega^2 cs^2 v_2^2 - 24cs^2 v_2^2 - \omega^3 cs^4 + 36\omega cs^2 v_2^2 - 3\omega^3 v_1^2 v_2^2 + \omega^3 v_1^2 cs^2 + 16cs^4 + 36\omega v_1^2 cs^2 + 10\omega^2 cs^4 - 84\omega v_1^2 v_2^2 + \omega^3 cs^2 v_2^2 - 24v_1^2 cs^2 + 56v_1^2 v_2^2) \frac{1}{4\omega^3}$$

$$\begin{aligned} C_{\substack{(0), \text{MRT1} \\ \frac{D_2}{D_2} \frac{D_2}{D_2} y}} &= (-4w_2^0 v_2^2 w_2^2 w_3^3 c s^2 - 8 w_5^2 w_2^2 v_2^2 w_6^2 w_3 c s^2 - 38 w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3 - 3 w_5 w_3^2 v_2^2 w_6^2 w_3^3 c s^2 + 2 w_5 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 + 4 w_5^2 w_2^2 w_6^2 w_3^3 c s^4 + \\ w_5^2 v_1^2 w_3^2 w_6^2 w_3^3 c s^2 - 2 w_5 w_3^2 w_6^2 w_3^2 c s^4 - 36 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 2 w_5 v_1^2 w_2^2 w_6^2 w_3^3 c s^2 - 2 w_5 w_2^2 w_6^2 w_3^3 c s^4 + 2 w_5^2 v_1^2 w_3^2 w_6^2 w_3^3 c s^2 + 12 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 c s^2 - \\ 4 w_5^2 w_2^2 w_6^2 w_3^3 c s^4 - 2 w_5 v_1^2 w_3^2 w_6^2 w_3^2 c s^2 + 4 w_5^2 w_2^2 w_6^2 w_3^2 c s^2 + 20 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 20 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 - 4 w_5^2 w_3^2 w_2^2 w_6^2 w_3^2 c s^2 - 3 w_5 v_1^2 w_2^2 w_3^2 w_6^2 w_3^2 + \\ 4 w_5 v_1^2 w_2^2 w_6^2 w_3^2 c s^2 - 12 w_5^2 w_2^2 w_6^2 w_3^2 c s^4 + w_5 w_3^2 w_6^2 w_3^3 c s^4 - 8 w_5^2 v_1^2 w_3^2 w_6^2 w_3^2 c s^2 + 10 w_5 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 3 w_5^2 v_2^2 w_3^2 w_6^2 w_3^2 + 2 w_5 w_3^2 w_2^2 w_6^2 w_3^2 c s^2 - \\ w_5^2 w_3^2 w_2^2 w_6^2 w_3^3 c s^2 - 4 w_5^2 v_1^2 w_3^2 w_6^2 w_3 c s^2 + 20 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3 - 4 w_5^2 v_2^2 w_6^2 w_3^3 c s^2 + w_5 v_1^2 w_3^2 w_6^2 w_3^2 c s^2 - 2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^3 c s^2 + 20 w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 - \\ 4 w_5^2 v_2^2 w_2^2 w_6^2 w_3^3 c s^2 - 4 w_5^2 v_1^2 w_3^2 w_3^2 c s^2 + 4 w_5 w_3^2 w_6^2 w_3^3 c s^4 - 4 w_5 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 2 w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 + 10 w_5^2 v_1^2 w_2^2 w_6 w_3^2 c s^2 + \\ 20 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 4 w_5^2 w_2^2 w_6 w_3^2 c s^4 - 4 w_5 w_2^2 v_2^2 w_6^2 w_3^2 c s^2 + 10 w_5^2 w_2 v_1^2 w_2^2 w_6^2 w_3^2 c s^2 - 2 w_5^2 w_2 w_6^2 w_3^3 c s^4 - 4 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 10 w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2 + \\ 10 w_5^2 v_1^2 w_3^2 w_6^2 w_3^3 c s^2 - 4 w_5^2 v_1^2 w_3^2 v_2^2 w_2^2 + w_5^2 w_3^2 v_2^2 w_6 w_3^2 c s^2 - 38 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 4 w_5^2 w_2^2 w_6^2 w_3 c s^4 + w_5^2 w_3^2 w_6 w_3^2 c s^4 + 2 w_5^2 v_1^2 w_2^2 w_6 w_3^2 c s^2 - \\ 8 w_5^2 w_2^2 v_2^2 w_6^2 w_3^3 c s^2 - 8 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 c s^2 - 3 w_5^2 v_2^2 w_3^2 v_2^2 w_6 w_3^2 - 2 w_5^2 w_3^2 w_2^2 w_6^2 w_3 c s^4 - 4 w_5^2 v_1^2 w_2^2 w_6^2 w_3 c s^2 - 4 w_5 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 4 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 c s^2 - \\ 4 w_5^2 w_2^2 w_6^2 w_3^3 c s^2 + 4 w_5 w_2^2 w_6^2 w_3^2 c s^4 + 2 w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2 - 3 w_5^2 v_1^2 w_2^2 w_6 w_3^2 c s^2 + 2 w_5^2 v_2^2 w_6^2 w_3^2 c s^2 + 10 w_5 w_2^2 v_2^2 w_6^2 w_3^2 c s^2 - 2 w_5^2 w_2^2 w_6 w_3^2 c s^4 + \\ 4 w_5^2 w_3^2 v_2^2 w_6^2 w_3^2 c s^2 + 4 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 c s^2 - 4 w_5^2 v_1^2 w_3^2 v_2^2 w_6 w_3 + 12 w_5^2 w_2^2 v_2^2 w_6^2 w_3^2 c s^2 + 2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 - 2 w_5^2 w_3^2 w_6 w_3^2 c s^4 - 4 w_5 w_2^2 v_2^2 w_6^2 w_3^2 c s^2 - \\ 4 w_5^2 v_1^2 w_2^2 w_6 w_3^2 c s^2 - 2 w_5^2 w_3^2 v_2^2 w_6 w_3^2 c s^2 + 20 w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 - 4 w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2) \frac{1}{4 w_5^2 w_3^2 w_6^2 w_3^3} \end{aligned}$$

$$\begin{aligned}
C_{D_x^2 D_y^2}^{(0), \text{MRT2}} = & -38 w_5^2 v_1^2 w_2^3 v_2^2 w_6^2 w_3 + c s^4 w_5 w_3^2 w_6^2 w_3^3 - 12 c s^4 w_5^2 w_2^2 w_6^2 w_3^3 + 10 c s^2 w_5^2 v_1^2 w_2^3 w_6 w_3^2 + 10 c s^2 w_5^2 w_2 v_2^2 w_6^2 w_3^3 + 2 w_5 v_1^2 s_2^2 v_2^2 w_6^2 w_3^2 - \\
& 36 w_5^2 v_2^2 w_2^2 v_2^2 w_6^2 w_3^2 + c s^2 w_5^2 s_2^2 v_2^2 w_6 w_3^3 - 4 c s^2 w_5^2 w_2 v_2^2 w_6^2 w_3^3 - 3 c s^2 w_5^2 v_2^2 w_3^2 w_6 w_3^3 - 2 c s^4 w_5 w_3^2 w_2^2 w_6^2 w_3^2 - 4 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3 + 4 c s^4 w_5^2 w_2^2 w_6^2 w_3^3 + \\
& 2 c s^2 w_5^2 v_2^2 w_6^2 w_3^3 - 2 c s^2 w_5^2 v_2^2 w_2^2 w_6 w_3^2 + 20 w_5^2 v_1^2 w_2^3 v_2^2 w_6^2 w_3^3 + 20 w_5^2 v_1^2 v_2^2 w_6^2 w_3^3 - 4 c s^2 w_5 w_2 v_2^2 w_6^2 w_3^3 - 3 w_5 v_1^2 w_2^3 v_2^2 w_6^2 w_3^3 - 2 c s^2 w_5^2 v_2^2 w_6^2 w_3^3 - 10 w_5 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 2 c s^4 w_5^2 w_2^3 w_6 w_3^2 - 3 w_5^2 v_1^2 w_2^3 v_2^2 w_6^2 w_3^3 + 12 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 + 4 c s^2 w_5^2 w_2^2 v_2^2 w_6 w_3^2 - 4 c s^2 w_5^2 w_2^2 w_6^2 w_3^3 + 4 c s^2 w_5 v_1^2 w_2^2 w_6^2 w_3^2 - \\
& 4 c s^2 w_5^2 v_2^2 w_6^2 w_3^3 + 20 w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2 - 2 c s^2 w_5^2 v_2^2 w_5^2 w_6 w_3^3 + 4 c s^4 w_5^2 w_2^2 w_5^2 w_6 w_3^3 - 4 c s^2 w_5^2 v_1^2 w_2^2 w_5^2 w_6 w_3^3 + 20 w_5^2 v_2^2 w_2^2 v_2^2 w_6^2 w_3^3 + c s^4 w_5^2 w_2^2 w_6^2 w_3^3 - 4 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 2 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 + 20 w_5^2 v_2^2 w_2^2 v_2^2 w_6^2 w_3^3 - 4 c s^2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^2 - 4 v_2^2 w_5^2 v_2^2 w_6^2 w_3^3 + 2 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3^3 + \\
& 10 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 8 c s^2 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 - 8 c s^2 w_5^2 v_2^2 w_2^2 v_2^2 w_6^2 w_3^3 - c s^4 w_5^2 w_2^2 v_2^2 w_6^2 w_3^2 + 4 c s^4 w_5^2 w_2^2 w_6^2 w_3^3 + 10 c s^2 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + 4 c s^2 w_5^2 w_2^2 w_6^2 w_3^3 - 10 c s^2 w_5 w_2 v_2^2 w_6^2 w_3^3 - 4 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 38 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 + 4 c s^2 w_5^2 v_2^2 w_2^2 w_6^2 w_3^2 - 2 c s^4 w_5 w_2 v_2^2 w_6^2 w_3^3 + 12 c s^2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^3 - 4 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 + 4 c s^2 w_5^2 v_2^2 w_2^2 w_6^2 w_3^3 - 3 w_5^2 v_1^2 s_2^2 v_2^2 w_6 w_3^2 - 4 c s^2 w_5^2 v_1^2 w_2^2 w_6 w_3^2 + c s^2 w_5^2 v_1^2 s_2^2 v_2^2 w_6 w_3^3 - 2 c s^4 w_5^2 w_2^2 w_6^2 w_3^2 - 3 c s^2 w_5 w_2 v_2^2 w_6^2 w_3^3 - 8 c s^2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^3 + \\
& 4 c s^4 w_5^2 w_2 v_2^2 w_6^2 w_3^2 - 4 w_5 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 - 2 c s^4 w_5^2 w_2^2 w_6 w_3^3 + 2 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3^3 + 2 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 - 4 c s^2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^2 - 2 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3^3 - 4 c s^2 w_5^2 v_2^2 w_2^2 w_6^2 w_3^2 + 4 c s^4 w_5^2 w_2^2 w_6^2 w_3^3 - 4 w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2 + 2 c s^2 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 + 2 c s^2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^2 - 2 c s^4 w_5^2 w_2^2 w_6^2 w_3^3 - 8 c s^2 w_5^2 v_1^2 w_2^2 w_6^2 w_3^2 + \\
& c s^2 w_5 v_1^2 w_2^2 w_6^2 w_3^3 + 20 w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 + c s^2 w_5^2 w_2^2 v_2^2 w_6^2 w_3^3 - 4 w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2
\end{aligned}$$

$$\begin{aligned}
C_{\substack{\text{D}_2^2 \text{D}_2^2 y}}^{(0), \text{CLBM1}} = & (-14w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3 - 4w_5^2 v_2^2 c s^2 w_6^2 w_3^3 - 2w_5^2 w_2^2 c s^4 w_6 w_3^3 + w_5^2 w_3^2 v_2^2 c s^2 w_6^2 w_3^3 - 2w_5 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 - 2w_5^2 v_1^2 w_2^2 c s^2 w_6^2 w_3^3 - \\
& 28w_8^2 v_1^2 w_2^2 v_3^2 w_6^2 w_3^2 - w_5 v_1^2 w_3^2 c s^2 w_6^2 w_3^3 - 4w_5^2 w_3^2 v_2^2 c s^2 w_6 w_3^2 + 4w_5^2 w_2^2 c s^4 w_6 w_3^2 - 2w_5^2 w_3^2 v_2^2 c s^2 w_6^2 w_3^2 + 10w_5^2 v_1^2 w_3^2 c s^2 w_6^2 w_3^3 + 2w_5 v_1^2 w_3^2 c s^2 w_6^2 w_3^2 + \\
& 2w_5^2 w_2^2 c s^2 w_6 w_3^3 + 14w_5^2 v_1^2 w_2^2 v_3^2 w_6^2 w_3^3 + 4w_5^2 v_1^2 w_2^2 w_6^2 w_3^3 + 8w_5^2 v_1^2 w_2^2 c s^2 w_6^2 w_3^2 + 3w_5 v_1^2 w_2^2 v_3^2 w_6^2 w_3^3 + 2w_5 w_3^2 v_2^2 c s^2 w_6^2 w_3^2 - 4w_5^2 v_1^2 w_2^2 c s^2 w_6^2 w_3^3 - \\
& 2w_5^2 w_3^2 c s^4 w_6 w_3^2 - 10w_5 v_1^2 w_2^2 v_3^2 w_6^2 w_3^3 - 8w_5^2 v_1^2 w_3^2 c s^2 w_6^2 w_3^2 - 3w_5^2 v_2^2 w_3^2 v_2^2 w_6^2 w_3^3 - 4w_5 v_1^2 w_2^2 c s^2 w_6^2 w_3^2 + 4w_5^2 w_2^2 c s^4 w_6 w_3^2 + w_5^2 w_3^2 c s^4 w_6 w_3^2 + \\
& 12w_8^2 v_1^2 w_2^2 v_3^2 w_6^2 w_3^2 - 3w_5 w_3^2 v_2^2 c s^2 w_6^2 w_3^3 - 4w_2^2 v_2^2 c s^2 w_6^2 w_3^2 + 2w_5 v_2^2 w_2^2 c s^2 w_6^2 w_3^2 - 2w_5^2 w_2^2 c s^4 w_6^2 w_3^3 + 14w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 + w_5^2 v_2^2 w_3^2 c s^2 w_6^2 w_3^2 + \\
& 4w_5 v_1^2 w_2^2 v_3^2 w_6^2 w_3^2 - 2w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^3 - 4w_5 w_2^2 v_2^2 c s^2 w_6^2 w_3^2 + 12w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - w_5^2 w_2^2 c s^4 w_6^2 w_3^2 + 4v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 + 2w_5^2 v_1^2 w_3^2 c s^2 w_6^2 w_3^2 - \\
& 10w_8^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 - 2w_5 w_3^2 c s^4 w_6^2 w_3^2 - 4w_5 w_2^2 v_2^2 c s^2 w_6^2 w_3^2 - 3w_5^2 v_1^2 w_3^2 c s^2 w_6^2 w_3^2 + 4w_5^2 w_3^2 c s^4 w_6^2 w_3^2 + 4w_5^2 v_2^2 w_3^2 v_2^2 w_6^2 w_3^2 - 14w_5^2 v_1^2 w_2^2 v_2^2 w_6^2 w_3^3 + \\
& 10w_5 w_2^2 v_2^2 c s^2 w_6^2 w_3^3 + 10w_5^2 v_1^2 w_3^2 c s^2 w_6^2 w_3^2 + 4w_5^2 w_3^2 c s^4 w_6^2 w_3^2 + w_5 w_3^2 c s^4 w_6^2 w_3^2 + 2w_3^2 v_2^2 c s^2 w_6^2 w_3^3 + 3w_5^2 v_1^2 w_3^2 v_2^2 w_6^2 w_3^2 - 4w_5^2 v_1^2 w_3^2 c s^2 w_6^2 w_3^2 - \\
& 4w_5^2 v_1^2 w_3^2 c s^2 w_6 w_3 + 2w_5^2 w_3^2 v_2^2 c s^2 w_6 w_3^2 - 12w_5^2 w_2^2 c s^4 w_6 w_3^2 - 4w_5^2 w_2^2 v_2^2 c s^2 w_6^2 w_3^2 + 4w_5 v_1^2 w_2^2 v_2^2 w_6^2 w_3^2 - 2w_5^2 v_1^2 w_2^2 v_2^2 w_6 w_3^2 - 8w_5^2 w_2^2 v_2^2 c s^2 w_6^2 w_3^2 -
\end{aligned}$$

$$2\omega_5\omega_5^2cs^4\omega_6^2\omega_3^3 - 2\omega_5^2\omega_3^2cs^4\omega_6^2\omega_3 - 4\omega_5^2v_1^2\omega_5^2\omega_2^2cs^2\omega_6\omega_3 + 4\omega_5^2v_1^2\omega_5^2v_2^2\omega_6\omega_3 - 2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^3 + 10\omega_5^2\omega_2v_2^2cs^2\omega_6^2\omega_3^3 - 4\omega_5^2v_1^2\omega_5^2cs^2\omega_6^2 - \omega_5^2\omega_2^3v_2^2cs^2\omega_6\omega_3^3 + 4\omega_5^2v_1^2\omega_2^2cs^2\omega_6\omega_3^3 + 4\omega_5\omega_2^2cs^4\omega_6^2\omega_3^3 + 4\omega_5^2v_1^2\omega_2^2v_2^2\omega_6\omega_3^3 + 8\omega_5^2\omega_2^2v_2^2cs^2\omega_6^2\omega_3^3 + 4\omega_5^2v_1^2\omega_2^2v_2^2\omega_6\omega_3^3) \frac{1}{4\omega_5^2\omega_3^2\omega_6^2\omega_3^3}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM2}} = & (4\omega_5^2\omega_3^2\omega_6^2\omega_3^2cs^4 - 14\omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3 - 2\omega_5\omega_2^2\omega_6^2\omega_3^2cs^4 + 8\omega_5^2v_1^2\omega_2^2\omega_6^2\omega_3^2cs^2 + 2\omega_5^2v_1^2\omega_3^2\omega_6^2\omega_3^2cs^2 - 4\omega_5^2\omega_2^2v_2^2\omega_6\omega_3^2cs^2 + \\ & 2\omega_5^2v_1^2\omega_3^2\omega_6^2\omega_3^2cs^2 - 2\omega_5v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2 - 28\omega_5^2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 - 2\omega_5^2\omega_3^2v_2^2\omega_6^2\omega_3^2cs^2 - 3\omega_5\omega_2^3v_2^2\omega_6^2\omega_3^2cs^2 - 4\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + \\ & \omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2cs^2 - 4\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + 2\omega_5^2\omega_2^2v_2^2\omega_6\omega_3^2cs^2 - 10\omega_5v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 - \omega_5v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2cs^2 - 3\omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2 - \\ & 4\omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2cs^2 - 2\omega_5^2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 + 4\omega_5\omega_2^2\omega_6^2\omega_3^2cs^4 + 2\omega_5v_1^2\omega_2^2\omega_6^2\omega_3^2cs^2 + 4\omega_5^2v_1^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_5v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2 - 4\omega_5^2v_1^2\omega_3^2\omega_6^2\omega_3^2cs^2 + \\ & 4\omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2cs^2 - 12\omega_5^2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 + 5\omega_5^2\omega_2^2\omega_6^2\omega_3^2cs^4 + 12\omega_5^2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 - 8\omega_5^2v_1^2\omega_3^2\omega_6^2\omega_3^2cs^2 - \\ & 12\omega_5^2\omega_2^2\omega_6^2\omega_3^2cs^4 + 14\omega_5^2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 + 2\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^2cs^2 + 4\omega_5v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 - 2\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 + 12\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 - \\ & \omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2cs^2 - 10\omega_5^2v_1^2\omega_2^2\omega_6^2\omega_3^2cs^2 + 4v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 - 2\omega_5^2v_1^2\omega_2^2\omega_6^2\omega_3^2cs^2 - 10\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 + \\ & 4\omega_5^2\omega_2^2\omega_6^2\omega_3^2cs^4 - 4\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + 10\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + 4\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + 10\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 - 14\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 - 2\omega_5^2\omega_2\omega_6^2\omega_3^2cs^4 + \\ & 3\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + 8\omega_5^2\omega_2^2v_2^2\omega_6^2\omega_3^2cs^2 - 4\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 + 4\omega_5v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 - 4\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^2cs^2 - 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2cs^4 - \\ & 2\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 - 4\omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2 + 4\omega_5^2v_1^2\omega_3^2v_2^2\omega_6^2\omega_3^2 - 2v_1^2\omega_5^2v_2^2\omega_6^2\omega_3^2 - 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2cs^4 - 4\omega_5^2v_2^2\omega_6^2\omega_3^2cs^2 - 4\omega_5^2\omega_2\omega_6^2\omega_3^2cs^2 + \\ & 4\omega_5^2\omega_2\omega_6^2\omega_3^2cs^4 + 4\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 + 10\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^2cs^2 - 2\omega_5^2\omega_2\omega_6^2\omega_3^2cs^4 + 4\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^2 + 3\omega_5^2v_1^2\omega_2^2\omega_6^2\omega_3^2cs^2 + 2\omega_5^2\omega_2^2\omega_6^2\omega_3^2cs^2) \frac{1}{4\omega_5^2\omega_3^2\omega_6^2\omega_3^3} \end{aligned}$$

coefficient  $C_{D_x^2 D_y^2 v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2}$ :

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{SRT}} = (-26\omega^2 cs^2 + 50\omega^2 v_2^2 - 4\omega^3 v_2^2 + \omega^3 cs^2 - 48cs^2 + 84v_2^2 + 72\omega cs^2 - 126\omega v_2^2) \frac{v_1 \rho}{12\omega^3}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}} = & (-12\omega_3^2\omega_6\omega_3cs^2 + 24\omega_2^2\omega_2^2\omega_6^2\omega_3 + 34\omega_3^2v_2^2\omega_6^2\omega_3^2 - 6\omega_2^2\omega_6^2\omega_3^2cs^2 - 12\omega_3^2v_2^2\omega_6^2\omega_3^2 - 14\omega_3^2\omega_6^2\omega_3^2cs^2 + 6\omega_3^2v_2^2\omega_6^2\omega_3^2 + 12\omega_2^2\omega_6^2\omega_3^2cs^2 + \\ & 48\omega_3^2v_2^2\omega_6^2\omega_3^2 + 22\omega_2^2v_2^2\omega_6^2\omega_3^2 - 78\omega_2^3v_2^2\omega_6^2\omega_3^2 + 48\omega_2^2v_2^2\omega_6^2\omega_3^2 - 12\omega_2^3\omega_6^2\omega_3^2cs^2 - 12\omega_2^2v_2^2\omega_6\omega_3^2 + 6\omega_2\omega_6^2\omega_3^2cs^2 + 12v_2^2\omega_6^2\omega_3^2 + 6\omega_3^2\omega_6^2\omega_3^2cs^2 - \\ & 6\omega_2^2\omega_6^2\omega_3^2cs^2 - 30\omega_2^2v_2^2\omega_6^2\omega_3^2 - 12\omega_2^3v_2^2\omega_6^2\omega_3^2 + 24\omega_2^2\omega_6^2\omega_3^2cs^2 - 6\omega_2^3v_2^2\omega_6^2\omega_3^2 - 12\omega_2\omega_6^2\omega_3^2cs^2 + 24\omega_2v_2^2\omega_6^2\omega_3^2 + 24\omega_3^2\omega_6^2\omega_3^2cs^2 + 24\omega_2^3\omega_6^2\omega_3^2) \frac{v_1 \rho}{12\omega_2^3\omega_6^2\omega_3^3} \end{aligned}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT2}} = & (24\omega_2^2v_2^2\omega_6^2\omega_3 + 34\omega_3^2v_2^2\omega_6^2\omega_3^2 + 6cs^2\omega_2\omega_6^2\omega_3^2 + 6cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 - 12\omega_3^2v_2^2\omega_6^2\omega_3^2 + 24cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 + 6\omega_3^2v_2^2\omega_6^2\omega_3^2 - 12cs^2\omega_2\omega_6^2\omega_3^2 - 12cs^2\omega_2\omega_6^2\omega_3^2 - \\ & 4\omega_3^2v_2^2\omega_6^2\omega_3^2 - 14cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 + 48\omega_3^2v_2^2\omega_6^2\omega_3^2 + 22\omega_2^2v_2^2\omega_6^2\omega_3^2 - 78\omega_2^3v_2^2\omega_6^2\omega_3^2 - 12cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 + cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 - 48\omega_2^2v_2^2\omega_6^2\omega_3^2 - 12\omega_3^2v_2^2\omega_6\omega_3^2 - 6cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 + \\ & 12v_2^2\omega_6^2\omega_3^2 + 24cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 - 30\omega_2v_2^2\omega_6^2\omega_3^2 - 12cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 - 6\omega_2^3v_2^2\omega_6^2\omega_3^2 + 24\omega_2v_2^2\omega_6^2\omega_3^2 + 12cs^2\omega_2^3v_2^2\omega_6^2\omega_3^2 + 24\omega_3^2v_2^2\omega_6^2\omega_3^2) \frac{v_1 \rho}{12\omega_2^3\omega_6^2\omega_3^3} \end{aligned}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM1}} = & (-12\omega_3^2cs^2\omega_3^2 + 24\omega_2^2v_2^2\omega_6^2\omega_3 + 22\omega_3^2v_2^2\omega_6^2\omega_3^2 + \omega_3^2cs^2\omega_6^2\omega_3^2 + 12\omega_3^2v_2^2\omega_6^2\omega_3^2 + 6\omega_3^2cs^2\omega_6^2\omega_3^2 - 6\omega_3^2v_2^2\omega_6^2\omega_3^2 - 14\omega_3^2cs^2\omega_6^2\omega_3^2 - 4\omega_3^2v_2^2\omega_6^2\omega_3^2 + \\ & 24\omega_2^2cs^2\omega_6^2\omega_3 + 22\omega_2^2v_2^2\omega_6^2\omega_3^2 - 12\omega_2^2cs^2\omega_6^2\omega_3^2 + 12\omega_2^2cs^2\omega_6^2\omega_3^2 - 18\omega_2^2v_2^2\omega_6^2\omega_3^2 - 6\omega_2^2cs^2\omega_6^2\omega_3^2 - 48\omega_2^2v_2^2\omega_6^2\omega_3^2 + 12\omega_2^2v_2^2\omega_6^2\omega_3^2 + 12\omega_2^2v_2^2\omega_6^2\omega_3^2 - \\ & 12\omega_2^3cs^2\omega_6\omega_3 - 12\omega_2cs^2\omega_6^2\omega_3^2 + 30\omega_2v_2^2\omega_6^2\omega_3^2 + 24\omega_2^3cs^2\omega_6\omega_3^2 + 6\omega_2^3v_2^2\omega_6^2\omega_3^2 + 24\omega_2v_2^2\omega_6^2\omega_3^2 + 6\omega_2cs^2\omega_6^2\omega_3^2 - 24\omega_2^3v_2^2\omega_6\omega_3^2 - 6\omega_2^3cs^2\omega_6\omega_3^2) \frac{v_1 \rho}{12\omega_2^3\omega_6^2\omega_3^3} \end{aligned}$$

coefficient  $C_{D_x^2 D_y^2 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2}$ :

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{SRT}} = (-26\omega^2 cs^2 + 50\omega^2 v_1^2 + 84v_1^2 + \omega^3 cs^2 - 4\omega^3 v_1^2 - 48cs^2 - 126\omega v_1^2 + 72\omega cs^2) \frac{v_2 \rho}{12\omega^3}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}} = & (24\omega_5v_1^2\omega_2^2\omega_3^3 + 24\omega_5^2\omega_2^2\omega_3^2cs^2 - 6\omega_5^2\omega_3^2\omega_2^2\omega_3^2cs^2 - 12\omega_5^2\omega_2^2\omega_3^2cs^2 + 6v_1^2\omega_5^2\omega_2^2\omega_3^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 - 6\omega_5v_1^2\omega_3^2\omega_2^2\omega_3^2 + 48\omega_5^2v_1^2\omega_3^2\omega_2^2\omega_3^2 - \\ & 12v_1^2\omega_5^2\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3^2cs^2 - 78\omega_5^2v_1^2\omega_2\omega_3^2 + \omega_5^2\omega_2^2\omega_3^2cs^2 + 6\omega_5^2\omega_3^2\omega_2^2\omega_3^2cs^2 + 12\omega_5^2\omega_2^2\omega_3^2cs^2 + 34\omega_5^2v_1^2\omega_2\omega_3^2 - 30\omega_5^2v_1^2\omega_3^2\omega_2^2\omega_3^2 - 48\omega_5^2v_1^2\omega_2\omega_3^2 + \\ & 12\omega_5^2v_1^2\omega_3^2 - 12\omega_5^2\omega_3^2cs^2 - 4\omega_5^2v_1^2\omega_2\omega_3^2 + 6\omega_5^2\omega_2^2\omega_3^2cs^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 - 14\omega_5^2\omega_2^2\omega_3^2cs^2 - 12\omega_5^2v_1^2\omega_2\omega_3^2 - 6\omega_5\omega_2^2\omega_3^2cs^2 + 22\omega_5^2v_1^2\omega_2\omega_3^2) \frac{v_1 \rho}{12\omega_5^2\omega_3^2\omega_2^2\omega_3^3} \end{aligned}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT2}} = & (24\omega_5v_1^2\omega_2^2\omega_3^3 - 12cs^2\omega_5\omega_2\omega_3^3 - 12cs^2\omega_5\omega_2\omega_3^3 + 6cs^2\omega_5^2\omega_2\omega_3^3 + 12cs^2\omega_5^2\omega_2\omega_3^3 + 6v_1^2\omega_5^2\omega_2\omega_3^3 - 14cs^2\omega_5^2\omega_2\omega_3^3 + 6cs^2\omega_5^2\omega_2\omega_3^3 - 12cs^2\omega_5^2\omega_2\omega_3^3 - \\ & 6cs^2\omega_5^2\omega_3^2\omega_2^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 - 6\omega_5^2v_1^2\omega_2\omega_3^2 + 48\omega_5^2v_1^2\omega_2\omega_3^2 + cs^2\omega_5^2\omega_2\omega_3^2 - 12cs^2\omega_5^2\omega_2\omega_3^2 - 12v_1^2\omega_5^2\omega_2\omega_3^2 - 78\omega_5^2v_1^2\omega_2\omega_3^2 + 34\omega_5^2v_1^2\omega_2\omega_3^2 - 30\omega_5^2v_1^2\omega_2\omega_3^2 - \\ & 6cs^2\omega_5\omega_2\omega_3^2 - 48\omega_5^2v_1^2\omega_2\omega_3^2 + 12\omega_5^2v_1^2\omega_2\omega_3^2 - 4\omega_5^2v_1^2\omega_2\omega_3^2 + 24\omega_5^2v_1^2\omega_2\omega_3^2 + 24cs^2\omega_5^2\omega_2\omega_3^2 - 12\omega_5^2v_1^2\omega_2\omega_3^2 + 22\omega_5^2v_1^2\omega_2\omega_3^2 + 24cs^2\omega_5\omega_2\omega_3^2) \frac{v_2 \rho}{12\omega_5^2\omega_3^2\omega_2^2\omega_3^3} \end{aligned}$$

$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM1}}$  =

$$\begin{aligned} & (-24\omega_5^2\omega_2^2\omega_3^2\omega_3^3 - 12\omega_5^2cs^2\omega_3^2\omega_3^3 + 6\omega_5^3cs^2\omega_3^2\omega_3^3 - 12\omega_5^2\omega_2^2cs^2\omega_3^2\omega_3^3 - 12\omega_5\omega_2cs^2\omega_3^2\omega_3^3 - 6v_1^2\omega_5^2\omega_2\omega_3^2\omega_3^3 + 24\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 - 6\omega_5\omega_2^2\omega_3^2\omega_3^3cs^2 + \\ & 6\omega_5v_1^2\omega_3^2\omega_2^2\omega_3^3 + 12v_1^2\omega_5^2\omega_2\omega_3^2\omega_3^3 - 14\omega_5^2\omega_2^2\omega_3^2\omega_3^3 - 18\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 6\omega_5^2\omega_2^2\omega_3^2\omega_3^3 - 12\omega_5^2\omega_2^2\omega_3^2\omega_3^3 - 12v_1^2\omega_5^2\omega_2\omega_3^2\omega_3^3 - 78\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 34\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 - 30\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 - \\ & 48\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 12\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 24\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 6\omega_5^2\omega_2^2\omega_3^2\omega_3^3 + 24\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 6\omega_5^2\omega_2^2\omega_3^2\omega_3^3 + 24\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3 + 22\omega_5^2v_1^2\omega_2\omega_3^2\omega_3^3) \frac{v_2 \rho}{12\omega_5^2\omega_3^2\omega_2^2\omega_3^3} \end{aligned}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM2}} = (-6\omega_5^2 \omega_2^3 \omega_3^2 c s^2 - 12\omega_2^2 \omega_3^3 c s^2 - 24\omega_5 v_1^2 \omega_2^2 \omega_3^3 + 24\omega_5^2 \omega_2 \omega_3^3 c s^2 - 6v_1^2 \omega_3^2 \omega_3^3 - 12\omega_5^2 \omega_2^2 \omega_3 c s^2 + 24\omega_5^2 v_1^2 \omega_2 \omega_3^2 + 6\omega_5 v_1^2 \omega_2^3 \omega_3^3 + \omega_5^2 \omega_3^3 c s^2 + 12v_1^2 \omega_2^2 \omega_3^3 + 24\omega_5 \omega_2^2 \omega_3^3 c s^2 - 18\omega_5^2 v_1^2 \omega_2 \omega_3^3 - 12\omega_5^2 \omega_3^2 c s^2 + 22\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 - 30\omega_5^2 v_1^2 \omega_3^2 \omega_3^3 + 6\omega_5^2 \omega_3^3 c s^2 + 12\omega_5^2 \omega_2^2 \omega_3^2 c s^2 - 48\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 12\omega_5 \omega_2 \omega_3^3 c s^2 + 12\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 - 4\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 6\omega_5 \omega_2^2 \omega_3^3 c s^2 + 24\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 + 12\omega_5 v_1^2 \omega_2 \omega_3^3 + 6\omega_5^2 \omega_2^3 \omega_3 c s^2 - 14\omega_5^2 \omega_2^2 \omega_3^2 \omega_3^3 + 22\omega_5^2 v_1^2 \omega_2^3 \omega_3^2) \frac{v_2 \rho}{12\omega_5^2 \omega_3^2}$$

coefficient  $C_{D_t D_y^3 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t \partial x_2^3}$ :

$$C_{D_t D_y^3 v_2}^{(0), \text{SRT}} = (-36 + 34\omega^2 c s^2 + 42\omega^2 v_2^2 - 3\omega^3 v_2^2 - 2\omega^3 c s^2 + 60c s^2 + 54\omega + 72v_2^2 + \omega^3 - 20\omega^2 - 90\omega c s^2 - 108\omega v_2^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{MRT1}} = (9\omega_6^3 \omega_3^2 c s^2 + 12v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 + 24\omega_6^2 c s^2 + \omega_6^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3 - 60v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3^2 - 36\omega_6 \omega_3^2 c s^2 - 6v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 15v_2^2 \omega_6 \omega_3^3 - 48\omega_6^2 \omega_3 c s^2 - 12\omega_3^2 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 12\omega_3^2 c s^2 + 25\omega_6^2 \omega_3^2 c s^2 + 27v_2^2 \omega_6^2 \omega_3^3 + 6\omega_3^3 + 24\omega_6 \omega_3 c s^2 - 2\omega_6^2 \omega_3^2 c s^2 - 6\omega_3^3 c s^2 - 9\omega_6 \omega_3^3 - 42v_2^2 \omega_6^2 \omega_3 + 36\omega_6 \omega_3^3) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{MRT2}} = (12c s^2 \omega_3^2 + 25c s^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 - 2c s^2 \omega_6^2 \omega_3^3 + \omega_6^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3 - 6c s^2 \omega_3^2 - 60v_2^2 \omega_6 \omega_3^2 + 24c s^2 \omega_6^2 + 12v_2^2 \omega_3^2 - 6v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 15v_2^2 \omega_6 \omega_3^3 - 48c s^2 \omega_6 \omega_3 - 12\omega_3^2 + 24c s^2 \omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 27v_2^2 \omega_6^2 \omega_3^2 + 6\omega_3^3 - 9\omega_6 \omega_3^3 - 42v_2^2 \omega_6^2 \omega_3 + 9c s^2 \omega_6 \omega_3^3 + 36\omega_6 \omega_3^2 - 36c s^2 \omega_6 \omega_3^3) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_t D_y^3 v_2}^{(0), \text{CLBM1}} = (24c s^2 \omega_6^2 + 24c s^2 \omega_6 \omega_3 - 36v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 + \omega_6^2 \omega_3^3 + 72v_2^2 \omega_6 \omega_3 - 108v_2^2 \omega_6 \omega_3^2 + 36v_2^2 \omega_3^2 + 9c s^2 \omega_6 \omega_3^3 + 12c s^2 \omega_6^2 - 36c s^2 \omega_6 \omega_3^2 - 18v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 27v_2^2 \omega_6 \omega_3^3 - 36\omega_6 \omega_3^2 c s^2 - 6c s^2 \omega_3^2 - 12\omega_3^2 + 25c s^2 \omega_6^2 \omega_3^2 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 15v_2^2 \omega_6^2 \omega_3^2 + 6\omega_3^3 + 12\omega_3^2 c s^2 + 25\omega_6^2 \omega_3^2 c s^2 - 9\omega_6 \omega_3^3 + 18v_2^2 \omega_6^2 \omega_3 - 48c s^2 \omega_6 \omega_3 + 36\omega_6 \omega_3^3) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM2}} = (24\omega_6^3 c s^2 - 36v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 + 9\omega_6 \omega_3^3 c s^2 + \omega_6^2 \omega_3^3 + 72v_2^2 \omega_6 \omega_3 - 108v_2^2 \omega_6 \omega_3^2 + 36v_2^2 \omega_3^2 - 48\omega_6^2 \omega_3 c s^2 - 18v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 27v_2^2 \omega_6 \omega_3^3 - 36\omega_6 \omega_3^2 c s^2 - 12\omega_3^2 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 24\omega_6 \omega_3 c s^2 + 15v_2^2 \omega_6^2 \omega_3^2 + 6\omega_3^3 + 12\omega_3^2 c s^2 + 25\omega_6^2 \omega_3^2 c s^2 - 9\omega_6 \omega_3^3 + 18v_2^2 \omega_6^2 \omega_3 - 2\omega_6^2 \omega_3^2 c s^2 - 6\omega_3^3 c s^2 + 36\omega_6 \omega_3^3) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

coefficient  $C_{D_x D_y^3 \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$ :

$$C_{D_x D_y^3 \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 c s^2 + 6\omega^3 c s^2 - 120c s^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega c s^2) \frac{v_1 v_2}{6\omega^3}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT1}} = (-24\omega_3^2 \omega_6 \omega_3 c s^2 + 12w_2^2 v_2^2 \omega_6^2 \omega_3 + 6w_3^2 v_2^2 \omega_6^2 \omega_3^2 + 6w_2^2 \omega_6 \omega_3^2 - 3w_3^2 \omega_3^3 - 12w_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_3^2 v_2^2 \omega_2^2 - 48\omega_3^2 \omega_6^2 \omega_3^2 c s^2 + 6w_3^2 v_2^2 \omega_6^2 \omega_3^3 + 6w_3^2 v_2^2 \omega_6^2 \omega_3^3 c s^2 - 6w_3^2 \omega_6^2 \omega_3^3 - 3w_2^2 \omega_6^2 \omega_3^3 + 42w_2^2 \omega_6^2 \omega_3^2 c s^2 + 7w_3^2 v_2^2 \omega_6^2 \omega_3^2 + 6w_2^2 \omega_6^2 \omega_3^3 + 6w_3^2 v_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 - 12w_3^2 \omega_6^2 \omega_3^3 c s^2 + 78w_2^2 \omega_6^2 \omega_3^2 c s^2 + 12w_2^2 \omega_6 \omega_3 + 6w_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 c s^2 + 42w_2^2 \omega_6^2 \omega_3^2 c s^2 - 3w_2^2 \omega_6^2 \omega_3^3 + 42w_2^2 v_2^2 \omega_6 \omega_3 + 6w_2^2 v_2^2 \omega_6^2 \omega_3^3 + 42w_2^2 v_2^2 \omega_6^2 \omega_3^2 c s^2 - 3w_2^2 \omega_6^2 \omega_3^3 + 42w_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1 v_2}{6w_2^2 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT2}} = (12w_2^2 v_2^2 \omega_6^2 \omega_3 + 6w_3^2 v_2^2 \omega_6^2 \omega_3^2 - 12c s^2 \omega_2^2 \omega_6 \omega_3^2 + 6w_2^2 \omega_6 \omega_3^2 + 6c s^2 \omega_2 \omega_6^2 \omega_3^2 - 3w_3^2 \omega_3^3 + 6c s^2 \omega_3^2 \omega_2^2 \omega_3^2 - 12c s^2 \omega_2^2 \omega_6^2 \omega_3^2 - 6w_3^2 \omega_6^2 \omega_3^2 + 12c s^2 \omega_2^2 \omega_6 \omega_3^2 - 3w_2^2 \omega_6 \omega_3^2 + 6cs^2 \omega_2^2 \omega_6 \omega_3^2 + 6w_2^2 v_2^2 \omega_6^2 \omega_3^2 - 30w_2^2 v_2^2 \omega_6^2 \omega_3^2 - 36w_2^2 v_2^2 \omega_6^2 \omega_3^2 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^2 c s^2 + 6w_2^2 v_2^2 \omega_6^2 \omega_3^3 + 6w_2^2 \omega_6 \omega_3^2 + 6w_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6 \omega_3^2 - 24w_2^2 \omega_6^2 \omega_3^2 c s^2 - 24w_2^2 \omega_6^2 \omega_3^3 + 18w_2^2 \omega_6^2 \omega_3^2 c s^2 + 12w_2^2 \omega_6 \omega_3 + 6w_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 c s^2 + 48c s^2 \omega_2^2 \omega_6^2 \omega_3^2 + 7w_2^2 \omega_6^2 \omega_3^2 c s^2 + 12w_2^2 \omega_6 \omega_3 + 6w_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 - 12w_2^2 v_2^2 \omega_6^2 \omega_3^3 c s^2 + 42w_2^2 \omega_6^2 \omega_3^2 + 42w_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1 v_2}{6w_2^2 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM1}} = (-36w_3^2 c s^2 \omega_3^2 - 6w_2^2 v_2^2 \omega_6^2 \omega_3^2 + 6w_2^2 \omega_6 \omega_3^2 - 3w_3^2 \omega_3^3 + 6w_3^2 c s^2 \omega_6^2 \omega_3^2 + 12w_3^2 v_2^2 \omega_2^2 - 12w_2^2 c s^2 \omega_6^2 \omega_3^2 - 6w_3^2 \omega_6 \omega_3^2 - 3w_2^2 \omega_6^2 \omega_3^2 - 3w_2^2 \omega_6 \omega_3^2 + 36w_2^2 c s^2 \omega_6^2 \omega_3^2 + 7w_3^2 v_2^2 \omega_6^2 \omega_3^2 + 6w_2^2 v_2^2 \omega_6 \omega_3^2 - 12w_2^2 c s^2 \omega_6^2 \omega_3^2 + 36w_2^2 \omega_6^2 \omega_3^2 + 12w_2^2 v_2^2 \omega_6^2 \omega_3^2 c s^2 + 6w_2^2 v_2^2 \omega_6^2 \omega_3^3 + 6w_2^2 \omega_6 \omega_3^2 + 12w_2^2 \omega_6^2 \omega_3^3 c s^2 - 21w_2^2 \omega_6^2 \omega_3^2 - 21w_2^2 v_2^2 \omega_6 \omega_3^2 + 42c s^2 \omega_2^2 \omega_6 \omega_3^2 + 6w_2^2 v_2^2 \omega_6 \omega_3^2 - 12w_2^2 v_2^2 \omega_6 \omega_3^2 + 12w_2^2 v_2^2 \omega_6 \omega_3^2 c s^2 - 12w_2^2 v_2^2 \omega_6 \omega_3^3 + 42w_2^2 \omega_6^2 \omega_3^2 + 42w_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1 v_2}{6w_2^2 \omega_6^2 \omega_3^2}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM2}} = (-36w_2^2 \omega_6^2 \omega_3^2 c s^2 - 6w_2^2 v_2^2 \omega_6^2 \omega_3^2 + 6w_2^2 \omega_6 \omega_3^2 - 3w_3^2 \omega_3^3 + 6w_3^2 c s^2 \omega_6^2 \omega_3^2 + 12w_3^2 v_2^2 \omega_2^2 - 12w_2^2 c s^2 \omega_6^2 \omega_3^2 - 6w_3^2 \omega_6 \omega_3^2 - 3w_2^2 \omega_6^2 \omega_3^2 - 3w_2^2 \omega_6 \omega_3^2 + 36w_2^2 c s^2 \omega_6^2 \omega_3^2 + 7w_3^2 v_2^2 \omega_6^2 \omega_3^2 + 6w_2^2 v_2^2 \omega_6 \omega_3^2 - 12w_2^2 c s^2 \omega_6^2 \omega_3^2 + 36w_2^2 \omega_6^2 \omega_3^2 + 12w_2^2 v_2^2 \omega_6^2 \omega_3^2 c s^2 + 6w_2^2 v_2^2 \omega_6^2 \omega_3^3 + 6w_2^2 \omega_6 \omega_3^2 + 12w_2^2 \omega_6^2 \omega_3^3 c s^2 - 12w_2^2 v_2^2 \omega_6 \omega_3^2 - 24w_2^2 \omega_6^2 \omega_3^2 c s^2 - 24w_2^2 \omega_6^2 \omega_3^3 + 18w_2^2 \omega_6^2 \omega_3^2 c s^2 + 72w_2^2 \omega_6 \omega_3^2 + 12w_2^2 v_2^2 \omega_6 \omega_3^2 c s^2 - 12w_2^2 v_2^2 \omega_6 \omega_3^3 + 42w_2^2 \omega_6^2 \omega_3^2 + 42w_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1 v_2}{6w_2^2 \omega_6^2 \omega_3^2}$$

coefficient  $C_{D_x D_y^3 v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^3}$ :

$$C_{\text{D}_x \text{D}_y^2 v_1}^{(0), \text{SRT}} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_2^2 + \omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 - 54\omega - 36v_2^2 - \omega^3 + 20\omega^2 + 144\omega cs^2 + 54\omega v_2^2) \frac{v_2 \rho}{12\omega^3}$$

$$\begin{aligned} C_{\substack{\text{D}_x \text{D}_y \\ v_1}}^{(0), \text{MRT1}} = & (-12\omega_6 w_3^3 c s^2 + 12v_2^2 w_6^2 + 11w_6^2 w_3^2 - 48w_6^2 c s^2 - w_6^2 w_3^3 - 36v_2^2 w_6 w_3 + 48v_2^2 w_6 w_3^2 - 12v_2^2 w_3^3 + 48w_6 w_3^2 c s^2 + 6v_2^2 w_3^3 - 12w_6^2 w_3 - 12v_2^2 w_6 w_3^3 + 90w_6^2 w_3 c s^2 + 12w_3^2 + 24w_6 w_3 + v_2^2 w_6^2 w_3^3 - 12w_3^2 c s^2 - 44w_6^2 w_3^2 c s^2 - 8v_2^2 w_6^2 w_3^2 - 6w_3^3 - 36w_6 w_3 c s^2 + 4w_6^2 w_3^2 c s^2 + 6w_3^2 c s^2 + 9w_6 w_3^3 - 36w_6 w_3^2) \frac{v_2^2 \rho}{12w_6^2 w_3^3} \end{aligned}$$

$$C_{\substack{D_x D_y v_1}}^{(0), \text{MRT2}} = (-12c^2\omega_3^2 - 44cs^2\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2 + 11\omega_6^2\omega_3^2 + 4cs^2\omega_6^2\omega_3^3 - \omega_6^2\omega_3^3 - 36v_2^2\omega_6\omega_3 + 6cs^2\omega_3^3 + 48v_2^2\omega_6\omega_3^2 - 48cs^2\omega_6^2 - 12v_2^2\omega_3^2 + 6v_2^2\omega_3^3 - 12\omega_6^2\omega_3 - 12v_2^2\omega_6\omega_3^3 + 90cs^2\omega_6^2\omega_3 + 12\omega_3^2 - 36cs^2\omega_6\omega_3 + 24\omega_6\omega_3 + v_2^2\omega_6^2\omega_3^3 - 8v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3 + 9\omega_6\omega_3^3 - 12cs^2\omega_6\omega_3^3 - 36\omega_6\omega_3^2 + 48cs^2\omega_6\omega_3^2) \frac{v_2^2\rho}{12\omega_6^2\omega_3^3}$$

$$\begin{aligned} C_{\substack{\mathrm{D}_x \mathrm{D}_y^3 \\ v_1}}^{(0), \mathrm{CLBM1}} = & (-36 c s^2 w_6 w_3 + 12 v_2^2 w_6^2 + 11 w_6^2 w_3^2 - w_6^2 w_3^3 - 60 v_2^2 w_6 w_3 + 48 v_2^2 w_6 w_3^2 + 12 v_2^2 w_6^2 - 30 c s^2 w_6 w_3^3 - 60 c s^2 w_3^2 + 96 c s^2 w_6 w_3^2 - 6 v_2^2 w_3^3 - 12 w_6^2 w_3 - 6 v_2^2 w_6 w_3^3 + 30 c s^2 w_3^3 + 12 w_3^2 - 26 c s^2 w_6^2 w_3^2 + 24 w_6 w_3 + v_2^2 w_6^2 w_3^3 - 14 v_2^2 w_6^2 w_3^2 + 4 c s^2 w_6^2 w_3^3 - 6 w_3^3 + 9 w_6 w_3^3 + 12 v_2^2 w_6^2 w_3 + 18 c s^2 w_6^2 w_3 - 36 w_6 w_3^2) \frac{v_2^2 \rho}{12 w_6^2 w_3^3} \end{aligned}$$

$$C_{\substack{\text{D}_x \text{D}_y \\ v_1}}^{(0), \text{CLBM2}} = (12v_2^2 w_6^2 + 11w_6^2 w_3^2 - 30w_6 w_3^3 c s^2 - w_6^2 w_3^3 - 60v_2^2 w_6 w_3 + 48v_2^2 w_6 w_3^2 + 12v_2^2 w_3^2 + 18w_6^2 w_3 c s^2 - 6v_2^2 w_3^3 - 12w_6^2 w_3 - 6v_2^2 w_6 w_3^3 + 96w_6 w_3^2 c s^2 + 12w_3^2 + 24w_6 w_3 + v_2^2 w_6^2 w_3^3 - 36w_6 w_3 c s^2 - 14v_2^2 w_6^2 w_3^2 - 6w_3^3 - 60w_3^2 c s^2 - 26w_6^2 w_3^2 c s^2 + 9w_6 w_3^3 + 12v_2^2 w_6^2 w_3 + 4w_6^2 w_3^2 c s^2 + 30w_3^3 c s^2 - 36w_6 w_3^2) \frac{v_2 \rho}{12w_6^2 w_3^3}$$

