

D3Q27 NSE,

a supplementary material for

Lattice Boltzmann Method Analysis Tool (LBMAT)

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1 Global definitions

In \mathbb{R}^3 , the position and velocity vectors are given by $\mathbf{x} = (x_1, x_2, x_3)^T$ and $\mathbf{v} = (v_1, v_2, v_3)^T$, respectively.

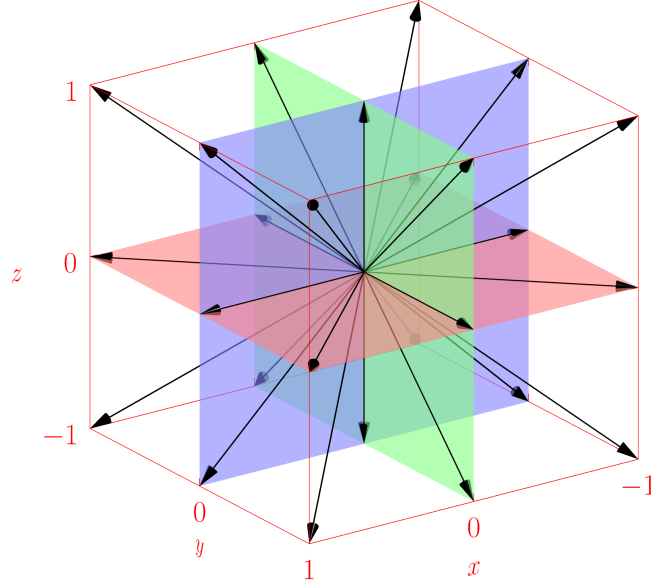
1.1 Discrete velocity vectors

Discrete velocity vectors and the lattice speed of sound are defined by

$$\{\mathbf{c}_i\}_{i=1}^{27} = \left(\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ -1 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} -1 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ -1 \\ -1 \end{pmatrix} \right),$$

$$c_s = \frac{1}{\sqrt{3}},$$

respectively [1].



1.2 Raw and central moments

The raw and central moments are defined by

$$m_{\alpha} := \sum_{i=1}^{27} f_i \mathbf{c}_i^{\alpha},$$

and

$$k_{\alpha} := \sum_{i=1}^{27} f_i (\mathbf{c}_i - \mathbf{v})^{\alpha},$$

respectively, where $\alpha = (\alpha_1, \alpha_2, \alpha_3) \in \mathbb{Z}^3$ denotes a multi-index (as a row vector) and $\mathbf{c}_i^{\alpha} := \prod_{j=1}^3 [\mathbf{c}_i]_j^{\alpha_j}$.

1.3 Transformation matrix \mathbf{M}

Matrix \mathbf{M} , that defines macroscopic quantities (moments) $\boldsymbol{\mu}$ by

$$\boldsymbol{\mu} = \mathbf{M} \mathbf{f},$$

with $\mathbf{f} = (f_1, f_2, \dots, f_{27})^T$, is selected such that

$$\boldsymbol{\mu} = \begin{pmatrix} m_{(0,0,0)}, m_{(1,0,0)}, m_{(0,1,0)}, m_{(0,0,1)}, m_{(1,1,0)}, m_{(1,0,1)}, m_{(0,1,1)}, m_{(1,1,1)}, m_{(2,0,0)}, \\ m_{(0,2,0)}, m_{(0,0,2)}, m_{(2,1,0)}, m_{(2,0,1)}, m_{(2,1,1)}, m_{(1,2,0)}, m_{(0,2,1)}, m_{(1,2,1)}, m_{(1,0,2)}, \\ m_{(0,1,2)}, m_{(1,1,2)}, m_{(2,2,0)}, m_{(2,0,2)}, m_{(0,2,2)}, m_{(2,2,1)}, m_{(2,1,2)}, m_{(1,2,2)}, m_{(2,2,2)} \end{pmatrix}^T,$$

i.e., \mathbf{M} is given by

[illegible]

1.4 Equilibrium

The corresponding equilibrium raw moments are defined using the continuous Maxwell–Boltzmann distribution function [1]

$$f^{(eq)}(\boldsymbol{\xi}) = \frac{\rho}{(2\pi c_s^2)^{\frac{3}{2}}} \exp\left(-\frac{\|\boldsymbol{\xi} - \mathbf{v}\|^2}{2c_s^2}\right)$$

as

$$m_{\alpha}^{(eq)} = \int_{\mathbb{R}^3} \xi^{\alpha} f^{(eq)}(\xi) d\xi,$$

where $\alpha_i \in \{0, 1, 2\}$, $i = 1, 2, 3$. Hence, the equilibrium moments $\boldsymbol{\mu}^{(eq)}$ satisfy

$$\boldsymbol{\mu}^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho v_1 v_2 \\ \rho v_1 v_3 \\ \rho v_2 v_3 \\ \rho v_1 v_2 v_3 \\ \rho (v_1^2 + c_s^2) \\ \rho (v_2^2 + c_s^2) \\ \rho (v_3^2 + c_s^2) \\ \rho (v_1^2 v_2 + v_2 c_s^2) \\ \rho (v_1^2 v_3 + v_3 c_s^2) \\ \rho (v_1^2 v_2 v_3 + v_2 v_3 c_s^2) \\ \rho (v_1 v_2^2 + v_1 c_s^2) \\ \rho (v_2^2 v_3 + v_3 c_s^2) \\ \rho (v_1 v_2^2 v_3 + v_1 v_3 c_s^2) \\ \rho (v_1 v_3^2 + v_1 c_s^2) \\ \rho (v_2 v_3^2 + v_2 c_s^2) \\ \rho (v_1 v_2 v_3^2 + v_1 v_3 c_s^2) \\ \rho (v_1^2 v_2^2 + v_2^2 c_s^2 + v_1^2 c_s^2 + c_s^4) \\ \rho (v_1^2 v_3^2 + v_3^2 c_s^2 + v_1^2 c_s^2 + c_s^4) \\ \rho (v_2^2 v_3^2 + v_3^2 c_s^2 + v_2^2 c_s^2 + c_s^4) \\ \rho (v_1^2 v_2^2 v_3 + v_2^2 v_3 c_s^2 + v_1^2 v_3 c_s^2 + v_3 c_s^4) \\ \rho (v_1^2 v_2 v_3^2 + v_2 v_3^2 c_s^2 + v_1^2 v_2 c_s^2 + v_2 c_s^4) \\ \rho (v_1 v_2^2 v_3^2 + v_1 v_3^2 c_s^2 + v_1 v_2^2 c_s^2 + v_1 c_s^4) \\ \rho (v_1^2 v_2^2 v_3^2 + v_2^2 v_3^2 c_s^2 + v_1^2 v_3^2 c_s^2 + v_2^2 c_s^4 + v_1^2 c_s^4 + c_s^6) \end{pmatrix}.$$

2 Spatial EPDEs

2.1 SRT

2.1.1 Definitions

Collision operator \mathcal{C} :

$$\mathcal{C}(\mathbf{f}) = \omega \left(\mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)} - \mathbf{f} \right),$$

$\omega \in (0, 2)$.

2.1.2 Conservation of mass: ρ



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$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{\delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{\delta_l^3 v_1}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\ & \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_l^3 v_3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \end{aligned}$$

$$\begin{aligned}
& + (3\omega v_1^2 - 2c_s^2 + 6v_1^4 - \omega c_s^4 - 12\omega v_1^2 c_s^2 - 3\omega v_1^4 + 2c_s^4 + 24v_1^2 c_s^2 - 6v_1^2 + \omega c_s^2) \frac{\delta_t^4}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 - 5\omega v_1^2 + 6c_s^2 + 2\omega + 10v_1^2 - 3\omega c_s^2) \frac{\rho\delta_t^4 v_1}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (2 + \omega v_1^2 - 6c_s^2 - \omega - 2v_1^2 + 3\omega c_s^2) \frac{\rho\delta_t^4 v_1}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + \omega) \frac{\delta_t^4 c_s^4}{6\omega\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + (2 - 6c_s^2 - \omega + \omega v_2^2 - 2v_2^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_t^4}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-2c_s^2 + 6v_2^4 + 3\omega v_2^2 - \omega c_s^4 + 24v_2^2 c_s^2 - 12\omega v_2^2 c_s^2 + 2c_s^4 - 6v_2^2 - 3\omega v_2^4 + \omega c_s^2) \frac{\delta_t^4}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 2\omega - 5\omega v_2^2 + 10v_2^2 - 3\omega c_s^2) \frac{\rho v_2 \delta_t^4}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (2 + \omega v_1^2 - 6c_s^2 - \omega - 2v_1^2 + 3\omega c_s^2) \frac{\rho\delta_t^4 v_1}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (2 - 6c_s^2 - \omega + \omega v_2^2 - 2v_2^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_t^4}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 + \omega) \frac{\delta_t^4 c_s^4}{6\omega\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& (2 - 6c_s^2 - \omega + \omega v_3^2 - 2v_3^2 + 3\omega c_s^2) \frac{\rho\delta_t^4 v_3}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + (2 - 6c_s^2 - \omega + \omega v_3^2 - 2v_3^2 + 3\omega c_s^2) \frac{\rho\delta_t^4 v_3}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-12\omega v_3^2 c_s^2 - 2c_s^2 - \omega c_s^4 + 3\omega v_3^2 + 24v_3^2 c_s^2 + 6v_3^4 - 3\omega v_3^4 - 6v_3^2 + 2c_s^4 + \omega c_s^2) \frac{\delta_t^4}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 6c_s^2 + 2\omega - 5\omega v_3^2 + 10v_3^2 - 3\omega c_s^2) \frac{\rho\delta_t^4 v_3}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.1.3 Conservation of momentum: ρv_1



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$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_t}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho\delta_t v_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_t v_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho v_2 \delta_t}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho\delta_t v_1}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_t v_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho\delta_t v_3}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\rho\delta_t v_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 - 3\omega v_1^2 + 4c_s^2 + \omega + 6v_1^2 - 2\omega c_s^2) \frac{\delta_t^2}{\omega\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega) \frac{3\rho\delta_t^2 v_1}{\omega\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (-2 + \omega) \frac{\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + \\
& (-2 + \omega) \frac{\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega) \frac{\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega) \frac{\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 - \omega v_1^2 + 6c_s^2 + \omega + 2v_1^2 - 3\omega c_s^2) \frac{\delta_t^2 v_1}{2\omega\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 - 3\omega v_1^2 + 2c_s^2 + \omega + 6v_1^2 - \omega c_s^2) \frac{\rho\delta_t^2}{2\omega\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega) \frac{\rho\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega) \frac{\rho\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega) \frac{\rho\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega) \frac{\rho\delta_t^2 c_s^2}{2\omega\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_t^3}{12\omega^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 - 60\omega v_1^2 + 36c_s^2 + 5\omega^2 c_s^2 + 24\omega - 4\omega^2 + 11\omega^2 v_1^2 + 60v_1^2 - 36\omega c_s^2) \frac{\rho\delta_t^3 v_1}{6\omega^2\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (12 + 12\omega v_1^2 - 36c_s^2 - 11\omega^2 c_s^2 - 12\omega + 3\omega^2 - 3\omega^2 v_1^2 - 12v_1^2 + 36\omega c_s^2) \frac{\rho\delta_t^3 v_1}{12\omega^2\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 + 12\omega - \omega^2) \frac{\delta_t^3 c_s^4}{6\omega^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{\rho\delta_t^3 v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_t^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^2} + \\
& (6 - 18c_s^2 - 3\omega^2 c_s^2 - 6\omega + 6\omega v_2^2 + \omega^2 - \omega^2 v_2^2 - 6v_2^2 + 18\omega c_s^2) \frac{\rho v_2 \delta_t^3}{6\omega^2\delta_t} \frac{\partial^3 v_1}{\partial x_3^2} + (-1 + c_s^2 + 3v_2^2) \frac{\rho\delta_t^3 v_1}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^2} + \\
& (12 + 12\omega v_1^2 - 36c_s^2 - 11\omega^2 c_s^2 - 12\omega + 3\omega^2 - 3\omega^2 v_1^2 - 12v_1^2 + 36\omega c_s^2) \frac{\rho\delta_t^3 v_1}{12\omega^2\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho\delta_t^3 v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-12 + 12\omega - \omega^2) \frac{\delta_t^3 c_s^4}{6\omega^2\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \frac{\rho\delta_t^3 v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\rho\delta_t^3 v_1 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_t^3 v_1 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^2} + \\
& (6 - 18c_s^2 - 3\omega^2 c_s^2 - 6\omega + 6\omega v_3^2 + \omega^2 - \omega^2 v_3^2 - 6v_3^2 + 18\omega c_s^2) \frac{\rho\delta_t^3 v_3}{6\omega^2\delta_t} \frac{\partial^3 v_1}{\partial x_3^2} + (-1 + c_s^2 + 3v_3^2) \frac{\rho\delta_t^3 v_1}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^2} + \\
& C_2 \frac{\delta_t^4 v_1}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_3 \frac{\rho\delta_t^4}{12\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_4 \frac{\rho\delta_t^4}{12\omega^3\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_5 \frac{\delta_t^4 v_1 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (-24 - 108\omega v_1^2 + 12c_s^2 + 8\omega^2 c_s^2 + 36\omega - \omega^3 c_s^2 - 12\omega^2 + 36\omega^2 v_1^2 + 72v_1^2 - 18\omega c_s^2) \frac{\rho\delta_t^4 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_6 \frac{v_2 \delta_t^4 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + \\
& + (2 - 6c_s^2 - \omega + \omega v_2^2 - 2v_2^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_t^4 v_1}{12\omega\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-12 + 2\omega^2 c_s^2 + 18\omega - 54\omega v_2^2 - \omega^3 c_s^2 - 6\omega^2 + 18\omega^2 v_2^2 + 36v_2^2) \frac{\rho\delta_t^4 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\
& (-2c_s^2 + 6v_2^4 + 3\omega v_2^2 - \omega c_s^4 + 24v_2^2 c_s^2 - 12\omega v_2^2 c_s^2 + 2c_s^4 - 6v_2^2 - 3\omega v_2^4 + \omega c_s^2) \frac{\delta_t^4 v_1}{24\omega\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_7 \frac{\rho\delta_t^4}{24\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 2\omega - 5\omega v_2^2 + 10v_2^2 - 3\omega c_s^2) \frac{\rho v_2 \delta_t^4 v_1}{12\omega\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_8 \frac{\rho\delta_t^4}{12\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-36 + 54\omega - 16\omega^2 - \omega^3) \frac{\rho\delta_t^4 c_s^4}{12\omega^3\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (2 - 6c_s^2 - \omega + \omega v_2^2 - 2v_2^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_t^4 v_1}{12\omega\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_9 \frac{\delta_t^4 v_1 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (-24 - 108\omega v_1^2 + 12c_s^2 + 8\omega^2 c_s^2 + 36\omega - \omega^3 c_s^2 - 12\omega^2 + 36\omega^2 v_1^2 + 72v_1^2 - 18\omega c_s^2) \frac{\rho\delta_t^4 c_s^2}{12\omega^3\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{10} \frac{\delta_t^4}{2\omega^3\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2}
\end{aligned}$$

$$\begin{aligned}
& + C_{11} \frac{\rho \delta_t^4}{2\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{12} \frac{\rho \delta_t^4}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + C_{13} \frac{\rho \delta_t^4 v_3}{\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{14} \frac{\delta_t^4}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{15} \frac{\rho \delta_t^4}{4\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3} + \\
& C_{16} \frac{\rho v_2 \delta_t^4}{2\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{17} \frac{\rho \delta_t^4}{4\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{18} \frac{\delta_t^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + (2 - 6c_s^2 - \omega + \omega v_3^2 - 2v_3^2 + 3\omega c_s^2) \frac{\rho \delta_t^4 v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} + \\
& (-12 + 2\omega^2 c_s^2 + 18\omega - \omega^3 c_s^2 - 54\omega v_3^2 - 6\omega^2 + 18\omega^2 v_3^2 + 36v_3^2) \frac{\rho \delta_t^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} + \\
& (2 - 6c_s^2 - \omega + \omega v_3^2 - 2v_3^2 + 3\omega c_s^2) \frac{\rho \delta_t^4 v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + \\
& (-12\omega v_3^2 c_s^2 - 2c_s^2 - \omega c_s^4 + 3\omega v_3^2 + 24v_3^2 c_s^2 + 6v_3^4 - 3\omega v_3^4 - 6v_3^2 + 2c_s^4 + \omega c_s^2) \frac{\delta_t^4 v_1}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_3} + C_{19} \frac{\rho \delta_t^4}{24\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_3} + \\
& (-4 + 6c_s^2 + 2\omega - 5\omega v_3^2 + 10v_3^2 - 3\omega c_s^2) \frac{\rho \delta_t^4 v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_3} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 36\omega v_1^2 - 12c_s^2 - \omega^2 c_s^2 + 36v_1^4 - 12\omega c_s^4 + 7\omega^2 v_1^4 + 24\omega^2 v_1^2 c_s^2 - 144\omega v_1^2 c_s^2 + \omega^2 c_s^4 - 36\omega v_1^4 + 12c_s^4 - 7\omega^2 v_1^2 + 144v_1^2 c_s^2 - 36v_1^2 + 12\omega c_s^2 \\
C_2 &= 12 + 234\omega v_1^2 - 132c_s^2 - 78\omega^2 c_s^2 + 144v_1^4 - 18\omega - 216\omega c_s^4 + 90\omega^2 v_1^4 + 6\omega^3 c_s^2 + 404\omega^2 v_1^2 c_s^2 - 9\omega^3 v_1^4 + 8\omega^2 - 5\omega^3 c_s^4 - 1008\omega v_1^2 c_s^2 - \omega^3 + \\
& 10\omega^3 v_1^2 + 82\omega^2 c_s^4 - 216\omega v_1^4 + 144c_s^4 - 34\omega^3 v_1^2 c_s^2 - 98\omega^2 v_1^2 + 672v_1^2 c_s^2 - 156v_1^2 + 198\omega c_s^2 \\
C_3 &= 12 + 378\omega v_1^2 - 36c_s^2 - 22\omega^2 c_s^2 + 504v_1^4 - 18\omega - 36\omega c_s^4 + 310\omega^2 v_1^4 + 2\omega^3 c_s^2 + 252\omega^2 v_1^2 c_s^2 - 29\omega^3 v_1^4 + 8\omega^2 - \omega^3 c_s^4 - 648\omega v_1^2 c_s^2 - \omega^3 + \\
& 14\omega^3 v_1^2 + 14\omega^2 c_s^4 - 756\omega v_1^4 + 24c_s^4 - 18\omega^3 v_1^2 c_s^2 - 154\omega^2 v_1^2 + 432v_1^2 c_s^2 - 252v_1^2 + 54\omega c_s^2 \\
C_4 &= -54\omega v_1^2 - 24c_s^2 - 12\omega^2 c_s^2 - 36v_1^4 - 54\omega c_s^4 - 26\omega^2 v_1^4 - 42\omega^2 v_1^2 c_s^2 + 4\omega^3 v_1^4 - \omega^3 c_s^4 + 54\omega v_1^2 c_s^2 - 4\omega^3 v_1^2 + 20\omega^2 c_s^4 + 54\omega v_1^4 + 36c_s^4 + \\
& 12\omega^3 v_1^2 c_s^2 + 26\omega^2 v_1^2 - 36v_1^2 c_s^2 + 36v_1^2 + 36\omega c_s^2 \\
C_5 &= 24 + 36\omega v_1^2 - 72c_s^2 - 46\omega^2 c_s^2 - 36\omega + 5\omega^3 c_s^2 + 14\omega^2 - \omega^3 + \omega^3 v_1^2 - 14\omega^2 v_1^2 - 24v_1^2 + 108\omega c_s^2 \\
C_6 &= 24 - 72c_s^2 - 42\omega^2 c_s^2 - 36\omega + 36\omega v_2^2 + 3\omega^3 c_s^2 + 14\omega^2 + \omega^3 v_2^2 - \omega^3 - 14\omega^2 v_2^2 - 24v_2^2 + 108\omega c_s^2 \\
C_7 &= -84\omega^2 v_2^2 c_s^2 - 24c_s^2 - 72v_2^4 - 14\omega^2 c_s^2 - 42\omega^2 v_2^4 - 108\omega v_2^2 - 72\omega c_s^4 + 3\omega^3 v_2^4 + \omega^3 c_s^2 - 3\omega^3 v_2^2 - 3\omega^3 c_s^4 - 144v_2^2 c_s^2 + 6\omega^3 v_2^2 c_s^2 + \\
& 216\omega v_2^2 c_s^2 + 30\omega^2 c_s^4 + 42\omega^2 v_2^2 + 48c_s^4 + 72v_2^2 + 108\omega v_2^4 + 36\omega c_s^2 \\
C_8 &= -54\omega v_1^2 - 24c_s^2 - 12\omega^2 c_s^2 - 36v_1^4 - 54\omega c_s^4 - 26\omega^2 v_1^4 - 42\omega^2 v_1^2 c_s^2 + 4\omega^3 v_1^4 - \omega^3 c_s^4 + 54\omega v_1^2 c_s^2 - 4\omega^3 v_1^2 + 20\omega^2 c_s^4 + 54\omega v_1^4 + 36c_s^4 + \\
& 12\omega^3 v_1^2 c_s^2 + 26\omega^2 v_1^2 - 36v_1^2 c_s^2 + 36v_1^2 + 36\omega c_s^2 \\
C_9 &= 24 + 36\omega v_1^2 - 72c_s^2 - 46\omega^2 c_s^2 - 36\omega + 5\omega^3 c_s^2 + 14\omega^2 - \omega^3 + \omega^3 v_1^2 - 14\omega^2 v_1^2 - 24v_1^2 + 108\omega c_s^2 \\
C_{10} &= 36\omega v_1 v_3^2 c_s^2 + 36\omega v_2^2 v_1 c_s^2 + 14\omega^2 v_2 v_1^2 v_3^2 - 36\omega v_2 v_1^2 c_s^2 - 14\omega^2 v_2^2 v_1 v_3^2 + 14\omega^2 v_2 v_3^2 c_s^2 + 24v_2 v_1^2 v_3^2 - \omega^3 v_2 v_3^2 c_s^2 + \omega^3 v_2^2 v_1 v_3^2 - \omega^3 v_2 v_1^2 v_3^2 + \\
& 24v_2 v_3^2 c_s^2 - 24v_2^2 v_1 v_3^2 - 14\omega^2 v_2^2 v_1 c_s^2 - 36\omega v_2 v_1^2 v_3^2 - 14\omega^2 v_1 v_3^2 c_s^2 - 36\omega v_2 v_3^2 c_s^2 + 14\omega^2 v_2 v_1^2 c_s^2 + 36\omega v_2^2 v_1 v_3^2 - 24v_1 v_3^2 c_s^2 - \omega^3 v_2 v_1^2 c_s^2 - \\
& 24v_2^2 v_1 c_s^2 + \omega^3 v_1 v_3^2 c_s^2 + 24v_2 v_1^2 c_s^2 + \omega^3 v_2^2 v_1 c_s^2 \\
C_{11} &= 36\omega v_3^2 c_s^2 - 14\omega^2 v_2^2 c_s^2 + \omega^3 v_2^2 v_3^2 + 48v_2 v_1 c_s^2 - 24v_2^2 v_3^2 - 2\omega^3 v_2 v_1 c_s^2 + 28\omega^2 v_2 v_1 c_s^2 - 24v_3^2 c_s^2 - 72\omega v_2 v_1 v_3^2 + \omega^3 v_3^2 c_s^2 + 36\omega v_2^2 v_3^2 - \\
& 2\omega^3 v_2 v_1 v_3^2 + 48v_2 v_1 v_3^2 - 24v_2^2 c_s^2 - 14\omega^2 v_2^2 v_3^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 72\omega v_2 v_1 c_s^2 - 14\omega^2 v_3^2 c_s^2 + 28\omega^2 v_2 v_1 v_3^2 \\
C_{12} &= -216\omega v_3^2 c_s^2 - 288v_2 v_1 c_s^2 + 54\omega c_s^4 - 216\omega v_1^2 v_3^2 + 12\omega^3 v_2 v_1 c_s^2 + 144v_1^2 v_3^2 + 84\omega^2 v_1^2 c_s^2 - 6\omega^3 v_1^2 v_3^2 - 168\omega^2 v_2 v_1 c_s^2 + 144v_3^2 c_s^2 + 432\omega v_2 v_1 v_3^2 - \\
& 6\omega^3 v_3^2 c_s^2 + 12\omega^3 v_2 v_1 v_3^2 - \omega^3 c_s^4 - 216\omega v_1^2 c_s^2 - 288v_2 v_1 v_3^2 + 432\omega v_2 v_1 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 - 36c_s^4 + 84\omega^2 v_1^2 v_3^2 - 6\omega^3 v_1^2 c_s^2 - 168\omega^2 v_2 v_1 v_3^2 + 144v_1^2 c_s^2 \\
C_{13} &= \omega^3 v_1 c_s^2 + 14\omega^2 v_2 v_1^2 - 24v_1 c_s^2 - 36\omega v_2 c_s^2 - 24v_2^2 v_1 + \omega^3 v_2^2 v_1 + 36\omega v_2^2 v_1 + 24v_2 c_s^2 - \omega^3 v_2 c_s^2 + 36\omega v_1 c_s^2 - 14\omega^2 v_2^2 v_1 - \omega^3 v_2 v_1^2 - \\
& 14\omega^2 v_1 c_s^2 + 24v_2 v_1^2 - 36\omega v_2 v_1^2 + 14\omega^2 v_2 c_s^2 \\
C_{14} &= -42\omega^2 v_2^2 v_3 c_s^2 - 108\omega v_1 v_3^2 c_s^2 - 108\omega v_2^2 v_1 c_s^2 + 42\omega^2 v_2^2 v_1 v_3^2 + 108\omega v_2^2 v_3 c_s^2 + 108\omega v_2^2 v_3 c_s^2 - 3\omega^3 v_2^2 v_1 v_3^2 - 72v_2^2 v_3 c_s^2 - 4\omega^2 v_1 c_s^4 + \\
& 72v_2^2 v_1 v_3^2 + 3\omega^3 v_2^2 v_3 c_s^2 + 42\omega^2 v_2^2 v_1 c_s^2 + 108\omega v_2^2 v_3 c_s^2 + 42\omega^2 v_1 v_3^2 c_s^2 - 42\omega^2 v_2^2 v_1 v_3^2 - 42\omega^2 v_1^2 v_3 c_s^2 - 108\omega v_2^2 v_1 v_3^2 + 72v_1 v_3^2 c_s^2 + 2\omega^3 v_1 c_s^4 + \\
& 3\omega^3 v_1^2 v_3 c_s^2 + 72v_2^2 v_1 c_s^2 + 3\omega^3 v_2^2 v_1 v_3 - 3\omega^3 v_1 v_3^2 c_s^2 - 72v_1^2 v_3 c_s^2 - 3\omega^3 v_2^2 v_1 c_s^2 - 72v_2^2 v_1 v_3 \\
C_{15} &= -36\omega v_3^2 c_s^2 + 14\omega^2 v_2^2 c_s^2 - \omega^3 v_2^2 v_3^2 + 2\omega^3 v_1 v_3^2 c_s^2 - 48v_2^2 v_1 v_3 + 24v_2^2 v_3^2 + 12\omega c_s^4 - 48v_1 v_3 c_s^2 + 2\omega^3 v_2^2 v_1 v_3 - 28\omega^2 v_2^2 v_1 v_3 + 24v_3^2 c_s^2 - \\
& \omega^3 v_3^2 c_s^2 - 36\omega v_2^2 v_3^2 - 28\omega^2 v_1 v_3 c_s^2 + 24v_2^2 c_s^2 + 14\omega^2 v_2^2 v_3^2 - \omega^3 v_2^2 c_s^2 - 36\omega v_2^2 c_s^2 + 14\omega^2 v_3^2 c_s^2 - 4\omega^2 c_s^4 + 72\omega v_2^2 v_1 v_3 - 8c_s^4 + 72\omega v_1 v_3 c_s^2 \\
C_{16} &= 14\omega^2 v_1 v_3^2 - \omega^3 v_1 c_s^2 + 24v_1 c_s^2 - 14\omega^2 v_3 c_s^2 + \omega^3 v_1^2 v_3 - 24v_1^2 v_3 + 36\omega v_1^2 v_3 - 36\omega v_1 c_s^2 - 24v_3 c_s^2 - 14\omega^2 v_1^2 v_3 + \omega^3 v_3 c_s^2 + 24v_1 v_3^2 + \\
& 14\omega^2 v_1 c_s^2 - \omega^3 v_1 v_3^2 - 36\omega v_1 v_3^2 + 36\omega v_3 c_s^2 \\
C_{17} &= -14\omega^2 v_2^2 c_s^2 - 2\omega^3 v_1 v_3 c_s^2 + 48v_2^2 v_1 v_3 + 48v_1 v_3 c_s^2 - 2\omega^3 v_2^2 v_1 v_3 + 36\omega v_2^2 v_1^2 + \omega^3 v_2^2 v_1^2 + 28\omega^2 v_2^2 v_1 v_3 - 24v_2^2 v_1^2 - 14\omega^2 v_1^2 c_s^2 + \\
& 28\omega^2 v_1 v_3 c_s^2 + 36\omega v_2^2 c_s^2 - 24v_2^2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 72\omega v_2^2 v_1 v_3 - 72\omega v_1 v_3 c_s^2 + \omega^3 v_1^2 c_s^2 - 24v_1^2 c_s^2 - 14\omega^2 v_2^2 v_1^2 \\
C_{18} &= 24 - 72c_s^2 - 42\omega^2 c_s^2 - 36\omega + 3\omega^3 c_s^2 + 36\omega v_3^2 + 14\omega^2 - \omega^3 - 14\omega^2 v_3^2 - 24v_3^2 + \omega^3 v_3^2 + 108\omega c_s^2
\end{aligned}$$

$$C_{19} = 216\omega v_3^2 c_s^2 - 24c_s^2 - 14\omega^2 c_s^2 + 3\omega^3 v_3^4 - 72\omega c_s^4 + \omega^3 c_s^2 - 108\omega v_3^2 - 144v_3^2 c_s^2 - 72v_3^4 + 6\omega^3 v_3^2 c_s^2 - 42\omega^2 v_3^4 - 3\omega^3 c_s^4 + 108\omega v_3^4 + 42\omega^2 v_3^2 + 72v_3^2 - 84\omega^2 v_3^2 c_s^2 + 30\omega^2 c_s^4 + 48c_s^4 - 3\omega^3 v_3^2 + 36\omega c_s^2$$

2.1.4 Conservation of momentum: ρv_2



attached text file: output_d3q27_nse_srt_symbolic_pde_02.txt

$$\begin{aligned} & v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_2 \delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho \delta_l v_1}{\delta_t} \frac{\partial v_2}{\partial x_1} + (c_s^2 + v_2^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2\rho v_2 \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 \delta_l v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l v_3}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\ & \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (-2 + 4c_s^2 + \omega - 3\omega v_2^2 + 6v_2^2 - 2\omega c_s^2) \frac{\delta_l^2}{\omega \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + \\ & (2 - \omega) \frac{3\rho v_2 \delta_l^2}{\omega \delta_t} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + (-2 + \omega) \frac{\delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega) \frac{\rho \delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + \\ & (-2 + \omega) \frac{\rho \delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + (-2 + 6c_s^2 + \omega - \omega v_2^2 + 2v_2^2 - 3\omega c_s^2) \frac{v_2 \delta_l^2}{2\omega \delta_t} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + 2c_s^2 + \omega - 3\omega v_2^2 + 6v_2^2 - \omega c_s^2) \frac{\rho \delta_l^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} \\ & + (-2 + \omega) \frac{\rho \delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega) \frac{\rho \delta_l^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_3^2} + (-1 + 3c_s^2 + v_1^2) \frac{v_2 \delta_l^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{\rho v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\ & (6 + 6\omega v_1^2 - 18c_s^2 - 3\omega^2 c_s^2 - 6\omega + \omega^2 - \omega^2 v_1^2 - 6v_1^2 + 18\omega c_s^2) \frac{\rho \delta_l^3 v_1}{6\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 + 12\omega - \omega^2) \frac{\delta_l^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \\ & \frac{\rho v_2 \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + (12 - 36c_s^2 - 11\omega^2 c_s^2 - 12\omega + 12\omega v_2^2 + 3\omega^2 - 3\omega^2 v_2^2 - 12v_2^2 + 36\omega c_s^2) \frac{\rho v_2 \delta_l^3}{12\omega^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & C_1 \frac{\delta_l^3}{12\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-24 + 36c_s^2 + 5\omega^2 c_s^2 + 24\omega - 60\omega v_2^2 - 4\omega^2 + 11\omega^2 v_2^2 + 60v_2^2 - 36\omega c_s^2) \frac{\rho v_2 \delta_l^3}{6\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \frac{\rho v_2 \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\ & (12 - 36c_s^2 - 11\omega^2 c_s^2 - 12\omega + 12\omega v_2^2 + 3\omega^2 - 3\omega^2 v_2^2 - 12v_2^2 + 36\omega c_s^2) \frac{\rho v_2 \delta_l^3}{12\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\rho v_2 \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\ & (-12 + 12\omega - \omega^2) \frac{\delta_l^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_2^3} - \frac{\rho v_2 \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_2^3} + (-1 + 3c_s^2 + v_3^2) \frac{v_2 \delta_l^3 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\ & (6 - 18c_s^2 - 3\omega^2 c_s^2 - 6\omega + 6\omega v_3^2 + \omega^2 - \omega^2 v_3^2 - 6v_3^2 + 18\omega c_s^2) \frac{\rho \delta_l^3 v_3}{6\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\ & (3\omega v_1^2 - 2c_s^2 + 6v_1^4 - \omega c_s^4 - 12\omega v_1^2 c_s^2 - 3\omega v_1^4 + 2c_s^4 + 24v_1^2 c_s^2 - 6v_1^2 + \omega c_s^2) \frac{v_2 \delta_l^4}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 - 5\omega v_1^2 + 6c_s^2 + 2\omega + 10v_1^2 - 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_1}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_2 \frac{\rho \delta_l^4}{24\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_3 \frac{\delta_l^4 v_1 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\ & (-12 - 54\omega v_1^2 + 2\omega^2 c_s^2 + 18\omega - \omega^3 c_s^2 - 6\omega^2 + 18\omega^2 v_1^2 + 36v_1^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\ & (2 + \omega v_1^2 - 6c_s^2 - \omega - 2v_1^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_1}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_4 \frac{v_2 \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_2^2} + \\ & (-24 + 12c_s^2 + 8\omega^2 c_s^2 + 36\omega - 108\omega v_2^2 - \omega^3 c_s^2 - 12\omega^2 + 36\omega^2 v_2^2 + 72v_2^2 - 18\omega c_s^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_5 \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\ & C_6 \frac{v_2 \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_7 \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + (2 + \omega v_1^2 - 6c_s^2 - \omega - 2v_1^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_1}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\ & (-36 + 54\omega - 16\omega^2 - \omega^3) \frac{\rho \delta_l^4 c_s^4}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_8 \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_9 \frac{\delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{10} \frac{\rho \delta_l^4}{4\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + \\ & C_{11} \frac{\rho \delta_l^4}{4\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{12} \frac{\rho \delta_l^4 v_3}{2\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{13} \frac{\delta_l^4}{2\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{14} \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{15} \frac{\rho v_2 \delta_l^4}{\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\ & C_{16} \frac{\rho \delta_l^4}{2\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{17} \frac{v_2 \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\ & (-24 + 12c_s^2 + 8\omega^2 c_s^2 + 36\omega - 108\omega v_2^2 - \omega^3 c_s^2 - 12\omega^2 + 36\omega^2 v_2^2 + 72v_2^2 - 18\omega c_s^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\ & (2 - 6c_s^2 - \omega + \omega v_3^2 - 2v_3^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{18} \frac{\delta_l^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\ & (2 - 6c_s^2 - \omega + \omega v_3^2 - 2v_3^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\ & (-12 + 2\omega^2 c_s^2 + 18\omega - \omega^3 c_s^2 - 54\omega v_3^2 - 6\omega^2 + 18\omega^2 v_3^2 + 36v_3^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\ & (-12\omega v_3^2 c_s^2 - 2c_s^2 - \omega c_s^4 + 3\omega v_3^2 + 24v_3^2 c_s^2 + 6v_3^4 - 3\omega v_3^4 - 6v_3^2 + 2c_s^4 + \omega c_s^2) \frac{v_2 \delta_l^4}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{19} \frac{\rho \delta_l^4}{24\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_3^4} + \\ & (-4 + 6c_s^2 + 2\omega - 5\omega v_3^2 + 10v_3^2 - 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0, \end{aligned}$$

where:

$$C_1 = 24\omega^2 v_2^2 c_s^2 - 12c_s^2 + 36v_2^4 - \omega^2 c_s^2 + 7\omega^2 v_2^4 + 36\omega v_2^2 - 12\omega c_s^4 + 144v_2^2 c_s^2 - 144\omega v_2^2 c_s^2 + \omega^2 c_s^4 - 7\omega^2 v_2^2 + 12c_s^4 - 36v_2^2 - 36\omega v_2^4 + 12\omega c_s^2$$

$$\begin{aligned}
C_2 &= -108\omega v_1^2 - 24c_s^2 - 14\omega^2 c_s^2 - 72v_1^4 - 72\omega c_s^4 - 42\omega^2 v_1^4 + \omega^3 c_s^2 - 84\omega^2 v_1^2 c_s^2 + 3\omega^3 v_1^4 - 3\omega^3 c_s^4 + 216\omega v_1^2 c_s^2 - 3\omega^3 v_1^2 + 30\omega^2 c_s^4 + 108\omega v_1^4 + 48c_s^4 + 6\omega^3 v_1^2 c_s^2 + 42\omega^2 v_1^2 - 144v_1^2 c_s^2 + 72v_1^2 + 36\omega c_s^2 \\
C_3 &= 24 + 36\omega v_1^2 - 72c_s^2 - 42\omega^2 c_s^2 - 36\omega + 3\omega^3 c_s^2 + 14\omega^2 - \omega^3 + \omega^3 v_1^2 - 14\omega^2 v_1^2 - 24v_1^2 + 108\omega c_s^2 \\
C_4 &= 24 - 72c_s^2 - 46\omega^2 c_s^2 - 36\omega + 36\omega v_2^2 + 5\omega^3 c_s^2 + 14\omega^2 + \omega^3 v_2^2 - \omega^3 - 14\omega^2 v_2^2 - 24v_2^2 + 108\omega c_s^2 \\
C_5 &= -42\omega^2 v_2^2 c_s^2 - 24c_s^2 - 36v_2^4 - 12\omega^2 c_s^2 - 26\omega^2 v_2^4 - 54\omega v_2^2 - 54\omega c_s^4 + 4\omega^3 v_2^4 - 4\omega^3 v_2^2 - \omega^3 c_s^4 - 36v_2^2 c_s^2 + 12\omega^3 v_2^2 c_s^2 + 54\omega v_2^2 c_s^2 + 20\omega^2 c_s^4 + 26\omega^2 v_2^2 + 36c_s^4 + 36v_2^2 + 54\omega v_2^4 + 36\omega c_s^2 \\
C_6 &= 12 + 404\omega^2 v_2^2 c_s^2 - 132c_s^2 + 144v_2^4 - 78\omega^2 c_s^2 + 90\omega^2 v_2^4 - 18\omega + 234\omega v_2^2 - 216\omega c_s^4 - 9\omega^3 v_2^4 + 6\omega^3 c_s^2 + 8\omega^2 + 10\omega^3 v_2^2 - 5\omega^3 c_s^4 - \omega^3 + 672v_2^2 c_s^2 - 34\omega^3 v_2^2 c_s^2 - 1008\omega v_2^2 c_s^2 + 82\omega^2 c_s^4 - 98\omega^2 v_2^2 + 144c_s^4 - 156v_2^2 - 216\omega v_2^4 + 198\omega c_s^2 \\
C_7 &= 12 + 252\omega^2 v_2^2 c_s^2 - 36c_s^2 + 504v_2^4 - 22\omega^2 c_s^2 + 310\omega^2 v_2^4 - 18\omega + 378\omega v_2^2 - 36\omega c_s^4 - 29\omega^3 v_2^4 + 2\omega^3 c_s^2 + 8\omega^2 + 14\omega^3 v_2^2 - \omega^3 c_s^4 - \omega^3 + 432v_2^2 c_s^2 - 18\omega^3 v_2^2 c_s^2 - 648\omega v_2^2 c_s^2 + 14\omega^2 c_s^4 - 154\omega^2 v_2^2 + 24c_s^4 - 252v_2^2 - 756\omega v_2^4 + 54\omega c_s^2 \\
C_8 &= -42\omega^2 v_2^2 c_s^2 - 24c_s^2 - 36v_2^4 - 12\omega^2 c_s^2 - 26\omega^2 v_2^4 - 54\omega v_2^2 - 54\omega c_s^4 + 4\omega^3 v_2^4 - 4\omega^3 v_2^2 - \omega^3 c_s^4 - 36v_2^2 c_s^2 + 12\omega^3 v_2^2 c_s^2 + 54\omega v_2^2 c_s^2 + 20\omega^2 c_s^4 + 26\omega^2 v_2^2 + 36c_s^4 + 36v_2^2 + 54\omega v_2^4 + 36\omega c_s^2 \\
C_9 &= 108\omega v_1 v_3 c_s^2 + 108\omega v_2 v_1 c_s^2 + 42\omega^2 v_2 v_1^2 v_3^2 - 108\omega v_2 v_1^2 c_s^2 - 42\omega^2 v_2^2 v_1 v_3^2 + 42\omega^2 v_2 v_3^2 c_s^2 - 4\omega^2 v_2 c_s^4 + 72v_2 v_1^2 v_3^2 - 3\omega^3 v_2 v_3^2 c_s^2 + 3\omega^3 v_2^2 v_1 v_3^2 - 3\omega^3 v_2 v_1^2 v_3^2 + 72v_2 v_3^2 c_s^2 - 72v_2^2 v_1 v_3^2 + 2\omega^3 v_2 c_s^4 - 42\omega^2 v_2^2 v_1 c_s^2 - 108\omega v_2 v_1^2 v_3^2 - 42\omega^2 v_1 v_3^2 c_s^2 - 108\omega v_2 v_3^2 c_s^2 + 42\omega^2 v_2 v_1^2 c_s^2 + 108\omega v_2^2 v_1 v_3^2 - 72v_1 v_3^2 c_s^2 - 3\omega^3 v_2 v_1^2 c_s^2 - 72v_2^2 v_1 c_s^2 + 3\omega^3 v_1 v_3^2 c_s^2 + 72v_2 v_1^2 c_s^2 + 3\omega^3 v_2^2 v_1 c_s^2 \\
C_{10} &= 36\omega v_3^2 c_s^2 - 14\omega^2 v_2^2 c_s^2 + \omega^3 v_2^2 v_3^2 + 48v_2 v_1 c_s^2 - 24v_2^2 v_3^2 - 2\omega^3 v_2 v_1 c_s^2 + 28\omega^2 v_2 v_1 c_s^2 - 24v_3^2 c_s^2 - 72\omega v_2 v_1 v_3^2 + \omega^3 v_3^2 c_s^2 + 36\omega v_2^2 v_3^2 - 2\omega^3 v_2 v_1 v_3^2 + 48v_2 v_1 v_3^2 - 24v_2^2 c_s^2 - 14\omega^2 v_2^2 v_3^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 72\omega v_2 v_1 c_s^2 - 14\omega^2 v_3^2 c_s^2 + 28\omega^2 v_2 v_1 v_3^2 \\
C_{11} &= -36\omega v_3^2 c_s^2 - 48v_2 v_1 c_s^2 + 12\omega c_s^4 - 36\omega v_1^2 v_3^2 + 2\omega^3 v_2 v_1 c_s^2 + 24v_1^2 v_3^2 + 14\omega^2 v_1^2 c_s^2 - \omega^3 v_1^2 v_3^2 - 28\omega^2 v_2 v_1 c_s^2 + 24v_3^2 c_s^2 + 72\omega v_2 v_1 v_3^2 - \omega^3 v_3^2 c_s^2 + 2\omega^3 v_2 v_1 v_3^2 - 36\omega v_1^2 c_s^2 - 48v_2 v_1 v_3^2 + 72\omega v_2 v_1 c_s^2 + 14\omega^2 v_3^2 c_s^2 - 4\omega^2 c_s^4 - 8c_s^4 + 14\omega^2 v_1^2 v_3^2 - \omega^3 v_1^2 c_s^2 - 28\omega^2 v_2 v_1 v_3^2 + 24v_1^2 c_s^2 \\
C_{12} &= \omega^3 v_1 c_s^2 + 14\omega^2 v_2 v_1^2 - 24v_1 c_s^2 - 36\omega v_2 c_s^2 - 24v_2^2 v_1 + \omega^3 v_2^2 v_1 + 36\omega v_2^2 v_1 + 24v_2 c_s^2 - \omega^3 v_2 c_s^2 + 36\omega v_1 c_s^2 - 14\omega^2 v_2^2 v_1 - \omega^3 v_2 v_1^2 - 14\omega^2 v_1 c_s^2 + 24v_2 v_1^2 - 36\omega v_2 v_1^2 + 14\omega^2 v_2^2 c_s^2 \\
C_{13} &= -14\omega^2 v_2^2 v_3 c_s^2 - 36\omega v_1 v_3^2 c_s^2 - 36\omega v_2^2 v_1 c_s^2 + 14\omega^2 v_2^2 v_1 v_3^2 + 36\omega v_2^2 v_1^2 v_3 + 36\omega v_1^2 v_3 c_s^2 - \omega^3 v_2^2 v_1 v_3^2 - 24v_2^2 v_3 c_s^2 + 24v_2^2 v_1 v_3^2 + \omega^3 v_2^2 v_3 c_s^2 + 14\omega^2 v_2^2 v_1 c_s^2 + 36\omega v_2^2 v_3 c_s^2 + 14\omega^2 v_1 v_3^2 c_s^2 - 14\omega^2 v_2^2 v_1^2 v_3 - 14\omega^2 v_1^2 v_3 c_s^2 - 36\omega v_2^2 v_1 v_3^2 + 24v_1 v_3^2 c_s^2 + \omega^3 v_1^2 v_3 c_s^2 + 24v_2^2 v_1 c_s^2 + \omega^3 v_2^2 v_1^2 v_3 - \omega^3 v_1 v_3^2 c_s^2 - 24v_1^2 v_3 c_s^2 - \omega^3 v_2^2 v_1 c_s^2 - 24v_2^2 v_1^2 v_3 \\
C_{14} &= -216\omega v_3^2 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 6\omega^3 v_2^2 v_3^2 + 12\omega^3 v_1 v_3 c_s^2 - 288v_2^2 v_1 v_3 + 144v_2^2 v_3^2 + 54\omega c_s^4 - 288v_1 v_3 c_s^2 + 12\omega^3 v_2^2 v_1 v_3 - 168\omega^2 v_2^2 v_1 v_3 + 144v_3^2 c_s^2 - 6\omega^3 v_3^2 c_s^2 - 216\omega v_2^2 v_3^2 - 168\omega^2 v_1 v_3 c_s^2 - \omega^3 c_s^4 + 144v_2^2 c_s^2 + 84\omega^2 v_2^2 v_3^2 - 6\omega^3 v_2^2 c_s^2 - 216\omega v_2^2 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 + 432\omega v_2^2 v_1 v_3 - 36c_s^4 + 432\omega v_1 v_3 c_s^2 \\
C_{15} &= 14\omega^2 v_1 v_3^2 - \omega^3 v_1 c_s^2 + 24v_1 c_s^2 - 14\omega^2 v_3 c_s^2 + \omega^3 v_1^2 v_3 - 24v_1^2 v_3 + 36\omega v_1^2 v_3 - 36\omega v_1 c_s^2 - 24v_3 c_s^2 - 14\omega^2 v_1^2 v_3 + \omega^3 v_3 c_s^2 + 24v_1 v_3^2 + 14\omega^2 v_1 c_s^2 - \omega^3 v_1 v_3^2 - 36\omega v_1 v_3^2 + 36\omega v_3 c_s^2 \\
C_{16} &= -14\omega^2 v_2^2 c_s^2 - 2\omega^3 v_1 v_3 c_s^2 + 48v_2^2 v_1 v_3 + 48v_1 v_3 c_s^2 - 2\omega^3 v_2^2 v_1 v_3 + 36\omega v_2^2 v_1^2 + \omega^3 v_2^2 v_1^2 + 28\omega^2 v_2^2 v_1 v_3 - 24v_2^2 v_1^2 - 14\omega^2 v_1^2 c_s^2 + 28\omega^2 v_1 v_3 c_s^2 + 36\omega v_1^2 c_s^2 - 24v_2^2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 72\omega v_2^2 v_1 v_3 - 72\omega v_1 v_3 c_s^2 + \omega^3 v_1^2 c_s^2 - 24v_1^2 c_s^2 - 14\omega^2 v_2^2 v_1^2 \\
C_{17} &= 24 - 72c_s^2 - 46\omega^2 c_s^2 - 36\omega + 36\omega v_2^2 + 5\omega^3 c_s^2 + 14\omega^2 + \omega^3 v_2^2 - \omega^3 - 14\omega^2 v_2^2 - 24v_2^2 + 108\omega c_s^2 \\
C_{18} &= 24 - 72c_s^2 - 42\omega^2 c_s^2 - 36\omega + 3\omega^3 c_s^2 + 36\omega v_3^2 + 14\omega^2 - \omega^3 - 14\omega^2 v_3^2 - 24v_3^2 + \omega^3 v_3^2 + 108\omega c_s^2 \\
C_{19} &= 216\omega v_3^2 c_s^2 - 24c_s^2 - 14\omega^2 c_s^2 + 3\omega^3 v_3^4 - 72\omega c_s^4 + \omega^3 c_s^2 - 108\omega v_3^2 - 144v_3^2 c_s^2 - 72v_3^4 + 6\omega^3 v_3^2 c_s^2 - 42\omega^2 v_3^4 - 3\omega^3 c_s^4 + 108\omega v_3^4 + 42\omega^2 v_3^2 + 72v_3^2 - 84\omega^2 v_3^2 c_s^2 + 30\omega^2 c_s^4 + 48c_s^4 - 3\omega^3 v_3^2 + 36\omega c_s^2
\end{aligned}$$

2.1.5 Conservation of momentum: ρv_3



attached text file: output_d3q27_nse_srt_symbolic_pde_03.txt

$$\begin{aligned}
& v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{\delta_1 v_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_1 v_3}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho \delta_1 v_1}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_2 \delta_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_1 v_3}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\rho v_2 \delta_1}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\
& \frac{2\rho \delta_1 v_3}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega) \frac{\delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (-2 + 4c_s^2 + \omega - 3\omega v_3^2 + 6v_3^2 - 2\omega c_s^2) \frac{\delta_1^2}{\omega \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega) \frac{3\rho \delta_1^2 v_3}{\omega \delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega) \frac{\rho \delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\
& (-2 + \omega) \frac{\rho \delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega) \frac{\rho \delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega) \frac{\rho \delta_1^2 c_s^2}{2\omega \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + (-2 + 6c_s^2 + \omega - \omega v_3^2 + 2v_3^2 - 3\omega c_s^2) \frac{\delta_1^2 v_3}{2\omega \delta_t} \frac{\partial^2 \rho}{\partial x_3^2}
\end{aligned}$$

$$\begin{aligned}
& + (-2 + 2c_s^2 + \omega - 3\omega v_3^2 + 6v_3^2 - \omega c_s^2) \frac{\rho \delta_l^2}{2\omega \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + (-1 + 3c_s^2 + v_1^2) \frac{\delta_l^3 v_1 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3 v_3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& (6 + 6\omega v_1^2 - 18c_s^2 - 3\omega^2 c_s^2 - 6\omega + \omega^2 - \omega^2 v_1^2 - 6v_1^2 + 18\omega c_s^2) \frac{\rho \delta_l^3 v_1}{6\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{\rho \delta_l^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\rho \delta_l^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_l^3 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3 v_3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (6 - 18c_s^2 - 3\omega^2 c_s^2 - 6\omega + 6\omega v_2^2 + \omega^2 - \omega^2 v_2^2 - 6v_2^2 + 18\omega c_s^2) \frac{\rho v_2 \delta_l^3}{6\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega - \omega^2) \frac{\delta_l^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\
& \frac{\rho \delta_l^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 + 12\omega - \omega^2) \frac{\delta_l^3 c_s^4}{6\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{\rho \delta_l^3 v_3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (12 - 36c_s^2 - 11\omega^2 c_s^2 - 12\omega + 12\omega v_3^2 + 3\omega^2 - 3\omega^2 v_3^2 - 12v_3^2 + 36\omega c_s^2) \frac{\rho \delta_l^3 v_3}{12\omega^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
& (12 - 36c_s^2 - 11\omega^2 c_s^2 - 12\omega + 12\omega v_3^2 + 3\omega^2 - 3\omega^2 v_3^2 - 12v_3^2 + 36\omega c_s^2) \frac{\rho \delta_l^3 v_3}{12\omega^2 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-24 + 36c_s^2 + 5\omega^2 c_s^2 + 24\omega - 60\omega v_3^2 - 4\omega^2 + 11\omega^2 v_3^2 + 60v_3^2 - 36\omega c_s^2) \frac{\rho \delta_l^3 v_3}{6\omega^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (3\omega v_1^2 - 2c_s^2 + 6v_1^4 - \omega c_s^4 - 12\omega v_1^2 c_s^2 - 3\omega v_1^4 + 2c_s^4 + 24v_1^2 c_s^2 - 6v_1^2 + \omega c_s^2) \frac{\delta_l^4 v_3}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 - 5\omega v_1^2 + 6c_s^2 + 2\omega + 10v_1^2 - 3\omega c_s^2) \frac{\rho \delta_l^4 v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_2 \frac{\rho \delta_l^4}{24\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + \\
& (2 + \omega v_1^2 - 6c_s^2 - \omega - 2v_1^2 + 3\omega c_s^2) \frac{\rho \delta_l^4 v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega) \frac{\delta_l^4 v_3 c_s^2}{6\omega \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + (-2 + 3\omega - \omega^2) \frac{\rho \delta_l^4 c_s^4}{\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (2 - 6c_s^2 - \omega + \omega v_2^2 - 2v_2^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_3}{12\omega \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-2c_s^2 + 6v_2^4 + 3\omega v_2^2 - \omega c_s^4 + 24v_2^2 c_s^2 - 12\omega v_2^2 c_s^2 + 2c_s^4 - 6v_2^2 - 3\omega v_2^2 + \omega c_s^2) \frac{\delta_l^4 v_3}{24\omega \delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 2\omega - 5\omega v_2^2 + 10v_2^2 - 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_3}{12\omega \delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_3 \frac{\rho \delta_l^4}{24\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^4} + C_4 \frac{\delta_l^4 v_1 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + \\
& (-12 - 54\omega v_1^2 + 2\omega^2 c_s^2 + 18\omega - \omega^3 c_s^2 - 6\omega^2 + 18\omega^2 v_1^2 + 36v_1^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + \\
& (2 + \omega v_1^2 - 6c_s^2 - \omega - 2v_1^2 + 3\omega c_s^2) \frac{\rho \delta_l^4 v_1 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + C_5 \frac{\delta_l^4}{2\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_6 \frac{\rho \delta_l^4}{2\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_7 \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_8 \frac{\rho \delta_l^4 v_3}{\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_9 \frac{\delta_l^4}{2\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{10} \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{11} \frac{\rho v_2 \delta_l^4}{\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{12} \frac{\rho \delta_l^4}{2\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{13} \frac{v_2 \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + (-12 + 2\omega^2 c_s^2 + 18\omega - 54\omega v_2^2 - \omega^3 c_s^2 - 6\omega^2 + 18\omega^2 v_2^2 + 36v_2^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& (2 - 6c_s^2 - \omega + \omega v_2^2 - 2v_2^2 + 3\omega c_s^2) \frac{\rho v_2 \delta_l^4 v_3}{12\omega \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{14} \frac{\delta_l^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + \\
& (-24 + 12c_s^2 + 8\omega^2 c_s^2 + 36\omega - \omega^3 c_s^2 - 108\omega v_3^2 - 12\omega^2 + 36\omega^2 v_3^2 + 72v_3^2 - 18\omega c_s^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + C_{15} \frac{\delta_l^4 v_3 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + \\
& (-24 + 12c_s^2 + 8\omega^2 c_s^2 + 36\omega - \omega^3 c_s^2 - 108\omega v_3^2 - 12\omega^2 + 36\omega^2 v_3^2 + 72v_3^2 - 18\omega c_s^2) \frac{\rho \delta_l^4 c_s^2}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{16} \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{17} \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{18} \frac{\delta_l^4 v_3}{12\omega^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{19} \frac{\rho \delta_l^4}{12\omega^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -144\omega v_3^2 c_s^2 - 12c_s^2 - \omega^2 c_s^2 - 12\omega c_s^4 + 36\omega v_3^2 + 144v_3^2 c_s^2 + 36v_3^4 + 7\omega^2 v_3^4 - 36\omega v_3^4 - 7\omega^2 v_3^2 - 36v_3^2 + 24\omega^2 v_3^2 c_s^2 + \omega^2 c_s^4 + 12c_s^4 + 12\omega c_s^2 \\
C_2 &= -108\omega v_1^2 - 24c_s^2 - 14\omega^2 c_s^2 - 72v_1^4 - 72\omega c_s^4 - 42\omega^2 v_1^4 + \omega^3 c_s^2 - 84\omega^2 v_1^2 c_s^2 + 3\omega^3 v_1^4 - 3\omega^3 c_s^4 + 216\omega v_1^2 c_s^2 - 3\omega^3 v_1^2 + 30\omega^2 c_s^4 + 108\omega v_1^4 + \\
& 48c_s^4 + 6\omega^3 v_1^2 c_s^2 + 42\omega^2 v_1^2 - 144v_1^2 c_s^2 + 72v_1^2 + 36\omega c_s^2 \\
C_3 &= -84\omega^2 v_2^2 c_s^2 - 24c_s^2 - 72v_2^4 - 14\omega^2 c_s^2 - 42\omega^2 v_2^4 - 108\omega v_2^2 - 72\omega c_s^4 + 3\omega^3 v_2^4 + \omega^3 c_s^2 - 3\omega^3 v_2^2 - 3\omega^3 c_s^4 - 144v_2^2 c_s^2 + 6\omega^3 v_2^2 c_s^2 + \\
& 216\omega v_2^2 c_s^2 + 30\omega^2 c_s^4 + 42\omega^2 v_2^2 + 48c_s^4 + 72v_2^2 + 108\omega v_2^2 + 36\omega c_s^2 \\
C_4 &= 24 + 36\omega v_1^2 - 72c_s^2 - 42\omega^2 c_s^2 - 36\omega + 3\omega^3 c_s^2 + 14\omega^2 - \omega^3 + \omega^3 v_1^2 - 14\omega^2 v_1^2 - 24v_1^2 + 108\omega c_s^2 \\
C_5 &= 36\omega v_1 v_3^2 c_s^2 + 36\omega v_2^2 v_1 c_s^2 + 14\omega^2 v_2 v_1^2 v_3^2 - 36\omega v_2 v_1^2 c_s^2 - 14\omega^2 v_2^2 v_1 v_3^2 + 14\omega^2 v_2 v_3^2 c_s^2 + 24v_2 v_1^2 v_3^2 - \omega^3 v_2 v_3^2 c_s^2 + \omega^3 v_2^2 v_1 v_3^2 - \omega^3 v_2 v_1^2 v_3^2 + \\
& 24v_2 v_3^2 c_s^2 - 24v_2^2 v_1 v_3^2 - 14\omega^2 v_2^2 v_1 c_s^2 - 36\omega v_2 v_1^2 v_3^2 - 14\omega^2 v_1 v_3^2 c_s^2 - 36\omega v_2 v_3^2 c_s^2 + 14\omega^2 v_2 v_1^2 c_s^2 + 36\omega v_2^2 v_1 v_3^2 - 24v_1 v_3^2 c_s^2 - \omega^3 v_2 v_1^2 c_s^2 - \\
& 24v_2^2 v_1 c_s^2 + \omega^3 v_1 v_3^2 c_s^2 + 24v_2 v_1^2 c_s^2 + \omega^3 v_2^2 v_1 c_s^2 \\
C_6 &= 36\omega v_3^2 c_s^2 - 14\omega^2 v_2^2 c_s^2 + \omega^3 v_2^2 v_3^2 + 48v_2 v_1 c_s^2 - 24v_2^2 v_3^2 - 2\omega^3 v_2 v_1 c_s^2 + 28\omega^2 v_2 v_1 c_s^2 - 24v_3^2 c_s^2 - 72\omega v_2 v_1 v_3^2 + \omega^3 v_3^2 c_s^2 + 36\omega v_2^2 v_3^2 - \\
& 2\omega^3 v_2 v_1 v_3^2 + 48v_2 v_1 v_3^2 - 24v_2^2 c_s^2 - 14\omega^2 v_2^2 v_3^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 72\omega v_2 v_1 c_s^2 - 14\omega^2 v_3^2 c_s^2 + 28\omega^2 v_2 v_1 v_3^2 \\
C_7 &= -216\omega v_3^2 c_s^2 - 288v_2 v_1 c_s^2 + 54\omega c_s^4 - 216\omega v_1^2 v_3^2 + 12\omega^3 v_2 v_1 c_s^2 + 144v_1^2 v_3^2 + 84\omega^2 v_1^2 c_s^2 - 6\omega^3 v_1^2 v_3^2 - 168\omega^2 v_2 v_1 c_s^2 + 144v_3^2 c_s^2 + 432\omega v_2 v_1 v_3^2 - \\
& 6\omega^3 v_3^2 c_s^2 + 12\omega^3 v_2 v_1 v_3^2 - \omega^3 c_s^4 - 216\omega v_1^2 c_s^2 - 288v_2 v_1 v_3^2 + 432\omega v_2 v_1 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 - 36c_s^4 + 84\omega^2 v_1^2 v_3^2 - 6\omega^3 v_1^2 c_s^2 - 168\omega^2 v_2 v_1 v_3^2 + 144v_1^2 c_s^2
\end{aligned}$$

$$C_8 = \omega^3 v_1 c_s^2 + 14\omega^2 v_2 v_1^2 - 24v_1 c_s^2 - 36\omega v_2 c_s^2 - 24v_2^2 v_1 + \omega^3 v_2^2 v_1 + 36\omega v_2^2 v_1 + 24v_2 c_s^2 - \omega^3 v_2 c_s^2 + 36\omega v_1 c_s^2 - 14\omega^2 v_2^2 v_1 - \omega^3 v_2 v_1^2 - 14\omega^2 v_1 c_s^2 + 24v_2 v_1^2 - 36\omega v_2 v_1^2 + 14\omega^2 v_2 c_s^2$$

$$C_9 = -14\omega^2 v_2^2 v_3 c_s^2 - 36\omega v_1 v_3^2 c_s^2 - 36\omega v_2^2 v_1 c_s^2 + 14\omega^2 v_2^2 v_1 v_3 + 36\omega v_2^2 v_1^2 v_3 + 36\omega v_1^2 v_3 c_s^2 - \omega^3 v_2^2 v_1 v_3 - 24v_2^2 v_3 c_s^2 + 24v_2^2 v_1 v_3 + \omega^3 v_2^2 v_3 c_s^2 + 14\omega^2 v_2^2 v_1 c_s^2 + 36\omega v_2^2 v_3 c_s^2 + 14\omega^2 v_1 v_3^2 c_s^2 - 14\omega^2 v_2^2 v_1^2 v_3 - 14\omega^2 v_1^2 v_3 c_s^2 - 36\omega v_2^2 v_1 v_3 + 24v_1 v_3^2 c_s^2 + \omega^3 v_1^2 v_3 c_s^2 + 24v_2^2 v_1 c_s^2 + \omega^3 v_2^2 v_1^2 v_3 - \omega^3 v_1 v_3^2 c_s^2 - 24v_1^2 v_3 c_s^2 - \omega^3 v_2^2 v_1 c_s^2 - 24v_2^2 v_1^2 v_3$$

$$C_{10} = -216\omega v_3^2 c_s^2 + 84\omega^2 v_2^2 c_s^2 - 6\omega^3 v_2^2 v_3^2 + 12\omega^3 v_1 v_3 c_s^2 - 288v_2^2 v_1 v_3 + 144v_2^2 v_3^2 + 54\omega c_s^4 - 288v_1 v_3 c_s^2 + 12\omega^3 v_2^2 v_1 v_3 - 168\omega^2 v_2^2 v_1 v_3 + 144v_3^2 c_s^2 - 6\omega^3 v_3^2 c_s^2 - 216\omega v_2^2 v_3 - 168\omega^2 v_1 v_3 c_s^2 - \omega^3 c_s^4 + 144v_2^2 c_s^2 + 84\omega^2 v_2^2 v_3^2 - 6\omega^3 v_2^2 c_s^2 - 216\omega v_2^2 c_s^2 + 84\omega^2 v_3^2 c_s^2 - 16\omega^2 c_s^4 + 432\omega v_2^2 v_1 v_3 - 36c_s^4 + 432\omega v_1 v_3 c_s^2$$

$$C_{11} = 14\omega^2 v_1 v_3^2 - \omega^3 v_1 c_s^2 + 24v_1 c_s^2 - 14\omega^2 v_3 c_s^2 + \omega^3 v_1^2 v_3 - 24v_1^2 v_3 + 36\omega v_1^2 v_3 - 36\omega v_1 c_s^2 - 24v_3 c_s^2 - 14\omega^2 v_1^2 v_3 + \omega^3 v_3 c_s^2 + 24v_1 v_3^2 + 14\omega^2 v_1 c_s^2 - \omega^3 v_1 v_3^2 - 36\omega v_1 v_3^2 + 36\omega v_3 c_s^2$$

$$C_{12} = -14\omega^2 v_2^2 c_s^2 - 2\omega^3 v_1 v_3 c_s^2 + 48v_2^2 v_1 v_3 + 48v_1 v_3 c_s^2 - 2\omega^3 v_2^2 v_1 v_3 + 36\omega v_2^2 v_1^2 + \omega^3 v_2^2 v_1^2 + 28\omega^2 v_2^2 v_1 v_3 - 24v_2^2 v_1^2 - 14\omega^2 v_1^2 c_s^2 + 28\omega^2 v_1 v_3 c_s^2 + 36\omega v_1^2 c_s^2 - 24v_2^2 c_s^2 + \omega^3 v_2^2 c_s^2 + 36\omega v_2^2 c_s^2 - 72\omega v_2^2 v_1 v_3 - 72\omega v_1 v_3 c_s^2 + \omega^3 v_1^2 c_s^2 - 24v_1^2 c_s^2 - 14\omega^2 v_2^2 v_1^2$$

$$C_{13} = 24 - 72c_s^2 - 42\omega^2 c_s^2 - 36\omega + 36\omega v_2^2 + 3\omega^3 c_s^2 + 14\omega^2 + \omega^3 v_2^2 - \omega^3 - 14\omega^2 v_2^2 - 24v_2^2 + 108\omega c_s^2$$

$$C_{14} = 24 - 72c_s^2 - 46\omega^2 c_s^2 - 36\omega + 5\omega^3 c_s^2 + 36\omega v_3^2 + 14\omega^2 - \omega^3 - 14\omega^2 v_3^2 - 24v_3^2 + \omega^3 v_3^2 + 108\omega c_s^2$$

$$C_{15} = 24 - 72c_s^2 - 46\omega^2 c_s^2 - 36\omega + 5\omega^3 c_s^2 + 36\omega v_3^2 + 14\omega^2 - \omega^3 - 14\omega^2 v_3^2 - 24v_3^2 + \omega^3 v_3^2 + 108\omega c_s^2$$

$$C_{16} = 54\omega v_3^2 c_s^2 - 24c_s^2 - 12\omega^2 c_s^2 + 4\omega^3 v_3^4 - 54\omega c_s^4 - 54\omega v_3^2 - 36v_3^2 c_s^2 - 36v_3^4 + 12\omega^3 v_3^2 c_s^2 - 26\omega^2 v_3^4 - \omega^3 c_s^4 + 54\omega v_3^4 + 26\omega^2 v_3^2 + 36v_3^2 - 42\omega^2 v_3^2 c_s^2 + 20\omega^2 c_s^4 + 36c_s^4 - 4\omega^3 v_3^2 + 36\omega c_s^2$$

$$C_{17} = 54\omega v_3^2 c_s^2 - 24c_s^2 - 12\omega^2 c_s^2 + 4\omega^3 v_3^4 - 54\omega c_s^4 - 54\omega v_3^2 - 36v_3^2 c_s^2 - 36v_3^4 + 12\omega^3 v_3^2 c_s^2 - 26\omega^2 v_3^4 - \omega^3 c_s^4 + 54\omega v_3^4 + 26\omega^2 v_3^2 + 36v_3^2 - 42\omega^2 v_3^2 c_s^2 + 20\omega^2 c_s^4 + 36c_s^4 - 4\omega^3 v_3^2 + 36\omega c_s^2$$

$$C_{18} = 12 - 1008\omega v_3^2 c_s^2 - 132c_s^2 - 78\omega^2 c_s^2 - 9\omega^3 v_3^4 - 18\omega - 216\omega c_s^4 + 6\omega^3 c_s^2 + 234\omega v_3^2 + 672v_3^2 c_s^2 + 144v_3^4 - 34\omega^3 v_3^2 c_s^2 + 90\omega^2 v_3^4 + 8\omega^2 - 5\omega^3 c_s^4 - 216\omega v_3^4 - \omega^3 - 98\omega^2 v_3^2 - 156v_3^2 + 404\omega^2 v_3^2 c_s^2 + 82\omega^2 c_s^4 + 144c_s^4 + 10\omega^3 v_3^2 + 198\omega c_s^2$$

$$C_{19} = 12 - 648\omega v_3^2 c_s^2 - 36c_s^2 - 22\omega^2 c_s^2 - 29\omega^3 v_3^4 - 18\omega - 36\omega c_s^4 + 2\omega^3 c_s^2 + 378\omega v_3^2 + 432v_3^2 c_s^2 + 504v_3^4 - 18\omega^3 v_3^2 c_s^2 + 310\omega^2 v_3^4 + 8\omega^2 - \omega^3 c_s^4 - 756\omega v_3^4 - \omega^3 - 154\omega^2 v_3^2 - 252v_3^2 + 252\omega^2 v_3^2 c_s^2 + 14\omega^2 c_s^4 + 24c_s^4 + 14\omega^3 v_3^2 + 54\omega c_s^2$$

2.2 MRT

2.2.1 Definitions

Collision operator C :

$$C(f) = \mathbf{M}^{-1} \mathbf{S} \left(\boldsymbol{\mu}^{(eq)} - \mathbf{M} f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \dots, \omega_{27}),$$

$$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2).$$

2.2.2 Conservation of mass: ρ



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$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{\delta_1 v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_1 \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_1 \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + v_1^2 + 3c_s^2) \frac{\delta_1^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & (-1 + 3v_1^2 + c_s^2) \frac{\delta_1^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\delta_1^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\delta_1^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{\delta_1^3 v_2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\delta_1^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\ & \frac{\delta_1^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\delta_1^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\delta_1^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\delta_1^3 c_s^2 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{\delta_1^3 v_3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\delta_1^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\ & + (-12\omega_9 c_s^2 v_1^2 + 3\omega_9 v_1^2 - 6v_1^2 + \omega_9 c_s^2 - 2c_s^2 + 2c_s^4 - \omega_9 c_s^4 + 24c_s^2 v_1^2 + 6v_1^4 - 3\omega_9 v_1^4) \frac{\delta_1^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 + 2\omega_9 - 5\omega_9 v_1^2 + 10v_1^2 - 3\omega_9 c_s^2 + 6c_s^2) \frac{\delta_1^4 \rho v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + (\omega_9 - \omega_9 v_1^2 - \omega_{12} - 3\omega_9 c_s^2 + 3\omega_{12} c_s^2 + \omega_{12} v_1^2) \frac{\delta_1^4 v_1 v_2}{4\omega_9 \omega_{12} \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} \\ & + (\omega_9 - 3\omega_9 v_1^2 - \omega_{12} - \omega_9 c_s^2 + \omega_{12} c_s^2 + 3\omega_{12} v_1^2) \frac{\delta_1^4 \rho v_2}{4\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + (\omega_{12} v_1^2 \omega_5 - \omega_9 \omega_{12} \omega_5 - 3\omega_9 c_s^2 \omega_5 + 3\omega_9 \omega_5 + \end{aligned}$$

$$\begin{aligned}
& 3\omega_9\omega_{12}c_s^2\omega_5 - 6\omega_9\omega_{12}c_s^2 + \omega_9\omega_{12}v_1^2\omega_5 - 3\omega_9v_1^2\omega_5 + 3\omega_{12}c_s^2\omega_5 - \omega_{12}\omega_5) \frac{\delta_t^4 \rho v_1}{12\omega_9\omega_{12}\delta_t\omega_5} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_5) \frac{\delta_t^4 c_s^4}{6\delta_t\omega_5} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} \\
& + (-\omega_{12} + \omega_5) \frac{\delta_t^4 c_s^2 \rho v_1}{2\omega_{12}\delta_t\omega_5} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + (-\omega_{15} + \omega_5) \frac{\delta_t^4 c_s^2 \rho v_2}{2\omega_{15}\delta_t\omega_5} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\
& (-\omega_{15} + 3\omega_{15}c_s^2 + \omega_{15}v_2^2 + \omega_{10} - 3c_s^2\omega_{10} - \omega_{10}v_2^2) \frac{\delta_t^4 v_1 v_2}{4\omega_{15}\delta_t\omega_{10}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + (\omega_{15}v_2^2\omega_5 + 3\omega_{15}c_s^2\omega_{10}\omega_5 - 3\omega_{10}v_2^2\omega_5 - \\
& \omega_{15}\omega_5 + \omega_{15}\omega_{10}v_2^2\omega_5 - \omega_{15}\omega_{10}\omega_5 + 3\omega_{15}c_s^2\omega_5 - 6\omega_{15}c_s^2\omega_{10} + 3\omega_{10}\omega_5 - 3c_s^2\omega_{10}\omega_5) \frac{\delta_t^4 \rho v_2}{12\omega_{15}\delta_t\omega_{10}\omega_5} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-\omega_{15} + \omega_{15}c_s^2 + 3\omega_{15}v_2^2 + \omega_{10} - c_s^2\omega_{10} - 3\omega_{10}v_2^2) \frac{\delta_t^4 \rho v_1}{4\omega_{15}\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\
& (-c_s^4\omega_{10} - 6v_2^2 - 3\omega_{10}v_2^4 - 2c_s^2 + 2c_s^4 + c_s^2\omega_{10} + 6v_2^4 + 3\omega_{10}v_2^2 - 12c_s^2\omega_{10}v_2^2 + 24c_s^2v_2^2) \frac{\delta_t^4}{24\delta_t\omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 10v_2^2 + 6c_s^2 + 2\omega_{10} - 3c_s^2\omega_{10} - 5\omega_{10}v_2^2) \frac{\delta_t^4 \rho v_2}{12\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (\omega_9 - \omega_9v_1^2 - 3\omega_9c_s^2 + v_1^2\omega_{13} - \omega_{13} + 3c_s^2\omega_{13}) \frac{\delta_t^4 v_1 v_3}{4\omega_9\delta_t\omega_{13}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& (\omega_9 - 3\omega_9v_1^2 - \omega_9c_s^2 + 3v_1^2\omega_{13} - \omega_{13} + c_s^2\omega_{13}) \frac{\delta_t^4 \rho v_3}{4\omega_9\delta_t\omega_{13}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + (\omega_6v_1^2\omega_{13} - 3\omega_9\omega_6v_1^2 - 6\omega_9c_s^2\omega_{13} - 3\omega_9\omega_6c_s^2 - \\
& \omega_9\omega_6\omega_{13} + 3\omega_9\omega_6c_s^2\omega_{13} - \omega_6\omega_{13} + \omega_9\omega_6v_1^2\omega_{13} + 3\omega_6c_s^2\omega_{13} + 3\omega_9\omega_6) \frac{\delta_t^4 \rho v_1}{12\omega_9\omega_6\delta_t\omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-\omega_8 + \omega_5) \frac{\delta_t^4 c_s^2 \rho v_3}{2\delta_t\omega_8\omega_5} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + (\omega_6 - \omega_8) \frac{\delta_t^4 c_s^2 \rho v_2}{2\omega_6\delta_t\omega_8} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + (-\omega_8 + \omega_5) \frac{\delta_t^4 c_s^2 \rho v_3}{2\delta_t\omega_8\omega_5} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (\omega_7 - \omega_8) \frac{\delta_t^4 c_s^2 \rho v_1}{2\delta_t\omega_7\omega_8} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (\omega_{16}v_2^2 - \omega_{16} + \omega_{10} - 3c_s^2\omega_{10} + 3c_s^2\omega_{16} - \omega_{10}v_2^2) \frac{\delta_t^4 v_2 v_3}{4\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + \\
& (3\omega_{16}v_2^2 - \omega_{16} + \omega_{10} - c_s^2\omega_{10} + c_s^2\omega_{16} - 3\omega_{10}v_2^2) \frac{\delta_t^4 \rho v_3}{4\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + (-3\omega_{10}v_2^2\omega_7 - 6c_s^2\omega_{16}\omega_{10} + 3c_s^2\omega_{16}\omega_{10}\omega_7 - \\
& \omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7 + 3c_s^2\omega_{16}\omega_7 + 3\omega_{10}\omega_7 - 3c_s^2\omega_{10}\omega_7 + \omega_{16}\omega_{10}v_2^2\omega_7 + \omega_{16}v_2^2\omega_7) \frac{\delta_t^4 \rho v_2}{12\delta_t\omega_{16}\omega_{10}\omega_7} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{\delta_t^4 c_s^4}{6\omega_6\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (\omega_6 - \omega_{13}) \frac{\delta_t^4 c_s^2 \rho v_1}{2\omega_6\delta_t\omega_{13}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + (\omega_6 - \omega_{18}) \frac{\delta_t^4 c_s^2 \rho v_3}{2\omega_6\delta_t\omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + (\omega_6 - \omega_8) \frac{\delta_t^4 c_s^2 \rho v_2}{2\omega_6\delta_t\omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (\omega_7 - \omega_8) \frac{\delta_t^4 c_s^2 \rho v_1}{2\delta_t\omega_7\omega_8} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + (-2 + \omega_7) \frac{\delta_t^4 c_s^4}{6\delta_t\omega_7} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + (-\omega_{16} + \omega_7) \frac{\delta_t^4 c_s^2 \rho v_2}{2\delta_t\omega_{16}\omega_7} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + (-\omega_{19} + \omega_7) \frac{\delta_t^4 c_s^2 \rho v_3}{2\omega_{19}\delta_t\omega_7} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} \\
& + (-3c_s^2\omega_{11} - v_3^2\omega_{11} + 3c_s^2\omega_{18} + \omega_{11} - \omega_{18} + v_3^2\omega_{18}) \frac{\delta_t^4 v_1 v_3}{4\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + (-3\omega_6v_3^2\omega_{11} + 3\omega_6\omega_{11} - 3\omega_6c_s^2\omega_{11} + \\
& 3\omega_6c_s^2\omega_{11}\omega_{18} + \omega_6v_3^2\omega_{11}\omega_{18} - \omega_6\omega_{11}\omega_{18} - \omega_6\omega_{18} + \omega_6v_3^2\omega_{18} + 3\omega_6c_s^2\omega_{18} - 6c_s^2\omega_{11}\omega_{18}) \frac{\delta_t^4 \rho v_3}{12\omega_6\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (-c_s^2\omega_{11} - 3v_3^2\omega_{11} + c_s^2\omega_{18} + \omega_{11} - \omega_{18} + 3v_3^2\omega_{18}) \frac{\delta_t^4 \rho v_1}{4\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (-3c_s^2\omega_{11} + 3\omega_{19}c_s^2 - \omega_{19} - v_3^2\omega_{11} + \omega_{19}v_3^2 + \omega_{11}) \frac{\delta_t^4 v_2 v_3}{4\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + (\omega_{19}\omega_7v_3^2 - \omega_{19}\omega_7\omega_{11} - \omega_{19}\omega_7 + \\
& \omega_{19}\omega_7v_3^2\omega_{11} + 3\omega_7\omega_{11} - 3c_s^2\omega_7\omega_{11} - 6\omega_{19}c_s^2\omega_{11} + 3\omega_{19}c_s^2\omega_7\omega_{11} - 3\omega_7v_3^2\omega_{11} + 3\omega_{19}c_s^2\omega_7) \frac{\delta_t^4 \rho v_3}{12\omega_{19}\delta_t\omega_7\omega_{11}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-c_s^2\omega_{11} + \omega_{19}c_s^2 - \omega_{19} - 3v_3^2\omega_{11} + 3\omega_{19}v_3^2 + \omega_{11}) \frac{\delta_t^4 \rho v_2}{4\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& (c_s^2\omega_{11} + 24c_s^2v_3^2 + 6v_3^4 - 2c_s^2 + 3v_3^2\omega_{11} - 12c_s^2v_3^2\omega_{11} + 2c_s^4 - c_s^4\omega_{11} - 3v_3^4\omega_{11} - 6v_3^2) \frac{\delta_t^4}{24\delta_t\omega_{11}} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 - 3c_s^2\omega_{11} + 6c_s^2 - 5v_3^2\omega_{11} + 2\omega_{11} + 10v_3^2) \frac{\delta_t^4 \rho v_3}{12\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.2.3 Conservation of momentum: ρv_1



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$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_t}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\delta_t \rho v_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_t v_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_t \rho v_2}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\delta_t v_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_t \rho v_3}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\delta_t \rho v_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_9 - 3\omega_9v_1^2 + 6v_1^2 - 2\omega_9c_s^2 + 4c_s^2) \frac{\delta_t^2}{\omega_9\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\delta_t^2 \rho v_1}{\omega_9\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{\delta_t^2 c_s^2}{2\delta_t\omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_t^2 c_s^2}{2\delta_t\omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{\delta_t^2 c_s^2}{2\omega_6\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_t^2 c_s^2}{2\omega_6\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + \omega_9 - \omega_9v_1^2 + 2v_1^2 - 3\omega_9c_s^2 + 6c_s^2) \frac{\delta_t^2 v_1}{2\omega_9\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_9 - 3\omega_9v_1^2 + 6v_1^2 - \omega_9c_s^2 + 2c_s^2) \frac{\delta_t^2 \rho}{2\omega_9\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{\delta_t^2 c_s^2 \rho}{2\delta_t\omega_5} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{\delta_t^2 c_s^2 \rho}{2\delta_t\omega_5} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{\delta_t^2 c_s^2 \rho}{2\omega_6\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{\delta_t^2 c_s^2 \rho}{2\omega_6\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_t^3}{12\omega_9^2\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} +
\end{aligned}$$

$$\begin{aligned}
& (-24 + 24\omega_9 - 60\omega_9 v_1^2 + 60v_1^2 - 36\omega_9 c_s^2 + 36c_s^2 + 5\omega_9^2 c_s^2 + 11\omega_9^2 v_1^2 - 4\omega_9^2) \frac{\delta_l^3 \rho v_1}{6\omega_9^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{\delta_l^3 v_1 v_2}{\omega_9^2 \omega_{12} \delta_t \omega_5} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& C_3 \frac{\delta_l^3 \rho v_2}{\omega_9^2 \omega_{12} \delta_t \omega_5} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + C_4 \frac{\delta_l^3 \rho v_1}{12\omega_9^2 \omega_{12} \delta_t \omega_5^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + (-12 - \omega_5^2 + 12\omega_5) \frac{\delta_l^3 c_s^4}{6\delta_t \omega_5^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (12\omega_9 \omega_{12} \omega_5 + 12\omega_9 \omega_5 - 12\omega_9 \omega_5^2 + 12\omega_5^2 - \omega_9 \omega_{12} \omega_5^2 - 12\omega_9 \omega_{12} - 12\omega_{12} \omega_5) \frac{\delta_l^3 c_s^2 \rho v_1}{6\omega_9 \omega_{12} \delta_t \omega_5^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-2\omega_{15} - \omega_5^2 + \omega_{15} \omega_5 + 2\omega_5) \frac{\delta_l^3 c_s^2 \rho v_2}{\omega_{15} \delta_t \omega_5^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{\delta_l^3 v_1 v_2}{12\omega_{15} \delta_t \omega_{10} \omega_5} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\delta_l^3 \rho v_2}{6\omega_{15} \delta_t \omega_5^2} \frac{\partial^3 v_1}{\partial x_2^2} + C_7 \frac{\delta_l^3 \rho v_1}{12\omega_{15} \delta_t \omega_{10} \omega_5} \frac{\partial^3 v_2}{\partial x_2^2} + \\
& C_8 \frac{\delta_l^3 v_1 v_3}{\omega_9^2 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + C_9 \frac{\delta_l^3 \rho v_3}{\omega_9^2 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + C_{10} \frac{\delta_l^3 \rho v_1}{12\omega_9^2 \omega_6^2 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (\omega_6 \omega_8 \omega_5 + \omega_5^2 - \omega_8 \omega_5 - \omega_6 \omega_5^2 - \omega_6 \omega_8 + \omega_6 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_3}{\omega_6 \delta_t \omega_8 \omega_5^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (-\omega_6^2 \omega_5 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5 + \omega_6^2 - \omega_6 \omega_8 + \omega_6 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_2}{\omega_6^2 \delta_t \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + \\
& (\omega_6 \omega_8 \omega_5 + \omega_5^2 - \omega_8 \omega_5 - \omega_6 \omega_5^2 - \omega_6 \omega_8 + \omega_6 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_3}{\omega_6 \delta_t \omega_8 \omega_5^2} \frac{\partial^3 v_1}{\partial x_2^2 \partial x_3} + \\
& (-\omega_6 \omega_7 \omega_8 \omega_5 + 6\omega_6 \omega_8 \omega_5 - 6\omega_8 \omega_5 + 6\omega_6 \omega_7 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 - 6\omega_6 \omega_7 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_1}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-12 + 12\omega_6 - \omega_6^2) \frac{\delta_l^3 c_s^4}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (-12\omega_9 \omega_{13} + 12\omega_9 \omega_6 \omega_{13} - \omega_9 \omega_6^2 \omega_{13} - 12\omega_6 \omega_{13} - 12\omega_9 \omega_6^2 + 12\omega_6^2 + 12\omega_9 \omega_6) \frac{\delta_l^3 c_s^2 \rho v_1}{6\omega_9 \omega_6^2 \delta_t \omega_{13}} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
& (2\omega_6 - \omega_6^2 + \omega_6 \omega_{18} - 2\omega_{18}) \frac{\delta_l^3 c_s^2 \rho v_3}{\omega_6^2 \delta_t \omega_{18}} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + (-\omega_6^2 \omega_5 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5 + \omega_6^2 - \omega_6 \omega_8 + \omega_6 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_2}{\omega_6^2 \delta_t \omega_8 \omega_5} \frac{\partial^3 v_1}{\partial x_2 \partial x_3^2} + \\
& (-\omega_6 \omega_7 \omega_8 \omega_5 + 6\omega_6 \omega_8 \omega_5 - 6\omega_8 \omega_5 + 6\omega_6 \omega_7 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 - 6\omega_6 \omega_7 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_1}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\
& C_{11} \frac{\delta_l^3 v_1 v_3}{12\omega_6 \delta_t \omega_{11} \omega_{18}} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\delta_l^3 \rho v_3}{6\omega_6^2 \delta_t \omega_{18}} \frac{\partial^3 v_1}{\partial x_3^3} + C_{13} \frac{\delta_l^3 \rho v_1}{12\omega_6 \delta_t \omega_{11} \omega_{18}} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{\delta_l^4 v_1}{12\omega_9^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\delta_l^4 \rho}{12\omega_9^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& C_{16} \frac{\delta_l^4 v_2}{4\omega_9^2 \omega_{12}^2 \delta_t \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{17} \frac{\delta_l^4 \rho v_1 v_2}{4\omega_9^2 \omega_{12}^2 \delta_t \omega_5^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{18} \frac{\delta_l^4 \rho}{12\omega_9^2 \omega_{12}^2 \delta_t \omega_5^2} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{19} \frac{\delta_l^4 v_1}{12\omega_{15} \omega_9^2 \omega_{12}^2 \delta_t \omega_5^2 \omega_{21}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2^2} + \\
& C_{20} \frac{\delta_l^4 \rho}{12\omega_{15} \omega_9^2 \omega_{12}^2 \delta_t \omega_5^2 \omega_{21}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2^2} + C_{21} \frac{\delta_l^4 \rho v_1 v_2}{2\omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t \omega_{10} \omega_5^2 \omega_{21}} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2^2} + C_{22} \frac{\delta_l^4 v_2}{12\omega_{15}^2 \omega_9 \omega_{12}^2 \delta_t \omega_{10}^2 \omega_5^2 \omega_{21}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + \\
& C_{23} \frac{\delta_l^4 \rho}{12\omega_{15}^2 \omega_9^2 \omega_{12}^2 \delta_t \omega_{10}^2 \omega_5^2 \omega_{21}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + C_{24} \frac{\delta_l^4 \rho}{12\omega_{15}^2 \omega_9 \omega_{12}^2 \delta_t \omega_{10}^2 \omega_5^2 \omega_{21}} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^2} + C_{25} \frac{\delta_l^4 v_1}{24\omega_{15}^2 \delta_t \omega_{10}^2 \omega_5^2} \frac{\partial^4 \rho}{\partial x_2^2} + C_{26} \frac{\delta_l^4 \rho}{24\omega_{15}^2 \delta_t \omega_{10}^2 \omega_5^2} \frac{\partial^4 v_1}{\partial x_2^2} + \\
& C_{27} \frac{\delta_l^4 \rho v_1 v_2}{12\omega_{15}^2 \delta_t \omega_{10}^2 \omega_5^2} \frac{\partial^4 v_2}{\partial x_2^2} + C_{28} \frac{\delta_l^4 v_3}{4\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{29} \frac{\delta_l^4 \rho v_1 v_3}{4\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{30} \frac{\delta_l^4 \rho}{12\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{31} \frac{\delta_l^4 v_1 v_2 v_3}{\omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{32} \frac{\delta_l^4 \rho v_2 v_3}{\omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{33} \frac{\delta_l^4 \rho v_1 v_3}{2\omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{\delta_l^4 \rho v_1 v_2}{2\omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{35} \frac{2\delta_l^4 c_s^4 v_3}{\omega_6^2 \delta_t \omega_8^2 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{36} \frac{\delta_l^4 c_s^2 \rho v_1 v_3}{2\omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{37} \frac{\delta_l^4 c_s^2 \rho v_2 v_3}{\omega_{15}^2 \omega_6^2 \delta_t \omega_{17} \omega_8^2 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{38} \frac{\delta_l^4 c_s^2 \rho}{12\omega_{15} \omega_9 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{17} \omega_{14} \omega_8^2 \omega_5^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{39} \frac{\delta_l^4 v_1 v_2 v_3}{4\omega_{15}^2 \omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_{17} \omega_{18} \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + \\
& + C_{40} \frac{\delta_l^4 \rho v_2 v_3}{2\omega_{15}^2 \omega_6^2 \delta_t \omega_{17} \omega_8^2 \omega_5^2} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3} + C_{41} \frac{\delta_l^4 \rho v_1 v_3}{4\omega_{15}^2 \omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_{17} \omega_{18} \omega_8 \omega_5^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{42} \frac{\delta_l^4 \rho v_1 v_2}{12\omega_{15}^2 \omega_6^2 \delta_t \omega_{16} \omega_{10}^2 \omega_{17} \omega_{18} \omega_8 \omega_5^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{43} \frac{\delta_l^4 v_1}{12\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{44} \frac{\delta_l^4 \rho}{12\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{45} \frac{\delta_l^4 \rho v_1 v_3}{2\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{46} \frac{\delta_l^4 \rho}{2\omega_9 \omega_{12} \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{47} \frac{\delta_l^4 \rho}{2\omega_9^2 \omega_{12} \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{48} \frac{\delta_l^4 \rho}{12\omega_9 \omega_{12} \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{49} \frac{\delta_l^4 \rho v_3}{\omega_9 \omega_{12} \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{\delta_l^4 v_1}{12\omega_{15} \omega_6^2 \delta_t \omega_{17}^2 \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{51} \frac{\delta_l^4 \rho}{4\omega_{15} \omega_6^2 \delta_t \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + \\
& C_{52} \frac{\delta_l^4 \rho v_2}{2\omega_{15} \omega_6^2 \delta_t \omega_{16} \omega_{10}^2 \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{\delta_l^4 \rho}{4\omega_{15} \omega_6^2 \omega_{19} \delta_t \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{54} \frac{\delta_l^4 v_3}{12\omega_9 \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{21}^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{\delta_l^4 \rho v_1 v_3}{12\omega_9^2 \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{21}^2 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{56} \frac{\delta_l^4 \rho}{12\omega_9 \omega_6^2 \omega_{22} \delta_t \omega_{13} \omega_{21}^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{57} \frac{\delta_l^4 v_1 v_2 v_3}{4\omega_6^2 \omega_{19} \delta_t \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{58} \frac{\delta_l^4 \rho v_2 v_3}{2\omega_6^2 \delta_t \omega_{20} \omega_8^2 \omega_5^2 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} + C_{59} \frac{\delta_l^4 \rho v_1 v_3}{12\omega_6^2 \omega_{19} \delta_t \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{60} \frac{\delta_l^4 \rho v_1 v_2}{4\omega_6^2 \omega_{19} \delta_t \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{\delta_l^4 v_1}{24\omega_6^2 \delta_t \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_3^4} + C_{62} \frac{\delta_l^4 \rho}{24\omega_6^2 \delta_t \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_3^4} + C_{63} \frac{\delta_l^4 \rho v_1 v_3}{12\omega_6^2 \delta_t \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$C_1 = 7\omega_9^2 v_1^4 - 144\omega_9 c_s^2 v_1^2 + 36\omega_9 v_1^2 - 36v_1^2 + 12\omega_9 c_s^2 - 12c_s^2 + \omega_9^2 c_s^4 + 12c_s^4 - 12\omega_9 c_s^4 - \omega_9^2 c_s^2 + 144c_s^2 v_1^2 - 7\omega_9^2 v_1^2 + 24\omega_9^2 c_s^2 v_1^2 + 36v_1^4 - 36\omega_9 v_1^4$$

$$\begin{aligned}
C_2 &= \omega_{12}v_1^2\omega_5 + \omega_9\omega_{12}\omega_5 - 3\omega_9c_s^2\omega_5 + \omega_9\omega_{12}v_1^2 + \omega_9^2v_1^2\omega_5 + \omega_9\omega_5 - 3\omega_9\omega_{12}c_s^2\omega_5 + 3\omega_9\omega_{12}c_s^2 - 3\omega_9^2c_s^2 - \omega_9\omega_{12}v_1^2\omega_5 + 3\omega_9^2c_s^2\omega_5 - \omega_9^2v_1^2 - \omega_9\omega_{12} + \omega_9^2 - \omega_9^2\omega_5 - \omega_9v_1^2\omega_5 + 3\omega_{12}c_s^2\omega_5 - \omega_{12}\omega_5 \\
C_3 &= 3\omega_{12}v_1^2\omega_5 + \omega_9\omega_{12}\omega_5 - \omega_9c_s^2\omega_5 + 3\omega_9\omega_{12}v_1^2 + 3\omega_9^2v_1^2\omega_5 + \omega_9\omega_5 - \omega_9\omega_{12}c_s^2\omega_5 + \omega_9\omega_{12}c_s^2 - \omega_9^2c_s^2 - 3\omega_9\omega_{12}v_1^2\omega_5 + \omega_9^2c_s^2\omega_5 - 3\omega_9^2v_1^2 - \omega_9\omega_{12} + \omega_9^2 - \omega_9^2\omega_5 - 3\omega_9v_1^2\omega_5 + \omega_{12}c_s^2\omega_5 - \omega_{12}\omega_5 \\
C_4 &= -12\omega_9^2v_1^2\omega_5 - 18\omega_9\omega_{12}c_s^2\omega_5^2 + 6\omega_9^2\omega_{12}v_1^2\omega_5 + 12\omega_9\omega_5^2 - 3\omega_9^2\omega_{12}v_1^2\omega_5^2 + 12\omega_9^2v_1^2\omega_5^2 - 24\omega_9\omega_{12}c_s^2\omega_5 + 12\omega_{12}v_1^2\omega_5^2 + 6\omega_9\omega_{12}\omega_5^2 - 12\omega_9c_s^2\omega_5^2 - 11\omega_9^2\omega_{12}c_s^2\omega_5^2 - 12\omega_9^2\omega_5^2 - 12\omega_9v_1^2\omega_5^2 + 36\omega_{12}c_s^2\omega_5^2 - 12\omega_{12}\omega_5^2 - 24\omega_9\omega_{12}c_s^2 + 12\omega_9^2c_s^2\omega_5^2 + 3\omega_9^2\omega_{12}\omega_5^2 - 12\omega_9^2c_s^2\omega_5 - 6\omega_9\omega_{12}v_1^2\omega_5^2 - 6\omega_9^2\omega_{12}\omega_5 + 12\omega_9^2\omega_5 + 42\omega_9^2\omega_{12}c_s^2\omega_5 \\
C_5 &= -12\omega_{15} + 36\omega_{15}c_s^2 - 6\omega_{15}v_2^2\omega_5 + 3\omega_{15}c_s^2\omega_{10}\omega_5 + 12\omega_{15}v_2^2 + 6\omega_{10}v_2^2\omega_5 + 12\omega_{10} + 6\omega_{15}\omega_5 + \omega_{15}\omega_{10}v_2^2\omega_5 - 36c_s^2\omega_{10} - \omega_{15}\omega_{10}\omega_5 - 18\omega_{15}c_s^2\omega_5 - 6\omega_{10}\omega_5 + 18c_s^2\omega_{10}\omega_5 - 12\omega_{10}v_2^2 \\
C_6 &= 3v_2^2\omega_5^2 - 12\omega_{15}c_s^2 + 3\omega_{15}v_2^2\omega_5 + \omega_{15}\omega_5^2 - 3\omega_5^2 - \omega_{15}v_2^2\omega_5^2 - 3\omega_{15}\omega_5 - 6v_2^2\omega_5 + 3c_s^2\omega_5^2 + 15\omega_{15}c_s^2\omega_5 - 3\omega_{15}c_s^2\omega_5^2 - 6c_s^2\omega_5 + 6\omega_5 \\
C_7 &= -12\omega_{15} + 12\omega_{15}c_s^2 - 18\omega_{15}v_2^2\omega_5 + \omega_{15}c_s^2\omega_{10}\omega_5 + 36\omega_{15}v_2^2 + 18\omega_{10}v_2^2\omega_5 + 12\omega_{10} + 6\omega_{15}\omega_5 + 3\omega_{15}\omega_{10}v_2^2\omega_5 - 12c_s^2\omega_{10} - \omega_{15}\omega_{10}\omega_5 - 6\omega_{15}c_s^2\omega_5 - 6\omega_{10}\omega_5 + 6c_s^2\omega_{10}\omega_5 - 36\omega_{10}v_2^2 \\
C_8 &= \omega_6v_1^2\omega_{13} - \omega_9\omega_6v_1^2 - \omega_9^2\omega_6 + 3\omega_9c_s^2\omega_{13} - 3\omega_9\omega_6c_s^2 - \omega_9\omega_{13} + \omega_9\omega_6\omega_{13} - 3\omega_9\omega_6c_s^2\omega_{13} + \omega_9v_1^2\omega_{13} + 3\omega_9^2\omega_6c_s^2 - \omega_6\omega_{13} - \omega_9\omega_6v_1^2\omega_{13} - 3\omega_9^2c_s^2 - \omega_9^2v_1^2 + 3\omega_6c_s^2\omega_{13} + \omega_9^2 + \omega_9\omega_6 + \omega_9^2\omega_6v_1^2 \\
C_9 &= 3\omega_6v_1^2\omega_{13} - 3\omega_9\omega_6v_1^2 - \omega_9^2\omega_6 + \omega_9c_s^2\omega_{13} - \omega_9\omega_6c_s^2 - \omega_9\omega_{13} + \omega_9\omega_6\omega_{13} - \omega_9\omega_6c_s^2\omega_{13} + 3\omega_9v_1^2\omega_{13} + \omega_9^2\omega_6c_s^2 - \omega_6\omega_{13} - 3\omega_9\omega_6v_1^2\omega_{13} - \omega_9^2c_s^2 - 3\omega_9^2v_1^2 + \omega_6c_s^2\omega_{13} + \omega_9^2 + \omega_9\omega_6 + 3\omega_9^2\omega_6v_1^2 \\
C_{10} &= 36\omega_6^2c_s^2\omega_{13} + 12\omega_9^2\omega_6^2v_1^2 - 11\omega_9^2\omega_6^2c_s^2\omega_{13} + 12\omega_9^2\omega_6 + 6\omega_9^2\omega_6v_1^2\omega_{13} - 12\omega_6^2\omega_{13} - 12\omega_9^2\omega_6^2 + 3\omega_9^2\omega_6^2\omega_{13} - 6\omega_9\omega_6^2v_1^2\omega_{13} + 12\omega_9^2\omega_6^2c_s^2 - 24\omega_9\omega_6c_s^2\omega_{13} - 12\omega_9^2\omega_6c_s^2 - 24\omega_9^2c_s^2\omega_{13} + 6\omega_9\omega_6^2\omega_{13} + 12\omega_9\omega_6^2 - 18\omega_9\omega_6^2c_s^2\omega_{13} - 6\omega_9^2\omega_6\omega_{13} - 12\omega_9\omega_6^2c_s^2 - 12\omega_9\omega_6^2v_1^2 + 12\omega_6^2v_1^2\omega_{13} + 42\omega_9^2\omega_6c_s^2\omega_{13} - 3\omega_9^2\omega_6^2v_1^2\omega_{13} - 12\omega_9^2\omega_6v_1^2 \\
C_{11} &= -36c_s^2\omega_{11} + 6\omega_6v_3^2\omega_{11} - 6\omega_6\omega_{11} + 18\omega_6c_s^2\omega_{11} + 3\omega_6c_s^2\omega_{11}\omega_{18} - 12v_3^2\omega_{11} + \omega_6v_3^2\omega_{11}\omega_{18} - \omega_6\omega_{11}\omega_{18} + 36c_s^2\omega_{18} + 12\omega_{11} + 6\omega_6\omega_{18} - 6\omega_6v_3^2\omega_{18} - 18\omega_6c_s^2\omega_{18} - 12\omega_{18} + 12v_3^2\omega_{18} \\
C_{12} &= -3\omega_6^2c_s^2\omega_{18} + 6\omega_6 - 6\omega_6v_3^2 + \omega_6^2\omega_{18} + 3\omega_6^2c_s^2 - \omega_6^2v_3^2\omega_{18} - 6\omega_6c_s^2 - 12c_s^2\omega_{18} - 3\omega_6^2 - 3\omega_6\omega_{18} + 3\omega_6v_3^2\omega_{18} + 15\omega_6c_s^2\omega_{18} + 3\omega_6^2v_3^2 \\
C_{13} &= -12c_s^2\omega_{11} + 18\omega_6v_3^2\omega_{11} - 6\omega_6\omega_{11} + 6\omega_6c_s^2\omega_{11} + \omega_6c_s^2\omega_{11}\omega_{18} - 36v_3^2\omega_{11} + 3\omega_6v_3^2\omega_{11}\omega_{18} - \omega_6\omega_{11}\omega_{18} + 12c_s^2\omega_{18} + 12\omega_{11} + 6\omega_6\omega_{18} - 18\omega_6v_3^2\omega_{18} - 6\omega_6c_s^2\omega_{18} - 12\omega_{18} + 36v_3^2\omega_{18} \\
C_{14} &= 12 + 90\omega_9^2v_1^4 - 18\omega_9 - 1008\omega_9c_s^2v_1^2 + 234\omega_9v_1^2 - 5\omega_9^3c_s^4 - 156v_1^2 - 9\omega_9^3v_1^4 + 198\omega_9c_s^2 - 132c_s^2 - 34\omega_9^3c_s^2v_1^2 + 82\omega_9^2c_s^4 + 144c_s^4 - 216\omega_9c_s^4 + 10\omega_9^3v_1^2 - 78\omega_9^2c_s^2 + 672c_s^2v_1^2 - 98\omega_9^2v_1^2 + 8\omega_9^2 + 404\omega_9^2c_s^2v_1^2 + 144v_1^4 + 6\omega_9^3c_s^2 - 216\omega_9v_1^4 - \omega_9^3 \\
C_{15} &= 12 + 310\omega_9^2v_1^4 - 18\omega_9 - 648\omega_9c_s^2v_1^2 + 378\omega_9v_1^2 - \omega_9^3c_s^4 - 252v_1^2 - 29\omega_9^3v_1^4 + 54\omega_9c_s^2 - 36c_s^2 - 18\omega_9^3c_s^2v_1^2 + 14\omega_9^2c_s^4 + 24c_s^4 - 36\omega_9c_s^4 + 14\omega_9^2v_1^2 - 22\omega_9^2c_s^2 + 432c_s^2v_1^2 - 154\omega_9^2v_1^2 + 8\omega_9^2 + 252\omega_9^2c_s^2v_1^2 + 504v_1^4 + 2\omega_9^3c_s^2 - 756\omega_9v_1^4 - \omega_9^3 \\
C_{16} &= 4\omega_9\omega_{12}^2c_s^4\omega_5 - 4\omega_9^3c_s^2\omega_5^2 + 4\omega_9^3\omega_{12}c_s^2 + 36\omega_9\omega_{12}^2v_1^2\omega_5^2 - 4\omega_9^3v_1^4\omega_5 - 4\omega_9^2c_s^4\omega_5^2 - 72\omega_9\omega_{12}c_s^2v_1^2\omega_5^2 + 24\omega_{12}^2v_1^4\omega_5^2 + 4\omega_9\omega_{12}c_s^2\omega_5^2 + 24\omega_9^3c_s^2v_1^2\omega_5^2 + 8\omega_9^2\omega_{12}c_s^4\omega_5^2 + 120\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^2 + 36\omega_9^2\omega_{12}^2c_s^2v_1^2 + 16\omega_9^2\omega_{12}v_1^2\omega_5 + 13\omega_9^2\omega_{12}v_1^2\omega_5^2 + 13\omega_9^2\omega_{12}^2v_1^4\omega_5^2 + 8\omega_9^2\omega_{12}^2c_s^2\omega_5 - 8\omega_9^2\omega_{12}^2v_1^2 + 8\omega_9^2\omega_{12}c_s^4\omega_5 - 20\omega_9^2\omega_{12}^2v_1^4\omega_5 - 20\omega_9^2\omega_{12}v_1^2\omega_5^2 - 4\omega_9^2\omega_{12}c_s^4\omega_5^2 - 24\omega_9^2c_s^2v_1^2\omega_5^2 - 48\omega_9^2\omega_{12}c_s^2v_1^2\omega_5 - 4\omega_9^2\omega_{12}^2c_s^2 - 24\omega_9^2c_s^2v_1^2\omega_5 - 32\omega_9^2\omega_{12}v_1^2\omega_5^2 - 8\omega_{12}^2c_s^2\omega_5^2 - 20\omega_9\omega_{12}v_1^4\omega_5^2 + 4\omega_9^2v_1^2\omega_5^2 + 8\omega_9^3\omega_{12}v_1^2 - 12\omega_9\omega_{12}^2c_s^4\omega_5^2 + 4\omega_9^3c_s^2\omega_5 - 20\omega_9\omega_{12}^2v_1^2\omega_5 + 4\omega_9^3v_1^4\omega_5^2 + 4\omega_9^2\omega_{12}^2c_s^4 - 8\omega_9^2\omega_{12}^2\omega_5^2 - 16\omega_9^2\omega_{12}v_1^4\omega_5 - 144\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 - 36\omega_9^3\omega_{12}c_s^2v_1^2 + 84\omega_9^3\omega_{12}c_s^2v_1^2\omega_5 - 13\omega_9^2\omega_{12}^2v_1^2\omega_5^2 - 13\omega_9^3\omega_{12}v_1^4\omega_5^2 - 8\omega_9^3\omega_{12}c_s^2\omega_5 - 8\omega_9^2\omega_{12}^2c_s^4\omega_5 - 4\omega_9\omega_{12}^2c_s^2\omega_5 + 4\omega_9^3c_s^4\omega_5^2 - 36\omega_9\omega_{12}^2v_1^4\omega_5^2 + 4\omega_9^3v_1^2\omega_5 + 4\omega_9^2c_s^2\omega_5^2 - 8\omega_9^3\omega_{12}v_1^4 - 4\omega_9\omega_{12}c_s^4\omega_5^2 - 24\omega_{12}^2v_1^2\omega_5^2 + 51\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 + 20\omega_9\omega_{12}v_1^2\omega_5^2 + 8\omega_{12}^2c_s^4\omega_5^2 - 4\omega_9^2v_1^4\omega_5^2 - 84\omega_9^2\omega_{12}^2c_s^2v_1^2\omega_5 + 12\omega_9\omega_{12}^2c_s^2\omega_5^2 - 4\omega_9^3c_s^2\omega_5 - 4\omega_9^2\omega_{12}c_s^4 + 20\omega_9\omega_{12}^2v_1^4\omega_5 - 4\omega_9^3v_1^2\omega_5^2 + 20\omega_9^3\omega_{12}v_1^4\omega_5 + 20\omega_9^2\omega_{12}^2v_1^2\omega_5 + 96\omega_{12}^2c_s^2v_1^2\omega_5^2 + 4\omega_9^2\omega_{12}^2c_s^4\omega_5^2 + 4\omega_9^3\omega_{12}c_s^2\omega_5^2 + 8\omega_9^2\omega_{12}^2v_1^4 - 51\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^2 + 32\omega_9^2\omega_{12}v_1^4\omega_5^2 + 72\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 \\
C_{17} &= 16\omega_9^3c_s^2\omega_5^2 - 20\omega_9^3\omega_{12}c_s^2 - 120\omega_9\omega_{12}^2v_1^2\omega_5^2 + 17\omega_9^3\omega_{12}\omega_5^2 - 32\omega_9\omega_{12}c_s^2\omega_5^2 - 48\omega_9^2\omega_{12}v_1^2\omega_5 + 28\omega_9^2\omega_{12}\omega_5 - 43\omega_9^3\omega_{12}v_1^2\omega_5^2 - 44\omega_9^2\omega_{12}^2c_s^2\omega_5 + 28\omega_9^2\omega_{12}^2v_1^2 + 68\omega_9^2\omega_{12}v_1^2\omega_5 - 32\omega_{12}^2\omega_5^2 + 25\omega_9^2\omega_{12}^2c_s^2\omega_5^2 + 20\omega_9^2\omega_{12}^2c_s^2 - 17\omega_9^2\omega_{12}^2\omega_5^2 + 104\omega_9^2\omega_{12}v_1^2\omega_5^2 - 12\omega_9^2\omega_{12}^2 + 48\omega_{12}^2c_s^2\omega_5^2 - 16\omega_9^2v_1^2\omega_5^2 - 28\omega_9^3\omega_{12}v_1^2 - 16\omega_9^3c_s^2\omega_5 + 12\omega_9^3\omega_{12} + 24\omega_9\omega_{12}\omega_5^2 + 64\omega_9\omega_{12}^2v_1^2\omega_5 - 28\omega_9^3\omega_{12}\omega_5 + 56\omega_9^2\omega_{12}c_s^2\omega_5^2 + 8\omega_9^3\omega_5 + 48\omega_9\omega_{12}^2\omega_5 + 43\omega_9^2\omega_{12}^2v_1^2\omega_5^2 + 44\omega_9^2\omega_{12}c_s^2\omega_5 + 32\omega_9\omega_{12}^2c_s^2\omega_5 + 8\omega_9^2\omega_5^2 - 16\omega_9^3v_1^2\omega_5 - 16\omega_9^2c_s^2\omega_5^2 - 40\omega_9^2\omega_{12}\omega_5^2 + 80\omega_{12}^2v_1^2\omega_5^2 - 64\omega_9\omega_{12}v_1^2\omega_5^2 + 16\omega_9^2\omega_{12}\omega_5 - 72\omega_9\omega_{12}^2c_s^2\omega_5^2 + 16\omega_9^3v_1^2\omega_5^2 - 68\omega_9^2\omega_{12}^2v_1^2\omega_5 - 24\omega_9\omega_{12}^2\omega_5 - 25\omega_9^2\omega_{12}c_s^2\omega_5^2 - 16\omega_9^2\omega_{12}c_s^2\omega_5 - 8\omega_9^3\omega_5^2 \\
C_{18} &= -6\omega_9^2\omega_{12}c_s^4\omega_5^3 + 12\omega_9^2c_s^2v_1^2\omega_5^3 + 54\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^3 + 102\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5 + 27\omega_9^3\omega_{12}v_1^2\omega_5^3 + 19\omega_9^2\omega_{12}^2v_1^4\omega_5^3 - 12\omega_9^3c_s^2v_1^2\omega_5^2 + 12\omega_9^2\omega_{12}c_s^4\omega_5^2 + 90\omega_9\omega_{12}^2v_1^2\omega_5^3 - 5\omega_9^3\omega_{12}^2c_s^2\omega_5^2 - 12\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^2 + 12\omega_9^3\omega_{12}^2v_1^4\omega_5 - 48\omega_9^3\omega_{12}v_1^2\omega_5^2 + 12\omega_9^2\omega_{12}^2c_s^4 + 12\omega_9^2\omega_{12}^2v_1^4\omega_5^2 + 72\omega_{12}^2v_1^4\omega_5^3 - 36\omega_9\omega_{12}c_s^2v_1^2\omega_5^3 + 12\omega_9^3\omega_{12}c_s^4\omega_5 - 48\omega_9^3\omega_{12}^2c_s^2v_1^2 + 24\omega_9^3\omega_{12}v_1^2\omega_5 + 12\omega_9^2v_1^2\omega_5^3 + 12\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5^3 - 18\omega_9^3\omega_{12}c_s^4\omega_5^2 - 36\omega_9\omega_{12}v_1^4\omega_5^3 - 6\omega_9^2\omega_{12}^2c_s^2\omega_5^2 - 12\omega_{12}^2c_s^2\omega_5^3 + 12\omega_9^3v_1^4\omega_5^3 + 6\omega_9^2\omega_{12}^2c_s^2\omega_5 + 24\omega_9^2\omega_{12}v_1^2\omega_5^2 - 12\omega_9\omega_{12}^2c_s^4\omega_5^3 - 18\omega_9^3\omega_{12}^2v_1^4\omega_5^2 - 12\omega_9^2c_s^2v_1^2\omega_5^3 + 6\omega_9^2\omega_{12}c_s^4\omega_5^3 - 81\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5^2 - \omega_9^2\omega_{12}^2c_s^2\omega_5^3 - 60\omega_9^3\omega_{12}v_1^2\omega_5^3 - 12\omega_9\omega_{12}^2c_s^4\omega_5 + 4\omega_9^3\omega_{12}^2v_1^4\omega_5^3 - 12\omega_9^3v_1^4\omega_5^2 + 13\omega_9^3\omega_{12}^2c_s^4\omega_5^2 - 90\omega_9\omega_{12}^2v_1^4\omega_5^3 - 12\omega_9^2\omega_{12}^2c_s^2\omega_5^2 - 108\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 - 12\omega_9^3\omega_{12}v_1^2\omega_5 - 12\omega_9^2\omega_{12}^2c_s^2v_1^2\omega_5^2 - 48\omega_9^2\omega_{12}^2v_1^2\omega_5^2 + 48\omega_9^3\omega_{12}v_1^4\omega_5^3 - 12\omega_9^2\omega_{12}^2c_s^2v_1^2\omega_5^2 + 48\omega_9^3\omega_{12}^2v_1^4\omega_5^2 + 60\omega_9^2\omega_{12}^2c_s^2v_1^2\omega_5^3 - 12\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5^3 - 12\omega_9^3\omega_{12}c_s^4\omega_5^3 - 306\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^3 - \omega_9^3\omega_{12}^2c_s^4\omega_5^3 + 6\omega_9^2\omega_{12}^2c_s^2\omega_5^3 - 19\omega_9^2\omega_{12}^2v_1^2\omega_5^3 + 162\omega_9^2\omega_{12}^2c_s^2v_1^2\omega_5^2 - 27\omega_9^3\omega_{12}v_1^4\omega_5^3 + \omega_9^2\omega_{12}^2c_s^4\omega_5^3 - 6\omega_9^2\omega_{12}^2c_s^2\omega_5^3 + 252\omega_{12}^2c_s^2v_1^2\omega_5^3 - 48\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5 - 21\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5^3 - 4\omega_9^3\omega_{12}^2v_1^2\omega_5^3 + 12\omega_9\omega_{12}^2c_s^2\omega_5^2 + 60\omega_9^2\omega_{12}v_1^4\omega_5^3 + 12\omega_9^3v_1^2\omega_5^2 - 24\omega_9^3\omega_{12}v_1^4\omega_5 - 12\omega_9^2v_1^4\omega_5^3 + 12\omega_{12}^2c_s^4\omega_5^3 + 6\omega_9^2\omega_{12}^2c_s^4\omega_5^2 + 36\omega_9\omega_{12}^2v_1^2\omega_5^3 + 18\omega_9^3\omega_{12}c_s^2\omega_5^2 - 12\omega_9^3v_1^2\omega_5^3 - 24\omega_9^2\omega_{12}^2c_s^4\omega_5 + 18\omega_9^3\omega_{12}^2v_1^4\omega_5^2 + 30\omega_9^3\omega_{12}^2c_s^2v_1^2\omega_5^2 + 12\omega_9\omega_{12}^2c_s^2\omega_5^3 - 24\omega_9^2\omega_{12}v_1^2\omega_5^2
\end{aligned}$$

$$\begin{aligned}
& 15\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 16\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 8\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - \omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - \\
& 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 4\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 4\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 8\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - \\
& 3\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 4\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 4\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 7\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - \\
& 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - 8\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + 2\omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} + \omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21} - \omega_{15}^2\omega_9\omega_{12}^2\omega_{10}\omega_5^3\omega_{21}
\end{aligned}$$

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$$C_{37} = \omega_{15}^2 \omega_{17} \omega_8 \omega_5^3 - 4 \omega_{15} \omega_6^2 \omega_{17} \omega_8^2 \omega_5^2 - \omega_{15}^2 \omega_6^2 \omega_8^2 \omega_5^3 + \omega_{15} \omega_6^2 \omega_{17} \omega_8^2 \omega_5^3 + 2 \omega_{15}^2 \omega_6^2 \omega_8^2 \omega_5^2 - 2 \omega_{15}^2 \omega_6 \omega_8 \omega_5^3 - \omega_{15}^2 \omega_6^2 \omega_{17} \omega_8^2 \omega_5^2 + 2 \omega_{15}^2 \omega_6 \omega_{17} \omega_8 \omega_5^2 + \omega_{15}^2 \omega_6^2 \omega_{17} \omega_5^2 + 5 \omega_{15}^2 \omega_8^2 \omega_{17} \omega_8 \omega_5 - \omega_{15}^2 \omega_6^2 \omega_{17} \omega_5^3 - 4 \omega_{15}^2 \omega_6^2 \omega_{17} \omega_8^2 - 2 \omega_{15}^2 \omega_6 \omega_{17} \omega_8 \omega_5^3 + 2 \omega_{15} \omega_6^2 \omega_{17} \omega_8^2 \omega_5 + 2 \omega_6^2 \omega_{17} \omega_8^2 \omega_5^2 + \omega_{15} \omega_6^2 \omega_8^2 \omega_5^3 + 2 \omega_{15} \omega_6 \omega_{17} \omega_8^2 \omega_5^2 + 2 \omega_{15}^2 \omega_6 \omega_{17} \omega_8^2 \omega_5^2 + \omega_{15}^2 \omega_6 \omega_{17} \omega_5^3 + 3 \omega_{15}^2 \omega_8^2 \omega_{17} \omega_8 \omega_5 - 2 \omega_{15} \omega_6^2 \omega_8^2 \omega_5^2 - \omega_6^2 \omega_{17} \omega_8^2 \omega_5^3 - \omega_{15} \omega_6 \omega_{17} \omega_8^2 \omega_5^3 - \omega_{15}^2 \omega_{17} \omega_8^2 \omega_5^2 + \omega_{15}^2 \omega_6 \omega_8^2 \omega_5^3 - 2 \omega_{15}^2 \omega_6 \omega_8 \omega_5^2 - 3 \omega_{15}^2 \omega_6 \omega_{17} \omega_8^2 \omega_5 - 4 \omega_{15}^2 \omega_6^2 \omega_{17} \omega_8 \omega_5^2 + \omega_{15}^2 \omega_6^2 \omega_{17} \omega_8 \omega_5^3 + 2 \omega_{15}^2 \omega_6^2 \omega_8 \omega_5^3$$

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$$\begin{aligned}
C_{45} = & 4\omega_3^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_3^6\omega_6^2\omega_{13}^2\omega_{11}\omega_{18} + 3\omega_2^9\omega_3^6\omega_{22}c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 8\omega_9\omega_6^6\omega_{22}c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_2^9\omega_3^6\omega_{13}\omega_{11}\omega_{18} - \omega_3^6\omega_6^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} + \\
& 2\omega_3^6\omega_6^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} - 2\omega_9^6\omega_6^6\omega_{22}v_1^2\omega_{13}\omega_{11}\omega_{18} + 2\omega_9\omega_6^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} + 11\omega_2^9\omega_3^6\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} + 2\omega_9^6\omega_6^6\omega_{22}\omega_{13}\omega_{11}\omega_{18} - \\
& 6\omega_3^6\omega_6^6\omega_{22}v_1^2\omega_{13}\omega_{11}\omega_{18} + 8\omega_2^9\omega_3^6\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} - 2\omega_9^6\omega_3^6\omega_{13}^2\omega_{11}\omega_{18} - 8\omega_3^6\omega_6^6\omega_{22}c_2^2\omega_{11}\omega_{18} + 2\omega_9^6\omega_6^6c_2^2\omega_{13}^2\omega_{11}\omega_{18} + 4\omega_2^9\omega_6^6v_1^2\omega_{13}\omega_{11}\omega_{18} + \\
& 4\omega_3^6\omega_6^6c_2^2\omega_{13}\omega_{11}\omega_{18} - 2\omega_3^6\omega_6^6v_1^2\omega_{13}^2\omega_{11}\omega_{18} + 4\omega_3^6\omega_6^6\omega_{22}c_2^2\omega_{13}\omega_{11} + 4\omega_2^9\omega_6^6\omega_{22}\omega_{11}\omega_{18} + 2\omega_3^6\omega_6^6v_1^2\omega_{13}^2\omega_{11}\omega_{18} + 4\omega_3^6\omega_6^6\omega_{22}v_1^2\omega_{11}\omega_{18} - \\
& 8\omega_9^6\omega_6^6\omega_{13}^2\omega_{11}\omega_{18} - 2\omega_9^6\omega_6^6c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 2\omega_9^6\omega_6^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} + 4\omega_2^9\omega_6^6c_2^2\omega_{13}\omega_{11}\omega_{18} + 4\omega_3^6\omega_6^6v_1^2\omega_{13}\omega_{11}\omega_{18} + \omega_3^6\omega_6^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} + \\
& \omega_2^9\omega_6^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} + 5\omega_9\omega_6^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} + 12\omega_3^6\omega_{22}c_2^2\omega_{13}^2\omega_{11}\omega_{18} + 2\omega_9^6\omega_6^6\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_9\omega_6^6\omega_{22}v_1^2\omega_{13}\omega_{11}\omega_{18} - 4\omega_2^9\omega_6^6\omega_{22}c_2^2\omega_{13}^2\omega_{11}\omega_{18} + \\
& 4\omega_3^6\omega_6^6\omega_{13}^2\omega_{11}\omega_{18} - 2\omega_3^6\omega_3^6\omega_{22}c_2^2\omega_{13}^2\omega_{18} - 6\omega_9^6\omega_6^6\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} + 3\omega_2^9\omega_6^6\omega_{22}\omega_{13}\omega_{11}\omega_{18} + \omega_3^6\omega_6^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} + 2\omega_2^9\omega_6^6\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} + \\
& 9\omega_2^9\omega_6^6\omega_{22}v_1^2\omega_{13}\omega_{11}\omega_{18} + 2\omega_9\omega_6^6\omega_{22}c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 16\omega_2^9\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} - 4\omega_3^6\omega_6^6v_1^2\omega_{13}\omega_{11}\omega_{18} + 4\omega_2^9\omega_6^6c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_9^6\omega_6^6\omega_{22}\omega_{11}\omega_{18} - \\
& 4\omega_3^6\omega_6^6v_1^2\omega_{13}^2\omega_{11}\omega_{18} - 2\omega_3^6\omega_6^6c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_3^6\omega_6^6\omega_{22}v_1^2\omega_{11}\omega_{18} + 6\omega_9\omega_6^6\omega_{22}\omega_{13}\omega_{11}\omega_{18} - 5\omega_2^9\omega_6^6\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} - 5\omega_9\omega_6^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} + \\
& 7\omega_2^9\omega_6^6\omega_{22}v_1^2\omega_{13}\omega_{11}\omega_{18} + 4\omega_9\omega_6^6\omega_{22}\omega_{13}\omega_{11}\omega_{18} + 4\omega_3^6\omega_6^6\omega_{22}c_2^2\omega_{13}^2\omega_{18} - 2\omega_2^9\omega_6^6\omega_{22}c_2^2\omega_{13}^2\omega_{11}\omega_{18} - 9\omega_3^6\omega_6^6\omega_{22}\omega_{13}\omega_{11}\omega_{18} - \\
& 2\omega_9\omega_6^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} - \omega_3^6\omega_6^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} - \omega_2^9\omega_6^6\omega_{22}c_2^2\omega_{13}\omega_{11}\omega_{18} + 4\omega_3^6\omega_6^6\omega_{22}v_1^2\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_3^6\omega_{22}\omega_{13}^2\omega_{11}\omega_{18} - 4\omega_9^6\omega_6^6\omega_{13}\omega_{11}\omega_{18} +
\end{aligned}$$

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$$C_{48} = 12\omega_6^3w_{22}c_4^5w_{13}w_{20}w_{14}\omega_8^5w_3^5w_{18} - 12\omega_9w_{12}\omega_6^3w_{22}v_7^3w_{13}w_7^3v_3^5w_{14}w_8w_5^3w_{18} + 24\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1v_{21}w_{13}w_7^3w_{20}w_8w_5^3w_{18} +$$

 $12\omega_{12}w_3^3c_5^6w_7^3v_3^5w_{20}w_{14}\omega_8^5w_5^3w_{18} + 12\omega_9w_{12}\omega_6^3w_{22}c_4^5w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3 + 12\omega_9w_{12}\omega_6^3w_{22}c_4^5w_{13}w_7^3w_{14}\omega_8^5w_5^3w_{18} +$
 $24\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}w_8w_5w_{18} - 12\omega_{12}w_3^3w_{22}c_5^6w_7^3v_3^5w_{20}w_{14}\omega_8^5w_5^3w_{18} - 12\omega_9w_{12}\omega_6^3w_{22}c_5^6w_{13}w_7^3w_{20}w_8^5w_5^3w_{18} -$
 $12\omega_9w_{12}\omega_6^3w_{22}c_5^6w_{13}w_7^3v_3^5w_{20}w_8w_5^3w_{18} + 12\omega_9w_{12}\omega_6^3w_{22}c_5^6w_{13}w_7^3v_3^5w_{20}w_{14}\omega_8^5w_5^3 - 12\omega_9w_6^3w_{22}c_4^5w_{13}w_7^3w_{20}w_8^5w_5^3w_{18} -$
 $12\omega_9w_{12}\omega_6^3w_{22}v_1^3w_{13}w_7^3v_3^5w_{20}w_8^5w_{18} + 24\omega_9w_{12}\omega_6^3w_{22}v_1v_{21}w_{13}w_7^3v_3^5w_{20}w_8^5w_{18} + 6\omega_9w_6^3w_{22}c_5^6w_{13}w_7^3v_3^5w_{20}w_{14}\omega_8^5w_5^3w_{18} +$
 $12\omega_9w_{12}\omega_6^3w_{22}v_1v_{21}w_{13}w_7^3v_3^5w_{14}\omega_8^5w_5^3w_{18} + 12\omega_9w_{12}\omega_6^3c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} - 12\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} -$
 $18\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} + 12\omega_9w_{12}\omega_6^3w_{22}c_5^6w_{13}w_7^3v_3^5w_{20}w_{14}w_8w_5w_{18} + 12\omega_9w_{12}\omega_6^3w_{22}c_5^6w_{13}w_7^3v_3^5w_{20}w_{14}\omega_8^5w_{18} +$
 $12\omega_9w_{12}\omega_6^3w_{22}c_5^6w_{13}w_7^3v_3^5w_{20}w_{14}w_8w_5^3w_{18} - 12\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_{20}w_{14}\omega_8^5w_5^3w_{18} + 12\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_{18} -$
 $6\omega_9w_{12}\omega_6^3w_{22}v_1^3w_{13}w_7^3v_3^5w_{20}w_{14}\omega_8^5w_5^3w_{18} - 24w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}w_8w_5^3w_{18} + 24\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1v_{21}w_7^3w_{20}w_8^5w_5^3w_{18} +$
 $12\omega_6^3w_{22}c_5^6v_1v_{21}w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} + 6\omega_9w_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} + 12\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_{18} +$
 $12\omega_9w_{12}\omega_6^3w_{22}v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_{18} - 12\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3 - 24\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1v_{21}w_{13}w_7^3w_{14}\omega_8^5w_5^3 +$
 $12\omega_9w_{12}\omega_6^3w_{22}v_1^3w_{13}w_7^3v_3^5w_{20}w_{14}\omega_8^5w_5^3w_{18} + 24\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1v_{21}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} - 6\omega_9w_{12}\omega_6^3w_{22}c_5^6v_1^3w_{13}w_7^3w_{20}w_{14}\omega_8^5w_5^3w_{18} -$

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$$\begin{aligned}
C_{50} = & 12w_{15}w_6v_1v_2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - 28w_{15}w_6^2c_8^4v_{17}w_7w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2v_1v_2^2w_2^2v_3w_{20}w_8w_5w_{18} + \\
& 3w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} + \\
& 12w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} + \\
& 6w_{15}w_6^2c_8^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - \\
& 12w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - 3w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} + \\
& 6w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 24w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - \\
& 3w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - 3w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{20}w_{17}w_8w_5w_{18} - 12w_{15}w_6^2c_8^2v_1^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} + 6w_{15}w_6^2v_1v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - \\
& 12w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{20}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{17}w_8w_5w_{18} + 12w_6^2v_1v_2^2w_2^2v_3^2w_{20}w_8w_5w_{18} - 12w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{17}w_8w_5w_{18} + \\
& 6w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{20}w_8w_5w_{18} - 24w_{15}w_6^2c_8^2v_1w_7^2w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1^2v_2^2v_3w_{17}w_8w_5w_{18} - 24w_{15}w_6^2c_8^4v_{17}w_{20}w_{17}w_8w_5w_{18} - \\
& 12w_{15}w_6v_1v_2^2w_2^2v_3^2w_{17}w_8w_5w_{18} + 12w_6^2c_8^2v_1v_2^2w_2^2w_{20}w_8w_5w_{18} - 48w_{15}w_6^2c_8^4v_{17}w_7^2w_{20}w_{17}w_8w_5w_{18} - 12w_{15}w_6v_1v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} - \\
& 12w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 12w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 3w_6^2c_8^2v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2v_1v_2^2w_2^2v_3w_{20}w_8w_5w_{18} - \\
& 12w_{15}w_6v_1^2v_2^2w_2^2v_3w_{20}w_8w_5w_{18} + 12w_{15}w_6^2v_1v_2^2w_2^2v_3^2w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{20}w_8w_5w_{18} + \\
& 6w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_8w_5w_{18} - 12w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} - 12w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 12w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - \\
& 6w_{15}w_6^2v_1v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 24w_{15}w_6^2c_8^2v_1w_7^2w_{20}w_{17}w_8w_5w_{18} - 12w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2v_1v_2^2w_2^2v_3w_{20}w_8w_5w_{18} + \\
& 2w_{15}w_6^2c_8^4v_{17}w_7^2w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2v_1v_2^2w_2^2v_3^2w_{17}w_8w_5w_{18} + 3w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_8w_5w_{18} - \\
& 6w_{15}w_6^2c_8^2v_1^2v_2^2v_3w_{20}w_{17}w_8w_5w_{18} + 24w_{15}c_8^4v_{17}w_7^2w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{20}w_{17}w_8w_5w_{18} + 6w_6^2c_8^2v_1^2v_2^2v_3w_{20}w_{17}w_8w_5w_{18} - \\
& 6w_{15}w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - 12w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{17}w_8w_5w_{18} - 6w_6^2c_8^2v_1v_2^2w_2^2w_{20}w_{17}w_8w_5w_{18} + \\
& 12w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} + 3w_6^2v_1v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_2^2w_2^2v_3w_{17}w_8w_5w_{18} + 6w_{15}w_6^2c_8^2v_1v_2^2w_2^2w_{20}w_8w_5w_{18} + \\
& 6w_6^2v_1^2v_2^2w_2^2v_3w_{20}w_8w_5w_{18} - 6w_{15}w_6^2c_8^2v_1^2v_2^2v_3w_{20}w_8w_5w_{18} + 6w_{15}w_6v_1v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 6w_{15}w_6v_1^2v_2^2w_2^2v_3w_{20}w_{17}w_8w_5w_{18} - \\
& 6w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w_5w_{18} - 48w_{15}w_6^2c_8^4v_{17}w_7^2w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6v_1v_2^2w_2^2v_3^2w_{17}w_8w_5w_{18} + 6w_{15}w_6v_1v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} + \\
& 3w_{15}w_6^2v_1v_2^2w_2^2v_3^2w_{20}w_{17}w_8w_5w_{18} + 6w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_8w_5w_{18} - 12w_{15}w_6^2v_1^2v_2^2v_3w_{20}w_{17}w_8w_5w_{18} + 12w_{15}w_6^2c_8^2v_1w_7^2v_3^2w_{20}w_{17}w_8w$$

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$$\begin{aligned} & \omega_6^2\omega_{19}\omega_7^2v_3^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2 + 12\omega_{19}\omega_7^2v_3^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 + 12\omega_{16}\omega_{19}\omega_7^2v_3^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 12\omega_6^2c_s^2\omega_7\omega_{20}\omega_{11}\omega_8^2\omega_5\omega_{18}^2 - 12\omega_6^2\omega_{19}\omega_7^2\omega_{11}^2\omega_8\omega_5\omega_{18}^2 - \\ & 24\omega_{16}\omega_{19}c_s^2\omega_7\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 36\omega_{16}\omega_{19}c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2 - 12\omega_{16}\omega_7^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 12\omega_{19}\omega_7^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 18\omega_{16}\omega_{19}\omega_7^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18} + \\ & 12\omega_6^2c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 + 30\omega_6^2\omega_{19}c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18}^2 - 12\omega_6^2\omega_{19}\omega_7^2v_3^2\omega_{11}^2\omega_8\omega_5^2\omega_{18}^2 + 12\omega_6^2\omega_{19}c_s^2\omega_7^2\omega_{11}\omega_8\omega_5^2\omega_{18}^2 + \\ & \omega_6^2\omega_{19}\omega_7^2v_3^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 6\omega_{16}\omega_{19}\omega_7\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18} + 12\omega_{16}\omega_{19}c_s^2\omega_7\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 12\omega_{16}\omega_7v_3^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18} + \\ & 6\omega_6^2c_s^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} - 6\omega_6^2\omega_{19}\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} + 12\omega_6^2\omega_{19}c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} - 6\omega_6^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} - 12\omega_6\omega_{19}\omega_7^2\omega_{11}^2\omega_8\omega_5^2\omega_{18} + \\ & 24\omega_6^2\omega_{19}c_s^2\omega_7\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18}^2 - 6\omega_6^2\omega_{19}\omega_7^2\omega_{11}\omega_8^2\omega_5^2\omega_{18} + 6\omega_6^2\omega_{19}\omega_7v_3^2\omega_{20}\omega_{11}\omega_8^2\omega_5^2\omega_{18} + 12\omega_{16}\omega_{19}\omega_7^2v_3^2\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 6\omega_6^2\omega_{19}\omega_7^2v_3^2\omega_{11}\omega_8^2\omega_5^2\omega_{18} - \\ & 6\omega_6^2\omega_{19}\omega_7^2v_3^2\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} + 6\omega_6^2\omega_{19}c_s^2\omega_7^2\omega_{11}\omega_8\omega_5^2\omega_{18} - 54\omega_{16}\omega_{19}c_s^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} + 12\omega_6^2\omega_{19}c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5^2\omega_{18} \end{aligned}$$

$$\begin{aligned}
C_{61} = & 24\omega_6 c_s^4 w_{18} + 36\omega_6 v_3^2 w_{18} - 24\omega_6 v_3^2 w_{11} w_{18} - \omega_6^2 c_s^4 w_{11}^2 w_{18} + 72\omega_6^2 c_s^2 v_3^2 w_{11}^2 + 72\omega_6^2 c_s^2 v_3^2 w_{11} w_{18} + 288\omega_6 c_s^2 v_3^2 w_{18} + 36\omega_6^2 v_3^4 w_{11} w_{18} + \\
& 12\omega_6^2 c_s^2 w_{11}^2 w_{18} - 144\omega_6 c_s^2 v_3^2 w_{11} w_{18} + 96\omega_6 v_3^4 w_{11}^2 w_{18} + 48\omega_6 c_s^2 w_{11} w_{18} + 24c_s^2 w_{11}^2 w_{18} + 48v_3^4 w_{11} w_{18} + 12\omega_6^2 v_3^4 w_{11}^2 + 24\omega_6 c_s^2 w_{11}^2 + 216c_s^2 v_3^2 w_{11}^2 w_{18} + \\
& 12\omega_6^2 c_s^2 w_{11}^2 w_{18} + 24\omega_6 v_3^4 w_{11} w_{18} - 432\omega_6 c_s^2 v_3^2 w_{11}^2 w_{18} + 12\omega_6^2 c_s^2 w_{11}^2 + 24\omega_6 v_3^2 w_{11}^2 - 36\omega_6^2 v_3^2 w_{11}^2 w_{18} + 72\omega_6 v_3^4 w_{11}^2 + 150\omega_6^2 c_s^2 v_3^2 w_{11}^2 w_{18} + \\
& 48\omega_6 c_s^2 w_{11}^2 w_{18} - 96\omega_6 v_3^2 w_{11}^2 w_{18} + 12\omega_6^2 c_s^2 w_{18} - 48v_3^4 w_{11}^2 w_{18} - 24c_s^4 w_{11}^2 w_{18} - 144\omega_6^2 c_s^2 v_3^2 w_{18} + 3\omega_6^2 v_3^2 w_{11}^2 w_{18} + 48\omega_6 v_3^2 w_{11}^2 w_{18} + \\
& 12\omega_6^2 c_s^2 v_3^2 w_{11}^2 w_{18} - 12\omega_6^2 v_3^2 w_{11}^2 - 24\omega_6 c_s^2 w_{11}^2 - 24\omega_6 c_s^2 w_{18} - 48v_3^4 w_{11}^2 w_{18} - 24c_s^4 w_{11}^2 w_{18} - 36\omega_6^2 v_3^4 w_{11}^2 - 14\omega_6^2 c_s^2 w_{11}^2 w_{18} - 30\omega_6^2 v_3^4 w_{11}^2 w_{18} - \\
& 48\omega_6 c_s^2 w_{11}^2 w_{18} - 96\omega_6 v_3^2 w_{11}^2 w_{18} - 3\omega_6^2 v_3^4 w_{11}^2 w_{18} - 72\omega_6 v_3^2 w_{18} + 432\omega_6^2 c_s^2 v_3^2 w_{11}^2 w_{18} - 48\omega_6 v_3^4 w_{11}^2 w_{18} - 12\omega_6^2 c_s^4 w_{18} - 216c_s^2 v_3^2 w_{11}^2 w_{18} + \\
& 24c_s^4 w_{11}^2 w_{18} + 48v_3^4 w_{11}^2 w_{18} + 30\omega_6^2 v_3^2 w_{11}^2 w_{18} + 14\omega_6^2 c_s^4 w_{11}^2 w_{18} - 12\omega_6^2 c_s^2 w_{11}^2 + 96\omega_6 v_3^2 w_{11}^2 w_{18} + 48\omega_6 c_s^2 w_{11}^2 w_{18} - 24\omega_6 v_3^4 w_{11}^2 - 126\omega_6^2 c_s^2 v_3^2 w_{11}^2 w_{18}
\end{aligned}$$

$$C_{63} = -60\omega_6^2 v_3^2 \omega_{18} + 36\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 33\omega_6^2 c_s^2 \omega_{11} \omega_{18} + 36\omega_{11}^2 \omega_{18} - 120\omega_6 c_s^2 \omega_{11} \omega_{18}^2 + 24\omega_6^2 \omega_{18}^3 - 60c_s^2 \omega_{11}^2 \omega_{18} - 48\omega_6 c_s^2 \omega_{11}^2 - 25\omega_6^2 \omega_{11} \omega_{18}^2 - 12\omega_6^2 \omega_{11} \omega_{18} - 3\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 24\omega_6 c_s^2 \omega_{11} \omega_{18} - 48\omega_6 v_3^2 \omega_{11}^2 + 24\omega_6 \omega_{18}^2 + 61\omega_6^2 v_3^2 \omega_{11} \omega_{18}^2 + 168\omega_6 v_3^2 \omega_{11}^2 \omega_{18} - 36\omega_6^2 c_s^2 \omega_{18}^2 - 72\omega_6 \omega_{11}^2 \omega_{18} + 84\omega_3 \omega_{11} \omega_{18} - 5\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 72\omega_6 v_3^2 \omega_{11} \omega_{18} + 24\omega_6 \omega_{11} \omega_{18} + 24\omega_6^2 v_3^2 \omega_{11}^2 + 21\omega_3^2 \omega_{11}^2 \omega_{18} + 72\omega_6 c_s^2 \omega_{18}^2 + 60c_s^2 \omega_{11} \omega_{18}^2 + 39\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 12\omega_6^2 \omega_{11}^2 - 36\omega_{11}^2 \omega_{18} + 120\omega_6 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 48\omega_6 \omega_{18}^2 + 120\omega_6 v_3^2 \omega_{18}^2 + 2\omega_6^2 \omega_{11}^2 \omega_{18} - 84v_3^2 \omega_{11}^2 \omega_{18} - 51\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 24\omega_6^2 c_s^2 \omega_{11}^2 - 168\omega_6 v_3^2 \omega_{11} \omega_{18}^2 + 72\omega_6 \omega_{11} \omega_{18}^2$$


attached text file: output_d3q27_nse_mrt1_symbolic_pde_02.txt

$$\begin{aligned}
& v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{\delta_1 v_1 v_2}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 \rho v_2}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_1 \rho v_1}{\delta_t} \frac{\partial v_2}{\partial x_1} + (v_2^2 + c_s^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2 \delta_1 \rho v_2}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_1 v_2 v_3}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\delta_1 \rho v_3}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\
& \frac{\delta_1 \rho v_2}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2}{2 \delta_t \omega_5} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2}{2 \delta_t \omega_5} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\
& (-2 + 6v_2^2 + 4c_s^2 + \omega_{10} - 2c_s^2 \omega_{10} - 3\omega_{10} v_2^2) \frac{\delta_1^2}{\delta_t \omega_{10}} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_{10}) \frac{3 \delta_1^2 \rho v_2}{\delta_t \omega_{10}} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2 \delta_t \omega_7} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\
& (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2 \delta_t \omega_7} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2 \rho}{2 \delta_t \omega_5} \frac{\partial^2 v_2}{\partial x^2} + (-2 + \omega_5) \frac{\delta_1^2 c_s^2 \rho}{2 \delta_t \omega_5} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} +
\end{aligned}$$

$$\begin{aligned}
& (-2 + 2v_2^2 + 6c_s^2 + \omega_{10} - 3c_s^2\omega_{10} - \omega_{10}v_2^2) \frac{\delta_l^2 v_2}{2\delta_t \omega_{10}} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + 6v_2^2 + 2c_s^2 + \omega_{10} - c_s^2\omega_{10} - 3\omega_{10}v_2^2) \frac{\delta_l^2 \rho}{2\delta_t \omega_{10}} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_7) \frac{\delta_l^2 c_s^2 \rho}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2 \rho}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_3^2} + C_1 \frac{\delta_l^3 v_1 v_2}{12\omega_9 \omega_{12} \delta_t \omega_5} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_l^3 \rho v_2}{12\omega_9 \omega_{12} \delta_t \omega_5} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{\delta_l^3 \rho v_1}{6\omega_{12} \delta_t \omega_5^2} \frac{\partial^3 v_2}{\partial x_1^3} + \\
& (-12 - \omega_5^2 + 12\omega_5) \frac{\delta_l^3 c_s^4}{6\delta_t \omega_5^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (-2\omega_{12} - \omega_5^2 + 2\omega_5 + \omega_{12}\omega_5) \frac{\delta_l^3 c_s^2 \rho v_1}{\omega_{12} \delta_t \omega_5^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (-12\omega_{15}\omega_{10} + 12\omega_5^2 - 12\omega_{15}\omega_5 + 12\omega_{15}\omega_{10}\omega_5 - 12\omega_{10}\omega_5^2 + 12\omega_{10}\omega_5 - \omega_{15}\omega_{10}\omega_5^2) \frac{\delta_l^3 c_s^2 \rho v_2}{6\omega_{15} \delta_t \omega_{10} \omega_5^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& C_4 \frac{\delta_l^3 v_1 v_2}{\omega_{15} \delta_t \omega_{10} \omega_5} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + C_5 \frac{\delta_l^3 \rho v_2}{12\omega_{15} \delta_t \omega_{10} \omega_5^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_6 \frac{\delta_l^3 \rho v_1}{\omega_{15} \delta_t \omega_{10} \omega_5} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_7 \frac{\delta_l^3 \rho}{12\delta_t \omega_{10}^2} \frac{\partial^3 \rho}{\partial x_2^2} + \\
& (-24 + 60v_2^2 + 11\omega_{10}^2 v_2^2 - 4\omega_{10}^2 + 36c_s^2 + 24\omega_{10} - 36c_s^2\omega_{10} + 5c_s^2\omega_{10}^2 - 60\omega_{10}v_2^2) \frac{\delta_l^3 \rho v_2}{6\delta_t \omega_{10}^2} \frac{\partial^3 v_2}{\partial x_3^2} + \\
& (\omega_5^2 - \omega_8\omega_5 - \omega_7\omega_8 + \omega_7\omega_5 + \omega_7\omega_8\omega_5 - \omega_7\omega_5^2) \frac{\delta_l^3 c_s^2 \rho v_3}{\delta_t \omega_7 \omega_8 \omega_5^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} + \\
& (-\omega_6\omega_7\omega_8\omega_5 - 6\omega_8\omega_5 - 6\omega_7\omega_8 + 6\omega_6\omega_7 + 6\omega_7\omega_8\omega_5 - 6\omega_6\omega_7\omega_5 + 6\omega_6\omega_5) \frac{\delta_l^3 c_s^2 \rho v_2}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (\omega_5^2 - \omega_8\omega_5 - \omega_7\omega_8 + \omega_7\omega_5 + \omega_7\omega_8\omega_5 - \omega_7\omega_5^2) \frac{\delta_l^3 c_s^2 \rho v_3}{\delta_t \omega_7 \omega_8 \omega_5^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (\omega_7^2 - \omega_7^2\omega_5 - \omega_8\omega_5 - \omega_7\omega_8 + \omega_7\omega_5 + \omega_7\omega_8\omega_5) \frac{\delta_l^3 c_s^2 \rho v_1}{\delta_t \omega_7^2 \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{\delta_l^3 v_2 v_3}{\delta_t \omega_{16} \omega_{10}^2 \omega_7} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_9 \frac{\delta_l^3 \rho v_3}{\delta_t \omega_{16} \omega_{10}^2 \omega_7} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} \\
& + C_{10} \frac{\delta_l^3 \rho v_2}{12\delta_t \omega_{16} \omega_{10}^2 \omega_7^2} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-\omega_6\omega_7\omega_8\omega_5 - 6\omega_8\omega_5 - 6\omega_7\omega_8 + 6\omega_6\omega_7 + 6\omega_7\omega_8\omega_5 - 6\omega_6\omega_7\omega_5 + 6\omega_6\omega_5) \frac{\delta_l^3 c_s^2 \rho v_2}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^3} + \\
& (\omega_7^2 - \omega_7^2\omega_5 - \omega_8\omega_5 - \omega_7\omega_8 + \omega_7\omega_5 + \omega_7\omega_8\omega_5) \frac{\delta_l^3 c_s^2 \rho v_1}{\delta_t \omega_7^2 \omega_8 \omega_5} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^3} + (-12 - \omega_7^2 + 12\omega_7) \frac{\delta_l^3 c_s^4}{6\delta_t \omega_7^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_2^3} + \\
& (12\omega_7^2 - \omega_{16}\omega_{10}\omega_7^2 - 12\omega_{16}\omega_{10} - 12\omega_{16}\omega_7 + 12\omega_{16}\omega_{10}\omega_7 + 12\omega_{10}\omega_7 - 12\omega_{10}\omega_7^2) \frac{\delta_l^3 c_s^2 \rho v_2}{6\delta_t \omega_{16} \omega_{10} \omega_7^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_2^3} + \\
& (-\omega_7^2 + \omega_{19}\omega_7 - 2\omega_{19} + 2\omega_7) \frac{\delta_l^3 c_s^2 \rho v_3}{\omega_{19} \delta_t \omega_7^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_2^3} + C_{11} \frac{\delta_l^3 v_2 v_3}{12\omega_{19} \delta_t \omega_7 \omega_{11}} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{\delta_l^3 \rho v_3}{6\omega_{19} \delta_t \omega_7^2} \frac{\partial^3 v_2}{\partial x_3^3} + C_{13} \frac{\delta_l^3 \rho v_2}{12\omega_{19} \delta_t \omega_7 \omega_{11}} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_{14} \frac{\delta_l^4 v_2}{24\omega_9^2 \omega_{12}^2 \delta_t \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\delta_l^4 \rho v_1 v_2}{12\omega_9^2 \omega_{12}^2 \delta_t \omega_5^2} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{\delta_l^4 \rho}{24\omega_{12}^2 \delta_t \omega_5^3} \frac{\partial^4 v_2}{\partial x_1^4} + C_{17} \frac{\delta_l^4 v_1}{12\omega_{15} \omega_9^2 \omega_{12}^2 \delta_t \omega_{10} \omega_5^3 \omega_{21}} \frac{\partial^4 \rho}{\partial x_1^4 \partial x_2} + \\
& C_{18} \frac{\delta_l^4 \rho}{12\omega_{15} \omega_9^2 \omega_{12}^2 \delta_t \omega_{10} \omega_5^3 \omega_{21}} \frac{\partial^4 v_1}{\partial x_1^4 \partial x_2} + C_{19} \frac{\delta_l^4 \rho v_1 v_2}{12\omega_{15} \omega_9^2 \omega_{12}^2 \delta_t \omega_{10} \omega_5^3 \omega_{21}} \frac{\partial^4 v_2}{\partial x_1^4 \partial x_2} + C_{20} \frac{\delta_l^4 v_2}{12\omega_{15} \omega_{12}^2 \delta_t \omega_{10} \omega_5^3 \omega_{21}} \frac{\partial^4 \rho}{\partial x_1^4 \partial x_2^2} + \\
& C_{21} \frac{\delta_l^4 \rho v_1 v_2}{2\omega_{15}^2 \omega_9 \omega_{12}^2 \delta_t \omega_{10}^3 \omega_{21}} \frac{\partial^4 v_1}{\partial x_1^4 \partial x_2^2} + C_{22} \frac{\delta_l^4 \rho}{12\omega_{15}^2 \omega_{12}^2 \delta_t \omega_{10}^3 \omega_{21}} \frac{\partial^4 v_2}{\partial x_1^4 \partial x_2^2} + C_{23} \frac{\delta_l^4 v_1}{4\omega_{15}^2 \delta_t \omega_{10}^3 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^4 \partial x_2^2} + \\
& C_{24} \frac{\delta_l^4 \rho}{12\omega_{15}^2 \delta_t \omega_{10}^3 \omega_5^3} \frac{\partial^4 v_1}{\partial x_1^4 \partial x_2^2} + C_{25} \frac{\delta_l^4 \rho v_1 v_2}{4\omega_{15}^2 \delta_t \omega_{10}^3 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1^4 \partial x_2^2} + C_{26} \frac{\delta_l^4 v_2}{12\delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_2^2} + C_{27} \frac{\delta_l^4 \rho}{12\delta_t \omega_{10}^3} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& C_{28} \frac{\delta_l^4 v_1 v_2 v_3}{4\omega_9^2 \omega_{12}^2 \omega_6 \delta_t \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^4 \partial x_3} + C_{29} \frac{\delta_l^4 \rho v_2 v_3}{4\omega_9^2 \omega_{12}^2 \omega_6 \delta_t \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_1}{\partial x_1^4 \partial x_3} + C_{30} \frac{\delta_l^4 \rho v_1 v_3}{2\omega_{12}^2 \delta_t \omega_7^2 \omega_{14} \omega_8 \omega_5^3} \frac{\partial^4 v_2}{\partial x_1^4 \partial x_3} + \\
& C_{31} \frac{\delta_l^4 \rho v_1 v_2}{12\omega_9^2 \omega_{12}^2 \omega_6^2 \delta_t \omega_{13} \omega_7^2 \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_3}{\partial x_1^4 \partial x_3} + C_{32} \frac{2\delta_l^4 c_s^4 v_3}{\delta_t \omega_7^2 \omega_8 \omega_5^3} \frac{\partial^4 \rho}{\partial x_1^4 \partial x_2 \partial x_3} + C_{33} \frac{\delta_l^4 c_s^2 \rho v_1 v_3}{\omega_{12}^2 \delta_t \omega_7^2 \omega_{14} \omega_8 \omega_5^3} \frac{\partial^4 v_1}{\partial x_1^4 \partial x_2 \partial x_3} + \\
& C_{34} \frac{\delta_l^4 c_s^2 \rho v_2 v_3}{2\omega_{12}^2 \omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^3} \frac{\partial^4 v_2}{\partial x_1^4 \partial x_2 \partial x_3} + C_{35} \frac{\delta_l^4 c_s^2 \rho}{12\omega_{15} \omega_{12}^2 \omega_6^2 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_{14} \omega_8 \omega_5^3} \frac{\partial^4 v_3}{\partial x_1^4 \partial x_2 \partial x_3} + \\
& C_{36} \frac{\delta_l^4 v_1 v_2 v_3}{\omega_{15}^2 \delta_t \omega_{16}^3 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{37} \frac{\delta_l^4 \rho v_2 v_3}{2\omega_{15}^2 \omega_6 \delta_t \omega_{16}^3 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{38} \frac{\delta_l^4 \rho v_1 v_3}{\omega_{15}^2 \delta_t \omega_{16}^3 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{39} \frac{\delta_l^4 \rho v_1 v_2}{2\omega_{15}^2 \omega_6 \delta_t \omega_{16}^3 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{40} \frac{\delta_l^4 v_3}{4\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{41} \frac{\delta_l^4 \rho v_2 v_3}{4\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& C_{42} \frac{\delta_l^4 \rho}{12\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{43} \frac{\delta_l^4}{12\omega_{12} \omega_6^2 \omega_{19} \delta_t \omega_7^2 \omega_{20} \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{44} \frac{\delta_l^4 \rho}{4\omega_9 \omega_{12} \omega_6^2 \omega_{19} \delta_t \omega_{13} \omega_7^2 \omega_{20} \omega_{14} \omega_8 \omega_5^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& C_{45} \frac{\delta_l^4 \rho}{4\omega_{12} \omega_{19} \delta_t \omega_7^3 \omega_{20} \omega_{14} \omega_8 \omega_5^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + C_{46} \frac{\delta_l^4 \rho v_3}{2\omega_{12} \omega_6^2 \omega_{19} \delta_t \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8 \omega_5^2 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{47} \frac{\delta_l^4}{2\omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{48} \frac{\delta_l^4 \rho}{12\omega_{15} \omega_6^2 \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^3 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{49} \frac{\delta_l^4 \rho v_2}{2\omega_{15} \omega_6 \omega_{19} \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{50} \frac{\delta_l^4 \rho}{2\omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^3 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{51} \frac{\delta_l^4 v_2}{12\omega_{19} \delta_t \omega_{16}^3 \omega_{10}^3 \omega_7^2 \omega_{23}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{52} \frac{\delta_l^4 \rho}{12\omega_{19} \delta_t \omega_{16}^3 \omega_{10}^3 \omega_7^2 \omega_{23}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{\delta_l^4 \rho v_2 v_3}{2\omega_{19}^2 \delta_t \omega_{16}^3 \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{54} \frac{\delta_l^4 v_1 v_2 v_3}{4\omega_6 \omega_{19} \delta_t \omega_{16}^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{\delta_l^4 \rho v_2 v_3}{12\omega_6^2 \omega_{19} \delta_t \omega_{16}^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{56} \frac{\delta_l^4 \rho v_1 v_3}{2\omega_{19} \delta_t \omega_{16}^3 \omega_{20} \omega_8 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^3} + \\
& C_{57} \frac{\delta_l^4 \rho v_1 v_2}{4\omega_6 \omega_{19} \delta_t \omega_{16}^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{58} \frac{\delta_l^4 v_3}{12\omega_{19}^2 \delta_t \omega_{16} \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{59} \frac{\delta_l^4 \rho v_2 v_3}{12\omega_{19}^2 \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{60} \frac{\delta_l^4 \rho}{12\omega_{19}^2 \delta_t \omega_{16} \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{\delta_l^4 v_2}{24\omega_{19}^2 \delta_t \omega_{16}^2 \omega_{11}^2} \frac{\partial^4 \rho}{\partial x_3^3} + C_{62} \frac{\delta_l^4 \rho}{24\omega_{19}^2 \delta_t \omega_7^3} \frac{\partial^4 v_2}{\partial x_3^3} + C_{63} \frac{\delta_l^4 \rho v_2 v_3}{12\omega_{19}^2 \delta_t \omega_7^2 \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_3^3} = 0,
\end{aligned}$$

where:

$$C_1 = -6\omega_{12}v_1^2\omega_5 - \omega_9\omega_{12}\omega_5 + 18\omega_9c_s^2\omega_5 + 12\omega_9 - 12\omega_9v_1^2 - 12\omega_{12} - 6\omega_9\omega_5 - 36\omega_9c_s^2 + 3\omega_9\omega_{12}c_s^2\omega_5 + 36\omega_{12}c_s^2 + \omega_9\omega_{12}v_1^2\omega_5 + 12\omega_{12}v_1^2 + 6\omega_9v_1^2\omega_5 - 18\omega_{12}c_s^2\omega_5 + 6\omega_{12}\omega_5$$

$$C_2 = -18\omega_{12}v_1^2\omega_5 - \omega_9\omega_{12}\omega_5 + 6\omega_9c_s^2\omega_5 + 12\omega_9 - 36\omega_9v_1^2 - 12\omega_{12} - 6\omega_9\omega_5 - 12\omega_9c_s^2 + \omega_9\omega_{12}c_s^2\omega_5 + 12\omega_{12}c_s^2 + 3\omega_9\omega_{12}v_1^2\omega_5 + 36\omega_{12}v_1^2 + 18\omega_9v_1^2\omega_5 - 6\omega_{12}c_s^2\omega_5 + 6\omega_{12}\omega_5$$

$$C_3 = 3\omega_{12}v_1^2\omega_5 - 6v_1^2\omega_5 - 3\omega_5^2 - \omega_{12}v_1^2\omega_5^2 + 3v_1^2\omega_5^2 + 3c_s^2\omega_5^2 - 12\omega_{12}c_s^2 - 3\omega_{12}c_s^2\omega_5^2 + \omega_{12}\omega_5^2 - 6c_s^2\omega_5 + 15\omega_{12}c_s^2\omega_5 + 6\omega_5 - 3\omega_{12}\omega_5$$

$$C_4 = -\omega_{10}^2v_2^2 + \omega_{15}v_2^2\omega_5 - 3\omega_{15}c_s^2\omega_{10}\omega_5 - \omega_{15}\omega_{10} - \omega_{10}^2\omega_5 + \omega_{10}^2 + 3c_s^2\omega_{10}^2\omega_5 - \omega_{10}v_2^2\omega_5 - \omega_{15}\omega_5 + \omega_{15}\omega_{10}v_2^2 - \omega_{15}\omega_{10}v_2^2\omega_5 + \omega_{10}^2v_2^2\omega_5 + \omega_{15}\omega_{10}\omega_5 + 3\omega_{15}c_s^2\omega_5 + 3\omega_{15}c_s^2\omega_{10} + \omega_{10}\omega_5 - 3c_s^2\omega_{10}\omega_5 - 3c_s^2\omega_{10}^2$$

$$C_5 = -24\omega_{15}c_s^2\omega_{10}\omega_5 - 12\omega_{15}\omega_5^2 - 12\omega_{10}v_2^2\omega_5^2 + 12\omega_{10}^2\omega_5 - 3\omega_{15}\omega_{10}^2v_2^2\omega_5^2 - 12c_s^2\omega_{10}^2\omega_5 + 3\omega_{15}\omega_{10}^2\omega_5^2 + 12c_s^2\omega_{10}^2\omega_5^2 - 6\omega_{15}\omega_{10}^2\omega_5 - 12\omega_{10}^2\omega_5^2 + 6\omega_{15}\omega_{10}^2v_2^2\omega_5^2 + 12\omega_{15}v_2^2\omega_5^2 - 18\omega_{15}c_s^2\omega_{10}\omega_5^2 - 11\omega_{15}c_s^2\omega_{10}^2\omega_5^2 - 12\omega_{10}^2v_2^2\omega_5 - 12c_s^2\omega_{10}\omega_5^2 - 24\omega_{15}c_s^2\omega_{10}^2 + 12\omega_{10}\omega_5^2 + 36\omega_{15}c_s^2\omega_5^2 + 6\omega_{15}\omega_{10}\omega_5^2 - 6\omega_{15}\omega_{10}v_2^2\omega_5^2 + 12\omega_{10}^2v_2^2\omega_5^2 + 42\omega_{15}c_s^2\omega_{10}^2\omega_5$$

$$C_6 = -3\omega_{10}^2v_2^2 + 3\omega_{15}v_2^2\omega_5 - \omega_{15}c_s^2\omega_{10}\omega_5 - \omega_{15}\omega_{10} - \omega_{10}^2\omega_5 + \omega_{10}^2 + c_s^2\omega_{10}^2\omega_5 - 3\omega_{10}v_2^2\omega_5 - \omega_{15}\omega_5 + 3\omega_{15}\omega_{10}v_2^2 - 3\omega_{15}\omega_{10}v_2^2\omega_5 + 3\omega_{10}^2v_2^2\omega_5 + \omega_{15}\omega_{10}\omega_5 + \omega_{15}c_s^2\omega_5 + \omega_{15}c_s^2\omega_{10} + \omega_{10}\omega_5 - c_s^2\omega_{10}\omega_5 - c_s^2\omega_{10}^2$$

$$C_7 = -12c_s^4\omega_{10} - 36v_2^2 - 7\omega_{10}^2v_2^2 + 24c_s^2\omega_{10}^2v_2^2 - 36\omega_{10}v_2^4 - 12c_s^2 + c_s^4\omega_{10}^2 + 12c_s^4 + 12c_s^2\omega_{10} - c_s^2\omega_{10}^2 + 36v_2^4 + 7\omega_{10}^2v_2^4 + 36\omega_{10}v_2^2 - 144c_s^2\omega_{10}v_2^2 + 144c_s^2v_2^2$$

$$C_8 = -\omega_{10}^2v_2^2 + \omega_{16}\omega_{10}v_2^2 - \omega_{10}v_2^2\omega_7 + \omega_{10}^2 + 3c_s^2\omega_{16}\omega_{10} - \omega_{16}\omega_{10} - 3c_s^2\omega_{16}\omega_{10}\omega_7 - \omega_{16}\omega_7 - \omega_{10}^2\omega_7 + \omega_{16}\omega_{10}\omega_7 + 3c_s^2\omega_{16}\omega_7 + 3c_s^2\omega_{10}^2\omega_7 + \omega_{10}\omega_7 - 3c_s^2\omega_{10}\omega_7 - \omega_{16}\omega_{10}v_2^2\omega_7 + \omega_{16}v_2^2\omega_7 - 3c_s^2\omega_{10}^2 + \omega_{10}^2v_2^2\omega_7$$

$$C_9 = -3\omega_{10}^2v_2^2 + 3\omega_{16}\omega_{10}v_2^2 - 3\omega_{10}v_2^2\omega_7 + \omega_{10}^2 + c_s^2\omega_{16}\omega_{10} - \omega_{16}\omega_{10} - c_s^2\omega_{16}\omega_{10}\omega_7 - \omega_{16}\omega_7 - \omega_{10}^2\omega_7 + \omega_{16}\omega_{10}\omega_7 + c_s^2\omega_{16}\omega_7 + c_s^2\omega_{10}^2\omega_7 + \omega_{10}\omega_7 - c_s^2\omega_{10}\omega_7 - 3\omega_{16}\omega_{10}v_2^2\omega_7 + 3\omega_{16}v_2^2\omega_7 - c_s^2\omega_{10}^2 + 3\omega_{10}^2v_2^2\omega_7$$

$$C_{10} = 6\omega_{16}\omega_{10}^2v_2^2\omega_7 + 12c_s^2\omega_{10}^2\omega_7^2 + 36c_s^2\omega_{16}\omega_7^2 - 12\omega_{10}^2\omega_7^2 - 12\omega_{16}\omega_7^2 + 6\omega_{16}\omega_{10}\omega_7^2 - 18c_s^2\omega_{16}\omega_{10}\omega_7^2 - 24c_s^2\omega_{16}\omega_{10}^2 - 24c_s^2\omega_{16}\omega_{10}\omega_7 + 12\omega_{10}^2\omega_7 - 12\omega_{10}v_2^2\omega_7^2 - 3\omega_{16}\omega_{10}^2v_2^2\omega_7^2 - 12c_s^2\omega_{10}^2\omega_7 - 6\omega_{16}\omega_{10}^2\omega_7 + 12\omega_{16}v_2^2\omega_7^2 + 12\omega_{10}^2v_2^2\omega_7^2 - 6\omega_{16}\omega_{10}v_2^2\omega_7^2 + 42c_s^2\omega_{16}\omega_{10}^2\omega_7 - 11c_s^2\omega_{16}\omega_{10}^2\omega_7^2 - 12\omega_{10}^2v_2^2\omega_7 - 12c_s^2\omega_{10}\omega_7^2 + 12\omega_{10}\omega_7^2 + 3\omega_{16}\omega_{10}^2\omega_7^2$$

$$C_{11} = -36c_s^2\omega_{11} - 6\omega_{19}\omega_7v_3^2 - \omega_{19}\omega_7\omega_{11} + 36\omega_{19}c_s^2 + 6\omega_{19}\omega_7 - 12\omega_{19} + \omega_{19}\omega_7v_3^2\omega_{11} - 12v_3^2\omega_{11} - 6\omega_7\omega_{11} + 18c_s^2\omega_7\omega_{11} + 3\omega_{19}c_s^2\omega_7\omega_{11} + 6\omega_7v_3^2\omega_{11} + 12\omega_{19}v_3^2 + 12\omega_{11} - 18\omega_{19}c_s^2\omega_7$$

$$C_{12} = 3\omega_{19}\omega_7v_3^2 - 3\omega_7^2 - 12\omega_{19}c_s^2 - 3\omega_{19}\omega_7 + \omega_{19}\omega_7^2 - 6\omega_7v_3^2 + 6\omega_7 - 3\omega_{19}c_s^2\omega_7^2 + 3\omega_7^2v_3^2 - 6c_s^2\omega_7 + 15\omega_{19}c_s^2\omega_7 - \omega_{19}\omega_7^2v_3^2 + 3c_s^2\omega_7^2$$

$$C_{13} = -12c_s^2\omega_{11} - 18\omega_{19}\omega_7v_3^2 - \omega_{19}\omega_7\omega_{11} + 12\omega_{19}c_s^2 + 6\omega_{19}\omega_7 - 12\omega_{19} + 3\omega_{19}\omega_7v_3^2\omega_{11} - 36v_3^2\omega_{11} - 6\omega_7\omega_{11} + 6c_s^2\omega_7\omega_{11} + \omega_{19}c_s^2\omega_7\omega_{11} + 18\omega_7v_3^2\omega_{11} + 36\omega_{19}v_3^2 + 12\omega_{11} - 6\omega_{19}c_s^2\omega_7$$

$$C_{14} = -48\omega_9\omega_{12}^4c_s^4\omega_5 - 36\omega_9\omega_{12}^2v_1^2\omega_5^2 - 48\omega_9^2\omega_{12}v_1^4 + 12\omega_9^2c_s^4\omega_5^2 - 24\omega_{12}^2c_s^2\omega_5 - 48\omega_9\omega_{12}v_1^4\omega_5 + 72\omega_9\omega_{12}c_s^2v_1^2\omega_5^2 + 24\omega_{12}^2v_1^2\omega_5 - 36\omega_{12}^2v_1^4\omega_5^2 - 12\omega_9^2\omega_{12}c_s^4\omega_5^2 + 48\omega_9\omega_{12}^2v_1^4 - 126\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^2 - 96\omega_9^2\omega_{12}v_1^2\omega_5 - 3\omega_9^2\omega_{12}^2v_1^4\omega_5^2 - 144\omega_9^2c_s^2v_1^2\omega_5^2 + 72\omega_9^2c_s^2v_1^2\omega_5^2 + \omega_9^2\omega_{12}^2c_s^2\omega_5^2 + 24\omega_9\omega_{12}^2c_s^4 + 432\omega_9^2\omega_{12}c_s^2v_1^2\omega_5 + 48\omega_9^2\omega_{12}c_s^4\omega_5 + 30\omega_9^2\omega_{12}v_1^2\omega_5^2 - 24\omega_9^2\omega_{12}c_s^2 - 24\omega_9c_s^4\omega_5 + 12\omega_{12}^2c_s^2\omega_5^2 + 24\omega_9\omega_{12}v_1^2\omega_5^2 - 144\omega_9\omega_{12}c_s^2v_1^2\omega_5^2 + 12\omega_9^2v_1^2\omega_5^2 + 72\omega_{12}^2v_1^4\omega_5 + 14\omega_9\omega_{12}^2c_s^4\omega_5^2 + 96\omega_9\omega_{12}^2v_1^2\omega_5 + 12\omega_9^2\omega_{12}c_s^2\omega_5^2 + 96\omega_9^2\omega_{12}v_1^4\omega_5 + 150\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 + 3\omega_9^2\omega_{12}^2v_1^2\omega_5^2 + 288\omega_{12}^2c_s^2v_1^2\omega_5 - 24\omega_9\omega_{12}^2c_s^2 + 48\omega_9\omega_{12}^2c_s^2\omega_5 + 36\omega_9\omega_{12}^2v_1^4\omega_5^2 + 24\omega_9^2\omega_{12}c_s^2 - 12\omega_9^2c_s^2\omega_5^2 + 216\omega_9\omega_{12}^2c_s^2v_1^2 + 48\omega_9\omega_{12}v_1^2\omega_5 + 24\omega_{12}^2c_s^4\omega_5 - 24\omega_9^2v_1^4\omega_5 + 36\omega_{12}^2v_1^2\omega_5^2 - 12\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 + 24\omega_9^2c_s^2\omega_5 - 24\omega_9\omega_{12}v_1^2\omega_5^2 - 12\omega_{12}^2c_s^4\omega_5^2 + 12\omega_9^2v_1^4\omega_5^2 - 72\omega_{12}^2v_1^2\omega_5 - 14\omega_9\omega_{12}^2c_s^2\omega_5^2 - 96\omega_9\omega_{12}^2v_1^4\omega_5 + 48\omega_9\omega_{12}v_1^2 - 216\omega_9\omega_{12}c_s^2v_1^2 - 144\omega_{12}^2c_s^2v_1^2\omega_5^2 - \omega_9^2\omega_{12}^2c_s^4\omega_5^2 - 48\omega_9\omega_{12}c_s^2\omega_5 - 48\omega_9\omega_{12}^2v_1^2 - 30\omega_9^2\omega_{12}v_1^4\omega_5^2 - 432\omega_9\omega_{12}^2c_s^2v_1^2\omega_5$$

$$C_{15} = 24\omega_9\omega_{12}\omega_5 + 61\omega_9\omega_{12}^2v_1^2\omega_5^2 + 72\omega_{12}^2c_s^2\omega_5 - 48\omega_9^2v_1^2\omega_5 + 12\omega_9\omega_{12}c_s^2\omega_5^2 + 168\omega_9^2\omega_{12}v_1^2\omega_5 + 36\omega_9^2\omega_{12} - 48\omega_{12}^2\omega_5 + 24\omega_{12}^2\omega_5^2 - 3\omega_9^2\omega_{12}^2c_s^2\omega_5^2 + 2\omega_9^2\omega_{12}^2\omega_5^2 - 51\omega_9^2\omega_{12}v_1^2\omega_5^2 - 36\omega_{12}^2c_s^2\omega_5^2 + 24\omega_9^2v_1^2\omega_5^2 - 24\omega_9\omega_{12}c_s^2\omega_5 - 12\omega_9\omega_{12}\omega_5^2 - 168\omega_9\omega_{12}^2v_1^2\omega_5 - 33\omega_9^2\omega_{12}c_s^2\omega_5^2 - 25\omega_9\omega_{12}\omega_5^2 - 5\omega_9^2\omega_{12}^2v_1^2\omega_5^2 + 60\omega_9\omega_{12}^2c_s^2 - 120\omega_9\omega_{12}^2c_s^2\omega_5 - 12\omega_9^2\omega_5^2 - 60\omega_9\omega_{12}c_s^2 + 24\omega_9^2c_s^2\omega_5^2 - 72\omega_9\omega_{12}v_1^2\omega_5 + 21\omega_9^2\omega_{12}\omega_5^2 - 36\omega_9\omega_{12}^2 - 60\omega_{12}^2v_1^2\omega_5^2 - 48\omega_9^2c_s^2\omega_5 + 36\omega_9\omega_{12}v_1^2\omega_5^2 - 72\omega_9^2\omega_{12}\omega_5 + 120\omega_{12}^2v_1^2\omega_5 + 39\omega_9\omega_{12}^2c_s^2\omega_5^2 + 24\omega_9^2\omega_5 - 84\omega_9^2\omega_{12}v_1^2 + 72\omega_9\omega_{12}^2\omega_5 + 120\omega_9^2\omega_{12}c_s^2\omega_5 + 84\omega_9\omega_{12}^2v_1^2$$

$$C_{16} = -96\omega_{12}^2c_s^2v_1^2 + 48\omega_{12}v_1^2\omega_5 - 24\omega_{12}c_s^4\omega_5^2 - 24\omega_{12}c_s^2v_1^2\omega_5 + 12\omega_{12}^2c_s^2\omega_5 - 24\omega_{12}^2v_1^4\omega_5^2 + 6\omega_{12}c_s^4\omega_5^3 + 3\omega_{12}^2v_1^4\omega_5^3 + 12c_s^2v_1^2\omega_5^3 + \omega_{12}^2c_s^2\omega_5^3 - 12\omega_{12}^2c_s^2v_1^2\omega_5^3 - 12v_1^2\omega_5^3 + 18\omega_{12}v_1^2\omega_5^3 - 24c_s^2v_1^2\omega_5^2 - 8\omega_{12}^2c_s^2\omega_5^2 + 24\omega_{12}^2v_1^4\omega_5 - 72\omega_{12}v_1^2\omega_5^2 + 24\omega_{12}^2c_s^4\omega_5 + 24v_1^2\omega_5^2 + 48\omega_{12}c_s^2v_1^2\omega_5^2 - 6\omega_{12}c_s^2\omega_5^3 - 3\omega_{12}^2v_1^2\omega_5^3 + 24\omega_{12}^2c_s^4 + 156\omega_{12}^2c_s^2v_1^2\omega_5 - 48\omega_{12}v_1^4\omega_5 + 24\omega_{12}^2c_s^2\omega_5^2 - 48\omega_{12}^2c_s^4\omega_5 + 24\omega_{12}^2v_1^2\omega_5^2 + 24\omega_{12}^2c_s^4\omega_5^2 + 6\omega_{12}^2c_s^2v_1^2\omega_5^3 - 24\omega_{12}^2v_1^2\omega_5 + 72\omega_{12}v_1^4\omega_5^2 - 24\omega_{12}v_1^2\omega_5^2 - 24v_1^4\omega_5^2 - 72\omega_{12}^2c_s^2v_1^2\omega_5^2 - 3\omega_{12}^2c_s^4\omega_5^3 + 12v_1^4\omega_5^3 - 18\omega_{12}v_1^4\omega_5^3$$

$$C_{17} = -24\omega_{15}\omega_9\omega_{12}^2v_2^2\omega_5^2\omega_{21} - 18\omega_{15}\omega_9^2\omega_{12}c_s^2\omega_{10}\omega_5^2\omega_{21} - 9\omega_{15}\omega_9\omega_{12}^2\omega_{10}v_2^2\omega_5^3\omega_{21} - 3\omega_{15}\omega_9^2\omega_{12}c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21} - 108\omega_{15}\omega_9\omega_{12}^2c_s^2\omega_{10}v_2^2\omega_5^2\omega_{21} + 18\omega_{15}\omega_9^2c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21} - 15\omega_{15}\omega_9^2\omega_{12}\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21} + 12\omega_9\omega_{12}^2c_s^2\omega_5^3\omega_{21} + 18\omega_{15}\omega_9^2\omega_{12}^2c_s^4\omega_{10}\omega_5^3 + 5\omega_{15}\omega_9\omega_{12}^2c_s^2\omega_{10}\omega_5^3\omega_{21} - 48\omega_{15}\omega_9^2\omega_{12}\omega_{10}v_2^2\omega_5^2\omega_{21} - 24\omega_{15}\omega_9^2\omega_{12}v_1^2v_2^2\omega_5^2\omega_{21} - 36\omega_9^2\omega_{12}^2c_s^4\omega_{10}\omega_5^3 + 24\omega_{15}\omega_9\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5\omega_{21} - 12\omega_{15}\omega_9\omega_{12}^2c_s^2\omega_{10}v_1^2\omega_5\omega_{21} - 6\omega_{15}\omega_9\omega_{12}^2c_s^2\omega_5^3\omega_{21} - 6\omega_{15}\omega_9\omega_{12}^2v_1^2v_2^2\omega_5^3\omega_{21} + 12\omega_{15}\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5^2\omega_{21} - 36\omega_{15}\omega_9^2\omega_{12}^2c_s^4\omega_{10}\omega_5^2 + 36\omega_{15}\omega_9^2\omega_{12}c_s^2v_2^2\omega_5^2\omega_{21} - 12\omega_9\omega_{12}^2v_1^2v_2^2\omega_5^2\omega_{21} + 36\omega_9\omega_{12}^2c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21} - 6\omega_{15}\omega_9^2c_s^4\omega_{10}\omega_5^2\omega_{21} + 72\omega_{15}\omega_9\omega_{12}^2c_s^2v_2^2\omega_5^2\omega_{21} - 6\omega_{15}\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^3\omega_{21} + 12\omega_{15}\omega_9^2\omega_{12}^2c_s^2\omega_{10}\omega_5^2\omega_{21} - 12\omega_9\omega_{12}^2c_s^2\omega_{10}\omega_5^3\omega_{21} + 18\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21} - 36\omega_{15}\omega_9\omega_{12}^2c_s^4\omega_{10}\omega_5\omega_{21} - 12\omega_9\omega_{12}^2\omega_{10}v_2^2\omega_5^3\omega_{21} - 12\omega_{15}\omega_9^2\omega_{12}^2c_s^2\omega_{10}v_1^2\omega_5^2\omega_{21} + 36\omega_9^2\omega_{12}^2c_s^4\omega_{10}\omega_5^2 - 96\omega_{15}\omega_9^2\omega_{12}c_s^4\omega_{10}\omega_{21} - 6\omega_{15}\omega_9^2\omega_{12}^2v_1^2v_2^2\omega_5^3 - 36\omega_9\omega_{12}^2c_s^4\omega_5^3\omega_{21} + 12\omega_9\omega_{12}^2v_2^2\omega_5^3\omega_{21} - 6\omega_{15}\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21} + 24\omega_{15}\omega_9\omega_{12}^2v_1^2v_2^2\omega_5^2\omega_{21} - 6\omega_{15}\omega_9^2\omega_{12}^2c_s^2\omega_{10}\omega_5^3 + 6\omega_{15}\omega_9^2\omega_{12}^2v_2^2\omega_5^3 + 12\omega_{15}\omega_9^2\omega_{12}v_1^2v_2^2\omega_5^3\omega_{21} -$$

$$\begin{aligned}
& 12\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}\omega_5^3 - 24\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^2\omega_5^2\omega_{21} + 12\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^3\omega_5^3 - 12\omega_{15}^2\omega_9\omega_{12}\omega_{10}^2v_1^2\omega_5^2\omega_{21} + 156\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^2\omega_5\omega_{21} - \\
& 12\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}v_1^3\omega_5^3 + 18\omega_{15}^2\omega_9\omega_{12}\omega_{10}^2\omega_5^2\omega_{21} + 24\omega_{15}^2\omega_9^2\omega_{10}^2\omega_5^2\omega_{21} - 12\omega_{15}^2\omega_9\omega_{12}\omega_{10}^2\omega_5^3\omega_{21} + 12\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}^2\omega_5^2\omega_{21} - 36\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^2\omega_5\omega_{21} - \\
& 24\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^3\omega_5^3 + 12\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}^2\omega_5^3 - 12\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}\omega_5^3\omega_{21} - 18\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}^2v_1^3\omega_5^3\omega_{21} - 24\omega_{15}^2\omega_9^2\omega_{12}\omega_{10}\omega_5^3 - 96\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^2\omega_{21} + \\
& 84\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^2\omega_5^2\omega_{21} - 18\omega_{15}^2\omega_9\omega_{12}\omega_{10}^2v_1^2\omega_5^2\omega_{21} - 132\omega_{15}^2\omega_9^2\omega_{12}c_s^2\omega_{10}^2\omega_5^2\omega_{21} - 24\omega_{15}^2\omega_9^2\omega_{10}^2v_1^2\omega_5^2\omega_{21} - 6\omega_{15}^2\omega_{12}\omega_{10}^2v_1^3\omega_5^3\omega_{21}
\end{aligned}$$

$$\begin{aligned}
C_{21} = & -9w_{15}\omega w_{12}^2w_{10}^2w_5^2w_{21} - 4w_{15}^2\omega w_{12}w_{10}^2w_5^2 + 26w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 4w_{15}\omega w_{12}w_{10}^2v_2^2w_5^2w_{21} + 3w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - \\
& 3w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + w_{15}^2\omega w_{12}w_{10}^2v_2^2w_5^2w_{21} - 8w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 8w_{15}w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 4w_{15}^2\omega w_{12}c_s^2w_{10}^2w_5^2 + 4w_{15}w_{12}^2w_{10}^2w_5^2w_{21} - \\
& 2w_{15}^2\omega w_{12}w_{10}^2w_5^2w_{21} + 4w_{15}\omega w_{12}^2w_{10}^2w_5^2w_{21} + 11w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 2w_{15}^2\omega w_{12}w_{10}^2w_5^2 + 4w_{15}\omega w_{12}w_{10}^2v_2^2w_5^2 + \\
& 12w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 2w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21} - 4w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 2w_{15}\omega w_{12}c_s^2w_{10}^2w_5^2 + 4w_{15}^2\omega w_{12}^2v_2^2w_5^2w_{21} - 4w_{15}^2\omega w_{12}^2w_5^2w_{21} + \\
& 5w_{15}^2\omega w_{12}w_{10}^2w_5^2w_{21} - 4w_{15}w_{12}^2w_5^2w_{21} - 6w_{15}\omega w_{12}w_{10}^2v_2^2w_5^2w_{21} + 8w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + w_{15}^2\omega w_{12}w_{10}^2v_2^2w_5^2w_{21} - w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} \\
& 2w_{15}^2\omega w_{12}w_{10}^2v_2^2w_5^2 - 2w_{15}^2\omega w_{12}w_{10}^2v_2^2w_5^2w_{21} + 4w_{15}^2\omega w_{12}w_{10}^2v_2^2w_5^2 + 3w_{15}\omega w_{12}^2w_{10}^2w_5^2w_{21} - 4w_{15}^2w_{12}c_s^2w_{10}^2w_5^2w_{21} + 8w_{15}^2\omega w_{12}c_s^2w_{10}^2w_5^2w_{21} + \\
& w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21} - w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} - 5w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 2w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2 + 12w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + \\
& 2w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} - 2w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21} - 4w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2 - w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21} - 4w_{15}\omega w_{12}^2w_{10}^2w_5^2 + 8w_{15}^2\omega w_{12}c_s^2w_{10}^2w_5^2w_{21} - \\
& 4w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2 + 4w_{15}^2w_{12}c_s^2w_{10}^2w_5^2w_{21} - 2w_{15}^2\omega w_{12}c_s^2w_{10}^2w_5^2w_{21} - 16w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 2w_{15}^2\omega w_{12}w_{10}^2v_2^2w_5^2w_{21} - 4w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + \\
& 2w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 7w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + 4w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 2w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 4w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + \\
& 2w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2 - w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21} + 4w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2 + 9w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} - 6w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 2w_{15}\omega w_{12}^2w_{10}^2w_5^2w_{21} + \\
& 2w_{15}^2\omega w_{12}^2w_{10}^2w_5^2 + 2w_{15}^2w_{12}c_s^2w_{10}^2w_5^2w_{21} - 2w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + 13w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 15w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - \\
& 4w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2 - 6w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 5w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + 4w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} + 4w_{15}^2\omega w_{12}^2w_{10}^2w_5^2 - 4w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2 + \\
& 4w_{15}\omega w_{12}^2w_{10}^2w_5^2 + 3w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21} - 2w_{15}^2w_{12}c_s^2w_{10}^2w_5^2w_{21} + 4w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 2w_{15}^2\omega w_{12}c_s^2w_{10}^2w_5^2w_{21} + 2w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2 - \\
& 2w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2 - 8w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} + 6w_{15}\omega w_{12}^2w_{10}^2w_5^2w_{21} + 4w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2 + 2w_{15}^2\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} - 7w_{15}\omega w_{12}^2w_{10}^2w_5^2w_{21} + \\
& 4w_{15}\omega w_{12}^2w_{10}^2w_5^2 - 3w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2w_{21} - 2w_{15}^2\omega w_{12}^2c_s^2w_{10}^2w_5^2 - 8w_{15}\omega w_{12}^2c_s^2w_{10}^2w_5^2w_{21} - 4w_{15}\omega w_{12}^2w_{10}^2v_2^2w_5^2 + 2w_{15}^2\omega w_{12}^2w_{10}^2w_5^2w_{21}
\end{aligned}$$

$$C_{33} = -3\omega_{12}^2\omega_7\omega_{14}\omega_8\omega_5 - 4\omega_{12}^2\omega_7^2\omega_{14}\omega_8\omega_5^2 + \omega_{12}^2\omega_7^2\omega_{14}\omega_8\omega_5^3 + \omega_{12}^2\omega_7\omega_{14}\omega_8^3 - \omega_{12}^2\omega_7^2\omega_8^3\omega_5^3 + 2\omega_{12}\omega_7\omega_{14}\omega_8\omega_5^2 - 2\omega_{12}^2\omega_7\omega_8\omega_5^3 + 2\omega_{12}^2\omega_7\omega_{14}\omega_8\omega_5^2 + 2\omega_{12}^2\omega_7^2\omega_8^2\omega_5^2 + 3\omega_{12}^2\omega_7^2\omega_{14}\omega_8\omega_5 - \omega_{12}\omega_7\omega_{14}\omega_8\omega_5^3 - \omega_{12}^2\omega_{14}\omega_8^2\omega_5^2 - 2\omega_{12}^2\omega_7\omega_8\omega_5^2 + 2\omega_{12}^2\omega_7\omega_{14}\omega_8\omega_5^2 + \omega_{12}^2\omega_7\omega_8^2\omega_5^3 - \omega_{12}^2\omega_7^2\omega_{14}\omega_8^3 - 4\omega_{12}^2\omega_7^2\omega_{14}\omega_8^2 + 5\omega_{12}^2\omega_7^2\omega_{14}\omega_8\omega_5 + \omega_{12}^2\omega_7^2\omega_{14}\omega_5^2 + 2\omega_{12}^2\omega_7^2\omega_8\omega_5^3 - 2\omega_{12}^2\omega_7\omega_{14}\omega_8\omega_5^3 + \omega_{12}^2\omega_{14}\omega_8\omega_5^3 + 2\omega_{12}\omega_7^2\omega_{14}\omega_8^2\omega_5 - 4\omega_{12}\omega_7^2\omega_{14}\omega_8\omega_5^2 - \omega_7^2\omega_{14}\omega_8^2\omega_5^3 + \omega_{12}\omega_7^2\omega_8^2\omega_5^3 + \omega_{12}\omega_7^2\omega_{14}\omega_8\omega_5^3 - \omega_{12}^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2 + 2\omega_7^2\omega_{14}\omega_8^2\omega_5^2 - 2\omega_{12}\omega_7^2\omega_8^2\omega_5^2$$

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$$C_{41} = 12\omega_{16}\omega_{10}^3 + 25c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 - 48\omega_{16}\omega_{10}^2\omega_7^2 - 16c_s^2\omega_{10}^3\omega_7^2 + 8\omega_{10}^4\omega_7^2 + 16\omega_{10}^3\omega_7^2\omega_7^2 - 20c_s^2\omega_{16}\omega_{10}^3 + 24\omega_{16}\omega_{10}\omega_7^2 - 120\omega_{16}^2\omega_{10}\omega_7^2\omega_7^2 - 16c_s^2\omega_{10}^3\omega_7^2 + 28\omega_{16}^2\omega_{10}^2\omega_7^2 - 32c_s^2\omega_{16}\omega_{10}\omega_7^2 - 17\omega_{16}^2\omega_{10}^2\omega_7^2 + 8\omega_{10}^4\omega_7^2 + 28\omega_{16}^2\omega_{10}\omega_7^2 - 8\omega_{10}^3\omega_7^2 + 16c_s^2\omega_{10}^2\omega_7^2 + 64\omega_{16}^2\omega_{10}\omega_7^2\omega_7^2 - 16\omega_{10}^3\omega_7^2\omega_7^2 + 80\omega_{16}^2\omega_{10}^2\omega_7^2 + 104\omega_{16}\omega_{10}^2\omega_7^2 - 44c_s^2\omega_{16}^2\omega_{10}\omega_7^2 + 16\omega_{16}\omega_{10}^2\omega_7^2 + 32c_s^2\omega_{16}\omega_{10}\omega_7^2 - 25c_s^2\omega_{16}^2\omega_{10}\omega_7^2 - 68\omega_{16}^2\omega_{10}^2\omega_7^2 - 24\omega_{16}^2\omega_{10}\omega_7^2 + 17\omega_{16}\omega_{10}^3\omega_7^2 - 16\omega_{10}^4\omega_7^2\omega_7^2 + 68\omega_{16}\omega_{10}\omega_7^2\omega_7^2 - 28\omega_{16}\omega_{10}^2\omega_7^2 - 64\omega_{16}\omega_{10}\omega_7^2\omega_7^2 - 16c_s^2\omega_{16}\omega_{10}^2\omega_7^2 - 43\omega_{16}\omega_{10}^2\omega_7^2\omega_7^2 + 56c_s^2\omega_{16}\omega_{10}\omega_7^2 - 12\omega_{16}^2\omega_{10} - 28\omega_{16}\omega_{10}^3\omega_7 + 48\omega_{16}^2\omega_{10}\omega_7^2 + 20c_s^2\omega_{16}^2\omega_{10}^2 + 44c_s^2\omega_{16}\omega_{10}^3\omega_7 - 72c_s^2\omega_{16}^2\omega_{10}\omega_7^2 + 43\omega_{16}^2\omega_{10}^2\omega_7^2 + 48c_s^2\omega_{16}^2\omega_7^2 - 32\omega_{16}^2\omega_7^2 - 40\omega_{16}\omega_{10}^2\omega_7^2$$

$$\begin{aligned} C_{43} = & -12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5 + 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{14}w_8w_5 - 6w_{12}w_{16}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5 + \\ & + 3w_{12}w_{16}^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 48w_{12}w_{16}w_{19}c_s^2v_2w_7w_{20}w_{14}w_8w_5 - 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_8w_5 + \\ & + 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5^2 + 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 - 3w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_{14}w_8w_5^2 - 3w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_8w_5 - 6w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_{14}w_8w_5 + 6w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{14}w_8w_5^2 + 6w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & + 12w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_8w_5 + 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + 6w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_8w_5^2 - \\ & - 12w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & - 6w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & - 12w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5^2 - 3w_{12}w_{16}c_s^2v_1v_2w_7w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_2w_7w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{14}w_8w_5 - \\ & - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_8w_5^2 - 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{14}w_8w_5^2 + 3w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_{14}w_8w_5 - \\ & - 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5^2 - 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 6w_{12}w_{16}^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + \\ & + 12w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5^2 + \\ & - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_8w_5 - 6w_{12}w_{16}c_s^2v_1v_2w_7v_3w_{14}w_8w_5^2 + 48w_{12}w_{16}w_{19}c_s^2v_2w_7w_{20}w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 + \\ & + 12w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_{14}w_8w_5 + 6w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + \\ & + 3w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{14}w_8w_5^2 - 24w_{12}w_{16}w_{19}c_s^2v_2w_7w_{20}w_{14}w_8w_5^2 + 6w_{12}w_{16}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + \\ & + 12w_{12}w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_{14}w_8w_5 + 2w_{12}w_{16}w_{19}c_s^2v_2w_7w_{20}w_{14}w_8w_5^2 + 6w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5^2 - 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 - \\ & - 3w_{12}w_{16}^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 3w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_8w_5^2 - 6w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{14}w_8w_5^2 + \\ & + 3w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_8w_5^2 + 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{14}w_8w_5^2 + \\ & + 24w_{12}w_{16}w_{19}c_s^2v_2w_7w_{20}w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + \\ & + 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{14}w_8w_5^2 - 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & - 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_8w_5^2 - 28w_{12}w_{16}w_{19}c_s^2v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 6w_{16}w_{19}c_s^2v_1w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & + 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{20}w_8w_5^2 - 12w_{12}w_{16}w_{19}c_s^2v_1v_2w_7v_3w_{14}w_8w_5^2 - 3w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 + 3w_{12}w_{16}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 + \\ & - 24w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{14}w_8w_5^2 - 48w_{12}w_{16}w_{19}c_s^2v_2w_7w_{20}w_{14}w_8w_5^2 - 6w_{12}w_{16}w_{19}c_s^2v_1v_2w_7w_{20}w_{14}w_8w_5^2 + 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w_{14}w_8w_5^2 - \\ & - 12w_{12}w_{16}w_{19}v_1v_2w_7v_3w_{20}w$$

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$$C_{49} = 4w_{15}w_{6w_{19}w_{16}w_{10}v_1w_7^3v_3^2w_{23}w_{20}w_8w_5} + 2w_{15}w_{6w_{19}w_{16}w_{10}v_1w_7^3v_3^2w_{23}w_{20}w_{17}w_8^2w_5} - 4w_{15}w_{6w_{19}w_{16}w_{10}v_1w_7^3v_3^2w_{23}w_{20}w_8^2w_5^2} + 2w_{6w_{19}c_s^2w_{16}w_{10}w_7^3v_3^2w_{23}w_{20}w_{17}w_8^2w_5^2} - 4w_{15}w_{6w_{19}w_{16}w_{10}v_1w_7^3v_3^2w_{23}w_{20}w_{17}w_8^2w_5^2} + 9w_{15}w_{6w_{19}c_s^2w_{16}w_{10}v_1w_7^3v_3^2w_{23}w_{20}w_{17}w_8^2w_5^2} + 2w_{15}w_{19}c_s^2w_{16}w_{10}v_1w_7^3w_{23}w_{20}w_{17}w_8w_5} - 4w_{15}w_{6w_{19}c_s^2w_{16}w_{10}v_1w_7^3v_3^2w_{23}w_{17}w_8w_5} + 4w_{15}w_{6w_{19}c_s^2w_{16}w_{10}v_1w_7^2w_{23}w_{20}w_{17}w_8^2w_5} - 4w_{15}w_{6w_{19}c_s^2w_{16}w_{10}w_7^2v_3w_{23}w_{20}w_8^2w_5^2} + 4w_{15}w_{6w_{19}w_{16}w_{10}v_1w_7^2v_3w_{23}w_{20}w_{17}w_8w_5^2} - 4w_{15}w_{6w_{19}c_s^2w_{16}w_{10}v_1w_7^2w_{20}w_{17}w_8^2w_5^2} +$$

$$C_{50} = -\omega_{15}\omega_{19}^2\omega_{16}\omega_{10}v_1^2v_2^2\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_8^2\omega_5 - 2\omega_{15}\omega_{19}^2c_s^2v_1^2\omega_7^3\omega_{23}\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{15}\omega_{19}c_s^2\omega_{16}\omega_{10}v_2^2\omega_7^2\omega_{23}\omega_{17}\omega_8^2\omega_5^2 -$$

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$$\begin{aligned}
& 2w_{15}w_{19}w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_{17}w_8w_5 + 2w_{15}w_{19}^2w_{16}v_1^2w_7^2w_{23}w_{20}w_8^2w_5^2 + 2w_{15}w_{19}w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_8^2w_5 - \\
& 2w_{15}w_{19}^2v_1^2w_7^2w_{23}w_{20}w_8^2w_5^2 + 2w_{15}w_{19}^2w_{16}w_{10}v_1w_7^2v_3w_{20}w_{17}w_8^2w_5^2 + 2w_{19}w_{16}w_{10}v_1v_2^2w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 - \\
& 2w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 - w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 + 4w_{15}w_{19}^2w_{16}^2w_{10}v_1w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 + \\
& 4w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2v_3w_{20}w_{17}w_8^2w_5^2 + 4w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2 + 2w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{17}w_8^2w_5^2 + \\
& 2w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_8^2w_5^2 + 4w_{15}w_{19}^2v_1^2w_7^2v_3w_{23}w_{20}w_8^2w_5^2 - 4w_{15}w_{19}^2w_{16}w_{10}v_1v_2^2w_7^2v_3w_{23}w_{20}w_8^2w_5^2 + \\
& 2w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_8w_5 + 4w_{15}w_{19}^2w_{16}w_{10}v_1w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2 + w_{15}w_{19}^2w_{16}w_{10}v_1w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2 + \\
& w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 + 4w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 + 4w_{15}w_{19}^2w_{16}w_{10}v_1w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2 + \\
& 4w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_8^2w_5^2 + 2w_{15}w_{19}^2w_{16}w_{10}v_1^2w_7^2w_{23}w_{20}w_{17}w_8^2w_5^2 - w_{15}w_{19}^2w_{16}^2w_{10}v_1w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2 - \\
& 4w_{15}w_{19}^2w_{16}w_{10}v_1w_7^2v_3w_{23}w_{20}w_8^2w_5^2 - 4w_{15}w_{19}^2w_{16}w_{10}v_1v_2^2w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2 + 2w_{15}w_{19}^2w_{16}w_{10}v_1w_7^2v_3w_{23}w_{20}w_{17}w_8^2w_5^2
\end{aligned}$$

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$$\begin{aligned}
C_{53} = & 4w_{19}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}w_{16}^2w_{16}^{10}v_2^2w_7^2w_{11} + w_{19}w_{16}^2w_{10}^3v_2^2w_7^2w_{23}w_{11} - w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{11} - \\
& 4w_{19}w_{16}w_{10}v_2^2w_7^2w_{11} - 2w_{19}^2w_{16}^2w_{10}^2w_7^2w_{11} + w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 9w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} + 2w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23} - 8w_{19}c_s^2w_{16}w_{10}w_7^2w_{23}w_{11} + \\
& w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} + 8w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{11} - 4w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{11} - 9w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - \\
& 15w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 5w_{19}^2w_{16}^2w_{10}v_2^2w_7^2w_{23}w_{11} - 2w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23} + 2w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{11} + 2w_{19}c_s^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} - \\
& 8w_{19}^2c_s^2w_{10}^2w_7^2w_{23}w_{11} + 2w_{19}w_{16}^2w_{10}^2w_7^2w_{11} + 2w_{19}^2w_{16}^2w_{10}^3v_2^2w_7^2w_{11} + 4c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 16w_{19}^2c_s^2w_{16}^2w_{10}^2w_{23}w_{11} - 4w_{19}^2w_{16}w_{10}v_2^2w_7^2w_{23}w_{11} + \\
& 2w_{19}w_{16}w_{10}w_7^2w_{23}w_{11} - 2w_{19}^2w_{16}^2w_{10}v_2^2w_7^2w_{11} + 4w_{19}^2w_{10}^3v_2^2w_7^2w_{23}w_{11} - 2w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{11} + 5w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{11} + \\
& 8w_{19}^2c_s^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}^2w_{16}^2w_{10}^2w_{11} + 11w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 2w_{19}w_{16}^2w_{10}^2v_2^2w_7^2w_{11} + 4w_{19}^2w_{16}w_{10}w_7^2w_{23}w_{11} + \\
& 12w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}^2w_{16}^2w_{10}v_2^2w_7^2w_{11} + 2w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} - 4w_{19}^2w_{16}^2w_{10}^2w_7^2w_{11} - 4w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{11} - \\
& 8w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 4w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{11} - 4w_{19}^2w_{10}^3w_7^2w_{23}w_{11} - w_{19}^2w_{16}^2w_{10}^3v_2^2w_7^2w_{23}w_{11} + 2w_{19}w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23} - \\
& 4w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 7w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} + 3w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 2w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{11} - 4w_{19}^2w_{10}^3v_2^2w_7^2w_{23}w_{11} + \\
& 13w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 2w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 3w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 4w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{11} - 4w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - \\
& 6w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 2w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} + 4w_{19}^2w_{16}^2v_2^2w_7^2w_{23}w_{11} - 3w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} + 26w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - \\
& 24w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + 12w_{19}^2c_s^2w_{16}^2w_7^2w_{23}w_{11} - 4w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{11} - 3w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} - 2w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} + \\
& 2w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} + 2w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{11} + 3w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 2w_{19}w_{16}^2w_{10}^3v_2^2w_7^2w_{23}w_{11} + 8w_{19}c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - \\
& w_{19}^2w_{16}^2w_{10}^3w_7^2w_{23}w_{11} - 6w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 2w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} - w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 4w_{19}^2w_{16}^2w_{10}^2w_7^2w_{11} + 4w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - \\
& 2w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 6w_{19}^2w_{16}^2w_{10}^2v_2^2w_7^2w_{23}w_{11} - 8w_{19}^2c_s^2w_{10}^2w_7^2w_{23}w_{11} - 5w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 2w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - \\
& 4w_{19}^2w_{10}^3v_2^2w_7^2w_{23}w_{11} + 6w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 4w_{19}^2c_s^2w_{16}^2w_{10}^3w_7^2w_{23} + 4w_{19}^2c_s^2w_{16}^2w_{10}^2w_7^2w_{11} - 2c_s^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 7w_{19}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11}
\end{aligned}$$

[illegible]

$$\begin{aligned}
& 36\omega_{19}^4c_s^4\omega_{16}\omega_{10}\omega_2^3\omega_{11}^2 - 72\omega_{19}^2c_s^5\omega_{16}\omega_2^3\omega_7^2\omega_{23}\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_{10}\omega_2^3\omega_7^2\omega_{11}^2 + 12\omega_{19}^2c_s^3\omega_7^3\omega_{23}\omega_{11} - 18\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_2^3\omega_7^2\omega_{23} - \\
& 12\omega_{19}^2c_s^5\omega_{16}\omega_{10}\omega_7\omega_3^2\omega_{23}\omega_{11} + 144\omega_{19}^2c_s^5\omega_{16}\omega_{10}\omega_2^3\omega_7^2\omega_{23}\omega_{11}^2 + 6\omega_{19}^2\omega_{16}\omega_{10}\omega_2^3\omega_7^3\omega_{11}^2 - 36\omega_{19}^4c_s^4\omega_{10}\omega_2^3\omega_{11}^2 + 12c_s^5\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11}^2 + \\
& 15\omega_{19}\omega_{16}\omega_{10}\omega_2^3\omega_7^2\omega_{23}\omega_{11}^2 - 12\omega_{19}^2c_s^5\omega_7^3\omega_3^2\omega_{23}\omega_{11} + 36\omega_{19}^2\omega_{16}\omega_{10}\omega_2^3\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}^4c_s^4\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11}^2 - 12\omega_{19}^2\omega_2^3\omega_7^3\omega_3^2\omega_{23}\omega_{11} - \\
& 6\omega_{19}^2\omega_{16}\omega_{10}\omega_2^3\omega_7^3\omega_3^2\omega_{23} - 60\omega_{19}^2c_s^4\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11}^2 + 12\omega_{19}^2c_s^5\omega_{16}\omega_{10}\omega_7^2\omega_{11}^2 + 18\omega_{19}^2c_s^5\omega_{16}\omega_{10}\omega_2^3\omega_7^2\omega_{11}^2
\end{aligned}$$

[illegible]

$$C_{62} = 48\omega_{19}\omega_7v_3^2 + 156\omega_{19}^2c_s^2\omega_7v_3^2 + 24\omega_{19}^2\omega_7v_3^4 + 6\omega_{19}c_s^4\omega_7^3 + 12\omega_7^3v_3^4 + 24\omega_{19}^2\omega_7^2v_3^2 + 24\omega_{19}^2c_s^4\omega_7^4 - 12\omega_{19}c_s^2\omega_7^3v_3^2 + 12\omega_{19}^2c_s^2\omega_7 - 24\omega_{19}c_s^4\omega_7^2 + 72\omega_{19}^2v_3^2v_3^4 + 24\omega_{19}c_s^6\omega_7 - 24\omega_7^2v_3^4 - 8\omega_{19}^2c_s^2\omega_7^2 - 18\omega_{19}\omega_7^3v_3^4 + 48\omega_{19}c_s^2\omega_7^2v_3^2 + \omega_{19}^2c_s^2\omega_7^3 - 3\omega_{19}^2\omega_7^3v_3^2 - 48\omega_{19}^2c_s^4\omega_7 - 24c_s^2\omega_7^2v_3^2 +$$

$$24\omega_{19}c_s^2\omega_7^2 + 24\omega_7^2v_3^2 - 24\omega_{19}c_s^2\omega_7v_3^2 - 96\omega_{19}^2c_s^2v_3^2 + 3\omega_{19}^2\omega_7^3v_3^4 + 18\omega_{19}\omega_7^3v_3^2 + 6\omega_{19}^2c_s^2\omega_7^3v_3^2 - 6\omega_{19}c_s^2\omega_7^3 - 24\omega_{19}^2\omega_7v_3^2 - 12\omega_7^3v_3^2 - 3\omega_{19}^2c_s^4\omega_7^3 + 12c_s^2\omega_7^3v_3^2 - 48\omega_{19}\omega_7v_3^4 - 24\omega_{19}c_s^2\omega_7 - 72\omega_{19}^2c_s^2\omega_7^2v_3^2 - 72\omega_{19}\omega_7^2v_3^2 - 24\omega_{19}^2\omega_7^2v_3^4 + 24\omega_{19}^2c_s^4\omega_7^2$$

$$C_{63} = -48c_s^2\omega_7\omega_{11}^2 + 61\omega_{19}^2\omega_7^2v_3^2\omega_{11} - 60\omega_{19}c_s^2\omega_{11}^2 + 24\omega_{19}\omega_7\omega_{11} - 120\omega_{19}^2c_s^2\omega_7\omega_{11} + 24\omega_7\omega_{11}^2 - 33\omega_{19}c_s^2\omega_7^2\omega_{11}^2 + 24\omega_7^2v_3^2\omega_{11}^2 - 60\omega_{19}^2\omega_7^2v_3^2 + 168\omega_{19}\omega_7v_3^2\omega_{11}^2 + 72\omega_{19}^2c_s^2\omega_7 - 25\omega_{19}^2\omega_7^2\omega_{11} + 2\omega_{19}^2\omega_7^2\omega_{11}^2 - 36\omega_{19}^2\omega_{11} - 36\omega_{19}^2c_s^2\omega_7^2 - 72\omega_{19}\omega_7v_3^2\omega_{11} - 84\omega_{19}v_3^2\omega_{11}^2 - 72\omega_{19}\omega_7\omega_{11}^2 + 12\omega_{19}c_s^2\omega_7^2\omega_{11} - 5\omega_{19}^2\omega_7^2v_3^2\omega_{11}^2 + 21\omega_{19}\omega_7^2\omega_{11} - 3\omega_{19}^2c_s^2\omega_7^2\omega_{11}^2 - 24\omega_{19}c_s^2\omega_7\omega_{11} + 36\omega_{19}\omega_7^2v_3^2\omega_{11} + 60\omega_{19}^2c_s^2\omega_{11} + 24\omega_{19}^2\omega_7^2 + 36\omega_{19}\omega_{11}^2 - 168\omega_{19}\omega_7v_3^2\omega_{11} + 120\omega_{19}^2\omega_7v_3^2 - 48\omega_{19}^2\omega_7 - 48\omega_7v_3^2\omega_{11}^2 + 72\omega_{19}^2\omega_7\omega_{11} + 84\omega_{19}^2v_3^2\omega_{11} - 51\omega_{19}\omega_7^2v_3^2\omega_{11}^2 + 24c_s^2\omega_7^2\omega_{11}^2 + 39\omega_{19}^2c_s^2\omega_7^2\omega_{11} - 12\omega_{19}\omega_7^2\omega_{11} + 120\omega_{19}c_s^2\omega_7\omega_{11}^2 - 12\omega_7^2\omega_{11}^2$$

2.2.5 Conservation of momentum: ρv_3



attached text file: output_d3q27_nse_mrt1_symbolic_pde_03.txt

$$\begin{aligned} & v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{\delta_l v_1 v_3}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\delta_l \rho v_3}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\delta_l \rho v_1}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{\delta_l v_2 v_3}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\delta_l \rho v_3}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\delta_l \rho v_2}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\ & \frac{2\delta_l \rho v_3}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\ & + (-2 - 2c_s^2\omega_{11} + 4c_s^2 - 3v_3^2\omega_{11} + \omega_{11} + 6v_3^2) \frac{\delta_l^2}{\delta_t \omega_{11}} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3\delta_l^2 \rho v_3}{\delta_t \omega_{11}} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{\delta_l^2 c_s^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\ & (-2 + \omega_7) \frac{\delta_l^2 c_s^2 \rho}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{\delta_l^2 c_s^2 \rho}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\ & (-2 - 3c_s^2\omega_{11} + 6c_s^2 - v_3^2\omega_{11} + \omega_{11} + 2v_3^2) \frac{\delta_l^2 v_3}{2\delta_t \omega_{11}} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 - c_s^2\omega_{11} + 2c_s^2 - 3v_3^2\omega_{11} + \omega_{11} + 6v_3^2) \frac{\delta_l^2 \rho}{2\delta_t \omega_{11}} \frac{\partial^2 v_3}{\partial x_3^2} + \\ & C_1 \frac{\delta_l^3 v_1 v_3}{12\omega_6 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\delta_l^3 \rho v_3}{12\omega_9 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{\delta_l^3 \rho v_1}{6\omega_6^2 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^3} + \\ & (-\omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_7 \omega_8 - 6\omega_6 \omega_7 \omega_5 + 6\omega_6 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\ & (-\omega_6^2 \omega_7 - \omega_7 \omega_8 + \omega_6 \omega_7 + \omega_6^2 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8) \frac{\delta_l^3 c_s^2 \rho v_2}{\omega_6^2 \delta_t \omega_7 \omega_8} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} + \\ & (-\omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 + 6\omega_7 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_7 \omega_8 - 6\omega_6 \omega_7 \omega_5 + 6\omega_6 \omega_5) \frac{\delta_l^3 c_s^2 \rho v_3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & (\omega_7^2 - \omega_7 \omega_8 + \omega_6 \omega_7 - \omega_6 \omega_7^2 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8) \frac{\delta_l^3 c_s^2 \rho v_1}{\omega_6 \delta_t \omega_7^2 \omega_8} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + C_4 \frac{\delta_l^3 v_2 v_3}{12\delta_t \omega_{16} \omega_{10} \omega_7} \frac{\partial^3 \rho}{\partial x_2^3} + C_5 \frac{\delta_l^3 \rho v_3}{12\delta_t \omega_{16} \omega_{10} \omega_7} \frac{\partial^3 v_2}{\partial x_2^3} + \\ & C_6 \frac{\delta_l^3 \rho v_2}{6\delta_t \omega_{16} \omega_7^2} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega_6 - \omega_6^2) \frac{\delta_l^3 c_s^4}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + (2\omega_6 - 2\omega_{13} + \omega_6 \omega_{13} - \omega_6^2) \frac{\delta_l^3 c_s^2 \rho v_1}{\omega_6^2 \delta_t \omega_{13}} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\ & (12\omega_6 \omega_{11} - \omega_6^2 \omega_{11} \omega_{18} + 12\omega_6 \omega_{11} \omega_{18} + 12\omega_6^2 - 12\omega_6 \omega_{18} - 12\omega_6^2 \omega_{11} - 12\omega_{11} \omega_{18}) \frac{\delta_l^3 c_s^2 \rho v_3}{6\omega_6^2 \delta_t \omega_{11} \omega_{18}} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\ & (-\omega_6^2 \omega_7 - \omega_7 \omega_8 + \omega_6 \omega_7 + \omega_6^2 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8) \frac{\delta_l^3 c_s^2 \rho v_2}{\omega_6^2 \delta_t \omega_7 \omega_8} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\ & (\omega_7^2 - \omega_7 \omega_8 + \omega_6 \omega_7 - \omega_6 \omega_7^2 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8) \frac{\delta_l^3 c_s^2 \rho v_1}{\omega_6 \delta_t \omega_7^2 \omega_8} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + (-12 - \omega_7^2 + 12\omega_7) \frac{\delta_l^3 c_s^4}{6\delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\ & (-\omega_7^2 - 2\omega_{16} + \omega_{16} \omega_7 + 2\omega_7) \frac{\delta_l^3 c_s^2 \rho v_2}{\delta_t \omega_{16} \omega_7^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\ & (12\omega_{19} \omega_7 \omega_{11} + 12\omega_7^2 - 12\omega_{19} \omega_7 + 12\omega_7 \omega_{11} - 12\omega_7^2 \omega_{11} - 12\omega_{19} \omega_{11} - \omega_{19} \omega_7^2 \omega_{11}) \frac{\delta_l^3 c_s^2 \rho v_3}{6\omega_{19} \delta_t \omega_7^2 \omega_{11}} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\ & C_7 \frac{\delta_l^3 v_1 v_3}{\omega_6 \delta_t \omega_{11}^2 \omega_{18}} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + C_8 \frac{\delta_l^3 \rho v_3}{12\omega_6^2 \delta_t \omega_{11}^2 \omega_{18}} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_9 \frac{\delta_l^3 \rho v_1}{\omega_6 \delta_t \omega_{11}^2 \omega_{18}} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{\delta_l^3 v_2 v_3}{\omega_{19} \delta_t \omega_7 \omega_{11}^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\ & C_{11} \frac{\delta_l^3 \rho v_3}{12\omega_{19} \delta_t \omega_7^2 \omega_{11}^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{12} \frac{\delta_l^3 \rho v_2}{\omega_{19} \delta_t \omega_7 \omega_{11}^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{13} \frac{\delta_l^3}{12\delta_t \omega_{11}^2} \frac{\partial^3 \rho}{\partial x_3^3} + \\ & (-24 - 36c_s^2\omega_{11} + 11v_3^2\omega_{11}^2 + 36c_s^2 - 60v_3^2\omega_{11} + 5c_s^2\omega_{11}^2 - 4\omega_{11}^2 + 24\omega_{11} + 60v_3^2) \frac{\delta_l^3 \rho v_3}{6\delta_t \omega_{11}^2} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{\delta_l^4 v_3}{24\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & C_{15} \frac{\delta_l^4 \rho v_1 v_3}{12\omega_9^2 \omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{\delta_l^4 \rho}{24\omega_9^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^4} + C_{17} \frac{\delta_l^4 v_1 v_2 v_3}{4\omega_9^2 \omega_{12} \omega_6^2 \delta_t \omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\ & C_{18} \frac{\delta_l^4 \rho v_2 v_3}{4\omega_9^2 \omega_{12} \omega_6^2 \delta_t \omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{\delta_l^4 \rho v_1 v_3}{12\omega_9^2 \omega_{12} \omega_6^2 \delta_t \omega_{13}^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{20} \frac{\delta_l^4 \rho v_1 v_2}{2\omega_9^2 \delta_t \omega_{13}^2 \omega_7^2 \omega_{14} \omega_8^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_2} + \\ & C_{21} \frac{\delta_l^4 c_s^4 v_3}{6\omega_6^2 \delta_t \omega_7^2 \omega_8^2 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{\delta_l^4 c_s^2 \rho v_1 v_3}{2\omega_9 \omega_{12} \omega_6^2 \delta_t \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{\delta_l^4 c_s^2 \rho v_2 v_3}{2\omega_{15} \omega_6^2 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\ & C_{24} \frac{\delta_l^4 c_s^2 \rho}{2\omega_6^2 \delta_t \omega_{16} \omega_{13} \omega_3^2 \omega_{17} \omega_{14} \omega_8^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + C_{25} \frac{\delta_l^4 v_1 v_2 v_3}{4\omega_{15} \omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + C_{26} \frac{\delta_l^4 \rho v_2 v_3}{12\omega_{15} \omega_6^2 \delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} + \\ & C_{27} \frac{\delta_l^4 \rho v_1 v_3}{4\omega_{15} \omega_6 \delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^2} + C_{28} \frac{\delta_l^4 \rho v_1 v_2}{2\omega_6^2 \delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^2} + C_{29} \frac{\delta_l^4 v_3}{24\delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2} \frac{\partial^4 \rho}{\partial x_2^4} + C_{30} \frac{\delta_l^4 \rho v_2 v_3}{12\delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2} \frac{\partial^4 v_2}{\partial x_2^4} + \\ & C_{31} \frac{\delta_l^4 \rho}{24\delta_t \omega_{16}^2 \omega_7^2} \frac{\partial^4 v_3}{\partial x_2^4} + C_{32} \frac{\delta_l^4 v_1}{12\omega_9^2 \omega_6^2 \omega_{22} \delta_t \omega_{13}^2 \omega_{11} \omega_{18}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{33} \frac{\delta_l^4 \rho}{12\omega_9^2 \omega_6^2 \omega_{22} \delta_t \omega_{13}^2 \omega_{11} \omega_{18}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \end{aligned}$$

$$\begin{aligned}
& C_{34} \frac{\delta_l^4 \rho v_1 v_3}{12\omega_9^2 \omega_6^2 \omega_{22} \delta_t \omega_{13}^2 \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{35} \frac{\delta_l^4}{2\omega_6^3 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{36} \frac{\delta_l^4 \rho}{2\omega_6^3 \omega_{22} \omega_{19} \delta_t \omega_{13}^2 \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{37} \frac{\delta_l^4 \rho}{12\omega_6^3 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{\delta_l^4 \rho v_3}{2\omega_6^3 \omega_{22} \omega_{19} \delta_t \omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\delta_l^4}{2\omega_6^3 \omega_{19} \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{40} \frac{\delta_l^4 \rho}{12\omega_6^3 \omega_{19} \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{\delta_l^4 \rho v_2}{\omega_6^2 \omega_{19} \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{42} \frac{\delta_l^4 \rho}{2\omega_6^2 \omega_{19} \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8^2 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{\delta_l^4 v_2}{12\omega_{19} \delta_t \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + \\
& C_{44} \frac{\delta_l^4 \rho}{12\omega_{19} \delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{45} \frac{\delta_l^4 \rho v_2 v_3}{12\omega_{19}^2 \delta_t \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{46} \frac{\delta_l^4 v_3}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& C_{47} \frac{\delta_l^4 \rho v_1 v_3}{2\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{48} \frac{\delta_l^4 \rho}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{49} \frac{\omega_6^2 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}}{\delta_l^4 v_1 v_2 v_3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{\delta_l^4 \rho v_2 v_3}{2\omega_6^3 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{51} \frac{\delta_l^4 \rho v_1 v_3}{2\omega_6^2 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{52} \frac{\delta_l^4 \rho}{\omega_6^2 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{53} \frac{\delta_l^4 v_3}{12\omega_{19}^2 \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{54} \frac{\delta_l^4 \rho v_2 v_3}{2\omega_{19}^2 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{55} \frac{\delta_l^4 \rho}{12\omega_{19}^2 \delta_t \omega_{16} \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{56} \frac{\delta_l^4 v_1}{4\omega_6^2 \delta_t \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{57} \frac{\delta_l^4 \rho}{12\omega_6^3 \delta_t \omega_{11}^3 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{58} \frac{\delta_l^4 \rho v_1 v_3}{4\omega_6^2 \delta_t \omega_{11}^3 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{59} \frac{\delta_l^4 v_2}{4\omega_{19}^2 \delta_t \omega_7^2 \omega_{11}^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{60} \frac{\delta_l^4 \rho}{12\omega_{19}^2 \delta_t \omega_7^2 \omega_{11}^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{61} \frac{\delta_l^4 \rho v_2 v_3}{4\omega_{19}^2 \delta_t \omega_7^2 \omega_{11}^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{62} \frac{\delta_l^4 v_3}{12\delta_t \omega_{11}^3} \frac{\partial^4 \rho}{\partial x_3^3} + C_{63} \frac{\delta_l^4 \rho}{12\delta_t \omega_{11}^3} \frac{\partial^4 v_3}{\partial x_3^3} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -6\omega_6 v_1^2 \omega_{13} + 12\omega_9 - 12\omega_9 v_1^2 + 6\omega_9 \omega_6 v_1^2 - 36\omega_9 c_s^2 + 12v_1^2 \omega_{13} + 18\omega_9 \omega_6 c_s^2 - 12\omega_{13} - \omega_9 \omega_6 \omega_{13} + 3\omega_9 \omega_6 c_s^2 \omega_{13} + 36c_s^2 \omega_{13} + 6\omega_6 \omega_{13} + \\
& \omega_9 \omega_6 v_1^2 \omega_{13} - 18\omega_6 c_s^2 \omega_{13} - 6\omega_9 \omega_6 \\
C_2 &= -18\omega_6 v_1^2 \omega_{13} + 12\omega_9 - 36\omega_9 v_1^2 + 18\omega_9 \omega_6 v_1^2 - 12\omega_9 c_s^2 + 36v_1^2 \omega_{13} + 6\omega_9 \omega_6 c_s^2 - 12\omega_{13} - \omega_9 \omega_6 \omega_{13} + \omega_9 \omega_6 c_s^2 \omega_{13} + 12c_s^2 \omega_{13} + 6\omega_6 \omega_{13} + \\
& 3\omega_9 \omega_6 v_1^2 \omega_{13} - 6\omega_6 c_s^2 \omega_{13} - 6\omega_9 \omega_6 \\
C_3 &= -3\omega_6^2 c_s^2 \omega_{13} + 3\omega_6^2 v_1^2 + 3\omega_6 v_1^2 \omega_{13} + 6\omega_6 + \omega_6^2 \omega_{13} + 3\omega_6^2 c_s^2 - 6\omega_6 c_s^2 - 12c_s^2 \omega_{13} - 3\omega_6 \omega_{13} - 3\omega_6^2 + 15\omega_6 c_s^2 \omega_{13} - \omega_6^2 v_1^2 \omega_{13} - 6\omega_6 v_1^2 \\
C_4 &= 12\omega_{16} v_2^2 + 6\omega_{10} v_2^2 \omega_7 + 3c_s^2 \omega_{16} \omega_{10} \omega_7 - 12\omega_{16} + 6\omega_{16} \omega_7 + 12\omega_{10} - \omega_{16} \omega_{10} \omega_7 - 18c_s^2 \omega_{16} \omega_7 - 6\omega_{10} \omega_7 + 18c_s^2 \omega_{10} \omega_7 - 36c_s^2 \omega_{10} + \\
& \omega_{16} \omega_{10} v_2^2 \omega_7 - 6\omega_{16} v_2^2 \omega_7 + 36c_s^2 \omega_{16} - 12\omega_{10} v_2^2 \\
C_5 &= 36\omega_{16} v_2^2 + 18\omega_{10} v_2^2 \omega_7 + c_s^2 \omega_{16} \omega_{10} \omega_7 - 12\omega_{16} + 6\omega_{16} \omega_7 + 12\omega_{10} - \omega_{16} \omega_{10} \omega_7 - 6c_s^2 \omega_{16} \omega_7 - 6\omega_{10} \omega_7 + 6c_s^2 \omega_{10} \omega_7 - 12c_s^2 \omega_{10} + \\
& 3\omega_{16} \omega_{10} v_2^2 \omega_7 - 18\omega_{16} v_2^2 \omega_7 + 12c_s^2 \omega_{16} - 36\omega_{10} v_2^2 \\
C_6 &= -3c_s^2 \omega_{16} \omega_7^2 + \omega_{16} \omega_7^2 - 3\omega_7^2 - 6v_2^2 \omega_7 + 3v_2^2 \omega_7^2 - 3\omega_{16} \omega_7 + 15c_s^2 \omega_{16} \omega_7 + 6\omega_7 - 6c_s^2 \omega_7 - \omega_{16} v_2^2 \omega_7^2 + 3\omega_{16} v_2^2 \omega_7 - 12c_s^2 \omega_{16} + 3c_s^2 \omega_7^2 \\
C_7 &= v_3^2 \omega_{11} \omega_{18} - v_3^2 \omega_{11}^2 - \omega_6 v_3^2 \omega_{11} + \omega_6 \omega_{11} + 3\omega_6 c_s^2 \omega_{11}^2 - 3\omega_6 c_s^2 \omega_{11} - 3\omega_6 c_s^2 \omega_{11} \omega_{18} + \omega_6 v_3^2 \omega_{11}^2 - \omega_6 \omega_{11}^2 - 3c_s^2 \omega_{11}^2 - \omega_6 v_3^2 \omega_{11} \omega_{18} + \\
& \omega_6 \omega_{11} \omega_{18} + \omega_{11}^2 - \omega_6 \omega_{18} + \omega_6 v_3^2 \omega_{18} - \omega_{11} \omega_{18} + 3\omega_6 c_s^2 \omega_{18} + 3c_s^2 \omega_{11} \omega_{18} \\
C_8 &= -6\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 36\omega_6^2 c_s^2 \omega_{18} - 11\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 24c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6 c_s^2 \omega_{11}^2 + 6\omega_6^2 \omega_{11} \omega_{18} - 24\omega_6 c_s^2 \omega_{11} \omega_{18} - 12\omega_6 v_3^2 \omega_{11}^2 + 12\omega_6 \omega_{11}^2 - \\
& 12\omega_6^2 \omega_{18} + 6\omega_6 v_3^2 \omega_{11}^2 \omega_{18} - 6\omega_6 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11} + 12\omega_6^2 v_3^2 \omega_{11}^2 + 3\omega_6^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 \omega_{11}^2 + 42\omega_6 c_s^2 \omega_{11}^2 \omega_{18} - 18\omega_6^2 c_s^2 \omega_{11} \omega_{18} + \\
& 12\omega_6^2 \omega_{11} - 12\omega_6^2 v_3^2 \omega_{11} - 3\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \\
C_9 &= 3v_3^2 \omega_{11} \omega_{18} - 3v_3^2 \omega_{11}^2 - 3\omega_6 v_3^2 \omega_{11} + \omega_6 \omega_{11} + \omega_6 c_s^2 \omega_{11}^2 - \omega_6 c_s^2 \omega_{11} - \omega_6 c_s^2 \omega_{11} \omega_{18} + 3\omega_6 v_3^2 \omega_{11}^2 - \omega_6 \omega_{11}^2 - c_s^2 \omega_{11}^2 - 3\omega_6 v_3^2 \omega_{11} \omega_{18} + \\
& \omega_6 \omega_{11} \omega_{18} + \omega_{11}^2 - \omega_6 \omega_{18} + 3\omega_6 v_3^2 \omega_{18} - \omega_{11} \omega_{18} + \omega_6 c_s^2 \omega_{18} + c_s^2 \omega_{11} \omega_{18} \\
C_{10} &= 3c_s^2 \omega_7 \omega_{11}^2 + \omega_{19} \omega_7 v_3^2 + \omega_{19} \omega_7 \omega_{11} + \omega_{19} v_3^2 \omega_{11} - \omega_7 \omega_{11}^2 - v_3^2 \omega_{11}^2 - \omega_{19} \omega_7 - \omega_{19} \omega_7 v_3^2 \omega_{11} + \omega_7 \omega_{11} - 3c_s^2 \omega_7 \omega_{11} - 3c_s^2 \omega_{11}^2 + 3\omega_{19} c_s^2 \omega_{11} + \\
& \omega_{11}^2 - 3\omega_{19} c_s^2 \omega_7 \omega_{11} - \omega_7 v_3^2 \omega_{11} - \omega_{19} \omega_{11} + \omega_7 v_3^2 \omega_{11} + 3\omega_{19} c_s^2 \omega_7 \\
C_{11} &= -12c_s^2 \omega_7 \omega_{11}^2 - 24\omega_{19} c_s^2 \omega_{11}^2 + 12\omega_7 \omega_{11}^2 - 11\omega_{19} c_s^2 \omega_{11}^2 + 12\omega_7^2 v_3^2 \omega_{11}^2 + 6\omega_{19} \omega_7 v_3^2 \omega_{11}^2 - 12\omega_{19} \omega_7^2 - 6\omega_{19} \omega_7 \omega_{11}^2 - 12\omega_7^2 v_3^2 \omega_{11} - \\
& 18\omega_{19} c_s^2 \omega_7 \omega_{11} + 3\omega_{19} \omega_7^2 \omega_{11}^2 + 12\omega_7^2 \omega_{11} - 24\omega_{19} c_s^2 \omega_7 \omega_{11} + 36\omega_{19} c_s^2 \omega_7^2 - 12c_s^2 \omega_7^2 \omega_{11} - 6\omega_{19} \omega_7^2 v_3^2 \omega_{11} - 12\omega_7 v_3^2 \omega_{11}^2 - 3\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 + \\
& 12c_s^2 \omega_7^2 \omega_{11}^2 + 12\omega_{19} \omega_7^2 v_3^2 + 6\omega_{19} \omega_7^2 \omega_{11} + 42\omega_{19} c_s^2 \omega_7 \omega_{11}^2 - 12\omega_7^2 \omega_{11}^2 \\
C_{12} &= c_s^2 \omega_7 \omega_{11}^2 + 3\omega_{19} \omega_7 v_3^2 + \omega_{19} \omega_7 \omega_{11} + 3\omega_{19} v_3^2 \omega_{11} - \omega_7 \omega_{11}^2 - 3v_3^2 \omega_{11}^2 - \omega_{19} \omega_7 - 3\omega_{19} \omega_7 v_3^2 \omega_{11} + \omega_7 \omega_{11} - c_s^2 \omega_7 \omega_{11} - c_s^2 \omega_{11}^2 + \omega_{19} c_s^2 \omega_{11} + \\
& \omega_{11}^2 - \omega_{19} c_s^2 \omega_7 \omega_{11} - 3\omega_7 v_3^2 \omega_{11} - \omega_{19} \omega_{11} + 3\omega_7 v_3^2 \omega_{11}^2 + \omega_{19} c_s^2 \omega_7 \\
C_{13} &= 12c_s^2 \omega_{11} + 24c_s^2 v_3^2 \omega_{11}^2 + 144c_s^2 v_3^2 - 7v_3^2 \omega_{11}^2 + 36v_3^4 - 12c_s^2 + 36v_3^2 \omega_{11} - 144c_s^2 v_3^2 \omega_{11} - c_s^2 \omega_{11}^2 + 12c_s^4 - 12c_s^4 \omega_{11} + 7v_3^4 \omega_{11}^2 - 36v_3^4 \omega_{11} + c_s^4 \omega_{11}^2 - 36v_3^2 \\
C_{14} &= -126\omega_9^2 \omega_6^2 c_s^2 v_1^2 \omega_{13} - 48\omega_9 \omega_6 v_1^4 \omega_{13} - 36\omega_6^2 v_1^4 \omega_{13} + 48\omega_9 \omega_6 c_s^2 \omega_{13}^2 + 24\omega_6 c_s^4 \omega_{13}^2 - 36\omega_9 \omega_6^2 v_1^2 \omega_{13}^2 - 12\omega_9^2 \omega_6^2 v_1^2 - 3\omega_6^2 \omega_6^2 v_1^4 \omega_{13} - \\
& 24\omega_9 c_s^2 \omega_{13}^2 + 12\omega_9^2 \omega_6^2 c_s^2 \omega_{13} - 144\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 - 24\omega_9^2 \omega_6^2 v_1^4 + 72\omega_9 \omega_6 c_s^2 v_1^2 \omega_{13} - 24\omega_9^2 c_s^2 \omega_{13} - 96\omega_9^2 \omega_6 v_1^2 \omega_{13} + 150\omega_9 \omega_6 c_s^2 v_1^2 \omega_{13}^2 + 48\omega_9^2 v_1^2 \omega_{13} -
\end{aligned}$$

$$\begin{aligned}
& 24\omega_9^2\omega_6c_s^4 + 48\omega_9^2\omega_6c_s^4\omega_{13} - 30\omega_9^2\omega_6^2v_1^4\omega_{13} + \omega_9^2\omega_6^2c_s^2\omega_{13}^2 + 48\omega_9v_1^2\omega_{13}^2 - 216\omega_9^2c_s^2v_1^2\omega_{13} - 72\omega_6v_1^2\omega_{13}^2 + 14\omega_9\omega_6^2c_s^4\omega_{13}^2 + 72\omega_9^2\omega_6^2c_s^2v_1^2 - \\
& 24\omega_9\omega_6^2v_1^2\omega_{13} - 12\omega_9^2\omega_6^2c_s^2 - 12\omega_9^2\omega_6^2c_s^2v_1^2\omega_{13}^2 + 12\omega_9^2c_s^2\omega_{13}^2 - 96\omega_9\omega_6v_1^4\omega_{13}^2 + 3\omega_9^2\omega_6^2v_1^2\omega_{13}^2 + 24\omega_9c_s^2\omega_{13}^2 + 216\omega_9c_s^2v_1^2\omega_{13}^2 - 12\omega_9^2\omega_6^2c_s^2\omega_{13} + \\
& 24\omega_9\omega_6c_s^2 + 24\omega_9^2\omega_6c_s^2v_1^2\omega_{13} + 432\omega_9\omega_6c_s^2v_1^2\omega_{13}^2 + 96\omega_9^2\omega_6v_1^4\omega_{13} + 12\omega_9^2\omega_6^2c_s^4 + 48\omega_9\omega_6^2c_s^2v_1^2\omega_{13} - 144\omega_9\omega_6^2c_s^2v_1^2\omega_{13} - 144\omega_9^2\omega_6c_s^2v_1^2 - \\
& 48\omega_9\omega_6^2c_s^2\omega_{13}^2 + 36\omega_9^2v_1^2\omega_{13}^2 + 288\omega_6^2v_1^2\omega_{13}^2 + 36\omega_9v_1^4\omega_{13}^2 - 24\omega_6c_s^2\omega_{13}^2 - 14\omega_9\omega_6^2c_s^2\omega_{13}^2 + 72\omega_6v_1^2\omega_{13}^2 + 24\omega_9\omega_6^2v_1^2\omega_{13} + 12\omega_9^2\omega_6^2v_1^4 + \\
& 96\omega_9\omega_6v_1^2\omega_{13}^2 - 12\omega_6^2c_s^4\omega_{13}^2 - 432\omega_9\omega_6c_s^2v_1^2\omega_{13}^2 - 48\omega_9^2v_1^4\omega_{13} - 48\omega_9\omega_6^2c_s^2\omega_{13} + 30\omega_9^2\omega_6^2v_1^2\omega_{13} + 24\omega_9^2\omega_6v_1^2 - \omega_9^2\omega_6^2c_s^4\omega_{13} - 48\omega_9v_1^2\omega_{13}^2
\end{aligned}$$

$$C_{16} = 24\omega_6^2 c_s^2 \omega_{13} + 24\omega_6^2 v_1^2 - 24\omega_6 v_1^4 \omega_{13} + 6\omega_6^3 c_s^4 \omega_{13} + 48\omega_6 v_1^2 \omega_{13} - 48\omega_6 c_s^4 \omega_{13}^2 - 3\omega_6^3 v_1^2 \omega_{13}^2 - 72\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 - 12\omega_6^3 c_s^2 v_1^2 \omega_{13} - 96c_s^2 v_1^2 \omega_{13}^2 + 6\omega_6^3 c_s^2 v_1^2 \omega_{13}^2 - 24\omega_6^2 c_s^2 v_1^2 - 12\omega_6^3 v_1^2 + 48\omega_6^2 c_s^2 v_1^2 \omega_{13} + 24c_s^4 \omega_{13} - 24\omega_6 v_1^2 \omega_{13} - 3\omega_6^3 c_s^4 \omega_{13}^2 + 18\omega_6^3 v_1^2 \omega_{13} + 24\omega_6 c_s^4 \omega_{13} - 8\omega_6^2 c_s^2 \omega_{13}^2 + 72\omega_6^4 \omega_{13} + 12\omega_6^3 v_1^4 - 24\omega_6^2 c_s^4 \omega_{13} + 24\omega_6^2 v_1^2 \omega_{13}^2 - 48\omega_6 v_1^4 \omega_{13} + 156\omega_6 c_s^2 v_1^2 \omega_{13} - 6\omega_6^3 c_s^2 \omega_{13}^2 + 3\omega_6^3 v_1^4 \omega_{13} + 12\omega_6 c_s^2 \omega_{13}^2 + \omega_6^3 c_s^2 \omega_{13}^2 + 24\omega_6 v_1^4 \omega_{13} - 24\omega_6 c_s^2 v_1^2 \omega_{13} - 24\omega_6 c_s^2 \omega_{13} - 18\omega_6^3 v_1^4 \omega_{13} + 24\omega_6^2 c_s^4 \omega_{13} - 24\omega_6^3 v_1^4 - 72\omega_6^2 v_1^2 \omega_{13} + 12\omega_6^3 c_s^2 v_1^2$$

$$\begin{aligned}
C_{18} = & 6w_9w_{12}w_{13}w_{14}w_{15}w_{16}w_{17}w_{18}w_{19}w_{20}w_{21}w_{22}w_{23}w_{24}w_{25}w_{26}w_{27}w_{28}w_{29}w_{30}w_{31}w_{32}w_{33}w_{34}w_{35}w_{36}w_{37}w_{38}w_{39}w_{40}w_{41}w_{42}w_{43}w_{44}w_{45}w_{46}w_{47}w_{48}w_{49}w_{50}w_{51}w_{52}w_{53}w_{54}w_{55}w_{56}w_{57}w_{58}w_{59}w_{60}w_{61}w_{62}w_{63}w_{64}w_{65}w_{66}w_{67}w_{68}w_{69}w_{70}w_{71}w_{72}w_{73}w_{74}w_{75}w_{76}w_{77}w_{78}w_{79}w_{80}w_{81}w_{82}w_{83}w_{84}w_{85}w_{86}w_{87}w_{88}w_{89}w_{90}w_{91}w_{92}w_{93}w_{94}w_{95}w_{96}w_{97}w_{98}w_{99}w_{100}w_{101}w_{102}w_{103}w_{104}w_{105}w_{106}w_{107}w_{108}w_{109}w_{110}w_{111}w_{112}w_{113}w_{114}w_{115}w_{116}w_{117}w_{118}w_{119}w_{120}w_{121}w_{122}w_{123}w_{124}w_{125}w_{126}w_{127}w_{128}w_{129}w_{130}w_{131}w_{132}w_{133}w_{134}w_{135}w_{136}w_{137}w_{138}w_{139}w_{140}w_{141}w_{142}w_{143}w_{144}w_{145}w_{146}w_{147}w_{148}w_{149}w_{150}w_{151}w_{152}w_{153}w_{154}w_{155}w_{156}w_{157}w_{158}w_{159}w_{160}w_{161}w_{162}w_{163}w_{164}w_{165}w_{166}w_{167}w_{168}w_{169}w_{170}w_{171}w_{172}w_{173}w_{174}w_{175}w_{176}w_{177}w_{178}w_{179}w_{180}w_{181}w_{182}w_{183}w_{184}w_{185}w_{186}w_{187}w_{188}w_{189}w_{190}w_{191}w_{192}w_{193}w_{194}w_{195}w_{196}w_{197}w_{198}w_{199}w_{200}w_{201}w_{202}w_{203}w_{204}w_{205}w_{206}w_{207}w_{208}w_{209}w_{210}w_{211}w_{212}w_{213}w_{214}w_{215}w_{216}w_{217}w_{218}w_{219}w_{220}w_{221}w_{222}w_{223}w_{224}w_{225}w_{226}w_{227}w_{228}w_{229}w_{230}w_{231}w_{232}w_{233}w_{234}w_{235}w_{236}w_{237}w_{238}w_{239}w_{240}w_{241}w_{242}w_{243}w_{244}w_{245}w_{246}w_{247}w_{248}w_{249}w_{250}w_{251}w_{252}w_{253}w_{254}w_{255}w_{256}w_{257}w_{258}w_{259}w_{260}w_{261}w_{262}w_{263}w_{264}w_{265}w_{266}w_{267}w_{268}w_{269}w_{270}w_{271}w_{272}w_{273}w_{274}w_{275}w_{276}w_{277}w_{278}w_{279}w_{280}w_{281}w_{282}w_{283}w_{284}w_{285}w_{286}w_{287}w_{288}w_{289}w_{290}w_{291}w_{292}w_{293}w_{294}w_{295}w_{296}w_{297}w_{298}w_{299}w_{300}w_{301}w_{302}w_{303}w_{304}w_{305}w_{306}w_{307}w_{308}w_{309}w_{310}w_{311}w_{312}w_{313}w_{314}w_{315}w_{316}w_{317}w_{318}w_{319}w_{320}w_{321}w_{322}w_{323}w_{324}w_{325}w_{326}w_{327}w_{328}w_{329}w_{330}w_{331}w_{332}w_{333}w_{334}w_{335}w_{336}w_{337}w_{338}w_{339}w_{340}w_{341}w_{342}w_{343}w_{344}w_{345}w_{346}w_{347}w_{348}w_{349}w_{350}w_{351}w_{352}w_{353}w_{354}w_{355}w_{356}w_{357}w_{358}w_{359}w_{360}w_{361}w_{362}w_{363}w_{364}w_{365}w_{366}w_{367}w_{368}w_{369}w_{370}w_{371}w_{372}w_{373}w_{374}w_{375}w_{376}w_{377}w_{378}w_{379}w_{380}w_{381}w_{382}w_{383}w_{384}w_{385}w_{386}w_{387}w_{388}w_{389}w_{390}w_{391}w_{392}w_{393}w_{394}w_{395}w_{396}w_{397}w_{398}w_{399}w_{400}w_{401}w_{402}w_{403}w_{404}w_{405}w_{406}w_{407}w_{408}w_{409}w_{410}w_{411}w_{412}w_{413}w_{414}w_{415}w_{416}w_{417}w_{418}w_{419}w_{420}w_{421}w_{422}w_{423}w_{424}w_{425}w_{426}w_{427}w_{428}w_{429}w_{430}w_{431}w_{432}w_{433}w_{434}w_{435}w_{436}w_{437}w_{438}w_{439}w_{440}w_{441}w_{442}w_{443}w_{444}w_{445}w_{446}w_{447}w_{448}w_{449}w_{450}w_{451}w_{452}w_{453}w_{454}w_{455}w_{456}w_{457}w_{458}w_{459}w_{460}w_{461}w_{462}w_{463}w_{464}w_{465}w_{466}w_{467}w_{468}w_{469}w_{470}w_{471}w_{472}w_{473}w_{474}w_{475}w_{476}w_{477}w_{478}w_{479}w_{480}w_{481}w_{482}w_{483}w_{484}w_{485}w_{486}w_{487}w_{488}w_{489}w_{490}w_{491}w_{492}w_{493}w_{494}w_{495}w_{496}w_{497}w_{498}w_{499}w_{500}w_{501}w_{502}w_{503}w_{504}w_{505}w_{506}w_{507}w_{508}w_{509}w_{510}w_{511}w_{512}w_{513}w_{514}w_{515}w_{516}w_{517}w_{518}w_{519}w_{520}w_{521}w_{522}w_{523}w_{524}w_{525}w_{526}w_{527}w_{528}w_{529}w_{530}w_{531}w_{532}w_{533}w_{534}w_{535}w_{536}w_{537}w_{538}w_{539}w_{540}w_{541}w_{542}w_{543}w_{544}w_{545}w_{546}w_{547}w_{548}w_{549}w_{550}w_{551}w_{552}w_{553}w_{554}w_{555}w_{556}w_{557}w_{558}w_{559}w_{560}w_{561}w_{562}w_{563}w_{564}w_{565}w_{566}w_{567}w_{568}w_{569}w_{570}w_{571}w_{572}w_{573}w_{574}w_{575}w_{576}w_{577}w_{578}w_{579}w_{580}w_{581}w_{582}w_{583}w_{584}w_{585}w_{586}w_{587}w_{588}w_{589}w_{590}w_{591}w_{592}w_{593}w_{594}w_{595}w_{596}w_{597}w_{598}w_{599}w_{600}w_{601}w_{602}w_{603}w_{604}w_{605}w_{606}w_{607}w_{608}w_{609}w_{610}w_{611}w_{612}w_{613}w_{614}w_{615}w_{616}w_{617}w_{618}w_{619}w_{620}w_{621}w_{622}w_{623}w_{624}w_{625}w_{626}w_{627}w_{628}w_{629}w_{630}w_{631}w_{632}w_{633}w_{634}w_{635}w_{636}w_{637}w_{638}w_{639}w_{640}w_{641}w_{642}w_{643}w_{644}w_{645}w_{646}w_{647}w_{648}w_{649}w_{650}w_{651}w_{652}w_{653}w_{654}w_{655}w_{656}w_{657}w_{658}w_{659}w_{660}w_{661}w_{662}w_{663}w_{664}w_{665}w_{666}w_{667}w_{668}w_{669}w_{670}w_{671}w_{672}w_{673}w_{674}w_{675}w_{676}w_{677}w_{678}w_{679}w_{680}w_{681}w_{682}w_{683}w_{684}w_{685}w_{686}w_{687}w_{688}w_{689}w_{690}w_{691}w_{692}w_{693}w_{694}w_{695}w_{696}w_{697}w_{698}w_{699}w_{700}w_{701}w_{702}w_{703}w_{704$$

$$\begin{aligned}
& 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_8 + 2w_6^2c_s^2w_{13}w_7^2w_{17}w_{14}w_8^2 + w_6^3c_s^2w_{16}w_7^3w_{17}w_8^2 - w_6^3w_{16}v_1^2w_7^2w_{17}w_{14}w_8^2 - 2w_6^3w_{16}v_1^2w_{13}w_7^3w_{17}w_{14} - \\
& w_6^3w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8^2 - w_6^3w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8^2 - w_6c_s^2w_{16}w_{13}w_7^3w_{17}w_{14}w_8^2 + 2w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_8^2 - w_6^2w_{16}v_2^2w_{13}w_7^3w_{14}w_8^2 + \\
& 2w_6^2w_{16}v_1^2w_{13}w_7^3w_{17}w_8 - 2w_6^2w_{16}v_2^2w_{13}w_7^3w_{14}w_8 - 2w_6^3w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8^2 + 2w_6^2w_{16}v_2^2w_{13}w_7^2w_{17}w_{14}w_8 + \\
& 2w_6w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8 + 2w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8 - 2w_6^2c_s^2w_{16}w_{13}w_7^3w_{17}w_8^2 - 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_{14}w_8 - 4w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8^2 - \\
& 6w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_{14}w_8^2 + 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{14}w_8^2 - w_6^3c_s^2w_{16}w_{13}w_7^3w_{17}w_8^2 - 2w_6w_{16}v_2^2w_{13}w_7^2w_{17}w_{14}w_8 + 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_{14}w_8^2 - \\
& 6w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8 - 2w_6^2v_2^2w_{13}w_7^2w_{14}w_8^2 - 6w_6^2w_{16}v_2^2w_{13}w_7^2w_{17}w_{14}w_8 - 2w_6^2w_{16}v_1^2w_{13}w_7^2w_{14}w_8 - 2w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_8^2 - \\
& 2w_6^2c_s^2w_{13}w_7^2w_{14}w_8^2 + w_6^3w_{16}v_1^2w_{13}w_7^2w_{17}w_8^2 - 2w_6^3w_{16}v_2^2w_{13}w_7^3w_{17}w_{14} + 4w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_{14}w_8^2 - 2w_6^3w_{16}v_1^2w_{13}w_7^2w_{17}w_8^2 + \\
& 2w_6^3w_{16}v_2^2w_{13}w_7^3w_{17}w_{14}w_8 + 2w_6^2w_{16}v_2^2w_{13}w_7^2w_{17}w_{14}w_8 - w_6^3c_s^2w_{16}w_7^2w_{17}w_{14}w_8^2 + 2w_6^2w_{16}v_2^2w_{13}w_7^2w_{17}w_{14}w_8 - w_6^3c_s^2w_{16}w_{13}w_7^2w_{17}w_{14}w_8^2 + \\
& 2w_6^2w_{16}v_1^2w_{13}w_7^2w_{17}w_{14} + 2w_6^2w_{16}v_2^2w_{13}w_7^2w_{14}w_8^2 - 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_8^2 + 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_8^2 - 2w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_{14}w_8 + \\
& 3w_6w_{16}v_2^2w_{13}w_7^2w_{17}w_{14}w_8^2 + 2w_6^2c_s^2w_{16}w_{13}w_7^3w_{17}w_8^2 + 3w_6^3w_{16}v_1^2w_{13}w_7w_{17}w_{14}w_8^2 + w_6^2c_s^2w_{16}w_{13}w_7^2w_{17}w_{14}w_8^2
\end{aligned}$$

[illegible]

[illegible]

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$$\begin{aligned}
C_{43} = & -12c_s^2w_{16}^2w_{10}^2v_3^2w_7^3w_{11} + 12w_{19}w_{16}w_{10}^2v_3^2w_7^3w_{23} + 72w_{19}c_s^2w_{16}^2w_{10}w_7v_3^2w_{23}w_{11} - 12c_s^2w_{16}^2w_{10}w_7^3w_{23}w_{11} - 3w_{19}c_s^2w_{16}w_{10}^2v_3^2w_7^3w_{23}w_{11} - \\
& -36c_s^4w_{16}^2w_{10}w_{10}^2w_{11} - 36w_{19}c_s^2w_{16}^2w_{10}w_{10}^2v_3^2w_{11} + 6w_{19}c_s^2w_{16}^2w_{10}v_3^2w_7^3w_{23} + 36c_s^2w_{16}^2w_{10}w_7^3v_3^2 - 12w_{19}w_{16}^2w_7^3v_3^2w_{23}w_{11} - \\
& -12w_{19}c_s^2w_{16}^2w_{10}w_7w_{23}w_{11} + 12c_s^2w_{16}^2w_{10}w_7^3w_{11} + 15w_{19}w_{16}w_{10}^2w_7^3v_3^2w_{23}w_{11} + 12w_{19}c_s^4w_{16}w_{10}^2w_7^3w_{23}w_{11} + 12w_{19}c_s^2w_{16}^2w_{10}^2v_2w_7w_{23}w_{11} + \\
& -6w_{19}w_{16}^2w_{10}^2v_2^2w_7^3w_{11} + 24w_{19}w_{16}w_{10}^2w_7^3v_2w_{23}w_{11} - 6w_{19}w_{16}w_{10}w_7^3v_2^2w_{23}w_{11} + 6w_{19}w_{16}w_{10}w_7^3v_2^2w_{23}w_{11} + 156w_{19}c_s^4w_{16}^2w_{10}^2w_7w_{23}w_{11} - \\
& -12w_{19}c_s^2w_{16}^2w_{10}^2w_{11} + 12w_{19}w_{10}^2v_2^2v_3^2w_{23}w_{11} - 12w_{16}^2w_{10}^2w_7^3v_3^2w_{11} - 12c_s^2w_{16}^2w_{10}^2w_7^3 + 48w_{19}w_{16}w_{10}^2v_3^2w_7^3w_{23}w_{11} + \\
& -36w_{19}w_{16}^2w_{10}w_7^3v_3^2w_{23}w_{11} - 12w_{19}c_s^2w_{16}^2w_{10}^2v_2w_7w_{23}w_{11} - 12w_{19}w_{16}w_{10}^2w_7^3v_3^2w_{23} + 36c_s^2w_{16}^2w_{10}w_7^3v_3^2w_{23}w_{11} - 6w_{19}w_{16}^2w_{10}^2v_2^2w_7^3 + \\
& -36c_s^4w_{16}^2w_{10}^2w_{23}w_{11} + 12w_{16}^2w_{10}^2v_2^2v_3^2w_{23}w_{11} + 36w_{19}c_s^4w_{16}^2w_{10}^2w_{11} - 24w_{19}w_{16}^2w_{10}^2w_7^3v_3^2w_{23} + 6w_{19}c_s^2w_{10}^2v_2^2w_7^3w_{23}w_{11} + \\
& -36w_{19}c_s^2w_{16}^2w_{10}^2w_{11} - 12c_s^2w_{16}^2w_{10}^2w_7^3w_{23}w_{11} + 12w_{19}c_s^2w_{16}^2w_{10}^2w_7w_{23}w_{11} - 36c_s^2w_{16}^2w_{10}^2w_7^3w_{23}w_{11} + 12w_{16}^2w_{10}^2v_2^2w_7^3w_{11} + \\
& -18w_{19}c_s^4w_{16}^2w_{10}^2w_{23} - 9w_{19}w_{16}^2w_{10}^2v_3^2w_{23}w_{11} - 15w_{19}w_{16}w_{10}^2v_2^2v_3^2w_{23}w_{11} + 3w_{19}c_s^2w_{16}^2w_{10}^2w_7^3w_{23}w_{11} - 72w_{19}c_s^2w_{16}^2w_{10}^2w_7^3v_3^2w_{23} - \\
& -6w_{19}c_s^2w_{10}^2w_7^3w_{23}w_{11} - 12c_s^2w_{16}^2w_{10}^2w_7^3w_{11} - 6w_{19}w_{10}^2w_7^3v_3^2w_{23}w_{11} - 12w_{19}w_{16}w_{10}^2w_7^3v_3^2w_{23}w_{11} + 12w_{19}w_{16}w_{10}^2v_3^2w_{23}w_{11} - \\
& -36c_s^2w_{16}^2w_{10}^2w_7^3w_{11} - 5w_{19}c_s^2w_{16}^2w_{10}^2w_7^3w_{23}w_{11} - 72w_{19}c_s^2w_{16}^2w_{10}^2w_7w_{23}w_{11} - 6w_{19}w_{16}^2w_{10}^2w_7^3v_3^2w_{23} + 6w_{19}w_{16}^2w_{10}^2v_3^2w_{11} - \\
& -6w_{19}c_s^2w_{16}^2w_{10}^2v_3^2 - 6w_{19}c_s^2w_{16}^2w_{10}^2w_{23}w_{11} - 18w_{19}c_s^4w_{16}^2w_{10}^2w_{11} - 18w_{19}c_s^2w_{16}^2w_{10}^2w_{23}w_{11} + 12c_s^2w_{16}^2w_{10}^2v_2^2w_{11} - \\
& -18w_{19}c_s^2w_{16}^2w_{10}^2v_3^2w_{23} + 3w_{19}c_s^4w_{16}^2w_{10}^2w_{23}w_{11} - 6w_{19}c_s^2w_{10}^2w_7^3w_{23}w_{11} + 36c_s^4w_{16}^2w_{10}^2w_{11} - 12w_{16}^2w_{10}^2v_2^2v_3^2w_7^3w_{23}w_{11} + \\
& -6w_{19}w_{16}^2w_{10}^2v_3^2w_{23}w_{11} + w_{19}c_s^2w_{16}^2w_{10}^2v_2^2w_7^3w_{23}w_{11} - 6w_{19}w_{16}^2w_{10}^2w_7^3v_3^2w_{11} - 12w_{16}^2w_{10}^2w_7^3v_3^2 - 18w_{19}c_s^4w_{16}^2w_{10}^2w_{11} + \\
& -15w_{19}c_s^2w_{16}^2w_{10}^2w_{23}w_{11} + 54w_{19}c_s^2w_{16}^2w_{10}^2w_{23}w_{11} + 12w_{16}^2w_{10}^2v_2^2w_{23} - w_{19}c_s^2w_{16}^2w_{10}^2w_{23}w_{11} + 6w_{19}c_s^2w_{16}^2w_{10}^2w_{11} - \\
& -12w_{19}c_s^2w_{16}^2w_{10}^2v_3^2w_{23}w_{11} - 6w_{19}w_{16}^2w_{10}^2v_2^2w_7^3w_{11} - 48w_{19}w_{16}^2w_{10}^2w_7^3v_3^2w_{23}w_{11} - 12w_{19}c_s^2w_{16}^2w_{10}^2v_2^2w_7^3w_{23}w_{11} + 6w_{19}w_{16}^2w_{10}^2v_3^2w_{23} + \\
& -12w_{19}c_s^2w_{16}^2w_{10}^2v_2^2w_{11} - 36w_{19}w_{16}^2w_{10}^2v_2^2v_3^2w_{23}w_{11} - 96w_{19}c_s^2w_{16}^2w_{10}^2w_{23}w_{11} + 12c_s^2w_{16}^2w_{10}^2v_2^2w_{23}w_{11} - 18w_{19}c_s^2w_{16}^2w_{10}^2w_7^3v_3^2w_{11} + \\
& -12w_{16}^2w_{10}^2w_7^3v_3^2w_{11} + 18w_{19}c_s^2w_{10}^2w_7^3v_3^2w_{23}w_{11} + 6w_{19}w_{16}^2w_{10}^2w_7^3v_3^2 + 18w_{19}c_s^2w_{16}^2w_{10}^2w_7^3w_{23}w_{11} + 12w_{19}c_s^2w_{16}^2w_{10}^2w_7w_{23}w_{11} - \\
& -36c_s^4w_{16}^2w_{10}^2w_{23}w_{11} - 12w_{19}w_{10}^2v_2^2v_3^2w_{23}w_{11} - 108w_{19}c_s^2w_{16}^2w_{10}^2w_7^3v_3^2w_{23}w_{11} + 24w_{19}w_{16}^2w_{10}^2w_7^3v_3^2w_{23} + 12c_s^2w_{16}^2w_{10}^2v_2^2w_7^3 + \\
& -12c_s^2w_{16}^2w_{10}^2w_{23}w_{11} - 45w_{19}c_s^2w_{16}^2w_{10}^2w_7^3w_{23}w_{11} + 36c_s^4w_{16}^2w_{10}^2w_{11} - 6w_{19}w_{16}^2w_{10}^2v_2^2w_7^3w_{23}w_{11} - 12w_{16}^2w_{10}^2w_7^3v_3^2w_{23}w_{11} - 36w_{19}c_s^4w_{16}^2w_{10}^2w_{11} - \\
& -12w_{19}w_{16}^2w_{10}^2w_7^3v_3^2w_{11} - 24w_{19}w_{16}^2w_{10}^2w_7^3v_2w_{23}w_{11} - 24w_{19}w_{16}^2w_{10}^2v_2^2w_7^3w_{23}w_{11} + 18w_{19}c_s^2w_{16}^2w_{10}^2v_2^2w_7^3w_{23}w_{11} - 24w_{19}w_{16}^2w_{10}^2v_2^2w_7^3v_3^2w_{23} + \\
& + 12c_s^2w_{16}^2w_{10}^2w_{23}w_{11} - 36c_s^2w_{16}^2w_{10}^2w_7^3v_3^2w_{23} - 36c$$

$$C_{44} = -36c_{s16}^2w_{10}^2v_7^2w_{11} + 36w_{19}w_{16}w_{10}^2v_7^2w_3^2w_{23} + 24w_{19}c_{s16}^2w_{16}w_{10}w_7w_3^2w_{23}w_{11} - 12c_{s16}^2w_{16}w_{10}w_7^2w_{23}w_{11} + 30w_{19}c_{s16}^2w_{16}w_{10}^2v_7^2w_3^2w_{23}w_{11} - 12c_{s16}^2w_{16}w_{10}^2w_{11} - 12w_{19}c_{s16}^2w_{16}w_{10}^2v_7^2w_{11} + 18w_{19}c_{s16}^2w_{16}w_{10}^2v_7^2w_{23} + 12c_{s16}^2w_{16}w_{10}^2w_3^2 - 12w_{19}w_{16}w_{10}^2v_7^2w_3^2w_{23}w_{11} + 12c_{s16}^2w_{16}w_{10}^2w_7^2w_{11} + 15w_{19}w_{16}w_{10}^2v_7^2w_3^2w_{23}w_{11} + 12w_{19}c_{s16}^2w_{16}w_{10}^2w_7w_{23}w_{11} + 60w_{19}c_{s16}^2w_{16}w_{10}^2w_7w_{23}w_{11} + 18w_{19}w_{16}w_{10}^2v_7^2w_{11} + 72w_{19}w_{16}w_{10}^2w_7w_3^2w_{23}w_{11} - 6w_{19}w_{16}w_{10}w_7^2v_3^2w_{23}w_{11} + 18w_{19}w_{16}w_{10}v_7^2w_7^2v_3^2w_{23}w_{11} + 18w_{19}c_{s16}^2w_{16}w_{10}^2w_7w_{23}w_{11} - 12w_{19}c_{s16}^2w_{16}w_{10}^2w_{11} + 12w_{19}w_{10}^2w_7^2v_3^2w_{23}w_{11} - 12c_{s16}^2w_{16}w_{10}^2w_7^2 + 14w_{19}w_{16}w_{10}^2v_7^2w_3^2w_{23}w_{11} + 36w_{19}c_{s16}^2w_{16}w_{10}^2w_7^2v_3^2w_{23}w_{11} - 36w_{19}c_{s16}^2w_{16}w_{10}^2v_7^2w_3^2w_{23}w_{11} - 12w_{19}w_{16}w_{10}^2v_7^2w_{23} + 12c_{s16}^2w_{16}w_{10}^2w_7^2v_3^2w_{23}w_{11} - 18w_{19}w_{16}w_{10}^2v_7^2w_3^2 + 12c_{s16}^2w_{16}w_{10}^2w_7^2v_3^2w_{23}w_{11} + 36w_{19}c_{s16}^2w_{16}w_{10}^2w_7^2v_3^2w_{23}w_{11} -$$

$$\begin{aligned}
& 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 12\omega_6\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 6\omega_6^3\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + \\
& 18\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 18\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 36\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 12\omega_6^2v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 108\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + \\
& 24\omega_6\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 18\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 24\omega_6\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 6\omega_6^3v_1^2\omega_{11}^2\omega_{18}^2 + \\
& 18\omega_6^2v_1^2\omega_{11}^2\omega_{18}^2 - 12\omega_6^2v_1^2\omega_{11}^2\omega_{18}^2 - 18\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 30\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 18\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - \\
& 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 12\omega_6\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 72\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 6\omega_6^3v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - \\
& 36\omega_6^2v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 36\omega_6^2v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 18\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 12\omega_6^2v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 24\omega_6\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + \\
& 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 72\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + 12\omega_6^2\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 + \omega_6^3\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2 - 24\omega_6\omega_{22}v_1^2v_3^2\omega_{11}^2\omega_{18}^2
\end{aligned}$$

[illegible]

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[illegible]

$$4\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + 96\omega_6^2 c_s^2 v_3^2 \omega_{18}^2 - 4\omega_6^2 c_s^4 \omega_{11} \omega_{18} - 13\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 8\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18}^2 - 36c_s^2 v_3^2 \omega_{11}^3 \omega_{18} + 51\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18}^2 + 4\omega_6^2 v_3^2 \omega_{11}^2 - 8v_3^2 \omega_{11}^2 \omega_{18} + 84\omega_6^2 c_s^2 v_3^2 \omega_{11}^3 \omega_{18} - 24\omega_6^2 c_s^2 v_3^2 \omega_{11}^3 + 8\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 36c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 51\omega_6^2 c_s^2 v_3^2 \omega_{11}^3 \omega_{18} + 24\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 13\omega_6^2 v_3^2 \omega_{11}^3 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 32\omega_6^2 v_3^4 \omega_{11} \omega_{18} + 8v_3^2 \omega_{11}^3 \omega_{18} - 4\omega_6^2 c_s^4 \omega_{11}^2 - 4\omega_6^2 v_3^2 \omega_{11}^3 - 84\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} + 20\omega_6^2 v_3^4 \omega_{11} \omega_{18} + 13\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} + 4\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 48\omega_6^2 c_s^2 v_3^2 \omega_{11} \omega_{18} + 8\omega_6^2 c_s^4 \omega_{18}^2 + 8\omega_6^2 c_s^2 \omega_{11} \omega_{18}^2 - 4\omega_6^2 v_3^4 \omega_{11}^3 - 4\omega_6^2 c_s^2 \omega_{11}^3 + 8v_3^4 \omega_{11}^2 \omega_{18} - 8\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} - 13\omega_6^2 v_3^4 \omega_{11}^3 \omega_{18} - 32\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11} \omega_{18} + 4\omega_6^2 c_s^2 \omega_{11}^2 - 20\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 120\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 8v_3^4 \omega_{11}^3 \omega_{18}$$

$$C_{57} = 12\omega_6^2 v_3^4 \omega_{11}^3 \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^3 + 12\omega_6^2 c_s^2 v_3^2 \omega_{11}^3 \omega_{18}^2 + 90\omega_6^2 v_3^2 \omega_{11} \omega_{18}^2 - 5\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 6\omega_6^2 c_s^4 \omega_{11} \omega_{18} + 6\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 6\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + 72\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 v_3^4 \omega_{11}^3 + 54\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^2 - \omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 24\omega_6^2 v_3^2 \omega_{11}^3 \omega_{18} - 36\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 12\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - \omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 18\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 13\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 90\omega_6^2 v_3^4 \omega_{11} \omega_{18} + 12\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 - 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 6\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 60\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} + 12c_s^4 \omega_{11}^3 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 108\omega_6^2 c_s^2 v_3^2 \omega_{11} \omega_{18} - 24\omega_6^2 v_3^4 \omega_{11} \omega_{18} - 12\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 + 12\omega_6^2 c_s^4 \omega_{18}^2 + \omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 18\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + 36\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 21\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 27\omega_6^2 v_3^4 \omega_{11}^3 \omega_{18} + 162\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} + 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 v_3^2 \omega_{11}^3 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11} \omega_{18} - 18\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 60\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 30\omega_6^2 c_s^2 v_3^2 \omega_{11}^3 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^3 + 19\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 48\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 306\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 72\omega_6^2 v_3^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11} \omega_{18}^2 - 4\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 24\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^3 - 48\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 27\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 36\omega_6^2 c_s^2 v_3^2 \omega_{11} \omega_{18} - 24\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} - 81\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{18}^2 + 18\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 60\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11} \omega_{18} + 102\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} - 19\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 48\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 252\omega_6^2 c_s^2 v_3^2 \omega_{18} + 4\omega_6^2 v_3^4 \omega_{11}^3 \omega_{18} + 24\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11} \omega_{18} - 48c_s^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 v_3^2 \omega_{11}^2 \omega_{18}$$

$$C_{58} = 80\omega_6^2 v_3^2 \omega_{18}^2 - 64\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 16\omega_6^2 c_s^2 \omega_{11}^2 - 68\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 28\omega_6^2 \omega_{11}^2 \omega_{18} + 56\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 32\omega_6^2 c_s^2 \omega_{11} \omega_{18}^2 - 32\omega_6^2 \omega_{18}^2 + 68\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 28\omega_6^2 \omega_{11}^2 \omega_{18} + 48\omega_6^2 \omega_{11} \omega_{18}^2 + 20c_s^2 \omega_{11}^2 \omega_{18} + 24\omega_6^2 \omega_{11} \omega_{18} + 25\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_{11}^2 \omega_{18} - 120\omega_6^2 v_3^2 \omega_{11} \omega_{18}^2 - 20c_s^2 \omega_{11}^2 \omega_{18} - 48\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 48\omega_6^2 c_s^2 \omega_{18}^2 + 16\omega_6^2 \omega_{11} \omega_{18} - 16\omega_6^2 v_3^2 \omega_{11}^2 + 8\omega_6 \omega_{11}^3 + 12\omega_{11}^3 \omega_{18} - 25\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + 43\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 16\omega_6^2 v_3^2 \omega_{11}^2 + 28v_3^2 \omega_{11}^2 \omega_{18} - 8\omega_6^2 \omega_{11}^3 - 40\omega_6^2 \omega_{11}^2 \omega_{18} - 43\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 72\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 28v_3^2 \omega_{11}^2 \omega_{18} + 8\omega_6^2 \omega_{11}^3 + 16\omega_6^2 v_3^2 \omega_{11}^2 - 16\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 32\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 44\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 17\omega_6^2 \omega_{11}^2 \omega_{18} + 16\omega_6^2 c_s^2 \omega_{11}^3 + 44\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} + 104\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 17\omega_6^2 \omega_{11}^3 \omega_{18} - 16\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 64\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 24\omega_6 \omega_{11} \omega_{18}^2$$

$$C_{59} = 24c_s^2 \omega_7^2 v_3^2 \omega_{11}^3 - 20\omega_{19} \omega_7 v_3^2 \omega_{11}^3 + 8\omega_{19}^2 v_3^4 \omega_{11}^2 + 36\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11} - 20\omega_{19}^2 \omega_7 v_3^4 \omega_{11}^2 - 4\omega_{19}^2 c_s^2 \omega_7 \omega_{11} - 8\omega_{19} c_s^2 \omega_7^2 \omega_{11} + 4\omega_7^2 v_3^2 \omega_{11}^2 - 48\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11} + 4\omega_{19} c_s^2 \omega_{11}^2 - 8\omega_{19}^2 c_s^4 \omega_7 \omega_{11}^2 - 24\omega_{19}^2 \omega_7^2 v_3^2 + 16\omega_{19} \omega_7 v_3^2 \omega_{11}^2 - 24c_s^2 \omega_7^2 v_3^2 \omega_{11} - 4\omega_{19} c_s^4 \omega_7^2 \omega_{11} + 4c_s^2 \omega_7 \omega_{11}^2 - 84\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11} + 84\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11} - 4\omega_7^2 v_3^2 \omega_{11}^2 + 4\omega_{19} v_3^2 \omega_{11}^2 - 20\omega_{19} \omega_7^2 v_3^4 \omega_{11} + 32\omega_{19} \omega_7^2 v_3^4 \omega_{11}^2 + 8\omega_{19} v_3^2 \omega_{11}^2 + 4\omega_{19}^2 c_s^4 \omega_7 \omega_{11} - 4\omega_7^2 v_3^2 \omega_{11}^2 - 8\omega_{19} c_s^2 \omega_7^2 + 72\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11} + 8\omega_{19} c_s^4 \omega_7^2 \omega_{11} + 20\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11} + 4\omega_{19}^2 c_s^4 \omega_{11}^2 + 8\omega_{19}^2 c_s^2 \omega_7 \omega_{11} - 4c_s^4 \omega_7 \omega_{11}^2 - 13\omega_{19} \omega_7^2 v_3^4 \omega_{11} + 4\omega_{19} c_s^2 \omega_7^2 \omega_{11} - 4\omega_{19} c_s^4 \omega_7^2 \omega_{11} - 13\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11} - 4\omega_{19} c_s^4 \omega_{11}^3 - 4\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11} - 16\omega_{19} \omega_7^2 v_3^2 \omega_{11} + 4c_s^4 \omega_7^2 \omega_{11}^2 - 144\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11} + 4\omega_7^2 v_3^2 \omega_{11}^2 + 8\omega_{19} c_s^4 \omega_7 \omega_{11} + 20\omega_{19} \omega_7^2 v_3^2 \omega_{11} - 4c_s^4 \omega_7^2 \omega_{11}^2 - 72\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11} + 20\omega_{19} \omega_7^2 v_3^2 \omega_{11} - 8\omega_{19} v_3^2 \omega_{11}^2 - 36\omega_{19}^2 \omega_7^2 v_3^4 \omega_{11} + 20\omega_{19} \omega_7^2 v_3^4 \omega_{11} - 12\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11} - 4\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11} + 4\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11} - 24c_s^2 \omega_7^2 v_3^2 \omega_{11} - 4c_s^2 \omega_7^2 \omega_{11}^2 + 13\omega_{19} \omega_7^2 v_3^2 \omega_{11} + 120\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11} - 8\omega_{19} c_s^4 \omega_7^2 \omega_{11} - 36\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11} + 13\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11} + 51\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11} - 32\omega_{19} \omega_7^2 v_3^2 \omega_{11} + 4c_s^2 \omega_7^2 \omega_{11}^2 + 96\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 - 8\omega_{19} v_3^4 \omega_{11} + 12\omega_{19}^2 c_s^2 \omega_7 \omega_{11} + 24\omega_{19}^2 \omega_7^2 v_3^4 + 4\omega_7^2 v_3^2 \omega_{11} + 8\omega_{19}^2 c_s^4 \omega_7^2 - 51\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11}^3$$

$$C_{60} = 102\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11}^3 - 6\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 - 12c_s^2 \omega_7^2 v_3^2 \omega_{11}^3 + 24\omega_{19} \omega_7^2 v_3^2 \omega_{11}^3 - 24\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 - 12\omega_7^2 v_3^4 \omega_{11}^2 - 36\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11} - 90\omega_{19}^2 \omega_7^2 v_3^4 \omega_{11} - 12\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 12\omega_7^2 v_3^4 \omega_{11}^2 + 36\omega_{19} \omega_7^2 v_3^2 \omega_{11} - 306\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11} + 6\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 - 48\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11} - 12\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11}^3 + 12\omega_7^2 v_3^2 \omega_{11}^3 + 18\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 12\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 + 6\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 - 24\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 + 4\omega_{19} \omega_7^2 v_3^4 \omega_{11}^2 + 6\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 - 48\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 - 21\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 + 12\omega_{19} c_s^4 \omega_{11}^2 - 60\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 + 18\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 + 60\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 + 12\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 + 54\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 + 48\omega_{19} \omega_7^2 v_3^4 \omega_{11}^2 + 19\omega_{19}^2 \omega_7^2 v_3^4 \omega_{11}^2 - 6\omega_{19} c_s^2 \omega_7^2 \omega_{11}^3 - 18\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 - 12\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 - 72\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 - 27\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 - 12\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 - 12\omega_7^2 v_3^2 \omega_{11}^2 - 36\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 - 6\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 - 108\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 - 12\omega_7^2 v_3^4 \omega_{11}^2 + 12\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 + \omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 - 12c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 - 12\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 - 24\omega_{19} \omega_7^2 v_3^4 \omega_{11}^2 + 12\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 + 72\omega_{19}^2 \omega_7^2 v_3^4 \omega_{11}^2 + 12\omega_7^2 v_3^2 \omega_{11}^2 - 5\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 12c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 - \omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 + 252\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 - 12\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 + 90\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 + 6\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 - 19\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 - 48\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 - 81\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 - 12\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 - 12\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 12\omega_{19}^2 c_s^4 \omega_7^2 - \omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 + 12\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 - 27\omega_{19} \omega_7^2 v_3^4 \omega_{11}^2 + 162\omega_{19}^2 c_s^2 \omega_7^2 v_3^2 \omega_{11}^2 - 4\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 + 24\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 + 13\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 - 12\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^2 - 18\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 + 12\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 + 60\omega_{19} \omega_7^2 v_3^4 \omega_{11}^2 + 30\omega_{19} c_s^2 \omega_7^2 v_3^2 \omega_{11}^3$$

$$C_{61} = 68\omega_{19} \omega_7^2 v_3^2 \omega_{11}^3 - 120\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11} + 32\omega_{19}^2 c_s^2 \omega_7 \omega_{11} + 56\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 - 16\omega_7^2 v_3^2 \omega_{11}^2 - 20\omega_{19} c_s^2 \omega_{11}^3 - 12\omega_{19}^2 \omega_{11}^2 + 80\omega_{19}^2 \omega_7^2 v_3^2 - 48\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 - 16c_s^2 \omega_7 \omega_{11}^2 + 8\omega_7 \omega_{11}^2 + 16\omega_7^2 v_3^2 \omega_{11}^2 - 25\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 48\omega_{19}^2 \omega_7^2 \omega_{11}^2 - 28\omega_{19} \omega_7^2 \omega_{11}^2 - 17\omega_{19}^2 \omega_7^2 \omega_{11}^2 + 48\omega_{19}^2 c_s^2 \omega_7^2 - 44\omega_{19}^2 c_s^2 \omega_7 \omega_{11} + 16\omega_{19} \omega_7 \omega_{11} - 32\omega_{19} c_s^2 \omega_7^2 \omega_{11} + 43\omega_{19} \omega_7^2 v_3^2 \omega_{11} - 40\omega_{19} \omega_7^2 \omega_{11}^2 + 25\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 - 64\omega_{19} \omega_7^2 v_3^2 \omega_{11} + 28\omega_{19}^2 \omega_7 \omega_{11} + 17\omega_{19} \omega_7 \omega_{11}^3 - 68\omega_{19}^2 \omega_7^2 v_3^2 \omega_{11}^2 - 32\omega_{19}^2 \omega_7^2 + 64\omega_{19} \omega_7^2 v_3^2 \omega_{11} + 20\omega_{19}^2 c_s^2 \omega_{11}^2 + 16c_s^2 \omega_7^2 \omega_{11}^2 - 43\omega_{19} \omega_7^2 v_3^2 \omega_{11}^3 + 44\omega_{19} c_s^2 \omega_7 \omega_{11}^2 - 8\omega_7^2 \omega_{11}^3 - 24\omega_{19}^2 \omega_7 \omega_{11} + 104\omega_{19} \omega_7^2 v_3^2 \omega_{11}^2 - 16c_s^2 \omega_7^2 \omega_{11}^2 + 12\omega_{19} \omega_{11}^3 - 72\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11} + 24\omega_{19} \omega_7^2 \omega_{11}^2 - 16\omega_7^2 v_3^2 \omega_{11}^3 - 16\omega_{19} c_s^2 \omega_7 \omega_{11}^2 + 8\omega_7^2 \omega_{11}^2$$

$$C_{62} = 12 + 198c_s^2 \omega_{11} + 404c_s^2 v_3^2 \omega_{11}^2 + 672c_s^2 v_3^2 - 98v_3^2 \omega_{11}^2 - 34c_s^2 v_3^2 \omega_{11}^3 + 144v_3^4 + 10v_3^2 \omega_{11}^3 - 132c_s^2 + 6c_s^2 \omega_{11}^3 + 234v_3^2 \omega_{11} - 1008c_s^2 v_3^2 \omega_{11} - 78c_s^2 \omega_{11}^2 + 144c_s^4 + 8\omega_{11}^4 - 9v_3^4 \omega_{11}^3 - \omega_{11}^3 - 216c_s^4 \omega_{11} - 18\omega_{11} + 90v_3^3 \omega_{11}^2 - 216v_3^4 \omega_{11} + 82c_s^4 \omega_{11}^2 - 156v_3^2 - 5c_s^4 \omega_{11}^3$$

$$C_{63} = 12 + 54c_s^2 \omega_{11} + 252c_s^2 v_3^2 \omega_{11}^2 + 432c_s^2 v_3^2 - 154v_3^2 \omega_{11}^2 - 18c_s^2 v_3^2 \omega_{11}^3 + 504v_3^4 + 14v_3^2 \omega_{11}^3 - 36c_s^2 + 2c_s^2 \omega_{11}^3 + 378v_3^2 \omega_{11} - 648c_s^2 v_3^2 \omega_{11} - 22c_s^2 \omega_{11}^2 + 24c_s^4 + 8\omega_{11}^4 - 29v_3^4 \omega_{11}^3 - \omega_{11}^3 - 36c_s^4 \omega_{11} - 18\omega_{11} + 310v_3^3 \omega_{11}^2 - 756v_3^4 \omega_{11} + 14c_s^4 \omega_{11}^2 - 252v_3^2 - c_s^4 \omega_{11}^3$$

