

# D3Q7 ADE,

## a supplementary material for

# Lattice Boltzmann Method Analysis Tool (LBMAT)

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## 1 Global definitions

In  $\mathbb{R}^3$ , the position and velocity vectors are given by  $\mathbf{x} = (x_1, x_2, x_3)^T$  and  $\mathbf{v} = (v_1, v_2, v_3)^T$ , respectively.

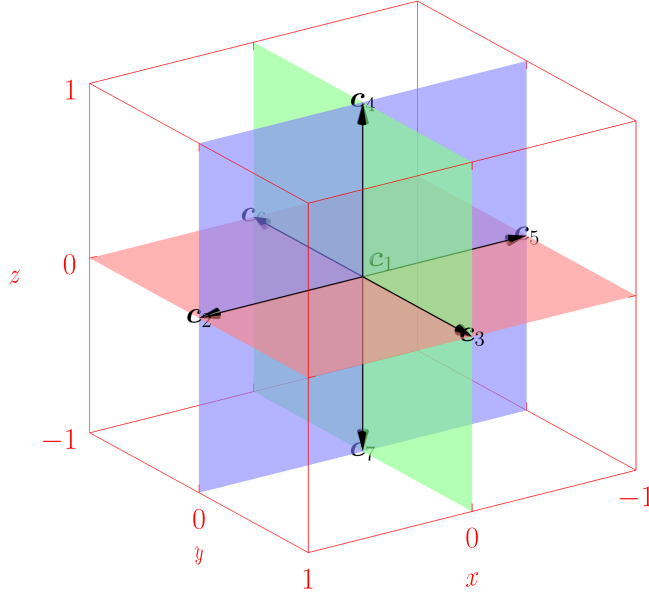
## 1.1 Discrete velocity vectors

Discrete velocity vectors and the lattice speed of sound are defined by

$$\{\mathbf{c}_i\}_{i=1}^7 = \left( \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix} \right),$$

$$c_s = \frac{1}{2},$$

respectively [1].



## 1.2 Raw and central moments

The raw and central moments are defined by

$$m_{\alpha} := \sum_{i=1}^7 f_i \mathbf{c}_i^{\alpha},$$

and

$$k_{\alpha} := \sum_{i=1}^7 f_i (\mathbf{c}_i - \mathbf{v})^{\alpha},$$

respectively, where  $\alpha = (\alpha_1, \alpha_2, \alpha_3) \in \mathbb{Z}^3$  denotes a multi-index (as a row vector) and  $\mathbf{c}_i^{\alpha} := \prod_{j=1}^3 [\mathbf{c}_i]_j^{\alpha_j}$ .

## 1.3 Transformation matrix M

Matrix  $\mathbf{M}$ , that defines macroscopic quantities (moments)  $\boldsymbol{\mu}$  by

$$\boldsymbol{\mu} = \mathbf{M} \mathbf{f},$$

with  $\mathbf{f} = (f_1, f_2, \dots, f_7)^T$ , is selected such that

$$\boldsymbol{\mu} = \left( m_{(0,0,0)}, m_{(1,0,0)}, m_{(0,1,0)}, m_{(0,0,1)}, m_{(2,0,0)}, m_{(0,2,0)}, m_{(0,0,2)} \right)^T,$$

i.e.,  $\mathbf{M}$  is given by

$$\mathbf{M} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 \end{pmatrix}.$$

## 1.4 Equilibrium

The corresponding equilibrium raw moments are defined using the continuous Maxwell–Boltzmann distribution function [1]

$$f^{(eq)}(\boldsymbol{\xi}) = \frac{\rho}{(2\pi c_s^2)^{\frac{3}{2}}} \exp\left(-\frac{\|\boldsymbol{\xi} - \mathbf{v}\|^2}{2c_s^2}\right)$$

as

$$m_{\boldsymbol{\alpha}}^{(eq)} = \int_{\mathbb{R}^3} \boldsymbol{\xi}^{\boldsymbol{\alpha}} f^{(eq)}(\boldsymbol{\xi}) d\boldsymbol{\xi},$$

where  $\alpha_i \in \{0, 1, 2\}$ ,  $i = 1, 2, 3$ . Hence, the equilibrium moments  $\boldsymbol{\mu}^{(eq)}$  satisfy

$$\boldsymbol{\mu}^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho(v_1^2 + c_s^2) \\ \rho(v_2^2 + c_s^2) \\ \rho(v_3^2 + c_s^2) \end{pmatrix}.$$

## 2 Spatial EPDEs

### 2.1 SRT

#### 2.1.1 Definitions

Collision operator  $\mathbf{C}$ :

$$\mathbf{C}(\mathbf{f}) = \omega \left( \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)} - \mathbf{f} \right),$$

$\omega \in (0, 2)$ .

#### 2.1.2 Conservation of mass equation



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[illegible]

$$\begin{aligned}
& + (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_1 v_2}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_4 \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& C_5 \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 - \omega^2 + 3\omega) \frac{3\delta_l^2 \delta_t \rho v_2}{2\omega^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + \\
& (34cs^2\omega^2 - 2cs^2\omega^3 - 2v_2^2\omega^2 + 60cs^2 + v_2^2\omega^3 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_1 v_2}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} \\
& + C_6 \frac{\delta_l^4}{4\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + (-26cs^2\omega^2 + cs^2\omega^3 - 126v_2^2\omega + 50v_2^2\omega^2 - 48cs^2 - 4v_2^2\omega^3 + 84v_2^2 + 72cs^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& (-26cs^2\omega^2 + 84v_1^2 + cs^2\omega^3 - 48cs^2 + 72cs^2\omega + 50v_1^2\omega^2 - 4v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_7 \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2^3} + \\
& (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_1 v_2}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_8 \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& C_9 \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{10} \frac{\delta_l^4}{24\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_2^4} + C_{11} \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 - \omega^2 + 3\omega) \frac{\delta_l^2 \delta_t^2 \rho}{2\omega^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_3}{12\omega^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_1}{12\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_1 v_3}{6\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + (34cs^2\omega^2 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega - 2v_1^2\omega^2 + v_1^2\omega^3) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} \\
& + (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_1 v_3}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{12} \frac{\delta_l^4 \rho v_3}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& C_{13} \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_3}{12\omega^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + (36 - \omega^3 + 20\omega^2 - 54\omega) \frac{\delta_l^2 \delta_t \rho v_2}{12\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& (-20 + \omega^3 - 12\omega^2 + 30\omega) \frac{\delta_l^3 \rho v_3 v_2}{2\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + (-20 + \omega^3 - 12\omega^2 + 30\omega) \frac{\delta_l^3 \rho v_1 v_3}{2\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + \\
& (-20 + \omega^3 - 12\omega^2 + 30\omega) \frac{\delta_l^3 \rho v_1 v_2}{2\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + \\
& (-12cs^2\omega^2 + 40v_1^2 + cs^2\omega^3 - 20cs^2 + 30cs^2\omega + 24v_1^2\omega^2 - 2v_1^2\omega^3 - 60v_1^2\omega) \frac{\delta_l^4 v_3 v_2}{\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (132 - 5\omega^3 + 76\omega^2 - 198\omega) \frac{\delta_l^4 \rho v_1 v_2 v_3}{6\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-56cs^2\omega^2 + 84v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega + 52v_1^2\omega^2 - 5v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_3}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-56cs^2\omega^2 + 84v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega + 52v_1^2\omega^2 - 5v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_3 v_2}{6\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + (34cs^2\omega^2 - 2cs^2\omega^3 - 2v_2^2\omega^2 + 60cs^2 + v_2^2\omega^3 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} \\
& + (-12cs^2\omega^2 + cs^2\omega^3 - 60v_2^2\omega + 24v_2^2\omega^2 - 20cs^2 - 2v_2^2\omega^3 + 40v_2^2 + 30cs^2\omega) \frac{\delta_l^4 v_1 v_3}{\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (-56cs^2\omega^2 + 4cs^2\omega^3 - 126v_2^2\omega + 52v_2^2\omega^2 - 96cs^2 - 5v_2^2\omega^3 + 84v_2^2 + 144cs^2\omega) \frac{\delta_l^4 \rho v_3}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (132 - 5\omega^3 + 76\omega^2 - 198\omega) \frac{\delta_l^4 \rho v_1 v_3 v_2}{6\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (-56cs^2\omega^2 + 4cs^2\omega^3 - 126v_2^2\omega + 52v_2^2\omega^2 - 96cs^2 - 5v_2^2\omega^3 + 84v_2^2 + 144cs^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_l^4 v_3 v_2}{6\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{14} \frac{\delta_l^4 \rho v_3}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + \\
& C_{15} \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 - \omega^2 + 3\omega) \frac{3\delta_l^2 \delta_t \rho v_3}{2\omega^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + \\
& (34cs^2\omega^2 - 2v_3^2\omega^2 + v_3^2\omega^3 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_1 v_3}{6\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} \\
& + C_{16} \frac{\delta_l^4}{4\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-26cs^2\omega^2 + 50v_3^2\omega^2 - 4v_3^2\omega^3 + cs^2\omega^3 + 84v_3^2 - 48cs^2 + 72cs^2\omega - 126v_3^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& (-26cs^2\omega^2 + 84v_1^2 + cs^2\omega^3 - 48cs^2 + 72cs^2\omega + 50v_1^2\omega^2 - 4v_1^2\omega^3 - 126v_1^2\omega) \frac{\delta_l^4 \rho v_3}{12\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& (34cs^2\omega^2 - 2v_3^2\omega^2 + v_3^2\omega^3 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega) \frac{\delta_l^3 \rho}{12\omega^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + (-24 + \omega^3 - 14\omega^2 + 36\omega) \frac{\delta_l^3 \rho v_3 v_2}{6\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} \\
& + (-12cs^2\omega^2 + 24v_3^2\omega^2 - 2v_3^2\omega^3 + cs^2\omega^3 + 40v_3^2 - 20cs^2 + 30cs^2\omega - 60v_3^2\omega) \frac{\delta_l^4 v_1 v_2}{\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (-56cs^2\omega^2 + 52v_3^2\omega^2 - 5v_3^2\omega^3 + 4cs^2\omega^3 + 84v_3^2 - 96cs^2 + 144cs^2\omega - 126v_3^2\omega) \frac{\delta_l^4 \rho v_2}{12\delta_t \omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (-56cs^2\omega^2 + 52v_3^2\omega^2 - 5v_3^2\omega^3 + 4cs^2\omega^3 + 84v_3^2 - 96cs^2 + 144cs^2\omega - 126v_3^2\omega) \frac{\delta_l^4 \rho v_1}{12\delta_t \omega^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (132 - 5\omega^3 + 76\omega^2 - 198\omega) \frac{\delta_l^4 \rho v_1 v_3 v_2}{6\delta_t \omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{17} \frac{\delta_l^4}{4\delta_t \omega^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} +
\end{aligned}$$

$$\begin{aligned}
& (-26cs^2\omega^2 + 50v_3^2\omega^2 - 4v_3^2\omega^3 + cs^2\omega^3 + 84v_3^2 - 48cs^2 + 72cs^2\omega - 126v_3^2\omega) \frac{\delta_t^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (-26cs^2\omega^2 + cs^2\omega^3 - 126v_2^2\omega + 50v_2^2\omega^2 - 48cs^2 - 4v_2^2\omega^3 + 84v_2^2 + 72cs^2\omega) \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{18} \frac{\delta_t^3 \rho}{12\omega^3} \frac{\partial^4 v_3}{\partial t \partial x_3^3} + \\
& (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_t^4 v_1 v_3}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{19} \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& C_{20} \frac{\delta_t^4 \rho v_1}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + (24 - 72cs^2\omega^2 + 6cs^2\omega^3 - 120cs^2 + 180cs^2\omega - \omega^3 + 14\omega^2 - 36\omega) \frac{\delta_t^4 v_3 v_2}{6\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\
& C_{21} \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{22} \frac{\delta_t^4 \rho v_2}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{23} \frac{\delta_t^4}{24\delta_t\omega^3} \frac{\partial^4 \rho}{\partial x_3^4} + C_{24} \frac{\delta_t^4 \rho v_3}{12\delta_t\omega^3} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -36 + 34cs^2\omega^2 + 72v_1^2 - 2cs^2\omega^3 + 60cs^2 - 90cs^2\omega + \omega^3 + 42v_1^2\omega^2 - 20\omega^2 - 3v_1^2\omega^3 + 54\omega - 108v_1^2\omega \\
C_2 &= -14cs^2\omega^2 + 3v_1^4\omega^3 - 84v_1^2cs^2\omega^2 + 72v_1^2 - 42v_1^4\omega^2 + cs^2\omega^3 + 6v_1^2cs^2\omega^3 + 108v_1^4\omega - 24cs^2 + 216v_1^2cs^2\omega - 144v_1^2cs^2 + 36cs^2\omega + \\
& 42v_1^2\omega^2 - 3cs^4\omega^3 + 48cs^4 + 30cs^4\omega^2 - 3v_1^2\omega^3 - 72v_1^4 - 72cs^4\omega - 108v_1^2\omega \\
C_3 &= 24 - 26cs^2\omega^2 - 36v_1^2 + cs^2\omega^3 - 48cs^2 + 72cs^2\omega - \omega^3 - 22v_1^2\omega^2 + 14\omega^2 + 2v_1^2\omega^3 - 36\omega + 54v_1^2\omega \\
C_4 &= 12 - 56cs^2\omega^2 - 12v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 12v_1^2\omega^2 + 8\omega^2 + 3v_1^2\omega^3 - 18\omega + 18v_1^2\omega \\
C_5 &= 36 - 56cs^2\omega^2 - 36v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 20v_1^2\omega^2 + 20\omega^2 + v_1^2\omega^3 - 54\omega + 54v_1^2\omega \\
C_6 &= -14v_1^2cs^2\omega^2 - 84v_1^2v_2^2\omega + 36cs^2v_2^2\omega + v_1^2cs^2\omega^3 - 14cs^2v_2^2\omega^2 + 56v_1^2v_2^2 + 34v_1^2v_2^2\omega^2 + 36v_1^2cs^2\omega + cs^2v_2^2\omega^3 - 24v_1^2cs^2 - 3v_1^2v_2^2\omega^3 - \\
& cs^4\omega^3 + 16cs^4 + 10cs^4\omega^2 - 24cs^4\omega - 24cs^2v_2^2 \\
C_7 &= -36 + 34cs^2\omega^2 - 2cs^2\omega^3 - 108v_2^2\omega + 42v_2^2\omega^2 + 60cs^2 - 3v_2^2\omega^3 + 72v_2^2 - 90cs^2\omega + \omega^3 - 20\omega^2 + 54\omega \\
C_8 &= 36 - 56cs^2\omega^2 + 4cs^2\omega^3 + 54v_2^2\omega - 20v_2^2\omega^2 - 96cs^2 + v_2^2\omega^3 - 36v_2^2 + 144cs^2\omega - \omega^3 + 20\omega^2 - 54\omega \\
C_9 &= 12 - 56cs^2\omega^2 + 4cs^2\omega^3 + 18v_2^2\omega - 12v_2^2\omega^2 - 96cs^2 + 3v_2^2\omega^3 - 12v_2^2 + 144cs^2\omega - \omega^3 + 8\omega^2 - 18\omega \\
C_{10} &= -14cs^2\omega^2 + cs^2\omega^3 - 108v_2^2\omega + 216cs^2v_2^2\omega + 42v_2^2\omega^2 - 84cs^2v_2^2\omega^2 - 24cs^2 + 6cs^2v_2^2\omega^3 - 3v_2^2\omega^3 + 72v_2^2 + 36cs^2\omega - 3cs^4\omega^3 + 48cs^4 + \\
& 108v_2^4\omega - 72v_2^4 + 30cs^4\omega^2 + 3v_2^4\omega^3 - 72cs^4\omega - 144cs^2v_2^2 - 42v_2^4\omega^2 \\
C_{11} &= 24 - 26cs^2\omega^2 + cs^2\omega^3 + 54v_2^2\omega - 22v_2^2\omega^2 - 48cs^2 + 2v_2^2\omega^3 - 36v_2^2 + 72cs^2\omega - \omega^3 + 14\omega^2 - 36\omega \\
C_{12} &= 12 - 56cs^2\omega^2 - 12v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 12v_1^2\omega^2 + 8\omega^2 + 3v_1^2\omega^3 - 18\omega + 18v_1^2\omega \\
C_{13} &= 36 - 56cs^2\omega^2 - 36v_1^2 + 4cs^2\omega^3 - 96cs^2 + 144cs^2\omega - \omega^3 - 20v_1^2\omega^2 + 20\omega^2 + v_1^2\omega^3 - 54\omega + 54v_1^2\omega \\
C_{14} &= 12 - 56cs^2\omega^2 + 4cs^2\omega^3 + 18v_2^2\omega - 12v_2^2\omega^2 - 96cs^2 + 3v_2^2\omega^3 - 12v_2^2 + 144cs^2\omega - \omega^3 + 8\omega^2 - 18\omega \\
C_{15} &= 36 - 56cs^2\omega^2 + 4cs^2\omega^3 + 54v_2^2\omega - 20v_2^2\omega^2 - 96cs^2 + v_2^2\omega^3 - 36v_2^2 + 144cs^2\omega - \omega^3 + 20\omega^2 - 54\omega \\
C_{16} &= -14cs^2v_3^2\omega^2 - 14v_1^2cs^2\omega^2 + 34v_1^2v_3^2\omega^2 + cs^2v_3^2\omega^3 - 3v_1^2v_3^2\omega^3 + v_1^2cs^2\omega^3 + 36v_1^2cs^2\omega - 84v_1^2v_3^2\omega - 24v_1^2cs^2 + 56v_1^2v_3^2 + 36cs^2v_3^2\omega - \\
& cs^4\omega^3 + 16cs^4 + 10cs^4\omega^2 - 24cs^4\omega - 24cs^2v_3^2 \\
C_{17} &= -14cs^2v_3^2\omega^2 + cs^2v_3^2\omega^3 - 84v_3^2v_2^2\omega + 36cs^2v_2^2\omega + 34v_3^2v_2^2\omega^2 - 14cs^2v_2^2\omega^2 + cs^2v_2^2\omega^3 - 3v_3^2v_2^2\omega^3 + 36cs^2v_3^2\omega - cs^4\omega^3 + 16cs^4 + \\
& 10cs^4\omega^2 - 24cs^4\omega + 56v_3^2v_2^2 - 24cs^2v_2^2 - 24cs^2v_3^2 \\
C_{18} &= -36 + 34cs^2\omega^2 + 42v_3^2\omega^2 - 3v_3^2\omega^3 - 2cs^2\omega^3 + 72v_3^2 + 60cs^2 - 90cs^2\omega - 108v_3^2\omega + \omega^3 - 20\omega^2 + 54\omega \\
C_{19} &= 36 - 56cs^2\omega^2 - 20v_3^2\omega^2 + v_3^2\omega^3 + 4cs^2\omega^3 - 36v_3^2 - 96cs^2 + 144cs^2\omega + 54v_3^2\omega - \omega^3 + 20\omega^2 - 54\omega \\
C_{20} &= 12 - 56cs^2\omega^2 - 12v_3^2\omega^2 + 3v_3^2\omega^3 + 4cs^2\omega^3 - 12v_3^2 - 96cs^2 + 144cs^2\omega + 18v_3^2\omega - \omega^3 + 8\omega^2 - 18\omega \\
C_{21} &= 36 - 56cs^2\omega^2 - 20v_3^2\omega^2 + v_3^2\omega^3 + 4cs^2\omega^3 - 36v_3^2 - 96cs^2 + 144cs^2\omega + 54v_3^2\omega - \omega^3 + 20\omega^2 - 54\omega \\
C_{22} &= 12 - 56cs^2\omega^2 - 12v_3^2\omega^2 + 3v_3^2\omega^3 + 4cs^2\omega^3 - 12v_3^2 - 96cs^2 + 144cs^2\omega + 18v_3^2\omega - \omega^3 + 8\omega^2 - 18\omega \\
C_{23} &= -84cs^2v_3^2\omega^2 - 14cs^2\omega^2 + 42v_3^2\omega^2 - 3v_3^2\omega^3 + cs^2\omega^3 + 6cs^2v_3^2\omega^3 + 72v_3^2 - 24cs^2 + 216cs^2v_3^2\omega + 36cs^2\omega - 108v_3^2\omega + 3v_3^4\omega^3 - 3cs^4\omega^3 - \\
& 72v_3^4 + 48cs^4 + 30cs^4\omega^2 - 42v_3^4\omega^2 - 72cs^4\omega + 108v_3^4\omega - 144cs^2v_3^2 \\
C_{24} &= 24 - 26cs^2\omega^2 - 22v_3^2\omega^2 + 2v_3^2\omega^3 + cs^2\omega^3 - 36v_3^2 - 48cs^2 + 72cs^2\omega + 54v_3^2\omega - \omega^3 + 14\omega^2 - 36\omega
\end{aligned}$$

## 2.2 MRT1

### 2.2.1 Definitions

Collision operator  $\mathcal{C}$ :

$$\mathcal{C}(f) = \mathbf{M}^{-1} \mathbf{S} \left( \boldsymbol{\mu}^{(eq)} - \mathbf{M} f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2).$$

### 2.2.2 Conservation of mass equation



attached text file: output\_d3q7\_ade\_mrt1\_symbolic\_pde\_00.txt

$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\ & (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\delta_t \omega_2} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_1 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\ & (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{\rho \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\ & (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{\rho \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_2 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\ & (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho \delta_l^2}{2\omega_3 \delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\ & (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{v_2 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{\rho \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + \\ & (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_3 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{v_3 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + \\ & (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\delta_t \omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\rho \delta_l^2}{2\delta_t \omega_4} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\rho \delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + \\ & (-2 + \omega_2) \frac{cs^2 \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho \delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + (\omega_3 - \omega_3 \omega_2 + \omega_2) \frac{v_2 v_1 \delta_l^2}{\omega_3 \delta_t \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + \\ & (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho \delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} \\ & + (-\omega_4 \omega_2 + \omega_4 + \omega_2) \frac{v_3 v_1 \delta_l^2}{\delta_t \omega_4 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\delta_t \omega_2} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + \\ & (\omega_3 - \omega_3 \omega_4 + \omega_4) \frac{v_3 v_2 \delta_l^2}{\omega_3 \delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_4) \frac{cs^2 \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_3^2} + \\ & (-2 + \omega_4) \frac{v_3 \rho \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 v_3}{\partial x_3^2} + (12 - 12\omega_2 + \omega_2^2) \frac{\delta_t \rho \delta_l}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_5 \omega_2 - 6\omega_5 - 6\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_5 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + C_1 \frac{\rho \delta_l^3}{6\delta_t \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & C_2 \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^3} + (12 + \omega_3^2 - 12\omega_3) \frac{\delta_t \rho \delta_l}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + (3\omega_3^2 - 6\omega_3 + 9\omega_3 \omega_2 - 2\omega_3^2 \omega_2 - 6\omega_2) \frac{v_2 \rho \delta_l^2}{6\omega_3^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + \\ & (-2\omega_3 \omega_2^2 - 6\omega_3 + 9\omega_3 \omega_2 - 6\omega_2 + 3\omega_2^2) \frac{v_1 \rho \delta_l^2}{6\omega_3 \omega_2^2} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + C_3 \frac{v_2 \delta_l^3}{2\omega_3^2 \delta_t \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\ & (-6\omega_3 \omega_2^2 + 6\omega_3^2 - 6\omega_3^2 \omega_2 + \omega_3^2 \omega_2^2 + 6\omega_2^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\ & (6v_1^2 \omega_2^2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 + 18cs^2 \omega_5 \omega_2 + 6cs^2 \omega_2^2 - 12v_1^2 \omega_5 + v_1^2 \omega_5 \omega_2^2 - 6v_1^2 \omega_5 \omega_2 - 12cs^2 \omega_5) \frac{\rho \delta_l^3}{12\delta_t \omega_5 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} \\ & + (12 - 6\omega_6 - 6\omega_3 + \omega_6 \omega_3) \frac{v_2 \rho \delta_l^2}{6\omega_6 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\omega_6 \omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-12\omega_6 cs^2 + 18\omega_6 \omega_3 cs^2 - 12\omega_3 v_2^2 + 6\omega_3^2 cs^2 + \\ & \omega_6 \omega_3^2 v_2^2 + 12\omega_6 v_2^2 - 6\omega_6 \omega_3 v_2^2 - 12\omega_3 cs^2 + 6\omega_3^2 v_2^2 - 3\omega_6 \omega_3^2 cs^2) \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & (-6\omega_3 \omega_2^2 + 6\omega_3^2 - 6\omega_3^2 \omega_2 + \omega_3^2 \omega_2^2 + 6\omega_2^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_3^2 \delta_t \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\ & (12 - 12\omega_4 + \omega_4^2) \frac{\delta_t \rho \delta_l}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (9\omega_4 \omega_2 - 6\omega_4 + 3\omega_4^2 - 6\omega_2 - 2\omega_4^2 \omega_2) \frac{v_3 \rho \delta_l^2}{6\omega_4 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\ & (9\omega_4 \omega_2 - 2\omega_4 \omega_2^2 - 6\omega_4 - 6\omega_2 + 3\omega_2^2) \frac{v_1 \rho \delta_l^2}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3 \delta_l^3}{2\delta_t \omega_4^2 \omega_5 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\ & (-6\omega_4 \omega_2^2 + \omega_4^2 \omega_2^2 + 6\omega_4^2 - 6\omega_4^2 \omega_2 + 6\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\delta_t \omega_4^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \end{aligned}$$

$$\begin{aligned}
& (6v_1^2\omega_2^2 - 3cs^2\omega_5\omega_2^2 - 12cs^2\omega_2 + 18cs^2\omega_5\omega_2 + 6cs^2\omega_2^2 - 12v_1^2\omega_2 + 12v_1^2\omega_5 + v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_5\omega_2 - 12cs^2\omega_5) \frac{\rho\delta_l^3}{12\delta_t\omega_5\omega_2^2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} \\
& + (-6\omega_3 + 9\omega_3\omega_4 - 2\omega_3\omega_4^2 - 6\omega_4 + 3\omega_4^2) \frac{v_3\rho\delta_l^2}{6\omega_3\omega_4^2} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (3\omega_3^2 - 6\omega_3 + 9\omega_3\omega_4 - 6\omega_4 - 2\omega_3^2\omega_4) \frac{v_2\rho\delta_l^2}{6\omega_3^2\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_3\omega_4^2\omega_2 + \omega_3^2\omega_4\omega_2 - 2\omega_3^2\omega_4\omega_2^2 - 2\omega_3\omega_4^2\omega_2^2 + \omega_3\omega_4\omega_2^2 + \omega_3^2\omega_4^2 + \omega_4^2\omega_2^2 + \omega_3^2\omega_4^2\omega_2^2 - 2\omega_3^2\omega_4^2\omega_2 + \omega_3^2\omega_2^2) \frac{2v_3v_2v_1\delta_l^3}{\omega_3^2\delta_t\omega_4^2\omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (3\omega_3^2 + 6\omega_3\omega_4 - 6\omega_3\omega_4^2 + 2\omega_3^2\omega_4^2 + 3\omega_4^2 - 6\omega_3^2\omega_4) \frac{v_3v_2\rho\delta_l^2}{3\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (6\omega_4\omega_2 - 6\omega_4\omega_2^2 + 2\omega_4^2\omega_2^2 + 3\omega_4^2 - 6\omega_4^2\omega_2 + 3\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{3\delta_t\omega_4^2\omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_3\omega_2^2 + 3\omega_3^2 + 6\omega_3\omega_2 - 6\omega_3^2\omega_2 + 2\omega_3^2\omega_2^2 + 3\omega_2^2) \frac{v_2v_1\rho\delta_l^3}{3\omega_3^2\delta_t\omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (6\omega_3^2 - 6\omega_3\omega_4^2 + \omega_3^2\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4) \frac{v_3v_2\rho\delta_l^3}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + (-12\omega_6cs^2 + 18\omega_6\omega_3cs^2 - 12\omega_3v_2^2 + 6\omega_3^2cs^2 + \omega_6\omega_3^2v_2^2 + \\
& 12\omega_6v_2^2 - 6\omega_6\omega_3v_2^2 - 12\omega_3cs^2 + 6\omega_3^2v_2^2 - 3\omega_6\omega_3cs^2) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (12 - 6\omega_7 - 6\omega_4 + \omega_7\omega_4) \frac{v_3\rho\delta_l^2}{6\omega_7\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_3} + \\
& C_9 \frac{v_1\delta_l^3}{2\delta_t\omega_7\omega_4^2\omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3} + (-6v_3^2\omega_7\omega_4 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 + v_3^2\omega_7\omega_4^2 - 12v_3^2\omega_4 + 6v_3^2\omega_4^2 + 18\omega_7\omega_4cs^2 + \\
& 12v_3^2\omega_7 - 12\omega_4cs^2) \frac{\rho\delta_l^3}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3} + (-6\omega_4\omega_2^2 + \omega_4^2\omega_2^2 + 6\omega_4^2 - 6\omega_4^2\omega_2 + 6\omega_2^2) \frac{v_3v_1\rho\delta_l^3}{6\delta_t\omega_4^2\omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_3} + \\
& C_{10} \frac{v_2\delta_l^3}{2\omega_3^2\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3} + (-6v_3^2\omega_7\omega_4 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 + v_3^2\omega_7\omega_4^2 - 12v_3^2\omega_4 + 6v_3^2\omega_4^2 + 18\omega_7\omega_4cs^2 + \\
& 12v_3^2\omega_7 - 12\omega_4cs^2) \frac{\rho\delta_l^3}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3} + (6\omega_3^2 - 6\omega_3\omega_4^2 + \omega_3^2\omega_4^2 + 6\omega_4^2 - 6\omega_3^2\omega_4) \frac{v_3v_2\rho\delta_l^3}{6\omega_3^2\delta_t\omega_4^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3} + C_{11} \frac{v_3\delta_l^3}{6\delta_t\omega_7\omega_4^2} \frac{\partial^3 \rho}{\partial x_3} + \\
& C_{12} \frac{\rho\delta_l^3}{12\delta_t\omega_7\omega_4^2} \frac{\partial^3 v_3}{\partial x_3} + (-2 + 3\omega_2 - \omega_2^2) \frac{\delta_t^2\rho\delta_l}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + \\
& (-4\omega_5\omega_2 + 2\omega_2^2 - 2\omega_5\omega_2^2 + 8\omega_5\omega_2^2 - \omega_3^2\omega_2^2 + 2\omega_2^2 - \omega_5^2\omega_2 - 4\omega_2^2) \frac{\delta_tv_1\rho\delta_l^2}{2\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\rho\delta_l^3}{12\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + \\
& C_{14} \frac{\delta_l^4}{24\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{v_1\rho\delta_l^4}{12\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3\omega_3) \frac{\delta_t^2\rho\delta_l}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (-24\omega_3\omega_2^2 + 12\omega_3^2 - 6\omega_3^3 + 12\omega_3\omega_2 - 24\omega_3^2\omega_2 - \omega_3^3\omega_2^2 + 7\omega_3^3\omega_2 + 13\omega_3^2\omega_2^2 + 12\omega_2^2) \frac{\delta_tv_2\rho\delta_l^2}{12\omega_3^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-24\omega_3\omega_2^2 + 12\omega_3^2 + 7\omega_3\omega_2^2 + 12\omega_3\omega_2 - 24\omega_3^2\omega_2 - \omega_3^3\omega_2^2 - 6\omega_3^2 + 13\omega_3^2\omega_2^2 + 12\omega_2^2) \frac{\delta_tv_1\rho\delta_l^2}{12\omega_3^3\omega_2^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& C_{16} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^3\omega_5\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{\rho\delta_l^3}{12\omega_3\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{18} \frac{v_2v_1\delta_l^4}{6\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\
& C_{20} \frac{v_1\rho\delta_l^4}{12\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-4\omega_3^2 - 4\omega_6\omega_3 + 2\omega_3^3 + 2\omega_6^2 + 8\omega_6\omega_3^2 - 2\omega_6\omega_3^3 - \omega_6^2\omega_3^2 - \omega_6^2\omega_3) \frac{\delta_tv_2\rho\delta_l^2}{2\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + \\
& C_{21} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^2\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + C_{22} \frac{v_2v_1\rho\delta_l^3}{6\omega_6\omega_3^3\omega_2^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + C_{23} \frac{\delta_l^4}{4\omega_6^2\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{v_1\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_5^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& C_{25} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + C_{27} \frac{v_2v_1\delta_l^4}{6\omega_6^2\omega_3^3\delta_t\omega_5^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{28} \frac{v_2\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{29} \frac{v_1\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + \\
& + C_{30} \frac{\delta_l^4}{24\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 \rho}{\partial x_2^2} + C_{31} \frac{v_2\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_2}{\partial x_2^2} + (-2 + 3\omega_4 - \omega_4^2) \frac{\delta_t^2\rho\delta_l}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (12\omega_4\omega_2 - 24\omega_4\omega_2^2 + 7\omega_4^3\omega_2 - 6\omega_4^3 + 13\omega_4^2\omega_2^2 + 12\omega_4^2 - 24\omega_4^2\omega_2 - \omega_4^3\omega_2^2 + 12\omega_2^2) \frac{\delta_tv_3\rho\delta_l^2}{12\omega_4^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (12\omega_4\omega_2 - 24\omega_4\omega_2^2 + 7\omega_4\omega_2^3 - \omega_4^2\omega_2^3 + 13\omega_4^2\omega_2^2 + 12\omega_4^2 - 6\omega_2^3 - 24\omega_4^2\omega_2 + 12\omega_2^2) \frac{\delta_tv_1\rho\delta_l^2}{12\omega_4^3\omega_2^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& C_{32} \frac{v_3v_1\rho\delta_l^3}{6\omega_4^3\omega_5\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + C_{33} \frac{\rho\delta_l^3}{12\omega_4\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{34} \frac{v_3v_1\delta_l^4}{6\delta_t\omega_4^3\omega_5^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{35} \frac{v_3\rho\delta_l^4}{12\delta_t\omega_4^3\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& C_{36} \frac{v_1\rho\delta_l^4}{12\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (12\omega_3^2 + 12\omega_3\omega_4 - 24\omega_3\omega_4^2 + 7\omega_3\omega_4^3 - \omega_2^2\omega_4^3 - 6\omega_4^3 + 13\omega_3^2\omega_4^2 + 12\omega_4^2 - 24\omega_3^2\omega_4) \frac{\delta_tv_3\rho\delta_l^2}{12\omega_3^3\omega_4^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (12\omega_3^2 - 6\omega_3^3 + 12\omega_3\omega_4 - 24\omega_3\omega_4^2 + 7\omega_3^3\omega_4 + 13\omega_3^2\omega_4^2 + 12\omega_4^2 - 24\omega_3^2\omega_4 - \omega_3^3\omega_4^2) \frac{\delta_tv_2\rho\delta_l^2}{12\omega_3^3\omega_4^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_3v_2\rho\delta_l^3}{6\omega_3^3\omega_4^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{38} \frac{v_3v_1\rho\delta_l^3}{6\omega_3\omega_4^3\omega_2^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{39} \frac{v_2v_1\rho\delta_l^3}{6\omega_3^3\omega_4\omega_2^2} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{40} \frac{v_3v_2\delta_l^4}{\omega_3^3\delta_t\omega_4^3\omega_2^2\omega_5^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{41} \frac{v_3v_2v_1\rho\delta_l^4}{6\omega_3^3\delta_t\omega_4^3\omega_2^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{42} \frac{v_3\rho\delta_l^4}{12\delta_t\omega_4^3\omega_5^2\omega_2^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{43} \frac{v_2\rho\delta_l^4}{12\omega_3^3\delta_t\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{44} \frac{v_3v_2\rho\delta_l^3}{6\omega_6\omega_3^3\omega_4^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\rho\delta_l^3}{12\omega_6^2\omega_3^3\omega_4^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{46} \frac{v_3v_1\delta_l^4}{\omega_6^2\omega_3^3\delta_t\omega_4^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{47} \frac{v_3\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_4^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{48} \frac{v_3v_2v_1\rho\delta_l^4}{6\omega_3^3\delta_t\omega_4^2\omega_2^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{49} \frac{v_1\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_2^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{50} \frac{v_3v_2\delta_l^4}{6\omega_6^2\omega_3^3\delta_t\omega_4^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{51} \frac{v_3\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t\omega_4^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{52} \frac{v_2\rho\delta_l^4}{12\omega_6^2\omega_3^3\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-\omega_7^2\omega_4 - \omega_7^2\omega_4^2 + 2\omega_4^3 - 2\omega_7\omega_4^3 + 8\omega_7\omega_4^2 - 4\omega_4^2 - 4\omega_7\omega_4 + 2\omega_7^2) \frac{\delta_t v_3 \rho \delta_l^2}{2\omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + C_{53} \frac{\rho \delta_l^3}{12\omega_7^2\omega_4^3\omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + \\
& C_{54} \frac{v_3 v_1 \rho \delta_l^3}{6\omega_7\omega_4^3\omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + C_{55} \frac{\delta_l^4}{4\delta_t \omega_7^2\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{56} \frac{v_1 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3\omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{57} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3\omega_5^2\omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{58} \frac{\rho \delta_l^3}{12\omega_3\omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + C_{59} \frac{v_3 v_2 \rho \delta_l^3}{6\omega_3^2\omega_7\omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + C_{60} \frac{v_2 v_1 \delta_l^4}{\omega_3^3 \delta_t \omega_7^2\omega_4^3\omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{61} \frac{v_2 \rho \delta_l^4}{12\omega_3^3 \delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{62} \frac{v_1 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3\omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{63} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_3^3 \delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{64} \frac{\delta_l^4}{4\omega_6^2\omega_3^3 \delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{65} \frac{v_2 \rho \delta_l^4}{12\omega_3^3 \delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{66} \frac{v_3 \rho \delta_l^4}{12\omega_6^2\omega_3^3 \delta_t \omega_4^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{67} \frac{\rho \delta_l^3}{12\omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3^2} + C_{68} \frac{v_3 v_1 \delta_l^4}{6\delta_t \omega_7^2\omega_4^3\omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + C_{69} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{70} \frac{v_1 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3\omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^2} \\
& + C_{71} \frac{v_3 v_2 \delta_l^4}{6\omega_3^3 \delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^2} + C_{72} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^2} + C_{73} \frac{v_2 \rho \delta_l^4}{12\omega_3^3 \delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^2} + C_{74} \frac{\delta_l^4}{24\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 \rho}{\partial x_3^4} + C_{75} \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -3\omega_5\omega_2 + 3v_1^2\omega_2^2 - 3cs^2\omega_5\omega_2^2 - 6cs^2\omega_2 + 15cs^2\omega_5\omega_2 + 3cs^2\omega_2^2 + \omega_5\omega_2^2 - 6v_1^2\omega_2 - v_1^2\omega_5\omega_2^2 + 3v_1^2\omega_5\omega_2 + 6\omega_2 - 12cs^2\omega_5 - 3\omega_2^2 \\
C_2 &= -6\omega_5\omega_2 + 6v_1^2\omega_2^2 - 3cs^2\omega_5\omega_2^2 - 12cs^2\omega_2 + 18cs^2\omega_5\omega_2 + 6cs^2\omega_2^2 + 2\omega_5\omega_2^2 - 12v_1^2\omega_2 - 12v_1^2\omega_5 - 5v_1^2\omega_5\omega_2^2 + 18v_1^2\omega_5\omega_2 + 12\omega_2 - 12cs^2\omega_5 - 6\omega_2^2 \\
C_3 &= \omega_3^2v_1^2\omega_2^2 - 3\omega_3v_1^2\omega_5\omega_2^2 - \omega_3^2cs^2\omega_5\omega_2^2 - 2\omega_3^2cs^2\omega_2 + \omega_3^2cs^2\omega_2^2 + 4\omega_3^2cs^2\omega_5\omega_2 + 2\omega_3v_1^2\omega_5\omega_2 - 2\omega_3^2v_1^2\omega_2 + \omega_3cs^2\omega_5\omega_2^2 + 4\omega_3^2v_1^2\omega_5 + \\
& \omega_3^2v_1^2\omega_5\omega_2^2 + 2v_1^2\omega_5\omega_2^2 - 4\omega_3^2v_1^2\omega_5\omega_2 - 2\omega_3cs^2\omega_5\omega_2 - 2\omega_3^2cs^2\omega_5 \\
C_4 &= -\omega_6\omega_3^2cs^2\omega_2^2 + \omega_6\omega_3^2v_2^2\omega_2^2 + \omega_3^2cs^2\omega_2^2 + \omega_3^2v_2^2\omega_2^2 - 3\omega_6\omega_3^2v_2^2\omega_2 + \omega_6\omega_3^2cs^2\omega_2 + 2\omega_6\omega_3^2v_2^2 - 2\omega_3cs^2\omega_2^2 - 2\omega_3v_2^2\omega_2^2 + 2\omega_6\omega_3v_2^2\omega_2 - \\
& 2\omega_6\omega_3cs^2\omega_2 + 4\omega_6\omega_3cs^2\omega_2^2 - 4\omega_6\omega_3v_2^2\omega_2^2 + 4\omega_6v_2^2\omega_2^2 - 2\omega_6cs^2\omega_2^2 \\
C_5 &= -12\omega_6cs^2 + 15\omega_6\omega_3cs^2 - 3\omega_3^2 + 6\omega_3 - 3\omega_6\omega_3 - 6\omega_3v_2^2 + \omega_6\omega_3^2 + 3\omega_3^2cs^2 - \omega_6\omega_3^2v_2^2 + 3\omega_6\omega_3v_2^2 - 6\omega_3cs^2 + 3\omega_3^2v_2^2 - 3\omega_6\omega_3^2cs^2 \\
C_6 &= -12\omega_6cs^2 + 18\omega_6\omega_3cs^2 - 6\omega_3^2 + 12\omega_3 - 6\omega_6\omega_3 - 12\omega_3v_2^2 + 2\omega_6\omega_3^2 + 6\omega_3^2cs^2 - 5\omega_6\omega_3^2v_2^2 - 12\omega_6v_2^2 + 18\omega_6\omega_3v_2^2 - 12\omega_3cs^2 + 6\omega_3^2v_2^2 - 3\omega_6\omega_3^2cs^2 \\
C_7 &= -2v_1^2\omega_2^2\omega_2 - 4v_1^2\omega_4^2\omega_5\omega_2 - \omega_2^2cs^2\omega_5\omega_2^2 + 4\omega_4^2cs^2\omega_5\omega_2 + v_1^2\omega_4^2\omega_5\omega_2^2 + v_1^2\omega_4^2\omega_2^2 - 2\omega_4^2cs^2\omega_5 - 3v_1^2\omega_4\omega_5\omega_2^2 + \omega_4cs^2\omega_5\omega_2^2 - 2\omega_4^2cs^2\omega_2 + \\
& 2v_1^2\omega_5\omega_2^2 + \omega_4^2cs^2\omega_2^2 - 2\omega_4cs^2\omega_5\omega_2 + 4v_1^2\omega_4^2\omega_5 + 2v_1^2\omega_4\omega_5\omega_2 \\
C_8 &= \omega_3^2v_2^2\omega_4^2 + \omega_3^2\omega_4^2cs^2 - 3\omega_6\omega_3^2v_2^2\omega_4 - 2\omega_6\omega_3\omega_4cs^2 + 2\omega_6\omega_3^2v_2^2 + \omega_6\omega_3^2v_2^2\omega_4^2 - \omega_6\omega_3^2\omega_4^2cs^2 + \omega_6\omega_3^2\omega_4cs^2 - 4\omega_6\omega_3v_2^2\omega_4^2 - 2\omega_6\omega_4^2cs^2 + \\
& 4\omega_6\omega_3\omega_4^2cs^2 + 4\omega_6v_2^2\omega_4^2 - 2\omega_3v_2^2\omega_4^2 + 2\omega_6\omega_3v_2^2\omega_4 - 2\omega_3\omega_4^2cs^2 \\
C_9 &= -2\omega_4cs^2\omega_2^2 - 2\omega_7\omega_4cs^2\omega_2 + 4v_3^2\omega_7\omega_2^2 + v_3^2\omega_7\omega_4^2\omega_2^2 - 3v_3^2\omega_7\omega_4^2\omega_2 + 2v_3^2\omega_7\omega_4^2 + 4\omega_7\omega_4cs^2\omega_2^2 - 2\omega_7cs^2\omega_2^2 + v_3^2\omega_4^2\omega_2^2 - 2v_3^2\omega_4\omega_2^2 + \\
& 2v_3^2\omega_7\omega_4\omega_2 - \omega_7\omega_4^2cs^2\omega_2^2 + \omega_4^2cs^2\omega_2^2 - 4v_3^2\omega_7\omega_4\omega_2^2 + \omega_7\omega_4^2cs^2\omega_2 \\
C_{10} &= \omega_3^2\omega_4^2cs^2 - 4\omega_3^2v_3^2\omega_7\omega_4 - \omega_3^2\omega_7\omega_4^2cs^2 - 2\omega_3^2\omega_7cs^2 - 2\omega_3\omega_7\omega_4cs^2 + 2v_3^2\omega_7\omega_4^2 + \omega_3^2v_3^2\omega_7\omega_4^2 + 2\omega_3v_3^2\omega_7\omega_4 - 2\omega_3^2v_3^2\omega_4 + \omega_3\omega_7\omega_4^2cs^2 + \\
& 4\omega_3^2\omega_7\omega_4cs^2 + \omega_3^2v_3^2\omega_4^2 + 4\omega_3^2v_3^2\omega_7 - 3\omega_3v_3^2\omega_7\omega_4^2 - 2\omega_3^2\omega_4cs^2 \\
C_{11} &= 3v_3^2\omega_7\omega_4 + 3\omega_3^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 - v_3^2\omega_7\omega_4^2 + 6\omega_4 + \omega_7\omega_4^2 - 6v_3^2\omega_4 - 3\omega_4^2 - 3\omega_7\omega_4 + 3v_3^2\omega_4^2 + 15\omega_7\omega_4cs^2 - 6\omega_4cs^2 \\
C_{12} &= 18v_3^2\omega_7\omega_4 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 - 5v_3^2\omega_7\omega_4^2 + 12\omega_4 + 2\omega_7\omega_4^2 - 12v_3^2\omega_4 - 6\omega_4^2 - 6\omega_7\omega_4 + 6v_3^2\omega_4^2 + 18\omega_7\omega_4cs^2 - 12v_3^2\omega_7 - 12\omega_4cs^2 \\
C_{13} &= -24\omega_5\omega_2 + 12v_1^2\omega_2^2 + 9cs^2\omega_5\omega_2^3 - 6v_1^2\omega_2^3 - 42v_1^2\omega_5^2\omega_2 - 36cs^2\omega_5\omega_2^2 + 24cs^2\omega_5\omega_2 + 12cs^2\omega_2^2 + 27v_1^2\omega_5^2\omega_2^2 - 9\omega_5\omega_2^3 - 6cs^2\omega_2^3 + 36\omega_5\omega_2^2 - \\
& 3v_1^2\omega_5^2\omega_2^2 + 15v_1^2\omega_5\omega_2^3 + 24cs^2\omega_5^2\omega_2 - 11\omega_5^2\omega_2^2 - 48cs^2\omega_5^2\omega_2 + \omega_5^2\omega_2^3 - 60v_1^2\omega_5\omega_2^2 + 48v_1^2\omega_5\omega_2 + 12v_1^2\omega_5^2 + 25cs^2\omega_5^2\omega_2^2 + 6\omega_2^3 + 12\omega_5^2\omega_2 - 12\omega_2^2 - 2cs^2\omega_5^2\omega_2^3 \\
C_{14} &= 24cs^4\omega_5\omega_2 + 24v_1^2\omega_2^2 - 6cs^2\omega_5\omega_2^3 - 24v_1^4\omega_5^2\omega_2^2 - 12v_1^2\omega_2^3 - 24v_1^2\omega_5^2\omega_2 + 3v_1^4\omega_5^2\omega_2^3 + 24cs^2\omega_5\omega_2^2 + 24cs^4\omega_5^2 + 156v_1^2cs^2\omega_5^2\omega_2 - \\
& 24cs^2\omega_5\omega_2 - 72v_1^2cs^2\omega_2^2\omega_2^2 - 96v_1^2cs^2\omega_5^2\omega_2^2 + 24v_1^2\omega_5^2\omega_2^2 + 6cs^4\omega_5\omega_2^3 + 6v_1^2cs^2\omega_5^2\omega_2^3 + 24v_1^4\omega_5^2\omega_2 - 24cs^4\omega_5\omega_2^2 - 3v_1^2\omega_5^2\omega_2^3 - 12v_1^2cs^2\omega_5\omega_2^3 - \\
& 24v_1^2cs^2\omega_2^2 + 12v_1^4\omega_2^3 - 48v_1^4\omega_5\omega_2 + 18v_1^2\omega_5\omega_2^3 + 24cs^4\omega_5^2\omega_2^2 + 12cs^2\omega_5^2\omega_2 - 24v_1^4\omega_2^2 + 12v_1^2cs^2\omega_2^3 + 48v_1^2cs^2\omega_5\omega_2^2 - 3cs^4\omega_5^2\omega_2^3 - 72v_1^2\omega_5\omega_2^2 + \\
& 48v_1^2\omega_5\omega_2 - 8cs^2\omega_5^2\omega_2^2 - 18v_1^4\omega_5\omega_2^3 - 24v_1^2cs^2\omega_5\omega_2 - 48cs^4\omega_5^2\omega_2 + 72v_1^4\omega_5\omega_2^2 + cs^2\omega_5^2\omega_2^3 \\
C_{15} &= 12\omega_5\omega_2 - 12v_1^2\omega_2^2 - 6cs^2\omega_5\omega_2^3 + 6v_1^2\omega_2^3 + 24v_1^2\omega_5^2\omega_2 + 24cs^2\omega_5\omega_2^2 - 12cs^2\omega_5\omega_2 - 12cs^2\omega_2^2 - 16v_1^2\omega_5^2\omega_2^2 + 6\omega_5\omega_2^3 + 6cs^2\omega_2^3 - 24\omega_5\omega_2^2 + \\
& 2v_1^2\omega_5^2\omega_2^3 - 6v_1^2\omega_5\omega_2^3 - 24cs^2\omega_5^2\omega_2^2 + 8\omega_5^2\omega_2^2 + 42cs^2\omega_5^2\omega_2 - \omega_5^2\omega_2^3 + 24v_1^2\omega_5\omega_2^2 - 12v_1^2\omega_5\omega_2 - 12v_1^2\omega_5^2 - 20cs^2\omega_5^2\omega_2^2 - 6\omega_2^3 - 6\omega_2^2\omega_2 + 12\omega_2^2 + cs^2\omega_5^2\omega_2^3 \\
C_{16} &= -12\omega_3^2\omega_5\omega_2 - 12\omega_3^3\omega_5 - 7\omega_3^2\omega_5\omega_2^3 - 6\omega_5\omega_2^3 + 12\omega_3^2\omega_5\omega_2^2 + 12\omega_3\omega_5\omega_2^3 + 3\omega_3^3\omega_2^3 + 24\omega_3^3\omega_5\omega_2 - 6\omega_3^3\omega_2^2 - 6\omega_3\omega_5\omega_2^2 - 10\omega_3^3\omega_5\omega_2^2 - \\
& 6\omega_3^2\omega_2^3 + \omega_3^3\omega_5\omega_2^2 + 12\omega_3^2\omega_2^2 \\
C_{17} &= 9\omega_3v_1^2\omega_5\omega_2^3 - 6cs^2\omega_5\omega_2^3 - 24\omega_3v_1^2\omega_5^2 - 12v_1^2\omega_5^2\omega_2 - 12v_1^2\omega_5^2\omega_2^2 - 30\omega_3v_1^2\omega_5\omega_2^2 + 12cs^2\omega_5\omega_2^2 - 30\omega_3cs^2\omega_5^2\omega_2 + 22\omega_3cs^2\omega_5^2\omega_2^2 + 12\omega_3v_1^2\omega_5\omega_2 + \\
& 6v_1^2\omega_5^2\omega_2^2 + 12\omega_3cs^2\omega_5^2\omega_2^2 - 2\omega_3cs^2\omega_5^2\omega_2^3 - v_1^2\omega_5^2\omega_2^3 + 12\omega_3cs^2\omega_2^2 + 9\omega_3cs^2\omega_5\omega_2^3 - 6v_1^2\omega_5\omega_2^3 - 30\omega_3cs^2\omega_5\omega_2^2 + 12cs^2\omega_2^2\omega_2 - 6\omega_3cs^2\omega_2^3 + \\
& 36\omega_3v_1^2\omega_5^2\omega_2 + 12v_1^2\omega_5\omega_2^2 + 12\omega_3v_1^2\omega_2^2 - 10\omega_3v_1^2\omega_5^2\omega_2^2 - 18cs^2\omega_5^2\omega_2^2 + 12\omega_3cs^2\omega_5\omega_2 + \omega_3v_1^2\omega_5^2\omega_2^3 - 6\omega_3v_1^2\omega_2^3 + 3cs^2\omega_5^2\omega_2^3 \\
C_{18} &= -\omega_3^3\omega_5^2\omega_2^3 + 6\omega_3^2cs^2\omega_5\omega_2^3 - 36\omega_3^3cs^2\omega_5^2 + 12\omega_3^2v_1^2\omega_5^2\omega_2 + 7\omega_3^3\omega_5^2\omega_2^2 - 24\omega_3^3cs^2\omega_5\omega_2 - 12\omega_3^2cs^2\omega_5\omega_2^2 + 6\omega_3^3v_1^2\omega_5^2\omega_2^2 - 12\omega_3cs^2\omega_5^2\omega_2^2 - \\
& 30\omega_3^3v_1^2\omega_5^2\omega_2 + 42\omega_3^3cs^2\omega_5\omega_2^2 - 6\omega_3^3\omega_5^2\omega_2 - 12\omega_3^2v_1^2\omega_2^2\omega_2^2 - 3\omega_3^2\omega_5\omega_2^3 + 24\omega_3^3v_1^2\omega_5^2 + 6\omega_3cs^2\omega_5^2\omega_2^3 + 6v_1^2\omega_5^2\omega_2^3 + 6\omega_3^2\omega_5\omega_2^2 - 12\omega_3^3cs^2\omega_5\omega_2^3 +
\end{aligned}$$



$$C_{32} = 12\omega_4\omega_5\omega_2^3 - 6\omega_4\omega_5\omega_2^2 + 24\omega_4^3\omega_5\omega_2 - 10\omega_4^3\omega_5\omega_2^2 - 12\omega_4^3\omega_5 - 6\omega_5\omega_2^3 + \omega_4^3\omega_5\omega_2^3 - 6\omega_4^3\omega_2^3 - 12\omega_4^2\omega_5\omega_2 + 12\omega_4^2\omega_2^2 - 7\omega_4^2\omega_5\omega_2^2 + 3\omega_4^3\omega_2^3 - 6\omega_4^3\omega_2^2 + 12\omega_4^2\omega_5\omega_2^2$$

$$C_{33} = 12\omega_4cs^2\omega_2^2 - 6cs^2\omega_5\omega_2^2 - 6\omega_4cs^2\omega_2^3 - 30\omega_4cs^2\omega_5\omega_2 - 12v_1^2\omega_5^2\omega_2 + 12cs^2\omega_5\omega_2^2 + 36v_1^2\omega_4\omega_5^2\omega_2 - 10v_1^2\omega_4\omega_5^2\omega_2^2 + 22\omega_4cs^2\omega_5^2\omega_2^2 - 24v_1^2\omega_4\omega_5^2 + 6v_1^2\omega_2^2\omega_2^2 + v_1^2\omega_4\omega_5^2\omega_2^3 - v_1^2\omega_5^2\omega_2^3 - 2\omega_4cs^2\omega_5^2\omega_2^3 + 12v_1^2\omega_4\omega_2^2 + 9v_1^2\omega_4\omega_5\omega_2^3 - 6v_1^2\omega_5\omega_2^3 + 9\omega_4cs^2\omega_5\omega_2^3 + 12cs^2\omega_5^2\omega_2 - 30v_1^2\omega_4\omega_5\omega_2^2 - 6v_1^2\omega_4\omega_2^3 - 30\omega_4cs^2\omega_5\omega_2^2 + 12v_1^2\omega_5\omega_2^2 + 12\omega_4cs^2\omega_5^2 + 12v_1^2\omega_4\omega_5\omega_2 + 3cs^2\omega_5^2\omega_2^3$$

$$C_{34} = 6\omega_4cs^2\omega_5\omega_2^2 + 6v_1^2\omega_4^3\omega_2^3 - 3\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4cs^2\omega_5\omega_2^2 + \omega_4^2\omega_5^2\omega_2^3 + 6v_1^2\omega_4^3\omega_5^2\omega_2^2 - 24\omega_4cs^2\omega_5\omega_2 + 12\omega_4^3\omega_5\omega_2 - 12v_1^2\omega_4^3\omega_2^2 + 42\omega_4^3cs^2\omega_5\omega_2^2 - 30v_1^2\omega_4^3\omega_5^2\omega_2 - 21\omega_4^3\omega_5\omega_2^2 + 6v_1^2\omega_4^3\omega_5\omega_2^3 + 6v_1^2\omega_4\omega_5^2\omega_2^2 - 12\omega_4cs^2\omega_5^2\omega_2^3 + 6\omega_4cs^2\omega_5^2\omega_2^2 - 12v_1^2\omega_4^3\omega_5^2\omega_2^2 - \omega_4^3\omega_5^2\omega_2^3 + 6\omega_4^3cs^2\omega_5^2\omega_2^3 - 24v_1^2\omega_4^3\omega_5\omega_2 - 48\omega_4^3cs^2\omega_5^2\omega_2^2 - 36\omega_4^3cs^2\omega_5^2 + 7\omega_4^3\omega_5^2\omega_2^2 + 6v_1^2\omega_4^3\omega_2^3 - 24\omega_4^3cs^2\omega_5^2\omega_2 + 42\omega_4^3cs^2\omega_5^2\omega_2^2 + 78\omega_4^3cs^2\omega_5^2\omega_2 - 3\omega_4^3\omega_5\omega_2^3 + 42v_1^2\omega_4^3\omega_5\omega_2^2 - 3\omega_4^3\omega_2^3 - 6\omega_4^3\omega_5^2\omega_2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 + 24v_1^2\omega_4^3\omega_5^2 + 12v_1^2\omega_4^3\omega_5^2\omega_2 + 6\omega_4^3\omega_2^2 - 12v_1^2\omega_4^3\omega_5\omega_2^2 + 6\omega_4^3\omega_5\omega_2^2$$

$$C_{35} = 12\omega_2^2cs^2\omega_5\omega_2^3 + 6v_1^2\omega_4^3\omega_2^3 + 3v_1^2\omega_4^3\omega_5^2\omega_2^3 - 6\omega_4^3\omega_5^2\omega_2^2 - 24\omega_4cs^2\omega_5\omega_2^2 + 2\omega_2^2\omega_5^2\omega_2^3 - 12\omega_4^3cs^2\omega_5\omega_2 - 12v_1^2\omega_4^3\omega_2^2 + 36\omega_4^3cs^2\omega_5\omega_2^2 - 30v_1^2\omega_4^3\omega_5^2\omega_2 - 6\omega_4^3\omega_5\omega_2^2 + 12v_1^2\omega_4^3\omega_5\omega_2^3 - 12\omega_4cs^2\omega_5^2\omega_2^2 + 6\omega_4^3cs^2\omega_2^3 - 18v_1^2\omega_4\omega_5^2\omega_2^3 - 24v_1^2\omega_4\omega_5\omega_2^2 + 3\omega_4^3\omega_5\omega_2^3 - 12\omega_4^3cs^2\omega_5\omega_2^3 + 12v_1^2\omega_5^2\omega_2^3 - 12\omega_4^3cs^2\omega_2^2 + 6\omega_4cs^2\omega_5^2\omega_2^3 + 12v_1^2\omega_4^3\omega_5^2\omega_2 - \omega_4^3\omega_5^2\omega_2^3 + 4\omega_4^3cs^2\omega_5^2\omega_2^3 - 12v_1^2\omega_4^3\omega_5\omega_2 - 32\omega_4^3cs^2\omega_5^2\omega_2^3 - 12\omega_4^3cs^2\omega_5^2 + 3\omega_4^3\omega_5^2\omega_2^2 - 24\omega_2^2cs^2\omega_5^2\omega_2 + 48\omega_4cs^2\omega_5^2\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 - 6\omega_4^3\omega_5\omega_2^3 + 36v_1^2\omega_4^3\omega_5\omega_2^2 - 12\omega_2^2cs^2\omega_5^2\omega_2^3 + 24v_1^2\omega_4^3\omega_5^2 - 12v_1^2\omega_4^3\omega_5\omega_2^2 + 12\omega_2^2\omega_5\omega_2^2$$

$$C_{36} = 24\omega_5\omega_2 - 12v_1^2\omega_2^2 - 12cs^2\omega_5\omega_2^3 + 6v_1^2\omega_2^3 + 48cs^2\omega_5\omega_2^2 - 36cs^2\omega_5\omega_2 - 12cs^2\omega_2^2 - 8v_1^2\omega_5^2\omega_2^2 + 9\omega_5\omega_2^3 + 6cs^2\omega_2^3 - 36\omega_5\omega_2^2 + v_1^2\omega_5^2\omega_2^3 - 12v_1^2\omega_5\omega_2^3 - 48cs^2\omega_5^2 + 11\omega_5^2\omega_2^2 + 90cs^2\omega_5^2\omega_2 - \omega_5^2\omega_2^3 + 48v_1^2\omega_5\omega_2^2 - 36v_1^2\omega_5\omega_2 + 12v_1^2\omega_5^2 - 44cs^2\omega_5^2\omega_2^2 - 6\omega_2^3 - 12\omega_5^2\omega_2 + 12\omega_2^2 + 4cs^2\omega_5^2\omega_2^3$$

$$C_{37} = -12\omega_3\omega_4^2\omega_2 + 3\omega_3^3\omega_4^2\omega_2 - 12\omega_3^2\omega_4\omega_2 + 18\omega_3\omega_4^3\omega_2 - 6\omega_3\omega_4^3 - 16\omega_3^2\omega_4^2\omega_2 - 6\omega_3^3\omega_4 - 6\omega_4^3\omega_2 - 16\omega_3^2\omega_4^3\omega_2 + 12\omega_3^2\omega_4^3 + 18\omega_3^3\omega_4\omega_2 - 12\omega_3^2\omega_4^2 - 6\omega_3^3\omega_2 - 4\omega_3^3\omega_4^3 + 30\omega_3^2\omega_4^2\omega_2 + 12\omega_3^3\omega_4^2$$

$$C_{38} = -12\omega_3\omega_4^2\omega_2 + 3\omega_3\omega_4^3\omega_2^3 - 6\omega_3\omega_2^3 - 16\omega_3\omega_4^3\omega_2^2 + 18\omega_3\omega_4^3\omega_2 - 16\omega_3\omega_4^2\omega_2^3 - 6\omega_3\omega_4^3 - 6\omega_4\omega_2^3 + 30\omega_3\omega_4^2\omega_2^2 - 6\omega_4^3\omega_2 + 12\omega_4^2\omega_2^3 - 12\omega_3\omega_4\omega_2^2 + 18\omega_3\omega_4\omega_2^3 - 12\omega_2^2\omega_2^2 - 4\omega_4^3\omega_2^3 + 12\omega_4^3\omega_2^2$$

$$C_{39} = -6\omega_3\omega_2^3 - 12\omega_3^2\omega_4\omega_2 + 30\omega_3^2\omega_4\omega_2^2 - 6\omega_4\omega_2^3 - 16\omega_3^2\omega_4\omega_2^3 - 6\omega_3^3\omega_4 - 12\omega_3\omega_4\omega_2^2 + 18\omega_3^2\omega_4\omega_2 - 4\omega_3^3\omega_2^3 + 18\omega_3\omega_4\omega_2^3 + 12\omega_3^2\omega_2^3 - 6\omega_3^3\omega_2 + 3\omega_3^3\omega_4\omega_2^3 - 12\omega_3^2\omega_2^3 - 16\omega_3^2\omega_4\omega_2^2$$

$$C_{40} = 7\omega_3^2v_1^2\omega_5^2\omega_2^3 + 6\omega_3^3\omega_4cs^2\omega_2^2\omega_2^2 + 6\omega_3^3\omega_3^3cs^2\omega_5^2\omega_2 + 6\omega_3^3v_1^2\omega_4^3\omega_5\omega_2^2 - 2\omega_3^3\omega_3^3cs^2\omega_2^2 + 3\omega_3^3v_1^2\omega_5^2\omega_2^3 + 3v_1^2\omega_3^3\omega_5^2\omega_2^3 + 4\omega_3v_1^2\omega_4^3\omega_5^2\omega_2^3 - 2\omega_3^3\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^2 + 7\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2 - 8\omega_3v_1^2\omega_4^3\omega_5^2\omega_2^3 + \omega_3^3\omega_4cs^2\omega_2^3 - 2\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^2 - 12\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^2 + \omega_3^3\omega_4cs^2\omega_5^2\omega_2^3 + 7\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^3 + \omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^3 + \omega_3^3\omega_4cs^2\omega_5^2\omega_2^3 + 3\omega_3^3v_1^2\omega_4\omega_5^2\omega_2^3 - 2\omega_3^3\omega_4cs^2\omega_2^2\omega_2^2 + 6\omega_3^3\omega_3^3cs^2\omega_5\omega_2^2 - 21\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2 + 3\omega_3v_1^2\omega_4^3\omega_5^2\omega_2^3 + 10\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^3 + \omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^3 - 2\omega_3\omega_4^3cs^2\omega_5^2\omega_2^2 + 4\omega_3^3v_1^2\omega_4\omega_5^2\omega_2^3 - 2\omega_3\omega_4^3cs^2\omega_5^2\omega_2^2 - 2\omega_3\omega_4cs^2\omega_5^2\omega_2^3 + 4\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^3 - 8\omega_3^3v_1^2\omega_4\omega_5^2\omega_2^3 - 2\omega_3^3v_1^2\omega_4\omega_5\omega_2^2 + \omega_3\omega_4^3cs^2\omega_5^2\omega_2^3 - 2\omega_3^3\omega_4^3cs^2\omega_5\omega_2^2 - 8\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^3 + 6\omega_3^3\omega_4^3cs^2\omega_2^2\omega_2^2 + \omega_3^3\omega_4cs^2\omega_5^2\omega_2^3 + \omega_3^3\omega_2^3cs^2\omega_5\omega_2^3 - 2\omega_3^3v_1^2\omega_4^3\omega_5\omega_2^2 - 2\omega_3^3\omega_3^3cs^2\omega_5^2\omega_2 - 2\omega_3^3\omega_4^3cs^2\omega_5^2\omega_2^2 - 2\omega_3^3v_1^2\omega_4\omega_5^2\omega_2^3 + \omega_3^3v_1^2\omega_4\omega_5\omega_2^2 - 2\omega_3^3\omega_4^3cs^2\omega_5\omega_2^2 + 12\omega_3^3v_1^2\omega_4^3\omega_5^2\omega_2^2 - 2\omega_3^3\omega_4^3cs^2\omega_5\omega_2 + \omega_3^3\omega_4cs^2\omega_5^2\omega_2^3$$

$$C_{41} = -30\omega_3\omega_4^3\omega_2^3 - 30\omega_3^3\omega_2^2\omega_2^2 - 36\omega_3^3\omega_4^3\omega_2 + 24\omega_3^3\omega_4^2\omega_2^3 + 6\omega_3\omega_3^3\omega_2^2 + 28\omega_3^3\omega_4^3\omega_2^2 + 18\omega_3\omega_4^2\omega_2^3 + 18\omega_3^3\omega_4\omega_2^3 + 18\omega_3^3\omega_4^2\omega_2 - 5\omega_3^3\omega_4^3\omega_2^3 - 42\omega_3^2\omega_4^2\omega_2^3 + 18\omega_3^2\omega_3^3\omega_2 + 12\omega_3^2\omega_2^3 + 12\omega_3^2\omega_4^2\omega_2^2 - 30\omega_3^2\omega_4\omega_2^3 + 24\omega_3^2\omega_4^3\omega_2^3 + 12\omega_3^3\omega_4^3 + 12\omega_4^3\omega_2^3 - 30\omega_3^2\omega_4^3\omega_2^2 + 6\omega_3^3\omega_4\omega_2^3$$

$$C_{42} = 12\omega_4^2cs^2\omega_5\omega_2^3 + 6v_1^2\omega_3^3\omega_2^3 - 5v_1^2\omega_4^3\omega_2^2\omega_2^3 - 24\omega_4^2cs^2\omega_5\omega_2^2 + 40v_1^2\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^2cs^2\omega_5\omega_2 - 12v_1^2\omega_4^3\omega_2^2 + 36\omega_4^2cs^2\omega_5\omega_2^2 - 90v_1^2\omega_4^3\omega_5^2\omega_2 + 12v_1^2\omega_4^3\omega_5\omega_2^3 + 24v_1^2\omega_4\omega_5^2\omega_2^3 - 12\omega_4cs^2\omega_5^2\omega_2^3 + 6\omega_4^3cs^2\omega_2^3 - 30v_1^2\omega_4\omega_5^2\omega_2^3 - 24v_1^2\omega_4^3\omega_5\omega_2^3 - 12\omega_4^2cs^2\omega_5\omega_2^3 + 12v_1^2\omega_5^2\omega_2^3 - 12\omega_4^3cs^2\omega_2^2 + 6\omega_4cs^2\omega_5^2\omega_2^3 - 60v_1^2\omega_4^3\omega_5^2\omega_2^3 + 4\omega_4^3cs^2\omega_5^2\omega_2^3 - 12v_1^2\omega_4^3\omega_5\omega_2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^2cs^2\omega_5^2 + 24v_1^2\omega_4\omega_5^2\omega_2^3 - 24\omega_4^2cs^2\omega_5^2\omega_2 + 48\omega_4^2cs^2\omega_5^2\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 + 36v_1^2\omega_4^3\omega_5\omega_2^3 - 12\omega_4^2cs^2\omega_5^2\omega_2^3 + 48v_1^2\omega_4^3\omega_5^2\omega_2 - 12v_1^2\omega_4^3\omega_5\omega_2^2$$

$$C_{43} = 12\omega_3^2cs^2\omega_5\omega_2^3 - 5\omega_3^3v_1^2\omega_5^2\omega_2^3 - 12\omega_3^3cs^2\omega_5^2\omega_2 + 48\omega_3^3v_1^2\omega_5^2\omega_2 - 12\omega_3^3cs^2\omega_5\omega_2 - 24\omega_3^2cs^2\omega_5\omega_2^2 + 40\omega_3^3v_1^2\omega_5^2\omega_2^2 - 12\omega_3cs^2\omega_5^2\omega_2^2 - 90\omega_3^3v_1^2\omega_5^2\omega_2 + 36\omega_3^3cs^2\omega_5\omega_2^2 - 60\omega_3^2v_1^2\omega_5^2\omega_2^2 + 48\omega_3^3v_1^2\omega_5^2\omega_2 + 6\omega_3cs^2\omega_5^2\omega_2^3 + 12v_1^2\omega_5^2\omega_2^3 - 12\omega_3^3cs^2\omega_5\omega_2^3 + 24\omega_3^2v_1^2\omega_5^2\omega_2^3 + 6\omega_3^3v_1^2\omega_2^3 + 12\omega_3^3v_1^2\omega_5\omega_2^3 + 4\omega_3^3cs^2\omega_5^2\omega_2^3 - 24\omega_3^2cs^2\omega_5^2\omega_2 - 12\omega_3^3v_1^2\omega_5\omega_2 - 24\omega_3^2v_1^2\omega_5\omega_2^2 - 32\omega_3^3cs^2\omega_5^2\omega_2^2 - 12\omega_3^3v_1^2\omega_2^2 + 36\omega_3^3cs^2\omega_5^2\omega_2 + 24\omega_3v_1^2\omega_5^2\omega_2^2 + 6\omega_3^3cs^2\omega_2^2 + 36\omega_3^3v_1^2\omega_5\omega_2^2 + 48\omega_3^2cs^2\omega_5^2\omega_2^2 - 30\omega_3v_1^2\omega_5^2\omega_2^3 - 12\omega_3^2v_1^2\omega_5\omega_2^3 - 12\omega_3^2cs^2\omega_5^2\omega_2^3 - 12\omega_3^3cs^2\omega_2^2$$

$$C_{44} = 12\omega_6\omega_3^2\omega_4^2 + 12\omega_6\omega_3^3\omega_4 - 10\omega_6\omega_3^2\omega_4^3 - 7\omega_6\omega_3^3\omega_4^2 - 6\omega_6\omega_3^2\omega_4 + \omega_6\omega_3^3\omega_4^3 - 6\omega_6\omega_3^3 - 6\omega_3^2\omega_4^3 + 12\omega_3^2\omega_4^2 + 24\omega_6\omega_3\omega_4^3 - 12\omega_6\omega_4^3 + 3\omega_3^3\omega_4^3 - 6\omega_3^3\omega_4^2 - 12\omega_6\omega_3\omega_4^2$$

$$C_{45} = 22\omega_6^2\omega_3\omega_4cs^2 - 24\omega_6^2v_2^2\omega_4 - 30\omega_6\omega_3^2v_2^2\omega_4 - 18\omega_6^2\omega_3cs^2 + 9\omega_6\omega_3\omega_4cs^2 + \omega_6^2\omega_3^3v_2^2\omega_4 - 6\omega_6\omega_3^3v_2^2 - 12\omega_6^2\omega_3v_2^2 + 36\omega_6^2\omega_3v_2^2\omega_4 - 6\omega_3^3\omega_4cs^2 + 12\omega_6\omega_3\omega_4cs^2 + 12\omega_6\omega_3^2v_2^2 + 12\omega_6^2\omega_3^2cs^2 - 10\omega_6^2\omega_3^2v_2^2\omega_4 + 12\omega_6^2\omega_4cs^2 - 30\omega_6\omega_3^2\omega_4cs^2 + 6\omega_6^2\omega_3^2v_2^2 + 9\omega_6\omega_3^2v_2^2\omega_4 - 6\omega_6\omega_3^3cs^2 - 2\omega_6^2\omega_3\omega_4cs^2 + 12\omega_6^2\omega_3cs^2 - 30\omega_6^2\omega_3\omega_4cs^2 - 6\omega_3^3v_2^2\omega_4 + 12\omega_6\omega_3v_2^2\omega_4 + 12\omega_6\omega_3^2cs^2 + 12\omega_3^2\omega_4cs^2 - \omega_6^2\omega_3^3v_2^2$$

$$C_{46} = 3\omega_6^2\omega_3^3v_2^2\omega_4\omega_2 - 2\omega_6\omega_3^2v_2^2\omega_4\omega_2^3 - 2\omega_6\omega_3\omega_4^3cs^2\omega_2^3 - 2\omega_6^2\omega_3^3v_2^2\omega_4\omega_2^3 + \omega_6\omega_3^3v_2^2\omega_4^3\omega_2^2 + 6\omega_6^2\omega_3^2\omega_4^3cs^2\omega_2^3 - 2\omega_6^2\omega_3\omega_4^3cs^2\omega_2^2 + 4\omega_6^2\omega_3^3v_2^2\omega_4^3\omega_2 - 2\omega_6\omega_3^3v_2^2\omega_4^3\omega_2^3 + 6\omega_6^2\omega_3\omega_4^3cs^2\omega_2^3 + \omega_6\omega_3^3\omega_4^3cs^2\omega_2^3 - 12\omega_6^2\omega_3^2v_2^2\omega_4^3\omega_2^2 + 6\omega_6\omega_3^2v_2^2\omega_4^3\omega_2^3 - 8\omega_6^2\omega_3^3v_2^2\omega_4^3\omega_2 + \omega_6^2\omega_3^3\omega_4^3cs^2\omega_2^2 + 7\omega_6^2\omega_3^3v_2^2\omega_4^3\omega_2^3 - 2\omega_6^2\omega_4^3cs^2\omega_2^3 + 12\omega_6^2\omega_3^2v_2^2\omega_4^3\omega_2^3 + \omega_6\omega_3^3v_2^2\omega_4^3\omega_2^3 + 10\omega_6^2\omega_3^2v_2^2\omega_4^3\omega_2^3 + 3\omega_6^2\omega_3^3v_2^2\omega_4^3\omega_2^3 - 8\omega_6^2\omega_3^3v_2^2\omega_4^3\omega_2^3 - 2\omega_6^2\omega_3^3\omega_4^3cs^2\omega_2^3 - 2\omega_6\omega_3^3v_2^2\omega_4^3\omega_2^3 - 2\omega_6^2\omega_3\omega_4^3cs^2\omega_2^3 + 6\omega_6^2\omega_3^2\omega_4^3cs^2\omega_2^2 - 2\omega_6^2\omega_3^2v_2^2\omega_4^3\omega_2^3 + \omega_6^2\omega_3^3\omega_4^3cs^2\omega_2^2 + 6\omega_6\omega_3^3v_2^2\omega_4\omega_2^2 + 7\omega_6^2\omega_3^3v_2^2\omega_4\omega_2^3 - 2\omega_6^2\omega_4^3cs^2\omega_2^3 - 6\omega_6^2\omega_3^2\omega_4^3cs^2\omega_2^3 + \omega_6^2\omega_3^3\omega_4^3cs^2\omega_2^3 - 8\omega_6^2\omega_3^3v_2^2\omega_4\omega_2^3 - 2\omega_6\omega_3^3v_2^2\omega_4\omega_2^3 + \omega_6^2\omega_3^3\omega_4^3cs^2\omega_2^3 + \omega_6\omega_3^3\omega_4^3cs^2\omega_2^3 + 7\omega_6^2\omega_3^2v_2^2\omega_4\omega_2^2 - 2\omega_6^2\omega_3^2\omega_4^3cs^2\omega_2^2 + 4\omega_6^2\omega_3^2v_2^2\omega_4\omega_2^3 - 2\omega_6^2\omega_3^2\omega_4^3cs^2\omega_2^2 - 2\omega_6\omega_3^3\omega_4^3cs^2\omega_2^2 - 2\omega_6^2\omega_3^3\omega_4^3cs^2\omega_2^2 - 21\omega_6^2\omega_3^3v_2^2\omega_4^3\omega_2^3 + \omega_3^3v_2^2\omega_4^3\omega_2^3$$

$$C_{47} = -12\omega_6^2\omega_3^2\omega_4cs^2 + 4\omega_6^2\omega_3^2\omega_4^3cs^2 - 90\omega_6^2\omega_3v_2^2\omega_4^3 + 36\omega_6^2\omega_3^2\omega_4^3cs^2 - 12\omega_3^2v_2^2\omega_4^3 - 24\omega_6^2\omega_3\omega_4^2cs^2 - 30\omega_6^2\omega_3^2v_2^2\omega_4 - 12\omega_6^2\omega_3^3cs^2 + 48\omega_6^2\omega_3v_2^2\omega_4^3 - 12\omega_3^2\omega_4^3cs^2 + 24\omega_6^2\omega_3^2v_2^2\omega_4 + 36\omega_6\omega_3^2v_2^2\omega_4^3 - 12\omega_6^2\omega_3^2\omega_4^2cs^2 + 48\omega_6^2v_2^2\omega_4^3 - 5\omega_6^2\omega_3^2v_2^2\omega_4 - 24\omega_6\omega_3^2v_2^2\omega_4 + 36\omega_6^2\omega_3\omega_4^3cs^2 - 24\omega_6\omega_3^2\omega_4^2cs^2 + 24\omega_6^2\omega_3^2v_2^2\omega_4 - 12\omega_6\omega_3v_2^2\omega_4^3 + 6\omega_3^2v_2^2\omega_4^3 - 12\omega_6\omega_3^2\omega_4^3cs^2 + 6\omega_6^2\omega_3^2\omega_4^3cs^2 - 32\omega_6^2\omega_3^2\omega_4^3cs^2 + 12\omega_6\omega_3^2\omega_4^3cs^2 + 12\omega_6\omega_3^2v_2^2\omega_4^3 + 40\omega_6^2\omega_3^2v_2^2\omega_4^3 + 48\omega_6^2\omega_3^2\omega_4^3cs^2 - 12\omega_6\omega_3\omega_4^3cs^2 - 12\omega_6\omega_3^2v_2^2\omega_4^3 + 6\omega_3^2\omega_4^3cs^2 - 60\omega_6^2\omega_3^2v_2^2\omega_4^3 + 12\omega_6^2\omega_3^2v_2^2$$

$$C_{48} = -36\omega_3\omega_4^3\omega_2^3 - 42\omega_3^2\omega_4^3\omega_2^2 - 30\omega_3^2\omega_4^3\omega_2 - 24\omega_3^2\omega_4^3\omega_2^2 + 18\omega_3\omega_4^3\omega_2^2 + 24\omega_3^2\omega_4^3\omega_2^2 + 18\omega_3\omega_4^3\omega_2^3 + 6\omega_3^2\omega_4\omega_2^3 + 18\omega_3^2\omega_4^2\omega_2 - 5\omega_3^2\omega_4^3\omega_2^2 - 30\omega_3^2\omega_4^3\omega_2^2 + 6\omega_3^2\omega_4^3\omega_2 + 12\omega_3^2\omega_2^3 + 12\omega_3^2\omega_4^2\omega_2^2 - 30\omega_3^2\omega_4\omega_2^3 + 28\omega_3^2\omega_4^3\omega_2^3 + 12\omega_3^2\omega_4^3 + 12\omega_3^2\omega_2^3 - 30\omega_3^2\omega_4^3\omega_2^2 + 18\omega_3^2\omega_4\omega_2^3$$

$$C_{49} = 36\omega_6\omega_3^2cs^2\omega_2^3 + 24\omega_6^2\omega_3^2v_2^2\omega_2^2 - 12\omega_6^2\omega_3^2cs^2\omega_2^2 + 36\omega_6\omega_3^2v_2^2\omega_2^3 + 48\omega_6^2v_2^2\omega_2^3 - 12\omega_6^2cs^2\omega_2^3 - 5\omega_6^2\omega_3^2v_2^2\omega_2^3 - 24\omega_6\omega_3^2cs^2\omega_2^2 - 24\omega_6\omega_3^2v_2^2\omega_2^2 + 4\omega_6^2\omega_3^2cs^2\omega_2^3 + 36\omega_6^2\omega_3cs^2\omega_2^3 - 90\omega_6^2\omega_3v_2^2\omega_2^3 - 12\omega_3^2cs^2\omega_2^3 - 12\omega_3^2v_2^2\omega_2^3 + 6\omega_6^2\omega_3^2cs^2\omega_2 - 30\omega_6^2\omega_3^2v_2^2\omega_2 - 24\omega_6^2\omega_3cs^2\omega_2^2 + 48\omega_6^2\omega_3v_2^2\omega_2^2 + 12\omega_6\omega_3^2v_2^2\omega_2^2 - 32\omega_6^2\omega_3^2cs^2\omega_2^3 + 40\omega_6^2\omega_3^2v_2^2\omega_2^3 + 12\omega_6\omega_3^2cs^2\omega_2^2 + 48\omega_6^2\omega_3^2cs^2\omega_2^2 - 12\omega_6\omega_3^2v_2^2\omega_2^3 - 12\omega_6\omega_3^2cs^2\omega_2^3 - 60\omega_6^2\omega_3^2v_2^2\omega_2^2 + 24\omega_6^2\omega_3^2v_2^2\omega_2 - 12\omega_6^2\omega_3cs^2\omega_2 - 12\omega_6\omega_3cs^2\omega_2^2 - 12\omega_6\omega_3v_2^2\omega_2^2 + 6\omega_3^2v_2^2\omega_2^2 + 6\omega_3^2cs^2\omega_2^2 + 12\omega_6^2\omega_3^2v_2^2$$

$$C_{50} = -12\omega_6^2\omega_3^2\omega_4cs^2 + 6\omega_6^2\omega_3^2\omega_4^3cs^2 - 30\omega_6^2\omega_3v_2^2\omega_4^3 + 6\omega_6\omega_3^2\omega_4^3 - 6\omega_6^2\omega_3\omega_4^3 + 42\omega_6\omega_3^2\omega_4^3cs^2 - 12\omega_3^2v_2^2\omega_4^3 - 24\omega_6\omega_3\omega_4^3cs^2 - 12\omega_6^2\omega_3^2v_2^2\omega_4 - 21\omega_6\omega_3^2\omega_4^3 - 36\omega_6^2\omega_3^2cs^2 + 12\omega_6^2\omega_3v_2^2\omega_4^3 - 3\omega_6\omega_3^2\omega_4^3 - 12\omega_3^2\omega_4^3cs^2 + 6\omega_6^2\omega_3^2v_2^2\omega_4^3 + 42\omega_6\omega_3^2v_2^2\omega_4^3 - 12\omega_6^2\omega_3^2\omega_4^3cs^2 + 24\omega_6^2v_2^2\omega_4^3 + 6\omega_6\omega_3^2\omega_4^3 - 12\omega_6\omega_3^2v_2^2\omega_4^3 + 78\omega_6^2\omega_3\omega_4^3cs^2 - 12\omega_6\omega_3^2\omega_4^3cs^2 + 6\omega_6^2\omega_3^2v_2^2\omega_4^3 + 6\omega_6^2\omega_3^2\omega_4^3 + \omega_6^2\omega_3^2\omega_4^3 - 24\omega_6\omega_3v_2^2\omega_4^3 + 6\omega_3^2v_2^2\omega_4^3 - 12\omega_6\omega_3^2\omega_4^3cs^2 - \omega_6^2\omega_3^2\omega_4^3 + 6\omega_6^2\omega_3^2\omega_4cs^2 - 48\omega_6^2\omega_3^2\omega_4^3cs^2 + 6\omega_6\omega_3^2\omega_4^3cs^2 + 12\omega_6\omega_3\omega_4^3 - 3\omega_6^2\omega_3^2\omega_4^3 + 6\omega_6\omega_3^2v_2^2\omega_4^3 + 6\omega_6^2\omega_3^2v_2^2\omega_4^3 - 3\omega_3^2\omega_4^3 + 42\omega_6^2\omega_3^2\omega_4^3cs^2 - 24\omega_6\omega_3\omega_4^3cs^2 - 12\omega_6\omega_3^2v_2^2\omega_4^3 + 6\omega_3^2\omega_4^3cs^2 - 12\omega_6^2\omega_3^2v_2^2\omega_4^3 + 7\omega_6^2\omega_3^2\omega_4^3 + 6\omega_6^2\omega_3^2v_2^2$$

$$C_{51} = -12\omega_6^2\omega_3^2\omega_4cs^2 + 4\omega_6^2\omega_3^2\omega_4^3cs^2 - 30\omega_6^2\omega_3v_2^2\omega_4^3 + 12\omega_6\omega_3^2\omega_4^3 + 36\omega_6\omega_3^2\omega_4^3cs^2 - 12\omega_3^2v_2^2\omega_4^3 - 24\omega_6^2\omega_3\omega_4^3cs^2 - 18\omega_6^2\omega_3^2v_2^2\omega_4 - 6\omega_6\omega_3^2\omega_4^3 - 12\omega_6^2\omega_4^3cs^2 - 6\omega_6\omega_3^2\omega_4^3 - 12\omega_3^2\omega_4^3cs^2 + 36\omega_6\omega_3^2v_2^2\omega_4^3 - 12\omega_6^2\omega_3^2\omega_4^3cs^2 + 24\omega_6^2v_2^2\omega_4^3 + 3\omega_6\omega_3^2\omega_4^3 - 24\omega_6\omega_3^2v_2^2\omega_4^3 + 2\omega_6^2\omega_3^2\omega_4^3 - 12\omega_6\omega_3v_2^2\omega_4^3 + 6\omega_3^2v_2^2\omega_4^3 - 12\omega_6\omega_3^2\omega_4^3cs^2 - \omega_6^2\omega_3^2\omega_4^3 + 6\omega_6^2\omega_3^2\omega_4cs^2 - 32\omega_6^2\omega_3^2\omega_4^3cs^2 + 12\omega_6\omega_3^2\omega_4^3cs^2 - 6\omega_6^2\omega_3^2\omega_4^3 + 12\omega_6\omega_3^2v_2^2\omega_4^3 + 48\omega_6^2\omega_3^2\omega_4^3cs^2 - 12\omega_6\omega_3\omega_4^3cs^2 - 12\omega_6\omega_3^2v_2^2\omega_4^3 + 6\omega_3^2\omega_4^3cs^2 + 12\omega_6^2\omega_3^2v_2^2\omega_4^3 + 3\omega_6^2\omega_3^2\omega_4^3 + 12\omega_6^2\omega_3^2v_2^2$$

$$C_{52} = 6\omega_3^3cs^2 - 36\omega_6\omega_3cs^2 + 12\omega_3^3 + 24\omega_6\omega_3 - 44\omega_6^2\omega_3^2cs^2 - 12\omega_6\omega_3^2v_2^2 - 6\omega_3^3 - 36\omega_6\omega_3^2 - 12\omega_3^2cs^2 + 12\omega_6^2v_2^2 + 48\omega_6\omega_3^2v_2^2 + 4\omega_6^2\omega_3^3cs^2 + 9\omega_6\omega_3^3 + 6\omega_3^3v_2^2 - 36\omega_6\omega_3v_2^2 - \omega_6^2\omega_3^3 - 8\omega_6^2\omega_3^2v_2^2 - 12\omega_6\omega_3^3cs^2 + 11\omega_6^2\omega_3^3 + 90\omega_6\omega_3cs^2 - 12\omega_6^2\omega_3 - 12\omega_3^2v_2^2 - 48\omega_6^2cs^2 + 48\omega_6\omega_3^2cs^2 + \omega_6^2\omega_3^3v_2^2$$

$$C_{53} = 12\omega_6^2\omega_4cs^2 - 6\omega_4^3cs^2\omega_2 + 12v_3^2\omega_4^2\omega_2 + 12\omega_7\omega_4cs^2\omega_2 + 9v_3^2\omega_7\omega_4^3\omega_2 + 12\omega_7\omega_4^2cs^2 + 22\omega_7^2\omega_4^2cs^2\omega_2 - 30v_3^2\omega_7\omega_4^3\omega_2 - 6v_3^2\omega_7\omega_4^3 - 6v_3^2\omega_4^2\omega_2 + 12v_3^2\omega_7\omega_4^3 + 36v_3^2\omega_7^2\omega_4\omega_2 + 9\omega_7\omega_4^3cs^2\omega_2 - 6\omega_7\omega_4^3cs^2 - 10v_3^2\omega_7^2\omega_2 - 10v_3^2\omega_7^2\omega_2 + 6\omega_7^2\omega_4^3cs^2\omega_2 - v_3^2\omega_7^2\omega_4^3 + 12v_3^2\omega_7\omega_4\omega_2 - 24v_3^2\omega_7^2\omega_2 + 12\omega_4^3cs^2\omega_2 + 3\omega_7^2\omega_4^3cs^2 + 12\omega_7^2cs^2\omega_2 + v_3^2\omega_7^2\omega_4^3\omega_2 - 30\omega_7\omega_4^2cs^2\omega_2 - 18\omega_7^2\omega_4^2cs^2 - 2\omega_7^2\omega_4^3cs^2\omega_2 - 12v_3^2\omega_7^2\omega_4$$

$$C_{54} = 24\omega_7\omega_4\omega_3^3 - 12\omega_7\omega_4\omega_2^2 - 6\omega_4^2\omega_3^3 + 12\omega_7\omega_4^2\omega_2^2 - 6\omega_7\omega_4^3 + 12\omega_4^2\omega_2^2 - 10\omega_7\omega_4^2\omega_2^2 + 12\omega_7\omega_4^3\omega_2 - 7\omega_7\omega_4^3\omega_2^2 - 12\omega_7\omega_2^3 + 3\omega_4^3\omega_2^3 + \omega_7\omega_4^3\omega_2^2 - 6\omega_7\omega_4^3\omega_2 - 6\omega_4^3\omega_2^2$$