**coefficient**  $C_{D_x D_y^3 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^3}$ :

$$C_{\substack{D_1 D_2 v_2}}^{(0), \text{SRT}} = (12 - 56\omega^2 cs^2 - 12\omega^2 v_2^2 + 3\omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 - 18\omega - 12v_2^2 - \omega^3 + 8\omega^2 + 144\omega cs^2 + 18\omega v_2^2) \frac{v_1 \rho}{12\omega^3}$$

$$\begin{aligned} C_{\substack{\text{D}_x \text{D}_y^3 \\ v_2}}^{(0), \text{MRT1}} = & -12w_3^2 w_6 w_3 c s^2 + 12w_2^2 w_6 w_3^2 - 12w_2^2 w_6^2 w_3^3 c s^2 - 12w_3^2 v_2^2 w_3^2 - 32w_3^2 w_6^2 w_3^3 c s^2 + 6w_3^2 v_2^2 w_3^3 - 6w_2^2 w_6 w_3^3 + 3w_3^2 v_2^2 w_6^2 w_3^3 + \\ & 48w_2^2 w_6^2 w_3^2 c s^2 + 3w_3^2 w_6^2 w_3^2 + 24w_3^2 v_2^2 w_6^2 - 30w_3^2 v_2^2 w_6^2 w_3 - w_3^2 w_6^2 w_3^3 + 4w_3^2 w_6^2 w_3^3 c s^2 + 12w_3^2 v_2^2 w_6^2 w_3^2 - 12w_3^2 w_6^2 w_3^2 c s^2 - 12w_2^3 v_2^2 w_6 w_3 + 6w_2 w_6^2 w_3^3 c s^2 - 24w_2^2 w_6 w_3^2 c s^2 + 12v_2^2 w_6^2 w_3^3 + 3w_3^2 w_6 w_3^3 + 6w_3^2 w_3^3 c s^2 - 24w_2^2 v_2^2 w_6 w_3^2 - 24w_2^2 w_6^2 w_3 c s^2 - 6w_3^2 w_6^2 w_3^2 + 12w_2^2 v_2^2 w_6 w_3^2 - 12w_3^2 w_6 w_3^3 c s^2 - 18w_2 v_2^2 w_6^2 w_3^3 - 12w_2^3 v_2^2 c s^2 + 36w_2^3 w_6^2 w_3 c s^2 + 12w_2^2 w_6 w_3^3 c s^2 - 12w_2^2 v_2^2 w_6 w_3^2 - 12w_2 w_6^2 w_3^2 c s^2 + 2w_2^2 v_2^2 w_3^3 + 36w_2^3 w_6 w_3^2 c s^2 - 6w_2^2 w_6^2 w_3^3 + 36w_2^3 v_2^2 w_6 w_3^2) \frac{v_1 \rho}{12c_2^3 w_6^2 w_3^3} \end{aligned}$$

$$C_{\substack{\text{D}_x \text{D}_y \\ v_2}}^{(0), \text{MRT2}} = -24c s^2 w_2^2 w_6 w_3^2 + 12 w_2^2 w_6 w_3^3 + 6 c s^2 w_2 w_6^2 w_3^3 + 6 c s^2 w_2^3 w_3^2 w_3^3 - 12 w_3^2 v_2^2 w_3^2 + 36 c s^2 w_3^2 w_6^2 w_3 + 6 w_3^2 v_2^2 w_3^3 - 12 c s^2 w_3^2 w_6^2 - 12 c s^2 w_2 w_6^2 w_3^2 - 6 w_2^2 w_6 w_3^3 + 3 w_2^3 v_2^2 w_6^2 w_3^3 + 12 c s^2 w_2^2 w_6 w_3^3 - 32 c s^2 w_2^3 w_6^2 w_3^3 + 3 w_2^3 w_6^2 w_3^2 + 24 w_3^3 v_2^2 w_6^2 - 30 w_3^2 v_2^2 w_6^2 w_3 - w_3^2 w_6^2 w_3^3 - 12 c s^2 w_3^2 w_6^2 w_3^2 + 4 c s^2 w_3^2 w_6^2 w_3^3 + 12 w_2^2 w_6^2 w_3^2 - 12 w_3^2 v_2^2 w_6 w_3 - 24 c s^2 w_2^2 w_6^2 w_3 - 12 c s^2 w_3^2 w_6 w_3^3 + 12 v_2^2 w_6^2 w_3^3 + 3 w_2^3 w_6^2 w_3^3 - 24 w_2^2 v_2^2 w_6 w_3^2 - 6 w_2^3 w_6 w_3^2 + 36 c s^2 w_3^2 w_6 w_3^2 + 12 w_2^3 v_2^2 w_6 w_3^3 - 18 w_2 v_2^2 w_6^2 w_3^3 - 12 c s^2 w_2 w_6^2 w_3 - 12 c s^2 w_2^2 w_6^2 w_3^3 - 12 w_3^2 v_2^2 w_6 w_3^3 + 2 w_2^2 w_6^2 w_3^3 - 6 w_2^3 w_6^2 w_3^2 + 48 c s^2 w_2^2 w_6^2 w_3^2 + 36 w_2^3 v_2^2 w_6 w_3^2) \frac{v_1 \rho}{12 c s^2 w_2^2 w_3^2}$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(0), \text{CLBM1}} = (-12 w_3^2 c s^2 w_3^2 - 12 w_3^2 v_2^2 w_6^2 w_3^2 + 12 w_2^2 w_6 w_3^2 + 4 w_3^2 c s^2 w_6^2 w_3^3 + 12 w_3^2 v_2^2 w_3^2 + 6 w_3^2 c s^2 w_3^3 - 24 w_2^2 c s^2 w_6^2 w_3 - 6 w_3^2 v_2^2 w_3^3 - 32 w_3^2 c s^2 w_6^2 w_3^2 - 6 w_2^2 w_6 w_3^3 + 3 w_3^2 v_2^2 w_6^2 w_3^3 + 36 w_3^2 c s^2 w_6^2 w_3^2 + 3 w_3^2 w_6^2 w_3^2 - 24 w_3^2 v_2^2 w_6^2 - 12 w_3^2 c s^2 w_6^2 + 48 w_2^2 c s^2 w_6^2 w_3^2 + 30 w_3^2 v_2^2 w_6^2 w_3 - w_3^2 v_6^2 w_3^3 - 12 w_2^2 c s^2 w_6^2 w_3^3 + 12 w_2^2 v_2^2 w_6^2 w_3^2 + 12 w_3^2 v_2^2 w_6 w_3 + 3 w_3^2 w_6 w_3^3 + 12 w_2^2 c s^2 w_6 w_3^2 - 24 w_2^2 v_2^2 w_6 w_3^2 - 6 w_3^2 w_6 w_3^2 - 12 w_3^2 c s^2 w_6 w_3 + 12 w_2^2 v_2^2 w_6 w_3^3 - 24 w_2^2 c s^2 w_6 w_3^2 - 12 w_2^2 c s^2 w_6^2 w_3^2 - 18 w_2^2 v_2^2 w_6^2 w_3^2 + 36 w_2^2 c s^2 w_6 w_3^2 + 2 w_2^2 w_6^2 w_3^3 + 6 w_2^2 c s^2 w_6^2 w_3^3 - 6 w_2^2 w_6^2 w_3^2 - 12 w_3^2 v_2^2 w_6 w_3^2 - 12 w_3^2 c s^2 w_6 w_3^3) \frac{v_1 \rho}{12 w_3^2 w_6^2 w_3^3}$$

**coefficient**  $C_{D_y^4 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_2^4}$ :

$$\begin{aligned} C_{\frac{D^4}{Dy^4}\rho}^{(0), \text{SRV}} = & (-14\omega^2 cs^2 + 42\omega^2 v_2^2 + 108\omega v_2^4 - 72\omega cs^4 - 3\omega^3 v_2^2 + \omega^3 cs^2 - 84\omega^2 cs^2 v_2^2 - 24cs^2 + 72v_2^2 - 144cs^2 v_2^2 - 3\omega^3 cs^4 + 3\omega^3 v_2^4 + \\ & 216\omega cs^2 v_2^2 - 72v_2^4 + 48cs^4 - 42\omega^2 v_2^4 + 30\omega^2 cs^4 + 6\omega^3 cs^2 v_2^2 + 36\omega cs^2 - 108\omega v_2^2) \frac{1}{24\omega^3} \end{aligned}$$

$$C_{\frac{D^4 y}{w_3}}^{(0), \text{MRTI}} = (72 v_2^4 w_6 w_3^2 - 6 w_6 w_3^3 c s^2 + 156 v_2^2 w_6^2 w_3 c s^2 - 3 w_6^2 w_3^3 c^4 + 48 v_2^2 w_6 w_3^2 c s^2 - 24 v_2^2 w_3^2 c s^2 - 18 v_2^4 w_6 w_3^3 + 48 v_2^2 w_6 w_3 - 72 v_2^2 w_6 w_3^2 + 24 v_2^2 w_3^2 + 24 w_6^2 w_3^2 c s^4 + 24 w_6 w_3^2 c s^2 + 24 w_6 w_3 c s^4 - 12 v_2^2 w_3^3 + 18 v_2^2 w_6 w_3^3 + 12 v_2^2 w_3^3 c s^2 - 48 v_4^4 w_6 w_3 + 12 w_6^2 w_3 c s^2 - 12 v_2^2 w_6 w_3^3 c s^2 - 24 w_6 w_3^3 c s^4 - 3 v_2^2 w_6^2 w_3^3 + 24 v_2^4 w_6^2 w_3 - 96 v_2^2 w_6^2 c s^2 - 8 w_6^2 w_3^2 c s^2 + 24 v_2^2 w_6^2 w_3^2 - 48 w_6^2 w_3 c s^4 - 24 w_6 w_3 c s^2 + 6 v_2^2 w_6^2 w_3^2 c s^2 + w_6^2 w_3^3 c s^2 - 24 v_2^2 w_6 w_3 c s^2 + 12 v_2^4 w_3^3 + 3 v_2^4 w_6^2 w_3^3 - 24 v_2^2 w_6^2 w_3 + 6 w_6 w_3^3 c s^4 - 24 v_2^4 w_6^2 w_3^2 - 24 v_2^4 w_3^2 - 72 v_2^2 w_6^2 w_3^2 c s^2 + 24 w_6^2 c s^4) \frac{1}{24 w_6^2 w_3^3}$$

$$48v_2^4\omega_6\omega_3 - 24cs^2\omega_6\omega_3 - 3v_2^2\omega_6^2\omega_3^3 + 6cs^2v_2^2\omega_6^2\omega_3^3 + 24v_2^4\omega_6^2\omega_3 + 6cs^4\omega_6\omega_3^3 - 72cs^2v_2^2\omega_6^2\omega_3^2 + 24v_2^2\omega_6^2\omega_3^2 - 24cs^4\omega_6\omega_3^2 + 24cs^4\omega_6\omega_3 + 3v_2^4\omega_6^2\omega_3^3 + 156cs^2v_2^2\omega_6^2\omega_3 - 24v_2^2\omega_6^2\omega_3 - 6cs^2\omega_6\omega_3^3 + 24cs^4\omega_6^2 - 24v_2^4\omega_6^2\omega_3^2 - 24v_2^4\omega_6^2\omega_3 + 24cs^2\omega_6\omega_3^2) \frac{1}{24\omega_6^2\omega_3^3}$$

$$C_{D_y^4\rho}^{(0),\text{CLBM1}} = (72v_2^4\omega_6\omega_3^2 + 6cs^4\omega_6\omega_3^2 - 24cs^2\omega_6\omega_3 + 144v_2^2cs^2\omega_6\omega_3^2 - 24cs^4\omega_6\omega_3^2 - 30v_2^4\omega_6\omega_3^2 - 72v_2^2cs^2\omega_6\omega_3^2 - 72v_2^2\omega_6\omega_3^2 + 72v_2^2\omega_6^2\omega_3^2 - 6cs^2\omega_6\omega_3^3 + 24cs^4\omega_6\omega_3 + 24cs^2\omega_6\omega_3^2 + 72v_2^2cs^2\omega_6\omega_3 - 36v_2^2\omega_6^2\omega_3^3 + 30v_2^2\omega_6\omega_3^3 - 36v_2^2cs^2\omega_6^2\omega_3^2 - 8cs^2\omega_6^2\omega_3^2 - 3v_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^3 + 24cs^4\omega_6^2 - 48cs^4\omega_6\omega_3 + 24cs^4\omega_6^2\omega_3^2 + 108v_2^2cs^2\omega_6^2\omega_3^3 + 36v_2^2\omega_6^2\omega_3^3 + 3v_2^4\omega_6^2\omega_3^3 + 6v_2^2cs^2\omega_6^2\omega_3^2 - 12v_2^4\omega_6^2\omega_3^2 - 72v_2^4\omega_6^2\omega_3^2 - 216v_2^2cs^2\omega_6^2 - 3cs^4\omega_6\omega_3^2 - 12v_2^2cs^2\omega_6^2\omega_3^2 + 12cs^2\omega_6^2\omega_3^2) \frac{1}{24\omega_6^2\omega_3^3}$$

$$C_{D_y^4\rho}^{(0),\text{CLBM2}} = \\ (144v_2^2\omega_6\omega_3^2cs^2 + 72v_2^4\omega_6\omega_3^2 - 216v_2^2\omega_6^2\omega_3^2cs^2 - 30v_2^4\omega_6\omega_3^3 - 6\omega_6\omega_3^3cs^2 - 36v_2^2\omega_6^2\omega_3cs^2 - 3\omega_6^2\omega_3^3cs^4 - 72v_2^2\omega_6\omega_3^2 + 24\omega_6\omega_3cs^4 + 72v_2^2\omega_6^2\omega_3^2 + 108v_2^2\omega_6^3\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 + 12\omega_6^2\omega_3cs^2 - 72v_2^2\omega_6\omega_3^2cs^2 - 36v_2^2\omega_6^2\omega_3^2 + 24\omega_6^2\omega_3^2cs^4 + 30v_2^2\omega_6\omega_3^3 + 24\omega_6\omega_3^2cs^2 - 3v_2^2\omega_6^2\omega_3^3 - 48\omega_6^2\omega_3cs^4 - 24\omega_6\omega_3cs^2 + 6v_2^2\omega_6^2\omega_3^2cs^2 + 12v_2^2\omega_6^2\omega_3^2 + 24\omega_6\omega_3^2cs^4 - 8\omega_6^2\omega_3^2cs^2 - 12v_2^2\omega_6^2\omega_3^2cs^2 + 36v_2^4\omega_6^2\omega_3^3 + 3v_2^4\omega_6^2\omega_3^3 + 24\omega_6^2cs^4 + \omega_6^2\omega_3^3cs^2 + 72v_2^2\omega_6\omega_3cs^2 - 12v_2^4\omega_6^2\omega_3^2 - 72v_2^4\omega_6^2\omega_3^2 + 6\omega_6\omega_3^3cs^4) \frac{1}{24\omega_6^2\omega_3^3}$$

coefficient  $C_{D_y^4 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t^4}$ :

$$C_{D_y^4 v_2}^{(0),\text{SRT}} = (24 - 26\omega^2cs^2 - 22\omega^2v_2^2 + 2\omega^3v_2^2 + \omega^3cs^2 - 48cs^2 - 36\omega - 36v_2^2 - \omega^3 + 14\omega^2 + 72\omega cs^2 + 54\omega v_2^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_y^4 v_2}^{(0),\text{MRT1}} = \\ (-6\omega_6\omega_3^3cs^2 - 12v_2^2\omega_6^2 + 8\omega_6^2\omega_3^2 - 24\omega_6^2cs^2 - \omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3 + 24v_2^2\omega_6\omega_3^2 - 12v_2^2\omega_6^2 + 24\omega_6\omega_3^2cs^2 + 6v_2^2\omega_6^3 - 6\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^3 + 42\omega_6^2\omega_3cs^2 + 12\omega_3^2 + 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^2 - 12\omega_3^2cs^2 - 20\omega_6^2\omega_3^2cs^2 - 16v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3 - 12\omega_6\omega_3cs^2 + \omega_6^2\omega_3^3cs^2 + 6\omega_6\omega_3^3 + 24v_2^2\omega_6^2\omega_3 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4 v_2}^{(0),\text{MRT2}} = \\ (-12cs^2\omega_3^2 - 20cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6^2 + 8\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^3 - \omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3 + 6cs^2\omega_6\omega_3^2 + 24v_2^2\omega_6\omega_3^2 - 24cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6^2 + 6v_2^2\omega_6^3 - 6\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^3 + 42\omega_6^2\omega_3cs^2 + 12\omega_3^2 + 12\omega_6\omega_3 - 12cs^2\omega_6\omega_3 + 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^2 - 16v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3 + 6\omega_6\omega_3^3 + 24v_2^2\omega_6^2\omega_3 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4 v_2}^{(0),\text{CLBM1}} = \\ (24cs^2\omega_6^2 - 12cs^2\omega_6\omega_3 - 12v_2^2\omega_6^2 + 2\omega_6^2\omega_3^2 - \omega_6^2\omega_3^3 + 60v_2^2\omega_6\omega_3 + 24v_2^2\omega_6\omega_3^2 - 84v_2^2\omega_6^2 - 24cs^2\omega_6\omega_3^2 - 60cs^2\omega_6^2 + 72cs^2\omega_6\omega_3^2 + 42v_2^2\omega_6^3 + 6\omega_6^2\omega_3 - 24v_2^2\omega_6\omega_3^3 + 30cs^2\omega_3^3 + 36\omega_3^2 - 2cs^2\omega_6^2\omega_3^2 - 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^2 + 2v_2^2\omega_6^2\omega_3^3 - 18\omega_3^3 + 12\omega_6\omega_3^3 - 12v_2^2\omega_6^2\omega_3 - 30cs^2\omega_6\omega_3^2 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4 v_2}^{(0),\text{CLBM2}} = \\ (24\omega_6^2cs^2 - 12v_2^2\omega_6^2 + 2\omega_6^2\omega_3^2 - 24\omega_6\omega_3^3cs^2 - \omega_6^2\omega_3^3 + 60v_2^2\omega_6\omega_3 + 24v_2^2\omega_6\omega_3^2 - 84v_2^2\omega_6^2 - 30\omega_6^2\omega_3cs^2 + 42v_2^2\omega_6^3 + 6\omega_6^2\omega_3 - 24v_2^2\omega_6\omega_3^3 + 72\omega_6\omega_3^2cs^2 + 36\omega_3^2 - 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^2 - 12\omega_6\omega_3cs^2 + 2v_2^2\omega_6^2\omega_3^2 - 18\omega_3^3 - 60\omega_3^2cs^2 - 2\omega_6^2\omega_3^2cs^2 + 12\omega_6\omega_3^3 - 12v_2^2\omega_6^2\omega_3 + \omega_6^2\omega_3^3cs^2 + 30\omega_3^3cs^2 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

coefficient  $C_{D_t^3 D_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t^3 \partial x_3}$ :

$$C_{D_t^3 D_z v_3}^{(0),\text{SRT}} = (-2 + 3\omega - \omega^2) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3 D_z v_3}^{(0),\text{MRT1}} = (-2 - \omega_4^2 + 3\omega_4) \frac{\rho}{2\omega_4^3}$$

$$C_{D_t^3 D_z v_3}^{(0),\text{MRT2}} = C_{D_t^3 D_z v_3}^{(0),\text{MRT1}}$$

$$C_{D_t^3 D_z v_3}^{(0),\text{CLBM1}} = C_{D_t^3 D_z v_3}^{(0),\text{MRT1}}$$

$$C_{D_t^3 D_z v_3}^{(0),\text{CLBM2}} = C_{D_t^3 D_z v_3}^{(0),\text{MRT1}}$$

coefficient  $C_{D_t^2 D_x D_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3}$ :

$$C_{D_t^2 D_x D_z v_1}^{(0),\text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_t^2 D_x D_z v_1}^{(0),\text{MRT1}} = (13\omega_4^2\omega_2^2 - 6\omega_4^3 + 12\omega_4^2 + 7\omega_4^3\omega_2 - \omega_4^3\omega_2^2 + 12\omega_2^2 - 24\omega_4^2\omega_2 + 12\omega_4\omega_2 - 24\omega_4\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_2^2}$$

$$C_{D_t^2 D_x D_z v_1}^{(0),\text{MRT2}} = C_{D_t^2 D_x D_z v_1}^{(0),\text{MRT1}}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_1}^{(0), \text{CLBM1}} = C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_1}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_1}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3}$ :

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{MRT1}} = (13\omega_4^2 \omega_2^2 + 12\omega_4^2 - \omega_4^2 \omega_2^3 - 6\omega_2^3 + 12\omega_2^2 - 24\omega_4^2 \omega_2 + 12\omega_4 \omega_2 + 7\omega_4 \omega_2^3 - 24\omega_4 \omega_2^2) \frac{v_1 \rho}{12\omega_4^2 \omega_2^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{MRT2}} = C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{CLBM1}} = C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t^2 \mathbf{D}_x \mathbf{D}_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3}$ :

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 \rho v_3}{6\omega^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{MRT1}} = (12\omega_4^2 \omega_2^2 - 12\omega_4^3 \omega_5 - 6\omega_5 \omega_2^3 - 6\omega_4 \omega_5 \omega_2^2 + 24\omega_4^3 \omega_5 \omega_2 - 6\omega_4^2 \omega_2^3 + 12\omega_4 \omega_5 \omega_2^3 + \omega_4^3 \omega_5 \omega_2^3 - 6\omega_4^3 \omega_2^2 - 10\omega_4^3 \omega_5 \omega_2^2 + 3\omega_4^3 \omega_2^3 - 12\omega_4^2 \omega_5 \omega_2 + 12\omega_4^2 \omega_5 \omega_2^2 - 7\omega_4^2 \omega_5 \omega_2^3) \frac{v_1 \rho v_3}{6\omega_4^3 \omega_5 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{MRT2}} = C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{CLBM1}} = (6\omega_4^2 \omega_2^2 - 12\omega_4^3 - 7\omega_4^2 \omega_2^3 + 18\omega_4^3 \omega_2 - 6\omega_2^3 - 7\omega_4^3 \omega_2^2 + \omega_4^3 \omega_2^3 + 12\omega_4 \omega_2^3 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_4^3 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_1}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3}$ :

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_3}^{(0), \text{SRT}} = (34\omega^2 c s^2 - 2\omega^2 v_1^2 - 2\omega^3 c s^2 + \omega^3 v_1^2 + 60c s^2 - 90\omega c s^2) \frac{\rho}{12\omega^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_3}^{(0), \text{MRT1}} = (9\omega_4 \omega_5 v_1^2 \omega_3^2 - 2\omega_4 \omega_5^2 \omega_3^2 c s^2 - 18\omega_5^2 \omega_2^2 c s^2 + 12\omega_4 \omega_5^2 \omega_2^2 - 6\omega_4 \omega_3^2 c s^2 + 22\omega_4 \omega_5^2 \omega_2^2 c s^2 + 12\omega_4 \omega_5 v_1^2 \omega_2 + 12\omega_5 v_1^2 \omega_2^2 + 12\omega_5 \omega_2^2 c s^2 + 12\omega_4 \omega_5 \omega_2 c s^2 - 6\omega_5 v_1^2 \omega_3^2 + 3\omega_5^2 \omega_3^2 c s^2 + 36\omega_4 \omega_5^2 v_1^2 \omega_2 - 30\omega_4 \omega_5 \omega_2^2 c s^2 + 6\omega_5^2 v_1^2 \omega_2^2 - 30\omega_4 \omega_5^2 \omega_2 c s^2 - 6\omega_5 \omega_2^3 c s^2 - \omega_5^2 v_1^2 \omega_2^3 + 12\omega_5 \omega_2^2 c s^2 - 24\omega_4 \omega_5^2 v_1^2 + 12\omega_4 v_1^2 \omega_2^2 + 9\omega_4 \omega_5 \omega_2^2 c s^2 + \omega_4 \omega_5^2 v_1^2 \omega_2^3 - 12\omega_5^2 v_1^2 \omega_2 + 12\omega_5 \omega_2^2 c s^2 - 10\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_3}^{(0), \text{MRT2}} = (-6c s^2 \omega_5 \omega_2^3 + 9\omega_4 \omega_5 v_1^2 \omega_2^3 + 12c s^2 \omega_5 \omega_2^2 + 12\omega_4 c s^2 \omega_5 \omega_2 - 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 30\omega_4 c s^2 \omega_5 \omega_2^2 + 12\omega_4 \omega_5 v_1^2 \omega_2 + 12\omega_5 v_1^2 \omega_2^2 + 9\omega_4 c s^2 \omega_5 \omega_2^3 - 6\omega_5 v_1^2 \omega_3^2 + 36\omega_4 \omega_5^2 v_1^2 \omega_2 - 2\omega_4 c s^2 \omega_5^2 \omega_2^3 + 6\omega_5^2 v_1^2 \omega_2^2 + 22\omega_4 c s^2 \omega_5^2 \omega_2^2 + 12c s^2 \omega_5^2 \omega_2^2 - \omega_5^2 v_1^2 \omega_3^2 - 18c s^2 \omega_5^2 \omega_2^2 - 24\omega_4 \omega_5^2 v_1^2 + 12\omega_4 c s^2 \omega_5^2 \omega_2^2 - 30\omega_4 c s^2 \omega_5^2 \omega_2 + 12\omega_4 v_1^2 \omega_2^2 + \omega_4 \omega_5^2 v_1^2 \omega_3^2 - 12\omega_5^2 v_1^2 \omega_2 - 6\omega_4 c s^2 \omega_5^2 + 12\omega_4 c s^2 \omega_5^2 \omega_2^3 + 3c s^2 \omega_5^2 \omega_2^3 - 10\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_3}^{(0), \text{CLBM1}} = (12\omega_5^2 \omega_2 c s^2 + 9\omega_4 \omega_5 \omega_2^3 c s^2 - 9\omega_4 \omega_5 v_1^2 \omega_2^3 + 12\omega_5 \omega_2^2 c s^2 + 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 12\omega_4 \omega_5 v_1^2 \omega_2 - 30\omega_4 \omega_5 \omega_2^2 c s^2 - 12\omega_5 v_1^2 \omega_2^2 - 30\omega_4 \omega_5 \omega_2^3 c s^2 + 6\omega_5 v_1^2 \omega_3^2 - 36\omega_4 \omega_5^2 v_1^2 \omega_2 + 22\omega_4 \omega_5^2 \omega_2^2 c s^2 - 6\omega_5^2 v_1^2 \omega_2^2 + 12\omega_4 \omega_5 \omega_2 c s^2 - \omega_5^2 v_1^2 \omega_3^2 + 3\omega_5^2 \omega_3^2 c s^2 + 24\omega_4 \omega_5^2 v_1^2 - 12\omega_4 v_1^2 \omega_2^2 + \omega_4 \omega_5^2 v_1^2 \omega_3^2 - 2\omega_4 \omega_5^2 \omega_2^3 c s^2 + 12\omega_5^2 v_1^2 \omega_2 - 18\omega_5^2 \omega_2^2 c s^2 + 12\omega_4 \omega_5^2 \omega_2^3 + 8\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4 \omega_5^2 c s^2 + 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^2 \mathbf{D}_z v_3}^{(0), \text{CLBM2}} = (-18\omega_5^2 \omega_2^2 c s^2 + 12\omega_4 \omega_5^2 c s^2 - 9\omega_4 \omega_5 v_1^2 \omega_2^3 - 6\omega_4 \omega_3^2 c s^2 + 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 2\omega_4 \omega_5^2 \omega_2^3 c s^2 + 12\omega_4 \omega_5 v_1^2 \omega_2 + 12\omega_4 \omega_5 \omega_2 c s^2 - 12\omega_5 v_1^2 \omega_2^2 + 3\omega_5^2 \omega_3^2 c s^2 + 22\omega_4 \omega_5^2 \omega_2^2 c s^2 + 6\omega_5 v_1^2 \omega_3^2 - 30\omega_4 \omega_5^2 \omega_2 c s^2 - 36\omega_4 \omega_5^2 v_1^2 \omega_2 - 6\omega_5 \omega_3^2 c s^2 - 6\omega_5^2 v_1^2 \omega_2^2 - 30\omega_4 \omega_5 \omega_2^2 c s^2 - \omega_5^2 v_1^2 \omega_2^3 + 24\omega_4 \omega_5^2 v_1^2 + 12\omega_5 \omega_2^2 c s^2 - 12\omega_4 v_1^2 \omega_2^2 + \omega_4 \omega_5^2 v_1^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2^2 + 9\omega_4 \omega_5 \omega_2^2 c s^2 + 8\omega_4 \omega_5^2 v_1^2 \omega_2^2 + 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

**coefficient**  $C_{\mathbf{D}_x^3 \mathbf{D}_z \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_3}$ :

$$C_{\mathbf{D}_x^3 \mathbf{D}_z \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 c s^2 + 6\omega^3 c s^2 - 120c s^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega c s^2) \frac{v_1 v_3}{6\omega^3}$$

$$\begin{aligned} C_{D_x^3 D_z^2}^{(0), \text{MRT1}} = & (6\omega_4^3 \omega_5^2 v_1^2 w_2^2 + \omega_4^2 \omega_5^2 w_2^3 - 12\omega_4^2 \omega_5 w_2^2 c s^2 + 6\omega_4 w_2^2 \omega_3^2 c s^2 + 12\omega_4^2 \omega_5^2 v_1^2 w_2 + 12\omega_4^3 \omega_5 w_2 - 12\omega_4^3 \omega_2^2 c s^2 - 12\omega_4^3 \omega_5 w_2^3 c s^2 - \\ & 24\omega_4^2 \omega_5^2 w_2 c s^2 - 3\omega_4^2 \omega_5^2 w_2^2 + 6\omega_4^3 \omega_5 w_2^3 - 12\omega_4 w_5^2 \omega_2^2 c s^2 + 6\omega_4^2 \omega_5^2 v_1^2 w_2^3 + 6\omega_3^3 w_5^3 c s^2 + 6\omega_4^2 \omega_5 w_3^3 c s^2 + 78\omega_3^3 w_5^2 w_2 c s^2 - 36\omega_3^3 \omega_5^2 c s^2 + 6\omega_3^4 w_2^2 - \\ & 21\omega_3^3 \omega_5 w_2^2 - 12\omega_4^2 \omega_5^2 v_1^2 w_2^2 - 30\omega_3^3 \omega_5^2 v_1^2 w_2 - 3\omega_4^3 w_3^2 + 42\omega_3^4 \omega_5 w_2^2 c s^2 - 12\omega_4^2 \omega_5^2 w_2^3 c s^2 + 6\omega_3^4 v_1^2 w_2^3 + 7\omega_3^4 \omega_5^2 w_2^2 + 6\omega_4^2 \omega_5 v_2^2 w_2^3 - 24\omega_4^3 \omega_5 w_2 c s^2 - \\ & 12\omega_4^2 \omega_5 v_2^2 w_2^2 - \omega_4^3 \omega_5^2 w_2^3 - 12\omega_4^3 v_2^2 w_2^2 - 48\omega_4^3 \omega_5^2 w_2^2 c s^2 + 6\omega_5^2 v_2^2 w_2^3 - 24\omega_4^3 \omega_5 v_2^2 w_2 + 24\omega_4^3 \omega_5^2 v_1^2 + 42\omega_4^2 \omega_5 v_1^2 w_2^2 + 42\omega_4^2 \omega_5^2 w_2^2 c s^2 - \\ & 12\omega_4^2 \omega_5^3 v_1^2 w_2^3 + 6\omega_4^2 \omega_5 w_2^2 - 12\omega_4^3 \omega_5 v_1^2 w_2^3 + 6\omega_4^3 \omega_5^2 w_2^2 c s^2 - 3\omega_4^2 \omega_5 w_2^3 + 6\omega_4 \omega_5^2 v_1^2 w_2^2 - 6\omega_4^2 \omega_5^2 w_2) \frac{v_1^3 v_2^3}{6\omega_4^3 \omega_5^2 w_2^3} \end{aligned}$$

$$\begin{aligned}
C_{D_3^3 D_2^2 \zeta_p}^{(0), \text{MRT2}} = & (6w_4^3 w_5^2 v_1^2 w_2^2 + w_4^2 w_5^2 w_2^3 - 12w_4^2 c s^2 w_5^2 w_3^3 + 12w_4^2 w_5^2 v_1^2 w_2 + 12w_3^3 w_5 w_2 + 78w_3^3 c s^2 w_5^2 w_2 + 42w_4^2 c s^2 w_5^2 w_2^2 - 3w_4^2 w_5^2 w_2^3 + 6w_3^4 w_5 w_2^3 + 6w_4^2 w_5^2 v_1^2 w_2^3 - 24w_4^2 c s^2 w_5^2 w_2 - 48w_3^4 c s^2 w_5^2 w_2^2 + 6w_4^3 w_2^2 - 21w_3^4 w_5 w_2^2 - 12w_3^2 w_5^2 v_1^2 w_2^2 - 30w_3^4 w_5^2 v_1^2 w_2 - 3w_4^3 w_2^3 + 6w_4^3 c s^2 w_5^2 w_2^3 + 6w_4^3 v_1^2 w_2^3 + 7w_4^2 w_5^2 w_2^3 + 6w_4 c s^2 w_5^2 w_3^2 + 6w_4^2 w_5 v_1^2 w_3^2 - 36w_3^4 c s^2 w_5^2 + 6w_4^3 c s^2 w_3^2 - 12w_4^3 c s^2 w_5 w_2^3 - 12w_4^2 w_5 v_1^2 w_2^2 - 12w_4 c s^2 w_5^2 w_2^2 - w_3^4 w_5^2 w_2^3 - 12w_3^2 v_1^2 w_2^2 + 42w_4^3 c s^2 w_5 w_2^2 - 12w_4^2 c s^2 w_2^2 + 6w_5^2 v_1^2 w_2^3 - 24w_4^3 w_5 v_1^2 w_2 + 24w_4^3 w_5^2 v_1^2 - 24w_4^3 c s^2 w_5 w_2 + 42w_3^4 w_5 v_1^2 w_2^2 - 12w_4 w_5^2 v_1^2 w_2 + 6w_4^2 w_5 w_2^2 - 12w_4^2 c s^2 w_5 w_2^2 - 12w_3^4 w_5 w_1 v_1^2 w_2^3 + 6w_4^2 c s^2 w_5 w_2^3 - 3w_4^2 w_5 w_2^3 + 6w_4 w_5^2 v_1^2 w_2^2 - 6w_4^3 w_5^2 w_2) \frac{v_1 v_3}{6w_4^3 c s^2 w_5^2 w_2^3}
\end{aligned}$$

$$\begin{aligned} C_{\substack{(0), \text{CLBM1}}}_{\substack{D_x^3 \\ x}} &= \\ & (-6w_3^4 w_5^2 v_1^2 w_2^2 + w_4^2 w_5^2 w_3^3 + 36w_4^2 w_5^2 w_2^2 c s^2 + 12w_4^3 w_5 w_2 + 6w_4^3 w_5^2 w_3^2 c s^2 - 3w_4^2 w_5^2 w_2^2 + 6w_3^3 w_5 w_2^3 + 6w_4^2 w_5^2 v_1^2 w_3^2 - 12w_4^2 w_5^2 w_3^2 c s^2 - 24w_4^3 w_5 w_2 c s^2 + \\ & 6w_3^2 w_2^2 - 21w_4^3 w_5 w_2^2 - 6w_4^2 w_5^2 v_1^2 w_2^2 + 12w_4^3 w_5^2 w_1^2 w_2 - 3w_4^3 w_2^3 - 36w_4^3 w_5^2 w_2^2 c s^2 + 18w_4^3 w_3^2 c s^2 - 6w_3^4 v_1^2 w_2^3 - 12w_4 w_2^2 w_3^2 c s^2 + 12w_4^2 w_5 w_3^2 c s^2 + \\ & 7w_4^3 w_5^2 w_2^2 + 36w_4^2 w_5^2 w_2 c s^2 - 12w_4^3 w_5^2 c s^2 - w_4^3 w_5^2 w_3^2 + 12w_4^3 v_1^2 w_2^2 + 6w_5^2 v_1^2 w_3^2 - 24w_4^3 w_5 v_1^2 w_2 + 72w_4^3 w_5 w_2^2 c s^2 + 12w_4^3 w_5 v_2^2 w_2^2 - 24w_4^3 w_5 w_2^2 c s^2 - \\ & 12w_4 w_5^2 v_1^2 w_3^2 - 36w_4^3 w_2^2 c s^2 + 6w_4^2 w_5 w_2^2 + 6w_4 w_5^2 w_3^2 c s^2 - 24w_4^3 w_5 w_2^3 c s^2 - 3w_4^2 w_5 w_2^3 + 6w_4 w_5^2 v_1^2 w_2^2 - 6w_4^2 w_5^2 w_2 w_3 + 12w_4^2 w_5^2 w_2^2 c s^2) \frac{v_1^4 v_3}{6w_3^4 w_5^2 w_2^3} \end{aligned}$$

$$C_{D_3^3 D_{2P}}^{(0), \text{CLBM2}} = (-6w_3^3 w_5^2 v_1^2 w_2^2 - 24w_3^4 w_5 w_2^3 c s^2 + w_4^2 w_5^2 w_3^2 - 12w_4^2 w_5^2 w_2 c s^2 + 12w_4^3 w_5 w_2 - 24w_4^2 w_5 w_2^2 c s^2 - 36w_4^3 w_2^2 c s^2 - 3w_4^2 w_5^2 w_2^2 + 6w_4 w_5^2 w_3^2 c s^2 + 6w_3^5 w_5^3 w_2^3 + 6w_2^4 w_5^2 v_1^2 w_2^3 + 72w_3^4 w_5 w_2^2 c s^2 + 6w_3^4 w_2^2 + 18w_3^4 w_3^2 c s^2 - 12w_4 w_5^2 w_2^2 c s^2 + 12w_4^2 w_5 w_3^2 c s^2 - 21w_4^3 w_5 w_2^2 - 6w_4^2 w_5^2 v_1^2 w_2^2 + 12w_4^3 w_5^2 v_2^2 w_2 - 3w_4^3 w_3^2 + 36w_4^3 w_5^2 w_2 c s^2 - 12w_4^3 w_5^2 c s^2 - 6w_3^4 w_1^2 w_3^2 + 7w_3^4 w_5^2 w_2^2 - 36w_4^3 w_5^2 w_2^2 c s^2 - 12w_4^2 w_5^2 w_3^2 c s^2 - w_4^3 w_5^2 w_3^2 + 12w_3^4 v_1^2 w_2^2 - 24w_3^4 w_5 w_2 c s^2 + 6w_5^2 v_1^2 w_2^3 - 24w_4^3 w_5 v_1^2 w_2 + 6w_4^3 w_5^2 w_2^3 c s^2 + 12w_4^3 w_5 v_1^2 w_2^2 - 12w_4 w_5^2 v_1^2 w_3^2 + 6w_4^2 w_5 w_2^3 - 3w_4^2 w_5 w_2^2 + 6w_4 w_5^2 v_1^2 w_2^2 - 6w_4^3 w_5^2 w_2 + 36w_4^2 w_5^2 w_2^2 c s^2) \frac{v_1 v_3}{6w_4^4 w_5^2 v_2^3}$$