2.3 MRT2

2.3.1 Definitions

Collision operator C :

$$C(f) = \mathbf{M}_2^{-1} \mathbf{S} \left(\mu_2^{(eq)} - \mathbf{M}_2 f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \omega_3, \dots, \omega_{27}),$$

$$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2).$$

Matrix \mathbf{M}_2 corresponds to the transformation matrix to the raw moment basis defined by

$$\mu_2 = \begin{pmatrix} m_{(0,0,0)} \\ m_{(1,0,0)} \\ m_{(0,1,0)} \\ m_{(0,0,1)} \\ m_{(1,1,0)} \\ m_{(1,0,1)} \\ m_{(0,1,1)} \\ m_{(2,0,0)} - m_{(0,2,0)} \\ m_{(2,0,0)} - m_{(0,0,2)} \\ m_{(2,0,0)} + m_{(0,2,0)} + m_{(0,0,2)} \\ m_{(1,2,0)} + m_{(1,0,2)} \\ m_{(2,1,0)} + m_{(0,1,2)} \\ m_{(2,0,1)} + m_{(0,2,1)} \\ m_{(1,2,0)} - m_{(1,0,2)} \\ m_{(2,1,0)} - m_{(0,1,2)} \\ m_{(2,0,1)} - m_{(0,2,1)} \\ m_{(1,1,1)} \\ m_{(2,2,0)} - 2m_{(2,0,2)} + m_{(0,2,2)} \\ m_{(2,2,0)} + m_{(2,0,2)} - 2m_{(0,2,2)} \\ m_{(2,2,0)} + m_{(2,0,2)} + m_{(0,2,2)} \\ m_{(2,1,1)} \\ m_{(1,2,1)} \\ m_{(1,1,2)} \\ m_{(2,2,1)} \\ m_{(2,1,2)} \\ m_{(1,2,2)} \\ m_{(2,2,2)} \end{pmatrix}$$

and is given by

[illegible]

The equilibrium moments $\boldsymbol{\mu}_2^{(eq)}$ are defined by

$$\boldsymbol{\mu}_2^{(eq)} = \mathbf{M}_2 \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\mu}_2^{(eq)} = \begin{pmatrix} \rho \\ \rho v_1 \\ \rho v_2 \\ \rho v_3 \\ \rho v_1 v_2 \\ \rho v_1 v_3 \\ \rho v_2 v_3 \\ \rho(v_1^2 - v_2^2) \\ \rho(v_1^2 - v_3^2) \\ \rho(v_2^2 + v_3^2 + v_1^2 + 3c_s^2) \\ \rho(v_1 v_3^2 + v_1 v_2^2 + 2c_s^2 v_1) \\ \rho(v_2 v_3^2 + v_1^2 v_2 + 2c_s^2 v_2) \\ \rho(v_2^2 v_3 + v_1^2 v_3 + 2c_s^2 v_3) \\ \rho(v_1 v_2^2 - v_1 v_3^2) \\ \rho(v_1^2 v_2 - v_2 v_3^2) \\ \rho(v_1^2 v_3 - v_2^2 v_3) \\ \rho v_1 v_2 v_3 \\ \rho(v_2^2 v_3^2 - 2v_1^2 v_3^2 - c_s^2 v_3^2 + v_1^2 v_2^2 + 2c_s^2 v_2^2 - c_s^2 v_1^2) \\ \rho(-2v_2^2 v_3^2 + v_1^2 v_3^2 - c_s^2 v_3^2 + v_1^2 v_2^2 - c_s^2 v_2^2 + 2c_s^2 v_1^2) \\ \rho(v_2^2 v_3^2 + v_1^2 v_3^2 + 2c_s^2 v_3^2 + v_1^2 v_2^2 + 2c_s^2 v_2^2 + 2c_s^2 v_1^2 + 3c_s^4) \\ \rho(v_1^2 v_2 v_3 + c_s^2 v_2 v_3) \\ \rho(v_1 v_2^2 v_3 + c_s^2 v_1 v_3) \\ \rho(v_1 v_2 v_3^2 + c_s^2 v_1 v_2) \\ \rho(v_1^2 v_2^2 v_3 + c_s^2 v_2^2 v_3 + c_s^2 v_1^2 v_3 + c_s^4 v_3) \\ \rho(v_1^2 v_2 v_3^2 + c_s^2 v_2 v_3^2 + c_s^2 v_1^2 v_2 + c_s^4 v_2) \\ \rho(v_1 v_2^2 v_3^2 + c_s^2 v_1 v_3^2 + c_s^2 v_1 v_2^2 + c_s^4 v_1) \\ \rho(v_1^2 v_2^2 v_3^2 + c_s^2 v_2^2 v_3^2 + c_s^2 v_1^2 v_3^2 + c_s^4 v_3^2 + c_s^2 v_1^2 v_2^2 + c_s^4 v_2^2 + c_s^4 v_1^2 + c_s^6) \end{pmatrix}.$$

2.3.2 Conservation of mass: ρ



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$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{v_1 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\ & \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + v_3^2 + 3c_s^2) \frac{v_3 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\ & + (24c_s^2 v_1^2 + 6v_1^4 + 3v_1^2 \omega_9 - 2c_s^2 + c_s^2 \omega_9 - 3v_1^4 \omega_9 + 2c_s^4 - 12c_s^2 v_1^2 \omega_9 - 6v_1^2 - c_s^4 \omega_9) \frac{\delta_l^4}{24 \delta_t \omega_9} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 - 5v_1^2 \omega_9 + 6c_s^2 - 3c_s^2 \omega_9 + 10v_1^2 + 2\omega_9) \frac{\rho v_1 \delta_l^4}{12 \delta_t \omega_9} \frac{\partial^4 v_1}{\partial x_1^4} + \\ & (-\omega_{12} + \omega_{12} v_1^2 - v_1^2 \omega_9 - 3c_s^2 \omega_9 + 3\omega_{12} c_s^2 + \omega_9) \frac{v_1 v_2 \delta_l^4}{4 \omega_{12} \delta_t \omega_9} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\ & (-\omega_{12} + 3\omega_{12} v_1^2 - 3v_1^2 \omega_9 - c_s^2 \omega_9 + \omega_{12} c_s^2 + \omega_9) \frac{\rho v_2 \delta_l^4}{4 \omega_{12} \delta_t \omega_9} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + (-\omega_{12} \omega_5 + 3\omega_{12} c_s^2 \omega_5 \omega_9 + 3\omega_5 \omega_9 - 3v_1^2 \omega_5 \omega_9 - \end{aligned}$$

$$\begin{aligned}
& 6\omega_{12}c_s^2\omega_9 + \omega_{12}v_1^2\omega_5 - 3c_s^2\omega_5\omega_9 - \omega_{12}\omega_5\omega_9 + \omega_{12}v_1^2\omega_5\omega_9 + 3\omega_{12}c_s^2\omega_5) \frac{\rho v_1 \delta_l^4}{12\omega_{12}\delta_t\omega_5\omega_9} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_5) \frac{c_s^4 \delta_l^4}{6\delta_t\omega_5} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} \\
& + (-\omega_{12} + \omega_5) \frac{c_s^2 \rho v_1 \delta_l^4}{2\omega_{12}\delta_t\omega_5} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + (\omega_5 - \omega_{15}) \frac{c_s^2 \rho v_2 \delta_l^4}{2\delta_t\omega_5\omega_{15}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\
& (-\omega_{10}v_2^2 - 3c_s^2\omega_{10} + 3c_s^2\omega_{15} + \omega_{10} + v_2^2\omega_{15} - \omega_{15}) \frac{v_1 v_2 \delta_l^4}{4\delta_t\omega_{10}\omega_{15}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + (3\omega_{10}\omega_5 - \omega_5\omega_{15} + 3c_s^2\omega_{10}\omega_5\omega_{15} + \\
& 3c_s^2\omega_5\omega_{15} + v_2^2\omega_5\omega_{15} - 3\omega_{10}v_2^2\omega_5 - 6c_s^2\omega_{10}\omega_{15} - 3c_s^2\omega_{10}\omega_5 - \omega_{10}\omega_5\omega_{15} + \omega_{10}v_2^2\omega_5\omega_{15}) \frac{\rho v_2 \delta_l^4}{12\delta_t\omega_{10}\omega_5\omega_{15}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-3\omega_{10}v_2^2 - c_s^2\omega_{10} + c_s^2\omega_{15} + \omega_{10} + 3v_2^2\omega_{15} - \omega_{15}) \frac{\rho v_1 \delta_l^4}{4\delta_t\omega_{10}\omega_{15}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\
& (3\omega_{10}v_2^2 + 6v_2^4 + 24c_s^2v_2^2 + c_s^2\omega_{10} - 2c_s^2 - c_s^4\omega_{10} + 2c_s^4 - 3\omega_{10}v_2^4 - 6v_2^2 - 12c_s^2\omega_{10}v_2^2) \frac{\delta_l^4}{24\delta_t\omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 - 5\omega_{10}v_2^2 - 3c_s^2\omega_{10} + 6c_s^2 + 2\omega_{10} + 10v_2^2) \frac{\rho v_2 \delta_l^4}{12\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (3c_s^2\omega_{13} - v_1^2\omega_9 - 3c_s^2\omega_9 - \omega_{13} + \omega_{13}v_1^2 + \omega_9) \frac{v_3 v_1 \delta_l^4}{4\delta_t\omega_{13}\omega_9} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& (c_s^2\omega_{13} - 3v_1^2\omega_9 - c_s^2\omega_9 - \omega_{13} + 3\omega_{13}v_1^2 + \omega_9) \frac{v_3 \rho \delta_l^4}{4\delta_t\omega_{13}\omega_9} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + (-\omega_6\omega_{13} + \omega_6\omega_{13}v_1^2\omega_9 + 3\omega_6\omega_9 - \omega_6\omega_{13}\omega_9 + \\
& 3\omega_6c_s^2\omega_{13} - 3\omega_6v_1^2\omega_9 - 3\omega_6c_s^2\omega_9 + \omega_6\omega_{13}v_1^2 - 6c_s^2\omega_{13}\omega_9 + 3\omega_6c_s^2\omega_{13}\omega_9) \frac{\rho v_1 \delta_l^4}{12\omega_6\delta_t\omega_{13}\omega_9} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-\omega_8 + \omega_5) \frac{v_3 c_s^2 \rho \delta_l^4}{2\delta_t\omega_8\omega_5} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + (\omega_6 - \omega_8) \frac{c_s^2 \rho v_2 \delta_l^4}{2\omega_6\delta_t\omega_8} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + (-\omega_8 + \omega_5) \frac{v_3 c_s^2 \rho \delta_l^4}{2\delta_t\omega_8\omega_5} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (\omega_7 - \omega_8) \frac{c_s^2 \rho v_1 \delta_l^4}{2\delta_t\omega_7\omega_8} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (-\omega_{10}v_2^2 + 3c_s^2\omega_{16} - 3c_s^2\omega_{10} + \omega_{16}v_2^2 - \omega_{16} + \omega_{10}) \frac{v_3 v_2 \delta_l^4}{4\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 \rho}{\partial x_3^3 \partial x_3} + \\
& (-3\omega_{10}v_2^2 + c_s^2\omega_{16} - c_s^2\omega_{10} + 3\omega_{16}v_2^2 - \omega_{16} + \omega_{10}) \frac{v_3 \rho \delta_l^4}{4\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 v_2}{\partial x_3^3 \partial x_3} + (-\omega_{16}\omega_7 + \omega_{16}\omega_{10}\omega_7v_2^2 + 3\omega_{10}\omega_7 + \\
& 3c_s^2\omega_{16}\omega_{10}\omega_7 + \omega_{16}\omega_7v_2^2 + 3c_s^2\omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7 - 3c_s^2\omega_{10}\omega_7 - 6c_s^2\omega_{16}\omega_{10} - 3\omega_{10}\omega_7v_2^2) \frac{\rho v_2 \delta_l^4}{12\delta_t\omega_{16}\omega_{10}\omega_7} \frac{\partial^4 v_3}{\partial x_3^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{c_s^4 \delta_l^4}{6\omega_6\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (\omega_6 - \omega_{13}) \frac{c_s^2 \rho v_1 \delta_l^4}{2\omega_6\delta_t\omega_{13}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + (\omega_6 - \omega_{18}) \frac{v_3 c_s^2 \rho \delta_l^4}{2\omega_6\delta_t\omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + (\omega_6 - \omega_8) \frac{c_s^2 \rho v_2 \delta_l^4}{2\omega_6\delta_t\omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (\omega_7 - \omega_8) \frac{c_s^2 \rho v_1 \delta_l^4}{2\delta_t\omega_7\omega_8} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + (-2 + \omega_7) \frac{c_s^4 \delta_l^4}{6\delta_t\omega_7} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + (-\omega_{16} + \omega_7) \frac{c_s^2 \rho v_2 \delta_l^4}{2\delta_t\omega_{16}\omega_7} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + (-\omega_{19} + \omega_7) \frac{v_3 c_s^2 \rho \delta_l^4}{2\omega_{19}\delta_t\omega_7} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} \\
& + (-v_3^2\omega_{11} + 3c_s^2\omega_{18} - 3c_s^2\omega_{11} + \omega_{11} + v_3^2\omega_{18} - \omega_{18}) \frac{v_3 v_1 \delta_l^4}{4\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + (-3\omega_6c_s^2\omega_{11} + \omega_6v_3^2\omega_{18} - \omega_6\omega_{18} + \\
& \omega_6v_3^2\omega_{11}\omega_{18} - \omega_6\omega_{11}\omega_{18} + 3\omega_6\omega_{11} - 3\omega_6v_3^2\omega_{11} - 6c_s^2\omega_{11}\omega_{18} + 3\omega_6c_s^2\omega_{11}\omega_{18} + 3\omega_6c_s^2\omega_{18}) \frac{v_3 \rho \delta_l^4}{12\omega_6\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (-3v_3^2\omega_{11} + c_s^2\omega_{18} - c_s^2\omega_{11} + \omega_{11} + 3v_3^2\omega_{18} - \omega_{18}) \frac{\rho v_1 \delta_l^4}{4\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (v_3^2\omega_{19} - \omega_{19} - v_3^2\omega_{11} + 3\omega_{19}c_s^2 - 3c_s^2\omega_{11} + \omega_{11}) \frac{v_3 v_2 \delta_l^4}{4\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + (v_3^2\omega_{19}\omega_7\omega_{11} - 3c_s^2\omega_7\omega_{11} + 3\omega_{19}c_s^2\omega_7 + \\
& v_3^2\omega_{19}\omega_7 - \omega_{19}\omega_7\omega_{11} - 3v_3^2\omega_7\omega_{11} - \omega_{19}\omega_7 + 3\omega_{19}c_s^2\omega_7\omega_{11} + 3\omega_7\omega_{11} - 6\omega_{19}c_s^2\omega_{11}) \frac{v_3 \rho \delta_l^4}{12\omega_{19}\delta_t\omega_7\omega_{11}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (3v_3^2\omega_{19} - \omega_{19} - 3v_3^2\omega_{11} + \omega_{19}c_s^2 - c_s^2\omega_{11} + \omega_{11}) \frac{\rho v_2 \delta_l^4}{4\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& (-6v_3^2 - c_s^4\omega_{11} - 2c_s^2 + 3v_3^2\omega_{11} + 24v_3^2c_s^2 + c_s^2\omega_{11} + 2c_s^4 - 12v_3^2c_s^2\omega_{11} - 3v_3^4\omega_{11} + 6v_3^4) \frac{\delta_l^4}{24\delta_t\omega_{11}} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 10v_3^2 + 6c_s^2 - 5v_3^2\omega_{11} - 3c_s^2\omega_{11} + 2\omega_{11}) \frac{v_3 \rho \delta_l^4}{12\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.3.3 Conservation of momentum: ρv_1



attached text file: output_d3q27_nse_mrt2_symbolic_pde_01.txt

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho v_1 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 - 3v_1^2\omega_9 + 4c_s^2 - 2c_s^2\omega_9 + 6v_1^2 + \omega_9) \frac{\delta_l^2}{\delta_t\omega_9} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\rho v_1 \delta_l^2}{\delta_t\omega_9} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{c_s^2 \delta_l^2}{2\delta_t\omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{c_s^2 \delta_l^2}{2\delta_t\omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 - v_1^2\omega_9 + 6c_s^2 - 3c_s^2\omega_9 + 2v_1^2 + \omega_9) \frac{v_1 \delta_l^2}{2\delta_t\omega_9} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 - 3v_1^2\omega_9 + 2c_s^2 - c_s^2\omega_9 + 6v_1^2 + \omega_9) \frac{\rho \delta_l^2}{2\delta_t\omega_9} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{c_s^2 \rho \delta_l^2}{2\delta_t\omega_5} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{c_s^2 \rho \delta_l^2}{2\delta_t\omega_5} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\delta_t\omega_9^2} \frac{\partial^3 \rho}{\partial x_1^3} +
\end{aligned}$$

$$\begin{aligned}
& (-24 + 5c_s^2\omega_9^2 - 60v_1^2\omega_9 + 36c_s^2 - 36c_s^2\omega_9 + 11v_1^2\omega_9^2 - 4\omega_9^2 + 60v_1^2 + 24\omega_9) \frac{\rho v_1 \delta_l^3}{6\delta_t \omega_9^2} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{v_1 v_2 \delta_l^3}{\omega_{12} \delta_t \omega_5 \omega_9^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\
& C_3 \frac{\rho v_2 \delta_l^3}{\omega_{12} \delta_t \omega_5 \omega_9^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + C_4 \frac{\rho v_1 \delta_l^3}{12\omega_{12} \delta_t \omega_5^2 \omega_9^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_5^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\
& (-12\omega_{12}\omega_5 + 12\omega_5\omega_9 - 12\omega_{12}\omega_9 - \omega_{12}\omega_5^2\omega_9 + 12\omega_{12}\omega_5\omega_9 - 12\omega_5^2\omega_9 + 12\omega_5^2) \frac{c_s^2 \rho v_1 \delta_l^3}{6\omega_{12} \delta_t \omega_5^2 \omega_9} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (\omega_5\omega_{15} - \omega_5^2 + 2\omega_5 - 2\omega_{15}) \frac{c_s^2 \rho v_2 \delta_l^3}{\delta_t \omega_5^2 \omega_{15}} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_5 \frac{v_1 v_2 \delta_l^3}{12\delta_t \omega_{10} \omega_5 \omega_{15}} \frac{\partial^3 \rho}{\partial x_2^3} + C_6 \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_5^2 \omega_{15}} \frac{\partial^3 v_1}{\partial x_2^3} + C_7 \frac{\rho v_1 \delta_l^3}{12\delta_t \omega_{10} \omega_5 \omega_{15}} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& C_8 \frac{v_3 v_1 \delta_l^3}{\omega_6 \delta_t \omega_{13} \omega_9^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + C_9 \frac{v_3 \rho \delta_l^3}{\omega_6 \delta_t \omega_{13} \omega_9^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + C_{10} \frac{\rho v_1 \delta_l^3}{12\omega_6^2 \delta_t \omega_{13} \omega_9^2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (\omega_6\omega_5 + \omega_6\omega_8\omega_5 - \omega_6\omega_5^2 - \omega_8\omega_5 + \omega_5^2 - \omega_6\omega_8) \frac{v_3 c_s^2 \rho \delta_l^3}{\omega_6 \delta_t \omega_8 \omega_5^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\
& (\omega_6\omega_5 + \omega_6\omega_8\omega_5 + \omega_6^2 - \omega_8\omega_5 - \omega_6\omega_8 - \omega_6^2\omega_5) \frac{c_s^2 \rho v_2 \delta_l^3}{\omega_6^2 \delta_t \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + \\
& (\omega_6\omega_5 + \omega_6\omega_8\omega_5 - \omega_6\omega_5^2 - \omega_8\omega_5 + \omega_5^2 - \omega_6\omega_8) \frac{v_3 c_s^2 \rho \delta_l^3}{\omega_6 \delta_t \omega_8 \omega_5^2} \frac{\partial^3 v_1}{\partial x_2^2 \partial x_3} + \\
& (6\omega_6\omega_8\omega_5 + 6\omega_6\omega_7 + 6\omega_7\omega_5 - 6\omega_8\omega_5 - \omega_6\omega_7\omega_8\omega_5 - 6\omega_6\omega_7\omega_5 - 6\omega_6\omega_8) \frac{c_s^2 \rho v_1 \delta_l^3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4 \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + \\
& (-12\omega_{13}\omega_9 - 12\omega_6\omega_{13} + 12\omega_6^2 - \omega_6^2\omega_{13}\omega_9 + 12\omega_6\omega_9 + 12\omega_6\omega_{13}\omega_9 - 12\omega_6^2\omega_9) \frac{c_s^2 \rho v_1 \delta_l^3}{6\omega_6^2 \delta_t \omega_{13} \omega_9} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
& (2\omega_6 - \omega_6^2 + \omega_6\omega_{18} - 2\omega_{18}) \frac{v_3 c_s^2 \rho \delta_l^3}{\omega_6^2 \delta_t \omega_{18}} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + (\omega_6\omega_5 + \omega_6\omega_8\omega_5 + \omega_6^2 - \omega_8\omega_5 - \omega_6\omega_8 - \omega_6^2\omega_5) \frac{c_s^2 \rho v_2 \delta_l^3}{\omega_6^2 \delta_t \omega_8 \omega_5} \frac{\partial^3 v_1}{\partial x_2 \partial x_3^2} + \\
& (6\omega_6\omega_8\omega_5 + 6\omega_6\omega_7 + 6\omega_7\omega_5 - 6\omega_8\omega_5 - \omega_6\omega_7\omega_8\omega_5 - 6\omega_6\omega_7\omega_5 - 6\omega_6\omega_8) \frac{c_s^2 \rho v_1 \delta_l^3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{11} \frac{v_3 v_1 \delta_l^3}{12\omega_6 \delta_t \omega_{11} \omega_{18}} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& + C_{12} \frac{v_3 \rho \delta_l^3}{6\omega_6^2 \delta_t \omega_{18}} \frac{\partial^3 v_1}{\partial x_3^3} + C_{13} \frac{\rho v_1 \delta_l^3}{12\omega_6 \delta_t \omega_{11} \omega_{18}} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{v_1 \delta_l^4}{12\delta_t \omega_9^3} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\rho \delta_l^4}{12\delta_t \omega_9^3} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{v_2 \delta_l^4}{4\omega_{12}^2 \delta_t \omega_5^2 \omega_9^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_{17} \frac{\rho v_1 v_2 \delta_l^4}{4\omega_{12}^2 \delta_t \omega_5^2 \omega_9^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{18} \frac{\rho \delta_l^4}{12\omega_{12}^2 \delta_t \omega_5^2 \omega_9^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_1 \delta_l^4}{12\omega_{12}^2 \delta_t \omega_5^2 \omega_{21} \omega_{15} \omega_9^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{20} \frac{\rho \delta_l^4}{12\omega_{12}^2 \delta_t \omega_5^2 \omega_{21} \omega_{15} \omega_9^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& C_{21} \frac{\rho v_1 v_2 \delta_l^4}{2\omega_{12}^2 \delta_t \omega_{10} \omega_5^2 \omega_{21} \omega_{15} \omega_9^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_2 \delta_l^4}{12\omega_{12} \delta_t \omega_{10}^2 \omega_5^2 \omega_{21} \omega_{15} \omega_9} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + C_{23} \frac{\rho v_1 v_2 \delta_l^4}{12\omega_{12}^2 \delta_t \omega_{10}^2 \omega_5^2 \omega_{21} \omega_{15} \omega_9^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
& C_{24} \frac{\rho \delta_l^4}{12\omega_{12} \delta_t \omega_{10}^2 \omega_5^2 \omega_{21} \omega_{15} \omega_9} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{25} \frac{v_1 \delta_l^4}{24\delta_t \omega_{10}^2 \omega_5^2 \omega_{15}} \frac{\partial^4 \rho}{\partial x_2^4} + C_{26} \frac{\rho \delta_l^4}{24\delta_t \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_1}{\partial x_2^4} + C_{27} \frac{\rho v_1 v_2 \delta_l^4}{12\delta_t \omega_{10}^2 \omega_5^2 \omega_{15}} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& C_{28} \frac{v_3 \delta_l^4}{4\omega_6^2 \delta_t \omega_{13}^2 \omega_9^3} \frac{\partial^4 \rho}{\partial x_3^4} + C_{29} \frac{v_3 \rho v_1 \delta_l^4}{4\omega_6^2 \delta_t \omega_{13}^2 \omega_9^3} \frac{\partial^4 v_1}{\partial x_3^4} + C_{30} \frac{\rho \delta_l^4}{12\omega_6^2 \delta_t \omega_{13}^2 \omega_9^3} \frac{\partial^4 v_3}{\partial x_3^4} + C_{31} \frac{v_3 v_1 v_2 \delta_l^4}{\omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{32} \frac{v_3 \rho v_2 \delta_l^4}{\omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{33} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{34} \frac{\rho v_1 v_2 \delta_l^4}{2\omega_{12}^2 \omega_6^2 \delta_t \omega_{13}^2 \omega_{14} \omega_8 \omega_5^2 \omega_9^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& + C_{35} \frac{2v_3 c_s^4 \delta_l^4}{\omega_6^2 \delta_t \omega_8 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{36} \frac{v_3 c_s^2 \rho v_1 \delta_l^4}{2\omega_{12}^2 \omega_6^2 \delta_t \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{37} \frac{v_3 c_s^2 \rho v_2 \delta_l^4}{\omega_6^2 \delta_t \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{38} \frac{c_s^2 \rho \delta_l^4}{12\omega_{12} \omega_6^3 \delta_t \omega_{13} \omega_{14} \omega_8 \omega_5^3 \omega_{15} \omega_9} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{39} \frac{v_3 v_1 v_2 \delta_l^4}{4\omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{40} \frac{v_3 \rho v_2 \delta_l^4}{2\omega_6^2 \delta_t \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2} \frac{\partial^4 v_1}{\partial x_2^3 \partial x_3} + \\
& C_{41} \frac{v_3 \rho v_1 \delta_l^4}{4\omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{42} \frac{\rho v_1 v_2 \delta_l^4}{12\omega_6^2 \delta_t \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{43} \frac{v_1 \delta_l^4}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{18} \omega_9^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_{44} \frac{\rho \delta_l^4}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{18} \omega_9^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{45} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11} \omega_{18} \omega_9^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{46} \frac{\delta_l^4}{2\omega_{12} \omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5^2 \omega_{18} \omega_9} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{47} \frac{\rho \delta_l^4}{2\omega_{12} \omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5^2 \omega_{18} \omega_9} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{48} \frac{\rho \delta_l^4}{12\omega_{12} \omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5^2 \omega_{18} \omega_9} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{49} \frac{v_3 \rho \delta_l^4}{\omega_{12} \omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5^2 \omega_{18} \omega_9} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{50} \frac{\delta_l^4}{12\omega_6^2 \delta_t \omega_{17} \omega_{20} \omega_{17} \omega_8 \omega_5^2 \omega_{18} \omega_{15}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{51} \frac{\rho \delta_l^4}{4\omega_6^3 \delta_t \omega_{20} \omega_{17} \omega_8 \omega_5^3 \omega_{18} \omega_{15}} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + C_{52} \frac{\rho v_2 \delta_l^4}{2\omega_6^2 \delta_t \omega_{16} \omega_{10} \omega_7 \omega_{20} \omega_{17} \omega_8 \omega_5^2 \omega_{18} \omega_{15}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{53} \frac{\rho \delta_l^4}{4\omega_6^2 \omega_{19} \delta_t \omega_{17} \omega_{20} \omega_{17} \omega_{11} \omega_8 \omega_5^2 \omega_{18} \omega_{15}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{54} \frac{v_3 \delta_l^4}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2 \omega_{18} \omega_9} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2 \omega_{18} \omega_9} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& C_{56} \frac{\rho \delta_l^4}{12\omega_6^3 \omega_{22} \delta_t \omega_{13} \omega_{11}^2 \omega_{18} \omega_9} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{57} \frac{v_3 v_1 v_2 \delta_l^4}{4\omega_6^2 \omega_{19} \delta_t \omega_{17} \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{58} \frac{v_3 \rho v_2 \delta_l^4}{2\omega_6^2 \delta_t \omega_{20} \omega_8 \omega_5^2 \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} + \\
& C_{59} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_6^2 \omega_{19} \delta_t \omega_{17} \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{60} \frac{\rho v_1 v_2 \delta_l^4}{4\omega_6^2 \omega_{19} \delta_t \omega_{17} \omega_{20} \omega_{11}^2 \omega_8 \omega_5^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{v_1 \delta_l^4}{24\omega_6^2 \delta_t \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{62} \frac{\rho \delta_l^4}{24\omega_6^3 \delta_t \omega_{18}^2} \frac{\partial^4 v_1}{\partial x_3^4} + C_{63} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_6^2 \delta_t \omega_{11}^2 \omega_{18}^2} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$C_1 = 144c_s^2v_1^2 - c_s^2\omega_9^2 + 36v_1^4 + 36v_1^2\omega_9 - 12c_s^2 + 12c_s^2\omega_9 - 7v_1^2\omega_9^2 + c_s^4\omega_9^2 - 36v_1^4\omega_9 + 24c_s^2v_1^2\omega_9^2 + 12c_s^4 - 144c_s^2v_1^2\omega_9 - 36v_1^2 - 12c_s^4\omega_9 + 7v_1^4\omega_9^2$$

$$\begin{aligned}
C_2 &= v_1^2 \omega_5 \omega_9^2 - 3c_s^2 \omega_9^2 - \omega_{12} \omega_5 - \omega_5 \omega_9^2 - 3\omega_{12} c_s^2 \omega_5 \omega_9 + \omega_5 \omega_9 - v_1^2 \omega_9^2 - \omega_{12} \omega_9 - v_1^2 \omega_5 \omega_9 + 3\omega_{12} c_s^2 \omega_9 + \omega_{12} v_1^2 \omega_5 - 3c_s^2 \omega_5 \omega_9 + \omega_{12} \omega_5 \omega_9 - \\
&\omega_{12} v_1^2 \omega_5 \omega_9 + \omega_9^2 + 3\omega_{12} c_s^2 \omega_5 + \omega_{12} v_1^2 \omega_9 + 3c_s^2 \omega_5 \omega_9^2 \\
C_3 &= 3v_1^2 \omega_5 \omega_9^2 - c_s^2 \omega_9^2 - \omega_{12} \omega_5 - \omega_5 \omega_9^2 - \omega_{12} c_s^2 \omega_5 \omega_9 + \omega_5 \omega_9 - 3v_1^2 \omega_9^2 - \omega_{12} \omega_9 - 3v_1^2 \omega_5 \omega_9 + \omega_{12} c_s^2 \omega_9 + 3\omega_{12} v_1^2 \omega_5 - c_s^2 \omega_5 \omega_9 + \omega_{12} \omega_5 \omega_9 - \\
&3\omega_{12} v_1^2 \omega_5 \omega_9 + \omega_9^2 + \omega_{12} c_s^2 \omega_5 + 3\omega_{12} v_1^2 \omega_9 + c_s^2 \omega_5 \omega_9^2 \\
C_4 &= -12v_1^2 \omega_5 \omega_9^2 + 3\omega_{12} \omega_5^2 \omega_9^2 + 12c_s^2 \omega_5^2 \omega_9^2 - 6\omega_{12} v_1^2 \omega_5^2 \omega_9 + 12\omega_5 \omega_9^2 - 24\omega_{12} c_s^2 \omega_5 \omega_9 + 42\omega_{12} c_s^2 \omega_5 \omega_9^2 - 12\omega_{12} \omega_5^2 - 3\omega_{12} v_1^2 \omega_5^2 \omega_9^2 - \\
&12c_s^2 \omega_5^2 \omega_9 + 6\omega_{12} \omega_5^2 \omega_9 + 36\omega_{12} c_s^2 \omega_5^2 - 12v_1^2 \omega_5^2 \omega_9 + 12\omega_5^2 \omega_9 - 11\omega_{12} c_s^2 \omega_5^2 \omega_9^2 + 6\omega_{12} v_1^2 \omega_5 \omega_9^2 - 18\omega_{12} c_s^2 \omega_5^2 \omega_9 - 12\omega_5^2 \omega_9^2 - 6\omega_{12} \omega_5 \omega_9^2 + \\
&12v_1^2 \omega_5^2 \omega_9^2 + 12\omega_{12} v_1^2 \omega_5^2 - 24\omega_{12} c_s^2 \omega_9^2 - 12c_s^2 \omega_5 \omega_9^2 \\
C_5 &= -6\omega_{10} \omega_5 - 12\omega_{10} v_2^2 - 36c_s^2 \omega_{10} + 36c_s^2 \omega_{15} + 12\omega_{10} + 12v_2^2 \omega_{15} + 6\omega_5 \omega_{15} + 3c_s^2 \omega_{10} \omega_5 \omega_{15} - 18c_s^2 \omega_5 \omega_{15} - 6v_2^2 \omega_5 \omega_{15} + 6\omega_{10} v_2^2 \omega_5 + \\
&18c_s^2 \omega_{10} \omega_5 - \omega_{10} \omega_5 \omega_{15} - 12\omega_{15} + \omega_{10} v_2^2 \omega_5 \omega_{15} \\
C_6 &= -6v_2^2 \omega_5 - 6c_s^2 \omega_5 - 12c_s^2 \omega_{15} - 3\omega_5 \omega_{15} + 3c_s^2 \omega_5^2 + 3v_2^2 \omega_5^2 - v_2^2 \omega_5^2 \omega_{15} - 3c_s^2 \omega_5^2 \omega_{15} + 15c_s^2 \omega_5 \omega_{15} + 3v_2^2 \omega_5 \omega_{15} - 3\omega_5^2 + \omega_5^2 \omega_{15} + 6\omega_5 \\
C_7 &= -6\omega_{10} \omega_5 - 36\omega_{10} v_2^2 - 12c_s^2 \omega_{10} + 12c_s^2 \omega_{15} + 12\omega_{10} + 36v_2^2 \omega_{15} + 6\omega_5 \omega_{15} + c_s^2 \omega_{10} \omega_5 \omega_{15} - 6c_s^2 \omega_5 \omega_{15} - 18v_2^2 \omega_5 \omega_{15} + 18\omega_{10} v_2^2 \omega_5 + \\
&6c_s^2 \omega_{10} \omega_5 - \omega_{10} \omega_5 \omega_{15} - 12\omega_{15} + 3\omega_{10} v_2^2 \omega_5 \omega_{15} \\
C_8 &= -\omega_6 \omega_9^2 - \omega_{13} \omega_9 - 3c_s^2 \omega_9^2 - \omega_6 \omega_{13} - \omega_6 \omega_{13} v_1^2 \omega_9 - v_1^2 \omega_9^2 + \omega_{13} v_1^2 \omega_9 + \omega_6 \omega_9 + \omega_6 \omega_{13} \omega_9 + 3\omega_6 c_s^2 \omega_{13} + 3\omega_6 c_s^2 \omega_9^2 - \omega_6 v_1^2 \omega_9 - 3\omega_6 c_s^2 \omega_9 + \\
&\omega_6 \omega_{13} v_1^2 + \omega_9^2 + \omega_6 v_1^2 \omega_9^2 + 3c_s^2 \omega_{13} \omega_9 - 3\omega_6 c_s^2 \omega_{13} \omega_9 \\
C_9 &= -\omega_6 \omega_9^2 - \omega_{13} \omega_9 - c_s^2 \omega_9^2 - \omega_6 \omega_{13} - 3\omega_6 \omega_{13} v_1^2 \omega_9 - 3v_1^2 \omega_9^2 + 3\omega_{13} v_1^2 \omega_9 + \omega_6 \omega_9 + \omega_6 \omega_{13} \omega_9 + \omega_6 c_s^2 \omega_{13} + \omega_6 c_s^2 \omega_9^2 - 3\omega_6 v_1^2 \omega_9 - \omega_6 c_s^2 \omega_9 + \\
&3\omega_6 \omega_{13} v_1^2 + \omega_9^2 + 3\omega_6 v_1^2 \omega_9^2 + c_s^2 \omega_{13} \omega_9 - \omega_6 c_s^2 \omega_{13} \omega_9 \\
C_{10} &= 12\omega_6^2 \omega_{13} v_1^2 + 12\omega_6^2 v_1^2 \omega_9^2 + 12\omega_6 \omega_9^2 - 12\omega_6^2 c_s^2 \omega_9 - 11\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 6\omega_6 \omega_{13} v_1^2 \omega_9^2 + 3\omega_6^2 \omega_{13} \omega_9^2 + 6\omega_6^2 \omega_{13} \omega_9 + 36\omega_6^2 c_s^2 \omega_{13} - \\
&18\omega_6^2 c_s^2 \omega_{13} \omega_9 - 12\omega_6^2 v_1^2 \omega_9 + 12\omega_6^2 c_s^2 \omega_9^2 + 42\omega_6 c_s^2 \omega_{13} \omega_9^2 + 12\omega_6^2 \omega_9 - 24c_s^2 \omega_{13} \omega_9^2 - 3\omega_6^2 \omega_{13} v_1^2 \omega_9^2 - 12\omega_6 c_s^2 \omega_9^2 - 12\omega_6 v_1^2 \omega_9^2 - 12\omega_6^2 \omega_{13} - \\
&6\omega_6^2 \omega_{13} v_1^2 \omega_9 - 12\omega_6^2 \omega_9^2 - 24\omega_6 c_s^2 \omega_{13} \omega_9 - 6\omega_6 \omega_{13} \omega_9^2 \\
C_{11} &= 18\omega_6 c_s^2 \omega_{11} - 6\omega_6 v_3^2 \omega_{18} + 6\omega_6 \omega_{18} - 12v_3^2 \omega_{11} + \omega_6 v_3^2 \omega_{11} \omega_{18} + 36c_s^2 \omega_{18} - \omega_6 \omega_{11} \omega_{18} - 36c_s^2 \omega_{11} + 12\omega_{11} + 12v_3^2 \omega_{18} - 6\omega_6 \omega_{11} + \\
&6\omega_6 v_3^2 \omega_{11} - 12\omega_{18} + 3\omega_6 c_s^2 \omega_{11} \omega_{18} - 18\omega_6 c_s^2 \omega_{18} \\
C_{12} &= 3\omega_6^2 v_3^2 + 6\omega_6 - 3\omega_6^2 + 3\omega_6 v_3^2 \omega_{18} - 3\omega_6^2 c_s^2 \omega_{18} - 3\omega_6 \omega_{18} + 3\omega_6^2 c_s^2 - 12c_s^2 \omega_{18} - 6\omega_6 c_s^2 + \omega_6^2 \omega_{18} - 6\omega_6 v_3^2 + 15\omega_6 c_s^2 \omega_{18} - \omega_6^2 v_3^2 \omega_{18} \\
C_{13} &= 6\omega_6 c_s^2 \omega_{11} - 18\omega_6 v_3^2 \omega_{18} + 6\omega_6 \omega_{18} - 36v_3^2 \omega_{11} + 3\omega_6 v_3^2 \omega_{11} \omega_{18} + 12c_s^2 \omega_{18} - \omega_6 \omega_{11} \omega_{18} - 12c_s^2 \omega_{11} + 12\omega_{11} + 36v_3^2 \omega_{18} - 6\omega_6 \omega_{11} + \\
&18\omega_6 v_3^2 \omega_{11} - 12\omega_{18} + \omega_6 c_s^2 \omega_{11} \omega_{18} - 6\omega_6 c_s^2 \omega_{18} \\
C_{14} &= 12 + 6c_s^2 \omega_9^3 + 672c_s^2 v_1^2 - 78c_s^2 \omega_9^2 + 144v_1^4 + 234v_1^2 \omega_9 - 132c_s^2 + 198c_s^2 \omega_9 - 98v_1^2 \omega_9^2 + 10v_1^2 \omega_9^3 + 82c_s^4 \omega_9^2 - 216v_1^4 \omega_9 + 404c_s^2 v_1^2 \omega_9^2 + \\
&144c_s^4 - 5c_s^4 \omega_9^3 - 34c_s^2 v_1^2 \omega_9^3 + 8\omega_9^2 - 9v_1^4 \omega_9^3 - \omega_9^3 - 1008c_s^2 v_1^2 \omega_9 - 156v_1^2 - 216c_s^4 \omega_9 - 18\omega_9 + 90v_1^4 \omega_9^2 \\
C_{15} &= 12 + 2c_s^2 \omega_9^3 + 432c_s^2 v_1^2 - 22c_s^2 \omega_9^2 + 504v_1^4 + 378v_1^2 \omega_9 - 36c_s^2 + 54c_s^2 \omega_9 - 154v_1^2 \omega_9^2 + 14v_1^2 \omega_9^3 + 14c_s^4 \omega_9^2 - 756v_1^4 \omega_9 + 252c_s^2 v_1^2 \omega_9^2 + 24c_s^4 - \\
&c_s^4 \omega_9^3 - 18c_s^2 v_1^2 \omega_9^3 + 8\omega_9^2 - 29v_1^4 \omega_9^3 - \omega_9^3 - 648c_s^2 v_1^2 \omega_9 - 252v_1^2 - 36c_s^4 \omega_9 - 18\omega_9 + 310v_1^4 \omega_9^2 \\
C_{16} &= -36\omega_{12} c_s^2 v_1^2 \omega_9^3 + 120\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^2 - 12\omega_{12}^2 c_s^4 \omega_5^2 \omega_9 - 8\omega_{12} v_1^4 \omega_9^3 + 32\omega_{12} v_1^4 \omega_5^2 \omega_9^2 + 4c_s^2 \omega_5^2 \omega_9^2 + 20\omega_{12}^2 v_1^4 \omega_5 \omega_9 - 51\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^3 + \\
&4v_1^2 \omega_5 \omega_9^3 + 20\omega_{12} v_1^2 \omega_5^2 \omega_9 + 20\omega_{12}^2 v_1^2 \omega_5 \omega_9^2 + 8\omega_{12} c_s^4 \omega_5 \omega_9^3 - 24\omega_{12}^2 v_1^2 \omega_5^2 - 4\omega_{12}^2 c_s^2 \omega_9^2 - 4c_s^2 \omega_5^2 \omega_9^3 - 4\omega_{12}^2 c_s^2 \omega_5^2 \omega_9^2 - 13\omega_{12} v_1^4 \omega_5^2 \omega_9^3 + 51\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^2 + \\
&12\omega_{12}^2 c_s^2 \omega_5^2 \omega_9 - 8\omega_{12}^2 v_1^2 \omega_9^2 - 144\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9 - 8\omega_{12}^2 c_s^2 \omega_5^2 + 24c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 32\omega_{12} v_1^2 \omega_5^2 \omega_9^2 - 20\omega_{12}^2 v_1^2 \omega_5 \omega_9 - 4c_s^4 \omega_5^2 \omega_9^2 - 20\omega_{12} v_1^4 \omega_5^2 \omega_9 - \\
&4v_1^4 \omega_5 \omega_9^3 - 8\omega_{12} c_s^2 \omega_5 \omega_9^3 - 20\omega_{12}^2 v_1^4 \omega_5 \omega_9^2 + 4c_s^4 \omega_5^2 \omega_9^3 - 4\omega_{12} c_s^4 \omega_9^3 + 13\omega_{12} v_1^2 \omega_5^2 \omega_9^3 + 4\omega_{12}^2 c_s^4 \omega_5^2 \omega_9^2 - 24c_s^2 v_1^2 \omega_5^2 \omega_9^2 - 72\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9 + \\
&4v_1^4 \omega_5^2 \omega_9^3 + 13\omega_{12} v_1^4 \omega_5^2 \omega_9 + 4\omega_{12} c_s^2 \omega_5^2 \omega_9^3 - 4c_s^4 \omega_5 \omega_9^3 - 4\omega_{12} c_s^4 \omega_5^2 \omega_9 + 4\omega_{12}^2 c_s^4 \omega_9^2 + 24\omega_{12}^2 v_1^4 \omega_5^2 - 8\omega_{12}^2 c_s^4 \omega_5 \omega_9^2 - 20\omega_{12} v_1^2 \omega_5 \omega_9^3 - 8\omega_{12} c_s^2 \omega_5^2 \omega_9^2 - \\
&4v_1^4 \omega_5^2 \omega_9^2 + 72\omega_{12} c_s^2 v_1^2 \omega_5 \omega_9 + 8\omega_{12} v_1^2 \omega_9^3 - 4\omega_{12}^2 c_s^2 \omega_5 \omega_9 + 16\omega_{12} v_1^2 \omega_5 \omega_9^2 - 24c_s^2 v_1^2 \omega_5 \omega_9^3 + 36\omega_{12}^2 c_s^2 v_1^2 \omega_9^2 + 36\omega_{12} v_1^2 \omega_5^2 \omega_9 - 4v_1^2 \omega_5^2 \omega_9^3 + \\
&84\omega_{12} c_s^2 v_1^2 \omega_5 \omega_9^3 - 4\omega_{12} c_s^4 \omega_5^2 \omega_9^3 + 96\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 - 13\omega_{12}^2 v_1^2 \omega_5^2 \omega_9^2 + 4\omega_{12} c_s^2 \omega_5^2 \omega_9 + 4c_s^2 \omega_5 \omega_9^3 + 4\omega_{12} c_s^2 \omega_9^3 + 20\omega_{12} v_1^4 \omega_5 \omega_9^3 - 84\omega_{12}^2 c_s^2 v_1^2 \omega_5 \omega_9^2 + \\
&8\omega_{12}^2 c_s^2 \omega_5 \omega_9^2 + 8\omega_{12} c_s^4 \omega_5^2 \omega_9^2 - 48\omega_{12} c_s^2 v_1^2 \omega_5 \omega_9^2 + 4\omega_{12}^2 c_s^4 \omega_5 \omega_9 + 8\omega_{12}^2 c_s^4 \omega_5^2 + 8\omega_{12}^2 v_1^4 \omega_9^2 + 4v_1^2 \omega_5^2 \omega_9^2 - 16\omega_{12} v_1^4 \omega_5 \omega_9^2 - 36\omega_{12}^2 v_1^4 \omega_5^2 \omega_9 \\
C_{17} &= 12\omega_{12} \omega_9^3 - 40\omega_{12} \omega_5^2 \omega_9^2 + 8\omega_5 \omega_9^3 - 16c_s^2 \omega_5^2 \omega_9^2 + 17\omega_{12} \omega_5^2 \omega_9^3 + 28\omega_{12}^2 \omega_5 \omega_9^2 - 16v_1^2 \omega_5 \omega_9^3 - 64\omega_{12} v_1^2 \omega_5^2 \omega_9 - 68\omega_{12}^2 v_1^2 \omega_5 \omega_9^2 + 80\omega_{12}^2 v_1^2 \omega_5^2 + \\
&20\omega_{12}^2 c_s^2 \omega_9^2 + 16c_s^2 \omega_5^2 \omega_9^3 + 25\omega_{12}^2 c_s^2 \omega_5^2 \omega_9^2 - 16\omega_{12} c_s^2 \omega_5 \omega_9^2 - 72\omega_{12}^2 c_s^2 \omega_5^2 \omega_9 + 28\omega_{12}^2 v_1^2 \omega_9^2 + 48\omega_{12}^2 c_s^2 \omega_5^2 + 104\omega_{12} v_1^2 \omega_5^2 \omega_9^2 - 24\omega_{12}^2 \omega_5 \omega_9 + \\
&64\omega_{12}^2 v_1^2 \omega_5 \omega_9 + 44\omega_{12} c_s^2 \omega_5 \omega_9^3 - 43\omega_{12} v_1^2 \omega_5^2 \omega_9^3 + 24\omega_{12} \omega_5^2 \omega_9 - 25\omega_{12} c_s^2 \omega_5^2 \omega_9^3 + 68\omega_{12} v_1^2 \omega_5 \omega_9^3 + 56\omega_{12} c_s^2 \omega_5^2 \omega_9^2 - 28\omega_{12} v_1^2 \omega_9^3 + 32\omega_{12}^2 c_s^2 \omega_5 \omega_9 - \\
&48\omega_{12} v_1^2 \omega_5 \omega_9^2 + 48\omega_{12}^2 \omega_5^2 \omega_9 - 32\omega_{12}^2 \omega_5^2 - 120\omega_{12}^2 v_1^2 \omega_5^2 \omega_9 + 16v_1^2 \omega_5^2 \omega_9^3 - 17\omega_{12} \omega_5^2 \omega_9^2 - 28\omega_{12} \omega_5 \omega_9^3 - 12\omega_{12}^2 \omega_9^2 + 43\omega_{12}^2 v_1^2 \omega_5^2 \omega_9^2 - \\
&32\omega_{12} c_s^2 \omega_5 \omega_9 - 16c_s^2 \omega_5 \omega_9^3 + 8\omega_5^2 \omega_9^2 - 20\omega_{12} c_s^2 \omega_9^3 - 44\omega_{12}^2 c_s^2 \omega_5 \omega_9^2 + 16\omega_{12} \omega_5 \omega_9^2 - 16v_1^2 \omega_5^2 \omega_9^2 - 8\omega_5^2 \omega_9^3 \\
C_{18} &= -12\omega_{12}^2 v_1^2 \omega_5 \omega_9^3 - \omega_{12}^2 c_s^4 \omega_5^2 \omega_9^3 + 12c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 12\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^2 - 12\omega_{12}^2 c_s^4 \omega_5^2 \omega_9 - 60\omega_{12} v_1^2 \omega_5^2 \omega_9^2 + 12\omega_{12}^2 c_s^2 \omega_5^2 \omega_9^3 - 81\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^3 - \\
&24\omega_{12} v_1^4 \omega_5^2 \omega_9^2 - 306\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 72\omega_{12}^2 v_1^2 \omega_5^2 + 27\omega_{12} v_1^2 \omega_5^2 \omega_9^3 + 30\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 36\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9 - 12c_s^2 v_1^2 \omega_5^2 \omega_9^2 + \\
&\omega_{12}^2 c_s^4 \omega_5^2 \omega_9^3 + 12\omega_{12} c_s^4 \omega_5 \omega_9^3 - 6\omega_{12}^2 c_s^2 \omega_5^2 \omega_9^2 - 36\omega_{12} v_1^4 \omega_5^2 \omega_9 + 48\omega_{12} v_1^4 \omega_5^2 \omega_9^3 + 162\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^2 + 12\omega_{12}^2 v_1^4 \omega_5 \omega_9^3 + 12\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^3 + \\
&60\omega_{12} v_1^4 \omega_5^2 \omega_9^3 + 12\omega_{12}^2 c_s^2 \omega_5^2 \omega_9 - 108\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9 - 12c_s^2 v_1^2 \omega_5^2 \omega_9^3 + 13\omega_{12}^2 c_s^4 \omega_5^2 \omega_9^3 + 24\omega_{12} v_1^2 \omega_5^2 \omega_9^2 - 12\omega_{12}^2 c_s^4 \omega_5^2 \omega_9^3 + 54\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^2 - \\
&\omega_{12}^2 c_s^2 \omega_5^2 \omega_9^3 - 12\omega_{12}^2 c_s^2 \omega_5^2 - 27\omega_{12} v_1^4 \omega_5^2 \omega_9^3 + 60\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 12\omega_{12} c_s^2 \omega_5 \omega_9^3 - 21\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 48\omega_{12} v_1^2 \omega_5^2 \omega_9^3 + 36\omega_{12} v_1^2 \omega_5^2 \omega_9 + 6\omega_{12}^2 c_s^4 \omega_5^2 \omega_9^2 - \\
&12v_1^4 \omega_5^2 \omega_9^3 + 12\omega_{12}^2 v_1^4 \omega_5^2 \omega_9^2 + 18\omega_{12}^2 c_s^2 \omega_5^2 \omega_9^3 + 6\omega_{12} c_s^4 \omega_5^2 \omega_9^3 - 19\omega_{12}^2 v_1^2 \omega_5^2 \omega_9^2 - 48\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 12v_1^2 \omega_5^2 \omega_9^3 + 24\omega_{12} v_1^2 \omega_5^2 \omega_9^3 - 90\omega_{12}^2 v_1^4 \omega_5^2 \omega_9 - \\
&12\omega_{12} c_s^2 \omega_5^2 \omega_9^2 - 18\omega_{12}^2 v_1^4 \omega_5^2 \omega_9^3 + 12v_1^2 \omega_5^2 \omega_9^2 - 24\omega_{12}^2 c_s^2 \omega_5 \omega_9^3 + 12\omega_{12}^2 c_s^4 \omega_9^3 - 4\omega_{12}^2 v_1^2 \omega_5^2 \omega_9^3 + 72\omega_{12}^2 v_1^4 \omega_5^2 - 6\omega_{12} c_s^4 \omega_5^2 \omega_9^2 + 12\omega_{12}^2 c_s^4 \omega_5^2 + \\
&12v_1^2 \omega_5^2 \omega_9^3 - 12\omega_{12} c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 18\omega_{12} c_s^4 \omega_5^2 \omega_9^3 - 12\omega_{12}^2 v_1^2 \omega_5^2 \omega_9^2 + 19\omega_{12}^2 v_1^4 \omega_5^2 \omega_9^2 - 6\omega_{12} c_s^2 \omega_5^2 \omega_9^3 - 24\omega_{12} v_1^4 \omega_5 \omega_9^3 - 48\omega_{12}^2 c_s^2 v_1^2 \omega_5 \omega_9^2 + 12v_1^4 \omega_5^2 \omega_9^3 + \\
&252\omega_{12}^2 c_s^2 v_1^2 \omega_5^2 + 18\omega_{12}^2 v_1^2 \omega_5^2 \omega_9^3 + 12\omega_{12}^2 c_s^4 \omega_5^2 \omega_9^2 + 90\omega_{12}^2 v_1^2 \omega_5^2 \omega_9 + 6\omega_{12}^2 c_s^2 \omega_5 \omega_9^3 - 12v_1^4 \omega_5^2 \omega_9^2 + 102\omega_{12}^2 c_s^2 v_1^2 \omega_5 \omega_9^3 + 6\omega_{12} c_s^2 \omega_5^2 \omega_9^2 + 4\omega_{12}^2 v_1^4 \omega_5^2 \omega_9^3
\end{aligned}$$

$$\begin{aligned}
C_{19} = & 36w_{12}v_1^2w_5^2w_{21}w_{15}w_3^3 + 36w_{12}c_8^4w_3^3w_{15}w_5^3 - 12w_{12}c_2^2v_1^2w_5w_{21}w_{15}w_5^3 - 18w_{12}c_8^4w_3^3w_5^3 + 36c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}v_1^2v_2^2w_3^3w_5^3 - \\
& 84w_{12}c_8^4w_3^3w_{21}w_{15}w_5^3 - 12w_{12}v_2^2w_3^3w_{15}w_5^3 - 96w_{12}c_2^4w_{21}w_{15}w_5^3 - 36w_{12}c_2^2v_2^2w_3^3w_{15}w_5^3 + 12w_{12}c_2^2v_1^2w_3^3w_5^3 - 12w_{12}v_2^2v_1^2w_3^3w_5^3 - \\
& 24w_{12}c_2^2v_2^2w_{15}w_{21}w_{15}w_5^3 - 12w_{12}c_2^2w_3^3w_{15}w_5^3 - 12w_{12}v_1^2v_2^2w_3^3w_{15}w_5^3 - 12w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}v_2^2v_1^2w_3^3w_{21}w_{15} + 12w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 + \\
& 18w_{12}c_2^2v_1^2w_3^3w_{15}w_5^3 - 6w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 - 36w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 36c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}v_2^2v_1^2w_3^3w_{15}w_5^3 + 180w_{12}c_2^4w_3^3w_5w_{21}w_{15}w_5^3 + \\
& 12v_2^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}v_2^2w_3^3w_{21}w_{15} + 12w_{12}c_2^2w_3^3w_{15}w_5^3 + 12w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}c_2^2w_3^3w_{21}w_{15} + 18w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 - \\
& 36w_{12}c_2^4w_3^3w_{15}w_5^3 - 12w_{12}c_2^2v_2^2w_3^3w_{15}w_5^3 + 12w_{12}c_2^2v_1^2w_3^3w_{21}w_{15} - 12w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12c_2^4w_3^3w_{21}w_{15}w_5^3 - 12w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 - \\
& 12w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - 18w_{12}c_2^4w_3^3w_{15}w_5^3 - 72w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 + 18w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 + 12c_2^4w_3^3w_{21}w_{15}w_5^3 + 36w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + \\
& 36w_{12}c_2^2v_1^2w_3^3w_{15}w_5^3 + 6w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 12c_2^2w_3^3w_{21}w_{15}w_5^3 + 24w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - \\
& 6w_{12}c_2^2v_1^2w_3^3w_5^3 - 6w_{12}c_2^2w_3^3w_{21}w_5^3 + 12w_{12}c_2^2v_1^2w_3^3w_{15}w_5^3 - 72w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 6w_{12}c_2^2w_3^3w_5^3 - 6w_{12}v_2^2w_3^3w_{21}w_5^3 + 6w_{12}v_2^2w_3^3w_5^3 - \\
& 12v_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 + 36w_{12}c_2^4w_3^3w_5^3 - 54w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 12c_2^4w_3^3w_{21}w_{15}w_5^3 - 6w_{12}v_1^2v_2^2w_3^3w_5^3 - \\
& 18w_{12}c_2^2v_2^2w_3^3w_{15}w_5^3 + 24w_{12}v_2^2w_3^3w_{21}w_{15}w_5^3 - 36c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12v_2^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12c_2^2w_3^3w_{21}w_{15}w_5^3 + \\
& 12w_{12}v_1^2v_2^2w_3^3w_{15}w_5^3 - 36w_{12}c_2^4w_3^3w_{21}w_5^3 + 18w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 + 18w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12c_2^4w_3^3w_{21}w_{15}w_5^3 + 6w_{12}v_1^2v_2^2w_3^3w_{21}w_5^3 + \\
& 24w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 18w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - 36w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 24w_{12}v_2^2w_3^3w_{21}w_{15}w_5^3 - 36w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - 36w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 - \\
& 18w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 + 6w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}v_2^2w_3^3w_{15}w_5^3 + 24w_{12}v_2^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}c_2^2w_3^3w_{15}w_5^3 - 6w_{12}v_1^2v_2^2w_3^3w_{15}w_5^3 - \\
& 12v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 + 18w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 - 18w_{12}v_2^2w_3^3w_{21}w_{15}w_5^3 - 6w_{12}c_2^2w_3^3w_{15}w_5^3 - 6w_{12}v_2^2w_3^3w_{15}w_5^3 + \\
& 12w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 150w_{12}c_2^4w_3^3w_{21}w_{15}w_5^3 + 6w_{12}c_2^2v_1^2w_3^3w_{15}w_5^3 - 24w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 36w_{12}c_2^4w_3^3w_{15}w_5^3 + 12w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - \\
& 42w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - 36w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 6w_{12}v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}c_2^2w_3^3w_{15}w_5^3 + 12v_1^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 36w_{12}c_2^2v_2^2w_3^3w_{15}w_5^3 + \\
& 6w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}v_2^2w_3^3w_{15}w_5^3 + 12w_{12}v_2^2w_3^3w_{21}w_{15}w_5^3 + 108w_{12}c_2^2v_2^2w_3^3w_{21}w_{15}w_5^3 + 12w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 + 18w_{12}c_2^2v_2^2w_3^3w_{21}w_5^3 + \\
& 36w_{12}c_2^2w_3^3w_{21}w_{15} - 36w_{12}c_2^4w_3^3w_{15}w_5^3 + 30w_{12}c_2^2w_3^3w_{21}w_{15}w_5^3 - 6w_{12}c_2^2v_1^2w_3^3w_{15}w_5^3 + 6w_{12}v_2^2w_3^3w_{15}w_5^3 - 88w_{12}c_2^4w_3^3w_{21}w_{15}w_5^3 - \\
& 12c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 - 12w_{12}c_2^2v_1^2w_3^3w_{21}w_{15}w_5^3 - 18w_{12}c_2^2v_2^2w_3^3w_{15}w_5^3 + w_{12}c_2^2w_3^3w_{15}w_5^3 + 36w_{12}c_2^2v_2^2w_3^3w_{21}w_{15} -$$

$$\begin{aligned}
C_{22} = & 24w_{12}w_{10}^2v_1^2w_5w_{21}w_{15}w_9 - 12w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{21}w_9 - 42w_{12}c_s^4w_{10}^2w_5^2w_{21}w_{15}w_9 - 12w_{12}c_s^2w_{10}^2v_2^2w_5w_{21}w_{15}w_9 + 6w_{12}c_s^2w_{10}^2w_5^3w_{15}^2 + \\
& 6w_{12}c_s^2w_{10}^2v_2^2w_5^3w_{21}w_9 + 24w_{12}w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}^2 + 72w_{12}c_s^2w_{10}v_1^2w_5^2w_{21}w_{15}^2 + 18w_{12}c_s^2w_{10}v_2^2w_5^2w_{21}w_{15}^2w_9 - 18w_{12}c_s^2w_{10}^2v_1^2w_5^3w_{15}w_9 - \\
& 36c_s^4w_{10}w_5^2w_{21}w_{15}^2w_9 - 12w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{15}w_9 + w_{12}c_s^2w_{10}^2v_2^2w_5^3w_{21}w_{15}w_9 + 6w_{12}c_s^2w_{10}^2v_2^2w_5^3w_{15}w_9 + 36w_{12}w_{10}v_1^2w_5^2w_{21}w_{15}^2w_9 - \\
& 24w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{21}w_{15} - 12w_{12}w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}w_9 + 6w_{12}w_{10}^2v_1^2w_5^2w_{15}^2 + 6w_{12}c_s^2w_{10}w_5^2w_{21}w_{15}^2 - 45w_{12}c_s^2w_{10}^2v_2^2w_5^2w_{21}w_{15}w_9 - \\
& 18w_{12}c_s^2w_{10}^2w_5^2w_{21}w_{15}w_9 + 24w_{12}w_{10}v_1^2w_5^2w_{21}w_{15} + 6w_{12}c_s^2w_{10}^2w_5^3w_{15}w_9 + 12c_s^2w_{10}^2w_5^3w_{15}w_9 + 12w_{12}w_{10}v_1^2w_5^2w_{15}w_9 - \\
& 36w_{12}c_s^2w_{10}v_1^2w_5^2w_{21}w_{15}w_9 - 18w_{12}c_s^4w_{10}^2w_5^3w_{15}w_9 - 36c_s^4w_{10}^2w_5^3w_{15}w_9 + 18w_{12}c_s^4w_{10}w_5^2w_{21}w_{15}^2 + 12w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}^2w_9 + \\
& 12w_{10}v_1^2w_5^2w_{21}w_{15}^2 - 6w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{15}^2 + 12w_{12}w_{10}^2v_1^2w_5^2w_{21}w_9 - 36c_s^2w_{10}^2v_1^2w_5^2w_{15}^2w_9 + 12c_s^2w_{10}w_5^2w_{21}w_{15}^2w_9 + 36c_s^2w_{10}v_1^2w_5^3w_{21}w_{15}^2w_9 + \\
& 18w_{12}c_s^2w_{10}v_1^2w_5^3w_{21}w_{15}w_9 - 36w_{12}c_s^2w_{10}^2v_1^2w_5^3w_{15}w_9 - 6w_{12}w_{10}^2v_1^2v_2^2w_5^3w_{15}w_9 - 36w_{12}c_s^4w_{10}w_5w_{21}w_{15}^2w_9 + 144w_{12}c_s^2w_{10}^2v_1^2w_5^2w_{21}w_{15}w_9 + \\
& 6w_{12}w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}w_9 + 12w_{12}c_s^2w_{10}v_2^2w_5^2w_{15}w_9 + 3w_{12}c_s^2w_{10}w_5^2w_{21}w_{15}w_9 - 72w_{12}c_s^2w_{10}^2v_1^2v_2^2w_5^2w_{21}w_{15} - 36w_{12}c_s^2w_{10}^2v_1^2w_5^2w_{21}w_9 - \\
& 36c_s^2w_{10}v_1^2w_5^2w_{21}w_{15}^2w_9 + 72w_{12}c_s^2w_{10}v_1^2w_5w_{21}w_{15}^2w_9 - 12c_s^2w_{10}w_5^2w_{21}w_{15}^2w_9 + 6w_{12}c_s^2w_{10}v_2^2w_5^2w_{15}^2 - 12w_{10}v_1^2w_5^3w_{15}^2 - \\
& 12w_{12}c_s^2w_{10}^2w_5w_{21}w_{15}^2w_9 - 12w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}^2w_9 + 24w_{12}w_{10}v_1^2v_2^2w_5w_{21}w_{15}^2w_9 - 36w_{12}c_s^4w_{10}w_5^2w_{15}^2w_9 + 12c_s^2w_{10}^2v_2^2w_5^2w_{15}w_9 - \\
& 24w_{12}w_{10}v_1^2w_5^2w_{21}w_{15}^2 - 6w_{12}c_s^2w_{10}^2v_2^2w_5^3w_{15}^2 + 12w_{12}c_s^2w_{10}^2w_5^2w_{21}w_9 + 15w_{12}c_s^4w_{10}^2w_5^3w_{21}w_{15}w_9 - 12w_{10}v_1^2v_2^2w_5^2w_{15}w_9 + \\
& 12w_{12}c_s^2w_{10}w_5w_{21}w_{15}^2w_9 - 12w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}^2 + 12w_{12}c_s^4w_{10}^2w_5^2w_{21}w_9 + 156w_{12}c_s^4w_{10}^2w_5w_{21}w_{15}^2w_9 - 36c_s^2w_{10}v_1^2w_5^3w_{21}w_{15}^2 - \\
& 12w_{12}c_s^2w_{10}^2v_2^2w_5^2w_{15}^2w_9 + 12w_{12}c_s^2w_{10}^2w_5^2w_{21}w_{15}^2w_9 - 9w_{12}w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}^2w_9 - 24w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{21}w_{15}w_9 + 36c_s^2w_{10}^2v_1^2w_5^2w_{15}^2 + \\
& 6w_{12}w_{10}^2v_1^2w_5^3w_{15}w_9 + 12w_{10}^2v_1^2w_5^3w_{15}w_9 - 12c_s^2w_{10}^2w_5^3w_{15}w_9 - 5w_{12}c_s^4w_{10}v_2^2w_5^3w_{21}w_{15}^2w_9 + 36c_s^4w_{10}w_5^3w_{21}w_{15}^2w_9 + 3w_{12}c_s^4w_{10}w_5^3w_{21}w_{15}^2w_9 + \\
& 12c_s^2w_{10}^2v_2^2w_5^3w_{15}^2 - 18w_{12}c_s^4w_{10}^2w_5^3w_{15}^2 - 24w_{12}w_{10}v_1^2w_5^2w_{21}w_{15}^2w_9 - 15w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{21}w_{15}w_9 + 36c_s^4w_{10}^2w_5^2w_{15}^2w_9 + 36w_{12}c_s^4w_{10}^2w_5^2w_{15}w_9 - \\
& 12w_{12}c_s^2w_{10}v_2^2w_5^2w_{21}w_{15}^2w_9 - 12c_s^2w_{10}^2v_2^2w_5^2w_{21}w_{15}^2w_9 + 36c_s^2w_{10}v_1^2w_5^2w_{15}^2w_9 - 6w_{12}w_{10}^2v_1^2w_5^3w_{21}w_9 - 12c_s^2w_{10}^2w_5^3w_{15}^2w_9 - 12w_{12}w_{10}^2v_1^2w_5^3w_{21}w_{15} - \\
& 12w_{12}c_s^2w_{10}^2w_5^2w_{15}w_9 - 6w_{12}w_{10}v_1^2w_5^2w_{21}w_{15}w_9 - 18w_{12}c_s^2w_{10}^2v_1^2w_5^2w_{15}^2 + 12w_{12}c_s^4w_{10}^2w_5^2w_{21}w_{15}w_9 + 18w_{12}c_s^2w_{10}^2v_2^2w_5^2w_{21}w_{15}w_9 - \\
& 12w_{12}w_{10}v_2^2w_5^2w_{21}w_{15}^2 - 48w_{12}w_{10}^2v_1^2w_5^2w_{21}w_{15}w_9 - 6w_{12}w_{10}^2v_1^2w_5^3w_{15}w_9 + 5w_{12}c_s^2w_{10}^2w_5^2w_{21}w_{15}^2w_9 - 18w_{12}c_s^2w_{10}^2v_1^2w_5^2w_{21}w_{15}^2w_9 + \\
& 6w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{15}w_9 + 27w_{12}c_s^2w_{10}v_1^2w_5^2w_{21}w_{15}^2w_9 + 36w_{12}c_s^2w_{10}^2v_1^2w_5^2w_{15}w_9 - 12w_{12}v_1^2w_5^2w_{21}w_{15}^2w_9 + 12w_{12}w_{10}^2v_1^2v_2^2w_5^2w_{21}w_{15} - \\
& 12w_{12}c_s^2w_{10}^2v_2^2w_5^2w_{15}^2w_9 - w_{12}c_s^4w_{10}^2w_5^2w_{21}w_{15}^2w_9 + 9w_{12}w_{10}v_1^2v_2^2w_5^2w_{21}w_{15}^2w_9 - 15w_{12}c_s^2w_{10}w_5^2w_{21}w_{15}^2w_9 + 6w_{12}w_{10}^2v_1^2v_$$

$$\begin{aligned}
C_{24} = & 24\omega_{12}\omega_{10}^2\omega_1^2\omega_5\omega_{21}\omega_{15}\omega_9 - 36\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_9 - 18\omega_{12}c_4^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 60\omega_{12}c_2^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 6\omega_{12}c_2^2\omega_{10}^2\omega_5^3\omega_{15} - \\
& 12\omega_{12}c_2^2\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_9 + 72\omega_{12}\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15} + 24\omega_{12}c_2^2\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15} + 54\omega_{12}c_2^2\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 6\omega_{12}c_2^2\omega_{10}^2\omega_1^2\omega_5^2\omega_{15}\omega_9 - \\
& 2c_8^2\omega_{10}^2\omega_{15}\omega_{21}\omega_{15}\omega_9 - 48\omega_{12}c_2^2\omega_{10}^2\omega_{15}\omega_{21}\omega_{15}\omega_9 - 36\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{15}\omega_9 + 18\omega_{12}c_2^2\omega_{10}^2\omega_1^2\omega_5^2\omega_{15}\omega_9 + 36\omega_{12}\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - \\
& 72\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_{15} - 36\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 6\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{15} - 6\omega_{12}c_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{15} - 15\omega_{12}c_2^2\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + \\
& 18\omega_{12}c_2^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 24\omega_{12}\omega_{10}^2\omega_5^2\omega_{21}\omega_{15} + 6\omega_{12}c_2^2\omega_{10}^2\omega_5^3\omega_{15}\omega_9 + 12c_2^2\omega_{10}^2\omega_5^3\omega_{15}\omega_9 + 12\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{15}\omega_9 - \\
& 12\omega_{12}c_2^2\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 6\omega_{12}c_2^2\omega_{10}\omega_5^2\omega_{15}\omega_9 - 12c_4^2\omega_{10}^2\omega_5^2\omega_{15}\omega_9 + 6\omega_{12}c_4^2\omega_{10}\omega_5^2\omega_{21}\omega_{15} + 36\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 12\omega_{10}\omega_1^2\omega_5^3\omega_{21}\omega_{15} - \\
& 18\omega_{12}\omega_{10}^2\omega_1^2\omega_5^3\omega_{15} + 12\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_9 - 12c_8^2\omega_{10}^2\omega_1^2\omega_5^3\omega_{15}\omega_9 + 12c_2^2\omega_{10}\omega_1\omega_5^2\omega_{21}\omega_{15}\omega_9 + 12c_2^2\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + \\
& 6\omega_{12}c_2^2\omega_{10}\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 12\omega_{12}c_2^2\omega_{10}\omega_1^2\omega_5^2\omega_{15}\omega_9 - 18\omega_{12}\omega_{10}^2\omega_1^2\omega_5^2\omega_{15}\omega_9 - 12\omega_{12}c_4^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9 + 48\omega_{12}c_2^2\omega_{10}^2\omega_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 +
\end{aligned}$$

$$\begin{aligned}
& 18\omega_{12}\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + 36\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{15}\omega_9 - 6\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9 - 24\omega_{12}c_s^2\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_{12}c_s^2\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_9 - \\
& 12c_s^2\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 24\omega_{12}c_s^2\omega_{10}v_1^2\omega_5\omega_{21}\omega_{15}^2\omega_9 - 12c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 18\omega_{12}c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15}^2 - 12\omega_{10}^2v_1^2\omega_5^2\omega_{15} - \\
& 36\omega_{10}v_1^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 72\omega_{12}\omega_{10}v_1^2v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9 - 12\omega_{12}c_s^4\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9 + 36c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{15}^2\omega_9 - 24\omega_{12}\omega_{10}v_1^2\omega_5^2\omega_{21}\omega_{15}^2 - \\
& 18\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^3\omega_{15}^2 + 6\omega_{12}c_s^4\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 36\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{15}^2\omega_9 + 12\omega_{12}c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9 - 36\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15}^2 + \\
& 18\omega_{12}c_s^4\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9 - 12c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}^2 - 15\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 12\omega_{12}c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9 - 9\omega_{12}\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - \\
& 72\omega_{12}\omega_{10}^2v_1^2v_2^2\omega_5\omega_{21}\omega_{15}\omega_9 + 12c_s^2\omega_{10}^2v_1^2\omega_5^3\omega_{15}^2 + 6\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{15}\omega_9 + 12\omega_{10}^2v_1^2\omega_5^3\omega_{15}^2\omega_9 - 12c_s^2\omega_{10}^2\omega_5^3\omega_{15}^2 - 15\omega_{12}c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + \\
& 12c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - \omega_{12}c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 36c_s^2\omega_{10}^2v_2^2\omega_5^3\omega_{15}^2 - 6\omega_{12}c_s^4\omega_{10}\omega_5^3\omega_{15}^2 - 24\omega_{12}\omega_{10}v_1^2\omega_5\omega_{21}\omega_{15}^2\omega_9 - 45\omega_{12}\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + \\
& 12c_s^4\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9 + 12\omega_{12}c_s^4\omega_{10}\omega_5^3\omega_{15}\omega_9 - 36\omega_{12}c_s^2\omega_{10}v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9 - 36c_s^2\omega_{10}v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 12c_s^2\omega_{10}^2v_1^2\omega_5^2\omega_{15}^2\omega_9 - \\
& 6\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_9 - 12c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9 - 12\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_{12}c_s^2\omega_{10}\omega_5^2\omega_{15}\omega_9 - 6\omega_{12}\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 6\omega_{12}c_s^2\omega_{10}^2v_1^2\omega_5^3\omega_{15}^2 + \\
& 12\omega_{12}c_s^4\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9 - 102\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 36c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15}^2 - 48\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 6\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{15}^2\omega_9 + \\
& 5\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - 6\omega_{12}c_s^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + 18\omega_{12}\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{15}\omega_9 + 9\omega_{12}c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 12\omega_{12}c_s^2\omega_{10}v_1^2\omega_5^3\omega_{15}\omega_9 - \\
& 12\omega_{12}v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 36\omega_{12}\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15} - 36\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{15}^2\omega_9 + 27\omega_{12}\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - 5\omega_{12}c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + \\
& 18\omega_{12}\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{21}\omega_9 - 6\omega_{12}c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 36\omega_{12}v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - 18\omega_{12}\omega_{10}v_2^2v_2^2\omega_5^3\omega_{21}\omega_{15}^2 + \\
& 24\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{21}\omega_9 - 12\omega_{12}c_s^2\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9 - 6\omega_{12}c_s^2\omega_{10}^2\omega_5^3\omega_{15}\omega_9 + \omega_{12}c_s^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - 108\omega_{12}\omega_{10}v_1^2v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + \\
& 12c_s^2\omega_{10}^2\omega_{21}\omega_{15}^2 + 6\omega_{12}v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - 36\omega_{12}c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 12\omega_{10}^2v_1^2\omega_5^3\omega_{15}^2\omega_9 - 12\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{15}\omega_9 - 12\omega_{12}\omega_{10}^2v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - \\
& 24\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5\omega_{21}\omega_{15}\omega_9 + 6\omega_{12}\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15}^2 - 12c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2 - 18\omega_{12}v_2^2v_2^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 6\omega_{12}c_s^4\omega_{10}\omega_5^3\omega_{15}^2\omega_9 - \\
& 36c_s^2\omega_{10}^2v_2^2\omega_5^3\omega_{15}^2\omega_9 + 12\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 36\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{15}\omega_9 + 18\omega_{12}c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9 - 12\omega_{12}c_s^4\omega_{10}\omega_{21}\omega_{15}^2\omega_9 + 36\omega_{10}^2v_1^2v_2^2\omega_5^3\omega_{15}^2 + \\
& 36c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 6\omega_{12}c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_9 - 5\omega_{12}c_s^4\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 60\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9 + 144\omega_{12}\omega_{10}^2v_1^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 - \\
& 18\omega_{12}c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 12c_s^4\omega_{10}^2\omega_5^3\omega_{15}^2 + 36\omega_{12}\omega_{10}^2v_1^2\omega_5^2\omega_{15}\omega_9 + 15\omega_{12}\omega_{10}^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 6\omega_{12}c_s^2\omega_{10}^2v_1^2\omega_5^3\omega_{15}^2\omega_9 + \\
& 12\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^3\omega_{21}\omega_{15} - 18\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^3\omega_{15}\omega_9 + 12\omega_{12}\omega_{10}v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 30\omega_{12}c_s^2\omega_{10}^2v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9
\end{aligned}$$

$$\begin{aligned}
C_{25} = & 12c_s^2\omega_{10}^2\omega_{15}^2 + 36v_2^2\omega_{15}^2 + 48c_s^2\omega_{10}\omega_5\omega_{15}^2 + 12c_s^4\omega_{10}^2\omega_5^2 - 24\omega_{10}v_2^2\omega_{15}^2 + 216c_s^2\omega_{10}v_2^2\omega_{15}^2 - 24c_s^4\omega_{10}^2\omega_{15} - 12\omega_{10}^2v_2^2\omega_{15}^2 + c_s^2\omega_{10}\omega_5^2\omega_{15}^2 + \\
& 36\omega_{10}v_2^2\omega_{15}^2 + 48\omega_{10}v_2^2\omega_{15}^2 + 96\omega_{10}^2v_2^2\omega_{15}\omega_5 + 72c_s^2\omega_{10}v_2^2\omega_{15}\omega_5 + 48\omega_{10}^2v_2^2\omega_{15}\omega_5 + 48c_s^4\omega_{10}\omega_5\omega_{15} + 24c_s^2\omega_{10}^2\omega_5\omega_{15} - 12c_s^4\omega_{10}^2\omega_5^2\omega_{15} - 36v_2^2\omega_5^2\omega_{15}^2 + \\
& 150c_s^2\omega_{10}v_2^2\omega_5\omega_{15}^2 - 12c_s^2\omega_{10}^2\omega_5^2 + 432c_s^2\omega_{10}^2v_2^2\omega_5\omega_{15} + 12c_s^2\omega_{10}^2\omega_5^2\omega_{15} + 24\omega_{10}^2v_2^2\omega_5 + 24\omega_{10}v_2^4\omega_5^2\omega_{15} + 24c_s^2\omega_{10}^2\omega_{15} - 36\omega_{10}v_2^2\omega_5^2\omega_{15} + \\
& 14c_s^4\omega_{10}\omega_5^2\omega_{15}^2 - 96\omega_{10}^2v_2^2\omega_5\omega_{15} + 288c_s^2v_2^2\omega_5\omega_{15}^2 - 24c_s^4\omega_{10}^2\omega_5 + 12\omega_{10}^2v_2^2\omega_5^2 - 48c_s^4\omega_{10}\omega_5\omega_{15}^2 + 96\omega_{10}v_2^2\omega_5\omega_{15}^2 + 30\omega_{10}^2v_2^2\omega_5^2\omega_{15} + 24c_s^4\omega_{10}\omega_{15}^2 - \\
& 48\omega_{10}v_2^2\omega_{15}^2 - 48\omega_{10}^2v_2^2\omega_{15} - 144c_s^2v_2^2\omega_5^2\omega_{15}^2 + 72v_2^4\omega_5\omega_{15}^2 - 216c_s^2\omega_{10}^2v_2^2\omega_{15} - 432c_s^2\omega_{10}v_2^2\omega_5\omega_{15}^2 + 24c_s^4\omega_5\omega_{15}^2 - c_s^4\omega_{10}\omega_5^2\omega_{15}^2 - 126c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{15} + \\
& 72c_s^2\omega_{10}^2v_2^2\omega_{15}^2 - 48\omega_{10}v_2^2\omega_5\omega_{15} - 48c_s^2\omega_{10}^2\omega_5\omega_{15} - 3\omega_{10}^2v_2^2\omega_{15}^2 - 96\omega_{10}v_2^4\omega_5\omega_{15}^2 - 144c_s^2\omega_{10}^2v_2^2\omega_5^2 - 24c_s^2\omega_{10}^2v_2^2\omega_{15}^2 - 30\omega_{10}^2v_2^4\omega_5\omega_{15} - \\
& 144c_s^2\omega_{10}v_2^2\omega_5\omega_{15} - 12c_s^4\omega_{10}\omega_5\omega_{15} - 12c_s^2\omega_{10}^2v_2^2\omega_5^2\omega_{15} - 72v_2^2\omega_5^2\omega_{15}^2 - 24c_s^2\omega_5\omega_{15}^2 - 14c_s^2\omega_{10}\omega_5^2\omega_{15}^2 - 24\omega_{10}^2v_2^4\omega_5 + 48\omega_{10}v_2^2\omega_5\omega_{15} + 3\omega_{10}^2v_2^2\omega_5^2\omega_{15}^2
\end{aligned}$$

$$\begin{aligned}
C_{26} = & -24c_s^2v_2^2\omega_5\omega_{15} - 8c_s^2\omega_5^2\omega_{15}^2 + 24v_2^2\omega_5^2\omega_{15}^2 + 3v_2^4\omega_5^3\omega_{15} - 3c_s^4\omega_5^3\omega_{15} - 6c_s^2\omega_5^3\omega_{15} + 18v_2^2\omega_5^3\omega_{15} + 72v_2^4\omega_5^2\omega_{15} - 24c_s^4\omega_5^2\omega_{15} + \\
& 24c_s^4\omega_5^2\omega_{15} - 24v_2^4\omega_5^2\omega_{15} - 3v_2^2\omega_5^3\omega_{15} + c_s^2\omega_5^3\omega_{15}^2 + 24v_2^2\omega_5^3 + 6c_s^2\omega_5^3\omega_{15} + 156c_s^2v_2^2\omega_5\omega_{15}^2 - 12v_2^2\omega_5^3 - 72v_2^2\omega_5^2\omega_{15} + 24c_s^2\omega_5^2\omega_{15} - \\
& 24c_s^2\omega_5\omega_{15} + 48v_2^2\omega_5\omega_{15} - 72c_s^2v_2^2\omega_5^2\omega_{15} - 24c_s^2v_2^2\omega_5^2 + 24c_s^4\omega_{15}^2 + 24v_2^4\omega_5^2\omega_{15} - 48c_s^4\omega_5\omega_{15}^2 + 12c_s^2v_2^2\omega_5^3 - 12c_s^2v_2^2\omega_5^3\omega_{15} + 6c_s^2v_2^2\omega_5^3\omega_{15}^2 + \\
& 12v_2^4\omega_5^3 + 24c_s^4\omega_5\omega_{15} - 48v_2^4\omega_5\omega_{15} - 24v_2^2\omega_5\omega_{15}^2 + 12c_s^2\omega_5\omega_{15}^2 + 48c_s^2v_2^2\omega_5^2\omega_{15} - 96c_s^2v_2^2\omega_{15}^2 - 24v_2^2\omega_5^2
\end{aligned}$$

$$\begin{aligned}
C_{27} = & -36c_s^2\omega_5^2\omega_{15}^2 - 36\omega_{10}\omega_{15}^2 - 60v_2^2\omega_5^2\omega_{15}^2 - 120c_s^2\omega_{10}\omega_5\omega_{15}^2 - 12\omega_{10}\omega_5^2\omega_{15} + 36\omega_{10}v_2^2\omega_5^2\omega_{15} + 24\omega_{10}^2v_2^2\omega_5^2 - 3c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - \\
& 72\omega_{10}^2\omega_5\omega_{15} - 48\omega_5\omega_{15}^2 - 84\omega_{10}^2v_2^2\omega_{15} - 48c_s^2\omega_{10}^2\omega_5 + 24c_s^2\omega_{10}^2\omega_5^2 - 33c_s^2\omega_{10}^2\omega_5\omega_{15} - 48\omega_{10}^2v_2^2\omega_5 - 60c_s^2\omega_{10}^2\omega_{15} + 61\omega_{10}v_2^2\omega_5^2\omega_{15} + \\
& 168\omega_{10}^2v_2^2\omega_5\omega_{15} - 24c_s^2\omega_{10}\omega_5\omega_{15} - 25\omega_{10}\omega_5^2\omega_{15}^2 - 168\omega_{10}v_2^2\omega_5\omega_{15}^2 - 12\omega_{10}^2\omega_5^2 - 51\omega_{10}^2v_2^2\omega_5^2\omega_{15} + 84\omega_{10}v_2^2\omega_{15}^2 + 36\omega_{10}^2\omega_5\omega_{15}^2 + \\
& 12c_s^2\omega_{10}\omega_5^2\omega_{15} + 2\omega_{10}^2\omega_5^2\omega_{15}^2 + 120c_s^2\omega_{10}^2\omega_5\omega_{15} + 21\omega_{10}^2\omega_5^2\omega_{15} + 24\omega_5^2\omega_{15}^2 + 60c_s^2\omega_{10}\omega_{15}^2 + 120v_2^2\omega_5\omega_{15}^2 + 72c_s^2\omega_5\omega_{15}^2 + 24\omega_{10}\omega_5\omega_{15} + \\
& 39c_s^2\omega_{10}\omega_5^2\omega_{15}^2 + 24\omega_{10}^2\omega_5 - 72\omega_{10}v_2^2\omega_5\omega_{15} - 5\omega_{10}^2v_2^2\omega_5^2\omega_{15}^2
\end{aligned}$$

$$\begin{aligned}
C_{28} = & 4\omega_6^2v_1^2\omega_9^2 + 4c_s^4\omega_{13}^2\omega_9^2 + 32\omega_6^2\omega_{13}v_1^4\omega_9^2 + 24\omega_6^2c_s^2v_1^2\omega_9^3 + 36\omega_6^2\omega_{13}^2v_1^2\omega_9 + 4\omega_6c_s^2\omega_{13}^2\omega_9 - 84\omega_6c_s^2\omega_{13}^2v_1^2\omega_9^2 - 20\omega_6\omega_{13}v_1^2\omega_9^3 - 8\omega_6^2c_s^2\omega_{13}\omega_9^2 - \\
& 13\omega_6^2\omega_{13}v_1^4\omega_9^3 - 24\omega_6^2c_s^2v_1^2\omega_9^3 - 8\omega_6c_s^4\omega_{13}^2\omega_9^2 - 4\omega_6^2c_s^4\omega_{13}\omega_9 + 51\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9^2 - 4\omega_6^2v_1^2\omega_9^3 + 20\omega_6\omega_{13}^2v_1^2\omega_9 - 8\omega_6^2c_s^2\omega_{13} + 24\omega_6^2\omega_{13}^2v_1^4 + \\
& 4\omega_6^2c_s^2\omega_{13}\omega_9^3 + 8\omega_{13}v_1^2\omega_9^3 + 16\omega_6\omega_{13}v_1^2\omega_9^3 - 4\omega_6c_s^4\omega_{13}^2 + 36c_s^2\omega_{13}^2v_1^2\omega_9^2 - 4\omega_6v_1^4\omega_9^3 - 4c_s^2\omega_{13}^2\omega_9^2 - 4\omega_6c_s^2\omega_{13}^2\omega_9 + 4\omega_6c_s^2\omega_{13}^2v_1^2\omega_9 - \\
& 20\omega_6\omega_{13}^2v_1^4\omega_9^3 + 8\omega_6c_s^4\omega_{13}\omega_9^2 + 8\omega_6c_s^2\omega_{13}^2\omega_9^2 - 13\omega_6^2\omega_{13}^2v_1^2\omega_9^2 + 72\omega_6c_s^2\omega_{13}^2v_1^2\omega_9 + 4\omega_6^2c_s^2\omega_{13}\omega_9 - 4\omega_6^2c_s^4\omega_{13}\omega_9^3 + 8\omega_{13}^2v_1^4\omega_9^2 + 4\omega_6^2c_s^2\omega_9^2 - \\
& 20\omega_6^2\omega_{13}v_1^4\omega_9 + 13\omega_6^2\omega_{13}v_1^2\omega_9^3 + 4c_s^2\omega_{13}\omega_9^3 - 20\omega_6\omega_{13}^2v_1^2\omega_9 + 4\omega_6^2v_1^4\omega_9^3 + 12\omega_6^2c_s^2\omega_{13}^2\omega_9 + 8\omega_6^2c_s^4\omega_{13}^2 - 72\omega_6^2c_s^2\omega_{13}v_1^2\omega_9 - 16\omega_6\omega_{13}v_1^4\omega_9^2 - \\
& 24\omega_6c_s^2v_1^2\omega_9^3 - 8\omega_{13}v_1^4\omega_9^3 + 4\omega_6c_s^2\omega_9^3 - 4\omega_6^2v_1^4\omega_9^2 - 36c_s^2\omega_{13}v_1^2\omega_9^3 - 8\omega_6c_s^2\omega_{13}\omega_9^3 - 32\omega_6^2\omega_{13}v_1^2\omega_9^2 - 36\omega_6^2\omega_{13}v_1^4\omega_9 + 20\omega_6\omega_{13}v_1^4\omega_9^3 + \\
& 4\omega_6^2c_s^4\omega_{13}\omega_9^2 + 13\omega_6^2\omega_{13}^2v_1^4\omega_9^2 - 4c_s^4\omega_{13}\omega_9^3 + 96\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9 - 51\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9^3 - 12\omega_6^2c_s^4\omega_{13}\omega_9 - 8\omega_{13}^2v_1^2\omega_9^2 - 48\omega_6c_s^2\omega_{13}v_1^2\omega_9 + 20\omega_6^2\omega_{13}v_1^2\omega_9 - \\
& 4\omega_6c_s^2\omega_9^2 - 24\omega_6^2\omega_{13}^2v_1^4 + 4\omega_6v_1^2\omega_9^3 + 120\omega_6^2c_s^2\omega_{13}v_1^2\omega_9^2 + 8\omega_6c_s^4\omega_{13}\omega_9^3 + 4\omega_6^2c_s^4\omega_9^3 - 4\omega_6^2c_s^2\omega_{13}^2\omega_9 + 84\omega_6c_s^2\omega_{13}v_1^2\omega_9^3 + 20\omega_6\omega_{13}^2v_1^2\omega_9^2
\end{aligned}$$

$$\begin{aligned}
C_{29} = & -16\omega_6^2v_1^2\omega_9^2 - 120\omega_6^2\omega_{13}^2v_1^2\omega_9 + 28\omega_6\omega_{13}^2\omega_9^2 + 32\omega_6c_s^2\omega_{13}\omega_9 + 17\omega_6^2\omega_{13}\omega_9^3 + 68\omega_6\omega_{13}v_1^2\omega_9^3 + 56\omega_6^2c_s^2\omega_{13}\omega_9^2 + 8\omega_6\omega_9^3 + 16\omega_6^2v_1^2\omega_9^3 + \\
& 48\omega_6^2c_s^2\omega_{13} - 25\omega_6^2c_s^2\omega_{13}\omega_9^3 - 28\omega_{13}v_1^2\omega_9^3 - 48\omega_6\omega_{13}v_1^2\omega_9^2 - 40\omega_6^2\omega_{13}\omega_9^2 + 24\omega_6^2\omega_{13}\omega_9 + 12\omega_{13}\omega_9^3 + 20c_s^2\omega_{13}\omega_9^2 + 16\omega_6^2c_s^2\omega_9^2 - 44\omega_6c_s^2\omega_{13}\omega_9^2 + \\
& 43\omega_6^2\omega_{13}^2v_1^2\omega_9^2 - 24\omega_6\omega_{13}^2\omega_9 - 32\omega_6^2c_s^2\omega_{13}\omega_9 - 16\omega_6^2c_s^2\omega_9^2 - 43\omega_6^2\omega_{13}v_1^2\omega_9^3 - 20c_s^2\omega_{13}\omega_9^3 - 16\omega_6c_s^2\omega_{13}\omega_9^2 - 12\omega_{13}^2\omega_9^3 + 64\omega_6\omega_{13}^2v_1^2\omega_9 - \\
& 72\omega_6^2c_s^2\omega_{13}\omega_9 - 16\omega_6c_s^2\omega_9^3 + 44\omega_6c_s^2\omega_{13}\omega_9^3 + 48\omega_6^2\omega_{13}^2\omega_9 + 104\omega_6^2\omega_{13}v_1^2\omega_9^2 - 32\omega_6^2\omega_{13} - 8\omega_6^2\omega_9^3 + 28\omega_{13}^2v_1^2\omega_9^2 - 28\omega_6\omega_{13}\omega_9^3 - 17\omega_6^2\omega_{13}\omega_9^2 - \\
& 64\omega_6^2\omega_{13}v_1^2\omega_9 + 80\omega_6^2\omega_{13}^2v_1^2 - 16\omega_6v_1^2\omega_9^3 + 8\omega_6^2\omega_9^2 + 16\omega_6\omega_{13}\omega_9^2 + 25\omega_6^2c_s^2\omega_{13}\omega_9^2 - 68\omega_6\omega_{13}^2v_1^2\omega_9
\end{aligned}$$

$$\begin{aligned}
C_{30} = & -81\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9^3 - 24\omega_6c_s^4\omega_{13}\omega_9^3 - 24\omega_6^2\omega_{13}v_1^4\omega_9^2 - 19\omega_6^2\omega_{13}^2v_1^2\omega_9^2 - 12\omega_6^2c_s^2v_1^2\omega_9^3 - 21\omega_6^2c_s^2\omega_{13}v_1^2\omega_9^3 - 12\omega_6^3v_1^4\omega_9^2 - 36\omega_6^3\omega_{13}v_1^4\omega_9 - \\
& 48\omega_6c_s^2\omega_{13}^2v_1^2\omega_9^2 + 24\omega_6\omega_{13}^2v_1^2\omega_9^3 + 6\omega_6^2c_s^4\omega_{13}\omega_9^3 - 12\omega_6^2c_s^2\omega_{13}\omega_9^2 + 48\omega_6^2\omega_{13}^2v_1^4\omega_9^3 - 4\omega_6^2\omega_{13}^2v_1^2\omega_9^3 + 12c_s^4\omega_{13}^2\omega_9^3 + 162\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9^2 + 12\omega_6^2v_1^2\omega_9^3 + \\
& 18\omega_6^2c_s^2\omega_{13}\omega_9^3 + 102\omega_6c_s^2\omega_{13}^2v_1^2\omega_9^3 - 6\omega_6^2c_s^4\omega_{13}\omega_9^2 + 12\omega_6^2c_s^4\omega_{13} + 54\omega_6^2c_s^2\omega_{13}v_1^2\omega_9^2 + 12\omega_6^2v_1^4\omega_9^3 + 6\omega_6c_s^2\omega_{13}^2\omega_9^3 - 27\omega_6^3\omega_{13}v_1^4\omega_9^3 + 18\omega_6^2\omega_{13}^2v_1^2\omega_9^3 - \\
& 36\omega_6^3c_s^2\omega_{13}v_1^2\omega_9 - 12\omega_6^2c_s^2v_1^2\omega_9^2 - 72\omega_6^2\omega_{13}^2v_1^2\omega_9 + 12\omega_6^2c_s^4\omega_{13}\omega_9^2 - 6\omega_6^2c_s^2\omega_{13}\omega_9^3 + 60\omega_6^2\omega_{13}^2v_1^2\omega_9 + 12\omega_6^2c_s^2v_1^2\omega_9^3 - 12\omega_6^2\omega_{13}^2v_1^2\omega_9^2 - \\
& 48c_s^2\omega_{13}^2v_1^2\omega_9^3 + 6\omega_6^2c_s^2\omega_{13}\omega_9^2 + 12\omega_6\omega_{13}^2v_1^4\omega_9^3 - 18\omega_6^2c_s^4\omega_{13}\omega_9^3 + 90\omega_6^2\omega_{13}^2v_1^2\omega_9 + 4\omega_6^3\omega_{13}^2v_1^4\omega_9^3 - 48\omega_6^2\omega_{13}^2v_1^2\omega_9^3 - 306\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9 + \\
& 72\omega_6^3\omega_{13}^2v_1^4 - 12\omega_6^2v_1^4\omega_9^3 + 12\omega_6^2c_s^2\omega_{13}\omega_9^2 + 13\omega_6^2c_s^4\omega_{13}\omega_9^3 - \omega_6^2c_s^2\omega_{13}\omega_9^2 - 12\omega_6^2c_s^2\omega_{13} - 12\omega_6^3v_1^2\omega_9^3 - 12\omega_6^3c_s^4\omega_{13}\omega_9^2 - 12\omega_6c_s^2\omega_{13}\omega_9^3 + \\
& 252\omega_6^2c_s^2\omega_{13}^2v_1^2 + 19\omega_6^3\omega_{13}^2v_1^4\omega_9 + 24\omega_6^2\omega_{13}^2v_1^2\omega_9^2 + 12\omega_6^2v_1^2\omega_9^2 + 36\omega_6^2\omega_{13}^2v_1^2\omega_9^3 - 24\omega_6\omega_{13}^2v_1^4\omega_9^3 + 6\omega_6^2c_s^4\omega_{13}\omega_9^2 + 12\omega_6^2\omega_{13}^2v_1^4\omega_9^2 - 60\omega_6^2\omega_{13}^2v_1^2\omega_9^2 + \\
& 30\omega_6^2c_s^2\omega_{13}^2v_1^2\omega_9^3 - 12\omega_6^2c_s^2\omega_{13}\omega_9^2 + \omega_6^2c_s^4\omega_{13}\omega_9^2 - 5\omega_6^2c_s^2\omega_{13}\omega_9^3 - 12\omega_6^2\omega_{13}^2v_1^2\omega_9^3$$

[illegible]

$$C_{36} = -4\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8\omega_5^3\omega_9 + 12\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5\omega_9^2 + 2\omega_{12}^2\omega_6^2\omega_{13}\omega_{14}\omega_8\omega_5^2\omega_9^2 + 4\omega_{12}^2\omega_6^2\omega_{13}\omega_{14}\omega_8\omega_5^2\omega_9^2 - 4\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^3\omega_9 - 4\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^3\omega_9^2 - 2\omega_{12}^2\omega_6^2\omega_{13}\omega_{14}\omega_8^2\omega_5^2\omega_9^2 + 8\omega_{12}^2\omega_6\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^2\omega_9^2 + 4\omega_{12}\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^3\omega_9^2 - 10\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8\omega_5^2\omega_9^2 + 2\omega_{12}^2\omega_6\omega_{13}\omega_{14}\omega_8\omega_5^3\omega_9^2 - 4\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^3\omega_9^2 + 4\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^3\omega_9 + 4\omega_{12}^2\omega_6\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^3\omega_9^2 - 2\omega_{12}^2\omega_6^2\omega_{13}\omega_{14}\omega_8\omega_5^3\omega_9^2 - 4\omega_{12}^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^2\omega_9^2 - 8\omega_{12}^2\omega_6\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^2\omega_9 - 8\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8^2\omega_5^2\omega_9 + 4\omega_{12}^2\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8\omega_5^2\omega_9 - 8\omega_{12}\omega_6^2\omega_{13}\omega_{7\omega_{14}}\omega_8\omega_5^3\omega_9 -$$

$$\begin{aligned}
& 4w_{12}^2w_6^2w_7w_8w_5^3w_9 + 4w_{12}^2w_6^2w_{13}w_7w_8w_5^3w_9 - 4w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 5w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 - 8w_{12}w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 - \\
& 4w_{12}w_6^2w_{13}w_7w_8w_5^3w_9 + 4w_{12}w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 8w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_{12}w_6w_{13}w_7w_{14}w_8w_5^3w_9 - 4w_{12}^2w_6w_{13}w_7w_8w_5^3w_9 - \\
& 4w_{12}^2w_6^2w_{13}w_7w_8w_5^3w_9 - 2w_{12}^2w_6^2w_{13}w_{14}w_8w_5^3w_9 - 4w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 - 4w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 - 2w_{12}^2w_6w_{13}w_7w_{14}w_8w_5^3w_9 - \\
& 4w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_{12}w_6w_{13}w_7w_{14}w_8w_5^3w_9 - 8w_{12}w_6w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_{12}^2w_{13}w_7w_{14}w_8w_5^3w_9 + 2w_{12}^2w_6^2w_{13}w_{14}w_8w_5^3w_9 + \\
& 4w_{12}^2w_6w_{13}w_{14}w_8w_5^3w_9 + 4w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 6w_{12}^2w_{13}w_7w_{14}w_8w_5^3w_9 - 4w_{12}^2w_6w_{13}w_7w_{14}w_8w_5^3w_9 + \\
& 4w_{12}^2w_6w_{13}w_7w_{14}w_8w_5^3w_9 + 2w_{12}^2w_6w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 - 5w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 2w_{12}^2w_6w_{13}w_7w_{14}w_8w_5^3w_9 - \\
& 4w_{12}w_6w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_{12}^2w_6w_{13}w_7w_{14}w_8w_5^3w_9 + 2w_{12}^2w_6^2w_{13}w_7w_{14}w_8w_5^3w_9 + 4w_{12}^2w_6^2w_{13}w_7w_8w_5^3w_9 + 4w_{12}^2w_6^2w_{13}w_7w_8w_5^3w_9 -
\end{aligned}$$

[illegible]

$$\begin{aligned}
& 7\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + \omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 - 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 4\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 4\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + \\
& 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 4\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + 8\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 4\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 6\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + \\
& 2\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 5\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 2\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 9\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 4\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - \\
& 2\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - \omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + 2\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 - \omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 4\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + \\
& \omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 15\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 4\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 2\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + \\
& 2\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 4\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 8\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 2\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 4\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 4\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + \\
& 4\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^3 - 2\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 + 7\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 2\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9^3 - 2\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3 - 4\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^3
\end{aligned}$$

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$$\begin{aligned}
& (-2 + \omega_7) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_5} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_5) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_5} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\
& (-2 - \omega_{10} v_2^2 - 3c_s^2 \omega_{10} + 6c_s^2 + \omega_{10} + 2v_2^2) \frac{v_2 \delta_l^2}{2\delta_t \omega_{10}} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 - 3\omega_{10} v_2^2 - c_s^2 \omega_{10} + 2c_s^2 + \omega_{10} + 6v_2^2) \frac{\rho \delta_l^2}{2\delta_t \omega_{10}} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_7) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_7) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_3^2} + C_1 \frac{v_1 v_2 \delta_l^3}{12\omega_{12} \delta_t \omega_5 \omega_9} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{\rho v_2 \delta_l^3}{12\omega_{12} \delta_t \omega_5 \omega_9} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{\rho v_1 \delta_l^3}{6\omega_{12} \delta_t \omega_5^2} \frac{\partial^3 v_2}{\partial x_1^3} + \\
& (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_5^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + (-2\omega_{12} + \omega_{12} \omega_5 - \omega_5^2 + 2\omega_5) \frac{c_s^2 \rho v_1 \delta_l^3}{\omega_{12} \delta_t \omega_5^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + \\
& (-\omega_{10} \omega_5^2 \omega_{15} + 12\omega_{10} \omega_5 - 12\omega_5 \omega_{15} - 12\omega_{10} \omega_5^2 - 12\omega_{10} \omega_{15} + 12\omega_5^2 + 12\omega_{10} \omega_5 \omega_{15}) \frac{c_s^2 \rho v_2 \delta_l^3}{6\delta_t \omega_{10} \omega_5^2 \omega_{15}} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& C_4 \frac{v_1 v_2 \delta_l^3}{\delta_t \omega_{10}^2 \omega_5 \omega_{15}} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + C_5 \frac{\rho v_2 \delta_l^3}{12\delta_t \omega_{10}^2 \omega_5^2 \omega_{15}} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_6 \frac{\rho v_1 \delta_l^3}{\delta_t \omega_{10}^2 \omega_5 \omega_{15}} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_7 \frac{\delta_l^3}{12\delta_t \omega_{10}^2} \frac{\partial^3 \rho}{\partial x_2^3} + \\
& (-24 - 60\omega_{10} v_2^2 - 36c_s^2 \omega_{10} + 5c_s^2 \omega_{10}^2 + 36c_s^2 + 24\omega_{10} - 4\omega_{10}^2 + 60v_2^2 + 11\omega_{10}^2 v_2^2) \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_{10}^2} \frac{\partial^3 v_2}{\partial x_2^3} + \\
& (-\omega_7 \omega_5^2 + \omega_7 \omega_5 - \omega_8 \omega_5 + \omega_7 \omega_8 \omega_5 - \omega_7 \omega_8 + \omega_5^2) \frac{v_3 c_s^2 \rho \delta_l^3}{\delta_t \omega_7 \omega_8 \omega_5^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} + \\
& (6\omega_6 \omega_5 + 6\omega_6 \omega_7 - 6\omega_8 \omega_5 + 6\omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_6 \omega_7 \omega_5) \frac{c_s^2 \rho v_2 \delta_l^3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& (-\omega_7 \omega_5^2 + \omega_7 \omega_5 - \omega_8 \omega_5 + \omega_7 \omega_8 \omega_5 - \omega_7 \omega_8 + \omega_5^2) \frac{v_3 c_s^2 \rho \delta_l^3}{\delta_t \omega_7 \omega_8 \omega_5^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\
& (\omega_7 \omega_5 - \omega_8 \omega_5 + \omega_7^2 + \omega_7 \omega_8 \omega_5 - \omega_7 \omega_8 - \omega_7^2 \omega_5) \frac{c_s^2 \rho v_1 \delta_l^3}{\delta_t \omega_7^2 \omega_8 \omega_5} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{v_3 v_2 \delta_l^3}{\delta_t \omega_{16} \omega_{10}^2 \omega_7} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_9 \frac{v_3 \rho \delta_l^3}{\delta_t \omega_{16} \omega_{10}^2 \omega_7} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} \\
& + C_{10} \frac{\rho v_2 \delta_l^3}{12\delta_t \omega_{16} \omega_{10}^2 \omega_7^2} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\
& (6\omega_6 \omega_5 + 6\omega_6 \omega_7 - 6\omega_8 \omega_5 + 6\omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_6 \omega_7 \omega_5) \frac{c_s^2 \rho v_2 \delta_l^3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (\omega_7 \omega_5 - \omega_8 \omega_5 + \omega_7^2 + \omega_7 \omega_8 \omega_5 - \omega_7 \omega_8 - \omega_7^2 \omega_5) \frac{c_s^2 \rho v_1 \delta_l^3}{\delta_t \omega_7^2 \omega_8 \omega_5} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + (-12 + 12\omega_7 - \omega_7^2) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_2^2} + \\
& (-12\omega_{16} \omega_7 - 12\omega_{16} \omega_{10} + 12\omega_{10} \omega_7 - 12\omega_{10} \omega_7^2 + 12\omega_7^2 - \omega_{16} \omega_{10} \omega_7^2 + 12\omega_{16} \omega_{10} \omega_7) \frac{c_s^2 \rho v_2 \delta_l^3}{6\delta_t \omega_{16} \omega_{10}^2 \omega_7^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_2^2} + \\
& (-2\omega_{19} + 2\omega_7 - \omega_7^2 + \omega_{19} \omega_7) \frac{v_3 c_s^2 \rho \delta_l^3}{\omega_{19} \delta_t \omega_7^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_2^2} + C_{11} \frac{v_3 v_2 \delta_l^3}{12\omega_{19} \delta_t \omega_7 \omega_{11}} \frac{\partial^3 \rho}{\partial x_3^3} + C_{12} \frac{v_3 \rho \delta_l^3}{6\omega_{19} \delta_t \omega_7^2} \frac{\partial^3 v_2}{\partial x_3^3} + C_{13} \frac{\rho v_2 \delta_l^3}{12\omega_{19} \delta_t \omega_7 \omega_{11}} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_{14} \frac{v_2 \delta_l^4}{24\omega_{12}^2 \delta_t \omega_5^2 \omega_9} \frac{\partial^4 \rho}{\partial x_1^4} + C_{15} \frac{\rho v_1 v_2 \delta_l^4}{12\omega_{12}^2 \delta_t \omega_5^2 \omega_9} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{24\omega_{12}^2 \delta_t \omega_5^2}{\delta_l^4} \frac{\partial^4 v_2}{\partial x_1^4} + C_{17} \frac{v_1 \delta_l^4}{12\omega_{12}^2 \delta_t \omega_{10} \omega_5^2 \omega_{21} \omega_{15} \omega_9} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_{18} \frac{\rho \delta_l^4}{12\omega_{12}^2 \delta_t \omega_{10} \omega_5^2 \omega_{21} \omega_{15} \omega_9} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{\rho v_1 v_2 \delta_l^4}{12\omega_{12}^2 \delta_t \omega_{10}^3 \omega_5^2 \omega_{21} \omega_{15} \omega_9} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{20} \frac{12\omega_{12} \delta_t \omega_{10}^3 \omega_5^2 \omega_{21} \omega_{15}^2}{v_2 \delta_l^4} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& C_{21} \frac{\rho v_1 v_2 \delta_l^4}{2\omega_{12}^2 \delta_t \omega_{10}^3 \omega_5^2 \omega_{21} \omega_{15} \omega_9} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{\rho \delta_l^4}{12\omega_{12} \delta_t \omega_{10}^3 \omega_5^2 \omega_{21} \omega_{15}^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{v_1 \delta_l^4}{4\delta_t \omega_{10}^3 \omega_5^2 \omega_{15}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2} + \\
& C_{24} \frac{\rho \delta_l^4}{12\delta_t \omega_{10}^3 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{25} \frac{\rho v_1 v_2 \delta_l^4}{4\delta_t \omega_{10}^3 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} + C_{26} \frac{v_2 \delta_l^4}{12\delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_2^4} + C_{27} \frac{\rho \delta_l^4}{12\delta_t \omega_{10}^3} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& C_{28} \frac{v_3 v_1 v_2 \delta_l^4}{4\omega_{12}^2 \omega_6 \delta_t \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{29} \frac{v_3 \rho v_2 \delta_l^4}{4\omega_{12}^2 \omega_6 \delta_t \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{30} \frac{2\omega_{12}^2 \delta_t \omega_7^2 \omega_{14} \omega_8^2 \omega_5^3}{v_3 \rho v_1 \delta_l^4} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_3} + \\
& C_{31} \frac{\rho v_1 v_2 \delta_l^4}{12\omega_{12}^2 \omega_6^2 \delta_t \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{32} \frac{2v_3 c_s^4 \delta_l^4}{\delta_t \omega_7^2 \omega_8^2 \omega_5^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{33} \frac{v_3 c_s^2 \rho v_1 \delta_l^4}{\omega_{12}^2 \delta_t \omega_7^2 \omega_{14} \omega_8^2 \omega_5^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{34} \frac{v_3 c_s^2 \rho v_2 \delta_l^4}{2\omega_6 \delta_t \omega_{16} \omega_{10}^2 \omega_7^2 \omega_8^2 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{35} \frac{c_s^2 \rho \delta_l^4}{12\omega_{12} \omega_6^2 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^3 \omega_{15}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{36} \frac{v_3 v_1 v_2 \delta_l^4}{\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{37} \frac{v_3 \rho v_2 \delta_l^4}{2\omega_6 \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{38} \frac{v_3 \rho v_1 \delta_l^4}{\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} \\
& + C_{39} \frac{\rho v_1 v_2 \delta_l^4}{2\omega_6 \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{40} \frac{v_3 \delta_l^4}{4\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{41} \frac{v_3 \rho v_2 \delta_l^4}{4\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& C_{42} \frac{\rho \delta_l^4}{12\delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + C_{43} \frac{\delta_l^4}{12\omega_{12} \omega_6^2 \omega_{19} \delta_t \omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{44} \frac{\rho \delta_l^4}{4\omega_{12} \omega_6^2 \omega_{19} \delta_t \omega_{13} \omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^2 \omega_9} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + \\
& C_{45} \frac{\rho \delta_l^4}{4\omega_{12} \omega_{19} \delta_t \omega_7^2 \omega_{20} \omega_{14} \omega_8^2 \omega_5^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + C_{46} \frac{v_3 \rho \delta_l^4}{2\omega_{12} \omega_6^2 \omega_{19} \delta_t \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{47} \frac{\delta_l^4}{2\omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{48} \frac{\rho \delta_l^4}{12\omega_6^2 \omega_{19} \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{49} \frac{\rho v_2 \delta_l^4}{2\omega_6 \omega_{19} \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{50} \frac{\rho \delta_l^4}{2\omega_{19}^2 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{51} \frac{v_2 \delta_l^4}{12\omega_{19} \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{23}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{52} \frac{\rho \delta_l^4}{12\omega_{19} \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{23}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{53} \frac{v_3 \rho v_2 \delta_l^4}{2\omega_{19}^2 \delta_t \omega_{16}^3 \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{54} \frac{v_3 v_1 v_2 \delta_l^4}{4\omega_6 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{55} \frac{v_3 \rho v_2 \delta_l^4}{12\omega_6^2 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8^2 \omega_5^2 \omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{56} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_8^2 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^3} + \\
& C_{57} \frac{\rho v_1 v_2 \delta_l^4}{4\omega_6 \omega_{19}^2 \delta_t \omega_7^2 \omega_{20} \omega_{11}^2 \omega_8 \omega_5 \omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{58} \frac{v_3 \delta_l^4}{12\omega_{19}^2 \delta_t \omega_{16} \omega_{10} \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{59} \frac{v_3 \rho v_2 \delta_l^4}{12\omega_{19}^2 \delta_t \omega_{16}^2 \omega_{10}^3 \omega_7^2 \omega_{23} \omega_{11}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} +
\end{aligned}$$

$$C_{60} \frac{\rho \delta_1^4}{12\omega_{19}^2 \delta_t \omega_{16} \omega_{10} \omega_7^3 \omega_{23}^2 \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{61} \frac{v_2 \delta_1^4}{24\omega_{19}^2 \delta_t \omega_7^2 \omega_{11}^2} \frac{\partial^4 \rho}{\partial x_3^4} + C_{62} \frac{\rho \delta_1^4}{24\omega_{19}^2 \delta_t \omega_7^3} \frac{\partial^4 v_2}{\partial x_3^4} + C_{63} \frac{v_3 \rho v_2 \delta_1^4}{12\omega_{19}^2 \delta_t \omega_7^2 \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_3^4} = 0,$$

where:

$$C_1 = -12\omega_{12} + 12\omega_{12}v_1^2 + 6\omega_{12}\omega_5 - 12v_1^2\omega_9 + 3\omega_{12}c_s^2\omega_5\omega_9 - 6\omega_5\omega_9 - 36c_s^2\omega_9 + 6v_1^2\omega_5\omega_9 - 6\omega_{12}v_1^2\omega_5 + 18c_s^2\omega_5\omega_9 - \omega_{12}\omega_5\omega_9 + 36\omega_{12}c_s^2 + \omega_{12}v_1^2\omega_5\omega_9 - 18\omega_{12}c_s^2\omega_5 + 12\omega_9$$

$$C_2 = -12\omega_{12} + 36\omega_{12}v_1^2 + 6\omega_{12}\omega_5 - 36v_1^2\omega_9 + \omega_{12}c_s^2\omega_5\omega_9 - 6\omega_5\omega_9 - 12c_s^2\omega_9 + 18v_1^2\omega_5\omega_9 - 18\omega_{12}v_1^2\omega_5 + 6c_s^2\omega_5\omega_9 - \omega_{12}\omega_5\omega_9 + 12\omega_{12}c_s^2 + 3\omega_{12}v_1^2\omega_5\omega_9 - 6\omega_{12}c_s^2\omega_5 + 12\omega_9$$

$$C_3 = 3v_1^2\omega_5^2 - 3\omega_{12}\omega_5 - 6c_s^2\omega_5 + \omega_{12}\omega_5^2 - 6v_1^2\omega_5 + 3c_s^2\omega_5^2 - 3\omega_{12}c_s^2\omega_5^2 + 3\omega_{12}v_1^2\omega_5 - 12\omega_{12}c_s^2 - 3\omega_5^2 + 6\omega_5 + 15\omega_{12}c_s^2\omega_5 - \omega_{12}v_1^2\omega_5^2$$

$$C_4 = \omega_{10}\omega_5 + 3c_s^2\omega_{10}^2\omega_5 - 3c_s^2\omega_{10}^2 + \omega_{10}^2v_2^2\omega_5 - \omega_5\omega_{15} - \omega_{10}\omega_{15} - 3c_s^2\omega_{10}\omega_5\omega_{15} + 3c_s^2\omega_5\omega_{15} + v_2^2\omega_5\omega_{15} - \omega_{10}v_2^2\omega_5 + \omega_{10}^2 + 3c_s^2\omega_{10}\omega_{15} - 3c_s^2\omega_{10}\omega_5 + \omega_{10}\omega_5\omega_{15} - \omega_{10}^2\omega_5 - \omega_{10}v_2^2\omega_5\omega_{15} + \omega_{10}v_2^2\omega_{15} - \omega_{10}^2v_2^2$$

$$C_5 = 6\omega_{10}\omega_5^2\omega_{15} - 6\omega_{10}v_2^2\omega_5^2\omega_{15} + 12\omega_{10}^2v_2^2\omega_5^2 - 6\omega_{10}^2\omega_5\omega_{15} - 12c_s^2\omega_{10}^2\omega_5 + 12c_s^2\omega_{10}^2\omega_5^2 - 11c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 12\omega_{10}^2v_2^2\omega_5 - 24c_s^2\omega_{10}^2\omega_{15} + 12\omega_{10}\omega_5^2 + 6\omega_{10}^2v_2^2\omega_5\omega_{15} + 12v_2^2\omega_5^2\omega_{15} + 36c_s^2\omega_5^2\omega_{15} - 24c_s^2\omega_{10}\omega_5\omega_{15} - 12\omega_{10}^2\omega_5^2 - 3\omega_{10}^2v_2^2\omega_5^2\omega_{15} - 18c_s^2\omega_{10}\omega_5^2\omega_{15} - 12c_s^2\omega_{10}\omega_5^2 + 42c_s^2\omega_{10}^2\omega_5\omega_{15} - 12\omega_5^2\omega_{15} + 3\omega_{10}^2\omega_5^2\omega_{15} - 12\omega_{10}v_2^2\omega_5^2 + 12\omega_{10}^2\omega_5$$

$$C_6 = \omega_{10}\omega_5 + c_s^2\omega_{10}\omega_5 - c_s^2\omega_{10}^2 + 3\omega_{10}^2v_2^2\omega_5 - \omega_5\omega_{15} - \omega_{10}\omega_{15} - c_s^2\omega_{10}\omega_5\omega_{15} + c_s^2\omega_5\omega_{15} + 3v_2^2\omega_5\omega_{15} - 3\omega_{10}v_2^2\omega_5 + \omega_{10}^2 + c_s^2\omega_{10}\omega_{15} - c_s^2\omega_{10}\omega_5 + \omega_{10}\omega_5\omega_{15} - \omega_{10}^2\omega_5 - 3\omega_{10}v_2^2\omega_5\omega_{15} + 3\omega_{10}v_2^2\omega_{15} - 3\omega_{10}^2v_2^2$$

$$C_7 = 36\omega_{10}v_2^2 + 36v_2^4 + 144c_s^2v_2^2 + 7\omega_{10}^2v_2^4 + 24c_s^2\omega_{10}^2v_2^2 + 12c_s^2\omega_{10} - c_s^2\omega_{10}^2 - 12c_s^2 - 12c_s^4\omega_{10} + 12c_s^4 - 36\omega_{10}v_2^4 - 36v_2^2 - 144c_s^2\omega_{10}v_2^2 + c_s^4\omega_{10}^2 - 7\omega_{10}^2v_2^2$$

$$C_8 = 3c_s^2\omega_{10}^2\omega_7 - \omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7v_2^2 - \omega_{16}\omega_{10} + \omega_{10}\omega_7 + \omega_{10}^2\omega_7v_2^2 - 3c_s^2\omega_{16}\omega_{10}\omega_7 - 3c_s^2\omega_{10}^2 + \omega_{10}^2 + \omega_{16}\omega_7v_2^2 + 3c_s^2\omega_{16}\omega_7 - \omega_{10}^2\omega_7 + \omega_{16}\omega_{10}\omega_7 + \omega_{16}\omega_{10}v_2^2 - 3c_s^2\omega_{10}\omega_7 + 3c_s^2\omega_{16}\omega_{10} - \omega_{10}\omega_7v_2^2 - \omega_{10}^2v_2^2$$

$$C_9 = c_s^2\omega_{10}^2\omega_7 - \omega_{16}\omega_7 - 3\omega_{16}\omega_{10}\omega_7v_2^2 - \omega_{16}\omega_{10} + \omega_{10}\omega_7 + 3\omega_{10}^2\omega_7v_2^2 - c_s^2\omega_{16}\omega_{10}\omega_7 - c_s^2\omega_{10}^2 + \omega_{10}^2 + 3\omega_{16}\omega_7v_2^2 + c_s^2\omega_{16}\omega_7 - \omega_{10}^2\omega_7 + \omega_{16}\omega_{10}\omega_7 + 3\omega_{16}\omega_{10}v_2^2 - c_s^2\omega_{10}\omega_7 + c_s^2\omega_{16}\omega_{10} - 3\omega_{10}\omega_7v_2^2 - 3\omega_{10}^2v_2^2$$

$$C_{10} = -12c_s^2\omega_{10}^2\omega_7 - 12\omega_{10}\omega_7^2v_2^2 - 3\omega_{16}\omega_{10}^2\omega_7^2v_2^2 - 12\omega_{10}^2\omega_7v_2^2 - 6\omega_{16}\omega_{10}^2\omega_7 - 18c_s^2\omega_{16}\omega_{10}\omega_7^2 + 3\omega_{16}\omega_{10}^2\omega_7^2 - 24c_s^2\omega_{16}\omega_{10}\omega_7 + 12\omega_{16}\omega_7^2v_2^2 + 12\omega_{10}\omega_7^2 + 12c_s^2\omega_{10}^2\omega_7^2 - 12\omega_{16}\omega_7^2 - 12c_s^2\omega_{10}\omega_7^2 - 24c_s^2\omega_{16}\omega_{10}^2 + 42c_s^2\omega_{16}\omega_{10}\omega_7 + 6\omega_{16}\omega_{10}\omega_7^2 + 36c_s^2\omega_{16}\omega_7^2 - 12\omega_{10}^2\omega_7^2 + 6\omega_{16}\omega_{10}^2\omega_7v_2^2 + 12\omega_{10}^2\omega_7 - 11c_s^2\omega_{16}\omega_{10}^2\omega_7^2 + 12\omega_{10}^2\omega_7^2v_2^2 - 6\omega_{16}\omega_{10}\omega_7^2v_2^2$$

$$C_{11} = 12v_3^2\omega_{19} + v_3^2\omega_{19}\omega_7\omega_{11} - 12\omega_{19} + 18c_s^2\omega_7\omega_{11} - 12v_3^2\omega_{11} + 36\omega_{19}c_s^2 - 18\omega_{19}c_s^2\omega_7 - 36c_s^2\omega_{11} + 12\omega_{11} - 6v_3^2\omega_{19}\omega_7 - \omega_{19}\omega_7\omega_{11} + 6v_3^2\omega_7\omega_{11} + 6\omega_{19}\omega_7 + 3\omega_{19}c_s^2\omega_7\omega_{11} - 6\omega_7\omega_{11}$$

$$C_{12} = -3\omega_{19}c_s^2\omega_7^2 - 6c_s^2\omega_7 + 6\omega_7 + 3c_s^2\omega_7^2 - 12\omega_{19}c_s^2 + 15\omega_{19}c_s^2\omega_7 - 3\omega_7^2 + 3v_3^2\omega_{19}\omega_7 + 3v_3^2\omega_7^2 + \omega_{19}\omega_7^2 - 3\omega_{19}\omega_7 - 6v_3^2\omega_7 - v_3^2\omega_{19}\omega_7^2$$

$$C_{13} = 36v_3^2\omega_{19} + 3v_3^2\omega_{19}\omega_7\omega_{11} - 12\omega_{19} + 6c_s^2\omega_7\omega_{11} - 36v_3^2\omega_{11} + 12\omega_{19}c_s^2 - 6\omega_{19}c_s^2\omega_7 - 12c_s^2\omega_{11} + 12\omega_{11} - 18v_3^2\omega_{19}\omega_7 - \omega_{19}\omega_7\omega_{11} + 18v_3^2\omega_7\omega_{11} + 6\omega_{19}\omega_7 + \omega_{19}c_s^2\omega_7\omega_{11} - 6\omega_7\omega_{11}$$

$$C_{14} = 48\omega_{12}c_s^4\omega_5\omega_9^2 + 24v_1^2\omega_5\omega_9^2 - 126\omega_{12}c_s^2v_1^2\omega_5^2\omega_9^2 + 14\omega_{12}^2c_s^4\omega_5^2\omega_9 - 30\omega_{12}v_1^4\omega_5^2\omega_9^2 - 12c_s^2\omega_5^2\omega_9^2 - 96\omega_{12}^2v_1^4\omega_5\omega_9 - 48\omega_{12}v_1^4\omega_9^2 - 24\omega_{12}v_1^2\omega_5^2\omega_9 - 216\omega_{12}c_s^2v_1^2\omega_5^2 + 36\omega_{12}^2v_1^2\omega_5^2 + \omega_{12}^2c_s^2\omega_5^2\omega_9^2 - 24\omega_{12}^2c_s^2\omega_5 - 48\omega_{12}^2v_1^2\omega_9 - 12\omega_{12}^2c_s^2v_1^2\omega_5^2\omega_9^2 - 24\omega_{12}^2c_s^2\omega_5\omega_9 - 48\omega_{12}c_s^2\omega_5\omega_9^2 - 72\omega_{12}^2v_1^2\omega_5 - 14\omega_{12}^2c_s^2\omega_5^2\omega_9 - 24v_1^4\omega_5\omega_9^2 + 150\omega_{12}^2c_s^2v_1^2\omega_5^2\omega_9 + 12\omega_{12}^2c_s^2\omega_5^2 + 30\omega_{12}v_1^2\omega_5^2\omega_9^2 - 24\omega_{12}c_s^4\omega_9^2 + 96\omega_{12}^2v_1^2\omega_5\omega_9 + 12c_s^4\omega_5^2\omega_9^2 + 24\omega_{12}v_1^4\omega_5^2\omega_9 - \omega_{12}^2c_s^2\omega_5^2\omega_9^2 + 72c_s^2v_1^2\omega_5^2\omega_9^2 + 72\omega_{12}c_s^2v_1^2\omega_5^2\omega_9 + 48\omega_{12}v_1^2\omega_9^2 - 48\omega_{12}v_1^4\omega_5\omega_9 - 3\omega_{12}^2v_1^4\omega_5^2\omega_9^2 - 36\omega_{12}^2v_1^4\omega_5^2 - 144\omega_{12}c_s^2v_1^2\omega_5\omega_9 - 144c_s^2v_1^2\omega_5\omega_9^2 + 48\omega_{12}^2v_1^4\omega_9 + 24\omega_{12}^2c_s^4\omega_5 + 12\omega_{12}c_s^2\omega_5^2\omega_9^2 + 12v_1^4\omega_5^2\omega_9^2 - 432\omega_{12}^2c_s^2v_1^2\omega_5\omega_9 + 48\omega_{12}^2c_s^2\omega_5\omega_9 - 96\omega_{12}v_1^2\omega_5\omega_9^2 - 24c_s^4\omega_5\omega_9^2 - 36\omega_{12}^2v_1^2\omega_5^2\omega_9 + 288\omega_{12}^2c_s^2v_1^2\omega_5 + 48\omega_{12}v_1^2\omega_5\omega_9 + 216\omega_{12}^2c_s^2v_1^2\omega_9 - 144\omega_{12}^2c_s^2v_1^2\omega_5^2 + 3\omega_{12}^2v_1^2\omega_5^2\omega_9^2 + 72\omega_{12}^2v_1^4\omega_5 - 12\omega_{12}c_s^4\omega_5^2\omega_9^2 + 24\omega_{12}^2c_s^4\omega_9 + 432\omega_{12}c_s^2v_1^2\omega_5\omega_9^2 - 48\omega_{12}^2c_s^4\omega_5\omega_9 - 12\omega_{12}^2c_s^4\omega_5^2 - 12v_1^2\omega_5^2\omega_9^2 + 96\omega_{12}v_1^4\omega_5\omega_9^2 + 36\omega_{12}^2v_1^4\omega_5^2\omega_9 + 24\omega_{12}c_s^2\omega_9^2 + 24c_s^2\omega_5\omega_9^2$$

$$C_{15} = -48v_1^2\omega_5\omega_9^2 + 21\omega_{12}\omega_5^2\omega_9^2 + 24c_s^2\omega_5^2\omega_9^2 + 36\omega_{12}v_1^2\omega_5^2\omega_9 + 36\omega_{12}\omega_9^2 + 24\omega_5\omega_9^2 - 60\omega_{12}^2v_1^2\omega_5^2 - 24\omega_{12}c_s^2\omega_5\omega_9 - 3\omega_{12}^2c_s^2\omega_5^2\omega_9^2 + 72\omega_{12}^2c_s^2\omega_5 + 84\omega_{12}^2v_1^2\omega_9 + 60\omega_{12}^2c_s^2\omega_9 + 120\omega_{12}c_s^2\omega_5\omega_9^2 + 120\omega_{12}^2v_1^2\omega_5 + 39\omega_{12}^2c_s^2\omega_5^2\omega_9 - 36\omega_{12}^2c_s^2\omega_5^2 - 51\omega_{12}v_1^2\omega_5^2\omega_9^2 + 72\omega_{12}^2\omega_5\omega_9 - 168\omega_{12}^2v_1^2\omega_5\omega_9 - 12\omega_{12}\omega_5^2\omega_9 - 84\omega_{12}v_1^2\omega_9^2 + 24\omega_{12}\omega_5\omega_9 - 33\omega_{12}c_s^2\omega_5^2\omega_9^2 - 120\omega_{12}^2c_s^2\omega_5\omega_9 + 168\omega_{12}v_1^2\omega_5\omega_9^2 - 25\omega_{12}^2\omega_5^2\omega_9 + 24\omega_{12}^2\omega_5^2 - 36\omega_{12}\omega_9 + 61\omega_{12}^2v_1^2\omega_5^2\omega_9 - 48\omega_{12}^2\omega_5 + 2\omega_{12}^2\omega_5^2\omega_9^2 - 72\omega_{12}v_1^2\omega_5\omega_9 - 5\omega_{12}^2v_1^2\omega_5^2\omega_9 + 12\omega_{12}c_s^2\omega_5^2\omega_9 - 12\omega_5^2\omega_9^2 - 72\omega_{12}\omega_5\omega_9^2 + 24v_1^2\omega_5^2\omega_9^2 - 60\omega_{12}c_s^2\omega_9^2 - 48c_s^2\omega_5\omega_9^2$$

$$C_{16} = -12v_1^2\omega_5^3 - 96\omega_{12}^2c_s^2v_1^2 + 6\omega_{12}c_s^4\omega_5^3 - 3\omega_{12}^2v_1^2\omega_5^3 - 24\omega_{12}c_s^4\omega_5^2 + 24v_1^2\omega_5^2 - 24\omega_{12}c_s^2v_1^2\omega_5 - 48\omega_{12}v_1^4\omega_5 + 24\omega_{12}^2v_1^2\omega_5^2 + 12\omega_{12}^2c_s^2\omega_5 - 24\omega_{12}^2v_1^2\omega_5 - 8\omega_{12}^2c_s^2\omega_5^2 + 24\omega_{12}c_s^4\omega_5 + 48\omega_{12}c_s^2v_1^2\omega_5^2 + 72\omega_{12}v_1^4\omega_5^2 + \omega_{12}^2c_s^2\omega_5^3 - 18\omega_{12}v_1^4\omega_5^3 - 12\omega_{12}c_s^2v_1^2\omega_5^3 + 24\omega_{12}c_s^2\omega_5^2 - 24v_1^4\omega_5^2 + 48\omega_{12}v_1^2\omega_5 - 24\omega_{12}^2v_1^4\omega_5^2 + 24\omega_{12}^2c_s^4 - 48\omega_{12}^2c_s^4\omega_5 + 12v_1^4\omega_5^3 - 6\omega_{12}c_s^2\omega_5^3 + 3\omega_{12}^2v_1^4\omega_5^3 + 156\omega_{12}^2c_s^2v_1^2\omega_5 - 3\omega_{12}^2c_s^4\omega_5^3 + 12c_s^2v_1^2\omega_5^3 - 72\omega_{12}^2c_s^2v_1^2\omega_5^2 + 18\omega_{12}v_1^2\omega_5^3 + 6\omega_{12}^2c_s^2v_1^2\omega_5^3 + 24\omega_{12}^2v_1^4\omega_5 - 24c_s^2v_1^2\omega_5^2 + 24\omega_{12}^2c_s^4\omega_5^2 - 24\omega_{12}c_s^2\omega_5^2 - 72\omega_{12}v_1^2\omega_5^2$$

$$C_{17} = -6\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21}\omega_{15} + 12\omega_{12}^2\omega_{10}v_2^2\omega_5^2\omega_{15}\omega_9^2 - 12\omega_{12}^2v_1^2v_2^2\omega_5^3\omega_{21}\omega_9 - 36\omega_{12}^2c_s^4\omega_{10}\omega_5^2\omega_{15}\omega_9^2 + 3\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9^2 + 36\omega_{12}c_s^2\omega_{10}v_2^2\omega_5^2\omega_{15}\omega_9^2 + 27\omega_{12}^2c_s^2\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + 156\omega_{12}^2c_s^4\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9^2 + 12\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5^3\omega_{21}\omega_9 - 72\omega_{12}^2c_s^2\omega_{10}v_2^2\omega_5\omega_{21}\omega_{15}\omega_9^2 - 36c_s^2\omega_{10}v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9^2 + 12\omega_{12}^2c_s^2\omega_{10}v_1^2\omega_5^3\omega_{21}\omega_9 + 12\omega_{12}^2c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9^2 - 12\omega_{12}^2c_s^2\omega_{10}v_2^2\omega_5\omega_{21}\omega_{15}\omega_9 + 36\omega_{12}^2c_s^4\omega_5^3\omega_9^2 - 12\omega_{12}\omega_{10}v_1^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 15\omega_{12}c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9^2 + 12\omega_{12}\omega_{10}v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + 12\omega_{12}^2c_s^2\omega_{10}v_1^2\omega_5^2\omega_9^2 - 12\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5^2\omega_{15}\omega_9^2 + 6\omega_{12}^2\omega_{10}v_2^2\omega_5^3\omega_{21}\omega_{15} + 12\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5^2\omega_9^2 + 24\omega_{12}^2\omega_{10}v_1^2v_2^2\omega_5\omega_{21}\omega_{15}\omega_9 - 12\omega_{12}^2c_s^2\omega_{10}v_1^2\omega_5^2\omega_{15}\omega_9^2 - 12\omega_{12}^2c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_9 -$$

[illegible]

$$\begin{aligned}
C_{24} = & -12c_s^2\omega_{10}^3\omega_5\omega_{15} + 24\omega_{10}^3v_2^2\omega_5\omega_{15} - 12c_s^2\omega_{10}^3v_2^2\omega_5^2 + 6c_s^2\omega_{10}^3\omega_5^3\omega_{15} + 12\omega_{10}^3v_2^2\omega_5^3 - 36\omega_{10}^3v_2^4\omega_5^3\omega_{15} + 12\omega_{10}^3v_2^3\omega_5^3 - 306c_s^2\omega_{10}^3v_2^2\omega_5^3\omega_{15}^2 + \\
& 72v_2^3\omega_5^3\omega_{15}^2 + 12c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2 + 13c_s^4\omega_{10}^3v_2^2\omega_5^2\omega_{15}^2 - 12c_s^4\omega_{10}^3v_2^2\omega_5\omega_{15}^2 - 6c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2 + 12c_s^4\omega_{10}^3v_2^2\omega_5^3 + 12c_s^4\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 + 12\omega_{10}^3v_2^4\omega_5\omega_{15}^2 - 12\omega_{10}^3v_2^3\omega_5^2 + \\
& 10c_s^2\omega_{10}^3\omega_5^3\omega_{15} + 90\omega_{10}^3v_2^3\omega_5^3\omega_{15}^2 - 48c_s^2\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 - 12c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2 - 108c_s^2\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 - c_s^4\omega_{10}^3\omega_5^3\omega_{15}^2 - 24\omega_{10}^3v_2^4\omega_5\omega_{15}^2 + 36\omega_{10}^3v_2^2\omega_5^3\omega_{15} + \\
& 60c_s^2\omega_{10}^3v_2^2\omega_5\omega_{15}^2 - 12c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 - 72v_2^3\omega_5^2\omega_{15}^2 - 12c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 - 48c_s^2\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 - 12c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2 - 36c_s^2\omega_{10}^3v_2^3\omega_5^3\omega_{15}^2 - 18c_s^2\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 - \\
& 12\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 + 6c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 - c_s^2\omega_{10}^3\omega_5^3\omega_{15}^2 - 90\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 + 60c_s^2\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 - 6c_s^4\omega_{10}^3\omega_5^3\omega_{15}^2 + 24\omega_{10}^3v_2^4\omega_5\omega_{15}^2 + 4\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 + \\
& 12c_s^4\omega_{10}^3\omega_5\omega_{15}^2 - 5c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 + 60\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 + 18\omega_{10}^3v_2^2\omega_5^2\omega_{15}^2 + 12\omega_{10}^3v_2^2\omega_5^2 - 12c_s^2\omega_{10}^3v_2^2\omega_5^3 - 21c_s^2\omega_{10}^3v_2^3\omega_5^3\omega_{15}^2 + 48\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 - \\
& 19\omega_{10}^3v_2^3\omega_5^3\omega_{15}^2 + 6c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 - 12c_s^2\omega_{10}^3v_2^3\omega_5^2\omega_{15}^2 - 12\omega_{10}^3v_2^3\omega_{15}^2 + 12c_s^2\omega_{10}^3\omega_5^3\omega_{15}^2 - 81c_s^2\omega_{10}^3v_2^2\omega_5^2\omega_{15}^2 - 12\omega_{10}^3v_2^2\omega_5^3 - 6c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 + \\
& 27\omega_{10}^3v_2^2\omega_5^3\omega_{15}^2 + 12\omega_{10}^3v_2^4\omega_5^2\omega_{15}^2 + 30c_s^2\omega_{10}^3v_2^4\omega_5^2\omega_{15}^2 + 252c_s^2v_2^4\omega_5^2\omega_{15}^2 - 24\omega_{10}^3v_2^4\omega_5\omega_{15}^2 - 4\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 - 60\omega_{10}^3v_2^3\omega_5^3\omega_{15}^2 - 18\omega_{10}^3v_2^4\omega_5^2\omega_{15}^2 + \\
& 12\omega_{10}^3v_2^4\omega_5\omega_{15}^2 + 162c_s^2\omega_{10}^3v_2^4\omega_5^2\omega_{15}^2 - 48\omega_{10}^3v_2^2\omega_5^2\omega_{15}^2 + 19\omega_{10}^3v_2^4\omega_{15}^2 + 18c_s^2\omega_{10}^3v_2^4\omega_{15}^2 + 12c_s^2\omega_{10}^3v_2^2\omega_5^3\omega_{15}^2 + 12c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2 + \\
& 54c_s^2\omega_{10}^3v_2^2\omega_5^3\omega_{15}^2 + c_s^4\omega_{10}^3\omega_5^3\omega_{15}^2 - 24c_s^4\omega_{10}^3\omega_5\omega_{15}^2 - 27\omega_{10}^3v_2^4\omega_5^3\omega_{15}^2 - 12\omega_{10}^3v_2^2\omega_5^2\omega_{15}^2
\end{aligned}$$

$$C_{26} = 12 + 234\omega_{10}v_2^2 + 144v_4^2 + 672c_s^2v_2^2 + 90\omega_{10}^2v_4^2 + 404c_s^2\omega_{10}^2v_2^2 + 198c_s^2\omega_{10} - 78c_s^2\omega_{10}^2 - 132c_s^2 - 18\omega_{10} + 6c_s^2\omega_{10}^3 - 34c_s^2\omega_{10}^3v_2^2 - 9\omega_{10}^3v_2^4 - \omega_{10}^3 - 216c_s^4\omega_{10} + 144c_s^4 + 10\omega_{10}^3v_2^2 + 8\omega_{10}^2 - 5c_s^4\omega_{10}^3 - 216\omega_{10}v_4^2 - 156v_2^2 - 1008c_s^2\omega_{10}v_2^2 + 82c_s^4\omega_{10}^2 - 98\omega_{10}^2v_2^2$$

$$C_{32} = 2\omega_7\omega_8^2\omega_5^2 + \omega_7^2\omega_8\omega_5^3 - 2\omega_7^2\omega_8^2 + \omega_7\omega_5^3 - \omega_8^2\omega_5^2 - 2\omega_7^2\omega_8\omega_5^2 + \omega_7^2\omega_8\omega_5 - \omega_7\omega_8^2\omega_5 + 3\omega_7^2\omega_8^2\omega_5 - 2\omega_7\omega_8\omega_5^3 - \omega_7^2\omega_8^2\omega_5^2 + \omega_7^2\omega_5^2 + \omega_8\omega_5^3 - \omega_7^2\omega_5^3$$

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$$C_{36} = -\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2 + \omega_{16}^2\omega_{10}^2\omega_{17}^2v_2^2\omega_{18}\omega_{15} - 3c_s^2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 - \omega_{16}^2\omega_{10}^2\omega_{17}^2v_2^2\omega_{17}\omega_{18}\omega_{15}^2\omega_{15}^2 - 2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15} + \omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 + \omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 + 3c_s^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 + 6c_s^2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 - 3c_s^2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 + 3\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 + 3c_s^2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 + \omega_{16}^2\omega_{10}^2v_2^2\omega_{17}\omega_{18}\omega_{15}^2\omega_{15}^2 - 9c_s^2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 - 3c_s^2\omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{15}^2\omega_{15}^2 + \omega_{16}^2\omega_{10}^2\omega_{17}^2\omega_{18}\omega_{15}^2\omega_{15}^2 - \omega_{16}^2\omega_{10}^2\omega_{17}^2v_2^2\omega_{18}\omega_{15}^2\omega_{15}^2 + \omega_{16}^2\omega_{10}^2\omega_{17}^2v_2^2\omega_{17}\omega_{18}\omega_{15}^2\omega_{15}^2 - \omega_{16}^2\omega_{10}^2\omega_{17}^2v_2^2\omega_{17}\omega_{15}^2\omega_{15}^2 - \omega_{16}^2\omega_{10}^2\omega_{17}^2v_2^2\omega_{17}\omega_{18}\omega_{15}^2\omega_{15}^2 -$$

$$C_4 = -24\omega_{16}\omega_{10}\omega_7 + 17\omega_{16}\omega_{10}^3\omega_7^2 + 25c_s^2\omega_{16}\omega_{10}^3\omega_7^2 + 104\omega_{16}\omega_{10}^3\omega_7^2v_2^2 + 16c_s^2\omega_{10}^3\omega_7^2 + 16\omega_{16}\omega_{10}^3\omega_7 - 32c_s^2\omega_{16}\omega_{10}\omega_7^2 - 40\omega_{16}\omega_{10}^3\omega_7^2 + 48c_s^2\omega_{16}\omega_7^2 - 16c_s^2\omega_{10}^3\omega_7 - 68\omega_{16}\omega_{10}^3\omega_7v_2^2 - 28\omega_{16}\omega_{10}^3\omega_7^2 + 16\omega_{10}^3\omega_7^2v_2^2 - 28\omega_{16}\omega_{10}^3\omega_7 + 48\omega_{16}\omega_{10}\omega_7^2 - 44c_s^2\omega_{16}\omega_{10}\omega_7 - 16c_s^2\omega_{10}\omega_7^2 - 120\omega_{16}\omega_{10}^3\omega_7^2 + 68\omega_{16}\omega_{10}^3\omega_7v_2^2 + 12\omega_{16}\omega_{10}^3 + 20c_s^2\omega_{16}\omega_{10}^3 - 16\omega_{10}^3\omega_7v_2^2 + 32c_s^2\omega_{16}\omega_{10}\omega_7 - 25c_s^2\omega_{16}\omega_{10}^3\omega_7^2 - 17\omega_{16}\omega_{10}\omega_7^2 - 43\omega_{16}\omega_{10}^3\omega_7^2v_2^2 + 8\omega_{10}^3\omega_7 + 64\omega_{16}\omega_{10}\omega_7v_2^2 - 32\omega_{16}\omega_7^2 + 80\omega_{16}\omega_7^2v_2^2 - 16c_s^2\omega_{16}\omega_{10}\omega_7 + 24\omega_{16}\omega_{10}\omega_7^2 - 20c_s^2\omega_{16}\omega_{10}^3 - 12\omega_{16}\omega_{10}^3 + 8\omega_{10}^3\omega_7^2 + 43\omega_{16}\omega_{10}^3\omega_7^2v_2^2 - 48\omega_{16}\omega_{10}^3\omega_7v_2^2 + 28\omega_{16}\omega_{10}^3\omega_7^2 + 56c_s^2\omega_{16}\omega_{10}^3\omega_7^2 - 16\omega_{10}^3\omega_7^2v_2^2 - 8\omega_{10}^3\omega_7^2 - 64\omega_{16}\omega_{10}\omega_7^2v_2^2 + 44c_s^2\omega_{16}\omega_{10}^3\omega_7 - 72c_s^2\omega_{16}\omega_{10}\omega_7^2 + 28\omega_{16}\omega_{10}^3\omega_7$$

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$$\begin{aligned}
& 2\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_5^2 \omega_{15} + 4\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + 4\omega_6 v_{19}^3 \omega_{16} \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + \\
& 4\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + 2\omega_6 v_{19} v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} - 4\omega_6 v_{19} v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + \\
& 4\omega_6 v_{19} v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + 2\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + 2\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} - \\
& 4\omega_6 v_{19} v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + 4\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + 12\omega_6 v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} + \\
& 4\omega_6 v_{19} v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} - 2\omega_6 v_{19} v_{19} c_{s16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15} - 4\omega_6 v_{19}^3 \omega_{16} \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_{16}^2 \omega_7^2 v_{123} \omega_{20} \omega_{17} \omega_8^2 \omega_{15}^2 \omega_{15}
\end{aligned}$$

$$C_{61} = 288v_3^2\omega_{19}^2c_s^2\omega_7 - 36v_3^2\omega_{19}^2\omega_7^2\omega_{11} - 24c_s^4\omega_7\omega_{11}^2 + 36v_3^2\omega_{19}^2\omega_7^2 + 24\omega_{19}^2c_s^4\omega_7 - 126v_3^2\omega_{19}^2c_s^2\omega_7^2\omega_{11}^2 - 432v_3^2\omega_{19}^2c_s^2\omega_7\omega_{11} + 72v_3^2c_s^2\omega_7^2\omega_{11}^2 - 48v_3^4\omega_{19}\omega_{11}^2 - 24\omega_{19}c_s^4\omega_{11}^2 + 48v_3^2\omega_{19}\omega_7\omega_{11} - 30v_3^4\omega_{19}\omega_7^2\omega_{11}^2 - 12\omega_{19}c_s^4\omega_7^2\omega_{11}^2 - 216v_3^2\omega_{19}c_s^2\omega_{11}^2 + 72v_3^4\omega_{19}\omega_7 - 24\omega_{19}c_s^2\omega_{11} - 48\omega_{19}c_s^4\omega_7\omega_{11} - 12v_3^2\omega_7^2\omega_{11}^2 + 24v_3^4\omega_{19}\omega_7^2\omega_{11} + 24c_s^2\omega_7\omega_{11}^2 - 36v_3^4\omega_{19}^2\omega_7^2 - 96v_3^2\omega_{19}\omega_7\omega_{11}^2 + 48v_3^4\omega_{19}\omega_{11}^2 - 12\omega_{19}^2c_s^4\omega_7^2 + 72v_3^2\omega_{19}c_s^2\omega_7^2\omega_{11} - 96v_3^4\omega_{19}\omega_7\omega_{11} - 144v_3^2\omega_{19}^2c_s^2\omega_7^2 + 12\omega_{19}c_s^2\omega_7^2\omega_{11}^2 + 3v_3^2\omega_{19}\omega_7^2\omega_{11}^2 + 12v_3^4\omega_7^2\omega_{11}^2 - 72v_3^2\omega_{19}\omega_7 + 48\omega_{19}^2c_s^2\omega_7\omega_{11} - 144v_3^2\omega_{19}c_s^2\omega_7\omega_{11} + 24\omega_{19}^2c_s^2\omega_{11}^2 + 216v_3^2\omega_{19}^2c_s^2\omega_{11} - 12v_3^2\omega_{19}^2c_s^2\omega_7^2\omega_{11} + 36v_3^4\omega_{19}\omega_7^2\omega_{11} - 48\omega_{19}^2c_s^2\omega_7\omega_{11}^2 - 14\omega_{19}^2c_s^2\omega_7^2\omega_{11} + 24\omega_{19}^2c_s^4\omega_{11} - 24v_3^4\omega_7\omega_{11}^2 - 48v_3^4\omega_{19}\omega_7\omega_{11} - \omega_{19}^2c_s^4\omega_7^2\omega_{11}^2 - 12c_s^2\omega_7^2\omega_{11}^2 + 48v_3^4\omega_{19}\omega_{11} - 24\omega_{19}^2c_s^2\omega_7 + 30v_3^2\omega_{19}\omega_7^2\omega_{11}^2 + 12\omega_{19}^2c_s^2\omega_7^2 - 24v_3^2\omega_{19}\omega_7^2\omega_{11} + 48\omega_{19}^2c_s^4\omega_7\omega_{11} + 96v_3^4\omega_{19}\omega_7\omega_{11}^2 + 24v_3^2\omega_7\omega_{11}^2 + 14\omega_{19}^2c_s^4\omega_7^2\omega_{11} + 96v_3^2\omega_{19}\omega_7\omega_{11} + 12c_s^4\omega_7^2\omega_{11}^2 + \omega_{19}^2c_s^2\omega_7^2\omega_{11}^2 + 432v_3^2\omega_{19}c_s^2\omega_7\omega_{11}^2 - 48v_3^2\omega_{19}\omega_{11} - 144v_3^2c_s^2\omega_7\omega_{11}^2 - 3v_3^4\omega_{19}\omega_7^2\omega_{11}^2 + 150v_3^2\omega_{19}^2c_s^2\omega_7\omega_{11}$$

$$C_{62} = 156v_3^2\omega_{19}^2c_s^2\omega_7 - 24v_3^4\omega_7^2 + 24\omega_{19}^2c_s^2\omega_7^2 + 24v_3^2\omega_{19}^2\omega_7^2 - 48\omega_{19}^2c_s^4\omega_7 + 12v_3^2c_s^2\omega_7^3 - 6\omega_{19}^2c_s^2\omega_7^3 - 3v_3^2\omega_{19}^2\omega_7^3 + 12v_3^4\omega_7^3 + 24v_3^4\omega_{19}^2\omega_7 - 24v_3^2c_s^2\omega_7^2 + 24\omega_{19}^2c_s^4\omega_7^3 - 24v_3^4\omega_{19}^2\omega_7^2 - 3\omega_{19}^2c_s^4\omega_7^3 + 6v_3^2\omega_{19}^2c_s^2\omega_7^3 + 24\omega_{19}^2c_s^4\omega_7^2 + 3v_3^4\omega_{19}^2\omega_7^3 - 72v_3^2\omega_{19}^2c_s^2\omega_7^2 - 24v_3^2\omega_{19}^2\omega_7 - 24\omega_{19}^2c_s^2\omega_7 - 18v_3^2\omega_{19}\omega_7^3 + 6\omega_{19}^2c_s^4\omega_7^3 - 12v_3^2\omega_7^3 - 12v_3^2\omega_{19}c_s^2\omega_7^3 + 48v_3^2\omega_{19}\omega_7 + 24v_3^2\omega_7^2 + 72v_3^4\omega_{19}\omega_7^2 - 24\omega_{19}^2c_s^4\omega_7^2 + 12\omega_{19}^2c_s^2\omega_7 + 48v_3^2\omega_{19}c_s^2\omega_7^2 - 8\omega_{19}^2c_s^2\omega_7^2 + 18v_3^2\omega_{19}\omega_7^3 - 96v_3^2\omega_{19}^2c_s^2 - 24v_3^2\omega_{19}c_s^2\omega_7 + 24\omega_{19}^2c_s^4\omega_7 - 48v_3^4\omega_{19}\omega_7 - 72v_3^2\omega_{19}\omega_7^2 + \omega_{19}^2c_s^2\omega_7^3$$

$$C_{63} = 12\omega_{19}c_s^2\omega_7^2\omega_{11} + 61v_3^2\omega_{19}^2\omega_7^2\omega_{11} + 21\omega_{19}\omega_7^2\omega_{11}^2 - 60v_3^2\omega_{19}^2\omega_7^2 - 48\omega_{19}^2\omega_7 - 72v_3^2\omega_{19}\omega_7\omega_{11} + 36\omega_{19}\omega_{11}^2 + 60\omega_{19}^2c_s^2\omega_{11} + 24v_3^2\omega_7^2\omega_{11}^2 - 48c_s^2\omega_7\omega_{11}^2 + 72\omega_{19}\omega_7\omega_{11} + 24\omega_{19}^2\omega_7^2 + 168v_3^2\omega_{19}\omega_7\omega_{11}^2 - 84v_3^2\omega_{19}\omega_{11}^2 - 12\omega_7^2\omega_{11}^2 - 33\omega_{19}c_s^2\omega_7^2\omega_{11} - 5v_3^2\omega_{19}^2\omega_7^2\omega_{11}^2 - 12\omega_{19}\omega_7^2\omega_{11} + 120v_3^2\omega_{19}^2\omega_7 - 120\omega_{19}^2c_s^2\omega_7\omega_{11} + 24\omega_7\omega_{11}^2 - 60\omega_{19}c_s^2\omega_{11}^2 + 120\omega_{19}c_s^2\omega_7\omega_{11} + 39\omega_{19}^2c_s^2\omega_7^2\omega_{11} + 24\omega_{19}\omega_7\omega_{11} - 36\omega_{19}^2\omega_{11} + 24c_s^2\omega_7^2\omega_{11}^2 + 72\omega_{19}^2c_s^2\omega_7 - 25\omega_{19}^2\omega_7^2\omega_{11} - 51v_3^2\omega_{19}\omega_7^2\omega_{11}^2 - 36\omega_{19}^2c_s^2\omega_7^2 + 2\omega_{19}^2\omega_7^2\omega_{11} + 36v_3^2\omega_{19}\omega_7^2\omega_{11} - 48v_3^2\omega_7\omega_{11}^2 - 168v_3^2\omega_{19}\omega_7\omega_{11} - 24\omega_{19}^2c_s^2\omega_7\omega_{11} - 3\omega_{19}^2c_s^2\omega_7^2\omega_{11} - 72\omega_{19}\omega_7\omega_{11}^2 + 84v_3^2\omega_{19}\omega_{11}$$

2.3.5 Conservation of momentum: ρv_3



attached text file: output_d3q27_nse_mrt2_symbolic_pde_03.txt

$$\begin{aligned} & v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_3 v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_2} + (v_3^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\ & \frac{2v_3 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\ & + (-2 + 6v_3^2 + 4c_s^2 - 3v_3^2\omega_{11} - 2c_s^2\omega_{11} + \omega_{11}) \frac{\delta_l^2}{\delta_t \omega_{11}} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3v_3 \rho \delta_l^2}{\delta_t \omega_{11}} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\ & (-2 + \omega_7) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\ & (-2 + 2v_3^2 + 6c_s^2 - v_3^2\omega_{11} - 3c_s^2\omega_{11} + \omega_{11}) \frac{v_3 \delta_l^2}{2\delta_t \omega_{11}} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + 6v_3^2 + 2c_s^2 - 3v_3^2\omega_{11} - c_s^2\omega_{11} + \omega_{11}) \frac{\rho \delta_l^2}{2\delta_t \omega_{11}} \frac{\partial^2 v_3}{\partial x_3^2} + \\ & C_1 \frac{v_3 v_1 \delta_l^3}{12\omega_6 \delta_t \omega_{13} \omega_9} \frac{\partial^3 \rho}{\partial x_1^3} + C_2 \frac{v_3 \rho \delta_l^3}{12\omega_6 \delta_t \omega_{13} \omega_9} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{\rho v_1 \delta_l^3}{6\omega_6^2 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^3} + \\ & (6\omega_6\omega_5 + 6\omega_6\omega_7\omega_8 + 6\omega_7\omega_5 - 6\omega_7\omega_8 - \omega_6\omega_7\omega_8\omega_5 - 6\omega_6\omega_7\omega_5 - 6\omega_6\omega_8) \frac{v_3 c_s^2 \rho \delta_l^3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\ & (\omega_6\omega_7\omega_8 + \omega_6^2 + \omega_6\omega_7 - \omega_7\omega_8 - \omega_6\omega_8 - \omega_6^2\omega_7) \frac{c_s^2 \rho v_2 \delta_l^3}{\omega_6^2 \delta_t \omega_7 \omega_8} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} + \\ & (6\omega_6\omega_5 + 6\omega_6\omega_7\omega_8 + 6\omega_7\omega_5 - 6\omega_7\omega_8 - \omega_6\omega_7\omega_8\omega_5 - 6\omega_6\omega_7\omega_5 - 6\omega_6\omega_8) \frac{v_3 c_s^2 \rho \delta_l^3}{6\omega_6 \delta_t \omega_7 \omega_8 \omega_5} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & (\omega_6\omega_7\omega_8 + \omega_6\omega_7 - \omega_6\omega_7^2 + \omega_7^2 - \omega_7\omega_8 - \omega_6\omega_8) \frac{c_s^2 \rho v_1 \delta_l^3}{\omega_6 \delta_t \omega_7^2 \omega_8} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + C_4 \frac{v_3 v_2 \delta_l^3}{12\delta_t \omega_{16} \omega_{10} \omega_7} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \rho \delta_l^3}{12\delta_t \omega_{16} \omega_{10} \omega_7} \frac{\partial^3 v_2}{\partial x_2^3} + \\ & C_6 \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_{16} \omega_7^2} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4 \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3 \partial x_3} + (2\omega_6 + \omega_6\omega_{13} - \omega_6^2 - 2\omega_{13}) \frac{c_s^2 \rho v_1 \delta_l^3}{\omega_6^2 \delta_t \omega_{13}} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + \\ & (-12\omega_{11}\omega_{18} + 12\omega_6^2 - 12\omega_6\omega_{18} - \omega_6^2\omega_{11}\omega_{18} - 12\omega_6^2\omega_{11} + 12\omega_6\omega_{11}\omega_{18} + 12\omega_6\omega_{11}) \frac{v_3 c_s^2 \rho \delta_l^3}{6\omega_6^2 \delta_t \omega_{11}\omega_{18}} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\ & (\omega_6\omega_7\omega_8 + \omega_6^2 + \omega_6\omega_7 - \omega_7\omega_8 - \omega_6\omega_8 - \omega_6^2\omega_7) \frac{c_s^2 \rho v_2 \delta_l^3}{\omega_6^2 \delta_t \omega_7 \omega_8} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + \\ & (\omega_6\omega_7\omega_8 + \omega_6\omega_7 - \omega_6\omega_7^2 + \omega_7^2 - \omega_7\omega_8 - \omega_6\omega_8) \frac{c_s^2 \rho v_1 \delta_l^3}{\omega_6 \delta_t \omega_7^2 \omega_8} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + (-12 + 12\omega_7 - \omega_7^2) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\ & (\omega_{16}\omega_7 - 2\omega_{16} + 2\omega_7 - \omega_7^2) \frac{c_s^2 \rho v_2 \delta_l^3}{\delta_t \omega_{16} \omega_7^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\ & (-12\omega_7^2\omega_{11} - 12\omega_{19}\omega_{11} - \omega_{19}\omega_7^2\omega_{11} + 12\omega_7^2 + 12\omega_{19}\omega_7\omega_{11} - 12\omega_{19}\omega_7 + 12\omega_7\omega_{11}) \frac{v_3 c_s^2 \rho \delta_l^3}{6\omega_{19} \delta_t \omega_7^2 \omega_{11}} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\ & C_7 \frac{v_3 v_1 \delta_l^3}{\omega_6 \delta_t \omega_{17}^2 \omega_{18}} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + C_8 \frac{v_3 \rho \delta_l^3}{12\omega_6^2 \delta_t \omega_{17}^2 \omega_{18}} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_9 \frac{\rho v_1 \delta_l^3}{\omega_6 \delta_t \omega_{17}^2 \omega_{18}} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{10} \frac{v_3 v_2 \delta_l^3}{\omega_{19} \delta_t \omega_7 \omega_{11}^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + \\ & C_{11} \frac{v_3 \rho \delta_l^3}{12\omega_{19} \delta_t \omega_7^2 \omega_{11}^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{12} \frac{\rho v_2 \delta_l^3}{\omega_{19} \delta_t \omega_7 \omega_{11}^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{13} \frac{\delta_l^3}{12\delta_t \omega_{11}^2} \frac{\partial^3 \rho}{\partial x_3^3} + \\ & (-24 - 4\omega_{11}^2 + 11v_3^2\omega_{11}^2 + 60v_3^2 + 36c_s^2 - 60v_3^2\omega_{11} - 36c_s^2\omega_{11} + 24\omega_{11} + 5c_s^2\omega_{11}^2) \frac{v_3 \rho \delta_l^3}{6\delta_t \omega_{11}^2} \frac{\partial^3 v_3}{\partial x_3^3} + C_{14} \frac{v_3 \delta_l^4}{24\omega_6^2 \delta_t \omega_{13} \omega_9^2} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & C_{15} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_6^2 \delta_t \omega_{13}^2 \omega_9^2} \frac{\partial^4 v_1}{\partial x_1^4} + C_{16} \frac{\rho \delta_l^4}{24\omega_6^2 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^4} + C_{17} \frac{v_3 v_1 v_2 \delta_l^4}{4\omega_{12} \omega_6^2 \delta_t \omega_{13}^2 \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \end{aligned}$$

$$\begin{aligned}
& C_{18} \frac{v_3 \rho v_2 \delta_l^4}{4\omega_{12}\omega_6^2\delta_t\omega_{13}^2\omega_7\omega_{14}\omega_8\omega_5\omega_9^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{19} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_{12}\omega_6^2\delta_t\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9^2} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{20} \frac{\rho v_1 v_2 \delta_l^4}{2\omega_6^3\delta_t\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_2} + \\
& C_{21} \frac{v_3 c_s^4 \delta_l^4}{6\omega_6^2\delta_t\omega_7^2\omega_8^2\omega_5^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{22} \frac{v_3 c_s^2 \rho v_1 \delta_l^4}{2\omega_{12}\omega_6^2\delta_t\omega_{13}\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{23} \frac{v_3 c_s^2 \rho v_2 \delta_l^4}{2\omega_6^2\delta_t\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + \\
& C_{24} \frac{c_s^2 \rho \delta_l^4}{2\omega_6^3\delta_t\omega_{16}\omega_{13}\omega_7^3\omega_{17}\omega_{14}\omega_8^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + C_{25} \frac{v_3 v_1 v_2 \delta_l^4}{4\omega_6\delta_t\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_{26} \frac{12\omega_6^2\delta_t\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}}{v_3 \rho v_2 \delta_l^4} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& C_{27} \frac{v_3 \rho v_1 \delta_l^4}{4\omega_6\delta_t\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{28} \frac{\rho v_1 v_2 \delta_l^4}{2\omega_6^2\delta_t\omega_{16}^2\omega_7^3\omega_{17}\omega_8^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^3} + C_{29} \frac{v_3 \delta_l^4}{24\delta_t\omega_{16}^2\omega_{10}^2\omega_7^2} \frac{\partial^4 \rho}{\partial x_2^4} + C_{30} \frac{v_3 \rho v_2 \delta_l^4}{12\delta_t\omega_{16}^2\omega_{10}^2\omega_7^2} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& C_{31} \frac{\rho \delta_l^4}{24\delta_t\omega_{16}^2\omega_7^3} \frac{\partial^4 v_3}{\partial x_2^4} + C_{32} \frac{v_1 \delta_l^4}{12\omega_6^3\omega_{22}\delta_t\omega_{13}^2\omega_{11}\omega_{18}\omega_9^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{33} \frac{\rho \delta_l^4}{12\omega_6^3\omega_{22}\delta_t\omega_{13}^2\omega_{11}\omega_{18}\omega_9^2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& C_{34} \frac{v_3 \rho v_1 \delta_l^4}{12\omega_6^3\omega_{22}\delta_t\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{35} \frac{\delta_l^4}{2\omega_6^3\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2\omega_{18}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{36} \frac{\rho \delta_l^4}{2\omega_6^3\omega_{22}\omega_{19}\delta_t\omega_{13}^2\omega_{10}^2\omega_{20}\omega_{11}\omega_{14}\omega_8^2\omega_{18}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{37} \frac{\rho \delta_l^4}{12\omega_6^3\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7^3\omega_{20}\omega_{11}\omega_{14}\omega_8^2\omega_5^2\omega_{18}} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{38} \frac{v_3 \rho \delta_l^4}{2\omega_6^3\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_{10}^2\omega_{20}\omega_{11}^2\omega_{14}\omega_8^2\omega_5^2\omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\delta_l^4}{2\omega_6^2\omega_{19}\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8^2\omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{40} \frac{\rho \delta_l^4}{12\omega_6^3\omega_{19}\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8^2\omega_5^2\omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{\rho v_2 \delta_l^4}{\omega_6^2\omega_{19}\delta_t\omega_{16}^2\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8^2\omega_{18}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{42} \frac{\rho \delta_l^4}{2\omega_6^3\omega_{19}\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_{11}^2\omega_8^2\omega_5\omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{v_2 \delta_l^4}{12\omega_{19}\delta_t\omega_{16}^2\omega_{10}^2\omega_7^3\omega_{23}\omega_{11}} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + \\
& C_{44} \frac{\rho \delta_l^4}{12\omega_{19}\delta_t\omega_{16}^2\omega_{10}^2\omega_7^3\omega_{23}\omega_{11}} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{45} \frac{v_3 \rho v_2 \delta_l^4}{12\omega_{19}^2\delta_t\omega_{16}^2\omega_{10}^2\omega_7^3\omega_{23}\omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{46} \frac{v_3 \delta_l^4}{12\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}^2\omega_{18}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{47} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}^2\omega_{18}\omega_9^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{48} \frac{\rho \delta_l^4}{12\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}^3\omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{49} \frac{v_3 v_1 v_2 \delta_l^4}{\omega_6^2\omega_{19}^2\delta_t\omega_7^2\omega_{20}\omega_{11}^3\omega_8\omega_{18}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{v_3 \rho v_2 \delta_l^4}{2\omega_6^3\omega_{19}^2\delta_t\omega_7^2\omega_{20}\omega_{11}^3\omega_8^2\omega_5\omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{51} \frac{v_3 \rho v_1 \delta_l^4}{2\omega_6^2\omega_{19}^2\delta_t\omega_7^2\omega_{20}\omega_{11}^3\omega_8^2\omega_5\omega_{18}^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{52} \frac{\rho v_1 v_2 \delta_l^4}{\omega_6^2\omega_{19}^2\delta_t\omega_7^2\omega_{20}\omega_{11}^3\omega_8\omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{53} \frac{v_3 \delta_l^4}{12\omega_{19}^2\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{11}^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{54} \frac{v_3 \rho v_2 \delta_l^4}{2\omega_{19}^2\delta_t\omega_{16}^2\omega_{10}^2\omega_7^3\omega_{23}\omega_{11}^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& C_{55} \frac{\rho \delta_l^4}{12\omega_{19}^2\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{11}^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{56} \frac{v_1 \delta_l^4}{4\omega_6^2\delta_t\omega_{11}^3\omega_{18}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{57} \frac{\rho \delta_l^4}{12\omega_6^3\delta_t\omega_{11}^3\omega_{18}^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{58} \frac{v_3 \rho v_1 \delta_l^4}{4\omega_6^2\delta_t\omega_{11}^3\omega_{18}^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{59} \frac{v_2 \delta_l^4}{4\omega_{19}^2\delta_t\omega_7^2\omega_{11}^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{60} \frac{\rho \delta_l^4}{12\omega_{19}^2\delta_t\omega_7^3\omega_{11}^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{61} \frac{v_3 \rho v_2 \delta_l^4}{4\omega_{19}^2\delta_t\omega_7^3\omega_{11}^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{62} \frac{v_3 \delta_l^4}{12\delta_t\omega_{11}^3} \frac{\partial^4 \rho}{\partial x_3^4} + C_{63} \frac{\rho \delta_l^4}{12\delta_t\omega_{11}^3} \frac{\partial^4 v_3}{\partial x_3^4} \\
& = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 36c_s^2\omega_{13} + 6\omega_6\omega_{13} - 12v_1^2\omega_9 + \omega_6\omega_{13}v_1^2\omega_9 - 36c_s^2\omega_9 - 12\omega_{13} + 12\omega_{13}v_1^2 - 6\omega_6\omega_9 - \omega_6\omega_{13}\omega_9 - 18\omega_6c_s^2\omega_{13} + 6\omega_6v_1^2\omega_9 + 18\omega_6c_s^2\omega_9 - \\
& 6\omega_6\omega_{13}v_1^2 + 3\omega_6c_s^2\omega_{13}\omega_9 + 12\omega_9 \\
C_2 &= 12c_s^2\omega_{13} + 6\omega_6\omega_{13} - 36v_1^2\omega_9 + 3\omega_6\omega_{13}v_1^2\omega_9 - 12c_s^2\omega_9 - 12\omega_{13} + 36\omega_{13}v_1^2 - 6\omega_6\omega_9 - \omega_6\omega_{13}\omega_9 - 6\omega_6c_s^2\omega_{13} + 18\omega_6v_1^2\omega_9 + 6\omega_6c_s^2\omega_9 - \\
& 18\omega_6\omega_{13}v_1^2 + \omega_6c_s^2\omega_{13}\omega_9 + 12\omega_9 \\
C_3 &= -\omega_6^2\omega_{13}v_1^2 - 12c_s^2\omega_{13} + 6\omega_6 - 3\omega_6\omega_{13} - 3\omega_6^2 - 6\omega_6v_1^2 - 3\omega_6^2c_s^2\omega_{13} + 3\omega_6^2c_s^2 - 6\omega_6c_s^2 + 15\omega_6c_s^2\omega_{13} + 3\omega_6\omega_{13}v_1^2 + \omega_6^2\omega_{13} + 3\omega_6^2v_1^2 \\
C_4 &= 6\omega_{16}\omega_7 + \omega_{16}\omega_{10}\omega_7v_2^2 - 12\omega_{10}v_2^2 + 36c_s^2\omega_{16} - 6\omega_{10}\omega_7 - 36c_s^2\omega_{10} + 12\omega_{16}v_2^2 - 12\omega_{16} + 3c_s^2\omega_{16}\omega_{10}\omega_7 + 12\omega_{10} - 6\omega_{16}\omega_7v_2^2 - \\
& 18c_s^2\omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7 + 18c_s^2\omega_{10}\omega_7 + 6\omega_{10}\omega_7v_2^2 \\
C_5 &= 6\omega_{16}\omega_7 + 3\omega_{16}\omega_{10}\omega_7v_2^2 - 36\omega_{10}v_2^2 + 12c_s^2\omega_{16} - 6\omega_{10}\omega_7 - 12c_s^2\omega_{10} + 36\omega_{16}v_2^2 - 12\omega_{16} + c_s^2\omega_{16}\omega_{10}\omega_7 + 12\omega_{10} - 18\omega_{16}\omega_7v_2^2 - \\
& 6c_s^2\omega_{16}\omega_7 - \omega_{16}\omega_{10}\omega_7 + 6c_s^2\omega_{10}\omega_7 + 18\omega_{10}\omega_7v_2^2 \\
C_6 &= -3\omega_{16}\omega_7 - 6c_s^2\omega_7 - 12c_s^2\omega_{16} - 6\omega_7v_2^2 - \omega_{16}\omega_7v_2^2 + 6\omega_7 + 3c_s^2\omega_7^2 + \omega_{16}\omega_7^2 - 3\omega_7^2 + 3\omega_7^2v_2^2 - 3c_s^2\omega_{16}\omega_7^2 + 3\omega_{16}\omega_7v_2^2 + 15c_s^2\omega_{16}\omega_7 \\
C_7 &= \omega_{11}^2 - 3\omega_6c_s^2\omega_{11} - \omega_{11}\omega_{18} - v_3^2\omega_{11}^2 + \omega_6v_3^2\omega_{18} - \omega_6\omega_{18} + v_3^2\omega_{11}\omega_{18} - \omega_6v_3^2\omega_{11}\omega_{18} + 3\omega_6c_s^2\omega_{11}^2 + \omega_6\omega_{11}\omega_{18} + \omega_6v_3^2\omega_{11}^2 + \omega_6\omega_{11} - \\
& \omega_6\omega_{11}^2 - \omega_6v_3^2\omega_{11} + 3c_s^2\omega_{11}\omega_{18} - 3c_s^2\omega_{11}^2 - 3\omega_6c_s^2\omega_{11}\omega_{18} + 3\omega_6c_s^2\omega_{18} \\
C_8 &= -12\omega_6^2v_3^2\omega_{11} + 42\omega_6c_s^2\omega_{11}^2\omega_{18} - 3\omega_6^2v_3^2\omega_{11}\omega_{18} - 12\omega_6^2\omega_{11}^2 + 36\omega_6^2c_s^2\omega_{18} - 24c_s^2\omega_{11}^2\omega_{18} + 6\omega_6^2\omega_{11}\omega_{18} + 12\omega_6^2\omega_{11} - 6\omega_6\omega_{11}^2\omega_{18} - \\
& 18\omega_6^2c_s^2\omega_{11}\omega_{18} + 12\omega_6^2v_3^2\omega_{11}^2 - 12\omega_6c_s^2\omega_{11}^2 + 6\omega_6v_3^2\omega_{11}^2\omega_{18} - 11\omega_6^2c_s^2\omega_{11}^2\omega_{18} - 12\omega_6^2\omega_{18} + 3\omega_6^2\omega_{11}\omega_{18} + 12\omega_6^2c_s^2\omega_{11}^2 - 12\omega_6v_3^2\omega_{11}^2 - \\
& 12\omega_6^2c_s^2\omega_{11} + 12\omega_6\omega_{11}^2 - 24\omega_6c_s^2\omega_{11}\omega_{18} - 6\omega_6^2v_3^2\omega_{11}\omega_{18} + 12\omega_6^2v_3^2\omega_{18} \\
C_9 &= \omega_{11}^2 - \omega_6c_s^2\omega_{11} - \omega_{11}\omega_{18} - 3v_3^2\omega_{11}^2 + 3\omega_6v_3^2\omega_{18} - \omega_6\omega_{18} + 3v_3^2\omega_{11}\omega_{18} - 3\omega_6v_3^2\omega_{11}\omega_{18} + \omega_6c_s^2\omega_{11}^2 + \omega_6\omega_{11}\omega_{18} + 3\omega_6v_3^2\omega_{11}^2 + \omega_6\omega_{11} - \\
& \omega_6\omega_{11}^2 - 3\omega_6v_3^2\omega_{11} + c_s^2\omega_{11}\omega_{18} - c_s^2\omega_{11}^2 - \omega_6c_s^2\omega_{11}\omega_{18} + \omega_6c_s^2\omega_{18} \\
C_{10} &= \omega_{11}^2 + v_3^2\omega_{19}\omega_{11} - v_3^2\omega_{11}^2 - v_3^2\omega_{19}\omega_7\omega_{11} - 3c_s^2\omega_7\omega_{11} + 3c_s^2\omega_7\omega_{11}^2 - \omega_{19}\omega_{11} + 3\omega_{19}c_s^2\omega_7 - \omega_7\omega_{11}^2 + v_3^2\omega_{19}\omega_7 + \omega_{19}\omega_7\omega_{11} - v_3^2\omega_7\omega_{11} - \\
& \omega_{19}\omega_7 + v_3^2\omega_7\omega_{11}^2 - 3\omega_{19}c_s^2\omega_7\omega_{11} - 3c_s^2\omega_{11}^2 + \omega_7\omega_{11} + 3\omega_{19}c_s^2\omega_{11}
\end{aligned}$$

$$\begin{aligned}
& 6\omega_6\omega_{16}\omega_{10}\omega_7^2v_2^2\omega_{17}\omega_8^2\omega_5\omega_{15} - 12\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_5^2\omega_{15} - 42\omega_6c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5^2\omega_{15} - 36\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_3^2\omega_5\omega_{15} + \\
& 12\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5^2 + 18\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5^2\omega_{15} - 12\omega_6^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 6\omega_6^2\omega_{16}\omega_{10}\omega_7^2v_2^2\omega_8^2\omega_5^2\omega_{15} - 12\omega_6^2\omega_{16}\omega_{10}\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \\
& 12\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 18\omega_6^2\omega_{16}\omega_{10}\omega_7v_2^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + 6\omega_6\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5^2\omega_{15} + 54\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_3^2\omega_5\omega_{15} + \\
& 6\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5^2 + 6\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5^2\omega_{15} - 9\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + 42\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_3^2\omega_5\omega_{15} - \\
& 24\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_{15} - 6\omega_6\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8^2\omega_5^2 + 30\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5^2\omega_{15} - 36\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_3^2\omega_5\omega_{15} - \\
& 6\omega_6^2\omega_{16}\omega_{10}\omega_7^2v_2^2\omega_{17}\omega_8^2\omega_5\omega_{15} - 24\omega_6^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8^2\omega_{15} + 6\omega_6\omega_{16}\omega_{10}\omega_7^2v_2^2\omega_{17}\omega_8^2\omega_5^2 - 6\omega_6\omega_{16}\omega_{10}\omega_7^2v_2^2\omega_{17}\omega_8\omega_5^2\omega_{15}
\end{aligned}$$

$$\begin{aligned}
C_{28} = & -\omega_6^2\omega_3^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + 4\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2 - \omega_6\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 8\omega_6^2c_s^2\omega_{16}\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}\omega_7^2\omega_8^2 - \\
& 2\omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}^2\omega_7^2v_2^2\omega_8^2 + 6\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}^2\omega_7^2v_2^2\omega_{17}\omega_8^2 - \omega_6\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - 7\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - \\
& 2\omega_6\omega_{16}^2\omega_7^2\omega_8^2 - 6\omega_6c_s^2\omega_{16}^2\omega_7\omega_{17}\omega_8^2 - 2\omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2c_s^2\omega_{17}^2\omega_{17}\omega_8^2 + \omega_6\omega_{16}^2\omega_7^2\omega_8^2 + 5\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - \\
& 2\omega_6^2\omega_{16}\omega_7^2v_2^2\omega_8^2 - \omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2 + 13\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - \omega_6^2\omega_{16}\omega_7^2v_2^2\omega_8^2 + 4\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \\
& 4\omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}^2\omega_7^2\omega_8^2 + \omega_6\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 + 2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 - 5\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + \\
& \omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2 - 4\omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 - \omega_6c_s^2\omega_{16}^2\omega_7^2\omega_8^2 + 2\omega_6\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \\
& 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2 - \omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - \omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - \omega_6^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - \\
& \omega_6\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - \omega_6^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 - \omega_6\omega_{16}\omega_7^2v_2^2\omega_8^2 + 2\omega_6c_s^2\omega_{16}\omega_7^2\omega_8^2 + \omega_6c_s^2\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 - 2\omega_6\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 - 11\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \\
& \omega_6^2\omega_{16}^2\omega_7^2v_2^2\omega_8^2 - \omega_6\omega_{16}\omega_7^2v_2^2\omega_{17}\omega_8^2 - 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2 + \omega_6\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + 7\omega_6c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6^2\omega_{16}\omega_7^2\omega_8^2 - 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2
\end{aligned}$$

$$C_{30} = -48c_s^2\omega_{10}^2\omega_7 - 84\omega_{16}\omega_{10}^2\omega_7^2 + 60c_s^2\omega_{16}^2\omega_{10}\omega_7 - 72\omega_{16}\omega_{10}\omega_7\omega_7^2 + 72\omega_{16}^2\omega_{10}\omega_7 - 3c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 - 51\omega_{16}\omega_{10}^2\omega_7^2\omega_7^2 + 72c_s^2\omega_{16}^2\omega_7 + 84\omega_{16}^2\omega_{10}\omega_7^2 - 48\omega_{10}^2\omega_7\omega_7^2 - 72\omega_{16}\omega_{10}^2\omega_7 + 12c_s^2\omega_{16}\omega_{10}\omega_7^2 + 21\omega_{16}\omega_{10}^2\omega_7^2 - 24c_s^2\omega_{16}\omega_{10}\omega_7 + 36\omega_{16}\omega_{10}^2 - 36c_s^2\omega_{16}^2\omega_7^2 - 25\omega_{16}^2\omega_{10}\omega_7^2 + 24c_s^2\omega_{10}^2\omega_7^2 + 61\omega_{16}^2\omega_{10}\omega_7^2\omega_7^2 + 120\omega_{16}^2\omega_7\omega_7^2 - 120c_s^2\omega_{16}^2\omega_{10}\omega_7 + 2\omega_{16}^2\omega_{10}^2\omega_7^2 - 168\omega_{16}^2\omega_{10}\omega_7\omega_7^2 - 60c_s^2\omega_{16}\omega_{10}^2 + 24\omega_{16}^2\omega_7^2 - 60\omega_{16}^2\omega_7^2\omega_7^2 + 120c_s^2\omega_{16}\omega_{10}\omega_7 - 12\omega_{16}\omega_{10}\omega_7^2 - 12\omega_{10}^2\omega_7^2 - 5\omega_{16}^2\omega_{10}^2\omega_7^2 + 168\omega_{16}\omega_{10}^2\omega_7\omega_7^2 - 36\omega_{16}^2\omega_{10} + 24\omega_{10}^2\omega_7 - 33c_s^2\omega_{16}\omega_{10}^2\omega_7^2 + 24\omega_{16}\omega_{10}\omega_7 + 24\omega_{10}^2\omega_7^2\omega_7^2 + 36\omega_{16}\omega_{10}\omega_7^2\omega_7^2 - 48\omega_{16}^2\omega_7 + 39c_s^2\omega_{16}^2\omega_{10}\omega_7^2$$

$$\begin{aligned}
& 12\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{13}\omega_{17}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + \\
& 24\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 - \\
& 4\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 - 96\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{22}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 156\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 - \\
& 12\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - \omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 84\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + \\
& 12\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{22}\omega_{13}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 24\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 24\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 - 66\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - \\
& 18\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 - 132\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 - \\
& 24\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 48\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^3\omega_{22}\omega_{13}\omega_{17}\omega_{11}\omega_{18}\omega_9^2
\end{aligned}$$

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$$\begin{aligned}
& 9v_3w_{19}w_{16}w_{10}w_7w_{23}w_{11} + 6v_3w_{19}w_{16}w_{10}w_7w_{23} - 6w_{19}c_{16}^2w_{16}w_{10}w_7w_{11} - 12w_{19}c_{16}^4w_{16}w_{10}w_7w_{23}w_{11} - 12v_3^2w_{16}^2w_{10}w_7^2 + \\
& 24v_3^2w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + 18v_3^2w_{19}w_{16}w_{10}w_7w_{23}v_2^2w_{11} - 48v_3^2w_{19}w_{16}w_{10}w_7w_{23}w_{11} - 36c_{16}^2w_{16}^2w_{10}w_7w_{23}v_2^2 + 6v_3^2w_{19}w_{16}^2w_{10}w_7^2 + \\
& 6w_{19}c_{16}^4w_{16}^2w_{10}w_7w_{11} - 36w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} - 36v_3^2w_{16}^2w_{10}^2w_7^2v_2w_{11} - 108v_3w_{19}w_{16}^2w_{10}w_7w_{23}v_2w_{11} + 12c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + \\
& 12w_{19}^2w_{16}w_{10}w_7w_{23} + 36v_3^2w_{19}w_{16}w_{10}w_7w_{23}v_2^2 - 12v_3^2w_{16}^2w_{10}w_7w_{23}w_{11} - 12c_{16}^2w_{16}^2w_{10}w_7w_{11} + 36c_{16}^2w_{16}^2w_{10}w_7w_{23}v_2^2w_{11} + \\
& 36v_3^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} - 45v_3^2w_{19}w_{16}w_{10}w_7w_{23}v_2w_{11} - 6v_3w_{19}c_{16}^2w_{16}^2w_{10}w_7w_{11} + 60w_{19}c_{16}^2w_{16}^2w_{10}w_7w_{23}v_2w_{11} - 6w_{19}c_{16}^2w_{16}w_{10}w_7w_{23} - \\
& 12c_{16}^2w_{16}^2w_{10}w_7^2 + 18v_3w_{19}w_{16}^2w_{10}w_7^2w_{11} - 12c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + 12c_{16}^2w_{16}w_{10}w_7^2w_{11} + 36c_{16}^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} + 6w_{19}c_{16}^4w_{16}w_{10}w_7w_{23} \\
& 6v_3^2w_{19}w_{16}w_{10}w_7w_{23}w_{11} + 12w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + 12v_3^2c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + 12v_3^2w_{16}^2w_{10}w_7^2w_{11} + 12v_3^2w_{19}c_{16}^2w_{16}w_7w_{23}w_{11} - \\
& 6v_3^2w_{19}c_{16}^2w_{16}^2w_{10}w_7^2 - 12w_{19}c_{16}^2w_{16}^2w_{10}w_7w_{11} - 5w_{19}c_{16}^4w_{16}^2w_{10}w_7w_{23}w_{11} + 6v_3^2w_{19}w_{16}^2w_{10}w_7w_{23}w_{11} + 5w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} - \\
& 36v_3^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} + 144v_3^2w_{19}w_{16}w_{10}w_7w_{23}v_2^2w_{11} - 18w_{19}c_{16}^2w_{16}w_{10}^2w_7^2v_2w_{11} + 60w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} - 12c_{16}^2w_{16}w_{10}w_7w_{23} - \\
& 24v_3^2w_{19}w_{16}w_{10}w_7w_{23} + 12w_{19}c_{16}^2w_{16}^2w_{10}w_7w_{11} + 12v_3^2c_{16}^2w_{16}^2w_{10}w_7^2 + 12c_{16}^2w_{16}w_{10}w_7w_{23} + 12v_3^2w_{19}c_{16}^2w_{16}w_{10}^2w_7^2w_{11} - \\
& 36c_{16}^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} + 18w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + 6v_3^2w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} - 12v_3^2w_{19}w_{16}w_{10}w_7^2w_{23} + 6v_3^2w_{19}c_{16}^2w_{10}w_7^2w_{23}w_{11} + \\
& 12v_3^2w_{19}w_{10}^2w_7^2w_{23}w_{11} - 12v_3^2w_{16}^2w_{10}^2w_7^2w_{11} + 9v_3^2w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + w_{19}c_{16}^2w_{16}^2w_{10}^2w_7^2w_{23}w_{11} - 5w_{19}c_{16}^4w_{16}^2w_{10}w_7w_{23}w_{11} - \\
& 12w_{19}c_{16}^2w_{16}^2w_{10}w_{11} - 12c_{16}^2w_{16}^2w_{10}^2w_7^2w_{11} + 27v_3^2w_{19}w_{16}w_{10}w_7w_{23}v_2^2w_{11} - 24v_3^2w_{19}w_{16}w_{10}w_7w_{23}w_{11} + 12v_3^2w_{19}w_{16}^2w_{10}w_7^2w_{11} + \\
& 48v_3^2w_{19}c_{16}^2w_{16}^2w_{10}w_7w_{23}w_{11} - 18w_{19}c_{16}^4w_{16}w_{10}w_7w_{23}w_{11} + 12c_{16}^2w_{16}^2w_{10}w_7^2w_{11} - 36v_3^2w_{19}w_{16}w_{10}w_7w_{23}v_2^2w_{11} + 18w_{19}c_{16}^2w_{16}^2w_{10}w_7^2v_2w_{11} - \\
& 6w_{19}c_{16}^2w_{16}w_{10}w_7^2w_{11} + 36v_3^2w_{19}w_{16}^2w_{10}w_7w_{23}v_2^2w_{11} + 54w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}v_2^2w_{11} + 36v_3^2w_{16}^2w_{10}w_7^2v_2^2 + 72v_3^2w_{19}w_{16}^2w_{10}w_7w_{23}v_2^2w_{11} + \\
& 12c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} - 36v_3^2w_{19}w_{16}^2w_{10}w_7^2v_2w_{11} - 12w_{19}c_{16}^2w_{10}w_7^2w_{23}v_2^2w_{11} + 18w_{19}c_{16}^4w_{16}^2w_{10}w_7w_{23}w_{11} - 12v_3^2c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + \\
& 6w_{19}c_{16}^2w_{16}^2w_{10}w_7^2 + 12v_3^2w_{19}w_{16}w_{10}w_7w_{23}w_{11} - 36c_{16}^2w_{16}w_{10}w_7^2v_2^2w_{11} - 12v_3^2c_{16}^2w_{16}w_{10}w_7w_{23} - 48w_{19}c_{16}^2w_{16}^2w_{10}w_{11} + 12v_3^2w_{19}w_{16}^2w_{10}w_7^2w_{11} - \\
& 12v_3^2w_{16}w_{10}w_7w_{23}w_{11} - 18v_3^2w_{19}w_{16}^2w_{10}w_7^2v_2^2 + 6w_{19}c_{16}^2w_{16}w_{10}w_7^2w_{11} - 12w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + 6v_3^2w_{19}c_{16}^2w_{16}^2w_{10}w_7^2w_{11} - \\
& 36v_3^2w_{16}w_{10}w_7w_{23}v_2^2 + 15v_3^2w_{19}w_{16}w_{10}w_7w_{23}w_{11} - 72v_3^2w_{19}w_{16}w_{10}^2w_7w_{23}v_2^2 - 36v_3^2w_{19}w_{10}^2w_7w_{23}v_2^2w_{11} - 12c_{16}^2w_{16}w_{10}w_7^2w_{23}w_{11} + \\
& 36v_3^2w_{16}^2w_{10}w_7^2v_2w_{11} + 6v_3^2w_{19}w_{16}w_{10}^2w_7^2w_{11} - 15w_{19}c_{16}^2w_{16}^2w_{10}w_7w_{23}v_2^2w_{11} - 12v_3^2c_{16}^2w_{16}^2w_{10}w_7^2w_{11} - 18w_{19}c_{16}^2w_{16}^2w_{10}w_7^2v_2^2 - \\
& 18v_3^2w_{19}w_{16}^2w_{10}w_7w_{23}v_2^2 + 36v_3^2w_{19}w_{16}w_{10}^2w_7^2v_2w_{11} - 24v_3^2w_{19}c_{16}^2w_{16}w_{10}w_7^2w_{23} - 6v_3^2w_{19}c_{16}^2w_{16}w_{10}w_7w_{23} - 24v_3^2w_{19}c_{16}^2w_{16}w_{10}w_7w_{23}w_{11} + \\
& 30w_{19}c_{16}^2w_{16}w_{1$$

$$\begin{aligned}
& 2w_{19}^2w_{17}w_{23}v_{11}^2w_{11}^3 - 36w_{19}^4w_{16}w_{17}^3w_{11}^3 + 12v_{19}^3w_{19}^2w_{16}w_{17}w_{23}w_{11}^3 + 12w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 18w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 + 150w_{19}^4w_{16}w_{17}^3w_{23}w_{11}^3 - \\
& 36v_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 12v_{19}^2w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2 + 12v_{19}^3w_{19}^2w_{16}w_{17}^3w_{11}^3 - 12w_{19}^2w_{17}^3v_{11}^2w_{11}^3 + v_{19}^3w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 18w_{19}^2w_{16}w_{17}^3w_{11}^3 + \\
& 12w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 18w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 54w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 12w_{19}w_{16}w_{17}^3v_{11}^2w_{11}^3 - 6w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - \\
& 12w_{19}^2w_{19}^2w_{16}w_{17}^3w_{11}^3 - 12w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 88w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 18w_{19}^2w_{16}w_{17}^3w_{11}^3 + 36w_{19}^2w_{16}w_{17}^3w_{11}^3 + 12c_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + \\
& 12w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 - 12w_{19}^2w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 12c_{19}^4w_{16}w_{17}^3w_{23}w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 24v_{19}^3w_{19}w_{16}w_{17}w_{23}v_{11}^3w_{11}^3 - \\
& 2v_{19}^3w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 36w_{19}w_{16}w_{17}^3w_{23}v_{11}^3w_{11}^3 + 18w_{19}^2w_{16}w_{17}^3w_{11}^3 - 6v_{19}^3w_{19}^2w_{16}w_{17}^3w_{11}^3 - 12v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^3w_{11}^3 - 84w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - \\
& 12w_{19}^2w_{19}^2w_{16}w_{17}^3w_{11}^3 + 36w_{19}^2w_{16}w_{17}^3w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 12v_{19}^3w_{16}w_{17}^3w_{23}v_{11}^3w_{11}^3 + 18v_{19}^3w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 12w_{19}^2w_{19}^2w_{16}w_{17}^3w_{23} - \\
& 18w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 36w_{19}^4w_{16}w_{17}^3w_{23}w_{11}^3 - 36w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 36w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + \\
& 12w_{19}^2w_{19}w_{16}w_{17}^3v_{11}^2w_{11}^3 - 12w_{19}^2w_{16}w_{17}^3w_{11}^3 - 12w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2 - 42w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 6w_{19}^2w_{16}w_{17}^3w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + \\
& 18w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 108w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 12v_{19}^3w_{19}^2w_{16}w_{17}^3w_{11}^3 - 24v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 12w_{19}^2w_{19}w_{16}w_{17}^3v_{11}^2w_{11}^3 + \\
& 6w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 24w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 12v_{19}^3w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{11}^3 + 24v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 12v_{19}^3w_{16}w_{17}^3w_{23}w_{11}^3 + \\
& 180w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 36w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 + 30w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 18w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 - 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 18v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + \\
& 18w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 12v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{11}^3 - w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 12w_{19}^2w_{16}w_{17}^3w_{11}^3 - 12v_{19}^3w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - \\
& 12c_{19}^4w_{16}w_{17}^3w_{23}w_{11}^3 - 12w_{19}w_{16}w_{17}^3v_{11}^2w_{11}^3 + 6v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 36w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 36w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + \\
& 18w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 12c_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 36w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 + 5w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 6w_{19}w_{16}w_{17}^3v_{11}^2w_{11}^3 - \\
& 18w_{19}^2w_{16}w_{17}^3w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 6w_{19}^2w_{16}w_{17}^3w_{11}^3 + 72w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - 12v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 24w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 - \\
& 24w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 72w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 6w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 + 12c_{19}^4w_{16}w_{17}^3w_{23}w_{11}^3 + 36v_{19}^3w_{19}w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + \\
& 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 + 6v_{19}^3w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + 2w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 12w_{19}^2w_{16}w_{17}^3w_{11}^3 - 6w_{19}^2w_{16}w_{17}^3w_{11}^3 - 36w_{19}^2w_{16}w_{17}^3w_{23}v_{11}^2w_{11}^3 + \\
& 6w_{19}^2w_{16}w_{17}^3v_{11}^2w_{11}^3 + 12w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 6w_{19}^2w_{16}w_{17}^3w_{23}w_{11}^3 - 6v_{19}^3w_{19}^2w_{16}w_{17}^3w_{11}^3 + 12c_{19}^2w_{16}w_{17}^3w$$

[illegible]

$$\begin{aligned}
C_{56} = & -13\omega_6^2 v_3^4 \omega_{11} \omega_{18} - 72\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} - 24\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 - 8\omega_6 c_s^4 \omega_{11}^3 \omega_{18} + 4c_s^4 \omega_{11}^2 \omega_{18}^2 - 20\omega_6 v_3^2 \omega_{11} \omega_{18}^2 - 4\omega_6^2 c_s^4 \omega_{11}^2 + 12\omega_6^2 c_s^2 \omega_{11} \omega_{18}^2 - \\
& 32\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 8\omega_6 c_s^2 \omega_{11}^2 \omega_{18} - 4c_s^4 \omega_{11}^3 \omega_{18} + 24\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 - 13\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 4\omega_6^2 c_s^4 \omega_{11} \omega_{18} + 24\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 4\omega_6 v_3^2 \omega_{11}^3 + 4\omega_6^2 c_s^4 \omega_{11}^3 + \\
& 72\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18}^2 + 13\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 8\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 4c_s^4 \omega_{11}^3 \omega_{18} - 8\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 4\omega_6 c_s^2 \omega_{11}^3 - 4\omega_6^2 v_3^2 \omega_{11}^3 \omega_{18} + 32\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - \\
& 12\omega_6^2 c_s^4 \omega_{11} \omega_{18} + 4c_s^4 \omega_{11}^3 \omega_{18} + 8\omega_6 c_s^2 \omega_{11}^2 \omega_{18} + 4\omega_6^2 c_s^2 \omega_{11} \omega_{18} - 13\omega_6^2 v_3^2 \omega_{11} \omega_{18} - 144\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} + 4\omega_6^2 v_3^2 \omega_{11}^2 - 4\omega_6 c_s^2 \omega_{11} \omega_{18}^2 + \\
& 16\omega_6 v_3^2 \omega_{11} \omega_{18} + 36\omega_6^2 v_3^2 \omega_{11} \omega_{18}^2 + 84\omega_6 v_3^2 c_s^2 \omega_{11} \omega_{18} - 8\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 24\omega_6^2 v_3^2 \omega_{18}^2 - 4\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 51\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 4\omega_6 v_3^2 \omega_{11}^3 + \\
& 20\omega_6 v_3^2 \omega_{11} \omega_{18} - 4\omega_6^2 c_s^2 \omega_{11}^2 + 8v_3^4 \omega_{11}^2 \omega_{18} - 84\omega_6 v_3^2 c_s^2 \omega_{11} \omega_{18} + 4\omega_6^2 c_s^2 \omega_{11}^2 - 24\omega_6 v_3^2 c_s^2 \omega_{11} - 20\omega_6 v_3^2 \omega_{11}^2 \omega_{18} - 8v_3^4 \omega_{11}^3 \omega_{18} + 4\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - \\
& 20\omega_6^2 v_3^4 \omega_{11} \omega_{18} - 51\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 16\omega_6 v_3^4 \omega_{11} \omega_{18} + 4\omega_6^2 c_s^4 \omega_{11} \omega_{18}^2 + 8\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 36\omega_6^2 v_3^4 \omega_{11} \omega_{18}^2 - 36v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 4\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} - \\
& 48\omega_6 v_3^2 c_s^2 \omega_{11} \omega_{18} - 4\omega_6^2 v_3^2 \omega_{11}^2 - 8v_3^2 \omega_{11}^2 \omega_{18} - 20\omega_6 v_3^2 \omega_{11} \omega_{18} + 8\omega_6^2 c_s^4 \omega_{18}^2 + 12\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} + 8v_3^4 \omega_{11}^3 \omega_{18} + 96\omega_6^2 v_3^2 c_s^2 \omega_{18}^2 - 4\omega_6 c_s^4 \omega_{11}^3 + \\
& 20\omega_6 v_3^2 \omega_{11} \omega_{18} + 4\omega_6^2 v_3^4 \omega_{11}^2 + 20\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 36v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 4\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}
\end{aligned}$$

$$C_{58} = -8\omega_6^2\omega_{11}^3 + 64\omega_6\omega_3^2\omega_{11}\omega_{18} + 28\omega_6\omega_{11}^2\omega_{18} - 16\omega_6c_s^2\omega_{11}^2\omega_{18} - 72\omega_6^2c_s^2\omega_{11}\omega_{18} + 104\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} + 8\omega_6^2\omega_{11}^3 - 28\omega_6\omega_{11}^2\omega_{18} + 48\omega_6^2\omega_{11}\omega_{18} - 43\omega_6^3\omega_{11}^2\omega_{18} + 48\omega_6^2c_s^2\omega_{11}^2\omega_{18} + 20c_s^2\omega_{11}^3\omega_{18} + 24\omega_6^2\omega_{11}\omega_{18} + 44\omega_6c_s^2\omega_{11}^2\omega_{18} - 16\omega_6c_s^2\omega_{11}^3 + 16\omega_6^3\omega_{11}^2\omega_{18} - 20c_s^2\omega_{11}^3\omega_{18} - 44\omega_6c_s^2\omega_{11}^2\omega_{18} + 16\omega_6^2\omega_{11}^3 - 32\omega_6^2c_s^2\omega_{11}\omega_{18} + 43\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} - 16\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} - 16\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} + 32\omega_6c_s^2\omega_{11}\omega_{18} - 12\omega_{11}^2\omega_{18} - 48\omega_6^3\omega_{11}^2\omega_{18} - 120\omega_6^2\omega_{11}\omega_{18} + 56\omega_6^2\omega_{11}^3\omega_{18} + 80\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} - 16\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} + 16\omega_6^2\omega_3^2\omega_{11}^2\omega_{18} - 40\omega_6^2\omega_{11}\omega_{18} + 12\omega_{11}^2\omega_{18} - 16\omega_6^2c_s^2\omega_{11}^2 - 25\omega_6^2c_s^2\omega_{11}^2\omega_{18} - 32\omega_6^2\omega_{18} - 17\omega_6^2\omega_{11}^2\omega_{18} + 28\omega_3^2\omega_{11}^2\omega_{18} + 68\omega_6\omega_3^2\omega_{11}\omega_{18} + 8\omega_6\omega_{11}^3 + 17\omega_3^2\omega_{11}^3\omega_{18} - 24\omega_6\omega_{11}^2\omega_{18} - 28\omega_3^2\omega_{11}^2\omega_{18} - 68\omega_6\omega_3^2\omega_{11}^2\omega_{18} - 64\omega_6^3\omega_{11}^2\omega_{18} - 64\omega_6^2\omega_3^2\omega_{11}\omega_{18} + 25\omega_6^2c_s^2\omega_{11}^2\omega_{18}$$

$$\begin{aligned} C_{60} = & -4v_3^2w_{19}w_7^3\omega_{11}^3 - 6w_{19}c_2^3w_7^3\omega_{11}^3 + 12v_3^4w_7^3\omega_{11}^3 + 12v_3^2w_7^3\omega_{11}^3 - 12v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 - 36v_3^4w_{19}w_7^3\omega_{11}^3 - 18w_{19}c_4^4w_7^3\omega_{11}^3 + 48v_3^4w_{19}w_7^3\omega_{11}^3 + \\ & 6w_{19}c_2^3w_7^3\omega_{11}^3 - 12v_3^3w_7^3\omega_{11}^3 - 72v_3^3w_{19}w_7^3\omega_{11}^3 + 6w_{19}c_7^3w_7^3\omega_{11}^3 - 19v_3^5w_{19}w_7^3\omega_{11}^3 - 12v_3^5c_7^3w_7^3\omega_{11}^3 - 24v_3^3w_{19}w_7^3\omega_{11}^3 + 12w_{19}c_8^3w_7^3\omega_{11}^3 + \\ & 12v_3^4w_{19}w_7^3\omega_{11}^3 + 30v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 - 36v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 + 6w_{19}c_4^4w_7^3\omega_{11}^3 + 102v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 - 12v_3^2c_2^3w_7^3\omega_{11}^3 - 27v_3^4w_{19}w_7^3\omega_{11}^3 - 12v_3^2w_7^3\omega_{11}^3 + \\ & 54v_3^4w_{19}c_2^3w_7^3\omega_{11}^3 + 12w_{19}c_7^3w_7^3\omega_{11}^3 - 12v_3^4w_7^3\omega_{11}^3 + 18v_3^2w_{19}w_7^3\omega_{11}^3 + 18w_{19}c_8^3w_7^3\omega_{11}^3 + 252v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 + 90v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 - 21v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 + \\ & 12v_3^3w_7^3\omega_{11}^3 - 24w_{19}c_8^3w_7^3\omega_{11}^3 + 72v_3^4w_{19}w_7^3\omega_{11}^3 - 48v_3^2w_{19}c_8^3w_7^3\omega_{11}^3 + 60v_3^4w_{19}w_7^3\omega_{11}^3 + 12v_3^2c_2^3w_7^3\omega_{11}^3 - 6w_{19}c_2^3w_7^3\omega_{11}^3 + 24v_3^2w_{19}w_7^3\omega_{11}^3 - \\ & 12w_{19}c_2^3w_7^3\omega_{11}^3 - 12v_3^2w_{19}w_7^3\omega_{11}^3 + 13w_{19}c_4^4w_7^3\omega_{11}^3 - 12w_{19}c_4^4w_7^3\omega_{11}^3 + 4v_3^4w_{19}w_7^3\omega_{11}^3 + 162v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 + 36v_3^3w_{19}w_7^3\omega_{11}^3 - 48v_3^3w_{19}w_7^3\omega_{11}^3 + \\ & 12w_{19}c_8^3w_7^3\omega_{11}^3 - 81v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 - 30v_3^3w_{19}c_8^3w_7^3\omega_{11}^3 + 19v_3^2w_{19}w_7^3\omega_{11}^3 + 6w_{19}c_2^3w_7^3\omega_{11}^3 - w_{19}c_8^3w_7^3\omega_{11}^3 - 12w_{19}c_2^3w_7^3\omega_{11}^3 + 24v_3^2w_{19}w_7^3\omega_{11}^3 - \\ & 12v_3^2w_{19}w_7^3\omega_{11}^3 + 12w_{19}c_2^3w_7^3\omega_{11}^3 - 5w_{19}c_8^3w_7^3\omega_{11}^3 + 12w_{19}c_8^3w_7^3\omega_{11}^3 + 27v_3^2w_{19}w_7^3\omega_{11}^3 - 18v_3^4w_{19}w_7^3\omega_{11}^3 - 90v_3^4w_{19}w_7^3\omega_{11}^3 + 60v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 - \\ & 48v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 - w_{19}c_2^3w_7^3\omega_{11}^3 - 12v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 - 12w_{19}c_8^3w_7^3\omega_{11}^3 - 60v_3^3w_{19}w_7^3\omega_{11}^3 - 6w_{19}c_8^3w_7^3\omega_{11}^3 - 12w_{19}c_2^3w_7^3\omega_{11}^3 + w_{19}c_8^3w_7^3\omega_{11}^3 + \\ & 12v_3^3w_{19}c_2^3w_7^3\omega_{11}^3 - 24v_3^4w_{19}w_7^3\omega_{11}^3 + 12v_3^4w_{19}w_7^3\omega_{11}^3 + 12w_{19}c_8^3w_7^3\omega_{11}^3 - 108v_3^2w_{19}c_2^3w_7^3\omega_{11}^3 \end{aligned}$$

$$C_{62} = 12 + 8\omega_{11}^2 + 10v_3^2\omega_{11}^3 - 98v_3^2\omega_{11}^3 - \omega_{11}^3 - 156v_3^2 - 216c_s^4\omega_{11} + 82c_s^4\omega_{11}^2 - 132c_s^2 + 234v_3^2\omega_{11} - 5c_s^4\omega_{11}^3 + 672v_3^2c_s^2 + 90v_3^4\omega_{11}^2 + 198c_s^2\omega_{11} + 144c_s^4 - 18\omega_{11} - 34v_3^2c_s^2\omega_{11}^3 - 9v_3^4\omega_{11}^3 + 404v_3^2c_s^2\omega_{11}^2 - 1008v_3^2c_s^2\omega_{11} + 6c_s^2\omega_{11}^3 - 78c_s^2\omega_{11}^2 - 216v_3^4\omega_{11} + 144v_3^4$$

2.4 CLBM1

2.4.1 Definitions

Collision operator \mathbf{C} :

$$\mathbf{C}(f) = \mathbf{K}^{-1} \mathbf{S} \left(\boldsymbol{\kappa}^{(eq)} - \mathbf{K}f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \dots, \omega_{27}),$$

$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2)$.

Matrix \mathbf{K} corresponds to the transformation matrix to the central moment basis defined by

$$\begin{aligned} \boldsymbol{\kappa} = & \left(k_{(0,0,0)}, k_{(1,0,0)}, k_{(0,1,0)}, k_{(0,0,1)}, k_{(1,1,0)}, k_{(1,0,1)}, k_{(0,1,1)}, k_{(1,1,1)}, k_{(2,0,0)}, \right. \\ & k_{(0,2,0)}, k_{(0,0,2)}, k_{(2,1,0)}, k_{(2,0,1)}, k_{(2,1,1)}, k_{(1,2,0)}, k_{(0,2,1)}, k_{(1,2,1)}, k_{(1,0,2)}, \\ & \left. k_{(0,1,2)}, k_{(1,1,2)}, k_{(2,2,0)}, k_{(2,0,2)}, k_{(0,2,2)}, k_{(2,2,1)}, k_{(2,1,2)}, k_{(1,2,2)}, k_{(2,2,2)} \right)^T, \end{aligned}$$

and is given by

$$\begin{aligned} \mathbf{K}_{1,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,0)}, & \mathbf{K}_{2,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,0)}, & \mathbf{K}_{3,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,0)}, \\ \mathbf{K}_{4,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,1)}, & \mathbf{K}_{5,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,0)}, & \mathbf{K}_{6,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,1)}, \\ \mathbf{K}_{7,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,1)}, & \mathbf{K}_{8,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,1)}, & \mathbf{K}_{9,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)}, \\ \mathbf{K}_{10,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,2,0)}, & \mathbf{K}_{11,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,2)}, & \mathbf{K}_{12,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,0)}, \\ \mathbf{K}_{13,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,1)}, & \mathbf{K}_{14,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,1)}, & \mathbf{K}_{15,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)}, \\ \mathbf{K}_{16,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,2,1)}, & \mathbf{K}_{17,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,1)}, & \mathbf{K}_{18,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,2)}, \\ \mathbf{K}_{19,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,2)}, & \mathbf{K}_{20,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,2)}, & \mathbf{K}_{21,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)}, \\ \mathbf{K}_{22,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,2)}, & \mathbf{K}_{23,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,2,2)}, & \mathbf{K}_{24,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,1)}, \\ \mathbf{K}_{25,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,2)}, & \mathbf{K}_{26,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,2)}, & \mathbf{K}_{27,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,2)}, \end{aligned}$$

$\forall i \in \{1, 2, \dots, 27\}$.

The equilibrium central moments are defined as

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K} \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left(\rho, 0, 0, 0, 0, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2, 0, 0, 0, 0, 0, 0, 0, 0, \rho c_s^4, \rho c_s^4, \rho c_s^4, 0, 0, 0, \rho c_s^6 \right)^T.$$

2.4.2 Conservation of mass: ρ



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$$\begin{aligned} & \frac{\partial \rho}{\partial t} + \frac{v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{v_1 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\ & \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho \delta_l^3}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \end{aligned}$$

$$\begin{aligned}
& + (3\omega_9 v_1^2 - 2c_s^2 - \omega_9 c_s^4 + 6v_1^4 - 12\omega_9 c_s^2 v_1^2 - 3\omega_9 v_1^4 + 2c_s^4 + 24c_s^2 v_1^2 + \omega_9 c_s^2 - 6v_1^2) \frac{\delta_l^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 2\omega_9 - 5\omega_9 v_1^2 + 6c_s^2 - 3\omega_9 c_s^2 + 10v_1^2) \frac{\rho v_1 \delta_l^4}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& (3\omega_9 - 3\omega_9 v_1^2 - \omega_{12} + \omega_9 \omega_{12} v_1^2 - \omega_9 \omega_{12} + \omega_{12} v_1^2 + 3\omega_{12} c_s^2 + 3\omega_9 \omega_{12} c_s^2 - 9\omega_9 c_s^2) \frac{\rho v_1 \delta_l^4}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + \omega_5) \frac{c_s^4 \delta_l^4}{6\delta_t \omega_5} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (3c_s^2 \omega_{15} - 3\omega_{10} v_2^2 + 3c_s^2 \omega_{10} \omega_{15} + 3\omega_{10} - 9c_s^2 \omega_{10} + v_2^2 \omega_{15} - \omega_{10} \omega_{15} + \omega_{10} v_2^2 \omega_{15} - \omega_{15}) \frac{\rho v_2 \delta_l^4}{12\delta_t \omega_{10} \omega_{15}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (6v_2^4 - 2c_s^2 + 3\omega_{10} v_2^2 + c_s^2 \omega_{10} - 3\omega_{10} v_2^4 + 24c_s^2 v_2^2 - c_s^4 \omega_{10} - 6v_2^2 + 2c_s^4 - 12c_s^2 \omega_{10} v_2^2) \frac{\delta_l^4}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 - 5\omega_{10} v_2^2 + 2\omega_{10} - 3c_s^2 \omega_{10} + 10v_2^2) \frac{\rho v_2 \delta_l^4}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (3\omega_9 - 3\omega_9 v_1^2 - \omega_{13} + 3c_s^2 \omega_{13} + \omega_9 \omega_{13} v_1^2 + 3\omega_9 c_s^2 \omega_{13} + \omega_{13} v_1^2 - \omega_9 \omega_{13} - 9\omega_9 c_s^2) \frac{\rho v_1 \delta_l^4}{12\omega_9 \delta_t \omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-3\omega_{10} v_2^2 + \omega_{16} \omega_{10} v_2^2 + \omega_{16} v_2^2 - \omega_{16} + 3\omega_{10} + 3c_s^2 \omega_{16} - 9c_s^2 \omega_{10} + 3c_s^2 \omega_{16} \omega_{10} - \omega_{16} \omega_{10}) \frac{\rho v_2 \delta_l^4}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{c_s^4 \delta_l^4}{6\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-2 + \omega_7) \frac{c_s^4 \delta_l^4}{6\delta_t \omega_7} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (3c_s^2 \omega_{18} + 3c_s^2 \omega_{11} \omega_{18} + v_3^2 \omega_{18} - 3v_3^2 \omega_{11} + 3\omega_{11} - \omega_{11} \omega_{18} - 9c_s^2 \omega_{11} - \omega_{18} + v_3^2 \omega_{11} \omega_{18}) \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_{11} \omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (\omega_{19} v_3^2 + \omega_{19} v_3^2 \omega_{11} - \omega_{19} + 3\omega_{19} c_s^2 + 3\omega_{19} c_s^2 \omega_{11} - 3v_3^2 \omega_{11} + 3\omega_{11} - 9c_s^2 \omega_{11} - \omega_{19} \omega_{11}) \frac{v_3 \rho \delta_l^4}{12\omega_{19} \delta_t \omega_{11}} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3^3} + \\
& (-2c_s^2 - 6v_3^2 - 3v_3^2 \omega_{11} + 24c_s^2 v_3^2 - 12c_s^2 v_3^2 \omega_{11} - c_s^4 \omega_{11} + 3v_3^2 \omega_{11} + c_s^2 \omega_{11} + 2c_s^4 + 6v_3^4) \frac{\delta_l^4}{24\delta_t \omega_{11}} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 6c_s^2 + 10v_3^2 - 5v_3^2 \omega_{11} + 2\omega_{11} - 3c_s^2 \omega_{11}) \frac{v_3 \rho \delta_l^4}{12\delta_t \omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.4.3 Conservation of momentum: ρv_1



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$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho v_1 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_9 - 3\omega_9 v_1^2 + 4c_s^2 - 2\omega_9 c_s^2 + 6v_1^2) \frac{\delta_l^2}{\omega_9 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\rho v_1 \delta_l^2}{\omega_9 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + \omega_9 - \omega_9 v_1^2 + 6c_s^2 - 3\omega_9 c_s^2 + 2v_1^2) \frac{v_1 \delta_l^2}{2\omega_9 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + \omega_9 - 3\omega_9 v_1^2 + 2c_s^2 - \omega_9 c_s^2 + 6v_1^2) \frac{\rho \delta_l^2}{2\omega_9 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_5} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_5} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\omega_9^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 + 24\omega_9 - 60\omega_9 v_1^2 + 36c_s^2 + 5\omega_9^2 c_s^2 - 4\omega_9^2 + 11\omega_9^2 v_1^2 - 36\omega_9 c_s^2 + 60v_1^2) \frac{\rho v_1 \delta_l^3}{6\omega_9^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{\rho v_1 \delta_l^3}{12\omega_9^2 \omega_{12} \delta_t \omega_5} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_5^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_3 \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_5 \omega_{15}} \frac{\partial^3 v_1}{\partial x_2^2} + \\
& (-1 + c_s^2 + 3v_2^2) \frac{\rho v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_4 \frac{\rho v_1 \delta_l^3}{12\omega_9 \omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4 \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \\
& \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \rho \delta_l^3}{6\omega_6 \delta_t \omega_{18}} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_6 \frac{v_1 \delta_l^4}{12\omega_9^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_7 \frac{\rho \delta_l^4}{12\omega_9^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_8 \frac{\rho \delta_l^4}{12\omega_9^3 \omega_{12}^2 \delta_t \omega_5^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_9 \frac{c_s^2 v_1 \delta_l^4}{12\omega_9^3 \omega_{12}^2 \delta_t \omega_5^3 \omega_{21} \omega_{15}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& C_{10} \frac{c_s^2 \rho \delta_l^4}{12\omega_9^2 \omega_{12} \delta_t \omega_5^3 \omega_{21} \omega_{15}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{c_s^2 v_2 \delta_l^4}{12\omega_9 \omega_{12} \delta_t \omega_{10} \omega_5^2 \omega_{21} \omega_{15}^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& (3c_s^2 \omega_{15} - 3\omega_{10} v_2^2 + 3c_s^2 \omega_{10} \omega_{15} + 3\omega_{10} - 9c_s^2 \omega_{10} + v_2^2 \omega_{15} - \omega_{10} \omega_{15} + \omega_{10} v_2^2 \omega_{15} - \omega_{15}) \frac{\rho v_2 v_1 \delta_l^4}{12\delta_t \omega_{10} \omega_{15}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& C_{12} \frac{c_s^2 \rho \delta_l^4}{12\omega_9 \omega_{12} \delta_t \omega_{10} \omega_5^3 \omega_{21} \omega_{15}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\
& (6v_2^4 - 2c_s^2 + 3\omega_{10} v_2^2 + c_s^2 \omega_{10} - 3\omega_{10} v_2^4 + 24c_s^2 v_2^2 - c_s^4 \omega_{10} - 6v_2^2 + 2c_s^4 - 12c_s^2 \omega_{10} v_2^2) \frac{v_1 \delta_l^4}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + C_{13} \frac{\rho \delta_l^4}{24\delta_t \omega_5^3 \omega_{15}^2} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (-4 + 6c_s^2 - 5\omega_{10} v_2^2 + 2\omega_{10} - 3c_s^2 \omega_{10} + 10v_2^2) \frac{\rho v_2 v_1 \delta_l^4}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + C_{14} \frac{\rho \delta_l^4}{12\omega_9^3 \omega_6^3 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& C_{15} \frac{c_s^4 \rho \delta_l^4}{12\omega_9\omega_{12}\omega_6^2\delta_t\omega_{13}\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (-3\omega_{10}v_2^2 + \omega_{16}\omega_{10}v_2^2 + \omega_{16}v_2^2 - \omega_{16} + 3\omega_{10} + 3c_s^2\omega_{16} - 9c_s^2\omega_{10} + 3c_s^2\omega_{16}\omega_{10} - \omega_{16}\omega_{10}) \frac{\rho v_2 v_1 \delta_l^4}{12\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& C_{16} \frac{c_s^2 v_1 \delta_l^4}{12\omega_9^3\omega_6^2\omega_{22}\delta_t\omega_{13}\omega_{18}} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{17} \frac{c_s^2 \rho \delta_l^4}{12\omega_9^3\omega_6^2\omega_{22}\delta_t\omega_{13}\omega_{18}} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + C_{18} \frac{\delta_l^4}{2\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_{20}\omega_{14}\omega_8\omega_5\omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{19} \frac{\rho \delta_l^4}{2\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_{20}\omega_{14}\omega_8\omega_5\omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{20} \frac{\rho \delta_l^4}{12\omega_9\omega_{12}\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{17}\omega_{20}\omega_{14}\omega_8\omega_5^2\omega_{18}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{21} \frac{v_3 \rho \delta_l^4}{\omega_9\omega_{12}\omega_6\omega_{22}\delta_t\omega_{13}\omega_{20}\omega_{14}\omega_8\omega_5\omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{22} \frac{\delta_l^4}{12\omega_6\delta_t\omega_{17}\omega_{20}\omega_{17}\omega_8\omega_5\omega_{18}\omega_{15}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{23} \frac{\rho \delta_l^4}{4\omega_6^2\delta_t\omega_{20}\omega_{17}\omega_8\omega_5^2\omega_{18}\omega_{15}} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3} + C_{24} \frac{\rho v_2 \delta_l^4}{2\omega_6\delta_t\omega_{20}\omega_{17}\omega_8\omega_5\omega_{18}\omega_{15}} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{25} \frac{\rho \delta_l^4}{4\omega_6\delta_t\omega_{20}\omega_{17}\omega_8\omega_5\omega_{18}\omega_{15}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{26} \frac{c_s^2 v_3 \delta_l^4}{12\omega_9\omega_6^2\omega_{22}\delta_t\omega_{13}\omega_{11}\omega_{18}} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + \\
& (3c_s^2\omega_{18} + 3c_s^2\omega_{11}\omega_{18} + v_3^2\omega_{18} - 3v_3^2\omega_{11} + 3\omega_{11} - \omega_{11}\omega_{18} - 9c_s^2\omega_{11} - \omega_{18} + v_3^2\omega_{11}\omega_{18}) \frac{v_3 \rho v_1 \delta_l^4}{12\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} + \\
& C_{27} \frac{c_s^2 \rho \delta_l^4}{12\omega_9\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}\omega_{18}} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} + \\
& (\omega_{19}v_3^2 + \omega_{19}v_3^2\omega_{11} - \omega_{19} + 3\omega_{19}c_s^2 + 3\omega_{19}c_s^2\omega_{11} - 3v_3^2\omega_{11} + 3\omega_{11} - 9c_s^2\omega_{11} - \omega_{19}\omega_{11}) \frac{v_3 \rho v_1 \delta_l^4}{12\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^2} + \\
& (-2c_s^2 - 6v_3^2 - 3v_3^2\omega_{11} + 24c_s^2v_3^2 - 12c_s^2v_3^2\omega_{11} - c_s^4\omega_{11} + 3v_3^2\omega_{11} + c_s^2\omega_{11} + 2c_s^4 + 6v_3^4) \frac{v_1 \delta_l^4}{24\delta_t\omega_{11}} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho \delta_l^4}{24\omega_6^3\delta_t\omega_{18}} \frac{\partial^4 v_1}{\partial x_3} + (-4 + 6c_s^2 + 10v_3^2 - 5v_3^2\omega_{11} + 2\omega_{11} - 3c_s^2\omega_{11}) \frac{v_3 \rho v_1 \delta_l^4}{12\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_3} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 36\omega_9v_1^2 - 12c_s^2 + 24\omega_9c_s^2v_1^2 - \omega_9^2c_s^2 - 12\omega_9c_s^4 + 36v_1^4 + 7\omega_9^2v_1^4 + \omega_9^2c_s^4 - 144\omega_9c_s^2v_1^2 - 36\omega_9v_1^4 + 12c_s^4 + 144c_s^2v_1^2 - 7\omega_9^2v_1^2 + 12\omega_9c_s^2 - 36v_1^2 \\
C_2 &= 36\omega_{12}c_s^2\omega_5 - 3\omega_9^2\omega_{12}v_1^2\omega_5 - 36\omega_9^2c_s^2 + 18\omega_9^2\omega_{12}c_s^2 + 3\omega_9^2\omega_{12}\omega_5 - 36\omega_9c_s^2\omega_5 - 18\omega_9\omega_{12}c_s^2\omega_5 - 12\omega_9^2\omega_5 + 12\omega_9^2v_1^2\omega_5 - 6\omega_9\omega_{12}v_1^2\omega_5 + \\
& 12\omega_9\omega_5 + 12\omega_9^2 + 36\omega_9^2c_s^2\omega_5 + 6\omega_9\omega_{12}\omega_5 - 12\omega_{12}\omega_5 - 12\omega_9v_1^2\omega_5 + 6\omega_9^2\omega_{12}v_1^2 - 12\omega_9^2v_1^2 + 12\omega_{12}v_1^2\omega_5 - 11\omega_9^2\omega_{12}c_s^2\omega_5 - 6\omega_9^2\omega_{12} \\
C_3 &= 6 + 9c_s^2\omega_{15} - 18c_s^2 - 3c_s^2\omega_5\omega_{15} - v_2^2\omega_5\omega_{15} + 9c_s^2\omega_5 + 3v_2^2\omega_{15} - 3\omega_5 + 3v_2^2\omega_5 - 6v_2^2 + \omega_5\omega_{15} - 3\omega_{15} \\
C_4 &= 3\omega_9^2\omega_6\omega_{13} - 11\omega_9^2\omega_6c_s^2\omega_{13} - 36\omega_9^2c_s^2 + 12\omega_9\omega_6 - 3\omega_9^2\omega_6\omega_{13}v_1^2 + 36\omega_9^2\omega_6c_s^2 - 6\omega_9^2\omega_{13} - 12\omega_9\omega_6v_1^2 - 36\omega_9\omega_6c_s^2 + 12\omega_9^2 + 6\omega_9^2\omega_{13}v_1^2 - \\
& 18\omega_9\omega_6c_s^2\omega_{13} - 6\omega_9\omega_6\omega_{13}v_1^2 + 18\omega_9^2c_s^2\omega_{13} + 12\omega_9^2\omega_6v_1^2 + 12\omega_6\omega_{13}v_1^2 + 6\omega_9\omega_6\omega_{13} - 12\omega_9^2\omega_6 - 12\omega_9^2v_1^2 + 36\omega_6c_s^2\omega_{13} - 12\omega_6\omega_{13} \\
C_5 &= 6 - 18c_s^2 - 3\omega_6 + 9c_s^2\omega_{18} - 6v_3^2 + 3v_3^2\omega_{18} - 3\omega_6c_s^2\omega_{18} + \omega_6\omega_{18} + 3\omega_6v_3^2 + 9\omega_6c_s^2 - \omega_6v_3^2\omega_{18} - 3\omega_{18} \\
C_6 &= 12 - 18\omega_9 + 234\omega_9v_1^2 - 132c_s^2 + 404\omega_9c_s^2v_1^2 - 78\omega_9^2c_s^2 - 216\omega_9c_s^4 + 144v_1^4 + 90\omega_9^2v_1^4 + 6\omega_9^2c_s^2 - 9\omega_9^3v_1^4 + 8\omega_9^2 - 5\omega_9^2c_s^4 - 34\omega_9^2c_s^2v_1^2 - \omega_9^3 + \\
& 10\omega_9^3v_1^2 + 82\omega_9^2c_s^4 - 1008\omega_9c_s^2v_1^2 - 216\omega_9v_1^4 + 144c_s^4 + 672c_s^2v_1^2 - 98\omega_9^2v_1^2 + 198\omega_9c_s^2 - 156v_1^2 \\
C_7 &= 12 - 18\omega_9 + 378\omega_9v_1^2 - 36c_s^2 + 252\omega_9^2c_s^2v_1^2 - 22\omega_9^2c_s^2 - 36\omega_9c_s^4 + 504v_1^4 + 310\omega_9^2v_1^4 + 2\omega_9^2c_s^2 - 29\omega_9^3v_1^4 + 8\omega_9^2 - \omega_9^2c_s^4 - 18\omega_9^2c_s^2v_1^2 - \omega_9^3 + \\
& 14\omega_9^3v_1^2 + 14\omega_9^2c_s^4 - 648\omega_9c_s^2v_1^2 - 756\omega_9v_1^4 + 24c_s^4 + 432c_s^2v_1^2 - 154\omega_9^2v_1^2 + 54\omega_9c_s^2 - 252v_1^2 \\
C_8 &= -18\omega_9^3\omega_{12}c_s^2v_1^2\omega_5 - 36\omega_9^3\omega_{12}v_1^2\omega_5^2 - 6\omega_9^2\omega_{12}c_s^4\omega_5^3 - 36\omega_9^3v_1^4\omega_5^2 + 90\omega_9\omega_{12}^2v_1^2\omega_5^3 + 198\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^3 + 39\omega_9^3\omega_{12}v_1^2\omega_5^3 + 12\omega_9^2\omega_{12}c_s^4\omega_5^2 + \\
& 19\omega_9^2\omega_{12}^2v_1^4\omega_5^3 - 5\omega_9^3\omega_{12}^2c_s^2\omega_5^2 - 108\omega_9\omega_{12}c_s^2v_1^2\omega_5^3 + 36\omega_9^2v_1^2\omega_5^3 + 36\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^2 + 36\omega_9^3v_1^4\omega_5^3 + 12\omega_9^3\omega_{12}c_s^4\omega_5^3 - 18\omega_9^3\omega_{12}c_s^4\omega_5^2 - \\
& 72\omega_9^3\omega_{12}v_1^2\omega_5^3 - 6\omega_9^2\omega_{12}c_s^2\omega_5^3 + 4\omega_9^3\omega_{12}^2v_1^4\omega_5^3 + 6\omega_9^3\omega_{12}c_s^2\omega_5^3 - 12\omega_9\omega_{12}^2c_s^4\omega_5^3 + 12\omega_9^3\omega_{12}c_s^2v_1^2\omega_5^3 + 6\omega_9^3\omega_{12}c_s^4\omega_5^3 - \omega_9^2\omega_{12}c_s^2\omega_5^3 - 6\omega_9^2\omega_{12}v_1^4\omega_5^3 - \\
& 12\omega_9\omega_{12}^2c_s^4\omega_5^2 - 36\omega_9\omega_{12}v_1^4\omega_5^3 - 3\omega_9^3\omega_{12}c_s^2v_1^2\omega_5^2 + 252\omega_{12}^2c_s^2v_1^2\omega_5^3 - 72\omega_{12}^2v_1^2\omega_5^3 + 60\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^3 + 13\omega_9^3\omega_{12}^2c_s^4\omega_5^2 - 19\omega_9^2\omega_{12}^2v_1^2\omega_5^3 - \\
& 12\omega_9^2\omega_{12}c_s^2\omega_5^3 - 39\omega_9^3\omega_{12}v_1^4\omega_5^3 - 36\omega_9^2v_1^4\omega_5^3 - 108\omega_9^2c_s^2v_1^2\omega_5^3 - 36\omega_9^3v_1^4\omega_5^3 - 12\omega_9^3\omega_{12}c_s^2\omega_5^3 + 36\omega_9^3\omega_{12}c_s^2v_1^2\omega_5^3 - 12\omega_{12}^2c_s^2\omega_5^3 - 36\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^2 - \\
& \omega_9^3\omega_{12}c_s^4\omega_5^3 + 12\omega_9^3\omega_{12}c_s^4 + 18\omega_9^2\omega_{12}c_s^2v_1^2\omega_5^2 + 6\omega_9^2\omega_{12}c_s^2\omega_5^3 + 36\omega_9^3\omega_{12}v_1^4\omega_5^2 - 306\omega_9\omega_{12}^2c_s^2v_1^2\omega_5^3 + 108\omega_9^3c_s^2v_1^2\omega_5^3 + 36\omega_9^3v_1^2\omega_5^2 - \\
& 90\omega_9\omega_{12}^2v_1^4\omega_5^3 + 6\omega_9^3\omega_{12}v_1^2\omega_5^2 + \omega_9^2\omega_{12}c_s^4\omega_5^3 - 99\omega_9^3\omega_{12}c_s^2v_1^2\omega_5^3 - 6\omega_9^3\omega_{12}c_s^2\omega_5^3 + 36\omega_9\omega_{12}v_1^2\omega_5^3 + 12\omega_9\omega_{12}^2c_s^2\omega_5^2 - 108\omega_9^2c_s^2v_1^2\omega_5^3 + 72\omega_{12}^2v_1^4\omega_5^3 - \\
& 4\omega_9^3\omega_{12}v_1^2\omega_5^3 + 6\omega_9^2\omega_{12}c_s^4\omega_5^2 + 72\omega_9\omega_{12}v_1^4\omega_5^3 + 18\omega_9^3\omega_{12}c_s^2\omega_5^2 + 54\omega_9^3\omega_{12}c_s^2v_1^2\omega_5^2 - 24\omega_9^3\omega_{12}c_s^4\omega_5 + 12\omega_9\omega_{12}^2c_s^2\omega_5^3 \\
C_9 &= 12\omega_9^2\omega_{12}v_1^2\omega_5^2\omega_{15} - 12\omega_9\omega_{12}^2v_1^2\omega_5^2\omega_{21}\omega_{15} + 12\omega_9^3v_1^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9^3\omega_{12}^2\omega_5 + 12\omega_9^3\omega_5\omega_{21}\omega_{15} + 36\omega_{12}^2c_s^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_{12}^2\omega_5^2\omega_{21}\omega_{15} + \\
& 18\omega_9^3\omega_{12}c_s^2\omega_5^2\omega_{21} - 6\omega_9^2\omega_{12}^2\omega_5\omega_{21} - 12\omega_9^3\omega_{12}\omega_5\omega_{15} - 12\omega_9^3\omega_{12}v_1^2\omega_5\omega_{21}\omega_{15} - 36\omega_9^3\omega_{12}c_s^2\omega_5^2\omega_{15} - 18\omega_9^3\omega_{12}c_s^2\omega_5^2 - 18\omega_9^2\omega_{12}^2\omega_5\omega_{21}\omega_{15} + \\
& 36\omega_9^3\omega_{12}c_s^2\omega_{21}\omega_{15} + 54\omega_9^2\omega_{12}^2c_s^2\omega_5\omega_{21}\omega_{15} + 18\omega_9^3\omega_{12}v_1^2\omega_5\omega_{21}\omega_{15} - 6\omega_9^3\omega_{12}^2\omega_5^2\omega_{15} - \omega_9^3\omega_{12}^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9^2\omega_{12}^2v_1^2\omega_5\omega_{21} - \\
& 12\omega_9\omega_{12}^2v_1^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9^2\omega_{12}^2v_1^2\omega_{21}\omega_{15} + 12\omega_9^3\omega_{12}v_1^2\omega_5\omega_{15} + 6\omega_9^3\omega_{12}^2v_1^2\omega_5^2\omega_{15} + 12\omega_9\omega_{12}\omega_5^2\omega_{21}\omega_{15} - 36\omega_9^3c_s^2\omega_5\omega_{21}\omega_{15} + 36\omega_9^3\omega_{12}^2c_s^2\omega_5 + \\
& 18\omega_9^3\omega_{12}v_1^2\omega_5^2\omega_{21}\omega_{15} - 36\omega_9^2c_s^2\omega_5^2\omega_{21}\omega_{15} + 5\omega_9^3\omega_{12}^2c_s^2\omega_5^2\omega_{21}\omega_{15} + 12\omega_9^3\omega_{12}\omega_5\omega_{21}\omega_{15} + 6\omega_9^2\omega_{12}^2\omega_5^2\omega_{15} - 18\omega_9^2\omega_{12}^2c_s^2\omega_5^2\omega_{15} - \\
& 2\omega_9^2\omega_{12}^2v_1^2\omega_5^2\omega_{21}\omega_{15} - 36\omega_9^2\omega_{12}^2c_s^2\omega_5\omega_{15} - 18\omega_9^3\omega_{12}\omega_5\omega_{21}\omega_{15} - 18\omega_9^3\omega_{12}c_s^2\omega_5^2\omega_{21}\omega_{15} - 18\omega_9^2\omega_{12}^2\omega_5^2\omega_{21}\omega_{15} + 6\omega_9^3\omega_{12}^2\omega_5^2 - 12\omega_9^3\omega_{12}v_1^2\omega_{21}\omega_{15} + \\
& 36\omega_9^3c_s^2\omega_5^2\omega_{21}\omega_{15} + 18\omega_9^3\omega_{12}^2c_s^2\omega_5^2\omega_{15} - 36\omega_9\omega_{12}^2c_s^2\omega_5^2\omega_{21}\omega_{15} - 40\omega_9^3\omega_{12}^2c_s^2\omega_5\omega_{21}\omega_{15} - 12\omega_9^2\omega_{12}^2\omega_5^2\omega_{15} - 12\omega_9^2\omega_{12}^2\omega_5\omega_{21}\omega_{15} + \\
& 12\omega_{12}^2v_1^2\omega_5^2\omega_{21}\omega_{15} - 6\omega_9^2\omega_{12}^2v_1^2\omega_5^2\omega_{15} + 54\omega_9^3\omega_{12}c_s^2\omega_5\omega_{21}\omega_{15} - 12\omega_9^3\omega_{12}^2v_1^2\omega_5\omega_{15} + 6\omega_9^3\omega_{12}\omega_5^2\omega_{21}\omega_{15} + 18\omega_9^2\omega_{12}^2v_1^2\omega_5\omega_{21}\omega_{15} + \\
& 12\omega_9^2\omega_5^2\omega_{21}\omega_{15} + 12\omega_9^3\omega_{12}^2v_1^2\omega_5 - 36\omega_9\omega_{12}^2c_s^2\omega_5^2\omega_{21}\omega_{15} - 36\omega_9^3\omega_{12}^2c_s^2\omega_{21}\omega_{15} - 6\omega_9^3\omega_{12}^2v_1^2\omega_5^2 - 12\omega_9^3v_1^2\omega_5\omega_{21}\omega_{15} + 36\omega_9^2\omega_{12}^2c_s^2\omega_5^2\omega_{15} + \\
& 6\omega_9^2\omega_{12}^2v_1^2\omega_5^2\omega_{21} - 12\omega_9^2v_1^2\omega_5^2\omega_{21}\omega_{15} + 12\omega_9^2\omega_{12}^2\omega_5\omega_{15} + \omega_9^2\omega_{12}^2v_1^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9^2\omega_{12}^2v_1^2\omega_5^2\omega_{15} + 54\omega_9^2\omega_{12}^2c_s^2\omega_5\omega_{21}\omega_{15} + \\
& 12\omega_9\omega_{12}^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9^3\omega_5^2\omega_{21}\omega_{15} + 12\omega_9^3\omega_{12}^2v_1^2\omega_{21}\omega_{15} - 6\omega_9^3\omega_{12}v_1^2\omega_5^2\omega_{21}\omega_{15} + 2\omega_9^2\omega_{12}^2\omega_5^2\omega_{21}\omega_{15} - 6\omega_9^2\omega_{12}^2c_s^2\omega_5^2\omega_{21}\omega_{15} - \\
& 36\omega_9^2\omega_{12}^2c_s^2\omega_5\omega_{21} + 12\omega_9^2\omega_{12}^2\omega_5\omega_{21} + 36\omega_9^3\omega_{12}c_s^2\omega_5\omega_{15} - 36\omega_9^3\omega_{12}c_s^2\omega_{21}\omega_{15} + 12\omega_9^3\omega_{12}^2\omega_5\omega_{21}\omega_{15} + 12\omega_9^3\omega_{12}\omega_5^2\omega_{15} + 12\omega_9^2\omega_{12}^2\omega_5\omega_{21}\omega_{15}
\end{aligned}$$

$$\begin{aligned}
C_{10} = & 36\omega_9v_1^2\omega_5^3\omega_{15} - 36\omega_9^2\omega_{12}v_1^2\omega_5^2\omega_{15} + 6\omega_9^2\omega_{12}\omega_5^3 + 12\omega_9^2c_s^2\omega_5^2\omega_{15} - 12\omega_9^2\omega_5^3\omega_{21}\omega_{15} - 6\omega_9\omega_{12}c_s^2\omega_5^2\omega_{21}\omega_{15} + 18\omega_9^2\omega_{12}c_s^2\omega_5\omega_{21}\omega_{15} - \\
& 6\omega_9\omega_{12}\omega_5^3\omega_{21} + 18\omega_{12}v_1^2\omega_5^3\omega_{21}\omega_{15} + 36\omega_9^2v_1^2\omega_5\omega_{21}\omega_{15} + 18\omega_9\omega_{12}v_1^2\omega_5^2\omega_{21} - 12\omega_{12}c_s^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9^2\omega_{12}\omega_5^2 - 12\omega_9\omega_5^3\omega_{21}\omega_{15} + \\
& 72\omega_9\omega_{12}v_1^2\omega_5^2\omega_{21}\omega_{15} - 6\omega_{12}\omega_5^3\omega_{21}\omega_{15} + 12\omega_9\omega_{12}\omega_5^2\omega_{21} - 24\omega_9\omega_{12}\omega_5^2\omega_{21}\omega_{15} - 18\omega_9^2\omega_{12}v_1^2\omega_5^3 + 6\omega_9\omega_{12}\omega_5^2\omega_{15} - 36\omega_9v_1^2\omega_5^3\omega_{21}\omega_{15} - \\
& 24\omega_9^2c_s^2\omega_5^2\omega_{21}\omega_{15} + 18\omega_9^2\omega_{12}v_1^2\omega_5^3\omega_{15} - 12\omega_9^2c_s^2\omega_5^3\omega_{15} + 36\omega_9^2\omega_{12}v_1^2\omega_5^3 + 36\omega_9^2v_1^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_9\omega_5^3\omega_{15} - 12\omega_9^2\omega_{12}c_s^2\omega_{15} - \\
& 18\omega_9\omega_{12}v_1^2\omega_5^3\omega_{15} + 12\omega_9c_s^2\omega_5^2\omega_{21}\omega_{15} - \omega_9^2\omega_{12}c_s^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_9\omega_{12}c_s^2\omega_5\omega_{21}\omega_{15} - 36\omega_9\omega_{12}v_1^2\omega_5^2\omega_{21} - 12\omega_9^2\omega_5\omega_{21}\omega_{15} - 18\omega_9\omega_{12}v_1^2\omega_5^3\omega_{21}\omega_{15} + \\
& 12\omega_9^2\omega_{12}c_s^2\omega_5^3 + 12\omega_{12}\omega_5^3\omega_{21}\omega_{15} + 12\omega_9\omega_{12}\omega_5\omega_{21}\omega_{15} + 12\omega_9^2\omega_{12}\omega_5^2\omega_{15} + 12\omega_9^2c_s^2\omega_5\omega_{21}\omega_{15} + 6\omega_{12}c_s^2\omega_5^3\omega_{21}\omega_{15} - 36\omega_9v_1^2\omega_5^3\omega_{15} + \\
& 6\omega_9^2\omega_{12}c_s^2\omega_5\omega_{15} + 12\omega_9\omega_5^3\omega_{21}\omega_{15} + 12\omega_9^2\omega_5^3\omega_{15} - 36\omega_{12}v_1^2\omega_5^2\omega_{15} - 6\omega_9^2\omega_{12}c_s^2\omega_5 - 6\omega_9\omega_{12}c_s^2\omega_5^3\omega_{21}\omega_{15} + 24\omega_9^2\omega_{12}c_s^2\omega_5\omega_{21}\omega_{15} - \\
& 12\omega_9^2\omega_{12}c_s^2\omega_5\omega_{21} + 36\omega_9^2v_1^2\omega_5\omega_{15} + 12\omega_9^2c_s^2\omega_5^3\omega_{15} - 12\omega_9^2\omega_{12}c_s^2\omega_5^2\omega_{15} - 6\omega_9^2\omega_{12}\omega_5^3\omega_{15} - 72\omega_9^2v_1^2\omega_5^2\omega_{21}\omega_{15} - 4\omega_9^2\omega_{12}c_s^2\omega_5^2\omega_{21}\omega_{15} - \\
& 12\omega_9c_s^2\omega_5^3\omega_{21}\omega_{15} + 36\omega_9v_1^2\omega_5^2\omega_{21}\omega_{15} + 6\omega_9\omega_{12}c_s^2\omega_5^2\omega_{21} + 12\omega_9^2c_s^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_9^2\omega_5^2\omega_{15} + 6\omega_9\omega_{12}\omega_5^3\omega_{21}\omega_{15} - 36\omega_9\omega_{12}v_1^2\omega_5\omega_{21}\omega_{15}
\end{aligned}$$

$$C_{12} = 18\omega_9\omega_{12}\omega_{10}\omega_5^2\omega_{21} - 5\omega_9\omega_{12}c_s^2\omega_5^3\omega_{21}\omega_{15} - 6\omega_9\omega_{12}\omega_{10}\omega_5^3\omega_{15} - 12c_s^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_9\omega_{12}c_s^2\omega_{10}\omega_{21}\omega_{15} - 6\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^3 + 12\omega_9\omega_{12}c_s^2\omega_{10}\omega_5\omega_{21} + 54\omega_9\omega_{12}v_2^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_{10}v_2^2\omega_5^3\omega_{15} - 3\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^2\omega_{21}\omega_{15} - 12\omega_9\omega_{10}v_2^2\omega_5^3\omega_{15} - 36\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^2\omega_{15} + 12\omega_9\omega_{12}v_2^2\omega_5^2\omega_{21}\omega_{15} + 18\omega_{12}v_2^2\omega_5^3\omega_{21}\omega_{15} - 18\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^3\omega_{21} - 12\omega_9c_s^2\omega_{10}\omega_5^3\omega_{15} + 12\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^3 - 6\omega_{12}v_2^2\omega_5^3\omega_{21}\omega_{15} - 5\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15} - 18\omega_9\omega_{12}\omega_5^2\omega_{21}\omega_{15} + 12\omega_9\omega_{12}\omega_{10}\omega_5^3\omega_{21} + 12\omega_9c_s^2\omega_{10}\omega_5^2\omega_{15} + 36\omega_{10}v_2^2\omega_5^3\omega_{15} - 12\omega_9c_s^2\omega_5^2\omega_{21}\omega_{15} - 54\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^2\omega_{21} - 12\omega_9\omega_{12}c_s^2\omega_5\omega_{21}\omega_{15} - 6\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{15} + 36\omega_9v_2^2\omega_5^3\omega_{21}\omega_{15} + 12\omega_9\omega_{10}\omega_5^3\omega_{15} + 18\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^3\omega_{15} + 36\omega_9\omega_{12}\omega_{10}v_2^2\omega_5\omega_{21} - \omega_9\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15} + 12\omega_9\omega_{12}\omega_5^2\omega_{21}\omega_{15} + 6\omega_{12}c_s^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_9\omega_5^3\omega_{21}\omega_{15} + 6\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{21} - 36\omega_9\omega_{10}v_2^2\omega_5^3\omega_{15} - 15\omega_9\omega_{12}v_2^2\omega_5^3\omega_{21}\omega_{15} - 36v_2^2\omega_5^3\omega_{21}\omega_{15} - 12\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^2\omega_{15} + 18\omega_9\omega_{12}c_s^2\omega_5^2\omega_{21}\omega_{15} + \omega_9\omega_{12}\omega_{10}\omega_5^2\omega_{21}\omega_{15} - 12\omega_9\omega_{12}\omega_{10}\omega_5^2 - 36\omega_9v_2^2\omega_5^2\omega_{21}\omega_{15} - 36\omega_9\omega_{12}v_2^2\omega_5^2\omega_{21}\omega_{15} + 12\omega_9c_s^2\omega_{10}\omega_{21}\omega_{15} - 18\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^3 + 6\omega_{12}\omega_{10}\omega_5^3\omega_{15} - 18\omega_{12}\omega_{10}v_2^2\omega_5^3\omega_{15} - 12\omega_9\omega_{12}\omega_{10}\omega_5\omega_{21} + 6\omega_9\omega_{12}\omega_{10}\omega_5^2 + 6\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^3\omega_{15} + 18\omega_9\omega_{12}c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15} + 36\omega_9\omega_{12}\omega_{10}v_2^2\omega_5^2 + 36\omega_9\omega_{10}v_2^2\omega_5^2\omega_{15} + 5\omega_9\omega_{12}\omega_5^3\omega_{21}\omega_{15} + 12c_s^2\omega_{10}\omega_5^3\omega_{15} + 12\omega_5^3\omega_{21}\omega_{15} - 18\omega_9\omega_{12}c_s^2\omega_{10}\omega_5^2\omega_{21}$$

$$C_{14} = -\omega_9^2 \omega_6^3 c_s^2 \omega_{13}^2 + 36 \omega_9^2 \omega_6^3 v_1^2 - 36 \omega_9 \omega_6^3 \omega_{13} v_1^4 - 18 \omega_9^3 \omega_6^2 c_s^2 \omega_{13}^2 v_1^2 - 18 \omega_9^3 \omega_6^2 c_s^4 \omega_{13} + 6 \omega_9^3 \omega_6^2 c_s^4 \omega_{13}^2 + 6 \omega_9^3 \omega_6^2 c_s^2 \omega_{13}^2 - 306 \omega_9 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2 + 4 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^4 - 99 \omega_9^3 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2 - 6 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} - 108 \omega_9^3 \omega_6^3 c_s^2 v_1^2 + 60 \omega_9^2 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2 + 12 \omega_9 \omega_6^3 c_s^2 \omega_{13}^2 + 39 \omega_9^3 \omega_6^3 \omega_{13} v_1^2 - 36 \omega_9^3 \omega_6^2 v_1^4 + 90 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^2 - 12 \omega_9 \omega_6^3 c_s^4 \omega_{13} - 72 \omega_9^3 \omega_6^3 \omega_{13} v_1^2 + 36 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^2 - 72 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^2 - 12 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} + 36 \omega_9^3 \omega_6^3 v_1^4 + 12 \omega_9^3 \omega_6^3 c_s^4 \omega_{13} + 54 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} v_1^2 + 19 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^2 + 6 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} - 36 \omega_9 \omega_6^3 c_s^2 \omega_{13}^2 + 13 \omega_9^3 \omega_6^3 c_s^2 \omega_{13}^2 + 6 \omega_9^3 \omega_6^3 \omega_{13} v_1^2 - 12 \omega_9 \omega_6^3 c_s^4 \omega_{13} + 72 \omega_9^3 \omega_6^3 v_1^4 - 3 \omega_9^3 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2 + 72 \omega_9^3 \omega_6^3 \omega_{13} v_1^4 - 36 \omega_9^3 \omega_6^3 \omega_{13} v_1^2 + 12 \omega_9 \omega_6^3 c_s^2 \omega_{13}^2 - 19 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^2 + \omega_9^3 \omega_6^3 c_s^2 \omega_{13} + 108 \omega_9^3 \omega_6^3 c_s^2 v_1^2 + 18 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} - 6 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^4 + 36 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} v_1^2 - 24 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} - 6 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} - 36 \omega_9^3 \omega_6^3 v_1^4 + 6 \omega_9^3 \omega_6^3 c_s^4 \omega_{13} - 12 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} + 198 \omega_9^3 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2 + 12 \omega_9^3 \omega_6^4 \omega_{13}^2 + 12 \omega_9^3 \omega_6^4 \omega_{13} - 108 \omega_9^3 \omega_6^3 c_s^2 v_1^2 - 4 \omega_9^3 \omega_6^3 \omega_{13}^2 v_1^2 - \omega_9^3 \omega_6^4 \omega_{13}^2 - 36 \omega_9^3 \omega_6^4 \omega_{13} - 6 \omega_9^3 \omega_6^4 \omega_{13} + 252 \omega_9^3 \omega_6^4 \omega_{13}^2 v_1^2 + 36 \omega_9 \omega_6^3 \omega_{13} v_1^2 - 5 \omega_9^3 \omega_6^2 c_s^2 \omega_{13} + 36 \omega_9^3 \omega_6^2 v_1^2 - 90 \omega_9 \omega_6^3 \omega_{13}^2 v_1^4 + 36 \omega_9^3 \omega_6^3 c_s^2 \omega_{13} v_1^2 - 108 \omega_9 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2 - 12 \omega_6^3 c_s^2 \omega_{13} - 39 \omega_9^3 \omega_6^3 \omega_{13} v_1^4 + 12 \omega_9^3 \omega_6^3 c_s^2 \omega_{13}^2 v_1^2$$

$$\begin{aligned}
& 6\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{22}\omega_{18} - 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_9\omega_6\omega_{22}\omega_{13}\omega_{18} - 6\omega_2^3\omega_6^2\omega_{13}\omega_{18} - \\
& 12\omega_2^3\omega_6\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 6\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 12\omega_9\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 6\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - \\
& 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 54\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 18\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - \\
& 6\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 18\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{22}\omega_{18} - 12\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{13}\omega_{18} - 6\omega_2^3\omega_6\omega_{13}\omega_{18} - 36\omega_2^3\omega_6^2\omega_{13}\omega_{18} - \\
& 36\omega_2^3\omega_6\omega_{22}\omega_{13} - 6\omega_2^3\omega_6\omega_{13}\omega_{18} - 36\omega_2^3\omega_6^2\omega_{13}\omega_{18} + 54\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 36\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{13} - \\
& 6\omega_2^3\omega_6\omega_{22}\omega_{13} - 18\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{13}\omega_{18} + 6\omega_2^3\omega_6\omega_{13}\omega_{18} + 18\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 12\omega_2^3\omega_6\omega_{22}\omega_{13} - 18\omega_2^3\omega_6^2\omega_{13} + \\
& 36\omega_2^3\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_{22}\omega_{13}\omega_{18} - 12\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} - 18\omega_2^3\omega_6\omega_{22}\omega_{13}\omega_{18} + 36\omega_2^3\omega_{22}\omega_{13}\omega_{18} - 18\omega_2^3\omega_{22}\omega_{13}\omega_{18}
\end{aligned}$$

[illegible]

$2w_{9w12w6w22c_{13}w13w14v2w5w18} + 2w_{12w6c_{13}w20w14v2w8w5w18} + 2w_{9w12w6w22w13w14v2v_{17}w18} + 2w_{9w12w22c_{13}w20w14v1w5w18} +$
 $2w_{9w12w22w13w20v2v_{17}w5w18} + w_{9w6w22w13w20w14v2w8v_{17}w5w18} + 2w_{12w6w22c_{13}w20w14w8v1w5w18} + 2w_{9w12w6w22w20w14v2w8v_{17}w5w18} -$
 $2w_{9w12w6w22c_{13}w13w20v2w8w18} + w_{12w6c_{13}w13w20w14w8v1w5w18} - 2w_{9w12w22c_{13}w20w14w8v1w5w18} + 2w_{12w6w22c_{13}w20v2w8w5w18} -$
 $2w_{9w12w6w22w13w20v2v_{17}w5w18} - 2w_{6w6w22w13w20v2v_{17}w8v1w5w18} + w_{9w12w6w13w20w14v2w8v_{17}w5w18} - 2w_{9w12w22c_{13}w13w20v2w8w5w18} +$
 $w_{9w12w6w22c_{13}w13w14w8v1w5} + 2w_{9w12c_{13}w13w20w14w8v1w5w18} - 2w_{9w12w22c_{13}w20w14w8v1w5w18} - 2w_{9w12c_{13}w20w14w8v1w5w18} -$
 $w_{9w12w6w13w20w14v2w8v_{17}w5} + 2w_{9w12w22w13w14v2v_{17}w5w18} + 2w_{9w12w22c_{13}w20w14w8v1w5w18} - 2w_{12w6w22c_{13}w20v2w8w5w18} -$
 $2w_{9w12w6w22w20v2w8v_{17}w5w18} + w_{9w6w22w13w20w14v2v_{17}w8v1w5w18} - 2w_{9w12w6w22w13w20w14v2v_{17}w5w18} -$
 $2w_{9w12w6w22w13w20w14v2v_{17}w5w18} - 2w_{12w6w22w20v2v_{17}w8v1w5w18} + w_{9w12w6w22w13w20w14v2v_{17}w5w18} - 2w_{9w12w6w22c_{13}w13w14v2w5w18} +$
 $w_{6w22w13w20w14v2v_{17}w5w18} + w_{6w22w13w20w14v2v_{17}w5w18} - 2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} +$
 $2w_{9w12w6w22w13w20w14v2v_{17}w5w18} - w_{9w12w6w22w13w20w14v2v_{17}w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} -$
 $2w_{9w12w6w22c_{13}w13w20w14v2v_{17}w5w18} + 2w_{9w12w6w22c_{13}w13w20w14v1w18} + w_{9w6w22c_{13}w13w20w14v2w8w5w18} + w_{9w12w6c_{13}w13w20w14w8v1w5} -$
 $2w_{9w12w6w22c_{13}w13w20w14v1w5w18} - w_{9w12w6w22w13w20w14v1w5w18} - w_{9w12w6w22w13w20w14v1w5w18} - w_{9w12w6w22w13w20w14v1w5w18} -$
 $w_{6w22w13w20w14v2v_{17}w5w18} + w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} -$
 $w_{6w22w13w20w14v2w8w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} -$
 $w_{9w12w6w22c_{13}w13w14w8v1w5w18} - w_{9w12w6w22w13w20w14v2v_{17}w5w18} - w_{9w12w6w22w13w20w14v2v_{17}w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} +$
 $2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} + 2w_{9w12w6w22c_{13}w13w20v2w8w5w18} - w_{6w22c_{13}w13w20w14v2w8w5w18} + w_{12w6w22w13w20w14v2w8v_{17}w5w18} +$
 $2w_{9w12w22c_{13}w13w20w14w8v1w5w18} + w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - 2w_{9w12w22c_{13}w13w20w14w8v1w5w18} - 2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} -$
 $2w_{9w12w6w22c_{13}w13w20w14w8v1w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} -$
 $2w_{9w12w6w22c_{13}w13w14v2w8w5w18} - 2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22c_{13}w13w20w14v2w8v_{17}w5w18} +$
 $2w_{9w12w6w22c_{13}w13w14v1w18} - 2w_{9w12w6c_{13}w20w14v2w8w5w18} - w_{9w12w6c_{13}w13w20w14w8v1w5w18} + 2w_{12w6w22w13w20v2w8v_{17}w5w18} +$
 $2w_{9w12w22w13w20w14v2w8v_{17}w5w18} + w_{9w6w22c_{13}w13w20w14w8v1w18} - 2w_{9w12w22c_{13}w13w14v1w5w18} + 2w_{9w12w6w22c_{13}w13w20v2w8w5w18} -$
 $w_{9w6w22w13w20v2w8v_{17}w5w18} - w_{9w12w6w22c_{13}w13w14v2w8w5w18} + w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} + w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} +$
 $2w_{9w12w6w22c_{13}w13w14v1w18} - 2w_{9w12w6c_{13}w20w14v2w8w5w18} - w_{9w12w6c_{13}w13w20w14w8v1w5w18} + 2w_{12w6w22w13w20v2w8v_{17}w5w18} +$
 $2w_{9w12w22w13w20w14v2w8v_{17}w5w18} + w_{9w6w22c_{13}w13w20w14w8v1w18} - 2w_{9w12w22c_{13}w13w14v1w5w18} + 2w_{9w12w6w22c_{13}w13w20v2w8w5w18} -$
 $w_{9w6w22w13w20v2w8v_{17}w5w18} - w_{9w12w6w22c_{13}w13w14v2w8w5w18} + w_{9w12w6w22w13w14v2v_{17}w5w18} - 2w_{9w12w13w20w14v2w8v_{17}w5w18} +$
 $w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} + 2w_{9w12w6w22c_{13}w13w20v2w8w5w18} - 2w_{9w12w22w13w20v2w8w5w18} - 2w_{9w12w6w22w13w20v2w8v_{17}w5w18} -$
 $2w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} - 2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} -$
 $2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} -$
 $2w_{9w12w6w22c_{13}w13w20w14v2w8w5w18} - w_{9w12w6w22w13w20w14v2w8v_{17}w5w18} - w_{9w12w6w22w13w2$

$$\begin{aligned}
C_{25} = & -4\omega_6 c_s^2 v_3 w_1 v_1 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 v_3 w_2 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 w_2 v_2 w_2 w_8 w_1 w_5 - 2w_2 w_1 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - \\
& 4\omega_6 v_3 w_2 v_2 w_8 v_1 w_5 w_1 w_5 - 2\omega_6 c_s^2 w_1 v_2 w_8 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_2 w_2 w_8 v_1 w_5 w_1 w_5 + 4w_1 v_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4\omega_6 v_3 w_1 v_1 v_2 w_8 v_1 w_5 w_1 w_5 - \\
& 4\omega_6 c_s^2 w_2 v_2 w_1 w_5 w_1 w_5 - 2\omega_6 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4c_s^2 w_2 v_2 w_2 w_8 v_1 w_5 w_1 w_5 - 2c_s^2 w_2 w_1 w_1 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_2 w_1 v_2 w_8 w_1 w_5 + \\
& 4c_s^2 w_1 v_2 w_2 w_8 w_1 w_5 + 8\omega_6 v_3 w_2 v_2 v_1 w_1 w_5 w_1 w_5 + 4\omega_6 v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 2\omega_6 c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + \omega_6 c_s^2 w_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 - \\
& 4\omega_6 w_1 v_2 v_2 w_1 w_5 w_1 w_5 + \omega_6 w_2 w_1 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4c_s^2 w_2 v_1 w_5 w_1 w_5 - 4c_s^2 v_3 w_2 w_2 w_8 v_1 w_5 w_1 w_5 + 8\omega_6 v_3 w_2 v_2 w_2 w_8 v_1 w_5 w_1 w_5 - \\
& 8v_3 w_2 w_1 v_2 v_1 w_5 w_1 w_5 - \omega_6 c_s^2 w_2 w_1 v_2 w_8 w_5 w_1 w_5 + 8c_s^2 v_3 w_1 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_1 v_2 w_8 w_5 w_1 w_5 + 4c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + \\
& 2w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 w_2 w_1 v_2 w_5 w_1 w_5 + 8v_3 w_1 v_2 v_1 w_5 w_1 w_5 + \omega_6 c_s^2 w_2 w_1 v_2 w_8 w_5 w_1 w_5 + 4\omega_6 c_s^2 w_1 v_2 w_2 w_8 v_1 w_5 w_1 w_5 - \\
& 4c_s^2 w_2 w_1 v_1 w_8 v_1 w_5 w_1 w_5 - \omega_6 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 8\omega_6 c_s^2 v_3 w_1 v_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 w_2 v_2 w_8 w_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 v_3 w_2 w_2 w_8 v_1 w_5 w_1 w_5 - \\
& 2\omega_6 c_s^2 w_1 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 w_1 v_2 w_5 w_1 w_5 w_1 w_5 - 8\omega_6 v_3 w_2 w_1 v_2 v_1 w_5 w_1 w_5 - \omega_6 c_s^2 w_2 w_1 v_2 w_8 w_5 w_1 w_5 + 2w_2 v_2 w_2 w_8 v_1 w_5 w_1 w_5 - \\
& 4c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 w_2 v_2 w_8 v_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 w_2 w_1 v_2 w_5 w_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_1 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 w_2 v_2 v_2 w_5 w_1 w_5 w_1 w_5 + \\
& 4\omega_6 c_s^2 w_2 w_1 v_2 w_8 w_1 w_5 + 4c_s^2 w_2 w_1 v_2 w_5 w_1 w_5 w_1 w_5 - 4\omega_6 v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 8\omega_6 v_3 w_2 w_1 v_2 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + \\
& 2c_s^2 w_2 w_1 v_2 w_8 w_5 w_1 w_5 - 2\omega_6 w_2 v_2 w_8 v_1 w_5 w_1 w_5 - \omega_6 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4c_s^2 w_1 w_8 v_1 w_5 w_1 w_5 + 4c_s^2 w_1 w_8 v_2 w_5 w_1 w_5 w_1 w_5 - \\
& 4\omega_6 c_s^2 w_1 v_2 w_8 w_1 w_5 w_1 w_5 - 2c_s^2 w_2 w_1 v_2 w_8 w_5 w_1 w_5 - 8c_s^2 v_3 w_1 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - \\
& 8\omega_6 c_s^2 v_3 w_2 w_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 w_2 v_1 w_8 w_1 w_5 + 8c_s^2 v_3 w_1 w_8 v_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + 4v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + \\
& 8v_3 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 8\omega_6 c_s^2 v_3 w_2 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 8\omega_6 c_s^2 v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 8\omega_6 c_s^2 v_3 w_2 w_1 v_1 w_5 w_1 w_5 - \\
& 4\omega_6 v_3 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 w_2 v_2 w_8 v_1 w_5 w_1 w_5 + 8\omega_6 c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 - 8v_3 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 4\omega_6 c_s^2 v_3 w_1 w_8 v_1 w_5 w_1 w_5 + \\
& 8c_s^2 v_3 w_2 v_1 w_5 w_1 w_5 - 8c_s^2 v_3 w_2 w_1 v_1 w_5 w_1 w_5 + 2c_s^2 w_2 v_2 w_8 w_5 w_1 w_5 + 4\omega_6 v_3 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 w_2 w_8 v_1 w_8 w_1 w_5 - \\
& 2\omega_6 c_s^2 w_2 v_2 w_8 w_5 w_1 w_5 + 4\omega_6 c_s^2 v_3 w_1 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 8\omega_6 v_3 w_2 v_2 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_2 v_2 w_8 w_5 w_1 w_5 - \\
& 4w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 v_3 w_2 v_2 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_2 w_1 w_8 v_1 w_5 w_1 w_5 - 4c_s^2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 + 2c_s^2 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - \\
& 4\omega_6 w_2 w_1 v_2 v_2 w_5 w_1 w_5 + 2c_s^2 w_2 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 v_3 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + 4w_2 w_1 v_2 v_2 w_5 w_1 w_5 + \omega_6 c_s^2 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + \\
& 2w_6 w_1 v_2 w_8 v_1 w_8 w_1 w_5 - 4\omega_6 w_2 v_2 w_8 v_1 w_5 w_1 w_5 - 2\omega_6 c_s^2 w_2 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_1 v_2 w_8 w_1 w_5 w_1 w_5 - 8\omega_6 c_s^2 v_3 w_2 w_8 v_1 w_8 w_1 w_5 + \\
& 4\omega_6 w_1 v_2 v_2 w_5 w_1 w_5 + 2\omega_6 w_2 v_2 w_8 v_1 w_5 w_1 w_5 - 4w_2 v_2 v_2 w_5 w_1 w_5 - 2\omega_6 v_3 w_2 w_1 v_2 w_8 v_1 w_5 w_1 w_5 - 8\omega_6 v_3 w_2 v_2 w_8 v_1 w_5 w_1 w_5 - \\
& 4\omega_6 c_s^2 w_1 v_1 w_8 w_1 w_5 - 4c_s^2 w_1 v_2 w_5 w_1 w_5 w_1 w_5 - 4\omega_6 w_2 v_2 v_2 w_1 w_5 w_1 w_5 + 8\omega_6 v_3 w_1 v_2 v_1 w_5 w_1 w_5 - 4v_3 w_2 v_2 w_8 v_1 w_5 w_1 w_5 + 8\omega_6 c_s^2 v_3 w_1 v_1 w_8 w_1 w_5 - \\
& \omega_6 c_s^2 w_2 w_1 w_8 v_1 w_5 w_1 w_5 + 2\omega_6 c_s^2 w_1 w_8 v_1 w_5 w_1 w_5 + 4\omega_6 c_s^2 w_2 w_1 v_2 w_8 w_1 w_5 + 8v_3 w_2 w_2 v_1 w_5 w_1 w_5 - 2\omega_6 c_s^2 w_2 w_1 v_2 w_8 w_1 w_5 w_1 w_5
\end{aligned}$$

$$\begin{aligned}
C_{27} = & 36\omega_9\omega_6^2v_3^2w_{13}w_{11} + 12\omega_9\omega_6\omega_{22}w_{13}w_{18} - 6\omega_9\omega_6^3w_{22}w_{13}w_{11} + 6\omega_9\omega_3^2w_{22}c_s^2w_{13}w_{11} + 12\omega_9\omega_3^3w_{11}w_{18} - 12\omega_9\omega_6w_{22}c_s^2w_{13}w_{18} - \\
& 3\omega_9\omega_6^2w_{22}v_3^2w_{13}w_{11}w_{18} - 12\omega_9\omega_3^2w_{22}c_s^2w_{18} + 36\omega_9\omega_6^2w_{22}v_3^2w_{18} - 12\omega_9\omega_3^2c_s^2w_{11}w_{18} - 6\omega_9\omega_6^3w_{13}w_{11}w_{18} + 18\omega_9\omega_6^2w_{22}c_s^2w_{13}w_{18} - 6\omega_6^2w_{22}w_{13}w_{18} + \\
& \omega_9\omega_6^2w_{22}w_{13}w_{11}w_{18} + 18\omega_9\omega_6^3v_3^2w_{13}w_{11}w_{18} + 18\omega_9\omega_6w_{22}c_s^2w_{13}w_{11}w_{18} + 12\omega_9\omega_6^2w_{22}w_{18} + 12\omega_9\omega_6^2w_{13}w_{11}w_{18} + 36\omega_6^3v_3^2w_{11}w_{18} + \\
& 12\omega_9\omega_6^2c_s^2w_{11}w_{18} - 36\omega_9\omega_6^2w_{22}v_3^2w_{18} + 36\omega_9\omega_6w_{22}v_3^2w_{13}w_{11} - 12\omega_9\omega_6^2w_{22}v_3^2w_{13}w_{11} - 15\omega_9\omega_6^2w_{22}v_3^2w_{13}w_{18} - 5\omega_9\omega_6^2w_{22}c_s^2w_{13}w_{11}w_{18} - \\
& 12\omega_3^3w_{11}w_{18} - 18\omega_9\omega_3^2v_3^2w_{13}w_{11} + 6\omega_6^2w_{22}c_s^2w_{13}w_{18} + 18\omega_9\omega_6w_{22}w_{13}w_{11} + 12\omega_9\omega_3^2w_{22}c_s^2w_{18} + 6\omega_9\omega_6^3c_s^2w_{13}w_{11}w_{18} - 54\omega_9\omega_6^2w_{22}v_3^2w_{13}w_{11} - \\
& 36\omega_9\omega_6^3v_3^2w_{11}w_{18} + 54\omega_9\omega_6^2w_{22}v_3^2w_{13}w_{18} + 12\omega_6^3w_{22}w_{18} - 18\omega_9\omega_6^2w_{22}w_{13}w_{18} + 12\omega_9\omega_6^2c_s^2w_{13}w_{11} - 18\omega_3^2v_3^2w_{13}w_{11}w_{18} + 18\omega_9\omega_6^2w_{22}v_3^2w_{13}w_{11} - \\
& 12\omega_9\omega_6^2c_s^2w_{13}w_{11}w_{18} - 36\omega_9\omega_6w_{22}v_3^2w_{13}w_{18} - 12\omega_9\omega_6^2w_{11}w_{18} - 12\omega_6^2w_{22}c_s^2w_{18} - 6\omega_9\omega_6^2c_s^2w_{13}w_{11} + 18\omega_6^2w_{22}v_3^2w_{13}w_{18} - 12\omega_9\omega_6^2c_s^2w_{13}w_{11}w_{18} - \\
& 18\omega_9\omega_6^2w_{22}c_s^2w_{13}w_{11} - 6\omega_6^3c_s^2w_{13}w_{11}w_{18} + 6\omega_9\omega_6^3w_{13}w_{11} + 6\omega_3^2w_{13}w_{11}w_{18} - 36\omega_9\omega_6^2v_3^2w_{13}w_{11}w_{18} + 12\omega_6^2c_s^2w_{11}w_{18} + 36\omega_9\omega_6^2v_3^2w_{11}w_{18} + \\
& 12\omega_9\omega_6w_{22}c_s^2w_{13}w_{11} - 36\omega_6^2w_{22}w_{18} - \omega_9\omega_3^2w_{22}c_s^2w_{13}w_{11}w_{18} - 5\omega_9\omega_6^2w_{22}c_s^2w_{13}w_{18} - 12\omega_9\omega_6^2w_{22}w_{18} + 5\omega_9\omega_6^2w_{22}w_{13}w_{18} - 12\omega_9\omega_6^2w_{22}w_{13}w_{11}
\end{aligned}$$