$$C_{55} = 10v_3^2v_1^2\omega_7^2\omega_4^3\omega_5\omega_2^2 + 4\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 3v_3^2\omega_7^2\omega_4^3cs^2\omega_5\omega_2^2 + v_1^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 20v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2 + 2v_1^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2^2 + \omega_7\omega_4^3cs^4\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2 + 4v_3^2\omega_7^2\omega_4cs^2\omega_5^2\omega_2^2 - 4v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 20v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2 - 4v_1^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 10v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2 - \omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 4v_3^2v_1^2\omega_7\omega_4\omega_5^2\omega_2^2 - 3v_3^2v_1^2\omega_7^2\omega_4^3\omega_5\omega_2^2 - 8v_3^2\omega_7^2\omega_4cs^2\omega_5^2\omega_2^2 - 2\omega_7\omega_4^3cs^4\omega_5^2\omega_2^2 - 3v_1^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2 - 4v_1^2\omega_7^2cs^2\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 4v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 12v_1^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 4v_1^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2 - 4v_3^2v_1^2\omega_7\omega_4^3\omega_5^2\omega_2^2 + 10v_1^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2^2 - 36v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 4\omega_7\omega_4^3cs^4\omega_5^2\omega_2^2 + 2v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 8v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 2v_3^2\omega_7^2\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 4v_3^2v_1^2\omega_7^2\omega_4^3\omega_5\omega_2 - 2\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2 - 2\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 4v_1^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2^2 + 2v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 20v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 2v_1^2\omega_7^2\omega_4^3cs^2\omega_5\omega_2^2 + 12v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 20v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 2v_3^2v_1^2\omega_7^2\omega_4^3\omega_5\omega_2^2 + 4v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 10v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2 - 2v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 2v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 + 4v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 - 38v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 4v_3^2v_1^2\omega_7^2\omega_4\omega_5^2\omega_2^2 + 10v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2 - 2v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 2v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + \omega_7^2\omega_4^3cs^4\omega_5\omega_2^2 - 2v_1^2\omega_7^2\omega_4^3cs^2\omega_5\omega_2^2 - 4v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 - 8v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 - 3v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 4v_1^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2^2 - 4v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 2\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2 - 4v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 4v_1^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + v_3^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2^2 - 4v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + 20v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 10v_3^2v_1^2\omega_7\omega_4^3\omega_5^2\omega_2^2 + v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 + v_1^2\omega_7^2\omega_4^3cs^2\omega_5\omega_2^2 + 2v_3^2\omega_7^2\omega_4^3cs^2\omega_5^2\omega_2^2 - 4v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 - 2\omega_7^2\omega_4^3cs^4\omega_5\omega_2^2 - 2v_3^2\omega_7\omega_4^3cs^2\omega_5^2\omega_2^2 + 2v_3^2v_1^2\omega_7^2\omega_4^3\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^4\omega_5^2\omega_2^2$$

$$C_{56} = 6v_3^2\omega_4^3\omega_2^3 + 24v_3^2\omega_7\omega_4^2\omega_2^3 + 24v_3^2\omega_7^2\omega_4\omega_2^3 - 14\omega_7^2\omega_4^2cs^2\omega_2^3 - 6\omega_7\omega_4^3cs^2\omega_2^3 + 12\omega_7^2\omega_4^2cs^2\omega_2^2 - 78v_3^2\omega_7^2\omega_4\omega_2^3 - 12\omega_7^2\omega_4^2cs^2\omega_2 - 6v_3^2\omega_7\omega_4^3\omega_2^3 - 12\omega_7\omega_4^2cs^2\omega_2^2 - 12v_3^2\omega_4^2\omega_2^3 + 6\omega_4^3cs^2\omega_2^3 - 6\omega_7^2\omega_4^3cs^2\omega_2^2 + 24v_3^2\omega_7^2\omega_2^3 + 24\omega_7\omega_4^2cs^2\omega_2^3 - 4v_3^2\omega_7^2\omega_4^3\omega_2^3 - 12\omega_7^2cs^2\omega_2^3 + 22v_3^2\omega_7^2\omega_4\omega_2^3 + 12v_3^2\omega_7^2\omega_4^3 + \omega_7^2\omega_4^3cs^2\omega_2^3 + 24\omega_7^2\omega_4cs^2\omega_2^3 - 30v_3^2\omega_7^2\omega_4^3\omega_2^2 + 34v_3^2\omega_7^2\omega_4^2\omega_2^3 - 12\omega_4^2cs^2\omega_2^3 + 48v_3^2\omega_7^2\omega_4\omega_2^3 + 6\omega_7^2\omega_4^3cs^2\omega_2^3 - 12v_3^2\omega_7\omega_4\omega_2^3$$

$$C_{57} = 6v_1^2\omega_4^3\omega_2^3 - 4v_1^2\omega_4^3\omega_5^2\omega_2^3 + 34v_1^2\omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2 - 12v_1^2\omega_4^3\omega_2^3 + 24\omega_4^3cs^2\omega_5\omega_2^2 - 78v_1^2\omega_4^3\omega_5^2\omega_2 + 24v_1^2\omega_4\omega_5^2\omega_2^2 - 12\omega_4cs^2\omega_5^2\omega_2^2 + 6\omega_4^3cs^2\omega_2^2 - 30v_1^2\omega_4\omega_5^2\omega_2^2 - 6\omega_4^3cs^2\omega_5\omega_2^2 + 12v_1^2\omega_5^2\omega_2^3 - 12\omega_4^3cs^2\omega_2^2 + 6\omega_4cs^2\omega_5^2\omega_2^2 - 48v_1^2\omega_4^3\omega_5^2\omega_2^2 + \omega_3^2cs^2\omega_5^2\omega_2^2 - 12v_1^2\omega_4^3\omega_5\omega_2 - 14\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 + 22v_1^2\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^3cs^2\omega_5^2\omega_2^2 + 24\omega_4^3cs^2\omega_5^2\omega_2 + 24v_1^2\omega_3^3\omega_5\omega_2^2 - 6\omega_7^2cs^2\omega_5^2\omega_2^2 + 48v_1^2\omega_4^3\omega_5^2 + 24v_1^2\omega_4^3\omega_5^2\omega_2 - 6v_1^2\omega_4^3\omega_5\omega_2^2$$

$$C_{58} = 12\omega_7^2\omega_4cs^2 + 12\omega_3v_3^2\omega_4^2 - 10\omega_3v_3^2\omega_7^2\omega_4^2 - 6\omega_3v_3^2\omega_4^3 - 2\omega_3\omega_7^2\omega_4^3cs^2 + 12\omega_7\omega_4^2cs^2 + \omega_3v_3^2\omega_7^2\omega_4^3 - 6v_3^2\omega_7\omega_4^3 - 24\omega_3v_3^2\omega_7^2 + 12\omega_3\omega_7\omega_4cs^2 + 12v_3^2\omega_7\omega_4^2 + 36\omega_3v_3^2\omega_7^2\omega_4 + 12\omega_3\omega_7^2cs^2 - 6\omega_7\omega_4^3cs^2 + 22\omega_3\omega_7^2\omega_4^2cs^2 + 6v_3^2\omega_7^2\omega_4^2 + 12\omega_3v_3^2\omega_7\omega_4 - 6\omega_3\omega_4^3cs^2 - 30\omega_3\omega_7^2\omega_4cs^2 - v_3^2\omega_7^2\omega_4^3 + 3\omega_7^2\omega_4^3cs^2 - 30\omega_3\omega_7\omega_4^2cs^2 + 12\omega_3\omega_4^2cs^2 + 9\omega_3v_3^2\omega_7\omega_4^3 + 9\omega_3\omega_7\omega_4^3cs^2 - 18\omega_7^2\omega_4^2cs^2 - 30\omega_3v_3^2\omega_7\omega_4^2 - 12v_3^2\omega_7^2\omega_4$$

$$C_{59} = -10\omega_3^3\omega_7\omega_4^2 + \omega_3^3\omega_7\omega_4^3 + 12\omega_3\omega_7\omega_4^3 + 24\omega_3^3\omega_7\omega_4 - 6\omega_3\omega_7\omega_4^2 - 6\omega_3^2\omega_4^3 - 7\omega_3^2\omega_7\omega_4^3 - 6\omega_7\omega_4^3 + 12\omega_3^2\omega_4^2 + 12\omega_3^2\omega_7\omega_4^2 - 12\omega_3^2\omega_7\omega_4 + 3\omega_3^3\omega_4^3 - 12\omega_3^3\omega_7 - 6\omega_3^3\omega_4^2$$

$$C_{60} = 6\omega_3^2\omega_7^2\omega_4cs^2\omega_2^3 - 2\omega_3^2v_3^2\omega_7\omega_4^2\omega_2^3 + 6\omega_3^2\omega_7^2\omega_4cs^2\omega_2^3 - 8\omega_3^2v_3^2\omega_7\omega_4^3\omega_2 + 12\omega_3^2v_3^2\omega_7^2\omega_4^2\omega_2^3 + 7\omega_3^2v_3^2\omega_7^2\omega_4\omega_2^3 - 2\omega_3^2\omega_7^2cs^2\omega_2^2 + \omega_7^2\omega_4^3cs^2\omega_2^3 - 12\omega_3^2v_3^2\omega_7^2\omega_2^3 - 2\omega_3\omega_7^2\omega_4^2cs^2\omega_2^3 + \omega_3^2\omega_7^2\omega_4^2cs^2\omega_2^3 - 2\omega_3^2v_3^2\omega_7\omega_4\omega_2^3 - 2\omega_3^2v_3^2\omega_7^2\omega_2^3 - 2\omega_3^2\omega_7^2\omega_4cs^2\omega_2^2 + \omega_3^2\omega_4^3cs^2\omega_2^3 - 2\omega_3^2\omega_7^2\omega_4cs^2\omega_2^2 + 4\omega_3^2v_3^2\omega_7\omega_4^2\omega_2 + 6\omega_3^2\omega_7\omega_4^2cs^2\omega_2^2 - 2\omega_3^2v_3^2\omega_7^2\omega_4\omega_2^3 + \omega_3^2v_3^2\omega_7\omega_4^2\omega_2^3 + \omega_3^2\omega_7^2\omega_4^2\omega_2^3 + \omega_3^2\omega_7^2\omega_4cs^2\omega_2^2 -$$



$$\begin{aligned}
C_{73} &= 36\omega_3^3 v_3^2 \omega_7 \omega_4^2 - 6\omega_3^3 \omega_7 \omega_4^2 - 24\omega_3^2 \omega_7^2 \omega_4 cs^2 - 12\omega_3^3 \omega_7 \omega_4^3 cs^2 - 12\omega_3^3 \omega_7^2 cs^2 - 24\omega_3^2 \omega_7 \omega_4^2 cs^2 + 6\omega_3 \omega_7^2 \omega_4^3 cs^2 + 24\omega_3^3 v_3^2 \omega_7^2 + 3\omega_3^3 \omega_7 \omega_4^3 - \\
&12\omega_3^3 v_3^2 \omega_7 \omega_4^3 - 18\omega_3 v_3^2 \omega_7^2 \omega_4^3 + 12\omega_3^2 v_3^2 \omega_7 \omega_4^3 + 36\omega_3^3 \omega_7 \omega_4^2 cs^2 - 6\omega_3^2 \omega_7^2 \omega_4^3 + 6\omega_3^3 v_3^2 \omega_4^3 + 36\omega_3^3 \omega_7^2 \omega_4 cs^2 - 24\omega_3^2 v_3^2 \omega_7 \omega_4^2 - 12\omega_3^3 v_3^2 \omega_4^2 - \\
&12\omega_3^3 v_3^2 \omega_7 \omega_4 - 12\omega_3 \omega_7^2 \omega_4^2 cs^2 + 12\omega_3^2 \omega_7 \omega_4^3 cs^2 + 2\omega_3^2 \omega_7^2 \omega_4^3 - 32\omega_3^3 \omega_7^2 \omega_4^2 cs^2 + 12\omega_3^2 v_3^2 \omega_7^2 \omega_4^2 - 30\omega_3^3 v_3^2 \omega_7^2 \omega_4 - 6\omega_3^2 \omega_7 \omega_4^3 + 12v_3^2 \omega_7^2 \omega_4^3 - \\
&12\omega_3^3 \omega_7 \omega_4 cs^2 - 12\omega_3^3 \omega_4^2 cs^2 - 12\omega_3^2 \omega_7^2 \omega_4^3 cs^2 + 12\omega_3^2 \omega_7 \omega_4^2 - \omega_3^3 \omega_7^2 \omega_4^3 + 3\omega_3^3 v_3^2 \omega_7^2 \omega_4^3 + 4\omega_3^3 \omega_7^2 \omega_4^3 cs^2 + 3\omega_3^3 \omega_7^2 \omega_4^3 + 48\omega_3^2 \omega_7^2 \omega_4^2 cs^2 + 6\omega_3^3 \omega_4^3 cs^2 \\
C_{74} &= 12\omega_7^2 \omega_4 cs^2 - 18v_3^4 \omega_7 \omega_4^3 + 48v_3^3 \omega_7 \omega_4 + 24\omega_7 \omega_4 cs^4 + 6v_3^2 \omega_7^2 \omega_4^3 cs^2 + 72v_3^4 \omega_7 \omega_4^2 + 24\omega_7 \omega_4^2 cs^2 + 24\omega_7^2 \omega_4^2 cs^4 - 72v_3^2 \omega_7^2 \omega_4^2 cs^2 + 12v_3^4 \omega_4^3 + \\
&18v_3^3 \omega_7 \omega_4^3 - 48v_3^4 \omega_7 \omega_4 - 72v_3^2 \omega_7 \omega_4^2 - 24v_3^4 \omega_4^3 - 3\omega_7^2 \omega_4^3 cs^4 - 24v_3^2 \omega_7 \omega_4 cs^2 - 6\omega_7 \omega_4^3 cs^2 + 24\omega_7^2 cs^4 - 96v_3^2 \omega_7^2 cs^2 + 24v_3^2 \omega_7^2 \omega_4^2 + \\
&48v_3^3 \omega_7 \omega_4^2 cs^2 + 12v_3^2 \omega_4^3 cs^2 + 6\omega_7 \omega_4^3 cs^4 + 156v_3^2 \omega_7^2 \omega_4 cs^2 - 3v_3^2 \omega_7^2 \omega_4^3 + 24v_3^4 \omega_7^2 \omega_4 + \omega_7^2 \omega_4^3 cs^2 + 24v_3^2 \omega_4^2 - 24v_3^4 \omega_7^2 \omega_4 - 24v_3^2 \omega_4^2 cs^2 - \\
&24\omega_7 \omega_4 cs^2 - 48\omega_7^2 \omega_4 cs^4 - 12v_3^2 \omega_7 \omega_4^3 cs^2 - 8\omega_7^2 \omega_4^2 cs^2 + 3v_3^4 \omega_7^2 \omega_4^3 - 12v_3^2 \omega_4^3 - 24v_3^2 \omega_7 \omega_4 - 24\omega_7 \omega_4^2 cs^4 \\
C_{75} &= 42\omega_7^2 \omega_4 cs^2 - 12v_3^2 \omega_7 \omega_4 - 12\omega_4^2 cs^2 - 6\omega_7^2 \omega_4 + 24\omega_7 \omega_4^2 cs^2 + 6\omega_4^3 cs^2 - 6v_3^2 \omega_7 \omega_4^3 + 8\omega_7^2 \omega_4^2 + 24v_3^2 \omega_7 \omega_4^2 - 6\omega_7 \omega_4^3 cs^2 - \omega_7^2 \omega_4^3 - 16v_3^2 \omega_7^2 \omega_4^2 - \\
&6\omega_4^3 - 12v_3^2 \omega_7^2 + 6\omega_7 \omega_4^3 - 24\omega_7^2 cs^2 + 2v_3^2 \omega_7^2 \omega_4^3 - 24\omega_7 \omega_4^2 + 12\omega_4^2 + \omega_7^2 \omega_4^3 cs^2 + 12\omega_7 \omega_4 - 12v_3^2 \omega_4^2 - 12\omega_7 \omega_4 cs^2 - 20\omega_7^2 \omega_4^2 cs^2 + 6v_3^2 \omega_4^3 + 24v_3^2 \omega_7^2 \omega_4
\end{aligned}$$

## 2.3 MRT2

### 2.3.1 Definitions

Collision operator  $C$ :

$$C(f) = \mathbf{M}_2^{-1} \mathbf{S} \left( \mu_2^{(eq)} - \mathbf{M}_2 f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2)$ .

Matrix  $\mathbf{M}_2$  corresponds to the transformation matrix to the raw moment basis defined by

$$\mu_2 = \begin{pmatrix} m_{(0,0,0)} \\ m_{(1,0,0)} \\ m_{(0,1,0)} \\ m_{(0,0,1)} \\ m_{(2,0,0)} + m_{(0,2,0)} + m_{(0,0,2)} \\ m_{(2,0,0)} - m_{(0,2,0)} \\ m_{(2,0,0)} - m_{(0,0,2)} \end{pmatrix},$$

and is given by

$$\mathbf{M}_2 = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & -1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & -1 & 1 & 0 & -1 \end{pmatrix}.$$

The equilibrium moments  $\mu_2^{(eq)}$  are defined by

$$\mu_2^{(eq)} = \mathbf{M}_2 \mathbf{M}^{-1} \mu^{(eq)},$$

i.e.,

$$\mu_2^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho(v_3^2 + v_2^2 + v_1^2 + 3c_s^2) \\ \rho(v_1^2 - v_2^2) \\ \rho(v_1^2 - v_3^2) \end{pmatrix}.$$

### 2.3.2 Conservation of mass equation



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$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\ & (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\delta_l^2 \rho}{2\omega_2 \delta_t} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\ & (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{\delta_l^2 \rho}{\omega_2 \omega_3 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\ & (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{\delta_l^2 \rho}{\omega_4 \omega_2 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + \\ & + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\delta_l^2 \rho}{2\omega_3 \delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\ & (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{\delta_l^2 \rho}{\omega_4 \omega_3 \delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_3 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + \\ & + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_3 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l^2 \rho}{2\omega_4 \delta_t} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + \\ & (-2 + \omega_2) \frac{\delta_l \rho}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{cs^2 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \delta_l^2 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\delta_l \rho}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + \\ & (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \delta_l^2 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\ & (-2 + \omega_3) \frac{v_2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\delta_l \rho}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + (\omega_4 + \omega_2 - \omega_4 \omega_2) \frac{v_3 v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \delta_l^2 \rho}{2\omega_4 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\ & (2 - \omega_2) \frac{v_1 \delta_l^2 \rho}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_3 v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \delta_l^2 \rho}{2\omega_4 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + \\ & (-2 + \omega_4) \frac{cs^2 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{v_3 \delta_l^2 \rho}{2\omega_4 \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + (12 + \omega_2^2 - 12\omega_2) \frac{\delta_l \rho \delta_t}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 - 6\omega_5 - 6\omega_2 + \omega_5 \omega_2) \frac{v_1 \delta_l^2 \rho}{6\omega_5 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + \\ & + C_1 \frac{v_1 \delta_l^3}{6\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + (12 - 12\omega_3 + \omega_3^2) \frac{\delta_l \rho \delta_t}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + \\ & (-6\omega_2 - 2\omega_2 \omega_3^2 + 9\omega_2 \omega_3 - 6\omega_3 + 3\omega_3^2) \frac{v_2 \delta_l^2 \rho}{6\omega_2 \omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + (-2\omega_2^2 \omega_3 + 3\omega_2^2 - 6\omega_2 + 9\omega_2 \omega_3 - 6\omega_3) \frac{v_1 \delta_l^2 \rho}{6\omega_2^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + \\ & C_3 \frac{v_2 \delta_l^3}{2\omega_5 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (-6\omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 + 6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2) \frac{v_2 v_1 \delta_l^3 \rho}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + (-12\omega_2 v_1^2 + 6cs^2 \omega_2^2 - 6\omega_5 \omega_2 v_1^2 + \\ & 18cs^2 \omega_5 \omega_2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 - 12cs^2 \omega_5 + \omega_5 \omega_2^2 v_1^2 + 12\omega_5 v_1^2 + 6\omega_2^2 v_1^2) \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\ & (12 - 6\omega_6 - 6\omega_3 + \omega_6 \omega_3) \frac{v_2 \delta_l^2 \rho}{6\omega_6 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\omega_2^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-3cs^2 \omega_6 \omega_3^2 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_6 \omega_3 + 18cs^2 \omega_6 \omega_3 + \\ & 6cs^2 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 - 12v_2^2 \omega_3 + 12v_2^2 \omega_6 - 12cs^2 \omega_6) \frac{\delta_l^3 \rho}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & (-6\omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 + 6\omega_2^2 - 6\omega_2 \omega_3^2 + 6\omega_3^2) \frac{v_2 v_1 \delta_l^3 \rho}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\delta_l^3 \rho}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\ & (12 - 12\omega_4 + \omega_4^2) \frac{\delta_l \rho \delta_t}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-2\omega_4^2 \omega_2 - 6\omega_4 + 3\omega_4^2 - 6\omega_2 + 9\omega_4 \omega_2) \frac{v_3 \delta_l^2 \rho}{6\omega_4^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\ & (-6\omega_4 + 3\omega_2^2 - 6\omega_2 - 2\omega_4 \omega_2^2 + 9\omega_4 \omega_2) \frac{v_1 \delta_l^2 \rho}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3 \delta_l^3}{2\omega_4^2 \omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\ & (-6\omega_4^2 \omega_2 + 6\omega_4^2 + 6\omega_2^2 + \omega_4^2 \omega_2^2 - 6\omega_4 \omega_2^2) \frac{v_3 v_1 \delta_l^3 \rho}{6\omega_4^2 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + (-12\omega_2 v_1^2 + 6cs^2 \omega_2^2 - 6\omega_5 \omega_2 v_1^2 + 18cs^2 \omega_5 \omega_2 - \\ & 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 - 12cs^2 \omega_5 + \omega_5 \omega_2^2 v_1^2 + 12\omega_5 v_1^2 + 6\omega_2^2 v_1^2) \frac{\delta_l^3 \rho}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \end{aligned}$$

$$\begin{aligned}
& (-6\omega_4 + 3\omega_4^2 + 9\omega_4\omega_3 - 2\omega_4^2\omega_3 - 6\omega_3) \frac{v_3\delta_1^2\rho}{6\omega_4^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-6\omega_4 - 2\omega_4\omega_3^2 + 9\omega_4\omega_3 - 6\omega_3 + 3\omega_3^2) \frac{v_2\delta_1^2\rho}{6\omega_4\omega_3^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_4^2\omega_2^2\omega_3^2 + \omega_4\omega_2\omega_3^2 + \omega_2^2\omega_3^2 - 2\omega_4^2\omega_2^2\omega_3 + \omega_4^2\omega_2^2 + \omega_4^2\omega_2\omega_3 + \omega_4\omega_2^2\omega_3 + \omega_4^2\omega_3^2 - 2\omega_4\omega_2^2\omega_3^2 - 2\omega_4^2\omega_2\omega_3^2) \frac{2v_3v_2v_1\delta_1^3}{\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (-6\omega_4\omega_3^2 + 3\omega_4^2 + 6\omega_4\omega_3 - 6\omega_4^2\omega_3 + 3\omega_3^2 + 2\omega_4^2\omega_3^2) \frac{v_3v_2\delta_1^3\rho}{3\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_4^2\omega_2 + 3\omega_4^2 + 3\omega_2^2 + 2\omega_4^2\omega_2^2 - 6\omega_4\omega_2^2 + 6\omega_4\omega_2) \frac{v_3v_1\delta_1^3\rho}{3\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2^2\omega_3 + 2\omega_2^2\omega_3^2 + 3\omega_2^2 - 6\omega_2\omega_3^2 + 6\omega_2\omega_3 + 3\omega_3^2) \frac{v_2v_1\delta_1^3\rho}{3\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_1^3}{2\omega_4^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_4\omega_3^2 + 6\omega_4^2 - 6\omega_4^2\omega_3 + 6\omega_3^2 + \omega_4^2\omega_3^2) \frac{v_3v_2\delta_1^3\rho}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + (-3cs^2\omega_6\omega_3^2 + v_2^2\omega_6\omega_3^2 - 6v_2^2\omega_6\omega_3 + 18cs^2\omega_6\omega_3 + \\
& 6cs^2\omega_3^2 + 6v_2^2\omega_3^2 - 12cs^2\omega_3 - 12v_2^2\omega_3 + 12v_2^2\omega_6 - 12cs^2\omega_6) \frac{\delta_1^3\rho}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (12 - 6\omega_7 - 6\omega_4 + \omega_7\omega_4) \frac{v_3\delta_1^2\rho}{6\omega_7\omega_4} \frac{\partial^3 v_3}{\partial t \partial x_3} \\
& + C_9 \frac{v_1\delta_1^3}{2\omega_7\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3} + \\
& (6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 - 6\omega_7\omega_4v_3^2 - 12\omega_4v_3^2 + 6\omega_4^2v_3^2 + 12\omega_7v_3^2 + \omega_7\omega_4^2v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_4cs^2) \frac{\delta_1^3\rho}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3} \\
& + (-6\omega_4^2\omega_2 + 6\omega_4^2 + 6\omega_2^2 + \omega_4^2\omega_2^2 - 6\omega_4\omega_2^2) \frac{v_3v_1\delta_1^3\rho}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3} + C_{10} \frac{v_2\delta_1^3}{2\omega_7\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& (6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 - 12\omega_7cs^2 - 6\omega_7\omega_4v_3^2 - 12\omega_4v_3^2 + 6\omega_4^2v_3^2 + 12\omega_7v_3^2 + \omega_7\omega_4^2v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_4cs^2) \frac{\delta_1^3\rho}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + (-6\omega_4\omega_3^2 + 6\omega_4^2 - 6\omega_4^2\omega_3 + 6\omega_3^2 + \omega_4^2\omega_3^2) \frac{v_3v_2\delta_1^3\rho}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3\delta_1^3}{6\omega_7\omega_4^2\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\delta_1^3\rho}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2 - \omega_2^2 + 3\omega_2) \frac{\delta_1\rho\delta_t^2}{2\omega_3^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-\omega_5^2\omega_2^2 + 2\omega_2^2 - \omega_5^2\omega_2 - 4\omega_2^2 + 2\omega_5^2 - 4\omega_5\omega_2 + 8\omega_5\omega_2^2 - 2\omega_5\omega_2^3) \frac{v_1\delta_1^2\rho\delta_t}{2\omega_5^2\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + \\
& C_{13} \frac{\delta_1^3\rho}{12\omega_5^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_1^4}{24\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{v_1\delta_1^4\rho}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 + 3\omega_3 - \omega_3^2) \frac{\delta_1\rho\delta_t^2}{2\omega_3^3} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (-24\omega_2^2\omega_3 + 13\omega_2^2\omega_3^2 + 12\omega_2^2 - \omega_2^2\omega_3^3 + 7\omega_2\omega_3^3 - 24\omega_2\omega_3^2 + 12\omega_2\omega_3 + 12\omega_3^2 - 6\omega_3^3) \frac{v_2\delta_1^2\rho\delta_t}{12\omega_2^2\omega_3^3} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (-\omega_2^2\omega_3^2 - 24\omega_2^2\omega_3 - 6\omega_2^2 + 13\omega_2^2\omega_3^2 + 12\omega_2^2 + 7\omega_2^2\omega_3 - 24\omega_2\omega_3^2 + 12\omega_2\omega_3 + 12\omega_3^2) \frac{v_1\delta_1^2\rho\delta_t}{12\omega_2^2\omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& C_{16} \frac{v_2v_1\delta_1^3\rho}{6\omega_5\omega_3^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{\delta_1^3\rho}{12\omega_5^2\omega_3^2\omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{18} \frac{v_2v_1\delta_1^4}{6\omega_5^2\omega_3^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2} + C_{19} \frac{v_2\delta_1^4\rho}{12\omega_5^2\omega_3^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2} + \\
& C_{20} \frac{v_1\delta_1^4\rho}{12\omega_5^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + (-\omega_6^2\omega_3 - \omega_6^2\omega_3^2 - 2\omega_6\omega_3^3 + 8\omega_6\omega_3^2 - 4\omega_3^2 - 4\omega_6\omega_3 + 2\omega_6^2 + 2\omega_3^3) \frac{v_2\delta_1^2\rho\delta_t}{2\omega_6^2\omega_3^3} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + \\
& C_{21} \frac{\delta_1^3\rho}{12\omega_2\omega_6^2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + C_{22} \frac{v_2v_1\delta_1^3\rho}{6\omega_3^2\omega_6\omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + C_{23} \frac{\delta_1^4}{4\omega_2^2\omega_3^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{v_1\delta_1^4\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& C_{25} \frac{v_2\delta_1^4\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\delta_1^3\rho}{12\omega_2^2\omega_6^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + C_{27} \frac{v_2v_1\delta_1^4}{6\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{28} \frac{v_2\delta_1^4\rho}{12\omega_2^2\omega_6^2\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{29} \frac{v_1\delta_1^4\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} \\
& + C_{30} \frac{\delta_1^4}{24\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{31} \frac{v_2\delta_1^4\rho}{12\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (-2 + 3\omega_4 - \omega_4^2) \frac{\delta_1\rho\delta_t^2}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (-24\omega_4^2\omega_2 - 6\omega_4^3 - \omega_4^3\omega_2^2 + 12\omega_4^2 + 7\omega_4^2\omega_2 + 12\omega_2^2 + 13\omega_4^2\omega_2^2 - 24\omega_4\omega_2^2 + 12\omega_4\omega_2) \frac{v_3\delta_1^2\rho\delta_t}{12\omega_4^3\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (-24\omega_4^2\omega_2 + 12\omega_4^2 - 6\omega_2^2 - \omega_4^2\omega_3^2 + 12\omega_2^2 + 13\omega_4^2\omega_2^2 - 24\omega_4\omega_2^2 + 7\omega_4\omega_3^2 + 12\omega_4\omega_2) \frac{v_1\delta_1^2\rho\delta_t}{12\omega_4^2\omega_2^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} + \\
& C_{32} \frac{v_3v_1\delta_1^3\rho}{6\omega_4^2\omega_5\omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + C_{33} \frac{\delta_1^3\rho}{12\omega_4\omega_5^2\omega_2^2} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{34} \frac{v_3v_1\delta_1^4}{6\omega_4^2\omega_5^2\omega_2^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{35} \frac{v_3\delta_1^4\rho}{12\omega_4^2\omega_5^2\omega_2^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + \\
& C_{36} \frac{v_1\delta_1^4\rho}{12\omega_5^2\omega_2^2\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + \\
& (-6\omega_4^3 - 24\omega_4\omega_3^2 + 12\omega_4^2 + 12\omega_4\omega_3 - \omega_4^3\omega_3^2 - 24\omega_4^2\omega_3 + 12\omega_3^2 + 13\omega_4^2\omega_3^2 + 7\omega_4^3\omega_3) \frac{v_3\delta_1^2\rho\delta_t}{12\omega_4^3\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (7\omega_4\omega_3^3 - 24\omega_4\omega_3^2 + 12\omega_4^2 + 12\omega_4\omega_3 - 24\omega_4^2\omega_3 + 12\omega_3^2 + 13\omega_4^2\omega_3^2 - 6\omega_3^3 - \omega_4^2\omega_3^3) \frac{v_2\delta_1^2\rho\delta_t}{12\omega_4^2\omega_3^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_3v_2\delta_1^3\rho}{6\omega_4^2\omega_2\omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{38} \frac{v_3v_1\delta_1^3\rho}{6\omega_4^2\omega_2^2\omega_3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{39} \frac{v_2v_1\delta_1^3\rho}{6\omega_4\omega_2^2\omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{40} \frac{v_3v_2\delta_1^4}{\omega_4^2\omega_5^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{41} \frac{v_3v_2v_1\delta_1^4\rho}{6\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{42} \frac{v_3\delta_1^4\rho}{12\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{43} \frac{v_2\delta_1^4\rho}{12\omega_2^2\omega_3^2\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{44} \frac{v_3v_2\delta_1^3\rho}{6\omega_4^2\omega_6\omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{\delta_1^3\rho}{12\omega_4\omega_2^2\omega_3^2} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{46} \frac{v_3v_1\delta_1^4\rho}{\omega_4^2\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{47} \frac{v_3\delta_1^4\rho}{12\omega_4^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{48} \frac{v_3v_2v_1\delta_1^4\rho}{6\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{49} \frac{v_1\delta_1^4\rho}{12\omega_2^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{50} \frac{v_3v_2\delta_1^4\rho}{6\omega_4^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{51} \frac{v_3\delta_1^4\rho}{12\omega_4^2\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{52} \frac{v_2\delta_1^4\rho}{12\omega_6^2\omega_3^2\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& (8\omega_7\omega_4^2 + 2\omega_4^3 - 2\omega_7\omega_4^3 - 4\omega_4^2 + 2\omega_7^2 - 4\omega_7\omega_4 - \omega_7^2\omega_4 - \omega_7^2\omega_4^2) \frac{v_3\delta_1^2\rho\delta_t}{2\omega_7^2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + C_{53} \frac{\delta_1^3\rho}{12\omega_7\omega_4^2\omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& C_{54} \frac{v_3 v_1 \delta_1^3 \rho}{6\omega_7 \omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + C_{55} \frac{\delta_1^4}{4\omega_7 \omega_4^3 \omega_5^3 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{56} \frac{v_1 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{57} \frac{v_3 \delta_1^4 \rho}{12\omega_4^3 \omega_5^3 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{58} \frac{\delta_1^5 \rho}{12\omega_7 \omega_4^3 \omega_3} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + C_{59} \frac{v_3 v_2 \delta_1^3 \rho}{6\omega_7 \omega_4^3 \omega_3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + C_{60} \frac{v_2 v_1 \delta_1^4 \rho}{\omega_7 \omega_4^3 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{61} \frac{v_2 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{62} \frac{v_1 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \omega_2^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{63} \frac{v_3 v_2 v_1 \delta_1^4 \rho}{6\omega_4^3 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{64} \frac{\delta_1^4}{4\omega_7 \omega_4^3 \omega_6^3 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{65} \frac{v_2 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{66} \frac{v_3 \delta_1^4 \rho}{12\omega_4^3 \omega_6^3 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{67} \frac{\delta_1^5 \rho}{12\omega_7 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3^3} + C_{68} \frac{v_3 v_1 \delta_1^4 \rho}{6\omega_7 \omega_4^3 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{69} \frac{v_3 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{70} \frac{v_1 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} \\
& + C_{71} \frac{v_3 v_2 \delta_1^4 \rho}{6\omega_7 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{72} \frac{v_3 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{73} \frac{v_2 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{74} \frac{\delta_1^4}{24\omega_7 \omega_4^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{75} \frac{v_3 \delta_1^4 \rho}{12\omega_7 \omega_4^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -6\omega_2 v_1^2 + 3cs^2 \omega_2^2 + 3\omega_5 \omega_2 v_1^2 + 15cs^2 \omega_5 \omega_2 - 3cs^2 \omega_5 \omega_2^2 - 6cs^2 \omega_2 - 3\omega_2^2 + 6\omega_2 - 12cs^2 \omega_5 - 3\omega_5 \omega_2 + \omega_5 \omega_2^2 - \omega_5 \omega_2^2 v_1^2 + 3\omega_2^2 v_1^2 \\
C_2 &= -12\omega_2 v_1^2 + 6cs^2 \omega_2^2 + 18\omega_5 \omega_2 v_1^2 + 18cs^2 \omega_5 \omega_2 - 3cs^2 \omega_5 \omega_2^2 - 12cs^2 \omega_2 - 6\omega_2^2 + 12\omega_2 - 12cs^2 \omega_5 - 6\omega_5 \omega_2 + 2\omega_5 \omega_2^2 - 5\omega_5 \omega_2^2 v_1^2 - 12\omega_5 v_1^2 + 6\omega_2^2 v_1^2 \\
C_3 &= cs^2 \omega_5 \omega_2^2 \omega_3 - 3\omega_5 \omega_2^2 v_1^2 \omega_3 + \omega_2^2 v_1^2 \omega_3^2 - 2cs^2 \omega_2 \omega_3^2 + 4\omega_5 v_1^2 \omega_3^2 + \omega_5 \omega_2^2 v_1^2 \omega_3^2 - cs^2 \omega_5 \omega_2^2 \omega_3^2 + 4cs^2 \omega_5 \omega_2 \omega_3^2 - 4\omega_5 \omega_2 v_1^2 \omega_3^2 + 2\omega_5 \omega_2^2 v_1^2 + \\
& cs^2 \omega_2^2 \omega_3^2 - 2\omega_2 v_1^2 \omega_3^2 + 2\omega_5 \omega_2 v_1^2 \omega_3 - 2cs^2 \omega_5 \omega_3^2 - 2cs^2 \omega_5 \omega_2 \omega_3 \\
C_4 &= 2v_2^2 \omega_6 \omega_3^2 + cs^2 \omega_2 \omega_6 \omega_3^2 - 3v_2^2 \omega_2 \omega_6 \omega_3^2 + 2v_2^2 \omega_2 \omega_6 \omega_3 - 2cs^2 \omega_2 \omega_6 \omega_3 - 2cs^2 \omega_2^2 \omega_6 + 4v_2^2 \omega_2^2 \omega_6 - 4v_2^2 \omega_2^2 \omega_6 \omega_3 + 4cs^2 \omega_2^2 \omega_6 \omega_3 - 2v_2^2 \omega_2^2 \omega_3 - \\
& 2cs^2 \omega_2^2 \omega_3 + cs^2 \omega_2^2 \omega_3^2 + v_2^2 \omega_2^2 \omega_3^2 - cs^2 \omega_2^2 \omega_6 \omega_3^2 + v_2^2 \omega_2^2 \omega_6 \omega_3^2 \\
C_5 &= -3cs^2 \omega_6 \omega_3^2 - v_2^2 \omega_6 \omega_3^2 + 3v_2^2 \omega_6 \omega_3 + 15cs^2 \omega_6 \omega_3 + \omega_6 \omega_3^2 + 3cs^2 \omega_3^2 + 3v_2^2 \omega_3^2 - 6cs^2 \omega_3 - 6v_2^2 \omega_3 + 6\omega_3 - 3\omega_3^2 - 3\omega_6 \omega_3 - 12cs^2 \omega_6 \\
C_6 &= -3cs^2 \omega_6 \omega_3^2 - 5v_2^2 \omega_6 \omega_3^2 + 18v_2^2 \omega_6 \omega_3 + 18cs^2 \omega_6 \omega_3 + 2\omega_6 \omega_3^2 + 6cs^2 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 - 12v_2^2 \omega_3 + 12\omega_3 - 6\omega_3^2 - 6\omega_6 \omega_3 - 12v_2^2 \omega_6 - 12cs^2 \omega_6 \\
C_7 &= -2\omega_4^2 cs^2 \omega_2 - 2\omega_4 cs^2 \omega_5 \omega_2 + 2\omega_4 \omega_5 \omega_2 v_1^2 + \omega_4^2 \omega_5 \omega_2^2 v_1^2 - 2\omega_4^2 \omega_2 v_1^2 + \omega_4 cs^2 \omega_5 \omega_2^2 + \omega_4^2 cs^2 \omega_2^2 + 4\omega_4^2 \omega_5 v_1^2 + \omega_4^2 \omega_2^2 v_1^2 - 4\omega_4^2 \omega_5 \omega_2 v_1^2 + \\
& 4\omega_4^2 cs^2 \omega_5 \omega_2 - 2\omega_2^2 cs^2 \omega_5 + 2\omega_5 \omega_2^2 v_1^2 - 3\omega_4 \omega_5 \omega_2^2 v_1^2 - \omega_4^2 cs^2 \omega_5 \omega_2^2 \\
C_8 &= \omega_4 cs^2 \omega_6 \omega_3^2 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + 2\omega_4 v_2^2 \omega_6 \omega_3 - 2\omega_4 cs^2 \omega_6 \omega_3 - 2\omega_4^2 v_2^2 \omega_3 - 2\omega_4^2 cs^2 \omega_3 - 2\omega_4^2 cs^2 \omega_6 + 4\omega_4^2 v_2^2 \omega_6 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - \\
& \omega_4^2 cs^2 \omega_6 \omega_3^2 + 4\omega_4^2 cs^2 \omega_6 \omega_3 - 4\omega_4^2 v_2^2 \omega_6 \omega_3 + \omega_4^2 v_2^2 \omega_3^2 + \omega_4^2 cs^2 \omega_3^2 \\
C_9 &= 4\omega_7 v_3^2 \omega_2^2 - \omega_7 \omega_4^2 cs^2 \omega_2^2 + \omega_7 \omega_4^2 v_3^2 \omega_2^2 - 2\omega_7 cs^2 \omega_2^2 - 3\omega_7 \omega_4^2 v_3^2 \omega_2 + \omega_4^2 cs^2 \omega_2^2 + \omega_4^2 v_3^2 \omega_2^2 + \omega_7 \omega_4^2 cs^2 \omega_2 + 2\omega_7 \omega_4 v_3^2 \omega_2 - 2\omega_4 cs^2 \omega_2^2 - \\
& 2\omega_4 v_3^2 \omega_2^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 cs^2 \omega_2 + 4\omega_7 \omega_4 cs^2 \omega_2^2 - 4\omega_7 \omega_4 v_3^2 \omega_2^2 \\
C_{10} &= -2\omega_4 v_3^2 \omega_3^2 - 2\omega_7 \omega_4 cs^2 \omega_3 + 2\omega_7 \omega_4 v_3^2 \omega_3 - 2\omega_4 cs^2 \omega_3^2 - 4\omega_7 \omega_4 v_3^2 \omega_3^2 + 4\omega_7 \omega_4 cs^2 \omega_3^2 + \omega_7 \omega_4^2 v_3^2 \omega_3^2 - 2\omega_7 cs^2 \omega_3^2 + 4\omega_7 v_3^2 \omega_3^2 - \\
& \omega_7 \omega_4^2 cs^2 \omega_3^2 + 2\omega_7 \omega_4^2 v_3^2 + \omega_4^2 v_3^2 \omega_3^2 + \omega_7 \omega_4^2 cs^2 \omega_3 - 3\omega_7 \omega_4^2 v_3^2 \omega_3 + \omega_4^2 cs^2 \omega_3^2 \\
C_{11} &= \omega_7 \omega_4^2 + 3\omega_4^2 cs^2 + 6\omega_4 - 3\omega_7 \omega_4^2 cs^2 - 3\omega_4^2 - 12\omega_7 cs^2 + 3\omega_7 \omega_4 v_3^2 - 3\omega_7 \omega_4 - 6\omega_4 v_3^2 + 3\omega_4^2 v_3^2 - \omega_7 \omega_4^2 v_3^2 + 15\omega_7 \omega_4 cs^2 - 6\omega_4 cs^2 \\
C_{12} &= 2\omega_7 \omega_4^2 + 6\omega_4^2 cs^2 + 12\omega_4 - 3\omega_7 \omega_4^2 cs^2 - 6\omega_4^2 - 12\omega_7 cs^2 + 18\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 - 12\omega_4 v_3^2 + 6\omega_4^2 v_3^2 - 12\omega_7 v_3^2 - 5\omega_7 \omega_4^2 v_3^2 + 18\omega_7 \omega_4 cs^2 - 12\omega_4 cs^2 \\
C_{13} &= \omega_5^2 \omega_3^3 + 12cs^2 \omega_2^2 + 27\omega_5^2 \omega_2^2 v_1^2 - 11\omega_5^2 \omega_2^2 + 48\omega_5 \omega_2 v_1^2 + 12\omega_5^2 v_1^2 - 6cs^2 \omega_2^3 + 24cs^2 \omega_5 \omega_2 - 3\omega_5^2 \omega_2^3 v_1^2 - 36cs^2 \omega_5 \omega_2^2 + 6\omega_2^3 + 12\omega_5^2 \omega_2 + 9cs^2 \omega_5 \omega_2^3 - \\
& 12\omega_2^2 - 2cs^2 \omega_5^2 \omega_2^2 + 15\omega_5 \omega_2^3 v_1^2 + 25cs^2 \omega_5^2 \omega_2^2 - 6\omega_2^3 v_1^2 - 24\omega_5 \omega_2 + 36\omega_5 \omega_2^2 - 60\omega_5 \omega_2^2 v_1^2 - 48cs^2 \omega_5^2 \omega_2 - 9\omega_5 \omega_2^3 + 12\omega_2^2 v_1^2 - 42\omega_5^2 \omega_2 v_1^2 + 24cs^2 \omega_5^2 \\
C_{14} &= 72\omega_5 \omega_2^2 v_1^4 - 24cs^4 \omega_5 \omega_2^2 - 72cs^2 \omega_5^2 \omega_2^2 v_1^2 + 24\omega_5^2 \omega_2^2 v_1^2 + 6cs^4 \omega_5 \omega_2^2 + 24\omega_5^2 \omega_2 v_1^4 + 12cs^2 \omega_2^3 v_1^2 + 48\omega_5 \omega_2 v_1^2 - 24cs^2 \omega_5 \omega_2 v_1^2 - 24\omega_2^3 v_1^4 - \\
& 24cs^2 \omega_5 \omega_2 - 3\omega_5^2 \omega_2^3 v_1^2 + 6cs^2 \omega_5^2 \omega_2^2 v_1^2 + 24cs^2 \omega_5 \omega_2^2 - 18\omega_5 \omega_2^3 v_1^4 + 24cs^4 \omega_5^2 - 6cs^2 \omega_5 \omega_2^3 + 12\omega_2^3 v_1^4 - 24cs^2 \omega_2^3 v_1^2 + 24cs^4 \omega_5 \omega_2 - \\
& 12cs^2 \omega_5 \omega_2^2 v_1^2 + cs^2 \omega_5^2 \omega_2^2 + 18\omega_5 \omega_2^3 v_1^2 + 3\omega_5^2 \omega_2^3 v_1^4 - 48cs^4 \omega_5^2 \omega_2 - 8cs^2 \omega_5^2 \omega_2^2 - 12\omega_2^3 v_1^2 - 96cs^2 \omega_5^2 v_1^2 - 3cs^4 \omega_5^2 \omega_2^2 - 24\omega_5^2 \omega_2^2 v_1^4 - 72\omega_5 \omega_2^2 v_1^2 + \\
& 12cs^2 \omega_5^2 \omega_2 + 48cs^2 \omega_5 \omega_2^2 v_1^2 - 48\omega_5 \omega_2 v_1^4 + 24\omega_2^2 v_1^2 + 24cs^4 \omega_5^2 \omega_2^2 + 156cs^2 \omega_5^2 \omega_2 v_1^2 - 24\omega_5^2 \omega_2 v_1^2 \\
C_{15} &= -\omega_5^2 \omega_2^3 - 12cs^2 \omega_2^2 - 16\omega_5^2 \omega_2^2 v_1^2 + 8\omega_5^2 \omega_2^2 - 12\omega_5 \omega_2 v_1^2 - 12\omega_5^2 v_1^2 + 6cs^2 \omega_2^3 - 12cs^2 \omega_5 \omega_2 + 2\omega_5^2 \omega_2^3 v_1^2 + 24cs^2 \omega_5 \omega_2^2 - 6\omega_2^3 - 6\omega_5^2 \omega_2 - 6cs^2 \omega_5 \omega_2^3 + \\
& 12\omega_2^2 + cs^2 \omega_5^2 \omega_2^2 - 6\omega_5 \omega_2^3 v_1^2 - 20cs^2 \omega_5^2 \omega_2^2 + 6\omega_2^3 v_1^2 + 12\omega_5 \omega_2 - 24\omega_5 \omega_2^2 + 24\omega_5 \omega_2^2 v_1^2 + 42cs^2 \omega_5^2 \omega_2 + 6\omega_5 \omega_2^3 - 12\omega_2^2 v_1^2 + 24\omega_5^2 \omega_2 v_1^2 - 24cs^2 \omega_5^2 \\
C_{16} &= -6\omega_2^3 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3 + \omega_5 \omega_2^3 \omega_3^2 + 3\omega_2^3 \omega_3^2 - 7\omega_5 \omega_2^3 \omega_3^2 - 12\omega_5 \omega_3^3 + 12\omega_5 \omega_2^3 \omega_3 - 10\omega_5 \omega_2^2 \omega_3^3 + 12\omega_2^2 \omega_3^3 + 12\omega_5 \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3^3 - \\
& 12\omega_5 \omega_2 \omega_3^3 + 24\omega_5 \omega_2 \omega_3^2 - 6\omega_5 \omega_2^2 \\
C_{17} &= \omega_5^2 \omega_2^3 v_1^2 \omega_3 - 30cs^2 \omega_5 \omega_2^2 \omega_3 + 6\omega_5^2 \omega_2^2 v_1^2 - 30\omega_5 \omega_2^2 v_1^2 \omega_3 - 30cs^2 \omega_5^2 \omega_2 \omega_3 - \omega_5^2 \omega_2^3 v_1^2 + 9cs^2 \omega_5 \omega_2^3 \omega_3 + 12cs^2 \omega_5 \omega_2^2 + 12\omega_2^2 v_1^2 \omega_3 - \\
& 6cs^2 \omega_5 \omega_2^3 + 36\omega_5^2 \omega_2 v_1^2 \omega_3 + 12cs^2 \omega_2^2 \omega_3 + 3cs^2 \omega_2^2 \omega_3^2 - 6\omega_5 \omega_2^3 v_1^2 - 2cs^2 \omega_2^2 \omega_2^3 \omega_3 + 9\omega_5 \omega_2^3 v_1^2 \omega_3 - 18cs^2 \omega_5^2 \omega_2^2 + 12cs^2 \omega_2^2 \omega_3 - 10\omega_5^2 \omega_2^2 v_1^2 \omega_3 + \\
& 22cs^2 \omega_5^2 \omega_2^2 \omega_3 + 12\omega_5 \omega_2^2 v_1^2 + 12cs^2 \omega_5^2 \omega_2 + 12\omega_5 \omega_2 v_1^2 \omega_3 - 6\omega_2^2 v_1^2 \omega_3 - 6cs^2 \omega_2^2 \omega_3 - 24\omega_5^2 v_1^2 \omega_3 + 12cs^2 \omega_5 \omega_2 \omega_3 - 12\omega_5^2 \omega_2 v_1^2 \\
C_{18} &= -12\omega_2^2 v_1^2 \omega_3^3 + 12\omega_5 \omega_2 v_1^2 \omega_3^2 - 12\omega_5^2 \omega_2^3 v_1^2 \omega_3 + 6\omega_5 \omega_2^3 \omega_3^2 - 12cs^2 \omega_5 \omega_2^3 \omega_3^2 - 36cs^2 \omega_5^2 \omega_3^2 - 3\omega_2^3 \omega_3^2 - 30\omega_5^2 \omega_2 v_1^2 \omega_3^2 + 6cs^2 \omega_5 \omega_2^3 \omega_3^2 - \\
& 3\omega_5 \omega_2^3 \omega_3^2 + 42cs^2 \omega_5 \omega_2^2 \omega_3^2 - 24cs^2 \omega_2^2 \omega_2^3 \omega_3 + 6\omega_5^2 \omega_2^3 v_1^2 - 21\omega_5 \omega_2^2 \omega_3^2 - 12\omega_5 \omega_2^2 v_1^2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - 6\omega_5^2 \omega_2 \omega_3^2 + 78cs^2 \omega_5^2 \omega_2 \omega_3^2 - 12cs^2 \omega_5 \omega_2^2 \omega_3^2 + \\
& 6\omega_2^2 \omega_3^2 + 6\omega_5^2 \omega_2^2 v_1^2 \omega_3^2 + 42\omega_5 \omega_2^2 v_1^2 \omega_3^2 + 7\omega_5^2 \omega_2^2 \omega_3^2 + 6cs^2 \omega_5^2 \omega_2^2 \omega_3 - 48cs^2 \omega_5^2 \omega_2^2 \omega_3^2 + 42cs^2 \omega_5^2 \omega_2^2 \omega_3^2 - 24cs^2 \omega_5 \omega_2 \omega_3^2 + 12\omega_5 \omega_2 \omega_3^2 + 24\omega_5^2 v_1^2 \omega_3^2 +
\end{aligned}$$



$$C_{32} = 3\omega_4\omega_2^3 + \omega_3^3\omega_5\omega_2^3 - 6\omega_4^3\omega_2^2 - 10\omega_4^3\omega_5\omega_2^2 + 24\omega_4^3\omega_5\omega_2 - 6\omega_4\omega_5\omega_2^2 - 6\omega_4^2\omega_2^3 + 12\omega_4\omega_5\omega_2^3 + 12\omega_4^2\omega_2^2 + 12\omega_4^2\omega_5\omega_2^2 - 7\omega_4^2\omega_5\omega_2^3 - 12\omega_4^3\omega_5 - 6\omega_5\omega_2^3 - 12\omega_4^2\omega_5\omega_2$$

$$C_{33} = -10\omega_4\omega_5^2\omega_2^3v_1^2 + 6\omega_5^2\omega_2^2v_1^2 - 6\omega_4\omega_2^3v_1^2 + 12\omega_4cs^2\omega_5\omega_2 + 12\omega_4\omega_5\omega_2v_1^2 - 30\omega_4cs^2\omega_5\omega_2^2 - \omega_5^2\omega_2^3v_1^2 + 12cs^2\omega_5\omega_2^2 + \omega_4\omega_5^2\omega_2^3v_1^2 - 6cs^2\omega_5\omega_2^2 + 9\omega_4cs^2\omega_5\omega_2^2 + 12\omega_4\omega_2^3v_1^2 + 12\omega_4cs^2\omega_5^2 + 9\omega_4\omega_5\omega_2^3v_1^2 + 3cs^2\omega_5^2\omega_2^3 - 6\omega_5\omega_2^3v_1^2 - 2\omega_4cs^2\omega_5^2\omega_2^3 + 12\omega_4cs^2\omega_2^2 + 22\omega_4cs^2\omega_5^2\omega_2^2 - 18cs^2\omega_5^2\omega_2^2 - 24\omega_4\omega_5^2v_1^2 - 6\omega_4cs^2\omega_2^3 - 30\omega_4cs^2\omega_5^2\omega_2 + 12\omega_5\omega_2^2v_1^2 + 12cs^2\omega_5^2\omega_2 - 30\omega_4\omega_5\omega_2^2v_1^2 + 36\omega_4\omega_5^2\omega_2v_1^2 - 12\omega_5^2\omega_2v_1^2$$

$$C_{34} = -36\omega_3^3cs^2\omega_5^2 - 3\omega_4^3\omega_2^3 - 30\omega_4^3\omega_5^2\omega_2v_1^2 - 12\omega_4^3\omega_2^2v_1^2 + 6\omega_4\omega_5^2\omega_2^3v_1^2 - 12\omega_4^2cs^2\omega_5^2\omega_2^3 + 6\omega_4^3\omega_5\omega_2^3 + 6\omega_4^2\omega_5\omega_2^3v_1^2 + 78\omega_4^3cs^2\omega_5^2\omega_2 + 6\omega_4^3\omega_2^2 + 42\omega_4^3\omega_5\omega_2^2v_1^2 - 21\omega_4^3\omega_5\omega_2^2 + 42\omega_4^2cs^2\omega_5^2\omega_2^2 - 12\omega_4^2\omega_5\omega_2^2v_1^2 + 6\omega_5^2\omega_2^3v_1^2 + 12\omega_4^3\omega_5\omega_2 + \omega_4^2\omega_5^2\omega_2^3 - 24\omega_4^2cs^2\omega_5^2\omega_2 + 6\omega_4^3\omega_2^3v_1^2 - 12\omega_4\omega_5^2\omega_2^3v_1^2 - 48\omega_3^3cs^2\omega_5^2\omega_2^2 - 3\omega_4^2\omega_5^2\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2v_1^2 - 12\omega_4^3\omega_5\omega_2^3v_1^2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2 + 6\omega_4^2\omega_5\omega_2^2 - 12\omega_4^2\omega_5^2\omega_2^3v_1^2 + 6\omega_4cs^2\omega_5^2\omega_2^3 - 12\omega_3^3cs^2\omega_5\omega_2^3 - 6\omega_4^3\omega_2^2\omega_2 - 12\omega_4cs^2\omega_5^2\omega_2^2 - 3\omega_4^2\omega_5\omega_2^3 + 42\omega_4^2cs^2\omega_5\omega_2^2 - 24\omega_4^3cs^2\omega_5\omega_2 + 6\omega_4^3cs^2\omega_2^3 + 24\omega_4^3\omega_5^2v_1^2 - 24\omega_4^3\omega_5\omega_2v_1^2 + 7\omega_4^3\omega_5^2\omega_2^2 + 6\omega_4^2\omega_5^2\omega_2^3v_1^2 - 12\omega_4^2cs^2\omega_5\omega_2^2 + 6\omega_4^2\omega_5^2\omega_2v_1^2 - 12\omega_4^2cs^2\omega_2^2 + 6\omega_4^2cs^2\omega_5\omega_2^2 - \omega_4^3\omega_5^2\omega_2^3$$

$$C_{35} = -12\omega_3^3cs^2\omega_5^2 - 30\omega_3^3\omega_5^2\omega_2v_1^2 - 12\omega_4^3\omega_2^2v_1^2 - 12\omega_4^2cs^2\omega_5^2\omega_2^3 + 3\omega_3^3\omega_5\omega_2^3 + 12\omega_4^2\omega_5\omega_2^3v_1^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 + 36\omega_3^3\omega_5\omega_2^3v_1^2 - 6\omega_4^3\omega_5\omega_2^2 + 48\omega_2^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^2\omega_5\omega_2^2v_1^2 + 12\omega_5^2\omega_2^3v_1^2 + 2\omega_4^2\omega_5^2\omega_2^3 - 24\omega_4^2cs^2\omega_5^2\omega_2 + 6\omega_4^3\omega_2^3v_1^2 - 18\omega_4\omega_5^2\omega_2^3v_1^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 6\omega_4^2\omega_5^2\omega_2^2 - 12\omega_3^3\omega_5\omega_2^3v_1^2 + 4\omega_4^3cs^2\omega_5^2\omega_2^2 + 12\omega_4^2\omega_5\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2^3v_1^2 + 6\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_3^3cs^2\omega_5\omega_2^3 - 12\omega_4cs^2\omega_5^2\omega_2^2 - 6\omega_4^2\omega_5\omega_2^3 + 36\omega_4^3cs^2\omega_5\omega_2^2 + 3\omega_4^3\omega_5^2\omega_2^3v_1^2 - 12\omega_4^3cs^2\omega_5\omega_2 + 6\omega_3^3cs^2\omega_2^2 + 24\omega_4^3\omega_5^2v_1^2 - 12\omega_4^3\omega_5\omega_2v_1^2 + 3\omega_4^3\omega_2^3\omega_2^2 - 24\omega_4^2cs^2\omega_5\omega_2^2 - 12\omega_4^3cs^2\omega_2^2 + 12\omega_4^2cs^2\omega_5\omega_2^2 - \omega_4^3\omega_5^2\omega_2^3$$

$$C_{36} = -\omega_5^2\omega_2^3 - 12cs^2\omega_2^2 - 8\omega_5^2\omega_2^3v_1^2 + 11\omega_5^2\omega_2^2 - 36\omega_5\omega_2v_1^2 + 12\omega_5^2v_1^2 + 6cs^2\omega_2^2 - 36cs^2\omega_5\omega_2 + \omega_5^2\omega_2^3v_1^2 + 48cs^2\omega_5\omega_2^2 - 6\omega_2^3 - 12\omega_5^2\omega_2 - 12cs^2\omega_5\omega_2^2 + 12\omega_2^2 + 4cs^2\omega_5^2\omega_2^2 - 12\omega_5\omega_2^3v_1^2 - 44cs^2\omega_5^2\omega_2^2 + 6\omega_2^3v_1^2 + 24\omega_5\omega_2 - 36\omega_5\omega_2^2 + 48\omega_5\omega_2^3v_1^2 + 90cs^2\omega_5^2\omega_2 + 9\omega_5\omega_2^3 - 12\omega_2^2v_1^2 - 48cs^2\omega_5^2$$

$$C_{37} = 18\omega_4\omega_2\omega_3^3 - 6\omega_4\omega_3^3 + 18\omega_4^3\omega_2\omega_3 - 12\omega_4\omega_2\omega_3^2 - 16\omega_4^3\omega_2\omega_3 - 6\omega_4^3\omega_2 + 3\omega_4^3\omega_2\omega_3^3 - 12\omega_4^2\omega_2\omega_3 + 12\omega_4^3\omega_3^2 - 6\omega_2\omega_3^3 - 4\omega_4^3\omega_3^3 - 12\omega_4^2\omega_3^2 - 16\omega_4^2\omega_2\omega_3^3 + 30\omega_4^2\omega_2\omega_3^2 + 12\omega_4^2\omega_3^3 - 6\omega_4^3\omega_3$$

$$C_{38} = -4\omega_4^3\omega_2^3 + 12\omega_4^3\omega_2^2 + 18\omega_4^3\omega_2\omega_3 - 16\omega_4^2\omega_2^3\omega_3 - 6\omega_4^3\omega_2 + 12\omega_4^2\omega_2^3 + 30\omega_4^2\omega_2\omega_3 - 12\omega_4^2\omega_2^2 - 6\omega_2^3\omega_3 - 12\omega_4^2\omega_2\omega_3 + 3\omega_4^3\omega_2^3\omega_3 - 12\omega_4\omega_2^3\omega_3 - 6\omega_4\omega_2^2 - 16\omega_4^2\omega_2^3\omega_3 + 18\omega_4^3\omega_2^3\omega_3 - 6\omega_4^3\omega_3$$

$$C_{39} = 12\omega_3^3\omega_2^3 + 18\omega_4\omega_2\omega_3^3 - 6\omega_4\omega_3^3 - 4\omega_2^3\omega_3^3 - 12\omega_4\omega_2\omega_3^2 - 12\omega_2^2\omega_3^2 + 12\omega_2^2\omega_3^3 - 6\omega_2^3\omega_3 - 16\omega_4\omega_2^3\omega_3^2 - 6\omega_2\omega_3^3 - 12\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_2^3\omega_3^3 - 6\omega_4\omega_2^2 + 30\omega_4\omega_2^2\omega_3^2 + 18\omega_4\omega_2\omega_3^2 - 16\omega_4\omega_2^2\omega_3^3$$

$$C_{40} = -2\omega_4^3cs^2\omega_5^2\omega_2^3\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_3^3 + 7\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_3^3 + \omega_4^3\omega_5\omega_2^3v_1^2\omega_3^2 + 12\omega_3^3\omega_5^2\omega_2^2v_1^2\omega_3^3 + 3\omega_4^2\omega_5^2\omega_2^3v_1^2\omega_3 - 2\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3 + \omega_4^3cs^2\omega_2^2\omega_3^3 - 2\omega_4^3\omega_5\omega_2^3v_1^2\omega_3^2 - 2\omega_4^3\omega_5^2\omega_2^2v_1^2\omega_3^2 + 4\omega_4^3\omega_5^2\omega_2^2v_1^2\omega_3 - 2\omega_4^2cs^2\omega_5^2\omega_2\omega_3^3 + \omega_4^3\omega_2^3v_1^2\omega_3^3 - 2\omega_4^3\omega_5\omega_2v_1^2\omega_3 + \omega_4^3cs^2\omega_2^2\omega_3^3 + 3\omega_5^2\omega_2^3v_1^2\omega_3^3 + 10\omega_3^3\omega_5^2v_1^2\omega_3^3 - 2\omega_4^2\omega_5\omega_2^2v_1^2\omega_3^3 + 6\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 - 8\omega_4^3\omega_5^2\omega_2^3v_1^2\omega_3^2 - 2\omega_4^3cs^2\omega_5\omega_2\omega_3^3 - 2\omega_4^3\omega_5\omega_2^2v_1^2\omega_3^3 + \omega_4^3cs^2\omega_5^2\omega_2^2\omega_3 + 7\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_3^3 - 6\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 + 7\omega_4^3\omega_5^2\omega_2^2v_1^2\omega_3^2 - 2\omega_4^2cs^2\omega_5^2\omega_2^2\omega_3 + 6\omega_4^3\omega_5\omega_2^2v_1^2\omega_3^3 + 6\omega_4^3cs^2\omega_5^2\omega_2\omega_3^2 - 2\omega_4^3cs^2\omega_5\omega_2^2\omega_3^2 - 2\omega_4cs^2\omega_5^2\omega_2^2\omega_3^3 + 6\omega_4^2cs^2\omega_5^2\omega_2^2\omega_3^2 - 2\omega_4^2\omega_5\omega_2^2v_1^2\omega_3^3 + \omega_4cs^2\omega_5^2\omega_2^2\omega_3^3 + \omega_3^3cs^2\omega_5\omega_2^2\omega_3^2 - 21\omega_3^3\omega_5^2\omega_2v_1^2\omega_3^3 + \omega_4^2cs^2\omega_5^2\omega_2^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_3^3 - 2\omega_4^3cs^2\omega_5\omega_2^2\omega_3^3 + 4\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_3^3 + \omega_4\omega_5\omega_2^2v_1^2\omega_3^3 + 4\omega_4\omega_5^2\omega_2^2v_1^2\omega_3^3 - 8\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_3 - 2\omega_4^2cs^2\omega_5^2\omega_2^2\omega_3^2 + 7\omega_4^3\omega_5^2\omega_2v_1^2\omega_3^2 - 2\omega_4^2\omega_2^2v_1^2\omega_3^3$$

$$C_{41} = 12\omega_3^3\omega_2^3 + 12\omega_2^2\omega_2^2\omega_3^2 + 12\omega_2^3\omega_3^3 - 30\omega_4^2\omega_2^3\omega_3^2 + 18\omega_2^2\omega_2^2\omega_3 + 18\omega_4^3\omega_2\omega_3^2 - 42\omega_4^2\omega_2^3\omega_3^2 + 24\omega_4^2\omega_2^2\omega_3^3 - 36\omega_4^3\omega_2\omega_3^2 + 18\omega_4\omega_2^3\omega_3^2 - 30\omega_3^3\omega_2^3\omega_3 + 28\omega_4^2\omega_2^3\omega_3^2 - 30\omega_3^3\omega_2^2\omega_3^2 + 12\omega_4^3\omega_3^3 - 30\omega_4\omega_2^3\omega_3^3 + 6\omega_4^3\omega_2^3\omega_3 - 5\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4^2\omega_2\omega_3^2 + 6\omega_4\omega_2^2\omega_3^2 + 24\omega_4^3\omega_2^3\omega_3^2$$

$$C_{42} = -12\omega_3^3cs^2\omega_5^2 - 90\omega_3^3\omega_5^2\omega_2v_1^2 - 12\omega_4^3\omega_2^2v_1^2 + 24\omega_4\omega_5^2\omega_2^2v_1^2 - 12\omega_4^2cs^2\omega_5^2\omega_2^3 + 12\omega_4^2\omega_5\omega_2^3v_1^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 + 36\omega_4^3\omega_5\omega_2^3v_1^2 + 48\omega_2^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^2\omega_5\omega_2^2v_1^2 + 12\omega_5^2\omega_2^3v_1^2 - 24\omega_4^2cs^2\omega_5^2\omega_2 + 6\omega_4^3\omega_2^3v_1^2 - 30\omega_4\omega_5^2\omega_2^3v_1^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 + 48\omega_4^2\omega_5^2\omega_2^2v_1^2 - 12\omega_4^3\omega_5\omega_2^3v_1^2 + 4\omega_4^3cs^2\omega_5^2\omega_2^2 - 60\omega_4^2\omega_5^2\omega_2^2v_1^2 + 6\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_4cs^2\omega_5^2\omega_2^2 + 36\omega_4^3cs^2\omega_5\omega_2^2 - 5\omega_4^3\omega_5^2\omega_2^2v_1^2 - 12\omega_4^3cs^2\omega_5\omega_2 + 6\omega_4^3cs^2\omega_2^2 + 48\omega_4^3\omega_5^2v_1^2 - 12\omega_4^3\omega_5\omega_2v_1^2 + 24\omega_4^2\omega_5^2\omega_2^2v_1^2 - 24\omega_4^2cs^2\omega_5\omega_2^2 + 40\omega_4^2\omega_5^2\omega_2^2v_1^2 - 12\omega_4^3cs^2\omega_2^2 + 12\omega_4^2cs^2\omega_5\omega_2^2$$

$$C_{43} = -12\omega_2^3v_1^2\omega_3^3 + 48\omega_5^2\omega_2v_1^2\omega_3^2 - 30\omega_5^2\omega_2^3v_1^2\omega_3 - 12cs^2\omega_5\omega_2^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^3 - 90\omega_5^2\omega_2v_1^2\omega_3^2 + 12cs^2\omega_5\omega_2^3\omega_3^2 + 36cs^2\omega_5\omega_2^2\omega_3^3 - 24cs^2\omega_2^2\omega_2^2\omega_3^2 + 12\omega_5^2\omega_2^3v_1^2\omega_3^2 - 5\omega_5^2\omega_2^3v_1^2\omega_3^2 - 24\omega_5\omega_2^2v_1^2\omega_3^2 + 36cs^2\omega_5^2\omega_2^2\omega_3^2 + 36\omega_5^2\omega_2^2v_1^2\omega_3^2 + 6cs^2\omega_5^2\omega_2^2\omega_3^2 - 32cs^2\omega_5^2\omega_2^2\omega_3^2 + 48cs^2\omega_5^2\omega_2^2\omega_3^2 - 12cs^2\omega_5\omega_2\omega_3^2 + 48\omega_5^2v_1^2\omega_3^2 + 6cs^2\omega_2^3\omega_3^2 - 12\omega_5\omega_2v_1^2\omega_3^2 + 6\omega_2^3v_1^2\omega_3^2 + 24\omega_5^2\omega_2^2v_1^2\omega_3 - 12\omega_5\omega_2^3v_1^2\omega_3^2 - 60\omega_2^2\omega_2^2v_1^2\omega_3^2 - 12cs^2\omega_5^2\omega_2^2\omega_3 + 4cs^2\omega_5^2\omega_2^2\omega_3^2 + 12\omega_5\omega_2^2v_1^2\omega_3^2 + 40\omega_2^2\omega_2^2v_1^2\omega_3^2 - 12cs^2\omega_2^2\omega_3^2 - 12cs^2\omega_5^2\omega_2^2\omega_3^2$$

$$C_{44} = 12\omega_4\omega_6\omega_3^3 + 24\omega_4^3\omega_6\omega_3 - 6\omega_4\omega_6\omega_2^3 - 10\omega_4^3\omega_6\omega_2^3 + \omega_4^3\omega_6\omega_3^3 - 6\omega_6\omega_3^3 - 6\omega_4^2\omega_3^2 - 12\omega_4^2\omega_6\omega_3 + 3\omega_4^3\omega_3^3 - 7\omega_4^2\omega_6\omega_3^2 - 12\omega_4^3\omega_6 + 12\omega_4^2\omega_3^2 + 12\omega_4^2\omega_6\omega_3^2 - 6\omega_4^3\omega_3$$

$$C_{45} = -6v_2^3\omega_6\omega_3^3 - 6cs^2\omega_6\omega_3^2 + 9\omega_4v_2^2\omega_6\omega_3^2 + 9\omega_4cs^2\omega_6\omega_3^2 - 6\omega_4v_2^2\omega_3^2 - 6\omega_4cs^2\omega_3^2 - 24\omega_4v_2^2\omega_6^2 + 12\omega_4cs^2\omega_6^2 - 30\omega_4cs^2\omega_6\omega_3^2 - 30\omega_4v_2^2\omega_6\omega_3^2 + 12cs^2\omega_6\omega_3^2 + 12v_2^2\omega_6\omega_3^2 + 12\omega_4cs^2\omega_6\omega_3^2 + 12\omega_4v_2^2\omega_6^2 + 12\omega_4v_2^2\omega_6\omega_3 + 12\omega_4cs^2\omega_6\omega_3 + 36\omega_4v_2^2\omega_6^2\omega_3 - 30\omega_4cs^2\omega_6^2\omega_3 - 12v_2^2\omega_6\omega_3 + 12cs^2\omega_6^2\omega_3 + 22\omega_4cs^2\omega_6^2\omega_3 - 10\omega_4v_2^2\omega_6^2\omega_3 - 18cs^2\omega_6^2\omega_3 + 6v_2^2\omega_6^2\omega_3 - v_2^2\omega_6^2\omega_3 + 3cs^2\omega_6^2\omega_3 + \omega_4v_2^2\omega_6^2\omega_3 - 2\omega_4cs^2\omega_6^2\omega_3$$

$$C_{46} = -8\omega_4^3v_2^2\omega_2\omega_6^2\omega_3^3 + \omega_4^3cs^2\omega_2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 + \omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^3 - 8\omega_4^2v_2^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_4^3v_2^2\omega_6^2\omega_3^3 + 3\omega_4v_2^2\omega_2^2\omega_6^2\omega_3^2 - 21\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3 + 6\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3 + \omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 + \omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 + 4\omega_4^3v_2^2\omega_2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 4\omega_4^2v_2^2\omega_2^2\omega_6^2\omega_3^2 + \omega_4^2cs^2\omega_2^2\omega_6\omega_3^2 + \omega_4^2v_2^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6^2 - 10\omega_4^3v_2^2\omega_2^2\omega_6^2 + \omega_4^3cs^2\omega_2^2\omega_3^2 + \omega_4^3v_2^2\omega_2^2\omega_3^2 - 6\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 12\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^2cs^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^2v_2^2\omega_2^2\omega_6\omega_3^2 + \omega_4^2cs^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^2v_2^2\omega_2^2\omega_6\omega_3^2 + \omega_4^2cs^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^2\omega_2^2\omega_6^2\omega_3^2 + 3v_2^2\omega_2^2\omega_6^2\omega_3^2 - 12\omega_4^2v_2^2\omega_2^2\omega_6^2\omega_3^2 + 6\omega_4^2cs^2\omega_2^2\omega_6^2\omega_3^2 + \omega_4cs^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 - 8\omega_4v_2^2\omega_2^2\omega_6^2\omega_3^2 + 7\omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 + 7\omega_4^2v_2^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^2cs^2\omega_2^2\omega_6\omega_3^2 + 2\omega_4^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^2cs^2\omega_2^2\omega_6\omega_3^2 + 4\omega_4v_2^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 + 7\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_4^2v_2^2\omega_2\omega_6^2\omega_3^2 - 12\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 + 6\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 - 2\omega_4^2cs^2\omega_2^2\omega_6^2\omega_3 + 7\omega_4^2v_2^2\omega_2^2\omega_6^2\omega_3^2$$





$$C_{73} = -12\omega_7\omega_4^3v_3^2\omega_3^3 + 12\omega_7^2\omega_4^2v_3^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^3 + 3\omega_7^2\omega_4^3\omega_3^3 + 12\omega_7\omega_4^3v_3^2\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2\omega_3^2 - 6\omega_7^2\omega_4^2\omega_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^3 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 + 24\omega_7^2v_3^2\omega_3^3 - 12\omega_7^2\omega_4^2cs^2\omega_3 - \omega_7^2\omega_4^3\omega_3^3 - 12\omega_7\omega_4^3cs^2\omega_3^3 + 6\omega_4^3v_3^2\omega_3^3 + 6\omega_7^3cs^2\omega_3^3 + 2\omega_7^2\omega_4^3\omega_3^2 - 12\omega_7\omega_4^3v_3^2\omega_3^3 - 12\omega_7^2cs^2\omega_3^3 - 12\omega_7^2\omega_4^3cs^2\omega_3^3 + 36\omega_7\omega_4^3cs^2\omega_3^3 + 3\omega_7^2\omega_4^3v_3^2\omega_3^3 - 24\omega_7\omega_4^3v_3^2\omega_3^2 - 6\omega_7\omega_4^3\omega_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^3 - 24\omega_7\omega_4^3cs^2\omega_3^2 + 36\omega_7\omega_4^3v_3^2\omega_3^3 - 18\omega_7^2\omega_4^3v_3^2\omega_3 - 6\omega_7\omega_4^3\omega_3^3 - 12\omega_4^2cs^2\omega_3^3 + 36\omega_7\omega_4^2cs^2\omega_3^3 - 12\omega_4^2v_3^2\omega_3^3 - 30\omega_7^2\omega_4^3v_3^2\omega_3^3 + 6\omega_7^2\omega_4^3cs^2\omega_3 - 24\omega_7^2\omega_4^3cs^2\omega_3^2 + 12\omega_7\omega_4^3\omega_3^3$$

$$C_{74} = 24\omega_7^2cs^4 + 12\omega_7^3cs^2v_3^2 + 12\omega_7^2\omega_4cs^2 + 12\omega_7^3v_3^4 - 96\omega_7^2cs^2v_3^2 + 24\omega_7\omega_4cs^4 - 3\omega_7^2\omega_4^3v_3^2 + 24\omega_7\omega_4^2cs^2 - 24\omega_7\omega_4cs^2v_3^2 + 24\omega_7^2\omega_4^2cs^4 - 18\omega_7\omega_4^3v_3^4 + 24\omega_7^2\omega_4v_3^4 - 24\omega_4^2v_3^4 - 12\omega_7\omega_4^3cs^2v_3^2 + 48\omega_7\omega_4v_3^3 + 72\omega_7\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3cs^4 - 6\omega_7\omega_4^3cs^2 - 72\omega_7^2\omega_4^2cs^2v_3^2 + 24\omega_7^2\omega_4^2v_3^2 - 48\omega_7\omega_4^3v_3^4 + 24\omega_4^2v_3^2 - 24\omega_7^2\omega_4v_3^2 + 6\omega_7\omega_4^3cs^4 - 24\omega_7^2\omega_4^2v_3^4 - 72\omega_7\omega_4^2v_3^2 - 24\omega_4^2cs^2v_3^2 + 156\omega_7^2\omega_4cs^2v_3^2 + \omega_7^2\omega_4^3cs^2 - 12\omega_4^3v_3^2 - 24\omega_7\omega_4cs^2 + 6\omega_7^2\omega_4^3cs^2v_3^2 - 48\omega_7^2\omega_4cs^4 - 8\omega_7^2\omega_4^2cs^2 + 48\omega_7\omega_4^2cs^2v_3^2 + 18\omega_7\omega_4^3v_3^2 + 3\omega_7^2\omega_4^3v_3^4 - 24\omega_7\omega_4^2cs^4$$

$$C_{75} = -24\omega_7\omega_4^2 - 12\omega_4^2cs^2 + 42\omega_7^2\omega_4cs^2 - 6\omega_4^3 + 2\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3 + 24\omega_7\omega_4^2cs^2 + 12\omega_4^2 - 12\omega_7^2v_3^2 - 12\omega_7\omega_4v_3^2 + 6\omega_4^3cs^2 - 6\omega_7\omega_4^3cs^2 + 12\omega_7\omega_4 - 16\omega_7^2\omega_4^3v_3^2 - 6\omega_7^2\omega_4 - 12\omega_4^2v_3^2 + 24\omega_7^2\omega_4v_3^2 + 24\omega_7\omega_4^2v_3^2 + \omega_7^2\omega_4^3cs^2 + 6\omega_4^3v_3^2 - 12\omega_7\omega_4cs^2 - \omega_7^2\omega_4^3 - 24\omega_7^2cs^2 - 20\omega_7^2\omega_4^2cs^2 + 8\omega_7^2\omega_4^2 - 6\omega_7\omega_4^3v_3^2$$

## 2.4 CLBM1

### 2.4.1 Definitions

Collision operator  $C$ :

$$C(f) = \mathbf{K}^{-1}\mathbf{S}\left(\boldsymbol{\kappa}^{(eq)} - \mathbf{K}f\right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2)$ .

Matrix  $\mathbf{K}$  corresponds to the transformation matrix to the central moment basis defined as

$$\boldsymbol{\kappa} = (k_{(0,0,0)}, k_{(1,0,0)}, k_{(0,1,0)}, k_{(0,0,1)}, k_{(2,0,0)}, k_{(0,2,0)}, k_{(0,0,2)})^T,$$

and is given by

$$\mathbf{K} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ -v_1 & 1-v_1 & -v_1 & -v_1 & -v_1-1 & -v_1 & -v_1 \\ -v_2 & -v_2 & 1-v_2 & -v_2 & -v_2 & -v_2-1 & -v_2 \\ -v_3 & -v_3 & -v_3 & 1-v_3 & -v_3 & -v_3 & -v_3-1 \\ v_1^2 & (1-v_1)^2 & v_1^2 & v_1^2 & (v_1+1)^2 & v_1^2 & v_1^2 \\ v_2^2 & v_2^2 & (1-v_2)^2 & v_2^2 & v_2^2 & (v_2+1)^2 & v_2^2 \\ v_3^2 & v_3^2 & v_3^2 & (1-v_3)^2 & v_3^2 & v_3^2 & (v_3+1)^2 \end{pmatrix}.$$

The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K}\mathbf{M}^{-1}\boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left(\rho, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2\right)^T.$$