**coefficient**  $C_{D_x^3 D_z v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_3}$ :

$$C_{\substack{(0), \text{SRT} \\ D_x^3 D_z v_1}} = (12 - 56\omega^2 c s^2 - 12\omega^2 v_1^2 - 12v_1^2 + 4\omega^3 c s^2 + 3\omega^3 v_1^2 - 96c s^2 - 18\omega - \omega^3 + 8\omega^2 + 18\omega v_1^2 + 144\omega c s^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\frac{D_x}{D_z} \frac{D_z}{D_x} v_1}^{(0), \text{MRT1}} = (2w_4^2 w_5^2 w_3^2 - 24 w_4^2 w_5 w_2^2 c s^2 + 6 w_4 w_5^2 w_3^2 c s^2 - 12 w_4^3 w_5 w_2^3 c s^2 + 3 w_4^3 w_5^2 v_1^2 w_3^2 - 24 w_4^2 w_5^2 w_2 c s^2 - 6 w_4^2 w_5^2 w_2^2 + 3 w_4^3 w_5 w_3^2 - 12 w_4 w_5^2 w_2^2 c s^2 + 6 w_4^2 w_5^2 c s^2 + 12 w_4^2 w_5 w_3^2 c s^2 + 36 w_4^3 w_5^2 w_2 c s^2 - 12 w_4^3 w_5^2 c s^2 - 6 w_4^3 w_5 w_2^2 + 12 w_4^2 w_5^2 v_1^2 w_3^2 - 30 w_4^3 w_5^2 v_1^2 w_2 + 36 w_4^3 w_5 w_2^2 c s^2 - 12 w_4^2 w_5^2 w_3^2 c s^2 + 6 w_4^3 w_5^2 w_1^3 + 3 w_4^3 w_5^2 w_2^2 + 12 w_4^2 w_5 v_1^2 w_3^2 - 12 w_4^3 w_5 w_2 c s^2 - 24 w_4^2 w_5 v_1^2 w_2^2 - w_4^3 w_5 w_3^2 - 12 w_4^3 v_1^2 w_2^2 - 32 w_4^3 w_5^2 w_2^2 c s^2 + 12 w_4^2 w_5^2 w_3^2 - 12 w_4^2 w_5 v_1^2 w_2 + 24 w_4^3 w_5^2 v_1^2 + 36 w_4^3 w_5^2 w_1^2 w_3^2 + 48 w_4^3 w_5^2 w_2^2 c s^2 - 18 w_4^2 w_5 v_1^2 w_3^2 + 12 w_4^3 w_5 w_2^2 - 12 w_4^3 w_5 v_1^2 w_3^2 + 4 w_4^3 w_5^2 w_3^2 c s^2 - 6 w_4^2 w_5 w_3^2) \frac{v_3^2}{12 w_4^2 w_5^2 w_3^2}$$

$$C_{\substack{O \\ D_x^3 D_z v_1}}^{(0), \text{MRT2}} = (2w_4^2 w_5^2 w_3^2 - 12w_4^2 c s^2 w_5^2 w_3^2 + 36w_3^4 c s^2 w_5^2 w_2 + 3w_3^4 w_5^2 w_1^2 w_3^2 + 48w_4^2 c s^2 w_5^2 w_2^2 - 6w_4^2 w_5^2 w_2^2 + 3w_3^4 w_5 w_3^2 - 24w_4^2 c s^2 w_5^2 w_2 - 32w_4^2 c s^2 w_5^2 w_2^2 - 6w_3^4 w_5 w_2^2 + 12w_4^2 w_5^2 w_1^2 w_2^2 - 30w_3^4 w_5^2 v_1^2 w_2 + 4w_3^4 c s^2 w_5^2 w_3^2 + 6w_3^4 v_1^2 w_3^2 + 3w_3^4 w_5^2 w_2^2 + 6w_4^2 c s^2 w_5^2 w_3^2 + 12w_4^2 w_5 v_1^2 w_3^2 - 12w_3^4 c s^2 w_5^2 w_2^2 + 6w_3^4 c s^2 w_5^2 w_3^2 - 12w_3^4 c s^2 w_5 w_2^2 - 24w_4^2 w_5 v_1^2 w_2^2 - 12w_4 c s^2 w_5^2 w_2^2 - w_4^2 w_5^2 w_3^2 - 12w_3^4 v_1^2 w_2^2 + 36w_3^4 c s^2 w_5 w_2^2 - 12w_3^4 c s^2 w_2^2 + 12w_5^2 v_1^2 w_2^2 - 12w_3^4 w_5 v_1^2 w_2^2 + 24w_4^2 w_5^2 v_1^2 - 12w_3^4 c s^2 w_5 w_2 + 36w_3^4 w_5 v_1^2 w_2^2 - 18w_4^2 w_5^2 v_1^2 w_2^2 + 12w_4^2 w_5 w_2^2 - 24w_4^2 c s^2 w_5^2 w_2^2 - 12w_3^4 w_5 v_1^2 w_3^2 + 12w_4^2 c s^2 w_5 w_2^2 - 6w_4^2 w_5 w_3^2) \frac{v_3}{12w_3^4 w_5^2 w_2^2}$$

$$\begin{aligned} C_{\substack{0,0,0,0,0,0 \\ D_x^3 D_y^3 v_1^3}}^{(0), \text{CLBM1}} = & (-12w_3^4 w_5^2 v_2^2 w_2^2 + 2w_4^2 w_5^2 w_3^2 + 48w_4^2 w_5^2 w_2^2 c s^2 + 4w_4^3 w_5^2 w_3^2 c s^2 + 3w_4^3 w_5^2 v_1^2 w_2^3 - 6w_4^2 w_5^2 w_2^2 + 3w_4^3 w_5 w_3^2 - 12w_4^2 w_5^2 w_3^2 c s^2 - \\ & 12w_5^2 w_5 w_2 c s^2 - 6w_3^4 w_5 w_2^2 + 12w_4^2 w_5^2 v_1^2 w_2^2 + 30w_4^3 w_5^2 v_1^2 w_2 - 32w_3^3 w_5^2 w_2^2 c s^2 + 6w_4^3 w_5^2 c s^2 - 6w_3^4 v_1^2 w_2^3 - 12w_4 w_5^2 w_2^2 c s^2 + 12w_4^2 w_5 w_3^2 c s^2 + 3w_4^3 w_5^2 w_2^2 + \\ & 12w_2^3 w_5 w_2 c s^2 - 12w_4^2 w_5^2 c s^2 - 24w_4^3 w_5 v_1^2 w_2^2 - w_4^3 w_5^2 w_3^2 + 12w_4^3 v_1^2 w_2^2 + 12w_5^2 v_1^1 w_3^2 + 12w_4^3 w_5 v_1^2 w_2 - 24w_4^3 w_5^2 v_1^2 + 36w_4^3 w_5 w_2^2 c s^2 - \\ & 12w_4^3 w_5 v_1^1 w_2^2 - 24w_4^2 w_5 w_2^2 c s^2 - 18w_4 w_5 v_1^2 w_3^2 - 12w_4^3 w_2^2 c s^2 + 12w_4^2 w_5 w_2^2 + 6w_4 w_5^2 w_3^2 c s^2 - 12w_4^2 w_5 w_3^2 c s^2 - 6w_4^2 w_5 w_3^2 - 24w_4^2 w_5 w_2^2 c s^2) \frac{v_3^3}{12w_4^3 w_5^2 w_2^2} \end{aligned}$$

$$C_{\substack{D_3 D_2 v_1}}^{(0), \text{CLBM2}} = (-12w_3^4 w_5^2 v_1^2 w_2^2 - 12w_4^3 w_5 w_3 c s^2 + 2w_4^2 w_5^2 w_3^2 - 24w_4^2 w_5^2 w_2 c s^2 + 3w_4^3 w_5^2 v_1^2 w_3^2 - 24w_4^2 w_5 w_2^2 c s^2 - 12w_3^4 w_2^2 c s^2 - 6w_4^2 w_5^2 w_2^2 + 6w_4 w_2^2 w_3^2 c s^2 + 3w_4^3 w_5 w_3 w_2^3 + 36w_4^3 w_5 w_2^2 c s^2 + 6w_4^3 w_3^2 c s^2 - 12w_4 w_2^2 w_3^2 c s^2 + 12w_4^2 w_5 w_3^2 c s^2 - 6w_4^3 w_5 w_2^2 + 12w_4^2 w_5^2 v_1^2 w_2^2 + 30w_4^3 w_5^2 v_2^2 w_2 + 36w_4^3 w_5^2 w_2 c s^2 - 12w_4^3 w_5^2 c s^2 - 6w_4^3 v_1^2 w_3^2 + 3w_4^3 w_5^2 w_2^2 + 12w_4^2 w_5 v_1^2 w_3^2 - 32w_4^3 w_5^2 w_2^2 c s^2 - 24w_4^2 w_5 v_1^2 w_2^2 - 12w_4^2 w_5^2 w_2^3 c s^2 - w_4^3 w_5^2 w_2^3 + 12w_4^3 v_1^2 w_2^2 - 12w_4^3 w_5 w_2 c s^2 + 12w_5^4 v_1^2 w_3^2 + 12w_4^3 w_5 v_1^2 w_2 - 24w_4^3 w_5^2 v_1^2 + 4w_4^3 w_5^2 w_3^2 c s^2 - 12w_4^3 w_5 v_1^2 w_2^2 - 18w_4 w_5 v_1^2 w_2^3 + 12w_4^2 w_5 w_2^2 - 6w_4^2 w_5 w_2^3 + 48w_4^3 w_5^2 w_2^2 c s^2) \frac{\rho v_3}{12w_3^4 w_5^2 w_3^2}$$

**coefficient**  $C_{D_x^3 D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_1^3 \partial x_3}$ :

$$C_{\substack{D_x^0 SRT \\ D_x^3 z v_3}}^{(0),SRT} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_1^2 - 36v_1^2 + 4\omega^3 cs^2 + \omega^3 v_1^2 - 96cs^2 - 54\omega - \omega^3 + 20\omega^2 + 54\omega v_1^2 + 144\omega cs^2) \frac{v_1 \rho}{12w^3}$$

$$C_{\substack{D^3 \\ \mathcal{D}_x \\ \mathcal{D}_z \\ v_3}}^{(0), \text{MRT1}} = (-36w_5w_2cs^2 + 9w_5w_2^3 + 6w_2^3cs^2 - 48w_5^2cs^2 - 44w_5^2w_2^2cs^2 - 36w_5w_2^2 - 36w_5v_1^2w_2 - 6w_2^3 + 24w_5w_2 - 12w_2^2cs^2 + 48w_5v_1^2w_2^2 + 12w_2^2 - 12w_5v_1^2w_3^2 + 4w_5^2w_2^3cs^2 - 8w_5^2v_1^2w_2^2 - 12w_5^2w_2 - 12w_5w_2^3cs^2 + w_5^2v_1^2w_3^2 + 11w_5^2w_2^2 + 90w_5^2w_2cs^2 + 6v_1^2w_3^2 - 12v_1^2w_2^2 - w_5^2w_2^3 + 48w_5w_2^2cs^2 + 12w_5^2v_1^2) \frac{v_1\rho}{12w_5^2w_3^2}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT2}} = (-12cs^2\omega_5\omega_2^3 + 9\omega_5\omega_2^3 + 48cs^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 36cs^2\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^3 - 8\omega_5^2v_1^2\omega_2^2 + 90cs^2\omega_5^2\omega_2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^3 + 11\omega_5^2\omega_2^2 - 44cs^2\omega_5^2\omega_2^2 + 6v_1^2\omega_2^3 + 6cs^2\omega_5^2\omega_2^3 - 48cs^2\omega_5^2 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 4cs^2\omega_5^2\omega_2^3 + 12\omega_5^2v_1^2 - 12cs^2\omega_5^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBIM1}} = (18\omega_5^2\omega_2cs^2 + 9\omega_5\omega_2^3 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 96\omega_5\omega_2^2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 30\omega_5\omega_2^3cs^2 - 6\omega_5v_1^2\omega_2^3 - 60\omega_2^2cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^3 + 4\omega_5^2\omega_2^3cs^2 + 11\omega_5^2\omega_2^2 + 30\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6v_1^2\omega_2^3 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - 26\omega_5^2\omega_2^2cs^2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBIM2}} = (-26\omega_5^2\omega_2^2cs^2 + 9\omega_5\omega_2^3 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 30\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 4\omega_5^2\omega_2^3cs^2 + 12\omega_2^2 - 60\omega_2^2cs^2 - 6\omega_5v_1^2\omega_2^3 - 30\omega_5\omega_2^3cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^3 + 11\omega_5^2\omega_2^2 + 96\omega_5\omega_2^2cs^2 - 6v_1^2\omega_2^3 + 18\omega_5^2\omega_2^2cs^2 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

**coefficient**  $C_{D_t^2 D_y D_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3}$ :

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}} = (-24\omega_4\omega_3^2 - 6\omega_4^3 + 12\omega_4^2 + 12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4^2\omega_3 - \omega_4^3\omega_3^2 + 7\omega_4^3\omega_3 + 13\omega_4^2\omega_3^2) \frac{\rho v_3}{12\omega_4^3\omega_3^2}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{CLBIM1}} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{CLBIM2}} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t^2 D_y D_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3}$ :

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}} = (-24\omega_4\omega_3^2 + 12\omega_4^2 + 7\omega_4\omega_3^3 + 12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4^2\omega_3 - 6\omega_3^3 - \omega_4^2\omega_3^3 + 13\omega_4^2\omega_3^2) \frac{v_2\rho}{12\omega_4^2\omega_3^2}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{CLBIM1}} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{CLBIM2}} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x D_y D_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{SRT}} = (-20 + 30\omega + \omega^3 - 12\omega^2) \frac{v_2\rho v_3}{2\omega^3}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}} = (-12\omega_4^2\omega_2\omega_3 - 6\omega_4^3\omega_2 - 6\omega_4\omega_3^3 - 16\omega_4^2\omega_2\omega_3^2 + 30\omega_4^2\omega_2\omega_3^2 - 4\omega_4^3\omega_3^2 + 18\omega_4\omega_2\omega_3^2 - 6\omega_2\omega_3^3 + 18\omega_4^3\omega_2\omega_3 - 12\omega_4\omega_2\omega_3^2 + 12\omega_4^3\omega_2\omega_3^2 + 12\omega_4^2\omega_3^3 - 6\omega_4^3\omega_3 - 12\omega_4^2\omega_3^2 + 3\omega_4^3\omega_2\omega_3^2) \frac{v_2\rho v_3}{6\omega_4^3\omega_2\omega_3^2}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{CLBIM1}} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{CLBIM2}} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x D_y D_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{SRT}} = (-20 + 30\omega + \omega^3 - 12\omega^2) \frac{v_1\rho v_3}{2\omega^3}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT1}} = (-12\omega_4^2\omega_2^2 - 12\omega_4^2\omega_2\omega_3 + 3\omega_4^3\omega_2^3\omega_3 + 12\omega_4^2\omega_2^3 - 6\omega_4^3\omega_2 - 12\omega_4\omega_2^2\omega_3 - 6\omega_2^3\omega_3 - 16\omega_4^3\omega_2^2\omega_3 + 12\omega_4^3\omega_2^2 - 4\omega_4^3\omega_2^3 + 18\omega_4\omega_2^3\omega_3 + 18\omega_4^3\omega_2\omega_3 - 16\omega_4^2\omega_2^3\omega_3 - 6\omega_4^3\omega_3 - 6\omega_4\omega_2^3 + 30\omega_4^2\omega_2^2\omega_3) \frac{\omega_1 v_3}{6\omega_4^3\omega_2^3\omega_3}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_2}^{(0), \text{MRT2}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_2}^{(0), \text{MRT1}}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_2}^{(0), \text{CLBM1}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_2}^{(0), \text{MRT1}}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_2}^{(0), \text{CLBM2}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_3}^{(0), \text{SRT}} = (-20 + 30\omega + \omega^3 - 12\omega^2) \frac{v_1 v_2 \rho}{2\omega^3}$$

$$C_{D_1^{(0)}, MRT1}^{(0), D_2 D_3 D_4 D_5 v_3} = (-16\omega_4\omega_3^2\omega_3^2 - 4\omega_3^2\omega_3^3 + 3\omega_4\omega_2^3\omega_3^3 - 6\omega_4\omega_3^3 - 12\omega_4\omega_2^2\omega_3 + 12\omega_2^3\omega_2^2 + 12\omega_2^2\omega_3^3 - 6\omega_2^3\omega_3 + 30\omega_4\omega_2^2\omega_3^2 - 12\omega_2^2\omega_3^2 - 16\omega_4\omega_2^2\omega_3^3 + 18\omega_4\omega_2^3\omega_3 + 18\omega_4\omega_2\omega_3^3 - 6\omega_2\omega_3^3 - 12\omega_4\omega_2\omega_3^2 - 6\omega_4\omega_2^3) \frac{v_1 v_2 \rho}{6\omega_4\omega_3^2\omega_3^3}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_3}^{(0), \text{MRT2}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_3}^{(0), \text{MRT1}}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_3}^{(0), \text{CLBM1}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_3}^{(0), \text{MRT1}}$$

$$C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_3}^{(0), \text{CLBM2}} = C_{\mathrm{D}_t \mathrm{D}_x \mathrm{D}_y \mathrm{D}_z v_3}^{(0), \text{MRT1}}$$

coefficient  $C_{D_x^2 D_y D_z \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{\frac{D_x^2}{D_y D_z} \rho}^{(0), \text{SRT}} = (-12\omega^2 cs^2 + 24\omega^2 v_1^2 + 40v_1^2 + \omega^3 cs^2 - 2\omega^3 v_1^2 - 20cs^2 - 60\omega v_1^2 + 30\omega cs^2) \frac{v_2 v_3}{\omega^3}$$

$$G_{\frac{D_2}{D_2}y_Dz_\rho}^{(0), \text{MRT1}} = (-8w_4w_5^2v_1^2w_3^2w_3^3 + w_3^2w_3^2w_3^3cs^2 - 2w_3^2w_5v_1^2w_2^2w_3^2 - 2w_4w_5^2w_2^2w_3^3cs^2 - 2w_3^4w_5^2w_3^2w_3^2cs^2 + w_2^2w_5w_3^2w_3^3cs^2 - 2w_3^2w_5^2w_2^2w_3^2cs^2 - 2w_3^2w_5^2w_3^2w_3^3cs^2 + 6w_3^4w_5v_1^2w_2^2w_3^3 + 3w_3^4w_5w_2^2v_1^2w_3^3 + 6w_4^3w_5^2w_2^2w_3^3cs^2 + 3w_4w_5^2v_1^2w_3^2w_3^2 + 7w_4^2w_5^2v_1^2w_3^3w_3^3 + 6w_4^2w_5^2w_2^2w_3^3cs^2 + 4w_2^2w_5^2w_2^2w_3^2w_3^2 + w_3^4w_5^2w_3^2w_3^3cs^2 - 21w_3^4w_5^2v_1^2w_2^2w_3^3 + 4w_4w_5^2v_1^2w_2^2w_3^3 + w_3^2w_5v_1^2w_2^2w_3^2w_3^2 - 2w_3^4w_5^2w_2^2w_3^3cs^2 - 2w_2^2w_5^2w_2^2w_3^2cs^2 - 12w_4^2w_5^2v_1^2w_2^2w_3^3 + 3w_4w_5^2v_1^2w_2^2w_3^2 - 2w_3^4w_5v_1^2w_2^2w_3^3 - 2w_3^2w_5^2w_2^2w_3^2cs^2 + 7w_3^4w_5^2v_1^2w_2^2w_3^3 + 6w_3^4w_5w_2^2w_3^3cs^2 + 7w_4^2w_5^2v_1^2w_2^2w_3^3 - 2w_4^2w_5^2w_2^2w_3^2cs^2 + w_3^2w_5w_2^2w_3^2cs^2 - 12w_3^4w_5^2v_1^2w_2^2w_3^2 - 2w_4w_5w_2^2w_3^3cs^2 + w_4^2w_5v_1^2w_2^2w_3^3 + 12w_3^4w_5^2v_1^2w_2^2w_3^3 - 2w_3^4w_2^2w_3^3cs^2 - 8w_3^4w_5^2v_1^2w_2^2w_3^3 - 2w_4^3w_5w_2^2w_3^3cs^2 + 6w_4^2w_5w_2^2w_3^2cs^2 + w_3^4v_2^2w_3^2w_3^3 + w_4w_5^2w_2^2w_3^3cs^2 + 3w_5^2w_5^2w_2^2w_3^2w_3^3 + 7w_3^4w_5^2v_1^2w_2^2w_3^3 + 10w_3^4w_5^2v_1^2w_3^3 - 2w_3^4w_5w_2^2w_3^2cs^2 - 2w_3^2w_5v_1^2w_2^2w_3^3 + w_4^2w_5w_2^2w_3^2cs^2 - 2w_3^4v_1^2w_2^2w_3^3 - 6w_4^2w_5w_2^2w_3^2cs^2 + w_3^4w_5^2w_3^2w_3^3cs^2 - 2w_3^4w_5^2v_1^2w_2^2w_3^3 + 4w_3^4w_5^2v_1^2w_2^2w_3^3 - 2w_4^2w_5^2w_2^2w_3^2cs^2) \frac{v_2v_3}{w_4^2w_5^2w_2^2w_3^3}$$

$$\begin{aligned}
C_{D_x^2 D_z}^{(0), \text{MRT2}} = & (-8w_4 w_2 v_1^2 w_3^2 w_3 - 2 w_3^2 w_5 v_1^2 w_2^2 w_3 - 2 w_2^4 c s^2 w_5 w_2^2 w_3^3 - 6 w_3^4 c s^2 w_5^2 w_2^2 w_3^3 + w_4^3 c s^2 w_5^2 w_2^3 w_3 - 8 w_2^4 w_5^2 v_1^2 w_2^3 w_3^2 - 2 w_2^4 c s^2 w_5^2 w_2 w_3^3 + \\
& 6 w_3^2 w_5^2 v_2^2 w_2^2 w_3^3 + 3 w_4^3 w_5^2 v_1^2 w_3^2 + 3 w_4 w_5^2 v_2^2 w_3^2 w_3^3 + 7 w_4^2 w_5^2 v_1^2 w_3^2 w_3^3 - 2 w_3^4 c s^2 w_5 w_2 w_3^3 + 6 w_4^3 c s^2 w_5^2 w_2^2 w_3^2 + w_4^3 c s^2 w_5^2 w_3^2 w_3^3 - 2 w_3^4 c s^2 w_5^2 w_2^2 w_3^2 + \\
& 4 w_4^2 w_5^2 v_1^2 w_2^2 w_3^3 + w_4^2 c s^2 w_5 w_2^2 w_3^3 - 21 w_3^2 w_5^2 v_1^2 w_2 w_3^3 + 4 w_4 w_5^2 v_1^2 w_2^2 w_3^3 + w_4^3 w_5 v_1^2 w_3^2 w_3^2 - 12 w_3^2 w_5^2 v_1^2 w_3^2 w_3^3 - 2 w_3^3 c s^2 w_5^2 w_2^2 w_3^2 + 3 w_4^2 w_5^2 v_1^2 w_2^2 w_3^3 - \\
& 2 w_4^2 w_5 v_1^2 w_2^3 w_3 + 7 w_4^2 w_5^2 v_1^2 w_2 w_3^2 + 7 w_4^2 w_5^2 v_1^2 w_2 w_3^3 - 2 w_3^4 c s^2 w_5 w_2^2 w_3^3 + w_4^3 c s^2 w_5^2 w_3^3 - 2 w_3^4 c s^2 w_5^2 w_3^3 - 2 w_2^2 c s^2 w_5^2 w_3^2 w_3^3 - 12 w_3^2 w_5^2 v_1^2 w_2^2 w_3^2 + \\
& w_4^3 c s^2 w_5 w_2^2 w_3^3 + w_4^2 w_5 v_1^2 w_3^2 w_3^3 + w_4 c s^2 w_5^2 w_3^2 w_3^3 + 12 w_4^2 w_5^2 v_2^2 w_2^2 w_3^3 - 8 w_4^2 w_5^2 v_2^2 w_3^2 w_3^3 + w_4^2 c s^2 w_5^2 w_2^2 w_3^2 + w_4^3 v_1^2 w_3^2 w_3^3 + 3 w_5^2 v_1^2 w_3^2 w_3^3 + \\
& 6 w_4^2 c s^2 w_5^2 w_3^2 w_3^3 + 7 w_3^2 w_5^2 v_1^2 w_3^2 w_3^3 + 10 w_4^3 w_5^2 v_2^2 w_3^3 - 2 w_3^4 w_5 v_1^2 w_2 w_3^3 - 2 w_3^3 c s^2 w_5^2 w_2 w_3^3 - 2 w_3^4 c s^2 w_5^2 w_2^2 w_3^2 + 6 w_4^3 c s^2 w_5 w_2^2 w_3^3 - 2 w_4^2 v_1^2 w_2^2 w_3^3 - \\
& 2 w_4^2 w_5^2 v_1^2 w_2^3 w_3 + 4 w_4^3 w_5^2 v_1^2 w_2 w_3^2 - 2 w_4^2 c s^2 w_5^2 w_2^2 w_3^2 - 2 w_4 c s^2 w_5^2 w_2^2 w_3^3 - 2 w_4^2 w_5 v_1^2 w_2^2 w_3^3 - 2 w_3^4 c s^2 w_5 w_2^2 w_3^2 + 6 w_4^3 c s^2 w_5^2 w_2 w_3^3) \frac{v_2 v_3}{w_3^4 w_5^2 w_3^2 w_3^3}
\end{aligned}$$

$$\begin{aligned}
C_{D_2^2 D_2^2 D_2^2}^{(0), \text{CLBM1}} = & (-2w_4^3 w_2^2 c s^2 w_3 - 8w_4 w_2^5 v_2^2 w_2^3 w_3 + 2w_3^4 w_5 v_2^2 w_2^2 w_3 - 2w_4^3 w_5 w_2 c s^2 w_3 - 2w_3^4 w_2^2 w_2^2 c s^2 w_3 + w_4 w_5^2 w_3 c s^2 w_3 + w_4' w_5^2 w_3^2 c s^2 w_3 - \\
& 2w_2^2 w_5 w_2^2 c s^2 w_3 - 8w_4^2 w_5^2 v_2^2 w_3^2 w_3 - 6w_4^3 w_5 v_2^1 w_2^3 w_3 + 3w_3^3 w_5^2 v_2^1 w_2^3 w_3 + 3w_4 w_5^2 v_2^1 w_3^2 w_3 + 7w_2^4 w_5^2 v_2^1 w_3^2 w_3 - 2w_4^2 w_5^2 w_3^2 c s^2 w_3 - 2w_3^2 w_5^2 w_2 c s^2 w_3 + \\
& 4w_4 w_5^2 v_1^2 w_2^2 w_3 - 6w_4^3 w_5^2 w_2^2 c s^2 w_3 + w_3^4 w_5 w_2^2 c s^2 w_3^2 - 7w_4^3 w_5 v_1^2 w_2^3 w_3 + 4w_4 w_5 v_1^2 w_2^3 w_3 - w_4^3 w_5 v_1^2 w_3^2 w_3 - 10w_4^2 w_5 v_1^2 w_3^2 w_3 + 3w_3^2 w_5^2 v_1^2 w_3^2 w_3 + \\
& 2w_3^4 w_5 v_1^2 w_2^3 w_3 + 3w_4^3 w_5^2 v_1^2 w_2^2 w_3^2 + 6w_4^2 w_5^2 w_2^2 c s^2 w_3^2 - 2w_3^3 w_5 w_2^2 c s^2 w_3^3 + 6w_4^2 w_5^2 w_2^2 c s^2 w_3^3 + 3w_4^2 w_5^2 v_1^2 w_2 w_3^3 - 2w_3^4 w_5^2 c s^2 w_3^3 - 10w_4^3 w_5^2 v_1^2 w_2^2 w_3^3 + \\
& 6w_3^4 w_5^2 w_2 c s^2 w_3^3 + w_4^2 w_5 w_2^2 c s^2 w_3^3 - 2w_4^2 w_5^2 w_2^2 c s^2 w_3^3 - w_4^2 w_5 v_1^2 w_2^3 w_3^3 - 2w_3^4 w_5^2 w_2^2 c s^2 w_3^3 + 8w_3^4 w_5^2 v_1^2 w_2^2 w_3^3 - 8w_4^3 w_5^2 v_1^2 w_3^2 w_3 + w_4^3 w_5^2 c s^2 w_3^3 + \\
& w_4^3 w_5^2 w_3^2 c s^2 w_3 - 2w_4 w_5^2 w_2^2 c s^2 w_3^3 - w_3^3 v_1^2 w_2^3 w_3^3 + 3w_5^2 v_2^2 w_3^2 w_3^3 + 7w_4^3 w_5^2 v_2^2 w_3^2 w_3^3 + 6w_4^3 w_5 w_2^2 c s^2 w_3^3 - 2w_3^4 w_5^2 w_2^2 c s^2 w_3^3 + 2w_3^2 w_5^2 v_1^2 w_3^3 + \\
& 2w_4^3 w_5 v_1^2 w_2 w_3^3 + 2w_3^4 v_1^1 w_2^2 w_3^3 - 2w_3^4 w_5 w_2^2 c s^2 w_3^3 + w_4^3 w_5 w_2^2 c s^2 w_3^3 - 2w_3^4 w_5^2 v_1^2 w_3^2 w_3^3 + 4w_3^4 v_1^2 w_2^2 w_3^3 + 2w_4^2 w_5 v_1^2 w_3^2 w_3^3) \frac{v_2 v_3}{w_4^3 w_5^2 w_3^2 w_3^3}
\end{aligned}$$

$$8\omega_4^3\omega_5^2v_1^2\omega_2^3\omega_3 - \omega_4^3v_1^2\omega_2^3\omega_3 + 3\omega_4^2v_1^2\omega_2^3\omega_3^2 + 7\omega_4^2\omega_5^2v_1^2\omega_2^3\omega_3^2 - 6\omega_4^3\omega_5^2\omega_2^2\omega_3^3cs^2 + \omega_4^3\omega_5^2\omega_2^3\omega_3cs^2 + 2\omega_4^3\omega_5^2v_1^2\omega_3^3 + 2\omega_4^3\omega_5v_1^2\omega_2\omega_3^3 - 2\omega_4^2\omega_5^2\omega_2\omega_3^3cs^2 + 2\omega_4^3v_1^2\omega_2^3\omega_3^2 - 2\omega_4^3\omega_5\omega_2^3\omega_3^3cs^2 - 2\omega_4^3\omega_5^2v_1^2\omega_2^3\omega_3^2 + 4\omega_4^3\omega_5^2v_1^2\omega_2^2\omega_3 + \omega_4^2\omega_5^2\omega_2^3\omega_3^2cs^2 + 2\omega_4^2\omega_5v_1^2\omega_2^2\omega_3^3) \frac{v_2v_3}{\omega_4^3\omega_5^2\omega_2^3\omega_3^3}$$

coefficient  $C_{D_x^2 D_y D_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{D_x^2 D_y D_z v_1}^{(0), SRT} = (132 - 198\omega - 5\omega^3 + 76\omega^2) \frac{v_1 v_2 \rho v_3}{6\omega^3}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), MRT1} = (18\omega_4^3\omega_5^2\omega_3^2 + 28\omega_4^3\omega_2^2\omega_3^3 - 30\omega_4^3\omega_2^3\omega_3 + 12\omega_4^3\omega_2^3\omega_3^2 - 30\omega_4^3\omega_2^2\omega_3^2 - 30\omega_4^3\omega_2^3\omega_3^3 - 5\omega_4^3\omega_2^3\omega_3^2 + 6\omega_4^3\omega_2^2\omega_3 + 18\omega_4^2\omega_2\omega_3^3 + 12\omega_4^2\omega_2\omega_3^2 + 24\omega_4^3\omega_2^3\omega_3^2 + 12\omega_4^3\omega_2^3\omega_3^3 + 12\omega_4^2\omega_2^2\omega_3^2 + 18\omega_4^2\omega_2^3\omega_3 + 30\omega_4^2\omega_2^2\omega_3^3 + 18\omega_4^3\omega_2\omega_3^2 - 42\omega_4^2\omega_2^3\omega_3^2 + 24\omega_4^2\omega_2^3\omega_3^3 - 36\omega_4^3\omega_2\omega_3^3) \frac{v_1 v_2 \rho v_3}{6\omega_4^3\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), MRT2} = C_{D_x^2 D_y D_z v_1}^{(0), MRT1}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), CLBM1} = C_{D_x^2 D_y D_z v_1}^{(0), MRT1}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), CLBM2} = C_{D_x^2 D_y D_z v_1}^{(0), MRT1}$$

coefficient  $C_{D_x^2 D_y D_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{D_x^2 D_y D_z v_2}^{(0), SRT} = (-56\omega^2 cs^2 + 52\omega^2 v_1^2 + 84v_1^2 + 4\omega^3 cs^2 - 5\omega^3 v_1^2 - 96cs^2 - 126\omega v_1^2 + 144\omega cs^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), MRT1} = (40\omega_4^3\omega_5^2v_1^2\omega_2^2 - 24\omega_4^2\omega_5\omega_2^2cs^2 + 6\omega_4\omega_5^2\omega_2^3cs^2 + 48\omega_4^2\omega_5^2v_1^2\omega_2 - 12\omega_4^3\omega_2^2\omega_3^2cs^2 - 12\omega_4^3\omega_5\omega_2^3cs^2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 - 24\omega_4^2\omega_5^2\omega_2cs^2 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2^3 + 6\omega_4^3\omega_5^2\omega_2^3cs^2 + 12\omega_4^2\omega_5\omega_2^3cs^2 + 36\omega_4^3\omega_5^2\omega_2\omega_3^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^3 - 60\omega_4^2\omega_5^2v_1^2\omega_2^2 - 90\omega_4^3\omega_5^2v_1^2\omega_2 + 36\omega_4^3\omega_5\omega_2^2cs^2 - 12\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 - 32\omega_4^3\omega_5^2\omega_2^2cs^2 + 12\omega_4^2\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2\omega_2^2 + 36\omega_4^3\omega_5^2v_1^2\omega_2^3 + 48\omega_4^2\omega_5^2\omega_2^2cs^2 - 30\omega_4^2\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2^3 + 4\omega_4^3\omega_5^2\omega_2^3cs^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), MRT2} = (40\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^2cs^2\omega_5^2\omega_2^3 + 48\omega_4^2\omega_5^2v_1^2\omega_2 + 36\omega_4^3cs^2\omega_5^2\omega_2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 + 48\omega_4^2cs^2\omega_5^2\omega_2^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2^3 - 24\omega_4^2\omega_5^2\omega_2^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 60\omega_4^2\omega_5^2v_1^2\omega_2^2 - 90\omega_4^3\omega_5^2v_1^2\omega_2 + 4\omega_4^3cs^2\omega_5^2\omega_2^3 + 6\omega_4^3\omega_5^2v_1^2\omega_2^3 + 12\omega_4^2\omega_5^2\omega_2^3cs^2 + 36\omega_4^3\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 + 36\omega_4^3\omega_5^2v_1^2\omega_2^3 + 12\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 + 48\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^3\omega_5^2cs^2\omega_5\omega_2 + 36\omega_4^3\omega_5^2v_1^2\omega_2^2 - 30\omega_4^2\omega_5^2v_1^2\omega_2^3 - 24\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^3 + 12\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), CLBM1} = (16\omega_4^3\omega_5^2v_1^2\omega_2^2 + 48\omega_4^2\omega_5^2\omega_2^2cs^2 + 4\omega_4^3\omega_5^2\omega_2^3cs^2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 + 24\omega_4^2\omega_5^2v_1^2\omega_2^3 - 12\omega_4^2\omega_5^2\omega_2^3cs^2 - 12\omega_4^3\omega_5\omega_2^2cs^2 - 36\omega_4^2\omega_5^2v_1^2\omega_2^2 - 32\omega_4^3\omega_5^2\omega_2^2cs^2 + 6\omega_4^3\omega_5^2\omega_2^3cs^2 - 6\omega_4^3v_1^2\omega_2^3 - 12\omega_4^2\omega_5^2\omega_2^2cs^2 + 12\omega_4^2\omega_5\omega_2^3cs^2 - 12\omega_4^2\omega_5^2v_1^2\omega_2^3 + 36\omega_4^3\omega_5^2\omega_2\omega_2^3 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 + 36\omega_4^3\omega_5^2v_1^2\omega_2^3 - 36\omega_4^3\omega_5^2\omega_2^2 - 24\omega_4^2\omega_5^2\omega_2^2cs^2 - 30\omega_4^2\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), CLBM2} = (16\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^3\omega_5\omega_2^3cs^2 - 24\omega_4^2\omega_5^2\omega_2cs^2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 - 24\omega_4^2\omega_5\omega_2^2cs^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^3 + 6\omega_4\omega_5^2\omega_2^3cs^2 + 36\omega_4^2\omega_5^2\omega_2^3cs^2 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 12\omega_4^2\omega_5^2\omega_2^3cs^2 - 36\omega_4^2\omega_5^2v_1^2\omega_2^2 - 6\omega_4^3\omega_5^2v_1^2\omega_2^3 + 36\omega_4^3\omega_5^2\omega_2\omega_2^3 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2 + 36\omega_4^3\omega_5^2v_1^2\omega_2^3 - 36\omega_4^3\omega_5^2\omega_2^2 - 24\omega_4^2\omega_5^2\omega_2^2cs^2 - 30\omega_4^2\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

coefficient  $C_{D_x^2 D_y D_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{D_x^2 D_y D_z v_3}^{(0), SRT} = (-56\omega^2 cs^2 + 52\omega^2 v_1^2 + 84v_1^2 + 4\omega^3 cs^2 - 5\omega^3 v_1^2 - 96cs^2 - 126\omega v_1^2 + 144\omega cs^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), MRT1} = (36\omega_5^2v_1^2\omega_2^3 + 36\omega_5^2\omega_2\omega_3^2cs^2 - 24\omega_5^2\omega_2^2\omega_3^2cs^2 - 12\omega_5^2\omega_2^3\omega_3^2cs^2 - 24\omega_5^2v_1^2\omega_2^3 + 6v_1^2\omega_2^3\omega_3^3 + 36\omega_5\omega_2^2\omega_3^3cs^2 + 48\omega_5^2v_1^2\omega_2^3\omega_3^3 - 12\omega_5v_1^2\omega_2^3\omega_3^3 + 48\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3^2cs^2 - 12\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3^2cs^2 + 12\omega_5^2v_1^2\omega_2^3\omega_3^2 - 90\omega_5^2v_1^2\omega_2^3\omega_3^3 + 4\omega_5^2\omega_2^3\omega_3^3cs^2 + 6\omega_5^2\omega_2^3\omega_3^3cs^2 + 48\omega_5^2\omega_2^2\omega_3^2cs^2 + 40\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5\omega_2\omega_3^2cs^2 - 30\omega_5^2v_1^2\omega_2^3\omega_3^2 - 60\omega_5^2v_1^2\omega_2^2\omega_3^2 + 12\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3^2cs^2 + 12\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5\omega_2\omega_3^2cs^2 + 24\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3^2cs^2 - 30\omega_5^2v_1^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3^2 - 12\omega_5^2v_1^2\omega_2^3\omega_3^2) \frac{v_2 \rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), MRT2} = (36\omega_5^2v_1^2\omega_2^3 + 36\omega_5^2\omega_2\omega_3^2 - 12cs^2\omega_5\omega_2\omega_3^3 - 12cs^2\omega_5\omega_2\omega_3^2 + 48cs^2\omega_5^2\omega_2^2\omega_3^2 - 24\omega_5^2v_1^2\omega_2^2\omega_3^2 + 6v_1^2\omega_2^3\omega_3^3 + 36\omega_5\omega_2^2\omega_3^3cs^2 + 6cs^2\omega_5^2\omega_2^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^2\omega_3^2 - 12cs^2\omega_5^2\omega_2^3\omega_3^2 + 48\omega_5^2v_1^2\omega_2^2\omega_3^2 - 12\omega_5^2v_1^2\omega_2^3\omega_3^2 + 48\omega_5^2v_1^2\omega_2^2\omega_3^3 + 4cs^2\omega_5^2\omega_2^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^2\omega_3^2 - 12\omega_5^2v_1^2\omega_2^2\omega_3^3 + 12\omega_5^2v_1^2\omega_2^2\omega_3^2 - 12\omega_5^2\omega_2\omega_3^2cs^2 + 12\omega_5^2v_1^2\omega_2^2\omega_3^2 - 12\omega_5^2\omega_2\omega_3^2 - 12\omega_5^2v_1^2\omega_2^2\omega_3^2) \frac{v_2 \rho}{12\omega_5^2\omega_2^2\omega_3^3}$$

$$\begin{aligned} C_{\mathbf{D}_t^2 \mathbf{D}_y \mathbf{D}_z v_3}^{(0), \text{CLBM1}} &= (-36\omega_5 v_1^2 \omega_2^2 \omega_3^3 - 12\omega_5^2 c s^2 \omega_3^2 + 6\omega_3^2 c s^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 c s^2 \omega_3 - 12\omega_5 \omega_2 c s^2 \omega_3^2 + 24\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 6v_1^2 \omega_2^3 \omega_3^2 - 12\omega_5 \omega_2^3 c s^2 \omega_3^2 + \\ 48\omega_5^2 \omega_2^2 c s^2 \omega_3^2 + 12\omega_5 v_1^2 \omega_2^3 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 - 12\omega_5 v_1^2 \omega_2^3 \omega_3^2 + 12\omega_5 \omega_2^3 c s^2 \omega_3^2 - 32\omega_5^2 \omega_2^2 c s^2 \omega_3^2 - 6\omega_5^2 v_1^2 \omega_2 \omega_3^2 + 6\omega_5^2 \omega_2^3 c s^2 \omega_3 - 12\omega_5^2 c s^2 \omega_3^2 + \\ 16\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 24\omega_5^2 \omega_2 c s^2 \omega_3^2 - 30\omega_5^2 v_1^2 \omega_2^3 \omega_3^2 + 36\omega_5^2 \omega_2 c s^2 \omega_3^2 - 36\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2^3 \omega_3^2 - 5\omega_5^2 v_1^2 \omega_2^3 \omega_3^2 + 24\omega_5^2 v_1^2 \omega_2^2 \omega_3 + 4\omega_5^2 \omega_2^3 c s^2 \omega_3^2 - \\ 24\omega_5 \omega_2 c s^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 c s^2 \omega_3^2 + 36\omega_5 \omega_2^2 c s^2 \omega_3^2 + 12\omega_5 v_1^2 \omega_2 \omega_3^2 + 24\omega_5^2 v_1^2 \omega_2^3 \omega_3^2) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t^2 \mathbf{D}_y \mathbf{D}_z v_3}^{(0), \text{CLBM2}} &= (-12\omega_5^2 \omega_2^3 \omega_3^2 c s^2 - 12\omega_2^2 \omega_3^3 c s^2 - 36\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 36\omega_5^2 \omega_2 \omega_3^3 c s^2 - 24\omega_5 \omega_2^2 \omega_3^2 c s^2 + 24\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 6v_1^2 \omega_2^3 \omega_3^2 - 12\omega_5^2 \omega_2^2 \omega_3 c s^2 + \\ 12\omega_5 v_1^2 \omega_2^3 \omega_3^2 + 4\omega_5^2 \omega_2^3 \omega_3^3 c s^2 + 12v_1^2 \omega_2^2 \omega_3^2 + 36\omega_5 \omega_2^2 \omega_3^2 c s^2 - 12\omega_5 v_1^2 \omega_2^3 \omega_3^2 - 24\omega_5^2 \omega_2 \omega_3^2 c s^2 - 6\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 12\omega_5^2 \omega_2^3 \omega_3^2 c s^2 + 12\omega_5 \omega_2^3 \omega_3^2 c s^2 + \\ 16\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 30\omega_5^2 v_1^2 \omega_2^3 \omega_3^2 + 6\omega_5^2 \omega_2^3 \omega_3^2 c s^2 + 48\omega_5^2 \omega_2^2 \omega_3^2 c s^2 - 36\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 12\omega_5 \omega_2 \omega_3^2 c s^2 + 12\omega_5^2 v_1^2 \omega_2^3 - 5\omega_5^2 v_1^2 \omega_2^3 \omega_3^2 - 12\omega_5 \omega_2^3 \omega_3^2 c s^2 + \\ 24\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 + 12\omega_5 v_1^2 \omega_2 \omega_3^2 + 6\omega_5^2 \omega_2^3 \omega_3 c s^2 - 32\omega_5^2 \omega_2 \omega_3^2 c s^2 + 24\omega_5^2 v_1^2 \omega_2^3 \omega_3^2) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^2} \end{aligned}$$

coefficient  $C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3}$ :

$$C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_2 \rho v_3}{6\omega^3}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0), \text{MRT1}} &= (12\omega_4^2 \omega_6 \omega_3^2 - 7\omega_4^2 \omega_6 \omega_3^3 - 12\omega_4^2 \omega_6 \omega_3 + 3\omega_4^3 \omega_3^3 - 12\omega_4^3 \omega_6 + \omega_4^3 \omega_6 \omega_3^2 - 10\omega_4^3 \omega_6 \omega_3^2 - 6\omega_4^3 \omega_3^2 + 24\omega_4^3 \omega_6 \omega_3 - 6\omega_4 \omega_6 \omega_3^2 - 6\omega_4^2 \omega_3^3 - \\ 6\omega_6 \omega_3^3 + 12\omega_4 \omega_6 \omega_3^2 + 12\omega_4^2 \omega_3^2) \frac{v_2 \rho v_3}{6\omega_4^3 \omega_6 \omega_3^2} \end{aligned}$$

$$C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0), \text{MRT2}} = C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0), \text{CLBM1}}$$

$$C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_2}^{(0), \text{CLBM1}}$$

coefficient  $C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3}$ :