2.4.4 Conservation of momentum: ρv_2

attached text file: output_d3q27_nse_clbm1_symbolic_pde_02.txt

$$\begin{aligned}
& (-2 + 4c_s^2 - 3\omega_{10}v_2^2 + \omega_{10} - 2c_s^2\omega_{10} + 6v_2^2) \frac{\delta_l^2}{\delta_t\omega_{10}} \frac{\partial\rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_{10}) \frac{3\rho v_2\delta_l^2}{\delta_t\omega_{10}} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_7) \frac{c_s^2\delta_l^2}{2\delta_t\omega_7} \frac{\partial\rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\
& (-2 + \omega_7) \frac{c_s^2\delta_l^2}{2\delta_t\omega_7} \frac{\partial\rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{c_s^2\rho\delta_l^2}{2\delta_t\omega_5} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_5) \frac{c_s^2\rho\delta_l^2}{2\delta_t\omega_5} \frac{\partial^2 v_1}{\partial x_1\partial x_2} + \\
& (-2 + 6c_s^2 - \omega_{10}v_2^2 + \omega_{10} - 3c_s^2\omega_{10} + 2v_2^2) \frac{v_2\delta_l^2}{2\delta_t\omega_{10}} \frac{\partial^2\rho}{\partial x_2^2} + (-2 + 2c_s^2 - 3\omega_{10}v_2^2 + \omega_{10} - c_s^2\omega_{10} + 6v_2^2) \frac{\rho\delta_l^2}{2\delta_t\omega_{10}} \frac{\partial^2 v_2}{\partial x_2^2} + \\
& (-2 + \omega_7) \frac{c_s^2\rho\delta_l^2}{2\delta_t\omega_7} \frac{\partial^2 v_3}{\partial x_2\partial x_3} + (-2 + \omega_7) \frac{c_s^2\rho\delta_l^2}{2\delta_t\omega_7} \frac{\partial^2 v_2}{\partial x_3^2} + (-1 + 3c_s^2 + v_1^2) \frac{v_2v_1\delta_l^3}{12\delta_t} \frac{\partial^3\rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{\rho v_2\delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\
& C_1 \frac{\rho v_1\delta_l^3}{6\omega_{12}\delta_t\omega_5} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 - \omega_5^2 + 12\omega_5) \frac{c_s^4\delta_l^3}{6\delta_t\omega_5^2} \frac{\partial^3\rho}{\partial x_1^2\partial x_2} - \frac{c_s^2\rho v_2\delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2\partial x_2} + C_2 \frac{\rho v_2\delta_l^3}{12\delta_t\omega_{10}^2\omega_5\omega_{15}} \frac{\partial^3 v_1}{\partial x_1\partial x_2^2} + C_3 \frac{\delta_l^3}{12\delta_t\omega_{10}^2} \frac{\partial^3\rho}{\partial x_2^2} + \\
& (-24 + 5c_s^2\omega_{10}^2 + 36c_s^2 - 4\omega_{10}^2 - 60\omega_{10}v_2^2 + 24\omega_{10} - 36c_s^2\omega_{10} + 60v_2^2 + 11\omega_{10}^2v_2^2) \frac{\rho v_2\delta_l^3}{6\delta_t\omega_{10}^2} \frac{\partial^3 v_2}{\partial x_2^2} - \frac{c_s^2\rho v_2\delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2\partial x_3} + \\
& C_4 \frac{\rho v_2\delta_l^3}{12\delta_t\omega_{16}\omega_{10}^2\omega_7} \frac{\partial^3 v_3}{\partial x_2^2\partial x_3} - \frac{c_s^2\rho v_2\delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1\partial x_3^2} + (-12 - \omega_7^2 + 12\omega_7) \frac{c_s^4\delta_l^3}{6\delta_t\omega_7^2} \frac{\partial^3\rho}{\partial x_2\partial x_3^2} - \frac{c_s^2\rho v_2\delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2\partial x_3^2} + \\
& (-1 + 3c_s^2 + v_3^2) \frac{v_3v_2\delta_l^3}{12\delta_t} \frac{\partial^3\rho}{\partial x_3^3} + C_5 \frac{v_3\rho\delta_l^3}{6\omega_{19}\delta_t\omega_7} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho v_2\delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (3\omega_9v_1^2 - 2c_s^2 - \omega_9c_s^4 + 6v_1^4 - 12\omega_9c_s^2v_1^2 - 3\omega_9v_1^4 + 2c_s^4 + 24c_s^2v_1^2 + \omega_9c_s^2 - 6v_1^2) \frac{v_2\delta_l^4}{24\omega_9\delta_t} \frac{\partial^4\rho}{\partial x_1^4} + \\
& (-4 + 2\omega_9 - 5\omega_9v_1^2 + 6c_s^2 - 3\omega_9c_s^2 + 10v_1^2) \frac{\rho v_2v_1\delta_l^4}{12\omega_9\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho\delta_l^4}{24\omega_{12}^2\delta_t\omega_3^2} \frac{\partial^4 v_2}{\partial x_1^4} + C_7 \frac{c_s^2v_1\delta_l^4}{12\omega_9\omega_{12}^2\delta_t\omega_{10}\omega_5^2\omega_{21}\omega_{15}} \frac{\partial^4\rho}{\partial x_1^2\partial x_2} + \\
& C_8 \frac{c_s^2\rho\delta_l^4}{12\omega_9\omega_{12}\delta_t\omega_{10}\omega_5^2\omega_{21}\omega_{15}} \frac{\partial^4 v_1}{\partial x_1^3\partial x_2} + \\
& (3\omega_9 - 3\omega_9v_1^2 - \omega_{12} + \omega_9\omega_{12}v_1^2 - \omega_9\omega_{12} + \omega_{12}v_1^2 + 3\omega_{12}c_s^2 + 3\omega_9\omega_{12}c_s^2 - 9\omega_9c_s^2) \frac{\rho v_2v_1\delta_l^4}{12\omega_9\omega_{12}\delta_t} \frac{\partial^4 v_2}{\partial x_1^3\partial x_2} + \\
& C_9 \frac{c_s^2v_2\delta_l^4}{12\omega_{12}\delta_t\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}^2} \frac{\partial^4\rho}{\partial x_1^2\partial x_2^2} + C_{10} \frac{c_s^2\rho\delta_l^4}{12\omega_{12}\delta_t\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2^2} + C_{11} \frac{\rho\delta_l^4}{12\delta_t\omega_{10}^3\omega_5^3\omega_{15}^2} \frac{\partial^4 v_1}{\partial x_1\partial x_2^3} + C_{12} \frac{v_2\delta_l^4}{12\delta_t\omega_{10}^3} \frac{\partial^4\rho}{\partial x_2^4} + \\
& C_{13} \frac{\rho\delta_l^4}{12\delta_t\omega_{10}^3} \frac{\partial^4 v_2}{\partial x_2^4} + (3\omega_9 - 3\omega_9v_1^2 - \omega_{13} + 3c_s^2\omega_{13} + \omega_9\omega_{13}v_1^2 + 3\omega_9c_s^2\omega_{13} + \omega_{13}v_1^2 - \omega_9\omega_{13} - 9\omega_9c_s^2) \frac{\rho v_2v_1\delta_l^4}{12\omega_9\delta_t\omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + \\
& C_{14} \frac{c_s^4\rho\delta_l^4}{12\omega_{12}\omega_6\delta_t\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2\partial x_3} + C_{15} \frac{\rho\delta_l^4}{12\delta_t\omega_{16}^3\omega_{10}^3\omega_7^3} \frac{\partial^4 v_3}{\partial x_2^2\partial x_3} + C_{16} \frac{\delta_l^4}{12\omega_{12}\omega_6\omega_{19}\delta_t\omega_7\omega_{20}\omega_{14}\omega_8\omega_5} \frac{\partial^4\rho}{\partial x_1^2\partial x_3^2} + \\
& C_{17} \frac{\rho\delta_l^4}{4\omega_{12}\omega_{19}\delta_t\omega_7\omega_{20}\omega_{14}\omega_8\omega_5} \frac{\partial^4 v_1}{\partial x_1^2\partial x_3^2} + C_{18} \frac{\rho\delta_l^4}{4\omega_{12}\omega_{19}\delta_t\omega_7^2\omega_{20}\omega_{14}\omega_8\omega_5^2} \frac{\partial^4 v_2}{\partial x_1^2\partial x_3^2} + C_{19} \frac{v_3\rho\delta_l^4}{2\omega_{12}\omega_{19}\delta_t\omega_7\omega_{20}\omega_{14}\omega_8\omega_5} \frac{\partial^4 v_3}{\partial x_1^2\partial x_3^2} + \\
& C_{20} \frac{\delta_l^4}{2\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_8\omega_5\omega_{15}} \frac{\partial^4\rho}{\partial x_1\partial x_2\partial x_3^2} + C_{21} \frac{\rho\delta_l^4}{12\omega_6\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_8\omega_5^2\omega_{15}} \frac{\partial^4 v_1}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{22} \frac{\rho v_2\delta_l^4}{\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_8\omega_5\omega_{15}} \frac{\partial^4 v_2}{\partial x_1\partial x_2\partial x_3^2} + C_{23} \frac{\rho\delta_l^4}{2\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_8\omega_5\omega_{15}} \frac{\partial^4 v_3}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{24} \frac{c_s^2v_2\delta_l^4}{12\omega_{19}\delta_t\omega_{16}^3\omega_{10}^2\omega_7^2\omega_{23}} \frac{\partial^4\rho}{\partial x_2^2\partial x_3^2} + C_{25} \frac{c_s^2\rho\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_{10}^2\omega_7^2\omega_{23}} \frac{\partial^4 v_2}{\partial x_2^2\partial x_3^2} + \\
& (3c_s^2\omega_{18} + 3c_s^2\omega_{11}\omega_{18} + v_3^2\omega_{18} - 3v_3^2\omega_{11} + 3\omega_{11} - \omega_{11}\omega_{18} - 9c_s^2\omega_{11} - \omega_{18} + v_3^2\omega_{11}\omega_{18}) \frac{v_3\rho v_2\delta_l^4}{12\delta_t\omega_{11}\omega_{18}} \frac{\partial^4 v_1}{\partial x_1\partial x_3^3} + \\
& C_{26} \frac{c_s^2v_3\delta_l^4}{12\omega_{19}^2\delta_t\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11}} \frac{\partial^4\rho}{\partial x_2\partial x_3^3} + \\
& (\omega_{19}v_3^2 + \omega_{19}v_3^2\omega_{11} - \omega_{19} + 3\omega_{19}c_s^2 + 3\omega_{19}c_s^2\omega_{11} - 3v_3^2\omega_{11} + 3\omega_{11} - 9c_s^2\omega_{11} - \omega_{19}\omega_{11}) \frac{v_3\rho v_2\delta_l^4}{12\omega_{19}\delta_t\omega_{11}} \frac{\partial^4 v_2}{\partial x_2\partial x_3^3} + \\
& C_{27} \frac{c_s^2\rho\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11}} \frac{\partial^4 v_3}{\partial x_2\partial x_3^3} + \\
& (-2c_s^2 - 6v_3^2 - 3v_3^2\omega_{11} + 24c_s^2v_3^2 - 12c_s^2v_3^2\omega_{11} - c_s^4\omega_{11} + 3v_3^2\omega_{11} + c_s^2\omega_{11} + 2c_s^4 + 6v_3^4) \frac{v_2\delta_l^4}{24\delta_t\omega_{11}} \frac{\partial^4\rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho\delta_l^4}{24\omega_{19}^2\delta_t\omega_7^3} \frac{\partial^4 v_2}{\partial x_3^4} + (-4 + 6c_s^2 + 10v_3^2 - 5v_3^2\omega_{11} + 2\omega_{11} - 3c_s^2\omega_{11}) \frac{v_3\rho v_2\delta_l^4}{12\delta_t\omega_{11}} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 3\omega_{12} - 18c_s^2 - 3\omega_{12}c_s^2\omega_5 + 3\omega_{12}v_1^2 + 9c_s^2\omega_5 + 3v_1^2\omega_5 + \omega_{12}\omega_5 - 3\omega_5 + 9\omega_{12}c_s^2 - \omega_{12}v_1^2\omega_5 - 6v_1^2 \\
C_2 &= -36c_s^2\omega_{10}^2 + 12\omega_{10}^2 + 36c_s^2\omega_5\omega_{15} + 6\omega_{10}^2v_2^2\omega_{15} - 6\omega_{10}^2\omega_{15} + 12\omega_{10}^2v_2^2\omega_5 - 3\omega_{10}^2v_2^2\omega_5\omega_{15} - 36c_s^2\omega_{10}\omega_5 - 18c_s^2\omega_{10}\omega_5\omega_{15} + 12v_2^2\omega_5\omega_{15} - \\
& 12\omega_{10}^2\omega_5 + 3\omega_{10}^2\omega_5\omega_{15} - 11c_s^2\omega_{10}^2\omega_5\omega_{15} - 12\omega_{10}v_2^2\omega_5 + 6\omega_{10}\omega_5\omega_{15} + 36c_s^2\omega_{10}^2\omega_5 + 12\omega_{10}\omega_5 + 18c_s^2\omega_{10}^2\omega_{15} - 6\omega_{10}v_2^2\omega_5\omega_{15} - 12\omega_5\omega_{15} - 12\omega_{10}^2v_2^2 \\
C_3 &= 24c_s^2\omega_{10}^2v_2^2 - c_s^2\omega_{10}^2 + 36v_2^4 - 12c_s^2 + 36\omega_{10}v_2^2 + 7\omega_{10}^2v_2^4 + 12c_s^2\omega_{10} + c_s^4\omega_{10}^2 - 36\omega_{10}v_2^4 + 144c_s^2v_2^2 - 12c_s^4\omega_{10} - 36v_2^2 + 12c_s^4 - 144c_s^2\omega_{10}v_2^2 - 7\omega_{10}^2v_2^2 \\
C_4 &= -36c_s^2\omega_{10}^2 - 36c_s^2\omega_{10}\omega_7 + 18c_s^2\omega_{16}\omega_{10}^2 + 12\omega_{10}^2 + 3\omega_{16}\omega_{10}^2\omega_7 - 12\omega_{10}^2\omega_7 - 18c_s^2\omega_{16}\omega_{10}\omega_7 + 36c_s^2\omega_{16}\omega_7 + 12\omega_{10}^2\omega_7v_2^2 - 3\omega_{16}\omega_{10}^2\omega_7v_2^2 + \\
& 12\omega_{16}\omega_7v_2^2 - 12\omega_{16}\omega_7 + 36c_s^2\omega_{10}^2\omega_7 - 6\omega_{16}\omega_{10}\omega_7v_2^2 - 12\omega_{10}\omega_7v_2^2 + 6\omega_{16}\omega_{10}^2v_2^2 + 12\omega_{10}\omega_7 - 12\omega_{10}^2v_2^2 + 6\omega_{16}\omega_{10}\omega_7 - 11c_s^2\omega_{16}\omega_{10}^2\omega_7 - 6\omega_{16}\omega_{10}^2 \\
C_5 &= 6 + \omega_{19}\omega_7 - 18c_s^2 + 3\omega_{19}v_3^2 - 6v_3^2 + 9c_s^2\omega_7 - 3\omega_{19} + 9\omega_{19}c_s^2 - 3\omega_7 + 3v_3^2\omega_7 - 3\omega_{19}c_s^2\omega_7 - \omega_{19}v_3^2\omega_7
\end{aligned}$$

$$C_6 = -216c_s^2v_1^2\omega_5^2 - 24\omega_{12}c_s^2\omega_5 - 30\omega_{12}v_1^4\omega_5^3 + 24\omega_{12}^2c_s^4\omega_5^2 - 36\omega_{12}^2c_s^2v_1^2\omega_5 + 108c_s^2v_1^2\omega_5^3 + 72\omega_{12}v_1^4\omega_5^2 - 3\omega_{12}^2c_s^4\omega_5^3 - 6\omega_{12}^2c_s^2\omega_5^3 - 12\omega_{12}^2c_s^2v_1^2\omega_5^2 + 12\omega_{12}^2v_1^2\omega_5^2 - 72v_1^4\omega_5^2 - 48\omega_{12}^2c_s^4\omega_5 + 36v_1^4\omega_5^3 + 6\omega_{12}^2c_s^2v_1^2\omega_5^3 + 24\omega_{12}^2c_s^2\omega_5^2 - 3\omega_{12}^2v_1^2\omega_5^3 + \omega_{12}^2c_s^2\omega_5^3 - 72\omega_{12}v_1^2\omega_5^2 + 24\omega_{12}^2c_s^4\omega_5 - 8\omega_{12}^2c_s^2\omega_5^2 + 30\omega_{12}v_1^2\omega_5^2 + 72\omega_{12}c_s^2v_1^2\omega_5 + 12\omega_{12}^2c_s^2\omega_5 + 144\omega_{12}c_s^2v_1^2\omega_5^2 - 36v_1^2\omega_5^3 + 3\omega_{12}^2v_1^4\omega_5^3 - 24\omega_{12}c_s^4\omega_5^2 + 24\omega_{12}^2c_s^4 - 72\omega_{12}c_s^2v_1^2\omega_5^3 - 12\omega_{12}^2v_1^4\omega_5^2 + 6\omega_{12}^2c_s^4\omega_5^3 + 72v_1^2\omega_5^2$$

$$\begin{aligned} C_8 = & 18\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15} + 54\omega_{12}\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15} - 6\omega_{9\omega_{12}\omega_{10}\omega_s^3\omega_{15}} - 12\omega_{9\omega_{12}c_s^2\omega_{10}\omega_{21}\omega_{15}} - 12\omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^3} + 18\omega_{9\omega_{10}\omega_s^2\omega_{21}\omega_{15}} + \\ & 18\omega_{12}v_1^2\omega_s^2\omega_{21}\omega_{15} - 12\omega_{9\omega_{10}\omega_s^2\omega_{15}} + 6\omega_{9c_s^2\omega_{10}\omega_s^3\omega_{21}\omega_{15}} + 18\omega_{9\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15}} - 12\omega_{12}c_s^2\omega_s^3\omega_{21} - 3\omega_{9\omega_{12}\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15}} + 12\omega_{9\omega_{12}c_s^2\omega_s^3} - \\ & 6\omega_{9c_s^2\omega_{10}\omega_s^3\omega_{15}} + 12\omega_{12}c_s^2\omega_{10}\omega_s^3\omega_{21} + 12\omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^3} - 6\omega_{12}\omega_s^3\omega_{21}\omega_{15} - 18\omega_{9\omega_{10}v_1^2\omega_s^3\omega_{15}} + 36\omega_{12}\omega_{10}v_1^2\omega_s^3\omega_{21} - 5\omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15}} + \\ & 12\omega_{9\omega_{12}\omega_{10}\omega_s^2\omega_{15}} + 6\omega_{9\omega_{12}\omega_s^2\omega_{15}} + 36\omega_{9\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15}} - 18\omega_{12}\omega_{10}\omega_s^2\omega_{21}\omega_{15} + 12\omega_{9c_s^2\omega_{10}\omega_s^2\omega_{15}} + 12\omega_{9c_s^2\omega_{10}\omega_s^2\omega_{15}} - 12\omega_{12}\omega_s^2\omega_{10}\omega_s^2\omega_{21} + \\ & 36\omega_{9\omega_{10}v_1^2\omega_s^2\omega_{15}} - 36\omega_{12}\omega_{10}v_1^2\omega_s^2\omega_{21} - 18\omega_{9\omega_{12}v_1^2\omega_s^3\omega_{15}} + 6\omega_{9\omega_{10}\omega_s^3\omega_{15}} + 12\omega_{12}\omega_s^3\omega_{21} - \omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15}} + 12\omega_{12}\omega_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15} - \\ & 18\omega_{9c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15}} - 12\omega_{12}\omega_{10}\omega_s^2\omega_{21} - 36\omega_{9\omega_{12}\omega_{10}v_1^2\omega_s^3} + 6\omega_{12}c_s^2\omega_s^3\omega_{21}\omega_{15} - 54\omega_{9\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15}} - 6\omega_{9\omega_{10}\omega_s^2\omega_{21}\omega_{15}} - 6\omega_{9\omega_{12}c_s^2\omega_s^3\omega_{15}} - \\ & 15\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15} - 36\omega_{9\omega_{12}\omega_{10}v_1^2\omega_s^3\omega_{15}} - 12\omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{15}} + 36\omega_{9\omega_{12}\omega_{10}v_1^2\omega_s^2} - 15\omega_{12}\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15} + \omega_{9\omega_{12}\omega_{10}\omega_s^2\omega_{21}\omega_{15}} - \\ & 36\omega_{12}\omega_{10}v_1^2\omega_s^2\omega_{21}\omega_{15} - 12\omega_{9\omega_{12}\omega_{10}\omega_s^2} - 12\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15} - 12\omega_{9\omega_{12}\omega_s^2} + 12\omega_{12}\omega_{10}\omega_s^2\omega_{21} + 36\omega_{9\omega_{12}v_1^2\omega_s^3} - 12\omega_{9\omega_{10}\omega_s^2\omega_{21}\omega_{15}} + \\ & 18\omega_{9\omega_{12}\omega_{10}v_1^2\omega_s^3\omega_{15}} + 12\omega_{9\omega_{12}\omega_{10}\omega_s^2} + 5\omega_{12}\omega_{10}\omega_s^2\omega_{21}\omega_{15} + 6\omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{15}} - 36\omega_{12}v_1^2\omega_s^3\omega_{21} + 18\omega_{9\omega_{12}c_s^2\omega_{10}\omega_s^2\omega_{21}\omega_{15}} \end{aligned}$$

$$C_{10} = 24w_{12}w_{10}^2w_5^2w_{21} + 24w_{12}c_s^2w_{10}w_5^2w_{21}w_{15} - 12c_s^2w_{10}w_5^2w_{21}w_{15} + 36w_{12}w_{10}v_2^2w_5^3 - 6w_{12}w_{10}^2w_5^3w_{15} + 12w_{12}c_s^2w_{10}w_5^3 - 36w_{12}w_{10}^2v_2^2w_5^3w_{15} - 12w_{12}c_s^2w_5^2w_{21}w_{15} + 72w_{12}w_{10}v_2^2w_5^2w_{21}w_{15} - w_{12}c_s^2w_{10}^2w_5^2w_{21}w_{15} - 36w_{10}v_2^2w_5^2w_{21}w_{15} + 36w_{12}w_{10}^2v_2^2w_5^2w_{21} + 18w_{12}v_2^2w_5^2w_{21}w_{15} - 12w_{12}c_s^2w_{10}w_5^3w_{21} - 6c_s^2w_{10}^2w_5^3w_{15} - 6w_{12}w_5^3w_{21}w_{15} - 12w_{12}c_s^2w_{10}^2w_5^3 - 12w_{12}c_s^2w_{10}w_{21}w_{15} - 12w_{12}w_{10}^2w_5^3 + 12w_{12}c_s^2w_{10}w_5w_{21} + 18w_{12}c_s^2w_{10}w_5w_{21}w_{15} - 12w_{12}w_{10}^2w_5^2w_{21} - 24w_{12}w_{10}w_5^2w_{21}w_{15} + 12c_s^2w_{10}w_5^2w_{15} + 12w_{12}c_s^2w_{10}w_5^2w_{21} + 12w_{12}w_{10}^2w_5^2 - 72w_{12}w_{10}^2v_2^2w_5^2w_{21} - 6w_{10}w_5^2w_{21}w_{15} - 6w_{12}c_s^2w_{10}w_5^3w_{15} + 18w_{12}w_{10}^2v_2^2w_5^3w_{15} - 36w_{12}v_2^2w_5^2w_{21}w_{15} - 12w_{10}^2w_5^3 + 36w_{12}w_{10}^2v_2^2w_5w_{21} + 12w_{12}w_5^2w_{21}w_{15} - 12w_{12}w_{10}w_5^3 + 12w_{12}w_{10}w_5w_{21}w_{15} - 18w_{12}w_{10}v_2^2w_5^2w_{21}w_{15} + 12w_{12}w_{10}w_5^3w_{21}w_{15} + 6w_{12}c_s^2w_5^3w_{21}w_{15} + 18w_{10}v_2^2w_5^3w_{21}w_{15} - 4w_{12}c_s^2w_{10}^2w_5^2w_{21}w_{15} + 36w_{10}^2v_2^2w_5^3w_{15} - 36w_{12}w_{10}v_2^2w_5^3w_{21} - 24w_{12}c_s^2w_{10}^2w_5^3w_{21} - 6w_{12}c_s^2w_{10}w_5^3w_{21}w_{15} + 6c_s^2w_{10}w_5^3w_{21}w_{15} + 6w_{12}c_s^2w_{10}^2w_5^3w_{15} - 12w_{12}c_s^2w_{10}w_5w_{21}w_{15} - 12w_{12}w_{10}w_5^2w_{21} + 6w_{10}^2w_5^3w_{15} + 12w_{12}c_s^2w_{10}w_5^3 + 12w_{10}w_5^2w_{21}w_{15} - 36w_{12}w_{10}^2v_2^2w_5^3 - 36w_{12}w_{10}w_5^3w_{21}w_{15} + 6w_{12}w_{10}w_5^3w_{15} - 18w_{12}w_{10}v_2^2w_5^3w_{15} - 12w_{12}c_s^2w_{10}^2w_5^3w_{15} - 12w_{12}w_{10}^2w_5^2w_{21} - 36w_{12}w_{10}v_2^2w_5^2w_{21}w_{15} + 6w_{12}w_{10}w_5^3w_{21}w_{15} + 36w_{12}w_{10}^2v_2^2w_5^3 + 36w_{12}w_{10}v_2^2w_5^3w_{21} + 12w_{12}c_s^2w_{10}^2w_5^3w_{21} - 18w_{10}^2v_2^2w_5^3w_{15}$$

$$C_{12} = 12 + 404c_s^2\omega_{10}^2v_2^2 - 78c_s^2\omega_{10}^4 + 144v_2^4 - 132c_s^2 + 8\omega_{10}^2 + 234\omega_{10}v_2^2 + 90\omega_{10}^2v_2^4 + 6c_s^2\omega_{10}^3 - \omega_{10}^3 - 18\omega_{10} - 34c_s^2\omega_{10}^3v_2^2 + 198c_s^2\omega_{10} - 9\omega_{10}^3v_2^4 - 5c_s^4\omega_{10}^3 + 82c_s^4\omega_{10}^2 + 10\omega_{10}^3v_2^2 - 216\omega_{10}v_2^4 + 672c_s^2v_2^2 - 216c_s^4\omega_{10} - 156v_2^2 + 144c_s^4 - 1008c_s^2\omega_{10}v_2^2 - 98\omega_{10}^2v_2^2$$

$$\begin{aligned}
C_{14} = & -12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_5^2w_{15} + 12w_{12}w_7^2w_{17}w_{14}w_8w_5^2w_{15} + 12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_8w_5^3 + 6w_{12}w_6w_{16}w_{10}w_7w_{17}w_8w_5^3w_{15} + \\
& 12w_6w_{16}w_{10}w_7w_{17}w_{14}w_8w_5^2w_{15} - 18w_{12}w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^2w_{15} - 18w_{12}w_{16}w_{10}w_7w_{17}w_{14}w_8w_5^3w_{15} - 12w_6w_{16}w_{10}w_7^2w_{17}w_8w_5^3w_{15} - \\
& 24w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_8w_5^3w_{15} - 12w_{12}w_6w_{16}w_{10}w_7w_{17}w_5^3w_{15} - 12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_8w_5^2 + 12w_{12}w_6w_{16}w_{10}w_7w_{14}w_8w_5^3w_{15} + \\
& 6w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^3w_{15} - 6w_{12}w_6w_{16}w_{10}w_{17}w_{14}w_8w_5^3w_{15} + 12w_{12}w_6w_{10}w_7^2w_{14}w_8w_5^3w_{15} + 10w_{12}w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^3w_{15} - \\
& 6w_6w_{16}w_{10}w_7w_{17}w_{14}w_8w_5^3w_{15} + 12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_5^3w_{15} + 12w_{12}w_6w_{16}w_{10}w_7w_{17}w_{14}w_8w_5w_{15} + 12w_{12}w_{16}w_{10}w_{17}w_{14}w_8w_5^3w_{15} - \\
& 12w_{12}w_{16}w_{10}w_7w_{17}w_{14}w_8w_5^3w_{15} + 12w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_8w_5^2w_{15} - 12w_{12}w_6w_{10}w_7w_{14}w_8w_5^3w_{15} + 6w_6w_{16}w_{10}w_7^2w_{17}w_8w_5^3w_{15} - \\
& w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^3w_{15} - 12w_{12}w_{10}w_7^2w_{17}w_{14}w_8w_5^3w_{15} - 24w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_{15} + 12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_8w_5^2w_{15} + \\
& 12w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_5^3w_{15} + 12w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_{14}w_5^2w_{15} - 18w_{12}w_6w_{16}w_{10}w_7w_{17}w_{14}w_8w_5^2w_{15} - 12w_{12}w_6w_{16}w_{10}w_7w_{14}w_8w_5^3w_{15} + \\
& 12w_{12}w_6w_{16}w_{10}w_7w_{14}w_8w_5^3w_{15} - 12w_{12}w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^3 + 12w_{12}w_6w_{16}w_{10}w_7w_{17}w_{14}w_5^3w_{15} + 12w_{12}w_{16}w_{10}w_{17}w_{14}w_8w_5^3 - \\
& 2w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^3w_{15} + 6w_{12}w_6w_{16}w_{10}w_7w_{17}w_{14}w_8w_5^3w_{15} + 12w_{12}w_{10}w_7w_{17}w_{14}w_8w_5^3w_{15} - 12w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_{14}w_5^3w_{15} - \\
& 12w_{12}w_6w_7^2w_{14}w_8w_5^3w_{15} - 12w_{12}w_6w_{16}w_{10}w_7^2w_{17}w_5^3w_{15} + 12w_{12}w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5^2 - 12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_8w_5^3w_{15} + \\
& 12w_{12}w_{16}w_{10}w_7^2w_{17}w_{14}w_8w_5w_{15} - 12w_{12}w_6w_{16}w_{10}w_7^2w_{14}w_8w_5^3
\end{aligned}$$

[illegible]

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$$C_{22} = 2\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{17}v_1\omega_{15} - \omega_{19}c_s^2\omega_{16}\omega_{10}v_3\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_8\omega_{15} - 2\omega_{19}\omega_{16}v_3^2\omega_7\omega_{23}\omega_{20}\omega_8v_1\omega_5\omega_{15} + \omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_8v_1\omega_5\omega_{15} - \omega_{19}\omega_{16}v_3^2\omega_7\omega_{20}\omega_{17}\omega_8v_1\omega_5\omega_{15} - \omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_8v_1\omega_5\omega_{15} + 2\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{20}\omega_8v_1 + 2\omega_{19}v_3^2\omega_7\omega_{23}\omega_{20}\omega_8v_1\omega_5\omega_{15} - 2\omega_{16}\omega_{10}v_3\omega_{20}\omega_{17}\omega_8v_2^2\omega_5\omega_{15} + 2\omega_{16}\omega_{10}v_3^2\omega_{20}\omega_{17}\omega_8v_1\omega_5\omega_{15} +$$

$$12\omega_{19}c_s^2\omega_{10}\omega_7^3 + 12\omega_{19}\omega_{10}^2\omega_7^3 - 18\omega_{19}\omega_{16}\omega_{10}\omega_7^3v_2^2 + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3 + 72\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}v_2^2 - \omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3$$

$$\begin{aligned} C_{26} = & -12\omega_{19}^2\omega_{10}\omega_7^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_{23}\omega_{11} + 3\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 54\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 15\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} + \\ & 12\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{23} - 12\omega_{19}^2\omega_{10}v_3^2\omega_7^2\omega_{11} - 12\omega_{19}^2v_3^2\omega_7^2\omega_{23} - 36\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - 18\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - \\ & 12\omega_{19}^2\omega_{10}v_3^2\omega_7\omega_{23} - 12\omega_{19}^2\omega_{10}\omega_7\omega_{11} + 18c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - 18\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - \\ & 12\omega_{19}^2\omega_7^2\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_{23}\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{11} - 3\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}^2\omega_{16}\omega_7^2\omega_{23} + \\ & 12\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 5\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 36\omega_{19}^2c_s^2\omega_{10}\omega_7\omega_{23} - 5\omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23} + 36\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{11} + 6\omega_{19}^2\omega_{16}v_3^2\omega_7^2\omega_{23} + \\ & 12\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_{23}\omega_{11} + 36\omega_{19}^2c_s^2\omega_7^2\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_7\omega_{11} - 36\omega_{19}^2c_s^2\omega_{10}\omega_7^2\omega_{11} - \\ & 12\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{11} + 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - \omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}^2\omega_{16}v_3^2\omega_7^2\omega_{11} + 18\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{11} + \\ & \omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23}\omega_{11} + 36\omega_{19}^2c_s^2\omega_{10}\omega_7\omega_{11} + 6\omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 6\omega_{19}^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 6\omega_{19}^2\omega_{16}\omega_7^2\omega_{11} - \\ & 6\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 18\omega_{19}^2\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23} + 36\omega_{19}^2c_s^2\omega_{10}\omega_7^2\omega_{23} - 18\omega_{19}^2\omega_{16}\omega_{10}\omega_7\omega_{23} + 6\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23}\omega_{11} - \\ & 18\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{23} - 36\omega_{19}^2c_s^2\omega_7^2\omega_{23} - 9\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 12\omega_{19}^2\omega_{10}v_3^2\omega_7^2\omega_{23} + \\ & 12\omega_{19}^2v_3^2\omega_7^2\omega_{11} + 18\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 12\omega_{19}^2\omega_{10}\omega_7^2\omega_{11} + 3\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 18\omega_{19}^2c_s^2\omega_{16}\omega_7^2\omega_{23} + 12\omega_{19}^2\omega_7^2\omega_{23} + \\ & 54\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23} + 12\omega_{19}^2\omega_{10}\omega_7\omega_{23} + 12\omega_{19}^2\omega_{10}v_3^2\omega_7\omega_{11} - 6\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{11} - 36c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} \end{aligned}$$

$$\begin{aligned} C_{27} = & 18\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23}\omega_{11} + 36\omega_{19}v_3^2\omega_7^2\omega_{11} + 18\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 12\omega_{19}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - \\ & 12\omega_{19}^2\omega_{10}\omega_7^2\omega_{11} + 5\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 36\omega_{19}\omega_{10}v_3^2\omega_7^2\omega_{11} + 54\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23} - 6\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 5\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} - \\ & 18c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 18\omega_{19}\omega_{16}v_3^2\omega_7^2\omega_{11} + 6\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 3\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}c_s^2\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{11} - \\ & 6\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{11} - 12\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 6\omega_{19}\omega_{16}\omega_7^2\omega_{11} + 18\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 15\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23} + 12\omega_{19}\omega_7^2\omega_{23} - 12\omega_{19}c_s^2\omega_7^2\omega_{23} - \\ & \omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 36\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23}\omega_{11} - 36\omega_{19}\omega_{10}v_3^2\omega_7^2\omega_{11} + 6c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^2\omega_{23} + \\ & 36\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{11} + 6\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} - 6c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}c_s^2\omega_{10}\omega_7^2\omega_{11} + \\ & 18\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} + 36\omega_{19}\omega_{10}v_3^2\omega_7^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 12\omega_{19}c_s^2\omega_7^2\omega_{11} - 12\omega_{19}\omega_7^2\omega_{11} + \\ & 18\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{11} - 54\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 5\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}c_s^2\omega_{10}\omega_7^2\omega_{23} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} - \\ & 36\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7\omega_{23} + 12c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 36\omega_{19}v_3^2\omega_7^2\omega_{23} - 18\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{11} + \omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 18\omega_{19}\omega_{16}v_3^2\omega_7^2\omega_{11} + \\ & 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 36\omega_{19}\omega_{16}\omega_{10}v_3^2\omega_7^2\omega_{11} + 12c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 36\omega_{19}\omega_{10}v_3^2\omega_7^2\omega_{23} - 6\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{11} \end{aligned}$$

$$\begin{aligned} C_{28} = & 24\omega_{19}^2c_s^4 + 72\omega_{19}v_3^4\omega_7^2 + 72v_3^2\omega_7^2 + \omega_{19}^2c_s^2\omega_7^3 + 6\omega_{19}^2c_s^2v_3^2\omega_7^3 + 24\omega_{19}c_s^4\omega_7 - 36v_3^2\omega_7^3 - 30\omega_{19}v_3^4\omega_7^3 - 12\omega_{19}^2c_s^2v_3^2\omega_7^2 - 8\omega_{19}^2c_s^2\omega_7^2 - 3\omega_{19}^2v_3^2\omega_7^3 + \\ & 12\omega_{19}^2c_s^2\omega_7 - 36\omega_{19}^2c_s^2v_3^2\omega_7 - 24\omega_{19}c_s^4\omega_7^2 + 12\omega_{19}^2v_3^2\omega_7^2 + 6\omega_{19}c_s^4\omega_7^3 + 36v_3^4\omega_7^3 - 24\omega_{19}^2c_s^2\omega_7 - 72\omega_{19}c_s^2v_3^2\omega_7^3 + 30\omega_{19}v_3^2\omega_7^3 + 24\omega_{19}^2c_s^4\omega_7^2 - 72\omega_{19}v_3^2\omega_7^2 + \\ & 144\omega_{19}c_s^2v_3^2\omega_7^2 - 72v_3^2\omega_7^2 - 3\omega_{19}^2c_s^4\omega_7^2 - 12\omega_{19}^2v_3^2\omega_7^2 + 72\omega_{19}c_s^2v_3^2\omega_7 + 108c_s^2v_3^2\omega_7^3 - 6\omega_{19}c_s^2\omega_7^3 + 3\omega_{19}^2v_3^2\omega_7^3 - 48\omega_{19}^2c_s^4\omega_7 + 24\omega_{19}c_s^2\omega_7^2 - 216c_s^2v_3^2\omega_7^2 \end{aligned}$$

2.4.5 Conservation of momentum: ρv_3



attached text file: output_d3q27_nse_clbm1_symbolic_pde_03.txt

$$\begin{aligned} & v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_3 v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \\ & \frac{2v_3 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{c_s^2 \delta_l^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_7} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\ & + (-2 + 4c_s^2 + 6v_3^2 - 3v_3^2\omega_{11} + \omega_{11} - 2c_s^2\omega_{11}) \frac{\delta_l^2}{\delta_t \omega_{11}} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3v_3 \rho \delta_l^2}{\delta_t \omega_{11}} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \\ & (-2 + \omega_7) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_7} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{c_s^2 \rho \delta_l^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_7} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\ & (-2 + 6c_s^2 + 2v_3^2 - v_3^2\omega_{11} + \omega_{11} - 3c_s^2\omega_{11}) \frac{v_3 \delta_l^2}{2\delta_t \omega_{11}} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + 2c_s^2 + 6v_3^2 - 3v_3^2\omega_{11} + \omega_{11} - c_s^2\omega_{11}) \frac{\rho \delta_l^2}{2\delta_t \omega_{11}} \frac{\partial^2 v_3}{\partial x_3^2} + \\ & (-1 + 3c_s^2 + v_1^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{\rho v_1 \delta_l^3}{6\omega_6 \delta_t \omega_{13}} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\ & (-1 + 3c_s^2 + v_2^2) \frac{v_3 v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_2 \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_{16} \omega_7} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4 \delta_l^3}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\ & \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 - \omega_7^2 + 12\omega_7) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_7^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_3 \frac{v_3 \rho \delta_l^3}{12\omega_6 \delta_t \omega_{11}^2 \omega_{18}} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\ & C_4 \frac{v_3 \rho \delta_l^3}{12\omega_{19} \delta_t \omega_7 \omega_{11}^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_5 \frac{\delta_l^3}{12\delta_t \omega_{11}^2} \frac{\partial^3 \rho}{\partial x_3^3} + \\ & (-24 + 36c_s^2 + 60v_3^2 - 60v_3^2\omega_{11} + 24\omega_{11} + 5c_s^2\omega_{11}^2 - 4\omega_{11}^2 - 36c_s^2\omega_{11} + 11v_3^2\omega_{11}^2) \frac{v_3 \rho \delta_l^3}{6\delta_t \omega_{11}^2} \frac{\partial^3 v_3}{\partial x_3^3} + \\ & (3\omega_9 v_1^2 - 2c_s^2 - \omega_9 c_s^4 + 6v_1^4 - 12\omega_9 c_s^2 v_1^2 - 3\omega_9 v_1^4 + 2c_s^4 + 24c_s^2 v_1^2 + \omega_9 c_s^2 - 6v_1^2) \frac{v_3 \delta_l^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 + 2\omega_9 - 5\omega_9 v_1^2 + 6c_s^2 - 3\omega_9 c_s^2 + 10v_1^2) \frac{v_3 \rho v_1 \delta_l^4}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_l^4}{24\omega_6^3 \delta_t \omega_{13}^2} \frac{\partial^4 v_3}{\partial x_1^4} + \\ & (3\omega_9 - 3\omega_9 v_1^2 - \omega_{12} + \omega_9 \omega_{12} v_1^2 - \omega_9 \omega_{12} + \omega_{12} v_1^2 + 3\omega_{12} c_s^2 + 3\omega_9 \omega_{12} c_s^2 - 9\omega_9 c_s^2) \frac{v_3 \rho v_1 \delta_l^4}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + \\ & (-2 + \omega_5) \frac{c_s^4 v_3 \delta_l^4}{6\delta_t \omega_5} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_7 \frac{c_s^4 \rho \delta_l^4}{2\omega_6^2 \delta_t \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \end{aligned}$$

$$\begin{aligned}
& (3c_s^2\omega_{15} - 3\omega_{10}v_2^2 + 3c_s^2\omega_{10}\omega_{15} + 3\omega_{10} - 9c_s^2\omega_{10} + v_2^2\omega_{15} - \omega_{10}\omega_{15} + \omega_{10}v_2^2\omega_{15} - \omega_{15}) \frac{v_3\rho v_2\delta_l^4}{12\delta_t\omega_{10}\omega_{15}} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2} + \\
& (6v_2^4 - 2c_s^2 + 3\omega_{10}v_2^2 + c_s^2\omega_{10} - 3\omega_{10}v_2^4 + 24c_s^2v_2^2 - c_s^4\omega_{10} - 6v_2^2 + 2c_s^4 - 12c_s^2\omega_{10}v_2^2) \frac{v_3\delta_l^4}{24\delta_t\omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 - 5\omega_{10}v_2^2 + 2\omega_{10} - 3c_s^2\omega_{10} + 10v_2^2) \frac{v_3\rho v_2\delta_l^4}{12\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_2^2} + C_8 \frac{\rho\delta_l^4}{24\delta_t\omega_{16}^2\omega_7^3} \frac{\partial^4 v_3}{\partial x_2^4} + C_9 \frac{c_s^2v_1\delta_l^4}{12\omega_9\omega_6^2\omega_{22}\delta_t\omega_{13}^2\omega_{11}\omega_{18}} \frac{\partial^4 \rho}{\partial x_1^3\partial x_3} + \\
& C_{10} \frac{c_s^2\rho\delta_l^4}{12\omega_9\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}\omega_{18}} \frac{\partial^4 v_1}{\partial x_1^3\partial x_3} + \\
& (3\omega_9 - 3\omega_9v_1^2 - \omega_{13} + 3c_s^2\omega_{13} + \omega_9\omega_{13}v_1^2 + 3\omega_9c_s^2\omega_{13} + \omega_{13}v_1^2 - \omega_9\omega_{13} - 9\omega_9c_s^2) \frac{v_3\rho v_1\delta_l^4}{12\omega_9\delta_t\omega_{13}} \frac{\partial^4 v_3}{\partial x_1^3\partial x_3} + \\
& C_{11} \frac{\delta_l^4}{2\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}\omega_{11}\omega_{14}\omega_8\omega_{18}} \frac{\partial^4 \rho}{\partial x_1^2\partial x_2\partial x_3} + C_{12} \frac{\rho\delta_l^4}{2\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}\omega_{11}\omega_{14}\omega_8\omega_{18}} \frac{\partial^4 v_1}{\partial x_1^2\partial x_2\partial x_3} + \\
& C_{13} \frac{\rho\delta_l^4}{12\omega_6^3\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7^2\omega_{20}\omega_{11}\omega_{14}\omega_8\omega_{18}} \frac{\partial^4 v_2}{\partial x_1^2\partial x_2\partial x_3} + C_{14} \frac{v_3\rho\delta_l^4}{\omega_6\omega_{22}\omega_{19}\delta_t\omega_{13}\omega_7\omega_{20}\omega_{11}\omega_{14}\omega_8\omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2\partial x_2\partial x_3} + \\
& C_{15} \frac{\delta_l^4}{2\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8\omega_{18}} \frac{\partial^4 \rho}{\partial x_1\partial x_2^2\partial x_3} + C_{16} \frac{\rho\delta_l^4}{12\omega_6^2\omega_{19}\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8\omega_{18}} \frac{\partial^4 v_1}{\partial x_1\partial x_2^2\partial x_3} + \\
& C_{17} \frac{\rho v_2\delta_l^4}{\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8\omega_{18}} \frac{\partial^4 v_2}{\partial x_1\partial x_2^2\partial x_3} + C_{18} \frac{\rho\delta_l^4}{2\omega_6\omega_{19}\delta_t\omega_{16}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8\omega_{18}} \frac{\partial^4 v_3}{\partial x_1\partial x_2^2\partial x_3} + \\
& C_{19} \frac{c_s^2v_2\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11}} \frac{\partial^4 \rho}{\partial x_3^3\partial x_3} + C_{20} \frac{c_s^2\rho\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11}} \frac{\partial^4 v_2}{\partial x_3^3\partial x_3} + \\
& (-3\omega_{10}v_2^2 + \omega_{16}\omega_{10}v_2^2 + \omega_{16}v_2^2 - \omega_{16} + 3\omega_{10} + 3c_s^2\omega_{16} - 9c_s^2\omega_{10} + 3c_s^2\omega_{16}\omega_{10} - \omega_{16}\omega_{10}) \frac{v_3\rho v_2\delta_l^4}{12\delta_t\omega_{16}\omega_{10}} \frac{\partial^4 v_3}{\partial x_2^3\partial x_3} + \\
& C_{21} \frac{c_s^2v_3\delta_l^4}{12\omega_6^2\omega_{22}\delta_t\omega_{13}\omega_{11}^2\omega_{18}} \frac{\partial^4 \rho}{\partial x_1^2\partial x_3^2} + C_{22} \frac{c_s^2\rho\delta_l^4}{12\omega_6^3\omega_{22}\delta_t\omega_{13}\omega_{11}^2\omega_{18}} \frac{\partial^4 v_3}{\partial x_1^2\partial x_3^2} + C_{23} \frac{c_s^2v_3\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_7^2\omega_{23}\omega_{11}^3} \frac{\partial^4 \rho}{\partial x_2^3\partial x_3^2} + \\
& C_{24} \frac{c_s^2\rho\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_7^3\omega_{23}\omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2^3\partial x_3^2} + C_{25} \frac{\rho\delta_l^4}{12\omega_6^3\delta_t\omega_{11}^2\omega_{18}} \frac{\partial^4 v_1}{\partial x_1\partial x_3^3} + C_{26} \frac{\rho\delta_l^4}{12\omega_{19}\delta_t\omega_{16}\omega_{11}^3} \frac{\partial^4 v_2}{\partial x_2\partial x_3^3} + C_{27} \frac{v_3\delta_l^4}{12\delta_t\omega_{11}^3} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho\delta_l^4}{12\delta_t\omega_{11}^3} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 18c_s^2 - 3\omega_6 + 3\omega_6v_1^2 - 3\omega_{13} + 9c_s^2\omega_{13} + 3\omega_{13}v_1^2 + 9\omega_6c_s^2 - \omega_6\omega_{13}v_1^2 - 3\omega_6c_s^2\omega_{13} + \omega_6\omega_{13} - 6v_1^2 \\
C_2 &= 6 - 18c_s^2 - 3c_s^2\omega_{16}\omega_7 + 9c_s^2\omega_7 + 3\omega_{16}v_2^2 - 3\omega_{16} - 3\omega_7 + 9c_s^2\omega_{16} - \omega_{16}\omega_7v_2^2 + 3\omega_7v_2^2 + \omega_{16}\omega_7 - 6v_2^2 \\
C_3 &= -12\omega_6\omega_{11}^2 + 6v_3^2\omega_{11}\omega_{18} + 36\omega_6c_s^2\omega_{11}^2 + 6\omega_6\omega_{11}\omega_{18} - 18\omega_6c_s^2\omega_{11}\omega_{18} - 12\omega_6v_3^2\omega_{11} - 3\omega_6v_3^2\omega_{11}\omega_{18} - 6\omega_{11}^2\omega_{18} + 12\omega_6v_3^2\omega_{11}^2 + 12\omega_6\omega_{11} - \\
& 36\omega_6c_s^2\omega_{11} + 36\omega_6c_s^2\omega_{18} - 12\omega_6\omega_{18} - 36c_s^2\omega_{11}^2 + 18c_s^2\omega_{11}^2\omega_{18} + 12\omega_{11}^2 - 6\omega_6v_3^2\omega_{11}\omega_{18} + 12\omega_6v_3^2\omega_{18} + 3\omega_6\omega_{11}^2\omega_{18} - 12v_3^2\omega_{11}^2 - 11\omega_6c_s^2\omega_{11}^2\omega_{18} \\
C_4 &= -12\omega_{19}\omega_7 + 18\omega_{19}c_s^2\omega_{11}^2 + 6\omega_{19}\omega_7\omega_{11} - 18\omega_{19}c_s^2\omega_7\omega_{11} + 36c_s^2\omega_7\omega_{11}^2 - 36c_s^2\omega_7\omega_{11} + 6\omega_{19}v_3^2\omega_{11}^2 + 3\omega_{19}\omega_7\omega_{11}^2 - 11\omega_{19}c_s^2\omega_7\omega_{11}^2 + \\
& 36\omega_{19}c_s^2\omega_7 - 6\omega_{19}\omega_{11}^2 + 12v_3^2\omega_7\omega_{11}^2 - 36c_s^2\omega_{11}^2 + 12\omega_{11}^2 - 6\omega_{19}v_3^2\omega_7\omega_{11} + 12\omega_7\omega_{11} - 3\omega_{19}v_3^2\omega_7\omega_{11}^2 - 12\omega_7\omega_{11}^2 + 12\omega_{19}v_3^2\omega_7 - 12v_3^2\omega_7\omega_{11} - 12v_3^2\omega_{11}^2 \\
C_5 &= 24c_s^2v_3^2\omega_{11}^2 + c_s^4\omega_{11}^2 - 12c_s^2 - 36v_3^2 - 36v_3^4\omega_{11} + 144c_s^2v_3^2 + 7v_3^4\omega_{11}^2 - 144c_s^2v_3^2\omega_{11} - 12c_s^4\omega_{11} + 36v_3^2\omega_{11} - c_s^2\omega_{11}^2 + 12c_s^2\omega_{11} + 12c_s^4 + 36v_3^4 - 7v_3^2\omega_{11}^2 \\
C_6 &= -72\omega_6^2\omega_{13}\omega_{13}v_1^2 - 48\omega_6c_s^4\omega_{13}^2 + 36\omega_6^3v_1^4 + 6\omega_6^3c_s^4\omega_{13} - 36\omega_6c_s^2\omega_{13}^2v_1^2 + 108\omega_6^3c_s^2v_1^2 - 12\omega_6^2\omega_{13}^2v_1^4 - 72\omega_6^3c_s^2\omega_{13}v_1^2 + 24\omega_6^2c_s^2\omega_{13} - 8\omega_6^2c_s^2\omega_{13}^2 + 24\omega_6c_s^4\omega_{13} + \\
& 144\omega_6^2c_s^2\omega_{13}v_1^2 - 3\omega_6^3c_s^4\omega_{13}^2 - 3\omega_6^3\omega_{13}^2v_1^2 - 30\omega_6^3\omega_{13}v_1^4 - 72\omega_6^2v_1^4 + 12\omega_6c_s^2\omega_{13}^2 - 6\omega_6^3c_s^2\omega_{13} + 24c_s^4\omega_{13}^2 + 3\omega_6^2\omega_{13}^2v_1^4 - 216\omega_6^2c_s^2v_1^2 - 24\omega_6^2c_s^4\omega_{13} + \\
& 72\omega_6^2v_1^2 - 12\omega_6^2c_s^2\omega_{13}^2v_1^2 + 30\omega_6^3\omega_{13}v_1^2 + 72\omega_6c_s^2\omega_{13}v_1^2 + 6\omega_6^3c_s^2\omega_{13}^2v_1^2 + 72\omega_6^2\omega_{13}v_1^4 + 12\omega_6^2\omega_{13}^2v_1^2 + 24\omega_6^2c_s^4\omega_{13}^2 - 24\omega_6c_s^2\omega_{13} + \omega_6^3c_s^2\omega_{13} - 36\omega_6^3v_1^2 \\
C_7 &= -\omega_6^2\omega_{16}\omega_{13}\omega_7^2\omega_{17}\omega_8 - 2\omega_6\omega_{16}\omega_{13}\omega_7^2\omega_{17} - \omega_6^2\omega_{16}\omega_7\omega_{17}\omega_{14}\omega_8 - 2\omega_6^2\omega_{16}\omega_{13}\omega_7^2\omega_{17}\omega_{14} - \omega_6\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8 + 2\omega_6^2\omega_{16}\omega_{13}\omega_7\omega_{14}\omega_8 + \\
& 2\omega_6^2\omega_{16}\omega_{13}\omega_7^2\omega_{17} + \omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8 + 2\omega_6\omega_{16}\omega_7\omega_{17}\omega_{14}\omega_8 + 2\omega_6\omega_{16}\omega_{13}\omega_7^2\omega_{17}\omega_{14} + \omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8 - \omega_{16}\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8 + \\
& 2\omega_6^2\omega_{16}\omega_{13}\omega_7^2\omega_{14} - 6\omega_6\omega_{16}\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8 - 2\omega_6\omega_{16}\omega_{13}\omega_7^2\omega_{14} + 2\omega_6\omega_{16}\omega_{13}\omega_7^2\omega_{17}\omega_8 - 2\omega_6\omega_{16}\omega_7^2\omega_{17}\omega_8 + \omega_6\omega_{16}\omega_{13}\omega_7^2\omega_{14}\omega_8 - \\
& 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8 + \omega_6^2\omega_{16}\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8 - \omega_6^2\omega_{16}\omega_{13}\omega_{17}\omega_{14}\omega_8 - 2\omega_6^2\omega_{16}\omega_{13}\omega_7\omega_{14} + 2\omega_6\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8 + \omega_6\omega_{16}\omega_{13}\omega_7^2\omega_{17}\omega_{14}\omega_8 - \\
& 2\omega_6^2\omega_{16}\omega_{13}\omega_7\omega_{17} + 2\omega_{16}\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8 + \omega_6^2\omega_{16}\omega_{13}\omega_7\omega_{17}\omega_8 - \omega_6^2\omega_{16}\omega_{13}\omega_7^2\omega_{14}\omega_8 + 2\omega_6^2\omega_{16}\omega_{13}\omega_7\omega_{17}\omega_{14} + 2\omega_6\omega_{16}\omega_{13}\omega_{17}\omega_{14}\omega_8 \\
C_8 &= 3\omega_{16}^2\omega_7^3v_2^4 - 24c_s^4\omega_{16}\omega_7^2 - 36\omega_7^3v_2^2 + 30\omega_{16}\omega_7^3v_2^2 - 24c_s^2\omega_{16}\omega_7 + 6c_s^2\omega_{16}^2\omega_7^3v_2^2 + 6c_s^4\omega_{16}\omega_7^3 + 72\omega_7^2v_2^2 - 72\omega_{16}\omega_7^2v_2^2 + 72c_s^2\omega_{16}\omega_7v_2^2 + 24c_s^2\omega_{16}\omega_7^2 - \\
& 12\omega_{16}^2\omega_7^2v_2^2 - 12c_s^2\omega_{16}\omega_7^2v_2^2 + 24c_s^4\omega_{16}\omega_7 - 6c_s^2\omega_{16}\omega_7^2 - 48c_s^4\omega_{16}^2\omega_7 - 36c_s^2\omega_{16}\omega_7^2v_2^2 + 12\omega_{16}^2\omega_7^2v_2^2 - 72\omega_7^2v_2^4 + 72\omega_{16}\omega_7^2v_2^4 + c_s^2\omega_{16}\omega_7^3 + 144c_s^2\omega_{16}\omega_7^2v_2^2 - \\
& 216c_s^2\omega_7^2v_2^2 + 24c_s^4\omega_{16}^2 - 8c_s^2\omega_{16}\omega_7^2 + 12c_s^2\omega_{16}\omega_7 + 36\omega_7^3v_2^4 - 30\omega_{16}\omega_7^3v_2^2 - 3\omega_{16}^2\omega_7^3v_2^2 - 3c_s^4\omega_{16}\omega_7^3 + 108c_s^2\omega_7^3v_2^2 + 24c_s^4\omega_{16}\omega_7^2 - 72c_s^2\omega_{16}\omega_7^3v_2^2 \\
C_9 &= -3\omega_9\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} - 36\omega_9\omega_6\omega_{22}c_s^2\omega_{11}\omega_{18} - 18\omega_9\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18} + 36\omega_9\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} + 6\omega_6^2\omega_{22}\omega_{13}v_1^2\omega_{18} + \\
& 12\omega_9\omega_6^2\omega_{13}\omega_{11}\omega_{18} + 12\omega_9\omega_6\omega_{22}\omega_{11}\omega_{18} + 12\omega_9\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} + 12\omega_6^2\omega_{22}\omega_{13}^2 + 36\omega_9\omega_6^2c_s^2\omega_{13} - 12\omega_9\omega_{22}\omega_{13}\omega_{11}\omega_{18} + 18\omega_9\omega_6^2\omega_{22}c_s^2\omega_{11}\omega_{18} + \\
& 3\omega_9\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18} + 54\omega_9\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} - 12\omega_9\omega_6^2\omega_{13}\omega_{11}v_1^2 + 6\omega_9\omega_6^2\omega_{13}\omega_{18} + 6\omega_9\omega_6^2\omega_{13}\omega_{11}\omega_{18} - 36\omega_9\omega_6^2c_s^2\omega_{13}\omega_{11} - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11} - \\
& 12\omega_9\omega_6\omega_{22}\omega_{11}v_1^2\omega_{18} + 18\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18} - 12\omega_9\omega_6^2\omega_{13} - 12\omega_9\omega_6\omega_{13}\omega_{11}v_1^2\omega_{18} - 9\omega_9\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} - 18\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18} - \\
& 36\omega_9\omega_6c_s^2\omega_{13}\omega_{11}\omega_{18} + 18\omega_9\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} + 6\omega_9\omega_6^2\omega_{13}\omega_{11}v_1^2\omega_{18} + 18\omega_9\omega_6^2c_s^2\omega_{13}\omega_{11}\omega_{18} + 5\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18} - 12\omega_9\omega_6\omega_{13}\omega_{11} - \\
& 12\omega_6^2\omega_{22}\omega_{13}v_1^2 + 6\omega_9\omega_6^2\omega_{22}\omega_{11}v_1^2\omega_{18} - 12\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} - 6\omega_9\omega_6^2\omega_{22}\omega_{11}\omega_{18} - 12\omega_9\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} - 6\omega_9\omega_6^2\omega_{13}\omega_{11}\omega_{18} + 12\omega_9\omega_6^2\omega_{13}v_1^2 - \\
& 36\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} - 12\omega_6\omega_{22}\omega_{13}\omega_{11}v_1^2 + 3\omega_9\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} - 36\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11} + 36\omega_9\omega_6c_s^2\omega_{13}\omega_{11}\omega_{18} + \omega_9\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} - \\
& 5\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2\omega_{18} + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}v_1^2 - 18\omega_9\omega_6^2c_s^2\omega_{13}\omega_{11}\omega_{18} + 36\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11} - 15\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} - 18\omega_9\omega_6^2c_s^2\omega_{13}\omega_{18} -
\end{aligned}$$

$$\begin{aligned}
& 2w_{6w19c_s^2w16w7w23w17w11w8v1} + 2w_{6c_s^2w16w7w20w17w8v1w18} + 2w_{6w19c_s^2w16v3w7w23w17w8w18} + 2w_{6c_s^2w16v3w23w20w17w11w8w18} - \\
& 2w_{6w16v3w7w20w17w8v1w18} + 2w_{6w19w16v3w7w23w17w8v1} + 2w_{6w16v3w23w20w17w11w8v1w18} - w_{6w19c_s^2w16w7w23w20w17w8v1} + \\
& 2w_{6w19c_s^2w16v3w7w23w20w11w18} - 2w_{6w16v3w7w23w20w17w11w8v1w18} + 2w_{6w16v3w20w17w11w8v1w18} + w_{19c_s^2w16w7w23w20w17w11w8v1w18} - \\
& 2w_{6w19w16v3w7w23w17w8v1} - 2w_{6w19c_s^2w16v3w23w20w17w11w8v1} + 2w_{6w19c_s^2w16v3w7w23w20w17w11w8v1} + 2w_{6c_s^2w16w20w17w11w8v1w18} - \\
& 2w_{6w19w16v3w23w20w17w11w8v1w18} - w_{6w19w16v3w7w23w20w17w11w8v1w18} + 2w_{6c_s^2w16w20w17w11w8v1w18} \\
C_{18} = & 2w_{6w19c_s^2w16v3w7w23w20w17w11w8v1} + 4w_{6w19v3w20w17w11v2w8v1w18} + w_{19w16w7w23w20w17w11v2w8v1} - \\
& w_{6w19w16w7w23w20w17v2w8v1w18} + 2w_{6w19c_s^2w16w7w23w17v2w8w18} - 2w_{6w19w16v3w7w23w20w17v2w8v1} - \\
& 2w_{19w16v3w7w23w20w17w11v2w8v1} + 2w_{19w16w7w23w20w17w11v2v1w18} + w_{6w19c_s^2w7w20w17w11v2w8w18} + 4w_{6w19v3w23w20w11v2w8v1w18} - \\
& 4w_{6w19w16v3w23w17w11v2w8v1w18} - w_{6w19c_s^2w16w7w23w20w17v2w8w18} - w_{19c_s^2w16w7w23w20w17w11w8v1w18} + \\
& 2w_{19w16w7w23w17w11v2w8v1w18} + w_{6w19c_s^2w7w23w20w11v2w8w18} - 4w_{6w19w16v3w7w23w17w11v2w8v1w18} + 2w_{6w19c_s^2w16v3w20w17w11v2w8v1} + \\
& 2w_{6w19c_s^2w16w23w20w17w11v2w8w18} - 4w_{6w19c_s^2w16w7w23w20w17w11w8v1w18} - 2w_{6w19w16v3w7w23w20w17w11v2w8v1w18} + \\
& 2w_{6c_s^2w16w7w23w20w17v2w8w18} + 4w_{6w16v3w23w17w11v2w8v1w18} - 4w_{6w19c_s^2w16v3w23w20w11w8v1w18} - 2w_{6c_s^2w16w20w17w11w8v1w18} - \\
& w_{6w19c_s^2w7w23w20w17w11v2w8w18} - 2w_{6w19c_s^2w16w7w23w17w8v1} - 4w_{6w19c_s^2w16v3w20w17w11w8v1w18} + 2w_{6w19w16w7w23w17w11v2w8v1} - \\
& 2w_{6c_s^2w16w23w17w11v2w8w18} + 2w_{6w19c_s^2w3w7w23w20w17w11w8v1w18} - 4w_{19c_s^2w16v3w7w23w20w17w11v2w8v1w18} - \\
& 2w_{6w19w16v3w7w23w20w17w11v2w8v1w18} - 4w_{6w19w16v3w7w23w20w11v2v1w18} - 2w_{19c_s^2w16w7w23w20w17w11v2w8v1} - \\
& 2w_{6w19c_s^2w16w23w20w11v1w18} - 4w_{19c_s^2w16v3w7w23w20w17w11v1w18} + 2w_{6w16w23w20w17w11v2w8v1w18} + 2w_{6w19w16v3w7w23w20w17w11v2w8v1} - \\
& 2w_{6w19c_s^2w16v3w7w23w20w17w11v2w8v1w18} - 2w_{6w19c_s^2w16w7w20w17w8v1w18} - 2w_{6c_s^2w16w7w20w17w8v1w18} + 4w_{6w16v3w7w23w17v2w8v1w18} - \\
& 2w_{6w19c_s^2w16v3w7w23w17w8v1w18} + 2w_{6w19c_s^2w16w7w23w20w17w11v2w8v1w18} + w_{6w19w16w7w23w20w17w11v2w8v1w18} - \\
& 2w_{6w19c_s^2w16v3w7w23w17w8v1w18} - 2w_{6w19c_s^2w16w23w20w11v2w8w18} - 2w_{6w19c_s^2w16w7w23w20w11v2w8w18} - \\
& w_{6w19c_s^2w16w7w23w20w17w11v2w8w18} + 2w_{6w19c_s^2w16w23w17w11w8v1w18} + 2w_{6c_s^2w16w23w20w17w11w8v1w18} - 2w_{6w19w16w23w20w11v2v1w18} - \\
& 4w_{6w19c_s^2w16v3w7w23w17w8v1w18} - 4w_{6c_s^2w16v3w23w20w17w11w8v1w18} + 2w_{6w19c_s^2w16v3w7w23w20w11w8v1w18} + \\
& 2w_{6w19w16w20w17w11v2w8v1w18} - 2w_{6w19c_s^2w16w7w23w20w17w11w8v1w18} - 2w_{6c_s^2w16w7w23w20w17v2w8w18} + w_{6w19c_s^2w16w7w23w20w17v2w8w18} + \\
& 4w_{6w19w16v3w7w23w20w11v2w8v1w18} - w_{6w19c_s^2w16w7w23w20w11w8v1w18} - w_{6w19w16v3w7w23w20w17w11v2w8v1w18} + w_{6w19c_s^2w16w7w23w20w17v2w8w18} + \\
& w_{6c_s^2w16w7w23w20w17w11v2w8v1w18} + w_{6w19w16w7w23w20w17v2w8v1w18} + 2w_{6c_s^2w16w7w23w20w17w11v2w8v1w18} + 2w_{6w19w16v3w7w23w20w17w11v2w8v1w18} - \\
& 2w_{19w16w7w23w17w11v2w8v1} + 4w_{6w19c_s^2w16v3w23w20w17w11w8v1w18} + 2w_{6c_s^2w16w7w23w17w11v2w8w18} + w_{19c_s^2w16w7w23w20w17w11w8v1w18} + \\
& w_{6w19c_s^2w16w7w23w20w17v2w8v1w18} - 2w_{19w16w7w23w20w17w11v2v1w18} + 2w_{19c_s^2w16w7w23w20w17w11v1w18} + w_{6w19c_s^2w16w7w23w20w17w11v2w8w18} - \\
& 2w_{6w19c_s^2w16w23w20w11v2w8w18} + 2w_{6w19w16v3w7w23w20w11v2w8v1w18} - 2w_{19w16w7w23w20w17w11v2w8v1w18} - \\
& 2w_{6w19c_s^2w16w23w20w17w11v2w8w18} + w_{19c_s^2w16w7w23w20w17w11v2w8v1w18} - 4w_{19w16v3w7w23w20w17w11v2w8v1w18} - \\
& 4w_{19w16v3w7w23w20w17w11v2v1w18} - 2w_{6w16w7w23w20w17w11v2w8v1w18} - 4w_{6w19w23w20w17w11v2w8v1w18} + \\
& 2w_{6w19c_s^2w16w7w23w20w17w11v2w8v1w18} - w_{6w19c_s^2w16w7w23w20w17w11w8v1w18} + 4w_{6w16v3w20w17w11v2w8v1w18} - 2w_{19w16w7w23w20w11v2v1w18} - \\
& 2w_{19c_s^2w16w7w23w20w11v2w8w18} + w_{6w19c_s^2w16w7w23w20w17w11w8v1w18} + 2w_{6w19w23w20w17w11v2w8v1w18} + 4w_{6w19w23w20w17w11v2w8v1w18} + \\
& 4w_{6w19c_s^2w16v3w7w20w17w11v2w8v1w18} + 2w_{6w19w23w20w17w11v2w8v1w18} - 2w_{6w19w16v3w7w20w17w11v2w8v1w18} + 4w_{6w19c_s^2w16w7w23w20w17w11v2w8v1w18} - \\
& 4w_{6c_s^2w16v3w7w23w20w17w11v2w8v1w18} - 2w_{6w19c_s^2w16w7w23w20w17w11v2w8v1w18} + 2w_{6c_s^2w16w7w23w20w17w11w8v1w1$$

$$\begin{aligned}
& 2\omega_6\omega_{19}c_s^2\omega_{16}\omega_7\omega_{23}\omega_{17}\omega_{11}v_2^2\omega_{18} - \omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_{11}v_2^2\omega_8v_1^2\omega_{18} + 2\omega_6\omega_{19}\omega_{16}\omega_{23}\omega_{20}\omega_{17}\omega_{11}v_2^2v_1^2\omega_{18} - \\
& 4\omega_6\omega_{16}v_3\omega_{23}\omega_{20}\omega_{17}\omega_{11}v_2^2\omega_8v_1\omega_{18} - 2\omega_{19}c_s^2\omega_{16}\omega_7\omega_{23}\omega_{20}\omega_{11}v_2^2\omega_{18} - 4\omega_6\omega_{19}\omega_{16}v_3\omega_7\omega_{23}\omega_{17}\omega_{11}v_2^2v_1\omega_{18} - 2\omega_6\omega_{19}c_s^2\omega_{16}\omega_7\omega_{23}\omega_{17}v_2^2\omega_8 + \\
& 2\omega_6\omega_{19}c_s^2\omega_{23}\omega_{20}\omega_{17}\omega_{11}\omega_8v_1^2\omega_{18} - 2\omega_6\omega_{19}\omega_{16}v_3\omega_7\omega_{20}\omega_{17}v_2^2\omega_8v_1\omega_{18} + 4\omega_{19}c_s^2\omega_{16}v_3\omega_7\omega_{23}\omega_{17}\omega_{11}v_1\omega_{18} + \\
& 4\omega_6\omega_{16}v_3\omega_7\omega_{23}\omega_{20}\omega_{17}\omega_{11}v_2^2\omega_8v_1\omega_{18} + 4\omega_{19}\omega_{16}v_3\omega_7\omega_{23}\omega_{20}\omega_{11}v_2^2v_1\omega_{18} - 2\omega_{19}c_s^2\omega_{16}v_3\omega_7\omega_{23}\omega_{20}\omega_{11}\omega_8v_1\omega_{18}
\end{aligned}$$

$$\begin{aligned}
C_{20} = & 18\omega_{19}\omega_{16}\omega_{17}^3\omega_{23}v_2^2 + 18\omega_{19}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 - 5\omega_{19}c_s^2\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} + 18\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_{23}\omega_{11} + 12\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} + 6\omega_{19}\omega_{10}\omega_{17}^3\omega_{11} - \\
& 12\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} + 5\omega_{19}\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - 6\omega_{19}c_s^2\omega_{10}\omega_{17}^3\omega_{11} - 18\omega_{19}c_s^2\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} - 18\omega_{19}\omega_{10}\omega_{17}^3\omega_{11}v_2^2 - \\
& 36\omega_{16}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 - 12c_s^2\omega_{16}\omega_{17}^3\omega_{23} + 18\omega_{19}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} + 36\omega_{16}\omega_{10}\omega_{17}^3\omega_{11}v_2^2 - 15\omega_{19}\omega_{16}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 - 36\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3\omega_{11}v_2^2 + \\
& 12c_s^2\omega_{16}\omega_{10}\omega_{17}^3 + 12\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} + 12\omega_{19}c_s^2\omega_{10}\omega_{17}^3\omega_{11} + 36\omega_{16}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 - 12\omega_{19}\omega_{10}\omega_{17}^3\omega_{11} + 54\omega_{19}\omega_{16}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 + 36\omega_{16}\omega_{10}\omega_{17}^3v_2^2 + \\
& 12\omega_{19}\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - 54\omega_{19}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 + 12c_s^2\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_{17}\omega_{23}\omega_{11} - \omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} - 6\omega_{19}\omega_{16}\omega_{17}^3\omega_{23} - \\
& 6\omega_{19}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} + 6\omega_{19}c_s^2\omega_{16}\omega_{17}^3\omega_{23} - 36\omega_{16}\omega_{10}\omega_{17}^3\omega_{11}v_2^2 + 36\omega_{19}\omega_{10}\omega_{17}^3\omega_{11}v_2^2 - 12c_s^2\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} + 6\omega_{19}c_s^2\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} + \\
& 12\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} - 12\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - 12\omega_{16}\omega_{10}\omega_{17}^3 - 18\omega_{19}\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} + 18\omega_{19}c_s^2\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - \\
& 36\omega_{16}\omega_{17}^3\omega_{23}v_2^2 - 5\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} - 12c_s^2\omega_{16}\omega_{17}^3\omega_{23}\omega_{11} - 36\omega_{19}\omega_{16}\omega_{17}\omega_{23}\omega_{11}v_2^2 - 3\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11}v_2^2 + 12c_s^2\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} + \\
& 12\omega_{16}\omega_{17}^3\omega_{23} + \omega_{19}\omega_{16}\omega_{10}\omega_{17}^3\omega_{23}\omega_{11} - 18\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3v_2^2 + 12\omega_{19}c_s^2\omega_{10}\omega_{17}\omega_{23}\omega_{11} + 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} + 36\omega_{19}\omega_{10}\omega_{17}\omega_{23}\omega_{11}v_2^2 + \\
& 18\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3\omega_{11}v_2^2 + 6\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3 - 12\omega_{19}\omega_{10}\omega_{17}\omega_{23}\omega_{11} - 6\omega_{19}\omega_{16}\omega_{10}\omega_{17}^3\omega_{11} - 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{17}^3
\end{aligned}$$

$$\begin{aligned}
C_{22} = & -6\omega_3^3\omega_{13}\omega_{11}^2\omega_{18} + 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18} + 12\omega_6^3c_s^2\omega_{13}\omega_{11} + 6\omega_3^3c_s^2\omega_{13}\omega_{11}^2\omega_{18} - 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18} - 36\omega_6^2\omega_{22}v_3^2\omega_{11}\omega_{18} - \\
& 6\omega_3^3c_s^2\omega_{11}^2\omega_{18} - 36\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{18} + 12\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18} + 72\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18} - 6\omega_6^3\omega_{22}\omega_{11}\omega_{18} - 24\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18} - \\
& 6\omega_6^2\omega_{22}\omega_{13}\omega_{18} - 36\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11} - 12\omega_6^2\omega_{11}^2\omega_{18} + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11} - 12\omega_6^2\omega_{13}\omega_{11}^2 - 36\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18} + 18\omega_3^3\omega_{13}\omega_{11}^2\omega_{18} + \\
& 36\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}^2 + 12\omega_6^2\omega_{22}\omega_{11}\omega_{18} - 12\omega_6\omega_{22}v_3^2\omega_{11}^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11} - 24\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} + 12\omega_6^2c_s^2\omega_{11}^2\omega_{18} + 6\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18} + \\
& 12\omega_6^2\omega_{13}\omega_{11}^2\omega_{18} - 12\omega_6^3c_s^2\omega_{11}\omega_{18} + 6\omega_6^3\omega_{22}c_s^2\omega_{11}\omega_{18} + 6\omega_3^3\omega_{22}\omega_{13}\omega_{11}\omega_{18} - 12\omega_6^3\omega_{13}\omega_{11} - 4\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18} + 6\omega_3^3\omega_{11}^2\omega_{18} - \\
& 72\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}^2 + 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18} - 18\omega_6^3\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18} - 12\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11} - 36\omega_6^2v_3^2\omega_{13}\omega_{11}^2\omega_{18} - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11} - \\
& 18\omega_6^2v_3^2\omega_{13}\omega_{11}\omega_{18} + 36\omega_6^2v_3^2\omega_{13}\omega_{11} + 36\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}^2 - 12\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18} - 24\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18} - 12\omega_6^2\omega_{22}c_s^2\omega_{11}\omega_{18} - 18\omega_3^3v_3^2\omega_{11}^2\omega_{18} - \\
& 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18} + 36\omega_6^2v_3^2\omega_{13}\omega_{11}^2 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2 + 36\omega_6^2v_3^2\omega_{11}^2\omega_{18} + 12\omega_6^3\omega_{22}\omega_{13}\omega_{11} + 18\omega_3^3\omega_{22}v_3^2\omega_{13}\omega_{18} - 36\omega_6^2v_3^2\omega_{13}\omega_{11}^2 + \\
& 24\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2 + 18\omega_3^3\omega_{22}v_3^2\omega_{11}\omega_{18} - 6\omega_3^3\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18} - 12\omega_6^3\omega_{22}\omega_{13}\omega_{11}^2\omega_{18} + 18\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18} + 36\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11} - \\
& 6\omega_3^3c_s^2\omega_{13}\omega_{11}\omega_{18} + 6\omega_6^3\omega_{13}\omega_{11}\omega_{18} + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}^2 + 12\omega_3^3\omega_{13}\omega_{11}^2
\end{aligned}$$

$$\omega_{19}\omega_{16}v_3^2\omega_{23}\omega_{11}^3 - 36\omega_{19}c_s^2\omega_{16}\omega_{23}\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 + 2\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11}^3 + 12\omega_{19}\omega_{16}\omega_{23}\omega_{11}^3 + 12\omega_{16}v_3^2\omega_7^2\omega_{23}\omega_{11}^3 - 36\omega_{19}c_s^2\omega_{16}\omega_{23}\omega_{11}^3 - 6\omega_{19}\omega_{16}v_3^2\omega_7^2\omega_{11}^2$$

$$\begin{aligned} C_{24} = & 12c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 18\omega_{19}c_s^2\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 12\omega_{16}\omega_7^3\omega_{11} - 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} - 36\omega_{19}v_3^2\omega_7^2\omega_{23}\omega_{11} - 12\omega_{16}\omega_7^2\omega_{23}\omega_{11} - \\ & 36\omega_{16}v_3^2\omega_7^2\omega_{23}\omega_{11} - 36\omega_{19}\omega_{16}v_3^2\omega_7\omega_{23}\omega_{11} + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23}\omega_{11} + 36\omega_{16}v_3^2\omega_7\omega_{23}\omega_{11}^2 + 36\omega_{19}v_3^2\omega_7^2\omega_{11}^2 + 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{11}^2 - 6\omega_{19}\omega_{16}\omega_7^3\omega_{11}^2 - \\ & 12\omega_{16}\omega_7^3\omega_{11}^2 - 36\omega_{16}v_3^2\omega_7^3\omega_{11}^2 + 18\omega_{19}\omega_{16}v_3^2\omega_7^3\omega_{23} + 12\omega_{19}\omega_7^2\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{11} + 6\omega_{19}\omega_{16}\omega_7^2\omega_{11} + \\ & 36\omega_{16}v_3^2\omega_7^3\omega_{11} + 12\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11} + 36\omega_{16}v_3^2\omega_7^2\omega_{23}\omega_{11}^2 + 24\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 36\omega_{19}\omega_{16}v_3^2\omega_7^2\omega_{23} - 18\omega_{19}\omega_{16}v_3^2\omega_7^3\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 - \\ & 12c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_7\omega_{23}\omega_{11} + 36\omega_{16}v_3^2\omega_7^2\omega_{11}^2 + 12\omega_{16}\omega_7^3\omega_{11}^2 - 12\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} - \omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23}\omega_{11}^2 - \\ & 18\omega_{19}v_3^2\omega_7^3\omega_{11}^2 + 12\omega_{19}c_s^2\omega_7^2\omega_{11}^2 - 12\omega_{19}\omega_7^2\omega_{11}^2 - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23} + 18\omega_{19}\omega_{16}v_3^2\omega_7^3\omega_{11}^2 - 12c_s^2\omega_{16}\omega_7^3\omega_{11}^2 + 36\omega_{16}v_3^2\omega_7^2\omega_{23}\omega_{11} + \\ & 12\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 24\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 12\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 24c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 18\omega_{19}v_3^2\omega_7^2\omega_{23}\omega_{11} + 24\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} + 12c_s^2\omega_{16}\omega_7^2\omega_{11}^2 + \\ & 12c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 36\omega_{19}\omega_{16}v_3^2\omega_7^2\omega_{11}^2 - 4\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 12\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 12\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{23}\omega_{11}^2 - 72\omega_{16}v_3^2\omega_7^2\omega_{23}\omega_{11}^2 - \\ & 6\omega_{19}c_s^2\omega_7^2\omega_{11}^2 + 72\omega_{19}\omega_{16}v_3^2\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_7^2\omega_{23} + 6\omega_{19}\omega_7^3\omega_{11}^2 - 18\omega_{19}\omega_{16}v_3^2\omega_7^3\omega_{11} + 12c_s^2\omega_{16}\omega_7^3\omega_{11} - 6\omega_{19}\omega_7^3\omega_{23}\omega_{11} + 6\omega_{19}c_s^2\omega_7^3\omega_{23}\omega_{11} \end{aligned}$$

$$\begin{aligned} C_{25} = & 18\omega_6^2c_s^2v_3^2\omega_{11}^2\omega_{18}^2 - 36\omega_6^3v_3^2\omega_{11}^3 - 36\omega_6^3v_3^4\omega_{11}\omega_{18} + 13\omega_6^2c_s^4\omega_{11}^3\omega_{18}^2 + 6\omega_6^3c_s^2\omega_{11}^2\omega_{18} - 6\omega_6^2c_s^2\omega_{11}^2\omega_{18}^2 + 6\omega_6^3c_s^4\omega_{11}^3\omega_{18} + 36\omega_6c_s^2v_3^2\omega_{11}^3\omega_{18} - \\ & 36\omega_6^2v_3^4\omega_{11}^2 + 12\omega_6^3c_s^4\omega_{18}^2 + 36\omega_6^3v_3^2\omega_{11}^2 + 12\omega_6^2c_s^4\omega_{11}^2\omega_{18} + 54\omega_6^2c_s^2v_3^2\omega_{11}^3\omega_{18} + \omega_6^3c_s^4\omega_{11}^2\omega_{18} + 18\omega_6^2c_s^2\omega_{11}^3\omega_{18} + 90\omega_6^3v_3^2\omega_{11}\omega_{18}^2 - 306\omega_6^3c_s^2v_3^2\omega_{11}\omega_{18}^2 + \\ & 36\omega_6^3v_3^2\omega_{11}\omega_{18} - 5\omega_6^2c_s^2\omega_{11}^3\omega_{18} - 6\omega_6^3c_s^4\omega_{11}^2\omega_{18} - 108\omega_6^3c_s^2v_3^2\omega_{11}\omega_{18} + 252\omega_6^3c_s^2v_3^2\omega_{18}^2 + 6\omega_6^2c_s^4\omega_{11}^2\omega_{18} - 6\omega_6^3c_s^2\omega_{11}^3\omega_{18} - 3\omega_6^2c_s^2v_3^2\omega_{11}^3\omega_{18} - \\ & \omega_6^3c_s^4\omega_{11}^3\omega_{18} - 12\omega_6^2c_s^2\omega_{11}^3\omega_{18} - 18\omega_6c_s^2v_3^2\omega_{11}^3\omega_{18} + 36\omega_6^2c_s^2v_3^2\omega_{11}^3\omega_{18} + 72\omega_6^3v_3^4\omega_{11}^2 - \omega_6^3c_s^2\omega_{11}^2\omega_{18} - 18\omega_6^2c_s^4\omega_{11}^3\omega_{18} - 90\omega_6^3v_3^4\omega_{11}\omega_{18} - 12\omega_6^3c_s^2\omega_{18}^2 + \\ & 12\omega_6^3c_s^2\omega_{11}^2\omega_{18} - 4\omega_6^3v_3^2\omega_{11}^3\omega_{18} - 36\omega_6^3v_3^4\omega_{11}^2 + 108\omega_6^3c_s^2v_3^2\omega_{11}^3\omega_{18} - 24\omega_6^3c_s^4\omega_{11}^3\omega_{18} + 19\omega_6^3v_3^4\omega_{11}^2\omega_{18} - 36\omega_6^2v_3^2\omega_{11}^3\omega_{18} + 12\omega_6^3c_s^2\omega_{11}\omega_{18}^2 - \\ & 12\omega_6c_s^2\omega_{11}^3\omega_{18} - 108\omega_6^3c_s^2v_3^2\omega_{11}^2 + 36\omega_6^3v_3^4\omega_{11}^3 + 198\omega_6^3c_s^2v_3^2\omega_{11}^3\omega_{18} - 6\omega_6^2v_3^4\omega_{11}^3\omega_{18} - 72\omega_6^3v_3^4\omega_{11}^3\omega_{18} - 39\omega_6^3v_3^4\omega_{11}^3\omega_{18} - 12\omega_6^3c_s^4\omega_{11}\omega_{18}^2 + \\ & 36\omega_6^3v_3^2\omega_{11}^2 + 4\omega_6^3v_3^4\omega_{11}^3\omega_{18} + 12c_s^4\omega_{11}^3\omega_{18}^2 - 72\omega_6^3v_3^2\omega_{18}^2 + 6\omega_6c_s^2\omega_{11}^3\omega_{18} + 60\omega_6^3c_s^2v_3^2\omega_{11}^3\omega_{18} - 19\omega_6^3v_3^2\omega_{11}^3\omega_{18} + 36\omega_6^3v_3^4\omega_{11}^3\omega_{18} - 12\omega_6^3c_s^4\omega_{11}\omega_{18}^2 + \\ & 12\omega_6c_s^4\omega_{11}^3\omega_{18} - 36\omega_6^2c_s^2v_3^2\omega_{11}\omega_{18}^2 - 108\omega_6^2c_s^2v_3^2\omega_{11}^2 + 6\omega_6^2v_3^2\omega_{11}^3\omega_{18} + 72\omega_6^3v_3^4\omega_{11}^3\omega_{18} - 99\omega_6^3c_s^2v_3^2\omega_{11}^3\omega_{18} + 39\omega_6^3v_3^4\omega_{11}^3\omega_{18} + 12\omega_6^2c_s^2\omega_{11}\omega_{18}^2 \end{aligned}$$

$$\begin{aligned} C_{26} = & -108\omega_{19}c_s^2v_3^2\omega_7^3\omega_{11} + 54\omega_{19}c_s^2v_3^2\omega_7^3\omega_{11}^3 + \omega_{19}c_s^4\omega_7^3\omega_{11}^2 - 36v_3^2\omega_7^3\omega_{11}^3 + 36\omega_{19}v_3^2\omega_7^3\omega_{11} - 36\omega_{19}v_3^2\omega_7^2\omega_{11}^3 + 12\omega_{19}c_s^4\omega_7\omega_{11}^3 - 12\omega_{19}c_s^2\omega_7^3 + \\ & 252\omega_{19}c_s^2v_3^2\omega_7^3 - 39\omega_{19}v_3^4\omega_7^3\omega_{11}^3 - 36v_3^4\omega_7^2\omega_{11}^3 - 6\omega_{19}c_s^2\omega_7^2\omega_{11}^2 + 18\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11}^2 + 36v_3^2\omega_7^2\omega_{11}^2 + 36\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11}^2 - \omega_{19}c_s^4\omega_7^3\omega_{11}^3 - 12\omega_{19}c_s^4\omega_7^2\omega_{11} + \\ & 12\omega_{19}c_s^2\omega_7^3\omega_{11} - 306\omega_{19}c_s^2v_3^2\omega_7^3\omega_{11} - 5\omega_{19}c_s^2\omega_7^2\omega_{11}^2 - 3\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11}^2 + 72\omega_{19}v_3^4\omega_7^3\omega_{11}^2 - 72\omega_{19}v_3^2\omega_7^3 + 60\omega_{19}c_s^2v_3^2\omega_7^3\omega_{11}^2 - \omega_{19}c_s^2\omega_7^2\omega_{11}^2 + \\ & 36\omega_{19}v_3^2\omega_7^3\omega_{11}^2 + 12\omega_{19}c_s^4\omega_{11}^3 - 12\omega_{19}c_s^2\omega_7\omega_{11}^3 + 36v_3^4\omega_7^3\omega_{11}^3 - 36\omega_{19}v_3^4\omega_7^3\omega_{11} + 36v_3^2\omega_7^2\omega_{11}^2 + 39\omega_{19}v_3^2\omega_7^2\omega_{11}^2 + 6\omega_{19}c_s^4\omega_7^2\omega_{11}^2 - 99\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11}^2 - \\ & 36v_3^4\omega_7^3\omega_{11}^2 - 36\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11} + 12\omega_{19}c_s^2\omega_7^2\omega_{11} + 12\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11} + 13\omega_{19}c_s^4\omega_7^2\omega_{11}^2 + 198\omega_{19}c_s^2v_3^2\omega_7^2\omega_{11}^2 - 12\omega_{19}c_s^4\omega_7^2\omega_{11} - 72\omega_{19}v_3^2\omega_7^2\omega_{11}^2 - \\ & 12\omega_{19}c_s^2\omega_7^2\omega_{11} + 4\omega_{19}v_3^4\omega_7^3\omega_{11}^3 + 90\omega_{19}v_3^2\omega_7^3\omega_{11} + 6\omega_{19}v_3^2\omega_7^2\omega_{11}^2 - 24\omega_{19}c_s^4\omega_7\omega_{11}^3 - 6\omega_{19}c_s^4\omega_7^3\omega_{11}^2 + 19\omega_{19}v_3^4\omega_7^3\omega_{11}^2 + 18\omega_{19}c_s^2\omega_7^2\omega_{11}^2 + 12\omega_{19}c_s^4\omega_7^3 + \\ & 6\omega_{19}c_s^4\omega_7^3\omega_{11} - 108c_s^2v_3^2\omega_7^2\omega_{11}^2 + 12\omega_{19}c_s^4\omega_7^2\omega_{11}^2 - 4\omega_{19}v_3^2\omega_7^3\omega_{11}^2 - 108c_s^2v_3^2\omega_7^2\omega_{11}^2 - 18\omega_{19}c_s^2v_3^2\omega_7\omega_{11} - 6\omega_{19}v_3^4\omega_7^3\omega_{11} + 6\omega_{19}c_s^2\omega_7\omega_{11}^3 - \\ & 90\omega_{19}v_3^2\omega_7^3\omega_{11} + 6\omega_{19}c_s^2\omega_7^2\omega_{11}^2 + 72\omega_{19}v_3^4\omega_7^3 + 36\omega_{19}c_s^2v_3^2\omega_7\omega_{11}^2 + 108c_s^2v_3^2\omega_7^3\omega_{11}^2 - 19\omega_{19}^2v_3^2\omega_7^3\omega_{11}^2 - 18\omega_{19}c_s^4\omega_7^3\omega_{11}^2 - 6\omega_{19}c_s^2\omega_7^3\omega_{11}^2 \end{aligned}$$

$$C_{27} = 12 + 404c_s^2v_3^2\omega_{11}^2 + 82c_s^4\omega_{11}^2 - 132c_s^2 - 156v_3^2 - 216v_3^4\omega_{11} - 5c_s^4\omega_{11}^3 - 34c_s^2v_3^2\omega_{11}^3 + 672c_s^2v_3^2 + 90v_3^4\omega_{11}^2 - 1008c_s^2v_3^2\omega_{11} - 216c_s^4\omega_{11} - 9v_3^4\omega_{11}^3 + 234v_3^2\omega_{11} + 6c_s^2\omega_{11}^3 - 18\omega_{11} - \omega_{11}^3 - 78c_s^2\omega_{11}^2 + 8\omega_{11}^2 + 198c_s^2\omega_{11} + 10v_3^2\omega_{11}^3 + 144c_s^4 + 144v_3^4 - 98v_3^2\omega_{11}^2$$

$$C_{28} = 12 + 252c_s^2v_3^2\omega_{11}^2 + 14c_s^4\omega_{11}^2 - 36c_s^2 - 252v_3^2 - 756v_3^4\omega_{11} - c_s^4\omega_{11}^3 - 18c_s^2v_3^2\omega_{11}^3 + 432c_s^2v_3^2 + 310v_3^4\omega_{11}^2 - 648c_s^2v_3^2\omega_{11} - 36c_s^4\omega_{11} - 29v_3^4\omega_{11}^3 + 378v_3^2\omega_{11} + 2c_s^2\omega_{11}^3 - 18\omega_{11} - \omega_{11}^3 - 22c_s^2\omega_{11}^2 + 8\omega_{11}^2 + 54c_s^2\omega_{11} + 14v_3^2\omega_{11}^3 + 24c_s^4 + 504v_3^4 - 154v_3^2\omega_{11}^2$$

2.5 CLBM2

2.5.1 Definitions

Collision operator C :

$$C(f) = \mathbf{K}^{-1}\mathbf{S} \left(\kappa^{(eq)} - \mathbf{K}f \right),$$

where

$$\mathbf{S} = \text{diag}(\omega_1, \omega_2, \dots, \omega_{27}),$$

$$\omega_1, \omega_2, \dots, \omega_{27} \in (0, 2).$$

Matrix \mathbf{K} corresponds to the transformation matrix to the central moment basis defined by

$$\boldsymbol{\kappa} = \begin{pmatrix} k_{(0,0,0)} \\ k_{(1,0,0)} \\ k_{(0,1,0)} \\ k_{(0,0,1)} \\ k_{(1,1,0)} \\ k_{(1,0,1)} \\ k_{(0,1,1)} \\ k_{(2,0,0)} - k_{(0,2,0)} \\ k_{(2,0,0)} - k_{(0,0,2)} \\ k_{(2,0,0)} + k_{(0,2,0)} + k_{(0,0,2)} \\ k_{(1,2,0)} + k_{(1,0,2)} \\ k_{(2,1,0)} + k_{(0,1,2)} \\ k_{(2,0,1)} + k_{(0,2,1)} \\ k_{(1,2,0)} - k_{(1,0,2)} \\ k_{(2,1,0)} - k_{(0,1,2)} \\ k_{(2,0,1)} - k_{(0,2,1)} \\ k_{(1,1,1)} \\ k_{(2,2,0)} - 2k_{(2,0,2)} + k_{(0,2,2)} \\ k_{(2,2,0)} + k_{(2,0,2)} - 2k_{(0,2,2)} \\ k_{(2,2,0)} + k_{(2,0,2)} + k_{(0,2,2)} \\ k_{(2,1,1)} \\ k_{(1,2,1)} \\ k_{(1,1,2)} \\ k_{(2,2,1)} \\ k_{(2,1,2)} \\ k_{(1,2,2)} \\ k_{(2,2,2)} \end{pmatrix},$$

The transformation matrix \mathbf{K} satisfies

$$\begin{aligned}
\mathbf{K}_{1,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,0)} \\
\mathbf{K}_{2,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,0)} \\
\mathbf{K}_{3,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,0)} \\
\mathbf{K}_{4,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,0,1)} \\
\mathbf{K}_{5,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,0)} \\
\mathbf{K}_{6,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,0,1)} \\
\mathbf{K}_{7,i} &= (\mathbf{c}_i - \mathbf{v})^{(0,1,1)} \\
\mathbf{K}_{8,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} \\
\mathbf{K}_{9,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,0,2)} \\
\mathbf{K}_{10,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,0,2)} \\
\mathbf{K}_{11,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(1,0,2)} \\
\mathbf{K}_{12,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,0)} + (\mathbf{c}_i - \mathbf{v})^{(0,1,2)} \\
\mathbf{K}_{13,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,0,1)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,1)} \\
\mathbf{K}_{14,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)} - (\mathbf{c}_i - \mathbf{v})^{(1,0,2)} \\
\mathbf{K}_{15,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,1,2)} \\
\mathbf{K}_{16,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,0)} - (\mathbf{c}_i - \mathbf{v})^{(0,2,1)} \\
\mathbf{K}_{17,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,1)} \\
\mathbf{K}_{18,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)} - 2(\mathbf{c}_i - \mathbf{v})^{(2,0,2)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,2)} \\
\mathbf{K}_{19,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(2,0,2)} - 2(\mathbf{c}_i - \mathbf{v})^{(0,2,2)} \\
\mathbf{K}_{20,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,0)} + (\mathbf{c}_i - \mathbf{v})^{(2,0,2)} + (\mathbf{c}_i - \mathbf{v})^{(0,2,2)} \\
\mathbf{K}_{21,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,1)} \\
\mathbf{K}_{22,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,1)} \\
\mathbf{K}_{23,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,1,2)} \\
\mathbf{K}_{24,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,1)} \\
\mathbf{K}_{25,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,1,2)} \\
\mathbf{K}_{26,i} &= (\mathbf{c}_i - \mathbf{v})^{(1,2,2)} \\
\mathbf{K}_{27,i} &= (\mathbf{c}_i - \mathbf{v})^{(2,2,2)},
\end{aligned}$$

$\forall i \in \{1, 2, \dots, 27\}$. The equilibrium central moments are defined by

$$\boldsymbol{\kappa}^{(eq)} = \mathbf{K} \mathbf{M}^{-1} \boldsymbol{\mu}^{(eq)},$$

i.e.,

$$\boldsymbol{\kappa}^{(eq)} = \left(\rho, 0, 0, 0, 0, 0, 0, 0, 0, 3\rho c_s^2, 0, 0, 0, 0, 0, 0, 0, 3\rho c_s^4, 0, 0, 0, 0, 0, 0, 3\rho c_s^6 \right)^T.$$

2.5.2 Conservation of mass: ρ



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$$\begin{aligned}
& \frac{\partial \rho}{\partial t} + \frac{\delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{\rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-1 + 3c_s^2 + v_1^2) \frac{\delta_l^3 v_1}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-1 + c_s^2 + 3v_1^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\
& \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\rho \delta_l^3 c_s^2}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 \delta_l^3}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\
& + (\omega_9 c_s^2 + 24v_1^2 c_s^2 - 12v_1^2 \omega_9 c_s^2 - 2c_s^2 + 6v_1^4 - 3v_1^4 \omega_9 + 2c_s^4 - 6v_1^2 - \omega_9 c_s^4 + 3v_1^2 \omega_9) \frac{\delta_l^4}{24 \omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 - 3\omega_9 c_s^2 + 6c_s^2 + 10v_1^2 + 2\omega_9 - 5v_1^2 \omega_9) \frac{\rho \delta_l^4 v_1}{12 \omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& (-9\omega_9 c_s^2 + 3\omega_{12} c_s^2 + 3\omega_9 \omega_{12} c_s^2 + v_1^2 \omega_9 \omega_{12} + 3\omega_9 - \omega_{12} + v_1^2 \omega_{12} - \omega_9 \omega_{12} - 3v_1^2 \omega_9) \frac{\rho \delta_l^4 v_1}{12 \omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + \omega_5) \frac{\delta_l^4 c_s^4}{6 \omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (v_2^2 \omega_{15} + 3\omega_{15} c_s^2 - \omega_{15} \omega_{10} - 3v_2^2 \omega_{10} + v_2^2 \omega_{15} \omega_{10} - \omega_{15} + 3\omega_{15} c_s^2 \omega_{10} - 9c_s^2 \omega_{10} + 3\omega_{10}) \frac{v_2 \rho \delta_l^4}{12 \omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-12v_2^2 c_s^2 \omega_{10} - 3v_2^4 \omega_{10} - c_s^4 \omega_{10} - 2c_s^2 - 6v_2^2 + 2c_s^4 + 3v_2^2 \omega_{10} + 6v_2^4 + c_s^2 \omega_{10} + 24v_2^2 c_s^2) \frac{\delta_l^4}{24 \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 10v_2^2 - 5v_2^2 \omega_{10} - 3c_s^2 \omega_{10} + 2\omega_{10}) \frac{v_2 \rho \delta_l^4}{12 \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-\omega_{13} - 9\omega_9 c_s^2 + 3\omega_{13} \omega_9 c_s^2 - \omega_{13} \omega_9 + \omega_{13} v_1^2 + 3\omega_{13} c_s^2 + 3\omega_9 + \omega_{13} v_1^2 \omega_9 - 3v_1^2 \omega_9) \frac{\rho \delta_l^4 v_1}{12 \omega_{13} \omega_9 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-\omega_{16} \omega_{10} + 3c_s^2 \omega_{16} \omega_{10} + v_2^2 \omega_{16} - 3v_2^2 \omega_{10} + v_2^2 \omega_{16} \omega_{10} - 9c_s^2 \omega_{10} + 3c_s^2 \omega_{16} - \omega_{16} + 3\omega_{10}) \frac{v_2 \rho \delta_l^4}{12 \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_6) \frac{\delta_l^4 c_s^4}{6 \omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-2 + \omega_7) \frac{\delta_l^4 c_s^4}{6 \omega_7 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (-\omega_{11} \omega_{18} + \omega_{11} v_3^2 \omega_{18} + v_3^2 \omega_{18} + 3\omega_{11} - \omega_{18} - 9\omega_{11} c_s^2 - 3\omega_{11} v_3^2 + 3\omega_{11} \omega_{18} c_s^2 + 3\omega_{18} c_s^2) \frac{v_3 \rho \delta_l^4}{12 \omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (3\omega_{19} c_s^2 + 3\omega_{11} \omega_{19} c_s^2 + 3\omega_{11} - 9\omega_{11} c_s^2 - 3\omega_{11} v_3^2 - \omega_{11} \omega_{19} + \omega_{11} v_3^2 \omega_{19} + v_3^2 \omega_{19} - \omega_{19}) \frac{v_3 \rho \delta_l^4}{12 \omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-\omega_{11} c_s^4 - 3\omega_{11} v_3^4 - 2c_s^2 - 6v_3^2 + 2c_s^4 - 12\omega_{11} v_3^2 c_s^2 + 24v_3^2 c_s^2 + 6v_3^4 + \omega_{11} c_s^2 + 3\omega_{11} v_3^2) \frac{\delta_l^4}{24 \omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 2\omega_{11} + 6c_s^2 + 10v_3^2 - 3\omega_{11} c_s^2 - 5\omega_{11} v_3^2) \frac{v_3 \rho \delta_l^4}{12 \omega_{11} \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0.
\end{aligned}$$

2.5.3 Conservation of momentum: ρv_1



attached text file: output_d3q27_nse_clbm2_symbolic_pde_01.txt

$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho \delta_l v_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_2 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho \delta_l v_1}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{\rho \delta_l v_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 - 2\omega_9 c_s^2 + 4c_s^2 + 6v_1^2 + \omega_9 - 3v_1^2 \omega_9) \frac{\delta_l^2}{\omega_9 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_9) \frac{3\rho \delta_l^2 v_1}{\omega_9 \delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 - 3\omega_9 c_s^2 + 6c_s^2 + 2v_1^2 + \omega_9 - v_1^2 \omega_9) \frac{\delta_l^2 v_1}{2\omega_9 \delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 - \omega_9 c_s^2 + 2c_s^2 + 6v_1^2 + \omega_9 - 3v_1^2 \omega_9) \frac{\rho \delta_l^2}{2\omega_9 \delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_6) \frac{\rho \delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_6) \frac{\rho \delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12 \omega_9^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 - 36\omega_9 c_s^2 + 36c_s^2 + 11v_1^2 \omega_9^2 + 60v_1^2 + 24\omega_9 - 4\omega_9^2 + 5\omega_9^2 c_s^2 - 60v_1^2 \omega_9) \frac{\rho \delta_l^3 v_1}{6 \omega_9^2 \delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{\rho \delta_l^3 v_1}{12 \omega_5 \omega_9^2 \delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 - \omega_5^2 + 12\omega_5) \frac{\delta_l^3 c_s^4}{6 \omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{\rho \delta_l^3 v_1 c_s^2}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 \delta_l^3 v_1}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_3 \frac{v_2 \rho \delta_l^3}{6 \omega_5 \omega_{15} \delta_t} \frac{\partial^3 v_1}{\partial x_2^3} + \\
& (-1 + c_s^2 + 3v_2^2) \frac{\rho \delta_l^3 v_1}{12 \delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_4 \frac{\rho \delta_l^3 v_1}{12 \omega_{13} \omega_9 \omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{\rho \delta_l^3 v_1 c_s^2}{6 \delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (-12 - \omega_6^2 + 12\omega_6) \frac{\delta_l^3 c_s^4}{6 \omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \\
& \frac{\rho \delta_l^3 v_1 c_s^2}{6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{\rho \delta_l^3 v_1 c_s^2}{6 \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 \delta_l^3 v_1}{12 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \rho \delta_l^3}{6 \omega_{18} \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho \delta_l^3 v_1}{12 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} +
\end{aligned}$$

$$\begin{aligned}
& C_6 \frac{\delta_l^4 v_1}{12\omega_3^3 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_7 \frac{\rho \delta_l^4}{12\omega_3^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_8 \frac{\rho \delta_l^4}{12\omega_5^3 \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_9 \frac{\delta_l^4 v_1 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& C_{10} \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{v_2 \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\
& (v_2^2 \omega_{15} + 3\omega_{15} c_s^2 - \omega_{15} \omega_{10} - 3v_2^2 \omega_{10} + v_2^2 \omega_{15} \omega_{10} - \omega_{15} + 3\omega_{15} c_s^2 \omega_{10} - 9c_s^2 \omega_{10} + 3\omega_{10}) \frac{v_2 \rho \delta_l^4 v_1}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& C_{12} \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\
& (-12v_2^2 c_s^2 \omega_{10} - 3v_2^2 \omega_{10} - c_s^2 \omega_{10} - 2c_s^2 - 6v_2^2 + 2c_s^4 + 3v_2^2 \omega_{10} + 6v_2^4 + c_s^2 \omega_{10} + 24v_2^2 c_s^2) \frac{\delta_l^4 v_1}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& C_{13} \frac{\rho \delta_l^4}{24\omega_5^3 \omega_{15}^3 \delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + (-4 + 6c_s^2 + 10v_2^2 - 5v_2^2 \omega_{10} - 3c_s^2 \omega_{10} + 2\omega_{10}) \frac{v_2 \rho \delta_l^4 v_1}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + C_{14} \frac{\rho \delta_l^4}{12\omega_{13}^2 \omega_3^3 \omega_6^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\
& C_{15} \frac{\rho \delta_l^4 c_s^4}{12\omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 \omega_5^3 \omega_{15} \omega_9 \omega_{12} \omega_6^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (-\omega_{16} \omega_{10} + 3c_s^2 \omega_{16} \omega_{10} + v_2^2 \omega_{16} - 3v_2^2 \omega_{10} + v_2^2 \omega_{16} \omega_{10} - 9c_s^2 \omega_{10} + 3c_s^2 \omega_{16} - \omega_{16} + 3\omega_{10}) \frac{v_2 \rho \delta_l^4 v_1}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{16} \frac{\delta_l^4 v_1 c_s^2}{12\omega_{13}^2 \omega_{18} \omega_5^3 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{17} \frac{\rho \delta_l^4 c_s^2}{12\omega_{13} \omega_{18} \omega_5^3 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{18} \frac{\delta_l^4}{2\omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} \omega_6 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{19} \frac{\rho \delta_l^4}{2\omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} \omega_6 \omega_{22}^2 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{20} \frac{\rho \delta_l^4}{12\omega_{13} \omega_7 \omega_{20} \omega_{14} \omega_8 \omega_5^2 \omega_{18} \omega_9 \omega_{12} \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{21} \frac{v_3 \rho \delta_l^4}{\omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} \omega_6 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{22} \frac{\delta_l^4}{12\omega_7 \omega_{20} \omega_{17} \omega_8 \omega_5 \omega_{18} \omega_{15} \omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{23} \frac{\rho \delta_l^4}{4\omega_{20} \omega_{17} \omega_8 \omega_5^2 \omega_{18} \omega_{15} \omega_6^2 \delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + C_{24} \frac{v_2 \rho \delta_l^4}{2\omega_{20} \omega_{17} \omega_8 \omega_5 \omega_{18} \omega_{15} \omega_6 \delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\rho \delta_l^4}{4\omega_{20} \omega_{17} \omega_8 \omega_5 \omega_{18} \omega_{15} \omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{26} \frac{v_3 \delta_l^4 c_s^2}{12\omega_{13} \omega_{11} \omega_{18}^3 \omega_9 \omega_6^2 \omega_{22}^2 \delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + \\
& (-\omega_{11} \omega_{18} + \omega_{11} v_3^2 \omega_{18} + v_3^2 \omega_{18} + 3\omega_{11} - \omega_{18} - 9\omega_{11} c_s^2 - 3\omega_{11} v_3^2 + 3\omega_{11} \omega_{18} c_s^2 + 3\omega_{18} c_s^2) \frac{v_3 \rho \delta_l^4 v_1}{12\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& C_{27} \frac{\rho \delta_l^4 c_s^2}{12\omega_{13} \omega_{11} \omega_{18} \omega_9 \omega_6^3 \omega_{22}^2 \delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (3\omega_{19} c_s^2 + 3\omega_{11} \omega_{19} c_s^2 + 3\omega_{11} - 9\omega_{11} c_s^2 - 3\omega_{11} v_3^2 - \omega_{11} \omega_{19} + \omega_{11} v_3^2 \omega_{19} + v_3^2 \omega_{19} - \omega_{19}) \frac{v_3 \rho \delta_l^4 v_1}{12\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-\omega_{11} c_s^4 - 3\omega_{11} v_3^4 - 2c_s^2 - 6v_3^2 + 2c_s^4 - 12\omega_{11} v_3^2 c_s^2 + 24v_3^2 c_s^2 + 6v_3^4 + \omega_{11} c_s^2 + 3\omega_{11} v_3^2) \frac{\delta_l^4 v_1}{24\omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho \delta_l^4}{24\omega_{18}^2 \omega_6^3 \delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + (-4 + 2\omega_{11} + 6c_s^2 + 10v_3^2 - 3\omega_{11} c_s^2 - 5\omega_{11} v_3^2) \frac{v_3 \rho \delta_l^4 v_1}{12\omega_{11} \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 12\omega_9 c_s^2 + \omega_9^2 c_s^4 + 7v_1^4 \omega_9 + 144v_1^2 c_s^2 - 144v_1^2 \omega_9 c_s^2 - 12c_s^2 + 36v_1^4 - 36v_1^4 \omega_9 + 12c_s^4 - 7v_1^2 \omega_9^2 - 36v_1^2 + 24v_1^2 \omega_9^2 c_s^2 - 12\omega_9 c_s^4 - \omega_9^2 c_s^2 + 36v_1^2 \omega_9 \\
C_2 &= -12\omega_5 v_1^2 \omega_9 + 6\omega_5 \omega_9 \omega_{12} + 36\omega_5 \omega_9^2 c_s^2 - 6\omega_9^2 \omega_{12} + 12\omega_5 v_1^2 \omega_{12} + 6v_1^2 \omega_5^2 \omega_{12} - 6\omega_5 v_1^2 \omega_9 \omega_{12} - 11\omega_5 \omega_9^2 \omega_{12} c_s^2 + 12\omega_5 v_1^2 \omega_9^2 - 12\omega_5 \omega_{12} - 12v_1^2 \omega_9^2 + 18\omega_9^2 \omega_{12} c_s^2 - 18\omega_5 \omega_9 \omega_{12} c_s^2 + 12\omega_5 \omega_9 + 36\omega_5 \omega_{12} c_s^2 - 3\omega_5 v_1^2 \omega_9^2 \omega_{12} - 12\omega_5 \omega_9^2 - 36\omega_5 \omega_9 c_s^2 + 3\omega_5 \omega_9^2 \omega_{12} + 12\omega_9^2 - 36\omega_9^2 c_s^2 \\
C_3 &= 6 + 3v_2^2 \omega_{15} + 9\omega_{15} c_s^2 - 18c_s^2 + 9\omega_5 c_s^2 - 6v_2^2 - 3\omega_5 - v_2^2 \omega_5 \omega_{15} + 3v_2^2 \omega_5 - 3\omega_{15} + \omega_5 \omega_{15} - 3\omega_5 \omega_{15} c_s^2 \\
C_4 &= 12\omega_9 \omega_6 + 12\omega_{13} v_1^2 \omega_6 - 6\omega_{13} v_1^2 \omega_9 \omega_6 - 11\omega_{13} \omega_9^2 \omega_6 c_s^2 + 6\omega_{13} \omega_9 \omega_6 - 6\omega_{13} \omega_9^2 - 12v_1^2 \omega_9 \omega_6 + 36\omega_9^2 \omega_6 c_s^2 + 36\omega_{13} \omega_6 c_s^2 - 12v_1^2 \omega_9^2 - 12\omega_{13} \omega_6 + 6\omega_{13} v_1^2 \omega_9^2 - 36\omega_9 \omega_6 c_s^2 + 12v_1^2 \omega_9^2 \omega_6 + 3\omega_{13} \omega_9^2 \omega_6 + 18\omega_{13} \omega_9^2 c_s^2 - 12\omega_9^2 \omega_6 - 3\omega_{13} v_1^2 \omega_9^2 \omega_6 + 12\omega_9^2 - 18\omega_{13} \omega_9 \omega_6 c_s^2 - 36\omega_9^2 c_s^2 \\
C_5 &= 6 + 3v_3^2 \omega_{18} - 18c_s^2 - 3\omega_{18} \omega_6 c_s^2 - 6v_3^2 - 3\omega_{18} + 3v_3^2 \omega_6 + 9\omega_6 c_s^2 - 3\omega_6 - v_3^2 \omega_{18} \omega_6 + 9\omega_{18} c_s^2 + \omega_{18} \omega_6 \\
C_6 &= 12 - 9v_1^4 \omega_9^3 + 198\omega_9 c_s^2 + 82\omega_9^2 c_s^4 + 90v_1^4 \omega_9^2 + 672v_1^2 c_s^2 - 1008v_1^2 \omega_9 c_s^2 - 132c_s^2 + 144v_1^4 - 216v_1^4 \omega_9 - 5\omega_9^2 c_s^4 + 144c_s^4 - 98v_1^2 \omega_9^2 - 156v_1^2 + 404v_1^2 \omega_9^2 c_s^2 + 10v_1^2 \omega_9^3 + 6\omega_9^3 c_s^2 - 18\omega_9 - \omega_9^3 - 216\omega_9 c_s^4 + 8\omega_9^2 - 78\omega_9^2 c_s^2 - 34v_1^2 \omega_9^3 c_s^2 + 234v_1^2 \omega_9 \\
C_7 &= 12 - 29v_1^4 \omega_9^3 + 54\omega_9 c_s^2 + 14\omega_9^2 c_s^4 + 310v_1^4 \omega_9^2 + 432v_1^2 c_s^2 - 648v_1^2 \omega_9 c_s^2 - 36c_s^2 + 504v_1^4 - 756v_1^4 \omega_9 - \omega_9^3 c_s^4 + 24c_s^4 - 154v_1^2 \omega_9^2 - 252v_1^2 + 252v_1^2 \omega_9^2 c_s^2 + 14v_1^2 \omega_9^3 + 2\omega_9^3 c_s^2 - 18\omega_9 - \omega_9^3 - 36\omega_9 c_s^4 + 8\omega_9^2 - 22\omega_9^2 c_s^2 - 18v_1^2 \omega_9^3 c_s^2 + 378v_1^2 \omega_9 \\
C_8 &= 12\omega_5 \omega_9^3 \omega_{12} c_s^4 + 18\omega_5^2 v_1^2 \omega_9^2 \omega_{12}^2 c_s^2 + 6\omega_5^2 v_1^2 \omega_9^3 \omega_{12} + 72\omega_5^3 v_1^4 \omega_9^2 \omega_{12} - 12\omega_5^2 \omega_9 \omega_{12}^2 c_s^4 + 36\omega_5^2 v_1^2 \omega_9^2 - \omega_5^3 \omega_9^3 \omega_{12}^2 c_s^4 + 12\omega_9^3 \omega_{12}^2 c_s^4 - 306\omega_5^3 v_1^2 \omega_9 \omega_{12}^2 c_s^2 - 6\omega_5^2 \omega_9^2 \omega_{12}^2 c_s^2 + 39\omega_5^3 v_1^2 \omega_9^3 \omega_{12} - 36\omega_5^3 v_1^2 \omega_9^3 - 72\omega_5^3 v_1^2 \omega_{12}^2 - 6\omega_5^3 \omega_9^3 \omega_{12} c_s^2 + 4\omega_5^3 v_1^4 \omega_9^3 \omega_{12} + 12\omega_5^2 \omega_9^2 \omega_{12} c_s^4 - 12\omega_5^3 \omega_{12}^2 c_s^2 - 19\omega_5^3 v_1^2 \omega_9^2 \omega_{12} + 36\omega_5^2 v_1^4 \omega_9^3 \omega_{12} + 6\omega_5 \omega_9^3 \omega_{12}^2 c_s^2 - 36\omega_5^2 v_1^4 \omega_9^3 + 198\omega_5^3 v_1^2 \omega_9^2 \omega_{12} c_s^2 - 6\omega_5^3 \omega_9^2 \omega_{12} c_s^4 - 6\omega_5^2 v_1^4 \omega_9^3 \omega_{12}^2 - 72\omega_5^3 v_1^2 \omega_9^2 \omega_{12} + 18\omega_5^2 \omega_9^3 \omega_{12} c_s^2 + 54\omega_5^2 v_1^2 \omega_9^3 \omega_{12} c_s^2 - 39\omega_5^3 v_1^4 \omega_9^3 \omega_{12} + 36\omega_5 v_1^2 \omega_9^3 \omega_{12} c_s^2 - 4\omega_5^2 v_1^2 \omega_9^3 \omega_{12} - 12\omega_5^3 \omega_9 \omega_{12}^2 c_s^4 + 12\omega_5^3 v_1^4 \omega_9^3 \omega_{12}^2 c_s^2 + 19\omega_5^3 v_1^4 \omega_9^3 \omega_{12} - 36\omega_5^2 v_1^2 \omega_9^3 \omega_{12} - \omega_5^3 \omega_9^2 \omega_{12}^2 c_s^2 + 13\omega_5^2 \omega_9^3 \omega_{12}^2 c_s^4 + 36\omega_5^3 v_1^4 \omega_9^3 + 72\omega_5^3 v_1^4 \omega_{12}^2 - 18\omega_5 v_1^2 \omega_9^2 \omega_{12}^2 c_s^2 - 99\omega_5^3 v_1^2 \omega_9^3 \omega_{12} c_s^2 - 90\omega_5^3 v_1^4 \omega_9 \omega_{12} + 6\omega_5^3 \omega_9^2 \omega_{12} c_s^2 + 36\omega_5^2 v_1^4 \omega_9^3 - 108\omega_5^2 v_1^2 \omega_9^3 c_s^2 - 18\omega_5^2 \omega_9^3 \omega_{12} c_s^4 - 108\omega_5^3 v_1^2 \omega_9^2 c_s^2 + 36\omega_5^3 v_1^2 \omega_9 \omega_{12} + \omega_5^3 \omega_9^2 \omega_{12} c_s^4 - 5\omega_5^2 \omega_9^3 \omega_{12} c_s^2 - 36\omega_5^3 v_1^4 \omega_9 - 3\omega_5^2 v_1^2 \omega_9^3 \omega_{12}^2 c_s^2 + 12\omega_5^3 \omega_9 \omega_{12}^2 c_s^2 + 6\omega_5^2 \omega_9^2 \omega_{12}^2 c_s^4 - 36\omega_5^2 v_1^2 \omega_9 \omega_{12}^2 c_s^2 - 12\omega_5 \omega_9^3 \omega_{12}^2 c_s^2 + 90\omega_5^3 v_1^2 \omega_9 \omega_{12}^2 + 12\omega_5^2 \omega_9 \omega_{12}^2 c_s^2 + 60\omega_5^3 v_1^2 \omega_9^2 \omega_{12}^2 c_s^2 - 36\omega_5^3 v_1^4 \omega_9 \omega_{12} - 24\omega_5 \omega_9^3 \omega_{12}^2 c_s^2 + 36\omega_5^2 v_1^2 \omega_9^2 \omega_{12}^2 c_s^2 - 108\omega_5^2 v_1^2 \omega_9 \omega_{12} c_s^2 + 6\omega_5^3 \omega_9^3 \omega_{12} c_s^4 + 252\omega_5^3 v_1^2 \omega_{12}^2 c_s^2 + 108\omega_5^2 v_1^2 \omega_9 c_s^2 - 12\omega_5^2 \omega_9^2 \omega_{12} c_s^2 + 12\omega_5^2 \omega_{12}^2 c_s^4
\end{aligned}$$

$$C_9 = -12\omega_{21}v_1^2\omega_{15}\omega_9^2\omega_{12}^2 + 6\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 36\omega_{21}\omega_{15}\omega_3^3\omega_{12}c_s^2 - 6\omega_5^2v_1^2\omega_3^3\omega_{12} - 6\omega_3^2\omega_{15}\omega_9^3\omega_{12}^2 + 6\omega_5^2\omega_3^3\omega_{12}^2 + 54\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}c_s^2 + 6\omega_5^2v_1^2\omega_{15}\omega_3^3\omega_{12}^2 - 12\omega_5\omega_{21}v_1^2\omega_9^2\omega_{12}^2 - 18\omega_5^2\omega_{15}\omega_9^2\omega_{12}c_s^2 - 18\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 12\omega_5^2\omega_{15}\omega_9^2\omega_{12} - 36\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2c_s^2 - 12\omega_5v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 6\omega_5^2\omega_{21}v_1^2\omega_3^3\omega_{12}^2 - 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9\omega_{12} + 2\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 - 12\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12} - 18\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36\omega_5\omega_9^3\omega_{12}^2c_s^2 + 12\omega_5\omega_{21}\omega_{15}\omega_9^3 + 12\omega_5^2v_1^2\omega_{15}\omega_9^2\omega_{12} - 40\omega_5\omega_{21}\omega_{15}\omega_3^2\omega_{12}c_s^2 + 12\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 - 6\omega_5^2v_1^2\omega_{15}\omega_9^2\omega_{12}^2 - 36\omega_5^2\omega_{15}\omega_9^3\omega_{12}c_s^2 - 36\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2c_s^2 + 12\omega_5v_1\omega_{15}\omega_9^2\omega_{12} + 6\omega_5^2\omega_{15}\omega_9^2\omega_{12}^2 - 36\omega_5\omega_{21}\omega_9^2\omega_{12}c_s^2 - 18\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 12\omega_{21}v_1^2\omega_{15}\omega_9^2\omega_{12} + 5\omega_3^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}c_s^2 + 18\omega_5^2\omega_{21}\omega_9^2\omega_{12}c_s^2 - 12\omega_3^2v_1^2\omega_{15}\omega_9^3\omega_{12} - 6\omega_3^2\omega_{21}\omega_9^2\omega_{12}^2 - \omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36\omega_5\omega_{15}\omega_9^3\omega_{12}c_s^2 + 12\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^2\omega_{21}\omega_{15}\omega_9 - 12\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 54\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2c_s^2 + 12\omega_5\omega_{15}\omega_9^3\omega_{12}^2 - 6\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12} + 12\omega_5v_1^2\omega_9^3\omega_{12}^2 - 36\omega_5\omega_{15}\omega_9^3\omega_{12}^2c_s^2 - 12\omega_{21}\omega_{15}\omega_3^3\omega_{12}^2 - 18\omega_5^2\omega_3^3\omega_{12}^2c_s^2 + 18\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2c_s^2 - 12\omega_5^2\omega_{21}\omega_{15}\omega_{12}^2 - 12\omega_3^2\omega_{21}\omega_{15}\omega_9 - 36\omega_5^2\omega_{21}\omega_{15}\omega_9^2c_s^2 + 12\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 2\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12}^2 - 18\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2 - 12\omega_5\omega_9^3\omega_{12}^2 - 36\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2 - 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^2\omega_{12} + 18\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^2\omega_{12} + 12\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 - 36\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^3c_s^2 - 12\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^2 + 54\omega_5\omega_{21}\omega_{15}\omega_3^3\omega_{12}c_s^2 + 18\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^2\omega_{12}^2 + 12\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 36\omega_5^2\omega_{21}\omega_{15}\omega_9^3c_s^2 + 36\omega_5^2\omega_{21}\omega_{15}\omega_{12}^2c_s^2 - 12\omega_5\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_{12}^2 + 12\omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^2 + \omega_5^2\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12}^2 + 36\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2c_s^2 - 6\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12}c_s^2 + 18\omega_5\omega_{21}v_1^2\omega_{15}\omega_9^3\omega_{12} + 12\omega_5\omega_{21}\omega_9^2\omega_{12}^2 + 12\omega_{21}\omega_{15}\omega_9^2\omega_{12}^2 + 36\omega_5^2\omega_{15}\omega_9^2\omega_{12}c_s^2$$

$$C_{11} = -12v_2^2\omega_5\omega_{21}\omega_9\omega_{12}\omega_{10} - 12v_2^2\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} - 36\omega_5^2\omega_{15}^2\omega_9c_s^2\omega_{10} + 12v_2^2\omega_5^2\omega_{15}\omega_{10} + 12\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} + 36\omega_{21}\omega_{15}^2\omega_9\omega_{12}c_s^2\omega_{10} + 12\omega_5\omega_{21}\omega_9\omega_{12}\omega_{10} - 12\omega_5^2\omega_{21}\omega_{15}\omega_9 + 12v_2^2\omega_5\omega_{15}^2\omega_9\omega_{10} - 12\omega_5\omega_{15}^2\omega_9\omega_{10} + 12v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9 + v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12}\omega_{10} + 36\omega_5^2\omega_{15}^2c_s^2\omega_{10} - 36\omega_5\omega_{21}\omega_9\omega_{12}c_s^2\omega_{10} - 6\omega_5^2\omega_{21}\omega_9\omega_{12}\omega_{10} - 36\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10} + 6v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - \omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12}\omega_{10} + 12\omega_5^2\omega_{21}\omega_{15}^2 + 6v_2^2\omega_5^2\omega_{21}\omega_9\omega_{12}\omega_{10} + 36\omega_5\omega_{15}\omega_9c_s^2\omega_{10} + 54\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2 - 6\omega_5^2\omega_{21}\omega_{15}\omega_{12} - 18\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 18\omega_5^2\omega_{21}\omega_9\omega_{12}c_s^2\omega_{10} - 6v_2^2\omega_5^2\omega_{15}\omega_9\omega_{12}\omega_{10} + 12\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} + 18v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 6\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 15\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2 - 9\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10} - 5v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 12\omega_5\omega_{15}\omega_9\omega_{12}\omega_{10} + 3\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12}c_s^2\omega_{10} + 5\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 12v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12}\omega_{10} + 12v_2^2\omega_5\omega_{15}\omega_9\omega_{12}\omega_{10} + 18\omega_5^2\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10} - 12v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9 + 12\omega_5^2\omega_{15}\omega_9\omega_{10} - 3v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} - 12\omega_5^2\omega_{15}\omega_{10} - 12\omega_{21}\omega_{15}^2\omega_9\omega_{12}\omega_{10} - 12v_2^2\omega_5^2\omega_{15}\omega_9\omega_{10} + 12\omega_5\omega_{21}\omega_{15}^2\omega_9 + 36\omega_5^2\omega_{21}\omega_{15}^2\omega_9c_s^2 + 54\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10} + 12v_2^2\omega_{21}\omega_{15}^2\omega_9\omega_{12}\omega_{10} - 36\omega_5\omega_{21}\omega_{15}^2\omega_9c_s^2 - 12v_2^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 36\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12}c_s^2\omega_{10} + 3\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} + 12\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 18\omega_5^2\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10} - 12v_2^2\omega_5^2\omega_{21}\omega_{15} - 18\omega_5^2\omega_{15}^2\omega_{12}c_s^2\omega_{10} - 6\omega_5^2\omega_{15}\omega_9\omega_{12}\omega_{10} + 18\omega_5^2\omega_{21}\omega_{15}^2\omega_{12}c_s^2 - 18\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} + 6v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} + 36\omega_5\omega_{15}\omega_9\omega_{12}c_s^2\omega_{10} - 6v_2^2\omega_5^2\omega_{15}^2\omega_{12}\omega_{10} - 36\omega_5^2\omega_{21}\omega_{15}^2c_s^2 + 6\omega_5^2\omega_{15}\omega_{12}\omega_{10} + 18\omega_5^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12}\omega_{10} - 36\omega_{21}\omega_{15}^2\omega_9\omega_{12}c_s^2 - 12v_2^2\omega_5\omega_{15}^2\omega_9\omega_{12}\omega_{10} - 36\omega_5\omega_{15}^2\omega_9\omega_{12}c_s^2\omega_{10} + 12\omega_5\omega_{15}\omega_9\omega_{12}\omega_{10}$$

$$C_{13} = 24\omega_5^2\omega_{15}c_s^2 + 24\omega_{15}^2c_s^4 + 108v_2^2\omega_5^2c_s^2 + 24\omega_5\omega_{15}c_s^4 + 12\omega_5\omega_{15}^2c_s^2 - 72v_2^2\omega_5^2\omega_{15}c_s^2 + 24\omega_5^2\omega_{15}^2c_s^4 - 216v_2^2\omega_5^2c_s^2 + 72v_2^2\omega_5\omega_{15}c_s^2 + \omega_5^3\omega_{15}^2c_s^2 - 72v_2^2\omega_5^2 - 12v_2^2\omega_5^2\omega_{15}^2c_s^2 + 6\omega_5^3\omega_{15}c_s^4 + 36v_2^2\omega_5^3 - 3\omega_5^3\omega_{15}^2c_s^4 - 30v_2^2\omega_5^3\omega_{15} + 144v_2^2\omega_5^2\omega_{15}c_s^2 - 72v_2^2\omega_5^2\omega_{15} - 12v_2^2\omega_5^2\omega_{15}^2c_s^2 - 36v_2^2\omega_5\omega_{15}^2c_s^2 - 3v_2^2\omega_5^3\omega_{15} - 6\omega_5^3\omega_{15}^2c_s^2 + 30v_2^2\omega_5^3\omega_{15} - 24\omega_5\omega_{15}c_s^2 - 24\omega_5^2\omega_{15}c_s^4 - 36v_2^2\omega_5^3 + 6v_2^2\omega_5^3\omega_{15}^2c_s^2 + 72v_2^2\omega_5^2\omega_{15} - 8\omega_5^2\omega_{15}^2c_s^2 + 12v_2^2\omega_5^2\omega_{15} + 3v_2^2\omega_5^3\omega_{15} - 48\omega_5\omega_{15}^2c_s^4 + 72v_2^2\omega_5^2$$

$$\begin{aligned}
& 12\omega_7\omega_{17}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6 + 12\omega_{13}\omega_7\omega_{14}\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6^2 + 6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}\omega_{17}\omega_{14}\omega_8\omega_5\omega_{15}\omega_9\omega_{12}\omega_6^2 + \\
& 12\omega_7\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6 + 12\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}\omega_6 - 6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6^2 + 12\omega_{13}\omega_7\omega_{17}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6^2 - \\
& 12\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6^2 - 12\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}\omega_6^2 - 12\omega_7\omega_{17}\omega_8\omega_5^3\omega_{15}\omega_{12}\omega_6^2 - 6\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_9\omega_{12}\omega_6 + \\
& 12\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6 + 12\omega_{13}\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12} - 12\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6 - 12\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6^2 + \\
& 12\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_{12}\omega_6^2 + 6\omega_{13}\omega_7\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6 + 12\omega_{13}\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_{12}\omega_6^2 + 6\omega_{13}\omega_7\omega_{17}\omega_{14}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6 + \\
& 12\omega_7\omega_{17}\omega_8\omega_5^3\omega_{15}\omega_9\omega_{12}\omega_6^2 - 12\omega_{13}\omega_7\omega_{17}\omega_8\omega_5^3\omega_{15}\omega_{12}\omega_6^2
\end{aligned}$$

$$\begin{aligned}
C_{17} = & 36w_{18}v_1^7w_9w_6^2w_{22} - 12w_{13}w_{18}w_6^2w_{22}c_s^2 - 12w_{13}w_{18}w_9w_6w_{22}c_s^2 - 12w_{18}w_9w_6^3w_{22}c_s^2 - 36w_{18}v_1^7w_9^3w_6^3 - 6w_{13}w_{18}w_9^3w_6^3 - 12w_{18}w_9^3w_6^3w_{22} + \\
& 36w_{18}v_1^7w_9^3w_6^3 + 18w_{13}w_{18}v_1^7w_9^3w_6^3w_{22} - 24w_{18}w_9^3w_6^3w_{22}c_s^2 - 12w_{18}w_9^3w_6^3c_s^2 - 18w_{13}w_{18}v_1^7w_9^3w_6^3w_{22} + 36w_{18}v_1^7w_9^3w_6^3w_{22} + 18w_{13}v_1^7w_9^3w_6^3w_{22} - \\
& 24w_{13}w_{18}w_9^3w_6^3w_{22} + 12w_{13}w_9^3w_6^3w_{22} + 12w_{13}w_{18}w_9^3w_6^3 + 24w_{18}w_9^3w_6^3w_{22} + 12w_{18}w_9^3w_6^3 - 6w_{13}w_{18}w_9^3w_6^3c_s^2 - 18w_{13}w_{18}v_1^7w_9^3w_6^3 - \\
& 4w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 - 36w_{18}v_1^7w_9^3w_6^3w_{22} - 12w_{18}w_9^3w_6^3 - 6w_{13}w_9^3w_6^3w_{22} + 6w_{13}w_{18}w_9^3w_6^3w_{22} - 12w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 + 72w_{13}w_{18}v_1^7w_9^3w_6^3w_{22} - \\
& 36w_{13}v_1^7w_9^3w_6^3w_{22} - 6w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 - 36w_{13}w_{18}v_1^7w_9^3w_6^3w_{22} + 6w_{13}w_9^3w_6^3w_{22}c_s^2 + 12w_{18}w_9^3w_6^3c_s^2 - 12w_{18}w_9^3w_6^3w_{22} - 6w_{13}w_{18}w_9^3w_6^3w_{22} + \\
& 6w_{13}w_9^3w_6^3 + 12w_{18}w_9^3w_6^3w_{22}c_s^2 - 36w_{13}w_{18}v_1^7w_9^3w_6^3w_{22} + 36w_{18}v_1^7w_9^3w_6^3w_{22} - 36w_{13}w_{18}v_1^7w_9^3w_6^3 + 18w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 + 36w_{13}v_1^7w_9^3w_6^3 + \\
& 6w_{13}w_{18}w_9^3w_6^3c_s^2 - 6w_{13}w_9^3w_6^3c_s^2 - 12w_{18}w_9^3w_6^3 - 12w_{18}w_9^3w_6w_{22} + 18w_{13}w_{18}v_1^7w_9^3w_6^3 + 6w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 - 18w_{13}v_1^7w_9^3w_6^3 + 12w_{18}w_9^3w_6^3w_{22}c_s^2 - \\
& 12w_{13}w_9^3w_6^3 + 12w_{13}w_9^3w_6^3c_s^2 - 12w_{13}w_{18}w_9^3w_6^3c_s^2 - 12w_{13}w_9^3w_6^3w_{22}c_s^2 - 72w_{18}v_1^7w_9^3w_6^3w_{22} + 24w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 + 12w_{18}w_9^3w_6^3w_{22} + \\
& 12w_{13}w_{18}w_9^3w_6^3w_{22} + 12w_{13}w_{18}w_9w_6w_{22} - w_{13}w_{18}w_9^3w_6^3w_{22}c_s^2 + 12w_{18}w_9^3w_6^3c_s^2 + 12w_{18}w_9^3w_6w_{22}c_s^2 + 36w_{18}v_1^7w_9^3w_6^3 + 6w_{13}w_{18}w_9^3w_6^3
\end{aligned}$$

[illegible]

$$\begin{aligned}
& 3w_7w_{20}w_{17}w_8v_3^2w_5w_{18}v_{11}w_{15}w_6c_s^2 + 5w_7w_{20}w_{17}w_8v_2^2w_5v_{11}w_{15}w_6c_s^2 + 12w_7w_{20}v_2^2w_{18}v_{11}w_{15}w_6c_s^2 - 12w_7w_{17}v_3w_{18}v_{11}w_{15}w_6c_s^2 + \\
& 12w_7w_{20}w_8v_2^2v_3w_{18}v_{11}w_{15}w_6 - 12w_7w_{17}w_8v_2^2w_5w_{18}v_{11}w_{15}c_s^2 - 12w_7w_{20}v_2^2v_3w_5w_{18}v_{11}w_{15} + 12w_7w_{20}v_3w_5w_{18}v_{11}w_{15}w_6c_s^2 - \\
& 6w_7w_{20}w_{17}w_8v_2^2v_3w_{18}v_{11}w_6 - 12w_7w_{20}w_{17}v_2^2w_5w_{18}v_{11}w_{15}c_s^2 + 6w_7w_{17}w_8v_2^2w_5w_{18}v_{11}w_{15}w_6c_s^2 - 6w_7w_{20}w_{17}w_8v_2^2w_5v_{11}w_{15}c_s^2 + \\
& 6w_7w_{20}w_{17}w_8v_2^2w_5w_{18}v_{11}w_{15}c_s^2 + 3w_7w_{20}w_{17}w_8v_2^2w_5w_{18}v_{11}w_6c_s^2 - 12w_7w_{20}w_{17}v_2^2v_3w_5w_{18}v_{11}w_{15} - 12w_7w_{20}v_2^2v_3w_{18}w_{15}w_6c_s^2 - \\
& 12w_7w_{17}w_8v_2^2v_3w_5v_{11}w_{15} + 3w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}w_{15}w_6c_s^2 - 6w_7w_{20}w_8v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 + 6w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_{15} - \\
& 6w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}w_{15}c_s^2 + 6w_7w_{20}w_{17}w_8v_2^2v_3w_{18}w_6c_s^2 - 12w_7w_{20}w_{17}v_2^2v_3w_5w_{18}w_{15}w_6c_s^2 + 12w_7w_{20}w_{17}v_2^2v_3w_5w_{18}w_{15}c_s^2 - \\
& 12w_7w_{20}w_8v_2^2v_3w_{18}v_{11}w_{15}w_6 + 6w_7w_{20}w_8v_3w_5w_{18}v_{11}w_{15}c_s^2 + 12w_7w_{17}v_3w_{18}v_{11}w_{15}w_6c_s^2 + 6w_7w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 - \\
& 3w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_6 + 12w_7w_{17}v_2v_3w_5w_{18}v_{11}w_{15}w_6 - 12w_7w_{20}v_2^2v_3w_5w_{18}v_{11}w_{15} + 6w_7w_{17}w_8v_2^2v_3w_5v_{11}w_{15}w_6 - \\
& 6w_7w_{20}w_{17}w_8v_2^2v_3w_{18}w_{15}w_6c_s^2 + 12w_7w_{17}v_2^2w_5w_{18}v_{11}w_{15}c_s^2 - 3w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 + 12w_7w_{20}w_{17}v_2^2v_3w_{18}w_{15}w_6c_s^2 + \\
& 12w_7w_{17}v_3w_5w_{18}v_{11}w_{15}w_6c_s^2 - 6w_7w_{20}w_8v_2^2w_5w_{18}v_{11}w_{15}c_s^2 - 12w_7w_{20}w_8v_2^2v_3w_{18}w_6c_s^2 - 6w_7w_{20}w_8v_3w_5w_{18}v_{11}w_6c_s^2 - \\
& 12w_7w_{20}v_2^2v_3w_5w_{18}w_{15}c_s^2 + 12w_7w_{20}w_{17}v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 - 4w_{20}w_{17}w_8w_5w_{18}v_{11}w_{15}w_6c_s^4 - 6w_7w_{20}w_8v_3w_5w_{18}v_{11}w_{15}w_6c_s^2 + \\
& 6w_7w_{17}w_8v_2^2v_3w_{18}v_{11}w_{15}w_6 - 3w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}w_{15}w_6c_s^2 - 6w_7w_{20}w_{17}w_8v_2^2w_5v_{11}w_{15}c_s^2 - 6w_7w_{17}w_8v_2^2v_3w_5w_{18}w_{15}w_6c_s^2 - \\
& 6w_7w_{20}w_{17}w_8v_2^2v_3w_5v_{11}w_{15} + 6w_7w_{17}w_8v_3w_{18}v_{11}w_{15}w_6c_s^2 - 6w_7w_{20}w_8v_2^2v_3w_5w_{18}v_{11}w_{15} + 6w_7w_{20}w_8v_2^2w_5w_{18}v_{11}w_{15}w_6c_s^2 - \\
& 12w_7w_{17}v_2^2v_3w_5w_{18}w_{15}c_s^2 + 3w_7w_{20}w_{17}w_8v_2^2v_3w_5v_{11}w_{15}w_6 + 6w_7w_{20}w_{17}w_8v_2^2v_3w_5v_{11}w_{15} + 6w_7w_{20}w_{17}w_8v_2^2v_3w_{18}v_{11}w_6c_s^2 + \\
& 12w_7w_{20}v_2^2v_3w_5w_{18}w_{15}c_s^2 + 12w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_{15} + 12w_7w_{20}v_2^2v_3w_5w_{18}w_{15}w_6c_s^2 + 6w_7w_{20}w_8v_2^2v_3w_5w_{18}w_{15}c_s^2 + \\
& 12w_7w_{17}v_2^2v_3w_5w_{18}v_{11}w_{15} - 12w_7w_{20}w_{17}v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 + 12w_7w_{20}w_{17}v_2^2v_3w_5w_{18}v_{11}w_{15}c_s^2 - 6w_7w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_6c_s^2 - \\
& 6w_7w_{20}w_{17}w_8v_2^2v_3w_5w_{18}v_{11}w_{15}c_s^2 + 6w_7w_{20}w_{17}w_8v_2^2v_3w_{18}v_{11}w_{15}w_6 - 12w_7w_{17}v_2^2w_5w_{18}v_{11}w_{15}w_6c_s^2 + 6w_7w_{20}w_8v_2^2v_3w_5w_{18}v_{11}w_{15}w_6c_s^2 - \\
& 12w_7w_{20}w_8v_2^2v_3w_{18}v_{11}w_6c_s^2 - 12w_7w_{20}w_{17}v_3w_{18}v_{11}w_{15}w_6c_s^2 + 6w_7w_{20}w_8v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 + 6w_7w_{20}w_8v_3w_5w_{18}v_{11}w_{15}w_6c_s^2 - \\
& 12w_7w_{17}w_8v_2^2w_5w_{18}v_{11}w_{15}c_s^2 + 12w_7w_{20}w_8v_2^2v_3w_{18}w_{15}w_6c_s^2 - 12w_7w_{20}w_{17}v_2^2w_5w_{18}v_{11}w_{15}c_s^2 - 12w_7w_{20}v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 - \\
& 12w_7w_{17}v_2^2v_3w_{18}w_{15}w_6c_s^2 - 12w_7w_{20}w_8v_3w_{18}v_{11}w_6c_s^2 + 6w_7w_{20}w_{17}w_8v_2^2w_5w_{18}v_{11}w_{15}c_s^2 + 3w_7w_{20}w_{17}w_8v_2^2w_5w_{18}v_{11}w_6c_s^2 - \\
& 6w_7w_{17}w_8v_2^2v_3w_5v_{11}w_{15}w_6c_s^2 - 12w_7w_{20}v_3w_5w_{18}v_{11}w_{15}c_s^2 + 12w_7w_{20}v_2^2v_3w_5w_{18}v_{11}w_{15}w_6 + 3w_7w_{20}w_{17}w_8v_2^2w_5v_{11}w_{15}w_6c_s^2 + \\
& 12w_7w_{17}w_8v_2^2w_5v_{11}w_{15}c_s^2 + 12w_7w_{17}w_8v_2^2v_3w_5v_{11}w_{15} - 12w_7w_{17}v_3w_5w_{18}v_{11}w_{15}w_6c_s^2 + 12w_7w_{20}v_2^2w_{18}v_{11}w_{15}w_6c_s^2 - 6w_7w_{20}w_{17}w_8v_2^2w_{18}v_{11}w_6c_s^2
\end{aligned}$$

$$\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{22}c_s^2 + \omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22} + 6\omega_{13}\omega_{11}\omega_{18}\omega_6^3 + 36\omega_{13}\omega_{11}v_3^2\omega_9\omega_6^2$$

$$C_{28} = -12v_3^4\omega_{18}\omega_6^2 - 12v_3^2\omega_{18}^2\omega_6^2c_s^2 + \omega_{18}^2\omega_6^3c_s^2 + 108v_3^2\omega_6^3c_s^2 + 72v_3^2\omega_{18}\omega_6c_s^2 + 3v_3^4\omega_{18}^2\omega_6^3 + 6\omega_{18}\omega_6^3c_s^4 - 72v_3^4\omega_6^2 + 6v_3^2\omega_{18}^2\omega_6^3c_s^2 - 48\omega_{18}^2\omega_6c_s^4 + 12v_3^2\omega_{18}^2\omega_6^2 - 24\omega_{18}\omega_6c_s^2 - 24\omega_{18}\omega_6^2c_s^4 + 36v_3^4\omega_6^3 - 216v_3^2\omega_6^2c_s^2 - 3v_3^2\omega_{18}^2\omega_6^3 - 8\omega_{18}^2\omega_6^2c_s^2 + 24\omega_{18}\omega_6c_s^4 - 72v_3^2\omega_{18}\omega_6^3c_s^2 + 30v_3^2\omega_{18}\omega_6^3 + 12\omega_{18}^2\omega_6c_s^2 + 24\omega_{18}\omega_6^2c_s^4 + 24\omega_{18}\omega_6^2c_s^2 - 72v_3^2\omega_{18}\omega_6^2 - 36v_3^2\omega_6^3 + 144v_3^2\omega_{18}\omega_6^2c_s^2 + 24\omega_{18}^2c_s^4 - 30v_3^4\omega_{18}\omega_6^3 + 72v_3^2\omega_6^2 - 6\omega_{18}\omega_6^3c_s^2 + 72v_3^4\omega_{18}\omega_6^2 - 3\omega_{18}^2\omega_6^3c_s^4 - 36v_3^2\omega_{18}\omega_6^2c_s^2$$

2.5.4 Conservation of momentum: ρv_2



attached text file: output_d3q27_nse_clbm2_symbolic_pde_02.txt

$$\begin{aligned} & v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_2 \delta_l v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_2 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho \delta_l v_1}{\delta_t} \frac{\partial v_2}{\partial x_1} + (c_s^2 + v_2^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2v_2 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\ & \frac{v_2 \rho \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_5) \frac{\delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\ & (-2 + 4c_s^2 + 6v_2^2 - 3v_2^2\omega_{10} - 2c_s^2\omega_{10} + \omega_{10}) \frac{\delta_l^2}{\delta_t \omega_{10}} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_{10}) \frac{3v_2 \rho \delta_l^2}{\delta_t \omega_{10}} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\omega_7 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\ & (-2 + \omega_7) \frac{\delta_l^2 c_s^2}{2\omega_7 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_5) \frac{\rho \delta_l^2 c_s^2}{2\omega_5 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\ & (-2 + 6c_s^2 + 2v_2^2 - v_2^2\omega_{10} - 3c_s^2\omega_{10} + \omega_{10}) \frac{v_2 \delta_l^2}{2\delta_t \omega_{10}} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 + 2c_s^2 + 6v_2^2 - 3v_2^2\omega_{10} - c_s^2\omega_{10} + \omega_{10}) \frac{\rho \delta_l^2}{2\delta_t \omega_{10}} \frac{\partial^2 v_2}{\partial x_2^2} + \\ & (-2 + \omega_7) \frac{\rho \delta_l^2 c_s^2}{2\omega_7 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_7) \frac{\rho \delta_l^2 c_s^2}{2\omega_7 \delta_t} \frac{\partial^2 v_2}{\partial x_2^2} + (-1 + 3c_s^2 + v_1^2) \frac{v_2 \delta_l^3 v_1}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{v_2 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\ & C_1 \frac{\rho \delta_l^3 v_1}{6\omega_5 \omega_{12} \delta_t} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 - \omega_5^2 + 12\omega_5) \frac{\delta_l^3 c_s^4}{6\omega_5^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \frac{v_2 \rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_2 \frac{v_2 \rho \delta_l^3}{12\omega_5 \omega_{15} \delta_t \omega_{10}^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_3 \frac{\delta_l^3}{12\delta_t \omega_{10}^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2^2} + \\ & (-24 - 4\omega_{10}^2 + 36c_s^2 + 60v_2^2 - 60v_2^2\omega_{10} + 5c_s^2\omega_{10}^2 - 36c_s^2\omega_{10} + 11v_2^2\omega_{10}^2 + 24\omega_{10}) \frac{v_2 \rho \delta_l^3}{6\delta_t \omega_{10}^2} \frac{\partial^3 v_2}{\partial x_2^2} - \frac{v_2 \rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\ & C_4 \frac{v_2 \rho \delta_l^3}{12\omega_7 \delta_t \omega_{16} \omega_{10}^2} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{v_2 \rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-12 + 12\omega_7 - \omega_7^2) \frac{\delta_l^3 c_s^4}{6\omega_7^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{v_2 \rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\ & (-1 + 3c_s^2 + v_3^2) \frac{v_2 v_3 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \rho \delta_l^3}{6\omega_7 \omega_{19} \delta_t} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{v_2 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\ & (\omega_9 c_s^2 + 24v_1^2 c_s^2 - 12v_1^2 \omega_9 c_s^2 - 2c_s^2 + 6v_1^4 - 3v_1^4 \omega_9 + 2c_s^4 - 6v_1^2 - \omega_9 c_s^4 + 3v_1^2 \omega_9) \frac{v_2 \delta_l^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & (-4 - 3\omega_9 c_s^2 + 6c_s^2 + 10v_1^2 + 2\omega_9 - 5v_1^2 \omega_9) \frac{v_2 \rho \delta_l^4 v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_l^4}{24\omega_5^3 \omega_{12}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_1^4} + C_7 \frac{\delta_l^4 v_1 c_s^2}{12\omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12}^2 \delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\ & C_8 \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + \\ & (-9\omega_9 c_s^2 + 3\omega_{12} c_s^2 + 3\omega_9 \omega_{12} c_s^2 + v_1^2 \omega_9 \omega_{12} + 3\omega_9 - \omega_{12} + v_1^2 \omega_{12} - \omega_9 \omega_{12} - 3v_1^2 \omega_9) \frac{v_2 \rho \delta_l^4 v_1}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\ & C_9 \frac{v_2 \delta_l^4 c_s^2}{12\omega_5^2 \omega_{21} \omega_{15}^2 \omega_{12} \delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{10} \frac{\rho \delta_l^4 c_s^2}{12\omega_5^3 \omega_{21} \omega_{15} \omega_{12} \delta_t \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\rho \delta_l^4}{12\omega_5^3 \omega_{15}^2 \delta_t \omega_{10}^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + C_{12} \frac{v_2 \delta_l^4}{12\delta_t \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\ & C_{13} \frac{\rho \delta_l^4}{12\delta_t \omega_{10}^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + (-\omega_{13} - 9\omega_9 c_s^2 + 3\omega_{13} \omega_9 c_s^2 - \omega_{13} \omega_9 + \omega_{13} v_1^2 + 3\omega_{13} c_s^2 + 3\omega_9 + \omega_{13} v_1^2 \omega_9 - 3v_1^2 \omega_9) \frac{v_2 \rho \delta_l^4 v_1}{12\omega_{13} \omega_9 \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + \\ & C_{14} \frac{\rho \delta_l^4 c_s^2}{12\omega_7^2 \omega_{17} \omega_{14} \omega_8 \omega_5^2 \omega_{15} \omega_{12} \omega_6 \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{15} \frac{\rho \delta_l^4}{12\omega_7^2 \delta_t \omega_{16}^2 \omega_{10}^3} \frac{\partial^4 v_3}{\partial x_3^2 \partial x_3} + C_{16} \frac{\delta_l^4}{12\omega_7 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{12} \omega_6 \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\ & C_{17} \frac{\rho \delta_l^4}{4\omega_7 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{12} \omega_{19} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{18} \frac{\rho \delta_l^4}{4\omega_7^2 \omega_{20} \omega_{14} \omega_8 \omega_5^2 \omega_{12} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + C_{19} \frac{v_3 \rho \delta_l^4}{2\omega_7 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{12} \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + \\ & C_{20} \frac{\delta_l^4}{2\omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5 \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{21} \frac{\rho \delta_l^4}{12\omega_7^3 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5^2 \omega_{15} \omega_6 \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\ & C_{22} \frac{v_2 \rho \delta_l^4}{\omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5 \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{23} \frac{\rho \delta_l^4}{2\omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_8 \omega_5 \omega_{15} \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\ & C_{24} \frac{v_2 \delta_l^4 c_s^2}{12\omega_7^2 \omega_{23} \omega_{19} \delta_t \omega_{16} \omega_{10}^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\rho \delta_l^4 c_s^2}{12\omega_7^3 \omega_{23} \omega_{19} \delta_t \omega_{16} \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\ & (-\omega_{11} \omega_{18} + \omega_{11} v_3^2 \omega_{18} + v_3^2 \omega_{18} + 3\omega_{11} - \omega_{18} - 9\omega_{11} c_s^2 - 3\omega_{11} v_3^2 + 3\omega_{11} \omega_{18} c_s^2 + 3\omega_{18} c_s^2) \frac{v_2 v_3 \rho \delta_l^4}{12\omega_{11} \omega_{18} \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\ & C_{26} \frac{v_3 \delta_l^4 c_s^2}{12\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + \\ & (3\omega_{19} c_s^2 + 3\omega_{11} \omega_{19} c_s^2 + 3\omega_{11} - 9\omega_{11} c_s^2 - 3\omega_{11} v_3^2 - \omega_{11} \omega_{19} + \omega_{11} v_3^2 \omega_{19} + v_3^2 \omega_{19} - \omega_{19}) \frac{v_2 v_3 \rho \delta_l^4}{12\omega_{11} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\ & C_{27} \frac{\rho \delta_l^4 c_s^2}{12\omega_7^3 \omega_{23} \omega_{11} \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\ & (-\omega_{11} c_s^4 - 3\omega_{11} v_3^4 - 2c_s^2 - 6v_3^2 + 2c_s^4 - 12\omega_{11} v_3^2 c_s^2 + 24v_3^2 c_s^2 + 6v_3^4 + \omega_{11} c_s^2 + 3\omega_{11} v_3^2) \frac{v_2 \delta_l^4}{24\omega_{11} \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \end{aligned}$$

$$\begin{aligned}
& 12\omega_7^2 v_{19}^2 \omega_{16} \omega_{10}^3 + 36\omega_7^2 \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 12\omega_7^2 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 - 36\omega_7 \omega_{23} c_s^* \omega_{16} \omega_{10}^3 + 12\omega_7 \omega_{19} \omega_{16} \omega_{10}^3 + 12\omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - \\
& 12\omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 + 12\omega_7 v_{19}^2 \omega_{16} \omega_{10}^3 - 12\omega_7 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 + 36\omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 54\omega_7 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 18\omega_7^2 \omega_{23} c_s^* \omega_{16} \omega_{10}^3 - \\
& 36\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 36\omega_7^2 \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 12\omega_7^2 v_{19}^2 \omega_{16} \omega_{10}^3 - 6\omega_7^2 v_{19}^2 \omega_{16}^3 \omega_{10}^3 - 6\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16}^2 \omega_{10}^3 - 18\omega_7 \omega_{23} \omega_{19} \omega_{16}^2 \omega_{10}^3 - 6\omega_7^2 \omega_{23} \omega_{16}^2 \omega_{10}^3 + \\
& 12\omega_7 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 + 36\omega_7 c_s^* \omega_{16} \omega_{10}^3 - 12\omega_7^2 \omega_{16}^3 \omega_{10}^3 + 12\omega_7 \omega_{23} \omega_{19} \omega_{10}^3 + 36\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 12\omega_7^2 \omega_{19} \omega_{16} \omega_{10}^3 - \omega_7^2 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 + \\
& 12\omega_7^2 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 + 12\omega_7^2 \omega_{23} v_{19} \omega_{16} \omega_{10}^3 + 12\omega_7^2 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 - 36\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 2\omega_7^2 \omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 - 12\omega_7 \omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 + \\
& 12\omega_7 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 + 5\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 36\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16}^2 \omega_{10}^3 + 2\omega_7^2 \omega_{23} \omega_{19} \omega_{16}^2 \omega_{10}^3 - 12\omega_7^2 \omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 - 36\omega_7 \omega_{23} \omega_{19} c_s^* \omega_{16}^2 \omega_{10}^3 + 6\omega_7^2 \omega_{16}^3 \omega_{10}^3 - \\
& 6\omega_7^2 \omega_{19} \omega_{16}^3 \omega_{10}^3 - 18\omega_7 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - 18\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 18\omega_7^2 \omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 - 18\omega_7^2 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - 6\omega_7^2 \omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 + \\
& 12\omega_7 v_{19}^2 \omega_{16} \omega_{10}^3 + 54\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 6\omega_7^2 \omega_{19} \omega_{16} \omega_{10}^3 + 6\omega_7^2 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - 36\omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 12\omega_7 v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 + \\
& 18\omega_7 \omega_{23} v_{19} \omega_{16} \omega_{10}^3 + 6\omega_7^2 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 - 12\omega_7^2 \omega_{23} \omega_{19} \omega_{10}^3 + 12\omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - 36\omega_7^2 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 6\omega_7^2 \omega_{19} \omega_{16} \omega_{10}^3 + 12\omega_7 \omega_{23} \omega_{16}^2 \omega_{10}^3 - \\
& 18\omega_7^2 c_s^* \omega_{16} \omega_{10}^3 + 18\omega_7^2 \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 12\omega_7^2 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - 12\omega_7^2 \omega_{23} \omega_{19} \omega_{16}^3 \omega_{10}^3 - 12\omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 + 54\omega_7 \omega_{23} \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - 36\omega_7 \omega_{19} c_s^* \omega_{16} \omega_{10}^3 - \\
& 18\omega_7^2 \omega_{19} c_s^* \omega_{16} \omega_{10}^3 + 6\omega_7^2 v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 - 12\omega_{23} \omega_{19} \omega_{16} \omega_{10}^3 - 12\omega_7 \omega_{23} v_{19}^2 \omega_{16} \omega_{10}^3 - 12\omega_7 \omega_{19} \omega_{16} \omega_{10}^3 - 12\omega_7^2 \omega_{23} v_{19}^2 \omega_{19} \omega_{16} \omega_{10}^3 + 12\omega_7^2 \omega_{23} \omega_{19} \omega_{16} \omega_{10}^3
\end{aligned}$$

$$\begin{aligned}
C_{26} = & 6\omega_7^2\omega_{23}v_3^2\omega_{19}\omega_{16} - 36\omega_7^2\omega_{23}\omega_{19}c_s^2 - 36\omega_7^2\omega_{19}c_s^2\omega_{16}\omega_{10} - 6\omega_7^2\omega_{11}\omega_{19}^2\omega_{16}\omega_{10} + 12\omega_7\omega_{11}v_3^2\omega_{19}\omega_{10} + 18\omega_7^2\omega_{11}\omega_{19}^2c_s^2\omega_{16}\omega_{10} + \\
& 12\omega_7^2\omega_{23}v_3^2\omega_{19}\omega_{10} - 18\omega_7\omega_{23}\omega_{19}\omega_{16}\omega_{10} - 18\omega_7\omega_{23}\omega_{11}\omega_{19}\omega_{16}\omega_{10} + 12\omega_7\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} + 18\omega_7^2\omega_{23}\omega_{11}c_s^2\omega_{16}\omega_{10} + \\
& 54\omega_7\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} - 12\omega_7\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} - 3\omega_7^2\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} - 12\omega_7\omega_{23}v_3^2\omega_{19}\omega_{10} + 5\omega_7^2\omega_{23}\omega_{19}\omega_{16}\omega_{10} + \\
& 54\omega_7\omega_{23}\omega_{19}c_s^2\omega_{16}\omega_{10} - 6\omega_7^2\omega_{11}v_3^2\omega_{19}\omega_{16} + 6\omega_7^2\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{10} + 12\omega_{23}\omega_{11}\omega_{19}\omega_{16}\omega_{10} + 12\omega_7\omega_{11}\omega_{19}^2\omega_{16}\omega_{10} - 12\omega_7^2\omega_{11}v_3^2\omega_{19}\omega_{10} - \\
& 36\omega_7\omega_{23}\omega_{11}c_s^2\omega_{16}\omega_{10} - 6\omega_7^2\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} - 15\omega_7^2\omega_{23}\omega_{11}c_s^2\omega_{16}\omega_{10} - 12\omega_7\omega_{23}\omega_{11}v_3^2\omega_{16}\omega_{10} - 12\omega_7^2\omega_{23}v_3^2\omega_{19}^2 - 12\omega_7\omega_{11}v_3^2\omega_{19}\omega_{10} - \\
& 12\omega_7^2\omega_{23}\omega_{19}\omega_{10} + 3\omega_7^2\omega_{23}\omega_{11}v_3^2\omega_{16}\omega_{10} - 36\omega_7\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} + 3\omega_7^2\omega_{23}\omega_{11}\omega_{19}\omega_{16}\omega_{10} - 6\omega_7^2\omega_{23}\omega_{19}\omega_{16} + 12\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} - \\
& 36\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} + 6\omega_7^2\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} - 18\omega_7^2\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} + 12\omega_{23}\omega_{19}\omega_{16}\omega_{10} + 36\omega_7^2\omega_{11}\omega_{19}^2c_s^2 - 12\omega_7^2\omega_{11}\omega_{19}^2 - \\
& 12\omega_{23}v_3^2\omega_{19}\omega_{16}\omega_{10} - 6\omega_7^2\omega_{23}\omega_{11}\omega_{16}\omega_{10} + 12\omega_7\omega_{23}\omega_{11}\omega_{16}\omega_{10} - 12\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} + 18\omega_7\omega_{23}v_3^2\omega_{19}\omega_{16}\omega_{10} - \omega_7^2\omega_{23}\omega_{11}\omega_{19}\omega_{16}\omega_{10} - \\
& 36\omega_7\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} + 36\omega_7\omega_{11}\omega_{19}^2c_s^2\omega_{16} + 6\omega_7^2\omega_{11}\omega_{19}\omega_{16}\omega_{10} + 18\omega_7^2\omega_{23}\omega_{19}c_s^2\omega_{16} + 12\omega_7\omega_{23}\omega_{11}\omega_{19}\omega_{16}\omega_{10} - 5\omega_7^2\omega_{23}v_3^2\omega_{19}\omega_{16}\omega_{10} + \\
& 36\omega_7^2\omega_{23}v_3^2\omega_{19}c_s^2\omega_{10} + 12\omega_7^2\omega_{23}\omega_{19} - 18\omega_7^2\omega_{11}\omega_{19}^2c_s^2\omega_{16} + 36\omega_{23}\omega_{11}\omega_{19}^2c_s^2\omega_{16}\omega_{10} + \omega_7^2\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} - 9\omega_7^2\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} - \\
& 36\omega_7\omega_{23}\omega_{19}c_s^2\omega_{10} + 6\omega_7^2\omega_{11}\omega_{19}\omega_{16} + 36\omega_7\omega_{11}\omega_{19}c_s^2\omega_{16}\omega_{10} - 12\omega_7\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} + 18\omega_7\omega_{23}\omega_{11}v_3^2\omega_{19}\omega_{16}\omega_{10} + 12\omega_7\omega_{23}\omega_{19}\omega_{10} + \\
& 12\omega_7^2\omega_{11}v_3^2\omega_{19} - 36\omega_7^2\omega_{11}\omega_{19}^2c_s^2\omega_{10} - 12\omega_7\omega_{11}\omega_{19}\omega_{16}\omega_{10} + 12\omega_7^2\omega_{11}\omega_{19}\omega_{10} - 12\omega_{23}\omega_{11}\omega_{19}\omega_{16}\omega_{10}
\end{aligned}$$

$$C_{28} = 72\omega_7^2 v_3^2 + 24\omega_7 \omega_{19} v_9 c_s^2 + 24\omega_{19}^2 c_s^4 + 24\omega_7 \omega_{19} c_s^4 + 108\omega_3^3 v_3^2 c_s^2 + 12\omega_7 \omega_{19}^2 c_s^2 - 72\omega_3^3 v_3^2 \omega_{19} c_s^2 - 12\omega_2^2 v_3^4 \omega_{19}^2 - 3\omega_3^3 v_3^2 \omega_{19}^2 + 24\omega_7^2 \omega_{19}^2 c_s^4 - 36\omega_7 v_3^2 \omega_{19}^2 c_s^2 + 144\omega_7^2 v_3^2 \omega_{19} c_s^2 + 30\omega_3^3 v_3^2 \omega_{19} - 36\omega_7^3 v_3^2 + \omega_7^2 \omega_{19}^2 c_s^2 + 72\omega_7^2 v_3^4 \omega_{19} + 6\omega_3^3 \omega_{19}^2 c_s^4 + 36\omega_7^3 v_3^4 + 12\omega_2^2 v_3^2 \omega_{19}^2 - 3\omega_3^3 \omega_{19}^2 c_s^4 + 3\omega_3^3 v_3^4 \omega_{19}^2 - 12\omega_2^2 v_3^2 \omega_{19}^2 c_s^2 - 216\omega_7^2 v_3^2 c_s^2 - 6\omega_3^3 \omega_{19} c_s^2 - 24\omega_7 \omega_{19} c_s^2 + 6\omega_7^3 v_3^2 \omega_{19} c_s^2 - 72\omega_7^2 v_3^4 + 72\omega_7 v_3^2 \omega_{19} c_s^2 - 24\omega_7^2 \omega_{19} c_s^4 - 8\omega_7^2 \omega_{19}^2 c_s^2 - 30\omega_7^3 v_3^4 \omega_{19} - 48\omega_7 \omega_{19}^2 c_s^4 - 72\omega_7^2 v_3^4 \omega_{19}$$


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$$\begin{aligned} & v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 \delta_1 v_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \rho \delta_1}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho \delta_1 v_1}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_2 v_3 \delta_1}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \rho \delta_1}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 \rho \delta_1}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_1}{\delta_t} \frac{\partial \rho}{\partial x_1} + \\ & \frac{2 v_3 \rho \delta_1}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_6) \frac{\delta_1^2 c_s^2}{2 \omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_6) \frac{\delta_1^2 c_s^2}{2 \omega_6 \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2 \omega_7 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_7) \frac{\delta_1^2 c_s^2}{2 \omega_7 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} \\ & + (-2 + \omega_{11} + 4c_s^2 + 6v_3^2 - 2\omega_{11}c_s^2 - 3\omega_{11}v_3^2) \frac{\delta_1^2}{\omega_{11} \delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (2 - \omega_{11}) \frac{3 v_3 \rho \delta_1^2}{\omega_{11} \delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_6) \frac{\rho \delta_1^2 c_s^2}{2 \omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_1^2} + \end{aligned}$$

$$\begin{aligned}
& (-2 + \omega_7) \frac{\rho \delta_l^2 c_s^2}{2\omega_7 \delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_6) \frac{\rho \delta_l^2 c_s^2}{2\omega_6 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_7) \frac{\rho \delta_l^2 c_s^2}{2\omega_7 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\
& (-2 + \omega_{11} + 6c_s^2 + 2v_3^2 - 3\omega_{11}c_s^2 - \omega_{11}v_3^2) \frac{v_3 \rho \delta_l^2}{2\omega_{11} \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_{11} + 2c_s^2 + 6v_3^2 - \omega_{11}c_s^2 - 3\omega_{11}v_3^2) \frac{\rho \delta_l^2}{2\omega_{11} \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (-1 + 3c_s^2 + v_1^2) \frac{v_3 \rho \delta_l^2}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{v_3 \rho \delta_l^2}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{\rho \delta_l^4 v_1}{6\omega_{13}\omega_6 \delta_t} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{v_3 \rho \delta_l^4 c_s^2}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{v_3 \rho \delta_l^4 c_s^2}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-1 + 3c_s^2 + v_2^2) \frac{v_2 v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_2 \frac{v_2 \rho \delta_l^3}{6\omega_7 \delta_t \omega_{16}} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 - \omega_6^2 + 12\omega_6) \frac{\delta_l^3 c_s^4}{6\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\
& \frac{v_3 \rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 + 12\omega_7 - \omega_7^2) \frac{\delta_l^3 c_s^4}{6\omega_7^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{v_3 \rho \delta_l^3 c_s^2}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_3 \frac{v_3 \rho \delta_l^3}{12\omega_{11}^2 \omega_{18} \omega_6 \delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\
& C_4 \frac{v_3 \rho \delta_l^3}{12\omega_7 \omega_{11}^2 \omega_{19} \delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_5 \frac{\delta_l^3}{12\omega_{11}^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + \\
& (-24 - 4\omega_{11}^2 + 24\omega_{11} + 36c_s^2 + 60v_3^2 + 11\omega_{11}^2 v_3^2 + 5\omega_{11}^2 c_s^2 - 36\omega_{11}c_s^2 - 60\omega_{11}v_3^2) \frac{v_3 \rho \delta_l^3}{6\omega_{11}^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (\omega_9 c_s^2 + 24v_1^2 c_s^2 - 12v_1^2 \omega_9 c_s^2 - 2c_s^2 + 6v_1^4 - 3v_1^4 \omega_9 + 2c_s^4 - 6v_1^2 - \omega_9 c_s^4 + 3v_1^2 \omega_9) \frac{v_3 \rho \delta_l^4}{24\omega_9 \delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 - 3\omega_9 c_s^2 + 6c_s^2 + 10v_1^2 + 2\omega_9 - 5v_1^2 \omega_9) \frac{v_3 \rho \delta_l^4 v_1}{12\omega_9 \delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\rho \delta_l^4}{24\omega_{13}^2 \omega_6^3 \delta_t} \frac{\partial^4 v_3}{\partial x_1^4} + \\
& (-9\omega_9 c_s^2 + 3\omega_{12} c_s^2 + 3\omega_9 \omega_{12} c_s^2 + v_1^2 \omega_9 \omega_{12} + 3\omega_9 - \omega_{12} + v_1^2 \omega_{12} - \omega_9 \omega_{12} - 3v_1^2 \omega_9) \frac{v_3 \rho \delta_l^4 v_1}{12\omega_9 \omega_{12} \delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\
& (-2 + \omega_5) \frac{v_3 \rho \delta_l^4 c_s^4}{6\omega_5 \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_7 \frac{\rho \delta_l^4 c_s^4}{2\omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 \omega_6^2 \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (v_2^2 \omega_{15} + 3\omega_{15} c_s^2 - \omega_{15} \omega_{10} - 3v_2^2 \omega_{10} + v_2^2 \omega_{15} \omega_{10} - \omega_{15} + 3\omega_{15} c_s^2 \omega_{10} - 9c_s^2 \omega_{10} + 3\omega_{10}) \frac{v_2 v_3 \rho \delta_l^4}{12\omega_{15} \delta_t \omega_{10}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
& (-12v_2^2 c_s^2 \omega_{10} - 3v_2^4 \omega_{10} - c_s^4 \omega_{10} - 2c_s^2 - 6v_2^2 + 2c_s^4 + 3v_2^2 \omega_{10} + 6v_2^4 + c_s^2 \omega_{10} + 24v_2^2 c_s^2) \frac{v_3 \rho \delta_l^4}{24\delta_t \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 + 6c_s^2 + 10v_2^2 - 5v_2^2 \omega_{10} - 3c_s^2 \omega_{10} + 2\omega_{10}) \frac{v_2 v_3 \rho \delta_l^4}{12\delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^4} + C_8 \frac{\rho \delta_l^4}{24\omega_7^2 \delta_t \omega_{16}^2} \frac{\partial^4 v_3}{\partial x_2^4} + C_9 \frac{\delta_l^4 v_1 c_s^2}{12\omega_{13}^2 \omega_{11} \omega_{18} \omega_9 \omega_6^2 \omega_{22} \delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_{10} \frac{\rho \delta_l^4 c_s^2}{12\omega_{13} \omega_{11} \omega_{18} \omega_9 \omega_6^3 \omega_{22} \delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& (-\omega_{13} - 9\omega_9 c_s^2 + 3\omega_{13} \omega_9 c_s^2 - \omega_{13} \omega_9 + \omega_{13} v_1^2 + 3\omega_{13} c_s^2 + 3\omega_9 + \omega_{13} v_1^2 \omega_9 - 3v_1^2 \omega_9) \frac{v_3 \rho \delta_l^4 v_1}{12\omega_{13} \omega_9 \delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{11} \frac{\delta_l^4}{2\omega_{13} \omega_7 \omega_{20} \omega_{11} \omega_{14} \omega_8 \omega_{18} \omega_6 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{12} \frac{\rho \delta_l^4}{2\omega_{13} \omega_7 \omega_{20} \omega_{11} \omega_{14} \omega_8 \omega_{18} \omega_6 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{13} \frac{\rho \delta_l^4}{12\omega_{13} \omega_7^2 \omega_{20} \omega_{11} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_6^3 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{14} \frac{v_3 \rho \delta_l^4}{\omega_{13} \omega_7 \omega_{20} \omega_{11} \omega_{14} \omega_8 \omega_{18} \omega_6 \omega_{22} \omega_{19} \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{15} \frac{\delta_l^4}{2\omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8 \omega_{18} \omega_6 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{16} \frac{\rho \delta_l^4}{12\omega_7^2 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8 \omega_5 \omega_{18} \omega_6^3 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{17} \frac{v_2 \rho \delta_l^4}{\omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8 \omega_{18} \omega_6 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{18} \frac{\rho \delta_l^4}{2\omega_7 \omega_{23} \omega_{20} \omega_{17} \omega_{11} \omega_8 \omega_{18} \omega_6 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{19} \frac{v_2 \rho \delta_l^4 c_s^2}{12\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t \omega_{16}^2 \omega_{10}} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{20} \frac{\rho \delta_l^4 c_s^2}{12\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + \\
& (-\omega_{16} \omega_{10} + 3c_s^2 \omega_{16} \omega_{10} + v_2^2 \omega_{16} - 3v_2^2 \omega_{10} + v_2^2 \omega_{16} \omega_{10} - 9c_s^2 \omega_{10} + 3c_s^2 \omega_{16} - \omega_{16} + 3\omega_{10}) \frac{v_2 v_3 \rho \delta_l^4}{12\delta_t \omega_{16} \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{21} \frac{v_3 \rho \delta_l^4 c_s^2}{12\omega_{13} \omega_{11}^2 \omega_{18} \omega_6^2 \omega_{22} \delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{22} \frac{\rho \delta_l^4 c_s^2}{12\omega_{13} \omega_{11}^2 \omega_{18} \omega_6^3 \omega_{22} \delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{23} \frac{v_3 \rho \delta_l^4 c_s^2}{12\omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& C_{24} \frac{\rho \delta_l^4 c_s^2}{12\omega_7^2 \omega_{23} \omega_{11}^2 \omega_{19} \delta_t \omega_{16}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{25} \frac{\rho \delta_l^4}{12\omega_{11}^3 \omega_{18}^2 \omega_6^3 \delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{26} \frac{\rho \delta_l^4}{12\omega_7^2 \omega_{11}^2 \omega_{19}^2 \delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{27} \frac{v_3 \rho \delta_l^4}{12\omega_{11}^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{28} \frac{\rho \delta_l^4}{12\omega_{11}^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 3\omega_{13} - \omega_{13} v_1^2 \omega_6 + 3v_1^2 \omega_6 + 3\omega_{13} v_1^2 - 18c_s^2 - 3\omega_{13} \omega_6 c_s^2 + 9\omega_{13} c_s^2 - 6v_1^2 + \omega_{13} \omega_6 + 9\omega_6 c_s^2 - 3\omega_6 \\
C_2 &= 6 - 3\omega_7 - 3\omega_7 c_s^2 \omega_{16} - 18c_s^2 - \omega_7 v_2^2 \omega_{16} - 6v_2^2 + 3v_2^2 \omega_{16} + \omega_7 \omega_{16} + 3\omega_7 v_2^2 + 9\omega_7 c_s^2 + 9c_s^2 \omega_{16} - 3\omega_{16} \\
C_3 &= 12\omega_{11}^2 + 18\omega_{11}^2 \omega_{18} c_s^2 + 3\omega_{11}^2 \omega_{18} \omega_6 + 36\omega_{18} \omega_6 c_s^2 - 18\omega_{11} \omega_{18} \omega_6 c_s^2 + 12\omega_{11}^2 v_3^2 \omega_6 - 3\omega_{11}^2 v_3^2 \omega_{18} \omega_6 + 36\omega_{11}^2 \omega_6 c_s^2 - 12\omega_{11}^2 \omega_6 - 12\omega_{11}^2 v_3^2 - \\
& 36\omega_{11}^2 c_s^2 + 12\omega_{11} \omega_6 - 12\omega_{11} v_3^2 \omega_6 - 36\omega_{11} \omega_6 c_s^2 - 6\omega_{11} v_3^2 \omega_{18} \omega_6 + 12v_3^2 \omega_{18} \omega_6 - 6\omega_{11}^2 \omega_{18} - 11\omega_{11}^2 \omega_{18} \omega_6 c_s^2 - 12\omega_{18} \omega_6 + 6\omega_{11} \omega_{18} \omega_6 + 6\omega_{11}^2 v_3^2 \omega_{18} \\
C_4 &= 6\omega_{11}^2 v_3^2 \omega_{19} - 6\omega_7 \omega_{11} v_3^2 \omega_{19} - 11\omega_7 \omega_{11}^2 \omega_{19} c_s^2 + 12\omega_{11}^2 + 6\omega_7 \omega_{11} \omega_{19} - 6\omega_{11}^2 \omega_{19} + 12\omega_7 v_3^2 \omega_{19} - 12\omega_{11}^2 v_3^2 - 12\omega_7 \omega_{11} v_3^2 - 36\omega_{11}^2 c_s^2 - \\
& 36\omega_7 \omega_{11} c_s^2 - 12\omega_7 \omega_{11}^2 v_3^2 + 36\omega_7 \omega_{11}^2 c_s^2 + 12\omega_7 \omega_{11}^2 v_3^2 - 12\omega_7 \omega_{19} + 36\omega_7 \omega_{19} c_s^2 + 3\omega_7 \omega_{11}^2 \omega_{19} - 3\omega_7 \omega_{11}^2 v_3^2 \omega_{19} + 12\omega_7 \omega_{11} + 18\omega_{11}^2 \omega_{19} c_s^2 - 18\omega_7 \omega_{11} \omega_{19} c_s^2 \\
C_5 &= -12\omega_{11} c_s^4 + 24\omega_{11}^2 v_3^2 c_s^2 - 36\omega_{11} v_3^4 - 12c_s^2 - 36v_3^2 - 7\omega_{11}^2 v_3^2 - \omega_{11}^2 c_s^2 + 12c_s^4 - 144\omega_{11} v_3^2 c_s^2 + 144v_3^2 c_s^2 + 36v_3^4 + 12\omega_{11} c_s^2 + 36\omega_{11} v_3^2 + 7\omega_{11}^2 v_3^4 + \omega_{11}^2 c_s^4
\end{aligned}$$

$$C_6 = -72\omega_{13}v_1^2\omega_6^3c_s^2 - 12\omega_{13}v_1^4\omega_6^2 - 216v_1^2\omega_6^2c_s^2 - 3\omega_{13}^2\omega_6^3c_s^4 - 36\omega_{13}v_1^2\omega_6c_s^2 - 6\omega_{13}\omega_6^3c_s^2 + 3\omega_{13}^2v_1^4\omega_6^3 + 12\omega_{13}\omega_6c_s^2 + 144\omega_{13}v_1^2\omega_6^2c_s^2 + 108v_1^2\omega_6^3c_s^2 + 72v_1^2\omega_6^2 + 30\omega_{13}v_1^2\omega_6^3 + 24\omega_{13}\omega_6c_s^4 + 24\omega_{13}\omega_6^2c_s^2 + 24\omega_{13}^2v_1^2\omega_6^2c_s^4 - 36v_1^2\omega_6^3 - 72\omega_{13}v_1^2\omega_6^2 + 6\omega_{13}^2v_1^2\omega_6^3c_s^2 - 24\omega_{13}\omega_6c_s^2 - 48\omega_{13}^2\omega_6c_s^4 - 3\omega_{13}^2v_1^2\omega_6^3 - 8\omega_{13}^2\omega_6^2c_s^2 + 72\omega_{13}v_1^2\omega_6c_s^2 + 12\omega_{13}^2v_1^2\omega_6^2 + 24\omega_{13}^2c_s^4 - 24\omega_{13}\omega_6^2c_s^4 - 12\omega_{13}^2v_1^2\omega_6^2c_s^2 + 72\omega_{13}v_1^2\omega_6^2 + 36v_1^4\omega_6^3 + 6\omega_{13}\omega_6^3c_s^4 - 30\omega_{13}v_1^4\omega_6^3 - 72v_1^4\omega_6^2 + \omega_{13}^2\omega_6^3c_s^2$$

$$C_8 = 72\omega_7^2 v_4^2 \omega_{16} + 24\omega_7^2 v_8^4 \omega_{16}^2 - 72\omega_7^2 v_2^2 c_s^2 \omega_{16} - 12\omega_7^2 v_2^2 c_s^2 \omega_{16}^2 - 24\omega_7^2 c_s^2 \omega_{16} + 30\omega_7^2 v_2^2 \omega_{16} + \omega_7^2 c_s^2 \omega_{16}^2 + 24c_s^4 \omega_{16}^2 + 72\omega_7^2 v_2^2 + 144\omega_7^2 v_2^2 c_s^2 \omega_{16} + 108\omega_7^2 v_2^2 c_s^2 + 12\omega_7^2 c_s^2 \omega_{16}^2 - 36\omega_7^2 v_2^2 - 6\omega_7^2 c_s^2 \omega_{16} - 3\omega_7^2 v_2^2 \omega_{16}^2 - 24\omega_7^2 c_s^4 \omega_{16} - 12\omega_7^2 v_2^2 \omega_{16}^2 + 6\omega_7^2 v_2^2 c_s^2 \omega_{16}^2 - 36\omega_7^2 v_2^2 c_s^2 \omega_{16}^2 - 8\omega_7^2 c_s^2 \omega_{16}^2 - 72\omega_7^2 v_2^2 \omega_{16} + 24\omega_7^2 c_s^4 \omega_{16} - 3\omega_7^2 c_s^4 \omega_{16}^2 + 36\omega_7^2 v_4^2 - 30\omega_7^2 v_4^2 \omega_{16} - 48\omega_7^2 c_s^4 \omega_{16}^2 + 3\omega_7^2 v_4^2 \omega_{16}^2 + 6\omega_7^2 c_s^4 \omega_{16} - 216\omega_7^2 v_2^2 c_s^2 + 12\omega_7^2 v_2^2 \omega_{16}^2 + 24\omega_7^2 c_s^2 \omega_{16} - 72\omega_7^2 v_4^2 + 72\omega_7^2 v_2^2 c_s^2 \omega_{16}$$

$$C_{10} = -54\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^2\omega_{22} + 12\omega_{13}\omega_{11}\omega_9\omega_6^3 + 12\omega_{13}\omega_3^2\omega_{22} - 12\omega_{13}\omega_{11}\omega_{18}\omega_6\omega_{22}c_s^2 + 6\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{22}c_s^2 - 6\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^3 + 18\omega_{13}\omega_{18}v_1^2\omega_6^3\omega_{22} - 36\omega_{13}v_1^2\omega_6^3\omega_{22} - 12\omega_{13}\omega_{11}\omega_9\omega_6^2 + 12\omega_{13}\omega_{11}\omega_6^2\omega_{22} - 18\omega_{13}\omega_{11}\omega_{18}v_1\omega_6\omega_{22} + 12\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^2 + 36\omega_{13}v_1^2\omega_9\omega_6^2 - 6\omega_{13}\omega_{18}\omega_9\omega_6^3c_s^2 + 12\omega_{13}\omega_{11}\omega_6^3\omega_{22}c_s^2 - 18\omega_{13}\omega_{18}v_1^2\omega_9\omega_6^2 + 12\omega_{13}\omega_9\omega_6^3c_s^2 - 36\omega_{13}\omega_{11}\omega_{18}v_1^2\omega_6\omega_{22} + 18\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^3\omega_{22} - 5\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{22}c_s^2 + 5\omega_{13}\omega_{11}\omega_{18}\omega_6^3\omega_{22} - 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22} - 12\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_{22}c_s^2 + 12\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}c_s^2 - 12\omega_{13}\omega_{11}\omega_3^2\omega_{22} - 12\omega_{13}\omega_9\omega_6^3 - 5\omega_{13}\omega_{11}\omega_{18}\omega_6^3\omega_{22}c_s^2 + 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22} - 6\omega_{13}\omega_{18}\omega_6^3\omega_{22} - 12\omega_{11}\omega_{18}\omega_9\omega_6^2 + 18\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6\omega_{22}c_s^2 + 36\omega_{13}\omega_{11}v_1^2\omega_9\omega_6^2 + 18\omega_{13}\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^3 + 6\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_3^2c_s^2 - 36\omega_{13}\omega_{11}v_1^2\omega_6^2\omega_{22} + 6\omega_{11}\omega_{18}\omega_9\omega_6^3 + 54\omega_{13}\omega_{11}\omega_{18}v_1^2\omega_6^2\omega_{22} + 12\omega_{11}\omega_{18}\omega_9\omega_6^3c_s^2 - 36\omega_{13}\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^2 - 36\omega_{13}\omega_{11}v_1^2\omega_9\omega_6^3 + 18\omega_{13}\omega_{18}\omega_6^2c_s^2 - 12\omega_{13}\omega_{11}\omega_9\omega_6^3c_s^2 - 12\omega_{13}\omega_6^3\omega_{22}c_s^2 - 18\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22}c_s^2 - 12\omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^2c_s^2 + 36\omega_{13}\omega_{11}v_1^2\omega_6^2\omega_{22} + 36\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^2 + 18\omega_{13}\omega_{11}\omega_{18}\omega_6^2\omega_{22}c_s^2 - 6\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22} + 12\omega_{13}\omega_{11}\omega_{18}\omega_6\omega_{22} - 12\omega_{13}\omega_{11}\omega_6^2\omega_{22}c_s^2 - 3\omega_{13}\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^2\omega_{22} + 36\omega_{11}\omega_{18}v_1^2\omega_9\omega_6\omega_{22} - 6\omega_{11}\omega_{18}\omega_9\omega_6^3c_s^2 - 18\omega_{11}\omega_{18}v_1^2\omega_9\omega_6^2 - 15\omega_{13}\omega_{11}\omega_{18}v_1^2\omega_3^2\omega_{22} + 12\omega_{13}\omega_{11}\omega_9\omega_6^2c_s^2 + \omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^3\omega_{22}c_s^2 + \omega_{13}\omega_{11}\omega_{18}\omega_9\omega_6^2\omega_{22} + 6\omega_{13}\omega_{18}\omega_9\omega_6^3$$

2w13w7w1w11w14w8v2v3w22w19 + 2w13w7w20w11v3w18w6w22w19c_s^2 + 2w13w7w20w11v2v3w18w6w22w19 - w7w20w11w14w8v2w18w6w22w19c_s^2 + 2w13w7w20w14w8v2v3w6w22w19c_s^2 + 2w13w7w20w14w8v2w18v1w6w22w19c_s^2 - w13w20w11w14w8v2w18w6w22w19c_s^2 + 2w13w7w1w11w14w8v2v3w18w6w22c_s^2 - w13w7w20w11w14w8v2w18w6w19c_s^2 - w13w7w20w11w14w8v2v3w18w6w22c_s^2 - 4w13w7w11w14v2v3w18v1w6w22w19 + 4w13w7w11w14w8v2v3w18v1w6w22w19c_s^2 - 2w13w7w20w14w8v2v3w6w19c_s^2 + 2w13w7w14w8v2v3w18w6w22w19c_s^2 + w13w20w11w8v2v3w18w6w22w19 + 4w13w7w11w14w8v2v3w18v1w6w22w19 + 4w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 4w13w11w14w8v2w18v1w6w22c_s^2 - 2w7w20w11w14w8v2v3w18w19c_s^2 + 4w13w7w11w14v2v3w18v1w22w19 + 2w13w7w20w14w8v2v3w18v1w6w22w19 + 4w7w20w11w8v2w18v1w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22 + 2w13w7w11w14v2v3w18v1w6w22w19c_s^2 + 4w13w7w11w14w8v2v3w18v1w6w22w19 - 4w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - 2w13w7w20w11w14w8v2w18v1w6w22c_s^2 + 4w13w7w20w11w14w8v2v3w18v1w6w22w19 + 2w13w7w20w11w14v2v3w18v1w6w22w19c_s^2 - 2w13w7w20w14w8v2v3w18v1w6w22w19 + 4w13w7w14w8v2w18v1w6w22c_s^2 + w13w20w11w14w8v2w18w6w22c_s^2 + w7w20w11w14w8v2v3w18w6w19c_s^2 + 4w13w7w20w11w14w8v2w18v1w22w19c_s^2 + 2w13w11w14w8v2v3w18w6w22w19c_s^2 + w7w20w11w14w8v2v3w18w6w22w19c_s^2 - 2w13w7w20w11w8v2v3w18w6w22w19c_s^2 - 2w13w7w11w14w8v2v3w18w6w22w19 + 2w13w7w11w14w8v2v3w18w22w19c_s^2 - 2w13w7w11w14w8v2v3w18w6w22w19c_s^2 - 2w13w7w14w8v2v3w18w6w22c_s^2 + 2w13w7w20w11w14v2v3w18w22w19 + 2w13w7w11w14w8v2v3w18w22w19c_s^2 - 2w13w7w11w14w8v2v3w18w6w22w19c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19c_s^2 + 4w13w7w11w14w8v2v3w18v1w6w22 + 4w13w20w11v2v3w18v1w6w22w19 - w13w7w20w14w8v2v3w18w6w22w19 - 2w13w7w20w11w14w8v2v3w6w22w19c_s^2 + 2w13w7w11w14w8v2v3w6w22w19c_s^2 - 2w13w7w11w14w8v2v3w18w6w22w19 + 4w13w7w20w11v2v3w18v1w6w22w19 + 4w13w7w20w11v2w18v1w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19 - w7w20w11w14w8v2v3w18w6w22 - 2w13w7w20w11w14v2v3w18v1w6w22w19c_s^2 + 4w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - w13w7w20w11w8v2v3w18w6w22w19c_s^2 + 4w7w20w11w14w8v2w18v1w19c_s^2 + 4w13w20w11w14v2w18v1w6w22w19c_s^2 - 2w13w7w14w8v2v3w18w6w22w19 - 4w13w7w20w11w14v2v3w18v1w6w22w19 + 2w13w7w20w11w14v2v3w18w22w19c_s^2 + w7w20w11w14w8v2v3w18w6w19c_s^2 + 2w13w7w20w11w8v2v3w18w22w19 + 4w13w11w14v2v3w18v1w6w22w19 - 2w13w7w20w14w8v2w18v1w6w22c_s^2 + 4w13w7w20w11w8v2v3w18w6w22w19c_s^2 - w13w7w20w11w14w8v2v3w18w6w22w19 - w13w7w20w14w8v2v3w18w6w22c_s^2 + 2w7w20w11w14w8v2w18v1w6w22w19c_s^2 + 4w7w20w11w14w8v2w18v1w22w19c_s^2 - 2w13w11w14v2v3w18w6w22w19c_s^2 + 2w13w7w20w11w8v2v3w18v1w6w22w19 - 2w13w11w14w8v2v3w18w6w22w19 - w7w20w11w14w8v2v3w18w6w22w19c_s^2 - 4w13w7w11w14w8v2w18v1w6w22c_s^2 - 2w13w7w14w8v2v3w18w6w22c_s^2 + 2w7w20w11w14w8v2w18v1w6w22w19c_s^2 + 4w7w20w11w14w8v2w18v1w22w19c_s^2 - 2w13w11w14v2v3w18w6w22w19c_s^2 + 2w13w7w20w11w8v2v3w18v1w6w22w19 - 2w13w11w14w8v2v3w18w6w22w19 - w13w7w20w14w8v2v3w18w6w22w19c_s^2 + w13w7w20w14w8v2v3w18w6w22c_s^2 - 2w13w7w11w14v2v3w18w22w19 - w13w20w11w14w8v2v3w18w6w22w19 + 2w13w20w11w14v2v3w18w6w22w19c_s^2 + 2w13w7w20w11v2v3w18w6w22w19c_s^2 - 2w13w7w11w14v2v3w18w22w19c_s^2 - 4w13w7w20w11w14w8v2v3v1w6w19 - 2w13w20w11w8v2w18v1w6w22w19c_s^2 - 4w13w7w20w11w14v2w18v1w6w22w19c_s^2 - 4w13w7w20w11w14w8v2v3w18v1w6w22w19 + 2w13w20w11w14w8v2v3w18v1w6w22w19 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 2w7w20w11w14w8v2v3w18v1w6w22w19 - 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 2w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - 2w13w7w11w14w8v2v3w18w6w22w19c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19c_s^2 - w13w7w20w11w14w8v2v3w18w6w22c_s^2 - w13w7w20w11w14w8v2v3w18w6w22c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19 + w13w7w20w11w14w8v2v3w18w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - 4w13w7w20w11w14w8v2v3w18v1w6w22w19 + w13w7w20w14w8v2v3w18w6w22c_s^2 - 2w7w20w11w14w8v2v3w18w6w22w19 - w13w20w11w14w8v2v3w18w6w22w19 + 2w13w20w11w14w8v2v3w18w6w22w19c_s^2 - 4w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19c_s^2 + 2w13w7w20w11w14w8v2v3w18v1w6w22w19c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19c_s^2 - 2w13w7w20w11w14w8v2v3w18w6w22w19

$$\begin{aligned}
& 21w_{13}w_{17}^2w_{11}w_{14}w_8w_5w_{18}v_1^2w_3^2w_{22}w_{19}c_s^2 - 12w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2w_5w_{18}v_1w_3^2w_{22}w_{19}c_s^2 + 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2w_5v_1w_3^6w_{19}c_s^2 - \\
& 12w_{13}w_{17}^2w_{11}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^2w_{22} - 12w_{13}w_{17}w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} - 6w_{13}w_{17}^2w_{20}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^6w_{22} + \\
& 21w_{13}w_{17}^2w_{14}w_8w_5v_1^2w_3^6w_{22}w_{19}c_s^2 + 12w_{17}^2w_{20}w_{11}w_8v_2w_5w_{18}v_1w_3^6w_{22}w_{19}c_s^2 - 12w_{13}w_{17}^2w_{20}w_{11}w_{14}v_3^2w_5w_{18}w_3^6w_{22}w_{19}c_s^2 + \\
& 24w_{13}w_{17}^2w_{11}w_{14}v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} + 12w_{17}^2w_{20}w_{11}w_{14}w_8v_2w_5w_{18}v_1w_3^6w_{22}w_{19}c_s^2 + 6w_{13}w_{17}w_{20}w_{11}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^6w_{22}w_{19} - \\
& 12w_{13}w_{17}^2w_{20}w_{14}w_8w_{18}w_3^6w_{22}w_{19}c_s^4 + 12w_{13}w_{17}w_{20}w_{11}w_{14}w_5w_{18}v_1^2w_3^6w_{22}w_{19}c_s^2 + 24w_{13}w_{17}^2w_{20}w_{14}w_8v_2w_5v_1w_3^6w_{22}w_{19}c_s^2 - \\
& 12w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8w_5w_{18}v_1^2w_3^6w_{22}c_s^4 - 24w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} - 12w_{13}w_{17}^2w_{11}w_{14}v_2^3w_5w_{18}v_1^2w_3^6w_{22}w_{19} - \\
& 12w_{17}^2w_{20}w_{11}w_8w_5w_{18}w_6^2w_{22}w_{19}c_s^4 + 6w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^6w_{22}w_{19} - 6w_{13}w_{17}^2w_{20}w_{11}w_8w_5w_{18}w_3^6w_{22}w_{19}c_s^4 + \\
& 12w_{17}^2w_{20}w_{11}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} + 12w_{13}w_{17}^2w_{11}w_{14}w_8v_2w_5w_{18}v_1^2w_3^6w_{22}c_s^2 + 24w_{13}w_{17}^2w_{11}w_{14}w_8v_2w_5v_1w_3^6w_{22}w_{19}c_s^2 - \\
& 12w_{13}w_{17}w_{20}w_{11}w_{14}w_8v_2w_5w_{18}v_1w_3^6w_{22}w_{19}c_s^2 + 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5v_1w_3^6w_{22}w_{19} - 24w_{13}w_{17}w_{11}w_{14}w_8v_2w_5w_{18}v_1w_3^6w_{22}c_s^2 + \\
& 12w_{17}^2w_{20}w_{11}w_{14}w_8w_5w_{18}v_1^2w_3^6w_{22}c_s^2 - 6w_{13}w_{17}^2w_{20}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^6w_{22}w_{19} - 24w_{13}w_{17}^2w_{20}w_{14}w_8v_2v_3^2w_5v_1w_3^6w_{22}w_{19} - \\
& 6w_{13}^2w_{20}w_{11}w_8v_2w_5w_{18}v_1w_3^6w_{22}w_{19}c_s^2 + 12w_{13}w_{17}^2w_{20}w_{11}w_{14}v_2^3w_5w_{18}v_1^2w_3^6w_{22}w_{19} - 6w_{13}w_{17}w_{20}w_{11}w_{14}w_8w_5w_{18}v_1^2w_3^6w_{22}c_s^2 - \\
& 6w_{13}w_{20}w_{11}w_{14}w_8w_5w_{18}w_3^6w_{22}w_{19}c_s^4 - 12w_{13}w_{17}w_{20}w_{11}w_{14}w_5w_{18}v_1^2w_3^6w_{22}w_{19}c_s^2 + 12w_{13}w_{17}^2w_{20}w_{14}w_8v_2w_5w_{18}v_1w_3^6w_{22}c_s^2 + \\
& 24w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} - 12w_{13}w_{17}^2w_{14}w_8w_5w_6^2w_{22}w_{19}c_s^4 - 24w_{13}w_{17}w_{20}w_{11}v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} - \\
& 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} - 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2w_5v_1w_3^6w_{22}w_{19}c_s^2 - 6w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^6w_{22}w_{19} - \\
& 24w_{13}w_{17}^2w_{20}w_{11}v_2w_5w_{18}v_1w_3^6w_{22}w_{19}c_s^2 + 12w_{13}w_{17}^2w_{20}w_{11}w_8w_5w_{18}w_3^6w_{22}w_{19}c_s^4 + 18w_{13}w_{17}w_{20}w_{11}w_{14}w_8w_{18}w_3^6w_{22}w_{19}c_s^4 + \\
& 12w_{13}w_{17}w_{20}w_{11}v_3^2w_5w_{18}w_3^6w_{22}w_{19}c_s^2 + 12w_{13}w_{17}^2w_{11}w_{14}w_8w_5w_{18}w_3^6w_{22}c_s^4 + 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8w_5w_{18}w_6w_{22}w_{19}c_s^4 - \\
& 24w_{13}w_{17}^2w_{20}w_{14}w_8v_2w_5v_1w_3^6w_{22}c_s^2 + 6w_{17}^2w_{20}w_{11}w_8w_5w_{18}w_3^6w_{22}w_{19}c_s^4 - 24w_{13}w_{17}^2w_{11}w_{14}v_2w_5w_{18}v_1w_3^6w_{22}w_{19}c_s^2 + \\
& 6w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2^3w_5w_{18}v_1^2w_3^6w_{22} - 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5v_1w_3^6w_{22}w_{19} - 12w_{17}^2w_{20}w_{11}w_{14}w_8v_2^3w_5w_{18}w_3^6w_{22}w_{19}c_s^2 + \\
& 12w_{13}w_{17}^2w_{20}w_{14}w_8w_5w_{18}w_3^6w_{22}w_{19}c_s^4 + 6w_{13}w_{17}w_{20}w_{11}w_{14}w_5w_{18}v_1^2w_3^6w_{22}w_{19}c_s^2 + 24w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1^2w_3^6w_{22}w_{19} - \\
& 18w_{13}w_{17}w_{20}w_{11}w_{14}w_8w_5w_{18}w_3^6w_{22}w_{19}c_s^4 + 6w_{13}w_{17}^2w_{20}w_{14}w_8v_2^3w_5w_{18}w_3^6w_{22}w_{19}c_s^2 + 24w_{13}w_{17}w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}w_{19} - \\
& 12w_{13}w_{17}^2w_{11}w_{14}w_5w_{18}w_3^6w_{22}w_{19}c_s^4 - 12w_{13}w_{17}^2w_{11}w_{14}w_8w_5w_{18}v_1^2w_3^6w_{22}w_{19}c_s^2 + 12w_{17}^2w_{20}w_{11}w_{14}w_8v_2^3w_5w_{18}w_3^6w_{22}w_{19}c_s^2 - \\
& 12w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22}c_s^2 - 12w_{13}w_{17}w_{11}w_{14}w_8w_5w_{18}w_3^6w_{22}c_s^4 + 12w_{13}w_{17}^2w_{20}w_{11}w_{14}w_8v_3^2w_5w_{18}w_3^6w_{22}w_{19}c_s^2 + \\
& 12w_{13}w_{17}^2w_{20}w_{14}w_8v_2v_3^2w_5w_{18}v_1w_3^6w_{22} + 12w_{13}w_{17}^2w_{11}w_{14}w_8v_2^3$$

[illegible]

$$\begin{aligned}
& 2w_7w_{23}w_{17}w_{18}w_{18}v_1^2w_6c_s^2w_{16} + 4w_{23}w_{20}w_{11}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16} + 2w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_3v_{17}w_{16}w_{19}c_s^2w_{16} + 2w_7w_{23}w_{20}w_{17}w_{18}w_{18}v_1^2w_6c_s^2w_{16} + \\
& 2w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2v_3v_{17}w_{16}w_{19}w_{16} - 2w_7w_{23}w_{17}w_{11}w_{18}v_1^2w_{19}c_s^2w_{16} - w_7w_{23}w_{20}w_{11}w_{18}v_2^2w_{18}v_{17}w_{16}w_{19}w_{16} - 2w_{23}w_{17}w_{11}w_{18}v_2^2w_{18}w_6c_s^2w_{16} + \\
& 2w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2w_{18}w_6c_s^2w_{16} + 4w_7w_{23}w_{20}w_{17}w_{11}v_2^2v_3w_{18}v_{17}w_{16}w_{19}w_{16} + w_7w_{23}w_{20}w_{11}w_{18}v_2^2w_{18}v_{17}w_{16}w_{19} + \\
& 2w_{23}w_{20}w_{11}w_{18}v_2^2w_{18}w_6w_{19}c_s^2w_{16} - 2w_{23}w_{20}w_{11}w_{18}v_2^2w_{18}w_6w_{19}c_s^2 + 2w_{20}w_{17}w_{11}w_{18}w_{18}v_2^2w_6w_{19}c_s^2w_{16} - 4w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{19} - \\
& 2w_{23}w_{20}w_{11}w_{18}v_2^2w_{16}w_{19}c_s^2w_{16} - 4w_7w_{23}w_{20}w_{17}w_{11}v_3w_{18}v_{17}w_{19}c_s^2w_{16} + 2w_7w_{23}w_{17}w_{11}w_{18}w_{18}v_2^2w_{19}c_s^2w_{16} - 2w_7w_{23}w_{17}w_{11}w_{18}v_2^2w_{19}c_s^2w_{16} + \\
& 2w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_1^2w_{19}c_s^2w_{16} + 2w_7w_{23}w_{17}w_{11}w_{18}w_{18}v_2^2w_6c_s^2w_{16} - w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2w_{18}v_{17}w_{19}w_{16} - 2w_7w_{20}w_{17}w_{18}w_{18}v_1^2w_6c_s^2w_{16} - \\
& 4w_7w_{23}w_{17}w_{11}w_{18}v_3w_{18}v_{17}w_{19}c_s^2w_{16} + 2w_7w_{23}w_{17}w_{11}w_{18}v_2^2w_{18}v_{17}w_{19}w_{16} - 2w_7w_{23}w_{20}w_{17}w_{11}w_{18}w_{18}v_2^2w_6c_s^2w_{16} - \\
& 2w_7w_{23}w_{17}w_{11}v_2^2w_{18}v_{17}w_{19}w_{16} - 4w_7w_{20}w_{17}w_{11}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{16} - 2w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16} + \\
& 4w_7w_{20}w_{17}w_{18}v_3w_{18}w_{17}w_6c_s^2w_{16} + 2w_7w_{23}w_{20}w_{17}w_{11}v_2^2w_{18}v_{17}w_{19}w_{16} - w_7w_{23}w_{20}w_{17}w_{11}w_{18}w_{18}v_2^2w_{17}w_{19}w_{16} + w_7w_{23}w_{20}w_{17}w_{11}w_{18}w_{18}v_2^2w_{17}w_{19}w_{16} + \\
& 4w_7w_{23}w_{20}w_{17}w_{11}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16} - 2w_7w_{23}w_{17}w_{11}w_{18}w_{18}v_2^2w_{16}w_{19}c_s^2w_{16} + w_7w_{20}w_{17}w_{18}w_{18}v_2^2w_{16}w_{19}c_s^2w_{16} - \\
& 2w_7w_{20}w_{17}w_{11}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{19} + 2w_7w_{23}w_{17}w_{11}w_{18}v_1^2w_{16}w_{19}c_s^2w_{16} + 2w_7w_{23}w_{17}w_{18}v_2^2w_{16}w_{19}w_{16} - \\
& w_7w_{23}w_{20}w_{17}w_{18}v_2^2w_{18}v_{17}w_{16}w_{19}w_{16} - 2w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2w_{16}w_{19}c_s^2w_{16} - 4w_{20}w_{17}w_{11}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{19}w_{16} + \\
& 2w_{23}w_{20}w_{17}w_{11}w_{18}w_{18}v_1^2w_{16}w_{19}c_s^2 + 4w_{23}w_{20}w_{11}v_2^2v_3w_{18}v_{17}w_{16}w_{19}w_{16} + w_7w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2w_{18}w_6w_{19}c_s^2w_{16} + \\
& 4w_{23}w_{17}w_{11}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{16} - 4w_{23}w_{20}w_{17}w_{11}w_{18}v_3w_{18}v_{17}w_{16}w_{19}c_s^2 + 4w_{20}w_{17}w_{11}w_{18}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16} - \\
& 4w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{16} + 4w_7w_{23}w_{17}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{16} + 2w_{23}w_{20}w_{17}w_{11}v_2^2w_{18}v_{17}w_{16}w_{19}w_{16} + 2w_7w_{23}w_{17}w_{11}v_2^2w_{18}w_6w_{19}c_s^2w_{16} + \\
& 4w_7w_{23}w_{17}w_{11}w_{18}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16} - 2w_{23}w_{17}w_{11}v_2^2w_{18}v_{17}w_{16}w_{19}w_{16} - 2w_7w_{23}w_{17}w_{11}w_{18}v_2^2w_{18}w_6w_{19}c_s^2w_{16} - \\
& 2w_7w_{20}w_{17}w_{18}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16} + w_7w_{20}w_{17}w_{18}v_2^2w_{18}w_6w_{19}c_s^2w_{16} - 2w_{23}w_{20}w_{17}w_{11}w_{18}v_2^2w_{18}v_{17}w_{16}w_{19}w_{16} + \\
& w_7w_{20}w_{17}w_{11}w_{18}w_{18}v_1^2w_{16}w_{19}c_s^2 + 2w_{23}w_{17}w_{11}w_{18}v_2^2w_{18}v_{17}w_{16}w_{19}w_{16} - 2w_7w_{23}w_{20}w_{17}w_{11}v_2^2w_{18}w_6w_{19}c_s^2w_{16} + \\
& w_7w_{23}w_{20}w_{17}w_{11}w_{18}w_{18}v_1^2w_{16}w_{19}c_s^2w_{16} - 4w_7w_{23}w_{20}w_{17}w_{18}v_2^2v_3w_{18}v_{17}w_{16}w_{16} - 4w_7w_{23}w_{17}w_{11}v_3w_{18}v_{17}w_{16}w_{19}c_s^2w_{16}
\end{aligned}$$

$$C_{20} = -36\omega_7^2 \omega_{23} \omega_{11} v_{2w}^2 \omega_{16} + 12\omega_7^3 c_{2w}^2 \omega_{16} \omega_{10} + 5\omega_7^3 \omega_{23} \omega_{11} \omega_{19} \omega_{16} - 6\omega_7^3 \omega_{11} \omega_{19} \omega_{16} \omega_{10} + 18\omega_7^3 \omega_{11} v_{2w}^2 \omega_{19} \omega_{16} \omega_{10} - 6\omega_7^3 \omega_{23} \omega_{11} \omega_{19} \omega_{10} - 12\omega_7^2 \omega_{11} \omega_{19} \omega_{10} + 18\omega_7 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} \omega_{10} + 12\omega_7^2 \omega_{23} \omega_{11} \omega_{16} + 18\omega_7^3 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{10} + 12\omega_7^3 \omega_{11} \omega_{16} \omega_{10} - 36\omega_7^2 \omega_{23} v_{2w}^2 \omega_{16} - 5\omega_7^3 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} + 36\omega_7^2 \omega_{11} v_{2w}^2 \omega_{19} \omega_{10} + 12\omega_7^3 \omega_{23} \omega_{16} + 12\omega_7^2 \omega_{11} \omega_{19} c_s^2 \omega_{10} + 6\omega_7^3 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{10} + 6\omega_7^3 \omega_{11} \omega_{19} c_s^2 \omega_{16} \omega_{10} - 15\omega_7^2 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{16} - 12\omega_7^2 \omega_{11} \omega_{16} \omega_{10} - 12\omega_7^3 \omega_{23} \omega_{11} \omega_{16} - 12\omega_7^3 \omega_{11} c_s^2 \omega_{16} \omega_{10} + 6\omega_7^3 \omega_{19} \omega_{16} \omega_{10} - 12\omega_7^2 \omega_{11} v_{2w}^2 c_s^2 \omega_{16} + 36\omega_7^2 \omega_{11} v_{2w}^2 \omega_{16} \omega_{10} + 6\omega_7^2 \omega_{11} \omega_{19} \omega_{10} - 12\omega_7^2 \omega_{23} \omega_{11} c_s^2 \omega_{16} + \omega_7^2 \omega_{23} \omega_{11} \omega_{19} \omega_{16} \omega_{10} - 12\omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} \omega_{10} - \omega_7^2 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} \omega_{10} + 54\omega_7^2 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{16} - 12\omega_7^2 \omega_{11} c_s^2 \omega_{16} \omega_{10} - 18\omega_7^2 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{10} + 12\omega_7^2 \omega_{11} c_s^2 \omega_{16} \omega_{10} - 18\omega_7^3 v_{2w}^2 \omega_{19} \omega_{16} \omega_{10} + 18\omega_7^2 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} + 54\omega_7^2 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{10} - 36\omega_7^2 \omega_{11} v_{2w}^2 \omega_{19} \omega_{16} \omega_{10} + 12\omega_7^2 \omega_{23} \omega_{11} c_s^2 \omega_{16} - 36\omega_7^2 \omega_{11} v_{2w}^2 \omega_{16} \omega_{10} - 6\omega_7^3 \omega_{19} c_s^2 \omega_{16} \omega_{10} - 3\omega_7^2 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{16} \omega_{10} + 18\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \omega_{10} + 12\omega_7^2 \omega_{11} \omega_{19} \omega_{16} \omega_{10} + 18\omega_7^3 \omega_{23} v_{2w}^2 \omega_{19} \omega_{16} + 36\omega_7^3 \omega_{23} \omega_{11} v_{2w}^2 \omega_{16} - 18\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \omega_{16} + 6\omega_7^3 \omega_{23} \omega_{19} c_s^2 \omega_{16} - 6\omega_7^3 \omega_{11} \omega_{19} c_s^2 \omega_{10} + 12\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \omega_{16} + 36\omega_7^2 v_{2w}^2 \omega_{16} \omega_{10} - 5\omega_7^2 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} \omega_{10} - 36\omega_7^2 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{16} + 12\omega_7^2 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{10} - 12\omega_7^2 \omega_{23} \omega_{11} \omega_{19} \omega_{10} - 18\omega_7^3 \omega_{11} v_{2w}^2 \omega_{19} \omega_{10} - 6\omega_7^3 \omega_{23} \omega_{19} \omega_{16} - 12\omega_7 \omega_{23} \omega_{11} \omega_{19} c_s^2 \omega_{16} + 36\omega_7 \omega_{23} \omega_{11} v_{2w}^2 \omega_{19} \omega_{10}$$

$$C_{22} = 18\omega_{13}v_3^2\omega_{18}\omega_6^3\omega_{22} - 12\omega_{13}\omega_{18}\omega_6^2\omega_{22}c_s^2 - 18\omega_{11}^2v_3^2\omega_{18}\omega_6^3 - 12\omega_{13}\omega_{11}\omega_{18}\omega_6\omega_{22}c_s^2 - 12\omega_{13}\omega_{11}^2\omega_6\omega_{22} + 6\omega_{11}\omega_{18}\omega_6^3\omega_{22}c_s^2 + 12\omega_{13}\omega_{11}^2\omega_{18}\omega_6^2 + 12\omega_{13}\omega_{11}^2\omega_6^3 - 18\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_6^3 + 12\omega_{11}^2v_3\omega_{18}\omega_6^2c_s^2 - 12\omega_{13}\omega_{11}\omega_6^2\omega_{22} + 36\omega_{11}^2v_3^2\omega_{18}\omega_6^2 + 18\omega_{13}\omega_{11}^2\omega_{18}\omega_6\omega_{22}c_s^2 - 12\omega_{13}\omega_{11}^2\omega_6^2 - 6\omega_{13}\omega_{11}^2\omega_{18}\omega_6^3 + 36\omega_{13}\omega_{11}^2v_3^2\omega_6^3\omega_{22} - 24\omega_{13}\omega_{11}\omega_{18}\omega_6^2\omega_{22} - 12\omega_{13}\omega_{11}^2\omega_{18}\omega_{22}c_s^2 + 12\omega_{13}\omega_{11}\omega_6^3c_s^2 - 12\omega_{11}^2\omega_{18}\omega_6^2 - \omega_{13}\omega_{11}^2\omega_{18}\omega_6^3\omega_{22}c_s^2 - 12\omega_{13}\omega_{11}\omega_6^3\omega_{22}c_s^2 -$$

$$\begin{aligned}
& 6\omega_{13}\omega_{11}\omega_{18}\omega_6^2c_s^2 - 36\omega_{13}v_3^2\omega_{18}\omega_6^2\omega_{22} - 36\omega_{13}\omega_{11}^2v_3^2\omega_6^2 + 6\omega_{13}\omega_{11}\omega_{18}\omega_6^2\omega_{22} - 72\omega_{13}\omega_{11}^2v_3^2\omega_6^2\omega_{22} + 6\omega_{11}^2\omega_{18}\omega_6^2 - 6\omega_{11}^2\omega_{18}\omega_6^2c_s^2 + \\
& 12\omega_{13}\omega_{11}\omega_6^2\omega_{22} + 36\omega_{13}\omega_{11}^2v_3^2\omega_6^2 - 36\omega_{13}\omega_{11}v_3^2\omega_{18}\omega_6\omega_{22} - 24\omega_{13}\omega_{11}^2v_3^2\omega_6^2\omega_{22}c_s^2 - 6\omega_{13}\omega_{11}\omega_{18}\omega_6^2\omega_{22}c_s^2 + 12\omega_{11}\omega_{18}\omega_6^2\omega_{22} - 6\omega_{13}\omega_{18}\omega_6^2\omega_{22} + \\
& 36\omega_{13}\omega_{11}^2v_3^2\omega_6\omega_{22} - 12\omega_{13}\omega_{11}^2\omega_6^2c_s^2 - 12\omega_{13}\omega_{11}^2\omega_{18}\omega_6^2c_s^2 + 12\omega_{13}\omega_{11}^2v_3^2\omega_{18}\omega_6^2\omega_{22} + 36\omega_{13}\omega_{11}^2v_3^2\omega_6^2 - 36\omega_{13}\omega_{11}^2v_3^2\omega_{18}\omega_6^2 - 36\omega_{13}\omega_{11}v_3^2\omega_6^2\omega_{22} + \\
& 12\omega_{13}\omega_{11}^2\omega_6\omega_{22}c_s^2 + 6\omega_{13}\omega_{18}\omega_6^2\omega_{22}c_s^2 + 18\omega_{11}^2v_3^2\omega_{18}\omega_6^2\omega_{22} - 12\omega_{13}\omega_{11}^2\omega_6^2\omega_{22} + 18\omega_{13}\omega_{11}^2v_3^2\omega_{18}\omega_6^2 - 12\omega_{11}\omega_{18}\omega_6^2\omega_{22}c_s^2 + 24\omega_{13}\omega_{11}\omega_{18}\omega_6^2\omega_{22}c_s^2 + \\
& 6\omega_{13}\omega_{11}^2\omega_{18}\omega_6^2c_s^2 - 18\omega_{13}\omega_{11}^2v_3^2\omega_{18}\omega_6^2\omega_{22} + 12\omega_{13}\omega_{11}\omega_6^2\omega_{22}c_s^2 + 12\omega_{13}\omega_{11}^2\omega_6^2c_s^2 - 6\omega_{11}\omega_{18}\omega_6^2\omega_{22} + 12\omega_{13}\omega_{11}\omega_{18}\omega_6\omega_{22} + 12\omega_{13}\omega_{11}\omega_{18}\omega_6^2\omega_{22} + \\
& 24\omega_{13}\omega_{11}^2\omega_6^2\omega_{22} - 36\omega_{11}v_3^2\omega_{18}\omega_6^2\omega_{22} + 12\omega_{13}\omega_{11}\omega_6^2\omega_{22}c_s^2 + 6\omega_{13}\omega_{11}\omega_{18}\omega_6^2 + 36\omega_{13}\omega_{11}v_3^2\omega_6^2\omega_{22} - 4\omega_{13}\omega_{11}^2\omega_{18}\omega_6^2\omega_{22}c_s^2 - 12\omega_{13}\omega_{11}\omega_6^2
\end{aligned}$$

$$\begin{aligned} C_{24} = & -12\omega_7^3\omega_{11}^2c_s^2\omega_{16} - 12\omega_7^2\omega_{11}^3\omega_{19} - 12\omega_7^2\omega_{23}\omega_{19}c_s^2\omega_{16} - 4\omega_7^2\omega_{23}\omega_{11}^3\omega_{19}c_s^2\omega_{16} + 12\omega_7^2\omega_{23}\omega_{11}\omega_{19} - 36\omega_7^3\omega_{11}^2v_3^2\omega_{16} + 6\omega_7^3\omega_{23}\omega_{11}\omega_{19}\omega_{16} - \\ & - 18\omega_7^3\omega_{11}^2v_3^2\omega_{19}\omega_{16} - 36\omega_7\omega_{23}\omega_{11}^3v_3^2\omega_{19}\omega_{16} - 18\omega_7^2\omega_{11}^3v_3^2\omega_{19} - 12\omega_7^2\omega_{23}\omega_{11}\omega_{16} - 6\omega_7^2\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16} - 12\omega_7^2\omega_{11}^3\omega_{16} + 18\omega_7^3\omega_{23}v_3^2\omega_{19}\omega_{16} + \\ & + 36\omega_7^2\omega_{11}^3v_3^2\omega_{19} + 12\omega_7^3\omega_{23}\omega_{11}\omega_{16} - 12\omega_7^2\omega_{11}^3\omega_{19}c_s^2\omega_{16} - 36\omega_7^2\omega_{11}^3v_3^2\omega_{19}\omega_{16} - 12\omega_7\omega_{23}\omega_{11}^3\omega_{16} - 36\omega_7^2\omega_{23}\omega_{11}^3v_3^2\omega_{19} + 6\omega_7^3\omega_{11}\omega_{19}\omega_{16} + \\ & + 18\omega_7\omega_{23}\omega_{11}^3\omega_{19}c_s^2\omega_{16} - 6\omega_7^3\omega_{23}\omega_{11}\omega_{19} + 36\omega_7^2\omega_{11}^3v_3^2\omega_{16} + 36\omega_7^2\omega_{23}\omega_{11}^3v_3^2\omega_{16} + 12\omega_7^2\omega_{11}^3c_s^2\omega_{16} + 6\omega_7^3\omega_{11}^3\omega_{19}c_s^2\omega_{16} + 12\omega_7^3\omega_{23}\omega_{11}^3c_s^2\omega_{16} + \\ & + 36\omega_7^2\omega_{23}\omega_{11}^3v_3^2\omega_{16} + 6\omega_7^3\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16} + 12\omega_7^2\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16} + 72\omega_7^2\omega_{23}\omega_{11}^3v_3^2\omega_{19}\omega_{16} - 12\omega_7^3\omega_{11}\omega_{16} + 18\omega_7^3\omega_{23}\omega_{11}^3v_3^2\omega_{19} + \\ & + 12\omega_7\omega_{23}\omega_{11}^3c_s^2\omega_{16} + 18\omega_7^3\omega_{11}^3v_3^2\omega_{19}\omega_{16} + 36\omega_7\omega_{23}\omega_{11}^3v_3^2\omega_{16} + 12\omega_7^2\omega_{23}\omega_{19}\omega_{16} + 12\omega_7^3\omega_{11}^3\omega_{16} + 24\omega_7^2\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16} - 12\omega_7^3\omega_{23}\omega_{11}c_s^2\omega_{16} - \\ & - 36\omega_7^2\omega_{23}\omega_{11}^3v_3^2\omega_{16} - 12\omega_7^2\omega_{23}\omega_{11}^3\omega_{16} - 6\omega_7^3\omega_{11}^3\omega_{19}\omega_{16} - 12\omega_7^2\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16} - \omega_7^3\omega_{23}\omega_{11}^3\omega_{19}c_s^2\omega_{16} - 24\omega_7^2\omega_{23}\omega_{11}^3c_s^2\omega_{16} - 12\omega_7^2\omega_{11}^3\omega_{19}c_s^2\omega_{16} + \\ & + 6\omega_7^3\omega_{11}^3\omega_{19} + 12\omega_7^2\omega_{11}^3\omega_{19}c_s^2\omega_{16} - 72\omega_7^2\omega_{23}\omega_{11}^3v_3^2\omega_{16} + 12\omega_7^2\omega_{11}^3\omega_{19}\omega_{16} + 24\omega_7^2\omega_{23}\omega_{11}^3\omega_{16} + 36\omega_7^3\omega_{11}^3v_3^2\omega_{16} + 12\omega_7^3\omega_{11}^3c_s^2\omega_{16} - \\ & - 18\omega_7^3\omega_{23}\omega_{11}^3v_3^2\omega_{19}\omega_{16} - 6\omega_7^3\omega_{11}^3\omega_{19}c_s^2\omega_{16} - 24\omega_7^2\omega_{23}\omega_{11}\omega_{19}\omega_{16} + 6\omega_7^2\omega_{23}\omega_{19}c_s^2\omega_{16} - 36\omega_7^2\omega_{23}v_3^2\omega_{19}\omega_{16} + 12\omega_7\omega_{23}\omega_{11}\omega_{19}\omega_{16} - \\ & - 6\omega_7^3\omega_{11}\omega_{19}c_s^2\omega_{16} - 6\omega_7^3\omega_{23}\omega_{19}\omega_{16} - 12\omega_7\omega_{23}\omega_{11}\omega_{19}c_s^2\omega_{16} \end{aligned}$$

$$\begin{aligned}
C_{26} = & -6\omega_7^3\omega_{11}\omega_{19}c_4^4 + 36\omega_7^2\omega_{11}^3v_3 + 18\omega_7^2\omega_{11}\omega_{19}c_8^2 + 60\omega_7^2\omega_{11}^3v_3\omega_{19}c_8^2 - 72\omega_7^2\omega_{11}^3v_3\omega_{19} + 36\omega_7^2\omega_{11}^3v_3\omega_{19}c_8^2 - 6\omega_7^2\omega_{11}^3v_3^4\omega_{19} - 12\omega_7^2\omega_{11}\omega_{19}c_8^4 - \\
& -\omega_7^2\omega_{11}\omega_{19}c_8^2 - 39\omega_7^2\omega_{11}^3v_3^4\omega_{19} - 36\omega_7^2\omega_{11}^3v_3^4 + 13\omega_7^2\omega_{11}^3\omega_{19}c_8^4 - 72\omega_7^2v_3^4\omega_{19} - 90\omega_7^2\omega_{11}^3v_3^4\omega_{19} + 4\omega_7^2\omega_{11}^3v_3^4\omega_{19} - 12\omega_7^2\omega_{11}\omega_{19}c_8^2 + 54\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 + \\
& + 12\omega_7^2\omega_{11}\omega_{19}c_8^4 - 36\omega_7^2\omega_{11}^3v_3^4\omega_{19} - 36\omega_7^2\omega_{11}\omega_{19}c_8^2 - 19\omega_7^2\omega_{11}^3v_3^4\omega_{19} - \omega_7^2\omega_{11}^3\omega_{19}c_8^4 + 36\omega_7^2\omega_{11}^3v_3^4\omega_{19} - 12\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 - 6\omega_7^2\omega_{11}^3\omega_{19}c_8^4 - \\
& - 6\omega_7^2\omega_{11}\omega_{19}c_8^2 + 12\omega_7^2\omega_{11}\omega_{19}c_8^4 - 108\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 + 12\omega_7^2\omega_{11}^3\omega_{19}c_8^4 + 36\omega_7^2\omega_{11}^3v_3^4 + 6\omega_7\omega_{11}^3\omega_{19}c_8^2 - 108\omega_7^2\omega_{11}^3v_3^4c_8^2 + 36\omega_7\omega_{11}^3v_3^4\omega_{19}c_8^2 - \\
& + 12\omega_7^3\omega_{11}^3v_3^4\omega_{19}c_8^2 + 72\omega_7^2\omega_{11}^3v_3^4\omega_{19} + 6\omega_7^2\omega_{11}^3\omega_{19}c_8^4 + 12\omega_7^3\omega_{19}c_8^2 - 306\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 + 6\omega_7^2\omega_{11}^3v_3^4\omega_{19} + 39\omega_7^3\omega_{11}^3v_3^4\omega_{19} - 18\omega_7^3\omega_{11}^3v_3^4\omega_{19}c_8^2 + \\
& + 12\omega_7^2\omega_{11}\omega_{19}c_8^2 - 12\omega_7\omega_{11}\omega_{19}c_8^2 + 90\omega_7^2\omega_{11}^3v_3^4\omega_{19} + 72\omega_7^3v_3^4\omega_{19} - 99\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 - 3\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 - 24\omega_7\omega_{11}^3\omega_{19}c_8^4 - 108\omega_7^2\omega_{11}^3v_3^4c_8^2 + \\
& - 6\omega_7^3\omega_{19}c_8^4 - 12\omega_7^2\omega_{11}\omega_{19}c_8^2 - 36\omega_7^2\omega_{11}^3v_3^4 + 108\omega_7^3\omega_{11}^3v_3^4c_8^2 + 18\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 + 252\omega_7^3v_3^4\omega_{19}c_8^2 + 6\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 - 36\omega_7^2\omega_{11}^3v_3^4 + 18\omega_7^2\omega_{11}\omega_{19}c_8^4 - \\
& - 4\omega_7^3\omega_{11}^3v_3^4\omega_{19} + \omega_7^2\omega_{11}^3\omega_{19}c_8^4 + 36\omega_7^2\omega_{11}^3v_3^4 - 5\omega_7^2\omega_{11}^3\omega_{19}c_8^2 + 36\omega_7^2\omega_{11}^3v_3^4\omega_{19} + 198\omega_7^2\omega_{11}^3v_3^4\omega_{19}c_8^2 + 19\omega_7^2\omega_{11}^3v_3^4\omega_{19} - 36\omega_7^2\omega_{11}^3v_3^4\omega_{19} + 12\omega_7^2\omega_{11}\omega_{19}c_8^2
\end{aligned}$$

2.6 CuLBM1

2.6.1 Definitions

Based on [2], collision operator \mathcal{C} :

$$\mathcal{C}(\mathbf{f}) = \mathbf{M}^{-1} \mathbf{G}^{-1} \left(\mathbf{S} \left(\gamma^{(eq)} - \mathbf{G}(\mathbf{M}\mathbf{f}) \right) \right),$$

where

$$\mathbf{S} = \text{diag}(0, 0, 0, 0, \omega_1, \omega_2, \omega_3, \omega_4, \omega_5, \omega_6, \omega_7, \omega_8, \omega_9, \omega_{10}, \omega_{11}, \omega_{12}, \omega_{13}, \omega_{14}, \omega_{15}, \omega_{16}, \omega_{17}, \omega_{18}, \omega_{19}, \omega_{20}, \omega_{21}, \omega_{22}, \omega_{23}),$$

$$\omega_1, \omega_2, \dots, \omega_{10} \in (0, 2).$$

The nonlinear operator \mathbf{G} (with its inverse \mathbf{G}^{-1}) transforms the raw moment vector $\boldsymbol{\mu}$ defined by matrix \mathbf{M} to the cumulant vector

$$\boldsymbol{\gamma} = \mathbf{G}(\boldsymbol{\mu}) = \left(\gamma_{(0,0,0)}, \gamma_{(1,0,0)}, \gamma_{(0,1,0)}, \dots, \gamma_{(2,2,2)} \right)^T$$

as:

$$\gamma_{(0,0,0)} = m_{(0,0,0)}$$

$$\gamma_{(1,0,0)} = m_{(1,0,0)} - v_1 m_{(0,0,0)}$$

$$\gamma_{(0,1,0)} = m_{(0,1,0)} - v_2 m_{(0,0,0)}$$

$$\gamma_{(0,0,1)} = m_{(0,0,1)} - v_3 m_{(0,0,0)}$$

$$\gamma_{(1,1,0)} = m_{(1,1,0)} - v_1 m_{(0,1,0)} - v_2 m_{(1,0,0)} - v_1 v_2 m_{(0,0,0)}$$

$$\gamma_{(1,0,1)} = m_{(1,0,1)} - v_1 m_{(0,0,1)} - v_3 m_{(1,0,0)} - v_1 v_3 m_{(0,0,0)}$$

$$\gamma_{(0,1,1)} = m_{(0,1,1)} - v_3 m_{(0,1,0)} - v_2 m_{(0,0,1)} - v_3 v_2 m_{(0,0,0)}$$

$$\gamma_{(2,0,0)} = m_{(2,0,0)} - 2v_1 m_{(1,0,0)} + v_1 v_1 m_{(0,0,0)}$$

$$\gamma_{(0,2,0)} = m_{(0,2,0)} - 2v_2 m_{(0,1,0)} + v_2 v_2 m_{(0,0,0)}$$

$$\gamma_{(0,0,2)} = m_{(0,0,2)} - 2v_3 m_{(0,0,1)} + v_3 v_3 m_{(0,0,0)}$$

$$\gamma_{(1,2,0)} = m_{(1,2,0)} - 2v_2 m_{(1,1,0)} + v_2 v_2 m_{(1,0,0)} - v_1 m_{(0,2,0)} + 2v_1 v_2 m_{(0,1,0)} - v_1 v_2 v_2 m_{(0,0,0)}$$

$$\gamma_{(1,0,2)} = m_{(1,0,2)} - 2v_3 m_{(1,0,1)} + v_3 v_3 m_{(1,0,0)} - v_1 m_{(0,0,2)} + 2v_1 v_3 m_{(0,0,1)} - v_1 v_3 v_3 m_{(0,0,0)}$$

$$\gamma_{(0,1,2)} = m_{(0,1,2)} - 2v_3 m_{(0,1,1)} + v_3 v_3 m_{(0,1,0)} - v_2 m_{(0,0,2)} + 2v_2 v_3 m_{(0,0,1)} - v_2 v_3 v_3 m_{(0,0,0)}$$

$$\gamma_{(2,1,0)} = m_{(2,1,0)} - 2v_1 m_{(1,1,0)} + v_1 v_1 m_{(0,1,0)} - v_2 m_{(2,0,0)} + 2v_1 v_2 m_{(1,0,0)} - v_1 v_1 v_2 m_{(0,0,0)}$$

$$\gamma_{(2,0,1)} = m_{(2,0,1)} - 2v_1 m_{(1,0,1)} + v_1 v_1 m_{(0,0,1)} - v_3 m_{(2,0,0)} + 2v_1 v_3 m_{(1,0,0)} - v_1 v_1 v_3 m_{(0,0,0)}$$

$$\gamma_{(0,2,1)} = m_{(0,2,1)} - 2v_2 m_{(0,1,1)} + v_2 v_2 m_{(0,0,1)} - v_3 m_{(0,2,0)} + 2v_2 v_3 m_{(0,1,0)} - v_2 v_2 v_3 m_{(0,0,0)}$$

$$\gamma_{(1,1,1)} = m_{(1,1,1)} - v_3 m_{(1,1,0)} - v_2 m_{(1,0,1)} + v_2 v_3 m_{(1,0,0)} - v_1 m_{(0,1,1)} + v_1 v_3 m_{(0,1,0)} + v_1 v_2 m_{(0,0,1)} - v_1 v_2 v_3 m_{(0,0,0)}$$

$$\gamma_{(2,2,0)} = -2v_2 m_{(2,1,0)} - 2m_{(0,0,0)} v_1^2 v_2^2 - 4m_{(1,0,0)} v_1 v_2^2 - \frac{2m_{(1,0,0)}^2 v_2^2}{m_{(0,0,0)}} - 4m_{(0,1,0)} v_1^2 v_2 + 8m_{(1,1,0)} v_1 v_2 -$$

$$\begin{aligned}
& \frac{8m_{(0,1,0)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} - \frac{2m_{(0,1,0)}^2v_1^2}{m_{(0,0,0)}} - 2m_{(1,2,0)}v_1 + \frac{4m_{(0,1,0)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,2,0)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,2,0)} - \frac{m_{(0,2,0)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{2m_{(1,1,0)}^2}{m_{(0,0,0)}} \\
\gamma_{(2,0,2)} = & -2v_3m_{(2,0,1)} - 2m_{(0,0,0)}v_1^2v_3^2 - 4m_{(1,0,0)}v_1v_3^2 - \frac{2m_{(1,0,0)}^2v_3^2}{m_{(0,0,0)}} - 4m_{(0,0,1)}v_1^2v_3 + 8m_{(1,0,1)}v_1v_3 - \\
& \frac{8m_{(0,0,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} + \frac{2m_{(0,0,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}} - \frac{2m_{(0,0,1)}^2v_1^2}{m_{(0,0,0)}} - 2m_{(1,0,2)}v_1 + \frac{4m_{(0,0,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,0,2)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,0,2)} - \frac{m_{(0,0,2)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,1)}^2}{m_{(0,0,0)}} \\
\gamma_{(0,2,2)} = & -2v_3m_{(0,2,1)} - 2m_{(0,0,0)}v_2^2v_3^2 - 4m_{(0,1,0)}v_2v_3^2 - \frac{2m_{(0,1,0)}^2v_3^2}{m_{(0,0,0)}} - 4m_{(0,0,1)}v_2^2v_3 + 8m_{(0,1,1)}v_2v_3 - \\
& \frac{8m_{(0,0,1)}m_{(0,1,0)}v_2v_3}{m_{(0,0,0)}} + \frac{2m_{(0,0,1)}m_{(0,2,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(0,1,1)}v_3}{m_{(0,0,0)}} - \frac{2m_{(0,0,1)}^2v_2^2}{m_{(0,0,0)}} - 2m_{(0,1,2)}v_2 + \frac{4m_{(0,0,1)}m_{(0,1,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,0,2)}m_{(0,1,0)}v_2}{m_{(0,0,0)}} + m_{(0,2,2)} - \frac{m_{(0,0,2)}m_{(0,2,0)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,1)}^2}{m_{(0,0,0)}} \\
\gamma_{(2,1,1)} = & -8m_{(1,0,0)}v_1v_2v_3 + 2m_{(2,0,0)}v_2v_3 - \frac{2m_{(1,0,0)}^2v_2v_3}{m_{(0,0,0)}} - 2m_{(0,1,0)}v_1^2v_3 + 4m_{(1,1,0)}v_1v_3 - \frac{4m_{(0,1,0)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} - \\
& m_{(2,1,0)}v_3 + \frac{m_{(0,1,0)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} - 2m_{(0,0,1)}v_1^2v_2 + 4m_{(1,0,1)}v_1v_2 - \frac{4m_{(0,0,1)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} - m_{(2,0,1)}v_2 + \\
& \frac{m_{(0,0,1)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} - \frac{2m_{(0,0,1)}m_{(0,1,0)}v_1^2}{m_{(0,0,0)}} - 2m_{(1,1,1)}v_1 + \frac{2m_{(0,0,1)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,1,1)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,1,1)} - \frac{m_{(0,1,1)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,1)}m_{(1,1,0)}}{m_{(0,0,0)}} \\
\gamma_{(1,2,1)} = & -2m_{(1,0,0)}v_2^2v_3 - 8m_{(0,1,0)}v_1v_2v_3 + 4m_{(1,1,0)}v_2v_3 - \frac{4m_{(0,1,0)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}} + 2m_{(0,2,0)}v_1v_3 - \\
& \frac{2m_{(0,1,0)}^2v_1v_3}{m_{(0,0,0)}} - m_{(1,2,0)}v_3 + \frac{2m_{(0,1,0)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} + \frac{m_{(0,2,0)}m_{(1,0,0)}v_3}{m_{(0,0,0)}} - 2m_{(0,0,1)}v_1v_2^2 - \frac{2m_{(0,0,1)}m_{(1,0,0)}v_2^2}{m_{(0,0,0)}} + 4m_{(0,1,1)}v_1v_2 - \\
& \frac{4m_{(0,0,1)}m_{(0,1,0)}v_1v_2}{m_{(0,0,0)}} - 2m_{(1,1,1)}v_2 + \frac{2m_{(0,0,1)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,1)}m_{(1,0,0)}v_2}{m_{(0,0,0)}} - m_{(0,2,1)}v_1 + \\
& \frac{m_{(0,0,1)}m_{(0,2,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(0,1,1)}v_1}{m_{(0,0,0)}} + m_{(1,2,1)} - \frac{2m_{(0,1,1)}m_{(1,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(1,0,1)}}{m_{(0,0,0)}} \\
\gamma_{(1,1,2)} = & -2m_{(1,0,0)}v_2v_3^2 - 2m_{(0,1,0)}v_1v_3^2 - \frac{2m_{(0,1,0)}m_{(1,0,0)}v_3^2}{m_{(0,0,0)}} - 8m_{(0,0,1)}v_1v_2v_3 + 4m_{(1,0,1)}v_2v_3 - \frac{4m_{(0,0,1)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}} + \\
& 4m_{(0,1,1)}v_1v_3 - \frac{4m_{(0,0,1)}m_{(0,1,0)}v_1v_3}{m_{(0,0,0)}} - 2m_{(1,1,1)}v_3 + \frac{2m_{(0,0,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,1,1)}m_{(1,0,0)}v_3}{m_{(0,0,0)}} + \\
& 2m_{(0,0,2)}v_1v_2 - \frac{2m_{(0,0,1)}^2v_1v_2}{m_{(0,0,0)}} - m_{(1,0,2)}v_2 + \frac{2m_{(0,0,1)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} + \frac{m_{(0,0,2)}m_{(1,0,0)}v_2}{m_{(0,0,0)}} - m_{(0,1,2)}v_1 + \frac{2m_{(0,0,1)}m_{(0,1,1)}v_1}{m_{(0,0,0)}} + \frac{m_{(0,0,2)}m_{(0,1,0)}v_1}{m_{(0,0,0)}} + m_{(1,1,2)} - \\
& \frac{m_{(0,0,2)}m_{(1,1,0)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,1)}m_{(1,0,1)}}{m_{(0,0,0)}} \\
\gamma_{(1,2,2)} = & -m_{(0,0,0)}v_1^2v_2^2v_3^2 - 6m_{(0,0,0)}v_1v_2^2v_3^2 - m_{(1,0,0)}v_2^2v_3^2 + 2m_{(0,1,0)}v_1v_2v_3^2 - 2m_{(1,1,0)}v_2v_3^2 + \\
& \frac{12m_{(0,1,0)}m_{(1,0,0)}v_2v_3^2}{m_{(0,0,0)}} - m_{(0,2,0)}v_1v_3^2 + \frac{6m_{(0,1,0)}^2v_1v_3^2}{m_{(0,0,0)}} - \frac{6m_{(0,1,0)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} - \frac{3m_{(0,2,0)}m_{(1,0,0)}v_3^2}{m_{(0,0,0)}} + 2m_{(0,0,1)}v_1v_2^2v_3 - \\
& 2m_{(1,0,1)}v_2^2v_3 + \frac{12m_{(0,0,1)}m_{(1,0,0)}v_2^2v_3}{m_{(0,0,0)}} - 12m_{(0,1,1)}v_1v_2v_3 + \frac{24m_{(0,0,1)}m_{(0,1,0)}v_1v_2v_3}{m_{(0,0,0)}} + 8m_{(1,1,1)}v_2v_3 - \frac{12m_{(0,0,1)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}} - \\
& \frac{12m_{(0,1,0)}m_{(1,0,1)}v_2v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,1)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}} + 4m_{(0,2,1)}v_1v_3 - \frac{6m_{(0,0,1)}m_{(0,2,0)}v_1v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,0)}m_{(0,1,1)}v_1v_3}{m_{(0,0,0)}} - 2m_{(1,2,1)}v_3 + \\
& \frac{2m_{(0,0,1)}m_{(1,2,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(1,1,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,2,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,2,1)}m_{(1,0,0)}v_3}{m_{(0,0,0)}} - m_{(0,0,2)}v_1v_2^2 + \\
& \frac{6m_{(0,0,1)}^2v_1v_2^2}{m_{(0,0,0)}} - \frac{6m_{(0,0,1)}m_{(1,0,1)}v_2^2}{m_{(0,0,0)}} - \frac{3m_{(0,0,2)}m_{(1,0,0)}v_2^2}{m_{(0,0,0)}} + 4m_{(0,1,2)}v_1v_2 - \frac{12m_{(0,0,1)}m_{(0,1,1)}v_1v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,2)}m_{(0,1,0)}v_1v_2}{m_{(0,0,0)}} - \\
& 2m_{(1,1,2)}v_2 + \frac{4m_{(0,0,1)}m_{(1,1,1)}v_2}{m_{(0,0,0)}} + \frac{4m_{(0,0,2)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,2)}v_2}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(1,0,1)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,2)}m_{(1,0,0)}v_2}{m_{(0,0,0)}} - \\
& m_{(0,2,2)}v_1 + \frac{2m_{(0,0,1)}m_{(0,2,1)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,0,2)}m_{(0,2,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(0,1,2)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,1,1)}^2v_1}{m_{(0,0,0)}} + m_{(1,2,2)} - \frac{m_{(0,0,2)}m_{(1,2,0)}}{m_{(0,0,0)}} -
\end{aligned}$$

$$\begin{aligned}
& \frac{4m_{(0,1,1)}m_{(1,1,1)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,2)}m_{(1,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(1,0,2)}}{m_{(0,0,0)}} - \frac{2m_{(0,2,1)}m_{(1,0,1)}}{m_{(0,0,0)}} \\
\gamma_{(2,1,2)} = & -m_{(0,0,0)}v_1^2v_2^2v_3^2 - 6m_{(0,0,0)}v_1^2v_2v_3^2 + 2m_{(1,0,0)}v_1v_2v_3^2 - m_{(2,0,0)}v_2v_3^2 + \frac{6m_{(1,0,0)}^2v_2v_3^2}{m_{(0,0,0)}} - \\
& m_{(0,1,0)}v_1^2v_3^2 - 2m_{(1,1,0)}v_1v_3^2 + \frac{12m_{(0,1,0)}m_{(1,0,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{3m_{(0,1,0)}m_{(2,0,0)}v_3^2}{m_{(0,0,0)}} - \frac{6m_{(1,0,0)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} + 2m_{(0,0,1)}v_1^2v_2v_3 - \\
& 12m_{(1,0,1)}v_1v_2v_3 + \frac{24m_{(0,0,1)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}} + 4m_{(2,0,1)}v_2v_3 - \frac{6m_{(0,0,1)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}} - \frac{12m_{(1,0,0)}m_{(1,0,1)}v_2v_3}{m_{(0,0,0)}} - 2m_{(0,1,1)}v_1^2v_3 + \\
& \frac{12m_{(0,0,1)}m_{(0,1,0)}v_1^2v_3}{m_{(0,0,0)}} + 8m_{(1,1,1)}v_1v_3 - \frac{12m_{(0,0,1)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,0)}m_{(1,0,1)}v_1v_3}{m_{(0,0,0)}} - \frac{12m_{(0,1,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} - 2m_{(2,1,1)}v_3 + \\
& \frac{2m_{(0,0,1)}m_{(2,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,1)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,1,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(1,0,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}} - m_{(0,0,2)}v_1^2v_2 + \\
& \frac{6m_{(0,0,1)}^2v_1^2v_2}{m_{(0,0,0)}} + 4m_{(1,0,2)}v_1v_2 - \frac{12m_{(0,0,1)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,2)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} - m_{(2,0,2)}v_2 + \frac{2m_{(0,0,1)}m_{(2,0,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,0,2)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,0,2)}v_2}{m_{(0,0,0)}} + \frac{4m_{(1,0,1)}^2v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,1)}m_{(0,1,1)}v_1^2}{m_{(0,0,0)}} - \frac{3m_{(0,0,2)}m_{(0,1,0)}v_1^2}{m_{(0,0,0)}} - 2m_{(1,1,2)}v_1 + \\
& \frac{4m_{(0,0,1)}m_{(1,1,1)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,0,2)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(1,0,2)}v_1}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,1,2)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,1,2)} - \\
& \frac{m_{(0,0,2)}m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{2m_{(0,1,1)}m_{(2,0,1)}}{m_{(0,0,0)}} - \frac{m_{(0,1,2)}m_{(2,0,0)}}{m_{(0,0,0)}} - \frac{4m_{(1,0,1)}m_{(1,1,1)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,2)}m_{(1,1,0)}}{m_{(0,0,0)}} \\
\gamma_{(2,2,1)} = & -m_{(0,0,0)}v_1^2v_2^2v_3^2 - 6m_{(0,0,0)}v_1^2v_2^2v_3 + 2m_{(1,0,0)}v_1v_2^2v_3 - m_{(2,0,0)}v_2^2v_3 + \frac{6m_{(1,0,0)}^2v_2^2v_3}{m_{(0,0,0)}} + 2m_{(0,1,0)}v_1^2v_2v_3 - \\
& 12m_{(1,1,0)}v_1v_2v_3 \\
& + \frac{24m_{(0,1,0)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}} + 4m_{(2,1,0)}v_2v_3 - \frac{6m_{(0,1,0)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}} - \frac{12m_{(1,0,0)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}} - m_{(0,2,0)}v_1^2v_3 + \frac{6m_{(0,1,0)}^2v_1^2v_3}{m_{(0,0,0)}} + \\
& 4m_{(1,2,0)}v_1v_3 \\
& - \frac{12m_{(0,1,0)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}} - \frac{6m_{(0,2,0)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} - m_{(2,2,0)}v_3 + \frac{2m_{(0,1,0)}m_{(2,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,2,0)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(1,0,0)}m_{(1,2,0)}v_3}{m_{(0,0,0)}} + \\
& \frac{4m_{(1,1,0)}^2v_3}{m_{(0,0,0)}} - m_{(0,0,1)}v_1^2v_2^2 - 2m_{(1,0,1)}v_1v_2^2 + \frac{12m_{(0,0,1)}m_{(1,0,0)}v_1v_2^2}{m_{(0,0,0)}} - \frac{3m_{(0,0,1)}m_{(2,0,0)}v_2^2}{m_{(0,0,0)}} - \frac{6m_{(1,0,0)}m_{(1,0,1)}v_2^2}{m_{(0,0,0)}} - \\
& 2m_{(0,1,1)}v_1^2v_2 + \frac{12m_{(0,0,1)}m_{(0,1,0)}v_1^2v_2}{m_{(0,0,0)}} + 8m_{(1,1,1)}v_1v_2 - \frac{12m_{(0,0,1)}m_{(1,1,0)}v_1v_2}{m_{(0,0,0)}} - \frac{12m_{(0,1,0)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}} - \\
& \frac{12m_{(0,1,1)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} - 2m_{(2,1,1)}v_2 + \frac{2m_{(0,0,1)}m_{(2,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,1)}v_2}{m_{(0,0,0)}} + \frac{4m_{(0,1,1)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} + \frac{4m_{(1,0,0)}m_{(1,1,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{8m_{(1,0,1)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} - \frac{3m_{(0,0,1)}m_{(0,2,0)}v_1^2}{m_{(0,0,0)}} - \frac{6m_{(0,1,0)}m_{(0,1,1)}v_1^2}{m_{(0,0,0)}} - 2m_{(1,2,1)}v_1 + \frac{2m_{(0,0,1)}m_{(1,2,0)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(1,1,1)}v_1}{m_{(0,0,0)}} + \\
& \frac{8m_{(0,1,1)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,2,0)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} + \frac{2m_{(0,2,1)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} + m_{(2,2,1)} - \frac{2m_{(0,1,1)}m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(2,0,1)}}{m_{(0,0,0)}} - \frac{m_{(0,2,1)}m_{(2,0,0)}}{m_{(0,0,0)}} - \\
& \frac{2m_{(1,0,1)}m_{(1,2,0)}}{m_{(0,0,0)}} - \frac{4m_{(1,1,0)}m_{(1,1,1)}}{m_{(0,0,0)}} \\
\gamma_{(2,2,2)} = & 2v_2^2v_3m_{(2,0,1)} - \frac{4m_{(0,1,0)}v_2v_3m_{(2,0,1)}}{m_{(0,0,0)}} + \frac{2m_{(0,2,0)}v_3m_{(2,0,1)}}{m_{(0,0,0)}} + 2v_1^2v_3m_{(0,2,1)} - \frac{4m_{(1,0,0)}v_1v_3m_{(0,2,1)}}{m_{(0,0,0)}} + \\
& \frac{2m_{(2,0,0)}v_3m_{(0,2,1)}}{m_{(0,0,0)}} - 4m_{(0,0,0)}v_1v_2v_3^4 - 4m_{(1,0,0)}v_2v_3^4 - 4m_{(0,1,0)}v_1v_3^4 + 4m_{(1,1,0)}v_3^4 + 16m_{(0,0,1)}v_1v_2v_3^3 + \\
& \frac{16m_{(0,0,1)}m_{(1,0,0)}v_2v_3^3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}v_1v_3^3}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(1,1,0)}v_3^3}{m_{(0,0,0)}} + 2v_2m_{(2,1,0)}v_3^2 - 7m_{(0,0,0)}v_1^2v_2^2v_3^2 + v_1^2v_2^2v_3^2 - \\
& 20m_{(1,0,0)}v_1v_2^2v_3^2 + 4m_{(2,0,0)}v_2^2v_3^2 - \frac{26m_{(1,0,0)}^2v_2^2v_3^2}{m_{(0,0,0)}} - 20m_{(0,1,0)}v_1^2v_2v_3^2 + 16m_{(1,1,0)}v_1v_2v_3^2 - \frac{128m_{(0,1,0)}m_{(1,0,0)}v_1v_2v_3^2}{m_{(0,0,0)}} - \\
& 8m_{(0,0,2)}v_1v_2v_3^2 - \frac{16m_{(0,0,1)}^2v_1v_2v_3^2}{m_{(0,0,0)}} - 4m_{(2,1,0)}v_2v_3^2 + \frac{18m_{(0,1,0)}m_{(2,0,0)}v_2v_3^2}{m_{(0,0,0)}} + \frac{44m_{(1,0,0)}m_{(1,1,0)}v_2v_3^2}{m_{(0,0,0)}} - \\
& \frac{24m_{(0,1,0)}m_{(1,0,0)}^2v_2v_3^2}{m_{(0,0,0)}} - \frac{8m_{(0,0,2)}m_{(1,0,0)}v_2v_3^2}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}^2m_{(1,0,0)}v_2v_3^2}{m_{(0,0,0)}} + 4m_{(0,2,0)}v_1^2v_3^2 - \frac{26m_{(0,1,0)}^2v_1^2v_3^2}{m_{(0,0,0)}} - 2m_{(1,2,0)}v_1v_3^2 + \\
& \frac{44m_{(0,1,0)}m_{(1,1,0)}v_1v_3^2}{m_{(0,0,0)}} + \frac{18m_{(0,2,0)}m_{(1,0,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{24m_{(0,1,0)}^2m_{(1,0,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{8m_{(0,0,2)}m_{(0,1,0)}v_1v_3^2}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}^2m_{(0,1,0)}v_1v_3^2}{m_{(0,0,0)}} - \\
& \frac{6m_{(0,1,0)}m_{(2,1,0)}v_3^2}{m_{(0,0,0)}} - \frac{2m_{(0,2,0)}m_{(2,0,0)}v_3^2}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}^2m_{(2,0,0)}v_3^2}{m_{(0,0,0)}} - \frac{6m_{(1,0,0)}m_{(1,2,0)}v_3^2}{m_{(0,0,0)}} - \frac{8m_{(1,1,0)}^2v_3^2}{m_{(0,0,0)}} + \frac{16m_{(0,1,0)}m_{(1,0,0)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}^2} + \\
& \frac{8m_{(0,0,2)}m_{(1,1,0)}v_3^2}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}^2m_{(1,1,0)}v_3^2}{m_{(0,0,0)}^2} + \frac{4m_{(0,2,0)}m_{(1,0,0)}^2v_3^2}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,1)}v_2m_{(2,1,0)}v_3}{m_{(0,0,0)}} - 4m_{(0,0,1)}v_1^2v_2^2v_3 + 8m_{(1,0,1)}v_1v_2^2v_3 - \\
& \frac{104m_{(0,0,1)}m_{(1,0,0)}v_1v_2^2v_3}{m_{(0,0,0)}} - 4m_{(2,0,1)}v_2^2v_3 + \frac{18m_{(0,0,1)}m_{(2,0,0)}v_2^2v_3}{m_{(0,0,0)}} + \frac{36m_{(1,0,0)}m_{(1,0,1)}v_2^2v_3}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(1,0,0)}^2v_2^2v_3}{m_{(0,0,0)}^2} +
\end{aligned}$$

$$\begin{aligned}
& 8m_{(0,1,1)}v_1^2v_2v_3 - \frac{104m_{(0,0,1)}m_{(0,1,0)}v_1^2v_2v_3}{m_{(0,0,0)}} - 24m_{(1,1,1)}v_1v_2v_3 + \frac{88m_{(0,0,1)}m_{(1,1,0)}v_1v_2v_3}{m_{(0,0,0)}} + \frac{104m_{(0,1,0)}m_{(1,0,1)}v_1v_2v_3}{m_{(0,0,0)}} + \\
& \frac{104m_{(0,1,1)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}} - \frac{80m_{(0,0,1)}m_{(0,1,0)}m_{(1,0,0)}v_1v_2v_3}{m_{(0,0,0)}^2} + \frac{16m_{(0,0,1)}m_{(0,0,2)}v_1v_2v_3}{m_{(0,0,0)}} + 8m_{(2,1,1)}v_2v_3 - \frac{8m_{(0,0,1)}m_{(2,1,0)}v_2v_3}{m_{(0,0,0)}} - \\
& \frac{8m_{(0,1,0)}m_{(2,0,1)}v_2v_3}{m_{(0,0,0)}} - \frac{24m_{(0,1,1)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}m_{(2,0,0)}v_2v_3}{m_{(0,0,0)}^2} - \frac{24m_{(1,0,0)}m_{(1,1,1)}v_2v_3}{m_{(0,0,0)}} - \frac{48m_{(1,0,1)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}} + \\
& \frac{16m_{(0,0,1)}m_{(1,0,0)}m_{(1,1,0)}v_2v_3}{m_{(0,0,0)}^2} + \frac{32m_{(0,1,0)}m_{(1,0,0)}m_{(1,0,1)}v_2v_3}{m_{(0,0,0)}^2} + \frac{16m_{(0,1,1)}m_{(1,0,0)}^2v_2v_3}{m_{(0,0,0)}^2} + \frac{16m_{(0,0,1)}m_{(0,0,2)}m_{(1,0,0)}v_2v_3}{m_{(0,0,0)}^2} - \\
& 4m_{(0,2,1)}v_1^2v_3 + \frac{18m_{(0,0,1)}m_{(0,2,0)}v_1^2v_3}{m_{(0,0,0)}} + \frac{36m_{(0,1,0)}m_{(0,1,1)}v_1^2v_3}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(0,1,0)}^2v_1^2v_3}{m_{(0,0,0)}^2} + 8m_{(1,2,1)}v_1v_3 - \\
& \frac{12m_{(0,0,1)}m_{(1,2,0)}v_1v_3}{m_{(0,0,0)}} - \frac{24m_{(0,1,0)}m_{(1,1,1)}v_1v_3}{m_{(0,0,0)}} - \frac{48m_{(0,1,1)}m_{(1,1,0)}v_1v_3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}m_{(1,2,1)}v_1v_3}{m_{(0,0,0)}^2} - \frac{24m_{(0,2,0)}m_{(1,0,1)}v_1v_3}{m_{(0,0,0)}} + \\
& \frac{16m_{(0,1,0)}^2m_{(1,0,1)}v_1v_3}{m_{(0,0,0)}^2} - \frac{8m_{(0,2,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,2,0)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}^2} + \frac{32m_{(0,1,0)}m_{(0,1,1)}m_{(1,0,0)}v_1v_3}{m_{(0,0,0)}^2} + \\
& \frac{16m_{(0,0,1)}m_{(0,0,2)}m_{(0,1,0)}v_1v_3}{m_{(0,0,0)}^2} - 2m_{(2,2,1)}v_3 + \frac{2m_{(0,0,1)}m_{(2,2,0)}v_3}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(2,1,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(2,1,0)}v_3}{m_{(0,0,0)}} + \frac{2m_{(0,2,0)}m_{(2,0,1)}v_3}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,2,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}} - \frac{4m_{(0,0,1)}m_{(0,2,0)}m_{(2,0,0)}v_3}{m_{(0,0,0)}^2} - \frac{8m_{(0,1,0)}m_{(0,1,1)}m_{(2,0,0)}v_3}{m_{(0,0,0)}^2} + \frac{4m_{(1,0,0)}m_{(1,2,1)}v_3}{m_{(0,0,0)}} + \frac{8m_{(1,0,1)}m_{(1,2,0)}v_3}{m_{(0,0,0)}} + \\
& \frac{16m_{(1,1,0)}m_{(1,1,1)}v_3}{m_{(0,0,0)}} - \frac{16m_{(0,1,0)}m_{(1,0,1)}m_{(1,1,0)}v_3}{m_{(0,0,0)}^2} - \frac{16m_{(0,1,1)}m_{(1,0,0)}m_{(1,1,0)}v_3}{m_{(0,0,0)}^2} - \frac{16m_{(0,0,1)}m_{(0,0,2)}m_{(1,1,0)}v_3}{m_{(0,0,0)}^2} - \\
& \frac{8m_{(0,2,0)}m_{(1,0,0)}m_{(1,0,1)}v_3}{m_{(0,0,0)}^2} + \frac{2m_{(0,0,2)}v_2m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{22m_{(0,0,1)}^2v_1^2v_2^2}{m_{(0,0,0)}} - 2m_{(1,0,2)}v_1v_2^2 + \frac{36m_{(0,0,1)}m_{(1,0,1)}v_1v_2^2}{m_{(0,0,0)}} + \\
& \frac{10m_{(0,0,2)}m_{(1,0,0)}v_1v_2^2}{m_{(0,0,0)}} - \frac{24m_{(0,0,1)}^2m_{(1,0,0)}v_1v_2^2}{m_{(0,0,0)}^2} - \frac{6m_{(0,0,1)}m_{(2,0,1)}v_2^2}{m_{(0,0,0)}} - \frac{2m_{(0,0,2)}m_{(2,0,0)}v_2^2}{m_{(0,0,0)}} + \frac{4m_{(0,0,1)}^2m_{(2,0,0)}v_2^2}{m_{(0,0,0)}^2} - \\
& \frac{6m_{(1,0,0)}m_{(1,0,2)}v_2^2}{m_{(0,0,0)}} - \frac{4m_{(1,0,1)}^2v_2^2}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(1,0,0)}m_{(1,0,1)}v_2^2}{m_{(0,0,0)}^2} - 2m_{(0,1,2)}v_1^2v_2 + \frac{36m_{(0,0,1)}m_{(0,1,1)}v_1^2v_2}{m_{(0,0,0)}} + \\
& \frac{10m_{(0,0,2)}m_{(0,1,0)}v_1^2v_2}{m_{(0,0,0)}} - \frac{24m_{(0,0,1)}^2m_{(0,1,0)}v_1^2v_2}{m_{(0,0,0)}^2} + 8m_{(1,1,2)}v_1v_2 - \frac{24m_{(0,0,1)}m_{(1,1,1)}v_1v_2}{m_{(0,0,0)}} - \frac{16m_{(0,0,2)}m_{(1,1,0)}v_1v_2}{m_{(0,0,0)}} + \\
& \frac{16m_{(0,0,1)}^2m_{(1,1,0)}v_1v_2}{m_{(0,0,0)}^2} - \frac{12m_{(0,1,0)}m_{(1,0,2)}v_1v_2}{m_{(0,0,0)}} - \frac{48m_{(0,1,1)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}} + \frac{32m_{(0,0,1)}m_{(0,1,0)}m_{(1,0,1)}v_1v_2}{m_{(0,0,0)}^2} - \frac{12m_{(0,1,2)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}} + \\
& \frac{32m_{(0,0,1)}m_{(0,1,1)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}^2} + \frac{8m_{(0,0,2)}m_{(0,1,0)}m_{(1,0,0)}v_1v_2}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,2)}^2v_1v_2}{m_{(0,0,0)}} - 2m_{(2,1,2)}v_2 + \frac{4m_{(0,0,1)}m_{(2,1,1)}v_2}{m_{(0,0,0)}} + \\
& \frac{2m_{(0,0,2)}m_{(2,1,0)}v_2}{m_{(0,0,0)}} + \frac{2m_{(0,1,0)}m_{(2,0,2)}v_2}{m_{(0,0,0)}} + \frac{8m_{(0,1,1)}m_{(2,0,1)}v_2}{m_{(0,0,0)}} + \frac{4m_{(0,1,2)}m_{(2,0,0)}v_2}{m_{(0,0,0)}} - \frac{8m_{(0,0,1)}m_{(0,1,1)}m_{(2,0,0)}v_2}{m_{(0,0,0)}^2} - \\
& \frac{4m_{(0,0,2)}m_{(0,1,0)}m_{(2,0,0)}v_2}{m_{(0,0,0)}^2} + \frac{4m_{(1,0,0)}m_{(1,1,2)}v_2}{m_{(0,0,0)}} + \frac{16m_{(1,0,1)}m_{(1,1,1)}v_2}{m_{(0,0,0)}} + \frac{8m_{(1,0,2)}m_{(1,1,0)}v_2}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(1,0,1)}m_{(1,1,0)}v_2}{m_{(0,0,0)}^2} - \\
& \frac{8m_{(0,1,0)}m_{(1,0,1)}^2v_2}{m_{(0,0,0)}^2} - \frac{16m_{(0,1,1)}m_{(1,0,0)}m_{(1,0,1)}v_2}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,2)}^2m_{(1,0,0)}v_2}{m_{(0,0,0)}} - \frac{6m_{(0,0,1)}m_{(0,2,1)}v_1^2}{m_{(0,0,0)}} - \frac{2m_{(0,0,2)}m_{(0,2,0)}v_1^2}{m_{(0,0,0)}} + \\
& \frac{4m_{(0,0,1)}^2m_{(0,2,0)}v_1^2}{m_{(0,0,0)}^2} - \frac{6m_{(0,1,0)}m_{(0,1,2)}v_1^2}{m_{(0,0,0)}} - \frac{4m_{(0,1,1)}^2v_1^2}{m_{(0,0,0)}} + \frac{16m_{(0,0,1)}m_{(0,1,0)}m_{(0,1,1)}v_1^2}{m_{(0,0,0)}^2} - 2m_{(1,2,2)}v_1 + \frac{4m_{(0,0,1)}m_{(1,2,1)}v_1}{m_{(0,0,0)}} + \\
& \frac{4m_{(0,0,2)}m_{(1,2,0)}v_1}{m_{(0,0,0)}} + \frac{4m_{(0,1,0)}m_{(1,1,2)}v_1}{m_{(0,0,0)}} + \frac{16m_{(0,1,1)}m_{(1,1,1)}v_1}{m_{(0,0,0)}} + \frac{8m_{(0,1,2)}m_{(1,1,0)}v_1}{m_{(0,0,0)}} - \frac{16m_{(0,0,1)}m_{(0,1,1)}m_{(1,1,0)}v_1}{m_{(0,0,0)}^2} + \\
& \frac{4m_{(0,2,0)}m_{(1,0,2)}v_1}{m_{(0,0,0)}} + \frac{8m_{(0,2,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}} - \frac{8m_{(0,0,1)}m_{(0,2,0)}m_{(1,0,1)}v_1}{m_{(0,0,0)}^2} - \frac{16m_{(0,1,0)}m_{(0,1,1)}m_{(1,0,1)}v_1}{m_{(0,0,0)}^2} + \frac{2m_{(0,2,2)}m_{(1,0,0)}v_1}{m_{(0,0,0)}} - \\
& \frac{4m_{(0,0,2)}m_{(0,2,0)}m_{(1,0,0)}v_1}{m_{(0,0,0)}^2} - \frac{8m_{(0,1,1)}^2m_{(1,0,0)}v_1}{m_{(0,0,0)}^2} - \frac{4m_{(0,0,2)}^2m_{(0,1,0)}v_1}{m_{(0,0,0)}^2} + m_{(2,2,2)} - \frac{m_{(0,0,2)}m_{(2,2,0)}}{m_{(0,0,0)}} - \frac{4m_{(0,1,1)}m_{(2,1,1)}}{m_{(0,0,0)}} - \\
& \frac{2m_{(0,1,2)}m_{(2,1,0)}}{m_{(0,0,0)}} - \frac{m_{(0,2,0)}m_{(2,0,2)}}{m_{(0,0,0)}} - \frac{2m_{(0,2,1)}m_{(2,0,1)}}{m_{(0,0,0)}} - \frac{m_{(0,2,2)}m_{(2,0,0)}}{m_{(0,0,0)}} + \frac{2m_{(0,0,2)}m_{(0,2,0)}m_{(2,0,0)}}{m_{(0,0,0)}^2} + \frac{4m_{(0,1,1)}^2m_{(2,0,0)}}{m_{(0,0,0)}^2} - \\
& \frac{4m_{(1,0,1)}m_{(1,2,1)}}{m_{(0,0,0)}} - \frac{2m_{(1,0,2)}m_{(1,2,0)}}{m_{(0,0,0)}} - \frac{4m_{(1,1,0)}m_{(1,1,2)}}{m_{(0,0,0)}} - \frac{4m_{(1,1,1)}^2}{m_{(0,0,0)}} + \frac{16m_{(0,1,1)}m_{(1,0,1)}m_{(1,1,0)}}{m_{(0,0,0)}^2} + \frac{4m_{(0,0,2)}^2m_{(1,1,0)}}{m_{(0,0,0)}^2} + \\
& \frac{4m_{(0,2,0)}m_{(1,0,1)}^2}{m_{(0,0,0)}^2}.
\end{aligned}$$

The equilibrium cumulant vector $\gamma^{(eq)}$ is defined by

$$\gamma^{(eq)} = (\rho, 0, 0, 0, 0, 0, 0, \rho c_s^2, \rho c_s^2, \rho c_s^2, 0, 0, \dots, 0)^T.$$