### 2.4.2 Conservation of mass equation



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$$\frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\omega_2 \delta_t} \left(\frac{\partial v_1}{\partial x_1}\right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-\omega_2 \omega_3 + \omega_2 + \omega_3) \frac{v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} +$$

$$\begin{aligned}
& (-\omega_2\omega_3 + \omega_2 + \omega_3) \frac{\rho\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{v_1\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{\rho\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (-\omega_2\omega_3 + \omega_2 + \omega_3) \frac{v_2\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + \\
& (2 - \omega_2) \frac{v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_3) \frac{v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho\delta_l^2}{2\omega_3\delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{v_2\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{\rho\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + \\
& (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{v_3\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{v_3\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} \\
& + (-2 + \omega_4) \frac{v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\rho\delta_l^2}{2\omega_4\delta_t} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\rho\delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{cs^2\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + \\
& (-2 + \omega_2) \frac{\rho v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho\delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} + (-\omega_2\omega_3 + \omega_2 + \omega_3) \frac{v_2 v_1\delta_l^2}{\omega_2\omega_3\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{\rho v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (2 - \omega_2) \frac{\rho v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + \omega_3) \frac{\rho v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho\delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + \\
& (\omega_4 + \omega_2 - \omega_4\omega_2) \frac{v_1 v_3\delta_l^2}{\omega_4\omega_2\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{\rho v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (2 - \omega_2) \frac{\rho v_1\delta_l^2}{2\omega_2\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (\omega_4 + \omega_3 - \omega_4\omega_3) \frac{v_2 v_3\delta_l^2}{\omega_4\omega_3\delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} \\
& + (2 - \omega_4) \frac{\rho v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{\rho v_2\delta_l^2}{2\omega_3\delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_4) \frac{cs^2\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{\rho v_3\delta_l^2}{2\omega_4\delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (12 + \omega_2^2 - 12\omega_2) \frac{\rho\delta_l\delta_t}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_2^2 - 12\omega_2) \frac{\rho v_1\delta_l^2}{6\omega_2^2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + C_1 \frac{v_1\delta_l^3}{6\omega_5\omega_2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (12 + \omega_3^2 - 12\omega_3) \frac{\rho\delta_l\delta_t}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + (-2\omega_2\omega_3^2 + 3\omega_3^2 + 9\omega_2\omega_3 - 6\omega_2 - 6\omega_3) \frac{\rho v_2\delta_l^2}{6\omega_2\omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + \\
& (3\omega_2^2 + 9\omega_2\omega_3 - 6\omega_2 - 2\omega_2^2\omega_3 - 6\omega_3) \frac{\rho v_1\delta_l^2}{6\omega_2^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + C_3 \frac{v_2\delta_l^3}{2\omega_5\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& (-6\omega_2\omega_3^2 + 6\omega_3^2 + 6\omega_2^2 - 6\omega_2^2\omega_3 + \omega_2^2\omega_3^2) \frac{\rho v_2 v_1\delta_l^3}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (v_1^2\omega_5\omega_2^2 - 3cs^2\omega_5\omega_2^2 + 6v_1^2\omega_5\omega_2 + 18cs^2\omega_5\omega_2 - 6v_1^2\omega_2^2 + 6cs^2\omega_2^2 - 12cs^2\omega_5 - 12v_1^2\omega_5 + 12v_1^2\omega_2 - 12cs^2\omega_2) \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} \\
& + (12 + \omega_3^2 - 12\omega_3) \frac{\rho v_2\delta_l^2}{6\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1\delta_l^3}{2\omega_2^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + (-3cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6 - 12cs^2\omega_6 + 18cs^2\omega_6\omega_3 + \\
& v_2^2\omega_6\omega_3^2 - 12cs^2\omega_3 - 6v_2^2\omega_3^2 + 12v_2^2\omega_3 + 6cs^2\omega_3^2 + 6v_2^2\omega_6\omega_3) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-6\omega_2\omega_3^2 + 6\omega_3^2 + 6\omega_2^2 - 6\omega_2^2\omega_3 + \omega_2^2\omega_3^2) \frac{\rho v_2 v_1\delta_l^3}{6\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2\delta_l^3}{6\omega_6\omega_3\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\rho\delta_l\delta_t}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-6\omega_4 - 2\omega_4^2\omega_2 - 6\omega_2 + 3\omega_4^2 + 9\omega_4\omega_2) \frac{\rho v_3\delta_l^2}{6\omega_4^2\omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (-6\omega_4 + 3\omega_2^2 - 6\omega_2 + 9\omega_4\omega_2 - 2\omega_4\omega_2^2) \frac{\rho v_1\delta_l^2}{6\omega_4\omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3\delta_l^3}{2\omega_4^2\omega_5\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2 + 6\omega_2^2 + 6\omega_4^2 - 6\omega_4\omega_2^2) \frac{\rho v_1 v_3\delta_l^3}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\
& (v_1^2\omega_5\omega_2^2 - 3cs^2\omega_5\omega_2^2 + 6v_1^2\omega_5\omega_2 + 18cs^2\omega_5\omega_2 - 6v_1^2\omega_2^2 + 6cs^2\omega_2^2 - 12cs^2\omega_5 - 12v_1^2\omega_5 + 12v_1^2\omega_2 - 12cs^2\omega_2) \frac{\rho\delta_l^3}{12\omega_5\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} \\
& + (-6\omega_4 - 2\omega_4^2\omega_3 + 3\omega_4^2 - 6\omega_3 + 9\omega_4\omega_3) \frac{\rho v_3\delta_l^2}{6\omega_4^2\omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (-6\omega_4 + 3\omega_3^2 - 2\omega_4\omega_3^2 - 6\omega_3 + 9\omega_4\omega_3) \frac{\rho v_2\delta_l^2}{6\omega_4\omega_3^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_4^2\omega_2\omega_3 + \omega_4^2\omega_2^2 + \omega_4\omega_2^2\omega_3 + \omega_4^2\omega_3^2 - 2\omega_4\omega_2^2\omega_3^2 - 2\omega_4^2\omega_2\omega_3^2 + \omega_4^2\omega_2^2\omega_3^2 + \omega_4\omega_2\omega_3^2 + \omega_2^2\omega_3^2 - 2\omega_4^2\omega_2^2\omega_3) \frac{2v_2 v_1 v_3\delta_l^3}{\omega_4^2\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (-6\omega_4^2\omega_3 + 3\omega_3^2 + 2\omega_4^2\omega_3^2 + 3\omega_4^2 - 6\omega_4\omega_3^2 + 6\omega_4\omega_3) \frac{\rho v_2 v_3\delta_l^3}{3\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (2\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2 + 3\omega_2^2 + 3\omega_4^2 + 6\omega_4\omega_2 - 6\omega_4\omega_2^2) \frac{\rho v_1 v_3\delta_l^3}{3\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-6\omega_2\omega_3^2 + 3\omega_3^2 + 3\omega_2^2 + 6\omega_2\omega_3 - 6\omega_2^2\omega_3 + 2\omega_2^2\omega_3^2) \frac{\rho v_2 v_1\delta_l^3}{3\omega_2^2\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3\delta_l^3}{2\omega_4^2\omega_6\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (-6\omega_4^2\omega_3 + 6\omega_3^2 + \omega_4^2\omega_3^2 + 6\omega_4^2 - 6\omega_4\omega_3^2) \frac{\rho v_2 v_3\delta_l^3}{6\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + (-3cs^2\omega_6\omega_3^2 - 12v_2^2\omega_6 - 12cs^2\omega_6 + 18cs^2\omega_6\omega_3 + \\
& v_2^2\omega_6\omega_3^2 - 12cs^2\omega_3 - 6v_2^2\omega_3^2 + 12v_2^2\omega_3 + 6cs^2\omega_3^2 + 6v_2^2\omega_6\omega_3) \frac{\rho\delta_l^3}{12\omega_6\omega_3^2\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (12 - 12\omega_4 + \omega_4^2) \frac{\rho v_3\delta_l^2}{6\omega_4^2} \frac{\partial^3 v_3}{\partial t \partial x_3^2} + \\
& C_9 \frac{v_1\delta_l^3}{2\omega_7\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (\omega_7\omega_4^2v_3^2 + 18\omega_7\omega_4cs^2 - 12\omega_7cs^2 - 12\omega_4cs^2 - 6\omega_4^2v_3^2 + 12\omega_4v_3^2 + 6\omega_4^2cs^2 - 3\omega_7\omega_4^2cs^2 + 6\omega_7\omega_4v_3^2 - 12\omega_7v_3^2) \frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} \\
& + (\omega_4^2\omega_2^2 - 6\omega_4^2\omega_2 + 6\omega_2^2 + 6\omega_4^2 - 6\omega_4\omega_2^2) \frac{\rho v_1 v_3\delta_l^3}{6\omega_4^2\omega_2^2\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{v_2\delta_l^3}{2\omega_7\omega_4^2\omega_3^2\delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} +
\end{aligned}$$

$$\begin{aligned}
& (\omega_7\omega_4^2v_3^2+18\omega_7\omega_4cs^2-12\omega_7cs^2-12\omega_4cs^2-6\omega_4^2v_3^2+12\omega_4v_3^2+6\omega_4^2cs^2-3\omega_7\omega_4^2cs^2+6\omega_7\omega_4v_3^2-12\omega_7v_3^2)\frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t}\frac{\partial^3v_2}{\partial x_2\partial x_3^2} \\
& + (-6\omega_4^2\omega_3+6\omega_3^2+\omega_4^2\omega_3^2+6\omega_4^2-6\omega_4\omega_3^2)\frac{\rho v_2v_3\delta_l^3}{6\omega_4^2\omega_3^2\delta_t}\frac{\partial^3v_3}{\partial x_2\partial x_3^2} + C_{11}\frac{v_3\delta_l^3}{6\omega_7\omega_4\delta_t}\frac{\partial^3\rho}{\partial x_3^3} + C_{12}\frac{\rho\delta_l^3}{12\omega_7\omega_4^2\delta_t}\frac{\partial^3v_3}{\partial x_3^3} + \\
& (-2-\omega_2^2+3\omega_2)\frac{\rho\delta_l\delta_t^2}{2\omega_3^2}\frac{\partial^4v_1}{\partial t^3\partial x_1} + (-2-\omega_2^2+3\omega_2)\frac{3\rho v_1\delta_l^2\delta_t}{2\omega_3^2}\frac{\partial^4v_1}{\partial t^2\partial x_1^2} + C_{13}\frac{\rho\delta_l^3}{12\omega_5^2\omega_3^2}\frac{\partial^4v_1}{\partial t\partial x_1^3} + C_{14}\frac{\delta_l^4}{24\omega_5^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1^4} + \\
& C_{15}\frac{\rho v_1\delta_l^4}{12\omega_5^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1^4} + (-2-\omega_3^2+3\omega_3)\frac{\rho\delta_l\delta_t^2}{2\omega_3^2}\frac{\partial^4v_2}{\partial t^3\partial x_2} + \\
& (7\omega_2\omega_3^3-6\omega_3^3-24\omega_2\omega_3^2+12\omega_3^2+12\omega_2^2+12\omega_2\omega_3-24\omega_2^2\omega_3+13\omega_2^2\omega_3^2-\omega_2^2\omega_3^3)\frac{\rho v_2\delta_l^2\delta_t}{12\omega_2^2\omega_3^3}\frac{\partial^4v_1}{\partial t^2\partial x_1\partial x_2} + \\
& (-24\omega_2\omega_3^2+12\omega_3^2+12\omega_2^2+12\omega_2\omega_3-6\omega_3^2-\omega_2^2\omega_3^2-24\omega_2^2\omega_3+13\omega_2^2\omega_3^2+7\omega_2^2\omega_3^3)\frac{\rho v_1\delta_l^2\delta_t}{12\omega_2^2\omega_3^3}\frac{\partial^4v_2}{\partial t^2\partial x_1\partial x_2} + \\
& (18\omega_2\omega_3^3-12\omega_3^3-6\omega_2^2-7\omega_2^2\omega_3^2-6\omega_2^2\omega_3+\omega_2^2\omega_3^3+6\omega_2^2\omega_3^2+12\omega_2^2\omega_3-7\omega_2^2\omega_3^3)\frac{\rho v_2v_1\delta_l^3}{6\omega_2^2\omega_3^3}\frac{\partial^4v_1}{\partial t\partial x_1^2\partial x_2} + \\
& C_{16}\frac{\rho\delta_l^3}{12\omega_5^2\omega_3^2\omega_2}\frac{\partial^4v_2}{\partial t\partial x_1^2\partial x_2} + C_{17}\frac{v_2v_1\delta_l^4}{6\omega_5^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1^3\partial x_2} + C_{18}\frac{\rho v_2\delta_l^4}{12\omega_5^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1^3\partial x_2} + C_{19}\frac{\rho v_1\delta_l^4}{12\omega_5^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_1^3\partial x_2} + \\
& (-2-\omega_3^2+3\omega_3)\frac{3\rho v_2\delta_l^2\delta_t}{2\omega_3^2}\frac{\partial^4v_2}{\partial t^2\partial x_2^2} + C_{20}\frac{\rho\delta_l^3}{12\omega_2\omega_6^2\omega_3^2}\frac{\partial^4v_1}{\partial t\partial x_1\partial x_2^2} + \\
& (12\omega_2\omega_3^3-6\omega_3^3-6\omega_2\omega_3^2-12\omega_2^2-7\omega_2^2\omega_3^2+\omega_2^2\omega_3^3+6\omega_2^2\omega_3^2+18\omega_2^2\omega_3-7\omega_2^2\omega_3^3)\frac{\rho v_2v_1\delta_l^3}{6\omega_2^2\omega_3^3}\frac{\partial^4v_2}{\partial t\partial x_1\partial x_2^2} + \\
& C_{21}\frac{\delta_l^4}{4\omega_5^2\omega_3^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1^2\partial x_2^2} + C_{22}\frac{\rho v_1\delta_l^4}{12\omega_5^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1^2\partial x_2^2} + C_{23}\frac{\rho v_2\delta_l^4}{12\omega_5^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_1^2\partial x_2^2} + C_{24}\frac{\rho\delta_l^3}{12\omega_6^2\omega_3^2}\frac{\partial^4v_2}{\partial t\partial x_2^3} + \\
& C_{25}\frac{v_2v_1\delta_l^4}{6\omega_5^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1\partial x_2^3} + C_{26}\frac{\rho v_2\delta_l^4}{12\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1\partial x_2^3} + C_{27}\frac{\rho v_1\delta_l^4}{12\omega_5^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_1\partial x_2^3} + C_{28}\frac{\delta_l^4}{24\omega_6^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_2^4} + C_{29}\frac{\rho v_2\delta_l^4}{12\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_2^4} + \\
& (-2+3\omega_4-\omega_4^2)\frac{\rho\delta_l\delta_t^2}{2\omega_4^2}\frac{\partial^4v_3}{\partial t^3\partial x_3} + \\
& (7\omega_4^3\omega_2+13\omega_4^2\omega_2^2-24\omega_4^2\omega_2+12\omega_2^2-\omega_4^3\omega_2^2+12\omega_4^2+12\omega_4\omega_2-6\omega_4^3-24\omega_4\omega_2^2)\frac{\rho v_3\delta_l^2\delta_t}{12\omega_4^2\omega_2^2}\frac{\partial^4v_1}{\partial t^2\partial x_1\partial x_3} + \\
& (-\omega_4^2\omega_2^3+13\omega_4^2\omega_2^2-24\omega_4^2\omega_2+12\omega_2^2-6\omega_2^3+12\omega_4^2+12\omega_4\omega_2-24\omega_4\omega_2^2+7\omega_4\omega_2^3)\frac{\rho v_1\delta_l^2\delta_t}{12\omega_4^2\omega_2^2}\frac{\partial^4v_3}{\partial t^2\partial x_1\partial x_3} + \\
& (-7\omega_4^2\omega_2^3+18\omega_4^2\omega_2+6\omega_4^2\omega_2^2+\omega_4^3\omega_2^2-6\omega_2^3-7\omega_4^3\omega_2^2-12\omega_4^3-6\omega_4\omega_2^2+12\omega_4\omega_2^3)\frac{\rho v_1v_3\delta_l^3}{6\omega_4^2\omega_2^2}\frac{\partial^4v_1}{\partial t\partial x_1^2\partial x_3} + \\
& C_{30}\frac{\rho\delta_l^3}{12\omega_4\omega_5^2\omega_3^2}\frac{\partial^4v_3}{\partial t\partial x_1^2\partial x_3} + C_{31}\frac{v_1v_3\delta_l^4}{6\omega_4^2\omega_5^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1^3\partial x_3} + C_{32}\frac{\rho v_3\delta_l^4}{12\omega_4^2\omega_5^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1^3\partial x_3} + C_{33}\frac{\rho v_1\delta_l^4}{12\omega_5^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_1^3\partial x_3} + \\
& (-\omega_4^3\omega_3^2-24\omega_4^2\omega_3+12\omega_3^2+13\omega_4^2\omega_3^2+7\omega_4^3\omega_3+12\omega_4^2-24\omega_4\omega_3^2-6\omega_4^3+12\omega_4\omega_3^3)\frac{\rho v_3\delta_l^2\delta_t}{12\omega_4^2\omega_3^2}\frac{\partial^4v_2}{\partial t^2\partial x_2\partial x_3} + \\
& (-6\omega_3^3-24\omega_4^2\omega_3+12\omega_3^2+13\omega_4^2\omega_3^2-\omega_4^2\omega_3^3+7\omega_4\omega_3^3+12\omega_4^2-24\omega_4\omega_3^2+12\omega_4\omega_3^3)\frac{\rho v_2\delta_l^2\delta_t}{12\omega_4^2\omega_3^2}\frac{\partial^4v_3}{\partial t^2\partial x_2\partial x_3} + \\
& C_{34}\frac{\rho v_2v_3\delta_l^3}{6\omega_4^2\omega_3^2}\frac{\partial^4v_1}{\partial t\partial x_1\partial x_2\partial x_3} + C_{35}\frac{\rho v_1v_3\delta_l^3}{6\omega_4^2\omega_3^2}\frac{\partial^4v_2}{\partial t\partial x_1\partial x_2\partial x_3} + C_{36}\frac{\rho v_2v_1\delta_l^3}{6\omega_4\omega_3^2\omega_3^2}\frac{\partial^4v_3}{\partial t\partial x_1\partial x_2\partial x_3} + C_{37}\frac{v_2v_3\delta_l^4}{\omega_4^2\omega_5^2\omega_2^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1^2\partial x_2\partial x_3} + \\
& C_{38}\frac{\rho v_2v_1v_3\delta_l^4}{6\omega_4^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1^2\partial x_2\partial x_3} + C_{39}\frac{\rho v_3\delta_l^4}{12\omega_4^2\omega_5^2\omega_2^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_1^2\partial x_2\partial x_3} + C_{40}\frac{\rho v_2\delta_l^4}{12\omega_5^2\omega_2^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_1^2\partial x_2\partial x_3} + \\
& (-6\omega_3^3-7\omega_4^3\omega_3^2+\omega_4^3\omega_3^3+6\omega_4^2\omega_3^2+18\omega_4^3\omega_3-7\omega_4^2\omega_3^3+12\omega_4\omega_3^3-6\omega_4\omega_3^2-12\omega_4^3)\frac{\rho v_2v_3\delta_l^3}{6\omega_4^2\omega_3^2}\frac{\partial^4v_2}{\partial t\partial x_2^2\partial x_3} + \\
& C_{41}\frac{\rho\delta_l^3}{12\omega_4\omega_6^2\omega_3^2}\frac{\partial^4v_3}{\partial t\partial x_2^2\partial x_3} + C_{42}\frac{v_1v_3\delta_l^4}{\omega_4^2\omega_3^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1\partial x_2^2\partial x_3} + C_{43}\frac{\rho v_3\delta_l^4}{12\omega_4^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1\partial x_2^2\partial x_3} + C_{44}\frac{\rho v_2v_1v_3\delta_l^4}{6\omega_4^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_1\partial x_2^2\partial x_3} + \\
& C_{45}\frac{\rho v_1\delta_l^4}{12\omega_3^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_1\partial x_2^2\partial x_3} + C_{46}\frac{v_2v_3\delta_l^4}{6\omega_4^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_2^3\partial x_3} + C_{47}\frac{\rho v_3\delta_l^4}{12\omega_4^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_2^3\partial x_3} + C_{48}\frac{\rho v_2\delta_l^4}{12\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_2^3\partial x_3} + \\
& (-2+3\omega_4-\omega_4^2)\frac{3\rho v_3\delta_l^2\delta_t}{2\omega_4^2}\frac{\partial^4v_3}{\partial t^2\partial x_3^2} + C_{49}\frac{\rho\delta_l^3}{12\omega_7^2\omega_4^2\omega_2}\frac{\partial^4v_1}{\partial t\partial x_1\partial x_3^2} + \\
& (-7\omega_4^2\omega_2^3+12\omega_3^3\omega_2+6\omega_4^2\omega_2^2+\omega_4^3\omega_2^2-6\omega_4^2\omega_2-12\omega_2^3-7\omega_4^3\omega_2^2-6\omega_4^3+18\omega_4\omega_2^3)\frac{\rho v_1v_3\delta_l^3}{6\omega_4^2\omega_2^2}\frac{\partial^4v_3}{\partial t\partial x_1\partial x_3^2} + \\
& C_{50}\frac{\delta_l^4}{4\omega_7^2\omega_4^2\omega_3^2\omega_2^2\delta_t}\frac{\partial^4\rho}{\partial x_1^2\partial x_3^2} + C_{51}\frac{\rho v_1\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1^2\partial x_3^2} + C_{52}\frac{\rho v_3\delta_l^4}{12\omega_4^2\omega_7^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_1^2\partial x_3^2} + C_{53}\frac{\rho\delta_l^3}{12\omega_7^2\omega_4^2\omega_3^2}\frac{\partial^4v_2}{\partial t\partial x_2\partial x_3^2} + \\
& (-12\omega_3^3-7\omega_4^3\omega_3^2-6\omega_4^2\omega_3+ \omega_4^3\omega_3^3+6\omega_4^2\omega_3^2+12\omega_4^3\omega_3-7\omega_4^2\omega_3^3+18\omega_4\omega_3^3-6\omega_4^3)\frac{\rho v_2v_3\delta_l^3}{6\omega_4^2\omega_3^2}\frac{\partial^4v_3}{\partial t\partial x_2\partial x_3^2} + \\
& C_{54}\frac{v_2v_1\delta_l^4}{\omega_7^2\omega_4^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1\partial x_2\partial x_3^2} + C_{55}\frac{\rho v_2\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1\partial x_2\partial x_3^2} + C_{56}\frac{\rho v_1\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_1\partial x_2\partial x_3^2} + C_{57}\frac{\rho v_2v_1v_3\delta_l^4}{6\omega_4^2\omega_3^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{58}\frac{\delta_l^4}{4\omega_7^2\omega_4^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_2^2\partial x_3^2} + C_{59}\frac{\rho v_2\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_2}{\partial x_2^2\partial x_3^2} + C_{60}\frac{\rho v_3\delta_l^4}{12\omega_4^2\omega_6^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_2^2\partial x_3^2} + C_{61}\frac{\rho\delta_l^3}{12\omega_7^2\omega_4^2}\frac{\partial^4v_3}{\partial t\partial x_3^3} + \\
& C_{62}\frac{v_1v_3\delta_l^4}{6\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_1\partial x_3^3} + C_{63}\frac{\rho v_3\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_1}{\partial x_1\partial x_3^3} + C_{64}\frac{\rho v_1\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_1\partial x_3^3} + C_{65}\frac{v_2v_3\delta_l^4}{6\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4\rho}{\partial x_2\partial x_3^3} + \\
& C_{66}\frac{\rho v_3\delta_l^4}{12\omega_7^2\omega_4^2\delta_t}\frac{\partial^4v_2}{\partial x_2\partial x_3^3} + C_{67}\frac{\rho v_2\delta_l^4}{12\omega_7^2\omega_4^2\omega_3^2\delta_t}\frac{\partial^4v_3}{\partial x_2\partial x_3^3} + C_{68}\frac{\delta_l^4}{24\omega_7^2\omega_4^2\delta_t}\frac{\partial^4\rho}{\partial x_3^4} + C_{69}\frac{\rho v_3\delta_l^4}{12\omega_7^2\omega_4^2\delta_t}\frac{\partial^4v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - v_1^2 \omega_5 \omega_2 - 3cs^2 \omega_5 \omega_2 - 3\omega_5 + \omega_5 \omega_2 - 3\omega_2 - 18cs^2 - 6v_1^2 + 9cs^2 \omega_5 + 3v_1^2 \omega_5 + 3v_1^2 \omega_2 + 9cs^2 \omega_2 \\
C_2 &= 2\omega_5 \omega_2^2 - 5v_1^2 \omega_5 \omega_2^2 - 3cs^2 \omega_5 \omega_2^2 - 6\omega_2^2 + 6v_1^2 \omega_5 \omega_2 + 18cs^2 \omega_5 \omega_2 - 6\omega_5 \omega_2 + 12\omega_2 + 18v_1^2 \omega_2^2 + 6cs^2 \omega_2^2 - 12cs^2 \omega_5 + 12v_1^2 \omega_5 - 36v_1^2 \omega_2 - 12cs^2 \omega_2 \\
C_3 &= -2v_1^2 \omega_5 \omega_2 \omega_3^2 + 2v_1^2 \omega_5 \omega_3^2 + 4cs^2 \omega_5 \omega_2 \omega_3^2 - 2cs^2 \omega_2 \omega_3^2 + 2v_1^2 \omega_2 \omega_3^2 - 2cs^2 \omega_5 \omega_2 \omega_3 + 2v_1^2 \omega_5 \omega_2 \omega_3 - 2cs^2 \omega_5 \omega_3^2 + cs^2 \omega_5 \omega_2 \omega_3 - \\
& 3v_1^2 \omega_5 \omega_2^2 \omega_3 + cs^2 \omega_2^2 \omega_3 - v_1^2 \omega_2^2 \omega_3 + v_1^2 \omega_5 \omega_2^2 \omega_3 - cs^2 \omega_5 \omega_2^2 \omega_3 \\
C_4 &= 4cs^2 \omega_2^2 \omega_6 \omega_3 - 2v_2^2 \omega_2^2 \omega_6 \omega_3 + 2v_2^2 \omega_2^2 \omega_3 - v_2^2 \omega_2^2 \omega_3^2 - 2cs^2 \omega_2^2 \omega_6 - cs^2 \omega_2^2 \omega_6 \omega_3^2 + v_2^2 \omega_2^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 - 2cs^2 \omega_2^2 \omega_3 - 3v_2^2 \omega_2 \omega_6 \omega_3^2 + \\
& cs^2 \omega_2 \omega_6 \omega_3^2 + 2v_2^2 \omega_2 \omega_6 \omega_3 - 2cs^2 \omega_2 \omega_6 \omega_3 + cs^2 \omega_2^2 \omega_3^2 \\
C_5 &= 6 + 3v_2^2 \omega_6 + 9cs^2 \omega_6 + \omega_6 \omega_3 - 3cs^2 \omega_6 \omega_3 + 9cs^2 \omega_3 - 3\omega_6 - 3\omega_3 - 18cs^2 + 3v_2^2 \omega_3 - 6v_2^2 - v_2^2 \omega_6 \omega_3 \\
C_6 &= -3cs^2 \omega_6 \omega_3^2 + 2\omega_6 \omega_3^2 + 12v_2^2 \omega_6 - 6\omega_3^2 - 12cs^2 \omega_6 - 6\omega_6 \omega_3 + 18cs^2 \omega_6 \omega_3 - 5v_2^2 \omega_6 \omega_3^2 - 12cs^2 \omega_3 + 18v_2^2 \omega_3^2 + 12\omega_3 - 36v_2^2 \omega_3 + 6cs^2 \omega_3^2 + 6v_2^2 \omega_6 \omega_3 \\
C_7 &= -3\omega_4 v_1^2 \omega_5 \omega_2^2 + 2v_1^2 \omega_5 \omega_2^2 + \omega_4 cs^2 \omega_5 \omega_2^2 + 2\omega_4 v_1^2 \omega_5 \omega_2 - 2\omega_4 cs^2 \omega_5 \omega_2 - \omega_4^2 cs^2 \omega_5 \omega_2^2 + \omega_4^2 v_1^2 \omega_5 \omega_2^2 - 2\omega_4^2 cs^2 \omega_5 - 2\omega_4^2 cs^2 \omega_2 + 2\omega_4^2 v_1^2 \omega_2 + \\
& \omega_4^2 cs^2 \omega_2^2 - \omega_4^2 v_1^2 \omega_2^2 + 4\omega_4^2 cs^2 \omega_5 \omega_2 - 2\omega_4^2 v_1^2 \omega_5 \omega_2 \\
C_8 &= \omega_4 cs^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - 2\omega_4^2 cs^2 \omega_6 - 2\omega_4^2 v_2^2 \omega_6 \omega_3 - 2\omega_4 cs^2 \omega_6 \omega_3 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + 2\omega_4^2 v_2^2 \omega_3 - \omega_4^2 cs^2 \omega_6 \omega_3^2 + \omega_4^2 cs^2 \omega_3^2 - \\
& 2\omega_4^2 cs^2 \omega_3 - \omega_4^2 v_2^2 \omega_3 + 4\omega_4^2 cs^2 \omega_6 \omega_3 + 2\omega_4 v_2^2 \omega_6 \omega_3 \\
C_9 &= 2\omega_7 \omega_4^2 v_3^2 - 2\omega_4 cs^2 \omega_2^2 + 2\omega_7 \omega_4 v_3^2 \omega_2 - \omega_7 \omega_4^2 cs^2 \omega_2^2 - \omega_4^2 v_3^2 \omega_2^2 + \omega_7 \omega_4^2 cs^2 \omega_2 - 2\omega_7 \omega_4 v_3^2 \omega_2^2 + 2\omega_4 v_3^2 \omega_2^2 - 2\omega_7 \omega_4 cs^2 \omega_2 + \omega_7 \omega_4^2 v_3^2 \omega_2^2 + \\
& \omega_4^2 cs^2 \omega_2^2 - 3\omega_7 \omega_4^2 v_3^2 \omega_2 + 4\omega_7 \omega_4 cs^2 \omega_2^2 - 2\omega_7 cs^2 \omega_2^2 \\
C_{10} &= 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 v_3^2 \omega_3^2 - \omega_4^2 v_3^2 \omega_3^2 + \omega_7 \omega_4^2 cs^2 \omega_3 - \omega_7 \omega_4^2 cs^2 \omega_3^2 - 2\omega_4 cs^2 \omega_3^2 + 2\omega_7 \omega_4 v_3^2 \omega_3 + 4\omega_7 \omega_4 cs^2 \omega_3^2 - 2\omega_7 cs^2 \omega_3^2 + \omega_4^2 cs^2 \omega_3^2 - \\
& 3\omega_7 \omega_4^2 v_3^2 \omega_3 + \omega_7 \omega_4^2 v_3^2 \omega_3^2 + 2\omega_4 v_3^2 \omega_3^2 - 2\omega_7 \omega_4 cs^2 \omega_3 \\
C_{11} &= 6 - 3\omega_7 - 6v_3^2 + \omega_7 \omega_4 - 3\omega_4 - 3\omega_7 \omega_4 cs^2 + 9\omega_7 cs^2 + 9\omega_4 cs^2 + 3\omega_4 v_3^2 - 18cs^2 - \omega_7 \omega_4 v_3^2 + 3\omega_7 v_3^2 \\
C_{12} &= -5\omega_7 \omega_4^2 v_3^2 - 6\omega_7 \omega_4 + 12\omega_4 + 18\omega_7 \omega_4 cs^2 - 12\omega_7 cs^2 - 12\omega_4 cs^2 + 18\omega_4^2 v_3^2 + 2\omega_7 \omega_4^2 - 36\omega_4 v_3^2 - 6\omega_4^2 + 6\omega_4^2 cs^2 - 3\omega_7 \omega_4^2 cs^2 + 6\omega_7 \omega_4 v_3^2 + 12\omega_7 v_3^2 \\
C_{13} &= 36\omega_5 \omega_2^2 - 108v_1^2 \omega_5 \omega_2^2 - 36cs^2 \omega_5 \omega_2^2 - 9\omega_5 \omega_2^2 + 9cs^2 \omega_5 \omega_2^2 + 27v_1^2 \omega_5 \omega_2^2 - 12\omega_2^2 + 72v_1^2 \omega_5 \omega_2 + 24cs^2 \omega_5 \omega_2 + 6\omega_3^2 - 24\omega_5 \omega_2 + 18v_1^2 \omega_5^2 \omega_2 + \\
& 36v_1^2 \omega_2^2 - 48cs^2 \omega_5^2 \omega_2 + 12cs^2 \omega_2^2 + 12\omega_5^2 \omega_2 - 6cs^2 \omega_2^2 - 18v_1^2 \omega_2^2 + 24cs^2 \omega_5^2 - 36v_1^2 \omega_5^2 + \omega_5^2 \omega_2^2 - 2cs^2 \omega_5^2 \omega_2 - 3v_1^2 \omega_5^2 \omega_2 - 11\omega_5^2 \omega_2^2 + 15v_1^2 \omega_5^2 \omega_2^2 + 25cs^2 \omega_5^2 \omega_2^2 \\
C_{14} &= \\
& 36v_1^4 \omega_2^2 + 24cs^4 \omega_5^2 - 72cs^2 v_1^2 \omega_5 \omega_2^2 - 72v_1^2 \omega_5 \omega_2^2 + 24cs^2 \omega_5 \omega_2^2 + 144cs^2 v_1^2 \omega_5 \omega_2^2 - 72v_1^4 \omega_2^2 + 24cs^4 \omega_5 \omega_2 - 6cs^2 \omega_5 \omega_2^2 + 30v_1^2 \omega_5 \omega_2^2 + 72cs^2 v_1^2 \omega_5 \omega_2 + \\
& 72v_1^4 \omega_5 \omega_2^2 - 24cs^4 \omega_5 \omega_2^2 - 24cs^2 \omega_5 \omega_2 + 6cs^4 \omega_5 \omega_2^2 - 30v_1^4 \omega_5 \omega_2^2 + 72v_1^2 \omega_2^2 + 12cs^2 \omega_5^2 \omega_2 - 216cs^2 v_1^2 \omega_2^2 - 3cs^4 \omega_5^2 \omega_2^2 + 3v_1^4 \omega_5^2 \omega_2^2 - 36v_1^2 \omega_2^2 - \\
& 36cs^2 v_1^2 \omega_2^2 \omega_2 - 12v_1^4 \omega_2^2 \omega_2^2 + 24cs^4 \omega_5^2 \omega_2^2 + 108cs^2 v_1^2 \omega_2^2 - 12cs^2 v_1^2 \omega_5^2 \omega_2^2 - 48cs^4 \omega_2^2 \omega_2 + cs^2 \omega_2^2 \omega_2^2 - 3v_1^2 \omega_5^2 \omega_2^2 + 6cs^2 v_1^2 \omega_5^2 \omega_2^2 + 12v_1^2 \omega_5^2 \omega_2^2 - 8cs^2 \omega_5^2 \omega_2^2 \\
C_{15} &= -24\omega_5 \omega_2^2 + 24v_1^2 \omega_5 \omega_2^2 + 72cs^2 \omega_5 \omega_2^2 + 12\omega_5 \omega_2^2 - 24cs^2 \omega_5 \omega_2^2 - 24v_1^2 \omega_5 \omega_2^2 + 36\omega_2^2 + 60v_1^2 \omega_5 \omega_2 - 12cs^2 \omega_5 \omega_2 - 18\omega_3^2 - 12\omega_5 \omega_2 - 12v_1^2 \omega_5^2 \omega_2 - \\
& 84v_1^2 \omega_2^2 - 30cs^2 \omega_5^2 \omega_2 - 60cs^2 \omega_2^2 + 6\omega_5^2 \omega_2 + 30cs^2 \omega_2^2 + 42v_1^2 \omega_2^2 + 24cs^2 \omega_5^2 - 12v_1^2 \omega_5^2 - \omega_5^2 \omega_2^2 + cs^2 \omega_5^2 \omega_2^2 + 2v_1^2 \omega_5^2 \omega_2^2 + 2\omega_5^2 \omega_2^2 + 2v_1^2 \omega_5^2 \omega_2^2 - 2cs^2 \omega_5^2 \omega_2^2 \\
C_{16} &= v_1^2 \omega_2^2 \omega_3^2 \omega_3 - 12v_1^2 \omega_5 \omega_2^2 + 12cs^2 \omega_5 \omega_2^2 - 2cs^2 \omega_5^2 \omega_2^2 \omega_3 - 6cs^2 \omega_5 \omega_2^2 + 6v_1^2 \omega_5 \omega_2^2 + 22cs^2 \omega_5^2 \omega_2^2 \omega_3 + 8v_1^2 \omega_5^2 \omega_2^2 \omega_3 + 12cs^2 \omega_5 \omega_2 \omega_3 - \\
& 12v_1^2 \omega_5 \omega_2 \omega_3 + 12v_1^2 \omega_5^2 \omega_2 - 30cs^2 \omega_5 \omega_2^2 \omega_3 + 12cs^2 \omega_5^2 \omega_2 + 30v_1^2 \omega_5 \omega_2^2 \omega_3 + 12cs^2 \omega_5^2 \omega_3 - 30cs^2 \omega_5^2 \omega_2 \omega_3 - 12v_1^2 \omega_2^2 \omega_3 - 36v_1^2 \omega_5^2 \omega_2 \omega_3 - \\
& 9v_1^2 \omega_5 \omega_2^2 \omega_3 + 3cs^2 \omega_5^2 \omega_2^2 + 9cs^2 \omega_5 \omega_2^2 \omega_3 - v_1^2 \omega_5^2 \omega_2^2 + 24v_1^2 \omega_5^2 \omega_3 + 12cs^2 \omega_5^2 \omega_3 - 6v_1^2 \omega_5^2 \omega_2^2 + 6v_1^2 \omega_2^2 \omega_3 - 6cs^2 \omega_2^2 \omega_3 - 18cs^2 \omega_5^2 \omega_2^2 \\
C_{17} &= -6v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 - 3\omega_5^2 \omega_2^2 \omega_3^2 - 12v_1^2 \omega_5^2 \omega_2^2 \omega_3 + 12\omega_5 \omega_2 \omega_3^2 - 36cs^2 \omega_5^2 \omega_2^2 \omega_3 + 6cs^2 \omega_5^2 \omega_2^2 \omega_3 - 24v_1^2 \omega_5 \omega_2 \omega_3^2 + 7\omega_5^2 \omega_2^2 \omega_3^2 - 6v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 - \\
& 24cs^2 \omega_5 \omega_2 \omega_3^2 + 36cs^2 \omega_5^2 \omega_2^2 \omega_3 + 6cs^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5^2 \omega_2^2 \omega_3 + \omega_5^2 \omega_2^2 \omega_3 + 6v_1^2 \omega_5^2 \omega_2^2 \omega_3 - 12cs^2 \omega_5^2 \omega_2^2 \omega_3 - \omega_5^2 \omega_2^2 \omega_3 + 6v_1^2 \omega_5^2 \omega_2^2 \omega_3 - \\
& 24cs^2 \omega_5 \omega_2^2 \omega_3^2 - 3\omega_5 \omega_2^2 \omega_3^2 + 12cs^2 \omega_5 \omega_2^2 \omega_3^2 + 18cs^2 \omega_2^2 \omega_3^2 - 6v_1^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5^2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - 3\omega_2^2 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 + 12v_1^2 \omega_5 \omega_2^2 \omega_3^2 - \\
& 12cs^2 \omega_5^2 \omega_2 \omega_3^2 + 72cs^2 \omega_5 \omega_2^2 \omega_3^2 + 6v_1^2 \omega_5^2 \omega_2^2 - 21\omega_5 \omega_2^2 \omega_3^2 + 6\omega_2^2 \omega_3^2 + 12v_1^2 \omega_5^2 \omega_2 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 - 24cs^2 \omega_5 \omega_2^2 \omega_3^2 + 36cs^2 \omega_5^2 \omega_2 \omega_3^2 - 36cs^2 \omega_2^2 \omega_3^2 \\
C_{18} &= -12v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 - 6\omega_5^2 \omega_2^2 \omega_3^2 - 18v_1^2 \omega_2^2 \omega_3^2 \omega_3 - 32cs^2 \omega_5^2 \omega_2^2 \omega_3^2 + 6cs^2 \omega_5^2 \omega_2^2 \omega_3 + 12v_1^2 \omega_5 \omega_2 \omega_3^2 + 3\omega_5^2 \omega_2^2 \omega_3^2 + 12v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5 \omega_2 \omega_3^2 + \\
& 48cs^2 \omega_5^2 \omega_2^2 \omega_3^2 + 4cs^2 \omega_5^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5^2 \omega_2^2 \omega_3 + 3v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 + 2\omega_5^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5^2 \omega_2^2 \omega_3^2 - \omega_5^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5 \omega_2^2 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3^2 + \\
& 12cs^2 \omega_5 \omega_2^2 \omega_3^2 + 6cs^2 \omega_2^2 \omega_3^2 - 6v_1^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5^2 \omega_3^2 + 12v_1^2 \omega_5 \omega_2^2 \omega_3^2 + 3\omega_5 \omega_2^2 \omega_3^2 - 24v_1^2 \omega_5^2 \omega_3^2 + 12\omega_5 \omega_2^2 \omega_3^2 - 12v_1^2 \omega_5 \omega_2^2 \omega_3^2 - 24cs^2 \omega_5^2 \omega_2 \omega_3^2 + \\
& 36cs^2 \omega_5 \omega_2^2 \omega_3^2 + 12v_1^2 \omega_5^2 \omega_2^2 - 24v_1^2 \omega_5 \omega_2^2 \omega_3^2 - 6\omega_5 \omega_2^2 \omega_3^2 + 30v_1^2 \omega_5^2 \omega_2 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 - 24cs^2 \omega_5 \omega_2^2 \omega_3^2 + 36cs^2 \omega_5^2 \omega_2 \omega_3^2 - 12cs^2 \omega_2^2 \omega_3^2 \\
C_{19} &= -36\omega_5 \omega_2^2 + 48v_1^2 \omega_5 \omega_2^2 + 96cs^2 \omega_5 \omega_2^2 + 9\omega_5 \omega_2^2 - 30cs^2 \omega_5 \omega_2^2 - 6v_1^2 \omega_5 \omega_2^2 + 12\omega_2^2 - 60v_1^2 \omega_5 \omega_2 - 36cs^2 \omega_5 \omega_2 - 6\omega_3^2 + 24\omega_5 \omega_2 + 12v_1^2 \omega_5^2 \omega_2 + \\
& 12v_1^2 \omega_2^2 + 18cs^2 \omega_5^2 \omega_2 - 60cs^2 \omega_2^2 - 12\omega_5^2 \omega_2 + 30cs^2 \omega_2^2 - 6v_1^2 \omega_2^2 + 12v_1^2 \omega_5^2 - \omega_5^2 \omega_2^2 + 4cs^2 \omega_5^2 \omega_2^2 + v_1^2 \omega_5^2 \omega_2^2 + 11\omega_5^2 \omega_2^2 - 14v_1^2 \omega_5^2 \omega_2^2 - 26cs^2 \omega_5^2 \omega_2^2 \\
C_{20} &= 12cs^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3 - 6cs^2 \omega_2 \omega_3^2 - 30cs^2 \omega_2 \omega_6^2 \omega_3 - 6cs^2 \omega_6 \omega_3^2 - 36v_2^2 \omega_2 \omega_6^2 \omega_3 + 12cs^2 \omega_2 \omega_3^2 + 24v_2^2 \omega_2 \omega_6^2 - v_2^2 \omega_6^2 \omega_3^2 + \\
& 22cs^2 \omega_2 \omega_6^2 \omega_3^2 + 8v_2^2 \omega_2 \omega_6^2 \omega_3^2 - 6v_2^2 \omega_6^2 \omega_3^2 + v_2^2 \omega_2 \omega_6^2 \omega_3^2 - 2cs^2 \omega_2 \omega_6^2 \omega_3^2 - 12v_2^2 \omega_6 \omega_3^2 + 9cs^2 \omega_2 \omega_6 \omega_3^2 + 12cs^2 \omega_6^2 \omega_3 - 9v_2^2 \omega_2 \omega_6 \omega_3^2 + 6v_2^2 \omega_2 \omega_3^2 + \\
& 6v_2^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_2 \omega_3^2 + 30v_2^2 \omega_2 \omega_6 \omega_3^2 - 30cs^2 \omega_2 \omega_6 \omega_3^2 - 12v_2^2 \omega_2 \omega_6 \omega_3 + 3cs^2 \omega_6^2 \omega_3^2 + 12cs^2 \omega_2 \omega_6^2 + 12cs^2 \omega_2 \omega_6 \omega_3 - 18cs^2 \omega_6^2 \omega_2^2 \\
C_{21} &= 2cs^2 v_1^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 + v_2^2 cs^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 - 8cs^2 v_1^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 - 4v_2^2 cs^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 + 4v_2^2 v_1^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 - 4cs^2 v_1^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 + 14v_2^2 v_1^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 - \\
& 2cs^4 \omega_5^2 \omega_3^2 \omega_6 \omega_3^2 - 10v_2^2 v_1^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 - 4cs^2 v_1^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 - 2v_2^2 cs^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 + cs^2 v_1^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 + 10v_2^2 cs^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 + cs^4 \omega_5^2 \omega_3^2 \omega_6 \omega_3^2 - \\
& 3v_2^2 v_1^2 \omega_5^2 \omega_3^2 \omega_6^2 \omega_3^2 + 4v_2^2 v_1^2 \omega_5 \omega_2^2 \omega_6^2 \omega_3^2 + 2cs^2 v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 - 2v_2^2 v_1^2 \omega_5^2 \omega_2^2 \omega_3^2 + 4cs^4 \omega_5^2 \omega_2^2 \omega_6^2 \omega_3^2 - 14v_2^2 v_1^2 \omega_5^2 \omega_2 \omega_6^2 \omega_3^2 + 4v_2^2 v_1^2 \omega_5^2 \omega_2^2 \omega_6 \omega_3^2 -
\end{aligned}$$

$$\begin{aligned}
& 12cs^4\omega_5^2\omega_2^2\omega_3^2 - 4v_2^2cs^2\omega_5^2\omega_2^2\omega_3^3 + cs^4\omega_5\omega_3^2\omega_6^2\omega_3 - 4v_2^2cs^2\omega_5^2\omega_2\omega_6^2\omega_3^2 + 2v_2^2cs^2\omega_5^2\omega_2^2\omega_6\omega_3 + 4v_2^2v_1^2\omega_5^2\omega_6^2\omega_3 - 4cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^2 + \\
& 4cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3^3 - 2v_2^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^3 - 2cs^4\omega_5\omega_3^2\omega_6^2\omega_3^2 + 12v_2^2v_1^2\omega_5^2\omega_2\omega_6^2\omega_3^2 + 2v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - 14v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 + 2v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^3 + \\
& 10cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - 4v_2^2cs^2\omega_5^2\omega_2^2\omega_6\omega_3^2 + 2cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^2 + 10v_2^2cs^2\omega_5^2\omega_2\omega_6^2\omega_3 + 4cs^4\omega_5^2\omega_2\omega_6^2\omega_3 - 2v_2^2v_1^2\omega_5\omega_2^2\omega_6^2\omega_3 - 2cs^4\omega_5^2\omega_2^2\omega_6\omega_3^2 + \\
& 14v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3^3 - 2cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3 + 4v_2^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3 - 4cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3 - 3v_2^2cs^2\omega_5\omega_2^2\omega_6^2\omega_3 - 2cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 + 8v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3^2 + \\
& 2cs^2v_1^2\omega_5\omega_2^2\omega_6^2\omega_3 + 3v_2^2v_1^2\omega_5\omega_2^2\omega_6^2\omega_3 - 28v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 + 4cs^4\omega_5^2\omega_2\omega_6^2\omega_3 - 2cs^4\omega_5^2\omega_2\omega_6^2\omega_3 + 2v_2^2cs^2\omega_5\omega_2^2\omega_6^2\omega_3 + 8cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - \\
& 8v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - cs^2v_1^2\omega_5\omega_2^2\omega_6^2\omega_3 + 4v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - 4cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - 3cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3 + 2v_2^2cs^2\omega_5^2\omega_2^2\omega_6\omega_3 + 4v_2^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + \\
& 4cs^4\omega_5\omega_2^2\omega_6^2\omega_3 - cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3 + 3v_2^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3 - 4v_2^2cs^2\omega_5^2\omega_2^2\omega_6^2\omega_3 + 12v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 + 10cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3 - v_2^2cs^2\omega_5^2\omega_2^2\omega_6\omega_3 - \\
& 4cs^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - 4v_2^2cs^2\omega_5\omega_2\omega_6^2\omega_3 + 4v_2^2v_1^2\omega_5^2\omega_2^2\omega_6^2\omega_3 - 2cs^4\omega_5\omega_2^2\omega_6^2\omega_3 - 10v_2^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3 + 4cs^4\omega_5^2\omega_2^2\omega_6^2\omega_3
\end{aligned}$$

$$\begin{aligned}
C_{22} = & 12v_2^2\omega_2^3\omega_3^3 - 4v_2^2\omega_2^3\omega_2^2\omega_3^3 + cs^2\omega_2^3\omega_2^2\omega_3^3 - 14cs^2\omega_2^3\omega_2^2\omega_3^3 - 6v_2^2\omega_2^3\omega_3^3 + 22v_2^2\omega_2^3\omega_2^2\omega_3^3 + 12v_2^2\omega_2^3\omega_3^3 + 24cs^2\omega_2^3\omega_2^2\omega_3^3 - 18v_2^2\omega_2^3\omega_2^2\omega_3^3 - \\
& 12cs^2\omega_2\omega_6^2\omega_3^2 + 24v_2^2\omega_2\omega_6^2\omega_3^2 - 30v_2^2\omega_2\omega_6^2\omega_3^3 + 6cs^2\omega_2\omega_6^2\omega_3^3 - 12cs^2\omega_2^3\omega_6^2 - 12cs^2\omega_2^3\omega_3^3 - 48v_2^2\omega_2^2\omega_6^2\omega_3^2 + 12cs^2\omega_2^2\omega_6^2\omega_3^2 + 6cs^2\omega_2^3\omega_3^3 + \\
& 12v_2^2\omega_2^2\omega_6\omega_3 - 12cs^2\omega_2^2\omega_6\omega_3 - 6cs^2\omega_2^2\omega_6^2\omega_3 + 22v_2^2\omega_2^2\omega_6^2\omega_3 - 24v_2^2\omega_2^2\omega_6\omega_3 + 24cs^2\omega_2^2\omega_6\omega_3 + 24v_2^2\omega_2^2\omega_6^2\omega_3 - 6cs^2\omega_2^2\omega_6\omega_3 + 6v_2^2\omega_2^2\omega_6\omega_3
\end{aligned}$$

$$\begin{aligned}
C_{23} = & 22v_1^2\omega_5^2\omega_2^2\omega_3^3 - 30v_1^2\omega_5^2\omega_2^2\omega_3 - 14cs^2\omega_5^2\omega_2^2\omega_3^3 + 6cs^2\omega_5^2\omega_2^2\omega_3 + 12v_1^2\omega_5\omega_2\omega_3^3 - 48v_1^2\omega_5^2\omega_2^2\omega_3 - 12cs^2\omega_5\omega_2\omega_3^3 + 12cs^2\omega_5^2\omega_2^2\omega_3^3 + \\
& cs^2\omega_5^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_2^2\omega_3 - 4v_1^2\omega_5^2\omega_2^3\omega_3 + 24v_1^2\omega_5^2\omega_2^2\omega_3 - 6cs^2\omega_5^2\omega_2^3\omega_3 + 22v_1^2\omega_5^2\omega_2^3\omega_3 - 6cs^2\omega_5\omega_2^3\omega_3 + 6v_1^2\omega_5\omega_2^3\omega_3 + 6cs^2\omega_2^3\omega_3^3 - \\
& 6v_1^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_3^3 + 24v_1^2\omega_5^2\omega_2\omega_3^3 - 24v_1^2\omega_5\omega_2^2\omega_3^3 + 24cs^2\omega_5\omega_2^2\omega_3^3 + 12v_1^2\omega_5^2\omega_2^2 - 18v_1^2\omega_5^2\omega_2\omega_3^3 + 12v_1^2\omega_2^2\omega_3^3 + 24cs^2\omega_5^2\omega_2\omega_3^3 - 12cs^2\omega_2^2\omega_3^3
\end{aligned}$$

$$\begin{aligned}
C_{24} = & -36cs^2\omega_6\omega_3^2 + 24cs^2\omega_6^2 + 6\omega_3^3 + 18v_2^2\omega_6^2\omega_3 + 36\omega_6\omega_3^2 + 9cs^2\omega_6\omega_3^3 - 9\omega_6\omega_3^3 - 12\omega_3^3 - 3v_2^2\omega_6^2\omega_3^3 - 36v_2^2\omega_6^2 + 15v_2^2\omega_6^2\omega_3 - 24\omega_6\omega_3 + 24cs^2\omega_6\omega_3 - \\
& 108v_2^2\omega_6\omega_3 - 18v_2^2\omega_3^3 + 12\omega_2^2\omega_3 - 48cs^2\omega_6^2\omega_3 + 36v_2^2\omega_3^3 + 27v_2^2\omega_6\omega_3^3 - 6cs^2\omega_3^3 - 2cs^2\omega_6^2\omega_3 + \omega_6^2\omega_3^3 + 25cs^2\omega_6^2\omega_3 + 12cs^2\omega_3^3 + 72v_2^2\omega_6\omega_3 - 11\omega_6^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{25} = & 12v_2^2\omega_2^3\omega_3^2 + 6cs^2\omega_2^3\omega_2^2\omega_3^3 + 7\omega_2^3\omega_6^2\omega_3^2 - 36cs^2\omega_2^3\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^3 - 6v_2^2\omega_2^3\omega_6^2\omega_3^2 - \omega_2^3\omega_6^2\omega_3^3 + 6\omega_2^2\omega_6\omega_3^2 + 6v_2^2\omega_6^2\omega_3^3 + 36cs^2\omega_2^3\omega_6^2\omega_3 + \\
& 12v_2^2\omega_2^3\omega_6^2\omega_3 - 12cs^2\omega_2\omega_6^2\omega_3^2 + 12cs^2\omega_2^2\omega_6\omega_3^3 + 6v_2^2\omega_2\omega_6^2\omega_3^2 - 6\omega_2^3\omega_6^2\omega_3 - 3\omega_2^2\omega_6\omega_3^3 - 12v_2^2\omega_2\omega_6^2\omega_3 - 24cs^2\omega_2^2\omega_6\omega_3^2 + 6cs^2\omega_2\omega_6^2\omega_3^3 - \\
& 12cs^2\omega_2^3\omega_6^2 + 12\omega_2^3\omega_6\omega_3 - 36cs^2\omega_2^2\omega_3^2 + \omega_2^2\omega_6^2\omega_3^3 + 6\omega_2^3\omega_3^3 - 6v_2^2\omega_2^2\omega_6^2\omega_3 + 36cs^2\omega_2^2\omega_6^2\omega_3 - 3\omega_2^2\omega_6^2\omega_3 + 18cs^2\omega_2^3\omega_3^3 - 24v_2^2\omega_2^3\omega_6\omega_3 - \\
& 24cs^2\omega_2^2\omega_6\omega_3 - 12cs^2\omega_2^2\omega_6^2\omega_3 + 6v_2^2\omega_2^2\omega_6^2\omega_3 - 3\omega_2^2\omega_3^3 + 12v_2^2\omega_2^2\omega_6\omega_3^2 + 72cs^2\omega_2^2\omega_6\omega_3^2 + 6\omega_2^2\omega_6\omega_3^3 - 12cs^2\omega_2^2\omega_6^2\omega_3 - 24cs^2\omega_2^2\omega_6\omega_3^3 - 21\omega_2^3\omega_6\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{26} = & 96cs^2\omega_6\omega_3^2 - 6\omega_3^3 + 12v_2^2\omega_2^2\omega_3 - 36\omega_6\omega_3^2 - 30cs^2\omega_6\omega_3^3 + 9\omega_6\omega_3^3 + 12\omega_3^3 + v_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_6^2 - 14v_2^2\omega_6^2\omega_3 + 24\omega_6\omega_3 - 36cs^2\omega_6\omega_3 + \\
& 48v_2^2\omega_6\omega_3^2 - 6v_2^2\omega_3^3 - 12\omega_2^2\omega_3 + 18cs^2\omega_6^2\omega_3 + 12v_2^2\omega_3^3 - 6v_2^2\omega_6\omega_3^3 + 30cs^2\omega_3^3 + 4cs^2\omega_6^2\omega_3^3 - \omega_6^2\omega_3^3 - 26cs^2\omega_6^2\omega_3 - 60cs^2\omega_3^3 - 60v_2^2\omega_6\omega_3 + 11\omega_6^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{27} = & 12v_2^2\omega_2^3\omega_3^2 + 3v_2^2\omega_2^3\omega_6^2\omega_3^3 + 4cs^2\omega_2^3\omega_2^2\omega_3^3 + 3\omega_2^3\omega_6^2\omega_3^2 - 32cs^2\omega_2^3\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^3 - 12v_2^2\omega_2^3\omega_6^2\omega_3^2 - \omega_2^3\omega_6^2\omega_3^3 + 12\omega_2^2\omega_6\omega_3^2 + 12v_2^2\omega_6^2\omega_3^3 + \\
& 36cs^2\omega_2^3\omega_6^2\omega_3 + 30v_2^2\omega_2^3\omega_6^2\omega_3 + 12v_2^2\omega_2^2\omega_6\omega_3^3 - 12cs^2\omega_2\omega_6^2\omega_3^2 + 12cs^2\omega_2^2\omega_6\omega_3^3 - 6\omega_2^2\omega_6\omega_3^3 - 18v_2^2\omega_2\omega_6^2\omega_3 - 24cs^2\omega_2^2\omega_6\omega_3^2 + 6cs^2\omega_2\omega_6^2\omega_3^3 - \\
& 12cs^2\omega_2^3\omega_6^2 - 24v_2^2\omega_2^2\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_3^2 + 2\omega_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_2^2\omega_6^2\omega_3 + 48cs^2\omega_2^2\omega_6^2\omega_3 - 6\omega_2^2\omega_6^2\omega_3 + 6cs^2\omega_2^3\omega_3^3 + 12v_2^2\omega_2^3\omega_6\omega_3 - \\
& 12cs^2\omega_2^2\omega_6\omega_3 - 12cs^2\omega_2^2\omega_6^2\omega_3 - 12v_2^2\omega_2^2\omega_6\omega_3^2 + 36cs^2\omega_2^2\omega_6\omega_3^2 + 3\omega_2^2\omega_6\omega_3^3 - 24cs^2\omega_2^2\omega_6^2\omega_3 - 12cs^2\omega_2^2\omega_6\omega_3^3 - 6\omega_2^2\omega_6\omega_3^2 - 24v_2^2\omega_2^2\omega_6^2
\end{aligned}$$

$$\begin{aligned}
C_{28} = & 24cs^2\omega_6\omega_3^2 - 72v_2^4\omega_3^2 + 3v_1^4\omega_5^2\omega_3^2 - 72v_2^2cs^2\omega_6\omega_3^3 - 12v_1^4\omega_6^2\omega_3^2 + 36v_1^4\omega_3^3 - 6cs^2\omega_6\omega_3^3 + 144v_2^2cs^2\omega_6\omega_3^2 + 24cs^4\omega_6\omega_3 + 72v_2^2cs^2\omega_6\omega_3 - 24cs^4\omega_6\omega_3^2 - \\
& 3v_2^2\omega_6^2\omega_3^3 + 108v_2^2cs^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^2 + 6cs^4\omega_6\omega_3^3 - 216v_2^2cs^2\omega_3^2 - 24cs^2\omega_6\omega_3^3 - 72v_2^2\omega_6\omega_3^2 - 36v_2^2\omega_3^3 - 3cs^4\omega_6^2\omega_3^3 + 12cs^2\omega_6^2\omega_3^2 + 24cs^4\omega_6^2\omega_3^2 - \\
& 36v_2^2cs^2\omega_6\omega_3 + 72v_2^2\omega_3^3 + 30v_2^2\omega_6\omega_3^3 + 24cs^4\omega_6^2 + 72v_2^2\omega_6\omega_3^2 + cs^2\omega_6^2\omega_3^3 - 48cs^4\omega_6^2\omega_3 - 12v_2^2cs^2\omega_6^2\omega_3 - 8cs^2\omega_6^2\omega_3^2 - 30v_2^4\omega_6\omega_3 + 6v_2^2cs^2\omega_6\omega_3^3
\end{aligned}$$

$$\begin{aligned}
C_{29} = & 72cs^2\omega_6\omega_3^2 + 24cs^2\omega_6^2 - 18\omega_3^3 - 12v_2^2\omega_6^2\omega_3 - 24\omega_6\omega_3^2 - 24cs^2\omega_6\omega_3^3 + 12\omega_6\omega_3^3 + 36\omega_3^2 + 2v_2^2\omega_6^2\omega_3^3 - 12v_2^2\omega_6^2 + 2v_2^2\omega_6^2\omega_3^2 - 12\omega_6\omega_3 - 12cs^2\omega_6\omega_3 + \\
& 24v_2^2\omega_6\omega_3^2 + 42v_2^2\omega_3^3 + 6\omega_6^2\omega_3 - 30cs^2\omega_6^2\omega_3 - 84v_2^2\omega_3^3 - 24v_2^2\omega_6\omega_3^3 + 30cs^2\omega_3^3 + cs^2\omega_6^2\omega_3^3 - \omega_6^2\omega_3^3 - 2cs^2\omega_6^2\omega_3 - 60cs^2\omega_3^3 + 60v_2^2\omega_6\omega_3 + 2\omega_6^2\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{30} = & -12\omega_4v_1^2\omega_2^2 + 12\omega_4cs^2\omega_2^2 + 30\omega_4v_1^2\omega_5\omega_2^2 - 12v_1^2\omega_5\omega_2^2 - 30\omega_4cs^2\omega_5\omega_2^2 + 12cs^2\omega_5\omega_2^2 - 6\omega_4cs^2\omega_2^2 + 6\omega_4v_1^2\omega_3^2 + 12\omega_4cs^2\omega_5^2 + \\
& 24\omega_4v_1^2\omega_5^2 + 9\omega_4cs^2\omega_5\omega_2^2 - 6cs^2\omega_5\omega_2^2 - 9\omega_4v_1^2\omega_5\omega_2^2 + 6v_1^2\omega_5\omega_2^2 - 12\omega_4v_1^2\omega_5\omega_2 + 12\omega_4cs^2\omega_5\omega_2 - 36\omega_4v_1^2\omega_5^2\omega_2 + 12v_1^2\omega_5^2\omega_2 - 30\omega_4cs^2\omega_5^2\omega_2 + \\
& 12cs^2\omega_5^2\omega_2 + 3cs^2\omega_5^2\omega_2^2 - 2\omega_4cs^2\omega_5^2\omega_2 - v_1^2\omega_5^2\omega_2^2 + \omega_4v_1^2\omega_5^2\omega_2^2 - 6v_1^2\omega_5^2\omega_2^2 + 8\omega_4v_1^2\omega_5^2\omega_2^2 - 18cs^2\omega_5^2\omega_2^2 + 22\omega_4cs^2\omega_5^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{31} = & -6\omega_4^3v_1^2\omega_5^2\omega_2^2 - 36\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2 + 7\omega_4^3\omega_5^2\omega_2^2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 + 6\omega_4^3v_1^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 + 6\omega_4^3\omega_5\omega_2^2 - \\
& 12\omega_4^3cs^2\omega_5^2 - 3\omega_4^3\omega_2^3 + 18\omega_4^3cs^2\omega_2^3 - 6\omega_4^3v_1^2\omega_2^3 - 3\omega_4^3\omega_5\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2^2 - 6\omega_4^3v_1^2\omega_5^2\omega_2^2 - 6\omega_4^3\omega_5^2\omega_2 + 12\omega_4^3v_1^2\omega_2^2 + 12\omega_4^3v_1^2\omega_5^2\omega_2 - \\
& 36\omega_4^3cs^2\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 + 6\omega_4^3\omega_2^2 - 24\omega_4^3cs^2\omega_5\omega_2^2 + \omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^3\omega_5\omega_2 - 24\omega_4^3v_1^2\omega_5\omega_2 - 24\omega_4^3cs^2\omega_5\omega_2 - 3\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^3cs^2\omega_5\omega_2^2 - \\
& 24\omega_4^3cs^2\omega_5\omega_2^2 + 6\omega_4cs^2\omega_5^2\omega_2^2 + 6\omega_4^3\omega_5\omega_2^2 + 6v_1^2\omega_5^2\omega_2^2 - 12\omega_4v_1^2\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2^2 + 72\omega_4^3cs^2\omega_5\omega_2^2 + 6\omega_4v_1^2\omega_5^2\omega_2^2 - 21\omega_4^3\omega_5\omega_2^2 - 12\omega_4cs^2\omega_5^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{32} = & -12\omega_4^3v_1^2\omega_5^2\omega_2^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^3cs^2\omega_5^2\omega_2 + 3\omega_4^3\omega_5^2\omega_2^2 + 4\omega_4^3cs^2\omega_5^2\omega_2^2 + 3\omega_4^3v_1^2\omega_5^2\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 + 12\omega_4^3\omega_5\omega_2^2 - \\
& 12\omega_4^3cs^2\omega_5^2 - 24\omega_4^3v_1^2\omega_5^2 - 6\omega_4^3cs^2\omega_2^3 - 6\omega_4^3v_1^2\omega_2^3 - 6\omega_4^3\omega_5\omega_2^2 + 48\omega_4^3cs^2\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_2^2 + 30\omega_4^3v_1^2\omega_5^2\omega_2 - 12\omega_4^3cs^2\omega_2^2 + \\
& 36\omega_4^3cs^2\omega_5^2\omega_2 - 24\omega_4^3cs^2\omega_5\omega_2^2 + 2\omega_4^3\omega_5^2\omega_2^2 - 24\omega_4^3v_1^2\omega_5\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2 - 12\omega_4^3cs^2\omega_5\omega_2 + 12\omega_4^3v_1^2\omega_5\omega_2^2 - 6\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^3cs^2\omega_5\omega_2^2 - \\
& 12\omega_4^3cs^2\omega_5\omega_2^2 + 6\omega_4cs^2\omega_5^2\omega_2^2 + 3\omega_4^3\omega_5\omega_2^2 + 12v_1^2\omega_5^2\omega_2^2 - 18\omega_4v_1^2\omega_5^2\omega_2^2 - 12\omega_4^3v_1^2\omega_5\omega_2^2 + 36\omega_4^3cs^2\omega_5\omega_2^2 - 6\omega_4^3\omega_5\omega_2^2 - 12\omega_4cs^2\omega_5^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{33} = & -36\omega_5\omega_2^2 + 48v_1^2\omega_5\omega_2^2 + 96cs^2\omega_5\omega_2^2 + 9\omega_5\omega_2^2 - 30cs^2\omega_5\omega_2^2 - 6v_1^2\omega_5\omega_2^2 + 12\omega_2^2 - 60v_1^2\omega_5\omega_2 - 36cs^2\omega_5\omega_2 - 6\omega_2^2 + 24\omega_5\omega_2 + 12v_1^2\omega_5^2\omega_2 + \\
& 12v_1^2\omega_2^2 + 18cs^2\omega_5^2\omega_2 - 60cs^2\omega_2^2 - 12\omega_2^2\omega_2 + 30cs^2\omega_2^2 - 6v_1^2\omega_2^2 + 12v_1^2\omega_5^2 - \omega_2^2\omega_2^2 + 4cs^2\omega_5^2\omega_2^2 + v_1^2\omega_5^2\omega_2^2 + 11\omega_5^2\omega_2^2 - 14v_1^2\omega_5^2\omega_2^2 - 26cs^2\omega_5^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{34} = & -6\omega_2\omega_3^3 - 6\omega_4^3\omega_2 - 12\omega_4^3\omega_2\omega_3 + 12\omega_4^3\omega_3^3 - 4\omega_4^3\omega_3^3 - 12\omega_4^3\omega_2^2 - 16\omega_4^3\omega_2\omega_3^3 + 30\omega_4^3\omega_2\omega_3^3 - 6\omega_4^3\omega_3 + 12\omega_4^3\omega_3^3 + 18\omega_4\omega_2\omega_3^3 - 6\omega_4\omega_3^3 + \\
& 18\omega_4^3\omega_2\omega_3 - 12\omega_4\omega_2\omega_3^3 - 16\omega_4^3\omega_2\omega_3^3 + 3\omega_4^3\omega_2\omega_3^3
\end{aligned}$$

$$\begin{aligned}
C_{35} = & 12\omega_2^3\omega_2^2 - 6\omega_4^3\omega_2 - 12\omega_4^3\omega_2\omega_3 + 3\omega_4^3\omega_2^3\omega_3 - 12\omega_4^3\omega_2^2 - 12\omega_4\omega_2^2\omega_3 - 16\omega_4^3\omega_2^2\omega_3 - 4\omega_4^3\omega_2^3 + 18\omega_4\omega_2^2\omega_3 - 6\omega_4^3\omega_3 + 12\omega_4^3\omega_2^2 + \\
& 18\omega_4^3\omega_2\omega_3 - 16\omega_4^3\omega_2^2\omega_3 - 6\omega_2^3\omega_3 - 6\omega_4\omega_2^2 + 30\omega_4^3\omega_2^2\omega_3
\end{aligned}$$

$$\begin{aligned}
C_{36} = & -6\omega_2\omega_3^3 - 16\omega_4\omega_2^2\omega_3^3 - 12\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_2^2\omega_3^3 + 30\omega_4\omega_2^2\omega_3^3 + 18\omega_4\omega_2^2\omega_3 - 16\omega_4\omega_2^2\omega_3^3 + 18\omega_4\omega_2\omega_3^3 - 6\omega_4\omega_3^3 + 12\omega_2^2\omega_3^2 - 12\omega_4\omega_2\omega_3^2 - \\
& 4\omega_2^2\omega_3^3 - 12\omega_2^2\omega_3^2 - 6\omega_2^2\omega_3 + 12\omega_2^2\omega_3^3 - 6\omega_4\omega_2^2
\end{aligned}$$



$$C_{61} = -108\omega_7\omega_4^2v_3^2 - 36\omega_7^2v_3^2 + 25\omega_7^2\omega_4^2cs^2 - 24\omega_7\omega_4 + 24\omega_7\omega_4cs^2 - 18\omega_4^3v_3^2 + 18\omega_7^2\omega_4v_3^2 - 9\omega_7\omega_4^3 - 2\omega_7^2\omega_4^3cs^2 + 27\omega_7\omega_4^3v_3^2 + 36\omega_4^4v_3^2 + 36\omega_7\omega_4^4 - 3\omega_7^2\omega_4^4v_3^2 - 12\omega_4^4 + 9\omega_7\omega_4^3cs^2 - 11\omega_7^2\omega_4^4 + 6\omega_4^3 + 12\omega_7^2cs^2 + \omega_7^2\omega_4^3 - 36\omega_7\omega_4^4cs^2 + 15\omega_7^2\omega_4^4v_3^2 + 24\omega_7^2cs^2 + 72\omega_7\omega_4v_3^2 + 12\omega_7^2\omega_4 - 48\omega_7^2\omega_4cs^2 - 6\omega_4^3cs^2$$

$$\begin{aligned}
C_{62} &= -12\omega_7^2\omega_4^3cs^2\omega_2^2 + 72\omega_7\omega_4^2cs^2\omega_2^3 + 6\omega_4^2\omega_2^3 - 3\omega_7\omega_4^3\omega_2^2 - 6\omega_7^2\omega_1^2v_3^2\omega_2^3 - 12\omega_7^2cs^2\omega_2^3 + 6\omega_7\omega_4^3\omega_2^3 + 6\omega_7^2\omega_4^3cs^2\omega_2^3 - 24\omega_7\omega_4^2cs^2\omega_2^2 - \\
& 6\omega_7^2\omega_4^3v_3^2\omega_2^2 - 24\omega_7\omega_4v_3^2\omega_2^3 + 6\omega_7^2\omega_1^2v_3^2\omega_2 + 6\omega_7\omega_4^2\omega_2^2 + 36\omega_7^2\omega_4cs^2\omega_2^3 - 3\omega_4^3\omega_2^3 - 6\omega_7^2\omega_4\omega_2^3 + 18\omega_4^3cs^2\omega_2^3 + 12\omega_4^2v_3^2\omega_2^3 + 6\omega_7^2\omega_4^3cs^2\omega_2 - \\
& 21\omega_7\omega_4^2\omega_2^3 - 12\omega_7^2\omega_4cs^2\omega_2^2 + 6\omega_7^2\omega_4^3v_3^2\omega_2^2 + 12\omega_7\omega_4^2v_3^2\omega_2^3 + 6\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4\omega_2^3 + 12\omega_7\omega_4^3cs^2\omega_2^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 36\omega_7^2\omega_4cs^2\omega_2^3 + 7\omega_7^2\omega_4^2\omega_2^3 - \\
& 24\omega_7\omega_4^3cs^2\omega_2^2 + 36\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7^2\omega_4^2cs^2\omega_2 + \omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4cs^2\omega_2^2 - 6\omega_4^3v_3^2\omega_2^3 + 12\omega_7\omega_4v_3^2\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 36\omega_4^2cs^2\omega_2^2 - 12\omega_7^2\omega_4^3v_3^2\omega_2 \\
C_{63} &= 48\omega_7\omega_4^2v_3^2 + 12\omega_7^2v_3^2 - 26\omega_7^2\omega_4^2cs^2 + 24\omega_7\omega_4 - 36\omega_7\omega_4cs^2 - 6\omega_4^3v_3^2 + 12\omega_7^2\omega_4v_3^2 + 9\omega_7\omega_4^3 + 4\omega_7^2\omega_4^3cs^2 - 6\omega_7\omega_4^3v_3^2 + 12\omega_4^2v_3^2 - 36\omega_7\omega_4^2 + \\
& \omega_7^2\omega_4^3v_3^2 + 12\omega_4^2 - 30\omega_7\omega_4^3cs^2 + 11\omega_7^2\omega_4^2 - 6\omega_4^3 - 60\omega_4^2cs^2 - \omega_7^2\omega_4^3 + 96\omega_7\omega_4^2cs^2 - 14\omega_7^2\omega_4^2v_3^2 - 60\omega_7\omega_4v_3^2 - 12\omega_7^2\omega_4 + 18\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 \\
C_{64} &= -12\omega_7^2\omega_4^3cs^2\omega_2^2 + 36\omega_7\omega_4^2cs^2\omega_2^3 - 6\omega_7\omega_4^3\omega_2^2 + 12\omega_7\omega_4^2v_3^2\omega_2^2 - 12\omega_7^2\omega_4^2v_3^2\omega_2^3 - 12\omega_7^2cs^2\omega_2^3 + 3\omega_7\omega_4^3\omega_2^3 + 4\omega_7^2\omega_4^3cs^2\omega_2^3 - 24\omega_7\omega_4^2cs^2\omega_2^2 + \\
& 12\omega_7^2\omega_4^2v_3^2\omega_2^2 + 12\omega_7\omega_4v_3^2\omega_2^3 + 12\omega_7\omega_4^2\omega_2^2 + 36\omega_7^2\omega_4cs^2\omega_2^3 + 6\omega_4^3cs^2\omega_2^3 + 12\omega_7^2v_3^2\omega_2^3 + 6\omega_7^2\omega_4^3cs^2\omega_2 - 6\omega_7\omega_4^3\omega_2^3 - 24\omega_7^2\omega_4cs^2\omega_2^2 - \\
& 12\omega_7\omega_4^2v_3^2\omega_2^3 - 24\omega_7^2v_3^2\omega_2^3 + 12\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4^3cs^2\omega_2^2 - 6\omega_7^2\omega_4^2\omega_2^2 - 32\omega_7^2\omega_4^2cs^2\omega_2^3 + 3\omega_7^2\omega_4^3v_3^2\omega_2^3 - 24\omega_7\omega_4^2v_3^2\omega_2^2 + 3\omega_7^2\omega_4^2\omega_2^3 - \\
& 12\omega_7\omega_4^3cs^2\omega_2^2 + 48\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7^2\omega_4^2cs^2\omega_2 + 2\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7\omega_4cs^2\omega_2^2 - 6\omega_4^3v_3^2\omega_2^3 + 30\omega_7\omega_4v_3^2\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_4^2cs^2\omega_2^2 - 18\omega_7^2\omega_4^3v_3^2\omega_2 \\
C_{65} &= 12\omega_7^2v_3^2\omega_3^3 + 6\omega_7^2\omega_3^3cs^2\omega_3 - 12\omega_7^2\omega_4cs^2\omega_3^2 - 21\omega_7\omega_4^2\omega_3^3 - 24\omega_7\omega_4v_3^2\omega_3^3 + 6\omega_7^2\omega_4^2v_3^2\omega_3 - 6\omega_7^2\omega_4\omega_3^3 + 36\omega_7^2\omega_4cs^2\omega_3^3 - 3\omega_4^3\omega_3^3 + 6\omega_7\omega_4^2\omega_3^2 + \\
& 18\omega_4^3cs^2\omega_3^3 + 6\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3^3 - 6\omega_7^2\omega_4^2v_3^2\omega_3^2 + 72\omega_7\omega_4^2cs^2\omega_3^3 - 12\omega_7^2\omega_4^3cs^2\omega_3^2 - 3\omega_7\omega_4^3\omega_3^2 + 6\omega_4^3\omega_3^2 - 6\omega_7^2\omega_4^2v_3^2\omega_3^2 - \\
& 12\omega_7^2cs^2\omega_3^3 - 36\omega_7^2cs^2\omega_3^2 - \omega_7^2\omega_4^3\omega_3^2 + 6\omega_7^2\omega_4^2v_3^2\omega_3^2 - 12\omega_7^2\omega_4^3v_3^2\omega_3^2 + \omega_7^2\omega_4^3\omega_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3^2 - 24\omega_7\omega_4cs^2\omega_3^2 - 6\omega_4^3v_3^2\omega_3^2 + 12\omega_7^2\omega_4^2v_3^2\omega_3^2 + \\
& 36\omega_7^2\omega_4^2cs^2\omega_3^2 + 7\omega_7^2\omega_4^3\omega_3^2 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 12\omega_7\omega_4^3v_3^2\omega_3^2 + 6\omega_7^2\omega_4^3v_3^2\omega_3^2 - 36\omega_7^2\omega_4^2cs^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 3\omega_7^2\omega_4^2\omega_3^2 + 12\omega_7\omega_4\omega_3^3 \\
C_{66} &= 48\omega_7\omega_4^2v_3^2 + 12\omega_7^2v_3^2 - 26\omega_7^2\omega_4^2cs^2 + 24\omega_7\omega_4 - 36\omega_7\omega_4cs^2 - 6\omega_4^3v_3^2 + 12\omega_7^2\omega_4v_3^2 + 9\omega_7\omega_4^3 + 4\omega_7^2\omega_4^3cs^2 - 6\omega_7\omega_4^3v_3^2 + 12\omega_4^2v_3^2 - 36\omega_7\omega_4^2 + \\
& \omega_7^2\omega_4^3v_3^2 + 12\omega_4^2 - 30\omega_7\omega_4^3cs^2 + 11\omega_7^2\omega_4^2 - 6\omega_4^3 - 60\omega_4^2cs^2 - \omega_7^2\omega_4^3 + 96\omega_7\omega_4^2cs^2 - 14\omega_7^2\omega_4^2v_3^2 - 60\omega_7\omega_4v_3^2 - 12\omega_7^2\omega_4 + 18\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 \\
C_{67} &= 12\omega_7^2v_3^2\omega_3^3 + 6\omega_7^2\omega_3^3cs^2\omega_3 - 24\omega_7^2\omega_4cs^2\omega_3^2 - 6\omega_7\omega_4^2\omega_3^3 + 12\omega_7\omega_4v_3^2\omega_3^3 + 36\omega_7^2\omega_4cs^2\omega_3^3 + 12\omega_7\omega_4^2\omega_3^2 + 6\omega_4^3cs^2\omega_3^3 + 3\omega_7\omega_4^3\omega_3^2 - \\
& 24\omega_7\omega_4^2cs^2\omega_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^3 + 12\omega_7^2\omega_4^2v_3^2\omega_3^2 + 36\omega_7\omega_4^2cs^2\omega_3^3 - 12\omega_7^2\omega_4^3cs^2\omega_3^2 - 6\omega_7\omega_4^3\omega_3^2 - 12\omega_7^2\omega_4^2v_3^2\omega_3^2 + 12\omega_7\omega_4^3v_3^2\omega_3^2 - 12\omega_7^2cs^2\omega_3^3 - \\
& 12\omega_7^2cs^2\omega_3^2 - \omega_7^2\omega_4^3\omega_3^2 + 12\omega_7^2\omega_4^2v_3^2\omega_3^2 - 18\omega_7^2\omega_4^3v_3^2\omega_3^2 + 2\omega_7^2\omega_4^3\omega_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3^2 - 12\omega_7\omega_4cs^2\omega_3^2 - 6\omega_4^3v_3^2\omega_3^2 + 30\omega_7^2\omega_4v_3^2\omega_3^2 - 24\omega_7\omega_4^2v_3^2\omega_3^2 + \\
& 3\omega_7^2\omega_4^3v_3^2\omega_3^2 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 + 3\omega_7^2\omega_4^3\omega_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^2 - 12\omega_7\omega_4^2v_3^2\omega_3^2 - 24\omega_7^2v_3^2\omega_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 6\omega_7^2\omega_4^2\omega_3^2 \\
C_{68} &= -72\omega_7\omega_4^2v_3^2 - 8\omega_7^2\omega_4^2cs^2 - 24\omega_7\omega_4^2cs^4 - 12\omega_7^2\omega_4^2v_3^4 + 24\omega_7^2cs^4 + 108\omega_7^3cs^2v_3^2 - 24\omega_7\omega_4cs^2 - 36\omega_7^2\omega_4cs^2v_3^2 - 36\omega_4^3v_3^2 - 48\omega_7^2\omega_4cs^4 + 3\omega_7^2\omega_4^3v_3^4 + \\
& 6\omega_7\omega_4^3cs^4 + 6\omega_7^2\omega_4^3cs^2v_3^2 + \omega_7^2\omega_4^3cs^2 + 30\omega_7\omega_4^3v_3^2 + 72\omega_4^2v_3^2 + 144\omega_7\omega_4^2cs^2v_3^2 - 3\omega_7^2\omega_4^3cs^4 - 30\omega_7\omega_4^3v_3^4 - 3\omega_7^2\omega_4^3v_3^2 - 216\omega_4^2cs^2v_3^2 - 6\omega_7\omega_4^3cs^2 - \\
& 72\omega_4^2v_3^4 + 72\omega_7\omega_4cs^2v_3^2 + 24\omega_7\omega_4^2cs^2 + 12\omega_7^2\omega_4^2v_3^2 - 72\omega_7\omega_4^3cs^2v_3^2 + 72\omega_7\omega_4^2v_3^4 + 24\omega_7^2\omega_4^2cs^4 - 12\omega_7^2\omega_4^2cs^2v_3^2 + 12\omega_7^2\omega_4cs^2 + 24\omega_7\omega_4cs^4 + 36\omega_4^3v_3^4 \\
C_{69} &= 24\omega_7\omega_4^2v_3^2 - 12\omega_7^2v_3^2 - 2\omega_7^2\omega_4^2cs^2 - 12\omega_7\omega_4 - 12\omega_7\omega_4cs^2 + 42\omega_4^3v_3^2 - 12\omega_7^2\omega_4v_3^2 + 12\omega_7\omega_4^3 + \omega_7^2\omega_4^3cs^2 - 24\omega_7\omega_4^3v_3^2 - 84\omega_4^2v_3^2 - 24\omega_7\omega_4^2 + \\
& 2\omega_7^2\omega_4^3v_3^2 + 36\omega_4^2 - 24\omega_7\omega_4^3cs^2 + 2\omega_7^2\omega_4^2 - 18\omega_4^3 - 60\omega_4^2cs^2 - \omega_7^2\omega_4^3 + 72\omega_7\omega_4^2cs^2 + 2\omega_7^2\omega_4^2v_3^2 + 24\omega_7^2cs^2 + 60\omega_7\omega_4v_3^2 + 6\omega_7^2\omega_4 - 30\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2
\end{aligned}$$

## 2.5 CLBM2

### 2.5.1 Definitions

Collision operator  $C$ :

$$C(f) = \mathbf{K}^{-1} \mathbf{S} \left( \boldsymbol{\kappa}^{(eq)} - \mathbf{K} f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7),$$

$$\omega_1, \omega_2, \dots, \omega_7 \in (0, 2).$$

Matrix  $\mathbf{K}$  corresponds to the transformation matrix to the central moment basis defined by

$$\boldsymbol{\kappa} = \begin{pmatrix} k_{(0,0,0)} \\ k_{(1,0,0)} \\ k_{(0,1,0)} \\ k_{(0,0,1)} \\ k_{(2,0,0)} + k_{(0,2,0)} + k_{(0,0,2)} \\ k_{(2,0,0)} - k_{(0,2,0)} \\ k_{(2,0,0)} - k_{(0,0,2)} \end{pmatrix},$$

Thus, the transformation matrix  $\mathbf{K}$  satisfies

$$\begin{aligned}
\mathbf{K}_{1,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,0)}, \\
\mathbf{K}_{2,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,0)}, \\
\mathbf{K}_{3,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,0)}, \\
\mathbf{K}_{4,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,1)}, \\
\mathbf{K}_{5,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,0,2)}, \\
\mathbf{K}_{6,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,0)}, \\
\mathbf{K}_{7,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,0,2)},
\end{aligned}$$

$\forall i \in \{1, 2, \dots, 7\}$ .

The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K} \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left( \rho, 0, 0, 0, 3\rho c_s^2, 0, 0 \right)^T.$$

### 2.5.2 Conservation of mass equation



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$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{\delta_l}{2\omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t} + \\
& (-2 + \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (-2 + \omega_2) \frac{\rho \delta_l^2}{2\omega_2 \delta_t} \left( \frac{\partial v_1}{\partial x_1} \right)^2 + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\
& (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{\rho \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\
& (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{\rho \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_3) \frac{\delta_l}{2\omega_3} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t} + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1} + (2 - \omega_2) \frac{v_1 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\
& + (-2 + \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (-2 + \omega_3) \frac{\rho \delta_l^2}{2\omega_3 \delta_t} \left( \frac{\partial v_2}{\partial x_2} \right)^2 + (2 - \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} \\
& + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{\rho \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_4) \frac{\delta_l}{2\omega_4} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t} + (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + \\
& (2 - \omega_2) \frac{v_1 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_3 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + (2 - \omega_3) \frac{v_2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_4) \frac{v_3 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + \\
& (-2 + \omega_4) \frac{\rho \delta_l^2}{2\omega_4 \delta_t} \left( \frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{\rho \delta_l}{2\omega_2} \frac{\partial^2 v_1}{\partial t \partial x_1} + (-2 + \omega_2) \frac{cs^2 \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_2) \frac{v_1 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + (-2 + \omega_3) \frac{\rho \delta_l}{2\omega_3} \frac{\partial^2 v_2}{\partial t \partial x_2} \\
& + (\omega_2 - \omega_2 \omega_3 + \omega_3) \frac{v_2 v_1 \delta_l^2}{\omega_2 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_3) \frac{cs^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + \\
& (-2 + \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-2 + \omega_4) \frac{\rho \delta_l}{2\omega_4} \frac{\partial^2 v_3}{\partial t \partial x_3} + (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3 v_1 \delta_l^2}{\omega_4 \omega_2 \delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\
& (2 - \omega_2) \frac{v_1 \rho \delta_l^2}{2\omega_2 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-\omega_4 \omega_3 + \omega_4 + \omega_3) \frac{v_3 v_2 \delta_l^2}{\omega_4 \omega_3 \delta_t} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + (2 - \omega_4) \frac{v_3 \rho \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (2 - \omega_3) \frac{v_2 \rho \delta_l^2}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + \\
& (-2 + \omega_4) \frac{cs^2 \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_4) \frac{v_3 \rho \delta_l^2}{2\omega_4 \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + (12 + \omega_2^2 - 12\omega_2) \frac{\rho \delta_l \delta_t}{12\omega_2^2} \frac{\partial^3 v_1}{\partial t^2 \partial x_1} + (12 + \omega_2^2 - 12\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_2^2} \frac{\partial^3 v_1}{\partial t \partial x_1^2} + \\
& C_1 \frac{v_1 \delta_l^3}{6\omega_5 \omega_2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\rho \delta_l^3}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + (12 + \omega_3^2 - 12\omega_3) \frac{\rho \delta_l \delta_t}{12\omega_3^2} \frac{\partial^3 v_2}{\partial t^2 \partial x_2} + \\
& (3\omega_3^2 - 6\omega_2 + 9\omega_2 \omega_3 - 6\omega_3 - 2\omega_2 \omega_3^2) \frac{v_2 \rho \delta_l^2}{6\omega_2 \omega_3^2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2} + (3\omega_2^2 - 2\omega_2^2 \omega_3 - 6\omega_2 + 9\omega_2 \omega_3 - 6\omega_3) \frac{v_1 \rho \delta_l^2}{6\omega_2^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2} + \\
& C_3 \frac{v_2 \delta_l^3}{2\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (6\omega_2^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + (-12cs^2 \omega_5 - 12cs^2 \omega_2 + 6cs^2 \omega_2^2 + \\
& 12v_1^2 \omega_2 - 3cs^2 \omega_5 \omega_2^2 + 6v_1^2 \omega_5 \omega_2 - 12v_1^2 \omega_5 + v_1^2 \omega_5 \omega_2^2 + 18cs^2 \omega_5 \omega_2 - 6v_1^2 \omega_2^2) \frac{\rho \delta_l^3}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} +
\end{aligned}$$

$$\begin{aligned}
& (12 + \omega_3^2 - 12\omega_3) \frac{v_2 \rho \delta_l^2}{6\omega_3^2} \frac{\partial^3 v_2}{\partial t \partial x_2^2} + C_4 \frac{v_1 \delta_l^3}{2\omega_2^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (6v_2^2 \omega_6 \omega_3 + 6cs^2 \omega_3^2 - 12cs^2 \omega_3 - 12v_2^2 \omega_6 + v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3 - 3cs^2 \omega_6 \omega_3^2 - 12cs^2 \omega_6 + 18cs^2 \omega_6 \omega_3 - 6v_2^2 \omega_3^2) \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} \\
& + (6\omega_2^2 + \omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_2 \delta_l^3}{6\omega_6 \omega_3 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (12 - 12\omega_4 + \omega_4^2) \frac{\rho \delta_l \delta_t}{12\omega_4^2} \frac{\partial^3 v_3}{\partial t^2 \partial x_3} + (-6\omega_4 + 9\omega_4 \omega_2 - 6\omega_2 - 2\omega_4^2 \omega_2 + 3\omega_4^2) \frac{v_3 \rho \delta_l^2}{6\omega_4^2 \omega_2} \frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3} + \\
& (3\omega_2^2 - 2\omega_4 \omega_2^2 - 6\omega_4 + 9\omega_4 \omega_2 - 6\omega_2) \frac{v_1 \rho \delta_l^2}{6\omega_4 \omega_2^2} \frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3} + C_7 \frac{v_3 \delta_l^3}{2\omega_4^2 \omega_5 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\
& (6\omega_2^2 - 6\omega_4 \omega_2^2 - 6\omega_4^2 \omega_2 + 6\omega_4^2 + \omega_4^2 \omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\omega_2^2 \omega_5^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + (-12cs^2 \omega_5 - 12cs^2 \omega_2 + 6cs^2 \omega_2^2 + 12v_1^2 \omega_2 - 3cs^2 \omega_5 \omega_2^2 + \\
& 6v_1^2 \omega_5 \omega_2 - 12v_1^2 \omega_5 + v_1^2 \omega_5 \omega_2^2 + 18cs^2 \omega_5 \omega_2 - 6v_1^2 \omega_2^2) \frac{\rho \delta_l^3}{12\omega_5 \omega_2^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (9\omega_4 \omega_3 - 6\omega_4 - 6\omega_3 + 3\omega_4^2 - 2\omega_4^2 \omega_3) \frac{v_3 \rho \delta_l^2}{6\omega_4^2 \omega_3} \frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3} + (9\omega_4 \omega_3 - 6\omega_4 + 3\omega_3^2 - 2\omega_4 \omega_3^2 - 6\omega_3) \frac{v_2 \rho \delta_l^2}{6\omega_4 \omega_3^2} \frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3} + \\
& (\omega_4 \omega_2 \omega_3^2 + \omega_2^2 \omega_3^2 + \omega_4^2 \omega_2^2 \omega_3^2 - 2\omega_4^2 \omega_2^2 \omega_3 + \omega_4^2 \omega_3^2 + \omega_4 \omega_2^2 \omega_3 + \omega_4^2 \omega_2 \omega_3 - 2\omega_4^2 \omega_2 \omega_3^2 - 2\omega_4 \omega_2^2 \omega_3^2 + \omega_4^2 \omega_2^2) \frac{2v_3 v_2 v_1 \delta_l^3}{\omega_4^2 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} \\
& + (6\omega_4 \omega_3 + 3\omega_3^2 - 6\omega_4 \omega_3^2 + 2\omega_4^2 \omega_3^2 + 3\omega_4^2 - 6\omega_4^2 \omega_3) \frac{v_3 v_2 \rho \delta_l^3}{3\omega_4^2 \omega_3^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (3\omega_2^2 - 6\omega_4 \omega_2^2 + 6\omega_4 \omega_2 - 6\omega_4^2 \omega_2 + 3\omega_4^2 + 2\omega_4^2 \omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{3\omega_4^2 \omega_2^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (3\omega_2^2 + 2\omega_2^2 \omega_3^2 - 6\omega_2^2 \omega_3 + 3\omega_3^2 + 6\omega_2 \omega_3 - 6\omega_2 \omega_3^2) \frac{v_2 v_1 \rho \delta_l^3}{3\omega_2^2 \omega_3^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3 \delta_l^3}{2\omega_4^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& (6\omega_3^2 - 6\omega_4 \omega_3^2 + \omega_4^2 \omega_3^2 + 6\omega_4^2 - 6\omega_4^2 \omega_3) \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^2 \omega_3^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\
& (6v_2^2 \omega_6 \omega_3 + 6cs^2 \omega_3^2 - 12cs^2 \omega_3 - 12v_2^2 \omega_6 + v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3 - 3cs^2 \omega_6 \omega_3^2 - 12cs^2 \omega_6 + 18cs^2 \omega_6 \omega_3 - 6v_2^2 \omega_3^2) \frac{\rho \delta_l^3}{12\omega_6 \omega_3^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} \\
& + (12 - 12\omega_4 + \omega_4^2) \frac{v_3 \rho \delta_l^2}{6\omega_4^2} \frac{\partial^3 v_3}{\partial t \partial x_3^2} + C_9 \frac{v_1 \delta_l^3}{2\omega_7 \omega_4^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (6\omega_4^2 cs^2 + \omega_7 \omega_4^2 v_3^2 - 3\omega_7 \omega_4^2 cs^2 - 6\omega_4^2 v_3^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_4 cs^2 + 12\omega_4 v_3^2 + 18\omega_7 \omega_4 cs^2 - 12\omega_7 v_3^2 - 12\omega_7 cs^2) \frac{\rho \delta_l^3}{12\omega_7 \omega_4^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} \\
& + (6\omega_2^2 - 6\omega_4 \omega_2^2 - 6\omega_4^2 \omega_2 + 6\omega_4^2 + \omega_4^2 \omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^2 \omega_2^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{v_2 \delta_l^3}{2\omega_7 \omega_4^2 \omega_2^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\
& (6\omega_4^2 cs^2 + \omega_7 \omega_4^2 v_3^2 - 3\omega_7 \omega_4^2 cs^2 - 6\omega_4^2 v_3^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_4 cs^2 + 12\omega_4 v_3^2 + 18\omega_7 \omega_4 cs^2 - 12\omega_7 v_3^2 - 12\omega_7 cs^2) \frac{\rho \delta_l^3}{12\omega_7 \omega_4^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + (6\omega_3^2 - 6\omega_4 \omega_3^2 + \omega_4^2 \omega_3^2 + 6\omega_4^2 - 6\omega_4^2 \omega_3) \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^2 \omega_3^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3 \delta_l^3}{6\omega_7 \omega_4 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\rho \delta_l^3}{12\omega_7 \omega_4^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (-2 - \omega_2^2 + 3\omega_2) \frac{\rho \delta_l \delta_t^2}{2\omega_2^2} \frac{\partial^4 v_1}{\partial t^3 \partial x_1} + (-2 - \omega_2^2 + 3\omega_2) \frac{3v_1 \rho \delta_l^2 \delta_t}{2\omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1^2} + C_{13} \frac{\rho \delta_l^3}{12\omega_5^2 \omega_2^2} \frac{\partial^4 v_1}{\partial t \partial x_1^3} + C_{14} \frac{\delta_l^4}{24\omega_5^2 \omega_2^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& C_{15} \frac{v_1 \rho \delta_l^4}{12\omega_5^2 \omega_2^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (-2 - \omega_3^2 + 3\omega_3) \frac{\rho \delta_l \delta_t^2}{2\omega_3^2} \frac{\partial^4 v_2}{\partial t^3 \partial x_2} + \\
& (12\omega_2^2 + 13\omega_2^2 \omega_3^2 - \omega_2^2 \omega_3^3 - 6\omega_3^3 - 24\omega_2^2 \omega_3 + 12\omega_3^2 + 12\omega_2 \omega_3 + 7\omega_2 \omega_3^3 - 24\omega_2 \omega_3^2) \frac{v_2 \rho \delta_l^2 \delta_t}{12\omega_2^2 \omega_3^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2} + \\
& (12\omega_2^2 + 13\omega_2^2 \omega_3^2 - 6\omega_3^2 + 7\omega_2^2 \omega_3 - \omega_2^2 \omega_3^2 - 24\omega_2^2 \omega_3 + 12\omega_3^2 + 12\omega_2 \omega_3 - 24\omega_2 \omega_3^2) \frac{v_1 \rho \delta_l^2 \delta_t}{12\omega_2^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2} + \\
& (6\omega_2^2 \omega_3^2 - 6\omega_3^2 + 12\omega_2^2 \omega_3 - 7\omega_2^2 \omega_3^3 - 7\omega_2^2 \omega_3^2 - 12\omega_3^3 - 6\omega_2^2 \omega_3 + \omega_2^2 \omega_3^3 + 18\omega_2 \omega_3^3) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_2^2 \omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2} + \\
& C_{16} \frac{\rho \delta_l^3}{12\omega_5^2 \omega_2^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2} + C_{17} \frac{v_2 v_1 \rho \delta_l^4}{6\omega_2^2 \omega_3^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{18} \frac{v_2 \rho \delta_l^4}{12\omega_2^2 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_1 \rho \delta_l^4}{12\omega_2^2 \omega_2^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 - \omega_3^2 + 3\omega_3) \frac{3v_2 \rho \delta_l^2 \delta_t}{2\omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2^2} + C_{20} \frac{\rho \delta_l^3}{12\omega_2 \omega_6 \omega_3^2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2} + \\
& (6\omega_2^2 \omega_3^2 - 12\omega_3^2 + 18\omega_2^2 \omega_3 - 7\omega_2^2 \omega_3^3 - 7\omega_2^2 \omega_3^2 - 6\omega_3^3 + \omega_2^2 \omega_3^3 + 12\omega_2 \omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_2 v_1 \rho \delta_l^3}{6\omega_2^2 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2^2} + \\
& C_{21} \frac{\delta_l^4}{4\omega_2^2 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_1 \rho \delta_l^4}{12\omega_2^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{v_2 \rho \delta_l^4}{12\omega_2^2 \omega_2^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{24} \frac{\rho \delta_l^3}{12\omega_6^2 \omega_3^2} \frac{\partial^4 v_2}{\partial t \partial x_2^2} + \\
& C_{25} \frac{v_2 v_1 \rho \delta_l^4}{6\omega_2^2 \omega_6 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{26} \frac{v_2 \rho \delta_l^4}{12\omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{27} \frac{v_1 \rho \delta_l^4}{12\omega_2^2 \omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{28} \frac{\delta_l^4}{24\omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{29} \frac{v_2 \rho \delta_l^4}{12\omega_6^2 \omega_3^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-2 + 3\omega_4 - \omega_4^2) \frac{\rho \delta_l \delta_t^2}{2\omega_4^2} \frac{\partial^4 v_3}{\partial t^3 \partial x_3} + \\
& (12\omega_2^2 - 24\omega_4 \omega_2^2 + 12\omega_4 \omega_2 - 24\omega_4^2 \omega_2 - \omega_4^3 \omega_2^2 + 12\omega_4^2 + 7\omega_4^3 \omega_2 - 6\omega_4^3 + 13\omega_4^2 \omega_2^2) \frac{v_3 \rho \delta_l^2 \delta_t}{12\omega_4^2 \omega_2^2} \frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3} + \\
& (12\omega_2^2 - 24\omega_4 \omega_2^2 - 6\omega_2^2 + 7\omega_4 \omega_2^3 + 12\omega_4 \omega_2 - 24\omega_4^2 \omega_2 + 12\omega_4^2 - \omega_4^2 \omega_2^3 + 13\omega_4^2 \omega_2^2) \frac{v_1 \rho \delta_l^2 \delta_t}{12\omega_4^2 \omega_2^2} \frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-6\omega_4\omega_2^2 - 6\omega_2^3 + 12\omega_4\omega_2^2 + \omega_4^3\omega_2^3 - 7\omega_4^3\omega_2^2 - 7\omega_4^2\omega_2^3 + 18\omega_4^3\omega_2 - 12\omega_4^3 + 6\omega_4^2\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^3 \omega_2^3} \frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3} + \\
& C_{30} \frac{\rho \delta_l^3}{12\omega_4 \omega_5^2 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3} + C_{31} \frac{v_3 v_1 \delta_l^4}{6\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{32} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{33} \frac{v_1 \rho \delta_l^4}{12\omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4\omega_3^2 + 13\omega_4^2\omega_3^2 + 7\omega_4^3\omega_3 + 12\omega_4^2 - \omega_4^3\omega_3^2 - 24\omega_4^2\omega_3 - 6\omega_4^3) \frac{v_3 \rho \delta_l^3 \delta_t}{12\omega_4^3 \omega_3^2} \frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3} + \\
& (12\omega_4\omega_3 - 6\omega_3^3 + 7\omega_4\omega_3^3 + 12\omega_3^2 - 24\omega_4\omega_3^2 + 13\omega_4^2\omega_3^2 - \omega_4^2\omega_3^3 + 12\omega_4^2 - 24\omega_4^2\omega_3) \frac{v_2 \rho \delta_l^3 \delta_t}{12\omega_4^3 \omega_3^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^3 \omega_2^3 \omega_3^3} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{35} \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^3 \omega_2^3 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{36} \frac{v_2 v_1 \rho \delta_l^3}{6\omega_4 \omega_2^3 \omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_2 \partial x_3} + C_{37} \frac{v_3 v_2 \delta_l^4}{\omega_4^3 \omega_5^2 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_4^3 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{40} \frac{v_2 \rho \delta_l^4}{12\omega_5^2 \omega_2^3 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& (-6\omega_3^3 + 12\omega_4\omega_3^3 - 6\omega_4\omega_3^2 + 6\omega_4^2\omega_3^2 + 18\omega_4^2\omega_3 - 7\omega_4^2\omega_3^2 - 7\omega_4^3\omega_3^2 - 12\omega_4^3 + \omega_4^3\omega_3^3) \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^3 \omega_3^3} \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{41} \frac{\rho \delta_l^3}{12\omega_4 \omega_6^2 \omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + C_{42} \frac{v_3 v_1 \delta_l^4}{\omega_4^3 \omega_5^2 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{44} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_4^3 \omega_5^2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{45} \frac{v_1 \rho \delta_l^4}{12\omega_5^2 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{46} \frac{v_3 v_2 \delta_l^4}{6\omega_4^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{47} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{48} \frac{v_2 v_2 \delta_l^4}{12\omega_6^2 \omega_3^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + 3\omega_4 - \omega_4^2) \frac{3v_3 \rho \delta_l^3 \delta_t}{2\omega_4^3} \frac{\partial^4 v_3}{\partial t^2 \partial x_3^2} + C_{49} \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3 \omega_2} \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + \\
& (-12\omega_2^3 + 18\omega_4\omega_2^2 + \omega_4^3\omega_2^2 - 6\omega_4^2\omega_2 - 7\omega_4^3\omega_2^2 - 7\omega_4^2\omega_2^2 + 12\omega_4^2\omega_2 - 6\omega_4^3 + 6\omega_4^2\omega_2^2) \frac{v_3 v_1 \rho \delta_l^3}{6\omega_4^3 \omega_2^3} \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + \\
& C_{50} \frac{\delta_l^4}{4\omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{51} \frac{v_1 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{52} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{53} \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3 \omega_5^2} \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
& (-12\omega_3^3 + 18\omega_4\omega_3^3 + 6\omega_4^2\omega_3^2 + 12\omega_4^2\omega_3 - 7\omega_4^2\omega_3^2 - 7\omega_4^3\omega_3^2 - 6\omega_4^2\omega_3 - 6\omega_4^3 + \omega_4^3\omega_3^3) \frac{v_3 v_2 \rho \delta_l^3}{6\omega_4^3 \omega_3^3} \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + \\
& C_{54} \frac{v_2 v_1 \delta_l^4}{\omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{55} \frac{v_2 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{56} \frac{v_1 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{57} \frac{v_3 v_2 v_1 \rho \delta_l^4}{6\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{58} \frac{\delta_l^4}{4\omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{59} \frac{v_2 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{60} \frac{v_3 \rho \delta_l^4}{12\omega_4^3 \omega_5^2 \omega_2^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{61} \frac{\rho \delta_l^3}{12\omega_7^2 \omega_4^3} \frac{\partial^4 v_3}{\partial t \partial x_3^2} + \\
& C_{62} \frac{v_3 v_1 \delta_l^4}{6\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + C_{63} \frac{v_3 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{64} \frac{v_1 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^2} + C_{65} \frac{v_3 v_2 \delta_l^4}{6\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^2} + \\
& C_{66} \frac{v_3 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^2} + C_{67} \frac{v_2 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \omega_5^2 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^2} + C_{68} \frac{\delta_l^4}{24\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^2} + C_{69} \frac{v_3 \rho \delta_l^4}{12\omega_7^2 \omega_4^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^2} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 + 9cs^2\omega_5 + 9cs^2\omega_2 - 6v_1^2 - 3\omega_5 - 3\omega_2 + 3v_1^2\omega_2 - 18cs^2 + \omega_5\omega_2 - v_1^2\omega_5\omega_2 + 3v_1^2\omega_5 - 3cs^2\omega_5\omega_2 \\
C_2 &= -6\omega_2^2 - 12cs^2\omega_5 - 12cs^2\omega_2 + 6cs^2\omega_2^2 + 12\omega_2 - 36v_1^2\omega_2 - 3cs^2\omega_5\omega_2^2 - 6\omega_5\omega_2 + 6v_1^2\omega_5\omega_2 + 12v_1^2\omega_5 - 5v_1^2\omega_5\omega_2^2 + 18cs^2\omega_5\omega_2 + 2\omega_5\omega_2^2 + 18v_1^2\omega_2^2 \\
C_3 &= -3v_1^2\omega_5\omega_2^2\omega_3 + 4cs^2\omega_5\omega_2\omega_3^2 - v_1^2\omega_2^2\omega_3^2 + cs^2\omega_2^2\omega_3^2 - 2cs^2\omega_5\omega_2\omega_3 + v_1^2\omega_5\omega_2^2\omega_3^2 - 2v_1^2\omega_5\omega_2\omega_3^2 - 2cs^2\omega_2\omega_3^2 + cs^2\omega_5\omega_2^2\omega_3 + 2v_1^2\omega_2\omega_3^2 + 2v_1^2\omega_5\omega_2^2 - cs^2\omega_5\omega_2^2\omega_3^2 + 2v_1^2\omega_5\omega_2\omega_3 - 2cs^2\omega_5\omega_3^2 \\
C_4 &= -cs^2\omega_2^2\omega_6\omega_3^2 - 2cs^2\omega_2^2\omega_3 + 2v_2^2\omega_2\omega_6\omega_3 - 3v_2^2\omega_2\omega_6\omega_3^2 + cs^2\omega_2^2\omega_3^2 + 4cs^2\omega_2^2\omega_6\omega_3 + 2v_2^2\omega_6\omega_3^2 + v_2^2\omega_2^2\omega_6\omega_3^2 - v_2^2\omega_2^2\omega_3^2 - 2cs^2\omega_2\omega_6\omega_3 + cs^2\omega_2\omega_6\omega_3^2 + 2v_2^2\omega_2^2\omega_3 - 2cs^2\omega_2^2\omega_6 - 2v_2^2\omega_2^2\omega_6\omega_3 \\
C_5 &= 6 - v_2^2\omega_6\omega_3 + 9cs^2\omega_3 + 3v_2^2\omega_6 - 6v_2^2 - 18cs^2 + 3v_2^2\omega_3 - 3\omega_6 + 9cs^2\omega_6 + \omega_6\omega_3 - 3\omega_3 - 3cs^2\omega_6\omega_3 \\
C_6 &= 6v_2^2\omega_6\omega_3 + 6cs^2\omega_3^2 - 12cs^2\omega_3 + 12v_2^2\omega_6 - 6\omega_3^2 - 5v_2^2\omega_6\omega_3^2 - 36v_2^2\omega_3 - 3cs^2\omega_6\omega_3^2 - 12cs^2\omega_6 - 6\omega_6\omega_3 + 12\omega_3 + 18cs^2\omega_6\omega_3 + 2\omega_6\omega_3^2 + 18v_2^2\omega_3^2 \\
C_7 &= -2\omega_4cs^2\omega_5\omega_2 - 2\omega_4^2cs^2\omega_2 - 2\omega_4^2cs^2\omega_5 - 3\omega_4v_1^2\omega_5\omega_2^2 + 2\omega_4v_1^2\omega_5\omega_2 + \omega_4^2cs^2\omega_2^2 + \omega_4cs^2\omega_5\omega_2^2 + 4\omega_4^2cs^2\omega_5\omega_2 + \omega_4^2v_1^2\omega_5\omega_2^2 + 2\omega_4^2v_1^2\omega_2 - \omega_4^2v_1^2\omega_2^2 + 2v_1^2\omega_5\omega_2^2 - 2\omega_4^2v_1^2\omega_5\omega_2 - \omega_4^2cs^2\omega_5\omega_2^2 \\
C_8 &= \omega_4^2v_2^2\omega_6\omega_3^2 + \omega_4^2cs^2\omega_3^2 - 2\omega_4cs^2\omega_6\omega_3 + \omega_4cs^2\omega_6\omega_3^2 - 2\omega_4^2v_2^2\omega_6\omega_3 - 2\omega_4^2cs^2\omega_3 + 2v_2^2\omega_6\omega_3^2 - 2\omega_4^2cs^2\omega_6 + 2\omega_4^2v_2^2\omega_3 - 3\omega_4v_2^2\omega_6\omega_3^2 + 4\omega_4^2cs^2\omega_6\omega_3 - \omega_4^2cs^2\omega_6\omega_3^2 + 2\omega_4v_2^2\omega_6\omega_3 - \omega_4^2v_2^2\omega_3^2 \\
C_9 &= -3\omega_7\omega_4^2v_3^2\omega_2 + \omega_7\omega_4^2cs^2\omega_2 - 2\omega_7cs^2\omega_2^2 - \omega_4^2v_3^2\omega_2^2 - \omega_7\omega_4^2cs^2\omega_2^2 + \omega_7\omega_4^2v_3^2\omega_2^2 + 2\omega_7\omega_4^2v_3^2 + \omega_4^2cs^2\omega_2^2 + 4\omega_7\omega_4cs^2\omega_2^2 + 2\omega_4v_3^2\omega_2^2 - 2\omega_4cs^2\omega_2^2 - 2\omega_7\omega_4v_3^2\omega_2^2 + 2\omega_7\omega_4v_3^2\omega_2 - 2\omega_7\omega_4cs^2\omega_2 \\
C_{10} &= \omega_7\omega_4^2v_3^2\omega_3^2 + \omega_4^2cs^2\omega_3^2 - 2\omega_7cs^2\omega_3^2 - \omega_4^2v_3^2\omega_3^2 - \omega_7\omega_4^2cs^2\omega_3^2 + \omega_7\omega_4^2cs^2\omega_3 + 2\omega_7\omega_4^2v_3^2 - 3\omega_7\omega_4^2v_3^2\omega_3 - 2\omega_7\omega_4cs^2\omega_3 + 2\omega_7\omega_4v_3^2\omega_3 - 2\omega_4cs^2\omega_3^2 - 2\omega_7\omega_4v_3^2\omega_3^2 + 4\omega_7\omega_4cs^2\omega_3^2 + 2\omega_4v_3^2\omega_3^2 \\
C_{11} &= 6 - 3\omega_7 - 3\omega_4 - \omega_7\omega_4v_3^2 + 9\omega_4cs^2 - 6v_3^2 + 3\omega_4v_3^2 - 18cs^2 - 3\omega_7\omega_4cs^2 + \omega_7\omega_4 + 3\omega_7v_3^2 + 9\omega_7cs^2 \\
C_{12} &= 12\omega_4 + 6\omega_4^2cs^2 - 5\omega_7\omega_4^2v_3^2 - 3\omega_7\omega_4^2cs^2 + 18\omega_4^2v_3^2 + 6\omega_7\omega_4v_3^2 - 12\omega_4cs^2 - 36\omega_4v_3^2 + 18\omega_7\omega_4cs^2 + 2\omega_7\omega_4^2 - 6\omega_4^2 - 6\omega_7\omega_4 + 12\omega_7v_3^2 - 12\omega_7cs^2
\end{aligned}$$