$$C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_3}^{(0), \text{SRT}} = (34\omega^2 c s^2 - 2\omega^2 v_2^2 + \omega^3 v_2^2 - 2\omega^3 c s^2 + 60c s^2 - 90\omega c s^2) \frac{\rho}{12\omega^3}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_3}^{(0), \text{MRT1}} &= (-6\omega_6 \omega_3^3 c s^2 + 9\omega_4 v_2^2 \omega_6 \omega_3^3 + 12\omega_4 \omega_6^2 \omega_3 c s^2 - 30\omega_4 \omega_6^2 \omega_3 c s^2 - 30\omega_4 v_2^2 \omega_6 \omega_3^2 - 24\omega_4 v_2^2 \omega_6^2 - 30\omega_4 \omega_6 \omega_3^2 c s^2 + 12v_2^2 \omega_6 \omega_3^2 + \\ 12\omega_4 v_2^2 \omega_6 \omega_3 + 12\omega_6 \omega_3^2 c s^2 - 6\omega_4 v_2^2 \omega_3^3 + 9\omega_4 \omega_6 \omega_3^3 c s^2 - 6v_2^2 \omega_6 \omega_3^2 + 12\omega_4 v_2^2 \omega_3^2 + 12\omega_6^2 \omega_3 c s^2 - v_2^2 \omega_6^2 \omega_3^2 - 18\omega_6^2 \omega_3^2 c s^2 + 12\omega_4 \omega_6^2 \omega_3^2 c s^2 - 2\omega_4 \omega_6^2 \omega_3^2 c s^2 + \\ 6v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_6^2 \omega_3^3 c s^2 - 10\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_4 \omega_6 \omega_3 c s^2 - 12v_2^2 \omega_6^2 \omega_3 + 4\omega_2^2 \omega_6^2 \omega_3^2 - 6\omega_4 \omega_3^3 c s^2 + 22\omega_4 \omega_6^2 \omega_3^2 c s^2) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_3}^{(0), \text{MRT2}} &= (-6\omega_4 c s^2 \omega_3^3 + 9\omega_4 v_2^2 \omega_6 \omega_3^3 - 30\omega_4 c s^2 \omega_6 \omega_3^2 - 18\omega_4 c s^2 \omega_6 \omega_3^2 - 30\omega_4 v_2^2 \omega_6 \omega_3^2 + 12\omega_4 c s^2 \omega_6^2 - 24\omega_4 v_2^2 \omega_6^2 + 3c s^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6 \omega_3^2 - \\ 2\omega_4 c s^2 \omega_6^2 \omega_3^2 + 12\omega_4 v_2^2 \omega_6 \omega_3 - 6\omega_4 v_2^2 \omega_3^3 - 6v_2^2 \omega_6 \omega_3^2 + 12c s^2 \omega_6^2 \omega_3 + 12\omega_4 c s^2 \omega_6^2 + 12\omega_4 v_2^2 \omega_3^2 + 22\omega_4 c s^2 \omega_6^2 \omega_3^2 - v_2^2 \omega_6^2 \omega_3^2 - 30\omega_4 c s^2 \omega_6 \omega_3^2 + \\ 6v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 9\omega_4 c s^2 \omega_6 \omega_3 - 10\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 12v_2^2 \omega_6^2 \omega_3 - 6c s^2 \omega_6 \omega_3 + 12\omega_4 c s^2 \omega_6 \omega_3 + 4\omega_2^2 \omega_6^2 \omega_3^2 + 12c s^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_3}^{(0), \text{CLBM1}} &= (-30\omega_4 c s^2 \omega_6 \omega_3^2 - 9\omega_4 v_2^2 \omega_6 \omega_3^3 + 30\omega_4 v_2^2 \omega_6 \omega_3^2 + 24\omega_4 v_2^2 \omega_6^2 + 9\omega_4 c s^2 \omega_6 \omega_3^2 + 12\omega_4 c s^2 \omega_6^2 - 12v_2^2 \omega_6 \omega_3^2 - 6\omega_4 c s^2 \omega_6 \omega_3^2 - 6c s^2 \omega_6 \omega_3^2 - \\ 12\omega_4 v_2^2 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_3^3 + 12c s^2 \omega_6 \omega_3^2 + 12\omega_4 c s^2 \omega_6^2 \omega_3^2 + 6v_2^2 \omega_6 \omega_3^2 + 12\omega_4 c s^2 \omega_6 \omega_3 - 12\omega_4 v_2^2 \omega_3^2 - 18c s^2 \omega_6 \omega_3^2 - v_2^2 \omega_6^2 \omega_3^2 - 30\omega_4 c s^2 \omega_6 \omega_3^2 - \\ 6v_2^2 \omega_6^2 \omega_3^2 + 3c s^2 \omega_6 \omega_3^2 - 36\omega_4 v_2^2 \omega_6 \omega_3^2 + 8\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_4 c s^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3 + 22\omega_4 c s^2 \omega_6 \omega_3^2 + 4\omega_2^2 \omega_6^2 \omega_3^2 + 12c s^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_y^2 \mathbf{D}_z v_3}^{(0), \text{CLBM2}} &= (-9\omega_4 v_2^2 \omega_6 \omega_3^3 - 30\omega_4 \omega_6 \omega_3^2 c s^2 + 30\omega_4 v_2^2 \omega_6 \omega_3^2 - 6\omega_6 \omega_3^3 c s^2 + 24\omega_4 v_2^2 \omega_6^2 + 12\omega_4 \omega_6^2 \omega_3^2 c s^2 - 30\omega_4 \omega_6^2 \omega_3 c s^2 - 12v_2^2 \omega_6 \omega_3^2 + \\ 9\omega_4 \omega_6 \omega_3^2 c s^2 - 12\omega_4 v_2^2 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_3^3 + 12\omega_6 \omega_3^2 c s^2 + 6v_2^2 \omega_6 \omega_3^2 - 12\omega_4 v_2^2 \omega_3^2 + 12\omega_6 \omega_3^2 c s^2 - 2\omega_4 \omega_6 \omega_3^2 c s^2 + 12\omega_4 \omega_6^2 \omega_3^2 c s^2 - v_2^2 \omega_6^2 \omega_3^2 - 6v_2^2 \omega_6^2 \omega_3^2 - \\ 36\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 18\omega_6 \omega_3^2 c s^2 + 8\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^2 + 22\omega_4 \omega_6 \omega_3^2 c s^2 - 6\omega_4 \omega_3^3 c s^2 + 3\omega_6^2 \omega_3^3 c s^2 + \omega_4 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_4 \omega_6 \omega_3 c s^2) \frac{\rho}{12\omega_4 \omega_6 \omega_3^2} \end{aligned}$$

coefficient  $C_{\mathbf{D}_x \mathbf{D}_y^2 \mathbf{D}_z \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \mathbf{D}_z \rho}^{(0), \text{SRT}} = (-12\omega^2 c s^2 + 24\omega^2 v_2^2 - 2\omega^3 v_2^2 + \omega^3 c s^2 - 20c s^2 + 40v_2^2 + 30\omega c s^2 - 60\omega v_2^2) \frac{v_1 v_3}{\omega^3}$$

$$\begin{aligned} C_{\mathbf{D}_x \mathbf{D}_y^2 \mathbf{D}_z \rho}^{(0), \text{MRT1}} &= (-6\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^3 \omega_2^3 \omega_6 \omega_3^3 c s^2 - 2\omega_4^3 \omega_2^3 \omega_6^2 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - \\ 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 3\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 12\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 3\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 21\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - \\ \omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 12\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 6\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 7\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 - \\ 2\omega_4^3 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 4\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 3\omega_4 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 7\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 8\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \\ \omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 7\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + 6\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2) \frac{v_1 v_3}{\omega^3} \end{aligned}$$

$$+ 4w_3^4 w_2 v_2 w_6 w_3^2 + 10w_3^4 w_3^2 v_2^2 w_6^2 + 4w_4 w_3^2 v_2^2 w_6^2 w_3^2 + 6w_2^2 w_3^2 w_6^2 w_3^2 c s^2 + 6w_3^4 w_3^2 v_2^2 w_6 w_3^2 - 12w_2^4 w_3^2 v_2^2 w_6^2 w_3^2 - 8w_3^4 w_2 v_2^2 w_6^2 w_3^3 + 6w_4^3 w_3^2 v_2^2 w_3 c s^2 - 2w_3^4 w_3^2 w_6^2 c s^2 - 2w_4 w_3^2 w_6^2 w_3^2 c s^2 + w_4^2 w_2^2 w_6^2 w_3^3 c s^2 - 2w_3^4 w_2^2 w_6^2 w_3^2 c s^2 - 2w_3^4 w_2 w_6^2 w_3^2 c s^2 + w_4^3 w_2^2 w_6 w_3^3 c s^2 - 8w_4 w_3^2 w_2^2 w_6^2 w_3^3) \frac{v_1^4 t_3^2}{w_3^4 w_2^2 w_6^2 w_3^3}$$

$$C_{\frac{D_x(0)}{D_y(2)} D_z p}^{(0), \text{MRT2}} = (-2w_4^2 c s^2 w_5^2 w_6^2 w_3^2 - 2w_2^4 w_3^2 v_2^2 w_6 w_3^2 - 2w_3^4 c s^2 w_2 w_6^2 w_3^2 + w_3^4 c s^2 w_2 w_6 w_3^3 - 2w_4^3 w_3^2 v_2^2 w_6^2 w_3^3 + 6w_4^3 c s^2 w_3^2 w_6^2 w_3 + 3w_3^4 v_2^2 w_6^2 w_3^3 + 7w_3^2 w_2^2 w_6^2 w_3 + w_4^2 c s^2 w_2^2 w_6^2 w_3^3 + w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_3^4 c s^2 w_2^2 w_6 w_3^2 + 3w_4^2 w_2 v_2^2 w_6^2 w_3^3 + 12w_4^3 w_3^2 v_2^2 w_6^2 w_3^2 + 3w_3^2 v_2^2 w_6^2 w_3^3 + w_4^3 c s^2 w_2 w_6^2 w_3^3 + w_3^4 c s^2 w_3^2 w_6^2 w_3^2 - 21w_4^3 w_3^2 v_2^2 w_6^2 w_3 - 2w_4^2 c s^2 w_3^2 w_6 w_3^2 - 12w_4^3 w_2^2 v_2^2 w_6^2 w_3^2 - 6w_4^3 c s^2 w_3^2 w_6^2 w_3^2 + w_4^2 c s^2 w_3^2 w_6 w_3^3 + 7w_4^3 w_2^2 v_2^2 w_6^2 w_3^2 - 2w_4 c s^2 w_3^2 w_6^2 w_3^2 - 2w_3^4 w_2^2 v_2^2 w_6^2 w_3^2 + 4w_4^2 w_2^2 v_2^2 w_6^2 w_3^2 + w_3^4 c s^2 w_3^2 w_6^2 w_3^2 + 6w_4^3 c s^2 w_3^2 w_6 w_3^2 + 3w_4 w_2^2 v_2^2 w_6^2 w_3^2 + 7w_4^2 w_3^2 v_2^2 w_6^2 w_3 + w_4^3 w_2^2 v_2^2 w_6 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6^2 w_3^2 - 8w_2^2 w_5^2 v_2^2 w_6^2 w_3^2 - 2w_4^3 c s^2 w_3^2 w_6 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6^2 w_3^2 + w_3^4 w_2^2 v_2^2 w_6^2 w_3^2 - 2w_3^4 c s^2 w_2^2 w_6^2 w_3^2 + w_4 c s^2 w_3^2 w_6^2 w_3^2 - 2w_4^3 w_2^2 v_2^2 w_6 w_3^2 - 2w_3^4 w_2^2 v_2^2 w_6^2 w_3^2 + 6w_4^3 c s^2 w_3^2 w_6^2 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6^2 w_3^2 - 2w_4^2 c s^2 w_3^2 w_6^2 w_3^2 + 7w_4^2 w_2^2 v_2^2 w_6^2 w_3^2 + 4w_4^3 w_2 v_2^2 w_6^2 w_3^2 + 10w_4^3 w_3^2 v_2^2 w_6^2 + 4w_4 w_2^2 v_2^2 w_6^2 w_3^2 + 6w_4^3 w_3^2 v_2^2 w_6 w_3^2 + 6w_4^3 c s^2 w_2^2 w_6^2 w_3^2 - 12w_4^2 w_3^2 v_2^2 w_6^2 w_3^2 - 8w_4^3 w_2 v_2^2 w_6^2 w_3^2 - 2w_4^3 w_3^2 v_2^2 w_6 w_3^2 - 2w_3^4 c s^2 w_2^2 w_6^2 w_3^2 - 2w_4^3 c s^2 w_3^2 w_6 w_3^2 - 8w_4 w_2^2 v_2^2 w_6^2 w_3^2) \frac{v_1 v_3}{w_4^3 w_2^2 w_6^2 w_3^2}$$

$$\begin{aligned} C^{(6)}_{\mathbf{D}_x^2 \mathbf{D}_y^2 \mathbf{D}_z p} = & (2w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_4^2 w_3^2 c s^2 w_6^2 w_3 + w_4^2 w_3^2 c s^2 w_6 w_3^3 - 2w_4^2 w_3^2 v_2^2 w_6^2 w_3^3 - 6w_4^3 w_3^2 c s^2 w_6^2 w_3^3 + 3w_4^3 v_2^2 w_6^2 w_3^3 - 2w_4^2 w_3^2 c s^2 w_6 w_3^4 + \\ & 3w_4^2 w_3^2 v_2^2 w_6^2 w_3 - w_4^2 w_3^2 v_2^2 w_6 w_3^3 + w_3^2 w_3^2 c s^2 w_6^2 w_3^3 + 3w_4^2 w_3^2 v_2^2 w_6^2 w_3^3 + 8w_4^3 w_3^2 v_2^2 w_6^2 w_3^3 + 3w_3^2 v_2^2 w_6^2 w_3^3 - 7w_4^3 w_3^2 v_2^2 w_6^2 w_3 - 10w_4^3 w_3^2 v_2^2 w_6^2 w_3^2 - \\ & 2w_4^3 w_3^2 c s^2 w_6^2 w_3^3 + 6w_4^3 w_3^2 c s^2 w_6^2 w_3 + 6w_4^3 w_3^2 c s^2 w_6^2 w_3^2 + 7w_4^3 w_3^2 v_2^2 w_6^2 w_3^3 + w_3^2 w_3^2 c s^2 w_6^2 w_3^3 + 2w_4^3 w_3^2 v_2^2 w_6^2 w_3^3 - 2w_3^2 w_3^2 c s^2 w_6 w_3 + 4w_4^2 w_2^2 v_2^2 w_6^2 w_3^2 + \\ & 3w_4^2 w_3^2 v_2^2 w_6^2 w_3^3 - 2w_4^2 w_3^2 c s^2 w_6 w_3^2 + 3w_4^2 w_3^2 v_2^2 w_6^2 w_2 - 2w_3^2 w_3^2 c s^2 w_6^2 w_3^2 - w_4^2 w_3^2 v_2^2 w_6^2 w_3^3 - w_3^2 w_3^2 v_2^2 w_6^2 w_3 + 2w_3^2 w_3^2 v_2^2 w_6 w_3 - \\ & 2w_4^2 w_3^2 c s^2 w_6^2 w_3^2 + 2w_4^2 w_3^2 v_2^2 w_6^2 w_3 - 2w_4^2 w_3^2 c s^2 w_6^2 w_3^2 + w_3^2 w_3^2 c s^2 w_6^2 w_3^3 + w_4^2 w_3^2 c s^2 w_6^2 w_3^2 - 2w_4^2 w_3^2 c s^2 w_6^2 w_3^2 + 6w_4^2 w_3^2 c s^2 w_6^2 w_3^2 + \\ & 7w_4^2 w_3^2 v_2^2 w_6^2 w_3^3 + 4w_4^2 w_3^2 v_2^2 w_6^2 w_3^2 + 2w_3^2 w_3^2 v_2^2 w_6^2 w_3^2 - 2w_4^2 w_3^2 c s^2 w_6^2 w_3^3 + w_4^2 w_3^2 c s^2 w_6^2 w_3^2 - 6w_4^3 w_3^2 v_2^2 w_6 w_3^2 - 10w_4^2 w_3^2 v_2^2 w_6^2 w_3^2 - \\ & 8w_4^2 w_3^2 v_2^2 w_6^2 w_3^3 - 2w_4^2 w_3^2 c s^2 w_6^2 w_3^2 - 2w_4^2 w_3^2 c s^2 w_6^2 w_3^3 + 2w_4^2 w_3^2 v_2^2 w_6^2 w_3^2 - 2w_4 w_3^2 c s^2 w_6^2 w_3^2 + 6w_4^3 w_3^2 c s^2 w_6 w_3^2 - 8w_4 w_3^2 v_2^2 w_6^2 w_3^3) \frac{v_1 v_2 v_3}{w_3^4 w_2^2 w_6 w_3^2} \end{aligned}$$

$$\begin{aligned} C_{\frac{D}{D_x} \frac{D}{D_y} \frac{D}{D_z}}^{G, \text{LM2}} &= (2w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_4^2 w_3^2 w_6 w_3 c s^2 - 2w_4^2 w_2^2 w_6 w_3^2 c s^2 - 2w_4^2 w_2^2 v_2^2 w_6 w_3^2 - 2w_4^2 w_2^2 w_6 w_3 c s^2 + 3w_4^2 v_2^2 w_6 w_3^2 + w_4^2 w_2^2 w_3^2 c s^2 + 3w_4^2 w_2^2 v_2^2 w_6 w_3^2 - 6w_4^2 w_3^2 w_6 w_3^2 c s^2 - w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_4^2 w_3^2 w_6 w_3^2 c s^2 + 3w_4^2 w_2 v_2^2 w_6 w_3^2 + 8w_4^2 w_3^2 v_2^2 w_6 w_3^2 + 3w_3^2 v_2^2 w_6 w_3^2 - 7w_3^2 v_2^2 w_6 w_3^2 + 6w_4^2 w_3^2 w_6 w_3^2 c s^2 - 10w_4^2 w_3^2 v_2^2 w_6 w_3^2 + w_4^2 w_3^2 w_6 w_3^2 c s^2 - 2w_3^2 w_3^2 w_6 w_3^2 c s^2 + 7w_4^2 w_2 v_2^2 w_6 w_3^2 + w_3^2 w_3^2 w_6 w_3^2 c s^2 - 2w_3^2 w_2 v_2^2 w_6 w_3^2 c s^2 + w_3^2 w_2 v_2^2 w_6 w_3^2 - 4w_4^2 w_2 v_2^2 w_6 w_3^2 - 2w_2^2 w_3^2 w_6 w_3^2 c s^2 + 3w_4^2 w_2 v_2^2 w_6 w_3^2 + 3w_4^2 w_3^2 v_2^2 w_6 w_3^2 + w_3 w_3^2 w_6 w_3^2 c s^2 - w_3^2 w_2 v_2^2 w_6 w_3^2 - 8w_4^2 w_2 v_2^2 w_6 w_3^2 - w_4^2 w_2 v_2^2 w_6 w_3^2 c s^2 - 2w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_4^2 w_3^2 w_6 w_3^2 c s^2 + 2w_4^2 w_3^2 v_2^2 w_6 w_3^2 + 2w_4^2 w_2 v_2^2 w_6 w_3^2 + 2w_4^2 w_3^2 w_6 w_3^2 c s^2 - 2w_4^2 w_3^2 v_2^2 w_6 w_3^2 + 7w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_4^2 w_3^2 w_6 w_3^2 c s^2 + 4w_4^2 w_2 v_2^2 w_6 w_3^2 - 2w_3^2 w_3^2 w_6 w_3^2 c s^2 + 2w_3^2 w_3^2 v_2^2 w_6 w_3^2 + 4w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 2w_3^2 w_2 v_2^2 w_6 w_3^2 c s^2 + w_4^2 w_2 v_2^2 w_6 w_3^2 - 6w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 10w_4^2 w_3^2 v_2^2 w_6 w_3^2 - 8w_4^2 w_2 v_2^2 w_6 w_3^2 + 6w_4^2 w_3^2 w_6 w_3^2 c s^2 + 2w_4^2 w_3^2 v_2^2 w_6 w_3^2 + 6w_4^2 w_3^2 w_6 w_3^2 c s^2 - 8w_4^2 w_2 v_2^2 w_6 w_3^2) \frac{v_1 v_3}{w_3^2 w_2^2 w_6 w_3^2} \end{aligned}$$

**coefficient**  $C_{D_x D_y^2 D_z v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{\substack{D_x D_y^2 D_z v_1}}^{(0), \text{SR1}} = (-56\omega^2 cs^2 + 52\omega^2 v_2^2 - 5\omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 + 84v_2^2 + 144\omega cs^2 - 126\omega v_2^2) \frac{\rho v_3}{12\omega^3}$$

$$\begin{aligned} C_{\substack{\text{O}, \text{MRT1} \\ \text{D}_1 \text{D}_2 \text{D}_3 \text{D}_4 \text{v}_1 \text{v}_2}} &= (-32w_4^3w_6^2w_3^2cs^2 - 12w_4^3v_2^2w_3^2 - 5w_4^3v_2^2w_6^2w_3^2 - 12w_4^3w_6w_3cs^2 + 6w_4^3v_2^2w_3^3 + 48w_4^2v_2^2w_6^2w_3 + 40w_4^3v_2^2w_6^2w_3^2 - 12w_4^2w_6^2w_3^3cs^2 - \\ 90w_4^3v_2^2w_6^2w_3 + 4w_4^3w_6^2w_3^2cs^2 + 48w_4^3v_2^2w_6^2 - 60w_4^2v_2^2w_6^2w_3^2 + 48w_2^2w_6^2w_3^2cs^2 - 12w_3^2w_6^2cs^2 + 24w_4^2v_2^2w_6^2w_3^3 + 6w_4^3w_6^2w_3^2cs^2 - 24w_4^2w_6^2w_3cs^2 + \\ 12v_2^2w_6^2w_3^3 + 12w_4^2v_2^2w_6w_3^3 - 12w_4^3w_6w_3^2cs^2 + 6w_4w_6^2w_3^2cs^2 - 12w_4^3v_2^2w_6w_3 - 24w_4^2v_2^2w_6w_3^2cs^2 - 24w_4^2v_2^2w_6w_3^2 + 36w_4^3w_6w_3^2cs^2 + 24w_4v_2^2w_6^2w_3^2 + \\ 36w_4^3v_2^2w_6w_3^2 - 12w_4^3w_6^2cs^2 - 30w_4v_2^2w_6^2w_3^3 + 36w_4^3w_6^2w_3cs^2 + 12w_4^2w_6w_3^2cs^2 - 12w_4^3v_2^2w_6w_3^2 - 12w_4w_6^2w_3^2cs^2) \frac{v_3^3}{12w_4^2w_6^2w_3^3} \end{aligned}$$

$$G_{\mathbf{D}_2^0 \mathbf{D}_2^0 \mathbf{D}_2^0 v_1}^{(0), \text{LBBM1}} = (-24\omega_4^2 c s^2 \omega_6^2 w_3 + 12\omega_4^3 v_2^2 w_3^2 - 32\omega_4^3 c s^2 \omega_6^2 w_3^2 - 5\omega_4^3 v_2^2 \omega_6^2 w_3^3 - 12\omega_4^3 c s^2 \omega_3^2 - 6\omega_4^3 v_2^2 w_3^3 + 6\omega_4^3 c s^2 \omega_3^3 + 16\omega_4^3 v_2^2 \omega_6^2 w_3^2 + 4\omega_4^3 c s^2 \omega_6^2 w_3^3 - 6\omega_4^3 v_2^2 \omega_6^2 w_3 - 12\omega_4^3 c s^2 \omega_6^2 - 12\omega_4^2 c s^2 \omega_6^2 w_3^2 + 36\omega_4^2 c s^2 \omega_6^2 w_3^3 + 24\omega_4^2 v_2^2 \omega_6^2 w_3^3 + 48\omega_4^2 c s^2 \omega_6^2 w_3^2 - 12\omega_4^3 c s^2 \omega_6 w_3 + 12v_2^2 \omega_6^2 w_3^3 - 12\omega_4^2 v_2^2 \omega_6 w_3^3 - 24\omega_4^2 c s^2 \omega_6 w_3^2 + 12\omega_4^3 v_2^2 \omega_6 w_3 + 12\omega_4^2 c s^2 \omega_6 w_3^3 + 24\omega_4^2 v_2^2 \omega_6 w_3^2 + 24\omega_4 v_2^2 \omega_6 w_3^3 + 6\omega_4 c s^2 \omega_6 w_3^3 - 36\omega_4^3 v_2^2 \omega_6 w_3^2 - 12\omega_4^3 c s^2 \omega_6 w_3^3 - 12\omega_4 c s^2 \omega_6^2 w_3^2 - 30\omega_4 v_2^2 \omega_6^2 w_3^3 + 36\omega_4^3 c s^2 \omega_6 w_3^2 + 12\omega_4^3 v_2^2 \omega_6 w_3^3) \frac{v_3}{12\omega_4^3 \omega_6^2 w_3^3}$$

$$C_{\substack{D_x D_y D_z v_1}}^{(0), CLBM2} = (-12\omega_4^3 \omega_6 \omega_3 c s^2 + 12\omega_4^3 v_2^2 \omega_3^2 - 12\omega_4^2 \omega_6^2 \omega_3^2 c s^2 - 5\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 - 6\omega_4^3 v_2^2 \omega_3^3 - 32\omega_4^3 \omega_6^2 \omega_3^2 c s^2 + 16\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 48\omega_4^2 \omega_6^2 \omega_3^2 c s^2 - 12\omega_4^3 \omega_6^2 c s^2 - 36\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 24\omega_4^2 v_2^2 \omega_6^2 \omega_3^3 + 4\omega_4^3 \omega_6^2 \omega_3^2 c s^2 + 6\omega_4 v_2^2 \omega_6^3 c s^2 + 12v_2^2 \omega_6^2 \omega_3^3 - 24\omega_4^2 \omega_6 \omega_3^2 c s^2 + 6\omega_4^3 \omega_6^3 c s^2 + 12\omega_4^3 v_2^2 \omega_6 \omega_3 + 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_3^3 \omega_6 \omega_3^2 c s^2 + 24\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3 c s^2 + 12\omega_4^2 \omega_6 \omega_3^2 c s^2 - 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 30\omega_4 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_4^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_4^3 \omega_6^2 \omega_3^2 c s^2) \frac{\rho v_3}{12\omega_4^3 \omega_6^2 \omega_3^3}$$

coefficient  $C_{D_x D_y^2 D_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{\mathrm{D}_x \mathrm{D}_y^2 \mathrm{D}_z v_2}^{(0), \mathrm{SRT}} = (132 - 198\omega - 5\omega^3 + 76\omega^2) \frac{v_1 v_2 \rho v_3}{6\omega^3}$$

$$C_{\substack{\text{D}_x \text{D}_y^2 \text{D}_z v_2}}^{(0), \text{MRT1}} = (6w_4 w_3^2 w_3^2 + 24w_4^3 w_2^2 w_3^3 - 36w_4^3 w_3^2 w_3 + 12w_3^2 w_3^3 - 30w_4^3 w_2^2 w_3^2 - 30w_4 w_3^2 w_3^3 - 5w_4^3 w_3^2 w_3^3 + 18w_4^3 w_2^2 w_3 + 18w_4^2 w_2 w_3^3 + 12w_4^3 w_2^3 + 18w_4 w_2^3 w_3^2 + 28w_4^3 w_3^2 w_3^2 + 12w_4^3 w_3^3 + 12w_4^2 w_2^2 w_3^2 + 18w_4^2 w_2^3 w_3 - 42w_4^2 w_2^2 w_3^3 + 6w_4^3 w_2 w_3^2 - 30w_4^2 w_2^3 w_3^2 + 24w_4^2 w_2^3 w_3^3 - 30w_4^3 w_2 w_3^3) \frac{v_1 v_2 \rho v_3}{6w_3^2 w_4^3 w_3^3}$$

$$C_{\text{D}_x \text{D}_y^2 \text{D}_z v_2}^{(0), \text{MRT2}} = C_{\text{D}_x \text{D}_y^2 \text{D}_z v_2}^{(0), \text{MRT1}}$$

$$C_{\mathrm{D}_x \mathrm{D}_y^2 \mathrm{D}_z v_2}^{(0), \text{CLBM1}} = C_{\mathrm{D}_x \mathrm{D}_y^2 \mathrm{D}_z v_2}^{(0), \text{MRT1}}$$

$$C_{\mathrm{D}_x \mathrm{D}_y^2 \mathrm{D}_z v_2}^{(0), \text{CLBM2}} = C_{\mathrm{D}_x \mathrm{D}_y^2 \mathrm{D}_z v_2}^{(0), \text{MRT1}}$$

coefficient  $C_{D_x D_y^2 D_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{\substack{D_x D_y D_z v_3}}^{(0), \text{SRT}} = (-56\omega^2 cs^2 + 52\omega^2 v_2^2 - 5\omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 + 84v_2^2 + 144\omega cs^2 - 126\omega v_2^2) \frac{v_1 \rho}{12w^3}$$

$$\begin{aligned} C_{\substack{\text{D}_x \text{D}_y \\ \text{D}_z \text{D}_w}}^{(0), \text{MRT1}} = & (-12w_3^2 w_6 w_3 c s^2 + 48 w_2^2 v_2^2 w_6^2 w_3 + 40 w_3^2 v_2^2 w_6^2 w_3^2 - 12 w_2^2 w_6^2 w_3^2 c s^2 - 12 w_3^2 v_2^2 w_3^2 - 32 w_3^2 w_6^2 w_3^2 c s^2 + 6 w_3^2 v_2^2 w_3^3 - 5 w_3^2 v_2^2 w_6^2 w_3^3 + \\ & 48 w_2^2 w_6^2 w_3^2 c s^2 + 48 w_3^2 v_2^2 w_6^2 + 24 w_2^2 v_2^2 w_6^2 w_3^3 - 90 w_3^2 v_2^2 w_6^2 w_3 + 4 w_3^2 w_6^2 w_3^2 c s^2 - 60 w_2^2 v_2^2 w_6^2 w_3^2 - 12 w_3^2 w_6^2 c s^2 - 12 w_2^2 v_2^2 w_6 w_3 + 6 w_2^2 w_6^2 w_3^2 c s^2 - \\ & 24 w_2^2 w_6^2 w_3^2 c s^2 + 12 v_2^2 w_6^2 w_3 + 6 w_2^3 w_3^2 c s^2 - 24 w_2^2 v_2^2 w_6 w_3^2 - 24 w_2^2 w_6^2 w_3 c s^2 + 12 w_2^2 v_2^2 w_6 w_3^3 - 12 w_2^3 w_6^2 w_3^2 c s^2 - 30 w_2 v_2^2 w_6^2 w_3^3 - 12 w_3^2 w_3^2 c s^2 + \\ & 36 w_2^3 w_6^2 w_3 c s^2 + 12 w_2^2 w_6 w_3^2 c s^2 - 12 w_3^2 v_2^2 w_6 w_3^2 - 12 w_2 w_6^2 w_3^2 c s^2 + 24 w_2 v_2^2 w_6^2 w_3^3 + 36 w_2^3 w_6 w_3^2 c s^2 + 36 w_3^2 v_2^2 w_6 w_3^2) \frac{v_1^1 \rho^2}{12 w_3^2 w_6^2 w_3^3} \end{aligned}$$

$$\begin{aligned} C_{\substack{\text{D}_x \text{D}_y \\ \text{D}_z \text{D}_w}}^{(0), \text{MRT2}} = & (48 w_2^2 v_2^2 w_2^2 w_3 + 40 w_3^2 v_2^2 w_2^2 w_3^2 - 24 c s^2 w_2^2 w_6 w_3^2 + 6 c s^2 w_2 w_6^2 w_3^3 + 6 c s^2 w_3^2 w_6^3 - 12 w_3^2 v_2^2 w_2^2 w_3^3 + 36 c s^2 w_3^2 w_6^2 w_3 + 6 w_3^2 v_2^2 w_3^3 - 12 c s^2 w_3^2 w_6^3 - 12 c s^2 w_2 w_6^2 w_3^2 - 5 w_3^2 s_2^2 w_2^2 w_3^3 + 12 c s^2 w_2^2 w_6 w_3^3 - 32 c s^2 w_3^2 w_6^2 w_3^2 + 48 w_3^2 v_2^2 w_6^2 + 24 w_2^2 s_2^2 w_6^2 w_3^3 - 90 w_3^2 v_2^2 w_6^2 w_3 - 12 c s^2 w_2^3 w_6^2 + 4 c s^2 w_3^2 w_6^2 w_3^3 - 60 w_2^2 s_2^2 w_6^2 w_3^2 - 12 w_3^2 v_2^2 w_6 w_3 - 24 c s^2 w_2^2 w_6^2 w_3^3 - 12 c s^2 w_3^2 w_6 w_3^2 + 12 v_2^2 w_6^2 w_3^3 - 24 w_2^2 s_2^2 w_6 w_3^2 + 36 c s^2 w_3^2 w_6^2 w_3^2 + 12 w_2^2 v_2^2 w_6 w_3^3 - 30 w_2 v_2^2 w_6^2 w_3^3 - 12 c s^2 w_3^2 w_6 w_3 - 12 c s^2 w_2^2 w_6^2 w_3^3 - 12 w_2^3 v_2^2 w_6 w_3^3 + 24 w_2 v_2^2 w_6^2 w_3^2 + 48 c s^2 w_2^2 w_6^2 w_3^3 + 36 w_3^2 v_2^2 w_6 w_3^2) \frac{v_1 \rho}{12 w_3^2 w_6^2 w_3^3} \end{aligned}$$

$$C_{\substack{D_x D_y D_z v_3}}^{(0), \text{CLBM1}} = (-12w_3^2 c s^2 w_3^2 + 16w_3^2 v_2^2 w_6^2 w_3^2 + 4w_3^2 c s^2 w_6^2 w_3^3 + 12w_3^2 v_2^2 w_3^2 + 6w_3^2 c s^2 w_3^3 - 24w_3^2 c s^2 w_6^2 w_3 - 6w_3^2 v_2^2 w_3^3 - 32w_3^2 c s^2 w_6^2 w_3^2 - 5w_3^2 v_2^2 w_6^2 w_3^3 + 36w_3^2 c s^2 w_6^2 w_3 + 24w_2^2 v_2^2 w_6^2 w_3^3 - 12w_3^2 c s^2 w_6^2 + 48w_2^2 c s^2 w_6^2 w_3^2 - 6w_3^2 v_2^2 w_6^2 w_3 - 12w_2^2 c s^2 w_6^2 w_3^3 - 36w_2^2 v_2^2 w_6^2 w_3^2 + 12w_2^2 w_6^2 w_3^3 + 12w_2^2 c s^2 w_6 w_3^3 + 24w_2^2 v_2^2 w_6 w_3^2 - 12w_2^3 c s^2 w_6 w_3 - 12w_2^2 v_2^2 w_6 w_3^3 - 24w_2^2 c s^2 w_6 w_3^2 - 12w_2 c s^2 w_6^2 w_3^3 - 30w_2 v_2^2 w_6^2 w_3^3 + 36w_2^3 c s^2 w_6 w_3^2 + 12w_2^2 v_2^2 w_6 w_3^3 + 24w_2 v_2^2 w_6^2 w_3^2 + 6w_2 c s^2 w_6^2 w_3^3 - 36w_2^2 v_2^2 w_6 w_3^2 - 12w_2^2 c s^2 w_6 w_3^3) \frac{v_1 \rho}{12w_2^3 v_2^2 w_6^2 w_3^3}$$

$$C_{\text{D}_x \text{D}_y \text{D}_z v_3}^{(0), \text{CLBM2}} = (-32w_3^2 w_6^2 w_3^2 c s^2 + 16w_3^2 v_2^2 w_6^2 w_3^2 + 12w_3^2 v_2^2 w_3^2 - 12w_3^2 w_6 w_3 c s^2 - 6w_3^2 v_2^2 w_3^3 - 12w_2^2 w_6^2 w_3^3 c s^2 - 5w_2^2 v_2^2 w_6^2 w_3^3 + 24w_2^2 v_2^2 w_6^2 w_3^3 + 4w_2^2 w_6^2 w_3^3 c s^2 - 12w_3^2 w_6^2 c s^2 + 48w_2^2 w_6^2 w_3^2 c s^2 - 6w_3^2 v_2^2 w_6^2 w_3 - 36w_2^2 v_2^2 w_6^2 w_3^2 + 12w_3^2 v_2^2 w_6 w_3 - 24w_2^2 w_6^2 w_3 c s^2 + 12v_2^2 w_6^2 w_3^3 - 12w_3^2 w_6 w_3^3 c s^2 + 4w_2^2 w_6^2 w_3^3 + 6w_2^2 w_6^2 w_3^3 c s^2 - 24w_2^2 w_6 w_3^2 c s^2 + 6w_2^2 w_6^2 w_3^3 c s^2 - 12w_2^2 v_2^2 w_6 w_3^3 + 36w_2^2 w_6 w_3^2 c s^2 - 30w_2 v_2^2 w_6^2 w_3^3 + 12w_2^2 v_2^2 w_6 w_3^3 + 24w_2 v_2^2 w_6^2 w_3^3 + 36w_2^3 w_6^2 w_3 c s^2 - 12w_2^3 w_6^2 w_3^2 c s^2 - 36w_2^3 v_2^2 w_6 w_3^2 + 12w_2^2 w_6 w_3^3 c s^2 - 12w_2 w_6^2 w_3^3 c s^2) \frac{v_1 \rho}{12w_2^2 w_6^2 w_3^3}$$

**coefficient**  $C_{D_y^3 D_z \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_2^3 \partial x_3}$ :

$$C_{\substack{D^3 D^2 \rho \\ y}}^{(0), \text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_2 v_3}{6\omega^3}$$

$$\begin{aligned} C_{\substack{\text{D}_3^0 \text{D}_2^1 \\ \zeta}}^{(0), \text{MRT1}} = & (6w_4^2 w_6 w_3^2 - 48w_3^3 w_6^2 w_3^2 c s^2 - 12w_4^3 v_2^2 w_3^2 - 24w_4^3 w_6 w_3 c s^2 + 6w_4^3 v_2^2 w_3^3 - 6w_4^3 w_6^2 w_3 - 3w_4^2 w_6 w_3^3 + 12w_4^2 v_2^2 w_6^2 w_3 + 6w_3^3 v_2^2 w_6^2 w_3^2 - \\ & 12w_4^2 w_6^2 w_3^3 c s^2 - 30w_4^3 v_2^2 w_6^2 w_3 + 6w_4^3 w_6^2 w_3^3 c s^2 + 24w_4^3 v_2^2 w_6^2 + 7w_4^3 w_6^2 w_3^2 - 12w_4^2 v_2^2 w_6^2 w_3^2 + 42w_4^2 w_6^2 w_3^2 c s^2 - 36w_4^3 w_6^2 c s^2 + 6w_4^2 v_2^2 w_6^2 w_3^3 - \\ & w_4^3 w_6^2 w_3^3 + 6w_4^3 w_3^3 c s^2 - 24w_4^2 w_6^2 w_3 c s^2 + 6v_2^2 w_6^2 w_3^3 - 3w_3^3 w_3^3 + 6w_4^2 v_2^2 w_6 w_3^3 - 12w_4^3 w_6 w_3 c s^2 + 6w_3^3 w_6 w_3^3 + 6w_4 w_6^2 w_3^2 c s^2 - 24w_4^3 v_2^2 w_6 w_3 - \\ & 12w_4^2 w_6^2 w_3^3 c s^2 - 21w_4^3 w_6 w_3^2 - 12w_4^2 v_2^2 w_6 w_3^2 + 6w_4^3 w_3^2 + 12w_4^3 w_6 w_3 + 42w_4^3 w_6 w_3^2 c s^2 + 6w_4 v_2^2 w_6^2 w_3^2 + w_4^2 w_6^2 w_3^3 + 42w_4^3 v_2^2 w_6 w_3^2 - 12w_4^3 w_3^2 c s^2 - \\ & 3w_4^2 w_6^2 w_3^3 - 12w_4 v_2^2 w_6^2 w_3^3 + 78w_3^3 w_6^2 w_3 c s^2 + 6w_4^2 w_6 w_3^3 c s^2 - 12w_4^3 v_2^2 w_6 w_3^3 - 12w_4 w_6^2 w_3^2 c s^2) \frac{v_2^2 v_3^3}{6w_3^3 w_6^2 w_3^3} \end{aligned}$$

$$C_{\substack{D_3^0 D_2^1 D_2^1 \rho}}^{(0), \text{MRT2}} = (-12w_4^2 c s^2 w_6 w_3^2 + 6w_4^2 w_6 w_3^2 - 36w_4^3 c s^2 w_6^2 - 12w_4^3 v_2^2 w_3^2 - 24w_4^3 c s^2 w_6 w_3 + 6w_4^3 v_2^2 w_3^3 - 6w_4^3 w_6^2 w_3 - 3w_4^2 w_6 w_3^3 + 12w_4^2 v_2^2 w_6^2 w_3 + 6w_4^2 c s^2 w_6 w_3^3 + 6w_4^2 v_3^2 w_6^2 w_3^2 - 30w_4^3 v_2^2 w_6^2 w_3 - 12w_4^3 c s^2 w_6 w_3^3 + 6w_4 c s^2 w_6^2 w_3^3 - 12w_4^3 c s^2 w_3^2 + 24w_4^3 v_2^2 w_6^2 + 7w_4^3 w_6^2 w_3^2 - 12w_4^2 v_2^2 w_6^2 w_3^2 + 42w_4^3 c s^2 w_6 w_3^3 + 6w_4^2 v_2^2 w_6^2 w_3^3 - w_4^3 w_6^2 w_3^2 - 12w_4 c s^2 w_6^2 w_3^3 + 6w_4^3 c s^2 w_3^3 - 48w_4^3 c s^2 w_6^2 w_3^2 + 6v_2^2 w_6^2 w_3^3 - 3w_4^3 w_3^3 + 6w_4^2 v_2^2 w_6 w_3^3 - 24w_4^2 c s^2 w_6^2 w_3 + 6w_4^2 w_6 w_3^3 + 6w_4^3 c s^2 w_6^2 w_3^2 - 24w_4^3 v_2^2 w_6 w_3^2 - 21w_4^3 w_6 w_3^2 - 12w_4^2 v_2^2 w_6 w_3^2 + 6w_4^3 w_3^3 + 12w_4^3 w_6 w_3 + 6w_4 v_2^2 w_6 w_3^2 - 12w_4^2 c s^2 w_6^2 w_3^2 + w_4^2 w_6 w_3^3 + 42w_4^3 v_2^2 w_6 w_3^2 - 3w_4^2 w_6 w_3^2 + 42w_4^3 c s^2 w_6^2 w_3^2 - 12w_4 v_2^2 w_6^2 w_3^2 - 12w_4^3 v_2^2 w_6 w_3^2 + 78w_4^3 c s^2 w_6^2 w_3) \frac{v_2 v_3}{6w_4^4 w_6^2 w_3^3}$$

$$C_{D_3^2 D_3^2}^{(0),\text{CLBM1}} = (6w_4^2 w_6 w_3^2 - 12 w_4^2 c s^2 w_6^2 w_3 + 12 w_4^3 v_2^2 w_3^2 - 36 w_3^3 c s^2 w_6^2 w_3^2 - 36 w_3^3 c s^2 w_3^2 - 6 w_3^4 v_2^2 w_3^3 - 6 w_3^4 w_6^2 w_3 - 3 w_4^2 w_6 w_3^3 + 18 w_4^3 c s^2 w_3^3 - 6 w_4^2 v_2^2 w_6^2 w_3^2 + 6 w_4^3 c s^2 w_6^2 w_3^2 + 12 w_4^3 v_2^2 w_6^2 w_3 - 12 w_4^3 c s^2 w_6^2 - 12 w_4^2 c s^2 w_6^2 w_3^3 + 7 w_3^2 w_6^2 w_3^2 - 6 w_4^2 v_2^2 w_6^2 w_3^2 + 36 w_4^3 c s^2 w_6^2 w_3 + 6 w_4^2 v_2^2 w_6^2 w_3^3 - 3 w_4^3 w_6^2 w_3^2 - 24 w_4^2 c s^2 w_6 w_3 + 6 v_2^2 w_6^2 w_3^3 - 3 w_4^3 w_3^2 - 24 w_4^2 c s^2 w_6 w_3^2 + 6 w_4^3 w_6 w_3^3 - 24 w_4^3 v_2^2 w_6 w_3 - 21 w_4^3 w_6 w_3^2 + 12 w_4^2 c s^2 w_6 w_3^3 + 6 w_4^2 w_3^2 + 12 w_3^3 w_6 w_3 + 6 w_4 v_2^2 w_6^2 w_3^2 + 6 w_4 c s^2 w_6^2 w_3^2 + w_4^2 w_6^2 w_3^3 + 12 w_4^3 v_2^2 w_6 w_3^2 - 24 w_4^3 c s^2 w_6 w_3^3 - 3 w_4^2 w_6^2 w_3^2 - 12 w_4 c s^2 w_6^2 w_3^2 - 12 w_4 v_2^2 w_6^2 w_3^3 + 72 w_4^3 c s^2 w_6 w_3^2) \frac{v_2 v_3}{6 w_4^2 w_6^2 w_3^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(0), \text{CLBM2}} = (6\omega_4^2 \omega_6 \omega_3^2 - 24\omega_4^3 \omega_6 \omega_3 c s^2 + 12\omega_4^3 v_2^2 \omega_3^2 - 12\omega_4^2 \omega_6^2 \omega_3^3 c s^2 - 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^3 \omega_6^2 \omega_3^3 - 3\omega_4^2 \omega_6 \omega_3^3 - 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^2 \omega_6^2 \omega_3^2 c s^2 + 7\omega_4^3 \omega_6^2 \omega_3^2 - 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_4^3 \omega_6^2 \omega_3^3 c s^2 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4^2 \omega_6^2 \omega_3^3 c s^2 + 6v_2^2 \omega_6^2 \omega_3^3 - 24\omega_4^2 \omega_6 \omega_3^2 c s^2 - 3\omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4^3 \omega_6 \omega_3^3 - 12\omega_4^2 \omega_6^2 \omega_3^2 c s^2 + 18\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 24\omega_4^3 \omega_6^2 \omega_6 \omega_3 - 21\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 24\omega_4^3 \omega_6^2 \omega_3^2 c s^2 + 6\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^3 \omega_6 \omega_3 + 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 + \omega_4^2 \omega_6^2 \omega_3^2 + 12\omega_4^2 \omega_6 \omega_3^2 c s^2 + 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_4 \omega_6^2 \omega_3^2 c s^2 - 3\omega_4^2 \omega_6^2 \omega_3^2 + 72\omega_4^3 \omega_6 \omega_3^2 c s^2 - 12\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2) \frac{\rho v_3}{6\omega_4^3 \omega_6^2 \omega_3^3}$$

coefficient  $C_{\text{D}_y^3 \text{D}_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_2^3 \partial x_3}$ :