2.6.2 Conservation of mass: ρ



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$$\frac{\partial \rho}{\partial t} + v_1 \delta_1 \frac{\partial \rho}{\partial x_1} + \frac{\delta_1 \rho}{\delta_1} \frac{\partial v_1}{\partial x_1} + \frac{v_2 \delta_1}{\delta_1} \frac{\partial \rho}{\partial x_2} + \frac{\delta_1 \rho}{\delta_1} \frac{\partial v_2}{\partial x_2} + \frac{v_3 \delta_1}{\delta_1} \frac{\partial \rho}{\partial x_3} + \frac{\delta_1 \rho}{\delta_1} \frac{\partial v_3}{\partial x_3} + (-1 + v_1^2 + 3c_s^2) \frac{v_1 \delta_1^3}{12 \delta_1} \frac{\partial^3 \rho}{\partial x_1^3} +$$

$$\begin{aligned}
& (-1 + 3v_1^2 + c_s^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} - \\
& \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + v_3^2 + 3c_s^2) \frac{v_3 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{\delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} \\
& + (2c_s^4 - 3v_1^4 \omega_4 - c_s^4 \omega_4 - 6v_1^2 + 24v_1^2 c_s^2 + 6v_1^4 + 3v_1^2 \omega_4 + c_s^2 \omega_4 - 2c_s^2 - 12v_1^2 c_s^2 \omega_4) \frac{\delta_l^4}{24\delta_t \omega_4} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 10v_1^2 + 2\omega_4 - 5v_1^2 \omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_1 \delta_l^4 \rho}{12\delta_t \omega_4} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& (-\omega_9 + 3\omega_9 c_s^2 \omega_4 + v_1^2 \omega_9 \omega_4 - \omega_9 \omega_4 + 3\omega_4 + v_1^2 \omega_9 - 3v_1^2 \omega_4 - 9c_s^2 \omega_4 + 3\omega_9 c_s^2) \frac{v_1 \delta_l^4 \rho}{12\omega_9 \delta_t \omega_4} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_1) \frac{c_s^4 \delta_l^4}{6\delta_t \omega_1} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} \\
& + (-3v_2^2 \omega_5 + v_2^2 \omega_7 \omega_5 - \omega_7 \omega_5 - 9c_s^2 \omega_5 + v_2^2 \omega_7 + 3c_s^2 \omega_7 \omega_5 + 3c_s^2 \omega_7 - \omega_7 + 3\omega_5) \frac{v_2 \delta_l^4 \rho}{12\delta_t \omega_7 \omega_5} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} + \\
& (-12v_2^2 c_s^2 \omega_5 + 3v_2^2 \omega_5 + 2c_s^4 + c_s^2 \omega_5 + 24v_2^2 c_s^2 - 6v_2^2 + 6v_2^4 - c_s^4 \omega_5 - 3v_2^4 \omega_5 - 2c_s^2) \frac{\delta_l^4}{24\delta_t \omega_5} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 - 5v_2^2 \omega_5 - 3c_s^2 \omega_5 + 10v_2^2 + 2\omega_5 + 6c_s^2) \frac{v_2 \delta_l^4 \rho}{12\delta_t \omega_5} \frac{\partial^4 v_2}{\partial x_2^2} + \\
& (-\omega_{12} - \omega_{12} \omega_4 + v_1^2 \omega_{12} \omega_4 + 3\omega_4 - 3v_1^2 \omega_4 - 9c_s^2 \omega_4 + 3\omega_{12} c_s^2 \omega_4 + v_1^2 \omega_{12} + 3\omega_{12} c_s^2) \frac{v_1 \delta_l^4 \rho}{12\omega_{12} \delta_t \omega_4} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& (-3v_2^2 \omega_5 + 3c_s^2 \omega_{11} \omega_5 - 9c_s^2 \omega_5 - \omega_{11} \omega_5 + v_2^2 \omega_{11} \omega_5 - \omega_{11} + 3c_s^2 \omega_{11} + 3\omega_5 + v_2^2 \omega_{11}) \frac{v_2 \delta_l^4 \rho}{12\delta_t \omega_{11} \omega_5} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-2 + \omega_2) \frac{c_s^4 \delta_l^4}{6\delta_t \omega_2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + (-2 + \omega_3) \frac{c_s^4 \delta_l^4}{6\omega_3 \delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (3\omega_6 c_s^2 \omega_8 + v_3^2 \omega_6 \omega_8 + 3\omega_6 - 9\omega_6 c_s^2 + v_3^2 \omega_8 - 3v_3^2 \omega_6 - \omega_6 \omega_8 - \omega_8 + 3c_s^2 \omega_8) \frac{v_3 \delta_l^4 \rho}{12\omega_6 \delta_t \omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (3\omega_6 - 9\omega_6 c_s^2 + 3c_s^2 \omega_{10} + v_3^2 \omega_{10} - \omega_{10} - \omega_6 \omega_{10} - 3v_3^2 \omega_6 + 3\omega_6 c_s^2 \omega_{10} + v_3^2 \omega_6 \omega_{10}) \frac{v_3 \delta_l^4 \rho}{12\omega_6 \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (-3v_3^4 \omega_6 + 24v_3^2 c_s^2 + 2c_s^4 + \omega_6 c_s^2 - 6v_3^2 - 12v_3^2 \omega_6 c_s^2 + 3v_3^2 \omega_6 + 6v_3^4 - 2c_s^2 - \omega_6 c_s^4) \frac{\delta_l^4}{24\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (-4 + 2\omega_6 - 3\omega_6 c_s^2 + 10v_3^2 - 5v_3^2 \omega_6 + 6c_s^2) \frac{v_3 \delta_l^4 \rho}{12\omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_3^3} = 0.
\end{aligned}$$

2.6.3 Conservation of momentum: ρv_1



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$$\begin{aligned}
& v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2v_1 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_2 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{v_1 \delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_1 v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\
& \frac{v_1 \delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + 6v_1^2 + \omega_4 - 3v_1^2 \omega_4 - 2c_s^2 \omega_4 + 4c_s^2) \frac{\delta_l^2}{\delta_t \omega_4} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + (2 - \omega_4) \frac{3v_1 \delta_l^2 \rho}{\delta_t \omega_4} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + \\
& (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\
& (-2 + 2v_1^2 + \omega_4 - v_1^2 \omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_1 \delta_l^2}{2\delta_t \omega_4} \frac{\partial^2 \rho}{\partial x_1^2} + (-2 + 6v_1^2 + \omega_4 - 3v_1^2 \omega_4 - c_s^2 \omega_4 + 2c_s^2) \frac{\delta_l^2 \rho}{2\delta_t \omega_4} \frac{\partial^2 v_1}{\partial x_1^2} + \\
& (-2 + \omega_1) \frac{c_s^2 \delta_l^2 \rho}{2\delta_t \omega_1} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2 \rho}{2\delta_t \omega_1} \frac{\partial^2 v_1}{\partial x_2^2} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2 \rho}{2\delta_t \omega_2} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_2) \frac{c_s^2 \delta_l^2 \rho}{2\delta_t \omega_2} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\delta_t \omega_4} \frac{\partial^3 \rho}{\partial x_1^3} + \\
& (-24 - 4\omega_4^2 + 60v_1^2 + 24\omega_4 - 60v_1^2 \omega_4 - 36c_s^2 \omega_4 + 36c_s^2 + 11v_1^2 \omega_4^2 + 5c_s^2 \omega_4^2) \frac{v_1 \delta_l^3 \rho}{6\delta_t \omega_4^2} \frac{\partial^3 v_1}{\partial x_1^3} + C_2 \frac{v_1 \delta_l^3 \rho}{12\omega_9 \delta_t \omega_4^2 \omega_1} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& (-12 - \omega_1^2 + 12\omega_1) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_1^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \frac{v_1 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + (-1 + v_2^2 + 3c_s^2) \frac{v_2 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_3 \frac{v_2 \delta_l^3 \rho}{6\delta_t \omega_7 \omega_1} \frac{\partial^3 v_1}{\partial x_2^3} + \\
& (-1 + 3v_2^2 + c_s^2) \frac{v_1 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} + C_4 \frac{v_1 \delta_l^3 \rho}{12\omega_{12} \delta_t \omega_4^2 \omega_2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} - \frac{v_1 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + (-12 - \omega_2^2 + 12\omega_2) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \\
& \frac{v_1 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} - \frac{v_1 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + (-1 + v_3^2 + 3c_s^2) \frac{v_1 v_3 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \delta_l^3 \rho}{6\delta_t \omega_8 \omega_2} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{v_1 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_6 \frac{v_1 \delta_l^4}{12\delta_t \omega_4^3} \frac{\partial^4 \rho}{\partial x_1^4} + C_7 \frac{\delta_l^4 \rho}{12\delta_t \omega_4^3} \frac{\partial^4 v_1}{\partial x_1^4} + C_8 \frac{\delta_l^4 \rho}{12\omega_9 \delta_t \omega_4^3 \omega_1^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_9 \frac{v_1 c_s^2 \delta_l^4}{12\omega_9 \delta_t \omega_4^3 \omega_1^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{10} \frac{c_s^2 \delta_l^4 \rho}{12\omega_9 \delta_t \omega_4^3 \omega_1^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& C_{11} \frac{v_2 c_s^2 \delta_l^4}{12\delta_t \omega_7^2 \omega_5} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^2} + (-3v_2^2 \omega_5 + v_2^2 \omega_7 \omega_5 - \omega_7 \omega_5 - 9c_s^2 \omega_5 + v_2^2 \omega_7 + 3c_s^2 \omega_7 \omega_5 + 3c_s^2 \omega_7 - \omega_7 + 3\omega_5) \frac{v_2 v_1 \delta_l^4 \rho}{12\delta_t \omega_7 \omega_5} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^2} \\
& + C_{12} \frac{c_s^2 \delta_l^4 \rho}{12\delta_t \omega_7 \omega_1^3 \omega_5} \frac{\partial^4 v_2}{\partial x_1 \partial x_3^2} + \\
& (-12v_2^2 c_s^2 \omega_5 + 3v_2^2 \omega_5 + 2c_s^4 + c_s^2 \omega_5 + 24v_2^2 c_s^2 - 6v_2^2 + 6v_2^4 - c_s^4 \omega_5 - 3v_2^4 \omega_5 - 2c_s^2) \frac{v_1 \delta_l^4}{24\delta_t \omega_5} \frac{\partial^4 \rho}{\partial x_2^4} + C_{13} \frac{\delta_l^4 \rho}{24\delta_t \omega_7^2 \omega_1^3} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (-4 - 5v_2^2 \omega_5 - 3c_s^2 \omega_5 + 10v_2^2 + 2\omega_5 + 6c_s^2) \frac{v_2 v_1 \delta_l^4 \rho}{12\delta_t \omega_5} \frac{\partial^4 v_2}{\partial x_2^4} + C_{14} \frac{\delta_l^4 \rho}{12\omega_{12}^2 \delta_t \omega_4^3 \omega_2^2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{15} \frac{c_s^4 \delta_l^4 \rho}{12\omega_3 \delta_t \omega_{13} \omega_1^3 \omega_2^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} +
\end{aligned}$$

$$\begin{aligned}
& (-3v_2^2\omega_5 + 3c_s^2\omega_{11}\omega_5 - 9c_s^2\omega_5 - \omega_{11}\omega_5 + v_2^2\omega_{11}\omega_5 - \omega_{11} + 3c_s^2\omega_{11} + 3\omega_5 + v_2^2\omega_{11}) \frac{v_2v_1\delta_t^4\rho}{12\delta_t\omega_{11}\omega_5} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& C_{16} \frac{v_1c_s^2\delta_t^4}{12\omega_{12}^2\delta_t\omega_3^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3} + C_{17} \frac{c_s^2\delta_t^4\rho}{12\omega_{12}\delta_t\omega_4^2\omega_3^2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3} + C_{18} \frac{c_s^4\delta_t^4\rho}{12\omega_3\delta_t\omega_{13}\omega_1^2\omega_3^2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3} + (-2 + \omega_3) \frac{v_1c_s^4\delta_t^4}{6\omega_3\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + \\
& (-\omega_{13}\omega_1\omega_2 + \omega_{13}\omega_2 + 2\omega_1^2\omega_2 - \omega_1^2\omega_2^2 - \omega_1^2 - \omega_2^2 + 2\omega_1\omega_2^2 - 2\omega_1\omega_2 + \omega_{13}\omega_1) \frac{c_s^4\delta_t^4\rho}{\delta_t\omega_{13}\omega_1^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3} + \\
& C_{19} \frac{v_3c_s^2\delta_t^4}{12\omega_6\delta_t\omega_8^2\omega_2^2} \frac{\partial^4 \rho}{\partial x_1 \partial x_3} + (3\omega_6c_s^2\omega_8 + v_3^2\omega_6\omega_8 + 3\omega_6 - 9\omega_6c_s^2 + v_3^2\omega_8 - 3v_3^2\omega_6 - \omega_6\omega_8 - \omega_8 + 3c_s^2\omega_8) \frac{v_1v_3\delta_t^4\rho}{12\omega_6\delta_t\omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_3} \\
& + C_{20} \frac{c_s^2\delta_t^4\rho}{12\omega_6\delta_t\omega_8\omega_2^2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3} + \\
& (3\omega_6 - 9\omega_6c_s^2 + 3c_s^2\omega_{10} + v_3^2\omega_{10} - \omega_{10} - \omega_6\omega_{10} - 3v_3^2\omega_6 + 3\omega_6c_s^2\omega_{10} + v_3^2\omega_6\omega_{10}) \frac{v_1v_3\delta_t^4\rho}{12\omega_6\delta_t\omega_{10}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3} + \\
& (-3v_3^4\omega_6 + 24v_3^2c_s^2 + 2c_s^4 + \omega_6c_s^2 - 6v_3^2 - 12v_3^2\omega_6c_s^2 + 3v_3^2\omega_6 + 6v_3^4 - 2c_s^2 - \omega_6c_s^4) \frac{v_1\delta_t^4}{24\omega_6\delta_t} \frac{\partial^4 \rho}{\partial x_3} + C_{21} \frac{\delta_t^4\rho}{24\delta_t\omega_8^2\omega_2^2} \frac{\partial^4 v_1}{\partial x_3} + \\
& (-4 + 2\omega_6 - 3\omega_6c_s^2 + 10v_3^2 - 5v_3^2\omega_6 + 6c_s^2) \frac{v_1v_3\delta_t^4\rho}{12\omega_6\delta_t} \frac{\partial^4 v_3}{\partial x_3} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 12c_s^4 - 36v_1^4\omega_4 - 12c_s^4\omega_4 + 7v_1^4\omega_4^2 + c_s^4\omega_4^2 - 36v_1^2 + 144v_1^2c_s^2 + 36v_1^4 + 36v_1^2\omega_4 + 12c_s^2\omega_4 + 24v_1^2c_s^2\omega_4^2 - 12c_s^2 - 144v_1^2c_s^2\omega_4 - 7v_1^2\omega_4^2 - c_s^2\omega_4^2 \\
C_2 &= -6\omega_9\omega_4^2 + 3\omega_9\omega_4^2\omega_1 + 12v_1^2\omega_9\omega_1 - 12v_1^2\omega_4\omega_1 - 36c_s^2\omega_4\omega_1 + 36\omega_9c_s^2\omega_1 - 18\omega_9c_s^2\omega_4\omega_1 + 12\omega_4^2 + 6v_1^2\omega_9\omega_4^2 - 12\omega_9\omega_1 + 18\omega_9c_s^2\omega_4^2 + \\
& 12\omega_4\omega_1 - 6v_1^2\omega_9\omega_4\omega_1 - 12\omega_4^2\omega_1 - 3v_1^2\omega_9\omega_4^2\omega_1 + 12v_1^2\omega_4^2\omega_1 + 36c_s^2\omega_2^2\omega_1 - 11\omega_9c_s^2\omega_4^2\omega_1 - 12v_1^2\omega_4^2 - 36c_s^2\omega_4^2 + 6\omega_9\omega_4\omega_1 \\
C_3 &= 6 - 6v_2^2 + 3v_2^2\omega_7 + 9c_s^2\omega_7 - 3\omega_7 + 3v_2^2\omega_1 - 3\omega_1 - v_2^2\omega_7\omega_1 + \omega_7\omega_1 + 9c_s^2\omega_1 - 18c_s^2 - 3c_s^2\omega_7\omega_1 \\
C_4 &= 6v_1^2\omega_{12}\omega_4^2 + 12v_1^2\omega_4^2\omega_2 - 6v_1^2\omega_{12}\omega_4\omega_2 + 36c_s^2\omega_4^2\omega_2 + 12\omega_4^2 - 11\omega_{12}c_s^2\omega_4^2\omega_2 + 3\omega_{12}\omega_4^2\omega_2 - 6\omega_{12}\omega_4^2 + 36\omega_{12}c_s^2\omega_2 - 12\omega_4^2\omega_2 + 12\omega_4\omega_2 + \\
& 12v_1^2\omega_{12}\omega_2 - 18\omega_{12}c_s^2\omega_4\omega_2 + 6\omega_{12}\omega_4\omega_2 - 12v_1^2\omega_4\omega_2 - 36c_s^2\omega_4\omega_2 - 3v_1^2\omega_{12}\omega_4^2\omega_2 + 18\omega_{12}c_s^2\omega_4^2 - 12\omega_{12}\omega_2 - 12v_1^2\omega_4^2 - 36c_s^2\omega_4^2 \\
C_5 &= 6 + 3v_3^2\omega_2 - 3c_s^2\omega_8\omega_2 + 9c_s^2\omega_2 - 6v_3^2 + \omega_8\omega_2 + 3v_3^2\omega_8 - 3\omega_8 - v_3^2\omega_8\omega_2 - 18c_s^2 - 3\omega_2 + 9c_s^2\omega_8 \\
C_6 &= 12 + 144c_s^4 - 216v_1^4\omega_4 - 216c_s^4\omega_4 + 90v_1^4\omega_4^2 + 8\omega_4^2 + 82c_s^4\omega_4^2 - 156v_1^2 - \omega_4^3 - 5c_s^4\omega_4^3 - 9v_1^4\omega_4^3 + 672v_1^2c_s^2 - 34v_1^2c_s^2\omega_4^3 - 18\omega_4 + 144v_1^4 + \\
& 234v_1^2\omega_4 + 198c_s^2\omega_4 + 404v_1^2c_s^2\omega_4^2 + 6c_s^2\omega_4^3 + 10v_1^2\omega_4^3 - 132c_s^2 - 1008v_1^2c_s^2\omega_4 - 98v_1^2\omega_4^2 - 78c_s^2\omega_4^2 \\
C_7 &= 12 + 24c_s^4 - 756v_1^4\omega_4 - 36c_s^4\omega_4 + 310v_1^4\omega_4^2 + 8\omega_4^2 + 14c_s^4\omega_4^2 - 252v_1^2 - \omega_4^3 - c_s^4\omega_4^3 - 29v_1^4\omega_4^3 + 432v_1^2c_s^2 - 18v_1^2c_s^2\omega_4^3 - 18\omega_4 + 504v_1^4 + \\
& 378v_1^2\omega_4 + 54c_s^2\omega_4 + 252v_1^2c_s^2\omega_4^2 + 2c_s^2\omega_4^3 + 14v_1^2\omega_4^3 - 36c_s^2 - 648v_1^2c_s^2\omega_4 - 154v_1^2\omega_4^2 - 22c_s^2\omega_4^2 \\
C_8 &= -108v_1^2c_s^2\omega_4^2\omega_1^3 + 12\omega_9^2c_s^4\omega_1^3 - 19v_1^2\omega_9^2\omega_4^2\omega_1^3 - \omega_9^2c_s^4\omega_4^2\omega_1^3 + 6\omega_9^2c_s^2\omega_4^2\omega_1 + 18v_1^2\omega_9^2c_s^2\omega_4^2\omega_1^3 - \omega_9^2c_s^2\omega_4^2\omega_1^3 - 39v_1^4\omega_9\omega_4^3\omega_1^3 + 13\omega_9^2c_s^4\omega_4^3\omega_1^2 + \\
& 12\omega_9^2c_s^4\omega_4^3 + 36v_1^2\omega_9\omega_4\omega_1^3 + 252v_1^2\omega_9^2c_s^2\omega_4^3\omega_1^3 + 36v_1^4\omega_9\omega_4^3\omega_1^2 + 60v_1^2\omega_9^2c_s^2\omega_4^3\omega_1^3 - 6\omega_9^2c_s^2\omega_4^3\omega_1^2 - 18v_1^2\omega_9^2c_s^2\omega_4^3\omega_1 + 72v_1^4\omega_9\omega_4^3\omega_1^3 - \\
& 108v_1^2\omega_9c_s^2\omega_4\omega_1^3 - 3v_1^2\omega_9^2c_s^2\omega_4^3\omega_1^2 + \omega_9^2c_s^4\omega_4^3\omega_1^3 - 24\omega_9^2c_s^4\omega_4^3\omega_1 + 108v_1^2c_s^2\omega_4^3\omega_1^3 - 4v_1^2\omega_9^2\omega_4^3\omega_1^3 - 5\omega_9^2c_s^2\omega_4^3\omega_1^3 + 12v_1^2\omega_9^2c_s^2\omega_4^3\omega_1^3 - 90v_1^4\omega_9^2\omega_4\omega_1^3 + \\
& 6v_1^2\omega_9^2\omega_4^3\omega_1^3 - 108v_1^2c_s^2\omega_4^3\omega_1^2 + 6\omega_9^2c_s^4\omega_4^3\omega_1^2 + 36v_1^4\omega_4^3\omega_1^3 - 12\omega_9c_s^2\omega_4^3\omega_1 + 36v_1^2\omega_9c_s^2\omega_4^3\omega_1^2 + 19v_1^4\omega_9^2\omega_4^3\omega_1^3 + 6\omega_9c_s^2\omega_4^3\omega_1^3 + 39v_1^2\omega_9\omega_4^3\omega_1^3 + \\
& 6\omega_9c_s^4\omega_4^3\omega_1^3 - 12\omega_9^2c_s^4\omega_4\omega_1^2 + 36v_1^2\omega_4^3\omega_1^3 + 198v_1^2\omega_9c_s^2\omega_4^3\omega_1^3 - 12\omega_9c_s^2\omega_4^3\omega_1^2 - 12\omega_9^2c_s^2\omega_4^3\omega_1 + 36v_1^2\omega_9c_s^2\omega_4^3\omega_1^3 - 36v_1^4\omega_9\omega_4\omega_1^3 - 36v_1^4\omega_4^3\omega_1^2 - \\
& 72v_1^2\omega_9\omega_4^3\omega_1^3 - 12\omega_9^2c_s^4\omega_4\omega_1^3 - 18\omega_9c_s^4\omega_4^3\omega_1^3 - 36v_1^2\omega_9\omega_4^3\omega_1^2 - 36v_1^2\omega_4^3\omega_1^3 - 72v_1^2\omega_9\omega_4^3\omega_1^3 - 6\omega_9c_s^4\omega_4^3\omega_1^3 + 12\omega_9c_s^4\omega_4^3\omega_1 - 6\omega_9c_s^2\omega_4^3\omega_1^3 + \\
& 4v_1^4\omega_9\omega_4^3\omega_1^3 + 54v_1^2\omega_9c_s^2\omega_4^3\omega_1^2 + 12\omega_9^2c_s^2\omega_4\omega_1^2 - 306v_1^2\omega_9^2c_s^2\omega_4\omega_1^3 - 36v_1^4\omega_4^3\omega_1^3 + 90v_1^2\omega_9^2\omega_4\omega_1^3 + 12\omega_9c_s^4\omega_4^3\omega_1^2 + 36v_1^2\omega_4^3\omega_1^2 + 72v_1^4\omega_9^2\omega_1^3 + \\
& 12\omega_9^2c_s^2\omega_4\omega_1^3 - 36v_1^2\omega_9^2c_s^2\omega_4\omega_1^2 + 18\omega_9c_s^2\omega_4^3\omega_1^2 - 99v_1^2\omega_9c_s^2\omega_4^3\omega_1^3 - 6v_1^4\omega_9^2\omega_4^3\omega_1^2 \\
C_9 &= -12v_1^2\omega_9^2\omega_4^3\omega_1 - 12\omega_9\omega_4^2\omega_1 - 40\omega_9^2c_s^2\omega_4^3\omega_1 + 4v_1^2\omega_9^2\omega_4^2\omega_1^2 + 6\omega_9\omega_4^3\omega_1^2 + 12\omega_9\omega_4^3 + 12\omega_9^2c_s^2\omega_4^2\omega_1^2 - 36\omega_9c_s^2\omega_4^3 + 18\omega_9^2c_s^2\omega_4^2\omega_1 + \\
& 6v_1^2\omega_9^2\omega_4^2\omega_1 - 18\omega_9\omega_4^3\omega_1 + 18\omega_9^2\omega_4\omega_1^2 + 5\omega_9^2c_s^2\omega_4^3\omega_1^2 - 12v_1^2\omega_9\omega_4^3 + v_1^2\omega_9^2\omega_4^3\omega_1^2 - 6\omega_9\omega_4^2\omega_1^2 + 12v_1^2\omega_9^2\omega_4^3 + 12v_1^2\omega_9^2\omega_1^2 + 36\omega_9^2c_s^2\omega_4^3 + \\
& 54\omega_9c_s^2\omega_4^3\omega_1 + 36\omega_9^2c_s^2\omega_1^2 - 36c_s^2\omega_4^3\omega_1 + 12\omega_9^2\omega_4^3\omega_1 + 12v_1^2\omega_9\omega_4^2\omega_1 - 12v_1^2\omega_4^3\omega_1 + 18\omega_9c_s^2\omega_4^2\omega_1^2 - 36\omega_9^2c_s^2\omega_4^2 - 12\omega_4^3\omega_1^2 - 12v_1^2\omega_9^2\omega_4^2 - \\
& 12v_1^2\omega_4^2\omega_1^2 - 36c_s^2\omega_4^2\omega_1^2 - 4\omega_9^2\omega_4^2\omega_1^2 - 6v_1^2\omega_9\omega_4^3\omega_1^2 - 12\omega_9^2\omega_4^3 - 12\omega_9^2\omega_1^2 - 18v_1^2\omega_9^2\omega_4\omega_1^2 - 6\omega_9^2\omega_4^2\omega_1 + 18v_1^2\omega_9\omega_4^3\omega_1 + 36\omega_9c_s^2\omega_4^2\omega_1 + 12\omega_4^3\omega_1 - \\
& 54\omega_9^2c_s^2\omega_4\omega_1^2 + 36c_s^2\omega_4^3\omega_1^2 - \omega_9^2\omega_4^3\omega_1^2 + 12\omega_9^2\omega_4^2 + 6v_1^2\omega_9\omega_4^2\omega_1^2 + 12v_1^2\omega_4^3\omega_1^2 - 18\omega_9c_s^2\omega_4^3\omega_1^2 + 12\omega_4^2\omega_1^2 \\
C_{10} &= 36v_1^2\omega_9\omega_4\omega_1^2 - 24\omega_4\omega_1^2 + 12\omega_9\omega_1^2 + 24\omega_4\omega_1^3 - 12\omega_9c_s^2\omega_4\omega_1 - 12\omega_1^3 - 12\omega_9c_s^2\omega_1^2 + 12\omega_9c_s^2\omega_4\omega_1^2 + 72v_1^2\omega_4\omega_1^2 + 24c_s^2\omega_4\omega_1^2 - 36v_1^2\omega_9\omega_1^2 - \\
& 12\omega_9c_s^2\omega_4^2 - 24c_s^2\omega_4\omega_1^3 - 36v_1^2\omega_9\omega_4\omega_1 - 72v_1^2\omega_4\omega_1^3 - \omega_9c_s^2\omega_4^2\omega_1^3 - 12\omega_4^2\omega_1 - 12\omega_9\omega_4\omega_1^2 + 12c_s^2\omega_4^2\omega_1^3 + 36v_1^2\omega_4^2\omega_1^3 - 4\omega_9c_s^2\omega_4^2\omega_1^2 - 72v_1^2\omega_4^2\omega_1^2 - \\
& 24c_s^2\omega_4^2\omega_1^2 + 36v_1^2\omega_4^2\omega_1 + 12c_s^2\omega_4^2\omega_1 - 12\omega_4^2\omega_1^3 + 18\omega_9c_s^2\omega_4^2\omega_1 + 12c_s^2\omega_1^3 + 36v_1^2\omega_1^3 + 12\omega_9\omega_4\omega_1 + 24\omega_4^2\omega_1^2 \\
C_{11} &= -36c_s^2\omega_7^2 + 18c_s^2\omega_2^2\omega_1 + 12\omega_7^2\omega_1\omega_5 + v_2^2\omega_7^2\omega_1^2 - 12v_2^2\omega_7\omega_5 + 18c_s^2\omega_1^2\omega_5 + 3\omega_7\omega_1^2\omega_5 + 12\omega_7\omega_5 - \omega_7^2\omega_1^2 - 12v_2^2\omega_7^2 - 6\omega_7^2\omega_1 + \\
& 54c_s^2\omega_7\omega_1\omega_5 - 6\omega_7^2\omega_5 - 3v_2^2\omega_7\omega_1^2\omega_5 + 3c_s^2\omega_7^2\omega_1^2\omega_5 - 36c_s^2\omega_7\omega_5 + 6v_2^2\omega_1^2\omega_5 - 12v_2^2\omega_7^2\omega_1\omega_5 + 3c_s^2\omega_7^2\omega_1^2 + 6v_2^2\omega_7^2\omega_1 - 36c_s^2\omega_7^2\omega_1\omega_5 - \\
& 12v_2^2\omega_1\omega_5 + 36c_s^2\omega_7^2\omega_5 - 18c_s^2\omega_7\omega_1^2 + v_2^2\omega_7^2\omega_1^2\omega_5 + 12v_2^2\omega_7\omega_1 + 12\omega_7^2 - 12\omega_7\omega_1 - 9c_s^2\omega_7\omega_1^2\omega_5 + 12\omega_1\omega_5 + 18v_2^2\omega_7\omega_1\omega_5 - 18\omega_7\omega_1\omega_5 - \\
& 12\omega_7^2\omega_5 + 6\omega_7\omega_1^2 + 36c_s^2\omega_7\omega_1 - 6v_2^2\omega_7\omega_1^2 - \omega_7^2\omega_1^2\omega_5 - 36c_s^2\omega_1\omega_5 + 12\omega_2^2\omega_5 \\
C_{12} &= -6\omega_1^3\omega_5 - 18c_s^2\omega_1^2\omega_5 + \omega_7\omega_1^2\omega_5 + 18v_2^2\omega_1^3\omega_5 + 6\omega_1^3 + 18c_s^2\omega_7\omega_1\omega_5 + 6c_s^2\omega_1^2\omega_5 + 18\omega_1^2\omega_5 - 3v_2^2\omega_7\omega_1^2\omega_5 - 12c_s^2\omega_7\omega_5 - 54v_2^2\omega_1^2\omega_5 - \\
& 12\omega_1^2 + 36v_2^2\omega_1\omega_5 + 6c_s^2\omega_7\omega_1^2 - 36v_2^2\omega_7\omega_1 + 12\omega_7\omega_1 - 5c_s^2\omega_7\omega_1^2\omega_5 - 12\omega_1\omega_5 + c_s^2\omega_7\omega_1^3 + 3v_2^2\omega_7\omega_1^3 + 12c_s^2\omega_1^2\omega_5 - 6\omega_7\omega_1^2 - 18v_2^2\omega_1^3 - \\
& 12c_s^2\omega_7\omega_1 - 6c_s^2\omega_1^3 + 18v_2^2\omega_7\omega_1^2 + 36v_2^2\omega_1^2 + 12c_s^2\omega_1\omega_5 - c_s^2\omega_7\omega_1^3\omega_5 - \omega_7\omega_1^3
\end{aligned}$$

$$C_{13} = 12c_s^2\omega_7^2\omega_1 - 12v_2^2c_s^2\omega_7^2\omega_1^2 + 12v_2^2\omega_7^2\omega_1^2 - 3c_s^4\omega_7^3\omega_1^3 - 3v_2^2\omega_7^2\omega_1^3 + 6v_2^2c_s^2\omega_7^2\omega_1^2 + 24c_s^4\omega_7^2\omega_1^2 - 48c_s^4\omega_7\omega_1 - 12v_1^4\omega_7^2\omega_1^2 - 72v_2^4\omega_7^2\omega_1^2 + c_s^2\omega_7^2\omega_1^3 + 3v_2^3\omega_7^2\omega_1^3 - 8c_s^2\omega_7^2\omega_1^3 + 36v_2^3\omega_1^3 - 36v_2^2c_s^2\omega_7^2\omega_1 - 30v_2^2\omega_7\omega_1^3 + 24c_s^2\omega_7\omega_1 + 72v_2^2c_s^2\omega_7\omega_1 + 24c_s^4\omega_7^2 + 24c_s^4\omega_7\omega_1 + 72v_2^2\omega_7\omega_1^2 - 6c_s^2\omega_7\omega_1^3 + 30v_2^2\omega_7\omega_1^3 - 72v_2^2c_s^2\omega_7\omega_1^2 - 24c_s^4\omega_7\omega_1^2 - 36v_2^2\omega_1^3 + 108v_2^2c_s^2\omega_1^3 - 24c_s^2\omega_7\omega_1 + 144v_2^2c_s^2\omega_7\omega_1^2 - 72v_2^2\omega_7\omega_1^2 - 216v_2^2c_s^2\omega_1^3 + 72v_2^2\omega_1^3 + 6c_s^4\omega_7\omega_1^3$$

$$C_{14} = -12\omega_1^2c_s^4\omega_4\omega_2^2 - 4v_1^2\omega_1^2\omega_4^3\omega_2^2 + 36v_1^2\omega_4^3\omega_2^2 + 6\omega_1^2c_s^4\omega_4^3\omega_2^2 - 12\omega_1^2c_s^2\omega_4^3\omega_2 - 72v_1^2\omega_1^2\omega_2^3 + 6\omega_1^2c_s^2\omega_4^3\omega_2^2 + 36v_1^2\omega_1^2c_s^2\omega_4^3\omega_2^2 + 72v_1^4\omega_1^2\omega_4^3\omega_2^2 - 36v_1^4\omega_4^3\omega_2^2 - 18\omega_1^2c_s^4\omega_4^3\omega_2^2 + 6v_1^4\omega_1^2\omega_4^3\omega_2^2 - 12\omega_1^2c_s^4\omega_4\omega_2^2 - 90v_1^4\omega_1^2\omega_4\omega_2^2 - 12\omega_1^2c_s^2\omega_4^3\omega_2^2 - 36v_1^4\omega_4^3\omega_2^2 + 198v_1^4\omega_1^2c_s^2\omega_4^3\omega_2^2 + 36v_1^4\omega_1^2c_s^2\omega_4^3\omega_2 - 39v_1^4\omega_1^2\omega_4^3\omega_2^2 - 306v_1^2\omega_1^2c_s^2\omega_4\omega_2^2 + 12\omega_1^2c_s^2\omega_4\omega_2^2 + 54v_1^2\omega_1^2c_s^2\omega_4^3\omega_2^2 - 36v_1^4\omega_4^3\omega_2^2 - 6\omega_1^2c_s^2\omega_4^3\omega_2^2 - 6\omega_1^2c_s^4\omega_4^3\omega_2^2 + 12\omega_1^2c_s^4\omega_4^3\omega_2 + 72v_1^4\omega_1^2\omega_2^3 + 12\omega_1^2c_s^4\omega_4^3\omega_2^2 - 19v_1^2\omega_1^2\omega_2^3\omega_2^2 - 99v_1^2\omega_1^2c_s^2\omega_4^3\omega_2^2 + 36v_1^4\omega_4^3\omega_2^2 + 18\omega_1^2c_s^2\omega_4^3\omega_2^2 - 36v_1^4\omega_1^2c_s^2\omega_4\omega_2^2 + 12\omega_1^2c_s^2\omega_4\omega_2^2 + 252v_1^2\omega_1^2c_s^2\omega_2^3 + 36v_1^4\omega_1^2\omega_2^3\omega_2^2 + 36v_1^2\omega_1^2\omega_2\omega_4\omega_2^2 + 12\omega_1^2c_s^4\omega_4^3\omega_2^2 + 36v_1^2\omega_1^2\omega_2^3 + 6\omega_1^2c_s^2\omega_4^3\omega_2 - \omega_1^2c_s^2\omega_4^3\omega_2^2 + 4v_1^4\omega_1^2\omega_2^3\omega_2^2 + 18v_1^4\omega_1^2c_s^2\omega_4^3\omega_2^2 - 108v_1^2c_s^2\omega_4^3\omega_2^2 - 72v_1^4\omega_1^2\omega_4\omega_2^2 - \omega_1^2c_s^4\omega_4^3\omega_2^2 + 12\omega_1^2c_s^4\omega_4^3 - 6\omega_1^2c_s^2\omega_4^3\omega_2^2 + 60v_1^2\omega_1^2c_s^2\omega_4^3\omega_2^2 - 6v_1^4\omega_1^2\omega_2^3\omega_2^2 - 18v_1^4\omega_1^2c_s^2\omega_4^3\omega_2 + 90v_1^2\omega_1^2\omega_2^3\omega_2^2 + 108v_1^2c_s^2\omega_4^3\omega_2^2 + 13\omega_1^2c_s^4\omega_4^3\omega_2^2 + \omega_1^2c_s^4\omega_4^3\omega_2^2 + 39v_1^2\omega_1^2\omega_4\omega_2^2 - 24\omega_1^2c_s^4\omega_4^3\omega_2 + 19v_1^4\omega_1^2\omega_4\omega_2^2 - 3v_1^4\omega_1^2c_s^2\omega_4^3\omega_2^2 - 108v_1^2\omega_1^2c_s^2\omega_4\omega_2^2 - 36v_1^2\omega_1^2\omega_4\omega_2^2 + 6\omega_1^2c_s^4\omega_4^3\omega_2^2 - 108v_1^2c_s^2\omega_4^3\omega_2^2 + 12v_1^2\omega_1^2c_s^2\omega_4^3\omega_2^2 - 5\omega_1^2c_s^2\omega_4^3\omega_2^2 - 12\omega_1^2c_s^2\omega_2^3 - 36v_1^4\omega_1^2\omega_4\omega_2^2$$

$$C_{15} = 12\omega_1^3\omega_2^2 + 12\omega_3\omega_1^2\omega_2^2 - 2\omega_3\omega_1\omega_3\omega_1^2\omega_2^2 + 24\omega_3\omega_1^3\omega_2 - 24\omega_3\omega_1\omega_3\omega_2^2 - 12\omega_3\omega_1^3\omega_2^2 - 12\omega_1^2\omega_2^2 - 6\omega_3\omega_1\omega_3\omega_1^2\omega_2 + 12\omega_3\omega_1\omega_3\omega_2^2 - 12\omega_1^3\omega_2 - 12\omega_3\omega_1^2\omega_2 - \omega_3\omega_1\omega_3\omega_1^2\omega_2^2 - 6\omega_3\omega_1\omega_3\omega_2^2 + 12\omega_3\omega_1^3 - 6\omega_3\omega_1\omega_3\omega_2 + 12\omega_3\omega_1\omega_3\omega_1\omega_2 + 24\omega_3\omega_1\omega_3\omega_1\omega_2^2 - 2\omega_3\omega_1\omega_3\omega_2^2 - 12\omega_3\omega_1^3$$

$$C_{16} = -18\omega_1^2\omega_2^3\omega_2 + 6v_1^2\omega_1^2\omega_4^2\omega_2 + 18\omega_1^2\omega_4\omega_2^2 + 36c_s^2\omega_4^3\omega_2^2 + 12v_1^2\omega_4^3\omega_2^2 + 54\omega_1^2c_s^2\omega_4^3\omega_2 - 36\omega_1^2c_s^2\omega_4^2\omega_2 + 12\omega_4^2\omega_2^2 - 6\omega_1^2\omega_4^2\omega_2^2 + v_1^2\omega_1^2\omega_2^3\omega_2^2 + 12\omega_1^2\omega_2^3\omega_2 + 36\omega_1^2c_s^2\omega_4^3\omega_2 - 12v_1^2\omega_1^2\omega_2^3 + 18\omega_1^2c_s^2\omega_4^3\omega_2^2 + 12v_1^2\omega_1^2\omega_2^2 - 12\omega_1^2c_s^2\omega_4\omega_2^2 + 36\omega_1^2c_s^2\omega_4^3\omega_2^2 - 12v_1^2\omega_4^3\omega_2^2 - 12\omega_1^2\omega_2^3\omega_2 - 12v_1^2\omega_1^2\omega_4\omega_2 - 36c_s^2\omega_4^2\omega_2^2 - 18\omega_1^2c_s^2\omega_4^3\omega_2^2 + 12\omega_1^2\omega_4^3 + 6\omega_1^2\omega_4^3\omega_2^2 + 4v_1^2\omega_1^2\omega_2^3\omega_2^2 - 12\omega_1^2\omega_2^2 - 36c_s^2\omega_4^3\omega_2 - 12v_1^2\omega_4^3\omega_2 - 40\omega_1^2c_s^2\omega_4^3\omega_2 - 12\omega_1^2\omega_4^3 - 18v_1^2\omega_1^2\omega_4\omega_2^2 + 18v_1^2\omega_1^2\omega_4^2\omega_2 - 6\omega_1^2\omega_4^2\omega_2 + 12\omega_1^2c_s^2\omega_4^3\omega_2^2 + 12\omega_1^2\omega_4^3 + 6v_1^2\omega_1^2\omega_4^2\omega_2 - \omega_1^2\omega_4^3\omega_2^2 + 12v_1^2\omega_1^2\omega_4^2\omega_2 + 12\omega_1^2\omega_4^2\omega_2 + 18\omega_1^2c_s^2\omega_4^2\omega_2 + 36\omega_1^2c_s^2\omega_2^2 + 12v_1^2\omega_1^2\omega_4^3 - 6v_1^2\omega_1^2\omega_4^3\omega_2^2 - 4\omega_1^2\omega_4^2\omega_2^2 - 12v_1^2\omega_1^2\omega_4^3 + 5\omega_1^2c_s^2\omega_4^3\omega_2^2 - 36\omega_1^2c_s^2\omega_4^3$$

$$C_{17} = 36v_1^2\omega_2^3 + 12c_s^2\omega_2^3 - \omega_1^2c_s^2\omega_4^2\omega_2^3 - 12\omega_1^2c_s^2\omega_2^3 + 24\omega_4^2\omega_2^3 + 36v_1^2\omega_4^2\omega_2 - 36v_1^2\omega_1^2\omega_4\omega_2 + 12c_s^2\omega_4^2\omega_2 - 12\omega_4^2\omega_2^3 - 4\omega_1^2c_s^2\omega_4^2\omega_2^2 + 18\omega_1^2c_s^2\omega_4^2\omega_2 - 72v_1^2\omega_4^2\omega_2^2 + 36v_1^2\omega_1^2\omega_4\omega_2^2 - 24c_s^2\omega_4^2\omega_2^2 - 12\omega_4^2\omega_2 + 12c_s^2\omega_4^2\omega_2^3 + 36v_1^2\omega_4^2\omega_2^2 + 12\omega_1^2\omega_2^2 - 24c_s^2\omega_4\omega_2^3 - 72v_1^2\omega_4\omega_2^3 - 12\omega_2^3 - 12\omega_1^2c_s^2\omega_4\omega_2 + 72v_1^2\omega_4\omega_2^2 + 24c_s^2\omega_4\omega_2^2 + 12\omega_1^2\omega_4\omega_2 - 12\omega_1^2\omega_4\omega_2^2 + 24\omega_4\omega_2^3 - 12\omega_1^2c_s^2\omega_4^2 - 36v_1^2\omega_1^2\omega_2^2 + 12\omega_1^2c_s^2\omega_4\omega_2^2 - 24\omega_4\omega_2^2$$

$$C_{18} = -\omega_3\omega_1\omega_3\omega_1^2\omega_2^3 - 12\omega_3\omega_2^3 + 12\omega_3\omega_1^2\omega_2^2 - 2\omega_3\omega_1\omega_3\omega_1^2\omega_2^2 - 12\omega_3\omega_1^2\omega_2^3 + 12\omega_3\omega_2^3 - 12\omega_1^2\omega_2^2 - 6\omega_3\omega_1\omega_3\omega_2^3 + 24\omega_3\omega_1\omega_3\omega_1^2\omega_2 + 12\omega_1^2\omega_2^3 - 12\omega_1\omega_2^3 - 6\omega_3\omega_1\omega_3\omega_2^2 - 2\omega_3\omega_1\omega_3\omega_2^3 + 12\omega_3\omega_1\omega_3\omega_1\omega_2 - 6\omega_3\omega_1\omega_3\omega_1\omega_2^2 + 24\omega_3\omega_1\omega_3\omega_2^3 - 24\omega_3\omega_1\omega_3\omega_1^2 + 12\omega_3\omega_1\omega_3\omega_2 - 12\omega_3\omega_1\omega_2^3$$

$$C_{19} = 12\omega_6\omega_2 + 6\omega_8\omega_2^2 - \omega_6\omega_8\omega_2^2 - 36\omega_6c_s^2\omega_8 - 12v_3^2\omega_6\omega_8 - 36\omega_6c_s^2\omega_8^2\omega_2 + 6v_3^2\omega_8^2\omega_2 + 36c_s^2\omega_8\omega_2 - 12v_3^2\omega_6\omega_8^2\omega_2 + 12\omega_8^2 + v_3^2\omega_8^2\omega_2^2 - 18c_s^2\omega_8\omega_2^2 + v_3^2\omega_6\omega_8^2\omega_2^2 + 3\omega_6c_s^2\omega_8^2\omega_2^2 + 12\omega_6\omega_8^2\omega_2 + 36\omega_6c_s^2\omega_8^2 + 12v_3^2\omega_6\omega_8^2 - 6\omega_6\omega_2^2 - 12\omega_8\omega_2 - 18\omega_6\omega_8\omega_2 - 6\omega_8^2\omega_2 - 36c_s^2\omega_8^2 - 6v_3^2\omega_8\omega_2^2 - 36\omega_6c_s^2\omega_2 - 3v_3^2\omega_6\omega_8\omega_2^2 - 12v_3^2\omega_6\omega_2 + 3c_s^2\omega_8^2\omega_2^2 + 12\omega_6\omega_8 - 9\omega_6c_s^2\omega_8\omega_2^2 - 12\omega_6\omega_8^2 + 54\omega_6c_s^2\omega_8\omega_2 + 18\omega_6c_s^2\omega_2^2 + 12v_3^2\omega_8\omega_2 + 6v_3^2\omega_6\omega_2^2 + 18v_3^2\omega_6\omega_8\omega_2 + 18c_s^2\omega_8^2\omega_2 - \omega_8^2\omega_2^2 - 12v_3^2\omega_8^2 + 3\omega_6\omega_8\omega_2^2$$

$$C_{20} = -12\omega_6\omega_2 - 6c_s^2\omega_2^3 - 6\omega_8\omega_2^2 - 12\omega_6c_s^2\omega_8 - \omega_8\omega_2^3 + 12c_s^2\omega_2^2 - 12c_s^2\omega_8\omega_2 + 6c_s^2\omega_8\omega_2^2 - 6\omega_6\omega_2^3 + 36v_3^2\omega_2^2 + c_s^2\omega_8\omega_2^3 - 18v_3^2\omega_2^3 + 18\omega_6\omega_2^2 + 12\omega_8\omega_2 - 12\omega_2^2 + 3v_3^2\omega_8\omega_2^2 - \omega_6c_s^2\omega_8\omega_2^2 + 18v_3^2\omega_8\omega_2^2 + 12\omega_6c_s^2\omega_2 + 6\omega_2^3 - 3v_3^2\omega_6\omega_8\omega_2^2 + 36v_3^2\omega_6\omega_2 - 5\omega_6c_s^2\omega_8\omega_2^2 + 18\omega_6c_s^2\omega_8\omega_2 - 18\omega_6c_s^2\omega_2^2 - 36v_3^2\omega_8\omega_2 - 54v_3^2\omega_6\omega_2^2 + 18v_3^2\omega_6\omega_2^2 + \omega_6\omega_8\omega_2^2 + 6\omega_6c_s^2\omega_2^2$$

$$C_{21} = -12v_1^4\omega_2^2\omega_2^2 - 24c_s^4\omega_8\omega_2^2 + 144v_3^2c_s^2\omega_8\omega_2^2 + 6c_s^4\omega_8\omega_2^3 + 3v_3^4\omega_2^3\omega_2^3 - 24c_s^2\omega_8\omega_2 - 72v_3^2c_s^2\omega_8\omega_2^2 + 24c_s^4\omega_2^2 + 12v_3^2\omega_8^2\omega_2^2 + 24c_s^2\omega_8\omega_2^2 + 72v_3^2\omega_2^2 - 6c_s^2\omega_8\omega_2^2 + 72v_3^2c_s^2\omega_8\omega_2 - 3v_3^2\omega_8^2\omega_2^2 - 36v_3^2\omega_2^2 + 24c_s^4\omega_8\omega_2 - 36v_3^2c_s^2\omega_8^2\omega_2 + c_s^2\omega_8^2\omega_2^2 - 216v_3^2c_s^2\omega_2^2 + 30v_3^2\omega_8\omega_2^2 - 48c_s^4\omega_2^2\omega_2^2 - 72v_3^2\omega_8\omega_2^2 + 108v_3^2c_s^2\omega_2^2 - 8c_s^2\omega_8^2\omega_2^2 - 3c_s^4\omega_8^2\omega_2^2 - 30v_3^2\omega_8\omega_2^2 + 36v_3^4\omega_2^2 + 6v_3^2c_s^2\omega_8^2\omega_2^2 + 12c_s^2\omega_8^2\omega_2 + 72v_3^4\omega_8\omega_2^2 + 24c_s^4\omega_2^2\omega_2^2 - 12v_3^2c_s^2\omega_8^2\omega_2^2 - 72v_3^4\omega_2^2$$

2.6.4 Conservation of momentum: ρv_2



attached text file: output_d3q27_nse_culbm1_symbolic_pde_02.txt

$$\begin{aligned} & v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_2 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_2 \delta_l \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_1} + (v_2^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2v_2 \delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 v_3 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \delta_l \rho}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\ & \frac{v_2 \delta_l \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\ & (-2 - 3v_2^2\omega_5 - 2c_s^2\omega_5 + 6v_2^2 + \omega_5 + 4c_s^2) \frac{\delta_l^2}{\delta_t \omega_5} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + (2 - \omega_5) \frac{3v_2 \delta_l^2 \rho}{\delta_t \omega_5} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\ & (-2 + \omega_3) \frac{c_s^2 \delta_l^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2 \rho}{2\delta_t \omega_1} \frac{\partial^2 v_2}{\partial x_1^2} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2 \rho}{2\delta_t \omega_1} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\ & (-2 - v_2^2\omega_5 - 3c_s^2\omega_5 + 2v_2^2 + \omega_5 + 6c_s^2) \frac{v_2 \delta_l^2}{2\delta_t \omega_5} \frac{\partial^2 \rho}{\partial x_2^2} + (-2 - 3v_2^2\omega_5 - c_s^2\omega_5 + 6v_2^2 + \omega_5 + 2c_s^2) \frac{\delta_l^2 \rho}{2\delta_t \omega_5} \frac{\partial^2 v_2}{\partial x_2^2} + \\ & (-2 + \omega_3) \frac{c_s^2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_3) \frac{c_s^2 \delta_l^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_3^2} + (-1 + v_1^2 + 3c_s^2) \frac{v_2 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_2 \delta_l^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + \\ & C_1 \frac{v_1 \delta_l^3 \rho}{6\omega_9 \delta_t \omega_1} \frac{\partial^3 v_2}{\partial x_1^3} + (-12 - \omega_1^2 + 12\omega_1) \frac{c_s^4 \delta_l^3}{6\delta_t \omega_1^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} - \frac{v_2 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_2 \frac{v_2 \delta_l^3 \rho}{12\delta_t \omega_7 \omega_1 \omega_5^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_3 \frac{\delta_l^3}{12\delta_t \omega_5^2} \frac{\partial^3 \rho}{\partial x_2^2} + \\ & (-24 - 60v_2^2\omega_5 - 36c_s^2\omega_5 + 60v_2^2 + 5c_s^2\omega_5^2 + 11v_2^2\omega_5^2 + 24\omega_5 + 36c_s^2 - 4\omega_5^2) \frac{v_2 \delta_l^3 \rho}{6\delta_t \omega_5^2} \frac{\partial^3 v_2}{\partial x_2^2} - \frac{v_2 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\ & C_4 \frac{v_2 \delta_l^3 \rho}{12\omega_3 \delta_t \omega_{11} \omega_5^2} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{v_2 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + (-12 - \omega_3^2 + 12\omega_3) \frac{c_s^4 \delta_l^3}{6\omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{v_2 c_s^2 \delta_l^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \end{aligned}$$

$$\begin{aligned}
& (-1 + v_3^2 + 3c_s^2) \frac{v_2 v_3 \delta_t^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_5 \frac{v_3 \delta_t^3 \rho}{6\omega_3 \delta_t \omega_{10}} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + 3v_3^2 + c_s^2) \frac{v_2 \delta_t^3 \rho}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (2c_s^4 - 3v_1^4 \omega_4 - c_s^4 \omega_4 - 6v_1^2 + 24v_1^2 c_s^2 + 6v_1^4 + 3v_1^2 \omega_4 + c_s^2 \omega_4 - 2c_s^2 - 12v_1^2 c_s^2 \omega_4) \frac{v_2 \delta_t^4 \rho}{24\delta_t \omega_4} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 10v_1^2 + 2\omega_4 - 5v_1^2 \omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_2 v_1 \delta_t^4 \rho}{12\delta_t \omega_4} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\delta_t^4 \rho}{24\omega_9 \delta_t \omega_1^3} \frac{\partial^4 v_2}{\partial x_1^4} + C_7 \frac{v_1 c_s^2 \delta_t^4}{12\omega_9 \delta_t \omega_4 \omega_1^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + \\
& C_8 \frac{c_s^2 \delta_t^4 \rho}{12\omega_9 \delta_t \omega_4 \omega_1^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + (-\omega_9 + 3\omega_9 c_s^2 \omega_4 + v_1^2 \omega_9 \omega_4 - \omega_9 \omega_4 + 3\omega_4 + v_1^2 \omega_9 - 3v_1^2 \omega_4 - 9c_s^2 \omega_4 + 3\omega_9 c_s^2) \frac{v_2 v_1 \delta_t^4 \rho}{12\omega_9 \delta_t \omega_4} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} \\
& + C_9 \frac{v_2 c_s^2 \delta_t^4}{12\delta_t \omega_7^2 \omega_1^2 \omega_5^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{10} \frac{c_s^2 \delta_t^4 \rho}{12\delta_t \omega_7 \omega_1^3 \omega_5^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{11} \frac{\delta_t^4 \rho}{12\delta_t \omega_7^2 \omega_1^3 \omega_5^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{12} \frac{v_2 \delta_t^4}{12\delta_t \omega_5^3} \frac{\partial^4 \rho}{\partial x_2^4} + C_{13} \frac{\delta_t^4 \rho}{12\delta_t \omega_5^3} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& (-\omega_{12} - \omega_{12} \omega_4 + v_1^2 \omega_{12} \omega_4 + 3\omega_4 - 3v_1^2 \omega_4 - 9c_s^2 \omega_4 + 3\omega_{12} c_s^2 \omega_4 + v_1^2 \omega_{12} + 3\omega_{12} c_s^2) \frac{v_2 v_1 \delta_t^4 \rho}{12\omega_{12} \delta_t \omega_4} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\
& C_{14} \frac{c_s^4 \delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{13} \omega_1^3 \omega_2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{15} \frac{\delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{11}^3 \omega_5^3} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + (-2 + \omega_2) \frac{v_2 c_s^4 \delta_t^4}{6\delta_t \omega_2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& (-\omega_3^2 \omega_1^2 - \omega_3^2 + 2\omega_3^2 \omega_1 + \omega_3 \omega_{13} - \omega_1^2 - \omega_3 \omega_{13} \omega_1 - 2\omega_3 \omega_1 + 2\omega_3 \omega_1^2 + \omega_{13} \omega_1) \frac{c_s^4 \delta_t^4 \rho}{\omega_3^2 \delta_t \omega_{13} \omega_1^2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_3^2} + \\
& C_{16} \frac{c_s^4 \delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{13} \omega_1^3 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{17} \frac{v_2 c_s^2 \delta_t^4}{12\omega_3^3 \delta_t \omega_{11}^3 \omega_5^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{18} \frac{c_s^2 \delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{11}^3 \omega_5^2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (3\omega_6 c_s^2 \omega_8 + v_3^2 \omega_6 \omega_8 + 3\omega_6 - 9\omega_6 c_s^2 + v_3^2 \omega_8 - 3v_3^2 \omega_6 - \omega_6 \omega_8 - \omega_8 + 3c_s^2 \omega_8) \frac{v_2 v_3 \delta_t^4 \rho}{12\omega_6 \delta_t \omega_8} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{19} \frac{v_3 c_s^2 \delta_t^4}{12\omega_6 \omega_3^2 \delta_t \omega_{10}^2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} \\
& + (3\omega_6 - 9\omega_6 c_s^2 + 3c_s^2 \omega_{10} + v_3^2 \omega_{10} - \omega_{10} - \omega_6 \omega_{10} - 3v_3^2 \omega_6 + 3\omega_6 c_s^2 \omega_{10} + v_3^2 \omega_6 \omega_{10}) \frac{v_2 v_3 \delta_t^4 \rho}{12\omega_6 \delta_t \omega_{10}} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& C_{20} \frac{c_s^2 \delta_t^4 \rho}{12\omega_6 \omega_3^3 \delta_t \omega_{10}} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + (-3v_3^4 \omega_6 + 24v_3^2 c_s^2 + 2c_s^4 + \omega_6 c_s^2 - 6v_3^2 - 12v_3^2 \omega_6 c_s^2 + 3v_3^2 \omega_6 + 6v_3^4 - 2c_s^2 - \omega_6 c_s^4) \frac{v_2 \delta_t^4}{24\omega_6 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} \\
& + C_{21} \frac{\delta_t^4 \rho}{24\omega_3^3 \delta_t \omega_{10}^3} \frac{\partial^4 v_3}{\partial x_3^4} + (-4 + 2\omega_6 - 3\omega_6 c_s^2 + 10v_3^2 - 5v_3^2 \omega_6 + 6c_s^2) \frac{v_2 v_3 \delta_t^4 \rho}{12\omega_6 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 3\omega_9 - v_1^2 \omega_9 \omega_1 - 3\omega_9 c_s^2 \omega_1 + \omega_9 \omega_1 - 6v_1^2 + 3v_1^2 \omega_9 - 3\omega_1 + 9\omega_9 c_s^2 + 3v_1^2 \omega_1 + 9c_s^2 \omega_1 - 18c_s^2 \\
C_2 &= 18c_s^2 \omega_7 \omega_5^2 - 11c_s^2 \omega_7 \omega_1 \omega_5^2 - 36c_s^2 \omega_5^2 - 18c_s^2 \omega_7 \omega_1 \omega_5 - 6\omega_7 \omega_5^2 + 6v_2^2 \omega_7 \omega_5^2 - 12v_2^2 \omega_5^2 + 36c_s^2 \omega_1 \omega_5^2 - 12v_2^2 \omega_1 \omega_5 + 12v_2^2 \omega_7 \omega_1 - 12\omega_7 \omega_1 + \\
& 3\omega_7 \omega_1 \omega_5^2 + 12\omega_1 \omega_5 - 6v_2^2 \omega_7 \omega_1 \omega_5 - 12\omega_1 \omega_5^2 + 6\omega_7 \omega_1 \omega_5 - 3v_2^2 \omega_7 \omega_1 \omega_5^2 + 36c_s^2 \omega_7 \omega_1 + 12\omega_5^2 - 36c_s^2 \omega_1 \omega_5 + 12v_2^2 \omega_1 \omega_5^2 \\
C_3 &= -144v_2^2 c_s^2 \omega_5 + 36v_2^2 \omega_5 + 12c_s^4 + 12c_s^2 \omega_5 + 144v_2^2 c_s^2 - 36v_2^2 - c_s^2 \omega_5^2 + 24v_2^2 c_s^2 \omega_5^2 - 7v_2^4 \omega_5^2 + 36v_2^4 - 12c_s^4 \omega_5 - 36v_2^4 \omega_5 + 7v_2^4 \omega_5^2 - 12c_s^2 + c_s^4 \omega_5^2 \\
C_4 &= -12v_2^2 \omega_3 \omega_5 - 3v_2^2 \omega_3 \omega_{11} \omega_5^2 + 6\omega_3 \omega_{11} \omega_5 + 36\omega_3 c_s^2 \omega_5^2 + 6v_2^2 \omega_{11} \omega_5^2 - 6\omega_{11} \omega_5^2 + 12\omega_3 \omega_5 - 36c_s^2 \omega_5^2 - 12\omega_3 \omega_5^2 - 36\omega_3 c_s^2 \omega_5 + 18c_s^2 \omega_{11} \omega_5^2 + \\
& 12v_2^2 \omega_3 \omega_5^2 - 6v_2^2 \omega_3 \omega_{11} \omega_5 - 12v_2^2 \omega_5^2 + 3\omega_3 \omega_{11} \omega_5^2 + 36\omega_3 c_s^2 \omega_{11} - 18\omega_3 c_s^2 \omega_{11} \omega_5 - 11\omega_3 c_s^2 \omega_{11} \omega_5^2 - 12\omega_3 \omega_{11} + 12\omega_5^2 + 12v_2^2 \omega_3 \omega_{11} \\
C_5 &= 6 + \omega_3 \omega_{10} + 9c_s^2 \omega_{10} - 3\omega_3 + 3v_3^2 \omega_{10} - 3\omega_{10} - 6v_3^2 + 9\omega_3 c_s^2 - 3\omega_3 c_s^2 \omega_{10} - v_3^2 \omega_3 \omega_{10} + 3v_3^2 \omega_3 - 18c_s^2 \\
C_6 &= -3\omega_9^2 c_s^4 \omega_1^3 - 30v_1^4 \omega_9 \omega_1^3 - 12v_1^2 \omega_9^2 c_s^2 \omega_1^2 + 72v_1^4 \omega_9 \omega_1^2 + 24\omega_9^2 c_s^4 \omega_1^2 - 24\omega_9 c_s^2 \omega_1 + 6v_1^2 \omega_9^2 c_s^2 \omega_1^3 + 24\omega_9 c_s^2 \omega_1^2 + 36v_1^4 \omega_1^3 + 30v_1^2 \omega_9 \omega_1^3 - \\
& 48\omega_9^2 c_s^4 \omega_1 - 72v_1^2 \omega_9 \omega_1^2 - 72v_1^4 \omega_1^2 - 36v_1^2 \omega_9^2 c_s^2 \omega_1 - 6\omega_9 c_s^2 \omega_1^3 - 216v_1^2 c_s^2 \omega_1^2 + 12v_1^2 \omega_9^2 \omega_1^2 - 8\omega_9^2 c_s^2 \omega_1^2 + 24\omega_9 c_s^2 \omega_1 + \omega_9^2 c_s^2 \omega_1^3 + 72v_1^2 \omega_9 c_s^2 \omega_1 + \\
& 108v_1^2 c_s^2 \omega_1^3 - 3v_1^2 \omega_9^2 \omega_1^3 + 24\omega_9^2 c_s^4 - 12v_1^4 \omega_9^2 \omega_1^2 + 72v_1^2 \omega_1^2 + 6\omega_9 c_s^4 \omega_1^3 + 144v_2^2 \omega_9 c_s^2 \omega_1^2 - 24\omega_9 c_s^4 \omega_1^2 - 36v_1^2 \omega_1^3 + 3v_1^4 \omega_5^2 \omega_1^3 - 72v_1^2 \omega_9 c_s^2 \omega_1^3 + 12\omega_9^2 c_s^2 \omega_1 \\
C_7 &= -3v_1^2 \omega_9 \omega_4 \omega_1^2 + 12v_1^2 \omega_9 \omega_1 - 6\omega_4 \omega_1^2 - 36\omega_9 c_s^2 \omega_4 - 12v_1^2 \omega_4 \omega_1 + 12\omega_9^2 \omega_4 \omega_1 + 6\omega_9 \omega_1^2 - 36c_s^2 \omega_4 \omega_1 + 36\omega_9 c_s^2 \omega_1 + 54\omega_9 c_s^2 \omega_4 \omega_1 - \\
& 12v_1^2 \omega_9 \omega_4 - 18\omega_9 c_s^2 \omega_1^2 - 9\omega_9 c_s^2 \omega_4 \omega_1^2 + 6v_1^2 \omega_4 \omega_1^2 - 12\omega_9 \omega_1 - \omega_9^2 \omega_4 \omega_1^2 + 18c_s^2 \omega_4 \omega_1^2 + 12\omega_9^2 - 6v_1^2 \omega_9 \omega_1^2 + 12\omega_4 \omega_1 + 18v_1^2 \omega_9 \omega_4 \omega_1 + 12\omega_9 \omega_4 - \\
& 36\omega_9^2 c_s^2 + v_1^2 \omega_9 \omega_1^2 + 3\omega_9^2 c_s^2 \omega_1^2 - 12\omega_9^2 \omega_4 + 3\omega_9 \omega_4 \omega_1^2 - 36\omega_9^2 c_s^2 \omega_4 \omega_1 - 6\omega_9^2 \omega_1 - 12v_1^2 \omega_9^2 \omega_4 \omega_1 - \omega_9^2 \omega_1^2 + v_1^2 \omega_9^2 \omega_4 \omega_1^2 + 36\omega_9^2 c_s^2 \omega_4 + 3\omega_9^2 c_s^2 \omega_4 \omega_1^2 + \\
& 12v_1^2 \omega_9^2 \omega_4 - 18\omega_9 \omega_4 \omega_1 + 6v_1^2 \omega_9 \omega_1 - 12v_1^2 \omega_9^2 + 18\omega_9^2 c_s^2 \omega_1 \\
C_8 &= -3v_1^2 \omega_9 \omega_4 \omega_1^2 - \omega_9 \omega_1^3 - 36v_1^2 \omega_9 \omega_1 + 18\omega_4 \omega_1^2 - 12\omega_9 c_s^2 \omega_4 + 36v_1^2 \omega_4 \omega_1 - 6\omega_9 \omega_1^2 + 12c_s^2 \omega_4 \omega_1 - 12\omega_9 c_s^2 \omega_1 - 6\omega_4 \omega_1^3 + 18\omega_9 c_s^2 \omega_4 \omega_1 + \\
& 6\omega_1^3 + 6\omega_9 c_s^2 \omega_1^2 - 5\omega_9 c_s^2 \omega_4 \omega_1^2 + 3v_1^2 \omega_9 \omega_1^3 - 54v_1^2 \omega_4 \omega_1^2 + 12\omega_9 \omega_1 - 18c_s^2 \omega_4 \omega_1^2 + 18v_1^2 \omega_9 \omega_1^2 - \omega_9 c_s^2 \omega_4 \omega_1^3 - 12\omega_4 \omega_1 - 12\omega_1^2 + \omega_9 c_s^2 \omega_1^3 + \\
& 6c_s^2 \omega_4 \omega_1^3 + 18v_1^2 \omega_4 \omega_1^3 + \omega_9 \omega_4 \omega_1^2 + 36v_1^2 \omega_1^2 + 12c_s^2 \omega_1^2 - 6c_s^2 \omega_1^3 - 18v_1^2 \omega_1^3 \\
C_9 &= 6v_2^2 \omega_7^2 \omega_1^2 \omega_5^2 - 6v_2^2 \omega_7 \omega_1^2 \omega_5^3 - 12\omega_1^2 \omega_5^3 + 12v_2^2 \omega_7^2 \omega_1^2 + 12c_s^2 \omega_7^2 \omega_1^2 \omega_5^2 + 54c_s^2 \omega_7 \omega_1 \omega_5^3 - 12v_2^2 \omega_1^2 \omega_5^2 + 12\omega_1^2 \omega_5^2 + 6v_2^2 \omega_7 \omega_1^2 \omega_5^2 - 12v_2^2 \omega_7^2 \omega_1 \omega_5^3 + \\
& 12v_2^2 \omega_1^2 \omega_5^3 - 12\omega_7^2 \omega_1^2 - 36c_s^2 \omega_7 \omega_1^3 + 36c_s^2 \omega_7 \omega_1 \omega_5^2 + 5c_s^2 \omega_7^2 \omega_1^2 \omega_5^3 + 36c_s^2 \omega_1^2 \omega_5^3 - 12v_2^2 \omega_7 \omega_1^3 - 6\omega_7 \omega_1^2 \omega_5^2 + 12\omega_7^2 \omega_1 \omega_5^3 - 54c_s^2 \omega_7^2 \omega_1^2 \omega_5 - \\
& 36c_s^2 \omega_1^2 \omega_5^2 + 12\omega_7 \omega_5^2 + 36c_s^2 \omega_7^2 \omega_1^2 - 6\omega_7^2 \omega_1 \omega_5^2 + 6\omega_7 \omega_1^2 \omega_5^3 - 12v_2^2 \omega_7^2 \omega_5^2 - 12\omega_7^2 \omega_5^3 - 18v_2^2 \omega_7^2 \omega_1^2 \omega_5 - 18\omega_7 \omega_1 \omega_5^3 - 4\omega_7^2 \omega_1^2 \omega_5^2 + 12v_2^2 \omega_7^2 \omega_5^3 - \\
& 36c_s^2 \omega_1 \omega_5^3 - \omega_7^2 \omega_1^2 \omega_5^3 - 12\omega_7 \omega_1 \omega_5^2 + 12\omega_7^2 \omega_5^2 + v_2^2 \omega_7^2 \omega_1^2 \omega_5^3 + 12v_2^2 \omega_7 \omega_1 \omega_5^2 + 36c_s^2 \omega_7^2 \omega_5^3 - 12v_2^2 \omega_1 \omega_5^3 - 40c_s^2 \omega_7^2 \omega_1 \omega_5^3 + 18c_s^2 \omega_7 \omega_1^2 \omega_5^2 + \\
& 18v_2^2 \omega_7 \omega_1 \omega_5^3 + 4v_2^2 \omega_7^2 \omega_5^2 + 12\omega_1 \omega_5^3 + 18\omega_7^2 \omega_1^2 \omega_5 - 18c_s^2 \omega_7 \omega_1^2 \omega_5^3 + 18c_s^2 \omega_7^2 \omega_1 \omega_5^2 - 36c_s^2 \omega_7^2 \omega_5^2 \\
C_{10} &= 24\omega_1^3 \omega_5 + 24c_s^2 \omega_1^2 \omega_5 - 12c_s^2 \omega_7 \omega_5^2 - 72v_2^2 \omega_1^2 \omega_5^2 + 24\omega_1^2 \omega_5^2 - 12\omega_7 \omega_1^2 \omega_5 - 72v_2^2 \omega_1^3 \omega_5 + 18c_s^2 \omega_7 \omega_1 \omega_5^2 + 12c_s^2 \omega_1^3 \omega_5^2 - 12\omega_1^3 + 36v_2^2 \omega_1^3 \omega_5^2 - \\
& 12c_s^2 \omega_7 \omega_1 \omega_5 - 24c_s^2 \omega_1^3 \omega_5 - 24\omega_1^2 \omega_5 + 36v_2^2 \omega_7 \omega_1^2 \omega_5 - 24c_s^2 \omega_1^2 \omega_5^2 + 72v_2^2 \omega_1^2 \omega_5 - 12\omega_1^3 \omega_5^2 + 12c_s^2 \omega_1 \omega_5^2 - c_s^2 \omega_7 \omega_1^2 \omega_5^2 - 12c_s^2 \omega_7 \omega_1^2 + \\
& 12c_s^2 \omega_7 \omega_1^2 \omega_5 - 36v_2^2 \omega_7 \omega_1 \omega_5 - 12\omega_1 \omega_5^2 + 12\omega_7 \omega_1 \omega_5 + 12\omega_7 \omega_1^2 - 4c_s^2 \omega_7 \omega_1^2 \omega_5^2 + 36v_2^2 \omega_1^3 + 12c_s^2 \omega_1^3 - 36v_2^2 \omega_7 \omega_1^2 + 36v_2^2 \omega_1 \omega_5^2 \\
C_{11} &= 36v_2^2 \omega_7 \omega_1^3 \omega_5 - 108v_2^2 c_s^2 \omega_7 \omega_1^3 \omega_5 - 36v_2^4 \omega_1^3 \omega_5^2 - 36v_2^2 \omega_7 \omega_1^2 \omega_5^3 + 54v_2^2 c_s^2 \omega_7 \omega_1^2 \omega_5^3 - 6c_s^4 \omega_7 \omega_1^3 \omega_5^2 - 6c_s^2 \omega_7^2 \omega_1^2 \omega_5^2 - 12c_s^2 \omega_7 \omega_1 \omega_5^3 + \\
& 4v_2^2 \omega_7^2 \omega_1^3 \omega_5^2 + 12c_s^2 \omega_7^2 \omega_1^3 - 72v_2^2 \omega_7^2 \omega_1^3 + 252v_2^2 c_s^2 \omega_7^2 \omega_1^3 + 6c_s^4 \omega_7 \omega_1^3 \omega_5^2 + 36v_2^2 c_s^2 \omega_7 \omega_1^2 \omega_5^2 - 18v_2^2 c_s^2 \omega_7^2 \omega_1 \omega_5^2 + 36v_2^2 \omega_1^3 \omega_5^2 + 36v_2^2 \omega_1^2 \omega_5^3 -
\end{aligned}$$

$$108v_2^2c_s^2\omega_5^3 + 19v_2^4\omega_7^2\omega_5^3 + 12c_s^2\omega_7^2\omega_5^3 - 5c_s^2\omega_7^2\omega_5^3 - 6v_2^4\omega_7^2\omega_5^3 + 36v_2^2\omega_5^3\omega_7^2 - 108v_2^2c_s^2\omega_5^3\omega_7^2 - 90v_2^4\omega_7^2\omega_5^3\omega_7^2 - c_s^2\omega_7^2\omega_5^3\omega_7^2 - 24c_s^4\omega_7^2\omega_5^3 + 12c_s^4\omega_7^2\omega_5^3 - 12c_s^2\omega_7^2\omega_5^3 - 99v_2^2c_s^2\omega_7^2\omega_5^3 + 39v_2^2\omega_7^2\omega_5^3 + 12c_s^2\omega_7^2\omega_5^3 + 72v_2^4\omega_7^2\omega_5^3 + 108v_2^2c_s^2\omega_5^3\omega_7^2 - 36v_2^2\omega_5^3\omega_7^2 + 198v_2^2c_s^2\omega_7^2\omega_5^3 - 72v_2^2\omega_7^2\omega_5^3 - 36v_2^4\omega_7^2\omega_5^3 - 18c_s^4\omega_7^2\omega_5^3 + 6c_s^2\omega_7^2\omega_5^3 - 36v_2^4\omega_7^2\omega_5^3 + 36v_2^2\omega_7^2\omega_5^3 + 12v_2^2c_s^2\omega_7^2\omega_5^3 - 4v_2^2\omega_7^2\omega_5^3 - 36v_2^2c_s^2\omega_7^2\omega_5^3 + 12c_s^4\omega_7^2\omega_5^3 + 6c_s^4\omega_7^2\omega_5^3 + 12c_s^4\omega_7^2\omega_5^3 - 6c_s^2\omega_7^2\omega_5^3 - 12c_s^4\omega_7^2\omega_5^3 + 13c_s^4\omega_7^2\omega_5^3 + 60v_2^2c_s^2\omega_7^2\omega_5^3 - 19v_2^2\omega_7^2\omega_5^3 + c_s^4\omega_7^2\omega_5^3 + 6v_2^2\omega_7^2\omega_5^3 - 3v_2^2c_s^2\omega_7^2\omega_5^3 + 90v_2^2\omega_7^2\omega_5^3 - 306v_2^2c_s^2\omega_7^2\omega_5^3 - 39v_2^4\omega_7^2\omega_5^3 + 6c_s^2\omega_7^2\omega_5^3 - 12c_s^2\omega_7^2\omega_5^3 + 36v_2^2c_s^2\omega_7^2\omega_5^3 + 18v_2^2c_s^2\omega_7^2\omega_5^3 - 12c_s^4\omega_7^2\omega_5^3 - c_s^4\omega_7^2\omega_5^3 + 18c_s^2\omega_7^2\omega_5^3 + 72v_2^4\omega_7^2\omega_5^3$$

$$C_{12} = 12 - 1008v_2^2c_s^2\omega_5 + 234v_2^2\omega_5 + 144c_s^4 + 198c_s^2\omega_5 + 672v_2^2c_s^2 - 156v_2^2 - 78c_s^2\omega_5^2 + 10v_2^2\omega_5^3 - 34v_2^2c_s^2\omega_5^3 + 6c_s^2\omega_5^3 + 404v_2^2c_s^2\omega_5^2 - 98v_2^2\omega_5^2 + 144v_2^4 - 216c_s^4\omega_5 - 216v_2^4\omega_5 - 5c_s^4\omega_5^3 - \omega_5^3 - 18\omega_5 + 90v_2^4\omega_5^2 - 132c_s^4 + 82c_s^4\omega_5^2 + 8\omega_5^2 - 9v_2^4\omega_5^3$$

$$C_{13} = 12 - 648v_2^2c_s^2\omega_5 + 378v_2^2\omega_5 + 24c_s^4 + 54c_s^2\omega_5 + 432v_2^2c_s^2 - 252v_2^2 - 22c_s^2\omega_5^2 + 14v_2^2\omega_5^3 - 18v_2^2c_s^2\omega_5^3 + 2c_s^2\omega_5^3 + 252v_2^2c_s^2\omega_5^2 - 154v_2^2\omega_5^2 + 504v_2^4 - 36c_s^4\omega_5 - 756v_2^4\omega_5 - c_s^4\omega_5^3 - \omega_5^3 - 18\omega_5 + 310v_2^4\omega_5^2 - 36c_s^4 + 14c_s^4\omega_5^2 + 8\omega_5^2 - 29v_2^4\omega_5^3$$

$$C_{14} = 12\omega_2^2\omega_1^3 - 6\omega_3^2\omega_{13}\omega_1^2 - 12\omega_3^2\omega_1^2 + 24\omega_3^2\omega_{13}\omega_1\omega_2 + 24\omega_3\omega_1^3\omega_2 - 2\omega_2^2\omega_{13}\omega_1^3 - 6\omega_3\omega_{13}\omega_1^2\omega_2 + 12\omega_2^2\omega_{13}\omega_1 - 12\omega_3^3\omega_2 - 12\omega_3\omega_1^2\omega_2 - 24\omega_3^2\omega_{13}\omega_2 - \omega_3^2\omega_{13}\omega_1^2\omega_2 + 12\omega_{13}\omega_1^2 + 12\omega_3^2\omega_1^2\omega_2 + 12\omega_3\omega_{13}\omega_1\omega_2 - 2\omega_3^2\omega_{13}\omega_1^2\omega_2 - 12\omega_3\omega_1^3 - 6\omega_3\omega_{13}\omega_1^3 - 12\omega_3^2\omega_1^3\omega_2$$

$$C_{15} = 6v_2^2\omega_3^2\omega_{11}^3\omega_5^3 + 6\omega_3^2c_s^2\omega_{11}^3\omega_5^3 + 12v_2^2\omega_3^2c_s^2\omega_{11}^3\omega_5^3 + 36v_2^2\omega_3^2\omega_{11}\omega_5 - 108v_2^2\omega_3^2c_s^2\omega_5^2 + 19v_2^4\omega_3^2\omega_{11}^2\omega_5^2 - 6\omega_3^2c_s^2\omega_{11}\omega_5^3 + 36v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 + 12\omega_3^2c_s^4\omega_{11}\omega_5^3 + 60v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 - 18\omega_3^2c_s^4\omega_{11}\omega_5^3 - 72v_2^2\omega_3^2\omega_{11}^2\omega_5^3 + 6\omega_3^2c_s^2\omega_{11}\omega_5^2 + 12\omega_3^2c_s^4\omega_{11}^2\omega_5^3 - 36v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 + 4v_2^2\omega_3^2\omega_{11}\omega_5^3 + 108v_2^2\omega_3^2c_s^2\omega_5^3 + 18v_2^2\omega_3^2c_s^2\omega_{11}^2\omega_5^3 - 24\omega_3^2c_s^4\omega_{11}^2\omega_5^3 + 39v_2^2\omega_3^2\omega_{11}\omega_5^3 - 306v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 - 12\omega_2^2c_s^2\omega_{11}\omega_5^2 + 6\omega_3^2c_s^4\omega_{11}\omega_5^3 - 90v_2^2\omega_3^2\omega_{11}^2\omega_5^3 - 3v_2^2\omega_3^2c_s^2\omega_{11}^2\omega_5^3 + 36v_2^2\omega_3^2\omega_{11}\omega_5^3 - 6\omega_3^2c_s^4\omega_{11}\omega_5^3 + 18\omega_3^2c_s^2\omega_{11}\omega_5^3 + 72v_2^2\omega_3^2\omega_{11}^2\omega_5^3 - 72v_2^2\omega_3^2\omega_{11}\omega_5^2 + 54v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 - 36v_2^2\omega_3^2\omega_{11}\omega_5^3 - 12\omega_3^2c_s^4\omega_{11}^2\omega_5^3 - 108v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^2 + 12\omega_3^2c_s^2\omega_{11}\omega_5^2 + 12\omega_3^2c_s^4\omega_{11}^2\omega_5^3 + 36v_2^2\omega_3^2\omega_{11}\omega_5^3 - 5\omega_3^2c_s^2\omega_{11}\omega_5^3 - 12\omega_3^2c_s^2\omega_{11}^2\omega_5^3 + \omega_3^2c_s^4\omega_{11}\omega_5^2 + 19v_2^2\omega_3^2\omega_{11}\omega_5^2 + 12\omega_3^2c_s^2\omega_{11}\omega_5^3 + 36v_2^2\omega_3^2\omega_{11}\omega_5^3 - 36v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 - 108v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 - 4v_2^2\omega_3^2\omega_{11}\omega_5^3 + 36v_2^2\omega_3^2\omega_5^3 - \omega_3^2c_s^4\omega_{11}\omega_5^3 - 6\omega_3^2c_s^2\omega_{11}\omega_5^3 + 198v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^2 + 12\omega_3^2c_s^2\omega_{11}\omega_5^3 + 36v_2^2\omega_3^2\omega_5^3 - \omega_3^2c_s^2\omega_{11}^2\omega_5^2 + 13\omega_3^2c_s^4\omega_{11}\omega_5^3 - 39v_2^2\omega_3^2\omega_{11}\omega_5^3 - 36v_2^2\omega_3^2\omega_5^3 + 12c_s^4\omega_{11}^2\omega_5^3 - 12\omega_3^2c_s^4\omega_{11}\omega_5^3 - 36v_2^2\omega_3^2\omega_{11}\omega_5^3 + 90v_2^2\omega_3^2\omega_{11}\omega_5^3 - 12\omega_3^2c_s^2\omega_{11}\omega_5^3 - 99v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3 + 252v_2^2\omega_3^2c_s^2\omega_{11}^2\omega_5^3 + 72v_2^2\omega_3^2\omega_{11}\omega_5^2 + 6\omega_3^2c_s^4\omega_{11}\omega_5^3 - 36v_2^2\omega_3^2\omega_5^3 - 18v_2^2\omega_3^2c_s^2\omega_{11}\omega_5^3$$

$$C_{16} = -12\omega_3^3\omega_1 - 12\omega_3^3\omega_1^2\omega_2 - 6\omega_2^2\omega_{13}\omega_1^2 - 12\omega_2^2\omega_1^2 - 6\omega_3^2\omega_{13}\omega_1\omega_2 - 12\omega_2^2\omega_1\omega_2 + 24\omega_3\omega_{13}\omega_1^2\omega_2 + 12\omega_3^3\omega_1^2 - 2\omega_3^2\omega_{13}\omega_1^2 + 12\omega_3^2\omega_1^2\omega_2 - \omega_3^3\omega_{13}\omega_1^2\omega_2 + 12\omega_3\omega_{13}\omega_1\omega_2 - 2\omega_2^2\omega_{13}\omega_1^2\omega_2 - 6\omega_3^2\omega_{13}\omega_1 + 12\omega_3\omega_{13}\omega_1^2 + 12\omega_3^3\omega_{13} - 12\omega_3^3\omega_2 + 24\omega_3^3\omega_1\omega_2 - 24\omega_{13}\omega_1^2\omega_2$$

$$C_{17} = v_2^2\omega_3^2\omega_{11}^3\omega_5^3 + 12v_2^2\omega_3\omega_{11}\omega_5^2 + 12\omega_{11}\omega_5^3 - 40\omega_3c_s^2\omega_{11}^3\omega_5^3 + 36\omega_3^2c_s^2\omega_{11}^3\omega_5^3 + 18\omega_2^2\omega_{11}^2\omega_5^2 + 18\omega_3c_s^2\omega_{11}^2\omega_5^2 + 18v_2^2\omega_3\omega_{11}\omega_5^3 + 4v_2^2\omega_3^2\omega_{11}^2\omega_5^2 - 12v_2^2\omega_{11}\omega_5^3 - 36\omega_3c_s^2\omega_5^3 - 36c_s^2\omega_{11}\omega_5^3 - 18\omega_3\omega_{11}\omega_5^3 - 12\omega_3^2\omega_{11}^2\omega_5^3 - 4\omega_3^2\omega_{11}\omega_5^3 + 18\omega_3^2c_s^2\omega_{11}\omega_5^3 - 18v_2^2\omega_3^2\omega_{11}^2\omega_5^3 - 12v_2^2\omega_3\omega_5^3 + 12\omega_3\omega_5^3 + 12v_2^2\omega_3^2\omega_{11}^2\omega_5^3 - 18\omega_2^2c_s^2\omega_{11}\omega_5^3 - \omega_3^2\omega_{11}\omega_5^3 - 12\omega_3\omega_{11}\omega_5^2 - 12\omega_2^2\omega_5^3 - 36c_s^2\omega_{11}^2\omega_5^3 + 5\omega_3^2c_s^2\omega_{11}^2\omega_5^3 - 12v_2^2\omega_3^2\omega_5^3 - 6\omega_3\omega_{11}^2\omega_5^2 + 6\omega_3^2\omega_{11}\omega_5^3 + 36c_s^2\omega_{11}\omega_5^3 + 12\omega_3^2\omega_5^3 - 6\omega_2^2\omega_{11}\omega_5^2 + 12\omega_3\omega_{11}^2\omega_5^3 + 12v_2^2\omega_3^2\omega_5^3 + 12\omega_3^2c_s^2\omega_{11}^2\omega_5^3 + 36\omega_3c_s^2\omega_{11}\omega_5^2 + 6v_2^2\omega_3^2\omega_{11}\omega_5^2 + 12\omega_{11}^2\omega_5^2 - 54\omega_3^2c_s^2\omega_{11}\omega_5^3 - 12v_2^2\omega_3\omega_{11}^2\omega_5^3 + 12v_2^2\omega_{11}^2\omega_5^3 - 36\omega_3^2c_s^2\omega_5^2 + 6v_2^2\omega_3\omega_{11}^2\omega_5^2 - 12\omega_{11}^2\omega_5^3 - 6v_2^2\omega_3^2\omega_{11}\omega_5^3 + 54\omega_3c_s^2\omega_{11}\omega_5^3 + 36\omega_3^2c_s^2\omega_5^3 - 12v_2^2\omega_{11}^2\omega_5^2$$

$$C_{18} = -12\omega_3^3 + 12\omega_3\omega_{11}\omega_5 + 12\omega_3c_s^2\omega_5^2 - 36v_2^2\omega_3^2\omega_{11} - 24\omega_3^3c_s^2\omega_5 + 12\omega_3^2\omega_{11} + 12\omega_3^2c_s^2\omega_{11}\omega_5 - \omega_3^3c_s^2\omega_{11}\omega_5^2 - 12\omega_3\omega_5^2 - 12\omega_3^2c_s^2\omega_{11} - 4\omega_3^2c_s^2\omega_{11}\omega_5^2 + 12\omega_3^2c_s^2\omega_5^2 - 12c_s^2\omega_{11}\omega_5^2 + 36v_2^2\omega_3\omega_5^2 - 36v_2^2\omega_3\omega_{11}\omega_5 + 24\omega_3^3\omega_5 - 72v_2^2\omega_3^2\omega_5^2 + 36v_2^2\omega_3^3 + 24\omega_3^3\omega_5^2 + 24\omega_3^2c_s^2\omega_5 - 12\omega_3c_s^2\omega_{11}\omega_5 + 36v_2^2\omega_3^2\omega_{11}\omega_5 - 72v_2^2\omega_3^2\omega_5 + 18\omega_3c_s^2\omega_{11}\omega_5^2 - 12\omega_3^2\omega_{11}\omega_5 + 12\omega_3^2c_s^2 + 36v_2^2\omega_3^2\omega_5^2 - 24\omega_3^3\omega_5 - 24\omega_3^2c_s^2\omega_5^2 + 72v_2^2\omega_3^2\omega_5 - 12\omega_3^3\omega_5^2$$

$$C_{19} = -12\omega_6\omega_{10}^2 + 18\omega_3c_s^2\omega_{10}^2 - 12v_3^2\omega_6\omega_3 + v_3^2\omega_6\omega_3^2\omega_{10}^2 + v_3^2\omega_3^2\omega_{10}^2 - 12\omega_3\omega_{10} - 12v_2^2\omega_{10}^2 + 3\omega_6\omega_3^2c_s^2\omega_{10}^2 + 3\omega_6\omega_3^2\omega_{10} - 9\omega_6\omega_3^2c_s^2\omega_{10} - \omega_6\omega_3^2\omega_{10} - 6\omega_3\omega_{10} - 36c_s^2\omega_{10}^2 - 3v_3^2\omega_6\omega_3^2\omega_{10} + 18\omega_6\omega_3^2c_s^2 - 6v_3^2\omega_3^2\omega_{10} + 12\omega_6\omega_{10} + 6v_3^2\omega_6\omega_3 + 36\omega_3c_s^2\omega_{10} + 18v_3^2\omega_6\omega_3\omega_{10} + 54\omega_6\omega_3c_s^2\omega_{10} + 12v_3^2\omega_3\omega_{10} - 36\omega_6\omega_3c_s^2 + 12\omega_6\omega_3 + 36\omega_6c_s^2\omega_{10}^2 + 12v_3^2\omega_6\omega_3\omega_{10} - \omega_3^2\omega_{10} - 18\omega_3^2c_s^2\omega_{10} + 6\omega_3^2\omega_{10} + 3\omega_3^2c_s^2\omega_{10}^2 - 36\omega_6c_s^2\omega_{10} - 6\omega_6\omega_3^2 - 18\omega_6\omega_3\omega_{10} - 12v_3^2\omega_6\omega_{10} - 12v_3^2\omega_6\omega_3\omega_{10} + 6v_3^2\omega_3\omega_{10}^2 - 36\omega_6\omega_3c_s^2\omega_{10}^2 + 12\omega_{10}^2$$

$$C_{20} = \omega_3^3c_s^2\omega_{10} + 6\omega_3^3 + 36v_3^2\omega_6\omega_3 + 12\omega_3\omega_{10} - 12\omega_3^2 + 6\omega_6\omega_3c_s^2 + 3v_3^2\omega_3^3\omega_{10} + \omega_6\omega_3^2\omega_{10} - 5\omega_6\omega_3^2c_s^2\omega_{10} + 18v_3^2\omega_6\omega_3^3 - 3v_3^2\omega_6\omega_3^2\omega_{10} - 18\omega_6\omega_3^2\omega_{10} + 18v_3^2\omega_3^3\omega_{10} - 54v_3^2\omega_6\omega_3^2 - 12\omega_3c_s^2\omega_{10} + 18\omega_6\omega_3c_s^2\omega_{10} - 36v_3^2\omega_3\omega_{10} + 12\omega_6\omega_3c_s^2 + 12\omega_3^2c_s^2 - \omega_3^3\omega_{10} - 12\omega_6\omega_3 + 6\omega_3^2c_s^2\omega_{10} - 6\omega_3^2\omega_{10} - 6\omega_3^3c_s^2 - 18v_3^2\omega_3^3 - 12\omega_6c_s^2\omega_{10} + 18\omega_6\omega_3^2 - \omega_6\omega_3^3c_s^2\omega_{10} - 6\omega_6\omega_3^3 + 36v_3^2\omega_3^3$$

$$C_{21} = 3v_3^4\omega_3^3\omega_{10}^2 - 6\omega_3^3c_s^2\omega_{10} + 12\omega_3c_s^2\omega_{10}^2 - 24\omega_3^2c_s^4\omega_{10} + 12v_3^2\omega_3^2\omega_{10}^2 + 72v_3^2\omega_3c_s^2\omega_{10} + 72v_3^4\omega_3^3\omega_{10} + 6v_3^2\omega_3^3c_s^2\omega_{10}^2 + 30v_3^2\omega_3^3\omega_{10} - 216v_3^3\omega_3^2c_s^2 - 3v_3^3\omega_3^3\omega_{10}^2 - 36v_3^2\omega_3^2c_s^2\omega_{10}^2 - 12v_3^4\omega_3^2\omega_{10}^2 - 72v_3^4\omega_3^3 - 72v_3^2\omega_3^3c_s^2\omega_{10} + 24\omega_3^2c_s^4\omega_{10}^2 + 108v_3^2\omega_3^3c_s^2 - 72v_3^2\omega_3^2\omega_{10} + 36v_3^4\omega_3^3 - 30v_3^4\omega_3^3\omega_{10} + \omega_3^3c_s^2\omega_{10}^2 - 24\omega_3c_s^2\omega_{10} - 12v_3^2\omega_3^2c_s^2\omega_{10}^2 + 6\omega_3^3c_s^4\omega_{10} - 48\omega_3c_s^4\omega_{10}^2 + 24\omega_3^2c_s^2\omega_{10} - 8\omega_3^2c_s^2\omega_{10}^2 - 3\omega_3^3c_s^4\omega_{10} - 36v_3^2\omega_3^3 + 24\omega_3c_s^4\omega_{10} + 144v_3^2\omega_3^2c_s^2\omega_{10} + 24c_s^4\omega_{10}^2 + 72v_3^2\omega_3^3$$

2.6.5 Conservation of momentum: ρv_3



attached text file: output_d33q27_nse_culbm1_symbolic_pde_03.txt

$$v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_1 v_3 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \delta_t \rho}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_1 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_2 v_3 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \delta_t \rho}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_2 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_2} + (v_3^2 + c_s^2) \frac{\delta_t}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{2v_3 \delta_t \rho}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_2) \frac{c_s^2 \delta_t^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_2) \frac{c_s^2 \delta_t^2}{2\delta_t \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + (-2 + \omega_3) \frac{c_s^2 \delta_t^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + (-2 + \omega_3) \frac{c_s^2 \delta_t^2}{2\omega_3 \delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_6 - 2\omega_6 c_s^2 + 6v_3^2 - 3v_2^2\omega_6 + 4c_s^2) \frac{\delta_t^2}{\omega_6 \delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + (2 - \omega_6) \frac{3v_3 \delta_t^2 \rho}{\omega_6 \delta_t} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_2) \frac{c_s^2 \delta_t^2 \rho}{2\delta_t \omega_2} \frac{\partial^2 v_3}{\partial x_1^2} + (-2 + \omega_3) \frac{c_s^2 \delta_t^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_3}{\partial x_2^2} + (-2 + \omega_3) \frac{c_s^2 \delta_t^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + (-2 + \omega_3) \frac{c_s^2 \delta_t^2 \rho}{2\omega_3 \delta_t} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} +$$

$$\begin{aligned}
& (-2 + \omega_6 - 3\omega_6 c_s^2 + 2v_3^2 - v_3^2 \omega_6 + 6c_s^2) \frac{v_3 \delta_t^2}{2\omega_6 \delta_t} \frac{\partial^2 \rho}{\partial x_3^2} + (-2 + \omega_6 - \omega_6 c_s^2 + 6v_3^2 - 3v_3^2 \omega_6 + 2c_s^2) \frac{\delta_t^2 \rho}{2\omega_6 \delta_t} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (-1 + v_1^2 + 3c_s^2) \frac{v_1 v_3 \delta_t^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + 3v_1^2 + c_s^2) \frac{v_3 \delta_t^3 \rho}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{v_1 \delta_t^3 \rho}{6\omega_{12} \delta_t \omega_2} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{v_3 c_s^2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} - \frac{v_3 c_s^2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + \\
& (-1 + v_2^2 + 3c_s^2) \frac{v_2 v_3 \delta_t^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + (-1 + 3v_2^2 + c_s^2) \frac{v_3 \delta_t^3 \rho}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_2 \frac{v_2 \delta_t^3 \rho}{6\omega_3 \delta_t \omega_{11}} \frac{\partial^3 v_3}{\partial x_2^3} + (-12 - \omega_2^2 + 12\omega_2) \frac{c_s^4 \delta_t^3}{6\delta_t \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} - \\
& \frac{v_3 c_s^2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + (-12 - \omega_3^2 + 12\omega_3) \frac{c_s^4 \delta_t^3}{6\omega_3^2 \delta_t} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} - \frac{v_3 c_s^2 \delta_t^3 \rho}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_3 \frac{v_3 \delta_t^3 \rho}{12\omega_6^2 \delta_t \omega_8 \omega_2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_4 \frac{v_3 \delta_t^3 \rho}{12\omega_6^2 \omega_3 \delta_t \omega_{10}} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} \\
& + C_5 \frac{\delta_t^3}{12\omega_6^2 \delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + (-24 - 4\omega_6^2 + 24\omega_6 - 36\omega_6 c_s^2 + 60v_3^2 - 60v_3^2 \omega_6 + 5\omega_6^2 c_s^2 + 11v_3^2 \omega_6^2 + 36c_s^2) \frac{v_3 \delta_t^3 \rho}{6\omega_6^2 \delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& (2c_s^4 - 3v_1^4 \omega_4 - c_s^4 \omega_4 - 6v_1^2 + 24v_1^2 c_s^2 + 6v_1^4 + 3v_1^2 \omega_4 + c_s^2 \omega_4 - 2c_s^2 - 12v_1^2 c_s^2 \omega_4) \frac{v_3 \delta_t^4}{24\delta_t \omega_4} \frac{\partial^4 \rho}{\partial x_1^4} + \\
& (-4 + 10v_1^2 + 2\omega_4 - 5v_1^2 \omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_1 v_3 \delta_t^4 \rho}{12\delta_t \omega_4} \frac{\partial^4 v_1}{\partial x_1^4} + C_6 \frac{\delta_t^4 \rho}{24\omega_{12} \delta_t \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^4} + \\
& (-\omega_9 + 3\omega_9 c_s^2 \omega_4 + v_1^2 \omega_9 \omega_4 - \omega_9 \omega_4 + 3\omega_4 + v_1^2 \omega_9 - 3v_1^2 \omega_4 - 9c_s^2 \omega_4 + 3\omega_9 c_s^2) \frac{v_1 v_3 \delta_t^4 \rho}{12\omega_9 \delta_t \omega_4} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + (-2 + \omega_1) \frac{v_3 c_s^4 \delta_t^4}{6\delta_t \omega_1} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} \\
& + (\omega_{13} \omega_2 + 2\omega_3 \omega_2^2 - \omega_3^2 - \omega_3 \omega_{13} \omega_2 - 2\omega_3 \omega_2 + \omega_3 \omega_{13} - \omega_2^2 + 2\omega_3^2 \omega_2 - \omega_3^2 \omega_2^2) \frac{c_s^4 \delta_t^4 \rho}{\omega_3^2 \delta_t \omega_{13} \omega_2^2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2} + \\
& (-3v_2^2 \omega_5 + v_2^2 \omega_7 \omega_5 - \omega_7 \omega_5 - 9c_s^2 \omega_5 + v_2^2 \omega_7 + 3c_s^2 \omega_7 \omega_5 + 3c_s^2 \omega_7 - \omega_7 + 3\omega_5) \frac{v_2 v_3 \delta_t^4 \rho}{12\delta_t \omega_7 \omega_5} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (-12v_2^2 c_s^2 \omega_5 + 3v_2^2 \omega_5 + 2c_s^4 + c_s^2 \omega_5 + 24v_2^2 c_s^2 - 6v_2^2 + 6v_2^4 - c_s^4 \omega_5 - 3v_2^4 \omega_5 - 2c_s^2) \frac{v_3 \delta_t^4 \rho}{24\delta_t \omega_5} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (-4 - 5v_2^2 \omega_5 - 3c_s^2 \omega_5 + 10v_2^2 + 2\omega_5 + 6c_s^2) \frac{v_2 v_3 \delta_t^4 \rho}{12\delta_t \omega_5} \frac{\partial^4 v_2}{\partial x_2^4} + C_7 \frac{\delta_t^4 \rho}{24\omega_3^3 \delta_t \omega_{11}^2} \frac{\partial^4 v_3}{\partial x_2^4} + C_8 \frac{v_1 c_s^2 \delta_t^4}{12\omega_{12}^2 \delta_t \omega_4 \omega_2^2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& C_9 \frac{c_s^2 \delta_t^4 \rho}{12\omega_{12} \delta_t \omega_4 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + \\
& (-\omega_{12} - \omega_{12} \omega_4 + v_1^2 \omega_{12} \omega_4 + 3\omega_4 - 3v_1^2 \omega_4 - 9c_s^2 \omega_4 + 3\omega_{12} c_s^2 \omega_4 + v_1^2 \omega_{12} + 3\omega_{12} c_s^2) \frac{v_1 v_3 \delta_t^4 \rho}{12\omega_{12} \delta_t \omega_4} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3} + \\
& C_{10} \frac{c_s^4 \delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{13} \omega_1 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{11} \frac{c_s^4 \delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{13} \omega_1 \omega_2^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{12} \frac{v_2 c_s^2 \delta_t^4}{12\omega_3^3 \delta_t \omega_{11}^2 \omega_5} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{13} \frac{c_s^2 \delta_t^4 \rho}{12\omega_3^3 \delta_t \omega_{11} \omega_5} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\
& (-3v_2^2 \omega_5 + 3c_s^2 \omega_{11} \omega_5 - 9c_s^2 \omega_5 - \omega_{11} \omega_5 + v_2^2 \omega_{11} \omega_5 - \omega_{11} + 3c_s^2 \omega_{11} + 3\omega_5 + v_2^2 \omega_{11}) \frac{v_2 v_3 \delta_t^4 \rho}{12\delta_t \omega_{11} \omega_5} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \\
& C_{14} \frac{v_3 c_s^2 \delta_t^4}{12\omega_6^2 \delta_t \omega_8 \omega_2^2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{15} \frac{c_s^2 \delta_t^4 \rho}{12\omega_6^2 \delta_t \omega_8 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{16} \frac{v_3 c_s^2 \delta_t^4}{12\omega_6^2 \omega_3^3 \delta_t \omega_{10}^2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{17} \frac{c_s^2 \delta_t^4 \rho}{12\omega_6^2 \omega_3^3 \delta_t \omega_{10}} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& C_{18} \frac{\delta_t^4 \rho}{12\omega_6^2 \delta_t \omega_8 \omega_2^2} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{19} \frac{\delta_t^4 \rho}{12\omega_6^3 \omega_3^3 \delta_t \omega_{10}^2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{20} \frac{v_3 \delta_t^4 \rho}{12\omega_6^3 \delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{21} \frac{\delta_t^4 \rho}{12\omega_6^3 \delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 6 - 3\omega_{12} + 9c_s^2 \omega_2 + 3v_1^2 \omega_2 - 6v_1^2 - 3\omega_{12} c_s^2 \omega_2 + 3v_1^2 \omega_{12} - v_1^2 \omega_{12} \omega_2 + 9\omega_{12} c_s^2 - 18c_s^2 + \omega_{12} \omega_2 - 3\omega_2 \\
C_2 &= 6 - 3\omega_3 - 6v_2^2 + 9\omega_3 c_s^2 - 3\omega_3 c_s^2 \omega_{11} - 3\omega_{11} + \omega_3 \omega_{11} + 3v_2^2 \omega_3 + 9c_s^2 \omega_{11} - 18c_s^2 + 3v_2^2 \omega_{11} - v_2^2 \omega_3 \omega_{11} \\
C_3 &= 12\omega_6^2 + 12\omega_6 \omega_2 - 3v_3^2 \omega_6^2 \omega_8 \omega_2 + 36c_s^2 \omega_8 \omega_2 + 3\omega_6^2 \omega_8 \omega_2 + 12v_3^2 \omega_6^2 \omega_2 - 11\omega_6^2 c_s^2 \omega_8 \omega_2 - 6\omega_6^2 \omega_8 + 36\omega_6^2 c_s^2 \omega_2 - 12\omega_8 \omega_2 + 6\omega_6 \omega_8 \omega_2 - \\
& 36\omega_6 c_s^2 \omega_2 - 12v_3^2 \omega_6 \omega_2 - 36\omega_6^2 c_s^2 - 18\omega_6 c_s^2 \omega_8 \omega_2 + 12v_3^2 \omega_8 \omega_2 - 12v_3^2 \omega_6^2 - 6v_3^2 \omega_6 \omega_8 \omega_2 + 18\omega_6^2 c_s^2 \omega_8 - 12\omega_6^2 \omega_2 + 6v_3^2 \omega_6^2 \omega_8 \\
C_4 &= 12\omega_6^2 - 12v_3^2 \omega_6 \omega_3 - 11\omega_6^2 \omega_3 c_s^2 \omega_{10} + 3\omega_6^2 \omega_3 \omega_{10} + 18\omega_6^2 c_s^2 \omega_{10} - 12\omega_3 \omega_{10} + 6v_3^2 \omega_6^2 \omega_{10} + 36\omega_6^2 \omega_3 c_s^2 - 12\omega_6^2 \omega_3 - 3v_3^2 \omega_6^2 \omega_3 \omega_{10} + \\
& 36\omega_3 c_s^2 \omega_{10} - 6v_3^2 \omega_6 \omega_3 \omega_{10} - 18\omega_6 \omega_3 c_s^2 \omega_{10} + 12v_3^2 \omega_3 \omega_{10} - 36\omega_6 \omega_3 c_s^2 - 6\omega_6^2 \omega_{10} + 12\omega_6 \omega_3 - 36\omega_6^2 c_s^2 - 12v_3^2 \omega_6^2 + 6\omega_6 \omega_3 \omega_{10} + 12v_3^2 \omega_6^2 \omega_3 \\
C_5 &= -36v_3^4 \omega_6 + 144v_3^2 c_s^2 + 12c_s^4 + \omega_6^2 c_s^4 + 12\omega_6 c_s^2 - 36v_3^2 + 24v_3^2 \omega_6^2 c_s^2 + 7v_3^4 \omega_6^2 - 144v_3^2 \omega_6 c_s^2 + 36v_3^2 \omega_6 + 36v_3^4 - \omega_6^2 c_s^2 - 7v_3^2 \omega_6^2 - 12c_s^2 - 12\omega_6 c_s^4 \\
C_6 &= -36v_1^2 \omega_2^3 - 48\omega_{12}^2 c_s^4 \omega_2 - 3v_1^2 \omega_{12}^2 \omega_2^3 + 24\omega_{12} c_s^2 \omega_2^2 + 72v_1^2 \omega_2^2 - 36v_1^2 \omega_{12}^2 c_s^2 \omega_2 - 6\omega_{12} c_s^2 \omega_2^3 + 12v_1^2 \omega_{12}^2 \omega_2^2 - 12v_1^2 \omega_{12}^2 c_s^2 \omega_2^2 + 108v_1^2 c_s^2 \omega_2^3 + 3v_1^4 \omega_{12}^2 \omega_2^3 - \\
& 3\omega_{12}^2 c_s^4 \omega_2^3 - 216v_1^2 c_s^2 \omega_2^2 - 24\omega_{12} c_s^2 \omega_2^2 + 6v_1^2 \omega_{12}^2 c_s^2 \omega_2^3 + 24\omega_{12}^2 c_s^4 \omega_2^2 - 12v_1^4 \omega_{12}^2 \omega_2^2 - 72v_1^4 \omega_2^2 + 144v_1^2 \omega_{12}^2 c_s^2 \omega_2^2 + 6\omega_{12} c_s^4 \omega_2^3 + 72v_1^4 \omega_{12}^2 \omega_2^2 - 72v_1^2 \omega_{12}^2 c_s^2 \omega_2^3 + \\
& 36v_1^4 \omega_2^3 + 12\omega_{12}^2 c_s^2 \omega_2 - 30v_1^4 \omega_{12} \omega_2^3 - 24\omega_{12} c_s^4 \omega_2^2 + 24\omega_{12}^2 c_s^4 \omega_2 - 8\omega_{12}^2 c_s^2 \omega_2^3 - 72v_1^2 \omega_{12}^2 \omega_2^2 + 24\omega_{12}^2 c_s^4 + 30v_1^2 \omega_{12} \omega_2^3 + \omega_{12}^2 c_s^2 \omega_2^3 + 72v_1^2 \omega_{12}^2 c_s^2 \omega_2 \\
C_7 &= -30v_2^4 \omega_3^4 \omega_{11} - 72v_2^4 \omega_3^3 - 72v_2^2 \omega_3^3 \omega_{11} + 24c_s^4 \omega_{11}^2 - 8\omega_3^2 c_s^2 \omega_{11}^2 + 144v_2^2 \omega_3^2 c_s^2 \omega_{11} - 12v_2^4 \omega_3^2 \omega_{11}^2 - 3v_2^2 \omega_3^2 \omega_{11}^2 - 3\omega_3^3 c_s^4 \omega_{11} + 36v_2^4 \omega_3^3 + 24\omega_3 c_s^4 \omega_{11} + \\
& 30v_2^2 \omega_3^3 \omega_{11} + 6\omega_3^3 c_s^4 \omega_{11} - 48\omega_3 c_s^4 \omega_{11}^2 + 24\omega_3^2 c_s^2 \omega_{11}^2 - 12v_2^2 \omega_3^2 c_s^2 \omega_{11}^2 + 72v_2^2 \omega_3^2 \omega_{11} + 12v_2^2 \omega_3^2 \omega_{11}^2 + 3v_2^4 \omega_3^3 \omega_{11}^2 + 24\omega_3^2 c_s^4 \omega_{11}^2 - 36v_2^2 \omega_3^2 c_s^2 \omega_{11}^2 + \omega_3^3 c_s^2 \omega_{11}^2 - \\
& 36v_2^2 \omega_3^3 - 72v_2^2 \omega_3^3 c_s^2 \omega_{11} - 24\omega_3 c_s^2 \omega_{11} - 216v_2^2 \omega_3^2 c_s^2 + 72v_2^2 \omega_3^2 + 72v_2^2 \omega_3^2 c_s^2 \omega_{11} - 6\omega_3^3 c_s^2 \omega_{11} + 6v_2^2 \omega_3^3 c_s^2 \omega_{11}^2 + 12\omega_3 c_s^2 \omega_{11}^2 - 24\omega_3^2 c_s^4 \omega_{11} + 108v_2^2 \omega_3^2 c_s^2 \\
C_8 &= -\omega_{12}^2 \omega_4 \omega_2^2 - 6\omega_{12}^2 \omega_2 - 18\omega_{12} c_s^2 \omega_2^2 - 36\omega_{12}^2 c_s^2 + 18v_1^2 \omega_{12} \omega_4 \omega_2 + 12\omega_{12} \omega_4 - 36\omega_{12}^2 c_s^2 \omega_4 \omega_2 + v_1^2 \omega_{12}^2 \omega_2^2 + 3\omega_{12}^2 c_s^2 \omega_4 \omega_2^2 + 6v_1^2 \omega_{12}^2 \omega_2 - \\
& 3v_1^2 \omega_{12} \omega_4 \omega_2^2 - 12v_1^2 \omega_{12} \omega_4 + 36\omega_{12} c_s^2 \omega_2 + 36\omega_{12}^2 c_s^2 \omega_4 + 12\omega_{12}^2 \omega_4 \omega_2 + 12\omega_{12}^2 - \omega_{12}^2 \omega_2^2 + 12v_1^2 \omega_{12}^2 \omega_4 + 12\omega_4 \omega_2 + 6\omega_{12} \omega_2^2 + v_1^2 \omega_{12}^2 \omega_4 \omega_2^2 - \\
& 36\omega_{12} c_s^2 \omega_4 + 18\omega_{12}^2 c_s^2 \omega_2 + 12v_1^2 \omega_{12} \omega_2 + 54\omega_{12} c_s^2 \omega_4 \omega_2 + 6v_1^2 \omega_4 \omega_2^2 + 18c_s^2 \omega_4 \omega_2^2 - 18\omega_{12} \omega_4 \omega_2 - 12v_1^2 \omega_4 \omega_2 - 36c_s^2 \omega_4 \omega_2 - 12\omega_{12}^2 \omega_4 + \\
& 3\omega_{12} \omega_4 \omega_2^2 - 12v_1^2 \omega_{12}^2 + 3\omega_{12}^2 c_s^2 \omega_2^2 - 6v_1^2 \omega_{12} \omega_2^2 - 9\omega_{12} c_s^2 \omega_4 \omega_2^2 - 12\omega_{12} \omega_2 - 12v_1^2 \omega_{12}^2 \omega_4 \omega_2 - 6\omega_4 \omega_2^2
\end{aligned}$$

$$C_9 = -18v_1^2\omega_3^2 - 6c_s^2\omega_3^2 + 6\omega_{12}c_s^2\omega_2^2 + 12c_s^2\omega_2^2 + 36v_1^2\omega_2^2 + \omega_{12}c_s^2\omega_3^2 - 3v_1^2\omega_{12}\omega_4\omega_2^2 - 12\omega_{12}c_s^2\omega_2 - 12\omega_2^2 - 12\omega_4\omega_2 - 6\omega_{12}\omega_2^2 + 6c_s^2\omega_4\omega_3^2 + 18v_1^2\omega_4\omega_3^2 + 6\omega_3^3 - 12\omega_{12}c_s^2\omega_4 - 36v_1^2\omega_{12}\omega_2 + 18\omega_{12}c_s^2\omega_4\omega_2 - 54v_1^2\omega_4\omega_2^2 - 18c_s^2\omega_4\omega_2^2 - \omega_{12}\omega_2^2 + 36v_1^2\omega_4\omega_2 + 12c_s^2\omega_4\omega_2 + \omega_{12}\omega_4\omega_2^2 - 6\omega_4\omega_3^2 + 18v_1^2\omega_{12}\omega_2^2 - 5\omega_{12}c_s^2\omega_4\omega_2^2 + 12\omega_{12}\omega_2 - \omega_{12}c_s^2\omega_4\omega_3^2 + 3v_1^2\omega_{12}\omega_2^2 + 18\omega_4\omega_2^2$$

$$C_{10} = -12\omega_3\omega_2^3 - 6\omega_3\omega_{13}\omega_3^2 - 12\omega_3^2\omega_1\omega_2^3 + 24\omega_3^2\omega_{13}\omega_1\omega_2 + 12\omega_3^2\omega_1\omega_2^2 + 12\omega_{13}\omega_2^3 - 2\omega_3^2\omega_{13}\omega_1\omega_2^2 - 24\omega_3^2\omega_{13}\omega_1 - \omega_3^2\omega_{13}\omega_1\omega_2^3 - 12\omega_1\omega_2^3 + 12\omega_3^2\omega_{13}\omega_2 + 12\omega_3\omega_{13}\omega_1\omega_2 - 12\omega_3^2\omega_2^2 - 6\omega_3\omega_{13}\omega_1\omega_2^2 + 24\omega_3\omega_1\omega_2^2 - 2\omega_3^2\omega_{13}\omega_2^2 + 12\omega_3^2\omega_2^2 - 6\omega_3^2\omega_{13}\omega_2^2 - 12\omega_3\omega_1\omega_2^2$$

$$C_{11} = -12\omega_3^2\omega_1 - 6\omega_3^2\omega_{13}\omega_1\omega_2 - 6\omega_3^2\omega_{13}\omega_2 + 12\omega_3^2\omega_1\omega_2^2 + 12\omega_3\omega_{13}\omega_2^2 - \omega_3^3\omega_{13}\omega_1\omega_2^2 - 12\omega_3^2\omega_1\omega_2 - 2\omega_3^2\omega_{13}\omega_2^2 - 2\omega_3^2\omega_{13}\omega_1\omega_2^2 - 24\omega_{13}\omega_1\omega_2^2 - 12\omega_3^2\omega_1\omega_2^2 + 12\omega_3^2\omega_2^2 + 12\omega_3\omega_{13}\omega_1\omega_2 - 12\omega_3^2\omega_2^2 + 24\omega_3\omega_{13}\omega_1\omega_2^2 + 12\omega_3^3\omega_{13} - 12\omega_3^3\omega_2 - 6\omega_3^3\omega_{13}\omega_2^2 + 24\omega_3^3\omega_1\omega_2$$

$$C_{12} = -12v_2^2\omega_3\omega_5 - 18\omega_3\omega_{11}\omega_5 - 6v_2^2\omega_3^2\omega_{11} + 12\omega_{11}^2 - 36c_s^2\omega_{11}\omega_5 + 3\omega_3^2c_s^2\omega_{11}^2 + 6\omega_3^2\omega_{11} - \omega_3^2\omega_{11}^2\omega_5 - 9\omega_3^2c_s^2\omega_{11}\omega_5 + 12\omega_3\omega_5 - 18\omega_3^2c_s^2\omega_{11} - 36\omega_3c_s^2\omega_{11}^2\omega_5 - \omega_3^2\omega_{11}^2 + 12\omega_{11}\omega_5 + v_2^2\omega_3^2\omega_{11}^2\omega_5 - 36\omega_3c_s^2\omega_5 - 12v_2^2\omega_{11}\omega_5 + v_2^2\omega_3^2\omega_{11}^2 + 18v_2^2\omega_3\omega_{11}\omega_5 + 12v_2^2\omega_{11}^2\omega_5 - 12v_2^2\omega_{11}^2 + 6v_2^2\omega_3^2\omega_{11}^2 - 12v_2^2\omega_3\omega_{11}^2\omega_5 + 36\omega_3c_s^2\omega_{11} + 18\omega_3^2c_s^2\omega_5 - 6\omega_3\omega_{11}^2 + 54\omega_3c_s^2\omega_{11}\omega_5 - 36c_s^2\omega_{11}^2 - 3v_2^2\omega_3^2\omega_{11}\omega_5 - 12\omega_{11}^2\omega_5 - 12\omega_3\omega_{11} + 3\omega_3^2\omega_{11}\omega_5 + 3\omega_3^2c_s^2\omega_{11}^2\omega_5 - 6\omega_3^2\omega_5 + 6v_2^2\omega_3^2\omega_5 + 12\omega_3\omega_{11}^2\omega_5 + 18\omega_3c_s^2\omega_{11}^2 + 36c_s^2\omega_{11}^2\omega_5 + 12v_2^2\omega_3\omega_{11}$$

$$C_{13} = 36v_2^2\omega_3\omega_5 + 6\omega_3^3 + 18v_2^2\omega_3^2\omega_{11} + 6\omega_3^3c_s^2\omega_5 - 12c_s^2\omega_{11}\omega_5 - 6\omega_3^2\omega_{11} - 5\omega_3^2c_s^2\omega_{11}\omega_5 - 12\omega_3^2 - 12\omega_3\omega_5 + 3v_2^2\omega_3^3\omega_{11} - \omega_3^3c_s^2\omega_{11}\omega_5 + 6\omega_3^2c_s^2\omega_{11} + 12\omega_3c_s^2\omega_5 - \omega_3^2\omega_{11} - 6\omega_3^2\omega_5 + 12\omega_3^2c_s^2 - 18v_2^2\omega_3^2 - 12\omega_3c_s^2\omega_{11} - 18\omega_3^2c_s^2\omega_5 + 18\omega_3c_s^2\omega_{11}\omega_5 + 36v_2^2\omega_3^2 - 3v_2^2\omega_3^2\omega_{11}\omega_5 + 18v_2^2\omega_3^2\omega_5 + 12\omega_3\omega_{11} + \omega_3^2\omega_{11}\omega_5 - 6\omega_3^2c_s^2 + 18\omega_3^2\omega_5 - 54v_2^2\omega_3^2\omega_5 + \omega_3^3c_s^2\omega_{11} - 36v_2^2\omega_3\omega_{11}$$

$$C_{14} = 12\omega_6^2\omega_3\omega_8 + 18\omega_6\omega_8\omega_2^2 - 12v_3^2\omega_6^2\omega_2 + 12v_3^2\omega_6^2\omega_8\omega_2 + 12\omega_6^3\omega_8\omega_2 + 12\omega_6^2c_s^2\omega_8^2 + 36\omega_6^3c_s^2\omega_8^2 + 18\omega_6^2c_s^2\omega_8\omega_2^2 + 12\omega_6^2\omega_8^2 + v_3^2\omega_6^3\omega_8^2\omega_2^2 - 6\omega_6^2\omega_8\omega_2^2 + 54\omega_6^3c_s^2\omega_8\omega_2 - 12v_3^2\omega_6^2\omega_2^2 - 12v_3^2\omega_6^2\omega_8\omega_2 + 12v_3^2\omega_8^2\omega_2^2 - 12\omega_6^2\omega_8\omega_2 - 18\omega_6^2c_s^2\omega_8\omega_2^2 + 36\omega_6^2c_s^2\omega_8\omega_2 - 54\omega_6^2c_s^2\omega_8\omega_2^2 + 12v_3^2\omega_6^2\omega_8^2\omega_2^2 + 6v_3^2\omega_6^2\omega_8\omega_2^2 - \omega_6^3\omega_8^2\omega_2^2 - 36\omega_6^3c_s^2\omega_8 - 12\omega_6^3\omega_8^2 + 4v_3^2\omega_6^2\omega_8^2\omega_2^2 - 12v_3^2\omega_6^2\omega_8^2 + 6\omega_6^3\omega_8\omega_2^2 + 12\omega_6^2\omega_2^2 + 18v_3^2\omega_6^2\omega_8\omega_2 - 12v_3^2\omega_6^2\omega_8 - 36\omega_6^2c_s^2\omega_8^2 + 5\omega_6^3c_s^2\omega_8^2\omega_2^2 + 36\omega_6^3c_s^2\omega_2^2 - 6\omega_6^2\omega_8^2\omega_2 + 36c_s^2\omega_8^2\omega_2^2 + 18\omega_6^2c_s^2\omega_2^2\omega_2 + 12\omega_6^3\omega_2 + 12\omega_6^2c_s^2\omega_8^2\omega_2^2 - 12\omega_6^3\omega_2^2 + 12v_3^2\omega_6^2\omega_8^2 - 6v_3^2\omega_6^2\omega_8\omega_2^2 - 36\omega_6^3c_s^2\omega_2 - 4\omega_6^3c_s^2\omega_8^2\omega_2 - 4\omega_6^2\omega_8^2\omega_2^2 - 12\omega_8^2\omega_2^2 + 6v_3^2\omega_6^2\omega_8^2\omega_2 - 18\omega_6^3\omega_8\omega_2$$

$$C_{15} = 12c_s^2\omega_3^2 + 12\omega_8\omega_2^2 - \omega_6^2c_s^2\omega_8\omega_3^2 + 36v_3^2\omega_6^2\omega_3^2 - 24\omega_6^2c_s^2\omega_2^2 - 4\omega_6^2c_s^2\omega_8\omega_2^2 + 12\omega_6^2c_s^2\omega_3^2 - 72v_3^2\omega_6^2\omega_2^2 - 12c_s^2\omega_8\omega_2^2 + 36v_3^2\omega_6^2\omega_2 + 18\omega_6^2c_s^2\omega_8\omega_2 + 24\omega_6\omega_2^3 + 12\omega_6^2c_s^2\omega_2 + 36v_3^2\omega_3^2 - 24\omega_6\omega_2^2 + 12\omega_6\omega_8\omega_2 + 24\omega_6^2\omega_2^2 - 36v_3^2\omega_8\omega_2^2 - 12\omega_3^2 + 36v_3^2\omega_6\omega_8\omega_2^2 + 12\omega_6c_s^2\omega_8\omega_2^2 - 12\omega_6^2\omega_3^2 - 12\omega_6c_s^2\omega_8\omega_2 + 24\omega_6c_s^2\omega_2^2 + 72v_3^2\omega_6\omega_2^2 - 36v_3^2\omega_6\omega_8\omega_2 - 12\omega_6^2c_s^2\omega_8 - 12\omega_6^2\omega_2 - 72v_3^2\omega_6\omega_3^2 - 12\omega_6\omega_8\omega_2^2 - 24\omega_6c_s^2\omega_3^2$$

$$C_{16} = -40\omega_6^3\omega_3c_s^2\omega_{10}^2 + 36\omega_6^2\omega_3c_s^2\omega_{10} - 12\omega_6^2\omega_3\omega_{10} + 36\omega_6^3\omega_3^2c_s^2 + 12v_3^2\omega_6^3\omega_{10}^2 - 18v_3^2\omega_6\omega_3^2\omega_{10} + 12\omega_6^3\omega_3 - 6v_3^2\omega_6^3\omega_3^2\omega_{10} + 12v_3^2\omega_3^2\omega_{10}^2 - \omega_6^3\omega_3^2\omega_{10}^2 + 12\omega_6^2\omega_3^2 - 54\omega_6\omega_3^2c_s^2\omega_{10}^2 + 6v_3^2\omega_6^2\omega_3\omega_{10}^2 + 6\omega_6^2\omega_3^2\omega_{10} - 12v_3^2\omega_6^2\omega_{10}^2 + 18\omega_6\omega_3^2\omega_{10} + 12v_3^2\omega_6^2\omega_3\omega_{10} - 12v_3^2\omega_6^2\omega_{10} + 18\omega_6^2\omega_3c_s^2\omega_{10}^2 - 6\omega_6^2\omega_3\omega_{10}^2 - 12\omega_6^2\omega_3^2 - 36\omega_6^2c_s^2\omega_{10} + v_3^2\omega_6^3\omega_3^2\omega_{10}^2 + 54\omega_6^3\omega_3c_s^2\omega_{10} - 4\omega_6^3\omega_3^2\omega_{10}^2 - 12v_3^2\omega_6^3\omega_3\omega_{10}^2 - 12v_3^2\omega_6^3\omega_3^2 - 18\omega_6^3\omega_3\omega_{10} - 36\omega_6^2\omega_3^2c_s^2 + 6v_3^2\omega_6^2\omega_3\omega_{10} - 36\omega_6^3c_s^2\omega_{10} + 12\omega_6^2\omega_3^2\omega_{10}^2 - 12\omega_6^2\omega_3^2 - 18\omega_6^3\omega_3^2c_s^2\omega_{10} - 12v_3^2\omega_6^2\omega_3^2\omega_{10} - 12v_3^2\omega_6^2\omega_3 - 12\omega_6^2\omega_{10}^2 + 5\omega_6^3\omega_3^2c_s^2\omega_{10} + 36\omega_3c_s^2\omega_{10}^2 + 12v_3^2\omega_6^2\omega_3^2 + 12\omega_6^3\omega_{10} + 12\omega_6^2\omega_3\omega_{10} + 4v_3^2\omega_6^2\omega_3^2\omega_{10} + 18\omega_6^2\omega_3^2c_s^2\omega_{10} + 36\omega_6^2c_s^2\omega_{10}^2 + 12\omega_6^2\omega_{10}^2 - 36\omega_6^3\omega_3c_s^2 - 6\omega_6^2\omega_3^2\omega_{10} + 18v_3^2\omega_6^2\omega_3\omega_{10}$$

$$C_{17} = -12\omega_3^3 + 18\omega_6^2\omega_3c_s^2\omega_{10} - 12\omega_6^2c_s^2\omega_{10} - 12\omega_6^2\omega_3^3 - 24\omega_6\omega_3^2c_s^2 + 24\omega_6^2\omega_3^2 - 12\omega_6\omega_3^2\omega_{10} + 12\omega_6^2\omega_3c_s^2 - 12\omega_6^2\omega_3 + 12\omega_6\omega_3^2c_s^2\omega_{10} - 72v_3^2\omega_6\omega_3^2\omega_{10} + 36v_3^2\omega_6\omega_3^2\omega_{10} - \omega_6^2\omega_3^2c_s^2\omega_{10} + 24\omega_6\omega_3^2c_s^2 - 36v_3^2\omega_3^2\omega_{10} + 72v_3^2\omega_6\omega_3^2 - 36v_3^2\omega_6\omega_3c_s^2\omega_{10} - 12\omega_6\omega_3c_s^2\omega_{10} - 72v_3^2\omega_6^2\omega_3^2 - 24\omega_6^2\omega_3^2c_s^2 + 36v_3^2\omega_6^2\omega_3^2 - 12\omega_3^2c_s^2\omega_{10} + 12\omega_3^2\omega_{10} + 12\omega_3^2c_s^2 + 36v_3^2\omega_3^2 - 24\omega_6\omega_3^2 + 12\omega_6\omega_3\omega_{10} - 4\omega_6^2\omega_3^2c_s^2\omega_{10} + 36v_3^2\omega_6^2\omega_3 + 24\omega_6\omega_3^2 + 12\omega_6^2\omega_3^2c_s^2$$

$$C_{18} = -18\omega_6^3c_s^4\omega_8\omega_2^2 + 36v_3^4\omega_6^3\omega_8\omega_2^2 + 6\omega_6^2c_s^2\omega_8\omega_3^2 - 36v_3^4\omega_6\omega_8\omega_2^2 + 36v_3^2\omega_6^2\omega_8\omega_2^2 - 3v_3^2\omega_6^3c_s^2\omega_8^2\omega_2^2 - 4v_3^2\omega_6^3\omega_8^2\omega_2^2 - 12\omega_6c_s^4\omega_8^2\omega_2^2 - 36v_3^4\omega_6^3\omega_8\omega_2^2 - 12\omega_6^2c_s^2\omega_8\omega_2^2 + 19v_3^4\omega_6^2\omega_8^2\omega_2^2 + 6\omega_6^3c_s^4\omega_8\omega_2^2 - 108v_3^2\omega_6c_s^2\omega_8\omega_2^2 + 72v_3^2\omega_8^2\omega_2^2 - 12\omega_6c_s^4\omega_8^2\omega_2^2 + 6v_3^2\omega_6^3\omega_8^2\omega_2^2 + 12v_3^2\omega_6^2c_s^2\omega_8^2\omega_2^2 - 12\omega_6^2c_s^2\omega_8\omega_2 - 36v_3^2\omega_6^2\omega_8\omega_2^2 - 72v_3^2\omega_6^2\omega_8\omega_2^2 - 6\omega_6^2c_s^4\omega_8\omega_2^2 + 18\omega_6^3c_s^2\omega_8\omega_2^2 + 60v_3^2\omega_6^2c_s^2\omega_8^2\omega_2^2 - 36v_3^4\omega_6^2\omega_8\omega_2^2 + 36v_3^4\omega_6^3\omega_8\omega_2^2 + 12\omega_6c_s^2\omega_8^2\omega_2^2 + 90v_3^2\omega_6\omega_8\omega_2^2 - 6\omega_6^3c_s^2\omega_8\omega_2^2 + 36v_3^2\omega_6^3\omega_8^2\omega_2^2 - 18v_3^2\omega_6^3c_s^2\omega_8^2\omega_2^2 + 12\omega_6^2c_s^4\omega_8\omega_2^2 - 72v_3^2\omega_6^2\omega_8^2\omega_2^2 - 108v_3^2\omega_6^2c_s^2\omega_8^2\omega_2^2 + 12\omega_6c_s^4\omega_8\omega_2 + 18\omega_6^2\omega_6^2c_s^2\omega_8^2\omega_2^2 + 36v_3^2\omega_6^2c_s^2\omega_8\omega_2 + 6\omega_6^2c_s^4\omega_8\omega_2^2 - 12c_s^2\omega_8^2\omega_2^2 + 36v_3^2\omega_6\omega_8\omega_2^2 + 4v_3^2\omega_6^3\omega_8^2\omega_2^2 - 24\omega_6^3c_s^4\omega_8\omega_2^2 + 36v_3^2\omega_6^2c_s^2\omega_8\omega_2^2 - 5\omega_6^2c_s^2\omega_8^2\omega_2^2 + \omega_6^2c_s^4\omega_8^2\omega_2^2 - 19v_3^2\omega_6^2\omega_8^2\omega_2^2 + 198v_3^2\omega_6^2c_s^2\omega_8\omega_2^2 + 12\omega_6^2c_s^4\omega_8 - 6v_3^4\omega_6^2\omega_8^2\omega_2^2 - \omega_6^3c_s^4\omega_8^2\omega_2^2 + 72v_3^4\omega_6^2\omega_8\omega_2^2 - 6\omega_6^2c_s^2\omega_8^2\omega_2^2 + 12c_s^4\omega_8^2\omega_2^2 - 306v_3^2\omega_6c_s^2\omega_8^2\omega_2^2 - 36v_3^2\omega_6^3\omega_8\omega_2^2 + 108v_3^2\omega_6^3c_s^2\omega_8^2\omega_2^2 + 6\omega_6^3c_s^2\omega_8^2\omega_2^2 + 252v_3^2c_s^2\omega_8^2\omega_2^2 - 99v_3^2\omega_6^3c_s^2\omega_8\omega_2^2 - 36v_3^2\omega_6c_s^2\omega_8^2\omega_2^2 - \omega_6^2c_s^2\omega_8^2\omega_2^2 - 90v_3^4\omega_6\omega_8^2\omega_2^2 + 13\omega_6^3c_s^4\omega_8\omega_2^2 + 54v_3^2\omega_6^3c_s^2\omega_8\omega_2^2 - 108v_3^2\omega_6^3c_s^2\omega_2^2 + 39v_3^2\omega_6^3\omega_8\omega_2^2$$

$$C_{19} = 72v_3^4\omega_3^2\omega_{10}^2 - 6\omega_6^3\omega_3^2c_s^2\omega_{10} + 19v_3^4\omega_6^2\omega_3^2\omega_{10}^2 + 54v_3^2\omega_6^2\omega_3^2c_s^2\omega_{10} + 6\omega_6^2\omega_3^2c_s^4\omega_{10}^2 + 6\omega_6^2\omega_3c_s^2\omega_{10}^2 + 18v_3^2\omega_6^2\omega_3^2c_s^2\omega_{10}^2 - 18\omega_6^3\omega_3^2c_s^4\omega_{10} + 108v_3^2\omega_6^3\omega_3^2c_s^2\omega_{10} - \omega_6^2\omega_3^2c_s^2\omega_{10}^2 - 36v_3^2\omega_6^2\omega_3^2\omega_{10} - 12\omega_6\omega_3^2c_s^4\omega_{10}^2 + 252v_3^2\omega_3^2c_s^2\omega_{10}^2 - 4v_3^2\omega_6^3\omega_3^2\omega_{10}^2 + 12\omega_6\omega_3^2c_s^2\omega_{10}^2 - 306v_3^2\omega_6\omega_3^2c_s^2\omega_{10}^2 + 36v_3^2\omega_6\omega_3^2\omega_{10} - 72v_3^2\omega_3^2\omega_{10}^2 + 39v_3^2\omega_6^2\omega_3^2\omega_{10} + 90v_3^2\omega_6\omega_3^2\omega_{10} - 108v_3^2\omega_6^2\omega_3^2c_s^2\omega_{10} - 108v_3^2\omega_6\omega_3^2c_s^2\omega_{10} + 13\omega_6^3\omega_3^2c_s^4\omega_{10}^2 + 36v_3^2\omega_6^2\omega_3^2c_s^2\omega_{10} + 6\omega_6^2\omega_3^2c_s^2\omega_{10} + 6v_3^2\omega_6^2\omega_3^2\omega_{10} - 12\omega_3^2c_s^2\omega_{10}^2 + 72v_3^4\omega_6^2\omega_3^2\omega_{10} - 12\omega_6^3\omega_3^2c_s^2\omega_{10} + 12\omega_6^2\omega_3^2c_s^4\omega_{10} - 3v_3^2\omega_6^3\omega_3^2c_s^2\omega_{10}^2 + 12\omega_6^3c_s^4\omega_{10}^2 + 12\omega_6\omega_3^2c_s^2\omega_{10}^2 - 19v_3^2\omega_6^2\omega_3^2\omega_{10}^2 - 36v_3^4\omega_6^2\omega_3^2\omega_{10}^2 - 36v_3^2\omega_6\omega_3^2c_s^2\omega_{10}^2 - 12\omega_6\omega_3^2c_s^4\omega_{10}^2 + 36v_3^4\omega_6^2\omega_3^2\omega_{10} + 36v_3^2\omega_6^2\omega_3^2\omega_{10} - 18v_3^2\omega_6^2\omega_3^2c_s^2\omega_{10} - 36v_3^4\omega_6\omega_3^2\omega_{10} - 99v_3^2\omega_6^3\omega_3^2c_s^2\omega_{10} + \omega_6^2\omega_3^2c_s^4\omega_{10}^2 + 4v_3^4\omega_6^3\omega_3^2\omega_{10} + 36v_3^2\omega_6^3\omega_3^2c_s^2\omega_{10} - 5\omega_6^3\omega_3^2c_s^2\omega_{10} + 36v_3^2\omega_6^2\omega_3^2\omega_{10} - 90v_3^2\omega_6\omega_3^2\omega_{10} - 6\omega_6^2\omega_3^2c_s^4\omega_{10} + 12v_3^2\omega_6^3\omega_3^2c_s^2\omega_{10} - 39v_3^4\omega_6^2\omega_3^2\omega_{10} + 12\omega_3^2c_s^4\omega_{10}^2 - \omega_6^3\omega_3^2c_s^4\omega_{10}^2 + 198v_3^2\omega_6^2\omega_3^2c_s^2\omega_{10} - 12\omega_6^2\omega_3^2c_s^2\omega_{10} + 12\omega_6^2\omega_3c_s^4\omega_{10} - 6v_3^4\omega_6^2\omega_3^2\omega_{10} - 36v_3^2\omega_6^2\omega_3^2\omega_{10} - 36v_3^2\omega_6^2\omega_3^2$$

$$C_{20} = 12 + 8\omega_6^2 - 216v_3^4\omega_6 + 672v_3^2c_s^2 + 144c_s^4 + 82\omega_6^2c_s^4 - 18\omega_6 + 198\omega_6c_s^2 - \omega_6^3 - 34v_3^2\omega_6^3c_s^2 - 5\omega_6^3c_s^4 - 9v_3^4\omega_6^3 - 156v_3^2 + 404v_3^2\omega_6^2c_s^2 + 90v_3^4\omega_6^2 - 1008v_3^2\omega_6c_s^2 + 6\omega_6^3c_s^2 + 234v_3^2\omega_6 + 144v_3^4 - 78\omega_6^2c_s^2 - 98v_3^2\omega_6^2 - 132c_s^2 - 216\omega_6c_s^4 + 10v_3^2\omega_6^3$$

$$C_{21} = 12 + 8\omega_6^2 - 756v_3^4\omega_6 + 432v_3^2c_s^2 + 24c_s^4 + 14\omega_6^2c_s^4 - 18\omega_6 + 54\omega_6c_s^2 - \omega_6^3 - 18v_3^2\omega_6^3c_s^2 - \omega_6^3c_s^4 - 29v_3^4\omega_6^3 - 252v_3^2 + 252v_3^2\omega_6^2c_s^2 + 310v_3^4\omega_6^2 - 648v_3^2\omega_6c_s^2 + 2\omega_6^3c_s^2 + 378v_3^2\omega_6 + 504v_3^4 - 22\omega_6^2c_s^2 - 154v_3^2\omega_6^2 - 36c_s^2 - 36\omega_6c_s^4 + 14v_3^2\omega_6^3$$

$$\begin{aligned}
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_2 v_1 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_3 \frac{\rho v_2 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + \\
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{\rho v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_4 \frac{\delta_l^4}{72 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2^4} + \\
& (10 \omega_1 v_2^2 + 12 c_s^2 \omega_2 - 9 c_s^2 \omega_1 \omega_2 - 4 \omega_1 + 6 \omega_1 \omega_2 - 8 \omega_2 - 15 \omega_1 v_2^2 \omega_2 + 6 c_s^2 \omega_1 + 20 v_2^2 \omega_2) \frac{\rho v_2 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2^3} + \\
& (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 v_1 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\
& (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \rho \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_5 \frac{\rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_6 \frac{v_3 \rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} \\
& + C_7 \frac{\rho v_2 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_8 \frac{v_3 \rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_9 \frac{\rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 v_2 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + \\
& (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \rho \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{10} \frac{\rho v_2 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& (-3v_3^2 \omega_2 + 3\omega_1 v_1^2 - 14c_s^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 2\omega_1 - 3v_1^2 \omega_2 + 3v_3^2 \omega_1 + 2\omega_2 + 2c_s^2 \omega_1) \frac{c_s^2 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{\rho v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^3} + \\
& (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \rho \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^3} + C_{11} \frac{\rho v_2 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{12} \frac{\rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (-3v_3^2 \omega_2 + 3\omega_1 v_2^2 - 14c_s^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 3v_3^2 \omega_1 + 2\omega_2 + 2c_s^2 \omega_1 - 3v_2^2 \omega_2) \frac{c_s^2 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + \\
& (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{\rho v_2 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + \\
& (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \rho \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + \\
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 v_1 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{13} \frac{v_3 \rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + \\
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{\rho v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{v_3 v_2 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{14} \frac{v_3 \rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + \\
& (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{\rho v_2 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{15} \frac{\delta_l^4}{72 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& (20v_3^2 \omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 10v_3^2 \omega_1 + 6\omega_1 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1 - 15v_3^2 \omega_1 \omega_2) \frac{v_3 \rho \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_3^3} = 0,
\end{aligned}$$

$$C_1 = 12\omega_1^4\omega_2 - 9\omega_1v_1^4\omega_2 - 3c_s^4\omega_1\omega_2 - 6\omega_1v_1^2 - 36c_s^2\omega_1v_1^2\omega_2 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 48c_s^2v_1^2\omega_2 - 12v_1^2\omega_2 + 9\omega_1v_1^2\omega_2 + 6\omega_1v_1^4 + 24c_s^2\omega_1v_1^2 - 2c_s^2\omega_1 + 4c_s^4\omega_2$$

$$C_3 = -18\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 + 4\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 6\omega_3\omega_4\omega_1v_2^2\omega_2 + 18\omega_3\omega_4\omega_1v_1^2 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_4\omega_1v_2^2\omega_2 - 9\omega_3\omega_1v_2^2\omega_2$$

$$C_4 = -3c_s^4\omega_1\omega_2 - 36c_s^2\omega_1v_2^2\omega_2 + 48c_s^2v_2^2\omega_2 - 6\omega_1v_2^2 - 9\omega_1v_2^4\omega_2 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 12v_2^4\omega_2 + 24c_s^2\omega_1v_2^2 + 9\omega_1v_2^2\omega_2 + 6\omega_1v_2^4 - 2c_s^2\omega_1 + 4c_s^4\omega_2 - 12v_2^2\omega_2$$

$$C_5 = 4\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 - 18\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 + 18\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 6\omega_3\omega_4\omega_1v_1^2\omega_2$$

$$C_6 = 6\omega_3 c_s^2 \omega_4 \omega_1 - 2\omega_3 v_3^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 9v_3^2 \omega_4 \omega_1 \omega_2 - 9\omega_3 \omega_1 \omega_2 + 2\omega_3 v_3^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1 + 9\omega_3 v_3^2 \omega_1 \omega_2$$

$$C_7 = 6\omega_3 c_s^2 \omega_4 \omega_1 + 9\omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 v_2^2 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_1 v_2^2 - 9\omega_3 \omega_1 \omega_2 - 6\omega_3 c_s^2 \omega_4 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1 - 9\omega_4 \omega_1 v_2^2 \omega_2 + 9\omega_3 \omega_1 v_2^2 \omega_2$$

$$C_8 = 6\omega_3 c_s^2 \omega_4 \omega_1 - 2\omega_3 v_3^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 9v_3^2 \omega_4 \omega_1 \omega_2 - 9\omega_3 \omega_1 \omega_2 + 2\omega_3 v_3^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1 + 9\omega_3 v_3^2 \omega_1 \omega_2$$

$$C_9 = -2\omega_3\omega_4v_1^2\omega_2 + 6\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 + 9\omega_3\omega_1v_1^2\omega_2 - 9\omega_3\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 - 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 2\omega_3\omega_4\omega_1$$

$$C_{10} = -6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 - 18\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 4\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 6\omega_3\omega_4\omega_1v_2^2\omega_2 + 18\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_4\omega_1v_2^2\omega_2 - 9\omega_3\omega_1v_2^2\omega_2$$

$$C_{11} = 6\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 - 2\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_2^2 - 9\omega_3\omega_1\omega_2 - 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 - 9\omega_4\omega_1v_2^2\omega_2 + 9\omega_3\omega_1v_2^2\omega_2$$

$$C_{12} = -2\omega_3\omega_4v_1^2\omega_2 + 6\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 + 9\omega_3\omega_1v_1^2\omega_2 - 9\omega_3\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 - 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 2\omega_3\omega_4\omega_1$$

$$C_{13} = -18\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 18\omega_3\omega_4\omega_1v_1^2 + 2\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2$$

$$C_{14} = -6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 - 18\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 + 18\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2$$

$$C_{15} = -36c_s^2v_3^2\omega_1\omega_2 - 3c_s^4\omega_1\omega_2 + 6v_3^4\omega_1 - 12v_3^2\omega_2 + 24c_s^2v_3^2\omega_1 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 - 9v_3^4\omega_1\omega_2 + 12v_3^4\omega_2 - 6v_3^2\omega_1 + 48c_s^2v_3^2\omega_2 - 2c_s^2\omega_1 + 4c_s^4\omega_2 + 9v_3^4\omega_1\omega_2$$

2.7.3 Conservation of momentum: ρv_1



attached text file: output_d3q27_nse_culbm2_symbolic_pde_01.txt

$$\begin{aligned} & v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (c_s^2 + v_1^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{2\rho v_1 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{v_2 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\ & \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (6\omega_1 v_1^2 + 8c_s^2 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 12v_1^2 \omega_2 - 9\omega_1 v_1^2 \omega_2 + 3\omega_1 \omega_2 - 4\omega_2 + 4c_s^2 \omega_1) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + \\ & (2\omega_1 - 3\omega_1 \omega_2 + 4\omega_2) \frac{\rho v_1 \delta_l^2}{\delta_t \omega_1 \omega_2} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + (3\omega_1 v_2^2 - c_s^2 \omega_2 - \omega_1 + \omega_2 + c_s^2 \omega_1 - 3v_2^2 \omega_2) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\ & (\omega_1 - \omega_2) \frac{2\rho v_2 \delta_l^2}{\delta_t \omega_1 \omega_2} \frac{\partial v_2}{\partial x_1} \frac{\partial v_2}{\partial x_2} + (-3v_3^2 \omega_2 - c_s^2 \omega_2 - \omega_1 + 3v_3^2 \omega_1 + \omega_2 + c_s^2 \omega_1) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (\omega_1 - \omega_2) \frac{2v_3 \rho \delta_l^2}{\delta_t \omega_1 \omega_2} \frac{\partial v_3}{\partial x_1} \frac{\partial v_3}{\partial x_3} + \\ & (6\omega_1 v_2^2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 2\omega_2 + 6c_s^2 \omega_1 - 6v_2^2 \omega_2) \frac{\delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + \\ & (-6v_3^2 \omega_2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 2\omega_2 + 6c_s^2 \omega_1) \frac{\delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + \\ & (2\omega_1 v_1^2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 2\omega_1 + 4v_1^2 \omega_2 - 3\omega_1 v_1^2 \omega_2 + 3\omega_1 \omega_2 - 4\omega_2 + 6c_s^2 \omega_1) \frac{v_1 \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_1^2} + \\ & (6\omega_1 v_1^2 + 4c_s^2 \omega_2 - 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 12v_1^2 \omega_2 - 9\omega_1 v_1^2 \omega_2 + 3\omega_1 \omega_2 - 4\omega_2 + 2c_s^2 \omega_1) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_1}{\partial x_1^2} + \\ & (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{v_2 \delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + \\ & (6\omega_1 v_2^2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 2\omega_2 + 2c_s^2 \omega_1 - 6v_2^2 \omega_2) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_1} \frac{\partial^2 v_1}{\partial x_2^2} + \\ & (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + \\ & (-6v_3^2 \omega_2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 2\omega_2 + 2c_s^2 \omega_1) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_1} \frac{\partial^2 v_1}{\partial x_3^2} + C_1 \frac{\delta_l^3}{12\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^3} \\ & + C_2 \frac{\rho v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^3} + C_3 \frac{v_2 v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + C_4 \frac{\rho v_2 \delta_l^3}{6\omega_3 \delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + C_5 \frac{\rho v_1 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_6 \frac{\delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} - \\ & \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_7 \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_2 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_8 \frac{\rho v_2 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_1}{\partial x_2^3} + (-1 + c_s^2 + 3v_2^2) \frac{\rho v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} \\ & + C_9 \frac{v_3 v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + C_{10} \frac{v_3 \rho \delta_l^3}{6\omega_3 \delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + C_{11} \frac{\rho v_1 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + C_{12} \frac{v_3 v_2 \delta_l^3}{3\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\ & C_{13} \frac{v_3 \rho \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + C_{14} \frac{\rho v_2 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{15} \frac{v_3 \rho \delta_l^3}{4\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_1}{\partial x_2^2 \partial x_3} - \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + \\ & C_{16} \frac{\delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} - \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_{17} \frac{v_3 \rho \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{18} \frac{\rho v_2 \delta_l^3}{4\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_1}{\partial x_2 \partial x_3^2} - \frac{c_s^2 \rho v_1 \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\ & (-1 + 3c_s^2 + v_3^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{19} \frac{v_3 \rho \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_1}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + C_{20} \frac{v_1 \delta_l^4}{36\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^4} + \\ & C_{21} \frac{\rho \delta_l^4}{36\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^4} + C_{22} \frac{v_2 \delta_l^4}{36\omega_3^2 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{23} \frac{\rho v_2 v_1 \delta_l^4}{18\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{24} \frac{\rho \delta_l^4}{72\omega_3^2 \delta_t \omega_4^3 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\ & C_{25} \frac{v_1 \delta_l^4}{36\omega_3^2 \delta_t \omega_4^3 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\rho \delta_l^4}{36\omega_3^2 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{27} \frac{\rho v_2 v_1 \delta_l^4}{18\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{28} \frac{v_2 \delta_l^4}{72\omega_3^2 \delta_t \omega_4^3 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \end{aligned}$$

$$\begin{aligned}
& C_{29} \frac{\rho v_2 v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{30} \frac{\rho \delta_l^4}{36 \omega_3 \delta_t \omega_4 \omega_1 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{31} \frac{v_1 \delta_l^4}{72 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2^4} + C_{32} \frac{\rho \delta_l^4}{24 \omega_3 \delta_t \omega_4 \omega_1^3} \frac{\partial^4 v_1}{\partial x_2^4} + \\
& (10 \omega_1 v_2^2 + 12 c_s^2 \omega_2 - 9 c_s^2 \omega_1 \omega_2 - 4 \omega_1 + 6 \omega_1 \omega_2 - 8 \omega_2 - 15 \omega_1 v_2^2 \omega_2 + 6 c_s^2 \omega_1 + 20 v_2^2 \omega_2) \frac{\rho v_2 v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2^4} + \\
& C_{33} \frac{v_3 \delta_l^4}{36 \omega_3 \delta_t \omega_1 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{34} \frac{v_3 \rho v_1 \delta_l^4}{18 \omega_3 \delta_t \omega_1 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{35} \frac{\rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + C_{36} \frac{v_3 v_2 v_1 \delta_l^4}{6 \delta_t \omega_1 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{37} \frac{v_3 \rho v_2 \delta_l^4}{6 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{38} \frac{v_3 \rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{\rho v_2 v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \\
& C_{40} \frac{v_3 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{v_3 \rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{42} \frac{v_3 \rho v_2 \delta_l^4}{6 \omega_3 \delta_t \omega_1 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{43} \frac{\rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_5 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + (-v_3^2 \omega_2 - 3 c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3 c_s^2 \omega_1) \frac{v_3 v_2 v_1 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + \\
& C_{44} \frac{v_3 \rho v_2 \delta_l^4}{8 \omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^4 v_1}{\partial x_3^3 \partial x_3} + (-v_3^2 \omega_2 - 3 c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3 c_s^2 \omega_1) \frac{v_3 \rho v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{45} \frac{\rho v_2 v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + \\
& C_{46} \frac{v_1 \delta_l^4}{36 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{47} \frac{\rho \delta_l^4}{36 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + C_{48} \frac{v_3 \rho v_1 \delta_l^4}{18 \omega_3 \delta_t \omega_1 \omega_2^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{49} \frac{v_2 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{50} \frac{\rho v_2 v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + C_{51} \frac{\rho \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_5 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{52} \frac{v_3 \rho v_2 \delta_l^4}{6 \omega_3 \delta_t \omega_1 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& (-3 v_3^2 \omega_2 + 3 \omega_1 v_2^2 - 14 c_s^2 \omega_2 + 6 c_s^2 \omega_1 \omega_2 - 2 \omega_1 + 3 v_3^2 \omega_1 + 2 \omega_2 + 2 c_s^2 \omega_1 - 3 v_2^2 \omega_2) \frac{c_s^2 v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^3} + \\
& C_{53} \frac{\rho \delta_l^4}{8 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_5} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^3} + (\omega_1 v_2^2 - 3 c_s^2 \omega_2 - \omega_1 + \omega_2 + 3 c_s^2 \omega_1 - v_2^2 \omega_2) \frac{\rho v_2 v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^3} + \\
& (-v_3^2 \omega_2 - 3 c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3 c_s^2 \omega_1) \frac{v_3 \rho v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^3} + C_{54} \frac{v_3 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^3} + C_{55} \frac{v_3 \rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^3} + \\
& + C_{56} \frac{\rho \delta_l^4}{36 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^3} + (\omega_1 v_2^2 - 3 c_s^2 \omega_2 - \omega_1 + \omega_2 + 3 c_s^2 \omega_1 - v_2^2 \omega_2) \frac{v_3 v_2 v_1 \delta_l^4}{12 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{57} \frac{v_3 \rho v_2 \delta_l^4}{8 \omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} + \\
& C_{58} \frac{v_3 \rho v_1 \delta_l^4}{72 \omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + (\omega_1 v_2^2 - 3 c_s^2 \omega_2 - \omega_1 + \omega_2 + 3 c_s^2 \omega_1 - v_2^2 \omega_2) \frac{\rho v_2 v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{59} \frac{v_1 \delta_l^4}{72 \delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{60} \frac{\rho \delta_l^4}{24 \omega_3 \delta_t \omega_4 \omega_1^3} \frac{\partial^4 v_1}{\partial x_3^4} + \\
& (20 v_3^2 \omega_2 + 12 c_s^2 \omega_2 - 9 c_s^2 \omega_1 \omega_2 - 4 \omega_1 + 10 v_3^2 \omega_1 + 6 \omega_1 \omega_2 - 8 \omega_2 + 6 c_s^2 \omega_1 - 15 v_3^2 \omega_1 \omega_2) \frac{v_3 \rho v_1 \delta_l^4}{36 \delta_t \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= 24 c_s^2 \omega_1^2 v_1^2 + 16 \omega_1 v_1^4 \omega_2 - 7 \omega_1^2 v_1^2 \omega_2^2 + 72 c_s^2 v_1^2 \omega_2^2 + 4 \omega_1^2 v_1^4 - 96 c_s^2 \omega_1 v_1^2 \omega_2^2 - 8 c_s^2 \omega_2^2 + 4 c_s^4 \omega_1^2 + 8 c_s^2 \omega_1 \omega_2^2 + 48 c_s^2 \omega_1 v_1^2 \omega_2 + 12 \omega_1^2 v_1^2 \omega_2 + \\
& 16 v_1^4 \omega_2^2 - 24 \omega_1 v_1^4 \omega_2^2 - 8 c_s^4 \omega_1 \omega_2^2 - 48 c_s^2 \omega_1^2 v_1^2 \omega_2^2 - 4 c_s^2 \omega_1^2 + 8 c_s^4 \omega_2^2 + c_s^4 \omega_1^2 \omega_2^2 - 16 \omega_1 v_1^2 \omega_2 + 4 c_s^2 \omega_1^2 \omega_2 + 7 \omega_1^2 v_1^4 \omega_2^2 - 12 \omega_1^2 v_1^4 \omega_2 - 16 v_1^2 \omega_2^2 - \\
& c_s^2 \omega_1^2 \omega_2^2 + 24 \omega_1 v_1^2 \omega_2^2 - 4 c_s^4 \omega_1^2 \omega_2 - 4 \omega_1^2 v_1^2 + 24 c_s^2 \omega_1^2 v_1^2 \omega_2^2 \\
C_2 &= 11 \omega_1^2 v_1^2 \omega_2^2 - 12 \omega_2^2 - 4 \omega_1^2 \omega_2^2 + 20 c_s^2 \omega_2^2 - 24 c_s^2 \omega_1 \omega_2^2 + 8 c_s^2 \omega_1 \omega_2 + 8 \omega_1^2 \omega_2 - 20 \omega_1^2 v_1^2 \omega_2 - 4 \omega_1^2 + 8 c_s^2 \omega_1^2 + 24 \omega_1 v_1^2 \omega_2 - 12 c_s^2 \omega_1^2 \omega_2 - 8 \omega_1 \omega_2 + \\
& 16 \omega_1 \omega_2^2 + 28 v_1^2 \omega_2^2 + 5 c_s^2 \omega_1^2 \omega_2^2 - 40 \omega_1 v_1^2 \omega_2^2 + 8 \omega_1^2 v_1^2 \\
C_3 &= 2 \omega_2^2 - 3 \omega_1^2 v_2^2 \omega_2 - 6 c_s^2 \omega_2^2 + 9 c_s^2 \omega_1 \omega_2^2 - 6 c_s^2 \omega_1 \omega_2 + 3 \omega_1^2 \omega_2 - 4 \omega_1^2 + 3 \omega_1 v_2^2 \omega_2^2 + 12 c_s^2 \omega_1^2 - 4 v_2^2 \omega_2^2 - 4 \omega_1 v_1^2 \omega_2 - 9 c_s^2 \omega_1^2 \omega_2 + 2 \omega_1 \omega_2 - \\
& 3 \omega_1 \omega_2^2 + 2 v_1^2 \omega_2^2 + 2 \omega_1^2 v_2^2 + 2 \omega_1 v_2^2 \omega_2 + 2 \omega_1^2 v_1^2 \\
C_4 &= 3 \omega_3 c_s^2 \omega_1 \omega_2^2 - \omega_3 \omega_1^2 v_2^2 \omega_2 - 4 \omega_3 c_s^2 \omega_2^2 - 2 \omega_1^2 v_2^2 \omega_2 + 6 c_s^2 \omega_1 \omega_2^2 + \omega_3 \omega_1^2 \omega_2 + 2 \omega_1^2 \omega_2 - 4 \omega_3 c_s^2 \omega_1 \omega_2 - 2 \omega_3 v_2^2 \omega_2^2 + 8 \omega_3 c_s^2 \omega_1^2 - 12 \omega_3 \omega_1 v_1^2 \omega_2 - \\
& 3 \omega_3 c_s^2 \omega_1^2 \omega_2 + 2 \omega_1 v_2^2 \omega_2^2 + 4 \omega_3 \omega_1 \omega_2 + \omega_3 \omega_1 v_2^2 \omega_2^2 - 6 c_s^2 \omega_1^2 \omega_2 + 6 \omega_3 v_1^2 \omega_2^2 + 2 \omega_3 \omega_1^2 v_2^2 - 2 \omega_1 \omega_2^2 - \omega_3 \omega_1 \omega_2^2 - 4 \omega_3 \omega_1^2 + 6 \omega_3 \omega_1^2 v_1^2 \\
C_5 &= -36 \omega_3 c_s^2 \omega_1 \omega_2^2 - 4 \omega_3 \omega_4 \omega_1 \omega_2 - 12 c_s^2 \omega_4 \omega_1^2 \omega_2 - 11 \omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 6 \omega_3 \omega_1^2 v_1^2 \omega_2^2 - 6 \omega_3 \omega_1^2 \omega_2^2 - 24 \omega_3 \omega_4 v_2^2 \omega_2^2 + 6 \omega_4 \omega_1^2 v_1^2 \omega_2^2 - 2 \omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 - \\
& 4 \omega_4 \omega_1^2 v_1^2 \omega_2 - 3 \omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2^2 + 18 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12 \omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 8 \omega_4 \omega_1 \omega_2^2 + 4 \omega_3 \omega_4 \omega_1^2 v_1^2 - 8 \omega_3 \omega_4 \omega_1 \omega_2^2 + 16 \omega_3 c_s^2 \omega_4 \omega_1^2 - 18 \omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 + \\
& 8 \omega_3 \omega_4 v_1^2 \omega_2^2 + 12 \omega_3 \omega_4 \omega_1^2 v_2^2 + 2 \omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 + 3 \omega_3 \omega_4 \omega_1^2 \omega_2^2 + 4 \omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 24 c_s^2 \omega_4 \omega_1 \omega_2^2 + 12 \omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 8 \omega_3 \omega_4 \omega_1^2 - 6 \omega_4 \omega_1^2 \omega_2^2 + \\
& 12 \omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 + 4 \omega_4 \omega_1^2 \omega_2^2 + 16 \omega_3 c_s^2 \omega_4 \omega_2^2 + 18 \omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 + 12 \omega_3 \omega_1 \omega_2^2 + 18 \omega_3 c_s^2 \omega_1^2 \omega_2^2 - 12 \omega_3 \omega_1 v_1^2 \omega_2^2 + 8 \omega_3 \omega_4 \omega_1^2 \omega_2 - 8 \omega_4 \omega_1 v_1^2 \omega_2^2 \\
C_6 &= 2 \omega_1^2 v_2^4 + 6 c_s^2 \omega_1 v_2^2 \omega_2 + 12 c_s^2 \omega_1^2 v_2^2 + 3 \omega_1^2 v_2^2 \omega_2 + 3 \omega_1 v_2^4 \omega_2^2 + 2 c_s^2 \omega_2^2 + 2 c_s^4 \omega_1^2 - 4 v_2^4 \omega_2^2 - 2 c_s^2 \omega_1 \omega_2^2 + 2 \omega_1 v_2^4 \omega_2 - 18 c_s^2 v_2^2 \omega_2^2 + 15 c_s^2 \omega_1 v_2^2 \omega_2^2 + \\
& 14 c_s^4 \omega_1 \omega_2^2 - 3 \omega_1^2 v_2^4 \omega_2 - 3 \omega_1 v_2^2 \omega_2^2 - 2 c_s^2 \omega_1^2 - 14 c_s^4 \omega_2^2 - c_s^4 \omega_1^2 \omega_2^2 + 4 v_2^2 \omega_2^2 + 2 c_s^2 \omega_1^2 \omega_2 - 15 c_s^2 \omega_1^2 v_2^2 \omega_2 - 2 \omega_1^2 v_2^2 - 2 \omega_1 v_2^2 \omega_2 - 2 c_s^4 \omega_1^2 \omega_2 \\
C_7 &= 6 \omega_2^2 - 11 \omega_1^2 v_2^2 \omega_2 - 10 c_s^2 \omega_2^2 + 9 c_s^2 \omega_1 \omega_2^2 + 2 c_s^2 \omega_1 \omega_2 + 5 \omega_1^2 \omega_2 - 4 \omega_1^2 + 11 \omega_1 v_2^2 \omega_2^2 + 8 c_s^2 \omega_1^2 - 14 v_2^2 \omega_2^2 - 9 c_s^2 \omega_1^2 \omega_2 - 2 \omega_1 \omega_2 - 5 \omega_1 \omega_2^2 + 8 \omega_1^2 v_2^2 + 6 \omega_1 v_2^2 \omega_2 \\
C_8 &= -18 c_s^2 \omega_4 - 6 \omega_3 c_s^2 \omega_4 \omega_1 + 18 \omega_3 c_s^2 \omega_4 + 9 c_s^2 \omega_4 \omega_1 + 6 \omega_3 + 3 \omega_3 \omega_1 v_2^2 - 18 \omega_3 c_s^2 - 6 \omega_3 \omega_4 + 6 \omega_4 - 3 \omega_3 \omega_1 - 2 \omega_3 \omega_4 \omega_1 v_2^2 + 3 \omega_4 \omega_1 v_2^2 - \\
& 6 \omega_3 v_2^2 + 2 \omega_3 \omega_4 \omega_1 - 3 \omega_4 \omega_1 + 6 \omega_3 \omega_4 v_2^2 + 9 \omega_3 c_s^2 \omega_1 - 6 \omega_4 v_2^2 \\
C_9 &= -3 v_3^2 \omega_1^2 \omega_2 + 2 \omega_2^2 - 6 c_s^2 \omega_2^2 + 9 c_s^2 \omega_1 \omega_2^2 - 6 c_s^2 \omega_1 \omega_2 + 3 \omega_1^2 \omega_2 - 4 v_3^2 \omega_2^2 - 4 \omega_1^2 + 12 c_s^2 \omega_1^2 + 3 v_3^2 \omega_1 \omega_2^2 - 4 \omega_1 v_1^2 \omega_2 - 9 c_s^2 \omega_1^2 \omega_2 + 2 \omega_1 \omega_2 + \\
& 2 v_3^2 \omega_1^2 - 3 \omega_1 \omega_2^2 + 2 v_1^2 \omega_2^2 + 2 v_3^2 \omega_1 \omega_2 + 2 \omega_1^2 v_1^2 \\
C_{10} &= 3 \omega_3 c_s^2 \omega_1 \omega_2^2 - 2 v_3^2 \omega_1^2 \omega_2 - 4 \omega_3 c_s^2 \omega_2^2 - \omega_3 v_3^2 \omega_1^2 \omega_2 + 6 c_s^2 \omega_1 \omega_2^2 + \omega_3 \omega_1^2 \omega_2 + 2 \omega_1^2 \omega_2 - 4 \omega_3 c_s^2 \omega_1 \omega_2 - 2 \omega_3 v_3^2 \omega_2^2 + 8 \omega_3 c_s^2 \omega_1^2 - 12 \omega_3 \omega_1 v_1^2 \omega_2 - \\
& 3 \omega_3 c_s^2 \omega_1^2 \omega_2 + 2 v_3^2 \omega_1 \omega_2^2 + \omega_3 v_3^2 \omega_1 \omega_2^2 + 4 \omega_3 \omega_1 \omega_2 - 6 c_s^2 \omega_1^2 \omega_2 + 6 \omega_3 v_1^2 \omega_2^2 - 2 \omega_1 \omega_2^2 - \omega_3 \omega_1 \omega_2^2 + 2 \omega_3 v_3^2 \omega_1^2 - 4 \omega_3 \omega_1^2 + 6 \omega_3 \omega_1^2 v_1^2
\end{aligned}$$

$$C_{11} = -36\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 18\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - 12c_s^2 \omega_4 \omega_1^2 \omega_2 - 11\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 + 6\omega_4 \omega_1^2 v_1^2 \omega_2^2 - 2\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2 - 4\omega_4 \omega_1^2 v_1^2 \omega_2 - 3\omega_3 \omega_4 \omega_1^2 v_1^2 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_4 \omega_1 \omega_2^2 + 4\omega_3 \omega_4 \omega_1^2 v_1^2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 - 24\omega_3 v_3^2 \omega_4 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_1^2 + 8\omega_3 \omega_4 v_1^2 \omega_2^2 + 2\omega_3 \omega_4 \omega_1 v_1^2 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 18\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 24c_s^2 \omega_4 \omega_1 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 - 6\omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 + 16\omega_3 c_s^2 \omega_4 \omega_2^2 + 12\omega_3 v_3^2 \omega_4 \omega_1^2 + 12\omega_3 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_1 v_1^2 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 + 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 - 8\omega_4 \omega_1 v_1^2 \omega_2^2$$

$$C_{12} = -2\omega_2^2 + 6c_s^2 \omega_2^2 - 12c_s^2 \omega_1 \omega_2 + v_3^2 \omega_2^2 - 2\omega_1^2 + 6c_s^2 \omega_1^2 + v_2^2 \omega_2^2 + 4\omega_1 \omega_2 + v_3^2 \omega_1^2 + \omega_1^2 v_2^2 - 2\omega_1 v_2 \omega_2 - 2v_3^2 \omega_1 \omega_2$$

$$C_{13} = 18\omega_3 c_s^2 \omega_1 \omega_2^2 + 3v_3^2 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - \omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 + 3\omega_3 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_4 v_2^2 \omega_2^2 - 3\omega_3 v_3^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 2v_3^2 \omega_4 \omega_1^2 \omega_2 - \omega_3 \omega_4 \omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_4 \omega_2^2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 6\omega_3 \omega_4 \omega_1^2 v_2^2 + \omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_3^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 \omega_4 \omega_1 v_2^2 \omega_2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 + 2\omega_3 v_3^2 \omega_4 \omega_1^2 - 6\omega_3 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - 4v_3^2 \omega_4 \omega_1 \omega_2^2$$

$$C_{14} = -2\omega_4 \omega_1^2 v_2^2 \omega_2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 + 3\omega_3 \omega_1^2 \omega_2^2 - 2\omega_3 \omega_4 v_2^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 3\omega_3 \omega_1^2 v_2^2 \omega_2^2 - \omega_3 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_3^2 \omega_4 \omega_2^2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 3\omega_4 \omega_1^2 v_2^2 \omega_2^2 - \omega_3 \omega_4 \omega_1^2 v_2^2 \omega_2 + 2\omega_3 \omega_4 \omega_1^2 v_2^2 + 6\omega_3 \omega_1 v_2^2 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 - 4\omega_4 \omega_1 v_2^2 \omega_2^2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 + 6\omega_3 v_3^2 \omega_4 \omega_1^2 + \omega_3 \omega_4 \omega_1 v_2^2 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2$$

$$C_{15} = -6c_s^2 \omega_4 + 3c_s^2 \omega_4 \omega_1 - 2\omega_3 + 2\omega_3 v_3^2 - 2v_3^2 \omega_4 + 6\omega_3 c_s^2 + 2\omega_4 + v_3^2 \omega_4 \omega_1 + \omega_3 \omega_1 - \omega_3 v_3^2 \omega_1 - \omega_4 \omega_1 - 3\omega_3 c_s^2 \omega_1$$

$$C_{16} = 6c_s^2 v_3^2 \omega_1 \omega_2 + 3v_3^2 \omega_1^2 \omega_2 + 12c_s^2 v_3^2 \omega_1^2 + 2c_s^2 \omega_2^2 + 2c_s^4 \omega_1^2 - 2c_s^2 \omega_1 \omega_2^2 - 3v_3^4 \omega_1^2 \omega_2 + 2v_3^4 \omega_1^2 + 4v_3^2 \omega_2^2 + 15c_s^2 v_3^2 \omega_1 \omega_2^2 + 14c_s^4 \omega_1 \omega_2^2 - 18c_s^2 v_3^2 \omega_2^2 - 2c_s^2 \omega_1^2 - 14c_s^4 \omega_2^2 - c_s^4 \omega_1^2 \omega_2^2 - 3v_3^2 \omega_1 \omega_2^2 + 2v_3^4 \omega_1 \omega_2 + 2c_s^2 \omega_1^2 \omega_2 - 4v_3^4 \omega_2^2 - 2v_3^2 \omega_1^2 + 3v_3^2 \omega_1 \omega_2^2 - 15c_s^2 v_3^2 \omega_1^2 \omega_2 - 2v_3^2 \omega_1 \omega_2^2 - 2c_s^4 \omega_1^2 \omega_2$$

$$C_{17} = -11v_3^2 \omega_1^2 \omega_2 + 6\omega_2^2 - 10c_s^2 \omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 14v_3^2 \omega_2^2 - 4\omega_1^2 + 8c_s^2 \omega_1^2 + 11v_3^2 \omega_1 \omega_2^2 - 9c_s^2 \omega_1^2 \omega_2 - 2\omega_1 \omega_2 + 8v_3^2 \omega_1^2 - 5\omega_1 \omega_2^2 + 6v_3^2 \omega_1 \omega_2$$

$$C_{18} = -6c_s^2 \omega_4 + 3c_s^2 \omega_4 \omega_1 - 2\omega_3 - \omega_3 \omega_1 v_2^2 + 6\omega_3 c_s^2 + 2\omega_4 + \omega_3 \omega_1 + \omega_4 \omega_1 v_2^2 + 2\omega_3 v_2^2 - \omega_4 \omega_1 - 3\omega_3 c_s^2 \omega_1 - 2\omega_4 v_2^2$$

$$C_{19} = -18c_s^2 \omega_4 - 6\omega_3 c_s^2 \omega_4 \omega_1 + 18\omega_3 c_s^2 \omega_4 + 9c_s^2 \omega_4 \omega_1 + 6\omega_3 - 6\omega_3 v_3^2 + 6\omega_3 v_3^2 \omega_4 - 6v_3^2 \omega_4 - 18\omega_3 c_s^2 - 6\omega_3 \omega_4 + 6\omega_4 + 3v_3^2 \omega_4 \omega_1 - 3\omega_3 \omega_1 + 3\omega_3 v_3^2 \omega_1 - 2\omega_3 v_3^2 \omega_4 \omega_1 + 2\omega_3 \omega_4 \omega_1 - 3\omega_4 \omega_1 + 9\omega_3 c_s^2 \omega_1$$

$$C_{20} = -196\omega_3 \omega_1^2 v_1^2 \omega_2^3 - 80\omega_3 c_s^2 \omega_1 \omega_2^2 + 72\omega_3 c_s^4 \omega_1^3 - 184\omega_3 c_s^2 \omega_2^3 - 102\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2^3 - 8c_s^2 \omega_1 \omega_2^3 - 27\omega_3 \omega_1^3 v_1^4 \omega_2^3 - 10\omega_3 \omega_1^3 \omega_2 + 16\omega_3 \omega_1^2 \omega_2^3 + 8c_s^2 \omega_1 v_1^2 \omega_2^3 + 320\omega_3 c_s^2 \omega_1 \omega_2^3 + 280\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 16\omega_3 \omega_1^2 \omega_2^2 + 760\omega_3 c_s^2 v_1^2 \omega_2^3 + 90\omega_3 \omega_1^3 v_1^4 \omega_2^2 + 8c_s^2 \omega_1^3 v_1^2 \omega_2 + 404\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2^2 + 72\omega_3 c_s^4 \omega_1 \omega_2^2 + 168\omega_3 \omega_1 v_1^2 \omega_2^2 + 8\omega_3 \omega_1^2 \omega_2^2 - 3\omega_3 \omega_1^2 \omega_2^2 + 656\omega_3 c_s^2 \omega_1 v_1^2 \omega_2^2 + 144\omega_3 v_1^2 \omega_2^3 - 84\omega_3 \omega_1^3 v_1^4 \omega_2 - 464\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2 + 24c_s^4 \omega_1 \omega_2^3 - 104\omega_3 \omega_1^2 v_1^2 \omega_2 + 24\omega_3 \omega_1^3 v_1^4 + 160\omega_3 c_s^2 \omega_1^3 v_1^2 - 1472\omega_3 c_s^2 \omega_1 v_1^2 \omega_2^2 + 8\omega_3 \omega_1^2 \omega_2^2 - 372\omega_3 c_s^4 \omega_1 \omega_2^3 - 300\omega_3 \omega_1 v_1^2 \omega_2^2 + 16\omega_3 \omega_2^3 + 164\omega_3 c_s^4 \omega_1^2 \omega_2^3 - 1088\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2^2 - 264\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 156\omega_3 c_s^4 \omega_1^2 \omega_2^3 - 80\omega_3 c_s^2 \omega_1^2 \omega_2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^3 - 98\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 48c_s^4 \omega_1^2 \omega_2^2 + 180\omega_3 \omega_1^2 v_1^2 \omega_2^3 + 216\omega_3 c_s^4 \omega_2^3 - 52\omega_3 c_s^2 \omega_1^3 + 808\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2^3 - 120\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 30\omega_3 \omega_1^3 v_1^2 \omega_2^3 + 24c_s^4 \omega_1^3 \omega_2 - 28\omega_3 \omega_1^3 v_1^2 - 78\omega_3 c_s^2 \omega_1^3 \omega_2^2 + 122\omega_3 c_s^2 \omega_1^3 \omega_2 + 4\omega_3 \omega_1^3 + 328\omega_3 \omega_1 v_1^2 \omega_2^3 - 156\omega_3 c_s^2 \omega_1^2 \omega_2^3 - 15\omega_3 c_s^4 \omega_1^2 \omega_2^3 + 72\omega_3 c_s^4 \omega_1^2 \omega_2 + 8\omega_3 \omega_1 \omega_2^2 + 16c_s^2 \omega_1^2 \omega_2^2 + 152\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 176\omega_3 \omega_1 v_1^2 \omega_2^2 - 160\omega_3 v_1^2 \omega_2^2 + 94\omega_3 \omega_1^3 v_1^2 \omega_2 - 8c_s^2 \omega_1^3 \omega_2 + 440\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2 - 28\omega_3 \omega_1 \omega_2^2 + 82\omega_3 c_s^4 \omega_1^3 \omega_2^2 - 16c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 96\omega_3 \omega_1^2 v_1^4 \omega_2$$

$$C_{21} = -308\omega_3 \omega_1^2 v_1^2 \omega_2^3 - 16\omega_3 c_s^2 \omega_1 \omega_2^2 + 16\omega_3 c_s^4 \omega_1^3 - 56\omega_3 c_s^2 \omega_2^3 - 54\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2^3 - 8c_s^2 \omega_1 \omega_2^3 - 87\omega_3 \omega_1^3 v_1^4 \omega_2^3 - 10\omega_3 \omega_1^3 \omega_2 + 16\omega_3 \omega_1^2 \omega_2^3 + 24c_s^2 \omega_1 v_1^2 \omega_2^3 + 96\omega_3 c_s^2 \omega_1 \omega_2^3 + 408\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 16\omega_3 \omega_1^2 \omega_2^2 + 552\omega_3 c_s^2 v_1^2 \omega_2^3 + 310\omega_3 \omega_1^3 v_1^4 \omega_2^2 + 24c_s^2 \omega_1^3 v_1^2 \omega_2 + 252\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2^2 + 8\omega_3 c_s^4 \omega_1 \omega_2^2 + 552\omega_3 \omega_1 v_1^4 \omega_2^2 + 8\omega_3 \omega_1^2 \omega_2 - 3\omega_3 \omega_1^2 \omega_2^2 + 336\omega_3 c_s^2 \omega_1 v_1^2 \omega_2^2 + 528\omega_3 v_1^4 \omega_2^3 - 312\omega_3 \omega_1^3 v_1^4 \omega_2 - 360\omega_3 c_s^2 \omega_1^3 v_1^2 \omega_2 + 8c_s^4 \omega_1 \omega_2^3 - 168\omega_3 \omega_1^2 v_1^2 \omega_2 + 96\omega_3 \omega_1^3 v_1^4 + 144\omega_3 c_s^2 \omega_1^3 v_1^2 - 1008\omega_3 c_s^2 \omega_1 v_1^2 \omega_2^3 + 8\omega_3 \omega_1^2 \omega_2^2 - 68\omega_3 c_s^4 \omega_1 \omega_2^3 - 1068\omega_3 \omega_1 v_1^2 \omega_2^2 + 16\omega_3 \omega_2^3 + 28\omega_3 c_s^4 \omega_1^2 \omega_2^3 - 576\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2^2 - 888\omega_3 v_1^2 \omega_2^2 - 32\omega_3 c_s^4 \omega_1^3 \omega_2 - 16\omega_3 c_s^2 \omega_1^2 \omega_2 + 6\omega_3 c_s^2 \omega_1^2 \omega_2^3 - 154\omega_3 \omega_1^3 v_1^2 \omega_2^2 - 16c_s^4 \omega_1^2 \omega_2^2 + 620\omega_3 \omega_1^2 v_1^2 \omega_2^3 + 40\omega_3 c_s^4 \omega_2^3 - 20\omega_3 c_s^2 \omega_1^3 + 504\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2^3 - 8\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 42\omega_3 \omega_1^3 v_1^2 \omega_2^3 + 8c_s^4 \omega_1^3 \omega_2 - 60\omega_3 \omega_1^3 v_1^2 - 22\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 42\omega_3 c_s^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_1^3 + 552\omega_3 \omega_1 v_1^2 \omega_2^2 - 44\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 3\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 8\omega_3 c_s^4 \omega_1^2 \omega_2 + 8\omega_3 \omega_1 \omega_2^2 + 16c_s^2 \omega_1^2 \omega_2^2 + 24\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 240\omega_3 \omega_1 v_1^2 \omega_2^2 - 288\omega_3 v_1^2 \omega_2^2 + 174\omega_3 \omega_1^3 v_1^2 \omega_2 - 8c_s^2 \omega_1^3 \omega_2 + 264\omega_3 c_s^2 \omega_1^2 v_1^2 \omega_2 - 28\omega_3 \omega_1 \omega_2^2 + 14\omega_3 c_s^4 \omega_1^3 \omega_2^2 - 48c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 336\omega_3 \omega_1^2 v_1^4 \omega_2$$

$$C_{22} = -24\omega_3 \omega_1^3 v_1^2 \omega_2^2 + 96\omega_3 \omega_1 v_2^2 v_1^2 \omega_2^3 - 12c_s^2 \omega_1^3 v_2^2 \omega_2^2 - 4\omega_3 c_s^2 \omega_1^3 v_2^2 \omega_2 + 40\omega_3 c_s^2 \omega_1^2 \omega_2 + 72\omega_3 c_s^2 \omega_1^2 v_2^2 \omega_2^2 + 22\omega_3^2 c_s^2 \omega_1 v_2^2 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 72\omega_3^2 \omega_1^2 v_2^4 \omega_2^2 - 84\omega_3^2 c_s^4 \omega_1^3 \omega_2 + 8\omega_3^2 \omega_1 \omega_2^2 - 8\omega_3^2 \omega_1 v_2^2 \omega_2^3 - 5\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 + 8\omega_3 c_s^2 \omega_1 v_2^2 \omega_2^3 - 8\omega_3 c_s^2 \omega_1 \omega_2^3 + 24\omega_3^2 v_1^2 \omega_2^3 + 4\omega_3^2 \omega_1^3 + 24\omega_3^2 \omega_1 v_2^2 \omega_2^2 - 8\omega_3^2 \omega_1 v_2^2 \omega_2^2 - 20\omega_3^2 c_s^2 \omega_1^3 v_2^2 \omega_2 + 8\omega_3^2 \omega_1 \omega_2^3 + 4\omega_3^2 \omega_1^2 v_2^2 \omega_2 + 42\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 + 8\omega_3^2 c_s^2 \omega_1 v_2^2 \omega_2^2 + 2\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2^2 - \omega_3^2 \omega_1^3 v_2^2 \omega_2^2 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2 + 56\omega_3^2 c_s^2 \omega_1^2 \omega_2 + 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 60\omega_3^2 \omega_1 v_2^2 \omega_2^2 + 108\omega_3^2 c_s^2 \omega_1 v_1^2 \omega_2^2 - 4\omega_3^2 \omega_1^3 v_2^2 + 8\omega_3^2 v_2^2 \omega_2^2 + 6\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 - 52\omega_3^2 c_s^2 \omega_1^3 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 + 24\omega_3^2 c_s^4 \omega_1 \omega_2^3 + 84\omega_3^2 \omega_1^2 v_1^2 \omega_2 - 216\omega_3^2 c_s^2 \omega_1 v_1^2 \omega_2^2 + 18\omega_3^2 c_s^2 \omega_1^3 v_2^2 \omega_2 - 48\omega_3^2 \omega_1^2 v_1^2 \omega_2^2 + 48\omega_3^2 \omega_1 v_1^2 \omega_2^2 - 34\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 324\omega_3^2 c_s^2 \omega_1^2 v_1^2 \omega_2 - 4\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2 + 12c_s^2 \omega_1^3 \omega_2^2 - 8\omega_3^2 \omega_2^3 - 54\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 48\omega_3^2 v_1^4 \omega_2^3 + 4\omega_3^2 \omega_1^2 v_2^2 \omega_2 - 4\omega_3^2 \omega_1^2 \omega_2^2 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2 - 72\omega_3^2 c_s^2 \omega_1^2 v_1^2 \omega_2^2 + 24\omega_3^2 \omega_1^2 v_2^2 v_1^2 + 12c_s^2 \omega_1^2 v_2^2 \omega_2^3 - 24\omega_3^2 \omega_1^2 v_2^2 v_1^2 \omega_2^2 + 24\omega_3^2 \omega_1^2 v_2^2 \omega_2^2 - 8\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 + \omega_3^2 \omega_1^3 \omega_2^2 + 24\omega_3^2 \omega_1^3 v_1^2 - 48\omega_3^2 \omega_1^2 v_2^2 v_1^2 \omega_2 + 36c_s^4 \omega_1^2 \omega_2^2 - 22\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 48\omega_3^2 \omega_1^2 v_2^2 v_1^2 \omega_2 - 24\omega_3^2 \omega_1^2 v_2^2 \omega_2^2 + 216\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2 - 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2^2 - 24\omega_3^2 \omega_1^2 v_2^2 \omega_2 - 36c_s^4 \omega_1^2 \omega_2^2 + 24\omega_3^2 \omega_1^2 v_2^2 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2 + 20\omega_3^2 c_s^2 \omega_2^3 + 72\omega_3^2 c_s^4 \omega_1^3 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + \omega_3^2 \omega_1^2 v_2^2 \omega_2^2 - 36\omega_3^2 \omega_1^3 v_1^2 \omega_2 - \omega_3^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 \omega_1^2 \omega_2 - 72\omega_3^2 \omega_1 v_1^2 \omega_2^2 + 24\omega_3^2 \omega_1^2 v_2^2 v_1^2 \omega_2^2 + 16\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2 - 2\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 20\omega_3^2 c_s^2 v_2^2 \omega_2^2 - 18\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2^2 - 2\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2^2 - 36\omega_3^2 \omega_1 v_1^2 \omega_2^2 - 12c_s^2 \omega_1^2 \omega_2^2 + 42\omega_3^2 c_s^4 \omega_1 \omega_2^3 + 54\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 - 4\omega_3^2 \omega_1^2 \omega_2^2 + 4\omega_3^2 \omega_2^2 v_2^2 \omega_2^2 - 72\omega_3^2 v_2^2 v_1^2 \omega_2^2 + 216\omega_3^2 c_s^2 \omega_1^3 v_1^2$$

$$C_{23} = 9\omega_1^2 \omega_2^3 - 54\omega_3 c_s^2 \omega_1 \omega_2^2 + 6\omega_3 \omega_1^3 \omega_2 - 12\omega_3 c_s^2 \omega_2^3 + 36c_s^2 \omega_1 \omega_2^3 + 6\omega_3 \omega_1^2 v_2^2 \omega_2 + 48\omega_3 \omega_1^3 \omega_2 + 5\omega_3 \omega_1^2 \omega_2^3 + 27\omega_3 c_s^2 \omega_1 \omega_2^3 + 6\omega_1^2 \omega_2^2 + 132\omega_3 \omega_1^2 v_1^2 \omega_2^2 - 51\omega_3 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_1^2 \omega_2^2 - 5\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 12\omega_3 \omega_1^2 v_2^2 \omega_2 - 6\omega_1^2 v_2^2 \omega_2^2 - 9\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 5\omega_3 \omega_1^2 \omega_2^2 - 12\omega_3 \omega_2^3 - 9\omega_1^2 v_2^2 \omega_2^3 - 9\omega_1^3 \omega_2^2 + 27c_s^2 \omega_1^3 \omega_2^2 + 27\omega_3 \omega_1 v_2^2 \omega_2^3 + 12\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 6\omega_1^3 v_2^2 \omega_2 - 18\omega_3 \omega_1^3 v_2^2 \omega_2 + 84\omega_3 c_s^2 \omega_1^3 + 6\omega_3 \omega_1 v_2^2 \omega_2^2 - 24\omega_3 v_2^2 \omega_2^3 + 48\omega_3 \omega_1^3 v_1^2 + 15\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 12\omega_1 v_2^2 \omega_2^2 - 108\omega_3 c_s^2 \omega_1^2 \omega_2 - 36\omega_3 \omega_1^3 - 66\omega_3 \omega_1 v_1^2 \omega_2^3 - 15\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 5\omega_3 \omega_1^2 v_2^2 \omega_2^2 + 42\omega_3 \omega_1 \omega_2^2 - 18c_s^2 \omega_1^2 \omega_2^2 + 81\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 120\omega_3 \omega_1 v_1^2 \omega_2^2 + 84\omega_3 v_1^2 \omega_2^2 - 12\omega_1 \omega_2^2 + 9\omega_1^3 v_2^2 \omega_2^2 - 66\omega_3 \omega_1^3 v_1^2 \omega_2 - 18c_s^2 \omega_1^3 \omega_2 - 27c_s^2 \omega_1^2 \omega_2^2 + 3\omega_3 \omega_1 \omega_2^2$$

$$C_{40} = 72\omega_3^2 v_3^2 \omega_4^2 v_2^2 \omega_3^2 + 30\omega_3^2 c_4^2 \omega_4^2 \omega_1^2 \omega_3^2 + 54\omega_3^2 c_8^2 \omega_3^2 \omega_1^2 \omega_3^2 + 72\omega_3^2 \omega_4^2 \omega_1^2 v_2^2 \omega_3^2 + 64\omega_3^2 c_2^2 \omega_4^2 \omega_1^2 \omega_3^2 + 324\omega_3^2 c_4^2 \omega_1^2 \omega_3^3 - 81\omega_3^2 c_8^2 \omega_4^2 \omega_1^2 \omega_3^3 + 8\omega_3^2 \omega_4^2 \omega_3^2 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2 + 56\omega_3^2 c_8^2 \omega_4^2 \omega_1 \omega_2 - 72\omega_3^2 c_2^2 \omega_4^2 \omega_1 \omega_2 - 84c_8^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 - 56\omega_3^2 c_2^2 \omega_4^2 \omega_1 \omega_2 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 + 108\omega_3^2 c_2^2 \omega_4^2 \omega_1^2 \omega_2 + 128\omega_3^2 c_8^2 \omega_4^2 \omega_1 \omega_2 + 27\omega_3^2 c_2^2 v_3^2 \omega_4^2 \omega_1^2 + 120\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 v_2^2 \omega_3^2 - 104\omega_3^2 c_2^2 \omega_4^2 \omega_1^2 + 48\omega_3^2 c_8^2 \omega_4^2 \omega_1^2 v_2^2 - 252c_4^2 \omega_4^2 \omega_1^2 \omega_3^2 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_3^2 + 324\omega_3^2 c_4^2 \omega_1^2 \omega_3^3 + 432\omega_3^2 c_8^2 \omega_4^2 \omega_1^2 \omega_3^3 - 24\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 v_2^2 \omega_2 - 162\omega_3^2 c_4^2 \omega_1^2 \omega_3^3 - 96\omega_3^2 \omega_4^2 v_2^2 \omega_3^2 - 24\omega_3^2 c_2^2 \omega_4^2 \omega_1^2 \omega_2 + 8\omega_3^2 c_8^2 v_3^2 \omega_4^2 \omega_1^2 \omega_3^2 - 72c_4^2 \omega_4^2 \omega_1^2 \omega_2 + 96\omega_3^2 \omega_4^2 \omega_1 v_2^2 \omega_3^2 + 324\omega_3^2 c_8^2 \omega_4^2 \omega_1^2 \omega_2 + 192\omega_3^2 c_4^2 \omega_4^2 \omega_1^2 \omega_2 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1 \omega_2 - 24c_8^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 - 432\omega_3^2 c_8^2 \omega_4^2 \omega_1 v_2^2 \omega_3^2 - 108\omega_3^2 c_4^2 \omega_4^2 \omega_1 v_2^2 \omega_3^2 + 96\omega_3^2 \omega_4^2 \omega_1 v_2 \omega_2 - 96\omega_3^2 \omega_4^2 \omega_1 v_2 - 432\omega_3^2 c_8^2 \omega_4^2 \omega_1 v_2 \omega_2 - 27c_4^2 \omega_4^2 \omega_1^2 \omega_3^2 - 56\omega_3^2 c_2^2 \omega_4^2 \omega_1 \omega_3^2 + 192\omega_3^2 c_4^2 \omega_4^2 \omega_1^2 \omega_3^2 - 108\omega_3^2 c_8^2 \omega_4^2 \omega_1^2 \omega_3^2 + 96\omega_3^2 \omega_4^2 \omega_1^2 \omega_3^2 - 96\omega_3^2 \omega_4^2 \omega_1^2 v_2 - 432\omega_3^2 c_8^2 \omega_4^2 \omega_1^2 v_2 \omega_2 -$$

$$\begin{aligned}
& 168\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2 + 432\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 144\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 - 72\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 30\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 432\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 \omega_2^2 + 54c_s^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2^3 + \\
& 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 10\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 + 32\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 27\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 32\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^3 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 - 16\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 24\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - 104\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 + 27\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 54\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 48\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 80\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 168\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 10\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 192\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 40\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 84c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 324\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 864\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 216\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^3 + 8\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 432\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 108\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 24c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 36\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + \\
& 108\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 60\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 176\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 10\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 144\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 96\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + \\
& 64\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 24\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 64\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 54c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 81\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 36\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 112\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 60\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 10\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 108\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 96\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3
\end{aligned}$$

$$C_{42} = -24\omega_3 c_s^2 \omega_1 \omega_2^2 + 2\omega_3^2 \omega_2 + 26\omega_3 c_s^2 \omega_2^3 - 6c_s^2 \omega_1 \omega_2^3 - 22\omega_3 \omega_1^2 v_2^2 \omega_2 + 10\omega_3 \omega_3^2 \omega_2 - 24\omega_3 c_s^2 \omega_1 \omega_2^3 - 4\omega_1^2 \omega_2^3 - 20\omega_3 \omega_2^3 \omega_2^2 - 4\omega_3 v_3^2 \omega_1^2 \omega_2 + 14\omega_3 \omega_1^2 \omega_2 + 6\omega_3 v_3^2 \omega_1^2 \omega_2^2 - 2v_3^2 \omega_1^3 \omega_2 + 4\omega_3 v_3^2 \omega_2^3 + 26\omega_3 \omega_1^2 v_2^2 \omega_2^2 - 3\omega_3 v_3^2 \omega_1^3 \omega_2 - 10\omega_3 \omega_2^3 + 4v_3^2 \omega_1^2 \omega_2^2 - 13\omega_3 \omega_1 v_2^2 \omega_2^3 - 3\omega_3 v_3^2 \omega_1 \omega_2^3 + 16\omega_3 \omega_1^2 v_2^2 - 30\omega_3 c_s^2 \omega_1^2 \omega_2 - 13\omega_3 \omega_1^2 v_2^2 \omega_2 - 4\omega_3 v_3^2 \omega_1 \omega_2^2 + 28\omega_3 c_s^2 \omega_1^3 - 4\omega_3 \omega_1 v_2^2 \omega_2^2 + 10\omega_3 v_2^2 \omega_2^3 - 2v_3^2 \omega_1 \omega_2^3 - 24\omega_3 c_s^2 \omega_1^3 \omega_2 - 12\omega_3 \omega_1^3 + 8\omega_3 \omega_1 \omega_2^2 + 12c_s^2 \omega_1^2 \omega_2^2 + 48\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 2\omega_1 \omega_2^3 - 6c_s^2 \omega_1^3 \omega_2 + 4\omega_3 v_3^2 \omega_1^3 + 10\omega_3 \omega_1 \omega_2^3$$

$$C_{44} = -2\omega_3^2\omega_4\omega_1 - 6\omega_3\omega_4^2 - 18\omega_3c_s^2\omega_4\omega_1 - 6\omega_3^2v_2^2 + 36\omega_3c_s^2\omega_4 + 2\omega_3^2v_3\omega_4\omega_1 - 6v_3^2\omega_4^2 + 2\omega_3\omega_2^2\omega_1 - 6\omega_4^2\omega_1 + 6\omega_3v_3^2\omega_4^2 - 6\omega_3^2v_2^2 - 2\omega_3v_3^2\omega_2^2\omega_1 + 3v_3^2\omega_4^2\omega_1 + 12\omega_4^2 - 3\omega_3^2v_3\omega_1 + 3\omega_4^2\omega_1v_2^2 + 18\omega_3c_s^2\omega_4^2 - 36c_s^2\omega_4^2 - 12\omega_3\omega_4 + 6\omega_3^2c_s^2\omega_4\omega_1 - 6\omega_3^2v_3^2\omega_4 + 6\omega_3^2\omega_4 - 6\omega_3\omega_4\omega_1v_2^2 + 6\omega_3^2v_3^2 + 18c_s^2\omega_2^2\omega_1 + 6\omega_3\omega_4\omega_1 - 18\omega_3^2c_s^2\omega_4 + 12\omega_3\omega_4v_2^2 + 3\omega_3^2\omega_1v_2^2 - 6\omega_3c_s^2\omega_4^2\omega_1$$

$$\begin{aligned}
& 132\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2 + 72\omega_3v_3^4\omega_4^2\omega_1^3\omega_5\omega_2^2 + 9\omega_3^2\omega_4\omega_1^3v_1^4\omega_5\omega_2^3 - 168\omega_3c_s^2\omega_4^2\omega_1v_2^2\omega_5\omega_2^2 + 240\omega_3^2c_s^2\omega_4^2v_2^2\omega_5\omega_2^3 + 216\omega_3c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + \\
& 72\omega_3^2v_3^2\omega_4^2\omega_1\omega_5\omega_2^2 + 27\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5\omega_2^3 - 468\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 - 18\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2 - 24\omega_3v_3^4\omega_4^2\omega_1^3\omega_5\omega_2 + 144\omega_3^2v_3^2\omega_4\omega_1^2\omega_5\omega_2^3 - \\
& 72v_3^4\omega_4^2\omega_1^2\omega_5\omega_2^3 + 324\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 - 96\omega_3^2v_3^4\omega_4^2\omega_1\omega_5\omega_2^2 + 162c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - 28\omega_3c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^3 - 144\omega_3^2v_3^4\omega_4\omega_1^2\omega_5\omega_2^3 + 72v_3^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + \\
& 18\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_5\omega_2^2 + 24\omega_3v_3^2\omega_4^2\omega_1^3\omega_5\omega_2 + 8\omega_3^2\omega_4\omega_1^3\omega_5 - 108\omega_3^2c_s^2v_3^2\omega_4\omega_1^2\omega_5\omega_2^2 - 108\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + 144\omega_3^2v_3^2\omega_4^2\omega_1^3v_2^2\omega_5 - 40\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5 + \\
& 4\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^2 + 6\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 + 12\omega_3v_3^4\omega_4^2\omega_1\omega_5\omega_2^2 + 56\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^2 - 72\omega_3^2c_s^4\omega_4\omega_1^3\omega_5\omega_2^2 - 2\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 - 108c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2 - \\
& 54\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_5\omega_2^2 - 2\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 + 16\omega_3^2\omega_4^2\omega_1^2\omega_5\omega_2^2 + 36\omega_3^2v_3^2\omega_4\omega_1^2\omega_5\omega_2^2 - 9\omega_3\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + 264\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^2 + 48\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2 + \\
& 72\omega_3^2c_s^2\omega_4\omega_1^3\omega_5\omega_2^2 - 12\omega_3v_3^2\omega_4^2\omega_1\omega_5\omega_2^2 - 72\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^2 + 60\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2 - 216\omega_3^2c_s^2v_3^2\omega_4\omega_1^2\omega_5\omega_2^2 - 9\omega_3^2\omega_4\omega_1^3v_1^4\omega_5\omega_2^3 - 36\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{52} = & -24\omega_3c_s^2\omega_1\omega_2^2 + 2\omega_1^3\omega_2 + 26\omega_3c_s^2\omega_2^2 - 6c_s^2\omega_1\omega_2^3 - 4\omega_3\omega_1^2v_2^2\omega_2 + 10\omega_3\omega_1^2\omega_2 - 24\omega_3c_s^2\omega_1\omega_2^3 - 4\omega_1^2\omega_2^2 - 20\omega_3\omega_1^2\omega_2^2 - 22\omega_3v_3^2\omega_1^2\omega_2 + \\
& 14\omega_3\omega_1^2\omega_2 + 26\omega_3v_3^2\omega_1^2\omega_2^2 + 10\omega_3v_3^2\omega_2^2 + 4\omega_1^2v_2^2\omega_2^2 + 6\omega_3\omega_1^2v_2^2\omega_2^2 - 13\omega_3v_3^2\omega_1^2\omega_2^2 - 10\omega_3\omega_2^3 - 3\omega_3\omega_1v_2^2\omega_2^3 - 13\omega_3v_3^2\omega_1\omega_2^3 + 4\omega_3\omega_1^3v_2^2 - \\
& 30\omega_3c_s^2\omega_1^2\omega_2 - 2\omega_3^2v_2^2\omega_2 - 3\omega_3\omega_1^2v_2^2\omega_2 - 4\omega_3v_3^2\omega_1\omega_2^2 + 28\omega_3c_s^2\omega_1^3 - 4\omega_3\omega_1v_2^2\omega_2^2 + 4\omega_3v_2^2\omega_2^3 - 2\omega_1v_2^2\omega_2^3 - 24\omega_3c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_1^3 + \\
& 8\omega_3\omega_1\omega_2^2 + 12c_s^2\omega_1^2\omega_2^2 + 48\omega_3c_s^2\omega_1^2\omega_2^2 + 2\omega_1\omega_2^3 - 6c_s^2\omega_1^3\omega_2 + 16\omega_3v_3^2\omega_1^3 + 10\omega_3\omega_1\omega_2^3
\end{aligned}$$

$$\begin{aligned}
C_{53} = & -3\omega_4^2\omega_1^3v_2^2\omega_5 + 6\omega_3^2\omega_2^2v_2^2\omega_5 + 9c_s^2v_2^2\omega_4^2\omega_1^3\omega_5 - 6v_3^4\omega_4^2\omega_1^2\omega_5 + 6\omega_3^2v_3^2\omega_4\omega_1^2\omega_5 - 6\omega_4^2\omega_1^2v_3^4\omega_5 + 3\omega_3^2\omega_1^3v_2^2\omega_5 - 6\omega_3^2c_s^2v_3^2\omega_4\omega_1^2\omega_5 + \\
& 2\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 - 9\omega_3^2c_s^2\omega_1^3v_2^2\omega_5 - 32\omega_3^2c_s^4\omega_1^2\omega_5 - 3\omega_3v_3^4\omega_4^2\omega_1^3\omega_5 - 8\omega_3^2c_s^4\omega_4\omega_1\omega_5 - 6\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_5 - 8\omega_3c_s^4\omega_4^2\omega_1^2\omega_5 + 12\omega_3c_s^2\omega_4^2\omega_1v_2^2\omega_5 + \\
& 6\omega_3^2c_s^2v_3^2\omega_4\omega_1^3\omega_5 - 8\omega_3^2c_s^2\omega_4\omega_1^2\omega_5 - 18c_s^2v_3^2\omega_4^2\omega_1^2\omega_5 + 32\omega_3^2c_s^4\omega_4^2\omega_1^2 - 8\omega_3c_s^2\omega_4^2\omega_1\omega_5 + 3v_3^4\omega_4^2\omega_1^3\omega_5 - 3\omega_3^2v_3^2\omega_4\omega_1^3\omega_5 + 12\omega_3c_s^2v_3^2\omega_4^2\omega_1\omega_5 + \\
& 2\omega_3c_s^2\omega_4^2\omega_1^3\omega_5 + 6\omega_3\omega_4^2\omega_1^2v_2^2\omega_5 - 18c_s^2\omega_4^2\omega_1^2v_2^2\omega_5 + 6\omega_3^2\omega_4\omega_1^2v_2^2\omega_5 + 3\omega_3\omega_4^2\omega_1^3v_2^2\omega_5 - 6\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_5 + 3\omega_3^2\omega_4\omega_1^3v_2^2\omega_5 + 6\omega_3v_3^4\omega_4^2\omega_1^2\omega_5 - \\
& 8\omega_3^2\omega_4^2\omega_1^3 - 6\omega_3^2v_3^2\omega_4\omega_1^2\omega_5 - 6\omega_3^2v_3^2\omega_4\omega_1^2\omega_5 + 18\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_5 + 6\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_5 - 2\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5 - 2\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_5 - 6\omega_3^2\omega_4\omega_1^3v_2^2\omega_5 + \\
& 3\omega_4^2\omega_1^3v_3^4\omega_5 + 8\omega_3^2c_s^2\omega_4\omega_1\omega_5 + 3\omega_3v_3^2\omega_4^2\omega_1^3\omega_5 + 16\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_5 + 18\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5 + 8\omega_3c_s^2\omega_4^2\omega_1^2\omega_5 - 3\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_5 + 6\omega_4^2\omega_1^2v_2^2\omega_5 + \\
& 6\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_5 - 12\omega_3^2c_s^2\omega_4\omega_1v_2^2\omega_5 + 6\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_5 + 8\omega_3^2c_s^4\omega_4\omega_1^2\omega_5 + 6\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_5 - 6\omega_3\omega_4^2\omega_1^2v_2^2\omega_5 - 6\omega_3^2\omega_4\omega_1^2v_2^2\omega_5 + 9c_s^2\omega_4^2\omega_1^3v_2^2\omega_5 - \\
& 3\omega_3\omega_4^2\omega_1^3v_2^2\omega_5 - 9\omega_3^2c_s^2v_3^2\omega_1^3\omega_5 + 3\omega_3^2v_3^2\omega_1^2\omega_5 - 3\omega_3^2\omega_4\omega_1^3v_2^2\omega_5 - 3v_3^2\omega_4^2\omega_1^3\omega_5 + 3\omega_3^2v_3^2\omega_4\omega_1^3\omega_5 + 8\omega_3c_s^2\omega_4^2\omega_1\omega_5 - 6\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_5 - \\
& 2\omega_3c_s^2\omega_4^2\omega_1^3\omega_5 - 8\omega_3^2c_s^4\omega_4^2\omega_1\omega_5 - 6\omega_3v_3^2\omega_4^2\omega_1^2\omega_5 - 12\omega_3^2c_s^2v_3^2\omega_4\omega_1\omega_5
\end{aligned}$$

$$\begin{aligned}
C_{54} = & 144\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 368\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 96\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^2 - 108\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 - 16\omega_3^2\omega_2^2\omega_3^3 + 28\omega_3^2\omega_2^2\omega_1\omega_3^3 + \\
& 56\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 + 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 - 36c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 56\omega_3c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 - 8\omega_3^2\omega_4\omega_1\omega_2^3 - 784\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3 - 104\omega_3^2c_s^2\omega_4^2\omega_1^3 - \\
& 108\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 108c_s^2\omega_4^2\omega_1^2\omega_2^3 + 160\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 132\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 56\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 9\omega_3^2c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 - 78\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 + \\
& 54\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 78\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^3 + 48\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 + 1232\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 + 18\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 + 216\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + 12\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 - \\
& 6\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 - 256\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 + 36\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 54c_s^4\omega_4^2\omega_1^2\omega_2^3 + 9\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 120\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^2 - 56\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2^2 + 120\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + \\
& 36\omega_3^2c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 - 6\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 276\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 342\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 18c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 144\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 + \\
& 32\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^2 - 118\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 412\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 14\omega_3^2\omega_4^2\omega_1^2\omega_2^2 - 9\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + 320\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3 - 56\omega_3^2v_3^2\omega_4^2\omega_1^3 + \\
& 104\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 588\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 208\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 9\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1^2\omega_2 - 88\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 - 168\omega_3c_s^4\omega_4^2\omega_1\omega_2^3 - \\
& 460\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^3 - 6\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 712\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 36c_s^2\omega_4^2\omega_1^2\omega_2^3 + 108\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 152\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 + \\
& 92\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 - 144\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 - 36\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 8\omega_3^2\omega_4^2\omega_1^3 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 - 92\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 72\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 + 6\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + \\
& 16\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_2 + 72\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^2\omega_2^3 - 18\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 - 8\omega_3^2\omega_2^2\omega_1^2\omega_2^3 + 228\omega_3^2v_3^4\omega_4^2\omega_1\omega_2^3 + 52\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 394\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^2 + \\
& 48\omega_3^2v_3^2\omega_4^2\omega_1^3 - 288\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 40\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 18c_s^2\omega_4^2\omega_1^2\omega_2^3 - 136\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2 - 27\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^3 + 6\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^2 + \\
& 6\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 208\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 + 448\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^2\omega_2^3 - 24\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^2 + 184\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^3 - 14\omega_3^2\omega_2^2\omega_1^2\omega_2^3 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2^3
\end{aligned}$$

$$\begin{aligned}
C_{55} = & -18\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^4\omega_4\omega_1\omega_2 + 9\omega_3\omega_1\omega_2 + \\
& 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 18\omega_3\omega_4\omega_1v_1^2 + 2\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{56} = & -264\omega_3v_3^4\omega_4\omega_2^3 - 153\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 + 16\omega_3c_s^4\omega_4\omega_1^3 - 288\omega_3c_s^2v_3^2\omega_4\omega_1^3\omega_2 + 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 24\omega_3v_3^4\omega_4\omega_1\omega_2^2 + 18c_s^2\omega_4\omega_1^3\omega_2^2 + \\
& 42\omega_3c_s^2\omega_4\omega_1^3\omega_2 + 24c_s^2v_3^2\omega_4\omega_1\omega_2^3 + 8c_s^4\omega_4\omega_1\omega_2^3 - 96\omega_3v_3^2\omega_4\omega_1^2\omega_2 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 9c_s^2\omega_4\omega_1^3\omega_2^2 + 408\omega_3v_3^4\omega_4\omega_1\omega_2^3 - 3\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 - \\
& 36\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 108\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2^2 - 90\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2^2 - 8\omega_3\omega_4\omega_2^3 - 81\omega_3v_3^2\omega_4\omega_1^2\omega_2^3 + 144\omega_3c_s^2v_3^2\omega_4\omega_1^2 - 20\omega_3c_s^2\omega_4\omega_1^3 - \\
& 28\omega_3c_s^4\omega_4\omega_1\omega_2^2 + 81\omega_3v_3^2\omega_4\omega_1^2\omega_2^3 + 14\omega_3\omega_4\omega_1\omega_2^3 + 138\omega_3v_3^2\omega_4\omega_1^3\omega_2 - 20c_s^2\omega_4\omega_1^2\omega_2^2 - 16\omega_3c_s^2\omega_4\omega_1^2\omega_2 + \omega_3\omega_4\omega_1^3v_1^4\omega_2^2 + 120\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2 + \\
& \omega_3\omega_4\omega_1^2v_1^2\omega_2^3 + 94\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 4\omega_3\omega_4\omega_1\omega_2^2 + 84\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 36\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 153\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2^2 - 8c_s^2\omega_4\omega_1^3\omega_2 + 18c_s^2\omega_4\omega_1^2\omega_2^3 - \\
& 24\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 - 18c_s^4\omega_4\omega_1^3\omega_2^2 - 4\omega_3\omega_4\omega_1^2\omega_2^2 + 12\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 - 29\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 32\omega_3c_s^4\omega_4\omega_1^3\omega_2 - 36\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 + 27\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + \\
& 4\omega_3\omega_4\omega_1^3 - 9\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 - 8c_s^2\omega_4\omega_1\omega_2^2 - 54c_s^2v_3^2\omega_4\omega_1^3\omega_2^2 + 192\omega_3v_3^4\omega_4\omega_1^2\omega_2 - 68\omega_3c_s^4\omega_4\omega_2^3 + 96\omega_3v_3^4\omega_4\omega_1^3 - 10\omega_3\omega_4\omega_1^3\omega_2 - 222\omega_3v_3^2\omega_4\omega_1\omega_2^3 - \\
& 7\omega_3\omega_4\omega_1^2\omega_2^3 + 9c_s^4\omega_4\omega_1^3\omega_2^3 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 + 27c_s^2v_3^2\omega_4\omega_1^3\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2^2 + 138\omega_3v_3^4\omega_4\omega_1^3\omega_2^2 - 138\omega_3v_3^4\omega_4\omega_1^2\omega_2^2 - \omega_3\omega_4\omega_1^2v_1^4\omega_2^3 + \\
& 32\omega_3c_s^2\omega_4\omega_1\omega_2^2 - 240\omega_3v_3^4\omega_4\omega_1^3\omega_2 + 60c_s^2v_3^2\omega_4\omega_1^2\omega_2^2 - 60\omega_3c_s^2v_3^2\omega_4\omega_1\omega_2^2 - 108\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 + 9\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 - 3\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + \\
& 7\omega_3\omega_4\omega_1^2\omega_2^2 + 20c_s^4\omega_4\omega_2^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1^2\omega_2 - 312\omega_3c_s^2v_3^2\omega_4\omega_2^3 + 40\omega_3c_s^2\omega_4\omega_2^3 + 432\omega_3c_s^2v_3^2\omega_4\omega_1\omega_2^3 - 60\omega_3v_3^2\omega_4\omega_1^3 - 54c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 - \\
& 168\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 24c_s^2v_3^2\omega_4\omega_1^2\omega_2 - 54\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 8\omega_3\omega_4\omega_1^2\omega_2 + 8c_s^4\omega_4\omega_1^3\omega_2 + 17\omega_3c_s^4\omega_4\omega_1^2\omega_2 - 18c_s^2\omega_4\omega_1^2\omega_2^2 - \omega_3\omega_4\omega_1^3v_1^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{57} = & 2\omega_3^2\omega_4\omega_1v_2^2 - 2\omega_3^2\omega_4\omega_1 + 6\omega_3\omega_4^2v_2^2 - 6\omega_3\omega_4^2 - 18\omega_3c_s^2\omega_4\omega_1 - 6\omega_4^2v_2^2 + 36\omega_3c_s^2\omega_4 - 6v_3^2\omega_4^2 - 6\omega_3^2\omega_4v_2^2 + 2\omega_3\omega_4^2\omega_1 - 6\omega_4^2\omega_1 + \\
& 12\omega_3v_3^2\omega_4 - 2\omega_3\omega_4^2\omega_1v_2^2 + 6\omega_3^2v_2^2 + 3v_3^2\omega_4^2\omega_1 + 12\omega_4^2 + 3\omega_3^2v_3^2\omega_1 + 3\omega_2^2\omega_1v_2^2 + 18\omega_3c_s^2\omega_4^2 - 36c_s^2\omega_4^2 - 12\omega_3\omega_4 + 6\omega_3^2c_s^2\omega_4\omega_1 + 6\omega_3^2\omega_4 - \\
& 6\omega_3^2v_3^2 - 6\omega_3v_3^2\omega_4\omega_1 + 18c_s^2\omega_4^2\omega_1 + 6\omega_3\omega_4\omega_1 - 18\omega_3^2c_s^2\omega_4 - 3\omega_3^2\omega_1v_2^2 - 6\omega_3c_s^2\omega_4\omega_1
\end{aligned}$$

$$\begin{aligned}
C_{58} = & -6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 - 18\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^4\omega_4\omega_1\omega_2 + 18\omega_3\omega_4\omega_1v_2^2 + \\
& 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{59} = & -36c_s^2v_3^2\omega_1\omega_2 - 3c_s^4\omega_1\omega_2 + 6v_3^4\omega_1 - 12v_3^2\omega_2 + 24c_s^2v_3^2\omega_1 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 - 9v_3^4\omega_1\omega_2 + 12v_3^4\omega_2 - 6v_3^2\omega_1 + 48c_s^2v_3^2\omega_2 - \\
& 2c_s^2\omega_1 + 4c_s^2\omega_2 + 9v_3^2\omega_1\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{60} = & 24\omega_3^2c_s^4\omega_4^2 + 15\omega_3v_3^2\omega_4^2\omega_1^3 + 18\omega_3^2v_3^2\omega_4^2 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2 + 36\omega_3^2v_3^4\omega_4\omega_1^2 + 18v_3^2\omega_4^2\omega_1^2 - 48\omega_3^2c_s^4\omega_4^2\omega_1 - 36\omega_3v_3^2\omega_4^2\omega_1^2 + 36\omega_3^2c_s^2v_3^2\omega_4\omega_1 + \omega_3^2c_s^2\omega_4^2\omega_1^3 - \\
& 9\omega_3^2v_3^2\omega_4^2\omega_1^3 - 15\omega_3^2v_3^4\omega_4\omega_1^3 - 9v_3^2\omega_4^2\omega_1^3 + 54\omega_3c_s^2v_3^2\omega_4\omega_1^3 - 15\omega_3v_3^4\omega_4^2\omega_1^3 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 - 36\omega_3^2v_3^2\omega_4^2\omega_1^2 - 18v_3^4\omega_4^2\omega_1^2 + 72\omega_3^2c_s^2v_3^2\omega_4\omega_1^2 + 12\omega_3^2c_s^2\omega_4^2\omega_1 +
\end{aligned}$$

$$36\omega_3 v_3^4 \omega_4^2 \omega_1^2 - 108\omega_3 c_s^2 v_3^2 \omega_4 \omega_1^2 - 36\omega_3 c_s^2 v_3^2 \omega_4 \omega_1^3 - 3\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 + 15\omega_3^2 v_3^2 \omega_4 \omega_1^3 + 9v_3^4 \omega_4^2 \omega_1^3 - 12\omega_3^2 c_s^2 \omega_4 \omega_1 + 72\omega_3 c_s^2 v_3^2 \omega_4^2 \omega_1^2 + 12\omega_3 c_s^2 \omega_4^2 \omega_1^2 - 36\omega_3 v_3^4 \omega_4 \omega_1^2 - 54\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 + 6\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^3 - 3\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 + 3\omega_3^2 c_s^4 \omega_4 \omega_1^3 + 9\omega_3^2 v_3^4 \omega_4 \omega_1^3 - 3\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 18\omega_3 v_3^4 \omega_4 \omega_1^3 - 36\omega_3 c_s^2 v_3^2 \omega_4^2 \omega_1^3 + 12\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 - 18\omega_3^2 v_3^4 \omega_4 \omega_1^2 - 12\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 + 27\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^4 \omega_4 \omega_1^2 - 12\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 - 36\omega_3^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 + 36\omega_3 v_3^4 \omega_4 \omega_1^2 + 27c_s^2 v_3^2 \omega_4^2 \omega_1^3 + 3\omega_3^2 v_3^4 \omega_4^2 \omega_1^3 - 3\omega_3^2 c_s^2 \omega_4 \omega_1^3 + 3\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 - 18\omega_3 v_3^4 \omega_4 \omega_1^3 - 12\omega_3^2 v_3^4 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^2 \omega_4 \omega_1^2 + 36\omega_3 c_s^2 v_3^2 \omega_4^2 \omega_1^2 - 54c_s^2 v_3^2 \omega_4^2 \omega_1^2 - 12\omega_3 c_s^2 \omega_4^2 \omega_1^2$$

2.7.4 Conservation of momentum: ρv_2



attached text file: output_d3q27_nse_culbm2_symbolic_pde_02.txt

$$\begin{aligned} & v_2 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_2}{\partial t} + \frac{v_2 v_1 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho v_1 \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_1} + (c_s^2 + v_2^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{2\rho v_2 \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{v_3 v_2 \delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{v_3 \rho \delta_l}{\delta_t} \frac{\partial v_2}{\partial x_3} + \\ & \frac{\rho v_2 \delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1} + (6\omega_1 v_1^2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 6v_1^2 \omega_2 + 2\omega_2 + 6c_s^2 \omega_1) \frac{\delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\ & (\omega_1 - \omega_2) \frac{2\rho v_1 \delta_l^2}{\delta_t \omega_1 \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_2} + (3\omega_1 v_1^2 - c_s^2 \omega_2 - \omega_1 - 3v_1^2 \omega_2 + \omega_2 + c_s^2 \omega_1) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2} + \\ & (6\omega_1 v_2^2 + 8c_s^2 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 3\omega_1 \omega_2 - 4\omega_2 - 9\omega_1 v_2^2 \omega_2 + 4c_s^2 \omega_1 + 12v_2^2 \omega_2) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + \\ & (2\omega_1 - 3\omega_1 \omega_2 + 4\omega_2) \frac{\rho v_2 \delta_l^2}{\delta_t \omega_1 \omega_2} \left(\frac{\partial v_2}{\partial x_2} \right)^2 + (-3v_3^2 \omega_2 - c_s^2 \omega_2 - \omega_1 + 3v_3^2 \omega_1 + \omega_2 + c_s^2 \omega_1) \frac{\delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3} + \\ & (\omega_1 - \omega_2) \frac{2v_3 \rho \delta_l^2}{\delta_t \omega_1 \omega_2} \frac{\partial v_3}{\partial x_2} \frac{\partial v_3}{\partial x_3} + (-6v_3^2 \omega_2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 2\omega_2 + 6c_s^2 \omega_1) \frac{\delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2} + \\ & (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_1} \frac{\partial^2 v_2}{\partial x_1^2} + (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1 \delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_2} + \\ & (6\omega_1 v_1^2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 6v_1^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_1}{\partial x_1 \partial x_2} + \\ & (2\omega_1 v_2^2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 2\omega_1 + 3\omega_1 \omega_2 - 4\omega_2 - 3\omega_1 v_2^2 \omega_2 + 6c_s^2 \omega_1 + 4v_2^2 \omega_2) \frac{v_2 \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_2^2} + \\ & (6\omega_1 v_2^2 + 4c_s^2 \omega_2 - 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 3\omega_1 \omega_2 - 4\omega_2 - 9\omega_1 v_2^2 \omega_2 + 2c_s^2 \omega_1 + 12v_2^2 \omega_2) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_2}{\partial x_2^2} + \\ & (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + \\ & (-6v_3^2 \omega_2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 2\omega_2 + 2c_s^2 \omega_1) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_3}{\partial x_2 \partial x_3} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_1} \frac{\partial^2 v_2}{\partial x_3^2} + \\ & (-1 + 3c_s^2 + v_1^2) \frac{v_2 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{\rho v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{\rho v_1 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_2}{\partial x_1^3} + C_2 \frac{\delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + \\ & C_3 \frac{\rho v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} - \frac{c_s^2 \rho v_2 \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_4 \frac{v_2 v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + C_5 \frac{\rho v_2 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_6 \frac{\rho v_1 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + \\ & C_7 \frac{\delta_l^3}{12\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_2^2} + C_8 \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_2^2} + C_9 \frac{v_3 \rho \delta_l^3}{4\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_3} - \frac{c_s^2 \rho v_2 \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + C_{10} \frac{v_3 v_1 \delta_l^3}{3\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + \\ & C_{11} \frac{v_3 \rho \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_{12} \frac{\rho v_1 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{13} \frac{v_3 v_2 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + C_{14} \frac{v_3 \rho \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} + \\ & C_{15} \frac{\rho v_2 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} - \frac{c_s^2 \rho v_2 \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3} + C_{16} \frac{\rho v_1 \delta_l^3}{4\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_2}{\partial x_1 \partial x_3} + C_{17} \frac{\delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} - \frac{c_s^2 \rho v_2 \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + \\ & C_{18} \frac{v_3 \rho \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + (-1 + 3c_s^2 + v_3^2) \frac{v_3 v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{19} \frac{v_3 \rho \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_2}{\partial x_3^3} + (-1 + c_s^2 + 3v_3^2) \frac{\rho v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\ & C_{20} \frac{v_2 \delta_l^4}{72\delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^4} + (10\omega_1 v_1^2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 20v_1^2 \omega_2 - 15\omega_1 v_1^2 \omega_2 + 6\omega_1 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1) \frac{\rho v_2 v_1 \delta_l^4}{36\delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^4} + \\ & + C_{21} \frac{\rho \delta_l^4}{24\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1^4} + C_{22} \frac{v_1 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{23} \frac{\rho \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{24} \frac{\rho v_2 v_1 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + \\ & C_{25} \frac{v_2 \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + C_{26} \frac{\rho v_2 v_1 \delta_l^4}{18\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{27} \frac{\rho \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{28} \frac{v_1 \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + \\ & C_{29} \frac{\rho \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{30} \frac{\rho v_2 v_1 \delta_l^4}{18\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + C_{31} \frac{v_2 \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{32} \frac{\rho \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + \\ & (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 v_2 v_1 \delta_l^4}{12\delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + \\ & (-v_3^2 \omega_2 - 3c_s^2 \omega_2 - \omega_1 + v_3^2 \omega_1 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \rho v_2 \delta_l^4}{36\delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{33} \frac{v_3 \rho v_1 \delta_l^4}{8\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_3} + C_{34} \frac{\rho v_2 v_1 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\ & C_{35} \frac{v_3 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{36} \frac{v_3 \rho v_1 \delta_l^4}{6\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{37} \frac{v_3 \rho v_2 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + \\ & C_{38} \frac{\rho \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + C_{39} \frac{v_3 v_2 v_1 \delta_l^4}{6\delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{40} \frac{v_3 \rho v_2 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{41} \frac{v_3 \rho v_1 \delta_l^4}{6\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + \\ & + C_{42} \frac{\rho v_2 v_1 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + C_{43} \frac{v_3 \delta_l^4}{36\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3} + C_{44} \frac{v_3 \rho v_2 \delta_l^4}{18\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3} + C_{45} \frac{\rho \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3} + \end{aligned}$$

$$\begin{aligned}
& (-3v_3^2\omega_2 + 3\omega_1v_1^2 - 14c_s^2\omega_2 + 6c_s^2\omega_1\omega_2 - 2\omega_1 - 3v_1^2\omega_2 + 3v_3^2\omega_1 + 2\omega_2 + 2c_s^2\omega_1) \frac{c_s^2v_2\delta_l^4}{36\delta_t\omega_1\omega_2} \frac{\partial^4\rho}{\partial x_1^2\partial x_3^2} + \\
& (\omega_1v_1^2 - 3c_s^2\omega_2 - \omega_1 - v_1^2\omega_2 + \omega_2 + 3c_s^2\omega_1) \frac{\rho v_2v_1\delta_l^4}{36\delta_t\omega_1\omega_2} \frac{\partial^4v_1}{\partial x_1^2\partial x_3^2} + C_{46} \frac{\rho\delta_l^4}{8\omega_3^2\delta_t\omega_4^2\omega_1^3\omega_5} \frac{\partial^4v_2}{\partial x_1^2\partial x_3^2} + \\
& (-v_3^2\omega_2 - 3c_s^2\omega_2 - \omega_1 + v_3^2\omega_1 + \omega_2 + 3c_s^2\omega_1) \frac{v_3\rho v_2\delta_l^4}{36\delta_t\omega_1\omega_2} \frac{\partial^4v_3}{\partial x_1^2\partial x_3^2} + C_{47} \frac{v_1\delta_l^4}{72\omega_3^2\delta_t\omega_4^2\omega_1^3\omega_2^3} \frac{\partial^4\rho}{\partial x_1\partial x_2\partial x_3^2} + \\
& C_{48} \frac{\rho\delta_l^4}{72\omega_3^2\delta_t\omega_4^2\omega_1^3\omega_5\omega_2^3} \frac{\partial^4v_1}{\partial x_1\partial x_2\partial x_3^2} + C_{49} \frac{\rho v_2v_1\delta_l^4}{72\omega_3\delta_t\omega_4\omega_1\omega_2} \frac{\partial^4v_2}{\partial x_1\partial x_2\partial x_3^2} + C_{50} \frac{v_3\rho v_1\delta_l^4}{6\omega_3\delta_t\omega_1^3\omega_2^3} \frac{\partial^4v_3}{\partial x_1\partial x_2\partial x_3^2} + C_{51} \frac{v_2\delta_l^4}{36\omega_3^2\delta_t\omega_4^2\omega_1^3\omega_2^3} \frac{\partial^4\rho}{\partial x_2^2\partial x_3^2} + \\
& + C_{52} \frac{\rho\delta_l^4}{36\omega_3^2\delta_t\omega_4\omega_1^3\omega_2^3} \frac{\partial^4v_2}{\partial x_2^2\partial x_3^2} + C_{53} \frac{v_3\rho v_2\delta_l^4}{18\omega_3\delta_t\omega_1^3\omega_2^3} \frac{\partial^4v_3}{\partial x_2^2\partial x_3^2} + (\omega_1v_1^2 - 3c_s^2\omega_2 - \omega_1 - v_1^2\omega_2 + \omega_2 + 3c_s^2\omega_1) \frac{v_3v_2v_1\delta_l^4}{12\delta_t\omega_1\omega_2} \frac{\partial^4\rho}{\partial x_1\partial x_3^3} + \\
& C_{54} \frac{v_3\rho v_2\delta_l^4}{72\omega_3\delta_t\omega_4\omega_1\omega_2} \frac{\partial^4v_1}{\partial x_1\partial x_3^3} + C_{55} \frac{v_3\rho v_1\delta_l^4}{8\omega_3^2\delta_t\omega_4^2\omega_1} \frac{\partial^4v_2}{\partial x_1\partial x_3^3} + (\omega_1v_1^2 - 3c_s^2\omega_2 - \omega_1 - v_1^2\omega_2 + \omega_2 + 3c_s^2\omega_1) \frac{\rho v_2v_1\delta_l^4}{36\delta_t\omega_1\omega_2} \frac{\partial^4v_3}{\partial x_1\partial x_3^3} + \\
& C_{56} \frac{v_3\delta_l^4}{72\omega_3^2\delta_t\omega_4^2\omega_1^3\omega_2^3} \frac{\partial^4\rho}{\partial x_2\partial x_3^3} + C_{57} \frac{v_3\rho v_2\delta_l^4}{72\omega_3\delta_t\omega_4\omega_1\omega_2} \frac{\partial^4v_2}{\partial x_2\partial x_3^3} + C_{58} \frac{\rho\delta_l^4}{36\omega_3\delta_t\omega_4\omega_1^3\omega_2^3} \frac{\partial^4v_3}{\partial x_2\partial x_3^3} + C_{59} \frac{v_2\delta_l^4}{72\delta_t\omega_1\omega_2} \frac{\partial^4\rho}{\partial x_3^4} + \\
& C_{60} \frac{\rho\delta_l^4}{24\omega_3^2\delta_t\omega_4^2\omega_1^3} \frac{\partial^4v_2}{\partial x_3^4} + \\
& (20v_3^2\omega_2 + 12c_s^2\omega_2 - 9c_s^2\omega_1\omega_2 - 4\omega_1 + 10v_3^2\omega_1 + 6\omega_1\omega_2 - 8\omega_2 + 6c_s^2\omega_1 - 15v_3^2\omega_1\omega_2) \frac{v_3\rho v_2\delta_l^4}{36\delta_t\omega_1\omega_2} \frac{\partial^4v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

$$\begin{aligned}
C_1 &= -18c_s^2\omega_4 + 3\omega_3\omega_1v_1^2 - 6\omega_3c_s^2\omega_4\omega_1 + 18\omega_3c_s^2\omega_4 + 9c_s^2\omega_4\omega_1 + 6\omega_3 - 18\omega_3c_s^2 - 6\omega_3\omega_4 + 6\omega_4 + 3\omega_4\omega_1v_1^2 - 3\omega_3\omega_1 - 6\omega_3v_1^2 - \\
& 2\omega_3\omega_4\omega_1v_1^2 + 6\omega_3\omega_4v_1^2 + 2\omega_3\omega_4\omega_1 - 3\omega_4\omega_1 - 6\omega_4v_1^2 + 9\omega_3c_s^2\omega_1 \\
C_2 &= 12c_s^2\omega_1^2v_1^2 + 2\omega_1v_4^4\omega_2 - 18c_s^2v_1^2\omega_2^2 + 2\omega_1^2v_1^4 + 15c_s^2\omega_1v_1^2\omega_2^2 + 2c_s^2\omega_2^2 + 2c_s^4\omega_1^2 - 2c_s^2\omega_1\omega_2^2 + 6c_s^2\omega_1v_1^2\omega_2 + 3\omega_1^2v_1^2\omega_2 - 4v_1^4\omega_2^2 + 3\omega_1v_1^4\omega_2^2 + \\
& 14c_s^4\omega_1\omega_2^2 - 15c_s^2\omega_1^2v_1^2\omega_2 - 2c_s^2\omega_1^2 - 14c_s^4\omega_2^2 - c_s^4\omega_1^2\omega_2^2 - 2\omega_1v_1^2\omega_2 + 2c_s^2\omega_1^2\omega_2 - 3\omega_1^2v_1^4\omega_2 + 4v_1^2\omega_2^2 - 3\omega_1v_1^2\omega_2^2 - 2c_s^4\omega_1^2\omega_2 - 2\omega_1^2v_1^2 \\
C_3 &= 6\omega_2^2 - 10c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2c_s^2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 11\omega_1^2v_1^2\omega_2 - 4\omega_1^2 + 8c_s^2\omega_1^2 + 6\omega_1v_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 - 2\omega_1\omega_2 - 5\omega_1\omega_2^2 - 14v_1^2\omega_2^2 + 11\omega_1v_1^2\omega_2^2 + 8\omega_1^2v_1^2 \\
C_4 &= 2\omega_2^2 - 6c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 - 6c_s^2\omega_1\omega_2 + 3\omega_1^2\omega_2 - 3\omega_1^2v_1^2\omega_2 - 4\omega_1^2 + 12c_s^2\omega_1^2 + 2v_2^2\omega_2^2 + 2\omega_1v_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 + 2\omega_1\omega_2 - 3\omega_1\omega_2^2 - 4v_1^2\omega_2^2 + \\
& 2\omega_1^2v_2^2 + 3\omega_1v_1^2\omega_2^2 - 4\omega_1v_2^2\omega_2 + 2\omega_1^2v_1^2 \\
C_5 &= -4\omega_4\omega_1^2v_2^2\omega_2 - 36\omega_3c_s^2\omega_1\omega_2^2 - 3\omega_3\omega_4\omega_1^2v_2^2\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2 - 12c_s^2\omega_4\omega_1^2\omega_2 - 11\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 6\omega_3\omega_1^2\omega_2^2 + 8\omega_3\omega_4v_2^2\omega_2^2 - 18\omega_3\omega_4\omega_1^2v_2^2\omega_2 + \\
& 18c_s^2\omega_4\omega_1^2\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 8\omega_4\omega_1\omega_2^2 + 12\omega_3\omega_4\omega_1^2v_1^2 + 6\omega_3\omega_1^2v_2^2\omega_2^2 - 8\omega_3\omega_4\omega_1\omega_2^2 + 16\omega_3c_s^2\omega_4\omega_1^2 + 6\omega_4\omega_1^2v_2^2\omega_2^2 - 2\omega_3\omega_4\omega_1^2v_2^2\omega_2 - \\
& 24\omega_3\omega_4v_1^2\omega_2^2 + 4\omega_3\omega_4\omega_1^2v_2^2 + 18\omega_3\omega_4\omega_1v_1^2\omega_2^2 + 3\omega_3\omega_4\omega_1^2\omega_2^2 - 12\omega_3\omega_1v_2^2\omega_2^2 + 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 24c_s^2\omega_4\omega_1\omega_2^2 - 8\omega_3\omega_4\omega_1^2 - 6\omega_4\omega_1^2\omega_2^2 - \\
& 8\omega_4\omega_1v_2^2\omega_2^2 + 12\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 4\omega_4\omega_1^2\omega_2 + 16\omega_3c_s^2\omega_4\omega_2^2 + 2\omega_3\omega_4\omega_1v_2^2\omega_2^2 + 12\omega_3\omega_1\omega_2^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 + 8\omega_3\omega_4\omega_1^2\omega_2 + 12\omega_3\omega_4\omega_1v_1^2\omega_2 \\
C_6 &= 3\omega_3c_s^2\omega_1\omega_2^2 - 4\omega_3c_s^2\omega_2^2 + 6c_s^2\omega_1\omega_2^2 + \omega_3\omega_1^2\omega_2 - \omega_3\omega_1^2v_1^2\omega_2 + 2\omega_1^2\omega_2 - 2\omega_1^2v_1^2\omega_2 - 4\omega_3c_s^2\omega_1\omega_2 + 6\omega_3v_2^2\omega_2^2 + 8\omega_3c_s^2\omega_1^2 - 3\omega_3c_s^2\omega_1^2\omega_2 + \\
& 4\omega_3\omega_1\omega_2 - 6c_s^2\omega_1^2\omega_2 - 2\omega_3v_1^2\omega_2^2 + 6\omega_3\omega_1^2v_2^2 - 2\omega_1\omega_2^2 - \omega_3\omega_1\omega_2^2 + 2\omega_1v_1^2\omega_2^2 - 12\omega_3\omega_1v_2^2\omega_2 - 4\omega_3\omega_1^2 + \omega_3\omega_1v_1^2\omega_2^2 + 2\omega_3\omega_1^2v_1^2 \\
C_7 &= 4\omega_1^2v_4^2 + 48c_s^2\omega_1v_3^2\omega_2 + 24c_s^2\omega_1^2v_2^2 + 12\omega_1^2v_2^2\omega_2 - 24\omega_1v_4^4\omega_2^2 - 8c_s^2\omega_2^2 + 4c_s^4\omega_1^2 + 16v_4^4\omega_2^2 + 8c_s^2\omega_1\omega_2^2 + 16\omega_1v_4^4\omega_2 - 7\omega_1^2v_2^2\omega_2^2 + \\
& 72c_s^2v_3^2\omega_2^2 - 96c_s^2\omega_1v_2^2\omega_2^2 - 8c_s^4\omega_1\omega_2^2 - 12\omega_1^2v_4^2\omega_2 + 24\omega_1v_2^2\omega_2^2 - 4c_s^2\omega_1^2 + 8c_s^4\omega_2^2 + c_s^4\omega_1^2\omega_2^2 - 16v_2^2\omega_2^2 + 4c_s^2\omega_1^2\omega_2 + 24c_s^2\omega_1^2v_2^2\omega_2^2 - \\
& 48c_s^2\omega_1^2v_2^2\omega_2 - 4\omega_1^2v_2^2 - c_s^2\omega_1^2\omega_2^2 - 16\omega_1v_2^2\omega_2 - 4c_s^4\omega_1^2\omega_2 + 7\omega_1^2v_4^2\omega_2^2 \\
C_8 &= -12\omega_2^2 - 20\omega_1^2v_2^2\omega_2 - 4\omega_1^2\omega_2^2 + 20c_s^2\omega_2^2 - 24c_s^2\omega_1\omega_2^2 + 8c_s^2\omega_1\omega_2 + 11\omega_1^2v_2^2\omega_2^2 + 8\omega_1^2\omega_2 - 4\omega_1^2 - 40\omega_1v_2^2\omega_2^2 + 8c_s^2\omega_1^2 + 28v_2^2\omega_2^2 - \\
& 12c_s^2\omega_1^2\omega_2 - 8\omega_1\omega_2 + 16\omega_1\omega_2^2 + 8\omega_1^2v_2^2 + 5c_s^2\omega_1^2\omega_2^2 + 24\omega_1v_2^2\omega_2 \\
C_9 &= -6c_s^2\omega_4 + 3c_s^2\omega_4\omega_1 - 2\omega_3 + 2\omega_3v_3^2 - 2v_3^2\omega_4 + 6\omega_3c_s^2 + 2\omega_4 + v_3^2\omega_4\omega_1 + \omega_3\omega_1 - \omega_3v_3^2\omega_1 - \omega_4\omega_1 - 3\omega_3c_s^2\omega_1 \\
C_{10} &= -2\omega_2^2 + 6c_s^2\omega_2^2 - 12c_s^2\omega_1\omega_2 + v_3^2\omega_2^2 - 2\omega_1^2 + 6c_s^2\omega_1^2 - 2\omega_1v_1^2\omega_2 + 4\omega_1\omega_2 + v_3^2\omega_1^2 + v_1^2\omega_2^2 - 2v_3^2\omega_1\omega_2 + \omega_1^2v_1^2 \\
C_{11} &= 18\omega_3c_s^2\omega_1\omega_2^2 + 3v_3^2\omega_4\omega_1^2\omega_2^2 + 4\omega_3\omega_4\omega_1\omega_2 - \omega_3v_3^2\omega_4\omega_1^2\omega_2 - 6c_s^2\omega_4\omega_1^2\omega_2 + 3\omega_3\omega_1^2\omega_2^2 - 3\omega_3v_3^2\omega_1^2\omega_2^2 + 9c_s^2\omega_4\omega_1^2\omega_2^2 - 3\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 4\omega_4\omega_1\omega_2^2 + \\
& 6\omega_3\omega_4\omega_1^2v_1^2 - 2v_3^2\omega_4\omega_1^2\omega_2 - \omega_3\omega_4\omega_1\omega_2^2 - 2\omega_3v_3^2\omega_4\omega_2^2 + 8\omega_3c_s^2\omega_4\omega_1^2 + 6\omega_3\omega_4v_1^2\omega_2^2 + \omega_3v_3^2\omega_4\omega_1\omega_2^2 + 6\omega_3v_3^2\omega_1\omega_2^2 - 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 12c_s^2\omega_4\omega_1\omega_2^2 - \\
& 4\omega_3\omega_4\omega_1^2 - 3\omega_4\omega_1^2\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_4\omega_2^2 + 2\omega_3v_3^2\omega_4\omega_1^2 - 6\omega_3\omega_1\omega_2^2 - 9\omega_3c_s^2\omega_1^2\omega_2^2 + \omega_3\omega_4\omega_1^2\omega_2 - 12\omega_3\omega_4\omega_1v_1^2\omega_2 - 4v_3^2\omega_4\omega_1\omega_2^2 \\
C_{12} &= 18\omega_3c_s^2\omega_1\omega_2^2 + 4\omega_3\omega_4\omega_1\omega_2 - 6c_s^2\omega_4\omega_1^2\omega_2 - 3\omega_3\omega_1^2v_1^2\omega_2^2 + 3\omega_3\omega_1^2\omega_2^2 + 3\omega_4\omega_1^2v_1^2\omega_2^2 - \omega_3\omega_4\omega_1^2v_1^2\omega_2 - 2\omega_4\omega_1^2v_1^2\omega_2 + 9c_s^2\omega_4\omega_1^2\omega_2^2 - \\
& 3\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 4\omega_4\omega_1\omega_2^2 + 2\omega_3\omega_4\omega_1^2v_1^2 - \omega_3\omega_4\omega_1\omega_2^2 + 6\omega_3v_3^2\omega_4\omega_2^2 + 8\omega_3c_s^2\omega_4\omega_1^2 - 2\omega_3\omega_4v_1^2\omega_2^2 + \omega_3\omega_4\omega_1v_1^2\omega_2^2 - 4\omega_3c_s^2\omega_4\omega_1\omega_2 - \\
& 12c_s^2\omega_4\omega_1\omega_2^2 - 4\omega_3\omega_4\omega_1^2 - 3\omega_4\omega_1^2\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_4\omega_2^2 + 6\omega_3v_3^2\omega_4\omega_1^2 - 6\omega_3\omega_1\omega_2^2 - 9\omega_3c_s^2\omega_1^2\omega_2^2 + 6\omega_3\omega_1v_1^2\omega_2^2 + \\
& \omega_3\omega_4\omega_1^2\omega_2 - 12\omega_3v_3^2\omega_4\omega_1\omega_2 - 4\omega_4\omega_1v_1^2\omega_2^2 \\
C_{13} &= -3v_3^2\omega_1^2\omega_2 + 2\omega_2^2 - 6c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 - 6c_s^2\omega_1\omega_2 + 3\omega_1^2\omega_2 - 4v_3^2\omega_2^2 - 4\omega_1^2 + 12c_s^2\omega_1^2 + 2v_2^2\omega_2^2 + 3v_3^2\omega_1\omega_2^2 - 9c_s^2\omega_1^2\omega_2 + 2\omega_1\omega_2 + \\
& 2v_3^2\omega_1^2 - 3\omega_1\omega_2^2 + 2\omega_1^2v_2^2 - 4\omega_1v_2^2\omega_2 + 2v_3^2\omega_1\omega_2 \\
C_{14} &= 3\omega_3c_s^2\omega_1\omega_2^2 - 2v_3^2\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_2^2 - \omega_3v_3^2\omega_1^2\omega_2 + 6c_s^2\omega_1\omega_2^2 + \omega_3\omega_1^2\omega_2 + 2\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_1\omega_2 - 2\omega_3v_3^2\omega_2^2 + 6\omega_3v_2^2\omega_2^2 + 8\omega_3c_s^2\omega_1^2 - \\
& 3\omega_3c_s^2\omega_1^2\omega_2 + 2v_3^2\omega_1\omega_2^2 + \omega_3v_3^2\omega_1\omega_2^2 + 4\omega_3\omega_1\omega_2 - 6c_s^2\omega_1^2\omega_2 + 6\omega_3\omega_1^2v_2^2 - 2\omega_1\omega_2^2 - \omega_3\omega_1\omega_2^2 + 2\omega_3v_3^2\omega_1^2 - 12\omega_3\omega_1v_2^2\omega_2 - 4\omega_3\omega_1^2
\end{aligned}$$

$$C_{15} = -4\omega_4\omega_1^2v_2^2\omega_2 - 36\omega_3c_s^2\omega_1\omega_2^2 - 3\omega_3\omega_4\omega_1^2v_2^2\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2 - 18\omega_3v_3^2\omega_4\omega_1^2\omega_2 - 12c_s^2\omega_4\omega_1^2\omega_2 - 11\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 6\omega_3\omega_1^2\omega_2^2 + 8\omega_3\omega_4v_2^2\omega_2^2 + 18c_s^2\omega_4\omega_1^2\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 8\omega_4\omega_1\omega_2^2 + 6\omega_3\omega_1^2v_2^2\omega_2^2 + 6\omega_3\omega_4\omega_1\omega_2^2 - 8\omega_3\omega_4\omega_1\omega_2^2 - 24\omega_3v_3^2\omega_4\omega_2^2 + 16\omega_3c_s^2\omega_4\omega_1^2 + 6\omega_4\omega_1^2v_2^2\omega_2^2 - 2\omega_3\omega_4\omega_1^2v_2^2\omega_2 + 4\omega_3\omega_4\omega_1^2v_2^2 + 3\omega_3\omega_4\omega_1^2\omega_2^2 + 18\omega_3v_3^2\omega_4\omega_1\omega_2^2 - 12\omega_3\omega_1v_2^2\omega_2^2 + 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 24c_s^2\omega_4\omega_1\omega_2^2 - 8\omega_3\omega_4\omega_1^2 - 6\omega_4\omega_1^2\omega_2^2 - 8\omega_4\omega_1v_2^2\omega_2^2 + 12\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 4\omega_4\omega_1^2\omega_2 + 16\omega_3c_s^2\omega_4\omega_2^2 + 12\omega_3v_3^2\omega_4\omega_1^2 + 2\omega_3\omega_4\omega_1v_2^2\omega_2^2 + 12\omega_3\omega_1\omega_2^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 + 8\omega_3\omega_4\omega_1^2\omega_2 + 12\omega_3v_3^2\omega_4\omega_1\omega_2$$

$$C_{16} = -6c_s^2\omega_4 - \omega_3\omega_1v_1^2 + 3c_s^2\omega_4\omega_1 - 2\omega_3 + 6\omega_3c_s^2 + 2\omega_4 + \omega_4\omega_1v_1^2 + \omega_3\omega_1 + 2\omega_3v_1^2 - \omega_4\omega_1 - 2\omega_4v_1^2 - 3\omega_3c_s^2\omega_1$$

$$C_{17} = 6c_s^2v_3^2\omega_1\omega_2 + 3v_3^2\omega_1^2\omega_2 + 12c_s^2v_3^2\omega_1^2 + 2c_s^2\omega_2^2 + 2c_s^4\omega_1^2 - 2c_s^2\omega_1\omega_2^2 - 3v_3^4\omega_2^2\omega_2 + 2v_3^4\omega_1^2 + 4v_3^2\omega_2^2 + 15c_s^2v_3^2\omega_1\omega_2^2 + 14c_s^4\omega_1\omega_2^2 - 18c_s^2v_3^2\omega_2^2 - 2c_s^2\omega_1^2 - 14c_s^4\omega_2^2 - c_s^4\omega_1^2\omega_2^2 - 3v_3^2\omega_1\omega_2^2 + 2v_3^4\omega_1\omega_2 + 2c_s^2\omega_1^2\omega_2 - 4v_3^4\omega_2^2 - 2v_3^2\omega_1^2 + 3v_3^4\omega_1\omega_2^2 - 15c_s^2v_3^2\omega_1^2\omega_2 - 2v_3^2\omega_1\omega_2 - 2c_s^4\omega_1^2\omega_2$$

$$C_{18} = -11v_3^2\omega_1^2\omega_2 + 6\omega_2^2 - 10c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2c_s^2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 14v_3^2\omega_2^2 - 4\omega_1^2 + 8c_s^2\omega_1^2 + 11v_3^2\omega_1\omega_2^2 - 9c_s^2\omega_1^2\omega_2 - 2\omega_1\omega_2 + 8v_3^2\omega_1^2 - 5\omega_1\omega_2^2 + 6v_3^2\omega_1\omega_2$$

$$C_{19} = -18c_s^2\omega_4 - 6\omega_3c_s^2\omega_4\omega_1 + 18\omega_3c_s^2\omega_4 + 9c_s^2\omega_4\omega_1 + 6\omega_3 - 6\omega_3v_3^2 + 6\omega_3v_3^2\omega_4 - 6v_3^2\omega_4 - 18\omega_3c_s^2 - 6\omega_3\omega_4 + 6\omega_4 + 3v_3^2\omega_4\omega_1 - 3\omega_3\omega_1 + 3\omega_3v_3^2\omega_1 - 2\omega_3v_3^2\omega_4\omega_1 + 2\omega_3\omega_4\omega_1 - 3\omega_4\omega_1 + 9\omega_3c_s^2\omega_1$$

$$C_{20} = 12v_1^4\omega_2 - 9\omega_1v_1^4\omega_2 - 3c_s^4\omega_1\omega_2 - 6\omega_1v_1^2 - 36c_s^2\omega_1v_1^2\omega_2 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 48c_s^2v_1^2\omega_2 - 12v_1^2\omega_2 + 9\omega_1v_1^2\omega_2 + 6\omega_1v_1^4 + 24c_s^2\omega_1v_1^2 - 2c_s^2\omega_1 + 4c_s^4\omega_2$$

$$C_{21} = 24\omega_3^2c_s^4\omega_4^2 - 18\omega_3\omega_4\omega_1^3v_1^2 - 12\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2 + 12\omega_3^2\omega_4^2\omega_1^2v_1^2 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2 + 36\omega_3^2\omega_4\omega_1^2v_1^4 + 27c_s^2\omega_4^2\omega_1^3v_1^2 - 15\omega_3\omega_4^2\omega_1^3v_1^4 + 18\omega_3^2\omega_1^2v_1^2 - 48\omega_3^2c_s^4\omega_4\omega_1 + 9\omega_4^2\omega_1^3v_1^4 + 36\omega_3^2c_s^2\omega_4\omega_1v_1^2 + 72\omega_3c_s^2\omega_4^2\omega_1^2v_1^2 + \omega_3^2c_s^2\omega_4^2\omega_1^3 + 36\omega_3\omega_4^2\omega_1^2v_1^4 - 54c_s^2\omega_4^2\omega_1^2v_1^2 - 15\omega_3\omega_4\omega_1^3v_1^4 + 24\omega_3^2c_s^4\omega_4\omega_1^2 - 3\omega_3^2\omega_1^2\omega_1^3v_1^2 + 6\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2 + 36\omega_3\omega_4\omega_1^2v_1^2 + 12\omega_3^2c_s^2\omega_4^2\omega_1 - 36\omega_3c_s^2\omega_4^2\omega_1^3v_1^2 - 18\omega_4\omega_1^2v_1^4 - 9\omega_3^2\omega_1^3v_1^2 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 + 3\omega_3^2\omega_2^2\omega_1^3v_1^4 - 12\omega_3^2c_s^2\omega_4\omega_1 + 12\omega_3c_s^2\omega_2^2\omega_1^2 - 36\omega_3\omega_4\omega_1^2v_1^4 - 36\omega_3^2c_s^2\omega_4\omega_1^3v_1^2 - 36\omega_3\omega_4^2\omega_1^2v_1^2 + 3\omega_3^2c_s^4\omega_4\omega_1^3 + 15\omega_3^2\omega_4\omega_1^3v_1^2 - 3\omega_3c_s^2\omega_4^2\omega_1^3 + 54\omega_3c_s^2\omega_4\omega_1^3v_1^2 - 54\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2 + 9\omega_3^2\omega_1^3v_1^4 + 18\omega_4^2\omega_1^2v_1^2 - 12\omega_3^2c_s^4\omega_4\omega_1^2 + 12\omega_3c_s^2\omega_4\omega_1 + 12\omega_3^2c_s^4\omega_4\omega_1 - 36\omega_3^2\omega_4\omega_1^2v_1^2 - 12\omega_3c_s^4\omega_4\omega_1^2v_1^2 + 15\omega_3\omega_4^2\omega_1^3v_1^2 + 72\omega_3^2c_s^2\omega_4\omega_1^2v_1^2 + 36\omega_3^2c_s^2\omega_4\omega_1^2v_1^2 + 18\omega_3\omega_4\omega_1^3v_1^4 - 12\omega_3^2\omega_4^2\omega_1^2v_1^4 - 3\omega_3^2c_s^2\omega_4\omega_1^3 - 36\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2 + 3\omega_3c_s^4\omega_4\omega_1^3 - 9\omega_4^2\omega_1^3v_1^2 + 12\omega_3^2c_s^2\omega_4\omega_1^2 - 18\omega_3^2\omega_1^2v_1^4 - 108\omega_3c_s^2\omega_4\omega_2^2v_1^2 - 12\omega_3c_s^2\omega_4\omega_1 + 27\omega_3^2c_s^2\omega_1^3v_1^2$$

$$C_{22} = 160\omega_3^2\omega_4^2v_1^2\omega_2^2 + 18\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 256\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 9\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 784\omega_3^2c_s^2\omega_4^2v_1^2\omega_2^3 - 368\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 108\omega_3^2c_s^2\omega_4^2\omega_2^3 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 1232\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 - 6\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 16\omega_3^2\omega_4^2\omega_2^3 + 28\omega_3^2\omega_4^2\omega_1\omega_2^3 + 18\omega_3^2c_s^2\omega_1^3v_1^2\omega_2^3 + 152\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 + 56\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 6\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^3 + 72\omega_3^2c_s^4\omega_4^2\omega_2^2 + 18\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 32\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1\omega_2^2 - 56\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^2 + 120\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 104\omega_3^2c_s^2\omega_4^2\omega_1^3 - 108\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 - 108c_s^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 712\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2 + 56\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 96\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 54\omega_3^2c_s^4\omega_1^3\omega_2^3 + 48\omega_3c_s^4\omega_4^2\omega_1^3\omega_2 + 36\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 + 394\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 216\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 12\omega_3^2c_s^4\omega_4^2\omega_1^3v_1^2\omega_2 - 92\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 - 56\omega_3^2\omega_4^2\omega_1^3v_1^2 + 36\omega_3^2c_s^2\omega_1^3v_1^2\omega_2 - 36c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 320\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2 + 54c_s^4\omega_4^2\omega_1^3\omega_2^3 + 9\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 120\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 6\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^2 - 78\omega_3^2c_s^4\omega_4^2\omega_1^3v_1^2\omega_2^2 - 276\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3 - 56\omega_3c_s^2\omega_4^2\omega_1v_1^2\omega_2^2 - 342\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 118\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 - 132\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 + 48\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 + 6\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 24\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^2 + 448\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2 + 14\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 136\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 36\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 + 588\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 208\omega_3^2c_s^2\omega_4^2\omega_2^2 + 40\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 18\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 144\omega_3^2\omega_4^2\omega_1^3\omega_2^3 + 228\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 88\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 - 168\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 6\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 36c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 72\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 108\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 144\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 6\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 8\omega_3^2\omega_4^2\omega_1^3 - 16\omega_3c_s^2\omega_4^2\omega_1^2\omega_2 - 72\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 + 92\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 460\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2^2 + 52\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 288\omega_3^2c_s^4\omega_4^2\omega_2^3 + 104\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - 18c_s^2\omega_4^2\omega_1^2\omega_2^3 - 27\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 18c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 78\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 208\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 + 184\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 14\omega_3^2\omega_4^2\omega_1^2\omega_2^2 - 412\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 9\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2^2$$

$$C_{23} = 16\omega_3c_s^4\omega_4\omega_1^3 - 60\omega_3\omega_4\omega_1^3v_1^2 - 90\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 + 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 + 18c_s^2\omega_4\omega_1^3\omega_2^2 + 42\omega_3c_s^2\omega_4\omega_1^3\omega_2 + 24c_s^2\omega_4\omega_1v_1^2\omega_2^2 + 408\omega_3\omega_4\omega_1v_1^4\omega_2^3 + 8c_s^4\omega_4\omega_1\omega_2^3 + 27\omega_3c_s^2\omega_1^3v_1^2\omega_2^2 + \omega_3\omega_4\omega_1^3v_2^2\omega_2^2 - 24\omega_3\omega_4\omega_1v_1^4\omega_2^2 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 9c_s^2\omega_4\omega_1^3\omega_2^3 - 153\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 - 36\omega_3c_s^2\omega_1\omega_2^3 + \omega_3\omega_4\omega_1^2v_2^2\omega_2^3 - 240\omega_3\omega_4\omega_1^3v_1^4\omega_2 + 24c_s^2\omega_4\omega_1^3v_1^2\omega_2 - 8\omega_3\omega_4\omega_2^3 - 96\omega_3\omega_4\omega_1^2v_1^2\omega_2 - 20\omega_3c_s^2\omega_4\omega_1^3 - 28\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 14\omega_3\omega_4\omega_1\omega_2^3 + 84\omega_3c_s^2\omega_4^2v_1^2\omega_2^2 - 20c_s^2\omega_4\omega_1^2\omega_2^2 + 144\omega_3\omega_4v_1^2\omega_2^3 - 16\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 + 138\omega_3\omega_4\omega_1^3v_1^4\omega_2^2 - 54c_s^2\omega_4\omega_1^3v_1^2\omega_2^2 + 81\omega_3\omega_4\omega_1^2v_1^2\omega_2^2 - 3\omega_3c_s^2\omega_4\omega_1^2v_2^2\omega_2^3 + 94\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 4\omega_3\omega_4\omega_1\omega_2^3 + 108\omega_3c_s^2\omega_1v_1^2\omega_2^3 + 36\omega_3c_s^4\omega_1v_1^2\omega_2^3 + 27c_s^2\omega_4\omega_1^3v_1^2\omega_2^3 + 120\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2 - 8c_s^2\omega_4\omega_1^2\omega_2^3 + 18c_s^2\omega_4\omega_1^2\omega_2^3 - 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 18c_s^4\omega_4\omega_1^3\omega_2^2 + 12\omega_3\omega_4\omega_1v_1^2\omega_2^2 - 4\omega_3\omega_4\omega_1^2\omega_2^2 - 29\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 32\omega_3c_s^4\omega_4\omega_1\omega_2 - \omega_3\omega_4\omega_1^2v_2^2\omega_2^3 + 138\omega_3\omega_4\omega_1^3v_1^2\omega_2 - 36\omega_3c_s^4\omega_1^2\omega_2^2 + 4\omega_3\omega_4\omega_1^3 - 9\omega_3c_s^2\omega_1^3\omega_2^3 - 8c_s^2\omega_4\omega_1\omega_2^3 + 192\omega_3\omega_4\omega_1^2v_1^2\omega_2 + 144\omega_3c_s^2\omega_4\omega_1^3v_1^2 - 68\omega_3c_s^4\omega_4\omega_2^3 - 108\omega_3c_s^2\omega_1^2v_1^2\omega_2^3 - 10\omega_3\omega_4\omega_1^2\omega_2 - 7\omega_3\omega_4\omega_1^2\omega_2^3 - 222\omega_3\omega_4\omega_1v_1^2\omega_2^3 + 9c_s^4\omega_4\omega_1^3\omega_2^3 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2 - \omega_3\omega_4\omega_1^3v_2^2\omega_2^2 + 153\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2^2 - 288\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2 - 54c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 - 138\omega_3\omega_4\omega_1^2v_1^4\omega_2^3 + 32\omega_3c_s^2\omega_4\omega_1\omega_2^2 - 60\omega_3c_s^2\omega_4\omega_1v_1^2\omega_2^2 + 36\omega_3c_s^2\omega_1^2\omega_2^2 + 9\omega_3c_s^4\omega_1^3\omega_2^3 + 96\omega_3\omega_4\omega_1^3v_1^4 - 3\omega_3c_s^4\omega_4\omega_1^3\omega_2^3 + 7\omega_3\omega_4\omega_1^3\omega_2^2 + 20c_s^4\omega_4\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1^2\omega_2 + 40\omega_3c_s^2\omega_4\omega_2^3 + 432\omega_3c_s^2\omega_4\omega_1v_1^2\omega_2^2 - 54\omega_3c_s^2\omega_4\omega_1\omega_2^3 + 60c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 - 168\omega_3\omega_4\omega_1^2v_1^4\omega_2^2 - 312\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 8\omega_3\omega_4\omega_1^2\omega_2 + 8c_s^4\omega_4\omega_1^2\omega_2 + 17\omega_3c_s^4\omega_4\omega_1^2\omega_2 - 264\omega_3\omega_4v_1^4\omega_2^2 - 18c_s^4\omega_4\omega_1^2\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1^2v_2^2\omega_2^2 - 81\omega_3\omega_4\omega_1^3v_1^2\omega_2^2$$

$$C_{24} = 4\omega_3\omega_4v_2^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 - 18\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 + 18\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 6\omega_3\omega_4\omega_1v_2^2\omega_2$$

$$C_{25} = 24\omega_3^2\omega_4^2v_1^2\omega_2^3 + 8\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^2 + 36\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_2^3 - 42\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 30\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2 + 35\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 216\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 58\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 24c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 - 4\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^3 - 108\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 60\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 + 324\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 + 4\omega_3^2\omega_4^2\omega_2^3 - 4\omega_3^2\omega_4^2\omega_1\omega_2^3 + 66\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 + 28\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 + 15\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 + 3\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^3 + 12\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 - 4\omega_3^2\omega_4^2\omega_1\omega_2^3 - 28\omega_3c_s^2\omega_4^2\omega_1v_2^2\omega_2^3 - 52\omega_3^2c_s^2\omega_4^2\omega_1^3 - 72c_s^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 324\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2 + 28\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 16\omega_3^2c_s^2\omega_4^2v_2^2\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2^2 + 54\omega_3^2c_s^4\omega_1^3\omega_2^3 - 4\omega_3^2\omega_4^2v_2^2\omega_2^3 - 12\omega_3c_s^4\omega_4^2\omega_1^3\omega_2 - 9\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 36c_s^4\omega_4^2\omega_1^3\omega_2^2 + 4\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2 + 108\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 - 27\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 - 48\omega_3^2\omega_4^2\omega_1^3v_1^2 + 4\omega_3^2c_s^2\omega_4^2\omega_1v_2^2\omega_2^2 + 36\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 + 216\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2 + 4\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2 + 54c_s^4\omega_4^2\omega_1^3\omega_2^3 + 9\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 96\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 - 12\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 27\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2^2 + 4\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2 + 18\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 - 4\omega_3^2\omega_4^2\omega_1^3v_2^2 - 20\omega_3^2c_s^2\omega_1^3v_2^2\omega_2 - 102\omega_3^2c_s^4\omega_1^3\omega_2^3 + 16\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2 + 72\omega_3^2c_s^4\omega_1^3\omega_2^3 - 119\omega_3^2c_s^4\omega_1^2\omega_2^3 - 28\omega_3^2c_s^2\omega_4^2\omega_1v_2^2\omega_2^2 - 25\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 + 24\omega_3^2\omega_4^2\omega_1^3v_1^4 - 36\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^2 - 12c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 48\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2 + 12\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 + 78\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 20\omega_3^2c_s^2\omega_2^2\omega_2^3 - 32\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 - 30\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2 - 60\omega_3^2\omega_4^2v_1^4\omega_2^2 + 72\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^2 - 4\omega_3^2\omega_4^2\omega_1^2\omega_2 + 18c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 + 4\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 -$$

$$27\omega_3c_s^2\omega_1\omega_2^3 + 6\omega_2^2\omega_2^2 - 9\omega_3\omega_2^2v_1^2\omega_2^2 - 51\omega_3\omega_1^2\omega_2^2 - 9\omega_1^2v_1^2\omega_2^3 + 6\omega_3\omega_1^2\omega_2 + 6\omega_3\omega_1v_1^2\omega_2 + 132\omega_3\omega_1^2v_2^2\omega_2^2 - 5\omega_3\omega_1^3\omega_2^2 - 12\omega_3\omega_2^3 - 9\omega_1^3\omega_2^2 + 27c_s^2\omega_1^3\omega_2^2 - 66\omega_3\omega_1v_2^2\omega_2^3 + 48\omega_3\omega_1^3v_2^2 - 18\omega_3c_s^2\omega_1^2\omega_2 + 5\omega_3\omega_1^3v_1^2\omega_2^2 - 66\omega_3\omega_1^3v_2^2\omega_2 + 9\omega_1^3v_1^2\omega_2^2 + 84\omega_3c_s^2\omega_1^3 - 120\omega_3\omega_1v_2^2\omega_2^2 + 84\omega_3v_2^2\omega_2^3 + 12\omega_3\omega_1^3v_1^2 + 15\omega_3c_s^2\omega_1^2\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 36\omega_3\omega_1^3 + 27\omega_3\omega_1v_1^2\omega_2^3 - 15\omega_3c_s^2\omega_1^2\omega_2^3 - 6\omega_1^3v_1^2\omega_2 + 42\omega_3\omega_1\omega_2^2 - 18c_s^2\omega_1^2\omega_2^2 + 81\omega_3c_s^2\omega_1^2\omega_2^2 + 6\omega_3\omega_1v_1^2\omega_2^2 - 24\omega_3v_1^2\omega_2^3 - 12\omega_1\omega_2^3 - 18\omega_3\omega_1^3v_1^2\omega_2 - 18c_s^2\omega_1^3\omega_2 + 12\omega_1v_1^2\omega_2^3 - 27c_s^2\omega_1^2\omega_2^3 + 3\omega_3\omega_1\omega_2^3$$

$$C_{31} = -84\omega_3\omega_1^3v_2^4\omega_2 - 80\omega_3c_s^2\omega_1\omega_2^2 - 464\omega_3c_s^2\omega_1^3v_2^2\omega_2 + 72\omega_3c_s^4\omega_1^3 - 184\omega_3c_s^2\omega_2^3 + 168\omega_3\omega_1v_2^2\omega_2^2 + 656\omega_3c_s^2\omega_1v_2^2\omega_2^2 + 144\omega_3v_2^4\omega_2^3 - 8c_s^2\omega_1\omega_2^3 - 104\omega_3\omega_1^3v_2^2\omega_2 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 1472\omega_3c_s^2\omega_1v_2^2\omega_2^3 - 300\omega_3\omega_1v_2^4\omega_2^3 + 320\omega_3c_s^2\omega_1\omega_2^3 - 16\omega_3\omega_1^2\omega_2^3 + 24\omega_3\omega_1^3v_2^4 + 72\omega_3c_s^4\omega_1\omega_2^2 + 160\omega_3c_s^2\omega_1^3v_2^2 + 8\omega_3\omega_1^2\omega_2 - 3\omega_3\omega_1^3\omega_2^3 - 196\omega_3\omega_1^2v_2^2\omega_2^3 + 8c_s^2\omega_1v_2^2\omega_2^3 + 24c_s^4\omega_1\omega_2^3 - 102\omega_3c_s^2\omega_1^3v_2^2\omega_2^3 - 27\omega_3\omega_1^3v_2^4\omega_2^3 + 280\omega_3\omega_1^2v_2^2\omega_2^3 + 8\omega_3\omega_1^3\omega_2^3 - 372\omega_3c_s^4\omega_1\omega_2^3 + 16\omega_3\omega_2^3 + 90\omega_3\omega_1^3v_2^4\omega_2^2 + 8c_s^2\omega_1^3v_2^2\omega_2 + 404\omega_3c_s^2\omega_1^3v_2^2\omega_2^2 + 760\omega_3c_s^2\omega_1^3v_2^2\omega_2^3 + 328\omega_3\omega_1v_2^2\omega_2^3 + 164\omega_3c_s^4\omega_1^2\omega_2^3 - 156\omega_3c_s^4\omega_1^3\omega_2 - 28\omega_3\omega_1^3v_2^2 - 80\omega_3c_s^2\omega_1^2\omega_2 + 18\omega_3c_s^2\omega_1^3\omega_2^3 - 48c_s^4\omega_1^2\omega_2^2 + 94\omega_3\omega_1^3v_2^2\omega_2 + 216\omega_3c_s^2\omega_1^3\omega_2^3 - 52\omega_3c_s^2\omega_1^3 - 120\omega_3c_s^4\omega_1^2\omega_2^3 - 176\omega_3\omega_1v_2^2\omega_2^2 - 160\omega_3v_2^2\omega_2^3 + 440\omega_3c_s^2\omega_1^2v_2^2\omega_2 - 16c_s^2\omega_1^2v_2^2\omega_2^2 + 96\omega_3\omega_1^2v_2^4\omega_2 + 24c_s^4\omega_1^3\omega_2 - 78\omega_3c_s^2\omega_1^3\omega_2^2 - 1088\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 - 264\omega_3\omega_1^3v_2^2\omega_2^2 + 122\omega_3c_s^2\omega_1^3\omega_2 + 4\omega_3\omega_1^3 - 156\omega_3c_s^2\omega_1^2\omega_2^3 - 15\omega_3c_s^4\omega_1^3\omega_2^3 - 98\omega_3\omega_1^3v_2^2\omega_2^2 + 72\omega_3c_s^4\omega_1^2\omega_2 + 8\omega_3\omega_1\omega_2^2 + 16c_s^2\omega_1^2\omega_2^2 + 152\omega_3c_s^2\omega_1^2\omega_2^2 + 180\omega_3\omega_1^2v_2^4\omega_2^3 + 808\omega_3c_s^2\omega_1^2v_2^2\omega_2^3 - 8c_s^2\omega_1^2\omega_2 - 28\omega_3\omega_1\omega_2^2 + 82\omega_3c_s^4\omega_1^3\omega_2^2 + 30\omega_3\omega_1^3v_2^2\omega_2^3$$

$$C_{32} = -312\omega_3\omega_1^3v_2^4\omega_2 - 16\omega_3c_s^2\omega_1\omega_2^2 - 360\omega_3c_s^2\omega_1^3v_2^2\omega_2 + 16\omega_3c_s^4\omega_1^3 - 56\omega_3c_s^2\omega_2^3 + 552\omega_3\omega_1v_2^2\omega_2^2 + 336\omega_3c_s^2\omega_1v_2^2\omega_2^2 + 528\omega_3v_2^4\omega_2^3 - 8c_s^2\omega_1\omega_2^3 - 168\omega_3\omega_1^3v_2^2\omega_2 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 1008\omega_3c_s^2\omega_1v_2^2\omega_2^3 - 1068\omega_3\omega_1v_2^4\omega_2^3 + 96\omega_3c_s^2\omega_1\omega_2^3 - 16\omega_3\omega_1^2\omega_2^3 + 96\omega_3\omega_1^3v_2^4 + 8\omega_3c_s^4\omega_1\omega_2^2 + 144\omega_3c_s^2\omega_1^3v_2^2 + 8\omega_3\omega_1^2\omega_2 - 3\omega_3\omega_1^3\omega_2^3 - 308\omega_3\omega_1^2v_2^2\omega_2^3 + 24c_s^2\omega_1v_2^2\omega_2^3 + 8c_s^4\omega_1\omega_2^3 - 54\omega_3c_s^2\omega_1^3v_2^2\omega_2^3 - 87\omega_3\omega_1^3v_2^4\omega_2^3 + 408\omega_3\omega_1^2v_2^2\omega_2^3 + 8\omega_3\omega_1^3\omega_2^3 - 68\omega_3c_s^4\omega_1\omega_2^3 + 16\omega_3\omega_2^3 + 310\omega_3\omega_1^3v_2^4\omega_2^2 + 24c_s^2\omega_1^3v_2^2\omega_2 + 252\omega_3c_s^2\omega_1^3v_2^2\omega_2^2 + 552\omega_3c_s^2\omega_1^3v_2^2\omega_2^3 + 552\omega_3\omega_1v_2^2\omega_2^3 + 28\omega_3c_s^4\omega_1^2\omega_2^3 - 32\omega_3c_s^4\omega_1^3\omega_2 - 60\omega_3\omega_1^3v_2^2 - 16\omega_3c_s^2\omega_1^2\omega_2 + 6\omega_3c_s^2\omega_1^3\omega_2^3 - 16c_s^4\omega_1^2\omega_2^2 + 174\omega_3\omega_1^3v_2^2\omega_2 + 40\omega_3c_s^4\omega_2^3 - 20\omega_3c_s^2\omega_1^3 - 8\omega_3c_s^4\omega_1^2\omega_2^2 - 240\omega_3\omega_1v_2^2\omega_2^2 - 288\omega_3v_2^2\omega_2^3 + 264\omega_3c_s^2\omega_1^2v_2^2\omega_2 - 48c_s^2\omega_1^2v_2^2\omega_2^2 + 336\omega_3\omega_1^2v_2^4\omega_2 + 8c_s^4\omega_1^3\omega_2 - 22\omega_3c_s^2\omega_1^3\omega_2^2 - 576\omega_3c_s^2\omega_1^2v_2^2\omega_2^2 - 888\omega_3\omega_1^2v_2^2\omega_2^2 + 42\omega_3c_s^2\omega_1^3\omega_2 + 4\omega_3\omega_1^3 - 44\omega_3c_s^2\omega_1^2\omega_2^3 - 3\omega_3c_s^4\omega_1^3\omega_2^3 - 154\omega_3\omega_1^3v_2^2\omega_2^2 + 8\omega_3c_s^4\omega_1^2\omega_2 + 8\omega_3\omega_1\omega_2^2 + 16c_s^2\omega_1^2\omega_2^2 + 24\omega_3c_s^2\omega_1^2\omega_2^2 + 620\omega_3\omega_1^2v_2^4\omega_2^3 + 504\omega_3c_s^2\omega_1^2v_2^2\omega_2^3 - 8c_s^2\omega_1^2\omega_2 - 28\omega_3\omega_1\omega_2^2 + 14\omega_3c_s^4\omega_1^3\omega_2^2 + 42\omega_3\omega_1^3v_2^2\omega_2^3$$

$$C_{33} = -2\omega_3^2\omega_4\omega_1 - 6\omega_3\omega_4^2 - 18\omega_3c_s^2\omega_4\omega_1 + 36\omega_3c_s^2\omega_4 + 2\omega_3^2v_3^2\omega_4\omega_1 - 6v_3^2\omega_4^2 + 2\omega_3\omega_4^2\omega_1 - 6\omega_4^2\omega_1 + 6\omega_3v_3^2\omega_4^2 - 6\omega_4^2v_1^2 + 3\omega_2^2\omega_1v_1^2 - 2\omega_3v_3^2\omega_2\omega_1 + 3v_3^2\omega_2^2\omega_1 + 12\omega_4^2 - 3\omega_3^2v_3^2\omega_1 + 18\omega_3c_s^2\omega_4^2 - 36c_s^2\omega_4^2 - 12\omega_3\omega_4 - 6\omega_3^2v_1^2 + 6\omega_3^2c_s^2\omega_4\omega_1 - 6\omega_3^2v_3^2\omega_4 + 6\omega_3^2\omega_4 + 6\omega_3^2v_3^2 - 6\omega_3\omega_4\omega_1v_1^2 + 18c_s^2\omega_4^2\omega_1 + 3\omega_3^2\omega_1v_1^2 + 12\omega_3\omega_4v_1^2 + 6\omega_3\omega_4\omega_1 - 18\omega_3^2c_s^2\omega_4 - 6\omega_3c_s^2\omega_4^2\omega_1$$