$$C_{13} = -11\omega_2^2\omega_2^2 - 12\omega_2^2 - 48cs^2\omega_5^2\omega_2 - 3v_1^2\omega_5^2\omega_2^3 + 6\omega_2^3 + \omega_5^2\omega_2^3 + 15v_1^2\omega_2^2\omega_2^2 + 18v_1^2\omega_2^2\omega_2 + 12cs^2\omega_2^2 - 2cs^2\omega_5^2\omega_2^3 + 24cs^2\omega_2^2 + 12\omega_2^3\omega_2 + 25cs^2\omega_5^2\omega_2^2 - 6cs^2\omega_2^2 - 36cs^2\omega_5\omega_2^2 - 24\omega_5\omega_2 + 72v_1^2\omega_5\omega_2 + 9cs^2\omega_5\omega_2^2 - 9\omega_5\omega_2^2 - 36v_1^2\omega_2^2 - 108v_1^2\omega_5\omega_2^2 - 18v_1^2\omega_2^2 + 24cs^2\omega_5\omega_2 + 36\omega_5\omega_2^2 + 36v_1^2\omega_2^2 + 27v_1^2\omega_5\omega_2^2$$

$$C_{14} = 12cs^2\omega_5^2\omega_2 - 3cs^4\omega_5^2\omega_2^3 - 72cs^2v_1^2\omega_5\omega_2^3 - 3v_1^2\omega_5^2\omega_2^2 + 12v_1^2\omega_5^2\omega_2^2 + 24cs^4\omega_5^2\omega_2^2 + 144cs^2v_1^2\omega_5\omega_2^2 + 72cs^2v_1^2\omega_5\omega_2 - 48cs^4\omega_5^2\omega_2 + cs^2\omega_5^2\omega_2^3 - 72v_1^4\omega_2^2 + 3v_1^4\omega_5^2\omega_2^3 - 12v_1^4\omega_5^2\omega_2^2 + 36v_1^4\omega_2^3 - 8cs^2\omega_5^2\omega_2^2 - 216cs^2v_1^2\omega_2^2 + 72v_1^4\omega_5\omega_2^2 + 24cs^2\omega_5\omega_2^2 + 24cs^4\omega_5\omega_2 + 108cs^2v_1^2\omega_2^2 - 36cs^2v_1^2\omega_5^2\omega_2 - 6cs^2\omega_5\omega_2^2 - 30v_1^4\omega_5\omega_2^2 + 24cs^4\omega_5^2 - 72v_1^2\omega_5\omega_2^2 - 36v_1^2\omega_2^2 - 12cs^2v_1^2\omega_5^2\omega_2^2 - 24cs^4\omega_5\omega_2^2 - 24cs^2\omega_5\omega_2 + 6cs^2v_1^2\omega_5^2\omega_2^2 + 6cs^4\omega_5\omega_2^2 + 72v_1^2\omega_2^2 + 30v_1^2\omega_5\omega_2^2$$

$$C_{15} = 2\omega_5^2\omega_2^2 + 36\omega_2^2 - 30cs^2\omega_5^2\omega_2 + 2v_1^2\omega_5^2\omega_2^3 - 18\omega_2^3 - \omega_5^2\omega_2^3 + 2v_1^2\omega_5^2\omega_2^2 - 12v_1^2\omega_5^2\omega_2 - 60cs^2\omega_2^2 + cs^2\omega_5^2\omega_2^3 + 24cs^2\omega_5^2 + 6\omega_5^2\omega_2 - 2cs^2\omega_5^2\omega_2^2 + 30cs^2\omega_2^2 + 72cs^2\omega_5\omega_2^2 - 12\omega_5\omega_2 + 60v_1^2\omega_5\omega_2 - 24cs^2\omega_5\omega_2^2 + 12\omega_5\omega_2^2 - 12v_1^2\omega_5^2 + 24v_1^2\omega_5\omega_2^2 + 42v_1^2\omega_2^2 - 12cs^2\omega_5\omega_2 - 24\omega_5\omega_2^2 - 84v_1^2\omega_2^2 - 24v_1^2\omega_5\omega_2^2$$

$$C_{16} = 6v_1^2\omega_2^3\omega_3 + 12cs^2\omega_5^2\omega_2 - v_1^2\omega_5^2\omega_2^3 + 30v_1^2\omega_5\omega_2^3\omega_3 - 2cs^2\omega_5^2\omega_2^3\omega_3 + 12cs^2\omega_2^3\omega_3 + 24v_1^2\omega_5^2\omega_3 - 36v_1^2\omega_2^3\omega_2\omega_3 - 6v_1^2\omega_2^3\omega_2^2 - 6cs^2\omega_2^3\omega_3 + 12v_1^2\omega_5^2\omega_2 + 22cs^2\omega_5^2\omega_2\omega_3 - 9v_1^2\omega_5\omega_2^3\omega_3 + 3cs^2\omega_5^2\omega_2^3 - 12v_1^2\omega_2^3\omega_3 + 12cs^2\omega_5^2\omega_3 + 12cs^2\omega_5\omega_2\omega_3 - 18cs^2\omega_5^2\omega_2^2 - 30cs^2\omega_5\omega_2^2\omega_3 + v_1^2\omega_5^2\omega_2^3\omega_3 + 12cs^2\omega_5\omega_2^2 - 30cs^2\omega_5^2\omega_2\omega_3 - 6cs^2\omega_5\omega_2^2 + 8v_1^2\omega_2^3\omega_2\omega_3 - 12v_1^2\omega_5\omega_2^2 + 9cs^2\omega_5\omega_2^3\omega_3 - 12v_1^2\omega_5\omega_2\omega_3 + 6v_1^2\omega_5\omega_2^3$$

$$C_{17} = 12v_1^2\omega_2^3\omega_3^3 + 6\omega_5\omega_2^3\omega_3^3 - 6\omega_2^3\omega_2\omega_3^3 - 36cs^2\omega_2^3\omega_2^3\omega_3^3 + 6v_1^2\omega_5^2\omega_3^3 + 18cs^2\omega_2^3\omega_3^3 + 6cs^2\omega_5^2\omega_3^3\omega_3 - 24cs^2\omega_5\omega_2\omega_3^3 + 6\omega_2^3\omega_3^3 + 36cs^2\omega_5^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_3^3 - 21\omega_5\omega_2^3\omega_3^3 - 36cs^2\omega_2^3\omega_3^3 + 12v_1^2\omega_5\omega_2^3\omega_3^3 + 6cs^2\omega_5^2\omega_3^3\omega_3^3 - 12cs^2\omega_2^3\omega_2\omega_3^3 - 3\omega_5\omega_2^3\omega_3^3 - 6v_1^2\omega_2^3\omega_3^3 + 6\omega_5\omega_2^3\omega_3^3 + 12v_1^2\omega_5\omega_2\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^3 - 3\omega_2^3\omega_3^3 + \omega_5^2\omega_2^3\omega_3^3 - 12v_1^2\omega_5^2\omega_2^3\omega_3 - 6v_1^2\omega_5^2\omega_2^3\omega_3 - 24cs^2\omega_5\omega_2^3\omega_3^3 + 12cs^2\omega_5\omega_2^3\omega_3^3 - 6v_1^2\omega_5^2\omega_2^3\omega_3^3 - 24v_1^2\omega_5\omega_2\omega_3^3 - \omega_5^2\omega_2^3\omega_3^3 + 6v_1^2\omega_5^2\omega_2^3\omega_3 - 12cs^2\omega_5^2\omega_2\omega_3^3 + 72cs^2\omega_5\omega_2^3\omega_3 + 12\omega_5\omega_2\omega_3^3 - 3\omega_2^3\omega_2^3\omega_3^3 + 7\omega_5^2\omega_2^3\omega_3^3 + 6v_1^2\omega_5^2\omega_2^3\omega_3^3 - 24cs^2\omega_5\omega_2^3\omega_3^3 + 36cs^2\omega_5^2\omega_2\omega_3^3$$

$$C_{18} = 12v_1^2\omega_2^3\omega_3^3 + 12\omega_5\omega_2^3\omega_3^3 - 32cs^2\omega_5^2\omega_2^3\omega_3^3 + 12v_1^2\omega_5^2\omega_2^3 + 6cs^2\omega_2^3\omega_3^3 + 6cs^2\omega_5^2\omega_2^3\omega_3 - 12cs^2\omega_5\omega_2\omega_3^3 + 12v_1^2\omega_5\omega_2^3\omega_3^3 + 48cs^2\omega_2^3\omega_2^3\omega_3^3 - 12cs^2\omega_2^3\omega_3^3 - 6\omega_5\omega_2^3\omega_3^3 - 12cs^2\omega_2^3\omega_3^3 - 12v_1^2\omega_5\omega_2^3\omega_3^3 + 4cs^2\omega_2^3\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3 - 6\omega_5\omega_2^3\omega_3^3 - 6v_1^2\omega_2^3\omega_3^3 + 3\omega_5\omega_2^3\omega_3^3 + 30v_1^2\omega_5^2\omega_2\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^3 - 24v_1^2\omega_5\omega_2^3\omega_3^3 - 24v_1^2\omega_5^2\omega_3^3 + 2\omega_2^3\omega_2^3\omega_3^3 - 18v_1^2\omega_2^3\omega_2\omega_3^3 - 12v_1^2\omega_2^3\omega_2^3\omega_3^3 - 12cs^2\omega_5\omega_2^3\omega_3^3 + 12cs^2\omega_5\omega_2^3\omega_3^3 + 12v_1^2\omega_5^2\omega_2^3\omega_3^3 + 12v_1^2\omega_5\omega_2\omega_3^3 - \omega_5^2\omega_2^3\omega_3^3 - 24cs^2\omega_5^2\omega_2\omega_3^3 + 36cs^2\omega_5\omega_2^3\omega_3^3 + 3v_1^2\omega_5^2\omega_2^3\omega_3^3 - 6\omega_5^2\omega_2^3\omega_3^3 + 3\omega_5^2\omega_2^3\omega_3^3 - 24cs^2\omega_5\omega_2^3\omega_3^3 + 36cs^2\omega_5^2\omega_2\omega_3^3$$

$$C_{19} = 11\omega_2^3\omega_2^2 + 12\omega_2^2 + 18cs^2\omega_5^2\omega_2 + v_1^2\omega_5^2\omega_2^3 - 6\omega_2^3 - \omega_5^2\omega_2^3 - 14v_1^2\omega_5^2\omega_2^2 + 12v_1^2\omega_5^2\omega_2 - 60cs^2\omega_2^2 + 4cs^2\omega_5^2\omega_2^3 - 12\omega_5^2\omega_2 - 26cs^2\omega_5^2\omega_2^2 + 30cs^2\omega_2^3 + 96cs^2\omega_5\omega_2^2 + 24\omega_5\omega_2 - 60v_1^2\omega_5\omega_2 - 30cs^2\omega_5\omega_2^3 + 9\omega_5\omega_2^3 + 12v_1^2\omega_5^2 + 48v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_2^3 - 36cs^2\omega_5\omega_2 - 36\omega_5\omega_2^2 + 12v_1^2\omega_2^2 - 6v_1^2\omega_5\omega_2^2$$

$$C_{20} = -2cs^2\omega_2\omega_6^3\omega_3^3 + 22cs^2\omega_2\omega_6^2\omega_3^3 + 12cs^2\omega_6^2\omega_3 - 12v_2^2\omega_2\omega_6\omega_3 + 30v_2^2\omega_2\omega_6\omega_3^2 - 12v_2^2\omega_2\omega_3^2 + 6v_2^2\omega_6\omega_3^3 - 30cs^2\omega_2\omega_6^2\omega_3 - 18cs^2\omega_6^2\omega_3^3 + 6v_2^2\omega_2\omega_3^3 - 9v_2^2\omega_2\omega_6\omega_3^3 + 3cs^2\omega_6^2\omega_3^3 + 12cs^2\omega_2\omega_6\omega_3 - 12v_2^2\omega_6\omega_3^3 + v_2^2\omega_2\omega_6^2\omega_3^3 + 12cs^2\omega_2\omega_6\omega_3^2 - 6cs^2\omega_6\omega_3^3 - 6v_2^2\omega_6^2\omega_3^3 - 6cs^2\omega_2\omega_6\omega_3^3 + 8v_2^2\omega_2\omega_6^2\omega_3^3 + 12cs^2\omega_2\omega_6\omega_3 + 24v_2^2\omega_2\omega_6 - v_2^2\omega_6^2\omega_3^3 + 12cs^2\omega_6\omega_3^3 - 30cs^2\omega_2\omega_6\omega_3^2 - 36v_2^2\omega_2\omega_6^2\omega_3 + 12v_2^2\omega_6^2\omega_3 + 9cs^2\omega_2\omega_6\omega_3^3$$

$$C_{21} = 2cs^2v_1^2\omega_5^2\omega_2^3\omega_3^3 - 4cs^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 10cs^2v_2^2\omega_5^2\omega_2\omega_6^2\omega_3^3 + 4v_2^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^2 - 2v_2^2v_1^2\omega_5^2\omega_2^3\omega_3^3 + 2cs^2v_1^2\omega_5^2\omega_2^2\omega_6\omega_3^2 - 14v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 10cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4cs^2v_2^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 4cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 2cs^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 14v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 12v_2^2v_1^2\omega_5^2\omega_2\omega_6^2\omega_3^2 - 4cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 + 14v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 10v_2^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 - 4cs^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 12cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 + cs^4\omega_5\omega_2^3\omega_6\omega_3^2 + 10cs^2v_2^2\omega_5\omega_2^3\omega_6\omega_3^2 - 2cs^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4cs^4\omega_2^3\omega_2^3\omega_6\omega_3^2 - 2cs^4\omega_5\omega_2^3\omega_6\omega_3^2 + 2cs^2v_1^2\omega_5\omega_2^3\omega_6\omega_3^2 - 8cs^2v_1^2\omega_2^3\omega_2^3\omega_6\omega_3^2 - 3v_2^2v_1^2\omega_2^3\omega_2^3\omega_6\omega_3^2 + 4v_2^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 - 4cs^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4cs^2v_2^2\omega_5\omega_2\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4cs^2v_2^2\omega_5\omega_2\omega_6^2\omega_3^2 - 3cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 10v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2cs^4\omega_2^3\omega_2^3\omega_6\omega_3^2 - 4cs^2v_2^2\omega_5\omega_2\omega_6^2\omega_3^2 - 3cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 10v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2cs^4\omega_2^3\omega_2^3\omega_6\omega_3^2 + 2cs^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 3v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 10cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4v_2^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_2^3\omega_2^3\omega_6\omega_3^2 - cs^2v_2^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4cs^2v_2^2\omega_5\omega_2\omega_6^2\omega_3^2 - 4cs^2v_2^2\omega_5\omega_2\omega_6^2\omega_3^2 - 3cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 - 10v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 4cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 2cs^4\omega_2^3\omega_2^3\omega_6\omega_3^2 + 4cs^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + 4cs^4\omega_5\omega_2\omega_6^2\omega_3^2 + 4v_2^2v_1^2\omega_2^3\omega_2^3\omega_6\omega_3^2 - cs^4\omega_2^3\omega_2^3\omega_6\omega_3^2 - 2v_2^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + 14v_2^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 8cs^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 - cs^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + 8cs^2v_2^2\omega_5\omega_2\omega_6^2\omega_3^2 - 2cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2 + 2cs^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 + 3v_2^2v_1^2\omega_5\omega_2\omega_6^2\omega_3^2 - 28v_2^2v_1^2\omega_2^3\omega_2^3\omega_6\omega_3^2 - 2cs^4\omega_5\omega_2\omega_6^2\omega_3^2 + 4cs^4\omega_5^2\omega_2^3\omega_6\omega_3^2 - 4cs^2v_1^2\omega_5^2\omega_2^3\omega_6\omega_3^2$$

$$C_{22} = 6cs^2\omega_2\omega_6^2\omega_3^3 + 24v_2^2\omega_2^3\omega_6^2\omega_3 + 6cs^2\omega_2^3\omega_3^3 + 6v_2^2\omega_2^3\omega_6\omega_3^3 - 12cs^2\omega_2\omega_6^2\omega_3^2 + 24cs^2\omega_2^3\omega_6\omega_3^2 - 24v_2^2\omega_2^3\omega_6^2\omega_3 - 14cs^2\omega_2^3\omega_6^2\omega_3^2 + cs^2\omega_2^3\omega_6^2\omega_3^2 - 30v_2^2\omega_2\omega_6^2\omega_3^2 - 6cs^2\omega_2^3\omega_6\omega_3^3 - 18v_2^2\omega_2^3\omega_6^2\omega_3 + 24v_2^2\omega_2\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2\omega_3^3 + 24cs^2\omega_2^3\omega_6\omega_3^2 - 6cs^2\omega_2^3\omega_6^2\omega_3^2 - 12cs^2\omega_2^3\omega_6^2 - 12cs^2\omega_2^3\omega_6\omega_3 + 22v_2^2\omega_2^3\omega_6^2\omega_3 - 6v_2^2\omega_2^3\omega_3^3 + 12cs^2\omega_2^3\omega_6^2\omega_3 + 12v_2^2\omega_2^3\omega_3^3 - 4v_2^2\omega_2^3\omega_6^2\omega_3^2$$

$$C_{23} = 12v_1^2\omega_2^3\omega_3^3 - 14cs^2\omega_5^2\omega_2^3\omega_3^3 + 6v_1^2\omega_5\omega_2^3\omega_3^3 + 12v_1^2\omega_5^2\omega_3^3 + 6cs^2\omega_2^3\omega_3^3 + 6cs^2\omega_5^2\omega_2^3\omega_3 - 12cs^2\omega_5\omega_2\omega_3^3 + 12cs^2\omega_5^2\omega_2^2\omega_3^2 - 12cs^2\omega_5^2\omega_2^3\omega_3^3 - 12cs^2\omega_2^3\omega_3^3 - 24v_1^2\omega_5\omega_2^3\omega_3^3 + cs^2\omega_5^2\omega_2^3\omega_3^3 + 24v_1^2\omega_5^2\omega_2\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3 - 6v_1^2\omega_2^3\omega_3^3 - 18v_1^2\omega_5^2\omega_2\omega_3^3 - 6cs^2\omega_5^2\omega_2^2\omega_3^2 - 30v_1^2\omega_5^2\omega_2^3\omega_3 + 22v_1^2\omega_5^2\omega_2^3\omega_3^3 - 6cs^2\omega_5\omega_2^3\omega_3^3 - 48v_1^2\omega_5^2\omega_2^3\omega_3 + 12v_1^2\omega_5\omega_2\omega_3^3 + 24v_1^2\omega_5^2\omega_2\omega_3 + 24cs^2\omega_5\omega_2^3\omega_3^3 - 4v_1^2\omega_5^2\omega_2^3\omega_3^3 + 22v_1^2\omega_5^2\omega_2^3\omega_3^3 + 24cs^2\omega_2^3\omega_2\omega_3^3$$

$$C_{24} = \omega_6^2\omega_3^3 + 72v_2^2\omega_6\omega_3 - 6cs^2\omega_3^3 - 11\omega_6^2\omega_3^2 - 36v_2^2\omega_6^2 - 48cs^2\omega_2^3\omega_3 + 12cs^2\omega_2^3\omega_3^2 + 6\omega_3^3 + 27v_2^2\omega_6\omega_3^3 + 12\omega_6^2\omega_3 + 25cs^2\omega_2^3\omega_3^2 - 12\omega_2^3 - 2cs^2\omega_6^2\omega_3^3 - 108v_2^2\omega_6\omega_3^2 + 9cs^2\omega_6\omega_3^3 + 15v_2^2\omega_6^2\omega_3^2 - 3v_2^2\omega_6^2\omega_3^3 - 36cs^2\omega_6\omega_3^3 - 24\omega_6\omega_3 + 24cs^2\omega_6^2 + 24cs^2\omega_6\omega_3 + 36\omega_6\omega_3^2 + 36v_2^2\omega_3^2 - 9\omega_6\omega_3^3 + 18v_2^2\omega_6^2\omega_3 - 18v_2^2\omega_3^3$$

$$C_{25} = -3\omega_2^3\omega_6^2\omega_3^2 + 6cs^2\omega_2\omega_6^2\omega_3^2 - 24cs^2\omega_2^3\omega_6\omega_3^2 + 18cs^2\omega_2^3\omega_3^2 + 12\omega_2^3\omega_6\omega_3^2 + 12cs^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2\omega_6^2\omega_3^2 + 36cs^2\omega_2^3\omega_6^2\omega_3 + \omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3^2 - 36cs^2\omega_2^3\omega_3^2 - 24v_2^2\omega_2^3\omega_6\omega_3 + 6\omega_2^3\omega_3^2 + 6v_2^2\omega_2^3\omega_6^2\omega_3^2 - 21\omega_2^3\omega_6\omega_3^2 - 36cs^2\omega_2^3\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_6^2\omega_3^2 - 3\omega_2^3\omega_3^3 + 6cs^2\omega_2^3\omega_6^2\omega_3^2 + 6\omega_2^3\omega_6\omega_3^2 - 12v_2^2\omega_2\omega_6^2\omega_3^2 - 24cs^2\omega_2^3\omega_6\omega_3^2 - \omega_2^3\omega_6^2\omega_3^2 - 12cs^2\omega_2^3\omega_6^2\omega_3 + 12v_2^2\omega_2^3\omega_6^2\omega_3 + 6v_2^2\omega_2\omega_6^2\omega_3^2 + 7\omega_2^3\omega_6^2\omega_3^2 + 6v_2^2\omega_6^2\omega_3^2 + 72cs^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6^2\omega_3^2 - 6\omega_2^3\omega_6\omega_3^2 - 3\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6^2 - 24cs^2\omega_2^3\omega_6\omega_3 - 6v_2^2\omega_2^3\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^2 + 6\omega_2^3\omega_6\omega_3^2 + 36cs^2\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6^2\omega_3^2$$

$$C_{26} = -\omega_6^2\omega_3^3 - 60v_2^2\omega_6\omega_3 + 30cs^2\omega_3^3 + 11\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2 + 18cs^2\omega_6^2\omega_3 - 60cs^2\omega_2^3\omega_3 - 6\omega_3^3 - 6v_2^2\omega_6\omega_3^3 - 12\omega_6^2\omega_3 - 26cs^2\omega_6^2\omega_3^2 + 12\omega_2^3 + 4cs^2\omega_6^2\omega_3^3 + 48v_2^2\omega_6\omega_3^2 - 30cs^2\omega_6\omega_3^3 - 14v_2^2\omega_6^2\omega_3^2 + v_2^2\omega_6^2\omega_3^3 + 96cs^2\omega_6\omega_3^2 + 24\omega_6\omega_3 - 36cs^2\omega_6\omega_3 - 36\omega_6\omega_3^2 + 12v_2^2\omega_3^2 + 9\omega_6\omega_3^3 + 12v_2^2\omega_6^2\omega_3 - 6v_2^2\omega_3^3$$

$$C_{27} = -6\omega_2^3\omega_6^2\omega_3^2 + 6cs^2\omega_2\omega_6^2\omega_3^2 - 24v_2^2\omega_2^3\omega_6^2 - 24cs^2\omega_2^3\omega_6\omega_3^2 + 6cs^2\omega_2^3\omega_3^2 + 12cs^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2\omega_6^2\omega_3^2 + 36cs^2\omega_2^3\omega_6^2\omega_3 + 2\omega_2^3\omega_6^2\omega_3^2 - 12v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_3^2 + 12v_2^2\omega_2^3\omega_6\omega_3 - 32cs^2\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_6^2\omega_3^2 + 4cs^2\omega_2^3\omega_6^2\omega_3^2 + 3\omega_2^3\omega_6\omega_3^2 - 18v_2^2\omega_2\omega_6^2\omega_3^2 - 24v_2^2\omega_2^3\omega_6\omega_3^2 - 12cs^2\omega_2^3\omega_6\omega_3^2 - \omega_2^3\omega_6^2\omega_3^2 - 24cs^2\omega_2^3\omega_6^2\omega_3 + 30v_2^2\omega_2^3\omega_6^2\omega_3 + 12v_2^2\omega_2^3\omega_6\omega_3^2 + 3\omega_2^3\omega_6^2\omega_3^2 + 12v_2^2\omega_6^2\omega_3^2 + 36cs^2\omega_2^3\omega_6\omega_3^2 -$$

$$12cs^2\omega_2^2\omega_6^3\omega_3^3 - 6\omega_2^2\omega_6\omega_3^3 - 12cs^2\omega_2^3\omega_6^2 - 12cs^2\omega_2^3\omega_6\omega_3 - 12v_2^2\omega_2^3\omega_6^2\omega_3^2 - 6v_2^2\omega_2^3\omega_3^3 + 12\omega_2^2\omega_6\omega_3^2 + 48cs^2\omega_2^2\omega_6^2\omega_3^2 + 12v_2^2\omega_2^3\omega_3^3 + 3v_2^2\omega_2^3\omega_6^2\omega_3^3$$

$$C_{28} = -36cs^2v_2^2\omega_6\omega_3 - 30v_2^4\omega_6\omega_3^3 + 24cs^4\omega_6^2\omega_3^2 + 12cs^2\omega_6^2\omega_3 - 3cs^4\omega_6^2\omega_3^3 + 72v_2^4\omega_6\omega_3^2 + 30v_2^2\omega_6\omega_3^3 + 36v_2^4\omega_3^3 + 6cs^2v_2^2\omega_6^2\omega_3^3 - 8cs^2\omega_6^2\omega_3^2 - 48cs^4\omega_6^2\omega_3 + 24cs^4\omega_6^2 - 12cs^2v_2^2\omega_6^2\omega_3^3 + cs^2\omega_6^2\omega_3^3 - 72v_2^4\omega_3^3 - 72v_2^2\omega_6\omega_3^2 + 108cs^2v_2^2\omega_3^3 + 24cs^4\omega_6\omega_3 - 6cs^2\omega_6\omega_3^3 + 144cs^2v_2^2\omega_6\omega_3^2 + 12v_2^2\omega_6^2\omega_3^3 - 216cs^2v_2^2\omega_3^3 - 3v_2^2\omega_6^2\omega_3^3 + 24cs^2\omega_6\omega_3^2 - 72cs^2v_2^2\omega_6\omega_3^3 - 24cs^2\omega_6\omega_3 + 6cs^4\omega_6\omega_3^3 + 72v_2^2\omega_3^3 - 12v_2^4\omega_6^2\omega_3^2 + 72cs^2v_2^2\omega_6\omega_3 + 3v_2^4\omega_6^2\omega_3^3 - 36v_2^2\omega_3^3 - 24cs^4\omega_6\omega_3^3$$

$$C_{29} = -\omega_6^2\omega_3^3 + 60v_2^2\omega_6\omega_3 + 30cs^2\omega_3^3 + 2\omega_6^2\omega_3^2 - 12v_2^2\omega_6^2 - 30cs^2\omega_6^2\omega_3 - 60cs^2\omega_3^2 - 18\omega_3^3 - 24v_2^2\omega_6\omega_3^3 + 6\omega_6^2\omega_3 - 2cs^2\omega_6^2\omega_3^2 + 36\omega_3^2 + cs^2\omega_6^2\omega_3^3 + 24v_2^2\omega_6\omega_3^2 - 24cs^2\omega_6\omega_3^2 + 2v_2^2\omega_6^2\omega_3^2 + 2v_2^2\omega_6^2\omega_3^3 + 72cs^2\omega_6\omega_3^2 - 12\omega_6\omega_3 + 24cs^2\omega_6^2 - 12cs^2\omega_6\omega_3 - 24\omega_6\omega_3^2 - 84v_2^2\omega_3^2 + 12\omega_6\omega_3^3 - 12v_2^2\omega_6^2\omega_3 + 42v_2^2\omega_3^3$$

$$C_{30} = -12\omega_4v_1^2\omega_5^2 + 12cs^2\omega_5^2\omega_2 + 12\omega_4cs^2\omega_5\omega_2 - 9\omega_4v_1^2\omega_5\omega_2^2 - v_1^2\omega_5^2\omega_2^2 + 6\omega_4v_1^2\omega_5^2 - 6v_1^2\omega_5^2\omega_2^2 + 30\omega_4v_1^2\omega_5\omega_2^2 + 24\omega_4v_1^2\omega_5^2 - 12\omega_4v_1^2\omega_5\omega_2 + 12v_1^2\omega_5^2\omega_2 + 3cs^2\omega_5^2\omega_2^2 + 9\omega_4cs^2\omega_5\omega_2^2 - 30\omega_4cs^2\omega_5\omega_2^2 - 18cs^2\omega_5^2\omega_2^2 - 6\omega_4cs^2\omega_5^2 + 12\omega_4cs^2\omega_5^2 + 22\omega_4cs^2\omega_5^2\omega_2^2 + 12cs^2\omega_5\omega_2^2 - 36\omega_4v_1^2\omega_5^2\omega_2 + 12\omega_4cs^2\omega_2^2 - 6cs^2\omega_5\omega_2^2 - 2\omega_4cs^2\omega_5^2\omega_2^2 - 12v_1^2\omega_5\omega_2^2 + 8\omega_4v_1^2\omega_5^2\omega_2^2 - 30\omega_4cs^2\omega_5^2\omega_2 + \omega_4v_1^2\omega_5^2\omega_2^2 + 6v_1^2\omega_5^2\omega_2^2$$

$$C_{31} = 36\omega_4^3cs^2\omega_5^2\omega_2^2 + 12\omega_4^3\omega_5\omega_2 + 6v_1^2\omega_5^2\omega_2^2 + \omega_4^3\omega_5^2\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 - 6\omega_4^3v_1^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 - 3\omega_4^3\omega_5^2\omega_2^2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2 - 6\omega_4^3v_1^2\omega_5^2\omega_2^2 + 6\omega_4^3\omega_5\omega_2^2 + 3\omega_4^3v_1^2\omega_2^2 + 12\omega_4^3v_1^2\omega_5^2\omega_2 - 6\omega_4^3\omega_5\omega_2^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^3cs^2\omega_5^2\omega_2 + 12\omega_4^3v_1^2\omega_2^2 + 7\omega_4^3\omega_5^2\omega_2^2 - 3\omega_4^3\omega_2^2 + 72\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^3cs^2\omega_5\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 + 6\omega_4^3\omega_2^2 - 24\omega_4^3v_1^2\omega_5\omega_2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2^2 + 12\omega_4^3cs^2\omega_5\omega_2^2 + 6\omega_4^3\omega_5\omega_2^2 + 6\omega_4^3v_1^2\omega_5^2\omega_2^2 - 36\omega_4^3cs^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2 - 24\omega_4^3cs^2\omega_5\omega_2^2 - 6\omega_4^3\omega_5\omega_2 + 18\omega_4^3cs^2\omega_2^2 - 24\omega_4^3cs^2\omega_5\omega_2 - 12\omega_4^3v_1^2\omega_5^2\omega_2^2 - 3\omega_4^3\omega_5\omega_2^2$$

$$C_{32} = 48\omega_4^3cs^2\omega_5^2\omega_2^2 + 3\omega_4^3v_1^2\omega_5^2\omega_2^2 + 12v_1^2\omega_5^2\omega_2^2 + 2\omega_4^3\omega_5^2\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 - 12\omega_4^3v_1^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 - 6\omega_4^3\omega_5^2\omega_2^2 + 4\omega_4^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^3v_1^2\omega_5^2 + 12\omega_4^3v_1^2\omega_5^2\omega_2^2 + 3\omega_4^3\omega_5\omega_2^2 - 6\omega_4^3v_1^2\omega_2^2 + 30\omega_4^3v_1^2\omega_5^2\omega_2 - 6\omega_4^3\omega_5\omega_2^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^3cs^2\omega_5^2\omega_2 + 12\omega_4^3v_1^2\omega_2^2 + 3\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2^2 + 36\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 - 24\omega_4^3v_1^2\omega_5\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3v_1^2\omega_5\omega_2^2 + 12\omega_4^3cs^2\omega_5\omega_2^2 + 12\omega_4^3\omega_5\omega_2^2 - 12\omega_4^3cs^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2 - 24\omega_4^3cs^2\omega_5\omega_2^2 + 6\omega_4^3cs^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2 - 18\omega_4^3v_1^2\omega_5^2\omega_2^2 - 6\omega_4^3\omega_5\omega_2^2$$

$$C_{33} = 11\omega_2^2\omega_2^2 + 12\omega_2^2 + 18cs^2\omega_5^2\omega_2 + v_1^2\omega_5^2\omega_2^2 - 6\omega_2^3 - \omega_2^2\omega_2^2 - 14v_1^2\omega_5^2\omega_2^2 + 12v_1^2\omega_5^2\omega_2 - 60cs^2\omega_2^2 + 4cs^2\omega_5^2\omega_2^2 - 12\omega_5^2\omega_2 - 26cs^2\omega_5^2\omega_2^2 + 30cs^2\omega_2^2 + 96cs^2\omega_5\omega_2^2 + 24\omega_5\omega_2 - 60v_1^2\omega_5\omega_2 - 30cs^2\omega_5\omega_2^2 + 9\omega_5\omega_2^2 + 12v_1^2\omega_5^2 + 48v_1^2\omega_5\omega_2^2 - 6v_1^2\omega_2^2 - 36cs^2\omega_5\omega_2 - 36\omega_5\omega_2^2 + 12v_1^2\omega_2^2 - 6v_1^2\omega_5\omega_2^2$$

$$C_{34} = 18\omega_4^3\omega_2\omega_3 - 12\omega_4\omega_2\omega_3^2 + 18\omega_4\omega_2\omega_3^3 - 6\omega_4\omega_3^3 + 3\omega_4^3\omega_2\omega_3^3 - 16\omega_4^3\omega_2\omega_3^2 - 12\omega_4^3\omega_3^2 - 12\omega_4^3\omega_2\omega_3 - 6\omega_4^3\omega_3 + 12\omega_4^3\omega_3^2 + 30\omega_4^3\omega_2\omega_3^2 + 12\omega_3^3\omega_3^2 - 6\omega_2\omega_3^3 - 6\omega_4^3\omega_2 - 4\omega_4^3\omega_3^3 - 16\omega_4^3\omega_2\omega_3^3$$

$$C_{35} = 18\omega_4^3\omega_2\omega_3 - 16\omega_4^3\omega_3^2\omega_3 - 6\omega_2^3\omega_3 - 6\omega_4\omega_3^2 + 30\omega_4^3\omega_2^2\omega_3 - 4\omega_4^3\omega_2^2 - 12\omega_4\omega_2^2\omega_3 + 12\omega_4^3\omega_2^2 - 12\omega_4^3\omega_2\omega_3 + 3\omega_4^3\omega_2^2\omega_3 - 6\omega_4^3\omega_3 + 18\omega_4\omega_2^2\omega_3 + 12\omega_4^3\omega_2^2 - 6\omega_4^3\omega_2 - 16\omega_4^3\omega_2^2\omega_3 - 12\omega_4^3\omega_2^2$$

$$C_{36} = -12\omega_4\omega_2\omega_3^2 - 12\omega_2^2\omega_3^2 + 18\omega_4\omega_2\omega_3^3 - 6\omega_2^2\omega_3 + 12\omega_2^2\omega_3^2 - 6\omega_4\omega_2^2 + 12\omega_2^2\omega_3^2 - 6\omega_4\omega_3^2 - 4\omega_2^2\omega_3^3 - 12\omega_4\omega_2^2\omega_3 + 3\omega_4\omega_2^2\omega_3^3 - 16\omega_4\omega_2^2\omega_3^2 + 18\omega_4\omega_2^2\omega_3 - 16\omega_4\omega_2^2\omega_3^2 - 6\omega_2\omega_3^3 + 30\omega_4\omega_2^2\omega_3^2$$

$$C_{37} = -2\omega_4^3cs^2\omega_5^2\omega_2\omega_3^2 - 8\omega_4^3v_1^2\omega_5^2\omega_3^2\omega_2^2 + \omega_4^3cs^2\omega_2^2\omega_3^3 + 3\omega_3^3v_1^2\omega_5^2\omega_2^2 + 6\omega_3^3cs^2\omega_5^2\omega_2^2\omega_2^2 - \omega_3^3v_1^2\omega_5\omega_2^2\omega_3^2 - 2\omega_4^3cs^2\omega_5\omega_2\omega_3^2 + 2\omega_3^3v_1^2\omega_5^2\omega_3^2 - 8\omega_4^3v_1^2\omega_5^2\omega_3^2 - 2\omega_3^3cs^2\omega_5^2\omega_3^2 - 2\omega_2^2cs^2\omega_5^2\omega_2^2\omega_3^2 + 7\omega_2^2v_1^2\omega_5^2\omega_2^2\omega_3^2 + 3\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + \omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 + 2\omega_4^3v_1^2\omega_5\omega_2^2\omega_3^2 - 6\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 + 4\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + 3\omega_3^3v_1^2\omega_5^2\omega_2\omega_3^2 - 2\omega_4^3cs^2\omega_5^2\omega_2\omega_3^2 + \omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 + 4\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + \omega_4^3cs^2\omega_5\omega_2^2\omega_3^2 + 3\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + 2\omega_4^3v_1^2\omega_5\omega_2\omega_3^2 - 10\omega_2^2v_1^2\omega_5^2\omega_2^2\omega_3^2 + \omega_4^3cs^2\omega_5\omega_2^2\omega_3^2 + \omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 + 3\omega_4^3v_1^2\omega_5^2\omega_2\omega_3^2 - 2\omega_4^3cs^2\omega_5\omega_2^2\omega_3^2 + 8\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 - 8\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + 2\omega_4^3v_1^2\omega_5\omega_2^2\omega_3^2 - 2\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 - 2\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 - 2\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 + 3v_1^2\omega_5^2\omega_2^2\omega_3^2 + 6\omega_4^3cs^2\omega_5^2\omega_2\omega_3^2 - 2\omega_4^3cs^2\omega_5\omega_2^2\omega_3^2 + 7\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2\omega_3^2 - \omega_4^3v_1^2\omega_5\omega_2^2\omega_3^2 - 2\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3^2 + 6\omega_4^3cs^2\omega_5\omega_2^2\omega_3^2 + 4\omega_4^3v_1^2\omega_5^2\omega_2^2\omega_3 - 2\omega_4^3cs^2\omega_5^2\omega_2\omega_2\omega_3^2$$

$$C_{38} = -30\omega_4^3\omega_2^2\omega_3^3 + 18\omega_4^3\omega_2^2\omega_3 + 12\omega_4^3\omega_2^2\omega_3^2 + 24\omega_4^3\omega_2^2\omega_3^3 - 36\omega_4^3\omega_2\omega_3^3 + 12\omega_2^2\omega_3^3 + 18\omega_4^3\omega_2\omega_3^2 - 42\omega_4^3\omega_2^2\omega_3^2 + 12\omega_2^3\omega_3^2 - 30\omega_4^3\omega_2^2\omega_3^2 - 30\omega_4\omega_2^2\omega_3^3 + 18\omega_4\omega_2^2\omega_3^2 - 30\omega_4^3\omega_2^2\omega_3 + 28\omega_4^3\omega_2^2\omega_3^2 + 6\omega_4\omega_2^2\omega_3^2 + 24\omega_4^3\omega_2^2\omega_3^2 + 6\omega_4^3\omega_2^2\omega_3 + 12\omega_4^3\omega_3^3 - 5\omega_4^3\omega_2^2\omega_3^3 + 18\omega_4^3\omega_2\omega_3^3$$

$$C_{39} = 48\omega_4^3cs^2\omega_5^2\omega_2^2 - 5\omega_4^3v_1^2\omega_5^2\omega_2^2 + 12v_1^2\omega_5^2\omega_2^2 + 36\omega_4^3cs^2\omega_5^2\omega_2 + 16\omega_4^3v_1^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 + 4\omega_4^3cs^2\omega_5^2\omega_2^2 - 36\omega_4^3v_1^2\omega_5^2\omega_2^2 - 6\omega_4^3v_1^2\omega_5^2\omega_2 + 24\omega_4^3v_1^2\omega_5^2\omega_2^2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 24\omega_4^3cs^2\omega_5^2\omega_2 + 12\omega_4^3v_1^2\omega_2^2 - 12\omega_4^3v_1^2\omega_5\omega_2^2 + 36\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2^2 + 24\omega_4^3v_1^2\omega_5\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2 + 6\omega_4^3cs^2\omega_5^2\omega_2^2 - 36\omega_4^3v_1^2\omega_5\omega_2^2 + 12\omega_4^3cs^2\omega_5\omega_2^2 + 24\omega_4^3v_1^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2 - 24\omega_4^3cs^2\omega_5\omega_2^2 + 12\omega_4^3v_1^2\omega_5\omega_2^2 + 6\omega_4^3cs^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2 - 30\omega_4^3v_1^2\omega_5^2\omega_2^2$$

$$C_{40} = 12v_1^2\omega_2^2\omega_3^3 - 32cs^2\omega_5^2\omega_2^2\omega_3^3 + 12v_1^2\omega_5\omega_2^2\omega_3^3 + 12v_1^2\omega_2^2\omega_3^2 + 6cs^2\omega_2^2\omega_3^3 + 6cs^2\omega_5^2\omega_2^2\omega_3 - 12cs^2\omega_5\omega_2\omega_3^2 - 12v_1^2\omega_5\omega_2^2\omega_3^2 + 48cs^2\omega_5^2\omega_2^2\omega_3^2 - 12cs^2\omega_5^2\omega_3^3 - 12cs^2\omega_2^2\omega_3^3 - 36v_1^2\omega_5\omega_2^2\omega_3^3 + 4cs^2\omega_5^2\omega_2^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^2\omega_3 - 6v_1^2\omega_2^2\omega_3^3 - 6v_1^2\omega_5^2\omega_2\omega_3^3 - 12cs^2\omega_5^2\omega_2^2\omega_3^2 + 24v_1^2\omega_5\omega_2^2\omega_3^2 - 30v_1^2\omega_5^2\omega_2^2\omega_3 + 16v_1^2\omega_2^2\omega_3^2\omega_3^3 - 12cs^2\omega_5\omega_2^2\omega_3^3 + 12cs^2\omega_5\omega_2^2\omega_3^2 - 36v_1^2\omega_2^2\omega_3^2 + 12v_1^2\omega_5\omega_2\omega_3^3 + 24v_1^2\omega_5^2\omega_2\omega_3 - 24cs^2\omega_5^2\omega_2\omega_3^2 + 36cs^2\omega_5\omega_2^2\omega_3^3 - 5v_1^2\omega_5^2\omega_2^2\omega_3^3 + 24v_1^2\omega_5^2\omega_2^2\omega_3^2 - 24cs^2\omega_5\omega_2^2\omega_3^2 + 36cs^2\omega_5^2\omega_2\omega_2\omega_3^3$$

$$C_{41} = 6\omega_4v_2^2\omega_3^3 - 36\omega_4v_2^2\omega_6^2\omega_3 - 12\omega_4v_2^2\omega_3^2 + 12\omega_4cs^2\omega_6\omega_3 + 12cs^2\omega_6^2\omega_3 + 12\omega_4cs^2\omega_6^2 + \omega_4v_2^2\omega_6^2\omega_3^3 + 6v_2^2\omega_6\omega_3^3 - 18cs^2\omega_6^2\omega_3^2 - 30\omega_4cs^2\omega_6\omega_3^2 + 9\omega_4cs^2\omega_6\omega_3^2 + 3cs^2\omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3^2 + 8\omega_4v_2^2\omega_6^2\omega_3 - 2\omega_4cs^2\omega_6^2\omega_3^2 - 6cs^2\omega_6\omega_3^3 - 6v_2^2\omega_6^2\omega_3^2 + 30\omega_4v_2^2\omega_6\omega_3^2 - 9\omega_4v_2^2\omega_6\omega_3^3 - v_2^2\omega_6^2\omega_3^3 + 12cs^2\omega_6\omega_3^2 + 22\omega_4cs^2\omega_6^2\omega_3^2 + 12\omega_4cs^2\omega_6^2\omega_3 - 30\omega_4cs^2\omega_6^2\omega_3 + 24\omega_4v_2^2\omega_6^2 - 12\omega_4v_2^2\omega_6\omega_3 + 12v_2^2\omega_6^2\omega_3 - 6\omega_4cs^2\omega_6^2\omega_3^3$$

$$C_{42} = -2\omega_4^3cs^2\omega_2\omega_2^2\omega_6^2\omega_3^2 + 7\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 + \omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 + \omega_4^3cs^2\omega_2^2\omega_3^2 + 6\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3 - 6\omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 4\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 + 2\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3 - 2\omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 - 10\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 + \omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3 + 2\omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 + \omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 + 7\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 - 6\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 - 7\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3 + 4\omega_4^3v_2^2\omega_2\omega_6^2\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 - \omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 - 2\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 6\omega_4^3cs^2\omega_2^2\omega_6\omega_3^2 + 4\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^2 + 2\omega_4^3v_2^2\omega_2^2\omega_6\omega_3^2 + 6\omega_4^3cs^2\omega_2^2\omega_6^2\omega_3^2 + 3\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^3 - 8\omega_4^3v_2^2\omega_2\omega_6^2\omega_3^2 - 8\omega_4^3v_2^2\omega_2^2\omega_6^2\omega_3^3 -$$



$$C_{68} = 72\omega_7\omega_4cs^2v_3^2 - 6\omega_7\omega_3cs^2 + 3\omega_7^2\omega_3^2v_3^4 - 36\omega_3^2v_3^3 - 3\omega_7^2\omega_4^2cs^4 + 30\omega_7\omega_4^3v_3^3 - 12\omega_7^2\omega_2^2cs^2v_3^3 + 24\omega_7\omega_4cs^4 + 12\omega_7^2\omega_4cs^2 + 108\omega_3^2cs^2v_3^2 - 72\omega_7\omega_4^3cs^2v_3^2 - 72\omega_7\omega_2^2v_3^3 + 24\omega_7^2\omega_2^2cs^4 - 12\omega_7^2\omega_4^3v_3^4 + 24\omega_7\omega_4^2cs^2 + 72\omega_4^3v_3^3 - 36\omega_7^2\omega_4cs^2v_3^3 - 48\omega_7\omega_4cs^4 - 24\omega_7\omega_4cs^2 - 24\omega_7\omega_4^2cs^4 + 12\omega_7^2\omega_4^3v_3^3 - 72\omega_4^3v_3^4 - 8\omega_7^2\omega_4^2cs^2 + 72\omega_7\omega_4^3v_3^4 + 24\omega_2^2cs^4 + 144\omega_7\omega_2^2cs^2v_3^3 - 216\omega_2^2cs^2v_3^3 - 30\omega_7\omega_4^3v_3^4 + \omega_7^2\omega_4^3cs^2 - 3\omega_7^2\omega_3^2v_3^3 + 6\omega_7\omega_4^3cs^4 + 36\omega_4^3v_3^4 + 6\omega_7^2\omega_4^3cs^2v_3^3$$



$$\begin{aligned}
& + C_{D_x^2 D_y D_z v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_t D_y^2 D_z v_2}^{(0)} \delta_l^3 \frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3} + C_{D_t D_y^2 D_z v_3}^{(0)} \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3} + \\
& C_{D_x D_y^2 D_z \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{D_y^3 D_z \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_t^2 D_z^2 v_3}^{(0)} \delta_l^2 \delta_t \frac{\partial^4 v_3}{\partial t^2 \partial x_2^2} + C_{D_t D_x D_z^2 v_1}^{(0)} \delta_l^3 \frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2} + \\
& C_{D_t D_x D_z^2 v_3}^{(0)} \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2} + C_{D_t^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{D_t^2 D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{D_t^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + C_{D_t D_y D_z^2 v_2}^{(0)} \delta_l^3 \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} + \\
& + C_{D_t D_y D_z^2 v_3}^{(0)} \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{D_x D_y D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_y^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{D_t D_z^3 v_3}^{(0)} \delta_l^3 \frac{\partial^4 v_3}{\partial t \partial x_3^3} + \\
& C_{D_x D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{D_y D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{D_y D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{D_z^4 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{D_z^4 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

**coefficient**  $C_{D_x \rho, D_t v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial t}$ :

$$\begin{aligned}
C_{D_x \rho, D_t v_1}^{(0), \text{SRT}} &= (-2 + \omega) \frac{1}{2\omega} \\
C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}} &= (-2 + \omega_2) \frac{1}{2\omega_2} \\
C_{D_x \rho, D_t v_1}^{(0), \text{MRT2}} &= C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}} \\
C_{D_x \rho, D_t v_1}^{(0), \text{CLBM1}} &= C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}} \\
C_{D_x \rho, D_t v_1}^{(0), \text{CLBM2}} &= C_{D_x \rho, D_t v_1}^{(0), \text{MRT1}}
\end{aligned}$$

**coefficient**  $C_{D_x \rho, D_x v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1}$ :

$$\begin{aligned}
C_{D_x \rho, D_x v_1}^{(0), \text{SRT}} &= (-2 + \omega) \frac{v_1}{2\omega} \\
C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}} &= (-2 + \omega_2) \frac{v_1}{2\omega_2} \\
C_{D_x \rho, D_x v_1}^{(0), \text{MRT2}} &= C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}} \\
C_{D_x \rho, D_x v_1}^{(0), \text{CLBM1}} &= C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}} \\
C_{D_x \rho, D_x v_1}^{(0), \text{CLBM2}} &= C_{D_x \rho, D_x v_1}^{(0), \text{MRT1}}
\end{aligned}$$

**coefficient**  $C_{D_x v_1, D_x v_1}^{(0)}$  **at**  $\left(\frac{\partial v_1}{\partial x_1}\right)^2$ :

$$\begin{aligned}
C_{D_x v_1, D_x v_1}^{(0), \text{SRT}} &= (-2 + \omega) \frac{\rho}{2\omega} \\
C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}} &= (-2 + \omega_2) \frac{\rho}{2\omega_2} \\
C_{D_x v_1, D_x v_1}^{(0), \text{MRT2}} &= C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}} \\
C_{D_x v_1, D_x v_1}^{(0), \text{CLBM1}} &= C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}} \\
C_{D_x v_1, D_x v_1}^{(0), \text{CLBM2}} &= C_{D_x v_1, D_x v_1}^{(0), \text{MRT1}}
\end{aligned}$$

**coefficient**  $C_{D_x \rho, D_y v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2}$ :

$$C_{D_x \rho, D_y v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{2\omega}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{MRT2}} = C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{CLBM1}} = C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(0), \text{CLBM2}} = C_{D_x \rho, D_y v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x \rho, D_y v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2}$  :

$$C_{D_x \rho, D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{\omega}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{v_1}{\omega_2 \omega_3}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{MRT2}} = C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{CLBM1}} = C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_2}^{(0), \text{CLBM2}} = C_{D_x \rho, D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x v_1, D_y v_2}^{(0)}$  **at**  $\frac{\partial v_1}{\partial x_1} \frac{\partial v_2}{\partial x_2}$  :

$$C_{D_x v_1, D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{MRT1}} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{\rho}{\omega_2 \omega_3}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{MRT2}} = C_{D_x v_1, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{CLBM1}} = C_{D_x v_1, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_x v_1, D_y v_2}^{(0), \text{CLBM2}} = C_{D_x v_1, D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x \rho, D_z v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3}$  :

$$C_{D_x \rho, D_z v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{2\omega}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{MRT2}} = C_{D_x \rho, D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{CLBM1}} = C_{D_x \rho, D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_1}^{(0), \text{CLBM2}} = C_{D_x \rho, D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x \rho, D_z v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3}$  :

$$C_{D_x \rho, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{\omega}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1}{\omega_4 \omega_2}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{MRT2}} = C_{D_x \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{CLBM1}} = C_{D_x \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_3}^{(0), \text{CLBM2}} = C_{D_x \rho, D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x v_1, D_z v_3}^{(0)}$  **at**  $\frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3}$  :

$$C_{D_x v_1, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{\rho}{\omega_4 \omega_2}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{MRT2}} = C_{D_x v_1, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{CLBM1}} = C_{D_x v_1, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x v_1, D_z v_3}^{(0), \text{CLBM2}} = C_{D_x v_1, D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y \rho, D_t v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial t}$ :

$$C_{D_y \rho, D_t v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{1}{2\omega_3}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_t v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_t v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_t v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_t v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y \rho, D_x v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1}$ :

$$C_{D_y \rho, D_x v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{\omega}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{v_2}{\omega_2 \omega_3}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{MRT2}} = C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{CLBM1}} = C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_1}^{(0), \text{CLBM2}} = C_{D_y \rho, D_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y \rho, D_x v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1}$ :

$$C_{D_y \rho, D_x v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{2\omega}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_x v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y \rho, D_y v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2}$ :

$$C_{D_y \rho, D_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_2}{2\omega}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y v_2, D_y v_2}^{(0)}$  **at**  $\left(\frac{\partial v_2}{\partial x_2}\right)^2$ :

$$C_{D_y v_2, D_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{\rho}{2\omega_3}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{MRT2}} = C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{CLBM1}} = C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(0), \text{CLBM2}} = C_{D_y v_2, D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y \rho, D_z v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3}$ :

$$C_{D_y \rho, D_z v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{2\omega}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{MRT2}} = C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{CLBM1}} = C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(0), \text{CLBM2}} = C_{D_y \rho, D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y \rho, D_z v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_y \rho, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{\omega}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2}{\omega_4 \omega_3}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{MRT2}} = C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{CLBM1}} = C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_3}^{(0), \text{CLBM2}} = C_{D_y \rho, D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y v_2, D_z v_3}^{(0)}$  **at**  $\frac{\partial v_2}{\partial x_2} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_y v_2, D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho}{\omega}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{\rho}{\omega_4 \omega_3}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{MRT2}} = C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{CLBM1}} = C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y v_2, D_z v_3}^{(0), \text{CLBM2}} = C_{D_y v_2, D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z \rho, D_t v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial t}$ :

$$C_{D_z \rho, D_t v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{1}{2\omega}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{1}{2\omega_4}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_t v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_t v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z \rho, D_x v_1}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1}$ :

$$C_{D_z \rho, D_x v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{\omega}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_3}{\omega_4 \omega_2}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{MRT2}} = C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{CLBM1}} = C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_1}^{(0), \text{CLBM2}} = C_{D_z \rho, D_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z \rho, D_x v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1}$ :

$$C_{D_z \rho, D_x v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1}{2\omega}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1}{2\omega_2}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_x v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z \rho, D_y v_2}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2}$ :

$$C_{D_z \rho, D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_3}{\omega}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_3}{\omega_4 \omega_3}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{MRT2}} = C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{CLBM1}} = C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_2}^{(0), \text{CLBM2}} = C_{D_z \rho, D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z \rho, D_y v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2}$ :

$$C_{D_z \rho, D_y v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2}{2\omega}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2}{2\omega_3}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_y v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z \rho, D_z v_3}^{(0)}$  **at**  $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3}$ :

$$C_{D_z \rho, D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_3}{2\omega}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{v_3}{2\omega_4}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{MRT2}} = C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{CLBM1}} = C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(0), \text{CLBM2}} = C_{D_z \rho, D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z v_3, D_z v_3}^{(0)}$  **at**  $\left(\frac{\partial v_3}{\partial x_3}\right)^2$ :

$$C_{D_z v_3, D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho}{2\omega_4}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{MRT2}} = C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{CLBM1}} = C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(0), \text{CLBM2}} = C_{D_z v_3, D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial t \partial x_1}$ :

$$C_{D_t D_x v_1}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_x v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{\rho}{2\omega_2}$$

$$C_{D_t D_x v_1}^{(0), \text{MRT2}} = C_{D_t D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x v_1}^{(0), \text{CLBM1}} = C_{D_t D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x v_1}^{(0), \text{CLBM2}} = C_{D_t D_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x^2 \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_1^2}$ :

$$C_{D_x^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{cs^2}{2\omega}$$

$$C_{D_x^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

$$C_{D_x^2 \rho}^{(0), \text{MRT2}} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

$$C_{D_x^2 \rho}^{(0), \text{CLBM1}} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

$$C_{D_x^2 \rho}^{(0), \text{CLBM2}} = (-2 + \omega_2) \frac{cs^2}{2\omega_2}$$

**coefficient**  $C_{D_x^2 v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial x_1^2}$ :

$$C_{D_x^2 v_1}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_1 \rho}{2\omega}$$

$$C_{D_x^2 v_1}^{(0), \text{MRT1}} = (-2 + \omega_2) \frac{v_1 \rho}{2\omega_2}$$

$$C_{D_x^2 v_1}^{(0), \text{MRT2}} = C_{D_x^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(0), \text{CLBM1}} = C_{D_x^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(0), \text{CLBM2}} = C_{D_x^2 v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_y v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial t \partial x_2}$ :

$$C_{D_t D_y v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_y v_2}^{(0), \text{MRT}1} = (-2 + \omega_3) \frac{\rho}{2\omega_3}$$

$$C_{D_t D_y v_2}^{(0), \text{MRT}2} = C_{D_t D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_t D_y v_2}^{(0), \text{CLBM}1} = C_{D_t D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_t D_y v_2}^{(0), \text{CLBM}2} = C_{D_t D_y v_2}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_x D_y \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 v_2}{\omega}$$

$$C_{D_x D_y \rho}^{(0), \text{MRT}1} = (\omega_2 + \omega_3 - \omega_2 \omega_3) \frac{v_1 v_2}{\omega_2 \omega_3}$$

$$C_{D_x D_y \rho}^{(0), \text{MRT}2} = C_{D_x D_y \rho}^{(0), \text{MRT}1}$$

$$C_{D_x D_y \rho}^{(0), \text{CLBM}1} = C_{D_x D_y \rho}^{(0), \text{MRT}1}$$

$$C_{D_x D_y \rho}^{(0), \text{CLBM}2} = C_{D_x D_y \rho}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_x D_y v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_x D_y v_1}^{(0), \text{MRT}1} = (2 - \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_x D_y v_1}^{(0), \text{MRT}2} = C_{D_x D_y v_1}^{(0), \text{MRT}1}$$

$$C_{D_x D_y v_1}^{(0), \text{CLBM}1} = C_{D_x D_y v_1}^{(0), \text{MRT}1}$$

$$C_{D_x D_y v_1}^{(0), \text{CLBM}2} = C_{D_x D_y v_1}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_x D_y v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial x_1 \partial x_2}$ :

$$C_{D_x D_y v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 \rho}{2\omega}$$

$$C_{D_x D_y v_2}^{(0), \text{MRT}1} = (2 - \omega_2) \frac{v_1 \rho}{2\omega_2}$$

$$C_{D_x D_y v_2}^{(0), \text{MRT}2} = C_{D_x D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_x D_y v_2}^{(0), \text{CLBM}1} = C_{D_x D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_x D_y v_2}^{(0), \text{CLBM}2} = C_{D_x D_y v_2}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_y^2 \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_2^2}$ :

$$C_{D_y^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{cs^2}{2\omega}$$

$$C_{D_y^2 \rho}^{(0), \text{MRT}1} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{MRT}2} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{CLBM}1} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

$$C_{D_y^2 \rho}^{(0), \text{CLBM}2} = (-2 + \omega_3) \frac{cs^2}{2\omega_3}$$

**coefficient**  $C_{D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial x_2^2}$ :

$$C_{D_y^2 v_2}^{(0), \text{SRT}} = (-2 + \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_y^2 v_2}^{(0), \text{MRT1}} = (-2 + \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(0), \text{CLBM1}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_y^2 v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_z v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial t \partial x_3}$ :

$$C_{D_t D_z v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho}{2\omega}$$

$$C_{D_t D_z v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho}{2\omega_4}$$

$$C_{D_t D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_z \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$ :

$$C_{D_x D_z \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 v_3}{\omega}$$

$$C_{D_x D_z \rho}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_2 + \omega_2) \frac{v_1 v_3}{\omega_4 \omega_2}$$

$$C_{D_x D_z \rho}^{(0), \text{MRT2}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z \rho}^{(0), \text{CLBM1}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z \rho}^{(0), \text{CLBM2}} = C_{D_x D_z \rho}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_z v_1}^{(0)}$  **at**  $\frac{\partial^2 v_1}{\partial x_1 \partial x_3}$ :

$$C_{D_x D_z v_1}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho v_3}{2\omega}$$

$$C_{D_x D_z v_1}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{\rho v_3}{2\omega_4}$$

$$C_{D_x D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_x D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_z v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial x_1 \partial x_3}$ :

$$C_{D_x D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_1 \rho}{2\omega}$$

$$C_{D_x D_z v_3}^{(0), \text{MRT1}} = (2 - \omega_2) \frac{v_1 \rho}{2\omega_2}$$

$$C_{D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(0), \text{CLBM1}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(0), \text{CLBM2}} = C_{D_x D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y D_z \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$ :

$$C_{D_y D_z \rho}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 v_3}{\omega}$$

$$C_{D_y D_z \rho}^{(0), \text{MRT1}} = (\omega_4 - \omega_4 \omega_3 + \omega_3) \frac{v_2 v_3}{\omega_4 \omega_3}$$

$$C_{D_y D_z \rho}^{(0), \text{MRT2}} = C_{D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y D_z \rho}^{(0), \text{CLBM1}} = C_{D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y D_z \rho}^{(0), \text{CLBM2}} = C_{D_y D_z \rho}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^2 v_2}{\partial x_2 \partial x_3}$ :

$$C_{D_y D_z v_2}^{(0), \text{SRT}} = (2 - \omega) \frac{\rho v_3}{2\omega}$$

$$C_{D_y D_z v_2}^{(0), \text{MRT1}} = (2 - \omega_4) \frac{\rho v_3}{2\omega_4}$$

$$C_{D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_y D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial x_2 \partial x_3}$ :

$$C_{D_y D_z v_3}^{(0), \text{SRT}} = (2 - \omega) \frac{v_2 \rho}{2\omega}$$

$$C_{D_y D_z v_3}^{(0), \text{MRT1}} = (2 - \omega_3) \frac{v_2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_y D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^2 \rho}{\partial x_3^2}$ :

$$C_{D_z^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{cs^2}{2\omega}$$

$$C_{D_z^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{cs^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), \text{MRT2}} = (-2 + \omega_4) \frac{cs^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), \text{CLBM1}} = (-2 + \omega_4) \frac{cs^2}{2\omega_4}$$

$$C_{D_z^2 \rho}^{(0), \text{CLBM2}} = (-2 + \omega_4) \frac{cs^2}{2\omega_4}$$

**coefficient**  $C_{D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^2 v_3}{\partial x_3^2}$ :

$$C_{D_z^2 v_3}^{(0), \text{SRT}} = (-2 + \omega) \frac{\rho v_3}{2\omega}$$

$$C_{D_z^2 v_3}^{(0), \text{MRT1}} = (-2 + \omega_4) \frac{\rho v_3}{2\omega_4}$$

$$C_{D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t^2 D_x v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial t^2 \partial x_1}$ :

$$C_{D_t^2 D_x v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{MRT1}} = (12 + \omega^2 - 12\omega_2) \frac{\rho}{12\omega_2^2}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{MRT2}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x^2 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial t \partial x_1^2}$ :

$$C_{D_t D_x^2 v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 \rho}{6\omega^2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{MRT1}} = (12 + \omega_5 \omega_2 - 6\omega_5 - 6\omega_2) \frac{v_1 \rho}{6\omega_5 \omega_2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{CLBM1}} = (12 + \omega_2^2 - 12\omega_2) \frac{v_1 \rho}{6\omega_2^2}$$

$$C_{D_t D_x^2 v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 v_1}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_x^3 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1^3}$ :

$$C_{D_x^3 \rho}^{(0), \text{SRT}} = (6 - 3\omega^2 cs^2 - \omega^2 v_1^2 - 6v_1^2 - 18cs^2 - 6\omega + \omega^2 + 6\omega v_1^2 + 18\omega cs^2) \frac{v_1}{6\omega^2}$$

$$C_{D_x^3 \rho}^{(0), \text{MRT1}} = (15\omega_5 \omega_2 cs^2 + \omega_5 \omega_2^2 + 3\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2 + 3\omega_2^2 cs^2 - \omega_5 v_1^2 \omega_2^2 - 3\omega_2^2 - 6v_1^2 \omega_2 + 6\omega_2 - 6\omega_2 cs^2 + 3v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2) \frac{v_1}{6\omega_5 \omega_2^2}$$

$$C_{D_x^3 \rho}^{(0), \text{MRT2}} = (-3cs^2 \omega_5 \omega_2^2 + \omega_5 \omega_2^2 + 3\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2 + 15cs^2 \omega_5 \omega_2 - \omega_5 v_1^2 \omega_2^2 - 3\omega_2^2 - 6cs^2 \omega_2 - 6v_1^2 \omega_2 + 6\omega_2 - 12cs^2 \omega_5 + 3v_1^2 \omega_2^2 + 3cs^2 \omega_2^2) \frac{v_1}{6\omega_5 \omega_2^2}$$

$$C_{D_x^3 \rho}^{(0), \text{CLBM1}} = (6 + 3\omega_5 v_1^2 - \omega_5 v_1^2 \omega_2 + 9\omega_5 cs^2 + \omega_5 \omega_2 - 6v_1^2 + 9\omega_2 cs^2 - 18cs^2 - 3\omega_5 + 3v_1^2 \omega_2 - 3\omega_2 - 3\omega_5 \omega_2 cs^2) \frac{v_1}{6\omega_5 \omega_2}$$

$$C_{D_x^3 \rho}^{(0), \text{CLBM2}} = (6 + 3\omega_5 v_1^2 - \omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2 cs^2 + \omega_5 \omega_2 - 6v_1^2 - 3\omega_5 + 3v_1^2 \omega_2 - 3\omega_2 + 9\omega_2 cs^2 - 18cs^2 + 9\omega_5 cs^2) \frac{v_1}{6\omega_5 \omega_2}$$

**coefficient**  $C_{D_x^3 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1^3}$ :

$$C_{D_x^3 v_1}^{(0), \text{SRT}} = (12 - 3\omega^2 cs^2 - 5\omega^2 v_1^2 - 24v_1^2 - 24cs^2 - 12\omega + 2\omega^2 + 24\omega v_1^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^3 v_1}^{(0), \text{MRT1}} = (18\omega_5 \omega_2 cs^2 - 12\omega_5 v_1^2 + 2\omega_5 \omega_2^2 + 18\omega_5 v_1^2 \omega_2 - 6\omega_5 \omega_2 + 6\omega_2^2 cs^2 - 5\omega_5 v_1^2 \omega_2^2 - 6\omega_2^2 - 12v_1^2 \omega_2 + 12\omega_2 - 12\omega_2 cs^2 + 6v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^3 v_1}^{(0), \text{MRT}2} = (-12\omega_5 v_1^2 - 3cs^2 \omega_5 \omega_2^2 + 2\omega_5 \omega_2^2 + 18\omega_5 v_1^2 \omega_2 - 6\omega_5 \omega_2 + 18cs^2 \omega_5 \omega_2 - 5\omega_5 v_1^2 \omega_2^2 - 6\omega_2^2 - 12cs^2 \omega_2 - 12v_1^2 \omega_2 + 12\omega_2 - 12cs^2 \omega_5 + 6v_1^2 \omega_2^2 + 6cs^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^3 v_1}^{(0), \text{CLBM}1} = (12\omega_5 v_1^2 + 2\omega_5 \omega_2^2 + 6\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2 - 6\omega_5 \omega_2 - 5\omega_5 v_1^2 \omega_2^2 - 6\omega_2^2 - 12\omega_2 cs^2 + 6\omega_2^2 cs^2 - 36v_1^2 \omega_2 + 12\omega_2 + 18\omega_5 \omega_2 cs^2 + 18v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^3 v_1}^{(0), \text{CLBM}2} = (12\omega_5 v_1^2 + 2\omega_5 \omega_2^2 + 6\omega_5 v_1^2 \omega_2 + 18\omega_5 \omega_2 cs^2 - 6\omega_5 \omega_2 - 5\omega_5 v_1^2 \omega_2^2 - 6\omega_2^2 + 6\omega_2^2 cs^2 - 36v_1^2 \omega_2 + 12\omega_2 - 12\omega_2 cs^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2 + 18v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

**coefficient**  $C_{D_t^2 D_y v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial t^2 \partial x_2}$ :

$$C_{D_t^2 D_y v_2}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{MRT}1} = (12 + \omega_3^2 - 12\omega_3) \frac{\rho}{12\omega_3^2}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{MRT}2} = C_{D_t^2 D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{CLBM}1} = C_{D_t^2 D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_t^2 D_y v_2}^{(0), \text{CLBM}2} = C_{D_t^2 D_y v_2}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_t D_x D_y v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_2}$ :

$$C_{D_t D_x D_y v_1}^{(0), \text{SRT}} = (-6 + 6\omega - \omega^2) \frac{v_2 \rho}{3\omega^2}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{MRT}1} = (3\omega_3^2 - 2\omega_2 \omega_3^2 - 6\omega_2 - 6\omega_3 + 9\omega_2 \omega_3) \frac{v_2 \rho}{6\omega_2 \omega_3^2}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{MRT}2} = C_{D_t D_x D_y v_1}^{(0), \text{MRT}1}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{CLBM}1} = C_{D_t D_x D_y v_1}^{(0), \text{MRT}1}$$

$$C_{D_t D_x D_y v_1}^{(0), \text{CLBM}2} = C_{D_t D_x D_y v_1}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_t D_x D_y v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial t \partial x_1 \partial x_2}$ :

$$C_{D_t D_x D_y v_2}^{(0), \text{SRT}} = (-6 + 6\omega - \omega^2) \frac{v_1 \rho}{3\omega^2}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{MRT}1} = (-2\omega_2^2 \omega_3 + 3\omega_2^2 - 6\omega_2 - 6\omega_3 + 9\omega_2 \omega_3) \frac{v_1 \rho}{6\omega_2^2 \omega_3}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{MRT}2} = C_{D_t D_x D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{CLBM}1} = C_{D_t D_x D_y v_2}^{(0), \text{MRT}1}$$

$$C_{D_t D_x D_y v_2}^{(0), \text{CLBM}2} = C_{D_t D_x D_y v_2}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_x^2 D_y \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1^2 \partial x_2}$ :

$$C_{D_x^2 D_y \rho}^{(0), \text{SRT}} = (-\omega^2 cs^2 + \omega^2 v_1^2 + 6v_1^2 - 6cs^2 - 6\omega v_1^2 + 6\omega cs^2) \frac{v_2}{2\omega^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{MRT}1} = (-\omega_5 \omega_2^2 \omega_3^2 cs^2 - 2\omega_5 \omega_2 \omega_3 cs^2 - 2\omega_5 \omega_3^2 cs^2 + \omega_5 v_1^2 \omega_2^2 \omega_3^2 + v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 + \omega_2^2 \omega_3^2 cs^2 - 2\omega_2 \omega_3^2 cs^2 + 4\omega_5 v_1^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 - 2v_1^2 \omega_2 \omega_3^2 + 4\omega_5 \omega_2 \omega_3^2 cs^2 - 4\omega_5 v_1^2 \omega_2 \omega_3^2 + \omega_5 \omega_2^2 \omega_3 cs^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{MRT}^2} = (\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 4cs^2 \omega_5 \omega_2 \omega_3^2 - 2cs^2 \omega_5 \omega_2 \omega_3 + v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 + cs^2 \omega_2^2 \omega_3^2 - 2cs^2 \omega_2 \omega_3^2 + cs^2 \omega_5 \omega_2^2 \omega_3 + 4\omega_5 v_1^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 - 2v_1^2 \omega_2 \omega_3^2 - 2cs^2 \omega_5 \omega_3^2 - 4\omega_5 v_1^2 \omega_2 \omega_3^2 - cs^2 \omega_5 \omega_2^2 \omega_3^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{CLBM}^1} = (4\omega_5 \omega_2 cs^2 \omega_3^2 + \omega_5 v_1^2 \omega_2^2 \omega_3^2 - v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 - 2\omega_5 \omega_2 cs^2 \omega_3 - 2\omega_2 cs^2 \omega_3^2 + \omega_2^2 cs^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 + \omega_5 \omega_2^2 cs^2 \omega_3 + 2v_1^2 \omega_2 \omega_3^2 - 2\omega_5 v_1^2 \omega_2 \omega_3^2 - \omega_5 \omega_2^2 cs^2 \omega_3^2 - 2\omega_5 cs^2 \omega_3^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y \rho}^{(0), \text{CLBM}^2} = (-2\omega_5 \omega_2 \omega_3 cs^2 - 2\omega_5 \omega_3^2 cs^2 - \omega_5 \omega_2^2 \omega_3^2 cs^2 + \omega_5 v_1^2 \omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2 cs^2 - v_1^2 \omega_2^2 \omega_3^2 + 2\omega_5 v_1^2 \omega_2^2 - 3\omega_5 v_1^2 \omega_2^2 \omega_3 - 2\omega_2 \omega_3^2 cs^2 + 2\omega_5 v_1^2 \omega_2 \omega_3 + 2v_1^2 \omega_2 \omega_3^2 + \omega_5 \omega_2^2 \omega_3 cs^2 - 2\omega_5 v_1^2 \omega_2 \omega_3^2 + 4\omega_5 \omega_2 \omega_3^2 cs^2) \frac{v_2}{2\omega_5 \omega_2^2 \omega_3^2}$$

**coefficient**  $C_{D_x^2 D_y v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_2}$ :

$$C_{D_x^2 D_y v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 v_2 \rho}{6\omega^2}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{MRT}^1} = (-6\omega_2^2 \omega_3 + 6\omega_2^2 + \omega_2^2 \omega_3^2 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_1 v_2 \rho}{6\omega_2^2 \omega_3^2}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{MRT}^2} = C_{D_x^2 D_y v_1}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{CLBM}^1} = C_{D_x^2 D_y v_1}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_y v_1}^{(0), \text{CLBM}^2} = C_{D_x^2 D_y v_1}^{(0), \text{MRT}^1}$$

**coefficient**  $C_{D_x^2 D_y v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_2}$ :

$$C_{D_x^2 D_y v_2}^{(0), \text{SRT}} = (-3\omega^2 cs^2 + \omega^2 v_1^2 - 24cs^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{MRT}^1} = (18\omega_5 \omega_2 cs^2 + 12\omega_5 v_1^2 - 6\omega_5 v_1^2 \omega_2 + 6\omega_2^2 cs^2 + \omega_5 v_1^2 \omega_2^2 - 12v_1^2 \omega_2 - 12\omega_2 cs^2 + 6v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{MRT}^2} = (12\omega_5 v_1^2 - 3cs^2 \omega_5 \omega_2^2 - 6\omega_5 v_1^2 \omega_2 + 18cs^2 \omega_5 \omega_2 + \omega_5 v_1^2 \omega_2^2 - 12cs^2 \omega_2 - 12v_1^2 \omega_2 - 12cs^2 \omega_5 + 6v_1^2 \omega_2^2 + 6cs^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{CLBM}^1} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2 + \omega_5 v_1^2 \omega_2^2 - 12\omega_2 cs^2 + 6\omega_2^2 cs^2 + 12v_1^2 \omega_2 + 18\omega_5 \omega_2 cs^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_y v_2}^{(0), \text{CLBM}^2} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 + 18\omega_5 \omega_2 cs^2 + \omega_5 v_1^2 \omega_2^2 + 6\omega_2^2 cs^2 + 12v_1^2 \omega_2 - 12\omega_2 cs^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

**coefficient**  $C_{D_t D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial t \partial x_2^2}$ :

$$C_{D_t D_y^2 v_2}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_2 \rho}{6\omega^2}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{MRT}^1} = (12 + \omega_6 \omega_3 - 6\omega_6 - 6\omega_3) \frac{v_2 \rho}{6\omega_6 \omega_3}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{MRT}^2} = C_{D_t D_y^2 v_2}^{(0), \text{MRT}^1}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{CLBM}^1} = (12 + \omega_3^2 - 12\omega_3) \frac{v_2 \rho}{6\omega_3^2}$$

$$C_{D_t D_y^2 v_2}^{(0), \text{CLBM}^2} = C_{D_t D_y^2 v_2}^{(0), \text{CLBM}^1}$$

**coefficient**  $C_{D_x D_y^2 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1 \partial x_2^2}$ :

$$C_{D_x D_y^2 \rho}^{(0), \text{SRT}} = (-\omega^2 cs^2 + \omega^2 v_2^2 - 6cs^2 + 6v_2^2 + 6\omega cs^2 - 6\omega v_2^2) \frac{v_1}{2\omega^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{MRT}^1} = (-3\omega_2^2 v_2^2 \omega_6 \omega_3^2 + \omega_2 \omega_6 \omega_3^2 cs^2 - 2\omega_2^2 \omega_6 cs^2 + 2v_2^2 \omega_6 \omega_3^2 + 4\omega_2^2 \omega_6 \omega_3 cs^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 + \omega_2^2 \omega_3^2 cs^2 + 4\omega_2^2 v_2^2 \omega_6 - \omega_2^2 \omega_6 \omega_3^2 cs^2 - 2\omega_2^2 \omega_3 cs^2 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 + \omega_2^2 v_2^2 \omega_3^2 - 2\omega_2^2 v_2^2 \omega_3 - 4\omega_2^2 v_2^2 \omega_6 \omega_3 - 2\omega_2 \omega_6 \omega_3 cs^2) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{MRT}^2} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 - cs^2 \omega_2^2 \omega_6 \omega_3^2 - 2cs^2 \omega_2^2 \omega_3 + 2v_2^2 \omega_6 \omega_3^2 - 2cs^2 \omega_2^2 \omega_6 + 4cs^2 \omega_2^2 \omega_6 \omega_3 + cs^2 \omega_2^2 \omega_3^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 + 4\omega_2^2 v_2^2 \omega_6 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 + \omega_2^2 v_2^2 \omega_3^2 - 2cs^2 \omega_2 \omega_6 \omega_3 - 2\omega_2^2 v_2^2 \omega_3 + cs^2 \omega_2 \omega_6 \omega_3^2 - 4\omega_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{CLBM}^1} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 + \omega_2 cs^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 - 2\omega_2 cs^2 \omega_6 \omega_3 + 2\omega_2 v_2^2 \omega_6 \omega_3 - 2\omega_2^2 cs^2 \omega_6 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 - \omega_2^2 v_2^2 \omega_3^2 + \omega_2^2 cs^2 \omega_3^2 - \omega_2^2 cs^2 \omega_6 \omega_3^2 - 2\omega_2^2 cs^2 \omega_3 + 4\omega_2^2 cs^2 \omega_6 \omega_3 + 2\omega_2^2 v_2^2 \omega_3 - 2\omega_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 \rho}^{(0), \text{CLBM}^2} = (-3\omega_2 v_2^2 \omega_6 \omega_3^2 - 2\omega_2^2 \omega_6 cs^2 + \omega_2 \omega_6 \omega_3^2 cs^2 + 2v_2^2 \omega_6 \omega_3^2 + 4\omega_2^2 \omega_6 \omega_3 cs^2 + \omega_2^2 \omega_3^2 cs^2 + 2\omega_2 v_2^2 \omega_6 \omega_3 + \omega_2^2 v_2^2 \omega_6 \omega_3^2 - \omega_2^2 v_2^2 \omega_3^2 - \omega_2^2 \omega_6 \omega_3^2 cs^2 - 2\omega_2^2 \omega_3 cs^2 - 2\omega_2 \omega_6 \omega_3 cs^2 + 2\omega_2^2 v_2^2 \omega_3 - 2\omega_2^2 v_2^2 \omega_6 \omega_3) \frac{v_1}{2\omega_2^2 \omega_6 \omega_3^2}$$

**coefficient**  $C_{D_x D_y^2 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1 \partial x_2^2}$ :

$$C_{D_x D_y^2 v_1}^{(0), \text{SRT}} = (-3\omega^2 cs^2 + \omega^2 v_2^2 - 24cs^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{MRT}^1} = (-6v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 3\omega_6 \omega_3^2 cs^2 + 12v_2^2 \omega_6 - 12\omega_3 cs^2 + 6\omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 - 12\omega_6 cs^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{MRT}^2} = (6cs^2 \omega_3^2 - 12cs^2 \omega_6 - 6v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 + 12v_2^2 \omega_6 + 18cs^2 \omega_6 \omega_3 - 3cs^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{CLBM}^1} = (18cs^2 \omega_6 \omega_3 - 12cs^2 \omega_3 + 6v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^2 + 6cs^2 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_6 - 12cs^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_x D_y^2 v_1}^{(0), \text{CLBM}^2} = (6v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^2 - 12\omega_3 cs^2 - 12v_2^2 \omega_6 - 3\omega_6 \omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 + 6\omega_3^2 cs^2 - 12\omega_6 cs^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

**coefficient**  $C_{D_x D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_1 \partial x_2^2}$ :

$$C_{D_x D_y^2 v_2}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 v_2 \rho}{6\omega^2}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{MRT}^1} = (-6\omega_2^2 \omega_3 + 6\omega_2^2 + \omega_2^2 \omega_3^2 + 6\omega_3^2 - 6\omega_2 \omega_3^2) \frac{v_1 v_2 \rho}{6\omega_2^2 \omega_3^2}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{MRT}^2} = C_{D_x D_y^2 v_2}^{(0), \text{MRT}^1}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{CLBM}^1} = C_{D_x D_y^2 v_2}^{(0), \text{MRT}^1}$$

$$C_{D_x D_y^2 v_2}^{(0), \text{CLBM}^2} = C_{D_x D_y^2 v_2}^{(0), \text{MRT}^1}$$

**coefficient**  $C_{D_y^3 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_2^3}$ :

$$C_{D_y^3 \rho}^{(0), \text{SRT}} = (6 - 3\omega^2 cs^2 - \omega^2 v_2^2 - 18cs^2 - 6\omega - 6v_2^2 + \omega^2 + 18\omega cs^2 + 6\omega v_2^2) \frac{v_2}{6\omega^2}$$

$$C_{D_y^3 \rho}^{(0), \text{MRT}^1} = (3v_2^2 \omega_6 \omega_3 - 6v_2^2 \omega_3 - v_2^2 \omega_6 \omega_3^2 + 3v_2^2 \omega_3^2 - 3\omega_6 \omega_3^2 cs^2 - 6\omega_3 cs^2 - 3\omega_3^2 - 3\omega_6 \omega_3 + 3\omega_3^2 cs^2 + 15\omega_6 \omega_3 cs^2 - 12\omega_6 cs^2 + 6\omega_3 + \omega_6 \omega_3^2) \frac{v_2}{6\omega_6 \omega_3^2}$$

$$C_{D_y^3 \rho}^{(0), \text{MRT}^2} = (3cs^2 \omega_3^2 - 12cs^2 \omega_6 + 3v_2^2 \omega_6 \omega_3 - 6v_2^2 \omega_3 - v_2^2 \omega_6 \omega_3^2 + 3v_2^2 \omega_3^2 - 6cs^2 \omega_3 - 3\omega_3^2 + 15cs^2 \omega_6 \omega_3 - 3\omega_6 \omega_3 + 6\omega_3 + \omega_6 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2) \frac{v_2}{6\omega_6 \omega_3^2}$$

$$C_{D_y^3 \rho}^{(0), \text{CLBM}^1} = (6 - 3cs^2 \omega_6 \omega_3 + 9cs^2 \omega_3 - v_2^2 \omega_6 \omega_3 + 3v_2^2 \omega_3 + 3v_2^2 \omega_6 - 6v_2^2 + 9cs^2 \omega_6 - 18cs^2 + \omega_6 \omega_3 - 3\omega_6 - 3\omega_3) \frac{v_2}{6\omega_6 \omega_3}$$

$$C_{D_y^3 \rho}^{(0), \text{CLBM}^2} = (6 - v_2^2 \omega_6 \omega_3 + 3v_2^2 \omega_3 + 9\omega_3 cs^2 + 3v_2^2 \omega_6 - 6v_2^2 + \omega_6 \omega_3 - 3\omega_6 \omega_3 cs^2 - 18cs^2 - 3\omega_6 - 3\omega_3 + 9\omega_6 cs^2) \frac{v_2}{6\omega_6 \omega_3}$$