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(0), \text{SRT}} = (12 - 56\omega^2 c s^2 - 12\omega^2 v_2^2 + 3\omega^3 v_2^2 + 4\omega^3 c s^2 - 96c s^2 - 18\omega - 12v_2^2 - \omega^3 + 8\omega^2 + 144\omega c s^2 + 18\omega v_2^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(0), \text{MRT1}} = (12\omega_4^2 \omega_6 \omega_3^2 - 32\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 12\omega_4^3 v_2^2 \omega_3^2 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 \omega_6 \omega_3^2 c s^2 + 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^2 \omega_6 \omega_3^3 - 12\omega_4^2 \omega_6^2 \omega_3^3 c s^2 - 30\omega_4^3 \omega_6^2 \omega_3^2 + 4\omega_4^2 \omega_6^2 \omega_3^2 c s^2 + 24\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 48\omega_4^2 \omega_6^2 \omega_3^2 c s^2 - 12\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4^3 \omega_6^2 \omega_3^3 c s^2 - 24\omega_4^2 \omega_6^2 \omega_3^2 c s^2 + 12v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 72\omega_4^3 \omega_6 \omega_3^2 c s^2 - 12\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2) \frac{\rho v_3}{6\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(0), \text{MRT2}} = (-24\omega_4^2 c s^2 \omega_6 \omega_3^2 + 12\omega_4^2 \omega_6 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^2 \omega_6 \omega_3^2 + 12\omega_4^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6 \omega_3^2 + 6\omega_4 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 24\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2) \frac{\rho v_3}{12\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(0), \text{CLBM1}} = (12\omega_4^2 \omega_6 \omega_3^2 - 24\omega_4^2 c s^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 32\omega_4^3 c s^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4^2 \omega_6 \omega_3^2 + 6\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - \omega_4^3 \omega_6^2 \omega_3^3 - 12\omega_4 c s^2 \omega_6^2 \omega_3^2 + 48\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_4^3 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2) \frac{\rho v_3}{12\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(0), \text{CLBM2}} = (12\omega_4^2 \omega_6 \omega_3^2 - 12\omega_4^3 \omega_6 \omega_3^2 c s^2 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^2 \omega_6^2 \omega_3^3 c s^2 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 32\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 30\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 24\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4^2 \omega_6^2 \omega_3^2 c s^2 + 48\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_4^3 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6^2 \omega_3^2 c s^2) \frac{\rho v_3}{12\omega_4^3 \omega_6^2 \omega_3^3}$$

coefficient  $C_{\text{D}_y^3 \text{D}_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_2^3 \partial x_3}$ :

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{SRT}} = (36 - 56\omega^2 c s^2 - 20\omega^2 v_2^2 + \omega^3 v_2^2 + 4\omega^3 c s^2 - 96c s^2 - 54\omega - 36v_2^2 - \omega^3 + 20\omega^2 + 144\omega c s^2 + 54\omega v_2^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{MRT1}} = (-12\omega_6 \omega_3^2 c s^2 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - 48\omega_6^2 c s^2 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6^2 \omega_3^2 + 6v_2^2 \omega_6^2 \omega_3^2 - 12\omega_6^2 \omega_3 + 90\omega_6^2 \omega_3 c s^2 + 12\omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^2 - 12\omega_3^2 c s^2 - 44\omega_6^2 \omega_3^2 c s^2 - 8v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 - 36\omega_6 \omega_3 c s^2 + 4\omega_6^2 \omega_3^2 c s^2 + 6\omega_3^3 c s^2 + 9\omega_6 \omega_3^2 - 36\omega_6 \omega_3^2) \frac{\rho v_3}{12\omega_6^2 \omega_3^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{MRT2}} = (-12c s^2 \omega_3^2 - 44c s^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 + 4c s^2 \omega_6^2 \omega_3^2 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 + 6c s^2 \omega_6^2 \omega_3^2 + 48v_2^2 \omega_6^2 \omega_3^2 - 48c s^2 \omega_6^2 \omega_3^2 - 12v_2^2 \omega_6^2 \omega_3^2 + 12\omega_6^2 \omega_3^2 - 12\omega_6^2 \omega_3^2 c s^2 + 90c s^2 \omega_6^2 \omega_3^2 + 12\omega_3^2 - 36c s^2 \omega_6 \omega_3 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^2 - 8v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 + 9\omega_6 \omega_3^2 - 12c s^2 \omega_6 \omega_3^2 - 36\omega_6 \omega_3^2 + 48c s^2 \omega_6 \omega_3^2) \frac{\rho v_3}{12\omega_6^2 \omega_3^3}$$

$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{CLBM1}} =$

$$(-36c s^2 \omega_6 \omega_3 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^2 - 30c s^2 \omega_6 \omega_3^2 - 60c s^2 \omega_6^2 \omega_3^2 + 96c s^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_6^2 \omega_3^2 - 12\omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^2 + 30c s^2 \omega_6^2 \omega_3^2 + 12\omega_3^2 - 26c s^2 \omega_6^2 \omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^2 - 14v_2^2 \omega_6^2 \omega_3^2 + 4c s^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 + 9\omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^2 + 18c s^2 \omega_6 \omega_3^2 - 36\omega_6 \omega_3^2) \frac{\rho v_3}{12\omega_6^2 \omega_3^3}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(0), \text{CLBM2}} = (12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - 30\omega_6 \omega_3^2 c s^2 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^2 + 18\omega_6^2 \omega_3 c s^2 - 6v_2^2 \omega_6^2 \omega_3^2 - 12\omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^2 + 96\omega_6 \omega_3^2 c s^2 + 12\omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^2 - 36\omega_6 \omega_3 c s^2 - 14v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 - 60\omega_6 \omega_3 c s^2 - 26\omega_6^2 \omega_3^2 c s^2 + 9\omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^2 + 4\omega_6^2 \omega_3^2 c s^2 + 30\omega_3^2 c s^2 - 36\omega_6 \omega_3^2) \frac{\rho v_3}{12\omega_6^2 \omega_3^3}$$

coefficient  $C_{\text{D}_t^2 \text{D}_z^2 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t^2 \partial x_3^2}$ :

$$C_{\text{D}_t^2 \text{D}_z^2 v_3}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{3\rho v_3}{2\omega^3}$$

$$C_{\text{D}_t^2 \text{D}_z^2 v_3}^{(0), \text{MRT1}} = (2\omega_4^3 + 8\omega_7 \omega_4^2 - 4\omega_4^2 - 2\omega_7 \omega_4^3 - 4\omega_7 \omega_4 + 2\omega_7^2 - \omega_7^2 \omega_4 - \omega_7^2 \omega_4^2) \frac{\rho v_3}{2\omega_7^2 \omega_4^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\mathbf{D}_t^2 \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}} = (-2 - \omega_4^2 + 3\omega_4) \frac{3\rho v_3}{2\omega_4^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t^2 \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2}$ :

$$C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{SRT}} = (34\omega^2 cs^2 - 2\omega^3 cs^2 + 60cs^2 + \omega^3 v_3^2 - 90\omega cs^2 - 2\omega^2 v_3^2) \frac{\rho}{12\omega^3}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{MRT1}} &= (3\omega_7^2 \omega_4^3 cs^2 + 12\omega_7 \omega_4 \omega_2 cs^2 - 24\omega_7^2 \omega_2 v_3^2 - \omega_7^2 \omega_4^3 v_3^2 + 12\omega_7 \omega_4 \omega_2 v_3^2 + 12\omega_7^2 \omega_2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 22\omega_7^2 \omega_4^2 \omega_2 cs^2 + 12\omega_4^2 \omega_2 cs^2 - \\ &18\omega_7^2 \omega_4^2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 cs^2 - 10\omega_7^2 \omega_4^2 \omega_2 v_3^2 + 12\omega_4^2 \omega_2 v_3^2 + 6\omega_7^2 \omega_4^2 v_3^2 - 30\omega_7^2 \omega_4 \omega_2 cs^2 + 12\omega_7 \omega_4^2 cs^2 - 12\omega_7^2 \omega_4 v_3^2 + 36\omega_7^2 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4^2 v_3^2 + \\ &12\omega_7^2 \omega_4 cs^2 - 6\omega_7 \omega_4^3 cs^2 - 6\omega_7^2 \omega_4 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 - 30\omega_7 \omega_4^2 \omega_2 cs^2 - 6\omega_7 \omega_4^3 v_3^2 - 6\omega_4^2 \omega_2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_2 cs^2 - 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{MRT2}} &= (12\omega_7^2 cs^2 \omega_2 - 24\omega_7^2 \omega_2 v_3^2 + 12\omega_7 \omega_4 \omega_2 cs^2 \omega_2 - \omega_7^2 \omega_4^3 v_3^2 + 12\omega_7 \omega_4 \omega_2 v_3^2 - 18\omega_7^2 \omega_4^2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 9\omega_7 \omega_4^3 cs^2 \omega_2 + 3\omega_7^2 \omega_4^3 cs^2 - \\ &10\omega_7^2 \omega_4^2 \omega_2 v_3^2 + 12\omega_4^2 \omega_2 v_3^2 + 12\omega_4^2 cs^2 \omega_2 + 6\omega_7^2 \omega_4^2 v_3^2 + 22\omega_7^2 \omega_4^2 cs^2 \omega_2 - 12\omega_7^2 \omega_4 v_3^2 - 6\omega_7 \omega_4^3 cs^2 + 36\omega_7^2 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4^2 v_3^2 - 30\omega_7 \omega_4^2 cs^2 \omega_2 - \\ &2\omega_7^2 \omega_4^3 cs^2 \omega_2 - 6\omega_7^2 \omega_4 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 + 12\omega_7 \omega_4 \omega_2 cs^2 - 6\omega_7 \omega_4^3 v_3^2 - 30\omega_7 \omega_4^2 cs^2 \omega_2 + 12\omega_7 \omega_4^2 cs^2 - 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{CLBM1}} &= (-6\omega_7 \omega_4^3 cs^2 - 30\omega_7 \omega_4^2 \omega_2 cs^2 + 24\omega_7^2 \omega_2 v_3^2 - \omega_7^2 \omega_4^3 v_3^2 - 12\omega_7 \omega_4 \omega_2 v_3^2 - 6\omega_4^3 \omega_2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_2 cs^2 - 30\omega_7^2 \omega_4 \omega_2 cs^2 - 9\omega_7 \omega_4^3 \omega_2 v_3^2 + \\ &12\omega_7 \omega_4^2 \omega_2 v_3^2 + 8\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 12\omega_7^2 \omega_4 \omega_2 v_3^2 - 6\omega_7^2 \omega_4^2 v_3^2 + 12\omega_7^2 \omega_4 \omega_2 cs^2 + 22\omega_7^2 \omega_4^2 \omega_2 cs^2 + 12\omega_7^2 \omega_4 v_3^2 - 18\omega_7^2 \omega_4^2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 cs^2 - \\ &36\omega_7^2 \omega_4 \omega_2 v_3^2 - 12\omega_7 \omega_4^2 v_3^2 + 3\omega_7^2 \omega_4^3 \omega_2 cs^2 + 6\omega_4^3 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 + 12\omega_7 \omega_4 \omega_2 cs^2 + 6\omega_7 \omega_4^3 v_3^2 + 12\omega_7^2 \omega_4 \omega_2 cs^2 + 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_1}^{(0), \text{CLBM2}} &= (12\omega_7^2 \omega_2 cs^2 + 24\omega_7^2 \omega_2 v_3^2 + 3\omega_7^2 \omega_4^3 cs^2 - \omega_7^2 \omega_4^3 v_3^2 - 12\omega_7 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4 \omega_2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 cs^2 - 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 8\omega_7^2 \omega_4^2 \omega_2 v_3^2 - \\ &12\omega_4^2 \omega_2 v_3^2 + 22\omega_7^2 \omega_4^2 \omega_2 cs^2 + 12\omega_4^2 \omega_2 cs^2 - 6\omega_7^2 \omega_4^2 v_3^2 - 18\omega_7^2 \omega_4^2 cs^2 + 12\omega_7^2 \omega_4 v_3^2 + 12\omega_7^2 \omega_4 \omega_2 cs^2 - 30\omega_7^2 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4^2 cs^2 - \\ &12\omega_7 \omega_4^2 v_3^2 + 6\omega_4^3 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 - 6\omega_4^3 \omega_2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_2 cs^2 + 6\omega_7 \omega_4^3 v_3^2 - 6\omega_7 \omega_4^3 \omega_2 cs^2 + 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2} \end{aligned}$$

**coefficient**  $C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2}$ :

$$C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 \rho v_3}{6\omega^3}$$

$$\begin{aligned} C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}} &= (12\omega_4^2 \omega_2^2 - 7\omega_7 \omega_4^3 \omega_2^2 - 6\omega_4^2 \omega_2^3 - 6\omega_7 \omega_4^3 - 6\omega_7 \omega_4^2 \omega_2 + \omega_7 \omega_4^3 \omega_2^3 + 12\omega_7 \omega_4^2 \omega_2^2 - 6\omega_4^3 \omega_2^2 + 12\omega_7 \omega_4^3 \omega_2 - 10\omega_7 \omega_4^2 \omega_2^3 - 12\omega_7 \omega_2^3 + \\ &3\omega_4^3 \omega_2^3 + 24\omega_7 \omega_4 \omega_2^3 - 12\omega_7 \omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_7 \omega_4^3 \omega_2^3} \end{aligned}$$

$$C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}} = (6\omega_4^2 \omega_2^2 - 6\omega_4^3 - 7\omega_4^2 \omega_2^3 + 12\omega_4^3 \omega_2 - 12\omega_2^3 - 7\omega_4^2 \omega_2^2 + \omega_4^3 \omega_2^3 - 6\omega_4^2 \omega_2 + 18\omega_4 \omega_2^3) \frac{v_1 \rho v_3}{6\omega_4^3 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t \mathbf{D}_x \mathbf{D}_z^2 v_3}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{\mathbf{D}_x^2 \mathbf{D}_z^2 \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2}$ :

$$C_{\mathbf{D}_x^2 \mathbf{D}_z^2 \rho}^{(0), \text{SRT}} = (-14\omega^2 v_1^2 cs^2 + 56v_1^2 v_3^2 - 84\omega v_1^2 v_3^2 - 24\omega cs^4 + \omega^3 cs^2 v_3^2 + 36\omega cs^2 v_3^2 - 3\omega^3 v_1^2 v_3^2 - 24cs^2 v_3^2 - \omega^3 cs^4 - 14\omega^2 cs^2 v_3^2 + \omega^3 v_1^2 cs^2 + \\ 16cs^4 + 36\omega v_1^2 cs^2 + 10\omega^2 cs^4 - 24v_1^2 cs^2 + 34\omega^2 v_1^2 v_3^2) \frac{1}{4\omega^3}$$

$$\begin{aligned} C_{\mathbf{D}_x^2 \mathbf{D}_z^2 \rho}^{(0), \text{MRT1}} &= (20\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + \omega_7 \omega_4^3 \omega_5^2 \omega_2^2 v_3^2 + 10\omega_7 \omega_4^3 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^4 + 10\omega_7 \omega_4^3 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^2 - 12\omega_7 \omega_4^2 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^4 - 4\omega_4^2 \omega_5 \omega_2^2 v_1^2 \omega_2^3 v_3^2 - 4\omega_7 \omega_4^2 \omega_5 \omega_2^2 v_1^2 \omega_2^2 v_3^2 - \\ &10\omega_7^2 \omega_4^3 \omega_5 v_1^2 \omega_2^2 v_3^2 + 10\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + \omega_7 \omega_4^3 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^4 + \omega_7 \omega_4^3 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^2 + 4\omega_7 \omega_4^2 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^2 - 4\omega_7 \omega_4^2 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^4 - 4\omega_7 \omega_4^2 \omega_5 \omega_2^2 v_3^2 \omega_2 cs^2 + \omega_7 \omega_4^3 \omega_5 \omega_2^2 v_3^2 \omega_2 v_3^2 - \\ &38\omega_7^2 \omega_4 \omega_5 \omega_2^2 v_3^2 \omega_2 v_3^2 - \omega_7 \omega_4^3 \omega_5 \omega_2^2 v_3^2 \omega_2 v_3^2 - 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + \\ &10\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + \\ &10\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 36\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 12\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 38\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + \\ &20\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + \omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 10\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 38\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - \\ &4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 20\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 8\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 8\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - \\ &2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 20\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - \\ &3\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 3\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 + 4\omega_7^2 \omega_4 \omega_5 v_1^2 \omega_2^2 v_3^2 - \end{aligned}$$

$$4w_7^2w_3^3v_2^2v_3^2cs^2 - 2w_7^2w_4w_5^2w_3^2cs^4 - 4w_7^2w_5^2v_2^2w_3^2cs^2 + 2w_3^4w_2^2v_1^2w_3^2v_3^2 - 4w_7^2w_4w_5w_2^2v_3^2cs^2 - 4w_7^2w_3^4v_1^2w_2^2v_3^2 - 3w_7^2w_3^2w_5^2v_1^2w_2^2v_3^2 + \\ 2w_7w_4^2w_5^2v_2^2w_3^2v_3^2 + 4w_7^2w_5^2w_3^2w_2^2cs^4 + 4w_7^2w_4w_5v_1^2w_2^2cs^2 - 2w_7w_4^2w_5^2w_2^2v_3^2cs^2 + w_2^2w_3^4w_5w_3^2cs^4 + w_7^2w_3^4w_5^2v_1^2w_3^2cs^2 + 20w_7^2w_3^4w_5^2v_1^2v_3^2 - \\ 4w_7^2w_4w_5^2w_3^2v_2^2cs^2 + 20w_7^2w_5^2v_1^2w_3^2v_3^2 - 4w_7^2w_3^4w_5v_1^2w_2^2v_3^2 + 2w_3^4w_5^2v_1^2w_3^2cs^2) \frac{1}{4w_7^2w_3^2w_5^2w_3^2}$$

$$\begin{aligned}
C_{D_2^2 D_{2P}}^{(0), \text{MRT2}} = & (20w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 v_3 - 4w_7^2 w_4^3 c s^2 w_5 w_2 v_3^2 + w_7 w_4^3 c s^4 w_5^2 w_3^3 + 4w_7^2 w_4^2 c s^4 w_5^2 w_2 - 4w_7 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 - 4w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - \\
& 4w_7 w_4^2 c s^2 w_5^2 v_2^2 w_3^2 - 4w_7^2 w_4^2 c s^2 w_5^2 w_3 v_3^2 + w_7 w_4^3 c s^2 w_5^2 w_3^2 v_3^2 + 4w_7^2 w_4^3 c s^4 w_5^2 w_2^2 - 8w_7^2 w_4^2 c s^2 w_5^2 v_2^2 w_2 + 10w_7^2 w_4^3 c s^2 w_5^2 v_1^2 w_3^2 - \\
& 4w_7 w_3^3 c s^4 w_5^2 w_2^2 - 8w_7^2 w_4^3 c s^2 w_5^2 w_2^2 v_3^2 - 38w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - w_2^2 w_4^3 c s^4 w_5^2 w_3^2 - 4w_7 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - 4w_7^2 w_4^2 c s^2 w_5 w_2^2 v_3^2 - 8w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_3^2 - \\
& 3w_7^2 w_4^3 c s^2 w_5 v_1^2 w_3^2 v_3^2 + 4w_7 w_4^2 c s^4 w_5^2 w_2^2 - 2w_7 w_4^3 c s^2 w_5^2 w_3^2 v_3^2 - 4w_7^2 c s^2 w_5^2 v_1^2 w_3^2 + w_7 w_4^3 c s^2 w_5^2 v_1^2 w_2^2 - 4w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + 4w_7^2 w_4^2 c s^4 w_5^2 w_3^2 - \\
& 4w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 - 36w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + 2w_7^2 w_4^2 c s^2 w_5 w_3 v_3^2 + 10w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 38w_7 w_3^3 c s^2 w_5^2 v_1^2 w_2^2 v_3^2 - 2w_7^2 w_4^2 c s^4 w_5^2 w_2^2 - 2w_7 w_4^2 c s^4 w_5^2 w_3^2 + \\
& 12w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 + 20w_7 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + 10w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_3^2 + w_7 w_4^3 c s^2 w_5^2 w_3^2 v_3^2 - 12w_7^2 w_4^2 c s^4 w_5^2 w_2^2 - 2w_7^2 w_4^2 c s^2 w_5 w_1^2 w_2^2 + 2w_7^2 w_4^2 v_1^2 w_3^2 v_3^2 + \\
& 20w_7^2 w_4^2 w_5^2 v_2^2 w_3^2 v_3^2 - 2w_7^2 w_4^2 c s^2 w_5^2 w_3^2 v_3^2 + 4w_7 w_4^2 c s^2 w_5^2 w_2^2 v_3^2 + 2w_3^4 c s^2 w_5^2 v_1^2 w_3^2 + 4w_7^2 w_4^2 c s^4 w_5 w_2^2 + 2w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + w_7 w_4^3 c s^2 w_5^2 v_1^2 w_3^2 + \\
& 4w_7^2 w_4^2 c s^2 w_5^2 w_3^2 v_3^2 - 4w_7^2 w_4^2 c s^2 w_5^2 w_3^2 v_3^2 + 4w_7^2 w_4^2 c s^2 w_5 v_2^2 w_2^2 - 4w_2^2 w_4^2 c s^2 w_5^2 w_3^2 v_3^2 - 4w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 - 2w_7^2 w_4^2 c s^4 w_5 w_3^2 + 2w_7^2 w_4^2 c s^2 w_5^2 v_3^2 - \\
& 4w_7^2 c s^2 w_5^2 v_1^2 w_2^2 + 20w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - 3w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 3w_7^2 w_4^2 c s^2 w_5 w_2^2 v_3^2 + 4w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 - 8w_7^2 w_4^2 c s^2 w_5^2 v_2^2 v_3^2 - 4w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - \\
& 2w_7 w_4^2 c s^2 w_5^2 w_3^2 v_3^2 + 10w_7^2 w_4^2 c s^2 w_5^2 w_2^2 v_3^2 - 2w_7 w_4^2 c s^4 w_5^2 w_3^2 + 2w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + 2w_7 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 - 4w_7^2 w_4^2 v_1^2 w_2^2 v_3^2 + w_7 w_4^3 c s^4 w_5 w_3^2 - \\
& 3w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + 10w_7^2 w_4^2 c s^2 w_5 w_2^2 v_3^2 + 2w_7 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 v_3^2 + 4w_7^2 w_4^2 c s^4 w_5^2 w_2^2 - 4w_7^2 w_4^2 c s^2 w_5^2 v_2^2 v_3^2 - 2w_7^2 w_4^2 c s^4 w_5 w_2^2 + 12w_7^2 w_4^2 c s^2 w_5^2 w_2^2 v_3^2 + \\
& 20w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 - 3w_7 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 + 20w_7^2 w_4^2 v_1^2 w_3^2 v_3^2 - 4w_7^2 w_4^2 c s^2 w_5^2 v_1^2 w_2^2 v_3^2) \frac{1}{4w_2^2 w_4^2 w_5^2 w_3^2}
\end{aligned}$$

$$\begin{aligned}
C_{D_2^2 D_2^2 Z_2^2}^{(0), \text{CLBM1}} = & (2w_7 w_3^4 w_2^2 w_2^2 c s^2 v_3^2 + 14 w_7 w_4^2 w_2^2 v_1^2 w_3^2 v_3^2 + 4 w_2^2 w_4^2 w_5 w_2^2 c s^4 - 2 w_7 w_4^2 w_5^2 w_3^2 c s^2 v_3^2 - 2 w_7 w_4 w_5^2 w_3^3 c s^4 + 2 w_7 w_3^4 w_5^2 v_1^2 w_3^2 c s^2 + \\
& 4 w_2^2 w_5^2 v_1^2 w_3^2 v_3^2 - 4 w_2^2 w_5^2 v_2^2 w_3^2 c s^2 - 10 w_7 w_3^4 w_5 v_1^2 w_3^2 v_3^2 - 4 w_7 w_4^2 w_5 w_2^2 c s^2 v_3^2 - 4 w_2^2 w_4^2 w_5 v_2^2 w_3^2 c s^2 + 4 w_2^2 w_4^2 w_5^2 w_2 c s^4 + w_7^2 w_3^4 w_5 w_3^3 c s^4 - \\
& 4 w_2^2 w_3^4 w_5 w_2 c s^2 v_3^2 + w_7^2 w_4^2 w_5 v_1^2 w_3^2 c s^2 - 14 w_7 w_4 w_5^2 v_1^2 w_3^2 v_3^2 + 2 w_3^4 w_5^2 v_1^2 w_3^2 c s^2 + 4 w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 4 w_7^2 w_3^4 w_5^2 w_2 c s^2 v_3^2 - 2 w_7^2 w_3^4 w_5^2 w_2 c s^4 + \\
& 3 w_7 w_3^4 w_5 v_1^2 w_3^2 v_3^2 - 3 w_2^2 w_4^2 w_5 w_3^3 c s^2 v_3^2 + 4 w_7 w_4 w_5^2 v_1^2 w_3^2 v_3^2 + 4 w_7^2 w_4 w_5^2 w_3^2 c s^4 - 3 w_7 w_3^4 w_5^2 v_1^2 w_3^2 c s^2 - 2 w_7 w_3^4 w_5 w_3^3 c s^4 - 28 w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - \\
& 10 w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 14 w_7 w_3^4 w_5^2 v_1^2 w_2 v_3^2 - 8 w_7 w_3^4 w_5^2 w_2 c s^2 v_3^2 - 2 w_2^2 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 - 2 w_7 w_3^4 w_5 w_2 c s^4 + 2 w_7 w_4^2 w_5^2 w_3^3 c s^2 v_3^2 + 12 w_7^2 w_4 w_5^2 v_1^2 w_2 v_3^2 + \\
& 2 w_7^2 w_2^2 w_5 v_1^2 w_3^2 c s^2 - 4 w_7 w_4^2 w_5^2 w_2 c s^2 v_3^2 - 2 w_7 w_3^4 w_5^2 v_1^2 w_3^2 v_3^2 - 4 w_7 w_4 w_5^2 v_1^2 w_2 v_3^2 c s^2 + 14 w_7 w_3^4 w_5^2 v_1^2 w_2 v_3^2 + 2 w_7 w_3^4 w_5^2 w_3^2 c s^2 v_3^2 + 10 w_7 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 + \\
& 4 w_7 w_3^4 w_5^2 w_3^3 c s^4 + 2 w_7^2 w_4^2 w_5 w_3^2 c s^2 v_3^2 - 2 w_7 w_3^4 w_5^2 w_2 c s^2 v_3^2 - 2 w_7^2 w_4^2 w_5 v_1^2 w_3^2 v_3^2 - 4 w_7 w_4^2 w_5^2 w_2 c s^2 v_3^2 - 2 w_7 w_4^2 w_5^2 w_3^2 c s^4 + 4 w_2^2 w_3^4 w_5^2 w_2 c s^4 + \\
& 10 w_7 w_3^4 w_5^2 w_2 c s^2 v_3^2 - w_2^2 w_3^4 w_5 v_1^2 w_3^2 c s^2 + 8 w_2^2 w_4^2 w_5^2 v_1^2 w_2 c s^2 - w_7 w_3^4 w_5^2 w_3^2 c s^2 v_3^2 + 12 w_7^2 w_4^2 w_5^2 v_1^2 w_2 v_3^2 + 3 w_7 w_3^4 w_5^2 v_1^2 w_3^2 v_3^2 + 8 w_7^2 w_4^2 w_5^2 w_3^2 c s^2 v_3^2 - \\
& 4 w_7 w_4 w_5^2 v_1^2 w_3^2 c s^2 + 4 w_7^2 w_4^2 w_5 v_1^2 w_3^2 v_3^2 - 12 w_7^2 w_4^2 w_5^2 w_3^2 c s^4 + w_7 w_4^2 w_5^2 w_3^2 c s^2 + w_7^2 w_3^4 w_5^2 w_3^2 c s^2 v_3^2 - 2 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 4 w_7 w_3^4 w_5^2 v_1^2 w_3^2 c s^2 + \\
& 4 w_7 w_3^4 v_1^2 w_2 v_3^2 + 10 w_7 w_4 w_5^2 v_1^2 w_3^2 c s^2 - 4 w_7 w_4^2 w_5^2 w_2 c s^2 v_3^2 - 3 w_7^2 w_4^2 w_5^2 v_1^2 w_2 v_3^2 - 2 w_7 w_3^4 w_5^2 v_1^2 w_2 v_3^2 - 4 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 - 8 w_7 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 + \\
& 2 w_7 w_3^4 w_5 v_1^2 w_3^2 c s^2 + 4 w_7 w_3^4 w_5^2 v_1^2 v_3^2 + 4 w_7 w_4^2 w_5^2 w_2 c s^4 + 4 w_7 w_5^2 v_1^2 w_3^2 v_3^2 + 4 w_7^2 w_3^4 w_5 v_1^2 w_2 v_3^2 + 10 w_7 w_4^2 w_5 w_2 c s^2 v_3^2 - w_7 w_3^4 w_5^2 w_3^2 c s^4) \frac{1}{4 w_2^2 w_3^4 w_5^2 w_3^2}
\end{aligned}$$

$$\begin{aligned}
C_{D_x^2 D_y^2}^{(0), \text{CLBM2}} = & (-4w_4^2 w_5^2 v_2^2 w_3^2 c s^2 + 14w_7^2 w_4^2 w_5^2 v_2^2 w_3^2 v_3^2 + w_7^2 w_4^2 w_5^2 w_3^2 v_2^3 c s^2 - 8w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 - 4w_7 w_4^2 w_5^2 w_2^2 v_3^2 c s^2 + 4w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + \\
& 2w_7^2 w_5^2 v_1^2 w_3^2 c s^2 + 4w_7 w_4^2 w_5^2 w_3^2 c s^4 - w_7^2 w_3^2 w_5^2 w_3^2 c s^4 - 10w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + 10w_7^2 w_3^2 w_5^2 w_2^2 v_2^2 c s^2 - 12w_7^2 w_4^2 w_5^2 w_2^2 c s^4 + w_7 w_3^2 w_5^2 w_3^2 c s^4 - \\
& 14w_7^2 w_4^2 w_5^2 v_2^2 w_3^2 v_3^2 - 4w_7 w_4^2 w_5^2 v_1^2 w_2^2 c s^2 + 4w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + 10w_7^2 w_4^2 w_5^2 v_2^2 w_3^2 c s^2 - 2w_7 w_4^2 w_5^2 w_3^2 c s^4 + 2w_7^2 w_4^2 w_5 w_3^2 v_2^2 c s^2 + 4w_7^2 w_4^2 w_5^2 w_3^2 c s^4 + \\
& 3w_7^2 w_3^2 w_5 v_1^2 w_3^2 v_3^2 - w_7^2 w_3^2 w_5 v_1^2 w_3^2 c s^2 + 8w_7^2 w_3^2 w_5 v_1^2 w_3^2 c s^2 + 4w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + 2w_7^2 w_3^2 w_5^2 v_2^2 c s^2 - 4w_7 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 - 28w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - \\
& 4w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 c s^2 - 10w_7 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - 14w_7^2 w_4^2 w_5^2 v_2^2 w_2^2 v_3^2 - w_7 w_3^2 w_5^2 v_1^2 w_3^2 c s^2 + 8w_7^2 w_4^2 w_5^2 v_2^2 v_3^2 c s^2 + 10w_7 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 + 12w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + \\
& 4w_7^2 w_4^2 w_5^2 w_3^2 c s^4 - 4w_7^2 w_4^2 w_5^2 v_2^2 c s^2 - 2w_7 w_4^2 w_5^2 w_2^2 v_3^2 c s^2 + 10w_7^2 w_4^2 w_5^2 w_2^2 v_2^2 c s^2 - 2w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 + 14w_7^2 w_4^2 w_5^2 v_2^2 w_2^2 v_3^2 - 2w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 c s^2 - \\
& 2w_7^2 w_4^2 w_5^2 w_3^2 c s^4 + 2w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 - 2w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 3w_7^2 w_4^2 w_5^2 w_3^2 v_2^2 c s^2 - 2w_7^2 w_4^2 w_5^2 w_2^2 c s^4 - 4w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 c s^2 - 8w_7^2 w_4^2 w_5^2 w_2^2 v_3^2 c s^2 + \\
& 4w_7^2 w_4^2 w_5^2 w_3^2 c s^4 - 3w_7 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 + 2w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 c s^2 + 12w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + 3w_7 w_4^2 w_5^2 v_1^2 w_3^2 v_3^2 - 2w_7^2 w_4^2 w_5^2 w_3^2 c s^4 + 4w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - \\
& 4w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 + 4w_7^2 w_4^2 w_5^2 w_2^2 c s^4 + w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 c s^4 + w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 c s^4 - 2w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 + 2w_7 w_4^2 w_5^2 w_2^2 v_3^2 c s^2 + 2w_7^2 w_4^2 v_1^2 w_3^2 c s^2 + \\
& 4w_7^2 w_3^2 v_1^2 w_2^2 v_3^2 - 2w_7 w_4^2 w_5^2 w_3^2 v_2^2 c s^2 - 3w_7^2 w_3^2 w_5^2 v_1^2 w_3^2 v_3^2 - 2w_7 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2 - 4w_7^2 w_4^2 w_5^2 w_3^2 v_2^2 c s^2 + 4w_7^2 w_4^2 w_5^2 w_2^2 c s^4 - 2w_7^2 w_4^2 w_5^2 w_3^2 c s^4 + \\
& 2w_7 w_4^2 w_5^2 v_1^2 w_2^2 c s^2 - 4w_7^2 w_4^2 w_5^2 v_2^2 c s^2 - 4w_7^2 w_4^2 w_5 w_2^2 v_3^2 c s^2 - 4w_7^2 w_4^2 w_5^2 v_1^2 w_3^2 c s^2 + 4w_7^2 w_4^2 w_5^2 v_1^2 v_3^2 + 4w_7^2 w_4^2 w_5^2 v_1^2 w_2^2 v_3^2) \frac{1}{4w_2^2 w_4^2 w_5^2 w_3^2}
\end{aligned}$$

**coefficient**  $C_{D_x^2 D_z^2 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2}$ :

$$C_{\frac{D^2_x}{D^2_z}v_1}^{(0),\text{SRT}} = (-26\omega^2 cs^2 - 126\omega v_3^2 + \omega^3 cs^2 - 48cs^2 + 84v_3^2 - 4\omega^3 v_3^2 + 72\omega cs^2 + 50\omega^2 v_3^2) \frac{\frac{v_1 \rho}{12w^3}}{12w^3}$$

$$\begin{aligned} C^{(0),\text{MRTT}}_x &= \\ & (-78w_7^2w_4w_3^3v_3^2 - 6w_7^2w_4^3w_2^2cs^2 + 12w_7^2w_3^4v_3^2 + 22w_7^2w_3^3w_2^2v_3^2 + 24w_7^2w_4w_3^3cs^2 + 24w_7w_4^2w_3^2v_3^2 + 6w_3^3w_4^3cs^2 + w_7^2w_4^3w_3^2cs^2 - 12w_7^2w_4^2w_2cs^2 + 24w_7^2w_4w_3^2v_3^2 + 24w_7^2w_4^2w_2v_3^2 + 24w_7w_7^2w_3^2cs^2 + 6w_4^3w_3^2v_3^2 - 4w_7^2w_3^3w_2^2v_3^2 - 48w_7^2w_2^2w_3^2v_3^2 - 12w_7w_4w_3^2v_3^2 - 12w_7^2w_3^2cs^2 - 12w_7w_4w_3^2cs^2 + 48w_7^2w_3^3v_3^2 + 12w_7^2w_4^2w_2^2cs^2 - 30w_7^2w_4^3w_2v_3^2 + 34w_7^2w_4^2w_3^2v_3^2 - 12w_4^2w_3^3v_3^2 - 6w_7w_4^3w_3^2cs^2 - 14w_7^2w_4^2w_3^2cs^2 - 12w_7^2w_3^2cs^2 - 6w_7w_4^3w_3^2v_3^2 + 6w_7^2w_4^3w_2cs^2) \frac{v_1\rho}{12w_7^2w_4^3w_3^2} \end{aligned}$$

$$\begin{aligned} C_{\frac{D^2}{D_x^2}v_1}^{(0,1), \text{MRI}} &= \\ (12\omega_7^2\omega_2^2c^2s^2\omega_2^2 - 6\omega_7\omega_4^3c^2s^2\omega_3^2 - 78\omega_2^2\omega_4\omega_3^2v_2^2 - 14\omega_7^2\omega_4^2c^2s^2\omega_3^2 - 12\omega_4^2cs^2\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 22\omega_7^2\omega_3^2\omega_2^2v_3^2 + 24\omega_7\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4\omega_3^2v_3^2 - 12\omega_7^2cs^2\omega_3^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 4\omega_7^2\omega_4^3\omega_2^2v_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7\omega_4cs^2\omega_2^2 - 48\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4\omega_2^3v_3^2 + 6\omega_4^3cs^2\omega_2^2 + \omega_7^2\omega_3^2cs^2\omega_3^2 + 48\omega_7^2\omega_3^2v_3^2 + 24\omega_7\omega_4^2cs^2\omega_3^2 - 6\omega_7^2\omega_3^2cs^2\omega_2^2 + 6\omega_7^2\omega_4^3cs^2\omega_2^2 - 30\omega_7^2\omega_4^2\omega_2^2v_3^2 + 34\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4cs^2\omega_3^2 - 6\omega_7\omega_4^3\omega_3^2v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^2\omega_3^2} \end{aligned}$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_1}^{G^{\alpha\beta} G^{\gamma\delta} G^{\mu\nu}} = & (-18w_7^2 w_4 w_2 v_3^2 - 6w_7 w_4^3 w_2^3 c s^2 + 12w_7^2 w_4 v_3^2 - 14w_7^2 w_4^2 w_3^2 c s^2 + 22w_7^2 w_4^2 w_2 v_3^2 - 12w_4^2 w_3^2 c s^2 + 6w_7^2 w_4^3 w_2 c s^2 - 24w_7 w_4^2 w_3^2 v_3 - 12w_7^2 w_2^2 c s^2 + 24w_7^2 w_4 w_2 v_3^2 - 12w_7 w_4 w_2^3 c s^2 + 24w_7^2 w_4^2 w_2 v_3^2 - 6w_4^2 w_3^2 v_3^2 - 4w_7^2 w_4^3 w_3^2 v_3^2 + 12w_7^2 w_4^2 w_2^2 c s^2 + 6w_4^2 w_3^2 c s^2 + w_7^2 w_4^3 w_3^2 c s^2 - 48w_7^2 w_4^2 w_2^2 v_3^2 - \end{aligned}$$

$$12\omega_7^2\omega_4^2\omega_2cs^2 + 12\omega_7\omega_4\omega_2^3v_3^2 + 24\omega_7\omega_4^2\omega_2^3cs^2 - 30\omega_7^2\omega_4^3\omega_2v_3^2 + 22\omega_7^2\omega_4^2\omega_2^3v_3^2 - 6\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_4^2\omega_3^3v_3^2 + 6\omega_7\omega_4^3\omega_2^3v_3^2 + 24\omega_7^2\omega_4\omega_2^3cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x^2 D_z^2 v_1}^{(0), CLBM2} = (-18\omega_7^2\omega_4\omega_2^3v_3^2 + 24\omega_7\omega_4\omega_2^3cs^2 + 12\omega_7^2\omega_4^3v_3^2 + 22\omega_7^2\omega_4^3\omega_2^2v_3^2 - 6\omega_7^2\omega_4^3\omega_2^2cs^2 - 24\omega_7\omega_4^2\omega_2^3v_3^2 + 24\omega_7\omega_4^2\omega_2^3cs^2 + 24\omega_7^2\omega_4\omega_2^2v_3^2 + 6\omega_7^3\omega_2^3cs^2 + \omega_7^2\omega_4^3\omega_2^3cs^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 6\omega_4^3\omega_3^3v_3^2 - 4\omega_7^2\omega_4^3\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_2^3cs^2 - 48\omega_7^2\omega_4^2\omega_2^2v_3^2 + 12\omega_7\omega_4\omega_2^3v_3^2 + 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 30\omega_7^2\omega_4^3\omega_2^2v_3^2 - 14\omega_7^2\omega_4^2\omega_2^3cs^2 - 12\omega_4^2\omega_3^3v_3^2 + 22\omega_7^2\omega_4^2\omega_2^2v_3^2 + 12\omega_4^2\omega_3^3v_3^2 + 6\omega_7\omega_4^3\omega_2^3v_3^2 - 6\omega_7\omega_4^3\omega_2^3cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^3}$$

**coefficient**  $C_{D_x^2 D_z^2 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2}$ :

$$C_{D_x^2 D_z^2 v_3}^{(0), SRT} = (-26\omega^2 cs^2 + 50\omega^2 v_1^2 + 84v_1^2 + \omega^3 cs^2 - 4\omega^3 v_1^2 - 48cs^2 - 126\omega v_1^2 + 72\omega cs^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), MRT1} = (34\omega_4^3\omega_5^2v_1^2\omega_2^2 + 6\omega_4\omega_5^2\omega_3^2cs^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 - 12\omega_4^3\omega_2^2cs^2 - 6\omega_4^3\omega_5\omega_3^2cs^2 - 4\omega_4^3\omega_5^2v_1^2\omega_2^3 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 22\omega_4^2\omega_5^2v_1^2\omega_2^3 + 6\omega_4^3\omega_3^2cs^2 + 24\omega_4^3\omega_5^2\omega_2^2v_2^2 - 78\omega_4^3\omega_5^2v_1^2\omega_2^2 + 24\omega_4^3\omega_5\omega_2^2cs^2 - 6\omega_4^2\omega_5^2\omega_2^2cs^2 + 6\omega_4^3v_1^2\omega_2^3 - 12\omega_4^3\omega_5\omega_2^2cs^2 - 12\omega_4^3v_1^2\omega_2^2 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 + 12\omega_5^3v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2 + 24\omega_4^3\omega_5v_1^2\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2^2cs^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 6\omega_4^3\omega_5v_1^2\omega_2^3 + \omega_4^3\omega_5^2\omega_2^2cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^2}$$

$C_{D_x^2 D_z^2 v_3}^{(0), MRT2} =$

$$(34\omega_4^3\omega_5^2v_1^2\omega_2^2 - 6\omega_4^2cs^2\omega_5^2\omega_2^3 + 24\omega_4^2\omega_5^2v_1^2\omega_2 + 24\omega_4^3cs^2\omega_5^2\omega_2 - 4\omega_4^3\omega_5^2v_1^2\omega_2^3 + 12\omega_4^2cs^2\omega_5^2\omega_2^2 + 22\omega_4^2\omega_5^2v_1^2\omega_2^3 - 14\omega_4^3cs^2\omega_5^2\omega_2^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 78\omega_4^3\omega_5^2v_1^2\omega_2 + \omega_3^3cs^2\omega_5^2\omega_2^3 + 6\omega_4cs^2\omega_5^2\omega_2^3 - 12\omega_4^3cs^2\omega_5^2\omega_2^3 + 6\omega_4^3cs^2\omega_5^2\omega_2^3 - 12\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_4^3v_1^2\omega_2^2 + 24\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5\omega_2^2cs^2 - 12\omega_4^3v_1^2\omega_2^2 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 + 12\omega_4^3v_1^2\omega_2^2 + 12\omega_4^2\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2 - 12\omega_4^3cs^2\omega_5\omega_2 + 24\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 6\omega_4^3\omega_5v_1^2\omega_2^3 + \omega_4^3\omega_5^2\omega_2^2cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^2}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), CLBM1} = (22\omega_4^3\omega_5^2v_1^2\omega_2^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 + 12\omega_4^2\omega_5^2\omega_2^2cs^2 + \omega_4^3\omega_5^2\omega_2^3cs^2 - 4\omega_4^3\omega_5^2v_1^2\omega_2^3 + 22\omega_4^2\omega_5^2v_1^2\omega_2^3 - 6\omega_4^2\omega_5^2\omega_2^3cs^2 - 12\omega_4^3\omega_5\omega_2^2cs^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 18\omega_4^3\omega_5^2v_1^2\omega_2 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 + 6\omega_4^3\omega_5^2\omega_2^3 - 6\omega_4^3v_1^2\omega_2^3 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 24\omega_4^3\omega_5^2\omega_2^2cs^2 - 12\omega_4^3\omega_5^2\omega_2^3 - 12\omega_4^3v_1^2\omega_2^2 + 12\omega_4^3\omega_5\omega_2^2cs^2 - 24\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5^2\omega_2^2cs^2 + 6\omega_4^3\omega_5v_1^2\omega_2^3 - 6\omega_4^3\omega_5\omega_2^3cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^2}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), CLBM2} = (22\omega_4^3\omega_5^2v_1^2\omega_2^2 - 6\omega_4^3\omega_5\omega_3^2cs^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 - 4\omega_4^3\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_2^2cs^2 + 6\omega_4\omega_5^2\omega_3^2cs^2 + 22\omega_4^2\omega_5^2v_1^2\omega_2^3 + 24\omega_4^3\omega_5\omega_2^2cs^2 + 6\omega_4^3\omega_2^3v_1^2\omega_2^2 - 18\omega_4\omega_5^2\omega_2^2cs^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 18\omega_4^3\omega_5^2v_1^2\omega_2^2 + 24\omega_4^3\omega_5^2\omega_2^2cs^2 - 12\omega_4^3\omega_5^2\omega_2^3 - 6\omega_4^3v_1^2\omega_2^3 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 - 6\omega_4^2\omega_5^2\omega_2^3cs^2 + 12\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^3\omega_5\omega_2^2cs^2 + 12\omega_4^3\omega_5v_1^2\omega_2^2 + 48\omega_4^3\omega_5^2v_1^2 - 12\omega_4^3cs^2\omega_5\omega_2 + 24\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 6\omega_4^3\omega_5v_1^2\omega_2^3 + \omega_4^3\omega_5^2\omega_2^2cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^2}$$