$$C_{34} = 4\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 - 18\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 + 18\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 6\omega_3\omega_4\omega_1v_2^2\omega_2$$

$$C_{35} = -96\omega_3^2\omega_4^2v_1^2\omega_2^3 + 96\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 + 30\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 54\omega_3^2c_s^2\omega_1^3\omega_2^3 - 24\omega_3^2v_3^2\omega_4^2\omega_1^2v_1^2\omega_2 + 432\omega_3^2c_s^2\omega_4^2v_1^2\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 324\omega_3^2c_s^4\omega_4^2\omega_2^3 - 81\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 - 432\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 + 8\omega_3^2\omega_4^2\omega_2^3 + 48\omega_3^2v_3^2\omega_4^2\omega_1^3v_1^2 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 + 96\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 + 56\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 72\omega_3^2c_s^4\omega_4^2\omega_1\omega_2 - 84c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 56\omega_3c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 + 96\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1\omega_2^2 - 432\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 + 32\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3 - 72\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 - 104\omega_3^2c_s^2\omega_4^2\omega_2^3 - 252c_s^4\omega_4^2\omega_1^3\omega_2^3 - 8\omega_3^2v_3^2\omega_4^2\omega_2^3 - 108\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 432\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2 + 128\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 27\omega_3^2c_s^2v_3^2\omega_4\omega_1^3\omega_2^3 + 72\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 - 162\omega_3^2c_s^4\omega_1^3\omega_2^3 - 24\omega_3c_s^4\omega_4^2\omega_2^3\omega_2 + 72\omega_3^2v_3^2\omega_4^2v_1^2\omega_2^3 + 8\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 - 72c_s^4\omega_1^3\omega_2^3 + 324\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + 192\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 96\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 8\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 - 24c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 108\omega_3^2c_s^2\omega_4^2\omega_2^3 + 432\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2 + 162c_s^4\omega_4^2\omega_2^3\omega_2 - 27\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - 56\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2^2 + 192\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 - 108\omega_3^2c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 - 168\omega_3^2c_s^4\omega_4^2\omega_2^3\omega_2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3 + 120\omega_3^2v_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 30\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 54c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 + 8\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 - 10\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2 + 32\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 - 432\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2 + 96\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 - 27\omega_3c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 + 32\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3 - 8\omega_3^2v_3^2\omega_4^2\omega_1^3 - 16\omega_3^2v_3^2\omega_4^2\omega_2^2\omega_2 - 24\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 - 104\omega_3^2c_s^2\omega_4^2\omega_2^3 - 60\omega_3^2v_3^2\omega_4^2\omega_1v_1^2\omega_2^3 + 27\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 54\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 + 24\omega_3^2\omega_4^2v_1^4\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^3 - 8\omega_3^2\omega_4^2v_1^4\omega_2 + 80\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 168\omega_3c_s^4\omega_4^2\omega_1\omega_2^3 - 10\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 - 40\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2 + 84c_s^2\omega_4^2\omega_1^3\omega_2^3 - 96\omega_3^2v_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 324\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 8\omega_3^2v_3^2\omega_4^2\omega_2^3\omega_2 - 216\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 - 60\omega_3^2v_3^2\omega_4^2\omega_1^3v_1^2\omega_2 + 8\omega_3^2\omega_4^2\omega_2^3 + 8\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 - 108\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 24c_s^2\omega_4^2\omega_1^3\omega_2^3 - 8\omega_3c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 + 108\omega_3c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 - 176\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 10\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 + 144\omega_3^2c_s^4\omega_4^2\omega_2^3\omega_2 + 64\omega_3c_s^2v_3^2\omega_4^2\omega_2^3\omega_2 - 192\omega_3^2\omega_4^2v_1^4\omega_2^3 - 64\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 54c_s^2\omega_4^2\omega_1^3\omega_2^3 + 8\omega_3^2v_3^2\omega_4^2\omega_2^2\omega_2 + 81\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 112\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - 8\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2 + 10\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 108\omega_3^2c_s^2v_3^2\omega_1^2\omega_2^3 + 864\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2$$

$$C_{36} = -24\omega_3c_s^2\omega_1\omega_2^2 + 2\omega_1^3\omega_2 + 26\omega_3c_s^2\omega_2^3 - 6c_s^2\omega_1\omega_2^3 + 10\omega_3\omega_1^3\omega_2 - 24\omega_3c_s^2\omega_1\omega_2^3 - 4\omega_1^2\omega_2^2 + 26\omega_3\omega_1^2v_1^2\omega_2^2 - 20\omega_3\omega_1^2\omega_2^2 - 4\omega_3v_3^2\omega_1^2\omega_2 + 14\omega_3\omega_1^2\omega_2 + 6\omega_3v_3^2\omega_1^2\omega_2^2 - 2v_3^2\omega_1^3\omega_2 + 4\omega_3v_3^2\omega_2^3 - 22\omega_3\omega_1^2v_1^2\omega_2 - 3\omega_3v_3^2\omega_1^3\omega_2 - 10\omega_3\omega_2^3 + 4v_3^2\omega_1^2\omega_2^2 - 3\omega_3v_3^2\omega_1\omega_2^3 - 30\omega_3c_s^2\omega_1^2\omega_2 - 4\omega_3v_3^2\omega_1\omega_2^2 + 28\omega_3c_s^2\omega_1^3 - 2v_3^2\omega_1\omega_2^3 + 16\omega_3\omega_1^3v_1^2 - 24\omega_3c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_1^3 - 13\omega_3\omega_1v_1^2\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 12c_s^2\omega_1^2\omega_2^2 + 48\omega_3c_s^2\omega_1^2\omega_2^2 - 4\omega_3\omega_1v_1^2\omega_2^2 + 10\omega_3v_1^2\omega_2^3 + 2\omega_1\omega_2^3 - 13\omega_3\omega_1^3v_1^2\omega_2 - 6c_s^2\omega_1^3\omega_2 + 4\omega_3v_3^2\omega_1^3 + 10\omega_3\omega_1\omega_2^3$$

$$C_{37} = 6\omega_3c_s^2\omega_4\omega_1 - 2\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 - 9\omega_3\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 - 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 + 9\omega_3v_3^2\omega_1\omega_2$$

$$C_{38} = -108\omega_3^2\omega_1^2v_1^2\omega_5\omega_2^3 + 8\omega_3^2c_s^4\omega_4^2\omega_1\omega_5\omega_2^3 + 24\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_5\omega_2 - 88\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + 54\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + 300\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 36\omega_3^2\omega_4\omega_1v_1^2\omega_5\omega_2^3 - 96\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_5 - 72\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - 8\omega_3^2\omega_1^2\omega_5\omega_2^3 - 6\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + 8\omega_3^2\omega_4^2\omega_5\omega_2^3 - 180\omega_3^2v_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 + 180\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 + 264\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_5 + 36\omega_3^2c_s^2\omega_4^2\omega_1\omega_5\omega_2^3 + 72\omega_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^2 + 12\omega_3\omega_4^2\omega_1v_1^4\omega_5\omega_2^3 + 162\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^3 + 72\omega_3c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^3 + 324\omega_3^2c_s^2\omega_1^2v_1^2\omega_5\omega_2^3 - 288\omega_3^2v_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1\omega_5\omega_2^2 + 72\omega_3c_s^2\omega_4^2\omega_1^3\omega_5\omega_2^2 - 28\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_5\omega_2 - 72\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5\omega_2^2 - 36\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^2 - 54\omega_3^2\omega_1^3v_1^4\omega_5\omega_2^2 - 216\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^2 - 24\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^2 - 56\omega_3^2c_s^4\omega_4^2\omega_1\omega_5\omega_2^2 + 72\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^3\omega_5\omega_2 + 9\omega_3^2\omega_4\omega_1^3v_2^2\omega_5\omega_2^3 + 2\omega_3^2\omega_4\omega_1^3v_2^2\omega_5\omega_2^2 - 72\omega_3c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^2 - 180\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^2 + 36\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5\omega_2 - 108\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_5\omega_2^3 + 24\omega_3^2\omega_4^2v_1^2\omega_5\omega_2^3 + 2\omega_3^2\omega_4^2v_1^2v_2^2\omega_5\omega_2^2 - 648\omega_3^2c_s^2v_3^2\omega_4\omega_1\omega_5\omega_2^2 - 108\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 - 48\omega_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1\omega_5\omega_2^2 + 9\omega_3\omega_4^2\omega_1^3v_2^2\omega_5\omega_2^2 - 96\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_5\omega_2 + 48\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2 + 16\omega_3c_s^4\omega_4^2\omega_1^3\omega_5\omega_2 - 54\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 4\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5\omega_2^2 - 288\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^2 - 24\omega_3^2v_3^2\omega_4^2\omega_5\omega_2^3 + 108\omega_3^2\omega_4^2v_1^4\omega_5\omega_2^2 + 6\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2^2 - 162\omega_3^2c_s^2v_3^2\omega_4\omega_1^3\omega_5\omega_2^3 + 36\omega_3^2\omega_4\omega_1v_1^2\omega_5\omega_2^2 + 132\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_5\omega_2^2 + 32\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5 + 24\omega_3^2\omega_4^2\omega_1v_1^4\omega_5\omega_2^2 - 72\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 288\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^2 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_5\omega_2 + 27\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_5\omega_2^2 + 4\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^2 + 240\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 - 12\omega_3\omega_4^2\omega_1v_1^2\omega_5\omega_2^2 - 6\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_5\omega_2^2 + 336\omega_3c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + 160\omega_3c_s^2\omega_4^2\omega_1\omega_5\omega_2^2 + 108\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_5\omega_2^2 - 72\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2 - 72\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 9\omega_3^2\omega_4\omega_1^3v_2^2\omega_5\omega_2^2 + 36\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 + 54\omega_3^2\omega_1^3v_1^2\omega_5\omega_2^3 -$$

$$C_{39} = 6\omega_3^2\omega_2 - 6v_3^2\omega_1^2\omega_2 - 18c_s^2\omega_1^2\omega_2^2 + 6\omega_1^2v_1^2\omega_2^2 - 12\omega_1^2v_2^2\omega_2 - 12\omega_1^2\omega_2^2 + 36c_s^2\omega_1\omega_2^2 + 2v_3^2\omega_3^2 - 3v_3^2\omega_1^2\omega_2 + 24\omega_1^2\omega_2 - 6\omega_1^2v_1^2\omega_2 + 6v_3^2\omega_1^2\omega_2^2 + 4\omega_3^2v_2^2 + 12\omega_1v_2^2\omega_2^2 + 4\omega_1^2v_1^2 - 72c_s^2\omega_1^2\omega_2 - 12\omega_1^3 - 3v_3^2\omega_1\omega_2^2 - 4v_2^2\omega_2^2 + 36c_s^2\omega_1^3 - 12\omega_1\omega_2^2 - 3\omega_1^2v_1^2\omega_2 + 36c_s^2\omega_1^2\omega_2^2 + 6\omega_1\omega_2^2 + 4v_3^2\omega_1^3 - 18c_s^2\omega_1^3\omega_2 - 3\omega_1v_1^2\omega_2^2 + 2v_1^2\omega_2^2$$

$$C_{41} = -3\omega_3^2\omega_1^3v_1^2\omega_2^2 - 3\omega_3\omega_1^2v_1^2\omega_2^3 - 18\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 18\omega_s^2\omega_4\omega_1^3\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^3\omega_2 - 4\omega_3\omega_4\omega_1^2v_1^2\omega_2 - 3\omega_3^2v_3\omega_1\omega_2^3 + 3\omega_4\omega_1^2v_1^2\omega_2^3 + 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 - 12\omega_3^2\omega_4\omega_1^2\omega_2^2 + 3\omega_3v_3^2\omega_1^3\omega_2^2 + 6\omega_3c_s^2\omega_1^3\omega_2^3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^2 + 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 4\omega_3^2v_3\omega_4\omega_1^2\omega_2 + 6\omega_3^2\omega_4\omega_1^3\omega_2 + 6\omega_3^2\omega_1\omega_2^3 + 3\omega_3v_3\omega_4\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2\omega_4\omega_1\omega_2 + 3v_3^2\omega_4\omega_1^2\omega_2^3 - 36\omega_3^2\omega_4\omega_1^2v_1^2\omega_2 - 3v_3^2\omega_4\omega_1^3\omega_2^2 - 3\omega_3v_3^2\omega_4\omega_1^2\omega_2 + \omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 2\omega_3\omega_4\omega_1\omega_2^3 + 6\omega_3^2v_3^2\omega_4\omega_1^2\omega_2^2 + 18\omega_3^2c_s^2\omega_1^2\omega_2^3 - 3\omega_3^2\omega_1v_1^2\omega_2^3 - 12\omega_3^2\omega_4\omega_1^3 - 3\omega_3\omega_4\omega_1^2v_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 + \omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 20\omega_3^2\omega_4\omega_1^2\omega_2 - 6\omega_3\omega_1^3\omega_2^2 - 3\omega_3v_3^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^2\omega_s^2\omega_2^2 + 20\omega_3^2c_s^2\omega_4\omega_2^3 - 3\omega_3^2v_3^2\omega_4\omega_1^2\omega_2 + 18c_s^2\omega_4\omega_1^2\omega_2^2 + 4\omega_3^2v_3^2\omega_1\omega_2^3 + 6\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^2 + 18\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 - 2\omega_3\omega_4\omega_1^2\omega_2^2 - 3\omega_3^2v_3^2\omega_1^3\omega_2^2 - 12\omega_3^2\omega_4\omega_1^2\omega_2^2 - 2\omega_3\omega_4\omega_1^3v_1^2\omega_2 - 3\omega_4\omega_1^3v_1^2\omega_2^2 - 6\omega_4\omega_1^2\omega_3^3 + 3\omega_3\omega_1^3v_1^2\omega_2^2 + 3\omega_3^2\omega_1^2v_1^2\omega_2^2 + 4\omega_3^2\omega_4\omega_1^3v_1^2 - 3\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 - 3\omega_3^2\omega_4\omega_1v_1^2\omega_2^3 + 6\omega_3^2\omega_1^3\omega_2^2 + 4\omega_3\omega_4\omega_1^3\omega_2^2 + \omega_3v_3^2\omega_4\omega_1^2\omega_2^3 + 6\omega_3\omega_4\omega_1^2\omega_2^3 + \omega_3\omega_4\omega_1v_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_1^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 - 4\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + 3\omega_3^2\omega_1^2v_1^2\omega_2^2 + 12\omega_3^2\omega_4\omega_1^3\omega_2^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 - 3\omega_3^2\omega_4\omega_1^3\omega_2 + 4\omega_3\omega_4v_1^2\omega_2^2 - 18\omega_3c_s^2\omega_s^2\omega_2^2 - 6\omega_3^2\omega_1^3\omega_2^2 + 6\omega_3^2\omega_4\omega_1\omega_2^2 - 6\omega_3\omega_4\omega_1^2\omega_2^2 + 3\omega_3^2v_3^2\omega_1^2\omega_2^2 + 4\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 + 28\omega_3^2c_s^2\omega_4\omega_1^3 + 6\omega_4\omega_1^3\omega_2^2 + 6\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 12\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 + 3\omega_3^2v_3^2\omega_1^2\omega_2^2 + 36\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1^3 + 3\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 6\omega_3^2\omega_2^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1\omega_2^2$$

$$C_{43} = 24\omega_3^2 v_3^2 \omega_1^2 v_2^2 \omega_2^2 + 40\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3^2 v_3^2 \omega_1 \omega_2^3 + 108\omega_3^2 c_s^2 \omega_1 v_2^2 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 84\omega_3^2 c_s^4 \omega_1^3 \omega_2 + 8\omega_3^2 \omega_1 \omega_2^3 - 60\omega_3^2 \omega_1 v_2^2 \omega_2^3 - 20\omega_3^2 c_s^2 v_2^2 \omega_2^3 + 22\omega_3^2 c_s^2 v_3^2 \omega_1 \omega_2^3 - 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 + 4\omega_3^2 \omega_1^3 + 8\omega_3^2 c_s^2 v_3^2 \omega_1 \omega_2^3 + 48\omega_3^2 \omega_1 v_2^2 \omega_2^3 + 8\omega_3^2 c_s^2 v_3^2 \omega_1 \omega_2^3 - 324\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2 + 8\omega_3^2 \omega_1 \omega_2^3 + 84\omega_3^2 \omega_1^2 v_2^2 \omega_2 - 4\omega_3^2 v_3^2 \omega_1^3 - 8\omega_3^2 v_3^2 \omega_1 \omega_2^3 + 42\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 216\omega_3^2 c_s^2 \omega_1 v_2^2 \omega_2^2 - 72\omega_3^2 v_3^2 v_2^2 \omega_2^3 + 72\omega_3^2 c_s^2 \omega_1^2 v_2^2 \omega_2^2 - 24\omega_3^2 \omega_1^2 v_2^2 \omega_2^2 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2 + 96\omega_3^2 v_3^2 \omega_1 v_2^2 \omega_2^3 +$$

$$\begin{aligned}
& 56\omega_3^2c_s^2\omega_1^3\omega_2 + 5\omega_3^2c_s^2\omega_1^2\omega_3 - 48\omega_3^2\omega_1^3v_2^2 + 72\omega_3^2\omega_1^2v_2^4\omega_2 + 24\omega_3^2v_2^3\omega_1^3 + 6\omega_3^2c_s^4\omega_1^3\omega_2 - 52\omega_3^2c_s^2\omega_1^3 - 36\omega_3^2c_s^4\omega_1^3\omega_2 + 24\omega_3^2c_s^4\omega_1\omega_3 - 48\omega_3^2v_2^3\omega_1^3v_2^2\omega_2 + \\
& 24\omega_3^2v_2^3\omega_1^3v_2^2 - 34\omega_3^2c_s^2\omega_1^2\omega_2 + 48\omega_3^2v_2^3\omega_1v_2^2\omega_2 - \omega_3^2v_2^3\omega_1^2\omega_2 + 12c_s^2\omega_1^3\omega_2 - 8\omega_3^2\omega_1^3 - 54\omega_3^2c_s^4\omega_1^3\omega_2 + 24\omega_3^2\omega_1^3v_2^4 - 24\omega_3^2\omega_1^3v_2^2\omega_2 + 2\omega_3^2c_s^2v_2^3\omega_1^3\omega_2 - \\
& 4\omega_3^2\omega_1^2\omega_2 - 12\omega_3^2c_s^4\omega_1^3\omega_2 - 72\omega_3^2\omega_1^2v_2^4\omega_2 - 36\omega_3^2\omega_1^2v_2^4\omega_2 + 8\omega_3^2v_2^3\omega_1^3 - 8\omega_3^2c_s^2\omega_1\omega_2 - 24\omega_3^2v_2^3\omega_1^2v_2^2\omega_3 - 4\omega_3^2c_s^2v_2^3\omega_1^2\omega_2 - 12\omega_3^2c_s^4\omega_1^2\omega_2 + \omega_3^2\omega_1^3\omega_2^2 + \\
& 4\omega_3^2v_2^3\omega_1^2\omega_2 + 36c_s^2\omega_1^2\omega_3 - 48\omega_3^2v_2^3\omega_1^2v_2^2\omega_2 - 22\omega_3^2c_s^2\omega_1\omega_3 - 18\omega_3^2c_s^2\omega_1^3\omega_2 + 18\omega_3^2c_s^2v_2^3\omega_1^3\omega_2 + 16\omega_3^2c_s^2v_2^3\omega_1^3 - 36\omega_3^2\omega_1v_2^3\omega_2 + 12c_s^2v_2^3\omega_1^2\omega_3 + \\
& 48\omega_3^2v_2^4\omega_3 + 24\omega_3^2v_2^3\omega_1^2v_2^2\omega_2 - 36c_s^4\omega_1^3\omega_2 - 12c_s^2v_2^3\omega_1^3\omega_2 + 4\omega_3^2c_s^2\omega_1\omega_2 - 18\omega_3^2c_s^2v_2^3\omega_1^2\omega_3 + 20\omega_3^2c_s^2\omega_1^3\omega_2 + 72\omega_3^2c_s^4\omega_1^3 - 4\omega_3^2c_s^2v_2^3\omega_1^3\omega_2 + 18\omega_3^2c_s^2\omega_1^3\omega_3 + \\
& 24\omega_3^2\omega_1^2v_2^2\omega_3 - \omega_3^2\omega_1^2\omega_3 - 4\omega_3^2\omega_1^3\omega_2 - 2\omega_3^2c_s^2v_2^3\omega_1^2\omega_2 + 4\omega_3^2v_2^3\omega_1^2\omega_2 + 216\omega_3^2c_s^2\omega_1^3v_2^2 - 72\omega_3^2c_s^2\omega_1^2v_2^2\omega_3 + 4\omega_3^2c_s^2\omega_1^2\omega_2 - 4\omega_3^2c_s^2v_2^3\omega_1^2\omega_2 + \\
& 216\omega_3^2c_s^2\omega_1^2v_2^2\omega_2 + 4\omega_3^2v_2^3\omega_1^2\omega_2 - 12c_s^2\omega_1^3\omega_2 + 42\omega_3^2c_s^4\omega_1\omega_2 + \omega_3^2v_2^3\omega_1^2\omega_3 - 2\omega_3^2c_s^2v_2^3\omega_1^2\omega_3 + 54\omega_3^2c_s^2\omega_1^3\omega_2 - 4\omega_3^2\omega_1^3\omega_2 - 24\omega_3^2\omega_1^2v_2^2\omega_3 - 20\omega_3^2c_s^2v_2^3\omega_1^3\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{44} = & 9\omega_1^2\omega_3^3 - 54\omega_3^2c_s^2\omega_1\omega_2 + 6\omega_1^3\omega_2 - 12\omega_3^2c_s^2\omega_1^2 + 36c_s^2\omega_1\omega_3 - 12\omega_3\omega_1^2v_2^2\omega_2 + 5\omega_3v_2^3\omega_1^3\omega_2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_3 + 9v_2^3\omega_1^3\omega_2 + \\
& 27\omega_3c_s^2\omega_1\omega_3 + 6\omega_1^2\omega_2 - 51\omega_3\omega_1^2\omega_2 + 6\omega_3v_2^3\omega_1^2\omega_2 + 6\omega_3\omega_1^2\omega_2 - 9\omega_3v_2^3\omega_1^2\omega_2 - 6v_2^3\omega_1^3\omega_2 - 9v_2^3\omega_1^2\omega_3 - 24\omega_3v_2^3\omega_1^2\omega_3 + 132\omega_3\omega_1^2v_2^2\omega_3 - \\
& 18\omega_3v_2^3\omega_1^3\omega_2 - 5\omega_3\omega_1^3\omega_2 - 5\omega_3v_2^3\omega_1^2\omega_2 - 12\omega_3\omega_3^2 - 9\omega_1^3\omega_2^2 - 6v_2^3\omega_1^2\omega_2^2 + 27c_s^2\omega_1^3\omega_2^2 - 66\omega_3\omega_1v_2^2\omega_3^2 + 27\omega_3v_2^3\omega_1\omega_3^2 + 48\omega_3\omega_1^3v_2^2 - \\
& 18\omega_3c_s^2\omega_1^2\omega_2 - 66\omega_3\omega_1^3v_2^2\omega_2 + 6\omega_3v_2^3\omega_1\omega_2 + 84\omega_3c_s^2\omega_1^3 - 120\omega_3\omega_1v_2^2\omega_2 + 84\omega_3v_2^2\omega_3^2 + 12v_2^3\omega_1\omega_3^2 + 15\omega_3c_s^2\omega_1^2\omega_2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 36\omega_3\omega_1^3 - \\
& 15\omega_3c_s^2\omega_1^2\omega_2 + 42\omega_3\omega_1\omega_2^2 - 18c_s^2\omega_1^2\omega_2^2 + 81\omega_3c_s^2\omega_1^2\omega_2^2 - 12\omega_1\omega_3^2 - 18c_s^2\omega_1^3\omega_2 + 12\omega_3v_2^3\omega_1^3 - 27c_s^2\omega_1^2\omega_3^2 + 3\omega_3\omega_1\omega_3^2
\end{aligned}$$

$$\begin{aligned}
C_{45} = & 168\omega_3^2c_s^2\omega_4\omega_3^3v_2^2\omega_2 + 117\omega_3\omega_4\omega_1^3v_2^2\omega_3 + 648\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 432\omega_3^2v_2^3\omega_4v_2^2\omega_3 - 2\omega_3^2c_s^4\omega_1^3\omega_2^2 - 117\omega_3^2\omega_4\omega_3^3v_2^4\omega_3 - 144\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 + \\
& 48\omega_3^2c_s^2\omega_4\omega_1\omega_3^3 - 216c_s^2\omega_1^2\omega_2^2v_2^2\omega_3 + 216\omega_3\omega_2^2\omega_1^3v_2^4\omega_3 - 72\omega_3^2c_s^2\omega_1^3v_2^2\omega_2 - 36\omega_3\omega_4\omega_1^3v_2^4\omega_2 + 18\omega_3c_s^4\omega_4\omega_1^3\omega_3 - 288\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - \\
& 86\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 - 144\omega_3^2v_2^3\omega_1^2v_2^2\omega_3 - 16\omega_3^2\omega_4\omega_3^2 + 16\omega_3^2\omega_1\omega_3^2 + 36\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 - 16\omega_3^2c_s^2\omega_4\omega_1\omega_3^2 + 40\omega_3^2\omega_2^2\omega_1^3v_2^4\omega_2 - 56\omega_3^2c_s^4\omega_4\omega_1^3\omega_2 - \\
& 6\omega_3^2c_s^4\omega_1^3\omega_2^2 - 108\omega_3\omega_4\omega_1^3v_2^2\omega_3 + 72\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 96\omega_3^2c_s^2v_2^3\omega_4\omega_1\omega_3^2 + 180\omega_3\omega_4\omega_1^3v_2^2\omega_3 - 108\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 16\omega_3^2\omega_1^3\omega_2^2 + \\
& 24\omega_3^2c_s^2v_2^3\omega_1^2\omega_3 + 36\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 72\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 288\omega_3^2v_2^3\omega_2^2\omega_1^3v_2^2\omega_2 - 24\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - 40\omega_3^2c_s^2\omega_1^3\omega_2^2 + 144\omega_3^2v_2^3\omega_4\omega_1^3v_2 - \\
& 36\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 + 48\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 + 72\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 60\omega_3\omega_2^2\omega_1^3v_2^4\omega_2 - 32\omega_3^2c_s^2\omega_4\omega_1\omega_3^2 + 108\omega_3\omega_4\omega_1^3v_2^4\omega_2 + 432\omega_3^2c_s^2\omega_4v_2^2\omega_2 + \\
& 144\omega_3^2v_2^3\omega_4\omega_1^3v_2^2\omega_2 - 48\omega_3^2\omega_1^3v_2^2\omega_3 + 16\omega_3^2c_s^4\omega_2^2\omega_1^3\omega_2 - 297\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 12\omega_3^2c_s^2v_2^3\omega_4\omega_1\omega_3^2 + 96\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - 36\omega_3^2c_s^2\omega_1^2\omega_3^2 + \\
& 20\omega_3^2c_s^4\omega_1^3\omega_2^2 - 48\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 - 852\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 + 72\omega_3^2c_s^2\omega_4\omega_1\omega_3^2 + 24\omega_3\omega_4\omega_1^3v_2^2\omega_2 + 36\omega_4\omega_1^3v_2^2\omega_2 - 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_3 + \\
& 288\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 48\omega_3^2c_s^2v_2^3\omega_4\omega_1\omega_3^2 + 40\omega_3^2c_s^4\omega_1^3\omega_2^2 - 540\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 72\omega_4\omega_1^3v_2^4\omega_2 - 54\omega_3^2\omega_1^3v_2^2\omega_3 + 204\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + \\
& 162\omega_3^2c_s^2\omega_1^3v_2^2\omega_3 - 54\omega_4\omega_1^3v_2^2\omega_3 - 108\omega_3^2\omega_1^3v_2^2\omega_3 - 96\omega_3^2\omega_4\omega_1^3v_2^2 - 72\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 - 492\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 28\omega_3^2c_s^4\omega_1^3\omega_2 + 264\omega_3^2c_s^2\omega_4\omega_1^3v_2^2 + \\
& 32\omega_3^2c_s^4\omega_1^3\omega_2^2 + 96\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 86\omega_3^2c_s^4\omega_1^3\omega_2^2 + 336\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 24\omega_3\omega_4\omega_1^3v_2^2\omega_3 - 48\omega_3^2v_2^3\omega_4\omega_1\omega_3^2 + 144\omega_3^2v_2^3\omega_4\omega_1^3v_2^2\omega_2 + \\
& 8\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - 36\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 24\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 - 180\omega_3\omega_4\omega_1^3v_2^2\omega_3 + 108\omega_3\omega_4\omega_1^3v_2^4\omega_2 - 108c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 2\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 + 24\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 - \\
& 36\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 24\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 - 24\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 + 172\omega_3^2c_s^4\omega_1^3\omega_2^2 + 8\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 108\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 108\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 + \\
& 60\omega_3\omega_4\omega_1^3v_2^2\omega_3 + 174\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^2 + 48\omega_3^2\omega_1^3\omega_2^2 - 117\omega_3\omega_4\omega_1^3v_2^4\omega_2 - 8\omega_3^2\omega_1^3\omega_2^2 + 162\omega_3^2\omega_1^3v_2^2\omega_3 + 64\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 + \\
& 16\omega_3^2c_s^4\omega_1^3\omega_2^2 + 12\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 + 240\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 117\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - 12\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 - 297\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 36\omega_3\omega_4\omega_1^3v_2^2\omega_2 - \\
& 72\omega_3^2c_s^4\omega_4\omega_1^3\omega_2 + 24\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 + 36\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 492\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 216\omega_3\omega_4\omega_1^3v_2^2\omega_3 + 6\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 + 16\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 + \\
& 38\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 - 72\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 + 288\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 8\omega_3^2\omega_1^3\omega_2^2 - 16\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 264\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 96\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - 6\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 + \\
& 36\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 + 54\omega_3^2\omega_1^3v_2^4\omega_2 + 72\omega_4\omega_1^3v_2^2\omega_3 + 48\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 - 108\omega_3^2\omega_1^3v_2^4\omega_2 + 72\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 + 108\omega_3^2\omega_1^3v_2^2\omega_3 + 54\omega_4\omega_1^3v_2^4\omega_2 + \\
& 72\omega_3^2\omega_4\omega_1^3v_2^2\omega_3 - 8\omega_3^2\omega_4\omega_1^3\omega_2 + 324\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 108\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 576\omega_3^2v_2^3\omega_4\omega_1^3v_2^2\omega_2 - 12\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 72\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - \\
& 12\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 - 24\omega_3\omega_4\omega_1^3v_2^4\omega_2 + 80\omega_3^2c_s^4\omega_1^3\omega_2^2 - 324\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_3 - 144\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 48\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 + 192\omega_3^2\omega_4\omega_1^3v_2^4\omega_2 - \\
& 40\omega_3^2c_s^4\omega_4\omega_1^3\omega_2 + 24\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 + 18\omega_3^2c_s^4\omega_4\omega_1^3\omega_2 - 288\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 - 36\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 288\omega_3^2v_2^3\omega_4\omega_1^3\omega_2 - 96\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2 - \\
& 36\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 108\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 24\omega_3\omega_4\omega_1^3v_2^2\omega_2 - 2\omega_3^2\omega_4\omega_1^3\omega_2 + 144\omega_3^2v_2^3\omega_4\omega_1^3v_2^2\omega_2 + 468\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 8\omega_3^2\omega_4\omega_1^3\omega_2 - 36\omega_4\omega_1^3v_2^4\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{46} = & 12\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5 + 9c_s^2v_2^3\omega_4\omega_1^3\omega_5 - 6v_2^4\omega_4\omega_1^2\omega_5 + 6\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 - 6\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_5 + 2\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 - 32\omega_3^2c_s^4\omega_4\omega_1 - 3\omega_3v_2^4\omega_4\omega_1^3\omega_5 - \\
& 8\omega_3^2c_s^4\omega_4\omega_1\omega_5 + 6\omega_3^2\omega_4\omega_1^2v_2^2\omega_5 - 18c_s^2\omega_4\omega_1^2v_2^2\omega_5 + 6\omega_3\omega_4\omega_1^2v_2^2\omega_5 + 3\omega_3^2\omega_4\omega_1^3v_1^2\omega_5 - 6\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5 + 3\omega_3\omega_4\omega_1^3v_1^2\omega_5 - 8\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 + \\
& 6\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_5 + 6\omega_3^2\omega_1^3v_1^4\omega_5 - 8\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 - 3\omega_4\omega_1^3v_1^4\omega_5 - 18c_s^2v_2^3\omega_4\omega_1^3\omega_5 + 32\omega_3^2c_s^4\omega_4\omega_1^3 - 9\omega_3^2c_s^2\omega_1^3v_1^2\omega_5 - 8\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 + 3v_2^4\omega_4\omega_1^3\omega_5 - \\
& 3\omega_3^2v_2^3\omega_4\omega_1^3\omega_5 + 3\omega_3^2\omega_1^3v_1^2\omega_5 - 6\omega_4\omega_1^2v_1^4\omega_5 + 12\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5 + 2\omega_3^2c_s^4\omega_1^3v_1^2\omega_5 - 6\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5 + 6\omega_3^2v_2^3\omega_4\omega_1^3\omega_5 - 8\omega_3^2c_s^2\omega_4\omega_1^3 - 6\omega_3^2v_2^3\omega_4\omega_1^3\omega_5 - \\
& 6\omega_3^2\omega_4\omega_1^3v_1^2\omega_5 + 6v_2^4\omega_4\omega_1^2\omega_5 - 6\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 + 18\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_5 - 6\omega_3\omega_4\omega_1^2v_1^4\omega_5 + 6\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5 - 3\omega_3^2\omega_4\omega_1^3v_1^2\omega_5 - 3\omega_3\omega_4\omega_1^3v_1^4\omega_5 + \\
& 9c_s^2\omega_4\omega_1^2\omega_5 - 3\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 - 2\omega_3^2c_s^4\omega_4\omega_1^2\omega_5 + 8\omega_3^2c_s^2\omega_4\omega_1^2\omega_5 + 3\omega_3v_2^3\omega_4\omega_1^2\omega_5 + 16\omega_3^2c_s^4\omega_4\omega_1^2\omega_5 + 8\omega_3^2c_s^2\omega_4\omega_1^2\omega_5 + 6\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_5 + 8\omega_3^2c_s^2\omega_4\omega_1^2\omega_5 + \\
& 6\omega_3^2c_s^2\omega_1^3v_1^2\omega_5 + 6\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 - 9\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_5 - 3\omega_3^2c_s^2\omega_1^3v_1^2\omega_5 - 3\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 + 3\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 + 8\omega_3^2c_s^2\omega_4\omega_1^2\omega_5 - 6\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_5 + 18\omega_3^2c_s^2v_1^2\omega_5 - \\
& 2\omega_3^2c_s^2\omega_1^3\omega_5 + 3\omega_4\omega_1^3v_1^4\omega_5 - 8\omega_3^2c_s^4\omega_4\omega_1\omega_5 - 6\omega_3^2\omega_1^3v_1^2\omega_5 - 6\omega_3^2v_2^3\omega_4\omega_1^2\omega_5 - 12\omega_3^2c_s^2v_2^3\omega_4\omega_1\omega_5 - 12\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_5 + 6\omega_4\omega_1^2v_1^2\omega_5 - 3\omega_3^2\omega_1^3v_1^4\omega_5
\end{aligned}$$

$$\begin{aligned}
C_{47} = & -8\omega_3^2\omega_1^2v_1^2\omega_3^2 + 8\omega_3^2\omega_1^2v_1^2\omega_3^2 - 27\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_3^2 + 30\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 + 54\omega_3^2c_s^2\omega_1^3\omega_2^2 - 24\omega_3^2v_2^3\omega_4\omega_1^3v_1^2\omega_2 + 32\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^2 + \\
& 64\omega_3^2c_s^2\omega_4\omega_1\omega_3^2 + 72\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 + 324\omega_3^2c_s^2\omega_1^2\omega_3^2 - 81\omega_3^2c_s^4\omega_1^2\omega_3^2 + 8\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_3^2 + 8\omega_3^2\omega_4\omega_2^2 + 48\omega_3^2v_2^3\omega_4\omega_1^3v_1^2 - 8\omega_3^2\omega_4\omega_1\omega_3^2 - \\
& 54\omega_3^2c_s^2\omega_1^3v_1^2\omega_3^2 + 8\omega_3^2\omega_1^3v_1^2\omega_2 + 56\omega_3^2c_s^2\omega_4\omega_1\omega_3^2 - 72\omega_3^2c_s^4\omega_1^2\omega_2 + 8\omega_3^2\omega_4\omega_1v_1^2\omega_2 - 8\omega_3^2\omega_4\omega_1\omega_2^2 - 56\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_2 + 432\omega_3^2c_s^2v_2^3\omega_1^2\omega_3^2 - \\
& 104\omega_3^2c_s^2\omega_4\omega_1^3 - 252c_s^4\omega_4\omega_1^3\omega_2^2 - 96\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 - 36\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 + 108\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - 40\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_2 + 128\omega_3^2c_s^2\omega_4\omega_1\omega_2 - 162\omega_3^2c_s^2\omega_1^3\omega_2^2 - \\
& 24\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 + 72\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 - 432\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_2 - 72c_s^4\omega_4\omega_1^2\omega_2 - 108\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2 + 10\omega_3^2c_s^2\omega_1^3v_1^2\omega_2 + 324\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 + \\
& 192\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - 8\omega_3^2\omega_1^3v_1^2\omega_2 + 96\omega_3^2v_2^3\omega_4\omega_1\omega_3^2 - 108\omega_3^2c_s^2\omega_1^2\omega_3^2 - 8\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_2 - 84c_s^2\omega_4\omega_1^2v_1^2\omega_2 + 32\omega_3^2c_s^2\omega_4\omega_1^3v_1^2 + 162c_s^4\omega_4\omega_1^3\omega_2^2 - \\
& 27\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^2 - 72\omega_3^2v_2^4\omega_4\omega_1^2\omega_2 - 432\omega_3^2c_s^2v_2^3\omega_4\omega_1\omega_2 + 192\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 - 168\omega_3^2c_s^4\omega_4\omega_1^3\omega_2 + 144\omega_3^2c_s^4\omega_4\omega_1^3 + 120\omega_3^2v_2^3\omega_4\omega_1^2v_1^2\omega_2 - \\
& 56\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_2 - 30\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 + 24\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 + 96\omega_3^2v_2^3\omega_4\omega_1\omega_2 - 10\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 + 864\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_2 - 8\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2 + \\
& 8\omega_3^2\omega_4\omega_1^2v_1^2\omega_2 + 108\omega_3^2c_s^2\omega_1^2v_1^2\omega_2 + 432\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_2 - 96\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 - 192\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 - 24\omega_3^2c_s^4\omega_4\omega_1\omega_2 - 104\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - \\
& 60\omega_3^2v_2^3\omega_4\omega_1^2v_1^2\omega_2 + 64\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2 + 27\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - 8\omega_3^2\omega_1^3v_1^2\omega_2 + 80\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - 168\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 - 432\omega_3^2c_s^2v_2^3\omega_4\omega_1^2\omega_2 + \\
& 84c_s^2\omega_4\omega_1^2\omega_2 + 108\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2 - 96\omega_3^2v_2^3\omega_4\omega_1^2v_1^2\omega_2 - 324\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 + 96\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 - 216\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 - 60\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 + \\
& 8\omega_3^2\omega_4\omega_2^2 - 24c_s^2\omega_4\omega_2^2v_1^2\omega_2 + 8\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 108\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 + 24c_s^2\omega_4\omega_2^2\omega_2 - 10\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2 + 16\omega_3^2\omega_4\omega_2^2\omega_2 - 36\omega_3^2v_2^3\omega_4\omega_1\omega_2 - \\
& 176\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 + 48\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 + 144\omega_3^2c_s^4\omega_4\omega_2^2 - 16\omega_3^2\omega_4\omega_2^2v_1^2\omega_2 - 64\omega_3^2c_s^2\omega_4\omega_2^2\omega_2 - 54c_s^2\omega_4\omega_2^2\omega_2 + 96\omega_3^2v_2^3\omega_4\omega_1^2\omega_2 + 81\omega_3^2c_s^4\omega_4\omega_2^2\omega_2 + \\
& 54c_s^2\omega_4\omega_2^2v_1^$$

$$6\omega_3v_3^4\omega_4\omega_1^2\omega_2^2 - 6\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 8\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 28\omega_3^2c_s^4\omega_4\omega_1^2\omega_2 + 12\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 32\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 - 9\omega_3^2v_3^4\omega_4\omega_1^2\omega_2^3 - 36\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 72\omega_3^2c_s^4\omega_1\omega_2^3 + 72\omega_3^2v_3^4\omega_4\omega_1^3v_2^2 - 36\omega_3^2v_3^4\omega_4\omega_1^3\omega_2 + 18\omega_3^2v_3^4\omega_1^2\omega_2^3 - 54\omega_3^2c_s^2v_3^4\omega_1^2\omega_2^3 - 90\omega_3c_s^2\omega_4\omega_1^3v_2^2\omega_2^2 + 12\omega_3^2\omega_4\omega_1v_2^3\omega_2^2 + 4\omega_3^2\omega_4\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2^2$$

$$C_{53} = 6\omega_1^3\omega_2 - 66\omega_3c_s^2\omega_2^2 - 18c_s^2\omega_1\omega_2^3 - 12\omega_3\omega_1^2v_2^2\omega_2 + 50\omega_3v_3^2\omega_1^3\omega_2^2 + 48\omega_3\omega_1^3\omega_2 + 23\omega_3\omega_1^2\omega_2^3 + 108\omega_3c_s^2\omega_1\omega_2^2 - 12\omega_1^2\omega_2^2 + 12\omega_3\omega_1^2\omega_2^2 + 6\omega_3v_3^2\omega_2^2 + 6\omega_3\omega_1^2\omega_2 - 66\omega_3v_3^2\omega_1^2\omega_2^2 - 114\omega_3v_3^2\omega_2^3 + 12\omega_1^2v_2^2\omega_2^2 + 18\omega_3\omega_1^2v_2^2\omega_2^2 - 75\omega_3v_3^2\omega_1^3\omega_2 - 23\omega_3\omega_1^3\omega_2^2 - 50\omega_3v_3^2\omega_1^2\omega_2^2 + 42\omega_3\omega_2^3 - 9\omega_3\omega_1v_2^2\omega_2^2 + 141\omega_3v_3^2\omega_1\omega_2^3 + 12\omega_3c_s^2\omega_1^2\omega_2^2 - 18\omega_3c_s^2\omega_1^2\omega_2 - 6\omega_1^3v_2^2\omega_2 - 9\omega_3\omega_1^3v_2^2\omega_2 + 60\omega_3v_3^2\omega_1\omega_2^2 + 84\omega_3c_s^2\omega_1^3 - 12\omega_3\omega_1v_2^2\omega_2^2 + 12\omega_3v_2^2\omega_2^2 + 42\omega_3c_s^2\omega_1^2\omega_2^2 - 6\omega_1v_2^2\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 36\omega_3\omega_1^3 - 42\omega_3c_s^2\omega_1^2\omega_2^2 - 12\omega_3\omega_1\omega_2^2 + 36c_s^2\omega_1^2\omega_2^2 + 6\omega_1\omega_2^3 - 18c_s^2\omega_1^3\omega_2 + 48\omega_3v_3^2\omega_1^3 - 60\omega_3\omega_1\omega_2^3$$

$$C_{54} = -18\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 18\omega_3\omega_4\omega_1v_1^2 + 2\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2$$

$$C_{55} = -2\omega_3^2\omega_4\omega_1 - 6\omega_3\omega_4^2 - 6\omega_3^2\omega_4v_1^2 - 18\omega_3c_s^2\omega_4\omega_1 + 36\omega_3c_s^2\omega_4 + 2\omega_3^2\omega_4\omega_1v_1^2 - 6v_3^2\omega_4^2 + 6\omega_3\omega_1^2v_1^2 + 2\omega_3\omega_4^2\omega_1 - 6\omega_4^2\omega_1 - 6\omega_4^2v_1^2 + 12\omega_3v_3^2\omega_4 + 3\omega_4^2\omega_1v_1^2 + 3v_3^2\omega_4^2\omega_1 + 12\omega_4^2 + 3\omega_3^2v_3^2\omega_1 + 18\omega_3c_s^2\omega_4^2 - 36c_s^2\omega_4^2 - 12\omega_3\omega_4 - 2\omega_3\omega_4^2\omega_1v_1^2 + 6\omega_3^2v_1^2 + 6\omega_3^2c_s^2\omega_4\omega_1 + 6\omega_3^2\omega_4 - 6\omega_3^2v_3^2 - 6\omega_3v_3^2\omega_4\omega_1 + 18c_s^2\omega_4^2\omega_1 - 3\omega_3^2\omega_4^2\omega_1 - 6\omega_3\omega_4\omega_1 - 18\omega_3^2c_s^2\omega_4 - 6\omega_3c_s^2\omega_4^2\omega_1$$

$$C_{56} = 18\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^2 + 144\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 368\omega_3^2c_s^2\omega_1^2\omega_1\omega_2^3 - 96\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^2 - 108\omega_3^2c_s^4\omega_1^2\omega_2^3 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 - 6\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 16\omega_3^2\omega_4^2\omega_2^3 + 28\omega_3^2\omega_4^2\omega_1\omega_2^3 + 56\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 6\omega_3^2\omega_4^2\omega_2^3v_2^2\omega_2^2 + 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 56\omega_3c_s^2v_3^2\omega_1^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 - 784\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3 - 104\omega_3^2c_s^2\omega_4^2\omega_1^3 - 108\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 - 108c_s^4\omega_1^2\omega_1^3\omega_2^2 + 160\omega_3^2v_3^2\omega_2^3\omega_2^2 - 132\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2 - 36\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 56\omega_3^2c_s^2\omega_1^2\omega_1\omega_2^2 - 9\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 78\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^3 + 54\omega_3^2c_s^4\omega_1^3\omega_2^3 + 78\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^2 + 48\omega_3c_s^4\omega_4^2\omega_1^3\omega_2 + 1232\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 + 216\omega_3c_s^4\omega_1^2\omega_1^3\omega_2^2 + 12\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^2 - 256\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 + 36\omega_3^2c_s^2\omega_1^2\omega_2^3 + 54c_s^4\omega_1^2\omega_1^3\omega_2^2 + 9\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 120\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2 - 56\omega_3^2c_s^2v_3^2\omega_1^2\omega_2^2 + 120\omega_3c_s^4\omega_1^2\omega_1^3\omega_2^2 - 276\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3 - 342\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 18c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 144\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^2 + 32\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 - 118\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 6\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 412\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 14\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 9\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + 320\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3 - 56\omega_3^2v_3^2\omega_4^2\omega_1^3 + 104\omega_3^2v_3^2\omega_4^2\omega_2^2 + 588\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 + 208\omega_3^2c_s^2\omega_4^2\omega_2^3 - 18\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 18\omega_3^2c_s^2v_3^2\omega_4^2\omega_2^3 + 16\omega_3^2\omega_4^2\omega_2^2\omega_2^2 - 88\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 - 168\omega_3c_s^4\omega_4^2\omega_1\omega_2^3 - 460\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^3 - 6\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 - 712\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_2 + 36c_s^2\omega_1^2\omega_1^3\omega_2^2 + 108\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 152\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 + 92\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 - 144\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 + 6\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 36\omega_3c_s^2v_3^2\omega_4^2\omega_1^3\omega_2^2 + 8\omega_3^2\omega_2^3\omega_1^3 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 - 92\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 72\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 + 16\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_2 + 72\omega_3c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2^2 + 228\omega_3^2v_3^4\omega_4^2\omega_1\omega_2^2 + 52\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 394\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 48\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 288\omega_3^2c_s^4\omega_4^2\omega_2^3 + 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - 18c_s^2\omega_4^2\omega_1^3\omega_2^3 - 136\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2 - 27\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 6\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2^2 + 208\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 + 448\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_2 - 24\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^2 + 184\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 36\omega_3^2c_s^2v_3^2\omega_1^2\omega_2^2 - 14\omega_3^2\omega_4^2\omega_1^2\omega_2^2 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2$$

$$C_{57} = -6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 - 18\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 + 18\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2$$

$$C_{58} = -264\omega_3v_3^4\omega_4\omega_2^3 - 153\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 + 16\omega_3c_s^4\omega_4\omega_2^3 - 288\omega_3c_s^2v_3^2\omega_4\omega_2^3\omega_2 + 24\omega_3c_s^2\omega_4\omega_2^3\omega_2^2 - 24\omega_3v_3^4\omega_4\omega_1\omega_2^2 + 18c_s^2\omega_4\omega_2^3\omega_2^2 + 42\omega_3c_s^2\omega_4\omega_2^3\omega_2 + 24c_s^2v_3^2\omega_4\omega_1\omega_2^3 + 8c_s^4\omega_4\omega_1\omega_2^3 + \omega_3\omega_4\omega_2^3v_2^2\omega_2^2 - 96\omega_3v_3^4\omega_4\omega_1^2\omega_2 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 9c_s^2\omega_4\omega_1^3\omega_2^2 + 408\omega_3v_3^4\omega_4\omega_1\omega_2^2 - 36\omega_3c_s^2\omega_1\omega_2^3 + \omega_3\omega_4\omega_1^2v_2^2\omega_2^2 + 108\omega_3c_s^2v_3^2\omega_1\omega_2^3 - 90\omega_3c_s^2v_3^2\omega_4\omega_2^2\omega_2^2 - 8\omega_3\omega_4\omega_2^3 - 81\omega_3v_3^2\omega_4\omega_1^3\omega_2^2 + 144\omega_3c_s^2v_3^2\omega_4\omega_1^3 + 144\omega_3v_3^2\omega_4\omega_2^3 - 20\omega_3c_s^2\omega_4\omega_1 - 28\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 81\omega_3v_3^2\omega_4\omega_1\omega_2^3 + 14\omega_3\omega_4\omega_1\omega_2^3 + 138\omega_3v_3^2\omega_4\omega_1^3\omega_2 - 20c_s^2\omega_4\omega_1^2\omega_2^2 - 16\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 120\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2 - 3\omega_3c_s^2\omega_4\omega_1^2v_2^2\omega_2^2 + 94\omega_3c_s^4\omega_4\omega_1\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2^2 + 84\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 36\omega_3c_s^4\omega_1\omega_2^2 + 153\omega_3c_s^2v_3^2\omega_4\omega_1^3\omega_2^2 - 8c_s^2\omega_4\omega_1^3\omega_2 + 18c_s^2\omega_4\omega_1^2\omega_2^2 - 24\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 - 18c_s^4\omega_4\omega_2^3\omega_2^2 - 4\omega_3\omega_4\omega_2^3\omega_2^2 + 12\omega_3v_3^2\omega_4\omega_1\omega_2^2 - 29\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 32\omega_3c_s^4\omega_4\omega_1^3\omega_2 - \omega_3\omega_4\omega_1^2v_2^2\omega_2^2 - 36\omega_3c_s^4\omega_1^2\omega_2^2 + 27\omega_3c_s^2v_3^2\omega_4\omega_1^3\omega_2^2 + 4\omega_3\omega_4\omega_1^3 - 9\omega_3c_s^2\omega_1^3\omega_2^2 - 8c_s^2\omega_4\omega_1\omega_2^2 - 54c_s^2v_3^2\omega_4\omega_1^3\omega_2^2 + 192\omega_3v_3^4\omega_4\omega_1^2\omega_2 - 68\omega_3c_s^4\omega_4\omega_2^3 + 96\omega_3v_3^4\omega_4\omega_1^3 - 10\omega_3\omega_4\omega_2^3\omega_2 - 222\omega_3v_3^4\omega_4\omega_1\omega_2^2 - 7\omega_3\omega_4\omega_1^2\omega_2^2 + 9c_s^4\omega_4\omega_2^3\omega_2^2 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - \omega_3\omega_4\omega_1^3v_2^2\omega_2^2 + 27c_s^2v_3^2\omega_4\omega_1^3\omega_2^2 + 138\omega_3v_3^4\omega_4\omega_2^3\omega_2^2 - 138\omega_3v_3^4\omega_4\omega_1^2\omega_2^2 + 32\omega_3c_s^2\omega_4\omega_1\omega_2^2 - 240\omega_3v_3^4\omega_4\omega_1^3\omega_2 + 60c_s^2v_3^2\omega_4\omega_1^2\omega_2^2 - 60\omega_3c_s^2v_3^2\omega_4\omega_1\omega_2^2 - 108\omega_3c_s^2v_3^2\omega_1^2\omega_2^2 + 36\omega_3c_s^2\omega_1^2\omega_2^2 + 9\omega_3c_s^4\omega_1^3\omega_2^2 - 3\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 7\omega_3\omega_4\omega_1^2\omega_2^2 + 20c_s^4\omega_4\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1\omega_2^2 - 312\omega_3c_s^2v_3^2\omega_4\omega_1\omega_2^2 + 40\omega_3c_s^2v_3^2\omega_4\omega_1\omega_2^2 + 432\omega_3c_s^2v_3^2\omega_4\omega_1\omega_2^2 - 60\omega_3v_3^2\omega_4\omega_2^3 - 54c_s^2v_3^2\omega_4\omega_1^2\omega_2^2 - 168\omega_3v_3^4\omega_4\omega_2^2\omega_2^2 + 24c_s^2v_3^2\omega_4\omega_2^3\omega_2 - 54\omega_3c_s^2\omega_4\omega_1\omega_2^3 + 8\omega_3\omega_4\omega_1^2\omega_2 + 8c_s^4\omega_4\omega_1^2\omega_2 + 17\omega_3c_s^4\omega_4\omega_2^3\omega_2^2 - 18c_s^4\omega_4\omega_2^3\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1^3v_2^2\omega_2^2$$

$$C_{59} = -36c_s^2v_3^2\omega_1\omega_2 - 3c_s^4\omega_1\omega_2 + 6v_3^4\omega_1 - 12v_3^2\omega_2 + 24c_s^2v_3\omega_1 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 - 9v_3^4\omega_1\omega_2 + 12v_3^2\omega_2 - 6v_3^2\omega_1 + 48c_s^2v_3^2\omega_2 - 2c_s^2\omega_1 + 4c_s^4\omega_2 + 9v_3^2\omega_1\omega_2$$

$$C_{60} = 24\omega_3^2c_s^4\omega_4^2 + 15\omega_3v_3^2\omega_4^2\omega_1^3 + 18\omega_3^2v_3^2\omega_1^2 - 8\omega_3^2c_s^2\omega_1^2\omega_2^2 + 36\omega_3^2v_3^4\omega_4\omega_1^2 + 18v_3^2\omega_4^2\omega_1^2 - 48\omega_3^2c_s^4\omega_4^2\omega_1 - 36\omega_3v_3^2\omega_4^2\omega_1^2 + 36\omega_3^2c_s^2v_3^2\omega_4\omega_1 + \omega_3^2c_s^2\omega_4^2\omega_1^3 - 9\omega_3^2v_3^2\omega_1^3 - 15\omega_3^2v_3^4\omega_4\omega_1^3 - 9v_3^2\omega_4^2\omega_1^3 + 54\omega_3c_s^2v_3^2\omega_4\omega_1^3 - 15\omega_3v_3^4\omega_4\omega_1^3 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 - 36\omega_3^2v_3^2\omega_4\omega_1^2 - 18v_3^4\omega_4^2\omega_1^2 + 72\omega_3^2c_s^2v_3^2\omega_4\omega_1^2 + 12\omega_3^2c_s^2\omega_4^2\omega_1 + 36\omega_3v_3^4\omega_4^2\omega_1^2 - 108\omega_3c_s^2v_3^2\omega_4\omega_1^2 - 36\omega_3^2c_s^2v_3^2\omega_4\omega_1^3 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 + 15\omega_3^2v_3^2\omega_4\omega_1^3 + 9v_3^2\omega_4^2\omega_1^3 - 12\omega_3^2c_s^2\omega_4\omega_1 + 72\omega_3c_s^2v_3^2\omega_4^2\omega_1^2 + 12\omega_3c_s^2\omega_4^2\omega_1^2 - 36\omega_3v_3^4\omega_4\omega_1^2 - 54\omega_3^2c_s^2v_3^2\omega_1^2 + 6\omega_3^2c_s^2v_3^2\omega_4\omega_1^2 - 3\omega_3^2v_3^2\omega_4\omega_1^2 + 3\omega_3^2c_s^4\omega_4\omega_1^2 + 9\omega_3^2v_3^4\omega_1^3 - 3\omega_3c_s^2\omega_4^2\omega_1^3 + 18\omega_3v_3^4\omega_4\omega_2^3 - 36\omega_3c_s^2v_3^2\omega_4\omega_1^2 + 12\omega_3^2v_3^2\omega_4\omega_1^2 - 18\omega_3^2c_s^4\omega_4\omega_1^2 - 12\omega_3^2c_s^2v_3^2\omega_4\omega_1^2 + 12\omega_3c_s^4\omega_4\omega_1^2 + 27\omega_3^2c_s^2v_3^2\omega_1^3 + 12\omega_3^2c_s^4\omega_4\omega_1 - 12\omega_3c_s^4\omega_4\omega_1^2 - 36\omega_3^2c_s^2v_3^2\omega_4\omega_1 + 36\omega_3v_3^4\omega_4\omega_1^2 + 27c_s^2v_3^4\omega_4\omega_1^3 + 3\omega_3^2v_3^4\omega_4\omega_1^3 - 3\omega_3^2c_s^2\omega_4\omega_1^3 + 3\omega_3c_s^4\omega_4\omega_1^3 - 18\omega_3v_3^2\omega_4\omega_1^3 - 12\omega_3^2v_3^4\omega_4\omega_1^2 + 12\omega_3^2c_s^2\omega_4\omega_1^2 + 36\omega_3c_s^2v_3^2\omega_4\omega_1 - 54c_s^2v_3^2\omega_4\omega_1^2 - 12\omega_3c_s^2\omega_4\omega_1$$

2.7.5 Conservation of momentum: ρv_3



attached text file: output_d3q27_nse_culbm2_symbolic_pde_03.txt

$$v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + \frac{v_3 v_1 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_1} + \frac{v_3 \rho \delta_t}{\delta_t} \frac{\partial v_1}{\partial x_1} + \frac{\rho v_1 \delta_t}{\delta_t} \frac{\partial v_3}{\partial x_1} + \frac{v_3 v_2 \delta_t}{\delta_t} \frac{\partial \rho}{\partial x_2} + \frac{v_3 \rho \delta_t}{\delta_t} \frac{\partial v_2}{\partial x_2} + \frac{\rho v_2 \delta_t}{\delta_t} \frac{\partial v_3}{\partial x_2} + (c_s^2 + v_3^2) \frac{\delta_t}{\delta_t} \frac{\partial \rho}{\partial x_3} + \frac{2v_3 \rho \delta_t}{\delta_t} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_t^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + (6\omega_1 v_1^2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 6v_1^2 \omega_2 + 2\omega_2 + 6c_s^2 \omega_1) \frac{\delta_t^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3}$$

$$\begin{aligned}
& + (\omega_1 - \omega_2) \frac{2\rho v_1 \delta_l^2}{\delta_t \omega_1 \omega_2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_3}{\partial x_3} + (-2 + \omega_1) \frac{c_s^2 \delta_l^2}{2\delta_t \omega_1} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2} + \\
& (6\omega_1 v_2^2 - 12c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 2\omega_2 + 6c_s^2 \omega_1 - 6v_2^2 \omega_2) \frac{\delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + (\omega_1 - \omega_2) \frac{2\rho v_2 \delta_l^2}{\delta_t \omega_1 \omega_2} \frac{\partial v_2}{\partial x_2} \frac{\partial v_2}{\partial x_3} + \\
& (3\omega_1 v_1^2 - c_s^2 \omega_2 - \omega_1 - 3v_1^2 \omega_2 + \omega_2 + c_s^2 \omega_1) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + (3\omega_1 v_2^2 - c_s^2 \omega_2 - \omega_1 + \omega_2 + c_s^2 \omega_1 - 3v_2^2 \omega_2) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + \\
& (12v_3^2 \omega_2 + 8c_s^2 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 3\omega_1 \omega_2 - 4\omega_2 + 4c_s^2 \omega_1 - 9v_3^2 \omega_1 \omega_2) \frac{\delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + \\
& (2\omega_1 - 3\omega_1 \omega_2 + 4\omega_2) \frac{v_3 \rho \delta_l^2}{\delta_t \omega_1 \omega_2} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_1} \frac{\partial^2 v_3}{\partial x_1^2} + (-2 + \omega_1) \frac{c_s^2 \rho \delta_l^2}{2\delta_t \omega_1} \frac{\partial^2 v_3}{\partial x_2^2} + \\
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1 \delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + \\
& (6\omega_1 v_1^2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 6v_1^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + \\
& (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{v_2 \delta_l^2}{3\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + \\
& (6\omega_1 v_2^2 - 8c_s^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 2\omega_2 + 2c_s^2 \omega_1 - 6v_2^2 \omega_2) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + \\
& (4v_3^2 \omega_2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 2\omega_1 + 2v_3^2 \omega_1 + 3\omega_1 \omega_2 - 4\omega_2 + 6c_s^2 \omega_1 - 3v_3^2 \omega_1 \omega_2) \frac{v_3 \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 \rho}{\partial x_3^2} + \\
& (12v_3^2 \omega_2 + 4c_s^2 \omega_2 - 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 3\omega_1 \omega_2 - 4\omega_2 + 2c_s^2 \omega_1 - 9v_3^2 \omega_1 \omega_2) \frac{\rho \delta_l^2}{6\delta_t \omega_1 \omega_2} \frac{\partial^2 v_3}{\partial x_3^2} + \\
& (-1 + 3c_s^2 + v_1^2) \frac{v_3 v_1 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + (-1 + c_s^2 + 3v_1^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_1 \frac{\rho v_1 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_3}{\partial x_1^3} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + \\
& C_2 \frac{\rho v_2 \delta_l^3}{4\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_3 \frac{\rho v_1 \delta_l^3}{4\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} + (-1 + 3c_s^2 + v_2^2) \frac{v_3 v_2 \delta_l^3}{12\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + \\
& (-1 + c_s^2 + 3v_2^2) \frac{v_3 \rho \delta_l^3}{12\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_4 \frac{\rho v_2 \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1} \frac{\partial^3 v_3}{\partial x_2^3} + C_5 \frac{\delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + C_6 \frac{\rho v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + \\
& C_7 \frac{v_2 v_1 \delta_l^3}{3\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_8 \frac{\rho v_2 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3} + C_9 \frac{\rho v_1 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + C_{10} \frac{\delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_2^2 \partial x_3} + \\
& C_{11} \frac{\rho v_2 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} - \frac{c_s^2 v_3 \rho \delta_l^3}{6\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_{12} \frac{v_3 v_1 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + C_{13} \frac{v_3 \rho \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + C_{14} \frac{\rho v_1 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + \\
& C_{15} \frac{v_3 v_2 \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_2 \partial x_3^2} + C_{16} \frac{v_3 \rho \delta_l^3}{12\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{17} \frac{\rho v_2 \delta_l^3}{6\omega_3 \delta_t \omega_4 \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_2 \partial x_3^2} + C_{18} \frac{\delta_l^3}{12\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 \rho}{\partial x_3^3} + C_{19} \frac{v_3 \rho \delta_l^3}{6\delta_t \omega_1^2 \omega_2^2} \frac{\partial^3 v_3}{\partial x_3^3} + \\
& C_{20} \frac{v_3 \delta_l^4}{72\delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^4} + (10\omega_1 v_1^2 + 12c_s^2 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 20v_1^2 \omega_2 - 15\omega_1 v_1^2 \omega_2 + 6\omega_1 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1) \frac{v_3 \rho v_1 \delta_l^4}{36\delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^4} + \\
& + C_{21} \frac{\rho \delta_l^4}{24\omega_3^2 \delta_t \omega_4^2 \omega_1^3} \frac{\partial^4 v_3}{\partial x_1^4} + (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{v_3 v_2 v_1 \delta_l^4}{12\delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2} + \\
& (\omega_1 v_2^2 - 3c_s^2 \omega_2 - \omega_1 + \omega_2 + 3c_s^2 \omega_1 - v_2^2 \omega_2) \frac{v_3 \rho v_2 \delta_l^4}{36\delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2} + C_{22} \frac{v_3 \rho v_1 \delta_l^4}{72\omega_3 \delta_t \omega_4 \omega_1 \omega_2} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2} + C_{23} \frac{\rho v_2 v_1 \delta_l^4}{8\omega_3^2 \delta_t \omega_4^2 \omega_1} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2} + \\
& (3\omega_1 v_1^2 + 3\omega_1 v_2^2 - 14c_s^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 2\omega_1 - 3v_1^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1 - 3v_2^2 \omega_2) \frac{c_s^2 v_3 \delta_l^4}{36\delta_t \omega_1 \omega_2} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\
& (\omega_1 v_1^2 - 3c_s^2 \omega_2 - \omega_1 - v_1^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 \rho v_1 \delta_l^4}{36\delta_t \omega_1 \omega_2} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + \\
& (\omega_1$$

$$C_{54} \frac{\rho \delta_1^4}{72\omega_3^2 \delta_t \omega_4^2 \omega_1^3 \omega_2^3} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{55} \frac{v_3 \rho v_1 \delta_1^4}{18\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{56} \frac{v_2 \delta_1^4}{36\omega_3^2 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{57} \frac{\rho \delta_1^4}{72\omega_3^2 \delta_t \omega_4^2 \omega_1^3 \omega_2^3} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{58} \frac{v_3 \rho v_2 \delta_1^4}{18\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{59} \frac{v_3 \delta_1^4}{36\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 \rho}{\partial x_3^4} + C_{60} \frac{\rho \delta_1^4}{36\omega_3 \delta_t \omega_1^3 \omega_2^3} \frac{\partial^4 v_3}{\partial x_3^4} = 0,$$

where:

$$C_1 = -18c_s^2\omega_4 + 3\omega_3\omega_1v_1^2 - 6\omega_3c_s^2\omega_4\omega_1 + 18\omega_3c_s^2\omega_4 + 9c_s^2\omega_4\omega_1 + 6\omega_3 - 18\omega_3c_s^2 - 6\omega_3\omega_4 + 6\omega_4 + 3\omega_4\omega_1v_1^2 - 3\omega_3\omega_1 - 6\omega_3v_1^2 - 2\omega_3\omega_4\omega_1v_1^2 + 6\omega_3\omega_4v_1^2 + 2\omega_3\omega_4\omega_1 - 3\omega_4\omega_1 - 6\omega_4v_1^2 + 9\omega_3c_s^2\omega_1$$

$$C_2 = -6c_s^2\omega_4 + 3c_s^2\omega_4\omega_1 - 2\omega_3 - \omega_3\omega_1v_2^2 + 6\omega_3c_s^2 + 2\omega_4 + \omega_3\omega_1 + \omega_4\omega_1v_2^2 + 2\omega_3v_2^2 - \omega_4\omega_1 - 3\omega_3c_s^2\omega_1 - 2\omega_4v_2^2$$

$$C_3 = -6c_s^2\omega_4 - \omega_3\omega_1v_1^2 + 3c_s^2\omega_4\omega_1 - 2\omega_3 + 6\omega_3c_s^2 + 2\omega_4 + \omega_4\omega_1v_1^2 + \omega_3\omega_1 + 2\omega_3v_1^2 - \omega_4\omega_1 - 2\omega_4v_1^2 - 3\omega_3c_s^2\omega_1$$

$$C_4 = -18c_s^2\omega_4 - 6\omega_3c_s^2\omega_4\omega_1 + 18\omega_3c_s^2\omega_4 + 9c_s^2\omega_4\omega_1 + 6\omega_3 + 3\omega_3\omega_1v_2^2 - 18\omega_3c_s^2 - 6\omega_3\omega_4 + 6\omega_4 - 3\omega_3\omega_1 - 2\omega_3\omega_4\omega_1v_2^2 + 3\omega_4\omega_1v_2^2 - 6\omega_3v_2^2 + 2\omega_3\omega_4\omega_1 - 3\omega_4\omega_1 + 6\omega_3\omega_4v_2^2 + 9\omega_3c_s^2\omega_1 - 6\omega_4v_2^2$$

$$C_5 = 12c_s^2\omega_1^2v_1^2 + 2\omega_1v_1^4\omega_2 - 18c_s^2v_1^2\omega_2^2 + 2\omega_1^2v_1^4 + 15c_s^2\omega_1v_1^2\omega_2^2 + 2c_s^2\omega_2^2 + 2c_s^4\omega_1^2 - 2c_s^2\omega_1\omega_2^2 + 6c_s^2\omega_1v_1^2\omega_2 + 3\omega_1^2v_1^2\omega_2 - 4v_1^4\omega_2^2 + 3\omega_1v_1^4\omega_2^2 + 14c_s^4\omega_1\omega_2^2 - 15c_s^2\omega_1^2v_1^2\omega_2 - 2c_s^2\omega_1^2 - 14c_s^4\omega_2^2 - c_s^4\omega_1^2\omega_2^2 - 2\omega_1v_1^2\omega_2 + 2c_s^2\omega_1^2\omega_2 - 3\omega_1^2v_1^4\omega_2 + 4v_1^2\omega_2^2 - 3\omega_1v_1^2\omega_2^2 - 2c_s^4\omega_1^2\omega_2 - 2\omega_1^2v_1^2$$

$$C_6 = 6\omega_2^2 - 10c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2c_s^2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 11\omega_1^2v_1^2\omega_2 - 4\omega_1^2 + 8c_s^2\omega_1^2 + 6\omega_1v_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 - 2\omega_1\omega_2 - 5\omega_1\omega_2^2 - 14v_1^2\omega_2^2 + 11\omega_1v_1^2\omega_2^2 + 8\omega_1^2v_1^2$$

$$C_7 = -2\omega_2^2 + 6c_s^2\omega_2^2 - 12c_s^2\omega_1\omega_2 - 2\omega_1^2 + 6c_s^2\omega_1^2 + v_2^2\omega_2^2 - 2\omega_1v_1^2\omega_2 + 4\omega_1\omega_2 + v_1^2\omega_2^2 + \omega_1^2v_2^2 - 2\omega_1v_2^2\omega_2 + \omega_1^2v_1^2$$

$$C_8 = -2\omega_4\omega_1^2v_2^2\omega_2 + 18\omega_3c_s^2\omega_1\omega_2^2 + 4\omega_3\omega_4\omega_1\omega_2 - 6c_s^2\omega_4\omega_1^2\omega_2 + 3\omega_3\omega_1^2\omega_2^2 - 2\omega_3\omega_4v_2^2\omega_2^2 + 9c_s^2\omega_4\omega_1^2\omega_2^2 - 3\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 4\omega_4\omega_1\omega_2^2 + 6\omega_3\omega_4\omega_1^2v_1^2 - 3\omega_3\omega_1^2v_2^2\omega_2^2 - \omega_3\omega_4\omega_1\omega_2^2 + 8\omega_3c_s^2\omega_4\omega_1^2 + 3\omega_4\omega_1^2v_2^2\omega_2^2 - \omega_3\omega_4\omega_1^2v_2^2\omega_2 + 6\omega_3\omega_4v_1^2\omega_2^2 + 2\omega_3\omega_4\omega_1^2v_2^2 + 6\omega_3\omega_1v_2^2\omega_2^2 - 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 12c_s^2\omega_4\omega_1\omega_2^2 - 4\omega_3\omega_4\omega_1^2 - 3\omega_4\omega_1^2\omega_2^2 - 4\omega_4\omega_1v_2^2\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_4\omega_2^2 + \omega_3\omega_4\omega_1v_2^2\omega_2^2 - 6\omega_3\omega_1\omega_2^2 - 9\omega_3c_s^2\omega_1^2\omega_2^2 + \omega_3\omega_4\omega_1^2\omega_2 - 12\omega_3\omega_4\omega_1v_1^2\omega_2^2$$

$$C_9 = 18\omega_3c_s^2\omega_1\omega_2^2 + 4\omega_3\omega_4\omega_1\omega_2 - 6c_s^2\omega_4\omega_1^2\omega_2 - 3\omega_3\omega_1^2v_1^2\omega_2^2 + 3\omega_3\omega_1^2\omega_2^2 + 6\omega_3\omega_4v_2^2\omega_2^2 + 3\omega_4\omega_1^2v_1^2\omega_2^2 - \omega_3\omega_4\omega_1^2v_1^2\omega_2 - 2\omega_4\omega_1^2v_1^2\omega_2 + 9c_s^2\omega_4\omega_1^2\omega_2^2 - 3\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 4\omega_4\omega_1\omega_2^2 + 2\omega_3\omega_4\omega_1^2v_1^2 - \omega_3\omega_4\omega_1\omega_2^2 + 8\omega_3c_s^2\omega_4\omega_1^2 - 2\omega_3\omega_4v_1^2\omega_2^2 + 6\omega_3\omega_4\omega_1^2v_2^2 + \omega_3\omega_4\omega_1v_1^2\omega_2^2 - 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 12c_s^2\omega_4\omega_1\omega_2^2 - 12\omega_3\omega_4\omega_1v_2^2\omega_2 - 4\omega_3\omega_4\omega_1^2 - 3\omega_4\omega_1^2\omega_2^2 + 3\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 2\omega_4\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_4\omega_2^2 - 6\omega_3\omega_1\omega_2^2 - 9\omega_3c_s^2\omega_1^2\omega_2^2 + 6\omega_3\omega_1v_1^2\omega_2^2 + \omega_3\omega_4\omega_1^2\omega_2 - 4\omega_4\omega_1v_1^2\omega_2^2$$

$$C_{10} = 2\omega_1^2v_2^4 + 6c_s^2\omega_1v_2^2\omega_2 + 12c_s^2\omega_1^2v_2^2 + 3\omega_1^2v_2^2\omega_2 + 3\omega_1v_2^4\omega_2^2 + 2c_s^2\omega_2^2 + 2c_s^4\omega_1^2 - 4v_2^4\omega_2^2 - 2c_s^2\omega_1\omega_2^2 + 2\omega_1v_2^4\omega_2 - 18c_s^2v_2^2\omega_2^2 + 15c_s^2\omega_1v_2^2\omega_2^2 + 14c_s^4\omega_1\omega_2^2 - 3\omega_1^2v_2^4\omega_2 - 3\omega_1v_2^2\omega_2^2 - 2c_s^2\omega_1^2 - 14c_s^4\omega_2^2 - c_s^4\omega_1^2\omega_2^2 + 4v_2^2\omega_2^2 + 2c_s^2\omega_1^2\omega_2 - 15c_s^2\omega_1^2v_2^2\omega_2 - 2\omega_1^2v_2^2 - 2\omega_1v_2^2\omega_2 - 2c_s^4\omega_1^2\omega_2$$

$$C_{11} = 6\omega_2^2 - 11\omega_1^2v_2^2\omega_2 - 10c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2c_s^2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 4\omega_1^2 + 11\omega_1v_2^2\omega_2^2 + 8c_s^2\omega_1^2 - 14v_2^2\omega_2^2 - 9c_s^2\omega_1^2\omega_2 - 2\omega_1\omega_2 - 5\omega_1\omega_2^2 + 8\omega_1^2v_2^2 + 6\omega_1v_2^2\omega_2$$

$$C_{12} = 2\omega_2^2 - 6c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 - 6c_s^2\omega_1\omega_2 + 3\omega_1^2\omega_2 - 3\omega_1^2v_1^2\omega_2 + 2v_3^2\omega_2^2 - 4\omega_1^2 + 12c_s^2\omega_1^2 + 2\omega_1v_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 + 2\omega_1\omega_2 + 2v_3^2\omega_1^2 - 3\omega_1\omega_2^2 - 4v_1^2\omega_2^2 + 3\omega_1v_1^2\omega_2^2 - 4v_3^2\omega_1\omega_2 + 2\omega_1^2v_1^2$$

$$C_{13} = -36\omega_3c_s^2\omega_1\omega_2^2 + 6v_2^2\omega_4\omega_1^2\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2 - 2\omega_3v_3^2\omega_4\omega_1^2\omega_2 - 12c_s^2\omega_4\omega_1^2\omega_2 - 11\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 6\omega_3\omega_2^2\omega_2^2 - 18\omega_3\omega_4\omega_1^2v_1^2\omega_2 + 6\omega_3v_3^2\omega_1^2\omega_2^2 + 18c_s^2\omega_4\omega_1^2\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 8\omega_4\omega_1\omega_2^2 + 12\omega_3\omega_4\omega_1^2v_1^2 - 4v_3^2\omega_4\omega_1^2\omega_2 - 8\omega_3\omega_4\omega_1\omega_2^2 - 3\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 8\omega_3v_3^2\omega_4\omega_2^2 + 16\omega_3c_s^2\omega_4\omega_1 - 24\omega_3\omega_4v_1^2\omega_2^2 + 18\omega_3\omega_4\omega_1v_1^2\omega_2^2 + 3\omega_3\omega_4\omega_1^2\omega_2^2 + 2\omega_3v_3^2\omega_4\omega_1\omega_2^2 - 12\omega_3v_3^2\omega_1\omega_2^2 + 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 24c_s^2\omega_4\omega_1\omega_2^2 - 8\omega_3\omega_4\omega_1^2 - 6\omega_4\omega_1^2\omega_2^2 + 12\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 4\omega_4\omega_1^2\omega_2 + 16\omega_3c_s^2\omega_4\omega_2^2 + 4\omega_3v_3^2\omega_4\omega_1^2 + 12\omega_3\omega_1\omega_2^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 + 8\omega_3\omega_4\omega_1^2\omega_2 + 12\omega_3\omega_4\omega_1v_1^2\omega_2 - 8v_3^2\omega_4\omega_1\omega_2^2$$

$$C_{14} = 3\omega_3c_s^2\omega_1\omega_2^2 - 4\omega_3c_s^2\omega_2^2 + 6c_s^2\omega_1\omega_2^2 + \omega_3\omega_1^2\omega_2 - \omega_3\omega_1^2v_1^2\omega_2 + 2\omega_1^2\omega_2 - 2\omega_1^2v_1^2\omega_2 - 4\omega_3c_s^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_2^2 + 8\omega_3c_s^2\omega_1^2 - 3\omega_3c_s^2\omega_1\omega_2 + 4\omega_3\omega_1\omega_2 - 6c_s^2\omega_1^2\omega_2 - 2\omega_3v_1^2\omega_2^2 - 2\omega_1\omega_2^2 - 12\omega_3v_3^2\omega_1\omega_2 - \omega_3\omega_1\omega_2^2 + 6\omega_3v_3^2\omega_1^2 + 2\omega_1v_1^2\omega_2^2 - 4\omega_3\omega_1^2 + \omega_3\omega_1v_1^2\omega_2^2 + 2\omega_3\omega_1^2v_1^2$$

$$C_{15} = 2\omega_2^2 - 3\omega_1^2v_2^2\omega_2 - 6c_s^2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 - 6c_s^2\omega_1\omega_2 + 3\omega_1^2\omega_2 + 2v_3^2\omega_2^2 - 4\omega_1^2 + 3\omega_1v_2^2\omega_2^2 + 12c_s^2\omega_1^2 - 4v_2^2\omega_2^2 - 9c_s^2\omega_1^2\omega_2 + 2\omega_1\omega_2 + 2v_3^2\omega_1^2 - 3\omega_1\omega_2^2 + 2\omega_1^2v_2^2 + 2\omega_1v_2^2\omega_2 - 4v_3^2\omega_1\omega_2$$

$$C_{16} = -36\omega_3c_s^2\omega_1\omega_2^2 + 6v_2^2\omega_4\omega_1^2\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2 - 2\omega_3v_3^2\omega_4\omega_1^2\omega_2 - 12c_s^2\omega_4\omega_1^2\omega_2 - 11\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 6\omega_3\omega_2^2\omega_2^2 - 24\omega_3\omega_4v_2^2\omega_2^2 + 6\omega_3v_3^2\omega_1^2\omega_2^2 + 18c_s^2\omega_4\omega_1^2\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 8\omega_4\omega_1\omega_2^2 - 4v_3^2\omega_4\omega_1^2\omega_2 - 8\omega_3\omega_4\omega_1\omega_2^2 - 3\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 8\omega_3v_3^2\omega_4\omega_2^2 + 16\omega_3c_s^2\omega_4\omega_1^2 - 18\omega_3\omega_4\omega_1^2v_2^2\omega_2 + 12\omega_3\omega_4\omega_1^2v_2^2 + 3\omega_3\omega_4\omega_1^2\omega_2^2 + 2\omega_3v_3^2\omega_4\omega_1\omega_2^2 - 12\omega_3v_3^2\omega_1\omega_2^2 + 4\omega_3c_s^2\omega_4\omega_1\omega_2 - 24c_s^2\omega_4\omega_1\omega_2^2 + 12\omega_3\omega_4\omega_1v_2^2\omega_2 - 8\omega_3\omega_4\omega_1^2 - 6\omega_4\omega_1^2\omega_2^2 + 12\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 4\omega_4\omega_1^2\omega_2 + 16\omega_3c_s^2\omega_4\omega_2^2 + 4\omega_3v_3^2\omega_4\omega_1^2 + 18\omega_3\omega_4\omega_1v_2^2\omega_2^2 + 12\omega_3\omega_1\omega_2^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 + 8\omega_3\omega_4\omega_1^2\omega_2 + 12\omega_3\omega_4\omega_1v_1^2\omega_2 - 8v_3^2\omega_4\omega_1\omega_2^2$$

$$C_{17} = 3\omega_3c_s^2\omega_1\omega_2^2 - \omega_3\omega_1^2v_2^2\omega_2 - 4\omega_3c_s^2\omega_2^2 - 2\omega_1^2v_2^2\omega_2 + 6c_s^2\omega_1\omega_2^2 + \omega_3\omega_1^2\omega_2 + 2\omega_1^2\omega_2 - 4\omega_3c_s^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_2^2 - 2\omega_3v_2^2\omega_2^2 + 8\omega_3c_s^2\omega_1^2 - 3\omega_3c_s^2\omega_1\omega_2 + 2\omega_1v_2^2\omega_2^2 + 4\omega_3\omega_1\omega_2 + \omega_3\omega_1v_2^2\omega_2^2 - 6c_s^2\omega_1^2\omega_2 + 2\omega_3\omega_1^2v_2^2 - 2\omega_1\omega_2^2 - 12\omega_3v_3^2\omega_1\omega_2 - \omega_3\omega_1\omega_2^2 + 6\omega_3v_3^2\omega_1^2 - 4\omega_3\omega_1^2$$

$$C_{18} = 48c_s^2v_3^2\omega_1\omega_2 + 12v_3^2\omega_1^2\omega_2 + 24c_s^2v_3^2\omega_1^2 - 8c_s^4\omega_2^2 + 4c_s^4\omega_1^2 + 7v_3^4\omega_1^2\omega_2^2 + 8c_s^2\omega_1\omega_2^2 - 12v_3^4\omega_1^2\omega_2 + 4v_3^4\omega_1^2 - 16v_3^2\omega_2^2 - 96c_s^2v_3^2\omega_1\omega_2^2 - 7v_3^2\omega_1^2\omega_2^2 - 8c_s^4\omega_1\omega_2^2 + 72c_s^2v_3^2\omega_2^2 + 24c_s^2v_3^2\omega_1^2\omega_2^2 - 4c_s^2\omega_1^2 + 8c_s^4\omega_2^2 + c_s^4\omega_1^2\omega_2^2 + 24v_3^2\omega_1\omega_2^2 + 16v_3^4\omega_1\omega_2 + 4c_s^2\omega_1^2\omega_2 + 16v_3^4\omega_2^2 - 4v_3^2\omega_1^2 - c_s^2\omega_1^2\omega_2^2 - 24v_3^2\omega_1\omega_2^2 - 48c_s^2v_3^2\omega_1^2\omega_2 - 16v_3^2\omega_1\omega_2 - 4c_s^4\omega_1^2\omega_2$$

$$C_{19} = -20v_3^2\omega_1^2\omega_2 - 12\omega_2^2 - 4\omega_1^2\omega_2^2 + 20c_s^2\omega_2^2 - 24c_s^2\omega_1\omega_2^2 + 8c_s^2\omega_1\omega_2 + 8\omega_1^2\omega_2 + 28v_3^2\omega_2^2 + 11v_3^2\omega_1^2\omega_2^2 - 4\omega_1^2 + 8c_s^2\omega_1^2 - 40v_3^2\omega_1\omega_2^2 - 12c_s^2\omega_1^2\omega_2 - 8\omega_1\omega_2 + 8v_3^2\omega_1^2 + 16\omega_1\omega_2^2 + 5c_s^2\omega_1^2\omega_2^2 + 24v_3^2\omega_1\omega_2$$

$$C_{20} = 12v_1^4\omega_2 - 9\omega_1v_1^4\omega_2 - 3c_s^4\omega_1\omega_2 - 6\omega_1v_1^2 - 36c_s^2\omega_1v_1^2\omega_2 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 48c_s^2v_1^2\omega_2 - 12v_1^2\omega_2 + 9\omega_1v_1^2\omega_2 + 6\omega_1v_1^4 + 24c_s^2\omega_1v_1^2 - 2c_s^2\omega_1 + 4c_s^4\omega_2$$

$$C_{21} = 24\omega_3^2c_s^4\omega_4^2 - 18\omega_3\omega_4\omega_3^3v_1^2 - 12\omega_3^2c_s^2\omega_4^2v_1^2 + 12\omega_3^2\omega_4^2v_1^2 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2 + 36\omega_3^2\omega_4\omega_1^2v_1^4 + 27c_s^2\omega_4^2\omega_1^3v_1^2 - 15\omega_3\omega_4^2\omega_1^3v_1^4 + 18\omega_3^2\omega_1^2v_1^2 - 48\omega_3^2c_s^4\omega_4^2\omega_1 + 9\omega_4^2\omega_1^3v_1^4 + 36\omega_3^2c_s^2\omega_4\omega_1v_1^2 + 72\omega_3c_s^2\omega_4^2\omega_1^2v_1^2 + \omega_3^2c_s^2\omega_4^2\omega_1^3 + 36\omega_3\omega_4^2\omega_1^2v_1^4 - 54c_s^2\omega_4^2\omega_1^2v_1^2 - 15\omega_3^2\omega_4\omega_1^3v_1^4 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 - 3\omega_3^2\omega_1^2\omega_1^3v_1^2 + 6\omega_3^2c_s^2\omega_1^3v_1^2 + 36\omega_3\omega_4\omega_1^2v_1^2 + 12\omega_3^2c_s^2\omega_4^2\omega_1 - 36\omega_3c_s^2\omega_4^2\omega_1^3v_1^2 - 18\omega_4^2\omega_1^2v_1^4 - 9\omega_3^2\omega_1^3v_1^2 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 + 3\omega_3^2\omega_4^2\omega_1^3v_1^4 - 12\omega_3^2c_s^2\omega_4\omega_1 + 12\omega_3c_s^2\omega_4^2\omega_1^2 - 36\omega_3\omega_4\omega_1^2v_1^4 - 36\omega_3^2c_s^2\omega_4\omega_1^3v_1^2 - 36\omega_3\omega_4^2\omega_1^2v_1^2 + 3\omega_3^2c_s^4\omega_4\omega_1^3 + 15\omega_3^2\omega_4\omega_1^3v_1^2 - 3\omega_3c_s^2\omega_4^2\omega_1^3 + 54\omega_3c_s^2\omega_4\omega_1^3v_1^2 - 54\omega_3^2c_s^2\omega_1^3v_1^2 + 9\omega_3^2\omega_1^3v_1^4 + 18\omega_3^2\omega_1^2v_1^2 - 12\omega_3^2c_s^4\omega_4\omega_1^2 + 12\omega_3c_s^2\omega_4^2\omega_1 + 12\omega_3^2c_s^4\omega_4\omega_1 - 36\omega_3^2\omega_4\omega_1^2v_1^2 - 12\omega_3c_s^2\omega_4^2\omega_1^2 + 15\omega_3\omega_1^2\omega_1^3v_1^2 + 72\omega_3^2c_s^2\omega_4\omega_1^2v_1^2 + 36\omega_3c_s^2\omega_4^2\omega_1v_1^2 + 18\omega_3\omega_4\omega_1^3v_1^4 - 12\omega_3^2\omega_4^2\omega_1^2v_1^4 - 3\omega_3^2c_s^2\omega_4\omega_1^3 - 36\omega_3^2c_s^2\omega_1^2v_1^2 + 3\omega_3c_s^4\omega_4^2\omega_1^3 - 9\omega_3^2\omega_1^3v_1^2 + 12\omega_3^2c_s^2\omega_4\omega_1^2 - 18\omega_3^2v_1^4 - 108\omega_3c_s^2\omega_4\omega_1^2v_1^2 - 12\omega_3c_s^2\omega_4^2\omega_1 + 27\omega_3^2c_s^2\omega_1^3v_1^2$$

$$C_{22} = 4\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 - 18\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 - 9\omega_3\omega_1v_1^2\omega_2 + 18\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 6\omega_3\omega_4\omega_1v_1^2\omega_2$$

$$C_{23} = 2\omega_3^2\omega_4\omega_1v_2^2 - 2\omega_3^2\omega_4\omega_1 + 6\omega_3\omega_4^2v_2^2 - 6\omega_3\omega_4^2 - 18\omega_3c_s^2\omega_4\omega_1 - 6\omega_4^2v_2^2 + 36\omega_3c_s^2\omega_4 - 6\omega_3^2\omega_4v_2^2 + 2\omega_3\omega_4^2\omega_1 - 6\omega_4^2\omega_1 - 6\omega_4^2v_1^2 + 3\omega_4^2\omega_1v_1^2 - 2\omega_3\omega_4^2\omega_1v_2^2 + 6\omega_3^2v_2^2 + 12\omega_4^2 + 3\omega_4^2\omega_1v_2^2 + 18\omega_3c_s^2\omega_4^2 - 36c_s^2\omega_4^2 - 12\omega_3\omega_4 - 6\omega_3^2v_1^2 + 6\omega_3^2c_s^2\omega_4\omega_1 + 6\omega_3^2\omega_4 - 6\omega_3\omega_4\omega_1v_1^2 + 18c_s^2\omega_4^2\omega_1 + 3\omega_3^2\omega_1v_1^2 + 12\omega_3\omega_4v_1^2 + 6\omega_3\omega_4\omega_1 - 18\omega_3^2c_s^2\omega_4 - 3\omega_3^2\omega_1v_2^2 - 6\omega_3c_s^2\omega_4\omega_1$$

$$C_{24} = -3\omega_4^2\omega_1^3v_2^2\omega_5 + 6\omega_3^2\omega_1^2v_2^2\omega_5 + 12\omega_3c_s^2\omega_4^2\omega_1v_2^2\omega_5 - 6\omega_4^2\omega_1^2v_2^2\omega_5 + 3\omega_3^2\omega_1^2v_2^2\omega_5 + 2\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 - 9\omega_3^2c_s^2\omega_1^3v_2^2\omega_5 - 32\omega_3^2c_s^4\omega_4^2\omega_1 - 8\omega_3^2c_s^4\omega_4\omega_1\omega_5 + 6\omega_3^2\omega_4\omega_1^2v_1^2\omega_5 - 18c_s^2\omega_4^2\omega_1^2v_1^2\omega_5 + 6\omega_3\omega_4^2\omega_1^2v_1^4\omega_5 + 3\omega_3^2\omega_4\omega_1^3v_1^4\omega_5 - 6\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_5 - 6\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_5 + 3\omega_3\omega_4^2\omega_1^3v_1^2\omega_5 - 8\omega_3c_s^2\omega_4^2\omega_1^2\omega_5 + 12\omega_3c_s^2\omega_4\omega_1^2v_2^2\omega_5 + 6\omega_3^2\omega_1^2v_2^2\omega_5 - 8\omega_3^2c_s^2\omega_4\omega_1^3\omega_5 - 3\omega_3^2\omega_1^2v_2^2\omega_5 - 6\omega_4^2\omega_1^2v_1^4\omega_5 + 2\omega_3c_s^4\omega_4^2\omega_1^3\omega_5 + 6\omega_3\omega_4^2\omega_1^2v_2^2\omega_5 - 18c_s^2\omega_4^2\omega_1^2v_2^2\omega_5 + 6\omega_3\omega_4\omega_1^2v_2^2\omega_5 + 6\omega_3^2\omega_4\omega_1^2v_2^2\omega_5 - 6\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_5 - 6\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_5 + 6\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_5 + 6\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_5 - 3\omega_3^2\omega_4\omega_1^3v_1^2\omega_5 - 3\omega_3\omega_4^2\omega_1^3v_1^4\omega_5 + 9c_s^2\omega_4^2\omega_1^3v_2^2\omega_5 - 2\omega_3^2c_s^4\omega_4\omega_1^3\omega_5 - 6\omega_3^2\omega_1^2v_2^2\omega_5 + 3\omega_4^2\omega_1^2v_2^2\omega_5 + 8\omega_3^2c_s^2\omega_4\omega_1\omega_5 + 16\omega_3^2c_s^4\omega_4^2\omega_5 + 18\omega_3^2c_s^2\omega_1^2v_2^2\omega_5 + 8\omega_3c_s^2\omega_4^2\omega_1^2\omega_5 - 3\omega_3^2\omega_1^2v_2^2\omega_5 + 6\omega_4^2\omega_1^2v_2^2\omega_5 - 12\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_5 + 6\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_5 + 8\omega_3^2c_s^4\omega_4\omega_1^2\omega_5 + 6\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_5 - 6\omega_3\omega_4^2\omega_1^2v_2^2\omega_5 - 6\omega_3^2\omega_4\omega_1^2v_2^2\omega_5 + 9c_s^2\omega_4^2\omega_1^3v_2^2\omega_5 - 3\omega_3\omega_4^2\omega_1^3v_2^2\omega_5 - 3\omega_3^2\omega_4\omega_1^3v_2^2\omega_5 + 8\omega_3c_s^4\omega_4^2\omega_1\omega_5 + 18\omega_3^2c_s^2\omega_1^2v_2^2\omega_5 - 2\omega_3c_s^2\omega_4^2\omega_1^3\omega_5 + 3\omega_4^2\omega_1^3v_1^4\omega_5 - 8\omega_3^2c_s^4\omega_4\omega_1\omega_5 - 6\omega_3^2\omega_1^2v_2^2\omega_5 - 12\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_5 + 6\omega_4^2\omega_1^2v_2^2\omega_5 - 3\omega_3^2\omega_1^2v_2^2\omega_5$$

$$C_{25} = -18\omega_3\omega_4v_1^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 + 4\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 6\omega_3\omega_4\omega_1v_2^2\omega_2 + 18\omega_3\omega_4\omega_1v_1^2 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_4\omega_1v_2^2\omega_2 - 9\omega_3\omega_1v_2^2\omega_2$$

$$C_{26} = -2\omega_3^2\omega_4\omega_1 - 6\omega_3\omega_4^2 - 6\omega_3^2\omega_4v_1^2 - 18\omega_3c_s^2\omega_4\omega_1 - 6\omega_4^2v_2^2 + 36\omega_3c_s^2\omega_4 + 2\omega_3^2\omega_4\omega_1v_1^2 + 6\omega_3\omega_4^2v_1^2 + 2\omega_3\omega_4^2\omega_1 - 6\omega_4^2\omega_1 - 6\omega_4^2v_1^2 + 3\omega_4^2\omega_1v_1^2 - 6\omega_3^2v_2^2 + 12\omega_4^2 + 3\omega_4^2\omega_1v_2^2 + 18\omega_3c_s^2\omega_4^2 - 36c_s^2\omega_4^2 - 12\omega_3\omega_4 - 2\omega_3\omega_4^2\omega_1v_1^2 + 6\omega_3^2v_1^2 + 6\omega_3^2c_s^2\omega_4\omega_1 + 6\omega_3^2\omega_4 - 6\omega_3\omega_4\omega_1v_2^2 + 18c_s^2\omega_4^2\omega_1 - 3\omega_3^2\omega_1v_1^2 + 6\omega_3\omega_4\omega_1 - 18\omega_3^2c_s^2\omega_4 + 12\omega_3\omega_4v_2^2 + 3\omega_3^2\omega_1v_2^2 - 6\omega_3c_s^2\omega_4^2\omega_1$$

$$C_{27} = -3c_s^4\omega_1\omega_2 - 36c_s^2\omega_1v_2^2\omega_2 + 48c_s^2v_2^2\omega_2 - 6\omega_1v_2^2 - 9\omega_1v_2^4\omega_2 - 4c_s^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 12v_2^4\omega_2 + 24c_s^2\omega_1v_2^2 + 9\omega_1v_2^2\omega_2 + 6\omega_1v_2^4 - 2c_s^2\omega_1 + 4c_s^4\omega_2 - 12v_2^2\omega_2$$

$$C_{28} = 24\omega_3^2c_s^4\omega_4^2 + 9\omega_4^2\omega_3^3v_2^4 + 18\omega_3^2\omega_1^2v_2^2 + 36\omega_3^2c_s^2\omega_4\omega_1v_2^2 + 72\omega_3c_s^2\omega_4^2\omega_1^2v_2^2 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2 - 12\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2 - 18\omega_3\omega_4\omega_1^3v_2^2 - 48\omega_3^2c_s^4\omega_4^2\omega_1 + 12\omega_3^2\omega_4^2\omega_1^2v_2^2 + 36\omega_3^2\omega_4\omega_1^2v_2^4 + \omega_3^2c_s^2\omega_4^2\omega_1^3 - 15\omega_3\omega_4^2\omega_1^3v_2^4 + 27c_s^2\omega_4^2\omega_1^3v_2^2 - 36\omega_3c_s^2\omega_4^2\omega_1^3v_2^2 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 - 9\omega_3^2\omega_1^2v_2^2 - 18\omega_4^2\omega_1^2v_2^4 - 54c_s^2\omega_4^2\omega_1^2v_2^2 + 36\omega_3\omega_4^2\omega_1^2v_2^4 + 12\omega_3^2c_s^2\omega_4\omega_1 - 15\omega_3^2\omega_4\omega_1^3v_2^4 - 3\omega_3^2\omega_4\omega_1^3v_2^2 + 36\omega_3\omega_4\omega_1^2v_2^2 + 6\omega_3^2c_s^2\omega_4\omega_1^3v_2^2 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 - 54\omega_3^2c_s^2\omega_1^2v_2^2 - 12\omega_3^2c_s^2\omega_4\omega_1^2v_2^2 + 18\omega_4^2\omega_1^2v_2^4 + 9\omega_3^2\omega_4\omega_1^2v_2^2 + 18\omega_4^2\omega_1^2v_2^4 + 12\omega_3^2c_s^2\omega_4\omega_1^2v_2^2 + 18\omega_4^2\omega_1^2v_2^4 + 12\omega_3^2c_s^2\omega_4\omega_1^2v_2^2 + 18\omega_4^2\omega_1^2v_2^4 + 12\omega_3^2c_s^2\omega_4\omega_1^2v_2^2 + 18\omega_4^2\omega_1^2v_2^4 - 36\omega_3\omega_4^2\omega_1^2v_2^2 - 12\omega_3^2c_s^4\omega_4\omega_1^3v_2^2 + 15\omega_3^2\omega_4\omega_1^3v_2^2 + 12\omega_3c_s^4\omega_4^2\omega_1 + 12\omega_3^2c_s^4\omega_4\omega_1 - 36\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2 - 12\omega_3c_s^4\omega_4^2\omega_1^2 - 18\omega_3^2\omega_1^2v_2^4 - 9\omega_4^2\omega_1^2v_2^2 + 27\omega_3^2c_s^2\omega_1^2v_2^2 - 108\omega_3c_s^2\omega_4\omega_1^2v_2^2 - 3\omega_3^2c_s^2\omega_4\omega_1^3 - 36\omega_3^2\omega_4\omega_1^2v_2^2 + 3\omega_3c_s^4\omega_4^2\omega_1^3 + 72\omega_3^2c_s^2\omega_4\omega_1^2v_2^2 + 15\omega_3\omega_4^2\omega_1^3v_2^2 + 18\omega_3\omega_4\omega_1^3v_2^2 + 12\omega_3^2c_s^2\omega_4\omega_1^2v_2^2 + 36\omega_3c_s^2\omega_4^2\omega_1v_2^2 - 12\omega_3^2\omega_4^2\omega_1^2v_2^2 - 12\omega_3c_s^2\omega_4^2\omega_1$$

$$C_{29} = 160\omega_3^2\omega_4^2v_1^2\omega_2^3 - 256\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 9\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 144\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_1^2\omega_2^3 - 784\omega_3^2c_s^2\omega_4^2v_1^2\omega_2^3 - 368\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 108\omega_3^2c_s^4\omega_1^2\omega_2^3 - 27\omega_3c_s^4\omega_4^2\omega_1^2v_1^2\omega_2^3 + 1232\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 - 16\omega_3^2\omega_4^2\omega_2^3 + 28\omega_3^2\omega_4^2\omega_1\omega_2^3 + 18\omega_3^2c_s^2\omega_1^2v_1^2\omega_2^3 + 152\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2 + 56\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 + 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2 + 18\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 32\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 - 56\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_2^3 + 120\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2 - 104\omega_3^2c_s^2\omega_4^2\omega_1^3 - 108\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 - 108c_s^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 712\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2 + 56\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 6\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^3 - 96\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2 + 54\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 + 6\omega_3^2\omega_4^2\omega_1^3\omega_2^3 + 48\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + 36\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 + 394\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 + 216\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + 12\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 92\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^3 - 56\omega_3^2\omega_4^2\omega_1^3v_1^2 + 36\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 + 16\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 - 36c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 + 320\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2 + 54c_s^4\omega_4^2\omega_1^3\omega_2^3 + 9\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 120\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + 6\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 - 78\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^3 - 276\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3 - 56\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 - 342\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 118\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 132\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 + 48\omega_3^2\omega_4^2\omega_1^3v_1^4 + 24\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^3 + 448\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 14\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - 136\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 588\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 + 208\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 40\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 9\omega_3c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 144\omega_3^2\omega_4^2\omega_1^3\omega_2^3 + 228\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1^2\omega_2^3 - 88\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 168\omega_3c_s^4\omega_4^2\omega_1\omega_2^3 - 18\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 6\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 36c_s^2\omega_4^2\omega_1^2\omega_2^3 + 72\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 108\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 36\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 6\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^3 - 144\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 + 8\omega_3^2\omega_4^2\omega_1^3 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 6\omega_3^2v_3^4\omega_4^2\omega_1^2\omega_2^3 - 72\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 92\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 460\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2^3 + 52\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^2v_3^4\omega_4^2\omega_1^2\omega_2^3 - 288\omega_3^2c_s^4\omega_4^2\omega_2^3 + 104\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 - 18c_s^2\omega_4^2\omega_1^3\omega_2^3 - 27\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 18c_s^4\omega_4^2\omega_1^3v_1^2\omega_2^3 + 78\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^3 + 208\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 184\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 14\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - 412\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 - 9\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_2^3 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2^3$$

$$C_{30} = -3\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 16\omega_3c_s^4\omega_4\omega_1^3 - 60\omega_3\omega_4\omega_1^3v_1^2 - 90\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 + 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 18c_s^2\omega_4\omega_1^3\omega_2^3 + 42\omega_3c_s^2\omega_4\omega_1^3\omega_2 + 24c_s^2\omega_4\omega_1v_1^2\omega_2^3 + 408\omega_3\omega_4\omega_1v_1^4\omega_2^3 + 8c_s^4\omega_4\omega_1\omega_2^3 + 27\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 - 24\omega_3\omega_4\omega_1v_1^4\omega_2^3 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 9c_s^2\omega_4\omega_1^3\omega_2^3 - 153\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 - 36\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^3 - 240\omega_3\omega_4\omega_1^2v_1^2\omega_2 + 24c_s^4\omega_4\omega_1^2v_1^2\omega_2 - 8\omega_3\omega_4\omega_2^3 - \omega_3v_3^4\omega_4\omega_1^2\omega_2^3 - 96\omega_3\omega_4\omega_2^3v_1^2\omega_2 - 20\omega_3c_s^2\omega_4\omega_1^2\omega_2 + \omega_3v_3^4\omega_4\omega_1^2\omega_2^3 + 14\omega_3\omega_4\omega_1\omega_2^3 + 84\omega_3\omega_4\omega_2^3v_1^2\omega_2^3 - 20c_s^2\omega_4\omega_1^2\omega_2^3 + 144\omega_3\omega_4\omega_1^2\omega_2^3 - 16\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 138\omega_3\omega_4\omega_1^3v_1^4\omega_2^3 - 54c_s^2\omega_4\omega_1^3v_1^2\omega_2^3 + 81\omega_3\omega_4\omega_1^2v_1^2\omega_2^3 + 94\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 4\omega_3\omega_4\omega_1\omega_2^3 + 108\omega_3c_s^2\omega_1v_1^2\omega_2^3 + 36\omega_3c_s^4\omega_1\omega_2^3 + 27c_s^2\omega_4\omega_1^3v_1^2\omega_2^3 + 3\omega_3c_s^2v_3^4\omega_4\omega_1^2\omega_2^3 + 120\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2 - 8c_s^2\omega_4\omega_1^2\omega_2 + 18c_s^2\omega_4\omega_1^2\omega_2^3 - 24\omega_3c_s^2\omega_4\omega_1^3\omega_2^3 - 18c_s^4\omega_4\omega_1^3\omega_2^3 + 12\omega_3\omega_4\omega_1v_1^2\omega_2^3 - 4\omega_3\omega_4\omega_1^2\omega_2^3 - 29\omega_3c_s^4\omega_4\omega_1^2\omega_2^3 - 32\omega_3c_s^4\omega_4\omega_1^3\omega_2 + 138\omega_3\omega_4\omega_1^3v_1^2\omega_2 -$$

$$\begin{aligned}
& 36\omega_3c_s^4\omega_1^2\omega_2^3 + 4\omega_3\omega_4\omega_1^3 - 9\omega_3c_s^2\omega_1^3\omega_2^3 - 8c_s^2\omega_4\omega_1\omega_2^3 + 192\omega_3\omega_4\omega_1^2v_1^4\omega_2 + 144\omega_3c_s^2\omega_4\omega_1^3v_1^2 - 68\omega_3c_s^4\omega_4\omega_2^3 - 108\omega_3c_s^2\omega_1^2v_2^2\omega_2^3 - \\
& 10\omega_3\omega_4\omega_1^3\omega_2 - 7\omega_3\omega_4\omega_1^2\omega_2^3 - 222\omega_3\omega_4\omega_1v_1^2\omega_2^3 + 9c_s^4\omega_4\omega_1^3\omega_2^3 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2^3 + 153\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2^3 + \omega_3v_3^4\omega_4\omega_1^3\omega_2^3 - 288\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2 - \\
& \omega_3v_3^4\omega_4\omega_1^2\omega_2^3 - 54c_s^2\omega_4\omega_1^2v_2^2\omega_2^3 - 138\omega_3\omega_4\omega_1^2v_1^4\omega_2^3 + 32\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 60\omega_3c_s^2\omega_4\omega_1v_1^2\omega_2^3 + 36\omega_3c_s^2\omega_1^2\omega_2^3 + 9\omega_3c_s^4\omega_1^3\omega_2^3 + 96\omega_3\omega_4\omega_1^3v_1^4 - \\
& 3\omega_3c_s^4\omega_4\omega_1^3\omega_2^3 + 7\omega_3\omega_4\omega_1^3\omega_2^2 + 20c_s^4\omega_4\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1^2\omega_2 + 40\omega_3c_s^2\omega_4\omega_1^3\omega_2^3 + 432\omega_3c_s^2\omega_4\omega_1v_1^2\omega_2^3 - 54\omega_3c_s^2\omega_4\omega_1\omega_2^3 + 60c_s^2\omega_4\omega_1^2v_2^2\omega_2^2 - \\
& 168\omega_3\omega_4\omega_1^2v_1^4\omega_2^2 - 312\omega_3c_s^2\omega_4v_1^2\omega_2^3 + 8\omega_3\omega_4\omega_1^2\omega_2 + 8c_s^4\omega_4\omega_1^3\omega_2 + 17\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 - 264\omega_3\omega_4v_1^4\omega_2^3 - 18c_s^4\omega_4\omega_1^2\omega_2^3 - 81\omega_3\omega_4\omega_1^3v_1^2\omega_2^3
\end{aligned}$$

$$\begin{aligned}
C_{31} = & 4\omega_3\omega_4v_2^2\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 - 18\omega_3v_3^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 9\omega_4\omega_1v_1^2\omega_2 - 9\omega_3\omega_1v_2^2\omega_2 + \\
& 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_1^2 + 18\omega_3v_3^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 6\omega_3\omega_4\omega_1v_1^2\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{32} = & -96\omega_3^2\omega_1^2v_2^2\omega_2^3 + 10\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 - 108\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_2^3 + 96\omega_3^2\omega_4\omega_1v_1^2\omega_2^3 - 60\omega_3^2\omega_1^3v_2^2v_1^2\omega_2 + 30\omega_3^2c_s^4\omega_1^2\omega_2^3\omega_2^2 + 54\omega_3^2c_s^2\omega_1^3\omega_2^3 + \\
& 432\omega_3^2c_s^2\omega_4^2v_1^2\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 84c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 - 8\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_2 + 324\omega_3^2c_s^4\omega_1^2\omega_2^3 - 81\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 120\omega_3^2\omega_4^2\omega_1^2v_2^2v_1^2\omega_2^2 - \\
& 432\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 + 8\omega_3^2\omega_4^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 + 96\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 + 56\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2 + 96\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1\omega_2^3 - \\
& 432\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_2^3 - 72\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2 - 56\omega_3c_s^2\omega_4^2\omega_1v_2^2\omega_2^3 - 104\omega_3^2c_s^2\omega_1^3\omega_2^3 - 252c_s^4\omega_1^2\omega_2^3\omega_2^2 + 108\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 432\omega_3^2c_s^2\omega_1^3v_1^2\omega_2^2 + \\
& 128\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 32\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^3 + 72\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2 - 162\omega_3^2c_s^4\omega_1^3\omega_2^3 - 8\omega_3^2\omega_4^2v_2^2\omega_2^3 - 24\omega_3c_s^4\omega_1^2\omega_2^3\omega_2^2 - 27\omega_3c_s^2\omega_1^3v_2^2\omega_2^3 - 72c_s^4\omega_1^2\omega_2^3\omega_2^2 + \\
& 8\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^3 + 324\omega_3c_s^4\omega_1^2\omega_2^3\omega_2^2 + 192\omega_3^2c_s^4\omega_1^2\omega_2^3 - 96\omega_3^2\omega_1^3v_1^2 + 8\omega_3^2c_s^2\omega_4^2\omega_1v_2^2\omega_2^3 - 108\omega_3^2c_s^2\omega_1^2\omega_2^3 + 432\omega_3^2c_s^2\omega_1^3v_1^2 + 8\omega_3^2\omega_4^2\omega_1v_2^2\omega_2^2 + \\
& 162c_s^4\omega_1^2\omega_2^3\omega_2^3 - 27\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 192\omega_3c_s^4\omega_1^2\omega_2^3\omega_2^2 - 24\omega_3^2\omega_4^2\omega_1^2v_2^2v_1^2\omega_2 + 8\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2 - 54\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^3v_2^2 - 40\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_2 - \\
& 168\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2 + 32\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3 - 30\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 56\omega_3^2c_s^2\omega_4^2\omega_1v_2^2\omega_2^3 - 10\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_2 + \\
& 48\omega_3^2\omega_4^2\omega_1^3v_1^4 - 24c_s^2\omega_4^2\omega_1^3v_2^2\omega_2^3 - 432\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2 - 96\omega_3^2\omega_4^2\omega_1v_2^2v_1^2\omega_2 + 96\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 24\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 - 104\omega_3^2c_s^2\omega_4^2\omega_2^3 - \\
& 10\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 27\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 60\omega_3^2\omega_4^2\omega_1v_2^2v_1^2\omega_2^3 + 24\omega_3^2\omega_1^3v_1^4\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1v_1^4\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2 + 54c_s^2\omega_1^3v_2^2\omega_2^3 + 80\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 - \\
& 168\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 16\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 + 72\omega_3^2\omega_4^2v_2^2v_1^2\omega_2^3 + 27\omega_3^2c_s^2\omega_4\omega_1^2v_2^2\omega_2^3 + 84c_s^2\omega_4^2\omega_1^2\omega_2^3 - 324\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^3 + 32\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - \\
& 216\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 + 8\omega_3^2\omega_4^2\omega_1^3 + 8\omega_3c_s^2\omega_4^2\omega_1^2\omega_2 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2 + 48\omega_3^2\omega_4^2\omega_1^3v_2^2v_1^2 - 108\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 24c_s^2\omega_4^2\omega_1^3\omega_2^2 + 16\omega_3^2\omega_4^2\omega_1^2\omega_2^2 + \\
& 64\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 176\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 108\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 8\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2 - 192\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 64\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - \\
& 54c_s^2\omega_4^2\omega_1^2\omega_2^2 + 81\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^3 + 112\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 + 10\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 864\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_2^3 + 108\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2^3
\end{aligned}$$

$$\begin{aligned}
C_{33} = & -24\omega_3c_s^2\omega_1^2\omega_2^2 + 2\omega_3^2\omega_2 + 26\omega_3c_s^2\omega_2^3 - 6c_s^2\omega_1\omega_2^3 - 4\omega_3\omega_1^2v_2^2\omega_2 + 10\omega_3\omega_1^2\omega_2 - 24\omega_3c_s^2\omega_1\omega_2^3 - 4\omega_1^2\omega_2^2 + 26\omega_3\omega_1^2v_1^2\omega_2^2 - 20\omega_3\omega_1^2\omega_2^2 + \\
& 14\omega_3\omega_1^2\omega_2 - 22\omega_3\omega_1^2v_2^2\omega_2 + 4\omega_1^2v_2^2\omega_2^2 + 6\omega_3\omega_1^2v_2^2\omega_2^2 - 10\omega_3\omega_2^3 - 3\omega_3\omega_1^2v_2^2\omega_2^2 + 4\omega_3\omega_1^3v_2^2 - 30\omega_3c_s^2\omega_1^2\omega_2 - 2\omega_1^3v_2^2\omega_2 + 3\omega_3\omega_1^3v_2^2\omega_2 + \\
& 28\omega_3c_s^2\omega_1^3 - 4\omega_3\omega_1v_2^2\omega_2^2 + 4\omega_3v_2^2\omega_2^3 + 16\omega_3\omega_1^3v_1^2 - 2\omega_1v_2^2\omega_2^3 - 24\omega_3c_s^2\omega_1^2\omega_2 - 12\omega_3\omega_1^3 - 13\omega_3\omega_1v_1^2\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 12c_s^2\omega_1^2\omega_2^2 + \\
& 48\omega_3c_s^2\omega_1^2\omega_2^2 - 4\omega_3\omega_1v_1^2\omega_2^2 + 10\omega_3v_1^2\omega_2^3 + 2\omega_1\omega_2^3 - 13\omega_3\omega_1^3v_1^2\omega_2 - 6c_s^2\omega_1^3\omega_2 + 10\omega_3\omega_1\omega_2^3
\end{aligned}$$

$$\begin{aligned}
C_{34} = & -108\omega_3^2\omega_1^2v_2^2\omega_5\omega_2^3 + 8\omega_3^2c_s^4\omega_1^2\omega_5\omega_2^3 - 88\omega_3^2c_s^2\omega_4^2\omega_5\omega_2^3 + 54\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + 300\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 + 24\omega_3^2\omega_1^3v_2^2\omega_5\omega_2 - 36\omega_3^2\omega_4\omega_1v_2^2\omega_5\omega_2^3 - \\
& 96\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_5 - 72\omega_3c_s^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1\omega_5\omega_2^3 - 6\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + 8\omega_3^2\omega_4^2\omega_5\omega_2^3 + 180\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 264\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_5 + \\
& 36\omega_3^2c_s^2\omega_4^2\omega_1\omega_5\omega_2^3 + 72\omega_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 48\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + 12\omega_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 72\omega_3^2\omega_4^2\omega_1^2v_2^2v_1^2\omega_5\omega_2 - 27\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + \\
& 72\omega_3c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^3 + 324\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 + 144\omega_3^2\omega_4^2\omega_1^3v_2^2v_1^2\omega_5 + 132\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1\omega_5\omega_2^3 + 72\omega_3c_s^2\omega_4^2\omega_1\omega_5\omega_2 - \\
& 72\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_5\omega_2^3 - 36\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 - 54\omega_3^2\omega_1^3v_1^4\omega_5\omega_2^3 - 216\omega_3^2c_s^2\omega_4^2v_1^2\omega_5\omega_2^3 - 24\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 56\omega_3^2c_s^4\omega_4^2\omega_1\omega_5\omega_2^3 + \\
& 72\omega_1^2\omega_1^2v_1^2\omega_5\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^3\omega_5\omega_2 - 72\omega_3c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^3 + 36\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2 - 108\omega_3^2c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 + 24\omega_3^2\omega_4^2v_1^2\omega_5\omega_2^3 - 108\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - \\
& 48\omega_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1\omega_5\omega_2^3 - 12\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2 + 648\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + 16\omega_3c_s^4\omega_4^2\omega_1^3\omega_5\omega_2 - 54\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 4\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - \\
& 288\omega_3^2c_s^2\omega_4^2\omega_1\omega_5\omega_2^3 - 24\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_5 + 108\omega_3^2\omega_1^3v_2^2\omega_5\omega_2^3 - 2\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^3 + 6\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2^3 + 27\omega_3^2c_s^2v_3^2\omega_4\omega_1^3\omega_5\omega_2^3 + 36\omega_3^2\omega_4\omega_1v_1^2\omega_5\omega_2^3 + \\
& 32\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_5 + 24\omega_3^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 72\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 288\omega_3^2c_s^4\omega_4\omega_1^2\omega_5\omega_2^3 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_5\omega_2 - 162\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_5\omega_2^3 + 4\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^3 - \\
& 96\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2 + 336\omega_3c_s^2\omega_4^2\omega_1v_2^2\omega_5\omega_2^3 - 288\omega_3^2\omega_4^2\omega_1v_2^2v_1^2\omega_5\omega_2^3 + 24\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_5 + 2\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - 12\omega_3\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - \\
& 6\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + 160\omega_3c_s^4\omega_4^2\omega_1\omega_5\omega_2^3 + 108\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 + 9\omega_3^2\omega_4^2\omega_1\omega_5\omega_2^3 - 72\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2 - 72\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + \\
& 24\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2 + 36\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 54\omega_3^2\omega_1^3v_1^2\omega_5\omega_2^3 + 360\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + 216\omega_3^2\omega_4^2v_2^2v_1^2\omega_5\omega_2^3 - 96\omega_3^2\omega_4^2v_1^2\omega_5\omega_2^3 - 9\omega_3^2v_2^2\omega_4\omega_1^3\omega_5\omega_2^3 - \\
& 180\omega_3^2\omega_1^2v_2^2v_1^2\omega_5\omega_2^3 - 160\omega_3c_s^2\omega_4^2\omega_1\omega_5\omega_2^3 - 162\omega_3^2c_s^2\omega_1^3v_1^2\omega_5\omega_2^3 + 108\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 - 6\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_5\omega_2^3 + 288\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + \\
& 108\omega_3\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 108\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 + 24\omega_3^2\omega_4^2\omega_1v_2^2\omega_5\omega_2^3 - 180\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2^3 + 36\omega_3\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 - 216c_s^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 + \\
& 64\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2 + 112\omega_3c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^3 - 72\omega_3\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 152\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^3 + 9\omega_3v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^3 + 288\omega_3^2c_s^2\omega_4\omega_1\omega_5\omega_2^3 - 84\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 + \\
& 132\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2 - 120\omega_3^2c_s^2\omega_4^2\omega_1v_2^2\omega_5\omega_2^3 + 144\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 - 56\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_5\omega_2 - 112\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 36\omega_3^2\omega_4\omega_1^3v_1^4\omega_5\omega_2^3 - \\
& 288\omega_3^2c_s^4\omega_4\omega_1\omega_5\omega_2^3 - 9\omega_3v_3^4\omega_4^2\omega_1^3\omega_5\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_5\omega_2 - 288\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 60\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 - 648\omega_3^2c_s^2\omega_4\omega_1v_2^2\omega_5\omega_2^3 + 18\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 - \\
& 24\omega_3^2\omega_4^2v_2^2\omega_5\omega_2^3 + 18\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 - 216\omega_3c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^3 + 48\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_5 + 54\omega_3\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 348\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2 + 24\omega_3^2\omega_4^2\omega_1v_2^2\omega_5\omega_2^3 - \\
& 216\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 + 12\omega_3\omega_4^2\omega_1^2v_1^4\omega_5\omega_2^3 + 162\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2^3 - 24\omega_3\omega_4^2\omega_1^3v_1^4\omega_5\omega_2 + 36\omega_3\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 + 48\omega_3^2c_s^2\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^2 + \\
& 36\omega_3\omega_4\omega_1^3v_1^2\omega_5\omega_2^3 + 24\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_5\omega_2 + 54\omega_3^2\omega_4\omega_1^3v_1^4\omega_5\omega_2^3 + 36\omega_3\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 - 168\omega_3^2c_s^2\omega_4^2\omega_1v_2^2\omega_5\omega_2^3 + 240\omega_3^2c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + \\
& 216\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + 108\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 - 24\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2 - 468\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 + 72\omega_3\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 - 108c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^2 - \\
& 2\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - 180\omega_3^2\omega_4^2\omega_1^3v_2^2v_1^2\omega_5\omega_2 - 36\omega_3\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + 180\omega_3c_s^2\omega_4^2\omega_1v_1^2\omega_5\omega_2^3 - 28\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^3 - \\
& 36\omega_3^2\omega_4\omega_1^3v_1^2\omega_5\omega_2^3 + 2\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_5\omega_2^3 - 144\omega_3^2\omega_4\omega_1^2v_1^4\omega_5\omega_2^3 - 72\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_5\omega_2 + 8\omega_3^2\omega_4^2\omega_1^3\omega_5 - 40\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_5 + 4\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + \\
& 60\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 + 56\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_5\omega_2^3 - 72\omega_3^2c_s^4\omega_4\omega_1^2\omega_5\omega_2^3 - 18\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 18\omega_3^2\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 - 12\omega_3\omega_4^2\omega_1^2v_1^2\omega_5\omega_2^3 + \\
& 108\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_5\omega_2^3 + 162c_s^2\omega_4^2\omega_1^3v_1^2\omega_5\omega_2^3 - 54\omega_3\omega_4^2\omega_1^3v_1^4\omega_5\omega_2^3 + 264\omega_3c_s^2\omega_4^2\omega_1^2v_2^2\omega_5\omega_2^3 - 36\omega_3\omega_4\omega_1^3v_1^4\omega_5\omega_2^3 + 48\omega_3c_s^2\omega_4^2\omega_1^3v_2^2\omega_5\omega_2 + \\
& 72\omega_3^2c_s^2\omega_4\omega_1^3\omega_5\omega_2^3 - 36\omega_3\omega_4\omega_1^2v_1^2\omega_5\omega_2^3 + 24\omega_3\omega_4^2\omega_1^3v_1^2\omega_5\omega_2 - 72\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_5\omega_2^3 + 6\omega_3^2c_s^2v_3^2\omega_4^2\omega_1^3\omega_5\omega_2^3 - 36\omega_3^2\omega_4\omega_1^3v_1^4\omega_5\omega_2^3 - 54\omega_3^2\omega_4\omega_1^3v_2^2\omega_5\omega_2^3
\end{aligned}$$

$$\begin{aligned}
C_{35} = & 6\omega_3c_s^2\omega_4\omega_1 + 9\omega_4\omega_1\omega_2 - 2\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_2^2 - 9\omega_3\omega_1\omega_2 - 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 - \\
& 9\omega_4\omega_1v_2^2\omega_2 + 9\omega_3\omega_1v_2^2\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{36} = & -8\omega_3^2\omega_4^2v_1^2\omega_2^3 + 8\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^3 - 27\omega_3c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^3 - 60\omega_3^2\omega_4^2\omega_1^3v_2^2v_1^2\omega_2 + 30\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 + 54\omega_3^2c_s^2\omega_1^3\omega_2^3 + 72\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + \\
& 32\omega_3^2c_s^2\omega_4^2v_1^2\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1\omega_$$

$$\begin{aligned}
& 153\omega_3c_s^2\omega_4\omega_1^2v_2^2\omega_3^2 + 94\omega_3c_s^4\omega_4\omega_1\omega_3^2 - 4\omega_3\omega_4\omega_1\omega_2^2 - 24\omega_3\omega_4\omega_1v_2^4\omega_2^2 + 36\omega_3c_s^4\omega_1\omega_3^2 - 96\omega_3\omega_4\omega_1^2v_2^2\omega_2 + 3\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 8c_s^2\omega_4\omega_1^3\omega_2 + 18c_s^2\omega_4\omega_1^2\omega_3^2 - 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 18c_s^4\omega_4\omega_1^2\omega_2^2 - 4\omega_3\omega_4\omega_1^2\omega_3^2 - 60\omega_3c_s^2\omega_4\omega_1v_2^2\omega_2^2 + 144\omega_3c_s^2\omega_4\omega_1^3v_2^2 - 32\omega_3c_s^2\omega_4\omega_1^3\omega_2 - 138\omega_3\omega_4\omega_1^3v_2^4\omega_3^2 - 54c_s^2\omega_4\omega_1^3v_2^2\omega_3^2 - 36\omega_3c_s^4\omega_1^2\omega_3^2 - 288\omega_3c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 4\omega_3\omega_4\omega_1^3 - 9\omega_3c_s^2\omega_1^3\omega_3^2 - 8c_s^2\omega_4\omega_1\omega_3^2 - 68\omega_3c_s^4\omega_4\omega_3^2 - 168\omega_3\omega_4\omega_1^3v_2^2\omega_2^2 + 60c_s^2\omega_4\omega_1^2v_2^2\omega_2^2 - 10\omega_3\omega_4\omega_1^3\omega_2 - 7\omega_3\omega_4\omega_1^2\omega_3^2 + 9c_s^4\omega_4\omega_1^3\omega_3^2 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 + 432\omega_3c_s^2\omega_4\omega_1v_2^2\omega_3^2 - 81\omega_3\omega_4\omega_1^3v_2^2\omega_2^2 + \omega_3v_2^4\omega_4\omega_1^3\omega_2^2 - 312\omega_3c_s^4\omega_4v_2^2\omega_3^2 - 264\omega_3\omega_4v_2^4\omega_3^2 - \omega_3v_2^4\omega_4\omega_1^2\omega_3^2 + 138\omega_3\omega_4\omega_1^3v_2^2\omega_2 + 32\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 12\omega_3\omega_4\omega_1v_2^2\omega_2^2 + 36\omega_3c_s^2\omega_1^2\omega_3^2 + 9\omega_3c_s^4\omega_1^2\omega_3^2 + 192\omega_3\omega_4\omega_1^2v_2^4\omega_2 - 3\omega_3c_s^4\omega_4\omega_1^3\omega_3^2 + 7\omega_3\omega_4\omega_1^2\omega_3^2 + 20c_s^4\omega_4\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1\omega_2 + 40\omega_3c_s^2\omega_4\omega_3^2 - 222\omega_3\omega_4\omega_1v_2^2\omega_3^2 - 108\omega_3c_s^2\omega_1^2v_2^2\omega_3^2 - 54\omega_3c_s^2\omega_4\omega_1\omega_3^2 + 96\omega_3\omega_4\omega_1^3v_2^4 + 8\omega_3\omega_4\omega_1^2\omega_3^2 + 8c_s^4\omega_4\omega_1^3\omega_2 + 17\omega_3c_s^4\omega_4\omega_1^2\omega_3^2 - 18c_s^4\omega_4\omega_1^2\omega_3^2 + 153\omega_3c_s^2\omega_4\omega_1^3v_2^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{42} = & -6\omega_3\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 - 18\omega_3v_2^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 + 4\omega_3\omega_4v_2^2\omega_2 + 2\omega_3\omega_4\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 + 2\omega_3\omega_4\omega_1v_2^2 + 9\omega_3\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 + 6\omega_3\omega_4\omega_1v_2^2\omega_2 + 18\omega_3v_2^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 - 27c_s^4\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_4\omega_1v_2^2\omega_2 - 9\omega_3\omega_1v_2^2\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{43} = & 24\omega_3^2\omega_4^2v_1^2\omega_2^2 - 42\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 + 35\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2\omega_1^3\omega_3^2 - 12\omega_3^2v_2^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 216\omega_3^2c_s^2\omega_2^2v_1^2\omega_3^2 - 58\omega_3^2c_s^2\omega_2^2\omega_1\omega_3^2 - 108\omega_3^2c_s^4\omega_1^2\omega_3^2 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^2 + 324\omega_3c_s^2\omega_4^2\omega_1v_1^2\omega_2^2 + 4\omega_3^2\omega_2^2\omega_3^2 + 24\omega_3^2v_2^2\omega_4^2\omega_1^3v_1^2 - 4\omega_3^2\omega_4^2\omega_1\omega_3^2 + 66\omega_3^2\omega_4^2\omega_3^2v_1^2\omega_2 + 28\omega_3c_s^2\omega_2^2\omega_1\omega_3^2 - 24c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 + 15\omega_3^2c_s^4\omega_2^2\omega_1\omega_3^2 - 28\omega_3c_s^2v_2^2\omega_4^2\omega_1\omega_3^2 + 12\omega_3^2\omega_2^2\omega_1v_2^2\omega_3^2 - 4\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 - 36\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_3^2 - 324\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2 + 28\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 9\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_3^2 - 36\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2^2 + 54\omega_3^2c_s^4\omega_3^2\omega_2^2 - 12\omega_3c_s^4\omega_4^2\omega_1^3\omega_2 + 36\omega_3^2v_2^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 4\omega_3^2c_s^2v_2^2\omega_4^2\omega_1\omega_3^2 - 36c_s^4\omega_2^2\omega_1^3\omega_3^2 + 138\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 108\omega_3c_s^4\omega_1^2\omega_1\omega_3^2 + 24\omega_3^2c_s^4\omega_2^2\omega_1^2\omega_3^2 - 27\omega_3^2\omega_2^2\omega_1^3v_2^2\omega_3^2 - 48\omega_3^2\omega_4^2\omega_3^2v_1^2 + 4\omega_3^2v_2^2\omega_4^2\omega_1\omega_2^2 - 12c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 36\omega_3^2c_s^2\omega_1^2\omega_3^2 + 216\omega_3^2c_s^2\omega_4^2\omega_1^3v_1^2 + 54c_s^4\omega_2^2\omega_1^3\omega_3^2 + 9\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_3^2 - 28\omega_3^2c_s^2v_2^2\omega_4^2\omega_1\omega_2^2 + 96\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 - 27\omega_3^2\omega_4^2\omega_1^2v_1^4\omega_2^2 - 102\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_3^2 + 60\omega_3^2v_2^2\omega_4^2\omega_1^2v_1^2\omega_2^2 - 119\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_3^2 + 18c_s^2v_2^2\omega_4^2\omega_3^2\omega_2^2 + 4\omega_3^2v_2^2\omega_4^2\omega_1\omega_2^2 - 25\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2 + 24\omega_3^2\omega_4^2\omega_1^3v_1^4 + 16\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3^2\omega_2^2\omega_1v_1^4\omega_2^2 + 12\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2 - 9\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_3^2 + 16\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3 - 4\omega_3^2v_2^2\omega_4^2\omega_1^3 - 8\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^2 + 78\omega_3^2c_s^4\omega_4^2\omega_1\omega_3^2 + 20\omega_3^2c_s^2\omega_4^2\omega_2^2 - 30\omega_3^2v_2^2\omega_4^2\omega_1v_1^2\omega_2^2 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_3^2 + 18\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 - 60\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 72\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 - 4\omega_3^2\omega_4^2\omega_1^2\omega_2 + 4\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 84\omega_3c_s^4\omega_4^2\omega_1\omega_3^2 - 32\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 - 3\omega_3^2c_s^2\omega_2^2\omega_1^3\omega_3^2 - 20\omega_3^2\omega_2^2\omega_1^3v_2^2\omega_3^2 + 24c_s^2\omega_4^2\omega_1^2\omega_2^2 - 48\omega_3^2v_2^2\omega_4^2\omega_1v_2^2\omega_2^2 - 12\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 - 72\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 - 30\omega_3^2v_2^2\omega_4^2\omega_1^3v_2^2\omega_3^2 + 4\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2 + 138\omega_3^2c_s^2\omega_4^2\omega_1^3v_2^2\omega_3^2 + 8\omega_3^2\omega_4^2\omega_1^2\omega_2^2 - 16\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 8\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 + 32\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 24\omega_3^2\omega_2^2\omega_1^2v_2^2\omega_2^2 - 32\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - 18c_s^4\omega_2^2\omega_3^2\omega_2^2 + 4\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2 - 27\omega_3^2c_s^4\omega_4\omega_1\omega_3^2 + 3\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 27\omega_3^2\omega_4^2\omega_1^3v_1^2\omega_2^2 + 74\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 - 4\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 + 49\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_3^2 - 36\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 - 4\omega_3^2\omega_4^2\omega_1^3\omega_2
\end{aligned}$$

$$\begin{aligned}
C_{44} = & -50\omega_3\omega_1^2v_2^2\omega_3^2 + 6\omega_3^3\omega_2 - 66\omega_3c_s^2\omega_3^2 - 18c_s^2\omega_1\omega_3^2 + 48\omega_3\omega_1^3\omega_2 + 23\omega_3\omega_1^2\omega_3^2 + 108\omega_3c_s^2\omega_1\omega_3^2 - 12\omega_1^2\omega_2^2 - 66\omega_3\omega_1^2v_2^2\omega_2^2 + 12\omega_3\omega_1^2\omega_2^2 - 12\omega_3v_2^2\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 18\omega_3v_2^2\omega_1^2\omega_2^2 - 6v_2^3\omega_1^3\omega_2 + 12\omega_3v_2^3\omega_3^2 + 6\omega_3\omega_1^2v_2^2\omega_2 - 9\omega_3v_2^3\omega_1^3\omega_2 - 23\omega_3\omega_1^3\omega_2 + 42\omega_3\omega_2^2 + 12v_2^3\omega_2^2\omega_2^2 - 9\omega_3v_2^3\omega_1\omega_3^2 - 18\omega_3c_s^2\omega_1^2\omega_2 + 50\omega_3\omega_1^3v_2^2\omega_2^2 - 12\omega_3v_2^2\omega_1\omega_2^2 + 84\omega_3c_s^2\omega_1^3 - 6v_2^3\omega_1\omega_2^2 + 48\omega_3\omega_1^3v_2^2 + 42\omega_3c_s^2\omega_1^2\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 36\omega_3\omega_1^3 + 141\omega_3\omega_1v_2^2\omega_2^2 - 42\omega_3c_s^2\omega_1^2\omega_2^2 - 12\omega_3\omega_1\omega_2^2 + 36c_s^2\omega_1^2\omega_2^2 + 60\omega_3\omega_1v_2^2\omega_2^2 - 114\omega_3v_2^2\omega_1^2\omega_2^2 + 6\omega_1\omega_2^2 - 75\omega_3\omega_1^3v_2^2\omega_2^2 - 18c_s^2\omega_3^2\omega_2 + 12\omega_3v_2^3\omega_1^3 - 60\omega_3\omega_1\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{45} = & -18\omega_3^2\omega_1^3v_1^2\omega_2^2 - 18\omega_3\omega_1^2v_1^2\omega_3^2 - 126\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_3^2 - 90\omega_3^2v_2^2\omega_4\omega_1v_1^2\omega_2^2 + 54\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 + 24\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2 + 36\omega_3c_s^2\omega_4\omega_1^2\omega_3^2 - 18\omega_3^2c_s^2\omega_1^3\omega_3^2 - 8\omega_3c_s^2\omega_4\omega_1^3\omega_2 - \omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 + 54\omega_3^2c_s^2\omega_1^2v_1^2\omega_2^2 + 6\omega_3\omega_4\omega_1v_1^4\omega_3^2 + 6\omega_3^2c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 + 12\omega_3^2\omega_4\omega_1v_1^4\omega_2^2 - 72\omega_3^2c_s^4\omega_1^3\omega_3^2 - 12\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2 - 18\omega_4\omega_1^2v_1^2\omega_3^2 - 18\omega_3\omega_1^2v_1^2\omega_2^2 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_3^2 + 216\omega_3^2c_s^2v_2^2\omega_4\omega_1^3v_1^2\omega_2 - 90\omega_3^2v_2^2\omega_4\omega_1^3v_1^2\omega_2 - 56\omega_3c_s^2\omega_4\omega_1^2\omega_3^2 + 12\omega_3^2v_2^2\omega_4\omega_1^2\omega_2 - 90\omega_3c_s^2\omega_4\omega_1^2v_1^2\omega_3^2 - 144\omega_3^2v_2^2\omega_4\omega_1v_1^2\omega_2^2 - 12\omega_3\omega_4\omega_1^3v_1^4\omega_2 - 18\omega_4\omega_1^3v_1^4\omega_2^2 + 132\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 4\omega_3^2\omega_4\omega_1^3\omega_2 - 48\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 - 68\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 - 18\omega_3\omega_1^3v_1^4\omega_2^2 + 54\omega_3^2\omega_4\omega_1v_1^4\omega_2^2 - 54\omega_3c_s^2\omega_1^3v_1^2\omega_2^2 + 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 9\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^2 - 24\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 72\omega_3^2c_s^2\omega_2^2\omega_3^2 - 18\omega_3^2\omega_1^2v_1^2\omega_2^2 + 76\omega_3^2c_s^4\omega_4\omega_1\omega_3^2 + 36\omega_3\omega_4\omega_1^3v_1^4\omega_2^2 + 54\omega_3^2c_s^2\omega_1v_1^2\omega_2^2 + 54\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 54c_s^2\omega_4\omega_1^3v_2^2\omega_2^2 + 4\omega_3^2\omega_4\omega_1^3 + 24\omega_3^2c_s^2\omega_4\omega_1^2v_1^2\omega_2^2 + 36\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 + 32\omega_3^2c_s^2\omega_4\omega_1\omega_3^2 + 8\omega_3c_s^2\omega_4\omega_1\omega_3^2 - 6\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 9\omega_3^2\omega_4\omega_1^3v_1^4\omega_2^2 - 4\omega_3^2\omega_4\omega_1^2\omega_2^2 - 48\omega_3^2\omega_4v_1^4\omega_2^2 + 12\omega_3^2c_s^2v_2^2\omega_4\omega_1^3 - 90\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 + \omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 - 28\omega_3^2c_s^4\omega_4\omega_1\omega_2^2 + 28\omega_3^2c_s^2\omega_4\omega_2^2 + 12\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 - 12\omega_3^2v_2^2\omega_4\omega_1^3 - 42\omega_3^2\omega_4\omega_1^3v_1^2\omega_2^2 + 36\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 + 108\omega_3^2v_2^2\omega_4v_1^2\omega_2^2 + 48\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^2 + 150\omega_3^2c_s^2\omega_4\omega_1v_1^2\omega_2^2 - 36\omega_3c_s^4\omega_4\omega_1^2\omega_3^2 + \omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1^3\omega_2 + 12\omega_3\omega_4\omega_1^3v_1^2\omega_2 + 18\omega_4\omega_1^3v_1^2\omega_2^2 + 132\omega_3^2c_s^2\omega_4\omega_1^3v_1^2 - 54\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^2 - 36\omega_3^2v_2^2\omega_4\omega_1^2v_1^2\omega_2 + 18\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 16\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_3^2 + 18\omega_3^2\omega_1^2v_1^2\omega_2^2 + 28\omega_3^2c_s^2\omega_4\omega_1^2\omega_3^2 - 48\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^2 + 12\omega_3^2v_2^2\omega_4\omega_1\omega_2^2 - 24\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 + 18\omega_3\omega_4\omega_1v_1^2\omega_2^2 - 6\omega_3\omega_4\omega_1v_1^2\omega_2^2 - 84\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^2 + 56\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 + 12\omega_3^2\omega_4\omega_1^2v_1^4\omega_2 - 72\omega_3^2c_s^2\omega_1\omega_2^2 - 14\omega_3^2c_s^4\omega_4\omega_1^2\omega_3^2 + 36\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 + 12\omega_3^2v_2^2\omega_4\omega_1\omega_2^2 + 90\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2^2 - 14\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 + 18\omega_3^2\omega_1^2v_2^2\omega_2^2 + 18\omega_4\omega_1^3v_1^4\omega_2^2 - 54\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^2 + 66\omega_3^2\omega_4\omega_1^3v_1^2\omega_2 - 36\omega_3c_s^2\omega_4\omega_1^3v_1^2\omega_2 - 108\omega_3^2c_s^2\omega_4v_1^2\omega_2^2 + 54c_s^2\omega_4\omega_1^2v_2^2\omega_2^2 - 36\omega_3\omega_4\omega_1^2v_1^4\omega_2^2 + 2\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 - 9\omega_3^2\omega_4\omega_1^3v_2^2\omega_2^2 + 12\omega_3^2\omega_4v_1^2\omega_2^2 + 72\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 - 96\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1\omega_3^2 + 30\omega_3^2c_s^2\omega_4\omega_1^3v_1^2\omega_2^2 + 18\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 - 12\omega_3^2v_2^2\omega_4\omega_1^3 - 18\omega_3^2\omega_4\omega_1^3v_1^4\omega_2^2 - 18\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 - 20\omega_3^2c_s^2\omega_4\omega_1^3 + 180\omega_3^2v_2^2\omega_4\omega_1^2v_1^2\omega_2^2 - 18\omega_3c_s^2\omega_4\omega_1v_1^2\omega_2^2 + 60\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^2 - 3\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 - 8\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 6\omega_3\omega_4\omega_1^2v_1^4\omega_2^2 - 28\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^2 + 32\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 - 9\omega_3^2\omega_4\omega_1^2v_1^4\omega_2^2 - \omega_3^2v_2^4\omega_4\omega_1^2\omega_2^2 + 18\omega_3^2\omega_1v_1^4\omega_2^2 - 36\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 72\omega_3^2c_s^4\omega_1\omega_3^2 - 216\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^2 + 4\omega_3^2\omega_4\omega_2^2 - 36\omega_3\omega_4\omega_1^3v_1^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{46} = & 6\omega_3^3\omega_2 - 12v_2^3\omega_1^2\omega_2 - 18c_s^2\omega_1\omega_3^2 + 6\omega_1^2v_2^2\omega_2^2 - 6\omega_1^2v_2^2\omega_2 - 12\omega_1^2\omega_2^2 + 36c_s^2\omega_1\omega_2^2 - 4v_2^3\omega_2^2 + 6\omega_1^2v_2^2\omega_2^2 + 24\omega_1^2\omega_2 - 6\omega_1^2v_2^2\omega_2 + 4\omega_1^3v_2^2 - 3\omega_3^3v_2^2\omega_2 + 12v_2^3\omega_1\omega_2^2 + 4\omega_3^3v_2^2 - 72c_s^2\omega_1\omega_2^2 - 12\omega_1^3 + 2v_2^2\omega_2^2 + 36c_s^2\omega_1^3 - 3\omega_1^2v_2^2\omega_2^2 - 12\omega_1\omega_2^2 - 3\omega_1^3v_2^2\omega_2 + 36c_s^2\omega_1^2\omega_2^2 + 6\omega_1\omega_2^2 + 4v_2^3\omega_1^3 - 18c_s^2\omega_1^3\omega_2 - 3\omega_1v_2^3\omega_2^2 + 2v_2^2\omega_2^2
\end{aligned}$$

$$\begin{aligned}
C_{47} = & 72\omega_3^2\omega_4^2v_1^2\omega_2^2 - 108\omega_4^2\omega_1^3\omega_3^2 - 63\omega_3\omega_4^2\omega_1^3v_2^2\omega_3^2 - 108\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 + 432\omega_3c_s^2\omega_4\omega_1^2\omega_3^2 - 36\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 + 180\omega_3^2c_s^2\omega_4^2\omega_1\omega_3^2 - 108\omega_3v_2^2\omega_4\omega_1^3\omega_3^2 - 108\omega_3\omega_4^2\omega_1^3\omega_2^2 + 216\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 - 180\omega_3^2\omega_4\omega_1^2v_2^2\omega_3^2 - 72\omega_3^2\omega_4\omega_1^2\omega_2^2 + 20\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 + 24\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 36\omega_3^2\omega_4^2\omega_1\omega_3^2 - 336\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 + 48\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^2 - 432\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 + 63\omega_3\omega_4^2\omega_1^3\omega_2^2 + 36\omega_3v_2^2\omega_4\omega_1^3\omega_2^2 - 72\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 72\omega_3^2\omega_4\omega_1^2\omega_2^2 - 96\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 + 180\omega_3v_2^2\omega_4\omega_1^2\omega_2^2 - 216\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 + 48\omega_3\omega_4^2\omega_1^2\omega_2^2 + 108\omega_3^2\omega_4^2\omega_1v_1^2\omega_2^2 + 144\omega_3^2\omega_4^2\omega_1^3v_1^2 - 36\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^2 - 324\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 + 36\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 144\omega_3^2\omega_1^2\omega_2^2 - 24\omega_3\omega_4^2\omega_1^3v_2^2\omega_2 - 36\omega_4^2\omega_1^3v_2^2\omega_2^2 - 108\omega_3\omega_2^2\omega_1^2\omega_3^2 + 24\omega_3^2\omega_2^2\omega_1v_2^2\omega_2^2 + 12\omega_3v_2^2\omega_2^2\omega_1\omega_3^2 + 189\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 48\omega_3\omega_4^2\omega_1^3\omega_2^2 - 54\omega_3^2\omega_4^2\omega_1^3v_2^2\omega_2^2 - 72\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 63\omega_3^2\omega_4\omega_1^3\omega_2^2 + 54\omega_4^2\omega_1^3v_2^2\omega_2^2 + 48\omega_3^2\omega_4^2\omega_1^3v_2^2 + 36\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 216\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 24\omega_3\omega_2^2\omega_1v_2^2\omega_2^2 - 48\omega_3^2v_2^2\omega_2^2\omega_1\omega_2^2 + 60\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^2 - 20\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^2 - 24\omega_3v_2^2\omega_4\omega_1^3\omega_2^2 - 36\omega_3^2\omega_4\omega_1^3v_2^2\omega_2^2 - 36v_2^2\omega_4^2\omega_1^3\omega_2^2 + 12\omega_3\omega_4^2\omega_1\omega_3^2 - 36\omega_3v_2^2\omega_4^2\omega_1^3\omega_2^2 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 216\omega_3^2\omega_4^2\omega_1^2v_1^2\omega_2^2 + 48\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 72\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 - 120\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 60\omega_3\omega_4^2\omega_1^2v_2^2\omega_2^2 - 36\omega_3^2v_2^2\omega_4\omega_1\omega_2^2 -
\end{aligned}$$

$$\begin{aligned}
& 189\omega_3c_s^2\omega_4^3\omega_1^3\omega_2^3 + 96\omega_3^2\omega_4^2\omega_1^2\omega_2 + 54v_3^2\omega_2^3\omega_1^3\omega_2^3 - 144\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 + 12\omega_3v_3^2\omega_4^2\omega_1^2\omega_2^3 + 54\omega_3^2v_3^2\omega_1^3\omega_2^3 - 144\omega_3\omega_4\omega_1^2\omega_2^3 - 36\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + \\
& 63\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^3 - 432c_s^2\omega_1^2\omega_1^3\omega_2^3 + 36\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 - 36c_s^2v_3^2\omega_1^2\omega_1^3\omega_2 + 324\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 144\omega_3\omega_1^2v_2^2\omega_2^3 - 144\omega_3^2\omega_1^3\omega_2^3 - 144\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 + \\
& 324\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 - 72\omega_4\omega_1^2v_2^2\omega_2^3 - 216c_s^2\omega_4^2\omega_1^3\omega_2^3 + 108\omega_3^2\omega_1^2v_2^2\omega_2^3 - 36\omega_3^2\omega_4\omega_1^2\omega_2^3 + 72\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^3 - 108\omega_3^2\omega_4^2\omega_1^2\omega_2^3 - 72\omega_3\omega_4\omega_1^2\omega_2^3 + \\
& 180\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 108\omega_3^2\omega_4\omega_1^2\omega_4\omega_1\omega_2 + 24\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 + 216\omega_3^2\omega_4^2\omega_1^2v_2^2\omega_2^3 - 144\omega_3c_s^2\omega_1^2\omega_1^3\omega_2^3 + 324c_s^2\omega_4^2\omega_1^2\omega_2^3 - 48\omega_3^2v_3^2\omega_1^2\omega_1^3\omega_2 + \\
& 36\omega_3v_3^2\omega_4^2\omega_1^3\omega_2^3 - 72v_3^2\omega_4^2\omega_1^2\omega_2^3 - 360\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - 60\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3^2v_3^2\omega_1^2\omega_2^3 + 108\omega_3\omega_4\omega_1^2\omega_2^3 + 20\omega_3^2\omega_4^2\omega_1^2\omega_2^3 + 144\omega_3^2\omega_4^2\omega_1^3\omega_2
\end{aligned}$$

$$\begin{aligned}
49 = & -3\omega_3\omega_1^2v_1^2\omega_2^2 - 3\omega_3\omega_1^2v_1^2\omega_2^2 + \omega_3\omega_4\omega_1^2v_2^2\omega_2^2 - 18\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 18c_s^2\omega_4\omega_1^3\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^3\omega_2 - 4\omega_3^2\omega_4\omega_1^2v_1^2\omega_2 + 3\omega_4\omega_1^2v_1^2\omega_2^3 + 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 - \\
& 12\omega_3\omega_4\omega_1^2\omega_2^2 - 3\omega_3\omega_1^2v_1^2\omega_2^2 + 6\omega_3\omega_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - 36\omega_3^2\omega_4\omega_1^2\omega_2^3 - 3\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 + 6\omega_3^2\omega_4\omega_1^2v_1^2\omega_2 + 6\omega_3^2\omega_4\omega_1^2v_2^2\omega_2^2 + \\
& 6\omega_3^2\omega_4\omega_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 - 4\omega_3^2\omega_4\omega_1^2v_1^2\omega_2 - 3\omega_3\omega_4\omega_1^2v_2^2\omega_2^3 - 2\omega_3\omega_4\omega_1\omega_2^3 - 3\omega_3^2\omega_1^2v_1^2\omega_2^2 + \omega_3\omega_4\omega_1^2v_1^2\omega_2^2 + 18\omega_3^2c_s^2\omega_1^2\omega_2^3 - 3\omega_3^2\omega_1v_1^2\omega_2^3 - 12\omega_3^2\omega_4\omega_1^3 + \\
& 3\omega_4\omega_1^2v_1^2\omega_2^3 - 3\omega_3\omega_4\omega_1^2v_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 + 20\omega_3^2\omega_4\omega_1^2\omega_2^2 - 6\omega_3\omega_1^3\omega_2^2 + 18\omega_3^2c_s^2\omega_1^2\omega_2^2 + 20\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 + 18c_s^2\omega_4\omega_1^2\omega_2^3 + 12\omega_3^2\omega_3\omega_4\omega_1^3 + \\
& 6\omega_3^2\omega_4\omega_1^2v_1^2\omega_2^2 + 18\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 - 2\omega_3\omega_4\omega_1^2\omega_2^2 + 4\omega_3^2\omega_4\omega_1^2\omega_2^3 - 2\omega_3\omega_4\omega_1^3v_1^2\omega_2 - 3\omega_4\omega_1^3v_1^2\omega_2^2 - 6\omega_4\omega_1^2\omega_2^3 + 3\omega_3\omega_1^2v_1^2\omega_2^2 + 3\omega_3^2\omega_1^2v_1^2\omega_2^3 + 4\omega_3^2\omega_4\omega_1^3v_1^2 - \\
& 3\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 + 6\omega_3^2\omega_1^3\omega_2^2 + 4\omega_3\omega_4\omega_1^3\omega_2 + 6\omega_3\omega_4\omega_1^2\omega_2^3 + \omega_3\omega_4\omega_1v_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_1\omega_2^3 + 3\omega_3\omega_4\omega_1^2v_2^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1v_1^2\omega_2^2 + 36\omega_3^2\omega_3\omega_4\omega_1\omega_2^2 + \\
& 3\omega_3^2\omega_1v_1^2\omega_2^2 + 4\omega_3^2\omega_4\omega_1^2\omega_2^2 - 3\omega_3^2\omega_4\omega_1^3v_1^2\omega_2 - 2\omega_3\omega_4\omega_1^3v_2^2\omega_2^2 - 3\omega_4\omega_1^3v_2^2\omega_2^2 + 4\omega_3^2\omega_4v_1^2\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2^3 + 3\omega_3^2\omega_1^2v_2^2\omega_2^3 - 6\omega_3^2\omega_1^2\omega_2^2 + \\
& 3\omega_3\omega_1^2v_2^2\omega_2^2 + 6\omega_3^2\omega_4\omega_1\omega_2^3 - 3\omega_3^2\omega_4\omega_1v_2^2\omega_2^3 - 6\omega_3\omega_4\omega_1^2\omega_2^3 - 12\omega_3^2\omega_3\omega_4\omega_1^2 - 18\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 + 28\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 + 6\omega_3\omega_1^2\omega_2^2 + \omega_3\omega_4\omega_1v_2^2\omega_2^2 + \\
& 6\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 3\omega_3^2\omega_4\omega_1^2v_2^2\omega_2 - 12\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 - 4\omega_3^2\omega_4\omega_1v_2^2\omega_2^2 - 4\omega_3^2\omega_4\omega_2^3 + 3\omega_3\omega_4\omega_1^3v_1^2\omega_2 - 6\omega_3^2\omega_1^2\omega_2^2 + 3\omega_3^2\omega_1^2v_2^2\omega_2^2 - 4\omega_3^2\omega_4\omega_1\omega_2^2
\end{aligned}$$

$$C_{51} = 6\omega_1^3\omega_2 - 66\omega_3c_s^*\omega_2^3 - 18c_s^*\omega_1\omega_2^3 + 6\omega_3\omega_1^2v_2^2\omega_2 + 48\omega_3\omega_1^3\omega_2 + 23\omega_3\omega_1^2\omega_2^3 + 108\omega_3c_s^*\omega_1\omega_2^3 - 12\omega_1^4\omega_2^2 + 12\omega_3\omega_1^2\omega_2^2 - 12\omega_3v_2^3\omega_1^2\omega_2 + 6\omega_3\omega_1^2\omega_2 + 18\omega_3v_2^3\omega_1^2\omega_2^2 - 50\omega_3\omega_1^2v_2^2\omega_2^3 - 6v_2^3\omega_1^3\omega_2 + 12\omega_3v_2^3\omega_2^3 - 66\omega_3\omega_1^2v_2^2\omega_2^3 - 9\omega_3v_2^3\omega_1^3\omega_2 - 23\omega_3\omega_1^3\omega_2^2 + 42\omega_3\omega_2^3 + 12v_2^3\omega_1^2\omega_2^2 + 141\omega_3\omega_1v_2^2\omega_2^3 - 9\omega_3v_2^3\omega_1\omega_2^3 + 48\omega_3\omega_1^3v_2^2 - 18\omega_3c_s^*\omega_1^2\omega_2 - 75\omega_3\omega_1^3v_2^2\omega_2 - 12\omega_3v_2^3\omega_1\omega_2^2 + 84\omega_3c_s^*\omega_1^3 + 60\omega_3\omega_1v_2^2\omega_2^2 - 114\omega_3v_2^2\omega_2^3 - 6v_2^3\omega_1\omega_2^3 + 42\omega_3c_s^*\omega_1^3\omega_2^2 - 108\omega_3c_s^*\omega_1^3\omega_2 - 36\omega_3\omega_1^3 - 42\omega_3c_s^*\omega_1^2\omega_2^3 + 50\omega_3\omega_1^3v_2^2\omega_2^2 - 12\omega_3\omega_1\omega_2^3 + 36c_s^*\omega_1^2\omega_2^2 + 6\omega_1\omega_2^3 - 18c_s^*\omega_1^3\omega_2 + 12\omega_3v_2^3\omega_1^3 - 60\omega_3\omega_1\omega_2^3$$

$$\begin{aligned}
& 36\omega_3\omega_4\omega_1^3v_2^2\omega_2^2 - 14\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 12\omega_3^2v_3^2\omega_4\omega_1\omega_2^2 - 14\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 + 132\omega_3^2c_s^2\omega_4\omega_1^3v_2^2 - 48\omega_3^2\omega_4\omega_1^3v_2^2 - 9\omega_3^2\omega_4\omega_1^3v_4^2\omega_2^3 + 18\omega_3^2\omega_1v_4^2\omega_2^3 + \\
& 12\omega_3^2\omega_4\omega_1^3v_2^2\omega_2 + 18\omega_4\omega_1^3v_2^2\omega_2^3 + 2\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 150\omega_3^2c_s^2\omega_4\omega_1v_2^2\omega_2^3 + 108\omega_3^2v_3^2\omega_4v_2^2\omega_2^3 + 18\omega_3^2\omega_1v_2^2\omega_2^3 + 18\omega_3\omega_1^3v_2^2\omega_2^2 - 96\omega_3^2c_s^2v_3^2\omega_4\omega_2^3 - \\
& 4\omega_3^2\omega_4\omega_1\omega_2^3 - 24\omega_3^2\omega_4\omega_1v_2^2\omega_2^3 + 18\omega_3^2c_s^2\omega_4\omega_2^3\omega_2^3 - 12\omega_3^2v_3^2\omega_4\omega_2^3 - 36\omega_3^2v_3^2\omega_4\omega_1^3v_2^2\omega_2 - 18\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 20\omega_3^2c_s^2\omega_4\omega_1^3 - 54\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^3 + \\
& 12\omega_3^2c_s^2\omega_1^3v_4^2\omega_2 + 60\omega_3^2c_s^2v_3^2\omega_4\omega_1\omega_2^3 - 6\omega_3\omega_4\omega_1v_2^2\omega_2^3 - 12\omega_3^2c_s^2\omega_4\omega_1v_2^2\omega_2^3 + 18\omega_3^2v_3^2\omega_4\omega_2^3 + 18\omega_3^2\omega_1v_4^2\omega_2^3 + 54\omega_3c_s^2\omega_1^3v_2^2\omega_2^3 - \\
& 174\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 - 8\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 28\omega_3^2c_s^2\omega_4\omega_1^3\omega_2 + 66\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2 + 32\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 54\omega_3^2c_s^2\omega_1^3v_2^2\omega_2 - v_3^2v_3\omega_4\omega_1\omega_2^3 - 36\omega_3c_s^2\omega_4\omega_1^3\omega_2^3 + \\
& 72\omega_3^2c_s^2\omega_1\omega_2^3 + 72\omega_3^2v_3^2\omega_4\omega_1^3v_2^2 - 216\omega_3^2c_s^2v_3^2\omega_2^3 + 90\omega_3^2c_s^2\omega_4\omega_1^3v_2^2\omega_2^3 + 36\omega_3^2\omega_4\omega_1v_2^2\omega_2^3 + 4\omega_3^2\omega_4\omega_2^3 + 18\omega_3^2\omega_1^3v_2^2\omega_2^3 + 18\omega_4\omega_1^3v_2^2\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2^3
\end{aligned}$$

$C_{54} = 48\omega_3c_4^2v_1^2w_2^3 - 540\omega_3c_5^2v_3^2w_4w_1^2w_2^3 - 48\omega_3^2c_4^2w_1v_1^2w_2^3 - 24\omega_3v_3^4w_4^2w_1^3w_2 - 2\omega_3^2c_4^4w_4^2w_1^3w_2^2 + 216\omega_3v_3^4w_4^2w_1^2w_2^3 + 144\omega_3^2v_3^2w_4^2w_1^2v_1^2w_2 + 24\omega_3^2c_4^2w_4^2v_1^2w_2^3 - 36\omega_3^2v_3^2w_4w_1^3w_2^2 - 36v_3^4w_2^2w_1^3w_2^2 + 48\omega_3^2c_5^2w_4^2w_1w_2^3 + 108\omega_3^2c_5^2v_3^2w_4w_1^3w_2^2 - 108\omega_3v_3^2w_4w_1^3w_2^3 - 144\omega_3^2v_3^2w_4^2w_1^2w_2^2 + 18\omega_3c_4^2w_2^2w_1^3w_2^3 - 72\omega_3^2v_3^4w_4w_1w_2^3 - 12\omega_3^2c_5^2w_4^2w_1v_1^2w_2^3 - 16\omega_3^2w_2^2w_1^3w_2^3 + 144\omega_3^2v_3^4w_4^2w_1^3v_1^2 + 16\omega_3^2w_2^2w_1^3w_2^3 - 60\omega_3v_3^4w_2^2w_1^2w_2^3 + 24\omega_3^2w_4^2w_1^3v_1^2w_2 - 16\omega_3c_5^2w_4^2w_1w_2^3 + 54v_3^4w_4^2w_1^3w_2^3 + 117\omega_3^2v_3^2w_4w_1^3w_2^3 - 56\omega_3^2c_5^2w_2^2w_1^2w_2 - 216c_4^2v_3^2w_2^2w_1^3w_2^3 - 6\omega_3^2c_4^4w_2^2w_1^3w_2^3 + 72\omega_3^2c_5^2v_3^2w_4^2w_1w_2^3 - 72\omega_3^2c_4^2w_4^2w_1^2w_2^3 - 48\omega_3^2w_2^2w_4w_1^3v_1^2w_2^2 + 16\omega_3^2v_3^2w_4w_1^3v_1^2w_2^2 + 16\omega_3^2v_3^2w_4w_1^3v_1^2w_2^2 + 48\omega_3^2c_4^2w_4^2w_1v_1^2w_2^2 + 432\omega_3^2c_5^2v_3^2w_4^2w_1^3 - 36\omega_3^2c_4^4w_2^2w_1^3w_2^3 - 48\omega_3^2v_3^2w_4^2w_1^3w_2^3 - 108\omega_3^2v_3^2w_4^2w_1^2w_2^2 + 72\omega_3^2c_5^2w_4^2w_1^2w_2^3 - 12\omega_3^2c_4^2w_2^2v_1^2w_2^3 + 36\omega_3^2v_3^2w_4^2w_1^3w_2^3 + 36\omega_3^2c_5^2w_4^2w_1^3w_2^3 - 32\omega_3^2c_4^2w_2^2w_1^2w_2^3 - 297\omega_3^2c_5^2v_3^2w_4^2w_1^2w_2^3 + 40\omega_3^2v_3^2w_4^2w_1^2w_2^3 + 38\omega_3^2v_3^4w_2^2w_1^3w_2^3 + 16\omega_3^2c_4^4w_2^2w_1^3w_2^3 + 180\omega_3^2v_3^2w_4w_1^3w_2^3 - 108\omega_3^2c_5^2v_3^2w_4w_1^2w_2^3 - 432\omega_3^2v_3^2w_4^2v_1^2w_2^3 - 852\omega_3^2c_5^2v_3^2w_2^2w_1^3w_2^3 - 12\omega_3^2c_4^4w_2^2w_1^3v_1^2w_2^3 - 36\omega_3^2c_4^4w_2^2w_1^3w_2^3 - 144\omega_3^2v_3^2w_4^2w_1^2v_1^2w_2^3 + 20\omega_3^2c_4^4w_2^2w_1^3w_2^3 - 6\omega_3^2w_4^2w_1^3v_1^2w_2^3 - 24\omega_3^2w_4^2w_1^3v_1^2 + 96\omega_3^2v_3^2w_4^2w_1w_2^3 - 108c_5^2v_3^2w_4^2w_1^2w_2^3 + 36\omega_3^2v_3^2w_4^2w_1^2w_2^3 - 117\omega_3v_3^2w_4^2w_1^3w_2^3 + 72\omega_3^2c_4^4w_4w_1w_2^3 + 324\omega_3^2c_5^2v_3^2w_4w_1^3w_2^3 + 48\omega_3^2c_4^2w_4^2w_1^3v_1^2w_2^3 + 24\omega_3^2c_5^2w_2^2w_1^3v_1^2 + 24\omega_3v_3^2w_4^2w_1w_2^3 - 18\omega_3^2c_5^2w_4w_1^3w_2^3 + 96\omega_3^2v_3^4w_2^2w_1^2w_2 + 336\omega_3^2c_5^2v_3^2w_4w_1^2w_2^3 + 40\omega_3^2c_4^4w_4^2w_1^2w_2^3 + 24\omega_3^2v_3^4w_2^2w_1^3w_2^3 + 648\omega_3^2c_5^2v_3^2w_4w_1^2w_2^3 - 108\omega_3^2c_5^2v_3^2w_4w_1^3w_2^3 - 72v_3^4w_2^2w_1^3w_2^3 - 28\omega_3^2c_4^4w_2^2w_1^3w_2^3 - 288\omega_3^2v_3^2w_4w_1^3w_2^3 + 108\omega_3^2v_3^2w_4w_1^3w_2^3 + 32\omega_3^2c_4^4w_2^2w_1^3w_2^3 - 288\omega_3^2v_3^2w_4^2w_1^2v_1^2w_2^3 - 96\omega_3^2c_5^2w_4^2w_1^2v_1^2w_2^3 + 86\omega_3^2c_4^4w_4^2w_1^2w_2^3 + 162c_5^2v_3^2w_2^2w_1^3w_2^3 + 192\omega_3^2v_3^4w_2^2w_1^3w_2^3 - 144\omega_3^2v_3^2w_2^2w_1^3w_2^3 + 24\omega_3v_3^2w_2^2w_1^3w_2^3 + 36\omega_3^2v_3^4w_4w_1^3w_2^3 + 36\omega_3^2v_3^4w_4^2w_1^3w_2^3 - 216\omega_3v_3^2w_2^2w_1^3w_2^3 - 492\omega_3^2c_5^2v_3^2w_2^2w_1^3w_2^3 - 96\omega_3^2c_5^2w_4^2w_1^2v_1^2w_2 + 2\omega_3^2w_4^2w_1^2w_2^3 + 24\omega_3^2w_4^2w_1^2v_1^2w_2 - 297\omega_3^2c_5^2v_3^2w_4^2w_1^2w_2^3 + 264\omega_3^2c_5^2v_3^2w_4^2w_1^3 - 96\omega_3^2v_3^2w_4^2w_1^3 + 240\omega_3^2v_3^2w_2^2w_1^2w_2^3 + 108\omega_3v_3^2w_4w_1^3w_2^3 - 172\omega_3^2c_4^4w_4^2w_1w_2^3 + 8\omega_3^2c_5^2w_4^2w_1^3w_2^3 + 576\omega_3^2v_3^2w_4^2w_1v_1^2w_2^3 + 48\omega_3^2c_4^2w_4^2w_1^2v_1^2w_2^3 + 72\omega_3^2v_3^2w_4w_1w_2^3 - 18\omega_3^2c_4^4w_2^2w_1^3w_2^3 + 162\omega_3^2c_5^2v_3^2w_1^3w_2^3 - 8\omega_3^2w_4^2w_1^2w_2^3 - 54\omega_3^2w_4^2w_1^3w_2^3 + 64\omega_3^2c_5^2w_4^2w_1^2w_2^3 - 117\omega_3^2v_3^2w_4w_1^3v_1^2w_2^3 + 16\omega_3^2c_4^4w_4^2w_1^2w_2^3 + 174\omega_3^2c_5^2v_3^2w_4^2w_1^2w_2^3 + 60\omega_3v_3^2w_4^2w_1^2w_2^3 - 54\omega_3^2v_3^2w_4^2w_1^2w_2^3 - 492\omega_3^2c_5^2v_3^2w_2^2w_1^2w_2 + 72\omega_3^2c_4^4w_2^2w_1^2v_1^2w_2^3 + 144\omega_3^2v_3^2w_4^2w_1^2v_1^2w_2^3 - 72\omega_3^2c_5^2w_4w_1^2w_2^3 + 204\omega_3^2v_3^2w_4^2w_1^2w_2^3 + 36\omega_3^2c_4^4w_4^2w_1^2w_2^3 - 108\omega_3^2v_3^2w_4^2w_1^3w_2^3 + 8\omega_3^2v_3^4w_4^2w_1^2w_2^3 + 16\omega_3^2c_4^4w_4^2w_1^2w_2^3 - 36\omega_3v_3^4w_4w_1^3w_2^3 - 288\omega_3^2v_3^2w_2^2w_1^3v_1^2w_2^3 + 288\omega_3^2c_5^2v_3^2w_4^2w_1^3w_2^3 + 8\omega_3^2w_4^2w_1^3 - 180\omega_3^2v_3^2w_4w_1^3w_2^3 - 16\omega_3^2c_4^4w_2^2w_1^3w_2^3 - 86\omega_3^2v_3^2w_2^2w_1^3w_2^3 + 36\omega_3^2c_5^2w_4^2w_1^2w_2^3 + 6\omega_3^2w_2^2w_1^3v_1^2w_2^3 - 72\omega_3^2c_5^2v_3^2w_2^2w_1^3w_2^3 + 144\omega_3^2v_3^2w_4^2w_1^3v_1^2w_2^3 + 468\omega_3^2c_5^2v_3^2w_2^2w_1^3w_2^3 + 12\omega_3^2c_4^4w_2^2w_1^3v_1^2w_2^3 - 8\omega_3^2w_4^2w_1^2w_2^3 - 288\omega_3^2v_3$

$$\begin{aligned}
C_{56} = & -12c_s^2\omega_1^2v_2^2\omega_2^2 - 4\omega_3c_s^2\omega_1^3v_2^2\omega_2 + 24\omega_3^2v_2^3\omega_1^3v_2^2\omega_2^2 + 40\omega_3^2c_s^2\omega_1^2\omega_2 - 60\omega_3^2v_2^3\omega_1\omega_2^3 + 22\omega_3^2c_s^2\omega_1v_2^2\omega_2^3 - 6\omega_3^2c_s^4\omega_1^2\omega_2^3 - 84\omega_3^2c_s^4\omega_1^3\omega_2 + \\
& 8\omega_3^2\omega_1\omega_2^2 - 8\omega_3^2\omega_1v_2^3\omega_2^3 + 108\omega_3^2c_s^2v_2^3\omega_1\omega_2^3 - 5\omega_3^2c_s^2\omega_1^2\omega_2^2 + 8\omega_3^2c_s^2\omega_1v_2^2\omega_2^3 - 8\omega_3^2c_s^2\omega_1\omega_2^3 + 4\omega_3^2\omega_1^3 - 8\omega_3^2\omega_1v_2^2\omega_2^3 - 216\omega_3^2c_s^2v_2^3\omega_1\omega_2^3 - \\
& 20\omega_3^2c_s^2\omega_1^3v_2^2\omega_2 + 8\omega_3^2\omega_1\omega_2^3 + 4\omega_3^2\omega_1^2v_2^2\omega_2 + 48\omega_3^2v_2^3\omega_2^3 - 48\omega_3^2v_2^3\omega_1^3 + 48\omega_3^2v_2^3\omega_1\omega_2^2 + 42\omega_3^2c_s^4\omega_1^2\omega_2^2 + 8\omega_3^2c_s^4\omega_1v_2^2\omega_2^3 - 72\omega_3^2v_2^3v_2^3\omega_2^3 + \\
& 2\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 - \omega_3^2\omega_1^3v_2^2\omega_2^2 - 36\omega_3^2c_s^4\omega_1^2\omega_2 + 96\omega_3^2v_2^3\omega_1v_2^3\omega_2^2 + 56\omega_3^2c_s^2\omega_1^3\omega_2 - 36\omega_3^2v_2^3\omega_1\omega_2^3 + 5\omega_3^2c_s^2\omega_1^2\omega_2^3 - 4\omega_3^2\omega_1^3\omega_2^3 + 8\omega_3^2v_2^3\omega_2^3 + \\
& 6\omega_3^2c_s^4\omega_1^2\omega_2^2 - 52\omega_3^2c_s^4\omega_1^3\omega_2 - 36\omega_3^2c_s^4\omega_2^3 + 24\omega_3^2c_s^2\omega_1\omega_2^3 + 48\omega_3^2v_2^3v_2^3\omega_2^2 + 18\omega_3^2c_s^2v_2^3\omega_1^2\omega_2^2 + 18\omega_3^2c_s^2v_2^3\omega_1\omega_2^3 - 72\omega_3^2v_2^3\omega_1^2v_2^2 - 24\omega_3^2v_2^3\omega_1^2v_2^2 - 34\omega_3^2c_s^2\omega_1^2\omega_2^2 + \\
& 24\omega_3^2v_2^3\omega_1v_2^2\omega_2^2 - 4\omega_3^2c_s^2\omega_1^2v_2^2\omega_2 - 24\omega_3^2v_2^3\omega_1^2\omega_2^2 + 12c_s^2\omega_1^3\omega_2^3 - 8\omega_3^2\omega_2^3 - 54\omega_3^2c_s^4\omega_1^2\omega_2^3 + 4\omega_3^2\omega_1^2v_2^2\omega_2 + 72\omega_3^2c_s^2v_2^3\omega_1^3\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2 - \\
& 12\omega_3^2c_s^4\omega_1^3\omega_2 + 12c_s^2\omega_1^2v_2^2\omega_2^3 + 24\omega_3^2v_2^4\omega_1^3 + 24\omega_3^2v_2^3\omega_2^3 - 8\omega_3^2c_s^2\omega_1\omega_2^2 - 24\omega_3^2v_2^3\omega_1^2v_2^2\omega_2^3 + 72\omega_3^2v_2^4\omega_1^2\omega_2^2 - 12\omega_3^2c_s^4\omega_1^2\omega_2^3 + \omega_3^2\omega_1^3\omega_2^2 - \\
& 24\omega_3^2v_2^3\omega_1^2\omega_2 + 36c_s^4\omega_1^2\omega_2^3 - 48\omega_3^2v_2^3v_2^2v_2^2\omega_2^2 - 22\omega_3^2c_s^2\omega_1\omega_2^3 - 36\omega_3^2v_2^4\omega_1^3\omega_2 - 18\omega_3^2c_s^2\omega_1^2\omega_2^3 + 216\omega_3^2c_s^2v_2^3\omega_1^3 - 4\omega_3^2c_s^2\omega_1^3v_2^2\omega_2^2 + \\
& 24\omega_3^2v_2^3\omega_1^2v_2^2\omega_2 - 36c_s^4\omega_1^3\omega_2^2 - 4\omega_3^2c_s^2\omega_1^2\omega_2 + 20c_s^2\omega_1^3\omega_2^3 + 72\omega_3^2c_s^4\omega_1^2\omega_2^3 + 18\omega_3^2c_s^2\omega_1^2\omega_2^3 + \omega_3^2\omega_1^2v_2^2\omega_2^3 - \omega_3^2\omega_1^2\omega_2^3 - 4\omega_3^2\omega_1^3\omega_2 + 216\omega_3^2c_s^2v_2^3\omega_1^2\omega_2^2 - \\
& 24\omega_3^2v_2^3\omega_1^2\omega_2^2 + 16\omega_3^2c_s^2v_2^3\omega_2^3 - 2\omega_3^2c_s^2\omega_1^2v_2^2\omega_2^3 + 4\omega_3^2c_s^2\omega_1^2\omega_2^3 - 20\omega_3^2c_s^2v_2^3\omega_2^3 - 18\omega_3^2c_s^2v_2^3\omega_1^2v_2^2\omega_2^2 - 2\omega_3^2c_s^2\omega_1^2\omega_2^2 + 84\omega_3^2v_2^3\omega_1^3\omega_2 - 12c_s^2\omega_1^2\omega_2^3 + \\
& 42\omega_3^2c_s^4\omega_1\omega_2^3 + 24\omega_3^2v_2^3\omega_1^2\omega_2^3 - 72\omega_3^2c_s^2v_2^3\omega_1^2\omega_2^3 + 54\omega_3^2c_s^4\omega_1^2\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2^2 + 4\omega_3^2\omega_1^2v_2^2\omega_2^3 - 324\omega_3^2c_s^2v_2^3\omega_1^3\omega_2^2
\end{aligned}$$

$$\begin{aligned}
& C_{D_y^3 D_z v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_x^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{D_x D_y D_z^2 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{D_x D_y D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_y^2 D_z^2 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{D_x D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + \\
& C_{D_x D_z^3 v_1}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + C_{D_y D_z^3 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_2}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + \\
& C_{D_z^4 \rho}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{D_z^4 v_3}^{(0)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

coefficient $C_{D_x^4 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^4}$:

$$C_{D_x^4 \rho}^{(0), \text{SRT}} = (-6v_1^2 - 12c_s^2 v_1^2 \omega + 3v_1^2 \omega + 2c_s^4 - c_s^4 \omega - 3v_1^4 \omega + 6v_1^4 + c_s^2 \omega - 2c_s^2 + 24c_s^2 v_1^2) \frac{1}{24\omega}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT1}} = (-6v_1^2 - 12c_s^2 v_1^2 \omega_9 + 3v_1^2 \omega_9 + 2c_s^4 - c_s^4 \omega_9 - 3v_1^4 \omega_9 + 6v_1^4 + c_s^2 \omega_9 - 2c_s^2 + 24c_s^2 v_1^2) \frac{1}{24\omega_9}$$

$$C_{D_x^4 \rho}^{(0), \text{MRT2}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM1}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CLBM2}} = C_{D_x^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(0), \text{CuLBM1}} = (-6v_1^2 - 12c_s^2 v_1^2 \omega_4 + 3v_1^2 \omega_4 + 2c_s^4 - c_s^4 \omega_4 - 3v_1^4 \omega_4 + c_s^2 \omega_4 + 6v_1^4 - 2c_s^2 + 24c_s^2 v_1^2) \frac{1}{24\omega_4}$$

$$\begin{aligned}
C_{D_x^4 \rho}^{(0), \text{CuLBM2}} &= (-3c_s^4 \omega_1 \omega_2 - 6v_1^2 \omega_1 + 4c_s^4 \omega_2 + 24c_s^2 v_1^2 \omega_1 - 12v_1^2 \omega_2 + 48c_s^2 v_1^2 \omega_2 + 2c_s^4 \omega_1 + 3c_s^2 \omega_1 \omega_2 + 6v_1^4 \omega_1 - 4c_s^2 \omega_2 - 9v_1^4 \omega_1 \omega_2 - \\
& 36c_s^2 v_1^2 \omega_1 \omega_2 + 12v_1^4 \omega_2 - 2c_s^2 \omega_1 + 9v_1^2 \omega_1 \omega_2) \frac{1}{72\omega_1 \omega_2}
\end{aligned}$$

coefficient $C_{D_x^4 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^4}$:

$$C_{D_x^4 v_1}^{(0), \text{SRT}} = (-4 + 10v_1^2 - 5v_1^2 \omega + 2\omega - 3c_s^2 \omega + 6c_s^2) \frac{v_1 \rho}{12\omega}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT1}} = (-4 + 10v_1^2 - 5v_1^2 \omega_9 - 3c_s^2 \omega_9 + 6c_s^2 + 2\omega_9) \frac{v_1 \rho}{12\omega_9}$$

$$C_{D_x^4 v_1}^{(0), \text{MRT2}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM1}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CLBM2}} = C_{D_x^4 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(0), \text{CuLBM1}} = (-4 + 10v_1^2 - 5v_1^2 \omega_4 + 2\omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_1 \rho}{12\omega_4}$$

$$C_{D_x^4 v_1}^{(0), \text{CuLBM2}} = (10v_1^2 \omega_1 + 20v_1^2 \omega_2 + 6\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 12c_s^2 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1 - 15v_1^2 \omega_1 \omega_2) \frac{v_1 \rho}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_y \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_y \rho}^{(0), \text{MRT1}} = (v_1^2 \omega_{12} - v_1^2 \omega_9 - 3c_s^2 \omega_9 + \omega_9 - \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_2 v_1}{4\omega_9 \omega_{12}}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{MRT2}} = C_{D_x^3 D_y \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_y \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y \rho}^{(0), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_2 v_1}{12 \omega_1 \omega_2}$$

$$\text{coefficient } C_{\text{D}_x^3 \text{D}_y v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} :$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{SRT}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{MRT1}} = (3v_1^2 \omega_{12} - 3v_1^2 \omega_9 - c_s^2 \omega_9 + \omega_9 - \omega_{12} + c_s^2 \omega_{12}) \frac{v_2 \rho}{4 \omega_9 \omega_{12}}$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{MRT2}} = C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{\text{D}_x^3 \text{D}_y v_1}^{(0), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_2 \rho}{36 \omega_1 \omega_2}$$

$$\text{coefficient } C_{\text{D}_x^3 \text{D}_y v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} :$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{SRT}} = (2 - 2v_1^2 + v_1^2 \omega - \omega + 3c_s^2 \omega - 6c_s^2) \frac{v_1 \rho}{12 \omega}$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{MRT1}} = (3c_s^2 \omega_5 \omega_{12} + 3\omega_5 \omega_9 - 6c_s^2 \omega_9 \omega_{12} - \omega_5 \omega_{12} - 3c_s^2 \omega_5 \omega_9 + v_1^2 \omega_5 \omega_{12} + v_1^2 \omega_5 \omega_9 \omega_{12} - 3v_1^2 \omega_5 \omega_9 - \omega_5 \omega_9 \omega_{12} + 3c_s^2 \omega_5 \omega_9 \omega_{12}) \frac{v_1 \rho}{12 \omega_5 \omega_9 \omega_{12}}$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{MRT2}} = C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{CLBM1}} = (-\omega_9 \omega_{12} + 3c_s^2 \omega_9 \omega_{12} + v_1^2 \omega_{12} - 3v_1^2 \omega_9 + v_1^2 \omega_9 \omega_{12} - 9c_s^2 \omega_9 + 3\omega_9 - \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_1 \rho}{12 \omega_9 \omega_{12}}$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{CLBM2}} = C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{CLBM1}}$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{CuLBM1}} = (-3v_1^2 \omega_4 + v_1^2 \omega_9 - \omega_4 \omega_9 + 3c_s^2 \omega_4 \omega_9 + 3\omega_4 - 9c_s^2 \omega_4 + 3c_s^2 \omega_9 - \omega_9 + v_1^2 \omega_4 \omega_9) \frac{v_1 \rho}{12 \omega_4 \omega_9}$$

$$C_{\text{D}_x^3 \text{D}_y v_2}^{(0), \text{CuLBM2}} = (-18\omega_3 v_2^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 + 18\omega_3 v_2^2 \omega_4 \omega_1 - 9v_1^2 \omega_4 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 9\omega_3 v_1^2 \omega_1 \omega_2 + 2\omega_3 v_1^2 \omega_4 \omega_1 + 6\omega_3 v_1^2 \omega_4 \omega_1 \omega_2 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 4\omega_3 v_1^2 \omega_4 \omega_2 + 9\omega_3 \omega_1 \omega_2) \frac{v_1 \rho}{72 \omega_3 \omega_4 \omega_1 \omega_2}$$

$$\text{coefficient } C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} :$$

$$C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^4}{6 \omega}$$

$$C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^4}{6 \omega_5}$$

$$C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{MRT2}} = C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{CLBM1}} = C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{CLBM2}} = C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{MRT1}}$$

$$C_{\text{D}_x^2 \text{D}_y^2 \rho}^{(0), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^4}{6 \omega_1}$$

$$C_{D_x^2 D_y^2 \rho}^{(0), \text{CuLBM2}} = (3v_1^2 \omega_1 - 3v_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 2\omega_1 - 14c_s^2 \omega_2 - 3v_2^2 \omega_2 + 2\omega_2 + 3v_2^2 \omega_1 + 2c_s^2 \omega_1) \frac{c_s^2}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y^2 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}} = (\omega_5 - \omega_{12}) \frac{c_s^2 v_1 \rho}{2\omega_5 \omega_{12}}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT2}} = C_{D_x^2 D_y^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(0), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1 \rho}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y^2 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}} = (\omega_5 - \omega_{15}) \frac{c_s^2 v_2 \rho}{2\omega_5 \omega_{15}}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT2}} = C_{D_x^2 D_y^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(0), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_2 \rho}{36\omega_1 \omega_2}$$

coefficient $C_{D_x D_y^3 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT1}} = (\omega_{10} - 3c_s^2 \omega_{10} - v_2^2 \omega_{10} + 3c_s^2 \omega_{15} - \omega_{15} + v_2^2 \omega_{15}) \frac{v_2 v_1}{4\omega_{10} \omega_{15}}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{MRT2}} = C_{D_x D_y^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^3 \rho}^{(0), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_2 v_1}{12\omega_1 \omega_2}$$

coefficient $C_{D_x D_y^3 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 v_1}^{(0), \text{SRT}} = (2 - \omega + v_2^2 \omega + 3c_s^2 \omega - 6c_s^2 - 2v_2^2) \frac{v_2 \rho}{12\omega}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT1}} = (-3v_2^2 \omega_{10} \omega_5 + 3c_s^2 \omega_5 \omega_{15} - \omega_5 \omega_{15} - 3c_s^2 \omega_{10} \omega_5 - \omega_{10} \omega_5 \omega_{15} + 3\omega_{10} \omega_5 + v_2^2 \omega_5 \omega_{15} + 3c_s^2 \omega_{10} \omega_5 \omega_{15} + v_2^2 \omega_{10} \omega_5 \omega_{15} - 6c_s^2 \omega_{10} \omega_{15}) \frac{v_2 \rho}{12\omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{MRT2}} = C_{D_x D_y^3 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM1}} = (3\omega_{10} - 9c_s^2 \omega_{10} - 3v_2^2 \omega_{10} + v_2^2 \omega_{10} \omega_{15} + 3c_s^2 \omega_{15} - \omega_{15} - \omega_{10} \omega_{15} + 3c_s^2 \omega_{10} \omega_{15} + v_2^2 \omega_{15}) \frac{v_2 \rho}{12\omega_{10} \omega_{15}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CLBM2}} = C_{D_x D_y^3 v_1}^{(0), \text{CLBM1}}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CuLBM1}} = (-\omega_7 \omega_5 + 3c_s^2 \omega_7 \omega_5 - 3v_2^2 \omega_5 + v_2^2 \omega_7 \omega_5 - \omega_7 - 9c_s^2 \omega_5 + v_2^2 \omega_7 + 3c_s^2 \omega_7 + 3\omega_5) \frac{v_2 \rho}{12\omega_7 \omega_5}$$

$$C_{D_x D_y^3 v_1}^{(0), \text{CuLBM2}} = (4\omega_3 v_2^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 v_2^2 \omega_4 \omega_1 + 6\omega_3 v_2^2 \omega_4 \omega_1 \omega_2 - 9\omega_3 v_2^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 9v_2^2 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 18\omega_3 v_1^2 \omega_4 \omega_1 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 - 18\omega_3 v_1^2 \omega_4 \omega_2 + 9\omega_3 \omega_1 \omega_2) \frac{v_2 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x D_y^3 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1 \partial x_2^3}$:

$$C_{D_x D_y^3 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT1}} = (\omega_{10} - c_s^2 \omega_{10} - 3v_2^2 \omega_{10} + c_s^2 \omega_{15} - \omega_{15} + 3v_2^2 \omega_{15}) \frac{v_1 \rho}{4\omega_{10} \omega_{15}}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{MRT2}} = C_{D_x D_y^3 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^3 v_2}^{(0), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1 \rho}{36\omega_1 \omega_2}$$

coefficient $C_{D_y^4 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_2^4}$:

$$C_{D_y^4 \rho}^{(0), \text{SRT}} = (24c_s^2 v_2^2 + 6v_2^4 + 2c_s^4 - c_s^4 \omega - 3v_2^4 \omega + 3v_2^2 \omega - 12c_s^2 v_2^2 \omega + c_s^2 \omega - 2c_s^2 - 6v_2^2) \frac{1}{24\omega}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT1}} = (24c_s^2 v_2^2 - 3v_2^4 \omega_{10} - c_s^4 \omega_{10} + 6v_2^4 + 2c_s^4 + c_s^2 \omega_{10} + 3v_2^2 \omega_{10} - 12c_s^2 v_2^2 \omega_{10} - 2c_s^2 - 6v_2^2) \frac{1}{24\omega_{10}}$$

$$C_{D_y^4 \rho}^{(0), \text{MRT2}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CLBM1}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CLBM2}} = C_{D_y^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(0), \text{CuLBM1}} = (24c_s^2 v_2^2 + 6v_2^4 + 2c_s^4 + 3v_2^2 \omega_5 - 12c_s^2 v_2^2 \omega_5 + c_s^2 \omega_5 - c_s^4 \omega_5 - 3v_2^4 \omega_5 - 2c_s^2 - 6v_2^2) \frac{1}{24\omega_5}$$

$$C_{D_y^4 \rho}^{(0), \text{CuLBM2}} = (9v_2^2 \omega_1 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 12v_2^4 \omega_2 - 36c_s^2 v_2^2 \omega_1 \omega_2 + 4c_s^4 \omega_2 - 9v_2^4 \omega_1 \omega_2 + 2c_s^4 \omega_1 + 3c_s^2 \omega_1 \omega_2 + 6v_2^4 \omega_1 - 4c_s^2 \omega_2 + 48c_s^2 v_2^2 \omega_2 - 12v_2^2 \omega_2 + 24c_s^2 v_2^2 \omega_1 - 6v_2^2 \omega_1 - 2c_s^2 \omega_1) \frac{1}{72\omega_1 \omega_2}$$

coefficient $C_{D_y^4 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_2^4}$:

$$C_{D_y^4 v_2}^{(0), \text{SRT}} = (-4 + 2\omega - 5v_2^2\omega - 3c_s^2\omega + 6c_s^2 + 10v_2^2) \frac{v_2\rho}{12\omega}$$

$$C_{D_y^4 v_2}^{(0), \text{MRT1}} = (-4 + 2\omega_{10} - 3c_s^2\omega_{10} - 5v_2^2\omega_{10} + 6c_s^2 + 10v_2^2) \frac{v_2\rho}{12\omega_{10}}$$

$$C_{D_y^4 v_2}^{(0), \text{MRT2}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CLBM1}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CLBM2}} = C_{D_y^4 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(0), \text{CuLBM1}} = (-4 - 5v_2^2\omega_5 - 3c_s^2\omega_5 + 2\omega_5 + 6c_s^2 + 10v_2^2) \frac{v_2\rho}{12\omega_5}$$

$$C_{D_y^4 v_2}^{(0), \text{CuLBM2}} = (-15v_2^2\omega_1\omega_2 + 6\omega_1\omega_2 - 9c_s^2\omega_1\omega_2 - 4\omega_1 + 12c_s^2\omega_2 + 20v_2^2\omega_2 - 8\omega_2 + 10v_2^2\omega_1 + 6c_s^2\omega_1) \frac{v_2\rho}{36\omega_1\omega_2}$$

coefficient $C_{D_x^3 D_z \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{MRT1}} = (-v_1^2\omega_9 - \omega_{13} + v_1^2\omega_{13} + 3c_s^2\omega_{13} - 3c_s^2\omega_9 + \omega_9) \frac{v_3 v_1}{4\omega_{13}\omega_9}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{MRT2}} = C_{D_x^3 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(0), \text{CuLBM2}} = (-\omega_1 + v_3^2\omega_1 - 3c_s^2\omega_2 + \omega_2 + 3c_s^2\omega_1 - v_3^2\omega_2) \frac{v_3 v_1}{12\omega_1\omega_2}$$

coefficient $C_{D_x^3 D_z v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{MRT1}} = (-3v_1^2\omega_9 - \omega_{13} + 3v_1^2\omega_{13} + c_s^2\omega_{13} - c_s^2\omega_9 + \omega_9) \frac{v_3\rho}{4\omega_{13}\omega_9}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{MRT2}} = C_{D_x^3 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_z v_1}^{(0), \text{CuLBM2}} = (-\omega_1 + v_3^2\omega_1 - 3c_s^2\omega_2 + \omega_2 + 3c_s^2\omega_1 - v_3^2\omega_2) \frac{v_3\rho}{36\omega_1\omega_2}$$

coefficient $C_{D_x^3 D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1^3 \partial x_3}$:

$$C_{D_x^3 D_z v_3}^{(0), \text{SRT}} = (2 - 2v_1^2 + v_1^2\omega - \omega + 3c_s^2\omega - 6c_s^2) \frac{v_1\rho}{12\omega}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT}^1} = (\omega_6 v_1^2 \omega_{13} + 3\omega_6 c_s^2 \omega_{13} \omega_9 - 3\omega_6 v_1^2 \omega_9 - 3\omega_6 c_s^2 \omega_9 - \omega_6 \omega_{13} \omega_9 - \omega_6 \omega_{13} + \omega_6 v_1^2 \omega_{13} \omega_9 + 3\omega_6 \omega_9 + 3\omega_6 c_s^2 \omega_{13} - 6c_s^2 \omega_{13} \omega_9) \frac{v_1 \rho}{12\omega_6 \omega_{13} \omega_9}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{MRT}^2} = C_{D_x^3 D_z v_3}^{(0), \text{MRT}^1}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^1} = (-3v_1^2 \omega_9 - \omega_{13} + v_1^2 \omega_{13} + v_1^2 \omega_{13} \omega_9 + 3c_s^2 \omega_{13} - 9c_s^2 \omega_9 - \omega_{13} \omega_9 + 3c_s^2 \omega_{13} \omega_9 + 3\omega_9) \frac{v_1 \rho}{12\omega_{13} \omega_9}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^2} = C_{D_x^3 D_z v_3}^{(0), \text{CLBM}^1}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CuLBM}^1} = (-3v_1^2 \omega_4 + v_1^2 \omega_{12} + 3c_s^2 \omega_4 \omega_{12} - \omega_4 \omega_{12} + 3\omega_4 - 9c_s^2 \omega_4 + v_1^2 \omega_4 \omega_{12} - \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_1 \rho}{12\omega_4 \omega_{12}}$$

$$C_{D_x^3 D_z v_3}^{(0), \text{CuLBM}^2} = (9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 - 9v_1^2 \omega_4 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 9\omega_3 v_1^2 \omega_1 \omega_2 + 2\omega_3 v_1^2 \omega_4 \omega_1 - 18\omega_3 v_3^2 \omega_4 \omega_2 + 6\omega_3 v_1^2 \omega_4 \omega_1 \omega_2 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 18\omega_3 v_3^2 \omega_4 \omega_1 + 4\omega_3 v_1^2 \omega_4 \omega_2 + 9\omega_3 \omega_1 \omega_2) \frac{v_1 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y D_z v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3}$:

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT}^1} = (-\omega_8 + \omega_5) \frac{v_3 c_s^2 \rho}{2\omega_8 \omega_5}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT}^2} = C_{D_x^2 D_y D_z v_2}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM}^1} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CLBM}^2} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CuLBM}^1} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(0), \text{CuLBM}^2} = (9\omega_4 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 c_s^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 2\omega_3 v_3^2 \omega_4 \omega_2 - 9v_3^2 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1 + 9\omega_3 v_3^2 \omega_1 \omega_2 + 2\omega_3 v_3^2 \omega_4 \omega_1 - 9\omega_3 \omega_1 \omega_2) \frac{v_3 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y D_z v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3}$:

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT}^1} = (\omega_6 - \omega_8) \frac{c_s^2 v_2 \rho}{2\omega_6 \omega_8}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT}^2} = C_{D_x^2 D_y D_z v_3}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM}^1} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CLBM}^2} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CuLBM}^1} = 0$$

$$C_{D_x^2 D_y D_z v_3}^{(0), \text{CuLBM}^2} = (-2\omega_3 v_2^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 c_s^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 v_2^2 \omega_4 \omega_1 + 9\omega_3 v_2^2 \omega_1 \omega_2 - 9v_2^2 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 2\omega_3 \omega_4 \omega_1 - 9\omega_3 \omega_1 \omega_2) \frac{v_2 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x D_y^2 D_z v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3}$:

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{MRT}^1} = (-\omega_8 + \omega_5) \frac{v_3 c_s^2 \rho}{2\omega_8 \omega_5}$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{MRT2}} = C_{D_x D_y^2 D_z v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(0), \text{CuLBM2}} = (9\omega_4\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 + 6\omega_3c_s^2\omega_4\omega_1 - 6\omega_3c_s^2\omega_4\omega_2 + 2\omega_3\omega_4\omega_2 - 2\omega_3v_3^2\omega_4\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 - 2\omega_3\omega_4\omega_1 + 9\omega_3v_3^2\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 - 9\omega_3\omega_1\omega_2) \frac{v_3\rho}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}} = (\omega_7 - \omega_8) \frac{c_s^2 v_1 \rho}{2\omega_7 \omega_8}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT2}} = C_{D_x D_y^2 D_z v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(0), \text{CuLBM2}} = (9\omega_4\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 + 6\omega_3c_s^2\omega_4\omega_1 - 6\omega_3c_s^2\omega_4\omega_2 - 9v_1^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 9\omega_3v_1^2\omega_1\omega_2 + 2\omega_3v_1^2\omega_4\omega_1 - 2\omega_3\omega_4\omega_1 - 2\omega_3v_1^2\omega_4\omega_2 - 9\omega_3\omega_1\omega_2) \frac{v_1\rho}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT1}} = (-\omega_{16} + \omega_{10} + 3c_s^2\omega_{16} - 3c_s^2\omega_{10} - v_2^2\omega_{10} + \omega_{16}v_2^2) \frac{v_3v_2}{4\omega_{16}\omega_{10}}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{MRT2}} = C_{D_y^3 D_z \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^3 D_z \rho}^{(0), \text{CuLBM2}} = (-\omega_1 + v_3^2\omega_1 - 3c_s^2\omega_2 + \omega_2 + 3c_s^2\omega_1 - v_3^2\omega_2) \frac{v_3v_2}{12\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT1}} = (-\omega_{16} + \omega_{10} + c_s^2\omega_{16} - c_s^2\omega_{10} - 3v_2^2\omega_{10} + 3\omega_{16}v_2^2) \frac{v_3\rho}{4\omega_{16}\omega_{10}}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{MRT}^2} = C_{D_y^3 D_z v_2}^{(0), \text{MRT}^1}$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM}^1} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CLBM}^2} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CuLBM}^1} = 0$$

$$C_{D_y^3 D_z v_2}^{(0), \text{CuLBM}^2} = (-\omega_1 + v_3^2 \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1 - v_3^2 \omega_2) \frac{v_3 \rho}{36 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z v_3}^{(0), \text{SRT}} = (2 - \omega + v_2^2 \omega + 3c_s^2 \omega - 6c_s^2 - 2v_2^2) \frac{v_2 \rho}{12 \omega}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT}^1} = (3c_s^2 \omega_{16} \omega_{10} \omega_7 - \omega_{16} \omega_{10} \omega_7 + \omega_{16} v_2^2 \omega_7 - 6c_s^2 \omega_{16} \omega_{10} + 3c_s^2 \omega_{16} \omega_7 - \omega_{16} \omega_7 - 3c_s^2 \omega_{10} \omega_7 + 3\omega_{10} \omega_7 + \omega_{16} v_2^2 \omega_{10} \omega_7 - 3v_2^2 \omega_{10} \omega_7) \frac{v_2 \rho}{12 \omega_{16} \omega_{10} \omega_7}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{MRT}^2} = C_{D_y^3 D_z v_3}^{(0), \text{MRT}^1}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM}^1} = (\omega_{16} v_2^2 \omega_{10} - \omega_{16} + 3\omega_{10} + 3c_s^2 \omega_{16} \omega_{10} - \omega_{16} \omega_{10} + 3c_s^2 \omega_{16} - 9c_s^2 \omega_{10} - 3v_2^2 \omega_{10} + \omega_{16} v_2^2) \frac{v_2 \rho}{12 \omega_{16} \omega_{10}}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CLBM}^2} = C_{D_y^3 D_z v_3}^{(0), \text{CLBM}^1}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CuLBM}^1} = (3c_s^2 \omega_{11} \omega_5 + v_2^2 \omega_{11} - \omega_{11} \omega_5 + 3c_s^2 \omega_{11} - 3v_2^2 \omega_5 + v_2^2 \omega_{11} \omega_5 - 9c_s^2 \omega_5 - \omega_{11} + 3\omega_5) \frac{v_2 \rho}{12 \omega_{11} \omega_5}$$

$$C_{D_y^3 D_z v_3}^{(0), \text{CuLBM}^2} = (4\omega_3 v_2^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 v_2^2 \omega_4 \omega_1 + 6\omega_3 v_2^2 \omega_4 \omega_1 \omega_2 - 9\omega_3 v_2^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 9v_2^2 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 18\omega_3 v_3^2 \omega_4 \omega_2 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 18\omega_3 v_3^2 \omega_4 \omega_1 + 9\omega_3 \omega_1 \omega_2) \frac{v_2 \rho}{72 \omega_3 \omega_4 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^2 D_z^2 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} :$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^4}{6 \omega}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT}^1} = (-2 + \omega_6) \frac{c_s^4}{6 \omega_6}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT}^2} = C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{CLBM}^1} = C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{CLBM}^2} = C_{D_x^2 D_z^2 \rho}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{CuLBM}^1} = (-2 + \omega_2) \frac{c_s^4}{6 \omega_2}$$

$$C_{D_x^2 D_z^2 \rho}^{(0), \text{CuLBM}^2} = (3v_1^2 \omega_1 - 3v_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 3v_3^2 \omega_1 - 14c_s^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1 - 3v_3^2 \omega_2) \frac{c_s^2}{36 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x^2 D_z^2 v_1}^{(0)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} :$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{MRT}^1} = (\omega_6 - \omega_{13}) \frac{c_s^2 v_1 \rho}{2 \omega_6 \omega_{13}}$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{MRT}^2} = C_{D_x^2 D_z^2 v_1}^{(0), \text{MRT}^1}$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(0), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1 \rho}{36 \omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_z^2 v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT1}} = (\omega_6 - \omega_{18}) \frac{v_3 c_s^2 \rho}{2 \omega_6 \omega_{18}}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_x^2 D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(0), \text{CuLBM2}} = (-\omega_1 + v_3^2 \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1 - v_3^2 \omega_2) \frac{v_3 \rho}{36 \omega_1 \omega_2}$$

coefficient $C_{D_x D_y D_z^2 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2}$:

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT1}} = (\omega_6 - \omega_8) \frac{c_s^2 v_2 \rho}{2 \omega_6 \omega_8}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_1}^{(0), \text{CuLBM2}} = (-2\omega_3 v_2^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 c_s^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 v_2^2 \omega_4 \omega_1 + 9\omega_3 v_2^2 \omega_1 \omega_2 - 9v_2^2 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 2\omega_3 \omega_4 \omega_1 - 9\omega_3 \omega_1 \omega_2) \frac{v_2 \rho}{72 \omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x D_y D_z^2 v_2}^{(0)}$ **at** $\frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2}$:

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}} = (\omega_7 - \omega_8) \frac{c_s^2 v_1 \rho}{2 \omega_7 \omega_8}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT2}} = C_{D_x D_y D_z^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z^2 v_2}^{(0), \text{CuLBM2}} = (9\omega_4\omega_1\omega_2 + 27\omega_3c_s^2\omega_1\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 + 6\omega_3c_s^2\omega_4\omega_1 - 6\omega_3c_s^2\omega_4\omega_2 - 9v_1^2\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 9\omega_3v_1^2\omega_1\omega_2 + 2\omega_3v_1^2\omega_4\omega_1 - 2\omega_3\omega_4\omega_1 - 2\omega_3v_1^2\omega_4\omega_2 - 9\omega_3\omega_1\omega_2) \frac{v_1\rho}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^2 D_z^2 \rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{SRT}} = (-2 + \omega) \frac{c_s^4}{6\omega}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^4}{6\omega_7}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT2}} = C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CLBM1}} = C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CLBM2}} = C_{D_y^2 D_z^2 \rho}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^4}{6\omega_3}$$

$$C_{D_y^2 D_z^2 \rho}^{(0), \text{CuLBM2}} = (6c_s^2\omega_1\omega_2 - 2\omega_1 + 3v_3^2\omega_1 - 14c_s^2\omega_2 - 3v_2^2\omega_2 + 2\omega_2 + 3v_2^2\omega_1 + 2c_s^2\omega_1 - 3v_3^2\omega_2) \frac{c_s^2}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^2 D_z^2 v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{SRT}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT1}} = (-\omega_{16} + \omega_7) \frac{c_s^2 v_2 \rho}{2\omega_{16}\omega_7}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT2}} = C_{D_y^2 D_z^2 v_2}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_2}^{(0), \text{CuLBM2}} = (-\omega_1 - 3c_s^2\omega_2 - v_2^2\omega_2 + \omega_2 + v_2^2\omega_1 + 3c_s^2\omega_1) \frac{v_2\rho}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^2 D_z^2 v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} :$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT1}} = (-\omega_{19} + \omega_7) \frac{v_3 c_s^2 \rho}{2\omega_{19}\omega_7}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT2}} = C_{D_y^2 D_z^2 v_3}^{(0), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z^2 v_3}^{(0), \text{CuLBM2}} = (-\omega_1 + v_3^2 \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1 - v_3^2 \omega_2) \frac{v_3 \rho}{36 \omega_1 \omega_2}$$

coefficient $C_{D_x D_z^3 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_1 \partial x_3^3}$:

$$C_{D_x D_z^3 \rho}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT1}} = (-3c_s^2 \omega_{11} - v_3^2 \omega_{11} + \omega_{11} + 3c_s^2 \omega_{18} + v_3^2 \omega_{18} - \omega_{18}) \frac{v_3 v_1}{4 \omega_{11} \omega_{18}}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{MRT2}} = C_{D_x D_z^3 \rho}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^3 \rho}^{(0), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 v_1}{12 \omega_1 \omega_2}$$

coefficient $C_{D_x D_z^2 v_1}^{(0)}$ **at** $\frac{\partial^4 v_1}{\partial x_1 \partial x_3^3}$:

$$C_{D_x D_z^2 v_1}^{(0), \text{SRT}} = (2 - \omega + v_3^2 \omega - 2v_3^2 + 3c_s^2 \omega - 6c_s^2) \frac{v_3 \rho}{12 \omega}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{MRT1}} = (3\omega_6 \omega_{11} - 3\omega_6 v_3^2 \omega_{11} + 3\omega_6 c_s^2 \omega_{11} \omega_{18} - 3\omega_6 c_s^2 \omega_{11} + \omega_6 v_3^2 \omega_{11} \omega_{18} - \omega_6 \omega_{11} \omega_{18} - \omega_6 \omega_{18} + \omega_6 v_3^2 \omega_{18} - 6c_s^2 \omega_{11} \omega_{18} + 3\omega_6 c_s^2 \omega_{18}) \frac{v_3 \rho}{12 \omega_6 \omega_{11} \omega_{18}}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{MRT2}} = C_{D_x D_z^2 v_1}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{CLBM1}} = (v_3^2 \omega_{11} \omega_{18} - 9c_s^2 \omega_{11} - 3v_3^2 \omega_{11} + 3\omega_{11} + 3c_s^2 \omega_{18} - \omega_{11} \omega_{18} + 3c_s^2 \omega_{11} \omega_{18} + v_3^2 \omega_{18} - \omega_{18}) \frac{v_3 \rho}{12 \omega_{11} \omega_{18}}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{CLBM2}} = C_{D_x D_z^2 v_1}^{(0), \text{CLBM1}}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{CuLBM1}} = (-3\omega_6 v_3^2 + 3\omega_6 + 3\omega_6 c_s^2 \omega_8 + v_3^2 \omega_8 - 9\omega_6 c_s^2 + 3c_s^2 \omega_8 - \omega_6 \omega_8 + \omega_6 v_3^2 \omega_8 - \omega_8) \frac{v_3 \rho}{12 \omega_6 \omega_8}$$

$$C_{D_x D_z^2 v_1}^{(0), \text{CuLBM2}} = (9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 + 6\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 18\omega_3 v_1^2 \omega_4 \omega_1 + 4\omega_3 v_3^2 \omega_4 \omega_2 - 9v_3^2 \omega_4 \omega_1 \omega_2 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 - 9\omega_3 v_3^2 \omega_1 \omega_2 + 2\omega_3 v_3^2 \omega_4 \omega_1 - 18\omega_3 v_1^2 \omega_4 \omega_2 + 9\omega_3 \omega_1 \omega_2) \frac{v_3 \rho}{72 \omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x D_z^3 v_3}^{(0)}$ **at** $\frac{\partial^4 v_3}{\partial x_1 \partial x_3^3}$:

$$C_{D_x D_z^3 v_3}^{(0), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{MRT1}} = (-c_s^2 \omega_{11} - 3v_3^2 \omega_{11} + \omega_{11} + c_s^2 \omega_{18} + 3v_3^2 \omega_{18} - \omega_{18}) \frac{v_1 \rho}{4 \omega_{11} \omega_{18}}$$

$$C_{D_x D_z^3 v_3}^{(0), \text{MRT2}} = C_{D_x D_z^3 v_3}^{(0), \text{MRT1}}$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CLBM1}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CLBM2}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CuLBM1}} = 0$$

$$C_{D_x D_z^3 v_3}^{(0), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1 \rho}{36 \omega_1 \omega_2}$$

coefficient $C_{D_y D_z^3 \rho}^{(0)}$ **at** $\frac{\partial^4 \rho}{\partial x_2 \partial x_3^3}$:

$$C_{\text{DyD}_z^3\rho}^{(0),\text{SRT}} = 0$$

$$C_{\text{DyD}_z^3\rho}^{(0),\text{MRT1}} = (-3c_s^2\omega_{11} - \omega_{19} - v_3^2\omega_{11} + \omega_{19}v_3^2 + \omega_{11} + 3\omega_{19}c_s^2) \frac{v_3v_2}{4\omega_{19}\omega_{11}}$$

$$C_{\text{DyD}_z^3\rho}^{(0),\text{MRT2}} = C_{\text{DyD}_z^3\rho}^{(0),\text{MRT1}}$$

$$C_{\text{DyD}_z^3\rho}^{(0),\text{CLBM1}} = 0$$

$$C_{\text{DyD}_z^3\rho}^{(0),\text{CLBM2}} = 0$$

$$C_{\text{DyD}_z^3\rho}^{(0),\text{CuLBM1}} = 0$$

$$C_{\text{DyD}_z^3\rho}^{(0),\text{CuLBM2}} = (-\omega_1 - 3c_s^2\omega_2 - v_2^2\omega_2 + \omega_2 + v_2^2\omega_1 + 3c_s^2\omega_1) \frac{v_3v_2}{12\omega_1\omega_2}$$

$$\text{coefficient } C_{\text{DyD}_z^3v_2}^{(0)} \text{ at } \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} :$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{SRT}} = (2 - \omega + v_3^2\omega - 2v_3^2 + 3c_s^2\omega - 6c_s^2) \frac{v_3\rho}{12\omega}$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{MRT1}} = (-\omega_{19}\omega_7 - \omega_{19}\omega_7\omega_{11} + \omega_{19}v_3^2\omega_7\omega_{11} + 3\omega_7\omega_{11} - 3c_s^2\omega_7\omega_{11} - 6\omega_{19}c_s^2\omega_{11} + \omega_{19}v_3^2\omega_7 - 3v_3^2\omega_7\omega_{11} + 3\omega_{19}c_s^2\omega_7\omega_{11} + 3\omega_{19}c_s^2\omega_7) \frac{v_3\rho}{12\omega_{19}\omega_7\omega_{11}}$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{MRT2}} = C_{\text{DyD}_z^3v_2}^{(0),\text{MRT1}}$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{CLBM1}} = (\omega_{19}v_3^2\omega_{11} - 9c_s^2\omega_{11} - \omega_{19} - 3v_3^2\omega_{11} + 3\omega_{19}c_s^2\omega_{11} + \omega_{19}v_3^2 - \omega_{19}\omega_{11} + 3\omega_{11} + 3\omega_{19}c_s^2) \frac{v_3\rho}{12\omega_{19}\omega_{11}}$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{CLBM2}} = C_{\text{DyD}_z^3v_2}^{(0),\text{CLBM1}}$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{CuLBM1}} = (-3\omega_6v_3^2 + 3\omega_6 - 9\omega_6c_s^2 - \omega_{10} + 3c_s^2\omega_{10} + \omega_6v_3^2\omega_{10} - \omega_6\omega_{10} + 3\omega_6c_s^2\omega_{10} + v_3^2\omega_{10}) \frac{v_3\rho}{12\omega_6\omega_{10}}$$

$$C_{\text{DyD}_z^3v_2}^{(0),\text{CuLBM2}} = (-18\omega_3v_2^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2 + 18\omega_3v_2^2\omega_4\omega_1 - 6\omega_3\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 4\omega_3v_3^2\omega_4\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 + 9\omega_3\omega_1\omega_2) \frac{v_3\rho}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{\text{DyD}_z^3v_3}^{(0)} \text{ at } \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} :$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{SRT}} = 0$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{MRT1}} = (-c_s^2\omega_{11} - \omega_{19} - 3v_3^2\omega_{11} + 3\omega_{19}v_3^2 + \omega_{11} + \omega_{19}c_s^2) \frac{v_2\rho}{4\omega_{19}\omega_{11}}$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{MRT2}} = C_{\text{DyD}_z^3v_3}^{(0),\text{MRT1}}$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{CLBM1}} = 0$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{CLBM2}} = 0$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{CuLBM1}} = 0$$

$$C_{\text{DyD}_z^3v_3}^{(0),\text{CuLBM2}} = (-\omega_1 - 3c_s^2\omega_2 - v_2^2\omega_2 + \omega_2 + v_2^2\omega_1 + 3c_s^2\omega_1) \frac{v_2\rho}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{\text{D}_z^4\rho}^{(0)} \text{ at } \frac{\partial^4 \rho}{\partial x_3^4} :$$

$$C_{\text{D}_z^4\rho}^{(0),\text{SRT}} = (6v_3^4 - 3v_3^4\omega - 12v_3^2c_s^2\omega + 2c_s^4 - c_s^4\omega + 24v_3^2c_s^2 + 3v_3^2\omega - 6v_3^2 + c_s^2\omega - 2c_s^2) \frac{1}{24\omega}$$

$$C_{\text{D}_z^4\rho}^{(0),\text{MRT1}} = (6v_3^4 + c_s^2\omega_{11} + 2c_s^4 + 3v_3^2\omega_{11} + 24v_3^2c_s^2 - c_s^4\omega_{11} - 6v_3^2 - 3v_3^4\omega_{11} - 2c_s^2 - 12v_3^2c_s^2\omega_{11}) \frac{1}{24\omega_{11}}$$

$$C_{D_z^4 \rho}^{(0), \text{MRT2}} = C_{D_z^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(0), \text{CLBM1}} = C_{D_z^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(0), \text{CLBM2}} = C_{D_z^4 \rho}^{(0), \text{MRT1}}$$

$$C_{D_z^4 \rho}^{(0), \text{CuLBM1}} = (3\omega_6 v_3^2 + 6v_3^4 + \omega_6 c_s^2 - 12\omega_6 v_3^2 c_s^2 + 2c_s^4 + 24v_3^2 c_s^2 - 3\omega_6 v_3^4 - 6v_3^2 - \omega_6 c_s^4 - 2c_s^2) \frac{1}{24\omega_6}$$

$$C_{D_z^4 \rho}^{(0), \text{CuLBM2}} = (-3c_s^4 \omega_1 \omega_2 + 24v_3^2 c_s^2 \omega_1 + 6v_3^4 \omega_1 + 4c_s^4 \omega_2 + 48v_3^2 c_s^2 \omega_2 + 2c_s^4 \omega_1 + 12v_3^4 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 6v_3^2 \omega_1 - 4c_s^2 \omega_2 + 9v_3^2 \omega_1 \omega_2 - 9v_3^4 \omega_1 \omega_2 - 2c_s^2 \omega_1 - 36v_3^2 c_s^2 \omega_1 \omega_2 - 12v_3^2 \omega_2) \frac{1}{72\omega_1 \omega_2}$$

coefficient $C_{D_z^4 v_3}^{(0)}$ at $\frac{\partial^4 v_3}{\partial x_3^4}$:

$$C_{D_z^4 v_3}^{(0), \text{SRT}} = (-4 + 2\omega - 5v_3^2 \omega + 10v_3^2 - 3c_s^2 \omega + 6c_s^2) \frac{v_3 \rho}{12\omega}$$

$$C_{D_z^4 v_3}^{(0), \text{MRT1}} = (-4 - 3c_s^2 \omega_{11} - 5v_3^2 \omega_{11} + 2\omega_{11} + 10v_3^2 + 6c_s^2) \frac{v_3 \rho}{12\omega_{11}}$$

$$C_{D_z^4 v_3}^{(0), \text{MRT2}} = C_{D_z^4 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(0), \text{CLBM1}} = C_{D_z^4 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(0), \text{CLBM2}} = C_{D_z^4 v_3}^{(0), \text{MRT1}}$$

$$C_{D_z^4 v_3}^{(0), \text{CuLBM1}} = (-4 - 5\omega_6 v_3^2 + 2\omega_6 - 3\omega_6 c_s^2 + 10v_3^2 + 6c_s^2) \frac{v_3 \rho}{12\omega_6}$$

$$C_{D_z^4 v_3}^{(0), \text{CuLBM2}} = (6\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 10v_3^2 \omega_1 + 12c_s^2 \omega_2 - 15v_3^2 \omega_1 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1 + 20v_3^2 \omega_2) \frac{v_3 \rho}{36\omega_1 \omega_2}$$

3.2 Conservation of momentum: ρv_1

$$\begin{aligned} & v_1 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_1}{\partial t} + (v_1^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + 2v_1 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + v_2 v_1 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + v_2 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_2} + v_1 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + v_3 v_1 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + v_3 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_3} + \\ & v_1 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + C_{D_x \rho, D_x v_1}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1} + C_{D_x v_1, D_x v_1}^{(1)} \frac{\delta_l^2}{\delta_t} \left(\frac{\partial v_1}{\partial x_1} \right)^2 + C_{D_x \rho, D_y v_2}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2} + C_{D_x v_2, D_y v_2}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_2}{\partial x_1} \frac{\partial v_2}{\partial x_2} + \\ & C_{D_x \rho, D_z v_3}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3} + C_{D_x v_3, D_z v_3}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial v_3}{\partial x_1} \frac{\partial v_3}{\partial x_3} + C_{D_y \rho, D_x v_2}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1} + C_{D_y v_2, D_x v_2}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2} + \\ & C_{D_z \rho, D_x v_3}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1} + C_{D_z v_3, D_x v_3}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3} + C_{D_z^2 \rho}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + C_{D_z^2 v_1}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_1^2} + C_{D_x \rho, D_y v_2}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1^2} + \\ & C_{D_x D_y v_2}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_2}{\partial x_1 \partial x_2} + C_{D_y^2 v_1}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_2^2} + C_{D_x D_z \rho}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + C_{D_x D_z v_3}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_3}{\partial x_1 \partial x_3} + C_{D_z^2 v_1}^{(1)} \frac{\delta_l^2}{\delta_t} \frac{\partial^2 v_1}{\partial x_3^2} + C_{D_x^3 \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1^3} + \\ & C_{D_z^3 v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1^3} + C_{D_x^2 D_y \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} + C_{D_x^2 D_y v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} + C_{D_x^2 D_y v_2}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_{D_x D_y^2 \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} + \\ & C_{D_x D_y^2 v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} + C_{D_x D_y^2 v_2}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} + C_{D_y^3 \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_2^3} + C_{D_y^3 v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_2^3} + C_{D_y^3 v_2}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_2^3} + C_{D_x^2 D_z \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} + \\ & C_{D_x^2 D_z v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} + C_{D_x^2 D_z v_3}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_3} + C_{D_x D_y D_z \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3} + C_{D_x D_y D_z v_2}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3} + \\ & C_{D_x D_y D_z v_3}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3} + C_{D_y^2 D_z v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_2^2 \partial x_3} + C_{D_y^2 D_z v_3}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} + C_{D_x D_z^2 \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} + C_{D_x D_z^2 v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_1 \partial x_3^2} + \\ & C_{D_x D_z^2 v_3}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_1 \partial x_3^2} + C_{D_y D_z^2 v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_2 \partial x_3^2} + C_{D_y D_z^2 v_2}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_2}{\partial x_2 \partial x_3^2} + C_{D_z^3 \rho}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 \rho}{\partial x_3^3} + C_{D_z^3 v_1}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_1}{\partial x_3^3} + C_{D_z^3 v_3}^{(1)} \frac{\delta_l^3}{\delta_t} \frac{\partial^3 v_3}{\partial x_3^3} + \\ & C_{D_x^4 \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^4} + C_{D_x^4 v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^4} + C_{D_x^3 D_y \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} + C_{D_x^3 D_y v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_2} + C_{D_x^3 D_y v_2}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^3 \partial x_2} + C_{D_x^2 D_y^2 \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} + \\ & C_{D_x^2 D_y^2 v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} + C_{D_x^2 D_y^2 v_2}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2} + C_{D_x D_y^3 \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} + C_{D_x D_y^3 v_2}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} + \\ & C_{D_y^4 \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^4} + C_{D_y^4 v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_2^4} + C_{D_y^4 v_2}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^4} + C_{D_x^3 D_z \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} + C_{D_x^3 D_z v_3}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} + \\ & C_{D_x^2 D_y D_z \rho}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_1}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_2}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3} + C_{D_x^2 D_y D_z v_3}^{(1)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3} + \end{aligned}$$

$$\begin{aligned}
& C_{D_x D_y D_z \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y^2 D_z v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y D_z v_2}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} + C_{D_x D_y D_z v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2^2 \partial x_3} + \\
& C_{D_y^3 D_z \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_2}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} + C_{D_y^3 D_z v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^3 \partial x_3} + C_{D_x^2 D_z^2 \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2} + \\
& C_{D_x^2 D_z^2 v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2} + C_{D_x^2 D_z^2 v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2} + C_{D_x D_y D_z^2 \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_2 \partial x_3^2} + \\
& C_{D_x D_y D_z^2 v_2}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_x D_y D_z^2 v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_2 \partial x_3^2} + C_{D_y^2 D_z^2 \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_2^2 \partial x_3^2} + \\
& C_{D_y^2 D_z^2 v_2}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2} + C_{D_y^2 D_z^2 v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2} + C_{D_x D_z^3 \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} + C_{D_x D_z^3 v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} + \\
& C_{D_y D_z^3 \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_2}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} + C_{D_y D_z^3 v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{D_z^4 \rho}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + \\
& C_{D_z^4 v_1}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_1}{\partial x_3^4} + C_{D_z^4 v_3}^{(1)} \frac{\delta_t^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,
\end{aligned}$$

where:

coefficient $C_{D_x \rho, D_x v_1}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_1}$:

$$\begin{aligned}
C_{D_x \rho, D_x v_1}^{(1), \text{SRT}} &= (-2 + 6v_1^2 - 3v_1^2 \omega + \omega - 2c_s^2 \omega + 4c_s^2) \frac{1}{\omega} \\
C_{D_x \rho, D_x v_1}^{(1), \text{MRT1}} &= (-2 + 6v_1^2 - 3v_1^2 \omega_9 - 2c_s^2 \omega_9 + 4c_s^2 + \omega_9) \frac{1}{\omega_9} \\
C_{D_x \rho, D_x v_1}^{(1), \text{MRT2}} &= C_{D_x \rho, D_x v_1}^{(1), \text{MRT1}} \\
C_{D_x \rho, D_x v_1}^{(1), \text{CLBM1}} &= C_{D_x \rho, D_x v_1}^{(1), \text{MRT1}} \\
C_{D_x \rho, D_x v_1}^{(1), \text{CLBM2}} &= C_{D_x \rho, D_x v_1}^{(1), \text{MRT1}} \\
C_{D_x \rho, D_x v_1}^{(1), \text{CuLBM1}} &= (-2 + 6v_1^2 - 3v_1^2 \omega_4 + \omega_4 - 2c_s^2 \omega_4 + 4c_s^2) \frac{1}{\omega_4} \\
C_{D_x \rho, D_x v_1}^{(1), \text{CuLBM2}} &= (6v_1^2 \omega_1 + 12v_1^2 \omega_2 + 3\omega_1 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 8c_s^2 \omega_2 - 4\omega_2 + 4c_s^2 \omega_1 - 9v_1^2 \omega_1 \omega_2) \frac{1}{3\omega_1 \omega_2}
\end{aligned}$$

coefficient $C_{D_x v_1, D_x v_1}^{(1)}$ **at** $\left(\frac{\partial v_1}{\partial x_1}\right)^2$:

$$\begin{aligned}
C_{D_x v_1, D_x v_1}^{(1), \text{SRT}} &= (2 - \omega) \frac{3v_1 \rho}{\omega} \\
C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}} &= (2 - \omega_9) \frac{3v_1 \rho}{\omega_9} \\
C_{D_x v_1, D_x v_1}^{(1), \text{MRT2}} &= C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}} \\
C_{D_x v_1, D_x v_1}^{(1), \text{CLBM1}} &= C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}} \\
C_{D_x v_1, D_x v_1}^{(1), \text{CLBM2}} &= C_{D_x v_1, D_x v_1}^{(1), \text{MRT1}} \\
C_{D_x v_1, D_x v_1}^{(1), \text{CuLBM1}} &= (2 - \omega_4) \frac{3v_1 \rho}{\omega_4} \\
C_{D_x v_1, D_x v_1}^{(1), \text{CuLBM2}} &= (-3\omega_1 \omega_2 + 2\omega_1 + 4\omega_2) \frac{v_1 \rho}{\omega_1 \omega_2}
\end{aligned}$$

coefficient $C_{D_x \rho, D_y v_2}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_2}$:

$$\begin{aligned}
C_{D_x \rho, D_y v_2}^{(1), \text{SRT}} &= 0 \\
C_{D_x \rho, D_y v_2}^{(1), \text{MRT1}} &= 0 \\
C_{D_x \rho, D_y v_2}^{(1), \text{MRT2}} &= 0 \\
C_{D_x \rho, D_y v_2}^{(1), \text{CLBM1}} &= 0
\end{aligned}$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x \rho, D_y v_2}^{(1), \text{CuLBM2}} = (-\omega_1 - c_s^2 \omega_2 - 3v_2^2 \omega_2 + \omega_2 + 3v_2^2 \omega_1 + c_s^2 \omega_1) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_x v_2, D_y v_2}^{(1)}$ **at** $\frac{\partial v_2}{\partial x_1} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_x v_2, D_y v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{MRT1}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{MRT2}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x v_2, D_y v_2}^{(1), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2v_2 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_x \rho, D_z v_3}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_x \rho, D_z v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{MRT1}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{MRT2}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x \rho, D_z v_3}^{(1), \text{CuLBM2}} = (-\omega_1 + 3v_3^2 \omega_1 - c_s^2 \omega_2 + \omega_2 + c_s^2 \omega_1 - 3v_3^2 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_x v_3, D_z v_3}^{(1)}$ **at** $\frac{\partial v_3}{\partial x_1} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_x v_3, D_z v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{MRT1}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{MRT2}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x v_3, D_z v_3}^{(1), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2v_3 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_x v_2}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_1}$:

$$C_{D_y \rho, D_x v_2}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2}{2\omega_5}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{MRT2}} = C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CLBM1}} = C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CLBM2}} = C_{D_y \rho, D_x v_2}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

$$C_{D_y \rho, D_x v_2}^{(1), \text{CuLBM2}} = (3c_s^2\omega_1\omega_2 - 2\omega_1 - 12c_s^2\omega_2 - 6v_2^2\omega_2 + 2\omega_2 + 6v_2^2\omega_1 + 6c_s^2\omega_1) \frac{1}{6\omega_1\omega_2}$$

coefficient $C_{D_y \rho, D_y v_1}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_2}$:

$$C_{D_y \rho, D_y v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2}{2\omega_5}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{MRT2}} = C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CLBM1}} = C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CLBM2}} = C_{D_y \rho, D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

$$C_{D_y \rho, D_y v_1}^{(1), \text{CuLBM2}} = C_{D_y \rho, D_y v_1}^{(1), \text{CuLBM1}}$$

coefficient $C_{D_z \rho, D_x v_3}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_1}$:

$$C_{D_z \rho, D_x v_3}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2}{2\omega_6}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{MRT2}} = C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CLBM1}} = C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CLBM2}} = C_{D_z \rho, D_x v_3}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_z \rho, D_x v_3}^{(1), \text{CuLBM2}} = (3c_s^2\omega_1\omega_2 - 2\omega_1 + 6v_3^2\omega_1 - 12c_s^2\omega_2 + 2\omega_2 + 6c_s^2\omega_1 - 6v_3^2\omega_2) \frac{1}{6\omega_1\omega_2}$$

coefficient $C_{D_z \rho, D_z v_1}^{(1)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_3}$:

$$C_{D_z \rho, D_z v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2}{2\omega_6}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{MRT2}} = C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CLBM1}} = C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CLBM2}} = C_{D_z \rho, D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_z \rho, D_z v_1}^{(1), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_x^2 \rho}^{(1)}$ **at** $\frac{\partial^2 \rho}{\partial x_1^2}$:

$$C_{D_x^2 \rho}^{(1), \text{SRT}} = (-2 + 2v_1^2 - v_1^2 \omega + \omega - 3c_s^2 \omega + 6c_s^2) \frac{v_1}{2\omega}$$

$$C_{D_x^2 \rho}^{(1), \text{MRT1}} = (-2 + 2v_1^2 - v_1^2 \omega_9 - 3c_s^2 \omega_9 + 6c_s^2 + \omega_9) \frac{v_1}{2\omega_9}$$

$$C_{D_x^2 \rho}^{(1), \text{MRT2}} = C_{D_x^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 \rho}^{(1), \text{CLBM1}} = C_{D_x^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 \rho}^{(1), \text{CLBM2}} = C_{D_x^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 \rho}^{(1), \text{CuLBM1}} = (-2 + 2v_1^2 - v_1^2 \omega_4 + \omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_1}{2\omega_4}$$

$$C_{D_x^2 \rho}^{(1), \text{CuLBM2}} = (2v_1^2 \omega_1 + 4v_1^2 \omega_2 + 3\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 2\omega_1 + 12c_s^2 \omega_2 - 4\omega_2 + 6c_s^2 \omega_1 - 3v_1^2 \omega_1 \omega_2) \frac{v_1}{6\omega_1 \omega_2}$$

coefficient $C_{D_x^2 v_1}^{(1)}$ **at** $\frac{\partial^2 v_1}{\partial x_1^2}$:

$$C_{D_x^2 v_1}^{(1), \text{SRT}} = (-2 + 6v_1^2 - 3v_1^2 \omega + \omega - c_s^2 \omega + 2c_s^2) \frac{\rho}{2\omega}$$

$$C_{D_x^2 v_1}^{(1), \text{MRT1}} = (-2 + 6v_1^2 - 3v_1^2 \omega_9 - c_s^2 \omega_9 + 2c_s^2 + \omega_9) \frac{\rho}{2\omega_9}$$

$$C_{D_x^2 v_1}^{(1), \text{MRT2}} = C_{D_x^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(1), \text{CLBM1}} = C_{D_x^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(1), \text{CLBM2}} = C_{D_x^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 v_1}^{(1), \text{CuLBM1}} = (-2 + 6v_1^2 - 3v_1^2 \omega_4 + \omega_4 - c_s^2 \omega_4 + 2c_s^2) \frac{\rho}{2\omega_4}$$

$$C_{D_x^2 v_1}^{(1), \text{CuLBM2}} = (6v_1^2 \omega_1 + 12v_1^2 \omega_2 + 3\omega_1 \omega_2 - 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 4c_s^2 \omega_2 - 4\omega_2 + 2c_s^2 \omega_1 - 9v_1^2 \omega_1 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_x D_y \rho}^{(1)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{MRT1}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{MRT2}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(1), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_2}{3\omega_1 \omega_2}$$

coefficient $C_{D_x D_y v_2}^{(1)}$ **at** $\frac{\partial^2 v_2}{\partial x_1 \partial x_2}$:

$$C_{D_x D_y v_2}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_y v_2}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_x D_y v_2}^{(1), \text{MRT2}} = C_{D_x D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(1), \text{CLBM1}} = C_{D_x D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(1), \text{CLBM2}} = C_{D_x D_y v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y v_2}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_x D_y v_2}^{(1), \text{CuLBM2}} = (3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 8c_s^2 \omega_2 - 6v_2^2 \omega_2 + 2\omega_2 + 6v_2^2 \omega_1 + 2c_s^2 \omega_1) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_y^2 v_1}^{(1)}$ **at** $\frac{\partial^2 v_1}{\partial x_2^2}$:

$$C_{D_y^2 v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y^2 v_1}^{(1), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_y^2 v_1}^{(1), \text{MRT2}} = C_{D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 v_1}^{(1), \text{CLBM1}} = C_{D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 v_1}^{(1), \text{CLBM2}} = C_{D_y^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_y^2 v_1}^{(1), \text{CuLBM2}} = C_{D_y^2 v_1}^{(1), \text{CuLBM1}}$$

coefficient $C_{D_x D_z \rho}^{(1)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{MRT1}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{MRT2}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(1), \text{CuLBM2}} = (-\omega_1 + v_3^2 \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1 - v_3^2 \omega_2) \frac{v_3}{3\omega_1 \omega_2}$$

coefficient $C_{D_x D_z v_3}^{(1)}$ **at** $\frac{\partial^2 v_3}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z v_3}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_z v_3}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_x D_z v_3}^{(1), \text{MRT2}} = C_{D_x D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(1), \text{CLBM1}} = C_{D_x D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(1), \text{CLBM2}} = C_{D_x D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z v_3}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_x D_z v_3}^{(1), \text{CuLBM2}} = (3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 - 8c_s^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1 - 6v_3^2 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_z^2 v_1}^{(1)}$ **at** $\frac{\partial^2 v_1}{\partial x_3^2}$:

$$C_{D_z^2 v_1}^{(1), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_z^2 v_1}^{(1), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_z^2 v_1}^{(1), \text{MRT2}} = C_{D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^2 v_1}^{(1), \text{CLBM1}} = C_{D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^2 v_1}^{(1), \text{CLBM2}} = C_{D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^2 v_1}^{(1), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_z^2 v_1}^{(1), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_x^3 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^3}$:

$$C_{D_x^3 \rho}^{(1), \text{SRT}} = (-36v_1^2 - 144c_s^2 v_1^2 \omega + c_s^4 \omega^2 + 36v_1^2 \omega + 12c_s^4 - 7v_1^2 \omega^2 - 12c_s^4 \omega + 24c_s^2 v_1^2 \omega^2 - 36v_1^4 \omega - c_s^2 \omega^2 + 36v_1^4 + 12c_s^2 \omega + 7v_1^4 \omega^2 - 12c_s^2 + 144c_s^2 v_1^2) \frac{1}{12\omega^2}$$

$$C_{D_x^3 \rho}^{(1), \text{MRT1}} = (-36v_1^2 - 144c_s^2 v_1^2 \omega_9 + 36v_1^2 \omega_9 + c_s^4 \omega_9^2 + 12c_s^4 - 12c_s^4 \omega_9 - 7v_1^2 \omega_9^2 + 24c_s^2 v_1^2 \omega_9^2 - c_s^2 \omega_9^2 - 36v_1^4 \omega_9 + 36v_1^4 + 7v_1^4 \omega_9^2 + 12c_s^2 \omega_9 - 12c_s^2 + 144c_s^2 v_1^2) \frac{1}{12\omega_9^2}$$

$$C_{D_x^3 \rho}^{(1), \text{MRT2}} = C_{D_x^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(1), \text{CLBM1}} = C_{D_x^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(1), \text{CLBM2}} = C_{D_x^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 \rho}^{(1), \text{CuLBM1}} = (-36v_1^2 - 144c_s^2 v_1^2 \omega_4 + 36v_1^2 \omega_4 + c_s^4 \omega_4^2 + 12c_s^4 - 12c_s^4 \omega_4 - 7v_1^2 \omega_4^2 + 24c_s^2 v_1^2 \omega_4^2 - c_s^2 \omega_4^2 - 36v_1^4 \omega_4 + 7v_1^4 \omega_4^2 + 12c_s^2 \omega_4 + 36v_1^4 - 12c_s^2 + 144c_s^2 v_1^2) \frac{1}{12\omega_4^2}$$

$$C_{D_x^3 \rho}^{(1), \text{CuLBM2}} = (12v_1^2 \omega_1^2 \omega_2 + 4c_s^4 \omega_1^2 + 72c_s^2 v_1^2 \omega_2^2 + 7v_1^4 \omega_1^2 \omega_2^2 + 8c_s^2 \omega_1 \omega_2^2 - 48c_s^2 v_1^2 \omega_1^2 \omega_2 - 16v_1^2 \omega_2^2 + 24c_s^2 v_1^2 \omega_1^2 + 24c_s^2 v_1^2 \omega_1^2 \omega_2^2 + 8c_s^4 \omega_2^2 - 4v_1^4 \omega_1^2 - 12v_1^4 \omega_1^2 \omega_2 - 8c_s^4 \omega_1 \omega_2^2 - 7v_1^2 \omega_1^2 \omega_2^2 - 4c_s^2 \omega_1^2 + 24v_1^2 \omega_1 \omega_2^2 + c_s^4 \omega_1^2 \omega_2^2 + 16v_1^4 \omega_2^2 - 96c_s^2 v_1^2 \omega_1 \omega_2^2 + 4c_s^2 \omega_1^2 \omega_2 + 16v_1^4 \omega_1 \omega_2 - c_s^2 \omega_1^2 \omega_2^2 - 24v_1^4 \omega_1 \omega_2^2 + 48c_s^2 v_1^2 \omega_1 \omega_2 - 8c_s^2 \omega_2^2 + 4v_1^4 \omega_1^2 - 16v_1^2 \omega_1 \omega_2 - 4c_s^4 \omega_1^2 \omega_2) \frac{1}{12\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^3 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^3}$:

$$C_{D_x^3 v_1}^{(1), \text{SRT}} = (-24 + 60v_1^2 - 60v_1^2 \omega + 11v_1^2 \omega^2 - 4\omega^2 + 24\omega + 5c_s^2 \omega^2 - 36c_s^2 \omega + 36c_s^2) \frac{v_1 \rho}{6\omega^2}$$

$$C_{D_x^3 v_1}^{(1), \text{MRT1}} = (-24 + 60v_1^2 - 60v_1^2 \omega_9 + 11v_1^2 \omega_9^2 - 4\omega_9^2 + 5c_s^2 \omega_9^2 - 36c_s^2 \omega_9 + 36c_s^2 + 24\omega_9) \frac{v_1 \rho}{6\omega_9^2}$$

$$C_{D_x^3 v_1}^{(1), \text{MRT2}} = C_{D_x^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(1), \text{CLBM1}} = C_{D_x^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(1), \text{CLBM2}} = C_{D_x^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(1), \text{CuLBM1}} = (-24 + 60v_1^2 - 60v_1^2\omega_4 - 4\omega_4^2 + 24\omega_4 + 11v_1^2\omega_4^2 + 5c_s^2\omega_4^2 - 36c_s^2\omega_4 + 36c_s^2)\frac{v_1\rho}{6\omega_4^2}$$

$$C_{D_x^3 v_1}^{(1), \text{CuLBM2}} = (-12\omega_2^2 - 20v_1^2\omega_1^2\omega_2 - 24c_s^2\omega_1\omega_2^2 + 28v_1^2\omega_2^2 + 16\omega_1\omega_2^2 - 8\omega_1\omega_2 + 8v_1^2\omega_1^2 + 8c_s^2\omega_1\omega_2 + 11v_1^2\omega_1^2\omega_2^2 - 4\omega_1^2 + 8c_s^2\omega_1^2 - 40v_1^2\omega_1\omega_2^2 + 8\omega_1^2\omega_2 - 12c_s^2\omega_1^2\omega_2 + 5c_s^2\omega_1^2\omega_2^2 - 4\omega_1^2\omega_2^2 + 20c_s^2\omega_2^2 + 24v_1^2\omega_1\omega_2)\frac{v_1\rho}{6\omega_1^2\omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_y \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{MRT1}} = (3c_s^2\omega_5\omega_{12} - \omega_9\omega_{12} + \omega_5\omega_9 + 3c_s^2\omega_9\omega_{12} - \omega_5\omega_{12} - 3c_s^2\omega_5\omega_9 - v_1^2\omega_9^2 + \omega_9^2 + 3c_s^2\omega_5\omega_9^2 - \omega_5\omega_9^2 - 3c_s^2\omega_9^2 + v_1^2\omega_5\omega_{12} - v_1^2\omega_5\omega_9\omega_{12} + v_1^2\omega_9\omega_{12} - v_1^2\omega_5\omega_9 + \omega_5\omega_9\omega_{12} + v_1^2\omega_5\omega_9^2 - 3c_s^2\omega_5\omega_9\omega_{12})\frac{v_2 v_1}{\omega_5\omega_9^2\omega_{12}}$$

$$C_{D_x^2 D_y \rho}^{(1), \text{MRT2}} = C_{D_x^2 D_y \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y \rho}^{(1), \text{CuLBM2}} = (2v_2^2\omega_1\omega_2 + 2\omega_2^2 + 9c_s^2\omega_1\omega_2^2 + 2v_1^2\omega_2^2 - 3\omega_1\omega_2^2 + 2\omega_1\omega_2 + 2v_1^2\omega_1^2 - 6c_s^2\omega_1\omega_2 - 4\omega_1^2 + 3v_2^2\omega_1\omega_2^2 + 12c_s^2\omega_1^2 + 2v_2^2\omega_1^2 + 3\omega_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 - 4v_2^2\omega_2^2 - 6c_s^2\omega_2^2 - 3v_2^2\omega_1^2\omega_2 - 4v_1^2\omega_1\omega_2)\frac{v_2 v_1}{6\omega_1^2\omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_y v_1}^{(1)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{MRT1}} = (c_s^2\omega_5\omega_{12} - \omega_9\omega_{12} + \omega_5\omega_9 + c_s^2\omega_9\omega_{12} - \omega_5\omega_{12} - c_s^2\omega_5\omega_9 - 3v_1^2\omega_9^2 + \omega_9^2 + c_s^2\omega_5\omega_9^2 - \omega_5\omega_9^2 - c_s^2\omega_9^2 + 3v_1^2\omega_5\omega_{12} - 3v_1^2\omega_5\omega_9\omega_{12} + 3v_1^2\omega_9\omega_{12} - 3v_1^2\omega_5\omega_9 + \omega_5\omega_9\omega_{12} + 3v_1^2\omega_5\omega_9^2 - c_s^2\omega_5\omega_9\omega_{12})\frac{v_2 \rho}{\omega_5\omega_9^2\omega_{12}}$$

$$C_{D_x^2 D_y v_1}^{(1), \text{MRT2}} = C_{D_x^2 D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y v_1}^{(1), \text{CuLBM2}} = (\omega_3 v_2^2 \omega_1 \omega_2^2 + \omega_3 \omega_1^2 \omega_2 + 2\omega_3 v_2^2 \omega_1^2 - 4\omega_3 c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 + 3\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_2^2 - 2\omega_3 v_2^2 \omega_2^2 + 2v_2^2 \omega_1 \omega_2^2 - 12\omega_3 v_1^2 \omega_1 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_2^2 - \omega_3 v_2^2 \omega_1^2 \omega_2 + 2\omega_1^2 \omega_2 - 6c_s^2 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_1^2 - 2v_2^2 \omega_1^2 \omega_2 + 6\omega_3 v_1^2 \omega_1^2 + 4\omega_3 \omega_1 \omega_2)\frac{v_2 \rho}{6\omega_3 \omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_y v_2}^{(1)} \text{ at } \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_2}^{(1), \text{SRT}} = (12 - 12v_1^2 + 12v_1^2\omega - 3v_1^2\omega^2 + 3\omega^2 - 12\omega - 11c_s^2\omega^2 + 36c_s^2\omega - 36c_s^2)\frac{v_1\rho}{12\omega^2}$$

$$C_{D_x^2 D_y v_2}^{(1), \text{MRT1}} = (6\omega_5^2\omega_9\omega_{12} + 42c_s^2\omega_5\omega_9^2\omega_{12} - 18c_s^2\omega_5^2\omega_9\omega_{12} - 6\omega_5\omega_9^2\omega_{12} + 12v_1^2\omega_5^2\omega_9^2 + 6v_1^2\omega_5\omega_9^2\omega_{12} + 12v_1^2\omega_5^2\omega_{12} - 12v_1^2\omega_5^2\omega_9 - 6v_1^2\omega_5^2\omega_9\omega_{12} - 12c_s^2\omega_5\omega_9^2 + 12\omega_5\omega_9^2 + 12c_s^2\omega_5^2\omega_9^2 - 3v_1^2\omega_5^2\omega_9^2\omega_{12} - 12\omega_5^2\omega_9^2 - 11c_s^2\omega_5^2\omega_9^2\omega_{12} - 12v_1^2\omega_5\omega_9^2 + 36c_s^2\omega_5^2\omega_{12} - 24c_s^2\omega_5\omega_9\omega_{12} + 3\omega_5^2\omega_9^2\omega_{12} + 12\omega_5^2\omega_9 - 12\omega_5^2\omega_{12} - 24c_s^2\omega_9^2\omega_{12} - 12c_s^2\omega_5^2\omega_9)\frac{v_1\rho}{12\omega_5^2\omega_9^2\omega_{12}}$$

$$C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{MRT}^2} = C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{MRT}^1}$$

$$C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{CLBM}^1} = (36c_s^2\omega_5\omega_{12} + 12\omega_5\omega_9 - 11c_s^2\omega_5\omega_9^2\omega_{12} - 12\omega_5\omega_{12} - 36c_s^2\omega_5\omega_9 + 3\omega_5\omega_9^2\omega_{12} - 3v_1^2\omega_5\omega_9^2\omega_{12} - 12v_1^2\omega_9^2 + 6v_1^2\omega_9^2\omega_{12} + 12\omega_9^2 + 36c_s^2\omega_5\omega_9^2 - 12\omega_5\omega_9^2 - 36c_s^2\omega_9^2 + 12v_1^2\omega_5\omega_{12} - 6v_1^2\omega_5\omega_9\omega_{12} - 12v_1^2\omega_5\omega_9 + 6\omega_5\omega_9\omega_{12} + 12v_1^2\omega_5\omega_9^2 - 6\omega_9^2\omega_{12} - 18c_s^2\omega_5\omega_9\omega_{12} + 18c_s^2\omega_9^2\omega_{12}) \frac{v_1\rho}{12\omega_5\omega_9^2\omega_{12}}$$

$$C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{CLBM}^2} = C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{CLBM}^1}$$

$$C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{CuLBM}^1} = (12v_1^2\omega_1^2\omega_1 - 6v_1^2\omega_4\omega_1\omega_9 + 6v_1^2\omega_4^2\omega_9 + 36c_s^2\omega_1\omega_9 - 12\omega_1\omega_9 + 12\omega_4^2 - 36c_s^2\omega_4\omega_1 - 18c_s^2\omega_4\omega_1\omega_9 + 12\omega_4\omega_1 - 12v_1^2\omega_4^2 + 6\omega_4\omega_1\omega_9 + 12v_1^2\omega_1\omega_9 - 11c_s^2\omega_4^2\omega_1\omega_9 + 36c_s^2\omega_4^2\omega_1 - 6\omega_4^2\omega_9 + 3\omega_4^2\omega_1\omega_9 + 18c_s^2\omega_4^2\omega_9 - 36c_s^2\omega_4^2 - 12\omega_4^2\omega_1 - 3v_1^2\omega_4^2\omega_1\omega_9 - 12v_1^2\omega_4\omega_1) \frac{v_1\rho}{12\omega_4^2\omega_1\omega_9}$$

$$C_{\mathbf{D}_x^2 \mathbf{D}_y v_2}^{(1), \text{CuLBM}^2} = (18\omega_3v_2^2\omega_4\omega_1\omega_2^2 - 8\omega_3\omega_4\omega_1\omega_2^2 - 3\omega_3v_1^2\omega_4\omega_1^2\omega_2^2 + 12\omega_3v_2^2\omega_4\omega_1^2 + 6\omega_3v_1^2\omega_1^2\omega_2^2 - 8v_1^2\omega_4\omega_1\omega_2^2 + 16\omega_3c_s^2\omega_4\omega_2^2 - 12\omega_3c_s^2\omega_4\omega_1^2\omega_2 - 11\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 + 16\omega_3c_s^2\omega_4\omega_1^2 - 36\omega_3c_s^2\omega_1\omega_2^2 - 24c_s^2\omega_4\omega_1\omega_2^2 - 6\omega_3\omega_1^2\omega_2^2 + 12\omega_3v_2^2\omega_4\omega_1\omega_2 - 24\omega_3v_2^2\omega_4\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2 - 2\omega_3v_1^2\omega_4\omega_1^2\omega_2 + 8\omega_4\omega_1\omega_2^2 + 12\omega_3\omega_1\omega_2^2 + 8\omega_3v_1^2\omega_4\omega_2^2 - 4v_1^2\omega_4\omega_1^2\omega_2 + 8\omega_3\omega_4\omega_1^2\omega_2 - 18\omega_3v_2^2\omega_4\omega_1^2\omega_2 - 8\omega_3\omega_4\omega_1^2 - 6\omega_4\omega_1^2\omega_2^2 + 12\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 18\omega_3c_s^2\omega_1^2\omega_2^2 + 18c_s^2\omega_4\omega_1^2\omega_2^2 - 12c_s^2\omega_4\omega_1^2\omega_2 + 4\omega_3c_s^2\omega_4\omega_1\omega_2 + 3\omega_3\omega_4\omega_1^2\omega_2^2 + 4\omega_3v_1^2\omega_4\omega_1^2 + 4\omega_4\omega_1^2\omega_2 + 2\omega_3v_1^2\omega_4\omega_1\omega_2^2 - 12\omega_3v_1^2\omega_1\omega_2^2 + 6v_1^2\omega_4\omega_1^2\omega_2^2) \frac{v_1\rho}{12\omega_3\omega_4\omega_1^2\omega_2^2}$$

$$\text{coefficient } C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_1 \partial x_2^2} :$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{MRT}^1} = (-12 + 12\omega_5 - \omega_5^2) \frac{c_s^4}{6\omega_5^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{MRT}^2} = C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{MRT}^1}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{CLBM}^1} = C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{MRT}^1}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{CLBM}^2} = C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{MRT}^1}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{CuLBM}^1} = (-12 - \omega_1^2 + 12\omega_1) \frac{c_s^4}{6\omega_1^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 \rho}^{(1), \text{CuLBM}^2} = (2v_2^4\omega_1^2 - 2v_2^2\omega_1\omega_2 + 2c_s^4\omega_1^2 + 6c_s^2v_2^2\omega_1\omega_2 - 2c_s^2\omega_1\omega_2^2 + 3v_2^4\omega_1\omega_2^2 - 14c_s^4\omega_2^2 + 2v_2^4\omega_1\omega_2 + 15c_s^2v_2^2\omega_1\omega_2^2 + 14c_s^4\omega_1\omega_2^2 - 4v_2^4\omega_2^2 - 3v_2^2\omega_1\omega_2^2 - 2c_s^2\omega_1^2 - c_s^4\omega_1^2\omega_2^2 - 2v_2^2\omega_1^2 - 3v_2^4\omega_1^2\omega_2 + 2c_s^2\omega_1^2\omega_2 + 12c_s^2v_2^2\omega_1^2 - 15c_s^2v_2^2\omega_1^2\omega_2 + 4v_2^2\omega_2^2 - 18c_s^2v_2^2\omega_2^2 + 2c_s^2\omega_2^2 + 3v_2^2\omega_1^2\omega_2 - 2c_s^4\omega_1^2\omega_2) \frac{1}{6\omega_1^2\omega_2^2}$$

$$\text{coefficient } C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1)} \text{ at } \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} :$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{SRT}} = \frac{-c_s^2 v_1 \rho}{6}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{MRT}^1} = (-12\omega_9\omega_{12} - \omega_5^2\omega_9\omega_{12} + 12\omega_5\omega_9 - 12\omega_5\omega_{12} + 12\omega_5\omega_9\omega_{12} + 12\omega_5^2 - 12\omega_5^2\omega_9) \frac{c_s^2 v_1 \rho}{6\omega_5^2\omega_9\omega_{12}}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{MRT}^2} = C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{MRT}^1}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{CLBM}^1} = C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{SRT}}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{CLBM}^2} = C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{SRT}}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{CuLBM}^1} = C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{SRT}}$$

$$C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{CuLBM}^2} = C_{\mathbf{D}_x \mathbf{D}_y^2 v_1}^{(1), \text{SRT}}$$

$$\text{coefficient } C_{\mathbf{D}_x \mathbf{D}_y^2 v_2}^{(1)} \text{ at } \frac{\partial^3 v_2}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{MRT1}} = (\omega_5 \omega_{15} + 2\omega_5 - 2\omega_{15} - \omega_5^2) \frac{c_s^2 v_2 \rho}{\omega_5^2 \omega_{15}}$$

$$C_{D_x D_y^2 v_2}^{(1), \text{MRT2}} = C_{D_x D_y^2 v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 v_2}^{(1), \text{CuLBM2}} = (6v_2^2 \omega_1 \omega_2 + 6\omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 5\omega_1 \omega_2^2 - 2\omega_1 \omega_2 + 2c_s^2 \omega_1 \omega_2 - 4\omega_1^2 + 11v_2^2 \omega_1 \omega_2^2 + 8c_s^2 \omega_1^2 + 8v_2^2 \omega_1^2 + 5\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 - 14v_2^2 \omega_2^2 - 10c_s^2 \omega_2^2 - 11v_2^2 \omega_1^2 \omega_2) \frac{v_2 \rho}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^3 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^3}$:

$$C_{D_y^3 \rho}^{(1), \text{SRT}} = (-1 + 3c_s^2 + v_2^2) \frac{v_2 v_1}{12}$$

$$C_{D_y^3 \rho}^{(1), \text{MRT1}} = (6v_2^2 \omega_{10} \omega_5 - 18c_s^2 \omega_5 \omega_{15} + 6\omega_5 \omega_{15} + 18c_s^2 \omega_{10} \omega_5 + 12\omega_{10} - \omega_{10} \omega_5 \omega_{15} - 6\omega_{10} \omega_5 - 6v_2^2 \omega_5 \omega_{15} + 3c_s^2 \omega_{10} \omega_5 \omega_{15} - 36c_s^2 \omega_{10} - 12v_2^2 \omega_{10} + 36c_s^2 \omega_{15} + v_2^2 \omega_{10} \omega_5 \omega_{15} - 12\omega_{15} + 12v_2^2 \omega_{15}) \frac{v_2 v_1}{12\omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_y^3 \rho}^{(1), \text{MRT2}} = C_{D_y^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(1), \text{CLBM1}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(1), \text{CLBM2}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(1), \text{CuLBM1}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(1), \text{CuLBM2}} = C_{D_y^3 \rho}^{(1), \text{SRT}}$$

coefficient $C_{D_y^3 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_2^3}$:

$$C_{D_y^3 v_1}^{(1), \text{SRT}} = (6 + \omega^2 - 6\omega - 3c_s^2 \omega^2 - v_2^2 \omega^2 + 6v_2^2 \omega + 18c_s^2 \omega - 18c_s^2 - 6v_2^2) \frac{v_2 \rho}{6\omega^2}$$

$$C_{D_y^3 v_1}^{(1), \text{MRT1}} = (3c_s^2 \omega_5^2 + 15c_s^2 \omega_5 \omega_{15} + 3v_2^2 \omega_5^2 - 3\omega_5 \omega_{15} - 6v_2^2 \omega_5 - 6c_s^2 \omega_5 + 3v_2^2 \omega_5 \omega_{15} - v_2^2 \omega_5^2 \omega_{15} + 6\omega_5 - 3c_s^2 \omega_5^2 \omega_{15} - 12c_s^2 \omega_{15} + \omega_5^2 \omega_{15} - 3\omega_5^2) \frac{v_2 \rho}{6\omega_5^2 \omega_{15}}$$

$$C_{D_y^3 v_1}^{(1), \text{MRT2}} = C_{D_y^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^3 v_1}^{(1), \text{CLBM1}} = (6 - 3c_s^2 \omega_5 \omega_{15} + \omega_5 \omega_{15} + 3v_2^2 \omega_5 + 9c_s^2 \omega_5 - v_2^2 \omega_5 \omega_{15} - 3\omega_5 + 9c_s^2 \omega_{15} - 3\omega_{15} - 18c_s^2 - 6v_2^2 + 3v_2^2 \omega_{15}) \frac{v_2 \rho}{6\omega_5 \omega_{15}}$$

$$C_{D_y^3 v_1}^{(1), \text{CLBM2}} = C_{D_y^3 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_y^3 v_1}^{(1), \text{CuLBM1}} = (6 - 3\omega_7 - 3\omega_1 - 3c_s^2 \omega_7 \omega_1 + 3v_2^2 \omega_7 + \omega_7 \omega_1 + 9c_s^2 \omega_7 - v_2^2 \omega_7 \omega_1 + 3v_2^2 \omega_1 - 18c_s^2 + 9c_s^2 \omega_1 - 6v_2^2) \frac{v_2 \rho}{6\omega_7 \omega_1}$$

$$C_{D_y^3 v_1}^{(1), \text{CuLBM2}} = (6\omega_3 + 3v_2^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_1 - 18\omega_3 c_s^2 + 9\omega_3 c_s^2 \omega_1 + 9c_s^2 \omega_4 \omega_1 - 3\omega_4 \omega_1 - 6\omega_3 v_2^2 + 6\omega_3 v_2^2 \omega_4 + 3\omega_3 v_2^2 \omega_1 - 2\omega_3 v_2^2 \omega_4 \omega_1 + 6\omega_4 + 18\omega_3 c_s^2 \omega_4 - 6\omega_3 \omega_4 - 3\omega_3 \omega_1 - 18c_s^2 \omega_4 - 6v_2^2 \omega_4 + 2\omega_3 \omega_4 \omega_1) \frac{v_2 \rho}{12\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_y^3 v_2}^{(1)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^3}$:

$$C_{D_y^3 v_2}^{(1), \text{SRT}} = (-1 + c_s^2 + 3v_2^2) \frac{v_1 \rho}{12}$$

$$C_{D_y^3 v_2}^{(1), \text{MRT1}} = (18v_2^2 \omega_{10} \omega_5 - 6c_s^2 \omega_5 \omega_{15} + 6\omega_5 \omega_{15} + 6c_s^2 \omega_{10} \omega_5 + 12\omega_{10} - \omega_{10} \omega_5 \omega_{15} - 6\omega_{10} \omega_5 - 18v_2^2 \omega_5 \omega_{15} + c_s^2 \omega_{10} \omega_5 \omega_{15} - 12c_s^2 \omega_{10} - 36v_2^2 \omega_{10} + 12c_s^2 \omega_{15} + 3v_2^2 \omega_{10} \omega_5 \omega_{15} - 12\omega_{15} + 36v_2^2 \omega_{15}) \frac{v_1 \rho}{12\omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_y^3 v_2}^{(1), \text{MRT2}} = C_{D_y^3 v_2}^{(1), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(1), \text{CLBM1}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(1), \text{CLBM2}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(1), \text{CuLBM1}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(1), \text{CuLBM2}} = C_{D_y^3 v_2}^{(1), \text{SRT}}$$

$$\text{coefficient } C_{D_x^2 D_z \rho}^{(1)} \text{ at } \frac{\partial^3 \rho}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{MRT1}} = (\omega_6 v_1^2 \omega_{13} + \omega_6 v_1^2 \omega_9^2 - v_1^2 \omega_9^2 + v_1^2 \omega_{13} \omega_9 + \omega_9^2 - 3\omega_6 c_s^2 \omega_{13} \omega_9 - \omega_6 v_1^2 \omega_9 - 3c_s^2 \omega_9^2 - 3\omega_6 c_s^2 \omega_9 + \omega_6 \omega_{13} \omega_9 - \omega_6 \omega_{13} - \omega_6 \omega_9^2 - \omega_6 v_1^2 \omega_{13} \omega_9 + \omega_6 \omega_9 + 3\omega_6 c_s^2 \omega_{13} + 3\omega_6 c_s^2 \omega_9^2 - \omega_{13} \omega_9 + 3c_s^2 \omega_{13} \omega_9) \frac{v_3 v_1}{\omega_6 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z \rho}^{(1), \text{MRT2}} = C_{D_x^2 D_z \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z \rho}^{(1), \text{CuLBM2}} = (2\omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 + 2v_1^2 \omega_2^2 - 3\omega_1 \omega_2^2 + 2\omega_1 \omega_2 + 2v_1^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 - 4\omega_1^2 - 3v_3^2 \omega_1^2 \omega_2 + 12c_s^2 \omega_1^2 - 4v_3^2 \omega_2^2 + 2v_3^2 \omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 + 2v_3^2 \omega_1^2 - 6c_s^2 \omega_2^2 + 3v_3^2 \omega_1 \omega_2^2 - 4v_1^2 \omega_1 \omega_2) \frac{v_3 v_1}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_x^2 D_z v_1}^{(1)} \text{ at } \frac{\partial^3 v_1}{\partial x_1^2 \partial x_3} :$$

$$C_{D_x^2 D_z v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{MRT1}} = (3\omega_6 v_1^2 \omega_{13} + 3\omega_6 v_1^2 \omega_9^2 - 3v_1^2 \omega_9^2 + 3v_1^2 \omega_{13} \omega_9 + \omega_9^2 - \omega_6 c_s^2 \omega_{13} \omega_9 - 3\omega_6 v_1^2 \omega_9 - c_s^2 \omega_9^2 - \omega_6 c_s^2 \omega_9 + \omega_6 \omega_{13} \omega_9 - \omega_6 \omega_{13} - \omega_6 \omega_9^2 - 3\omega_6 v_1^2 \omega_{13} \omega_9 + \omega_6 \omega_9 + \omega_6 c_s^2 \omega_{13} + \omega_6 c_s^2 \omega_9^2 - \omega_{13} \omega_9 + c_s^2 \omega_{13} \omega_9) \frac{v_3 \rho}{\omega_6 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z v_1}^{(1), \text{MRT2}} = C_{D_x^2 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(1), \text{CuLBM2}} = (-\omega_3 v_3^2 \omega_1^2 \omega_2 + \omega_3 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 + 3\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_2^2 + 2\omega_3 v_3^2 \omega_1^2 - 2v_3^2 \omega_1^2 \omega_2 - 12\omega_3 v_1^2 \omega_1 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_2^2 + \omega_3 v_3^2 \omega_1 \omega_2^2 + 2\omega_1^2 \omega_2 - 6c_s^2 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_1^2 + 6\omega_3 v_1^2 \omega_1^2 + 2v_3^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2) \frac{v_3 \rho}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_z v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_3}^{(1), \text{SRT}} = (12 - 12v_1^2 + 12v_1^2\omega - 3v_1^2\omega^2 + 3\omega^2 - 12\omega - 11c_s^2\omega^2 + 36c_s^2\omega - 36c_s^2) \frac{v_1\rho}{12\omega^2}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{MRT1}} = (-12\omega_6 v_1^2 \omega_9^2 + 3\omega_6^2 \omega_{13} \omega_9^2 + 42\omega_6 c_s^2 \omega_{13} \omega_9^2 + 12\omega_6^2 c_s^2 \omega_9^2 + 36\omega_6^2 c_s^2 \omega_{13} - 3\omega_6^2 v_1^2 \omega_{13} \omega_9^2 + 12\omega_6^2 \omega_9 - 12\omega_6^2 \omega_{13} - 12\omega_6^2 \omega_9^2 - 6\omega_6^2 v_1^2 \omega_{13} \omega_9 + 6\omega_6^2 \omega_{13} \omega_9 - 12\omega_6^2 c_s^2 \omega_9 - 24\omega_6 c_s^2 \omega_{13} \omega_9 - 24c_s^2 \omega_{13} \omega_9^2 - 11\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 6\omega_6 v_1^2 \omega_{13} \omega_9^2 - 12\omega_6^2 v_1^2 \omega_9 + 12\omega_6 \omega_9^2 + 12\omega_6^2 v_1^2 \omega_9^2 + 12\omega_6^2 v_1^2 \omega_{13} - 12\omega_6 c_s^2 \omega_9^2 - 6\omega_6 \omega_{13} \omega_9^2 - 18\omega_6^2 c_s^2 \omega_{13} \omega_9) \frac{v_1\rho}{12\omega_6^2 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{MRT2}} = C_{D_x^2 D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CLBM1}} = (12\omega_6 v_1^2 \omega_{13} + 12\omega_6 v_1^2 \omega_9^2 - 11\omega_6 c_s^2 \omega_{13} \omega_9^2 + 6v_1^2 \omega_{13} \omega_9^2 - 12v_1^2 \omega_9^2 + 12\omega_9^2 - 18\omega_6 c_s^2 \omega_{13} \omega_9 - 12\omega_6 v_1^2 \omega_9 + 18c_s^2 \omega_{13} \omega_9^2 - 36c_s^2 \omega_9^2 - 6\omega_{13} \omega_9^2 - 36\omega_6 c_s^2 \omega_9 + 6\omega_6 \omega_{13} \omega_9 - 3\omega_6 v_1^2 \omega_{13} \omega_9^2 - 12\omega_6 \omega_{13} - 12\omega_6 \omega_9^2 - 6\omega_6 v_1^2 \omega_{13} \omega_9 + 12\omega_6 \omega_9 + 36\omega_6 c_s^2 \omega_{13} + 36\omega_6 c_s^2 \omega_9^2 + 3\omega_6 \omega_{13} \omega_9^2) \frac{v_1\rho}{12\omega_6 \omega_{13} \omega_9^2}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CLBM2}} = C_{D_x^2 D_z v_3}^{(1), \text{CLBM1}}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CuLBM1}} = (6v_1^2 \omega_4^2 \omega_{12} - 3v_1^2 \omega_4^2 \omega_2 \omega_{12} - 36c_s^2 \omega_4 \omega_2 + 12\omega_4 \omega_2 + 12\omega_4^2 - 11c_s^2 \omega_4^2 \omega_2 \omega_{12} + 12v_1^2 \omega_2 \omega_{12} + 3\omega_4^2 \omega_2 \omega_{12} + 12v_1^2 \omega_4^2 \omega_2 - 12v_1^2 \omega_4^2 - 18c_s^2 \omega_4 \omega_2 \omega_{12} - 12v_1^2 \omega_4 \omega_2 + 18c_s^2 \omega_4^2 \omega_{12} + 6\omega_4 \omega_2 \omega_{12} - 6\omega_4^2 \omega_{12} - 36c_s^2 \omega_4^2 - 6v_1^2 \omega_4 \omega_2 \omega_{12} + 36c_s^2 \omega_4^2 \omega_{12} - 12\omega_4^2 \omega_2 - 12\omega_2 \omega_{12} + 36c_s^2 \omega_2 \omega_{12}) \frac{v_1\rho}{12\omega_4^2 \omega_2 \omega_{12}}$$

$$C_{D_x^2 D_z v_3}^{(1), \text{CuLBM2}} = (-8\omega_3 \omega_4 \omega_1 \omega_2^2 - 3\omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2^2 + 6\omega_3 v_1^2 \omega_1^2 \omega_2^2 - 8v_1^2 \omega_4 \omega_1 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_2^2 + 18\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 - 11\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_1^2 - 36\omega_3 c_s^2 \omega_1 \omega_2^2 - 24c_s^2 \omega_4 \omega_1 \omega_2^2 + 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 - 6\omega_3 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 2\omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_4 \omega_1 \omega_2^2 + 12\omega_3 \omega_1 \omega_2^2 + 8\omega_3 v_1^2 \omega_4 \omega_2^2 + 12\omega_3 v_3^2 \omega_4 \omega_1^2 - 4v_1^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1^2 - 6\omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 18\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12c_s^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 24\omega_3 v_3^2 \omega_4 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_3 v_1^2 \omega_4 \omega_1^2 + 4\omega_4 \omega_1^2 \omega_2 + 2\omega_3 v_1^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 v_1^2 \omega_1 \omega_2^2 + 6v_1^2 \omega_4 \omega_1^2 \omega_2^2) \frac{v_1\rho}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{MRT1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{MRT2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(1), \text{CuLBM2}} = (-2v_2^2 \omega_1 \omega_2 - 2\omega_2^2 + 4\omega_1 \omega_2 - 12c_s^2 \omega_1 \omega_2 - 2\omega_1^2 + 6c_s^2 \omega_1^2 + v_3^2 \omega_2^2 - 2v_3^2 \omega_1 \omega_2 + v_2^2 \omega_1^2 + v_2^2 \omega_2^2 + v_3^2 \omega_1^2 + 6c_s^2 \omega_2^2) \frac{v_3 v_2}{3\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_2}^{(1)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{MRT1}} = (-\omega_6 \omega_5^2 + \omega_6 \omega_5 - \omega_6 \omega_8 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5 + \omega_5^2) \frac{v_3 c_s^2 \rho}{\omega_6 \omega_8 \omega_5^2}$$

$$C_{D_x D_y D_z v_2}^{(1), \text{MRT2}} = C_{D_x D_y D_z v_2}^{(1), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_2}^{(1), \text{CuLBM2}} = (-\omega_3 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_2^2 \omega_4 \omega_1^2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 + \omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 3v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 - 2v_3^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 3\omega_3 v_3^2 \omega_1^2 \omega_2^2 - 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 v_2^2 \omega_4 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 + 2\omega_3 v_3^2 \omega_4 \omega_1^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 v_3^2 \omega_1 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - \omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 4v_3^2 \omega_4 \omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_4 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2) \frac{v_3 \rho}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{MRT1}} = (\omega_6 \omega_5 - \omega_6 \omega_8 + \omega_6 \omega_8 \omega_5 + \omega_6^2 - \omega_6^2 \omega_5 - \omega_8 \omega_5) \frac{c_s^2 v_2 \rho}{\omega_6^2 \omega_8 \omega_5}$$

$$C_{D_x D_y D_z v_3}^{(1), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(1), \text{CuLBM2}} = (\omega_3 v_2^2 \omega_4 \omega_1 \omega_2^2 - \omega_3 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_2^2 \omega_1 \omega_2^2 + 2\omega_3 v_2^2 \omega_4 \omega_1^2 + 3v_2^2 \omega_4 \omega_1^2 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 + 3\omega_3 \omega_1^2 \omega_2^2 - 2v_2^2 \omega_4 \omega_1^2 \omega_2 - 2\omega_3 v_2^2 \omega_4 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 + 6\omega_3 v_3^2 \omega_4 \omega_1^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - \omega_3 v_2^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 3\omega_3 v_2^2 \omega_1^2 \omega_2^2 + 6\omega_3 v_3^2 \omega_4 \omega_2^2 + 2\omega_4 \omega_1^2 \omega_2 - 4v_2^2 \omega_4 \omega_1 \omega_2^2) \frac{v_2 \rho}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{MRT1}} = (-\omega_6 \omega_5^2 + \omega_6 \omega_5 - \omega_6 \omega_8 + \omega_6 \omega_8 \omega_5 - \omega_8 \omega_5 + \omega_5^2) \frac{v_3 c_s^2 \rho}{\omega_6 \omega_8 \omega_5^2}$$

$$C_{D_y^2 D_z v_1}^{(1), \text{MRT2}} = C_{D_y^2 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z v_1}^{(1), \text{CuLBM2}} = (-2\omega_3 - \omega_3 v_3^2 \omega_1 + 6\omega_3 c_s^2 - 3\omega_3 c_s^2 \omega_1 + 3c_s^2 \omega_4 \omega_1 - \omega_4 \omega_1 + 2\omega_4 + 2\omega_3 v_3^2 + v_3^2 \omega_4 \omega_1 + \omega_3 \omega_1 - 2v_3^2 \omega_4 - 6c_s^2 \omega_4) \frac{v_3 \rho}{4\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_y^2 D_z v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_3}^{(1), \text{SRT}} = \frac{-c_s^2 v_1 \rho}{6}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{MRT1}} = (6\omega_7 \omega_5 - 6\omega_6 \omega_7 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_7 + 6\omega_6 \omega_8 \omega_5 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_8 \omega_5) \frac{c_s^2 v_1 \rho}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{MRT2}} = C_{D_y^2 D_z v_3}^{(1), \text{MRT1}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CLBM1}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CLBM2}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CuLBM1}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(1), \text{CuLBM2}} = C_{D_y^2 D_z v_3}^{(1), \text{SRT}}$$

coefficient $C_{D_x D_z^2 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 \rho}^{(1), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{MRT1}} = (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4}{6\omega_6^2}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{MRT2}} = C_{D_x D_z^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CLBM1}} = C_{D_x D_z^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CLBM2}} = C_{D_x D_z^2 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CuLBM1}} = (-12 - \omega_2^2 + 12\omega_2) \frac{c_s^4}{6\omega_2^2}$$

$$C_{D_x D_z^2 \rho}^{(1), \text{CuLBM2}} = (-15v_3^2 c_s^2 \omega_1^2 \omega_2 + 2c_s^4 \omega_1^2 - 4v_3^4 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 - 18v_3^2 c_s^2 \omega_2^2 - 3v_3^4 \omega_1^2 \omega_2 + 2v_3^4 \omega_1^2 - 14c_s^4 \omega_2^2 + 12v_3^2 c_s^2 \omega_1^2 + 14c_s^4 \omega_1 \omega_2^2 + 3v_3^2 \omega_1^2 \omega_2 - 2c_s^2 \omega_1^2 + 4v_3^2 \omega_2^2 + 15v_3^2 c_s^2 \omega_1 \omega_2^2 - c_s^4 \omega_1^2 \omega_2^2 - 2v_3^2 \omega_1 \omega_2 + 3v_3^4 \omega_1 \omega_2^2 + 2c_s^2 \omega_1^2 \omega_2 + 2v_3^4 \omega_1 \omega_2 - 2v_3^2 \omega_1^2 + 2c_s^2 \omega_2^2 - 3v_3^2 \omega_1 \omega_2^2 + 6v_3^2 c_s^2 \omega_1 \omega_2 - 2c_s^4 \omega_1^2 \omega_2) \frac{1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_1}^{(1), \text{SRT}} = \frac{-c_s^2 v_1 \rho}{6}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{MRT1}} = (-12\omega_6^2 \omega_9 - \omega_6^2 \omega_{13} \omega_9 + 12\omega_6^2 + 12\omega_6 \omega_{13} \omega_9 - 12\omega_6 \omega_{13} + 12\omega_6 \omega_9 - 12\omega_{13} \omega_9) \frac{c_s^2 v_1 \rho}{6\omega_6^2 \omega_{13} \omega_9}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{MRT2}} = C_{D_x D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CLBM1}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CLBM2}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CuLBM1}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(1), \text{CuLBM2}} = C_{D_x D_z^2 v_1}^{(1), \text{SRT}}$$

coefficient $C_{D_x D_z^2 v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_3}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{MRT1}} = (2\omega_6 - \omega_6^2 + \omega_6 \omega_{18} - 2\omega_{18}) \frac{v_3 c_s^2 \rho}{\omega_6^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_3}^{(1), \text{MRT2}} = C_{D_x D_z^2 v_3}^{(1), \text{MRT1}}$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_z^2 v_3}^{(1), \text{CuLBM1}} = 0$$

$$C_{\text{D}_x \text{D}_z^2 v_3}^{(1), \text{CuLBM2}} = (6\omega_2^2 + 9c_s^2\omega_1\omega_2^2 - 5\omega_1\omega_2^2 - 2\omega_1\omega_2 + 2c_s^2\omega_1\omega_2 - 4\omega_1^2 - 11v_3^2\omega_1^2\omega_2 + 8c_s^2\omega_1^2 - 14v_3^2\omega_2^2 + 6v_3^2\omega_1\omega_2 + 5\omega_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 + 8v_3^2\omega_1^2 - 10c_s^2\omega_2^2 + 11v_3^2\omega_1\omega_2^2) \frac{v_3\rho}{6\omega_1^2\omega_2^2}$$

coefficient $C_{\text{D}_y \text{D}_z^2 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_2 \partial x_3^2}$:

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{SRT}} = 0$$

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{MRT1}} = (\omega_6\omega_5 - \omega_6\omega_8 + \omega_6\omega_8\omega_5 + \omega_6^2 - \omega_6^2\omega_5 - \omega_8\omega_5) \frac{c_s^2 v_2 \rho}{\omega_6^2 \omega_8 \omega_5}$$

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{MRT2}} = C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{\text{D}_y \text{D}_z^2 v_1}^{(1), \text{CuLBM2}} = (-2\omega_3 + v_2^2\omega_4\omega_1 + 6\omega_3c_s^2 - 3\omega_3c_s^2\omega_1 + 3c_s^2\omega_4\omega_1 - \omega_4\omega_1 + 2\omega_3v_2^2 - \omega_3v_2^2\omega_1 + 2\omega_4 + \omega_3\omega_1 - 6c_s^2\omega_4 - 2v_2^2\omega_4) \frac{v_2\rho}{4\omega_3\omega_4\omega_1}$$

coefficient $C_{\text{D}_y \text{D}_z^2 v_2}^{(1)}$ **at** $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$:

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{SRT}} = \frac{-c_s^2 v_1 \rho}{6}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{MRT1}} = (6\omega_7\omega_5 - 6\omega_6\omega_7\omega_5 - 6\omega_6\omega_8 + 6\omega_6\omega_7 + 6\omega_6\omega_8\omega_5 - \omega_6\omega_7\omega_8\omega_5 - 6\omega_8\omega_5) \frac{c_s^2 v_1 \rho}{6\omega_6\omega_7\omega_8\omega_5}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{MRT2}} = C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{MRT1}}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{CLBM1}} = C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{SRT}}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{CLBM2}} = C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{SRT}}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{CuLBM1}} = C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{SRT}}$$

$$C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{CuLBM2}} = C_{\text{D}_y \text{D}_z^2 v_2}^{(1), \text{SRT}}$$

coefficient $C_{\text{D}_z^3 \rho}^{(1)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{\text{D}_z^3 \rho}^{(1), \text{SRT}} = (-1 + v_3^2 + 3c_s^2) \frac{v_3 v_1}{12}$$

$$C_{\text{D}_z^3 \rho}^{(1), \text{MRT1}} = (-6\omega_6\omega_{11} + 6\omega_6v_3^2\omega_{11} - 36c_s^2\omega_{11} + 3\omega_6c_s^2\omega_{11}\omega_{18} - 12v_3^2\omega_{11} + 18\omega_6c_s^2\omega_{11} + \omega_6v_3^2\omega_{11}\omega_{18} - \omega_6\omega_{11}\omega_{18} + 12\omega_{11} + 6\omega_6\omega_{18} - 6\omega_6v_3^2\omega_{18} + 36c_s^2\omega_{18} + 12v_3^2\omega_{18} - 12\omega_{18} - 18\omega_6c_s^2\omega_{18}) \frac{v_3 v_1}{12\omega_6\omega_{11}\omega_{18}}$$

$$C_{\text{D}_z^3 \rho}^{(1), \text{MRT2}} = C_{\text{D}_z^3 \rho}^{(1), \text{MRT1}}$$

$$C_{\text{D}_z^3 \rho}^{(1), \text{CLBM1}} = C_{\text{D}_z^3 \rho}^{(1), \text{SRT}}$$

$$C_{\text{D}_z^3 \rho}^{(1), \text{CLBM2}} = C_{\text{D}_z^3 \rho}^{(1), \text{SRT}}$$

$$C_{\text{D}_z^3 \rho}^{(1), \text{CuLBM1}} = C_{\text{D}_z^3 \rho}^{(1), \text{SRT}}$$

$$C_{\text{D}_z^3 \rho}^{(1), \text{CuLBM2}} = C_{\text{D}_z^3 \rho}^{(1), \text{SRT}}$$

coefficient $C_{D_z^3 v_1}^{(1)}$ **at** $\frac{\partial^3 v_1}{\partial x_3^3}$:

$$C_{D_z^3 v_1}^{(1), \text{SRT}} = (6 + \omega^2 - 6\omega + 6v_3^2\omega - 3c_s^2\omega^2 - 6v_3^2 + 18c_s^2\omega - 18c_s^2 - v_3^2\omega^2) \frac{v_3\rho}{6\omega^2}$$

$$C_{D_z^3 v_1}^{(1), \text{MRT1}} = (-6\omega_6 v_3^2 + 6\omega_6 - 6\omega_6 c_s^2 - 3\omega_6^2 c_s^2 \omega_{18} - \omega_6^2 v_3^2 \omega_{18} + \omega_6^2 \omega_{18} - 3\omega_6^2 - 3\omega_6 \omega_{18} + 3\omega_6 v_3^2 \omega_{18} - 12c_s^2 \omega_{18} + 3\omega_6^2 c_s^2 + 3\omega_6^2 v_3^2 + 15\omega_6 c_s^2 \omega_{18}) \frac{v_3\rho}{6\omega_6^2 \omega_{18}}$$

$$C_{D_z^3 v_1}^{(1), \text{MRT2}} = C_{D_z^3 v_1}^{(1), \text{MRT1}}$$

$$C_{D_z^3 v_1}^{(1), \text{CLBM1}} = (6 + 3\omega_6 v_3^2 - 3\omega_6 + 9\omega_6 c_s^2 + \omega_6 \omega_{18} - \omega_6 v_3^2 \omega_{18} + 9c_s^2 \omega_{18} + 3v_3^2 \omega_{18} - 3\omega_{18} - 6v_3^2 - 18c_s^2 - 3\omega_6 c_s^2 \omega_{18}) \frac{v_3\rho}{6\omega_6 \omega_{18}}$$

$$C_{D_z^3 v_1}^{(1), \text{CLBM2}} = C_{D_z^3 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_z^3 v_1}^{(1), \text{CuLBM1}} = (6 - 3c_s^2 \omega_8 \omega_2 + 3v_3^2 \omega_8 + \omega_8 \omega_2 + 9c_s^2 \omega_8 + 9c_s^2 \omega_2 - 3\omega_8 - 3\omega_2 - 6v_3^2 - v_3^2 \omega_8 \omega_2 - 18c_s^2 + 3v_3^2 \omega_2) \frac{v_3\rho}{6\omega_8 \omega_2}$$

$$C_{D_z^3 v_1}^{(1), \text{CuLBM2}} = (6\omega_3 v_3^2 \omega_4 + 6\omega_3 + 3\omega_3 v_3^2 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_1 - 18\omega_3 c_s^2 + 9\omega_3 c_s^2 \omega_1 + 9c_s^2 \omega_4 \omega_1 - 3\omega_4 \omega_1 + 6\omega_4 + 18\omega_3 c_s^2 \omega_4 - 6\omega_3 v_3^2 + 3v_3^2 \omega_4 \omega_1 - 6\omega_3 \omega_4 - 3\omega_3 \omega_1 - 6v_3^2 \omega_4 - 18c_s^2 \omega_4 + 2\omega_3 \omega_4 \omega_1 - 2\omega_3 v_3^2 \omega_4 \omega_1) \frac{v_3\rho}{12\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_z^3 v_3}^{(1)}$ **at** $\frac{\partial^3 v_3}{\partial x_3^3}$:

$$C_{D_z^3 v_3}^{(1), \text{SRT}} = (-1 + 3v_3^2 + c_s^2) \frac{v_1\rho}{12}$$

$$C_{D_z^3 v_3}^{(1), \text{MRT1}} = (-6\omega_6 \omega_{11} + 18\omega_6 v_3^2 \omega_{11} - 12c_s^2 \omega_{11} + \omega_6 c_s^2 \omega_{11} \omega_{18} - 36v_3^2 \omega_{11} + 6\omega_6 c_s^2 \omega_{11} + 3\omega_6 v_3^2 \omega_{11} \omega_{18} - \omega_6 \omega_{11} \omega_{18} + 12\omega_{11} + 6\omega_6 \omega_{18} - 18\omega_6 v_3^2 \omega_{18} + 12c_s^2 \omega_{18} + 36v_3^2 \omega_{18} - 12\omega_{18} - 6\omega_6 c_s^2 \omega_{18}) \frac{v_1\rho}{12\omega_6 \omega_{11} \omega_{18}}$$

$$C_{D_z^3 v_3}^{(1), \text{MRT2}} = C_{D_z^3 v_3}^{(1), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(1), \text{CLBM1}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(1), \text{CLBM2}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(1), \text{CuLBM1}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(1), \text{CuLBM2}} = C_{D_z^3 v_3}^{(1), \text{SRT}}$$

coefficient $C_{D_x^4 \rho}^{(1)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^4}$:

$$C_{D_x^4 \rho}^{(1), \text{SRT}} = (12 - 156v_1^2 - 5c_s^4 \omega^3 - 1008c_s^2 v_1^2 \omega + 82c_s^4 \omega^2 + 234v_1^2 \omega + 144c_s^4 - 98v_1^2 \omega^2 - 216c_s^4 \omega - \omega^3 + 404c_s^2 v_1^2 \omega^2 + 8\omega^2 + 10v_1^2 \omega^3 - 18\omega - 34c_s^2 v_1^2 \omega^3 - 216v_1^4 \omega - 78c_s^2 \omega^2 + 6c_s^2 \omega^3 - 9v_1^4 \omega^3 + 144v_1^4 + 198c_s^2 \omega + 90v_1^4 \omega^2 - 132c_s^2 + 672c_s^2 v_1^2) \frac{v_1}{12\omega^3}$$

$$C_{D_x^4 \rho}^{(1), \text{MRT1}} = (12 - 156v_1^2 - 5c_s^4 \omega_9^3 - 1008c_s^2 v_1^2 \omega_9 + 82c_s^4 \omega_9^2 + 144c_s^4 - 216c_s^4 \omega_9 - 98v_1^2 \omega_9^2 - \omega_9^3 + 404c_s^2 v_1^2 \omega_9^2 + 8\omega_9^2 + 10v_1^2 \omega_9^3 - 34c_s^2 v_1^2 \omega_9^3 - 78c_s^2 \omega_9^2 - 216v_1^4 \omega_9 + 6c_s^2 \omega_9^3 - 9v_1^4 \omega_9^3 + 144v_1^4 + 90v_1^4 \omega_9^2 + 198c_s^2 \omega_9 - 132c_s^2 - 18\omega_9 + 672c_s^2 v_1^2) \frac{v_1}{12\omega_9^3}$$

$$C_{D_x^4 \rho}^{(1), \text{MRT2}} = C_{D_x^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(1), \text{CLBM1}} = C_{D_x^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(1), \text{CLBM2}} = C_{D_x^4 \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(1), \text{CuLBM1}} = (12 - 156v_1^2 - 1008c_s^2 v_1^2 \omega_4 + 234v_1^2 \omega_4 + 82c_s^4 \omega_4^2 - 5c_s^4 \omega_4^3 + 144c_s^4 + 10v_1^2 \omega_4^3 + 8\omega_4^2 - 34c_s^2 v_1^2 \omega_4^3 - \omega_4^3 - 18\omega_4 - 216c_s^4 \omega_4 - 98v_1^2 \omega_4^2 + 404c_s^2 v_1^2 \omega_4^2 + 6c_s^2 \omega_4^3 - 78c_s^2 \omega_4^2 - 216v_1^4 \omega_4 + 90v_1^4 \omega_4^2 + 198c_s^2 \omega_4 + 144v_1^4 - 9v_1^4 \omega_4^3 - 132c_s^2 + 672c_s^2 v_1^2) \frac{v_1}{12\omega_4^3}$$

$$C_{D_x^4 \rho}^{(1), \text{CuLBM2}} = (-8c_s^2 \omega_1 \omega_2^3 + 144\omega_3 v_1^4 \omega_2^3 + 90\omega_3 v_1^4 \omega_1^3 \omega_2^2 + 72\omega_3 c_s^4 \omega_1 \omega_2^2 + 8\omega_3 \omega_1^2 \omega_2 + 160\omega_3 c_s^2 v_1^2 \omega_1^3 - 52\omega_3 c_s^2 \omega_1^3 - 3\omega_3 \omega_1^3 \omega_2^3 +$$

$$\begin{aligned}
& 280\omega_3v_1^2\omega_1^2\omega_2^2 + 96\omega_3v_1^4\omega_1^2\omega_2 - 27\omega_3v_1^4\omega_1^3\omega_2^3 + 8\omega_3\omega_1^3\omega_2^2 - 196\omega_3v_1^2\omega_1^2\omega_2^3 - 372\omega_3c_s^4\omega_1\omega_2^3 + 94\omega_3v_1^2\omega_1^3\omega_2 + 24c_s^4\omega_1\omega_2^3 - 16c_s^2v_1^2\omega_1^2\omega_2^2 - \\
& 10\omega_3\omega_1^3\omega_2 - 98\omega_3v_1^2\omega_1^3\omega_2^2 + 16\omega_3\omega_1^2\omega_2^3 + 656\omega_3c_s^2v_1^2\omega_1\omega_2^2 - 264\omega_3v_1^4\omega_1^2\omega_2^2 - 80\omega_3c_s^2\omega_1\omega_2^2 + 30\omega_3v_1^2\omega_1^3\omega_2^3 + 24\omega_3v_1^4\omega_1^3 - 16\omega_3\omega_1^2\omega_2^2 - \\
& 104\omega_3v_1^2\omega_1^2\omega_2 + 8c_s^2v_1^2\omega_1^3\omega_2 - 184\omega_3c_s^2\omega_2^3 + 760\omega_3c_s^2v_1^2\omega_2^3 + 320\omega_3c_s^2\omega_1\omega_2^2 - 84\omega_3v_1^4\omega_1^3\omega_2 + 180\omega_3v_1^4\omega_1^2\omega_2^3 - 1472\omega_3c_s^2v_1^2\omega_1\omega_2^3 - \\
& 15\omega_3c_s^4\omega_1^3\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 72\omega_3c_s^4\omega_1^2\omega_2 + 8c_s^2v_1^2\omega_1\omega_2^3 - 48c_s^4\omega_1^2\omega_2^2 - 300\omega_3v_1^4\omega_1\omega_2^3 + 808\omega_3c_s^2v_1^2\omega_1^2\omega_2^3 + 122\omega_3c_s^2\omega_1^3\omega_2 - 464\omega_3c_s^2v_1^2\omega_1^3\omega_2 + \\
& 16\omega_3\omega_2^3 - 156\omega_3c_s^2\omega_1^2\omega_2^3 - 160\omega_3v_1^2\omega_2^3 + 24c_s^4\omega_1^3\omega_2 - 28\omega_3\omega_1\omega_2^3 + 82\omega_3c_s^4\omega_1^3\omega_2^2 + 72\omega_3c_s^4\omega_1^3 + 152\omega_3c_s^2\omega_1^2\omega_2^2 - 1088\omega_3c_s^2v_1^2\omega_1^2\omega_2^2 + \\
& 168\omega_3v_1^4\omega_1\omega_2^2 - 80\omega_3c_s^2\omega_1^2\omega_2 - 28\omega_3v_1^2\omega_1^3 - 102\omega_3c_s^2v_1^2\omega_1^3\omega_2^3 + 18\omega_3c_s^2\omega_1^3\omega_2^3 + 440\omega_3c_s^2v_1^2\omega_1^2\omega_2 + 16c_s^2\omega_1^2\omega_2^2 + 216\omega_3c_s^4\omega_2^3 + 164\omega_3c_s^4\omega_1^2\omega_2^3 + \\
& 328\omega_3v_1^2\omega_1\omega_2^3 - 156\omega_3c_s^4\omega_1^3\omega_2 - 8c_s^2\omega_1^3\omega_2 - 78\omega_3c_s^2\omega_1^3\omega_2^2 + 404\omega_3c_s^2v_1^2\omega_1^3\omega_2^2 - 176\omega_3v_1^4\omega_1\omega_2^2 - 120\omega_3c_s^4\omega_1^2\omega_2^2 + 4\omega_3\omega_1^3) \frac{v_1}{36\omega_3\omega_1^3\omega_2^3}
\end{aligned}$$

coefficient $C_{D_x^4 v_1}^{(1)}$ at $\frac{\partial^4 v_1}{\partial x_1^4}$:

$$C_{D_x^4 v_1}^{(1), \text{SRT}} = (12 - 252v_1^2 - c_s^4\omega^3 - 648c_s^2v_1^2\omega + 14c_s^4\omega^2 + 378v_1^2\omega + 24c_s^4 - 154v_1^2\omega^2 - 36c_s^4\omega - \omega^3 + 252c_s^2v_1^2\omega^2 + 8\omega^2 + 14v_1^2\omega^3 - 18\omega - 18c_s^2v_1^2\omega^3 - 756v_1^4\omega - 22c_s^2\omega^2 + 2c_s^2\omega^3 - 29v_1^4\omega^3 + 504v_1^4 + 54c_s^2\omega + 310v_1^4\omega^2 - 36c_s^2 + 432c_s^2v_1^2) \frac{\rho}{12\omega^3}$$

$$C_{D_x^4 v_1}^{(1), \text{MRT1}} = (12 - 252v_1^2 - c_s^4\omega_9^3 - 648c_s^2v_1^2\omega_9 + 378v_1^2\omega_9 + 14c_s^4\omega_9^2 + 24c_s^4 - 36c_s^4\omega_9 - 154v_1^2\omega_9^2 - \omega_9^3 + 252c_s^2v_1^2\omega_9^2 + 8\omega_9^2 + 14v_1^2\omega_9^3 - 18c_s^2v_1^2\omega_9^3 - 22c_s^2\omega_9^2 - 756v_1^4\omega_9 + 2c_s^2\omega_9^3 - 29v_1^4\omega_9^3 + 504v_1^4 + 310v_1^4\omega_9^2 + 54c_s^2\omega_9 - 36c_s^2 - 18\omega_9 + 432c_s^2v_1^2) \frac{\rho}{12\omega_9^3}$$

$$C_{D_x^4 v_1}^{(1), \text{MRT2}} = C_{D_x^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(1), \text{CLBM1}} = C_{D_x^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(1), \text{CLBM2}} = C_{D_x^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(1), \text{CuLBM1}} = (12 - 252v_1^2 - 648c_s^2v_1^2\omega_4 + 378v_1^2\omega_4 + 14c_s^4\omega_4^2 - c_s^4\omega_4^3 + 24c_s^4 + 14v_1^2\omega_4^3 + 8\omega_4^2 - 18c_s^2v_1^2\omega_4^3 - \omega_4^3 - 18\omega_4 - 36c_s^4\omega_4 - 154v_1^2\omega_4^2 + 252c_s^2v_1^2\omega_4^2 + 2c_s^2\omega_4^3 - 22c_s^2\omega_4^2 - 756v_1^4\omega_4 + 310v_1^4\omega_4^2 + 54c_s^2\omega_4 + 504v_1^4 - 29v_1^4\omega_4^3 - 36c_s^2 + 432c_s^2v_1^2) \frac{\rho}{12\omega_4^3}$$

$$\begin{aligned}
C_{D_x^4 v_1}^{(1), \text{CuLBM2}} = & (-8c_s^2\omega_1\omega_2^3 + 528\omega_3v_1^4\omega_2^3 + 310\omega_3v_1^4\omega_2^3\omega_2^2 + 8\omega_3c_s^4\omega_1\omega_2^2 + 8\omega_3\omega_1^2\omega_2 + 144\omega_3c_s^2v_1^2\omega_1^3 - 20\omega_3c_s^2\omega_1^3 - 3\omega_3\omega_1^3\omega_2^3 + \\
& 408\omega_3v_1^2\omega_1^2\omega_2^2 + 336\omega_3v_1^4\omega_1^2\omega_2 - 87\omega_3v_1^4\omega_1^3\omega_2^3 + 8\omega_3\omega_1^3\omega_2^2 - 308\omega_3v_1^2\omega_1^2\omega_2^3 - 68\omega_3c_s^4\omega_1\omega_2^3 + 174\omega_3v_1^2\omega_1^3\omega_2 + 8c_s^4\omega_1\omega_2^3 - 48c_s^2v_1^2\omega_1^2\omega_2^2 - \\
& 10\omega_3\omega_1^3\omega_2 - 154\omega_3v_1^2\omega_1^3\omega_2^2 + 16\omega_3\omega_1^2\omega_2^3 + 336\omega_3c_s^2v_1^2\omega_1\omega_2^2 - 888\omega_3v_1^4\omega_1^2\omega_2^2 - 16\omega_3c_s^2\omega_1\omega_2^2 + 42\omega_3v_1^2\omega_1^3\omega_2^3 + 96\omega_3v_1^4\omega_1^3 - 16\omega_3\omega_1^2\omega_2^2 - \\
& 168\omega_3v_1^2\omega_1^2\omega_2 + 24c_s^2v_1^2\omega_1^3\omega_2 - 56\omega_3c_s^2\omega_2^3 + 552\omega_3c_s^2v_1^2\omega_2^3 + 96\omega_3c_s^2\omega_1\omega_2^3 - 312\omega_3v_1^4\omega_1^3\omega_2 + 620\omega_3v_1^4\omega_1^2\omega_2^3 - 1008\omega_3c_s^2v_1^2\omega_1\omega_2^3 - \\
& 3\omega_3c_s^4\omega_1^3\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 8\omega_3c_s^4\omega_1^2\omega_2 + 24c_s^2v_1^2\omega_1\omega_2^3 - 16c_s^4\omega_1^2\omega_2^2 - 1068\omega_3v_1^4\omega_1\omega_2^3 + 504\omega_3c_s^2v_1^2\omega_1^2\omega_2^3 + 42\omega_3c_s^2\omega_1^3\omega_2 - 360\omega_3c_s^2v_1^2\omega_1^3\omega_2 + \\
& 16\omega_3\omega_2^3 - 44\omega_3c_s^2\omega_1^3\omega_2^3 - 288\omega_3v_1^2\omega_2^3 + 8c_s^4\omega_1^3\omega_2 - 28\omega_3\omega_1\omega_2^3 + 14\omega_3c_s^4\omega_1^3\omega_2^2 + 16\omega_3c_s^4\omega_1^3 + 24\omega_3c_s^2\omega_1^2\omega_2^2 - 576\omega_3c_s^2v_1^2\omega_1^2\omega_2^2 + 552\omega_3v_1^4\omega_1\omega_2^2 - \\
& 16\omega_3c_s^2\omega_1^2\omega_2 - 60\omega_3v_1^2\omega_1^3 - 54\omega_3c_s^2v_1^2\omega_1^3\omega_2^3 + 6\omega_3c_s^2\omega_1^3\omega_2^3 + 264\omega_3c_s^2v_1^2\omega_1^2\omega_2 + 16c_s^2\omega_1^2\omega_2^2 + 40\omega_3c_s^4\omega_2^3 + 28\omega_3c_s^4\omega_1^2\omega_2^3 + 552\omega_3v_1^2\omega_1\omega_2^3 - \\
& 32\omega_3c_s^4\omega_1^3\omega_2 - 8c_s^2\omega_1^3\omega_2 - 22\omega_3c_s^2\omega_1^3\omega_2^2 + 252\omega_3c_s^2v_1^2\omega_1^3\omega_2^2 - 240\omega_3v_1^4\omega_1\omega_2^2 - 8\omega_3c_s^4\omega_1^2\omega_2^2 + 4\omega_3\omega_1^3) \frac{\rho}{36\omega_3\omega_1^3\omega_2^3}
\end{aligned}$$

coefficient $C_{D_x^3 D_y \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y \rho}^{(1), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^3 D_y \rho}^{(1), \text{MRT1}} = & (-4v_1^2\omega_5^2\omega_9^3 - 24c_s^2v_1^2\omega_5^2\omega_9^2 - 4c_s^4\omega_5\omega_9^3 + 32v_1^4\omega_5^2\omega_9^2\omega_{12} + 8v_1^2\omega_5^3\omega_{12} + 36c_s^2v_1^2\omega_5^2\omega_{12}^2 - 48c_s^2v_1^2\omega_5\omega_9^2\omega_{12} + 4c_s^4\omega_5\omega_9\omega_{12}^2 - \\
& 4c_s^4\omega_5^3\omega_{12}^2 + 96c_s^2v_1^2\omega_5^2\omega_{12}^2 + 36v_1^2\omega_5^2\omega_9\omega_{12}^2 - 20v_1^2\omega_5\omega_9^3\omega_{12} + 4c_s^2\omega_5^2\omega_9\omega_{12} - 8v_1^2\omega_5^2\omega_{12}^2 - 36c_s^2v_1^2\omega_5^3\omega_{12} + 24c_s^2v_1^2\omega_5^2\omega_9^3 + 4v_1^2\omega_5^2\omega_9^2 - \\
& 24v_1^2\omega_5^2\omega_{12}^2 + 20v_1^2\omega_5\omega_9^2\omega_{12} - 72c_s^2v_1^2\omega_5^2\omega_9\omega_{12} + 4c_s^4\omega_5^2\omega_9^2\omega_{12} + 16v_1^4\omega_5\omega_9^2\omega_{12} + 4c_s^2\omega_5\omega_9^3 + 4v_1^4\omega_5^2\omega_9^3 - 144c_s^2v_1^2\omega_5^2\omega_9\omega_{12} + 84c_s^2v_1^2\omega_5\omega_9^3\omega_{12} + \\
& 8c_s^4\omega_5^2\omega_{12}^2 - 8v_1^4\omega_9^3\omega_{12} - 8c_s^2\omega_5\omega_9^3\omega_{12} + 12c_s^2\omega_5^2\omega_9\omega_{12}^2 - 13v_1^4\omega_5^2\omega_9^3\omega_{12} + 20v_1^4\omega_5\omega_9\omega_{12}^2 - 84c_s^2v_1^2\omega_5\omega_9^2\omega_{12} + 8v_1^4\omega_5^2\omega_{12}^2 - 4v_1^4\omega_5^2\omega_9^2 + \\
& 20v_1^2\omega_5^2\omega_9\omega_{12} + 13v_1^4\omega_5^2\omega_9^2\omega_{12} + 24v_1^4\omega_5^2\omega_{12}^2 + 8c_s^2\omega_5\omega_9^2\omega_{12} + 72c_s^2v_1^2\omega_5\omega_9\omega_{12}^2 - 4c_s^2\omega_9^2\omega_{12}^2 - 51c_s^2v_1^2\omega_5^2\omega_9^3\omega_{12} + 4c_s^2\omega_5^2\omega_9^2 - 32v_1^2\omega_5^2\omega_9^2\omega_{12} + \\
& 20v_1^4\omega_5\omega_9^3\omega_{12} - 36v_1^4\omega_5\omega_9\omega_{12}^2 - 8c_s^2\omega_5^2\omega_{12}^2 + 4c_s^2\omega_5^2\omega_9^3\omega_{12} - 4c_s^2\omega_5\omega_9\omega_{12}^2 - 4v_1^4\omega_5\omega_9^3 - 4c_s^2\omega_5^2\omega_9^3 - 4c_s^4\omega_5^2\omega_9\omega_{12} + 51c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12} + 4c_s^2\omega_9^3\omega_{12} - \\
& 4c_s^2\omega_5^2\omega_9^3\omega_{12} - 20v_1^4\omega_5\omega_9^2\omega_{12} + 4c_s^4\omega_9^2\omega_{12} - 8c_s^2\omega_5^2\omega_9^2\omega_{12} - 16v_1^4\omega_5\omega_9^2\omega_{12} - 4c_s^4\omega_5^2\omega_9^2 - 24c_s^2v_1^2\omega_5\omega_9^3 + 8c_s^4\omega_5^2\omega_{12}^2 - 20v_1^2\omega_5\omega_9\omega_{12}^2 + 13v_1^2\omega_5^2\omega_9^3\omega_{12} - \\
& 12c_s^4\omega_5^2\omega_9\omega_{12}^2 + 8c_s^4\omega_5\omega_9^3\omega_{12} + 120c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12} + 4c_s^4\omega_5^2\omega_9^3 - 20v_1^4\omega_5^2\omega_9\omega_{12} + 4v_1^2\omega_5\omega_9^3 - 4c_s^4\omega_9^3\omega_{12} - 8c_s^4\omega_5\omega_9^2\omega_{12} - 13v_1^2\omega_5^2\omega_9^2\omega_{12}^2) \frac{v_2}{4\omega_5^3\omega_9^3\omega_{12}^2}
\end{aligned}$$

$$C_{D_x^3 D_y \rho}^{(1), \text{MRT2}} = C_{D_x^3 D_y \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y \rho}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x^3 D_y \rho}^{(1), \text{CuLBM2}} = & (-36\omega_3 v_1^4 \omega_1 \omega_2^3 + 56\omega_3 c_s^2 \omega_1^3 \omega_2 - 4\omega_3 c_s^2 v_2^2 \omega_1^2 \omega_2 + 5\omega_3 c_s^2 \omega_2^2 \omega_1^3 - 48\omega_3 v_2^2 v_1^2 \omega_1^3 \omega_2 + 4\omega_3 v_2^2 \omega_1^2 \omega_2 - 48\omega_3 v_2^2 \omega_1^3 - \\
& 24\omega_3^2 v_2^2 \omega_1^2 \omega_2^3 - 20\omega_3^2 c_s^2 v_2^2 \omega_2^3 + 18\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2 - 36\omega_3^2 c_s^4 \omega_2^3 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2 + 4\omega_3^2 \omega_1^3 - 48\omega_3^2 v_2^2 v_1^2 \omega_1^2 \omega_2 - \omega_3^2 v_2^2 \omega_1^3 \omega_2^3 - 34\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 + \\
& 2\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2^3 - 72\omega_3^2 v_1^4 \omega_1 \omega_2^3 + 6\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 + 24\omega_3^2 c_s^4 \omega_1 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 4\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 - 60\omega_3^2 v_1^2 \omega_1 \omega_2^3 - 84\omega_3^2 c_s^4 \omega_1^3 \omega_2 + 8\omega_3^2 \omega_1 \omega_2^3 + \\
& 108\omega_3^2 c_s^2 v_1^2 \omega_1 \omega_2^3 + 4\omega_3^2 v_2^2 \omega_1^3 \omega_2 + 24\omega_3^2 v_2^2 v_1^2 \omega_1^2 \omega_2 + \omega_3^2 v_2^2 \omega_1^3 \omega_2^3 - 20\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2 + 40\omega_3^2 c_s^2 \omega_1^2 \omega_2 - 2\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2^3 - 216\omega_3^2 c_s^2 v_1^2 \omega_1 \omega_2^3 + \\
& 8\omega_3^2 \omega_1 \omega_2^3 + 48\omega_3^2 v_1^2 \omega_1 \omega_2^3 + 24\omega_3^2 v_2^2 \omega_2^3 - 4\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2 - 18\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 + 42\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 2\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 - 5\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 + 16\omega_3^2 c_s^2 v_2^2 \omega_1^3 - \\
& 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 + 4\omega_3^2 v_2^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_2^3 + 24\omega_3^2 v_2^2 v_1^2 \omega_1^2 \omega_2 + 72\omega_3^2 c_s^4 \omega_1^3 - \omega_3^2 \omega_1^2 \omega_2^3 - 4\omega_3^2 \omega_1^3 \omega_2 + 216\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2 + 216\omega_3^2 c_s^2 v_1^2 \omega_1^3 + 8\omega_3^2 c_s^2 v_2^2 \omega_1 \omega_2^3 - \\
& 24\omega_3^2 v_1^2 \omega_1^2 \omega_2 + 8\omega_3^2 v_2^2 \omega_2^3 + 12c_s^2 \omega_1^3 \omega_2^3 + 8\omega_3^2 c_s^2 v_2^2 \omega_1 \omega_2^3 + 4\omega_3^2 c_s^2 \omega_1^3 \omega_2 + 12c_s^2 v_2^2 \omega_1^2 \omega_2^3 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 v_2^2 \omega_1 \omega_2^3 + 24\omega_3^2 v_1^2 \omega_1^2 \omega_2^3 + \\
& 36c_s^4 \omega_1^2 \omega_2^3 + 42\omega_3^2 c_s^4 \omega_1 \omega_2^3 + 84\omega_3^2 v_1^2 \omega_1^3 \omega_2 - 72\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2^3 + 54\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 + 24\omega_3^2 v_1^4 \omega_1^3 - 4\omega_3^2 \omega_1^2 \omega_2^3 - 324\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2 - 8\omega_3^2 v_2^2 \omega_1 \omega_2^3 + \\
& 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 + 20\omega_3^2 c_s^2 \omega_2^3 + 22\omega_3^2 c_s^2 v_2^2 \omega_1 \omega_2^3 - 72\omega_3^2 v_2^2 v_1^2 \omega_2^3 + 24\omega_3^2 v_2^2 v_1^2 \omega_1 \omega_2^3 + 48\omega_3^2 v_1^4 \omega_2^3 + 72\omega_3^2 v_1^4 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 36c_s^4 \omega_1^3 \omega_2^3 - \\
& 24\omega_3^2 v_1^2 \omega_1^3 \omega_2^3 - 54\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 24\omega_3^2 v_2^2 v_1^2 \omega_1^3 + 72\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2^3 - 4\omega_3^2 \omega_1^2 \omega_2^3 - 52\omega_3^2 c_s^2 \omega_1^3 - 12\omega_3^2 c_s^4 \omega_1^3 \omega_2 - 22\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 36\omega_3^2 v_1^4 \omega_1^3 \omega_2 - \\
& 12c_s^2 \omega_1^2 \omega_2^3 - 18\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 - 12c_s^2 v_2^2 \omega_1^3 \omega_2^3 + 96\omega_3^2 v_2^2 v_1^2 \omega_1 \omega_2^3 + \omega_3^2 \omega_1^3 \omega_2^3 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 4\omega_3^2 v_2^2 \omega_1^3 - 24\omega_3^2 v_1^2 \omega_1^2 \omega_2^3) \frac{v_2}{36\omega_3^2 \omega_1^3 \omega_2^3}
\end{aligned}$$

coefficient $C_{D_x^3 D_y v_1}^{(1)}$ at $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_1}^{(1), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^3 D_y v_1}^{(1), \text{MRT1}} = & (16v_1^2 \omega_5^2 \omega_9^3 + 24\omega_5^2 \omega_9 \omega_{12} - 28v_1^2 \omega_9^3 \omega_{12} - 16c_s^2 \omega_5 \omega_9^2 \omega_{12} - 120v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 + 68v_1^2 \omega_5 \omega_9^3 \omega_{12} - 32c_s^2 \omega_5^2 \omega_9 \omega_{12} + 16\omega_5 \omega_9^2 \omega_{12} + \\
& 28v_1^2 \omega_5^2 \omega_{12}^3 - 16v_1^2 \omega_5^2 \omega_9^2 + 80v_1^2 \omega_5^2 \omega_{12}^2 - 68v_1^2 \omega_5 \omega_9^2 \omega_{12}^2 - 48v_1^2 \omega_5 \omega_9^2 \omega_{12} - 16c_s^2 \omega_5 \omega_9^3 + 28\omega_5 \omega_9^2 \omega_{12}^2 + 44c_s^2 \omega_5 \omega_9^3 \omega_{12} - 72c_s^2 \omega_5^2 \omega_9 \omega_{12}^2 + 8\omega_5 \omega_9^3 - \\
& 64v_1^2 \omega_5^2 \omega_9 \omega_{12} - 28\omega_5 \omega_9^3 \omega_{12} - 44c_s^2 \omega_5 \omega_9^2 \omega_{12}^2 + 48\omega_5^2 \omega_9 \omega_{12}^2 - 32\omega_5^2 \omega_{12}^2 + 20c_s^2 \omega_9^2 \omega_{12}^2 - 16c_s^2 \omega_5^2 \omega_9^2 + 104v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 12\omega_9^2 \omega_{12}^2 + 48c_s^2 \omega_5^2 \omega_{12}^2 + \\
& 8\omega_5^2 \omega_9^2 - 25c_s^2 \omega_5^2 \omega_9 \omega_{12} - 17\omega_5^2 \omega_9^2 \omega_{12}^2 + 32c_s^2 \omega_5 \omega_9 \omega_{12}^2 + 16c_s^2 \omega_5^2 \omega_9^3 - 20c_s^2 \omega_9^3 \omega_{12} - 8\omega_5^2 \omega_9^3 + 25c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 17\omega_5^2 \omega_9^3 \omega_{12} - 24\omega_5 \omega_9 \omega_{12}^2 + \\
& 12\omega_5^2 \omega_{12}^2 + 56c_s^2 \omega_5^2 \omega_9^2 \omega_{12} + 64v_1^2 \omega_5 \omega_9 \omega_{12}^2 - 43v_1^2 \omega_5^2 \omega_9 \omega_{12} - 16v_1^2 \omega_5 \omega_9^3 - 40\omega_5^2 \omega_9^2 \omega_{12} + 43v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2) \frac{v_2 v_1 \rho}{4\omega_5^2 \omega_9^3 \omega_{12}^2}
\end{aligned}$$

$$C_{D_x^3 D_y v_1}^{(1), \text{MRT2}} = C_{D_x^3 D_y v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y v_1}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x^3 D_y v_1}^{(1), \text{CuLBM2}} = & (36c_s^2 \omega_1 \omega_2^3 + 6\omega_3 v_2^2 \omega_1 \omega_2^3 + 6\omega_3 \omega_1^2 \omega_2 + 84\omega_3 c_s^2 \omega_1^3 - 12\omega_1 \omega_2^3 + 132\omega_3 v_1^2 \omega_1^2 \omega_2^3 + 27\omega_3 v_2^2 \omega_1 \omega_2^3 - 5\omega_3 \omega_1^3 \omega_2^3 + 12\omega_3 v_2^2 \omega_1^3 - \\
& 66\omega_3 v_1^2 \omega_1^3 \omega_2 + 48\omega_3 \omega_1^3 \omega_2 + 5\omega_3 \omega_1^2 \omega_2^3 + 12v_2^2 \omega_1 \omega_2^3 - 54\omega_3 c_s^2 \omega_1 \omega_2^3 - 24\omega_3 v_2^2 \omega_2^3 - 51\omega_3 \omega_1^2 \omega_2^3 - 12\omega_3 c_s^2 \omega_2^3 + 27\omega_3 c_s^2 \omega_1 \omega_2^3 + \\
& 42\omega_3 \omega_1 \omega_2^3 - 9\omega_1^3 \omega_2^3 + 27c_s^2 \omega_1^3 \omega_2^3 + 6\omega_3 v_2^2 \omega_1^2 \omega_2 - 6v_2^2 \omega_1^2 \omega_2^3 - 108\omega_3 c_s^2 \omega_1^3 \omega_2 - 12\omega_3 \omega_2^3 - 15\omega_3 c_s^2 \omega_1^3 \omega_2^3 + 84\omega_3 v_1^2 \omega_2^3 + 3\omega_3 \omega_1 \omega_2^3 - 6v_2^2 \omega_1^3 \omega_2 + \\
& 81\omega_3 c_s^2 \omega_1^2 \omega_2^3 - 9v_2^2 \omega_1^2 \omega_2^3 + 5\omega_3 v_2^2 \omega_1^3 \omega_2^3 - 18\omega_3 c_s^2 \omega_1^2 \omega_2 + 48\omega_3 v_1^2 \omega_1^3 + 9v_2^2 \omega_1^3 \omega_2^3 - 18\omega_3 v_2^2 \omega_1^3 \omega_2 - 18c_s^2 \omega_1^2 \omega_2^3 - 5\omega_3 v_2^2 \omega_1^2 \omega_2^3 - 66\omega_3 v_1^2 \omega_1 \omega_2^3 + \\
& 6\omega_1^2 \omega_2^3 - 9\omega_3 v_2^2 \omega_1^2 \omega_2^3 - 18c_s^2 \omega_1^3 \omega_2 - 27c_s^2 \omega_1^2 \omega_2^3 + 15\omega_3 c_s^2 \omega_1^3 \omega_2^3 - 120\omega_3 v_1^2 \omega_1 \omega_2^3 + 9\omega_1^2 \omega_2^3 + 6\omega_1^3 \omega_2 - 36\omega_3 \omega_1^3) \frac{v_2 v_1 \rho}{18\omega_3 \omega_1^3 \omega_2^3}
\end{aligned}$$

coefficient $C_{D_x^3 D_y v_2}^{(1)}$ at $\frac{\partial^4 v_2}{\partial x_1^3 \partial x_2}$:

$$\begin{aligned}
C_{D_x^3 D_y v_2}^{(1), \text{SRT}} = & (36v_1^2 - c_s^4 \omega^3 + 54c_s^2 v_1^2 \omega + 20c_s^4 \omega^2 - 54v_1^2 \omega + 36c_s^4 + 26v_1^2 \omega^2 - 54c_s^4 \omega - 42c_s^2 v_1^2 \omega^2 - 4v_1^2 \omega^3 + 12c_s^2 v_1^2 \omega^3 + 54v_1^4 \omega - 12c_s^2 \omega^2 + \\
& 4v_1^4 \omega^3 - 36v_1^4 + 36c_s^2 \omega - 26v_1^4 \omega^2 - 24c_s^2 - 36c_s^2 v_1^2) \frac{\rho}{12\omega^3}
\end{aligned}$$

$$\begin{aligned}
C_{D_x^3 D_y v_2}^{(1), \text{MRT1}} = & (12v_1^2 \omega_5^2 \omega_9^3 - c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 24v_1^4 \omega_5^2 \omega_9^2 \omega_{12} - 4v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 - 18c_s^4 \omega_5^2 \omega_9^3 \omega_{12} + 60c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 24v_1^2 \omega_5 \omega_9^3 \omega_{12} + 12v_1^4 \omega_5^3 \omega_9^3 + \\
& 6c_s^2 \omega_5 \omega_9^3 \omega_{12}^2 - 90v_1^4 \omega_5^3 \omega_9 \omega_{12}^2 - 12c_s^2 v_1^2 \omega_5^2 \omega_9^3 - 6c_s^2 \omega_5^3 \omega_9^3 \omega_{12} + 72v_1^4 \omega_5^3 \omega_{12}^2 - 18v_1^4 \omega_5^2 \omega_9^3 \omega_{12}^2 - 21c_s^2 v_1^2 \omega_5^2 \omega_9^3 \omega_{12} - 12v_1^4 \omega_5^3 \omega_9^2 + 102c_s^2 v_1^2 \omega_5 \omega_9^3 \omega_{12}^2 - \\
& 60v_1^2 \omega_5^2 \omega_9^2 \omega_{12} + 6c_s^4 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12c_s^2 v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 + 252c_s^2 v_1^2 \omega_5^3 \omega_{12}^2 - 12v_1^4 \omega_5^2 \omega_9^3 - 19v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 108c_s^2 v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 - 12c_s^2 v_1^2 \omega_5 \omega_9^3 \omega_{12} + \\
& 12c_s^4 \omega_5^2 \omega_9^2 \omega_{12} - 12c_s^2 \omega_5 \omega_9^3 \omega_{12} - 48c_s^2 v_1^2 \omega_5^3 \omega_{12}^2 + 12c_s^2 \omega_5^2 \omega_9 \omega_{12}^2 - 36v_1^4 \omega_5^3 \omega_9 \omega_{12} - 12v_1^2 \omega_5^2 \omega_9^3 + 48v_1^4 \omega_5^3 \omega_9 \omega_{12} - 12c_s^2 v_1^2 \omega_5^2 \omega_9^2 + 27v_1^2 \omega_5^3 \omega_9 \omega_{12} - \\
& 48c_s^2 v_1^2 \omega_5 \omega_9^2 \omega_{12} + 13c_s^4 \omega_5^2 \omega_9^3 \omega_{12}^2 - 12v_1^2 \omega_5 \omega_9^3 \omega_{12}^2 + 54c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 72v_1^2 \omega_5^3 \omega_{12}^2 - 12c_s^4 \omega_5^3 \omega_9 \omega_{12} + 6c_s^2 \omega_5^3 \omega_9^2 \omega_{12} + 12c_s^2 v_1^2 \omega_5^3 \omega_9 + \\
& 12v_1^4 \omega_5^2 \omega_9^2 \omega_{12} + 12v_1^2 \omega_5^3 \omega_9^2 + 30c_s^2 v_1^2 \omega_5^2 \omega_9^3 \omega_{12} + c_s^4 \omega_5^3 \omega_9^2 \omega_{12} + 12c_s^4 \omega_5^3 \omega_{12}^2 - 36c_s^2 v_1^2 \omega_5^3 \omega_9 \omega_{12} + 24v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 24v_1^4 \omega_5 \omega_9^3 \omega_{12} + 4v_1^4 \omega_5^3 \omega_9^3 \omega_{12}^2 + \\
& 12c_s^4 \omega_9^3 \omega_{12}^2 + 18c_s^2 \omega_5^2 \omega_9^2 \omega_{12} + 6c_s^4 \omega_5^3 \omega_9^2 \omega_{12} + 18v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 - 24c_s^4 \omega_5 \omega_9^3 \omega_{12}^2 + 90v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 + 162c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} + 60v_1^4 \omega_5^3 \omega_9 \omega_{12} - 6c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + \\
& 19v_1^4 \omega_5^3 \omega_9^2 \omega_{12} - 12c_s^2 \omega_5^2 \omega_9^2 \omega_{12} - 12c_s^2 \omega_5^3 \omega_{12}^2 - c_s^4 \omega_5^3 \omega_9^2 \omega_{12} - 48v_1^2 \omega_5^2 \omega_9^3 \omega_{12} - 12c_s^4 \omega_5^2 \omega_9 \omega_{12}^2 + 12c_s^4 \omega_5 \omega_9^3 \omega_{12} - 12c_s^2 v_1^2 \omega_5^2 \omega_9 \omega_{12} + 36v_1^2 \omega_5^3 \omega_9 \omega_{12} + \\
& 12v_1^4 \omega_5 \omega_9^2 \omega_{12} + 12c_s^2 \omega_5^2 \omega_9 \omega_{12}^2 - 27v_1^4 \omega_5^3 \omega_9 \omega_{12} - 5c_s^2 \omega_5^2 \omega_9^3 \omega_{12}^2 - 81c_s^2 v_1^2 \omega_5^2 \omega_9^3 \omega_{12} - 6c_s^4 \omega_5^3 \omega_9^2 \omega_{12} - 12v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 306c_s^2 v_1^2 \omega_5^3 \omega_9 \omega_{12}^2) \frac{\rho}{12\omega_5^3 \omega_9^3 \omega_{12}^2}
\end{aligned}$$

$$C_{D_x^3 D_y v_2}^{(1), \text{MRT2}} = C_{D_x^3 D_y v_2}^{(1), \text{MRT1}}$$

$$\begin{aligned}
C_{D_x^3 D_y v_2}^{(1), \text{CLBM1}} = & (36v_1^2 \omega_5^2 \omega_9^3 - c_s^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 - 18c_s^4 \omega_5^2 \omega_9^3 \omega_{12} + 60c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 36v_1^2 \omega_5^3 \omega_9^3 + 6c_s^2 \omega_5 \omega_9^3 \omega_{12}^2 - 90v_1^4 \omega_5^3 \omega_9 \omega_{12}^2 - \\
& 108c_s^2 v_1^2 \omega_5^2 \omega_9^2 \omega_{12} - 6c_s^4 \omega_5^2 \omega_9^2 \omega_{12}^2 + 72v_1^4 \omega_5^3 \omega_{12}^2 - 6v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 - 99c_s^2 v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 - 36v_1^4 \omega_5^3 \omega_9^2 - 18c_s^2 v_1^2 \omega_5 \omega_9^3 \omega_{12}^2 - 72v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 6c_s^4 \omega_5^2 \omega_9^2 \omega_{12}^2 + \\
& 12c_s^2 v_1^2 \omega_5^2 \omega_9^3 \omega_{12}^2 + 252c_s^2 v_1^2 \omega_5^3 \omega_{12}^2 - 36v_1^4 \omega_5^2 \omega_9^3 - 19v_1^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 36c_s^2 v_1^2 \omega_5^2 \omega_9 \omega_{12}^2 + 36c_s^2 v_1^2 \omega_5 \omega_9^3 \omega_{12} + 12c_s^4 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12c_s^2 \omega_5 \omega_9^3 \omega_{12}^2 +
\end{aligned}$$

$$12c_s^2\omega_2^3\omega_9\omega_{12}^2 - 36v_1^4\omega_5^3\omega_9\omega_{12} - 36v_1^2\omega_5^3\omega_9^3 + 36v_1^4\omega_2^3\omega_9^3\omega_{12} - 108c_s^2v_1^2\omega_2^3\omega_9^3 + 39v_1^2\omega_5^3\omega_9^3\omega_{12} + 13c_s^4\omega_2^5\omega_9^3\omega_{12} + 198c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12} - 72v_1^4\omega_2^3\omega_9^3\omega_{12} - 12c_s^4\omega_2^3\omega_9\omega_{12} + 6c_s^2\omega_2^3\omega_9^3\omega_{12} + 108c_s^2v_1^2\omega_2^3\omega_9^3 + 36v_1^2\omega_2^3\omega_9^3 + 54c_s^2v_1^2\omega_2^3\omega_9^3\omega_{12} + c_s^4\omega_2^3\omega_9^3\omega_{12} + 12c_s^4\omega_2^3\omega_9^3\omega_{12} - 108c_s^2v_1^2\omega_2^3\omega_9\omega_{12} + 4c_s^4\omega_2^3\omega_9^3\omega_{12} + 12c_s^4\omega_2^3\omega_9^3\omega_{12} + 18c_s^2\omega_2^3\omega_9^3\omega_{12} + 6c_s^4\omega_2^3\omega_9^3\omega_{12} + 6v_1^2\omega_2^3\omega_9^3\omega_{12} + 6v_1^4\omega_2^3\omega_9^3\omega_{12} + 90v_1^2\omega_5^3\omega_9\omega_{12} + 18c_s^2v_1^2\omega_2^3\omega_9^3\omega_{12} + 72v_1^4\omega_2^3\omega_9^3\omega_{12} - 6c_s^4\omega_2^3\omega_9^3\omega_{12} + 19v_1^4\omega_2^3\omega_9^3\omega_{12} - 12c_s^4\omega_2^3\omega_9^3\omega_{12} - 12c_s^4\omega_2^3\omega_9^3\omega_{12} - c_s^4\omega_2^3\omega_9^3\omega_{12} - 24v_1^4\omega_2^3\omega_9^3\omega_{12} - 12c_s^4\omega_2^3\omega_9^3\omega_{12} + 12c_s^4\omega_2^3\omega_9^3\omega_{12} + 36c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12} + 36v_1^4\omega_2^3\omega_9\omega_{12} + 12c_s^4\omega_2^3\omega_9\omega_{12} - 39v_1^4\omega_5^3\omega_9^3\omega_{12} - 5c_s^2\omega_2^3\omega_9^3\omega_{12} - 3c_s^2v_1^2\omega_2^3\omega_9^3\omega_{12} - 6c_s^4\omega_2^3\omega_9^3\omega_{12} - 306c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12} \Big) \frac{\rho}{12\omega_2^3\omega_9^3\omega_{12}^2}$$

$$C_{\text{D}_3^x \text{D}_{9/2}}^{(1), \text{CuLBMI}} = (72v_1^2\omega_1^2\omega_9^2 - 36v_7^2\omega_4^3\omega_1^3 - 6c_s^2\omega_4^2\omega_7^2\omega_9^2 + 36v_1^4\omega_1^3\omega_7^3\omega_9 - 108c_s^2v_1^2\omega_4^3\omega_7^2 + 18c_s^2v_7^2\omega_4^2\omega_7^2\omega_9^2 - 36v_1^4\omega_1^2\omega_7^3 - 12c_s^4\omega_4\omega_3^3\omega_9^2 - 19v_1^2\omega_1^2\omega_7^3\omega_9^2 + 6c_s^4\omega_4^3\omega_7^3\omega_9 + 108c_s^2v_1^2\omega_1^3\omega_7^3 + 6c_s^2\omega_4^3\omega_7^3\omega_9 + 4v_1^4\omega_4^3\omega_7^3\omega_9^2 + 36v_7^2\omega_4^3\omega_7^2 - 12c_s^2\omega_4^3\omega_1\omega_9 - 36v_1^4\omega_4\omega_7^3\omega_9 + 36c_s^2v_7^2\omega_4^3\omega_1\omega_9 + 13c_s^4\omega_3^3\omega_1^2\omega_9^2 + 198c_s^2v_7^2\omega_4^2\omega_7^3\omega_9 - 72v_7^2\omega_1^2\omega_9^2 - 18c_s^2v_7^2\omega_4^3\omega_1\omega_9^2 - 18c_s^4\omega_4^3\omega_7^3\omega_9 + 60c_s^2v_7^2\omega_4^2\omega_7^3\omega_9^2 - 12c_s^4\omega_4\omega_7^2\omega_9^2 + 36v_1^4\omega_1^3\omega_7^3 - c_s^2\omega_4^3\omega_7^3\omega_9^2 + 36v_7^2\omega_7^3\omega_1^3 - 39v_1^4\omega_4^3\omega_7^3\omega_9 + 6c_s^2\omega_4^3\omega_1\omega_9^2 - 90v_1^4\omega_4^3\omega_7^2\omega_9 - 36v_1^4\omega_4^2\omega_7^3 + 36c_s^2v_1^4\omega_4^2\omega_7^3 + 252c_s^2v_1^2\omega_1^3\omega_9^2 - 72v_1^2\omega_7^2\omega_1^3\omega_9 - c_s^4\omega_4^3\omega_1^3\omega_9^2 - 12c_s^2\omega_7^2\omega_1^2\omega_9 - 108c_s^2v_1^2\omega_1^2\omega_7^3 - 6v_1^4\omega_4^3\omega_1^2\omega_9^2 + 6c_s^4\omega_4^3\omega_7^2\omega_9^2 - 36v_1^2\omega_4^2\omega_7^2\omega_9 - 306c_s^2v_1^2\omega_4^2\omega_7^2\omega_9^2 - 99c_s^2v_7^2\omega_4^3\omega_1\omega_9 + 19v_1^4\omega_4^2\omega_7^2\omega_9^2 - 6c_s^4\omega_4^3\omega_7^2\omega_9 + 12c_s^2\omega_4^3\omega_7^2\omega_9 + 12c_s^4\omega_4\omega_1\omega_9 + 36v_7^2\omega_4\omega_1\omega_9^2 + 3c_s^2v_7^2\omega_4^2\omega_1^2\omega_9^2 - 6c_s^4\omega_4^2\omega_7^3\omega_9 - 4v_7^2\omega_4^3\omega_1^3\omega_9^2 - 5c_s^2\omega_4^3\omega_1^2\omega_9^2 + 12c_s^2\omega_4\omega_7^2\omega_9^2 + 18c_s^2\omega_4^3\omega_7^2\omega_9 - 24c_s^4\omega_4\omega_1\omega_9^2 + 54c_s^2v_1^2\omega_1^3\omega_7^2\omega_9 + 12c_s^4\omega_3^3\omega_9^2 + 90v_7^2\omega_4\omega_7^2\omega_9^2 + c_s^4\omega_4^3\omega_1\omega_9^2 - 36c_s^2v_1^2\omega_4\omega_7^2\omega_9^2 + 39v_7^2\omega_4^3\omega_1^2\omega_9 + 72v_1^4\omega_4^3\omega_7^2\omega_9 - 12c_s^2\omega_1^3\omega_9^2 + 12c_s^4\omega_4^2\omega_1\omega_9 - 108c_s^2v_1^2\omega_4\omega_1^2\omega_9 + 6v_7^2\omega_4^2\omega_1^2\omega_9^2 + 12c_s^2v_1^2\omega_1^3\omega_4^3\omega_9^2) \frac{\rho}{12\omega_3^2\omega_9^2}$$

$$\begin{aligned}
& 24\omega_3 v_1^2 w_4^1 \omega_1 \omega_3^2 + 96\omega_3 v_1^4 w_4^1 \omega_1^2 \omega_2 + 162c_6^2 v_1^2 w_4^1 \omega_1^3 \omega_3^2 - 144\omega_3 v_1^2 w_4^1 \omega_1 \omega_2^2 - 40\omega_3^3 c_2^2 w_4^1 \omega_1^3 - 288\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 108\omega_3 c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 + \\
& 108\omega_3 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 24\omega_3 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 86\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2^2 + 72v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 28\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2 + 144\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 48\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 12\omega_3^3 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2 + \\
& 38\omega_3^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 180\omega_3 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 12\omega_3^3 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 24\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 36\omega_3 c_4^2 w_4^1 \omega_1^2 \omega_2^2 - 108\omega_3^2 c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 852\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2 + \\
& 16\omega_3^3 c_4^2 w_4^1 \omega_1^2 \omega_2 + 24\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_2 + 72\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2^2 - 72\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 20\omega_3^3 c_4^2 w_4^1 \omega_1^2 \omega_2^2 + 6\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 80\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2 + 324\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + \\
& 36\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 117\omega_3 v_1^2 w_4^1 \omega_1^2 \omega_2^2 + 96\omega_3^3 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 108c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 54v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 72\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 6\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 6\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2^2 - \\
& 56\omega_3^3 c_4^2 w_4^1 \omega_1^2 \omega_2 - 16\omega_3 c_2^2 w_4^1 \omega_1^3 \omega_2^2 - 24\omega_3^2 v_1^2 w_4^1 \omega_1^3 \omega_2 + 48\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 216c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 + 72\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 60\omega_3 v_1^4 w_4^1 \omega_1^2 \omega_2^2 + \\
& 144\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_2 + 24\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2 + 117\omega_3^3 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 36\omega_3 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 32\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2^2 - 12\omega_3^3 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 16\omega_3^2 w_4^1 \omega_1^2 \omega_2^2 + 40\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - \\
& 108\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2 - 32\omega_3^2 c_2^2 w_4^1 \omega_1^2 \omega_3^2 - 36\omega_3^3 c_4^2 w_4^1 \omega_1^3 \omega_2^2 - 297\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2 + 72\omega_3^2 c_6^2 w_4^1 \omega_1^2 \omega_3^2 + 576\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 + 216\omega_3 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - \\
& 36\omega_3^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 540\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 24\omega_3 v_1^4 w_4^1 \omega_1^2 \omega_2 + 24\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 2\omega_3^2 c_2^2 w_4^1 \omega_1^2 \omega_2^2 + 48\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 36v_1^2 w_4^1 \omega_1^2 \omega_3^2 + \\
& 108\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 18\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 8\omega_3^2 c_2^2 w_4^1 \omega_1^3 \omega_2^2 + 48\omega_3^2 c_6^2 w_4^1 \omega_1^2 \omega_3^2 - 432\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 96\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 72\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 + 16\omega_3^2 w_4^1 \omega_1^3 \omega_2^2 - \\
& 108\omega_3 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 144\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - 108\omega_3 c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 24\omega_3^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 288\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 144\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 144\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - \\
& 24\omega_3 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 40\omega_3 c_6^2 w_4^1 \omega_1^2 \omega_3^2 + 18\omega_3^3 c_2^2 w_4^1 \omega_1^3 \omega_2^2 + 8\omega_3^2 w_4^1 \omega_1^3 \omega_2^2 + 72\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 72v_1^4 w_4^1 \omega_1^2 \omega_2^2 + 192\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - 36\omega_3^2 c_2^2 w_4^1 \omega_1^3 \omega_2^2 + \\
& 264\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_2 + 36\omega_3^2 c_2^2 w_4^1 \omega_1^3 \omega_2 + 96\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2 - 2\omega_3^2 w_4^1 \omega_1^3 \omega_2^2 - 108\omega_3 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 8\omega_3^2 w_4^1 \omega_1^3 \omega_2 + 288\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 + 36\omega_3^2 c_2^2 w_4^1 \omega_1^3 \omega_2^2 + \\
& 108\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 96\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 16\omega_3 c_2^2 w_4^1 \omega_1^2 \omega_3^2 - 72\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 324\omega_3^2 c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 288\omega_3^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 180\omega_3 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - \\
& 86\omega_3^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 468\omega_3 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 96\omega_3^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + 117\omega_3 v_1^2 w_4^1 \omega_1^2 \omega_3^2 - 36\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - 288\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_3^2 - 8\omega_3^2 w_4^1 \omega_1^3 \omega_2^2 + 264\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - \\
& 72\omega_3^2 c_2^2 w_4^1 \omega_1^3 \omega_2^2 + 168\omega_3^2 c_6^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 54\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 - 12\omega_3^2 c_2^2 w_4^1 \omega_1^3 \omega_2^2 - 12\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^3 \omega_2^2 - 8\omega_3^2 w_4^1 \omega_1^3 \omega_2^2 - 117\omega_3^2 v_1^4 w_4^1 \omega_1^2 \omega_2^2 + 60\omega_3 v_1^2 w_4^1 \omega_1^3 \omega_2^2 + \\
& 54v_1^4 w_4^1 \omega_1^2 \omega_2^2 + 174\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_3^2 + 16\omega_3 c_2^2 w_4^1 \omega_1^2 \omega_3^2 + 64\omega_3^2 c_2^2 v_1^2 w_4^1 \omega_1^2 \omega_2^2 - 4$$

$$G_{\text{D}_2^2 \text{D}_2^2 \rho}^{(1), \text{SRT}} = (24 - 24v_1^2 + 36v_1^2\omega - 14v_1^2\omega^2 - \omega^3 + 14\omega^2 + v_1^2\omega^3 - 36\omega - 46c_s^2\omega^2 + 5c_s^2\omega^3 + 108c_s^2\omega - 72c_s^2) \frac{c_s^2 v_1}{12u_3^3}$$

$$\begin{aligned}
& 24v_2^2v_1^2w_5^2w_{15}w_{50}w_{12} - c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12c_2^2v_1^2w_5^2w_{21}w_{15}w_{50} + 18c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 6v_2^2v_1^2w_5^2w_{50}w_{12} - 36c_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} + \\
& 36c_2^2v_2^2w_5^2w_{12}w_{12} - 12v_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12v_2^2w_5^2w_{21}w_{15}w_{50} - 6c_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} + 24v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 18v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - \\
& 12v_2^2v_1^2w_5^2w_{21}w_{50}w_{12} - 36c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 18c_2^2v_2^2w_5^2w_{15}w_{50}w_{12} + 12c_2^4w_5^2w_{21}w_{15}w_{50} + 5c_2^4w_5^2w_{21}w_{15}w_{50}w_{12} - 12v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - \\
& 24v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12v_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} - 18c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 12v_2^2w_5^2w_{21}w_{15}w_{50} - 6v_2^2v_1^2w_5^2w_{15}w_{50}w_{12} - 2c_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} + \\
& 36c_2^2v_2^2w_5^2w_{15}w_{50}w_{12} - 36v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 12v_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} + 12c_2^2w_5^2w_{21}w_{15}w_{50} - 72c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 6c_2^2v_1^2w_5^2w_{12}w_{12} + \\
& 12v_2^2v_1^2w_5^2w_{12}w_{12} - 36c_2^2v_2^2w_5^2w_{15}w_{50}w_{12} + 18c_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12c_2^2w_5^2w_{21}w_{15}w_{50} - 12v_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12c_2^2v_1^2w_5^2w_{21}w_{15}w_{50} - \\
& 48c_2^4w_5^2w_{21}w_{15}w_{50}w_{12} + 6v_2^2v_1^2w_5^2w_{21}w_{50}w_{12} + 12v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12c_2^2w_5^2w_{21}w_{15}w_{50} + 12c_2^2v_1^2w_5^2w_{21}w_{15}w_{12} + 6c_2^2w_5^2w_{12}w_{12} + \\
& 30c_2^4w_5^2w_{21}w_{15}w_{50}w_{12} - 72c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 36c_2^2v_2^2w_5^2w_{15}w_{50}w_{12} + 2c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 36c_2^2v_2^2w_5^2w_{21}w_{12}w_{12} - 12c_2^2w_5^2w_{21}w_{15}w_{12} + \\
& 12c_2^2v_2^2w_5^2w_{21}w_{15}w_{50} + 36c_2^4w_5^2w_{12}w_{12} - 54c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 72c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 12c_2^4w_5^2w_{21}w_{15}w_{50} + 6v_2^2v_1^2w_5^2w_{15}w_{50}w_{12} + \\
& 12v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + c_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} + 12v_2^2w_5^2w_{21}w_{15}w_{50} - 6c_2^4w_5^2w_{21}w_{15}w_{50}w_{12} - 18c_2^2v_2^2w_5^2w_{15}w_{50}w_{12} + 108c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + \\
& 12v_2^2v_1^2w_5^2w_{15}w_{50}w_{12} + 6c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 24v_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} + 36c_2^4w_5^2w_{21}w_{15}w_{50}w_{12} + 12c_2^2w_5^2w_{21}w_{15}w_{50} + 18c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - \\
& 12c_2^2v_1^2w_5^2w_{15}w_{50}w_{12} - 42c_2^4w_5^2w_{21}w_{15}w_{50}w_{12} + 12c_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} - 18c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 18c_2^4w_5^2w_{15}w_{50}w_{12} - 6v_2^2w_5^2w_{15}w_{50}w_{12} + \\
& 12c_2^2w_5^2w_{21}w_{15}w_{12} + 36c_2^2v_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12v_2^2v_1^2w_5^2w_{21}w_{15}w_{50} - 36c_2^2v_2^2w_5^2w_{21}w_{15}w_{50} - 12v_2^2v_1^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12v_2^2w_5^2w_{15}w_{50}w_{12} - \\
& 36c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 36c_2^2w_5^2w_{21}w_{50}w_{12} - 84c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} + 6c_2^2w_5^2w_{15}w_{50}w_{12} + 12c_2^2w_5^2w_{21}w_{15}w_{50}w_{12} - 12c_2^2v_1^2w_5^2w_{15}w_{50}w_{12} - \\
\end{aligned}$$

$$\begin{aligned}
& 36c_s^4\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 12c_s^2v_1^3\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 12v_2^3\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 6c_s^2v_1^2\omega_5^3\omega_{15}\omega_9^3\omega_{12}^2 - 36c_s^2v_2^3\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 + \\
& 150c_s^4\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 - 12v_2^3v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 18c_s^2v_2^2\omega_5^3\omega_9^3\omega_{12}^2 - 18c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 6v_2^2\omega_5^3\omega_{21}\omega_9^3\omega_{12} + 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + \\
& 12c_s^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} + 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 24v_2^2v_1^3\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12v_2^3v_1^2\omega_5^3\omega_9^3\omega_{12}^2 + 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - \\
& 12c_s^2v_1^2\omega_5^2\omega_{21}\omega_9^3\omega_{12} - 36c_s^4\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 36c_s^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 36c_s^2v_2^3\omega_5^3\omega_{21}\omega_{15}\omega_9^3 + 12v_2^2\omega_5^3\omega_{21}\omega_9^3\omega_{12}^2 + 180c_s^4\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - \\
& 6v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 18c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 6c_s^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 24v_2^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 12v_2^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + \\
& 36c_s^4\omega_5^2\omega_{15}\omega_9^3\omega_{12} - 12c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 6v_2^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 12v_2^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3 + 18c_s^4\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 36c_s^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - \\
& 18c_s^2\omega_5^3\omega_9^3\omega_{12} + 6c_s^2v_1^2\omega_5^2\omega_{21}\omega_9^3\omega_{12} - 12c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12c_s^2v_1^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} + 12c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 24v_2^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - \\
& 12c_s^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 18v_2^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 6c_s^2\omega_5^2\omega_{21}\omega_9^3\omega_{12} + 12c_s^4\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 12v_2^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12c_s^2v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + \\
& 12v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 18c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2\omega_5^3\omega_9^3\omega_{12} + 24v_2^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} - \\
& 88c_s^4\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 72c_s^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 6c_s^2v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12c_s^2v_1^2\omega_5^3\omega_9^3\omega_{12} + 36v_2^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 18c_s^4\omega_5^3\omega_{21}\omega_9^3\omega_{12} - \\
& 12c_s^2v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12v_2^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 36c_s^4\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 12v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12v_2^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3 + 6v_2^2\omega_5^3\omega_9^3\omega_{12}^2 \frac{v_1}{12\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2}
\end{aligned}$$

$$C_{D_x^2 D_y^2 \rho}^{(1), \text{MRT}^2} = C_{D_x^2 D_y^2 \rho}^{(1), \text{MRT}^1}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 \rho}^{(1), \text{CLBM}^1} = & (-12\omega_5\omega_9^3\omega_{12}^2 + 36c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_{12}^2 + 6\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 36c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - 12\omega_5\omega_{15}\omega_9^3\omega_{12} - 36c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + \\
& 12v_1^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 36c_s^2\omega_5\omega_{21}\omega_9^3\omega_{12} + 36c_s^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 18\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 6v_1^2\omega_5^2\omega_{21}\omega_9^3\omega_{12} + 12\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36c_s^2\omega_5\omega_9^3\omega_{12}^2 + \\
& 2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3 - 36c_s^2\omega_5\omega_{15}\omega_9^3\omega_{12}^2 + 12\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - 12v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 6v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} - \\
& 18\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36c_s^2\omega_5\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^2\omega_{21}\omega_{15}\omega_9^3 + 12\omega_5\omega_{21}\omega_9^3\omega_{12}^2 - 12\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 36c_s^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 12\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 - \\
& 12v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 18\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12\omega_5^2\omega_{21}\omega_{15}\omega_{12}^2 - 36c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12\omega_5\omega_{15}\omega_9^3\omega_{12}^2 - \\
& 36c_s^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 6v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2 + 12v_1^2\omega_5\omega_9^3\omega_{12}^2 - 12\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - \omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 12v_1^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_5\omega_{21}\omega_9^3\omega_{12}^2 - \\
& 6v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 36c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - 6c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2 + 12\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 18c_s^2\omega_5^2\omega_{21}\omega_9^3\omega_{12}^2 + \\
& 18v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_{12}^2 + 54c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 6\omega_5^2\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_5\omega_{15}\omega_9^3\omega_{12} - 36c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3 - 6v_1^2\omega_5^2\omega_9^3\omega_{12}^2 - \\
& 2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 18c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - 18c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 18v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + \\
& 54c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12}^2 + 6\omega_5^2\omega_9^3\omega_{12}^2 - 12\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 12v_1^2\omega_5\omega_{15}\omega_9^3\omega_{12} - 36c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + \\
& 18v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 5c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 6\omega_5^2\omega_{21}\omega_9^3\omega_{12}^2 - 40c_s^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 18c_s^2\omega_5^2\omega_9^3\omega_{12}^2 - \\
& 18c_s^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12v_1^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 54c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 12\omega_5\omega_{21}\omega_{15}\omega_9^3 - 6\omega_5^2\omega_{15}\omega_9^3\omega_{12}^2) \frac{c_s^2 v_1}{12\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12}^2}
\end{aligned}$$

$$C_{D_x^2 D_y^2 \rho}^{(1), \text{CLBM}^2} = C_{D_x^2 D_y^2 \rho}^{(1), \text{CLBM}^1}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 \rho}^{(1), \text{CuLBM}^1} = & (-18\omega_4^3\omega_1\omega_9 + 12c_s^2\omega_4^2\omega_1^2\omega_9^2 - 12v_1^2\omega_4^3\omega_1\omega_9^2 + 12v_1^2\omega_1^2\omega_9^2 - 4\omega_4^2\omega_1^2\omega_9^2 + 12v_1^2\omega_4^3\omega_1^2 + 54c_s^2\omega_4^3\omega_1\omega_9 + 6v_1^2\omega_4^2\omega_1^2\omega_9 + \\
& 12v_1^2\omega_4^3\omega_9^2 + 4v_1^2\omega_1^2\omega_9^2 - 12v_1^2\omega_4^3\omega_9 - 6\omega_4^2\omega_1^2\omega_9 - 12v_1^2\omega_4^3\omega_1 - 40c_s^2\omega_4^3\omega_1\omega_9^2 + 18v_1^2\omega_4^3\omega_1\omega_9 - 12v_1^2\omega_4^3\omega_9^2 + 12\omega_4^3\omega_1\omega_9^2 + 18c_s^2\omega_4^2\omega_1^2\omega_9 - \\
& 12v_1^2\omega_4^3\omega_1^2 + 36c_s^2\omega_4^3\omega_9^2 - 12\omega_4^3\omega_9^2 - 6v_1^2\omega_4^3\omega_1^2\omega_9 - 18v_1^2\omega_4\omega_1^2\omega_9^2 + 36c_s^2\omega_4^3\omega_9^2 - \omega_4^3\omega_1^2\omega_9^2 - 12\omega_4^3\omega_1^2 + 36c_s^2\omega_4^2\omega_1\omega_9 + 6v_1^2\omega_4^2\omega_1\omega_9^2 - 12\omega_1^2\omega_9^2 - \\
& 12\omega_2^2\omega_1\omega_9 + 5c_s^2\omega_4^3\omega_1^2\omega_9^2 + 36c_s^2\omega_1^2\omega_9^2 - 6\omega_4^2\omega_1\omega_9^2 - 54c_s^2\omega_4\omega_1^2\omega_9^2 - 36c_s^2\omega_4^2\omega_9^2 + 12\omega_2^2\omega_1^2 - 18c_s^2\omega_4^3\omega_1^2\omega_9 + 12v_1^2\omega_4^2\omega_1\omega_9 - 36c_s^2\omega_1^2\omega_1^2 + \\
& 12\omega_1^2\omega_9^2 - 36c_s^2\omega_4^3\omega_9 + 12\omega_4^3\omega_1 + 6\omega_4^3\omega_1^2\omega_9 + 18c_s^2\omega_4^3\omega_1\omega_9^2 + 18\omega_4\omega_1^2\omega_9^2 - 36c_s^2\omega_4^3\omega_1 + v_1^2\omega_4^3\omega_1^2\omega_9^2 + 12\omega_4^3\omega_9) \frac{c_s^2 v_1}{12\omega_4^3\omega_1^2\omega_9^2}
\end{aligned}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 \rho}^{(1), \text{CuLBM}^2} = & (-28\omega_3^2c_s^2v_1^2\omega_4^2\omega_1\omega_2^2 + 24\omega_3^2v_2^4\omega_4^2\omega_1^3 + 9\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 36\omega_3^2c_s^2v_1^2\omega_4\omega_1^2\omega_2^3 + 96\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3^2c_s^2\omega_1^2\omega_2^3 - 18c_s^2\omega_4^2\omega_1^3\omega_2^3 + \\
& 18c_s^2v_1^2\omega_4^3\omega_2^3 + 4\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^2 - 52\omega_3^2c_s^2\omega_4^2\omega_1^3 - 24\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_2^3 - 119\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 54\omega_3^2c_s^4\omega_1^3\omega_2^3 - 102\omega_3^2c_s^4\omega_2^2\omega_1^3\omega_2 + 24\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^3 + \\
& 24\omega_3^2v_2^2\omega_1^2\omega_2^3 - 324\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^3 + 12c_s^2\omega_4^2\omega_1^3\omega_2^2 - 138\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^3 - 216\omega_3^2c_s^2v_2^2\omega_4^2\omega_2^3 + 108\omega_3c_s^4\omega_1^2\omega_1^2\omega_2^3 + 4\omega_3^2c_s^2v_1^2\omega_4^2\omega_1\omega_2^3 - \\
& 12\omega_3c_s^4\omega_4^2\omega_1^2\omega_2 + 66\omega_3^2v_2^2\omega_2^2\omega_1^3\omega_2 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 27\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_2^3 + 4\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^3 - 12c_s^2v_1^2\omega_4^3\omega_1^3\omega_2^3 - 108\omega_3^2c_s^4\omega_1^2\omega_2^3 - 27\omega_3^2v_2^3\omega_4^2\omega_1^3\omega_2^3 + \\
& 15\omega_3^2c_s^4\omega_2^2\omega_1^3\omega_2^3 + 28\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 48\omega_3^2v_2^2\omega_1^2\omega_2^3 - 24c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^3 - 28\omega_3c_s^2v_1^2\omega_1^2\omega_2^3 - 48\omega_3^2v_2^2v_1^2\omega_4^2\omega_1\omega_2^3 + 216\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3 + 72\omega_3^2c_s^4\omega_4^2\omega_1^3 + \\
& 138\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^3 - 4\omega_3^2\omega_4^2\omega_1\omega_2^3 + 24c_s^2\omega_4^2\omega_1^2\omega_2^3 + 28\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 72\omega_3^2v_2^2\omega_4^2\omega_1\omega_2^3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 9\omega_3^2c_s^2v_1^2\omega_4\omega_1\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - \\
& 30\omega_3^2v_2^2v_1^2\omega_4\omega_1\omega_2^3 - 60\omega_3^2v_2^2\omega_4^2\omega_2^3 + 12\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_2 + 35\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 27\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 + 36\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^3 - 58\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + \\
& 36\omega_3^2v_2^2v_1^2\omega_4^2\omega_2^3 - 4\omega_3^2\omega_1^2\omega_1\omega_2^3 + 32\omega_3c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^3 + 54c_s^4\omega_4^2\omega_1^2\omega_2^3 - 30\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^2\omega_2 + 4\omega_3^2v_1^2\omega_4^2\omega_1^2\omega_2 - 32\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 - 27\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + \\
& 4\omega_3^2\omega_4^2\omega_1^3 + 3\omega_3^2c_s^2v_1^2\omega_4^2\omega_2^3\omega_2^3 - 36\omega_3^2v_4^2\omega_1^2\omega_2^3 + 49\omega_3^2c_s^2\omega_4^2\omega_2^3\omega_2^3 - 4\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^2\omega_2 + 74\omega_3^2c_s^2\omega_4^2\omega_2^3\omega_2 - 4\omega_3^2\omega_1^2\omega_1^3\omega_2 - 36\omega_3c_s^2\omega_4^2\omega_2^3\omega_2^3 + \\
& 4\omega_3^2c_s^2\omega_1^2\omega_2 - 4\omega_3c_s^2v_1^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^3 + 60\omega_3^2v_2^2v_1^2\omega_1^2\omega_2^3 - 36c_s^4\omega_1^2\omega_2^3 + 36\omega_3c_s^2v_1^2\omega_4^2\omega_2^3\omega_2^3 - 4\omega_3^2v_1^2\omega_4^2\omega_1^3 + 8\omega_3^2\omega_4^2\omega_1^2\omega_2^3 + \\
& 16\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^3 - 36\omega_3^2v_4^2\omega_4^2\omega_1^3\omega_2 + 8\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^3\omega_2 - 16\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 27\omega_3^2v_4^2\omega_4^2\omega_1^2\omega_2^3 + 324\omega_3^2c_s^2v_2^2\omega_4^2\omega_1\omega_2^3 - 4\omega_3^2\omega_4^2\omega_1^2\omega_2 + 27\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - \\
& 3\omega_3^2c_s^2\omega_1^2\omega_2^3 - 32\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^3 - 84\omega_3c_s^4\omega_4^2\omega_1\omega_2^3 + 4\omega_3^2c_s^2v_1^2\omega_4^2\omega_1\omega_2 - 20\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^3\omega_2 - 72\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 42\omega_3^2v_2^2\omega_4^2\omega_1\omega_2^3 + \\
& 108\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^3 - 4\omega_3^2v_1^2\omega_4^2\omega_2^3 - 12\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^2\omega_2 - 72c_s^4\omega_4^2\omega_1^2\omega_2^3 + 4\omega_3^2v_1^2\omega_4^2\omega_1^3\omega_2 + 16\omega_3^2c_s^2v_1^2\omega_4^2\omega_2^3 - 25\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 16\omega_3^2c_s^2v_1^2\omega_4^2\omega_2^3 + \\
& 18\omega_3^2c_s^2v_1^2\omega_1^3\omega_2^3 - 9\omega_3c_s^2v_1^2\omega_4^2\omega_1^3\omega_2^3 - 8\omega_3^2v_1^2\omega_4^2\omega_1^2\omega_2^3 + 4\omega_3^2\omega_4^2\omega_2^3 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 12\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 78\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3) \frac{v_1}{36\omega_3^2\omega_4^2\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y^2 v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 v_1}^{(1), \text{SRT}} = (-24 + 72v_1 - 108v_1^2\omega + 36v_1^2\omega^2 - 12\omega^2 + 36\omega + 8c_s^2\omega^2 - c_s^2\omega^3 - 18c_s^2\omega + 12c_s^2) \frac{c_s^2 \rho}{12\omega^3}$$

$$\begin{aligned}
C_{D_x^2 D_y^2 v_1}^{(1), \text{MRT}^1} = & (12c_s^2v_2^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 12c_s^4\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 12c_s^4\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 24v_2^2\omega_5\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 18v_2^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} - \\
& 36v_2^2v_1^2\omega_5^2\omega_{15}\omega_9^3\omega_{12} + 24c_s^2v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3 - 108c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 6c_s^2v_2^2\omega_5^3\omega_{21}\omega_9^3\omega_{12} - 18v_2^2v_1^2\omega_5^3\omega_9^3\omega_{12} - 12c_s^2v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + \\
& 12c_s^2v_2^2\omega_5^3\omega_9^3\omega_{12} - 36v_2^2v_1^2\omega_5^3\omega_{15}\omega_9^3\omega_{12} - 12v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3 + 78c_s^2v_1^2\omega_5^3\omega_{21}\omega_{15}\omega_9^3\omega_{12} + 24v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} - 48c_s^2v_1^2\omega_{21}\omega_{15}\omega_9^3\omega_{12} +
\end{aligned}$$

$$36\omega_3 c_s^4 \omega_4 \omega_1^2 \omega_2^3 + \omega_3 v_1^4 \omega_4 \omega_1^3 \omega_2^2 - 30\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^2 \omega_2^3 - 174\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^3 \omega_2 + 54\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2^3 + 12\omega_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 20\omega_3^2 c_s^2 \omega_4 \omega_1^3 + 18\omega_3^2 v_2^4 \omega_1 \omega_2^3 + 72\omega_3^2 v_2^2 v_1^2 \omega_4 \omega_1^3 + 90\omega_3 c_s^3 v_2^2 \omega_4 \omega_1^3 \omega_2^2 + 9\omega_3^2 v_2^2 \omega_4 \omega_1^2 \omega_2^3 + 28\omega_3^2 c_s^3 \omega_4 \omega_1^2 \omega_2^2 + 66\omega_3^2 v_2^2 \omega_4 \omega_1^3 \omega_2 - 18\omega_3 v_2^2 \omega_1^3 \omega_2^2) \frac{\rho}{36\omega_3^2 \omega_4 \omega_1^3 \omega_2^3}$$

coefficient $C_{D_x^2 D_y^2 v_2}^{(1)}$ at $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{SRT}} = 0$$

[illegible]

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{MRT2}} = C_{D_x^2 D_y^2 v_2}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(1), \text{CuLBM2}} =$$

$$\begin{aligned} & (-18c_s^2\omega_1\omega_3^2 + 60\omega_3v_2^2\omega_1\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 84\omega_3c_s^2\omega_1^3 + 6\omega_1\omega_3^2 + 18\omega_3v_1^2\omega_1^2\omega_2^2 + 141\omega_3v_2^2\omega_1\omega_3^2 - 23\omega_3\omega_1^3\omega_2^2 + 48\omega_3v_2^2\omega_1^3 - 9\omega_3v_1^2\omega_1^3\omega_2 - 6v_1^2\omega_1^3\omega_2 + \\ & 48\omega_3\omega_1^4\omega_2 + 23\omega_3\omega_1^2\omega_3^2 - 114\omega_3v_2^2\omega_3^2 + 12\omega_3\omega_1^2\omega_3^2 - 12\omega_3v_1^2\omega_1^2\omega_3^2 + 12v_2^2\omega_1^2\omega_3^2 - 66\omega_3c_s^2\omega_3^3 + 108\omega_3c_s^2\omega_1\omega_3^3 - 12\omega_3\omega_1\omega_3^2 + 6\omega_3v_2^2\omega_1^2\omega_3^2 - \\ & 108\omega_3c_s^2\omega_1^3\omega_3^2 + 42\omega_3\omega_3^3 - 42\omega_3c_s^2\omega_1^2\omega_3^3 - 6v_1^2\omega_1\omega_3^3 + 12\omega_3v_1^2\omega_3^3 - 60\omega_3\omega_1\omega_3^3 + 50\omega_3v_2^2\omega_1\omega_3^3 - 18\omega_3c_s^2\omega_1^2\omega_3^2 + 12\omega_3v_1^2\omega_1^3 - 75\omega_3v_2^2\omega_1^3\omega_2 + \\ & 36c_s^2\omega_1^2\omega_3^2 - 50\omega_3v_2^2\omega_1^2\omega_3^2 - 9\omega_3v_1^2\omega_1\omega_3^2 - 12\omega_1^2\omega_3^2 - 66\omega_3v_2^2\omega_1^2\omega_3^2 - 18c_s^2\omega_1^3\omega_2 + 42\omega_3c_s^2\omega_1^3\omega_2^2 - 12\omega_3v_1^2\omega_1\omega_3^2 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3) \frac{v_2v_1\rho}{18\omega_3\omega_1^3\omega_3^2} \end{aligned}$$

coefficient $C_{D_x D_y^3 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1 \partial x_2^3}$:

$$C_{D_X D_Y^3 \rho}^{(1), \text{SRT}} = (24 - \omega^3 + 14\omega^2 - 36\omega + v_2^2\omega^3 - 42c_s^2\omega^2 + 3c_s^2\omega^3 - 14v_2^2\omega^2 + 36v_2^2\omega + 108c_s^2\omega - 72c_s^2 - 24v_2^2) \frac{c_s^2 v_2}{12\omega^3}$$

$$C_{D, \mathbf{x} \frac{3}{2} \rho}^{(1), \text{MRT1}} = (-72c_s^2 v_1^2 \omega_{10}^5 \omega_5 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 36c_s^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_9 + 36c_s^2 v_1^2 \omega_{10}^5 \omega_{15}^2 \omega_5 \omega_{21} \omega_{15} \omega_{12} - 6v_1^2 \omega_{10} \omega_5^3 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 36c_s^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_9 \omega_{12} - 6c_s^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_9 \omega_{12} - 12c_s^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_9 \omega_{12} + 36v_1^2 \omega_{10} \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} - 12c_s^2 v_2^2 \omega_{10} \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 - 12v_1^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_9 + 54c_s^4 \omega_{10} \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 12v_2^2 v_1^2 \omega_{10} \omega_5^2 \omega_{21} \omega_{15}^2 - 12c_s^2 \omega_{10}^5 \omega_5 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} - 18c_s^2 v_1^2 \omega_{10}^5 \omega_5^3 \omega_{15} \omega_9 \omega_{12} - 18c_s^2 v_1^2 \omega_{10}^5 \omega_5^3 \omega_{15}^2 \omega_{12} - 12c_s^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_9 \omega_{12} - 6c_s^4 \omega_{10}^5 \omega_5^3 \omega_{21} \omega_9 \omega_{12} + 9v_2^2 v_1^2 \omega_{10} \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} + 12v_1^2 \omega_{10} \omega_5^3 \omega_{21} \omega_{15}^2 - 36c_s^4 \omega_{10}^5 \omega_5^3 \omega_{15}^2 \omega_9 - 24v_1^2 \omega_{10} \omega_5 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} - 6v_1^2 \omega_{10}^5 \omega_3^2 \omega_{21} \omega_9 \omega_{12} - 36c_s^4 \omega_{10} \omega_5 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} - 6v_2^2 v_1^2 \omega_{10}^5 \omega_5^3 \omega_{15} \omega_9 \omega_{12} + 12v_2^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_{12} + 12c_s^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_9 \omega_{12} + 6v_2^2 v_1^2 \omega_{10}^5 \omega_{15}^2 \omega_9 \omega_{12} + 24v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_{12} - 5c_s^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} + 12v_2^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_{12} - 12v_1^2 \omega_{10}^5 \omega_5^2 \omega_{15} \omega_9 \omega_{12} + 36c_s^4 \omega_{10}^5 \omega_5^2 \omega_{15} \omega_9 \omega_{12} + 12v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_{12} + 14c_s^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 12v_1^2 \omega_{10}^5 \omega_5^3 \omega_{15}^2 + 12c_s^2 \omega_{10}^5 \omega_5^3 \omega_{15}^2 \omega_9 - 12v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 12v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 3c_s^2 \omega_{10}^5 \omega_3^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 18c_s^4 \omega_{10}^5 \omega_5^2 \omega_{15}^2 \omega_{12} + 27c_s^2 v_1^2 \omega_{10} \omega_5^3 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} + 156c_s^4 \omega_{10}^5 \omega_5 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} - 96c_s^4 \omega_{10}^5 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} + 12v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{15} \omega_9 \omega_{12} - 12v_1^2 \omega_{10}^5 \omega_5^3 \omega_{21} \omega_{15} \omega_{12} + c_s^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} + 12c_s^4 \omega_{10}^5 \omega_5^2 \omega_{15} \omega_9 \omega_{12} + 12v_1^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_9 \omega_{12} - 18c_s^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} + 48v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 36c_s^2 v_1^2 \omega_{10} \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 6v_2^2 v_1^2 \omega_{10}^5 \omega_3^2 \omega_{21} \omega_9 \omega_{12} - 12c_s^2 v_2^2 \omega_{10} \omega_5^3 \omega_{21} \omega_{15}^2 + 6v_1^2 \omega_{10}^5 \omega_3^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 18c_s^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 24v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_{12} - 6v_2^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 18c_s^2 \omega_{10}^5 \omega_5^2 \omega_{15} \omega_9 \omega_{12} + 12c_s^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_9 \omega_{12} - 24v_2^2 v_1^2 \omega_{10}^5 \omega_5 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 6c_s^2 v_2^2 \omega_{10} \omega_5^2 \omega_{21} \omega_{15}^2 \omega_{12} + 6c_s^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{15} \omega_9 \omega_{12} + 15v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 15c_s^4 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} + 36c_s^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{15}^2 + 18c_s^2 v_1^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_9 \omega_{12} + 12c_s^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_{12} - 12c_s^2 v_2^2 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15} \omega_9 \omega_{12} - 60c_s^4 \omega_{10}^5 \omega_5^2 \omega_{21} \omega_{15}^2 \omega_9 \omega_{12} +$$

$$\begin{aligned}
& 6c_s^2\omega_{10}\omega_5^3\omega_{15}\omega_9\omega_{12} + 36c_s^2v_1^2\omega_{10}^2\omega_5^2\omega_{15}\omega_9\omega_{12} + 12c_s^2v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 12c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 12c_s^2\omega_{10}^2\omega_5^3\omega_{15}^2 - 36c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2 - \\
& 12c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9 - 6v_2^2v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_{12} + 12v_2^2v_1^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 3c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 15v_2^2v_1^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - \\
& 12v_2^2v_1^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} + 12c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{15}^2 + 24v_1^2\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} + 24v_2^2v_1^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} + 18c_s^2v_1^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + \\
& 36c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 12c_s^4\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 12v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 18c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 6v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} - \\
& 12c_s^2v_2^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 6v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} + 18c_s^4\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} + 36c_s^4\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9 + 5c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} - \\
& 12v_2^2v_1^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 - 108c_s^2v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9 - 108c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 12c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - 36c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + \\
& 12v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9 + 12c_s^2v_2^2\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 36c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 3c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 72c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} - \\
& 6c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{15}\omega_9\omega_{12} + 36c_s^2v_1^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 12c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2 + 36c_s^2v_1^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9 - 48v_1^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - \\
& 36c_s^2v_1^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} + 72c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 6c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 12c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{21}\omega_9\omega_{12} + 6v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_{12} - \\
& 42c_s^4\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 6c_s^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} + 12c_s^2v_2^2\omega_{10}^2\omega_5^2\omega_{15}\omega_9\omega_{12} - 12c_s^2v_2^2\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 6c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_{12} + \\
& 24v_2^2v_1^2\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 9v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 36c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 12c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 - 15c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + \\
& 6c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{21}\omega_9\omega_{12} + 12c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} + 12c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} + 18c_s^2v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} - 18c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - \\
& 12c_s^2v_2^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9 + 12v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 36c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 12v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 6v_2^2v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} - \\
& 18c_s^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 6v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 45c_s^2v_1^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 6v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - c_s^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} - \\
& 12v_1^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 18c_s^2v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 36c_s^4\omega_{10}^2\omega_5^3\omega_{15}^2 - 36v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 12v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + \\
& 12v_1^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 36c_s^4\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 24v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12}) \frac{v_2}{12\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12}}
\end{aligned}$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{MRT}^2} = C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{MRT}^1}$$

$$\begin{aligned}
C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{CLBM1}} &= (-12v_2^2\omega_5^2\omega_{21}\omega_{15}^2 - 18c_s^2\omega_{10}\omega_5^2\omega_{15}^2\omega_{12} - 12v_2^2\omega_{10}\omega_{21}\omega_{15}\omega_9\omega_{12} - \omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 36c_s^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} - \\
& 12\omega_{10}\omega_5\omega_{15}\omega_9\omega_{12} - 36c_s^2\omega_{10}\omega_5^2\omega_{15}^2\omega_9 - 36c_s^2\omega_5\omega_{21}\omega_{15}^2\omega_9 - 18c_s^2\omega_{10}\omega_5^2\omega_{15}\omega_9\omega_{12} + 12v_2^2\omega_{10}\omega_5\omega_{15}\omega_9\omega_{12} + 12\omega_{10}\omega_{21}\omega_{15}\omega_9\omega_{12} + \\
& 12\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 6\omega_{10}\omega_5^2\omega_{15}^2\omega_9\omega_{12} + 12\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 5v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 12\omega_{10}\omega_5^2\omega_{15}^2\omega_9 - 6v_2^2\omega_{10}\omega_5^2\omega_{15}^2\omega_{12} + 12\omega_5\omega_{21}\omega_{15}^2\omega_9 - \\
& 12v_2^2\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 12v_2^2\omega_{10}\omega_5^2\omega_{15}^2 - 18\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 3c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 12v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9 - 12v_2^2\omega_{10}\omega_5\omega_{21}\omega_9\omega_{12} + \\
& 18c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12} - 12v_2^2\omega_{10}\omega_5^2\omega_{15}^2\omega_9 + 6\omega_{10}\omega_5^2\omega_{15}^2\omega_{12} - 12v_2^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 36c_s^2\omega_{10}\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 12\omega_{10}\omega_5\omega_{21}\omega_9\omega_{12} + \\
& 18v_2^2\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 6v_2^2\omega_{10}\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 36c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 5\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 36c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} + v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + \\
& 18v_2^2\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 9c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 36c_s^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 - 12\omega_{10}\omega_5\omega_{15}^2\omega_9 + 6\omega_{10}\omega_5^2\omega_{15}\omega_9\omega_{12} + 12\omega_5^2\omega_{21}\omega_{15}^2 - \\
& 36c_s^2\omega_{10}\omega_{21}\omega_{15}\omega_9\omega_{12} + 18c_s^2\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} + 12v_2^2\omega_{10}\omega_5\omega_{15}^2\omega_9 - 36c_s^2\omega_5^2\omega_{21}\omega_{15}^2 + 54c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 3v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - \\
& 6v_2^2\omega_{10}\omega_5^2\omega_{15}\omega_9\omega_{12} + 36c_s^2\omega_{10}\omega_5\omega_{15}\omega_9\omega_{12} - 12\omega_{10}\omega_5^2\omega_{15}^2 - 12v_2^2\omega_{10}\omega_{21}\omega_{15}\omega_9\omega_{12} + 3\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9 - \\
& 6\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - 36c_s^2\omega_{10}\omega_5\omega_{21}\omega_9\omega_{12} + 6v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12} - 12\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 6v_2^2\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} + 36c_s^2\omega_{10}\omega_5\omega_{15}^2\omega_9 + 12\omega_{10}\omega_5\omega_{15}^2\omega_9\omega_{12} - \\
& 15c_s^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 18c_s^2\omega_{10}\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 12v_2^2\omega_{10}\omega_5\omega_{15}^2\omega_9\omega_{12} + 36c_s^2\omega_{10}\omega_5^2\omega_{15}^2 + 54c_s^2\omega_5\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 6\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12} - \\
& 18\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 12\omega_{10}\omega_{21}\omega_{15}^2\omega_9\omega_{12}) \frac{c_s^2v_2}{12\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12}}
\end{aligned}$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{CLBM2}} = C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{CLBM1}}$$

$$\begin{aligned}
C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{CuLBM1}} &= (-\omega_7^2\omega_1^2 + 12\omega_7\omega_5 - 3v_2^2\omega_7\omega_1^2\omega_5 + 3c_s^2\omega_7^2\omega_1^2 + 6v_2^2\omega_7^2\omega_5 - 36c_s^2\omega_7\omega_5 - 12v_2^2\omega_7^2\omega_1\omega_5 + 12\omega_7^2 + 6v_2^2\omega_7^2\omega_1 + v_2^2\omega_7^2\omega_1^2 + \\
& 18c_s^2\omega_1^2\omega_5 - \omega_7^2\omega_1^2\omega_5 - 12v_2^2\omega_7\omega_5 + 54c_s^2\omega_7\omega_1\omega_5 - 6\omega_7^2\omega_5 + 18c_s^2\omega_7^2\omega_1 + 3c_s^2\omega_7^2\omega_1^2\omega_5 - 18\omega_7\omega_1\omega_5 - 6\omega_7^2\omega_1 + 3\omega_7\omega_1^2\omega_5 - 36c_s^2\omega_7^2\omega_1\omega_5 + \\
& 36c_s^2\omega_7\omega_1 - 12\omega_7\omega_1 - 36c_s^2\omega_1\omega_5 - 6v_2^2\omega_7\omega_1^2 + 12v_2^2\omega_7^2\omega_5 - 9c_s^2\omega_7\omega_1^2\omega_5 + 12\omega_7^2\omega_1\omega_5 + 12\omega_1\omega_5 + v_2^2\omega_7^2\omega_1^2\omega_5 + 12v_2^2\omega_7\omega_1 - 36c_s^2\omega_7^2 + 6\omega_7\omega_1^2 + \\
& 18v_2^2\omega_7\omega_1\omega_5 - 12\omega_7^2\omega_5 - 12v_2^2\omega_1\omega_5 - 18c_s^2\omega_7\omega_1^2 - 12v_2^2\omega_7^2 + 36c_s^2\omega_7^2\omega_5) \frac{c_s^2v_2}{12\omega_7^2\omega_1^2\omega_5}
\end{aligned}$$

$$\begin{aligned}
C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(1),\text{CuLBM2}} &= \\
& (48\omega_3^2v_2^4\omega_4^3\omega_1^3 + 9\omega_3^2c_s^2\omega_4^3\omega_1^3\omega_2^3 + 18\omega_3^2c_s^2v_2^3\omega_1^3\omega_2^3 + 120\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3^2c_s^2\omega_1^2\omega_2^3 - 18c_s^2\omega_4^2\omega_1^3\omega_2^3 - 412\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 104\omega_3^2c_s^2\omega_4^2\omega_1^3 + \\
& 104\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_2^2 - 342\omega_3^2c_s^4\omega_1^2\omega_2^2\omega_3^2 + 54\omega_3^2c_s^4\omega_1^3\omega_3^2 - 9\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_3^2 - 276\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2 + 160\omega_3^2v_2^2\omega_4^2\omega_3^2 - 712\omega_3^2c_s^2v_2^3\omega_4^2\omega_1^2\omega_2 + 6\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2^2 - \\
& 460\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_3^2 - 784\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 + 216\omega_3c_s^4\omega_4^2\omega_1^2\omega_3^2 + 48\omega_3c_s^4\omega_1^2\omega_3^2\omega_2 + 152\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2 - 36\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 12\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + \\
& 92\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_3^2 - 288\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_3^2 + 72\omega_3c_s^2v_2^3\omega_4^2\omega_1^2\omega_3^2 - 108\omega_3^2c_s^4\omega_1^2\omega_3^2 - 92\omega_3^2v_2^3\omega_4^2\omega_1^3\omega_2^2 + 18\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_3^2 + 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2 + 56\omega_3c_s^2\omega_4^2\omega_1\omega_3^2 - \\
& 56\omega_3^2v_2^2\omega_4^2\omega_1^3 + 16\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 + 320\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3 + 144\omega_3^2c_s^2\omega_1^2\omega_3^2 + 394\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1\omega_2^2 + 36c_s^2\omega_4^2\omega_1^2\omega_3^2 - 6\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2^2 + \\
& 56\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 228\omega_3^2v_2^3\omega_4^2\omega_1\omega_3^2 - 18\omega_3^2c_s^2\omega_1^3\omega_3^2 - 108\omega_3c_s^4\omega_4^2\omega_1^2\omega_3^2 - 36\omega_3^2c_s^2v_2^2\omega_1^2\omega_3^2 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_3^2 - 144\omega_3^2v_2^3\omega_4^2\omega_1^3\omega_2^2 - 136\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2 + \\
& 144\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 40\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^2 + 208\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 24\omega_3^2v_2^3\omega_4^2\omega_1\omega_2^2 - 368\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 448\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 + \\
& 28\omega_3^2\omega_4^2\omega_1\omega_2^2 + 6\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 54c_s^4\omega_4^2\omega_1^3\omega_2^2 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - 27\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 + 8\omega_3^2\omega_4^2\omega_1^3 - 96\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_2^2 + 184\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + \\
& 208\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - 14\omega_3^2\omega_4^2\omega_1^2\omega_2^2 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2 - 72\omega_3c_s^2\omega_4^2\omega_1^2\omega_3^2 - 56\omega_3c_s^2v_2^2\omega_4^2\omega_1\omega_3^2 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 - 36c_s^2v_2^2\omega_4^2\omega_1^2\omega_3^2 - 6\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2^2 - \\
& 9\omega_3^2c_s^2v_2^3\omega_4\omega_1^3\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 132\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2 + 18\omega_3^2c_s^2v_1^4\omega_4^2\omega_1^3\omega_2^2 + 52\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 78\omega_3^2v_2^3\omega_4^2\omega_1^2\omega_2^2 + 1232\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_3^2 + \\
& 16\omega_3^2\omega_4^2\omega_1^2\omega_2 + 78\omega_3^2v_2^3\omega_4^2\omega_1^3\omega_2^2 - 6\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 - 18\omega_3^2c_s^2v_1^4\omega_4^2\omega_1^3\omega_2^2 - 168\omega_3c_s^4\omega_4^2\omega_1\omega_3^2 - 88\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2 - 144\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 - 256\omega_3^2v_2^2\omega_4^2\omega_1\omega_3^2 + \\
& 108\omega_3^2c_s^4\omega_4\omega_1^2\omega_3^2 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 + 6\omega_3^2v_1^4\omega_4^2\omega_1^2\omega_2^2 - 108c_s^4\omega_4^2\omega_1^2\omega_3^2 + 120\omega_3^2v_2^4\omega_4^2\omega_1^2\omega_2 - 118\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^2 + 36\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_3^2 - \\
& 56\omega_3^2c_s^2v_2^2\omega_4^2\omega_1\omega_2^2 + 14\omega_3^2\omega_4^2\omega_1^3\omega_2^2 - 16\omega_3^2\omega_4^2\omega_2^3 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 + 32\omega_3^2v_2^2\omega_4^2\omega_1\omega_2^2 + 18c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 588\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2) \frac{v_2}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2} :$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(1),\text{SRT}} = (2 - \omega + v_2^2\omega + 3c_s^2\omega - 6c_s^2 - 2v_2^2) \frac{v_2v_1\rho}{12\omega}$$

$$12c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9 - 5c_s^4\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12} - 12c_s^2v_2^2\omega_{10}^3\omega_5^3\omega_{21}\omega_9\omega_{12} + 12c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 12c_s^2\omega_{10}^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} + 6c_s^2v_2^2\omega_{10}^2\omega_5^2\omega_{15}\omega_9\omega_{12} - 6c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 36c_s^2v_2^2\omega_{10}\omega_5^3\omega_{15}^2\omega_9 + 12v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 12c_s^4\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 12v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9 + 18v_2^2v_1^2\omega_{10}^2\omega_5^3\omega_{15}^2\omega_9\omega_{12} + 18c_s^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 18v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 15c_s^2v_1^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 18v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 12v_1^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 54c_s^2v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 12c_s^4\omega_{10}^2\omega_5^2\omega_{15}^2 - 108v_2^2v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_9\omega_{12} + 36v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_9 + 12v_1^2\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 12c_s^4\omega_{10}^2\omega_5^2\omega_{15}^2\omega_9\omega_{12} - 24v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_{12}) \frac{\rho}{12\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}^2\omega_9\omega_{12}}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{MRT}2} = C_{D_x D_y^3 v_2}^{(1), \text{MRT}1}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CLBM}1} = (6\omega_{10}\omega_5^3\omega_{15}\omega_{12} - 36v_2^2\omega_{10}\omega_5^3\omega_{15}\omega_9 + 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + 6c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 18c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 18v_2^2\omega_{10}\omega_5^3\omega_{15}\omega_{12} + 12\omega_{10}\omega_5^3\omega_{15}\omega_9 - 12c_s^2\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 12c_s^2\omega_{10}\omega_5^3\omega_{15}\omega_9\omega_{12} - 36v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 6c_s^2\omega_{10}\omega_5^3\omega_9\omega_{12} + 12\omega_5^3\omega_{21}\omega_{15}\omega_9 + 6c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_9\omega_{12} + 6c_s^2\omega_{10}\omega_5^3\omega_{15}\omega_9\omega_{12} - 6\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 36v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9 + 12\omega_5^3\omega_{21}\omega_{15} - 12c_s^2\omega_{10}\omega_5^3\omega_{15}\omega_9 - 15v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 36v_2^2\omega_{10}\omega_5\omega_{21}\omega_9\omega_{12} - 18c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12} - 6c_s^2\omega_{10}\omega_5^3\omega_{15}\omega_{12} - c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} + 18v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 12\omega_5^3\omega_{21}\omega_{15}\omega_9 - 12c_s^2\omega_5^3\omega_{21}\omega_{15}\omega_9 - 12c_s^2\omega_5^3\omega_{21}\omega_{15} + 6\omega_{10}\omega_5^3\omega_9\omega_{12} + 36v_2^2\omega_{10}\omega_5^3\omega_{15} - 12\omega_{10}\omega_5\omega_{21}\omega_9\omega_{12} + 5\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12} - 18v_2^2\omega_{10}\omega_5^3\omega_9\omega_{12} + 12\omega_5\omega_{21}\omega_{15}\omega_9\omega_{12} - 5c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} + 12c_s^2\omega_{10}\omega_5^2\omega_9\omega_{12} + 54v_2^2\omega_5^2\omega_{21}\omega_{15}\omega_9\omega_{12} - 12\omega_{10}\omega_5^2\omega_{15}\omega_9\omega_{12} - 12c_s^2\omega_{10}\omega_5^2\omega_{15}\omega_9\omega_{12} - 6\omega_{10}\omega_5^3\omega_{21}\omega_9\omega_{12} + 18v_2^2\omega_{10}\omega_5^3\omega_{15}\omega_9\omega_{12} - 12\omega_{10}\omega_5^3\omega_{15} + 18\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12} + 12c_s^2\omega_{10}\omega_5^2\omega_{15}\omega_9) \frac{c_s^2\rho}{12\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9\omega_{12}}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CLBM}2} = C_{D_x D_y^3 v_2}^{(1), \text{CLBM}1}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CuLBM}1} = (-6\omega_3^2\omega_5 - 3v_2^2\omega_7\omega_1^2\omega_5 - 54v_2^2\omega_1^2\omega_5 - 12c_s^2\omega_7\omega_5 + 6c_s^2\omega_1^2\omega_5 - 18c_s^2\omega_1^2\omega_5 + 18v_2^2\omega_1^3\omega_5 + 18c_s^2\omega_7\omega_1\omega_5 + 18\omega_1^2\omega_5 + 6\omega_1^3 - 12\omega_1^2 + \omega_7\omega_1^2\omega_5 + 12c_s^2\omega_1^2 - 12c_s^2\omega_7\omega_1 - 18v_2^2\omega_1^3 + 3v_2^2\omega_7\omega_1^3 + 12\omega_7\omega_1 + 12c_s^2\omega_1\omega_5 + 18v_2^2\omega_7\omega_1^2 - 5c_s^2\omega_7\omega_1^2\omega_5 + 36v_2^2\omega_1^2 - 6c_s^2\omega_1^3 - 12\omega_1\omega_5 - \omega_7\omega_1^3 - 36v_2^2\omega_7\omega_1 + c_s^2\omega_7\omega_1^3 - 6\omega_7\omega_1^2 + 36v_2^2\omega_1\omega_5 - c_s^2\omega_7\omega_1^3\omega_5 + 6c_s^2\omega_7\omega_1^2) \frac{c_s^2\rho}{12\omega_7\omega_1^3\omega_5}$$

$$C_{D_x D_y^3 v_2}^{(1), \text{CuLBM}2} = (12\omega_3v_2^2\omega_4\omega_1\omega_2^2 + 94\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 4\omega_3\omega_4\omega_1\omega_2^2 + 40\omega_3c_s^2\omega_4\omega_2^3 + 8c_s^4\omega_4\omega_1\omega_2 - 18c_s^4\omega_4\omega_1\omega_2^3 + 3\omega_3c_s^2v_1^2\omega_4\omega_1\omega_2^2 - 264\omega_3v_2^4\omega_4\omega_1^3\omega_2^3 - 24\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 + 192\omega_3v_2^4\omega_4\omega_1^3\omega_2 - 54c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 + \omega_3v_1^2\omega_4\omega_1^2\omega_2^3 + 14\omega_3\omega_4\omega_1\omega_2^3 - 28\omega_3c_s^4\omega_4\omega_1\omega_2^2 - 222\omega_3v_2^2\omega_4\omega_1\omega_2^3 + 16\omega_3c_s^4\omega_4\omega_1^3 + 27c_s^2v_2^2\omega_4\omega_1^3\omega_2^3 - 16\omega_3c_s^2\omega_4\omega_1^2\omega_2 + 27\omega_3c_s^2v_2^2\omega_1^3\omega_2^3 + 138\omega_3v_2^4\omega_4\omega_1^3\omega_2^2 + 20c_s^4\omega_4\omega_1^2\omega_2^3 - 60\omega_3v_2^3\omega_4\omega_1^3 + 36\omega_3c_s^4\omega_1\omega_2^3 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 138\omega_3v_2^4\omega_4\omega_1^2\omega_2^3 + 60c_s^2v_2^2\omega_4\omega_1^2\omega_2^3 - 240\omega_3v_2^4\omega_4\omega_1^3\omega_2 - 60\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^2 - 68\omega_3c_s^4\omega_4\omega_2^3 + 9c_s^4\omega_4\omega_1^3\omega_2^3 - \omega_3v_1^2\omega_4\omega_1^3\omega_2^2 + 144\omega_3v_2^5\omega_4\omega_2^3 - 3\omega_3c_s^2v_1^2\omega_4\omega_1^3\omega_2^3 - 18c_s^4\omega_4\omega_1^3\omega_2^3 + 42\omega_3c_s^2\omega_4\omega_1^3\omega_2 + 432\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 54c_s^2v_2^2\omega_4\omega_1^2\omega_2^3 - 20\omega_3c_s^2\omega_4\omega_1^3 + 24c_s^2v_2^2\omega_4\omega_1^3\omega_2 - 168\omega_3v_2^4\omega_4\omega_1^2\omega_2^3 + 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 108\omega_3c_s^2v_2^2\omega_1^2\omega_2^3 - 8c_s^2\omega_4\omega_1\omega_2^3 - 36\omega_3c_s^2\omega_1\omega_2^3 + 96\omega_3v_2^4\omega_4\omega_1^3 + 9\omega_3c_s^4\omega_1^3\omega_2^3 + 108\omega_3c_s^2v_2^2\omega_1\omega_2^3 - 24\omega_3v_2^4\omega_4\omega_1\omega_2^2 - 288\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2 - 54\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 153\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2^3 + 24c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 17\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 8\omega_3\omega_4\omega_1^2\omega_2 - 96\omega_3v_2^2\omega_4\omega_1^2\omega_2 + 144\omega_3c_s^2v_2^2\omega_4\omega_1^3 - 8c_s^2\omega_4\omega_1^3\omega_2 + 18c_s^2\omega_4\omega_1^2\omega_2^3 + 36\omega_3c_s^2\omega_1^2\omega_2^3 - 90\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 32\omega_3c_s^2\omega_4\omega_1\omega_2^2 + 408\omega_3v_2^4\omega_4\omega_1\omega_2^3 - \omega_3v_1^4\omega_4\omega_1^3\omega_2^3 - 20c_s^2\omega_4\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1^2\omega_2 + 7\omega_3\omega_4\omega_1^3\omega_2 + 4\omega_3\omega_4\omega_1^3 - 81\omega_3v_2^4\omega_4\omega_1^3\omega_2^2 - 3\omega_3c_s^4\omega_4\omega_1^3\omega_2^3 - 9c_s^2\omega_4\omega_1^3\omega_2^3 - 9\omega_3c_s^2\omega_1^3\omega_2^3 - 10\omega_3\omega_4\omega_1^3\omega_2 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 + 81\omega_3v_2^4\omega_4\omega_1^2\omega_2^3 + 138\omega_3v_2^4\omega_4\omega_1^3\omega_2 - 7\omega_3\omega_4\omega_1^2\omega_2^3 + 120\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2 - 36\omega_3c_s^4\omega_1^2\omega_2^3 + \omega_3v_4\omega_4\omega_1^3\omega_2^2 - 8\omega_3\omega_4\omega_2^3 - 4\omega_3\omega_4\omega_1^2\omega_2^2 - 32\omega_3c_s^4\omega_4\omega_1^3\omega_2 + 84\omega_3v_2^4\omega_4\omega_1^2\omega_2^2 - 29\omega_3c_s^4\omega_4\omega_1^3\omega_2^3 + 18c_s^4\omega_4\omega_1^3\omega_2^2 + 8c_s^4\omega_4\omega_1\omega_2^3 + 153\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 - 312\omega_3c_s^2v_2^2\omega_4\omega_2^3) \frac{\rho}{36\omega_3\omega_4\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_y^4 \rho}^{(1)} \text{ at } \frac{\partial^4 g}{\partial x_2^4}:$$

$$C_{D_y^4 \rho}^{(1), \text{SRT}} = (24c_s^2v_2^2 + 6v_2^4 + 2c_s^4 - c_s^4\omega - 3v_2^4\omega + 3v_2^2\omega - 12c_s^2v_2^2\omega + c_s^2\omega - 2c_s^2 - 6v_2^2) \frac{v_1}{24\omega}$$

$$C_{D_y^4 \rho}^{(1), \text{MRT}1} = (-48v_2^4\omega_{10}^2\omega_{15} - 3v_2^4\omega_{10}^2\omega_5^2\omega_{15} + 48c_s^2\omega_{10}\omega_5\omega_{15}^2 - 72v_2^2\omega_5\omega_{15}^2 - 96v_2^2\omega_{10}\omega_5\omega_{15} + 24c_s^4\omega_5\omega_{15}^2 + 24c_s^2\omega_{10}^2\omega_{15} + 150c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15}^2 - 96v_2^2\omega_{10}\omega_5\omega_{15}^2 + c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 + 288c_s^2v_2^2\omega_5\omega_{15}^2 + 48c_s^4\omega_{10}\omega_5\omega_{15} - 24v_2^2\omega_{10}\omega_5^2\omega_{15} + 432c_s^2v_2^2\omega_{10}\omega_5\omega_{15} + 72v_2^4\omega_5\omega_{15}^2 + 48v_2^2\omega_{10}^2\omega_{15} - 36v_2^2\omega_{10}\omega_5^2\omega_{15}^2 - 48v_2^4\omega_{10}\omega_5\omega_{15} + 12c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 24c_s^4\omega_{10}^2\omega_{15} - 24c_s^2\omega_5\omega_{15}^2 + 14c_s^4\omega_{10}\omega_5^2\omega_{15}^2 - 216c_s^2v_2^2\omega_{10}^2\omega_{15} + 72c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15} - 30v_2^4\omega_{10}^2\omega_5^2\omega_{15} + 3v_2^2\omega_{10}^2\omega_5^2\omega_{15} - 12v_2^2\omega_{10}^2\omega_5 - 48c_s^4\omega_{10}\omega_5\omega_{15} - 144c_s^2v_2^2\omega_{10}\omega_5\omega_{15} - 24c_s^2\omega_{10}^2\omega_{15} + 12c_s^4\omega_{10}^2\omega_5^2 + 96v_2^4\omega_{10}\omega_5\omega_{15} + 48v_2^2\omega_{10}\omega_{15}^2 - 126c_s^2v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 24c_s^2\omega_{10}^2\omega_5 + 96v_2^2\omega_{10}\omega_5\omega_{15}^2 - 36v_2^4\omega_5^2\omega_{15}^2 + 72c_s^2v_2^2\omega_{10}^2\omega_5 - c_s^4\omega_{10}^2\omega_5^2\omega_{15} - 48c_s^2\omega_{10}^2\omega_5\omega_{15} - 24v_2^4\omega_{10}^2\omega_5 + 24v_2^4\omega_{10}\omega_5^2\omega_{15} + 12c_s^2\omega_5^2\omega_{15} - 144c_s^2v_2^2\omega_5^2\omega_{15} + 12v_2^4\omega_{10}^2\omega_5^2 + 36v_2^4\omega_{10}\omega_5^2\omega_{15} + 24c_s^4\omega_{10}\omega_{15}^2 - 12c_s^2v_2^2\omega_{10}^2\omega_5^2\omega_{15} - 12c_s^2\omega_{10}^2\omega_5 - 48v_2^2\omega_{10}\omega_{15}^2 + 48v_2^2\omega_{10}\omega_5\omega_{15} - 12c_s^4\omega_{10}^2\omega_5^2\omega_{15} - 144c_s^2v_2^2\omega_{10}^2\omega_5 - 24c_s^4\omega_{10}^2\omega_{15} - 14c_s^2\omega_{10}\omega_5^2\omega_{15} + 36v_2^2\omega_5^2\omega_{15}^2 + 30v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 216c_s^2v_2^2\omega_{10}\omega_{15}^2 + 24v_2^2\omega_{10}^2\omega_5 - 432c_s^2v_2^2\omega_{10}\omega_5\omega_{15}^2 - 12c_s^4\omega_5^2\omega_{15}^2) \frac{v_1}{24\omega_{10}^2\omega_5^2\omega_{15}^2}$$

$$C_{D_y^4 \rho}^{(1), \text{MRT}2} = C_{D_y^4 \rho}^{(1), \text{MRT}1}$$

$$C_{D_y^4 \rho}^{(1), \text{CLBM}1} = (24c_s^2v_2^2 - 3v_2^4\omega_{10} - c_s^4\omega_{10} + 6v_2^4 + 2c_s^4 + c_s^2\omega_{10} + 3v_2^2\omega_{10} - 12c_s^2v_2^2\omega_{10} - 2c_s^2 - 6v_2^2) \frac{v_1}{24\omega_{10}}$$

$$C_{D_y^4 \rho}^{(1), \text{CLBM}2} = C_{D_y^4 \rho}^{(1), \text{CLBM}1}$$

$$C_{D_y^4 \rho}^{(1), \text{CuLBM1}} = (24c_s^2 v_2^2 + 6v_2^4 + 2c_s^4 + 3v_2^2 \omega_5 - 12c_s^2 v_2^2 \omega_5 + c_s^2 \omega_5 - c_s^4 \omega_5 - 3v_2^4 \omega_5 - 2c_s^2 - 6v_2^2) \frac{v_1}{24\omega_5}$$

$$C_{D_y^4 \rho}^{(1), \text{CuLBM2}} = (9v_2^2 \omega_1 \omega_2 - 3c_s^4 \omega_1 \omega_2 + 12v_2^4 \omega_2 - 36c_s^2 v_2^2 \omega_1 \omega_2 + 4c_s^4 \omega_2 - 9v_2^4 \omega_1 \omega_2 + 2c_s^4 \omega_1 + 3c_s^2 \omega_1 \omega_2 + 6v_2^4 \omega_1 - 4c_s^2 \omega_2 + 48c_s^2 v_2^2 \omega_2 - 12v_2^2 \omega_2 + 24c_s^2 v_2^2 \omega_1 - 6v_2^2 \omega_1 - 2c_s^2 \omega_1) \frac{v_1}{72\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y^4 v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_2^4} :$$

$$C_{D_y^4 v_1}^{(1), \text{SRT}} = (-144c_s^2 v_2^2 - 3c_s^4 \omega^3 - 42v_2^4 \omega^2 - 72v_2^4 \omega^3 + 30c_s^4 \omega^2 + 48c_s^4 - 72c_s^4 \omega + 108v_2^4 \omega + 6c_s^2 v_2^2 \omega^3 - 3v_2^2 \omega^3 - 14c_s^2 \omega^2 - 84c_s^2 v_2^2 \omega^2 + c_s^2 \omega^3 + 42v_2^2 \omega^2 - 108v_2^2 \omega + 216c_s^2 v_2^2 \omega + 36c_s^2 \omega - 24c_s^2 + 72v_2^2) \frac{\rho}{24\omega^3}$$

$$C_{D_y^4 v_1}^{(1), \text{MRT1}} = (24c_s^4 \omega_{15}^2 + 12c_s^2 v_2^2 \omega_5^3 - 24v_2^2 \omega_5 \omega_{15}^2 - 48c_s^4 \omega_5 \omega_{15}^2 - 12v_2^2 \omega_5^3 - 24c_s^2 v_2^2 \omega_5^2 + 156c_s^2 v_2^2 \omega_5 \omega_{15}^2 - 24c_s^2 \omega_5 \omega_{15} + 24v_2^2 \omega_5^2 - 48v_2^4 \omega_5 \omega_{15} + 24v_2^2 \omega_5 \omega_{15}^2 - 24c_s^2 v_2^2 \omega_5 \omega_{15} + 12c_s^2 \omega_5 \omega_{15}^2 + 24c_s^4 \omega_5 \omega_{15} + 48v_2^2 \omega_5 \omega_{15} - 18v_2^4 \omega_5^3 \omega_{15} - 24c_s^4 \omega_5^2 \omega_{15} - 6c_s^2 \omega_5^3 \omega_{15} - 24v_2^4 \omega_5^2 - 72v_2^2 \omega_5^2 \omega_{15} + 6c_s^2 v_2^2 \omega_5^3 \omega_{15} - 96c_s^2 v_2^2 \omega_{15}^2 - 3c_s^4 \omega_5^3 \omega_{15}^2 - 24v_2^4 \omega_5^2 \omega_{15}^2 - 3v_2^2 \omega_5^3 \omega_{15}^2 + 48c_s^2 v_2^2 \omega_5^2 \omega_{15} - 8c_s^2 \omega_5^2 \omega_{15}^2 + 12v_2^4 \omega_5^3 + 18v_2^2 \omega_5^3 \omega_{15} - 72c_s^2 v_2^2 \omega_5^2 \omega_{15}^2 + 24c_s^2 \omega_5^2 \omega_{15} + 6c_s^4 \omega_5^3 \omega_{15} + 72v_2^4 \omega_5^2 \omega_{15} + c_s^2 \omega_5^2 \omega_{15}^2 + 24v_2^2 \omega_5^2 \omega_{15} - 12c_s^2 v_2^2 \omega_5^3 \omega_{15} + 3v_2^4 \omega_5^3 \omega_{15}^2 + 24c_s^4 \omega_5^2 \omega_{15}^2) \frac{\rho}{24\omega_5^2 \omega_{15}^2}$$

$$C_{D_y^4 v_1}^{(1), \text{MRT2}} = C_{D_y^4 v_1}^{(1), \text{MRT1}}$$

$$C_{D_y^4 v_1}^{(1), \text{CLBM1}} = (24c_s^4 \omega_{15}^2 + 108c_s^2 v_2^2 \omega_5^3 - 48c_s^4 \omega_5 \omega_{15}^2 - 36v_2^2 \omega_5^3 - 216c_s^2 v_2^2 \omega_5^2 - 36c_s^2 v_2^2 \omega_5 \omega_{15}^2 - 24c_s^2 \omega_5 \omega_{15} + 72v_2^2 \omega_5^2 + 72c_s^2 v_2^2 \omega_5 \omega_{15} + 12c_s^2 \omega_5 \omega_{15}^2 + 24c_s^4 \omega_5 \omega_{15} - 30v_2^4 \omega_5^3 \omega_{15} - 24c_s^4 \omega_5^2 \omega_{15} - 6c_s^2 \omega_5^3 \omega_{15} - 72v_2^4 \omega_5^2 - 72v_2^2 \omega_5^2 \omega_{15} + 6c_s^2 v_2^2 \omega_5^3 \omega_{15} - 3c_s^4 \omega_5^3 \omega_{15}^2 - 12v_2^4 \omega_5^2 \omega_{15}^2 - 3v_2^2 \omega_5^3 \omega_{15}^2 + 144c_s^2 v_2^2 \omega_5^2 \omega_{15} - 8c_s^2 \omega_5^2 \omega_{15}^2 + 36v_2^4 \omega_5^3 + 30v_2^2 \omega_5^3 \omega_{15} - 12c_s^2 v_2^2 \omega_5^2 \omega_{15} + 24c_s^2 \omega_5^2 \omega_{15} + 6c_s^4 \omega_5^3 \omega_{15} + 72v_2^4 \omega_5^2 \omega_{15} + c_s^2 \omega_5^3 \omega_{15}^2 + 12v_2^2 \omega_5^2 \omega_{15}^2 - 72c_s^2 v_2^2 \omega_5^3 \omega_{15} + 3v_2^4 \omega_5^3 \omega_{15}^2 + 24c_s^4 \omega_5^2 \omega_{15}^2) \frac{\rho}{24\omega_5^2 \omega_{15}^2}$$

$$C_{D_y^4 v_1}^{(1), \text{CLBM2}} = C_{D_y^4 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_y^4 v_1}^{(1), \text{CuLBM1}} = (-12v_2^4 \omega_7^2 \omega_1^2 - 72v_2^4 \omega_1^2 - 8c_s^2 \omega_7^2 \omega_1^2 - 36c_s^2 v_2^2 \omega_7 \omega_1 + 36v_2^4 \omega_1^3 - 48c_s^4 \omega_7 \omega_1 + 3v_2^4 \omega_7^2 \omega_1^3 + c_s^2 \omega_7^2 \omega_1^3 + 12v_2^2 \omega_7^2 \omega_1^2 + 6c_s^2 v_2^2 \omega_7^2 \omega_1^3 + 24c_s^2 \omega_7^2 \omega_1 + 12c_s^2 v_2^2 \omega_7^2 \omega_1^2 - 3v_2^2 \omega_7^2 \omega_1^3 - 3c_s^4 \omega_7^2 \omega_1^3 + 24c_s^4 \omega_7^2 - 24c_s^2 \omega_7 \omega_1 - 36v_2^2 \omega_1^3 + 30v_2^2 \omega_7 \omega_1^3 + 144c_s^2 v_2^2 \omega_7 \omega_1^3 + 108c_s^2 v_2^2 \omega_1^3 + 6c_s^4 \omega_7 \omega_1^3 - 72c_s^2 v_2^2 \omega_7 \omega_1^3 - 72v_2^2 \omega_7 \omega_1^2 + 72v_2^2 \omega_1^2 - 24c_s^4 \omega_7 \omega_1^2 - 216c_s^2 v_2^2 \omega_1^2 + 24c_s^4 \omega_7 \omega_1 - 30v_2^4 \omega_7 \omega_1^3 - 6c_s^2 \omega_7 \omega_1^3 + 72v_2^4 \omega_7 \omega_1^2 + 24c_s^2 \omega_7 \omega_1^2 + 72c_s^2 v_2^2 \omega_7 \omega_1) \frac{\rho}{24\omega_7^2 \omega_1^3}$$

$$C_{D_y^4 v_1}^{(1), \text{CuLBM2}} = (3\omega_3^2 v_2^4 \omega_4^3 \omega_1^3 - 48\omega_3^2 c_s^4 \omega_4^2 \omega_1 - 36\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1 + \omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 36\omega_3 v_2^2 \omega_4 \omega_1^2 + 36\omega_3 c_s^2 v_2^2 \omega_4 \omega_1 - 12\omega_3^2 v_2^4 \omega_4^2 \omega_1^2 - 18\omega_3 v_2^2 \omega_4 \omega_1^3 - 8\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 - 3\omega_3^2 v_2^2 \omega_4^2 \omega_1^3 + 12\omega_3^2 c_s^2 \omega_4^2 \omega_1 + 6\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1^3 - 36\omega_3 v_2^4 \omega_4 \omega_1^2 - 3\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 + 72\omega_3 c_s^2 v_2^2 \omega_4^2 \omega_1^2 + 9\omega_3^2 v_2^4 \omega_1^3 - 54\omega_3^2 c_s^2 v_2^2 \omega_1^2 - 12\omega_3^2 c_s^2 v_2^2 \omega_1^2 + 12\omega_3^2 v_2^2 \omega_1^2 + 24\omega_3^2 c_s^4 \omega_4^2 + 27\omega_3^2 c_s^2 v_2^2 \omega_1^3 - 18\omega_3^2 v_2^4 \omega_1^2 - 36\omega_3 c_s^2 v_2^2 \omega_4^2 \omega_1^3 + 24\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 + 18\omega_3 v_2^4 \omega_4 \omega_1^3 + 72\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^2 + 18v_2^2 \omega_4^2 \omega_1^2 - 36\omega_3^2 v_2^2 \omega_4 \omega_1^2 - 3\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 27c_s^2 v_2^2 \omega_1^3 + 12\omega_3 c_s^4 \omega_4^2 \omega_1 + 54\omega_3 c_s^2 v_2^2 \omega_4 \omega_1^3 - 12\omega_3^2 c_s^4 \omega_4 \omega_1^2 - 15\omega_3 v_2^4 \omega_4 \omega_1^3 + 12\omega_3 c_s^2 \omega_4^2 \omega_1^2 + 15\omega_3^2 v_2^2 \omega_4 \omega_1^3 - 54c_s^2 v_2^2 \omega_4^2 \omega_1^2 - 9v_2^2 \omega_4^2 \omega_1^3 - 36\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^3 - 12\omega_3^2 c_s^2 \omega_4 \omega_1 + 36\omega_3 v_2^4 \omega_4 \omega_1^2 + 3\omega_3^2 c_s^4 \omega_4 \omega_1^3 - 108\omega_3 c_s^2 v_2^2 \omega_4 \omega_1^2 + 3\omega_3 c_s^4 \omega_4^2 \omega_1^3 + 36\omega_3^2 v_2^4 \omega_4 \omega_1^2 - 18v_2^4 \omega_4^2 \omega_1^2 - 12\omega_3 c_s^2 \omega_4^2 \omega_1 + 18\omega_3^2 v_2^2 \omega_1^2 + 15\omega_3 v_2^2 \omega_4^2 \omega_1^3 + 12\omega_3^2 c_s^2 \omega_4 \omega_1^2 + 9v_2^4 \omega_4^2 \omega_1^3 - 15\omega_3^2 v_2^4 \omega_4 \omega_1^3 - 12\omega_3 c_s^4 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^4 \omega_4 \omega_1 - 3\omega_3^2 c_s^2 \omega_4 \omega_1^3 - 36\omega_3 v_2^2 \omega_4^2 \omega_1^2 + 36\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1 - 9\omega_3^2 v_2^2 \omega_1^3) \frac{\rho}{24\omega_3^2 \omega_4^2 \omega_1^3}$$

$$\text{coefficient } C_{D_y^4 v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^2} :$$

$$C_{D_y^4 v_2}^{(1), \text{SRT}} = (-4 + 2\omega - 5v_2^2 \omega - 3c_s^2 \omega + 6c_s^2 + 10v_2^2) \frac{v_2 v_1 \rho}{12\omega}$$

$$C_{D_y^4 v_2}^{(1), \text{MRT1}} = (36\omega_{10}^2 \omega_{15} + 2\omega_{10}^2 \omega_5^2 \omega_{15} - 120c_s^2 \omega_{10} \omega_5 \omega_{15}^2 + 120v_2^2 \omega_5 \omega_{15} + 168v_2^2 \omega_{10} \omega_5 \omega_{15} - 60c_s^2 \omega_{10} \omega_{15} - 3c_s^2 \omega_{10}^2 \omega_5^2 \omega_{15} + 72\omega_{10} \omega_5 \omega_{15}^2 + 36v_2^2 \omega_{10} \omega_5^2 \omega_{15} - 48\omega_5 \omega_{15} - 84v_2^2 \omega_{10}^2 \omega_{15} + 61v_2^2 \omega_{10} \omega_5^2 \omega_{15} + 24\omega_{10} \omega_5 \omega_{15} - 33c_s^2 \omega_{10}^2 \omega_5^2 \omega_{15} + 72c_s^2 \omega_5 \omega_{15}^2 - 24c_s^2 \omega_{10} \omega_5 \omega_{15} + 21\omega_{10}^2 \omega_5^2 \omega_{15} - 5v_2^2 \omega_{10}^2 \omega_5^2 \omega_{15} + 24v_2^2 \omega_{10}^2 \omega_5 + 60c_s^2 \omega_{10} \omega_{15}^2 - 72\omega_{10}^2 \omega_5 \omega_{15} + 12c_s^2 \omega_{10} \omega_5^2 \omega_{15} - 36\omega_{10} \omega_{15}^2 - 48c_s^2 \omega_{10}^2 \omega_5 - 168v_2^2 \omega_{10} \omega_5 \omega_{15}^2 + 24\omega_5^2 \omega_{15}^2 + 24\omega_{10}^2 \omega_5 + 120c_s^2 \omega_{10}^2 \omega_5 \omega_{15} - 12\omega_{10} \omega_5^2 \omega_{15} - 36c_s^2 \omega_5^2 \omega_{15} - 25\omega_{10} \omega_5^2 \omega_{15} - 12\omega_{10}^2 \omega_5^2 + 24c_s^2 \omega_{10}^2 \omega_5^2 + 84v_2^2 \omega_{10} \omega_{15}^2 - 72v_2^2 \omega_{10} \omega_5 \omega_{15} + 39c_s^2 \omega_{10} \omega_5^2 \omega_{15} - 60v_2^2 \omega_5^2 \omega_{15} - 51v_2^2 \omega_{10}^2 \omega_5^2 \omega_{15} - 48v_2^2 \omega_{10}^2 \omega_5) \frac{v_2 v_1 \rho}{12\omega_{10}^2 \omega_5^2 \omega_{15}^2}$$

$$C_{D_y^4 v_2}^{(1), \text{MRT2}} = C_{D_y^4 v_2}^{(1), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(1), \text{CLBM1}} = (-4 + 2\omega_{10} - 3c_s^2 \omega_{10} - 5v_2^2 \omega_{10} + 6c_s^2 + 10v_2^2) \frac{v_2 v_1 \rho}{12\omega_{10}}$$

$$C_{D_y^4 v_2}^{(1), \text{CLBM2}} = C_{D_y^4 v_2}^{(1), \text{CLBM1}}$$

$$C_{D_y^4 v_2}^{(1), \text{CuLBM1}} = (-4 - 5v_2^2\omega_5 - 3c_s^2\omega_5 + 2\omega_5 + 6c_s^2 + 10v_2^2) \frac{v_2 v_1 \rho}{12\omega_5}$$

$$C_{D_y^4 v_2}^{(1), \text{CuLBM2}} = (-15v_2^2\omega_1\omega_2 + 6\omega_1\omega_2 - 9c_s^2\omega_1\omega_2 - 4\omega_1 + 12c_s^2\omega_2 + 20v_2^2\omega_2 - 8\omega_2 + 10v_2^2\omega_1 + 6c_s^2\omega_1) \frac{v_2 v_1 \rho}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^3 D_z \rho}^{(1)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{MRT1}} = (13\omega_6^2 v_1^2 \omega_{13} \omega_9^3 + 8v_1^2 \omega_{13} \omega_9^3 + 84\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9^3 + 120\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9^2 - 20\omega_6 v_1^4 \omega_{13} \omega_9^2 + 4\omega_6^2 c_s^2 \omega_9^2 + 24\omega_6^2 v_1^4 \omega_{13} + 12\omega_6^2 c_s^2 \omega_{13} \omega_9 - 20\omega_6^2 v_1^4 \omega_{13} \omega_9 + 4c_s^4 \omega_{13}^2 \omega_9^2 - 36c_s^2 v_1^2 \omega_{13} \omega_9^3 - 48\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9^2 + 4\omega_6 v_1^2 \omega_9^3 - 20\omega_6 v_1^2 \omega_{13} \omega_9 + 96\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 - 32\omega_6^2 v_1^2 \omega_{13} \omega_9^2 + 4\omega_6^2 c_s^4 \omega_{13}^2 \omega_9^2 - 8\omega_6 c_s^2 \omega_{13} \omega_9^3 - 4\omega_6^2 c_s^2 \omega_9^3 - 51\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9^3 - 13\omega_6^2 v_1^4 \omega_{13} \omega_9^3 + 4\omega_6^2 v_1^4 \omega_9^3 - 8v_1^4 \omega_{13} \omega_9^3 - 4\omega_6 c_s^4 \omega_9^3 + 20\omega_6 v_1^2 \omega_{13}^2 \omega_9^2 - 24\omega_6^2 c_s^2 v_1^2 \omega_9^2 + 20\omega_6^2 v_1^2 \omega_{13} \omega_9 - 12\omega_6^2 c_s^4 \omega_{13}^2 \omega_9 + 20\omega_6 v_1^4 \omega_{13} \omega_9 - 72\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9 - 4c_s^2 \omega_{13}^2 \omega_9^2 - 4\omega_6^2 v_1^4 \omega_9^2 - 8\omega_6^2 c_s^2 \omega_{13}^2 - 4\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 32\omega_6^2 v_1^4 \omega_{13} \omega_9^2 + 24\omega_6^2 c_s^2 v_1^2 \omega_9^3 + 8\omega_6 c_s^4 \omega_{13} \omega_9^3 - 4\omega_6 c_s^2 \omega_{13}^2 \omega_9 - 144\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 \omega_9 + 8v_1^4 \omega_{13}^2 \omega_9^2 - 4\omega_6 v_1^4 \omega_9^3 + 13\omega_6^2 v_1^4 \omega_{13} \omega_9^2 - 8\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 4\omega_6^2 c_s^4 \omega_9^3 - 20\omega_6 v_1^2 \omega_{13} \omega_9^3 + 4\omega_6^2 c_s^2 \omega_{13} \omega_9^3 + 4c_s^2 \omega_{13} \omega_9^3 + 16\omega_6 v_1^2 \omega_{13} \omega_9^2 - 4\omega_6^2 c_s^4 \omega_9^2 - 8\omega_6 c_s^4 \omega_{13} \omega_9^2 + 72\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9 - 4\omega_6^2 c_s^4 \omega_{13} \omega_9 - 24\omega_6^2 v_1^2 \omega_{13}^2 + 36\omega_6^2 v_1^2 \omega_{13} \omega_9 - 8v_1^2 \omega_{13}^2 \omega_9^2 + 4\omega_6^2 v_1^2 \omega_9^2 + 4\omega_6 c_s^4 \omega_{13} \omega_9 - 84\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9^2 + 8\omega_6^2 c_s^4 \omega_{13} \omega_9^2 + 8\omega_6^2 c_s^4 \omega_{13}^2 - 13\omega_6^2 v_1^2 \omega_{13} \omega_9^2 + 20\omega_6 v_1^4 \omega_{13} \omega_9^3 - 4\omega_6^2 c_s^4 \omega_{13} \omega_9^3 + 36c_s^2 v_1^2 \omega_{13} \omega_9^2 - 4\omega_6^2 v_1^2 \omega_9^3 - 4c_s^4 \omega_{13} \omega_9^3 - 24\omega_6 c_s^2 v_1^2 \omega_9^3 + 8\omega_6 c_s^2 \omega_{13} \omega_9^2 - 16\omega_6 v_1^4 \omega_{13} \omega_9^2 + 51\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9^2 + 4\omega_6 c_s^2 \omega_9^3 - 36\omega_6^2 v_1^4 \omega_{13} \omega_9 + 4\omega_6^2 c_s^2 \omega_{13} \omega_9) \frac{v_3}{4\omega_6^2 \omega_{13}^3 \omega_9^3}$$

$$C_{D_x^3 D_z \rho}^{(1), \text{MRT2}} = C_{D_x^3 D_z \rho}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_z \rho}^{(1), \text{CuLBM2}} = (-36\omega_3^2 v_1^4 \omega_1 \omega_2^3 + 56\omega_3^2 c_s^2 \omega_1^3 \omega_2 - 48\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 + 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 48\omega_3^2 v_1^2 \omega_1^3 - 8\omega_3^2 v_3^2 \omega_1 \omega_2^2 - 36\omega_3^2 c_s^4 \omega_2^3 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2 + 4\omega_3^2 \omega_1^3 - 8\omega_3^2 v_3^2 \omega_1 \omega_2^2 - 24\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 - 34\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 72\omega_3^2 v_1^4 \omega_1 \omega_2^2 - 48\omega_3^2 v_3^2 v_1^2 \omega_1^3 \omega_2 - 72\omega_3^2 v_3^2 v_1^2 \omega_2^3 + 6\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 - 12v_3^2 c_s^2 \omega_1^3 \omega_2^2 + 24\omega_3^2 c_s^4 \omega_1 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 60\omega_3^2 v_1^2 \omega_1 \omega_2^3 + 8\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^2 - 84\omega_3^2 c_s^4 \omega_1^3 \omega_2 + 8\omega_3^2 \omega_1 \omega_2^2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1^3 + 108\omega_3^2 c_s^2 v_1^2 \omega_1 \omega_2^3 + 12v_3^2 c_s^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^3 + 40\omega_3^2 c_s^2 \omega_1^2 \omega_2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 - 216\omega_3^2 c_s^2 v_1^2 \omega_1 \omega_2^2 + 8\omega_3^2 \omega_1 \omega_2^3 + 48\omega_3^2 v_1^2 \omega_1 \omega_2^2 + 24\omega_3^2 v_1^2 \omega_2^3 + 22\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^3 + 42\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 5\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 8\omega_3^2 \omega_2^3 + 72\omega_3^2 c_s^4 \omega_1^3 - \omega_2^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 \omega_1^3 \omega_2 + 216\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 + 216\omega_3^2 c_s^2 v_1^2 \omega_1^3 - 20\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2 - 2\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 - 24\omega_3^2 v_1^2 \omega_1^2 \omega_2^2 + 12c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 + 4\omega_3^2 v_3^2 \omega_1^2 \omega_2 + 16\omega_3^2 v_3^2 c_s^2 \omega_1^3 + 4\omega_3^2 c_s^2 \omega_1^3 \omega_2 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 2\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 + 36c_s^4 \omega_1^2 \omega_2^3 + 42\omega_3^2 c_s^4 \omega_1 \omega_2^3 + 84\omega_3^2 v_1^2 \omega_1^3 \omega_2 - 72\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 + 54\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 + 24\omega_3^2 v_1^4 \omega_1^3 - 4\omega_3^2 \omega_1^2 \omega_2^2 - 324\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2 - \omega_3^2 v_3^2 \omega_1^3 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + 20\omega_3^2 c_s^2 \omega_2^3 - 4\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2 - 4\omega_3^2 v_3^2 \omega_1^3 - 18\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 + 4\omega_3^2 v_3^2 \omega_1^3 \omega_2 + \omega_3^2 v_3^2 \omega_1^2 \omega_2^3 + 48\omega_3^2 v_1^4 \omega_2^3 + 18\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2^2 + 72\omega_3^2 v_1^4 \omega_1^2 \omega_2^2 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^2 + 96\omega_3^2 v_3^2 v_1^2 \omega_1 \omega_2^2 - 4\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2 - 36c_s^4 \omega_1^3 \omega_2^2 - 24\omega_3^2 v_1^2 \omega_1^3 \omega_2^2 + 8\omega_3^2 v_3^2 \omega_2^3 - 54\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 72\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2^2 - 4\omega_3^2 \omega_1^2 \omega_2^2 - 52\omega_3^2 c_s^2 \omega_1^3 - 12\omega_3^2 c_s^4 \omega_1^3 \omega_2 - 22\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 36\omega_3^2 v_1^4 \omega_1^3 \omega_2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_1^3 \omega_2^3 - 18\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 + 4\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 + \omega_3^2 \omega_1^3 \omega_2^2 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 + 2\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2^2 - 24\omega_3^2 v_1^2 \omega_1^2 \omega_2 - 20\omega_3^2 v_3^2 c_s^2 \omega_2^3) \frac{v_3}{36\omega_3^2 \omega_1^3 \omega_2^3}$$

$$\text{coefficient } C_{D_x^3 D_z v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x^3 D_z v_1}^{(1), \text{MRT1}} = (-43\omega_6^2 v_1^2 \omega_{13} \omega_9^3 - 28v_1^2 \omega_{13} \omega_9^3 - 40\omega_6^2 \omega_{13} \omega_9^2 - 16\omega_6 c_s^2 \omega_{13} \omega_9^2 - 16\omega_6^2 c_s^2 \omega_9^2 - 72\omega_6^2 c_s^2 \omega_{13} \omega_9 - 16\omega_6 v_1^2 \omega_9^3 + 64\omega_6 v_1^2 \omega_{13} \omega_9 - 32\omega_6^2 \omega_{13}^2 + 104\omega_6^2 v_1^2 \omega_{13} \omega_9^2 + 44\omega_6 c_s^2 \omega_{13} \omega_9^3 + 28\omega_6 \omega_{13} \omega_9^2 + 16\omega_6^2 c_s^2 \omega_9^3 + 17\omega_6^2 \omega_{13} \omega_9^3 - 24\omega_6 \omega_{13} \omega_9 - 68\omega_6 v_1^2 \omega_{13} \omega_9^2 + 8\omega_6^2 \omega_9^2 - 64\omega_6^2 v_1^2 \omega_{13} \omega_9 + 24\omega_6^2 \omega_{13} \omega_9 + 20c_s^2 \omega_{13}^2 \omega_9^2 + 48\omega_6^2 c_s^2 \omega_{13}^2 + 25\omega_6^2 c_s^2 \omega_{13} \omega_9^2 - 12\omega_{13}^2 \omega_9^2 - 8\omega_6^2 \omega_9^3 + 32\omega_6 c_s^2 \omega_{13} \omega_9 + 48\omega_6^2 \omega_{13}^2 \omega_9 + 56\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 8\omega_6 \omega_9^3 + 68\omega_6 v_1^2 \omega_{13} \omega_9^3 - 25\omega_6^2 c_s^2 \omega_{13} \omega_9^3 - 20c_s^2 \omega_{13} \omega_9^3 - 48\omega_6 v_1^2 \omega_{13} \omega_9^2 + 12\omega_{13} \omega_9^3 + 80\omega_6^2 v_1^2 \omega_{13}^2 - 120\omega_6^2 v_1^2 \omega_{13} \omega_9 + 28v_1^2 \omega_{13} \omega_9^2 - 16\omega_6^2 v_1^2 \omega_9^3 + 43\omega_6^2 v_1^2 \omega_{13} \omega_9^2 + 16\omega_6 \omega_{13} \omega_9^2 + 16\omega_6^2 v_1^2 \omega_9^3 - 28\omega_6 \omega_{13} \omega_9^3 - 44\omega_6 c_s^2 \omega_{13} \omega_9^2 - 17\omega_6^2 \omega_{13} \omega_9^2 - 16\omega_6 c_s^2 \omega_9^3 - 32\omega_6^2 c_s^2 \omega_{13} \omega_9) \frac{v_3 v_1 \rho}{4\omega_6^2 \omega_{13}^3 \omega_9^3}$$

$$C_{D_x^3 D_z v_1}^{(1), \text{MRT2}} = C_{D_x^3 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_x^3 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_1}^{(1), \text{CuLBM2}} = (36c_s^2\omega_1\omega_2^3 + 6\omega_3v_3^2\omega_2^2\omega_2 - 6v_3^2\omega_1^2\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 84\omega_3c_s^2\omega_1^3 - 24\omega_3v_3^2\omega_2^3 - 12\omega_1\omega_2^3 + 132\omega_3v_1^2\omega_2^2\omega_2 - 6v_3^2\omega_1^3\omega_2 - 9v_3^2\omega_1^2\omega_2^2 + 5\omega_3v_3^2\omega_1^3\omega_2 - 5\omega_3\omega_1^2\omega_2^2 - 66\omega_3v_1^2\omega_1^3\omega_2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^2 + 9v_3^2\omega_1^3\omega_2^2 - 54\omega_3c_s^2\omega_1\omega_2^2 - 18\omega_3v_3^2\omega_1^3\omega_2 - 5\omega_3v_3^2\omega_1^2\omega_2^2 - 51\omega_3\omega_1^2\omega_2^2 - 12\omega_3v_1^2\omega_1^3\omega_2 - 9\omega_3v_3^2\omega_1^2\omega_2^2 + 12\omega_3v_3^2\omega_1^3 - 12\omega_3c_s^2\omega_2^3 + 27\omega_3c_s^2\omega_1\omega_2^3 + 42\omega_3\omega_1\omega_2^3 - 9\omega_1^3\omega_2^2 + 27c_s^2\omega_2^3\omega_2^2 + 6\omega_3v_3^2\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_2^3 - 15\omega_3c_s^2\omega_1^2\omega_2^3 + 84\omega_3v_1^2\omega_2^3 + 3\omega_3\omega_1\omega_2^3 + 81\omega_3c_s^2\omega_1^2\omega_2^2 + 27\omega_3v_3^2\omega_1\omega_2^3 + 12v_3^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 + 48\omega_3v_1^2\omega_1^3 - 18c_s^2\omega_1^2\omega_2^2 - 66\omega_3v_1^2\omega_1\omega_2^3 + 6\omega_1^2\omega_2^2 - 18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^3 + 15\omega_3c_s^2\omega_1^3\omega_2^2 - 120\omega_3v_1^2\omega_1\omega_2^2 + 9\omega_1^2\omega_2^2 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3) \frac{v_3v_1\rho}{18\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^3 \partial x_3} :$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{SRT}} = (36v_1^2 - c_s^4\omega^3 + 54c_s^2v_1^2\omega + 20c_s^4\omega^2 - 54v_1^2\omega + 36c_s^4 + 26v_1^2\omega^2 - 54c_s^4\omega - 42c_s^2v_1^2\omega^2 - 4v_1^2\omega^3 + 12c_s^2v_1^2\omega^3 + 54v_1^4\omega - 12c_s^2\omega^2 + 4v_1^4\omega^3 - 36v_1^4 + 36c_s^2\omega - 26v_1^4\omega^2 - 24c_s^2 - 36c_s^2v_1^2) \frac{\rho}{12\omega^3}$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{MRT1}} = (12\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 60\omega_6^3v_1^4\omega_{13}\omega_9^2 + 13\omega_6^3c_s^4\omega_{13}\omega_9^3 - 48\omega_6^2v_1^2\omega_{13}\omega_9^3 - \omega_6^3c_s^2\omega_{13}\omega_9^2 - 72\omega_6^3v_1^2\omega_{13}^2 + 12c_s^4\omega_{13}^2\omega_9^3 - 12\omega_6^2c_s^2v_1^2\omega_{13}\omega_9^3 - 12\omega_6^2c_s^2v_1^2\omega_9^3 + 12\omega_6^2c_s^2\omega_{13}\omega_9^3 + 30\omega_6^2c_s^2v_1^2\omega_{13}\omega_9^3 + 12\omega_6^2v_1^4\omega_{13}\omega_9^3 + 48\omega_6^2v_1^4\omega_{13}\omega_9^3 + \omega_6^3c_s^4\omega_{13}\omega_9^2 - 60\omega_6^3v_1^2\omega_{13}\omega_9^2 - 5\omega_6^3c_s^2\omega_{13}\omega_9^3 + 252\omega_6^3c_s^2v_1^2\omega_{13}^2 - 12\omega_6^3v_1^4\omega_9^3 - 12\omega_6^3c_s^4\omega_{13}\omega_9^2 - 12\omega_6^3v_1^2\omega_9^3 - 306\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 27\omega_6^3v_1^2\omega_{13}\omega_9^3 - 6\omega_6^3c_s^2\omega_{13}\omega_9^2 - 24\omega_6^3v_1^4\omega_{13}\omega_9^2 - \omega_6^3c_s^4\omega_{13}\omega_9^3 - 36\omega_6^3v_1^4\omega_{13}\omega_9^2 + 12\omega_6^3v_1^2\omega_9^2 + 12\omega_6^3c_s^2\omega_{13}\omega_9^2 - 12\omega_6^3c_s^2v_1^2\omega_9^3 - 12\omega_6^3v_1^2\omega_{13}\omega_9^3 + 12\omega_6^3c_s^4\omega_{13}\omega_9^3 + 12\omega_6^3c_s^4\omega_{13}^2 - 108\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 + 6\omega_6^3c_s^4\omega_{13}\omega_9^3 + 12\omega_6^3v_1^4\omega_{13}\omega_9^2 - 12\omega_6^3c_s^2\omega_{13}\omega_9^2 - 4\omega_6^3v_1^2\omega_{13}\omega_9^3 - 90\omega_6^3v_1^2\omega_{13}\omega_9^2 - 24\omega_6^3c_s^2\omega_{13}\omega_9^3 + 24\omega_6^3v_1^2\omega_{13}\omega_9^3 + 18\omega_6^3c_s^2\omega_{13}\omega_9^3 - 19\omega_6^3v_1^2\omega_{13}\omega_9^2 - 6\omega_6^3c_s^4\omega_{13}\omega_9^2 - 18\omega_6^3v_1^4\omega_{13}\omega_9^3 + 72\omega_6^3v_1^2\omega_{13}\omega_9^2 - 36\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 - 48c_s^2v_1^2\omega_{13}\omega_9^3 - 48\omega_6^2c_s^2v_1^2\omega_{13}\omega_9^2 + 12\omega_6^3c_s^4\omega_{13}\omega_9^2 + 4\omega_6^3v_1^4\omega_{13}\omega_9^3 + 54\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 - 6\omega_6^3c_s^2\omega_{13}\omega_9^3 - 12\omega_6^3v_1^2\omega_{13}\omega_9^2 - 12\omega_6^3v_1^2\omega_9^2 + 90\omega_6^3v_1^2\omega_{13}\omega_9^2 - 24\omega_6^3v_1^4\omega_{13}\omega_9^3 - 81\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 6\omega_6^3c_s^2\omega_{13}\omega_9^2 - 12\omega_6^3c_s^2\omega_{13}^2 + 6\omega_6^3c_s^2\omega_{13}\omega_9^3 + 18\omega_6^3v_1^2\omega_{13}\omega_9^3 - 18\omega_6^3c_s^4\omega_{13}\omega_9^3 - 21\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 19\omega_6^3v_1^4\omega_{13}\omega_9^2 + 102\omega_6^2c_s^2v_1^2\omega_{13}\omega_9^3 + 12\omega_6^2v_1^2\omega_9^3 + 162\omega_6^2c_s^2v_1^2\omega_{13}\omega_9^2 + 12\omega_6^3v_1^4\omega_9^3) \frac{\rho}{12\omega_6^3\omega_{13}^2\omega_9^3}$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{MRT2}} = C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{MRT1}}$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{CLBM1}} = (12\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 72\omega_6^3v_1^4\omega_{13}\omega_9^2 + 13\omega_6^3c_s^4\omega_{13}\omega_9^3 - 36\omega_6^3v_1^2\omega_{13}\omega_9^3 - \omega_6^3c_s^2\omega_{13}\omega_9^2 - 72\omega_6^3v_1^2\omega_{13}^2 + 12c_s^4\omega_{13}^2\omega_9^3 + 36\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 36\omega_6^3c_s^2v_1^2\omega_9^3 + 108\omega_6^3c_s^2v_1^2\omega_9^3 + 12\omega_6^3c_s^2\omega_{13}\omega_9^3 - 39\omega_6^3v_1^4\omega_{13}\omega_9^3 + 60\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 + 6\omega_6^3c_s^4\omega_{13}\omega_9^2 - 12\omega_6^3c_s^4\omega_{13}\omega_9^3 - 108\omega_6^3c_s^2v_1^2\omega_9^2 + 36\omega_6^3v_1^4\omega_{13}\omega_9^2 - 12\omega_6^3c_s^2\omega_{13}\omega_9^2 + 54\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 36\omega_6^3v_1^4\omega_{13}\omega_9^3 + \omega_6^3c_s^4\omega_{13}\omega_9^2 - 72\omega_6^3v_1^2\omega_{13}\omega_9^2 - 5\omega_6^3c_s^2\omega_{13}\omega_9^3 + 252\omega_6^3c_s^2v_1^2\omega_{13}^2 - 12\omega_6^3v_1^4\omega_9^3 - 12\omega_6^3c_s^4\omega_{13}\omega_9^2 - 12\omega_6^3v_1^2\omega_9^3 - 306\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 39\omega_6^3v_1^2\omega_{13}\omega_9^3 - 6\omega_6^3c_s^2\omega_{13}\omega_9^2 - \omega_6^3c_s^4\omega_{13}\omega_9^3 - 36\omega_6^3v_1^4\omega_{13}\omega_9^2 - 36\omega_6^3v_1^2\omega_{13}\omega_9^3 + 12\omega_6^3c_s^4\omega_{13}\omega_9^3 + 12\omega_6^3c_s^4\omega_{13}^2 - 36\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 + 6\omega_6^3c_s^4\omega_{13}\omega_9^3 - 12\omega_6^3c_s^2\omega_{13}\omega_9^2 - 4\omega_6^3v_1^2\omega_{13}\omega_9^3 - 90\omega_6^3v_1^2\omega_{13}\omega_9^2 - 24\omega_6^3c_s^2\omega_{13}\omega_9^3 + 24\omega_6^3v_1^2\omega_{13}\omega_9^3 + 18\omega_6^3c_s^2\omega_{13}\omega_9^3 - 19\omega_6^3v_1^2\omega_{13}\omega_9^2 - 6\omega_6^3c_s^4\omega_{13}\omega_9^2 - 6\omega_6^3v_1^4\omega_{13}\omega_9^3 + 72\omega_6^3v_1^2\omega_{13}^2 - 108\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 + 12\omega_6^3c_s^4\omega_{13}\omega_9^2 + 4\omega_6^3v_1^4\omega_{13}\omega_9^3 + 198\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 - 6\omega_6^3c_s^2\omega_{13}\omega_9^3 - 36\omega_6^3v_1^4\omega_9^2 + 90\omega_6^3v_1^2\omega_{13}\omega_9^2 - 3\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 6\omega_6^3c_s^2\omega_{13}\omega_9^3 - 12\omega_6^3c_s^2\omega_{13}^2 + 6\omega_6^3c_s^2\omega_{13}\omega_9^2 + 6\omega_6^3v_1^2\omega_{13}\omega_9^3 - 18\omega_6^3c_s^2\omega_{13}\omega_9^3 - 99\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 19\omega_6^3v_1^4\omega_{13}\omega_9^2 - 18\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^3 + 36\omega_6^3v_1^2\omega_9^3 + 18\omega_6^3c_s^2v_1^2\omega_{13}\omega_9^2 + 36\omega_6^3v_1^4\omega_9^3) \frac{\rho}{12\omega_6^3\omega_{13}^2\omega_9^3}$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{CLBM2}} = C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{CLBM1}}$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{CuLBM1}} = (-24c_s^4\omega_1^3\omega_2^2\omega_{12}^2 - 36v_1^4\omega_4^3\omega_{12}^2 + 54c_s^2v_1^3\omega_1^2\omega_2^2\omega_{12} + 90v_1^2\omega_4\omega_2^3\omega_{12}^2 + c_s^4\omega_4^2\omega_2^3\omega_{12}^2 - 36c_s^2v_1^2\omega_4\omega_2^2\omega_{12}^2 + 39v_1^2\omega_4^3\omega_2^2\omega_{12} + 12c_s^2\omega_4\omega_2^2\omega_{12}^2 + 18c_s^2\omega_4^2\omega_{12}^2\omega_{12} - 108c_s^2v_1^2\omega_1^2\omega_2^2 + 12c_s^4\omega_2^2\omega_{12}^2\omega_{12} - 108c_s^2v_1^2\omega_4\omega_2^3\omega_{12} + 6v_1^4\omega_4^3\omega_{12}^2 + 36v_1^4\omega_4^3\omega_2^2 + 12c_s^2v_1^2\omega_4^3\omega_{12}^2 + 72v_1^4\omega_2^2\omega_{12}^2\omega_{12} - 12c_s^2\omega_2^2\omega_{12}^2 + 36v_1^2\omega_2^2\omega_{12}^3 + 36v_1^2\omega_1^2\omega_2^2 + 19v_1^2\omega_4^2\omega_2^3\omega_{12} - 6c_s^2\omega_1^2\omega_2^2\omega_{12} + 108c_s^2v_1^2\omega_4^3\omega_{12}^2 + 12c_s^2\omega_4\omega_2^3\omega_{12}^2 + 6c_s^4\omega_4^2\omega_2^3\omega_{12}^2 - 36v_1^2\omega_4^2\omega_{12}^2\omega_{12} - 306c_s^2v_1^2\omega_4\omega_2^3\omega_{12} - 99c_s^2v_1^2\omega_4^3\omega_{12}^2 - 108c_s^2v_1^2\omega_4^2\omega_{12}^2 - 5c_s^2\omega_4^2\omega_{12}^2\omega_{12} - 36v_1^2\omega_4^3\omega_{12}^2 + 12c_s^4\omega_2^3\omega_{12}^2 + 12c_s^4\omega_4^3\omega_2\omega_{12} - 36v_1^4\omega_2^2\omega_{12}^2 + 36v_1^2\omega_4\omega_2^2\omega_{12} - 3c_s^2v_1^2\omega_1^2\omega_2^2\omega_{12} - 6c_s^4\omega_4^2\omega_{12}^2\omega_{12} - 4v_1^4\omega_4^2\omega_{12}^2\omega_{12} - c_s^2\omega_1^2\omega_2^2\omega_{12} - 39v_1^4\omega_2^2\omega_{12}^2 + 6c_s^2\omega_4^3\omega_2\omega_{12}^2 - 90v_1^4\omega_2^2\omega_{12}^2\omega_{12} - 18c_s^2v_1^2\omega_4^3\omega_2\omega_{12}^2 - 72v_1^2\omega_2^2\omega_{12}^2\omega_{12} - 18c_s^4\omega_4^3\omega_2\omega_{12} + 60c_s^2v_1^2\omega_1^2\omega_2^2\omega_{12} - 12c_s^4\omega_4\omega_2^2\omega_{12}^2 - 12c_s^2\omega_4\omega_2^2\omega_{12} - 6v_1^4\omega_4^3\omega_2^2\omega_{12} + 36c_s^2v_1^2\omega_4^2\omega_2\omega_{12} - 72v_1^2\omega_4^2\omega_2^2\omega_{12} + 252c_s^2v_1^2\omega_2^2\omega_{12}^2 - c_s^4\omega_4^3\omega_2^2\omega_{12} + 18c_s^2v_1^2\omega_4^2\omega_2^2\omega_{12} - 12c_s^4\omega_4\omega_2^2\omega_{12}^2 + 12c_s^4\omega_4^3\omega_{12}^2 - 19v_1^2\omega_2^2\omega_{12}^2\omega_{12} + 6c_s^4\omega_4^3\omega_2\omega_{12} + 72v_1^4\omega_2^2\omega_{12}^2 - 6c_s^2\omega_4^2\omega_2^2\omega_{12}^2 + 36v_1^4\omega_4^2\omega_2^2\omega_{12} + 36c_s^2v_1^2\omega_1^2\omega_2\omega_{12} + 13c_s^4\omega_4^3\omega_2^2\omega_{12} + 198c_s^2v_1^2\omega_1^2\omega_2^2\omega_{12} + 6c_s^2\omega_4^2\omega_2^2\omega_{12} + 4v_1^4\omega_4^3\omega_2^2\omega_{12} - 12c_s^2\omega_4^3\omega_2\omega_{12} - 36v_1^4\omega_4\omega_2^3\omega_{12}) \frac{\rho}{12\omega_4^3\omega_2^3\omega_{12}^2}$$

$$C_{\text{D}_3^2 \text{D}_z \text{v}_3}^{(1), \text{CuLBM2}} = (336\omega_3^2c_s^2v_1^2\omega_4^2\omega_1\omega_2^2 - 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 144\omega_3^2v_3^2v_1^2\omega_4^2\omega_1\omega_2^2 + 648\omega_3^2c_s^2v_1^2\omega_4\omega_2^2\omega_2^3 - 96\omega_3v_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 40\omega_3c_s^4\omega_4^2\omega_2^2\omega_2^2 + 24\omega_3^2v_1^4\omega_4^3\omega_1^3\omega_2^3 + 24\omega_3v_1^2\omega_4^2\omega_1\omega_2^3 + 96\omega_3^2v_1^4\omega_4^2\omega_1^2\omega_2^3 + 6\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + 162c_s^2v_1^2\omega_4^2\omega_1^3\omega_2^3 - 144\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^3 + 24\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 - 40\omega_3^2c_s^2\omega_4^2\omega_1^3 - 288\omega_3^2v_1^2\omega_4\omega_1^2\omega_2^3 - 108\omega_3c_s^2v_1^2\omega_4\omega_1^3\omega_2^2 + 108\omega_3v_1^4\omega_4^2\omega_1^3\omega_2^2 + 86\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 72v_1^2\omega_4^2\omega_1^2\omega_2^3 - 28\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2 + 38\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2 + 180\omega_3v_1^2\omega_4\omega_1^2\omega_2^3 + 576\omega_3^2v_3^2v_1^2\omega_4^2\omega_1\omega_2^3 - 36\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^2 - 108\omega_3^2c_s^2v_1^2\omega_4\omega_1^2\omega_2^2 - 852\omega_3^2c_s^2v_1^2\omega_4^2\omega_1\omega_2^3 + 16\omega_3c_s^4\omega_4^2\omega_1^3\omega_2 + 72\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 20\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 80\omega_3^2c_s^4\omega_4^2\omega_2^3 + 324\omega_3c_s^2v_1^2\omega_4\omega_1^3\omega_2^3 + 36\omega_3^2v_1^2\omega_4\omega_1^2\omega_2^2 + 144\omega_3^2v_3^2v_1^2\omega_4^2\omega_1^3 - 117\omega_3v_3^4\omega_4^2\omega_1^3\omega_2^3 + 24\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 + 96\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^3 - 108c_s^2v_1^2\omega_4^2\omega_1^3\omega_2^2 - 54v_1^4\omega_4^2\omega_1^3\omega_2^3 - 6\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 - 56\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 - 16\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 216c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^3 + 72\omega_3c_s^2v_1^2\omega_4\omega_1\omega_2^3 - 60\omega_3v_1^4\omega_4^2\omega_1^2\omega_2^3 + 48\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^2 + 24\omega_3^2v_3^2\omega_4^2\omega_2^2\omega_2 + 117\omega_3^2v_1^2\omega_4\omega_1^3\omega_2^3 + 36\omega_3^2v_1^2\omega_4\omega_1^3\omega_2^2 + 32\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1\omega_2^3 + 40\omega_3^2v_1^4\omega_4^2\omega_1^2\omega_2^3 - 108\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2 - 32\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 432\omega_3^2v_3^2v_1^2\omega_4^2\omega_2^3 - 36\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^2 - 297\omega_3^2c_s^2v_1^2\omega_4\omega_1^3\omega_2^3 + 72\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 + 216\omega_3v_1^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2v_1^2\omega_4\omega_1^3\omega_2^2 - 540\omega_3c_s^2v_1^2\omega_4\omega_1^2\omega_2^3 - 12\omega_3^2v_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 24\omega_3v_1^4\omega_4^2\omega_1^3\omega_2 - 6\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^2 - 2\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 36v_1^2\omega_4^2\omega_1^3\omega_2^2 + 108\omega_3^2c_s^2v_1^2\omega_4\omega_1^3\omega_2^2 + 18\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 8\omega_3^2c_s^4\omega_4^2\omega_2^3 + 48\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 72\omega_3^2v_1^4\omega_4\omega_1\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1\omega_2^3 - 108\omega_3v_1^2\omega_4\omega_1^3\omega_2^3 - 144\omega_3^2v_1^4\omega_4^2\omega_1^2\omega_2^3 - 12\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - 108\omega_3c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^3 - 24\omega_3^2v_1^2\omega_4^2\omega_1^3\omega_2^3 + 12\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 144\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^3 - 24\omega_3v_1^4\omega_4^2\omega_1\omega_2^3 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 8\omega_3^2\omega_4^2\omega_1^3 + 144\omega_3^2v_3^2v_1^2\omega_4^2\omega_1\omega_2 + 72\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^3\omega_2^3 - 72v_1^4\omega_4^2\omega_1^3\omega_2^3 + 192\omega_3^2v_1^4\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 264\omega_3^2c_s^2v_1^2\omega_4^2\omega_1\omega_2 + 36\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - 72\omega_3v_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 96\omega_3^2v_1^4\omega_4\omega_1\omega_2^2 - 2\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3v_1^2\omega_4^2\omega_1^3\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2 + 288\omega_3^2v_1^4\omega_4\omega_1^2\omega_2^3 + 24\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3 + 36\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 108\omega_3^2v_1^2\omega_4^2\omega_1^3\omega_2^3 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 + 24\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 - 72\omega_3c_s^2v_1^2\omega_4^2\omega_1^3\omega_2 - 324\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^3 - 180\omega_3v_1^4\omega_4\omega_1^2\omega_2^3 - 86\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2^2 + 468\omega_3c_s^2v_1^2\omega_4^2\omega_1^3\omega_2^3 - 96\omega_3^2v_1^2\omega_4^2\omega_1^3 + 117\omega_3v_1^2\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3^2v_1^4\omega_4\omega_1^2\omega_2^2 + 48\omega_3^2v_3^2\omega_4^2\omega_2^3 - 288\omega_3^2v_1^4\omega_4^2\omega_1\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2^2 + 144\omega_3^2v_3^2v_1^2\omega_4^2\omega_1^3\omega_2^2 +$$

$$C_{D^2 D_y D_z v_1}^{(1), \text{MRT1}} =$$

$$C_{D_x D_y^2 D_z \rho}^{(1), \text{MRT2}} = C_{D_x D_y^2 D_z \rho}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 D_z \rho}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 D_z \rho}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 D_z \rho}^{(1), \text{CuLBM2}} = (48\omega_3^2 v_2^4 \omega_4^2 \omega_1^3 - 27\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 - 56\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 84v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 192\omega_3 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 - 108\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 54c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 + 864\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2^2 + 120\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2^2 + 27\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2 - 104\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 - 192\omega_3^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2^2 - 30\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 162\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 - 168\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2 - 96\omega_3^2 v_2^2 \omega_4^2 \omega_2^3 - 432\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2 + 24c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 60\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_1^3 \omega_2 + 432\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_2^3 + 324\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 24\omega_3 c_s^4 \omega_4^2 \omega_1^3 \omega_2 + 96\omega_3^2 v_2^2 \omega_4^2 \omega_1^3 \omega_2 + 192\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 + 144\omega_3^2 c_s^4 \omega_4^2 \omega_2^3 - 16\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 324\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 72\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2 + 56\omega_3 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 96\omega_3^2 v_2^2 \omega_4^2 \omega_1^3 - 108\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + 432\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1^3 - 56\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^2 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 + 144\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 + 84c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 128\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^2 - 36\omega_3^2 v_2^2 \omega_4^2 \omega_1 \omega_2^3 + 54v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 + 54\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 108\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 + 24\omega_3^2 v_2^2 \omega_4^2 \omega_2^3 + 96\omega_3^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2 + 30\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 - 81\omega_3 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - 24v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 104\omega_3^2 c_s^2 \omega_4^2 \omega_2^3 + 64\omega_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 432\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 - 24\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2 - 40\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2 + 162c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - 10\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 108\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 64\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 81\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^3 + 72\omega_3^2 v_2^2 \omega_4^2 \omega_1^2 \omega_2^2 + 10\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 + 112\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 - 8\omega_3^2 \omega_4^2 \omega_1^3 \omega_2 + 32\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 - 108\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2 + 32\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 72\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_2^3 - 72c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_2^3 + 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 36\omega_3^2 v_2^2 \omega_4^2 \omega_1^3 \omega_2 - 27\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 - 176\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 432\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1 \omega_2^2 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2 - 60\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_1 \omega_2^2 - 168\omega_3 c_s^4 \omega_4^2 \omega_1 \omega_2^3 + 48\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_1^3 + 64\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 80\omega_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^2 - 216\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_2^2 + 96\omega_3^2 v_2^2 \omega_4^2 \omega_1 \omega_2^3 - 324\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2^3 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 - 54\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 252c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 - 8\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 - 72\omega_3^2 v_2^2 \omega_4^2 \omega_1 \omega_2^2 + 108\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 10\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 8\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 - 96\omega_3^2 v_3^2 v_2^2 \omega_4^2 \omega_1 \omega_2^2 - 432\omega_3^2 c_s^2 v_2^2 \omega_4^2 \omega_1 \omega_2^2 + 10\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 8\omega_3^2 \omega_4^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1 \omega_2^3 + 32\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_2^3 + 27\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 + 96\omega_3^2 v_2^2 \omega_4^2 \omega_1 \omega_2^2 - 24\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_2^3) \frac{v_3}{72\omega_3^2 \omega_4^2 \omega_1^3 \omega_2^3}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{MRT1}} = (12\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 2\omega_6^2 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12} + 4\omega_6^2 \omega_{13} \omega_7 \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 4\omega_6 \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 4\omega_6 \omega_7 \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 + 4\omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 + 2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 8\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 - 2\omega_6^2 \omega_{13} \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 - 10\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 - 2\omega_6 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 8\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 8\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 - 4\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 2\omega_6^2 \omega_{13} \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 - 8\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 8\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 8\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 5\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 + 5\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 8\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12}^2 - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9 \omega_{12}^2) \frac{v_3 c_s^2 v_1 \rho}{2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_9^2 \omega_{12}^2}$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{MRT2}} = C_{D_x D_y^2 D_z v_1}^{(1), \text{MRT1}}$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 D_z v_1}^{(1), \text{CuLBM2}} = (9\omega_4 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 c_s^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 2\omega_3 v_3^2 \omega_4 \omega_2 - 9v_3^2 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1 + 9\omega_3 v_3^2 \omega_1 \omega_2 + 2\omega_3 v_3^2 \omega_4 \omega_1 - 9\omega_3 \omega_1 \omega_2) \frac{v_3 v_1 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_y^2 D_z v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2 \partial x_3} :$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_2}^{(1), \text{MRT1}} = (\omega_6^2 \omega_8^2 \omega_3^3 \omega_{15} + 2\omega_6 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} - 4\omega_6^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} + 2\omega_6^2 \omega_8^2 \omega_5^2 \omega_{15}^2 - 2\omega_6 \omega_8 \omega_3^3 \omega_{15}^2 - \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - \omega_6 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} -$$

$$C_{D_x D_y^2 D_z v_3}^{(1), \text{MRT2}} = C_{D_x D_y^2 D_z v_3}^{(1), \text{MRT1}}$$

$$\begin{aligned} C_{\text{D}_{3\text{D},\rho}}^{(1),\text{MRT1}} = & (4\omega_{10}^2\omega_{17}\omega_{8\omega_5}^2\omega_{15}^2 + 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_{7\omega_{17}}\omega_{17}^2\omega_{15}^2 + 4\omega_{16}\omega_{10}^2\omega_{7\omega_{17}}\omega_{17}\omega_{8\omega_5}\omega_{15} - 2\omega_6\omega_{10}\omega_{7\omega_{17}}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 12\omega_6c_s^2\omega_{10}^2\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + \\ & 24\omega_6c_s^2\omega_{10}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 12\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_{7\omega_5}\omega_{15}^2 - 6\omega_6c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - \\ & 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6v_{12}^2\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 6\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_{7\omega_{17}}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + \\ & 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 6c_s^2\omega_{16}\omega_{10}^2\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - \\ & 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_{16}^2\omega_{10}^2\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 6\omega_6c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_6\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - \\ & 24\omega_6c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 2\omega_{16}\omega_{10}^2\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_{16}\omega_{10}^2\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 12c_s^2\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 24\omega_6c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + \\ & 2\omega_{16}\omega_{10}^2\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 6\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 12\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + \\ & 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - 4\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 8\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 + 6c_s^2\omega_{16}\omega_{10}^2\omega_{17}\omega_{17}\omega_{8\omega_5}\omega_{15}^2 - \end{aligned}$$

$$\begin{aligned}
& 8\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 3\omega_6\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 - 4\omega_6v_2^2\omega_{10}^2\omega_{17}\omega_8\omega_5\omega_{15}^2 - 12c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_5^2\omega_{15}^2 + 8\omega_6\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 - \\
& 12\omega_6c_s^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 - 8\omega_6\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 - 6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_{15} - \\
& 4\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_{15} + 4\omega_6\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_5\omega_{15}^2 - 4\omega_6\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_5\omega_{15}^2 + 2\omega_{16}\omega_{10}^2\omega_7\omega_8\omega_5^2\omega_{15}^2 + 2\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} - \\
& 2\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 4\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_5^2\omega_{15}^2 - 12c_s^2\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6v_2^2\omega_{10}^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 4\omega_6\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 + \\
& 3\omega_6\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 12c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 - 3\omega_6\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 4\omega_{16}\omega_{10}\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 6\omega_6c_s^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + \\
& 6c_s^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 4\omega_6\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_5^2\omega_{15}^2 - 4\omega_6\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 9\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 2\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_8\omega_5^2\omega_{15}^2 + \\
& 4\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 + 2\omega_6v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 12c_s^2\omega_{10}\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 12\omega_6c_s^2\omega_{16}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 + 2v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + \\
& 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15}^2 + 4\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_5^2\omega_{15}^2 - 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_8\omega_5\omega_{15}^2 - 6\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} - 4\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + \\
& 4\omega_6\omega_{10}^2\omega_{17}\omega_8\omega_5\omega_{15}^2 - 2\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_8\omega_5^2\omega_{15} + 2\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_8\omega_5^2\omega_{15} - 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_8\omega_5^2\omega_{15} - 2\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + \\
& 2\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} - 3\omega_6v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 4\omega_6\omega_{16}v_2^2\omega_{10}\omega_{17}\omega_8\omega_5\omega_{15}^2 + 12\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_7\omega_8\omega_5\omega_{15} - 4\omega_6\omega_{16}\omega_{10}\omega_{17}\omega_8\omega_5\omega_{15}^2 - \\
& 2\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_8\omega_5^2\omega_{15} + 2\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_8\omega_5^2\omega_{15} - 4\omega_6\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 + 4\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5 + 12c_s^2\omega_{16}\omega_{10}\omega_{17}\omega_8\omega_5^2\omega_{15} + \\
& 4\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_5\omega_{15}^2 - 2\omega_6\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 2\omega_6\omega_{16}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} - 2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} - 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_5\omega_{15}^2 - \\
& 2\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15} + 4\omega_6\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15}^2 - 4\omega_{16}\omega_{10}^2\omega_7\omega_5^2\omega_{15}^2 - 12\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15} - 9\omega_6c_s^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - \\
& 12\omega_6c_s^2\omega_{10}\omega_{17}\omega_8\omega_5\omega_{15}^2 - 4\omega_{16}v_2^2\omega_{10}\omega_7\omega_{17}\omega_5^2\omega_{15}^2 - 12\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_7\omega_5^2\omega_{15}^2 + 2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2) \frac{v_3v_2v_1}{4\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5^2\omega_{15}^2}
\end{aligned}$$

$$C_{D_y^3 D_z \rho}^{(1), \text{MRT}2} = C_{D_y^3 D_z \rho}^{(1), \text{MRT}1}$$

$$C_{D_y^3 D_z \rho}^{(1), \text{CLBM}1} = 0$$

$$C_{D_y^3 D_z \rho}^{(1), \text{CLBM}2} = 0$$

$$C_{D_y^3 D_z \rho}^{(1), \text{CuLBM}1} = 0$$

$$C_{D_y^3 D_z \rho}^{(1), \text{CuLBM}2} = (-\omega_1 + v_3\omega_1 - 3c_s^2\omega_2 + \omega_2 + 3c_s^2\omega_1 - v_3\omega_2) \frac{v_3v_2v_1}{12\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^3 D_z v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z v_1}^{(1), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_y^3 D_z v_1}^{(1), \text{MRT}1} = & (6\omega_6^2c_s^2\omega_{17}\omega_8\omega_5\omega_{15}^2 + \omega_6v_2^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}^2 - \omega_6^2c_s^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} - 2\omega_6^2c_s^2\omega_8^2\omega_5^2\omega_{15}^2 + 2\omega_6v_2^2\omega_8\omega_5^3\omega_{15}^2 + 4\omega_6^2v_2^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} - \\
& 2c_s^2\omega_{17}\omega_8^2\omega_{15}^2\omega_{15}^2 + \omega_6^2\omega_8^3\omega_{15}^3\omega_{15} + 2\omega_6\omega_{17}\omega_8^2\omega_5^2\omega_{15} - \omega_6^2c_s^2\omega_8^3\omega_{15}^3\omega_{15} - 4\omega_6^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6v_2^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} - 5\omega_6^2c_s^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}^2 + 2\omega_6^2\omega_8^2\omega_5^2\omega_{15}^2 - \\
& 2\omega_6c_s^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} - 2\omega_6\omega_8\omega_5^3\omega_{15}^2 - 2\omega_6^2v_2^2\omega_8\omega_5^3\omega_{15}^2 - \omega_6\omega_{17}\omega_8^2\omega_5^3\omega_{15} - 2\omega_6^2\omega_8^2\omega_5^2\omega_{15}^2 - \omega_6^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} + 7\omega_6c_s^2\omega_{17}\omega_8^2\omega_5^2\omega_{15}^2 - \omega_6^2v_2^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} - \\
& 2\omega_6^2c_s^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6^2c_s^2\omega_8^3\omega_{15}^3\omega_{15} + 4\omega_6^2c_s^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6c_s^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} - \omega_6^2v_2^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} - \omega_6c_s^2\omega_8^2\omega_5^3\omega_{15}^2 + \\
& 2\omega_6^2v_2^2\omega_8\omega_5^2\omega_{15}^2 + 2\omega_6^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} - \omega_6\omega_{17}\omega_8^2\omega_5^2\omega_{15} - \omega_6^2\omega_8^3\omega_{15}^3\omega_{15} - 2\omega_6v_2^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + \omega_6^2\omega_{17}\omega_8^2\omega_5^3\omega_{15} + \omega_6^2\omega_8^2\omega_5^2\omega_{15}^2 - \\
& \omega_6^2v_2^2\omega_8^3\omega_{15}^3\omega_{15} + \omega_6^2v_2^2\omega_{17}\omega_8^2\omega_5^2\omega_{15} + 4\omega_6c_s^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 + 2c_s^2\omega_{17}\omega_8\omega_5^3\omega_{15}^2 - \omega_6v_2^2\omega_{17}\omega_8\omega_5^3\omega_{15}^2 + \omega_6^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 2\omega_6^2c_s^2\omega_8\omega_5^3\omega_{15}^2 + \\
& 2\omega_6^2\omega_8\omega_5^3\omega_{15}^2 + 2\omega_6^2c_s^2\omega_{17}\omega_8^2\omega_{15}^2 + 2\omega_6c_s^2\omega_8\omega_5^3\omega_{15}^2 - 2\omega_6^2v_2^2\omega_8^2\omega_5^2\omega_{15}^2 - 6\omega_6c_s^2\omega_{17}\omega_8\omega_5\omega_{15}^2 - \omega_6^2v_2^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - \omega_6^2\omega_{17}\omega_8\omega_5\omega_{15}^2 + \\
& 5\omega_6^2c_s^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 2\omega_6^2c_s^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6^2c_s^2\omega_8\omega_5^2\omega_{15}^2 - \omega_6v_2^2\omega_8^2\omega_5^3\omega_{15}^2 - \omega_6^2\omega_{17}\omega_8\omega_5^3\omega_{15}^2 + 13\omega_6^2c_s^2\omega_{17}\omega_8\omega_5\omega_{15}^2 + 2\omega_6^2\omega_{17}\omega_8\omega_5\omega_{15} + \\
& 2\omega_6c_s^2\omega_{17}\omega_8^3\omega_{15}^2 + \omega_6^2v_2^2\omega_{17}\omega_8^2\omega_{15}^2 + 2\omega_6^2v_2^2\omega_8^2\omega_{15}^2\omega_{15} - 7\omega_6c_s^2\omega_{17}\omega_8\omega_5^3\omega_{15}^2 - 11\omega_6^2c_s^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2 - 8\omega_6^2c_s^2\omega_{17}\omega_8\omega_5^2\omega_{15} + \omega_6^2v_2^2\omega_8^2\omega_5^3\omega_{15}^2 + \\
& \omega_6^2v_2^2\omega_{17}\omega_8\omega_5^3\omega_{15}^2 - 2\omega_6^2v_2^2\omega_{17}\omega_8^2\omega_{15}^2 + \omega_6\omega_8^3\omega_5^3\omega_{15}^2 - 2\omega_6^2v_2^2\omega_{17}\omega_8\omega_5\omega_{15} - 2\omega_6^2\omega_8\omega_5^2\omega_{15}^2 + \omega_6\omega_{17}\omega_8\omega_5^3\omega_{15}^2 - 2\omega_6^2c_s^2\omega_{17}\omega_8\omega_5^2\omega_{15}^2) \frac{v_3v_2\rho}{2\omega_6^2\omega_{17}\omega_8^3\omega_5^3\omega_{15}^2}
\end{aligned}$$

$$C_{D_y^3 D_z v_1}^{(1), \text{MRT}2} = C_{D_y^3 D_z v_1}^{(1), \text{MRT}1}$$

$$C_{D_y^3 D_z v_1}^{(1), \text{CLBM}1} = 0$$

$$C_{D_y^3 D_z v_1}^{(1), \text{CLBM}2} = 0$$

$$C_{D_y^3 D_z v_1}^{(1), \text{CuLBM}1} = 0$$

$$\begin{aligned}
C_{D_y^3 D_z v_1}^{(1), \text{CuLBM}2} = & (2\omega_3\omega_4^2\omega_1 + 18\omega_3c_s^2\omega_4^2 - 2\omega_3v_3^2\omega_4^2\omega_1 - 2\omega_3^2\omega_4\omega_1 - 18\omega_3c_s^2\omega_4\omega_1 + 12\omega_4^2 + 12\omega_3v_2^2\omega_4 + 6\omega_3v_3^2\omega_4^2 - 6\omega_3v_2^2\omega_4\omega_1 + 3v_3^2\omega_4^2\omega_1 + \\
& 2\omega_3^2v_3^2\omega_4\omega_1 + 36\omega_3c_s^2\omega_4 + 6\omega_3^2\omega_4 - 6v_2^2\omega_4^2 + 6\omega_3^2v_3^2 - 12\omega_3\omega_4 + 3\omega_3^2v_2^2\omega_1 + 18c_s^2\omega_4^2\omega_1 + 6\omega_3^2c_s^2\omega_4\omega_1 - 6\omega_3^2v_2^2 - 36c_s^2\omega_4^2 - 18\omega_3^2c_s^2\omega_4 - \\
& 6\omega_4^2\omega_1 - 6\omega_3c_s^2\omega_4^2\omega_1 - 6v_3^2\omega_4^2 - 6\omega_3^2v_3^2\omega_4 - 3\omega_3^2v_3^2\omega_1 + 6\omega_3\omega_4\omega_1 - 6\omega_3\omega_4^2 + 3v_2^2\omega_4^2\omega_1) \frac{v_3v_2\rho}{8\omega_3^2\omega_4^2\omega_1}
\end{aligned}$$

$$\text{coefficient } C_{D_y^3 D_z v_2}^{(1)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^3 \partial x_3} :$$

$$C_{D_y^3 D_z v_2}^{(1), \text{SRT}} = 0$$

$$C_{D_2^2 D_2^2 \mathcal{P}}^{(1), CLMB1} = (12\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9 + \omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9^3 + 54\omega_6\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^3 + 18\omega_6^2c_s^2\omega_{13}\omega_{18}\omega_9^3 + 12\omega_6^2\omega_{22}\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 - 12\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9 - 12\omega_6\omega_{13}\omega_9^3 + 6\omega_6^2\omega_{13}\omega_{18}\omega_9^2 - 18\omega_6^2c_s^2\omega_{13}\omega_{18}\omega_9 - 2\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9^2 - 40\omega_6\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 - 6\omega_6^2\omega_{13}\omega_{18}\omega_9^3 - 36\omega_6c_s^2\omega_{13}\omega_{18}\omega_9^3 + 12\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9^3 - 12\omega_6^2\omega_{22}\omega_{18}\omega_9^3 + 12\omega_6\omega_{22}\omega_{13}\omega_{18}\omega_9 + 6\omega_6^2v_1^2\omega_{13}\omega_{18}\omega_9^3 - 18\omega_6c_s^2\omega_{13}\omega_9^3 + 12\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{18} + 18\omega_6\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9^2 + 5\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^3 + 36\omega_6^2\omega_{22}c_s^2\omega_{18}\omega_9^3 - 12\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9 - 36\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^2 - 12\omega_6\omega_{22}v_1^2\omega_{13}\omega_9^2 + 6\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9^3 - 12\omega_6\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9^3 - 36\omega_6\omega_{22}c_s^2\omega_{18}\omega_9^3 - 6\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^2 - 12\omega_6\omega_{13}\omega_{18}\omega_9^3 - 18\omega_6\omega_{22}\omega_{13}\omega_{18}\omega_9^3 + 6\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_9^2 - 6\omega_6^2v_1^2\omega_{13}\omega_{18}\omega_9^2 + 36\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^3 - 12\omega_6v_1^2\omega_{13}\omega_{18}\omega_9^3 - 18\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9^2 + 12\omega_6v_1^2\omega_{13}\omega_9^2 - 36\omega_6^2\omega_{22}c_s^2\omega_{18}\omega_9^3 - 18\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^3 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{18} - 12\omega_6\omega_{22}\omega_{13}\omega_{18}\omega_9^2 - 12\omega_6^2v_1^2\omega_{13}\omega_{18}\omega_9^3 -$$

$$C_{D_x^2 D_z^2 v_1}^{(1), \text{MRT2}} = C_{D_x^2 D_z^2 v_1}^{(1), \text{MRT1}}$$

$$C_{D_2^2 D_2^2 v_1}^{(1), CLMB1} = (-24\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9 + 36\omega_6^3\omega_{22}v_1^2\omega_{18}\omega_9^2 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{18} - 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18} - 18\omega_6^3v_1^2\omega_{13}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}c_s^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{18}\omega_9 - 12\omega_6^2\omega_{13}\omega_9^2 + 24\omega_6^2\omega_{22}\omega_{18}\omega_9^2 - 36\omega_6^3v_1^2\omega_{18}\omega_9^2 - \omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^2 - 18\omega_6^3\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9 + 18\omega_6^3\omega_{22}v_1^2\omega_{13}\omega_9 + 36\omega_6^2v_1^2\omega_{13}\omega_9^2 + 12\omega_6^2\omega_{22}\omega_{13}\omega_9 + 12\omega_6\omega_{22}\omega_{13}\omega_{18}\omega_9 + 6\omega_6^2c_s^2\omega_{13}\omega_{18}\omega_9^2 - 6\omega_6^2c_s^2\omega_{13}\omega_{18}\omega_9 - 12\omega_6^2\omega_{18}\omega_9^2 - 18\omega_6^3v_1^2\omega_{13}\omega_9^2 + 12\omega_6\omega_{22}c_s^2\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_9 - 6\omega_6^2\omega_{22}\omega_{13}\omega_9 - 12\omega_6^2\omega_{22}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{18} + 36\omega_6^3v_1^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 - 36\omega_6^3\omega_{22}v_1^2\omega_{18}\omega_9 + 18\omega_6^3\omega_{22}v_1^2\omega_{13}\omega_{18} + 36\omega_6^2v_1^2\omega_{18}\omega_9 + 18\omega_6^2v_1^2\omega_{13}\omega_{18}\omega_9^2 - 12\omega_6^2\omega_{22}\omega_{18}\omega_9^2 - 24\omega_6^2\omega_{22}c_s^2\omega_{18}\omega_9^2 - 12\omega_6^3\omega_{18}\omega_9 + 6\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_9 + 12\omega_6\omega_{22}\omega_{18}\omega_9 - 12\omega_6^2c_s^2\omega_{13}\omega_{18}\omega_9^2 + 72\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9 - 36\omega_6^2v_1^2\omega_{13}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_9^2 + 6\omega_6^3\omega_{13}\omega_9^2 + 36\omega_6^2\omega_{22}v_1^2\omega_{18}\omega_9 - 4\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{18} - 12\omega_6^2c_s^2\omega_{18}\omega_9^2 - 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 - 6\omega_6^3\omega_{13}\omega_{18}\omega_9^2 + 12\omega_6^2c_s^2\omega_{18}\omega_9 + 18\omega_6\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{13}\omega_{18}\omega_9 + 12\omega_6^2\omega_{13}\omega_{18}\omega_9^2 + 6\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{18} - 12\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{18} - 72\omega_6^2\omega_{22}v_1^2\omega_{18}\omega_9^2 + 6\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9 + 12\omega_6^2c_s^2\omega_{18}\omega_9^2 + 24\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 - 6\omega_6^3c_s^2\omega_{13}\omega_9^2 - 12\omega_6^2c_s^2\omega_{13}\omega_{18}\omega_9^2 + 36\omega_6\omega_{22}v_1^2\omega_{18}\omega_9^2 - 36\omega_6\omega_{22}v_1^2\omega_{13}\omega_{18}\omega_9 + 12\omega_6^3\omega_{18}\omega_9^2 - 36\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_9) \frac{c_s^2 \rho}{12\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9^2}$$

$$C_{D_x^2 D_z^2 v_1}^{(1), \text{CLBM2}} = C_{D_x^2 D_z^2 v_1}^{(1), \text{CLBM1}}$$

$$C_{D_2^+ D_2^+ v_1}^{(1), \text{CuLBM1}} = (12\omega_2^2\omega_{12} + 36v_1^2\omega_2^3 - 72v_1^2\omega_4^2\omega_2^2 - 12c_s^2\omega_2^2\omega_{12} + 36v_1^2\omega_4\omega_2^2\omega_{12} + 36v_1^2\omega_4^2\omega_2^3 - 12\omega_2^3 - 24\omega_4\omega_2^2 - 12\omega_4\omega_2^2\omega_{12} + 18c_s^2\omega_4^2\omega_2\omega_{12} + 24c_s^2\omega_4\omega_2^3 + 24\omega_4\omega_2^3 + 12c_s^2\omega_4\omega_2^2\omega_{12} + 36v_1^2\omega_4\omega_2^2 - 24c_s^2\omega_4\omega_2^3 - 12c_s^2\omega_4\omega_2\omega_{12} - 12\omega_4^2\omega_2^3 + 12c_s^2\omega_4^2\omega_2^3 - 12c_s^2\omega_4^2\omega_{12} - 4c_s^2\omega_4^2\omega_2^2\omega_{12} + 24\omega_4^2\omega_2^2 + 12\omega_4\omega_2\omega_{12} - 36v_1^2\omega_2^2\omega_{12} - 24c_s^2\omega_4^2\omega_2^2 - 36v_1^2\omega_4\omega_2\omega_{12} + 12c_s^2\omega_2^3 + 12c_s^2\omega_4^2\omega_2^2 - 72v_1^2\omega_4\omega_2^3 - 12\omega_4^2\omega_2 - c_s^2\omega_4^2\omega_2^3\omega_{12} + 72v_1^2\omega_4\omega_2^2) \frac{c_s^2\rho}{12\omega_2^3\omega_{12}}$$

$$\begin{aligned}
C(1), \text{CuLB2M2} &= (8\omega_3 c_4^4 \omega_4 \omega_1 \omega_2^3 + 32\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2 + 54\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^3 \omega_2 - 6\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^2 \omega_2^3 - 90\omega_3^2 v_3^2 v_1^2 \omega_4 \omega_1^3 \omega_2 + \\
D_2^2 D_2^2 \omega_1^2 \omega_2^3 &= 72\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 4\omega_3^2 \omega_4 \omega_1^2 \omega_2^2 + 12\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2 - 6\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^3 - 48\omega_3^2 v_3^4 \omega_4 \omega_2^3 + 4\omega_3^2 \omega_4 \omega_2^3 + 12\omega_3^2 v_1^2 \omega_4 \omega_1^3 \omega_2 + 36\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2^2 + \\
\omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 &- 90\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^3 \omega_2^2 + 36\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^2 - 12\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2 + 18\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 + 18\omega_3^2 v_3^4 \omega_1^2 \omega_2^3 + 36\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 - 18v_3^4 \omega_4 \omega_1^2 \omega_2^3 - \\
108\omega_3^2 v_3^2 c_s^4 \omega_4 \omega_2^3 &- 28\omega_3^2 c_s^4 \omega_4 \omega_1 \omega_2^2 + 9\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2^2 - 18\omega_3^2 v_3^4 \omega_1^3 \omega_2^2 + 18\omega_3^2 v_3^2 \omega_1^3 \omega_2^2 - 36\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2 - 2\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + 66\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 - \\
90\omega_3^2 c_s^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 &+ 180\omega_3^2 v_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 12\omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 + 76\omega_3^2 c_s^4 \omega_4 \omega_1 \omega_2^3 - 48\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2 - 18\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 - 96\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^3 \omega_2^2 + \\
54\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 &- 24\omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 24\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 + 30\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 56\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 72\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 6\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 - \\
30\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 &+ 12\omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 174\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2 + 216\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2^3 + 132\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 36\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2 - 4\omega_3^2 \omega_4 \omega_1^3 \omega_2^3 + \\
12\omega_3^2 v_3^4 \omega_4 \omega_2^3 &- 9\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^3 - 12\omega_3^2 v_1^2 \omega_4 \omega_1^3 \omega_2 - 48\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2 + 90\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 + 18\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2 - 18\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 - 36\omega_3^2 v_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 + \\
12\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 &+ 2\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 - 18\omega_3^2 v_3^2 \omega_1^3 \omega_2^3 - 12\omega_3^2 v_3^2 \omega_4 \omega_1^3 \omega_2 - \omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 126\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 36\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 + \\
18\omega_3^2 v_3^4 \omega_1^2 \omega_2^3 &+ 24\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^3 \omega_2 - 8\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2 + 18\omega_3^2 \omega_4 \omega_1^3 \omega_2^2 + 54\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2^3 - 18\omega_3^2 v_3^4 \omega_1^3 \omega_2^2 + 36\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + 6\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^3 \omega_2^2 - \\
36\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 &+ 4\omega_3^2 \omega_4 \omega_1^3 \omega_2 + 24\omega_3^2 v_3^2 \omega_1^3 \omega_2^3 + 132\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2 + 8\omega_3^2 \omega_4 \omega_1^2 \omega_2^2 - 18\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 - 12\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^2 + 6\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^2 + \\
18\omega_3^2 v_3^4 \omega_1^2 \omega_2^3 &+ 60\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 28\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2 - 8\omega_3^2 c_s^4 \omega_4 \omega_1 \omega_2^3 - 54\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 - 3\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2^3 - 36\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2^2 + 32\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^2 + \\
28\omega_3^2 c_s^2 \omega_4 \omega_2^3 &+ 18v_3^4 \omega_4 \omega_1^2 \omega_2^3 - 36\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 + 12\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^3 - 4\omega_3^2 \omega_4 \omega_1 \omega_2^2 - \omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 - 54\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 + 2\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2^2 + \\
72\omega_3^2 c_s^2 \omega_1 \omega_2^3 &- 216\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^3 - 9\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 - 18\omega_3^2 v_3^4 \omega_1^2 \omega_2^3 + 150\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 - 18\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 + 54\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^3 - 4\omega_3^2 \omega_4 \omega_1 \omega_2^3 + \\
16\omega_3^2 c_s^4 \omega_4 \omega_1^3 &- 18\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 + 108\omega_3^2 v_3^2 v_1^2 \omega_4 \omega_2^3 - 54\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 + 18\omega_3^2 c_s^4 \omega_4 \omega_2^3 + 54\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 - 6\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^2 + 18\omega_3^2 v_3^4 \omega_1^2 \omega_2^3 - \\
54\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 &- 144\omega_3^2 v_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 18\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 + 56\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2^2 + 54\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 - 84\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 68\omega_3^2 c_s^4 \omega_4 \omega_2^3 - \\
14\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2 &- 14\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2^3 + 66\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2 + 72\omega_3^2 v_3^4 v_1^2 \omega_4 \omega_2^3 + 9\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^3 + 12\omega_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 + 48\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 18v_3^4 \omega_4 \omega_1^3 \omega_2^2 - \\
72\omega_3^2 c_s^2 \omega_1 \omega_2^3 &+ 8\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2 - 90\omega_3^2 v_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 36\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2^3 + \omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^$$

coefficient $C_{D_x^2 D_z^2 v_3}^{(1)}$ at $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2}$:

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{SRT}} = 0$$

[illegible]

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{MRT2}} = C_{D_x^2 D_z^2 v_3}^{(1), \text{MRT1}}$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z^2 v_3}^{(1), \text{CuLBM1}} = 0$$

$$\begin{aligned} \mathcal{C}_2^{(1), \text{CuLBM2}} = & (-18c_s^2\omega_1\omega_3^2 + 6\omega_3v_2^2\omega_1\omega_2 + 6\omega_3v_3^2\omega_2 + 84\omega_3c_s^2\omega_3^3 - 114\omega_3v_2^2\omega_3^3 + 6\omega_1\omega_3^3 + 18\omega_3v_1^2\omega_1^2\omega_2^2 + 50\omega_3v_2^2\omega_1^3\omega_2^2 - 23\omega_3\omega_3^3\omega_2^2 - 9\omega_3v_2^2\omega_3^3\omega_2 - 6v_1^2\omega_3^3\omega_2 + 48\omega_3v_1^2\omega_2^2 + 23\omega_3v_1^2\omega_1^2 - 75\omega_3v_3^2\omega_1\omega_2 - 50\omega_3v_2^2\omega_1^2\omega_3^2 + 12\omega_3\omega_1^2\omega_2^2 - 12\omega_3v_1^2\omega_1^2\omega_2 + 12v_1^2\omega_1^2\omega_2^2 - 66\omega_3v_2^2\omega_1^2\omega_2^2 + 48\omega_3v_2^2\omega_3^3\omega_1^2 - 66\omega_3c_s^2\omega_3^3\omega_1^2 + 108\omega_3c_s^2\omega_1\omega_2^3 - 12\omega_3\omega_1\omega_2^2 + 60\omega_3v_3^2\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^2\omega_2 + 42\omega_3\omega_2^3 - 42\omega_3c_s^2\omega_1^2\omega_3^2 - 6v_1^2\omega_1\omega_3^2 + 12\omega_3v_1^2\omega_2^2 - 60\omega_3\omega_1\omega_2^2 + 141\omega_3v_2^2\omega_1\omega_2^2 - 18\omega_3c_s^2\omega_1^2\omega_2 + 12\omega_3v_1^2\omega_1^3 + 36c_s^2\omega_1^2\omega_2^2 - 9\omega_3v_1^2\omega_1\omega_2^3 - 12\omega_1^2\omega_2^2 - 18c_s^2\omega_1^3\omega_2 + 42\omega_3c_s^2\omega_1^2\omega_2^2 - 12\omega_3v_1^2\omega_1\omega_2^2 + 6\omega_1^3\omega_2 - 36\omega_3\omega_3^3) \frac{v_3v_1\rho}{18\omega_3v_1^2\omega_2^3} \end{aligned}$$

coefficient $C_{D_x D_y D_z^2 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_1 \partial x_2 \partial x_3^2}$:

$$\begin{aligned} \mathcal{D}_{\mathbf{C}_x \mathbf{D}_y \mathbf{D}_2^2 \rho}^{(1), \text{SRT}} = & (-36v_3^2 v_2 v_1^2 \omega - 14v_3^2 c_s^2 v_1 \omega^2 + 24c_s^2 v_2 v_1^2 + v_3^2 c_s^2 v_1 \omega^3 + 36v_3^2 v_2^2 v_1 \omega - v_3^2 v_2 v_1^2 \omega^3 - 14v_3^2 v_2^2 v_1 \omega^2 - 24v_3^2 c_s^2 v_1 + v_3^2 v_2^2 v_1 \omega^3 + \\ & 14v_3^2 v_2 v_1^2 \omega^2 + 36v_3^2 c_s^2 v_1 \omega - 24v_3^2 v_2^2 v_1 - 36c_s^2 v_2 v_1^2 \omega - 36v_3^2 c_s^2 v_2 \omega + 24v_3^2 c_s^2 v_2 - 24c_s^2 v_2^2 v_1 + 36c_s^2 v_2^2 v_1 \omega - v_3^2 c_s^2 v_2 \omega^3 - c_s^2 v_2 v_1^2 \omega^3 - \\ & 14c_s^2 v_2^2 v_1 \omega^2 + c_s^2 v_2^2 v_1 \omega^3 + 14c_s^2 v_2 v_1^2 \omega^2 + 14v_3^2 c_s^2 v_2 \omega^2 + 24v_3^2 v_2 v_1^2) \frac{1}{2\omega^3} \end{aligned}$$

[illegible]

$$C_{D_x D_y D_z^2 \rho}^{(1), \text{MRT}2} = C_{D_x D_y D_z^2 \rho}^{(1), \text{MRT}1}$$
$$C_{D_x D_y D_z^2 \rho}^{(1), \text{CLBM1}} =$$
$$(2v_3^2 c_s^2 v_2 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 v_2^2 v_1 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 v_2^2 v_1 \omega_{20} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - \omega_6 v_3^2 c_s^2 v_2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 v_2^2 v_1 \omega_{13} \omega_{20} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} + 2\omega_6 \omega_{22} v_3^2 v_2^2 v_1 \omega_{13} \omega_{20} \omega_8 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 c_s^2 v_2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} + \omega_6 \omega_{22} c_s^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - \omega_6 v_3^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 c_s^2 v_2 \omega_{13} \omega_{20} \omega_8 \omega_{18} \omega_9 \omega_{12} + 2\omega_6 \omega_{22} v_3^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{14} \omega_5 \omega_{18} \omega_9 \omega_{12} - \omega_6 \omega_{22} c_s^2 v_2 v_1 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} c_s^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_8 \omega_{18} \omega_9 \omega_{12} - \omega_6 \omega_{22} c_s^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} + 2\omega_6 \omega_{22} v_3^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 v_2 v_1^2 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} + 2\omega_6 \omega_{22} v_3^2 v_2 v_1 \omega_{13} \omega_{20} \omega_{14} \omega_5 \omega_{18} \omega_9 \omega_{12} - \omega_6 \omega_{22} v_3^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - 2\omega_6 \omega_{22} v_3^2 v_2^2 v_1 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} + 2\omega_6 \omega_{22} v_3^2 c_s^2 v_2 \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} - \omega_6 \omega_{22} v_3^2 v_2 v_1^2 \omega_{13} \omega_{20} \omega_{14} \omega_8 \omega_5 \omega_{18} \omega_9 \omega_{12} -$$

[illegible]

315

[illegible]

$$C_{D_2 D_2 v_2}^{(1), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_2 v_1 \rho}{36 \omega_1 \omega_2}$$

$$C_{D_2^2 D_3^2 v_3}^{(1), \text{SRT}} = (-14v_2^2 v_1^2 \omega^2 - 24c_s^2 v_2^2 + 36c_s^2 v_1^2 \omega + v_2^2 v_1^2 \omega^3 - 14c_s^2 v_1^2 \omega^2 + 36v_2^2 v_1^2 \omega + c_s^2 v_1^2 \omega^3 + 28v_3 c_s^2 v_1 \omega^2 + c_s^2 v_2^2 \omega^3 + 48v_3 c_s^2 v_1 - 72v_3 v_2^2 v_1 \omega - 2v_3 c_s^2 v_1 \omega^3 - 14c_s^2 v_2^2 \omega^2 + 48v_3 v_2^2 v_1 + 28v_3 v_2^2 v_1 \omega^2 + 36c_s^2 v_2^2 \omega - 24v_2^2 v_1^2 - 24c_s^2 v_1^2 - 72v_3 c_s^2 v_1 \omega - 2v_3 v_2^2 v_1 \omega^3) \frac{\rho}{4\omega^3}$$

[illegible]

$$C_{D_y^2 D_z^2 v_3}^{(1), \text{MRT2}} = C_{D_y^2 D_z^2 v_3}^{(1), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 v_3}^{(1), \text{CLBM1}} = (4\omega_6 v_2^2 v_1^2 \omega_{20} \omega_8 \omega_{18} \omega_{15} + 4\omega_6 c_s^2 v_1^2 \omega_{20} \omega_5 \omega_{18} \omega_{15} - 4\omega_6 v_3 c_s^2 v_1 \omega_{17} \omega_8 \omega_{18} \omega_{15} - 4\omega_6 c_s^2 v_2^2 \omega_{20} \omega_{17} \omega_5 \omega_{18} \omega_{15} -$$

$$\begin{aligned}
& 6\omega_6^3\omega_{22}v_3^2c_s^2\omega_{13}\omega_{11}^2\omega_9 + 12\omega_6^3v_1^2\omega_{11}^2\omega_{18}^2\omega_9 + 12\omega_6^2\omega_{22}v_3^2v_1^2\omega_{13}\omega_{18}^2\omega_9 + 12\omega_6^3\omega_{22}v_3^2v_1^2\omega_{13}\omega_{11}^2\omega_{18} - 96\omega_{22}c_s^4\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 - 36\omega_6^3c_s^2v_1^2\omega_{11}^2\omega_{18}^2\omega_9 - \\
& 12\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 + 36\omega_6^2c_s^4\omega_{11}^2\omega_{18}^2\omega_9 + 36\omega_6^3\omega_{22}c_s^2v_1^2\omega_{13}\omega_{11}^2\omega_{18} + 12\omega_6^2\omega_{22}c_s^2\omega_{11}^2\omega_{18}^2\omega_9 + 12\omega_6^2\omega_{22}v_3^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 - \\
& 12\omega_6^3v_3^2v_1^2\omega_{11}^2\omega_{18}^2\omega_9 - \omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 - 12\omega_6^2v_3^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 - 6\omega_6^3\omega_{22}v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 + 36\omega_6^2\omega_{22}v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 + \\
& 18\omega_6^3\omega_{22}c_s^4\omega_{13}\omega_{11}^2\omega_{18}^2 - 12\omega_6^3\omega_{22}v_3^2c_s^2\omega_{11}^2\omega_{18}^2 - 12\omega_6^2\omega_{22}v_3^2v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 + 36\omega_6^3\omega_{22}c_s^4\omega_{11}^2\omega_{18}^2\omega_9 - 36\omega_6^2\omega_{22}c_s^2v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 + \\
& 6\omega_6^3v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2 - 18\omega_6^3c_s^2v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2 + 6\omega_6^3v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 - 6\omega_6^3v_3^2v_1^2\omega_{13}\omega_{11}^2\omega_{18}^2 - 3\omega_6^2\omega_{22}v_3^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 \Big) \frac{v_3}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9}
\end{aligned}$$

$$C_{\mathbf{D}_x \mathbf{D}_x^2 \rho}^{(1), \text{MRT}^2} = C_{\mathbf{D}_x \mathbf{D}_x^2 \rho}^{(1), \text{MRT}^1}$$

$$\begin{aligned}
C_{\mathbf{D}_x \mathbf{D}_x^2 \rho}^{(1), \text{CLBM1}} = & (-36\omega_{22}c_s^2\omega_{13}\omega_{18}^2\omega_9 + 36\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + 12\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - 36\omega_6^2\omega_{22}c_s^2\omega_{18}^2 - 12\omega_6^2v_3^2\omega_{11}\omega_{18}^2\omega_9 + \\
& 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_9 - 6\omega_6^2\omega_{22}\omega_{13}\omega_{18}^2 + 12\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6\omega_{22}v_3^2\omega_{18}^2\omega_9 - 6\omega_6^2v_3^2\omega_{13}\omega_{11}\omega_{18}^2 - 6\omega_6^2v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6\omega_{22}\omega_{18}^2\omega_9 - \\
& 12\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_9 - 18\omega_6^2c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6v_3^2\omega_{11}\omega_{18}^2\omega_9 - 6\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_9 + 12\omega_6^2\omega_{22}\omega_{18}^2 + 3\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + \\
& 12\omega_6^2\omega_{22}v_3^2\omega_{18}^2\omega_9 - 12\omega_6^2\omega_{11}\omega_{18}^2 - 12\omega_6\omega_{11}\omega_{18}^2\omega_9 - 15\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}^2\omega_9 - 18\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 54\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + \\
& 18\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6\omega_{13}\omega_{11}\omega_{18}\omega_9 + 54\omega_6\omega_{22}c_s^2\omega_{13}\omega_{18}^2\omega_9 + 12\omega_6^2v_3^2\omega_{11}\omega_{18}^2 + 6\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}v_3^2\omega_{18}^2 + \\
& \omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + 3\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + 18\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}^2 + 6\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_9 + 36\omega_6c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - \\
& 12\omega_6^2\omega_{22}\omega_{18}^2\omega_9 - 12\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 6\omega_6^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - 36\omega_6^2c_s^2\omega_{11}\omega_{18}^2\omega_9 - 9\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 3\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - \\
& 12\omega_6v_3^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - 18\omega_6^2c_s^2\omega_{13}\omega_{11}\omega_{18}^2 - 36\omega_6c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 36\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_9 + 36\omega_6c_s^2\omega_{11}\omega_{18}^2\omega_9 + 6\omega_6^2\omega_{13}\omega_{11}\omega_{18}^2 + \\
& 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + 12\omega_6^2\omega_{11}\omega_{18}^2\omega_9 + 36\omega_6^2c_s^2\omega_{11}\omega_{18}^2 + 6\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{18}^2 - 5\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{18}^2\omega_9 + 12\omega_6\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - \\
& 12\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - 36\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - \omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}^2\omega_9 - 18\omega_6\omega_{22}\omega_{13}\omega_{18}^2\omega_9 - 36\omega_6\omega_{22}c_s^2\omega_{18}^2\omega_9 + 18\omega_6\omega_{22}v_3^2\omega_{13}\omega_{18}^2\omega_9 + \\
& 5\omega_6^2\omega_{22}\omega_{13}\omega_{18}^2\omega_9 - 12\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 36\omega_6^2\omega_{22}c_s^2\omega_{18}^2\omega_9 - 36\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_{22}\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + 18\omega_6^2c_s^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + \\
& 12\omega_{22}\omega_{13}\omega_{18}^2\omega_9 + 18\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^2v_3^2\omega_{13}\omega_{11}\omega_{18}^2\omega_9) \frac{v_3c_s^2}{12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}^2\omega_9}
\end{aligned}$$

$$C_{\mathbf{D}_x \mathbf{D}_x^3 \rho}^{(1), \text{CLBM2}} = C_{\mathbf{D}_x \mathbf{D}_x^3 \rho}^{(1), \text{CLBM1}}$$

$$\begin{aligned}
C_{\mathbf{D}_x \mathbf{D}_x^3 \rho}^{(1), \text{CuLBM1}} = & (-3\omega_6v_3^2\omega_8\omega_2^2 + 6v_3^2\omega_8^2\omega_2 - 36\omega_6c_s^2\omega_8 + 3\omega_6\omega_8\omega_2^2 - 12\omega_6\omega_8^2 + 12\omega_6v_3^2\omega_8^2 + 36c_s^2\omega_8\omega_2 + 3\omega_6c_s^2\omega_8^2\omega_2^2 - 12\omega_8\omega_2 - 36c_s^2\omega_8^2 + \\
& 6\omega_8\omega_2^2 - 36\omega_6c_s^2\omega_8^2\omega_2 - 18c_s^2\omega_8\omega_2^2 - 12v_3^2\omega_8^2 + 12\omega_6\omega_8 - 12\omega_6v_3^2\omega_8 + v_3^2\omega_8^2\omega_2 + 18\omega_6v_3^2\omega_8\omega_2 + 36\omega_6c_s^2\omega_8^2 - 18\omega_6\omega_8\omega_2 - 12\omega_6v_3^2\omega_8^2\omega_2 - \\
& 6v_3^2\omega_8\omega_2^2 + 12\omega_6\omega_8^2\omega_2 - \omega_8^2\omega_2^2 + 18\omega_6c_s^2\omega_2^2 + 3c_s^2\omega_8^2\omega_2^2 + 54\omega_6c_s^2\omega_8\omega_2 + 12\omega_6\omega_2 - 12\omega_6v_3^2\omega_2 - 9\omega_6c_s^2\omega_8\omega_2^2 + 18c_s^2\omega_8^2\omega_2 - 6\omega_6\omega_2^2 + 12\omega_8^2 + \\
& 6\omega_6v_3^2\omega_2^2 - 6\omega_8^2\omega_2 - 36\omega_6c_s^2\omega_2 + 12v_3^2\omega_8\omega_2 + \omega_6v_3^2\omega_8^2\omega_2^2 - \omega_6\omega_8^2\omega_2^2) \frac{v_3c_s^2}{12\omega_6\omega_8^2\omega_2^2}
\end{aligned}$$

$$\begin{aligned}
C_{\mathbf{D}_x \mathbf{D}_x^3 \rho}^{(1), \text{CuLBM2}} = & (9\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - 56\omega_3v_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 36v_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 + 120\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 36\omega_3^2c_s^2\omega_1^2\omega_2^3 - 18c_s^2\omega_4^2\omega_1^3\omega_2^3 + 92\omega_3^2v_3^2\omega_1^2\omega_2^3 - \\
& 9\omega_3^2v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 152\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2 - 104\omega_3^2c_s^2\omega_1^2\omega_2^3 - 342\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 54\omega_3^2c_s^4\omega_1^3\omega_2^3 - 276\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2 + 6\omega_3^2v_1^4\omega_1^3\omega_2^3 + 216\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^3 + \\
& 48\omega_3c_s^4\omega_4^2\omega_1^3\omega_2 + 12\omega_3^2c_s^4\omega_1^2\omega_2^3 - 288\omega_3^2c_s^4\omega_1^2\omega_2^3 + 104\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^2 - 108\omega_3^2c_s^4\omega_1^2\omega_2^3 + 18\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 72\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 56\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 + \\
& 36\omega_3^2v_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 56\omega_3^2v_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 136\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^2 - 24\omega_3^2v_1^4\omega_4^2\omega_1\omega_2^2 + 144\omega_3^2c_s^4\omega_4^2\omega_1^3 - 8\omega_3^2\omega_4^2\omega_1\omega_2^2 + 36c_s^2\omega_4^2\omega_1^2\omega_2^2 - 6\omega_3^2v_1^4\omega_4^2\omega_1\omega_2^2 + \\
& 56\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 + 18v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 108\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^2 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 + 1232\omega_3^2v_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 92\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + \\
& 144\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 - 27\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 208\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 368\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 228\omega_3^2v_1^4\omega_4^2\omega_1\omega_2^3 + 28\omega_3^2\omega_4^2\omega_1\omega_2^3 - 712\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 54c_s^4\omega_4^2\omega_1^3\omega_2^3 - \\
& 460\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3^2v_3^2c_s^2\omega_1^3\omega_2^3 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 - 27\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^2 + 8\omega_3^2\omega_4^2\omega_1^3 + 48\omega_3^2v_3^2\omega_4^2\omega_1^3 + 184\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 208\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - \\
& 36\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 14\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - 78\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 - 132\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2 - 20\omega_3^2\omega_4^2\omega_1^3\omega_2 + 320\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3 - 72\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 16\omega_3c_s^2\omega_4^2\omega_1^3\omega_2 - \\
& 412\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 6\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2^3 + 160\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - 96\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 - 9\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 18\omega_3^2c_s^2v_1^4\omega_4^2\omega_1^3\omega_2^3 + 52\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + \\
& 16\omega_3^2\omega_4^2\omega_1^3\omega_2 + 120\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2 - 6\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 18\omega_3^2c_s^2v_1^4\omega_4^2\omega_1^3\omega_2^3 - 168\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3 + 40\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 88\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2 - \\
& 144\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 108\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 56\omega_3^2v_3^2\omega_4^2\omega_1^3 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 18\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 6\omega_3^2v_1^4\omega_4^2\omega_1^3\omega_2^3 - 108c_s^4\omega_4^2\omega_1^3\omega_2^3 + 32\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 + \\
& 448\omega_3^2v_3^2c_s^2\omega_4^2\omega_1\omega_2^3 + 6\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 72\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 118\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 16\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 78\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 + 14\omega_3^2\omega_4^2\omega_1^3\omega_2^3 + \\
& 394\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 144\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 - 16\omega_3^2\omega_4^2\omega_1^3\omega_2^3 - 256\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 - 784\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 9\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 588\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3) \frac{v_3}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{\mathbf{D}_x \mathbf{D}_x^3 v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} :$$

$$C_{\mathbf{D}_x \mathbf{D}_x^3 v_1}^{(1), \text{SRT}} = (2 - \omega + v_3^2\omega - 2v_3^2 + 3c_s^2\omega - 6c_s^2) \frac{v_3v_1\rho}{12\omega}$$

$$\begin{aligned}
C_{\mathbf{D}_x \mathbf{D}_x^3 v_1}^{(1), \text{MRT}^1} = & (72\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18}^2\omega_9 + 12\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{18}^2\omega_9 + 12\omega_6^3\omega_{13}^2\omega_{11}^2\omega_{18}^2\omega_9 - 66\omega_6^2\omega_{22}\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9 + 6\omega_6^3\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + \\
& 24\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_9 + 6\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2c_s^2\omega_{13}^2\omega_{11}^2\omega_{18}^2\omega_9 - 12\omega_6^3v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 84\omega_6^2\omega_{22}c_s^2\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9 - \\
& 24\omega_6^2\omega_{22}v_3^2\omega_{13}^2\omega_{11}^2\omega_9 + 12\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}\omega_{13}^2\omega_{11}\omega_{18}\omega_9 - 96\omega_{22}c_s^2\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9 - 18\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{18}^2\omega_9 - \\
& 24\omega_6^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 24\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + \omega_6^3\omega_{22}v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 24\omega_6^2v_3^2\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9 + 3\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 12\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}^2\omega_9 + \\
& 24\omega_6^2v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 24\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 24\omega_6^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 12\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 66\omega_6^2\omega_{22}c_s^2\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9 + \\
& 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}v_3^2\omega_{13}^2\omega_{11}^2\omega_{18}^2\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}^2\omega_{11}^2\omega_{18}\omega_9 - \omega_6^3\omega_{22}\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 12\omega_6^3c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 24\omega_6^2\omega_{22}c_s^2\omega_{11}\omega_{18}\omega_9 + \\
& 36\omega_6\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^3v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^3\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - \\
& 36\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 24\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 36\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 24\omega_6^2\omega_{22}\omega_{13}\omega_{11}\omega_9 + \\
& 6\omega_6^3\omega_{22}\omega_{13}\omega_{18}\omega_9 + 24\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 36\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 + 24\omega_6^2v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 12\omega_6^2v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 12\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + \\
& 24\omega_3^2\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_{18} - 12\omega_6^2c_s^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 4\omega_3^2\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}^2\omega_9 + 156\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - \\
& 18\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2\omega_{18}\omega_9 + 12\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}^2\omega_{18}\omega_9 - 42\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 24\omega_6^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + \\
& 12\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 48\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}^2\omega_9 + 60\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^2\omega_{22}\omega_{13}\omega_{11}^2\omega_9 + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 +
\end{aligned}$$

$$\begin{aligned} & 12\omega_6^2\omega_{13}\omega_{11}\omega_9 - 5\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 3\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^3c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 18\omega_6^3v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - \\ & 12\omega_6^2c_s^2\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2c_s^2\omega_{11}\omega_{18} - 18\omega_6^3v_3^2\omega_{13}\omega_{11}\omega_{18} - 6\omega_6^3\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 + 12\omega_6^2c_s^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^3\omega_{13}\omega_{11}\omega_{18} - \\ & 36\omega_6^2\omega_{22}v_3^2\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{18} + 12\omega_6^3\omega_{22}c_s^2\omega_{18}\omega_9 + 5\omega_6^2\omega_{22}\omega_{13}\omega_{18}\omega_9 + 18\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{18}\omega_9 + 12\omega_6^3\omega_{22}\omega_{18} - \\ & 18\omega_6^3v_3^2\omega_{13}\omega_{11}\omega_9 + 6\omega_6^3\omega_{13}\omega_{11}\omega_9 - 15\omega_6^3\omega_{22}v_3^2\omega_{13}\omega_{18}\omega_9 - 12\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 12\omega_6^3\omega_{11}\omega_{18} + 36\omega_6^3v_3^2\omega_{11}\omega_{18}\omega_9 - \\ & 18\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_9 - 6\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_9 - \omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9) \frac{c_s^2\rho}{12\omega_6^3\omega_{22}\omega_{13}\omega_{11}\omega_{18}\omega_9} \end{aligned}$$

$$C_{D_x D_z^3 v_3}^{(1), \text{CLBM2}} = C_{D_x D_z^3 v_3}^{(1), \text{CLBM1}}$$

$$\begin{aligned} \mathcal{D}_{\text{CpD}^3\text{v}_3}^{(1), \text{CuLBMI}} = & (-3\omega_6 v_3^2 \omega_8 \omega_2^2 - 12\omega_6 c_s^2 \omega_8 + \omega_6 \omega_8 \omega_2^2 - 12\omega_2^2 - 12c_s^2 \omega_8 \omega_2 + 12\omega_8 \omega_2 + 6\omega_2^3 - 6\omega_8 \omega_2^2 + 6c_s^2 \omega_8 \omega_2^2 - \omega_8 \omega_2^3 + c_s^2 \omega_8 \omega_2^3 + \\ & 6\omega_6 c_s^2 \omega_2^3 + 36v_3^2 \omega_2^2 + 18v_3^2 \omega_8 \omega_2^2 - 18v_3^2 \omega_2^3 - 18\omega_6 c_s^2 \omega_2^2 + 18\omega_6 c_s^2 \omega_8 \omega_2 - 12\omega_6 \omega_2 + 3v_3^2 \omega_8 \omega_2^3 + 36\omega_6 v_3^2 \omega_2 - 5\omega_6 c_s^2 \omega_8 \omega_2^2 - 6c_s^2 \omega_2^3 + 18\omega_6 \omega_2^2 - \\ & 54\omega_6 v_3^2 \omega_2^2 + 12\omega_6 c_s^2 \omega_2 + 18\omega_6 v_3^2 \omega_2^3 + 12c_s^2 \omega_2^2 - 36v_3^2 \omega_8 \omega_2 - 6\omega_6 \omega_2^3 - \omega_6 c_s^2 \omega_8 \omega_2^3) \frac{c_s^2 \rho}{12\omega_6 \omega_8 \omega_2^3} \end{aligned}$$

$$C_{\text{D}_x \text{D}_x^2 \text{v}_3}^{(1), \text{CuLBM2}} = (94\omega_3 c_s^4 \omega_4 \omega_1 \omega_2^3 - 90\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2^2 - 222\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 40\omega_3 c_s^2 \omega_4 \omega_2^3 + 8c_s^4 \omega_4 \omega_1^3 \omega_2 + 138\omega_3 v_3^2 \omega_4 \omega_1^3 \omega_2^2 - 18\omega_4 \omega_1 \omega_2^3 + 3\omega_3 c_s^2 v_1^2 \omega_4 \omega_1^3 \omega_2^2 - 24\omega_3 c_s^2 \omega_4 \omega_1^3 \omega_2^2 + 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + \omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2^3 + 14\omega_3 \omega_4 \omega_1 \omega_2^3 - 288\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2 - 153\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 28\omega_3 c_s^4 \omega_4 \omega_1 \omega_2^2 - 312\omega_3 v_3^2 c_s^2 \omega_4 \omega_2^3 + 24v_3^2 c_s^4 \omega_4 \omega_1 \omega_2^3 + 16\omega_3 c_s^4 \omega_4 \omega_2^3 - 16\omega_3 c_s^4 \omega_4 \omega_1^2 \omega_2 + 20c_s^4 \omega_4 \omega_2^3 \omega_2^2 + 192\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 36\omega_3 c_s^4 \omega_1 \omega_2^3 - 6\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 68\omega_3 c_s^4 \omega_4 \omega_2^3 - 168\omega_3 v_3^4 \omega_4 \omega_1^2 \omega_2^2 + 144\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^3 + 9c_s^4 \omega_4 \omega_1^3 \omega_2^3 - \omega_3 v_1^2 \omega_4 \omega_1^3 \omega_2^2 + 108\omega_3 v_3^2 c_s^2 \omega_1 \omega_2^3 + 153\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 - 240\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 - 18c_s^4 \omega_4 \omega_1^3 \omega_2^2 - 138\omega_3 v_3^4 \omega_4 \omega_1^2 \omega_2^3 + 42\omega_3 c_s^2 \omega_4 \omega_1^3 \omega_2 - 20\omega_3 c_s^2 \omega_4 \omega_1^3 + 24\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^3 + 120\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2 - 8c_s^2 \omega_4 \omega_1^3 \omega_2^2 - 36\omega_3 c_s^2 \omega_1 \omega_2^3 + 9\omega_3 c_s^4 \omega_1^3 \omega_2^3 + 408\omega_3 v_3^4 \omega_4 \omega_1 \omega_2^2 - 264\omega_3 v_3^4 \omega_4 \omega_2^3 - 54\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^3 + 17\omega_3 c_s^4 \omega_4 \omega_1 \omega_2^2 + 27v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2^2 - 81\omega_3 v_3^2 \omega_4 \omega_1^3 \omega_2^2 - 8c_s^2 \omega_4 \omega_1^2 \omega_2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^3 + 36\omega_3 c_s^2 \omega_1^2 \omega_2^3 + 32\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 60\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - \omega_3 v_1^4 \omega_4 \omega_1^2 \omega_2^3 - 24\omega_3 v_3^4 \omega_4 \omega_1 \omega_2^2 - 96\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - 20c_s^4 \omega_4 \omega_1^2 \omega_2^2 + 8\omega_3 c_s^4 \omega_4 \omega_1^2 \omega_2 + 7\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1^3 - 54v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 - 3\omega_3 c_s^4 \omega_4 \omega_1^3 \omega_2^2 - 108\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2^2 + 84\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 9c_s^2 \omega_4 \omega_1^3 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^3 \omega_2^3 + 432\omega_3 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 - 10\omega_3 \omega_4 \omega_1^3 \omega_2^2 + 10\omega_3 c_s^4 \omega_4 \omega_1^2 \omega_2^2 - 54v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 + 144\omega_3 v_3^2 \omega_4 \omega_2^3 + 24c_s^2 c_s^2 \omega_4 \omega_2^3 \omega_2 - 7\omega_3 \omega_4 \omega_2^2 \omega_2^3 - 36\omega_3 c_s^4 \omega_2^2 \omega_2^3 + \omega_3 v_1^4 \omega_4 \omega_2^3 \omega_2^2 - 8\omega_3 \omega_4 \omega_2^3 - 4\omega_3 \omega_4 \omega_2^2 \omega_2^2 - 32\omega_3 c_s^4 \omega_4 \omega_2^3 \omega_2 + 27\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2^3 + 60v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 29\omega_3 c_s^4 \omega_4 \omega_1^2 \omega_2^2 - 60\omega_3 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^3 \omega_2^2 + 138\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 96\omega_3 v_3^2 \omega_4 \omega_1^3 + 81\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^2 + 8c_s^4 \omega_4 \omega_1 \omega_2^2) \frac{\rho}{36\omega_3 \omega_4 \omega_1 \omega_2^3 \omega_3^2}$$

coefficient $C_{D_y D_z^3 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_2 \partial x_3^3}$:

$$C_{D_y D_z^3 \rho}^{(1), \text{SRT}} = 0$$

$$C_{D_3 D_2 \rho}^{(1), MRT1} = (-4w_6 w_{19} w_{720} w_{85} w_{18}^2 + 8w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 3w_6^2 v_3^2 w_{720} w_{11} w_{85} w_{18}^2 - 4w_6 v_3^2 w_{720} w_{11} w_{85} w_{18}^2 +$$