**coefficient**  $C_{D_y^3 v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_2^3}$ :

$$C_{D_y^3 v_2}^{(0), \text{SRT}} = (12 - 3\omega^2 cs^2 - 5\omega^2 v_2^2 - 24cs^2 - 12\omega - 24v_2^2 + 2\omega^2 + 24\omega cs^2 + 24\omega v_2^2) \frac{\rho}{12\omega^2}$$

$$C_{D_y^3 v_2}^{(0), \text{MRT1}} = (18v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 - 5v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 3\omega_6 \omega_3^2 cs^2 - 12v_2^2 \omega_6 - 12\omega_3 cs^2 - 6\omega_3^2 - 6\omega_6 \omega_3 + 6\omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 - 12\omega_6 cs^2 + 12\omega_3 + 2\omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^3 v_2}^{(0), \text{MRT2}} = (6cs^2 \omega_3^2 - 12cs^2 \omega_6 + 18v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 - 5v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 - 12v_2^2 \omega_6 - 6\omega_3^2 + 18cs^2 \omega_6 \omega_3 - 6\omega_6 \omega_3 + 12\omega_3 + 2\omega_6 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^3 v_2}^{(0), \text{CLBM1}} = (18cs^2 \omega_6 \omega_3 - 12cs^2 \omega_3 + 6v_2^2 \omega_6 \omega_3 - 36v_2^2 \omega_3 - 5v_2^2 \omega_6 \omega_3^2 + 18v_2^2 \omega_3^2 + 6cs^2 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_6 - 12cs^2 \omega_6 - 6\omega_3^2 - 6\omega_6 \omega_3 + 12\omega_3 + 2\omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^3 v_2}^{(0), \text{CLBM2}} = (6v_2^2 \omega_6 \omega_3 - 36v_2^2 \omega_3 - 5v_2^2 \omega_6 \omega_3^2 + 18v_2^2 \omega_3^2 - 12\omega_3 cs^2 + 12v_2^2 \omega_6 - 3\omega_6 \omega_3^2 cs^2 - 6\omega_3^2 - 6\omega_6 \omega_3 + 18\omega_6 \omega_3 cs^2 + 6\omega_3^2 cs^2 + 12\omega_3 - 12\omega_6 cs^2 + 2\omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

**coefficient**  $C_{D_t^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial t^2 \partial x_3}$ :

$$C_{D_t^2 D_z v_3}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{\rho}{12\omega^2}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{MRT1}} = (12 + \omega_4^2 - 12\omega_4) \frac{\rho}{12\omega_4^2}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{CLBM1}} = C_{D_t^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_z v_3}^{(0), \text{CLBM2}} = C_{D_t^2 D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x D_z v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial t \partial x_1 \partial x_3}$ :

$$C_{D_t D_x D_z v_1}^{(0), \text{SRT}} = (-6 + 6\omega - \omega^2) \frac{\rho v_3}{3\omega^2}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{MRT1}} = (3\omega_4^2 - 6\omega_4 - 2\omega_4^2 \omega_2 + 9\omega_4 \omega_2 - 6\omega_2) \frac{\rho v_3}{6\omega_4^2 \omega_2}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{MRT2}} = C_{D_t D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_t D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_t D_x D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial t \partial x_1 \partial x_3}$ :

$$C_{D_t D_x D_z v_3}^{(0), \text{SRT}} = (-6 + 6\omega - \omega^2) \frac{v_1 \rho}{3\omega^2}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{MRT1}} = (-6\omega_4 + 3\omega_2^2 + 9\omega_4 \omega_2 - 6\omega_2 - 2\omega_4 \omega_2^2) \frac{v_1 \rho}{6\omega_4 \omega_2^2}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_x D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_x D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x^2 D_z \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1^2 \partial x_3}$ :

$$C_{D_x^2 D_z \rho}^{(0), \text{SRT}} = (-\omega^2 cs^2 + \omega^2 v_1^2 + 6v_1^2 - 6cs^2 - 6\omega v_1^2 + 6\omega cs^2) \frac{v_3}{2\omega^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{MRT}1} = (-2\omega_4^2 \omega_5 cs^2 - \omega_4^2 \omega_5 \omega_2^2 cs^2 + \omega_4^2 v_1^2 \omega_2^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - 2\omega_4^2 \omega_2 cs^2 + 2\omega_5 v_1^2 \omega_2^2 - 2\omega_4 \omega_5 \omega_2 cs^2 - 2\omega_4^2 v_1^2 \omega_2 + \omega_4 \omega_5 \omega_2^2 cs^2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + \omega_4^2 \omega_2^2 cs^2 - 4\omega_4^2 \omega_5 v_1^2 \omega_2 + 4\omega_4^2 \omega_5 v_1^2 + 4\omega_4^2 \omega_5 \omega_2 cs^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{MRT}2} = (\omega_4^2 cs^2 \omega_2^2 + \omega_4^2 v_1^2 \omega_2^2 - 2\omega_4 cs^2 \omega_5 \omega_2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + \omega_4 cs^2 \omega_5 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - 2\omega_4^2 cs^2 \omega_5 + 2\omega_5 v_1^2 \omega_2^2 - 2\omega_4^2 v_1^2 \omega_2 - 2\omega_4^2 cs^2 \omega_2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + 4\omega_4^2 cs^2 \omega_5 \omega_2 - 4\omega_4^2 \omega_5 v_1^2 \omega_2 - \omega_4^2 cs^2 \omega_5 \omega_2^2 + 4\omega_4^2 \omega_5 v_1^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{CLBM}1} = (-\omega_4^2 v_1^2 \omega_2^2 + 4\omega_4^2 \omega_5 \omega_2 cs^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 + \omega_4 \omega_5 \omega_2^2 cs^2 + 2\omega_5 v_1^2 \omega_2^2 + \omega_4^2 \omega_2^2 cs^2 + 2\omega_4^2 v_1^2 \omega_2 - 2\omega_4^2 \omega_2 cs^2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 - 2\omega_4 \omega_5 \omega_2 cs^2 - 2\omega_4^2 \omega_5 cs^2 - 2\omega_4^2 \omega_5 v_1^2 \omega_2 - \omega_4^2 \omega_5 \omega_2^2 cs^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(0), \text{CLBM}2} = (-\omega_4^2 v_1^2 \omega_2^2 - 2\omega_4^2 \omega_5 cs^2 - \omega_4^2 \omega_5 \omega_2^2 cs^2 - 3\omega_4 \omega_5 v_1^2 \omega_2^2 + 2\omega_4 \omega_5 v_1^2 \omega_2 - 2\omega_4 \omega_5 \omega_2 cs^2 + 2\omega_5 v_1^2 \omega_2^2 - 2\omega_4^2 \omega_2 cs^2 + 2\omega_4^2 v_1^2 \omega_2 + \omega_4^2 \omega_2^2 cs^2 + \omega_4^2 \omega_5 v_1^2 \omega_2^2 + \omega_4 \omega_5 \omega_2^2 cs^2 - 2\omega_4^2 \omega_5 v_1^2 \omega_2 + 4\omega_4^2 \omega_5 \omega_2 cs^2) \frac{v_3}{2\omega_4^2 \omega_5 \omega_2^2}$$

**coefficient**  $C_{D_x^2 D_z v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_3}$ :

$$C_{D_x^2 D_z v_1}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 \rho v_3}{6\omega^2}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{MRT}1} = (\omega_4^2 \omega_2^2 + 6\omega_4^2 + 6\omega_2^2 - 6\omega_4^2 \omega_2 - 6\omega_4 \omega_2) \frac{v_1 \rho v_3}{6\omega_4^2 \omega_2^2}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{MRT}2} = C_{D_x^2 D_z v_1}^{(0), \text{MRT}1}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{CLBM}1} = C_{D_x^2 D_z v_1}^{(0), \text{MRT}1}$$

$$C_{D_x^2 D_z v_1}^{(0), \text{CLBM}2} = C_{D_x^2 D_z v_1}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_x^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$ :

$$C_{D_x^2 D_z v_3}^{(0), \text{SRT}} = (-3\omega^2 cs^2 + \omega^2 v_1^2 - 24cs^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{MRT}1} = (18\omega_5 \omega_2 cs^2 + 12\omega_5 v_1^2 - 6\omega_5 v_1^2 \omega_2 + 6\omega_2^2 cs^2 + \omega_5 v_1^2 \omega_2^2 - 12v_1^2 \omega_2 - 12\omega_2 cs^2 + 6v_1^2 \omega_2^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{MRT}2} = (12\omega_5 v_1^2 - 3cs^2 \omega_5 \omega_2^2 - 6\omega_5 v_1^2 \omega_2 + 18cs^2 \omega_5 \omega_2 + \omega_5 v_1^2 \omega_2^2 - 12cs^2 \omega_2 - 12v_1^2 \omega_2 - 12cs^2 \omega_5 + 6v_1^2 \omega_2^2 + 6cs^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{CLBM}1} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2 + \omega_5 v_1^2 \omega_2^2 - 12\omega_2 cs^2 + 6\omega_2^2 cs^2 + 12v_1^2 \omega_2 + 18\omega_5 \omega_2 cs^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

$$C_{D_x^2 D_z v_3}^{(0), \text{CLBM}2} = (-12\omega_5 v_1^2 + 6\omega_5 v_1^2 \omega_2 + 18\omega_5 \omega_2 cs^2 + \omega_5 v_1^2 \omega_2^2 + 6\omega_2^2 cs^2 + 12v_1^2 \omega_2 - 12\omega_2 cs^2 - 3\omega_5 \omega_2^2 cs^2 - 12\omega_5 cs^2 - 6v_1^2 \omega_2^2) \frac{\rho}{12\omega_5 \omega_2^2}$$

**coefficient**  $C_{D_t D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial t \partial x_2 \partial x_3}$ :

$$C_{D_t D_y D_z v_2}^{(0), \text{SRT}} = (-6 + 6\omega - \omega^2) \frac{\rho v_3}{3\omega^2}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{MRT}1} = (3\omega_4^2 - 6\omega_4 + 9\omega_4 \omega_3 - 2\omega_4^2 \omega_3 - 6\omega_3) \frac{\rho v_3}{6\omega_4^2 \omega_3}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{MRT}2} = C_{D_t D_y D_z v_2}^{(0), \text{MRT}1}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{CLBM}1} = C_{D_t D_y D_z v_2}^{(0), \text{MRT}1}$$

$$C_{D_t D_y D_z v_2}^{(0), \text{CLBM}2} = C_{D_t D_y D_z v_2}^{(0), \text{MRT}1}$$

**coefficient**  $C_{D_t D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial t \partial x_2 \partial x_3}$ :

$$C_{D_t D_y D_z v_3}^{(0), \text{SRT}} = (-6 + 6\omega - \omega^2) \frac{v_2 \rho}{3\omega^2}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{MRT1}} = (-2\omega_4 \omega_3^2 - 6\omega_4 + 9\omega_4 \omega_3 + 3\omega_3^2 - 6\omega_3) \frac{v_2 \rho}{6\omega_4 \omega_3^2}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_t D_y D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z \rho}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_1 v_2 v_3}{\omega^2}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{MRT1}} = (\omega_4^2 \omega_2^2 + \omega_4^2 \omega_2 \omega_3 + \omega_4 \omega_2^2 \omega_3 - 2\omega_4 \omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2 - 2\omega_4^2 \omega_2 \omega_3^2 + \omega_4^2 \omega_2^2 \omega_3^2 + \omega_4 \omega_2 \omega_3^2 - 2\omega_4^2 \omega_2^2 \omega_3 + \omega_4^2 \omega_3^2) \frac{2v_1 v_2 v_3}{\omega_4^2 \omega_2^2 \omega_3^2}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{MRT2}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{CLBM1}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z \rho}^{(0), \text{CLBM2}} = C_{D_x D_y D_z \rho}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_1}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_2 \rho v_3}{3\omega^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT1}} = (-6\omega_4 \omega_3^2 + 3\omega_4^2 + 6\omega_4 \omega_3 + 3\omega_3^2 - 6\omega_4^2 \omega_3 + 2\omega_4^2 \omega_3^2) \frac{v_2 \rho v_3}{3\omega_4^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_2}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_1 \rho v_3}{3\omega^2}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT1}} = (2\omega_4^2 \omega_2^2 + 3\omega_4^2 + 3\omega_2^2 - 6\omega_4^2 \omega_2 + 6\omega_4 \omega_2 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{3\omega_4^2 \omega_2^2}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_x D_y D_z v_3}^{(0), \text{SRT}} = (6 - 6\omega + \omega^2) \frac{2v_1 v_2 \rho}{3\omega^2}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{MRT1}} = (-6\omega_2^2 \omega_3 + 3\omega_2^2 + 2\omega_2^2 \omega_3^2 + 3\omega_3^2 - 6\omega_2 \omega_3^2 + 6\omega_2 \omega_3) \frac{v_1 v_2 \rho}{3\omega_2^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM1}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM2}} = C_{D_x D_y D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y^2 D_z \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_2^2 \partial x_3}$ :

$$C_{D_y^2 D_z \rho}^{(0), \text{SRT}} = (-\omega^2 cs^2 + \omega^2 v_2^2 - 6cs^2 + 6v_2^2 + 6\omega cs^2 - 6\omega v_2^2) \frac{v_3}{2\omega^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{MRT1}} = (-3\omega_4 v_2^2 \omega_6 \omega_3^2 + \omega_4 \omega_6 \omega_3^2 cs^2 - 2\omega_4^2 \omega_6 cs^2 + 2v_2^2 \omega_6 \omega_3^2 + 4\omega_4^2 \omega_6 \omega_3 cs^2 + 2\omega_4 v_2^2 \omega_6 \omega_3 + \omega_4^2 \omega_3^2 cs^2 - 2\omega_4^2 \omega_3 cs^2 + 4\omega_4^2 v_2^2 \omega_6 - \omega_4^2 \omega_6 \omega_3^2 cs^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_3^2 - 2\omega_4^2 v_2^2 \omega_3 - 4\omega_4^2 v_2^2 \omega_6 \omega_3 - 2\omega_4 \omega_6 \omega_3 cs^2) \frac{v_3}{2\omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{MRT2}} = (-\omega_4^2 cs^2 \omega_6 \omega_3^2 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + 2\omega_4 v_2^2 \omega_6 \omega_3 + 4\omega_4^2 cs^2 \omega_6 \omega_3 + 4\omega_4^2 v_2^2 \omega_6 - 2\omega_4^2 cs^2 \omega_3 + \omega_4 cs^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 + \omega_4^2 v_2^2 \omega_3^2 - 2\omega_4^2 v_2^2 \omega_3 - 4\omega_4^2 v_2^2 \omega_6 \omega_3 - 2\omega_4^2 cs^2 \omega_6 + \omega_4^2 cs^2 \omega_3^2 - 2\omega_4 cs^2 \omega_6 \omega_3) \frac{v_3}{2\omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{CLBM1}} = (\omega_4 cs^2 \omega_6 \omega_3^2 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + 2\omega_4 v_2^2 \omega_6 \omega_3 - 2\omega_4 cs^2 \omega_6 \omega_3 - 2\omega_4^2 cs^2 \omega_6 - \omega_4^2 cs^2 \omega_6 \omega_3^2 + \omega_4^2 cs^2 \omega_3^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - \omega_4^2 v_2^2 \omega_3^2 + 2\omega_4^2 v_2^2 \omega_3 - 2\omega_4^2 v_2^2 \omega_6 \omega_3 - 2\omega_4^2 cs^2 \omega_3 + 4\omega_4^2 cs^2 \omega_6 \omega_3) \frac{v_3}{2\omega_4^2 \omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(0), \text{CLBM2}} = (\omega_4 \omega_6 \omega_3^2 cs^2 - 2\omega_4^2 \omega_6 cs^2 - 3\omega_4 v_2^2 \omega_6 \omega_3^2 + 2v_2^2 \omega_6 \omega_3^2 + \omega_4^2 \omega_3^2 cs^2 + 2\omega_4 v_2^2 \omega_6 \omega_3 + 4\omega_4^2 \omega_6 \omega_3 cs^2 - \omega_4^2 \omega_6 \omega_3^2 cs^2 - 2\omega_4^2 \omega_3 cs^2 + \omega_4^2 v_2^2 \omega_6 \omega_3^2 - \omega_4^2 v_2^2 \omega_3^2 + 2\omega_4^2 v_2^2 \omega_3 - 2\omega_4^2 v_2^2 \omega_6 \omega_3 - 2\omega_4 \omega_6 \omega_3 cs^2) \frac{v_3}{2\omega_4^2 \omega_6 \omega_3^2}$$

**coefficient**  $C_{D_y^2 D_z v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_2^2 \partial x_3}$ :

$$C_{D_y^2 D_z v_2}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_2 \rho v_3}{6\omega^2}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{MRT1}} = (-6\omega_4 \omega_3^2 + 6\omega_4^2 + 6\omega_3^2 - 6\omega_4^2 \omega_3 + \omega_4^2 \omega_3^2) \frac{v_2 \rho v_3}{6\omega_4^2 \omega_3^2}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{MRT2}} = C_{D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{CLBM1}} = C_{D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(0), \text{CLBM2}} = C_{D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$ :

$$C_{D_y^2 D_z v_3}^{(0), \text{SRT}} = (-3\omega^2 cs^2 + \omega^2 v_2^2 - 24cs^2 + 24\omega cs^2) \frac{\rho}{12\omega^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{MRT1}} = (-6v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 3\omega_6 \omega_3^2 cs^2 + 12v_2^2 \omega_6 - 12\omega_3 cs^2 + 6\omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 - 12\omega_6 cs^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{MRT2}} = (6cs^2 \omega_3^2 - 12cs^2 \omega_6 - 6v_2^2 \omega_6 \omega_3 - 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 + 6v_2^2 \omega_3^2 - 12cs^2 \omega_3 + 12v_2^2 \omega_6 + 18cs^2 \omega_6 \omega_3 - 3cs^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{CLBM1}} = (18cs^2 \omega_6 \omega_3 - 12cs^2 \omega_3 + 6v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^2 + 6cs^2 \omega_3^2 - 3cs^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_6 - 12cs^2 \omega_6) \frac{\rho}{12\omega_6 \omega_3^2}$$

$$C_{D_y^2 D_z v_3}^{(0), \text{CLBM2}} = (6v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_3 + v_2^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^2 - 12\omega_3 cs^2 - 12v_2^2 \omega_6 - 3\omega_6 \omega_3^2 cs^2 + 18\omega_6 \omega_3 cs^2 + 6\omega_3^2 cs^2 - 12\omega_6 cs^2) \frac{\rho}{12\omega_6 \omega_3^2}$$

**coefficient**  $C_{D_t D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial t \partial x_3}$ :

$$C_{D_t D_z^2 v_3}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{\rho v_3}{6\omega^2}$$

$$C_{D_t D_z^2 v_3}^{(0), \text{MRT1}} = (12 - 6\omega_7 - 6\omega_4 + \omega_7 \omega_4) \frac{\rho v_3}{6\omega_7 \omega_4}$$

$$C_{D_t D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_t D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_t D_z^2 v_3}^{(0), \text{CLBM1}} = (12 + \omega_4^2 - 12\omega_4) \frac{\rho v_3}{6\omega_4^2}$$

$$C_{D_t D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_t D_z^2 v_3}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_x D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_1 \partial x_3^2}$ :

$$C_{D_x D_z^2 \rho}^{(0), \text{SRT}} = (-\omega^2 cs^2 - 6\omega v_3^2 - 6cs^2 + 6v_3^2 + 6\omega cs^2 + \omega^2 v_3^2) \frac{v_1}{2\omega^2}$$

$$C_{D_x D_z^2 \rho}^{(0), \text{MRT1}} = (-2\omega_7 \omega_4 \omega_2 cs^2 - 2\omega_7 \omega_2^2 cs^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 4\omega_7 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - \omega_7 \omega_4^2 \omega_2^2 cs^2 - 2\omega_4 \omega_2^2 v_3^2 - 2\omega_4 \omega_2^2 cs^2 + \omega_4^2 \omega_2^2 v_3^2 + \omega_4^2 \omega_2^2 cs^2 + 2\omega_7 \omega_4^2 v_3^2 + \omega_7 \omega_4^2 \omega_2 cs^2 - 4\omega_7 \omega_4 \omega_2^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2 + 4\omega_7 \omega_4 \omega_2^2 cs^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{D_x D_z^2 \rho}^{(0), \text{MRT2}} = (\omega_4^2 cs^2 \omega_2^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 - 2\omega_7 \omega_4 cs^2 \omega_2 + 4\omega_7 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - 2\omega_4 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 cs^2 \omega_2^2 + \omega_4^2 \omega_2^2 v_3^2 - \omega_7 \omega_4^2 cs^2 \omega_2^2 - 2\omega_7 cs^2 \omega_2^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_4 cs^2 \omega_2^2 - 4\omega_7 \omega_4 \omega_2^2 v_3^2 + \omega_7 \omega_4^2 cs^2 \omega_2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{D_x D_z^2 \rho}^{(0), \text{CLBM1}} = (\omega_7 \omega_4^2 \omega_2 cs^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 + 4\omega_7 \omega_4 \omega_2^2 cs^2 + 2\omega_4 \omega_2^2 v_3^2 + \omega_4^2 \omega_2^2 cs^2 - \omega_4^2 \omega_2^2 v_3^2 - 2\omega_4 \omega_2^2 cs^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 \omega_2^2 v_3^2 - 2\omega_7 \omega_2^2 cs^2 - 2\omega_7 \omega_4 \omega_2 cs^2 - \omega_7 \omega_4^2 \omega_2^2 cs^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

$$C_{D_x D_z^2 \rho}^{(0), \text{CLBM2}} = (-\omega_7 \omega_4^2 \omega_2^2 cs^2 + \omega_7 \omega_4^2 \omega_2^2 v_3^2 + 2\omega_7 \omega_4 \omega_2 v_3^2 - 2\omega_7 \omega_4 \omega_2 cs^2 - 2\omega_7 \omega_2^2 cs^2 - 2\omega_4 \omega_2^2 cs^2 + 2\omega_4 \omega_2^2 v_3^2 - \omega_4^2 \omega_2^2 v_3^2 + \omega_4^2 \omega_2^2 cs^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 \omega_2^2 v_3^2 + 4\omega_7 \omega_4 \omega_2^2 cs^2 + \omega_7 \omega_4^2 \omega_2 cs^2 - 3\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{v_1}{2\omega_7 \omega_4^2 \omega_2^2}$$

**coefficient**  $C_{D_x D_z^2 v_1}^{(0)}$  **at**  $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$ :

$$C_{D_x D_z^2 v_1}^{(0), \text{SRT}} = (-3\omega^2 cs^2 - 24cs^2 + 24\omega cs^2 + \omega^2 v_3^2) \frac{\rho}{12\omega^2}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{MRT1}} = (-12\omega_4 v_3^2 - 12\omega_4 cs^2 - 6\omega_7 \omega_4 v_3^2 + 18\omega_7 \omega_4 cs^2 - 12\omega_7 cs^2 - 3\omega_7 \omega_4^2 cs^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 cs^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{MRT2}} = (-12\omega_4 v_3^2 + 18\omega_7 \omega_4 cs^2 - 12\omega_4 cs^2 - 6\omega_7 \omega_4 v_3^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 cs^2 - 12\omega_7 cs^2 - 3\omega_7 \omega_4^2 cs^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{CLBM1}} = (12\omega_4 v_3^2 + 6\omega_4^2 cs^2 - 12\omega_7 cs^2 - 3\omega_7 \omega_4^2 cs^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 v_3^2 + 18\omega_7 \omega_4 cs^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 - 12\omega_4 cs^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{CLBM2}} = (12\omega_4 v_3^2 - 12\omega_4 cs^2 + 18\omega_7 \omega_4 cs^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 cs^2 - 12\omega_7 v_3^2 - 3\omega_7 \omega_4^2 cs^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 + 6\omega_4^2 cs^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

**coefficient**  $C_{D_x D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_1 \partial x_3^2}$ :

$$C_{D_x D_z^2 v_3}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_1 \rho v_3}{6\omega^2}$$

$$C_{D_x D_z^2 v_3}^{(0), \text{MRT1}} = (\omega_4^2 \omega_2^2 + 6\omega_4^2 + 6\omega_2^2 - 6\omega_4^2 \omega_2 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_4^2 \omega_2^2}$$

$$C_{D_x D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_x D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_x D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_x D_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_2 \partial x_3^2}$ :

$$C_{D_y D_z^2 \rho}^{(0), \text{SRT}} = (-\omega^2 cs^2 - 6\omega v_3^2 - 6cs^2 + 6v_3^2 + 6\omega cs^2 + \omega^2 v_3^2) \frac{v_2}{2\omega^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{MRT1}} = (\omega_7 \omega_4^2 \omega_3 cs^2 - 4\omega_7 \omega_4 \omega_3^2 v_3^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 + 4\omega_7 \omega_4 \omega_3^2 cs^2 + \omega_4^2 \omega_3^2 v_3^2 + \omega_4^2 \omega_3^2 cs^2 - 2\omega_4 \omega_3^2 v_3^2 - 2\omega_4 \omega_3^2 cs^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_3^2 cs^2 - 2\omega_7 \omega_4 \omega_3 cs^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 + 4\omega_7 \omega_3^2 v_3^2 - \omega_7 \omega_4^2 \omega_3^2 cs^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{MRT2}} = (\omega_7 \omega_4^2 cs^2 \omega_3 - 4\omega_7 \omega_4 \omega_3^2 v_3^2 - 2\omega_4 cs^2 \omega_3^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 + \omega_4^2 \omega_3^2 v_3^2 - 2\omega_7 cs^2 \omega_3^2 - \omega_7 \omega_4^2 cs^2 \omega_3^2 - 2\omega_4 \omega_3^2 v_3^2 + 4\omega_7 \omega_4 cs^2 \omega_3^2 + 2\omega_7 \omega_4^2 v_3^2 - 2\omega_7 \omega_4 cs^2 \omega_3 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + \omega_4^2 cs^2 \omega_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 + 4\omega_7 \omega_3^2 v_3^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{CLBM1}} = (-2\omega_7 \omega_4 \omega_3^2 v_3^2 - 2\omega_7 c s^2 \omega_3^2 - \omega_7 \omega_4^2 c s^2 \omega_3^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 + \omega_7 \omega_4^2 c s^2 \omega_3 - \omega_4^2 \omega_3^2 v_3^2 - 2\omega_4 c s^2 \omega_3^2 + 2\omega_4 \omega_3^2 v_3^2 - 2\omega_7 \omega_4 c s^2 \omega_3 + \omega_4^2 c s^2 \omega_3^2 + 2\omega_7 \omega_4^2 v_3^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 + 4\omega_7 \omega_4 c s^2 \omega_3^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(0), \text{CLBM2}} = (-2\omega_7 \omega_4 \omega_3^2 v_3^2 + 4\omega_7 \omega_4 \omega_3^2 c s^2 + \omega_7 \omega_4^2 \omega_3 c s^2 - 3\omega_7 \omega_4^2 \omega_3 v_3^2 - \omega_4^2 \omega_3^2 v_3^2 + \omega_4^2 \omega_3^2 c s^2 - 2\omega_4 \omega_3^2 c s^2 + 2\omega_4 \omega_3^2 v_3^2 + 2\omega_7 \omega_4^2 v_3^2 - \omega_7 \omega_4^2 \omega_3^2 c s^2 + \omega_7 \omega_4^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4 \omega_3 v_3^2 - 2\omega_7 \omega_3^2 c s^2 - 2\omega_7 \omega_4 \omega_3 c s^2) \frac{v_2}{2\omega_7 \omega_4^2 \omega_3^2}$$

**coefficient**  $C_{D_y D_z^2 v_2}^{(0)}$  **at**  $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$ :

$$C_{D_y D_z^2 v_2}^{(0), \text{SRT}} = (-3\omega^2 c s^2 - 24c s^2 + 24\omega c s^2 + \omega^2 v_3^2) \frac{\rho}{12\omega^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{MRT1}} = (-12\omega_4 v_3^2 - 12\omega_4 c s^2 - 6\omega_7 \omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{MRT2}} = (-12\omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 - 12\omega_4 c s^2 - 6\omega_7 \omega_4 v_3^2 + 12\omega_7 v_3^2 + \omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{CLBM1}} = (12\omega_4 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 v_3^2 + 18\omega_7 \omega_4 c s^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 - 12\omega_4 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_y D_z^2 v_2}^{(0), \text{CLBM2}} = (12\omega_4 v_3^2 - 12\omega_4 c s^2 + 18\omega_7 \omega_4 c s^2 + 6\omega_7 \omega_4 v_3^2 - 12\omega_7 c s^2 - 12\omega_7 v_3^2 - 3\omega_7 \omega_4^2 c s^2 + \omega_7 \omega_4^2 v_3^2 - 6\omega_4^2 v_3^2 + 6\omega_4^2 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

**coefficient**  $C_{D_y D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_2 \partial x_3^2}$ :

$$C_{D_y D_z^2 v_3}^{(0), \text{SRT}} = (12 - 12\omega + \omega^2) \frac{v_2 \rho v_3}{6\omega^2}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{MRT1}} = (-6\omega_4 \omega_3^2 + 6\omega_4^2 + 6\omega_3^2 - 6\omega_4^2 \omega_3 + \omega_4^2 \omega_3^2) \frac{v_2 \rho v_3}{6\omega_4^2 \omega_3^2}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_y D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_z^3 \rho}^{(0)}$  **at**  $\frac{\partial^3 \rho}{\partial x_3^3}$ :

$$C_{D_z^3 \rho}^{(0), \text{SRT}} = (6 - 3\omega^2 c s^2 + 6\omega v_3^2 - 18c s^2 - 6\omega - 6v_3^2 + \omega^2 + 18\omega c s^2 - \omega^2 v_3^2) \frac{v_3}{6\omega^2}$$

$$C_{D_z^3 \rho}^{(0), \text{MRT1}} = (-6\omega_4 v_3^2 + \omega_7 \omega_4^2 - 3\omega_4^2 + 6\omega_4 - 6\omega_4 c s^2 + 3\omega_7 \omega_4 v_3^2 - 3\omega_7 \omega_4 + 15\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 - \omega_7 \omega_4^2 v_3^2 + 3\omega_4^2 c s^2 + 3\omega_4^2 v_3^2) \frac{v_3}{6\omega_7 \omega_4^2}$$

$$C_{D_z^3 \rho}^{(0), \text{MRT2}} = (-6\omega_4 v_3^2 + 15\omega_7 \omega_4 c s^2 + \omega_7 \omega_4^2 - 3\omega_4^2 + 6\omega_4 - 6\omega_4 c s^2 + 3\omega_7 \omega_4 v_3^2 - 3\omega_7 \omega_4 - \omega_7 \omega_4^2 v_3^2 + 3\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 3\omega_4^2 v_3^2) \frac{v_3}{6\omega_7 \omega_4^2}$$

$$C_{D_z^3 \rho}^{(0), \text{CLBM1}} = (6 + 3\omega_4 v_3^2 - 3\omega_7 - 3\omega_4 + 9\omega_7 c s^2 - \omega_7 \omega_4 v_3^2 + \omega_7 \omega_4 - 18c s^2 - 6v_3^2 + 3\omega_7 v_3^2 - 3\omega_7 \omega_4 c s^2 + 9\omega_4 c s^2) \frac{v_3}{6\omega_7 \omega_4}$$

$$C_{D_z^3 \rho}^{(0), \text{CLBM2}} = (6 + 3\omega_4 v_3^2 - 3\omega_7 + 9\omega_4 c s^2 - 3\omega_4 - 3\omega_7 \omega_4 c s^2 - \omega_7 \omega_4 v_3^2 + \omega_7 \omega_4 - 6v_3^2 - 18c s^2 + 9\omega_7 c s^2 + 3\omega_7 v_3^2) \frac{v_3}{6\omega_7 \omega_4}$$

**coefficient**  $C_{D_z^3 v_3}^{(0)}$  **at**  $\frac{\partial^3 v_3}{\partial x_3^3}$ :

$$C_{D_z^3 v_3}^{(0), \text{SRT}} = (12 - 3\omega^2 c s^2 + 24\omega v_3^2 - 24c s^2 - 12\omega - 24v_3^2 + 2\omega^2 + 24\omega c s^2 - 5\omega^2 v_3^2) \frac{\rho}{12\omega^2}$$

$$C_{D_z^3 v_3}^{(0), \text{MRT1}} =$$

$$(-12\omega_4 v_3^2 + 2\omega_7 \omega_4^2 - 6\omega_4^2 + 12\omega_4 - 12\omega_4 c s^2 + 18\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 + 18\omega_7 \omega_4 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 - 12\omega_7 v_3^2 - 5\omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{D_z^3 v_3}^{(0), \text{MRT2}} =$$

$$(-12\omega_4 v_3^2 + 18\omega_7 \omega_4 c s^2 + 2\omega_7 \omega_4^2 - 6\omega_4^2 + 12\omega_4 - 12\omega_4 c s^2 + 18\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 - 12\omega_7 v_3^2 - 5\omega_7 \omega_4^2 v_3^2 + 6\omega_4^2 c s^2 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_4^2 v_3^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\mathbf{D}_2^3 v_3}^{(0), \text{CLBM1}} = (-36\omega_4 v_3^2 + 2\omega_7 \omega_4^2 + 6\omega_4^2 c s^2 - 6\omega_4^2 + 12\omega_4 - 12\omega_7 c s^2 - 3\omega_7 \omega_4^2 c s^2 + 6\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 + 12\omega_7 v_3^2 + 18\omega_7 \omega_4 c s^2 - 5\omega_7 \omega_4^2 v_3^2 + 18\omega_4^2 v_3^2 - 12\omega_4 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

$$C_{\mathbf{D}_2^3 v_3}^{(0), \text{CLBM2}} = (-36\omega_4 v_3^2 + 2\omega_7 \omega_4^2 - 12\omega_4 c s^2 - 6\omega_4^2 + 12\omega_4 + 18\omega_7 \omega_4 c s^2 + 6\omega_7 \omega_4 v_3^2 - 6\omega_7 \omega_4 - 12\omega_7 c s^2 + 12\omega_7 v_3^2 - 3\omega_7 \omega_4^2 c s^2 - 5\omega_7 \omega_4^2 v_3^2 + 18\omega_4^2 v_3^2 + 6\omega_4^2 c s^2) \frac{\rho}{12\omega_7 \omega_4^2}$$

**coefficient**  $C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t^3 \partial x_1}$ :

$$C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{\rho}{2\omega^3}$$

$$C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{MRT1}} = (-2 - \omega^2 + 3\omega_2) \frac{\rho}{2\omega_2^3}$$

$$C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{MRT2}} = C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{CLBM1}} = C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t^3 \mathbf{D}_x v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t^2 \partial x_1^2}$ :

$$C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{3v_1 \rho}{2\omega^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{MRT1}} = (-2\omega_5 \omega_2^3 + 8\omega_5 \omega_2^2 + 2\omega_5^2 + 2\omega_2^3 - 4\omega_5 \omega_2 - 4\omega_2^2 - \omega_5^2 \omega_2 - \omega_5^2 \omega_2^2) \frac{v_1 \rho}{2\omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{MRT2}} = C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{MRT1}}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{CLBM1}} = (-2 - \omega_2^2 + 3\omega_2) \frac{3v_1 \rho}{2\omega_2^3}$$

$$C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{CLBM2}} = C_{\mathbf{D}_t^2 \mathbf{D}_x^2 v_1}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{\mathbf{D}_t \mathbf{D}_x^3 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1^3}$ :

$$C_{\mathbf{D}_t \mathbf{D}_x^3 v_1}^{(0), \text{SRT}} = (-36 + 34\omega^2 c s^2 + 42\omega^2 v_1^2 + 72v_1^2 - 2\omega^3 c s^2 - 3\omega^3 v_1^2 + 60c s^2 + 54\omega + \omega^3 - 20\omega^2 - 108\omega v_1^2 - 90\omega c s^2) \frac{\rho}{12\omega^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^3 v_1}^{(0), \text{MRT1}} = (24\omega_5 \omega_2 c s^2 - 9\omega_5 \omega_2^3 - 6\omega_2^3 c s^2 + 24\omega_5^2 c s^2 + 25\omega_5^2 \omega_2^2 c s^2 + 36\omega_5 \omega_2^2 + 48\omega_5 v_1^2 \omega_2 + 6\omega_2^3 - 24\omega_5 \omega_2 + 12\omega_2^2 c s^2 - 60\omega_5 v_1^2 \omega_2^2 - 12\omega_2^2 + 15\omega_5 v_1^2 \omega_2^3 - 2\omega_5^2 \omega_2^3 c s^2 + 27\omega_5^2 v_1^2 \omega_2^2 + 12\omega_5^2 \omega_2 + 9\omega_5 \omega_2^3 c s^2 - 3\omega_5^2 v_1^2 \omega_2^3 - 11\omega_5^2 \omega_2^2 - 48\omega_5^2 \omega_2 c s^2 - 6v_1^2 \omega_2^3 + 12v_1^2 \omega_2^2 - 42\omega_5^2 v_1^2 \omega_2 + \omega_5^2 \omega_2^3 - 36\omega_5 \omega_2^2 c s^2 + 12\omega_5^2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^3 v_1}^{(0), \text{MRT2}} = (9c s^2 \omega_5 \omega_2^3 - 9\omega_5 \omega_2^3 - 36c s^2 \omega_5 \omega_2^2 + 36\omega_5 \omega_2^2 + 48\omega_5 v_1^2 \omega_2 + 6\omega_2^3 - 24\omega_5 \omega_2 + 24c s^2 \omega_5 \omega_2 - 60\omega_5 v_1^2 \omega_2^2 - 12\omega_2^2 + 15\omega_5 v_1^2 \omega_2^3 + 27\omega_5^2 v_1^2 \omega_2^2 - 48c s^2 \omega_5^2 \omega_2 + 12\omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 - 11\omega_5^2 \omega_2^2 + 25c s^2 \omega_5^2 \omega_2^2 - 6v_1^2 \omega_2^3 - 6c s^2 \omega_2^3 + 24c s^2 \omega_5^2 + 12v_1^2 \omega_2^2 - 42\omega_5^2 v_1^2 \omega_2 + \omega_5^2 \omega_2^3 - 2c s^2 \omega_5^2 \omega_2^3 + 12\omega_5^2 v_1^2 + 12c s^2 \omega_2^2) \frac{\rho}{12\omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^3 v_1}^{(0), \text{CLBM1}} = (-48\omega_5^2 \omega_2 c s^2 - 9\omega_5 \omega_2^3 + 36\omega_5 \omega_2^2 + 72\omega_5 v_1^2 \omega_2 - 36\omega_5 \omega_2^2 c s^2 + 6\omega_2^3 - 24\omega_5 \omega_2 - 108\omega_5 v_1^2 \omega_2^2 - 12\omega_2^2 + 9\omega_5 \omega_2^3 c s^2 + 27\omega_5 v_1^2 \omega_2^3 + 12\omega_2^2 c s^2 + 15\omega_5^2 v_1^2 \omega_2^2 + 12\omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 - 2\omega_5^2 \omega_2^3 c s^2 - 11\omega_5^2 \omega_2^2 - 6\omega_2^3 c s^2 + 24\omega_5 \omega_2 c s^2 - 18v_1^2 \omega_2^3 + 24\omega_5^2 c s^2 + 36v_1^2 \omega_2^2 + 18\omega_5^2 v_1^2 \omega_2 + 25\omega_5^2 \omega_2^2 c s^2 + \omega_5^2 \omega_2^3 - 36\omega_5^2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_x^3 v_1}^{(0), \text{CLBM2}} = (25\omega_5^2 \omega_2^2 c s^2 - 9\omega_5 \omega_2^3 + 36\omega_5 \omega_2^2 + 72\omega_5 v_1^2 \omega_2 - 6\omega_2^3 c s^2 + 24\omega_5 \omega_2 c s^2 + 24\omega_5^2 c s^2 + 6\omega_2^3 - 24\omega_5 \omega_2 - 108\omega_5 v_1^2 \omega_2^2 - 2\omega_5^2 \omega_2^3 c s^2 - 12\omega_2^2 + 12\omega_2^2 c s^2 + 27\omega_5 v_1^2 \omega_2^3 + 9\omega_5 \omega_2^3 c s^2 + 15\omega_5^2 v_1^2 \omega_2^2 + 12\omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 - 11\omega_5^2 \omega_2^2 - 36\omega_5 \omega_2^2 c s^2 - 18v_1^2 \omega_2^3 - 48\omega_5^2 \omega_2 c s^2 + 36v_1^2 \omega_2^2 + 18\omega_5^2 v_1^2 \omega_2 + \omega_5^2 \omega_2^3 - 36\omega_5^2 v_1^2) \frac{\rho}{12\omega_5^2 \omega_2^3}$$

**coefficient**  $C_{\mathbf{D}_x^4 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1^4}$ :

$$C_{D_x^4 \rho}^{(0), \text{SRT}} = (-14\omega^2 cs^2 - 84\omega^2 v_1^2 cs^2 + 108\omega v_1^4 - 72\omega cs^4 + 42\omega^2 v_1^2 + 72v_1^2 + \omega^3 cs^2 - 3\omega^3 v_1^2 - 24cs^2 - 72v_1^4 - 3\omega^3 cs^4 + 3\omega^3 v_1^4 + 6\omega^3 v_1^2 cs^2 + 48cs^4 + 216\omega v_1^2 cs^2 + 30\omega^2 cs^4 - 108\omega v_1^2 + 36\omega cs^2 - 42\omega^2 v_1^4 - 144v_1^2 cs^2) \frac{1}{24\omega^3}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT1}} = (-24\omega_5 \omega_2 cs^2 - 48\omega_5^2 \omega_2 cs^4 + 48\omega_5 v_1^2 \omega_2^2 cs^2 + 3\omega_5^2 v_1^4 \omega_2^3 - 8\omega_5^2 \omega_2^3 cs^2 + 48\omega_5 v_1^2 \omega_2 - 24\omega_5^2 v_1^4 \omega_2^2 + 12v_1^2 \omega_2^3 cs^2 - 24\omega_5 \omega_2^2 cs^4 - 24v_1^4 \omega_2^2 + 24\omega_5^2 v_1^4 \omega_2 - 12\omega_5 v_1^2 \omega_2^3 cs^2 - 96\omega_5^2 v_1^2 \omega_2^3 cs^2 - 72\omega_5 v_1^2 \omega_2^2 - 24v_1^2 \omega_2^3 cs^2 + 6\omega_5 \omega_2^3 cs^4 + 156\omega_5^2 v_1^2 \omega_2 cs^2 + 12v_1^4 \omega_2^3 + 18\omega_5 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 - 48\omega_5 v_1^4 \omega_2 - 72\omega_5^2 v_1^2 \omega_2^2 cs^2 + 24\omega_5^2 v_1^2 \omega_2^2 - 3\omega_5^2 \omega_2^3 cs^4 - 6\omega_5 \omega_2^3 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + 12\omega_5^2 \omega_2 cs^2 + 24\omega_5^2 cs^4 - 12v_1^2 \omega_2^3 - 18\omega_5 v_1^4 \omega_2^3 + 6\omega_5^2 v_1^2 \omega_2^3 cs^2 + 24\omega_5 \omega_2 cs^4 + 24v_1^2 \omega_2^2 - 24\omega_5^2 v_1^2 \omega_2 + 24\omega_5 \omega_2^2 cs^2 + 24\omega_5^2 \omega_2^2 cs^4 - 24\omega_5 v_1^2 \omega_2 cs^2 + 72\omega_5 v_1^4 \omega_2^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT2}} = (-6cs^2 \omega_5 \omega_2^3 + 24cs^4 \omega_5 \omega_2 + 3\omega_5^2 v_1^4 \omega_2^3 + 24cs^2 \omega_5 \omega_2^2 + 48\omega_5 v_1^2 \omega_2 - 24cs^2 \omega_5 v_1^2 \omega_2 - 24\omega_5^2 v_1^4 \omega_2^2 - 24v_1^4 \omega_2^2 + 24\omega_5^2 v_1^4 \omega_2 + 6cs^4 \omega_5 \omega_2^3 - 24cs^2 \omega_5 \omega_2 - 72\omega_5 v_1^2 \omega_2^2 + 48cs^2 \omega_5 v_1^2 \omega_2^2 - 24cs^4 \omega_5 \omega_2^2 + 12v_1^4 \omega_2^3 - 12cs^2 \omega_5 v_1^2 \omega_2^3 + 18\omega_5 v_1^2 \omega_2^3 + 24cs^4 \omega_5^2 + 24cs^4 \omega_5^2 \omega_2^2 - 48\omega_5 v_1^4 \omega_2 - 72cs^2 \omega_5^2 v_1^2 \omega_2^2 + 24\omega_5^2 v_1^2 \omega_2^2 - 3cs^4 \omega_5^2 \omega_2^2 + 12cs^2 \omega_5^2 \omega_2 - 3\omega_5^2 v_1^2 \omega_2^3 + 6cs^2 \omega_5^2 v_1^2 \omega_2^3 - 8cs^2 \omega_5^2 \omega_2^2 - 12v_1^2 \omega_2^3 + 12cs^2 v_1^2 \omega_2^3 - 18\omega_5 v_1^4 \omega_2^3 + 24v_1^2 \omega_2^2 - 24cs^2 v_1^2 \omega_2^2 + 156cs^2 \omega_5^2 v_1^2 \omega_2 - 24\omega_5^2 v_1^2 \omega_2 + cs^2 \omega_5^2 \omega_2^3 - 96cs^2 \omega_5^2 v_1^2 - 48cs^4 \omega_5^2 \omega_2 + 72\omega_5 v_1^4 \omega_2^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM1}} = (12\omega_5^2 \omega_2 cs^2 + 24\omega_5^2 cs^4 + 6\omega_5^2 v_1^2 \omega_2^3 cs^2 + 3\omega_5^2 v_1^4 \omega_2^3 + 24\omega_5 \omega_2 cs^4 + 24\omega_5 \omega_2^2 cs^2 - 12\omega_5^2 v_1^4 \omega_2^2 + 72\omega_5 v_1^2 \omega_2 cs^2 + 24\omega_5^2 \omega_2^2 cs^4 - 72v_1^4 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2^3 cs^2 - 72\omega_5 v_1^2 \omega_2^2 - 3\omega_5^2 \omega_2^3 cs^4 + 36v_1^4 \omega_2^3 - 6\omega_5 \omega_2^3 cs^2 + 30\omega_5 v_1^2 \omega_2^3 - 72\omega_5 v_1^2 \omega_2^3 cs^2 + 12\omega_5^2 v_1^2 \omega_2^2 + 6\omega_5 \omega_2^3 cs^4 - 216v_1^2 \omega_2^2 cs^2 - 36\omega_5^2 v_1^2 \omega_2 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 - 24\omega_5 \omega_2 cs^2 - 36v_1^2 \omega_2^2 + 144\omega_5 v_1^2 \omega_2^2 cs^2 - 48\omega_5^2 \omega_2 cs^4 - 30\omega_5 v_1^4 \omega_2^3 + 72v_1^2 \omega_2^2 - 8\omega_5^2 \omega_2^3 cs^2 + 72\omega_5 v_1^4 \omega_2^2 - 24\omega_5 \omega_2^2 cs^4 + 108v_1^2 \omega_2^3 cs^2) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM2}} = (-8\omega_5^2 \omega_2^2 cs^2 + 3\omega_5^2 v_1^4 \omega_2^3 - 24\omega_5 \omega_2^2 cs^4 + 108v_1^2 \omega_2^3 cs^2 - 24\omega_5 \omega_2 cs^2 - 48\omega_5^2 \omega_2 cs^4 + 144\omega_5 v_1^2 \omega_2^2 cs^2 - 12\omega_5^2 v_1^4 \omega_2^2 + 6\omega_5 \omega_2^3 cs^4 - 72v_1^4 \omega_2^2 - 216v_1^2 \omega_2^3 cs^2 - 36\omega_5^2 v_1^2 \omega_2 cs^2 - 72\omega_5 v_1^2 \omega_2^2 + \omega_5^2 \omega_2^3 cs^2 - 72\omega_5 v_1^2 \omega_2^3 cs^2 + 36v_1^4 \omega_2^3 + 30\omega_5 v_1^2 \omega_2^3 - 3\omega_5^2 \omega_2^3 cs^4 - 6\omega_5 \omega_2^3 cs^2 + 12\omega_5^2 v_1^2 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2^2 cs^2 - 3\omega_5^2 v_1^2 \omega_2^3 + 24\omega_5 \omega_2^2 cs^2 - 36v_1^2 \omega_2^2 - 30\omega_5 v_1^4 \omega_2^3 + 24\omega_5^2 \omega_2^2 cs^4 + 72\omega_5 v_1^2 \omega_2 cs^2 + 12\omega_5^2 \omega_2 cs^2 + 72v_1^4 \omega_2^2 + 24\omega_5^2 cs^4 + 6\omega_5^2 v_1^2 \omega_2^3 cs^2 + 72\omega_5 v_1^4 \omega_2^2 + 24\omega_5 \omega_2 cs^4) \frac{1}{24\omega_5^2 \omega_2^3}$$

$$\text{coefficient } C_{D_x^4 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^4} :$$

$$C_{D_x^4 v_1}^{(0), \text{SRT}} = (24 - 26\omega^2 cs^2 - 22\omega^2 v_1^2 - 36v_1^2 + \omega^3 cs^2 + 2\omega^3 v_1^2 - 48cs^2 - 36\omega - \omega^3 + 14\omega^2 + 54\omega v_1^2 + 72\omega cs^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT1}} = (-12\omega_5 \omega_2 cs^2 + 6\omega_5 \omega_2^3 + 6\omega_2^3 cs^2 - 24\omega_5^2 cs^2 - 20\omega_5^2 \omega_2^2 cs^2 - 24\omega_5 \omega_2^2 - 12\omega_5 v_1^2 \omega_2 - 6\omega_2^3 + 12\omega_5 \omega_2 - 12\omega_2^2 cs^2 + 24\omega_5 v_1^2 \omega_2^2 + 12\omega_2^2 - 6\omega_5 v_1^2 \omega_2^3 + \omega_5^2 \omega_2^3 cs^2 - 16\omega_5^2 v_1^2 \omega_2^2 - 6\omega_5^2 \omega_2 - 6\omega_5 \omega_2^3 cs^2 + 2\omega_5^2 v_1^2 \omega_2^2 + 8\omega_5^2 \omega_2^2 + 42\omega_5^2 \omega_2 cs^2 + 6v_1^2 \omega_2^3 - 12v_1^2 \omega_2^2 + 24\omega_5^2 v_1^2 \omega_2 - \omega_5^2 \omega_2^3 + 24\omega_5 \omega_2^2 cs^2 - 12\omega_5^2 v_1^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT2}} = (-6cs^2 \omega_5 \omega_2^3 + 6\omega_5 \omega_2^3 + 24cs^2 \omega_5 \omega_2^2 - 24\omega_5 \omega_2^2 - 12\omega_5 v_1^2 \omega_2 - 6\omega_2^3 + 12\omega_5 \omega_2 - 12cs^2 \omega_5 \omega_2 + 24\omega_5 v_1^2 \omega_2^2 + 12\omega_2^2 - 6\omega_5 v_1^2 \omega_2^3 - 16\omega_5^2 v_1^2 \omega_2^2 + 42cs^2 \omega_5^2 \omega_2 - 6\omega_5^2 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^2 + 8\omega_5^2 \omega_2^2 - 20cs^2 \omega_5^2 \omega_2^2 + 6v_1^2 \omega_2^3 + 6cs^2 \omega_2^3 - 24cs^2 \omega_5^2 - 12v_1^2 \omega_2^2 + 24\omega_5^2 v_1^2 \omega_2 - \omega_5^2 \omega_2^3 + cs^2 \omega_5^2 \omega_2^3 - 12\omega_5^2 v_1^2 - 12cs^2 \omega_2^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM1}} = (-30\omega_5^2 \omega_2 cs^2 + 12\omega_5 \omega_2^3 - 24\omega_5 \omega_2^2 + 60\omega_5 v_1^2 \omega_2 + 72\omega_5 \omega_2^2 cs^2 - 18\omega_2^3 - 12\omega_5 \omega_2 + 24\omega_5 v_1^2 \omega_2^2 + 36\omega_2^2 - 24\omega_5 \omega_2^3 cs^2 - 24\omega_5 v_1^2 \omega_2^3 - 60\omega_2^2 cs^2 + 2\omega_5^2 v_1^2 \omega_2^2 + 6\omega_5^2 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^2 + \omega_5^2 \omega_2^3 cs^2 + 2\omega_5^2 \omega_2^2 + 30\omega_2^3 cs^2 - 12\omega_5 \omega_2 cs^2 + 42v_1^2 \omega_2^3 + 24\omega_5^2 cs^2 - 84v_1^2 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2 - 2\omega_5^2 \omega_2^2 cs^2 - \omega_5^2 \omega_2^3 - 12\omega_5^2 v_1^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM2}} = (-2\omega_5^2 \omega_2^2 cs^2 + 12\omega_5 \omega_2^3 - 24\omega_5 \omega_2^2 + 60\omega_5 v_1^2 \omega_2 + 30\omega_2^3 cs^2 - 12\omega_5 \omega_2 cs^2 + 24\omega_5^2 cs^2 - 18\omega_2^3 - 12\omega_5 \omega_2 + 24\omega_5 v_1^2 \omega_2^2 + \omega_5^2 \omega_2^3 cs^2 + 36\omega_2^3 - 60\omega_2^2 cs^2 - 24\omega_5 v_1^2 \omega_2^3 - 24\omega_5 \omega_2^3 cs^2 + 2\omega_5^2 v_1^2 \omega_2^2 + 6\omega_5^2 \omega_2 + 2\omega_5^2 v_1^2 \omega_2^2 + 2\omega_5^2 \omega_2^2 + 72\omega_5 \omega_2^2 cs^2 + 42v_1^2 \omega_2^3 - 30\omega_5^2 \omega_2 cs^2 - 84v_1^2 \omega_2^2 - 12\omega_5^2 v_1^2 \omega_2 - \omega_5^2 \omega_2^3 - 12\omega_5^2 v_1^2) \frac{v_1 \rho}{12\omega_5^2 \omega_2^3}$$

$$\text{coefficient } C_{D_t^3 D_y v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial t^3 \partial x_2} :$$

$$C_{D_t^3 D_y v_2}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{MRT1}} = (-2 - \omega_3^2 + 3\omega_3) \frac{\rho}{2\omega_3^3}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{MRT2}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{CLBM1}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^3 D_y v_2}^{(0), \text{CLBM2}} = C_{D_t^3 D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t^2 D_x D_y v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_2}$ :

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}} = (-24\omega^2 \omega_3 - \omega_2^2 \omega_3^3 + 12\omega_2^2 + 13\omega_2^2 \omega_3^2 + 12\omega_3^2 - 24\omega_2 \omega_3^2 + 7\omega_2 \omega_3^3 - 6\omega_3^3 + 12\omega_2 \omega_3) \frac{v_2 \rho}{12\omega_2^2 \omega_3^3}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_y v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t^2 D_x D_y v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t^2 \partial x_1 \partial x_2}$ :

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}} = (-24\omega^2 \omega_3 - \omega_2^2 \omega_3^3 + 7\omega_2^3 \omega_3 - 6\omega_2^2 + 12\omega_2^2 + 13\omega_2^2 \omega_3^2 + 12\omega_3^2 - 24\omega_2 \omega_3^2 + 12\omega_2 \omega_3) \frac{v_1 \rho}{12\omega_2^2 \omega_3^3}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_y v_2}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_y v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x^2 D_y v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_2}$ :

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 v_2 \rho}{6\omega^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{MRT1}} = (-6\omega_5 \omega_2^3 + 3\omega_2^3 \omega_3^3 + 24\omega_5 \omega_2 \omega_3^3 - 12\omega_5 \omega_2 \omega_3^3 - 6\omega_2^3 \omega_3^3 - 6\omega_2^2 \omega_3^3 + 12\omega_2^2 \omega_3^3 - 7\omega_5 \omega_2^3 \omega_3^3 + \omega_5 \omega_2^3 \omega_3^3 - 6\omega_5 \omega_2^2 \omega_3 + 12\omega_5 \omega_2^2 \omega_3^2 - 12\omega_5 \omega_3^3 - 10\omega_5 \omega_2^2 \omega_3^3 + 12\omega_5 \omega_2^3 \omega_3^3) \frac{v_1 v_2 \rho}{6\omega_5 \omega_2^3 \omega_3^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 D_y v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{CLBM1}} = (\omega_2^3 \omega_3^3 - 6\omega_2^2 \omega_3 - 7\omega_2^3 \omega_3^2 - 7\omega_2^2 \omega_3^3 + 12\omega_2^3 \omega_3 - 6\omega_2^2 + 6\omega_2^2 \omega_3^2 + 18\omega_2 \omega_3^3 - 12\omega_3^3) \frac{v_1 v_2 \rho}{6\omega_2^3 \omega_3^3}$$

$$C_{D_t D_x^2 D_y v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 D_y v_1}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_t D_x^2 D_y v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t \partial x_1^2 \partial x_2}$ :

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{SRT}} = (34\omega^2 cs^2 - 2\omega^2 v_1^2 - 2\omega^3 cs^2 + \omega^3 v_1^2 + 60cs^2 - 90\omega cs^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{MRT1}} = (12\omega_5^2 \omega_3 cs^2 + 9\omega_5 v_1^2 \omega_3^2 \omega_3 - 24\omega_5^2 v_1^2 \omega_3 + 12\omega_5 \omega_2 \omega_3 cs^2 - 18\omega_5^2 \omega_2^2 cs^2 + 36\omega_5^2 v_1^2 \omega_2 \omega_3 + 12v_1^2 \omega_2^2 \omega_3 - 6\omega_2^3 \omega_3 cs^2 + 12\omega_5 v_1^2 \omega_2^2 + 9\omega_5 \omega_2^3 \omega_3 cs^2 - 30\omega_5 v_1^2 \omega_2^2 \omega_3 - 6v_1^2 \omega_2^3 \omega_3 + 22\omega_5^2 \omega_2^2 \omega_3 cs^2 - 6\omega_5 v_1^2 \omega_2^3 + 3\omega_5^2 \omega_2^3 cs^2 + 6\omega_5^2 v_1^2 \omega_2^2 + 12\omega_2^2 \omega_3 cs^2 + \omega_5^2 v_1^2 \omega_2^3 \omega_3 - 6\omega_5 \omega_2^3 cs^2 - 30\omega_5^2 \omega_2 \omega_3 cs^2 + 12\omega_5 v_1^2 \omega_2 \omega_3 - \omega_5^2 v_1^2 \omega_2^3 - 2\omega_5^2 \omega_2^3 \omega_3 cs^2 + 12\omega_5^2 \omega_2 cs^2 - 10\omega_5^2 v_1^2 \omega_2^2 \omega_3 - 12\omega_5^2 v_1^2 \omega_2 - 30\omega_5 \omega_2^2 \omega_3 cs^2 + 12\omega_5 \omega_2^2 cs^2) \frac{\rho}{12\omega_5^2 \omega_2^3 \omega_3}$$

$$C_{D_t D_x^2 D_y v_2}^{(0), \text{MRT2}} = (9\omega_5 v_1^2 \omega_2^3 \omega_3 - 24\omega_5^2 v_1^2 \omega_3 - 6cs^2 \omega_5 \omega_2^3 + 12cs^2 \omega_2^2 \omega_3 + 36\omega_5^2 v_1^2 \omega_2 \omega_3 + 12cs^2 \omega_5 \omega_2^2 + 12v_1^2 \omega_2^2 \omega_3 - 2cs^2 \omega_5^2 \omega_2^3 \omega_3 - 6cs^2 \omega_2^3 \omega_3 + 12cs^2 \omega_5 \omega_2 \omega_3 + 12cs^2 \omega_5^2 \omega_3 + 12\omega_5 v_1^2 \omega_2^2 - 30\omega_5 v_1^2 \omega_2^2 \omega_3 + 22cs^2 \omega_5^2 \omega_2^2 \omega_3 - 6v_1^2 \omega_2^3 \omega_3 - 6\omega_5 v_1^2 \omega_2^3 - 30cs^2 \omega_5^2 \omega_2 \omega_3 + 6\omega_5^2 v_1^2 \omega_2^2 + \omega_5^2 v_1^2 \omega_2^3 \omega_3 - 30cs^2 \omega_5 \omega_2^2 \omega_3 + 12cs^2 \omega_5^2 \omega_2 + 12\omega_5 v_1^2 \omega_2 \omega_3 - \omega_5^2 v_1^2 \omega_2^3 - 18cs^2 \omega_2^3 \omega_2^2 - 10\omega_5^2 v_1^2 \omega_2^2 \omega_3 - 12\omega_5^2 v_1^2 \omega_2 + 3cs^2 \omega_5^2 \omega_2^3 + 9cs^2 \omega_5 \omega_2^3 \omega_3) \frac{\rho}{12\omega_5^2 \omega_2^3 \omega_3}$$

$$C_{\text{D}_t \text{D}_x^2 \text{D}_y v_2}^{(0), \text{CLB M2}} = (12\omega_5\omega_2\omega_3cs^2 - 9\omega_5v_1^2\omega_2^2\omega_3 + 24\omega_5^2v_1^2\omega_3 - 18\omega_5^2\omega_2^2cs^2 - 6\omega_2^2\omega_3cs^2 - 36\omega_5^2v_1^2\omega_2\omega_3 + 12\omega_5^2\omega_3cs^2 - 12v_1^2\omega_2^2\omega_3 + 22\omega_5^2\omega_2^2\omega_3cs^2 - 12\omega_5v_1^2\omega_2^2 + 3\omega_5^2\omega_3^2cs^2 + 30\omega_5v_1^2\omega_2^2\omega_3 + 6v_1^2\omega_3^2\omega_3 + 6\omega_5v_1^2\omega_2^2 + 9\omega_5\omega_2^2\omega_3cs^2 - 6\omega_5\omega_2^2cs^2 - 6\omega_5^2v_1^2\omega_2^2 - 30\omega_5^2\omega_2\omega_3cs^2 + \omega_5^2v_1^2\omega_2^2\omega_3 - 12\omega_5v_1^2\omega_2\omega_3 - \omega_5^2v_1^2\omega_2^2 + 12\omega_2^2\omega_3cs^2 + 8\omega_5^2v_1^2\omega_2^2\omega_3 - 30\omega_5\omega_2^2\omega_3cs^2 + 12\omega_5\omega_2^2cs^2 + 12\omega_5^2\omega_2cs^2 + 12\omega_5^2v_1^2\omega_2 - 2\omega_5^2\omega_2^2\omega_3cs^2) \frac{\rho}{12\omega_5^2\omega_2^2\omega_3}$$

$$C_{\text{D}_x\text{D}_y\rho}^{(0),\text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_1 v_2}{6\omega^3}$$

$$C_{(0),MRT2}^{(0),DPR} = (42\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 36cs^2 \omega_2^2 \omega_3^2 - 24cs^2 \omega_5 \omega_2 \omega_3^2 - 3\omega_2^2 \omega_3^2 - 3\omega_2^2 \omega_2^2 \omega_3^2 + 6cs^2 \omega_3^2 \omega_3^2 + 12\omega_5 \omega_2 \omega_3^2 + 42cs^2 \omega_5^2 \omega_2^2 \omega_3^2 - 12\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 6v_1^2 \omega_2^2 \omega_3^2 - 48cs^2 \omega_5^2 \omega_2^2 \omega_3^2 + 7\omega_2^2 \omega_2^2 \omega_3^2 + 6cs^2 \omega_2^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_2^2 \omega_2^2 \omega_3^2 + \omega_5^2 \omega_2^2 \omega_3^2 + 6\omega_2^2 \omega_3^2 - 12cs^2 \omega_2^2 \omega_2^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 12\omega_5 v_1^2 \omega_2^2 \omega_3^2 + 24\omega_5^2 v_1^2 \omega_3^2 + 6cs^2 \omega_5^2 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5^2 \omega_2^2 \omega_3^2 - \omega_5^2 \omega_2^2 \omega_3^2 - 12v_1^2 \omega_1^2 \omega_2^2 \omega_3^2 + 6\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 30\omega_5^2 v_1^2 \omega_2 \omega_3^2 + 6cs^2 \omega_5 \omega_2^2 \omega_3^2 - 3\omega_5 \omega_2^2 \omega_3^2 + 6\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 12\omega_5^2 v_1^2 \omega_2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - 12cs^2 \omega_5 \omega_2^2 \omega_3^2 + 78cs^2 \omega_5^2 \omega_2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - 24\omega_5 v_1^2 \omega_2 \omega_3^2 + 6\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 21\omega_5 \omega_2^2 \omega_3^2 - 24cs^2 \omega_5^2 \omega_2 \omega_3^2 + 42cs^2 \omega_5 \omega_2^2 \omega_3^2) \frac{v_1 v_2}{6\omega_5^2 \omega_2^2 \omega_3^2}$$

$$C_{D_{\mathbf{x}} D_{\mathbf{y}} \rho}^{(0), \text{CLBMM}} = (12\omega_5 v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5 c s^2 \omega_3^3 - 3\omega_3^2 \omega_3^3 - 3\omega_5^2 \omega_2^3 \omega_3^3 + 12\omega_5 \omega_2 \omega_3^3 + 18\omega_3^2 c s^2 \omega_3^3 - 12\omega_5^2 \omega_2^3 c s^2 \omega_3 - 24\omega_5 \omega_2 c s^2 \omega_3^3 - 6v_1^2 \omega_3^3 \omega_3^3 + 6\omega_3^2 \omega_2^3 \omega_3^3 + 6\omega_2^3 \omega_3^3 - 24\omega_5 \omega_2^3 c s^2 \omega_3^3 + 36\omega_2^3 \omega_2^3 c s^2 \omega_3^3 - \omega_5^2 \omega_2^3 \omega_3^3 + 12v_1^2 \omega_2^3 \omega_3^3 + 12\omega_5 \omega_2^3 c s^2 \omega_3^3 - 36\omega_5^2 \omega_2^3 c s^2 \omega_3^3 + 12\omega_5^2 v_1^2 \omega_2 \omega_3^3 - 3\omega_5 \omega_3^3 \omega_2^3 + 6\omega_2^3 \omega_3^2 c s^2 \omega_3 - 36\omega_2^2 c s^2 \omega_3^3 - 6\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5^2 \omega_2 c s^2 \omega_3^3 - 12\omega_5^2 v_1^2 \omega_2^3 \omega_3 + 6\omega_5 \omega_3^3 \omega_2^3 + 36\omega_2^2 \omega_2 c s^2 \omega_3^3 - 6\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 + 6\omega_5^2 v_1^2 \omega_2^3 + 6\omega_2^2 v_1^2 \omega_2^3 \omega_3 + 6\omega_5^2 \omega_2^3 c s^2 \omega_3^3 - 24\omega_5 \omega_2^2 c s^2 \omega_3^3 - 6\omega_5^2 \omega_2 \omega_3^3 + 6\omega_5 \omega_2^2 \omega_3^3 - 12\omega_5^2 \omega_2^3 c s^2 \omega_3^3 + 72\omega_5 \omega_2^2 c s^2 \omega_3^3 - 24\omega_5 v_1^2 \omega_2 \omega_3^3 + 6\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 21\omega_5 \omega_2^3 \omega_3^3) \frac{v_1 v_2}{6\omega_2^3 \omega_3^3}$$

$$C_{\vec{D}, \vec{\nu} \rho \nu}^{(0), \text{CLMB2}} = (-12\omega_2^2 \omega_3^2 \omega_3^2 \text{cs}^2 - 36\omega_2^2 \omega_3^2 \text{cs}^2 + 12\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 3\omega_2^2 \omega_3^2 - 3\omega_5^2 \omega_2^2 \omega_3^2 + 12\omega_5 \omega_2 \omega_3^2 + 36\omega_5^2 \omega_2 \omega_3^2 \text{cs}^2 - 24\omega_5 \omega_2^2 \omega_3^2 \text{cs}^2 - 6v_1^2 \omega_3^2 \omega_3^2 + 7\omega_5^2 \omega_2^2 \omega_3^2 + \omega_2^2 \omega_3^2 \omega_3^2 + 6\omega_2^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 \omega_3 \text{cs}^2 + 6\omega_5^2 \omega_3^2 \omega_3^2 \text{cs}^2 - \omega_5^2 \omega_3^2 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 + 72\omega_5 \omega_2^2 \omega_3^2 \text{cs}^2 - 12\omega_5^2 \omega_2 \omega_3^2 \text{cs}^2 + 12\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 3\omega_5 \omega_3^2 \omega_3^2 - 12\omega_5^2 \omega_3^2 \text{cs}^2 + 12\omega_5 \omega_3^2 \omega_3^2 \text{cs}^2 - 6\omega_2^2 v_1^2 \omega_3^2 \omega_3^2 - 12\omega_5^2 v_1^2 \omega_3^2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 + 18\omega_3^2 \omega_3^2 \text{cs}^2 + 36\omega_5^2 \omega_2^2 \omega_3^2 \text{cs}^2 - 6\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 24\omega_5 \omega_2 \omega_3^2 \text{cs}^2 + 6\omega_5^2 v_1^2 \omega_2^2 - 24\omega_5 \omega_2^2 \omega_3^2 \text{cs}^2 + 6\omega_5^2 v_1^2 \omega_2 \omega_3 - 6\omega_5^2 \omega_2 \omega_3^2 + 6\omega_5 \omega_2^2 \omega_3^2 - 24\omega_5 v_1^2 \omega_2 \omega_3^2 + 6\omega_5^2 \omega_2^2 \omega_3 \text{cs}^2 - 36\omega_5^2 \omega_2^2 \omega_3^2 \text{cs}^2 + 6\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 21\omega_5 \omega_2^2 \omega_3^2) \frac{v_1 v_2}{6\omega_2^2 \omega_3^2 \omega_3^2}$$

$$C_{D_x^3 D_y v_1}^{(0), \text{SRT}} = (12 - 56\omega^2 cs^2 - 12\omega^2 v_1^2 - 12v_1^2 + 4\omega^3 cs^2 + 3\omega^3 v_1^2 - 96cs^2 - 18\omega - \omega^3 + 8\omega^2 + 18\omega v_1^2 + 144\omega cs^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_3^2 D_3 D_3 v_1}^{(0), \text{MRT1}} = (36\omega_5 v_1^2 \omega_2^3 \omega_3^2 + 36\omega_2^3 \omega_2 \omega_3^3 c s^2 - 24\omega_5 \omega_2^3 \omega_3^3 c s^2 - 6\omega_5^2 \omega_2^3 \omega_3^2 - 12\omega_2^3 \omega_2^3 \omega_3^3 c s^2 - 12\omega_2^3 \omega_3^3 c s^2 - 24\omega_5 v_1^2 \omega_2^3 \omega_3^2 + 6v_1^2 \omega_2^3 \omega_3^3 + 3\omega_2^3 \omega_2^3 \omega_3^2 + 2\omega_5^2 \omega_2^3 \omega_3^2 + 36\omega_5 \omega_2^3 \omega_3^3 c s^2 - 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 + 24\omega_2^3 v_1^2 \omega_3^3 - 24\omega_2^3 \omega_2 \omega_3^3 c s^2 - \omega_5^2 \omega_3^3 \omega_3^3 - 12v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5^2 \omega_2^3 \omega_3 c s^2 + 12\omega_5 v_2^3 \omega_3^3 \omega_3^3 - 30\omega_2^3 v_1^2 \omega_2 \omega_3^3 + 4\omega_2^3 \omega_2^3 \omega_3^3 c s^2 - 6\omega_5 \omega_3^3 \omega_3^3 + 6\omega_2^3 \omega_3^3 c s^2 + 48\omega_2^3 \omega_2^3 \omega_3^3 c s^2 - 12\omega_5 \omega_2 \omega_3^3 c s^2 - 18\omega_5^2 v_1^2 \omega_3^3 \omega_3 + 3\omega_5 \omega_3^3 \omega_3^3 + 12\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 + 12\omega_5 \omega_2^3 \omega_3^3 c s^2 - 12\omega_5^2 \omega_3^3 c s^2 + 3\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 + 6\omega_5^2 \omega_2^3 \omega_3 c s^2 - 32\omega_5^2 \omega_2^3 \omega_3^3 c s^2 + 12\omega_5 \omega_2^3 \omega_3^3 - 12\omega_5 v_1^2 \omega_2 \omega_3^3 - 12\omega_5 \omega_2^3 \omega_3^3 c s^2 - 6\omega_5 \omega_2^3 \omega_3^3) \frac{v_2 p}{12\omega_2^3 \omega_3^3 \omega_3^3}$$

$$C_{D_3^2 D_2 v_1}^{(0), \text{MRT}^2} = (36\omega_5 v_1^2 \omega_2^3 \omega_3^3 - 12cs^2 \omega_5^2 \omega_3^3 - 12cs^2 \omega_5 \omega_2 \omega_3^3 - 6\omega_2^2 \omega_2^3 \omega_3^3 + 6cs^2 \omega_2^3 \omega_3^3 + 48cs^2 \omega_2^2 \omega_2^3 \omega_3^3 - 24\omega_5 v_1^2 \omega_2^2 \omega_3^3 + 6v_1^2 \omega_2^3 \omega_3^3 - 32cs^2 \omega_5^2 \omega_2^3 \omega_3^3 + 32cs^2 \omega_5^2 \omega_2^3 \omega_3^3 + 6cs^2 \omega_2^3 \omega_2^3 \omega_3^3 - 12cs^2 \omega_2^2 \omega_2^3 \omega_3^3 + 2\omega_5^2 \omega_2^3 \omega_3^3 - 12cs^2 \omega_5^2 \omega_2^3 \omega_3^3 - 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 + 24\omega_5^2 v_1^2 \omega_3^3 + 4cs^2 \omega_5^2 \omega_2^3 \omega_3^3 - 12cs^2 \omega_5^2 \omega_2^3 \omega_3 - \omega_5^2 \omega_2^3 \omega_3^3 - 12\omega_1^2 \omega_2^3 \omega_3^3 + 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 - 30\omega_2^2 v_1^2 \omega_2 \omega_3^3 + 12cs^2 \omega_5 \omega_2^3 \omega_3^3 - 6\omega_5 \omega_2^3 \omega_3^3 - 18\omega_5^2 v_1^2 \omega_2^3 \omega_3 + 3\omega_5 \omega_2^3 \omega_3^3 - 12cs^2 \omega_5 \omega_2^3 \omega_3^3 + 12\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 + 12\omega_5^2 v_1^2 \omega_2^3 + 3\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 24cs^2 \omega_5 \omega_2^2 \omega_3^3 + 36cs^2 \omega_5^2 \omega_2 \omega_3^3 + 12\omega_5 \omega_2^2 \omega_3^3 - 12\omega_5 v_1^2 \omega_2 \omega_3^3 - 6\omega_5 \omega_2^2 \omega_3^3 - 24cs^2 \omega_2^2 \omega_2 \omega_3^3 + 36cs^2 \omega_5 \omega_2^2 \omega_3^3) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^3}$$

$$C_{D_x^2 D_y^2 v_1 v_2}^{(0), \text{CLBMM1}} = (-12\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 12\omega_5^2 c s^2 \omega_3^2 - 6\omega_5^2 \omega_2^2 \omega_3^2 + 6\omega_5^2 c s^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 c s^2 \omega_3 - 12\omega_5 \omega_2 c s^2 \omega_3^2 - 24\omega_5 v_1^2 \omega_2^2 \omega_3^2 - 6v_1^2 \omega_2^2 \omega_3^2 + 3\omega_5^2 \omega_2^2 \omega_3^2 + 12\omega_5^2 \omega_2^2 \omega_3^2 - 12\omega_5 \omega_2^3 c s^2 \omega_3^2 + 48\omega_5^2 \omega_2^2 c s^2 \omega_3^2 - 24\omega_5^2 v_1^2 \omega_3^2 - \omega_5^2 \omega_2^3 \omega_3^2 + 12v_1^2 \omega_2^2 \omega_3^2 + 12\omega_5 v_1^2 \omega_3^2 \omega_3^2 + 12\omega_5 \omega_2^3 c s^2 \omega_3^2 - 32\omega_5^2 \omega_2^2 c s^2 \omega_3^2 + 30\omega_5^2 v_1^2 \omega_2 \omega_3^2 - 6\omega_5 \omega_2^3 \omega_3^2 + 6\omega_5^2 \omega_2^3 c s^2 \omega_3 - 12\omega_2^2 c s^2 \omega_3^2 - 12\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 - 24\omega_5^2 \omega_2 c s^2 \omega_3^2 - 18\omega_5^2 v_1^2 \omega_2^2 \omega_3 + 3\omega_5 \omega_2^3 \omega_3^2 + 36\omega_5 \omega_2 c s^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 + 12\omega_5^2 v_1^2 \omega_2^2 + 3\omega_5^2 v_1^2 \omega_2^2 \omega_3^2 + 4\omega_5^2 \omega_2^2 c s^2 \omega_3^2 - 24\omega_5 \omega_2^3 c s^2 \omega_3^2 + 12\omega_5 \omega_2^2 \omega_3^2 - 12\omega_5^2 \omega_2^2 c s^2 \omega_3^2 + 36\omega_5 \omega_2^2 c s^2 \omega_3^2 + 12\omega_5 v_1^2 \omega_2 \omega_3^2 - 6\omega_5 \omega_2^3 \omega_3^2) \frac{v_2 \rho}{12\omega_5^2 \omega_3^2 \omega_3^2}$$

$$G_{\mathbf{D}_3^3 \mathbf{D}_{\nu_1}}^{(0), \text{CLBM2}} = (-12\omega_5^2\omega_3^2\omega_3^2cs^2 - 12\omega_2^2\omega_3^3cs^2 - 12\omega_5v_1^2\omega_2^2\omega_3 - 6\omega_5^2\omega_2^2\omega_3 + 36\omega_5^2\omega_2\omega_3^3cs^2 - 24\omega_5\omega_2^2\omega_3^3cs^2 - 24\omega_5v_1^2\omega_2^2\omega_3 - 6v_1^2\omega_2^3\omega_3 +$$

$$3\omega_5^2\omega_2^2\omega_3^3 + 2\omega_5^2\omega_2^3\omega_3^2 - 12\omega_5^2\omega_2^2\omega_3cs^2 - 24\omega_5^2v_1^2\omega_3^3 + 4\omega_5^2\omega_2^3\omega_3cs^2 - \omega_5^2\omega_2^3\omega_3^3 + 12v_1^2\omega_2^2\omega_3^3 + 36\omega_5\omega_2^2\omega_3^3cs^2 + 12\omega_5v_1^2\omega_2^3\omega_3^2 - 24\omega_5^2\omega_2\omega_3^3cs^2 + 30\omega_5^2v_1^2\omega_2\omega_3^3 - 6\omega_5\omega_2^3\omega_3^3 - 12\omega_5^2\omega_3^3cs^2 + 12\omega_5\omega_2^3\omega_3^3cs^2 - 12\omega_5^2v_1^2\omega_2^3\omega_3^3 - 18\omega_5^2v_1^2\omega_2^3\omega_3 + 3\omega_5\omega_2^3\omega_3^3 + 6\omega_5^2\omega_3^3cs^2 + 48\omega_5^2\omega_2^3\omega_3^3cs^2 + 12\omega_5^2v_1^2\omega_2^3\omega_3^3 - 12\omega_5\omega_2^3\omega_3^3cs^2 + 12\omega_5^2v_1^2\omega_2^3 + 3\omega_5^2v_1^2\omega_2^3\omega_3^3 - 12\omega_5\omega_2^3\omega_3^3cs^2 + 12\omega_5\omega_2^3\omega_3^3 + 12\omega_5v_1^2\omega_2\omega_3^3 + 6\omega_5^2\omega_2^3\omega_3cs^2 - 32\omega_5^2\omega_2^3\omega_3^3cs^2 - 6\omega_5\omega_2^3\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_3^3}$$

**coefficient**  $C_{D_x^3 D_y v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_1^3 \partial x_2}$ :

$$C_{D_x^3 D_y v_2}^{(0), \text{SRT}} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_1^2 - 36v_1^2 + 4\omega^3 cs^2 + \omega^3 v_1^2 - 96cs^2 - 54\omega - \omega^3 + 20\omega^2 + 54\omega v_1^2 + 144\omega cs^2) \frac{v_1\rho}{12\omega^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{MRT1}} = (-36\omega_5\omega_2cs^2 + 9\omega_5\omega_2^3 + 6\omega_2^3cs^2 - 48\omega_5^2cs^2 - 44\omega_5^2\omega_2^3cs^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 12\omega_2^2cs^2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^2 + 4\omega_5^2\omega_2^3cs^2 - 8\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 - 12\omega_5\omega_2^3cs^2 + \omega_5^2v_1^2\omega_2^3 + 11\omega_5^2\omega_2^2 + 90\omega_5^2\omega_2cs^2 + 6v_1^2\omega_2^3 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 48\omega_5\omega_2^2cs^2 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{MRT2}} = (-12cs^2\omega_5\omega_2^3 + 9\omega_5\omega_2^3 + 48cs^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 36cs^2\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^2 - 8\omega_5^2v_1^2\omega_2^2 + 90cs^2\omega_5^2\omega_2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^2 + 11\omega_5^2\omega_2^2 - 44cs^2\omega_5^2\omega_2^2 + 6v_1^2\omega_2^3 + 6cs^2\omega_2^3 - 48cs^2\omega_5^2 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 4cs^2\omega_5^2\omega_2^3 + 12\omega_5^2v_1^2 - 12cs^2\omega_2^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CLBM1}} = (18\omega_5^2\omega_2cs^2 + 9\omega_5\omega_2^3 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 96\omega_5\omega_2^2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 30\omega_5\omega_2^3cs^2 - 6\omega_5v_1^2\omega_2^3 - 60\omega_2^2cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^2 + 4\omega_5^2\omega_2^3cs^2 + 11\omega_5^2\omega_2^2 + 30\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6v_1^2\omega_2^2 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - 26\omega_5^2\omega_2^2cs^2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_y v_2}^{(0), \text{CLBM2}} = (-26\omega_5^2\omega_2^2cs^2 + 9\omega_5\omega_2^3 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 30\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 4\omega_5^2\omega_2^3cs^2 + 12\omega_2^2 - 60\omega_2^2cs^2 - 6\omega_5v_1^2\omega_2^3 - 30\omega_5\omega_2^3cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^2 + 11\omega_5^2\omega_2^2 + 96\omega_5\omega_2^2cs^2 - 6v_1^2\omega_2^3 + 18\omega_5^2\omega_2cs^2 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

**coefficient**  $C_{D_t^2 D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t^2 \partial x_2^2}$ :

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{3v_2\rho}{2\omega^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{MRT1}} = (-\omega_6^2\omega_3^2 - \omega_6^2\omega_3 - 4\omega_3^2 - 4\omega_6\omega_3 + 2\omega_3^3 - 2\omega_6\omega_3^3 + 2\omega_6^2 + 8\omega_6\omega_3^2) \frac{v_2\rho}{2\omega_6^2\omega_3^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_t^2 D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{CLBM1}} = (-2 - \omega_3^2 + 3\omega_3) \frac{3v_2\rho}{2\omega_3^3}$$

$$C_{D_t^2 D_y^2 v_2}^{(0), \text{CLBM2}} = C_{D_t^2 D_y^2 v_2}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_t D_x D_y^2 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2^2}$ :

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{SRT}} = (34\omega^2 cs^2 - 2\omega^2 v_2^2 + \omega^3 v_2^2 - 2\omega^3 cs^2 + 60cs^2 - 90\omega cs^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{MRT1}} = (-30\omega_2v_2^2\omega_6\omega_3^2 + 12\omega_2\omega_6^2cs^2 - 6\omega_6\omega_3^3cs^2 - 30\omega_2\omega_6\omega_3^2cs^2 + 9\omega_2v_2^2\omega_6\omega_3^3 - 30\omega_2\omega_6^2\omega_3cs^2 - 24\omega_2v_2^2\omega_6^2 + 12v_2^2\omega_6\omega_3^2 - 6\omega_2v_2^2\omega_3^3 + 9\omega_2\omega_6\omega_3^3cs^2 + 12\omega_6\omega_3^3cs^2 + 12\omega_2v_2^2\omega_3^3 - 6v_2^2\omega_6\omega_3^3 + 12\omega_2v_2^2\omega_6\omega_3 + 12\omega_6^2\omega_3cs^2 - 2\omega_2\omega_6^2\omega_3^3cs^2 - v_2^2\omega_6^2\omega_3^3 + 36\omega_2v_2^2\omega_6^2\omega_3 - 18\omega_6^2\omega_3^3cs^2 + 6v_2^2\omega_6^2\omega_3^3 + 12\omega_2\omega_3^3cs^2 + 3\omega_6^2\omega_3^3cs^2 + \omega_2v_2^2\omega_6^2\omega_3^3 - 12v_2^2\omega_6^2\omega_3 + 22\omega_2\omega_6^2\omega_3^3cs^2 - 10\omega_2v_2^2\omega_6^2\omega_3^3 - 6\omega_2\omega_3^3cs^2 + 12\omega_2\omega_6\omega_3cs^2) \frac{\rho}{12\omega_2\omega_6^2\omega_3^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{MRT2}} = (-30\omega_2v_2^2\omega_6\omega_3^2 - 2cs^2\omega_2\omega_6^2\omega_3^3 - 18cs^2\omega_6^2\omega_3^2 + 9\omega_2v_2^2\omega_6\omega_3^3 + 3cs^2\omega_6^2\omega_3^3 + 22cs^2\omega_2\omega_6^2\omega_3^2 - 24\omega_2v_2^2\omega_6^2 + 12v_2^2\omega_6\omega_3^2 - 6\omega_2v_2^2\omega_3^3 - 30cs^2\omega_2\omega_6^2\omega_3 + 12\omega_2v_2^2\omega_3^3 - 6v_2^2\omega_6\omega_3^3 + 12cs^2\omega_6^2\omega_3 + 12\omega_2v_2^2\omega_6\omega_3 + 12cs^2\omega_2\omega_3^2 - v_2^2\omega_6^2\omega_3^3 + 36\omega_2v_2^2\omega_6^2\omega_3 + 6v_2^2\omega_6^2\omega_3^2 - 6cs^2\omega_2\omega_3^3 + 12cs^2\omega_2\omega_6\omega_3 + \omega_2v_2^2\omega_6^2\omega_3^3 + 12cs^2\omega_2\omega_6^2 - 12v_2^2\omega_6^2\omega_3 - 6cs^2\omega_6\omega_3^3 - 30cs^2\omega_2\omega_6\omega_3^2 - 10\omega_2v_2^2\omega_6^2\omega_3^2 + 9cs^2\omega_2\omega_6\omega_3^3 + 12cs^2\omega_6\omega_3^2) \frac{\rho}{12\omega_2\omega_6^2\omega_3^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{CLBM1}} = (30\omega_2v_2^2\omega_6\omega_3^2 + 9\omega_2cs^2\omega_6\omega_3^3 - 30\omega_2cs^2\omega_6\omega_3^2 + 12\omega_2cs^2\omega_6^2 - 9\omega_2v_2^2\omega_6\omega_3^3 + 24\omega_2v_2^2\omega_6^2 - 12v_2^2\omega_6\omega_3^2 + 6\omega_2v_2^2\omega_3^3 - 6cs^2\omega_6\omega_3^3 + 12\omega_2cs^2\omega_6\omega_3 - 6\omega_2cs^2\omega_3^3 + 12cs^2\omega_6\omega_3^2 - 12\omega_2v_2^2\omega_3^3 + 6v_2^2\omega_6\omega_3^3 - 12\omega_2v_2^2\omega_6\omega_3 + 12\omega_2cs^2\omega_3^2 - 18cs^2\omega_6^2\omega_3^2 - v_2^2\omega_6^2\omega_3^3 - 36\omega_2v_2^2\omega_6^2\omega_3 - 6v_2^2\omega_6^2\omega_3^3 + 3cs^2\omega_6^2\omega_3^3 - 30\omega_2cs^2\omega_6^2\omega_3 + 22\omega_2cs^2\omega_6^2\omega_3^2 + \omega_2v_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3 + 8\omega_2v_2^2\omega_6^2\omega_3^2 - 2\omega_2cs^2\omega_6^2\omega_3^3 + 12cs^2\omega_6^2\omega_3) \frac{\rho}{12\omega_2\omega_6^2\omega_3^3}$$

$$C_{D_t D_x D_y^2 v_1}^{(0), \text{CLBM2}} = (30\omega_2v_2^2\omega_6\omega_3^2 - 30\omega_2\omega_6^2\omega_3cs^2 + 12\omega_2\omega_6^2cs^2 - 6\omega_6\omega_3^3cs^2 - 9\omega_2v_2^2\omega_6\omega_3^3 - 30\omega_2\omega_6\omega_3^2cs^2 + 24\omega_2v_2^2\omega_6^2 - 12v_2^2\omega_6\omega_3^2 + 6\omega_2v_2^2\omega_3^3 + 12\omega_6^2\omega_3cs^2 - 12\omega_2v_2^2\omega_3^3 + 6v_2^2\omega_6\omega_3^3 + 9\omega_2\omega_6\omega_3^3cs^2 - 12\omega_2v_2^2\omega_6\omega_3 + 12\omega_6\omega_3^3cs^2 - v_2^2\omega_6^2\omega_3^3 + 12\omega_2\omega_3^2cs^2 - 36\omega_2v_2^2\omega_6^2\omega_3 - 2\omega_2\omega_6^2\omega_3^3cs^2 -$$



$$2\omega_5\omega_2^2cs^4\omega_6^2\omega_3^3 - 2\omega_5^2\omega_2^3cs^4\omega_6^2\omega_3 - 4\omega_5^2v_1^2\omega_2^2cs^2\omega_6\omega_3 + 4\omega_5^2v_1^2\omega_2^3v_2^2\omega_6\omega_3 - 2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 + 10\omega_5^2\omega_2v_2^2cs^2\omega_6^2\omega_3^3 - 4\omega_5^2v_1^2\omega_2^3cs^2\omega_6^2\omega_3^3 - \omega_5^2\omega_2^3v_2^2cs^2\omega_6\omega_3^3 + 4\omega_5^2\omega_2^2cs^4\omega_6^2\omega_3^3 + 2\omega_5^2v_1^2\omega_2^2cs^2\omega_6\omega_3^3 + 4\omega_5\omega_2^2cs^4\omega_6^2\omega_3^3 + 4\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2 + 8\omega_5^2\omega_2^2v_2^2cs^2\omega_6^2\omega_3^3 + 4\omega_5^2v_1^2\omega_2^2v_2^2\omega_6\omega_3^3) \frac{1}{4\omega_5^2\omega_2^2\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CLBM2}} = (4\omega_5^2\omega_2^3\omega_6^2\omega_3^4 - 14\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3 - 2\omega_5\omega_2^2\omega_6^2\omega_3^4 + 8\omega_5^2v_1^2\omega_2^2\omega_6^2\omega_3^3 + 2\omega_5^2v_1^2\omega_2^3\omega_3^3 - 4\omega_5^2\omega_2^2v_2^2\omega_6\omega_3^3cs^2 + 2\omega_5v_1^2\omega_2^3\omega_3^3cs^2 - 2\omega_5v_1^2\omega_2^3\omega_3^3cs^2 - 2\omega_5v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - 28\omega_5^2v_1^2\omega_2^2v_2^2\omega_6^2\omega_3^3 - 2\omega_5^2\omega_2^3v_2^2\omega_6^2\omega_3^3cs^2 - 3\omega_5\omega_2^3v_2^2\omega_6^2\omega_3^3cs^2 - 4\omega_2^3v_2^2\omega_6^2\omega_3^3cs^2 + \omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 - 2\omega_5\omega_2^3\omega_6^2\omega_3^3cs^4 + 14\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 + 4\omega_5^2\omega_2^3\omega_6^2\omega_3^3cs^4 + 2\omega_5v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 + 4\omega_5^2v_1^2v_2^2\omega_6^2\omega_3^3 + 3\omega_5v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - 4\omega_5^2v_1^2\omega_2^3\omega_6\omega_3cs^2 + \omega_5^2\omega_2^3v_2^2\omega_6^2\omega_3^3cs^2 - 4\omega_5^2v_2^2\omega_6^2\omega_3^3cs^2 + 2\omega_5^2\omega_2^3v_2^2\omega_6\omega_3cs^2 - 10\omega_5v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - \omega_5v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 - 3\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - \omega_5^2\omega_2^3\omega_6^2\omega_3^3cs^4 - 4\omega_5^2v_1^2\omega_2^3\omega_3^3cs^2 - 2\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 + 4\omega_5\omega_2^2\omega_6^2\omega_3^3cs^4 - 4\omega_5v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 + \omega_5\omega_2^3\omega_6^2\omega_3^3cs^4 + 12\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - 8\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 - 12\omega_5^2\omega_2^3\omega_6^2\omega_3^3cs^4 + 14\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 + 2\omega_5\omega_2^3v_2^2\omega_6^2\omega_3^3cs^2 + 4\omega_5v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - 2\omega_5^2v_1^2\omega_2^3v_2^2\omega_3^3 + 12\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^3 + 4\omega_5^2\omega_2^3\omega_6^2\omega_3cs^4 - \omega_5^2\omega_2^3v_2^2\omega_6\omega_3cs^2 + 10\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^3cs^2 + 4\omega_5^2v_1^2\omega_2^3v_2^2\omega_3^3 + 10\omega_5^2\omega_2v_2^2\omega_6^2\omega_3^3cs^2 - 14\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - 2\omega_5^2\omega_2v_2^2\omega_6^2\omega_3^3cs^4 + 3\omega_5^2v_1^2\omega_2^3v_2^2\omega_6\omega_3^3 + 8\omega_5^2\omega_2^3v_2^2\omega_6^2\omega_3^3cs^2 - 4\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^3cs^2 + 4\omega_5v_1^2\omega_2^3v_2^2\omega_6^2\omega_3^3 - 4\omega_5\omega_2v_2^2\omega_6^2\omega_3^3cs^2 - 2\omega_5^2\omega_2^3\omega_6\omega_3^3cs^4 + 2\omega_5^2\omega_2^3v_2^2\omega_6\omega_3^3cs^2 - 2\omega_5^2v_1^2v_2^2\omega_6\omega_3^3 - 4\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3cs^2 + 4\omega_5^2v_1^2\omega_2^3v_2^2\omega_6\omega_3 - 2v_1^2v_2^2\omega_6^2\omega_3^3 - 2\omega_5^2\omega_2^3\omega_6\omega_3cs^4 - 4\omega_5^2v_1^2\omega_2^3\omega_6^2\omega_3^3 - 4\omega_5^2\omega_2v_2^2\omega_6^2\omega_3^3cs^2 + 4\omega_5^2\omega_2\omega_6^2\omega_3^3cs^4 + 4\omega_5^2v_1^2\omega_2^3v_2^2\omega_6^2 + 10\omega_5\omega_2^2v_2^2\omega_6^2\omega_3^3cs^2 - 2\omega_5^2\omega_2\omega_6\omega_3cs^4 + 4\omega_5^2v_1^2\omega_2^3v_2^2\omega_6\omega_3^3 - 3\omega_5^2v_1^2\omega_2^3\omega_6\omega_3^3cs^2 + 2\omega_5^2v_2^2\omega_6^2\omega_3^3cs^2) \frac{1}{4\omega_5^2\omega_2^3\omega_6^2\omega_3^3}$$