**coefficient**  $C_{D_t D_y D_z^2 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2}$ :

$$C_{D_t D_y D_z^2 v_2}^{(0), SRT} = (34\omega^2 cs^2 - 2\omega^3 cs^2 + 60cs^2 + \omega^3 v_3^2 - 90\omega cs^2 - 2\omega^2 v_3^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), MRT1} = (3\omega_7^2\omega_4^3cs^2 - 30\omega_7\omega_4^2\omega_3cs^2 - 6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - \omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^2\omega_3v_3^2 - 6\omega_4^3\omega_3cs^2 - 2\omega_7^2\omega_4^3\omega_3cs^2 - 30\omega_7^2\omega_4\omega_3cs^2 - 18\omega_7^2\omega_4^2cs^2 + 36\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_7^2\omega_4^2v_3^2 + 22\omega_7^2\omega_4\omega_3cs^2 + 12\omega_7^2\omega_4\omega_3v_3^2 + 9\omega_7\omega_4^3\omega_3v_3^2 + 12\omega_7\omega_4^2\omega_3v_3^2 - 12\omega_7^2\omega_4v_3^2 + 9\omega_7\omega_4^3\omega_3cs^2 + 12\omega_7\omega_4\omega_3cs^2 - 24\omega_7^2\omega_4v_3^2 - 12\omega_7\omega_4\omega_3cs^2 - 24\omega_7^2\omega_3v_3^2 - 6\omega_7\omega_4^3v_3^2 + 12\omega_7\omega_4\omega_3v_3^2 + 12\omega_7\omega_4\omega_3cs^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3\omega_3v_3^2}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), MRT2} = (-30\omega_7\omega_4^2cs^2\omega_3 - 6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_4^3cs^2\omega_3 - 2\omega_7^2\omega_4^2cs^2\omega_3 - \omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^2\omega_3v_3^2 - 18\omega_7^2\omega_4^2cs^2 - 30\omega_7^2\omega_4\omega_3cs^2 + 3\omega_7^2\omega_4^3cs^2 + 36\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_7^2\omega_4^2v_3^2 + 9\omega_7\omega_4^3\omega_3v_3^2 - 12\omega_7^2\omega_4v_3^2 + 22\omega_7^2\omega_4^2cs^2\omega_3 + 12\omega_7^2\omega_4^2cs^2v_3^2 - 10\omega_7^2\omega_4^2\omega_3v_3^2 + 12\omega_7^2\omega_4\omega_3v_3^2 - 6\omega_7\omega_4^3\omega_3cs^2 + 12\omega_7\omega_4\omega_3cs^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3\omega_3v_3^2}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), CLBM1} = (-6\omega_7\omega_4^3cs^2 - 30\omega_7^2\omega_4\omega_3cs^2\omega_3 + 6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - \omega_7^2\omega_4^3v_3^2 + 30\omega_7\omega_4^2\omega_3v_3^2 - 30\omega_7\omega_4^2\omega_3v_3^2 + 12\omega_7\omega_4^2\omega_3cs^2 - 6\omega_4^3cs^2\omega_3 - 36\omega_7^2\omega_4\omega_3v_3^2 - 2\omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_7^2\omega_4^2v_3^2 + 12\omega_7\omega_4\omega_3cs^2 + 9\omega_7\omega_4^3\omega_3v_3^2 - 12\omega_7\omega_4\omega_3v_3^2 + 22\omega_7\omega_4\omega_3cs^2\omega_3 + 12\omega_7^2\omega_4^2cs^2\omega_3 + 24\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_7\omega_4^3v_3^2 - 12\omega_7\omega_4\omega_3v_3^2 + 9\omega_7\omega_4^3\omega_3cs^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3\omega_3v_3^2}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), CLBM2} = (6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_4^3\omega_3cs^2 - 2\omega_7^2\omega_4^3\omega_3cs^2 + 3\omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^2\omega_3cs^2 + 30\omega_7\omega_4^2\omega_3v_3^2 - 30\omega_7\omega_4^2\omega_3cs^2 + 36\omega_7^2\omega_4\omega_3v_3^2 - 6\omega_7^2\omega_4^2v_3^2 - 18\omega_7^2\omega_4^2cs^2 + 9\omega_7\omega_4^3\omega_3cs^2 - 9\omega_7\omega_4^3\omega_3v_3^2 + 12\omega_7\omega_4^2\omega_3v_3^2 - 18\omega_7^2\omega_4^2\omega_3v_3^2 + 8\omega_7^2\omega_4^2\omega_3v_3^2 - 12\omega_7\omega_4^2\omega_3v_3^2 + 12\omega_7\omega_4^2\omega_3cs^2 + 12\omega_7\omega_4^2\omega_3v_3^2 - 12\omega_7\omega_4^2\omega_3cs^2 + 12\omega_7\omega_4^2\omega_3v_3^2 + 6\omega_7\omega_4^3\omega_3v_3^2 + 9\omega_7\omega_4^3\omega_3cs^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3\omega_3v_3^2}$$

**coefficient**  $C_{D_t D_y D_z^2 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2}$ :

$$C_{D_t D_y D_z^2 v_3}^{(0), SRT} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{\rho v_3}{6\omega^3}$$

$$C_{D_t D_y D_z^2 v_3}^{(0), MRT1} = (-6\omega_7\omega_4^3 - 12\omega_7\omega_4\omega_3^2 + 24\omega_7\omega_4\omega_3^3 + 12\omega_7\omega_4^3\omega_3 - 10\omega_7\omega_4^2\omega_3^2 + 3\omega_4^3\omega_3^3 - 12\omega_7\omega_4^3 - 12\omega_7\omega_4\omega_3^2 - 6\omega_4^3\omega_3^2 - 6\omega_7\omega_4^2\omega_3 +$$

$$\omega_7\omega_4^3\omega_3^3 + 12\omega_4^2\omega_3^2 - 7\omega_7\omega_4^3\omega_3^2) \frac{v_2\rho v_3}{6\omega_7\omega_4^3\omega_3^3}$$

$$C_{\mathrm{D}_t \mathrm{D}_y \mathrm{D}_z^2 v_3}^{(0), \text{MRT2}} = C_{\mathrm{D}_t \mathrm{D}_y \mathrm{D}_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{\text{D}_t \text{D}_y \text{D}_z^2 v_3}^{(0), \text{CLBIM1}} = (-6\omega_4^3 + 18\omega_4\omega_3^3 + \omega_4^3\omega_3^3 - 6\omega_4^2\omega_3 - 12\omega_3^3 - 7\omega_4^3\omega_3^2 - 7\omega_4^2\omega_3^3 + 12\omega_4^3\omega_3 + 6\omega_4^2\omega_3^2) \frac{\nu_2 \rho \nu_3}{6\omega_4^3 \omega_3^3}$$

$$C_{\mathrm{D}_t \mathrm{D}_y \mathrm{D}_z^2 v_3}^{(0), \text{CLBM2}} = C_{\mathrm{D}_t \mathrm{D}_y \mathrm{D}_z^2 v_3}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_x D_y D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2}$ :

$$C_{D_x D_y D_z^2 \rho}^{(0),\text{SRT}} = (-12\omega^2 cs^2 - 60\omega v_3^2 + \omega^3 cs^2 - 20cs^2 + 40v_3^2 - 2\omega^3 v_3^2 + 30\omega cs^2 + 24\omega^2 v_3^2) \frac{v_1 v_2}{\omega^3}$$

$$\begin{aligned}
C_{D_X D_Y D_Z}^{(0), \text{MRT1}} = & (w_7^2 w_3^3 w_2^3 w_3^3 c s^2 + w_3^4 w_2^3 w_3^3 c s^2 - 2 w_7 w_4^2 w_2^3 w_3^3 c s^2 + 3 w_7^2 w_4^3 w_2 w_3^2 v_3^2 - 2 w_7^2 w_4^2 w_2 w_3^3 c s^2 - 2 w_7 w_3^3 w_2^3 w_3^3 v_3^2 - 12 w_7^2 w_2^3 w_3^2 w_3^2 v_3^2 + \\
& 3 w_2^2 w_3^2 w_2^3 w_3 v_3^2 - 2 w_7^2 w_3^2 w_2^3 w_3^3 v_3^2 + w_3^4 w_2^3 w_3^3 v_3^2 - 2 w_7 w_4^2 w_2^3 w_3^2 v_3^2 - 2 w_7 w_4^3 w_2^3 w_3^3 c s^2 + 6 w_7^2 w_4^2 w_2^3 w_3^2 c s^2 + 4 w_7^2 w_4^2 w_2^3 v_3^2 + w_7 w_4^3 w_2^3 w_3^2 v_3^2 - \\
& 2 w_4^2 w_3^2 w_2^3 v_3^2 - 2 w_7^2 w_4 w_5^2 w_2^3 c s^2 + 12 w_2^2 w_4^2 w_2^3 w_3^3 v_3^2 - 8 w_2^2 w_4^3 w_2 w_3^2 v_3^2 - 2 w_7^2 w_3^2 w_2^3 w_3^2 c s^2 + 6 w_7 w_4^2 w_2^3 w_3^3 c s^2 + w_7 w_4^3 w_2^3 w_3^2 c s^2 - 2 w_4^2 w_3^2 w_3^3 c s^2 + \\
& 7 w_7 w_4 w_2^3 w_3^3 v_3^2 - 6 w_7^2 w_4^2 w_2^3 w_3^3 c s^2 + 3 w_2^2 w_4^3 w_2^3 v_3^2 + 7 w_7 w_3^2 w_2^3 w_3^2 v_3^2 + 6 w_7 w_2^2 w_2^3 w_3^3 v_3^2 + w_7^2 w_4^3 w_2 w_3^3 c s^2 - 2 w_7 w_2^2 w_2^3 w_3^2 c s^2 + w_7 w_4^3 w_2^3 w_3^3 c s^2 + \\
& 7 w_7 w_4 w_2^3 w_3^3 v_3^2 - 2 w_7 w_3^2 w_2^3 c s^2 - 8 w_7^2 w_4^2 w_2^3 w_3 v_3^2 + 7 w_7 w_4^2 w_2^3 w_3^2 v_3^2 + 4 w_7 w_2^2 w_2^3 w_3^2 v_3^2 + 3 w_7^2 w_4^3 w_2^3 v_3^2 + w_7 w_4^3 w_2^3 w_3^2 v_3^2 - 2 w_2^2 w_4 w_5^2 w_2^3 c s^2 - \\
& 2 w_7^2 w_3^2 w_2^3 w_3^3 c s^2 + 10 w_2^2 w_3^2 w_3^3 v_3^2 + w_7^2 w_3^2 w_2^3 w_3 c s^2 - 2 w_7 w_4^2 w_2^3 w_3^2 v_3^2 - 8 w_7^2 w_4^3 w_2^3 w_3^2 v_3^2 - 2 w_7 w_4 w_5^2 w_2^3 c s^2 - 2 w_7^2 w_2^3 w_3^2 w_3 c s^2 + 6 w_7 w_4^2 w_2^3 w_3^3 c s^2 - \\
& 21 w_7 w_4 w_2^3 w_3^3 v_3^2 - 2 w_7 w_4^2 w_2^3 w_3^3 c s^2 + w_7^2 w_4^3 w_2^3 w_3^2 c s^2 - 2 w_7 w_4 w_5^2 w_2^3 v_3^2 - 12 w_7^2 w_4^2 w_2^3 w_3^3 v_3^2 + 6 w_7 w_4^3 w_2^3 w_3^2 c s^2 + 4 w_7^2 w_4^2 w_3^2 w_3 v_3^2) \frac{v_1 v_2}{w_2^2 w_4^3 w_2^3 w_3^3}
\end{aligned}$$

$$C^{(0), \text{MRT2}}_{\bar{\rho} D_2^0} = (3w_7^2 w_3^3 w_2 w_3^2 v_3^2 - 2w_7^2 c s^2 w_3^2 w_3^3 - 2w_7 w_3^4 w_2^3 w_3^3 v_3^2 - 12w_7^2 w_4^2 w_3^2 w_3^2 v_3^2 + 3w_7^2 w_4^3 w_2^2 w_3 v_3^2 - 2w_7^2 w_4 c s^2 w_2^2 w_3^3 - 2w_7^2 w_4^3 w_2^3 w_3^2 v_3^2 + w_4^3 w_2^3 w_3^3 v_3^2 - 2w_7 w_4^2 w_3^2 w_3^2 v_3^2 + w_7 w_4^3 w_2^3 w_3^2 v_3^2 - 2w_4^2 w_2^3 w_3^2 v_3^2 + 12w_7^2 w_4^2 w_3^2 w_3^2 v_3^2 - 2w_7 w_4 c s^2 w_2^2 w_3^3 - 2w_7^2 w_4 c s^2 w_3^2 w_3^2 - 8w_7^2 w_3^2 w_2 w_3^2 v_3^2 - 2w_7^2 w_4^2 c s^2 w_2 w_3^3 + 7w_7^2 w_4 w_2^2 w_3^2 v_3^2 + 3w_7^2 w_4^3 w_2^3 v_3^2 + 7w_7^2 w_4^3 w_3^2 w_3^2 v_3^2 + 6w_7 w_4^2 w_3^2 w_3^2 v_3^2 + 6w_7^2 w_4 c s^2 w_2^2 w_3^3 + 7w_7^2 w_4 w_2^2 w_3^2 v_3^2 + w_7^2 w_3^4 c s^2 w_3^2 w_3^3 + w_4^3 c s^2 w_3^2 w_3^3 - 2w_7 w_4^2 c s^2 w_2^2 w_3^3 - 2w_7^2 w_4 c s^2 w_2^2 w_3^3 - 8w_7^2 w_4^3 w_3^2 w_3^2 v_3^2 + w_7 w_4^3 c s^2 w_3^2 w_3^3 + 7w_7^2 w_4^2 w_2^3 w_3^2 v_3^2 - 2w_7 w_4^3 c s^2 w_3^2 w_3^3 + 4w_7^2 w_3^2 w_2^2 w_3^2 v_3^2 + 3w_7^2 w_4^3 w_3^2 v_3^2 + w_7 w_4^3 w_2^3 w_3^2 v_3^2 - 2w_7^2 w_4 c s^2 w_3^2 w_3^3 - 2w_7 w_4^3 c s^2 w_3^2 w_3^3 + 10w_7^2 w_3^2 w_3^2 v_3^2 + 6w_7^2 w_4^2 c s^2 w_2^2 w_3^3 - 2w_7 w_4^2 w_2^3 w_3^2 v_3^2 - 8w_7^2 w_4^3 w_2^2 w_3^2 v_3^2 + 6w_7^2 w_4 c s^2 w_3^2 w_3^3 - 2w_7^2 w_3^2 c s^2 w_2^2 w_3^3 + 6w_7^2 w_4^2 c s^2 w_3^2 w_3^3 + w_7 w_4^3 c s^2 w_3^2 w_3^3 - 21w_7^2 w_4 w_2^3 w_3^2 v_3^2 + w_7 w_4^4 c s^2 w_2^2 w_3^3 - 2w_4^2 c s^2 w_3^2 w_3^3 - 6w_7^2 w_4 c s^2 w_3^2 w_3^3 - 2w_7 w_4 w_2^3 w_3^2 v_3^2 - 12w_7^2 w_4^2 w_2^2 w_3^2 v_3^2 - 2w_7 w_4^2 c s^2 w_3^2 w_3^3 + 4w_7^2 w_4^3 w_2^3 w_3^2 v_3^2 + w_7 w_4^3 c s^2 w_2^2 w_3^3) \frac{v_1 v_2}{w_7^2 w_3^2 w_2^2 w_3^3}$$

$$\begin{aligned} C_{\text{D}_1 \text{D}_2 \text{D}_3}^{(0), \text{CLBM1}} = & (-2w_2^2 w_3^4 w_2^3 c s^2 w_3^3 + 3w_7^2 w_3^4 w_2^3 v_3^2 + 2w_7 w_3^4 w_2^3 v_3^2 - 10w_7^2 w_4^2 w_3^2 w_3^2 v_3^2 - 2w_7^2 w_3^2 c s^2 w_3^3 + 3w_7^2 w_3^4 w_2^3 w_3 v_3^2 + w_7 w_3^2 w_2^3 c s^2 w_3^2 - \\ & 2w_2^2 w_3^2 w_2^3 v_3^2 - w_3^4 w_3^2 w_3^3 v_3^2 + 2w_7 w_2^4 w_3^2 w_2^3 v_3^2 + w_7 w_3^2 w_2^3 c s^2 w_3^3 + 4w_2^2 w_2^4 w_2 w_3^2 v_3^2 - w_7 w_3^2 w_3^2 w_3^2 v_3^2 + 2w_4^2 w_3^2 w_3^2 v_3^2 + 8w_2^2 w_4^2 w_3^2 w_3^2 v_3^2 - \\ & 2w_7 w_2^2 w_3^2 c s^2 w_3^2 + 6w_7^2 w_3^2 w_2^3 c s^2 w_3^3 - 8w_7^2 w_3^4 w_2 w_3^2 v_3^2 - 2w_7 w_4^2 w_2^3 c s^2 w_3^3 + 6w_7^2 w_4^2 w_2^3 c s^2 w_3^2 - 2w_7 w_4 w_3^2 c s^2 w_3^2 + 3w_7^2 w_4 w_2^2 w_3^2 v_3^2 + 3w_7^2 w_3^4 w_2^3 w_3^2 v_3^2 + \\ & 7w_7 w_3^2 w_3^3 w_2^3 v_3^2 - 2w_7 w_4 w_3^2 c s^2 w_3^3 - 6w_7 w_4^2 w_3^2 w_3^3 v_3^2 - 2w_7 w_2^2 w_3^2 c s^2 w_3 - 2w_7 w_4^2 w_3^2 c s^2 w_3^3 + 3w_7^2 w_4 w_3^2 w_3^2 v_3^2 - 8w_7^2 w_4^2 w_3^2 w_3^2 v_3^2 - 2w_2^2 w_4^2 w_3^2 c s^2 w_3^2 + \\ & 7w_7 w_4^2 w_3^2 w_3^3 v_3^2 - 2w_7 w_2^2 w_3^2 c s^2 w_3^3 + 4w_7 w_4^2 w_3^2 w_3^2 v_3^2 + 3w_7^2 w_4^2 w_3^2 v_3^2 + w_7 w_3^4 w_3^2 c s^2 w_3^2 - w_7 w_4^2 w_3^2 w_3^3 + w_2^2 w_3^4 w_3^2 c s^2 w_3^3 + w_4^2 w_3^2 c s^2 w_3^2 + \\ & 2w_7^2 w_3^2 w_3^3 v_3^2 + 2w_7 w_4^2 w_3^2 w_3^3 v_3^2 - 2w_7 w_4^2 w_3^2 c s^2 w_3^2 - 8w_7^2 w_4^2 w_2 w_3^2 v_3^2 + w_7^2 w_3^4 w_3^2 c s^2 w_3^2 - 2w_4^2 w_3^2 c s^2 w_3^3 - 7w_7^2 w_4 w_3^2 w_3^2 v_3^2 - 6w_7^2 w_4^2 w_3^2 c s^2 w_3^2 + \\ & 6w_7 w_4^2 w_3^2 c s^2 w_3^3 + w_7 w_4^2 w_3^2 c s^2 w_3^2 + 2w_7 w_4 w_3^2 w_3^3 v_3^2 - 2w_7^2 w_4^2 w_3^2 c s^2 w_3^3 + 10w_7^2 w_4^2 w_2 w_3^2 w_3^2 v_3^2 + 6w_7^2 w_4^2 w_3^2 c s^2 w_3^2 + 4w_7^2 w_4^2 w_3^2 w_3 v_3^2) \frac{v_1 v_2}{w_2^2 w_3^4 w_2^3 w_3^2} \end{aligned}$$

$$\begin{aligned} C_{\text{D}_2 \text{D}_2 \text{D}_2}^{(0), \text{CLBM2}} = & (3w_7^2 w_4^3 w_2 w_2^2 v_3^2 + 6w_7^2 w_4^2 w_3^2 w_3^2 c s^2 - 2w_7 w_4^3 w_2^3 w_3^2 c s^2 + 2w_7 w_4^3 w_3^2 w_3^2 v_3^2 - 10w_7^2 w_4^2 w_3^2 v_3^2 - 2w_7 w_4^2 w_3^2 w_3^2 c s^2 + w_4^3 w_2^3 w_3^2 c s^2 + \\ & 3w_2^2 w_3^2 w_2^3 w_3 v_3^2 + w_7^2 w_4^3 w_2^3 w_3^2 c s^2 - 2w_2^2 w_4^3 w_3^2 w_3^2 v_3^2 - w_3^2 w_4^3 w_3^2 v_3^2 + 2w_7 w_4^2 w_3^2 w_2^3 v_3^2 - 2w_7^2 w_4^2 w_2 w_3^2 c s^2 + 4w_7^2 w_4^2 w_2 w_3^2 v_3^2 - w_7 w_4^3 w_3^2 v_3^2 + \\ & 2w_4^2 w_3^2 w_2^3 v_3^2 + 8w_7^2 w_4^2 w_3^2 w_3^2 v_3^2 - 6w_2^2 w_3^2 w_2^3 w_3^2 c s^2 - 2w_4^2 w_3^2 w_3^2 c s^2 + w_7 w_4^3 w_3^2 w_2^3 c s^2 - 8w_7^2 w_4^2 w_3^2 w_3^2 v_3^2 + w_7^2 w_4^3 w_3^2 w_3^2 c s^2 - 2w_7^2 w_4^2 w_2^3 w_3^2 c s^2 + \\ & 3w_7^2 w_4 w_2^3 w_3^2 v_3^2 + 3w_7^2 w_4^3 w_3^2 v_3^2 + 7w_2^2 w_4^3 w_3^2 w_3^2 v_3^2 - 6w_7 w_4^2 w_3^2 w_3^2 v_3^2 + 6w_7 w_4^2 w_3^2 w_3^2 c s^2 - 2w_7 w_4^3 w_3^2 w_3^2 c s^2 + 3w_7^2 w_4 w_3^2 w_3^2 v_3^2 - 2w_7^2 w_4 w_3^2 w_3^2 c s^2 - \\ & 2w_7 w_4^3 w_2^3 w_3^2 c s^2 - 8w_2^2 w_4^3 w_3^2 w_3^2 v_3^2 + w_7^2 w_4^3 w_3^2 w_3^2 c s^2 + 7w_7 w_4^2 w_3^2 w_3^2 v_3^2 + w_7 w_4^3 w_2^3 w_3^2 c s^2 - 2w_7^2 w_4^2 w_3^2 w_3^2 c s^2 + 4w_7^2 w_4^2 w_2^3 w_3^2 v_3^2 + 3w_7^2 w_4^3 w_3^2 w_3^2 v_3^2 - \\ & w_7 w_4^3 w_2^3 w_3^2 v_3^2 - 2w_7^2 w_3^2 w_3^2 c s^2 + 2w_7^2 w_3^2 w_3^2 v_3^2 + 2w_7 w_4^2 w_3^2 w_3^2 v_3^2 - 8w_7^2 w_4^3 w_2^3 w_3^2 v_3^2 + w_7^2 w_4^3 w_2^3 w_3^2 c s^2 - 2w_7 w_4^2 w_2^3 w_3^2 c s^2 + 6w_7^2 w_4 w_2^3 w_3^2 c s^2 - \\ & 7w_7^2 w_4 w_2^3 w_3^2 v_3^2 - 2w_7 w_4^3 w_3^2 w_3^2 c s^2 + 2w_7 w_4^2 w_3^2 w_3^2 v_3^2 - 10w_7 w_4^2 w_2^3 w_3^2 v_3^2 - 2w_7^2 w_4^2 w_3^2 w_3^2 c s^2 + 4w_7^2 w_4^2 w_2^3 w_3^2 v_3^2 + 6w_7^2 w_4^3 w_2^3 w_3^2 c s^2) \frac{v_1 v_2}{w_2^2 w_4^3 w_3^2 w_3^2} \end{aligned}$$

**coefficient**  $C_{D_x D_y D_z^2 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2}$ :

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{SRT}} = (-56\omega^2 cs^2 - 126\omega v_3^2 + 4\omega^3 cs^2 - 96cs^2 + 84v_3^2 - 5\omega^3 v_3^2 + 144\omega cs^2 + 52\omega^2 v_3^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{\substack{\text{D}_x^2 \text{D}_y^2 \text{D}_z^2 v_1}}^{(0), \text{MRT1}} = (-30w_2^2 w_3^4 w_3 v_3^2 - 12w_7 w_3^4 w_3^3 c s^2 + 40w_2^2 w_2^4 w_3^2 v_3^2 - 12w_2^4 w_3^3 v_3^2 + 12w_7^2 w_3^2 v_3^2 - 12w_7 w_3^4 w_3^3 v_3^2 - 32w_2^2 w_2^4 w_3^3 c s^2 - 12w_2^4 w_3^3 c s^2 + 6w_2^2 w_3^4 w_3 c s^2 + 12w_7 w_3^4 w_3^2 c s^2 - 60w_2^2 w_2^4 w_3^2 v_3^2 - 12w_7 w_4 w_3^3 v_3^2 - 12w_2^2 w_3^3 c s^2 - 12w_7 w_4 w_3^3 c s^2 + 48w_2^2 w_3^4 w_3^2 v_3^2 + 12w_7 w_3^4 w_3^2 v_3^2 + 48w_2^2 w_4^2 w_3^2 c s^2 + 6w_4^2 w_3^4 w_3^2 c s^2 + 4w_7 w_4^2 w_3^3 c s^2 + 36w_7 w_2^4 w_3^3 v_3^2 - 12w_7 w_4 w_3^3 c s^2 + 48w_2^2 w_4 w_3^2 v_3^2 + 24w_2^2 w_4^2 w_3 v_3^2 - 24w_2^2 w_4 w_3^2 c s^2 + 6w_3^4 w_3^3 v_3^2 - 5w_7 w_4^2 w_3^3 v_3^2 + 36w_7 w_4^2 w_3^3 c s^2 - 90w_7 w_4 w_3^3 v_3^2 - 12w_7^2 w_4^2 w_3^2 c s^2 - 24w_7 w_2^4 w_3^2 v_3^2 + 24w_7^2 w_4^2 w_3^2 v_3^2 - 24w_7 w_4^2 w_3^2 c s^2 + 36w_7 w_4 w_3^3 c s^2)^{\frac{v_2 \rho}{12w_2^2 w_3^4 w_3^3}}$$

$$\begin{aligned} C_{\text{D}_2\text{D}_3\text{D}_2^2\text{v}_1}^{(0), \text{MRT2}} = & (36\omega_7^2 w_4 c s^2 w_3 - 30\omega_7^2 w_3^3 w_3 v_3^2 + 40\omega_7^2 w_2^4 w_3^3 v_3^2 - 12\omega_7^2 w_3^3 v_3^2 + 6\omega_7^2 w_3^4 c s^2 w_3 - 24\omega_7^2 w_4 c s^2 w_3^2 + 12\omega_7^2 w_4^3 v_3^2 - \\ & 12\omega_7 w_3^4 w_3 v_3^2 - 60\omega_7^2 w_4^2 w_3^2 v_3^2 - 12\omega_7 w_4 w_3^3 v_3^2 - 12\omega_7^2 w_3^4 c s^2 w_3^2 + 36\omega_7 w_2^2 c s^2 w_3^2 + 48\omega_7^2 w_3^3 v_3^2 + 12\omega_7 w_3^2 w_3^2 v_3^2 + 4\omega_7^2 w_3^4 c s^2 w_3^3 + 6\omega_7^2 c s^2 w_3^3 - 24\omega_7 w_4^2 c s^2 w_3^2 + \\ & 12\omega_7^2 w_3^2 w_3^2 v_3^2 - 12\omega_7^2 w_3^4 c s^2 w_3^2 v_3^2 + 36\omega_7 w_2^2 c s^2 w_3^2 v_3^2 - 48\omega_7^2 w_3^3 v_3^2 + 12\omega_7 w_3^2 w_3^2 v_3^2 + 4\omega_7^2 w_3^4 c s^2 w_3^3 v_3^2 - 6\omega_7^2 c s^2 w_3^3 v_3^2 + 24\omega_7 w_4^2 c s^2 w_3^2 v_3^2 - 12\omega_7^2 w_3^2 w_3^2 v_3^2 v_3^2) \end{aligned}$$

$$36\omega_7\omega_4^2\omega_3^3v_3^2 + 48\omega_7^2\omega_4\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3 - 12\omega_7\omega_4cs^2\omega_3^2 + 24\omega_7^2\omega_4^2\omega_3v_3^2 + 6\omega_7^3\omega_4^3v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2cs^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 12\omega_4^2cs^2\omega_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^2 - 90\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_3^2v_3^2 - 12\omega_7\omega_4^2cs^2\omega_3^2 + 48\omega_7^2\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBIM1}} = (-30\omega_7^2\omega_4^3\omega_3v_3^2 + 16\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2\omega_4^3cs^2\omega_3^2 + 12\omega_4^2\omega_3^2v_3^2 + 36\omega_7\omega_4^2cs^2\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^2 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 - 36\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 36\omega_7^2\omega_4cs^2\omega_3^2 - 24\omega_7^2\omega_4^2cs^2\omega_3^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 - 36\omega_7\omega_4^3\omega_3^2v_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2 - 6\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 + 48\omega_7^2\omega_4^2\omega_3^2v_3^2 + 4\omega_7^2\omega_4^3\omega_3^2cs^2 - 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2\omega_3cs^2 - 6\omega_7^2\omega_4\omega_3^3v_3^2 - 12\omega_7\omega_4^2\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_3^2v_3^2 + 36\omega_7^2\omega_4^3\omega_3^2v_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2cs^2\omega_3^2) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBIM2}} = (-32\omega_7^2\omega_4^2\omega_3^3cs^2 - 12\omega_4^2\omega_3^3v_3^2 - 30\omega_7^2\omega_4^3\omega_3v_3^2 + 6\omega_7^2\omega_4^3\omega_3cs^2 + 16\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_4^2\omega_3^2v_3^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 - 36\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 48\omega_7^2\omega_4^2\omega_3^2cs^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 - 36\omega_7\omega_4^3\omega_3^2v_3^2 - 24\omega_7^2\omega_4\omega_3^3v_3^2 + 36\omega_7\omega_4^3\omega_3^2v_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2 + 6\omega_4^3\omega_3^2cs^2 + 4\omega_7^2\omega_4^3\omega_3^2cs^2 - 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2\omega_3cs^2 - 6\omega_7^2\omega_4\omega_3^3v_3^2 - 12\omega_7\omega_4^2\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_3^2v_3^2 + 36\omega_7^2\omega_4^3\omega_3^2v_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2cs^2\omega_3^2) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

coefficient  $C_{D_x D_y D_z^2 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2}$ :

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{SRT}} = (-56\omega^2 cs^2 - 126\omega v_3^2 + 4\omega^3 cs^2 - 96cs^2 + 84v_3^2 - 5\omega^3 v_3^2 + 144\omega cs^2 + 52\omega^2 v_3^2) \frac{v_1\rho}{12\omega^3}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}} = (-90\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_7^2\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 24\omega_7^2\omega_4^3\omega_2^2v_3^2 + 36\omega_7^2\omega_4\omega_3^3cs^2 + 36\omega_7\omega_4^2\omega_3^2v_3^2 + 6\omega_4^3\omega_3^2cs^2 + 4\omega_7^2\omega_4^3\omega_2^3cs^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 + 48\omega_7^2\omega_4\omega_2^2v_3^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 + 36\omega_7^2\omega_4^2\omega_2^3v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 60\omega_7^2\omega_4^2\omega_2^3v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 - 12\omega_7^2\omega_3^2v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 48\omega_7^2\omega_4^2\omega_2^2v_3^2 + 12\omega_7\omega_4^2\omega_2^2v_3^2 - 30\omega_7^2\omega_4^3\omega_2v_3^2 + 40\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 32\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT2}} = (48\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7\omega_4^3\omega_2^3v_3^2 - 90\omega_7^2\omega_4\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_2^2v_3^2 - 32\omega_7^2\omega_4^2\omega_2^3v_3^2 + 12\omega_7\omega_4^3\omega_2^2cs^2 - 12\omega_4^2cs^2\omega_2^3 + 12\omega_7\omega_4^3\omega_2^3v_3^2 + 24\omega_7^2\omega_4^2\omega_2^3v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 + 36\omega_7\omega_4^2\omega_2^3v_3^2 + 48\omega_7^2\omega_4\omega_2^2v_3^2 - 12\omega_7^2cs^2\omega_2^3 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 60\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_2^3v_3^2 + 4\omega_7^2\omega_4^3\omega_3^2v_3^2 + 48\omega_7^2\omega_4^2\omega_2^3v_3^2 + 12\omega_7\omega_4^2\omega_2^3v_3^2 + 36\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBIM1}} = (-6\omega_7^2\omega_4\omega_3^3v_3^2 + 24\omega_7\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4^3\omega_2^3v_3^2 + 12\omega_7^2\omega_4^2\omega_2^3cs^2 + 32\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_4^2\omega_2^3cs^2 + 6\omega_7^2\omega_4^3\omega_2cs^2 + 12\omega_7\omega_4^2\omega_2^3v_3^2 - 36\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 24\omega_7^2\omega_4^2\omega_2^3v_3^2 - 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 + 48\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 36\omega_7^2\omega_4^2\omega_2^3v_3^2 - 36\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 36\omega_7^2\omega_4^2\omega_2^3v_3^2 + 36\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 + 16\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 + 16\omega_7^2\omega_4^2\omega_2^3v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBIM2}} = (-6\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_3^2v_3^2 + 24\omega_7\omega_4^2\omega_2^2v_3^2 + 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 - 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 + 48\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 36\omega_7^2\omega_4^2\omega_2^2v_3^2 + 36\omega_7^2\omega_4^2\omega_2^2v_3^2 + 12\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 - 36\omega_7^2\omega_4^2\omega_2^2v_3^2 + 36\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4^2\omega_2^2v_3^2 - 36\omega_7^2\omega_4^2\omega_2^2v_3^2 + 36\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4^2\omega_2^2v_3^2 + 16\omega_7^2\omega_4^2\omega_2^2v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

coefficient  $C_{D_x D_y D_z^2 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2}$ :

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{SRT}} = (132 - 198\omega - 5\omega^3 + 76\omega^2) \frac{v_1 v_2 \rho v_3}{6\omega^3}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}} = (18\omega_4\omega_2^3\omega_3^2 + 24\omega_4^3\omega_2^2\omega_3^3 - 30\omega_4^3\omega_2^3\omega_3 + 12\omega_3^3\omega_2^3 - 42\omega_4^3\omega_2^2\omega_3^2 - 36\omega_4\omega_2^3\omega_3^2 - 5\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4^3\omega_2^2\omega_3 + 6\omega_4^2\omega_2\omega_3^3 + 12\omega_4^3\omega_2^3\omega_3^2 + 12\omega_4^2\omega_2^2\omega_3^2 + 6\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4^2\omega_2\omega_3^2 - 30\omega_4^2\omega_2^2\omega_3^2 + 18\omega_4^3\omega_2\omega_3^2 + 28\omega_4^2\omega_2^3\omega_3^2 - 30\omega_4^3\omega_2\omega_3^2) \frac{v_1 v_2 \rho v_3}{6\omega_4^3\omega_2^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{CLBIM1}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{CLBIM2}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

coefficient  $C_{D_y^2 D_z^2 \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2}$ :

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{SRT}} = (-3\omega^3 v_2^2 v_3^2 - 24\omega cs^4 + \omega^3 cs^2 v_3^2 + 36\omega cs^2 v_3^2 + 56v_2^2 v_3^2 - 24cs^2 v_2^2 - 14\omega^2 cs^2 v_2^2 - 84\omega v_2^2 v_3^2 - 24cs^2 v_2^2 - \omega^3 cs^4 - 14\omega^2 cs^2 v_3^2 +$$

$$36\omega c s^2 v_2^2 + 34\omega^2 v_2^2 v_3^2 + 16c s^4 + 10\omega^2 c s^4 + \omega^3 c s^2 v_2^2) \frac{1}{4\omega^3}$$

$$\begin{aligned}
C_{\substack{(0), \text{MRT1} \\ \text{D}_2^{\text{D}_2} \text{Z}_2}} &= (-2w_7^2 w_3^4 v_2^2 w_6 w_3^2 c s^2 + 10 w_7 w_4^2 v_2^2 w_6^2 w_3^3 v_3 - 38 w_7^2 w_3^4 v_2^2 w_6^2 w_3 v_3^2 - 8 w_7^2 w_4 w_6^2 w_3^2 v_3^2 c s^2 + 20 w_7^2 w_4 v_2^2 w_6^2 w_3^2 v_3^2 - 2 w_7^2 w_4^2 w_6 w_3^2 c s^4 + \\
&12 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + 2 w_7^2 w_4^2 w_6 w_3^3 v_3 c s^2 - 4 w_7 w_4 v_2^2 w_6^2 w_3 v_3^2 c s^2 + 10 w_7^2 w_4^2 v_2^2 w_6^3 v_3^2 c s^2 - 2 w_7^2 w_4^2 w_6 w_3^3 c s^4 - 4 w_7^2 w_4 v_2^2 w_6^2 w_3^2 c s^2 + 20 w_7^2 w_3^2 v_2^2 w_6^2 v_3^2 + \\
&10 w_7^2 w_4^3 v_2^2 w_6 w_3^2 v_3^2 - 4 w_7^2 w_4^3 w_6^2 w_3^2 c s^2 + 10 w_7 w_4^2 v_2^2 w_6^2 w_3^3 c s^2 + 4 w_7^2 w_4^2 v_2^2 w_6^2 w_3 c s^2 + 4 w_7^2 w_4 v_2^2 w_6^2 w_3^2 v_3^2 + 12 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 c s^2 - \\
&2 w_7^2 w_3^2 w_6^2 w_3 c s^4 + w_7 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 36 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 4 w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + w_7^2 w_4^2 w_6 w_3^2 c s^4 - 8 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + \\
&4 w_7 w_4^2 w_6^2 w_3^2 v_2^2 c s^2 + 4 w_7^2 w_4^2 w_6^2 w_3 c s^4 - 38 w_7^2 w_4 v_2^2 w_6^2 w_3^3 v_3 + w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 4 w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 c s^2 + 20 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - \\
&4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 2 w_7 w_4^2 w_6^2 w_3^2 c s^4 - 4 w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 3 w_7^2 w_4^2 v_2^2 w_6 w_3^2 v_3^2 + 10 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 c s^2 + 10 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^4 - \\
&2 w_7^2 w_4^2 v_2^2 w_6 w_3^2 c s^2 + 2 w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 4 w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^4 - 4 w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - w_7^2 w_4^2 w_6^2 w_3^2 c s^4 - 2 w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + \\
&w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + 20 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 2 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + 2 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 2 w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 4 w_7^2 w_4^2 w_6 w_3^2 v_3^2 c s^2 + 4 w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - \\
&4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 12 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^4 + 2 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + w_7 w_4^2 w_6^2 w_3^2 c s^4 - 4 w_7^2 w_4^2 w_6 w_3^2 v_3^2 c s^2 - 3 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 3 w_7^2 w_4^2 w_6 w_3^2 v_3^2 c s^2 + \\
&2 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 4 w_7^2 w_4^2 v_2^2 w_6 w_3^2 v_3^2 + 20 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 3 w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 2 w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + 4 w_7^2 w_4^2 v_2^2 w_6 w_3^2 c s^2 + \\
&4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^4 + 20 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 2 w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 c s^2 + 4 w_7^2 w_4^2 w_6^2 w_3^2 c s^4 - 2 w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^4 - 8 w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 8 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - \\
&3 w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 4 w_7^2 w_4^2 v_2^2 w_6 w_3^2 v_3^2 + 2 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 4 w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2) \frac{1}{4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2}
\end{aligned}$$

$$\begin{aligned}
C_{\substack{\text{D}_2^{\text{D}_2} \text{D}_2^{\text{D}_2} \\ \rho}}^{(0), \text{MRT2}} = & (10w_7w_4^2v_2^2w_6^2w_3^3v_3 + w_7^2w_4^3cs^4w_6w_3^3 - 38w_7w_4^3v_2^2w_6^2w_3v_3^2 - 3w_7^2w_4^3cs^2w_6w_3^3v_3^2 + 20w_7^2w_4v_2^2w_6^2w_3^2v_3^2 - 2w_7^2w_4cs^4w_6^2w_3^3 - \\
& 4w_7^2w_4^2cs^2w_6^2w_3^3v_3^2 + 10w_7w_4^2cs^2v_2^2w_6^2w_3^3 - 4w_7w_4cs^2v_2^2w_6^2w_3^3 + 4w_7^2w_4cs^2w_6^2w_3^3v_2^2 + 20w_7^2w_4^3v_2^2w_6^2w_3^2v_3^2 + 10w_7^2w_4^3cs^2v_2^2w_6^2w_3^2v_3^2 - 8w_7^2w_4^2cs^2v_2^2w_6^2w_3 - \\
& 4w_7^2w_4^3cs^2w_6^2w_3^3v_3^2 - 2w_7^2w_4^3cs^4w_6w_3^3 + 4w_7w_4^2cs^2w_6^2w_3^3v_3^2 - 4w_7w_4v_2^2w_6^2w_3^3v_3^2 + 4w_7^2w_4cs^4w_6^2w_3^3 - 4w_7w_4^2cs^2v_2^2w_6^2w_3^2v_3^2 - 36w_7^2w_4^2v_2^2w_6^2w_3^3v_3^2 + \\
& 4w_7^2w_4^2cs^4w_6w_3^3 + 10w_7^2w_4cs^2v_2^2w_6^2w_3^3 + 12w_7^2w_4^2cs^2w_6^2w_3^2v_3^2 + w_7^2w_4^3cs^2v_2^2w_6^2w_3^3 - 38w_7^2w_4v_2^2w_6^2w_3^3v_3^2 - 4w_7w_4^2v_2^2w_6^2w_3^3v_3^2 + 12w_7^2w_4^2cs^2v_2^2w_6^2w_3^2v_3^2 + \\
& 10w_7w_4^3cs^2w_6w_3^3v_3^2 + 20w_7^2w_4^2v_2^2w_6^2w_3^3v_3^2 - 2w_7^2w_4^3cs^2v_2^2w_6^2w_3^2 - 4w_7w_4cs^2v_2^2w_6^2w_3^2 - 2w_7^2w_4^2cs^4w_6w_3^3 - 4w_7^2w_4^2v_2^2w_6^2w_3^3v_3^2 + 2w_7^2w_4^3cs^2v_2^2w_6^2w_3^2v_3^2 - \\
& 3w_7^2w_4^3v_2^2w_6w_3^3v_3^2 - 2w_7w_4^2cs^2w_6^2w_3^3v_3^2 - 8w_7^2w_4^2cs^2v_2^2w_6^2w_3^3 + 10w_7^2w_4^3cs^2w_6^2w_3^2v_3^2 - 8w_7^2w_4cs^2w_6^2w_3^2v_3^2 - 4w_7^2w_4^2cs^2v_2^2w_6^2w_3^2v_3^2 - 4w_7^2w_4^3cs^2v_2^2w_6^2w_3^2v_3^2 + \\
& 2w_7w_4^3v_2^2w_6^2w_3^3v_3^2 - 4w_7^2w_4^2cs^2w_6w_3^3v_3^2 - 4w_7^2cs^2v_2^2w_6^2w_3^3 + 4w_7^2w_4^2cs^4w_6^2w_3^3 - 2w_7w_4^2cs^2v_2^2w_6w_3^3 - 4w_7^2w_4^3v_2^2w_6^2w_3^2v_3^2 - 8w_7^2w_4^3cs^2w_6^2w_3^2v_3^2 + \\
& 4w_7w_4^2cs^4w_6^2w_3^3 + 20w_7^2v_2^2w_6^2w_3^3v_3^2 - 4w_7^2w_4^3cs^2w_6^2w_3^2v_3^2 - 12w_7w_4^2cs^4w_6^2w_3^2 + 2w_7^2cs^2v_2^2w_6^2w_3^3 + 2w_7^2w_4^2v_2^2w_6w_3^3v_3^2 - 4w_7^2w_4^2cs^2w_6^2w_3^3v_3^2 + \\
& w_7^2w_4^3cs^2v_2^2w_6^2w_3^3 + w_7w_4^2cs^2v_2^2w_6^2w_3^3v_3^2 + 2w_4^2v_2^2w_6^2w_3^3v_3^2 - 2w_7w_4^2cs^4w_6^2w_3^3 - 4w_7^2w_4^3cs^2w_6w_3v_3^2 - 2w_7w_4^2cs^4w_6^2w_3^3 + 4w_7^2w_4^2cs^2v_2^2w_6w_3^2 - \\
& 3w_7^2w_4^3v_2^2w_6^2w_3^3v_3^2 - 3w_7w_4^2cs^2v_2^2w_6^2w_3^3 + 4w_7^2w_4^2cs^4w_6^2w_3^3 + w_7^2w_4^3cs^2w_6^2w_3^3v_3^2 + 2w_7^2w_4^3v_2^2w_6^2w_3^2v_3^2 - 4w_7^2w_4^2v_2^2w_6w_3v_3^2 + w_7w_4^2cs^4w_6^2w_3^3 + \\
& 4w_7^2w_4^2cs^4w_6^2w_3^3 + 20w_7^2w_4^2v_2^2w_6^2w_3^3v_3^2 - 3w_7w_4^3v_2^2w_6^2w_3^3v_3^2 + 2w_7^2w_4^2cs^2w_6w_3v_3^2 + 20w_7^2v_2^2w_6^2w_3^2v_3^2 - w_7^2w_4^3cs^4w_6^2w_3^3 + 2w_7w_4^2cs^2v_2^2w_6^2w_3^2 + \\
& 4w_7^2w_4^3cs^2v_2^2w_6^2w_3^3 - 4w_7^2w_4^2v_2^2w_6w_3^2v_3^2 - 2w_7w_4^3cs^2w_6^2w_3^2v_3^2 - 2w_7w_4^3cs^4w_6^2w_3^2) \frac{1}{4w_7^2w_4^3w_6^2w_3^3}
\end{aligned}$$