 $2w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} - 4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 4w_6^2 w_{20} w_{11} w_{85} w_{18}^2 + 24w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 9w_6^2 c_s^2 w_{720} w_{11} w_{85} w_{18}^2 -$
 $4w_6 w_{19} w_{20} w_{11} w_{85} w_{18}^2 - 12w_6 c_s^2 w_{720} w_{11} w_{85} w_{18}^2 - 4w_{19} w_{720} w_{11} w_{85} w_{18}^2 - 12w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 4w_6^2 w_{19} w_{720} w_{11} w_{18}^2 -$
 $4w_6 w_{720} w_{11} w_{85} w_{18}^2 + 4w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{18}^2 - 2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 12w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18}^2 + 2w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} -$
 $2w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} + 6w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 6w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 4w_6 v_3^2 w_{20} w_{11} w_{85} w_{18}^2 - 4w_6^2 w_{19} w_{20} w_{11} w_{85} w_{18}^2 +$
 $12w_6^2 w_{19} c_s^2 w_{20} w_{11} w_{85} w_{18} + 2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 6w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 12w_6^2 c_s^2 w_{20} w_{11} w_{85} w_{18} + 4w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} -$
 $2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6^2 w_{19} v_3^2 w_{20} w_{11} w_{85} w_{18} + 4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 12w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} +$
 $12w_6 w_{19} c_s^2 w_{720} w_{85} w_{18}^2 - 2w_6^2 w_{720} w_{11} w_{85} w_{18} - 2w_6^2 w_{720} w_{11} w_{85} w_{18} - 2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} v_3^2 w_{720} w_{85} w_{18}^2 +$
 $6w_6^2 c_s^2 w_{720} w_{11} w_{85} w_{18} + 12w_6 w_{19} c_s^2 w_{20} w_{11} w_{85} w_{18} + 6w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} + 2w_6^2 v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} v_3^2 w_{20} w_{11} w_{85} w_{18} +$
 $2w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} + 2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} w_{720} w_{11} w_{85} w_{18} - 4w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} + 8w_6 w_{19} w_{720} w_{11} w_{85} w_{18}^2 +$
 $4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} w_{20} w_{11} w_{85} w_{18}^2 + 12w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} + 12w_6^2 c_s^2 w_{720} w_{11} w_{85} w_{18}^2 + 4w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} +$
 $4w_6 w_{720} w_{11} w_{85} w_{18}^2 + 4w_6 w_{19} w_{20} w_{11} w_{85} w_{18} + 2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 4w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 6w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} +$
 $6w_6^2 c_s^2 w_{720} w_{11} w_{85} w_{18} - 12w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 4w_6 w_{19} w_{720} w_{11} w_{85} w_{18} + 4w_6 v_3^2 w_{720} w_{11} w_{85} w_{18}^2 - 2w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} -$
 $8w_6 w_{19} w_{720} w_{11} w_{85} w_{18} + 2w_6^2 v_3^2 w_{720} w_{11} w_{85} w_{18} + 12w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{18}^2 - 12w_6^2 c_s^2 w_{20} w_{11} w_{85} w_{18} + 12w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} -$
 $4w_6^2 v_3^2 w_{20} w_{11} w_{85} w_{18} - 12w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} -$
 $2w_6^2 w_{720} w_{11} w_{85} w_{18} + 3w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 4w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 12w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 12w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} -$
 $2w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 12w_6^2 w_{19} c_s^2 w_{20} w_{11} w_{85} w_{18} + 2w_6^2 w_{19} w_{720} w_{85} w_{18}^2 - 4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6^2 w_{19} v_3^2 w_{20} w_{11} w_{85} w_{18} +$
 $2w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18} + 9w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} + 3w_6^2 w_{720} w_{11} w_{85} w_{18} - 6w_6^2 w_{19} c_s^2 w_{720} w_{85} w_{18} - 4w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} +$
 $4w_6^2 w_{20} w_{11} w_{85} w_{18} + 12w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 2w_6^2 w_{19} v_3^2 w_{720} w_{85} w_{18} + 4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6^2 w_{19} w_{20} w_{11} w_{85} w_{18} -$
 $4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} + 4w_6 w_{19} w_{720} w_{11} w_{85} w_{18} - 4w_6^2 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 4w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} - 12w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} -$
 $12w_6^2 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18} - 8w_6 w_{19} v_3^2 w_{720} w_{11} w_{85} w_{18} +$
 $4w_{19} w_{720} w_{11} w_{85} w_{18} + 12w_6^2 c_s^2 w_{20} w_{11} w_{85} w_{18} + 4w_6^2 v_3^2 w_{20} w_{11} w_{85} w_{18} - 24w_6 w_{19} c_s^2 w_{720} w_{11} w_{85} w_{18}) \frac{v_3^2 v_2^2}{4w_6^2 w_{19} w_{720} w_{11} w_{85} w_{18}}$

$$C_{D_y D_z^3 \rho}^{(1), \text{MRT2}} = C_{D_y D_z^3 \rho}^{(1), \text{MRT1}}$$

$$C_{D_y D_z^3 \rho}^{(1), \text{CLBM1}} = 0$$

$$C_{D_y D_z^3 \rho}^{(1), \text{CLBM2}} = 0$$

coefficient $C_{D_z^4 \rho}^{(1)}$ at $\frac{\partial^4 \rho}{\partial x_3^4}$:

$$C_{D_z^4 \rho}^{(1), \text{SRT}} = (6v_3^4 - 3v_3^4\omega - 12v_3^2c_s^2\omega + 2c_s^4 - c_s^4\omega + 24v_3^2c_s^2 + 3v_3^2\omega - 6v_3^2 + c_s^2\omega - 2c_s^2) \frac{v_1}{24\omega}$$

$$C_{D_z^4 \rho}^{(1), \text{MRT}^1} = (216v_3^2c_s^2\omega_{11}\omega_{18}^2 - \omega_6^2c_s^4\omega_{11}^2\omega_{18}^2 + 12\omega_6^2v_3^4\omega_{11}^2 - 144\omega_6v_3^2c_s^2\omega_{11}^2 + 150\omega_6^2v_3^2c_s^2\omega_{11}\omega_{18}^2 - 144\omega_6^2v_3^2c_s^2\omega_{18}^2 + 24\omega_6c_s^2\omega_{11}^2 - 24\omega_6^2v_3^2\omega_{11}\omega_{18} + 36\omega_6^2v_3^2\omega_{18}^2 - 432\omega_6v_3^2c_s^2\omega_{11}\omega_{18}^2 + 96\omega_6v_3^2\omega_{11}\omega_{18} + 48v_3^4\omega_{11}\omega_{18}^2 + 36\omega_6^2v_3^4\omega_{11}\omega_{18}^2 + 24\omega_6c_s^4\omega_{18}^2 + 48\omega_6c_s^2\omega_{11}\omega_{18}^2 + 24c_s^2\omega_{11}^2\omega_{18} + 12\omega_6^2c_s^2\omega_{11}^2\omega_{18} + 12\omega_6^2c_s^2\omega_{18}^2 + \omega_6^2c_s^2\omega_{11}^2\omega_{18}^2 + 72\omega_6v_3^4\omega_{18}^2 - 144\omega_6v_3^2c_s^2\omega_{11}\omega_{18} + 24\omega_6^2v_3^4\omega_{11}\omega_{18} - 96\omega_6v_3^2\omega_{11}^2\omega_{18} - 48v_3^2\omega_{11}\omega_{18}^2 + 72\omega_6^2v_3^2c_s^2\omega_{11}\omega_{18} - 36\omega_6^2v_3^2\omega_{11}\omega_{18}^2 + 12\omega_6^2c_s^4\omega_{11}^2 - 48\omega_6c_s^4\omega_{11}\omega_{18}^2 - 24c_s^4\omega_{11}^2\omega_{18} - 12\omega_6^2c_s^4\omega_{11}^2\omega_{18} + 24\omega_6v_3^2\omega_{11}^2 - 126\omega_6^2v_3^2c_s^2\omega_{11}^2\omega_{18} - 36\omega_6^2v_3^4\omega_{18}^2 + 288\omega_6v_3^2c_s^2\omega_{18}^2 + 48\omega_6v_3^2\omega_{11}\omega_{18} + 3\omega_6^2v_3^2\omega_{11}^2\omega_{18}^2 - 24\omega_6c_s^2\omega_{18}^2 + 72\omega_6^2v_3^2c_s^2\omega_{11}^2 - 216v_3^2c_s^2\omega_{11}^2\omega_{18} - 48\omega_6c_s^2\omega_{11}^2\omega_{18} - 24c_s^2\omega_{11}\omega_{18}^2 - 14\omega_6^2c_s^2\omega_{11}\omega_{18}^2 + 432\omega_6v_3^2c_s^2\omega_{11}\omega_{18} - 96\omega_6v_3^4\omega_{11}\omega_{18} - 12\omega_6^2v_3^2\omega_{11}^2 - 48v_3^4\omega_{11}^2\omega_{18} - 24\omega_6c_s^4\omega_{11}^2 - 30\omega_6^2v_3^4\omega_{11}^2\omega_{18} - 48\omega_6v_3^4\omega_{11}\omega_{18} - 3\omega_6^2v_3^4\omega_{11}\omega_{18}^2 - 12\omega_6^2c_s^2\omega_{11}^2 - 24\omega_6v_3^4\omega_{11}^2 - 12\omega_6^2c_s^4\omega_{18}^2 + 48\omega_6c_s^4\omega_{11}\omega_{18} + 24c_s^4\omega_{11}\omega_{18}^2 + 14\omega_6^2c_s^4\omega_{11}\omega_{18}^2 - 72\omega_6v_3^2\omega_{18}^2 - 12\omega_6^2v_3^2c_s^2\omega_{11}\omega_{18}^2 + 96\omega_6v_3^2\omega_{11}\omega_{18}^2 + 48v_3^2\omega_{11}^2\omega_{18} + 30\omega_6^2v_3^2\omega_{11}^2\omega_{18}) \frac{v_1}{24\omega_6^2\omega_{11}^2\omega_{18}^2}$$

$$C_{D_z^4 \rho}^{(1), \text{MRT}^2} = C_{D_z^4 \rho}^{(1), \text{MRT}^1}$$

$$C_{D_z^4 \rho}^{(1), \text{CLBM}^1} = (6v_3^4 + c_s^2\omega_{11} + 2c_s^4 + 3v_3^2\omega_{11} + 24v_3^2c_s^2 - c_s^4\omega_{11} - 6v_3^2 - 3v_3^4\omega_{11} - 2c_s^2 - 12v_3^2c_s^2\omega_{11}) \frac{v_1}{24\omega_{11}}$$

$$C_{D_z^4 \rho}^{(1), \text{CLBM}^2} = C_{D_z^4 \rho}^{(1), \text{CLBM}^1}$$

$$C_{D_z^4 \rho}^{(1), \text{CuLBM}^1} = (3\omega_6v_3^2 + 6v_3^4 + \omega_6c_s^2 - 12\omega_6v_3^2c_s^2 + 2c_s^4 + 24v_3^2c_s^2 - 3\omega_6v_3^4 - 6v_3^2 - \omega_6c_s^4 - 2c_s^2) \frac{v_1}{24\omega_6}$$

$$C_{D_z^4 \rho}^{(1), \text{CuLBM}^2} = (-3c_s^4\omega_1\omega_2 + 24v_3^2c_s^2\omega_1 + 6v_3^4\omega_1 + 4c_s^4\omega_2 + 48v_3^2c_s^2\omega_2 + 2c_s^4\omega_1 + 12v_3^4\omega_2 + 3c_s^2\omega_1\omega_2 - 6v_3^2\omega_1 - 4c_s^2\omega_2 + 9v_3^2\omega_1\omega_2 - 9v_3^4\omega_1\omega_2 - 2c_s^2\omega_1 - 36v_3^2c_s^2\omega_1\omega_2 - 12v_3^2\omega_2) \frac{v_1}{72\omega_1\omega_2}$$

$$\text{coefficient } C_{D_z^4 v_1}^{(1)} \text{ at } \frac{\partial^4 v_1}{\partial x_3^4} :$$

$$C_{D_z^4 v_1}^{(1), \text{SRT}} = (-72v_3^4 - 3c_s^4\omega^3 + 108v_3^4\omega + 216v_3^2c_s^2\omega + 30c_s^4\omega^2 + 48c_s^4 - 84v_3^2c_s^2\omega^2 - 72c_s^4\omega - 42v_3^4\omega^2 + 6v_3^2c_s^2\omega^3 + 3v_3^4\omega^3 - 144v_3^2c_s^2 - 108v_3^2\omega - 14c_s^2\omega^2 + c_s^2\omega^3 - 3v_3^2\omega^3 + 72v_3^2 + 36c_s^2\omega - 24c_s^4 + 42v_3^2\omega^2) \frac{\rho}{24\omega^3}$$

$$C_{D_z^4 v_1}^{(1), \text{MRT}^1} = (-12\omega_6^3v_3^2c_s^2\omega_{18} - 96v_3^2c_s^2\omega_{18}^2 - 72\omega_6^2v_3^2c_s^2\omega_{18} + 24\omega_6^2v_3^2\omega_{18} + 6\omega_6^3c_s^4\omega_{18} - 48\omega_6c_s^4\omega_{18}^2 + 24\omega_6^2c_s^2\omega_{18} + 3\omega_6^3v_3^4\omega_{18}^2 - 24\omega_6^2v_3^4 - 48\omega_6v_3^4\omega_{18} - 8\omega_6^2c_s^2\omega_{18}^2 - 18\omega_6^3v_3^4\omega_{18} + 24\omega_6v_3^4\omega_{18}^2 + 12\omega_6^3v_3^2c_s^2 - 72\omega_6^2v_3^2\omega_{18} - 3\omega_6^3c_s^4\omega_{18}^2 + 24\omega_6c_s^4\omega_{18} + 24c_s^4\omega_{18}^2 + 12\omega_6^3v_3^4 + 48\omega_6^2v_3^2c_s^2\omega_{18} + 6\omega_6^3v_3^2c_s^2\omega_{18} - 24\omega_6^2v_3^4\omega_{18} - 6\omega_6^3c_s^2\omega_{18} + 156\omega_6v_3^2c_s^2\omega_{18} + 12\omega_6c_s^2\omega_{18}^2 - 24\omega_6^2c_s^4\omega_{18} - 3\omega_6^3v_3^2\omega_{18} + 48\omega_6v_3^2\omega_{18} - 12\omega_6^3v_3^2 + 24\omega_6^2c_s^4\omega_{18}^2 + 18\omega_6^2v_3^2\omega_{18} + 24\omega_6^2v_3^2 - 24\omega_6v_3^2\omega_{18}^2 + 72\omega_6^2v_3^2\omega_{18} - 24\omega_6v_3^2c_s^2\omega_{18} + \omega_6^3c_s^2\omega_{18}^2 - 24\omega_6^2v_3^2c_s^2 - 24\omega_6c_s^2\omega_{18}) \frac{\rho}{24\omega_6^3\omega_{18}^2}$$

$$C_{D_z^4 v_1}^{(1), \text{MRT}^2} = C_{D_z^4 v_1}^{(1), \text{MRT}^1}$$

$$C_{D_z^4 v_1}^{(1), \text{CLBM}^1} = (-72\omega_6^3v_3^2c_s^2\omega_{18} - 12\omega_6^2v_3^2c_s^2\omega_{18} + 12\omega_6^2v_3^2\omega_{18}^2 + 6\omega_6^3c_s^4\omega_{18} - 48\omega_6c_s^4\omega_{18}^2 + 24\omega_6^2c_s^2\omega_{18} + 3\omega_6^3v_3^4\omega_{18}^2 - 72\omega_6^2v_3^4 - 8\omega_6^2c_s^2\omega_{18}^2 - 30\omega_6^3v_3^4\omega_{18} + 108\omega_6^3v_3^2c_s^2 - 72\omega_6^2v_3^2\omega_{18} - 3\omega_6^3c_s^4\omega_{18}^2 + 24\omega_6c_s^4\omega_{18} + 24c_s^4\omega_{18}^2 + 36\omega_6^3v_3^4 + 144\omega_6^2v_3^2c_s^2\omega_{18} + 6\omega_6^3v_3^2c_s^2\omega_{18}^2 - 12\omega_6^2v_3^4\omega_{18} - 6\omega_6^3c_s^2\omega_{18} - 36\omega_6v_3^2c_s^2\omega_{18}^2 + 12\omega_6c_s^2\omega_{18}^2 - 24\omega_6^2c_s^4\omega_{18} - 3\omega_6^3v_3^2\omega_{18} - 36\omega_6^2v_3^2 + 24\omega_6^2c_s^4\omega_{18}^2 + 30\omega_6^3v_3^2\omega_{18} + 72\omega_6^2v_3^2 + 72\omega_6^2v_3^4\omega_{18} + 72\omega_6v_3^2c_s^2\omega_{18} + \omega_6^3c_s^2\omega_{18}^2 - 216\omega_6^2v_3^2c_s^2 - 24\omega_6c_s^2\omega_{18}) \frac{\rho}{24\omega_6^3\omega_{18}^2}$$

$$C_{D_z^4 v_1}^{(1), \text{CLBM}^2} = C_{D_z^4 v_1}^{(1), \text{CLBM}^1}$$

$$C_{D_z^4 v_1}^{(1), \text{CuLBM}^1} = (36v_3^4\omega_2^2 - 24c_s^4\omega_8\omega_2^2 + 3v_3^4\omega_8^2\omega_2^3 - 12v_3^2c_s^2\omega_8^2\omega_2^2 + 108v_3^2c_s^2\omega_2^3 - 24c_s^2\omega_8\omega_2 - 72v_3^4\omega_2^2 - 216v_3^2c_s^2\omega_2^2 - 12v_3^4\omega_8^2\omega_2^2 + 6v_3^2c_s^2\omega_8^2\omega_2^3 + 6c_s^4\omega_8\omega_2^3 + 24c_s^2\omega_8\omega_2^2 - 3v_3^2\omega_8^2\omega_2^3 + 24c_s^4\omega_8\omega_2 - 36v_3^2c_s^2\omega_8^2\omega_2 + 12v_3^2\omega_8^2\omega_2^2 - 6c_s^2\omega_8\omega_2^3 + 72v_3^2\omega_2^2 - 48c_s^4\omega_8^2\omega_2 + 72v_3^2c_s^2\omega_8\omega_2 - 72v_3^2\omega_8\omega_2^2 + 24c_s^4\omega_8^2 + c_s^2\omega_8^2\omega_2^2 - 36v_3^2\omega_2^2 - 8c_s^2\omega_8^2\omega_2^2 + 30v_3^2\omega_8\omega_2^2 + 12c_s^2\omega_8^2\omega_2 - 72v_3^2c_s^2\omega_8\omega_2^2 + 72v_3^4\omega_8\omega_2^2 - 3c_s^4\omega_8^2\omega_2^3 + 24c_s^4\omega_8^2\omega_2^2 + 144v_3^2c_s^2\omega_8\omega_2^2 - 30v_3^4\omega_8\omega_2^2) \frac{\rho}{24\omega_8^2\omega_2^3}$$

$$C_{D_z^4 v_1}^{(1), \text{CuLBM}^2} = (-15\omega_3v_3^4\omega_4^2\omega_1^3 - 48\omega_3^2c_s^4\omega_4^2\omega_1 + \omega_3^2c_s^2\omega_4^2\omega_1^3 + 18v_3^2\omega_4^2\omega_1^2 + 9\omega_3^2v_3^4\omega_1^3 - 36\omega_3^2v_3^2\omega_4^2\omega_1^2 + 36\omega_3v_3^4\omega_4^2\omega_1^2 + 36\omega_3v_3^2\omega_4^2\omega_1^3 - 18\omega_3^2v_3^4\omega_4^2\omega_1^2 + 15\omega_3^2v_3^2\omega_4^2\omega_1^3 - 9v_3^2\omega_4^2\omega_1^3 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2 + 12\omega_3^2c_s^2\omega_4^2\omega_1 + 54\omega_3v_3^2c_s^2\omega_4^2\omega_1^3 + 15\omega_3v_3^2\omega_4^2\omega_1^2 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 + 72\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2 + 36\omega_3^2v_3^4\omega_4^2\omega_1^2 - 18\omega_3^2\omega_4^2\omega_1^2 + 27v_3^2c_s^2\omega_4^2\omega_1^3 - 36\omega_3v_3^2c_s^2\omega_4^2\omega_1^2 - 108\omega_3v_3^2c_s^2\omega_4^2\omega_1^2 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 + 9v_3^4\omega_4^2\omega_1^3 - 54\omega_3^2c_s^2\omega_4^2\omega_1^2 - 15\omega_3^2v_3^4\omega_4^2\omega_1^3 - 36\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 + 72\omega_3v_3^2c_s^2\omega_4^2\omega_1^2 + 36\omega_3v_3^2\omega_4^2\omega_1^2 - 3\omega_3^2c_s^2\omega_4^2\omega_1^3 + 3\omega_3^2v_3^4\omega_4^2\omega_1^3 + 18\omega_3^2v_3^2\omega_4^2\omega_1^2 + 12\omega_3c_s^4\omega_4^2\omega_1^2 - 12\omega_3^2c_s^4\omega_4^2\omega_1^2 + 27\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3 + 6\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2 + 12\omega_3c_s^2\omega_4^2\omega_1^2 - 18\omega_3v_3^2\omega_4^2\omega_1^3 - 12\omega_3^2c_s^2\omega_4^2\omega_1 - 36\omega_3v_3^2c_s^2\omega_4^2\omega_1^3 - 12\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2 - 54\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2 - 54\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^2 + 3\omega_3^2c_s^4\omega_4^2\omega_1^3 - 12\omega_3^2v_3^4\omega_4^2\omega_1^2 - 9\omega_3^2v_3^2\omega_4^2\omega_1^3 - 36\omega_3^2v_3^2c_s^2\omega_4^2\omega_1 - 36\omega_3v_3^4\omega_4^2\omega_1^2 + 3\omega_3c_s^4\omega_4^2\omega_1^3 - 12\omega_3c_s^2\omega_4^2\omega_1 - 3\omega_3^2v_3^2\omega_4^2\omega_1^3 + 12\omega_3^2c_s^2\omega_4^2\omega_1^2 - 12\omega_3c_s^4\omega_4^2\omega_1^2 + 12\omega_3^2c_s^4\omega_4^2\omega_1 + 18\omega_3v_3^2\omega_4^2\omega_1^3 - 3\omega_3^2c_s^2\omega_4^2\omega_1^3 + 36\omega_3v_3^2c_s^2\omega_4^2\omega_1 + 12\omega_3^2v_3^2\omega_4^2\omega_1^2) \frac{\rho}{24\omega_3^2\omega_4^2\omega_1^3}$$

$$\text{coefficient } C_{D_z^4 v_3}^{(1)} \text{ at } \frac{\partial^4 v_3}{\partial x_3^4} :$$

$$C_{D_z^4 v_3}^{(1), \text{SRT}} = (-4 + 2\omega - 5v_3^2\omega + 10v_3^2 - 3c_s^2\omega + 6c_s^2) \frac{v_3 v_1 \rho}{12\omega}$$

$$C_{D_z^4 v_3}^{(1), \text{MRT2}} = C_{D_z^4 v_3}^{(1), \text{MRT1}}$$

$$C_{D_y D_z^3 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} + C_{D_z^4 \rho}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 \rho}{\partial x_3^4} + C_{D_z^4 v_2}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_2}{\partial x_3^4} + C_{D_z^4 v_3}^{(2)} \frac{\delta_l^4}{\delta_t} \frac{\partial^4 v_3}{\partial x_3^4} = 0,$$

where:

coefficient $C_{D_x \rho, D_x v_2}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_2}{\partial x_1}$:

$$C_{D_x \rho, D_x v_2}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2}{2\omega_5}$$

$$C_{D_x \rho, D_x v_2}^{(2), \text{MRT2}} = C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_2}^{(2), \text{CLBM1}} = C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_2}^{(2), \text{CLBM2}} = C_{D_x \rho, D_x v_2}^{(2), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_2}^{(2), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

$$C_{D_x \rho, D_x v_2}^{(2), \text{CuLBM2}} = C_{D_x \rho, D_x v_2}^{(2), \text{CuLBM1}}$$

coefficient $C_{D_x \rho, D_y v_1}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_2}$:

$$C_{D_x \rho, D_y v_1}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2}{2\omega_5}$$

$$C_{D_x \rho, D_y v_1}^{(2), \text{MRT2}} = C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(2), \text{CLBM1}} = C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(2), \text{CLBM2}} = C_{D_x \rho, D_y v_1}^{(2), \text{MRT1}}$$

$$C_{D_x \rho, D_y v_1}^{(2), \text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

$$C_{D_x \rho, D_y v_1}^{(2), \text{CuLBM2}} = (6v_1^2 \omega_1 - 6v_1^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 12c_s^2 \omega_2 + 2\omega_2 + 6c_s^2 \omega_1) \frac{1}{6\omega_1 \omega_2}$$

coefficient $C_{D_x v_1, D_y v_1}^{(2)}$ **at** $\frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_2}$:

$$C_{D_x v_1, D_y v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{MRT1}} = 0$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{MRT2}} = 0$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x v_1, D_y v_1}^{(2), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2v_1 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_x v_1}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_y \rho, D_x v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{MRT1}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{MRT2}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y \rho, D_x v_1}^{(2), \text{CuLBM2}} = (3v_1^2 \omega_1 - 3v_1^2 \omega_2 - \omega_1 - c_s^2 \omega_2 + \omega_2 + c_s^2 \omega_1) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_y v_2}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_y \rho, D_y v_2}^{(2), \text{SRT}} = (-2 + \omega - 3v_2^2 \omega - 2c_s^2 \omega + 4c_s^2 + 6v_2^2) \frac{1}{\omega}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}} = (-2 + \omega_{10} - 2c_s^2 \omega_{10} - 3v_2^2 \omega_{10} + 4c_s^2 + 6v_2^2) \frac{1}{\omega_{10}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{MRT2}} = C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CLBM1}} = C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CLBM2}} = C_{D_y \rho, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CuLBM1}} = (-2 - 3v_2^2 \omega_5 - 2c_s^2 \omega_5 + \omega_5 + 4c_s^2 + 6v_2^2) \frac{1}{\omega_5}$$

$$C_{D_y \rho, D_y v_2}^{(2), \text{CuLBM2}} = (-9v_2^2 \omega_1 \omega_2 + 3\omega_1 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 8c_s^2 \omega_2 + 12v_2^2 \omega_2 - 4\omega_2 + 6v_2^2 \omega_1 + 4c_s^2 \omega_1) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_y v_2, D_y v_2}^{(2)}$ **at** $\left(\frac{\partial v_2}{\partial x_2} \right)^2$:

$$C_{D_y v_2, D_y v_2}^{(2), \text{SRT}} = (2 - \omega) \frac{3v_2 \rho}{\omega}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}} = (2 - \omega_{10}) \frac{3v_2 \rho}{\omega_{10}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{MRT2}} = C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CLBM1}} = C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CLBM2}} = C_{D_y v_2, D_y v_2}^{(2), \text{MRT1}}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CuLBM1}} = (2 - \omega_5) \frac{3v_2 \rho}{\omega_5}$$

$$C_{D_y v_2, D_y v_2}^{(2), \text{CuLBM2}} = (-3\omega_1 \omega_2 + 2\omega_1 + 4\omega_2) \frac{v_2 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_y \rho, D_z v_3}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_y \rho, D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{MRT1}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{MRT2}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y \rho, D_z v_3}^{(2), \text{CuLBM2}} = (-\omega_1 + 3v_3^2 \omega_1 - c_s^2 \omega_2 + \omega_2 + c_s^2 \omega_1 - 3v_3^2 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_y v_3, D_z v_3}^{(2)}$ **at** $\frac{\partial v_3}{\partial x_2} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_y v_3, D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{MRT1}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{MRT2}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y v_3, D_z v_3}^{(2), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2v_3 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_y v_3}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_2}$:

$$C_{D_z \rho, D_y v_3}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{MRT2}} = C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CLBM1}} = C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CLBM2}} = C_{D_z \rho, D_y v_3}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_z \rho, D_y v_3}^{(2), \text{CuLBM2}} = (3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 - 12c_s^2 \omega_2 + 2\omega_2 + 6c_s^2 \omega_1 - 6v_3^2 \omega_2) \frac{1}{6\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_z v_2}^{(2)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_z \rho, D_z v_2}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{MRT2}} = C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CLBM1}} = C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CLBM2}} = C_{D_z \rho, D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_z \rho, D_z v_2}^{(2), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_x^2 v_2}^{(2)}$ **at** $\frac{\partial^2 v_2}{\partial x_1^2}$:

$$C_{D_x^2 v_2}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x^2 v_2}^{(2), \text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_x^2 v_2}^{(2),\text{MRT2}} = C_{D_x^2 v_2}^{(2),\text{MRT1}}$$

$$C_{D_x^2 v_2}^{(2),\text{CLBM1}} = C_{D_x^2 v_2}^{(2),\text{MRT1}}$$

$$C_{D_x^2 v_2}^{(2),\text{CLBM2}} = C_{D_x^2 v_2}^{(2),\text{MRT1}}$$

$$C_{D_x^2 v_2}^{(2),\text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_x^2 v_2}^{(2),\text{CuLBM2}} = C_{D_x^2 v_2}^{(2),\text{CuLBM1}}$$

$$\text{coefficient } C_{D_x D_y \rho}^{(2)} \text{ at } \frac{\partial^2 \rho}{\partial x_1 \partial x_2} :$$

$$C_{D_x D_y \rho}^{(2),\text{SRT}} = 0$$

$$C_{D_x D_y \rho}^{(2),\text{MRT1}} = 0$$

$$C_{D_x D_y \rho}^{(2),\text{MRT2}} = 0$$

$$C_{D_x D_y \rho}^{(2),\text{CLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(2),\text{CLBM2}} = 0$$

$$C_{D_x D_y \rho}^{(2),\text{CuLBM1}} = 0$$

$$C_{D_x D_y \rho}^{(2),\text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1}{3\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_x D_y v_1}^{(2)} \text{ at } \frac{\partial^2 v_1}{\partial x_1 \partial x_2} :$$

$$C_{D_x D_y v_1}^{(2),\text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_y v_1}^{(2),\text{MRT1}} = (-2 + \omega_5) \frac{c_s^2 \rho}{2\omega_5}$$

$$C_{D_x D_y v_1}^{(2),\text{MRT2}} = C_{D_x D_y v_1}^{(2),\text{MRT1}}$$

$$C_{D_x D_y v_1}^{(2),\text{CLBM1}} = C_{D_x D_y v_1}^{(2),\text{MRT1}}$$

$$C_{D_x D_y v_1}^{(2),\text{CLBM2}} = C_{D_x D_y v_1}^{(2),\text{MRT1}}$$

$$C_{D_x D_y v_1}^{(2),\text{CuLBM1}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

$$C_{D_x D_y v_1}^{(2),\text{CuLBM2}} = (6v_1^2 \omega_1 - 6v_1^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 8c_s^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1) \frac{\rho}{6\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_y^2 \rho}^{(2)} \text{ at } \frac{\partial^2 \rho}{\partial x_2^2} :$$

$$C_{D_y^2 \rho}^{(2),\text{SRT}} = (-2 + \omega - v_2^2 \omega - 3c_s^2 \omega + 6c_s^2 + 2v_2^2) \frac{v_2}{2\omega}$$

$$C_{D_y^2 \rho}^{(2),\text{MRT1}} = (-2 + \omega_{10} - 3c_s^2 \omega_{10} - v_2^2 \omega_{10} + 6c_s^2 + 2v_2^2) \frac{v_2}{2\omega_{10}}$$

$$C_{D_y^2 \rho}^{(2),\text{MRT2}} = C_{D_y^2 \rho}^{(2),\text{MRT1}}$$

$$C_{D_y^2 \rho}^{(2),\text{CLBM1}} = C_{D_y^2 \rho}^{(2),\text{MRT1}}$$

$$C_{D_y^2 \rho}^{(2),\text{CLBM2}} = C_{D_y^2 \rho}^{(2),\text{MRT1}}$$

$$C_{D_y^2 \rho}^{(2), \text{CuLBM1}} = (-2 - v_2^2 \omega_5 - 3c_s^2 \omega_5 + \omega_5 + 6c_s^2 + 2v_2^2) \frac{v_2}{2\omega_5}$$

$$C_{D_y^2 \rho}^{(2), \text{CuLBM2}} = (-3v_2^2 \omega_1 \omega_2 + 3\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 2\omega_1 + 12c_s^2 \omega_2 + 4v_2^2 \omega_2 - 4\omega_2 + 2v_2^2 \omega_1 + 6c_s^2 \omega_1) \frac{v_2}{6\omega_1 \omega_2}$$

coefficient $C_{D_y^2 v_2}^{(2)}$ **at** $\frac{\partial^2 v_2}{\partial x_2^2}$:

$$C_{D_y^2 v_2}^{(2), \text{SRT}} = (-2 + \omega - 3v_2^2 \omega - c_s^2 \omega + 2c_s^2 + 6v_2^2) \frac{\rho}{2\omega}$$

$$C_{D_y^2 v_2}^{(2), \text{MRT1}} = (-2 + \omega_{10} - c_s^2 \omega_{10} - 3v_2^2 \omega_{10} + 2c_s^2 + 6v_2^2) \frac{\rho}{2\omega_{10}}$$

$$C_{D_y^2 v_2}^{(2), \text{MRT2}} = C_{D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(2), \text{CLBM1}} = C_{D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(2), \text{CLBM2}} = C_{D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 v_2}^{(2), \text{CuLBM1}} = (-2 - 3v_2^2 \omega_5 - c_s^2 \omega_5 + \omega_5 + 2c_s^2 + 6v_2^2) \frac{\rho}{2\omega_5}$$

$$C_{D_y^2 v_2}^{(2), \text{CuLBM2}} = (-9v_2^2 \omega_1 \omega_2 + 3\omega_1 \omega_2 - 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 4c_s^2 \omega_2 + 12v_2^2 \omega_2 - 4\omega_2 + 6v_2^2 \omega_1 + 2c_s^2 \omega_1) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_y D_z \rho}^{(2)}$ **at** $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{MRT1}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{MRT2}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y D_z \rho}^{(2), \text{CuLBM2}} = (-\omega_1 + v_3^2 \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1 - v_3^2 \omega_2) \frac{v_3}{3\omega_1 \omega_2}$$

coefficient $C_{D_y D_z v_3}^{(2)}$ **at** $\frac{\partial^2 v_3}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z v_3}^{(2), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y D_z v_3}^{(2), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_y D_z v_3}^{(2), \text{MRT2}} = C_{D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(2), \text{CLBM1}} = C_{D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(2), \text{CLBM2}} = C_{D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y D_z v_3}^{(2), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_3}^{(2), \text{CuLBM2}} = (3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 - 8c_s^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1 - 6v_3^2 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_z^2 v_2}^{(2)}$ **at** $\frac{\partial^2 v_2}{\partial x_3^2}$:

$$C_{D_z^2 v_2}^{(2),\text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_z^2 v_2}^{(2),\text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_z^2 v_2}^{(2),\text{MRT2}} = C_{D_z^2 v_2}^{(2),\text{MRT1}}$$

$$C_{D_z^2 v_2}^{(2),\text{CLBM1}} = C_{D_z^2 v_2}^{(2),\text{MRT1}}$$

$$C_{D_z^2 v_2}^{(2),\text{CLBM2}} = C_{D_z^2 v_2}^{(2),\text{MRT1}}$$

$$C_{D_z^2 v_2}^{(2),\text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_z^2 v_2}^{(2),\text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_x^3 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^3}$:

$$C_{D_x^3 \rho}^{(2),\text{SRT}} = (-1 + v_1^2 + 3c_s^2) \frac{v_2 v_1}{12}$$

$$C_{D_x^3 \rho}^{(2),\text{MRT1}} = (-18c_s^2 \omega_5 \omega_{12} - 6\omega_5 \omega_9 + 6\omega_5 \omega_{12} + 18c_s^2 \omega_5 \omega_9 + 12v_1^2 \omega_{12} - 12v_1^2 \omega_9 - 6v_1^2 \omega_5 \omega_{12} + v_1^2 \omega_5 \omega_9 \omega_{12} + 6v_1^2 \omega_5 \omega_9 - \omega_5 \omega_9 \omega_{12} - 36c_s^2 \omega_9 + 36c_s^2 \omega_5 \omega_9 \omega_{12} + 12\omega_9 - 12\omega_{12} + 36c_s^2 \omega_{12}) \frac{v_2 v_1}{12\omega_5 \omega_9 \omega_{12}}$$

$$C_{D_x^3 \rho}^{(2),\text{MRT2}} = C_{D_x^3 \rho}^{(2),\text{MRT1}}$$

$$C_{D_x^3 \rho}^{(2),\text{CLBM1}} = C_{D_x^3 \rho}^{(2),\text{SRT}}$$

$$C_{D_x^3 \rho}^{(2),\text{CLBM2}} = C_{D_x^3 \rho}^{(2),\text{SRT}}$$

$$C_{D_x^3 \rho}^{(2),\text{CuLBM1}} = C_{D_x^3 \rho}^{(2),\text{SRT}}$$

$$C_{D_x^3 \rho}^{(2),\text{CuLBM2}} = C_{D_x^3 \rho}^{(2),\text{SRT}}$$

coefficient $C_{D_x^3 v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^3}$:

$$C_{D_x^3 v_1}^{(2),\text{SRT}} = (-1 + 3v_1^2 + c_s^2) \frac{v_2 \rho}{12}$$

$$C_{D_x^3 v_1}^{(2),\text{MRT1}} = (-6c_s^2 \omega_5 \omega_{12} - 6\omega_5 \omega_9 + 6\omega_5 \omega_{12} + 6c_s^2 \omega_5 \omega_9 + 36v_1^2 \omega_{12} - 36v_1^2 \omega_9 - 18v_1^2 \omega_5 \omega_{12} + 3v_1^2 \omega_5 \omega_9 \omega_{12} + 18v_1^2 \omega_5 \omega_9 - \omega_5 \omega_9 \omega_{12} - 12c_s^2 \omega_9 + c_s^2 \omega_5 \omega_9 \omega_{12} + 12\omega_9 - 12\omega_{12} + 12c_s^2 \omega_{12}) \frac{v_2 \rho}{12\omega_5 \omega_9 \omega_{12}}$$

$$C_{D_x^3 v_1}^{(2),\text{MRT2}} = C_{D_x^3 v_1}^{(2),\text{MRT1}}$$

$$C_{D_x^3 v_1}^{(2),\text{CLBM1}} = C_{D_x^3 v_1}^{(2),\text{SRT}}$$

$$C_{D_x^3 v_1}^{(2),\text{CLBM2}} = C_{D_x^3 v_1}^{(2),\text{SRT}}$$

$$C_{D_x^3 v_1}^{(2),\text{CuLBM1}} = C_{D_x^3 v_1}^{(2),\text{SRT}}$$

$$C_{D_x^3 v_1}^{(2),\text{CuLBM2}} = C_{D_x^3 v_1}^{(2),\text{SRT}}$$

coefficient $C_{D_x^3 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^3}$:

$$C_{D_x^3 v_2}^{(2),\text{SRT}} = (6 - 6v_1^2 + 6v_1^2 \omega - v_1^2 \omega^2 + \omega^2 - 6\omega - 3c_s^2 \omega^2 + 18c_s^2 \omega - 18c_s^2) \frac{v_1 \rho}{6\omega^2}$$

$$C_{D_x^3 v_2}^{(2), \text{MRT}^1} = (15c_s^2\omega_5\omega_{12} - 3\omega_5\omega_{12} + 3c_s^2\omega_5^2 - v_1^2\omega_5^2\omega_{12} - 6c_s^2\omega_5 + 3v_1^2\omega_5\omega_{12} + 6\omega_5 - 6v_1^2\omega_5 + 3v_1^2\omega_5^2 - 3c_s^2\omega_5^2\omega_{12} - 3\omega_5^2 + \omega_5^2\omega_{12} - 12c_s^2\omega_{12}) \frac{v_1\rho}{6\omega_5^2\omega_{12}}$$

$$C_{D_x^3 v_2}^{(2), \text{MRT}^2} = C_{D_x^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x^3 v_2}^{(2), \text{CLBM}^1} = (6 - 3c_s^2\omega_5\omega_{12} - 6v_1^2 + \omega_5\omega_{12} + 3v_1^2\omega_{12} + 9c_s^2\omega_5 - v_1^2\omega_5\omega_{12} - 3\omega_5 + 3v_1^2\omega_5 - 18c_s^2 - 3\omega_{12} + 9c_s^2\omega_{12}) \frac{v_1\rho}{6\omega_5\omega_{12}}$$

$$C_{D_x^3 v_2}^{(2), \text{CLBM}^2} = C_{D_x^3 v_2}^{(2), \text{CLBM}^1}$$

$$C_{D_x^3 v_2}^{(2), \text{CuLBM}^1} = (6 - 6v_1^2 + 3v_1^2\omega_1 - 3c_s^2\omega_1\omega_9 + 3v_1^2\omega_9 + \omega_1\omega_9 - 3\omega_1 - v_1^2\omega_1\omega_9 + 9c_s^2\omega_9 - 18c_s^2 + 9c_s^2\omega_1 - 3\omega_9) \frac{v_1\rho}{6\omega_1\omega_9}$$

$$C_{D_x^3 v_2}^{(2), \text{CuLBM}^2} = (-6v_1^2\omega_4 + 6\omega_3 - 6\omega_3c_s^2\omega_4\omega_1 - 18\omega_3c_s^2 + 9\omega_3c_s^2\omega_1 + 9c_s^2\omega_4\omega_1 - 3\omega_4\omega_1 + 6\omega_4 + 18\omega_3c_s^2\omega_4 - 2\omega_3v_1^2\omega_4\omega_1 + 3\omega_3v_1^2\omega_1 - 6\omega_3\omega_4 - 6\omega_3v_1^2 - 3\omega_3\omega_1 + 6\omega_3v_1^2\omega_4 - 18c_s^2\omega_4 + 2\omega_3\omega_4\omega_1 + 3v_1^2\omega_4\omega_1) \frac{v_1\rho}{12\omega_3\omega_4\omega_1}$$

coefficient $C_{D_x^2 D_y \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y \rho}^{(2), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{MRT}^1} = (-12 + 12\omega_5 - \omega_5^2) \frac{c_s^4}{6\omega_5^2}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{MRT}^2} = C_{D_x^2 D_y \rho}^{(2), \text{MRT}^1}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CLBM}^1} = C_{D_x^2 D_y \rho}^{(2), \text{MRT}^1}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CLBM}^2} = C_{D_x^2 D_y \rho}^{(2), \text{MRT}^1}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CuLBM}^1} = (-12 - \omega_1^2 + 12\omega_1) \frac{c_s^4}{6\omega_1^2}$$

$$C_{D_x^2 D_y \rho}^{(2), \text{CuLBM}^2} = (3v_1^2\omega_1^2\omega_2 + 2c_s^4\omega_1^2 - 18c_s^2v_1^2\omega_2^2 - 2c_s^2\omega_1\omega_2^2 - 15c_s^2v_1^2\omega_1^2\omega_2 + 4v_1^2\omega_2^2 + 12c_s^2v_1^2\omega_1^2 - 14c_s^4\omega_2^2 - 2v_1^2\omega_1^2 - 3v_1^4\omega_1^2\omega_2 + 14c_s^4\omega_1\omega_2^2 - 2c_s^2\omega_1^2 - 3v_1^2\omega_1\omega_2^2 - c_s^4\omega_1^2\omega_2^2 - 4v_1^4\omega_2^2 + 15c_s^2v_1^2\omega_1\omega_2^2 + 2c_s^2\omega_1^2\omega_2 + 2v_1^4\omega_1\omega_2 + 3v_1^4\omega_1\omega_2^2 + 6c_s^2v_1^2\omega_1\omega_2 + 2c_s^2\omega_2^2 + 2v_1^4\omega_1^2 - 2v_1^2\omega_1\omega_2 - 2c_s^4\omega_1^2\omega_2) \frac{1}{6\omega_1^2\omega_2^2}$$

coefficient $C_{D_x^2 D_y v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{MRT}^1} = (\omega_5\omega_{12} + 2\omega_5 - \omega_5^2 - 2\omega_{12}) \frac{c_s^2 v_1 \rho}{\omega_5^2 \omega_{12}}$$

$$C_{D_x^2 D_y v_1}^{(2), \text{MRT}^2} = C_{D_x^2 D_y v_1}^{(2), \text{MRT}^1}$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x^2 D_y v_1}^{(2), \text{CuLBM}^2} = (6\omega_2^2 - 11v_1^2\omega_1^2\omega_2 + 9c_s^2\omega_1\omega_2^2 - 14v_1^2\omega_2^2 - 5\omega_1\omega_2^2 - 2\omega_1\omega_2 + 8v_1^2\omega_1^2 + 2c_s^2\omega_1\omega_2 - 4\omega_1^2 + 8c_s^2\omega_1^2 + 11v_1^2\omega_1\omega_2^2 + 5\omega_1^2\omega_2 - 9c_s^2\omega_1^2\omega_2 - 10c_s^2\omega_2^2 + 6v_1^2\omega_1\omega_2) \frac{v_1\rho}{6\omega_1^2\omega_2^2}$$

coefficient $C_{D_x^2 D_y v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_2}^{(2), \text{SRT}} = \frac{-c_s^2 v_2 \rho}{6}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{MRT}^1} = (-12\omega_{10}\omega_5^2 - 12\omega_5\omega_{15} + 12\omega_{10}\omega_5\omega_{15} + 12\omega_{10}\omega_5 - \omega_{10}\omega_5^2\omega_{15} + 12\omega_5^2 - 12\omega_{10}\omega_{15}) \frac{c_s^2 v_2 \rho}{6\omega_{10}\omega_5^2\omega_{15}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{MRT}^2} = C_{D_x^2 D_y v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{CLBM}^1} = C_{D_x^2 D_y v_2}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{CLBM}^2} = C_{D_x^2 D_y v_2}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{CuLBM}^1} = C_{D_x^2 D_y v_2}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(2), \text{CuLBM}^2} = C_{D_x^2 D_y v_2}^{(2), \text{SRT}}$$

coefficient $C_{D_x D_y^2 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{MRT}^1} = (\omega_{10}^2 - v_2^2 \omega_{10} \omega_5 + 3c_s^2 \omega_5 \omega_{15} - \omega_5 \omega_{15} - 3c_s^2 \omega_{10} \omega_5 + \omega_{10} \omega_5 \omega_{15} + \omega_{10} \omega_5 + v_2^2 \omega_5 \omega_{15} - 3c_s^2 \omega_{10} \omega_5 \omega_{15} + 3c_s^2 \omega_{10}^2 \omega_5 + v_2^2 \omega_{10} \omega_{15} - \omega_{10}^2 \omega_5 - v_2^2 \omega_{10}^2 - v_2^2 \omega_{10} \omega_5 \omega_{15} - \omega_{10} \omega_{15} - 3c_s^2 \omega_{10}^2 + v_2^2 \omega_{10}^2 \omega_5 + 3c_s^2 \omega_{10} \omega_{15}) \frac{v_2 v_1}{\omega_{10} \omega_5 \omega_{15}}$$

$$C_{D_x D_y^2 \rho}^{(2), \text{MRT}^2} = C_{D_x D_y^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x D_y^2 \rho}^{(2), \text{CuLBM}^2} = (-4v_2^2 \omega_1 \omega_2 + 2\omega_2^2 - 3v_1^2 \omega_1^2 \omega_2 + 9c_s^2 \omega_1 \omega_2^2 - 4v_1^2 \omega_2^2 - 3\omega_1 \omega_2^2 + 2\omega_1 \omega_2 + 2v_1^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 - 4\omega_1^2 + 12c_s^2 \omega_1^2 + 3v_1^2 \omega_1 \omega_2^2 + 2v_2^2 \omega_1^2 + 3\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 + 2v_2^2 \omega_2^2 - 6c_s^2 \omega_2^2 + 2v_1^2 \omega_1 \omega_2) \frac{v_2 v_1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y^2 v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 v_1}^{(2), \text{SRT}} = (12 + 3\omega^2 - 12\omega - 11c_s^2 \omega^2 - 3v_2^2 \omega^2 + 12v_2^2 \omega + 36c_s^2 \omega - 36c_s^2 - 12v_2^2) \frac{v_2 \rho}{12\omega^2}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{MRT}^1} = (6v_2^2 \omega_{10}^2 \omega_5 \omega_{15} - 24c_s^2 \omega_{10}^2 \omega_{15} + 12\omega_{10} \omega_5^2 - 12c_s^2 \omega_{10} \omega_5^2 - 6v_2^2 \omega_{10} \omega_5^2 \omega_{15} - 11c_s^2 \omega_{10}^2 \omega_5^2 \omega_{15} - 12v_2^2 \omega_{10} \omega_5^2 - 24c_s^2 \omega_{10} \omega_5 \omega_{15} + 3\omega_{10}^2 \omega_5^2 \omega_{15} + 12v_2^2 \omega_{10}^2 \omega_5^2 - 6\omega_{10}^2 \omega_5 \omega_{15} + 12v_2^2 \omega_5^2 \omega_{15} - 18c_s^2 \omega_{10} \omega_5^2 \omega_{15} - 12c_s^2 \omega_{10}^2 \omega_5 + 12\omega_{10}^2 \omega_5 + 42c_s^2 \omega_{10}^2 \omega_5 \omega_{15} + 6\omega_{10} \omega_5^2 \omega_{15} - 12\omega_{10}^2 \omega_5^2 + 36c_s^2 \omega_5^2 \omega_{15} + 12c_s^2 \omega_{10}^2 \omega_5^2 - 12\omega_5^2 \omega_{15} - 3v_2^2 \omega_{10}^2 \omega_5^2 \omega_{15} - 12v_2^2 \omega_{10}^2 \omega_5) \frac{v_2 \rho}{12\omega_{10}^2 \omega_5^2 \omega_{15}}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{MRT}^2} = C_{D_x D_y^2 v_1}^{(2), \text{MRT}^1}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CLBM}^1} =$$

$$(12\omega_{10}^2 - 6\omega_{10}^2 \omega_{15} - 12v_2^2 \omega_{10} \omega_5 - 3v_2^2 \omega_{10}^2 \omega_5 \omega_{15} + 18c_s^2 \omega_{10}^2 \omega_{15} + 36c_s^2 \omega_5 \omega_{15} - 12\omega_5 \omega_{15} - 36c_s^2 \omega_{10} \omega_5 + 6v_2^2 \omega_{10}^2 \omega_{15} + 6\omega_{10} \omega_5 \omega_{15} + 12\omega_{10} \omega_5 + 12v_2^2 \omega_5 \omega_{15} - 18c_s^2 \omega_{10} \omega_5 \omega_{15} + 3\omega_{10}^2 \omega_5 \omega_{15} + 36c_s^2 \omega_{10}^2 \omega_5 - 12\omega_{10}^2 \omega_5 - 11c_s^2 \omega_{10}^2 \omega_5 \omega_{15} - 12v_2^2 \omega_{10}^2 - 6v_2^2 \omega_{10} \omega_5 \omega_{15} - 36c_s^2 \omega_{10}^2 + 12v_2^2 \omega_{10}^2 \omega_5) \frac{v_2 \rho}{12\omega_{10}^2 \omega_5 \omega_{15}}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CLBM}^2} = C_{D_x D_y^2 v_1}^{(2), \text{CLBM}^1}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CuLBM}^1} = (3\omega_7 \omega_1 \omega_5^2 - 36c_s^2 \omega_5^2 - 12v_2^2 \omega_5^2 - 11c_s^2 \omega_7 \omega_1 \omega_5^2 + 6v_2^2 \omega_7 \omega_5^2 - 18c_s^2 \omega_7 \omega_1 \omega_5 + 6\omega_7 \omega_1 \omega_5 + 18c_s^2 \omega_7 \omega_5^2 - 6\omega_7 \omega_5^2 + 12v_2^2 \omega_1 \omega_5^2 + 36c_s^2 \omega_7 \omega_1 - 12\omega_7 \omega_1 - 3v_2^2 \omega_7 \omega_1 \omega_5^2 - 36c_s^2 \omega_1 \omega_5 + 12\omega_1 \omega_5 - 12\omega_1 \omega_5^2 + 36c_s^2 \omega_1 \omega_5^2 + 12v_2^2 \omega_7 \omega_1 - 6v_2^2 \omega_7 \omega_1 \omega_5 + 12\omega_5^2 - 12v_2^2 \omega_1 \omega_5) \frac{v_2 \rho}{12\omega_7 \omega_1 \omega_5^2}$$

$$C_{D_x D_y^2 v_1}^{(2), \text{CuLBM}^2} = (2\omega_3 v_2^2 \omega_4 \omega_1 \omega_2^2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 v_2^2 \omega_1 \omega_2^2 + 4\omega_3 v_2^2 \omega_4 \omega_1^2 + 6v_2^2 \omega_4 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_2^2 - 12\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 - 11\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_1^2 - 36\omega_3 c_s^2 \omega_1 \omega_2^2 - 24c_s^2 \omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 - 4v_2^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 v_2^2 \omega_4 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 18\omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_4 \omega_1 \omega_2^2 + 12\omega_3 \omega_1 \omega_2^2 -$$

$$24\omega_3 v_1^2 \omega_4 \omega_2^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 2\omega_3 v_2^2 \omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1^2 - 6\omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 v_1^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12c_s^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 v_2^2 \omega_1^2 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 v_1^2 \omega_4 \omega_1^2 - 3\omega_3 v_2^2 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 + 18\omega_3 v_1^2 \omega_4 \omega_1 \omega_2^2 - 8v_2^2 \omega_4 \omega_1 \omega_2^2) \frac{v_2 \rho}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y^2 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_2^2}$:

$$C_{D_x D_y^2 v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{MRT1}} = (\omega_{10}^2 - 3v_2^2 \omega_{10} \omega_5 + c_s^2 \omega_5 \omega_{15} - \omega_5 \omega_{15} - c_s^2 \omega_{10} \omega_5 + \omega_{10} \omega_5 \omega_{15} + \omega_{10} \omega_5 + 3v_2^2 \omega_5 \omega_{15} - c_s^2 \omega_{10} \omega_5 \omega_{15} + c_s^2 \omega_{10}^2 \omega_5 + 3v_2^2 \omega_{10} \omega_{15} - \omega_{10}^2 \omega_5 - 3v_2^2 \omega_{10}^2 - 3v_2^2 \omega_{10} \omega_5 \omega_{15} - \omega_{10} \omega_{15} - c_s^2 \omega_{10}^2 + 3v_2^2 \omega_{10}^2 \omega_5 + c_s^2 \omega_{10} \omega_{15}) \frac{v_1 \rho}{\omega_{10}^2 \omega_5 \omega_{15}}$$

$$C_{D_x D_y^2 v_2}^{(2), \text{MRT2}} = C_{D_x D_y^2 v_2}^{(2), \text{MRT1}}$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 v_2}^{(2), \text{CuLBM2}} = (\omega_3 \omega_1^2 \omega_2 + 6\omega_3 v_2^2 \omega_1^2 - 2v_1^2 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 + 3\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_2^2 - \omega_3 v_1^2 \omega_1^2 \omega_2 + 6\omega_3 v_2^2 \omega_2^2 - 12\omega_3 v_2^2 \omega_1 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 2v_1^2 \omega_1 \omega_2^2 - 2\omega_3 v_1^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 6c_s^2 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_1^2 + 2\omega_3 v_1^2 \omega_1^2 + \omega_3 v_1^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2) \frac{v_1 \rho}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^3 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^3}$:

$$C_{D_y^3 \rho}^{(2), \text{SRT}} = (144c_s^2 v_2^2 + 7v_2^4 \omega^2 + 36v_2^4 + c_s^4 \omega^2 + 12c_s^4 - 12c_s^4 \omega - 36v_2^4 \omega - c_s^2 \omega^2 + 24c_s^2 v_2^2 \omega^2 - 7v_2^2 \omega^2 + 36v_2^2 \omega - 144c_s^2 v_2^2 \omega + 12c_s^2 \omega - 12c_s^2 - 36v_2^2) \frac{1}{12\omega^2}$$

$$C_{D_y^3 \rho}^{(2), \text{MRT1}} = (144c_s^2 v_2^2 - 36v_2^4 \omega_{10} - 12c_s^4 \omega_{10} + 36v_2^4 + 12c_s^4 + c_s^4 \omega_{10}^2 + 7v_2^4 \omega_{10}^2 + 12c_s^2 \omega_{10} + 36v_2^2 \omega_{10} - 144c_s^2 v_2^2 \omega_{10} + 24c_s^2 v_2^2 \omega_{10}^2 - 7v_2^2 \omega_{10}^2 - 12c_s^2 - c_s^2 \omega_{10}^2 - 36v_2^2) \frac{1}{12\omega_{10}}$$

$$C_{D_y^3 \rho}^{(2), \text{MRT2}} = C_{D_y^3 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(2), \text{CLBM1}} = C_{D_y^3 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(2), \text{CLBM2}} = C_{D_y^3 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(2), \text{CuLBM1}} = (144c_s^2 v_2^2 - c_s^2 \omega_5^2 + 24c_s^2 v_2^2 \omega_5^2 + 36v_2^4 - 7v_2^2 \omega_5^2 + 12c_s^4 + 36v_2^2 \omega_5 - 144c_s^2 v_2^2 \omega_5 + 12c_s^2 \omega_5 + 7v_2^4 \omega_5^2 + c_s^4 \omega_5^2 - 12c_s^4 \omega_5 - 36v_2^4 \omega_5 - 12c_s^2 - 36v_2^2) \frac{1}{12\omega_5^2}$$

$$C_{D_y^3 \rho}^{(2), \text{CuLBM2}} = (4v_2^4 \omega_1^2 - 16v_2^2 \omega_1 \omega_2 + 4c_s^4 \omega_1^2 + 48c_s^2 v_2^2 \omega_1 \omega_2 + 8c_s^2 \omega_1 \omega_2^2 - 24v_2^4 \omega_1 \omega_2^2 + 8c_s^4 \omega_2^2 + 16v_2^4 \omega_1 \omega_2 - 96c_s^2 v_2^2 \omega_1 \omega_2^2 - 8c_s^4 \omega_1 \omega_2^2 + 16v_2^4 \omega_2^2 + 24v_2^2 \omega_1 \omega_2^2 - 4c_s^2 \omega_1^2 + c_s^4 \omega_1^2 \omega_2^2 - 7v_2^2 \omega_1^2 \omega_2^2 - 4v_2^2 \omega_1^2 - 12v_2^4 \omega_1^2 \omega_2 + 24c_s^2 v_2^2 \omega_1^2 \omega_2^2 + 4c_s^2 \omega_1^2 \omega_2 + 24c_s^2 v_2^2 \omega_1^2 - 48c_s^2 v_2^2 \omega_1^2 \omega_2 - c_s^2 \omega_1^2 \omega_2^2 - 16v_2^2 \omega_2^2 + 72c_s^2 v_2^2 \omega_2^2 + 7v_2^4 \omega_1^2 \omega_2^2 - 8c_s^2 \omega_2^2 + 12v_2^2 \omega_2^2 \omega_2 - 4c_s^4 \omega_1^2 \omega_2^2) \frac{1}{12\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^3 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^3}$:

$$C_{D_y^3 v_2}^{(2), \text{SRT}} = (-24 - 4\omega^2 + 24\omega + 5c_s^2 \omega^2 + 11v_2^2 \omega^2 - 60v_2^2 \omega - 36c_s^2 \omega + 36c_s^2 + 60v_2^2) \frac{v_2 \rho}{6\omega^2}$$

$$C_{D_y^3 v_2}^{(2), \text{MRT1}} = (-24 - 4\omega_{10}^2 + 24\omega_{10} - 36c_s^2 \omega_{10} - 60v_2^2 \omega_{10} + 11v_2^2 \omega_{10}^2 + 36c_s^2 + 5c_s^2 \omega_{10}^2 + 60v_2^2) \frac{v_2 \rho}{6\omega_{10}^2}$$

$$C_{D_y^3 v_2}^{(2), \text{MRT2}} = C_{D_y^3 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(2), \text{CLBM1}} = C_{D_y^3 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(2), \text{CLBM2}} = C_{D_y^3 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(2), \text{CuLBM1}} = (-24 + 5c_s^2 \omega_5^2 + 11v_2^2 \omega_5^2 - 60v_2^2 \omega_5 - 36c_s^2 \omega_5 + 24\omega_5 - 4\omega_5^2 + 36c_s^2 + 60v_2^2) \frac{v_2 \rho}{6\omega_5^2}$$

$$C_{D_y^3 v_2}^{(2), \text{CuLBM2}} = (24v_2^2 \omega_1 \omega_2 - 12\omega_2^2 - 24c_s^2 \omega_1 \omega_2^2 + 16\omega_1 \omega_2^2 - 8\omega_1 \omega_2 + 8c_s^2 \omega_1 \omega_2 - 4\omega_1^2 - 40v_2^2 \omega_1 \omega_2^2 + 8c_s^2 \omega_1^2 + 11v_2^2 \omega_1^2 \omega_2^2 + 8v_2^2 \omega_1^2 + 8\omega_1^2 \omega_2 - 12c_s^2 \omega_1^2 \omega_2 + 5c_s^2 \omega_1^2 \omega_2^2 + 28v_2^2 \omega_2^2 - 4\omega_1^2 \omega_2^2 + 20c_s^2 \omega_2^2 - 20v_2^2 \omega_1^2 \omega_2) \frac{v_2 \rho}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_z v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{MRT1}} = (\omega_7 \omega_5 + \omega_7 \omega_8 \omega_5 - \omega_7 \omega_8 - \omega_7 \omega_5^2 - \omega_8 \omega_5 + \omega_5^2) \frac{v_3 c_s^2 \rho}{\omega_7 \omega_8 \omega_5^2}$$

$$C_{D_x^2 D_z v_2}^{(2), \text{MRT2}} = C_{D_x^2 D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z v_2}^{(2), \text{CuLBM2}} = (-2\omega_3 - \omega_3 v_3^2 \omega_1 + 6\omega_3 c_s^2 - 3\omega_3 c_s^2 \omega_1 + 3c_s^2 \omega_4 \omega_1 - \omega_4 \omega_1 + 2\omega_4 + 2\omega_3 v_3^2 + v_3^2 \omega_4 \omega_1 + \omega_3 \omega_1 - 2v_3^2 \omega_4 - 6c_s^2 \omega_4) \frac{v_3 \rho}{4\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_x^2 D_z v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_3}^{(2), \text{SRT}} = \frac{-c_s^2 v_2 \rho}{6}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{MRT1}} = (6\omega_7 \omega_8 \omega_5 - 6\omega_7 \omega_8 - 6\omega_6 \omega_7 \omega_5 + 6\omega_6 \omega_5 + 6\omega_6 \omega_7 - \omega_6 \omega_7 \omega_8 \omega_5 - 6\omega_8 \omega_5) \frac{c_s^2 v_2 \rho}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{MRT2}} = C_{D_x^2 D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CLBM1}} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CLBM2}} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CuLBM1}} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(2), \text{CuLBM2}} = C_{D_x^2 D_z v_3}^{(2), \text{SRT}}$$

coefficient $C_{D_x D_y D_z \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{MRT1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{MRT2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(2), \text{CuLBM2}} = (-2\omega_2^2 + v_1^2 \omega_2^2 + 4\omega_1 \omega_2 + v_1^2 \omega_1^2 - 12c_s^2 \omega_1 \omega_2 - 2\omega_1^2 + 6c_s^2 \omega_1^2 + v_3^2 \omega_2^2 - 2v_3^2 \omega_1 \omega_2 + v_3^2 \omega_1^2 + 6c_s^2 \omega_2^2 - 2v_1^2 \omega_1 \omega_2) \frac{v_3 v_1}{3\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{MRT1}} = (\omega_7 \omega_5 + \omega_7 \omega_8 \omega_5 - \omega_7 \omega_8 - \omega_7 \omega_5^2 - \omega_8 \omega_5 + \omega_5^2) \frac{v_3 c_s^2 \rho}{\omega_7 \omega_8 \omega_5^2}$$

$$C_{D_x D_y D_z v_1}^{(2), \text{MRT2}} = C_{D_x D_y D_z v_1}^{(2), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(2), \text{CuLBM2}} = (-\omega_3 \omega_4 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 + \omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 3v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 - 2v_3^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 3\omega_3 v_3^2 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_4 \omega_2^2 + 2\omega_3 v_3^2 \omega_4 \omega_1^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 v_3^2 \omega_1 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 - 12\omega_3 v_1^2 \omega_4 \omega_1 \omega_2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - \omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 4v_3^2 \omega_4 \omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_4 \omega_2^2 + 6\omega_3 v_1^2 \omega_4 \omega_1^2 + 2\omega_4 \omega_1^2 \omega_2) \frac{v_3 \rho}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{MRT1}} = (\omega_7 \omega_5 + \omega_7 \omega_8 \omega_5 + \omega_7^2 - \omega_7 \omega_8 - \omega_8 \omega_5 - \omega_7^2 \omega_5) \frac{c_s^2 v_1 \rho}{\omega_7^2 \omega_8 \omega_5}$$

$$C_{D_x D_y D_z v_3}^{(2), \text{MRT2}} = C_{D_x D_y D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_3}^{(2), \text{CuLBM2}} = (-\omega_3 \omega_4 \omega_1 \omega_2^2 - 3\omega_3 v_1^2 \omega_1^2 \omega_2^2 - 4v_1^2 \omega_4 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 + 3\omega_3 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - \omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 - 2\omega_3 v_1^2 \omega_4 \omega_2^2 + 6\omega_3 v_3^2 \omega_4 \omega_1^2 - 2v_1^2 \omega_4 \omega_1^2 \omega_2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 v_3^2 \omega_4 \omega_2^2 + 2\omega_3 v_1^2 \omega_4 \omega_1^2 + 2\omega_4 \omega_1^2 \omega_2 + \omega_3 v_1^2 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_1 \omega_2^2 + 3v_1^2 \omega_4 \omega_1^2 \omega_2^2) \frac{v_1 \rho}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{MRT1}} = (\omega_{10}^2 - 3c_s^2 \omega_{16} \omega_{10} \omega_7 + \omega_{16} v_2^2 \omega_{10} + \omega_{16} \omega_{10} \omega_7 + \omega_{16} v_2^2 \omega_7 + v_2^2 \omega_{10}^2 \omega_7 + 3c_s^2 \omega_{16} \omega_{10} - \omega_{16} \omega_{10} + 3c_s^2 \omega_{10}^2 \omega_7 + 3c_s^2 \omega_{16} \omega_7 - \omega_{10}^2 \omega_7 - \omega_{16} \omega_7 - 3c_s^2 \omega_{10} \omega_7 + \omega_{10} \omega_7 - \omega_{16} v_2^2 \omega_{10} \omega_7 - v_2^2 \omega_{10} \omega_7 - v_2^2 \omega_{10}^2 - 3c_s^2 \omega_{10}^2) \frac{v_3 v_2}{\omega_{16} \omega_{10}^2 \omega_7}$$

$$C_{D_y^2 D_z \rho}^{(2), \text{MRT2}} = C_{D_y^2 D_z \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z \rho}^{(2), \text{CuLBM2}} = (-4v_2^2 \omega_1 \omega_2 + 2\omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 3\omega_1 \omega_2^2 + 2\omega_1 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 4\omega_1^2 - 3v_3^2 \omega_1^2 \omega_2 + 12c_s^2 \omega_1^2 - 4v_3^2 \omega_2^2 + 2v_3^2 \omega_1 \omega_2 + 2v_2^2 \omega_1^2 + 3\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 + 2v_2^2 \omega_2^2 + 2v_3^2 \omega_1^2 - 6c_s^2 \omega_2^2 + 3v_3^2 \omega_1 \omega_2^2) \frac{v_3 v_2}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{MRT1}} = (\omega_{10}^2 - c_s^2 \omega_{16} \omega_{10} \omega_7 + 3\omega_{16} v_2^2 \omega_{10} + \omega_{16} \omega_{10} \omega_7 + 3\omega_{16} v_2^2 \omega_7 + 3v_2^2 \omega_{10}^2 \omega_7 + c_s^2 \omega_{16} \omega_{10} - \omega_{16} \omega_{10} + c_s^2 \omega_{10}^2 \omega_7 + c_s^2 \omega_{16} \omega_7 - \omega_{10}^2 \omega_7 - \omega_{16} \omega_7 - c_s^2 \omega_{10} \omega_7 + \omega_{10} \omega_7 - 3\omega_{16} v_2^2 \omega_{10} \omega_7 - 3v_2^2 \omega_{10} \omega_7 - 3v_2^2 \omega_{10}^2 - c_s^2 \omega_{10}^2) \frac{v_3 \rho}{\omega_{16} \omega_{10}^2 \omega_7}$$

$$C_{D_y^2 D_z v_2}^{(2), \text{MRT2}} = C_{D_y^2 D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z v_2}^{(2), \text{CuLBM2}} = (-\omega_3 v_3^2 \omega_1^2 \omega_2 + \omega_3 \omega_1^2 \omega_2 + 6\omega_3 v_2^2 \omega_1^2 - 4\omega_3 c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 + 3\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_2^2 + 2\omega_3 v_3^2 \omega_1^2 + 6\omega_3 v_2^2 \omega_2^2 - 12\omega_3 v_2^2 \omega_1 \omega_2 - 2v_3^2 \omega_1^2 \omega_2 - \omega_3 \omega_1 \omega_2^2 + \omega_3 v_3^2 \omega_1 \omega_2^2 + 2\omega_1^2 \omega_2 - 6c_s^2 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_1^2 + 2v_3^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2) \frac{v_3 \rho}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z v_3}^{(2), \text{SRT}} = (12 + 3\omega^2 - 12\omega - 11c_s^2 \omega^2 - 3v_2^2 \omega^2 + 12v_2^2 \omega + 36c_s^2 \omega - 36c_s^2 - 12v_2^2) \frac{v_2 \rho}{12\omega^2}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{MRT1}} = (-12\omega_{10}^2 \omega_7^2 - 12\omega_{16} \omega_7^2 - 24c_s^2 \omega_{16} \omega_{10} \omega_7 + 12c_s^2 \omega_{10}^2 \omega_7^2 + 36c_s^2 \omega_{16} \omega_7^2 - 3\omega_{16} v_2^2 \omega_{10}^2 \omega_7^2 - 12v_2^2 \omega_{10}^2 \omega_7^2 - 24c_s^2 \omega_{16} \omega_{10}^2 + 12v_2^2 \omega_{10}^2 \omega_7^2 + 12\omega_{16} v_2^2 \omega_7^2 + 6\omega_{16} \omega_{10} \omega_7^2 + 6\omega_{16} v_2^2 \omega_{10} \omega_7 - 12c_s^2 \omega_{10}^2 \omega_7 + 12\omega_{10}^2 \omega_7 - 18c_s^2 \omega_{16} \omega_{10} \omega_7^2 - 11c_s^2 \omega_{16} \omega_{10}^2 \omega_7^2 - 12v_2^2 \omega_{10} \omega_7^2 + 3\omega_{16} \omega_{10}^2 \omega_7^2 - 6\omega_{16} \omega_{10}^2 \omega_7 - 6\omega_{16} v_2^2 \omega_{10} \omega_7^2 + 12\omega_{10} \omega_7^2 + 42c_s^2 \omega_{16} \omega_{10}^2 \omega_7 - 12c_s^2 \omega_{10} \omega_7^2) \frac{v_2 \rho}{12\omega_{16} \omega_{10}^2 \omega_7^2}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{MRT2}} = C_{D_y^2 D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CLBM1}} =$$

$$(12\omega_{10}^2 - 18c_s^2 \omega_{16} \omega_{10} \omega_7 - 6\omega_{16} \omega_{10}^2 + 6\omega_{16} \omega_{10} \omega_7 + 12\omega_{16} v_2^2 \omega_7 + 12v_2^2 \omega_{10}^2 \omega_7 + 18c_s^2 \omega_{16} \omega_{10}^2 - 3\omega_{16} v_2^2 \omega_{10}^2 \omega_7 + 36c_s^2 \omega_{10}^2 \omega_7 + 36c_s^2 \omega_{16} \omega_7 + 6\omega_{16} v_2^2 \omega_{10}^2 - 12\omega_{10}^2 \omega_7 - 12\omega_{16} \omega_7 - 36c_s^2 \omega_{10} \omega_7 + 12\omega_{10} \omega_7 - 6\omega_{16} v_2^2 \omega_{10} \omega_7 + 3\omega_{16} \omega_{10}^2 \omega_7 - 12v_2^2 \omega_{10} \omega_7 - 12v_2^2 \omega_{10}^2 - 11c_s^2 \omega_{16} \omega_{10}^2 \omega_7 - 36c_s^2 \omega_{10}^2) \frac{v_2 \rho}{12\omega_{16} \omega_{10}^2 \omega_7}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CLBM2}} = C_{D_y^2 D_z v_3}^{(2), \text{CLBM1}}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CuLBM1}} = (-11\omega_3 c_s^2 \omega_{11} \omega_5^2 - 36c_s^2 \omega_5^2 - 6\omega_3 v_2^2 \omega_{11} \omega_5 + 6v_2^2 \omega_{11} \omega_5^2 - 12v_2^2 \omega_5^2 + 12\omega_3 \omega_5 - 12\omega_3 \omega_5^2 - 3\omega_3 v_2^2 \omega_{11} \omega_5^2 - 6\omega_{11} \omega_5^2 - 12\omega_3 \omega_{11} - 18\omega_3 c_s^2 \omega_{11} \omega_5 + 18c_s^2 \omega_{11} \omega_5^2 + 12\omega_3 v_2^2 \omega_5^2 + 36\omega_3 c_s^2 \omega_{11} + 36\omega_3 c_s^2 \omega_5^2 + 6\omega_3 \omega_{11} \omega_5 + 12\omega_3 v_2^2 \omega_{11} + 3\omega_3 \omega_{11} \omega_5^2 - 36\omega_3 c_s^2 \omega_5 + 12\omega_5^2 - 12\omega_3 v_2^2 \omega_5) \frac{v_2 \rho}{12\omega_3 \omega_{11} \omega_5^2}$$

$$C_{D_y^2 D_z v_3}^{(2), \text{CuLBM2}} = (2\omega_3 v_2^2 \omega_4 \omega_1 \omega_2^2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 v_2^2 \omega_1 \omega_2^2 + 4\omega_3 v_2^2 \omega_4 \omega_1^2 + 6v_2^2 \omega_4 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_2^2 + 18\omega_3 v_2^2 \omega_4 \omega_1 \omega_2^2 - 12\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 - 11\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_1^2 - 36\omega_3 c_s^2 \omega_1 \omega_2^2 - 24c_s^2 \omega_4 \omega_1 \omega_2^2 + 12\omega_3 v_3^2 \omega_4 \omega_1 \omega_2 - 6\omega_3 \omega_1^2 \omega_2^2 - 4v_2^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 v_2^2 \omega_4 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2 + 8\omega_4 \omega_1 \omega_2^2 + 12\omega_3 \omega_1 \omega_2^2 + 12\omega_3 v_3^2 \omega_4 \omega_1^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 2\omega_3 v_2^2 \omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1^2 - 6\omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 18\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12c_s^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 v_2^2 \omega_1^2 \omega_2^2 - 24\omega_3 v_3^2 \omega_4 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 - 3\omega_3 v_2^2 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2 - 8v_2^2 \omega_4 \omega_1 \omega_2^2) \frac{v_2 \rho}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_1}^{(2)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_1}^{(2), \text{SRT}} = \frac{-c_s^2 v_2 \rho}{6}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{MRT}^1} = (6\omega_7\omega_8\omega_5 - 6\omega_7\omega_8 - 6\omega_6\omega_7\omega_5 + 6\omega_6\omega_5 + 6\omega_6\omega_7 - \omega_6\omega_7\omega_8\omega_5 - 6\omega_8\omega_5) \frac{c_s^2 v_2 \rho}{6\omega_6\omega_7\omega_8\omega_5}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{MRT}^2} = C_{D_x D_z^2 v_1}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CLBM}^1} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CLBM}^2} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CuLBM}^1} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

$$C_{D_x D_z^2 v_1}^{(2), \text{CuLBM}^2} = C_{D_x D_z^2 v_1}^{(2), \text{SRT}}$$

coefficient $C_{D_x D_z^2 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{MRT}^1} = (\omega_7\omega_5 + \omega_7\omega_8\omega_5 + \omega_7^2 - \omega_7\omega_8 - \omega_8\omega_5 - \omega_7^2\omega_5) \frac{c_s^2 v_1 \rho}{\omega_7^2 \omega_8 \omega_5}$$

$$C_{D_x D_z^2 v_2}^{(2), \text{MRT}^2} = C_{D_x D_z^2 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x D_z^2 v_2}^{(2), \text{CuLBM}^2} = (-2v_1^2\omega_4 - 2\omega_3 + 6\omega_3c_s^2 - 3\omega_3c_s^2\omega_1 + 3c_s^2\omega_4\omega_1 - \omega_4\omega_1 + 2\omega_4 - \omega_3v_1^2\omega_1 + 2\omega_3v_1^2 + \omega_3\omega_1 - 6c_s^2\omega_4 + v_1^2\omega_4\omega_1) \frac{v_1\rho}{4\omega_3\omega_4\omega_1}$$

coefficient $C_{D_y D_z^2 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 \rho}^{(2), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1} = (-12 - \omega_7^2 + 12\omega_7) \frac{c_s^4}{6\omega_7^2}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{MRT}^2} = C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CLBM}^1} = C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CLBM}^2} = C_{D_y D_z^2 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CuLBM}^1} = (-12 + 12\omega_3 - \omega_3^2) \frac{c_s^4}{6\omega_3^2}$$

$$C_{D_y D_z^2 \rho}^{(2), \text{CuLBM}^2} = (-15v_3^2c_s^2\omega_1^2\omega_2 + 2c_s^4\omega_1^2 - 4v_3^4\omega_2^2 - 2c_s^2\omega_1\omega_2^2 - 18v_3^2c_s^2\omega_2^2 - 3v_3^4\omega_1^2\omega_2 + 2v_3^4\omega_1^2 - 14c_s^4\omega_2^2 + 12v_3^2c_s^2\omega_1^2 + 14c_s^4\omega_1\omega_2^2 + 3v_3^2\omega_1^2\omega_2 - 2c_s^2\omega_1^2 + 4v_3^2\omega_2^2 + 15v_3^2c_s^2\omega_1\omega_2^2 - c_s^4\omega_1^2\omega_2^2 - 2v_3^2\omega_1\omega_2 + 3v_3^4\omega_1\omega_2^2 + 2c_s^2\omega_1^2\omega_2 + 2v_3^4\omega_1\omega_2 - 2v_3^2\omega_1^2 + 2c_s^2\omega_2^2 - 3v_3^2\omega_1\omega_2^2 + 6v_3^2c_s^2\omega_1\omega_2 - 2c_s^4\omega_1^2\omega_2) \frac{1}{6\omega_1^2\omega_2^2}$$

coefficient $C_{D_y D_z^2 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_2}^{(2), \text{SRT}} = \frac{-c_s^2 v_2 \rho}{6}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{MRT}^1} = (12\omega_{16}\omega_{10}\omega_7 + 12\omega_7^2 - 12\omega_{16}\omega_{10} - \omega_{16}\omega_{10}\omega_7^2 - 12\omega_{16}\omega_7 + 12\omega_{10}\omega_7 - 12\omega_{10}\omega_7^2) \frac{c_s^2 v_2 \rho}{6\omega_{16}\omega_{10}\omega_7^2}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{MRT}^2} = C_{D_y D_z^2 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CLBM}^1} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CLBM}^2} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CuLBM}^1} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

$$C_{D_y D_z^2 v_2}^{(2), \text{CuLBM}^2} = C_{D_y D_z^2 v_2}^{(2), \text{SRT}}$$

coefficient $C_{D_y D_z^2 v_3}^{(2)}$ **at** $\frac{\partial^3 v_3}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{MRT}^1} = (\omega_{19} \omega_7 - 2\omega_{19} - \omega_7^2 + 2\omega_7) \frac{v_3 c_s^2 \rho}{\omega_{19} \omega_7^2}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{MRT}^2} = C_{D_y D_z^2 v_3}^{(2), \text{MRT}^1}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CuLBM}^2} = (6\omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 5\omega_1 \omega_2^2 - 2\omega_1 \omega_2 + 2c_s^2 \omega_1 \omega_2 - 4\omega_1^2 - 11v_3^2 \omega_1^2 \omega_2 + 8c_s^2 \omega_1^2 - 14v_3^2 \omega_2^2 + 6v_3^2 \omega_1 \omega_2 + 5\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 + 8v_3^2 \omega_1^2 - 10c_s^2 \omega_2^2 + 11v_3^2 \omega_1 \omega_2^2) \frac{v_3 \rho}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_z^3 \rho}^{(2)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{D_z^3 \rho}^{(2), \text{SRT}} = (-1 + v_3^2 + 3c_s^2) \frac{v_3 v_2}{12}$$

$$C_{D_z^3 \rho}^{(2), \text{MRT}^1} = (6\omega_{19} \omega_7 - \omega_{19} \omega_7 \omega_{11} + \omega_{19} v_3^2 \omega_7 \omega_{11} - 36c_s^2 \omega_{11} - 12\omega_{19} - 6\omega_7 \omega_{11} - 12v_3^2 \omega_{11} + 18c_s^2 \omega_7 \omega_{11} + 12\omega_{19} v_3^2 - 6\omega_{19} v_3^2 \omega_7 + 6v_3^2 \omega_7 \omega_{11} + 12\omega_{11} + 36\omega_{19} c_s^2 + 3\omega_{19} c_s^2 \omega_7 \omega_{11} - 18\omega_{19} c_s^2 \omega_7) \frac{v_3 v_2}{12\omega_{19} \omega_7 \omega_{11}}$$

$$C_{D_z^3 \rho}^{(2), \text{MRT}^2} = C_{D_z^3 \rho}^{(2), \text{MRT}^1}$$

$$C_{D_z^3 \rho}^{(2), \text{CLBM}^1} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(2), \text{CLBM}^2} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(2), \text{CuLBM}^1} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

$$C_{D_z^3 \rho}^{(2), \text{CuLBM}^2} = C_{D_z^3 \rho}^{(2), \text{SRT}}$$

coefficient $C_{D_z^3 v_2}^{(2)}$ **at** $\frac{\partial^3 v_2}{\partial x_3^3}$:

$$C_{D_z^3 v_2}^{(2), \text{SRT}} = (6 + \omega^2 - 6\omega + 6v_3^2 \omega - 3c_s^2 \omega^2 - 6v_3^2 + 18c_s^2 \omega - 18c_s^2 - v_3^2 \omega^2) \frac{v_3 \rho}{6\omega^2}$$

$$C_{D_z^3 v_2}^{(2), \text{MRT}^1} = (-3\omega_{19} \omega_7 - 3\omega_7^2 + 6\omega_7 + \omega_{19} \omega_7^2 + 3\omega_{19} v_3^2 \omega_7 - 3\omega_{19} c_s^2 \omega_7^2 - 6c_s^2 \omega_7 - 12\omega_{19} c_s^2 + 3v_3^2 \omega_7^2 - 6v_3^2 \omega_7 + 3c_s^2 \omega_7^2 + 15\omega_{19} c_s^2 \omega_7 - \omega_{19} v_3^2 \omega_7^2) \frac{v_3 \rho}{6\omega_{19} \omega_7^2}$$

$$C_{D_z^3 v_2}^{(2), \text{MRT}^2} = C_{D_z^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_z^3 v_2}^{(2), \text{CLBM1}} = (6 + \omega_{19}\omega_7 - 3\omega_{19} - 3\omega_7 + 3\omega_{19}v_3^2 - \omega_{19}v_3^2\omega_7 + 9c_s^2\omega_7 + 9\omega_{19}c_s^2 + 3v_3^2\omega_7 - 6v_3^2 - 3\omega_{19}c_s^2\omega_7 - 18c_s^2) \frac{v_3\rho}{6\omega_{19}\omega_7}$$

$$C_{D_z^3 v_2}^{(2), \text{CLBM2}} = C_{D_z^3 v_2}^{(2), \text{CLBM1}}$$

$$C_{D_z^3 v_2}^{(2), \text{CuLBM1}} = (6 - 3\omega_3 - 3\omega_3c_s^2\omega_{10} - 3\omega_{10} + 9\omega_3c_s^2 - \omega_3v_3^2\omega_{10} + 3\omega_3v_3^2 + 9c_s^2\omega_{10} + \omega_3\omega_{10} - 6v_3^2 + 3v_3^2\omega_{10} - 18c_s^2) \frac{v_3\rho}{6\omega_3\omega_{10}}$$

$$C_{D_z^3 v_2}^{(2), \text{CuLBM2}} = (6\omega_3v_3^2\omega_4 + 6\omega_3 + 3\omega_3v_3^2\omega_1 - 6\omega_3c_s^2\omega_4\omega_1 - 18\omega_3c_s^2 + 9\omega_3c_s^2\omega_1 + 9c_s^2\omega_4\omega_1 - 3\omega_4\omega_1 + 6\omega_4 + 18\omega_3c_s^2\omega_4 - 6\omega_3v_3^2 + 3v_3^2\omega_4\omega_1 - 6\omega_3\omega_4 - 3\omega_3\omega_1 - 6v_3^2\omega_4 - 18c_s^2\omega_4 + 2\omega_3\omega_4\omega_1 - 2\omega_3v_3^2\omega_4\omega_1) \frac{v_3\rho}{12\omega_3\omega_4\omega_1}$$

$$\text{coefficient } C_{D_z^3 v_3}^{(2)} \text{ at } \frac{\partial^3 v_3}{\partial x_3^3}:$$

$$C_{D_z^3 v_3}^{(2), \text{SRT}} = (-1 + 3v_3^2 + c_s^2) \frac{v_2\rho}{12}$$

$$C_{D_z^3 v_3}^{(2), \text{MRT1}} = (6\omega_{19}\omega_7 - \omega_{19}\omega_7\omega_{11} + 3\omega_{19}v_3^2\omega_7\omega_{11} - 12c_s^2\omega_{11} - 12\omega_{19} - 6\omega_7\omega_{11} - 36v_3^2\omega_{11} + 6c_s^2\omega_7\omega_{11} + 36\omega_{19}v_3^2 - 18\omega_{19}v_3^2\omega_7 + 18v_3^2\omega_7\omega_{11} + 12\omega_{11} + 12\omega_{19}c_s^2 + \omega_{19}c_s^2\omega_7\omega_{11} - 6\omega_{19}c_s^2\omega_7) \frac{v_2\rho}{12\omega_{19}\omega_7\omega_{11}}$$

$$C_{D_z^3 v_3}^{(2), \text{MRT2}} = C_{D_z^3 v_3}^{(2), \text{MRT1}}$$

$$C_{D_z^3 v_3}^{(2), \text{CLBM1}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(2), \text{CLBM2}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(2), \text{CuLBM1}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$C_{D_z^3 v_3}^{(2), \text{CuLBM2}} = C_{D_z^3 v_3}^{(2), \text{SRT}}$$

$$\text{coefficient } C_{D_x^4 \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^4}:$$

$$C_{D_x^4 \rho}^{(2), \text{SRT}} = (-6v_1^2 - 12c_s^2v_1^2\omega + 3v_1^2\omega + 2c_s^4 - c_s^4\omega - 3v_1^4\omega + 6v_1^4 + c_s^2\omega - 2c_s^2 + 24c_s^2v_1^2) \frac{v_2}{24\omega}$$

$$C_{D_x^4 \rho}^{(2), \text{MRT1}} = (72c_s^2v_1^2\omega_5^2\omega_9^2 - 30v_1^4\omega_5^2\omega_9^2\omega_{12} - 48c_s^2\omega_5\omega_9^2\omega_{12} + 432c_s^2v_1^2\omega_5\omega_9^2\omega_{12} - 48c_s^4\omega_5\omega_9\omega_{12}^2 - 48v_1^4\omega_9^2\omega_{12} - 144c_s^2v_1^2\omega_5^2\omega_{12} - 36v_1^2\omega_5^2\omega_9\omega_{12}^2 + 24c_s^4\omega_9\omega_{12}^2 - 24c_s^4\omega_5\omega_9^2 - 48v_1^4\omega_5\omega_9\omega_{12} - 12v_1^2\omega_5^2\omega_9^2 + 36v_1^2\omega_5^2\omega_{12}^2 + 24c_s^4\omega_5\omega_{12}^2 + 72c_s^2v_1^2\omega_5^2\omega_9\omega_{12} - c_s^4\omega_5^2\omega_9^2\omega_{12}^2 - 96v_1^2\omega_5\omega_9^2\omega_{12} + 150c_s^2v_1^2\omega_5^2\omega_9\omega_{12}^2 - 12c_s^4\omega_5^2\omega_9^2\omega_{12} + 48v_1^2\omega_9^2\omega_{12} - 14c_s^2\omega_5^2\omega_9\omega_{12}^2 - 96v_1^4\omega_5\omega_9\omega_{12}^2 - 24c_s^2\omega_9\omega_{12}^2 + 12v_1^4\omega_5^2\omega_9 - 24v_1^2\omega_5^2\omega_9\omega_{12} + 24c_s^2\omega_5\omega_9^2 - 24c_s^2\omega_5\omega_{12}^2 - 3v_1^4\omega_5^2\omega_9^2\omega_{12}^2 - 36v_1^4\omega_5^2\omega_{12}^2 - 216c_s^2v_1^2\omega_9^2\omega_{12} + 48v_1^4\omega_9\omega_{12}^2 + 48c_s^4\omega_5\omega_9^2\omega_{12} - 432c_s^2v_1^2\omega_5\omega_9\omega_{12}^2 - 12c_s^2\omega_5^2\omega_9^2 + 30v_1^2\omega_5^2\omega_9^2\omega_{12} - 24v_1^4\omega_5\omega_9^2 + 36v_1^4\omega_5^2\omega_9\omega_{12}^2 + 72v_1^2\omega_5\omega_{12}^2 + 12c_s^2\omega_5^2\omega_{12}^2 + 48c_s^2\omega_5\omega_9\omega_{12}^2 + 48v_1^2\omega_5\omega_9\omega_{12} - 12c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12}^2 - 24c_s^4\omega_9^2\omega_{12} + c_s^2\omega_5^2\omega_9^2\omega_{12}^2 - 48v_1^2\omega_9\omega_{12}^2 + 12c_s^2\omega_5^2\omega_9^2\omega_{12} + 96v_1^4\omega_5\omega_9^2\omega_{12} + 24v_1^2\omega_5\omega_{12}^2 + 12c_s^4\omega_5^2\omega_9^2 - 12c_s^4\omega_5^2\omega_{12}^2 + 96v_1^2\omega_5\omega_9\omega_{12}^2 - 72v_1^2\omega_5\omega_{12}^2 + 14c_s^4\omega_5^2\omega_9\omega_{12}^2 - 126c_s^2v_1^2\omega_5^2\omega_9^2\omega_{12} + 24v_1^4\omega_5^2\omega_9\omega_{12} - 144c_s^2v_1^2\omega_5\omega_9^2 + 216c_s^2v_1^2\omega_9\omega_{12}^2 + 24c_s^2\omega_9^2\omega_{12} - 144c_s^2v_1^2\omega_5\omega_9\omega_{12} + 3v_1^2\omega_5^2\omega_9^2\omega_{12}^2 + 288c_s^2v_1^2\omega_5\omega_{12}^2) \frac{v_2}{24\omega_5^2\omega_9^2\omega_{12}^2}$$

$$C_{D_x^4 \rho}^{(2), \text{MRT2}} = C_{D_x^4 \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^4 \rho}^{(2), \text{CLBM1}} = (-6v_1^2 - 12c_s^2v_1^2\omega_9 + 3v_1^2\omega_9 + 2c_s^4 - c_s^4\omega_9 - 3v_1^4\omega_9 + 6v_1^4 + c_s^2\omega_9 - 2c_s^2 + 24c_s^2v_1^2) \frac{v_2}{24\omega_9}$$

$$C_{D_x^4 \rho}^{(2), \text{CLBM2}} = C_{D_x^4 \rho}^{(2), \text{CLBM1}}$$

$$C_{D_x^4 \rho}^{(2), \text{CuLBM1}} = (-6v_1^2 - 12c_s^2v_1^2\omega_4 + 3v_1^2\omega_4 + 2c_s^4 - c_s^4\omega_4 - 3v_1^4\omega_4 + c_s^2\omega_4 + 6v_1^4 - 2c_s^2 + 24c_s^2v_1^2) \frac{v_2}{24\omega_4}$$

$$C_{D_x^4 \rho}^{(2), \text{CuLBM2}} = (-3c_s^4\omega_1\omega_2 - 6v_1^2\omega_1 + 4c_s^4\omega_2 + 24c_s^2v_1^2\omega_1 - 12v_1^2\omega_2 + 48c_s^2v_1^2\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 6v_1^4\omega_1 - 4c_s^2\omega_2 - 9v_1^4\omega_1\omega_2 - 36c_s^2v_1^2\omega_1\omega_2 + 12v_1^4\omega_2 - 2c_s^2\omega_1 + 9v_1^2\omega_1\omega_2) \frac{v_2}{72\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^4 v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^4}:$$

$$C_{D_x^4 v_1}^{(2), \text{SRT}} = (-4 + 10v_1^2 - 5v_1^2\omega + 2\omega - 3c_s^2\omega + 6c_s^2) \frac{v_2v_1\rho}{12\omega}$$

$$C_{D_x^4 v_1}^{(2), \text{MRT1}} = (-12\omega_5^2\omega_9\omega_{12} + 120c_s^2\omega_5\omega_9^2\omega_{12} + 61v_1^2\omega_5^2\omega_9\omega_{12}^2 + 12c_s^2\omega_5^2\omega_9\omega_{12} - 72\omega_5\omega_9^2\omega_{12} + 24v_1^2\omega_5^2\omega_9^2 - 60v_1^2\omega_5^2\omega_{12}^2 + 168v_1^2\omega_5\omega_9^2\omega_{12} - 84v_1^2\omega_9^2\omega_{12} + 39c_s^2\omega_5^2\omega_9\omega_{12}^2 + 60c_s^2\omega_9\omega_{12}^2 - 48\omega_5\omega_{12}^2 + 36v_1^2\omega_5^2\omega_9\omega_{12} - 48c_s^2\omega_5\omega_9^2 + 72c_s^2\omega_5\omega_{12}^2 - 36\omega_9\omega_{12}^2 + 24\omega_5\omega_9^2 - 25\omega_5^2\omega_9\omega_{12}^2 + 24\omega_5^2\omega_{12}^2 + 24c_s^2\omega_5^2\omega_9^2 - 51v_1^2\omega_5^2\omega_9^2\omega_{12} - 36c_s^2\omega_5^2\omega_{12}^2 - 12\omega_5^2\omega_9^2 + 2\omega_5^2\omega_9^2\omega_{12}^2 - 120c_s^2\omega_5\omega_9\omega_{12}^2 - 72v_1^2\omega_5\omega_9\omega_{12} - 3c_s^2\omega_5^2\omega_9^2\omega_{12}^2 + 72\omega_5\omega_9\omega_{12}^2 + 24\omega_5\omega_9\omega_{12} + 84v_1^2\omega_9\omega_{12}^2 - 33c_s^2\omega_5^2\omega_9^2\omega_{12} - 48v_1^2\omega_5\omega_9^2 - 168v_1^2\omega_5\omega_9\omega_{12}^2 + 120v_1^2\omega_5\omega_{12}^2 + 36\omega_9^2\omega_{12} - 24c_s^2\omega_5\omega_9\omega_{12} + 21\omega_5^2\omega_9^2\omega_{12} - 60c_s^2\omega_9^2\omega_{12} - 5v_1^2\omega_5^2\omega_9^2\omega_{12}^2) \frac{v_2 v_1 \rho}{12\omega_5^2\omega_9^2\omega_{12}^2}$$

$$C_{D_x^4 v_1}^{(2), \text{MRT2}} = C_{D_x^4 v_1}^{(2), \text{MRT1}}$$

$$C_{D_x^4 v_1}^{(2), \text{CLBM1}} = (-4 + 10v_1^2 - 5v_1^2\omega_9 - 3c_s^2\omega_9 + 6c_s^2 + 2\omega_9) \frac{v_2 v_1 \rho}{12\omega_9}$$

$$C_{D_x^4 v_1}^{(2), \text{CLBM2}} = C_{D_x^4 v_1}^{(2), \text{CLBM1}}$$

$$C_{D_x^4 v_1}^{(2), \text{CuLBM1}} = (-4 + 10v_1^2 - 5v_1^2\omega_4 + 2\omega_4 - 3c_s^2\omega_4 + 6c_s^2) \frac{v_2 v_1 \rho}{12\omega_4}$$

$$C_{D_x^4 v_1}^{(2), \text{CuLBM2}} = (10v_1^2\omega_1 + 20v_1^2\omega_2 + 6\omega_1\omega_2 - 9c_s^2\omega_1\omega_2 - 4\omega_1 + 12c_s^2\omega_2 - 8\omega_2 + 6c_s^2\omega_1 - 15v_1^2\omega_1\omega_2) \frac{v_2 v_1 \rho}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^4 v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_1^4} :$$

$$C_{D_x^4 v_2}^{(2), \text{SRT}} = (72v_1^2 - 3c_s^4\omega^3 + 216c_s^2v_1^2\omega + 30c_s^4\omega^2 - 108v_1^2\omega + 48c_s^4 + 42v_1^2\omega^2 - 72c_s^4\omega - 84c_s^2v_1^2\omega^2 - 3v_1^2\omega^3 + 6c_s^2v_1^2\omega^3 + 108v_1^4\omega - 14c_s^2\omega^2 + c_s^2\omega^3 + 3v_1^4\omega^3 - 72v_1^4 + 36c_s^2\omega - 42v_1^4\omega^2 - 24c_s^2 - 144c_s^2v_1^2) \frac{\rho}{24\omega^3}$$

$$C_{D_x^4 v_2}^{(2), \text{MRT1}} = (-24c_s^2\omega_5\omega_{12} + 72v_1^4\omega_5^2\omega_{12} + 18v_1^2\omega_5^3\omega_{12} - 72c_s^2v_1^2\omega_5^2\omega_{12}^2 + 24c_s^4\omega_{12}^2 + 3v_1^4\omega_5^3\omega_{12}^2 + 24v_1^2\omega_5^2\omega_{12}^2 - 12c_s^2v_1^2\omega_5^3\omega_{12} - 48c_s^4\omega_5\omega_{12}^2 - 72v_1^2\omega_5^2\omega_{12} + 6c_s^2v_1^2\omega_5^3\omega_{12}^2 + 24c_s^4\omega_5\omega_{12} + 12v_1^4\omega_5^3 - 96c_s^2v_1^2\omega_{12}^2 - 18v_1^4\omega_5^3\omega_{12} - 24v_1^4\omega_5^2 - 3v_1^2\omega_5^3\omega_{12}^2 + 48c_s^2v_1^2\omega_5^2\omega_{12} + 12c_s^2\omega_5\omega_{12}^2 - 24v_1^4\omega_5^2\omega_{12}^2 - 3c_s^4\omega_5^3\omega_{12}^2 - 24c_s^2v_1^2\omega_5\omega_{12} + 24v_1^4\omega_5\omega_{12}^2 - 8c_s^2\omega_5^2\omega_{12}^2 - 24c_s^4\omega_5^2\omega_{12} + 48v_1^2\omega_5\omega_{12} - 6c_s^2\omega_5^3\omega_{12} + 24v_1^2\omega_5^2 + c_s^2\omega_5^3\omega_{12}^2 + 24c_s^4\omega_5^2\omega_{12}^2 - 24v_1^2\omega_5\omega_{12}^2 - 24c_s^2v_1^2\omega_5^2 - 48v_1^4\omega_5\omega_{12} + 24c_s^2\omega_5^2\omega_{12} - 12v_1^2\omega_5^3 + 12c_s^2v_1^2\omega_5^3 + 6c_s^4\omega_5^3\omega_{12} + 156c_s^2v_1^2\omega_5\omega_{12}^2) \frac{\rho}{24\omega_5^2\omega_{12}^2}$$

$$C_{D_x^4 v_2}^{(2), \text{MRT2}} = C_{D_x^4 v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^4 v_2}^{(2), \text{CLBM1}} = (-24c_s^2\omega_5\omega_{12} + 72v_1^4\omega_5^2\omega_{12} + 30v_1^2\omega_5^3\omega_{12} - 12c_s^2v_1^2\omega_5^2\omega_{12}^2 + 24c_s^4\omega_{12}^2 + 3v_1^4\omega_5^3\omega_{12}^2 + 12v_1^2\omega_5^2\omega_{12}^2 - 72c_s^2v_1^2\omega_5^3\omega_{12} - 48c_s^4\omega_5\omega_{12}^2 - 72v_1^2\omega_5^2\omega_{12} + 6c_s^2v_1^2\omega_5^3\omega_{12}^2 + 24c_s^4\omega_5\omega_{12} + 36v_1^4\omega_5^3 - 30v_1^4\omega_5^3\omega_{12} - 72v_1^4\omega_5^2 - 3v_1^2\omega_5^3\omega_{12}^2 + 144c_s^2v_1^2\omega_5^2\omega_{12} + 12c_s^2\omega_5\omega_{12}^2 - 12v_1^4\omega_5^2\omega_{12}^2 - 3c_s^4\omega_5^3\omega_{12}^2 + 72c_s^2v_1^2\omega_5\omega_{12} - 8c_s^2\omega_5^2\omega_{12}^2 - 24c_s^4\omega_5^2\omega_{12} - 6c_s^2\omega_5^3\omega_{12} + 72v_1^2\omega_5^2 + c_s^2\omega_5^3\omega_{12}^2 + 24c_s^4\omega_5^2\omega_{12}^2 - 216c_s^2v_1^2\omega_5^2 + 24c_s^2\omega_5^2\omega_{12} - 36v_1^2\omega_5^3 + 108c_s^2v_1^2\omega_5^2 + 6c_s^4\omega_5^3\omega_{12} - 36c_s^2v_1^2\omega_5\omega_{12}^2) \frac{\rho}{24\omega_5^2\omega_{12}^2}$$

$$C_{D_x^4 v_2}^{(2), \text{CLBM2}} = C_{D_x^4 v_2}^{(2), \text{CLBM1}}$$

$$C_{D_x^4 v_2}^{(2), \text{CuLBM1}} = (3v_1^4\omega_1^3\omega_9^2 + 12v_1^2\omega_1^2\omega_9^2 - 72c_s^2v_1^2\omega_1^3\omega_9 - 48c_s^4\omega_1\omega_9^2 - 24c_s^2\omega_1\omega_9 + 72v_1^4\omega_1^2\omega_9 + 30v_1^2\omega_1^3\omega_9 + 24c_s^4\omega_9^2 - 12c_s^2v_1^2\omega_1^2\omega_9^2 - 3v_1^2\omega_1^3\omega_9^2 + 144c_s^2v_1^2\omega_1^2\omega_9 - 216c_s^2v_1^2\omega_1^2 + 72v_1^2\omega_1^2 + 12c_s^2\omega_1\omega_9^2 - 12v_1^4\omega_1^2\omega_9^2 + 108c_s^2v_1^2\omega_1^3 - 72v_1^2\omega_1^2\omega_9 + 6c_s^2v_1^2\omega_1^3\omega_9^2 + 24c_s^4\omega_1\omega_9 - 30v_1^4\omega_1^3\omega_9 - 36v_1^2\omega_1^3 - 24c_s^4\omega_1^2\omega_9 - 6c_s^2\omega_1^3\omega_9 - 3c_s^4\omega_1^3\omega_9^2 + 72c_s^2v_1^2\omega_1\omega_9 - 8c_s^2\omega_1^2\omega_9^2 + 24c_s^2\omega_1\omega_9 + 6c_s^4\omega_1^3\omega_9 - 36c_s^2v_1^2\omega_1\omega_9^2 + 36v_1^4\omega_1^3 + c_s^2\omega_1^3\omega_9^2 - 72v_1^4\omega_1^2 + 24c_s^4\omega_1^2\omega_9^2) \frac{\rho}{24\omega_1^3\omega_9^2}$$

$$C_{D_x^4 v_2}^{(2), \text{CuLBM2}} = (36\omega_3^2c_s^2v_1^2\omega_4\omega_1 - 36\omega_3v_1^2\omega_4^2\omega_1^2 - 9\omega_3^2v_1^2\omega_1^3 - 48\omega_3^2c_s^4\omega_4^2\omega_1 - 15\omega_3^2v_1^4\omega_4\omega_1^3 + 9v_1^4\omega_4^2\omega_1^3 + \omega_3^2c_s^2\omega_4^2\omega_1^3 + 18\omega_3^2v_1^2\omega_1^2 + 15\omega_3v_1^2\omega_4^2\omega_1^3 - 8\omega_3^2c_s^2\omega_1^2\omega_1^2 - 18v_1^4\omega_4^2\omega_1^2 + 36\omega_3v_1^4\omega_4\omega_1^2 + 36\omega_3v_1^4\omega_4^2\omega_1^2 - 108\omega_3c_s^2v_1^2\omega_4\omega_1^2 + 12\omega_3^2c_s^2\omega_4^2\omega_1 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 - 9v_1^2\omega_4^2\omega_1^3 - 54c_s^2v_1^2\omega_4^2\omega_1^2 + 15\omega_3^2v_1^2\omega_4\omega_1^3 - 36\omega_3^2c_s^2v_1^2\omega_4\omega_1^3 + 24\omega_3^2c_s^4\omega_4^2 + 54\omega_3c_s^2v_1^2\omega_4\omega_1^3 - 15\omega_3v_1^4\omega_4^2\omega_1^3 + 72\omega_3^2c_s^2v_1^2\omega_4\omega_1^2 + 27c_s^2v_1^2\omega_4^2\omega_1^3 - 36\omega_3^2v_1^2\omega_4\omega_1^2 + 18v_1^2\omega_4^2\omega_1^2 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 - 18\omega_3^2v_1^4\omega_1^2 + 27\omega_3^2c_s^2v_1^2\omega_1^3 - 36\omega_3c_s^2v_1^2\omega_4^2\omega_1^3 + 18\omega_3v_1^4\omega_4\omega_1^3 - 3\omega_3c_s^2\omega_4^2\omega_1^3 - 12\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^2 + 12\omega_3c_s^4\omega_4^2\omega_1 - 12\omega_3^2c_s^4\omega_4\omega_1^2 + 12\omega_3^2v_1^2\omega_4^2\omega_1^2 + 12\omega_3c_s^2\omega_4^2\omega_1^2 - 54\omega_3^2c_s^2v_1^2\omega_1^2 - 36\omega_3v_1^4\omega_4\omega_1^2 + 72\omega_3c_s^2v_1^2\omega_4^2\omega_1^2 - 12\omega_3^2c_s^2\omega_4\omega_1 + 9\omega_3^2v_1^4\omega_1^3 - 3\omega_3^2v_1^2\omega_4^2\omega_1^3 + 3\omega_3^2c_s^4\omega_4\omega_1^3 + 6\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^3 + 3\omega_3c_s^4\omega_4^2\omega_1^3 - 18\omega_3v_1^2\omega_4\omega_1^3 - 12\omega_3c_s^2\omega_4^2\omega_1 + 36\omega_3c_s^2v_1^2\omega_4^2\omega_1 - 12\omega_3^2v_1^4\omega_4^2\omega_1^2 + 12\omega_3^2c_s^2\omega_4\omega_1^2 + 36\omega_3v_1^2\omega_4\omega_1^2 - 12\omega_3c_s^4\omega_4^2\omega_1^2 - 36\omega_3^2c_s^2v_1^2\omega_4^2\omega_1 + 12\omega_3^2c_s^4\omega_4\omega_1 - 3\omega_3^2c_s^2\omega_4\omega_1^3 + 3\omega_3^2v_1^4\omega_4^2\omega_1^3) \frac{\rho}{24\omega_3^2\omega_4^2\omega_1^3}$$

$$\text{coefficient } C_{D_x^3 D_y \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^3 \partial x_2} :$$

$$C_{D_x^3 D_y \rho}^{(2), \text{SRT}} = (24 - 24v_1^2 + 36v_1^2\omega - 14v_1^2\omega^2 - \omega^3 + 14\omega^2 + v_1^2\omega^3 - 36\omega - 42c_s^2\omega^2 + 3c_s^2\omega^3 + 108c_s^2\omega - 72c_s^2) \frac{c_s^2 v_1}{12\omega^3}$$

$$C_{D_x^3 D_y \rho}^{(2), \text{MRT1}} = (-12v_2^2v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9^2 - 12c_s^2\omega_5^2\omega_9^2\omega_{12}^2 + 12c_s^2\omega_5^3\omega_{21}\omega_9\omega_{12}^2 - 45c_s^2v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_9^2\omega_{12} + 36c_s^4\omega_{10}\omega_5^2\omega_{12}^2\omega_{12}^2 + 18c_s^2v_2^2\omega_{10}\omega_5^3\omega_{15}\omega_9^2\omega_{12}^2 - 12v_2^2v_1^2\omega_{10}\omega_5^3\omega_9^2\omega_{12}^2 - 15v_2^2v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 36c_s^4\omega_{10}\omega_5^2\omega_{21}\omega_9\omega_{12}^2 + 12c_s^4\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_9^2\omega_{12} - 12c_s^2\omega_{10}\omega_5^2\omega_9^2\omega_{12}^2 - 36c_s^4\omega_5^3\omega_{21}\omega_9\omega_{12}^2 +$$

$$C_{\text{D}_3\text{D}_{xy}\text{v}_{11}}^{(2), \text{CuLB}_{\text{M2}}} = (94\omega_3 c_4^4 \omega_4 \omega_1 \omega_2^3 - 4\omega_3 \omega_4 \omega_1 \omega_2^2 - 312\omega_3 c_2^2 v_1^2 \omega_4 \omega_2^3 + 84\omega_3 v_1^2 \omega_4 \omega_1 \omega_2^2 + 40\omega_3 c_2^2 \omega_4 \omega_2^3 + 8c_4^4 \omega_4 \omega_3^2 \omega_2 - 18c_4^4 \omega_4 \omega_2^3 \omega_2^3 + 153\omega_3 c_2^2 v_1^2 \omega_4 \omega_3^2 \omega_2^2 - 24\omega_3 c_2^2 \omega_4 \omega_1 \omega_2^3 + 138\omega_3 v_1^2 \omega_4 \omega_3^2 \omega_2 + 81\omega_3 v_1^2 \omega_4 \omega_1 \omega_2^3 + 14\omega_3 \omega_4 \omega_1 \omega_2^3 - 28\omega_3 c_2^2 \omega_4 \omega_1 \omega_2^3 + 16\omega_3 c_2^2 \omega_4 \omega_1^3 - 16\omega_3 c_2^2 \omega_4 \omega_2^2 \omega_2 +$$

$$12c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - 6v_2^2\omega_{10}^3\omega_5^3\omega_{15}^2\omega_{12} - 6c_s^2v_1^3\omega_{10}\omega_5^3\omega_{15}^2 + 18v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 18c_s^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} + 60c_s^2v_2^3\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 12c_s^4\omega_{10}^3\omega_5^3\omega_{15}\omega_{12} - 12c_s^2v_1^2\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 12v_1^2\omega_{10}^3\omega_5^2\omega_{15} - 36v_2^2v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{12} + 24c_s^2\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_{12} - 24c_s^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - 12c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2\omega_{12} + 6c_s^2v_1^2\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} - 42c_s^2v_2^3\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - 54v_2^3v_1^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}^2\omega_{12} + 12v_1^2\omega_{10}^3\omega_5^3\omega_{21}\omega_{12} - 36v_2^2v_1^2\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 18v_2^2v_1^3\omega_{10}\omega_5^3\omega_{15}^2\omega_{12} - 36v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 12c_s^2\omega_{10}^3\omega_5^2\omega_{15}^2\omega_{12} - 24c_s^4\omega_{10}^3\omega_5^2\omega_{21}\omega_{15}\omega_{12} - 24c_s^2v_2^3\omega_{10}^2\omega_5^3\omega_{21}\omega_{12} + 12c_s^2v_1^2\omega_{10}^3\omega_5^3\omega_{15}\omega_{12} + 36c_s^2v_2^3\omega_{10}^2\omega_5^2\omega_{15}\omega_{12} - 12c_s^4\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_{12} - 12v_1^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}^2\omega_{12}) \frac{\rho}{12\omega_{10}^3\omega_5^3\omega_{21}\omega_{15}^2\omega_{12}}$$

$$C_{D_x^2 D_y^2 v_2}^{(2), \text{MRT}^2} = C_{D_x^2 D_y^2 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x^2 D_y^2 v_2}^{(2), \text{CLBM}^1} = (-4c_s^2\omega_{10}^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 6\omega_{10}\omega_5^3\omega_{15}\omega_{12} + 12c_s^2\omega_{10}\omega_5\omega_{21}\omega_{12} + 12\omega_{10}^2\omega_5^3\omega_{12} + 12\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_{12} - 6c_s^2\omega_{10}^2\omega_5^3\omega_{15} - 12\omega_{10}\omega_5^2\omega_{21}\omega_{12} + 6c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 36v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{12} - 18v_2^2\omega_{10}\omega_5^3\omega_{15}\omega_{12} + 12\omega_{10}\omega_5^2\omega_{21}\omega_{15} - 12\omega_{10}^2\omega_5^3\omega_{21}\omega_{12} - 12c_s^2\omega_{10}^2\omega_5^3\omega_{12} + 6\omega_{10}^3\omega_5\omega_{15} - 12c_s^2\omega_{10}^2\omega_5\omega_{15}\omega_{12} + 12\omega_{10}^2\omega_5^2\omega_{15}\omega_{12} + 12\omega_5^2\omega_{15}\omega_{12} - 36v_2^2\omega_{10}^2\omega_5^2\omega_{15}\omega_{12} - 36v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_{12} - 36v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 6\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 36v_2^2\omega_{10}\omega_5\omega_{21}\omega_{12} + 36v_2^2\omega_{10}\omega_5^2\omega_{12} - 12\omega_{10}^2\omega_5^2\omega_{12} - 6c_s^2\omega_{10}\omega_5^3\omega_{15}\omega_{12} + 12c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 6c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 12\omega_{10}\omega_5\omega_{21}\omega_{12} + 18v_2^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 12c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{12} - c_s^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_{12} + 12c_s^2\omega_{10}^2\omega_5^3\omega_{21}\omega_{12} - 12c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{15} + 12c_s^2\omega_{10}^2\omega_5^2\omega_{12} - 12c_s^2\omega_{10}\omega_5^2\omega_{15}\omega_{12} - 12\omega_{10}^2\omega_5^2\omega_{15} - 12c_s^2\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 18v_2^2\omega_{10}\omega_5^3\omega_{15}\omega_{12} - 36v_2^2\omega_{10}\omega_5^3\omega_{12} + 18v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15} - 72v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{12} - 24\omega_{10}\omega_5^2\omega_{21}\omega_{15}\omega_{12} + 24\omega_{10}^2\omega_5^2\omega_{12} - 6\omega_{10}\omega_5^3\omega_{21}\omega_{15} + 18c_s^2\omega_{10}\omega_5\omega_{21}\omega_{15}\omega_{12} - 6\omega_{10}^2\omega_5^3\omega_{15}\omega_{12} - 36v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{12} - 18v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12} - 18v_2^2\omega_{10}\omega_5^2\omega_{21}\omega_{12} - 18v_2^2\omega_{10}\omega_5^3\omega_{21}\omega_{15} - 24c_s^2\omega_{10}\omega_5^2\omega_{21}\omega_{12} - 12\omega_{10}\omega_5^3\omega_{12} + 6c_s^2\omega_{10}^2\omega_5^3\omega_{15}\omega_{12} + 36v_2^2\omega_{10}\omega_5^2\omega_{12} - 12c_s^2\omega_{10}\omega_5^3\omega_{21}\omega_{12} + 12c_s^2\omega_{10}\omega_5^2\omega_{12} + 36v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 6\omega_{10}\omega_5^3\omega_{21}\omega_{15}\omega_{12}) \frac{c_s^2\rho}{12\omega_{10}^2\omega_5^3\omega_{21}\omega_{15}\omega_{12}}$$

$$C_{D_x^2 D_y^2 v_2}^{(2), \text{CLBM}^2} = C_{D_x^2 D_y^2 v_2}^{(2), \text{CLBM}^1}$$

$$C_{D_x^2 D_y^2 v_2}^{(2), \text{CuLBM}^1} = (24\omega_1^3\omega_5 + 36v_2^2\omega_7\omega_1^2\omega_5 + 72v_2^2\omega_1^3\omega_5 - 24c_s^2\omega_1^3\omega_5 + 24\omega_1^2\omega_5^2 - 24c_s^2\omega_1^2\omega_5^2 + 18c_s^2\omega_7\omega_1\omega_5^2 + 36v_2^2\omega_1^3\omega_5^2 + 24c_s^2\omega_1^2\omega_5 - 72v_2^2\omega_1^3\omega_5 - 12c_s^2\omega_7\omega_1\omega_5 - 24\omega_1^2\omega_5 - 12\omega_1^3 - 72v_2^2\omega_1^2\omega_5^2 + 12\omega_7\omega_1\omega_5 + 12c_s^2\omega_1^3\omega_5^2 - 12c_s^2\omega_7\omega_5^2 - 12\omega_1^3\omega_5^2 - c_s^2\omega_7\omega_1^3\omega_5^2 - 12\omega_7\omega_1^2\omega_5 + 36v_2^2\omega_1\omega_5^2 + 36v_2^2\omega_1^3 - 36v_2^2\omega_7\omega_1^2 + 12c_s^2\omega_7\omega_1^2\omega_5 + 12c_s^2\omega_1^3 - 12\omega_1\omega_5^2 + 12c_s^2\omega_1\omega_5^2 - 4c_s^2\omega_7\omega_1^2\omega_5^2 + 12\omega_7\omega_1^2 - 36v_2^2\omega_7\omega_1\omega_5 - 12c_s^2\omega_7\omega_1^2) \frac{c_s^2\rho}{12\omega_7\omega_1^3\omega_5^2}$$

$$C_{D_x^2 D_y^2 v_2}^{(2), \text{CuLBM}^2} = (8\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 32\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 + 18\omega_3^2v_1^4\omega_1\omega_2^3 - 174\omega_3^2c_s^2v_1^2\omega_4\omega_1^3\omega_2 + \omega_3^2v_2^4\omega_4\omega_1^3\omega_2^2 + 54\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 - 30\omega_3^2c_s^2v_1^2\omega_4\omega_1^2\omega_2^3 + 72\omega_3^2c_s^2\omega_2^2\omega_1^3 - 18\omega_3v_1^4\omega_1^3\omega_2^2 - 4\omega_3^2\omega_4\omega_1^2\omega_2 - 6\omega_3v_1^2\omega_4\omega_1^2\omega_2^2 + 48\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 4\omega_3^2\omega_4\omega_2^3 + 66\omega_3^2v_1^2\omega_4\omega_1^3\omega_2 + 24\omega_3^2v_1^4\omega_4\omega_1^3 - 36\omega_3^2v_2^2v_1^2\omega_4\omega_1^2\omega_2 + 9\omega_3^2v_1^2\omega_4\omega_1^2\omega_2^3 + 90\omega_3c_s^2v_1^2\omega_4\omega_1^3\omega_2^2 + 18\omega_3^2c_s^4\omega_1^3\omega_2^3 + 36\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 + 12\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 28\omega_3^2c_s^4\omega_4\omega_1\omega_2^2 - 84\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^2 + 12\omega_3v_1^4\omega_4\omega_1^3\omega_2^2 + 36\omega_3v_2^2\omega_4\omega_1^2\omega_2^3 - 18v_1^4\omega_4\omega_1^3\omega_2^2 - 2\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 24\omega_3^2c_s^2v_1^2\omega_4\omega_1^2\omega_2^2 + 12\omega_3^2v_1^2\omega_4\omega_2^3 + 76\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 12\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 108\omega_3^2c_s^2v_1^2\omega_4\omega_2^3 - 42\omega_3^2v_1^2\omega_4\omega_1^2\omega_2^3 - 18\omega_3v_1^2\omega_1^3\omega_2^3 - 56\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 72\omega_3^2c_s^4\omega_1^2\omega_2^3 - 18\omega_3^2v_1^4\omega_1\omega_2^3 + 6\omega_3v_1^4\omega_4\omega_1\omega_2^3 + 54\omega_3^2c_s^2v_1^2\omega_1\omega_2^3 + 18\omega_3v_2^2\omega_1^3\omega_2^2 + 54\omega_3c_s^2v_1^2\omega_4\omega_1^2\omega_2^3 - 90\omega_3^2v_2^2v_1^2\omega_4\omega_1^3\omega_2 - 36\omega_3v_1^2\omega_4\omega_1^3\omega_2^2 - 4\omega_3^2\omega_4\omega_1^3\omega_2 + 12\omega_3^2v_1^4\omega_4\omega_1\omega_2^2 - 48\omega_3^2v_1^4\omega_4\omega_1^3 - 12\omega_3^2c_s^2v_1^2\omega_4\omega_1^2\omega_2 + 18\omega_3^2c_s^2\omega_4\omega_1^2\omega_2 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 216\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^3 + 132\omega_3^2c_s^2v_1^2\omega_4\omega_1^3 + 18v_1^4\omega_4\omega_1^3\omega_2^3 + 2\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 9\omega_3^2v_1^4\omega_4\omega_1^3\omega_2^2 - 90\omega_3c_s^2v_1^2\omega_4\omega_1^2\omega_2^3 - 36\omega_3c_s^2v_1^2\omega_4\omega_1^3\omega_2 + 180\omega_3^2v_2^2v_1^2\omega_4\omega_1^2\omega_2^2 - 8\omega_3c_s^2\omega_4\omega_1^3\omega_2 + 60\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 36\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 30\omega_3^2c_s^2v_1^2\omega_4\omega_1^3\omega_2^2 - \omega_2^2v_1^4\omega_4\omega_1^3\omega_2^2 - 36\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^2 - 48\omega_3^2v_1^4\omega_4\omega_2^3 + 4\omega_3^2\omega_4\omega_1^3 + 54\omega_3^2v_1^4\omega_4\omega_1\omega_2^3 + 8\omega_3^2\omega_4\omega_1^2\omega_2^3 + 18\omega_3v_1^4\omega_1\omega_2^3 + 6\omega_3v_1^4\omega_4\omega_1\omega_2^2 - 144\omega_3^2v_2^2v_1^2\omega_4\omega_1\omega_2^3 + 54c_s^2v_1^2\omega_4\omega_1^2\omega_2^3 - 18\omega_3c_s^2v_1^2\omega_4\omega_1\omega_2^3 - 54\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^2 - 28\omega_3^2c_s^4\omega_4\omega_1\omega_2^2 + 24\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2 - 8\omega_3^2c_s^2\omega_4\omega_1\omega_2^2 - 126\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2^3 - 3\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 + 18\omega_3^2v_1^2\omega_1^2\omega_2^2 - \omega_2^2v_2^4\omega_4\omega_1^3\omega_2^2 - 36\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 18\omega_3^2v_1^2\omega_4\omega_1^3\omega_2^2 - \omega_2^2v_2^4\omega_4\omega_1^3\omega_2^2 - 36\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 18\omega_3^2v_1^2\omega_4\omega_1^3\omega_2^2 + 12\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^3 + 108\omega_3^2v_2^2v_1^2\omega_4\omega_1^3\omega_2^2 - 9\omega_3^2v_1^4\omega_4\omega_1^3\omega_2^3 - 12\omega_3^2v_2^2\omega_4\omega_1^3 + 18\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^3 + 132\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 12\omega_3^2c_s^4\omega_1^2\omega_2^3 + 12\omega_3^2v_2^2\omega_4\omega_1^3\omega_2 + 12\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^3 - 54\omega_3^2c_s^2v_1^2\omega_2^3 - 90\omega_3^2v_2^2v_1^2\omega_4\omega_1\omega_2^3 - 36\omega_3v_1^4\omega_4\omega_1\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2v_1^4\omega_4\omega_1^2\omega_2^2 - 48\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 16\omega_3^2c_s^4\omega_4\omega_1^3 - 18\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 216\omega_3^2c_s^2v_2^2\omega_1\omega_2^3 + 18\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 - 6\omega_3v_1^2\omega_4\omega_1\omega_2^3 + 12\omega_3^2v_1^4\omega_4\omega_1^2\omega_2^2 + 66\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 - 12\omega_3^2v_2^2\omega_4\omega_2^3 - 18\omega_3^2v_1^4\omega_2^2\omega_2^2 + 56\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 12\omega_3^2c_s^2v_1^2\omega_4\omega_1\omega_2^2 - 96\omega_3^2c_s^2v_2^2\omega_4\omega_2^3 - 68\omega_3^2c_s^4\omega_4\omega_2^3 - 14\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 - 14\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^2 - 24\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 - 18\omega_3^2v_1^2\omega_1^3\omega_2^2 - 18v_1^4\omega_4\omega_1^2\omega_2^2 + 54\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 36\omega_3v_1^4\omega_4\omega_1^3\omega_2^2 + 54\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^2 + 150\omega_3^2c_s^2v_1^2\omega_4\omega_1\omega_2^3 - 72\omega_3^2c_s^2\omega_1\omega_2^3 + 8\omega_3c_s^4\omega_4\omega_1\omega_2^2 - 36\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 18\omega_3^2v_1^4\omega_1^2\omega_2^2 + 9\omega_3^2v_1^4\omega_4\omega_1\omega_2^2 - 6\omega_3^2c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 6\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 54\omega_3c_s^2v_1^2\omega_1^3\omega_2^2 - 54c_s^2v_1^2\omega_4\omega_1^3\omega_2^2 - 24\omega_3^2v_1^4\omega_4\omega_1\omega_2^3 - 20\omega_3^2c_s^2\omega_4\omega_1^3 + 72\omega_3^2v_2^2v_1^2\omega_4\omega_1^3 - 90\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 + \omega_3^2v_2^2\omega_4\omega_1^2\omega_2^3 + 28\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^2 + 12\omega_3^2v_2^2\omega_4\omega_1^3\omega_2) \frac{\rho}{36\omega_3^2\omega_4\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_x D_y^3 \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_2^3} :$$

$$C_{D_x D_y^3 \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y^3 \rho}^{(2), \text{MRT}^1} = (-4c_s^4\omega_{10}^3\omega_{15} - 8c_s^2\omega_{10}^3\omega_5\omega_{15} + 13v_2^4\omega_{10}^4\omega_5^2\omega_{15} - 4c_s^2\omega_{10}\omega_5\omega_{15} - 4c_s^4\omega_{10}\omega_5^2\omega_{15} - 51c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 8v_2^2\omega_{10}^3\omega_{15} + 36c_s^2v_2^2\omega_{10}^2\omega_{15} + 16v_2^2\omega_{10}^2\omega_5\omega_{15} - 144c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15} + 20v_2^4\omega_{10}\omega_5\omega_{15} - 4c_s^2\omega_{10}^2\omega_5^2\omega_{15} + 4c_s^4\omega_{10}^2\omega_{15} + 20v_2^4\omega_{10}^3\omega_5\omega_{15} - 84c_s^2v_2^2\omega_{10}^2\omega_5\omega_{15} + 20v_2^2\omega_{10}\omega_5^2\omega_{15} - 8v_2^2\omega_{10}^2\omega_{15} - 36c_s^2v_2^2\omega_{10}^3\omega_{15} + 4c_s^2\omega_{10}^3\omega_{15} - 48c_s^2v_2^2\omega_{10}^2\omega_5\omega_{15} + 13v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 8c_s^4\omega_{10}^2\omega_5\omega_{15} + 36v_2^2\omega_{10}\omega_5^2\omega_{15} - 8v_1^4\omega_{10}^3\omega_{15} - 8c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 12c_s^4\omega_{10}\omega_5^2\omega_{15} + 20v_2^2\omega_{10}^2\omega_5\omega_{15} - 4c_s^4\omega_{10}^3\omega_5\omega_{15} - 4c_s^2\omega_{10}^2\omega_{15} - 72c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15} + 32v_2^4\omega_{10}^2\omega_5^2\omega_{15} + 8v_1^4\omega_{10}^2\omega_{15} - 13v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 4v_2^2\omega_{10}^2\omega_5 - 24c_s^2v_2^2\omega_{10}^3\omega_5 + 4c_s^4\omega_{10}\omega_5\omega_{15} - 4c_s^2\omega_{10}^3\omega_5 + 8c_s^2\omega_{10}\omega_5\omega_{15} - 4c_s^4\omega_{10}^2\omega_5 + 4v_1^4\omega_{10}\omega_5^2 + 4c_s^4\omega_{10}\omega_5^2\omega_{15} - 16v_2^2\omega_{10}^2\omega_5\omega_{15} + 120c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15} - 20v_2^2\omega_{10}^3\omega_5\omega_{15} - 20v_2^2\omega_{10}\omega_5\omega_{15}^2 + 4v_2^2\omega_{10}^3\omega_5 + 24v_2^4\omega_5^2\omega_{15} - 24c_s^2v_2^2\omega_{10}^2\omega_5^2 + 4c_s^4\omega_{10}^2\omega_5^2\omega_{15} - 20v_2^2\omega_{10}\omega_5^2\omega_{15} - 8c_s^2\omega_5^2\omega_{15} - 4c_s^4\omega_{10}^3\omega_5 + 96c_s^2v_2^2\omega_5^2\omega_{15} - 4v_1^4\omega_{10}^2\omega_5^2 + 8c_s^2\omega_{10}^2\omega_5\omega_{15} - 36v_2^2\omega_{10}\omega_5^2\omega_{15} + 4c_s^4\omega_{10}^3\omega_5^2 - 13v_2^4\omega_{10}^3\omega_5^2\omega_{15} + 51c_s^2v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 4c_s^2\omega_{10}^2\omega_5^2 + 8c_s^4\omega_{10}^2\omega_2^2\omega_{15} - 4v_2^2\omega_{10}^3\omega_5^2 + 4c_s^2\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^2\omega_{10}\omega_5^2\omega_{15} - 24v_2^2\omega_5^2\omega_{15} - 4v_2^4\omega_{10}^3\omega_5 -$$

$$20v_2^4\omega_{10}^2\omega_5\omega_{15}^2 + 84c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} - 32v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 24c_s^2v_2^2\omega_{10}^3\omega_5^2 + 72c_s^2v_2^2\omega_{10}\omega_5\omega_{15}^2 + 4c_s^2\omega_{10}^3\omega_5 + 8c_s^4\omega_5^2\omega_{15}^2) \frac{v_1}{4\omega_{10}^3\omega_5^2\omega_{15}^2}$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(2),\text{MRT}^2} = C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(2),\text{MRT}^1}$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(2),\text{CLBM}^1} = 0$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(2),\text{CLBM}^2} = 0$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(2),\text{CuLBM}^1} = 0$$

$$\begin{aligned} C_{\mathbf{D}_x\mathbf{D}_y^3\rho}^{(2),\text{CuLBM}^2} = & (56\omega_3c_s^2\omega_1^3\omega_2 + 5\omega_3c_s^2\omega_1^2\omega_2^3 - 48\omega_3v_2^2v_1^3\omega_1^3\omega_2 - 24\omega_3^2v_2^2\omega_1^2\omega_2 - 4\omega_3^2v_1^2\omega_1^3 - 24\omega_3^2v_2^2v_1^3\omega_1^2\omega_2^3 - 36\omega_3^2v_2^4\omega_1^3\omega_2 - 36\omega_3^2c_s^4\omega_1^3\omega_2^3 - \\ & 12c_s^2v_1^4\omega_1^3\omega_2^2 - 36\omega_3^2c_s^4\omega_1^2\omega_2 + 4\omega_3^2\omega_1^3 - 48\omega_3^2v_2^2v_1^3\omega_1^2\omega_2^2 - 24\omega_3^2v_2^2\omega_1^3\omega_2^2 - 34\omega_3^2c_s^2\omega_1^2\omega_2^2 + 72\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^2 + 48\omega_3^2v_2^4\omega_1^3\omega_2^2 + 6\omega_3^2c_s^4\omega_1^3\omega_2^2 + 72\omega_3^2v_2^4\omega_1^3\omega_2^2 + \\ & 24\omega_3c_s^4\omega_1\omega_1^3\omega_2^3 - 6\omega_3^2c_s^4\omega_1^2\omega_2^3 - 8\omega_3^2v_1^2\omega_1\omega_2^3 - 84\omega_3^2c_s^4\omega_1^3\omega_2 + 8\omega_3^2\omega_1\omega_2^2 + 22\omega_3^2c_s^2v_1^2\omega_1\omega_2^3 + 84\omega_3^2v_2^2\omega_1^3\omega_2 + 24\omega_3^2v_2^2v_1^2\omega_1^2\omega_2^3 + 24\omega_3^2v_2^2\omega_1^2\omega_2^3 + \\ & 24\omega_3^2v_2^4\omega_1^3 - 324\omega_3^2c_s^2v_2^2\omega_1^3\omega_2 + 40\omega_3^2c_s^2\omega_1^2\omega_2 - 72\omega_3^2c_s^2v_2^2\omega_1^3\omega_2 + 8\omega_3^2c_s^2v_1^2\omega_1\omega_2^3 + 8\omega_3^2\omega_1\omega_2^3 - 8\omega_3^2v_1^2\omega_1\omega_2^3 + 12c_s^2v_1^2\omega_1^2\omega_2^3 + 8\omega_3^2v_1^2\omega_2^3 + 42\omega_3^2c_s^2\omega_1^2\omega_2^3 + \\ & 216\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^2 - 5\omega_3^2c_s^2\omega_1^3\omega_2^2 + 216\omega_3^2c_s^2v_2^2\omega_1^3 - 8\omega_3c_s^2\omega_1\omega_2^3 - 24\omega_3^2v_2^2\omega_1^2\omega_2^2 - 8\omega_3^2\omega_2^3 + 24\omega_3^2v_2^2v_1^2\omega_1^3\omega_2^2 + 72\omega_3^2c_s^4\omega_1^3 + 8\omega_3c_s^2v_1^2\omega_1\omega_2^3 - \omega_3^2\omega_1^2\omega_2^3 - \\ & 4\omega_3^2\omega_1^3\omega_2 - 2\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^2 + 16\omega_3^2c_s^2v_1^2\omega_1^3 + 4\omega_3^2v_1^2\omega_1^2\omega_2^2 + 24\omega_3^2v_2^2\omega_2^3 + 12c_s^2\omega_1^3\omega_2^2 - 216\omega_3^2c_s^2v_2^2\omega_1\omega_2^3 - 18\omega_3c_s^2v_1^2\omega_1^3\omega_2^3 + 4\omega_3c_s^2\omega_1^3\omega_2 - 4\omega_3c_s^2v_1^2\omega_1^3\omega_2 + \\ & 18\omega_3c_s^2\omega_1^2\omega_2^3 + 48\omega_3^2v_2^2\omega_1\omega_2^2 + \omega_3^2v_1^2\omega_1^2\omega_2^3 + 36c_s^4\omega_1^2\omega_2^3 + 42\omega_3^2c_s^4\omega_1\omega_2^3 + 4\omega_3^2v_1^2\omega_1^3\omega_2 - 2\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^3 + 54\omega_3c_s^4\omega_1^3\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2^2 - 20\omega_3^2c_s^2v_1^2\omega_1^3\omega_2 - \\ & 60\omega_3^2v_2^2\omega_1\omega_2^3 + 4\omega_3c_s^2\omega_1^2\omega_2^2 - 4\omega_3c_s^2v_1^2\omega_1^2\omega_2^2 + 20\omega_3^2c_s^2\omega_2^3 + 108\omega_3^2c_s^2v_2^2\omega_1\omega_2^3 - 72\omega_3^2v_2^2v_1^2\omega_2^3 + 24\omega_3^2v_2^2v_1^2\omega_1\omega_2^3 - 8\omega_3^2c_s^2\omega_1\omega_2^3 - 36c_s^4\omega_1^3\omega_2^2 - \omega_3^2v_1^2\omega_1^3\omega_2^2 - \\ & 72\omega_3^2v_2^4\omega_1\omega_2^2 - 54\omega_3c_s^4\omega_1^2\omega_2^3 + 24\omega_3^2v_2^2v_1^2\omega_1^3 + 2\omega_3^2c_s^2v_1^2\omega_1^3\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2 - 52\omega_3^2c_s^2\omega_1^3 - 12\omega_3c_s^4\omega_1^3\omega_2 - 22\omega_3^2c_s^2\omega_1\omega_2^3 - 12c_s^2\omega_1^2\omega_2^3 - 18\omega_3c_s^2\omega_1^3\omega_2^2 + \\ & 96\omega_3^2v_2^2\omega_1^2\omega_2^3 - 20\omega_3^2c_s^2v_1^2\omega_2^3 + 18\omega_3c_s^2v_1^2\omega_1^3\omega_2^2 - 4\omega_3^2c_s^2v_1^2\omega_1^2\omega_2 + \omega_3^2\omega_1^3\omega_2^2 - 12\omega_3c_s^4\omega_1^2\omega_2^2 - 36\omega_3^2v_2^4\omega_1\omega_2^3 - 48\omega_3^2v_2^2\omega_1^3 + 4\omega_3^2v_1^2\omega_1^2\omega_2) \frac{v_1}{36\omega_3^3\omega_1^3\omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_2^3} :$$

$$\begin{aligned} C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{SRT}} = & (-36c_s^2v_2^2 - c_s^4\omega^3 - 26v_2^4\omega^2 - 36v_2^4 + 4v_2^4\omega^3 + 20c_s^4\omega^2 + 36c_s^4 - 54c_s^4\omega + 54v_2^4\omega + 12c_s^2v_2^2\omega^3 - 4v_2^2\omega^3 - 12c_s^2\omega^2 - 42c_s^2v_2^2\omega^2 + \\ & 26v_2^2\omega^2 - 54v_2^2\omega + 54c_s^2v_2^2\omega + 36c_s^2\omega - 24c_s^2 + 36v_2^2) \frac{\rho}{12\omega^3} \end{aligned}$$

$$\begin{aligned} C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{MRT}^1} = & (-12c_s^2\omega_{10}^3\omega_5\omega_{15} + 12v_2^4\omega_{10}^2\omega_5^2\omega_{15}^2 + 6c_s^2\omega_{10}^3\omega_5^3\omega_{15} + 90v_2\omega_{10}\omega_5^3\omega_{15} + 30c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 13c_s^4\omega_{10}^3\omega_5^2\omega_{15} + 27v_2^2\omega_{10}^3\omega_5^3\omega_{15} - \\ & 108c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15}^2 + 60v_2^4\omega_{10}^2\omega_5^3\omega_{15} - 6c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - 24v_2^4\omega_{10}^3\omega_5\omega_{15} + 6c_s^4\omega_{10}^3\omega_5^3\omega_{15} + 18v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 48c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} - \\ & 36c_s^2v_2^2\omega_{10}\omega_5^3\omega_{15} - 12c_s^4\omega_{10}\omega_5^3\omega_{15}^2 + 12c_s^2v_2^2\omega_{10}^3\omega_5^3\omega_{15} - c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2 - 306c_s^2v_2^2\omega_{10}\omega_5^3\omega_{15} - 48v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 48c_s^2v_2^2\omega_{10}^3\omega_{15}^2 - \\ & 21c_s^2v_2^2\omega_{10}^3\omega_5^3\omega_{15} + 19v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 12c_s^2\omega_{10}^2\omega_5^2\omega_{15} + 12v_2^2\omega_{10}^3\omega_5\omega_{15} - 12c_s^4\omega_{10}\omega_5^2\omega_{15}^2 - 81c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 36v_2^2\omega_{10}\omega_5^2\omega_{15} - 18c_s^4\omega_{10}^3\omega_5^2\omega_{15} - \\ & 4v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^4\omega_{10}^3\omega_{15}^2 + 6c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - 24v_2^4\omega_{10}^2\omega_5^2\omega_{15} - c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - 12c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 12v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 102c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15}^2 - \\ & 6c_s^2\omega_{10}^2\omega_5\omega_{15} + 60c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^4\omega_{10}^3\omega_5\omega_{15} - 5c_s^2\omega_{10}^3\omega_5^2\omega_{15} - 27v_2^4\omega_{10}^3\omega_5^3\omega_{15} - 12v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 252c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 90v_2^2\omega_{10}\omega_5^3\omega_{15} - \\ & 12c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} + 24v_2^2\omega_{10}^3\omega_5\omega_{15} + 12c_s^4\omega_5^3\omega_{15} + 12v_2^2\omega_{10}^3\omega_5^3 - 60v_2^2\omega_{10}^3\omega_5^3\omega_{15} + 6c_s^4\omega_{10}^2\omega_5^2\omega_{15} - 72v_2^2\omega_5^3\omega_{15} + 12c_s^2\omega_{10}\omega_5^3\omega_{15} + 12v_2^4\omega_{10}^3\omega_5^3 - \\ & 6c_s^2\omega_{10}^3\omega_5^2\omega_{15} - 18v_2^4\omega_{10}^3\omega_5^2\omega_{15} + 48v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 12v_2^2\omega_{10}^3\omega_5\omega_{15} + 162c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 19v_2^2\omega_{10}^3\omega_5^3\omega_{15} + 12c_s^2v_2^2\omega_{10}^3\omega_5^3 + 12c_s^4\omega_{10}^3\omega_5^2\omega_{15} + \\ & 12v_2^2\omega_{10}^3\omega_5^2 + 18c_s^2\omega_{10}^3\omega_5^2\omega_{15} - 12c_s^2\omega_5^3\omega_{15} + 4v_2^4\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^2\omega_{10}\omega_5^2\omega_{15} - 12v_2^4\omega_{10}^3\omega_5^3 - 36v_2^4\omega_{10}\omega_5^3\omega_{15} - 12c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} + \\ & 24v_2^2\omega_{10}^2\omega_5^2\omega_{15} - 12v_2^2\omega_{10}^3\omega_5^3 + c_s^4\omega_{10}^3\omega_5^2\omega_{15} - 12c_s^2v_2^2\omega_{10}^3\omega_5^2 + 72v_2^4\omega_5^2\omega_{15} + 54c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} - 24c_s^4\omega_{10}^3\omega_5\omega_{15}^2) \frac{\rho}{12\omega_{10}^3\omega_5^3\omega_{15}^2} \end{aligned}$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{MRT}^2} = C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{MRT}^1}$$

$$\begin{aligned} C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{CLBM}^1} = & (-12c_s^2\omega_{10}^3\omega_5\omega_{15} + 6c_s^2\omega_{10}^3\omega_5^3\omega_{15} + 90v_2^2\omega_{10}\omega_5^3\omega_{15} + 54c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 13c_s^4\omega_{10}^3\omega_5^2\omega_{15} + 39v_2^2\omega_{10}^3\omega_5^3\omega_{15} - 36c_s^2v_2^2\omega_{10}\omega_5^2\omega_{15} + 72v_2^4\omega_{10}^2\omega_5^3\omega_{15} - \\ & 6c_s^2\omega_{10}^2\omega_5^2\omega_{15} + 6c_s^4\omega_{10}^3\omega_5^3\omega_{15} + 6v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 108c_s^2v_2^2\omega_{10}\omega_5^3\omega_{15} - 12c_s^4\omega_{10}\omega_5^3\omega_{15} + 12c_s^2v_2^2\omega_{10}^3\omega_5^3\omega_{15} - c_s^4\omega_{10}^3\omega_5^2\omega_{15}^2 - 306c_s^2v_2^2\omega_{10}\omega_5^3\omega_{15} - \\ & 36v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 99c_s^2v_2^2\omega_{10}^3\omega_5^3\omega_{15} + 19v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 12c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 12c_s^4\omega_{10}\omega_5^2\omega_{15}^2 - 3c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 36v_2^2\omega_{10}\omega_5^2\omega_{15} - 18c_s^4\omega_{10}^3\omega_5^2\omega_{15} - \\ & 4v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^4\omega_{10}^3\omega_{15}^2 + 6c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - 108c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 18c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} - 6c_s^4\omega_{10}^3\omega_5^3\omega_{15} + 60c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + \\ & 12c_s^4\omega_{10}^3\omega_5\omega_{15} - 5c_s^2\omega_{10}^3\omega_5^2\omega_{15} - 39v_2^2\omega_{10}^3\omega_5^3\omega_{15} - 36v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 252c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 90v_2^2\omega_{10}\omega_5^3\omega_{15} + 36c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^4\omega_5^3\omega_{15} + 36v_2^2\omega_{10}^3\omega_5^3 - \\ & 72v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 6c_s^4\omega_{10}^2\omega_5^2\omega_{15} - 72v_2^2\omega_5^3\omega_{15} + 12c_s^2\omega_{10}\omega_5^3\omega_{15} + 36v_2^4\omega_{10}^3\omega_5^3 - 6c_s^2\omega_{10}^3\omega_5^3\omega_{15} - 6v_2^4\omega_{10}^3\omega_5^2\omega_{15} + 36v_2^4\omega_{10}^3\omega_5^2\omega_{15} + 18c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - \\ & 19v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 108c_s^2v_2^2\omega_{10}^3\omega_5^3\omega_{15} + 12c_s^4\omega_{10}^3\omega_5^2\omega_{15} + 36v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 18c_s^2\omega_{10}^3\omega_5^2\omega_{15} - 12c_s^2\omega_5^3\omega_{15} + 4v_2^4\omega_{10}^3\omega_5^2\omega_{15} + 12c_s^2\omega_{10}\omega_5^2\omega_{15} - 36v_2^4\omega_{10}^3\omega_5^3 - \\ & 36v_2^2\omega_{10}\omega_5^3\omega_{15} + 36c_s^2v_2^2\omega_{10}^3\omega_5\omega_{15} - 36v_2^2\omega_{10}^3\omega_5^3 + c_s^4\omega_{10}^3\omega_5^2\omega_{15} - 108c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} + 72v_2^4\omega_5^2\omega_{15} + 198c_s^2v_2^2\omega_{10}^3\omega_5^2\omega_{15} - 24c_s^4\omega_{10}^3\omega_5\omega_{15}^2) \frac{\rho}{12\omega_{10}^3\omega_5^3\omega_{15}^2} \end{aligned}$$

$$C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{CLBM}^2} = C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{CLBM}^1}$$

$$\begin{aligned} C_{\mathbf{D}_x\mathbf{D}_y^3v_1}^{(2),\text{CuLBM}^1} = & (54c_s^2v_2^2\omega_7\omega_1^3\omega_5^3 - 108c_s^2v_2^2\omega_7\omega_1^3\omega_5 - 6c_s^4\omega_7\omega_1^3\omega_5^2 + 39v_2^2\omega_7\omega_1^3\omega_5^3 - 36v_2^4\omega_1^2\omega_5^3 - 12c_s^2\omega_7\omega_1\omega_5^3 - 36v_2^2\omega_1^3\omega_5^3 - 90v_2^4\omega_7\omega_1^3\omega_5 - \\ & 6v_2^4\omega_7\omega_1^2\omega_5^3 - 108c_s^2v_2^2\omega_1^3\omega_5^2 - 6c_s^2\omega_7^2\omega_1^2\omega_5^2 - 72v_2^2\omega_7\omega_1^3\omega_5^2 + 6c_s^4\omega_7\omega_1^3\omega_5^3 + 72v_2^4\omega_7^2\omega_1^3 - 18c_s^2v_2^2\omega_7^2\omega_1\omega_5^3 + 36c_s^2v_2^2\omega_7\omega_1^2\omega_5^2 - 5c_s^2\omega_7^2\omega_1^2\omega_5^3 + \\ & 108c_s^2v_2^2\omega_1^3\omega_5^3 - 12c_s^2\omega_7^2\omega_1^3 + 36v_2^2\omega_7^2\omega_1^3\omega_5 + 252c_s^2v_2^2\omega_7^2\omega_1^3 + 36v_2^2\omega_7^2\omega_1^3\omega_5^3 + 4v_2^4\omega_7^2\omega_1^3\omega_5^3 - c_s^2\omega_7^2\omega_1^3\omega_5^2 + 12c_s^4\omega_7\omega_1^2\omega_5^2 - \\ & 36v_2^2\omega_7\omega_1^2\omega_5^3 + 36v_2^2\omega_7\omega_1^3\omega_5 - 24c_s^4\omega_7^2\omega_1\omega_5^3 + 36v_2^4\omega_1^3\omega_5^3 - 99c_s^2v_2^2\omega_7\omega_1^3\omega_5^3 - 108c_s^2v_2^2\omega_1^3\omega_5^3 + 19v_2^4\omega_7^2\omega_1^3\omega_5^2 + 12c_s^2\omega_7^2\omega_1^2\omega_5 - 72v_2^2\omega_7^2\omega_1^3 + \end{aligned}$$

$$198c_s^2v_2^2\omega_7\omega_1^3\omega_5^2 - 36v_2^4\omega_3^3\omega_5^2 + 12c_s^4\omega_7\omega_1^3 - 18c_s^4\omega_7\omega_1^2\omega_5^3 + 6c_s^2\omega_7\omega_1^3\omega_5^2 - 39v_2^4\omega_7\omega_1^3\omega_5^3 - 36c_s^2v_2^2\omega_2^2\omega_1^5\omega_5 + 12c_s^2v_2^2\omega_2^2\omega_1^3\omega_5^3 + 90v_2^2\omega_2^2\omega_1^3\omega_5 + 12c_s^4\omega_7\omega_1\omega_5^3 + 6v_2^2\omega_2^2\omega_1^3\omega_5^3 + 6c_s^4\omega_2^2\omega_1^3\omega_5^2 + 72v_2^2\omega_7\omega_1^3\omega_5^2 - 6c_s^2\omega_7\omega_1^3\omega_5^3 + 13c_s^4\omega_2^2\omega_1^3\omega_5^3 - 12c_s^4\omega_2^2\omega_1^3\omega_5 + 60c_s^2v_2^2\omega_2^2\omega_1^3\omega_5^2 - 4v_2^2\omega_2^2\omega_1^3\omega_5^3 + c_s^4\omega_2^2\omega_1^3\omega_5^2 - 306c_s^2v_2^2\omega_2^2\omega_1^3\omega_5 - 3c_s^2v_2^2\omega_2^2\omega_1^3\omega_5^3 - 12c_s^2\omega_7\omega_1^2\omega_5^2 + 36v_2^4\omega_7\omega_1^3\omega_5^3 + 6c_s^2\omega_2^2\omega_1\omega_5^3 - 36v_2^4\omega_7\omega_1^3\omega_5 + 12c_s^4\omega_7^2\omega_5^3 + 18c_s^2v_2^2\omega_2^2\omega_1^3\omega_5^2 + 36c_s^2v_2^2\omega_7\omega_1\omega_5^3 - c_s^4\omega_7^2\omega_1\omega_5^3 - 19v_2^2\omega_2^2\omega_1^3\omega_5^2 - 12c_s^4\omega_7^2\omega_1\omega_5 + 18c_s^2\omega_7\omega_1^2\omega_5^3) \frac{\rho}{12\omega_7^2\omega_1^3\omega_5^3}$$

$$C_{\text{Dx D}^3\text{y } v_1}^{(2), \text{CuLBM2}} = (48\omega_3^2c_s^2v_1^2\omega_2^2\omega_1\omega_2^2 + 48\omega_3^2v_2^2\omega_4^2\omega_1^3 + 24\omega_3v_2^2\omega_2^4\omega_1^3\omega_2 - 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 36\omega_3^2v_2^4\omega_4\omega_1^3\omega_2^2 + 162\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 - 216\omega_3v_2^2\omega_4^2\omega_1^2\omega_2^3 + 40\omega_3c_s^4\omega_2^2\omega_1^2\omega_2^2 - 36v_2^4\omega_4^2\omega_1^3\omega_2^2 - 492\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 54\omega_3^2v_2^2\omega_1^3\omega_2^3 - 108\omega_3^2v_2^4\omega_1^2\omega_2^3 - 48\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^2 - 40\omega_3^2c_s^2\omega_4^2\omega_1^3 + 240\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^2 + 86\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^3 - 297\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 108\omega_3v_2^4\omega_4\omega_1^3\omega_2^2 - 28\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2 + 144\omega_3^2v_2^2v_1^2\omega_1^2\omega_2^3 + 72\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 48\omega_3^2v_2^2\omega_4^2\omega_2^3 - 492\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2 + 54v_2^4\omega_4^2\omega_1^3\omega_2^3 + 174\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 432\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 117\omega_3^2v_2^4\omega_4\omega_1^3\omega_2^3 - 36\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 60\omega_3v_2^2\omega_4^2\omega_1^2\omega_2^3 - 12\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^3 + 16\omega_3c_s^4\omega_4^2\omega_1^2\omega_2^2 + 204\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2 + 72\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 288\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 20\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 + 8\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^3 - 36\omega_3v_2^4\omega_4\omega_1^3\omega_2^3 + 80\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 48\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^3 - 180\omega_3v_2^4\omega_4\omega_1^2\omega_2^3 + 468\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^3 - 86\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 6\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - 56\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2 - 16\omega_3c_s^2\omega_4^2\omega_1\omega_2^3 - 96\omega_3^2v_2^2\omega_1^2\omega_2^3 - 72\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2 - 96\omega_3c_s^2v_1^2\omega_1^2\omega_2^3 + 54\omega_3^2v_2^4\omega_1^3\omega_2^3 + 144\omega_3^2v_2^2v_1^2\omega_4^2\omega_1\omega_2^2 + 264\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3 + 32\omega_3^2c_s^4\omega_4^2\omega_1^3 + 168\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 16\omega_3^2\omega_4^2\omega_1\omega_2^2 + 108\omega_3^2v_2^2\omega_1^2\omega_2^3 - 32\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 288\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 + 117\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^2 - 324\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 72\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 36\omega_3^2v_2^4\omega_4\omega_1^2\omega_2^3 + 192\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^3 - 24\omega_3v_2^4\omega_4\omega_1\omega_2^3 - 144\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2 - 2\omega_3^2c_s^4\omega_4^2\omega_1^2\omega_2^2 - 24\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 + 18\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3v_2^2\omega_4^2\omega_1^2\omega_2^2 + 288\omega_3^2v_2^4\omega_4\omega_1^2\omega_2^3 + 8\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 96\omega_3^2v_2^4\omega_4\omega_1\omega_2^2 + 48\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^3 - 432\omega_3^2v_2^2v_1^2\omega_1^2\omega_2^3 + 264\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 + 16\omega_3^2\omega_4^2\omega_1\omega_2^3 + 72\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 72v_2^2\omega_4^2\omega_1^2\omega_2^3 + 48\omega_3c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^2 + 36v_2^2\omega_4^2\omega_1^2\omega_2^2 - 288\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^2 - 144\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^2\omega_2^2 + 24\omega_3^2v_1^2\omega_4^2\omega_1\omega_2^2 - 24\omega_3v_2^4\omega_4^2\omega_1^2\omega_2^2 + 216\omega_3v_2^2\omega_4^2\omega_1^2\omega_2^2 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^2 - 540\omega_3c_s^2v_2^2\omega_4\omega_1^2\omega_2^3 + 18\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 36\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^3 - 108\omega_3v_2^2\omega_4\omega_1^2\omega_2^3 - 144\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^3 - 72\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 - 96\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 + 36\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 2\omega_3^2\omega_4^2\omega_1\omega_2^2 + 108\omega_3^2c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2 + 36\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 - 60\omega_3v_2^4\omega_4\omega_1^2\omega_2^2 + 117\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^3 + 72\omega_3c_s^2v_2^2\omega_4^2\omega_1\omega_2^3 - 16\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 216c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^3 + 48\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2 - 288\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^2\omega_2^2 - 6\omega_3^2v_1^2\omega_4^2\omega_1^3\omega_2^2 - 54v_2^2\omega_4^2\omega_1^3\omega_2^3 + 72\omega_3c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 297\omega_3^2c_s^2v_2^2\omega_4\omega_1^3\omega_2^3 - 24\omega_3^2v_1^2\omega_1^2\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^2\omega_2^2 + 24\omega_3^2c_s^2v_1^2\omega_1^2\omega_2^3 - 72\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 108\omega_3^2v_2^2\omega_4\omega_1^2\omega_2 - 12\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 36\omega_3v_2^2\omega_4\omega_1^3\omega_2^2 - 12\omega_3^2c_s^2\omega_4^2\omega_1^2\omega_2^2 + 40\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 852\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 8\omega_3^2v_1^2\omega_1^2\omega_2 - 108\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 38\omega_3^2v_2^4\omega_4\omega_1^3\omega_2^3 + 12\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 180\omega_3v_2^2\omega_4\omega_1^2\omega_2^3 + 16\omega_3c_s^4\omega_4^2\omega_1\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^2 - 12\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^3\omega_2 - 108c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 + 16\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^2 + 96\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 72\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 36\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 324\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^3 - 117\omega_3v_2^4\omega_4^2\omega_1^3\omega_2^3 + 48\omega_3^2v_1^2\omega_1^2\omega_2^3 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 + 6\omega_3^2v_1^2\omega_4^2\omega_1^2\omega_2^3 + 144\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^2\omega_2 - 72\omega_3c_s^2v_1^2\omega_4^2\omega_1^3\omega_2^2 + 24\omega_3^2v_1^2\omega_4^2\omega_1^2\omega_2 + 24\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^2 + 96\omega_3^2v_2^4\omega_4^2\omega_1^2\omega_2 + 24\omega_3v_2^2\omega_4^2\omega_1\omega_2^3 + 24\omega_3^2v_2^4\omega_4^2\omega_1^3\omega_2^3 + 24\omega_3^2c_s^2v_1^2\omega_4^2\omega_1^2\omega_2^2 + 648\omega_3^2c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 + 336\omega_3^2c_s^2v_2^2\omega_4^2\omega_1\omega_2^2 + 2\omega_3^2\omega_4^2\omega_1^3\omega_2^2 + 144\omega_3^2v_2^2v_1^2\omega_4^2\omega_1^3\omega_2^2 + 72v_2^2\omega_4^2\omega_1^2\omega_2^3 + 24\omega_3^2v_2^2\omega_4^2\omega_1^2\omega_2^2 - 16\omega_3^2\omega_4^2\omega_2^3 - 108\omega_3c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 288\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 - 18\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^2 + 108\omega_3v_2^2\omega_4^2\omega_1^3\omega_2^2 - 144\omega_3^2v_2^2\omega_4\omega_1\omega_2^2 + 162c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^2 - 172\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3) \frac{\rho}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{\text{Dx D}^3\text{y } v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_2^2} :$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{SRT}} = 0$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{MRT1}} = (44c_s^2\omega_{10}\omega_5\omega_{15} - 17\omega_{10}^2\omega_5^2\omega_{15} + 32c_s^2\omega_{10}\omega_5\omega_{15}^2 - 28v_2^2\omega_{10}^3\omega_{15} - 48v_2^2\omega_{10}^2\omega_5\omega_{15} + 25c_s^2\omega_{10}^2\omega_5^2\omega_{15}^2 - 24\omega_{10}\omega_5\omega_{15}^2 - 28\omega_{10}^3\omega_5\omega_{15} - 64v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 28v_2^2\omega_{10}^2\omega_{15}^2 - 20c_s^2\omega_{10}^3\omega_{15} - 43v_2^2\omega_{10}^3\omega_5\omega_{15} - 120v_2^2\omega_{10}^2\omega_5^2\omega_{15} + 12\omega_{10}^3\omega_{15} + 56c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 68v_2^2\omega_{10}^2\omega_5\omega_{15}^2 + 20c_s^2\omega_{10}^2\omega_{15}^2 - 12\omega_{10}^2\omega_{15}^2 - 40\omega_{10}^2\omega_5^2\omega_{15} + 43v_2^2\omega_{10}^2\omega_5^2\omega_{15} - 16v_2^2\omega_{10}^2\omega_5^2 + 16c_s^2\omega_{10}^3\omega_5^2 - 8\omega_{10}^2\omega_5^3 + 16\omega_{10}^2\omega_5\omega_{15} - 32c_s^2\omega_{10}\omega_5^2\omega_{15} + 68v_2^2\omega_{10}^3\omega_5\omega_{15} + 64v_2^2\omega_{10}\omega_5\omega_{15}^2 - 16v_2^2\omega_{10}^2\omega_5 - 32\omega_5^2\omega_{15}^2 - 16c_s^2\omega_{10}^2\omega_5\omega_{15} + 24\omega_{10}\omega_5^2\omega_{15} + 48c_s^2\omega_5^2\omega_{15} + 48\omega_{10}\omega_5^2\omega_{15} - 44c_s^2\omega_{10}^2\omega_5\omega_{15} + 8\omega_{10}^2\omega_5^2 + 17\omega_{10}^2\omega_5\omega_{15} - 16c_s^2\omega_{10}^2\omega_5^2 + 16v_2^2\omega_{10}^3\omega_5^2 - 25c_s^2\omega_{10}^2\omega_5^2\omega_{15} - 72c_s^2\omega_{10}\omega_5^2\omega_{15} + 80v_2^2\omega_5^2\omega_{15}^2 + 28\omega_{10}^2\omega_5\omega_{15} + 8\omega_{10}^3\omega_5 + 104v_2^2\omega_{10}^2\omega_5^2\omega_{15} - 16c_s^2\omega_{10}^3\omega_5) \frac{v_2 v_1 \rho}{4\omega_{10}^3\omega_5^2\omega_{15}^2}$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{MRT2}} = C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{MRT1}}$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{CuLBM1}} = 0$$

$$C_{\text{Dx D}^3\text{y } v_2}^{(2), \text{CuLBM2}} = (36c_s^2\omega_1\omega_2^3 - 120\omega_3v_2^2\omega_1\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 84\omega_3c_s^2\omega_1^3 - 12\omega_1\omega_2^3 - 9\omega_3v_1^2\omega_1^2\omega_2^2 - 66\omega_3v_2^2\omega_1\omega_2^3 + 9v_1^2\omega_1^3\omega_2^2 - 5\omega_3\omega_1^3\omega_2^2 - 5\omega_3v_1^2\omega_1^2\omega_2^3 + 48\omega_3v_2^2\omega_1^3 - 18\omega_3v_1^2\omega_1^3\omega_2 - 9v_1^2\omega_1^2\omega_2^3 - 6v_1^2\omega_1^3\omega_2 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3v_1^2\omega_1^2\omega_2^2 + 5\omega_3\omega_1^2\omega_2^3 - 54\omega_3c_s^2\omega_1\omega_2^2 + 84\omega_3v_2^2\omega_2^3 - 51\omega_3\omega_1^2\omega_2^2 + 6\omega_3v_1^2\omega_1^2\omega_2 - 6v_1^2\omega_1^2\omega_2^2 - 12\omega_3c_s^2\omega_2^3 + 27\omega_3c_s^2\omega_1\omega_2^3 + 42\omega_3\omega_1\omega_2^2 - 9\omega_1^3\omega_2^2 + 27c_s^2\omega_1^3\omega_2^2 - 12\omega_3v_2^2\omega_1^2\omega_2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_2^3 - 15\omega_3c_s^2\omega_1^2\omega_2^2 + 12v_1^2\omega_1\omega_2^3 - 24\omega_3v_1^2\omega_2^3 + 3\omega_3\omega_1\omega_2^3 + 81\omega_3c_s^2\omega_1^2\omega_2^2 - 18\omega_3c_s^2\omega_1^2\omega_2 + 12\omega_3v_1^2\omega_1^3 - 66\omega_3v_2^2\omega_2^3 - 18c_s^2\omega_1^2\omega_2^2 + 27\omega_3v_1^2\omega_1\omega_2^2 + 6\omega_1^2\omega_2^2 + 132\omega_3v_2^2\omega_1^2\omega_2^2 - 18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^3 + 15\omega_3c_s^2\omega_1^3\omega_2^2 + 6\omega_3v_1^2\omega_1\omega_2^2 + 9\omega_1^2\omega_2^2 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3) \frac{v_2 v_1 \rho}{18\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{\text{D}^4\text{y } \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_2^2} :$$

$$C_{\text{D}^4\text{y } \rho}^{(2), \text{SRT}} = (12 + 672c_s^2v_2^2 - 5c_s^4\omega^3 + 90v_2^4\omega^2 + 144v_2^4 - 9v_2^4\omega^3 + 82c_s^4\omega^2 + 144c_s^4 - 216c_s^4\omega - \omega^3 + 8\omega^2 - 216v_2^4\omega - 18\omega - 34c_s^2v_2^2\omega^3 + 10v_2^2\omega^3 - 78c_s^2\omega^2 + 404c_s^2v_2^2\omega^2 + 6c_s^2\omega^3 - 98v_2^2\omega^2 + 234v_2^2\omega - 1008c_s^2v_2^2\omega + 198c_s^2\omega - 132c_s^2 - 156v_2^2) \frac{v_2}{12\omega^3}$$

$$C_{D_y^4 \rho}^{(2), \text{MRT1}} = (12 + 8\omega_{10}^2 + 672c_s^2v_2^2 - 216v_2^4\omega_{10} - 216c_s^4\omega_{10} + 144v_2^4 - \omega_{10}^3 + 144c_s^4 - 18\omega_{10} + 82c_s^4\omega_{10}^2 - 9v_2^4\omega_{10}^3 + 90v_2^4\omega_{10}^2 - 5c_s^4\omega_{10}^3 + 198c_s^2\omega_{10} + 234v_2^2\omega_{10} - 1008c_s^2v_2^2\omega_{10} + 404c_s^2v_2^2\omega_{10}^2 - 98v_2^2\omega_{10}^3 + 6c_s^2\omega_{10}^3 - 34c_s^2v_2^2\omega_{10}^3 - 132c_s^2 - 78c_s^2\omega_{10}^2 + 10v_2^2\omega_{10}^3 - 156v_2^2) \frac{v_2}{12\omega_{10}^3}$$

$$C_{D_y^4 \rho}^{(2), \text{MRT2}} = C_{D_y^4 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(2), \text{CLBM1}} = C_{D_y^4 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(2), \text{CLBM2}} = C_{D_y^4 \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^4 \rho}^{(2), \text{CuLBM1}} = (12 - 34c_s^2v_2^2\omega_5^3 + 672c_s^2v_2^2 - 78c_s^2\omega_5^2 + 10v_2^2\omega_5^3 + 404c_s^2v_2^2\omega_5^2 + 144v_2^4 - 98v_2^2\omega_5^2 + 6c_s^2\omega_5^3 + 144c_s^4 + 234v_2^2\omega_5 - 1008c_s^2v_2^2\omega_5 + 198c_s^2\omega_5 + 90v_2^4\omega_5^2 - 5c_s^4\omega_5^3 - 18\omega_5 + 82c_s^4\omega_5^2 - 9v_2^4\omega_5^3 - \omega_5^3 - 216c_s^4\omega_5 - 216v_2^4\omega_5 + 8\omega_5^2 - 132c_s^2 - 156v_2^2) \frac{v_2}{12\omega_5^3}$$

$$C_{D_y^4 \rho}^{(2), \text{CuLBM2}} = (-8c_s^2\omega_1\omega_2^3 - 176\omega_3v_2^2\omega_1\omega_2^2 + 72\omega_3c_s^4\omega_1\omega_2^2 + 8\omega_3\omega_1^2\omega_2 - 52\omega_3c_s^2\omega_1^3 - 3\omega_3\omega_1^3\omega_2^3 + 404\omega_3c_s^2v_2^2\omega_1^3\omega_2^2 + 328\omega_3v_2^2\omega_1\omega_2^3 + 440\omega_3c_s^2v_2^2\omega_1^2\omega_2 - 102\omega_3c_s^2v_2^2\omega_1^3\omega_2^3 + 8\omega_3\omega_1^3\omega_2^2 - 28\omega_3v_2^2\omega_1^3 - 372\omega_3c_s^4\omega_1\omega_2^3 - 1088\omega_3c_s^2v_2^2\omega_1^2\omega_2^2 + 168\omega_3v_2^4\omega_1\omega_2^2 + 24c_s^4\omega_1\omega_2^3 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 80\omega_3c_s^2\omega_1\omega_2^2 - 160\omega_3v_2^2\omega_2^3 - 16\omega_3\omega_1^2\omega_2^2 - 464\omega_3c_s^2v_2^2\omega_1^3\omega_2 - 300\omega_3v_2^4\omega_1\omega_2^3 + 808\omega_3c_s^2v_2^2\omega_1^3\omega_2^3 - 184\omega_3c_s^2\omega_2^3 + 320\omega_3c_s^2\omega_1\omega_2^3 + 8c_s^2v_2^2\omega_1\omega_2^3 - 15\omega_3c_s^4\omega_1^3\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 72\omega_3c_s^4\omega_1^2\omega_2 + 180\omega_3v_2^4\omega_1^2\omega_2^3 - 1472\omega_3c_s^2v_2^2\omega_1\omega_2^3 + 760\omega_3c_s^2v_2^2\omega_2^3 - 84\omega_3v_2^4\omega_1^3\omega_2 - 48c_s^4\omega_1^2\omega_2^2 - 104\omega_3v_2^2\omega_1^2\omega_2 + 30\omega_3v_2^2\omega_1^3\omega_2^3 + 8c_s^2v_2^2\omega_1^3\omega_2 + 24\omega_3v_2^4\omega_1^3 + 122\omega_3c_s^2\omega_1^3\omega_2 + 16\omega_3\omega_2^3 - 156\omega_3c_s^2\omega_1^2\omega_2^3 + 656\omega_3c_s^2v_2^2\omega_1\omega_2^2 - 264\omega_3v_2^4\omega_1^2\omega_2^2 + 24c_s^4\omega_1^3\omega_2 - 28\omega_3\omega_1\omega_2^2 + 82\omega_3c_s^4\omega_1^3\omega_2^2 + 72\omega_3c_s^4\omega_1^3 - 16c_s^2v_2^2\omega_1^2\omega_2^2 + 152\omega_3c_s^2\omega_1^2\omega_2^2 - 98\omega_3v_2^2\omega_1^3\omega_2^2 - 80\omega_3c_s^2\omega_1^2\omega_2 + 18\omega_3c_s^2\omega_1^3\omega_2^3 + 94\omega_3v_2^2\omega_1^2\omega_2 + 16c_s^2\omega_1^2\omega_2^2 - 196\omega_3v_2^2\omega_1^2\omega_2^3 - 27\omega_3v_2^4\omega_1^3\omega_2^3 + 96\omega_3v_2^4\omega_1^2\omega_2 + 216\omega_3c_s^4\omega_2^3 + 164\omega_3c_s^4\omega_1^2\omega_2^3 - 156\omega_3c_s^4\omega_1^3\omega_2 + 280\omega_3v_2^2\omega_1^2\omega_2^2 - 8c_s^2\omega_1^3\omega_2 - 78\omega_3c_s^2\omega_1^3\omega_2^2 + 160\omega_3c_s^2v_2^2\omega_1^3 - 120\omega_3c_s^4\omega_1^2\omega_2^2 + 4\omega_3\omega_1^3 + 90\omega_3v_2^4\omega_1^3\omega_2^2 + 144\omega_3v_2^4\omega_2^3) \frac{v_2}{36\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_y^4 v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_2^4} :$$

$$C_{D_y^4 v_2}^{(2), \text{SRT}} = (12 + 432c_s^2v_2^2 - c_s^4\omega^3 + 310v_2^4\omega^2 + 504v_2^4 - 29v_2^4\omega^3 + 14c_s^4\omega^2 + 24c_s^4 - 36c_s^4\omega - \omega^3 + 8\omega^2 - 756v_2^4\omega - 18\omega - 18c_s^2v_2^2\omega^3 + 14v_2^2\omega^3 - 22c_s^2\omega^2 + 252c_s^2v_2^2\omega^2 + 2c_s^2\omega^3 - 154v_2^2\omega^2 + 378v_2^2\omega - 648c_s^2v_2^2\omega + 54c_s^2\omega - 36c_s^2 - 252v_2^2) \frac{\rho}{12\omega^3}$$

$$C_{D_y^4 v_2}^{(2), \text{MRT1}} = (12 + 8\omega_{10}^2 + 432c_s^2v_2^2 - 756v_2^4\omega_{10} - 36c_s^4\omega_{10} + 504v_2^4 - \omega_{10}^3 + 24c_s^4 - 18\omega_{10} + 14c_s^4\omega_{10}^2 - 29v_2^4\omega_{10}^3 + 310v_2^4\omega_{10}^2 - c_s^4\omega_{10}^3 + 54c_s^2\omega_{10} + 378v_2^2\omega_{10} - 648c_s^2v_2^2\omega_{10} + 252c_s^2v_2^2\omega_{10}^2 - 154v_2^2\omega_{10}^2 + 2c_s^2\omega_{10}^3 - 18c_s^2v_2^2\omega_{10}^3 - 36c_s^2 - 22c_s^2\omega_{10}^2 + 14v_2^2\omega_{10}^3 - 252v_2^2) \frac{\rho}{12\omega_{10}^3}$$

$$C_{D_y^4 v_2}^{(2), \text{MRT2}} = C_{D_y^4 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(2), \text{CLBM1}} = C_{D_y^4 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(2), \text{CLBM2}} = C_{D_y^4 v_2}^{(2), \text{MRT1}}$$

$$C_{D_y^4 v_2}^{(2), \text{CuLBM1}} = (12 - 18c_s^2v_2^2\omega_5^3 + 432c_s^2v_2^2 - 22c_s^2\omega_5^2 + 14v_2^2\omega_5^3 + 252c_s^2v_2^2\omega_5^2 + 504v_2^4 - 154v_2^2\omega_5^2 + 2c_s^2\omega_5^3 + 24c_s^4 + 378v_2^2\omega_5 - 648c_s^2v_2^2\omega_5 + 54c_s^2\omega_5 + 310v_2^4\omega_5^2 - c_s^4\omega_5^3 - 18\omega_5 + 14c_s^4\omega_5^2 - 29v_2^4\omega_5^3 - \omega_5^3 - 36c_s^4\omega_5 - 756v_2^4\omega_5 + 8\omega_5^2 - 36c_s^2 - 252v_2^2) \frac{\rho}{12\omega_5^3}$$

$$C_{D_y^4 v_2}^{(2), \text{CuLBM2}} = (-8c_s^2\omega_1\omega_2^3 - 240\omega_3v_2^2\omega_1\omega_2^2 + 8\omega_3c_s^4\omega_1\omega_2^2 + 8\omega_3\omega_1^2\omega_2 - 20\omega_3c_s^2\omega_1^3 - 3\omega_3\omega_1^3\omega_2^3 + 252\omega_3c_s^2v_2^2\omega_1^3\omega_2^2 + 552\omega_3v_2^2\omega_1\omega_2^3 + 264\omega_3c_s^2v_2^2\omega_1^2\omega_2 - 54\omega_3c_s^2v_2^2\omega_1^3\omega_2^3 + 8\omega_3\omega_1^3\omega_2^2 - 60\omega_3v_2^2\omega_1^3 - 68\omega_3c_s^4\omega_1\omega_2^3 - 576\omega_3c_s^2v_2^2\omega_1^2\omega_2^2 + 552\omega_3v_2^4\omega_1\omega_2^2 + 8c_s^4\omega_1\omega_2^3 - 10\omega_3\omega_1^3\omega_2 + 16\omega_3\omega_1^2\omega_2^3 - 16\omega_3c_s^2\omega_1\omega_2^2 - 288\omega_3v_2^2\omega_2^3 - 16\omega_3\omega_1^2\omega_2^2 - 360\omega_3c_s^2v_2^2\omega_1^3\omega_2 - 1068\omega_3v_2^4\omega_1\omega_2^3 + 504\omega_3c_s^2v_2^2\omega_1^2\omega_2^2 - 56\omega_3c_s^2\omega_2^3 + 96\omega_3c_s^2\omega_1\omega_2^3 + 24c_s^2v_2^2\omega_1\omega_2^3 - 3\omega_3c_s^4\omega_1^3\omega_2^3 + 8\omega_3\omega_1\omega_2^2 + 8\omega_3c_s^4\omega_1^2\omega_2 + 620\omega_3v_2^2\omega_1^3\omega_2^3 - 1008\omega_3c_s^2v_2^2\omega_1\omega_2^3 + 552\omega_3c_s^2v_2^2\omega_2^3 - 312\omega_3v_2^4\omega_1^3\omega_2 - 16c_s^4\omega_1^2\omega_2^2 - 168\omega_3v_2^2\omega_1^2\omega_2 + 42\omega_3v_2^2\omega_1^3\omega_2^3 + 24c_s^2v_2^2\omega_1^3\omega_2 + 96\omega_3v_2^4\omega_1^3 + 42\omega_3c_s^2\omega_1^3\omega_2 + 16\omega_3\omega_2^3 - 44\omega_3c_s^2\omega_1^2\omega_2^3 + 336\omega_3c_s^2v_2^2\omega_1\omega_2^2 - 888\omega_3v_2^4\omega_1^2\omega_2^2 + 8c_s^4\omega_1^3\omega_2 - 28\omega_3\omega_1\omega_2^2 + 14\omega_3c_s^4\omega_1^3\omega_2^2 + 16\omega_3c_s^4\omega_1^3 - 48c_s^2v_2^2\omega_1^2\omega_2^2 + 24\omega_3c_s^2\omega_1^2\omega_2^2 - 154\omega_3v_2^2\omega_1^3\omega_2^2 - 16\omega_3c_s^2\omega_1^2\omega_2 + 6\omega_3c_s^2\omega_1^3\omega_2^3 + 174\omega_3v_2^2\omega_1^3\omega_2 + 16c_s^2\omega_1^2\omega_2^2 - 308\omega_3v_2^2\omega_1^2\omega_2^3 - 87\omega_3v_2^4\omega_1^3\omega_2^3 + 336\omega_3v_2^4\omega_1^2\omega_2 + 40\omega_3c_s^4\omega_2^3 + 28\omega_3c_s^4\omega_1^2\omega_2^3 - 32\omega_3c_s^4\omega_1^3\omega_2 + 408\omega_3v_2^2\omega_1^2\omega_2^2 - 8c_s^2\omega_1^3\omega_2 - 22\omega_3c_s^2\omega_1^3\omega_2^2 + 144\omega_3c_s^2v_2^2\omega_1^3 - 8\omega_3c_s^4\omega_1^2\omega_2^2 + 4\omega_3\omega_1^3 + 310\omega_3v_2^4\omega_1^3\omega_2^2 + 528\omega_3v_2^4\omega_2^3) \frac{\rho}{36\omega_3\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_x^3 D_z \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3} :$$

$$C_{D_x^3 D_z \rho}^{(2), \text{SRT}} = 0$$

$$C_{D_x^3 D_z \rho}^{(2), \text{MRT1}} = (4\omega_6\omega_{13}\omega_7\omega_5^2\omega_9^2\omega_{12}^2 - 4\omega_6v_1^2\omega_{13}\omega_7\omega_{14}\omega_5\omega_9\omega_{12}^2 + 12c_s^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_5\omega_9\omega_{12}^2 - 4\omega_6v_1^2\omega_{13}\omega_7\omega_{14}\omega_8\omega_9\omega_{12}^2 +$$

$$\begin{aligned}
& 18\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12}^2 + 12\omega_6 \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12}^2 + 6\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 9\omega_6^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 24\omega_6 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12} - \\
& 6\omega_6 v_1^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 \omega_{13} \omega_7^2 \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_8 \omega_5 \omega_9^2 \omega_{12}^2 + 36\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12}^2 - 24c_s^2 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + \\
& 12\omega_6 v_1^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 c_s^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 + 30\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12}^2 - \\
& 6\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 c_s^2 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 54\omega_6 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 - 12\omega_6^2 \omega_{13} \omega_7^2 \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 + 6\omega_6^2 v_1^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12}^2 - \\
& 12\omega_6 c_s^2 \omega_{13} \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 6\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 \omega_{12}^2 - 6\omega_6^2 \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 6\omega_6 v_1^2 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - \\
& 24\omega_6 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 42\omega_6^2 c_s^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 3\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12\omega_6 v_1^2 \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + \\
& 24c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12\omega_6^2 \omega_{13} \omega_7 \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 6\omega_6^2 v_1^2 \omega_{13} \omega_7 \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 v_1^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 + \\
& 12\omega_6 c_s^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 c_s^2 \omega_{13} \omega_7^2 \omega_8 \omega_5 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 c_s^2 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 3\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12}^2 + \\
& 12\omega_6 c_s^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12}^2 + 12\omega_6^2 \omega_{13} \omega_7^2 \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 + 6\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2 - 6\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_9 \omega_{12}^2 + \\
& 12\omega_6 c_s^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9^2 \omega_{12}^2 - 12\omega_6^2 v_1^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2 + 12\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9^2 \omega_{12}^2) \frac{v_2 v_1 \rho}{12\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9^2 \omega_{12}^2}
\end{aligned}$$

$$C_{D_x^3 D_z v_3}^{(2), \text{MRT2}} = C_{D_x^3 D_z v_3}^{(2), \text{MRT1}}$$

$$C_{D_x^3 D_z v_3}^{(2), \text{CLBM1}} = (-3v_1^2 \omega_9 - \omega_{13} + v_1^2 \omega_{13} + v_1^2 \omega_{13} \omega_9 + 3c_s^2 \omega_{13} - 9c_s^2 \omega_9 - \omega_{13} \omega_9 + 3c_s^2 \omega_{13} \omega_9 + 3\omega_9) \frac{v_2 v_1 \rho}{12\omega_{13} \omega_9}$$

$$C_{D_x^3 D_z v_3}^{(2), \text{CLBM2}} = C_{D_x^3 D_z v_3}^{(2), \text{CLBM1}}$$

$$C_{D_x^3 D_z v_3}^{(2), \text{CuLBM1}} = (-3v_1^2 \omega_4 + v_1^2 \omega_{12} + 3c_s^2 \omega_4 \omega_{12} - \omega_4 \omega_{12} + 3\omega_4 - 9c_s^2 \omega_4 + v_1^2 \omega_4 \omega_{12} - \omega_{12} + 3c_s^2 \omega_{12}) \frac{v_2 v_1 \rho}{12\omega_4 \omega_{12}}$$

$$\begin{aligned}
C_{D_x^3 D_z v_3}^{(2), \text{CuLBM2}} &= (9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 - 9v_1^2 \omega_4 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 - \\
& 9\omega_3 v_1^2 \omega_1 \omega_2 + 2\omega_3 v_1^2 \omega_4 \omega_1 - 18\omega_3 v_3^2 \omega_4 \omega_2 + 6\omega_3 v_1^2 \omega_1 \omega_2 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 + 18\omega_3 v_3^2 \omega_4 \omega_1 + 4\omega_3 v_1^2 \omega_4 \omega_2 + 9\omega_3 \omega_1 \omega_2) \frac{v_2 v_1 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y D_z \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2 \partial x_3} :$$

$$C_{D_x^2 D_y D_z \rho}^{(2), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y D_z \rho}^{(2), \text{MRT1}} &= \\
& (3\omega_7^2 \omega_8^2 \omega_5 - 2\omega_7 \omega_8 \omega_5^3 - \omega_7^2 \omega_8^2 \omega_5^2 + \omega_7 \omega_5^3 - \omega_8^2 \omega_5^2 + 2\omega_7 \omega_8^2 \omega_5^2 + \omega_7^2 \omega_8 \omega_5^3 + \omega_8 \omega_5^3 + \omega_7^2 \omega_5^2 - 2\omega_7^2 \omega_8 \omega_5^2 - \omega_7^2 \omega_5^3 - 2\omega_7^2 \omega_8^2 + \omega_7^2 \omega_8 \omega_5 - \omega_7 \omega_8^2 \omega_5) \frac{2v_3 c_s^4}{\omega_7^2 \omega_8^2 \omega_5^3}
\end{aligned}$$

$$C_{D_x^2 D_y D_z \rho}^{(2), \text{MRT2}} = C_{D_x^2 D_y D_z \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x^2 D_y D_z \rho}^{(2), \text{CuLBM2}} &= (-432\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1 \omega_2^2 - 27\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 - 96\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^2 - 56\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 84v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 192\omega_3 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 108\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 54c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 - 72\omega_3^2 v_1^4 \omega_4^2 \omega_1^2 \omega_2 + 27\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + 96\omega_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^2 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2 - 104\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 - 30\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 162\omega_3^2 c_s^4 \omega_1^3 \omega_2^3 - 168\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 + 24c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 60\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^3 + 324\omega_3 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 432\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1 \omega_2^3 - 24\omega_3 c_s^4 \omega_4^2 \omega_1^3 \omega_2 + \\
& 192\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 144\omega_3^2 c_s^4 \omega_4^2 \omega_2^3 + 48\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^3 - 16\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 96\omega_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^3 + 324\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 72\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2 + 56\omega_3 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - \\
& 108\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 56\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1 \omega_2^2 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 + 144\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 + 84c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - 36\omega_3^2 v_1^4 \omega_4^2 \omega_1^3 \omega_2 + 128\omega_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 + \\
& 72\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_2^3 + 54v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 + 54\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 + 108\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 + 30\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - 81\omega_3 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - \\
& 24v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 104\omega_3^2 c_s^2 \omega_4^2 \omega_2^3 + 64\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 + 72\omega_3^2 v_1^4 \omega_4^2 \omega_1^2 \omega_2^2 - 40\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2 + 162c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - 10\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + \\
& 96\omega_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2 + 108\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_2^3 - 64\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 81\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2^3 + 8\omega_3^2 \omega_4^2 \omega_1^3 - 24\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2 + 24\omega_3^2 v_1^4 \omega_4^2 \omega_2^3 + 10\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 - \\
& 432\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2 + 112\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2 - 8\omega_3^2 \omega_4^2 \omega_1^3 \omega_2 + 32\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 - 108\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_2 + 32\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - \\
& 72c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 - 96\omega_3^2 v_1^2 \omega_4^2 \omega_1^3 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_2^3 - 36\omega_3^2 v_1^4 \omega_4^2 \omega_1 \omega_2^3 + 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 432\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^3 - 27\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 - 176\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - \\
& 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2 - 60\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^3 \omega_2 - 168\omega_3 c_s^4 \omega_4^2 \omega_1 \omega_2^3 + 64\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 + 80\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 - 432\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^3 \omega_2 - 216\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_2^3 - \\
& 324\omega_3^2 c_s^4 \omega_4 \omega_2^3 - 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 - 96\omega_3^2 v_1^2 \omega_4^2 \omega_2^3 - 54\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2^3 - 252c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 - 8\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 + 96\omega_3^2 v_1^2 \omega_4^2 \omega_1^3 \omega_2 + \\
& 432\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_2^3 + 108\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 120\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 - 10\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 8\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2 + 864\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + 10\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + \\
& 48\omega_3^2 v_1^4 \omega_4^2 \omega_1^3 - 192\omega_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + 8\omega_3^2 \omega_4^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1 \omega_2^3 + 32\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_2^3 + 27\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 - 24\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_2^3) \frac{v_3}{72\omega_3^2 \omega_4^2 \omega_1^3 \omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_x^2 D_y D_z v_1}^{(2)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^2 \partial x_2 \partial x_3} :$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{SRT}} = 0$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{MRT1}} = (3\omega_7^2 \omega_{14} \omega_8 \omega_5 \omega_{12}^2 + \omega_7^2 \omega_{14} \omega_8^2 \omega_5^3 \omega_{12} + \omega_7^2 \omega_8^2 \omega_5^3 \omega_{12} + 2\omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2 + \omega_7^2 \omega_{14} \omega_5^2 \omega_{12}^2 - 2\omega_7 \omega_8 \omega_5^3 \omega_{12}^2 - \omega_7^2 \omega_{14} \omega_5^2 \omega_{12}^2 + 2\omega_7^2 \omega_8^2 \omega_5^2 \omega_{12}^2 - \omega_7 \omega_{14} \omega_8^2 \omega_5^3 \omega_{12} - \omega_7^2 \omega_{14} \omega_5^3 \omega_{12}^2 - 4\omega_7^2 \omega_{14} \omega_8^2 \omega_{12}^2 - 4\omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12} - \omega_{14} \omega_8^2 \omega_5^2 \omega_{12}^2 - 2\omega_7^2 \omega_8^2 \omega_5^2 \omega_{12} + 2\omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_{12} - \omega_7^2 \omega_8^2 \omega_5^3 \omega_{12}^2 - 2\omega_7 \omega_{14} \omega_8 \omega_5^3 \omega_{12}^2 + 2\omega_7^2 \omega_8 \omega_5^3 \omega_{12}^2 + \omega_7^2 \omega_{14} \omega_8 \omega_5^3 \omega_{12}^2 + 2\omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12} + 2\omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 + 5\omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12}^2 + \omega_{14} \omega_8 \omega_5^3 \omega_{12}^2 + 2\omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_{12}^2 + \omega_7 \omega_{14} \omega_5^3 \omega_{12}^2 - 2\omega_7^2 \omega_8 \omega_5^2 \omega_{12}^2 - 4\omega_7^2 \omega_{14} \omega_8 \omega_5^2 \omega_{12}^2 - \omega_7^2 \omega_{14} \omega_8^2 \omega_5^3 + \omega_7 \omega_8^2 \omega_5^3 \omega_{12}^2 - 3\omega_7 \omega_{14} \omega_8^2 \omega_5 \omega_{12}^2) \frac{v_3 c_s^2 v_1 \rho}{\omega_7^2 \omega_{14} \omega_8^2 \omega_5^3 \omega_{12}^2}$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{MRT2}} = C_{D_x^2 D_y D_z v_1}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_1}^{(2), \text{CuLBM2}} = (-6c_s^2 \omega_1 \omega_2^3 - 4\omega_3 v_3^2 \omega_1^2 \omega_2 + 4v_3^2 \omega_1^2 \omega_2^2 + 14\omega_3 \omega_1^2 \omega_2 + 28\omega_3 c_s^2 \omega_1^3 + 4\omega_3 v_3^2 \omega_2^3 + 2\omega_1 \omega_2^3 + 26\omega_3 v_1^2 \omega_1^2 \omega_2^2 - 2v_3^2 \omega_1^3 \omega_2 - 13\omega_3 v_1^3 \omega_1^3 \omega_2 + 10\omega_3 \omega_1^3 \omega_2 - 24\omega_3 c_s^2 \omega_1 \omega_2^2 - 3\omega_3 v_3^2 \omega_1^3 \omega_2 - 20\omega_3 \omega_1^2 \omega_2^2 - 22\omega_3 v_1^2 \omega_1^2 \omega_2 + 6\omega_3 v_3^2 \omega_1^2 \omega_2^2 + 4\omega_3 v_3^2 \omega_1^3 + 26\omega_3 c_s^2 \omega_2^3 - 24\omega_3 c_s^2 \omega_1 \omega_2^3 + 8\omega_3 \omega_1 \omega_2^2 - 4\omega_3 v_3^2 \omega_1 \omega_2^2 - 24\omega_3 c_s^2 \omega_1^3 \omega_2 - 10\omega_3 \omega_2^3 + 10\omega_3 v_1^2 \omega_2^3 + 10\omega_3 \omega_1 \omega_2^3 + 48\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 3\omega_3 v_3^2 \omega_1 \omega_2^3 - 2v_3^2 \omega_1 \omega_2^3 - 30\omega_3 c_s^2 \omega_1^2 \omega_2 + 16\omega_3 v_1^3 \omega_1^3 + 12c_s^2 \omega_1^2 \omega_2^2 - 13\omega_3 v_1^3 \omega_1 \omega_2^3 - 4\omega_1^2 \omega_2^2 - 6c_s^2 \omega_1^3 \omega_2 - 4\omega_3 v_1^3 \omega_1 \omega_2^2 + 2\omega_1^3 \omega_2 - 12\omega_3 \omega_1^3) \frac{v_3 v_1 \rho}{6\omega_3 \omega_1^3 \omega_2^3}$$

coefficient $C_{D_x^2 D_y D_z v_2}^{(2)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2 \partial x_3}$:

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{MRT1}} = (4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} - 5\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 4\omega_6 \omega_{10}^2 \omega_7 \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 6\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 2\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_{15}^2 + 8\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 8\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_8 \omega_5^3 \omega_{15}^2 - 2\omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 8\omega_6 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 + 2\omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 8\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 2\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} - 8\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} - 8\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 5\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 8\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 2\omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15} - 4\omega_6 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 2\omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}^2 - 2\omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 + 2\omega_6 \omega_{16} \omega_{10}^2 \omega_7 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2 - 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5^3 \omega_{15}^2) \frac{v_3 c_s^2 v_2 \rho}{2\omega_6 \omega_{16} \omega_{10}^2 \omega_7^2 \omega_{17} \omega_8^2 \omega_5^3 \omega_{15}^2}$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{MRT2}} = C_{D_x^2 D_y D_z v_2}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y D_z v_2}^{(2), \text{CuLBM2}} = (9\omega_4 \omega_1 \omega_2 + 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 c_s^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 \omega_4 \omega_2 - 2\omega_3 v_3^2 \omega_4 \omega_2 - 9v_3^2 \omega_4 \omega_1 \omega_2 - 2\omega_3 \omega_4 \omega_1 + 9\omega_3 v_3^2 \omega_1 \omega_2 + 2\omega_3 v_3^2 \omega_4 \omega_1 - 9\omega_3 \omega_1 \omega_2) \frac{v_3 v_2 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y D_z v_3}^{(2)}$ **at** $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_2 \partial x_3}$:

$$C_{D_x^2 D_y D_z v_3}^{(2), \text{SRT}} = (-36 - \omega^3 - 16\omega^2 + 54\omega) \frac{c_s^4 \rho}{12\omega^3}$$

$$C_{D_x^2 D_y D_z v_3}^{(2), \text{MRT1}} = (24\omega_6^2 \omega_{16} v_2^2 \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5^2 \omega_{15} \omega_{12} + 24\omega_6^2 \omega_{16} v_2^2 \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5 \omega_{15} \omega_{12} - 12\omega_6^2 \omega_{16} v_1^2 \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8^3 \omega_{15} \omega_{12} - 12\omega_6 c_s^2 \omega_{16} \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8^2 \omega_5^3 \omega_{12} + 12\omega_6^2 c_s^2 \omega_{16} \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8^2 \omega_5^2 \omega_{15} \omega_{12} + 12\omega_6^2 c_s^2 \omega_{16} \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5^3 \omega_{15} \omega_{12} + 12\omega_6^2 c_s^2 \omega_{16} \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5^2 \omega_{15} \omega_{12} + 12\omega_6^2 c_s^2 \omega_{16} \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5 \omega_{15} \omega_{12} - 12\omega_6^2 c_s^2 \omega_{16} \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5^3 \omega_{15} \omega_{12} - 48\omega_6^2 \omega_{16} v_2^2 \omega_{10} \omega_7^3 \omega_{17} \omega_{14} \omega_8 \omega_5^3 \omega_{15} \omega_{12} -$$

$$C_{D_x D_y^2 D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$\begin{aligned}
& 4\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2 + 6\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 + 3\omega_3^2 v_1^2 \omega_2^2 \omega_2 - 12\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^2 + 20\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 + 3\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 4\omega_3^2 \omega_4 \omega_1 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^3 - \\
& 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + 12\omega_3^2 v_1^2 \omega_4 \omega_1^2 + 3\omega_3^2 v_1^2 \omega_1^2 \omega_2^2 - 3v_1^2 \omega_4 \omega_1^2 \omega_2^2 - 36\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2 - 6\omega_3^2 \omega_1^2 \omega_2^2 - 3\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 + 6\omega_3^2 \omega_4 \omega_1 \omega_2^2 - 6\omega_4 \omega_1^2 \omega_2^2 - \\
& 18\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 - 6\omega_3 \omega_4 \omega_1^2 \omega_2^3 + \omega_3 v_1^2 \omega_4 \omega_1 \omega_2^3 + 6\omega_4 \omega_1^2 \omega_2^3 + \omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^3 + 3\omega_3^2 v_1^2 \omega_2^3 \omega_2 - 12\omega_3^2 v_2^2 \omega_1^2 \omega_2^3 + 4\omega_3 \omega_4 \omega_1^2 \omega_2^3 + 6\omega_3 \omega_4 \omega_1^2 \omega_2^3 - \\
& 3\omega_3^2 v_1^2 \omega_1^2 \omega_2^3 + 3v_3^2 \omega_4 \omega_1^2 \omega_2^3 - 3\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 - 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 2\omega_3 \omega_4 \omega_1^2 \omega_2^3 + 18\omega_3^2 c_s^2 v_1^2 \omega_2^3 - 18c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 2\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 + \\
& 3\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 - 3\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^3 + 6\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2^3 - 3\omega_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 + 28\omega_3^2 c_s^2 \omega_4 \omega_1^2 + 6\omega_3^2 \omega_1^2 \omega_2^3) \frac{v_3 v_1 \rho}{6\omega_3^2 \omega_4 \omega_1^2 \omega_2^3}
\end{aligned}$$

$$C_{D_x D_y^2 D_z v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_y^2 D_z v_3}^{(2), \text{MRT2}} = C_{D_x D_y^2 D_z v_3}^{(2), \text{MRT1}}$$

$$\begin{aligned}
& 432c_s^2\omega_1^2\omega_2^3 - 108\omega_3^2v_2^2\omega_1^2\omega_2^3 + 144\omega_3^2\omega_4\omega_1^2\omega_2^3 - 72\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 63\omega_3\omega_4^2\omega_1^3\omega_2^3 - 432\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 36\omega_3^2v_1^2\omega_4\omega_1^3\omega_2^2 - 48\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 + \\
& 432\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 - 36v_1^2\omega_4^3\omega_1^3\omega_2^2 + 36\omega_3v_2^2\omega_4^3\omega_1^3\omega_2^2 + 216\omega_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 120\omega_3^2c_s^2\omega_1^2\omega_2^3 - 108\omega_3\omega_1^3\omega_2^3 + 180\omega_3^2c_s^2\omega_1^2\omega_2^3 + 144\omega_4^2\omega_1^2\omega_2^3 - \\
& 72\omega_3^2\omega_4\omega_1^2\omega_2^3 - 36\omega_3^2\omega_4\omega_1\omega_2^3 - 36v_2^2\omega_4^3\omega_1^3\omega_2^2 + 24\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^2 - 144\omega_3c_s^2\omega_4^3\omega_1^3\omega_2^2 - 36\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 - 144\omega_3^2\omega_4^3\omega_1^3 - 108\omega_3v_2^2\omega_4\omega_1^3\omega_2^3 - \\
& 60\omega_3^2c_s^2\omega_4^3\omega_1^3\omega_2^2 + 108\omega_3\omega_4\omega_1^3\omega_2^3 - 360\omega_3^2c_s^2\omega_4^3\omega_1^3\omega_2^2 + 20\omega_3^2\omega_4^3\omega_1^3\omega_2^3 + 72\omega_3v_1^2\omega_4^3\omega_1^3\omega_2^2 + 144\omega_3^2\omega_4^3\omega_1^3\omega_2^2 + 324\omega_3c_s^2\omega_4^3\omega_1^3\omega_2^2 + 108\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^2 - \\
& 144\omega_3c_s^2\omega_4^3\omega_1^3\omega_2^2 + 20\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^2 + 54v_2^2\omega_4^3\omega_1^3\omega_2^3 - 36\omega_3^2\omega_4\omega_1\omega_2^3 + 48\omega_3^2v_1^2\omega_4^3\omega_1^3 - 63\omega_3v_1^2\omega_4^3\omega_1^3\omega_2^3 + 72\omega_3^2v_2^2\omega_4^3\omega_1^3\omega_2^2 - 108\omega_3^2\omega_4^3\omega_1^3\omega_2^2 + \\
& 108\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 72\omega_3\omega_4\omega_1\omega_2^3 + 36\omega_3v_2^2\omega_4\omega_1\omega_2^3 + 180\omega_3^2c_s^2\omega_4^3\omega_1^3\omega_2^2 + 96\omega_3^2\omega_4^3\omega_1^3\omega_2^2 - 60\omega_3v_1^2\omega_4^3\omega_1^3\omega_2^2 + 180\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 144\omega_3^2c_s^2\omega_4^3\omega_1^3\omega_2^2 - \\
& 144\omega_3\omega_4\omega_1\omega_2^3 - 36\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 36\omega_3^2v_2^2\omega_4\omega_1\omega_2^2 + 144\omega_3^2v_3^2\omega_4^3\omega_1^3 - 96\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^3 + 324\omega_3c_s^2\omega_4^3\omega_1^3\omega_2^2 - 20\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^3 - 72\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^2 + \\
& 12\omega_3v_2^2\omega_4\omega_1\omega_2^3 + 60\omega_3^2c_s^2\omega_4^3\omega_1^3\omega_2^2 + 12\omega_3\omega_4\omega_1\omega_2^3 + 144\omega_3v_1^2\omega_4^3\omega_1^3\omega_2^2 - 20\omega_3^2\omega_4^3\omega_1^3\omega_2^2 - 24\omega_3v_1^2\omega_4^3\omega_1^3\omega_2^2 + 72\omega_3^2v_1^2\omega_4\omega_1\omega_2^3 - 72v_2^2\omega_4^3\omega_1^3\omega_2^2 - \\
& 36\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^2 + 24\omega_3^2\omega_4^3\omega_1^3\omega_2^2 - 108\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + 36\omega_3^2v_2^2\omega_4\omega_1\omega_2^2 - 54\omega_3^2v_1^2\omega_4^3\omega_1^3\omega_2^2 - 189\omega_3c_s^2\omega_4^3\omega_1^3\omega_2^2 - 48\omega_3^2v_2^2\omega_4\omega_1\omega_2^2) \frac{v_2v_1\rho}{72\omega_3^2\omega_4^3\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_y^3 D_z \rho}^{(2)} \text{ at } \frac{\partial^4 \rho}{\partial x_3^2 \partial x_3} :$$

$$C_{D_y^3 D_z \rho}^{(2), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_y^3 D_z \rho}^{(2), \text{MRT1}} = & (-20\omega_{16}v_2^2\omega_{10}^3\omega_7 + 8\omega_{16}^2v_2^4\omega_{10}^2 - 4v_2^4\omega_{10}^2\omega_7^2 - 144c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 48c_s^2\omega_{16}v_2^2\omega_{10}^2\omega_7 + 4c_s^4\omega_{10}^3\omega_7^2 + 8c_s^4\omega_{16}\omega_{10}^2\omega_7^2 - \\
& 36\omega_{16}^2v_2^4\omega_{10}\omega_7^2 + 4c_s^2\omega_{10}^3\omega_7^2 + 4c_s^2\omega_{16}\omega_{10}^3 - 4v_2^2\omega_{10}^3\omega_7^2 - 16\omega_{16}v_2^4\omega_{10}^3\omega_7^2 - 51c_s^2\omega_{16}v_2^2\omega_{10}^3\omega_7^2 - 20\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 8c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 - \\
& 32\omega_{16}v_2^2\omega_{10}^2\omega_7^2 - 4v_2^4\omega_{10}^2\omega_7^2 + 24\omega_{16}^2v_2^4\omega_{10}^2\omega_7^2 + 24c_s^2v_2^2\omega_{10}^3\omega_7^2 - 13\omega_{16}v_2^4\omega_{10}^3\omega_7^2 + 8c_s^4\omega_{16}\omega_{10}^3\omega_7^2 - 12c_s^4\omega_{16}^2\omega_{10}\omega_7^2 + 4c_s^2\omega_{10}^3\omega_7^2 - 24c_s^2v_2^2\omega_{10}^3\omega_7 + \\
& 4v_2^2\omega_{10}^3\omega_7^2 + 8\omega_{16}v_2^2\omega_{10}^3 + 20\omega_{16}v_2^4\omega_{10}^3\omega_7^2 - 4c_s^2\omega_{10}^3\omega_7^2 + 4c_s^4\omega_{16}\omega_{10}\omega_7^2 - 4c_s^4\omega_{16}\omega_{10}^3\omega_7^2 + 84c_s^2\omega_{16}v_2^2\omega_{10}^3\omega_7^2 - 4c_s^4\omega_{10}^3\omega_7^2 + 36\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - \\
& 4c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 + 16\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 4v_2^4\omega_{10}^2\omega_7^2 - 4c_s^4\omega_{16}\omega_{10}^3 + 20\omega_{16}^2v_2^4\omega_{10}\omega_7^2 - 24c_s^2v_2^2\omega_{10}^2\omega_7^2 + 4v_2^2\omega_{10}^3\omega_7^2 - 36c_s^2\omega_{16}v_2^2\omega_{10}^3 + 32\omega_{16}v_2^4\omega_{10}^2\omega_7^2 + \\
& 13\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 72c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 + 120c_s^2\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 4c_s^2\omega_{16}\omega_{10}\omega_7^2 - 4c_s^4\omega_{10}^3\omega_7^2 - 20\omega_{16}^2v_2^4\omega_{10}^2\omega_7^2 + 36c_s^2\omega_{16}^2v_2^2\omega_{10}^2 - 20\omega_{16}v_2^4\omega_{10}\omega_7^2 - \\
& 24\omega_{16}^2v_2^2\omega_{10}^2 - 84c_s^2\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 + 4c_s^4\omega_{16}^2\omega_{10}^2 - 8c_s^2\omega_{16}\omega_{10}^2\omega_7^2 - 72c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - 8\omega_{16}^2v_2^2\omega_{10}^2 + 96c_s^2\omega_{16}^2v_2^2\omega_{10}^2 - 8c_s^4\omega_{16}^2\omega_{10}^2\omega_7^2 - \\
& 13\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 12c_s^2\omega_{16}\omega_{10}\omega_7^2 - 8c_s^2\omega_{16}\omega_{10}^3\omega_7^2 + 4c_s^2\omega_{16}\omega_{10}^3\omega_7^2 + 20\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 4c_s^2\omega_{16}^2\omega_{10}\omega_7^2 + 20\omega_{16}v_2^2\omega_{10}\omega_7^2 - \\
& 4c_s^2\omega_{16}^2\omega_{10}^2 + 4c_s^4\omega_{16}^2\omega_{10}^2\omega_7^2 + 51c_s^2\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 - 8\omega_{16}v_2^4\omega_{10}^3 + 13\omega_{16}^2v_2^4\omega_{10}^2\omega_7^2 - 4c_s^4\omega_{16}\omega_{10}\omega_7^2 - 8c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2) \frac{v_3}{4\omega_{16}^2\omega_{10}^3\omega_7^2}
\end{aligned}$$

$$C_{D_y^3 D_z \rho}^{(2), \text{MRT2}} = C_{D_y^3 D_z \rho}^{(2), \text{MRT1}}$$

$$C_{D_y^3 D_z \rho}^{(2), \text{CLBM1}} = 0$$

$$C_{D_y^3 D_z \rho}^{(2), \text{CLBM2}} = 0$$

$$C_{D_y^3 D_z \rho}^{(2), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_y^3 D_z \rho}^{(2), \text{CuLBM2}} = & (56\omega_3^2c_s^2\omega_1^3\omega_2 + 5\omega_3^2c_s^2\omega_1^2\omega_2^3 - 24\omega_3^2v_2^2\omega_1^2\omega_2 - 8\omega_3^2v_3^2\omega_1\omega_2^2 + 24\omega_3^2v_3^2v_2^2\omega_1\omega_2^2 - 36\omega_3^2v_2^4\omega_1^3\omega_2 - 36\omega_3^2c_s^4\omega_2^3 - 36\omega_3^2c_s^4\omega_1^2\omega_2 + \\
& 4\omega_3^3\omega_2^3 - 8\omega_3^2v_3^2\omega_1\omega_2^3 - 24\omega_3^2v_2^2\omega_1^2\omega_2^3 - 34\omega_3^2c_s^2\omega_1^2\omega_2^3 + 72\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^3 + 48\omega_3^2v_4^4\omega_2^3 + 6\omega_3^2c_s^4\omega_2^3\omega_2^3 + 96\omega_3^2v_3^2v_2^2\omega_1\omega_2^3 - 12v_3^2c_s^2\omega_2^3\omega_2^3 + \\
& 72\omega_3^2v_4^4\omega_1^2\omega_2^3 + 24\omega_3^2c_s^4\omega_1^2\omega_2^3 + 8\omega_3^2v_3^2c_s^2\omega_1\omega_2^3 - 84\omega_3^2c_s^4\omega_1^3\omega_2^3 + 8\omega_3^2\omega_1\omega_2^3 + 12v_3^2c_s^2\omega_1^2\omega_2^3 + 84\omega_3^2v_2^2\omega_1^2\omega_2^3 + 24\omega_3^2v_2^2\omega_1^2\omega_2^3 + \\
& 24\omega_3^2v_4^4\omega_1^3 - 324\omega_3^2c_s^2v_2^2\omega_1^3\omega_2 + 8\omega_3^2v_3^2c_s^2\omega_1\omega_2^3 + 40\omega_3^2c_s^2\omega_1^2\omega_2^3 - 72\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^3 + 8\omega_3^2\omega_1\omega_2^3 + 22\omega_3^2v_3^2c_s^2\omega_1\omega_2^3 + 42\omega_3^2c_s^4\omega_1^2\omega_2^3 + \\
& 216\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^2 - 5\omega_3^2c_s^2\omega_1^3\omega_2^3 + 216\omega_3^2c_s^2v_2^2\omega_1^3 - 8\omega_3^2c_s^2\omega_1\omega_2^3 - 24\omega_3^2v_2^2\omega_1^2\omega_2^2 - 8\omega_3^2\omega_2^3 + 72\omega_3^2c_s^4\omega_1^3 + 24\omega_3^2v_3^2v_2^2\omega_1^2\omega_2^2 - \omega_3^2\omega_1^2\omega_2^3 - 4\omega_3^2\omega_1^3\omega_2 - \\
& 20\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^2 - 2\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^3 + 24\omega_3^2v_2^2\omega_2^3 + 12c_s^2\omega_1^3\omega_2^2 - 4\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^2 - 216\omega_3^2c_s^2v_2^2\omega_1\omega_2^2 + 4\omega_3^2v_3^2\omega_1^2\omega_2^2 + 16\omega_3^2v_3^2c_s^2\omega_1^3 + 4\omega_3^2c_s^2\omega_1^3\omega_2 + \\
& 18\omega_3^2c_s^2\omega_1^2\omega_2^2 + 48\omega_3^2v_2^2\omega_1\omega_2^2 - 2\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^2 + 36c_s^4\omega_1^3\omega_2^2 + 42\omega_3^2c_s^4\omega_1\omega_2^2 + 24\omega_3^2v_3^2v_2^2\omega_1^2\omega_2^2 + 54\omega_3^2c_s^4\omega_1^3\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2^2 - \omega_3^2v_3^2\omega_1^3\omega_2^2 + \\
& 24\omega_3^2v_3^2v_2^2\omega_1 - 60\omega_3^2v_2^2\omega_1^2\omega_2^2 + 4\omega_3^2c_s^2\omega_1^2\omega_2^2 + 20\omega_3^2c_s^2\omega_2^3 - 4\omega_3^2v_3^2c_s^2\omega_1^3\omega_2^2 + 108\omega_3^2c_s^2v_2^2\omega_1\omega_2^3 - 4\omega_3^2v_3^2\omega_1^3 - 18\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^3 + 4\omega_3^2v_3^2\omega_1^3\omega_2^2 + \\
& \omega_3^2v_3^2\omega_1^2\omega_2^3 + 18\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^2 - 8\omega_3^2c_s^2\omega_1\omega_2^2 - 4\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^2 - 36c_s^4\omega_1^3\omega_2^2 - 72\omega_3^2v_3^2v_2^2\omega_2^3 + 8\omega_3^2v_3^2\omega_2^3 - 48\omega_3^2v_3^2v_2^2\omega_1^3\omega_2 - 72\omega_3^2v_3^4\omega_1\omega_2^2 - \\
& 54\omega_3^2c_s^4\omega_1^2\omega_2^2 - 4\omega_3^2\omega_1^2\omega_2^2 - 52\omega_3^2c_s^4\omega_1^3 - 12\omega_3^2c_s^4\omega_1^3\omega_2 - 24\omega_3^2v_3^2v_2^2\omega_1^3\omega_2^2 - 22\omega_3^2c_s^2\omega_1\omega_2^3 - 12c_s^2\omega_1^2\omega_2^3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^2 + 4\omega_3^2v_3^2\omega_1^2\omega_2^2 - \\
& 48\omega_3^2v_3^2v_2^2\omega_1^2\omega_2^2 + \omega_3^2\omega_1^3\omega_2^2 - 12\omega_3^2c_s^4\omega_1^2\omega_2^2 - 36\omega_3^2v_2^4\omega_1\omega_2^2 - 48\omega_3^2v_2^2\omega_1^3 + 2\omega_3^2v_3^2c_s^2\omega_1^3\omega_2^2 - 20\omega_3^2v_3^2c_s^2\omega_2^3) \frac{v_3}{36\omega_3^2\omega_1^3\omega_2^3}
\end{aligned}$$

$$\text{coefficient } C_{D_y^3 D_z v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_3^2 \partial x_3} :$$

$$C_{D_y^3 D_z v_2}^{(2), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_y^3 D_z v_2}^{(2), \text{MRT1}} = & (68\omega_{16}v_2^2\omega_{10}^3\omega_7 + 8\omega_{10}^2\omega_7^2 + 28\omega_{16}^2\omega_{10}^2\omega_7 + 12\omega_{16}\omega_{10}^3 - 16c_s^2\omega_{10}^2\omega_7^2 - 20c_s^2\omega_{16}\omega_{10}^3 + 16v_2^2\omega_{10}^3\omega_7^2 + 64\omega_{16}^2v_2^2\omega_{10}\omega_7 - 44c_s^2\omega_{16}^2\omega_{10}^2\omega_7 + \\
& 104\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 8\omega_{10}^3\omega_7^2 - 16c_s^2\omega_{10}^3\omega_7^2 - 16v_2^2\omega_{10}^2\omega_7^2 - 28\omega_{16}v_2^2\omega_{10}^3 + 16c_s^2\omega_{10}^3\omega_7^2 + 24\omega_{16}\omega_{10}\omega_7^2 - 120\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 25c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 - \\
& 48\omega_{16}v_2^2\omega_{10}^2\omega_7^2 - 8\omega_{10}^3\omega_7^2 - 16v_2^2\omega_{10}^3\omega_7^2 - 43\omega_{16}v_2^2\omega_{10}^3\omega_7^2 - 32c_s^2\omega_{16}\omega_{10}\omega_7^2 - 17\omega_{16}^2\omega_{10}^2\omega_7^2 + 80\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 + 48\omega_{16}^2\omega_{10}\omega_7^2 + 56c_s^2\omega_{16}\omega_{10}^2\omega_7^2 - \\
& 28\omega_{16}\omega_{10}^3\omega_7 + 28\omega_{16}^2v_2^2\omega_{10}^2 + 43\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 - 72c_s^2\omega_{16}^2\omega_{10}\omega_7^2 + 44c_s^2\omega_{16}\omega_{10}^3\omega_7^2 - 40\omega_{16}\omega_{10}^2\omega_7^2 - 25c_s^2\omega_{16}\omega_{10}^3\omega_7^2 + 16\omega_{16}\omega_{10}^2\omega_7^2 - 68\omega_{16}^2v_2^2\omega_{10}^2\omega_7 + \\
& 32c_s^2\omega_{16}^2\omega_{10}\omega_7^2 - 12\omega_{16}^2\omega_{10}^2 - 64\omega_{16}v_2^2\omega_{10}\omega_7^2 + 20c_s^2\omega_{16}^2\omega_{10}^2 - 16c_s^2\omega_{16}\omega_{10}^2\omega_7^2 + 17\omega_{16}\omega_{10}^3\omega_7^2 - 24\omega_{16}^2\omega_{10}\omega_7^2 - 32\omega_{16}^2\omega_7^2 + 48c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2) \frac{v_3v_2\rho}{4\omega_{16}^2\omega_{10}^3\omega_7^2}
\end{aligned}$$

$$C_{D_y^3 D_z v_2}^{(2), \text{MRT2}} = C_{D_y^3 D_z v_2}^{(2), \text{MRT1}}$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(2), \text{CLBM1}} = 0$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(2), \text{CLBM2}} = 0$$

$$C_{\text{D}_y^3 \text{D}_z v_2}^{(2), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{\text{D}_y^3 \text{D}_z v_2}^{(2), \text{CuLBM2}} = & (36c_s^2\omega_1\omega_2^3 + 6\omega_3v_3^2\omega_1^2\omega_2 - 120\omega_3v_2^2\omega_1\omega_2^2 - 6v_3^2\omega_1^2\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 84\omega_3c_s^2\omega_1^3 - 24\omega_3v_3^2\omega_2^3 - 12\omega_1\omega_2^3 - 6v_3^2\omega_1^3\omega_2 - \\ & 9v_3^2\omega_1^2\omega_2^3 + 5\omega_3v_3^2\omega_2^3\omega_2^2 - 66\omega_3v_2^2\omega_1\omega_2^3 - 5\omega_3\omega_1^3\omega_2^2 + 48\omega_3v_2^2\omega_1^3 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^3 + 9v_3^2\omega_1^3\omega_2^2 - 54\omega_3c_s^2\omega_1\omega_2^2 - 18\omega_3v_3^2\omega_1^3\omega_2 + \\ & 84\omega_3v_2^2\omega_1^3 - 5\omega_3v_3^2\omega_1^2\omega_2^3 - 51\omega_3\omega_1^2\omega_2^2 - 9\omega_3v_2^2\omega_1^2\omega_2^3 + 12\omega_3v_3^2\omega_1^3 - 12\omega_3c_s^2\omega_2^3 + 27\omega_3c_s^2\omega_1\omega_2^3 + 42\omega_3\omega_1\omega_2^3 - 9\omega_1^3\omega_2^3 + 27c_s^2\omega_1^3\omega_2^2 - \\ & 12\omega_3v_2^2\omega_1^2\omega_2 + 6\omega_3v_3^2\omega_1\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_2^3 - 15\omega_3c_s^2\omega_2^2\omega_2^3 + 3\omega_3\omega_1\omega_2^3 + 81\omega_3c_s^2\omega_1^2\omega_2^2 + 27\omega_3v_3^2\omega_1\omega_2^3 + 12v_3^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 - \\ & 66\omega_3v_2^2\omega_1^2\omega_2 - 18c_s^2\omega_1^2\omega_2^2 + 6\omega_1^2\omega_2^2 + 132\omega_3v_2^2\omega_1^2\omega_2^2 - 18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^3 + 15\omega_3c_s^2\omega_1^3\omega_2^2 + 9\omega_1^2\omega_2^3 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3) \frac{v_3v_2\rho}{18\omega_3\omega_1^3\omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{\text{D}_y^3 \text{D}_z v_3}^{(2)} \text{ at } \frac{\partial^4 v_3}{\partial x_3^3 \partial x_3} :$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{SRT}} = (-36c_s^2v_2^2 - c_s^4\omega^3 - 26v_2^4\omega^2 - 36v_2^4 + 4v_2^4\omega^3 + 20c_s^4\omega^2 + 36c_s^4 - 54c_s^4\omega + 54v_2^4\omega + 12c_s^2v_2^2\omega^3 - 4v_2^2\omega^3 - 12c_s^2\omega^2 - 42c_s^2v_2^2\omega^2 + 26v_2^2\omega^2 - 54v_2^2\omega + 54c_s^2v_2^2\omega + 36c_s^2\omega - 24c_s^2 + 36v_2^2) \frac{\rho}{12\omega^3}$$

$$\begin{aligned} C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{MRT1}} = & (24\omega_{16}v_2^3\omega_{10}\omega_7 + 72\omega_{16}v_2^4\omega_7^3 - 60\omega_{16}v_2^2\omega_{10}\omega_7^3 - 108c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - 5c_s^2\omega_{16}^2\omega_{10}^3\omega_7^2 - 21c_s^2\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 12c_s^4\omega_{16}\omega_{10}^2\omega_7^2 - \\ & 12c_s^4\omega_{16}\omega_{10}\omega_7^3 - 27\omega_{16}v_2^4\omega_{10}\omega_7^3 + 12v_2^2\omega_{10}\omega_7^3 + 12c_s^2v_2^2\omega_{10}\omega_7^3 + 30c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 + 24\omega_{16}v_2^2\omega_{10}\omega_7^2 - 12v_2^4\omega_{10}\omega_7^3 - 306c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^3 - \\ & 12c_s^2v_2^2\omega_{10}\omega_7^2 - 12v_2^2\omega_{10}\omega_7^3 + 48\omega_{16}v_2^3\omega_{10}\omega_7^2 + 12c_s^4\omega_{16}\omega_{10}\omega_7^2 - 12c_s^4\omega_{16}\omega_{10}\omega_7^2 - 6c_s^4\omega_{16}\omega_{10}\omega_7^2 - 90\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 60\omega_{16}v_2^2\omega_{10}\omega_7^3 - \\ & 24\omega_{16}v_2^3\omega_{10}\omega_7^2 - 12c_s^2v_2^2\omega_{10}\omega_7^3 - 18c_s^4\omega_{16}\omega_{10}\omega_7^2 - 12c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 + 54c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - 6c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 - c_s^2\omega_{16}^2\omega_{10}\omega_7^3 + 90\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + \\ & 6c_s^2\omega_{16}\omega_{10}\omega_7^3 + 12v_2^2\omega_{10}\omega_7^3 - 24\omega_{16}v_2^4\omega_{10}\omega_7^2 - 48\omega_{16}v_2^3\omega_{10}\omega_7^2 + 12v_2^4\omega_{10}\omega_7^3 - 12c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - c_s^2\omega_{16}^2\omega_{10}\omega_7^3 + 90\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + \\ & 6c_s^2\omega_{16}\omega_{10}\omega_7^2 + 4\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 13c_s^4\omega_{16}\omega_{10}\omega_7^2 + 252c_s^2\omega_{16}^2v_2^2\omega_7^3 - 48c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 12c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 12c_s^4\omega_{16}\omega_7^3 - 12\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - \\ & 12c_s^2\omega_{16}\omega_{10}\omega_7^2 + 12c_s^2\omega_{16}\omega_{10}\omega_7^3 - 19\omega_{16}^2v_2^2\omega_{10}\omega_7^3 - 72\omega_{16}^2v_2^2\omega_7^3 - 36\omega_{16}v_2^2\omega_{10}\omega_7^2 - 48c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - c_s^4\omega_{16}\omega_{10}\omega_7^3 - 18\omega_{16}^2v_2^4\omega_{10}\omega_7^2 - \\ & 12\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 12c_s^2\omega_{16}\omega_{10}\omega_7^2 - 36c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^3 - 12c_s^2\omega_{16}\omega_{10}\omega_7^2 + 6c_s^2\omega_{16}\omega_{10}\omega_7^3 + 12c_s^4\omega_{16}\omega_{10}\omega_7^3 - 81c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 18c_s^2\omega_{16}\omega_{10}\omega_7^3 - \\ & 4\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 102c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 12c_s^2\omega_{16}\omega_7^3 + 19\omega_{16}^2v_2^4\omega_{10}\omega_7^3 + 6c_s^4\omega_{16}\omega_{10}\omega_7^2 + 12\omega_{16}^2v_2^4\omega_{10}\omega_7^2 + 162c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + \\ & 36\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 18\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 6c_s^2\omega_{16}\omega_{10}\omega_7^2 + c_s^4\omega_{16}\omega_{10}\omega_7^2 + 12\omega_{16}^2v_2^4\omega_{10}\omega_7^2 - 24c_s^4\omega_{16}\omega_{10}\omega_7^2) \frac{\rho}{12\omega_{16}^2\omega_{10}\omega_7^3} \end{aligned}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{MRT2}} = C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{MRT1}}$$

$$\begin{aligned} C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{CLBM1}} = & (72\omega_{16}^2v_2^4\omega_7^3 - 72\omega_{16}v_2^2\omega_{10}\omega_7^3 - 36c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 5c_s^2\omega_{16}^2\omega_{10}^3\omega_7^2 - 99c_s^2\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 12c_s^4\omega_{16}\omega_{10}^2\omega_7^2 - 12c_s^4\omega_{16}\omega_{10}\omega_7^3 - \\ & 39\omega_{16}v_2^4\omega_{10}\omega_7^3 + 36v_2^2\omega_{10}\omega_7^3 + 108c_s^2v_2^2\omega_{10}\omega_7^3 + 54c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - 36v_2^4\omega_{10}\omega_7^3 - 306c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^3 - 108c_s^2v_2^2\omega_{10}\omega_7^2 - 36v_2^2\omega_{10}\omega_7^3 + \\ & 36\omega_{16}v_2^2\omega_{10}\omega_7^2 + 12c_s^4\omega_{16}\omega_{10}\omega_7^2 - 12c_s^4\omega_{16}\omega_{10}\omega_7^2 - 6c_s^4\omega_{16}\omega_{10}\omega_7^2 - 90\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 72\omega_{16}v_2^2\omega_{10}\omega_7^3 - 108c_s^2v_2^2\omega_{10}\omega_7^3 - 18c_s^4\omega_{16}\omega_{10}\omega_7^2 + \\ & 36c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 + 198c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - 6c_s^2\omega_{16}\omega_{10}\omega_7^2 - 36v_2^2\omega_{10}\omega_7^2 + 39\omega_{16}v_2^2\omega_{10}\omega_7^3 + 6c_s^4\omega_{16}\omega_{10}\omega_7^3 + 36v_2^2\omega_{10}\omega_7^3 - 36\omega_{16}v_2^2\omega_{10}\omega_7^2 + \\ & 36v_2^4\omega_{10}\omega_7^3 + 36c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 - c_s^2\omega_{16}^2\omega_{10}\omega_7^3 + 90\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 6c_s^2\omega_{16}\omega_{10}\omega_7^2 + 4\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 13c_s^4\omega_{16}\omega_{10}\omega_7^2 + 252c_s^2\omega_{16}^2v_2^2\omega_7^3 + \\ & 12c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^3 + 12c_s^2\omega_{16}\omega_7^3 - 12c_s^2\omega_{16}\omega_{10}\omega_7^2 + 12c_s^2\omega_{16}\omega_{10}\omega_7^3 - 19\omega_{16}^2v_2^2\omega_{10}\omega_7^3 - 72\omega_{16}^2v_2^2\omega_7^3 - 36\omega_{16}v_2^2\omega_{10}\omega_7^3 - c_s^4\omega_{16}\omega_{10}\omega_7^3 - \\ & 6\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 12c_s^2\omega_{16}\omega_{10}\omega_7^2 - 108c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^3 - 12c_s^2\omega_{16}\omega_{10}\omega_7^2 + 6c_s^2\omega_{16}\omega_{10}\omega_7^3 + 12c_s^4\omega_{16}\omega_{10}\omega_7^3 - 3c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 18c_s^2\omega_{16}\omega_{10}\omega_7^2 - \\ & 4\omega_{16}^2v_2^2\omega_{10}\omega_7^3 - 18c_s^2\omega_{16}v_2^2\omega_{10}\omega_7^2 + 60c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^3 - 12c_s^2\omega_{16}\omega_7^3 + 19\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 6c_s^4\omega_{16}\omega_{10}\omega_7^2 + 18c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 36\omega_{16}v_2^2\omega_{10}\omega_7^2 + \\ & 6\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 6c_s^2\omega_{16}\omega_{10}\omega_7^3 + c_s^4\omega_{16}\omega_{10}\omega_7^3 - 24c_s^4\omega_{16}\omega_{10}\omega_7^3) \frac{\rho}{12\omega_{16}^2\omega_{10}\omega_7^3} \end{aligned}$$

$$C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{CLBM2}} = C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{CLBM1}}$$

$$\begin{aligned} C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{CuLBM1}} = & (19\omega_3^3v_2^4\omega_{11}\omega_5^2 + 6\omega_3^2v_2^2\omega_{11}\omega_5^3 + 12\omega_3^2c_s^2\omega_{11}\omega_5^3 - 3\omega_3^2c_s^2v_2^2\omega_{11}\omega_5^3 + 13\omega_3^2c_s^4\omega_{11}\omega_5^3 - \omega_3^3c_s^2\omega_{11}\omega_5^2 + 72\omega_3^3v_2^4\omega_{11}^2 + \\ & 198\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^2 - 12\omega_3^3c_s^4\omega_{11}\omega_5^2 + 18\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^2 - 12\omega_3^3c_s^2\omega_{11}\omega_5^3 + 4\omega_3^3v_2^4\omega_{11}\omega_5^3 + 12\omega_3^3c_s^4\omega_{11}\omega_5^3 - 99\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^3 + 90\omega_3^3v_2^2\omega_{11}\omega_5^2 - \\ & 18\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^3 + 6\omega_3^3c_s^4\omega_{11}\omega_5^2 - 6\omega_3^3v_2^4\omega_{11}\omega_5^3 - 19\omega_3^3v_2^2\omega_{11}\omega_5^2 - 12\omega_3^3c_s^4\omega_{11}\omega_5^2 - 36\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^2 + \omega_3^3c_s^4\omega_{11}\omega_5^2 - 36\omega_3^3v_2^4\omega_5^3 - 5\omega_3^3c_s^2\omega_{11}\omega_5^3 + \\ & 12\omega_3^3c_s^2\omega_{11}\omega_5^2 - 4\omega_3^3v_2^2\omega_{11}\omega_5^3 + 36\omega_3^3v_2^2\omega_5^3 + 12\omega_3^3c_s^4\omega_{11}\omega_5^3 - 108\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^2 - 90\omega_3^3v_2^4\omega_{11}\omega_5^2 + 36\omega_3^3v_2^4\omega_5^3 - 6\omega_3^3c_s^2\omega_{11}\omega_5^2 - \omega_3^3c_s^4\omega_{11}\omega_5^3 + \\ & 108\omega_3^3c_s^2v_2^2\omega_5^3 - 30\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^2 - 24\omega_3^3c_s^4\omega_{11}\omega_5^3 + 39\omega_3^3v_2^2\omega_{11}\omega_5^3 - 12\omega_3^3c_s^2\omega_{11}\omega_5^2 - 36\omega_3^3v_2^4\omega_{11}\omega_5^2 + 6\omega_3^3c_s^4\omega_{11}\omega_5^3 - 12\omega_3^3c_s^2\omega_{11}\omega_5^2 - \\ & 72\omega_3^3v_2^2\omega_{11}\omega_5^2 + 36\omega_3^3v_2^4\omega_{11}\omega_5^3 - 108\omega_3^3c_s^2v_2^2\omega_5^3 + 18\omega_3^3c_s^2\omega_{11}\omega_5^3 - 6\omega_3^3c_s^4\omega_{11}\omega_5^2 - 72\omega_3^3v_2^2\omega_{11}^2 + 36\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^2 - 39\omega_3^3v_2^4\omega_{11}\omega_5^3 - 36\omega_3^3v_2^4\omega_5^3 + \\ & 6\omega_3^3c_s^2\omega_{11}\omega_5^3 + 36\omega_3^3v_2^2\omega_{11}\omega_5^2 + 12\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^3 + 36\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^3 + 12\omega_3^3c_s^4\omega_{11}\omega_5^2 - 36\omega_3^3v_2^2\omega_5^3 - 6\omega_3^3c_s^2\omega_{11}\omega_5^3 - 36\omega_3^3v_2^2\omega_{11}\omega_5^3 + 252\omega_3^3c_s^2v_2^2\omega_{11}^2 + \\ & 72\omega_3^3v_2^4\omega_{11}\omega_5^2 - 108\omega_3^3c_s^2v_2^2\omega_5^3 + 54\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^3 + 6\omega_3^3c_s^2\omega_{11}\omega_5^3 + 12c_s^4\omega_{11}\omega_5^3 - 18\omega_3^3c_s^4\omega_{11}\omega_5^3 + 36\omega_3^3v_2^2\omega_5^2 + 60\omega_3^3c_s^2v_2^2\omega_{11}\omega_5^3) \frac{\rho}{12\omega_3^3\omega_{11}\omega_5^3} \end{aligned}$$

$$\begin{aligned} C_{\text{D}_y^3 \text{D}_z v_3}^{(2), \text{CuLBM2}} = & (48\omega_3^3v_2^4\omega_4\omega_1^3 + 24\omega_3v_2^2\omega_4\omega_1^3\omega_2 - 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 36\omega_3^2v_2^4\omega_4\omega_1^3\omega_2^2 + 162\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 - 96\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 216\omega_3v_2^2\omega_4\omega_1^2\omega_2^3 + \\ & 40\omega_3^3c_s^4\omega_4\omega_1^2\omega_2^2 - 36v_2^4\omega_4\omega_1^3\omega_2^2 - 492\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 - 288\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 - 54\omega_3^2v_2^2\omega_1^3\omega_2^3 - 108\omega_3^2v_2^4\omega_1\omega_2^3 + 6\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 24\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 - \\ & 40\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 240\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 86\omega_3^2c_s^4\omega_4\omega_1^2\omega_2^2 - 297\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 108\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^3 - 28\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^2 + 72\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 48\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^3 - \\ & 492\omega_3^2c_s^2v_2^2\omega_4\omega_1^3\omega_2^2 - 144\omega_3^2v_2^2\omega_4\omega_1^2\omega_2^2 + 54v_2^4\omega_4\omega_1^3\omega_2^2 - 288\omega_3^2v_2^2\omega_4\omega_1^3\omega_2^2 + 174\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 + 432\omega_3^2c_s^2v_2^2\omega_4\omega_1^2\omega_2^2 - 117\omega_3^2v_2^4\omega_4\omega_1^3\omega_2^2 - \end{aligned}$$

coefficient $C_{D_x^2 D_z^2 \rho}^{(2)}$ at $\frac{\partial^4 \rho}{\partial x_1^2 \partial x_3^2}$:

[illegible]

$$C_{D_x^2 D_z^2 \rho}^{(2), \text{MRT2}} = C_{D_x^2 D_z^2 \rho}^{(2), \text{MRT1}}$$

$$C_{D_x^2 D_z^2 \rho}^{(2), \text{CLBM2}} = C_{D_x^2 D_z^2 \rho}^{(2), \text{CLBM1}}$$

$$C_{D_2^2 D_2^2 \rho}^{(2), \text{CuLBM2}} = (3v_1^2\omega_1 - 3v_1^2\omega_2 + 6c_s^2\omega_1\omega_2 - 2\omega_1 + 3v_3^2\omega_1 - 14c_s^2\omega_2 + 2\omega_2 + 2c_s^2\omega_1 - 3v_3^2\omega_2) \frac{c_s^2 v_2}{36\omega_1\omega_2}$$

$$C_{D_2^2 D_2^2 v_1}^{(2), \text{SRT}} = (28c_s^2 v_2 v_1 \omega^2 - 24c_s^2 v_2^2 + 36v_2^3 v_2^2 \omega - 2c_s^2 v_2 v_1 \omega^3 + 36v_2^3 c_s^2 \omega - 14v_2^3 c_s^2 \omega^2 + v_2^3 v_2^2 \omega^3 + 48c_s^2 v_2 v_1 - 24v_2^3 v_2^2 - 14v_2^3 v_2^2 \omega^2 + v_2^3 c_s^2 \omega^3 -$$

[illegible]

[illegible]

$$C_{D_x^2 D_y^2 v_3}^{(2), CLBM1} = (2\omega_{19}c_s^2v_2w_7\omega_{14}w_8\omega_5\omega_{12} + 2\omega_{19}c_s^2v_1w_7\omega_{20}w_{14}w_8 + 4\omega_{19}c_s^2v_1w_7\omega_{20}w_5\omega_{12} - 2\omega_{19}c_s^2v_2w_7\omega_{20}w_8\omega_5 + 4\omega_{19}v_2v_1^2w_7\omega_{20}w_{14}w_5\omega_{12} - 4\omega_{19}c_s^2v_1w_{14}w_5\omega_{12} - 2\omega_{19}v_2v_1^2w_7\omega_{20}w_8\omega_5 - 2v_2v_1^2w_{20}w_{14}w_8\omega_5\omega_{12} + \omega_{19}v_2^2v_1w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} + 4\omega_{19}c_s^2v_2w_7\omega_{20}w_8 + 2\omega_{19}c_s^2v_1w_7\omega_{14}w_8\omega_{12} + 4\omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_5\omega_{12} + 4\omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_5\omega_{12} + 4\omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_5\omega_{12} - 4\omega_{19}v_2^2v_1w_7\omega_{20}w_8 + 2\omega_{19}v_2v_1^2w_7\omega_{14}w_8\omega_5\omega_{12} + 4\omega_{19}v_2v_1^2w_7\omega_{14}w_{12} - \omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} - 4\omega_{19}v_2^2v_1w_7\omega_{20}w_5\omega_{12} + 4\omega_{19}v_2^2v_1w_7\omega_{20}w_{14}w_{12} - 4\omega_{19}v_2^2v_1w_7\omega_{20}w_{12} - 2c_s^2v_2w_{20}w_{14}w_8\omega_5\omega_{12} + 2\omega_{19}v_2^2v_1w_8\omega_5\omega_{12} + \omega_{19}c_s^2v_1w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} + 2\omega_{19}v_2v_1^2w_7\omega_{20}w_{14}w_8\omega_{12} - 4\omega_{19}v_2^2v_1w_{14}w_5\omega_{12} + 2\omega_{19}v_2^2v_1w_7\omega_{20}w_8\omega_5 + 2\omega_{19}v_2v_1^2w_2w_{14}w_8\omega_5\omega_{12} + 4\omega_{19}c_s^2v_1w_7\omega_{20}w_8\omega_{12} - \omega_{19}c_s^2v_1w_7\omega_{20}w_{14}w_8\omega_5 - 4c_s^2v_1w_{14}w_8\omega_5\omega_{12} - 2c_s^2v_2w_7\omega_{14}w_8\omega_5\omega_{12} - 2\omega_{19}v_2^2v_1w_7\omega_{20}w_8\omega_5\omega_{12} + 4\omega_{19}c_s^2v_1w_2w_{14}w_5\omega_{12} - 4\omega_{19}c_s^2v_1w_2w_5\omega_{12} + 2\omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_8\omega_{12} + 4\omega_{19}c_s^2v_1w_7\omega_{14}w_5\omega_{12} - 4\omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_{12} - 2\omega_{19}c_s^2v_1w_7\omega_{20}w_8\omega_5\omega_{12} + 2\omega_{19}c_s^2v_2w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} - 2\omega_{19}v_2v_1^2w_7\omega_{14}w_8\omega_5\omega_{12} - 4\omega_{19}v_2v_1^2w_7\omega_{20}w_{14}w_{12} - 2\omega_{19}c_s^2v_2w_7\omega_{20}w_8\omega_5\omega_{12} - \omega_{19}v_2^2v_1w_7\omega_{20}w_{14}w_8\omega_5 + 4\omega_{19}c_s^2v_1w_{14}w_8\omega_5\omega_{12} - \omega_{19}v_2v_1^2w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} - 4\omega_{19}c_s^2v_1w_7\omega_{20}w_{12} + 2c_s^2v_1w_{20}w_{14}w_8\omega_5\omega_{12} - 4\omega_{19}v_2^2v_1w_7\omega_{20}w_8 - 4\omega_{19}c_s^2v_2w_{20}w_{14}w_5\omega_{12} + 4\omega_{19}v_2v_1^2w_2w_5\omega_{12} - 4\omega_{19}v_2v_1^2w_7\omega_{20}w_8\omega_{12} - 4\omega_{19}v_2v_1^2w_7\omega_{14}w_{12} - 2\omega_{19}v_2^2v_1w_7\omega_{14}w_8\omega_5\omega_{12} + 4c_s^2v_2w_{14}w_8\omega_5\omega_{12} + 4\omega_{19}c_s^2v_2w_2w_5\omega_{12} + 4\omega_{19}c_s^2v_2w_7\omega_{20}w_{12} - 4\omega_{19}v_2v_1^2w_2w_{14}w_5\omega_{12} - 4\omega_{19}c_s^2v_1w_7\omega_{20}w_{14}w_5\omega_{12} - 4\omega_{19}c_s^2v_2w_7\omega_{20}w_8\omega_{12} - v_2^2v_1w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} + 4v_2v_1^2w_{14}w_8\omega_5\omega_{12} + c_s^2v_2w_7\omega_{20}w_{14}w_8\omega_5\omega_{12} + 4\omega_{19}v_2v_1^2w_7\omega_{20}w_{12} + 2\omega_{19}v_2^2v_1w_7\omega_{20}w_{14}w_8 + 4\omega_{19}v_2^2v_1w_7\omega_{20}w_5\omega_{12} - 4\omega_{19}c_s^2v_2w_{14}w_8\omega_5\omega_{12} + 2\omega_{19}c_s^2v_1w_2w_8\omega_5\omega_{12} -$$

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$$\begin{aligned}
C_{\text{D}_x \text{D}_y \text{D}_z^2 v_3}^{(2), \text{MRT}^2} &= C_{\text{D}_x \text{D}_y \text{D}_z^2 v_3}^{(2), \text{MRT}^1} \\
C_{\text{D}_x \text{D}_y \text{D}_z^2 v_3}^{(2), \text{CLBM1}} &= \\
&(4w_{19}v_3c_s^2w_{16}v_{10}w_{23}w_{20}w_{17}w_8w_5w_{15} - 2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{15} + 2w_{19}c_s^2w_{16}v_{10}^2w_{17}w_{23}w_{20}w_8w_5w_{15} - 2w_{19}v_3^2v_{10}^2w_{10}w_{20}w_{17}w_8w_5w_{15} + \\
&4w_{19}v_3c_s^2v_{10}w_{10}w_{20}w_{17}w_8w_5w_{15} + 2w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{17}w_{23}w_{17}w_8w_5w_{15} - w_{19}c_s^2w_{16}v_{10}^2w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - 2w_{19}c_s^2v_{10}^2w_{10}w_{20}w_{17}w_8w_5w_{15} - \\
&2w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - 2w_{19}v_3c_s^2w_{16}v_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5 - 2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8w_5w_{15} + \\
&2w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} - 4w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{23}w_{20}w_{17}w_5w_{15} - 4w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{23}w_{20}w_8w_5w_{15} - \\
&2v_3c_s^2w_{16}v_{10}w_{10}w_{17}w_{23}w_{17}w_8w_5w_{15} - 4w_{19}v_3v_{10}^2v_{10}w_{10}w_{17}w_{20}w_{17}w_8w_5w_{15} - 2w_{16}v_{10}^2v_{10}^2w_{10}w_{23}w_{17}w_8w_5w_{15} + 2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_5w_{15} + \\
&2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8w_5 + 2w_{19}c_s^2v_{10}^2w_{10}w_{17}w_{20}w_{17}w_8w_5w_{15} - 2w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8 - 4w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_5w_{15} + \\
&2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{23}w_{17}w_8w_5w_{15} - 2c_s^2w_{16}v_{10}^2w_{10}w_{23}w_{17}w_8w_5w_{15} - 2w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8 - w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} + \\
&2w_{19}c_s^2w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_{15} - 2w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8w_5w_{15} + 4w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_8w_5w_{15} - \\
&w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} + 2w_{19}v_3w_{16}v_{10}^2v_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - 2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8 + \\
&2w_{16}v_{10}^2v_{10}w_{10}w_{23}w_{20}w_{17}w_8w_5w_{15} + w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{17}w_8w_5w_{15} + w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_8w_5w_{15} - 4w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{17}w_{23}w_{20}w_8w_{15} - \\
&2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{23}w_{17}w_5w_{15} - 4w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{20}w_{17}w_8w_5w_{15} + w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_8w_{15} - w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} - \\
&w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_8w_5w_{15} + 4v_3w_{16}v_{10}^2v_{10}w_{10}w_{23}w_{17}w_8w_5w_{15} + c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_8w_5w_{15} + w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} + \\
&4w_{19}v_3v_{10}^2v_{10}w_{10}w_{23}w_{20}w_8w_5w_{15} - 2w_{19}c_s^2v_{10}^2w_{10}w_{23}w_{20}w_8w_5w_{15} + 2c_s^2w_{16}v_{10}^2w_{10}w_{23}w_{20}w_{17}w_8w_5w_{15} + w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} - \\
&2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{23}w_{20}w_{17}w_8w_5w_{15} - 2w_{19}w_{16}v_{10}^2v_{10}w_{10}w_{23}w_{20}w_5w_{15} + 4w_{19}v_3v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} + \\
&4w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_5w_{15} - 2w_{19}c_s^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{20}w_{17}w_8w_5w_{15} - \\
&w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5 + 4w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{15} + 4w_{19}v_3c_s^2w_{16}v_{10}w_{10}w_{23}w_{17}w_5w_{15} - 2w_{19}w_{16}v_{10}^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8w_5 + \\
&2w_{19}c_s^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_8w_5w_{15} - 2w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_5 + 2w_{19}c_s^2v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - 4w_{19}v_3v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_8w_5w_{15} - \\
&4w_{19}v_3v_{10}^2v_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - 4w_{19}v_3c_s^2w_{16}v_{10}^2v_{10}w_{10}w_{20}w_{17}w_8w_5w_{15} + c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_5w_{15} - w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{20}w_{17}w_8w_5w_{15} - \\
&2w_{19}c_s^2v_{10}^2w_{10}w_{23}w_{20}w_8w_5w_{15} - 4w_{19}v_3w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_8w_{15} + w_{19}c_s^2w_{16}v_{10}^2w_{10}w_{17}w_{23}w_{17}w_8w_{15} + 4w_{19}v_3c_s^2v_{10}w_{10}w_{23}w_{20}w_8w_5w_{15} - \\
&2w_{19}c_s^2w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} - 2w_{19}c_s^2w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} - 2w_{19}c_s^2w_{16}v_{10}^2v_{10}w_{10}w_{17}w_{23}w_{20}w_{17}w_8w_{15} - \\
&2w_{19}c_s^2w_{16}v_{10}^2v_{10}w_{1$$

coefficient $C_{D_y^2 D_z^2 v_2}^{(2)}$ at $\frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2}$:

[illegible]

$$C_{D_2^2 D_2^2 v_2}^{(2), CLBM1} = (-18\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 24\omega_{19}c_s^2\omega_{16}\omega_{10}^3\omega_7^3\omega_{23} + 12\omega_{19}c_s^2\omega_{10}^3\omega_7^3\omega_{23} + 36\omega_{19}v_2^2\omega_{10}\omega_7^3 + 18\omega_{19}\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 12c_s^2\omega_{16}\omega_{10}^3\omega_7^3\omega_{23} - 6\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 6\omega_{19}\omega_{16}\omega_{10}^3\omega_7^3 + 12\omega_{19}c_s^2\omega_{10}^3\omega_7^3\omega_{23} - 36\omega_{19}\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 36\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 18\omega_{16}v_2^2\omega_{10}\omega_7^3\omega_{23} - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 18\omega_{19}c_s^2\omega_{16}\omega_{10}^3\omega_7^3\omega_{23} + 12\omega_{19}\omega_{16}v_2^2\omega_{10}^3\omega_7^3 + 18\omega_{19}\omega_{16}v_2^2\omega_{10}\omega_7^3\omega_{23} - 18\omega_{19}\omega_{16}v_2^2\omega_{10}\omega_7^3\omega_{23} + 36\omega_{19}v_2^2\omega_{10}^3\omega_7^3\omega_{23} - 12\omega_{19}v_2^2\omega_{10}^3\omega_7^3\omega_{23} + 12\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 12\omega_{19}\omega_{10}^3\omega_7^3 + 6c_s^2\omega_{16}\omega_{10}^3\omega_7^3\omega_{23} - 24\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_{10}\omega_7^3\omega_{23} - 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3 - 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23} + 12\omega_{19}c_s^2\omega_{10}\omega_7^3 + 24\omega_{19}\omega_{10}^3\omega_7^3\omega_{23} - 72\omega_{19}v_2^2\omega_{10}^3\omega_7^3\omega_{23} + 72\omega_{19}\omega_{16}v_2^2\omega_{10}\omega_7^3\omega_{23} - 36\omega_{19}\omega_{16}v_2^2\omega_7^3\omega_{23} + 12\omega_{19}\omega_{10}^3\omega_7^3 - 36\omega_{16}v_2^2\omega_{10}^3\omega_7^3\omega_{23} + 12\omega_{19}\omega_{16}\omega_7^3\omega_{23} + 36\omega_{19}v_2^2\omega_{10}^3\omega_7^3\omega_{23} - 12\omega_{19}\omega_{16}v_2^2\omega_{10}\omega_7^3\omega_{23} + 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3 - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}^3\omega_7^3 + 12\omega_{19}c_s^2\omega_{16}\omega_{10}^3\omega_7^3\omega_{23} + 6\omega_{16}v_2^2\omega_{10}^3\omega_7^3 - 12\omega_{19}\omega_{10}\omega_7^3\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23} + 36\omega_{19}v_2^2\omega_{10}\omega_7^3\omega_{23} - 12\omega_{16}v_2^2\omega_{10}^3\omega_7^3 - 6c_s^2\omega_{16}\omega_{10}^3\omega_7^3 - 12\omega_{19}c_s^2\omega_{10}\omega_7^3 + 6\omega_{19}c_s^2\omega_{16}\omega_{10}^3\omega_7^3 + 36\omega_{19}v_2^2\omega_{10}^3\omega_7^3 - 24\omega_{19}c_s^2\omega_{10}^3\omega_7^3\omega_{23} - 4\omega_{19}c_s^2\omega_{16}\omega_{10}^3\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23} - 18\omega_{19}\omega_{16}v_2^2\omega_{10}\omega_7^3\omega_{23} - 36\omega_{19}v_2^2\omega_{10}^3\omega_7^3 - 36\omega_{19}v_2^2\omega_{10}\omega_7^3\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^3\omega_{23} + 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3) \frac{c_s^2 \rho}{12\omega_{19}\omega_{16}\omega_{10}^3\omega_7^3\omega_{23}}$$

$$C_{D_2^2 D_2^2 v_2}^{(2), \text{CuLBM1}} = (18\omega_3 c_s^2 \omega_{11} \omega_5^2 + 24\omega_3^2 c_s^2 \omega_5 - 36\omega_3 v_2^2 \omega_{11} \omega_5 + 72\omega_3^2 v_2^2 \omega_5 - 72\omega_3^2 v_2^2 \omega_5^2 - 12\omega_3 \omega_5^2 - 12\omega_3^2 c_s^2 \omega_{11} - 24\omega_3^2 c_s^2 \omega_5^2 - 12\omega_3^2 \omega_{11} \omega_5 - 12\omega_3 c_s^2 \omega_{11} \omega_5 - 12c_s^2 \omega_{11} \omega_5^2 - 36\omega_3^2 v_2^2 \omega_{11} + 24\omega_3^3 \omega_5 - 72\omega_3^3 v_2^2 \omega_5 + 36\omega_3 v_2^2 \omega_5^2 + 12\omega_3^2 \omega_{11} - 12\omega_3^3 - 4\omega_3^2 c_s^2 \omega_{11} \omega_5^2 + 12\omega_3 c_s^2 \omega_5^2 + 12\omega_3 v_2^2 \omega_{11} \omega_5 + 24\omega_3^2 \omega_5^2 - 24\omega_3^2 c_s^2 \omega_5 + 36\omega_3^2 v_2^2 \omega_{11} \omega_5 - 24\omega_3^2 \omega_5 + 12\omega_3^2 c_s^2 \omega_5^2 + 36\omega_3^3 v_2^2 + 12\omega_3^2 c_s^2 \omega_{11} \omega_5 - \omega_3^2 c_s^2 \omega_{11} \omega_5^2 - 12\omega_3 \omega_5^2 + 36\omega_3^3 v_2^2 \omega_5^2 + 12\omega_3^2 c_s^2) \frac{c_s^2 \rho}{12\omega_3^2 \omega_{11} \omega_5^2}$$

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coefficient $C_{D_y^2 D_z^2 v_3}^{(2)}$ at $\frac{\partial^4 v_3}{\partial x_2^2 \partial x_3^2}$:

$$\begin{aligned} & 4w_{19}^2c_{16}^2w_{16}w_{10}^3w_{11} + 2w_{19}w_{16}^3c_{16}^2w_{10}^3w_{11} - 4w_{19}c_{16}^2w_{16}^2w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} - 2w_{19}^2w_{16}^3w_{10}^3w_{11} - 4w_{19}^3w_{10}^3w_{23}w_{11} + \\ & 7w_{19}^4w_{16}^3w_{10}^3w_{23}w_{11} + 4w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} + 2w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} + w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} + 2w_{19}^4c_{16}^2w_{16}^3w_{10}^3w_{11} + \\ & 8w_{19}^4c_{16}^2w_{10}^3w_{23}w_{11} + 11w_{19}^4c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 6w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} - 2w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} - 3w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} + \\ & 4w_{19}^4w_{10}^3w_{23}w_{11} + 4w_{19}^4w_{16}w_{10}^3w_{23}w_{11} - 4w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} + w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} - 15w_{19}^4c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 2w_{19}^4c_{16}^2w_{16}^2w_{10}^3w_{23}w_{11} - 8w_{19}^4c_{16}^2w_{10}^3w_{23}w_{11} + 3w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} - 16w_{19}^4c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 2w_{19}^4w_{16}^2w_{10}^3w_{23}w_{11} - \\ & 2w_{19}^4c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 2w_{19}w_{16}^3w_{10}^3w_{23}w_{11} + 2w_{19}w_{16}^3w_{10}^3w_{23}w_{11} - w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 2w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + 2w_{19}w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 8w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + 4w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + 5w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} - 8w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 2w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 8w_{19}^2c_{16}^2w_{10}^3w_{23}w_{11} - 2w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 5w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 4w_{19}^2w_{10}^3w_{23}w_{11} + 2w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} - \\ & 2w_{19}w_{16}^3w_{10}^3w_{23}w_{11} - w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 2w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 2w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - \\ & 4w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + 8w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 6w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + \\ & 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + 3w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 2w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + 26w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 6w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 24w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 4w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} - 2w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - \\ & 7w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 5w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + 3w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + 13w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 4w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 12w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + 4c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + \\ & 9w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} - 6w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} + 2w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} - 2w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11} + 2w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - \\ & 3w_{19}^2w_{16}^2w_{10}^3w_{23}w_{11} + 4w_{19}^2c_{16}^2w_{16}^3w_{10}^3w_{23}w_{11} - 4w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11}) \frac{w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11}}{2w_{19}^2w_{16}^3w_{10}^3w_{23}w_{11}} \end{aligned}$$

$$\begin{aligned} & (-18c_s^2\omega_1\omega_2^3 + 6\omega_3v_3^2\omega_1^2\omega_2 - 12\omega_3v_2^2\omega_1\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 84\omega_3c_s^2\omega_1^3 - 114\omega_3v_3^2\omega_1^2\omega_2^3 + 6\omega_1\omega_2^3 + 50\omega_3v_3^2\omega_1^3\omega_2^2 - 9\omega_3v_2^2\omega_1\omega_2^3 - 23\omega_3\omega_1^3\omega_2^2 + \\ & 12\omega_3v_2^2\omega_1^3 + 48\omega_3\omega_1^3\omega_2 + 23\omega_3\omega_1^3\omega_2^3 - 6v_2^2\omega_1\omega_2^3 - 75\omega_3v_3^2\omega_1^3\omega_2 + 12\omega_3v_2^2\omega_2^3 - 50\omega_3v_2^2\omega_1^2\omega_2^3 + 12\omega_3\omega_1^2\omega_2^2 - 66\omega_3v_3^2\omega_1^2\omega_2^3 + 48\omega_3v_3^2\omega_1^3 - 66\omega_3c_s^2\omega_2^3 + \\ & 108\omega_3c_s^2\omega_1\omega_2^3 - 12\omega_3\omega_1\omega_2^2 - 12\omega_3v_2^2\omega_1^2\omega_2 + 60\omega_3v_3^2\omega_1\omega_2^2 + 12v_2^2\omega_1^2\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 + 42\omega_3\omega_2^3 - 42\omega_3c_s^2\omega_1^2\omega_2^3 - 60\omega_3\omega_1\omega_2^3 - 6v_2^2\omega_1^3\omega_2 + \\ & 141\omega_3v_3^2\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_1^2\omega_2 - 9\omega_3v_2^2\omega_1^3\omega_2 + 36c_s^2\omega_1^2\omega_2^2 - 12\omega_1^2\omega_2^2 + 18\omega_3v_2^2\omega_1^2\omega_2^2 - 18c_s^2\omega_1^3\omega_2 + 42\omega_3c_s^2\omega_1^3\omega_2^2 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3) \frac{v_3v_2\rho}{18\omega_3\omega_1^3\omega_2^3} \end{aligned}$$

[illegible]

$$42\omega_6^2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} - 36\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 12\omega_6\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 12\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 12\omega_6^2\omega_{19}^2\omega_7\omega_{11}^2\omega_8\omega_5^2\omega_{18} - 6\omega_6^2\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_5^2\omega_{18} - 6\omega_6\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 12\omega_6^2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 12\omega_6^2\omega_{19}^2\omega_7\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} + 3\omega_6^2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} + 12\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 12\omega_6\omega_{19}^2\omega_7^2\omega_{11}^2\omega_8\omega_5^2\omega_{18} - 6\omega_6^2\omega_{19}^2\omega_7\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} + 12\omega_6^2\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} + \omega_6^2\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} + 6\omega_6^2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2 - 12\omega_6^2\omega_{19}^2\omega_7\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18} - 6\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5\omega_{18} - 6\omega_6^2\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2 + 6\omega_6^2\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2 - 24\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5\omega_{18}) \frac{v_3v_2\rho}{12\omega_6^2\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8^2\omega_5^2\omega_{18}}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{MRT}^2} = C_{D_x D_z^3 v_1}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CLBM}^1} = (v_3^2\omega_{11}\omega_{18} - 9c_s^2\omega_{11} - 3v_3^2\omega_{11} + 3\omega_{11} + 3c_s^2\omega_{18} - \omega_{11}\omega_{18} + 3c_s^2\omega_{11}\omega_{18} + v_3^2\omega_{18} - \omega_{18}) \frac{v_3v_2\rho}{12\omega_{11}\omega_{18}}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CLBM}^2} = C_{D_x D_z^3 v_1}^{(2), \text{CLBM}^1}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CuLBM}^1} = (-3\omega_6v_3^2 + 3\omega_6 + 3\omega_6c_s^2\omega_8 + v_3^2\omega_8 - 9\omega_6c_s^2 + 3c_s^2\omega_8 - \omega_6\omega_8 + \omega_6v_3^2\omega_8 - \omega_8) \frac{v_3v_2\rho}{12\omega_6\omega_8}$$

$$C_{D_x D_z^3 v_1}^{(2), \text{CuLBM}^2} = (9\omega_4\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 + 6\omega_3v_3^2\omega_4\omega_1\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 + 18\omega_3v_1^2\omega_4\omega_1 + 4\omega_3v_3^2\omega_4\omega_2 - 9v_3^2\omega_4\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 - 9\omega_3v_3^2\omega_1\omega_2 + 2\omega_3v_3^2\omega_4\omega_1 - 18\omega_3v_1^2\omega_4\omega_2 + 9\omega_3\omega_1\omega_2) \frac{v_3v_2\rho}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x D_z^3 v_2}^{(2)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_2}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{MRT}^1} = (5\omega_{19}^2c_s^2\omega_7^3\omega_{20}\omega_8\omega_5^2 - 2\omega_{19}^2c_s^2\omega_7^3\omega_8\omega_5^2 + \omega_{19}^2v_3^2\omega_7^3\omega_{20}\omega_8\omega_5^2 + 2\omega_{19}^2\omega_7^3\omega_8\omega_5^2 - \omega_{19}^2\omega_7\omega_{20}\omega_8^2\omega_5^2 + 13\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2v_3^2\omega_7^3\omega_8\omega_5^2 + \omega_{19}^2v_3^2\omega_7\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2\omega_7^3\omega_{20}\omega_8\omega_5^2 + 2\omega_{19}^2c_s^2\omega_7^3\omega_{20}\omega_8\omega_5^2 + 4\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8\omega_5 + 2\omega_{19}^2v_3^2\omega_7^3\omega_8\omega_5^2 + 2\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2c_s^2\omega_7^3\omega_{20}\omega_8\omega_5 - 2\omega_{19}^2v_3^2\omega_7^3\omega_8\omega_5^2 - 6\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_8^2\omega_5 + 2\omega_{19}^2c_s^2\omega_7^2\omega_8\omega_5^2 - \omega_{19}^2v_3^2\omega_7^3\omega_{20}\omega_8\omega_5^2 + \omega_{19}^2\omega_7^3\omega_{20}\omega_8\omega_5 - 11\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8\omega_5^2 - 7\omega_{19}^2c_s^2\omega_7^3\omega_{20}\omega_8\omega_5 - 2\omega_{19}^2v_3^2\omega_7\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2v_3^2\omega_7^3\omega_{20}\omega_8\omega_5 + \omega_{19}^2\omega_7^2\omega_{20}\omega_8\omega_5^2 + 2\omega_{19}^2c_s^2\omega_7^3\omega_8\omega_5 + \omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2\omega_7^3\omega_8\omega_5 - \omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 - 8\omega_{19}^2c_s^2\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2v_3^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2v_3^2\omega_7^3\omega_8\omega_5^2 - 5\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2c_s^2\omega_7^3\omega_8\omega_5 + v_3^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2 + \omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + c_s^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5 + \omega_{19}^2\omega_7^3\omega_8\omega_5 - 2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5 - 4\omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2\omega_{20}\omega_8^2\omega_5^2 + 2\omega_{19}^2c_s^2\omega_7^2\omega_8\omega_5^2 - 2\omega_{19}^2\omega_7^2\omega_8\omega_5^2 - \omega_{19}^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2 - 2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5 - \omega_{19}^2\omega_7^2\omega_{20}\omega_8^2\omega_5 + \omega_{19}^2c_s^2\omega_7^3\omega_8\omega_5^2 + 2\omega_{19}v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + 4\omega_{19}v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + 4\omega_{19}c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 - \omega_{19}^2\omega_7^3\omega_8\omega_5^2 + \omega_{19}c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5 + 2\omega_{19}v_3^2\omega_7^3\omega_8\omega_5 + \omega_{19}v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + 6\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_8\omega_5^2 + 2\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_5^2 + 7\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5 - 2c_s^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2 + \omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5 - 2v_3^2\omega_7^2\omega_{20}\omega_8^2\omega_5^2) \frac{v_3v_1\rho}{2\omega_{19}^2\omega_7^3\omega_{20}\omega_8^2\omega_5^2}$$

$$C_{D_x D_z^3 v_2}^{(2), \text{MRT}^2} = C_{D_x D_z^3 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CLBM}^1} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CLBM}^2} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CuLBM}^1} = 0$$

$$C_{D_x D_z^3 v_2}^{(2), \text{CuLBM}^2} = (2\omega_3\omega_4^2\omega_1 + 18\omega_3c_s^2\omega_4^2 + 2\omega_3^2v_1^2\omega_4\omega_1 + 3v_1^2\omega_4^2\omega_1 + 12\omega_3v_3^2\omega_4 - 2\omega_3^2\omega_4\omega_1 - 18\omega_3c_s^2\omega_4\omega_1 + 6\omega_3^2v_1^2 + 12\omega_4^2 - 3\omega_3^2v_1^2\omega_1 - 6\omega_3^2v_1^2\omega_4 - 6v_1^2\omega_4^2 + 3v_3^2\omega_4^2\omega_1 + 36\omega_3c_s^2\omega_4 - 2\omega_3v_1^2\omega_4^2\omega_1 + 6\omega_3^2\omega_4 - 6\omega_3^2v_3^2 - 12\omega_3\omega_4 + 18c_s^2\omega_7^2\omega_1 + 6\omega_3^2c_s^2\omega_4\omega_1 - 36c_s^2\omega_4^2 - 18\omega_3^2c_s^2\omega_4 - 6\omega_4^2\omega_1 - 6\omega_3c_s^2\omega_4^2\omega_1 + 6\omega_3v_1^2\omega_4^2 - 6v_3^2\omega_4^2 + 3\omega_3^2v_3^2\omega_1 + 6\omega_3\omega_4\omega_1 - 6\omega_3\omega_4^2 - 6\omega_3v_3^2\omega_4\omega_1) \frac{v_3v_1\rho}{8\omega_3^2\omega_4^2\omega_1}$$

$$\text{coefficient } C_{D_x D_z^3 v_3}^{(2)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 v_3}^{(2), \text{SRT}} = 0$$

$$C_{D_x D_z^3 v_3}^{(2), \text{MRT}^1} = (-4\omega_6\omega_{19}^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 24\omega_6\omega_{19}v_3^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 12\omega_6\omega_{19}^2v_3^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5 - 4\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8 - 24\omega_6\omega_{19}^2v_3^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 2\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} + 4\omega_6\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5 - 12\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8 - 4\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} - 12\omega_6\omega_{19}v_3^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_{18} + 12\omega_6\omega_{19}^2v_3^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} + 8\omega_6\omega_{19}c_s^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_5\omega_{18} - 4\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 12\omega_6\omega_{19}^2v_3^2\omega_7\omega_{11}^2\omega_8\omega_5\omega_{18} - 2\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5 - 8\omega_6\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 4\omega_6\omega_{19}c_s^2\omega_7\omega_{20}\omega_{11}^2\omega_8\omega_{18} + 4\omega_6\omega_{19}^2c_s^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_{18} - 4\omega_6\omega_{19}^2c_s^2\omega_7\omega_{11}^2\omega_8\omega_5\omega_{18} + 6\omega_6\omega_{19}v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_{18} + 6\omega_6\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} + 2\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 6\omega_6\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_{18} + 2\omega_6\omega_{19}c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_{18} + 4\omega_6\omega_{19}^2\omega_7\omega_{20}\omega_{11}\omega_8\omega_5 + 2\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_5\omega_{18} - 2\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_{18} - 9\omega_6\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_5 - 3\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_5 + 4\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8\omega_5 + 4\omega_6\omega_{19}^2c_s^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_{18} - 2\omega_6\omega_{19}^2\omega_7^2\omega_{20}\omega_{11}^2\omega_8 + 12\omega_{19}^2v_3^2\omega_7^2\omega_{20}\omega_{11}\omega_8\omega_{18} -$$

$$6\omega_{19}^2 v_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{11}^2 - 12\omega_{19}\omega_{16}v_{16}^2 \omega_{10}\omega_7^2 \omega_{11}^2 + 18\omega_{19}^2 c_s^2 \omega_{16}v_{16}^2 \omega_{10}\omega_7^2 \omega_{11}^2 - 36\omega_{19}c_s^2 \omega_{16}v_{16}^2 \omega_{10}\omega_7^2 \omega_{23}\omega_{11}) \frac{v_3}{12\omega_{19}^2 \omega_{16}^2 \omega_{10}^2 \omega_7^2 \omega_{23}^2 \omega_{11}^2}$$

$$C_{DyD\varphi}^{(2),CLB M1} = (-9\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} + 12\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{11} + 36\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{7}\omega_{11} - 18\omega_{19}^2c_s^2\omega_{16}\omega_{7}^2\omega_{11} - 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} - 3\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} + 6\omega_{19}^2\omega_{16}\omega_{7}^2\omega_{11} - 12\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 6\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} + 18c_s^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} - 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23} - 12\omega_{19}^2\omega_{10}\omega_{7}\omega_{11} + 36\omega_{19}^2c_s^2\omega_{10}\omega_{7}^2\omega_{23} + 36\omega_{19}^2c_s^2\omega_{10}\omega_{7}\omega_{11} + 12\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} - 12\omega_{19}\omega_{16}\omega_{10}\omega_{7}\omega_{11} - 36\omega_{19}^2c_s^2\omega_{10}\omega_{7}^2\omega_{23} - 18\omega_{19}\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{23} - 12\omega_{19}^2v_3^2\omega_{10}\omega_{7}\omega_{23} - 12\omega_{19}^2\omega_{10}\omega_{7}^2\omega_{11} - 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}\omega_{11} + 6\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{11} - 15\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23} - 12\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{11} - 5\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23} + 12\omega_{19}^2v_3^2\omega_{7}^2\omega_{11} + 5\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23} + 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}\omega_{11} + 18\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{23} + 6\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{11} + 54\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}\omega_{23} - 6\omega_{19}^2v_3^2\omega_{16}\omega_{7}^2\omega_{11} + 18\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{11} - 6\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} - 12\omega_{19}^2v_3^2\omega_{10}\omega_{7}^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_{23}\omega_{11} + 3\omega_{19}\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} - 6\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{11} - 18\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}\omega_{23} - 12\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} + 12\omega_{19}^2v_3^2\omega_{10}\omega_{7}^2\omega_{23} + 12\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} + \omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 18\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 12\omega_{19}^2\omega_{7}^2\omega_{23} + 3\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11} + 54\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 12\omega_{19}^2\omega_{10}\omega_{7}\omega_{11} + 12\omega_{19}^2\omega_{10}\omega_{7}\omega_{23} - 12\omega_{19}^2v_3^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - 36\omega_{19}^2c_s^2\omega_{10}\omega_{7}^2\omega_{11} - 36\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} - 36\omega_{19}^2c_s^2\omega_{10}\omega_{7}\omega_{23} - 36c_s^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} + 18\omega_{19}^2c_s^2\omega_{16}\omega_{7}^2\omega_{23} - 18\omega_{19}^2c_s^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{11} - 6\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{11} - 12v_3^2\omega_{16}\omega_{10}\omega_{7}\omega_{23}\omega_{11} - 6\omega_{19}^2\omega_{16}\omega_{7}^2\omega_{23} - \omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11}) \frac{v_3c_s^2}{12\omega_{19}^2\omega_{16}\omega_{10}\omega_{7}^2\omega_{23}\omega_{11}}$$

$$C_{D_y D_z \rho}^{(2), \text{CuLBM1}} = (12\omega_2^2 - 36\omega_6\omega_3c_s^2\omega_1 - 3\omega_6\omega_3^2v_3^2\omega_1 - \omega_6\omega_3^2\omega_1^2 + 3\omega_6\omega_3^2c_s^2\omega_1^2 + 12\omega_6\omega_3 + 6\omega_3^2v_3^2\omega_1^2 - 12\omega_6\omega_3v_3^2 + 6\omega_3^2\omega_1 + 36\omega_3c_s^2\omega_1 - \omega_3^2\omega_1^2 + 18\omega_3c_s^2\omega_1^2 + 12\omega_3v_3^2\omega_1 - 9\omega_6\omega_3^2c_s^2\omega_1 - 6\omega_6\omega_3^2 + \omega_6\omega_3^2v_3^2\omega_1^2 + 3\omega_6\omega_3^2\omega_1 + 3\omega_3^2c_s^2\omega_1^2 - 6\omega_3^2v_3^2\omega_1 - 12v_3^2\omega_1^2 - 18\omega_6\omega_3\omega_1 - 6\omega_3\omega_1^2 + 54\omega_6\omega_3c_s^2\omega_1 - 12\omega_6v_3^2\omega_1 + 12\omega_6\omega_1 + 36\omega_6c_s^2\omega_1^2 - 12\omega_6\omega_3v_3^2\omega_1^2 + 18\omega_6\omega_3^2v_3^2\omega_1 - 36\omega_6c_s^2\omega_1 - 12\omega_3\omega_1 + 6\omega_6\omega_3^2v_3^2 + 12\omega_6v_3^2\omega_1^2 - 36\omega_6\omega_3c_s^2\omega_1^2 - 12\omega_6\omega_1^2 + \omega_3^2v_3^2\omega_1^2 + 18\omega_6\omega_3^2c_s^2 + 12\omega_6\omega_3\omega_1^2 - 18\omega_3^2c_s^2\omega_1 - 36c_s^2\omega_1^2) \frac{v_3^2c_s^2\omega_1^2}{12\omega_6\omega_3^2\omega_1^2}$$

coefficient $C_{D_y D_z^3 v_2}^{(2)}$ at $\frac{\partial^4 v_2}{\partial x_2 \partial x_3^3}$:

[illegible]

$$C_{D_y D_z^3 v_3}^{(2), CLMB1} = (-5\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 54\omega_{19}v_3^3\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 18\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23} + 18\omega_{19}v_3^3\omega_{16}\omega_7^3\omega_{23} - 3\omega_{19}v_3^3\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{10}\omega_7^2\omega_{23} + 5\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23} + 12\omega_{19}\omega_{10}\omega_7^3\omega_{11} - 54v_3^3\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} - 18c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} - 36\omega_{19}v_3^3\omega_{10}\omega_7^3\omega_{11} - 6\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11} - 12\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 12\omega_{19}\omega_{10}\omega_7^2\omega_{11} - 18\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 36\omega_{19}v_3^3\omega_7^3\omega_{23} + 12\omega_{19}c_s^2\omega_{10}\omega_7^2\omega_{23} - 15\omega_{19}v_3^3\omega_{16}\omega_{10}\omega_7^2\omega_{23} - 5\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23} + 12\omega_{19}\omega_7^3\omega_{23} + 12\omega_{19}c_s^2\omega_7^2\omega_{11} + 36\omega_{19}v_3^3\omega_7^2\omega_{11} - 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{11} - 36\omega_{19}v_3^3\omega_{10}\omega_7^2\omega_{23} + 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_7^3\omega_{23} + 18\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 18v_3^3\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11} + \omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{23}\omega_{11} + 6c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11} - 12\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 36\omega_{19}v_3^3\omega_7^3\omega_{11} - 18v_3^3\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 12\omega_{19}\omega_{10}\omega_7^2\omega_{23} + 12\omega_{19}\omega_{16}\omega_{10}\omega_7\omega_{23} - 6c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{11} +$$

$$12\omega_{19}\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}c_s^2\omega_{10}\omega_7^3\omega_{11} - \omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11} + 6\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^3\omega_{11} - 12\omega_{19}\omega_7^3\omega_{11} + 18\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_7^3\omega_{11} + 6\omega_{19}\omega_{16}\omega_7^3\omega_{11} + 18\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} + 36\omega_{19}v_3^2\omega_{10}\omega_7^3\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_{23}\omega_{11} + 12c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7\omega_{23} - 12\omega_{19}c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 36\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_7\omega_{23} - 36\omega_{19}v_3^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} + 36v_3^2\omega_{16}\omega_{10}\omega_7\omega_{23}\omega_{11} - 18\omega_{19}v_3^2\omega_{16}\omega_7^3\omega_{11} + 12\omega_{19}c_s^2\omega_{10}\omega_7^2\omega_{11} + 36v_3^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 6\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{11} + 12c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{11} - 12\omega_{19}\omega_{10}\omega_7^3\omega_{23} + 6\omega_{16}\omega_{10}\omega_7^3\omega_{11}) \frac{c_s^2\rho}{12\omega_{19}\omega_{16}\omega_{10}\omega_7^3\omega_{23}\omega_{11}}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CLBM2}} = C_{D_y D_z^2 v_3}^{(2), \text{CLBM1}}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CuLBM1}} = (12\omega_6\omega_3c_s^2 - 3\omega_6\omega_3^2v_3^2\omega_{10} - 12\omega_6\omega_3 + 3\omega_3^3v_3^2\omega_{10} + 36\omega_6\omega_3v_3^2 - 6\omega_3^2\omega_{10} - 12\omega_3c_s^2\omega_{10} - 6\omega_6\omega_3^3 + \omega_3^3c_s^2\omega_{10} - 36\omega_3v_3^2\omega_{10} - 5\omega_6\omega_3^2c_s^2\omega_{10} + 18\omega_6\omega_3^2 - \omega_3^3\omega_{10} + \omega_6\omega_3^2\omega_{10} + 18\omega_6\omega_3^2v_3^2 + 18\omega_3^2v_3^2\omega_{10} + 6\omega_3^3 + 36\omega_3^2v_3^2 + 18\omega_6\omega_3c_s^2\omega_{10} + 12\omega_3^2c_s^2 - 12\omega_3^3 + 6\omega_6\omega_3^3c_s^2 - 18\omega_3^3v_3^2 - 12\omega_6c_s^2\omega_{10} - \omega_6\omega_3^3c_s^2\omega_{10} + 12\omega_3\omega_{10} - 54\omega_6\omega_3^2v_3^2 - 18\omega_6\omega_3^2c_s^2 + 6\omega_3^2c_s^2\omega_{10} - 6\omega_3^3c_s^2) \frac{c_s^2\rho}{12\omega_6\omega_3^3\omega_{10}}$$

$$C_{D_y D_z^2 v_3}^{(2), \text{CuLBM2}} = (94\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 90\omega_3v_3^2c_s^2\omega_4\omega_1^2\omega_2^2 - 4\omega_3\omega_4\omega_1\omega_2^2 - 222\omega_3v_3^2\omega_4\omega_1\omega_2^2 + 40\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 + 8c_s^4\omega_4\omega_1^3\omega_2 + 138\omega_3v_3^4\omega_4\omega_1^3\omega_2^2 - 18c_s^4\omega_4\omega_1^2\omega_2^3 - 24\omega_3c_s^2\omega_4\omega_1^3\omega_2^2 + 12\omega_3v_3^2\omega_4\omega_1\omega_2^2 + 14\omega_3\omega_4\omega_1\omega_2^3 - 288\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2 - 153\omega_3v_3^2c_s^2\omega_4\omega_1^2\omega_2^3 - 28\omega_3c_s^4\omega_4\omega_1\omega_2^2 - 312\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 24v_3^2c_s^2\omega_4\omega_1\omega_2^3 + 16\omega_3c_s^4\omega_4\omega_1^3 - 16\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 + \omega_3v_3^4\omega_4\omega_1^3\omega_2^2 + 20c_s^4\omega_4\omega_1^2\omega_2^2 + 192\omega_3v_3^4\omega_4\omega_1^2\omega_2 + 36\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 6\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 - \omega_3v_3^4\omega_4\omega_1^2\omega_2^3 - 68\omega_3c_s^4\omega_4\omega_1^3 - 168\omega_3v_3^4\omega_4\omega_1^2\omega_2^2 + 144\omega_3v_3^2c_s^2\omega_4\omega_1^3 + 9c_s^4\omega_4\omega_1^3\omega_2^3 + 108\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 153\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^2 - 240\omega_3v_3^4\omega_4\omega_1^3\omega_2 - 18c_s^4\omega_4\omega_1^2\omega_2^2 - 138\omega_3v_3^4\omega_4\omega_1^2\omega_2^3 + 42\omega_3c_s^2\omega_4\omega_1^3\omega_2 - 20\omega_3c_s^2\omega_4\omega_1^2\omega_2^2 + 24\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 120\omega_3v_3^2c_s^2\omega_4\omega_1^2\omega_2 - 8c_s^4\omega_4\omega_1\omega_2^3 - 36\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 9\omega_3c_s^4\omega_4\omega_1^2\omega_2^3 + 408\omega_3v_3^4\omega_4\omega_1\omega_2^3 - 264\omega_3v_3^4\omega_4\omega_1^2\omega_2^3 - 54\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 3\omega_3c_s^2v_3^2\omega_4\omega_1^2\omega_2^3 + 17\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 + 27v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 8\omega_3\omega_4\omega_1^2\omega_2^2 - 81\omega_3v_3^2\omega_4\omega_1^3\omega_2^2 - 8c_s^2\omega_4\omega_1^3\omega_2^2 + 18c_s^2\omega_4\omega_1^2\omega_2^3 + 36\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 32\omega_3c_s^2\omega_4\omega_1\omega_2^2 - 60\omega_3v_3^2\omega_4\omega_1^3 - 24\omega_3v_3^4\omega_4\omega_1\omega_2^2 - 96\omega_3v_3^2\omega_4\omega_1^2\omega_2 - 20c_s^2\omega_4\omega_1^2\omega_2^2 + 8\omega_3c_s^4\omega_4\omega_1^2\omega_2 + 7\omega_3\omega_4\omega_1^3\omega_2^2 + 4\omega_3\omega_4\omega_1^3 - 54v_3^2c_s^2\omega_4\omega_1^3\omega_2^2 - \omega_3v_3^2\omega_4\omega_1^3\omega_2^2 - 3\omega_3c_s^4\omega_4\omega_1^3\omega_2^2 - 108\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 84\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 - 9c_s^2\omega_4\omega_1^2\omega_2^2 - 9\omega_3c_s^2\omega_4\omega_1^2\omega_2^3 + 432\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 10\omega_3\omega_4\omega_1^3\omega_2 + 10\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 54v_3^2c_s^2\omega_4\omega_1^2\omega_2^3 + \omega_3v_3^2\omega_4\omega_1^2\omega_2^3 + 144\omega_3v_3^2\omega_4\omega_1^2\omega_2^3 + 24v_3^2c_s^2\omega_4\omega_1^3\omega_2^2 - 7\omega_3\omega_4\omega_1^2\omega_2^2 - 36\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 8\omega_3\omega_4\omega_1^3 - 4\omega_3\omega_4\omega_1^2\omega_2^2 - 32\omega_3c_s^4\omega_4\omega_1^3\omega_2 + 27\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^2 + 60v_3^2c_s^2\omega_4\omega_1^2\omega_2^2 - 29\omega_3c_s^4\omega_4\omega_1^2\omega_2^2 - 60\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^2 + 18c_s^2\omega_4\omega_1^3\omega_2^2 + 138\omega_3v_3^2\omega_4\omega_1^3\omega_2 + 96\omega_3v_3^4\omega_4\omega_1^3 + 81\omega_3v_3^2\omega_4\omega_1^2\omega_2^2 + 8c_s^4\omega_4\omega_1\omega_2^3 + 3\omega_3c_s^2v_3^2\omega_4\omega_1^3\omega_2^2) \frac{\rho}{36\omega_3\omega_4\omega_1^3\omega_2^3}$$

$$\text{coefficient } C_{D_z^4\rho}^{(2)} \text{ at } \frac{\partial^4\rho}{\partial x_3^4}:$$

$$C_{D_z^4\rho}^{(2), \text{SRT}} = (6v_3^4 - 3v_3^4\omega - 12v_3^2c_s^2\omega + 2c_s^4 - c_s^4\omega + 24v_3^2c_s^2 + 3v_3^2\omega - 6v_3^2 + c_s^2\omega - 2c_s^2) \frac{v_2}{24\omega}$$

$$C_{D_z^4\rho}^{(2), \text{MRT1}} = (-12v_3^2\omega_7^2\omega_{11}^2 - 12\omega_{19}c_s^4\omega_7^2\omega_{11}^2 - 216\omega_{19}v_3^2c_s^2\omega_{11}^2 - 48\omega_{19}c_s^4\omega_7\omega_{11} + 24\omega_{19}c_s^4\omega_{11} + 48\omega_{19}v_3^2\omega_7\omega_{11} - 144\omega_{19}v_3^2c_s^2\omega_7^2 + 24\omega_{19}c_s^2\omega_{11}^2 + 72\omega_{19}v_3^2c_s^2\omega_7\omega_{11} + 3\omega_{19}^2v_3^2\omega_7^2\omega_{11}^2 - 24\omega_{19}c_s^2\omega_7 + 96\omega_{19}v_3^4\omega_7\omega_{11} + 24c_s^2\omega_7\omega_{11}^2 + 150\omega_{19}^2v_3^2c_s^2\omega_7^2\omega_{11} + 36\omega_{19}^2v_3^2\omega_7^2 + 12\omega_{19}c_s^2\omega_7^2\omega_{11} - 72\omega_{19}^2v_3^2\omega_7^2 + 12v_3^4\omega_7^2\omega_{11} + 48\omega_{19}^2c_s^2\omega_7\omega_{11} - 48\omega_{19}v_3^4\omega_7\omega_{11} + 12\omega_{19}^2c_s^2\omega_7^2 - 12\omega_{19}^2v_3^2c_s^2\omega_7^2\omega_{11} - 3\omega_{19}^2v_3^4\omega_7^2\omega_{11}^2 - 126\omega_{19}v_3^2c_s^2\omega_7^2\omega_{11}^2 + 288\omega_{19}^2v_3^2c_s^2\omega_7 - 24c_s^4\omega_7\omega_{11} - 96\omega_{19}v_3^2\omega_7\omega_{11} + 48\omega_{19}^2v_3^4\omega_{11} - 36\omega_{19}^2v_3^2\omega_7\omega_{11} + 72v_3^2c_s^2\omega_7^2\omega_{11}^2 + 48\omega_{19}v_3^2\omega_{11}^2 + 12c_s^4\omega_7^2\omega_{11}^2 + 30\omega_{19}v_3^2\omega_7^2\omega_{11}^2 + 432\omega_{19}v_3^2c_s^2\omega_7\omega_{11}^2 + 24\omega_{19}^2c_s^4\omega_7 - 144v_3^2c_s^2\omega_7\omega_{11} + 96\omega_{19}^2v_3^2\omega_7\omega_{11} - 36\omega_{19}^2v_3^4\omega_7^2 - \omega_{19}^2c_s^4\omega_7^2\omega_{11} - 48\omega_{19}c_s^2\omega_7\omega_{11}^2 - 24v_3^4\omega_7\omega_{11}^2 - 24\omega_{19}^2c_s^2\omega_{11} - 14\omega_{19}^2c_s^2\omega_7\omega_{11} - 24\omega_{19}c_s^4\omega_{11}^2 + 24\omega_{19}v_3^4\omega_7\omega_{11} - 432\omega_{19}^2v_3^2\omega_7\omega_{11} - 30\omega_{19}v_3^4\omega_7^2\omega_{11} - 12c_s^2\omega_7^2\omega_{11} - 96\omega_{19}^2v_3^4\omega_7\omega_{11} - 48\omega_{19}^2v_3^2\omega_{11} - 48\omega_{19}v_3^4\omega_{11}^2 + \omega_{19}^2c_s^2\omega_7^2\omega_{11} + 24v_3^2\omega_7\omega_{11}^2 + 48\omega_{19}c_s^4\omega_7\omega_{11} + 72\omega_{19}^2v_3^4\omega_7 + 14\omega_{19}^2c_s^4\omega_7^2\omega_{11} + 216\omega_{19}^2v_3^2c_s^2\omega_{11} - 12\omega_{19}^2c_s^4\omega_7^2 - 144\omega_{19}v_3^2c_s^2\omega_7\omega_{11} - 24\omega_{19}v_3^2\omega_7^2\omega_{11}) \frac{v_2}{24\omega_{19}^2\omega_7^2\omega_{11}^2}$$

$$C_{D_z^4\rho}^{(2), \text{MRT2}} = C_{D_z^4\rho}^{(2), \text{MRT1}}$$

$$C_{D_z^4\rho}^{(2), \text{CLBM1}} = (6v_3^4 + c_s^2\omega_{11} + 2c_s^4 + 3v_3^2\omega_{11} + 24v_3^2c_s^2 - c_s^4\omega_{11} - 6v_3^2 - 3v_3^4\omega_{11} - 2c_s^2 - 12v_3^2c_s^2\omega_{11}) \frac{v_2}{24\omega_{11}}$$

$$C_{D_z^4\rho}^{(2), \text{CLBM2}} = C_{D_z^4\rho}^{(2), \text{CLBM1}}$$

$$C_{D_z^4\rho}^{(2), \text{CuLBM1}} = (3\omega_6v_3^2 + 6v_3^4 + \omega_6c_s^2 - 12\omega_6v_3^2c_s^2 + 2c_s^4 + 24v_3^2c_s^2 - 3\omega_6v_3^4 - 6v_3^2 - \omega_6c_s^4 - 2c_s^2) \frac{v_2}{24\omega_6}$$

$$C_{D_z^4\rho}^{(2), \text{CuLBM2}} = (-3c_s^4\omega_1\omega_2 + 24v_3^2c_s^2\omega_1 + 6v_3^4\omega_1 + 4c_s^4\omega_2 + 48v_3^2c_s^2\omega_2 + 2c_s^4\omega_1 + 12v_3^4\omega_2 + 3c_s^2\omega_1\omega_2 - 6v_3^2\omega_1 - 4c_s^2\omega_2 + 9v_3^2\omega_1\omega_2 - 9v_3^4\omega_1\omega_2 - 2c_s^2\omega_1 - 36v_3^2c_s^2\omega_1\omega_2 - 12v_3^2\omega_2) \frac{v_2}{72\omega_1\omega_2}$$

$$\text{coefficient } C_{D_z^4v_2}^{(2)} \text{ at } \frac{\partial^4v_2}{\partial x_3^4}:$$

$$C_{D_z^4v_2}^{(2), \text{SRT}} = (-72v_3^4 - 3c_s^4\omega^3 + 108v_3^4\omega + 216v_3^2c_s^2\omega + 30c_s^4\omega^2 + 48c_s^4 - 84v_3^2c_s^2\omega^2 - 72c_s^4\omega - 42v_3^4\omega^2 + 6v_3^2c_s^2\omega^3 + 3v_3^4\omega^3 - 144v_3^2c_s^2 - 108v_3^2\omega - 14c_s^2\omega^2 + c_s^2\omega^3 - 3v_3^2\omega^3 + 72v_3^2 + 36c_s^2\omega - 24c_s^2 + 42v_3^2\omega^2) \frac{\rho}{24\omega^3}$$

$$C_{D_z^4v_2}^{(2), \text{MRT1}} = (-24v_3^2c_s^2\omega_7^2 + 6\omega_{19}c_s^4\omega_7^3 - 72\omega_{19}^2v_3^2c_s^2\omega_7^2 - 24v_3^4\omega_7^2 - 3\omega_{19}^2v_3^2\omega_7^3 + 12\omega_{19}^2c_s^2\omega_7 + 12v_3^2c_s^2\omega_7^3 - 48\omega_{19}v_3^4\omega_7 + 24\omega_{19}^2v_3^2\omega_7^2 + 12v_3^4\omega_7^3 + 6\omega_{19}^2v_3^2c_s^2\omega_7^3 - 24\omega_{19}c_s^4\omega_7^2 - 24\omega_{19}^2v_3^2\omega_7 + 24\omega_{19}c_s^4\omega_7 - 8\omega_{19}^2c_s^2\omega_7^2 + 72\omega_{19}v_3^4\omega_7^2 + 156\omega_{19}^2v_3^2c_s^2\omega_7 - 18\omega_{19}v_3^4\omega_7^3 + \omega_{19}^2c_s^2\omega_7^3 + 24\omega_{19}^2c_s^4 - 48\omega_{19}^2c_s^4\omega_7 + 48\omega_{19}v_3^2c_s^2\omega_7^2 + 48\omega_{19}v_3^2\omega_7 - 24\omega_{19}^2v_3^4\omega_7^2 - 12v_3^2\omega_7^2 + 24\omega_{19}c_s^2\omega_7^2 - 12\omega_{19}v_3^2c_s^2\omega_7^3 - 6\omega_{19}c_s^2\omega_7^2 + 24v_3^2\omega_7^2 + 3\omega_{19}^2v_3^4\omega_7^3 + 18\omega_{19}v_3^2\omega_7^3 - 3\omega_{19}^2c_s^4\omega_7^3 + 24\omega_{19}^2v_3^4\omega_7^2 - 24\omega_{19}c_s^2\omega_7 + 24\omega_{19}^2v_3^2c_s^2 - 72\omega_{19}v_3^2\omega_7^2 - 24\omega_{19}v_3^2c_s^2\omega_7) \frac{\rho}{24\omega_{19}^2\omega_7^3}$$

$$C_{D_z^4 v_2}^{(2), \text{MRT}^2} = C_{D_z^4 v_2}^{(2), \text{MRT}^1}$$

$$C_{D_z^4 v_2}^{(2), \text{CLBM}^1} = (-216v_3^2 c_s^2 \omega_7^2 + 6\omega_{19} c_s^4 \omega_7^3 - 12\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 - 72v_3^4 \omega_7^2 - 3\omega_{19}^2 v_3^2 \omega_7^3 + 12\omega_{19}^2 c_s^2 \omega_7 + 108v_3^2 c_s^2 \omega_7^3 + 12\omega_{19}^2 v_3^2 \omega_7^2 + 36v_3^4 \omega_7^3 + 6\omega_{19}^2 v_3^2 c_s^2 \omega_7^3 - 24\omega_{19} c_s^4 \omega_7^2 + 24\omega_{19} c_s^4 \omega_7 - 8\omega_{19}^2 c_s^2 \omega_7^2 + 72\omega_{19} v_3^4 \omega_7^2 - 36\omega_{19}^2 v_3^2 c_s^2 \omega_7 - 30\omega_{19} v_3^4 \omega_7^3 + \omega_{19}^2 c_s^2 \omega_7^3 + 24\omega_{19}^2 c_s^4 \omega_7 - 48\omega_{19}^2 c_s^4 \omega_7 + 144\omega_{19} v_3^2 c_s^2 \omega_7^2 - 12\omega_{19}^2 v_3^4 \omega_7^2 - 36v_3^2 \omega_7^3 + 24\omega_{19} c_s^2 \omega_7^2 - 72\omega_{19} v_3^2 c_s^2 \omega_7^2 - 6\omega_{19} c_s^2 \omega_7^2 + 72v_3^2 \omega_7^2 + 3\omega_{19}^2 v_3^2 \omega_7^3 + 30\omega_{19} v_3^2 \omega_7^3 - 3\omega_{19}^2 c_s^4 \omega_7^3 - 24\omega_{19} c_s^4 \omega_7 + 24\omega_{19}^2 c_s^4 \omega_7^2 - 72\omega_{19} v_3^2 \omega_7^2 + 72\omega_{19} v_3^2 c_s^2 \omega_7) \frac{\rho}{24\omega_{19}^2 \omega_7^3}$$

$$C_{D_z^4 v_2}^{(2), \text{CLBM}^2} = C_{D_z^4 v_2}^{(2), \text{CLBM}^1}$$

$$C_{D_z^4 v_2}^{(2), \text{CuLBM}^1} = (-216\omega_3^2 v_3^2 c_s^2 + 36\omega_3^3 v_3^4 + 24\omega_3^3 c_s^4 \omega_{10}^2 + 30\omega_3^3 v_3^2 \omega_{10} + 72\omega_3 v_3^2 c_s^2 \omega_{10} + 72\omega_3^2 v_3^4 \omega_{10} + \omega_3^3 c_s^2 \omega_{10}^2 - 24\omega_3 c_s^2 \omega_{10} - 12\omega_3^2 v_3^4 \omega_{10}^2 - 6\omega_3^2 c_s^2 \omega_{10} - 72\omega_3^2 v_3^4 \omega_{10}^2 + 12\omega_3 c_s^2 \omega_{10}^2 + 24c_s^4 \omega_{10}^2 - 24\omega_3^2 c_s^4 \omega_{10} - 3\omega_3^3 v_3^2 \omega_{10}^2 - 36\omega_3 v_3^2 c_s^2 \omega_{10}^2 - 8\omega_3^2 c_s^2 \omega_{10}^2 - 30\omega_3^3 v_3^4 \omega_{10} - 72\omega_3^2 v_3^2 \omega_{10} - 3\omega_3^3 c_s^4 \omega_{10}^2 + 72\omega_3^2 v_3^2 + 24\omega_3 c_s^4 \omega_{10} + 6\omega_3^3 v_3^2 c_s^2 \omega_{10}^2 + 144\omega_3^2 v_3^2 c_s^2 \omega_{10} + 108\omega_3^3 v_3^2 c_s^2 - 12\omega_3^2 v_3^2 c_s^2 \omega_{10}^2 - 36\omega_3^3 v_3^2 - 72\omega_3^2 v_3^2 c_s^2 \omega_{10} + 12\omega_3^2 v_3^2 \omega_{10}^2 + 6\omega_3^3 c_s^4 \omega_{10} - 48\omega_3 c_s^4 \omega_{10}^2 + 24\omega_3^2 c_s^2 \omega_{10} + 3\omega_3^3 v_3^2 \omega_{10}^2) \frac{\rho}{24\omega_3^3 \omega_{10}^2}$$

$$C_{D_z^4 v_2}^{(2), \text{CuLBM}^2} = (-15\omega_3 v_3^4 \omega_4^2 \omega_1^3 - 48\omega_3^2 c_s^4 \omega_4^2 \omega_1 + \omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 18v_3^2 \omega_4^2 \omega_1^2 + 9\omega_3^2 v_3^4 \omega_1^3 - 36\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 + 36\omega_3 v_3^4 \omega_4^2 \omega_1^2 + 36\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1 - 18\omega_3^2 v_3^4 \omega_1^2 + 15\omega_3^2 v_3^2 \omega_4 \omega_1^3 - 9v_3^2 \omega_4^2 \omega_1^3 - 8\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^2 \omega_4^2 \omega_1 + 54\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^3 + 15\omega_3 v_3^2 \omega_4^2 \omega_1^3 - 3\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 + 72\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 + 36\omega_3^2 v_3^4 \omega_4 \omega_1^2 - 18v_3^4 \omega_4^2 \omega_1^2 + 27v_3^2 c_s^2 \omega_4^2 \omega_1^3 - 36\omega_3 v_3^2 \omega_4^2 \omega_1^2 - 108\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^2 + 24\omega_3^2 c_s^4 \omega_4^2 + 9v_3^4 \omega_4^2 \omega_1^3 - 54v_3^2 c_s^2 \omega_4^2 \omega_1^2 - 15\omega_3^2 v_3^4 \omega_4 \omega_1^3 - 36\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 + 24\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 + 72\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^2 + 36\omega_3 v_3^2 \omega_4^2 \omega_1^2 - 3\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 3\omega_3^2 v_3^4 \omega_4^2 \omega_1^3 + 18\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 + 12\omega_3 c_s^4 \omega_4^2 \omega_1 - 12\omega_3^2 c_s^4 \omega_4 \omega_1^2 + 27\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 + 6\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 + 12\omega_3 c_s^2 \omega_4^2 \omega_1^2 - 18\omega_3 v_3^2 \omega_4 \omega_1^3 - 12\omega_3^2 c_s^2 \omega_4 \omega_1 - 36\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^3 - 12\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 - 54\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 + 3\omega_3^2 c_s^4 \omega_4 \omega_1^3 - 12\omega_3^2 v_3^4 \omega_4^2 \omega_1 - 9\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 - 36\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1 - 36\omega_3 v_3^4 \omega_4^2 \omega_1 + 3\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 - 12\omega_3 c_s^2 \omega_4^2 \omega_1 - 3\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 + 12\omega_3^2 c_s^2 \omega_4 \omega_1^2 - 12\omega_3 c_s^4 \omega_4 \omega_1^2 + 12\omega_3^2 c_s^4 \omega_4 \omega_1 + 18\omega_3 v_3^4 \omega_4 \omega_1^3 - 3\omega_3^2 c_s^2 \omega_4 \omega_1^3 + 36\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1 + 12\omega_3^2 v_3^2 \omega_4^2 \omega_1^2) \frac{\rho}{24\omega_3^2 \omega_4^2 \omega_1^3}$$

$$\text{coefficient } C_{D_z^4 v_3}^{(2)} \text{ at } \frac{\partial^4 v_3}{\partial x_3^4} :$$

$$C_{D_z^4 v_3}^{(2), \text{SRT}} = (-4 + 2\omega - 5v_3^2 \omega + 10v_3^2 - 3c_s^2 \omega + 6c_s^2) \frac{v_3 v_2 \rho}{12\omega}$$

$$C_{D_z^4 v_3}^{(2), \text{MRT}^1} = (24v_3^2 \omega_7^2 \omega_{11}^2 + 24\omega_{19} \omega_7 \omega_{11} - 72\omega_{19} v_3^2 \omega_7 \omega_{11} - 60\omega_{19} c_s^2 \omega_{11}^2 - 5\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^2 + 72\omega_{19}^2 c_s^2 \omega_7 - 48c_s^2 \omega_7 \omega_{11}^2 - 25\omega_{19}^2 \omega_7^2 \omega_{11} - 60\omega_{19}^2 v_3^2 \omega_7^2 + 12\omega_{19} c_s^2 \omega_7^2 \omega_{11} + 24\omega_7 \omega_{11}^2 - 33\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 120\omega_{19}^2 v_3^2 \omega_7 - 120\omega_{19}^2 c_s^2 \omega_7 \omega_{11} - 36\omega_{19}^2 c_s^2 \omega_7^2 + 2\omega_{19}^2 \omega_7^2 \omega_{11}^2 + 168\omega_{19} v_3^2 \omega_7 \omega_{11}^2 - 36\omega_{19}^2 \omega_{11} + 61\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11} - 72\omega_{19} \omega_7 \omega_{11}^2 - 84\omega_{19} v_3^2 \omega_{11}^2 - 51\omega_{19} v_3^2 \omega_7^2 \omega_{11} - 168\omega_{19}^2 v_3^2 \omega_7 \omega_{11} + 24\omega_{19}^2 \omega_7^2 + 21\omega_{19} \omega_7^2 \omega_{11}^2 + 120\omega_{19} c_s^2 \omega_7 \omega_{11}^2 + 60\omega_{19}^2 c_s^2 \omega_{11} + 39\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11} + 24c_s^2 \omega_7^2 \omega_{11}^2 + 84\omega_{19}^2 v_3^2 \omega_{11} + 72\omega_{19}^2 \omega_7 \omega_{11} - 12\omega_7^2 \omega_{11}^2 - 24\omega_{19} c_s^2 \omega_7 \omega_{11} - 3\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^2 - 12\omega_{19} \omega_7^2 \omega_{11} - 48v_3^2 \omega_7 \omega_{11}^2 - 48\omega_{19}^2 \omega_7 + 36\omega_{19} v_3^2 \omega_7^2 \omega_{11} + 36\omega_{19} \omega_{11}^2) \frac{v_3 v_2 \rho}{12\omega_{19}^2 \omega_7^2 \omega_{11}^2}$$

$$C_{D_z^4 v_3}^{(2), \text{MRT}^2} = C_{D_z^4 v_3}^{(2), \text{MRT}^1}$$

$$C_{D_z^4 v_3}^{(2), \text{CLBM}^1} = (-4 - 3c_s^2 \omega_{11} - 5v_3^2 \omega_{11} + 2\omega_{11} + 10v_3^2 + 6c_s^2) \frac{v_3 v_2 \rho}{12\omega_{11}}$$

$$C_{D_z^4 v_3}^{(2), \text{CLBM}^2} = C_{D_z^4 v_3}^{(2), \text{CLBM}^1}$$

$$C_{D_z^4 v_3}^{(2), \text{CuLBM}^1} = (-4 - 5\omega_6 v_3^2 + 2\omega_6 - 3\omega_6 c_s^2 + 10v_3^2 + 6c_s^2) \frac{v_3 v_2 \rho}{12\omega_6}$$

$$C_{D_z^4 v_3}^{(2), \text{CuLBM}^2} = (6\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 10v_3^2 \omega_1 + 12c_s^2 \omega_2 - 15v_3^2 \omega_1 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1 + 20v_3^2 \omega_2) \frac{v_3 v_2 \rho}{36\omega_1 \omega_2}$$

3.4 Conservation of momentum: ρv_3

$$v_3 \frac{\partial \rho}{\partial t} + \rho \frac{\partial v_3}{\partial t} + v_3 v_1 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_1} + v_3 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_1}{\partial x_1} + v_1 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_1} + v_3 v_2 \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_2} + v_3 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_2}{\partial x_2} + v_2 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_2} + (v_3^2 + c_s^2) \frac{\delta_l}{\delta_t} \frac{\partial \rho}{\partial x_3} + 2v_3 \rho \frac{\delta_l}{\delta_t} \frac{\partial v_3}{\partial x_3} + C_{D_x \rho, D_x v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1} + C_{D_x \rho, D_z v_1}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3} + C_{D_x v_1, D_z v_1}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_3} + C_{D_y \rho, D_y v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2} + C_{D_y \rho, D_z v_2}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3} + C_{D_y v_2, D_z v_2}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial v_2}{\partial x_2} \frac{\partial v_2}{\partial x_3} + C_{D_z \rho, D_x v_1}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1} + C_{D_z \rho, D_y v_2}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2} + C_{D_z \rho, D_z v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3} + C_{D_z v_3, D_z v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \left(\frac{\partial v_3}{\partial x_3} \right)^2 + C_{D_z^2 v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_3}{\partial x_1^2} + C_{D_y^2 v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_3}{\partial x_2^2} + C_{D_x D_z \rho}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_1 \partial x_3} + C_{D_x D_z v_1}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_1}{\partial x_1 \partial x_3} + C_{D_y D_z \rho}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_2 \partial x_3} + C_{D_y D_z v_2}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_2}{\partial x_2 \partial x_3} + C_{D_z^2 \rho}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 \rho}{\partial x_3^2} + C_{D_z^2 v_3}^{(3)} \frac{\delta_l^2}{\delta_t^2} \frac{\partial^2 v_3}{\partial x_3^2} + C_{D_x^3 \rho}^{(3)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 \rho}{\partial x_1^3} + C_{D_x^3 v_1}^{(3)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1^3} + C_{D_x^3 v_3}^{(3)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_1^3} + C_{D_x^2 D_y v_2}^{(3)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_2}{\partial x_1^2 \partial x_2} + C_{D_x^2 D_y v_3}^{(3)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} + C_{D_x D_y^2 v_1}^{(3)} \frac{\delta_l^3}{\delta_t^3} \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} +$$