**coefficient**  $C_{D_x^2 D_y^2 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2}$ :

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{SRT}} = (-26\omega^2cs^2 + 50\omega^2v_2^2 - 4\omega^3v_2^2 + \omega^3cs^2 - 48cs^2 + 84v_2^2 + 72\omega cs^2 - 126\omega v_2^2) \frac{v_1\rho}{12\omega^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}} = (-12\omega_5^3\omega_6\omega_3cs^2 + 24\omega_5^3v_2^2\omega_6^2\omega_3 + 34\omega_5^3v_2^2\omega_6^2\omega_3^3 - 6\omega_5^2\omega_6^2\omega_3^3cs^2 - 12\omega_5^3v_2^2\omega_3^3 - 14\omega_5^3\omega_6^2\omega_3^3cs^2 + 6\omega_5^3v_2^2\omega_3^3 - 4\omega_5^3v_2^2\omega_6^2\omega_3^3 + 12\omega_5^2\omega_6^2\omega_3^3cs^2 + 48\omega_5^3v_2^2\omega_6^2 + 22\omega_5^2v_2^2\omega_6^2\omega_3^3 - 78\omega_5^3v_2^2\omega_6^2\omega_3 + \omega_5^2\omega_6^2\omega_3^3cs^2 - 48\omega_5^2v_2^2\omega_6^2\omega_3^3 - 12\omega_5^2\omega_6^2cs^2 - 12\omega_5^2v_2^2\omega_6\omega_3 + 6\omega_5\omega_6^2\omega_3^3cs^2 + 12v_2^2\omega_6^2\omega_3^3 + 6\omega_5^2\omega_3^3cs^2 - 6\omega_5^2\omega_6\omega_3^3cs^2 - 30\omega_5v_2^2\omega_6^2\omega_3^3 - 12\omega_5^2\omega_3^3cs^2 + 24\omega_5^2\omega_6^2\omega_3cs^2 - 6\omega_5^2v_2^2\omega_6\omega_3^3 - 12\omega_5\omega_6^2\omega_3^3cs^2 + 24\omega_5v_2^2\omega_6^2\omega_3^3 + 24\omega_5^2\omega_6\omega_3^3cs^2 + 24\omega_5^2v_2^2\omega_6\omega_3^3) \frac{v_1\rho}{12\omega_5^3\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT2}} = (24\omega_5^2v_2^2\omega_6^2\omega_3 + 34\omega_5^3v_2^2\omega_6^2\omega_3^3 + 6cs^2\omega_2\omega_6^2\omega_3^3 + 6cs^2\omega_2^3\omega_3^3 - 12\omega_5^3v_2^2\omega_3^3 + 24cs^2\omega_2^3\omega_6^2\omega_3 + 6\omega_5^3v_2^2\omega_3^3 - 12cs^2\omega_2^3\omega_3^3 - 12cs^2\omega_2\omega_6^2\omega_3^3 - 4\omega_5^3v_2^2\omega_6^2\omega_3^3 - 14cs^2\omega_2^3\omega_6^2\omega_3^3 + 48\omega_5^3v_2^2\omega_6^2 + 22\omega_5^2v_2^2\omega_6^2\omega_3^3 - 78\omega_5^3v_2^2\omega_6^2\omega_3 - 12cs^2\omega_2^3\omega_6^2 + cs^2\omega_2^3\omega_6^2\omega_3^3 - 48\omega_5^2v_2^2\omega_6^2\omega_3^3 - 12\omega_5^3v_2^2\omega_6\omega_3 - 6cs^2\omega_2^3\omega_6\omega_3^3 + 12v_2^2\omega_6^2\omega_3^3 + 24cs^2\omega_2^3\omega_6\omega_3^3 - 30\omega_5v_2^2\omega_6^2\omega_3^3 - 12cs^2\omega_2^3\omega_6\omega_3 - 6cs^2\omega_2^3\omega_6^2\omega_3^3 - 6\omega_5^2v_2^2\omega_6\omega_3^3 + 24\omega_5v_2^2\omega_6^2\omega_3^3 + 12cs^2\omega_2^3\omega_6^2\omega_3^3 + 24\omega_5^2v_2^2\omega_6\omega_3^3) \frac{v_1\rho}{12\omega_5^3\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM1}} = (-12\omega_5^2cs^2\omega_3^3 + 24\omega_5^2v_2^2\omega_6^2\omega_3 + 22\omega_5^3v_2^2\omega_6^2\omega_3^3 + \omega_5^2cs^2\omega_6^2\omega_3^3 + 12\omega_5^3v_2^2\omega_3^3 + 6\omega_5^2cs^2\omega_3^3 - 6\omega_5^3v_2^2\omega_3^3 - 14\omega_5^2cs^2\omega_6^2\omega_3^3 - 4\omega_5^3v_2^2\omega_6^2\omega_3^3 + 24\omega_5^3cs^2\omega_6^2\omega_3 + 22\omega_5^2v_2^2\omega_6^2\omega_3^3 - 12\omega_5^2cs^2\omega_6^2 + 12\omega_5^2cs^2\omega_6^2\omega_3^3 - 18\omega_5^3v_2^2\omega_6^2\omega_3 - 6\omega_5^2cs^2\omega_6^2\omega_3^3 - 48\omega_5^2v_2^2\omega_6^2\omega_3^3 + 12\omega_5^3v_2^2\omega_6\omega_3 + 12v_2^2\omega_6^2\omega_3^3 - 12\omega_5^2cs^2\omega_6\omega_3 - 12\omega_5^2cs^2\omega_6^2\omega_3^3 - 30\omega_5v_2^2\omega_6^2\omega_3^3 + 24\omega_5^2cs^2\omega_6\omega_3^3 + 6\omega_5^2v_2^2\omega_6\omega_3^3 + 24\omega_5v_2^2\omega_6^2\omega_3^3 + 6\omega_5^2cs^2\omega_6^2\omega_3^3 - 24\omega_5^2v_2^2\omega_6\omega_3^3 - 6\omega_5^2cs^2\omega_6\omega_3^3) \frac{v_1\rho}{12\omega_5^3\omega_6^2\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM2}} = (-14\omega_5^3\omega_6^2\omega_3^3cs^2 + 24\omega_5^2v_2^2\omega_6^2\omega_3 + 22\omega_5^3v_2^2\omega_6^2\omega_3^3 + 12\omega_5^3v_2^2\omega_3^3 - 12\omega_5^3\omega_6\omega_3cs^2 - 6\omega_5^3v_2^2\omega_3^3 - 6\omega_5^2\omega_6^2\omega_3^3cs^2 - 4\omega_5^3v_2^2\omega_6^2\omega_3^3 + 22\omega_5^3v_2^2\omega_6^2\omega_3^3 + \omega_5^3\omega_6^2\omega_3^3cs^2 - 12\omega_5^2\omega_6^2cs^2 + 12\omega_5^2\omega_6^2\omega_3^3cs^2 - 18\omega_5^3v_2^2\omega_6^2\omega_3 - 48\omega_5^2v_2^2\omega_6^2\omega_3^3 + 12\omega_5^3v_2^2\omega_6\omega_3 + 12v_2^2\omega_6^2\omega_3^3 - 6\omega_5^2\omega_6\omega_3^3cs^2 + 6\omega_5\omega_6^2\omega_3^3cs^2 + 24\omega_5^3\omega_6\omega_3^3cs^2 - 30\omega_5v_2^2\omega_6^2\omega_3^3 + 6\omega_5^3v_2^2\omega_6\omega_3^3 + 24\omega_5v_2^2\omega_6^2\omega_3^3 + 24\omega_5^2v_2^2\omega_6^2\omega_3cs^2 - 12\omega_5^3\omega_3^3cs^2 - 24\omega_5^3v_2^2\omega_6\omega_3^3 - 12\omega_5\omega_6^2\omega_3^3cs^2) \frac{v_1\rho}{12\omega_5^3\omega_6^2\omega_3^3}$$

**coefficient**  $C_{D_x^2 D_y^2 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2}$ :

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{SRT}} = (-26\omega^2cs^2 + 50\omega^2v_1^2 + 84v_1^2 + \omega^3cs^2 - 4\omega^3v_1^2 - 48cs^2 - 126\omega v_1^2 + 72\omega cs^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}} = (24\omega_5v_1^2\omega_2^2\omega_3^3 + 24\omega_5^2\omega_2\omega_3^3cs^2 - 6\omega_5^2\omega_2^3\omega_3^3cs^2 - 12\omega_5^2\omega_3^3cs^2 + 6v_1^2\omega_2^3\omega_3^3 + 24\omega_5\omega_2^2\omega_3^3cs^2 + 24\omega_5^2v_1^2\omega_2\omega_3^3 - 6\omega_5v_1^2\omega_2^3\omega_3^3 + 48\omega_5^2v_1^2\omega_3^3 - 12v_1^2\omega_2^3\omega_3^3 - 12\omega_5^2\omega_2\omega_3cs^2 - 78\omega_5^3v_1^2\omega_2\omega_3^3 + \omega_5^2\omega_2^3\omega_3^3cs^2 + 6\omega_5^2\omega_3^3cs^2 + 12\omega_5^2\omega_2^2\omega_3^3cs^2 + 34\omega_5^2v_1^2\omega_2^3\omega_3^3 - 12\omega_5\omega_2\omega_3^3cs^2 - 30\omega_5^2v_1^2\omega_2^3\omega_3 - 48\omega_5^3v_1^2\omega_2^2\omega_3^3 + 12\omega_5^2v_1^2\omega_2^3 - 12\omega_5^2\omega_3^3cs^2 - 4\omega_5^2v_1^2\omega_2^3\omega_3^3 + 6\omega_5^2\omega_2^2\omega_3cs^2 + 24\omega_5^2v_1^2\omega_2\omega_3 - 14\omega_5^2\omega_2^3\omega_3^3cs^2 - 12\omega_5v_1^2\omega_2\omega_3^3 - 6\omega_5\omega_2^3\omega_3^3cs^2 + 22\omega_5^2v_1^2\omega_2^2\omega_3^3) \frac{v_2\rho}{12\omega_5^3\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT2}} = (24\omega_5v_1^2\omega_2^2\omega_3^3 - 12cs^2\omega_5^2\omega_3^3 - 12cs^2\omega_5\omega_2\omega_3^3 + 6cs^2\omega_2^3\omega_3^3 + 12cs^2\omega_5^2\omega_2^2\omega_3^3 + 6v_1^2\omega_2^3\omega_3^3 - 14cs^2\omega_5^2\omega_2^2\omega_3^3 + 6cs^2\omega_5^2\omega_2^3\omega_3 - 12cs^2\omega_2^3\omega_3^3 - 6cs^2\omega_6^2\omega_3^3\omega_3^2 + 24\omega_5^2v_1^2\omega_2\omega_3^3 - 6\omega_5v_1^2\omega_2^3\omega_3^3 + 48\omega_5^3v_1^2\omega_3^3 + cs^2\omega_5^2\omega_2^2\omega_3^3 - 12cs^2\omega_5^2\omega_2^2\omega_3 - 12v_1^2\omega_2^2\omega_3^3 - 78\omega_5^2v_1^2\omega_2\omega_3^3 + 34\omega_5^2v_1^2\omega_2^3\omega_3^3 - 30\omega_5^2v_1^2\omega_2^3\omega_3 - 6cs^2\omega_5\omega_2^3\omega_3^3 - 48\omega_5^3v_1^2\omega_2^2\omega_3^3 + 12\omega_5^2v_1^2\omega_2^3 - 4\omega_5^2v_1^2\omega_2^3\omega_3^3 + 24\omega_5^2v_1^2\omega_2^2\omega_3 + 24cs^2\omega_5^2\omega_2\omega_3^3 - 12\omega_5v_1^2\omega_2\omega_3^3 + 22\omega_5^2v_1^2\omega_2^3\omega_3^3 + 24cs^2\omega_5\omega_2^3\omega_3^3) \frac{v_2\rho}{12\omega_5^3\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM1}} = (-24\omega_5v_1^2\omega_2^2\omega_3^3 - 12\omega_5^2cs^2\omega_3^3 + 6\omega_5^2cs^2\omega_3^3 - 12\omega_5^2\omega_2^2cs^2\omega_3 - 12\omega_5\omega_2cs^2\omega_3^3 - 6v_1^2\omega_2^3\omega_3^3 + 24\omega_5^2v_1^2\omega_2\omega_3^3 - 6\omega_5\omega_2^3cs^2\omega_3^3 + 12\omega_5^2\omega_2^2cs^2\omega_3^3 + 6\omega_5v_1^2\omega_2^3\omega_3^3 + 12v_1^2\omega_2^3\omega_3^3 - 14\omega_5^2\omega_2^2cs^2\omega_3^3 - 18\omega_5^2v_1^2\omega_2\omega_3^3 + 6\omega_5^2\omega_2^3cs^2\omega_3 - 12\omega_2^2cs^2\omega_3^3 + 22\omega_5^2v_1^2\omega_2^2\omega_3^3 - 30\omega_5^2v_1^2\omega_2^3\omega_3 + 24\omega_5^2\omega_2cs^2\omega_3^3 - 48\omega_5^3v_1^2\omega_2^2\omega_3^3 + 12\omega_5^2v_1^2\omega_2^3 - 4\omega_5^2v_1^2\omega_2^3\omega_3^3 + 24\omega_5^2v_1^2\omega_2^2\omega_3 + \omega_5^2\omega_2^3cs^2\omega_3^3 - 6\omega_5^2\omega_2^2cs^2\omega_3^3 + 24\omega_5\omega_2^3cs^2\omega_3^3 + 12\omega_5v_1^2\omega_2\omega_3^3 + 22\omega_5^2v_1^2\omega_2^3\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 v_2}^{(0), \text{CLBM2}} = (-6\omega_5^2 \omega_3^2 \omega_3^2 cs^2 - 12\omega_5^2 \omega_3^3 cs^2 - 24\omega_5 v_1^2 \omega_2^2 \omega_3^3 + 24\omega_5^2 \omega_2 \omega_3^3 cs^2 - 6v_1^2 \omega_3^3 \omega_3^3 - 12\omega_5^2 \omega_2^2 \omega_3 cs^2 + 24\omega_5^2 v_1^2 \omega_2 \omega_3^2 + 6\omega_5 v_1^2 \omega_2^2 \omega_3^3 + \omega_5^2 \omega_3^3 cs^2 + 12v_1^2 \omega_2^2 \omega_3^3 + 24\omega_5 \omega_2^2 \omega_3^3 cs^2 - 18\omega_5^2 v_1^2 \omega_2 \omega_3^3 - 12\omega_5^2 \omega_3^3 cs^2 + 22\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 - 30\omega_5^2 v_1^2 \omega_3^3 \omega_3^3 + 6\omega_5^3 \omega_3^3 cs^2 + 12\omega_5^2 \omega_2^2 \omega_3^3 cs^2 - 48\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 - 12\omega_5 \omega_2 \omega_3^3 cs^2 + 12\omega_5^2 v_1^2 \omega_3^3 - 4\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 - 6\omega_5 \omega_3^3 \omega_3^3 cs^2 + 24\omega_5^2 v_1^2 \omega_2^2 \omega_3 + 12\omega_5 v_1^2 \omega_2 \omega_3^3 + 6\omega_5^2 \omega_3^3 \omega_3^3 cs^2 - 14\omega_5^2 \omega_2^2 \omega_3^3 cs^2 + 22\omega_5^2 v_1^2 \omega_3^3 \omega_3^3) \frac{v_2^2 \rho}{12\omega_5^2 \omega_3^3 \omega_3^3}$$

**coefficient**  $C_{\mathbf{D}_t \mathbf{D}_y^3 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t \partial x_2^3}$ :

$$C_{\mathbf{D}_t \mathbf{D}_y^3 v_2}^{(0), \text{SRT}} = (-36 + 34\omega^2 cs^2 + 42\omega^2 v_2^2 - 3\omega^3 v_2^2 - 2\omega^3 cs^2 + 60cs^2 + 54\omega + 72v_2^2 + \omega^3 - 20\omega^2 - 90\omega cs^2 - 108\omega v_2^2) \frac{\rho}{12\omega^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_y^3 v_2}^{(0), \text{MRT1}} = (9\omega_6 \omega_3^3 cs^2 + 12v_2^2 \omega_6^2 \omega_3^3 - 11\omega_6^2 \omega_3^3 + 24\omega_6^2 cs^2 + \omega_6^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3 - 60v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3^2 - 36\omega_6 \omega_3^2 cs^2 - 6v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 15v_2^2 \omega_6 \omega_3^3 - 48\omega_6^2 \omega_3 cs^2 - 12\omega_3^3 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 12\omega_3^3 cs^2 + 25\omega_6^2 \omega_3^3 cs^2 + 27v_2^2 \omega_6^2 \omega_3^3 + 6\omega_3^3 + 24\omega_6 \omega_3 cs^2 - 2\omega_6^2 \omega_3^3 cs^2 - 6\omega_3^3 cs^2 - 9\omega_6 \omega_3^3 - 42v_2^2 \omega_6^2 \omega_3 + 36\omega_6 \omega_3^2) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_y^3 v_2}^{(0), \text{MRT2}} = (12cs^2 \omega_3^2 + 25cs^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 - 2cs^2 \omega_6^2 \omega_3^3 + \omega_6^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3 - 6cs^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3^2 + 24cs^2 \omega_6^2 + 12v_2^2 \omega_3^2 - 6v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 15v_2^2 \omega_6 \omega_3^3 - 48cs^2 \omega_6^2 \omega_3 - 12\omega_3^2 + 24cs^2 \omega_6 \omega_3 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 27v_2^2 \omega_6^2 \omega_3^2 + 6\omega_3^3 - 9\omega_6 \omega_3^3 - 42v_2^2 \omega_6^2 \omega_3 + 9cs^2 \omega_6 \omega_3^3 + 36\omega_6 \omega_3^2 - 36cs^2 \omega_6 \omega_3^2) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_y^3 v_2}^{(0), \text{CLBM1}} = (24cs^2 \omega_6^2 + 24cs^2 \omega_6 \omega_3 - 36v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 + \omega_6^2 \omega_3^3 + 72v_2^2 \omega_6 \omega_3 - 108v_2^2 \omega_6 \omega_3^2 + 36v_2^2 \omega_3^2 + 9cs^2 \omega_6 \omega_3^3 + 12cs^2 \omega_3^2 - 36cs^2 \omega_6 \omega_3^2 - 18v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 27v_2^2 \omega_6 \omega_3^3 - 6cs^2 \omega_3^3 - 12\omega_3^2 + 25cs^2 \omega_6^2 \omega_3^2 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 15v_2^2 \omega_6^2 \omega_3^2 - 2cs^2 \omega_6^2 \omega_3^3 + 6\omega_3^3 - 9\omega_6 \omega_3^3 + 18v_2^2 \omega_6^2 \omega_3 - 48cs^2 \omega_6^2 \omega_3 + 36\omega_6 \omega_3^2) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

$$C_{\mathbf{D}_t \mathbf{D}_y^3 v_2}^{(0), \text{CLBM2}} = (24\omega_6^2 cs^2 - 36v_2^2 \omega_6^2 - 11\omega_6^2 \omega_3^2 + 9\omega_6 \omega_3^3 cs^2 + \omega_6^2 \omega_3^3 + 72v_2^2 \omega_6 \omega_3 - 108v_2^2 \omega_6 \omega_3^2 + 36v_2^2 \omega_3^2 - 48\omega_6^2 \omega_3 cs^2 - 18v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 + 27v_2^2 \omega_6 \omega_3^3 - 36\omega_6 \omega_3^2 cs^2 - 12\omega_3^2 - 24\omega_6 \omega_3 - 3v_2^2 \omega_6^2 \omega_3^3 + 24\omega_6 \omega_3 cs^2 + 15v_2^2 \omega_6^2 \omega_3^2 + 6\omega_3^3 + 12\omega_3^2 cs^2 + 25\omega_6^2 \omega_3^2 cs^2 - 9\omega_6 \omega_3^3 + 18v_2^2 \omega_6^2 \omega_3 - 2\omega_6^2 \omega_3^2 cs^2 - 6\omega_3^3 cs^2 + 36\omega_6 \omega_3^2) \frac{\rho}{12\omega_6^2 \omega_3^3}$$

**coefficient**  $C_{\mathbf{D}_x \mathbf{D}_y^3 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$ :

$$C_{\mathbf{D}_x \mathbf{D}_y^3 \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_1 v_2}{6\omega^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 \rho}^{(0), \text{MRT1}} = (-24\omega_2^3 \omega_6 \omega_3 cs^2 + 12\omega_2^2 v_2^2 \omega_6^2 \omega_3 + 6\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_2^2 \omega_6 \omega_3^2 - 3\omega_2^3 \omega_3^3 - 12\omega_2^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_2^3 v_2^2 \omega_3^2 - 48\omega_2^3 \omega_6^2 \omega_3^2 cs^2 + 6\omega_2^3 v_2^2 \omega_3^3 + 6\omega_2^3 \omega_6^2 \omega_3 - 3\omega_2^2 \omega_6 \omega_3^3 + 42\omega_2^2 \omega_6^2 \omega_3^2 cs^2 + 7\omega_2^3 \omega_6^2 \omega_3^2 + 24\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_2^2 v_2^2 \omega_6^2 \omega_3^3 - 30\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 + 6\omega_2^3 \omega_6^2 \omega_3^3 cs^2 - 12\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 36\omega_2^3 \omega_6^2 cs^2 - 24\omega_2^3 v_2^2 \omega_6 \omega_3 + 6\omega_2 \omega_6^2 \omega_3^3 cs^2 - 12\omega_2^2 \omega_6 \omega_3^2 cs^2 + 6v_2^2 \omega_6^2 \omega_3^3 + 6\omega_2^3 \omega_6 \omega_3^3 + 6\omega_2^3 \omega_3^3 cs^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 - 24\omega_2^3 \omega_6^2 \omega_3 cs^2 - 21\omega_2^3 \omega_6 \omega_3^3 + 6\omega_2^2 v_2^2 \omega_6 \omega_3^3 - 12\omega_2^3 \omega_6 \omega_3^3 cs^2 - 12\omega_2 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 \omega_3^2 cs^2 + 78\omega_2^3 \omega_6^2 \omega_3 cs^2 + 12\omega_2^3 \omega_6 \omega_3 + 6\omega_2^2 \omega_6 \omega_3^3 cs^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_2 \omega_6^2 \omega_3^2 cs^2 + \omega_2^2 \omega_6^2 \omega_3^3 + 6\omega_2 v_2^2 \omega_6^2 \omega_3^2 + 42\omega_2^2 \omega_6 \omega_3^2 cs^2 - 3\omega_2^2 \omega_6^2 \omega_3^3 + 42\omega_2^3 v_2^2 \omega_6 \omega_3^2) \frac{v_1 v_2}{6\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 \rho}^{(0), \text{MRT2}} = (12\omega_2^2 v_2^2 \omega_6^2 \omega_3 + 6\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 12cs^2 \omega_2^2 \omega_6 \omega_3^2 + 6\omega_2^2 \omega_6 \omega_3^2 + 6cs^2 \omega_2 \omega_6^2 \omega_3^3 - 3\omega_2^3 \omega_3^3 + 6cs^2 \omega_2^2 \omega_3^3 - 12\omega_2^3 v_2^2 \omega_3^2 + 78cs^2 \omega_2^3 \omega_6^2 \omega_3 + 6\omega_2^3 v_2^2 \omega_3^3 + 6\omega_2^3 \omega_3^3 - 12cs^2 \omega_2^3 \omega_3^3 - 6\omega_2^3 \omega_6^2 \omega_3 - 12cs^2 \omega_2 \omega_6^2 \omega_3^2 - 3\omega_2^2 \omega_6 \omega_3^2 + 6cs^2 \omega_2^2 \omega_6 \omega_3^3 - 48cs^2 \omega_2^3 \omega_6^2 \omega_3^2 + 7\omega_2^3 \omega_6^2 \omega_3^2 + 24\omega_2^3 v_2^2 \omega_6^2 + 6\omega_2^2 v_2^2 \omega_6^2 \omega_3^3 - 30\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 - 36cs^2 \omega_2^3 \omega_6^2 + 6cs^2 \omega_2^3 \omega_6^2 \omega_3^3 - 12\omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_2^3 v_2^2 \omega_6 \omega_3 - 24cs^2 \omega_2^2 \omega_6^2 \omega_3 - 12cs^2 \omega_2^3 \omega_6 \omega_3^3 + 6v_2^2 \omega_6^2 \omega_3^3 + 6\omega_2^3 \omega_6 \omega_3^3 - 12\omega_2^2 v_2^2 \omega_6 \omega_3^2 - 21\omega_2^3 \omega_6 \omega_3^2 + 42cs^2 \omega_2^3 \omega_6 \omega_3^2 + 6\omega_2^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 \omega_6 \omega_3 - 24cs^2 \omega_2^3 \omega_6 \omega_3 - 12cs^2 \omega_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 + \omega_2^2 \omega_6^2 \omega_3^3 + 6\omega_2 v_2^2 \omega_6^2 \omega_3^2 - 3\omega_2^2 \omega_6^2 \omega_3^2 + 42cs^2 \omega_2^2 \omega_6^2 \omega_3^2 + 42\omega_2^3 v_2^2 \omega_6 \omega_3^2) \frac{v_1 v_2}{6\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 \rho}^{(0), \text{CLBM1}} = (-36\omega_2^3 cs^2 \omega_3^2 - 6\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_2^2 \omega_6 \omega_3^2 - 3\omega_2^3 \omega_3^3 + 6\omega_2^3 cs^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 v_2^2 \omega_3^2 + 18\omega_2^3 cs^2 \omega_3^3 - 12\omega_2^2 cs^2 \omega_6^2 \omega_3 - 6\omega_2^3 v_2^2 \omega_3^3 - 36\omega_2^3 cs^2 \omega_6^2 \omega_3^2 + 6\omega_2^3 \omega_3^2 - 6\omega_2^3 \omega_6 \omega_3 - 3\omega_2^2 \omega_6 \omega_3^3 + 36\omega_2^3 cs^2 \omega_6^2 \omega_3 + 7\omega_2^3 \omega_6^2 \omega_3^2 + 6\omega_2^2 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 cs^2 \omega_6^2 \omega_3 + 36\omega_2^2 cs^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 - 12\omega_2^2 cs^2 \omega_6^2 \omega_3^3 - 6\omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_2^3 v_2^2 \omega_6 \omega_3 + 6v_2^2 \omega_6^2 \omega_3^3 + 6\omega_2^3 \omega_6 \omega_3^3 + 12\omega_2^2 cs^2 \omega_6 \omega_3^3 - 21\omega_2^3 \omega_6 \omega_3^2 - 24\omega_2^3 cs^2 \omega_6 \omega_3 - 24\omega_2^2 cs^2 \omega_6 \omega_3^2 - 12\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 \omega_6 \omega_3 + 72\omega_2^3 cs^2 \omega_6 \omega_3^2 + \omega_2^2 \omega_6^2 \omega_3^3 + 6\omega_2 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_2 cs^2 \omega_6^2 \omega_3^3 - 3\omega_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 - 24\omega_2^3 cs^2 \omega_6 \omega_3^2) \frac{v_1 v_2}{6\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^3 \rho}^{(0), \text{CLBM2}} = (-36\omega_2^3 \omega_6^2 \omega_3^2 cs^2 - 6\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_2^2 \omega_6 \omega_3^2 - 3\omega_2^3 \omega_3^3 + 12\omega_2^3 v_2^2 \omega_3^2 - 24\omega_2^3 \omega_6 \omega_3 cs^2 - 6\omega_2^3 v_2^2 \omega_3^3 + 6\omega_2^3 \omega_3^2 - 6\omega_2^3 \omega_6^2 \omega_3 - 3\omega_2^2 \omega_6 \omega_3^3 - 12\omega_2^2 \omega_6^2 \omega_3^2 cs^2 + 7\omega_2^3 \omega_6^2 \omega_3^2 + 6\omega_2^2 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_2^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_2^3 \omega_6^2 cs^2 + 36\omega_2^2 \omega_6^2 \omega_3^2 cs^2 + 12\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 - 6\omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 24\omega_2^3 v_2^2 \omega_6 \omega_3 - 12\omega_2^2 \omega_6^2 \omega_3 cs^2 + 6v_2^2 \omega_6^2 \omega_3^3 + 6\omega_2^3 \omega_6 \omega_3^3 - 24\omega_2^3 \omega_6 \omega_3^2 cs^2 + 18\omega_2^3 \omega_3^2 cs^2 + 72\omega_2^3 \omega_6 \omega_3^2 cs^2 - 12\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 \omega_6 \omega_3 + \omega_2^2 \omega_6^2 \omega_3^3 + 6\omega_2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_2^2 \omega_6^2 \omega_3 cs^2 - 36\omega_2^3 \omega_3^2 cs^2 - 3\omega_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 + 12\omega_2^2 \omega_6 \omega_3^2 cs^2 - 12\omega_2 \omega_6^2 \omega_3^2 cs^2) \frac{v_1 v_2}{6\omega_2^3 \omega_6^2 \omega_3^3}$$

**coefficient**  $C_{\mathbf{D}_x \mathbf{D}_y^3 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^3}$ :

$$C_{D_x D_y^3 v_1}^{(0), \text{SRT}} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_2^2 + \omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 - 54\omega - 36v_2^2 - \omega^3 + 20\omega^2 + 144\omega cs^2 + 54\omega v_2^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT}^1} = (-12\omega_6 \omega_3^3 cs^2 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - 48\omega_6^2 cs^2 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_3^3 + 48\omega_6 \omega_3^2 cs^2 + 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 12v_2^2 \omega_6 \omega_3^3 + 90\omega_6^2 \omega_3 cs^2 + 12\omega_3^3 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 12\omega_3^3 cs^2 - 44\omega_6^2 \omega_3^2 cs^2 - 8v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 - 36\omega_6 \omega_3 cs^2 + 4\omega_6^2 \omega_3^3 cs^2 + 6\omega_3^3 cs^2 + 9\omega_6 \omega_3^3 - 36\omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT}^2} = (-12cs^2 \omega_3^2 - 44cs^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 + 4cs^2 \omega_6^2 \omega_3^3 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 + 6cs^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3^2 - 48cs^2 \omega_6^2 - 12v_2^2 \omega_3^2 + 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 12v_2^2 \omega_6 \omega_3^3 + 90cs^2 \omega_6^2 \omega_3 + 12\omega_3^3 - 36cs^2 \omega_6 \omega_3 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 8v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 + 9\omega_6 \omega_3^3 - 12cs^2 \omega_6 \omega_3^3 - 36\omega_6 \omega_3^2 + 48cs^2 \omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM}^1} = (-36cs^2 \omega_6 \omega_3 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3^2 - 30cs^2 \omega_6 \omega_3^3 - 60cs^2 \omega_3^2 + 96cs^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^3 + 30cs^2 \omega_3^3 + 12\omega_3^2 - 26cs^2 \omega_6^2 \omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 14v_2^2 \omega_6^2 \omega_3^2 + 4cs^2 \omega_6^2 \omega_3^3 - 6\omega_3^3 + 9\omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3 + 18cs^2 \omega_6^2 \omega_3 - 36\omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM}^2} = (12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - 30\omega_6^2 \omega_3^3 cs^2 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3^2 + 18\omega_6^2 \omega_3 cs^2 - 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^3 + 96\omega_6 \omega_3^2 cs^2 + 12\omega_3^3 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 36\omega_6 \omega_3 cs^2 - 14v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 - 60\omega_3^2 cs^2 - 26\omega_6^2 \omega_3^2 cs^2 + 9\omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3 + 4\omega_6^2 \omega_3^3 cs^2 + 30\omega_3^3 cs^2 - 36\omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_x D_y^3 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^3}$ :

$$C_{D_x D_y^3 v_2}^{(0), \text{SRT}} = (12 - 56\omega^2 cs^2 - 12\omega^2 v_2^2 + 3\omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 - 18\omega - 12v_2^2 - \omega^3 + 8\omega^2 + 144\omega cs^2 + 18\omega v_2^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT}^1} = (-12\omega_2^3 \omega_6 \omega_3 cs^2 + 12\omega_2^2 \omega_6 \omega_3^2 - 12\omega_2^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_2^3 v_2^2 \omega_3^2 - 32\omega_2^3 \omega_6^2 \omega_3^2 cs^2 + 6\omega_2^3 v_2^2 \omega_3^3 - 6\omega_2^2 \omega_6 \omega_3^3 + 3\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 48\omega_2^2 \omega_6^2 \omega_3^2 cs^2 + 3\omega_2^3 \omega_6^2 \omega_3^2 + 24\omega_2^3 v_2^2 \omega_6^2 - 30\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 + 4\omega_2^3 \omega_6^2 \omega_3^3 cs^2 + 12\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 \omega_6^2 cs^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3 + 6\omega_2 \omega_6^2 \omega_3^3 cs^2 - 24\omega_2^2 \omega_6 \omega_3^3 cs^2 + 12v_2^2 \omega_6^2 \omega_3^3 + 3\omega_2^3 \omega_6 \omega_3^3 + 6\omega_2^3 \omega_3^2 cs^2 - 24\omega_2^2 v_2^2 \omega_6 \omega_3^2 - 24\omega_2^2 \omega_6^2 \omega_3 cs^2 - 6\omega_2^3 \omega_6 \omega_3^2 + 12\omega_2^2 v_2^2 \omega_6 \omega_3^3 - 12\omega_2^3 \omega_6 \omega_3^3 cs^2 - 18\omega_2 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^2 \omega_3^3 cs^2 + 36\omega_2^2 \omega_6^2 \omega_3 cs^2 + 12\omega_2^2 \omega_6 \omega_3^2 cs^2 - 12\omega_2^2 v_2^2 \omega_6 \omega_3^3 - 12\omega_2 \omega_6^2 \omega_3^2 cs^2 + 2\omega_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^2 \omega_6 \omega_3^2 cs^2 - 6\omega_2^2 \omega_6^2 \omega_3^2 + 36\omega_2^2 v_2^2 \omega_6 \omega_3^2) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT}^2} = (-24cs^2 \omega_2^2 \omega_6 \omega_3^2 + 12\omega_2^2 \omega_6 \omega_3^2 + 6cs^2 \omega_2 \omega_6^2 \omega_3^3 + 6cs^2 \omega_2^3 \omega_3^3 - 12\omega_2^3 v_2^2 \omega_3^2 + 36cs^2 \omega_2^3 \omega_6^2 \omega_3 + 6\omega_2^3 v_2^2 \omega_3^3 - 12cs^2 \omega_2^3 \omega_3^2 - 12cs^2 \omega_2 \omega_6^2 \omega_3^2 - 6\omega_2^2 \omega_6 \omega_3^3 + 3\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 12cs^2 \omega_2^2 \omega_6 \omega_3^3 - 32cs^2 \omega_2^2 \omega_6^2 \omega_3^2 + 3\omega_2^3 \omega_6^2 \omega_3^2 + 24\omega_2^3 v_2^2 \omega_6^2 - 30\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 - 12cs^2 \omega_2^3 \omega_6^2 + 4cs^2 \omega_2^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3 + 24cs^2 \omega_2^2 \omega_6^2 \omega_3 - 12cs^2 \omega_2^3 \omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3^3 + 3\omega_2^3 \omega_6 \omega_3^3 - 24\omega_2^2 v_2^2 \omega_6 \omega_3^2 - 24\omega_2^2 \omega_6^2 \omega_3 cs^2 - 6\omega_2^3 \omega_6 \omega_3^2 + 36cs^2 \omega_2^3 \omega_6 \omega_3^2 + 12\omega_2^2 v_2^2 \omega_6 \omega_3^3 - 18\omega_2 v_2^2 \omega_6^2 \omega_3^3 - 12cs^2 \omega_2^2 \omega_6 \omega_3 - 12cs^2 \omega_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 + 2\omega_2^2 \omega_6^2 \omega_3^3 - 6\omega_2^2 \omega_6^2 \omega_3^2 + 48cs^2 \omega_2^2 \omega_6^2 \omega_3^2 + 36\omega_2^2 v_2^2 \omega_6 \omega_3^2) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM}^1} = (-12\omega_2^3 cs^2 \omega_3^2 - 12\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^2 \omega_6 \omega_3^2 + 4\omega_2^3 cs^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 v_2^2 \omega_3^2 + 6\omega_2^3 cs^2 \omega_3^3 - 24\omega_2^2 cs^2 \omega_6^2 \omega_3 - 6\omega_2^3 v_2^2 \omega_3^3 - 32\omega_2^2 cs^2 \omega_6^2 \omega_3^2 - 6\omega_2^2 \omega_6 \omega_3^3 + 3\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^3 cs^2 \omega_6^2 \omega_3 + 3\omega_2^3 \omega_6^2 \omega_3^2 - 24\omega_2^3 v_2^2 \omega_6^2 - 12\omega_2^3 cs^2 \omega_6^2 + 48\omega_2^2 cs^2 \omega_6^2 \omega_3 + 30\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 - 12\omega_2^2 cs^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_6^2 \omega_3^3 + 3\omega_2^3 \omega_6 \omega_3^3 + 12\omega_2^2 cs^2 \omega_6 \omega_3^3 - 24\omega_2^2 v_2^2 \omega_6 \omega_3^2 - 6\omega_2^3 \omega_6 \omega_3^2 - 12\omega_2^3 cs^2 \omega_6 \omega_3^2 - 12\omega_2^2 v_2^2 \omega_6^2 \omega_3^3 - 18\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^3 cs^2 \omega_6 \omega_3^2 + 2\omega_2^2 \omega_6^2 \omega_3^3 + 6\omega_2 cs^2 \omega_6^2 \omega_3^3 - 6\omega_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_2^3 cs^2 \omega_6 \omega_3^3) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM}^2} = (-32\omega_2^3 \omega_6^2 \omega_3^2 cs^2 - 12\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^2 \omega_6 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_3^2 - 12\omega_2^3 \omega_6 \omega_3 cs^2 - 6\omega_2^3 v_2^2 \omega_3^3 - 6\omega_2^2 \omega_6 \omega_3^3 - 12\omega_2^2 \omega_6^2 \omega_3^3 cs^2 + 3\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 3\omega_2^3 \omega_6^2 \omega_3^2 - 24\omega_2^3 v_2^2 \omega_6^2 + 4\omega_2^3 \omega_6^2 \omega_3^2 cs^2 - 12\omega_2^3 \omega_6^2 cs^2 + 48\omega_2^2 \omega_6^2 \omega_3^2 cs^2 + 30\omega_2^3 v_2^2 \omega_6^2 \omega_3 - \omega_2^3 \omega_6^2 \omega_3^3 + 12\omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3 + 12\omega_2^2 cs^2 \omega_6 \omega_3^3 - 24\omega_2^2 v_2^2 \omega_6 \omega_3^2 - 6\omega_2^3 \omega_6 \omega_3^2 + 6\omega_2 \omega_6^2 \omega_3^3 cs^2 - 24\omega_2^2 \omega_6 \omega_3^2 cs^2 + 6\omega_2^3 \omega_3^2 cs^2 + 12\omega_2^2 v_2^2 \omega_6 \omega_3^3 + 36\omega_2^3 \omega_6 \omega_3^2 cs^2 - 18\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 2\omega_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^2 \omega_6 \omega_3 cs^2 - 12\omega_2^3 \omega_3^2 cs^2 - 6\omega_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 + 12\omega_2^2 \omega_6 \omega_3^2 cs^2 - 12\omega_2 \omega_6^2 \omega_3^2 cs^2) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_y^4 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x^2}$ :

$$C_{D_y^4 \rho}^{(0), \text{SRT}} = (-14\omega^2 cs^2 + 42\omega^2 v_2^2 + 108\omega v_2^4 - 72\omega cs^4 - 3\omega^3 v_2^2 + \omega^3 cs^2 - 84\omega^2 cs^2 v_2^2 - 24cs^2 + 72v_2^2 - 144cs^2 v_2^2 - 3\omega^3 cs^4 + 3\omega^3 v_2^4 + 216\omega cs^2 v_2^2 - 72v_2^4 + 48cs^4 - 42\omega^2 v_2^4 + 30\omega^2 cs^4 + 6\omega^3 cs^2 v_2^2 + 36\omega cs^2 - 108\omega v_2^2) \frac{1}{24\omega^3}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT}^1} = (72v_2^4 \omega_6 \omega_3^2 - 6\omega_6 \omega_3^3 cs^2 + 156v_2^2 \omega_6^2 \omega_3 cs^2 - 3\omega_6^2 \omega_3^3 cs^4 + 48v_2^2 \omega_6 \omega_3^2 cs^2 - 24v_2^2 \omega_3^2 cs^2 - 18v_2^4 \omega_6 \omega_3^3 + 48v_2^2 \omega_6 \omega_3 - 72v_2^2 \omega_6 \omega_3^2 + 24v_2^2 \omega_3^2 + 24\omega_6^2 \omega_3^2 cs^4 + 24\omega_6 \omega_3^2 cs^2 + 24\omega_6 \omega_3 cs^4 - 12v_2^2 \omega_3^3 + 18v_2^2 \omega_6 \omega_3^3 + 12v_2^2 \omega_3^2 cs^2 - 48v_2^4 \omega_6 \omega_3 + 12\omega_6^2 \omega_3 cs^2 - 12v_2^2 \omega_6 \omega_3^3 cs^2 - 24\omega_6 \omega_3^3 cs^4 - 3v_2^2 \omega_6^2 \omega_3^3 + 24v_2^2 \omega_6^2 \omega_3 - 96v_2^2 \omega_6^2 cs^2 - 8\omega_6^2 \omega_3^2 cs^2 + 24v_2^2 \omega_6^2 \omega_3^2 - 48\omega_6^2 \omega_3 cs^4 - 24\omega_6 \omega_3 cs^2 + 6v_2^2 \omega_6^2 \omega_3^3 cs^2 + \omega_6^2 \omega_3^3 cs^2 - 24v_2^2 \omega_6 \omega_3 cs^2 + 12v_2^4 \omega_3^3 + 3v_2^4 \omega_6^2 \omega_3^3 - 24v_2^2 \omega_6^2 \omega_3 + 6\omega_6 \omega_3^3 cs^4 - 24v_2^4 \omega_6^2 \omega_3^2 - 24v_2^4 \omega_3^2 - 72v_2^2 \omega_6^2 \omega_3^2 cs^2 + 24\omega_6^2 cs^4) \frac{1}{24\omega_6^2 \omega_3^3}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT}^2} = (72v_2^4 \omega_6 \omega_3^2 - 8cs^2 \omega_6^2 \omega_3^2 - 96cs^2 v_2^2 \omega_6^2 - 18v_2^4 \omega_6 \omega_3^3 - 48cs^4 \omega_6^2 \omega_3 + cs^2 \omega_6^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3 - 24cs^2 v_2^2 \omega_6 \omega_3 - 72v_2^2 \omega_6 \omega_3^2 + 24v_2^2 \omega_3^2 + 48cs^2 v_2^2 \omega_6 \omega_3^2 - 24cs^2 v_2^2 \omega_3^2 + 24cs^4 \omega_6^2 \omega_3^2 - 12v_2^2 \omega_3^3 + 12cs^2 v_2^2 \omega_3^3 - 12cs^2 v_2^2 \omega_6 \omega_3^3 + 18v_2^2 \omega_6 \omega_3^3 + 12cs^2 \omega_6^2 \omega_3 - 3cs^4 \omega_6^2 \omega_3^3 -$$

$$48v_2^4\omega_6\omega_3 - 24cs^2\omega_6\omega_3 - 3v_2^2\omega_6^2\omega_3^3 + 6cs^2v_2^2\omega_6^2\omega_3^3 + 24v_2^4\omega_6^2\omega_3 + 6cs^4\omega_6\omega_3^3 - 72cs^2v_2^2\omega_6^2\omega_3^2 + 24v_2^2\omega_6^2\omega_3^2 - 24cs^4\omega_6\omega_3^2 + 12v_2^4\omega_3^3 + 24cs^4\omega_6\omega_3 + 3v_2^2\omega_6^2\omega_3^3 + 156cs^2v_2^2\omega_6^2\omega_3 - 24v_2^2\omega_6^2\omega_3 - 6cs^2\omega_6\omega_3^3 + 24cs^4\omega_6^2 - 24v_2^4\omega_6^2\omega_3^2 - 24v_2^4\omega_3^2 + 24cs^2\omega_6\omega_3^2) \frac{1}{24\omega_6^2\omega_3^3}$$

$$C_{D_y^4\rho}^{(0),CLBM1} = (72v_2^4\omega_6\omega_3^2 + 6cs^4\omega_6\omega_3^3 - 24cs^2\omega_6\omega_3 + 144v_2^2cs^2\omega_6\omega_3^2 - 24cs^4\omega_6\omega_3^2 - 30v_2^4\omega_6\omega_3^3 - 72v_2^2cs^2\omega_6\omega_3^3 - 72v_2^2\omega_6\omega_3^2 + 72v_2^2\omega_3^2 - 6cs^2\omega_6\omega_3^3 + 24cs^4\omega_6\omega_3 + 24cs^2\omega_6\omega_3^2 + 72v_2^2cs^2\omega_6\omega_3 - 36v_2^2\omega_3^3 + 30v_2^2\omega_6\omega_3^3 - 36v_2^2cs^2\omega_6^2\omega_3 - 8cs^2\omega_6^2\omega_3^2 - 3v_2^2\omega_6^2\omega_3^3 + 12v_2^2\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^3 + 24cs^4\omega_6^2 - 48cs^4\omega_6^2\omega_3 + 24cs^4\omega_6^2\omega_3^2 + 108v_2^2cs^2\omega_3^3 + 36v_2^4\omega_3^3 + 3v_2^4\omega_6^2\omega_3^3 + 6v_2^2cs^2\omega_6^2\omega_3^3 - 12v_2^4\omega_6^2\omega_3^2 - 72v_2^4\omega_3^2 - 216v_2^2cs^2\omega_3^2 - 3cs^4\omega_6^2\omega_3^3 - 12v_2^2cs^2\omega_6^2\omega_3^2 + 12cs^2\omega_6^2\omega_3^2) \frac{1}{24\omega_6^2\omega_3^3}$$

$$C_{D_y^4\rho}^{(0),CLBM2} = (144v_2^2\omega_6\omega_3^2cs^2 + 72v_2^4\omega_6\omega_3^2 - 216v_2^2\omega_3^2cs^2 - 30v_2^4\omega_6\omega_3^3 - 6\omega_6\omega_3^3cs^2 - 36v_2^2\omega_6^2\omega_3cs^2 - 3\omega_6^2\omega_3^3cs^4 - 72v_2^2\omega_6\omega_3^2 + 24\omega_6\omega_3cs^4 + 72v_2^2\omega_3^2 + 108v_2^2\omega_3^3cs^2 + 12\omega_6^2\omega_3cs^2 - 72v_2^2\omega_6\omega_3^3cs^2 - 36v_2^2\omega_3^3 + 24\omega_6^2\omega_3^3cs^4 + 30v_2^2\omega_6\omega_3^3 + 24\omega_6\omega_3^3cs^2 - 3v_2^2\omega_6^2\omega_3^3 - 48\omega_6^2\omega_3cs^4 - 24\omega_6\omega_3cs^2 + 6v_2^2\omega_6^2\omega_3^3cs^2 + 12v_2^2\omega_6^2\omega_3^2 - 24\omega_6\omega_3^3cs^4 - 8\omega_6^2\omega_3^3cs^2 - 12v_2^2\omega_6^2\omega_3^3cs^2 + 36v_2^4\omega_3^3 + 3v_2^4\omega_6^2\omega_3^3 + 24\omega_6^2cs^4 + \omega_6^2\omega_3^3cs^2 + 72v_2^2\omega_6\omega_3cs^2 - 12v_2^4\omega_6^2\omega_3^2 - 72v_2^4\omega_3^2 + 6\omega_6\omega_3^3cs^4) \frac{1}{24\omega_6^2\omega_3^3}$$

**coefficient**  $C_{D_y^4v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_2^4}$  :

$$C_{D_y^4v_2}^{(0),SRT} = (24 - 26\omega^2cs^2 - 22\omega^2v_2^2 + 2\omega^3v_2^2 + \omega^3cs^2 - 48cs^2 - 36\omega - 36v_2^2 - \omega^3 + 14\omega^2 + 72\omega cs^2 + 54\omega v_2^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_y^4v_2}^{(0),MRT1} = (-6\omega_6\omega_3^3cs^2 - 12v_2^2\omega_6^2 + 8\omega_6^2\omega_3^2 - 24\omega_6^2cs^2 - \omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3 + 24v_2^2\omega_6\omega_3^2 - 12v_2^2\omega_3^2 + 24\omega_6\omega_3^2cs^2 + 6v_2^2\omega_3^3 - 6\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^3 + 42\omega_6^2\omega_3cs^2 + 12\omega_3^2 + 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^3 - 12\omega_3^2cs^2 - 20\omega_6^2\omega_3^2cs^2 - 16v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3 - 12\omega_6\omega_3cs^2 + \omega_6^2\omega_3^3cs^2 + 6\omega_3^3cs^2 + 6\omega_6\omega_3^3 + 24v_2^2\omega_6^2\omega_3 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4v_2}^{(0),MRT2} = (-12cs^2\omega_3^2 - 20cs^2\omega_6^2\omega_3^2 - 12v_2^2\omega_6^2 + 8\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^3 - \omega_6^2\omega_3^3 - 12v_2^2\omega_6\omega_3 + 6cs^2\omega_3^3 + 24v_2^2\omega_6\omega_3^2 - 24cs^2\omega_6^2 - 12v_2^2\omega_3^2 + 6v_2^2\omega_3^3 - 6\omega_6^2\omega_3 - 6v_2^2\omega_6\omega_3^3 + 42cs^2\omega_6^2\omega_3 + 12\omega_3^2 - 12cs^2\omega_6\omega_3 + 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^3 - 16v_2^2\omega_6^2\omega_3^2 - 6\omega_3^3 + 6\omega_6\omega_3^3 + 24v_2^2\omega_6^2\omega_3 - 6cs^2\omega_6\omega_3^3 - 24\omega_6\omega_3^2 + 24cs^2\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4v_2}^{(0),CLBM1} = (24cs^2\omega_6^2 - 12cs^2\omega_6\omega_3 - 12v_2^2\omega_6^2 + 2\omega_6^2\omega_3^2 - \omega_6^2\omega_3^3 + 60v_2^2\omega_6\omega_3 + 24v_2^2\omega_6\omega_3^2 - 84v_2^2\omega_3^2 - 24cs^2\omega_6\omega_3^3 - 60cs^2\omega_3^2 + 72cs^2\omega_6\omega_3^2 + 42v_2^2\omega_3^3 + 6\omega_6^2\omega_3 - 24v_2^2\omega_6\omega_3^3 + 30cs^2\omega_3^3 + 36\omega_3^2 - 2cs^2\omega_6^2\omega_3^2 - 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^3 + 2v_2^2\omega_6^2\omega_3^2 + cs^2\omega_6^2\omega_3^3 - 18\omega_3^3 + 12\omega_6\omega_3^3 - 12v_2^2\omega_6^2\omega_3 - 30cs^2\omega_6^2\omega_3 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

$$C_{D_y^4v_2}^{(0),CLBM2} = (24\omega_6^2cs^2 - 12v_2^2\omega_6^2 + 2\omega_6^2\omega_3^2 - 24\omega_6\omega_3^3cs^2 - \omega_6^2\omega_3^3 + 60v_2^2\omega_6\omega_3 + 24v_2^2\omega_6\omega_3^2 - 84v_2^2\omega_3^2 - 30\omega_6^2\omega_3cs^2 + 42v_2^2\omega_3^3 + 6\omega_6^2\omega_3 - 24v_2^2\omega_6\omega_3^3 + 72\omega_6\omega_3^2cs^2 + 36\omega_3^2 - 12\omega_6\omega_3 + 2v_2^2\omega_6^2\omega_3^3 - 12\omega_6\omega_3cs^2 + 2v_2^2\omega_6^2\omega_3^2 - 18\omega_3^3 - 60\omega_3^2cs^2 - 2\omega_6^2\omega_3^3cs^2 + 12\omega_6\omega_3^3 - 12v_2^2\omega_6^2\omega_3 + \omega_6^2\omega_3^3cs^2 + 30\omega_3^3cs^2 - 24\omega_6\omega_3^2) \frac{v_2\rho}{12\omega_6^2\omega_3^3}$$

**coefficient**  $C_{D_t^3D_zv_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t^3 \partial x_3}$  :

$$C_{D_t^3D_zv_3}^{(0),SRT} = (-2 + 3\omega - \omega^2) \frac{\rho}{2\omega^3}$$

$$C_{D_t^3D_zv_3}^{(0),MRT1} = (-2 - \omega_4^2 + 3\omega_4) \frac{\rho}{2\omega_4^3}$$

$$C_{D_t^3D_zv_3}^{(0),MRT2} = C_{D_t^3D_zv_3}^{(0),MRT1}$$

$$C_{D_t^3D_zv_3}^{(0),CLBM1} = C_{D_t^3D_zv_3}^{(0),MRT1}$$

$$C_{D_t^3D_zv_3}^{(0),CLBM2} = C_{D_t^3D_zv_3}^{(0),MRT1}$$

**coefficient**  $C_{D_t^2D_xD_zv_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t^2 \partial x_1 \partial x_3}$  :

$$C_{D_t^2D_xD_zv_1}^{(0),SRT} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_t^2D_xD_zv_1}^{(0),MRT1} = (13\omega_4^2\omega_2^2 - 6\omega_4^3 + 12\omega_4^2 + 7\omega_4^3\omega_2 - \omega_4^3\omega_2^2 + 12\omega_2^2 - 24\omega_4^2\omega_2 + 12\omega_4\omega_2 - 24\omega_4\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_2^2}$$

$$C_{D_t^2D_xD_zv_1}^{(0),MRT2} = C_{D_t^2D_xD_zv_1}^{(0),MRT1}$$

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_1}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t^2 D_x D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t^2 \partial x_1 \partial x_3}$ :

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}} = (13\omega_4^2 \omega_2^2 + 12\omega_4^2 - \omega_4^2 \omega_2^3 - 6\omega_2^3 + 12\omega_2^2 - 24\omega_4^2 \omega_2 + 12\omega_4 \omega_2 + 7\omega_4 \omega_2^3 - 24\omega_4 \omega_2^2) \frac{v_1 \rho}{12\omega_4^2 \omega_2^3}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT2}} = C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{CLBM1}} = C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_t^2 D_x D_z v_3}^{(0), \text{CLBM2}} = C_{D_t^2 D_x D_z v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_t D_x^2 D_z v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1^2 \partial x_3}$ :

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 \rho v_3}{6\omega^3}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{MRT1}} = (12\omega_4^2 \omega_2^2 - 12\omega_4^3 \omega_5 - 6\omega_5 \omega_2^3 - 6\omega_4 \omega_5 \omega_2^2 + 24\omega_4^3 \omega_5 \omega_2 - 6\omega_4^2 \omega_2^3 + 12\omega_4 \omega_5 \omega_2^3 + \omega_4^3 \omega_5 \omega_2^3 - 6\omega_4^3 \omega_2^2 - 10\omega_4^3 \omega_5 \omega_2^2 + 3\omega_4^3 \omega_2^3 - 12\omega_4^2 \omega_5 \omega_2 + 12\omega_4^2 \omega_5 \omega_2^2 - 7\omega_4^2 \omega_5 \omega_2^3) \frac{v_1 \rho v_3}{6\omega_4^3 \omega_5 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{MRT2}} = C_{D_t D_x^2 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{CLBM1}} = (6\omega_4^2 \omega_2^2 - 12\omega_4^3 - 7\omega_4^2 \omega_2^3 + 18\omega_4^3 \omega_2 - 6\omega_2^3 - 7\omega_4^3 \omega_2^2 + \omega_4^3 \omega_2^3 + 12\omega_4 \omega_2^3 - 6\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_4^3 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_1}^{(0), \text{CLBM2}} = C_{D_t D_x^2 D_z v_1}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_t D_x^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t \partial x_1^2 \partial x_3}$ :

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{SRT}} = (34\omega^2 cs^2 - 2\omega^2 v_1^2 - 2\omega^3 cs^2 + \omega^3 v_1^2 + 60cs^2 - 90\omega cs^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{MRT1}} = (9\omega_4 \omega_5 v_1^2 \omega_2^3 - 2\omega_4 \omega_5^2 \omega_2^3 cs^2 - 18\omega_5^2 \omega_2^2 cs^2 + 12\omega_4 \omega_5^2 cs^2 - 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 6\omega_4 \omega_2^3 cs^2 + 22\omega_4 \omega_5^2 \omega_2^2 cs^2 + 12\omega_4 \omega_5 v_1^2 \omega_2 + 12\omega_5 v_1^2 \omega_2^2 + 12\omega_4 \omega_2^2 cs^2 + 12\omega_4 \omega_5 \omega_2 cs^2 - 6\omega_5 v_1^2 \omega_2^3 + 3\omega_5^2 \omega_2^2 cs^2 + 36\omega_4 \omega_2^3 v_1^2 \omega_2 - 30\omega_4 \omega_5 \omega_2^2 cs^2 + 6\omega_5^2 v_1^2 \omega_2^2 - 30\omega_4 \omega_5^2 \omega_2 cs^2 - 6\omega_5 \omega_2^3 cs^2 - \omega_5^2 v_1^2 \omega_2^3 + 12\omega_5^2 \omega_2 cs^2 - 24\omega_4 \omega_5^2 v_1^2 + 12\omega_4 v_1^2 \omega_2^2 + 9\omega_4 \omega_5 \omega_2^3 cs^2 + \omega_4 \omega_5^2 v_1^2 \omega_2^3 - 12\omega_5^2 v_1^2 \omega_2 + 12\omega_5 \omega_2^2 cs^2 - 10\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{MRT2}} = (-6cs^2 \omega_5 \omega_2^3 + 9\omega_4 \omega_5 v_1^2 \omega_2^3 + 12cs^2 \omega_5 \omega_2^2 + 12\omega_4 cs^2 \omega_5 \omega_2 - 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 30\omega_4 cs^2 \omega_5 \omega_2^2 + 12\omega_4 \omega_5 v_1^2 \omega_2 + 12\omega_5 v_1^2 \omega_2^2 + 9\omega_4 cs^2 \omega_5 \omega_2^3 - 6\omega_5 v_1^2 \omega_2^3 + 36\omega_4 \omega_5^2 v_1^2 \omega_2 - 2\omega_4 cs^2 \omega_5^2 \omega_2^3 + 6\omega_5^2 v_1^2 \omega_2^2 + 22\omega_4 cs^2 \omega_5^2 \omega_2^2 + 12cs^2 \omega_5^2 \omega_2 - \omega_5^2 v_1^2 \omega_2^3 - 18cs^2 \omega_5^2 \omega_2^2 - 24\omega_4 \omega_5^2 v_1^2 + 12\omega_4 cs^2 \omega_2^2 - 30\omega_4 cs^2 \omega_5^2 \omega_2 + 12\omega_4 v_1^2 \omega_2^2 + \omega_4 \omega_5^2 v_1^2 \omega_2^3 - 12\omega_5^2 v_1^2 \omega_2 - 6\omega_4 cs^2 \omega_2^3 + 12\omega_4 cs^2 \omega_5^2 + 3cs^2 \omega_5^2 \omega_2^3 - 10\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{CLBM1}} = (12\omega_5^2 \omega_2 cs^2 + 9\omega_4 \omega_5 \omega_2^3 cs^2 - 9\omega_4 \omega_5 v_1^2 \omega_2^3 + 12\omega_5 \omega_2^2 cs^2 + 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 12\omega_4 \omega_5 v_1^2 \omega_2 - 30\omega_4 \omega_5 \omega_2^2 cs^2 - 12\omega_5 v_1^2 \omega_2^3 - 30\omega_4 \omega_5^2 \omega_2 cs^2 - 6\omega_5 \omega_2^3 cs^2 + 6\omega_5 v_1^2 \omega_2^3 - 36\omega_4 \omega_5^2 v_1^2 \omega_2 + 22\omega_4 \omega_5^2 \omega_2^2 cs^2 - 6\omega_5^2 v_1^2 \omega_2^2 + 12\omega_4 \omega_2^2 cs^2 + 12\omega_4 \omega_5 \omega_2 cs^2 - \omega_5^2 v_1^2 \omega_2^3 + 3\omega_5^2 \omega_2^3 cs^2 + 24\omega_4 \omega_5^2 v_1^2 - 12\omega_4 v_1^2 \omega_2^2 + \omega_4 \omega_5^2 v_1^2 \omega_2^3 - 2\omega_4 \omega_5^2 \omega_2^2 cs^2 + 12\omega_5^2 v_1^2 \omega_2 - 18\omega_5^2 \omega_2^2 cs^2 + 12\omega_4 \omega_5^2 cs^2 + 8\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4 \omega_2^3 cs^2 + 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

$$C_{D_t D_x^2 D_z v_3}^{(0), \text{CLBM2}} = (-18\omega_5^2 \omega_2^2 cs^2 + 12\omega_4 \omega_5^2 cs^2 - 9\omega_4 \omega_5 v_1^2 \omega_2^3 - 6\omega_4 \omega_2^3 cs^2 + 30\omega_4 \omega_5 v_1^2 \omega_2^2 - 2\omega_4 \omega_5^2 \omega_2^3 cs^2 + 12\omega_4 \omega_2^2 cs^2 - 12\omega_4 \omega_5 v_1^2 \omega_2 + 12\omega_4 \omega_5 \omega_2 cs^2 - 12\omega_5 v_1^2 \omega_2^2 + 3\omega_5^2 \omega_2^3 cs^2 + 22\omega_4 \omega_5^2 \omega_2^2 cs^2 + 6\omega_5 v_1^2 \omega_2^3 - 30\omega_4 \omega_5^2 \omega_2 cs^2 - 36\omega_4 \omega_5^2 v_1^2 \omega_2 - 6\omega_5 \omega_2^3 cs^2 - 6\omega_5^2 v_1^2 \omega_2^2 - 30\omega_4 \omega_5 \omega_2^2 cs^2 - \omega_5^2 v_1^2 \omega_2^3 + 24\omega_4 \omega_5^2 v_1^2 + 12\omega_5 \omega_2^2 cs^2 - 12\omega_4 v_1^2 \omega_2^2 + \omega_4 \omega_5^2 v_1^2 \omega_2^3 + 12\omega_5^2 \omega_2 cs^2 + 12\omega_5^2 v_1^2 \omega_2 + 9\omega_4 \omega_5 \omega_2^3 cs^2 + 8\omega_4 \omega_5^2 v_1^2 \omega_2^2 + 6\omega_4 v_1^2 \omega_2^3) \frac{\rho}{12\omega_4 \omega_5^2 \omega_2^3}$$

**coefficient**  $C_{D_x^3 D_z \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_3}$ :

$$C_{D_x^3 D_z \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_1 v_3}{6\omega^3}$$

$$C_{D_3 \geq p}^{(0), \text{MRT1}} = (6\omega_4^3\omega_2^2v_1^2\omega_2^2 + \omega_4^2\omega_5^2\omega_2^3 - 12\omega_4^3\omega_5\omega_2^2cs^2 + 6\omega_4\omega_2^3\omega_5^2cs^2 + 12\omega_4^2\omega_5^2v_1^2\omega_2 + 12\omega_4^3\omega_5\omega_2 - 12\omega_4^3\omega_2^3cs^2 - 12\omega_4^3\omega_5\omega_2^3cs^2 - 24\omega_4^3\omega_2^3\omega_2cs^2 - 3\omega_4^2\omega_2^3\omega_2^2 + 6\omega_4^3\omega_5\omega_2^3 - 12\omega_4^3\omega_2^2\omega_2^2cs^2 + 6\omega_4^2\omega_2^3v_1^2\omega_2^3 + 6\omega_4^2\omega_2^3cs^2 + 6\omega_4^2\omega_5\omega_2^3cs^2 + 78\omega_4^3\omega_2^3\omega_2cs^2 - 36\omega_4^3\omega_2^3cs^2 + 6\omega_4^3\omega_2^2 - 24\omega_4^3\omega_5\omega_2^2 - 12\omega_4^3\omega_2^3v_1^2\omega_2^2 - 30\omega_4^3\omega_2^3v_1^2\omega_2 - 3\omega_4^3\omega_2^3 + 42\omega_4^3\omega_5\omega_2^3cs^2 - 12\omega_4^3\omega_2^3\omega_2^2cs^2 + 6\omega_4^3v_1^2\omega_2^3 + 7\omega_4^3\omega_5\omega_2^2 + 6\omega_4^2\omega_5v_1^2\omega_2^2 - 24\omega_4^3\omega_5\omega_2cs^2 - 12\omega_4^3\omega_5v_1^2\omega_2^2 - \omega_4^2\omega_5^2\omega_2^3 - 12\omega_4^2v_1^2\omega_2^3 - 48\omega_4^3\omega_5^2\omega_2^2cs^2 + 6\omega_5^2v_1^2\omega_2^3 - 24\omega_4^3\omega_5v_1^2\omega_2 + 24\omega_4^3\omega_5\omega_2v_1^2\omega_2 + 42\omega_4^3\omega_5v_1^2\omega_2^2 + 42\omega_4^2\omega_5\omega_2^3cs^2 - 12\omega_4^2\omega_5^2v_1^2\omega_2^3 + 6\omega_4^2\omega_5\omega_2^2 - 12\omega_4^3\omega_5v_1^2\omega_2^2 + 6\omega_4^3\omega_2^3\omega_5^2cs^2 - 3\omega_4^3\omega_5\omega_2^2 + 6\omega_4\omega_2^3v_1^2\omega_2^2 - 6\omega_4^3\omega_2^3\omega_2) \frac{v_1v_3}{6\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{\text{D3} \neq p}^{(0), \text{MRT2}} = (6\omega_4^3 \omega_2^2 v_1^2 \omega_2^2 + \omega_4^2 \omega_5^2 \omega_2^3 - 12\omega_4^3 c s^2 \omega_2^2 \omega_2^2 + 12\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 + 12\omega_4^3 \omega_5 \omega_2 + 78\omega_4^3 c s^2 \omega_2^2 \omega_2 + 42\omega_4^3 c s^2 \omega_2^2 \omega_2^2 - 3\omega_4^2 \omega_2^2 \omega_2^2 + 6\omega_4^3 \omega_5 \omega_2^3 + 6\omega_4^2 \omega_2^2 v_1^2 \omega_2^3 - 24\omega_4^2 c s^2 \omega_2^2 \omega_2^2 - 48\omega_4^3 c s^2 \omega_2^2 \omega_2^2 + 6\omega_4^3 \omega_2^3 - 21\omega_4^3 \omega_5 \omega_2^2 - 12\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 - 30\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 - 3\omega_4^3 \omega_2^3 + 6\omega_4^3 c s^2 \omega_2^2 \omega_2^3 + 6\omega_4^3 v_1^2 \omega_2^3 + 7\omega_4^3 \omega_2^2 \omega_2^2 + 6\omega_4 c s^2 \omega_2^2 \omega_2^2 + 6\omega_4^2 \omega_5 v_1^2 \omega_2^2 - 36\omega_4^3 c s^2 \omega_2^2 \omega_2^2 + 6\omega_4^3 c s^2 \omega_2^2 \omega_2^2 - 12\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 - 12\omega_4 c s^2 \omega_2^2 \omega_2^2 - \omega_4^3 \omega_2^2 \omega_2^2 - 12\omega_4^3 v_1^2 \omega_2^2 + 42\omega_4^3 c s^2 \omega_2^2 \omega_2^2 - 12\omega_4^3 c s^2 \omega_2^2 \omega_2^2 + 6\omega_5^2 v_1^2 \omega_2^2 - 12\omega_4^2 c s^2 \omega_2^2 \omega_2^2 - 12\omega_4^3 c s^2 \omega_2^2 \omega_2^2 - 12\omega_4^3 \omega_5 v_1^2 \omega_2^2 + 6\omega_4^3 c s^2 \omega_2^2 \omega_2^2 - 3\omega_4^2 \omega_5 \omega_2^3 + 6\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4^3 \omega_2^2 \omega_2^2) \frac{v_1 v_3}{6\omega_4^3 \omega_5^2 \omega_2^3}$$

$$C_{D_3^3 D_{\Sigma^2 \rho}}^{(0), \text{CLBM1}} = (-6\omega_4^3 \omega_5^2 v_1^2 \omega_2^2 + \omega_4^2 \omega_5^2 \omega_2^3 + 36\omega_4^2 \omega_5^2 \omega_2^2 c s^2 + 12\omega_4^3 \omega_5 \omega_2 + 6\omega_4^3 \omega_5^2 \omega_2^3 c s^2 - 3\omega_2^3 \omega_5^2 \omega_2^2 + 6\omega_4^3 \omega_5 \omega_2^3 + 6\omega_4^2 \omega_5^2 v_1^2 \omega_2^3 - 12\omega_4^2 \omega_5^2 \omega_2^3 c s^2 - 24\omega_4^3 \omega_5 \omega_2 c s^2 + 6\omega_4^3 \omega_5^2 - 21\omega_4^3 \omega_5 \omega_2^2 - 6\omega_4^2 \omega_5^2 v_1^2 \omega_2^3 + 12\omega_4^3 \omega_5^2 v_1^2 \omega_2^2 - 3\omega_4^3 \omega_2^3 - 36\omega_4^3 \omega_5^2 v_1^2 c s^2 + 18\omega_4^3 \omega_2^3 c s^2 - 6\omega_4^3 v_1^2 \omega_2^3 - 12\omega_4^3 \omega_5^2 c s^2 + 12\omega_4^2 \omega_5^3 c s^2 + 7\omega_4^3 \omega_5^2 \omega_2^2 + 36\omega_4^3 \omega_5^2 c s^2 - 12\omega_4^2 \omega_5^2 c s^2 - \omega_4^4 \omega_5^2 \omega_2^3 + 12\omega_4^3 v_1^2 \omega_2^3 + 6\omega_4^3 v_1^2 c s^2 - 24\omega_4^3 \omega_5 v_1^2 \omega_2 + 72\omega_4^3 \omega_5 \omega_2^3 c s^2 + 12\omega_4^3 \omega_5 v_1^2 \omega_2 - 24\omega_4^3 \omega_5 \omega_2^3 c s^2 - 12\omega_4 \omega_5^2 v_1^2 \omega_2^3 - 36\omega_4^3 \omega_2^3 c s^2 + 6\omega_4^2 \omega_5 \omega_2^2 + 6\omega_4 \omega_5^2 \omega_2^3 c s^2 - 24\omega_4^3 \omega_5 \omega_2^3 c s^2 - 3\omega_4^3 \omega_5 \omega_2^3 + 6\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4^3 \omega_5^2 \omega_2 - 12\omega_4^2 \omega_5^2 \omega_2 c s^2) \frac{v_1 v_3}{6\omega_4^3 \omega_5^2 \omega_2^3}$$

$$C_{D_3^2 D_2 \rho}^{(0), \text{CLMB2}} = (-6\omega_4^3 \omega_5^2 v_1^2 \omega_2^2 - 24\omega_4^3 \omega_5 \omega_2^3 c s^2 + \omega_4^4 \omega_5^2 \omega_3^2 - 12\omega_4^2 \omega_5^2 \omega_2 c s^2 + 12\omega_4^3 \omega_5 \omega_2 - 24\omega_4^4 \omega_5 \omega_2^2 c s^2 - 36\omega_4^4 \omega_5^2 c s^2 - 3\omega_4^4 \omega_5^2 \omega_2^2 + 6\omega_4 \omega_5^2 \omega_3^2 c s^2 + 6\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 + 72\omega_4^3 \omega_5 \omega_2^2 c s^2 + 6\omega_4^4 \omega_2^2 + 18\omega_4^3 \omega_2^3 c s^2 - 12\omega_4 \omega_5^2 \omega_2^3 c s^2 + 12\omega_4^2 \omega_5 \omega_2^3 c s^2 - 21\omega_4^3 \omega_5 \omega_2^2 - 6\omega_4^4 \omega_5^2 v_1^2 \omega_2^2 + 12\omega_4^3 \omega_5^2 v_1^2 \omega_2 - 3\omega_4^3 \omega_2^3 + 36\omega_4^4 \omega_5^2 \omega_2 c s^2 - 12\omega_4^3 \omega_5^2 c s^2 - 6\omega_4^4 v_1^2 \omega_2^3 + 7\omega_4^3 \omega_5^2 \omega_2^2 - 36\omega_4^4 \omega_5^2 \omega_2^2 c s^2 - 12\omega_4^2 \omega_5^2 \omega_2^3 c s^2 - \omega_4^3 \omega_5^2 \omega_2^3 + 12\omega_4^3 v_1^2 \omega_2^2 - 24\omega_4^3 \omega_5 \omega_2 c s^2 + 6\omega_5^2 v_1^2 \omega_2^3 - 24\omega_4^4 \omega_5 v_1^2 \omega_2 + 6\omega_4^4 \omega_5^2 c s^2 + 12\omega_4^3 \omega_5 v_1^2 \omega_2^2 - 12\omega_4 \omega_5^2 v_1^2 \omega_2^3 + 6\omega_4^4 \omega_5 \omega_2^2 - 3\omega_4^4 \omega_5 \omega_2^2 + 6\omega_4 \omega_5^2 v_1^2 \omega_2^2 - 6\omega_4^3 \omega_5^2 \omega_2 + 36\omega_4^4 \omega_5^2 \omega_2^2 c s^2) \frac{\gamma_1 \gamma_2}{6\omega_4^3 \omega_5^2 \omega_2^3}$$

coefficient  $C_{D_x^3 D_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_3}$ :

$$C_{D_x^3 D_z v_1}^{(0), \text{SRT}} = (12 - 56\omega^2 cs^2 - 12\omega^2 v_1^2 - 12v_1^2 + 4\omega^3 cs^2 + 3\omega^3 v_1^2 - 96cs^2 - 18\omega - \omega^3 + 8\omega^2 + 18\omega v_1^2 + 144\omega cs^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_3 D_2 v_1}^{(0), \text{MRT1}} = (2\omega_4^2 \omega_3^2 \omega_2^2 - 24\omega_4^2 \omega_5 \omega_3^2 c s^2 + 6\omega_4 \omega_3^2 \omega_2^2 c s^2 - 12\omega_3^3 \omega_2^2 c s^2 - 12\omega_4^3 \omega_5 \omega_3^2 c s^2 + 3\omega_4^3 \omega_2^2 v_1^2 \omega_3^2 - 24\omega_4^2 \omega_5^2 \omega_2 c s^2 - 6\omega_4^2 \omega_5^2 \omega_2^2 + 3\omega_4^3 \omega_5 \omega_2^2 - 12\omega_4^2 \omega_5^2 \omega_2^2 c s^2 + 6\omega_4^3 \omega_3^2 c s^2 + 12\omega_4^2 \omega_5 \omega_3^2 c s^2 + 36\omega_3^3 \omega_5^2 \omega_2 c s^2 - 12\omega_4^3 \omega_2^2 c s^2 - 6\omega_4^3 \omega_5 \omega_2^2 + 12\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 - 30\omega_3^3 \omega_5^2 v_1^2 \omega_2 + 36\omega_3^3 \omega_5 \omega_2^2 c s^2 - 12\omega_4^2 \omega_5^2 \omega_3^2 c s^2 + 6\omega_4^3 v_1^2 \omega_3^2 + 3\omega_4^3 \omega_2^2 \omega_2^2 + 12\omega_2^2 \omega_5 v_1^2 \omega_2^2 - 12\omega_3^3 \omega_5 \omega_2 c s^2 - 24\omega_4^2 \omega_5 v_1^2 \omega_2^2 - \omega_4^3 \omega_5^2 \omega_3^2 - 12\omega_4^3 v_1^2 \omega_2^2 - 32\omega_3^3 \omega_5^2 \omega_2^2 c s^2 + 12\omega_5^2 v_1^2 \omega_2^2 - 12\omega_4^3 \omega_5 v_1^2 \omega_2 + 24\omega_4^2 \omega_5^2 v_1^2 + 36\omega_4 \omega_5 v_1^2 \omega_2^2 + 48\omega_4^2 \omega_5^2 \omega_2^2 c s^2 - 18\omega_4 \omega_5^2 v_1^2 \omega_2^2 + 12\omega_4^2 \omega_5 \omega_2^2 - 12\omega_4^3 \omega_5 v_1^2 \omega_2^2 + 4\omega_4^3 \omega_5^2 \omega_2^2 c s^2 - 6\omega_4^3 \omega_5 \omega_2^2) \frac{\rho v_3}{12\omega_4^2 \omega_5^2 \omega_2^2}$$

$$C_{D_3^2 D_5 v_1}^{(0), \text{MRT}^2} = (2\omega_4^2 \omega_5^2 \omega_2^2 - 12\omega_4^2 c s^2 \omega_5^2 \omega_2^2 + 36\omega_4^2 c s^2 \omega_5^2 \omega_2 + 3\omega_4^3 \omega_5^2 v_1^2 \omega_3^2 + 48\omega_4^2 c s^2 \omega_5^2 \omega_2^2 - 6\omega_4^2 \omega_5^2 \omega_2^2 + 3\omega_4^3 \omega_5 \omega_3^2 - 24\omega_4^2 c s^2 \omega_5^2 \omega_2 - 6\omega_4^2 \omega_5^2 \omega_2^2 - 6\omega_4^2 \omega_5 \omega_2^2 + 12\omega_4^2 \omega_5^2 v_1^2 \omega_2^2 - 30\omega_4^3 \omega_5^2 v_1^2 \omega_2 + 4\omega_4^3 c s^2 \omega_5^2 \omega_3^2 + 6\omega_4^3 v_1^2 \omega_3^2 + 3\omega_4^3 \omega_5^2 \omega_2^2 + 6\omega_4 c s^2 \omega_5^2 \omega_3^2 + 12\omega_4^2 \omega_5 v_1^2 \omega_3^2 - 12\omega_4^2 c s^2 \omega_5^2 + 6\omega_4^3 c s^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_5 \omega_3^2 - 24\omega_4^2 \omega_5 v_1^2 \omega_2^2 - 12\omega_4 c s^2 \omega_5^2 \omega_2^2 - \omega_4^3 \omega_5^2 \omega_3^2 - 12\omega_4^2 v_1^2 \omega_2^2 + 36\omega_4^2 c s^2 \omega_5 \omega_2^2 - 12\omega_4^3 c s^2 \omega_2^2 + 12\omega_5^2 v_1^2 \omega_3^2 - 12\omega_4^3 \omega_5 v_1^2 \omega_2 + 24\omega_4^2 \omega_5^2 v_1^2 - 12\omega_4^2 c s^2 \omega_5 \omega_2 + 36\omega_4^2 \omega_5 v_1^2 \omega_2^2 - 18\omega_4 \omega_5^2 v_1^2 \omega_2^2 + 12\omega_4^2 \omega_5 \omega_2^2 - 24\omega_4^2 c s^2 \omega_5 \omega_2^2 - 12\omega_4^2 \omega_5 v_1^2 \omega_3^2 + 12\omega_4^2 c s^2 \omega_5 \omega_2^2 - 6\omega_4^2 \omega_5 \omega_3^2) \frac{\rho v_3}{12\omega_4^2 \omega_5^2 \omega_3^2}$$

$$C_{D_3^+ D_2 v_1}^{(0), CLMB1} = (-12\omega_3^3\omega_5^2v_1^2\omega_2^2 + 2\omega_4\omega_5^2\omega_3^2 + 48\omega_2^2\omega_5^2\omega_3^2cs^2 + 4\omega_4^3\omega_5^2\omega_3^2cs^2 + 3\omega_4^3\omega_5^2v_1^2\omega_3^2 - 6\omega_4^2\omega_5^2\omega_2^2 + 3\omega_4^3\omega_5\omega_2^2 - 12\omega_4^2\omega_5^2\omega_2^2cs^2 - 6\omega_4^3\omega_5\omega_2^2 - 12\omega_4^2\omega_5^2v_1^2\omega_2^2 + 30\omega_4^3\omega_5^2v_1^2\omega_2 - 32\omega_3^3\omega_5^2\omega_2^2cs^2 + 6\omega_4^3\omega_3^2cs^2 - 6\omega_4^3v_1^2\omega_3^2 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 12\omega_2^2\omega_5\omega_3^2cs^2 + 3\omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^2\omega_5^2v_1^2\omega_3^2 + 36\omega_4^3\omega_5^2\omega_2cs^2 - 12\omega_3^3\omega_5^2cs^2 - 24\omega_4^2\omega_5v_1^2\omega_2^2 - \omega_4^3\omega_5^2\omega_2^2 + 12\omega_4^3v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_3^2 + 12\omega_4^3\omega_5v_1^2\omega_2 - 24\omega_4^3\omega_5^2v_1^2 + 36\omega_4^3\omega_5\omega_2^2cs^2 - 12\omega_4^3\omega_5v_1^2\omega_2 - 24\omega_4^2\omega_5\omega_2^2cs^2 - 18\omega_4\omega_5^2v_1^2\omega_3^2 - 12\omega_4^3\omega_2^2cs^2 + 12\omega_4^2\omega_5\omega_2^2 + 6\omega_4\omega_5^2\omega_3^2cs^2 - 12\omega_4^3\omega_5\omega_2^2cs^2 - 6\omega_4^2\omega_5\omega_3^2 - 24\omega_4^2\omega_5^2\omega_2cs^2) \frac{\rho v_1}{12\omega_4^3\omega_5^2\omega_3^2}$$

$$C_{\vec{D}_3 \vec{D}_2 \vec{v}_1}^{(0), \text{CLB M2}} = (-12\omega_3^2 \omega_5^2 v_1^2 \omega_2^2 - 12\omega_3^4 \omega_5 \omega_3^2 c^2 + 2\omega_4^2 \omega_5^2 \omega_3^2 - 24\omega_4 \omega_5^2 \omega_2 c^2 + 3\omega_3^4 \omega_5^2 v_1^2 \omega_3^2 - 24\omega_3^2 \omega_5 \omega_3^2 c^2 - 12\omega_4^3 \omega_3^2 c^2 - 6\omega_4^2 \omega_5^2 \omega_2^2 + 6\omega_3^4 \omega_5 \omega_3^2 c^2 + 3\omega_4^3 \omega_5 \omega_3^2 + 36\omega_4^2 \omega_5 \omega_2^2 c^2 + 6\omega_3^4 \omega_3^2 c^2 - 12\omega_4 \omega_2^2 \omega_3^2 c^2 + 12\omega_4^2 \omega_5 \omega_3^2 c^2 - 6\omega_4^3 \omega_5 \omega_3^2 + 12\omega_3^2 \omega_5^2 v_1^2 \omega_2^2 + 30\omega_4^3 \omega_2^2 v_1^2 \omega_2 + 36\omega_4^2 \omega_5^2 \omega_2 c^2 - 12\omega_3^4 \omega_5^2 c^2 - 6\omega_3^3 v_1^2 \omega_3^2 + 3\omega_4^3 \omega_5^2 \omega_3^2 + 12\omega_4^2 \omega_5 v_1^2 \omega_3^2 - 32\omega_4^3 \omega_5^2 \omega_2^2 c^2 - 24\omega_4^2 \omega_5 v_1^2 \omega_2^2 - 12\omega_4^2 \omega_2^2 \omega_3^2 c^2 - \omega_4^3 \omega_5^2 \omega_3^2 + 12\omega_3^4 v_1^2 \omega_2^2 - 12\omega_4^3 \omega_5 \omega_2 c^2 + 12\omega_5^2 v_1^2 \omega_3^2 + 12\omega_4^2 \omega_5 v_1^2 \omega_2 - 24\omega_4^3 \omega_5^2 v_1^2 + 4\omega_4^2 \omega_5^2 \omega_3^2 c^2 - 12\omega_4^3 \omega_5 v_1^2 \omega_2^2 - 18\omega_4 \omega_5^2 v_1^2 \omega_3^2 + 12\omega_4^2 \omega_5 \omega_2^2 - 6\omega_4^3 \omega_5 \omega_3^2 + 48\omega_4^2 \omega_5^2 \omega_2^2 c^2) \frac{\rho \nu_3}{12\omega_3^2 \omega_5^2 \omega_3^2}$$

coefficient  $C_{D_x^3 D_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1^3 \partial x_3}$ :

$$C_{\mathbf{D}_x^3 \mathbf{D}_z v_3}^{(0), \text{SRT}} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_1^2 - 36v_1^2 + 4\omega^3 cs^2 + \omega^3 v_1^2 - 96cs^2 - 54\omega - \omega^3 + 20\omega^2 + 54\omega v_1^2 + 144\omega cs^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{\text{D}_3^+ \text{D}_2 \nu_3}^{(0), \text{MRT1}} = (-36\omega_5\omega_2cs^2 + 9\omega_5\omega_2^3 + 6\omega_2^3cs^2 - 48\omega_5^2cs^2 - 44\omega_5^2\omega_2^2cs^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 12\omega_2^2cs^2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^2 + 4\omega_5^2\omega_2^2cs^2 - 8\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 - 12\omega_5\omega_2^2cs^2 + \omega_5^2v_1^2\omega_2^2 + 11\omega_5^2\omega_2^2 + 90\omega_5^2\omega_2cs^2 + 6v_1^2\omega_2^3 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 48\omega_5\omega_2^2cs^2 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT}^2} = (-12cs^2\omega_5\omega_2^3 + 9\omega_5\omega_2^3 + 48cs^2\omega_5\omega_2^2 - 36\omega_5\omega_2^2 - 36\omega_5v_1^2\omega_2 - 6\omega_2^3 + 24\omega_5\omega_2 - 36cs^2\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 12\omega_5v_1^2\omega_2^3 - 8\omega_5^2v_1^2\omega_2^2 + 90cs^2\omega_5^2\omega_2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^2 + 11\omega_5^2\omega_2^2 - 44cs^2\omega_5^2\omega_2^2 + 6v_1^2\omega_2^3 + 6cs^2\omega_2^3 - 48cs^2\omega_5^2 - 12v_1^2\omega_2^2 - \omega_5^2\omega_2^3 + 4cs^2\omega_5^2\omega_2^3 + 12\omega_5^2v_1^2 - 12cs^2\omega_2^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^1} = (18\omega_5^2\omega_2cs^2 + 9\omega_5\omega_2^3 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 96\omega_5\omega_2^2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 12\omega_2^2 - 30\omega_5\omega_2^3cs^2 - 6\omega_5v_1^2\omega_2^3 - 60\omega_2^2cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^3 + 4\omega_5^2\omega_2^3cs^2 + 11\omega_5^2\omega_2^2 + 30\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6v_1^2\omega_2^3 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - 26\omega_5^2\omega_2^2cs^2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^2} = (-26\omega_5^2\omega_2^2cs^2 + 9\omega_5\omega_2^3 - 36\omega_5\omega_2^2 - 60\omega_5v_1^2\omega_2 + 30\omega_2^3cs^2 - 36\omega_5\omega_2cs^2 - 6\omega_2^3 + 24\omega_5\omega_2 + 48\omega_5v_1^2\omega_2^2 + 4\omega_5^2\omega_2^3cs^2 + 12\omega_2^2 - 60\omega_2^2cs^2 - 6\omega_5v_1^2\omega_2^3 - 30\omega_5\omega_2^3cs^2 - 14\omega_5^2v_1^2\omega_2^2 - 12\omega_5^2\omega_2 + \omega_5^2v_1^2\omega_2^3 + 11\omega_5^2\omega_2^2 + 96\omega_5\omega_2^2cs^2 - 6v_1^2\omega_2^3 + 18\omega_5^2\omega_2cs^2 + 12v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2 - \omega_5^2\omega_2^3 + 12\omega_5^2v_1^2) \frac{v_1\rho}{12\omega_5^2\omega_2^3}$$

**coefficient**  $C_{D_t^2 D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t^2 \partial x_2 \partial x_3}$ :

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT}^1} = (-24\omega_4\omega_3^2 - 6\omega_4^3 + 12\omega_4^2 + 12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4^2\omega_3 - \omega_4^3\omega_3^2 + 7\omega_4^3\omega_3 + 13\omega_4^2\omega_3^2) \frac{\rho v_3}{12\omega_4^3\omega_3^2}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT}^2} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT}^1}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{CLBM}^1} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT}^1}$$

$$C_{D_t^2 D_y D_z v_2}^{(0), \text{CLBM}^2} = C_{D_t^2 D_y D_z v_2}^{(0), \text{MRT}^1}$$

**coefficient**  $C_{D_t^2 D_y D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t^2 \partial x_2 \partial x_3}$ :

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{SRT}} = (36 - 54\omega - \omega^3 + 20\omega^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT}^1} = (-24\omega_4\omega_3^2 + 12\omega_4^2 + 7\omega_4\omega_3^3 + 12\omega_4\omega_3 + 12\omega_3^2 - 24\omega_4^2\omega_3 - 6\omega_3^3 - \omega_4^2\omega_3^3 + 13\omega_4^2\omega_3^2) \frac{v_2\rho}{12\omega_4^3\omega_3^3}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT}^2} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT}^1}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{CLBM}^1} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT}^1}$$

$$C_{D_t^2 D_y D_z v_3}^{(0), \text{CLBM}^2} = C_{D_t^2 D_y D_z v_3}^{(0), \text{MRT}^1}$$

**coefficient**  $C_{D_t D_x D_y D_z v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{SRT}} = (-20 + 30\omega + \omega^3 - 12\omega^2) \frac{v_2\rho v_3}{2\omega^3}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT}^1} = (-12\omega_4^2\omega_2\omega_3 - 6\omega_4^3\omega_2 - 6\omega_4\omega_3^3 - 16\omega_4^2\omega_2\omega_3^3 + 30\omega_4^2\omega_2\omega_3^2 - 4\omega_4^3\omega_3^3 + 18\omega_4\omega_2\omega_3^3 - 6\omega_2\omega_3^3 + 18\omega_4^3\omega_2\omega_3 - 12\omega_4\omega_2\omega_3^2 + 12\omega_4^3\omega_3^2 - 16\omega_4^3\omega_2\omega_3^2 + 12\omega_4^2\omega_3^3 - 6\omega_4^3\omega_3 - 12\omega_4^2\omega_3^2 + 3\omega_4^3\omega_2\omega_3^3) \frac{v_2\rho v_3}{6\omega_4^3\omega_2\omega_3^3}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT}^2} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT}^1}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{CLBM}^1} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT}^1}$$

$$C_{D_t D_x D_y D_z v_1}^{(0), \text{CLBM}^2} = C_{D_t D_x D_y D_z v_1}^{(0), \text{MRT}^1}$$

**coefficient**  $C_{D_t D_x D_y D_z v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t \partial x_1 \partial x_2 \partial x_3}$ :

$$C_{D_t D_x D_y D_z v_2}^{(0), \text{SRT}} = (-20 + 30\omega + \omega^3 - 12\omega^2) \frac{v_1\rho v_3}{2\omega^3}$$



$$8\omega_4^3\omega_5^2v_1^2\omega_2^3\omega_3 - \omega_4^3v_1^2\omega_2^3\omega_3^3 + 3\omega_5^2v_1^2\omega_2^3\omega_3^3 + 7\omega_1^3\omega_5^2v_1^2\omega_2^3\omega_3^2 - 6\omega_4^3\omega_5^2\omega_2^3\omega_3^3cs^2 + \omega_4^3\omega_5^2\omega_2^3\omega_3cs^2 + 2\omega_4^3\omega_5^2v_1^2\omega_3^3 + 2\omega_4^3\omega_5^2v_1^2\omega_2\omega_3^3 - 2\omega_4^3\omega_5^2\omega_2^3cs^2 + 2\omega_4^3v_1^2\omega_2^3\omega_3^3 - 2\omega_4^3\omega_5^2\omega_2^3\omega_3^3cs^2 - 2\omega_4^3\omega_5^2v_1^2\omega_2^3\omega_3^3 + 4\omega_4^3\omega_5^2v_1^2\omega_2\omega_3 + \omega_4^3\omega_5^2\omega_2^3\omega_3^3cs^2 + 2\omega_4^3\omega_5^2v_1^2\omega_2^3\omega_3^3) \frac{v_2\rho v_3}{\omega_4^3\omega_5^2\omega_2^3\omega_3^3}$$