$$\begin{aligned}
C_{D_2^2 D_2^2 p}^{(0), \text{CLBM1}} = & (-10 w_7 w_4^2 v_3^2 w_6^2 w_3^3 v_3^2 - 14 w_7^2 w_3^3 v_2^2 w_6^2 w_3 v_3^2 - 4 w_7^2 w_3^4 c s^2 w_6^2 v_3^2 + 8 w_7^2 w_4^2 v_2^2 c s^2 w_6^2 w_3^2 + 12 w_7^2 w_4 v_2^3 w_6^2 w_3^2 v_3^2 + 4 w_7 w_4^2 c s^4 w_6^2 w_3^2 + \\
& 4 w_7^2 w_2^4 c s^4 w_6^2 w_3^3 + 10 w_7^2 w_4 v_2^2 c s^2 w_6^2 v_3^3 - 4 w_7 w_2^2 c s^2 w_6^2 w_3^2 v_3^2 - w_7^2 w_3^4 v_2^2 c s^2 w_6^2 w_3^3 - 8 w_7^2 w_2^2 v_2^2 c s^2 w_6^2 w_3^2 - 2 w_7 w_4^2 c s^4 w_6^2 w_3^3 - 2 w_7^2 w_4^2 c s^2 w_6^2 w_3^3 v_3^2 - \\
& 2 w_7^2 w_3^3 c s^4 w_6^2 w_3^3 + 4 w_7^2 w_3^4 v_2^2 w_6^2 v_3^2 - 10 w_7^2 w_3^4 v_2^2 w_6 w_3^2 v_3^2 - 4 w_4^2 v_2^2 c s^2 w_6^2 w_3^2 + 2 w_7^2 w_3^4 c s^2 w_6 w_3^2 + 4 w_7 w_4 v_2^2 w_6^2 w_3^3 v_3^2 - 3 w_7^2 w_3^3 c s^2 w_6 w_3^2 v_3^2 - \\
& 12 w_7^2 w_4^2 c s^4 w_6^2 w_3^2 - 28 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 4 w_7^2 w_4 v_2^2 c s^2 w_6^2 w_3^2 + 10 w_7^2 w_4^2 c s^2 w_6^2 w_3^2 v_3^2 + 10 w_7^2 w_4 v_2^2 c s^2 w_6^2 w_3^2 v_3^2 + 2 w_7 w_4^2 c s^2 w_6^2 w_3^2 v_3^2 + 4 w_7^2 w_4^2 c s^4 w_6^2 w_3^2 + \\
& w_7 w_4^3 c s^4 w_6^2 w_3^3 + 4 w_7^2 w_4^3 c s^4 w_6^2 w_3^4 - 14 w_7^2 w_4 v_2^2 w_6^2 w_3^2 v_3^2 + 4 w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - 2 w_7 w_4^3 c s^4 w_6^2 w_3^2 v_3^2 + 14 w_7^2 w_4 v_2^2 w_6^2 w_3^2 v_3^2 - 4 w_7 w_4^2 v_2^2 c s^2 w_6^2 w_3^2 + \\
& 10 w_7 w_4^2 c s^2 w_6 w_3^2 v_3^2 + 4 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 3 w_7^2 w_4^3 v_2^2 w_6^2 w_3^3 v_3^2 - 4 w_7 w_4 v_2^2 c s^2 w_6^2 w_3^2 + 8 w_7^2 w_4^2 c s^2 w_6^2 w_3^2 v_3^2 - w_7^2 w_4^3 c s^4 w_6^2 w_3^2 - 2 w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 - \\
& 4 w_7^2 w_3^4 c s^2 w_6 w_3^2 v_3^2 - 2 w_7^2 w_4 c s^4 w_6^2 w_3^2 + 4 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 4 w_7^2 v_2^2 w_6^2 w_3^2 v_3^2 + w_7^2 w_3^4 c s^4 w_6 w_3^2 - w_7 w_4^3 c s^2 w_6^2 w_3^2 v_3^2 - 3 w_7 w_4^3 v_2^2 c s^2 w_6^2 w_3^2 - \\
& 4 w_7^2 w_4^2 c s^2 w_6^2 w_3^2 v_3^2 - 8 w_7^2 w_4^3 c s^2 w_6^2 w_3^2 v_3^2 + 4 w_7^2 w_4 c s^4 w_6^2 w_3^2 - 2 w_7^2 w_4 v_2^2 w_6 w_3^2 v_3^2 + 2 w_7 w_4^3 c s^2 c s^2 w_6^2 w_3^2 - 4 w_7^2 w_4^3 c s^2 w_6^2 w_3^2 v_3^2 - 2 w_3^4 v_2^2 c s^2 w_6^2 w_3^2 v_3^2 - \\
& 4 w_7^2 w_4^2 c s^2 w_6 w_3^2 v_3^2 - 2 w_7^2 w_4^3 c s^4 w_6 w_3^2 - 3 w_7^2 w_4^3 v_2^2 w_6^2 w_3^2 v_3^2 + 2 w_7^2 w_4^3 v_2^2 c s^2 w_6^2 w_3^2 v_3^2 + 2 w_7^2 w_4^3 v_2^2 w_6^2 w_3^2 v_3^2 + 4 w_7^2 w_4^3 v_2^2 w_6 w_3^2 v_3^2 - \\
& 2 w_7^2 w_4^2 v_2^2 c s^2 w_6^2 w_3^2 + 12 w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 3 w_7^2 w_4^3 v_2^2 w_6^2 w_3^2 v_3^2 + 4 w_7^2 w_4^2 c s^4 w_6 w_3^2 - 4 w_7^2 w_4 v_2^2 c s^2 w_6 w_3^2 + 14 w_7^2 w_4^3 v_2^2 w_6^2 w_3^2 v_3^2 + 2 w_7^2 w_4^3 c s^2 w_6^2 w_3^2 v_3^2 - \\
& 4 w_7^2 w_4^2 v_2^2 c s^2 w_6 w_3^2 + 2 w_7^2 w_4^2 c s^2 w_6 w_3^2 v_3^2 + 2 w_4^2 v_2^2 c s^2 w_6^2 w_3^2 + 4 w_7^2 w_4^2 v_2^2 w_6 w_3^2 v_3^2 - 2 w_7^2 w_4^2 c s^4 w_6 w_3^2 + w_7^2 w_4^3 c s^2 w_6^2 w_3^2 v_3^2 + w_7^2 w_4^3 v_2^2 c s^2 w_6^2 w_3^2) \frac{1}{4 w_7^2 \frac{3}{4} w_6^2 w_3^2}
\end{aligned}$$

$$\begin{aligned}
C_{\substack{\text{D}_2^0 \text{D}_2^0 \\ \rho}}^{(0), \text{CLB2M2}} = & (-4w_7^2 w_4 v_2^2 w_6^2 w_3^2 c s^2 - 2w_7^2 w_4^2 w_6 w_3^3 c s^4 - 10w_7 w_4^2 v_2^2 w_6^2 w_3^3 v_3^2 - 14w_7^2 w_3^4 v_2^2 w_6^2 w_3 v_3^2 + 10w_7^2 w_3^4 w_6^2 w_3 v_3^2 c s^2 + 10w_7 w_4^2 v_2^2 w_6^2 w_3^3 c s^2) \\
& + 4w_7^2 w_3^3 w_6^2 v_3^2 c s^2 + 12w_7^2 w_4 v_2^2 w_6^2 w_3^2 v_3^2 + 4w_7^2 w_4 w_6^2 w_3^2 c s^4 + 8w_7^2 w_3^4 w_6^2 w_3^2 v_3^2 c s^2 - w_7 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 2w_7^2 w_3^4 w_6^2 w_3^2 c s^4 + 2w_7^2 w_3^4 v_2^2 w_6^2 w_3^2 c s^2 + \\
& 4w_7^2 w_3^3 w_6^2 v_2^2 - 10w_7 w_3^3 v_2^2 w_6 w_3^2 v_3^2 + 8w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + 4w_7 w_4 v_2^2 w_6^2 w_3^3 v_3^2 - 2w_7^2 w_3^4 w_6 w_3^2 c s^4 - 4w_7 w_4 v_2^2 w_6^2 w_3^2 c s^2 - 28w_7^2 w_3^2 v_2^2 w_6^2 w_3^2 v_3^2 + \\
& 2w_7^2 w_4 v_2^2 w_6^2 w_3^3 c s^2 + 10w_7^2 w_3^4 w_6 w_3^2 v_2^2 c s^2 - 2w_7^2 w_4 w_6^2 w_3^2 c s^4 - 14w_7^2 w_4 v_2^2 w_6^2 w_3^3 v_2^2 - 4w_7 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 + 4w_7 w_4^2 v_2^2 w_6^2 w_3^2 v_2^2 + 4w_7^2 w_3^4 w_6 w_3^2 c s^4 + \\
& 10w_7^2 w_4 v_2^2 w_6^2 w_3^3 c s^2 - 4w_7^2 v_2^2 w_6^2 w_3^2 c s^2 + 14w_7^2 w_3^2 v_2^2 w_6^2 w_3^3 v_2^2 - 4w_7^2 w_3^4 w_6^2 w_3^2 c s^2 - 8w_7^2 w_3^2 v_2^2 w_6^2 w_3^3 c s^2 + w_7^2 w_3^4 w_6 w_3^2 c s^4 + 4w_7^2 v_2^2 w_6^2 w_3^2 v_2^2 + \\
& 4w_7^2 w_3^2 w_6^2 w_3 c s^4 + 3w_7^2 w_3^3 v_2^2 w_6 w_3^2 v_2^2 - 4w_7 w_4^2 w_6^2 w_3^2 v_2^2 c s^2 + w_7^2 w_3^4 w_6^2 w_3^2 v_2^2 c s^2 - w_7^2 w_3^4 v_2^2 w_6 w_3^2 c s^2 - 2w_7 w_3^2 v_2^2 w_6^2 w_3^2 v_2^2 - 4w_7^2 w_3^2 w_6 w_3^2 v_2^2 c s^2 + \\
& 2w_7 w_3^3 v_2^2 w_6^2 w_3^2 c s^2 + 4w_7^2 w_3^4 v_2^2 w_6^2 w_3^2 v_3^2 + w_7 w_3^4 v_2^2 w_6^2 w_3^3 c s^4 - 12w_7^2 w_4^2 w_6^2 w_3^2 c s^4 - 4w_7^2 w_2^2 w_6^2 w_3^2 c s^2 + 4w_7^2 v_2^2 w_6^2 w_3^2 v_3^2 - 4w_7^2 w_3^4 w_6 w_3^2 v_3^2 c s^2 - w_7^2 w_3^4 w_6^2 w_3^2 c s^4 + \\
& 4w_7 w_3^2 w_6^2 w_3^3 c s^4 + 2w_7^2 w_3^4 v_2^2 w_6 w_3^2 c s^2 - 2w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 2w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 2w_7 w_3^4 w_6^2 w_3^2 v_3^2 c s^2 + w_7^2 w_3^4 v_2^2 w_6^2 w_3^2 v_3^2 c s^2 - 2w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + \\
& 2w_4^2 v_2^2 w_6^2 w_3^3 c s^2 - 3w_7^2 w_3^4 v_2^2 w_6 w_3^2 v_3^2 + 2w_7 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 2w_7 w_4^2 w_6^2 w_3^2 v_3^2 c s^4 - 2w_7^2 w_3^4 v_2^2 w_6^2 w_3^2 v_3^2 - 8w_7^2 w_3^4 w_6^2 w_3^2 v_3^2 c s^2 + 4w_7 w_4^2 w_6^2 w_3^2 c s^4 + \\
& 4w_7^2 w_3^2 v_2^2 w_6 w_3^2 v_3^2 + 2w_7^2 w_3^4 w_6^2 w_3^2 v_3^2 c s^2 - 3w_7 w_3^4 v_2^2 w_6^2 w_3^2 v_3^2 c s^2 + 12w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 3w_7 w_3^4 v_2^2 w_6^2 w_3^2 v_3^2 - 4w_7^2 w_4^2 w_6^2 w_3^2 v_3^2 c s^2 - 3w_7^2 w_4^2 w_6 w_3^2 v_3^2 c s^2 + \\
& 14w_7^2 w_3^4 v_2^2 w_6^2 w_3^2 v_3^2 - 2w_7^2 w_3^4 v_2^2 w_6^2 w_3^2 c s^2 + 4w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 v_3^2 + 4w_7^2 w_3^4 w_6^2 w_3^2 c s^4 - 4w_7^2 w_4^2 v_2^2 w_6^2 w_3^2 c s^2 - 2w_7 w_4^2 w_6^2 w_3^2 c s^4) \frac{1}{4w_7^2 w_4^2 w_6^2 w_3^2}
\end{aligned}$$

**coefficient**  $C_{D_y^2 D_z^2 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2}$ :

$$C_{\substack{D_y^{(0)} D_2^{SRT} v_2}}^{(0),SRT} = (-26\omega^2 cs^2 - 126\omega v_3^2 + \omega^3 cs^2 - 48cs^2 + 84v_3^2 - 4\omega^3 v_3^2 + 72\omega cs^2 + 50\omega^2 v_3^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{\substack{D_2^0 D_2^1 v_2}}^{(0), \text{MRT1}} = (-30\omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_7\omega_4^3\omega_3^3cs^2 + 34\omega_7^2\omega_4^2\omega_3^3v_3^2 - 12\omega_4^2\omega_3^3v_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 6\omega_7\omega_4^3\omega_3^3v_3^2 - 14\omega_7^2\omega_4^2\omega_3^3cs^2 - 12\omega_4^2\omega_3^3cs^2 + 6\omega_7^2\omega_4^3\omega_3cs^2 - 48\omega_7^2\omega_4^2\omega_3^3v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4\omega_3^3cs^2 + 48\omega_7^2\omega_3^3v_3^2 + 12\omega_7^2\omega_4^2\omega_3^3cs^2 + 6\omega_3^3\omega_3^3cs^2 + \omega_7^2\omega_4^3\omega_3^3cs^2 + 24\omega_7\omega_4^2\omega_3^3v_3^2 - 12\omega_7^2\omega_4^2\omega_3cs^2 +$$

$$24w_7^2w_4w_3^2v_3^2 + 24w_7^2w_4^2w_3v_3^2 + 6w_4^3w_3^3v_3^2 - 4w_7^2w_4w_3^3v_3^2 + 24w_7w_4^2w_3^3cs^2 - 78w_7^2w_4w_3^2v_3^2 - 6w_7^2w_4^3w_3^2cs^2 + 22w_7^2w_4w_3^2v_3^2 + 24w_7^2w_4w_3^3cs^2) \frac{v_2\rho}{12w_7^2w_4^2w_3^3}$$

$$\begin{aligned} C_{\substack{\mathbf{D}_2^0 \mathbf{D}_2^2 v_2}}^{(0), \text{MRT2}} = & (24w_7^2 w_4 c s^2 w_3^3 - 30w_7^2 w_3^2 w_3 v_3^2 + 34w_7^2 w_4 w_3^3 v_3^2 - 12w_2^2 w_3^3 v_3^2 + 6w_7^2 w_4^3 c s^2 w_3 + 12w_7^2 w_4^3 v_3^2 - 6w_7 w_3^4 w_3^3 v_3^2 - 48w_7^2 w_4^2 w_3^2 v_3^2 - 12w_7 w_4 w_3^3 v_3^2 - \\ 6w_7^2 w_4^3 c s^2 w_3^3 + 24w_7 w_4^2 c s^2 w_3^3 + 48w_7^2 w_3^2 v_3^2 + w_7^2 w_4^3 c s^2 w_3^3 + 6w_4^3 c s^2 w_3^3 + 24w_7 w_4^2 w_3^3 v_3^2 + 24w_7^2 w_4 w_3^2 v_3^2 - 12w_7^2 w_4^2 c s^2 w_3^3 + 24w_7^2 w_4^2 w_3^2 v_3^2 + \\ 6w_4^3 w_3^3 v_3^2 - 4w_7^2 w_4^2 w_3^3 v_3^2 - 12w_7^2 c s^2 w_3^3 - 12w_4^2 c s^2 w_3^3 - 14w_7^2 w_4^2 c s^2 w_3^3 - 78w_7^2 w_4 w_3^3 v_3^2 - 6w_7 w_3^4 c s^2 w_3^3 + 12w_7^2 w_4^2 c s^2 w_3^3 + 22w_7^2 w_4^3 w_3^2 v_3^2) \frac{v_2 \rho}{12z^2 w_4^3 w_3^3} \end{aligned}$$

$$C_{\substack{D_2^0 D_2^1 v_2}}^{(0), \text{CLBM1}} = (-30\omega_7^2\omega_3^4w_3v_3^2 + 22\omega_7^2\omega_4^3w_3^2v_3 - 6\omega_7^2w_4^3cs^2w_3^2 + 12w_4^2w_3^3v_3^2 + 24w_7w_4^2cs^2w_3^3 + 12w_7^2w_4^3v_3^2 + w_7^2w_3^4cs^2w_3^3 + 6w_3^3cs^2w_3^3 + 6w_7w_4^3w_3^3v_3^2 - 48w_7^2w_4^3w_3^2v_3^2 + 12w_7w_4w_3^3v_3^2 + 24w_7^2w_4cs^2w_3^3 + 6w_7^2w_4^3cs^2w_3 - 12w_4^2cs^2w_3^3 - 24w_7w_4^2w_3^3v_3^2 - 14w_7^2w_4^2cs^2w_3^3 + 24w_7^2w_4w_3^2v_3^2 + 24w_7^2w_4^2w_3v_3^2 - 6w_3^4w_3^3v_3^2 - 6w_7w_4^3cs^2w_3^3 - 4w_7^2w_4^3w_3^2v_3^2 + 12w_7^2w_4cs^2w_3^2 - 18w_7^2w_4w_3^3v_3^2 - 12w_7w_4cs^2w_3^3 - 12w_7^2w_4^2cs^2w_3 + 22w_7^2w_4^3w_3^2v_3^2 - 12w_7^2cs^2w_3^3) \frac{v_2\rho}{12\omega_7^2w_4^3w_3^3}$$

$$\begin{aligned} C_{\substack{\text{D}_2^0 \text{D}_2^1 v_2}}^{(0), \text{CLBM2}} = & (-14\omega_7^2\omega_4^2\omega_3^3cs^2 - 12\omega_4^2\omega_3^3cs^2 - 30\omega_7^2\omega_4^3\omega_3v_3 + 6\omega_7^2\omega_4^3\omega_3cs^2 + 22\omega_7^2\omega_4^2\omega_3^2v_3 + 12\omega_4^2\omega_3^2v_3 + 12\omega_7^2\omega_4^3v_3 + 6\omega_7\omega_4^3\omega_3^3v_3 - 6\omega_7\omega_4^3\omega_3^2cs^2 - 12\omega_7\omega_4\omega_3^3cs^2 - 48\omega_7^2\omega_4^2\omega_3^2v_3 + 12\omega_7\omega_4\omega_3^3v_3 + 12\omega_7^2\omega_4^2\omega_3^2cs^2 - 12\omega_7^2\omega_4^3\omega_3cs^2 - 24\omega_7\omega_4^2\omega_3^2v_3 + 24\omega_7\omega_4^2\omega_3^3v_3 + 24\omega_7^2\omega_4\omega_3^2v_3 + 24\omega_7^2\omega_4^2\omega_3^2v_3 + 6\omega_4^3\omega_3^3cs^2 + \omega_7^2\omega_4^3\omega_3^2cs^2 - 6\omega_4^3\omega_3^3v_3 - 4\omega_7^2\omega_4^2\omega_3^2v_3 - 12\omega_7^2\omega_4^2\omega_3cs^2 - 18\omega_7\omega_4\omega_3^3v_3 + 24\omega_7^2\omega_4\omega_3^2cs^2 + 22\omega_7^2\omega_4^2\omega_3^2v_3 - 6\omega_7^2\omega_4^3\omega_3^2cs^2) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3} \end{aligned}$$

**coefficient**  $C_{D_y^2 D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2}$ :

$$C_{\frac{D_y^2}{D_z^2}v_3}^{(0),\text{SRT}} = (-26\omega^2 cs^2 + 50\omega^2 v_2^2 - 4\omega^3 v_2^2 + \omega^3 cs^2 - 48cs^2 + 84v_2^2 + 72\omega cs^2 - 126\omega v_2^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\substack{D_2^0 D_2^0 v_3}}^{(0), \text{MRT1}} = (-14w_4^3 w_6^2 w_3^2 c s^2 - 12w_4^3 v_2^2 w_3^2 - 4w_4^3 v_2^2 w_6^2 w_3^3 - 12w_4^3 w_6 w_3 c s^2 + 6w_4^3 v_2^2 w_3^3 + 24w_4^2 v_2^2 w_6^2 w_3 + 34w_4^3 v_2^2 w_6^2 w_3^2 - 6w_4^2 w_6^2 w_3^3 c s^2 - 78w_4^3 v_2^2 w_6^2 w_3 + w_4^3 w_6^2 w_3^3 c s^2 + 48w_4^3 v_2^2 w_6^2 - 48w_4^2 v_2^2 w_6^2 w_3^2 + 12w_4^2 w_6^2 w_3^2 c s^2 - 12w_4^3 w_6^2 c s^2 + 22w_4^2 v_2^2 w_6^2 w_3^3 + 6w_4^3 w_6^3 c s^2 + 12v_2^2 w_6^2 w_3^3 - 6w_4^3 w_6 w_3^2 c s^2 + 6w_4 w_6^2 w_3^3 c s^2 - 12w_4^3 v_2^2 w_6 w_3 + 24w_4^3 w_6 w_3^2 c s^2 + 24w_4 v_2^2 w_6^2 w_3^2 + 24w_4^3 v_2^2 w_6 w_3^3 - 12w_4^3 w_3^3 c s^2 - 30w_4 v_2^2 w_6^2 w_3^3 + 24w_4^3 w_6^2 w_3 c s^2 - 6w_4^2 v_2^2 w_6 w_3^3 - 12w_4 w_6^2 w_3^2 c s^2) \frac{\rho v_3}{12c^3 w_6^2 w_3^3}$$

$$C_{\substack{D_2^{(0)} D_2^{(1)} v_3}}^{(0), \text{MRT2}} = (-12w_3^4 c s^2 w_6^2 - 12w_3^4 v_2^2 w_3^2 - 12w_3^4 c s^2 w_6 w_3 - 4w_3^4 v_2^2 w_6^2 w_3^3 + 6w_3^4 v_2^2 w_3^3 + 24w_4^2 v_2^2 w_6^2 w_3 + 34w_4^2 v_2^2 w_6^2 w_3^2 - 78w_4^2 v_2^2 w_6^2 w_3 - 6w_4^3 c s^2 w_6 w_3^3 + 6w_4^4 c s^2 w_6^2 w_3^3 - 12w_4^3 c s^2 w_3^2 + 48w_4^3 v_2^2 w_6^2 - 48w_4^2 v_2^2 w_6^2 w_3^2 + 24w_4^3 c s^2 w_6 w_3^2 + 22w_4^2 v_2^2 w_6^2 w_3^3 - 12w_4 c s^2 w_6^2 w_3^2 + 6w_4^3 c s^2 w_3^3 - 14w_4^3 c s^2 w_6^2 w_3^2 + 12w_2^2 v_2^2 w_6^2 w_3^3 + w_4^3 c s^2 w_6^2 w_3^2 - 12w_4^3 v_2^2 w_6 w_3 + 24w_4 v_2^2 w_6^2 w_3^2 - 6w_4^2 c s^2 w_6^2 w_3^2 + 24w_4^3 v_2^2 w_6 w_3^2 + 12w_4^2 c s^2 w_6^2 w_3^3 - 30w_4 v_2^2 w_6^2 w_3^3 - 6w_4^3 v_2^2 w_6 w_3^3 + 24w_4^3 c s^2 w_6^2 w_3) \frac{\rho v_3}{12w_4^4 w_6^2 w_3^3}$$

$$C_{\frac{D_2^3}{D_2^2 v_3}}^{(0), \text{CLBM1}} = (12w_4^3v_2^2w_3^2 - 14w_4^3cs^2w_6^2w_3^2 - 4w_4^3v_2^2w_6^2w_3^3 - 12w_4^3cs^2w_3^2 - 6w_4^3v_2^2w_3^3 + 24w_4^2v_2^2w_6^2w_3 + 6w_4^3cs^2w_3^3 + 22w_4^3v_2^2w_6^2w_3^2 + w_4^3cs^2w_6^2w_3^3 - 18w_4^3v_2^2w_6^2w_3 - 12w_4^3cs^2w_6^2 - 6w_4^2cs^2w_6^2w_3^2 - 48w_4^2v_2^2w_6^2w_3^3 + 24w_4^3cs^2w_6^2w_3 + 22w_4^2v_2^2w_6^2w_3^3 + 12w_4^2cs^2w_6^2w_3^2 - 12w_4^3cs^2w_6w_3 + 12v_2^2w_6^2w_3^3 + 12w_4^3v_2^2w_6w_3 + 24w_4v_2^2w_6^2w_3^2 + 6w_4cs^2w_6^2w_3^3 - 24w_4^3v_2^2w_6w_3^3 - 6w_4^3cs^2w_6w_3^2 - 12w_4cs^2w_6^2w_3^2 - 30w_4v_2^2w_6^2w_3^3 + 24w_4^3cs^2w_6w_3^2 + 6w_4^3v_2^2w_6w_3^3) \frac{\rho v_3}{12w_4^2w_6^2w_3^3}$$

$$C_{\substack{D_2^0 D_2^1 v_3}}^{(0), \text{CLBM2}} = (-12w_4^3 w_6 w_3 c s^2 + 12w_4^3 v_2^2 w_3^2 - 6w_4^2 w_6^2 w_3 c s^2 - 4w_4^3 v_2^2 w_6^2 w_3^3 - 6w_3^4 v_2^2 w_3^3 + 24w_4^2 v_2^2 w_6^2 w_3 - 14w_4^3 w_6^2 w_3^2 c s^2 + 22w_3^4 v_2^2 w_6^2 w_3^2 - 18w_4^3 v_2^2 w_6^2 w_3 + 12w_4^2 w_6^2 w_3^2 c s^2 - 12w_4^3 w_6^2 c s^2 - 48w_4^2 v_2^2 w_6^2 w_3^2 + 22w_4^2 v_2^2 w_6^2 w_3^3 + w_3^4 w_6^2 w_3^2 c s^2 + 6w_4 w_6^2 w_3^2 c s^2 + 12w_2^2 w_6^2 w_3^3 + 6w_4^3 w_3^2 c s^2 + 12w_4^3 v_2^2 w_6 w_3 - 6w_4^3 w_6 w_3^2 c s^2 + 24w_4 v_2^2 w_6^2 w_3^2 + 24w_4^3 w_6^2 w_3 c s^2 - 24w_4^3 v_2^2 w_6 w_3^2 - 12w_4 w_6^2 w_3^2 c s^2 + 24w_4^3 w_6 w_3^2 c s^2 - 30w_4 v_2^2 w_6^2 w_3^3 + 6w_4^3 v_2^2 w_6 w_3^3 - 12w_4^3 v_2^2 c s^2) \frac{\rho v_3}{12z_3^4 w_6^2 w_3^3}$$

**coefficient**  $C_{D_t D_z^3 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t \partial x_3^3}$ :

$$C_{\substack{D_1 D_2 v_3}}^{(0), \text{SRT}} = (-36 + 34\omega^2 cs^2 - 108\omega v_3^2 - 2w^3 cs^2 + 60cs^2 + 54\omega + \omega^3 + 72v_3^2 - 20\omega^2 - 3\omega^3 v_3^2 - 90\omega cs^2 + 42w^2 v_3^2) \frac{\rho}{12w^3}$$

$$C_{\substack{D_7 D_3 v_3}}^{(0), \text{MRT1}} = (-2\omega_7^2\omega_4^3cs^2 + 6\omega_4^3 + 36\omega_7\omega_4^2 - 12\omega_4^2 - 3\omega_7^2\omega_4^3v_3^2 - 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 + 25\omega_7^2\omega_4^2cs^2 + 48\omega_7\omega_4v_3^2 + 24\omega_7^2cs^2 - 24\omega_7\omega_4 + 27\omega_7^2\omega_4^2v_3^2 + 24\omega_7\omega_4cs^2 - 6\omega_4^3cs^2 + 12\omega_7^2\omega_4 - 36\omega_7\omega_4^2cs^2 - 42\omega_7^2\omega_4v_3^2 - 6\omega_4^3v_3^2 - 60\omega_7\omega_4^2v_3^2 - 48\omega_7^2\omega_4cs^2 + 9\omega_7\omega_4^3cs^2 + \omega_7^2\omega_4^3 + 12\omega_4^2cs^2 + 15\omega_7\omega_4^3v_3^2 + 12\omega_4^2v_3^2 - 11\omega_7^2\omega_4^2) \frac{\rho}{12\omega_7^2\omega_4^3}$$

$$C_{D_t D_z^3 v_3}^{(0), \text{MRT2}} =$$

$$(24\omega_7^2cs^2+6w_4^3+24\omega_7w_4cs^2+36\omega_7w_4^2-12w_4^2-3w_7^2w_3v_3^2-9\omega_7w_4^3+25w_7^2w_4^2cs^2+12w_7^2v_3^2+48\omega_7w_4v_3^2-2w_7^2w_4^3cs^2-24\omega_7w_4+27w_7^2w_4^2v_3^2+12w_7^2w_4-42w_7^2w_4v_3^2+9\omega_7w_4^3cs^2-6w_4^3v_3^2-60\omega_7w_4v_3^2+12w_4^2cs^2+w_7^2w_4^3-48w_7^2w_4cs^2+15\omega_7w_4^3v_3^2-6w_4^3cs^2-36\omega_7w_4^2cs^2+12w_4^2v_3^2-11w_7^2w_4^2)\frac{\rho}{12w_7^2w_4^3}$$

$$C_{D_t D_z^3 v_3} = -$$

$$(6\psi^3 + 9\psi\omega\psi^3) c_t$$

$$(6w_4^4 + 9w_7w_4^4cs + 36w_7w_4^4 + 12w_4^4cs - 12w_4^4 - 3w_7w_4^4v_3 - 9w_7w_4^4 - 6w_4^4cs - 36w_7w_4^4v_3 - 36w_7w_4^4cs + (12w_7w_4^4v_3 - 24w_7w_4^4 + 15w_7w_4^4v_3 - 48w_7w_4^4cs + 12w_7^2w_4 + 18w_7^2w_4v_3^2 + 25w_7^2w_4^2cs^2 + 24w_7^2cs^2 - 18w_4^3v_3 + 24w_7w_4cs^2 - 108w_7w_4v_3^2 - 2w_7^2w_4^2cs^2 + w_7^2w_4^3 + 27w_7w_4^3v_3^2 + 36w_4^2v_3^2 - 11w_7^2w_4^2) \frac{p}{12w_2^2w_3^4})$$

$$C_{D_t D_z^3 v_3}^{(0), \text{CLBM2}} =$$

$$(6\omega_7^3 + 36\omega_7\omega_4^2 - 2\omega_7^2\omega_4^3)cs^2 - 12\omega_4^2 - 3\omega_7^2\omega_4^3v_3^2 - 9\omega_7\omega_4^3 + 24\omega_7^2cs^2 - 36\omega_7^2v_3^2 + 24\omega_7\omega_4cs^2 + 72\omega_7\omega_4v_3^2 - 24\omega_7\omega_4 + 15\omega_7^2\omega_4^2v_3^2 + 25\omega_7^2\omega_4^2cs^2 + 12\omega_7^2\omega_4 + 18\omega_7^2\omega_4v_3^2 - 48\omega_7^2\omega_4cs^2 - 6\omega_4^3cs^2 - 18\omega_4^3v_3^2 - 36\omega_7\omega_4^2cs^2 - 108\omega_7\omega_4^2v_3^2 + \omega_7^2\omega_4^3 + 27\omega_7\omega_4^3v_3^2 + 9\omega_7\omega_4^3cs^2 + 36\omega_4^2v_3^2 + 12\omega_4^2cs^2 - 11\omega_7^2\omega_4^2) \frac{\rho}{12\omega_7^2\omega_4^3}$$

**coefficient  $C_{D_x D_z^3 \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_1 \partial x_3^3}$ :**

$$C_{D_x D_z^3 \rho}^{(0), SRT} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_1 v_3}{6\omega^3}$$

$$\begin{aligned} C_{D_x D_z^3 \rho}^{(0), MRT1} &= (-3\omega_7\omega_4^3\omega_2^2 - 30\omega_7^2\omega_4\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 + 6\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^3v_3^2 - 12\omega_7\omega_4^2\omega_2^2cs^2 + 6\omega_7^2\omega_4^2\omega_2^2v_3^2 + \\ &78\omega_7^2\omega_4\omega_2^3cs^2 + 6\omega_7\omega_4^3\omega_2^3 + 42\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_4^3\omega_2^3cs^2 + 6\omega_7^2\omega_4^3\omega_2^3cs^2 + 6\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 6\omega_2^2\omega_4^2\omega_2^3 + 12\omega_7^2\omega_4\omega_2^2v_3^2 - 21\omega_7\omega_4^2\omega_2^3 + \\ &6\omega_7^2\omega_4^2\omega_2^2v_3^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 + 42\omega_7\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_2^3v_3^2 - 3\omega_7^3\omega_2^3 + 12\omega_7\omega_4\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_7\omega_4^3\omega_2^3cs^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4\omega_2^3v_3^2 - \\ &36\omega_7^2\omega_4^2\omega_2^3cs^2 - 24\omega_7\omega_4\omega_2^3v_3^2 + 24\omega_7^2\omega_4^3\omega_2^3 + 7\omega_7^2\omega_4^2\omega_2^3 + 42\omega_7^2\omega_4^2\omega_2^2cs^2 + 6\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3 - \\ &12\omega_7\omega_4^2\omega_2^3cs^2 - 48\omega_7^2\omega_4^2\omega_2^3cs^2 - 12\omega_4^2\omega_2^3cs^2 - \omega_7^2\omega_4^3\omega_2^3 - 12\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3cs^2) \frac{v_1 v_3}{6\omega_7^2\omega_4^3\omega_2^3} \end{aligned}$$

$$\begin{aligned} C_{D_x D_z^3 \rho}^{(0), MRT2} &= (42\omega_7\omega_4^2\omega_2^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^3\omega_2^3 - 3\omega_7\omega_4^3\omega_2^2 - 30\omega_7^2\omega_4\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^2v_3^2 - 48\omega_7^2\omega_4^2\omega_2^3\omega_2^3 + 6\omega_4^2\omega_2^3 + 6\omega_7\omega_4^3\omega_2^3\omega_2^2 - \\ &12\omega_4^2\omega_2^3\omega_2^3 + 6\omega_7^2\omega_4^3\omega_2^2 + 6\omega_2^2\omega_4^3\omega_2^2v_3^2 + 6\omega_7\omega_4^3\omega_2^3 + 42\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7\omega_4^2\omega_2^2 - 6\omega_7^2\omega_4\omega_2^3 + 12\omega_7^2\omega_4\omega_2^2v_3^2 - 36\omega_7^2\omega_4^2\omega_2^3 - 21\omega_7\omega_4^2\omega_2^3 + \\ &6\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_2^3\omega_2^3 - 3\omega_7^3\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^3cs^2 - 24\omega_7\omega_4\omega_2^3v_3^2 + 12\omega_7\omega_4\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^2v_3^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4\omega_2^3v_3^2 + 6\omega_4^3\omega_2^3\omega_2^3 - \\ &12\omega_7\omega_4^2\omega_2^3\omega_2^2 + 6\omega_7^2\omega_4^3\omega_2^3\omega_2^3 + 24\omega_7^2\omega_4^2\omega_2^3v_3^2 + 7\omega_7^2\omega_4^2\omega_2^3 + 6\omega_7\omega_4^2\omega_2^2v_3^2 + 42\omega_7\omega_4^2\omega_2^3cs^2 - 12\omega_7^2\omega_4^2\omega_2^3cs^2 + 6\omega_7^2\omega_4\omega_2^3\omega_2^2 - 24\omega_7\omega_4\omega_2^3\omega_2^2 - \\ &12\omega_7^2\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_4^2\omega_2^3v_3^2 + \omega_7^2\omega_4^3\omega_2^2 + 78\omega_7^2\omega_4\omega_2^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2) \frac{v_1 v_3}{6\omega_7^2\omega_4^3\omega_2^3} \end{aligned}$$

$$\begin{aligned} C_{D_x D_z^3 \rho}^{(0), CLBM1} &= (-3\omega_7\omega_4^3\omega_2^2 + 12\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^3\omega_2^3cs^2 + 6\omega_4^2\omega_2^3 + 6\omega_7\omega_4^3v_3^2 - 36\omega_7^2\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2^2v_3^2 - 36\omega_7\omega_4^3\omega_2^3cs^2 + 6\omega_7\omega_4^3\omega_2^3 + \\ &6\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 6\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2\omega_4^2\omega_2^3cs^2 - 6\omega_7^2\omega_4\omega_2^3 - 24\omega_7\omega_4\omega_2^3cs^2 - 21\omega_7\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^2\omega_2v_3^2 - 6\omega_4^3\omega_2^3\omega_2^3 + \\ &36\omega_7\omega_4^2\omega_2^2cs^2 - 3\omega_4^3\omega_2^3 + 18\omega_4^3\omega_2^3cs^2 + 12\omega_7\omega_4\omega_2^3 + 6\omega_7^2\omega_4^3\omega_2^3cs^2 - 6\omega_7^2\omega_4^2\omega_2^2v_3^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 24\omega_7\omega_4\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_2^3cs^2 + \\ &7\omega_7^2\omega_4^2\omega_2^3 + 72\omega_7\omega_4^2\omega_2^3cs^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 6\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3cs^2 + 12\omega_4^2\omega_2^3v_3^2 + \omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^3 - 24\omega_7\omega_4^2\omega_2^3cs^2 + 36\omega_7\omega_4\omega_2^3cs^2) \frac{v_1 v_3}{6\omega_7^2\omega_4^3\omega_2^3} \end{aligned}$$

$$\begin{aligned} C_{D_x D_z^3 \rho}^{(0), CLBM2} &= (-3\omega_7\omega_4^3\omega_2^2 + 12\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^3\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_2^3cs^2 + 6\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^3\omega_2^2v_3^2 - 12\omega_7\omega_4^3\omega_2^2cs^2 + 6\omega_7\omega_4^3\omega_2^2 + \\ &12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_2^3cs^2 + 6\omega_7\omega_4^2\omega_2^2 + 72\omega_7\omega_4^2\omega_2^3cs^2 - 6\omega_7^2\omega_4\omega_2^3 + 18\omega_4^3\omega_2^3cs^2 + 6\omega_7^2\omega_4^3\omega_2^3cs^2 - 21\omega_7\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^2\omega_2v_3^2 - 12\omega_7\omega_4^2\omega_2^2cs^2 - \\ &6\omega_4^3\omega_2^3v_3^2 - 3\omega_4^3\omega_2^3 - 24\omega_7\omega_4\omega_2^3cs^2 + 12\omega_7\omega_4\omega_2^3 - 6\omega_7^2\omega_4^2\omega_2^2v_3^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4\omega_2^3v_3^2 + 36\omega_7\omega_4^2\omega_2^2v_3^2 + 12\omega_7\omega_4^2\omega_2^3cs^2 + 7\omega_7^2\omega_4^2\omega_2^3 - \\ &12\omega_7\omega_4^2\omega_2^3cs^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 36\omega_7\omega_4^2\omega_2^3v_3^2 - 36\omega_7\omega_4^2\omega_2^3cs^2 - 6\omega_7^2\omega_4^2\omega_2^3v_3^2 + 12\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2^2cs^2 + \omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^3 - 24\omega_7\omega_4^2\omega_2^3cs^2) \frac{v_1 v_3}{6\omega_7^2\omega_4^3\omega_2^3} \end{aligned}$$

**coefficient  $C_{D_x D_z^3 v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1 \partial x_3^3}$ :**

$$C_{D_x D_z^3 v_1}^{(0), SRT} = (36 - 56\omega^2 cs^2 + 54\omega v_3^2 + 4\omega^3 cs^2 - 96cs^2 - 54\omega - \omega^3 - 36v_3^2 + 20\omega^2 + \omega^3 v_3^2 + 144\omega cs^2 - 20\omega^2 v_3^2) \frac{\rho v_3}{12\omega^3}$$

$$\begin{aligned} C_{D_x D_z^3 v_1}^{(0), MRT1} &= (4\omega_7^2\omega_4^3cs^2 - 6\omega_4^3 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 44\omega_7^2\omega_4^2cs^2 - 36\omega_7\omega_4v_3^2 - 48\omega_7^2cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 36\omega_7\omega_4cs^2 + \\ &6\omega_4^3cs^2 - 12\omega_7^2\omega_4 + 48\omega_7\omega_4^2cs^2 + 6\omega_4^3v_3^2 + 48\omega_7\omega_4^2v_3^2 + 90\omega_7^2\omega_4cs^2 - 12\omega_7\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 12\omega_4^2cs^2 - 12\omega_7\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3} \end{aligned}$$

$$\begin{aligned} C_{D_x D_z^3 v_1}^{(0), MRT2} &= (-48\omega_7^2\omega_4^3cs^2 - 6\omega_4^3 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 44\omega_7^2\omega_4^2cs^2 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4v_3^2 + 4\omega_7^2\omega_4^2cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 36\omega_7\omega_4cs^2 + \\ &12\omega_7\omega_4^2 - 12\omega_7\omega_4^3v_3^2 - 36\omega_7\omega_4^3v_3^2 - 36\omega_7\omega_4^3cs^2 - 6\omega_7^2\omega_4^3v_3^2 + 12\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2^3v_3^2 + 12\omega_7\omega_4^2\omega_2^3v_3^2 - 36\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2 + 12\omega_7\omega_4^2\omega_2^3v_3^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3} \end{aligned}$$

$$\begin{aligned} C_{D_x D_z^3 v_1}^{(0), CLBM1} &= (-6\omega_4^3 - 30\omega_7\omega_4^2cs^2 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4^2cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 + 96\omega_7\omega_4^2cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 + \\ &18\omega_7\omega_4cs^2 - 12\omega_7^2\omega_4 + 12\omega_7^2\omega_4v_3^2 - 26\omega_7^2\omega_4^2cs^2 - 6\omega_7^2\omega_4^3v_3^2 - 36\omega_7\omega_4cs^2 + 48\omega_7\omega_4^2v_3^2 + 4\omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^2v_3^2 + 12\omega_7^2\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3} \end{aligned}$$

$$\begin{aligned} C_{D_x D_z^3 v_1}^{(0), CLBM2} &= (-6\omega_4^3 - 36\omega_7\omega_4^2 + 4\omega_7^2\omega_4^3cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4^2cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 - 26\omega_7\omega_4^2cs^2 - 12\omega_7^2\omega_4 + \\ &12\omega_7\omega_4^2v_3^2 + 18\omega_7^2\omega_4^2cs^2 + 30\omega_4^3cs^2 - 6\omega_4^3v_3^2 + 96\omega_7\omega_4^2cs^2 + 48\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^2v_3^2 - 30\omega_7\omega_4^2cs^2 + 12\omega_4^2v_3^2 - 60\omega_4^2cs^2 + 11\omega_7\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3} \end{aligned}$$