[illegible]

coefficient $C_{D_{x\rho}, D_{xv_3}}^{(3)}$ at $\frac{\partial \rho}{\partial x_1} \frac{\partial v_3}{\partial x_1}$:

$$C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2}{2\omega_6}$$

$$C_{D_x \rho, D_x v_3}^{(3), \text{CLBM1}} = C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_3}^{(3), \text{CLBM2}} = C_{D_x \rho, D_x v_3}^{(3), \text{MRT1}}$$

$$C_{D_x \rho, D_x v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_x \rho, D_x v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_x \rho, D_z v_1}^{(3)}$ at $\frac{\partial \rho}{\partial x_1} \frac{\partial v_1}{\partial x_3}$:

$$C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2}{2\omega_6}$$

$$C_{D_x \rho, D_z v_1}^{(3), \text{MRT2}} = C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_1}^{(3), \text{CLBM1}} = C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_1}^{(3), \text{CLBM2}} = C_{D_x \rho, D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x \rho, D_z v_1}^{(3), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2}{2\omega_2}$$

$$C_{D_x \rho, D_z v_1}^{(3), \text{CuLBM2}} = (6v_1^2\omega_1 - 6v_1^2\omega_2 + 3c_s^2\omega_1\omega_2 - 2\omega_1 - 12c_s^2\omega_2 + 2\omega_2 + 6c_s^2\omega_1) \frac{1}{6\omega_1\omega_2}$$

coefficient $C_{D_x v_1, D_z v_1}^{(3)}$ **at** $\frac{\partial v_1}{\partial x_1} \frac{\partial v_1}{\partial x_3}$:

$$C_{D_x v_1, D_z v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{MRT1}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{MRT2}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x v_1, D_z v_1}^{(3), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2v_1\rho}{\omega_1\omega_2}$$

coefficient $C_{D_y \rho, D_y v_3}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_3}{\partial x_2}$:

$$C_{D_y \rho, D_y v_3}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{MRT2}} = C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CLBM1}} = C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CLBM2}} = C_{D_y \rho, D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_y \rho, D_y v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2}{2\omega_1}$$

coefficient $C_{D_y \rho, D_z v_2}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_2} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_y \rho, D_z v_2}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2}{2\omega}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2}{2\omega_7}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{MRT2}} = C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CLBM1}} = C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CLBM2}} = C_{D_y \rho, D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2}{2\omega_3}$$

$$C_{D_y \rho, D_z v_2}^{(3), \text{CuLBM2}} = (3c_s^2\omega_1\omega_2 - 2\omega_1 - 12c_s^2\omega_2 - 6v_2^2\omega_2 + 2\omega_2 + 6v_2^2\omega_1 + 6c_s^2\omega_1) \frac{1}{6\omega_1\omega_2}$$

coefficient $C_{D_y v_2, D_z v_2}^{(3)}$ **at** $\frac{\partial v_2}{\partial x_2} \frac{\partial v_2}{\partial x_3}$:

$$C_{D_y v_2, D_z v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{MRT1}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{MRT2}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y v_2, D_z v_2}^{(3), \text{CuLBM2}} = (\omega_1 - \omega_2) \frac{2v_2 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_x v_1}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_1}{\partial x_1}$:

$$C_{D_z \rho, D_x v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{MRT1}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{MRT2}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_z \rho, D_x v_1}^{(3), \text{CuLBM2}} = (3v_1^2 \omega_1 - 3v_1^2 \omega_2 - \omega_1 - c_s^2 \omega_2 + \omega_2 + c_s^2 \omega_1) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_y v_2}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_2}{\partial x_2}$:

$$C_{D_z \rho, D_y v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{MRT1}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{MRT2}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_z \rho, D_y v_2}^{(3), \text{CuLBM2}} = (-\omega_1 - c_s^2 \omega_2 - 3v_2^2 \omega_2 + \omega_2 + 3v_2^2 \omega_1 + c_s^2 \omega_1) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_z \rho, D_z v_3}^{(3)}$ **at** $\frac{\partial \rho}{\partial x_3} \frac{\partial v_3}{\partial x_3}$:

$$C_{D_z \rho, D_z v_3}^{(3), \text{SRT}} = (-2 + \omega - 3v_3^2 \omega + 6v_3^2 - 2c_s^2 \omega + 4c_s^2) \frac{1}{\omega}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}} = (-2 - 2c_s^2 \omega_{11} - 3v_3^2 \omega_{11} + \omega_{11} + 6v_3^2 + 4c_s^2) \frac{1}{\omega_{11}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{MRT2}} = C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CLBM1}} = C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CLBM2}} = C_{D_z \rho, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CuLBM1}} = (-2 - 3\omega_6 v_3^2 + \omega_6 - 2\omega_6 c_s^2 + 6v_3^2 + 4c_s^2) \frac{1}{\omega_6}$$

$$C_{D_z \rho, D_z v_3}^{(3), \text{CuLBM2}} = (3\omega_1 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 8c_s^2 \omega_2 - 9v_3^2 \omega_1 \omega_2 - 4\omega_2 + 4c_s^2 \omega_1 + 12v_3^2 \omega_2) \frac{1}{3\omega_1 \omega_2}$$

coefficient $C_{D_z v_3, D_z v_3}^{(3)}$ **at** $\left(\frac{\partial v_3}{\partial x_3}\right)^2$:

$$C_{D_z v_3, D_z v_3}^{(3), \text{SRT}} = (2 - \omega) \frac{3v_3 \rho}{\omega}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}} = (2 - \omega_{11}) \frac{3v_3 \rho}{\omega_{11}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{MRT2}} = C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CLBM1}} = C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CLBM2}} = C_{D_z v_3, D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CuLBM1}} = (2 - \omega_6) \frac{3v_3 \rho}{\omega_6}$$

$$C_{D_z v_3, D_z v_3}^{(3), \text{CuLBM2}} = (-3\omega_1 \omega_2 + 2\omega_1 + 4\omega_2) \frac{v_3 \rho}{\omega_1 \omega_2}$$

coefficient $C_{D_x^2 v_3}^{(3)}$ **at** $\frac{\partial^2 v_3}{\partial x_1^2}$:

$$C_{D_x^2 v_3}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x^2 v_3}^{(3), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_x^2 v_3}^{(3), \text{MRT2}} = C_{D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 v_3}^{(3), \text{CLBM1}} = C_{D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 v_3}^{(3), \text{CLBM2}} = C_{D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_x^2 v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_y^2 v_3}^{(3)}$ **at** $\frac{\partial^2 v_3}{\partial x_2^2}$:

$$C_{D_y^2 v_3}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y^2 v_3}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_y^2 v_3}^{(3), \text{MRT2}} = C_{D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 v_3}^{(3), \text{CLBM1}} = C_{D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 v_3}^{(3), \text{CLBM2}} = C_{D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 v_3}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_y^2 v_3}^{(3), \text{CuLBM2}} = (-2 + \omega_1) \frac{c_s^2 \rho}{2\omega_1}$$

coefficient $C_{D_x D_z \rho}^{(3)}$ **at** $\frac{\partial^2 \rho}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{MRT1}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{MRT2}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_z \rho}^{(3), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_1}{3\omega_1 \omega_2}$$

coefficient $C_{D_x D_z v_1}^{(3)}$ **at** $\frac{\partial^2 v_1}{\partial x_1 \partial x_3}$:

$$C_{D_x D_z v_1}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_x D_z v_1}^{(3), \text{MRT1}} = (-2 + \omega_6) \frac{c_s^2 \rho}{2\omega_6}$$

$$C_{D_x D_z v_1}^{(3), \text{MRT2}} = C_{D_x D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(3), \text{CLBM1}} = C_{D_x D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(3), \text{CLBM2}} = C_{D_x D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x D_z v_1}^{(3), \text{CuLBM1}} = (-2 + \omega_2) \frac{c_s^2 \rho}{2\omega_2}$$

$$C_{D_x D_z v_1}^{(3), \text{CuLBM2}} = (6v_1^2 \omega_1 - 6v_1^2 \omega_2 + 3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 8c_s^2 \omega_2 + 2\omega_2 + 2c_s^2 \omega_1) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_y D_z \rho}^{(3)}$ **at** $\frac{\partial^2 \rho}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{MRT1}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{MRT2}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y D_z \rho}^{(3), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_2}{3\omega_1 \omega_2}$$

coefficient $C_{D_y D_z v_2}^{(3)}$ **at** $\frac{\partial^2 v_2}{\partial x_2 \partial x_3}$:

$$C_{D_y D_z v_2}^{(3), \text{SRT}} = (-2 + \omega) \frac{c_s^2 \rho}{2\omega}$$

$$C_{D_y D_z v_2}^{(3), \text{MRT1}} = (-2 + \omega_7) \frac{c_s^2 \rho}{2\omega_7}$$

$$C_{D_y D_z v_2}^{(3), \text{MRT2}} = C_{D_y D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(3), \text{CLBM1}} = C_{D_y D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(3), \text{CLBM2}} = C_{D_y D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y D_z v_2}^{(3), \text{CuLBM1}} = (-2 + \omega_3) \frac{c_s^2 \rho}{2\omega_3}$$

$$C_{D_y D_z v_2}^{(3), \text{CuLBM2}} = (3c_s^2 \omega_1 \omega_2 - 2\omega_1 - 8c_s^2 \omega_2 - 6v_2^2 \omega_2 + 2\omega_2 + 6v_2^2 \omega_1 + 2c_s^2 \omega_1) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_z \rho}^{(3)}$ **at** $\frac{\partial^2 \rho}{\partial x_3^2}$:

$$C_{D_z \rho}^{(3), \text{SRT}} = (-2 + \omega - v_3^2 \omega + 2v_3^2 - 3c_s^2 \omega + 6c_s^2) \frac{v_3}{2\omega}$$

$$C_{D_z \rho}^{(3), \text{MRT1}} = (-2 - 3c_s^2 \omega_{11} - v_3^2 \omega_{11} + \omega_{11} + 2v_3^2 + 6c_s^2) \frac{v_3}{2\omega_{11}}$$

$$C_{D_z \rho}^{(3), \text{MRT2}} = C_{D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_z \rho}^{(3), \text{CLBM1}} = C_{D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_z \rho}^{(3), \text{CLBM2}} = C_{D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_z \rho}^{(3), \text{CuLBM1}} = (-2 - \omega_6 v_3^2 + \omega_6 - 3\omega_6 c_s^2 + 2v_3^2 + 6c_s^2) \frac{v_3}{2\omega_6}$$

$$C_{D_z \rho}^{(3), \text{CuLBM2}} = (3\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 2\omega_1 + 2v_3^2 \omega_1 + 12c_s^2 \omega_2 - 3v_3^2 \omega_1 \omega_2 - 4\omega_2 + 6c_s^2 \omega_1 + 4v_3^2 \omega_2) \frac{v_3}{6\omega_1 \omega_2}$$

coefficient $C_{D_z v_3}^{(3)}$ **at** $\frac{\partial^2 v_3}{\partial x_3^2}$:

$$C_{D_z v_3}^{(3), \text{SRT}} = (-2 + \omega - 3v_3^2 \omega + 6v_3^2 - c_s^2 \omega + 2c_s^2) \frac{\rho}{2\omega}$$

$$C_{D_z v_3}^{(3), \text{MRT1}} = (-2 - c_s^2 \omega_{11} - 3v_3^2 \omega_{11} + \omega_{11} + 6v_3^2 + 2c_s^2) \frac{\rho}{2\omega_{11}}$$

$$C_{D_z v_3}^{(3), \text{MRT2}} = C_{D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3}^{(3), \text{CLBM1}} = C_{D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3}^{(3), \text{CLBM2}} = C_{D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_z v_3}^{(3), \text{CuLBM1}} = (-2 - 3\omega_6 v_3^2 + \omega_6 - \omega_6 c_s^2 + 6v_3^2 + 2c_s^2) \frac{\rho}{2\omega_6}$$

$$C_{D_z v_3}^{(3), \text{CuLBM2}} = (3\omega_1 \omega_2 - 3c_s^2 \omega_1 \omega_2 - 2\omega_1 + 6v_3^2 \omega_1 + 4c_s^2 \omega_2 - 9v_3^2 \omega_1 \omega_2 - 4\omega_2 + 2c_s^2 \omega_1 + 12v_3^2 \omega_2) \frac{\rho}{6\omega_1 \omega_2}$$

coefficient $C_{D_x \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^3}$:

$$C_{D_x \rho}^{(3), \text{SRT}} = (-1 + v_1^2 + 3c_s^2) \frac{v_3 v_1}{12}$$

$$C_{D_x \rho}^{(3), \text{MRT1}} = (-6\omega_6 v_1^2 \omega_{13} - 12v_1^2 \omega_9 - 12\omega_{13} + 12v_1^2 \omega_{13} + 3\omega_6 c_s^2 \omega_{13} \omega_9 + 6\omega_6 v_1^2 \omega_9 + 36c_s^2 \omega_{13} + 18\omega_6 c_s^2 \omega_9 - \omega_6 \omega_{13} \omega_9 + 6\omega_6 \omega_{13} + \omega_6 v_1^2 \omega_{13} \omega_9 - 6\omega_6 \omega_9 - 18\omega_6 c_s^2 \omega_{13} - 36c_s^2 \omega_9 + 12\omega_9) \frac{v_3 v_1}{12\omega_6 \omega_{13} \omega_9}$$

$$C_{D_x \rho}^{(3), \text{MRT2}} = C_{D_x \rho}^{(3), \text{MRT1}}$$

$$C_{D_x \rho}^{(3), \text{CLBM1}} = C_{D_x \rho}^{(3), \text{SRT}}$$

$$C_{D_x \rho}^{(3), \text{CLBM2}} = C_{D_x \rho}^{(3), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(3), \text{CuLBM1}} = C_{D_x^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_x^3 \rho}^{(3), \text{CuLBM2}} = C_{D_x^3 \rho}^{(3), \text{SRT}}$$

coefficient $C_{D_x^3 v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^3}$:

$$C_{D_x^3 v_1}^{(3), \text{SRT}} = (-1 + 3v_1^2 + c_s^2) \frac{v_1 \rho}{12}$$

$$C_{D_x^3 v_1}^{(3), \text{MRT1}} = (-18\omega_6 v_1^2 \omega_{13} - 36v_1^2 \omega_9 - 12\omega_{13} + 36v_1^2 \omega_{13} + \omega_6 c_s^2 \omega_{13} \omega_9 + 18\omega_6 v_1^2 \omega_9 + 12c_s^2 \omega_{13} + 6\omega_6 c_s^2 \omega_9 - \omega_6 \omega_{13} \omega_9 + 6\omega_6 \omega_{13} + 3\omega_6 v_1^2 \omega_{13} \omega_9 - 6\omega_6 \omega_9 - 6\omega_6 c_s^2 \omega_{13} - 12c_s^2 \omega_9 + 12\omega_9) \frac{v_3 \rho}{12\omega_6 \omega_{13} \omega_9}$$

$$C_{D_x^3 v_1}^{(3), \text{MRT2}} = C_{D_x^3 v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^3 v_1}^{(3), \text{CLBM1}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(3), \text{CLBM2}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(3), \text{CuLBM1}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

$$C_{D_x^3 v_1}^{(3), \text{CuLBM2}} = C_{D_x^3 v_1}^{(3), \text{SRT}}$$

coefficient $C_{D_x^3 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^3}$:

$$C_{D_x^3 v_3}^{(3), \text{SRT}} = (6 - 6v_1^2 + 6v_1^2 \omega - v_1^2 \omega^2 + \omega^2 - 6\omega - 3c_s^2 \omega^2 + 18c_s^2 \omega - 18c_s^2) \frac{v_1 \rho}{6\omega 2}$$

$$C_{D_x^3 v_3}^{(3), \text{MRT1}} = (3\omega_6 v_1^2 \omega_{13} + 6\omega_6 - 3\omega_6^2 c_s^2 \omega_{13} - 6\omega_6 c_s^2 + 3\omega_6^2 v_1^2 + \omega_6^2 \omega_{13} - 3\omega_6^2 - 12c_s^2 \omega_{13} - 3\omega_6 \omega_{13} - \omega_6^2 v_1^2 \omega_{13} + 15\omega_6 c_s^2 \omega_{13} + 3\omega_6^2 c_s^2 - 6\omega_6 v_1^2) \frac{v_1 \rho}{6\omega_6^2 \omega_{13}}$$

$$C_{D_x^3 v_3}^{(3), \text{MRT2}} = C_{D_x^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^3 v_3}^{(3), \text{CLBM1}} = (6 - 6v_1^2 - \omega_6 v_1^2 \omega_{13} - 3\omega_6 + 9\omega_6 c_s^2 - 3\omega_{13} + 3v_1^2 \omega_{13} + 9c_s^2 \omega_{13} + \omega_6 \omega_{13} - 3\omega_6 c_s^2 \omega_{13} + 3\omega_6 v_1^2 - 18c_s^2) \frac{v_1 \rho}{6\omega_6 \omega_{13}}$$

$$C_{D_x^3 v_3}^{(3), \text{CLBM2}} = C_{D_x^3 v_3}^{(3), \text{CLBM1}}$$

$$C_{D_x^3 v_3}^{(3), \text{CuLBM1}} = (6 - 6v_1^2 + 3v_1^2 \omega_{12} + 3v_1^2 \omega_2 - v_1^2 \omega_2 \omega_{12} + 9c_s^2 \omega_2 - 3\omega_2 - 18c_s^2 + \omega_2 \omega_{12} - 3c_s^2 \omega_2 \omega_{12} - 3\omega_{12} + 9c_s^2 \omega_{12}) \frac{v_1 \rho}{6\omega_2 \omega_{12}}$$

$$C_{D_x^3 v_3}^{(3), \text{CuLBM2}} = (-6v_1^2 \omega_4 + 6\omega_3 - 6\omega_3 c_s^2 \omega_4 \omega_1 - 18\omega_3 c_s^2 + 9\omega_3 c_s^2 \omega_1 + 9c_s^2 \omega_4 \omega_1 - 3\omega_4 \omega_1 + 6\omega_4 + 18\omega_3 c_s^2 \omega_4 - 2\omega_3 v_1^2 \omega_4 \omega_1 + 3\omega_3 v_1^2 \omega_1 - 6\omega_3 \omega_4 - 6\omega_3 v_1^2 - 3\omega_3 \omega_1 + 6\omega_3 v_1^2 \omega_4 - 18c_s^2 \omega_4 + 2\omega_3 \omega_4 \omega_1 + 3v_1^2 \omega_4 \omega_1) \frac{v_1 \rho}{12\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_x^2 D_y v_2}^{(3)}$ **at** $\frac{\partial^3 v_2}{\partial x_1^2 \partial x_2}$:

$$C_{D_x^2 D_y v_2}^{(3), \text{SRT}} = \frac{-v_3 c_s^2 \rho}{6}$$

$$C_{D_x^2 D_y v_2}^{(3), \text{MRT1}} = (6\omega_7 \omega_5 - 6\omega_7 \omega_8 - 6\omega_6 \omega_7 \omega_5 + 6\omega_6 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_7 \omega_8 - \omega_6 \omega_7 \omega_8 \omega_5) \frac{v_3 c_s^2 \rho}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x^2 D_y v_2}^{(3), \text{MRT2}} = C_{D_x^2 D_y v_2}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_y v_2}^{(3), \text{CLBM1}} = C_{D_x^2 D_y v_2}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(3), \text{CLBM2}} = C_{D_x^2 D_y v_2}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(3), \text{CuLBM1}} = C_{D_x^2 D_y v_2}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_y v_2}^{(3), \text{CuLBM2}} = C_{D_x^2 D_y v_2}^{(3), \text{SRT}}$$

$$\text{coefficient } C_{D_x^2 D_y v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_1^2 \partial x_2} :$$

$$C_{D_x^2 D_y v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x^2 D_y v_3}^{(3), \text{MRT1}} = (-\omega_7 \omega_8 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8 - \omega_6^2 \omega_7 + \omega_6 \omega_7 + \omega_6^2) \frac{c_s^2 v_2 \rho}{\omega_6^2 \omega_7 \omega_8}$$

$$C_{D_x^2 D_y v_3}^{(3), \text{MRT2}} = C_{D_x^2 D_y v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_y v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y v_3}^{(3), \text{CuLBM2}} = (-2\omega_3 + v_2^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 - 3\omega_3 c_s^2 \omega_1 + 3c_s^2 \omega_4 \omega_1 - \omega_4 \omega_1 + 2\omega_3 v_2^2 - \omega_3 v_2^2 \omega_1 + 2\omega_4 + \omega_3 \omega_1 - 6c_s^2 \omega_4 - 2v_2^2 \omega_4) \frac{v_2 \rho}{4\omega_3 \omega_4 \omega_1}$$

$$\text{coefficient } C_{D_x D_y^2 v_1}^{(3)} \text{ at } \frac{\partial^3 v_1}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_1}^{(3), \text{SRT}} = \frac{-v_3 c_s^2 \rho}{6}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{MRT1}} = (6\omega_7 \omega_5 - 6\omega_7 \omega_8 - 6\omega_6 \omega_7 \omega_5 + 6\omega_6 \omega_5 - 6\omega_6 \omega_8 + 6\omega_6 \omega_7 \omega_8 - \omega_6 \omega_7 \omega_8 \omega_5) \frac{v_3 c_s^2 \rho}{6\omega_6 \omega_7 \omega_8 \omega_5}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{MRT2}} = C_{D_x D_y^2 v_1}^{(3), \text{MRT1}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CLBM1}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CLBM2}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CuLBM1}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$C_{D_x D_y^2 v_1}^{(3), \text{CuLBM2}} = C_{D_x D_y^2 v_1}^{(3), \text{SRT}}$$

$$\text{coefficient } C_{D_x D_y^2 v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_1 \partial x_2^2} :$$

$$C_{D_x D_y^2 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{MRT1}} = (\omega_7^2 - \omega_7 \omega_8 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8 + \omega_6 \omega_7 - \omega_6 \omega_7^2) \frac{c_s^2 v_1 \rho}{\omega_6 \omega_7^2 \omega_8}$$

$$C_{D_x D_y^2 v_3}^{(3), \text{MRT2}} = C_{D_x D_y^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y^2 v_3}^{(3), \text{CuLBM2}} = (-2v_1^2 \omega_4 - 2\omega_3 + 6\omega_3 c_s^2 - 3\omega_3 c_s^2 \omega_1 + 3c_s^2 \omega_4 \omega_1 - \omega_4 \omega_1 + 2\omega_4 - \omega_3 v_1^2 \omega_1 + 2\omega_3 v_1^2 + \omega_3 \omega_1 - 6c_s^2 \omega_4 + v_1^2 \omega_4 \omega_1) \frac{v_1 \rho}{4\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_y^3 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^3}$:

$$C_{D_y^3 \rho}^{(3), \text{SRT}} = (-1 + 3c_s^2 + v_2^2) \frac{v_3 v_2}{12}$$

$$C_{D_y^3 \rho}^{(3), \text{MRT1}} = (3c_s^2 \omega_{16} \omega_{10} \omega_7 - \omega_{16} \omega_{10} \omega_7 - 6\omega_{16} v_2^2 \omega_7 - 12\omega_{16} + 12\omega_{10} - 18c_s^2 \omega_{16} \omega_7 + 36c_s^2 \omega_{16} + 6\omega_{16} \omega_7 - 36c_s^2 \omega_{10} + 18c_s^2 \omega_{10} \omega_7 - 6\omega_{10} \omega_7 - 12v_2^2 \omega_{10} + \omega_{16} v_2^2 \omega_{10} \omega_7 + 6v_2^2 \omega_{10} \omega_7 + 12\omega_{16} v_2^2) \frac{v_3 v_2}{12\omega_{16} \omega_{10} \omega_7}$$

$$C_{D_y^3 \rho}^{(3), \text{MRT2}} = C_{D_y^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_y^3 \rho}^{(3), \text{CLBM1}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(3), \text{CLBM2}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(3), \text{CuLBM1}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

$$C_{D_y^3 \rho}^{(3), \text{CuLBM2}} = C_{D_y^3 \rho}^{(3), \text{SRT}}$$

coefficient $C_{D_y^3 v_2}^{(3)}$ **at** $\frac{\partial^3 v_2}{\partial x_2^3}$:

$$C_{D_y^3 v_2}^{(3), \text{SRT}} = (-1 + c_s^2 + 3v_2^2) \frac{v_3 \rho}{12}$$

$$C_{D_y^3 v_2}^{(3), \text{MRT1}} = (c_s^2 \omega_{16} \omega_{10} \omega_7 - \omega_{16} \omega_{10} \omega_7 - 18\omega_{16} v_2^2 \omega_7 - 12\omega_{16} + 12\omega_{10} - 6c_s^2 \omega_{16} \omega_7 + 12c_s^2 \omega_{16} + 6\omega_{16} \omega_7 - 12c_s^2 \omega_{10} + 6c_s^2 \omega_{10} \omega_7 - 6\omega_{10} \omega_7 - 36v_2^2 \omega_{10} + 3\omega_{16} v_2^2 \omega_{10} \omega_7 + 18v_2^2 \omega_{10} \omega_7 + 36\omega_{16} v_2^2) \frac{v_3 \rho}{12\omega_{16} \omega_{10} \omega_7}$$

$$C_{D_y^3 v_2}^{(3), \text{MRT2}} = C_{D_y^3 v_2}^{(3), \text{MRT1}}$$

$$C_{D_y^3 v_2}^{(3), \text{CLBM1}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(3), \text{CLBM2}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(3), \text{CuLBM1}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

$$C_{D_y^3 v_2}^{(3), \text{CuLBM2}} = C_{D_y^3 v_2}^{(3), \text{SRT}}$$

coefficient $C_{D_y^3 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_2^3}$:

$$C_{D_y^3 v_3}^{(3), \text{SRT}} = (6 + \omega^2 - 6\omega - 3c_s^2 \omega^2 - v_2^2 \omega^2 + 6v_2^2 \omega + 18c_s^2 \omega - 18c_s^2 - 6v_2^2) \frac{v_2 \rho}{6\omega^2}$$

$$C_{D_y^3 v_3}^{(3), \text{MRT1}} = (\omega_{16} \omega_7^2 - 3c_s^2 \omega_{16} \omega_7^2 - 3\omega_7^2 + 3\omega_{16} v_2^2 \omega_7 - \omega_{16} v_2^2 \omega_7^2 + 6\omega_7 + 15c_s^2 \omega_{16} \omega_7 - 12c_s^2 \omega_{16} - 3\omega_{16} \omega_7 - 6v_2^2 \omega_7 - 6c_s^2 \omega_7 + 3c_s^2 \omega_7^2 + 3v_2^2 \omega_7^2) \frac{v_2 \rho}{6\omega_{16} \omega_7^2}$$

$$C_{D_y^3 v_3}^{(3), \text{MRT2}} = C_{D_y^3 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^3 v_3}^{(3), \text{CLBM1}} = (6 - \omega_{16} v_2^2 \omega_7 - 3\omega_{16} - 3\omega_7 - 3c_s^2 \omega_{16} \omega_7 + 9c_s^2 \omega_{16} + \omega_{16} \omega_7 + 3v_2^2 \omega_7 + 9c_s^2 \omega_7 + 3\omega_{16} v_2^2 - 18c_s^2 - 6v_2^2) \frac{v_2 \rho}{6\omega_{16} \omega_7}$$

$$C_{D_y^3 v_3}^{(3), \text{CLBM2}} = C_{D_y^3 v_3}^{(3), \text{CLBM1}}$$

$$C_{D_y^3 v_3}^{(3), \text{CuLBM1}} = (6 + 3v_2^2 \omega_{11} - 3\omega_3 + 9c_s^2 \omega_{11} + 9\omega_3 c_s^2 + 3\omega_3 v_2^2 + \omega_3 \omega_{11} - 3\omega_{11} - 3\omega_3 c_s^2 \omega_{11} - \omega_3 v_2^2 \omega_{11} - 18c_s^2 - 6v_2^2) \frac{v_2 \rho}{6\omega_3 \omega_{11}}$$

$$C_{D_y^3 v_3}^{(3), \text{CuLBM2}} = (6\omega_3 + 3v_2^2 \omega_4 \omega_1 - 6\omega_3 c_s^2 \omega_4 \omega_1 - 18\omega_3 c_s^2 + 9\omega_3 c_s^2 \omega_1 + 9c_s^2 \omega_4 \omega_1 - 3\omega_4 \omega_1 - 6\omega_3 v_2^2 + 6\omega_3 v_2^2 \omega_4 + 3\omega_3 v_2^2 \omega_1 - 2\omega_3 v_2^2 \omega_4 \omega_1 + 6\omega_4 + 18\omega_3 c_s^2 \omega_4 - 6\omega_3 \omega_4 - 3\omega_3 \omega_1 - 18c_s^2 \omega_4 - 6v_2^2 \omega_4 + 2\omega_3 \omega_4 \omega_1) \frac{v_2 \rho}{12\omega_3 \omega_4 \omega_1}$$

coefficient $C_{D_x^2 D_z \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z \rho}^{(3), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{MRT1}} = (-12 + 12\omega_6 - \omega_6^2) \frac{c_s^4}{6\omega_6^2}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{MRT2}} = C_{D_x^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CLBM1}} = C_{D_x^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CLBM2}} = C_{D_x^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CuLBM1}} = (-12 - \omega_2^2 + 12\omega_2) \frac{c_s^4}{6\omega_2^2}$$

$$C_{D_x^2 D_z \rho}^{(3), \text{CuLBM2}} = (3v_1^2 \omega_1^2 \omega_2 + 2c_s^4 \omega_1^2 - 18c_s^2 v_1^2 \omega_2^2 - 2c_s^2 \omega_1 \omega_2^2 - 15c_s^2 v_1^2 \omega_1^2 \omega_2 + 4v_1^2 \omega_2^2 + 12c_s^2 v_1^2 \omega_1^2 - 14c_s^4 \omega_2^2 - 2v_1^2 \omega_1^2 - 3v_1^4 \omega_1^2 \omega_2 + 14c_s^4 \omega_1 \omega_2^2 - 2c_s^2 \omega_1^2 - 3v_1^2 \omega_1 \omega_2^2 - c_s^4 \omega_1^2 \omega_2^2 - 4v_1^4 \omega_2^2 + 15c_s^2 v_1^2 \omega_1 \omega_2^2 + 2c_s^2 \omega_1^2 \omega_2 + 2v_1^4 \omega_1 \omega_2 + 3v_1^4 \omega_1 \omega_2^2 + 6c_s^2 v_1^2 \omega_1 \omega_2 + 2c_s^2 \omega_2^2 + 2v_1^4 \omega_1^2 - 2v_1^2 \omega_1 \omega_2 - 2c_s^4 \omega_1^2 \omega_2) \frac{1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_z v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{MRT1}} = (2\omega_6 - 2\omega_{13} - \omega_6^2 + \omega_6 \omega_{13}) \frac{c_s^2 v_1 \rho}{\omega_6^2 \omega_{13}}$$

$$C_{D_x^2 D_z v_1}^{(3), \text{MRT2}} = C_{D_x^2 D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_z v_1}^{(3), \text{CuLBM2}} = (6\omega_2^2 - 11v_1^2 \omega_1^2 \omega_2 + 9c_s^2 \omega_1 \omega_2^2 - 14v_1^2 \omega_2^2 - 5\omega_1 \omega_2^2 - 2\omega_1 \omega_2 + 8v_1^2 \omega_1^2 + 2c_s^2 \omega_1 \omega_2 - 4\omega_1^2 + 8c_s^2 \omega_1^2 + 11v_1^2 \omega_1 \omega_2^2 + 5\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 - 10c_s^2 \omega_2^2 + 6v_1^2 \omega_1 \omega_2) \frac{v_1 \rho}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^2 D_z v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_1^2 \partial x_3}$:

$$C_{D_x^2 D_z v_3}^{(3), \text{SRT}} = \frac{-v_3 c_s^2 \rho}{6}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{MRT1}} = (12\omega_6 \omega_{11} - \omega_6^2 \omega_{11} \omega_{18} + 12\omega_6^2 + 12\omega_6 \omega_{11} \omega_{18} - 12\omega_6 \omega_{18} - 12\omega_{11} \omega_{18} - 12\omega_6^2 \omega_{11}) \frac{v_3 c_s^2 \rho}{6\omega_6^2 \omega_{11} \omega_{18}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{MRT2}} = C_{D_x^2 D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CLBM1}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CLBM2}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CuLBM1}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_x^2 D_z v_3}^{(3), \text{CuLBM2}} = C_{D_x^2 D_z v_3}^{(3), \text{SRT}}$$

coefficient $C_{D_x D_y D_z \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{MRT1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{MRT2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z \rho}^{(3), \text{CuLBM2}} = (-2v_2^2 \omega_1 \omega_2 - 2\omega_2^2 + v_1^2 \omega_2^2 + 4\omega_1 \omega_2 + v_1^2 \omega_1^2 - 12c_s^2 \omega_1 \omega_2 - 2\omega_1^2 + 6c_s^2 \omega_1^2 + v_2^2 \omega_1^2 + v_2^2 \omega_2^2 + 6c_s^2 \omega_2^2 - 2v_1^2 \omega_1 \omega_2) \frac{v_2 v_1}{3\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{MRT1}} = (-\omega_7 \omega_8 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8 - \omega_6^2 \omega_7 + \omega_6 \omega_7 + \omega_6^2) \frac{c_s^2 v_2 \rho}{\omega_6^2 \omega_7 \omega_8}$$

$$C_{D_x D_y D_z v_1}^{(3), \text{MRT2}} = C_{D_x D_y D_z v_1}^{(3), \text{MRT1}}$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_1}^{(3), \text{CuLBM2}} = (\omega_3 v_2^2 \omega_4 \omega_1 \omega_2^2 - \omega_3 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_2^2 \omega_1 \omega_2^2 + 2\omega_3 v_2^2 \omega_4 \omega_1^2 + 3v_2^2 \omega_4 \omega_1^2 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 2v_2^2 \omega_4 \omega_1^2 \omega_2 - 2\omega_3 v_2^2 \omega_4 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_4 \omega_2^2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - \omega_3 v_2^2 \omega_4 \omega_2^2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 - 12\omega_3 v_1^2 \omega_4 \omega_1 \omega_2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 3\omega_3 v_2^2 \omega_1^2 \omega_2^2 + 6\omega_3 v_1^2 \omega_4 \omega_1^2 + 2\omega_4 \omega_1^2 \omega_2 - 4v_2^2 \omega_4 \omega_1 \omega_2^2) \frac{v_2 \rho}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_y D_z v_2}^{(3)}$ **at** $\frac{\partial^3 v_2}{\partial x_1 \partial x_2 \partial x_3}$:

$$C_{D_x D_y D_z v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{MRT1}} = (\omega_7^2 - \omega_7 \omega_8 - \omega_6 \omega_8 + \omega_6 \omega_7 \omega_8 + \omega_6 \omega_7 - \omega_6 \omega_7^2) \frac{c_s^2 v_1 \rho}{\omega_6 \omega_7^2 \omega_8}$$

$$C_{D_x D_y D_z v_2}^{(3), \text{MRT2}} = C_{D_x D_y D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x D_y D_z v_2}^{(3), \text{CuLBM2}} = (-\omega_3 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_2^2 \omega_4 \omega_1^2 - 3\omega_3 v_1^2 \omega_1^2 \omega_2^2 - 4v_1^2 \omega_4 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_4 \omega_2^2 - 3\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_3 c_s^2 \omega_4 \omega_1^2 + 18\omega_3 c_s^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_4 \omega_1 \omega_2^2 + 3\omega_3 \omega_1^2 \omega_2^2 - 12\omega_3 v_2^2 \omega_4 \omega_1 \omega_2 + 6\omega_3 v_2^2 \omega_4 \omega_2^2 + 4\omega_3 \omega_4 \omega_1 \omega_2 - \omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2 + 4\omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1 \omega_2^2 - 2\omega_3 v_1^2 \omega_4 \omega_2^2 - 2v_1^2 \omega_4 \omega_1^2 \omega_2 + \omega_3 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 \omega_4 \omega_1^2 - 3\omega_4 \omega_1^2 \omega_2^2 + 3\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 9\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 9c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 6c_s^2 \omega_4 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 + 2\omega_3 v_1^2 \omega_4 \omega_1^2 + 2\omega_4 \omega_1^2 \omega_2 + \omega_3 v_1^2 \omega_4 \omega_1 \omega_2^2 + 6\omega_3 v_1^2 \omega_1 \omega_2^2 + 3v_1^2 \omega_4 \omega_1^2 \omega_2^2) \frac{v_1 \rho}{6\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y^2 D_z \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_2^2 \partial x_3}$:

$$C_{D_y^2 D_z \rho}^{(3), \text{SRT}} = (-12 - \omega^2 + 12\omega) \frac{c_s^4}{6\omega^2}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{MRT1}} = (-12 - \omega_7^2 + 12\omega_7) \frac{c_s^4}{6\omega_7^2}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{MRT2}} = C_{D_y^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CLBM1}} = C_{D_y^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CLBM2}} = C_{D_y^2 D_z \rho}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CuLBM1}} = (-12 + 12\omega_3 - \omega_3^2) \frac{c_s^4}{6\omega_3^2}$$

$$C_{D_y^2 D_z \rho}^{(3), \text{CuLBM2}} = (2v_2^4 \omega_1^2 - 2v_2^2 \omega_1 \omega_2 + 2c_s^4 \omega_1^2 + 6c_s^2 v_2^2 \omega_1 \omega_2 - 2c_s^2 \omega_1 \omega_2^2 + 3v_2^4 \omega_1 \omega_2^2 - 14c_s^4 \omega_2^2 + 2v_2^4 \omega_1 \omega_2 + 15c_s^2 v_2^2 \omega_1 \omega_2^2 + 14c_s^4 \omega_1 \omega_2^2 - 4v_2^4 \omega_2^2 - 3v_2^2 \omega_1 \omega_2^2 - 2c_s^2 \omega_1^2 - c_s^4 \omega_1^2 \omega_2^2 - 2v_2^2 \omega_1^2 - 3v_2^4 \omega_1^2 \omega_2 + 2c_s^2 \omega_1^2 \omega_2 + 12c_s^2 v_2^2 \omega_1^2 - 15c_s^2 v_2^2 \omega_1^2 \omega_2 + 4v_2^2 \omega_2^2 - 18c_s^2 v_2^2 \omega_2^2 + 2c_s^2 \omega_2^2 + 3v_2^2 \omega_1^2 \omega_2 - 2c_s^4 \omega_1^2 \omega_2) \frac{1}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_y^2 D_z v_2}^{(3)} \text{ at } \frac{\partial^3 v_2}{\partial x_2^2 \partial x_3} :$$

$$C_{D_y^2 D_z v_2}^{(3), \text{SRT}} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{MRT1}} = (-\omega_7^2 - 2\omega_{16} + 2\omega_7 + \omega_{16} \omega_7) \frac{c_s^2 v_2 \rho}{\omega_{16} \omega_7^2}$$

$$C_{D_y^2 D_z v_2}^{(3), \text{MRT2}} = C_{D_y^2 D_z v_2}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y^2 D_z v_2}^{(3), \text{CuLBM2}} = (6v_2^2 \omega_1 \omega_2 + 6\omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 5\omega_1 \omega_2^2 - 2\omega_1 \omega_2 + 2c_s^2 \omega_1 \omega_2 - 4\omega_1^2 + 11v_2^2 \omega_1 \omega_2^2 + 8c_s^2 \omega_1^2 + 8v_2^2 \omega_1^2 + 5\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 - 14v_2^2 \omega_2^2 - 10c_s^2 \omega_2^2 - 11v_2^2 \omega_1^2 \omega_2) \frac{v_2 \rho}{6\omega_1^2 \omega_2^2}$$

$$\text{coefficient } C_{D_y^2 D_z v_3}^{(3)} \text{ at } \frac{\partial^3 v_3}{\partial x_2^2 \partial x_3} :$$

$$C_{D_y^2 D_z v_3}^{(3), \text{SRT}} = \frac{-v_3 c_s^2 \rho}{6}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{MRT1}} = (-12\omega_{19} \omega_7 + 12\omega_{19} \omega_7 \omega_{11} + 12\omega_7^2 + 12\omega_7 \omega_{11} - 12\omega_{19} \omega_{11} - 12\omega_7^2 \omega_{11} - \omega_{19} \omega_7^2 \omega_{11}) \frac{v_3 c_s^2 \rho}{6\omega_{19} \omega_7^2 \omega_{11}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{MRT2}} = C_{D_y^2 D_z v_3}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CLBM1}} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CLBM2}} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CuLBM1}} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$C_{D_y^2 D_z v_3}^{(3), \text{CuLBM2}} = C_{D_y^2 D_z v_3}^{(3), \text{SRT}}$$

$$\text{coefficient } C_{D_x D_z^2 \rho}^{(3)} \text{ at } \frac{\partial^3 \rho}{\partial x_1 \partial x_3^2} :$$

$$C_{D_x D_z^2 \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{MRT}1} = (\omega_6 \omega_{11} - \omega_6 v_3^2 \omega_{11} + v_3^2 \omega_{11} \omega_{18} + 3\omega_6 c_s^2 \omega_{11}^2 - v_3^2 \omega_{11}^2 - 3\omega_6 c_s^2 \omega_{11} \omega_{18} - 3c_s^2 \omega_{11}^2 - 3\omega_6 c_s^2 \omega_{11} - \omega_6 \omega_{11}^2 + \omega_6 v_3^2 \omega_{11}^2 - \omega_6 v_3^2 \omega_{11} \omega_{18} + \omega_6 \omega_{11} \omega_{18} - \omega_6 \omega_{18} + \omega_6 v_3^2 \omega_{18} + \omega_{11}^2 - \omega_{11} \omega_{18} + 3c_s^2 \omega_{11} \omega_{18} + 3\omega_6 c_s^2 \omega_{18}) \frac{v_3 v_1}{\omega_6 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 \rho}^{(3), \text{MRT}2} = C_{D_x D_z^2 \rho}^{(3), \text{MRT}1}$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CLBM}1} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CLBM}2} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CuLBM}1} = 0$$

$$C_{D_x D_z^2 \rho}^{(3), \text{CuLBM}2} = (2\omega_2^2 - 3v_1^2 \omega_1^2 \omega_2 + 9c_s^2 \omega_1 \omega_2^2 - 4v_1^2 \omega_2^2 - 3\omega_1 \omega_2^2 + 2\omega_1 \omega_2 + 2v_1^2 \omega_1^2 - 6c_s^2 \omega_1 \omega_2 - 4\omega_1^2 + 12c_s^2 \omega_1^2 + 2v_3^2 \omega_2^2 + 3v_1^2 \omega_1 \omega_2^2 - 4v_3^2 \omega_1 \omega_2 + 3\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 + 2v_3^2 \omega_1^2 - 6c_s^2 \omega_2^2 + 2v_1^2 \omega_1 \omega_2) \frac{v_3 v_1}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_1}^{(3)}$ **at** $\frac{\partial^3 v_1}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_1}^{(3), \text{SRT}} = (12 + 3\omega^2 - 12\omega + 12v_3^2 \omega - 11c_s^2 \omega^2 - 12v_3^2 + 36c_s^2 \omega - 36c_s^2 - 3v_3^2 \omega^2) \frac{v_3 \rho}{12\omega^2}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{MRT}1} = (-12\omega_6 c_s^2 \omega_{11}^2 - 6\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 36\omega_6^2 c_s^2 \omega_{18} - 24c_s^2 \omega_{11}^2 \omega_{18} - 11\omega_6^2 c_s^2 \omega_{11} \omega_{18} + 6\omega_6^2 \omega_{11} \omega_{18} - 24\omega_6 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 v_3^2 \omega_{18} + 6\omega_6 v_3^2 \omega_{11}^2 \omega_{18} - 6\omega_6 \omega_{11}^2 \omega_{18} + 12\omega_6 \omega_{11}^2 - 12\omega_6^2 \omega_{18} - 12\omega_6 v_3^2 \omega_{11}^2 - 12\omega_6^2 \omega_{11}^2 + 42\omega_6 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11} + 3\omega_6^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^2 - 12\omega_6^2 v_3^2 \omega_{11} + 12\omega_6^2 c_s^2 \omega_{11}^2 - 18\omega_6^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 \omega_{11} - 3\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}) \frac{v_3 \rho}{12\omega_6^2 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{MRT}2} = C_{D_x D_z^2 v_1}^{(3), \text{MRT}1}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CLBM}1} = (12\omega_6 \omega_{11} - 12\omega_6 v_3^2 \omega_{11} + 36\omega_6 c_s^2 \omega_{11}^2 - 6\omega_{11}^2 \omega_{18} - 12v_3^2 \omega_{11}^2 + 18c_s^2 \omega_{11}^2 \omega_{18} - 18\omega_6 c_s^2 \omega_{11} \omega_{18} - 36c_s^2 \omega_{11}^2 - 3\omega_6 v_3^2 \omega_{11}^2 \omega_{18} + 3\omega_6 \omega_{11}^2 \omega_{18} - 36\omega_6 c_s^2 \omega_{11} - 12\omega_6 \omega_{11}^2 + 12\omega_6 v_3^2 \omega_{11}^2 - 6\omega_6 v_3^2 \omega_{11} \omega_{18} + 6\omega_6 \omega_{11} \omega_{18} - 12\omega_6 \omega_{18} + 12\omega_6 v_3^2 \omega_{18} - 11\omega_6 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_{11}^2 + 6v_3^2 \omega_{11}^2 \omega_{18} + 36\omega_6 c_s^2 \omega_{18}) \frac{v_3 \rho}{12\omega_6 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CLBM}2} = C_{D_x D_z^2 v_1}^{(3), \text{CLBM}1}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CuLBM}1} = (36\omega_6^2 c_s^2 \omega_2 + 36c_s^2 \omega_8 \omega_2 - 11\omega_6^2 c_s^2 \omega_8 \omega_2 - 12\omega_8 \omega_2 - 12\omega_6^2 \omega_2 + 12\omega_6^2 v_3^2 \omega_2 - 6\omega_6 v_3^2 \omega_8 \omega_2 + 6\omega_6 \omega_8 \omega_2 - 6\omega_6^2 \omega_8 + 12\omega_6^2 + 6\omega_6^2 v_3^2 \omega_8 - 18\omega_6 c_s^2 \omega_8 \omega_2 + 3\omega_6^2 \omega_8 \omega_2 + 12\omega_6 \omega_2 - 12\omega_6 v_3^2 \omega_2 + 18\omega_6^2 c_s^2 \omega_8 - 36\omega_6^2 c_s^2 - 36\omega_6 c_s^2 \omega_2 + 12v_3^2 \omega_8 \omega_2 - 12\omega_6^2 v_3^2 - 3\omega_6^2 v_3^2 \omega_8 \omega_2) \frac{v_3 \rho}{12\omega_6^2 \omega_8 \omega_2}$$

$$C_{D_x D_z^2 v_1}^{(3), \text{CuLBM}2} = (-8\omega_3 \omega_4 \omega_1 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_2^2 + 2\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 6v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 12\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 11\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 4v_3^2 \omega_4 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^2 \omega_4 \omega_1^2 - 36\omega_3 c_s^2 \omega_1 \omega_2^2 - 24c_s^2 \omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 + 6\omega_3 v_3^2 \omega_1^2 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2 - 18\omega_3 v_1^2 \omega_4 \omega_1^2 \omega_2 + 8\omega_4 \omega_1 \omega_2^2 + 12\omega_3 \omega_1 \omega_2^2 - 24\omega_3 v_1^2 \omega_4 \omega_2^2 + 4\omega_3 v_3^2 \omega_4 \omega_1^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 12\omega_3 v_3^2 \omega_1 \omega_2^2 - 8\omega_3 \omega_4 \omega_1^2 - 6\omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 v_1^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12c_s^2 \omega_4 \omega_1^2 \omega_2 - 3\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8v_3^2 \omega_4 \omega_1 \omega_2^2 + 8\omega_3 v_3^2 \omega_4 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 v_1^2 \omega_4 \omega_1^2 + 4\omega_4 \omega_1^2 \omega_2 + 18\omega_3 v_1^2 \omega_4 \omega_1 \omega_2^2) \frac{v_3 \rho}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_x D_z^2 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_1 \partial x_3^2}$:

$$C_{D_x D_z^2 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{MRT}1} = (\omega_6 \omega_{11} - 3\omega_6 v_3^2 \omega_{11} + 3v_3^2 \omega_{11} \omega_{18} + \omega_6 c_s^2 \omega_{11}^2 - 3v_3^2 \omega_{11}^2 - \omega_6 c_s^2 \omega_{11} \omega_{18} - c_s^2 \omega_{11}^2 - \omega_6 c_s^2 \omega_{11} - \omega_6 \omega_{11}^2 + 3\omega_6 v_3^2 \omega_{11}^2 - 3\omega_6 v_3^2 \omega_{11} \omega_{18} + \omega_6 \omega_{11} \omega_{18} - \omega_6 \omega_{18} + 3\omega_6 v_3^2 \omega_{18} + \omega_{11}^2 - \omega_{11} \omega_{18} + c_s^2 \omega_{11} \omega_{18} + \omega_6 c_s^2 \omega_{18}) \frac{v_1 \rho}{\omega_6 \omega_{11}^2 \omega_{18}}$$

$$C_{D_x D_z^2 v_3}^{(3), \text{MRT}2} = C_{D_x D_z^2 v_3}^{(3), \text{MRT}1}$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CLBM}1} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CLBM}2} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CuLBM}1} = 0$$

$$C_{D_x D_z^2 v_3}^{(3), \text{CuLBM2}} = (\omega_3 \omega_1^2 \omega_2 - 2v_1^2 \omega_1^2 \omega_2 - 4\omega_3 c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1 \omega_2^2 + 6\omega_3 v_3^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 + 3\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_2^2 + 6\omega_3 v_3^2 \omega_1^2 - \omega_3 v_1^2 \omega_1^2 \omega_2 - \omega_3 \omega_1 \omega_2^2 + 2v_1^2 \omega_1 \omega_2^2 - 2\omega_3 v_1^2 \omega_2^2 + 2\omega_1^2 \omega_2 - 6c_s^2 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_1^2 - 12\omega_3 v_3^2 \omega_1 \omega_2 + 2\omega_3 v_1^2 \omega_1^2 + \omega_3 v_1^2 \omega_1 \omega_2^2 + 4\omega_3 \omega_1 \omega_2) \frac{v_1 \rho}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{MRT1}} = (\omega_{19} v_3^2 \omega_{11} - \omega_{19} \omega_7 + \omega_{19} \omega_7 \omega_{11} - \omega_{19} v_3^2 \omega_7 \omega_{11} + 3c_s^2 \omega_7 \omega_{11}^2 - v_3^2 \omega_{11}^2 - \omega_7 \omega_{11}^2 + \omega_7 \omega_{11} - 3c_s^2 \omega_7 \omega_{11} - 3c_s^2 \omega_{11}^2 + 3\omega_{19} c_s^2 \omega_{11} - \omega_{19} \omega_{11} + \omega_{19} v_3^2 \omega_7 - v_3^2 \omega_7 \omega_{11} + \omega_{11}^2 - 3\omega_{19} c_s^2 \omega_7 \omega_{11} + v_3^2 \omega_7 \omega_{11}^2 + 3\omega_{19} c_s^2 \omega_7) \frac{v_3 v_2}{\omega_{19} \omega_7 \omega_{11}^2}$$

$$C_{D_y D_z^2 \rho}^{(3), \text{MRT2}} = C_{D_y D_z^2 \rho}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CuLBM2}} = (2v_2^2 \omega_1 \omega_2 + 2\omega_2^2 + 9c_s^2 \omega_1 \omega_2^2 - 3\omega_1 \omega_2^2 + 2\omega_1 \omega_2 - 6c_s^2 \omega_1 \omega_2 - 4\omega_1^2 + 3v_2^2 \omega_1 \omega_2^2 + 12c_s^2 \omega_1^2 + 2v_3^2 \omega_2^2 - 4v_3^2 \omega_1 \omega_2 + 2v_2^2 \omega_1^2 + 3\omega_1^2 \omega_2 - 9c_s^2 \omega_1^2 \omega_2 - 4v_2^2 \omega_2^2 + 2v_3^2 \omega_1^2 - 6c_s^2 \omega_2^2 - 3v_2^2 \omega_1^2 \omega_2) \frac{v_3 v_2}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 v_2}^{(3)}$ **at** $\frac{\partial^3 v_2}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_2}^{(3), \text{SRT}} = (12 + 3\omega^2 - 12\omega + 12v_3^2 \omega - 11c_s^2 \omega^2 - 12v_3^2 + 36c_s^2 \omega - 36c_s^2 - 3v_3^2 \omega^2) \frac{v_3 \rho}{12\omega^2}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{MRT1}} = (12v_3^2 \omega_7^2 \omega_{11}^2 - 24\omega_{19} c_s^2 \omega_{11}^2 - 12c_s^2 \omega_7 \omega_{11}^2 - 18\omega_{19} c_s^2 \omega_7^2 \omega_{11} + 12\omega_7 \omega_{11}^2 - 11\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 + 6\omega_{19} v_3^2 \omega_7 \omega_{11}^2 - 6\omega_{19} \omega_7 \omega_{11}^2 - 12v_3^2 \omega_7^2 \omega_{11} - 12\omega_{19} \omega_7^2 - 3\omega_{19} v_3^2 \omega_7^2 \omega_{11}^2 + 3\omega_{19} \omega_7^2 \omega_{11}^2 + 36\omega_{19} c_s^2 \omega_{11}^2 + 12\omega_7^2 \omega_{11} + 42\omega_{19} c_s^2 \omega_7 \omega_{11}^2 - 12c_s^2 \omega_7^2 \omega_{11} + 12c_s^2 \omega_7^2 \omega_{11}^2 - 12\omega_7^2 \omega_{11}^2 - 24\omega_{19} c_s^2 \omega_7 \omega_{11} + 6\omega_{19} \omega_7^2 \omega_{11} - 12v_3^2 \omega_7 \omega_{11}^2 - 6\omega_{19} v_3^2 \omega_7^2 \omega_{11} + 12\omega_{19} v_3^2 \omega_7^2) \frac{v_3 \rho}{12\omega_{19} \omega_7^2 \omega_{11}^2}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{MRT2}} = C_{D_y D_z^2 v_2}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CLBM1}} = (-12\omega_{19} \omega_7 + 6\omega_{19} \omega_7 \omega_{11} - 6\omega_{19} v_3^2 \omega_7 \omega_{11} + 18\omega_{19} c_s^2 \omega_{11}^2 + 36c_s^2 \omega_7 \omega_{11}^2 - 12v_3^2 \omega_{11}^2 - 12\omega_7 \omega_{11}^2 + 12\omega_7 \omega_{11} - 36c_s^2 \omega_7 \omega_{11} - 36c_s^2 \omega_{11}^2 - 3\omega_{19} v_3^2 \omega_7 \omega_{11}^2 + 3\omega_{19} \omega_7 \omega_{11}^2 + 6\omega_{19} v_3^2 \omega_{11}^2 + 12\omega_{19} v_3^2 \omega_7 - 12v_3^2 \omega_7 \omega_{11} - 11\omega_{19} c_s^2 \omega_7 \omega_{11}^2 + 12\omega_{11}^2 - 18\omega_{19} c_s^2 \omega_7 \omega_{11} + 12v_3^2 \omega_7 \omega_{11}^2 + 36\omega_{19} c_s^2 \omega_7 - 6\omega_{19} \omega_{11}^2) \frac{v_3 \rho}{12\omega_{19} \omega_7 \omega_{11}^2}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CLBM2}} = C_{D_y D_z^2 v_2}^{(3), \text{CLBM1}}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CuLBM1}} = (-36\omega_6 \omega_3 c_s^2 + 18\omega_6^2 c_s^2 \omega_{10} + 12\omega_6 \omega_3 - 12\omega_6 \omega_3 v_3^2 - 11\omega_6^2 \omega_3 c_s^2 \omega_{10} + 36\omega_3 c_s^2 \omega_{10} - 6\omega_6^2 \omega_{10} + 3\omega_6^2 \omega_3 \omega_{10} - 3\omega_6^2 \omega_3 v_3^2 \omega_{10} + 12\omega_3 v_3^2 \omega_{10} + 6\omega_6^2 v_3^2 \omega_{10} + 12\omega_6^2 + 6\omega_6 \omega_3 \omega_{10} - 18\omega_6 \omega_3 c_s^2 \omega_{10} - 6\omega_6 \omega_3 v_3^2 \omega_{10} + 36\omega_6^2 \omega_3 c_s^2 - 12\omega_3 \omega_{10} - 36\omega_6^2 c_s^2 - 12\omega_6^2 v_3^2 - 12\omega_6^2 \omega_3 + 12\omega_6^2 \omega_3 v_3^2) \frac{v_3 \rho}{12\omega_6^2 \omega_3 \omega_{10}}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{CuLBM2}} = (18\omega_3 v_2^2 \omega_4 \omega_1 \omega_2^2 - 8\omega_3 \omega_4 \omega_1 \omega_2^2 + 12\omega_3 v_2^2 \omega_4 \omega_1^2 + 16\omega_3 c_s^2 \omega_4 \omega_2^2 + 2\omega_3 v_3^2 \omega_4 \omega_1 \omega_2^2 + 6v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 12\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2 - 11\omega_3 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 4v_3^2 \omega_4 \omega_1^2 \omega_2 + 16\omega_3 c_s^2 \omega_4 \omega_1^2 - 36\omega_3 c_s^2 \omega_1 \omega_2^2 - 24c_s^2 \omega_4 \omega_1 \omega_2^2 - 6\omega_3 \omega_1^2 \omega_2^2 + 6\omega_3 v_3^2 \omega_1^2 \omega_2^2 + 12\omega_3 v_2^2 \omega_4 \omega_1 \omega_2 - 24\omega_3 v_2^2 \omega_4 \omega_2^2 - 4\omega_3 \omega_4 \omega_1 \omega_2 + 8\omega_4 \omega_1 \omega_2^2 + 12\omega_3 \omega_1 \omega_2^2 + 4\omega_3 v_3^2 \omega_4 \omega_1^2 + 8\omega_3 \omega_4 \omega_1^2 \omega_2 - 12\omega_3 v_3^2 \omega_1 \omega_2^2 - 18\omega_3 v_2^2 \omega_4 \omega_1^2 \omega_2 - 8\omega_3 \omega_4 \omega_1^2 - 6\omega_4 \omega_1^2 \omega_2^2 + 12\omega_3 c_s^2 \omega_4 \omega_1 \omega_2^2 - 2\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2 + 18\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 18c_s^2 \omega_4 \omega_1^2 \omega_2^2 - 12c_s^2 \omega_4 \omega_1^2 \omega_2 - 3\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8v_3^2 \omega_4 \omega_1 \omega_2^2 + 8\omega_3 v_3^2 \omega_4 \omega_2^2 + 3\omega_3 \omega_4 \omega_1^2 \omega_2^2 + 4\omega_4 \omega_1^2 \omega_2) \frac{v_3 \rho}{12\omega_3 \omega_4 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_y D_z^2 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_2 \partial x_3^2}$:

$$C_{D_y D_z^2 v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{MRT1}} = (3\omega_{19} v_3^2 \omega_{11} - \omega_{19} \omega_7 + \omega_{19} \omega_7 \omega_{11} - 3\omega_{19} v_3^2 \omega_7 \omega_{11} + c_s^2 \omega_7 \omega_{11}^2 - 3v_3^2 \omega_{11}^2 - \omega_7 \omega_{11}^2 + \omega_7 \omega_{11} - c_s^2 \omega_7 \omega_{11} - c_s^2 \omega_{11}^2 + \omega_{19} c_s^2 \omega_{11} - \omega_{19} \omega_{11} + 3\omega_{19} v_3^2 \omega_7 - 3v_3^2 \omega_7 \omega_{11} + \omega_{11}^2 - \omega_{19} c_s^2 \omega_7 \omega_{11} + 3v_3^2 \omega_7 \omega_{11}^2 + \omega_{19} c_s^2 \omega_7) \frac{v_2 \rho}{\omega_{19} \omega_7 \omega_{11}^2}$$

$$C_{D_y D_z^2 v_3}^{(3), \text{MRT}^2} = C_{D_y D_z^2 v_3}^{(3), \text{MRT}^1}$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CLBM}^1} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CLBM}^2} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CuLBM}^1} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CuLBM}^2} = (\omega_3 v_2^2 \omega_1 \omega_2^2 + \omega_3 \omega_1^2 \omega_2 + 2\omega_3 v_2^2 \omega_1^2 - 4\omega_3 c_s^2 \omega_1 \omega_2 + 6c_s^2 \omega_1 \omega_2^2 - 2\omega_1 \omega_2^2 + 6\omega_3 v_3^2 \omega_2^2 + 8\omega_3 c_s^2 \omega_1^2 + 3\omega_3 c_s^2 \omega_1 \omega_2^2 - 4\omega_3 c_s^2 \omega_2^2 + 6\omega_3 v_3^2 \omega_1^2 - 2\omega_3 v_2^2 \omega_2^2 + 2v_2^2 \omega_1 \omega_2^2 - \omega_3 \omega_1 \omega_2^2 - \omega_3 v_2^2 \omega_1^2 \omega_2 + 2\omega_1^2 \omega_2 - 6c_s^2 \omega_1^2 \omega_2 - 3\omega_3 c_s^2 \omega_1^2 \omega_2 - 4\omega_3 \omega_1^2 - 12\omega_3 v_3^2 \omega_1 \omega_2 - 2v_2^2 \omega_1^2 \omega_2 + 4\omega_3 \omega_1 \omega_2) \frac{v_3 \rho}{6\omega_3 \omega_1^2 \omega_2^2}$$

coefficient $C_{D_z^3 \rho}^{(3)}$ **at** $\frac{\partial^3 \rho}{\partial x_3^3}$:

$$C_{D_z^3 \rho}^{(3), \text{SRT}} = (36v_3^4 - 36v_3^4 \omega - 144v_3^2 c_s^2 \omega + c_s^4 \omega^2 + 12c_s^4 + 24v_3^2 c_s^2 \omega^2 - 12c_s^4 \omega + 7v_3^4 \omega^2 + 144v_3^2 c_s^2 + 36v_3^2 \omega - c_s^2 \omega^2 - 36v_3^2 + 12c_s^2 \omega - 12c_s^2 - 7v_3^2 \omega^2) \frac{1}{12\omega^2}$$

$$C_{D_z^3 \rho}^{(3), \text{MRT}^1} = (36v_3^4 + 12c_s^2 \omega_{11} - 7v_3^2 \omega_{11}^2 + 12c_s^4 + 36v_3^2 \omega_{11} - c_s^2 \omega_{11}^2 + 144v_3^2 c_s^2 + 24v_3^2 c_s^2 \omega_{11}^2 - 12c_s^4 \omega_{11} + 7v_3^4 \omega_{11}^2 - 36v_3^2 - 36v_3^4 \omega_{11} - 12c_s^2 - 144v_3^2 c_s^2 \omega_{11} + c_s^4 \omega_{11}^2) \frac{1}{12\omega_{11}^2}$$

$$C_{D_z^3 \rho}^{(3), \text{MRT}^2} = C_{D_z^3 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_z^3 \rho}^{(3), \text{CLBM}^1} = C_{D_z^3 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_z^3 \rho}^{(3), \text{CLBM}^2} = C_{D_z^3 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_z^3 \rho}^{(3), \text{CuLBM}^1} = (36\omega_6 v_3^2 + \omega_6^2 c_s^4 + 36v_3^4 + 12\omega_6 c_s^2 - 144\omega_6 v_3^2 c_s^2 + 7\omega_6^2 v_3^4 + 12c_s^4 + 144v_3^2 c_s^2 - 36\omega_6 v_3^4 - \omega_6^2 c_s^2 - 36v_3^2 - 12\omega_6 c_s^4 - 7\omega_6^2 v_3^2 - 12c_s^2 + 24\omega_6^2 v_3^2 c_s^2) \frac{1}{12\omega_6^2}$$

$$C_{D_z^3 \rho}^{(3), \text{CuLBM}^2} = (-7v_3^2 \omega_1^2 \omega_2^2 - 48v_3^2 c_s^2 \omega_1^2 \omega_2 + 4c_s^4 \omega_1^2 + 16v_3^4 \omega_2^2 + 8c_s^2 \omega_1 \omega_2^2 + 72v_3^2 c_s^2 \omega_2^2 - 12v_3^4 \omega_1^2 \omega_2 + 4v_3^4 \omega_1^2 + 8c_s^4 \omega_2^2 + 7v_3^4 \omega_1^2 \omega_2^2 + 24v_3^2 c_s^2 \omega_1^2 + 24v_3^2 c_s^2 \omega_1^2 \omega_2^2 - 8c_s^4 \omega_1 \omega_2^2 + 12v_3^2 \omega_1^2 \omega_2 - 4c_s^2 \omega_1^2 - 16v_3^2 \omega_2^2 - 96v_3^2 c_s^2 \omega_1 \omega_2^2 + c_s^4 \omega_1^2 \omega_2^2 - 16v_3^2 \omega_1 \omega_2 - 24v_3^4 \omega_1 \omega_2^2 + 4c_s^2 \omega_1^2 \omega_2 - c_s^2 \omega_1^2 \omega_2^2 + 16v_3^4 \omega_1 \omega_2 - 4v_3^2 \omega_1^2 - 8c_s^2 \omega_2^2 + 24v_3^2 \omega_1 \omega_2^2 + 48v_3^2 c_s^2 \omega_1 \omega_2 - 4c_s^4 \omega_1^2 \omega_2) \frac{1}{12\omega_1^2 \omega_2^2}$$

coefficient $C_{D_z^3 v_3}^{(3)}$ **at** $\frac{\partial^3 v_3}{\partial x_3^3}$:

$$C_{D_z^3 v_3}^{(3), \text{SRT}} = (-24 - 4\omega^2 + 24\omega - 60v_3^2 \omega + 5c_s^2 \omega^2 + 60v_3^2 - 36c_s^2 \omega + 36c_s^2 + 11v_3^2 \omega^2) \frac{v_3 \rho}{6\omega^2}$$

$$C_{D_z^3 v_3}^{(3), \text{MRT}^1} = (-24 - 36c_s^2 \omega_{11} + 11v_3^2 \omega_{11}^2 - 60v_3^2 \omega_{11} + 5c_s^2 \omega_{11}^2 + 24\omega_{11} - 4\omega_{11}^2 + 60v_3^2 + 36c_s^2) \frac{v_3 \rho}{6\omega_{11}^2}$$

$$C_{D_z^3 v_3}^{(3), \text{MRT}^2} = C_{D_z^3 v_3}^{(3), \text{MRT}^1}$$

$$C_{D_z^3 v_3}^{(3), \text{CLBM}^1} = C_{D_z^3 v_3}^{(3), \text{MRT}^1}$$

$$C_{D_z^3 v_3}^{(3), \text{CLBM}^2} = C_{D_z^3 v_3}^{(3), \text{MRT}^1}$$

$$C_{D_z^3 v_3}^{(3), \text{CuLBM}^1} = (-24 - 60\omega_6 v_3^2 + 24\omega_6 - 36\omega_6 c_s^2 - 4\omega_6^2 + 5\omega_6^2 c_s^2 + 60v_3^2 + 11\omega_6^2 v_3^2 + 36c_s^2) \frac{v_3 \rho}{6\omega_6^2}$$

$$C_{D_z^3 v_3}^{(3), \text{CuLBM}^2} = (11v_3^2 \omega_1^2 \omega_2^2 - 12\omega_2^2 - 24c_s^2 \omega_1 \omega_2^2 + 16\omega_1 \omega_2^2 - 8\omega_1 \omega_2 + 8c_s^2 \omega_1 \omega_2 - 4\omega_1^2 - 20v_3^2 \omega_1^2 \omega_2 + 8c_s^2 \omega_1^2 + 28v_3^2 \omega_2^2 + 24v_3^2 \omega_1 \omega_2 + 8\omega_1^2 \omega_2 - 12c_s^2 \omega_1^2 \omega_2 + 5c_s^2 \omega_1^2 \omega_2^2 - 4\omega_1^2 \omega_2^2 + 8v_3^2 \omega_1^2 + 20c_s^2 \omega_2^2 - 40v_3^2 \omega_1 \omega_2^2) \frac{v_3 \rho}{6\omega_1^2 \omega_2^2}$$

coefficient $C_{D_x^4 \rho}^{(3)}$ **at** $\frac{\partial^4 \rho}{\partial x_1^4}$:

$$C_{D_x^4 \rho}^{(3), \text{SRT}} = (-6v_1^2 - 12c_s^2 v_1^2 \omega + 3v_1^2 \omega + 2c_s^4 - c_s^4 \omega - 3v_1^4 \omega + 6v_1^4 + c_s^2 \omega - 2c_s^2 + 24c_s^2 v_1^2) \frac{v_3}{24\omega}$$

$$C_{D_{x\rho}^4}^{(3),\text{MRT1}} = (24\omega_6 c_s^4 \omega_{13}^2 + 24\omega_6 v_1^2 \omega_9^2 - 216c_s^2 v_1^2 \omega_{13} \omega_9^2 - 126\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9^2 - 48\omega_6 c_s^2 \omega_{13} \omega_9^2 - 12\omega_6^2 c_s^2 \omega_9^2 - 24c_s^2 \omega_{13} \omega_9 - 36\omega_6^2 v_1^4 \omega_{13}^2 - 14\omega_6^2 c_s^2 \omega_{13}^2 \omega_9 + 24\omega_6^2 v_1^4 \omega_{13} \omega_9 + 432\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9^2 + 96\omega_6 v_1^2 \omega_{13}^2 \omega_9 + 48v_1^2 \omega_{13} \omega_9^2 - 144\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 + 30\omega_6^2 v_1^2 \omega_{13} \omega_9^2 - \omega_6^2 c_s^4 \omega_{13}^2 \omega_9^2 - 144\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9 + 48\omega_6 c_s^4 \omega_{13} \omega_9^2 + 24c_s^4 \omega_{13}^2 \omega_9 + 72\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9^2 - 24\omega_6^2 v_1^2 \omega_{13} \omega_9 + 14\omega_6^2 c_s^4 \omega_{13}^2 \omega_9 - 96\omega_6 v_1^4 \omega_{13}^2 \omega_9 + 72\omega_6^2 c_s^2 v_1^2 \omega_{13} \omega_9 - 48v_1^4 \omega_{13} \omega_9^2 + 12\omega_6^2 v_1^4 \omega_9^2 + 12\omega_6^2 c_s^2 \omega_{13}^2 + \omega_6^2 c_s^2 \omega_{13} \omega_9^2 - 30\omega_6^2 v_1^4 \omega_{13} \omega_9^2 - 72\omega_6 v_1^2 \omega_{13}^2 - 24\omega_6 c_s^4 \omega_9^2 + 48\omega_6 c_s^2 \omega_{13} \omega_9 + 24c_s^2 \omega_{13} \omega_9^2 + 150\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 \omega_9 - 48\omega_6 v_1^4 \omega_{13} \omega_9 - 3\omega_6^2 v_1^4 \omega_{13}^2 \omega_9^2 + 12\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 216c_s^2 v_1^2 \omega_{13}^2 \omega_9 - 24\omega_6 c_s^2 \omega_{13}^2 - 24\omega_6 v_1^4 \omega_9^2 - 96\omega_6 v_1^2 \omega_{13} \omega_9^2 - 48v_1^2 \omega_{13}^2 \omega_9 + 12\omega_6^2 c_s^4 \omega_9^2 - 432\omega_6 c_s^2 v_1^2 \omega_{13} \omega_9 + 36\omega_6^2 v_1^2 \omega_{13}^2 - 36\omega_6^2 v_1^2 \omega_{13} \omega_9 + 288\omega_6 c_s^2 v_1^2 \omega_{13}^2 - 144\omega_6 c_s^2 v_1^2 \omega_9^2 + 48\omega_6 v_1^2 \omega_{13} \omega_9 - 12\omega_6^2 v_1^2 \omega_9^2 - 48\omega_6 c_s^4 \omega_{13}^2 \omega_9 - 24c_s^4 \omega_{13} \omega_9^2 - 12\omega_6^2 c_s^4 \omega_{13} \omega_9^2 - 12\omega_6^2 c_s^4 \omega_{13}^2 + 3\omega_6^2 v_1^2 \omega_{13}^2 \omega_9^2 + 72\omega_6 v_1^4 \omega_{13}^2 + 24\omega_6 c_s^2 \omega_9^2 + 96\omega_6 v_1^4 \omega_{13} \omega_9^2 + 48v_1^4 \omega_{13}^2 \omega_9 - 12\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 \omega_9^2 + 36\omega_6^2 v_1^4 \omega_{13} \omega_9^2) \frac{v_3}{24\omega_6^2 \omega_{13}^2 \omega_9^2}$$

$$C_{D_{x\rho}^4}^{(3),\text{MRT2}} = C_{D_{x\rho}^4}^{(3),\text{MRT1}}$$

$$C_{D_{x\rho}^4}^{(3),\text{CLBM1}} = (-6v_1^2 - 12c_s^2 v_1^2 \omega_9 + 3v_1^2 \omega_9 + 2c_s^4 - c_s^4 \omega_9 - 3v_1^4 \omega_9 + 6v_1^4 + c_s^2 \omega_9 - 2c_s^2 + 24c_s^2 v_1^2) \frac{v_3}{24\omega_9}$$

$$C_{D_{x\rho}^4}^{(3),\text{CLBM2}} = C_{D_{x\rho}^4}^{(3),\text{CLBM1}}$$

$$C_{D_{x\rho}^4}^{(3),\text{CuLBM1}} = (-6v_1^2 - 12c_s^2 v_1^2 \omega_4 + 3v_1^2 \omega_4 + 2c_s^4 - c_s^4 \omega_4 - 3v_1^4 \omega_4 + c_s^2 \omega_4 + 6v_1^4 - 2c_s^2 + 24c_s^2 v_1^2) \frac{v_3}{24\omega_4}$$

$$C_{D_{x\rho}^4}^{(3),\text{CuLBM2}} = (-3c_s^4 \omega_1 \omega_2 - 6v_1^2 \omega_1 + 4c_s^4 \omega_2 + 24c_s^2 v_1^2 \omega_1 - 12v_1^2 \omega_2 + 48c_s^2 v_1^2 \omega_2 + 2c_s^4 \omega_1 + 3c_s^2 \omega_1 \omega_2 + 6v_1^4 \omega_1 - 4c_s^2 \omega_2 - 9v_1^4 \omega_1 \omega_2 - 36c_s^2 v_1^2 \omega_1 \omega_2 + 12v_1^4 \omega_2 - 2c_s^2 \omega_1 + 9v_1^2 \omega_1 \omega_2) \frac{v_3}{72\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_{xv_1}^4}^{(3)} \text{ at } \frac{\partial^4 v_1}{\partial x_1^4} :$$

$$C_{D_{xv_1}^4}^{(3),\text{SRT}} = (-4 + 10v_1^2 - 5v_1^2 \omega + 2\omega - 3c_s^2 \omega + 6c_s^2) \frac{v_3 v_1 \rho}{12\omega}$$

$$C_{D_{xv_1}^4}^{(3),\text{MRT1}} = (-36\omega_{13}^2 \omega_9 - 48\omega_6 v_1^2 \omega_9^2 + 21\omega_6^2 \omega_{13} \omega_9^2 + 120\omega_6 c_s^2 \omega_{13} \omega_9^2 + 24\omega_6^2 c_s^2 \omega_9^2 + 60c_s^2 \omega_{13}^2 \omega_9 + 39\omega_6^2 c_s^2 \omega_{13} \omega_9 - 168\omega_6 v_1^2 \omega_{13}^2 \omega_9 - 84v_1^2 \omega_{13} \omega_9^2 + 24\omega_6^2 \omega_{13}^2 - 51\omega_6^2 v_1^2 \omega_{13} \omega_9^2 + 72\omega_6 \omega_{13}^2 \omega_9 - 12\omega_6^2 \omega_9^2 + 36\omega_6^2 v_1^2 \omega_{13} \omega_9 - 12\omega_6^2 \omega_{13} \omega_9 - 24\omega_6 c_s^2 \omega_{13} \omega_9 - 36\omega_6^2 c_s^2 \omega_{13}^2 - 3\omega_6^2 c_s^2 \omega_{13}^2 \omega_9^2 + 120\omega_6 v_1^2 \omega_{13}^2 - 120\omega_6 c_s^2 \omega_{13}^2 \omega_9 - 60c_s^2 \omega_{13} \omega_9^2 - 25\omega_6^2 \omega_{13}^2 \omega_9 - 33\omega_6^2 c_s^2 \omega_{13} \omega_9^2 + 36\omega_{13} \omega_9^2 + 72\omega_6 c_s^2 \omega_{13}^2 + 24\omega_6 \omega_{13} \omega_9 + 168\omega_6 v_1^2 \omega_{13} \omega_9^2 + 84v_1^2 \omega_{13}^2 \omega_9 - 60\omega_6^2 v_1^2 \omega_{13}^2 + 61\omega_6^2 v_1^2 \omega_{13}^2 \omega_9 + 24\omega_6 \omega_9^2 - 48\omega_6 \omega_{13}^2 - 72\omega_6 v_1^2 \omega_{13} \omega_9 + 24\omega_6^2 v_1^2 \omega_9^2 - 5\omega_6^2 v_1^2 \omega_{13}^2 \omega_9^2 - 48\omega_6 c_s^2 \omega_9^2 - 72\omega_6 \omega_{13} \omega_9^2 + 2\omega_6^2 \omega_{13}^2 \omega_9^2 + 12\omega_6^2 c_s^2 \omega_{13} \omega_9^2) \frac{v_3 v_1 \rho}{12\omega_6^2 \omega_{13}^2 \omega_9^2}$$

$$C_{D_{xv_1}^4}^{(3),\text{MRT2}} = C_{D_{xv_1}^4}^{(3),\text{MRT1}}$$

$$C_{D_{xv_1}^4}^{(3),\text{CLBM1}} = (-4 + 10v_1^2 - 5v_1^2 \omega_9 - 3c_s^2 \omega_9 + 6c_s^2 + 2\omega_9) \frac{v_3 v_1 \rho}{12\omega_9}$$

$$C_{D_{xv_1}^4}^{(3),\text{CLBM2}} = C_{D_{xv_1}^4}^{(3),\text{CLBM1}}$$

$$C_{D_{xv_1}^4}^{(3),\text{CuLBM1}} = (-4 + 10v_1^2 - 5v_1^2 \omega_4 + 2\omega_4 - 3c_s^2 \omega_4 + 6c_s^2) \frac{v_3 v_1 \rho}{12\omega_4}$$

$$C_{D_{xv_1}^4}^{(3),\text{CuLBM2}} = (10v_1^2 \omega_1 + 20v_1^2 \omega_2 + 6\omega_1 \omega_2 - 9c_s^2 \omega_1 \omega_2 - 4\omega_1 + 12c_s^2 \omega_2 - 8\omega_2 + 6c_s^2 \omega_1 - 15v_1^2 \omega_1 \omega_2) \frac{v_3 v_1 \rho}{36\omega_1 \omega_2}$$

$$\text{coefficient } C_{D_{xv_3}^4}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^4} :$$

$$C_{D_{xv_3}^4}^{(3),\text{SRT}} = (72v_1^2 - 3c_s^4 \omega^3 + 216c_s^2 v_1^2 \omega + 30c_s^4 \omega^2 - 108v_1^2 \omega + 48c_s^4 + 42v_1^2 \omega^2 - 72c_s^4 \omega - 84c_s^2 v_1^2 \omega^2 - 3v_1^2 \omega^3 + 6c_s^2 v_1^2 \omega^3 + 108v_1^4 \omega - 14c_s^2 \omega^2 + c_s^2 \omega^3 + 3v_1^4 \omega^3 - 72v_1^4 + 36c_s^2 \omega - 42v_1^4 \omega^2 - 24c_s^2 - 144c_s^2 v_1^2) \frac{\rho}{24\omega^3}$$

$$C_{D_{xv_3}^4}^{(3),\text{MRT1}} = (48\omega_6 v_1^2 \omega_{13} - 48\omega_6 c_s^4 \omega_{13}^2 - 3\omega_6^3 v_1^2 \omega_{13}^2 + 6\omega_6^3 c_s^4 \omega_{13} - 24\omega_6^2 v_1^4 \omega_{13}^2 + 24\omega_6^2 c_s^2 \omega_{13} - 72\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 - 96c_s^2 v_1^2 \omega_{13}^2 - 12\omega_6^3 c_s^2 v_1^2 \omega_{13} + 24\omega_6^2 v_1^2 + 6\omega_6^3 c_s^2 v_1^2 \omega_{13} + 24c_s^4 \omega_{13} + 48\omega_6^2 c_s^2 v_1^2 \omega_{13} - 12\omega_6^3 v_1^2 - 8\omega_6^2 c_s^2 \omega_{13}^2 + 72\omega_6^2 v_1^4 \omega_{13} - 24\omega_6^2 c_s^2 v_1^2 + 24\omega_6 c_s^4 \omega_{13} - 24\omega_6 v_1^2 \omega_{13}^2 - 3\omega_6^3 c_s^4 \omega_{13}^2 + 18\omega_6^3 v_1^2 \omega_{13} + 12\omega_6 c_s^2 \omega_{13}^2 - 48\omega_6 v_1^4 \omega_{13} - 6\omega_6^3 c_s^2 \omega_{13} + 3\omega_6^3 v_1^4 \omega_{13} + 12\omega_6^3 v_1^2 \omega_{13}^2 - 24\omega_6^2 c_s^4 \omega_{13} + 24\omega_6^2 v_1^2 \omega_{13} + 156\omega_6 c_s^2 v_1^2 \omega_{13}^2 + 12\omega_6^3 c_s^2 v_1^2 - 72\omega_6^2 v_1^2 \omega_{13} + 24\omega_6^2 c_s^4 \omega_{13}^2 - 24\omega_6 c_s^2 v_1^2 \omega_{13} + 24\omega_6 v_1^4 \omega_{13}^2 - 24\omega_6 c_s^2 \omega_{13} - 18\omega_6^3 v_1^4 \omega_{13} + \omega_6^3 c_s^2 \omega_{13}^2 - 24\omega_6^2 v_1^4) \frac{\rho}{24\omega_6^3 \omega_{13}^2}$$

$$C_{D_{xv_3}^4}^{(3),\text{MRT2}} = C_{D_{xv_3}^4}^{(3),\text{MRT1}}$$

$$C_{D_{xv_3}^4}^{(3),\text{CLBM1}} = (-48\omega_6 c_s^4 \omega_{13}^2 - 3\omega_6^3 v_1^2 \omega_{13}^2 + 6\omega_6^3 c_s^4 \omega_{13} - 12\omega_6^2 v_1^4 \omega_{13}^2 + 24\omega_6^2 c_s^2 \omega_{13} - 12\omega_6^2 c_s^2 v_1^2 \omega_{13}^2 - 72\omega_6^3 c_s^2 v_1^2 \omega_{13} + 72\omega_6^2 v_1^2 + 6\omega_6^3 c_s^2 v_1^2 \omega_{13}^2 + 24c_s^4 \omega_{13}^2 + 144\omega_6^2 c_s^2 v_1^2 \omega_{13} - 36\omega_6^3 v_1^2 - 8\omega_6^2 c_s^2 \omega_{13}^2 + 72\omega_6^2 v_1^4 \omega_{13} - 216\omega_6^2 c_s^2 v_1^2 + 24\omega_6 c_s^4 \omega_{13} - 3\omega_6^3 c_s^4 \omega_{13}^2 + 30\omega_6^3 v_1^2 \omega_{13} + 12\omega_6 c_s^2 \omega_{13}^2 - 6\omega_6^3 c_s^2 \omega_{13} + 3\omega_6^3 v_1^4 \omega_{13} + 36\omega_6^3 v_1^2 \omega_{13}^2 - 24\omega_6^2 c_s^4 \omega_{13} + 12\omega_6^2 v_1^2 \omega_{13}^2 - 36\omega_6 c_s^2 v_1^2 \omega_{13}^2 + 108\omega_6^3 c_s^2 v_1^2 - 72\omega_6^2 v_1^2 \omega_{13} + 24\omega_6^2 c_s^4 \omega_{13}^2 + 72\omega_6 c_s^2 v_1^2 \omega_{13} - 24\omega_6 c_s^2 \omega_{13} - 30\omega_6^3 v_1^4 \omega_{13} + \omega_6^3 c_s^2 \omega_{13}^2 - 72\omega_6^2 v_1^4) \frac{\rho}{24\omega_6^3 \omega_{13}^2}$$

$$C_{D_x^4 v_3}^{(3), \text{CLBM2}} = C_{D_x^4 v_3}^{(3), \text{CLBM1}}$$

$$C(3, \text{CuLBM1}) = \frac{D_4^4 v_3}{x} (6c_s^2 \omega_1^2 \omega_2 - 36c_s^2 v_1^2 \omega_2 \omega_{12} + 108c_s^2 v_1^2 \omega_3^2 - 36v_1^2 \omega_3^2 + 24c_s^2 \omega_2^2 \omega_{12} - 216c_s^2 v_1^2 \omega_2^2 + 24c_s^4 \omega_2^2 \omega_{12} + 24c_s^4 \omega_2^2 + c_s^2 \omega_3^2 \omega_{12} + 72v_1^2 \omega_2^2 - 6c_s^2 \omega_3^2 \omega_{12} - 24c_s^4 \omega_3^2 \omega_{12} - 8c_s^2 \omega_2^2 \omega_{12} - 3c_s^4 \omega_3^2 \omega_{12} + 72c_s^2 v_1^2 \omega_2 \omega_{12} + 12c_s^2 \omega_2^2 \omega_{12} - 12v_1^2 \omega_2^2 \omega_{12} + 144c_s^2 v_1^2 \omega_2^2 \omega_{12} - 3v_1^2 \omega_3^2 \omega_{12} - 72v_1^4 \omega_2^2 - 30v_1^4 \omega_3^2 \omega_{12} + 36v_1^4 \omega_3^2 + 6c_s^2 v_1^2 \omega_3^2 \omega_{12} - 72v_1^2 \omega_3^2 \omega_{12} + 24c_s^4 \omega_2 \omega_{12} - 72c_s^2 v_1^2 \omega_3^2 \omega_{12} + 12v_1^2 \omega_2^2 \omega_{12}^2 - 48c_s^4 \omega_2 \omega_{12}^2 + 3v_1^2 \omega_3^2 \omega_{12}^2 - 12c_s^2 v_1^2 \omega_2^2 \omega_{12}^2 + 30v_1^2 \omega_3^2 \omega_{12}^2 - 24c_s^2 \omega_2 \omega_{12}^2 + 72v_1^2 \omega_2^2 \omega_{12}^2) \frac{\ell}{24\omega_2^3 \omega_{12}^2}$$

$$\begin{aligned} C_{\frac{D_4 \times v_1}{2}}^{(3), \text{CuLBM2}} &= (36\omega_2^3 c_s^2 v_1^2 \omega_4 \omega_1 - 36\omega_3 v_1^2 \omega_4^2 \omega_1^2 - 9\omega_3^2 v_1^2 \omega_1^3 - 48\omega_3^2 c_s^4 \omega_1^2 \omega_1 - 15\omega_3^2 v_1^4 \omega_4 \omega_1^3 + 9v_1^4 \omega_4^2 \omega_1^3 + \omega_3^2 c_s^2 \omega_1^2 \omega_1^3 + 18\omega_3^2 v_1^2 \omega_1^2 + \\ &15\omega_3^2 v_1^2 \omega_4^2 \omega_1^3 - 8\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 - 18\omega_1^4 \omega_4^2 \omega_1^2 + 36\omega_3^2 v_1^4 \omega_4 \omega_1^2 + 36\omega_3 v_1^4 \omega_1^2 \omega_1^2 - 108\omega_3 c_s^2 v_1^4 \omega_4 \omega_1^2 + 12\omega_3^2 c_s^2 \omega_4^2 \omega_1 - 3\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 - 9v_1^2 \omega_4^2 \omega_1^3 - \\ &54c_s^2 v_1^2 \omega_2^2 \omega_1^2 + 15\omega_2^2 v_1^2 \omega_4 \omega_1^3 - 36\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^3 + 24\omega_3^2 c_s^4 \omega_1^2 + 54\omega_3 c_s^2 v_1^2 \omega_4 \omega_1^3 - 15\omega_3 v_1^2 \omega_2^2 \omega_1^3 + 72\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^2 + 27c_s^2 v_1^2 \omega_1^2 \omega_1^3 - 36\omega_3^2 v_1^2 \omega_4 \omega_1^2 + \\ &18v_1^2 \omega_1^2 \omega_1^2 + 24\omega_3^2 c_s^4 \omega_1^2 \omega_1^2 - 18\omega_3^2 v_1^4 \omega_1^2 + 27\omega_3^2 c_s^2 v_1^2 \omega_1^3 - 36\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_1^3 + 18\omega_3 v_1^4 \omega_4 \omega_1^3 - 3\omega_3^2 c_s^2 \omega_1^2 \omega_1^3 - 12\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^4 \omega_1^2 \omega_1 - \\ &12\omega_3^2 c_s^4 \omega_4 \omega_1^2 + 12\omega_3^2 v_1^2 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^4 \omega_1^2 \omega_1^2 - 54\omega_3^2 c_s^2 v_1^2 \omega_1^2 - 36\omega_3 v_1^2 \omega_1^2 \omega_1^2 + 72\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_1^2 - 12\omega_3^2 c_s^2 \omega_4 \omega_1^2 + 9\omega_3^2 v_1^4 \omega_1^3 - 3\omega_3^2 v_1^2 \omega_4^2 \omega_1 - \\ &3\omega_3^2 c_s^4 \omega_4 \omega_1^3 + 6\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^3 + 3\omega_3 c_s^2 \omega_4^2 \omega_1^3 - 18\omega_3 v_1^2 \omega_4 \omega_1^3 - 12\omega_3 c_s^2 \omega_1^2 \omega_1^2 + 36\omega_3 c_s^2 v_1^2 \omega_4 \omega_1^2 - 12\omega_3^2 v_1^4 \omega_4^2 \omega_1^2 + 12\omega_3^2 c_s^2 \omega_4 \omega_1^2 + 36\omega_3 v_1^2 \omega_4 \omega_1^2 - \\ &12\omega_3 c_s^2 \omega_4^2 \omega_1^2 - 36\omega_3 c_s^2 v_1^2 \omega_4^2 \omega_1 + 12\omega_3^2 c_s^2 \omega_4 \omega_1 - 3\omega_3^2 c_s^2 \omega_4 \omega_1^3 + 3\omega_3^2 v_1^4 \omega_4^2 \omega_1^3) \frac{\rho}{24\omega_3^2 \omega_1^2 \omega_1^3} \end{aligned}$$

coefficient $C_{D_x^3 D_y \rho}^{(3)}$ at $\frac{\partial^4 \rho}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y \rho}^{(3), \text{SRT}} = 0$$

$$\begin{aligned} C_{\frac{D_3 D_{10}}{D_6 D_9}}(3, \text{MRTI}) = & (-12w_6^2c_s^2w_{13}w_{14}w_5w_9w_{12} - 2w_6^2w_{13}w_{14}w_8w_5w_9^2 - 2w_6^2w_{13}w_7w_8w_5w_9^2w_{12} - 4w_6v_1^2w_{13}w_7w_8w_5w_9^2w_{12} - 12w_6^2c_s^2w_{13}w_7w_5w_9^2w_{12} - \\ & 2w_6^2w_{13}^2w_{13}w_7w_{14}w_8w_5w_{12} + 4v_1^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} + 2w_6^2v_1^2w_{13}w_7w_{14}w_8w_5w_9 - 4w_6v_1^2w_{13}^2w_7w_{14}w_5w_9w_{12} + 4w_{13}w_7w_{14}w_8w_5w_9^2w_{12} - \\ & 6w_6^2c_s^2w_{13}w_8w_5w_9^2w_{12} - 4w_6^2w_{13}w_7w_{14}w_5w_9w_{12} - 4w_6^2v_1^2w_{13}w_7w_{14}w_8w_5w_9w_{12} - 4v_1^2w_{13}w_7w_{14}w_8w_5w_9^2w_{12} + 2w_6^2v_1^2w_{13}w_{14}w_8w_5w_9^2w_{12} + \\ & 4w_6^2w_{13}^2w_{14}w_8w_9^2 - 4w_6^2v_1^2w_{13}^2w_7w_5w_9^2w_{12} - 4w_6^2v_1^2w_{13}^2w_{14}w_5w_9w_{12} - 4w_6w_{13}^2w_7w_{14}w_8w_5w_9^2 + 6w_6^2c_s^2w_7w_{14}w_8w_5w_9^2w_{12} + \\ & 12w_6c_s^2w_{13}w_7w_8w_5w_9^2w_{12} - 2w_6^2v_1^2w_{13}w_8w_5w_9^2w_{12} + 4w_6v_1^2w_{13}^2w_{14}w_8w_5w_9w_{12} + 2w_6^2w_{13}^2w_{14}w_8w_5w_9w_{12} - 4w_{13}^2w_7w_{14}w_8w_5w_9w_{12} - \\ & 9w_6^2c_s^2w_{13}w_7w_{14}w_8w_5w_9^2 + 4w_6w_7w_{14}w_8w_5w_9^2w_{12} + 4w_6v_1^2w_{13}w_{14}w_8w_9^2 - 12w_6^2c_s^2w_{13}w_7w_{14}w_8w_9w_{12} + 4w_6w_{13}^2w_7w_{14}w_8w_5w_9 + \\ & 9w_6^2c_s^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} + 24w_6c_s^2w_{13}w_7w_{14}w_8w_5w_9^2w_{12} - 4w_6w_{13}^2w_7w_{14}w_8w_9w_{12} - 12w_6^2c_s^2w_{13}w_7w_{14}w_5w_9w_{12} + 6w_6^2c_s^2w_{13}^2w_7w_{14}w_8w_5w_9 + \\ & 8w_6w_{13}^2w_7w_{14}w_8w_5w_9w_{12} - 6w_6^2c_s^2w_{13}^2w_7w_{14}w_8w_5w_{12} - 12w_6c_s^2w_{13}^2w_7w_8w_5w_9^2w_{12} - 12w_6^2c_s^2w_{13}^2w_{14}w_8w_9^2 - 4w_6^2w_{13}^2w_7w_{14}w_8w_9^2 - \\ & 4w_6v_1^2w_{13}^2w_7w_{14}w_8w_9^2 - 4w_6w_{13}^2w_7w_{14}w_8w_5w_{12} + 2w_6^2w_{13}^2w_7w_8w_5w_9^2w_{12} - 3w_6^2v_1^2w_{13}^2w_7w_{14}w_8w_5w_9^2 - 24w_6c_s^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} - \\ & 6w_6^2c_s^2w_{13}w_7w_{14}w_8w_5w_9^2w_{12} + 12w_6c_s^2w_{13}w_7w_{14}w_8w_5w_9w_{12} + 2w_6^2v_1^2w_7w_{14}w_8w_5w_9^2w_{12} + 4w_6v_1^2w_{13}w_7w_8w_5w_9^2w_{12} + 4w_6w_{13}^2w_{14}w_8w_5w_9^2w_{12} + \\ & 4w_6^2v_1^2w_{13}^2w_7w_8w_9^2w_{12} - 12w_6c_s^2w_{13}^2w_7w_{14}w_8w_9^2 - 4w_6^2w_{13}^2w_{14}w_8w_5w_{12} + 6w_6^2c_s^2w_{13}w_{14}w_8w_5w_9^2w_{12} - 8w_6v_1^2w_{13}w_7w_{14}w_8w_5w_9^2w_{12} + \\ & 4w_6^2v_1^2w_{13}^2w_7w_{14}w_5w_9w_{12} - 4w_6v_1^2w_{13}^2w_7w_{14}w_8w_5w_9 + 4w_6^2w_{13}^2w_7w_{14}w_8w_9w_{12} - 2w_6^2w_{13}^2w_7w_{14}w_8w_5w_9 + 4w_6v_1^2w_{13}^2w_7w_{14}w_8w_9w_{12} - \\ & 4w_6w_{13}^2w_7w_5w_9^2w_{12} + 2w_6^2w_{13}^2w_7w_{14}w_8w_5w_{12} + 4w_6^2v_1^2w_{13}^2w_7w_{14}w_8w_9^2 - 4w_6^2w_{13}^2w_5w_9^2w_{12} + 4w_6v_1^2w_{13}^2w_7w_{14}w_8w_5w_{12} + \\ & 12w_6c_s^2w_{13}^2w_{14}w_8w_9w_{12} + 2w_6^2v_1^2w_{13}^2w_7w_8w_5w_9^2w_{12} - 12c_s^2w_{13}^2w_7w_{14}w_8w_5w_9^2w_{12} - 2w_6^2v_1^2w_{13}^2w_{14}w_8w_5w_9w_{12} - 12w_6^2c_s^2w_7w_{14}w_8w_5w_9^2w_{12} - \\ & 6w_6^2c_s^2w_{13}w_7w_8w_5w_9^2w_{12} + 12w_6c_s^2w_{13}w_7w_{14}w_8w_5w_9^2 - 4w_6w_{13}w_7w_8w_5w_9^2w_{12} + 12c_s^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} + 4w_6^2v_1^2w_{13}^2w_{14}w_8w_9w_{12} - \\ & 4w_6v_1^2w_{13}^2w_{14}w_8w_5w_9^2w_{12} + 12w_6^2c_s^2w_{13}^2w_7w_{14}w_8w_9^2 - 2w_6^2w_{13}^2w_{14}w_8w_5w_9^2w_{12} + 12w_6c_s^2w_{13}^2w_7w_8w_5w_9^2w_{12} + 6w_6^2c_s^2w_{13}^2w_7w_8w_5w_9^2w_{12} - \\ & 4w_6^2v_1^2w_{13}^2w_{14}w_8w_9^2 + 12w_6c_s^2w_{13}^2w_7w_{14}w_8w_5w_{12} - 3w_6^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} + 2w_6^2v_1^2w_{13}^2w_{14}w_8w_5w_9^2 + 4w_6w_{13}^2w_7w_8w_5w_9^2w_{12} + \\ & 12w_6c_s^2w_{13}^2w_7w_{14}w_8w_9w_{12} + 4w_6^2w_{13}^2w_7w_{14}w_5w_9w_{12} - 8w_6v_1^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} - 12w_6c_s^2w_{13}^2w_7w_{14}w_8w_5w_9 - 2w_6^2v_1^2w_{13}^2w_7w_{14}w_8w_5w_9^2w_{12} + \\ & 12w_6^2c_s^2w_{13}^2w_7w_{14}w_5w_9w_{12} + 4w_6^2w_{13}^2w_7w_{14}w_5w_9w_{12} + 12w_6^2c_s^2w_{13}^2w_7w_{14}w_8w_5w_{12} + 6w_6^2c_s^2w_{13}^2w_{14}w_8w_5w_9^2 + 4w_6^2w_{13}^2w_7w_7w_5w_9^2w_{12} - \\ & 12w_6c_s^2w_{13}w_{14}w_8w_5w_9^2w_{12} + 2w_6^2w_{13}^2w_7w_{14}w_8w_5w_9^2w_{12} + 4w_6v_1^2w_{13}^2w_7w_5w_9^2w_{12} - 4w_6w_{13}^2w_{14}w_8w_5w_9w_{12} + 4w_6v_1^2w_{13}^2w_7w_{14}w_8w_5w_9^2 + \\ & 3w_6^2v_1^2w_{13}^2w_7w_{14}w_8w_5w_9w_{12} + 8w_6v_1^2w_{13}w_7w_{14}w_8w_5w_9^2w_{12} - 2w_6^2w_7w_{14}w_8w_5w_9^2w_{12} - 4w_6v_1^2w_7w_{14}w_8w_5w_9^2w_{12} - 2w_6^2v_1^2w_{13}w_7w_8w_5w_9^2w_{12} + \\ & 2w_6^2w_{13}w_8w_5w_9^2w_{12} + 3w_6^2w_{13}^2w_7w_{14}w_8w_5w_9^2 - 6w_6^2c_s^2w_{13}^2w_{14}w_8w_5w_9w_{12}) \frac{v_3 v_2 v_1}{4w_6^2w_{13}^2w_7w_{14}w_8w_5w_9^2w_{12}} \end{aligned}$$

$$C_{D_x^3 D_y \rho}^{(3), \text{MRT2}} = C_{D_x^3 D_y \rho}^{(3), \text{MRT1}}$$

$$C_{D_x^3 D_y \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^3 D_y \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x^3 D_y \rho}^{(3), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_3 v_2 v_1}{12 \omega_1 \omega_2}$$

coefficient $C_{D_x^3 D_y v_1}^{(3)}$ at $\frac{\partial^4 v_1}{\partial x_1^3 \partial x_2}$:

$$C_{D_x^3 D_y v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x^3 D_y v_1}^{(3), \text{MRT}^1} = (-4\omega_6^2 c_s^2 \omega_{13}^2 \omega_{14} \omega_5 \omega_9 \omega_{12} - 2\omega_6^2 \omega_{13}^2 \omega_{14} \omega_8 \omega_5 \omega_9^2 - 2\omega_6^2 \omega_{13}^2 \omega_7 \omega_8 \omega_5 \omega_9^2 \omega_{12} - 12\omega_6 v_1^2 \omega_{13}^2 \omega_7 \omega_8 \omega_5 \omega_9^2 \omega_{12} - 4\omega_6^2 c_s^2 \omega_{13}^2 \omega_7 \omega_5 \omega_9^2 \omega_{12} -$$

[illegible]

$$4\omega_6^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12} + 12\omega_6^2\omega_{13}^2\omega_7^2\omega_8\omega_5^2\omega_9\omega_{12} + 6\omega_6^2v_1^2\omega_{13}^2\omega_7^2\omega_8^2\omega_5^2\omega_9\omega_{12} + 24c_s^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8\omega_5^2\omega_9\omega_{12}) \frac{v_3 v_1 \rho}{12\omega_6^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2\omega_5^2\omega_9\omega_{12}}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{MRT}2} = C_{D_x^3 D_y v_2}^{(3), \text{MRT}1}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CLBM}1} = (-\omega_9\omega_{12} + 3c_s^2\omega_9\omega_{12} + v_1^2\omega_{12} - 3v_1^2\omega_9 + v_1^2\omega_9\omega_{12} - 9c_s^2\omega_9 + 3\omega_9 - \omega_{12} + 3c_s^2\omega_{12}) \frac{v_3 v_1 \rho}{12\omega_9\omega_{12}}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CLBM}2} = C_{D_x^3 D_y v_2}^{(3), \text{CLBM}1}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CuLBM}1} = (-3v_1^2\omega_4 + v_1^2\omega_9 - \omega_4\omega_9 + 3c_s^2\omega_4\omega_9 + 3\omega_4 - 9c_s^2\omega_4 + 3c_s^2\omega_9 - \omega_9 + v_1^2\omega_4\omega_9) \frac{v_3 v_1 \rho}{12\omega_4\omega_9}$$

$$C_{D_x^3 D_y v_2}^{(3), \text{CuLBM}2} = (-18\omega_3v_2^2\omega_4\omega_2 + 9\omega_4\omega_1\omega_2 - 27\omega_3c_s^2\omega_1\omega_2 - 27c_s^2\omega_4\omega_1\omega_2 + 12\omega_3c_s^2\omega_4\omega_1 + 6\omega_3c_s^2\omega_4\omega_2 + 18\omega_3v_2^2\omega_4\omega_1 - 9v_1^2\omega_4\omega_1\omega_2 - 6\omega_3\omega_4\omega_1\omega_2 + 2\omega_3\omega_4\omega_2 - 9\omega_3v_1^2\omega_1\omega_2 + 2\omega_3v_1^2\omega_4\omega_1 + 6\omega_3v_1^2\omega_4\omega_1\omega_2 + 18\omega_3c_s^2\omega_4\omega_1\omega_2 - 8\omega_3\omega_4\omega_1 + 4\omega_3v_1^2\omega_4\omega_2 + 9\omega_3\omega_1\omega_2) \frac{v_3 v_1 \rho}{72\omega_3\omega_4\omega_1\omega_2}$$

$$\text{coefficient } C_{D_x^3 D_y v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_1^3 \partial x_2} :$$

$$C_{D_x^3 D_y v_3}^{(3), \text{SRT}} = 0$$

$$C_{D_x^3 D_y v_3}^{(3), \text{MRT}1} = (4\omega_6^2c_s^2\omega_{13}^2\omega_7\omega_{14}\omega_8 - \omega_6^2\omega_{13}^2\omega_7\omega_{14}\omega_8^2 - \omega_6^3v_1^2\omega_{13}\omega_7^2\omega_8^2 - \omega_6^3v_1^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^2v_1^2\omega_7^2\omega_{14}\omega_8^2 - \omega_6^3\omega_{13}^2\omega_7^2\omega_8^2 - 2\omega_6^2v_1^2\omega_{13}^2\omega_7^2\omega_8^2 - 2\omega_6^2\omega_{13}^2\omega_7^2\omega_8 + 2\omega_6^3c_s^2\omega_{13}^2\omega_7\omega_8 - 6\omega_6c_s^2\omega_{13}^2\omega_7\omega_{14}\omega_8^2 - \omega_6^3\omega_7^2\omega_{14}\omega_8^2 - \omega_6^3v_1^2\omega_{13}\omega_7\omega_{14}\omega_8^2 - 4\omega_6^2c_s^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^2c_s^2\omega_7^2\omega_{14}\omega_8^2 + \omega_6^3v_1^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2 + 2\omega_6^2c_s^2\omega_{13}^2\omega_7^2\omega_{14} - 4\omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^2c_s^2\omega_{13}\omega_7^2\omega_8^2 - \omega_6^2v_1^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8 + \omega_6^3c_s^2\omega_{13}\omega_7\omega_{14}\omega_8^2 + 2\omega_6^3v_1^2\omega_{13}^2\omega_7\omega_8 + 2\omega_6^2v_1^2\omega_{13}\omega_7^2\omega_8^2 + 2\omega_6^2\omega_{13}^2\omega_7^2\omega_8^2 - \omega_6^3c_s^2\omega_{13}\omega_7\omega_8^2 + 2\omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - \omega_6^3\omega_{13}^2\omega_7^2\omega_{14}\omega_8 + 2\omega_6^3c_s^2\omega_{13}\omega_7\omega_{14} + 7\omega_6^2c_s^2\omega_{13}\omega_7\omega_{14}\omega_8^2 + 2\omega_6^2\omega_7^2\omega_{14}\omega_8^2 + 5\omega_6^3c_s^2\omega_{13}^2\omega_7\omega_{14}\omega_8 - 2\omega_6^2v_1^2\omega_{13}\omega_7\omega_{14}\omega_8^2 + 2\omega_6^3\omega_{13}\omega_7^2\omega_8 - 8c_s^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2 + \omega_6^3c_s^2\omega_{13}\omega_7^2\omega_8^2 - 2\omega_6^2c_s^2\omega_{13}^2\omega_{14}\omega_8^2 + \omega_6^3\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6c_s^2\omega_{13}\omega_7^2\omega_{14} - \omega_6^3c_s^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 + 2\omega_6^2c_s^2\omega_{13}\omega_7^2\omega_8^2 + \omega_6^3c_s^2\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6^3\omega_{13}\omega_7\omega_8 + 2\omega_6^2\omega_{13}\omega_7\omega_{14}\omega_8^2 + 6\omega_6c_s^2\omega_{13}\omega_7^2\omega_{14}\omega_8 + \omega_6^3\omega_{13}\omega_7\omega_{14}\omega_8 - 2\omega_6^2\omega_{13}\omega_7^2\omega_8^2 + 4\omega_6^2v_1^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 7\omega_6^3c_s^2\omega_{13}\omega_7\omega_{14}\omega_8 - 2\omega_6^3v_1^2\omega_{13}^2\omega_7^2\omega_8 + \omega_6^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8 - 5\omega_6^2c_s^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 + \omega_6^3\omega_{13}\omega_7^2\omega_8^2 + \omega_6^3v_1^2\omega_{13}\omega_7^2\omega_8^2 + \omega_6^3v_1^2\omega_{13}\omega_7\omega_{14}\omega_8^2 - 11\omega_6^2c_s^2\omega_{13}\omega_7^2\omega_{14}\omega_8 + \omega_6^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 - 2\omega_6v_1^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 + 13\omega_6c_s^2\omega_{13}\omega_7^2\omega_{14}\omega_8^2 + \omega_6^3v_1^2\omega_7^2\omega_{14}\omega_8^2 + 2\omega_6^2v_1^2\omega_{13}\omega_7^2\omega_8^2 + \omega_6^2v_1^2\omega_{13}\omega_7\omega_{14}\omega_8^2 - 2\omega_6^2c_s^2\omega_{13}\omega_7\omega_{14}\omega_8^2 + \omega_6^3\omega_{13}\omega_7\omega_8^2 + \omega_6^3v_1^2\omega_{13}\omega_7^2\omega_{14}\omega_8 - 2\omega_6^3c_s^2\omega_{13}\omega_7^2\omega_8 - \omega_6\omega_{13}\omega_7^2\omega_{14}\omega_8^2) \frac{v_2 v_1 \rho}{2\omega_6^2\omega_{13}^2\omega_7^2\omega_{14}\omega_8^2}$$

$$C_{D_x^3 D_y v_3}^{(3), \text{MRT}2} = C_{D_x^3 D_y v_3}^{(3), \text{MRT}1}$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CLBM}1} = 0$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CLBM}2} = 0$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CuLBM}1} = 0$$

$$C_{D_x^3 D_y v_3}^{(3), \text{CuLBM}2} = (2\omega_3\omega_4^2\omega_1 + 18\omega_3c_s^2\omega_4^2 + 3v_1^2\omega_4^2\omega_1 - 2\omega_3^2\omega_4\omega_1 + 6\omega_3v_2^2\omega_4^2 - 18\omega_3c_s^2\omega_4\omega_1 - 6\omega_3^2\omega_1^2 + 12\omega_4^2 + 3\omega_3^2v_1^2\omega_1 - 6v_1^2\omega_4^2 + 36\omega_3c_s^2\omega_4 + 6\omega_3^2\omega_4 - 2\omega_3v_2^2\omega_4^2\omega_1 - 6v_2^2\omega_4^2 - 6\omega_3v_1^2\omega_4\omega_1 - 6\omega_3^2v_2^2\omega_4 - 12\omega_3\omega_4 + 12\omega_3v_1^2\omega_4 - 3\omega_3^2v_2^2\omega_1 + 18c_s^2\omega_4^2\omega_1 + 6\omega_3^2c_s^2\omega_4\omega_1 + 6\omega_3^2v_2^2 - 36c_s^2\omega_4^2 - 18\omega_3^2c_s^2\omega_4 - 6\omega_4^2\omega_1 - 6\omega_3c_s^2\omega_4^2\omega_1 + 6\omega_3\omega_4\omega_1 - 6\omega_3\omega_4^2 + 3v_2^2\omega_4^2\omega_1 + 2\omega_3^2v_2^2\omega_4\omega_1) \frac{v_2 v_1 \rho}{8\omega_3^2\omega_4^2\omega_1}$$

$$\text{coefficient } C_{D_x^2 D_y^2 \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^2 \partial x_2^2} :$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{SRT}} = (-2 + \omega) \frac{v_3 c_s^4}{6\omega}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{MRT}1} = (-12\omega_6^2\omega_7^2\omega_5^2 - 24\omega_6\omega_7^2\omega_8\omega_5^2 - 12\omega_7^2\omega_8^2\omega_5 - 14\omega_6^2\omega_7^2\omega_8^2\omega_5 + 12\omega_6^2\omega_8\omega_5^2 + 12\omega_6^2\omega_7^2\omega_8^2 + \omega_6^2\omega_7^2\omega_8^2\omega_5^2 - 24\omega_6^2\omega_7\omega_8\omega_5^2 + 24\omega_6\omega_7^2\omega_8^2\omega_5 + 12\omega_7^2\omega_8\omega_5^2 - 12\omega_6^2\omega_8^2\omega_5 + 12\omega_6^2\omega_7^2\omega_8\omega_5^2 + 12\omega_6\omega_7^2\omega_5^2 - 12\omega_6^2\omega_7\omega_8^2 - 12\omega_6\omega_7^2\omega_8^2 + 24\omega_6^2\omega_7\omega_8^2\omega_5 + 12\omega_6^2\omega_7\omega_8^2) \frac{v_3 c_s^4}{6\omega_6^2\omega_7^2\omega_8^2\omega_5^2}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{MRT}2} = C_{D_x^2 D_y^2 \rho}^{(3), \text{MRT}1}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CLBM}1} = (-2 + \omega_5) \frac{v_3 c_s^4}{6\omega_5}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CLBM}2} = C_{D_x^2 D_y^2 \rho}^{(3), \text{CLBM}1}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CuLBM1}} = (-2 + \omega_1) \frac{v_3 c_s^4}{6\omega_1}$$

$$C_{D_x^2 D_y^2 \rho}^{(3), \text{CuLBM2}} = (3v_1^2 \omega_1 - 3v_1^2 \omega_2 + 6c_s^2 \omega_1 \omega_2 - 2\omega_1 - 14c_s^2 \omega_2 - 3v_2^2 \omega_2 + 2\omega_2 + 3v_2^2 \omega_1 + 2c_s^2 \omega_1) \frac{v_3 c_s^2}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y^2 v_1}^{(3)}$ **at** $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{SRT}} = 0$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_1}^{(3), \text{MRT1}} = & (-2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} - 4\omega_6 \omega_7^2 \omega_8^2 \omega_5^2 \omega_9 \omega_{12} + 2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12} - 4\omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} + \\ & 2\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12} - 4\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 + 4\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12} + 4\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 + 4\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 - 4\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 - 4\omega_6^2 \omega_{13} \omega_7 \omega_8 \omega_5^2 \omega_9 \omega_{12} + \\ & 2\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12} + 2\omega_6 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} + 4\omega_{13} \omega_7^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} + 6\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} - 2\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12} + \\ & 2\omega_6^2 \omega_7^2 \omega_8^2 \omega_5^2 \omega_9 \omega_{12} + 4\omega_6^2 \omega_{13} \omega_7^2 \omega_8 \omega_5^2 \omega_9 \omega_{12} - 2\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_5^2 \omega_9 \omega_{12} + 2\omega_6^2 \omega_{13} \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} + 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} - \\ & 2\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 + 2\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} - 4\omega_6 \omega_{13} \omega_7^2 \omega_8 \omega_5^2 \omega_9 \omega_{12} + 2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_5^2 \omega_9 \omega_{12} - 4\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8 \omega_5^2 \omega_9 \omega_{12} - \\ & 2\omega_6^2 \omega_{13} \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} - 4\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12} - 2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 + 2\omega_6^2 \omega_{13} \omega_7 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12} - 4\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_{12} + \\ & 4\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 - 2\omega_6^2 \omega_{13} \omega_7^2 \omega_8^2 \omega_5^2 \omega_9 \omega_{12} - 2\omega_6^2 \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} - 3\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5 \omega_9 \omega_{12} + 3\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 + \\ & 4\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 + 2\omega_6 \omega_{13} \omega_7^2 \omega_{14} \omega_8 \omega_5 \omega_9 \omega_{12}) \frac{v_3 c_s^2 v_1 \rho}{2\omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8^2 \omega_5^2 \omega_9 \omega_{12}} \end{aligned}$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{MRT2}} = C_{D_x^2 D_y^2 v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_1}^{(3), \text{CuLBM2}} = (v_1^2 \omega_1 - v_1^2 \omega_2 - \omega_1 - 3c_s^2 \omega_2 + \omega_2 + 3c_s^2 \omega_1) \frac{v_3 v_1 \rho}{36\omega_1 \omega_2}$$

coefficient $C_{D_x^2 D_y^2 v_2}^{(3)}$ **at** $\frac{\partial^4 v_2}{\partial x_1^2 \partial x_2^2}$:

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{SRT}} = 0$$

$$\begin{aligned} C_{D_x^2 D_y^2 v_2}^{(3), \text{MRT1}} = & (-4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_8 \omega_5^2 \omega_{15} - 2\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_8^2 \omega_{15} + 2\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_{15} + 4\omega_6^2 \omega_{16} \omega_7 \omega_{17} \omega_8^2 \omega_5^2 + \\ & 2\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5 \omega_{15} - 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_{15} + 3\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 + 2\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5^2 \omega_{15} - 4\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_8 \omega_5^2 \omega_{15} - \\ & 4\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 - 4\omega_6^2 \omega_{16} \omega_7 \omega_{17} \omega_8^2 \omega_5 \omega_{15} + 6\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5 \omega_{15} - 3\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15} - 4\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_{15} - \\ & 4\omega_6^2 \omega_{10} \omega_7 \omega_8^2 \omega_5^2 \omega_{15} - 6\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15} + 2\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_{15} + 2\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 + \\ & 4\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_8^2 \omega_5^2 \omega_{15} - 2\omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15} + 2\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8 \omega_5 \omega_{15} + 4\omega_6^2 \omega_{16} \omega_{10} \omega_{17} \omega_8 \omega_5^2 \omega_{15} + 4\omega_6^2 \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5 \omega_{15} - \\ & 4\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5^2 - 2\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5 \omega_{15} - 2\omega_6^2 \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15} - 2\omega_6^2 \omega_{16} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 - 4\omega_6^2 \omega_{16} \omega_{10} \omega_{17} \omega_8^2 \omega_5 \omega_{15} - \\ & 2\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15} + 2\omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5^2 \omega_{15} - 2\omega_6 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5 \omega_{15} + 4\omega_6^2 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8^2 \omega_5 - 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8 \omega_5^2 \omega_{15} + \\ & 4\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_8 \omega_5^2 \omega_{15} + 2\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_8^2 \omega_5^2 \omega_{15} + 2\omega_6 \omega_{16} \omega_{10} \omega_7 \omega_{17} \omega_8 \omega_5^2 \omega_{15} - 2\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 + 4\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_{15} + \\ & 2\omega_6^2 \omega_{10} \omega_7^2 \omega_8^2 \omega_5^2 \omega_{15} + 4\omega_6 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5 \omega_{15}) \frac{v_3 c_s^2 v_2 \rho}{2\omega_6^2 \omega_{16} \omega_{10} \omega_7^2 \omega_{17} \omega_8^2 \omega_5^2 \omega_{15}} \end{aligned}$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{MRT2}} = C_{D_x^2 D_y^2 v_2}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_x^2 D_y^2 v_2}^{(3), \text{CuLBM2}} = (-\omega_1 - 3c_s^2 \omega_2 - v_2^2 \omega_2 + \omega_2 + v_2^2 \omega_1 + 3c_s^2 \omega_1) \frac{v_3 v_2 \rho}{36\omega_1 \omega_2}$$

[illegible]

$$C_{\text{D}_2^+ \text{D}_2^+ \text{v}_3}^{(3), \text{CLB M1}} = (-2\omega_6 \omega_{16} \omega_7^2 \omega_{17} \omega_8 + 2\omega_6 \omega_{16} \omega_7 \omega_{17} \omega_{14} \omega_8 - 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{17} + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{14} \omega_8 + \omega_6^2 \omega_{13} \omega_7^2 \omega_{14} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} - \omega_6 \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 + \omega_6^2 \omega_{16} \omega_7^2 \omega_{17} \omega_8 + \omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 - \omega_6^2 \omega_{16} \omega_7 \omega_{17} \omega_{14} \omega_8 + 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} + 2\omega_6 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 - \omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_8 + \omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} \omega_8 + 2\omega_6 \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 - 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} - \omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} \omega_8 - \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} - 2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} - 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{14} - \omega_6^2 \omega_{16} \omega_{13} \omega_{17} \omega_{14} \omega_8 - 6\omega_6 \omega_{16} \omega_{13} \omega_7 \omega_{17} \omega_{14} \omega_8 + 2\omega_6 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_8 + 2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17}) \frac{c_s^4 \rho}{2\omega_6^2 \omega_{16} \omega_{13} \omega_7^2 \omega_{17} \omega_{14} \omega_8}$$

$$\begin{aligned} C_D^{(3), \text{CuLBM1}} \mathcal{D}_x^2 \mathcal{D}_y^2 v_3 &= (-\omega_2^2 + 2\omega_3^2\omega_2 - \omega_3\omega_{13}\omega_2 - \omega_3^2\omega_2^2 + \omega_{13}\omega_2 + 2\omega_3\omega_2^2 - \omega_3^3 - 2\omega_3\omega_2 + \omega_3\omega_{13}) \frac{c_s^4 \rho}{\omega_3^2 \omega_{13} \omega_2^2} \\ C_D^{(3), \text{CuLBM2}} \mathcal{D}_x^2 \mathcal{D}_y^2 v_3 &= (-3\omega_3^2 v_2^2 \omega_4 \omega_1^3 \omega_5 - 6\omega_3^2 v_1^2 \omega_1^2 \omega_5 + 8\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_5 - 18 c_s^2 v_2^2 \omega_4^2 \omega_1^2 \omega_5 + 12\omega_3 c_s^2 v_2^2 \omega_4^2 \omega_1 \omega_5 + 18\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_5 - 3v_2^2 \omega_4^2 \omega_1^3 \omega_5 + \\ & 6\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_5 - 32\omega_3^2 c_s^4 \omega_4^2 \omega_1 + 3\omega_3 v_2^2 \omega_4^2 \omega_1^3 \omega_5 + 6\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^3 \omega_5 + 8\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_5 - 3\omega_3^2 v_1^4 \omega_1^3 \omega_5 - 2\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_5 + 6\omega_3 v_2^4 \omega_1^2 \omega_5 - \\ & 6v_1^4 \omega_1^2 \omega_5 - 6\omega_3^2 v_1^4 \omega_4 \omega_1^2 \omega_5 - 12\omega_3^2 c_s^2 v_1^4 \omega_4 \omega_1 \omega_5 + 6\omega_3^2 v_1^4 \omega_1^2 \omega_5 - 6\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^2 \omega_5 - 6\omega_3 v_2^2 \omega_4^2 \omega_1^2 \omega_5 - 8\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 - 9\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_5 - \\ & 6\omega_3 c_s^2 v_1^2 \omega_2^2 \omega_1^3 \omega_5 + 6v_2^2 \omega_4^2 \omega_1^2 \omega_5 - 2\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_5 + 3\omega_3^2 v_2^2 \omega_1^3 \omega_5 + 6\omega_3^2 v_2^2 \omega_4 \omega_1^2 \omega_5 - 8\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_5 + 9c_s^2 v_2^2 \omega_4^2 \omega_1^3 \omega_5 + 3\omega_3^2 v_1^4 \omega_4 \omega_1^3 \omega_5 + \\ & 3v_1^4 \omega_1^2 \omega_5 + 8\omega_3 c_s^4 \omega_4^2 \omega_1 \omega_5 - 3\omega_3 v_2^2 \omega_4^2 \omega_1^2 \omega_5 + 8\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_5 + 32\omega_2^2 c_s^4 \omega_1^2 \omega_5 + 3v_2^4 \omega_4^2 \omega_1^3 \omega_5 - 8\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_5 + 3\omega_3^2 v_2^4 \omega_4 \omega_1^3 \omega_5 - \\ & 8\omega_3^2 c_s^4 \omega_4 \omega_1 \omega_5 + 16\omega_3^2 c_s^4 \omega_2^2 \omega_5 - 3\omega_3 v_1^2 \omega_1^2 \omega_5 - 6\omega_3 v_2^2 \omega_4^2 \omega_1^2 \omega_5 - 6\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1^2 \omega_5 - 9\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_5 + 2\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_5 + 3\omega_3^2 v_2^2 \omega_1^3 \omega_5 - \\ & 12\omega_3^2 c_s^2 v_2^2 \omega_4 \omega_1 \omega_5 + 9c_s^2 v_2^2 \omega_4^2 \omega_1^3 \omega_5 + 6\omega_3^2 v_2^2 \omega_1^2 \omega_5 + 6\omega_3^2 v_2^2 \omega_4 \omega_1^2 \omega_5 - 6\omega_3 c_s^2 v_2^2 \omega_4^2 \omega_1^3 \omega_5 + 6v_2^2 \omega_4^2 \omega_1^2 \omega_5 + 6\omega_3 v_2^2 \omega_4^2 \omega_1 \omega_5 - 6\omega_3^2 v_2^2 \omega_4 \omega_1^2 \omega_5 + \\ & 2\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_5 - 6v_2^4 \omega_1^2 \omega_5 - 3v_1^2 \omega_1^2 \omega_5 + 6\omega_3 c_s^2 v_2^2 \omega_1^2 \omega_5 - 8\omega_3 c_s^2 \omega_4^2 \omega_1 \omega_5 - 3\omega_3^2 v_2^2 \omega_1^3 \omega_5 + 12\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_5 - 18c_s^2 v_1^2 \omega_4^2 \omega_1^2 \omega_5 - \\ & 3\omega_3^2 v_1^2 \omega_4 \omega_1^3 \omega_5 - 6\omega_3^2 v_2^2 \omega_1^2 \omega_5 - 8\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_5 + 18\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_5 + 6\omega_3^2 c_s^2 v_1^2 \omega_4 \omega_1^3 \omega_5 + 3\omega_3 v_2^2 \omega_4^2 \omega_1^3 \omega_5) \frac{\rho}{8\omega_2^2 \omega_3^2 \omega_5} \end{aligned}$$

$$C_{\text{D}_x \text{D}_y^3 \rho}^{(3), \text{SRT}} = 0$$

$$C_{\text{D}_x \text{D}_y^3 \rho}^{(3), \text{MRT}^1} = (-2\omega_6\omega_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5 - 12\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 + 4\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5 - 12c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_5\omega_15 - 4\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_5\omega_{15} + 2\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} + 4\omega_{16}\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 4\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} - 4\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 4\omega_6\omega_{16}^2\omega_{10}^2\omega_7\omega_5\omega_{15} - 6c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6\omega_{16}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 12\omega_6c_s^2\omega_{16}\omega_{16}^2\omega_{10}^2\omega_{17}\omega_8\omega_5\omega_{15} - 12\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 12c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_5\omega_{15} - 4\omega_6\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15} - 4\omega_6\omega_{16}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 12c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 - 4\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_5\omega_{15} + 3\omega_6\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5 - 4\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 - 12\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8 + 4\omega_6\omega_{16}^2\omega_{10}\omega_7\omega_8\omega_5\omega_{15} + 6\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} - 2\omega_{16}\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 12c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8 + 4\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_5\omega_{15} + 4\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 12c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} + 12\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_{17}\omega_8\omega_5\omega_{15} - 2\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 6c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} +$$

$$C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{MRT}^2} = C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{MRT}^1}$$

$$C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{CLBM}^1} = (3\omega_{10} - 9c_s^2\omega_{10} - 3v_2^2\omega_{10} + v_2^2\omega_{10}\omega_{15} + 3c_s^2\omega_{15} - \omega_{15} - \omega_{10}\omega_{15} + 3c_s^2\omega_{10}\omega_{15} + v_2^2\omega_{15}) \frac{v_3 v_2 \rho}{12\omega_{10}\omega_{15}}$$

$$C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{CLBM}^2} = C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{CLBM}^1}$$

$$C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{CuLBM}^1} = (-\omega_7\omega_5 + 3c_s^2\omega_7\omega_5 - 3v_2^2\omega_5 + v_2^2\omega_7\omega_5 - \omega_7 - 9c_s^2\omega_5 + v_2^2\omega_7 + 3c_s^2\omega_7 + 3\omega_5) \frac{v_3 v_2 \rho}{12\omega_7\omega_5}$$

$$C_{\text{D}_x \text{D}_y^3 v_1}^{(3), \text{CuLBM}^2} = (4\omega_3 v_2^2 \omega_4 \omega_2 + 9\omega_4 \omega_1 \omega_2 - 27\omega_3 c_s^2 \omega_1 \omega_2 - 27c_s^2 \omega_4 \omega_1 \omega_2 + 12\omega_3 c_s^2 \omega_4 \omega_1 + 6\omega_3 c_s^2 \omega_4 \omega_2 + 2\omega_3 v_2^2 \omega_4 \omega_1 + 6\omega_3 v_2^2 \omega_4 \omega_1 \omega_2 - 9\omega_3 v_2^2 \omega_1 \omega_2 - 6\omega_3 \omega_4 \omega_1 \omega_2 - 9v_2^2 \omega_4 \omega_1 \omega_2 + 2\omega_3 \omega_4 \omega_2 + 18\omega_3 v_1^2 \omega_4 \omega_1 + 18\omega_3 c_s^2 \omega_4 \omega_1 \omega_2 - 8\omega_3 \omega_4 \omega_1 - 18\omega_3 v_1^2 \omega_4 \omega_2 + 9\omega_3 \omega_1 \omega_2) \frac{v_3 v_2 \rho}{72\omega_3 \omega_4 \omega_1 \omega_2}$$

$$\text{coefficient } C_{\text{D}_x \text{D}_y^3 v_2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x_1 \partial x_2^3} :$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{SRT}} = 0$$

$$\begin{aligned} C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{MRT}^1} = & (-2\omega_6\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 - 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 + 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 - 4c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_5\omega_{15} - \\ & 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_5\omega_{15} + 6\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_8\omega_5\omega_{15} + 4\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 4\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_{16}^2\omega_{10}\omega_7^2\omega_8\omega_5\omega_{15} - \\ & 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} - 4\omega_6\omega_{16}^2\omega_{10}^2\omega_7\omega_5\omega_{15} - 2c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6\omega_{16}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 4\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_{17}\omega_8\omega_5\omega_{15} - \\ & 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} + 4c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_5\omega_{15} - 4\omega_6\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15} - 4\omega_6\omega_{16}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 4c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + \\ & 4\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_{15} - 12\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_5\omega_{15} + 3\omega_6\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_{15} - 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15} - 4\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7\omega_{17}\omega_8 + \\ & 4\omega_6\omega_{16}^2\omega_{10}^2\omega_7\omega_8\omega_5\omega_{15} + 2\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_8\omega_5\omega_{15} - 2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 4c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8 + 4\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_5\omega_{15} + \\ & 12\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 4c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} + 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_{17}\omega_8\omega_5\omega_{15} - 6\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 2c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} + \\ & 8\omega_6c_s^2\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 12\omega_6v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6\omega_{16}\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_6c_s^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7\omega_5\omega_{15} + \\ & 24\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 8\omega_6\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 4\omega_6c_s^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 6\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} + 6\omega_6v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + \\ & 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_5\omega_{15} + 12\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8 + 4\omega_6\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_5\omega_{15} + 4\omega_6\omega_{16}^2\omega_{10}^2\omega_7\omega_{17}\omega_8 - 6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + \\ & 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_{17}\omega_8\omega_5\omega_{15} + 12\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} - 4\omega_{16}^2\omega_{10}^2\omega_7^2\omega_5\omega_{15} - 2\omega_6c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} + 6\omega_{16}v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - \\ & 12\omega_6\omega_{16}v_2^2\omega_{10}^2\omega_{17}\omega_8\omega_5\omega_{15} - 4c_s^2\omega_{16}\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6\omega_{16}\omega_{10}^2\omega_{17}\omega_8\omega_5\omega_{15} + 12\omega_6\omega_{16}^2v_2^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5 + \\ & 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15} - 24\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 2\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 12\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7\omega_8\omega_5\omega_{15} - 4\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_5\omega_{15} + \\ & 4\omega_6\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 + 2\omega_6c_s^2\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5 - 9\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5 - 2\omega_6\omega_{16}^2\omega_{10}^2\omega_7^2\omega_8\omega_5\omega_{15} - 4\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - \\ & 12\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8 - 4\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7\omega_8\omega_5\omega_{15} + 9\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 3\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5 - 4\omega_6\omega_{16}^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5 + \\ & 6\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_5 + 4\omega_6c_s^2\omega_{16}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - 6\omega_6\omega_{16}^2v_2^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 2c_s^2\omega_{16}\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 12\omega_{16}v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15} - \\ & 4\omega_6\omega_{16}^2v_2^2\omega_{10}^2\omega_7\omega_{17}\omega_8 + 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_8\omega_{15} + 12\omega_{16}^2v_2^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} + 4\omega_6\omega_{16}\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_{15} + 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_5\omega_{15} - \\ & 12\omega_6\omega_{16}^2v_2^2\omega_{10}\omega_7\omega_{17}\omega_8 + 4\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8 + 4\omega_6c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8 - 4\omega_6c_s^2\omega_{16}^2\omega_{10}\omega_7\omega_{17}\omega_5\omega_{15} + 6\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5 - \\ & 4\omega_6\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_5\omega_{15} - 3\omega_6\omega_{16}^2\omega_{10}\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15} - 8\omega_6c_s^2\omega_{16}\omega_{10}\omega_7\omega_{17}\omega_8\omega_5\omega_{15} + 4\omega_6\omega_{10}^2\omega_7\omega_{17}\omega_8\omega_5\omega_{15}) \frac{v_3 v_1 \rho}{4\omega_6\omega_{16}^2\omega_{10}^2\omega_7^2\omega_{17}\omega_8\omega_5\omega_{15}} \end{aligned}$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{MRT}^2} = C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{MRT}^1}$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{CLBM}^1} = 0$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{CLBM}^2} = 0$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{CuLBM}^1} = 0$$

$$C_{\text{D}_x \text{D}_y^3 v_2}^{(3), \text{CuLBM}^2} = (v_1^2\omega_1 - v_1^2\omega_2 - \omega_1 - 3c_s^2\omega_2 + \omega_2 + 3c_s^2\omega_1) \frac{v_3 v_1 \rho}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{\text{D}_x \text{D}_y^3 v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_1 \partial x_2^3} :$$

$$C_{\text{D}_x \text{D}_y^3 v_3}^{(3), \text{SRT}} = 0$$

$$\begin{aligned} C_{\text{D}_x \text{D}_y^3 v_3}^{(3), \text{MRT}^1} = & (-6\omega_6c_s^2\omega_{16}\omega_7\omega_{17}\omega_8^2 - 2\omega_6^2\omega_{16}\omega_7^2\omega_8^2 + \omega_6\omega_{16}^2v_2^2\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6^2c_s^2\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6\omega_{16}^2v_2^2\omega_7^3\omega_8 - 7\omega_6c_s^2\omega_{16}^2\omega_7^3\omega_{17}\omega_8 + \\ & \omega_6\omega_{16}^2\omega_7^3\omega_8^2 + \omega_6^2v_2^2\omega_7^3\omega_{17}\omega_8^2 - 2\omega_6^2\omega_{16}^2v_2^2\omega_7^2\omega_8^2 - \omega_6^2\omega_{16}\omega_7\omega_{17}\omega_8^2 + 6\omega_6^2c_s^2\omega_{16}\omega_7\omega_{17}\omega_8 - \omega_6^2\omega_{16}^2v_2^2\omega_7^2\omega_{17}\omega_8 - \omega_6^2\omega_{16}^2\omega_7^3\omega_{17}\omega_8 + \omega_6\omega_{16}^2\omega_7^3\omega_{17}\omega_8 + \\ & 4\omega_6^2c_s\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - 2\omega_6\omega_{16}v_2^2\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6^2\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6^2c_s^2\omega_{16}\omega_7^2\omega_8^2 - 2\omega_6^2\omega_{16}^2v_2^2\omega_7^2\omega_8 - 4\omega_6^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}^2v_2^2\omega_7^3\omega_8^2 + \end{aligned}$$

$$\begin{aligned}
& 2c_s^2\omega_{16}\omega_7^3\omega_{17}\omega_8 - 2\omega_6c_s^2\omega_{16}\omega_7^2\omega_{17}\omega_8^2 + 4\omega_6^2\omega_{16}v_2^2\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}\omega_7^3\omega_8^2 + 2\omega_6^2\omega_{16}v_2^2\omega_7^2\omega_8 - \omega_6^2c_s^2\omega_{16}\omega_7^3\omega_8^2 - \omega_6^2\omega_{16}v_2^2\omega_7^2\omega_{17}\omega_8^2 + \\
& 13\omega_6^2c_s^2\omega_{16}^2\omega_7\omega_{17}\omega_8^2 - 8\omega_6^2c_s^2\omega_{16}^2\omega_{17}\omega_8^2 + 5\omega_6^2c_s^2\omega_{16}^2\omega_7^3\omega_{17}\omega_8 + 2\omega_6\omega_{16}\omega_7^2\omega_{17}\omega_8^2 - \omega_6\omega_{16}^2v_2^2\omega_7^3\omega_8^2 - 2\omega_6\omega_{16}^2v_2^2\omega_7^3\omega_8 - 2\omega_6^2c_s^2\omega_{16}^2\omega_7^3\omega_{17} + \\
& \omega_6\omega_{16}v_2^2\omega_7^3\omega_{17}\omega_8^2 + 2\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_8 - \omega_6^2c_s^2\omega_{16}^2\omega_7^3\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}v_2^2\omega_7^2\omega_8^2 + 2\omega_6^2\omega_{16}\omega_7\omega_{17}\omega_8^2 - \omega_6^2\omega_7^3\omega_{17}\omega_8^2 - 2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - \omega_6^2\omega_{16}^2\omega_7^3\omega_8^2 - \\
& 2\omega_6^2\omega_{16}v_2^2\omega_7\omega_{17}\omega_8^2 - \omega_6c_s^2\omega_{16}^2\omega_7^3\omega_8^2 + \omega_6^2\omega_{16}^2v_2^2\omega_7^3\omega_{17}\omega_8 - 2\omega_6^2v_2^2\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}^2v_2^2\omega_7\omega_{17}\omega_8^2 - 5\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + \omega_6^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8 + \\
& \omega_6^2c_s^2\omega_{16}^2\omega_7^3\omega_8^2 + 2\omega_6c_s^2\omega_{16}^2\omega_7^3\omega_{17} + \omega_6^2c_s^2\omega_{16}^2\omega_7^3\omega_{17}\omega_8^2 - 2\omega_6^2\omega_{16}^2\omega_7^2\omega_8 + 4\omega_6c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8 - \omega_6\omega_{16}^2v_2^2\omega_7^3\omega_{17}\omega_8 - \omega_6\omega_{16}\omega_7^3\omega_{17}\omega_8^2 + 7\omega_6c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + \\
& 2\omega_6^2\omega_{16}^2\omega_7^2\omega_8^2 - \omega_6^2\omega_{16}v_2^2\omega_7^3\omega_8^2 + \omega_6^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 - 11\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17}\omega_8 - 2\omega_6^2c_s^2\omega_{16}^2\omega_7^3\omega_8 + 2\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_{17} - \omega_6^2\omega_{16}v_2^2\omega_7^3\omega_{17}\omega_8^2 + \\
& \omega_6c_s^2\omega_{16}\omega_7^3\omega_{17}\omega_8^2 + 2\omega_6^2\omega_{16}^2\omega_7^3\omega_8 - \omega_6\omega_{16}^2\omega_7^2\omega_{17}\omega_8^2 + 2\omega_6c_s^2\omega_{16}^2\omega_7^3\omega_8 - 2\omega_6^2c_s^2\omega_{16}^2\omega_7^2\omega_8^2 + \omega_6^2\omega_{16}\omega_7^3\omega_{17}\omega_8^2 - 2\omega_6^2c_s^2\omega_{16}\omega_7\omega_{17}\omega_8^2) \frac{v_2v_1\rho}{2\omega_6^2\omega_{16}^2\omega_7^3\omega_{17}\omega_8^2}
\end{aligned}$$

$$C_{D_x D_y^3 v_3}^{(3), \text{MRT}^2} = C_{D_x D_y^3 v_3}^{(3), \text{MRT}^1}$$

$$C_{D_x D_y^3 v_3}^{(3), \text{CLBM}^1} = 0$$

$$C_{D_x D_y^3 v_3}^{(3), \text{CLBM}^2} = 0$$

$$C_{D_x D_y^3 v_3}^{(3), \text{CuLBM}^1} = 0$$

$$\begin{aligned}
C_{D_x D_y^3 v_3}^{(3), \text{CuLBM}^2} &= (2\omega_3\omega_4^2\omega_1 + 18\omega_3c_s^2\omega_4^2 + 2\omega_3^2v_1^2\omega_4\omega_1 + 3v_1^2\omega_4^2\omega_1 - 2\omega_3^3\omega_4\omega_1 - 18\omega_3c_s^2\omega_4\omega_1 + 6\omega_3^2v_1^2 + 12\omega_4^2 - 3\omega_3^2v_1^2\omega_1 + 12\omega_3v_2^2\omega_4 - \\
& 6\omega_3v_2^2\omega_4\omega_1 - 6\omega_3^2v_1^2\omega_4 - 6v_1^2\omega_4^2 + 36\omega_3c_s^2\omega_4 - 2\omega_3v_1^2\omega_4^2\omega_1 + 6\omega_3^2\omega_4 - 6v_2^2\omega_4^2 - 12\omega_3\omega_4 + 3\omega_3^2v_2^2\omega_1 + 18c_s^2\omega_4^2\omega_1 + 6\omega_3^2c_s^2\omega_4\omega_1 - 6\omega_3^2v_2^2 - \\
& 36c_s^2\omega_4^2 - 18\omega_3^2c_s^2\omega_4 - 6\omega_4^2\omega_1 - 6\omega_3c_s^2\omega_4^2\omega_1 + 6\omega_3v_1^2\omega_4^2 + 6\omega_3\omega_4\omega_1 - 6\omega_3\omega_4^2 + 3v_2^2\omega_4^2\omega_1) \frac{v_2v_1\rho}{8\omega_3^2\omega_4^2\omega_1}
\end{aligned}$$

$$\text{coefficient } C_{D_y^4 \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x^2}:$$

$$C_{D_y^4 \rho}^{(3), \text{SRT}} = (24c_s^2v_2^2 + 6v_2^4 + 2c_s^4 - c_s^4\omega - 3v_2^4\omega + 3v_2^2\omega - 12c_s^2v_2^2\omega + c_s^2\omega - 2c_s^2 - 6v_2^2) \frac{v_3}{24\omega}$$

$$\begin{aligned}
C_{D_y^4 \rho}^{(3), \text{MRT}^1} &= \\
& (12v_2^4\omega_{10}^2\omega_7^2 + 150c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + 432c_s^2\omega_{16}v_2^2\omega_{10}\omega_7 - 12c_s^4\omega_{16}\omega_{10}^2\omega_7^2 + 36\omega_{16}^2v_2^4\omega_{10}\omega_7^2 - 12c_s^2\omega_{10}^2\omega_7^2 - 144c_s^2v_2^2\omega_{10}^2\omega_7 + 96\omega_{16}v_2^4\omega_{10}^2\omega_7 + \\
& 96\omega_{16}^2v_2^2\omega_{10}\omega_7 - 24c_s^4\omega_{10}^2\omega_7 + 30\omega_{16}v_2^2\omega_{10}^2\omega_7^2 - 36\omega_{16}^2v_2^4\omega_7^2 + 24v_2^2\omega_{10}^2\omega_7 + 24c_s^2\omega_{16}\omega_{10}^2 + 14c_s^4\omega_{16}^2\omega_{10}\omega_7^2 - 12v_2^2\omega_{10}^2\omega_7^2 - 216c_s^2\omega_{16}v_2^2\omega_{10}^2 - \\
& 48c_s^4\omega_{16}^2\omega_{10}\omega_7 + 12c_s^4\omega_{10}^2\omega_7^2 - 36\omega_{16}^2v_2^2\omega_{10}\omega_7^2 + c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 - 96\omega_{16}v_2^2\omega_{10}^2\omega_7 + 72\omega_{16}^2v_2^4\omega_7 + 24c_s^2\omega_{10}^2\omega_7 - 96\omega_{16}^2v_2^4\omega_{10}\omega_7 + 48c_s^4\omega_{16}\omega_{10}^2\omega_7 + \\
& 72c_s^2v_2^2\omega_{10}^2\omega_7^2 - 30\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 48\omega_{16}v_2^2\omega_{10}^2 - 24c_s^4\omega_{16}\omega_{10}^2 + 48\omega_{16}^2v_2^4\omega_{10} - 432c_s^2\omega_{16}^2v_2^2\omega_{10}\omega_7 - 24v_2^2\omega_{10}^2\omega_7 - 126c_s^2\omega_{16}v_2^2\omega_{10}^2\omega_7^2 + 24\omega_{16}v_2^2\omega_{10}\omega_7^2 - \\
& 24c_s^2\omega_{16}^2\omega_7 + 36\omega_{16}^2v_2^2\omega_7^2 + 12c_s^2\omega_{16}\omega_{10}^2\omega_7^2 + 72c_s^2\omega_{16}v_2^2\omega_{10}^2\omega_7^2 - 24c_s^2\omega_{16}^2\omega_{10} - 144c_s^2\omega_{16}^2v_2^2\omega_7^2 + 3\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 - 14c_s^2\omega_{16}^2\omega_{10}\omega_7^2 - 12c_s^4\omega_{16}^2\omega_7^2 + \\
& 48\omega_{16}v_2^2\omega_{10}\omega_7 + 48c_s^2\omega_{16}^2\omega_{10}\omega_7 + 24c_s^4\omega_{16}\omega_7 - 48\omega_{16}v_2^2\omega_{10}^2 - 24\omega_{16}v_2^2\omega_{10}\omega_7^2 - 48\omega_{16}^2v_2^2\omega_{10} + 288c_s^2\omega_{16}^2v_2^2\omega_7 - c_s^4\omega_{16}^2\omega_{10}^2\omega_7^2 - 12c_s^2\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 + \\
& 24c_s^4\omega_{16}^2\omega_{10} - 48c_s^2\omega_{16}\omega_{10}^2\omega_7 - 144c_s^2\omega_{16}v_2^2\omega_{10}\omega_7 - 3\omega_{16}^2v_2^4\omega_{10}^2\omega_7^2 - 48\omega_{16}v_2^4\omega_{10}\omega_7 + 216c_s^2\omega_{16}^2v_2^2\omega_{10} + 12c_s^2\omega_{16}^2\omega_7^2 - 72\omega_{16}^2v_2^2\omega_7) \frac{v_3}{24\omega_{16}^2\omega_{10}^2\omega_7^2}
\end{aligned}$$

$$C_{D_y^4 \rho}^{(3), \text{MRT}^2} = C_{D_y^4 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_y^4 \rho}^{(3), \text{CLBM}^1} = (24c_s^2v_2^2 - 3v_2^4\omega_{10} - c_s^4\omega_{10} + 6v_2^4 + 2c_s^4 + c_s^2\omega_{10} + 3v_2^2\omega_{10} - 12c_s^2v_2^2\omega_{10} - 2c_s^2 - 6v_2^2) \frac{v_3}{24\omega_{10}}$$

$$C_{D_y^4 \rho}^{(3), \text{CLBM}^2} = C_{D_y^4 \rho}^{(3), \text{CLBM}^1}$$

$$C_{D_y^4 \rho}^{(3), \text{CuLBM}^1} = (24c_s^2v_2^2 + 6v_2^4 + 2c_s^4 + 3v_2^2\omega_5 - 12c_s^2v_2^2\omega_5 + c_s^2\omega_5 - c_s^4\omega_5 - 3v_2^4\omega_5 - 2c_s^2 - 6v_2^2) \frac{v_3}{24\omega_5}$$

$$\begin{aligned}
C_{D_y^4 \rho}^{(3), \text{CuLBM}^2} &= (9v_2^2\omega_1\omega_2 - 3c_s^4\omega_1\omega_2 + 12v_2^4\omega_2 - 36c_s^2v_2^2\omega_1\omega_2 + 4c_s^4\omega_2 - 9v_2^4\omega_1\omega_2 + 2c_s^4\omega_1 + 3c_s^2\omega_1\omega_2 + 6v_2^4\omega_1 - 4c_s^2\omega_2 + 48c_s^2v_2^2\omega_2 - \\
& 12v_2^2\omega_2 + 24c_s^2v_2^2\omega_1 - 6v_2^2\omega_1 - 2c_s^2\omega_1) \frac{v_3}{72\omega_1\omega_2}
\end{aligned}$$

$$\text{coefficient } C_{D_y^4 v_2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x^2}:$$

$$C_{D_y^4 v_2}^{(3), \text{SRT}} = (-4 + 2\omega - 5v_2^2\omega - 3c_s^2\omega + 6c_s^2 + 10v_2^2) \frac{v_3v_2\rho}{12\omega^2}$$

$$\begin{aligned}
C_{D_y^4 v_2}^{(3), \text{MRT}^1} &= \\
& (-12\omega_{10}^2\omega_7^2 - 24c_s^2\omega_{16}\omega_{10}\omega_7 + 24c_s^2\omega_{10}^2\omega_7^2 + 36\omega_{16}\omega_{10}^2 - 168\omega_{16}^2v_2^2\omega_{10}\omega_7 + 24\omega_{16}\omega_{10}\omega_7 - 51\omega_{16}v_2^2\omega_{10}^2\omega_7^2 - 48v_2^2\omega_{10}^2\omega_7 - 60c_s^2\omega_{16}\omega_{10}^2 + 24v_2^2\omega_{10}^2\omega_7^2 - \\
& 12\omega_{16}\omega_{10}^2\omega_7^2 + 61\omega_{16}^2v_2^2\omega_{10}\omega_7^2 - 3c_s^2\omega_{16}^2\omega_{10}^2\omega_7^2 + 168\omega_{16}v_2^2\omega_{10}^2\omega_7 - 48c_s^2\omega_{10}^2\omega_7 - 84\omega_{16}v_2^2\omega_{10}^2 + 24\omega_{10}^2\omega_7 + 12c_s^2\omega_{16}\omega_{10}\omega_7^2 + 2\omega_{16}^2\omega_{10}^2\omega_7^2 + 72c_s^2\omega_{16}^2\omega_7 - \\
& 60\omega_{16}^2v_2^2\omega_7^2 - 25\omega_{16}^2\omega_{10}\omega_7^2 - 48\omega_{16}^2\omega_7 - 33c_s^2\omega_{16}\omega_{10}^2\omega_7^2 + 60c_s^2\omega_{16}^2\omega_{10} - 5\omega_{16}^2v_2^2\omega_{10}^2\omega_7^2 + 39c_s^2\omega_{16}^2\omega_{10}\omega_7^2 + 21\omega_{16}\omega_{10}^2\omega_7^2 - 36\omega_{16}^2\omega_{10} - 72\omega_{16}v_2^2\omega_{10}\omega_7 - \\
& 72\omega_{16}\omega_{10}^2\omega_7 - 120c_s^2\omega_{16}\omega_{10}\omega_7 + 36\omega_{16}v_2^2\omega_{10}\omega_7^2 + 84\omega_{16}^2v_2^2\omega_{10} + 120c_s^2\omega_{16}\omega_{10}^2\omega_7 + 72\omega_{16}^2\omega_{10}\omega_7 + 24\omega_{16}^2\omega_7^2 - 36c_s^2\omega_{16}^2\omega_7^2 + 120\omega_{16}^2v_2^2\omega_7) \frac{v_3v_2\rho}{12\omega_{16}^2\omega_{10}^2\omega_7^2}
\end{aligned}$$

$$C_{D_y^4 v_2}^{(3), \text{MRT}^2} = C_{D_y^4 v_2}^{(3), \text{MRT}^1}$$

$$C_{D_y^4 v_2}^{(3), \text{CLBM}^1} = (-4 + 2\omega_{10} - 3c_s^2\omega_{10} - 5v_2^2\omega_{10} + 6c_s^2 + 10v_2^2) \frac{v_3 v_2 \rho}{12\omega_{10}}$$

$$C_{D_y^4 v_2}^{(3), \text{CLBM}^2} = C_{D_y^4 v_2}^{(3), \text{CLBM}^1}$$

$$C_{D_y^4 v_2}^{(3), \text{CuLBM}^1} = (-4 - 5v_2^2\omega_5 - 3c_s^2\omega_5 + 2\omega_5 + 6c_s^2 + 10v_2^2) \frac{v_3 v_2 \rho}{12\omega_5}$$

$$C_{D_y^4 v_2}^{(3), \text{CuLBM}^2} = (-15v_2^2\omega_1\omega_2 + 6\omega_1\omega_2 - 9c_s^2\omega_1\omega_2 - 4\omega_1 + 12c_s^2\omega_2 + 20v_2^2\omega_2 - 8\omega_2 + 10v_2^2\omega_1 + 6c_s^2\omega_1) \frac{v_3 v_2 \rho}{36\omega_1\omega_2}$$

$$\text{coefficient } C_{D_y^4 v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_3^4}:$$

$$C_{D_y^4 v_3}^{(3), \text{SRT}} = (-144c_s^2v_2^2 - 3c_s^4\omega^3 - 42v_2^4\omega^2 - 72v_2^4 + 3v_2^4\omega^3 + 30c_s^4\omega^2 + 48c_s^4 - 72c_s^4\omega + 108v_2^4\omega + 6c_s^2v_2^2\omega^3 - 3v_2^2\omega^3 - 14c_s^2\omega^2 - 84c_s^2v_2^2\omega^2 + c_s^2\omega^3 + 42v_2^2\omega^2 - 108v_2^2\omega + 216c_s^2v_2^2\omega + 36c_s^2\omega - 24c_s^2 + 72v_2^2) \frac{\rho}{24\omega^3}$$

$$C_{D_y^4 v_3}^{(3), \text{MRT}^1} = (3\omega_{16}^2v_2^4\omega_7^3 + 24c_s^2\omega_{16}\omega_7^2 - 24c_s^2\omega_{16}v_2^2\omega_7 - 96c_s^2\omega_{16}^2v_2^2 + 24c_s^4\omega_{16}\omega_7 - 24\omega_{16}^2v_2^4\omega_7^2 + 48\omega_{16}v_2^2\omega_7 - 6c_s^2\omega_{16}\omega_7^3 - 72\omega_{16}v_2^2\omega_7^2 - 12c_s^2\omega_{16}v_2^2\omega_7^3 - 24v_2^4\omega_7^2 + 24\omega_{16}^2v_2^4\omega_7 - 24c_s^4\omega_{16}\omega_7^2 + 48c_s^2\omega_{16}v_2^2\omega_7^2 - 24c_s^2\omega_{16}\omega_7 + 18\omega_{16}v_2^2\omega_7^3 + 6c_s^4\omega_{16}\omega_7^3 + 12v_2^4\omega_7^3 + 6c_s^2\omega_{16}^2v_2^2\omega_7^3 + 12c_s^2\omega_{16}^2\omega_7 + 24\omega_{16}^2v_2^2\omega_7^2 - 48\omega_{16}v_2^4\omega_7 - 3c_s^4\omega_{16}^2\omega_7^3 - 3\omega_{16}^2v_2^2\omega_7^3 - 72c_s^2\omega_{16}^2v_2^2\omega_7^2 + 24c_s^4\omega_{16}^2 + 24c_s^4\omega_{16}^2\omega_7^2 - 48c_s^4\omega_{16}^2\omega_7 + 12c_s^2v_2^2\omega_7^3 - 18\omega_{16}v_2^2\omega_7^3 + c_s^2\omega_{16}^2\omega_7^3 + 156c_s^2\omega_{16}^2v_2^2\omega_7 - 12v_2^2\omega_7^3 - 24c_s^2v_2^2\omega_7^2 + 72\omega_{16}v_2^2\omega_7^2 + 24v_2^2\omega_7^2 - 8c_s^2\omega_{16}^2\omega_7^2 - 24\omega_{16}^2v_2^2\omega_7) \frac{\rho}{24\omega_{16}^2\omega_7^3}$$

$$C_{D_y^4 v_3}^{(3), \text{MRT}^2} = C_{D_y^4 v_3}^{(3), \text{MRT}^1}$$

$$C_{D_y^4 v_3}^{(3), \text{CLBM}^1} = (3\omega_{16}^2v_2^4\omega_7^3 + 24c_s^2\omega_{16}\omega_7^2 + 72c_s^2\omega_{16}v_2^2\omega_7 + 24c_s^4\omega_{16}\omega_7 - 12\omega_{16}^2v_2^4\omega_7^2 - 6c_s^2\omega_{16}\omega_7^3 - 72\omega_{16}v_2^2\omega_7^2 - 72c_s^2\omega_{16}v_2^2\omega_7^3 - 72v_2^4\omega_7^2 - 24c_s^4\omega_{16}\omega_7^2 + 144c_s^2\omega_{16}v_2^2\omega_7^2 - 24c_s^2\omega_{16}\omega_7 + 30\omega_{16}v_2^2\omega_7^3 + 6c_s^4\omega_{16}\omega_7^3 + 36v_2^4\omega_7^3 + 6c_s^2\omega_{16}^2v_2^2\omega_7^3 + 12c_s^2\omega_{16}^2\omega_7 + 12\omega_{16}^2v_2^2\omega_7^2 - 3c_s^4\omega_{16}^2\omega_7^3 - 3\omega_{16}^2v_2^2\omega_7^3 - 12c_s^2\omega_{16}^2v_2^2\omega_7^2 + 24c_s^4\omega_{16}^2\omega_7 - 48c_s^4\omega_{16}^2\omega_7 + 108c_s^2v_2^2\omega_7^3 - 30\omega_{16}v_2^4\omega_7^3 + c_s^2\omega_{16}^2\omega_7^3 - 36c_s^2\omega_{16}^2v_2^2\omega_7 - 36v_2^2\omega_7^3 - 216c_s^2v_2^2\omega_7^2 + 72\omega_{16}v_2^4\omega_7^2 + 72v_2^2\omega_7^2 - 8c_s^2\omega_{16}^2\omega_7^2) \frac{\rho}{24\omega_{16}^2\omega_7^3}$$

$$C_{D_y^4 v_3}^{(3), \text{CLBM}^2} = C_{D_y^4 v_3}^{(3), \text{CLBM}^1}$$

$$C_{D_y^4 v_3}^{(3), \text{CuLBM}^1} = (12\omega_3^2v_2^2\omega_{11}^2 - 36\omega_3c_s^2v_2^2\omega_{11}^2 + 3\omega_3^3v_2^4\omega_{11}^2 - 8\omega_3^2c_s^2\omega_{11}^2 - 3\omega_3^3c_s^4\omega_{11}^2 + 36\omega_3^3v_2^4 + 24\omega_3c_s^4\omega_{11} + 6\omega_3^3c_s^4\omega_{11} - 48\omega_3c_s^4\omega_{11}^2 + 24\omega_3^2c_s^2\omega_{11} + 72\omega_3c_s^2v_2^2\omega_{11} - 72\omega_3^2v_2^4 - 30\omega_3^3v_2^4\omega_{11} - 216\omega_3^2c_s^2v_2^2 - 72\omega_3^2v_2^2\omega_{11} + 24\omega_3^2c_s^4\omega_{11}^2 - 12\omega_3^2c_s^2v_2^2\omega_{11} + \omega_3^3c_s^2\omega_{11}^2 - 72\omega_3^2c_s^2v_2^2\omega_{11} - 24\omega_3^2c_s^2\omega_{11} - 12\omega_3^2v_2^2\omega_{11} + 72\omega_3^2v_2^2 - 3\omega_3^3v_2^2\omega_{11} + 30\omega_3^3v_2^2\omega_{11} + 108\omega_3^2c_s^2v_2^2 + 72\omega_3^2v_2^2\omega_{11} - 6\omega_3^3c_s^2\omega_{11} - 36\omega_3^3v_2^2 + 6\omega_3^3c_s^2v_2^2\omega_{11} + 12\omega_3c_s^2\omega_{11}^2 - 24\omega_3^2c_s^4\omega_{11} + 24c_s^4\omega_{11}^2 + 144\omega_3^2c_s^2v_2^2\omega_{11}) \frac{\rho}{24\omega_3^3\omega_{11}^2}$$

$$C_{D_y^4 v_3}^{(3), \text{CuLBM}^2} = (3\omega_3^2v_2^4\omega_4^3 - 48\omega_3^2c_s^4\omega_4^3 - 36\omega_3^2c_s^2v_2^2\omega_4^3 + \omega_3^3c_s^2\omega_4^3 + 36\omega_3v_2^2\omega_4\omega_1^2 + 36\omega_3c_s^2v_2^2\omega_4\omega_1 - 12\omega_3^2v_2^4\omega_4^2\omega_1^2 - 18\omega_3v_2^2\omega_4\omega_1^3 - 8\omega_3^2c_s^2\omega_4^2\omega_1^2 - 3\omega_3^2v_2^2\omega_4^3 + 12\omega_3^2c_s^2\omega_4^3 + 6\omega_3^2c_s^2v_2^2\omega_4^3 - 36\omega_3v_2^4\omega_4\omega_1^2 - 3\omega_3^2c_s^4\omega_4^2\omega_1^3 + 72\omega_3c_s^2v_2^2\omega_4^2\omega_1^2 + 9\omega_3^3v_2^4\omega_1^3 - 54\omega_3^2c_s^2v_2^2\omega_1^2 - 12\omega_3^2c_s^2v_2^2\omega_1^2 + 12\omega_3^2v_2^2\omega_1^2 + 24\omega_3^2c_s^4\omega_4^2 + 27\omega_3^2c_s^2v_2^2\omega_1^3 - 18\omega_3^2v_2^4\omega_1^2 - 36\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3 + 24\omega_3^2c_s^4\omega_4^2\omega_1^2 + 18\omega_3^2v_2^4\omega_1^2 - 36\omega_3^2v_2^2\omega_4\omega_1^2 - 3\omega_3^2c_s^2\omega_4^2\omega_1^3 + 27c_s^2v_2^2\omega_1^3 + 12\omega_3c_s^4\omega_4^2\omega_1 + 54\omega_3c_s^2v_2^2\omega_4\omega_1^3 - 12\omega_3^2c_s^4\omega_4\omega_1^2 - 15\omega_3v_2^4\omega_4^2\omega_1^3 + 12\omega_3c_s^2\omega_4^2\omega_1^2 + 15\omega_3^2v_2^2\omega_4\omega_1^3 - 54c_s^2v_2^2\omega_4^2\omega_1^2 - 9v_2^2\omega_4^2\omega_1^3 - 36\omega_3^2c_s^2v_2^2\omega_4\omega_1^3 - 12\omega_3^2c_s^2\omega_4\omega_1 + 36\omega_3v_2^4\omega_4^2\omega_1^2 + 3\omega_3^2c_s^4\omega_4\omega_1^3 - 108\omega_3c_s^2v_2^2\omega_4\omega_1^2 + 3\omega_3c_s^4\omega_4^2\omega_1^3 + 36\omega_3^2v_2^4\omega_4\omega_1^2 - 18v_2^4\omega_4^2\omega_1^2 - 12\omega_3c_s^2\omega_4^2\omega_1 + 18\omega_3^2v_2^2\omega_1^2 + 15\omega_3v_2^2\omega_4\omega_1^3 + 12\omega_3^2c_s^2\omega_4\omega_1^2 + 9v_2^4\omega_4^2\omega_1^3 - 15\omega_3^2v_2^4\omega_4\omega_1^3 - 12\omega_3c_s^4\omega_4^2\omega_1^2 + 12\omega_3^2c_s^4\omega_4\omega_1 - 3\omega_3^2c_s^2\omega_4\omega_1^3 - 36\omega_3v_2^2\omega_4^2\omega_1 + 36\omega_3^2c_s^2v_2^2\omega_4\omega_1 - 9\omega_3^2v_2^2\omega_1^3) \frac{\rho}{24\omega_3^2\omega_4^2\omega_1^3}$$

$$\text{coefficient } C_{D_x^3 D_z \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_1^3 \partial x_3}:$$

$$C_{D_x^3 D_z \rho}^{(3), \text{SRT}} = (24 - 24v_1^2 + 36v_1^2\omega - 14v_1^2\omega^2 - \omega^3 + 14\omega^2 + v_1^2\omega^3 - 36\omega - 42c_s^2\omega^2 + 3c_s^2\omega^3 + 108c_s^2\omega - 72c_s^2) \frac{c_s^2 v_1}{12\omega^3}$$

$$C_{D_x^3 D_z \rho}^{(3), \text{MRT}^1} = (3\omega_6^3\omega_{22}c_s^4\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 18\omega_6^2\omega_{22}c_s^2v_1^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 12\omega_6^2c_s^2\omega_{13}^2\omega_{11}\omega_9^2 - 12\omega_6^3\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_9 - 12\omega_6^3c_s^2\omega_{13}^2\omega_9^2 + 48\omega_6^2\omega_{22}v_3^2v_1^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 72\omega_6\omega_{22}v_3^2c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 18\omega_6^2\omega_{22}c_s^2\omega_{13}^2\omega_{11}\omega_{18}\omega_9 + 36\omega_6^3v_3^2c_s^2\omega_{13}\omega_9^2 + 36\omega_6^3\omega_{22}c_s^4\omega_{13}^2\omega_{11}\omega_9 + 36\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6\omega_{22}c_s^2v_1^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2v_3^2v_1^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - 72\omega_6^2\omega_{22}v_3^2c_s^2\omega_{13}\omega_{18}\omega_9^2 - 96\omega_{22}c_s^4\omega_{13}\omega_{11}\omega_{18}\omega_9^2 - \omega_6^3\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2c_s^2v_1^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 54\omega_6^2\omega_{22}c_s^4\omega_{13}^2\omega_{11}\omega_{18}\omega_9 - 36\omega_6^2v_3^2c_s^2\omega_{13}^2\omega_{11}\omega_{18}\omega_9^2 - 36\omega_6^3\omega_{22}c_s^4\omega_{13}\omega_9 + 6\omega_6^3\omega_{22}v_3^2\omega_{13}\omega_{18}\omega_9 + 12\omega_6\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 12\omega_6^2c_s^2v_1^2\omega_{13}^2\omega_9^2 + 24\omega_6^2\omega_{22}v_3^2\omega_{13}\omega_{18}\omega_9^2 + 18\omega_6^3\omega_{22}c_s^4\omega_{13}^2\omega_{18}\omega_9 + 24\omega_6\omega_{22}v_3^2\omega_{13}\omega_{11}\omega_{18}\omega_9^2 + 18\omega_6^3\omega_{22}v_3^2c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}v_3^2v_1^2\omega_{13}\omega_{18}\omega_9^2 - 5\omega_6^3\omega_{22}c_s^2v_1^2\omega_{13}\omega_{11}\omega_{18}\omega_9 + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_9 + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_9 + 12\omega_6^2\omega_{22}c_s^2\omega_{13}\omega_{11}\omega_{18}\omega_9 - 6\omega_6^3c_s^2\omega_{13}^2\omega_{11}\omega_{18}\omega_9^2 + 36\omega_6^3c_s^4\omega_{13}\omega_9^2 -$$

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[illegible]

[illegible]

[illegible]

C(3), CLBM1
D₂²D₃D₂v₃ = (-2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈ - 2w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈ + w₆w₂₂w₁₉c_s²v₁w₇w₂₀w₁₁w₁₄w₁₈ +

w₂₂w₁₉c_s²v₂w₁₃w₇w₁₁w₁₄w₁₈ - 2w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈ - 2w₆w₁₉v₂²v₁w₁₃w₇w₂₀w₁₄w₁₈ + 2w₆w₂₂w₁₉c_s²v₁w₁₃w₁₁w₁₄w₁₈w₁₈ -

2w₆w₂₂v₂²v₁w₁₃w₇w₁₄w₁₈w₁₈ - w₆w₂₂v₂²v₁w₁₃w₇w₂₀w₁₄w₁₈w₁₈ + 2w₆w₂₂w₁₉c_s²v₂w₁₃w₇w₂₀w₁₁w₁₄w₁₈ + 2w₆w₂₂w₁₉c_s²v₁w₁₃w₇w₁₁w₁₄w₁₈ +

w₆w₂₂w₁₉v₂²v₁w₁₃w₂₀w₁₁w₁₄w₁₈ - 2w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈ + 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₄w₁₈ - 2w₁₉c_s²v₁w₇w₂₀w₁₁w₁₄w₁₈w₁₈ -

w₆w₂₂v₂²v₁w₁₃w₂₀w₁₁w₁₄w₁₈ + 2w₆w₂₂w₁₉c_s²v₂w₁₃w₇w₁₁w₁₄w₁₈w₁₈ + w₆w₂₂c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - w₆w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈ +

2w₁₉v₂²v₁w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂v₂²v₁w₁₃w₇w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈ + 2w₆w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₄w₁₈w₁₈ +

w₆w₂₂v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ + 2w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ + w₆w₂₂c_s²v₁w₁₃w₇w₂₀w₁₄w₁₈w₁₈ + w₆w₂₂w₁₉v₂²v₁w₇w₂₀w₁₁w₁₄w₁₈w₁₈ +

2w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - w₆w₂₂v₂²v₁w₁₃w₇w₂₀w₁₄w₁₈w₁₈ - 2w₂₂w₁₉c_s²v₂w₁₃w₇w₁₁w₁₄w₁₈w₁₈ -

2w₆w₂₂w₁₉c_s²v₂w₁₃w₇w₁₁w₁₄w₁₈w₁₈ + 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ + 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ +

2w₆w₂₂w₁₉c_s²v₂w₁₃w₇w₂₀w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉c_s²v₂w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ -

2w₆w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉c_s²v₂w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉c_s²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ -

2w₆w₂₂w₁₉v₂²v₁w₁₃w₇w₂₀w₁₁w₁₄w₁₈w₁₈ - 2w₆w₂₂w₁₉c_{s</}

$$\begin{aligned}
& 2\omega_6\omega_{19}v_3^2c_s^2\omega_{16}v_{17}w_{23}w_{20}w_{17}w_{11}w_8w_{18} + 2\omega_6\omega_{19}v_3^2c_s^2\omega_{16}v_{17}w_{17}w_{23}w_{17}w_{11}w_8w_{18} + 2\omega_6v_3c_s^2\omega_{16}v_1^2w_{17}w_{20}w_{17}w_{11}w_8w_{18} - \\
& 2\omega_6\omega_{19}v_3^2\omega_{16}v_2^2v_{17}w_{17}w_{23}w_{17}w_{11}w_{18} + 2\omega_6v_3^2\omega_{16}v_2^2v_{17}w_{17}w_{23}w_{20}w_{17}w_{11}w_8w_{18} - 2\omega_6\omega_{19}v_3c_s^2v_1^2w_{23}w_{20}w_{11}w_8w_{18} - \\
& 2\omega_6v_3^2c_s^2\omega_{16}v_{17}w_{17}w_{23}w_{20}w_{17}w_{18}w_{18} - 2\omega_6\omega_{19}v_3c_s^2\omega_{16}v_2^2w_{17}w_{23}w_{20}w_{17}w_{11}w_{18} - 2\omega_6v_3\omega_{16}v_2^2v_1^2w_{17}w_{23}w_{17}w_{18}w_{18} + 2\omega_6c_s^2\omega_{16}v_2^2v_1w_{17}w_{23}w_{17}w_{18}w_{18} +
\end{aligned}$$

[illegible]

$$C_{D_x D_y^2 D_z v_1}^{(3), \text{MRT2}} = C_{D_x D_y^2 D_z v_1}^{(3), \text{MRT1}}$$

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[illegible]

$$\begin{aligned} \mathcal{D}_{\mathbf{C}_D \mathbf{D}_y^2 \mathbf{D}_z \mathbf{v}_2}^{(3), \text{SRT}} = & (-36v_3^2 v_1 \omega + 36v_3 v_1^2 \omega - v_3^2 v_1 \omega^3 - 14v_3 v_1^2 \omega^2 - 24v_3 v_1^2 + v_3 v_1^2 \omega^3 + 14v_3^2 v_1 \omega^2 + 24c_s^2 v_1 - 14v_3 c_s^2 \omega^2 - 24v_3 c_s^2 - c_s^2 v_1 \omega^3 + \\ & v_3 c_s^2 \omega^3 + 14c_s^2 v_1 \omega^2 - 36c_s^2 v_1 \omega + 24v_3^2 v_1 + 36v_3 c_s^2 \omega) \frac{v_2^2 \rho}{\omega_3^2} \end{aligned}$$

[illegible]

[illegible]

$$8\omega_3^2 v_3^2 c_s^2 \omega_4^3 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_1^4 \omega_4^2 \omega_1^3 - 24\omega_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_3^2 \omega_4^2 \omega_2^3 + 4\omega_3^2 v_3^2 \omega_4^2 \omega_1 \omega_2^3 + 16\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 + 9\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 + 78\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_2^3) \frac{v_3}{36\omega_3^2 \omega_4^3 \omega_1^3 \omega_2^3}$$

coefficient $C_{D_x^2 D_z^2 v_1}^{(3)}$ at $\frac{\partial^4 v_1}{\partial x_1^2 \partial x_3^2}$:

$$C_{D_x^2 D_z^2 v_1}^{(3), \text{SRT}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(3), \text{MRT1}} =$$

[illegible]

$$C_{D_x^2 D_z^2 v_1}^{(3), \text{MRT2}} = C_{D_x^2 D_z^2 v_1}^{(3), \text{MRT1}}$$

$$C_{D_x^2 D_z^2 v_1}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x^2 D_z^2 v_1}^{(3), \text{CuLBM1}} = 0$$

$$C_{D_2^+ D_2^+ v_1}^{(3), \text{CuLBM2}} = (-18c_s^2 \omega_1 \omega_2^2 - 12\omega_3 v_1^2 \omega_1^2 \omega_2 + 12v_3^2 \omega_1^2 \omega_2^2 + 6\omega_3 \omega_1^2 \omega_2 + 84\omega_3 c_s^2 \omega_1^3 + 12\omega_3 v_3^2 \omega_2^2 + 6\omega_1 \omega_2^2 - 66\omega_3 v_1^2 \omega_1^2 \omega_2^2 - 6v_3^2 \omega_1^3 \omega_2 - 23\omega_3 \omega_1^3 \omega_2^2 - 50\omega_3 v_1^2 \omega_1^2 \omega_2^2 - 75\omega_3 v_1^2 \omega_1^2 \omega_2 + 48\omega_3 \omega_1^3 \omega_2 + 50\omega_3 v_1^2 \omega_1^3 \omega_2^2 + 23\omega_3 \omega_1^2 \omega_2^3 - 9\omega_3 v_3^2 \omega_1^3 \omega_2 + 12\omega_3 \omega_1^2 \omega_2^2 + 6\omega_3 v_1^2 \omega_1^2 \omega_2 + 18\omega_3 v_3^2 \omega_1^2 \omega_2^2 + 12\omega_3 v_3^2 \omega_1^3 - 66\omega_3 c_s^2 \omega_2^3 + 108\omega_3 c_s^2 \omega_1 \omega_2^3 - 12\omega_3 \omega_1 \omega_2^2 - 12\omega_3 v_3^2 \omega_1 \omega_2^2 - 108\omega_3 c_s^2 \omega_1^3 \omega_2 + 42\omega_3 \omega_2^3 - 42\omega_3 c_s^2 \omega_1^2 \omega_2^3 - 114\omega_3 v_1^2 \omega_2^3 - 60\omega_3 \omega_1 \omega_2^3 - 9\omega_3 v_3^2 \omega_1 \omega_2^3 - 6v_3^2 \omega_1 \omega_2^2 - 18\omega_3 c_s^2 \omega_1^2 \omega_2 + 48\omega_3 v_1^2 \omega_1^2 + 36c_s^2 \omega_1^2 \omega_2^2 + 141\omega_3 v_1 \omega_1 \omega_2^2 - 12\omega_1^2 \omega_2^2 - 18c_s^2 \omega_1^3 \omega_2 + 42\omega_3 c_s^2 \omega_1^3 \omega_2^2 + 60\omega_3 v_1 \omega_1 \omega_2^2 + 6\omega_1^3 \omega_2 - 36\omega_3 \omega_1^3) \frac{v_3 v_1 \rho}{18\omega_3 \omega_1^3 \omega_2^3}$$

coefficient $C_{D_x^2 D_z^2 v_3}^{(3)}$ at $\frac{\partial^4 v_3}{\partial x_1^2 \partial x_3^2}$:

$$C_{\text{D}^2\text{v}_3}^{(3),\text{SRT}} = (-24 - 12\omega^2 + 36\omega - 108v_3^2\omega + 8c_s^2\omega^2 - c_s^2\omega^3 + 72v_3^2 - 18c_s^2\omega + 12c_s^2 + 36v_3^2\omega^2) \frac{c_s^2\rho}{12\omega^3}$$

[illegible]

[illegible]

$$C_{D_y^2 D_z^2 \rho}^{(3), \text{MRT2}} = C_{D_y^2 D_z^2 \rho}^{(3), \text{MRT1}}$$

$$C_{D_y^2 D_z^2 \rho}^{(3), \text{CLBM2}} = C_{D_y^2 D_z^2 \rho}^{(3), \text{CLBM1}}$$

$$C(3, \text{CuLB2M2})_{D_2^2 D_2^2 \rho} = (24\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 + 9\omega_2^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 - 28\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^2 - 24v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 96\omega_4 c_s^4 \omega_1^2 \omega_2^2 + 36\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 18c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 60\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 9\omega_2^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 + 4\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2 - 52\omega_2^2 c_s^2 \omega_4^2 \omega_1^3 - 24\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 119\omega_2^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 + 54\omega_2^2 c_s^4 \omega_1^3 \omega_2^2 - 102\omega_2^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2 + 24\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 - 324\omega_2^2 c_s^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2 + 12c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 30\omega_2^2 v_3^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2 - 138\omega_2^2 c_s^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 216\omega_2^2 c_s^2 v_3^2 \omega_4^2 \omega_2^2 + 108\omega_2^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 - 12\omega_2^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2 + 66\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2 + 24\omega_2^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 + 27\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 8\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 - 108\omega_2^2 c_s^4 \omega_1^3 \omega_2^2 - 27\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2^2 + 15\omega_2^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 + 28\omega_2^2 c_s^4 \omega_4^2 \omega_1 \omega_2^2 - 48\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 + 36\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 216\omega_2^2 c_s^2 v_3^2 \omega_4^2 \omega_1^3 - 28\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 + 72\omega_2^2 c_s^4 \omega_4^2 \omega_1^2 + 138\omega_2^2 c_s^4 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 4\omega_2^2 \omega_4^2 \omega_1^3 \omega_2^2 + 24c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 26\omega_2^2 c_s^2 \omega_4^2 \omega_1 \omega_2^2 + 72\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 18v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 18\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 36\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 60\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 + 12\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 + 35\omega_2^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 - 27\omega_2^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 12\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 20\omega_2^2 c_s^2 \omega_4^2 \omega_2^2 + 36\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 - 58\omega_2^2 c_s^2 \omega_4^2 \omega_1 \omega_2^2 - 4\omega_2^2 \omega_4^2 \omega_1 \omega_2^2 - 12\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 - 20\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 + 54c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 - 32\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 36\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_2^2 - 32\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 27\omega_2^2 c_s^2 \omega_4^2 \omega_1 \omega_2^2 + 4\omega_2^2 \omega_4^2 \omega_2^2 - 36\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2^2 + 49\omega_2^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 74\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 4\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 16\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_2^2 - 36\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 + 16\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 36\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 - 36c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 - 4\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 + 8\omega_2^2 \omega_4^2 \omega_1^2 \omega_2^2 - 36\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 - 9\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 16\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 27\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 \omega_2^2 + 324\omega_2^2 c_s^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 - 4\omega_2^2 \omega_4^2 \omega_2^2 \omega_2^2 - 30\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 + 27\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 \omega_2^2 - 3\omega_2^2 c_s^2 \omega_4^2 \omega_2^2 \omega_2^2 - 84\omega_2^2 c_s^4 \omega_4^2 \omega_1 \omega_2^2 + 24\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 \omega_2^2 + 32\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 72\omega_2^2 c_s^4 \omega_4^2 \omega_1 \omega_2^2 - 42\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 + 108\omega_2^2 c_s^4 \omega_4^2 \omega_2^2 \omega_2^2 - 4\omega_2^2 v_3^2 \omega_4^2 \omega_2^2 \omega_2^2 + 18\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_2^2 \omega_2^2 - 72c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 - 4\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2 + 3\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 36\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 25\omega_2^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 4\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_2^2 \omega_2^2 - 48\omega_2^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 8\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 4\omega_2^2 \omega_4^2 \omega_2^2 + 4\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 + 16\omega_2^2 v_3^2 c_s^2 \omega_4^2 \omega_2^2 + 9\omega_2^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 12\omega_2^2 v_3^2 \omega_4^2 \omega_1 \omega_2^2 + 78\omega_2^2 c_s^4 \omega_4^2 \omega_1 \omega_2^2) \frac{v_3}{36\omega_2^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2^2}$$

coefficient $C_{D_y^2 D_z^2 v_2}^{(3)}$ at $\frac{\partial^4 v_2}{\partial x_2^2 \partial x_3^2}$:

$$C_{D_y^2 D_z^2 v_2}^{(3), \text{SRT}} = 0$$

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$$C_{D_y^2 D_z^2 v_3}^{(3), \text{CLBM1}} = (36v_3^2\omega_{16}\omega_7\omega_{23}\omega_{11}^2 + 12c_s^2\omega_{16}\omega_7\omega_{23}\omega_{11}^2 + 12\omega_{19}\omega_{16}^2\omega_{23}\omega_{11} - 36v_3^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} + 18\omega_{19}v_3^2\omega_{16}\omega_7^3\omega_{23} - 12c_s^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} + 18\omega_{19}c_s^2\omega_{16}\omega_7\omega_{23}\omega_{11}^2 - 12c_s^2\omega_{16}\omega_7^3\omega_{11}^2 + 6\omega_{19}c_s^2\omega_7^3\omega_{23}\omega_{11} - 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} - 6\omega_{19}c_s^2\omega_7^3\omega_{11}^2 + 6\omega_{19}c_s^2\omega_{16}\omega_7^3\omega_{11}^2 - 18\omega_{19}v_3^2\omega_{16}\omega_7^3\omega_{23}\omega_{11} - 36\omega_{19}v_3^2\omega_7^3\omega_{23}\omega_{11}^2 + 12\omega_{19}\omega_{16}\omega_7\omega_{23}\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^3\omega_{23} - 12\omega_{16}\omega_7^3\omega_{23}\omega_{11}^2 + 12\omega_{16}\omega_7^3\omega_{11}^2 + 12\omega_{19}c_s^2\omega_7^2\omega_{11}^2 - 12\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{11}^2 - 12\omega_{16}\omega_7^2\omega_{11}^2 + 12c_s^2\omega_{16}\omega_7^2\omega_{11}^2 - 36\omega_{19}v_3^2\omega_{16}\omega_7\omega_{23}\omega_{11} - 12\omega_{16}\omega_7^2\omega_{11}^2 + 12c_s^2\omega_{16}\omega_7^2\omega_{11}^2 + 36\omega_{19}v_3^2\omega_7^2\omega_{11}^2 + 6\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23} - 12\omega_{19}\omega_7^2\omega_{11}^2 + 18\omega_{19}v_3^2\omega_7^2\omega_{23}\omega_{11} - 36v_3^2\omega_{16}\omega_7^2\omega_{11}^2 + 24\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 18\omega_{19}v_3^2\omega_{16}\omega_7^2\omega_{11}^2 - 12\omega_{19}c_s^2\omega_7^2\omega_{23}\omega_{11} + 72\omega_{19}v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} + 24\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}\omega_7^2\omega_{23}\omega_{11} + 12c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 6\omega_{19}\omega_{16}\omega_7^3\omega_{11}^2 + 36v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 36\omega_{19}v_3^2\omega_{16}\omega_7^2\omega_{11}^2 + 6\omega_{19}\omega_7^2\omega_{11}^2 + 6\omega_{19}\omega_{16}\omega_7^3\omega_{11} - 24c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 72v_3^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 + 36v_3^2\omega_{16}\omega_7^2\omega_{11}^2 - 12\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23} - 18\omega_{19}v_3^2\omega_7^3\omega_{11}^2 - 4\omega_{19}c_s^2\omega_{16}\omega_7^2\omega_{23}\omega_{11}^2 - 24\omega_{19}\omega_{16}\omega_7^2\omega_{23}\omega_{11} + 12\omega_{19}\omega_{16}\omega_7^2\omega_{11}^2 + 36v_3^2\omega_{16}\omega_7^3\omega_{11} - 12\omega_{16}\omega_7^2\omega_{23}\omega_{11} - 18\omega_{19}v_3^2\omega_{16}\omega_7^3\omega_{11}) \frac{c_s^2 \rho}{12\omega_{19}\omega_{16}\omega_7^3\omega_{23}\omega_{11}^2}$$

$$C_{D_y^2 D_z^2 v_3}^{(3), \text{CLBM2}} = C_{D_y^2 D_z^2 v_3}^{(3), \text{CLBM1}}$$

$$C_{D_y^2 D_z^2 v_3}^{(3), \text{CuLBM1}} = (36\omega_6\omega_3^2v_3^2\omega_{10} - 12\omega_6^2c_s^2\omega_{10} - 72\omega_6^2\omega_3^2v_3^2 - 24\omega_6^2\omega_3^2c_s^2 + 12\omega_3^2\omega_{10} + 18\omega_6^2\omega_3c_s^2\omega_{10} + 36\omega_6^2\omega_3^3v_3^2 + 24\omega_6\omega_3^3 - \omega_6^2\omega_3^3c_s^2\omega_{10} + 12\omega_6\omega_3^2c_s^2\omega_{10} - 24\omega_6\omega_3^2 + 12\omega_6^2\omega_3^3c_s^2 - 12\omega_6\omega_3^2\omega_{10} - 72\omega_6\omega_3^3v_3^2 + 24\omega_6^2\omega_3^3 - 36\omega_3^2v_3^2\omega_{10} - 12\omega_3^3 + 12\omega_6\omega_3\omega_{10} - 12\omega_6^2\omega_3^3 - 12\omega_6\omega_3c_s^2\omega_{10} - 24\omega_6\omega_3^3c_s^2 + 36\omega_3^3v_3^2 - 36\omega_6\omega_3v_3^2\omega_{10} + 12\omega_6^2\omega_3c_s^2 + 72\omega_6\omega_3^2v_3^2 + 24\omega_6\omega_3^2c_s^2 - 12\omega_3^2c_s^2\omega_{10} + 12\omega_3^2c_s^2 - 12\omega_6^2\omega_3 + 36\omega_6^2\omega_3v_3^2 - 4\omega_6^2\omega_3^2c_s^2\omega_{10}) \frac{c_s^2 \rho}{12\omega_6^2\omega_3^3\omega_{10}}$$

$$C_{D_y^2 D_z^2 v_3}^{(3), \text{CuLBM2}} = (8\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 32\omega_3^2c_s^2\omega_4\omega_1\omega_2 + 132\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^2 + 9\omega_3^2v_3^4\omega_4\omega_1\omega_2^2 + 72\omega_3^2c_s^2\omega_1\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2 - 90\omega_3^2v_3^2v_2^2\omega_4\omega_1\omega_2^3 + 150\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 4\omega_3^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2v_2^4\omega_1\omega_2^3 + 12\omega_3^2v_3^2\omega_4\omega_1\omega_2^2 - 48\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^2 + 18\omega_3^2c_s^4\omega_1^3\omega_2^3 - 54\omega_3c_s^2v_2^2\omega_1^3\omega_2^3 + 36\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 24\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 54c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 96\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 28\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + \omega_3^2v_3^4\omega_4\omega_1\omega_2^3 - 12\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2v_2^2\omega_1^3\omega_2^3 - 144\omega_3^2v_3^2v_2^2\omega_4\omega_1\omega_2^3 + 24\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 2\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 72\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + 54\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 - 126\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^3 + 12\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 - 6\omega_3v_2^2\omega_4\omega_1\omega_2^3 + 76\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 36\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 12\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 - 18\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2v_2^4\omega_1\omega_2^3 + 6\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 56\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 36\omega_3v_2^2\omega_4\omega_1\omega_2^3 - 72\omega_3^2c_s^4\omega_1^3\omega_2^3 - 12\omega_3v_2^4\omega_4\omega_1\omega_2^3 - 6\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 6\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 + 108\omega_3^2v_3^2v_2^2\omega_4\omega_1\omega_2^3 + 18v_2^2\omega_4\omega_1\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2^3 + 18\omega_3^2v_2^2\omega_1^3\omega_2^3 - 12\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 - \omega_3^2v_3^4\omega_4\omega_1\omega_2^3 - 90\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^3 + 18\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2c_s^2\omega_1^3\omega_2^3 - 54\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 + 2\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 + 66\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 + 18\omega_3^2v_2^4\omega_1\omega_2^3 - 8\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 54\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 216\omega_3^2v_3^2c_s^2\omega_1\omega_2^3 + 6\omega_3v_2^4\omega_4\omega_1\omega_2^3 + 36\omega_3c_s^2\omega_4\omega_1\omega_2^3 + 54\omega_3c_s^2v_2^2\omega_1^3\omega_2^3 - 54\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 - 9\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 - 36\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 4\omega_3^2\omega_4\omega_1\omega_2^3 + 54\omega_3v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 36\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 + 18\omega_3^2v_2^2\omega_1^3\omega_2^3 + 12\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 + 8\omega_3^2\omega_4\omega_1\omega_2^3 - 84\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 48\omega_3^2v_2^4\omega_4\omega_1\omega_2^3 + 12\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + 18\omega_3v_2^4\omega_1\omega_2^3 - 28\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 36\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 8\omega_3c_s^2\omega_4\omega_1\omega_2^3 - 216\omega_3^2v_3^2c_s^2\omega_1\omega_2^3 - 90\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 3\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 9\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 36\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 54\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 32\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 28\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2^3 + 30\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 48\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 2\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 54\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 72\omega_3^2c_s^4\omega_1\omega_2^3 + 6\omega_3v_2^4\omega_4\omega_1\omega_2^3 + 132\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - \omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + 48\omega_3^2v_3^2c_s^2\omega_4\omega_1\omega_2^3 - 4\omega_3^2\omega_4\omega_1\omega_2^3 - 18\omega_3^2v_2^2\omega_1\omega_2^3 + 18\omega_3v_2^4\omega_1\omega_2^3 + 54\omega_3^2c_s^2v_2^2\omega_1\omega_2^3 - 36\omega_3v_2^2\omega_4\omega_1\omega_2^3 + 18\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 180\omega_3^2v_3^2v_2^2\omega_4\omega_1\omega_2^3 - 18v_2^4\omega_4\omega_1\omega_2^3 + 24\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 12\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 60\omega_3v_2^2c_s^2\omega_4\omega_1\omega_2^3 + 56\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 36\omega_3v_2^2\omega_4\omega_1\omega_2^3 - 18\omega_3v_2^2\omega_1^3\omega_2^3 + 12\omega_3v_2^2\omega_4\omega_1\omega_2^3 - 108\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 68\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 14\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 14\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 - 42\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 54\omega_3^2v_3^2c_s^2\omega_1\omega_2^3 + 12\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + \omega_3^2v_3^2\omega_4\omega_1\omega_2^3 - 72\omega_3^2c_s^2\omega_1\omega_2^3 + 8\omega_3c_s^4\omega_4\omega_1\omega_2^3 + 24\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 6\omega_3v_2^2\omega_4\omega_1\omega_2^3 - 36\omega_3c_s^4\omega_4\omega_1\omega_2^3 - 90\omega_3^2v_3^2v_2^2\omega_4\omega_1\omega_2^3 - 30\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 174\omega_3^2c_s^2v_2^2\omega_4\omega_1\omega_2^3 - 24\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 - 20\omega_3^2c_s^2\omega_4\omega_1\omega_2^3 + 18\omega_3^2v_2^4\omega_1\omega_2^3 + 90\omega_3c_s^2v_2^2\omega_4\omega_1\omega_2^3 + 9\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 + 28\omega_3^2c_s^4\omega_4\omega_1\omega_2^3 + 66\omega_3^2v_2^2\omega_4\omega_1\omega_2^3 - 18\omega_3v_2^4\omega_1\omega_2^3) \frac{\rho}{36\omega_3^2\omega_4\omega_1\omega_2^3}$$

$$\text{coefficient } C_{D_x D_z^3 \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x_1 \partial x_3^3} :$$

$$C_{D_x D_z^3 \rho}^{(3), \text{SRT}} = 0$$

$$C_{D_x D_z^3 \rho}^{(3), \text{MRT1}} = (4c_s^4\omega_{11}^2\omega_{18} + 4\omega_6^2c_s^4\omega_{11}^2\omega_{18} - 4\omega_6^2v_3^4\omega_{11}^2 + 20\omega_6v_3^2\omega_{11}^2\omega_{18} - 144\omega_6^2v_3^2c_s^2\omega_{11}^2\omega_{18} + 96\omega_6^2v_3^2c_s^2\omega_{18} + 20\omega_6^2v_3^2\omega_{11}\omega_{18} - 24\omega_6^2v_3^2\omega_{18} + 72\omega_6v_3^2c_s^2\omega_{11}\omega_{18} - 16\omega_6v_3^4\omega_{11}\omega_{18} - 4\omega_6^2c_s^4\omega_{11}^3\omega_{18} - 4c_s^4\omega_{11}^3\omega_{18} - 36\omega_6^2v_3^4\omega_{11}\omega_{18} + 4\omega_6c_s^2\omega_{11}^3 - 4\omega_6c_s^2\omega_{11}\omega_{18} - 8\omega_6^2c_s^2\omega_{11}^3\omega_{18} - 20\omega_6v_3^2\omega_{11}\omega_{18} - 24\omega_6v_3^2c_s^2\omega_{11}^3 + 4\omega_6^2v_3^4\omega_{11}^3 - 8\omega_6^2c_s^2\omega_{11}^3\omega_{18} - 4\omega_6^2c_s^2\omega_{11}^3\omega_{18} + 4\omega_6v_3^2\omega_{11}^3 - 20\omega_6v_3^4\omega_{11}\omega_{18} - 20\omega_6^2v_3^4\omega_{11}\omega_{18} + 4\omega_6^2c_s^4\omega_{11}^3 + 16\omega_6v_3^2\omega_{11}^3\omega_{18} + 4\omega_6^2c_s^2\omega_{11}^3\omega_{18} - 72\omega_6^2v_3^2c_s^2\omega_{11}\omega_{18} + 36\omega_6^2v_3^2\omega_{11}\omega_{18} + 4c_s^2\omega_{11}^3\omega_{18} - 4\omega_6^2c_s^4\omega_{11}^3 + 4\omega_6c_s^2\omega_{11}\omega_{18} + 8\omega_6^2c_s^4\omega_{11}^2\omega_{18} + 20\omega_6v_3^4\omega_{11}\omega_{18} + 120\omega_6^2v_3^2c_s^2\omega_{11}\omega_{18} + 24\omega_6^2v_3^4\omega_{18} - 8v_3^2\omega_{11}^2\omega_{18} - 13\omega_6^2v_3^2\omega_{11}^2\omega_{18} - 24\omega_6^2v_3^2c_s^2\omega_{11}^2 - 4\omega_6c_s^4\omega_{11}^3 - 8\omega_6c_s^4\omega_{11}^2\omega_{18} - 4\omega_6^2c_s^4\omega_{11}\omega_{18} - 4\omega_6^2v_3^2\omega_{11}^3 + 24\omega_6^2v_3^2c_s^2\omega_{11}^3 + 13\omega_6^2v_3^2\omega_{11}^3\omega_{18} + 12\omega_6^2c_s^2\omega_{11}\omega_{18}^2 + 8v_3^2\omega_{11}^3\omega_{18} - 48\omega_6v_3^2c_s^2\omega_{11}^2\omega_{18} + 20\omega_6v_3^4\omega_{11}\omega_{18} + 4\omega_6^2v_3^2\omega_{11}^2 + 32\omega_6^2v_3^4\omega_{11}\omega_{18} + 8\omega_6c_s^4\omega_{11}^3\omega_{18} + 8v_3^2\omega_{11}^2\omega_{18} - 84\omega_6v_3^2c_s^2\omega_{11}^2\omega_{18} - 36v_3^2c_s^2\omega_{11}^2\omega_{18} + 13\omega_6^2v_3^2\omega_{11}^2\omega_{18} + 4\omega_6^2c_s^2\omega_{11}^2 + 8\omega_6c_s^2\omega_{11}^2\omega_{18} - 51\omega_6^2v_3^2c_s^2\omega_{11}^3\omega_{18} + 4\omega_6^2c_s^2\omega_{11}\omega_{18} + 8\omega_6^2c_s^4\omega_{18} - 13\omega_6^2v_3^4\omega_{11}^3\omega_{18} - 8v_3^4\omega_{11}^3\omega_{18} - 12\omega_6^2c_s^4\omega_{11}\omega_{18} + 84\omega_6v_3^2c_s^2\omega_{11}^3\omega_{18} + 36v_3^2c_s^2\omega_{11}^3\omega_{18} + 51\omega_6^2v_3^2c_s^2\omega_{11}^2\omega_{18} - 4\omega_6v_3^4\omega_{11}^2 - 20\omega_6v_3^2\omega_{11}\omega_{18} - 32\omega_6^2v_3^2\omega_{11}^2\omega_{18} - 8\omega_6c_s^2\omega_{11}^3\omega_{18} - 4\omega_6^2c_s^2\omega_{11}^3) \frac{v_1}{4\omega_6^2\omega_{11}^3\omega_{18}^2}$$

$$C_{D_x D_z^3 \rho}^{(3), \text{MRT2}} = C_{D_x D_z^3 \rho}^{(3), \text{MRT1}}$$

$$C_{D_x D_z^3 \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_z^3 \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 \rho}^{(3), \text{CuLBM1}} = 0$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 \rho}^{(3), \text{CuLBM2}} = (56\omega_3^2 c_s^2 \omega_1 \omega_2 - 48\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 + 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 v_1^2 \omega_1^3 + 48\omega_3^2 v_3^2 \omega_1 \omega_2^2 - 36\omega_3^2 c_s^4 \omega_2^2 - 12c_s^2 v_1^2 \omega_1^3 \omega_2^2 + 24\omega_3^2 v_3^4 \omega_1^3 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2 + 4\omega_3^2 \omega_1^3 - 60\omega_3^2 v_3^2 \omega_1 \omega_2^3 - 24\omega_3^2 v_1^2 \omega_1^2 \omega_2^3 - 34\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 48\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 - 72\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 + 6\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 + 24\omega_3^2 c_s^4 \omega_1 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 8\omega_3^2 v_1^2 \omega_1 \omega_2^3 - 216\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^2 - 84\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 72\omega_3^2 v_3^4 \omega_1 \omega_2^2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1^3 + 22\omega_3^2 c_s^4 v_1^2 \omega_1 \omega_2^2 + 40\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 + 8\omega_3^2 c_s^2 v_1^2 \omega_1 \omega_2^2 - 36\omega_3^2 v_3^4 \omega_1 \omega_2^2 + 8\omega_3^2 \omega_1 \omega_2^3 - 8\omega_3^2 v_1^2 \omega_1 \omega_2^2 + 12c_s^2 v_1^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_1^2 \omega_2^3 + 108\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^2 + 42\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^2 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 8\omega_3^2 \omega_2^3 + 48\omega_3^2 v_3^4 \omega_2^3 + 72\omega_3^2 c_s^4 \omega_1^3 + 8\omega_3^2 c_s^2 v_1^2 \omega_1 \omega_2^3 - \omega_3^2 \omega_1^2 \omega_2^3 - 4\omega_3^2 \omega_1^3 \omega_2^2 - 2\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 - 36\omega_3^2 v_3^4 \omega_1^3 \omega_2 + 16\omega_3^2 c_s^2 v_1^2 \omega_1^3 - 324\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2 - 72\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 + 4\omega_3^2 v_1^2 \omega_1^2 \omega_2^2 + 12c_s^2 \omega_1^2 \omega_2^3 - 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 - 18\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 + 216\omega_3^2 v_3^2 c_s^2 \omega_1^3 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2 - 4\omega_3^2 c_s^2 v_1^2 \omega_1^3 \omega_2 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 + 216\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 + \omega_3^2 v_1^2 \omega_1^2 \omega_2^3 + 36c_s^4 \omega_1^2 \omega_2^3 + 42\omega_3^2 c_s^4 \omega_1 \omega_2^2 + 4\omega_3^2 v_1^2 \omega_1^3 \omega_2 - 2\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^3 + 54\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 4\omega_3^2 \omega_2^2 \omega_2^2 + 72\omega_3^2 v_3^4 \omega_2^2 \omega_2^2 - 20\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2 - 24\omega_3^2 v_3^2 \omega_1^3 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 + 20\omega_3^2 c_s^2 \omega_2^3 - 48\omega_3^2 v_3^2 \omega_2^3 + 84\omega_3^2 v_3^2 \omega_1^2 \omega_2 + 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^2 + 96\omega_3^2 v_3^2 v_1^2 \omega_1 \omega_2^3 - 36c_s^4 \omega_1^2 \omega_2^2 - \omega_3^2 v_1^2 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^2 \omega_2^3 - 54\omega_3^2 c_s^4 \omega_2^2 \omega_2^2 + 2\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 \omega_1^2 \omega_2^2 - 52\omega_3^2 c_s^2 \omega_1^3 - 12\omega_3^2 c_s^2 \omega_1^2 \omega_2 - 22\omega_3^2 c_s^2 \omega_1 \omega_2^2 + 24\omega_3^2 v_3^2 v_1^2 \omega_1 \omega_2^2 - 12c_s^2 \omega_1^2 \omega_2^3 - 18\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 - 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 - 20\omega_3^2 c_s^2 v_1^2 \omega_2^2 + 18\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 - 4\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^2 + \omega_3^2 \omega_1^2 \omega_2^2 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 + 72\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 + 4\omega_3^2 v_1^2 \omega_1^2 \omega_2^2) \frac{v_1}{36\omega_3^2 \omega_1^3 \omega_2^3}$$

$$\text{coefficient } C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3)} \text{ at } \frac{\partial^4 v_1}{\partial x_1 \partial x_3^3} :$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{SRT}} = (-36v_3^4 - c_s^4 \omega^3 + 54v_3^4 \omega + 54v_3^2 c_s^2 \omega + 20c_s^4 \omega^2 + 36c_s^4 - 42v_3^2 c_s^2 \omega^2 - 54c_s^4 \omega - 26v_3^4 \omega^2 + 12v_3^2 c_s^2 \omega^3 + 4v_3^4 \omega^3 - 36v_3^2 c_s^2 - 54v_3^2 \omega - 12c_s^2 \omega^2 - 4v_3^2 \omega^3 + 36v_3^2 + 36c_s^2 \omega - 24c_s^2 + 26v_3^2 \omega^2) \frac{\rho}{12\omega^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{MRT1}} = (90\omega_6^3 v_3^2 \omega_{11} \omega_{18}^2 - 21\omega_6^3 v_3^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^3 v_3^2 \omega_{11}^2 + 12\omega_6 v_3^4 \omega_{11} \omega_{18}^2 + 6\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18}^2 - 6\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} - 5\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 6\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 108\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18}^2 - \omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 18\omega_6^2 c_s^4 \omega_{11} \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^2 + 60\omega_6^3 v_3^2 c_s^2 \omega_{11}^2 \omega_{18}^2 + 72\omega_6^3 v_3^4 \omega_{18}^2 - 36\omega_6^3 v_3^4 \omega_{11} \omega_{18} - \omega_6^3 c_s^4 \omega_{11}^3 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 24\omega_6 v_3^2 \omega_{11}^3 \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 6\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 13\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 252\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 24\omega_6 v_3^4 \omega_{11} \omega_{18} - 12\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11} \omega_{18}^2 - 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}^2 - 27\omega_6^3 v_3^4 \omega_{11} \omega_{18} + 12\omega_6^3 v_3^4 \omega_{11}^2 - 18\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 60\omega_6^3 v_3^2 \omega_{11}^2 \omega_{18} - 72\omega_6^3 v_3^2 \omega_{18}^2 + 102\omega_6 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^2 - 12\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 + 19\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 48\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}^2 - 81\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18}^2 + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 48\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 4\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}^2 - 24\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 36\omega_6^3 v_3^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 48\omega_6 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 306\omega_6^3 v_3^2 c_s^2 \omega_{11} \omega_{18} - 24\omega_6 c_s^4 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} + 27\omega_6^2 v_3^4 \omega_{11} \omega_{18} + 12\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 18\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}^2 + 60\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} + 30\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 48\omega_6 v_3^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 12\omega_6 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 162\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{18}^2 + 4\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18}^2 + 24\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}) \frac{\rho}{12\omega_6^3 \omega_{11}^2 \omega_{18}^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{MRT2}} = C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{MRT1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{CLBM1}} = (90\omega_6^3 v_3^2 \omega_{11} \omega_{18}^2 - 99\omega_6^3 v_3^2 c_s^2 \omega_{11} \omega_{18} + 36\omega_6^3 v_3^2 \omega_{11}^2 + 6\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18}^2 - 6\omega_6^2 c_s^2 \omega_{11}^3 \omega_{18} - 5\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 6\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 36\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18}^2 - \omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 18\omega_6^2 c_s^4 \omega_{11} \omega_{18} - 36\omega_6^2 v_3^2 \omega_{11}^2 + 60\omega_6^3 v_3^2 c_s^2 \omega_{11}^2 \omega_{18}^2 + 72\omega_6^3 v_3^4 \omega_{18}^2 - 36\omega_6^3 v_3^4 \omega_{11} \omega_{18} - \omega_6^3 c_s^4 \omega_{11}^3 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 36\omega_6^2 v_3^2 \omega_{11}^3 \omega_{18} - 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 6\omega_6^2 c_s^4 \omega_{11}^3 \omega_{18} + 13\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 6\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 198\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + \omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 18\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 252\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 72\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} - 36\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11} \omega_{18} - 39\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 36\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 6\omega_6^2 v_3^4 \omega_{11} \omega_{18} - 72\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 18\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 36\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 108\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 19\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 36\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 36\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 3\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 4\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 108\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} + 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} - 306\omega_6^2 v_3^2 c_s^2 \omega_{11} \omega_{18} - 24\omega_6 c_s^4 \omega_{11}^2 \omega_{18} + 39\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} + 108\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 6\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 72\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} + 54\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 108\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 19\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 36\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^4 \omega_{11}^2 \omega_{18} + 36\omega_6 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} + 18\omega_6^2 v_3^2 c_s^2 \omega_{11}^2 \omega_{18} - 12\omega_6^2 c_s^2 \omega_{18}^2 + 4\omega_6^2 v_3^4 \omega_{11}^2 \omega_{18}^2 - 12\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2) \frac{\rho}{12\omega_6^3 \omega_{11}^2 \omega_{18}^2}$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{CLBM2}} = C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{CLBM1}}$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{CuLBM1}} = (12\omega_6^3 c_s^4 \omega_8 \omega_2 + 18\omega_6^3 v_3^2 c_s^2 \omega_8 \omega_2^2 + 12\omega_6 c_s^2 \omega_8 \omega_2^3 - 108\omega_6^2 v_3^2 c_s^2 \omega_2^3 + 6\omega_6^3 v_3^2 \omega_8 \omega_2^2 - 99\omega_6^3 v_3^2 c_s^2 \omega_8 \omega_2^2 - 36\omega_6^3 v_3^4 \omega_2^2 + 19\omega_6^2 v_3^4 \omega_8 \omega_2^2 - 6\omega_6^2 c_s^2 \omega_8 \omega_2^2 + 72v_3^4 \omega_8 \omega_2^3 - 306\omega_6 v_3^2 c_s^2 \omega_8 \omega_2^3 + 12\omega_6^2 c_s^4 \omega_8 \omega_2^2 + 12\omega_6 c_s^2 \omega_8 \omega_2^3 + 60\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^3 + 36\omega_6^2 v_3^2 \omega_8 \omega_2^3 + 36\omega_6^2 v_3^2 \omega_8 \omega_2^3 - 6\omega_6^2 c_s^4 \omega_8 \omega_2^3 + 18\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 36\omega_6 v_3^2 c_s^2 \omega_8 \omega_2^2 + 252v_3^2 c_s^2 \omega_8 \omega_2^2 + 54\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^2 + 36\omega_6^2 v_3^2 \omega_8 \omega_2^2 - 4\omega_6^2 v_3^2 \omega_8 \omega_2^2 - 12\omega_6^2 c_s^2 \omega_8 \omega_2^2 + 36\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^2 - 12\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 108\omega_6^2 v_3^2 c_s^2 \omega_2^2 - 19\omega_6^2 v_3^2 \omega_8 \omega_2^2 - 6\omega_6^2 v_3^4 \omega_8 \omega_2^2 - 12\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 72v_3^2 \omega_8 \omega_2^3 + 6\omega_6^2 c_s^2 \omega_8 \omega_2^2 + 4\omega_6^2 v_3^4 \omega_8 \omega_2^2 + 108\omega_6^2 v_3^2 c_s^2 \omega_2^2 - 36\omega_6^2 v_3^4 \omega_2^2 - 90\omega_6 v_3^4 \omega_8 \omega_2^2 - \omega_6^2 c_s^4 \omega_8 \omega_2^2 + 13\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 36\omega_6^2 v_3^2 \omega_2^3 - 12c_s^2 \omega_8 \omega_2^3 - 39\omega_6^2 v_3^4 \omega_8 \omega_2^3 + 6\omega_6^2 c_s^2 \omega_8 \omega_2^2 - 18\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^2 + 12\omega_6^2 c_s^4 \omega_8 \omega_2^2 + 36\omega_6^2 v_3^4 \omega_8 \omega_2^2 - 72\omega_6^2 v_3^2 \omega_8 \omega_2^3 + 36\omega_6^2 v_3^2 \omega_2^2 - \omega_6^2 c_s^4 \omega_8 \omega_2^3 - 6\omega_6^2 c_s^2 \omega_8 \omega_2^2 + 90\omega_6 v_3^4 \omega_8 \omega_2^3 + 198\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^3 - 5\omega_6^2 c_s^2 \omega_8 \omega_2^2 + \omega_6^2 c_s^4 \omega_8 \omega_2^3 + 39\omega_6^2 v_3^2 \omega_8 \omega_2^3 + 12c_s^4 \omega_8 \omega_2^3 - 3\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^2 + 36\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^2 - 24\omega_6^2 c_s^4 \omega_8 \omega_2^2 + 72\omega_6^2 v_3^4 \omega_8 \omega_2^3 + 12\omega_6^2 v_3^2 c_s^2 \omega_8 \omega_2^3 - 36\omega_6^2 v_3^2 \omega_8 \omega_2^2 + 6\omega_6^2 c_s^4 \omega_8 \omega_2^2 - 108\omega_6 v_3^2 c_s^2 \omega_8 \omega_2^3) \frac{\rho}{12\omega_6^3 \omega_8 \omega_2^3}$$

$$C_{\mathbf{D}_x \mathbf{D}_2^3 v_1}^{(3), \text{CuLBM2}} = (54v_3^4 \omega_4^2 \omega_1^3 \omega_2^3 + 48\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1 \omega_2^2 - 18\omega_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + 144\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^2 + 72\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 216v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^3 + 40\omega_3 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 117\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2^3 + 60\omega_3 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 36\omega_3 v_3^4 \omega_4 \omega_1^3 \omega_2^3 - 297\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 - 48\omega_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^2 + 204\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2 - 40\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 86\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 28\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 + 36\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2^3 - 216\omega_3 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 24\omega_3 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 576\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1 \omega_2^3 - 36\omega_3 c_s^4 \omega_4^2 \omega_1^2 \omega_2^3 - 540\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 12\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1 \omega_2^3 - 36v_3^4 \omega_4^2 \omega_1^3 \omega_2^2 + 16\omega_3 c_s^4 \omega_4^2 \omega_1^3 \omega_2 + 72\omega_3^2 c_s^4 \omega_4 \omega_1 \omega_2^3 + 20\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 + 80\omega_3^2 c_s^4 \omega_4^2 \omega_2^3 +$$

$$\begin{aligned}
& 144\omega_3^2 v_3^2 v_1^2 \omega_1^3 + 72\omega_3^2 v_3^2 \omega_4 \omega_1 \omega_2^3 + 240\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 - 48\omega_3^2 v_1^2 \omega_4 \omega_1 \omega_2^3 + 108\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 + 108\omega_3 v_3^4 \omega_4 \omega_1^3 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 \omega_2^3 - \\
& 56\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 \omega_1^2 - 16\omega_3 c_s^2 \omega_1^2 \omega_2^3 \omega_1 \omega_2^2 + 648\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 96\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1 \omega_2^3 - 24\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2^3 - 24\omega_3 v_3^4 \omega_1^2 \omega_2^3 \omega_1 \omega_2^2 - \\
& 144\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 96\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^2 + 32\omega_3^2 c_s^4 \omega_4^2 \omega_1^3 + 16\omega_3^2 \omega_4 \omega_1 \omega_2^2 - 108\omega_3 v_3^2 \omega_4^2 \omega_1^3 \omega_2^2 + 288\omega_3^2 v_3^4 \omega_4 \omega_1^3 \omega_2^2 - 32\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 \omega_1 \omega_2^2 - 108\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^2 - \\
& 72v_3^4 \omega_4^2 \omega_1^2 \omega_2^3 - 432\omega_3^2 v_3^2 v_1^2 \omega_2^3 \omega_2^3 + 162v_3^2 c_s^2 \omega_2^2 \omega_1^3 \omega_2^3 - 36\omega_3 c_s^4 \omega_4^2 \omega_1^3 \omega_2^2 + 72\omega_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^3 - 852\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 - 108\omega_3^2 v_3^2 c_s^2 \omega_4 \omega_1^2 \omega_2^2 - \\
& 180\omega_3 v_3^4 \omega_4 \omega_1^2 \omega_2^3 - 86\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 \omega_2^2 - 2\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 \omega_1^2 + 18\omega_3 c_s^4 \omega_1^2 \omega_2^3 \omega_1^2 - 108v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 8\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 + 48\omega_3^2 c_s^2 \omega_4^2 \omega_1 \omega_2^3 + 324\omega_3 v_3^2 c_s^2 \omega_4 \omega_1^3 \omega_2^3 + \\
& 117\omega_3 v_3^2 \omega_4^2 \omega_1^3 \omega_2^3 - 36\omega_3^2 v_3^4 \omega_4 \omega_1^2 \omega_2^3 - 288\omega_3^2 v_3^4 \omega_4^2 \omega_1 \omega_2^3 + 16\omega_3^2 \omega_4^2 \omega_1 \omega_2^3 - 492\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 48\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 - 108\omega_3^2 v_3^4 \omega_1^2 \omega_2^3 + \\
& 174\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^3 - 60\omega_3 v_3^4 \omega_4^2 \omega_1^2 \omega_2^3 + 117\omega_3^2 v_3^2 \omega_4 \omega_1^3 \omega_2^3 + 24\omega_3^2 v_1^2 \omega_4 \omega_1^2 \omega_2^3 - 54v_3^4 \omega_4^2 \omega_1^3 \omega_2^3 - 324\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 - 40\omega_3 c_s^2 \omega_1^2 \omega_2^3 \omega_1^2 + 18\omega_3^2 c_s^4 \omega_4 \omega_1^3 \omega_2^3 + \\
& 8\omega_3^2 \omega_4^2 \omega_1^3 + 48\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 + 144\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 - 36\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 96\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + 36\omega_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 288\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 36\omega_3 v_3^2 \omega_4 \omega_1^3 \omega_2^2 - \\
& 2\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 40\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 - 54\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 - 108\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 264\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 36\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 16\omega_3 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + \\
& 36v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 216\omega_3 v_3^4 \omega_4^2 \omega_1^2 \omega_2^2 - 492\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 48\omega_3 c_s^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 - 36\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 24\omega_3 v_3^4 \omega_4^2 \omega_1^2 \omega_2^2 - 6\omega_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + \\
& 72\omega_3 c_s^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 - 72\omega_3^2 v_3^4 \omega_4 \omega_1 \omega_2^3 - 24\omega_3^2 v_1^2 \omega_1^2 \omega_2^3 - 48\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 - 108\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^3 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 - 144\omega_3^2 v_3^4 \omega_4^2 \omega_1^2 \omega_2^2 + 144\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + \\
& 24\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 - 72\omega_3^2 c_s^2 \omega_4 \omega_1 \omega_2^3 - 297\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 12\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^3 \omega_2^2 - 12\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^4 \omega_4^2 \omega_1^3 \omega_2^2 - 8\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 96\omega_3^2 v_3^4 \omega_4^2 \omega_1^2 \omega_2^2 + \\
& 24\omega_3 v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 108\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 + 12\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 - 288\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + 16\omega_3 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 - 108\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + 64\omega_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - \\
& 144\omega_3^2 v_3^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 - 12\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^3 \omega_2^2 + 72v_3^2 \omega_4^2 \omega_1^2 \omega_2^3 + 16\omega_3^2 c_s^4 \omega_4^2 \omega_1^2 \omega_2^2 - 72\omega_3^2 c_s^4 \omega_4 \omega_1^2 \omega_2^2 - 96\omega_3^2 v_3^2 \omega_4^2 \omega_1^3 + 48\omega_3^2 v_1^2 \omega_1^2 \omega_2^3 + 36\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + \\
& 162\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 + 54\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 + 6\omega_3^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 - 72\omega_3 c_s^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 - 144\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 264\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 288\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2^2 + \\
& 24\omega_3^2 v_1^2 \omega_4^2 \omega_1^3 \omega_2^2 + 72\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + 24\omega_3^2 c_s^2 v_1^2 \omega_4^2 \omega_1^3 + 108\omega_3 v_3^4 \omega_4^2 \omega_1^3 \omega_2^2 + 468\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 288\omega_3^2 v_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 - 72\omega_3 v_3^2 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 + \\
& 24\omega_3^2 c_s^2 v_1^2 \omega_1^2 \omega_2^3 \omega_1^2 + 38\omega_3^2 v_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 2\omega_3^2 \omega_4^2 \omega_1^3 \omega_2^2 + 180\omega_3 v_3^2 \omega_4 \omega_1^2 \omega_2^3 + 36\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2^2 - 117\omega_3 v_3^4 \omega_4^2 \omega_1^2 \omega_2^2 + 168\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 + \\
& 24\omega_3^2 v_1^2 \omega_4^2 \omega_1^2 \omega_2^2 + 192\omega_3^2 v_3^4 \omega_4^2 \omega_1^2 \omega_2^2 - 16\omega_3^2 \omega_4^2 \omega_1^2 \omega_2^2 + 96\omega_3^2 v_3^2 \omega_4 \omega_1^2 \omega_2^2 + 432\omega_3^2 v_3^2 c_s^2 \omega_4^2 \omega_1^2 \omega_2^2 - 18\omega_3 c_s^2 \omega_4^2 \omega_1^3 \omega_2^2 - 172\omega_3^2 c_s^4 \omega_4^2 \omega_1 \omega_2^3) \frac{\rho}{72\omega_3^2 \omega_4^2 \omega_1^3 \omega_2^3}
\end{aligned}$$

coefficient $C_{D_x D_x^2 v_3}^{(3)}$ at $\frac{\partial^4 v_3}{\partial x_1 \partial x_3^3}$:

$$C_{D_x D_x^2 v_3}^{(3), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_x D_x^2 v_3}^{(3), \text{MRT1}} = & (-32\omega_6^2 \omega_{18}^2 - 68\omega_6 v_3^2 \omega_{11}^2 \omega_{18}^2 + 28\omega_6 \omega_{11}^2 \omega_{18}^2 - 64\omega_6^2 v_3^2 \omega_{11} \omega_{18} + 80\omega_6^2 v_3^2 \omega_{18}^2 + 48\omega_6^2 \omega_{11} \omega_{18}^2 - 28\omega_6 \omega_{11}^2 \omega_{18} - 16\omega_6 c_s^2 \omega_{11}^3 + \\
& 32\omega_6 c_s^2 \omega_{11} \omega_{18}^2 + 56\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 68\omega_6 v_3^2 \omega_{11}^2 \omega_{18} + 48\omega_6^2 c_s^2 \omega_{18}^2 + 24\omega_6^2 \omega_{11} \omega_{18} + 20c_s^2 \omega_{11}^2 \omega_{18}^2 + 25\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 12\omega_{11}^2 \omega_{18}^2 - 16\omega_6 v_3^2 \omega_{11}^3 + \\
& 8\omega_6 \omega_{11}^3 - 48\omega_6 v_3^2 \omega_{11}^2 \omega_{18} - 25\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18} + 16\omega_6 \omega_{11}^2 \omega_{18} - 120\omega_6^2 v_3^2 \omega_{11} \omega_{18}^2 - 20c_s^2 \omega_{11}^2 \omega_{18} + 12\omega_{11}^2 \omega_{18} + 28v_3^2 \omega_{11}^2 \omega_{18}^2 + 43\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}^2 + 8\omega_6^2 \omega_{11}^2 + \\
& 16\omega_6^2 v_3^2 \omega_{11}^3 - 16\omega_6 c_s^2 \omega_{11}^2 \omega_{18} - 43\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} - 40\omega_6^2 \omega_{11}^2 \omega_{18} - 72\omega_6^2 c_s^2 \omega_{11} \omega_{18}^2 - 28v_3^2 \omega_{11}^2 \omega_{18} - 8\omega_6^2 \omega_{11}^3 - 16\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18}^2 - 16\omega_6^2 c_s^2 \omega_{11}^2 \omega_{18}^2 - 44\omega_6 c_s^2 \omega_{11}^2 \omega_{18}^2 - \\
& 17\omega_6^2 \omega_{11}^2 \omega_{18}^2 - 32\omega_6 c_s^2 \omega_{11} \omega_{18} + 64\omega_6 v_3^2 \omega_{11} \omega_{18}^2 + 104\omega_6^2 v_3^2 \omega_{11}^2 \omega_{18} + 44\omega_6 c_s^2 \omega_{11}^2 \omega_{18} - 24\omega_6 \omega_{11} \omega_{18}^2 + 17\omega_6^2 \omega_{11}^2 \omega_{18} + 16\omega_6^2 c_s^2 \omega_{11}^2) \frac{v_3 v_1 \rho}{4\omega_6^3 \omega_{11}^2 \omega_{18}^2}
\end{aligned}$$

$$C_{D_x D_x^2 v_3}^{(3), \text{MRT2}} = C_{D_x D_x^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_x D_x^2 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_x D_x^2 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_x D_x^2 v_3}^{(3), \text{CuLBM1}} = 0$$

$$\begin{aligned}
C_{D_x D_x^2 v_3}^{(3), \text{CuLBM2}} = & (36c_s^2 \omega_1 \omega_2^3 - 12\omega_3 v_3^2 \omega_1^2 \omega_2 + 6\omega_3 \omega_1^2 \omega_2 + 84\omega_3 c_s^2 \omega_1^3 + 84\omega_3 v_3^2 \omega_2^3 - 12\omega_1 \omega_2^3 - 9\omega_3 v_1^2 \omega_1^2 \omega_2^2 + 9v_1^2 \omega_1^3 \omega_2^2 - 5\omega_3 \omega_1^3 \omega_2^2 - \\
& 5\omega_3 v_1^2 \omega_1^3 \omega_2^2 - 18\omega_3 v_1^2 \omega_1^3 \omega_2 - 9v_1^2 \omega_1^2 \omega_2^3 - 6v_1^2 \omega_1^3 \omega_2 + 48\omega_3 \omega_1^2 \omega_2 + 5\omega_3 v_1^2 \omega_1^3 \omega_2^2 + 5\omega_3 \omega_1^2 \omega_2^3 - 54\omega_3 c_s^2 \omega_1 \omega_2^2 - 66\omega_3 v_3^2 \omega_1^2 \omega_2 - 51\omega_3 \omega_1^3 \omega_2^2 + \\
& 6\omega_3 v_1^2 \omega_1^3 \omega_2 - 6v_1^2 \omega_1^2 \omega_2^2 + 132\omega_3 v_3^2 \omega_1^2 \omega_2^2 + 48\omega_3 v_3^2 \omega_1^3 - 12\omega_3 c_s^2 \omega_2^3 + 27\omega_3 c_s^2 \omega_1 \omega_2^3 + 42\omega_3 \omega_1 \omega_2^3 - 9\omega_1^2 \omega_2^2 + 27c_s^2 \omega_1^3 \omega_2^2 - 120\omega_3 v_3^2 \omega_1 \omega_2^2 - \\
& 108\omega_3 c_s^2 \omega_1^2 \omega_2 - 12\omega_3 \omega_2^3 - 15\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 12v_1^2 \omega_1 \omega_2^3 - 24\omega_3 v_1^2 \omega_2^3 + 3\omega_3 \omega_1 \omega_2^2 + 81\omega_3 c_s^2 \omega_1^2 \omega_2^2 - 66\omega_3 v_3^2 \omega_1 \omega_2^2 - 18\omega_3 c_s^2 \omega_1^2 \omega_2 + 12\omega_3 v_1^2 \omega_1^3 - \\
& 18c_s^2 \omega_1^2 \omega_2^2 + 27\omega_3 v_1^2 \omega_1 \omega_2^2 + 6\omega_1^2 \omega_2^2 - 18c_s^2 \omega_1^2 \omega_2 - 27c_s^2 \omega_1^2 \omega_2^2 + 15\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 6\omega_3 v_1^2 \omega_1 \omega_2^2 + 9\omega_1^2 \omega_2^2 + 6\omega_1^3 \omega_2 - 36\omega_3 \omega_1^3) \frac{v_3 v_1 \rho}{18\omega_3 \omega_1^3 \omega_2^3}
\end{aligned}$$

coefficient $C_{D_y D_x^2 \rho}^{(3)}$ at $\frac{\partial^4 \rho}{\partial x_2 \partial x_3^3}$:

$$C_{D_y D_x^2 \rho}^{(3), \text{SRT}} = 0$$

$$\begin{aligned}
C_{D_y D_x^2 \rho}^{(3), \text{MRT1}} = & (4v_3^2 \omega_7^2 \omega_{11}^2 + 8\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 + 4\omega_{19}^2 c_s^4 \omega_7 \omega_{11} + 4c_s^2 \omega_7 \omega_{11}^3 + 20\omega_{19} v_3^4 \omega_7 \omega_{11}^3 + 96\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11} - 72\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11} - 13\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11} + \\
& 8\omega_{19}^2 v_3^4 \omega_{11}^2 - 16\omega_{19} v_3^4 \omega_7 \omega_{11} - 144\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11} - 36\omega_{19} v_3^2 c_s^2 \omega_{11}^3 - 4\omega_{19} c_s^4 \omega_7^2 \omega_{11}^3 - 4v_3^2 \omega_7^2 \omega_{11}^3 - 36\omega_{19}^2 v_3^4 \omega_7^2 \omega_{11} - 24\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 + \\
& 4\omega_{19} c_s^2 \omega_7^2 \omega_{11} + 4\omega_{19} c_s^2 \omega_{11}^3 + 8\omega_{19}^2 c_s^2 \omega_7 \omega_{11}^3 - 8\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 - 4v_3^4 \omega_7^2 \omega_{11}^2 + 24v_3^2 c_s^2 \omega_7^2 \omega_{11}^2 - 51\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11}^2 - 20\omega_{19} v_3^2 \omega_7 \omega_{11}^3 - 4c_s^4 \omega_7 \omega_{11}^3 - \\
& 4\omega_{19} c_s^2 \omega_7 \omega_{11} - 8\omega_{19}^2 c_s^2 \omega_7^2 + 51\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^2 + 8\omega_{19} v_3^2 \omega_{11}^3 + 13\omega_{19} v_3^4 \omega_7^2 \omega_{11}^2 + 120\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11}^2 + 16\omega_{19} v_3^2 \omega_7 \omega_{11}^2 + 36\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11} + \\
& 4v_3^4 \omega_7^2 \omega_{11}^3 + 4\omega_{19} c_s^2 \omega_7^2 \omega_{11}^2 - 24v_3^2 c_s^2 \omega_7^2 \omega_{11}^2 - 4\omega_{19} c_s^4 \omega_7^2 \omega_{11} + 4\omega_{19}^2 c_s^4 \omega_7 \omega_{11} - 8\omega_{19}^2 c_s^4 \omega_7 \omega_{11} - 4c_s^4 \omega_7^2 \omega_{11}^2 - 32\omega_{19} v_3^2 \omega_7^2 \omega_{11}^2 - 48\omega_{19} v_3^2 c_s^2 \omega_7 \omega_{11}^2 - \\
& 4v_3^4 \omega_7 \omega_{11}^3 - 8\omega_{19} c_s^2 \omega_7 \omega_{11}^3 - 20\omega_{19}^2 v_3^2 \omega_7 \omega_{11} + 24\omega_{19}^2 v_3^4 \omega_7^2 - 4\omega_{19} c_s^4 \omega_{11}^3 + 4\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11} + 36\omega_{19}^2 v_3^2 c_s^2 \omega_{11}^2 - 24v_3^2 c_s^2 \omega_7 \omega_{11}^3 + 12\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11} + \\
& 13\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + 4c_s^4 \omega_7^2 \omega_{11}^3 + 84\omega_{19} v_3^2 c_s^2 \omega_7 \omega_{11}^3 - 84\omega_{19}^2 v_3^2 c_s^2 \omega_7 \omega_{11}^3 - 20\omega_{19} v_3^4 \omega_7^2 \omega_{11} - 20\omega_{19}^2 v_3^4 \omega_7 \omega_{11} - 8\omega_{19}^2 v_3^4 \omega_{11}^2 + 72\omega_{19}^2 v_3^2 c_s^2 \omega_7 \omega_{11} + \\
& 32\omega_{19} v_3^4 \omega_7^2 \omega_{11} + 4c_s^2 \omega_7^2 \omega_{11}^2 + 20\omega_{19}^2 v_3^4 \omega_7 \omega_{11} + 8\omega_{19} c_s^4 \omega_7 \omega_{11}^3 + 4v_3^2 \omega_7 \omega_{11}^3 - 4\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11} - 4\omega_{19}^2 c_s^2 \omega_{11}^2 - 4c_s^2 \omega_7^2 \omega_{11}^2 - 13\omega_{19} v_3^4 \omega_7^2 \omega_{11}^2 - \\
& 12\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11} + 8\omega_{19}^2 c_s^4 \omega_7^2 + 20\omega_{19} v_3^2 \omega_7^2 \omega_{11} - 8\omega_{19} v_3^4 \omega_{11}^3 + 20\omega_{19}^2 v_3^2 \omega_7 \omega_{11}^3) \frac{v_2}{4\omega_{19}^2 \omega_7^2 \omega_{11}^3}
\end{aligned}$$

$$C_{D_y D_z^2 \rho}^{(3), \text{MRT}^2} = C_{D_y D_z^2 \rho}^{(3), \text{MRT}^1}$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 \rho}^{(3), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{D_y D_z^2 \rho}^{(3), \text{CuLBM2}} = & (56\omega_3^2 c_s^2 \omega_1 \omega_2 - 4\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2 + 5\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 + 4\omega_3^2 v_2^2 \omega_1^2 \omega_2 + 48\omega_3^2 v_3^2 \omega_1 \omega_2^2 + 24\omega_3^2 v_3^2 v_2^2 \omega_1 \omega_2^2 - 20\omega_3^2 c_s^2 v_2^2 \omega_2^3 + \\ & 18\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^2 - 36\omega_3^2 c_s^4 \omega_2^3 + 24\omega_3^2 v_3^4 \omega_1^3 - 36\omega_3^2 c_s^4 \omega_1^2 \omega_2 + 4\omega_3^2 \omega_1^3 - 60\omega_3^2 v_3^2 \omega_1 \omega_2^3 - \omega_3^2 v_2^2 \omega_1^3 \omega_2^2 - 34\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + 2\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2^2 + 6\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 + \\ & 96\omega_3^2 v_3^2 v_2^2 \omega_1 \omega_2^3 + 24\omega_3^2 c_s^4 \omega_1 \omega_2^3 - 6\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 4\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 - 216\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^3 - 84\omega_3^2 c_s^4 \omega_1 \omega_2^3 + 8\omega_3^2 \omega_1 \omega_2^3 - 72\omega_3^2 v_3^4 \omega_1 \omega_2^3 + 4\omega_3^2 v_2^2 \omega_1^3 \omega_2^3 + \\ & 18\omega_3^2 v_2^2 \omega_1^2 \omega_2^3 - 20\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2^3 + 40\omega_3^2 c_s^2 \omega_1^2 \omega_2^3 - 2\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 - 36\omega_3^2 v_3^4 \omega_1 \omega_2^3 + 8\omega_3^2 \omega_1 \omega_2^3 - 4\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2^3 + 108\omega_3^2 v_3^2 c_s^2 \omega_1 \omega_2^3 - \\ & 18\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 + 42\omega_3^2 c_s^2 v_2^2 \omega_1^3 \omega_2^3 - 2\omega_3^2 c_s^2 v_2^2 \omega_1^2 \omega_2^3 - 5\omega_3^2 c_s^2 \omega_1^3 \omega_2^3 + 16\omega_3^2 c_s^2 v_2^2 \omega_1^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^3 + 4\omega_3^2 v_2^2 \omega_1^3 \omega_2^3 - 8\omega_3^2 \omega_2^3 + 48\omega_3^2 v_3^4 \omega_2^3 + 72\omega_3^2 c_s^4 \omega_1^3 + \\ & 24\omega_3^2 v_3^2 v_2^2 \omega_2^3 - \omega_3^2 \omega_1^2 \omega_2^3 - 4\omega_3^2 \omega_1^3 \omega_2 - 36\omega_3^2 v_3^4 \omega_1^3 \omega_2 - 324\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2 + 8\omega_3^2 c_s^2 v_2^2 \omega_1 \omega_2^3 - 72\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^3 + 8\omega_3^2 v_2^2 \omega_2^3 + 12c_s^2 \omega_1^3 \omega_2^2 + \\ & 8\omega_3^2 c_s^2 v_2^2 \omega_1 \omega_2^2 - 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 + 216\omega_3^2 v_3^2 c_s^2 \omega_1^3 + 4\omega_3^2 c_s^2 \omega_1^3 \omega_2 + 12c_s^2 v_2^2 \omega_1^3 \omega_2^2 + 18\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 - 8\omega_3^2 v_2^2 \omega_1 \omega_2^2 + 216\omega_3^2 v_3^2 c_s^2 \omega_1^2 \omega_2^2 + 36c_s^4 \omega_1^2 \omega_2^2 + \\ & 42\omega_3^2 c_s^4 \omega_1 \omega_2^2 + 24\omega_3^2 v_3^2 v_2^2 \omega_2^3 + 54\omega_3^2 c_s^4 \omega_1^3 \omega_2^2 - 4\omega_3^2 \omega_1^2 \omega_2^2 + 72\omega_3^2 v_3^4 \omega_1^2 \omega_2^2 - 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 + 24\omega_3^2 v_3^2 v_2^2 \omega_1^3 - 8\omega_3^2 v_2^2 \omega_1 \omega_2^2 + 4\omega_3^2 c_s^2 \omega_1^2 \omega_2^2 + \\ & 20\omega_3^2 c_s^2 \omega_2^3 + 22\omega_3^2 c_s^2 v_2^2 \omega_1 \omega_2^3 - 48\omega_3^2 v_3^2 \omega_1^3 + 84\omega_3^2 v_3^2 \omega_1^2 \omega_2 + 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^3 - 8\omega_3^2 c_s^2 \omega_1 \omega_2^2 - 36c_s^4 \omega_1^2 \omega_2^2 - 72\omega_3^2 v_2^2 \omega_2^3 + 24\omega_3^2 v_2^2 \omega_2^3 - \\ & 48\omega_3^2 v_3^2 v_2^2 \omega_2^3 - 54\omega_3^2 c_s^4 \omega_1^2 \omega_2^3 - 4\omega_3^2 \omega_1^2 \omega_2^2 - 52\omega_3^2 c_s^2 \omega_1^3 - 12\omega_3^2 c_s^4 \omega_1^3 \omega_2 - 24\omega_3^2 v_3^2 v_2^2 \omega_1^3 - 22\omega_3^2 c_s^2 \omega_1 \omega_2^3 - 12c_s^2 \omega_1^2 \omega_2^3 - 18\omega_3^2 c_s^2 \omega_1^3 \omega_2^2 - \\ & 12c_s^2 v_2^2 \omega_1^2 \omega_2^2 - 24\omega_3^2 v_3^2 \omega_1^2 \omega_2^2 - 48\omega_3^2 v_3^2 v_2^2 \omega_1^2 \omega_2^2 + \omega_3^2 \omega_1^3 \omega_2^2 - 12\omega_3^2 c_s^4 \omega_1^2 \omega_2^2 - 4\omega_3^2 v_2^2 \omega_1^3 + 72\omega_3^2 v_3^2 c_s^2 \omega_1^3 \omega_2^2) \frac{v_2}{36\omega_3^2 \omega_1^3 \omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{D_y D_z^2 v_2}^{(3)} \text{ at } \frac{\partial^4 v_2}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_z^2 v_2}^{(3), \text{SRT}} = (-36v_3^4 - c_s^4 \omega^3 + 54v_3^4 \omega + 54v_3^2 c_s^2 \omega + 20c_s^4 \omega^2 + 36c_s^4 - 42v_3^2 c_s^2 \omega^2 - 54c_s^4 \omega - 26v_3^4 \omega^2 + 12v_3^2 c_s^2 \omega^3 + 4v_3^4 \omega^3 - 36v_3^2 c_s^2 - 54v_3^2 \omega - 12c_s^2 \omega^2 - 4v_3^2 \omega^3 + 36v_3^2 + 36c_s^2 \omega - 24c_s^2 + 26v_3^2 \omega^2) \frac{\rho}{12\omega^3}$$

$$\begin{aligned} C_{D_y D_z^3 v_2}^{(3), \text{MRT}^1} = & (12\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 + 19\omega_{19}^2 v_3^4 \omega_7^3 \omega_{11}^2 + 60\omega_{19}^2 v_3^2 c_s^2 \omega_7^3 \omega_{11}^2 - 24\omega_{19} v_3^4 \omega_7 \omega_{11}^3 - 21\omega_{19} v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 6\omega_{19}^2 c_s^2 \omega_7 \omega_{11}^3 - 12\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^2 + \\ & 12v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 - 12v_3^4 \omega_7^2 \omega_{11}^3 + 6\omega_{19} c_s^2 \omega_7^3 \omega_{11}^3 - 72\omega_{19}^2 v_3^2 \omega_7^3 + 12\omega_{19}^2 v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 - 108\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 18\omega_{19} c_s^4 \omega_7^3 \omega_{11}^3 + 12v_3^2 \omega_7^2 \omega_{11}^3 + \\ & 4\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 + 90\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 - 12v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 18\omega_{19}^2 v_3^2 \omega_7^3 \omega_{11}^3 - 6\omega_{19} c_s^2 \omega_7^3 \omega_{11}^3 + 12v_3^4 \omega_7^3 \omega_{11}^3 + 252\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - \\ & 12\omega_{19} c_s^2 \omega_7^2 \omega_{11}^3 - 12v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 19\omega_{19}^2 v_3^2 \omega_7^3 \omega_{11}^3 + 30\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 + 24\omega_{19} v_3^2 \omega_7 \omega_{11}^3 - 36\omega_{19} v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 12\omega_{19}^2 c_s^4 \omega_{11}^3 + 162\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - \\ & 24\omega_{19} c_s^4 \omega_7 \omega_{11}^3 + 12\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 - 6\omega_{19} c_s^4 \omega_7^2 \omega_{11}^3 + 12v_3^2 \omega_7^2 \omega_{11}^3 - 12\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 12v_3^4 \omega_7^2 \omega_{11}^3 + 18\omega_{19} c_s^2 \omega_7^2 \omega_{11}^3 - 4\omega_{19}^2 v_3^2 \omega_7^3 \omega_{11}^3 - \\ & 18\omega_{19}^2 v_3^4 \omega_7^2 \omega_{11}^3 - 12v_3^2 \omega_7^3 \omega_{11}^3 + 6\omega_{19} c_s^4 \omega_7^3 \omega_{11}^3 - 90\omega_{19}^2 v_3^4 \omega_7^2 \omega_{11}^3 - 81\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 306\omega_{19}^2 v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 - 12\omega_{19}^2 c_s^2 \omega_7^3 + 24\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 - \\ & \omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 - 12\omega_{19} c_s^2 \omega_7 \omega_{11}^3 + 12\omega_{19}^2 v_3^2 \omega_7 \omega_{11}^3 + 6\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 + 102\omega_{19}^2 v_3^2 c_s^2 \omega_7 \omega_{11}^3 + 60\omega_{19} v_3^4 \omega_7^2 \omega_{11}^3 + 36\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + 12\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 - \\ & 48\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 - 12\omega_{19} v_3^2 c_s^2 \omega_7 \omega_{11}^3 - 48\omega_{19}^2 v_3^2 c_s^2 \omega_7 \omega_{11}^3 - 48\omega_{19}^2 v_3^2 c_s^2 \omega_{11}^3 + 13\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 - 27\omega_{19} v_3^4 \omega_7^3 \omega_{11}^3 - 12\omega_{19}^2 c_s^4 \omega_7^3 \omega_{11}^3 + 72\omega_{19}^2 v_3^4 \omega_7^3 - \\ & 24\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + \omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 + 12\omega_{19} c_s^4 \omega_7 \omega_{11}^3 - 12\omega_{19}^2 v_3^2 \omega_7 \omega_{11}^3 - 6\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 - 60\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + 12\omega_{19}^2 c_s^4 \omega_7^3 + 48\omega_{19} v_3^4 \omega_7^2 \omega_{11}^3 - \\ & \omega_{19}^2 c_s^4 \omega_7^3 \omega_{11}^3 - 36\omega_{19} v_3^4 \omega_7^3 \omega_{11}^3 - 12\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 + 12\omega_{19}^2 c_s^2 \omega_7^3 \omega_{11}^3 - 5\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 + 27\omega_{19} v_3^2 \omega_7^3 \omega_{11}^3) \frac{\rho}{12\omega_{19}^2 \omega_7^3 \omega_{11}^3} \end{aligned}$$

$$C_{D_y D_z^2 v_2}^{(3), \text{MRT}^2} = C_{D_y D_z^2 v_2}^{(3), \text{MRT}^1}$$

$$\begin{aligned} C_{D_y D_z^3 v_2}^{(3), \text{CLBM1}} = & (12\omega_{19} c_s^4 \omega_7^2 \omega_{11}^2 + 19\omega_{19}^2 v_3^4 \omega_7^3 \omega_{11}^2 + 60\omega_{19}^2 v_3^2 c_s^2 \omega_7^3 \omega_{11}^2 - 99\omega_{19} v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 6\omega_{19}^2 c_s^2 \omega_7 \omega_{11}^3 + 108v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 - 36v_3^4 \omega_7^3 \omega_{11}^3 + \\ & 6\omega_{19} c_s^2 \omega_7^3 \omega_{11}^3 - 72\omega_{19}^2 v_3^2 \omega_7^3 + 12\omega_{19}^2 v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 - 36\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 18\omega_{19} c_s^4 \omega_7^3 \omega_{11}^3 + 36v_3^2 \omega_7^2 \omega_{11}^3 + 4\omega_{19}^2 v_3^4 \omega_7^3 \omega_{11}^3 + 90\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 - \\ & 108v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 6\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 - 6\omega_{19} c_s^2 \omega_7^3 \omega_{11}^3 + 36v_3^4 \omega_7^3 \omega_{11}^3 + 252\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 + 198\omega_{19} v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 - 12\omega_{19} c_s^2 \omega_7^2 \omega_{11}^3 - 108v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - \\ & 19\omega_{19}^2 v_3^2 \omega_7^3 \omega_{11}^3 + 54\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 108\omega_{19} v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 12\omega_{19}^2 c_s^4 \omega_{11}^3 + 18\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 24\omega_{19}^2 c_s^4 \omega_7 \omega_{11}^3 - 6\omega_{19} c_s^4 \omega_7^2 \omega_{11}^3 + 36v_3^2 \omega_7^3 \omega_{11}^3 + \\ & 36\omega_{19} v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 36v_3^2 \omega_7^2 \omega_{11}^3 + 18\omega_{19} c_s^2 \omega_7^2 \omega_{11}^3 - 4\omega_{19}^2 v_3^2 \omega_7^3 \omega_{11}^3 - 6\omega_{19}^2 v_3^2 \omega_7^2 \omega_{11}^3 - 36v_3^2 \omega_7^3 \omega_{11}^3 + 6\omega_{19} c_s^4 \omega_7^3 \omega_{11}^3 - 90\omega_{19}^2 v_3^2 \omega_7^3 \omega_{11}^3 - \\ & 3\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 306\omega_{19}^2 v_3^2 c_s^2 \omega_7^2 \omega_{11}^3 - 12\omega_{19}^2 c_s^2 \omega_7^3 - \omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 - 12\omega_{19} c_s^2 \omega_7 \omega_{11}^3 + 6\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 - 18\omega_{19}^2 v_3^2 c_s^2 \omega_7 \omega_{11}^3 + 72\omega_{19} v_3^4 \omega_7^3 \omega_{11}^3 + \\ & 36\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + 12\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 - 36\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + 36\omega_{19} v_3^2 c_s^2 \omega_7^3 \omega_{11}^3 + 13\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 - 39\omega_{19} v_3^4 \omega_7^3 \omega_{11}^3 - 12\omega_{19}^2 c_s^4 \omega_7^3 \omega_{11}^3 + 72\omega_{19}^2 v_3^4 \omega_7^3 + \\ & \omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 + 12\omega_{19} c_s^4 \omega_7 \omega_{11}^3 - 6\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 - 72\omega_{19} v_3^2 \omega_7^2 \omega_{11}^3 + 12\omega_{19}^2 c_s^4 \omega_7^3 + 36\omega_{19} v_3^4 \omega_7^2 \omega_{11}^3 - \omega_{19}^2 c_s^4 \omega_7^3 \omega_{11}^3 - 36\omega_{19} v_3^4 \omega_7^3 \omega_{11}^3 - \\ & 12\omega_{19}^2 c_s^4 \omega_7^2 \omega_{11}^3 + 12\omega_{19}^2 c_s^2 \omega_7^3 \omega_{11}^3 - 5\omega_{19}^2 c_s^2 \omega_7^2 \omega_{11}^3 + 39\omega_{19} v_3^2 \omega_7^3 \omega_{11}^3) \frac{\rho}{12\omega_{19}^2 \omega_7^3 \omega_{11}^3} \end{aligned}$$

$$C_{D_y D_z^3 v_2}^{(3), \text{CLBM2}} = C_{D_y D_z^3 v_2}^{(3), \text{CLBM1}}$$

$$\begin{aligned} C_{D_y D_z^3 v_2}^{(3), \text{CuLBM1}} = & (-12\omega_6 \omega_3^2 c_s^4 \omega_{10}^2 - 3\omega_6^3 \omega_3^2 v_3^2 c_s^2 \omega_{10}^2 - 36\omega_6 \omega_3^2 v_3^4 \omega_{10} + 12\omega_6 \omega_3^2 c_s^2 \omega_{10}^2 - 99\omega_6^3 \omega_3^3 v_3^2 c_s^2 \omega_{10} - 6\omega_6^3 \omega_3^2 v_3^4 \omega_{10} - 6\omega_6^3 \omega_3^3 c_s^2 \omega_{10} + \\ & 36\omega_6^3 \omega_3^3 v_3^4 - 72\omega_6^3 \omega_3^3 v_3^3 \omega_{10} + 6\omega_6^3 \omega_3^3 c_s^2 \omega_{10}^2 + 6\omega_6^2 \omega_3^2 c_s^4 \omega_{10}^2 - 18\omega_6^3 \omega_3^2 c_s^4 \omega_{10} - 12\omega_3^3 c_s^2 \omega_{10}^2 - 4\omega_6^3 \omega_3^3 v_3^2 \omega_{10}^2 - \omega_6^2 \omega_3^3 c_s^2 \omega_{10}^2 + 36\omega_6^2 \omega_3^3 v_3^2 + 13\omega_6^3 \omega_3^3 c_s^4 \omega_{10}^2 + \\ & 39\omega_6^3 \omega_3^3 v_3^3 \omega_{10} + 6\omega_6^2 \omega_3^3 c_s^2 \omega_{10} + 36\omega_6^2 \omega_3^3 v_3^4 \omega_{10} - 72\omega_3^3 v_3^3 \omega_{10}^2 - 19\omega_6^2 \omega_3^3 v_3^2 \omega_{10}^2 + 12\omega_6^2 \omega_3^3 c_s^4 \omega_{10} - 12\omega_6^3 \omega_3^3 c_s^2 \omega_{10} + 12\omega_3^3 c_s^4 \omega_{10} - 90\omega_6 \omega_3^3 v_3^4 \omega_{10}^2 - \\ & 108\omega_6^3 \omega_3^3 v_3^3 \omega_{10}^2 + 12\omega_6^3 \omega_3^3 v_3^2 c_s^2 \omega_{10}^2 + 54\omega_6^3 \omega_3^3 v_3^2 c_s^2 \omega_{10} - 36\omega_6^3 \omega_3^3 v_3^4 + 6\omega_6^3 \omega_3^3 v_3^3 \omega_{10}^2 - 306\omega_6 \omega_3^3 v_3^2 c_s^2 \omega_{10}^2 + 6\omega_6^3 \omega_3^3 c_s^4 \omega_{10} + 72\omega_6^3 \omega_3^3 v_3^4 \omega_{10} - \\ & 6\omega_6^2 \omega_3^3 c_s^2 \omega_{10}^2 - 24\omega_6^3 \omega_3^3 c_s^4 \omega_{10} - 36\omega_6^2 \omega_3^3 v_3^4 + 18\omega_6^2 \omega_3^3 c_s^2 \omega_{10} + 4\omega_6^2 \omega_3^3 v_3^4 \omega_{10}^2 + 12\omega_3^3 c_s^4 \omega_{10} + \omega_6^2 \omega_3^3 c_s^4 \omega_{10}^2 - 18\omega_6^3 \omega_3^3 v_3^2 c_s^2 \omega_{10}^2 + 12\omega_6 \omega_3^3 c_s^2 \omega_{10}^2 + \\ & 36\omega_6^2 \omega_3^3 v_3^2 c_s^2 \omega_{10} + 252\omega_3^3 v_3^2 c_s^2 \omega_{10}^2 + 36\omega_6^3 \omega_3^3 v_3^2 + 36\omega_6 \omega_3^3 v_3^2 \omega_{10} + 60\omega_6^2 \omega_3^3 v_3^2 c_s^2 \omega_{10}^2 - 12\omega_6 \omega_3^3 c_s^4 \omega_{10}^2 - 108\omega_6^2 \omega_3^3 v_3^2 c_s^2 + 90\omega_6 \omega_3^3 v_3^2 \omega_{10}^2 + \\ & 198\omega_6^2 \omega_3^3 v_3^2 c_s^2 \omega_{10} + 18\omega_6^2 \omega_3^3 v_3^2 c_s^2 \omega_{10}^2 + 108\omega_6^2 \omega_3^3 v_3^2 c_s^2 - 5\omega_6^2 \omega_3^3 c_s^2 \omega_{10}^2 - 39\omega_6^2 \omega_3^3 v_3^3 \omega_{10} + 36\omega_6^2 \omega_3^3 v_3^2 c_s^2 \omega_{10} - 36\omega_6 \omega_3^3 v_3^2 c_s^2 \omega_{10} - 6\omega_6^2 \omega_3^3 c_s^4 \omega_{10} - \end{aligned}$$

$$36\omega_6^3\omega_3v_3^2\omega_{10} - \omega_6^3\omega_3c_s^4\omega_{10} - 108\omega_6\omega_3v_3^2c_s^2\omega_{10} - 36\omega_6^3\omega_3v_3^2 + 72\omega_3v_3^4\omega_{10}^2 + 19\omega_6^3\omega_3v_3^4\omega_{10}^2 + 12\omega_6^3\omega_3c_s^4\omega_{10} - 12\omega_6^3\omega_3c_s^2\omega_{10}) \frac{\rho}{12\omega_6^3\omega_3\omega_{10}^2}$$

$$\begin{aligned} C_{D_y D_z^2 v_2}^{(3), \text{CuLBM2}} = & (54v_3^4\omega_1^2\omega_1^3\omega_2^3 - 18\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 72\omega_3v_3^2c_s^2\omega_1^2\omega_1\omega_2^3 - 216v_3^2c_s^2\omega_1^2\omega_1^3\omega_2^3 + 40\omega_3c_s^4\omega_1^2\omega_1^2\omega_2^3 + 24\omega_3^2c_s^2v_2^2\omega_1^2\omega_1^2\omega_2^3 - \\ & 117\omega_3^2v_3^4\omega_4\omega_1^3\omega_2^3 - 288\omega_3^2v_3^2v_2^2\omega_1^2\omega_1^2\omega_2^3 + 60\omega_3v_3^2\omega_4^2\omega_1^2\omega_2^3 + 8\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3v_3^4\omega_4\omega_1^3\omega_2^3 - 297\omega_3^2v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 204\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - \\ & 40\omega_3^2c_s^2\omega_1^2\omega_1^3 + 24\omega_3^2v_3^2\omega_4^2\omega_1^2\omega_2^3 + 86\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^3 - 28\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^3 + 36\omega_3^2v_3^4\omega_4\omega_1^3\omega_2^3 + 48\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 12\omega_3^2c_s^2v_2^2\omega_1^2\omega_1^3\omega_2^3 - 216\omega_3v_3^2\omega_1^2\omega_1^3\omega_2^3 - \\ & 144\omega_3^2v_3^2v_2^2\omega_1^2\omega_1^3\omega_2^3 - 288\omega_3^2v_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 24\omega_3v_3^2\omega_4^2\omega_1^3\omega_2^3 + 12\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 24\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3c_s^4\omega_1^2\omega_1^3\omega_2^3 - 540\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - \\ & 36v_3^4\omega_1^2\omega_1^3\omega_2^3 + 16\omega_3c_s^4\omega_1^2\omega_1^3\omega_2^3 + 24\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + 72\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 - 72\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 20\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 6\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 80\omega_3^2c_s^4\omega_4^2\omega_2^3 + \\ & 72\omega_3^2v_3^2\omega_4\omega_1\omega_2^3 + 240\omega_3^2v_3^2\omega_1^2\omega_1^3\omega_2^3 + 108\omega_3^2v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 108\omega_3v_3^4\omega_4\omega_1^3\omega_2^3 + 72\omega_3c_s^2v_2^2\omega_1^2\omega_1^3\omega_2^3 - 6\omega_3^2v_2^2\omega_1^2\omega_1^3\omega_2^3 - 6\omega_3^2c_s^4\omega_4^2\omega_1^3\omega_2^3 - \\ & 56\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^3 - 16\omega_3c_s^2\omega_1^2\omega_1^3\omega_2^3 - 24\omega_3^2v_2^2\omega_4^2\omega_1^3 + 48\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 648\omega_3^2v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - 24\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 24\omega_3v_3^4\omega_1^2\omega_1^3\omega_2^3 + \\ & 24\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 + 336\omega_3^2v_3^2c_s^2\omega_1^2\omega_1\omega_2^3 - 144\omega_3^2v_3^2\omega_1^2\omega_1^3\omega_2^3 + 96\omega_3^2v_3^4\omega_4\omega_1^2\omega_2^3 + 32\omega_3^2c_s^4\omega_1^2\omega_1^3 - 12\omega_3^2c_s^2v_2^2\omega_1^3\omega_2^3 + 16\omega_3^2\omega_4\omega_1\omega_2^3 - \\ & 108\omega_3v_3^2\omega_4^2\omega_1^3\omega_2^3 + 144\omega_3^2v_3^2v_2^2\omega_1^3\omega_2^3 + 288\omega_3^2v_3^4\omega_4\omega_1^2\omega_2^3 - 32\omega_3^2c_s^2\omega_4^2\omega_1\omega_2^3 - 108\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - 72v_3^4\omega_4^2\omega_1^2\omega_2^3 + 162v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - \\ & 36\omega_3c_s^4\omega_1^2\omega_1^3\omega_2^3 + 72\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - 852\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 180\omega_3v_3^4\omega_4\omega_1^3\omega_2^3 - 86\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 + 24\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - \\ & 2\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^3 + 48\omega_3c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 18\omega_3^2c_s^4\omega_1^2\omega_1^3\omega_2^3 - 108v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 8\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 324\omega_3v_3^2c_s^2\omega_4\omega_1^3\omega_2^3 + 117\omega_3v_3^2\omega_4^2\omega_1^3\omega_2^3 - \\ & 96\omega_3^2c_s^2v_2^2\omega_1^2\omega_2^3 - 36\omega_3^2v_3^2\omega_4\omega_1^3\omega_2^3 - 288\omega_3^2v_3^2\omega_4\omega_1^3\omega_2^3 + 16\omega_3^2\omega_4^2\omega_1\omega_2^3 + 144\omega_3^2v_3^2v_2^2\omega_4\omega_1^3\omega_2^3 - 492\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3^2v_3^4\omega_1^2\omega_2^3 + \\ & 174\omega_3^2v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 60\omega_3v_3^4\omega_4\omega_1^3\omega_2^3 + 117\omega_3^2v_3^2\omega_4\omega_1^3\omega_2^3 - 54v_3^2\omega_4^2\omega_1^3\omega_2^3 - 324\omega_3^2v_3^2c_s^2\omega_1^3\omega_2^3 - 40\omega_3c_s^2\omega_4^2\omega_1^2\omega_2^3 + 18\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 + 8\omega_3^2\omega_1^2\omega_2^3 + \\ & 48\omega_3^2v_3^4\omega_1^2\omega_2^3 - 36\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 36\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 288\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 36\omega_3v_3^2\omega_4\omega_1^3\omega_2^3 - 2\omega_3^2\omega_4^2\omega_1^2\omega_2^3 + 40\omega_3^2v_3^4\omega_1^2\omega_2^3 - 54\omega_3^2v_3^2\omega_1^3\omega_2^3 - \\ & 108\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 - 8\omega_3^2\omega_4^2\omega_1^3\omega_2^3 + 264\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^3 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 - 96\omega_3c_s^2v_2^2\omega_1^2\omega_2^3 - 16\omega_3c_s^2\omega_1^2\omega_2^3 + 36v_3^2\omega_4^2\omega_1^3\omega_2^3 + 216\omega_3v_3^4\omega_4^2\omega_1^3\omega_2^3 - \\ & 492\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^3 - 432\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 36\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 24\omega_3v_3^4\omega_4\omega_1^3\omega_2^3 - 72\omega_3^2v_3^4\omega_4\omega_1^3\omega_2^3 - 48\omega_3^2v_3^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3v_3^4\omega_4\omega_1^3\omega_2^3 - 8\omega_3^2\omega_1^2\omega_2^3 - \\ & 144\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 - 72\omega_3^2c_s^2\omega_4\omega_1^3\omega_2^3 - 297\omega_3v_3^2c_s^2\omega_1^2\omega_2^3\omega_1^3\omega_2^3 - 12\omega_3^2c_s^2\omega_1^2\omega_2^3\omega_1^3\omega_2^3 + 24\omega_3^2v_3^4\omega_4\omega_1^3\omega_2^3 - 12\omega_3^2c_s^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 8\omega_3^2\omega_1^2\omega_2^3 + 96\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 + \\ & 24\omega_3v_3^2\omega_1^2\omega_2^3 + 576\omega_3^2v_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 + 108\omega_3^2v_3^2\omega_1^3\omega_2^3 + 16\omega_3c_s^4\omega_4^2\omega_1^3\omega_2^3 + 144\omega_3^2v_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 108\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 64\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 72v_3^2\omega_1^2\omega_2^3 + \\ & 16\omega_3^2c_s^4\omega_1^2\omega_2^3 - 48\omega_3^2v_2^2\omega_4^2\omega_1^3\omega_2^3 - 72\omega_3^2c_s^4\omega_4\omega_1^3\omega_2^3 - 96\omega_3^2v_3^2\omega_1^3\omega_2^3 + 36\omega_3c_s^2\omega_4^2\omega_1^3\omega_2^3 + 162\omega_3^2v_3^2\omega_1^3\omega_2^3 + 54\omega_3^2\omega_4^3\omega_1^3\omega_2^3 - 144\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 + \\ & 264\omega_3^2v_3^2c_s^2\omega_1^2\omega_2^3 - 288\omega_3^2v_3^2\omega_4\omega_1^3\omega_2^3 + 72\omega_3^2v_3^2c_s^2\omega_1^3\omega_2^3 + 108\omega_3v_3^4\omega_4^2\omega_1^3\omega_2^3 + 468\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 72\omega_3v_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 + 144\omega_3^2v_3^2v_2^2\omega_4^2\omega_1\omega_2^3 + \\ & 38\omega_3^2v_3^4\omega_4^2\omega_1^3\omega_2^3 + 48\omega_3^2c_s^2v_3^2\omega_4^2\omega_1\omega_2^3 + 2\omega_3^2\omega_1^2\omega_2^3 + 180\omega_3v_3^2\omega_4\omega_1^3\omega_2^3 + 36\omega_3^2v_3^2\omega_4\omega_1^3\omega_2^3 - 117\omega_3v_3^4\omega_4^2\omega_1^3\omega_2^3 + 168\omega_3^2v_3^2\omega_1^2\omega_2^3\omega_1^3\omega_2^3 + \\ & 192\omega_3^2v_3^4\omega_4^2\omega_2^3 - 16\omega_3^2\omega_4^2\omega_2^3 + 96\omega_3^2v_3^2\omega_4^2\omega_1\omega_2^3 + 432\omega_3^2v_3^2c_s^2\omega_4^2\omega_2^3 - 18\omega_3^2c_s^2\omega_4^2\omega_1^3\omega_2^3 - 48\omega_3^2v_2^2\omega_4^2\omega_1\omega_2^3 - 172\omega_3^2c_s^4\omega_4^2\omega_1\omega_2^3) \frac{\rho}{72\omega_3^2\omega_4^2\omega_1^3\omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{D_y D_z^2 v_3}^{(3)} \text{ at } \frac{\partial^4 v_3}{\partial x_2 \partial x_3^3} :$$

$$C_{D_y D_z^2 v_3}^{(3), \text{SRT}} = 0$$

$$\begin{aligned} C_{D_y D_z^2 v_3}^{(3), \text{MRT1}} = & (-16v_2^2\omega_7^2\omega_{11}^3 - 16c_s^2\omega_7\omega_{11}^3 - 12\omega_{19}^2\omega_{11}^2 + 43\omega_{19}^2v_3^2\omega_7^2\omega_{11}^2 + 8\omega_7\omega_{11}^3 + 16v_2^2\omega_7^2\omega_{11}^3 + 48\omega_{19}^2\omega_7^2\omega_{11} + 80\omega_{19}^2v_3^2\omega_7^2 - 32\omega_{19}^2c_s^2\omega_7^2\omega_{11} - \\ & 20\omega_{19}^2c_s^2\omega_{11}^2 - 44\omega_{19}^2c_s^2\omega_7\omega_{11}^2 + 56\omega_{19}^2c_s^2\omega_7^2\omega_{11}^2 + 68\omega_{19}^2v_3^2\omega_7\omega_{11}^2 + 32\omega_{19}^2c_s^2\omega_7\omega_{11} + 48\omega_{19}^2c_s^2\omega_7^2 - 28\omega_{19}\omega_7\omega_{11}^3 - 28\omega_{19}v_3^2\omega_{11}^3 - 17\omega_{19}^2\omega_7^2\omega_{11} - \\ & 48\omega_{19}^2v_3^2\omega_7^2\omega_{11} - 120\omega_{19}^2v_3^2\omega_7^2\omega_{11} - 25\omega_{19}^2c_s^2\omega_7^2\omega_{11} + 16\omega_{19}\omega_7\omega_{11}^3 + 104\omega_{19}^2v_3^2\omega_7^2\omega_{11}^2 + 44\omega_{19}^2c_s^2\omega_7\omega_{11} + 64\omega_{19}^2v_3^2\omega_7\omega_{11} - 32\omega_{19}^2\omega_7^2 - 40\omega_{19}\omega_7^2\omega_{11}^2 - \\ & 16\omega_{19}^2c_s^2\omega_7\omega_{11} - 72\omega_{19}^2c_s^2\omega_7^2\omega_{11} - 43\omega_{19}^2v_3^2\omega_7^2\omega_{11} + 28\omega_{19}\omega_7\omega_{11}^2 + 28\omega_{19}^2v_3^2\omega_{11}^2 + 17\omega_{19}\omega_7\omega_{11}^3 - 16c_s^2\omega_7^2\omega_{11} - 24\omega_{19}^2\omega_7\omega_{11} - 16v_3^2\omega_7\omega_{11}^3 + \\ & 8\omega_7^2\omega_{11}^2 + 12\omega_{19}\omega_{11}^3 + 25\omega_{19}^2c_s^2\omega_7^2\omega_{11}^2 + 20\omega_{19}^2c_s^2\omega_{11}^2 + 24\omega_{19}\omega_7\omega_{11} + 16c_s^2\omega_7^2\omega_{11} - 64\omega_{19}v_3^2\omega_7^2\omega_{11} - 8\omega_7^2\omega_{11}^3 - 68\omega_{19}^2v_3^2\omega_7\omega_{11}^2) \frac{v_3 v_2 \rho}{4\omega_{19}^2\omega_7^2\omega_{11}^3} \end{aligned}$$

$$C_{D_y D_z^2 v_3}^{(3), \text{MRT2}} = C_{D_y D_z^2 v_3}^{(3), \text{MRT1}}$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CLBM1}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CLBM2}} = 0$$

$$C_{D_y D_z^2 v_3}^{(3), \text{CuLBM1}} = 0$$

$$\begin{aligned} C_{D_y D_z^2 v_3}^{(3), \text{CuLBM2}} = & (36c_s^2\omega_1\omega_2^3 - 12\omega_3v_3^2\omega_1^2\omega_2 + 6\omega_3v_2^2\omega_1\omega_2^2 + 6\omega_3\omega_1^2\omega_2 + 84\omega_3c_s^2\omega_1^3 + 84\omega_3v_3^2\omega_2^3 - 12\omega_1\omega_2^3 + 27\omega_3v_2^2\omega_1\omega_2^3 - 5\omega_3\omega_1^3\omega_2^2 + \\ & 12\omega_3v_2^2\omega_1^3 + 48\omega_3\omega_1^3\omega_2 + 5\omega_3\omega_1^2\omega_2^3 + 12v_2^2\omega_1\omega_2^3 - 54\omega_3c_s^2\omega_1\omega_2^2 - 66\omega_3v_3^2\omega_1^3\omega_2 - 24\omega_3v_2^2\omega_2^3 - 51\omega_3\omega_1^2\omega_2^2 + 132\omega_3v_3^2\omega_1^2\omega_2^2 + 48\omega_3v_3^2\omega_1^3 - \\ & 12\omega_3c_s^2\omega_2^3 + 27\omega_3c_s^2\omega_1\omega_2^3 + 42\omega_3\omega_1\omega_2^2 - 9\omega_1^3\omega_2^2 + 27c_s^2\omega_1^3\omega_2^2 + 6\omega_3v_2^2\omega_1^2\omega_2 - 120\omega_3v_3^2\omega_1\omega_2^2 - 6v_2^2\omega_1^2\omega_2^2 - 108\omega_3c_s^2\omega_1^3\omega_2 - 12\omega_3\omega_2^3 - \\ & 15\omega_3c_s^2\omega_1^2\omega_2^2 + 3\omega_3\omega_1\omega_2^3 - 6v_2^2\omega_1^3\omega_2 + 81\omega_3c_s^2\omega_1^2\omega_2^2 - 9v_2^2\omega_1^2\omega_2^2 - 66\omega_3v_3^2\omega_1\omega_2^2 + 5\omega_3v_2^2\omega_1^2\omega_2^2 - 18\omega_3c_s^2\omega_1^2\omega_2 + 9v_2^2\omega_1^2\omega_2^2 - 18\omega_3v_2^2\omega_1^3\omega_2 - \\ & 18c_s^2\omega_1^2\omega_2^2 - 5\omega_3v_2^2\omega_1^2\omega_2^2 + 6\omega_1^2\omega_2^2 - 9\omega_3v_2^2\omega_1^2\omega_2^2 - 18c_s^2\omega_1^3\omega_2 - 27c_s^2\omega_1^2\omega_2^2 + 15\omega_3c_s^2\omega_1^3\omega_2^2 + 9\omega_1^2\omega_2^3 + 6\omega_1^3\omega_2 - 36\omega_3\omega_1^3) \frac{v_3 v_2 \rho}{18\omega_3\omega_1^3\omega_2^3} \end{aligned}$$

$$\text{coefficient } C_{D_z^4 \rho}^{(3)} \text{ at } \frac{\partial^4 \rho}{\partial x^3} :$$

$$\begin{aligned} C_{D_z^4 \rho}^{(3), \text{SRT}} = & (12 + 144v_3^4 - 5c_s^4\omega^3 - 216v_3^4\omega - 1008v_3^2c_s^2\omega + 82c_s^4\omega^2 + 144c_s^4 + 404v_3^2c_s^2\omega^2 - 216c_s^4\omega - \omega^3 + 90v_3^4\omega^2 + 8\omega^2 - 34v_3^2c_s^2\omega^3 - 18\omega - \\ & 9v_3^4\omega^3 + 672v_3^2c_s^2 + 234v_3^2\omega - 78c_s^2\omega^2 + 6c_s^2\omega^3 + 10v_3^2\omega^3 - 156v_3^2 + 198c_s^2\omega - 132c_s^2 - 98v_3^2\omega^2) \frac{v_3}{12\omega^3} \end{aligned}$$

$$\begin{aligned} C_{D_z^4 \rho}^{(3), \text{MRT1}} = & (12 + 144v_3^4 + 10v_3^2\omega_{11}^3 + 198c_s^2\omega_{11} - 98v_3^2\omega_{11}^2 + 144c_s^4 + 234v_3^2\omega_{11} - 78c_s^2\omega_{11}^2 + 6c_s^2\omega_{11}^3 + 672v_3^2c_s^2 + 404v_3^2c_s^2\omega_{11}^2 - 216c_s^4\omega_{11} - \\ & \omega_{11}^3 - 18\omega_{11} + 90v_3^4\omega_{11}^2 + 8\omega_{11}^2 - 34v_3^2c_s^2\omega_{11}^3 - 9v_3^4\omega_{11}^3 - 5c_s^4\omega_{11}^3 - 156v_3^3 - 216v_3^4\omega_{11} - 132c_s^2 - 1008v_3^2c_s^2\omega_{11} + 82c_s^4\omega_{11}^2) \frac{v_3}{12\omega_{11}^3} \end{aligned}$$

$$C_{D_z^4 \rho}^{(3), \text{MRT}2} = C_{D_z^4 \rho}^{(3), \text{MRT}1}$$

$$C_{D_z^4 \rho}^{(3), \text{CLBM}1} = C_{D_z^4 \rho}^{(3), \text{MRT}1}$$

$$C_{D_z^4 \rho}^{(3), \text{CLBM}2} = C_{D_z^4 \rho}^{(3), \text{MRT}1}$$

$$C_{D_z^4 \rho}^{(3), \text{CuLBM}1} = (12 + 234\omega_6 v_3^2 + 82\omega_6^2 c_s^4 - 18\omega_6 + 144v_3^4 + 198\omega_6 c_s^2 - 1008\omega_6 v_3^2 c_s^2 + 90\omega_6^2 v_3^4 + 144c_s^4 - 34\omega_6^3 v_3^2 c_s^2 - 5\omega_6^3 c_s^4 - 9\omega_6^3 v_3^4 + 672v_3^2 c_s^2 + 8\omega_6^2 + 6\omega_6^2 c_s^2 - \omega_6^3 + 10\omega_6^3 v_3^2 - 216\omega_6 v_3^4 - 78\omega_6^2 c_s^2 - 156v_3^2 - 216\omega_6 c_s^4 - 98\omega_6^2 v_3^2 - 132c_s^2 + 404\omega_6^2 v_3^2 c_s^2) \frac{v_3}{12\omega_6^3}$$

$$C_{D_z^4 \rho}^{(3), \text{CuLBM}2} = (-8c_s^2 \omega_1 \omega_2^3 - 104\omega_3 v_3^2 \omega_1^2 \omega_2 + 160\omega_3 v_3^2 c_s^2 \omega_1^3 + 30\omega_3 v_3^2 \omega_1^3 \omega_2^3 + 72\omega_3 c_s^4 \omega_1 \omega_2^2 + 8\omega_3 \omega_1^2 \omega_2 - 52\omega_3 c_s^2 \omega_1^3 - 3\omega_3 \omega_1^3 \omega_2^3 - 160\omega_3 v_3^2 \omega_2^3 + 180\omega_3 v_3^4 \omega_1^2 \omega_2^3 - 84\omega_3 v_3^4 \omega_1^3 \omega_2 - 98\omega_3 v_3^2 \omega_1^3 \omega_2^2 - 264\omega_3 v_3^4 \omega_1^2 \omega_2^2 + 8\omega_3 \omega_1^3 \omega_2^2 - 372\omega_3 c_s^4 \omega_1 \omega_2^3 - 27\omega_3 v_3^4 \omega_1^3 \omega_2^3 + 96\omega_3 v_3^4 \omega_1^2 \omega_2 + 24c_s^4 \omega_1 \omega_2^3 + 8v_3^2 c_s^2 \omega_1^3 \omega_2 - 10\omega_3 \omega_1^3 \omega_2 + 16\omega_3 \omega_1^2 \omega_2^3 - 80\omega_3 c_s^2 \omega_1 \omega_2^2 - 1472\omega_3 v_3^2 c_s^2 \omega_1 \omega_2^3 + 94\omega_3 v_3^2 \omega_1^3 \omega_2 - 196\omega_3 v_3^2 \omega_1^2 \omega_2^3 - 16v_3^2 c_s^2 \omega_1^2 \omega_2^2 - 16\omega_3 \omega_1^2 \omega_2^2 + 760\omega_3 v_3^2 c_s^2 \omega_2^3 + 90\omega_3 v_3^4 \omega_1^3 \omega_2^2 + 280\omega_3 v_3^2 \omega_1^2 \omega_2^2 - 28\omega_3 v_3^2 \omega_1^3 - 184\omega_3 c_s^2 \omega_2^3 + 656\omega_3 v_3^2 c_s^2 \omega_1 \omega_2^2 + 320\omega_3 c_s^2 \omega_1 \omega_2^3 - 15\omega_3 c_s^4 \omega_1^3 \omega_2^3 + 8\omega_3 \omega_1 \omega_2^2 + 72\omega_3 c_s^4 \omega_1^2 \omega_2 - 48c_s^4 \omega_1^2 \omega_2^2 - 1088\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2^2 - 176\omega_3 v_3^2 \omega_1 \omega_2^2 + 122\omega_3 c_s^2 \omega_1^3 \omega_2 + 16\omega_3 \omega_2^3 - 156\omega_3 c_s^2 \omega_1^2 \omega_2^3 + 24c_s^4 \omega_1^3 \omega_2 - 28\omega_3 \omega_1 \omega_2^3 + 8v_3^2 c_s^2 \omega_1 \omega_2^3 + 82\omega_3 c_s^4 \omega_1^3 \omega_2^2 + 72\omega_3 c_s^4 \omega_1^3 + 152\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 144\omega_3 v_3^4 \omega_2^3 + 328\omega_3 v_3^2 \omega_1 \omega_2^3 - 464\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2 + 808\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2^3 - 80\omega_3 c_s^2 \omega_1^2 \omega_2 + 18\omega_3 c_s^2 \omega_1^3 \omega_2^2 + 404\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2^2 + 16c_s^2 \omega_1^2 \omega_2^2 + 24\omega_3 v_3^4 \omega_1^3 + 168\omega_3 v_3^4 \omega_1 \omega_2^2 + 216\omega_3 c_s^4 \omega_2^3 + 164\omega_3 c_s^4 \omega_1^2 \omega_2^2 - 156\omega_3 c_s^4 \omega_1^3 \omega_2 + 440\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2 - 8c_s^2 \omega_1^3 \omega_2 - 102\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2^2 - 78\omega_3 c_s^2 \omega_1^3 \omega_2^2 - 120\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_1^3 - 300\omega_3 v_3^4 \omega_1 \omega_2^3) \frac{v_3}{36\omega_3 \omega_1^3 \omega_2^3}$$

coefficient $C_{D_z^4 v_3}^{(3)}$ at $\frac{\partial^4 v_3}{\partial x_3^4}$:

$$C_{D_z^4 v_3}^{(3), \text{SRT}} = (12 + 504v_3^4 - c_s^4 \omega^3 - 756v_3^4 \omega - 648v_3^2 c_s^2 \omega + 14c_s^4 \omega^2 + 24c_s^4 + 252v_3^2 c_s^2 \omega^2 - 36c_s^4 \omega - \omega^3 + 310v_3^4 \omega^2 + 8\omega^2 - 18v_3^2 c_s^2 \omega^3 - 18\omega - 29v_3^4 \omega^3 + 432v_3^2 c_s^2 + 378v_3^2 \omega - 22c_s^2 \omega^2 + 2c_s^2 \omega^3 + 14v_3^2 \omega^3 - 252v_3^2 + 54c_s^2 \omega - 36c_s^2 - 154v_3^2 \omega^2) \frac{\rho}{12\omega^3}$$

$$C_{D_z^4 v_3}^{(3), \text{MRT}1} = (12 + 504v_3^4 + 14v_3^2 \omega_{11}^3 + 54c_s^2 \omega_{11} - 154v_3^2 \omega_{11}^2 + 24c_s^4 + 378v_3^2 \omega_{11} - 22c_s^2 \omega_{11}^2 + 2c_s^2 \omega_{11}^3 + 432v_3^2 c_s^2 + 252v_3^2 c_s^2 \omega_{11}^2 - 36c_s^4 \omega_{11} - \omega_{11}^3 - 18\omega_{11} + 310v_3^4 \omega_{11}^2 + 8\omega_{11}^2 - 18v_3^2 c_s^2 \omega_{11}^3 - 29v_3^4 \omega_{11}^3 - c_s^4 \omega_{11}^3 - 252v_3^2 - 756v_3^4 \omega_{11} - 36c_s^2 - 648v_3^2 c_s^2 \omega_{11} + 14c_s^4 \omega_{11}^2) \frac{\rho}{12\omega_{11}^3}$$

$$C_{D_z^4 v_3}^{(3), \text{MRT}2} = C_{D_z^4 v_3}^{(3), \text{MRT}1}$$

$$C_{D_z^4 v_3}^{(3), \text{CLBM}1} = C_{D_z^4 v_3}^{(3), \text{MRT}1}$$

$$C_{D_z^4 v_3}^{(3), \text{CLBM}2} = C_{D_z^4 v_3}^{(3), \text{MRT}1}$$

$$C_{D_z^4 v_3}^{(3), \text{CuLBM}1} = (12 + 378\omega_6 v_3^2 + 14\omega_6^2 c_s^4 - 18\omega_6 + 504v_3^4 + 54\omega_6 c_s^2 - 648\omega_6 v_3^2 c_s^2 + 310\omega_6^2 v_3^4 + 24c_s^4 - 18\omega_6^3 v_3^2 c_s^2 - \omega_6^3 c_s^4 - 29\omega_6^3 v_3^4 + 432v_3^2 c_s^2 + 8\omega_6^2 + 2\omega_6^2 c_s^2 - \omega_6^3 + 14\omega_6^3 v_3^2 - 756\omega_6 v_3^4 - 22\omega_6^2 c_s^2 - 252v_3^2 - 36\omega_6 c_s^4 - 154\omega_6^2 v_3^2 - 36c_s^2 + 252\omega_6^2 v_3^2 c_s^2) \frac{\rho}{12\omega_6^3}$$

$$C_{D_z^4 v_3}^{(3), \text{CuLBM}2} = (-8c_s^2 \omega_1 \omega_2^3 - 168\omega_3 v_3^2 \omega_1^2 \omega_2 + 144\omega_3 v_3^2 c_s^2 \omega_1^3 + 42\omega_3 v_3^2 \omega_1^3 \omega_2^3 + 8\omega_3 c_s^4 \omega_1 \omega_2^2 + 8\omega_3 \omega_1^2 \omega_2 - 20\omega_3 c_s^2 \omega_1^3 - 3\omega_3 \omega_1^3 \omega_2^3 - 288\omega_3 v_3^2 \omega_2^3 + 620\omega_3 v_3^4 \omega_1^2 \omega_2^3 - 312\omega_3 v_3^4 \omega_1^3 \omega_2 - 154\omega_3 v_3^2 \omega_1^3 \omega_2^2 - 888\omega_3 v_3^4 \omega_1^2 \omega_2^2 + 8\omega_3 \omega_1^3 \omega_2^2 - 68\omega_3 c_s^4 \omega_1 \omega_2^3 - 87\omega_3 v_3^4 \omega_1^3 \omega_2^3 + 336\omega_3 v_3^4 \omega_1^2 \omega_2 + 8c_s^4 \omega_1 \omega_2^3 + 24v_3^2 c_s^2 \omega_1^3 \omega_2 - 10\omega_3 \omega_1^3 \omega_2 + 16\omega_3 \omega_1^2 \omega_2^3 - 16\omega_3 c_s^2 \omega_1 \omega_2^2 - 1008\omega_3 v_3^2 c_s^2 \omega_1 \omega_2^3 + 174\omega_3 v_3^2 \omega_1^3 \omega_2 - 308\omega_3 v_3^2 \omega_1^2 \omega_2^3 - 48v_3^2 c_s^2 \omega_1^2 \omega_2^2 - 16\omega_3 \omega_1^2 \omega_2^2 + 552\omega_3 v_3^2 c_s^2 \omega_2^3 + 310\omega_3 v_3^4 \omega_1^3 \omega_2^2 + 408\omega_3 v_3^2 \omega_1^2 \omega_2^2 - 60\omega_3 v_3^2 \omega_1^3 - 56\omega_3 c_s^2 \omega_2^3 + 336\omega_3 v_3^2 c_s^2 \omega_1 \omega_2^2 + 96\omega_3 c_s^2 \omega_1 \omega_2^3 - 3\omega_3 c_s^4 \omega_1^3 \omega_2^3 + 8\omega_3 \omega_1 \omega_2^2 + 8\omega_3 c_s^4 \omega_1^2 \omega_2 - 16c_s^4 \omega_1^2 \omega_2^2 - 576\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2^2 - 240\omega_3 v_3^2 \omega_1 \omega_2^2 + 42\omega_3 c_s^2 \omega_1^3 \omega_2 + 16\omega_3 \omega_2^3 - 44\omega_3 c_s^2 \omega_1^2 \omega_2^3 + 8c_s^4 \omega_1^3 \omega_2 - 28\omega_3 \omega_1 \omega_2^3 + 24v_3^2 c_s^2 \omega_1 \omega_2^3 + 14\omega_3 c_s^4 \omega_1^3 \omega_2^2 + 16\omega_3 c_s^4 \omega_1^3 + 24\omega_3 c_s^2 \omega_1^2 \omega_2^2 + 528\omega_3 v_3^4 \omega_2^3 + 552\omega_3 v_3^2 \omega_1 \omega_2^3 - 360\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2 + 504\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2^3 - 16\omega_3 c_s^2 \omega_1^2 \omega_2 + 6\omega_3 c_s^2 \omega_1^3 \omega_2^2 + 252\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2^2 + 16c_s^2 \omega_1^2 \omega_2^2 + 96\omega_3 v_3^4 \omega_1^3 + 552\omega_3 v_3^4 \omega_1 \omega_2^2 + 40\omega_3 c_s^4 \omega_2^3 + 28\omega_3 c_s^4 \omega_1^2 \omega_2^3 - 32\omega_3 c_s^4 \omega_1^3 \omega_2 + 264\omega_3 v_3^2 c_s^2 \omega_1^2 \omega_2 - 8c_s^2 \omega_1^3 \omega_2 - 54\omega_3 v_3^2 c_s^2 \omega_1^3 \omega_2^2 - 22\omega_3 c_s^2 \omega_1^3 \omega_2^2 - 8\omega_3 c_s^4 \omega_1^2 \omega_2^2 + 4\omega_3 \omega_1^3 - 1068\omega_3 v_3^4 \omega_1 \omega_2^3) \frac{\rho}{36\omega_3 \omega_1^3 \omega_2^3}$$

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