**coefficient**  $C_{D_x^2 D_y D_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{D_x^2 D_y D_z v_1}^{(0), \text{SRT}} = (132 - 198\omega - 5\omega^3 + 76\omega^2) \frac{v_1 v_2 \rho v_3}{6\omega^3}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), \text{MRT1}} = (18\omega_4\omega_2^3\omega_3^2 + 28\omega_4^3\omega_2^3\omega_3 - 30\omega_4^3\omega_2^3\omega_3 + 12\omega_2^3\omega_3^3 - 30\omega_4^3\omega_2^3\omega_3^2 - 30\omega_4\omega_2^3\omega_3^3 - 5\omega_4^3\omega_2^3\omega_3 + 6\omega_4^3\omega_2^3\omega_3 + 18\omega_2^3\omega_2\omega_3^3 + 12\omega_4^3\omega_2^3 + 6\omega_4\omega_2^3\omega_3^3 + 24\omega_4^3\omega_2^3\omega_3^2 + 12\omega_4^3\omega_3^3 + 12\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4^3\omega_2^3\omega_3 - 30\omega_4^3\omega_2^3\omega_3^2 + 18\omega_4^3\omega_2\omega_3^3 - 42\omega_4^3\omega_2^3\omega_3^2 + 24\omega_4^3\omega_2^3\omega_3^3 - 36\omega_4^3\omega_2\omega_3^3) \frac{v_1 v_2 \rho v_3}{6\omega_4^3\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), \text{CLBM1}} = C_{D_x^2 D_y D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_1}^{(0), \text{CLBM2}} = C_{D_x^2 D_y D_z v_1}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x^2 D_y D_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{SRT}} = (-56\omega^2cs^2 + 52\omega^2v_1^2 + 84v_1^2 + 4\omega^3cs^2 - 5\omega^3v_1^2 - 96cs^2 - 126\omega v_1^2 + 144\omega cs^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT1}} = (40\omega_4^3\omega_5^2v_1^2\omega_2^2 - 24\omega_4^3\omega_5^2\omega_2^2cs^2 + 6\omega_4\omega_5^2\omega_2^3cs^2 + 48\omega_4^3\omega_5^2v_1^2\omega_2 - 12\omega_4^3\omega_5^2cs^2 - 12\omega_4^3\omega_5\omega_2^3cs^2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 - 24\omega_4^3\omega_5^2\omega_2cs^2 - 12\omega_4\omega_5^2\omega_2^3cs^2 + 24\omega_4^3\omega_5^2v_1^2\omega_2^3 + 6\omega_4^3\omega_2^3cs^2 + 12\omega_4^3\omega_5\omega_2^3cs^2 + 36\omega_4^3\omega_5^2\omega_2cs^2 - 12\omega_4^3\omega_5^2cs^2 - 60\omega_4^3\omega_5^2v_1^2\omega_2^3 - 90\omega_4^3\omega_5^2v_1^2\omega_2 - 36\omega_4^3\omega_5\omega_2^2cs^2 - 12\omega_2^3\omega_5^2\omega_3^3cs^2 + 6\omega_4^3v_1^2\omega_2^3 + 12\omega_4^3\omega_5v_1^2\omega_2^3 - 12\omega_4^3\omega_5\omega_2cs^2 - 24\omega_4^3\omega_5v_1^2\omega_2^3 - 12\omega_4^3v_1^2\omega_2^3 - 32\omega_4^3\omega_5^2\omega_2^3cs^2 + 12\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2 + 36\omega_4^3\omega_5v_1^2\omega_2^3 + 48\omega_4^3\omega_5^2\omega_2cs^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2^3 + 4\omega_4^3\omega_5^2\omega_2^3cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^3) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT2}} = (40\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2\omega_2^3 + 48\omega_4^3\omega_5^2v_1^2\omega_2 + 36\omega_4^3cs^2\omega_5^2\omega_2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 + 48\omega_4^3cs^2\omega_5^2\omega_2^2 + 24\omega_4^3\omega_5^2v_1^2\omega_2^3 - 24\omega_2^3cs^2\omega_5^2\omega_2 - 32\omega_4^3cs^2\omega_5^2\omega_2^2 - 60\omega_4^3\omega_5^2v_1^2\omega_2^3 - 90\omega_4^3\omega_5^2v_1^2\omega_2 + 4\omega_4^3cs^2\omega_5^2\omega_2^3 + 6\omega_4^3v_1^2\omega_2^3 + 6\omega_4cs^2\omega_5^2\omega_2^3 + 12\omega_4^3\omega_5v_1^2\omega_2^3 - 12\omega_4^3cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5\omega_2^3 - 24\omega_4^3\omega_5v_1^2\omega_2^3 - 12\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_4^3v_1^2\omega_2^3 + 36\omega_4^3cs^2\omega_5\omega_2^3 - 12\omega_4^3cs^2\omega_2^3 + 12\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2 - 12\omega_4^3cs^2\omega_5\omega_2 + 36\omega_4^3\omega_5v_1^2\omega_2^3 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 24\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_4^3\omega_5v_1^2\omega_2^3 + 12\omega_4^3cs^2\omega_5\omega_2^3 + 24\omega_4\omega_5^2v_1^2\omega_2^3) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM1}} = (16\omega_4^3\omega_5^2v_1^2\omega_2^2 + 48\omega_4^3\omega_5^2\omega_2^2cs^2 + 4\omega_4^3\omega_5^2\omega_2^3cs^2 - 5\omega_4^3\omega_5^2v_1^2\omega_2^3 + 24\omega_4^3\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_5^2\omega_2^3cs^2 - 12\omega_4^3\omega_5\omega_2cs^2 - 36\omega_4^3\omega_5^2v_1^2\omega_2^2 - 6\omega_4^3\omega_5^2v_1^2\omega_2 - 32\omega_4^3\omega_5^2\omega_2cs^2 + 6\omega_4^3\omega_2^3cs^2 - 6\omega_4^3v_1^2\omega_2^3 - 12\omega_4\omega_5^2\omega_2^3cs^2 + 12\omega_4^3\omega_5\omega_2^3cs^2 - 12\omega_4^3\omega_5v_1^2\omega_2^3 + 24\omega_4^3\omega_5v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_2^3 + 12\omega_4^3\omega_5v_1^2\omega_2 + 36\omega_4^3\omega_5\omega_2^2cs^2 - 36\omega_4^3\omega_5v_1^2\omega_2^2 - 24\omega_4^3\omega_5\omega_2^3cs^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 - 12\omega_4^3\omega_2^3cs^2 + 6\omega_4\omega_5^2\omega_2^3cs^2 + 12\omega_4^3\omega_5v_1^2\omega_2^3 - 12\omega_4^3\omega_5\omega_2^3cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^3 - 24\omega_4^3\omega_5^2\omega_2cs^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM2}} = (16\omega_4^3\omega_5^2v_1^2\omega_2^2 - 12\omega_4^3\omega_5\omega_2^3cs^2 - 24\omega_4^3\omega_5^2\omega_2cs^2 - 5\omega_4^3\omega_2^3v_1^2\omega_2^3 - 24\omega_4^3\omega_5\omega_2^2cs^2 - 12\omega_4^3\omega_2^3cs^2 + 6\omega_4\omega_5^2\omega_2^3cs^2 + 24\omega_4^3\omega_2^3v_1^2\omega_2^3 + 36\omega_4^3\omega_5\omega_2^2cs^2 + 6\omega_4^3\omega_2^3cs^2 - 12\omega_4\omega_5^2\omega_2^3cs^2 + 12\omega_4^3\omega_5\omega_2^3cs^2 - 36\omega_4^3\omega_5^2v_1^2\omega_2^2 - 6\omega_4^3v_1^2\omega_2^3 - 12\omega_2^3\omega_5^2\omega_3^3cs^2 - 32\omega_4^3\omega_5^2\omega_2^3cs^2 + 24\omega_4^3\omega_5v_1^2\omega_2^3 - 12\omega_4^3\omega_5^2\omega_2^3cs^2 + 12\omega_4^3v_1^2\omega_2^3 - 12\omega_4^3\omega_5\omega_2cs^2 + 12\omega_5^2v_1^2\omega_2^3 + 12\omega_4^3\omega_5v_1^2\omega_2 + 4\omega_4^3\omega_5^2\omega_2^3cs^2 - 36\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_2^3 + 12\omega_4^3\omega_5v_1^2\omega_2^3 + 24\omega_4\omega_5^2v_1^2\omega_2^3 + 48\omega_4^3\omega_5^2\omega_2cs^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_2^3}$$

**coefficient**  $C_{D_x^2 D_y D_z v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3}$ :

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{SRT}} = (-56\omega^2cs^2 + 52\omega^2v_1^2 + 84v_1^2 + 4\omega^3cs^2 - 5\omega^3v_1^2 - 96cs^2 - 126\omega v_1^2 + 144\omega cs^2) \frac{v_2\rho}{12\omega^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT1}} = (36\omega_5v_1^2\omega_2^3\omega_3^3 + 36\omega_5^2\omega_2\omega_3^3cs^2 - 24\omega_5\omega_2^3\omega_3^3cs^2 - 12\omega_5^2\omega_2^3\omega_3^3cs^2 - 12\omega_2^3\omega_3^3cs^2 - 24\omega_5v_1^2\omega_2^3\omega_3^3 + 6v_1^2\omega_2^3\omega_3^3 + 36\omega_5\omega_2^3\omega_3^3cs^2 + 48\omega_5^2v_1^2\omega_2\omega_3^3 - 12\omega_5v_1^2\omega_2^3\omega_3^3 + 48\omega_5^2v_1^2\omega_3^3 - 24\omega_5^2\omega_2\omega_3^3cs^2 - 12v_1^2\omega_2^3\omega_3^3 - 12\omega_5^2\omega_2^3\omega_3cs^2 + 12\omega_5v_1^2\omega_2^3\omega_3^3 - 90\omega_5^2v_1^2\omega_2\omega_3^3 + 4\omega_5^2\omega_2^3\omega_3^3cs^2 + 6\omega_2^3\omega_3^3cs^2 + 48\omega_5^2\omega_2^3\omega_3^3cs^2 + 40\omega_5^2v_1^2\omega_2^3\omega_3^3 - 12\omega_5\omega_2\omega_3^3cs^2 - 30\omega_5^2v_1^2\omega_2^3\omega_3 - 60\omega_5^2v_1^2\omega_2^3\omega_3^3 + 12\omega_5^2v_1^2\omega_2^3 + 12\omega_5^2\omega_2^3\omega_3^3cs^2 - 12\omega_5^2\omega_3^3cs^2 - 5\omega_5^2v_1^2\omega_2^3\omega_3^3 + 6\omega_5^2\omega_2^3\omega_3cs^2 + 24\omega_5^2v_1^2\omega_2^3\omega_3 - 32\omega_5^2\omega_2^3\omega_3^3cs^2 - 12\omega_5v_1^2\omega_2\omega_3^3 - 12\omega_5\omega_2^3\omega_3^3cs^2 + 24\omega_5^2v_1^2\omega_2^3\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT2}} = (36\omega_5v_1^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_3^3 - 12cs^2\omega_5\omega_2\omega_3^3 + 6cs^2\omega_2^3\omega_3^3 + 48cs^2\omega_5^2\omega_2^3\omega_3^3 - 24\omega_5v_1^2\omega_2^3\omega_3^3 + 6v_1^2\omega_2^3\omega_3^3 - 32cs^2\omega_5^2\omega_2^3\omega_3^3 + 6cs^2\omega_5^2\omega_2^3\omega_3 - 12cs^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3^3 + 48\omega_5^2v_1^2\omega_2\omega_3^3 - 12\omega_5v_1^2\omega_2^3\omega_3^3 + 48\omega_5^2v_1^2\omega_3^3 + 4cs^2\omega_5^2\omega_2^3\omega_3^3 - 12cs^2\omega_5^2\omega_2^3\omega_3 - 12v_1^2\omega_2^3\omega_3^3 + 12\omega_5v_1^2\omega_2^3\omega_3^3 - 90\omega_5^2v_1^2\omega_2\omega_3^3 + 12cs^2\omega_5\omega_2\omega_3^3 - 30\omega_5^2v_1^2\omega_2^3\omega_3 - 12cs^2\omega_5\omega_2\omega_3^3 - 60\omega_5^2v_1^2\omega_2^3\omega_3^3 + 12\omega_5^2v_1^2\omega_2^3 - 5\omega_5^2v_1^2\omega_2^3\omega_3^3 + 24\omega_5^2v_1^2\omega_2^3\omega_3 - 24cs^2\omega_5\omega_2^3\omega_3^3 + 36cs^2\omega_5\omega_2\omega_3^3) \frac{v_2\rho}{12\omega_5^2\omega_2^3\omega_3^3}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM1}} = (-36\omega_5 v_1^2 \omega_2^2 \omega_3^3 - 12\omega_5^2 c s^2 \omega_3^3 + 6\omega_5^3 c s^2 \omega_3^3 - 12\omega_5^2 \omega_2^2 c s^2 \omega_3 - 12\omega_5 \omega_2 c s^2 \omega_3^3 + 24\omega_5 v_1^2 \omega_2^2 \omega_3^3 - 6v_1^2 \omega_3^3 \omega_3^3 - 12\omega_5 \omega_2^3 c s^2 \omega_3^3 + 48\omega_5^2 \omega_2^3 c s^2 \omega_3^3 + 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 + 12v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 + 12\omega_5 \omega_2^3 c s^2 \omega_3^3 - 32\omega_5^2 \omega_2^3 c s^2 \omega_3^3 - 6\omega_5^2 v_1^2 \omega_2 \omega_3^3 + 6\omega_5^2 \omega_2^3 c s^2 \omega_3 - 12\omega_2^3 c s^2 \omega_3^3 + 16\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 24\omega_5^2 \omega_2^3 c s^2 \omega_3^3 - 30\omega_5^2 v_1^2 \omega_2^3 \omega_3 + 36\omega_5^2 \omega_2 c s^2 \omega_3^3 - 36\omega_5^2 v_1^2 \omega_2^2 \omega_3^3 + 12\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 5\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 + 24\omega_5^2 v_1^2 \omega_2^3 \omega_3 + 4\omega_5^2 \omega_2^3 c s^2 \omega_3^3 - 24\omega_5^2 \omega_2^3 c s^2 \omega_3^3 - 12\omega_5^2 \omega_2^3 c s^2 \omega_3^3 + 36\omega_5 \omega_2^3 c s^2 \omega_3^3 + 12\omega_5 v_1^2 \omega_2 \omega_3^3 + 24\omega_5^2 v_1^2 \omega_2^3 \omega_3^3) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^3}$$

$$C_{D_x D_y D_z v_3}^{(0), \text{CLBM2}} = (-12\omega_5^2 \omega_2^3 \omega_3^3 c s^2 - 12\omega_2^3 \omega_3^3 c s^2 - 36\omega_5 v_1^2 \omega_2^2 \omega_3^3 + 36\omega_5^2 \omega_2 \omega_3^3 c s^2 - 24\omega_5 \omega_2^2 \omega_3^3 c s^2 + 24\omega_5 v_1^2 \omega_2^2 \omega_3^3 - 6v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5^2 \omega_2^3 \omega_3^3 c s^2 + 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 + 4\omega_5^2 \omega_2^3 \omega_3^3 c s^2 + 12v_1^2 \omega_2^3 \omega_3^3 + 36\omega_5 \omega_2^3 \omega_3^3 c s^2 - 12\omega_5 v_1^2 \omega_2^3 \omega_3^3 - 24\omega_5^2 \omega_2 \omega_3^3 c s^2 - 6\omega_5^2 v_1^2 \omega_2 \omega_3^3 - 12\omega_5^2 \omega_2^3 c s^2 + 12\omega_5 \omega_2^3 \omega_3^3 c s^2 + 16\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 30\omega_5^2 v_1^2 \omega_2^3 \omega_3 + 6\omega_5^3 \omega_3^3 c s^2 + 48\omega_5^2 \omega_2^3 \omega_3^3 c s^2 - 36\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5 \omega_2 \omega_3^3 c s^2 + 12\omega_5^2 v_1^2 \omega_2^3 - 5\omega_5^2 v_1^2 \omega_2^3 \omega_3^3 - 12\omega_5 \omega_2^3 \omega_3^3 c s^2 + 24\omega_5^2 v_1^2 \omega_2^3 \omega_3 + 12\omega_5 v_1^2 \omega_2 \omega_3^3 + 6\omega_5^2 \omega_2^3 \omega_3^3 c s^2 - 32\omega_5^2 \omega_2^3 \omega_3^3 c s^2 + 24\omega_5^2 v_1^2 \omega_2^3 \omega_3^3) \frac{v_2 \rho}{12\omega_5^2 \omega_2^3 \omega_3^3}$$

**coefficient**  $C_{D_t D_y^2 D_z v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial t \partial x_2^2 \partial x_3}$ :

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_2 \rho v_3}{6\omega^3}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{MRT1}} = (12\omega^2 \omega_6 \omega_3^2 - 7\omega_4^2 \omega_6 \omega_3^3 - 12\omega_4^2 \omega_6 \omega_3 + 3\omega_4^3 \omega_3^3 - 12\omega_4^3 \omega_6 + \omega_4^3 \omega_6 \omega_3^3 - 10\omega_4^3 \omega_6 \omega_3^2 - 6\omega_4^3 \omega_3^2 + 24\omega_4^3 \omega_6 \omega_3 - 6\omega_4 \omega_6 \omega_3^2 - 6\omega_4^2 \omega_3^3 - 6\omega_6 \omega_3^3 + 12\omega_4 \omega_6 \omega_3^3 + 12\omega_4^2 \omega_3^3) \frac{v_2 \rho v_3}{6\omega_4^3 \omega_6 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{MRT2}} = C_{D_t D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{CLBM1}} = (-6\omega_4 \omega_3^2 - 12\omega_4^3 + 12\omega_4 \omega_3^3 + \omega_4^3 \omega_3^3 - 6\omega_3^3 - 7\omega_4^2 \omega_3^3 - 7\omega_4^2 \omega_3^3 + 18\omega_4^3 \omega_3 + 6\omega_4^2 \omega_3^3) \frac{v_2 \rho v_3}{6\omega_4^3 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_2}^{(0), \text{CLBM2}} = C_{D_t D_y^2 D_z v_2}^{(0), \text{CLBM1}}$$

**coefficient**  $C_{D_t D_y^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t \partial x_2^2 \partial x_3}$ :

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{SRT}} = (34\omega^2 c s^2 - 2\omega^2 v_2^2 + \omega^3 v_2^2 - 2\omega^3 c s^2 + 60c s^2 - 90\omega c s^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{MRT1}} = (-6\omega_6 \omega_3^3 c s^2 + 9\omega_4 v_2^2 \omega_6 \omega_3^3 + 12\omega_4 \omega_6^2 c s^2 - 30\omega_4 \omega_6^2 \omega_3 c s^2 - 30\omega_4 v_2^2 \omega_6 \omega_3^3 - 24\omega_4 v_2^2 \omega_6^2 - 30\omega_4 \omega_6 \omega_3^2 c s^2 + 12v_2^2 \omega_6 \omega_3^2 + 12\omega_4 v_2^2 \omega_6 \omega_3 + 12\omega_6 \omega_3^2 c s^2 - 6\omega_4 v_2^2 \omega_3^3 + 9\omega_4 \omega_6 \omega_3^3 c s^2 - 6v_2^2 \omega_6 \omega_3^3 + 12\omega_4 v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 c s^2 - v_2^2 \omega_6^2 \omega_3^3 - 18\omega_6^2 \omega_3^3 c s^2 + 12\omega_4 \omega_3^2 c s^2 - 2\omega_4 \omega_6^2 \omega_3^3 c s^2 + 6v_2^2 \omega_6^2 \omega_3^3 + 36\omega_4 v_2^2 \omega_6^2 \omega_3 + 3\omega_6^2 \omega_3^3 c s^2 - 10\omega_4 v_2^2 \omega_6^2 \omega_3 + 12\omega_4 \omega_6 \omega_3 c s^2 - 12v_2^2 \omega_6^2 \omega_3 + \omega_4 v_2^2 \omega_6^2 \omega_3^3 - 6\omega_4 \omega_3^3 c s^2 + 22\omega_4 \omega_6^2 \omega_3^3 c s^2) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{MRT2}} = (-6\omega_4 c s^2 \omega_3^3 + 9\omega_4 v_2^2 \omega_6 \omega_3^3 - 30\omega_4 c s^2 \omega_6^2 \omega_3 - 18c s^2 \omega_6^2 \omega_3^3 - 30\omega_4 v_2^2 \omega_6 \omega_3^3 + 12\omega_4 c s^2 \omega_3^3 - 24\omega_4 v_2^2 \omega_6^2 + 3c s^2 \omega_6^2 \omega_3^3 + 12v_2^2 \omega_6 \omega_3^2 - 2\omega_4 c s^2 \omega_6^2 \omega_3^3 + 12\omega_4 v_2^2 \omega_6 \omega_3 - 6\omega_4 v_2^2 \omega_3^3 - 6v_2^2 \omega_6 \omega_3^3 + 12c s^2 \omega_6^2 \omega_3 + 12\omega_4 c s^2 \omega_6^2 + 12\omega_4 v_2^2 \omega_3^3 + 22\omega_4 c s^2 \omega_6^2 \omega_3^3 - v_2^2 \omega_6^2 \omega_3^3 - 30\omega_4 c s^2 \omega_6 \omega_3^3 + 6v_2^2 \omega_6^2 \omega_3^3 + 36\omega_4 v_2^2 \omega_6^2 \omega_3 + 9\omega_4 c s^2 \omega_6 \omega_3^3 - 10\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 12v_2^2 \omega_6^2 \omega_3 - 6c s^2 \omega_6 \omega_3^3 + 12\omega_4 c s^2 \omega_6 \omega_3 + \omega_4 v_2^2 \omega_6^2 \omega_3^3 + 12c s^2 \omega_6 \omega_3^3) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{CLBM1}} = (-30\omega_4 c s^2 \omega_6 \omega_3^2 - 9\omega_4 v_2^2 \omega_6 \omega_3^3 + 30\omega_4 v_2^2 \omega_6 \omega_3^2 + 24\omega_4 v_2^2 \omega_6^2 + 9\omega_4 c s^2 \omega_6 \omega_3^3 + 12\omega_4 c s^2 \omega_6^2 - 12v_2^2 \omega_6 \omega_3^2 - 6\omega_4 c s^2 \omega_3^3 - 6c s^2 \omega_6 \omega_3^3 - 12\omega_4 v_2^2 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_3^3 + 12c s^2 \omega_6 \omega_3^2 + 12\omega_4 c s^2 \omega_6^2 + 6v_2^2 \omega_6 \omega_3^3 + 12\omega_4 c s^2 \omega_6 \omega_3 - 12\omega_4 v_2^2 \omega_3^2 - 18c s^2 \omega_6^2 \omega_3^3 - v_2^2 \omega_6^2 \omega_3^3 - 30\omega_4 c s^2 \omega_6^2 \omega_3 - 6v_2^2 \omega_6^2 \omega_3^3 + 3c s^2 \omega_6^2 \omega_3^3 - 36\omega_4 v_2^2 \omega_6^2 \omega_3 + 8\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_4 c s^2 \omega_6^2 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3 + 22\omega_4 c s^2 \omega_6^2 \omega_3^3 + \omega_4 v_2^2 \omega_6^2 \omega_3^3 + 12c s^2 \omega_6^2 \omega_3) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^3}$$

$$C_{D_t D_y^2 D_z v_3}^{(0), \text{CLBM2}} = (-9\omega_4 v_2^2 \omega_6 \omega_3^3 - 30\omega_4 \omega_6 \omega_3^2 c s^2 + 30\omega_4 v_2^2 \omega_6 \omega_3^2 - 6\omega_6 \omega_3^3 c s^2 + 24\omega_4 v_2^2 \omega_6^2 + 12\omega_4 \omega_6^2 c s^2 - 30\omega_4 \omega_6^2 \omega_3 c s^2 - 12v_2^2 \omega_6 \omega_3^2 + 9\omega_4 \omega_6 \omega_3^3 c s^2 - 12\omega_4 v_2^2 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_3^3 + 12\omega_6^2 \omega_3 c s^2 + 6v_2^2 \omega_6 \omega_3^3 - 12\omega_4 v_2^2 \omega_3^2 + 12\omega_6 \omega_3^2 c s^2 - 2\omega_4 \omega_6^2 \omega_3^3 c s^2 + 12\omega_4 \omega_3^2 c s^2 - v_2^2 \omega_6^2 \omega_3^3 - 6v_2^2 \omega_6^2 \omega_3^2 - 36\omega_4 v_2^2 \omega_6 \omega_3 - 18\omega_6^2 \omega_3^2 c s^2 + 8\omega_4 v_2^2 \omega_6^2 \omega_3 + 12v_2^2 \omega_6^2 \omega_3 + 22\omega_4 \omega_6^2 \omega_3^2 c s^2 - 6\omega_4 \omega_3^3 c s^2 + 3\omega_6^2 \omega_3^3 c s^2 + \omega_4 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_4 \omega_6 \omega_3 c s^2) \frac{\rho}{12\omega_4 \omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_x D_y^2 D_z \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{D_x D_y^2 D_z \rho}^{(0), \text{SRT}} = (-12\omega^2 c s^2 + 24\omega^2 v_2^2 - 2\omega^3 v_2^2 + \omega^3 c s^2 - 20c s^2 + 40v_2^2 + 30\omega c s^2 - 60\omega v_2^2) \frac{v_1 v_3}{\omega^3}$$

$$C_{D_x D_y^2 D_z \rho}^{(0), \text{MRT1}} = (-6\omega_4^3 \omega_2^3 \omega_6^2 \omega_3^2 c s^2 + \omega_4^3 \omega_2^3 \omega_3^2 c s^2 - 2\omega_4^2 \omega_3^3 v_2^2 \omega_6 \omega_3^2 - 2\omega_4^2 \omega_3^3 \omega_6 \omega_3^2 c s^2 - 2\omega_4^3 \omega_3^3 v_2^2 \omega_6^2 \omega_3^3 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 7\omega_4^3 \omega_2^2 v_2^2 \omega_6^2 \omega_3 - 2\omega_4^3 \omega_2^3 v_2^2 \omega_6 \omega_3^2 c s^2 + \omega_2^3 \omega_3^2 v_2^2 \omega_6 \omega_3^3 - 2\omega_4^2 \omega_2^3 \omega_6^2 \omega_3^3 c s^2 + 3\omega_2^2 \omega_3^2 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_4^2 \omega_3^3 v_2^2 \omega_6^2 \omega_3^3 + 3\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 - 2\omega_4^2 \omega_3^3 \omega_6^2 \omega_3 c s^2 - 21\omega_4^2 \omega_3^3 v_2^2 \omega_6^2 \omega_3 + \omega_4^2 \omega_3^3 \omega_6 \omega_3^3 c s^2 - 12\omega_4^2 \omega_3^3 v_2^2 \omega_6^2 \omega_3 + \omega_4^2 \omega_3^3 \omega_6^2 \omega_3^3 c s^2 - 2\omega_3^3 \omega_2^3 \omega_3^2 c s^2 + 6\omega_3^3 \omega_2^2 \omega_6^2 \omega_3^3 c s^2 + 7\omega_4^2 \omega_3^3 v_2^2 \omega_6^2 \omega_3^3 - 2\omega_4^2 \omega_3^3 \omega_6^2 \omega_3^3 c s^2 - 2\omega_4^2 \omega_3^3 \omega_6^2 \omega_3 c s^2 - 2\omega_4^3 \omega_3^3 v_2^2 \omega_6^2 + 4\omega_4^2 \omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 3\omega_4^2 \omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 7\omega_4^2 \omega_2^3 v_2^2 \omega_6^2 \omega_3 - 2\omega_3^3 \omega_2^3 \omega_6 \omega_3^3 c s^2 + \omega_4^2 \omega_2^3 v_2^2 \omega_6 \omega_3^3 - 8\omega_4^2 \omega_2^3 v_2^2 \omega_6^2 \omega_3^3 - 2\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 + \omega_4^3 \omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + \omega_4^2 \omega_2 \omega_6^2 \omega_3^3 c s^2 - 2\omega_4^2 \omega_2^3 v_2^2 \omega_6 \omega_3 - 2\omega_4^2 \omega_2^3 v_2^2 \omega_6 \omega_3^2 + \omega_4 \omega_2^3 \omega_6^2 \omega_3^3 c s^2 - 2\omega_4^2 \omega_2^2 \omega_6^2 \omega_3^2 c s^2 + 7\omega_4^2 \omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_4^2 \omega_2^3 \omega_6 \omega_3^2 c s^2 +$$

$$4\omega_3^2\omega_2v_2^2\omega_6^2\omega_3^2 + 10\omega_4^3\omega_3^2v_2^2\omega_6^2 + 4\omega_4\omega_3^2v_2^2\omega_6^2\omega_3^2 + 6\omega_2^2\omega_3^2\omega_6^2\omega_3^2cs^2 + 6\omega_3^3\omega_2^2v_2^2\omega_6\omega_3^2 - 12\omega_4^2\omega_3^2v_2^2\omega_6^2\omega_3^2 - 8\omega_3^2\omega_2v_2^2\omega_6\omega_3^2 + 6\omega_4^3\omega_3^2\omega_6\omega_3cs^2 - 2\omega_4^3\omega_2^2\omega_6^2cs^2 - 2\omega_4\omega_2^2\omega_6^2\omega_3^2cs^2 + \omega_4^2\omega_2^2\omega_6^2\omega_3^3cs^2 - 2\omega_4^3\omega_2^2v_2^2\omega_6\omega_3^3 - 2\omega_4^3\omega_2\omega_6^2\omega_3^2cs^2 + \omega_4^2\omega_2^2\omega_6\omega_3^3cs^2 - 8\omega_4\omega_2^2v_2^2\omega_6^2\omega_3^3 - \frac{\omega_4^2v_1v_3}{\omega_3^4\omega_2^2\omega_6^2\omega_3^3}$$

$$C_{-}(0, \text{CLBML})_{D_2 D_2 D_2 \rho} = (2\omega_1^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2\omega_4 \omega_2^2 c s^2 \omega_6^2 \omega_3 + \omega_1^2 \omega_2^2 c s^2 \omega_6 \omega_3^2 - 2\omega_3^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 6\omega_4 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 3\omega_3^2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_1^2 \omega_2^2 c s^2 \omega_6 \omega_3^2 + 3\omega_3^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3 - \omega_1^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 + \omega_1^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 3\omega_4^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 + 8\omega_4^2 \omega_3^2 v_2^2 \omega_6^2 \omega_3 + 3\omega_3^2 v_2^2 \omega_6^2 \omega_3^2 - 7\omega_4^2 \omega_3^2 v_2^2 \omega_6^2 \omega_3 - 10\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_1^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 6\omega_4^2 \omega_3^2 c s^2 \omega_6^2 \omega_3 + 6\omega_4^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 7\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + \omega_4^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 2\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_1^2 \omega_2^2 c s^2 \omega_6 \omega_3 + 4\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 3\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_1^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 - 2\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_1^2 \omega_2^2 c s^2 \omega_6 \omega_3 + \omega_1^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 4\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - \omega_1^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3 + 2\omega_1^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 + 2\omega_1^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 2\omega_1^2 \omega_2^2 c s^2 \omega_6 \omega_3^2 + 2\omega_1^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 + 4\omega_4^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 + 2\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3 + 4\omega_4^2 \omega_3^2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_1^2 \omega_2^2 c s^2 \omega_6 \omega_3^2 + \omega_4^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 - 6\omega_4^2 \omega_3^2 v_2^2 \omega_6^2 \omega_3^2 - 10\omega_4^2 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2 - 8\omega_4^2 \omega_2 v_2^2 \omega_6^2 \omega_3^2 - 2\omega_4^2 \omega_2 c s^2 \omega_6^2 \omega_3^2 - 2\omega_4^2 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 2\omega_4^2 \omega_2^2 v_2^2 \omega_6 \omega_3^2 - 2\omega_4 \omega_2^2 c s^2 \omega_6^2 \omega_3^2 + 6\omega_4^2 \omega_2^2 c s^2 \omega_6 \omega_3^2 - 8\omega_4 \omega_2^2 v_2^2 \omega_6^2 \omega_3^2) \frac{v_1 v_3}{\omega_4^2 \omega_6^2 \omega_3^2}$$

coefficient  $C_{D_x D_y^2 D_z v_1}^{(0)}$  at  $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{D_x D_y D_z v_1}^{(0), \text{MRT1}} = (-32\omega_3^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_4^2 v_2^2 \omega_3^2 - 5\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_3^2 \omega_6 \omega_3 cs^2 + 6\omega_4^2 v_2^2 \omega_3^2 + 48\omega_3^2 v_2^2 \omega_6^2 \omega_3 + 40\omega_3^2 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^2 \omega_6 \omega_3^3 cs^2 - 90\omega_3^2 v_2^2 \omega_3^2 + 4\omega_3^2 \omega_6^2 \omega_3^2 cs^2 + 48\omega_4^2 v_2^2 \omega_6^2 - 60\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 48\omega_4^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_3^2 \omega_6^2 cs^2 + 24\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_3^2 \omega_3^2 cs^2 - 24\omega_4^2 \omega_6^2 \omega_3 cs^2 + 12\omega_3^2 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_3^2 \omega_6 \omega_3^3 cs^2 + 6\omega_4 \omega_6^2 \omega_3^3 cs^2 - 12\omega_3^2 v_2^2 \omega_6 \omega_3 - 24\omega_4^2 \omega_6 \omega_3^2 cs^2 - 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 36\omega_3^2 \omega_6 \omega_3^2 cs^2 + 24\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^2 \omega_3^2 cs^2 - 30\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^2 \omega_6^2 \omega_3 cs^2 + 12\omega_4^2 \omega_6 \omega_3^3 cs^2 - 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_4 \omega_6^2 \omega_3^2 cs^2) \frac{\rho v_3}{12\omega_3^2 \omega_6^2 \omega_3^2}$$

$$C_{D_x D_y D_z v_1}^{(0), \text{CLB M1}} = (-24\omega^2 c s^2 \omega_6^2 \omega_3 + 12\omega_4^2 v_2^2 \omega_3^2 - 32\omega_4^3 c s^2 \omega_6^2 \omega_3^2 - 5\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_3^2 + 6\omega_4^3 c s^2 \omega_3^2 + 16\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 4\omega_4^3 c s^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12\omega_4^3 c s^2 \omega_6^2 - 12\omega_4^2 c s^2 \omega_6^2 \omega_3^2 - 36\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 c s^2 \omega_6^2 \omega_3 + 24\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 48\omega_4^2 c s^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 c s^2 \omega_6 \omega_3 + 12\omega_4^2 \omega_3^2 \omega_6^2 - 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 24\omega_4^2 c s^2 \omega_6 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_6 \omega_3 + 12\omega_4^2 c s^2 \omega_6 \omega_3^2 + 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 24\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4 c s^2 \omega_6^2 \omega_3 - 36\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^2 c s^2 \omega_6 \omega_3^2 - 12\omega_4 c s^2 \omega_6^2 \omega_3 - 30\omega_4 v_2^2 \omega_6^2 \omega_3 + 36\omega_4^2 c s^2 \omega_6 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^2) \frac{\rho v_3}{12\omega_4^2 \omega_6^2 \omega_3^2}$$

coefficient  $C_{D_x D_y^2 D_z v_2}^{(0)}$  at  $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3}$ :

$$C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT1}} = (6\omega_4 \omega_2^3 \omega_3^2 + 24\omega_4^3 \omega_2^2 \omega_3^3 - 36\omega_4^3 \omega_2^3 \omega_3 + 12\omega_2^3 \omega_3^3 - 30\omega_4^3 \omega_2^2 \omega_3^2 - 30\omega_4 \omega_2^3 \omega_3^3 - 5\omega_4^3 \omega_2^3 \omega_3^3 + 18\omega_4^3 \omega_2^2 \omega_3 + 18\omega_2^2 \omega_2 \omega_3^3 + 12\omega_4^3 \omega_2^3 + 18\omega_4 \omega_2^2 \omega_3^3 + 28\omega_4^3 \omega_2^2 \omega_3^3 + 12\omega_4^3 \omega_3^3 + 12\omega_4^2 \omega_2^2 \omega_3^3 + 18\omega_4^2 \omega_2^3 \omega_3 - 42\omega_4^2 \omega_2^2 \omega_3^3 + 6\omega_4^3 \omega_2 \omega_3^2 - 30\omega_4^2 \omega_2^3 \omega_3^2 + 24\omega_4^2 \omega_2^3 \omega_3^3 - 30\omega_4^3 \omega_2 \omega_3^3) \frac{v_1 v_2 \rho v_3}{6\omega_4^3 \omega_2^3 \omega_3^3}$$

$$C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT2}} = C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_2}^{(0), \text{CLBM1}} = C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_2}^{(0), \text{CLBM2}} = C_{D_x D_y^2 D_z v_2}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_x D_y^2 D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3}$  :

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{SRT}} = (-56\omega^2 cs^2 + 52\omega^2 v_2^2 - 5\omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 + 84v_2^2 + 144\omega cs^2 - 126\omega v_2^2) \frac{v_1 \rho}{12\omega^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}} = (-12\omega_2^3 \omega_6 \omega_3 cs^2 + 48\omega_2^3 v_2^2 \omega_6^2 \omega_3 + 40\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 \omega_6^2 \omega_3^3 cs^2 - 12\omega_2^3 v_2^2 \omega_3^3 - 32\omega_2^3 \omega_6^2 \omega_3^3 cs^2 + 6\omega_2^3 v_2^2 \omega_3^3 - 5\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 48\omega_2^3 \omega_6^2 \omega_3^3 cs^2 + 48\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 - 90\omega_2^3 v_2^2 \omega_6^2 \omega_3 + 4\omega_2^3 \omega_6^2 \omega_3^3 cs^2 - 60\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 \omega_6^2 cs^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3 + 6\omega_2 \omega_6^2 \omega_3^3 cs^2 - 24\omega_2^3 \omega_6 \omega_3^3 cs^2 + 12v_2^2 \omega_6^2 \omega_3^3 + 6\omega_2^3 \omega_3^3 cs^2 - 24\omega_2^3 v_2^2 \omega_6 \omega_3 - 24\omega_2^3 \omega_6^2 \omega_3 cs^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_2^3 \omega_6 \omega_3^3 cs^2 - 30\omega_2 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 \omega_3^3 cs^2 + 36\omega_2^3 \omega_6 \omega_3 cs^2 + 12\omega_2^3 \omega_6 \omega_3^3 cs^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_2 \omega_6^2 \omega_3^3 cs^2 + 24\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^3 \omega_6 \omega_3^3 cs^2 + 36\omega_2^3 v_2^2 \omega_6 \omega_3^2) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT2}} = (48\omega_2^3 v_2^2 \omega_6^2 \omega_3 + 40\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 24cs^2 \omega_2^3 \omega_6 \omega_3^2 + 6cs^2 \omega_2 \omega_6^2 \omega_3^3 + 6cs^2 \omega_2^3 \omega_3^3 - 12\omega_2^3 v_2^2 \omega_3^3 + 36cs^2 \omega_2^3 \omega_6^2 \omega_3 + 6\omega_2^3 v_2^2 \omega_3^3 - 12cs^2 \omega_2^3 \omega_3^3 - 12cs^2 \omega_2 \omega_6^2 \omega_3^2 - 5\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 12cs^2 \omega_2^3 \omega_6 \omega_3^3 - 32cs^2 \omega_2^3 \omega_6^2 \omega_3^2 + 48\omega_2^3 v_2^2 \omega_6^2 + 24\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 - 90\omega_2^3 v_2^2 \omega_6^2 \omega_3 - 12cs^2 \omega_2^3 \omega_6^2 + 4cs^2 \omega_2^3 \omega_6^2 \omega_3^3 - 60\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3 - 24cs^2 \omega_2^3 \omega_6^2 \omega_3 - 12cs^2 \omega_2^3 \omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3^3 - 24\omega_2^3 v_2^2 \omega_6 \omega_3^2 + 36cs^2 \omega_2^3 \omega_6 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 - 30\omega_2 v_2^2 \omega_6^2 \omega_3^3 - 12cs^2 \omega_2^3 \omega_6 \omega_3 - 12cs^2 \omega_2^3 \omega_6^2 \omega_3^3 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 + 24\omega_2 v_2^2 \omega_6^2 \omega_3^2 + 48cs^2 \omega_2^3 \omega_6^2 \omega_3^3 + 36\omega_2^3 v_2^2 \omega_6 \omega_3^2) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM1}} = (-12\omega_2^3 cs^2 \omega_3^2 + 16\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 4\omega_2^3 cs^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 v_2^2 \omega_3^3 + 6\omega_2^3 cs^2 \omega_3^3 - 24\omega_2^3 cs^2 \omega_6^2 \omega_3 - 6\omega_2^3 v_2^2 \omega_3^3 - 32\omega_2^3 cs^2 \omega_6^2 \omega_3^2 - 5\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^3 cs^2 \omega_6^2 \omega_3 + 24\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 cs^2 \omega_6^2 + 48\omega_2^3 cs^2 \omega_6^2 \omega_3^2 - 6\omega_2^3 v_2^2 \omega_6^2 \omega_3 - 12\omega_2^3 cs^2 \omega_6^2 \omega_3^3 - 36\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3 + 12v_2^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 cs^2 \omega_6 \omega_3^3 + 24\omega_2^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_2^3 cs^2 \omega_6 \omega_3 - 12\omega_2^3 cs^2 \omega_6^2 \omega_3^3 - 24\omega_2^3 cs^2 \omega_6 \omega_3^2 - 12\omega_2^3 cs^2 \omega_6^2 \omega_3^2 - 30\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_2^3 cs^2 \omega_6 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 + 24\omega_2 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_2 cs^2 \omega_6^2 \omega_3^3 - 36\omega_2^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_2^3 cs^2 \omega_6 \omega_3^3) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM2}} = (-32\omega_2^3 \omega_6^2 \omega_3^3 cs^2 + 16\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_3^3 - 12\omega_2^3 \omega_6 \omega_3 cs^2 - 6\omega_2^3 v_2^2 \omega_3^3 - 12\omega_2^3 \omega_6^2 \omega_3^3 cs^2 - 5\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 24\omega_2^3 v_2^2 \omega_6^2 \omega_3^3 + 4\omega_2^3 \omega_6^2 \omega_3^3 cs^2 - 12\omega_2^3 \omega_6^2 cs^2 + 48\omega_2^3 \omega_6^2 \omega_3^2 cs^2 - 6\omega_2^3 v_2^2 \omega_6^2 \omega_3 - 36\omega_2^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_2^3 v_2^2 \omega_6 \omega_3 - 24\omega_2^3 \omega_6^2 \omega_3 cs^2 + 12v_2^2 \omega_6^2 \omega_3^3 - 12\omega_2^3 \omega_6 \omega_3^3 cs^2 + 24\omega_2^3 v_2^2 \omega_6 \omega_3^2 + 6\omega_2 \omega_6^2 \omega_3^3 cs^2 - 24\omega_2^3 \omega_6 \omega_3^3 cs^2 + 6\omega_2^3 \omega_3^3 cs^2 - 12\omega_2^3 v_2^2 \omega_6 \omega_3^2 + 36\omega_2^3 \omega_6 \omega_3^2 cs^2 - 30\omega_2 v_2^2 \omega_6^2 \omega_3^3 + 12\omega_2^3 v_2^2 \omega_6 \omega_3^3 + 24\omega_2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_2^3 \omega_6 \omega_3 cs^2 - 12\omega_2^3 \omega_3^3 cs^2 - 36\omega_2^3 v_2^2 \omega_6 \omega_3^2 + 12\omega_2^3 \omega_6 \omega_3^3 cs^2 - 12\omega_2 \omega_6^2 \omega_3^3 cs^2) \frac{v_1 \rho}{12\omega_2^3 \omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_y^3 D_z \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_2^3 \partial x_3}$  :

$$C_{D_y^3 D_z \rho}^{(0), \text{SRT}} = (24 - 72\omega^2 cs^2 + 6\omega^3 cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_2 v_3}{6\omega^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT1}} = (6\omega_4^2 \omega_6 \omega_3^2 - 48\omega_4^3 \omega_6^2 \omega_3^2 cs^2 - 12\omega_4^3 v_2^2 \omega_3^2 - 24\omega_4^3 \omega_6 \omega_3 cs^2 + 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^3 \omega_6^2 \omega_3 - 3\omega_4^2 \omega_6 \omega_3^3 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3 + 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 \omega_6^2 \omega_3^3 cs^2 - 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 6\omega_4^3 \omega_6^2 \omega_3^3 cs^2 + 24\omega_4^3 v_2^2 \omega_6^2 + 7\omega_4^3 \omega_6^2 \omega_3^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 42\omega_4^2 \omega_6^2 \omega_3^3 cs^2 - 36\omega_4^3 \omega_6^2 cs^2 + 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^3 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4^3 \omega_3^3 cs^2 - 24\omega_4^2 \omega_6^2 \omega_3^3 cs^2 + 6v_2^2 \omega_6^2 \omega_3^3 - 3\omega_4^3 \omega_3^3 + 6\omega_4^2 v_2^2 \omega_6 \omega_3^3 - 12\omega_4^3 \omega_6 \omega_3^3 cs^2 + 6\omega_4^3 \omega_6 \omega_3^3 + 6\omega_4^2 \omega_6 \omega_3^3 cs^2 - 24\omega_4^3 v_2^2 \omega_6 \omega_3^2 + 12\omega_4^3 \omega_6 \omega_3^2 cs^2 - 21\omega_4^3 \omega_6 \omega_3^2 - 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 6\omega_4^3 \omega_3^2 + 12\omega_4^3 \omega_6 \omega_3 + 42\omega_4^3 \omega_6 \omega_3^2 cs^2 + 6\omega_4 v_2^2 \omega_6^2 \omega_3^2 + \omega_4^2 \omega_6^2 \omega_3^3 + 42\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^3 \omega_3^2 cs^2 - 3\omega_4^2 \omega_6^2 \omega_3^2 - 12\omega_4 v_2^2 \omega_6^2 \omega_3^3 + 78\omega_4^3 \omega_6^2 \omega_3^2 cs^2 + 6\omega_4^2 \omega_6 \omega_3^3 cs^2 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_4 \omega_6^2 \omega_3^3 cs^2) \frac{v_2 v_3}{6\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT2}} = (-12\omega_4^2 cs^2 \omega_6 \omega_3^2 + 6\omega_4^2 \omega_6 \omega_3^2 - 36\omega_4^3 cs^2 \omega_6^2 - 12\omega_4^3 v_2^2 \omega_3^2 - 24\omega_4^3 cs^2 \omega_6 \omega_3 + 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^3 \omega_6^2 \omega_3 - 3\omega_4^2 \omega_6 \omega_3^3 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3 + 6\omega_4^3 cs^2 \omega_6 \omega_3^3 + 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 - 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12\omega_4^3 cs^2 \omega_6 \omega_3^3 + 6\omega_4^2 cs^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 cs^2 \omega_6^2 \omega_3^2 + 24\omega_4^3 v_2^2 \omega_6^2 + 7\omega_4^3 \omega_6^2 \omega_3^2 - 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 42\omega_4^3 cs^2 \omega_6 \omega_3^3 + 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^3 - \omega_4^3 \omega_6^2 \omega_3^3 - 12\omega_4^2 cs^2 \omega_6^2 \omega_3^2 + 6\omega_4^3 cs^2 \omega_6^2 \omega_3^2 - 48\omega_4^3 cs^2 \omega_6^2 \omega_3^2 + 6v_2^2 \omega_6^2 \omega_3^3 - 3\omega_4^3 \omega_3^3 + 6\omega_4^2 v_2^2 \omega_6 \omega_3^3 - 24\omega_4^2 cs^2 \omega_6^2 \omega_3 + 6\omega_4^3 \omega_6 \omega_3^3 + 6\omega_4^3 cs^2 \omega_6^2 \omega_3^2 - 24\omega_4^3 v_2^2 \omega_6 \omega_3 - 21\omega_4^3 \omega_6 \omega_3^2 - 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 6\omega_4^3 \omega_3^2 + 12\omega_4^3 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_6^2 \omega_3^2 - 12\omega_4^2 cs^2 \omega_6^2 \omega_3^2 + \omega_4^2 \omega_6^2 \omega_3^3 + 42\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 3\omega_4^2 \omega_6^2 \omega_3^2 + 42\omega_4^2 cs^2 \omega_6^2 \omega_3^2 - 12\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^3 + 78\omega_4^3 cs^2 \omega_6^2 \omega_3^2) \frac{v_2 v_3}{6\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM1}} = (6\omega_4^2 \omega_6 \omega_3^2 - 12\omega_4^2 cs^2 \omega_6^2 \omega_3 + 12\omega_4^3 v_2^2 \omega_3^2 - 36\omega_4^3 cs^2 \omega_6^2 \omega_3^2 - 36\omega_4^3 cs^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^3 \omega_6^2 \omega_3 - 3\omega_4^2 \omega_6 \omega_3^3 + 18\omega_4^3 cs^2 \omega_3^3 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_4^3 cs^2 \omega_6^2 \omega_3^3 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12\omega_4^3 cs^2 \omega_6^2 - 12\omega_4^2 cs^2 \omega_6^2 \omega_3^3 + 7\omega_4^3 \omega_6^2 \omega_3^2 - 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 cs^2 \omega_6^2 \omega_3 + 6\omega_4^2 v_2^2 \omega_6^2 \omega_3^3 - \omega_4^3 \omega_6^2 \omega_3^3 + 36\omega_4^2 cs^2 \omega_6^2 \omega_3^2 - 24\omega_4^3 cs^2 \omega_6 \omega_3 + 6v_2^2 \omega_6^2 \omega_3^3 - 3\omega_4^3 \omega_3^3 - 24\omega_4^2 cs^2 \omega_6 \omega_3^2 + 6\omega_4^3 \omega_6 \omega_3^3 - 24\omega_4^3 v_2^2 \omega_6 \omega_3 - 21\omega_4^3 \omega_6 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 6\omega_4^3 \omega_3^2 + 12\omega_4^3 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4^2 cs^2 \omega_6^2 \omega_3^2 - 12\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^3 + 72\omega_4^3 cs^2 \omega_6 \omega_3^2) \frac{v_2 v_3}{6\omega_4^3 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM2}} = (6\omega_4^2 \omega_6 \omega_3^2 - 24\omega_4^3 \omega_6 \omega_3 cs^2 + 12\omega_4^3 v_2^2 \omega_3^2 - 12\omega_4^2 \omega_6^2 \omega_3^3 cs^2 - 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^3 \omega_6^2 \omega_3 - 3\omega_4^2 \omega_6 \omega_3^3 - 36\omega_4^3 \omega_6^2 \omega_3^2 cs^2 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 12\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 36\omega_4^2 \omega_6^2 \omega_3^3 cs^2 - 12\omega_4^3 \omega_6^2 cs^2 + 7\omega_4^3 \omega_6^2 \omega_3^3 - 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 6\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_4^3 \omega_6^2 \omega_3^3 cs^2 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4 \omega_6^2 \omega_3^3 cs^2 + 6v_2^2 \omega_6^2 \omega_3^3 - 24\omega_4^2 \omega_6 \omega_3^3 cs^2 - 3\omega_4^3 \omega_3^3 + 6\omega_4^3 \omega_6 \omega_3^3 - 12\omega_4^2 \omega_6^2 \omega_3 cs^2 + 18\omega_4^3 \omega_3^3 cs^2 - 24\omega_4^3 v_2^2 \omega_6 \omega_3 - 21\omega_4^3 \omega_6 \omega_3^2 - 24\omega_4^3 \omega_6 \omega_3^3 cs^2 + 6\omega_4^3 \omega_3^3 + 12\omega_4^3 \omega_6 \omega_3 + 6\omega_4 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^2 \omega_6^2 \omega_3 cs^2 + \omega_4^3 \omega_6^2 \omega_3^3 + 12\omega_4^2 \omega_6 \omega_3^3 cs^2 + 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_4 \omega_6^2 \omega_3^3 cs^2 - 3\omega_4^2 \omega_6^2 \omega_3^2 + 72\omega_4^3 \omega_6 \omega_3^3 cs^2 - 12\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 36\omega_4^3 \omega_3^3 cs^2) \frac{v_2^2 \omega_3^3}{6\omega_4^2 \omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_y^3 D_z v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_3^2 \partial x_3}$  :

$$C_{D_y^3 D_z v_2}^{(0), \text{SRT}} = (12 - 56\omega^2 cs^2 - 12\omega^2 v_2^2 + 3\omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 - 18\omega - 12v_2^2 - \omega^3 + 8\omega^2 + 144\omega cs^2 + 18\omega v_2^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT1}} = (12\omega_4^2 \omega_6 \omega_3^2 - 32\omega_4^3 \omega_6^2 \omega_3^3 cs^2 - 12\omega_4^3 v_2^2 \omega_3^2 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 \omega_6 \omega_3 cs^2 + 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^2 \omega_6 \omega_3^3 - 12\omega_4^2 \omega_6^2 \omega_3^3 cs^2 - 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 4\omega_4^3 \omega_6^2 \omega_3^3 cs^2 + 24\omega_4^3 v_2^2 \omega_6^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 48\omega_4^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_4^3 \omega_6^2 cs^2 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4^3 \omega_3^3 cs^2 - 24\omega_4^2 \omega_6^2 \omega_3 cs^2 + 12v_2^2 \omega_6^2 \omega_3^3 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^3 - 12\omega_4^3 \omega_6 \omega_3^3 cs^2 + 3\omega_4^3 \omega_6 \omega_3^3 + 6\omega_4 \omega_6^2 \omega_3^3 cs^2 - 12\omega_4^3 v_2^2 \omega_6 \omega_3 - 24\omega_4^2 \omega_6 \omega_3^3 cs^2 - 6\omega_4^3 \omega_6 \omega_3^2 - 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 36\omega_4^3 \omega_6 \omega_3^3 cs^2 + 2\omega_4^2 \omega_6^2 \omega_3^3 + 36\omega_4^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_4^3 \omega_3^3 cs^2 - 6\omega_4^2 \omega_6^2 \omega_3^3 - 18\omega_4 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_4^3 \omega_6^2 \omega_3 cs^2 + 12\omega_4^2 \omega_6 \omega_3^3 cs^2 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^3 - 12\omega_4 \omega_6^2 \omega_3^3 cs^2) \frac{\rho v_3}{12\omega_4^2 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT2}} = (-24\omega_4^2 cs^2 \omega_6 \omega_3^2 + 12\omega_4^2 \omega_6 \omega_3^2 - 12\omega_4^3 cs^2 \omega_6^2 - 12\omega_4^3 v_2^2 \omega_3^2 - 12\omega_4^3 cs^2 \omega_6 \omega_3 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 + 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^2 \omega_6 \omega_3^3 + 12\omega_4^2 cs^2 \omega_6 \omega_3^3 - 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12\omega_4^3 cs^2 \omega_6 \omega_3^3 + 6\omega_4 cs^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 cs^2 \omega_3^2 + 24\omega_4^3 v_2^2 \omega_6^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 cs^2 \omega_6 \omega_3^3 - \omega_4^3 \omega_6^2 \omega_3^3 - 12\omega_4 cs^2 \omega_6^2 \omega_3^2 + 6\omega_4^3 cs^2 \omega_3^2 - 32\omega_4^3 cs^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 \omega_3^3 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^3 - 24\omega_4^2 cs^2 \omega_6^2 \omega_3 + 3\omega_4^3 \omega_6 \omega_3^3 + 4\omega_4^3 cs^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 v_2^2 \omega_6 \omega_3 - 6\omega_4^3 \omega_6 \omega_3^2 - 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^3 cs^2 \omega_6^2 \omega_3^3 + 2\omega_4^2 \omega_6^2 \omega_3^3 + 36\omega_4^3 v_2^2 \omega_6 \omega_3^3 - 6\omega_4^2 \omega_6^2 \omega_3^3 + 48\omega_4^2 cs^2 \omega_6^2 \omega_3^2 - 18\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^3 + 36\omega_4^3 cs^2 \omega_6^2 \omega_3^3) \frac{\rho v_3}{12\omega_4^2 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM1}} = (12\omega_4^2 \omega_6 \omega_3^2 - 24\omega_4^2 cs^2 \omega_6^2 \omega_3 + 12\omega_4^3 v_2^2 \omega_3^2 - 32\omega_4^3 cs^2 \omega_6^2 \omega_3 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 cs^2 \omega_3^2 - 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^2 \omega_6 \omega_3^3 + 6\omega_4^3 cs^2 \omega_3^3 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 4\omega_4^3 cs^2 \omega_6^2 \omega_3^3 + 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 - 12\omega_4^3 cs^2 \omega_6^2 - 12\omega_4^2 cs^2 \omega_6^2 \omega_3^3 - 24\omega_4^3 v_2^2 \omega_6^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 cs^2 \omega_6^2 \omega_3 - \omega_4^3 \omega_6^2 \omega_3^3 + 48\omega_4^2 cs^2 \omega_6^2 \omega_3^2 - 12\omega_4^3 cs^2 \omega_6 \omega_3 + 12v_2^2 \omega_6^2 \omega_3^3 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^3 - 24\omega_4^2 cs^2 \omega_6^2 \omega_3 + 3\omega_4^3 \omega_6 \omega_3^3 + 12\omega_4^3 v_2^2 \omega_6 \omega_3 - 6\omega_4^3 \omega_6 \omega_3^2 + 12\omega_4^2 cs^2 \omega_6 \omega_3^3 - 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 + 6\omega_4 cs^2 \omega_6^2 \omega_3^3 + 2\omega_4^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^3 cs^2 \omega_6 \omega_3^3 - 6\omega_4^2 \omega_6^2 \omega_3^2 - 12\omega_4 cs^2 \omega_6^2 \omega_3^3 - 18\omega_4 v_2^2 \omega_6^2 \omega_3^3 + 36\omega_4^3 cs^2 \omega_6 \omega_3^3) \frac{\rho v_3}{12\omega_4^2 \omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM2}} = (12\omega_4^2 \omega_6 \omega_3^2 - 12\omega_4^3 \omega_6 \omega_3 cs^2 + 12\omega_4^3 v_2^2 \omega_3^2 - 12\omega_4^2 \omega_6^2 \omega_3^3 cs^2 + 3\omega_4^3 v_2^2 \omega_6^2 \omega_3^3 - 6\omega_4^3 v_2^2 \omega_3^3 - 6\omega_4^2 \omega_6 \omega_3^3 - 32\omega_4^3 \omega_6^2 \omega_3^2 cs^2 - 12\omega_4^3 v_2^2 \omega_6^2 \omega_3^2 + 30\omega_4^3 v_2^2 \omega_6^2 \omega_3 + 48\omega_4^2 \omega_6^2 \omega_3^2 cs^2 - 12\omega_4^3 \omega_6^2 cs^2 - 24\omega_4^3 v_2^2 \omega_6^2 + 3\omega_4^3 \omega_6^2 \omega_3^2 + 12\omega_4^2 v_2^2 \omega_6^2 \omega_3^2 + 4\omega_4^3 \omega_6^2 \omega_3^3 cs^2 - \omega_4^3 \omega_6^2 \omega_3^3 + 6\omega_4 \omega_6^2 \omega_3^3 cs^2 + 12v_2^2 \omega_6^2 \omega_3^3 - 24\omega_4^2 \omega_6 \omega_3^3 cs^2 + 12\omega_4^2 v_2^2 \omega_6 \omega_3^3 + 3\omega_4^3 \omega_6 \omega_3^3 - 24\omega_4^2 \omega_6^2 \omega_3 cs^2 + 6\omega_4^3 \omega_3^3 cs^2 + 12\omega_4^3 v_2^2 \omega_6 \omega_3 - 6\omega_4^3 \omega_6 \omega_3^2 - 24\omega_4^2 v_2^2 \omega_6 \omega_3^2 - 12\omega_4^3 \omega_6 \omega_3^3 cs^2 + 2\omega_4^2 \omega_6^2 \omega_3^3 + 12\omega_4^2 \omega_6 \omega_3^3 cs^2 - 12\omega_4^3 v_2^2 \omega_6 \omega_3^2 - 12\omega_4 \omega_6^2 \omega_3^3 cs^2 - 6\omega_4^2 \omega_6^2 \omega_3^2 + 36\omega_4^3 \omega_6 \omega_3^3 cs^2 - 18\omega_4 v_2^2 \omega_6^2 \omega_3^3 - 12\omega_4^3 \omega_3^3 cs^2) \frac{\rho v_3}{12\omega_4^2 \omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_y^3 D_z v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_3^2 \partial x_3}$  :

$$C_{D_y^3 D_z v_3}^{(0), \text{SRT}} = (36 - 56\omega^2 cs^2 - 20\omega^2 v_2^2 + \omega^3 v_2^2 + 4\omega^3 cs^2 - 96cs^2 - 54\omega - 36v_2^2 - \omega^3 + 20\omega^2 + 144\omega cs^2 + 54\omega v_2^2) \frac{v_2 \rho}{12\omega^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT1}} = (-12\omega_6 \omega_3^3 cs^2 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - 48\omega_6^2 cs^2 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 - 12v_2^2 \omega_3^2 + 48\omega_6 \omega_3^2 cs^2 + 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 12v_2^2 \omega_6 \omega_3^3 + 90\omega_6^2 \omega_3 cs^2 + 12\omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 12\omega_3^3 cs^2 - 44\omega_6^2 \omega_3^2 cs^2 - 8v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 - 36\omega_6 \omega_3 cs^2 + 4\omega_6^2 \omega_3^3 cs^2 + 6\omega_3^3 cs^2 + 9\omega_6 \omega_3^3 - 36\omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT2}} = (-12cs^2 \omega_3^2 - 44cs^2 \omega_6^2 \omega_3^2 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 + 4cs^2 \omega_6^2 \omega_3^3 - \omega_6^2 \omega_3^3 - 36v_2^2 \omega_6 \omega_3 + 6cs^2 \omega_3^3 + 48v_2^2 \omega_6 \omega_3^2 - 48cs^2 \omega_6^2 - 12v_2^2 \omega_3^2 + 6v_2^2 \omega_3^3 - 12v_2^2 \omega_6 \omega_3^3 + 90cs^2 \omega_6^2 \omega_3 + 12\omega_3^2 - 36cs^2 \omega_6 \omega_3 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 8v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 + 9\omega_6 \omega_3^3 - 12cs^2 \omega_6 \omega_3^3 - 36\omega_6 \omega_3^2 + 48cs^2 \omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM1}} = (-36cs^2 \omega_6 \omega_3 + 12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3^2 - 30cs^2 \omega_6 \omega_3^3 - 60cs^2 \omega_3^2 + 96cs^2 \omega_6 \omega_3^2 - 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^3 + 30cs^2 \omega_3^2 + 12\omega_3^2 - 26cs^2 \omega_6^2 \omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 14v_2^2 \omega_6^2 \omega_3^2 + 4cs^2 \omega_6^2 \omega_3^3 - 6\omega_3^3 + 9\omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3 + 18cs^2 \omega_6^2 \omega_3 - 36\omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM2}} = (12v_2^2 \omega_6^2 + 11\omega_6^2 \omega_3^2 - 30\omega_6 \omega_3^3 cs^2 - \omega_6^2 \omega_3^3 - 60v_2^2 \omega_6 \omega_3 + 48v_2^2 \omega_6 \omega_3^2 + 12v_2^2 \omega_3^2 + 18\omega_6^2 \omega_3 cs^2 - 6v_2^2 \omega_3^3 - 12\omega_6^2 \omega_3 - 6v_2^2 \omega_6 \omega_3^3 + 96\omega_6 \omega_3^2 cs^2 + 12\omega_3^2 + 24\omega_6 \omega_3 + v_2^2 \omega_6^2 \omega_3^3 - 36\omega_6 \omega_3 cs^2 - 14v_2^2 \omega_6^2 \omega_3^2 - 6\omega_3^3 - 60\omega_3^2 cs^2 - 26\omega_6^2 \omega_3^2 cs^2 + 9\omega_6 \omega_3^3 + 12v_2^2 \omega_6^2 \omega_3 + 4\omega_6^2 \omega_3^3 cs^2 + 30\omega_3^3 cs^2 - 36\omega_6 \omega_3^2) \frac{v_2 \rho}{12\omega_6^2 \omega_3^3}$$

**coefficient**  $C_{D_t^2 D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t^2 \partial x_3^2}$  :

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{SRT}} = (-2 + 3\omega - \omega^2) \frac{3\rho v_3}{2\omega^3}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{MRT1}} = (2\omega_4^3 + 8\omega_7 \omega_4^2 - 4\omega_4^2 - 2\omega_7 \omega_4^3 - 4\omega_7 \omega_4 + 2\omega_7^2 - \omega_7^2 \omega_4 - \omega_7^2 \omega_4^2) \frac{\rho v_3}{2\omega_7^2 \omega_4^3}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{MRT}^2} = C_{D_t^2 D_z^2 v_3}^{(0), \text{MRT}^1}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{CLBM}^1} = (-2 - \omega_4^2 + 3\omega_4) \frac{3\rho v_3}{2\omega_4^3}$$

$$C_{D_t^2 D_z^2 v_3}^{(0), \text{CLBM}^2} = C_{D_t^2 D_z^2 v_3}^{(0), \text{CLBM}^1}$$

**coefficient**  $C_{D_t D_x D_z^2 v_1}^{(0)}$  **at**  $\frac{\partial^4 v_1}{\partial t \partial x_1 \partial x_3^2}$ :

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{SRT}} = (34\omega^2 cs^2 - 2\omega^3 cs^2 + 60cs^2 + \omega^3 v_3^2 - 90\omega cs^2 - 2\omega^2 v_3^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{MRT}^1} = (3\omega_7^2 \omega_4^3 cs^2 + 12\omega_7 \omega_4 \omega_2 cs^2 - 24\omega_7^2 \omega_2 v_3^2 - \omega_7^2 \omega_4^3 v_3^2 + 12\omega_7 \omega_4 \omega_2 v_3^2 + 12\omega_7^2 \omega_2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 22\omega_7^2 \omega_4^2 \omega_2 cs^2 + 12\omega_4^2 \omega_2 cs^2 - 18\omega_7^2 \omega_4^3 cs^2 + 9\omega_7 \omega_4^3 \omega_2 cs^2 - 10\omega_7^2 \omega_4^2 \omega_2 v_3^2 + 12\omega_4^2 \omega_2 v_3^2 + 6\omega_7^2 \omega_4^3 v_3^2 - 30\omega_7^2 \omega_4 \omega_2 cs^2 + 12\omega_7 \omega_4^3 cs^2 - 12\omega_7^2 \omega_4 v_3^2 + 36\omega_7 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4^3 v_3^2 + 12\omega_7^2 \omega_4 cs^2 - 6\omega_7 \omega_4^3 cs^2 - 6\omega_4^3 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 - 30\omega_7 \omega_4^2 \omega_2 cs^2 - 6\omega_7 \omega_4^3 v_3^2 - 6\omega_4^3 \omega_2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_2 cs^2 - 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{MRT}^2} = (12\omega^2 cs^2 \omega_2 - 24\omega^2 \omega_2 v_3^2 + 12\omega_7 \omega_4 cs^2 \omega_2 - \omega_7^2 \omega_4^3 v_3^2 + 12\omega_7 \omega_4 \omega_2 v_3^2 - 18\omega_7^2 \omega_4^2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 9\omega_7 \omega_4^3 cs^2 \omega_2 + 3\omega_7^2 \omega_4^3 cs^2 - 10\omega_7^2 \omega_4^2 \omega_2 v_3^2 + 12\omega_7^2 \omega_2 v_3^2 + 12\omega_4^2 cs^2 \omega_2 + 6\omega_7^2 \omega_4^3 v_3^2 + 22\omega_7^2 \omega_4^2 cs^2 \omega_2 - 12\omega_7^2 \omega_4 v_3^2 - 6\omega_7 \omega_4^3 cs^2 + 36\omega_7^2 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4^3 v_3^2 - 30\omega_7^2 \omega_4 cs^2 \omega_2 - 2\omega_7^2 \omega_4^3 cs^2 \omega_2 - 6\omega_4^3 cs^2 \omega_2 - 6\omega_4^3 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 + 12\omega_7^2 \omega_4 cs^2 - 6\omega_7 \omega_4^3 v_3^2 - 30\omega_7 \omega_4^2 cs^2 \omega_2 + 12\omega_7 \omega_4^3 cs^2 - 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{CLBM}^1} = (-6\omega_7 \omega_4^3 cs^2 - 30\omega_7 \omega_4^2 \omega_2 cs^2 + 24\omega_7^2 \omega_2 v_3^2 - \omega_7^2 \omega_4^3 v_3^2 - 12\omega_7 \omega_4 \omega_2 v_3^2 - 6\omega_4^3 \omega_2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_2 cs^2 - 30\omega_7^2 \omega_4 \omega_2 cs^2 - 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 12\omega_7 \omega_4^3 cs^2 + 8\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 12\omega_4^2 \omega_2 v_3^2 - 6\omega_7^2 \omega_4^3 v_3^2 + 12\omega_7^2 \omega_4 cs^2 + 22\omega_7^2 \omega_4^2 \omega_2 cs^2 + 12\omega_4^2 \omega_2 cs^2 + 12\omega_7^2 \omega_4 v_3^2 - 18\omega_7^2 \omega_4^3 cs^2 + 9\omega_7 \omega_4^3 \omega_2 cs^2 - 36\omega_7^2 \omega_4 \omega_2 v_3^2 - 12\omega_7 \omega_4^3 v_3^2 + 3\omega_7^2 \omega_4^3 cs^2 + 6\omega_4^3 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 + 12\omega_7 \omega_4 \omega_2 cs^2 + 6\omega_7 \omega_4^3 v_3^2 + 12\omega_7^2 \omega_2 cs^2 + 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2}$$

$$C_{D_t D_x D_z^2 v_1}^{(0), \text{CLBM}^2} = (12\omega^2 \omega_2 cs^2 + 24\omega^2 \omega_2 v_3^2 + 3\omega_7^2 \omega_4^3 cs^2 - \omega_7^2 \omega_4^3 v_3^2 - 12\omega_7 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4 \omega_2 cs^2 + 9\omega_7 \omega_4^3 \omega_2 cs^2 - 9\omega_7 \omega_4^3 \omega_2 v_3^2 + 8\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 12\omega_7^2 \omega_2 v_3^2 + 22\omega_7^2 \omega_2 \omega_2 cs^2 + 12\omega_4^2 \omega_2 cs^2 - 6\omega_7^2 \omega_4^3 v_3^2 - 18\omega_7^2 \omega_2 cs^2 + 12\omega_7^2 \omega_4 v_3^2 + 12\omega_7^2 \omega_4 cs^2 - 30\omega_7^2 \omega_4 \omega_2 cs^2 - 36\omega_7^2 \omega_4 \omega_2 v_3^2 + 12\omega_7 \omega_4^3 cs^2 - 12\omega_7 \omega_4^3 v_3^2 + 6\omega_4^3 \omega_2 v_3^2 + \omega_7^2 \omega_4^3 \omega_2 v_3^2 - 6\omega_4^3 \omega_2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_2 cs^2 + 6\omega_7 \omega_4^3 v_3^2 - 6\omega_7 \omega_4^3 cs^2 - 30\omega_7 \omega_4^2 \omega_2 cs^2 + 30\omega_7 \omega_4^2 \omega_2 v_3^2) \frac{\rho}{12\omega_7^2 \omega_4^3 \omega_2}$$

**coefficient**  $C_{D_t D_x D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t \partial x_1 \partial x_3^2}$ :

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_1 \rho v_3}{6\omega^3}$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{MRT}^1} = (12\omega^2 \omega_2^2 - 7\omega_7 \omega_4^3 \omega_2^2 - 6\omega_4^2 \omega_2^3 - 6\omega_7 \omega_4^3 - 6\omega_7 \omega_4^2 \omega_2 + \omega_7 \omega_4^3 \omega_2^3 + 12\omega_7 \omega_4^2 \omega_2^2 - 6\omega_4^3 \omega_2^2 + 12\omega_7 \omega_4^3 \omega_2 - 10\omega_7 \omega_4^2 \omega_2^3 - 12\omega_7 \omega_2^3 + 3\omega_4^3 \omega_2^3 + 24\omega_7 \omega_4 \omega_2^2 - 12\omega_7 \omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_7 \omega_4^3 \omega_2^3}$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{MRT}^2} = C_{D_t D_x D_z^2 v_3}^{(0), \text{MRT}^1}$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{CLBM}^1} = (6\omega_4^2 \omega_2^2 - 6\omega_4^3 - 7\omega_4^2 \omega_2^3 + 12\omega_4^3 \omega_2 - 12\omega_2^3 - 7\omega_4^3 \omega_2^2 + \omega_4^3 \omega_2^3 - 6\omega_4^2 \omega_2 + 18\omega_4 \omega_2^2) \frac{v_1 \rho v_3}{6\omega_4^3 \omega_2^3}$$

$$C_{D_t D_x D_z^2 v_3}^{(0), \text{CLBM}^2} = C_{D_t D_x D_z^2 v_3}^{(0), \text{CLBM}^1}$$

**coefficient**  $C_{D_x^2 D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2}$ :

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{SRT}} = (-14\omega^2 v_1^2 cs^2 + 56v_1^2 v_3^2 - 84\omega v_1^2 v_3^2 - 24\omega cs^4 + \omega^3 cs^2 v_3^2 + 36\omega cs^2 v_3^2 - 3\omega^3 v_1^2 v_3^2 - 24cs^2 v_3^2 - \omega^3 cs^4 - 14\omega^2 cs^2 v_3^2 + \omega^3 v_1^2 cs^2 + 16cs^4 + 36\omega v_1^2 cs^2 + 10\omega^2 cs^4 - 24v_1^2 cs^2 + 34\omega^2 v_1^2 v_3^2) \frac{1}{4\omega^3}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT}^1} = (20\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^3 v_3^2 + \omega_7 \omega_4^3 \omega_5^2 \omega_2^3 cs^4 + 10\omega_7^2 \omega_4^3 \omega_5 \omega_2^3 v_3^2 cs^2 - 12\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 cs^4 - 4\omega_4^2 \omega_5^2 v_1^2 \omega_3^3 v_3^2 - 4\omega_7 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 cs^2 - 8\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^3 cs^2 - 2\omega_7^2 \omega_4^3 \omega_5 v_1^2 \omega_2^2 cs^2 - 38\omega_7^2 \omega_4 \omega_5^2 v_1^2 \omega_3^3 v_3^2 - \omega_7^2 \omega_4^3 \omega_5^2 v_3^3 cs^4 - 4\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 4\omega_7 \omega_4^2 \omega_5^2 \omega_2^2 cs^4 - 4\omega_7^2 \omega_4 \omega_5^2 v_1^2 \omega_2^2 cs^2 + \omega_7 \omega_4^3 \omega_5^2 v_3^3 v_3^2 cs^2 - 3\omega_7^2 \omega_4^3 \omega_5 v_1^2 \omega_3^3 v_3^2 + 10\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_3^3 cs^2 + 4\omega_7^2 \omega_4^3 \omega_5^2 v_2^2 \omega_2 cs^2 + 12\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 cs^2 - 4\omega_7^2 \omega_4^3 \omega_5^2 v_3^2 cs^2 - 2\omega_7 \omega_4^3 \omega_5^2 \omega_2^2 cs^4 - 4\omega_7 \omega_4 \omega_5^2 v_1^2 \omega_3^3 v_3^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 cs^4 + 10\omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 cs^2 - 36\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 2\omega_7^2 \omega_4^3 \omega_5 \omega_2^3 v_3^2 cs^2 + 10\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^3 v_3^2 - 38\omega_7^2 \omega_4^3 \omega_5^2 v_1^2 \omega_2 v_3^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 cs^4 - 2\omega_7 \omega_4^3 \omega_5^2 \omega_2^3 cs^4 + 20\omega_7^2 \omega_4 \omega_5^2 v_1^2 \omega_2^3 v_3^2 + \omega_7^2 \omega_4^3 \omega_5 v_1^2 \omega_2^3 cs^2 + 12\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 cs^2 - 4\omega_7 \omega_4^3 \omega_5^2 v_1^2 \omega_3^3 cs^2 - 8\omega_7^2 \omega_4 \omega_5^2 \omega_2^3 v_3^2 cs^2 + 2\omega_7^2 \omega_4^3 \omega_5^2 v_3^2 cs^2 + 2\omega_7^2 \omega_4^3 v_1^2 \omega_2^3 v_3^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2 v_3^2 cs^2 + 20\omega_7^2 \omega_4^3 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4^3 \omega_5^2 \omega_2 cs^4 - 8\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2 cs^2 - 3\omega_7 \omega_4^3 \omega_5^2 v_1^2 \omega_2^3 cs^2 - 8\omega_7^2 \omega_4^3 \omega_5^2 \omega_2^3 v_3^2 cs^2 + 4\omega_7^2 \omega_4 \omega_5^2 \omega_2^2 cs^4 - 2\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 cs^4 + 2\omega_7^2 \omega_4^2 \omega_5 v_1^2 \omega_2^3 v_3^2 - 2\omega_7 \omega_4^3 \omega_5^2 \omega_2^2 v_3^2 cs^2 - 4\omega_7^2 \omega_4^3 \omega_5^2 v_1^2 \omega_2^2 cs^2 - 2\omega_7^2 \omega_4^3 \omega_5 \omega_2^2 cs^4 - 2\omega_7^2 \omega_4^2 \omega_5 v_1^2 \omega_2^3 cs^2 + 20\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2 v_3^2 - 3\omega_7 \omega_4^3 \omega_5^2 v_1^2 \omega_2^3 v_3^2 - 3\omega_7^2 \omega_4^2 \omega_5 \omega_2^3 v_3^2 cs^2 - 4\omega_7^2 \omega_4^3 \omega_5 \omega_2^2 v_3^2 cs^2 + 4\omega_7^2 \omega_4^2 \omega_5 \omega_2^2 cs^4 - 4\omega_7^2 \omega_4^3 \omega_5 v_1^2 \omega_2^3 v_3^2 + 2\omega_7 \omega_4^3 \omega_5^2 v_1^2 \omega_2^2 cs^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^3 v_3^2 cs^2 -$$

$$C_{D_2 D_2 \rho}^{(0), \text{MRT2}} = (20\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - 4\omega_7^2\omega_3^2\omega_5^2\omega_2v_3^2 + \omega_7\omega_3^3\omega_4^2\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^2\omega_5^2\omega_2 - 4\omega_7\omega_4^2\omega_5^2\omega_2^2\omega_1^2\omega_2^2 - 4\omega_7^2\omega_5^2v_1^2\omega_2^2v_3^2 - 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_2^2 - 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 + 10\omega_7^2\omega_3^2\omega_5^2v_1^2\omega_2^2v_3^2 + 10\omega_7\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_2^2 - 2\omega_7\omega_4^2\omega_5^2\omega_2^2 - 8\omega_7^2\omega_3^2\omega_5^2\omega_2^2v_3^2 - 38\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - \omega_7^2\omega_3^3\omega_4^2\omega_5^2\omega_2^2 - 4\omega_7\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 - 8\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 3\omega_7^2\omega_5^2\omega_4\omega_1^2\omega_2^2v_3^2 + 4\omega_7\omega_3^2\omega_4^2\omega_5^2\omega_2^2 - 2\omega_7\omega_3^2\omega_4^2\omega_5^2\omega_2^2v_3^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 + \omega_7^2\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_2^2 - 4\omega_7\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 + 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2 - 4\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 36\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 + 2\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 + 10\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 38\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - 2\omega_7^2\omega_3^2\omega_4^2\omega_5^2\omega_2^2 - 2\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 + 2\omega_7\omega_3^2\omega_4^2\omega_5^2\omega_2^2 + 20\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - 2\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 + 4\omega_7\omega_4^2\omega_5^2\omega_2^2v_3^2 + 2\omega_3^3\omega_4^2\omega_5^2\omega_2^2 + 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 + 4\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_2^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_3^2 - 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_1^2\omega_2^2 - 2\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 + 2\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - 4\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_3^2 - 4\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 8\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 - 4\omega_7^2\omega_5^2\omega_4\omega_1^2\omega_2^2v_3^2 - 2\omega_7\omega_3^2\omega_4^2\omega_5^2\omega_2^2 + 10\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 - 2\omega_7^2\omega_4^2\omega_5^2\omega_2^2 - 2\omega_7\omega_4^2\omega_5^2\omega_2^2v_3^2 + 3\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 + 10\omega_7^2\omega_4^2\omega_5^2\omega_2^2v_3^2 + 2\omega_7\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2 + 4\omega_7^2\omega_4^2\omega_5^2\omega_2^2 - 4\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 2\omega_7^2\omega_3^2\omega_4^2\omega_5^2v_3^2 + 12\omega_7^2\omega_2^2\omega_3^2\omega_4^2\omega_5^2v_3^2 + 20\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2 - 3\omega_7\omega_3^2\omega_4^2\omega_5^2v_1^2\omega_2^2 + 20\omega_7^2\omega_5^2v_1^2\omega_2^2v_3^2 - 4\omega_7^2\omega_4^2\omega_5^2v_1^2\omega_2^2v_3^2) \frac{1}{4\omega_7^2\omega_1^2\omega_2^2\omega_3^2}$$

$$C_{D_2^2 D_2^2}^{(0), \text{CLMB2}} = (-4\omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 + 14\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 v_3^2 + \omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 8\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 - 4\omega_7 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 + 4\omega_4^2 \omega_5^2 v_1^2 \omega_3^2 v_3^2 + 2\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 + 4\omega_7 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 - \omega_7^2 \omega_4^2 \omega_5^2 \omega_3^2 c s^4 - 10\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 v_3^2 + 10\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 12\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 + \omega_7 \omega_4^2 \omega_5^2 \omega_3^2 c s^4 - 14\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 v_3^2 - 4\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 + 4\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 10\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 - 2\omega_7 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 + 2\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 + 3\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 v_3^2 - \omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 + 8\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 + 4\omega_7 \omega_4 \omega_5^2 v_1^2 \omega_3^2 v_3^2 + 2\omega_7^2 \omega_4^2 \omega_5^2 v_3^2 c s^2 - 4\omega_7 \omega_4 \omega_5^2 v_1^2 \omega_3^2 c s^2 - 28\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 - 10\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 14\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - \omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 c s^2 + 8\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 + 10\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 c s^2 + 12\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_3^2 c s^4 - 4\omega_7^2 \omega_4^2 \omega_5^2 v_3^2 c s^2 - 2\omega_7 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 + 10\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 2\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 14\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 - 2\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 + 2\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 8\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^4 - 3\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 + 2\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 12\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 + 4\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^4 + \omega_7^2 \omega_4^2 \omega_5^2 \omega_3^2 c s^4 + \omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 - 2\omega_4^2 \omega_5^2 v_1^2 \omega_3^2 v_3^2 + 2\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 + 2\omega_3^2 \omega_5^2 v_1^2 \omega_3^2 c s^2 + 4\omega_7^2 \omega_4^2 v_1^2 \omega_2^2 v_3^2 - 2\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 3\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 2\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 c s^4 - 2\omega_7 \omega_4 \omega_5^2 \omega_3^2 c s^4 + 2\omega_7 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 v_3^2 c s^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 4\omega_7^2 \omega_4^2 \omega_5^2 \omega_2^2 v_3^2 c s^2 - 4\omega_7^2 \omega_5^2 v_1^2 \omega_2^2 c s^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_3^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2 + 4\omega_7^2 \omega_4^2 \omega_5^2 v_1^2 \omega_2^2 v_3^2) \frac{1}{4\omega_2^2 \omega_4^2 \omega_5^2 \omega_3^2}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}} = (-78\omega_7^2\omega_4\omega_3^2v_3^2 - 6\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_7^2\omega_4^3v_3^2 + 22\omega_7^2\omega_3^3\omega_2^2v_3^2 + 24\omega_7^2\omega_4\omega_2^2cs^2 + 24\omega_7\omega_4^3\omega_2^3v_3^2 + 6\omega_7^3\omega_2^3cs^2 + \omega_7^2\omega_4^3\omega_2^3cs^2 - 12\omega_7^2\omega_4^2\omega_2cs^2 + 24\omega_7^2\omega_4\omega_2^3v_3^2 + 24\omega_7^2\omega_4^2\omega_2^3v_3^2 + 24\omega_7\omega_4^3\omega_2^3cs^2 + 6\omega_4^3\omega_2^3v_3^2 - 4\omega_7^3\omega_2^3v_3^2 - 48\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7\omega_4\omega_2^3v_3^2 - 12\omega_7^2\omega_2^3cs^2 - 12\omega_7\omega_4\omega_2^3cs^2 + 48\omega_7^2\omega_2^3v_3^2 + 12\omega_7^2\omega_4^2cs^2 - 30\omega_7^2\omega_4\omega_2v_3^2 + 34\omega_7^2\omega_4^2v_3^2 - 12\omega_4^3\omega_2^3v_3^2 - 6\omega_7\omega_4^3\omega_2^3cs^2 - 14\omega_7^2\omega_4^2\omega_2^3cs^2 - 12\omega_4^2\omega_2^3cs^2 - 6\omega_7\omega_4^3\omega_2^3v_3^2 + 6\omega_7^2\omega_4^2\omega_2cs^2) \frac{v_1\rho}{12\omega_2^3\omega_3^3}$$

$$C_{\mathbf{D}_x^2 \mathbf{D}_1 \mathbf{D}_2 \mathbf{D}_3}^{(0), \text{CLBMM1}} = (-18\omega_2^2 \omega_4 \omega_3^2 v_3^2 - 6\omega_7 \omega_4^2 \omega_3^2 cs^2 + 12\omega_7^2 \omega_4^2 v_3^2 - 14\omega_2^2 \omega_4^2 \omega_3^2 cs^2 + 22\omega_7^2 \omega_3^2 \omega_2^2 v_3^2 - 12\omega_4^2 \omega_3^2 cs^2 + 6\omega_7^2 \omega_4^2 \omega_2 cs^2 - 24\omega_7 \omega_4^2 \omega_3^2 v_3^2 - 12\omega_2^2 \omega_4^2 \omega_3^2 cs^2 + 24\omega_7^2 \omega_4^2 \omega_2^2 v_3^2 - 12\omega_7 \omega_4 \omega_3^2 cs^2 + 24\omega_7^2 \omega_4^2 \omega_2 v_3^2 - 6\omega_3^2 \omega_2^2 v_3^2 - 4\omega_7^2 \omega_3^2 \omega_2^2 v_3^2 + 12\omega_7^2 \omega_4^2 \omega_2^2 cs^2 + 6\omega_4^2 \omega_3^2 cs^2 + \omega_2^2 \omega_4^2 \omega_3^2 cs^2 - 48\omega_7^2 \omega_4^2 \omega_2^2 v_3^2 -$$

$$12\omega_7^2\omega_4^2\omega_2cs^2 + 12\omega_7\omega_4\omega_3^3v_3 + 24\omega_7\omega_4^2\omega_3^2cs^2 - 30\omega_7^2\omega_4^2\omega_3v_3^2 + 22\omega_7^2\omega_4^2\omega_3^2v_3^2 - 6\omega_7^2\omega_4^3\omega_3^2cs^2 + 12\omega_4^2\omega_3^3v_3^2 + 6\omega_7\omega_4^3\omega_3^2v_3^2 + 24\omega_7^2\omega_4\omega_3^3cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{CLBM2}} = (-18\omega_7^2\omega_4\omega_3^3v_3^2 + 24\omega_7^2\omega_4\omega_3^2cs^2 + 12\omega_7^2\omega_4^3v_3^2 + 22\omega_7^2\omega_4^3\omega_3^2v_3^2 - 6\omega_7^2\omega_4^3\omega_3^2cs^2 - 24\omega_7\omega_4^3\omega_3^3v_3^2 + 24\omega_7\omega_4^2\omega_3^3cs^2 + 24\omega_7^2\omega_4\omega_3^2v_3^2 + 6\omega_4^3\omega_3^3cs^2 + \omega_7^2\omega_4^3\omega_3^2cs^2 + 24\omega_7^2\omega_4^2\omega_3v_3^2 - 12\omega_7^2\omega_4^2\omega_3^2cs^2 - 6\omega_4^3\omega_3^3v_3^2 - 4\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4\omega_3^3cs^2 - 48\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_7\omega_4\omega_3^2v_3^2 + 12\omega_7^2\omega_4^2\omega_3^2cs^2 - 12\omega_7^2\omega_3^2cs^2 - 30\omega_7^2\omega_4\omega_3^2v_3^2 - 14\omega_7^2\omega_4^2\omega_3^2cs^2 - 12\omega_4^3\omega_3^2cs^2 + 22\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_4^3\omega_3^2v_3^2 + 6\omega_7^2\omega_4^3\omega_3^2cs^2 + 6\omega_7\omega_4^3\omega_3^2v_3^2 - 6\omega_7\omega_4^3\omega_3^2cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$\text{coefficient } C_{D_x^2 D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} :$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{SRT}} = (-26\omega^2cs^2 + 50\omega^2v_1^2 + 84v_1^2 + \omega^3cs^2 - 4\omega^3v_1^2 - 48cs^2 - 126\omega v_1^2 + 72\omega cs^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT1}} = (34\omega_4^3\omega_5^2v_1^2\omega_2^2 + 6\omega_4\omega_5^2\omega_3^3cs^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 - 12\omega_4^3\omega_5^2cs^2 - 6\omega_4^3\omega_5\omega_3^2cs^2 - 4\omega_4^3\omega_5^2v_1^2\omega_3^2 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 22\omega_4^2\omega_5^2v_1^2\omega_2^3 + 6\omega_4^3\omega_3^3cs^2 + 24\omega_4^3\omega_5^2\omega_2cs^2 - 12\omega_4^3\omega_5^2cs^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 78\omega_4^3\omega_5^2v_1^2\omega_2 + 24\omega_4^3\omega_5\omega_3^2cs^2 - 6\omega_4^2\omega_5^2\omega_3^2cs^2 + 6\omega_4^3v_1^2\omega_3^2 - 12\omega_4^3\omega_5\omega_2cs^2 - 12\omega_4^3v_1^2\omega_2^2 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 + 12\omega_5^2v_1^2\omega_3^2 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2 + 24\omega_4^3\omega_5v_1^2\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2^2cs^2 - 30\omega_4\omega_5^2v_1^2\omega_3^2 - 6\omega_4^3\omega_5v_1^2\omega_2^2 + \omega_4^3\omega_5^2\omega_3^2cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_3^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT2}} = (34\omega_4^3\omega_5^2v_1^2\omega_2^2 - 6\omega_4^3cs^2\omega_5^2\omega_3^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 + 24\omega_4^3cs^2\omega_5^2\omega_2 - 4\omega_4^3\omega_5^2v_1^2\omega_3^2 + 12\omega_4^2cs^2\omega_5^2\omega_2^2 + 22\omega_4^2\omega_5^2v_1^2\omega_3^2 - 14\omega_4^3cs^2\omega_5^2\omega_2^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 78\omega_4^3\omega_5^2v_1^2\omega_2 + \omega_4^3cs^2\omega_5^2\omega_2^2 + 6\omega_4^3v_1^2\omega_3^2 + 6\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_4^3cs^2\omega_5^2 + 6\omega_4^3cs^2\omega_3^2 - 6\omega_4^3cs^2\omega_5\omega_3^2 - 12\omega_4cs^2\omega_5^2\omega_2^2 - 12\omega_4^3v_1^2\omega_2^2 + 24\omega_4^3cs^2\omega_5\omega_2^2 - 12\omega_4^3cs^2\omega_2^2 + 12\omega_5^2v_1^2\omega_3^2 - 12\omega_4^3\omega_5v_1^2\omega_2 + 48\omega_4^3\omega_5^2v_1^2 - 12\omega_4^3cs^2\omega_5\omega_2 + 24\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_3^2 - 6\omega_4^3\omega_5v_1^2\omega_2^2 + \omega_4^3\omega_5^2\omega_3^2cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_3^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM1}} = (22\omega_4^3\omega_5^2v_1^2\omega_2^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 + 12\omega_4^2\omega_5^2\omega_3^2cs^2 + \omega_4^3\omega_5^2\omega_3^2cs^2 - 4\omega_4^3\omega_5^2v_1^2\omega_3^2 + 22\omega_4^2\omega_5^2v_1^2\omega_3^2 - 6\omega_4^2\omega_5^2\omega_3^2cs^2 - 12\omega_4^3\omega_5\omega_2cs^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 18\omega_4^3\omega_5^2v_1^2\omega_2 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 + 6\omega_4^3\omega_3^2cs^2 - 6\omega_4^3v_1^2\omega_3^2 - 12\omega_4\omega_5^2\omega_2^2cs^2 + 24\omega_4^3\omega_5^2\omega_2cs^2 - 12\omega_4^3\omega_5^2cs^2 + 12\omega_4^3v_1^2\omega_2^2 + 12\omega_5^2v_1^2\omega_3^2 + 12\omega_4^3\omega_5v_1^2\omega_2 + 24\omega_4^3\omega_5\omega_2^2cs^2 - 24\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_3^2 - 12\omega_4^3\omega_2^2cs^2 + 6\omega_4\omega_5^2\omega_3^2cs^2 + 6\omega_4^3\omega_5v_1^2\omega_3^2 - 6\omega_4^3\omega_5\omega_2^2cs^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_3^3}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM2}} = (22\omega_4^3\omega_5^2v_1^2\omega_2^2 - 6\omega_4^3\omega_5\omega_3^2cs^2 + 24\omega_4^2\omega_5^2v_1^2\omega_2 - 4\omega_4^3\omega_5^2v_1^2\omega_3^2 - 12\omega_4^3\omega_2^2cs^2 + 6\omega_4\omega_5^2\omega_3^2cs^2 + 22\omega_4^2\omega_5^2v_1^2\omega_3^2 + 24\omega_4^3\omega_5\omega_2^2cs^2 + 6\omega_4^3\omega_5^2\omega_2^2cs^2 - 12\omega_4\omega_5^2\omega_3^2cs^2 - 48\omega_4^2\omega_5^2v_1^2\omega_2^2 - 18\omega_4^3\omega_5^2v_1^2\omega_2 + 24\omega_4^3\omega_5^2\omega_2cs^2 - 12\omega_4^3\omega_5^2cs^2 - 6\omega_4^3v_1^2\omega_3^2 - 14\omega_4^3\omega_5^2\omega_2^2cs^2 - 6\omega_4^2\omega_5^2\omega_3^2cs^2 + 12\omega_4^3v_1^2\omega_2^2 - 12\omega_4^3\omega_5\omega_2cs^2 + 12\omega_5^2v_1^2\omega_3^2 + 12\omega_4^3\omega_5v_1^2\omega_2 + \omega_4^3\omega_5^2\omega_3^2cs^2 - 24\omega_4^3\omega_5v_1^2\omega_2^2 - 30\omega_4\omega_5^2v_1^2\omega_3^2 + 6\omega_4^3\omega_5v_1^2\omega_2^2 + 24\omega_4\omega_5^2v_1^2\omega_2^2 + 12\omega_4^2\omega_5^2\omega_2^2cs^2) \frac{\rho v_3}{12\omega_4^3\omega_5^2\omega_3^3}$$

$$\text{coefficient } C_{D_t D_y D_z^2 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial t \partial x_2 \partial x_3^2} :$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{SRT}} = (34\omega^2cs^2 - 2\omega^3cs^2 + 60cs^2 + \omega^3v_3^2 - 90\omega cs^2 - 2\omega^2v_3^2) \frac{\rho}{12\omega^3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{MRT1}} = (3\omega_7^2\omega_4^3cs^2 - 30\omega_7\omega_4^2\omega_3cs^2 - 6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - \omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^2\omega_3v_3^2 - 6\omega_4^3\omega_3cs^2 - 2\omega_7^2\omega_4^3\omega_3cs^2 - 30\omega_7^2\omega_4\omega_3cs^2 - 18\omega_7^2\omega_4^2\omega_3v_3^2 + 36\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_7^2\omega_4^2v_3^2 + 22\omega_7^2\omega_4^2\omega_3cs^2 + 12\omega_4^2\omega_3cs^2 + 9\omega_7\omega_4^3\omega_3v_3^2 + 12\omega_7\omega_4^2cs^2 - 12\omega_7^2\omega_4v_3^2 - 10\omega_7^2\omega_4^2\omega_3v_3^2 + 12\omega_4^2\omega_3v_3^2 + 9\omega_7\omega_4^3\omega_3cs^2 + 12\omega_7\omega_4^2v_3^2 + 12\omega_7^2\omega_4cs^2 - 6\omega_7\omega_4^3cs^2 + 12\omega_7\omega_4\omega_3cs^2 - 24\omega_7^2\omega_3v_3^2 - 6\omega_7\omega_4^3v_3^2 + 12\omega_7\omega_4\omega_3v_3^2 + 12\omega_7^2\omega_3cs^2) \frac{\rho}{12\omega_7^2\omega_4^3\omega_3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{MRT2}} = (-30\omega_7\omega_4^2cs^2\omega_3 - 6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_4^3cs^2\omega_3 - 2\omega_7^2\omega_4^3cs^2\omega_3 - \omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^2\omega_3v_3^2 - 18\omega_7^2\omega_4^2cs^2 - 30\omega_7^2\omega_4cs^2\omega_3 + 3\omega_7^2\omega_4^3cs^2 + 36\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_7^2\omega_4^2v_3^2 + 9\omega_7\omega_4^3\omega_3v_3^2 - 12\omega_7^2\omega_4v_3^2 + 22\omega_7^2\omega_4^2cs^2\omega_3 + 12\omega_4^2cs^2\omega_3 - 10\omega_7^2\omega_4^2\omega_3v_3^2 + 12\omega_4^2\omega_3v_3^2 - 6\omega_7\omega_4^3cs^2 + 12\omega_7\omega_4^2v_3^2 + 9\omega_7\omega_4^3cs^2\omega_3 + 12\omega_7\omega_4cs^2\omega_3 + 12\omega_7^2\omega_4cs^2 - 24\omega_7^2\omega_3v_3^2 - 6\omega_7\omega_4^3v_3^2 + 12\omega_7^2cs^2\omega_3 + 12\omega_7\omega_4^2cs^2 + 12\omega_7\omega_4\omega_3v_3^2) \frac{\rho}{12\omega_7^2\omega_4^3\omega_3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{CLBM1}} = (-6\omega_7\omega_4^3cs^2 - 30\omega_7^2\omega_4cs^2\omega_3 + 6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - \omega_7^2\omega_4^3v_3^2 + 30\omega_7\omega_4^2\omega_3v_3^2 - 30\omega_7\omega_4^2cs^2\omega_3 + 12\omega_7\omega_4^2cs^2 - 6\omega_4^3cs^2\omega_3 - 36\omega_7^2\omega_4\omega_3v_3^2 - 2\omega_7^2\omega_4^3cs^2\omega_3 - 6\omega_7^2\omega_4^2v_3^2 + 12\omega_7^2\omega_4cs^2 + 12\omega_7\omega_4cs^2\omega_3 - 9\omega_7\omega_4^3\omega_3v_3^2 + 12\omega_7^2\omega_4v_3^2 - 18\omega_7^2\omega_4^2cs^2 + 8\omega_7^2\omega_4^2\omega_3v_3^2 - 12\omega_4^2\omega_3v_3^2 + 12\omega_7^2cs^2\omega_3 - 12\omega_7\omega_4^2v_3^2 + 3\omega_7^2\omega_4^3cs^2 + 22\omega_7^2\omega_4^2cs^2\omega_3 + 12\omega_4^2cs^2\omega_3 + 24\omega_7^2\omega_3v_3^2 + 6\omega_7\omega_4^3v_3^2 - 12\omega_7\omega_4\omega_3v_3^2 + 9\omega_7\omega_4^3cs^2\omega_3) \frac{\rho}{12\omega_7^2\omega_4^3\omega_3}$$

$$C_{D_t D_y D_z^2 v_2}^{(0), \text{CLBM2}} = (6\omega_4^3\omega_3v_3^2 + \omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_4^3\omega_3cs^2 - 2\omega_7^2\omega_4^3\omega_3cs^2 + 3\omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^2\omega_3cs^2 + 30\omega_7\omega_4^2\omega_3v_3^2 - 30\omega_7^2\omega_4\omega_3cs^2 - 36\omega_7^2\omega_4\omega_3v_3^2 - 6\omega_7^2\omega_4^2v_3^2 - 18\omega_7^2\omega_4^2cs^2 + 9\omega_7\omega_4^3\omega_3cs^2 - 9\omega_7\omega_4^3\omega_3v_3^2 + 12\omega_7^2\omega_4v_3^2 + 12\omega_7^2\omega_4cs^2 + 8\omega_7^2\omega_4^2\omega_3v_3^2 - 12\omega_4^2\omega_3v_3^2 + 22\omega_7^2\omega_4^2\omega_3cs^2 + 12\omega_4^2\omega_3cs^2 + 12\omega_7\omega_4^2cs^2 - 12\omega_7\omega_4^2v_3^2 + 12\omega_7^2\omega_3cs^2 + 24\omega_7^2\omega_3v_3^2 + 6\omega_7\omega_4^3v_3^2 - 6\omega_7\omega_4^3cs^2 - 12\omega_7\omega_4\omega_3v_3^2 + 12\omega_7\omega_4\omega_3cs^2) \frac{\rho}{12\omega_7^2\omega_4^3\omega_3}$$

$$\text{coefficient } C_{D_t D_y D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial t \partial x_2 \partial x_3^2} :$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{SRT}} = (-24 + 36\omega + \omega^3 - 14\omega^2) \frac{v_2\rho v_3}{6\omega^3}$$

$$C_{D_t D_y D_z^2 v_3}^{(0), \text{MRT1}} = (-6\omega_7\omega_4^3 - 12\omega_7\omega_4\omega_3^2 + 24\omega_7\omega_4\omega_3^3 + 12\omega_7\omega_4^3\omega_3 - 10\omega_7\omega_4^2\omega_3^3 + 3\omega_4^3\omega_3^3 - 12\omega_7\omega_3^3 + 12\omega_7\omega_4^2\omega_3^3 - 6\omega_4^3\omega_3^3 - 6\omega_4^2\omega_3^3 - 6\omega_7\omega_4^2\omega_3 +$$



$$36\omega_7\omega_4\omega_3^3v_3^2 + 48\omega_7^2\omega_4\omega_3^2v_3^2 - 12\omega_7^2\omega_4cs^2\omega_3 - 12\omega_7\omega_4cs^2\omega_3^3 + 24\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_4^3\omega_3^3v_3^2 - 5\omega_7^2\omega_4^3\omega_3^3v_3^2 - 12\omega_7^2cs^2\omega_3^3 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 12\omega_4^3cs^2\omega_3^3 - 32\omega_7^2\omega_4^2cs^2\omega_3^3 - 90\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_3^3v_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^3 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 + 24\omega_7^2\omega_4\omega_3^3v_3^2) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM1}} = (-30\omega_7^2\omega_4^3\omega_3v_3^2 + 16\omega_7^2\omega_4^2\omega_3^3v_3^2 - 12\omega_7^2\omega_4^3cs^2\omega_3 + 12\omega_4^2\omega_3^3v_3^2 + 36\omega_7\omega_4^2cs^2\omega_3^3 + 12\omega_7^2\omega_4^3v_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^3 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 6\omega_4^3cs^2\omega_3^3 + 12\omega_7\omega_4^3\omega_3^3v_3^2 - 36\omega_7^2\omega_4^2\omega_3^3v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 36\omega_7^2\omega_4cs^2\omega_3^3 - 24\omega_7^2\omega_4cs^2\omega_3^2 - 12\omega_7\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3 - 12\omega_4^3cs^2\omega_3^3 + 12\omega_7\omega_4^2cs^2\omega_3^2 - 36\omega_7\omega_4^2\omega_3^3v_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_3^3 + 24\omega_7^2\omega_4^2\omega_3v_3^2 - 6\omega_4^3\omega_3^3v_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^3 - 5\omega_7^2\omega_4^3\omega_3^3v_3^2 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 - 6\omega_7^2\omega_4\omega_3^3v_3^2 - 12\omega_7\omega_4cs^2\omega_3^3 - 12\omega_7^2\omega_4^2cs^2\omega_3 + 24\omega_7\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4\omega_3^2v_3^2 - 12\omega_7^2cs^2\omega_3^3) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM2}} = (-32\omega_7^2\omega_4^3\omega_3cs^2 - 12\omega_4^3\omega_3cs^2 - 30\omega_7^2\omega_4\omega_3v_3^2 + 6\omega_7^2\omega_4\omega_3cs^2 + 16\omega_7^2\omega_4^3\omega_3^3v_3^2 + 12\omega_4^2\omega_3^3v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4^3\omega_3^3v_3^2 - 12\omega_7\omega_4^3\omega_3^3cs^2 - 12\omega_7\omega_4\omega_3^3cs^2 - 36\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 48\omega_7^2\omega_4^2\omega_3^2cs^2 + 12\omega_7\omega_4^3\omega_3^2cs^2 - 12\omega_7\omega_4^3\omega_3^3v_3^2 - 12\omega_7^2\omega_4^3cs^2 - 36\omega_7\omega_4^2\omega_3^3v_3^2 - 24\omega_7^2\omega_4\omega_3^3cs^2 + 36\omega_7\omega_4^3\omega_3^3cs^2 + 24\omega_7^2\omega_4^2\omega_3v_3^2 + 6\omega_4^3\omega_3^3cs^2 + 4\omega_7^2\omega_4^3\omega_3^3cs^2 - 6\omega_4^3\omega_3^3v_3^2 - 5\omega_7^2\omega_4^3\omega_3^3v_3^2 - 12\omega_7^2\omega_4\omega_3cs^2 - 6\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_3^3cs^2 + 36\omega_7^2\omega_4\omega_3^3cs^2 + 24\omega_7\omega_4^2\omega_3^2v_3^2 + 24\omega_7^2\omega_4\omega_3^2v_3^2 - 12\omega_7^2\omega_4^3\omega_3^3cs^2) \frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