**coefficient  $C_{D_x D_z^3 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1 \partial x_3^3}$ :**

$$C_{D_x D_z^3 v_3}^{(0), SRT} = (12 - 56\omega^2 cs^2 + 18\omega v_3^2 + 4\omega^3 cs^2 - 96cs^2 - 18\omega - \omega^3 - 12v_3^2 + 8\omega^2 + 3\omega^3 v_3^2 + 144\omega cs^2 - 12\omega^2 v_3^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\text{DxD3}^3 v_3}^{(0), \text{MRT1}} = (-6w_7 w_3^4 w_2^2 - 30w_7^2 w_4 w_3^2 v_3^2 - 24w_7 w_4^2 w_2^2 v_3^2 - 12w_7^2 w_3^4 w_2^2 c s^2 + 12w_7^2 w_3^4 v_3^2 - 24w_7 w_4^2 w_2^2 c s^2 + 36w_7^2 w_4 w_3^2 c s^2 + 3w_7 w_3^4 w_2^2 + 36w_7 w_2^4 w_3^2 v_3^2 + 6w_3^4 w_3^2 c s^2 + 4w_7^2 w_3^4 w_3^2 c s^2 + 12w_7 w_4^2 w_2^2 - 12w_7^2 w_4^2 w_2^2 c s^2 - 6w_7 w_4^2 w_2^2 v_3^2 - 24w_7^2 w_4 w_2^2 c s^2 + 36w_7 w_4^2 w_2^2 c s^2 + 6w_3^4 w_3^2 v_3^2 + 3w_7^2 w_3^4 w_3^2 v_3^2 + 12w_2^2 w_3^4 w_2^2 v_3^2 + 12w_7 w_4^3 w_2^2 c s^2 - 6w_2^2 w_3^2 w_2^2 - 12w_7 w_4 w_3^2 v_3^2 - 12w_2^2 w_3^2 c s^2 - 12w_7 w_4 w_3^2 c s^2 + 24w_7^2 w_3^2 v_3^2 + 3w_2^2 w_3^4 w_2^2 + 48w_7 w_2 w_3^2 c s^2 + 12w_7 w_3^4 w_2^2 v_3^2 - 18w_7 w_4^3 w_2 v_3 - 12w_4^2 w_3^2 v_3^2 + 2w_7^2 w_3^4 w_2^2 - 12w_7 w_4 w_3^2 c s^2 - 32w_7^2 w_4 w_3^2 c s^2 - 12w_4^2 w_3^2 c s^2 - w_7^2 w_3^4 w_2^2 - 12w_7 w_4^3 w_2^2 v_3^2 + 6w_7^2 w_4^2 w_2^2 c s^2) \frac{v_1 v_2}{12w_7^2 w_3^2 w_2^2}$$

$$\begin{aligned} C_{\substack{\text{D}_x \text{v}_2 \\ \text{D}_x \text{v}_3}}^{(0), \text{MRT2}} = & (48w_7^2 w_4^2 c s^2 w_2^2 - 12 w_7 w_4^3 c s^2 w_3^2 - 6 w_7 w_4^3 w_2^2 - 30 w_7^2 w_4 w_3^2 v_3^2 - 24 w_7 w_4^2 w_2^2 v_3^2 - 32 w_7^2 w_4^2 c s^2 w_3^2 + 12 w_7 w_4^3 c s^2 w_2^2 - 12 w_4^2 c s^2 w_3^2 + \\ & 12 w_2^2 w_4^3 v_3^2 + 3 w_7 w_4^3 w_3^2 + 36 w_7 w_4^2 w_3^2 v_3^2 + 12 w_7 w_4^2 w_2^2 - 12 w_7^2 c s^2 w_3^2 - 6 w_7 w_4^2 w_3^2 + 6 w_3^4 w_2^3 v_3^2 + 3 w_2^2 w_4^3 w_3^2 v_3^2 - 12 w_7^2 w_4^2 c s^2 w_2^2 - 12 w_7 w_4 c s^2 w_3^2 + \\ & 12 w_2^2 w_4^2 w_2^2 v_3^2 - 6 w_7^2 w_4^2 w_2^2 - 12 w_7 w_4 w_3^2 v_3^2 + 6 w_4^3 c s^2 w_3^2 - 24 w_7 w_4^2 c s^2 w_2^2 + 4 w_7^2 w_4^3 c s^2 w_3^2 + 24 w_7^2 w_4^2 w_3^2 v_3^2 + 3 w_2^2 w_4^2 w_3^2 + 12 w_7 w_4^3 w_2^2 v_3^2 + 36 w_7 w_4^2 c s^2 w_3^2 - \\ & 12 w_7^2 w_4^2 c s^2 w_2^2 + 6 w_7^2 w_4^3 c s^2 w_2^2 - 24 w_7^2 w_4 c s^2 w_2^2 - 18 w_7^2 w_4^3 w_2^2 v_3^2 - 12 w_4^2 w_2^3 v_3^2 + 2 w_7^2 w_4^2 w_2^2 + 36 w_7 w_4 c s^2 w_2^2 - w_7^2 w_4^3 w_2^2 - 12 w_7 w_4^3 w_2^3 v_3^2) \frac{v_1 \rho}{12 w_7^2 w_4^2 w_3^2} \end{aligned}$$

$$C_{\substack{O \\ D_x D_y D_z v_3}}^{(0), \text{CLBM}} = (-6w_7 w_4^3 w_2^2 + 30w_7^2 w_4 w_3^3 v_3^2 - 24w_7 w_4^2 w_2^2 v_3^2 - 12w_7 w_3^3 w_2^3 c s^2 + 12w_7^2 w_3^4 v_3^2 - 32w_7^2 w_2^2 w_3^2 c s^2 - 12w_2^2 w_3^2 c s^2 + 3w_7 w_3^3 w_2^3 + 6w_7^2 w_3^4 w_2 c s^2 + 12w_7 w_3^4 w_2^2 c s^2 - 12w_7 w_4^2 w_2^3 v_3^2 + 12w_7 w_2^2 w_2^2 - 12w_7^2 w_3^2 c s^2 - 12w_7 w_4 w_3^2 c s^2 - 6w_7 w_4^2 w_3^2 - 6w_4^3 w_3^2 v_3^2 + 3w_7 w_3^3 w_2^3 v_3^2 + 48w_7 w_2^2 w_2^2 c s^2 + 6w_3^4 w_3^2 c s^2 + 4w_7^2 w_3^4 w_3^2 c s^2 + 12w_7^2 w_4^2 w_2^2 v_3^2 - 6w_7^2 w_4^2 w_2^2 - 12w_7^2 w_4^2 w_2 c s^2 + 12w_7 w_4 w_3^2 v_3^2 - 24w_7 w_2 w_3^2 w_2^2 c s^2 - 24w_7 w_2^2 w_3^2 v_3^2 + 3w_2^2 w_2^2 w_3^2 + 12w_7 w_3^4 w_2^2 v_3^2 + 36w_7 w_4^2 w_3^2 c s^2 - 18w_7 w_3^4 w_2 v_3^2 - 12w_7^2 w_4^2 w_3^2 v_3^2 - 12w_7 w_3^4 w_2^3 c s^2 + 12w_2^4 w_3^2 v_3^2 + 2w_7^2 w_4^2 w_2^2 - w_7 w_3^4 w_2^3 - 24w_7 w_2^2 w_2^2 c s^2 + 36w_7 w_4 w_3^2 c s^2) \frac{v_1 \rho}{12w_7^2 w_4^3 w_2^3}$$

$$\begin{aligned} C_{\text{D}_x \text{D}_z^3 v_3}^{(0), \text{CLBM2}} = & (-6w_7 w_4^3 w_2^2 + 30w_7^2 w_4 w_3^2 v_3^2 - 24w_7 w_4^2 w_2^2 c s^2 + 36w_7^2 w_4 w_3^2 c s^2 - 24w_7 w_4^2 w_2^2 v_3^2 + 12w_7^2 w_3^4 v_3^2 - \\ & 12w_7^2 w_4^2 w_2^2 v_3^2 - 24w_7^2 w_4 w_2^2 c s^2 + 12w_7 w_4^2 w_2^2 + 36w_7 w_4^2 w_3^2 c s^2 + 6w_4^2 w_3^2 c s^2 + 4w_2^2 w_4^2 w_3^2 c s^2 - 6w_7 w_4^2 w_3^2 - 12w_7^2 w_4^2 w_2 c s^2 - 6w_3^2 w_3^2 v_3^2 + 3w_7^2 w_3^4 w_2^2 v_3^2 - \\ & 12w_7 w_4^2 w_3^2 c s^2 + 12w_7^2 w_2^2 w_3^2 v_3^2 - 6w_7^2 w_4^2 w_2^2 + 12w_7 w_4 w_2^2 v_3^2 + 48w_7^2 w_4^2 w_2^2 c s^2 + 12w_7 w_4^2 w_2^2 c s^2 - 24w_7^2 w_3^2 v_3^2 + 3w_7^2 w_4^2 w_2^2 v_3^2 - 12w_7 w_3^2 c s^2 + 12w_7 w_4^2 w_2^2 v_3^2 - \\ & 18w_7^2 w_4^2 w_2 v_3^2 - 32w_7^2 w_4^2 w_2^2 c s^2 - 12w_4^2 w_2^2 c s^2 - 12w_7^2 w_4^2 w_3^2 v_3^2 + 12w_4^2 w_3^2 v_3^2 + 6w_7^2 w_4^2 w_2 c s^2 + 2w_7^2 w_4^2 w_2^2 - w_7^2 w_4^2 w_2^2 - 12w_7 w_4^2 w_3^2 c s^2) \frac{v_1 p}{12w_7^2 w_4^2 w_3^2} \end{aligned}$$

coefficient  $C_{D_y D_z^3 \rho}^{(0)}$  at  $\frac{\partial^4 \rho}{\partial x_2 \partial x_3^3}$ :

$$C_{\text{D}_y \text{D}_z^3 \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_2 v_3}{6\omega^3}$$

$$C_{D_y D_y}^{(0), \text{MR11}} = -(\omega_7^2 w_4^3 w_3^3 - 12 w_7^2 w_4^3 w_3 v_3 - 12 w_7 w_4^3 w_3^3 c s^2 + 6 w_7^2 w_4^2 w_3^3 v_3 - 12 w_4^2 w_3^3 v_3^2 + 6 w_7^2 w_4^3 v_3^2 - 12 w_7 w_4^3 w_3^3 v_3^3 - 48 w_7^2 w_4^2 w_3^3 c s^2 - 12 w_4^2 w_3^3 c s^2 + w_7^2 w_4^3 w_3^2 + 6 w_7^2 w_4^3 w_3 c s^2 + 6 w_7 w_4^3 w_3^2 c s^2 - 12 w_7^2 w_4^2 w_3^2 v_3 - 24 w_7 w_4^3 w_3^2 v_3^2 + 7 w_7^2 w_4^2 w_3^3 - 36 w_7^2 w_3^3 c s^2 + 12 w_7 w_4 w_3^3 - 24 w_7 w_4 w_3^3 c s^2 + 24 w_7^2 w_4^3 v_3^2 - 3 w_7^2 w_4^2 w_2^2 + 6 w_7 w_4^3 w_3^2 v_3^2 + 42 w_7^2 w_4^2 w_3^2 c s^2 + 6 w_7^2 w_4^3 w_3^3 c s^2 + 42 w_7 w_4^2 w_3^3 v_3^2 - 21 w_7 w_4^3 w_3^3 - 12 w_7^2 w_4^2 w_3^3 c s^2 + 12 w_7 w_4^3 w_3^2 v_3^2 - 3 w_4^2 w_3^3 v_3^2 + 6 w_7^2 w_4^3 w_3^3 v_3^3 - 24 w_7^2 w_4^2 w_3^3 c s^2 + 6 w_7^2 w_4^3 w_3^3 v_3^2 + 6 w_7^2 w_4^3 w_3^3 v_3^3 - 42 w_7 w_4^2 w_3^3 c s^2 + 6 w_7^2 w_4^3 w_3^3 v_3^2 - 30 w_7^2 w_4 w_3^3 v_3^2 - 12 w_7 w_4^3 w_3^3 c s^2 + 6 w_7 w_4^3 w_3^2 - 12 w_7 w_4^2 w_3^2 v_3^2 - 3 w_7 w_4^3 w_3^2 + 6 w_7^2 w_4^3 w_3^2 v_3^2 - 12 w_7 w_4^2 w_3^2 c s^2 + 78 w_7^2 w_4 w_3^3 c s^2) \frac{v_2 v_3}{6 w_7^2 w_4^3 w_3^3}$$

$$\begin{aligned}
C_{(D_3^2 D_4^3)}^{(0), \text{MRT2}} = & (78 w_7^2 w_4 c s^2 w_3^3 - w_7^2 w_4^3 w_3^3 - 12 w_7^2 w_4^3 w_3 v_3 + 6 w_7^2 w_4^3 w_3^2 v_3 - 12 w_7^2 w_4^3 v_3^2 + 6 w_7^2 w_4^3 c s^2 w_3 - 24 w_7^2 w_4 c s^2 w_3^2 + 6 w_7^2 w_4^3 v_3^2 - \\
& 12 w_7 w_4^3 w_3^2 v_3^2 + w_7^2 w_4^3 w_3^2 - 12 w_7^2 w_4^2 w_3^2 v_3^2 - 24 w_7 w_4 w_3^3 v_3^2 + 7 w_7^2 w_4^2 w_3^3 - 12 w_7^2 w_4^3 c s^2 w_3^2 + 42 w_7 w_4^2 c s^2 w_3^3 + 12 w_7 w_4 w_3^3 + 24 w_7^2 w_3^3 v_3^2 - 3 w_7^2 w_4^2 w_3^2 + \\
& 6 w_7 w_4^3 w_3^2 v_3^2 + 6 w_7^2 w_4^3 c s^2 w_3^3 + 6 w_4^3 c s^2 w_3^3 - 12 w_7 w_4^2 c s^2 w_3^2 + 42 w_7 w_4^2 w_3^3 v_3^2 - 21 w_7 w_4^2 w_3^3 + 12 w_7^2 w_4 w_3^3 v_3^2 - 3 w_7^2 w_3^3 - 12 w_7^2 w_4^2 c s^2 w_3 - \\
& 24 w_7 w_4 c s^2 w_3^2 + 6 w_7^2 w_4^3 w_3 v_3^2 + 6 w_4^3 w_3^3 v_3^2 + 6 w_7 w_4^2 w_3^2 - 6 w_7^2 w_4 w_3^3 - 36 w_7^2 c s^2 w_3^3 + 6 w_7^2 w_4^3 c s^2 w_3^2 - 12 w_7^2 c s^2 w_3^3 - 48 w_7^2 w_4 c s^2 w_3^3 + 6 w_4^2 w_3^3 - \\
& 30 w_7^2 w_4 w_3^3 v_3^2 + 6 w_7 w_4^3 w_3^2 - 12 w_7 w_4^2 w_3^2 v_3^2 - 12 w_7 w_4 c s^2 w_3^2 + 42 w_7^2 w_4^2 c s^2 w_3^3 - 3 w_7 w_4^3 w_3^2 + 6 w_7^2 w_4^3 w_3^2 v_3^2) \frac{v_2 v_3}{6 w_7^2 w_4^3 w_3^3}
\end{aligned}$$

$$\begin{aligned} C_{(0),\text{CLBBM1}}^{(0)} &= (-\omega_7^2 w_3^4 w_3^3 - 12 w_7^2 w_3^4 w_3 v_3^2 - 6 w_7^2 w_4^2 w_3^3 v_3^2 - 12 w_7^2 w_4^3 c s^2 w_3^2 + 12 w_4^2 w_3^3 v_3^3 + 72 w_7 w_4^2 c s^2 w_3^3 + 6 w_7^2 w_4^3 v_3^2 + 6 w_7^2 w_4^3 c s^2 w_3^3 - 24 w_7 w_4^2 c s^2 w_3^2 + \\ &+ 18 w_4^3 c s^2 w_3^3 + w_7^2 w_3^4 w_3^2 - 6 w_7^2 w_4^2 w_3^2 v_3^2 - 24 w_7 w_4 w_3^3 v_3^2 + 7 w_7^2 w_2^2 w_3^3 + 36 w_7^2 w_4 c s^2 w_3^3 + 12 w_7 w_4 w_3^3 - 3 w_7^2 w_4^2 w_3^2 - 12 w_7^2 w_4 c s^2 w_3^2 + 6 w_7^2 w_4^3 c s^2 w_3 - 36 w_4^2 c s^2 w_3^3 + 12 w_7 w_4^3 c s^2 w_3^2 + 12 w_7 w_4^2 w_3^2 v_3^2 - 21 w_7 w_4^2 w_3^3 - 36 w_7^2 w_4^2 c s^2 w_3^3 - 3 w_7^2 w_3^3 + 6 w_7^2 w_4^2 w_3 v_3^2 - 6 w_4^3 w_3^3 v_3^2 - 24 w_7 w_4^3 c s^2 w_3^3 + 6 w_7 w_4^2 w_3^2 + \\ &+ 36 w_7^2 w_4^2 c s^2 w_3^2 - 6 w_7^2 w_4 w_3^3 + 6 w_4^2 w_3^3 + 12 w_7 w_4 w_3^3 v_3^2 - 24 w_7 w_4 c s^2 w_3^3 - 12 w_7 w_4^2 c s^2 w_3 + 6 w_7 w_4^3 w_3^3 - 3 w_7 w_4^3 w_3^2 + 6 w_7^2 w_4^2 w_3^2 v_3^2 - 12 w_7^2 c s^2 w_3^3) \frac{v_2^2 v_3}{6 w_7^2 w_4^3 w_3^3} \end{aligned}$$

$$C_{\frac{D}{D}y_3^3}^{(0), \text{CLBM2}} = (-\omega_7^2 w_3^3 w_3^3 - 36 w_7^2 w_4^2 w_3^3 c s^2 - 36 w_4^2 w_3^3 c s^2 - 12 w_7^2 w_4^3 w_3 t_3^2 + 6 w_7^2 w_4^3 w_3 c s^2 - 6 w_7^2 w_4^2 w_3^3 v_3 + 12 w_4^2 w_3^3 v_3 + 6 w_7^2 w_4^3 v_3 + w_2^2 w_4^3 w_3^2 - 24 w_7 w_4^3 w_3^2 c s^2 - 24 w_7 w_4 w_3^3 c s^2 - 6 w_7^2 w_4^2 w_3^2 v_3 - 24 w_7 w_4 w_3^3 v_3 + 36 w_7^2 w_4^2 w_3^2 c s^2 + 7 w_7^2 w_4^2 w_3^3 + 12 w_7 w_4 w_3^3 + 12 w_7 w_4^3 w_3^2 c s^2 - 3 w_7^2 w_4^2 w_3^2 - 12 w_7^2 w_4^3 c s^2 + 12 w_7 w_4^3 w_3^2 v_3^2 - 21 w_7 w_4^2 w_3^3 - 12 w_3^2 w_4 w_3^2 c s^2 + 72 w_7 w_4^2 w_3^3 c s^2 - 3 w_4^3 w_3^3 + 6 w_7^2 w_4^2 w_3 v_3^2 + 18 w_7^2 w_4^2 w_3^2 c s^2 + 6 w_7^2 w_4^3 w_3^2 c s^2 - 6 w_4^3 w_3^3 v_3^2 + 6 w_7 w_4^2 w_3^2 - 12 w_7 w_4^3 w_3^2 c s^2 - 6 w_7^2 w_4 w_3^3 + 6 w_4^2 w_3^3 + 12 w_7^2 w_4 w_3^3 v_3^2 - 24 w_7 w_4^2 w_3^2 c s^2 + 36 w_7^2 w_4 w_3^3 c s^2 + 6 w_7 w_4^3 w_3^3 - 3 w_7 w_4^3 w_3^2 + 6 w_7^2 w_4^3 w_3^2 v_3^2 - 12 w_7 w_4^3 w_3^2 c s^2) \frac{v_2 v_3}{6 \sqrt{2} \omega_7^3 w_4^3 w_3^3}$$

coefficient  $C_{D_y D_z^3 v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_2 \partial x_3^3}$ :

$$C_{\substack{(0), \text{SRT} \\ D_0 D_1^3 v_2}} = (36 - 56\omega^2 cs^2 + 54\omega v_3^2 + 4\omega^3 cs^2 - 96cs^2 - 54\omega - \omega^3 - 36v_3^2 + 20\omega^2 + \omega^3 v_3^2 + 144\omega cs^2 - 20\omega^2 v_3^2) \frac{\rho v_3}{12\omega^3}$$

$$\begin{aligned} C_{\text{D}_1 \text{D}_2 v_2}^{(0), \text{MRT1}} = & \\ & (4w_7^2 w_4^3 c s^2 - 6w_4^3 - 36w_7 w_4^2 + 12w_4^2 + w_7^2 w_4^3 v_3^2 + 9w_7 w_4^3 + 12w_7^2 v_3^2 - 44w_7^2 w_4^2 c s^2 - 36w_7 w_4 v_3^2 - 48w_7^2 c s^2 + 24w_7 w_4 - 8w_7^2 w_4^2 v_3^2 - 36w_7 w_4 c s^2 + 6w_4^3 c s^2 - 12w_7^2 w_4 + 48w_7 w_4^2 c s^2 + 6w_4^3 v_3^2 + 48w_7 w_4^2 v_3^2 + 90w_7^2 w_4 c s^2 - 12w_7 w_4^3 c s^2 - w_7^2 w_4^3 - 12w_4^2 c s^2 - 12w_7 w_4^3 v_3^2 - 12w_4^2 v_3^2 + 11w_7^2 w_4^2) \frac{\rho v_3}{12w_7^2 w_4^3} \end{aligned}$$

$$\begin{aligned} C_{\substack{(0), \text{MRT2} \\ \mathbf{D}_y \mathbf{D}_z^3 v_2}} = & (-48\omega_7^2 cs^2 - 6\omega_3^3 - 36\omega_7\omega_4 cs^2 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3 v_3^2 + 9\omega_7\omega_4^3 - 44\omega_7^2\omega_4^2 cs^2 + 12\omega_7^2 v_3^2 - 36\omega_7\omega_4 v_3^2 + 4\omega_7^2\omega_4^3 cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2 v_3^2 - 12\omega_7^2\omega_4 - 12\omega_7\omega_4^3 cs^2 + 6\omega_4^3 v_3^2 + 48\omega_7\omega_4^2 v_3^2 - 12\omega_4^2 cs^2 - \omega_7^2\omega_4^3 + 90\omega_7^2\omega_4 cs^2 - 12\omega_7\omega_4^3 v_3^2 + 6\omega_4^3 cs^2 + 48\omega_7\omega_4^2 cs^2 - 12\omega_4^2 v_3^2 + 11\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3} \end{aligned}$$

$$\begin{aligned} C_{\substack{\mathbf{D}_y \mathbf{D}_z^3 v_2}}^{(0), \text{CLBM1}} = & (-6w_4^3 - 30w_7w_4^3cs^2 - 36w_7w_4^2 - 60w_4^2cs^2 + 12w_4^2 + w_7^2w_4^3v_3^2 + 9w_7w_4^3 + 30w_4^3cs^2 + 12w_7^2v_3^2 + 96w_7w_4^2cs^2 - 60w_7w_4v_3^2 + 24w_7w_4 - 14w_7^2w_4^2v_3^2 + \\ & 18w_7^2w_4cs^2 - 12w_7^2w_4 + 12w_7^2w_4v_3^2 - 26w_7^2w_4^2cs^2 - 6w_4^3v_3^2 - 36w_7w_4cs^2 + 48w_7w_4^2v_3^2 + 4w_7^2w_4^3cs^2 - w_7^2w_4^3 - 6w_7w_4^3v_3^2 + 12w_4^2v_3^2 + 11w_7^2w_4^2) \frac{\rho v_3}{12w_7^2w_4^3} \end{aligned}$$

$$\begin{aligned} C_{\substack{D_y D^3 v_2}}^{(0), \text{CLBM2}} = & (-6\omega_4^3 - 36\omega_7\omega_4^2 + 4\omega_7^2\omega_4^3)cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 - 26\omega_7^2\omega_4^2cs^2 - 12\omega_7^2\omega_4 + \\ & 12\omega_7^2\omega_4v_3^2 + 18\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 - 6\omega_4^3v_3^2 + 96\omega_7\omega_4^2cs^2 + 48\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^3v_3^2 - 30\omega_7\omega_4^3cs^2 + 12\omega_4^2v_3^2 - 60\omega_4^2cs^2 + 11\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3} \end{aligned}$$

**coefficient**  $C_{D_y D_z^3 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_2 \partial x_3^3}$ :

$$C_{\frac{D_y}{D_z}v_3}^{(0),\text{SRT}} = (12 - 56\omega^2 cs^2 + 18\omega v_3^2 + 4\omega^3 cs^2 - 96cs^2 - 18\omega - \omega^3 - 12v_3^2 + 8\omega^2 + 3\omega^3 v_3^2 + 144\omega cs^2 - 12\omega^2 v_3^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{\substack{D_3 \\ D_3 \\ v_3}}^{(0), \text{MRT1}} = -(\omega_7^2 \omega_3^3 \omega_3^3 - 18 \omega_7^2 \omega_3^3 \omega_3 v_3^2 - 12 \omega_7 \omega_4^3 \omega_3^3 c s^2 - 12 \omega_4^2 \omega_3^3 v_3^2 + 12 \omega_7^2 \omega_4^3 v_3^2 - 12 \omega_7 \omega_4^3 \omega_3^3 v_3^2 - 32 \omega_7^2 \omega_4^2 \omega_3^3 c s^2 - 12 \omega_4^2 \omega_3^3 c s^2 + 2 \omega_7^2 \omega_4^3 \omega_3^2 + 6 \omega_7^2 \omega_4^3 \omega_3 c s^2 + 12 \omega_7 \omega_4^3 \omega_3^2 c s^2 + 12 \omega_7^2 \omega_4^2 \omega_3^2 v_3^2 - 12 \omega_7 \omega_4^3 \omega_3^2 v_3^2 + 3 \omega_7^2 \omega_4^2 \omega_3^2 - 12 \omega_7^2 \omega_4^3 \omega_3^2 c s^2 - 12 \omega_7 \omega_4^3 \omega_3^2 c s^2 + 24 \omega_7^2 \omega_4^3 \omega_3^2 v_3^2 - 6 \omega_7^2 \omega_4^2 \omega_3^2 + 12 \omega_7 \omega_4^3 \omega_3^2 v_3^2 + 48 \omega_7^2 \omega_4^2 \omega_3^2 c s^2 + 6 \omega_4^3 \omega_3^3 c s^2 + 4 \omega_7^2 \omega_4^3 \omega_3^2 c s^2 + 36 \omega_7 \omega_4^2 \omega_3^2 v_3^2 - 6 \omega_7 \omega_4^2 \omega_3^2 - 12 \omega_7^2 \omega_4^2 \omega_3 c s^2 - 24 \omega_7^2 \omega_4^2 \omega_3^2 c s^2 + 6 \omega_4^3 \omega_3^3 v_3^2 + 3 \omega_7^2 \omega_4^3 \omega_3^2 v_3^2 + 12 \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 36 \omega_7 \omega_4^2 \omega_3^2 c s^2 - 30 \omega_7^2 \omega_4 \omega_3^3 v_3^2 - 12 \omega_7^2 \omega_4^3 \omega_3^2 c s^2 + 3 \omega_7 \omega_4^3 \omega_3^3 - 24 \omega_7^2 \omega_4^2 \omega_3^2 v_3^2 - 6 \omega_7 \omega_4^3 \omega_3^2 - 24 \omega_7 \omega_4^2 \omega_3^2 c s^2 + 36 \omega_7^2 \omega_4 \omega_3^3 c s^2) \frac{v_2 \rho}{12 \omega_7^2 \omega_4^3 \omega_3^3}$$

$$\begin{aligned} C_{\substack{\text{D}_y \text{D}_z \\ v_3}}^{(0), \text{MRT2}} = & (36w_7^2 w_4 c s^2 w_3^3 - w_7^2 w_4^3 w_3^3 - 18w_7^2 w_4^3 w_3 v_3^2 - 12w_4^2 w_3^3 v_3^2 + 6w_7^2 w_4^3 c s^2 w_3 - 24w_7^2 w_4 c s^2 w_3^2 + 12w_7^2 w_4^3 v_3^2 - 12w_7 w_4^3 w_3^2 v_3^2 + 2w_7^2 w_4^3 w_3^2 + 12w_7^2 w_4^2 w_3^2 v_3^2 - 12w_7 w_4^3 v_3^2 + 3w_7^2 w_4^2 w_3^3 - 12w_7^2 w_4^3 c s^2 w_3^2 + 36w_7 w_4^2 c s^2 w_3^2 + 24w_7^2 w_4^3 v_3^2 - 6w_7^2 w_4^2 w_3^2 + 12w_7 w_4^3 w_3^2 v_3^2 + 4w_7^2 w_4^3 c s^2 w_3^2 + 6w_4^3 c s^2 w_3^3 - 24w_7 w_4^2 c s^2 w_3^2 + 36w_7 w_4^2 w_3^2 v_3^2 - 6w_7 w_4^2 w_3^3 - 12w_7^2 w_4^2 c s^2 w_3^2 - 12w_7 w_4 c s^2 w_3^2 + 6w_4^3 w_3^2 v_3^2 + 3w_7^2 w_4^3 w_3^2 v_3^2 + 12w_7 w_4^2 w_3^2 - 12w_7 c s^2 w_3^2 + 12w_7 w_4^3 c s^2 w_3^2 - 12w_4^2 c s^2 w_3^3 - 32w_7^2 w_4^2 c s^2 w_3^2 - 30w_7^2 w_4 w_3^3 v_3^2 + 3w_7 w_4^3 w_3^3 - 24w_7 w_4^2 w_3^2 v_3^2 - 12w_7 w_4^3 c s^2 w_3^2 + 48w_7^2 w_4^2 c s^2 w_3^2 - 6w_7 w_4^3 w_3^2)^{\frac{v_2 \rho}{12z_7^2 w_4^3 w_3^3}} \end{aligned}$$

$$\begin{aligned} C_{\substack{\text{D}_y \text{D}_z \\ v_3}}^{(0), \text{CLBM1}} = & (-\omega_7^2 w_4^3 w_3^3 - 18 w_7^2 w_4^3 w_3 v_3^2 - 12 w_7^2 w_4^2 w_3^2 v_3^2 - 12 w_7^2 w_4^3 c s^2 w_3^2 + 12 w_4^2 w_3^3 v_3^2 + 36 w_7 w_4^2 c s^2 w_3^3 + 12 w_7^2 w_3^3 v_3^2 + 4 w_7^2 w_4^3 c s^2 w_3^3 - \\ & 24 w_7 w_4^2 c s^2 w_3^2 + 6 w_4^3 c s^2 w_3^3 + 2 w_7^2 w_4^3 w_3^2 + 12 w_7^2 w_4^2 w_3^2 v_3^2 + 12 w_7 w_4 w_3^3 v_3^2 + 3 w_7^2 w_4^2 w_3^3 + 36 w_2^2 w_4 c s^2 w_3^3 - 24 w_7^2 w_3^3 v_3^2 - 6 w_7^2 w_4^2 w_3^2 - 24 w_7^2 w_4 c s^2 w_3^2 + \\ & 12 w_7 w_4^3 w_3^2 v_3^2 + 6 w_2^2 w_4^3 c s^2 w_3 + 12 w_4^2 c s^2 w_3^3 + 12 w_7 w_4^3 c s^2 w_3^2 - 12 w_7 w_4^2 w_3^2 v_3^2 - 6 w_7 w_4^2 w_3^3 - 32 w_7^2 w_4^2 c s^2 w_3^3 - 6 w_4^3 w_3^3 v_3^2 - 12 w_7 w_4^3 c s^2 w_3^3 + 3 w_7^2 w_4^3 w_3^2 v_3^2 + \\ & 12 w_7 w_4^2 w_3^2 + 48 w_7^2 w_4^2 c s^2 w_3^2 + 30 w_7^2 w_4 w_3^3 v_3^2 - 12 w_7 w_4 c s^2 w_3^3 - 12 w_7^2 w_4^2 c s^2 w_3 + 3 w_7 w_4^3 w_3^2 - 24 w_7 w_4^2 w_3^2 v_3^2 - 6 w_7 w_4^3 w_3^2 - 12 w_7^2 c s^2 w_3^3) \frac{v_2^2 \rho}{12 w_7^2 w_4^3 w_3^3} \end{aligned}$$

$$\begin{aligned} C_{\substack{(0), \text{CLBM2} \\ \text{D}_y \text{D}_z^3 v_3}} &= (-w_7^2 w_4^3 w_3^3 - 32 w_7^2 w_4^2 w_3^3 c s^2 - 12 w_4^2 w_3^3 c s^2 - 18 w_7^2 w_4^3 w_3 v_3 + 6 w_7^2 w_4^3 w_3 c s^2 - 12 w_7^2 w_4^2 w_3^3 v_3 + 12 w_4^2 w_3^3 v_3 + 12 w_7^2 w_4^3 v_3 + 2 w_7^2 w_4^3 w_3^2 - \\ &12 w_7 w_4^3 w_3^3 c s^2 - 12 w_7 w_4 w_3^3 c s^2 + 12 w_7^2 w_4^2 w_3^2 v_3^2 + 12 w_7 w_4 w_3^3 v_3^2 + 48 w_7^2 w_4^2 w_3^2 c s^2 + 3 w_7^2 w_4^2 w_3^3 - 24 w_7^2 w_3^3 v_3^2 + 12 w_7 w_4^3 w_3^2 c s^2 - 6 w_7^2 w_4^2 w_3^2 + \\ &12 w_7 w_4^3 w_3^2 v_3^2 - 12 w_7 w_4^2 w_3^3 c s^2 - 12 w_7 w_4^2 w_3^3 v_3 - 6 w_7 w_4^2 w_3^3 - 24 w_7^2 w_4 w_3^2 c s^2 + 36 w_7 w_4^2 w_3^3 c s^2 + 6 w_4^3 w_3^3 c s^2 + 4 w_7^2 w_3^3 w_3^3 c s^2 - 6 w_4^3 w_3^3 v_3^2 + 3 w_7^2 w_4^3 w_3^3 v_3^2 + \\ &12 w_7 w_4^2 w_3^2 - 12 w_7^2 w_4^2 w_3 c s^2 + 30 w_7^2 w_4 w_3^3 v_3^2 - 24 w_7 w_4^2 w_3^2 c s^2 + 36 w_7 w_4 w_3^3 c s^2 + 3 w_7 w_4^3 w_3^3 - 24 w_7 w_4^2 w_3^2 v_3 - 6 w_7 w_4^3 w_3^2 - 12 w_7^2 w_4^2 w_3^2 c s^2) \frac{v_2 \rho}{1232 w_3^3 w_4^3 w_5^3} \end{aligned}$$

**coefficient**  $C_{D_z^4 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_3^4}$ :

$$C_{\frac{D_4^4}{\rho}}^{(0),\text{SRF}} = (-14\omega^2 cs^2 - 108\omega v_3^2 - 42\omega^2 v_3^4 - 72\omega cs^4 + 6\omega^3 cs^2 v_3^2 + 216\omega cs^2 v_3^2 - 72v_3^4 + \omega^3 cs^2 - 144cs^2 v_3^2 - 24cs^2 + 3\omega^3 v_3^4 - 3\omega^3 cs^4 - 84\omega^2 cs^2 v_3^2 + 72v_3^2 - 3\omega^3 v_3^2 + 48cs^4 + 108\omega v_3^4 + 30\omega^2 cs^4 + 36\omega cs^2 + 42\omega^2 v_3^2) \frac{1}{24\omega^3}$$

$$C_{\substack{D_4 \\ \rho}}^{(0), \text{MRT1}} = (\omega_7^2 \omega_4^3 c s^2 + 6 \omega_7 \omega_4^3 c s^4 - 24 \omega_7 w_4 v_3^2 c s^2 - 24 \omega_4^2 v_3^4 - 3 \omega_7^2 \omega_3^3 v_3^2 - 18 \omega_7 w_3^3 v_3^4 - 96 \omega_7^2 v_3^2 c s^2 - 24 \omega_7 w_4^2 c s^4 + 24 \omega_7^2 w_4 v_3^4 - 72 \omega_2^2 w_4^2 v_3^2 c s^2 - 24 \omega_4^2 v_3^2 c s^2 - 8 \omega_7^2 w_4^2 c s^2 + 48 \omega_7 w_4 v_3^2 - 12 \omega_7 w_4^3 v_3^2 c s^2 + 72 \omega_7 w_4^2 v_3^4 - 48 \omega_7^2 w_4 c s^4 + 24 \omega_7^2 w_4^2 v_3^2 - 24 \omega_7 w_4 c s^2 + 12 w_3^3 v_3^4 + 156 \omega_7^2 w_4 v_3^2 c s^2 + 24 \omega_7^2 w_4^2 c s^4 - 48 \omega_7 w_4 v_3^4 + 24 \omega_7 w_4^2 c s^2 - 24 \omega_7^2 w_4 v_3^2 - 24 \omega_7^2 w_4^2 v_3^4 + 24 \omega_7 w_4 c s^4 - 12 w_3^3 v_3^2 + 24 \omega_7^2 c s^4 - 72 \omega_7 w_4^2 v_3^2 + 12 \omega_7^2 w_4 c s^2 - 6 \omega_7 w_4^3 c s^2 + 48 \omega_7 w_4^2 v_3^2 c s^2 - 3 \omega_7^2 w_4^3 c s^4 + 18 \omega_7 w_4^3 v_3^2 + 24 \omega_4^2 v_3^2 + 12 \omega_4^2 v_3^2 c s^2 + 6 \omega_7^2 w_4^3 v_3^2 c s^2 + 3 \omega_7^2 w_4^3 v_3^4) \frac{1}{24 \omega_7^2 w_4^3}$$

$$\begin{aligned} C_{\frac{D_4^4}{4}}^{(0),\text{MRT2}} = & (-48\omega_7^2 w_4 c s^4 - 24 w_7 w_4 c s^2 - 24 w_7 w_4^2 c s^4 - 24 w_4^2 v_3^4 - 3 w_2^2 \omega_4^3 v_3^2 - 18 w_7 w_4^3 v_3^4 + 156 w_7^2 w_4 c s^2 v_3^2 - 8 w_7^2 w_4^2 c s^2 + 12 w_4^3 c s^2 v_3^2 + \\ & 6 w_7^2 w_3^4 c s^2 v_3^2 + 24 w_7^2 w_4 v_3^4 + 48 w_7 w_4 v_3^2 + w_7^2 w_4^3 c s^2 + 72 w_7 w_2^2 v_3^4 + 48 w_7 w_4^2 c s^2 v_3^2 + 24 w_7^2 w_4^2 v_3^2 + 6 w_7 w_4^3 c s^4 + 12 w_3^4 v_3^4 - 96 w_7^2 c s^2 v_3^2 - 48 w_7 w_4 v_3^4 - \\ & 24 w_7^2 w_4 v_3^2 - 24 w_7 w_4 c s^2 v_3^2 - 24 w_2^2 w_4^3 v_3^4 - 6 w_7 w_4^3 c s^2 - 12 w_4^2 v_3^4 - 3 w_2^2 \omega_4^3 c s^4 - 72 w_7 w_4^2 v_3^2 + 24 w_7 w_4 c s^4 + 24 w_7^2 c s^4 + 12 w_7^2 w_4 c s^2 - \\ & 12 w_7 w_4^3 c s^2 v_3^2 + 18 w_7 w_4^3 v_3^2 + 24 w_7 w_4^4 c s^4 + 24 w_7 w_4^2 c s^2 - 72 w_7 w_4^2 c s^2 v_3^2 + 24 w_4^2 v_3^2 - 24 w_4^2 c s^2 v_3^2 + 3 w_7^2 w_4^3 v_3^4) \frac{1}{24 w_7^2 \omega_4^3} \end{aligned}$$

$$C_{D_4^2 \rho}^{(0),\text{CLBM1}} = (108w_3^4c^2v_2^2 + 6w_2^2w_3^4c^2v_2^2 - 6w_7w_4^3c^8 - 3w_2^2w_3^4c^4 + 144w_7w_4^2c^2v_2^2 - 72w_2^4v_3^4 - 3w_2^2w_4^3v_2^2 - 30w_7w_4^3v_4^2 + 24w_7w_4^2c^4 + 24w_7w_4^2c^2s^2 + 24w_7w_4c^4 + 72w_7w_4^2v_3^4 - 36w_7w_4c^2v_2^2 + 12w_2^2w_4^2v_3^2 + 24w_7^2c^8 + 12w_7w_4c^2s^2 + 36w_4^3v_4^2 - 24w_7w_4^2c^4 - 72w_7w_4^3c^2v_2^2 -$$

$$8\omega_7^2\omega_4^2cs^2 - 12\omega_7^2\omega_4^2v_3^4 - 36\omega_4^3v_3^2 - 48\omega_7^2\omega_4cs^4 - 24\omega_7\omega_4cs^2 - 12\omega_7^2\omega_4^2cs^2v_3^2 - 72\omega_7\omega_4^2v_3^2 - 216\omega_4^2cs^2v_3^2 + \omega_7^2\omega_4^3cs^2 + 6\omega_7\omega_4^3cs^4 + 36\omega_4^3v_3^2 + 72\omega_7\omega_4cs^2v_3^2 + 72\omega_4^2v_3^2 + 3\omega_7^2\omega_4^3v_3^4) \frac{1}{24\omega_7^2\omega_4^3}$$

$$C_{\text{D}_z^4 v_3}^{(0), \text{CLBM2}} = \\ (\omega_7^2\omega_4^3cs^2 - 72\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^3v_3^4 + 72\omega_7\omega_4v_3^2cs^2 + 6\omega_7\omega_4^3cs^4 - 72\omega_7\omega_4^3v_3^2cs^2 - 48\omega_7^2\omega_4cs^4 - 24\omega_7\omega_4cs^2 - 24\omega_7\omega_4^2cs^4 + 72\omega_7\omega_4^2v_3^4 - 12\omega_7^2\omega_4^2v_3^2cs^2 - 216\omega_4^2v_3^2cs^2 + 12\omega_7^2\omega_4^2v_3^4 - 8\omega_7^2\omega_4^2cs^2 + 36\omega_4^3v_3^4 + 24\omega_7\omega_4cs^4 + 24\omega_7^2cs^4 + 12\omega_7^2\omega_4cs^2 - 36\omega_7^2\omega_4v_3^2cs^2 - 12\omega_7^2\omega_4^2v_3^4 + 24\omega_7^2\omega_4^2cs^4 - 36\omega_4^3v_3^2 + 24\omega_7\omega_4^2cs^2 - 72\omega_7\omega_4^2v_3^2 + 108\omega_4^3v_3^2cs^2 + 6\omega_7^2\omega_4^3v_3^2cs^2 + 30\omega_7\omega_4^3v_3^2 - 6\omega_7\omega_4^3cs^2 - 3\omega_7^2\omega_4^3cs^4 + 144\omega_7\omega_4^2v_3^2cs^2 + 72\omega_4^2v_3^2 + 3\omega_7^2\omega_4^3v_3^4) \frac{1}{24\omega_7^2\omega_4^3}$$

**coefficient**  $C_{\text{D}_z^4 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_3^4}$ :

$$C_{\text{D}_z^4 v_3}^{(0), \text{SRT}} = (24 - 26\omega^2 cs^2 + 54\omega v_3^2 + \omega^3 cs^2 - 48cs^2 - 36\omega - \omega^3 - 36v_3^2 + 14\omega^2 + 2\omega^3 v_3^2 + 72\omega cs^2 - 22\omega^2 v_3^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\text{D}_z^4 v_3}^{(0), \text{MRT1}} = \\ (\omega_7^2\omega_4^3cs^2 - 6\omega_4^3 - 24\omega_7\omega_4^2 + 12\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3 - 12\omega_7^2v_3^2 - 20\omega_7^2\omega_4^2cs^2 - 12\omega_7\omega_4v_3^2 - 24\omega_7^2cs^2 + 12\omega_7\omega_4 - 16\omega_7^2\omega_4^2v_3^2 - 12\omega_7\omega_4cs^2 + 6\omega_4^3cs^2 - 6\omega_7^2\omega_4 + 24\omega_7\omega_4^2cs^2 + 24\omega_7^2\omega_4v_3^2 + 6\omega_4^3v_3^2 + 24\omega_7\omega_4^2v_3^2 + 42\omega_7^2\omega_4cs^2 - 6\omega_7\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 12\omega_4^2cs^2 - 6\omega_7\omega_4^2v_3^2 + 12\omega_4^2v_3^2 + 8\omega_7\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\text{D}_z^4 v_3}^{(0), \text{MRT2}} = \\ (-24\omega_7^2cs^2 - 6\omega_4^3 - 12\omega_7\omega_4cs^2 - 24\omega_7\omega_4^2 + 12\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3 - 20\omega_7^2\omega_4^2cs^2 - 12\omega_7^2v_3^2 - 12\omega_7\omega_4v_3^2 + \omega_7^2\omega_4^3cs^2 + 12\omega_7\omega_4 - 16\omega_7^2\omega_4^2v_3^2 - 6\omega_7^2\omega_4 + 24\omega_7\omega_4v_3^2 - 6\omega_7\omega_4^2cs^2 + 6\omega_4^3v_3^2 + 24\omega_7\omega_4^2cs^2 - 12\omega_4^2v_3^2 + 8\omega_7\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\text{D}_z^4 v_3}^{(0), \text{CLBM1}} = (-18\omega_4^3 - 24\omega_7\omega_4^3cs^2 - 24\omega_7\omega_4^2 - 60\omega_4^2cs^2 + 36\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4^3 + 30\omega_4^3cs^2 - 12\omega_7^2v_3^2 + 72\omega_7\omega_4^2cs^2 + 60\omega_7\omega_4v_3^2 - 12\omega_7\omega_4 - 2\omega_7^2\omega_4^2v_3^2 - 30\omega_7^2\omega_4^2v_3^2 - 30\omega_7^2\omega_4cs^2 + 6\omega_7^2\omega_4 - 12\omega_7^2\omega_4v_3^2 - 2\omega_7^2\omega_4^2cs^2 + 24\omega_7^2cs^2 + 42\omega_7^3v_3^2 - 12\omega_7\omega_4cs^2 + 24\omega_7\omega_4^2v_3^2 + \omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 24\omega_7\omega_4^3v_3^2 - 84\omega_4^2v_3^2 + 2\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\text{D}_z^4 v_3}^{(0), \text{CLBM2}} = \\ (-18\omega_4^3 - 24\omega_7\omega_4^2 + \omega_7^2\omega_4^3cs^2 + 36\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4^3 + 24\omega_7^2cs^2 - 12\omega_7^2v_3^2 - 12\omega_7\omega_4cs^2 + 60\omega_7\omega_4v_3^2 - 12\omega_7\omega_4 + 2\omega_7^2\omega_4^2v_3^2 - 2\omega_7^2\omega_4^2cs^2 + 6\omega_7\omega_4 - 12\omega_7\omega_4v_3^2 - 30\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 + 42\omega_4^3v_3^2 + 72\omega_7\omega_4^2cs^2 + 24\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 - 24\omega_7\omega_4^3v_3^2 - 24\omega_7\omega_4^3cs^2 - 84\omega_4^2v_3^2 - 60\omega_4^2cs^2 + 2\omega_7\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

## References

- [1] T. Krüger, H. Kusumaatmaja, A. Kuzmin, O. Shardt, G. Silva, E. M. Viggen, The lattice Boltzmann method, Springer International Publishing 10 (978-3) (2017) 4–15.