**coefficient**  $C_{D_x D_y D_z^2 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2}$ :

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{SRT}} = (-56\omega^2cs^2 - 126\omega v_3^2 + 4\omega^3cs^2 - 96cs^2 + 84v_3^2 - 5\omega^3v_3^2 + 144\omega cs^2 + 52\omega^2v_3^2) \frac{v_1\rho}{12\omega^3}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}} = (-90\omega_7^2\omega_4\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_2^2v_3^2 - 12\omega_7^2\omega_4\omega_2^2cs^2 + 12\omega_7^2\omega_4^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 24\omega_7^2\omega_4\omega_2^2v_3^2 + 36\omega_7^2\omega_4\omega_3^2cs^2 + 36\omega_7\omega_4^2\omega_3^2v_3^2 + 6\omega_4^3\omega_3^2cs^2 + 4\omega_7^2\omega_4^3\omega_3^2cs^2 - 12\omega_7^2\omega_4\omega_2^2cs^2 + 48\omega_7^2\omega_4\omega_2^2v_3^2 + 24\omega_7^2\omega_4\omega_2^2v_3^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 + 36\omega_7\omega_4^2\omega_3^2cs^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 60\omega_7^2\omega_4^2\omega_3^2v_3^2 + 12\omega_7\omega_4^3\omega_3^2cs^2 - 12\omega_7\omega_4\omega_3^2v_3^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4\omega_3^2cs^2 + 48\omega_7^2\omega_3^3v_3^2 + 48\omega_7^2\omega_4\omega_3^2cs^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 - 30\omega_7^2\omega_4^3\omega_2^2v_3^2 + 40\omega_7^2\omega_4^2\omega_3^3v_3^2 - 12\omega_7^2\omega_4^2\omega_3^3v_3^2 - 12\omega_7\omega_4^3\omega_3^2cs^2 - 32\omega_7^2\omega_4^2\omega_3^3cs^2 - 12\omega_4^2\omega_3^3cs^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 + 6\omega_7^2\omega_4^3\omega_2^2cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT2}} = (48\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7\omega_4^3cs^2\omega_2^2 - 90\omega_7^2\omega_4\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_2^2v_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_2^2 + 12\omega_7\omega_4^3cs^2\omega_2^2 - 12\omega_4^2cs^2\omega_2^3 + 12\omega_7^2\omega_4^3v_3^2 + 24\omega_7^2\omega_4^2\omega_3^3v_3^2 + 36\omega_7\omega_4^3\omega_3^3v_3^2 + 48\omega_7^2\omega_4\omega_3^2v_3^2 - 12\omega_7^2cs^2\omega_2^3 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_2 - 12\omega_7\omega_4cs^2\omega_2^3 - 60\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_7\omega_4\omega_3^2v_3^2 + 6\omega_4^3cs^2\omega_2^2 - 24\omega_7\omega_4^2cs^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^2\omega_2^2 + 48\omega_7^2\omega_3^2v_3^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36\omega_7\omega_4^2cs^2\omega_2^2 - 12\omega_7^2\omega_4^3cs^2\omega_2^2 + 6\omega_7^2\omega_4^3cs^2\omega_2 - 24\omega_7^2\omega_4cs^2\omega_2^2 - 30\omega_7^2\omega_4^3\omega_2^2v_3^2 + 40\omega_7^2\omega_4^2\omega_3^3v_3^2 - 12\omega_4^2\omega_3^3v_3^2 + 36\omega_7^2\omega_4cs^2\omega_2^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^2}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM1}} = (-6\omega_7^2\omega_4\omega_3^2v_3^2 + 24\omega_7\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4^3\omega_3^2cs^2 + 12\omega_7^2\omega_4^3v_3^2 - 32\omega_7^2\omega_4^2\omega_3^2cs^2 + 24\omega_7^2\omega_4^3\omega_2^2v_3^2 - 12\omega_4^2\omega_3^2cs^2 + 6\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_2^2cs^2 - 36\omega_7\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4\omega_3^2cs^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 - 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 + 48\omega_7^2\omega_4^2\omega_2^2cs^2 + 6\omega_4^3\omega_3^2cs^2 + 4\omega_7^2\omega_4^3\omega_3^2cs^2 - 36\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_7\omega_4\omega_3^3v_3^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 - 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36\omega_7\omega_4^2\omega_3^2cs^2 - 30\omega_7^2\omega_4^3\omega_2^2v_3^2 + 16\omega_7^2\omega_4^2\omega_3^2v_3^2 - 12\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_4^2\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36\omega_7^2\omega_4\omega_3^2cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM2}} = (-6\omega_7^2\omega_4\omega_3^2v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_3^2cs^2 + 24\omega_7\omega_4^2\omega_2^2v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 24\omega_7^2\omega_4^3\omega_2^2v_3^2 - 12\omega_7^2\omega_4^3\omega_2^2cs^2 - 36\omega_7\omega_4^2\omega_3^2v_3^2 - 24\omega_7^2\omega_4\omega_3^2cs^2 + 36\omega_7\omega_4^3\omega_3^2cs^2 + 6\omega_4^3\omega_3^2cs^2 + 4\omega_7^2\omega_4^3\omega_3^2cs^2 + 24\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 6\omega_4^3\omega_3^2v_3^2 - 5\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4\omega_3^2cs^2 - 36\omega_7^2\omega_4^2\omega_3^3v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 48\omega_7^2\omega_4^2\omega_2^2cs^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4^3\omega_2^2v_3^2 - 30\omega_7^2\omega_4^3\omega_2^2cs^2 - 12\omega_4^2\omega_3^2cs^2 + 16\omega_7^2\omega_4\omega_3^2v_3^2 + 12\omega_4^2\omega_3^2v_3^2 + 6\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4^3\omega_3^2cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_3^2}$$

**coefficient**  $C_{D_x D_y D_z^2 v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2}$ :

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{SRT}} = (132 - 198\omega - 5\omega^3 + 76\omega^2) \frac{v_1v_2\rho v_3}{6\omega^3}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}} = (18\omega_4\omega_2^3\omega_3^2 + 24\omega_4^3\omega_2^2\omega_3^3 - 30\omega_4^3\omega_2^3\omega_3 + 12\omega_2^3\omega_3^3 - 42\omega_4^3\omega_2^2\omega_3^2 - 36\omega_4\omega_2^3\omega_3^3 - 5\omega_4^3\omega_2^3\omega_3^3 + 18\omega_4^3\omega_2^2\omega_3 + 6\omega_4^2\omega_2\omega_3^3 + 12\omega_4^3\omega_2^3 + 18\omega_4\omega_2^2\omega_3^3 + 24\omega_4^3\omega_2^2\omega_3^3 + 12\omega_4^3\omega_2^3\omega_3 + 12\omega_4^2\omega_2^2\omega_3^2 + 6\omega_4^2\omega_2^2\omega_3 - 30\omega_4^2\omega_2^2\omega_3^3 + 18\omega_4^3\omega_2\omega_3^3 - 30\omega_4^2\omega_2^2\omega_3^3 + 28\omega_4^2\omega_2^3\omega_3^3 - 30\omega_4^3\omega_2\omega_3^3) \frac{v_1v_2\rho v_3}{6\omega_4^3\omega_3^3\omega_3^3}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{CLBM1}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_3}^{(0), \text{CLBM2}} = C_{D_x D_y D_z^2 v_3}^{(0), \text{MRT1}}$$

**coefficient**  $C_{D_y^2 D_z^2 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2}$ :

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{SRT}} = (-3\omega^3v_2^2v_3^2 - 24\omega cs^4 + \omega^3cs^2v_3^2 + 36\omega cs^2v_3^2 + 56v_2^2v_3^2 - 24cs^2v_3^2 - 14\omega^2cs^2v_2^2 - 84\omega v_2^2v_3^2 - 24cs^2v_2^2 - \omega^3cs^4 - 14\omega^2cs^2v_3^2 +$$



$$24\omega_7^2\omega_4\omega_3^2v_3^2+24\omega_7^2\omega_4\omega_3v_3^2+6\omega_4^3\omega_3^2v_3^2-4\omega_7^2\omega_4^3\omega_3^2v_3^2+24\omega_7\omega_4^2\omega_3^3cs^2-78\omega_7^2\omega_4\omega_3^3v_3^2-6\omega_7^2\omega_4^3\omega_3^2cs^2+22\omega_7^2\omega_4^3\omega_3^2v_3^2+24\omega_7^2\omega_4\omega_3^3cs^2)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_y^2D_z^2v_2}^{(0),\text{MRT}^2} = (24\omega_7^2\omega_4cs^2\omega_3^3-30\omega_7^2\omega_4^3\omega_3v_3^2+34\omega_7^2\omega_4^2\omega_3^3v_3^2-12\omega_4^2\omega_3^3v_3^2+6\omega_7^2\omega_4^3cs^2\omega_3+12\omega_7^2\omega_4^3v_3^2-6\omega_7\omega_4^3\omega_3^3v_3^2-48\omega_7^2\omega_4^2\omega_3^2v_3^2-12\omega_7\omega_4\omega_3^3v_3^2-6\omega_7^2\omega_4^3cs^2\omega_3^2+24\omega_7\omega_4^2cs^2\omega_3^3+48\omega_7^2\omega_4^3v_3^2+\omega_7^2\omega_4^3cs^2\omega_3^3+6\omega_4^3cs^2\omega_3^3+24\omega_7\omega_4^2\omega_3^3v_3^2+24\omega_7^2\omega_4\omega_3^3v_3^2-12\omega_7^2\omega_4^2cs^2\omega_3-12\omega_7\omega_4cs^2\omega_3^3+24\omega_7^2\omega_4^2\omega_3v_3^2+6\omega_4^3\omega_3^3v_3^2-4\omega_7^2\omega_4^3\omega_3^3v_3^2-12\omega_7^2cs^2\omega_3^3-12\omega_4^2cs^2\omega_3^3-14\omega_7^2\omega_4^2cs^2\omega_3^3-78\omega_7^2\omega_4\omega_3^3v_3^2-6\omega_7\omega_4^3cs^2\omega_3^3+12\omega_7^2\omega_4^2cs^2\omega_3^2+22\omega_7^2\omega_4^3\omega_3^2v_3^2)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_y^2D_z^2v_2}^{(0),\text{CLBM}^1} = (-30\omega_7^2\omega_4^3\omega_3v_3^2+22\omega_7^2\omega_4^2\omega_3^2v_3^2-6\omega_7^2\omega_4^3cs^2\omega_3^2+12\omega_4^2\omega_3^3v_3^2+24\omega_7\omega_4^2cs^2\omega_3^3+12\omega_7^2\omega_4^3v_3^2+\omega_7^2\omega_4^3cs^2\omega_3^3+6\omega_4^3cs^2\omega_3^3+6\omega_7\omega_4^3\omega_3^3v_3^2-48\omega_7^2\omega_4^2\omega_3^2v_3^2+12\omega_7\omega_4\omega_3^3v_3^2+24\omega_7^2\omega_4cs^2\omega_3^3+6\omega_7^2\omega_4^3cs^2\omega_3-12\omega_7^2cs^2\omega_3^3-24\omega_7\omega_4^2\omega_3^3v_3^2-14\omega_7^2\omega_4^2cs^2\omega_3^3+24\omega_7^2\omega_4\omega_3^2v_3^2+24\omega_7^2\omega_4\omega_3v_3^2-6\omega_4^3\omega_3^3v_3^2-6\omega_7\omega_4^3cs^2\omega_3^3-4\omega_7^2\omega_4^3\omega_3^3v_3^2+12\omega_7^2\omega_4^2cs^2\omega_3^2-18\omega_7^2\omega_4\omega_3^3v_3^2-12\omega_7\omega_4cs^2\omega_3^3-12\omega_7^2\omega_4^2cs^2\omega_3+22\omega_7^2\omega_4^3\omega_3^2v_3^2-12\omega_7^2cs^2\omega_3^3)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_y^2D_z^2v_2}^{(0),\text{CLBM}^2} = (-14\omega_7^2\omega_4^2\omega_3^3cs^2-12\omega_7^2\omega_3^3cs^2-30\omega_7^2\omega_4^3\omega_3v_3^2+6\omega_7^2\omega_4^3\omega_3cs^2+22\omega_7^2\omega_4^3\omega_3^2v_3^2+12\omega_4^2\omega_3^3v_3^2+12\omega_7^2\omega_4^3v_3^2+6\omega_7\omega_4^3\omega_3^3v_3^2-6\omega_7\omega_4^3\omega_3^3cs^2-12\omega_7\omega_4\omega_3^3cs^2-48\omega_7^2\omega_4^2\omega_3^2v_3^2+12\omega_7\omega_4\omega_3^3v_3^2+12\omega_7^2\omega_4^2\omega_3^3cs^2-12\omega_7^2\omega_3^3cs^2-24\omega_7\omega_4^2\omega_3^3v_3^2+24\omega_7\omega_4^2\omega_3^3cs^2+24\omega_7^2\omega_4\omega_3^2v_3^2+24\omega_7^2\omega_4\omega_3v_3^2+6\omega_4^3\omega_3^3cs^2+\omega_7^2\omega_4^3\omega_3^3cs^2-6\omega_4^3\omega_3^3v_3^2-4\omega_7^2\omega_4^3\omega_3^3v_3^2-12\omega_7^2\omega_4^2\omega_3cs^2-18\omega_7^2\omega_4\omega_3^3v_3^2+24\omega_7^2\omega_4\omega_3^3cs^2+22\omega_7^2\omega_4^3\omega_3^2v_3^2-6\omega_7^2\omega_4^3\omega_3^2cs^2)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

**coefficient**  $C_{D_y^2D_z^2v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2}$ :

$$C_{D_y^2D_z^2v_3}^{(0),\text{SRT}} = (-26\omega^2cs^2+50\omega^2v_2^2-4\omega^3v_2^2+\omega^3cs^2-48cs^2+84v_2^2+72\omega cs^2-126\omega v_2^2)\frac{\rho v_3}{12\omega^3}$$

$$C_{D_y^2D_z^2v_3}^{(0),\text{MRT}^1} = (-14\omega_4^3\omega_6^2\omega_3^2cs^2-12\omega_4^3v_2^2\omega_3^2-4\omega_4^3v_2^2\omega_6^2\omega_3^3-12\omega_4^3\omega_6\omega_3cs^2+6\omega_4^3v_2^2\omega_3^3+24\omega_4^2v_2^2\omega_6^2\omega_3+34\omega_4^3v_2^2\omega_6^2\omega_3^2-6\omega_4^2\omega_6^2\omega_3^3cs^2-78\omega_4^3v_2^2\omega_6^2\omega_3+ \omega_4^3\omega_6^2\omega_3^3cs^2+48\omega_4^3v_2^2\omega_6^2-48\omega_4^3v_2^2\omega_6^2\omega_3^2+12\omega_4^2\omega_6^2\omega_3^3cs^2-12\omega_4^3\omega_6^2cs^2+22\omega_4^2v_2^2\omega_6^2\omega_3^3+6\omega_4^3\omega_3^3cs^2+12v_2^2\omega_6^2\omega_3^3-6\omega_4^3\omega_6\omega_3^3cs^2+6\omega_4\omega_6^2\omega_3^3cs^2-12\omega_4^3v_2^2\omega_6\omega_3+24\omega_4^3\omega_6\omega_3^2cs^2+24\omega_4v_2^2\omega_6^2\omega_3^2+24\omega_4^2v_2^2\omega_6\omega_3^2-12\omega_4^3\omega_3^2cs^2-30\omega_4v_2^2\omega_6^2\omega_3^3+24\omega_4^2\omega_6^2\omega_3^2cs^2-6\omega_4^3v_2^2\omega_6\omega_3^3-12\omega_4\omega_6^2\omega_3^2cs^2)\frac{\rho v_3}{12\omega_4^3\omega_6^3\omega_3^3}$$

$$C_{D_y^2D_z^2v_3}^{(0),\text{MRT}^2} = (-12\omega_4^3cs^2\omega_6^2-12\omega_4^3v_2^2\omega_3^2-12\omega_4^3cs^2\omega_6\omega_3-4\omega_4^3v_2^2\omega_6^2\omega_3^3+6\omega_4^3v_2^2\omega_3^3+24\omega_4^2v_2^2\omega_6^2\omega_3+34\omega_4^3v_2^2\omega_6^2\omega_3^2-78\omega_4^3v_2^2\omega_6^2\omega_3-6\omega_4^3cs^2\omega_6\omega_3^3+6\omega_4cs^2\omega_6^2\omega_3^3-12\omega_4^3cs^2\omega_3^2+48\omega_4^3v_2^2\omega_6^2-48\omega_4^3v_2^2\omega_6^2\omega_3^2+24\omega_4^2cs^2\omega_6\omega_3^2+22\omega_4^2v_2^2\omega_6^2\omega_3^3-12\omega_4cs^2\omega_6^2\omega_3^3+6\omega_4^3cs^2\omega_3^3-14\omega_4^3cs^2\omega_6^2\omega_3^2+12v_2^2\omega_6^2\omega_3^3+\omega_4^3cs^2\omega_6^2\omega_3^3-12\omega_4^3v_2^2\omega_6\omega_3+24\omega_4v_2^2\omega_6^2\omega_3^2-6\omega_4^3cs^2\omega_6^2\omega_3^3+24\omega_4^2v_2^2\omega_6\omega_3^2+12\omega_4^2cs^2\omega_6^2\omega_3^3-30\omega_4v_2^2\omega_6^2\omega_3^3-6\omega_4^3v_2^2\omega_6\omega_3^3+24\omega_4^3cs^2\omega_6^2\omega_3)\frac{\rho v_3}{12\omega_4^3\omega_6^3\omega_3^3}$$

$$C_{D_y^2D_z^2v_3}^{(0),\text{CLBM}^1} = (12\omega_4^3v_2^2\omega_3^2-14\omega_4^3cs^2\omega_6^2\omega_3^2-4\omega_4^3v_2^2\omega_6^2\omega_3^3-12\omega_4^3cs^2\omega_3^2-6\omega_4^3v_2^2\omega_3^3+24\omega_4^2v_2^2\omega_6^2\omega_3+6\omega_4^3cs^2\omega_3^3+22\omega_4^3v_2^2\omega_6^2\omega_3^2+\omega_4^3cs^2\omega_6^2\omega_3^3-18\omega_4^3v_2^2\omega_6^2\omega_3-12\omega_4^3cs^2\omega_6^2-6\omega_4^3cs^2\omega_6^2\omega_3^3-48\omega_4^3v_2^2\omega_6^2\omega_3^2+24\omega_4^3cs^2\omega_6^2\omega_3+22\omega_4^2v_2^2\omega_6^2\omega_3^3+12\omega_4^3cs^2\omega_6^2\omega_3^2-12\omega_4^3cs^2\omega_6\omega_3+12v_2^2\omega_6^2\omega_3^3+12\omega_4^3v_2^2\omega_6\omega_3+24\omega_4v_2^2\omega_6^2\omega_3^2+6\omega_4cs^2\omega_6^2\omega_3^3-24\omega_4^3v_2^2\omega_6\omega_3^2-6\omega_4^3cs^2\omega_6\omega_3^3-12\omega_4cs^2\omega_6^2\omega_3^3-30\omega_4v_2^2\omega_6^2\omega_3^3+24\omega_4^3cs^2\omega_6\omega_3^2+6\omega_4^3v_2^2\omega_6\omega_3^3)\frac{\rho v_3}{12\omega_4^3\omega_6^3\omega_3^3}$$

$$C_{D_y^2D_z^2v_3}^{(0),\text{CLBM}^2} = (-12\omega_4^3\omega_6\omega_3cs^2+12\omega_4^3v_2^2\omega_3^2-6\omega_4^3\omega_6^2\omega_3^3cs^2-4\omega_4^3v_2^2\omega_6^2\omega_3^3-6\omega_4^3v_2^2\omega_3^3+24\omega_4^2v_2^2\omega_6^2\omega_3-14\omega_4^3\omega_6^2\omega_3^3cs^2+22\omega_4^3v_2^2\omega_6^2\omega_3^2-18\omega_4^3v_2^2\omega_6^2\omega_3+12\omega_4^2\omega_6^2\omega_3^2cs^2-12\omega_4^3\omega_6^2cs^2-48\omega_4^3v_2^2\omega_6^2\omega_3^2+22\omega_4^2v_2^2\omega_6^2\omega_3^3+\omega_4^3\omega_6^2\omega_3^3cs^2+6\omega_4\omega_6^2\omega_3^3cs^2+12v_2^2\omega_6^2\omega_3^3+6\omega_4^3\omega_6\omega_3^3cs^2+24\omega_4v_2^2\omega_6^2\omega_3^2+24\omega_4^3\omega_6^2\omega_3cs^2-24\omega_4^3v_2^2\omega_6\omega_3^2-12\omega_4\omega_6^2\omega_3^2cs^2+24\omega_4^3\omega_6\omega_3^2cs^2-30\omega_4v_2^2\omega_6^2\omega_3^3+6\omega_4^3v_2^2\omega_6\omega_3^3-12\omega_4^3\omega_3^2cs^2)\frac{\rho v_3}{12\omega_4^3\omega_6^3\omega_3^3}$$

**coefficient**  $C_{D_tD_z^3v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial t \partial x_3^3}$ :

$$C_{D_tD_z^3v_3}^{(0),\text{SRT}} = (-36+34\omega^2cs^2-108\omega v_3^2-2\omega^3cs^2+60cs^2+54\omega+\omega^3+72v_3^2-20\omega^2-3\omega^3v_3^2-90\omega cs^2+42\omega^2v_3^2)\frac{\rho}{12\omega^3}$$

$$C_{D_tD_z^3v_3}^{(0),\text{MRT}^1} = (-2\omega_7^2\omega_4^3cs^2+6\omega_4^3+36\omega_7\omega_4^2-12\omega_4^2-3\omega_7^2\omega_4^3v_3^2-9\omega_7\omega_4^3+12\omega_7^2v_3^2+25\omega_7^2\omega_4^2cs^2+48\omega_7\omega_4v_3^2+24\omega_7^2cs^2-24\omega_7\omega_4+27\omega_7^2\omega_4^2v_3^2+24\omega_7\omega_4cs^2-6\omega_4^3cs^2+12\omega_7^2\omega_4-36\omega_7\omega_4^2cs^2-42\omega_7^2\omega_4v_3^2-6\omega_4^3v_3^2-60\omega_7\omega_4^2v_3^2-48\omega_7^2\omega_4cs^2+9\omega_7\omega_4^3cs^2+\omega_7^2\omega_4^3+12\omega_4^2cs^2+15\omega_7\omega_4^3v_3^2+12\omega_4^2v_3^2-11\omega_7^2\omega_4^2)\frac{\rho}{12\omega_7^2\omega_4^3}$$

$$C_{D_tD_z^3v_3}^{(0),\text{MRT}^2} = (24\omega_7^2cs^2+6\omega_4^3+24\omega_7\omega_4cs^2+36\omega_7\omega_4^2-12\omega_4^2-3\omega_7^2\omega_4^3v_3^2-9\omega_7\omega_4^3+25\omega_7^2\omega_4^2cs^2+12\omega_7^2v_3^2+48\omega_7\omega_4v_3^2-2\omega_7^2\omega_4^3cs^2-24\omega_7\omega_4+27\omega_7^2\omega_4^2v_3^2+12\omega_7^2\omega_4-42\omega_7^2\omega_4v_3^2+9\omega_7\omega_4^3cs^2-6\omega_4^3v_3^2-60\omega_7\omega_4^2v_3^2+12\omega_4^2cs^2+\omega_7^2\omega_4^3-48\omega_7^2\omega_4cs^2+15\omega_7\omega_4^3v_3^2-6\omega_4^3cs^2-36\omega_7\omega_4^2cs^2+12\omega_4^2v_3^2-11\omega_7^2\omega_4^2)\frac{\rho}{12\omega_7^2\omega_4^3}$$

$$C_{D_tD_z^3v_3}^{(0),\text{CLBM}^1} = (6\omega_4^3+9\omega_7\omega_4^3cs^2+36\omega_7\omega_4^2+12\omega_4^2cs^2-12\omega_4^2-3\omega_7^2\omega_4^3v_3^2-9\omega_7\omega_4^3-6\omega_4^3cs^2-36\omega_7^2v_3^2-36\omega_7\omega_4^2cs^2+72\omega_7\omega_4v_3^2-24\omega_7\omega_4+15\omega_7^2\omega_4^2v_3^2-48\omega_7^2\omega_4cs^2+12\omega_7^2\omega_4+18\omega_7^2\omega_4v_3^2+25\omega_7^2\omega_4^2cs^2+24\omega_7^2cs^2-18\omega_4^3v_3^2+24\omega_7\omega_4cs^2-108\omega_7\omega_4^2v_3^2-2\omega_7^2\omega_4^3cs^2+\omega_7^2\omega_4^3+27\omega_7\omega_4^3v_3^2+36\omega_4^2v_3^2-11\omega_7^2\omega_4^2)\frac{\rho}{12\omega_7^2\omega_4^3}$$

$$C_{D_tD_z^3v_3}^{(0),\text{CLBM}^2} =$$

$$(6\omega_4^3 + 36\omega_7\omega_4^2 - 2\omega_7^2\omega_3^3cs^2 - 12\omega_4^2 - 3\omega_7^2\omega_4^3v_3^2 - 9\omega_7\omega_4^3 + 24\omega_7^2cs^2 - 36\omega_7^2v_3^2 + 24\omega_7\omega_4cs^2 + 72\omega_7\omega_4v_3^2 - 24\omega_7\omega_4 + 15\omega_7^2\omega_4^2v_3^2 + 25\omega_7^2\omega_4^2cs^2 + 12\omega_7^2\omega_4 + 18\omega_7^2\omega_4v_3^2 - 48\omega_7^2\omega_4cs^2 - 6\omega_4^3cs^2 - 18\omega_4^3v_3^2 - 36\omega_7\omega_4^2cs^2 - 108\omega_7\omega_4^2v_3^2 + \omega_7^3\omega_4^3 + 27\omega_7\omega_4^3v_3^2 + 9\omega_7\omega_4^3cs^2 + 36\omega_4^3v_3^2 + 12\omega_4^3cs^2 - 11\omega_7^2\omega_4^2)\frac{\rho}{12\omega_7^2\omega_4^3}$$

$$\text{coefficient } C_{D_x D_z^3 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 \rho}^{(0), \text{SRT}} = (24 - 72\omega^2cs^2 + 6\omega^3cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2)\frac{v_1v_3}{6\omega^3}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT}1} = (-3\omega_7\omega_4^3\omega_2^2 - 30\omega_7^2\omega_4\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^3\omega_2^2cs^2 + 6\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^3v_3^2 - 12\omega_7\omega_4^2\omega_2^2cs^2 + 6\omega_7^2\omega_4^3\omega_2^2v_3^2 + 78\omega_7^2\omega_4\omega_2^3cs^2 + 6\omega_7\omega_4^3\omega_2^3 + 42\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_4^3\omega_2^3cs^2 + 6\omega_7^2\omega_4^3\omega_2^3cs^2 + 6\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2\omega_4^3\omega_2cs^2 - 6\omega_7^2\omega_4\omega_2^3 + 12\omega_7^2\omega_4\omega_2^2v_3^2 - 21\omega_7\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^2\omega_2^2v_3^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 + 42\omega_7\omega_4^2\omega_2^3cs^2 + 6\omega_4^3\omega_2^3v_3^2 - 3\omega_4^3\omega_2^3 + 12\omega_7\omega_4\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_7\omega_4^3\omega_2^2cs^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4\omega_2^2v_3^2 - 36\omega_7^2\omega_2^3cs^2 - 24\omega_7\omega_4\omega_2^3cs^2 + 24\omega_7^2\omega_2^3v_3^2 + 7\omega_7^2\omega_4^2\omega_2^2 + 42\omega_7^2\omega_4^2\omega_2^2cs^2 + 6\omega_7\omega_4^3\omega_2^2v_3^2 - 12\omega_7^2\omega_4^3\omega_2v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_4^2\omega_2^3v_3^2 + \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^2\omega_2^3cs^2 - 48\omega_7^2\omega_4^2\omega_2^2cs^2 - 12\omega_4^2\omega_2^2cs^2 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^2v_3^2 + 6\omega_7^2\omega_4^3\omega_2cs^2)\frac{v_1v_3}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT}2} = (42\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7\omega_4^3cs^2\omega_2^3 - 3\omega_7\omega_4^3\omega_2^2 - 30\omega_7^2\omega_4\omega_2^3v_3^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 - 48\omega_7^2\omega_4^2cs^2\omega_2^3 + 6\omega_4^2\omega_2^3 + 6\omega_7\omega_4^3cs^2\omega_2^2 - 12\omega_4^2cs^2\omega_2^3 + 6\omega_7^2\omega_4^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2^3v_3^2 + 6\omega_7\omega_4^3\omega_2^3 + 42\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7\omega_4^2\omega_2^2 - 6\omega_7^2\omega_4\omega_2^3 + 12\omega_7^2\omega_4\omega_2^2v_3^2 - 36\omega_7^2cs^2\omega_2^3 - 21\omega_7\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^2\omega_2^2v_3^2 + 6\omega_4^3\omega_2^3v_3^2 - 3\omega_4^3\omega_2^3 - 12\omega_7^2\omega_4^2cs^2\omega_2 - 24\omega_7\omega_4cs^2\omega_2^3 + 12\omega_7\omega_4\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^2v_3^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4\omega_2^2v_3^2 + 6\omega_4^3cs^2\omega_2^3 - 12\omega_7\omega_4^2cs^2\omega_2^3 + 6\omega_7^2\omega_4^3cs^2\omega_2^3 + 24\omega_7^2\omega_2^3v_3^2 + 7\omega_7^2\omega_4^2\omega_2^2 + 6\omega_7\omega_4^3\omega_2^2v_3^2 + 42\omega_7\omega_4^2cs^2\omega_2^3 - 12\omega_7^2\omega_4^3cs^2\omega_2^2 + 6\omega_7^2\omega_4^3cs^2\omega_2 - 24\omega_7^2\omega_4cs^2\omega_2^2 - 12\omega_7^2\omega_4^2\omega_2v_3^2 + 6\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_4^2\omega_2^3v_3^2 + \omega_7^2\omega_4^3\omega_2^2 + 78\omega_7^2\omega_4cs^2\omega_2^3 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^3v_3^2)\frac{v_1v_3}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CLBM}1} = (-3\omega_7\omega_4^3\omega_2^2 + 12\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^3\omega_2^3cs^2 + 6\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^3v_3^2 - 36\omega_7^2\omega_4^3\omega_2^2cs^2 + 6\omega_7^2\omega_4^3\omega_2^2v_3^2 - 36\omega_4^2\omega_2^3cs^2 + 6\omega_7\omega_4^3\omega_2^2 + 6\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_2^2cs^2 + 12\omega_7\omega_4^2\omega_2^3v_3^2 + 6\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2\omega_2^3cs^2 - 6\omega_7^2\omega_4\omega_2^3 + 24\omega_7\omega_4\omega_2^3 - 12\omega_7^2\omega_4^2\omega_2^2v_3^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7\omega_4\omega_2^2v_3^2 + 6\omega_4^3cs^2\omega_2^3 + 7\omega_7^2\omega_4^2\omega_2^2 + 72\omega_7\omega_4^2\omega_2^2cs^2 - 12\omega_7^2\omega_4^3\omega_2v_3^2 - 6\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_4^2\omega_2^3v_3^2 + \omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_2^3cs^2)\frac{v_1v_3}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CLBM}2} = (-3\omega_7\omega_4^3\omega_2^2 + 12\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_2^3cs^2 + 6\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2^2v_3^2 - 12\omega_7^2\omega_4^3\omega_2^2cs^2 + 6\omega_7\omega_4^3\omega_2^2 + 12\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4\omega_2^3 + 72\omega_7\omega_4^2\omega_2^2cs^2 - 6\omega_7^2\omega_4\omega_2^3 + 18\omega_4^3\omega_2^3cs^2 + 6\omega_7^2\omega_4^3\omega_2^2cs^2 - 21\omega_7\omega_4^2\omega_2^3 + 6\omega_7^2\omega_4^2\omega_2^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 6\omega_4^3\omega_2^3v_3^2 - 3\omega_4^3\omega_2^3 - 24\omega_7\omega_4\omega_2^3cs^2 + 12\omega_7\omega_4\omega_2^3 - 6\omega_7^2\omega_4^2\omega_2^2v_3^2 - 3\omega_7^2\omega_4^2\omega_2^2 - 24\omega_7\omega_4\omega_2^2v_3^2 + 36\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_2^2cs^2 + 7\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7^2\omega_2^3cs^2 - 12\omega_7^2\omega_4\omega_2^3v_3^2 - 36\omega_7^2\omega_4^3\omega_2^2cs^2 - 36\omega_4^2\omega_2^3cs^2 - 6\omega_7^2\omega_4^3\omega_2^3v_3^2 + 12\omega_4^2\omega_2^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2cs^2 + \omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 24\omega_7\omega_4^3\omega_2^3cs^2)\frac{v_1v_3}{6\omega_7^2\omega_4^3\omega_2^3}$$

$$\text{coefficient } C_{D_x D_z^3 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_1}^{(0), \text{SRT}} = (36 - 56\omega^2cs^2 + 54\omega v_3^2 + 4\omega^3cs^2 - 96cs^2 - 54\omega - \omega^3 - 36v_3^2 + 20\omega^2 + \omega^3v_3^2 + 144\omega cs^2 - 20\omega^2v_3^2)\frac{\rho v_3}{12\omega^3}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{MRT}1} = (4\omega_7^2\omega_4^3cs^2 - 6\omega_4^3 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 44\omega_7^2\omega_4^2cs^2 - 36\omega_7\omega_4v_3^2 - 48\omega_7^2cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 36\omega_7\omega_4cs^2 + 6\omega_4^3cs^2 - 12\omega_7^2\omega_4 + 48\omega_7\omega_4^2cs^2 + 6\omega_4^3v_3^2 + 48\omega_7\omega_4^2v_3^2 + 90\omega_7^2\omega_4cs^2 - 12\omega_7\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 12\omega_4^2cs^2 - 12\omega_7\omega_4^3v_3^2 - 12\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{MRT}2} = (-48\omega_7^2cs^2 - 6\omega_4^3 - 36\omega_7\omega_4cs^2 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 - 44\omega_7^2\omega_4^2cs^2 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4v_3^2 + 4\omega_7^2\omega_4^3cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 12\omega_7^2\omega_4 - 12\omega_7\omega_4^3cs^2 + 6\omega_4^3v_3^2 + 48\omega_7\omega_4^2v_3^2 - 12\omega_4^2cs^2 - \omega_7^2\omega_4^3 + 90\omega_7^2\omega_4cs^2 - 12\omega_7\omega_4^3v_3^2 + 6\omega_4^3cs^2 + 48\omega_7\omega_4^2cs^2 - 12\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{CLBM}1} = (-6\omega_4^3 - 30\omega_7\omega_4^3cs^2 - 36\omega_7\omega_4^2 - 60\omega_2^2cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 30\omega_4^3cs^2 + 12\omega_7^2v_3^2 + 96\omega_7\omega_4^2cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 + 18\omega_7^2\omega_4cs^2 - 12\omega_7^2\omega_4 + 12\omega_7^2\omega_4v_3^2 - 26\omega_7^2\omega_4^2cs^2 - 6\omega_4^3v_3^2 - 36\omega_7\omega_4cs^2 + 48\omega_7\omega_4^2v_3^2 + 4\omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^3v_3^2 + 12\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{D_x D_z^3 v_1}^{(0), \text{CLBM}2} = (-6\omega_4^3 - 36\omega_7\omega_4^2 + 4\omega_7^2\omega_4^3cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 - 26\omega_7^2\omega_4^2cs^2 - 12\omega_7^2\omega_4 + 12\omega_7^2\omega_4v_3^2 + 18\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 - 6\omega_4^3v_3^2 + 96\omega_7\omega_4^2cs^2 + 48\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^3v_3^2 - 30\omega_7\omega_4^3cs^2 + 12\omega_4^2v_3^2 - 60\omega_4^2cs^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$\text{coefficient } C_{D_x D_z^3 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_3}^{(0), \text{SRT}} = (12 - 56\omega^2cs^2 + 18\omega v_3^2 + 4\omega^3cs^2 - 96cs^2 - 18\omega - \omega^3 - 12v_3^2 + 8\omega^2 + 3\omega^3v_3^2 + 144\omega cs^2 - 12\omega^2v_3^2)\frac{v_1\rho}{12\omega^3}$$

$$C_{D_x D_3^3 v_3}^{(0), \text{MRT}^1} = (-6\omega_7\omega_3\omega_2^3 - 30\omega_7\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4\omega_2^2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_7^2\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7\omega_4\omega_2^3cs^2 + 3\omega_7\omega_4^3\omega_2^3 + 36\omega_7\omega_4^3\omega_2^3v_3^2 + 6\omega_4^3\omega_2^3cs^2 + 4\omega_7^2\omega_4^3\omega_2^3cs^2 + 12\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 - 6\omega_7\omega_4^2\omega_2^3 - 24\omega_7^2\omega_4\omega_2^3cs^2 + 36\omega_7\omega_4^2\omega_2^3cs^2 + 6\omega_4^3\omega_2^3v_3^2 + 3\omega_7^2\omega_4^3\omega_2^3v_3^2 + 12\omega_7^2\omega_4^2\omega_2^2v_3^2 + 12\omega_7\omega_4^3\omega_2^2cs^2 - 6\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7\omega_4\omega_2^3v_3^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4\omega_2^3cs^2 + 24\omega_7^2\omega_3^3v_3^2 + 3\omega_7^2\omega_4^2\omega_2^3 + 48\omega_7^2\omega_4^2\omega_2^3cs^2 + 12\omega_7\omega_4^3\omega_2^2v_3^2 - 18\omega_7^2\omega_4^3\omega_2v_3^2 - 12\omega_4^2\omega_2^3v_3^2 + 2\omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^2cs^2 - 32\omega_7^2\omega_4^2\omega_2^3cs^2 - 12\omega_4^2\omega_2^2cs^2 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^3v_3^2 + 6\omega_7^2\omega_4^3\omega_2cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_2^3 v_3}^{(0), \text{MRT}^2} = (48\omega_7^2\omega_4^2cs^2\omega_2^2 - 12\omega_7\omega_4^3cs^2\omega_2^3 - 6\omega_7\omega_4^3\omega_2^2 - 30\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2v_3^2 - 32\omega_7^2\omega_4^2cs^2\omega_2^3 + 12\omega_7\omega_4^3cs^2\omega_2^2 - 12\omega_4^2cs^2\omega_2^3 + 12\omega_7^2\omega_4^3v_3^2 + 3\omega_7\omega_4^3\omega_2^3 + 36\omega_7\omega_4^2\omega_2^3v_3^2 + 12\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2cs^2\omega_2^3 - 6\omega_7\omega_4^2\omega_2^3 + 6\omega_4^3\omega_2^3v_3^2 + 3\omega_7^2\omega_4^3\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_2 - 12\omega_7\omega_4cs^2\omega_2^3 + 12\omega_7^2\omega_4^2\omega_2^2v_3^2 - 6\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7\omega_4\omega_2^3v_3^2 + 6\omega_4^3cs^2\omega_2^3 - 24\omega_7\omega_4^2cs^2\omega_2^2 + 4\omega_7^2\omega_4^3cs^2\omega_2^3 + 24\omega_7^2\omega_2^3v_3^2 + 3\omega_7^2\omega_4^2\omega_2^3 + 12\omega_7\omega_4^2\omega_2^2v_3^2 + 36\omega_7\omega_4^2cs^2\omega_2^3 - 12\omega_7^2\omega_4^3cs^2\omega_2^2 + 6\omega_7^2\omega_4^3cs^2\omega_2 - 24\omega_7\omega_4cs^2\omega_2^2 - 18\omega_7^2\omega_4^2\omega_2v_3^2 - 12\omega_4^2\omega_2^3v_3^2 + 2\omega_7^2\omega_4^3\omega_2^2 + 36\omega_7^2\omega_4cs^2\omega_2^3 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^3v_3^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_3^3 v_3}^{(0), \text{CLBM}^1} = (-6\omega_7\omega_3^3\omega_2^2 + 30\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2v_3^2 - 12\omega_7\omega_4^3\omega_2^3cs^2 + 12\omega_7^2\omega_4^3v_3^2 - 32\omega_7^2\omega_4^2\omega_2^3cs^2 - 12\omega_4^2\omega_2^3cs^2 + 3\omega_7\omega_3^3\omega_2^2 + 6\omega_7^2\omega_4^3\omega_2^2cs^2 + 12\omega_7\omega_4^3\omega_2^2cs^2 - 12\omega_7\omega_4^2\omega_2^3v_3^2 + 12\omega_7\omega_4^2\omega_2^2 - 12\omega_7^2\omega_2^3cs^2 - 12\omega_7\omega_4\omega_2^3cs^2 - 6\omega_7\omega_4^2\omega_2^3 - 6\omega_4^3\omega_2^3v_3^2 + 3\omega_7^2\omega_4^3\omega_2^3v_3^2 + 48\omega_7^2\omega_4^2\omega_2^3cs^2 + 6\omega_4^3\omega_2^3cs^2 + 4\omega_7^2\omega_4^3\omega_2^3cs^2 + 12\omega_7^2\omega_4^2\omega_2^2v_3^2 - 6\omega_7^2\omega_4^2\omega_2^2 - 12\omega_7^2\omega_4^2cs^2 + 12\omega_7\omega_4\omega_2^3v_3^2 - 24\omega_7^2\omega_4\omega_2^3cs^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 - 24\omega_7^2\omega_4\omega_2^3cs^2 - 12\omega_7\omega_4^3\omega_2^2v_3^2 + 3\omega_7^2\omega_4^2\omega_2^3 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36\omega_7\omega_4^3\omega_2^2cs^2 - 18\omega_7^2\omega_4^3\omega_2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_4^2\omega_2^3v_3^2 + 2\omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_2^3cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^3}$$

$$C_{D_x D_3^3 v_3}^{(0), \text{CLBM}^2} = (-6\omega_7\omega_3^3\omega_2^2 + 30\omega_7^2\omega_4\omega_2^3v_3^2 - 24\omega_7\omega_4^2\omega_2^2cs^2 + 36\omega_7^2\omega_4\omega_2^3cs^2 - 24\omega_7\omega_4^2\omega_2^2v_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3cs^2 + 3\omega_7\omega_4^3\omega_2^3 - 12\omega_7\omega_4^3\omega_2^3v_3^2 - 24\omega_7^2\omega_4\omega_2^3cs^2 + 12\omega_7\omega_4^2\omega_2^2 + 36\omega_7\omega_4^2\omega_2^3cs^2 + 6\omega_4^3\omega_2^3cs^2 + 4\omega_7^2\omega_4^3\omega_2^3cs^2 - 6\omega_7\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_7\omega_4\omega_2^3v_3^2 - 24\omega_7^2\omega_4\omega_2^3cs^2 - 24\omega_7^2\omega_4\omega_2^2cs^2 - 24\omega_7^2\omega_4\omega_2^3cs^2 - 12\omega_7\omega_4^3\omega_2^2v_3^2 + 3\omega_7^2\omega_4^2\omega_2^3 + 12\omega_7\omega_4^3\omega_2^2v_3^2 + 36\omega_7\omega_4^3\omega_2^2cs^2 - 18\omega_7^2\omega_4^3\omega_2v_3^2 - 12\omega_7^2\omega_4^2\omega_2^3v_3^2 - 12\omega_7^2\omega_4^2\omega_2^2cs^2 + 12\omega_4^2\omega_2^3v_3^2 + 2\omega_7^2\omega_4^3\omega_2^2 - \omega_7^2\omega_4^3\omega_2^2 - 12\omega_7\omega_4^3\omega_2^3cs^2) \frac{v_1\rho}{12\omega_7^2\omega_4^3\omega_2^3}$$

**coefficient**  $C_{D_y D_2^3 \rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_2 \partial x_3^3}$ :

$$C_{D_y D_2^3 \rho}^{(0), \text{SRT}} = (24 - 72\omega^2cs^2 + 6\omega^3cs^2 - 120cs^2 - 36\omega - \omega^3 + 14\omega^2 + 180\omega cs^2) \frac{v_2v_3}{6\omega^3}$$

$$C_{D_y D_2^3 \rho}^{(0), \text{MRT}^1} = (-\omega_7^2\omega_4^3\omega_3^3 - 12\omega_7^2\omega_3^3\omega_3v_3^2 - 12\omega_7\omega_4^3\omega_3^3cs^2 + 6\omega_7^2\omega_2^3\omega_3^3v_3^2 - 12\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_4^3v_3^2 - 12\omega_7\omega_3^3\omega_3^3v_3^2 - 48\omega_7^2\omega_2^3\omega_3^3cs^2 - 12\omega_7^2\omega_3^3cs^2 + \omega_7^2\omega_3^3\omega_3^2 + 6\omega_7^2\omega_3^3\omega_3cs^2 + 6\omega_7\omega_4^3\omega_3^3cs^2 - 12\omega_7^2\omega_4^3\omega_3^2v_3^2 - 24\omega_7\omega_4\omega_3^3v_3^2 + 7\omega_7^2\omega_4^3\omega_3^3 - 36\omega_7^2\omega_3^3cs^2 + 12\omega_7\omega_4\omega_3^3 - 24\omega_7\omega_4\omega_3^3cs^2 + 24\omega_7^2\omega_3^3v_3^2 - 3\omega_7^2\omega_4^3\omega_3^2 + 6\omega_7\omega_4^3\omega_3^2v_3^2 + 42\omega_7^2\omega_4^3\omega_3^2cs^2 + 6\omega_4^3\omega_3^3cs^2 + 6\omega_7^2\omega_4^3\omega_3^3cs^2 + 42\omega_7\omega_4^3\omega_3^3v_3^2 - 21\omega_7\omega_4^3\omega_3^3 - 12\omega_7^2\omega_4^3\omega_3cs^2 + 12\omega_7^2\omega_4\omega_3^2v_3^2 - 3\omega_4^3\omega_3^3 + 6\omega_7^2\omega_4^3\omega_3v_3^2 - 24\omega_7^2\omega_4\omega_3^2cs^2 + 6\omega_4^3\omega_3^3v_3^2 + 6\omega_7\omega_4^3\omega_3^2 - 6\omega_7^2\omega_4\omega_3^3 + 42\omega_7\omega_4^3\omega_3^3cs^2 + 6\omega_4^3\omega_3^3 - 30\omega_7^2\omega_4\omega_3^3v_3^2 - 12\omega_7^2\omega_4^3\omega_3^2cs^2 + 6\omega_7\omega_4^3\omega_3^3 - 12\omega_7\omega_4^2\omega_3^2v_3^2 - 3\omega_7\omega_4^3\omega_3^2 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7\omega_4^2\omega_3^2cs^2 + 78\omega_7^2\omega_4\omega_3^3cs^2) \frac{v_2v_3}{6\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_y D_3^3 \rho}^{(0), \text{MRT}^2} = (78\omega_7^2\omega_4cs^2\omega_3^3 - \omega_7^2\omega_3^3\omega_3^2 - 12\omega_7^2\omega_4^3\omega_3v_3^2 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3 - 24\omega_7\omega_4cs^2\omega_3^2 + 6\omega_7^2\omega_4^3v_3^2 - 12\omega_7\omega_4^3\omega_3^2v_3^2 + \omega_7^2\omega_3^3\omega_3^2 - 12\omega_7^2\omega_4^3\omega_3^2v_3^2 - 24\omega_7\omega_4\omega_3^3v_3^2 + 7\omega_7^2\omega_4^3\omega_3^3 - 12\omega_7^2\omega_4^3cs^2\omega_3^2 + 42\omega_7\omega_4^3cs^2\omega_3^2 + 12\omega_7\omega_4\omega_3^3 + 24\omega_7^2\omega_4^3v_3^2 - 3\omega_7^2\omega_4^3\omega_3^2 + 6\omega_7\omega_4^3\omega_3^2v_3^2 + 42\omega_7^2\omega_4^3\omega_3^2cs^2 + 6\omega_4^3\omega_3^3cs^2 + 6\omega_7^2\omega_4^3\omega_3^3cs^2 + 42\omega_7\omega_4^3\omega_3^3v_3^2 - 21\omega_7\omega_4^3\omega_3^3 - 12\omega_7^2\omega_4^3\omega_3cs^2 + 12\omega_7^2\omega_4\omega_3^2v_3^2 - 3\omega_4^3\omega_3^3 + 6\omega_7^2\omega_4^3\omega_3v_3^2 - 24\omega_7^2\omega_4\omega_3^2cs^2 + 6\omega_4^3\omega_3^3v_3^2 + 6\omega_7\omega_4^3\omega_3^2 - 6\omega_7^2\omega_4\omega_3^3 + 42\omega_7\omega_4^3\omega_3^3cs^2 + 6\omega_4^3\omega_3^3 - 30\omega_7^2\omega_4\omega_3^3v_3^2 + 6\omega_7\omega_4^3\omega_3^3 - 12\omega_7\omega_4^2\omega_3^2v_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^2 + 42\omega_7^2\omega_4cs^2\omega_3^2 - 3\omega_7\omega_4^3\omega_3^2 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2) \frac{v_2v_3}{6\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_y D_2^3 \rho}^{(0), \text{CLBM}^1} = (-\omega_7^2\omega_4^3\omega_3^3 - 12\omega_7^2\omega_4^3\omega_3v_3^2 - 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_3^3cs^2\omega_3^2 + 12\omega_4^3\omega_3^3v_3^2 + 72\omega_7\omega_4^2cs^2\omega_3^2 + 6\omega_7^2\omega_4^3v_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3^2 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 18\omega_4^3cs^2\omega_3^2 + \omega_7^2\omega_3^3\omega_3^2 - 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 24\omega_7\omega_4\omega_3^3v_3^2 + 7\omega_7^2\omega_4^3\omega_3^3 + 36\omega_7^2\omega_4cs^2\omega_3^2 + 12\omega_7\omega_4\omega_3^3 - 3\omega_7^2\omega_4^3\omega_3^2 - 12\omega_7^2\omega_4cs^2\omega_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3 - 36\omega_4^3cs^2\omega_3^2 + 12\omega_7\omega_4^3cs^2\omega_3^2 + 12\omega_7\omega_4^2\omega_3^2v_3^2 - 21\omega_7\omega_4^3\omega_3^2 - 36\omega_7^2\omega_4cs^2\omega_3^2 - 3\omega_4^3\omega_3^3 + 6\omega_7^2\omega_4\omega_3^2v_3^2 - 6\omega_4^3\omega_3^3v_3^2 - 24\omega_7\omega_4^3cs^2\omega_3^2 + 6\omega_7\omega_4^2\omega_3^2 + 36\omega_7^2\omega_4cs^2\omega_3^2 - 6\omega_7^2\omega_4\omega_3^3 + 6\omega_4^3\omega_3^3 + 12\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4cs^2\omega_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3 + 6\omega_7\omega_4\omega_3^3 - 3\omega_7\omega_4^3\omega_3^2 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2cs^2\omega_3^2) \frac{v_2v_3}{6\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{D_y D_2^3 \rho}^{(0), \text{CLBM}^2} = (-\omega_7^2\omega_4^3\omega_3^3 - 36\omega_7^2\omega_4^3\omega_3cs^2 - 36\omega_4^3\omega_3^3cs^2 - 12\omega_7^2\omega_4^3\omega_3v_3^2 + 6\omega_7^2\omega_4^3\omega_3cs^2 - 6\omega_7^2\omega_4^3\omega_3^2v_3^2 + 12\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_3^3v_3^2 + \omega_7^2\omega_3^3\omega_3^2 - 24\omega_7\omega_4\omega_3^3cs^2 - 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 24\omega_7\omega_4\omega_3^3v_3^2 + 36\omega_7^2\omega_4^3\omega_3^2cs^2 + 7\omega_7^2\omega_4^3\omega_3^3 + 12\omega_7\omega_4\omega_3^3 + 12\omega_7\omega_4^3\omega_3^2cs^2 - 3\omega_7^2\omega_4^3\omega_3^2 - 12\omega_7^2\omega_3^3cs^2 + 12\omega_7\omega_4^3\omega_3^2v_3^2 - 21\omega_7\omega_4^3\omega_3^2 - 12\omega_7^2\omega_4\omega_3^2cs^2 + 72\omega_7\omega_4^2\omega_3^2cs^2 - 3\omega_4^3\omega_3^3 + 6\omega_7^2\omega_4\omega_3^2v_3^2 + 18\omega_4^3\omega_3^3cs^2 + 6\omega_7^2\omega_4^3\omega_3^2cs^2 - 6\omega_4^3\omega_3^3v_3^2 + 6\omega_7\omega_4^2\omega_3^2 - 12\omega_7^2\omega_4\omega_3^2cs^2 - 6\omega_7^2\omega_4\omega_3^3 + 6\omega_4^3\omega_3^3 + 12\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4\omega_3^2cs^2 + 36\omega_7^2\omega_4\omega_3^3cs^2 + 6\omega_7\omega_4^3\omega_3^2 - 3\omega_7\omega_4^3\omega_3^2 + 6\omega_7^2\omega_4^3\omega_3^2v_3^2 - 12\omega_7^2\omega_4^2\omega_3^2cs^2) \frac{v_2v_3}{6\omega_7^2\omega_4^3\omega_3^3}$$

**coefficient**  $C_{D_y D_2^3 v_2}^{(0)}$  **at**  $\frac{\partial^4 v_2}{\partial x_2 \partial x_3^3}$ :

$$C_{D_y D_2^3 v_2}^{(0), \text{SRT}} = (36 - 56\omega^2cs^2 + 54\omega v_3^2 + 4\omega^3cs^2 - 96cs^2 - 54\omega - \omega^3 - 36v_3^2 + 20\omega^2 + \omega^3v_3^2 + 144\omega cs^2 - 20\omega^2v_3^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{D_y D_3^3 v_2}^{(0), \text{MRT}^1} = (4\omega_7^2\omega_4^3cs^2 - 6\omega_4^3 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_3^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 44\omega_7^2\omega_4^2cs^2 - 36\omega_7\omega_4v_3^2 - 48\omega_7^2cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 36\omega_7\omega_4cs^2 + 6\omega_4^3cs^2 - 12\omega_7^2\omega_4 + 48\omega_7\omega_4^2cs^2 + 6\omega_4^3v_3^2 + 48\omega_7\omega_4^2v_3^2 + 90\omega_7^2\omega_4cs^2 - 12\omega_7\omega_4^2cs^2 - \omega_7^2\omega_4^3 - 12\omega_4^2cs^2 - 12\omega_7\omega_4^3v_3^2 - 12\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\text{DyD}_2^3v_2}^{(0),\text{MRT}^2} = (-48\omega_7^2cs^2 - 6\omega_4^3 - 36\omega_7\omega_4cs^2 - 36\omega_7\omega_4^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 - 44\omega_7^2\omega_4^2cs^2 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4v_3^2 + 4\omega_7^2\omega_4^3cs^2 + 24\omega_7\omega_4 - 8\omega_7^2\omega_4^2v_3^2 - 12\omega_7^2\omega_4 - 12\omega_7\omega_4^3cs^2 + 6\omega_4^3v_3^2 + 48\omega_7\omega_4^2v_3^2 - 12\omega_4^2cs^2 - \omega_7^2\omega_4^3 + 90\omega_7^2\omega_4cs^2 - 12\omega_7\omega_4^3v_3^2 + 6\omega_4^3cs^2 + 48\omega_7\omega_4^2cs^2 - 12\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\text{DyD}_2^3v_2}^{(0),\text{CLBM}^1} = (-6\omega_4^3 - 30\omega_7\omega_4^3cs^2 - 36\omega_7\omega_4^2 - 60\omega_4^2cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 30\omega_4^3cs^2 + 12\omega_7^2v_3^2 + 96\omega_7\omega_4^2cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 + 18\omega_7^2\omega_4cs^2 - 12\omega_7^2\omega_4 + 12\omega_7^2\omega_4v_3^2 - 26\omega_7^2\omega_4^2cs^2 - 6\omega_4^3v_3^2 - 36\omega_7\omega_4cs^2 + 48\omega_7\omega_4^2v_3^2 + 4\omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^2v_3^2 + 12\omega_4^2v_3^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\text{DyD}_2^3v_2}^{(0),\text{CLBM}^2} = (-6\omega_4^3 - 36\omega_7\omega_4^2 + 4\omega_7^2\omega_4^3cs^2 + 12\omega_4^2 + \omega_7^2\omega_4^3v_3^2 + 9\omega_7\omega_4^3 + 12\omega_7^2v_3^2 - 36\omega_7\omega_4cs^2 - 60\omega_7\omega_4v_3^2 + 24\omega_7\omega_4 - 14\omega_7^2\omega_4^2v_3^2 - 26\omega_7^2\omega_4^2cs^2 - 12\omega_7^2\omega_4 + 12\omega_7^2\omega_4v_3^2 + 18\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 - 6\omega_4^3v_3^2 + 96\omega_7\omega_4^2cs^2 + 48\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 - 6\omega_7\omega_4^2v_3^2 - 30\omega_7\omega_4^3cs^2 + 12\omega_4^2v_3^2 - 60\omega_4^2cs^2 + 11\omega_7^2\omega_4^2)\frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

**coefficient**  $C_{\text{DyD}_2^3v_3}^{(0)}$  **at**  $\frac{\partial^4 v_3}{\partial x_2 \partial x_3^3}$ :

$$C_{\text{DyD}_2^3v_3}^{(0),\text{SRT}} = (12 - 56\omega^2cs^2 + 18\omega v_3^2 + 4\omega^3cs^2 - 96cs^2 - 18\omega - \omega^3 - 12v_3^2 + 8\omega^2 + 3\omega^3v_3^2 + 144\omega cs^2 - 12\omega^2v_3^2)\frac{v_2\rho}{12\omega^3}$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{MRT}^1} = (-\omega_7^2\omega_4^3\omega_3^3 - 18\omega_7^2\omega_3^3v_3^2 - 12\omega_7\omega_4^3\omega_3^3cs^2 - 12\omega_4^2\omega_3^3v_3^2 + 12\omega_7^2\omega_3^3v_3^2 - 12\omega_7\omega_4^3\omega_3^3v_3^2 - 32\omega_7^2\omega_4^3\omega_3^3cs^2 - 12\omega_4^2\omega_3^3cs^2 + 2\omega_7^2\omega_3^3\omega_3^2 + 6\omega_7^2\omega_4^3\omega_3^3cs^2 + 12\omega_7\omega_3^3\omega_3^3cs^2 + 12\omega_7^2\omega_3^3v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 3\omega_7^2\omega_3^3\omega_3^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4\omega_3^3cs^2 + 24\omega_7^2\omega_3^3v_3^2 - 6\omega_7^2\omega_4^3\omega_3^2 + 12\omega_7\omega_3^3\omega_3^3v_3^2 + 48\omega_7^2\omega_4^3\omega_3^3cs^2 + 6\omega_4^3\omega_3^3cs^2 + 4\omega_7^2\omega_4^3\omega_3^3cs^2 + 36\omega_7\omega_4^3\omega_3^3v_3^2 - 6\omega_7\omega_4^2\omega_3^3 - 12\omega_7^2\omega_4^3\omega_3^3cs^2 - 24\omega_7^2\omega_4\omega_3^3cs^2 + 6\omega_4^3\omega_3^3v_3^2 + 3\omega_7^2\omega_4^3\omega_3^3v_3^2 + 12\omega_7\omega_4^3\omega_3^3cs^2 + 36\omega_7\omega_4^3\omega_3^3cs^2 - 30\omega_7^2\omega_4\omega_3^3v_3^2 - 12\omega_7^2\omega_4^3\omega_3^3cs^2 + 3\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4^2\omega_3^3v_3^2 - 6\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4^3\omega_3^3cs^2 + 36\omega_7^2\omega_4\omega_3^3cs^2)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{MRT}^2} = (36\omega_7^2\omega_4cs^2\omega_3^3 - \omega_7^2\omega_4^3\omega_3^3 - 18\omega_7^2\omega_4^3\omega_3^3v_3^2 - 12\omega_4^2\omega_3^3v_3^2 + 6\omega_7^2\omega_3^3cs^2\omega_3 - 24\omega_7^2\omega_4cs^2\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2 - 12\omega_7\omega_3^3\omega_3^3v_3^2 + 2\omega_7^2\omega_3^3\omega_3^2 + 12\omega_7^2\omega_4^3\omega_3^3v_3^2 - 12\omega_7\omega_4\omega_3^3v_3^2 + 3\omega_7^2\omega_4^3\omega_3^3 - 12\omega_7^2\omega_4^3cs^2\omega_3^2 + 36\omega_7\omega_4^3cs^2\omega_3^3 + 24\omega_7^2\omega_3^3v_3^2 - 6\omega_7^2\omega_4^3\omega_3^2 + 12\omega_7\omega_4^3\omega_3^3v_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^3 + 6\omega_4^3cs^2\omega_3^3 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 36\omega_7\omega_4^3\omega_3^3v_3^2 - 6\omega_7\omega_4^2\omega_3^3 - 12\omega_7^2\omega_4^2cs^2\omega_3 - 12\omega_7\omega_4cs^2\omega_3^3 + 6\omega_4^3\omega_3^3v_3^2 + 3\omega_7^2\omega_4^3\omega_3^3v_3^2 + 12\omega_7\omega_4^2\omega_3^3 - 12\omega_7^2cs^2\omega_3^3 + 12\omega_7\omega_4^3cs^2\omega_3^2 - 12\omega_4^2cs^2\omega_3^3 - 32\omega_7^2\omega_4^2cs^2\omega_3^3 - 30\omega_7^2\omega_4\omega_3^3v_3^2 + 3\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4^2\omega_3^3v_3^2 - 12\omega_7\omega_4^3cs^2\omega_3^3 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 - 6\omega_7\omega_4^3\omega_3^2)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{CLBM}^1} = (-\omega_7^2\omega_4^3\omega_3^3 - 18\omega_7^2\omega_4^3\omega_3^3v_3^2 - 12\omega_7^2\omega_4^3\omega_3^3v_3^2 - 12\omega_7^2\omega_4^3cs^2\omega_3^2 + 12\omega_4^2\omega_3^3v_3^2 + 36\omega_7\omega_4^2cs^2\omega_3^3 + 12\omega_7^2\omega_3^3v_3^2 + 4\omega_7^2\omega_4^3cs^2\omega_3^3 - 24\omega_7\omega_4^2cs^2\omega_3^2 + 6\omega_4^3cs^2\omega_3^3 + 2\omega_7^2\omega_4^3\omega_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 3\omega_7^2\omega_4^3\omega_3^2 + 36\omega_7^2\omega_4cs^2\omega_3^3 - 24\omega_7^2\omega_3^3v_3^2 - 6\omega_7^2\omega_4^3\omega_3^2 - 24\omega_7^2\omega_4cs^2\omega_3^2 + 12\omega_7\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_4^3cs^2\omega_3 - 12\omega_7\omega_4^3cs^2\omega_3^2 + 12\omega_7\omega_4^3\omega_3^3v_3^2 + 48\omega_7^2\omega_4^2cs^2\omega_3^2 + 30\omega_7^2\omega_4\omega_3^3v_3^2 - 12\omega_7\omega_4cs^2\omega_3^3 - 12\omega_7^2\omega_4^2cs^2\omega_3 + 3\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4^2\omega_3^3v_3^2 - 6\omega_7\omega_4^3\omega_3^2 - 12\omega_7^2cs^2\omega_3^3)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

$$C_{\text{DyD}_2^3v_3}^{(0),\text{CLBM}^2} = (-\omega_7^2\omega_4^3\omega_3^3 - 32\omega_7^2\omega_4^3\omega_3^3cs^2 - 12\omega_4^2\omega_3^3cs^2 - 18\omega_7^2\omega_4^3\omega_3^3v_3^2 + 6\omega_7^2\omega_3^3\omega_3^3cs^2 - 12\omega_7^2\omega_4^3\omega_3^3v_3^2 + 12\omega_4^2\omega_3^3v_3^2 + 12\omega_7^2\omega_4^3v_3^2 + 2\omega_7^2\omega_3^3\omega_3^2 - 12\omega_7\omega_4^3\omega_3^3cs^2 - 12\omega_7\omega_4\omega_3^3cs^2 + 12\omega_7^2\omega_4^3\omega_3^3v_3^2 + 12\omega_7\omega_4\omega_3^3v_3^2 + 48\omega_7^2\omega_4^3\omega_3^3cs^2 + 3\omega_7^2\omega_4^3\omega_3^3 - 24\omega_7^2\omega_3^3v_3^2 + 12\omega_7\omega_4^3\omega_3^3cs^2 - 6\omega_7^2\omega_4^3\omega_3^2 + 12\omega_7\omega_4^3\omega_3^3v_3^2 - 12\omega_7^2\omega_3^3cs^2 - 12\omega_7\omega_4^3\omega_3^3v_3^2 - 6\omega_7\omega_4^3\omega_3^2 - 24\omega_7\omega_4^2\omega_3^3cs^2 + 36\omega_7\omega_4^3\omega_3^3cs^2 + 6\omega_4^3\omega_3^3cs^2 + 4\omega_7^2\omega_4^3\omega_3^3cs^2 - 6\omega_4^3\omega_3^3v_3^2 + 3\omega_7^2\omega_4^3\omega_3^3v_3^2 + 12\omega_7\omega_4^3\omega_3^3cs^2 - 12\omega_7^2\omega_4^3\omega_3^3cs^2 + 30\omega_7^2\omega_4\omega_3^3v_3^2 - 24\omega_7\omega_4^2\omega_3^3cs^2 + 36\omega_7^2\omega_4\omega_3^3cs^2 + 3\omega_7\omega_4^3\omega_3^3 - 24\omega_7\omega_4^2\omega_3^3v_3^2 - 6\omega_7\omega_4^3\omega_3^2 - 12\omega_7^2\omega_4^3\omega_3^3cs^2)\frac{v_2\rho}{12\omega_7^2\omega_4^3\omega_3^3}$$

**coefficient**  $C_{\text{D}_2^4\rho}^{(0)}$  **at**  $\frac{\partial^4 \rho}{\partial x_3^4}$ :

$$C_{\text{D}_2^4\rho}^{(0),\text{SRT}} = (-14\omega^2cs^2 - 108\omega v_3^2 - 42\omega^2v_3^4 - 72\omega cs^4 + 6\omega^3cs^2v_3^2 + 216\omega cs^2v_3^2 - 72v_3^4 + \omega^3cs^2 - 144cs^2v_3^2 - 24cs^2 + 3\omega^3v_3^4 - 3\omega^3cs^4 - 84\omega^2cs^2v_3^2 + 72v_3^2 - 3\omega^3v_3^2 + 48cs^4 + 108\omega v_3^4 + 30\omega^2cs^4 + 36\omega cs^2 + 42\omega^2v_3^2)\frac{1}{24\omega^3}$$

$$C_{\text{D}_2^4\rho}^{(0),\text{MRT}^1} = (\omega_7^2\omega_4^3cs^2 + 6\omega_7\omega_4^3cs^4 - 24\omega_7\omega_4v_3^2cs^2 - 24\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3v_3^2 - 18\omega_7\omega_4^3v_3^4 - 96\omega_7^2v_3^2cs^2 - 24\omega_7\omega_4^2cs^4 + 24\omega_7^2\omega_4v_3^4 - 72\omega_7^2\omega_4v_3^3cs^2 - 24\omega_4^2v_3^3cs^2 - 8\omega_7^2\omega_4^2cs^2 + 48\omega_7\omega_4v_3^3 - 12\omega_7\omega_4^3v_3^3cs^2 + 72\omega_7\omega_4^2v_3^4 - 48\omega_7^2\omega_4cs^4 + 24\omega_7^2\omega_4^2v_3^3 - 24\omega_7\omega_4cs^2 + 12\omega_4^3v_3^4 + 156\omega_7^2\omega_4v_3^2cs^2 + 24\omega_7^2\omega_4^2cs^4 - 48\omega_7\omega_4v_3^4 + 24\omega_7\omega_4^2cs^2 - 24\omega_7^2\omega_4v_3^2 - 24\omega_7^2\omega_4^2v_3^4 + 24\omega_7\omega_4^3v_3^4 + 24\omega_7\omega_4cs^4 - 12\omega_4^3v_3^2 + 24\omega_7^2cs^4 - 72\omega_7\omega_4^2v_3^3 + 12\omega_7^2\omega_4cs^2 - 6\omega_7\omega_4^3cs^2 + 48\omega_7\omega_4^2v_3^3cs^2 - 3\omega_7^2\omega_4^3cs^4 + 18\omega_7\omega_4^3v_3^2 + 24\omega_4^2v_3^2 + 12\omega_4^3v_3^2cs^2 + 6\omega_7^2\omega_4^3v_3^2cs^2 + 3\omega_7^2\omega_4^3v_3^4)\frac{1}{24\omega_7^2\omega_4^3}$$

$$C_{\text{D}_2^4\rho}^{(0),\text{MRT}^2} = (-48\omega_7^2\omega_4cs^4 - 24\omega_7\omega_4cs^2 - 24\omega_7\omega_4^2cs^4 - 24\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3v_3^2 - 18\omega_7\omega_4^3v_3^4 + 156\omega_7^2\omega_4cs^2v_3^2 - 8\omega_7^2\omega_4^2cs^2 + 12\omega_4^3cs^2v_3^2 + 6\omega_7^2\omega_4^3cs^2v_3^2 + 24\omega_7^2\omega_4v_3^4 + 48\omega_7\omega_4v_3^3 + \omega_7^2\omega_4^3cs^2 + 72\omega_7\omega_4^2v_3^4 + 48\omega_7\omega_4^2cs^2v_3^2 + 24\omega_7^2\omega_4^2v_3^3 + 6\omega_7\omega_4^3cs^4 + 12\omega_4^3v_3^4 - 96\omega_7^2cs^2v_3^2 - 48\omega_7\omega_4v_3^4 - 24\omega_7^2\omega_4v_3^3 - 24\omega_7\omega_4cs^2v_3^2 - 24\omega_7^2\omega_4^2v_3^4 - 6\omega_7\omega_4^3cs^2 - 12\omega_4^3v_3^2 - 3\omega_7^2\omega_4^3cs^4 - 72\omega_7\omega_4^2v_3^2 + 24\omega_7\omega_4cs^4 + 24\omega_7^2cs^4 + 12\omega_7^2\omega_4cs^2 - 12\omega_7\omega_4^3cs^2v_3^2 + 18\omega_7\omega_4^3v_3^2 + 24\omega_7^2\omega_4^2cs^4 + 24\omega_7\omega_4^2cs^2 - 72\omega_7^2\omega_4^2cs^2v_3^2 + 24\omega_4^2v_3^3 - 24\omega_4^2cs^2v_3^2 + 3\omega_7^2\omega_4^3v_3^4)\frac{1}{24\omega_7^2\omega_4^3}$$

$$C_{\text{D}_2^4\rho}^{(0),\text{CLBM}^1} = (108\omega_4^3cs^2v_3^2 + 6\omega_7^2\omega_4^3cs^2v_3^2 - 6\omega_7\omega_4^3cs^2 - 3\omega_7^2\omega_4^3cs^4 + 144\omega_7\omega_4^2cs^2v_3^2 - 72\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^3v_3^4 + 24\omega_7^2\omega_4^2cs^4 + 24\omega_7\omega_4^2cs^2 + 24\omega_7\omega_4cs^4 + 72\omega_7\omega_4^2v_3^4 - 36\omega_7^2\omega_4cs^2v_3^2 + 12\omega_7^2\omega_4^2v_3^3 + 24\omega_7^2cs^4 + 12\omega_7^2\omega_4cs^2 + 36\omega_4^3v_3^4 - 24\omega_7\omega_4^2cs^4 - 72\omega_7\omega_4^3cs^2v_3^2 -$$

$$8\omega_7^2\omega_4^2cs^2 - 12\omega_7^2\omega_4^2v_3^4 - 36\omega_4^3v_3^2 - 48\omega_7^2\omega_4cs^4 - 24\omega_7\omega_4cs^2 - 12\omega_7^2\omega_4^2cs^2v_3^2 - 72\omega_7\omega_4^2v_3^2 - 216\omega_4^2cs^2v_3^2 + \omega_7^2\omega_4^3cs^2 + 6\omega_7\omega_4^3cs^4 + 30\omega_7\omega_4^3v_3^2 + 72\omega_7\omega_4cs^2v_3^2 + 72\omega_4^2v_3^2 + 3\omega_7^2\omega_4^3v_3^4) \frac{1}{24\omega_7^2\omega_4^3}$$

$$C_{\mathbb{D}_z^4 \rho}^{(0), \text{CLBM2}} = (\omega_7^2\omega_4^3cs^2 - 72\omega_4^2v_3^4 - 3\omega_7^2\omega_4^3v_3^2 - 30\omega_7\omega_4^3v_3^4 + 72\omega_7\omega_4v_3^2cs^2 + 6\omega_7\omega_4^3cs^4 - 72\omega_7\omega_4^3v_3^2cs^2 - 48\omega_7^2\omega_4cs^4 - 24\omega_7\omega_4cs^2 - 24\omega_7\omega_4^2cs^4 + 72\omega_7\omega_4^2v_3^4 - 12\omega_7^2\omega_4^2v_3^2cs^2 - 216\omega_4^2v_3^2cs^2 + 12\omega_7^2\omega_4^2v_3^2 - 8\omega_7^2\omega_4^2cs^2 + 36\omega_4^3v_3^4 + 24\omega_7\omega_4cs^4 + 24\omega_7^2cs^4 + 12\omega_7^2\omega_4cs^2 - 36\omega_7^2\omega_4v_3^2cs^2 - 12\omega_7^2\omega_4^2v_3^4 + 24\omega_7^2\omega_4^2cs^4 - 36\omega_4^3v_3^2 + 24\omega_7\omega_4^2cs^2 - 72\omega_7\omega_4^2v_3^2 + 108\omega_4^3v_3^2cs^2 + 6\omega_7^2\omega_4^3v_3^2cs^2 + 30\omega_7\omega_4^3v_3^2 - 6\omega_7\omega_4^3cs^2 - 3\omega_7^2\omega_4^3cs^4 + 144\omega_7\omega_4^2v_3^2cs^2 + 72\omega_4^2v_3^2 + 3\omega_7^2\omega_4^3v_3^4) \frac{1}{24\omega_7^2\omega_4^3}$$

**coefficient**  $C_{\mathbb{D}_z^4 v_3}^{(0)}$  at  $\frac{\partial^4 v_3}{\partial x_3^4}$ :

$$C_{\mathbb{D}_z^4 v_3}^{(0), \text{SRT}} = (24 - 26\omega^2cs^2 + 54\omega v_3^2 + \omega^3cs^2 - 48cs^2 - 36\omega - \omega^3 - 36v_3^2 + 14\omega^2 + 2\omega^3v_3^2 + 72\omega cs^2 - 22\omega^2v_3^2) \frac{\rho v_3}{12\omega^3}$$

$$C_{\mathbb{D}_z^4 v_3}^{(0), \text{MRT1}} = (\omega_7^2\omega_4^3cs^2 - 6\omega_4^3 - 24\omega_7\omega_4^2 + 12\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3 - 12\omega_7^2v_3^2 - 20\omega_7^2\omega_4^2cs^2 - 12\omega_7\omega_4v_3^2 - 24\omega_7^2cs^2 + 12\omega_7\omega_4 - 16\omega_7^2\omega_4^2v_3^2 - 12\omega_7\omega_4cs^2 + 6\omega_4^3cs^2 - 6\omega_7^2\omega_4 + 24\omega_7\omega_4^2cs^2 + 24\omega_7^2\omega_4v_3^2 + 6\omega_4^3v_3^2 + 24\omega_7\omega_4^2v_3^2 + 42\omega_7^2\omega_4cs^2 - 6\omega_7\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 12\omega_4^2cs^2 - 6\omega_7\omega_4^3v_3^2 - 12\omega_4^2v_3^2 + 8\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\mathbb{D}_z^4 v_3}^{(0), \text{MRT2}} = (-24\omega_7^2cs^2 - 6\omega_4^3 - 12\omega_7\omega_4cs^2 - 24\omega_7\omega_4^2 + 12\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 6\omega_7\omega_4^3 - 20\omega_7^2\omega_4^2cs^2 - 12\omega_7^2v_3^2 - 12\omega_7\omega_4v_3^2 + \omega_7^2\omega_4^3cs^2 + 12\omega_7\omega_4 - 16\omega_7^2\omega_4^2v_3^2 - 6\omega_7^2\omega_4 + 24\omega_7\omega_4^2v_3^2 - 6\omega_7\omega_4^3cs^2 + 6\omega_4^3v_3^2 + 24\omega_7\omega_4^2v_3^2 - 12\omega_4^2cs^2 - \omega_7^2\omega_4^3 + 42\omega_7^2\omega_4cs^2 - 6\omega_7\omega_4^3v_3^2 + 6\omega_4^3cs^2 + 24\omega_7\omega_4^2cs^2 - 12\omega_4^2v_3^2 + 8\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\mathbb{D}_z^4 v_3}^{(0), \text{CLBM1}} = (-18\omega_4^3 - 24\omega_7\omega_4^3cs^2 - 24\omega_7\omega_4^2 - 60\omega_4^2cs^2 + 36\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4^3 + 30\omega_4^3cs^2 - 12\omega_7^2v_3^2 + 72\omega_7\omega_4^2cs^2 + 60\omega_7\omega_4v_3^2 - 12\omega_7\omega_4 + 2\omega_7^2\omega_4^2v_3^2 - 30\omega_7^2\omega_4cs^2 + 6\omega_7^2\omega_4 - 12\omega_7^2\omega_4v_3^2 - 2\omega_7^2\omega_4^2cs^2 + 24\omega_7^2cs^2 + 42\omega_4^3v_3^2 - 12\omega_7\omega_4cs^2 + 24\omega_7\omega_4^2v_3^2 + \omega_7^2\omega_4^3cs^2 - \omega_7^2\omega_4^3 - 24\omega_7\omega_4^3v_3^2 - 84\omega_4^2v_3^2 + 2\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

$$C_{\mathbb{D}_z^4 v_3}^{(0), \text{CLBM2}} = (-18\omega_4^3 - 24\omega_7\omega_4^2 + \omega_7^2\omega_4^3cs^2 + 36\omega_4^2 + 2\omega_7^2\omega_4^3v_3^2 + 12\omega_7\omega_4^3 + 24\omega_7^2cs^2 - 12\omega_7^2v_3^2 - 12\omega_7\omega_4cs^2 + 60\omega_7\omega_4v_3^2 - 12\omega_7\omega_4 + 2\omega_7^2\omega_4^2v_3^2 - 2\omega_7^2\omega_4^2cs^2 + 6\omega_7^2\omega_4 - 12\omega_7^2\omega_4v_3^2 - 30\omega_7^2\omega_4cs^2 + 30\omega_4^3cs^2 + 42\omega_4^3v_3^2 + 72\omega_7\omega_4^2cs^2 + 24\omega_7\omega_4^2v_3^2 - \omega_7^2\omega_4^3 - 24\omega_7\omega_4^3v_3^2 - 24\omega_7\omega_4^3cs^2 - 84\omega_4^2v_3^2 - 60\omega_4^2cs^2 + 2\omega_7^2\omega_4^2) \frac{\rho v_3}{12\omega_7^2\omega_4^3}$$

## References

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